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Statistical Thermodynamics

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1. Introduction

This chapter deals with the statistical thermodynamics (statistical mechanics) a modern alternative of the classical (phenomenological) thermodynamics. Its aim is to determine thermodynamic properties of matter from forces acting among molecules. Roots of the discipline are in kinetic theory of gases and are connected with the names Maxwell and Boltzmann. Father of the statistical thermodynamics is Gibbs who introduced its concepts such as the statistical ensemble and others, that have been used up to present.

Nothing can express an importance of the statistical thermodynamics better than the words of Richard Feynman Feynman et al. (2006), the Nobel Prize winner in physics: *If, in some cataclysm, all of scientific knowledge were to be destroyed, and only one sentence passed on to the next generations of creatures, what statement would contain the most information in the fewest words? I believe it is the atomic hypothesis (or the atomic fact, or whatever you wish to call it) that **All things are made of atoms – little particles that move around in perpetual motion, attracting each other when they are a little distance apart, but repelling upon being squeezed into one another.***

In that one sentence, you will see, there is an enormous amount of information about the world, if just a little imagination and thinking are applied.

The chapter is organized as follows. Next section contains axioms of the phenomenological thermodynamics. Basic concepts and axioms of the statistical thermodynamics and relations between the partition function and thermodynamic quantities are in Section 3. Section 4 deals with the ideal gas and Section 5 with the ideal crystal. Intermolecular forces are discussed in Section 6. Section 7 is devoted to the virial expansion and Section 8 to the theories of dense gases and liquids. The final section comments axioms of phenomenological thermodynamics in the light of the statistical thermodynamics.

2. Principles of phenomenological thermodynamics

The phenomenological thermodynamics or simply thermodynamics is a discipline that deals with the thermodynamic system, a macroscopic part of the world. The thermodynamic state of system is given by a limited number of thermodynamic variables. In the simplest case of one-component, one-phase system it is for example volume of the system, amount of substance (*e.g.* in moles) and temperature. Thermodynamics studies changes of thermodynamic quantities such as pressure, internal energy, entropy, *e.t.c.* with thermodynamic variables.

The phenomenological thermodynamics is based on six axioms (or postulates if you wish to call them), four of them are called the laws of thermodynamics:

- **Axiom of existence of the thermodynamic equilibrium**

For thermodynamic system at unchained external conditions there exists a state of the thermodynamic equilibrium in which its macroscopic parameters remain constant in time. The thermodynamic system at unchained external conditions always reaches the state of the thermodynamic equilibrium.

- **Axiom of additivity**

Energy of the thermodynamic system is a sum of energies of its macroscopic parts. This axiom allows to define extensive and intensive thermodynamic quantities.

- **The zeroth law of thermodynamics**

When two systems are in the thermal equilibrium, *i.e.* no heat flows from one system to the other during their thermal contact, then both systems have the same temperature as an intensive thermodynamic parameter. If system A has the same temperature as system B and system B has the same temperature as system C, then system A also has the same temperature as system C (temperature is transitive).

- **The first law of thermodynamics**

There is a function of state called internal energy U . For its total differential dU we write

$$dU = \delta W + \delta Q, \quad (1)$$

where the symbols δQ and δW are not total differentials but represent infinitesimal values of heat Q and work W supplied to the system.

- **The second law of thermodynamics**

There is a function of state called entropy S . For its total differential dS we write

$$dS = \frac{\delta Q}{T}, \quad [\text{reversible process}], \quad (2)$$

$$dS > \frac{\delta Q}{T}, \quad [\text{irreversible process}]. \quad (3)$$

- **The third law of thermodynamics**

At temperature of 0 K, entropy of a pure substance in its most stable crystalline form is zero

$$\lim_{T \rightarrow 0} S = 0. \quad (4)$$

This postulate supplements the second law of thermodynamics by defining a natural referential value of entropy. The third law of thermodynamics implies that temperature of 0 K cannot be attained by any process with a finite number of steps.

Phenomenological thermodynamics using its axioms radically reduces an amount of experimental effort necessary for a determination of the values of thermodynamic quantities. For example enthalpy or entropy of a pure fluid need not be measured at each temperature and pressure but they can be calculated from an equation of state and a temperature dependence of the isobaric heat capacity of ideal gas. However, empirical constants in an equation of state and in the heat capacity must be obtained experimentally.

3. Principles of statistical thermodynamics

3.1 Basic concepts

The statistical thermodynamics considers thermodynamic system as an assembly of a very large number (of the order of 10^{23}) of mutually interacting particles (usually molecules). It uses the following concepts:

- **Microscopic state of system**
The microscopic state of thermodynamic system is given by positions and velocities of all particles in the language of the Newton mechanics, or by the quantum states of the system in the language of quantum mechanics. There is a huge number of microscopic states that correspond to a given thermodynamic (macroscopic) state of the system.
- **Statistical ensemble**
Statistical ensemble is a collection of all systems that are in the same thermodynamic state but in the different microscopic states.
- **Microcanonical ensemble** or NVE ensemble is a collection of all systems at a given number of particles N , volume V and energy E .
- **Canonical ensemble** or NVT ensemble is a collection of all systems at a given number of particles N , volume V and temperature T .
There is a number of ensembles, *e.g.* the grandcanonical (μVT) or isothermal isobaric (NPT) that will not be considered in this work.
- **Time average of thermodynamic quantity**
The time average \bar{X}_τ of a thermodynamic quantity X is given by

$$\bar{X}_\tau = \frac{1}{\tau} \int_0^\tau X(t) dt, \quad (5)$$

where $X(t)$ is a value of X at time t and, τ is a time interval of a measurement.

- **Ensemble average of thermodynamic quantity**
The ensemble average \bar{X}_s of a thermodynamic quantity X is given by

$$\bar{X}_s = \sum_i P_i X_i, \quad (6)$$

where X_i is a value in the quantum state i , and P_i is the probability of the quantum state.

