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Frost Occurrence Risk Management for Pistachio Industry in Rafsanjan

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Abstract

This work develops a statistical model to assess the frost risk in Rafsanjan, one of the largest Pistachio production regions in the world. These models can be used to estimate the probability that: a frost happens in a given time-period in the year; a frost happens after 10 warm days in the growing season etc. These probability estimates then can be used for: (1) assessing the agroclimate risk of investing in this industry; (2) pricing of weather derivatives. Autoregressive models with different seasonal components and lags are compared using AIC, BIC, AICc and cross validation criterions. The optimal model is AR(1) with 12 terms from Fourier series. The long-term trends are also accounted for and estimated from data. The optimal models are then used to simulate future weather from which the probabilities of appropriate hazard events for pistachio yield are estimated.

Keywords: Pistachio; Frost; Weather derivative; Minimum temperature; Time-varying autoregressive coefficients.

1. Introduction

The greater Rafsanjan area in north of Kerman Province in Iran is a region with the largest pistachio production in the world and most of the region's economy relies on pistachio production. In the recent years the most important risk factor for pistachio producers and industry (e.g. farmers, distributors) has been frosts that have destroyed a large proportion of the yield. Therefore methods that can estimate the probability of such events is useful. In particular such methods can: (1) assess the agroclimate risk of investing in this industry; (2) pricing of weather derivatives. In fact weather derivatives, which may be created as part of a risk management program, can be written in terms of the attainment or non-attainment of specific target-values stipulated in the contract. Temperature-related trades account for 80% of the transactions among all weather derivatives [1]. Most of the work in this area has focused on HDD/CDD (heating degree days/cooling degree days) (e.g. [2,3]). In this paper we focus on the occurrence of frosts an issue recently considered in [4], for agricultural crops in Canada.

The models developed in this paper can be applied to estimate: the probability that a given period is frost-free; the probability that a given day is the start of a long frost-free period; the distribution of the length of the frost-free period and so on. The same model can be used to compute the

probability that a given day of the year is the beginning of the growing season (the first day that the mean temperature is higher than 5 degrees for 5 consequent days) as well as the length of the growing season which are important for agricultural applications. For example in this study we estimate the probability of a useful event: "the minimum temperature goes below zero at least one day in the period March 27th-April 20th". This is an important event because it coincides with the general flowering time of pistachio trees. Throughout this paper, temperature is measured in degrees Celsius. Let us denote the minimum temperature series by $\{Y(t)\}$, $t=0,1,2,\dots$, where t denotes time. We let F to be the investor's defined frost which we take it to be zero in this work. Then we can define the binary frost process:

$$Y_F(t) = \begin{cases} 1 & Y(t) \leq F \text{ (deg C)} \\ F & Y(t) > F \text{ (deg C)}. \end{cases}$$

In order to study frosts we can use these approaches among others: (a) Fit the continuous-valued Markov model to the $Y(t)$ chain; (b) Fit a binary Markov model to the $Y_F(t)$ chain. Hossein suggests using binary Markov models to avoid assumptions regarding the distribution of temperature and gain robustness for modeling frosts in Alberta, Canada [4]. They show time-varying high-order Markov models with complex seasonal structure are needed and therefore their computations become challenging. Here we investigate Method (a) in fitting such chains and calculating the probabilities of frost events. The advantages of Method (a) are: (1) The fitting can be done with standard packages such as R with less computational problems; (2) only this method can estimate the probability of complicated events. One such complicated event is: "the temperature in March-April is above 5 (deg C) for at least 3 consecutive days and is below zero after". A comparison of the two methods in terms of estimation when they are both applicable is left to future research.

2. Data and statistical models

The data in this study are daily minimum temperature values collected at Rafsanjan weather station from 1992 to 2010. At the moment we do not have access to more data from other stations in the area but we hope to acquire those data for future studies to offer more local predictions. In order to model frost occurrences, we introduce statistical models for minimum daily temperature in Rafsanjan. Several features of the temperature process should be considered in modeling: (1) seasonal trends over time; (2) long-term trends (possibly a result of global warming or volcanic events etc) (3) dependence over time. Let $\{Y(t)\}$, $t=0,1,2,\dots,T$ denote the daily minimum temperature process in centigrade, where t denotes the day starting from March 1st 1992 to December 28th 2010. Here we consider autoregressive models with a seasonal component and various lags:

