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Rate-Distortion Analysis for H.264/AVC Video Statistics

Luis Teixeira
Research Center for Science and Technology in Art (CITAR),
School of Arts, Portuguese Catholics University,
INESC PORTO – Instituto Nacional de Engenharia de Sistemas e Computadores
Portugal

1. Introduction

MPEG standards family specify the decoding process and the bit-stream syntaxes allowing research towards the optimizations of the encoding process regarding coding performance improvement and complexity reduction. The purpose of a video encoder for broadcast or storage is to generate the optimal perceptual video quality, or the minimized distortion, under a certain constraint such as storage space or channel bandwidth. In particular, by minimizing the distortion D, the video encoder should optimally compute a set of optimal quantisers to control the output bit-rate for each coding unit to satisfy the allocated bit budget.

There are two main approaches to solve the optimal bit allocation problem: Lagrange optimization (Everett, 1963; Ramchandran et al., 1994) and dynamic programming (DP) (Bellman, 2003). The optimal bit allocation was first addressed in (Huang & Schultheiss, 1963) where the Lagrange multiplier approach for R-D analysis in transform coding was used. Further improvements have been reported in (Shoham & Gersho, 1988) for source quantization and coding. However, the Lagrange multiplier method suffer from problems, such as having negative bits and real numbers (Schuster & Katsaggelos, 1997a) and the computational complexity is very high due to the need to determine R-D characteristics of current and future video frames. DP is employed to achieve the minimum overall distortion through a tree or trellis with known quantisers and their R-D characteristics (Forney, 1973; Ortega, 1996; Ramchandran et al., 1994).

The total of the required bits and coding distortion depend on the quantization step-size. The rate or distortion versus quantization parameter (Q) curve can be produce by encoding for all the possible quantisers to obtain the bit-rate and the quantization error. In order to know how to select a quantization parameter under a specific constraint, e.g., the target bit-budget or distortion, it is importance to model or estimate the coding bit rate in terms of the quantization parameter, namely rate-quantization (R-Q) functions. Together with distortion-quantization (D-Q) functions, R-Q functions characterize the rate-distortion (R-D) behaviour of video encoding, which is the key to obtain an optimum bit allocation. Many R-Q and D-Q functions have been reported in previous studies (Chiang & Zhang, 1997; Ding & Liu, 1996; Hang & J.J. Chen, 1997; ISO/IEC, 1993; ISO/IEC, 1997; ITU-T, 1997; Lin & Ortega, 1998;

Ortega, 1996; Ribas-Corbera & Lei, 1999; Sullivan & Wiegand, 1998; Yin & Boyce, 2004). Some of these schemes were adopted in standard-compliant video coders, such as TM-5 (ISO/IEC, 1993), the test model for MPEG-2, TMN-8 (ITU-T, 1997), the test model for H.263, and VM-8 (ISO/IEC, 1997), the verification model for MPEG-4.

Usually rate control algorithms accept as an assumption that video source statistics are stationary. In this case, video source statistics correspond to some form of probability model such as Gaussian (Hang & J.J. Chen, 1997) or Laplacian (Chiang & Zhang, 1997) and R-D models based on the R-D theory, the theoretical foundation of rate control, can be obtained (Berger, 1971; Chiang & Zhang, 1997; Ribas-Corbera & Lei, 1999).

A video coding algorithm focus on the trade-off between the distortion and bit rate, where usually to a decreasing distortion corresponds an increasing rate and vice-versa. In R-D theory, the R-D function allows to estimate the lower bound for the rate at a given distortion. However, this value may not be possible to obtain in practical video encoders implementations. Operational R-D (ORD) theory applies to lossy data compression with finite number of possible R-D pairs (Schuster & Katsaggelos, 1997a).
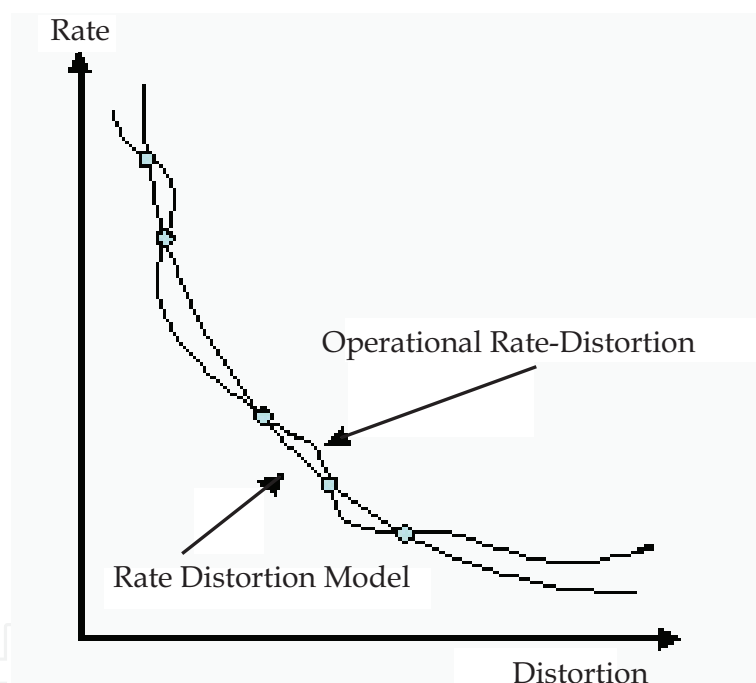

Fig. 1. Operational rate-distortion and rate-distortion model curves.

The ORD function presents the convex curve of the specific compression scheme such that the optimal solution of rate control, i.e., optimal quantiser achieving minimum distortion at given bit rate, can be obtained (Schuster& Katsaggelos, 1997a) (Figure 1). Efficiency problems in many practical video coding applications may occur due to high computational complexity in this approach (Z. Chen & Ngan, 2007). Therefore, in numerous systems, model-based rate control schemes have been adopted (Chiang & Zhang, 1997; Ding& Liu, 1996; Vetro et al., 1999; Z. Chen & Ngan, 2005a; Zhang et al., 2005). R-D models can be obtained based on the statistical properties of video signal and R-D theory (Chiang & Zhang, 1997; Hang & J.J. Chen, 1997; Ribas-Corbera & Lei, 1999), or on empirical observation and benefiting from various regression techniques (Ding& Liu, 1996; Kim, 2003; Lin & Ortega, 1998; Z. Chen & Ngan, 2004; Z. Chen & Ngan, 2005b).

Some rate control schemes incorporate spatio-temporal correlations to improve the accuracy of R-D models, by using statistical regress analysis for dynamical model parameters update. Representative of this approach is the MPEG-4 Q2 (Chiang & Zhang, 1997), and the linear MAD models (Lee et al., 2000), where model parameters are updated by linear regression method from previous coded parameters. H.264/AVC JM rate-control algorithm also uses a quadratic rate model. In addition, the H.264/AVC rate-control solves "chicken-and-egg" dilemma as the Lagrange multiplier is modelled as a function of quantization parameter (Wiegand & Girod, 2001). Rate-quantization relationship can be used to compute the quantization parameter. Nevertheless, the model-based rate functions frequently depend on the complexity of the coding unit that is obtained after the rate-constrained motion estimation and mode decision with the Lagrange multiplier. The JM algorithm of H.264/AVC proposes a linear prediction model to solve this problem by estimating the mean of absolute difference (MAD) from the previously coded units. Then the quadratic model can estimate the quantization parameter. However, rate-distortion re-analysis can be further investigated based on the coding characteristics of the H.264/AVC for improving the coding performance (Kamaci et al., 2005; Ma et al., 2005) particularly in the case of joint video coding and the use of different distortion metrics.

We may find in the literature extensive studies regarding optimizing a video encoder encoder with R-D considerations include mode decision (Chan & Siu, 2001; Chung & Chang, 2003), motion estimation (Pur et al., 1987; Rhee et al., 2001; Wiegand et al., 2003b), optimal bit allocation and rate control in video coding field (H.-Y.C. Tourapis & A.M. Tourapis, 2003; He & Mitra, 2002; J.J. Chen & Lin 1996; Ortega, 1996; Ramchandran et al., 1994; Ribas-Corbera & Neuhoff, 1998; Schuster& Katsaggelos, 1997b; Sullivan & Wiegand, 1997; Wiegand et al., 2003a, 2003c; Zhang et al., 2003).

In summary, to optimize a video encoder, the rate-distortion optimization techniques play a very important role. R-D models are functions that predict the expected distortion at a given bit rate. This is very important for joint video coding applications that attempt to optimized quality, e.g. minimize distortion, in environments where the channel conditions vary dynamically or the number of broadcast programs varies through time. Thus in this section we propose to present and evaluate several R-D models.

At the same time, we propose also to study the bit rate variability as a function of the video quality (Seeling et al., 2004, 2007). This type of analyse is typical of a communication network perspective. By re-analyzing the characteristics of the bit-rate and the data in the transform domain, a simple rate estimation function can be obtained that will allow support the allocating of video bandwidth within different video programmes.

2. Rate control in international standards

Although the MPEG video coding standard recommended a general coding methodology and syntax for the creation of a legitimate MPEG bitstream, there are many areas of research left open regarding how to generate high-quality MPEG bitstreams. This allows the designers of MPEG encoder great flexibility in developing and implementing their own MPEG specific algorithms. To optimise the performance-of an MPEG encoder system, it is important to study research areas such as motion estimation, coding mode decisions, and rate control.

The main goal of rate control is to manage the process of bit allocation within a video sequence and thus the quality of the encoded bitstream. Regarding rate control, encoders

can operate at Constant Bit Rate (CBR) or in Variable Bit Rate (VBR). In CBR, the video encoder maintains the average bit rate constant. The encoder output has a buffer and its occupancy is controlled dynamically by adjusting the quantization scale, denote as q in MPEG coders. Likewise, the quality of the video sequence varies due to the variations in the scene complexity. VBR reduces the variation in the picture quality by allocating more bits to complex images. A common use of VBR is Open-Loop Variable Bit Rate (OL-VBR), where the quantization scale is constant for all the images of the video sequence. Another VBR scheme is Constant Quality - Variable Bit Rate (CQ-VBR) which aims to maintain an objective video quality constant.

