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Ambiguity and Social Judgment: Fuzzy Set Model and Data Analysis

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1. Introduction

Comparative judgment is essential in human social lives. Comparative judgment is a type of human judgment procedure, in which the evaluator is asked which alternative is preferred (e.g., “Do you prefer Brand A to Brand B?” or “How do you estimate the probability of choosing Brand A over Brand B when you compare the two brands? ”). This type of judgment is distinguished from absolute judgment, in which the evaluator is asked to assess the attractiveness of an object (e.g., “How much do you like this brand on a scale of 0 to 100?”).

The ambiguity of social judgment has been conceptualized by the fuzzy set theory. The fuzzy set theory provides a formal framework for the presentation of the ambiguity. Fuzzy sets were defined by Zadeh(1965) who also outlined how they could be used to characterize complex systems and decision processes (Zadeh, 1973). Zadeh argues that the capacity of humans to manipulate fuzzy concepts should be viewed as a major asset, not a liability. The complexities in the real world often defy precise measurement and fuzzy logic defines concepts and its techniques provide a mathematical method able to deal with thought processes which are often too imprecise and ambiguous to deal with by classical mathematical techniques.

This chapter introduces a model of ambiguous comparative judgment (Takemura,2007) and provides a method of data analysis for the model, and then shows some examples of the data analysis of social judgments. Comparative judgments in social situations often involve ambiguity with regard to confidence, and people may be unable to make judgments without some confidence intervals. To measure the ambiguity (or vagueness) of human judgment, the fuzzy rating method has been proposed and developed (Hesketh, Pryor, Gleitzman, & Hesketh, 1988). In fuzzy rating, respondents select a representative rating point on a scale and indicate higher or lower rating points, depending on the relative ambiguity of their judgment. For example, fuzzy rating would be useful for perceived temperature, with the evaluator indicating a representative value and lower and upper values. This rating scale allows for asymmetries and overcomes the problem, identified by Smithson (1987), of researchers arbitrarily deciding the most representative value from a range of scores. By making certain simplifying assumptions (which is not uncommon in fuzzy set theory), the rating can be viewed as an L-R fuzzy number, thereby making the use of fuzzy set

theoretical operations possible (Hesketh et al., 1988; Takemura, 2000). Lastly, numerical illustrations of psychological experiments are provided to examine the ambiguous comparative judgment model (Takemura, 2007) using the proposed data analysis.

2. Model of ambiguous comparative judgment

2.1 Overview of ambiguous comparative judgment and the judgment model

Social psychological theory and research have demonstrated that comparative evaluation has a crucial role in the cognitive processes and structures that underlie people's judgments, decisions, and behaviors (e.g., Mussweiler, 2003). People comparison processes are almost ubiquitous in human social cognition. For example, people tend to compare their performance of others in situations that are ambiguous (Festinger, 1954). It is also obvious that they are critical in forming personal evaluations, and making purchase decisions (Kühberger, Schulte-Mecklenbeck, & Ranyard, 2011; Takemura, 2011).

The ambiguity or vagueness is inherent in people's comparative social judgment. Traditionally, psychological and philosophical theories implicitly had assumed the ambiguity of thought processes (Smithson, 1987, 1989). For example, Wittgenstein (1953) pointed out that lay categories were better characterized by a "family resemblance" model which assumed vague boundaries of concepts rather than a classical set-theoretic model. Rosch (1975) and Rosch & Mervice (1975) also suggested vagueness of lay categories in her prototype model and reinterpreted the family resemblance model. Moreover, the social judgment theory (Sherif & Hovland, 1961) and the information integration theory (Anderson, 1988) for describing judgment and decision making assumed that people evaluate the objects using natural languages which were inherently ambiguous. However, psychological theories did not explicitly treat the ambiguity in social judgment with the exception of using random error of judgment.

Takemura (2007) proposed fuzzy set models that explain ambiguous comparative judgment in social situations. Because ambiguous comparative judgment may not always hold transitivity and comparability properties, the models assume parameters based on biased responses that may not hold transitivity and comparability properties. The models consist of two types of fuzzy set components for ambiguous comparative judgment. The first is a fuzzy theoretical extension of the additive difference model for preference, which is used to explain ambiguous preference strength and does not always assume judgment scale boundaries, such as a willing to pay (WTP) measure. The second type of model is a fuzzy logistic model of the additive difference preference, which is used to explain ambiguous preference in which preference strength is bounded, such as a probability measure (e.g., a certain interval within a bounded interval from 0 to 100%).

Because judgment of a bounded scale, such as a probability judgment, causes a methodological problem when fuzzy linear regression is used, a fuzzy logistic function to prevent this problem was proposed. In both models, multi-attribute weighting parameters and all attribute values are assumed to be asymmetric fuzzy L-R numbers. For each model, A method of parameter estimation using fuzzy regression analysis was proposed. That is, a fuzzy linear regression model using the least squares method (Takemura, 1999, 2005) was

applied for the analysis of the former model, and a fuzzy logistic regression model (Takemura, 2004) was proposed for the analysis of the latter model.

2.2 Assumptions of the model

2.2.1 Definition 1: Set of multidimensional alternatives

Let $X = X_1 \times X_2 \times \dots \times X_n$ be a set of multidimensional alternatives with elements of the form $X_1 = (X_{11}, X_{12}, \dots, X_{1n})$, $X_2 = (X_{21}, X_{22}, \dots, X_{2n})$, ..., $X_m = (X_{m1}, X_{m2}, \dots, X_{mn})$, where X_{ij} ($i = 1..m$; $j = 1..n$) is the value of alternative X_i on dimension j . Note that the components of X_i may be ambiguous linguistic variables rather than crisp numbers.

2.2.2 Definition 2: Classic preference relation

Let \succ be a binary relation on X , that is, \succ is a subset of $X \times X$.

The relational structure $\langle X, \succ \rangle$ is a weak order if, and only if, for all X_a, X_b, X_c , the following two axioms are satisfied.

1. Connectedness (Comparability): $X_a \succ X_b$ or $X_b \succ X_a$,
2. Transitivity: If $X_a \succ X_b$ and $X_b \succ X_c$, then $X_a \succ X_c$.

However, the weak order relation is not always assumed in this paper. That is, transitivity or connectedness may be violated in the preference relations.

2.2.3 Definition 3: Fuzzy preference relation

As a classical preference relation \succ is a subset of $X \times X$, \succ is a classical set often viewed as a characteristic function c from $X \times X$ to $\{0,1\}$ such that:

$$c(X_j \succ X_k) = \begin{cases} 1 & \text{iff } X_a \succ X_b \\ 0 & \text{iff } \text{not}(X_a \succ X_b) \end{cases}.$$

Note that "iff" is short for "if and only if" and $\{0,1\}$ is called the valuation set. If the valuation set is allowed to be the real interval $[0,1]$, \succ is called a fuzzy preference relation.