3.2 Axioms of the statistical thermodynamics

The statistical thermodynamics is based on two axioms:

Axiom on equivalence of average values

It is postulated that the time average of thermodynamic quantity X is equivalent to its ensemble average

$$\bar{X}_\tau = \bar{X}_s. \quad (7)$$

Axiom on probability

Probability P_i of a quantum state i is only a function of energy of the quantum state, E_i ,

$$P_i = f(E_i). \quad (8)$$

3.3 Probability in the microcanonical and canonical ensemble

From Eq.(8) relations between the probability and energy can be derived:

Probability in the microcanonical ensemble

All the microscopic states in the microcanonical ensemble have the same energy. Therefore,

$$P_i = \frac{1}{W} \quad \text{for } i = 1, 2, \dots, W, \quad (9)$$

where W is a number of microscopical states (the statistical weight) of the microcanonical ensemble.

Probability in the canonical ensemble

In the canonical ensemble it holds

$$P_i = \frac{\exp(-\beta E_i)}{Q}, \quad (10)$$

where $\beta = \frac{1}{k_B T}$, k_B is the Boltzmann constant, T temperature and Q is the *partition function*

$$Q = \sum_i \exp(-\beta E_i), \quad (11)$$

where the sum is over the microscopic states of the canonical ensemble.

3.4 The partition function and thermodynamic quantities

If the partition function is known thermodynamic quantities may be determined. The following relations between the partition function in the canonical ensemble and thermodynamic quantities can be derived

$$A = -k_B T \ln Q \quad (12)$$

$$U = k_B T^2 \left(\frac{\partial \ln Q}{\partial T} \right)_V \quad (13)$$

$$S = k_B \ln Q + k_B T \left(\frac{\partial \ln Q}{\partial T} \right)_V. \quad (14)$$

$$C_V = \left(\frac{\partial U}{\partial T} \right)_V = k_B T^2 \frac{\partial^2 \ln Q}{\partial T^2} + 2k_B T \left(\frac{\partial \ln Q}{\partial T} \right)_V, \quad (15)$$

$$p = - \left(\frac{\partial A}{\partial V} \right)_T = k_B T \left(\frac{\partial \ln Q}{\partial V} \right)_T, \quad (16)$$

$$H = U + pV = k_B T^2 \left(\frac{\partial \ln Q}{\partial T} \right)_V + V k_B T \left(\frac{\partial \ln Q}{\partial V} \right)_T, \quad (17)$$

$$G = A + pV = -k_B T \ln Q + V k_B T \left(\frac{\partial \ln Q}{\partial V} \right)_T, \quad (18)$$

$$C_p = \left(\frac{\partial H}{\partial T} \right)_V = C_V + V k_B \frac{\partial^2 \ln Q}{\partial V \partial T}. \quad (19)$$

A is Helmholtz free energy, U internal energy, S entropy, C_V isochoric heat capacity, p pressure, H enthalpy, G Gibbs free energy and C_p isobaric heat capacity.

Unfortunately, the partition function is known only for the simplest cases such as the ideal gas (Section 4) or the ideal crystal (Section 5). In all the other cases, real gases and liquids considered here, it can be determined only approximatively.

3.5 Probability and entropy

A relation between entropy S and probabilities P_i of quantum states of a system can be proved in the canonical ensemble

$$S = -k_B \sum_i P_i \ln P_i. \quad (20)$$

For the microcanonical ensemble a similar relation holds

$$S = k_B \ln W, \quad (21)$$

where W is a number of accessible states. This equation (with log instead of ln) is written in the grave of Ludwig Boltzmann in Central Cemetery in Vienna, Austria.

4. Ideal gas

The ideal gas is in statistical thermodynamics modelled by a assembly of particles that do not mutually interact. Then the energy of i -th quantum state of system, E_i , is a sum of energies of individual particles

$$E_i = \sum_{j=1}^N \epsilon_{i,j}. \quad (22)$$

In this way a problem of a determination of the partition function of system is dramatically simplified. For one-component system of N molecules it holds

$$Q = \frac{q^N}{N!}, \quad (23)$$

where

$$q = \sum_j \exp(-\beta \epsilon_j) \quad (24)$$

is the partition function of molecule.

The partition function of molecule may be further simplified. The energy of molecule can be approximated by a sum of the translational ϵ_{trans} , the rotational ϵ_{rot} , the vibrational ϵ_{vib} , and the electronic ϵ_{el} contributions (subscript j in ϵ_j is omitted for simplicity of notation)

$$\epsilon = \epsilon_0 + \epsilon_{\text{trans}} + \epsilon_{\text{rot}} + \epsilon_{\text{vib}} + \epsilon_{\text{el}}, \quad (25)$$

where ϵ_0 is the zero point energy. The partition function of system then becomes a product

$$Q = \frac{\exp(-N\beta\epsilon_0)}{N!} q_{\text{trans}} q_{\text{rot}} q_{\text{vib}} q_{\text{el}}. \quad (26)$$

Consequently all thermodynamic quantities of the ideal gas become sums of the corresponding contributions. For example the Helmholtz free energy is

$$\begin{aligned} A &= -k_B T \ln Q \\ &= k_B T \ln N! + U_0 - Nk_B T \ln q_{\text{tr}} - Nk_B T \ln q_{\text{rot}} - Nk_B T \ln q_{\text{vib}} - Nk_B T \ln q_{\text{el}} \\ &= k_B T \ln N! + U_0 + A_{\text{tr}} + A_{\text{rot}} + A_{\text{vib}} + A_{\text{el}}, \end{aligned} \quad (27)$$

where $U_0 = N\epsilon_0$ and A_{tr} , A_{rot} , A_{vib} , A_{el} are the translational, rotational, vibrational, electronic contributions to the Helmholtz free energy, respectively.