The rate control algorithms usually adjust the coded bit stream according different constraints, such as buffer over- or underflow prevention, variable and/or low bandwidth constraints resulting from limited storage size or communication bandwidth (Ortega, 1996). In order to accomplish this goal rate control schemes are responsible to adjust the quantization parameters.
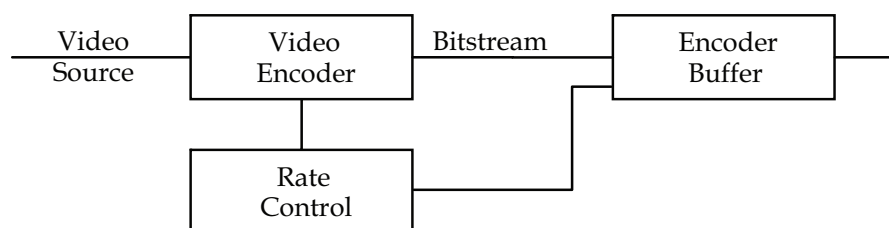

Fig. 2. Rate control in video coding system.

A generic bit rate control is composed the following steps: given an input video signal and a desired bit rate, constant or variable, what should be the encoder settings to maintain the picture quality as high and constant as possible. In MPEG encoding, a quantization scale controls the trade-off between picture quality and the bit rate. This parameter is used to compute the step size of the uniform quantisers used for the different AC DCT coefficients (ISO/IEC, 1993). For each macroblock, a quantiser, q, is selected. It is named "adaptive quantization" to the process for adjusting the value of q between macroblocks within an image frame. There are several schemes for doing the adaptive quantization. For example, in MPEG-2 Test Model 5 (TM5) (ISO/IEC, 1993), a non-linear mapping based on the block variance is used to adapt the q's. Besides the quantization scale, the quantization coarseness is also dependent of the quantization matrix. In MPEG-1, the quantization matrix can be altered in each sequence while in MPEG-2 on a picture basis. It sets the relative coarseness of quantization for each coefficient.

As MPEG does not specify how to control the bit rate, different approaches can be found in the literature (ISO/IEC, 1993; Keesman et al., 1995; Ramchandran et al., 1993). Two approaches have been used: 'feed forward bit rate control' and 'feed backward bit rate control'. In the first approach, after performing a pre-analysis, the optimum settings are compute. This process will increase the computational complexity and time needed while yielding better results. In the second approach, there is limited knowledge of the sequence complexity. Bits are allocated on a picture basis and spatially uniform distributed throughout the image. Thus, too many bits may be spent at the beginning of the picture while the end of the picture may present a higher degree of complexity. The 'feed backward bit rate control' is suitable for real time applications and 'feed forward bit rate control' for applications where the quality is the main goal and time is not a constraint.

3. Rate control in H.264/AVC

Existing studies indicate that H.264/AVC brings major improvement in coding performance in relation to prior coding standards (Wiegand et al., 2003a). H.264/AVC presents many new features, which represent huge challenges to the operative encoder control such as how to allocate the bandwidth between the texture coding and the overhead coding.

A major contributor to the high coding efficiency of H.264/AVC compared with previous video compression standards is the rate and distortion (R-D) optimized motion estimation and mode decision (also referred to as RDO) with various intra and inter prediction modes and multiple reference frames. Nevertheless, these innovations increase the rate control process complexity due to the inter-dependency between the RDO and rate control. Only after the end of intra/inters prediction, the rate control scheme can access the exact coding characteristics. This information is necessary for the computation of the quantization parameter. Such a dilemma prevents the rate control scheme from directly accessing the coding characteristic in advance. The dilemma of selecting which parameter should be first determine is sometimes referred in the literature as to the "chicken and egg" dilemma (Li et al., 2003c, 2004; Wu et al., 2005).

To avoid this dilemma, in JVT-D030 a two-pass scheme was proposed, where in each pass a TM-5-alike method was used (Ma et al., 2002). This approach uses an extremely simplified R-D function, which fails to achieve accurate and robust rate control and due to the two-pass increase the level of complexity. Because of these drawbacks, JVT-G012 (Li et al., 2003a) was proposed and accepted as the standardized rate control scheme for H.264/AVC. In JVT-G012, a linear MAD model predicts the coding complexity, and a MPEG-4 Q2 function employed to estimate the quantization parameter (Li et al., 2003a).

First step occurs at GOP level. This step estimates the bits available for the remaining frames in the GOP. In addition, it initializes the QP of instantaneous decoding refresh (IDR) frame. In the following step, rate control algorithm operates at Picture level: an estimation of the target bits for the current basic unit is determined. A basic unit is a group of macroblocks and its size can vary from one macroblock up to the entire picture. The target bits estimation should be allocate so that a similar number of bits are allocate for every picture and the target buffer level is preserve.

The next step is, based on the number of bits used to encode the previous basic units, to estimate the necessary bits to encode the header. The target texture is obtained by subtracting the header estimation to the total target bits estimate. After that, this value is converted to a target QP value using a quadratic model that correlates the QP with the texture bits. The quadratic model needs an estimation of the MAD of the motion-compensated or intra prediction error of the current basic unit's. Consequently, the rate control model requires an additional linear MAD model that, from the previous basic unit MAD, allows the computation of the current basic unit MAD. In summary, the Picture level process consist in computing the quantization step Qstep using a quadratic model and then performing a R-D optimization (RDO) (Wiegand et al., 2003a) for each MB in the frame.

The MAD of the current stored picture, , is predicted by a linear regression method similar to that of MPEG-4 Q2 after coding each picture or each basic unit (1) using the actual MAD of the previous stored picture, $\sigma_i(j-1-L)$

$$\tilde{\sigma}_i(j) = a_1 \times \sigma_i(j-1-L) + a_2 \qquad (1)$$

where a1 and a2 are the model parameters (first-order and second-order coefficients). The initial value of a1 and a2 are set to one and zero, respectively (Lim et al., 2007). The quantization step corresponding to the target bits is computed by the equation (2)

$$T_i(j) = c_1 \times \frac{\tilde{\sigma}_i(j)}{Q_{step,i}(j)} + c_2 \times \frac{\tilde{\sigma}_i(j)}{Q^2_{step,i}(j)} - m_{h,i}(j) \qquad (2)$$

where $m_{h,i}(j)$ is the total number of header bits and motion vector bits, c_1 and c_2 are two coefficients. The corresponding quantization parameter QPi(j) is computed by using the relationship between the quantization step and the quantization parameter of AVC (Lim et al., 2007). Final step consists in updating the quadratic QP/bits linear model and the MAD model. This process repeats for each basic unit until the complete video sequence has been encoded.

In this section, it was introduce the basis of rate control architecture in JM H.264/AVC (Lim et al., 2007). More detail information is available at (Li et al., 2003b , 2003c , 2004; Lim et al., 2007; Ma et al., 2002). Other solutions can be found in the literature. For example, Zhihai He (He, 2001) has proposed a new model that achieves a good performance for H.263 and MPEG4-2 (ISO/IEC 14496-2) codecs. The parameter ρ represents the percentage of zeros among the quantized transform coefficients. He found a linear relationship between the value ρ and the real bit rate because the percentage of zeros plays an important role in determining the final bit rate

4. Test video sequences

Selecting a representative set of video sequences is a crucial step in evaluating and analysing the performance of R-D models. A homogeneous set of video sequences may generate biased comparison results, because some models may perform especially well under certain sequences. Two key features are used to characterize video sequences: spatial complexity and temporal complexity. Usually, spatial complexity is measured by averaging all neighbourhood differences in the same frame while temporal complexity is measured by averaging neighbourhood differences between adjacent frames (Adjeroh & Lee, 2004).

The set of test video sequences is composed by twelve CIF video sequences, with the duration of 10 seconds that are known as test video sequences (ITU-T, 2005).

It were included sequences with low spatial and temporal complexity (low complexity sequences) up to sequences with high spatial and temporal complexity (high complexity sequences). Sequences that have either high spatial or temporal complexity but nor both the designated them as medium-complexity sequences. It follows a brief description of the sequences.

In seven video sequences, the position of the camera is fixed: Akiyo (aki), Deadline (dea), Hall (hal), Mother and Daughter (mad), News (new), Paris (par) and Silence (sil). In the Akiyo sequence, the camera is focus on a human subject with a synthetic background (a female anchor reading the news). The movements are very limited, mainly head movements in front of a fixed camera. In Deadline, Mother and Daughter and Paris sequences, the camera is still fixed but there are more movements of the bodies and heads. These are typical videoconferencing content. In the News sequence two reporters, a male and a female anchor, reading the news in front of a fixed camera in a newsroom while in the background, two dancers execute movements. Hall sequence is an example of a video supervision, with stationary camera and two moving persons: one people entering from the left with a

briefcase and then leaving the hall. In the middle of the sequence, a second person enters the hall from the right and then grabs a monitor. In the Silence sequence, one can observe a fast moving subject executing deaf gesture language.

| (a) Akiyo | (b) Coastguard | (c) Deadlined | (d) Flower Garden |

| (e) Football | (f) Foreman | (g) Hall | (h) Mobile & Calendar |

| (i) News | (j) Paris | (k) Silence | (l) Mother & Daughter |

Fig. 3. Video test sequences

The Foreman sequence (for) contain the head of a person talking and geometric shapes. Fast camera movement and content motion with a pan to a construction site at the end characterize this sequence. The main characteristics of the Flower Garden sequence (flg) is the slow and steady camera panning over landscape over landscape; the spatial and the colour detail. Coastguard sequence (cgd) was shot as a pan from left to right movement in the first third and a pan from left to right in the rest of the sequence. The camera movement follows the movements of two boats (the first from right to left and the second movement from left to right). The Mobile and Calendar (mcl) sequence is characterized by the slow panning and zooming of the camera, complex motion; high spatial and colour detail. Fast and complex motion movements of the camera and contents and the level of detail characterize the Football sequence (fot). This is a very diverse set of video sequences

5. Experimental setup

Simulations were performed with the JM reference software, the official MPEG and ITU reference implementation, for the H.264/AVC Main profile (ITU-T, 2005). Source code was compiled with Microsoft Visual C++:

GOP Pattern	IntraPeriod	Number of B Frames	Pattern
IBBP_GOP1	10	2	IBBPBBPBBPBBPBBPBBPBBPBBPBBPBB
IBBP_GOP2	4	2	IBBPBBPBBPBB
IPPP_GOP1	4	0	IPPP
IPPP_GOP2	10	0	IPPPPPPPPP

Table 1. Evaluated GOP Patterns

Four different type of GOP patterns were used (Table 1). A typical GOP pattern (IBBP_GOP2), an "extend" B frame version of the typical GOP pattern, and two GOP patterns without Interpolated images.

