



Stability Analysis of Uncertain Temperature control system with two additive delays and nonlinear perturbation

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ABSTRACT

In this paper, the problem of robust delay-dependent stability criterion is considered for a class of linear continuous time heat exchanger system with constant additive state-delays and bounded nonlinear perturbations using Lyapunov-Krasovskii (LK) functional approach. In the proposed delay-dependent stability analysis, the time-delays are considered to be time-invariant. In the proposed delay-dependent stability analysis, a candidate LK functional is considered, and take the time-derivative of the functional is bounded using the Jensen integral inequality. The proposed stability analysis finally culminates into a stability criterion in LMI framework. The effectiveness of the proposed stability criterion is illustrated using a network controlled temperature control of heat exchanger system

Indexing terms/Keywords

Constant Additive Time-Delay, Delay-dependent stability, Jensen Integral Inequality, Lyapunov-Krasovskii Functional, Nonlinear perturbations, Temperature Control system.

INTRODUCTION

Retarded time-delay differential equations with two additive state-delays provide ideal mathematical explanation for Networked Control Systems (NCSs) [1]. In real time conditions, the two time-delays in a typical NCS arise due to the transfer of state information from the plant to the controller and the succeeding transfer of controlled effort from the controller to the actuator to operate the plant [2, 3]. Since these two time-delays, owing to the network conditions, have unlike characteristic, analysis and synthesis of this class of time-delay systems pose interesting challenges and problems to the control engineering community [3]. Delay-dependent stability analysis of temperature control of heat exchanger system, based on Lyapunov-Krasovskii (LK) functional approach, yields sufficient conditions for computing the maximum allowable bound of the time-delays within which the temperature control of heat exchanger system under consideration remains asymptotically stable in the sense of Lyapunov. These sufficient conditions, referred generally as delay-dependent stability criteria, are expressed as a set of solvable LMI conditions. The conservatism of delay-dependent stability criteria depends mainly on the choice of the LK functional used in the analysis, and the techniques, many useful results have been reported in literature in recent time [2-13]. Among these results, except [14], all the other result present stability criteria for nominal systems with additive state-delays; in [14], a robust stability criterion is derived for additive state-delayed systems with time-varying parametric uncertainties.

In spite of many useful results existing in literature, there are no results available for ascertaining delay-dependent stability of linear (heat exchanger) system with additive state-delays subjected to bounded nonlinear perturbations. These nonlinear perturbations, expressed with respect to current and delayed states, account for system uncertainties like noisy ambient conditions, slowly varying system parameters etc., refer [14, 15, 20]. The robustness of nonlinear perturbed heat exchanger system can be ascertained by delay-dependent stability analysis based on Lyapunov approach [19]. Proposing one such analysis is the objective of this paper. In the proposed analysis, with the assumption that the network delays are constant, a fewer conservative delay-dependent stability criterion is derived using LK functional approach and Jensen integral inequality [16] in LMI formulation. By making use of this integral inequality, there is a substantial reduction in number of free-weighting matrices employed in the delay-dependent stability analysis. Since the proposed robust stability criterion is expressed in LMI framework, it can be solved efficiently in temperature control of heat exchanger system.

System Description and Problem Statement

In general the state-space model of the uncertain additive state-delayed temperature control of heat exchanger (PI control) system with nonlinear perturbations is given below:

$$\begin{aligned}\dot{x}(t) &= Ax(t) + A_d x(t - h_1 - h_2) + f + g, \\ x(t) &= \phi(t), t \in [-(\bar{h}_1 + \bar{h}_2), 0],\end{aligned}\quad (1)$$



where $x(t) \in \mathbb{R}^{n \times 1}$ is the state vector, $A \in \mathbb{R}^{n \times n}$ and $A_d \in \mathbb{R}^{n \times n}$ are represents the system matrices are associated with the current state and delayed state vectors, $\phi(t)$ is the vector-valued continuous-time function describing the initial condition of the system, for the temperature control system state vector, and system matrices are reduced the following:

$$A = \begin{bmatrix} -\frac{1}{T_V} & 0 & 0 & 0 \\ \frac{K_H}{T_H} & -\frac{1}{T_H} & 0 & 0 \\ 0 & \frac{K_F}{T_F} & -\frac{1}{T_F} & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}; \quad A_d = \begin{bmatrix} 0 & 0 & \frac{-K_p K_V}{T_V} & \frac{-K_I K_V}{T_V} \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