4.1 Translational contributions

Translational motions of a molecule are modelled by a particle in a box. For its energy a solution of the Schrödinger equation gives

$$\epsilon_{\text{tr}} = \frac{h^2}{8m} \left(\frac{n_x^2}{a^2} + \frac{n_y^2}{b^2} + \frac{n_z^2}{c^2} \right), \quad (28)$$

where h is the Planck constant, m mass of molecule, and $abc = V$ where V is volume of system. Quantities n_x, n_y, n_z are the quantum numbers of translation. The partition function of translation is

$$q_{\text{tr}} = \left(\frac{2\pi mk_B T}{h^2} \right)^{3/2} V. \quad (29)$$

Translational contribution to the Helmholtz energy is

$$A_{\text{tr}} = -RT \ln q_{\text{tr}} = -RT \ln (\lambda^{-3} V), \quad (30)$$

where $R = Nk_B$ is the gas constant and $\lambda = h/\sqrt{2\pi mk_B T}$ is the Broglie wavelength. The remaining thermodynamic functions are as follows

$$S_{\text{tr}} = - \left(\frac{\partial A_{\text{tr}}}{\partial T} \right)_V = R \ln (\lambda^{-3} V) + \frac{3}{2} R, \quad (31)$$

$$p_{\text{tr}} = - \left(\frac{\partial A_{\text{tr}}}{\partial V} \right)_T = \frac{RT}{V}, \quad (32)$$

$$U_{\text{tr}} = A_{\text{tr}} + TS_{\text{tr}} = \frac{3}{2} RT, \quad (33)$$

$$H_{\text{tr}} = U_{\text{tr}} + p_{\text{tr}} V = \frac{5}{2} RT, \quad (34)$$

$$G_{\text{tr}} = A_{\text{tr}} + p_{\text{tr}} V = -RT \ln (\lambda^{-3} V) + RT, \quad (35)$$

$$C_{V,\text{tr}} = \left(\frac{\partial U_{\text{tr}}}{\partial T} \right)_V = \frac{3}{2} R, \quad (36)$$

$$C_{p,\text{tr}} = \left(\frac{\partial H_{\text{tr}}}{\partial T} \right)_p = \frac{5}{2} R. \quad (37)$$

4.2 Rotational contributions

Rotations of molecule are modelled by the rigid rotator. For linear molecules there are two independent axes of rotation, for non-linear molecules there are three.

4.2.1 Linear molecules

For the partition function of rotation it holds

$$q_{\text{rot}} = \frac{8\pi I k_B T}{\sigma h^2}, \quad (38)$$

where σ is the symmetry number of molecule and I its moment of inertia

$$I = \sum_1^n m_i r_i^2,$$

with n a number of atoms in molecule, m_i their atomic masses and r_i their distances from the center of mass. Contributions to the thermodynamic quantities are

$$A_{\text{rot}} = -RT \ln q_{\text{rot}} = -RT \ln \left(\frac{8\pi^2 I k_B T}{\sigma h^2} \right), \quad (39)$$

$$S_{\text{rot}} = R \ln \left(\frac{8\pi^2 I k_B T}{\sigma h^2} \right) + R, \quad (40)$$

$$p_{\text{rot}} = 0, \quad (41)$$

$$U_{\text{rot}} = RT, \quad (42)$$

$$H_{\text{rot}} = U_{\text{rot}}, \quad (43)$$

$$G_{\text{rot}} = F_{\text{rot}}, \quad (44)$$

$$C_{V,\text{rot}} = R, \quad (45)$$

$$C_{p,\text{rot}} = C_{V,\text{rot}}. \quad (46)$$

4.2.2 Non-linear molecules

The partition function of rotation of a non-linear molecule is

$$q_{\text{rot}} = \frac{1}{\sigma} \left(\frac{8\pi^2 k_B T}{h^2} \right)^{3/2} (\pi I_A I_B I_C)^{1/2}, \quad (47)$$

where I_A , I_B and I_C the principal moments of inertia. Contributions to the thermodynamic quantities are

$$A_{\text{rot}} = -RT \ln q_{\text{rot}} = -RT \ln \left[\frac{1}{\sigma} \left(\frac{8\pi^2 k_B T}{h^2} \right)^{3/2} (\pi I_A I_B I_C)^{1/2} \right], \quad (48)$$

$$S_{\text{rot}} = R \ln \left[\frac{1}{\sigma} \left(\frac{8\pi^2 k_B T}{h^2} \right)^{3/2} (\pi I_A I_B I_C)^{1/2} \right] + \frac{3}{2}R, \quad (49)$$

$$p_{\text{rot}} = 0, \quad (50)$$

$$U_{\text{rot}} = \frac{3}{2}RT, \quad (51)$$

$$H_{\text{rot}} = U_{\text{rot}}, \quad (52)$$

$$G_{\text{rot}} = A_{\text{rot}}, \quad (53)$$

$$C_{V,\text{rot}} = \frac{3}{2}R, \quad (54)$$

$$C_{p,\text{rot}} = C_{V,\text{rot}}. \quad (55)$$

4.3 Vibrational contributions

Vibrations of atoms in molecule around their equilibrium states may be at not very high temperatures approximated by harmonic oscillators.

4.3.1 Diatomic molecules

In a diatomic molecule there is only one vibrational motion. Its partition function is

$$q_{\text{vib}} = [1 - \exp(h\nu_0/k_B T)]^{-1}, \quad (56)$$

where ν_0 is the fundamental harmonic frequency. Vibrational contributions to thermodynamic quantities are

$$A_{\text{vib}} = -RT \ln q_{\text{vib}} = RT \ln (1 - e^{-x}) , \quad (57)$$

$$S_{\text{vib}} = R \frac{xe^{-x}}{1 - e^{-x}} - R \ln (1 - e^{-x}) , \quad (58)$$

$$p_{\text{vib}} = 0 , \quad (59)$$

$$U_{\text{vib}} = RT \frac{xe^{-x}}{1 - e^{-x}} , \quad (60)$$

$$H_{\text{vib}} = U_{\text{vib}} , \quad (61)$$

$$G_{\text{vib}} = A_{\text{vib}} , \quad (62)$$

$$C_{V,\text{vib}} = R \frac{x^2 e^{-x}}{(1 - e^{-x})^2} , \quad (63)$$

$$C_{p,\text{vib}} = C_{V,\text{vib}} , \quad (64)$$

where $x = \frac{h\nu_0}{k_B T}$.