That is, the membership function μ_a is defined as:

$$\mu_a: X \times X \rightarrow [0,1].$$

2.2.4 Definition 4: Ambiguous preference relation

Ambiguous preference relations are defined as a fuzzy set of $X \times X \times S$, where S is a subset of one-dimensional real number space. S is interpreted as a domain of preference strength. S may be bounded, for example, $S = [0,1]$. The membership function μ_β is defined as:

$$\mu_\beta: X \times X \times S \rightarrow [0,1].$$

Ambiguous preference relation is interpreted as a fuzzified version of a classical characteristic function $c(X_a \succ X_b)$.

Therefore, the ambiguous preference relation for $X_a \succ X_b$ is represented as the fuzzy set $v(X_a \succ X_b)$. For simplicity, $v(X_a \succ X_b)$ will be assumed to be an asymmetrical L-R fuzzy number (see Figure 1).

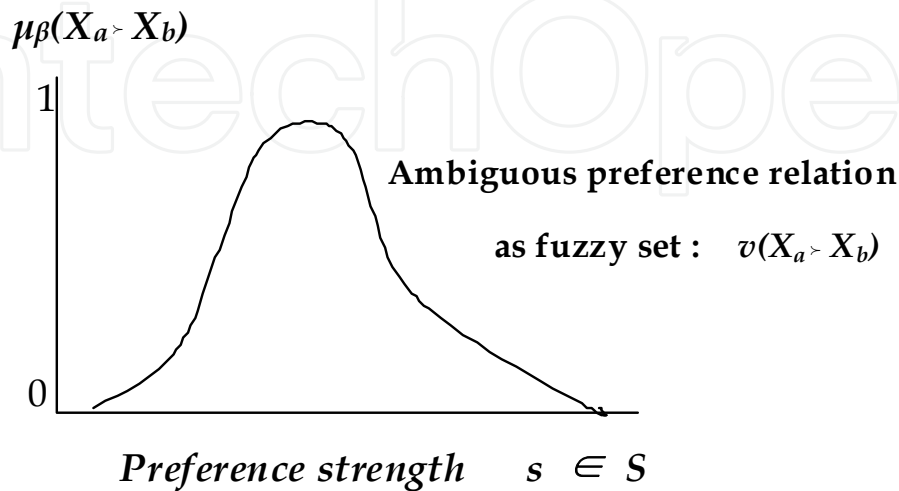


Fig. 1. Example of Ambiguous Preference Relation

2.2.5 Additive difference model of ambiguous comparative judgement

The ambiguous preference relation $v(X_a \succ X_b)$ for $X_a \succ X_b$ is represented as the following additive difference model using L-R fuzzy numbers:

$$v(X_a \succ X_b) =$$

$$A_{ab0} \oplus A_{ab1} \otimes (X_{a1} \ominus X_{b1}) \oplus \dots \oplus A_{abn} \otimes (X_{an} \ominus X_{bn}) \quad (1)$$

where \otimes , \oplus , and \ominus are the product, additive, and difference operation based on the extension principle for the fuzzy set, respectively.

The parameter A_{jko} involves a response bias owing to presentation order, context effects, and the scale parameter of the dependent variables. The parameter A_{jko} would be a fuzzy variable and larger than A_{ab0} if X_a were more salient than X_b . This model can be reduced to the Fuzzy Utility Difference Model (Nakamura, 1992) if multi-attribute weighting parameters are assumed to be crisp numbers, and reduced to the Additive Difference Model (Tversky, 1969) if multi-attribute weighting parameters and the values of multi-attributes are assumed to be crisp numbers.

2.2.6 Logistic model of ambiguous comparative judgement

Let an ambiguous preference relation that is bounded (e.g., fuzzy probability in $[0,1]$) be $p(X_a \succ X_b)$ for $X_a \succ X_b$. $p(X_a \succ X_b)$ and be represented as the following logistic model using L-R fuzzy numbers:

$$\log (p(X_a \succ X_b) \oplus (1 \ominus p(X_j \succ X_k))) = \ln X_{b1}) \text{ type correction and drawing figures. mments and } A_{ab0} \oplus A_{ab1} \otimes (X_{a1} \ominus X_{b1}) \oplus \dots \oplus A_{abn} \otimes (X_{an} \ominus X_{bn}) \quad (2)$$

where \log , \oplus , \otimes , \oplus , and \ominus are logarithmic, division, product, additive, and difference operations based on the extension principle for the fuzzy set, respectively.

The second model of the equation (2) is the model for $[0,1]$. However, the model could apply to not only the interval $[0,1]$ but also any finite interval $[a,b]$ ($a < b$). Therefore, the model of the equation (2) is considered to be a special case for the finite interval model.

2.2.7 Explaining non-comparability and intransitivity

Non-comparability and intransitivity properties are explained if a threshold of comparative judgment is assumed, if intransitivity is indicated by the necessity measure of fuzzy comparative relation resulting from the existence of the threshold, and if a necessity measure for fuzzy relation does not always lead to comparability. That is,

$$X_a \succ X_b \text{ iff } Nes (v(X_a \succ X_b) > \theta) \quad (3)$$

or

$$X_a \succ X_b \text{ iff } Nes(p(X_a \succ X_b) \oplus (1 \ominus p(X_a \succ X_b))) > P_\theta \quad (4)$$

where $Nes(\cdot)$ is a necessity measure, and θ and P_θ are threshold parameters for the additive difference model and the logistic regression model, respectively. Assuming the above relation of (3) or (4), it is clear that intransitivity and non-comparability hold in the comparative judgment.

3. Fuzzy data analysis for the ambiguous comparative judgment model

3.1 Fuzzy rating data and fuzzy set

Traditional approaches to the measurement of social judgment have involved methods such as the semantic differential, the Likert scale, or the Thurstone scale. Although insights into the ambiguous nature of social judgment were identified early in the development of measurement of social judgment, the subsequent methods used failed to capture this ambiguity, no doubt because traditional mathematics was not well developed for dealing with vagueness of judgment (Hesketh et al., 1988).

In order to measure the vagueness of human judgment, the fuzzy rating method has recently been proposed and developed (Hesketh et al., 1988; Takemura, 1996). In the fuzzy rating method, respondents select a representative rating point on a scale and indicate lower or upper rating points if they wish depending upon the relative vagueness of their judgment (see Figure 2). For example, the fuzzy rating method would be useful for measuring perceived temperature indicating the representative value and the lower or upper values. This rating scale allows for asymmetries, and overcomes the problem, identified by Smithson (1987), of researchers arbitrarily deciding most representative value from a range of scores. By making certain simplifying assumptions (not uncommon within fuzzy set theory), the rating can be viewed as a L-R fuzzy number, hence making possible the use of fuzzy set theoretic operations).

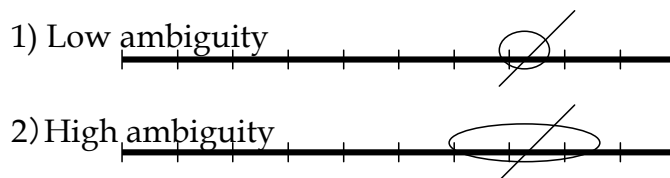


Fig. 2. Example of Fuzzy Rating

A fuzzy set A is defined as follows. Let X denote a universal set, such as $X = \{x_1, x_2, \dots, x_n\}$. Then, the membership function $\mu_A \subseteq X$ by which a fuzzy set A is defined has the form

$$\mu_A : X \rightarrow [0, 1],$$

where $[0, 1]$ denotes the interval of real numbers from 0 to 1, inclusive.