The additive state-delays h_1 and h_2 satisfy the following conditions:

$$0 \leq h_1 \leq \bar{h}_1, \quad 0 \leq h_2 \leq \bar{h}_2 \quad (2)$$

where \bar{h}_1 and \bar{h}_2 are the upper bound of the time-delays h_1 and h_2 . In (1), the terms $f = f(x(t), t)$ and $g = g(x(t - h_1 - h_2), t)$ represents the nonlinear perturbations with respect to current state and additive delayed state; they are assumed to satisfy $f(0, t) = g(0, t) = 0$ and following bounding conditions:

$$f^T f \leq \alpha^2 x^T(t) F^T F x(t), \quad (3)$$

$$g^T g \leq \beta^2 x^T(t - h_1 - h_2) G^T G x(t - h_1 - h_2), \quad (4)$$

where F and G are known constant matrices of appropriate dimensions; the non-negative scalars α and β quantify the magnitude of the nonlinear perturbations. The problem addressed in this paper is stated below:

To develop a robust stability criterion in LMI framework to ascertain delay-dependent stability of the system (1) subject to bounding conditions (3) and (4), and satisfying the additive time-delays (2) using Lyapunov-Krasovskii (LK) functional approach and Jensen integral inequality lemma. For deriving the robust stability criterion, following lemmas are unavoidable:

Lemma 1: For any positive symmetric constant matrix $M \in \mathbb{R}^{n \times n}$, scalar r_1 and r_2 satisfying $r_1 < r_2$, a vector valued function $\omega: [r_1, r_2] \rightarrow \mathbb{R}^n$ such that the integrations related are well defined, then following inequality holds:

$$\left(\int_{r_1}^{r_2} \omega(s) ds \right)^T M \left(\int_{r_1}^{r_2} \omega(s) ds \right) \leq r_{12} \int_{r_1}^{r_2} \omega^T(s) M \omega(s) ds.$$

where $r_{12} = r_2 - r_1$.

Lemma 2: For a continuous function $f(x)$ and its derivative $f'(x)$ defined on $[a, b]$, then

$$\int_a^b f'(x) dx = f(b) - f(a).$$

Lemma 3: For any positive symmetric constant matrix $Z \in \mathbb{R}^{n \times n}$, scalars γ_1 and γ_2 satisfying $\gamma_1 \leq \gamma_2$, a vector valued function $x(t - \gamma): [\gamma_1, \gamma_2] \rightarrow \mathbb{R}^n$ such that the integration concerned as well defined, then following inequality holds:

$$-\gamma_{12} \int_{t-\gamma_2}^{t-\gamma_1} \dot{x}^T(s) Z \dot{x}(s) ds \leq \begin{bmatrix} x(t - \gamma_1) \\ x(t - \gamma_2) \end{bmatrix}^T \begin{bmatrix} -Z & Z \\ Z & -Z \end{bmatrix} \begin{bmatrix} x(t - \gamma_1) \\ x(t - \gamma_2) \end{bmatrix} \quad (5)$$

Proof: By Lemma 1, we can write the following expression ($\omega(s) = \dot{x}(s), M = Z, r_1 = t - \gamma_2, r_2 = t - \gamma_1$):

$$-\gamma_{12} \int_{t-\gamma_2}^{t-\gamma_1} \dot{x}^T(s) Z \dot{x}(s) ds \leq \left(\int_{t-\gamma_2}^{t-\gamma_1} \dot{x}(s) ds \right)^T (-Z) \left(\int_{t-\gamma_2}^{t-\gamma_1} \dot{x}(s) ds \right) \quad (6)$$

By Lemma 2, we can express (6) as follows ($f(\cdot) = x(s), a = t - \gamma_2, b = t - \gamma_1$):

$$-\gamma_{12} \int_{t-\gamma_2}^{t-\gamma_1} \dot{x}^T(s) Z \dot{x}(s) ds \leq (x(t - \gamma_1) - x(t - \gamma_2))^T (-Z) (x(t - \gamma_1) - x(t - \gamma_2)), \quad (7)$$

which, in other words, is expressed quadratically as stated in (5) of the lemma.