4.3.2 Polyatomic molecules

In n -atomic molecule there is f fundamental harmonic frequencies ν_i where

$$f = \begin{cases} 3n - 5 & \text{linear molecule} \\ 3n - 6 & \text{non-linear molecule} \end{cases}$$

The partition function of vibration is

$$q_{\text{vib}} = \prod_{i=1}^f \frac{1}{1 - \exp(-h\nu_i/k_B T)} . \quad (65)$$

For the thermodynamic functions of vibration we get

$$A_{\text{vib}} = -RT \ln q_{\text{vib}} = RT \sum_{i=1}^f \ln (1 - e^{-x_i}) , \quad (66)$$

$$S_{\text{vib}} = R \sum_{i=1}^f \frac{x_i e^{-x_i}}{1 - e^{-x_i}} - R \sum_{i=1}^f \ln (1 - e^{-x_i}) , \quad (67)$$

$$p_{\text{vib}} = 0 , \quad (68)$$

$$U_{\text{vib}} = RT \sum_{i=1}^f \frac{x_i e^{-x_i}}{1 - e^{-x_i}} , \quad (69)$$

$$H_{\text{vib}} = U_{\text{vib}} , \quad (70)$$

$$G_{\text{vib}} = A_{\text{vib}} , \quad (71)$$

$$C_{V,\text{vib}} = R \sum_{i=1}^f \frac{x_i^2 e^{-x_i}}{(1 - e^{-x_i})^2} , \quad (72)$$

$$C_{p,\text{vib}} = C_{V,\text{vib}} , \quad (73)$$

where $x_i = \frac{h\nu_i}{k_B T}$.

4.4 Electronic contributions

The electronic partition function reads

$$q_{\text{el}} = \sum_{\ell=0}^{\infty} g_{\text{el},\ell} e^{-\varepsilon_{\text{el},\ell}/k_B T}, \quad (74)$$

where $\varepsilon_{\text{el},\ell}$ the energy level ℓ , and $g_{\text{el},\ell}$ is its degeneracy. In most cases the electronic contributions to the thermodynamic functions are negligible at not very high temperatures. Therefore they are not written here.

4.5 Ideal gas mixture

Let us consider two-component mixture of N_1 non-interacting molecules of component 1 and N_2 non-interacting molecules of component 2 (extension to the case of a multi-component mixture is straightforward). The partition function of mixture is

$$Q = \frac{q_1^{N_1} q_2^{N_2}}{N_1! N_2!} \quad (75)$$

where q_1 and q_2 are the partition functions of molecules 1 and 2, respectively. Let us denote $X_{m,i}$ the molar thermodynamic quantity of pure component i , $i = 1, 2$ and $x_i = \frac{N_i}{N_1+N_2}$ its mole fraction. Then

$$A = RT(x_1 \ln x_1 + x_2 \ln x_2) + x_1 A_{m,1} + x_2 A_{m,2} \quad (76)$$

$$S = -R(x_1 \ln x_1 + x_2 \ln x_2) + x_1 S_{m,1} + x_2 S_{m,2}, \quad (77)$$

$$G = RT(x_1 \ln x_1 + x_2 \ln x_2) + x_1 G_{m,1} + x_2 G_{m,2}, \quad (78)$$

$$p = x_1 p_{m,1} + x_2 p_{m,2} = x_1 \frac{RT}{V_m} + x_2 \frac{RT}{V_m}, \quad (79)$$

$$U = x_1 U_{m,1} + x_2 U_{m,2}, \quad (80)$$

$$H = x_1 H_{m,1} + x_2 H_{m,2}, \quad (81)$$

$$C_V = x_1 C_{V,m,1} + x_2 C_{V,m,2}, \quad (82)$$

$$C_p = x_1 C_{p,m,1} + x_2 C_{p,m,2}. \quad (83)$$

5. Ideal crystal

We will call the ideal crystal an assembly of molecules displayed in a regular lattice without any impurities or lattice deformations. Distances among lattice centers will not depend on temperature and pressure. For simplicity we will consider one-atomic molecules. The partition function of crystal is

$$Q = e^{-U_0/k_B T} Q_{\text{vib}}, \quad (84)$$

where U_0 is the lattice energy.

We will discuss here two models of the ideal crystal: the Einstein approximation and the Debye approximation.

5.1 Einstein model

An older and simpler Einstein model is based on the following postulates

1. Vibrations of molecules are independent:

$$Q_{\text{vib}} = q_{\text{vib}}^N, \quad (85)$$

where q_{vib} is the vibrational partition function of molecule.

2. Vibrations are isotropic:

$$q_{\text{vib}} = q_x q_y q_z = q_x^3. \quad (86)$$

3. Vibrations are harmonical

$$q_x = \sum_{v=0}^{\infty} e^{-\epsilon_v/k_B T}, \quad (87)$$

where

$$\epsilon_v = h\nu \left(v + \frac{1}{2} \right)$$

is the energy in quantum state v and ν is the fundamental vibrational frequency.

Combining these equations one obtains

$$Q = e^{-U_0/k_B T} \left(\frac{e^{-\Theta_E/(2T)}}{1 - e^{-\Theta_E/T}} \right)^{3N}, \quad (88)$$

where

$$\Theta_E = \frac{h\nu}{k_B}$$

is the *Einstein characteristic temperature*.