The concept of a fuzzy set is the foundation for analysis where fuzziness exists (Zadeh, 1965). a fuzzy set may be expressed as:

$$\begin{aligned} A &= \mu_A(x_1)/x_1 \oplus \mu_A(x_2)/x_2 \oplus \dots \oplus \mu_A(x_n)/x_n \\ &= \bigoplus_{i=1}^n \mu_A(x_i)/x_i, \end{aligned}$$

where $\mu_A(x_i)$ represents the "grade of membership" of x_i in A , or the degree to which x_i satisfies the properties of the set A . It should be noted that here the symbol "+" does not refer to the ordinary addition.

μ_A is called a membership function, or a possibility function. The x_i values are drawn from a global set of all possible values, X . Grade of membership take values between 0 and 1. The membership function has a value of 0 when the properties of the fuzzy set are not at all satisfied, and 1 when the properties of fuzzy set are completely satisfied.

Hesketh et al.(1988) pointed out that fuzzy rating data can be represented as fuzzy sets by making certain simplifying assumptions, which are not uncommon within fuzzy set theory. According to Hesketh et al.(1988), those assumptions are:

1. The fuzzy set has a convex membership function.
2. The global set X is represented along the horizontal axis.
3. The fuzzy membership function takes its maximum value, one, at the point on the fuzzy support represented by the representative point.
4. The extent of the fuzzy support is represented by the horizontal lines to either side of evaluated point.
5. The fuzzy membership function tapers uniformly from its value of one at the representative point to a value of zero beyond the fuzzy support or the left and right extensions. The membership value of the lower point and the upper point is 0.

Making those assumptions, fuzzy rating data in this study can be expressed as a fuzzy number which is a kind of fuzzy set. The concept of the fuzzy number can be defined from the concept of the fuzzy subset (Kaufman & Gupta, 1985). The properties of fuzzy numbers are the convexity and the normality of a fuzzy subset.

Firstly, the convexity of the fuzzy subset is defined as follows: A fuzzy subset $A \subseteq R$ is convex if and only if every ordinary

$$A_\alpha = \{x \mid \mu_A(x) \geq \alpha\}, \alpha \in [0,1],$$

subset is convex(That is, in the case of a closed interval of R).

Secondly, the normality of the fuzzy subset is defined as follows: A fuzzy subset $A \subseteq R$ is normal if and only if

$$\forall x \in R, \max_x \mu_A(x) = 1.$$

One of the most well known fuzzy numbers is the L-R fuzzy number (Dubois & Prade,1980).

The L-R fuzzy number is defined as follows:

$\forall x \in R:$

$$\begin{cases} \mu_A(x) = L((x - m)/u), & -\infty < x < m, \\ = 1, & x = m, \\ = R((x - m)/v), & m < x < \infty, \end{cases}$$

where $L((x - m)/u)$ is a increasing monotonic function, $R((x - m)/v)$ is a decreasing monotonic function, $u > 0$, and $v > 0$.

An example of the fuzzy rating scale and of the representation of the rating data using L-R fuzzy number are shown in Figure 3. Note in Figure 3 that representations of variables are abbreviated as follows: x_{ij}^L for $x_{ij} (0)^L$, x_{ij}^R for $x_{ij} (0)^R$, x_{ij}^M for $x_{ij} (1)^L = x_{ij} (1)^R$.

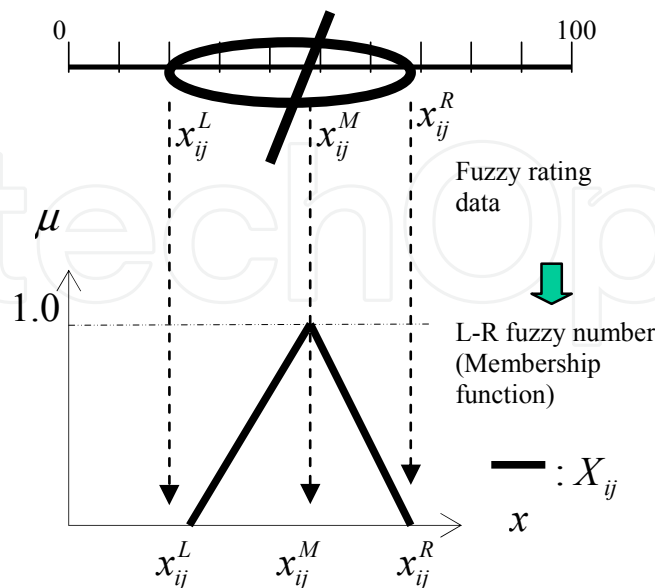


Fig. 3. Fuzzy Rating Data and Its Representation by L-R Fuzzy Numbers

3.2 Analysis of the additive difference type model

The set of fuzzy input-output data for the k -th observation is defined as:

$$(Y_{abk}; X_{a1k}, X_{a2k}, \dots, X_{ank}, X_{b1k}, X_{b2k}, \dots, X_{bnk}) \quad (5)$$

where Y_{abk} indicates the k -th observation's ambiguous preference for the a -th alternative (a) over the b -th alternative (b), which represented by fuzzy L-R numbers, and X_{ajk} and X_{bjk} are the j -th attribute values of the alternatives (a and b) for observation k .

Let X_{abjk} be $X_{ajk} - X_{bjk}$, where $-$ is a difference operator based on the fuzzy extension principle, and denote X_k as the abbreviation of X_{abk} in the following section. Therefore, a set of fuzzy input-output data for the i -th observation is re-written as:

$$(Y_k; X_{1k}, X_{2k}, \dots, X_{nk}), k=1, 2, \dots, N \quad (6)$$

where Y_k is a fuzzy dependent variable, and X_{jk} is a fuzzy independent variable represented by L-R fuzzy numbers. For simplicity, assume that Y_k and X_{jk} are positive for any membership value, $\alpha \in (0,1)$.

The fuzzy linear regression model (where both input and output data are fuzzy numbers) is represented as follows:

$$\bar{Y}_k = A_0 \oplus A_1 \otimes X_{1k} \oplus \dots \oplus A_n \otimes X_{nk} \quad (7)$$

where \bar{Y}_k is a fuzzy estimated variable, $A_j (j=1, \dots, n)$ is a fuzzy regression parameter represented by an L-R fuzzy number, \otimes is an additive operator, and \oplus is the product operator based on the extension principle.

It should be noted that although the explicit form of the membership function of \bar{Y}_k cannot be directly obtained, the α -level set of \bar{Y}_k can be obtained from Nguyen's theorem (Nguyen, 1978).

Let $z_{k(\alpha)}^L$ be a lower value of \bar{Y}_k , and $z_{k(\alpha)}^R$ be an upper value of \bar{Y}_k .