Additionally, each video test sequence was encoded in two modes: Open-loop (fixed QP with values ranging from 10 up to 42) and Constant Bit Rate (Fixed Rate - 64kbps, 128kbps, 256kbps, 384kbps, 512kbps, 640kbps, 768kbps, 1024kbps, 1536kbps, 2048kbps. The goal was to obtain sufficient data to obtain R-D curves.

Typical quality metrics include Peak signal-to-noise ratio (PSNR) and the Mean Square Error (MSE), Sum of Squared Differences (SSD), Mean Absolute Difference (MAD), and Sum of Absolute Differences (SAD).

$$PSNR = 10\log_{10}\frac{255^2}{MSE} \tag{3}$$

$$MSE = \frac{1}{HW}SSD \tag{4}$$

$$SSD = \sum_{x=0}^{H-1}\sum_{y=0}^{W-1}\left(p(x,y) - \hat{p}(x,y)\right)^2 \tag{5}$$

$$MAD = \frac{1}{HW}SAD \tag{6}$$

$$SAD = \sum_{x=0}^{H-1}\sum_{y=0}^{W-1}\left|p(x,y) - \hat{p}(x,y)\right| \tag{7}$$

where H and W are the height and the width of the image frame, and p(x, y) and $\hat{p}(x,y)$ represent the "original" and the reconstructed image frame pixels at (x, y).

Complementary with the study of rate-distortion performance it is propose to include an analysis of the bit rate variability as a function of the video quality. This is an important topic when considering multimedia traffic. The bit rate variability is usually characterized by the Coefficient of Variation (CoV) of the frame sizes (in bits), whereby the CoV is defined as the standard deviation of the frame sizes normalized by their mean $\overline{X}$ (Seeling et al., 2004, 2007)

$$CoV = \frac{\sigma}{\overline{X}} \tag{8}$$

where $\overline{X}$ is mean size (in bits)

$$\bar{X} = \frac{1}{M} \sum_{m=1}^{M} X_m \tag{9}$$

and the variance σ^2 (square of the standard deviation) of the frame sizes being defined as

$$\sigma^2 = \frac{1}{(M-1)} \sum_{m=1}^{M} \left(X_m - \bar{X} \right)^2 \tag{10}$$

6. Experimental results and discussion

This section presents experimental results: Rate-Distortion analysis and bit rate variability analysis as a function of the video quality.

6.1 R-D models

The RD graphs obtained for the video sequences Akiyo, Foreman and Football, in open loop, are show in Figure 4 (bit-rate axe is in logarithm scale). One can observe that a proportional relation exists between Bit-rate and Picture Quality and that quality depend on the video nature: for the same bit-rate, low complexity sequences present higher values of quality and vice-versa. This behaviour occurs in all the different GOP patterns. Figure 5
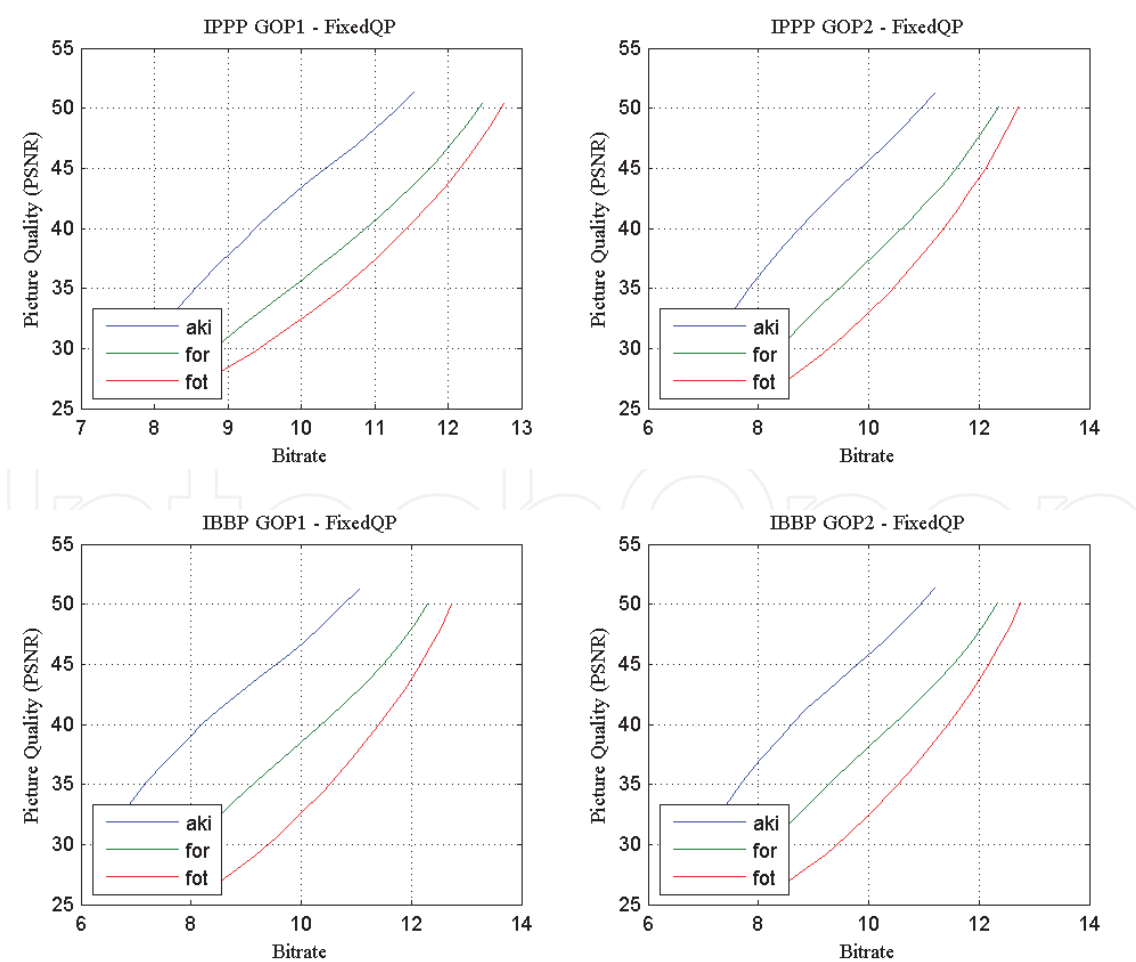

Fig. 4. Rate-distortion curve (Akiyo, Foreman, Football; FixeQP)

present graphic representation for RD data in Constant Bit Rate for the same three video sequences using JM rate control. In this case a relation between bit rate and quality can be observed.
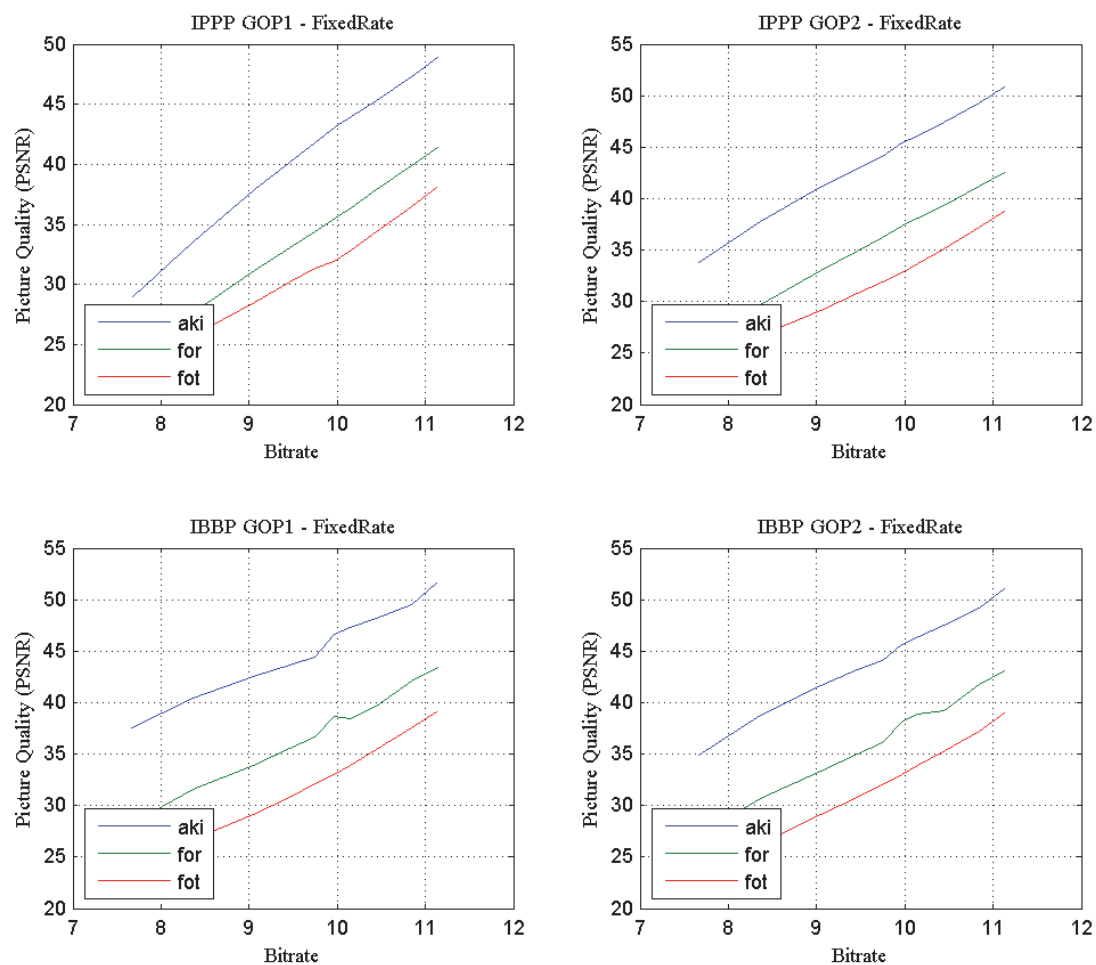