$$Y(t) = \mu(t) + \epsilon(t), \quad \mu(t) = a_0(t) + \sum_{i=1}^r a_i Y(t-i)$$

Where $\mu(t) = E\{Y(t) | Y(t-1), Y(t-2), \dots\}$ is the conditional mean of minimum temperature at time t ; $\epsilon(t)$ are independent identically distributed normal errors $\epsilon(t) \sim N(0, \delta^2)$; $a_0(t)$ is the fixed trend coefficient; a_1, a_2, \dots, a_r are autoregressive coefficients. We allow $a_0(t)$ to include both seasonal and long-term effects by using a Fourier series with period, $\omega = \frac{2\pi}{366}$, and a quadratic trend:

$$a_0(t) = \left\{ \alpha_0 + \sum_{j=1}^k \alpha_j \cos(j\omega t) + \beta_j \sin(j\omega t) \right\} + \left\{ \gamma_1 t + \gamma_2 t^2 \right\},$$

The estimation of the parameters is done by maximizing the (partial) likelihood of the data as discussed in [4]. The nice property of the gaussian error assumption is that maximization can be done in closed form exactly in the same way as minimizing the mean-square error of classical regression problem originally solved by Gauss and therefore the estimation is fast in statistical packages such as “R” (a free widely used software by statisticians and practitioners).

3. Statistical model selection

In the above we introduced several autoregressive models of: (1) various lags; (2) various seasonal complexity (number of Fourier terms); (3) various long-term trends. Therefore we need to use some criteria to select an optimal model. The problem of model selection is an important one in statistical theory and application. Various criteria are suggested in the literature for example: AIC in [5]; BIC in [6] and AICc in [7]. Denote the likelihood of the data by L (in this paper the “partial likelihood”), the number of covariates by p and the sample size by n. Then we have

$$AIC = 2p - 2 \ln(L), \quad AICc = AIC + \frac{2k(k+1)}{n-k-1}, \quad BIC = p \log(n) - 2 \ln(L).$$

Since n in our data is large compared to k, AIC and AICc are very close. When we compared the models using these criteria, AIC and AICc give rise to the same optimal model while BIC picked a simpler model. In Table 1 we have compared these optimal models using cross-validation error and cross-validated correlation. The cross-validation proceeds by: (1) taking an existing data point out; (2) fitting the model; (3) predicting the value of the point we took out (validation). Then the cross-validation error (CVE) is the mean square error of the predictions and the cross-validation correlation (CVR) is the correlation between the predictions and the observed. Table 1 shows that while the CVE and CVR are very close for the two models, the model picked by AIC/AICc slightly outperforms the one picked by BIC and therefore we use that model for estimation.

Criterion	optimal Model: Z_{t-1}	CVE	CVR
AIC and AICc	$\sin(\omega t), \cos(\omega t), \dots, \sin(6\omega t), \cos(6\omega t), Y_{t-1}, t, t^2$	2.691	0.9458
BIC	$\sin(\omega t), \cos(\omega t), Y_{t-1}$	2.696	0.9456

Tab 1. We compare the optimal model picked by AIC and AICc (first row) with the optimal model picked by BIC, (second row) using cross validation error and cross-validated correlation.

4. Applications in frost risk assessment

Previous section found an optimal fit to the data from which estimating the probability of any desired (possibly complex) event is possible by performing multiple simulations. In order to find out the probability of frost in any given day during 2011-2012 we have done 10000 simulations from the model for 2011-2011 and then for each day we have calculated the proportion of frost-days (number of frost days divided by 10000). The results are plotted in Figure 1. As we pointed

out in the introduction because the flowering time of different varieties of pistachios in Rafsanjan is generally between March 27th to April 20th, it is important to investigate the frost-occurrence during this period which we call the hazard period. Figure 2 shows the distribution of the “number of frost days” during the hazard period of 2012, where the frequency out of 10000 of any “number of frost days” is plotted. We observe that while it is most likely that no frost occurs in that period, there is a considerable probability that there are at least one frosts. This probability turns out to be about 9 percent which is a plausible number with our experience of pistachio damages caused by frosts in the past 20 years.