Then,

$$Z_k = [z_{k(\alpha)}^L, z_{k(\alpha)}^R], \quad \alpha \in (0, 1] \quad (8)$$

Where

$$z_{k(\alpha)}^L = \sum_{j=0}^n \left\{ \min \left(a_{j(\alpha)}^L x_{jk(\alpha)}^L, a_{j(\alpha)}^L x_{jk(\alpha)}^R \right) \right\} \quad (9)$$

$$z_{k(\alpha)}^R = \sum_{j=0}^n \left\{ \max \left(a_{j(\alpha)}^R x_{jk(\alpha)}^L, a_{j(\alpha)}^R x_{jk(\alpha)}^R \right) \right\} \quad (10)$$

$$x_{0k(\alpha)}^L = x_{0k(\alpha)}^R = 1 \tag{11}$$

In the above Equation (9), $a_{j(\alpha)}^L x_{jk(\alpha)}^L$ is a product between the lower value of the α -level fuzzy coefficient for the j -th attribute and the α -level set of fuzzy input data X_{jk} , $a_{j(\alpha)}^L x_{jk(\alpha)}^R$, $a_{j(\alpha)}^R x_{jk(\alpha)}^L$, or $a_{j(\alpha)}^R x_{jk(\alpha)}^R$ is defined in the same manner, respectively. $x_{0k(\alpha)}^L$ and $x_{0k(\alpha)}^R$ are assumed to be 1 (a crisp number) for the purpose of estimation for the fuzzy bias parameter A_0 .

To define the dissimilarity between the predicted and observed values of the dependent variable, the following indicator $D_k(\alpha)^2$ was adopted:

$$D_k(\alpha)^2 = (y_{k(\alpha)}^L - z_{k(\alpha)}^L)^2 + (y_{k(\alpha)}^R - z_{k(\alpha)}^R)^2 \tag{12}$$

The definition in Equation (12) can be applied to interval data as well as to L-R fuzzy numbers. That is, Equation (12) represents the sum of squares for the distance between interval data.

To generalize, a dissimilarity indicator representing the square of the distance for L-R fuzzy numbers can be written as follows:

$$Dk^2 = \sum_{j=0}^n w_j ((y_{k(\alpha_j)}^L - z_{k(\alpha_j)}^L)^2 + (y_{k(\alpha_j)}^R - z_{k(\alpha_j)}^R)^2) \tag{13}$$

where $\alpha_j = jh/n$, $j = 0, \dots, n$, h is an equal interval, and w_j is a weight for the j -th level.

In the case of a triangular fuzzy number with $w_j = 1$, the above equation is approximately represented as:

$$Dk^2 = (y_{k(0)}^L - z_{k(0)}^L)^2 + (y_{k(1)}^L - z_{k(1)}^L)^2 + (y_{k(0)}^R - z_{k(0)}^R)^2 \tag{14}$$

The proposed method is to estimate fuzzy coefficients using minimization of the sum of D_k^2 respecting k . That is,

$$\text{Objective function: Min } \sum_{k=1}^N D_k^2 \tag{15}$$

$$\text{Subject to: } a_{j(h)}^L \geq 0, j \in J_1 \tag{16}$$

$$a_{j(h)}^L \leq 0, a_{j(h)}^R \geq 0, j \in J_2 \tag{17}$$

$$a_{j(h)}^R \leq 0, j \in J_3 \tag{18}$$

$$-a_{j(h)}^L + a_{j(h)}^R \geq 0 \tag{19}$$

Where $j \in \{0, \dots, n\} = J_1 \cup J_2 \cup J_3$, $J_1 \cap J_2 = \emptyset$, $J_2 \cap J_3 = \emptyset$, $J_3 \cap J_1 = \emptyset$,

$$z_k^L(\alpha) = \sum_{j \in J_1} a_{j(\alpha)}^L x_{jk(\alpha)}^L + \sum_{j \in J_2} a_{j(\alpha)}^L x_{jk(\alpha)}^R \quad (20)$$

$$z_k^R(\alpha) = \sum_{j \in J_1, J_2} a_{j(\alpha)}^R x_{jk(\alpha)}^R + \sum_{j \in J_3} a_{j(\alpha)}^R x_{jk(\alpha)}^L \quad (21)$$

The estimated coefficients can be derived through quadratic programming. The proposed fuzzy least squares method is also shown in Figure 4.

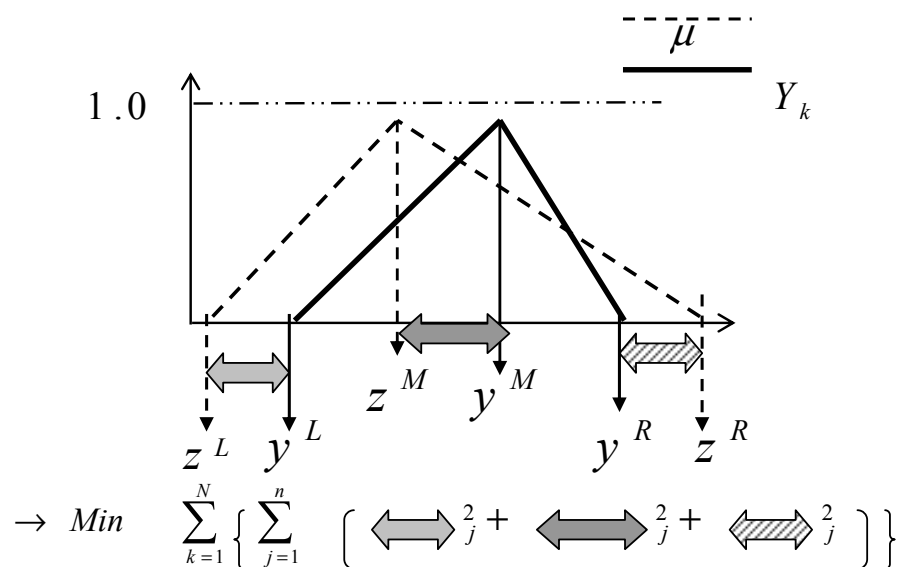


Fig. 4. Fuzzy Least Squares Regressions Analysis for Fuzzy Input and Output Data

3.3 Analysis of the logistic type model

Although the fuzzy linear regression analysis in the fuzzy additive difference model can give satisfactory results, these fuzzy regression analyses may fail to interpret psychological judgment data that have bounds on a psychological scale. For example, a perceived purchase probability has $[0,1]$ interval and cannot be greater than 1 or less than 0. For such data, these fuzzy regression analyses may predict the values that are greater than 1 or less than 0. It may happen that the predicted values are greater than the highest bound or less than the lowest bound, and this causes a significant problem if the predicted values are used in a subsequent analysis. Therefore, the present study also attempted to solve this problem by setting predicted values to be greater than the lowest value (such as 0) or less than the

highest value (such as 1). The present study develops the concept of logistic regression for the crisp numbers, and then proposes the fuzzy version of logistic regression analysis for fuzzy input and output data.

The set of fuzzy input-output data for the k -th observation is defined as:

$$(P_{abk}; X_{a1k}, X_{a2k}, \dots, X_{ank}; X_{b1k}, X_{b2k}, \dots, X_{bnk}) \tag{22}$$

where P_{abk} indicates the k -th observation's ambiguous preference for the a -th alternative (a) over the b -th alternative (b), which is represented by fuzzy L-R numbers, and X_{ajk} and X_{bjk} are the j -th attribute values of the alternatives (a and b) for observation k .