Main Result

The main result of the paper is stated in the form of a Theorem:

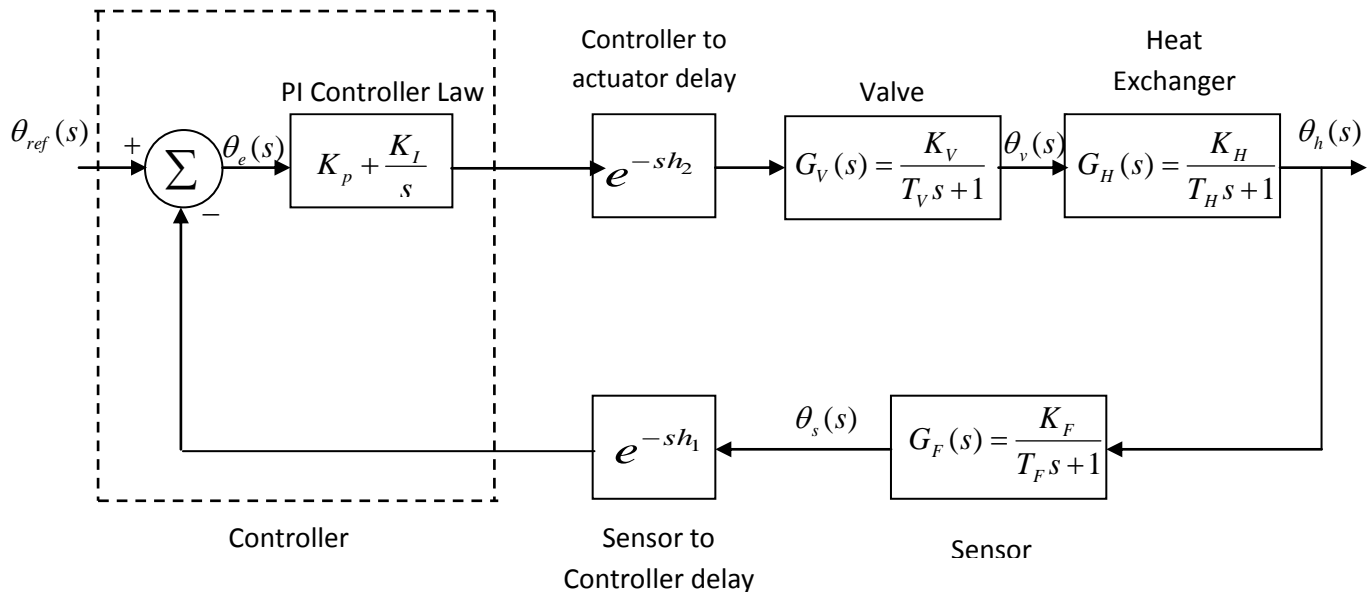


Fig. 1 Block diagram of closed loop temperature control of heat exchanger system with constant additive-delays

Theorem: The LTI system (1) is asymptotically stable in the sense of Lyapunov for a given value of \bar{h}_1 and \bar{h}_2 , if there exist real symmetric positive definite matrices P, Q_1, Q_2 , and R ; scalars $\varepsilon_1 > 0$ and $\varepsilon_2 > 0$ such that the LMI (17).

Proof: The Lyapunov-Krasovskii (LK) functional approach are used in the delay-dependent stability analysis of a LTI system controlled over a delayed network is given by

$$V(x(t)) = V_1(x(t)) + V_2(x(t)) + V_3(x(t)),$$

where

$$V_1(x(t)) = x^T(t)Px(t) \quad (8)$$

$$V_2(x(t)) = \int_{t-h_1}^t x^T(s)Q_1x(s)ds + \int_{t-h}^t x^T(s)Q_2x(s)ds, \quad (9)$$

$$V_3(x(t)) = \int_{-h}^0 \int_{t+\theta}^t \dot{x}^T(s)R\dot{x}(s)dsd\theta, \quad (10)$$

where P, Q_1, Q_2 and R ; are real symmetric positive definite matrices and $h = h_1 + h_2$. The time derivative of the LK functional $\dot{V}_i(x(t)), i = 1, 2, 3$ is given by

$$\dot{V}_1(x(t)) = \dot{x}^T(t)Px(t) + x^T(t)P\dot{x}(t),$$

$$\dot{V}_2(x(t)) = (Ax(t) + A_d x(t - h_1 - h_2) + f(x(t), t) + g(x(t - h_1 - h_2), t))^T Px(t) + x^T(t)P(Ax(t) + A_d x(t - h_1 - h_2) + f(x(t), t) + g(x(t - h_1 - h_2), t)) \quad (11)$$

$$\dot{V}_2(x(t)) = x^T(t)Q_1x(t) - x^T(t - h_1)Q_1x(t - h_1) + x^T(t)Q_2x(t) - x^T(t - h)Q_2x(t - h), \quad (12)$$

$$\dot{V}_3(x(t)) = h\dot{x}^T(t)R\dot{x}(t) - \int_{t-h}^t \dot{x}^T(s)R\dot{x}(s)ds$$

$$\dot{V}_3(x(t)) = h\dot{x}^T(t)R\dot{x}(t) - \int_{t-h}^{t-h_1} \dot{x}^T(s)R\dot{x}(s)ds - \int_{t-h_1}^t \dot{x}^T(s)R\dot{x}(s)ds. \quad (13)$$