For the isochoric heat capacity it follows

$$C_V = 3Nk_B \left(\frac{\Theta_E}{T} \right)^2 \frac{e^{-\Theta_E/T}}{(1 - e^{-\Theta_E/T})^2}. \quad (89)$$

5.2 Debye model

Debye considers crystal as a huge molecule (*i.e.* he replaces the postulates of independence and isotropy in the Einstein model) of an ideal gas; the postulate of harmonicity of vibrations remains. From these assumptions it can be derived for the partition function

$$\ln Q = -\frac{U_0}{k_B T} - \frac{9}{8} N \frac{\Theta_D}{T} - 9N \left(\frac{T}{\Theta_D} \right)^3 \int_0^{\Theta_D/T} x^2 \ln(1 - e^{-x}) dx, \quad (90)$$

where

$$\Theta_D = \frac{h\nu_{\text{max}}}{k_B}$$

is the *Debye characteristic temperature* with ν_{max} being the highest frequency of crystal.

For the isochoric heat capacity it follows

$$C_V = 3R \left(4D(u) - \frac{3u}{e^u - 1} \right). \quad (91)$$

where $u = \Theta_D/T$ and

$$D(u) = \frac{3}{u^3} \int_0^u \frac{x^3}{e^x - 1} dx.$$

It can be proved that at low temperatures the heat capacity becomes a cubic function of temperature

$$C_V = 36R \left(\frac{T}{\Theta_D} \right)^3 \int_0^\infty \frac{x^3}{e^x - 1} dx = a T^3,$$

while the Einstein model incorrectly gives

$$C_V = 3R \left(\frac{\Theta_E}{T} \right)^2 e^{-\Theta_E/T}.$$

Both models give a correct high-temperature limit (the Dulong-Petit law)

$$C_V = 3R.$$

The same is true for the zero temperature limit

$$\lim_{T \rightarrow 0} C_V = 0.$$

5.3 Beyond the Debye model

Both the Einstein and the Debye models assume harmonicity of lattice vibrations. This is not true at high temperatures near the melting point. The harmonic vibrations are not assumed in the lattice theories (the cell theory, the hole theory, ...) that used to be popular in forties and fifties of the last century for liquids. It was shown later that they are poor theories of liquids but very good theories for solids.

Thermodynamic functions cannot be obtained analytically in the lattice theories.

6. Intermolecular forces

Up to now forces acting among molecules have been ignored. In the ideal gas (Section 4) molecules are assumed to exert no forces upon each other. In the ideal crystal (Section 5) molecules are imprisoned in the lattice, and the intermolecular forces are counted indirectly in the lattice energy and in the Einstein or Debye temperature. For real gases and liquids the intermolecular force must be included explicitly.

6.1 The configurational integral and the molecular interaction energy

The partition function of the real gas or liquid may be written in a form

$$Q = \frac{1}{N!} \exp(-N\beta\epsilon_0) q_{\text{int}}^N \left(\frac{2\pi m k_B T}{h^2} \right)^{\frac{3}{2}N} Z. \quad (92)$$

where $q_{\text{int}} = q_{\text{rot}} q_{\text{vib}} q_{\text{el}}$ is the partition function of the internal motions in molecule. Quantity Z is the configurational integral

$$Z = \int_{(V)} \int_{(V)} \cdots \int_{(V)} \exp[-\beta u_N(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N)] d\vec{r}_1 d\vec{r}_2 \dots d\vec{r}_N, \quad (93)$$

where symbol

$$\int_{(V)} \cdots d\vec{r}_i = \int_0^L \int_0^L \int_0^L \cdots dx_i dy_i dz_i \quad \text{and} \quad L^3 = V.$$

The quantity $u_N(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N)$ is the potential energy of an assembly of N molecules. Here and in Eq.(93) one-atomic molecules are assumed for simplicity. More generally, the potential energy is a function not only positions of centers of molecules \vec{r}_i but also of their orientations $\vec{\omega}_i$. However, we will use the above simplified notation.

The interaction potential energy u_N of system may be written as an expansion in two-body, three-body, *e.t.c* contributions

$$u_N(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N) = \sum_{i<j} u_2(\vec{r}_i, \vec{r}_j) + \sum_{i<j<k} u_3(\vec{r}_i, \vec{r}_j, \vec{r}_k) + \cdots \quad (94)$$

Most often only the first term is considered. This approximation is called *the rule of pairwise additivity*

$$u_N = \sum_{i<j} u_2(\vec{r}_i, \vec{r}_j), \quad (95)$$

where u_2 is the pair intermolecular potential. The three-body potential u_3 is used rarely at very accurate calculations, and u_4 and higher order contributions are omitted as a rule.

6.2 The pair intermolecular potential

The pair potential depends of a distance between centers of two molecules r and on their mutual orientation $\vec{\omega}$. For simplicity we will omit the angular dependence of the pair potential (it is true for the spherically symmetric molecules) in further text, and write

$$u_2(\vec{r}_i, \vec{r}_j) = u_2(r_{ij}, \vec{\omega}_{ij}) = u(r)$$

where subscripts 2 and ij are omitted, too.

The following model pair potentials are most often used.

6.2.1 Hard spheres

It is after the ideal gas the simplest model. It ignores attractive interaction between molecules, and approximates strong repulsive interactions at low intermolecular distances by an infinite barrier

$$u(r) = \begin{cases} \infty & r < \sigma \\ 0 & r > \sigma \end{cases} \quad (96)$$

where σ is a diameter of molecule.

6.2.2 Square well potential

Molecules behave like hard spheres surrounded by an area of attraction

$$u(r) = \begin{cases} \infty & r < \sigma \\ -\epsilon & \sigma < r < \lambda\sigma \\ 0 & r > \lambda\sigma \end{cases} \quad (97)$$

Here σ is a hard-sphere diameter, ϵ a depth of the attractive well, and the attraction region ranges from σ to $\lambda\sigma$.