Fig. 5. Rate-distortion curve (Akiyo, Foreman, Football; FixeRate)

Frequently data can be noisy in its nature. Thus recognizing the trends in the data is important (Vardeman, 1994). One of the available methods for data analysis and identify existing trends in physical systems is curve fitting. The concept of curve fitting is rather simple: to use a simple function to describe a trend by minimizing the error between the selected function to fit and a set of data (Vardeman, 1994). The principle of least squares is applied to the fitting of a line to (x, y) data. Representative work for estimate the quantization step size has been most direct towards developing all kinds of rate-quantization (R-Q) models like polynomial (including linear and quadratic) (Chiang & Zhang, 1997; Lin & Ortega, 1998; Ronda et al., 1999; Yan & Liou, 1997), spline (Lin et al., 1996), logarithmic (Ding& Liu, 1996; Hang & J.J. Chen, 1997), power (Ding& Liu, 1996), etc. Yang et al. (Kyeong Ho Yang at al, 1997) proposed a more complex model that combines a logarithmic and a quadratic model. Most of the models only consider the rate function, and often implicitly assume that the distortion is a linear function of the quantization scale. This work has been extended to include D(QP) implementing several methods in order to compare their results. In fact, the goal is to model the quality versus quantization step

relationship and then to evaluate the different approaches to quality metric. It is presume that there is an inverse relationship between quality and distortion.

Before fitting data into a function that models the relationship between two measured quantities, it is a normal procedure to determine if a relationship exists between these quantities. It was decide to use the correlation method to confirm the degree of probability that a relationship exists between two measured quantities (Vardeman, 1994). In the case of no correlation between the two quantities, then there is no tendency for the values of one quantity to increase or decrease with the values of the second quantity. To evaluate the quality of the fit, it is used the sample correlation that represents the normalized measure of the strength of linear relationship between variables (Vardeman, 1994):

$$r = \frac{x^T y}{\sqrt{(x^T x)(y^T y)}} \tag{11}$$

$$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2 (y_i - \bar{y})^2}} = \frac{\sum x_i y_i - \frac{(\sum x_i)(\sum y_i)}{n}}{\sqrt{\left(\sum x_i^2 - \frac{(\sum x_i)^2}{n}\right)\left(\sum y_i^2 - \frac{(\sum y_i)^2}{n}\right)}} \tag{12}$$

where r is a matrix of correlation coefficients (Vardeman, 1994). The sample correlation always lies in the interval from -1 to 1. A value of r near of positive one or negative one, it is interpreted as indicating a relatively strong relationship and r near zero is inferred as indicating a lack of relationship. The sign of r indicates whether y tends to increase or decrease with increase x.

	IBBP-GOP1			IBBP-GOP2		
Sequence	I Type	P Type	B Type	I Type	P Type	B Type
Aki	0.8380	0.8470	0,9016	0,8645	0,8447	0,9034
Cgd	0.9210	0.9136	0,9595	0,9180	0,9139	0,9609
Dea	0.8853	0.8909	0,9303	0,8943	0,8878	0,9318
Flg	0.9137	0.9035	0,9349	0,9147	0,8962	0,9342
For	0.8964	0.8881	0,9197	0,8968	0,8836	0,9197
Fot	0.9588	0.9557	0,9691	0,9567	0,9550	0,9695
Hal	0.8154	0.7972	0,8589	0,8003	0,7936	0,8628
Mad	0.8797	0.8666	0,9124	0,8653	0,8645	0,9129
New	0.9554	0.9081	0,9511	0,9091	0,9128	0,9524
Par	0.9455	0.9435	0,9638	0,9461	0,9434	0,9651
Sil	0.9451	0.9412	0,9567	0,9419	0,9421	0,9576
Mcl	0.9356	0.9272	0,9470	0,9329	0,9250	0.9488

Table 2. Correlation coefficients between Bits Frames and Quality Metric (PSNR) for different H.264/AVC video sequences (IBBP-GOP1 and IBBP-GOP2).

Sequence	IPPP – GOP1		IPPP – GOP2	
	I Type	P Type	I Type	P Type
Aki	0.8962	0.9170	0.9107	0.9065
Cgd	0.9608	0.9617	0.9615	0.9609
Dea	0.9304	0.9406	0.9354	0.9348
Flg	0.9555	0.9586	0.9567	0.9572
For	0.9268	0.9333	0.9326	0.9289
Fot	0.9659	0.9686	0.9649	0.9665
Hal	0.8540	0.8848	0.8598	0.8646
Mad	0.9019	0.9200	0.9225	0.9121
New	0.9353	0.9492	0.9526	0.9391
Par	0.9609	0.9668	0.9627	0.9630
Sil	0.9605	0.9662	0.9613	0.9621
Mcl	0.9584	0.9715	0.9615	0.9636

Table 3. Correlation coefficients between Bits Frames and Quality Metric (PSNR) for different H.264/AVC video sequences (IPPP-GOP1 and IPPP-GOP2).

Equation (12) was computed for all the twelve sequences, and results were obtained according the different Picture Type and GOP pattern (Table 2 and Table 3). Thus, it was assess the hypothesis of a relationship between PSNR and Rate. Results are very high, for all the video sequences and GOP patterns, near positive one, pointing clearly to a strong positive linear relationship evident. Next step is thus to select what curve fitting functions should be assessed. Due to its simplicity, the first selected is one of the most commonly used techniques: the fitting of a straight line to a set of bivariate data generating a linear equation such as (13) (Vardeman, 1994):

$$\text{Linear} \quad y = \beta_0 + \beta_1 x \tag{13}$$

A natural generalization of equation (13) is the polynomial equation (14)

$$\text{Polynomial} \quad y = \beta_0 + \beta_1 x + \beta_2 x^2 + \ldots + \beta_k x^k \tag{14}$$

The goal is thus to minimize the function of k + 1 variables.

$$S(\beta_0, \beta_1, \beta_2, \ldots, \beta_k) = \sum_{i=1}^{n}(y_i - \hat{y}_i)^2$$
$$= \sum_{i=1}^{n}\left(y_i - \left(\beta_0 + \beta_1 x_i + \beta_2 x_i^2 + \ldots + \beta_k x_i^k\right)\right)^2 \tag{15}$$

by selecting the coefficients $\beta_0, \beta_1, \beta_2, \ldots, \beta_k$ (Vardeman, 1994). Upon setting the partial derivatives of $S(\beta_0, \beta_1, \beta_2, \ldots, \beta_k)$ equal to zero and doing some simplifications, one obtains the normal equations for this least squares problem:

$$n\beta_0 + \left(\sum x_i\right)\beta_1 + \left(\sum x_i^2\right)\beta_2 + \ldots + \left(\sum x_i^k\right)\beta_k = \sum y_i$$
$$\left(\sum x_i\right)\beta_0 + \left(\sum x_i^2\right)\beta_1 + \left(\sum x_i^3\right)\beta_2 + \ldots + \left(\sum x_i^{k+1}\right)\beta_k = \sum x_i y_i \tag{16}$$
$$\left(\sum x_i^k\right)\beta_0 + \left(\sum x_i^{k+1}\right)\beta_1 + \left(\sum x_i^{k+2}\right)\beta_2 + \ldots + \left(\sum x_i^{2k}\right)\beta_k = \sum x_i^k y_i$$

Solving the system of k+1 linear equations presented in Equation 16 it is typically possible to obtained a single set of values S($b_0, b_1, b_2, ..., b_k$) that minimize S($\beta_0, \beta_1, \beta_2, ..., \beta_k$). Polynomials are often used when a simple empirical model is required. One of the most uses polynomial models is the quadratic model (Equation 17):

$$\text{Quadratic} \quad y = \beta_0 + \beta_1 x + \beta_2 x^2 \tag{17}$$

To compare with the solution available in the literature it was decide to extend the models and thus include the logarithmic (18), the exponential (19), the power (20) and the linear with nonpolynomial model (LNP) (21).

$$\text{Logarithmic} \quad y = \beta_0 + \log x \tag{18}$$

$$\text{Exponential} \quad y = \beta_0 e^{\beta_1 x} \tag{19}$$

$$\text{Power} \quad y = \beta_0 + \beta_1 x^{\beta_2} \tag{20}$$

$$\text{Linear with nonpolynomial} \quad y = \beta_0 + \beta_1 e^{-x} + \beta_2 x e^{-x} \tag{21}$$

After selecting these six models, it was computed the average absolute error when trying to model the relation between bit-rate and quantization parameter (QP), PSNR and quantization parameter, and bit-rate and PSNR regarding the picture type using each of the six models for all the GOP patterns.

```
1. for each method do
2.       square error R(QP)(Picture Type) = 0;
3.       square error D(QP)(Picture Type) = 0;
4.       for each frame in the sequence do
5.              for each QP do
6.                     Extract Statistics [Bits, PSNR, Picture Type];
7.              endfor
8.              Estimate the parameters of the model for R(QP) (Picture Type);
9.              Compute the square error R for each D value (Picture Type);
10.             Update the accumulative squared error R(Picture Type);
11.             Estimate the parameters of the model for D(QP) (Picture Type);
12.             Compute the square error D for each D value (Picture Type);
13.             Update the accumulative squared error D(Picture Type);
14.             Estimate the parameters of the model for R(D) (Picture Type);
15.             Compute the square error R for each D value(Picture Type);
16.             Update the accumulative squared error R_D(Picture Type);
17.       endfor
18. endfor
```

Fig. 6. Pseudo code for R-D model fitting.