Let X_{abjk} be $X_{ajk} \ominus X_{bjk}$, where \ominus is a difference operator based on the fuzzy extension principle, and denote X_k as the abbreviation of X_{abk} in the following section. Therefore, a set of fuzzy input-output data for the i -th observation is re-written as:

$$(P_k; X_{1k}, X_{2k}, \dots, X_{nk}), k=1,2,\dots,N \tag{23}$$

where P_k is a fuzzy dependent variable, and X_{jk} is a fuzzy independent variable represented by L-R fuzzy numbers. For simplicity, I assume that P_k and X_{jk} are positive for any membership value, $\alpha \in (0,1)$.

The fuzzy logic regression model (where both input and output data are fuzzy numbers) is represented as follows:

$$\overline{\log(P_k \oslash (1 \ominus P_k))} = A_0 \otimes X_{i0} \oplus A_1 \otimes X_{i1} \oplus \dots \oplus A_m \otimes X_{im} \tag{24}$$

where $\overline{\log(P_k \oslash (1 \ominus P_k))}$ is the estimated fuzzy log odds, \oslash is the division operator, \ominus is the difference operator, \otimes is the product operator, and \oplus is the additive operator based on the extension principle for the fuzzy set, respectively.

It should be noted that although the explicit form of the membership function of $\overline{\log(P_k \oslash (1 \ominus P_k))}$ cannot be directly obtained, the α -level set of $\overline{\log(P_k \oslash (1 \ominus P_k))}$ can be obtained using Nguyen's theorem (Nguyen, 1978).

Let $P_{k(\alpha)}^L$ be the lower bound of the dependent fuzzy variable and $P_{k(\alpha)}^R$ be the upper bound. Then, the α level set of the fuzzy dependent variable P_k can be represented as $P_{k\alpha} = [P_{k(\alpha)}^L, P_{k(\alpha)}^R], \alpha \in (0,1)$.

Therefore, the α level set of the left term in Equation (24) is as follows:

$$\begin{aligned} & [\overline{\log(P_k \oslash (1 \ominus P_k))}]_{\alpha=} \\ & [\min(\overline{\log(P_{k(\alpha)}^L / (1 - P_{k(\alpha)}^L)), \log(P_{k(\alpha)}^R / (1 - P_{k(\alpha)}^R))}) \\ & \max(\overline{\log(P_{k(\alpha)}^L / (1 - P_{k(\alpha)}^L)), \log(P_{k(\alpha)}^R / (1 - P_{k(\alpha)}^R))})] \end{aligned} \tag{25}$$

Let $z_{k(\alpha)}^L$ be a lower value of $[\log(P_k \ominus (1 \ominus P_k))]_{\alpha}$, and $z_{k(\alpha)}^R$ be an upper value of $[\log(P_k \ominus (1 \ominus P_k))]_{\alpha}$

where

$$z_{k(\alpha)}^L = \sum_{j=0}^n \left\{ \min \left(a_{j(\alpha)}^L x_{jk(\alpha)}^L, a_{j(\alpha)}^L x_{jk(\alpha)}^R \right) \right\} \quad (26)$$

$$z_{k(\alpha)}^R = \sum_{j=0}^n \left\{ \max \left(a_{j(\alpha)}^R x_{jk(\alpha)}^L, a_{j(\alpha)}^R x_{jk(\alpha)}^R \right) \right\} \quad (27)$$

$$x_{0k(\alpha)}^L = x_{0k(\alpha)}^R = 1 \quad (28)$$

In the above Equation (26), is a product between the lower value of the α -level fuzzy coefficient for the j -th attribute and the α -level set of fuzzy input data X_{jk} , or is defined in the same manner, respectively. and are assumed to be 1 (a crisp number) for the purpose of estimation for the fuzzy bias parameter A_0 . The parameter estimation method is basically the same as the fuzzy logistic regression method and a more concrete procedure is described in Takemura (2004).

4. Numerical example of the data analysis method

To demonstrate the appropriateness of the proposed data analysis methods, the detail numerical examples are shown for the individual level analysis (Takemura, 2007) and group level analysis (Takemura, Matsumoto, Matsuyama, & Kobayashi, 2011) of ambiguous comparative judgments.

4.1. Individual level analysis of ambiguous comparative model

4.1.1 Example of additive difference model

4.1.1.1 Participant and procedure

The participant was a 43-year-old faculty member of Waseda University. The participant rated differences in WTP for two different computers (DELL brand) with three types of attribute information (hard disk: 100 or 60 GB; memory: 2.80 or 2.40 GHz; new or used product). The participant compared a certain alternative with seven different alternatives. The participant provided representative values and lower and upper WTP values using a fuzzy rating method. (see Figure 5)

The participant was asked the amount of money he would be willing to pay to upgrade the inferior from inferior alternative to superior alternative using fuzzy rating method. That is, the participant answered the lower value, the representative value, and upper value for the amount of money he would be willing to pay.

Lower Value	Representative Value	Upper Value
() Yen	() Yen	() Yen

Fig. 5. Example of a Fuzzy Rating in WTP Task.

The participant also rated the desirability of the attribute information for each computer using a fuzzy rating method. The fuzzy rating scale of desirability ranged from 0 point to 100 points. (see Figure 6). That is, the participant answered the lower value, the representative value, and upper value for each attribute value.

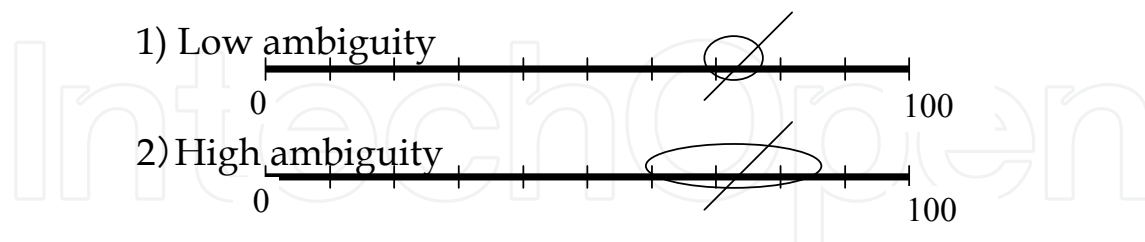


Fig. 6. Example of a Fuzzy Desirability Rating.

4.1.1.2 Analysis and results

The fuzzy coefficients were obtained by fuzzy linear regression analysis using the least squares under constraints, as shown in Tables 1 and 2. The dependent variable of Table 1 was the same as that in Table 2. However, the independent variables in Table 1 are objective values measured by crisp numbers, whereas in Table 2 the independent variables are fuzzy rating values measured by an L-R fuzzy number. The parameter of A_{jko} involves a response bias owing to presentation order, context effects, and the scale parameter of the dependent variables. The parameter A_{jko} would be a fuzzy variable and larger than A_{abo} if X_a were more salient than X_b . This model can be reduced to the Fuzzy Utility Difference Model (Nakamura, 1992) if multi-attribute weighting parameters are assumed to be crisp numbers, and reduced to the Additive Difference Model (Tversky, 1969) if multi-attribute weighting parameters and the values of multi-attributes are assumed to be crisp numbers as explained before. According to Tables 1 and 2, the preference strength concerning comparative judgment was influenced most by whether the target computer was new or used. The impact of the hard disks' attributes was smaller than that of the new-used dimension.