6.2.3 Lennard-Jones potential

This well known pair intermolecular potential realistically describes a dependence of pair potential energy on distance

$$u(r) = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right]. \quad (98)$$

ϵ is a depth of potential at minimum, and $2^{1/6}\sigma$ is its position. More generally, the Lennard-Jones n-m potential is

$$u(r) = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^n - \left(\frac{\sigma}{r} \right)^m \right]. \quad (99)$$

6.2.4 Pair potentials of non-spherical molecules

There are analogues of hard spheres for non-spherical particles: hard diatomics or dumbbells made of two fused hard spheres, hard triatomics, hard multiatomics, hard spherocylinders, hard ellipsoids, and so on.

Examples of soft pair potentials are Lennard-Jones multiatomics, molecules whose atoms interact according to the Lennard-Jones potential (98).

Another example is the Stockmayer potential, the Lennard-Jones potential with an indebted dipole moment

$$u(r, \theta_1, \theta_2, \phi) = 4\epsilon \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right] - \frac{\mu^2}{r^3} [2 \cos \theta_1 \cos \theta_2 - \sin \theta_1 \sin \theta_2 \cos \phi], \quad (100)$$

where μ is the dipole moment.

6.2.5 Pair potentials of real molecules

The above model pair potentials, especially the Lennard-Jones potential and its extensions, may be used to calculate properties of the real substances. In this case their parameters, for example ϵ and σ , are fitted to the experimental data such as the second virial coefficients, rare-gas transport properties and molecular properties.

More sophisticated approach involving a realistic dependence on the interparticle separation with a number of adjustable parameters was used by Aziz, see Aziz (1984) and references therein.

For simple molecules, there is a fully theoretical approach without any adjustable parameters utilizing the first principle quantum mechanics calculations, see for example Slaviček et al. (2003) and references therein.

6.3 The three-body potential

The three-body intermolecular interactions are caused by polarizabilities of molecules. The simplest and the most often used is the Axilrod-Teller-Muto term

$$u(r, s, t) = \frac{v}{rst} (3 \cos \theta_1 \cos \theta_2 \cos \theta_3 + 1), \quad (101)$$

where v is a strength parameter. It is a first term (DDD, dipole-dipole-dipole) in the multipole expansion. Analytical formulae and corresponding strength parameters are known for higher order terms (DDQ, dipole-dipole-quadrupole, DQQ, dipole-quadrupole-quadrupole, ...) as well.

More accurate three-body potentials can be obtained using quantum chemical *ab initio* calculations Malijevský et al. (2007).

7. The virial equation of state

The virial equation of state in the statistical thermodynamics is an expansion of the compressibility factor $z = \frac{pV}{RT}$ in powers of density $\rho = \frac{N}{V}$

$$z = 1 + B_2\rho + B_3\rho^2 + \dots, \quad (102)$$

where B_2 is the second virial coefficient, B_3 the third, *e.t.c.* The virial coefficients of pure gases are functions of temperature only. For mixtures they are functions of temperature and composition.

The first term in equation (102) gives the equation of state of ideal gas, the first two terms or three give corrections to non-ideality. Higher virial coefficients are not available experimentally. However, they can be determined from knowledge of intermolecular forces. The relations among the intermolecular forces and the virial coefficients are exact, the pair and the three-body of potentials are subjects of uncertainties, however.

7.1 Second virial coefficient

For the second virial coefficient of spherically symmetric molecules we find

$$B = -2\pi \int_0^\infty f(r) r^2 dr = -2\pi \int_0^\infty (e^{-\beta u(r)} - 1) r^2 dr, \quad (103)$$

where

$$f(r) = \exp[-\beta u(r)] - 1$$

is the *Mayer function*. For linear molecules we have

$$B = -\frac{1}{4} \int_0^\infty \int_0^\pi \int_0^\pi \int_0^{2\pi} [e^{-\beta u(r, \theta_1, \theta_2, \phi)} - 1] r^2 \sin \theta_1 \sin \theta_2 dr d\theta_1 d\theta_2 d\phi. \quad (104)$$

For general non-spherical molecules we obtain

$$B = -\frac{2\pi}{\int_{\vec{\omega}_1} \int_{\vec{\omega}_2} d\vec{\omega}_1 d\vec{\omega}_2} \int_0^\infty \int_{\omega_1} \int_{\omega_2} [e^{-\beta u(r, \vec{\omega}_1, \vec{\omega}_2)} - 1] r^2 dr d\vec{\omega}_1 d\vec{\omega}_2. \quad (105)$$

7.2 Third virial coefficient

The third virial coefficient may be written for spherically symmetric molecules as

$$C = C_{\text{add}} + C_{\text{nadd}}, \quad (106)$$

where

$$C_{\text{add}} = -\frac{8}{3}\pi^2 \int_0^\infty \int_0^r \int_{|r-s|}^{r+s} (e^{-\beta u(r)} - 1) (e^{-\beta u(s)} - 1) (e^{-\beta u(t)} - 1) r s t dr ds dt, \quad (107)$$

and

$$C_{\text{nadd}} = \frac{8}{3}\pi^2 \int_0^\infty \int_0^r \int_{|r-s|}^{r+s} e^{-\beta u(r)} e^{-\beta u(s)} e^{-\beta u(t)} \{\exp[-\beta u_3(r, s, t)] - 1\} r s t dr ds dt, \quad (108)$$

where $u_3(r, s, t)$ is the three-body potential. Analogous equations hold for non-spherical molecules.

7.3 Higher virial coefficients

Expressions for higher virial coefficients become more and more complicated due to an increasing dimensionality of the corresponding integrals and their number. For example, the ninth virial coefficient consists of 194 066 integrals with the Mayer integrands, and their dimensionalities are up to 21 Malijevský & Kolafa (2008) in a simplest case of spherically symmetric molecules. For hard spheres the virial coefficients are known up to ten, which is at the edge of a present computer technology Labík et al. (2005).