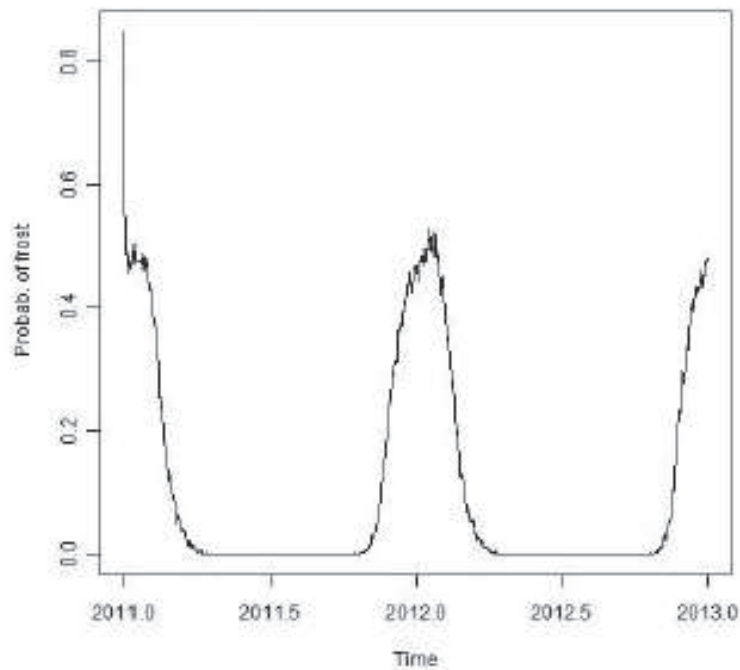


Fig 1. Estimated daily frost probability for 2011-2012 from the model, obtained using 1000 simulations of future weather.

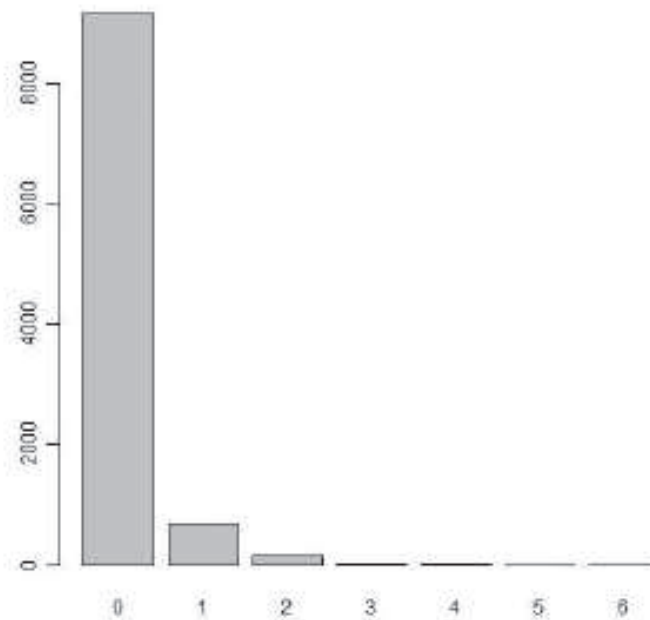


Fig 2. Distribution of frost days during the Hazard period (March 27th to April 20th 2012). This is based on 10000 simulations of the future chains. The probability of at least one frost based on this simulations is 0.0872 which is about 9 percent.

5. Summary and conclusion

This paper developed and compared several statistical models to estimate the probability of hazard frost events for pistachio industry in Rafsanjan. Despite the importance of such risk factors, no systematic studies and estimations of these risks are available in this region as far as we know; this paper is one of the first attempts in developing methods that can assess such risks. Assessing the probabilities of the hazard events are useful in estimating the risk of investing in this industry from production to distribution and exporting. However here we have not investigated other risk factors such as: extremely high temperature during summer; heavy short-time rain during flowering period; slow but long rain during the flowering time. For future studies we plan to acquire the data for precipitation, maximum temperature and developing models that assess these other risk factors.

Another important aspect of assessing the risk is relating the risk factors to the losses in yield or monetary values involved. For this study we relied on expert knowledge (by interviewing farmers and agriculture engineers) to define our hazard period. However if for example data for yield per km² becomes available for enough number of years and/or locations, one can develop a statistical model to relate the weather events to the losses in the yield in the same model.

6. Acknowledgements

We are indebted to Mr. Islami for providing the data for this study.

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