4.1.2 Example of the logistic model

4.1.2.1 Participant and procedure

The participant was a 43-year-old adult. The participant rated the ambiguous probability of preferring a certain computer (DELL brand) out of seven different computers. Three types of attribute information (hard disk: 100 or 60 GB; memory: 2.80 or 2.40 GHz; new or used product) were manipulated in the same manner as in the previous judgment task.. That is, the participant answered the lower value, the representative value, and upper value for the probability that superior alternative is preferred to inferior alternative. The participant used the fuzzy rating method to provide representative, lower, and upper values of probabilities (see Figure 7).

	Attribute	Value	
Fuzzy Coefficient	Hard Disk(L)	Lower	78.5
	Hard Disk (M)	Representative	85.7
	Hard Disk (R)	Upper	986.8
	Memory(L)	Lower	0.0
	Memory(M)	Representative	0.0
	Memory(R)	Upper	0.0
	New or Used (R)	Lower	22 332.5
	New or Used (M)	Representative	22 332.5
	New or Used (L)	Upper	22 332.5
	A_{jk0} (L)	Lower	25 450.8
A_{jk0} (M)	Representative	29 420.1	
A_{jk0} (R)	Upper	33 111.2	

Note: The independent variables are crisp numbers.

Table 1. Coefficients of Fuzzy Regression Analysis

	Attribute	Value	
Fuzzy Coefficient	Hard Disk(L)	Lower	33.9
	Hard Disk (M)	Representative	33.9
	Hard Disk (R)	Upper	33.9
	Memory(L)	Lower	0.0
	Memory(M)	Representative	0.0
	Memory(R)	Upper	0.0
	New or Used (R)	Lower	446.1
	New or Used (M)	Representative	446.1
	New or Used (L)	Upper	446.1
	A_{jk0} (L)	Lower	36 082.1
A_{jk0} (M)	Representative	36 082.1	
A_{jk0} (R)	Upper	48 004.0	

Note: The independent variables are fuzzy L-R numbers.

Table 2. Coefficients of Fuzzy Regression Analysis

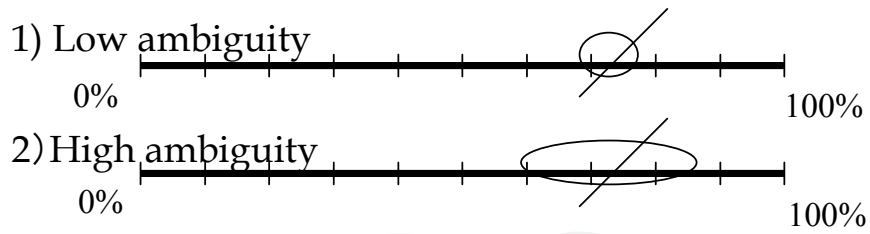


Fig. 7. Example of Fuzzy Probability Rating.

4.1.2.2 Analysis and results

The fuzzy coefficients were obtained by fuzzy linear regression analysis using least squares under constraints, as shown in Tables 3 and 4. However, in Table 3 the independent variables are objective values measured by crisp numbers, whereas in Table 4 the independent variables are fuzzy rating values measured by an L-R fuzzy number. The parameter A_{jk0} involves a response bias owing to presentation order, context effects, and the scale parameter of the dependent variables. According to Tables 3 and 4, the bounded preference strength was influenced most by whether the target computer was new or used. Interestingly, the impact of the attribute for memory was slightly greater than was the case in Tables 1 and 2.

	Attribute	Value	
	Hard Disk (L)	Lower	0.000
	Hard Disk(M)	Representative	0.000
	Hard Disk (R)	Upper	0.009
Fuzzy	Memory(L)	Lower	1.781
Coefficient	Memory(M)	Representative	1.781
	Memory(R)	Upper	1.881
	New or Used (R)	Lower	1.791
	New or Used (M)	Representative	2.097
	New or Used (L)	Upper	2.777
	A_{jk0} (L)	Lower	0.847
	A_{jk0} (M)	Representative	1.201
	A_{jk0} (R)	Upper	1.443

Note: The independent variables are crisp numbers.

Table 3. Coefficients of Fuzzy Logistic Regression Analysis

	Attribute	Value	
Fuzzy Coefficient	Hard Disk(L)	Lower	0.000
	Hard Disk (M)	Representative	0.000
	Hard Disk (R)	Upper	0.000
	Memory(L)	Lower	0.008
	Memory(M)	Representative	0.008
	Memory(R)	Upper	0.008
	New or Used (R)	Lower	0.043
	New or Used (M)	Representative	0.043
	New or Used (L)	Upper	0.043
	A_{jk0} (L)	Lower	1.806
A_{jk0} (M)	Representative	1.806	
A_{jk0} (R)	Upper	1.806	

Note: The independent variables are fuzzy L-R numbers.

Table 4. Coefficients of Fuzzy Logistic Regression Analysis

4.2 Group level analysis of ambiguous comparative model

4.2.1 Example of additive difference model

4.2.1.1 Participants and procedure

The participants were 100 undergraduate university students (68 female and 32 male students) enrolled in an economic

psychology class at Waseda University. They were recruited for an experiment investigating “consumer preference”.

Their average age was 21.3 years old. The participants rated differences in WTP for two different digital cameras with three types of attribute information (weight: 130 gram or 160 gram; memory: 25 or 50 MB; display size: 2.5 or 5.0 inches). The participants compared a certain alternative with seven different alternatives. The participants also rated differences in WTP for two different mobile phones with three types of attribute information (weight: 123 gram or 132 gram; pixel number: 3,200,000 or 5,070,000 pixels; display size: 2.8 or 3.0 inches). The participants compared a certain alternative with seven different mobile phones. The participant provided representative values and lower and upper WTP values using a fuzzy rating method. The participants were asked the amount of money he would be willing to pay to upgrade the inferior from inferior alternative to superior alternative using fuzzy rating method. That is, the participants answered the lower value, the representative value, and upper value for the amount of money he would be willing to pay. An example of fuzzy WTP rating is illustrated in the Figure 8.

Question:

Which alternative do you prefer ? Please circle the superior alternative.

Then, please estimate the amount of money you would be willing to pay to upgrade the inferior alternative from inferior alternative to superior alternative using fuzzy rating method. That is, the participants answered the lower value, the representative value, and upper value for the amount of money you would be willing to pay.