7.4 Virial coefficients of mixtures

For binary mixture of components 1 and 2 the second virial coefficient reads

$$B_2 = x_1^2 B_2(11) + 2x_1 x_2 B_2(12) + x_2^2 B_2(22), \quad (109)$$

where x_i are the mole fractions, $B_2(ii)$ the second virial coefficients of pure components and $B_2(12)$ the crossed virial coefficient representing an influence of the interaction between molecule 1 and molecule 2.

The third virial coefficient reads

$$B_3 = x_1^3 B_3(111) + 3x_1^2 x_2 B_3(112) + 3x_1 x_2^2 B_3(122) + x_2^3 B_3(222). \quad (110)$$

Extensions of these equations on multicomponent mixtures and higher virial coefficients is straightforward.

8. Dense gas and liquid

Determination of thermodynamic properties from intermolecular interactions is much more difficult for dense fluids (for gases at high densities and for liquids) than for rare gases and solids. This fact can be explained using a definition of the Helmholtz free energy

$$A = U - TS. \quad (111)$$

Free energy has a minimum in equilibrium at constant temperature and volume. At high temperatures and low densities the term TS dominates because not only temperature but also entropy is high. A minimum in A corresponds to a maximum in S and system, thus, is in the gas phase. Ideal gas properties may be calculated from a behavior of individual molecules only. At somewhat higher densities thermodynamic quantities can be expanded from their ideal-gas values using the virial expansion.

At low temperatures the energy term in equation (111) dominates because not only temperature but also entropy is small. For solids we may start from a concept of the ideal crystal.

No such simple molecular model as the ideal gas or the ideal crystal is known for liquid and dense gas. Theoretical studies of liquid properties are difficult and uncompleted up to now.

8.1 Internal structure of fluid

There is no internal structure of molecules in the ideal gas. There is a long-range order in the crystal. The fluid is between of the two extremal cases: it has a local order at short intermolecular distances (as crystal) and a long-range disorder (as gas).

The fundamental quantity describing the internal structure of fluid is the pair distribution function $g(r)$

$$g(r) = \frac{\rho(r)}{\rho}, \quad (112)$$

where $\rho(r)$ is local density at distance r from the center of a given molecule, and ρ is the average or macroscopic density of system. Here and in the next pages of this section we assume spherically symmetric interactions and the rule of the pair additivity of the intermolecular potential energy.

The pair distribution function may be written in terms of the intermolecular interaction energy u_N

$$g(r) = V^2 \frac{\int_{(V)} \cdots \int_{(V)} e^{-\beta u_N(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N)} d\vec{r}_3 \dots d\vec{r}_N}{\int_{(V)} \cdots \int_{(V)} e^{-\beta u_N(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N)} d\vec{r}_1 \dots d\vec{r}_N}. \quad (113)$$

It is related to the thermodynamic quantities using the pressure equation

$$z \equiv \frac{pV}{RT} = 1 - \frac{2}{3} \pi \rho \beta \int_0^\infty \frac{du(r)}{dr} g(r) r^3 dr, \quad (114)$$

the energy equation

$$\frac{U}{RT} = \frac{U^0}{RT} + 2\pi\rho\beta \int_0^\infty u(r)g(r)r^2 dr, \quad (115)$$

where U^0 internal energy if the ideal gas, and the compressibility equation

$$\beta \left(\frac{\partial p}{\partial \rho} \right)_\beta = \left\{ 1 + 4\pi\rho \int_0^\infty [g(r) - 1] r^2 dr \right\}^{-1}. \quad (116)$$

Present mainstream theories of liquids can be divided into two large groups: perturbation theories and integral equation theories Hansen & McDonald (2006), Martynov (1992).

8.2 Perturbation theories

A starting point of the perturbation theories is a separation of the intermolecular potential into two parts: a harsh, short-range repulsion and a smoothly varying long-range attraction

$$u(r) = u^0(r) + u^p(r). \quad (117)$$

The term $u^0(r)$ is called *the reference potential* and the term $u^p(r)$ *the perturbation potential*. In the simplest case of the first order expansion of the Helmholtz free energy in the perturbation potential it holds

$$\frac{A}{RT} = \frac{A^0}{RT} + 2\pi\rho\beta \int_0^\infty u^p(r)g^0(r)r^2 dr, \quad (118)$$

where A^0 is the Helmholtz free energy of a reference system.

In the perturbation theories knowledge of the pair distribution function and the Helmholtz free energy of the reference system is supposed. On one hand the reference system should be simple (the ideal gas is too simple and brings nothing new; a typical reference system is a fluid of hard spheres), and the perturbation potential should be small on the other hand. As a result of a battle between a simplicity of the reference potential (one must know its structural and thermodynamic properties) and an accuracy of a truncated expansion, a number of methods have been developed.

8.3 Integral equation theories

Among the integral equation theories the most popular are those based on the Ornstein-Zernike equation

$$h(r_{12}) = c(r_{12}) + \rho \int_{(V)} h(r_{13})c(r_{32}) d\vec{r}_3. \quad (119)$$

where $h(r) = g(r) - 1$ is the total correlation function and $c(r)$ the direct correlation function. This equation must be closed using a relation between the total and the direct correlation functions called *the closure* to the Ornstein-Zernike equation. From the diagrammatic analysis it follows

$$h(r) = \exp[-\beta u(r) + \gamma(r) + B(r)] - 1, \quad (120)$$

where

$$\gamma(r) = h(r) - c(r)$$

is the indirect (chain) correlation function and $B(r)$ is the bridge function, a sum of elementary diagrams. Equation (120) does not yet provide a closure. It must be completed by an approximation for the bridge function. The mostly used closures are in listed in Malijevský & Kolafa (2008). The simplest of them are the hypernetted chain approximation

$$B(r) = 0 \quad (121)$$

and the Percus-Yevick approximation

$$B(r) = \gamma(r) - \ln[\gamma(r) + 1]. \quad (122)$$

Let us compare the perturbation and the integral equation theories. The first ones are simpler but they need an extra input - the structural and thermodynamic properties of a reference system. The accuracy of the second ones depends on a chosen closure. Their examples shown here, the hypernetted chain and the Percus-Yevick, are too simple to be accurate.