Now, for any $\varepsilon_1 \geq 0$ and $\varepsilon_2 \geq 0$, it follows from (3) and (4) that

$$\varepsilon_1(\alpha^2 x^T(t)F^T Fx(t) - f^T f) \geq 0 \quad (14)$$

$$\varepsilon_2(\beta^2 x^T(t - h_1 - h_2)G^T Gx(t - h_1 - h_2) - g^T g) \geq 0 \quad (15)$$

Now, by applying Lemma 3 on (13), and by adding the positive quantities (14) and (15) to $\sum_{i=1}^3 \dot{V}_i(x(t))$, we express $\dot{V}(x(t))$ as follows:

$$\dot{V}(x(t)) \leq \xi^T(t)\Pi\xi(t) \quad (16)$$



The augmented state vector is:

$$\xi(t) = \begin{bmatrix} x^T(t) & x^T(t-h_1) & x^T(t-h_1-h_2) & f(\cdot)^T & g(\cdot)^T \end{bmatrix}^T$$

Now, if $\Pi < 0$, there exists a sufficient small scalar $\alpha > 0$ such that $\dot{V}(x(t)) \leq -\alpha \|x(t)\|^2$, which, in turn, implies that the additive state-delayed system (1) is asymptotically stable in the sense of Lyapunov. By taking Schur complement [17] on $\Pi < 0$, we deduce the delay-dependent stability criterion (LMI (17)) stated in the Theorem 1.

$$\begin{bmatrix} A^T P + PA + Q_1 + Q_2 - \frac{R}{h_1} + \varepsilon_1 \alpha^2 F^T F & \frac{R}{h_1} & PA_d & P & P & hA^T R \\ * & -Q_1 - \frac{R}{h_1} - \frac{R}{h_2} & \frac{R}{h_2} & 0 & 0 & 0 \\ * & * & -Q_2 - \frac{R}{h_2} + \varepsilon_2 \beta^2 G^T G & 0 & 0 & hA_d^T R \\ * & * & * & -\varepsilon_1 I & 0 & hR \\ * & * & * & * & -\varepsilon_2 I & hR \\ * & * & * & * & * & -hR \end{bmatrix} < 0. \quad (17)$$

$$\begin{bmatrix} A^T P + PA + Q_1 + Q_2 - \frac{R}{h_1} & \frac{R}{h_1} & PA_d & hA^T R \\ * & -Q_1 - \frac{R}{h_1} - \frac{R}{h_2} & \frac{R}{h_2} & 0 \\ * & * & -Q_2 - \frac{R}{h_2} & hA_d^T R \\ * & * & * & -hR \end{bmatrix} < 0 \quad (18)$$

* –Represents the symmetric matrices

Remark: For nominal system with $f(\cdot) = g(\cdot) = 0$, the delay-dependent stability criterion is presented in following corollary:

Corollary 1: The LTI system (1) with $f(\cdot) = g(\cdot) = 0$ is asymptotically stable in the sense of Lyapunov for a given value of \bar{h}_1 , and \bar{h}_2 , if there exists real symmetric positive definite matrices P, Q_1, Q_2 and R such that the LMI (18) stated.

Temperature Control System

For the temperature control of heat exchanger system, linear or linearized models are commonly used to analyze the system dynamics and to design a controller. Fig.1 shows the block diagram of a temperature control of heat exchanger system with including network-induced time-delays. Now that each component of the system namely heat exchanger, sensor, valve, controller is modelled by a first-order transfer function [18]. They repeated here for convince:

$$G_V(s) = \frac{K_V}{T_V s + 1}; G_H(s) = \frac{K_H}{T_H s + 1}; G_F(s) = \frac{K_F}{T_F s + 1}; \quad (19)$$

where K_V, K_H and K_F are the gains of valve, heat exchanger and sensor respectively, and T_V, T_H and T_F are the corresponding time constants.