Brand A	Brand B
Weight: 130g	Weight: 160g
Memory: 25MB	Memory: 50MB
Display: 50 inches	Display: 25 inches

Difference

Minimum: 2,000 yen ----- Maximum: 10,000 yen

Representative Value: 5,000 yen



Fig. 8. Example of Fuzzy WTP Rating

4.2.1.2 Analysis and results

The fuzzy coefficients were obtained by fuzzy linear regression analysis using the least squares under constraints, as shown in Tables 5 for the digital camera data and Table 6 for mobile phone data. The independent variables in Table 5 and Table 6 are objective values measured by crisp numbers. The parameter of A_{jk0} involves a response bias owing to presentation order, context effects, and the scale parameter of the dependent variables. According to Tables 5, the preference strength concerning comparative judgment was influenced most by whether the target digital camera was 2.5 or 5.0 inches. The impact of the memory's attribute was smaller than those of display size and weight dimensions. According to Tables 6, the preference strength concerning comparative judgment was influenced most by whether the target mobile phone was 2.8 or 3.0 inches. The impact of the pixel number's attribute was smaller than those of display size and weight dimensions. The participants also rated the desirability of the attribute information for each computer using a fuzzy rating method. The fuzzy rating scale of desirability ranged from 0 point to 100 points. (see Figure 6). That is, the participant answered the lower value, the representative value, and upper value for each attribute value.

	Attribute	Value	
Fuzzy Coefficient	Weight(L)	Lower	48.57
	Weight (M)	Representative	48.57
	Weight (R)	Upper	68.33
	Memory(L)	Lower	8.29
	Memory(M)	Representative	8.29
	Memory(R)	Upper	14.62
	Display Size (R)	Lower	223.10
	Display Size (M)	Representative	4791.98
	Display Size (L)	Upper	4791.98
	A_{jk0} (L)	Lower	11361.25
	A_{jk0} (M)	Representative	11361.25
	A_{jk0} (R)	Upper	15447.54

Note: The independent variables are crisp numbers.

Table 5. Coefficients of Fuzzy Regression Analysis for Digital Camera Data

	Attribute	Value	
Fuzzy Coefficient	Weight(L)	Lower	28.84
	Weight (M)	Representative	28.84
	Weight (R)	Upper	53.44
	Pixel Number(L)	Lower	-12.12
	Pixel Number(M)	Representative	28.55
	Pixel Number(R)	Upper	28.55
	Display Size (R)	Lower	-233.73
	Display Size (M)	Representative	190.29
	Display Size (L)	Upper	190.29
	A_{jk0} (L)	Lower	7758.98
	A_{jk0} (M)	Representative	8234.94
	A_{jk0} (R)	Upper	12569.35

Note: The independent variables are crisp numbers.

Table 6. Coefficients of Fuzzy Regression Analysis for Mobile Phone Data

4.2.2 Example of the logistic model

4.2.2.1 Participants and procedure

The participants were 100 undergraduate university students (68 female and 32 male students). Their average age was 21.3 years old. The participants rated the ambiguous probability of preferring a certain digital camera out of seven different digital cameras. The three types of attribute information (weight: 130 gram or 160 gram; memory: 25 or 50 MB; display size: 2.5 or 5.0 inches) were manipulated in the same manner as in the previous individual judgment task. They also rated the ambiguous probability of preferring a certain mobile phone out of seven different mobile phones. The three types of attribute information (weight: 123 gram or 132 gram; pixel number: 3,200,000 or 5,070,000 pixels; display size: 2.8 or 3.0 inches) were manipulated in the same manner in the previous judgment task. The participant provided representative values and lower and upper values of probabilities. That is, the participants answered the lower value, the representative value, and upper value for the probability that superior alternative is preferred to inferior alternative. The participants used the fuzzy rating method to provide representative, lower, and upper values of probabilities (see Figure 7).

4.2.2.2 Analysis and results

The fuzzy coefficients were obtained by fuzzy logistic regression analysis using the least squares under constraints, as shown in Tables 7 for the digital camera data and Table 8 for mobile phone data. The independent variables in Table 7 and Table 8 are objective values measured by crisp numbers. The parameter of A_{jk0} involves a response bias owing to presentation order, context effects, and the scale parameter of the dependent variables. According to Tables 7, the bounded preference strength was influenced most by whether the target digital camera was 2.5 or 5.0 inches. The impact of the memory's attribute was smaller than those of display size and weight dimensions. According to Tables 8, the bounded preference strength was influenced most by whether the target mobile phone was 2.8 or 3.0 inches. The impact of the weight's attribute was smaller than those of display size and pixel number dimensions.

	Attribute	Value	
Fuzzy Coefficient	Weight(L)	Lower	0.035
	Weight (M)	Representative	0.038
	Weight (R)	Upper	0.054
	Memory(L)	Lower	0.003
	Memory(M)	Representative	0.003
	Memory(R)	Upper	0.003
	Display Size (R)	Lower	2.625
	Display Size (M)	Representative	2.625
	Display Size (L)	Upper	2.625
	A_{jk0} (L)	Lower	-0.122
	A_{jk0} (M)	Representative	0.459
	A_{jk0} (R)	Upper	1.072

Note: The independent variables are crisp numbers.

Table 7. Coefficients of Fuzzy Logistic Regression Analysis for Digital Camera Data

	Attribute	Value	
Fuzzy Coefficient	Weight(L)	Lower	0.002
	Weight (M)	Representative	0.002
	Weight (R)	Upper	0.009
	Pixel Number(L)	Lower	0.012
	Pixel Number(M)	Representative	0.017
	Pixel Number(R)	Upper	0.024
	Display Size (R)	Lower	0.161
	Display Size (M)	Representative	0.165
	Display Size (L)	Upper	0.232
	A_{jk0} (L)	Lower	-0.871
A_{jk0} (M)	Representative	0.030	
A_{jk0} (R)	Upper	0.887	

Note: The independent variables are crisp numbers.

Table 8. Coefficients of Fuzzy Logistic Regression Analysis for Mobile Phone Data

5. Conclusion

This chapter introduces fuzzy set models for ambiguous comparative judgments, which do not always hold transitivity and comparability properties. The first type of model was a fuzzy theoretical extension of the additive difference model for preference that is used to explain ambiguous preference strength. This model can be reduced to the Fuzzy Utility Difference Model (Nakamura, 1992) if multi-attribute weighting parameters are assumed to be crisp numbers, and can be reduced to the Additive Difference Model (Tversky, 1969) if multi-attribute weighting parameters and the values of multi-attributes are assumed to be crisp numbers. The second type of model was a fuzzy logistic model for explaining ambiguous preference in which preference strength is bounded, such as a probability measure.

In both models, multi-attribute weighting parameters and all attribute values were assumed to be asymmetric fuzzy L-R numbers. For each model, parameter estimation method using fuzzy regression analysis was introduced. Numerical examples for comparison were also demonstrated. As the objective of the numerical examples was to demonstrate that the proposed estimation might be viable, further empirical studies will be needed. Moreover, because the two models require different evaluation methods, comparisons of the psychological effects of the two methods must be studied further.

In this chapter, the least squares method was used for data analyses of the two models. However, the possibilistic linear regression analysis (Sakawa & Yano, 1992) and the possibilistic logistic regression analysis (Takemura, 2004) could also be used in the data analysis of the additive difference type model and the logistic type model, respectively. The proposed models and the analyses for ambiguous comparative judgments will be applied to

marketing research, risk perception research, and human judgment and decision-making research. Empirical research using possibilistic analysis and least squares analysis will be needed to examine the validity of these models.