8.4 Computer simulations

Besides the above theoretical approaches there is another route to the thermodynamic quantities called the computer experiments or pseudoexperiments or simply simulations. For a given pair intermolecular potential they provide values of thermodynamic functions in the dependence on the state variables. In this sense they have characteristics of real experiments. Similarly to them they do not give an explanation of the bulk behavior of matter but they serve as tests of approximative theories. The thermodynamic values are free of approximations, or more precisely, their approximations such as a finite number of molecules in the basic box or a finite number of generated configurations can be systematically improved Kolafa et al. (2002). The computer simulations are divided into two groups: the Monte Carlo simulations and the molecular dynamic simulations. The Monte Carlo simulations generate the ensemble averages of structural and thermodynamic functions while the molecular dynamics simulations generate their time averages. The methods are described in detail in the monograph of Allen and Tildesley Allen & Tildesley (1987).

9. Interpretation of thermodynamic laws

In Section 2 the axioms of the classical or phenomenological thermodynamics have been listed. The statistical thermodynamics not only determines the thermodynamic quantities from knowledge of the intermolecular forces but also allows an interpretation of the phenomenological axioms.

9.1 Axiom on existence of the thermodynamic equilibrium

This axiom can be explained as follows. There is a very, very large number of microscopic states that correspond to a given macroscopic state. At unchained macroscopic parameters such as volume and temperature of a closed system there is much more equilibrium states than the states out of equilibrium. Consequently, a spontaneous transfer from non-equilibrium to equilibrium has a very, very high probability. However, a spontaneous transfer from an equilibrium state to a non-equilibrium state is not excluded.

Imagine a glass of whisky on rocks. This two-phase system at a room temperature transfers spontaneously to the one-phase system - a solution of water, ethanol and other components. It is not excluded but it is highly improbable that a glass with a dissolved ice will return to the initial state.

9.2 Axiom of additivity

This axiom postulates that the internal energy of the macroscopic system is a sum of its two macroscopic parts

$$U = U_1 + U_2. \quad (123)$$

However, if we consider a macroscopic system as an assembly of molecules, equation (123) does not take into account intermolecular interactions among molecules of subsystem 1 and molecules of subsystem 2. Correctly the equation should be

$$U = U_1 + U_2 + U_{12}. \quad (124)$$

Due to the fact that intermolecular interactions vanish at distances of the order of a few molecule diameters, the term U_{12} is negligible in comparison with U .

9.3 The zeroth law of thermodynamics and the negative absolute temperatures

The statistical thermodynamics introduces temperature formally as parameter $\beta = \frac{1}{k_B T}$ in the expression (11) for the partition function

$$Q = \sum_i \exp(-\beta E_i).$$

As energies of molecular systems are positive and unbounded, temperature must be positive otherwise the equation diverges. For systems with bounded energies

$$E_{\min} \leq E_i \leq E_{\max}$$

both negative and positive temperatures are allowed. Such systems are in lasers, for example.

9.4 The second law of thermodynamics

From equation (3) it follows that entropy of the adiabatically isolated system either grows for spontaneous processes or remains constant in equilibrium

$$dS \geq 0. \quad (125)$$

Entropy in the statistical thermodynamics is connected with probability via equation (20)

$$S = -k_B \sum_i P_i \ln P_i.$$

Thus, entropy may spontaneously decrease but with a low probability.

9.5 Statistical thermodynamics and the arrow of time

Direction of time from past to future is supported by three arguments

- **Cosmological time**
The cosmological time goes according the standard model of Universe from the Big Bang to future.
- **Psychological time**
We as human beings remember (as a rule) what was yesterday but we do not "remember" what will be tomorrow.
- **Thermodynamic time**
Time goes in the direction of the growth of entropy in the direction given by equation (125). The statistical thermodynamics allows due to its probabilistic nature a change of a direction of time "from coffin to the cradle" but again with a very, very low probability.

9.6 The third law of thermodynamics

Within the statistical thermodynamics the third law may be easily derived from equation (20) relating entropy and the probabilities. The state of the ideal crystal at $T = 0$ K is one. Its probability $P_0 = 1$. By substituting to the equation we get $S = 0$.

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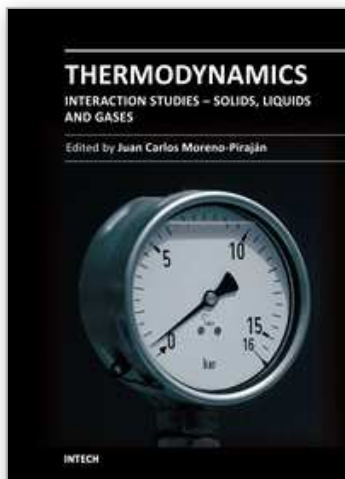
List of symbols

A	Helmholtz free energy
B	second virial coefficient
B_i	i-th virial coefficient
$B(r)$	bridge function
C_V	isochoric heat capacity
C_p	isobaric capacity
$c(r)$	direct correlation function
E	energy
ϵ	energy of molecule
G	Gibbs free energy
$g(r)$	pair distribution function
H	enthalpy
h	Planck constant
$h(r)$	total correlation function
k_B	Boltzmann constant
N	number of molecules, Avogadro number
P	probability
p	pressure
Q	heat
Q	partition function
q	partition function of molecule
R	(universal) gas constant (8.314 in SI units)
S	entropy
T	temperature

τ	time
U	internal energy
u_N	potential energy of N particles
u	pair potential
W	work
W	number of accessible states
X	measurable thermodynamic quantity
x	mole fraction

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