In the Fig.1 Portrays sensor to controller delay and portrays controller to actuator delay. The transfer function of the controller is given below.

$$G_C(s) = K_p + \frac{K_i}{s} \quad (20)$$

where K_p and K_i are the proportional and integral controller gains respectively; the proportional term control the rate of temperature rise after initial transients. The integral controller gain adds a pole at origin and increases the system type by one and hence reduces the steady-state error. The coordinated effort of the PI controller gains will structure the response of the temperature control of heat exchanger with reduced overshoot and faster settling time.

Case Study

In this section, the potency of the proposed stability criterion for temperature control of heat exchanger system with constant additive time delays is illustrated.

Table.1 Parameter values of Temperature Control system

System	Gain	Time-constant
Heat exchanger	$K_H = 34$	$T_H = 30$
Valve	$K_V = 1.25$	$T_V = 3$
Sensor	$K_F = 0.08$	$T_F = 2$

In this section, the maximum allowable delay margin for constant are validated additive time-delays \bar{h}_1 , and \bar{h}_2 for stability for a pick range of PI controller gains is computed. The gains and time constants of the temperature control of heat exchanger used in the analysis are as follows [18]. For the aforesaid system parameters, with delay free condition, the controller capability curve can be easily obtained; it is illustrated in Fig. 2.

From the Fig. 2, it is clear that for all values of K_P and K_I lying below the controller capability curve, the closed-loop system is asymptotically stable. From the curve we choose $K_P = 0.5$ and $K_I = 0.02s^{-1}$ for computation of delay margin. For these controller parameters, the closed loop system converges asymptotically to equilibrium point as illustrated in Fig. 3 for a unit step perturbation in heat exchanger output variable (from its equilibrium value).

When the network delay \bar{h} is made zero, the system equation (3) becomes

$$\dot{x}(t) = (A + A_d)x(t) \tag{21}$$

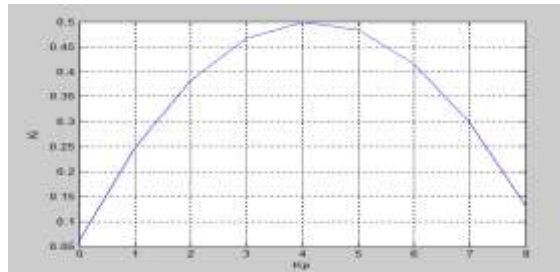


Fig. 2 The Maximum value of K_I for different values of K_P

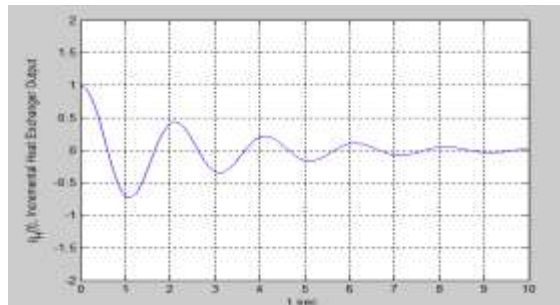


Fig. 3 Evolution of $\Delta\theta_H(t)$ less than zero delay condition.

Now, it is observed that the eigenvalues of the system state matrix and input matrix $(A + A_d)$ depend on the controller parameters K_P and K_I . Table II given the maximum values of $K_I s^{-1}$ for a fixed value of K_P for which the temperature control of heat exchanger system is on the verge of instability i.e. having one complex-conjugate pair of eigenvalues on the $j\omega$ axis. It is observed from the Fig. 3 that there is a tendency for the curve to decrease gradually with increase of K_I .

In this case study corresponding to temperature control of heat exchanger system with constant additive time-delays, the exogenous load disturbance effect of temperature control of heat exchanger system is assume to satisfy the norm-bounded condition is given in (3) and (4); the value of two matrices G and F are taken as $0.1I_n$ where n is the size of the system state vector $x(t)$, using Jensen integral inequality lemma stated for theorem1, the maximum value of the delay bound h_1 and h_2 is calculated for temperature control system for various values of α and β , as shown in Tables III and IV (refer Fig. 4 Stability margin for Temperature control of heat exchanger system). In the tables, it is clearly shows that as the values of α and β increases, the load disturbance effects for the temperature control system become more pronounced, and under such load disturbed condition, the maximum value of network delay that the PI controlled temperature control of heat exchanger system withstand without losing stability decreases.