Results of these applications to psychological study indicated that the parameter estimated in the proposed analysis was meaningful for social judgment study. This study has a methodological restriction on statistical inferences for fuzzy parameters. Therefore, we plan further work on the fuzzy theoretic analysis of social judgment directed toward the statistical study of fuzzy regression analysis and fuzzy logistic regression analysis such as statistical tests of parameters, outlier detection, and step-wise variable selection.

6. Acknowledgment

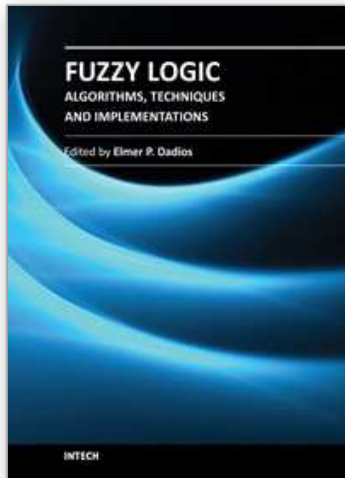
This work was supported in part by Grants in Aids for Grant-in-Aid for Scientific Research on Priority Area, The Ministry of Education, Culture, Sports, Science and Technology(MEXT). I thank Matsumoto,T., Matsuyama,S,and Kobayashi,M.. for their assistance, and the editor and the reviewers for their valuable comments.

7. References

- Anderson,N.H.(1988). A functional approach to person cognition. In T.K.Srull & R.S. Wyer (Eds.), *Advances in social cognition*. vol.1. Hillsdale, New Jersey: Lawrence Erlbaum Associates, pp.37-51.
- Dubois D. & Prade,H. (1980). *Fuzzy sets and systems: Theory and applications*, New York: Academic Press.
- Festinger, L. (1954). A theory of social comparison processes. *Human Relations*, 7, 114–140.
- Hesketh, B., Pryor, R., Gleitzman, M., & Hesketh, T. (1988). Practical applications and psychometric evaluation of a computerised fuzzy graphic rating scale. In T. Zetenyi (Ed.), *Fuzzy sets in psychology* (pp. 425–454). New York: North Holland.
- Kühberger,A.,Schulte-Mecklenbeck,M. & Ranyard,R. (2011). Introduction: Windows for understanding the mind, In M.Schulte-Mecklenbeck, A.Kühberger, & R. Ranyard(Eds.), *A handbook of process tracing methods for decision research*,New York: Psychology Press, pp.3-17.
- Mussweiler, T. (2003). Comparison processes in social judgment: Mechanisms and consequences. *Psychological Review*, 110, 472–489.
- Nakamura, K. (1992). On the nature of intransitivity in human referential judgments. In V. Novak (Ed.), *Fuzzy approach to reasoning and decision making, academia* (pp. 147–162). Prague: Kluwer Academic Publishers.
- Nguyen, H. T. (1978). A note on the extension principle for fuzzy sets. *Journal of Mathematical Analysis and Application*, 64, 369–380.
- Rosch,E. (1975). Cognitive representation of semantic categories. *Journal of Experimental Psychology: General*, 104, 192-233.
- Rosch,E., & Mervis,C.B. (1975). Family resemblances: Studies in the internal structure of categories. *Cognitive Psychology*, 7, 573-603.
- Sakawa, M., & Yano, H. (1992). Multiobjective fuzzy linear regression analysis for fuzzy input-output data. *Fuzzy Sets and Systems*, 47, 173–181.

- Sherif, M., & Hovland, C. I. (1961). *Social judgment: Assimilation and contrast effects in communication and attitude change*. New Haven: Yale University Press.
- Smithson, M. (1987). *Fuzzy set analysis for the behavioral and social sciences*. New York: Springer-Verlag.
- Smithson, M. (1989). *Ignorance and uncertainty*. New York: Springer-Verlag.
- Takemura, K. (1999). A fuzzy linear regression analysis for fuzzy input-output data using the least squares method under linear constraints and its application to fuzzy rating data. *Journal of Advanced Computational Intelligence*, 3, 36–40.
- Takemura, K. (2000). Vagueness in human judgment and decision making. In Z. Q. Liu & S. Miyamoto (Eds), *Soft Computing for Human Centered Machines* (pp. 249–281). Tokyo: Springer Verlag.
- Takemura, K. (2004). Fuzzy logistic regression analysis for fuzzy input and output data. Proceedings of the joint 2nd International Conference on Soft Computing and Intelligent Systems and the 5th International Symposium on Advanced Intelligent Systems 2004 (WE8-5), Yokohama, Japan.
- Takemura, K. (2005). Fuzzy least squares regression analysis for social judgment study. *Journal of Advanced Computational Intelligence*, 9, 461–466.
- Takemura, K. (2007). Ambiguous comparative judgment: Fuzzy set model and data analysis. *Japanese Psychology Research*, 49, 148–156.
- Takemura, K., Matsumoto, T., Matsuyama, S., & Kobayashi, M., (2011). Analysis of consumer's ambiguous comparative judgment. *Discussion Paper, Department of Psychology, Waseda University*.
- Takemura, K. (1996). *Psychology of decision making*. Tokyo: Fukumura Syuppan. (in Japanese).
- Takemura, K. (2011) Model of multi-attribute decision making and good decision. *Operations Research*, 56(10), 583–590 (In Japanese)
- Tversky, A. (1969). Intransitivity of preferences. *Psychological Review*, 76, 31–48.
- Wittgenstein, L. (1953). *Philosophical investigations*. New York: MacMillan.
- Zadeh, A. (1965). Fuzzy sets, *Information and Control*, 8, 338–353.
- Zadeh, A. (1973). Outline of a new approach to the analysis of complex systems and decision processes, *IEEE Transactions on Systems, Man and Cybernetics*, SMC 3(1), 28–44.

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Fuzzy Logic - Algorithms, Techniques and Implementations

Edited by Prof. Elmer Dadios

ISBN 978-953-51-0393-6

Hard cover, 294 pages

Publisher InTech

Published online 28, March, 2012

Published in print edition March, 2012

Fuzzy Logic is becoming an essential method of solving problems in all domains. It gives tremendous impact on the design of autonomous intelligent systems. The purpose of this book is to introduce Hybrid Algorithms, Techniques, and Implementations of Fuzzy Logic. The book consists of thirteen chapters highlighting models and principles of fuzzy logic and issues on its techniques and implementations. The intended readers of this book are engineers, researchers, and graduate students interested in fuzzy logic systems.

How to reference

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Kazuhisa Takemura (2012). Ambiguity and Social Judgment: Fuzzy Set Model and Data Analysis, Fuzzy Logic - Algorithms, Techniques and Implementations, Prof. Elmer Dadios (Ed.), ISBN: 978-953-51-0393-6, InTech, Available from: <http://www.intechopen.com/books/fuzzy-logic-algorithms-techniques-and-implementations/ambiguity-and-social-judgment-fuzzy-set-model-and-data-analysis>

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