It was implemented the procedure described in Figure 6. Results are presented in Table 4, Table 5, and Table 6 for the twelve video sequences.

Fit Method	IPPP GOP1		IPPP GOP2		IBBP GOP1			IBBP GOP2		
	I Type	P Type	I Type	P Type	I Type	P Type	B Type	I Type	P Type	B Type
Linear fit	1285	1110	2114	807	4290	1166	965	2453	1264	1051
Quadratic fit	231	154	361	128	1002	328	196	614	363	200
Exponential fit	542	505	864	358	1584	410	396	872	442	436
Logarithmic fit	996	762	1603	590	3329	980	740	1976	1065	782
Power Regression	1023	1045	1712	712	3255	747	780	1725	778	880
LNP fit	1606	2344	2998	1389	6326	802	1377	2830	856	1760

Table 4. Mean Absolute Error for Rate-QP curve fitting.

Fit Method	IPPP GOP1		IPPP GOP2		IBBP GOP1			IBBP GOP2		
	I Type	P Type	I Type	P Type	I Type	P Type	B Type	I Type	P Type	B Type
Linear fit	0.05	0.03	0.08	0.03	0.18	0.06	0.04	0.11	0.06	0.04
Quadratic fit	0.02	0.01	0.03	0.01	0.06	0.02	0.01	0.04	0.02	0.01
Exponential fit	0.05	0.03	0.08	0.03	0.15	0.05	0.03	0.10	0.06	0.04
Logarithmic fit	0.08	0.04	0.12	0.04	0.20	0.07	0.05	0.13	0.08	0.05
Power Regression	0.14	0.08	0.22	0.07	0.35	0.12	0.08	0.22	0.13	0.08
LNP fit	0.77	0.45	1.23	0.41	2.10	0.70	0.47	1.31	0.76	0.47

Table 5. Mean Absolute Error for PSNR-QP curve fitting.

Fit Method	IPPP GOP1		IPPP GOP2		IBBP GOP1			IBBP GOP2		
	I Type	P Type	I Type	P Type	I Type	P Type	BI Type	I Type	P Type	B Type
Linear fit	9789	13947	10153	11387	11411	9470	11659	10344	9421	12543
Quadratic fit	1548	1845	1576	1652	2045	1976	1914	1908	2013	1970
Exponential fit	6954	11853	7034	8854	9265	6966	9087	8261	6726	10193
Logarithmic fit	11497	17611	12097	13859	13586	10704	13852	12030	10613	15178
Power Regression	4541	7258	4312	5525	5788	4655	5934	5321	4616	6574
LNP fit	25074	50461	27787	35324	33094	19738	32635	26451	19489	38917

Table 6. Mean Absolute Error for Rate-PSNR curve fitting.

From the results, several observations can be produce. First, the linear with nonpolynomial model is the least accurate while the quadratic approach is the most accurate overall. The second observation is that the accuracy of all models varies with the level of complexity of the video source data. Results improve for low complexity video sequences while decrease for sequence with higher complexity. Third observation, GOP pattern has impact on the average of the absolute error for the different type of pictures. For most of the models, the average absolute error (excluding linear with nonpolynomial model) is rather small.

Sequence	Fit Method	Rate-QP		PSNR-QP		Rate - PSNR	
		I Type	P Type	I Type	P Type	I Type	P Type
Akiyo	Linear fit	237	406	0.03	0.02	2128	6295
	Quadratic fit	65	62	0.01	0.01	635	1175
	Exponential fit	79	46	0.07	0.04	761	718
	Logarithmic fit	185	269	0.11	0.07	2369	7386
	Power Regression	91	211	0.16	0.10	1024	1751
	LNP fit	329	856	0.75	0.44	5755	22485
Foreman	Linear fit	1052	1076	0.05	0.03	8368	13411
	Quadratic fit	288	209	0.01	0.01	1917	2238
	Exponential fit	320	449	0.05	0.03	2658	10807
	Logarithmic fit	866	780	0.08	0.04	9314	16117
	Power Regression	317	831	0.12	0.07	3151	7614
	LNP fit	930	1872	0.70	0.41	19274	44875
Football	Linear fit	1864	1393	0.07	0.04	13364	15256
	Quadratic fit	324	194	0.02	0.01	1931	2186
	Exponential fit	394	377	0.04	0.02	8330	15092
	Logarithmic fit	1370	981	0.05	0.03	15922	19000
	Power Regression	1191	1007	0.10	0.05	4711	9574
	LNP fit	2831	2481	0.68	0.39	38402	55186

Table 7. Absolute error for Rate-QP, PSNR-QP and Rate-PSNR curve fitting (IPPP GOP1)

Considering individual video sequence results, they can be analysed according model fit, picture type, and GOP pattern for the different rate-distortion-quantization models.

Regarding Rate-QP, quadratic approach is the best solution in most of the cases (for IPPP GOP1 and IPPP GOP2 quadratic approach is the best solution for 9 video sequences regarding pictures type Intra and 10 video sequences for pictures type P and for the remaining video sequences the best solution is the exponential fit and power regression). Worst results of quadratic approach take place with IBBP GOP1 and IBBP GOP2 patterns (regarding picture type I, P and B, quadratic approach present the best results in 11, 6 and 8 video sequences for IBBP GOP1 and 10, 6 and 10 for IBBP GOP2). Besides quadratic approach, exponential fit and power regression also present good results, particularly in GOP patterns containing B images and for low to medium spatial and temporal complexity where motion estimation is most effective. In these cases, quadratic approach is usually the second best approach. Finally, quadratic is also the best approach for modelling Rate-PSNR (11 of 12 video sequences for IPPP GOP1 for both I and P frame types; 10 and 11 of 12 video sequences regarding respectively Intra and P frames for IPPP GOP2; 10, 11 and 10 for I, P and B frames regarding IBBP GOP1 and 10, 9 and 10 for I, P and B frames regarding IBBP GOP2). In this case, also exponential and power regression presents good results. Thus, quadratic approach is a good solution particularly for GOP sequences without B frames. For quality versus quantization parameter global results from different models are very good. In

Sequence	Fit Method	Rate-QP		PSNR-QP		Rate - PSNR	
		I Type	P Type	I Type	P Type	I Type	P Type
Akiyo	Linear fit	462	228	0.03	0.01	2620	3879
	Quadratic fit	108	43	0.02	0.01	671	828
	Exponential fit	111	39	0.10	0.04	627	687
	Logarithmic fit	339	157	0.17	0.06	2985	4504
	Power Regression	212	112	0.25	0.09	974	1252
	LNP fit	791	451	1.18	0.40	8110	13199
Foreman	Linear fit	1776	717	0.09	0.03	8771	10188
	Quadratic fit	460	169	0.02	0.01	1804	2044
	Exponential fit	434	277	0.07	0.02	2585	6455
	Logarithmic fit	1444	550	0.11	0.04	9857	11844
	Power Regression	542	450	0.19	0.06	2680	5056
	LNP fit	1707	1045	1.11	0.37	21255	29684
Football	Linear fit	3043	1068	0.11	0.04	13687	13833
	Quadratic fit	532	179	0.03	0.01	2111	2059
	Exponential fit	664	250	0.07	0.02	8938	10504
	Logarithmic fit	2212	774	0.09	0.03	16452	16704
	Power Regression	1974	711	0.16	0.05	5008	6378
	LNP fit	4872	1722	1.09	0.36	40679	43617

Table 8. Absolute error for Rate-QP, PSNR-QP and Rate-PSNR curve fitting (IPPP GOP2).