These results clearly bring out the effect of load disturbance on the delay-dependent stability of the temperature control system. Hence, delay-dependent stability analysis of temperature control of heat exchanger system with load perturbation being modelled as bounded non-linear load disturbance with respect to current and delayed state vectors has not been reported so far literature; the results presented in this paper portray a more realistic system operating condition. The nominal system condition (i.e. when $\alpha = \beta = 0$) with two additive constant time-delays, the presented results (for ascertaining internal stability) are less conservative, and this is attributed to the higher bounding of the Lyapunov-Krasovskii (LK) functional in the stability analysis using the Jensen integral inequality as shows in Table V (for various values of K_P and K_I). For choosing the controller parameter $K_P = 0.5$ and $K_I = 0.02s^{-1}$, in the presence of network induced delays, according to the delay-dependent stability criterion presented in Theorem 1, the temperature control of heat exchanger system is stable upto $h_1 = 1$ second $h_2 = 18.3357$ seconds, and if network induced delays is increases far beyond this value, the system becomes unstable.



Table .2 Maximum Integral Controller Gain for A Given K_P

Sl.No :	K_P	$K_I (s^{-1})$	Eigen values of $(A + A_d)$
1	0	0.062	-0.4329±0.009j; -0.0004;-0.0790
2	1	0.248	-0.0000±0.167j; -0.5801;-0.2864
4	2	0.382	-0.0001±0.223j; -0.6415;-0.2250
5	3	0.466	-0.0000±0.267j; -0.6885;-0.1781
6	4	0.499	-0.0000±0.305j; -0.7282;-0.1385
7	5	0.482	-0.0000±0.339j; -0.7631;-0.1036
6	6	0.415	-0.0001±0.370j; -0.7946;-0.0719
8	7	0.298	-0.0000±0.398j; -0.8236;-0.0430
9	8	0.130	-0.0000±0.425j; -0.8506;-0.0160

Table. 3 Maximum Allowable Delay Bound \bar{h}_2 for a given \bar{h}_1 .

Method	α	β	$\bar{h}_1 = 0.1$	$\bar{h}_1 = 1$	$\bar{h}_1 = 5.0$	$\bar{h}_1 = 10$
Theorem 1	0	0	19.2352	18.3357	14.3363	9.3366
	0	0.005	10.6649	9.7651	5.7652	0.7652
	0.005	0.005	#	#	#	#

Table. 4 Maximum Allowable Delay Bound \bar{h}_1 for a given \bar{h}_2 .

Method	α	β	$\bar{h}_2 = 0.1$	$\bar{h}_2 = 1$	$\bar{h}_2 = 5.0$	$\bar{h}_2 = 10$
Theorem 1	0	0	19.2358	18.3357	14.3363	9.3363
	0	0.005	10.6652	9.7653	5.7651	0.7651
	0.005	0.005	#	#	#	#

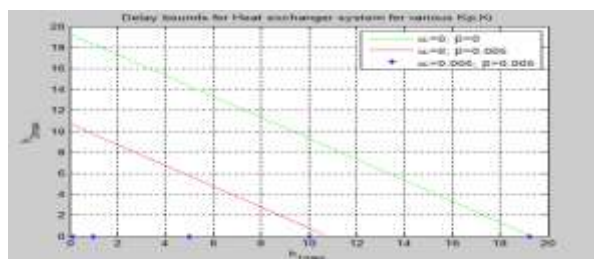


Fig. 4 Stability margin for Temperature control of heat exchanger system



Table 5. Maximum Delay Bound for h_2 given h_1 with various controller gains

K_P	K_I	$h_1 = 1$	$h_1 = 5$	$h_1 = 8$	$h_1 = 10$
0.20	0.01	38.29	34.29	31.29	29.29
0.20	0.02	17.49	13.49	10.49	8.49
0.20	0.03	10.10	6.10	3.10	1.10
0.50	0.01	26.71	22.71	19.71	17.71
0.50	0.02	18.33	14.33	11.33	9.33
0.50	0.03	13.08	9.08	6.08	4.08
0.75	0.01	16.24	12.24	9.24	7.24
0.75	0.02	13.75	9.75	6.75	4.75
0.75	0.03	11.40	7.40	4.40	2.40
1.0	0.01	10.88	6.88	3.88	1.88
1.0	0.02	9.90	5.90	2.90	0.90
1.0	0.03	8.87	4.87	1.87	#

Conclusion

In this paper, a robust stability criterion is proposed for a class of linear continuous time system with constant additive state-delays and bounded nonlinear perturbations using Lyapunov-Krasovskii functional approach the Jensen integral inequality, and it is expressed in Linear Matrix Inequalities (LMI) framework. The effectiveness of the proposed is illustrated in temperature control of heat exchanger system. The possibility of extending the proposed analysis procedure for an equivalent discrete-time system can be explored as a future work.

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