Sequence	Fit Method	Rate-QP			PSNR-QP			Rate - PSNR		
		I Type	P Type	B Type	I Type	P Type	B Type	I Type	P Type	B Type
Akiyo	Linear fit	1063	115	221	0.05	0.02	0.01	3554	1101	3211
	Quadratic fit	190	46	51	0.04	0.02	0.01	787	467	821
	Exponential fit	218	56	44	0.17	0.06	0.04	689	561	694
	Logarithmic fit	707	99	163	0.28	0.10	0.07	4164	1173	3649
	Power Regression	605	37	96	0.42	0.14	0.10	1134	683	1129
	LNP fit	2269	65	368	2.04	0.68	0.46	12646	2065	9806
Foreman	Linear fit	2736	726	767	0.14	0.04	0.03	8112	6506	9608
	Quadratic fit	894	312	209	0.06	0.02	0.01	2140	2286	2200
	Exponential fit	1123	389	286	0.11	0.05	0.03	2798	2561	5044
	Logarithmic fit	2175	634	605	0.19	0.08	0.04	9144	7028	10961
	Power Regression	1132	265	428	0.32	0.12	0.07	3557	3533	4228
	LNP fit	3396	414	970	1.92	0.66	0.43	22550	12363	25987
Football	Linear fit	5893	1564	1368	0.21	0.07	0.05	14309	12830	15554
	Quadratic fit	1038	289	241	0.07	0.03	0.02	2248	2243	2346
	Exponential fit	1779	558	369	0.12	0.04	0.03	12625	8303	11469
	Logarithmic fit	4261	1179	991	0.15	0.06	0.04	17668	15125	18796
	Power Regression	4411	1254	962	0.28	0.10	0.06	7311	4577	6842
	LNP fit	9912	2162	2207	1.95	0.67	0.43	45468	33470	47853

Table 9. Absolute error for Rate-QP, PSNR-QP and Rate-PSNR curve fitting (IBBP GOP1).

this case, linear fit results are very interesting as although they are not among the best approaches, the error is rather small, particularly for low complex video sequences. These results indicate that aggregate video results might be represented by the following equations:

$$R = \beta_0 + \beta_1 QP + \beta_2 QP^2 \tag{22}$$

$$PSNR = \beta_0' + \beta_1' \times QP + \beta_2' \times QP^2 \tag{23}$$

$$R = \beta_0'' + \beta_1'' \times PSNR + \beta_2'' \times PSNR^2 \tag{24}$$

Sequence	Fit Method	Rate-QP			PSNR-QP			Rate - PSNR		
		I Type	P Type	B Type	I Type	P Type	B Type	I Type	P Type	B Type
Akiyo	Linear fit	467	120	296	0.04	0.03	0.02	2452	1056	4331
	Quadratic fit	109	49	58	0.03	0.02	0.01	644	447	939
	Exponential fit	118	59	48	0.12	0.07	0.04	606	547	740
	Logarithmic fit	328	104	206	0.19	0.12	0.07	2835	1124	5009
	Power Regression	247	38	142	0.27	0.16	0.10	897	664	1358
	LNP fit	915	67	568	1.29	0.75	0.46	8218	1961	14468
Foreman	Linear fit	1559	768	861	0.08	0.04	0.03	7387	6307	10540
	Quadratic fit	565	331	206	0.04	0.02	0.01	2144	2255	2173
	Exponential fit	677	430	342	0.09	0.05	0.03	2361	2753	6879
	Logarithmic fit	1297	671	652	0.15	0.09	0.05	8159	6801	12310
	Power Regression	544	296	575	0.23	0.14	0.08	3318	3672	5214
	LNP fit	1517	431	1315	1.24	0.72	0.44	17604	11880	31947
Football	Linear fit	3228	1714	1428	0.12	0.07	0.05	13308	12846	15837
	Quadratic fit	547	328	237	0.04	0.03	0.02	2263	2280	2469
	Exponential fit	1047	609	398	0.08	0.05	0.03	10027	8032	12944
	Logarithmic fit	2368	1295	1024	0.11	0.06	0.04	16052	15114	19319
	Power Regression	2510	1357	1031	0.20	0.11	0.06	5714	4359	7924
	LNP fit	5049	2352	2398	1.27	0.73	0.44	38424	33451	51582

Table 10. Absolute error for Rate-QP, PSNR-QP and Rate-PSNR curve fitting (IBBP GOP2)

7. Rate variability as a function of the video quality.

A second important issue for joint video coding broadcasting is the Rate Variability-Distortion (VD). Two sub-sets have been consider from the initial set of twelve video sequences: a first sub-set with camera movement, medium to high spatial detail and temporal complexity (sequences Foreman, Football, Coastguard, Flower Garden, and Mobile and Calendar), and a second sub-set with fixed camera and low to medium spatial detail and motion activity (Akiyo, Deadline, Hall, Mother and Daughter, News, Paris, and Silence).

Results are presented in Figure 7, Figure 8, Figure 9, and Figure 10. In the left side it can be observe the results from the first sub-set and in the right the charts for the second sub-set. Simulations results are from open-loop coding setup.
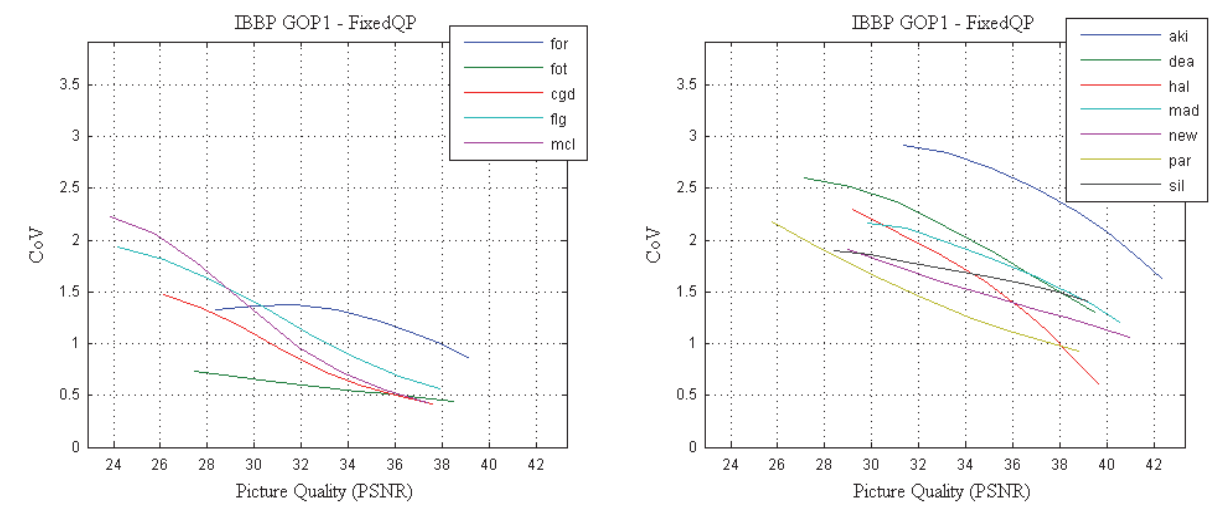
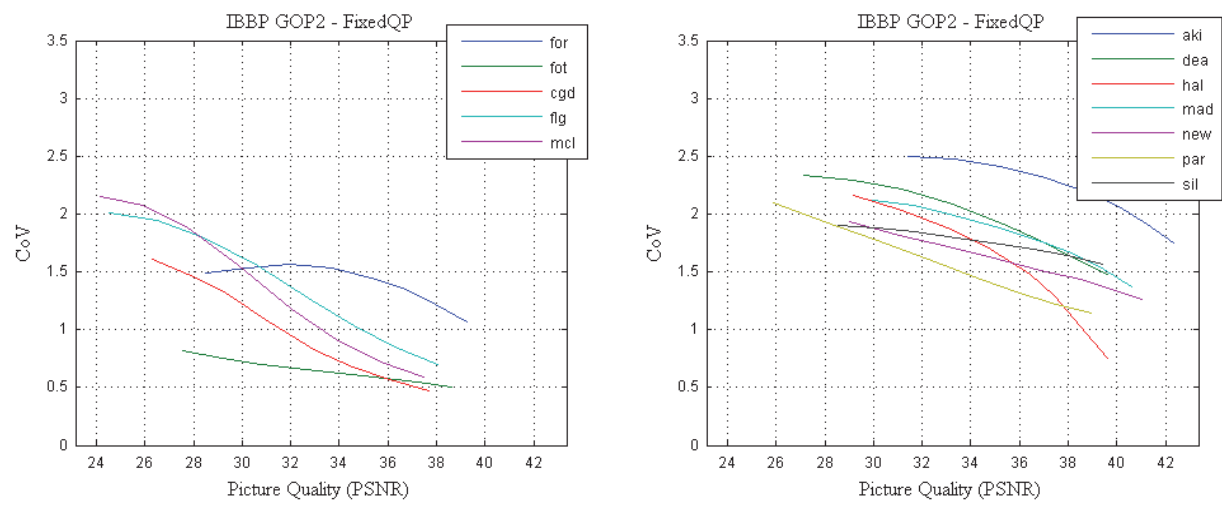Fig. 7. Rate Variability-distortion (VD) Curve (PSNR; IBBP GOP1).

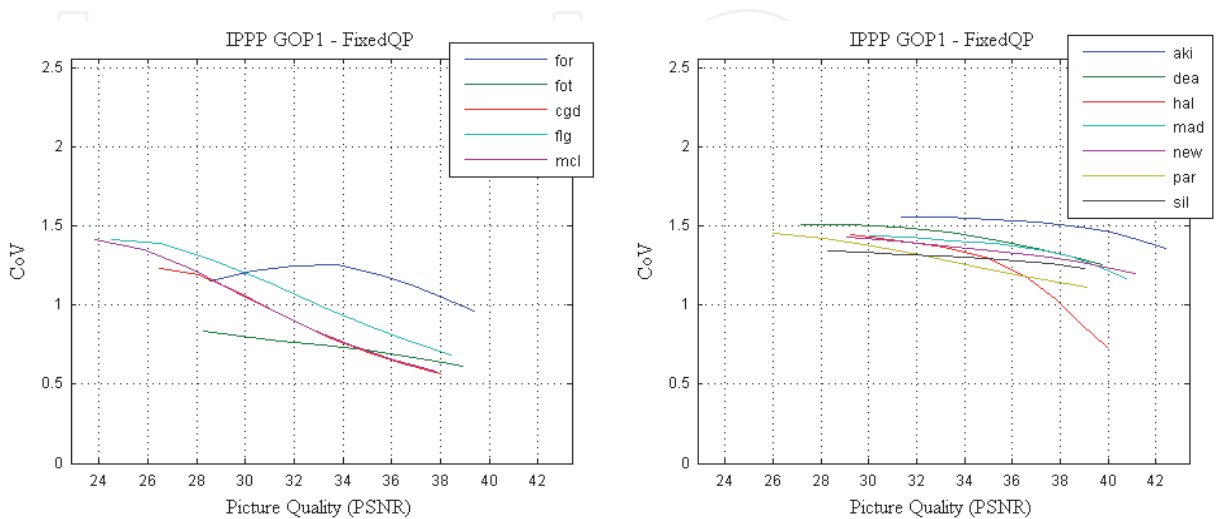Fig. 8. Rate Variability-distortion (VD) Curve (PSNR; IBBP GOP2).

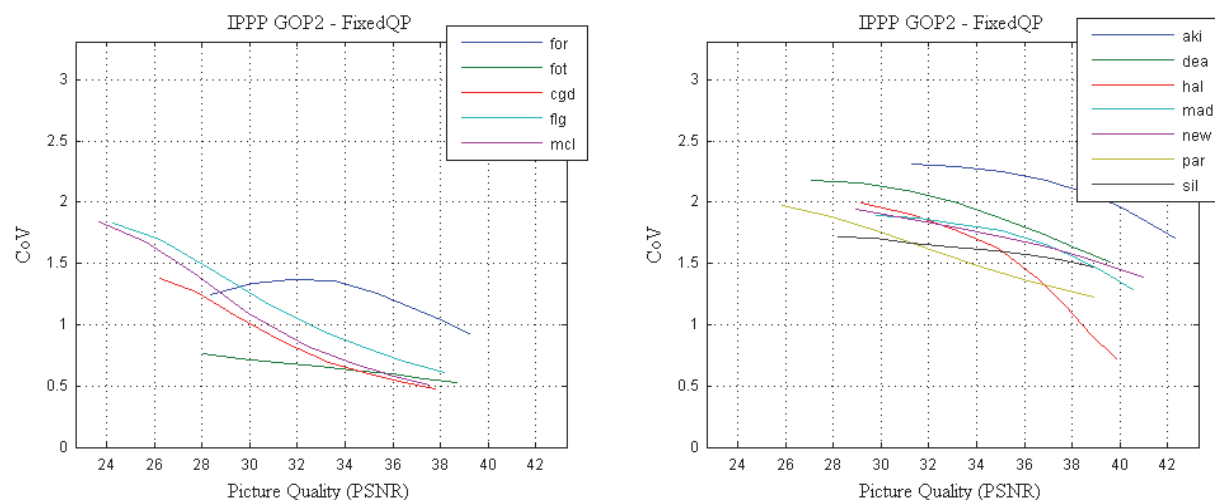Fig. 9. Rate Variability-distortion (VD) Curve (PSNR; IPPP GOP1).

Fig. 10. Rate Variability-distortion (VD) Curve (PSNR; IPPP GOP2).

For high spatial complexity and motion activity sequences, variability is significantly lower than the sub-set of sequences with lower spatial and temporal complexity. At the same time, GOP patterns with B frames present higher values of variability regarding GOP patterns without B frames. As frames of type I show lower compression ratio compared to Predicted and Interpolated frames type, the combination of the different types of frames results in the observed higher bit-rate variability.

As the GOP size increases, the amplitude variation regarding the variability increases. This effect is stronger with the video sub-set of lower spatial and temporal complexity sequences. In these cases, motion estimation is very effective resulting in higher compression ratios for P and B pictures comparing to the bits budget of a typical Intra image. B frames, in general, present a small reduction of the variability in sequences with higher complexity. The amplitude of this variation increases while the sequence complexity decreases.

8. Acknowledgment

9. References

Adjeroh, D.A. & Lee, M.C. (2004). Scene-adaptive transform domain video partitioning, *IEEE Transaction on Multimedia*, Vol. 6. No 1 (February 2004), pp 58-69, ISSN 1520-9210.

Bellman, R.E. (2003). *Dynamic Programming*, Princeton University Press, Dover paperback edition (2003), ISBN 0486428095.

Berger, T. (1971). Rate Distortion Theory, Prentice-Hall, Inc., ISBN 0137531036, Englewood Cliffs, NJ.

Chan, Y.-L & Siu, W.-C. (2001). An efficient search strategy for block motion estimation using image features, IEEE Transactions on Image Processing, Vol 10, No 8 (August 2001), pp 1223-1238, ISSN 1057-7149.

Chen, J.J. & Lin, D.W. (1996). Optimal bit allocation for video coding under multiple constraints, *Proceedings of the IEEE International Conference Image Processing 1996*, Vol. 3, pp 403 – 406, ISBN 0-7803-3259-8, Lausanne, Switzerland, Sep 16-19, 1996.

Chen, Z. & Ngan, K. N. (2004). Linear rate-distortion models for MPEG-4 shape coding, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 14, No 6 (June 2004), pp 869–873, ISSN 1051-8215.

Chen, Z. & Ngan, K. N. (2005b). Rate-distortion analysis for MPEG-4 binary shape coding, Proceedings of IEEE International Symposium on Intelligent Signal Processing and Communications Systems, pp 801 - 804, ISBN 0-7803-9266-3, Hong Kong, December 13-16, 2005.

Chen, Z. & Ngan, K. N. (2005a). Joint texture-shape optimization for MPEG-4 multiple video objects, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 15, No 2 (September 2005). pp 1170–1174, ISSN 1051-8215.

Chen, Z. & Ngan, K. N. (2007). Recent advances in rate control for video coding, Signal Processing: Image Communication, Vol 22, No 1 (January 2007), pp 19-38, ISSN 0923-5965.

Chiang, T. & Zhang, Y.-Q. (1997). A new rate control scheme using quadratic rate distortion model, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 7, No 1 (January 1997), pp 246-250, ISSN 1051-8215.

Chung, K.-L. & Chang, L-.C (2003). A new predictive search area approach for fast block motion estimation, *IEEE Transactions on Image Processing*, Vol. 12, No 6 (June 2003), pp 648-652, ISSN 1057-7149.

Ding, W. & Liu, B. (1996). Rate control of MPEG video coding and recording by rate-quantization modeling, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 6, No 1 (January 1996), pp 12-20, ISSN 1051-8215.

Everett, H. (1963). Generalized Lagrange multiplier method for solving problems of optimum allocation of resource, in Operations Research, Vol 11, N0. 3, pp 399–417, ISSN 0030-364X.

Forney, G. D. (1973). The Viterbi algorithm, Proceedings of the IEEE , Vol 61, No 3, pp 268–278, ISSN 0018-9219.

Kim, H.M. (2003). Adaptive rate control using nonlinear regression, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 13, No 5 (May 2003), pp 432-439, ISSN 1051-8215.

Hang, H. M. & Chen, J.J. (1997). Source model for transform video coder and its application – part I: fundamental theory, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 7, No 2 (April 1997), pp 287-298, ISSN 1051-8215.

He, Z. & Mitra, S. K. (2002). Optimum bit allocation and accurate rate control for video coding via-domain source modelling, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 12, No 10 (Octobre 2002), pp 840–849, ISSN 1051-8215.

He, Z. (2001). rho-Domain Rate-Distortion Analysis and Rate Control for Visual Coding and Communication, PhD Dissertation, University of California, Santa Barbara, June 2001.

Huang, J. J. Y. & Schultheiss, P.M. (1963). Block quantization of correlated Gaussian random variables, IEEE Transaction on Communications Systems, Vol 11, N 3, pp 289–296, ISSN 0096-1965.

ISO/IEC (1997). Text of ISO/IEC 14496-2 MPEG-4 Video VM-Version 8.0, ISO/IEC JTC1/SC29/WG11 Coding of Moving Pictures and Associated Audio MPEG 97/W1796, Stochholm, Sweden, July 1997.

ISO/IEC, JTC1/SC29/WG11 (1993). MPEG Video Test Model 5 (TM-5), document MPEG93/457, April 1993.

ITU-T (2005). Rec. H.264.2 : Reference software for advanced video coding, 2005.

ITU-T, SG16 (1997). Video Codec Test Model, near-term, Version 8 (TMN8), Document Q15-A-59, Portland, USA, June 1997.

Kamaci, N.; Altunbasak, Y. & Mersereau, R. M. (2005). Frame bit allocation for the H.264/AVC video coder via Cauchy-density-based rate and distortion models, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 15, No 5 (August 2005), pp 994–1006, ISSN 1051-8215.

Keesman, G.; Shah, I. & Klein-Gunnewiek, R. (1995). Bit-rate control for MPEG encoders, Signal Processing: Image Communication, Vol 6, No 6 (February 1995), pp 545-560, ISSN 0923-5965.

Lee, H. J.; Chiang, T. & Zhang, Y. Q. (2000). Scalable rate control for MPEG-4 video, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 10, No 6 (September 2000), pp 878-894, ISSN 1051-8215.

Li, Z. G.; Pan, F.; Lim, K. P.; Feng, G. ; Lin, X. & Rahardja, S. (2003a). Adaptive basic unit layer rate control for JVT, Joint Video Team of ISO/IEC MPEG and ITU-T VCEG, document JVT-G012r1, March 2003.

Li, Z. G.; Gao, W.; Pan, F.; Ma, S. ; Lin, K. P. ; Feng, G.; Lin, X.; Rahardja, S.; Lu, H. & Lu, Y. (2003b). Adaptive Rate Control with HRD Consideration, document JVT-H014, 8th meeting, Geneva, May 2003.

Li, Z. G.; Pan, F.; Lim, K.P.; Feng, G.N. ; Lin, X. ; Rahardja, S. & Wu, D.J. (2003c). Adaptive frame layer rate control for H.264, Proceedings. 2003 International Conference on Multimedia and Expo, 2003, Vol 1, pp 581-584, ISBN 0-7803-7965-9, July 6-9, 2003.

Li, Z. G.; Pan, F.; Lim, K.P.; Lin, X. & Rahardja, S. (2004). Adaptive rate control for H.264, 2004 International Conference on Image Processing, pp 745-748, ISBN 0-7803-8554-3, October 24-27, 2004.

Lim, K. P ; Sullivan, G. & Wiegand, T. (2007). Text Description of Joint Model Reference Encoding Methods and Decoding Concealment Methods, Joint Video Team of ISO/IEC MPEG and ITU-T VCEG, document JVT-W057, San Jose, April 2007.

Lin, L. J. & Ortega, A. (1998). Bit-rate control using piecewise approximated rate-distortion characteristics, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 8, No 4 (August 1998), pp 446-459, ISSN 1051-8215.

Lin, L. J.; Ortega, A. & Kuo, C.-C.J.(1996). Rate control using spline-interpolated R-D characteristics, SPIE Visual Communication Image Processing, Cambridge Visual Communication Image Processing, Cambridge, Orlando, FL, 1996, pp. 111-122.

Ma, S.; Gao, W & Lu, Y. (2002). Rate Control on JVT Standard, Joint Video Team (JVT) of ISO/IEC MPEG & ITU-T VCEG (ISO/IEC JTC1/SC29/WG11 and ITU-T SG16 Q.6), document JVT-D030, 4th Meeting: Klagenfurt, Austria, July 22-26, 2002.

Ma, S.; Gao, W. & Lu, Y. (2005). Rate-distortion analysis for H.264/AVC video coding and its application to rate control, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 15, No 12 (December 2005), pp 1533-1544, ISSN 1051-8215.

Ortega, A. (1996). Optimal bit allocation under multiple rate constraints, Proceedings of the Data Compression Conference, pp 349–358, ISBN 0-8186-7358-3, Snowbird, UT, USA, 31 Mar – 01 April, 1996.

Puri, A.; Hang, H.-M. & Schilling, D. L. (1987). Interframe coding with variable block-size motion compensation, *Proceedings of IEEE Global Telecomm. Conf. (GLOBECOM)*, pp 65-69, 1987.

Ramchandran, K.; Ortega, A. & Vetterli, M. (1993). Bit allocation for dependent quantization with applications to MPEG video codec, 1993 IEEE International Conference on Acoustics, Speech, and Signal Processing, pp. 381-385, ISBN 0-7803-7402-9, Minneapolis, April 27-30, 1993.

Ramchandran, K.; Ortega, A. & Vetterli, M. (1994). Bit allocation for dependent quantization with applications to multiresolution and MPEG video coders, IEEE Transactions on Image Processing, Vol.3, No.5, pp.533-545, ISSN 1057-7149.

Rhee, I.; Martin, G. R. ; Muthukrishnan, S. & Packwood, R. A. (2001). Quadtree-structured variable-size block-matching motion estimation with minimal error, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 10, No 2 (February 2001), pp 42-50, ISSN 1051-8215.

Ribas-Corbera, J. & Lei, S. (1999). Rate control in DCT video coding for low-delay communications, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 9, No 1 (February 1999), pp 172-185, ISSN 1051-8215.

Ribas-Corbera, J. & Neuhoff, David L. (1998). Optimizing block size in motion compensated video coding, *Journal of Electronic Imaging*, Vol. 7, No 1 (January 1998), pp.155-165, ISSN 1017-9909.

Ronda, J. I.; Eckert, M.; Jaureguizar, F. & Garcia, N. (1999). Rate control and bit allocation for MPEG-4, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 9, No 12 (December 1999), pp 1243–1258, ISSN 1051-8215.

Schuster, G. M. & Katsaggelos, A.K. (1997a). *Rate Distortion based Video Compression*, Kluwer Academic Publishers, ISBN 978-1-4419-5172-4, Norwell, MA.

Schuster, G. M. & Katsaggelos, A.K. (1997b). A video compression scheme with optimal bit allocation among segmentation motion and residual error, *IEEE Transactions on Image Processing*, Vol 6, No 11 (November 1997), pp 1487–1502, ISSN 1057-7149.

Seeling, P.; Fitzek, F. H. P. & Reisslein, M. (2007). Video Traces for Network Performance Evaluation - A Comprehensive Overview and Guide on Video Traces and Their Utilization in Networking Research, Springer Verlag, 272 pages, ISBN 978-1-4020-5565-2, 2007.

Seeling, P.; Reisslein, M. & Kulapala, B. (2004). Network Performance Evaluation with Frame Size and Quality Traces of Single-Layer and Two-Layer Video: A Tutorial,

IEEE Communications Surveys & Tutorials, Vol. 6, No. 3 (Third Quarter 2004), pp 58-78, ISSN 1553-877X.

Shoham, Y. & Gersho, A. (1988). Efficient bit allocation for an arbitrary set of quantizers, *IEEE Transaction in Acoustics, Speech and Signal Processing*, Vol. 36, pages 1445–1453, ISSN 1053-587X.

Sullivan, G. J. & Wiegand, T. (1998). Rate-distortion optimization for video compression, *IEEE Signal Processing Magazine*, Vol. 15, No. 6 (November 1998), pp 74–90, ISSN 1053-5888.

Sullivan, G.J. & Wiegand, T. (1997). A theory for the optimal bit allocation between displacement vector field and displaced frame difference, *IEEE Journal on Selected Areas in Communications*, Vol 15, No 9 (December 1997), pp 1739–1751, ISSN 0733-8716.

Tourapis, H.-Y.C. & Tourapis, A.M. (2003). Fast motion estimation within the H.264 codec, *Proceedings. 2003 International Conference on ICME '03*, Vol 3, pp 517-520, ISBN 0-7803-7965-9, July 6-9, 2003.

Vardeman, S. (1994). Statistics for Engineering Problem Solving, PWS Publishing Company, ISBN 0-534-92871-4, boston, USA.

Vetro, A. ; Sun, H. & Wang. Y. (1999). MPEG-4 rate control for multiple video objects, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 9, No 2 (February 1999), pp 186–199, ISSN 1051-8215.

Wiegand, T. & Girod, B. (2001). Lagrange multiplier selection in hybrid video coder control, *Proceedings of 2001 International Conference on Image Processing*, pp 542–545, ISBN 0-7803-6725-1, 07 Oct 2001-10 Oct 2001.

Wiegand, T.; Schwarz, H.; Joch, A.; Kossentini, F. & Sullivan, G. J. (2003a). Rate-Constrained Coder Control and Comparison of Video Coding Standards, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 13, No 7 (July 2003), pp 688-703, ISSN 1051-8215.

Wiegand, T.; Sullivan, G. J. & Luthran, A. (2003b). Draft ITU-T Recommendation H.264 and Final Draft International Standard 14496-10 Advanced Video Coding, Joint Video Team of ISO/IEC JTC1/SC29/WG11 and ITU-T SG16/Q.6, document JVT-G050rl; Geneva, Switzerland, May 2003

Wiegand, T.; Sullivan, G. J.; Bjontegaard, G. & Luthra, A. (2003c). Overview of the H.264/AVC video coding standard, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 13, No 7 (July 2003), pp 560-576, ISSN 1051-8215.

Wu, Y.; Shouxun, L. & Zhang (2005). Optimum Bit Allocation and Rate Control for H.264/AVC, Joint Video Team (JVT) of ISO/IEC MPEG & ITU-T VCEG (ISO/IEC JTC1/SC29/WG11 and ITU-T SG16 Q.6), document JVT- O016, 15th Meeting, Busan, KR, April 16-22, 2005.

Yan, A. Y. K. & Liou, M. L. (1997). Adaptive predictive rate control algorithm for MPEG videos by rate quantization method, *Proceedings on Picture Coding Symposium*, pp 619-624, Berlin, Germany, September 1997.

Yin, P. & Boyce, J. (2004). A new rate control scheme for H.264 video coding, Proceedings of ICIP '04. 2004 International Conference on Image Processing, pp 449-452, ISBN 0-7803-8554-3, October 24-27, 2004.

Zhang, J. ; He, Y. ; Yang, S. & Zhong, Y. (2003). Performance and complexity joint optimization for H.264 video coding, *Proceedings on IEEE International Symposium Circuits and Systems 2003 (ISCAS'03)*, pp 888-891, ISBN 0-7803-7761-3, May 25-28 , 2003.

Zhang, Z.; Liu, G. ; Li, H. & Li, Y. (2005). A novel PDE-based rate distortion model for rate control, *IEEE Transactions on Circuits and Systems for Video Technology*, Vol. 15, No (2005), pp 1354–1364, ISSN 1051-8215.
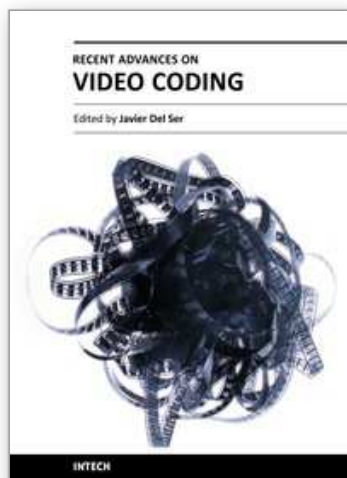
Recent Advances on Video Coding

Edited by Dr. Javier Del Ser Lorente

This book is intended to attract the attention of practitioners and researchers from industry and academia interested in challenging paradigms of multimedia video coding, with an emphasis on recent technical developments, cross-disciplinary tools and implementations. Given its instructional purpose, the book also overviews recently published video coding standards such as H.264/AVC and SVC from a simulational standpoint. Novel rate control schemes and cross-disciplinary tools for the optimization of diverse aspects related to video coding are also addressed in detail, along with implementation architectures specially tailored for video processing and encoding. The book concludes by exposing new advances in semantic video coding. In summary: this book serves as a technically sounding start point for early-stage researchers and developers willing to join leading-edge research on video coding, processing and multimedia transmission.

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