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# Adaptive Navigation Control for Swarms of Autonomous Mobile Robots 

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## 1. Introduction

Deploying a large number of resource-constrained mobile robots performing a common group task may offer many advantages in efficiency, costs per system, and fault-tolerance (Sahin, 2005). Therefore, robot swarms are expected to perform missions in a wide variety of applications such as environment and habitat monitoring, exploration, odor localization, medical service, and search-and-rescue. In order to perform the above-mentioned tasks successfully, one of the most important concerns is how to enable swarms of simple robots to autonomously navigate toward a specified destination in the presence of obstacles and dead-end passageways as seen in Fig. 1. From the standpoint of the decentralized coordination, the motions of individual robots need to be controlled to support coordinated collective behavior.
We address the coordinated navigation of a swarm of mobile robots through a cluttered environment without hitting obstacles and being trapped in dead-end passageways. Our study is motivated by the observation that schools of fish exhibit emergent group behavior. For instance, when schools of fish are faced with obstacles, they can split themselves into a plurality of smaller groups to avoid collision and then merge into a single group after passing around the obstacles (Wilson, 1976). It is also worth noting that a group of fish facing a dead end can get out of the area.
Based on the observation of schooling behavior in fish, this work aims to present a novel adaptive group behavior, enabling large-scale robot swarms with limited sensing capabilities to navigate toward a goal that is visible only to a limited number of robots. In particular, the coordinated navigation is achieved without using any leader, identifiers, common coordinate system, and explicit communication. Under such a minimal robot model, the adaptive navigation scheme exploits the geometric local interaction which allows three neighboring robots to form an equilateral triangle. Specifically, the proposed algorithm allows robot swarms to 1) navigate while maintaining equilateral triangular lattices, 2) split themselves into multiple groups while maintaining a uniform distance of each other, 3) merge into a single group while maintaining a uniform distance of each other,
and 4) escape from any dead-end passageways. During the adaptive navigation process, all robots execute the same algorithm and act independently and asynchronously of each other. Given any arbitrary initial positions, a large-scale swarm of robots is required to navigate toward a goal position in an environment while locally interacting with other robots. The basic necessities for the proposed solution are argued as follows. First, the robots can selfcontrol their travel direction according to environmental conditions, leading to enhancing autonomy of their behavior. Secondly, by being split into multiple groups or re-united into a single swarm, the robots can self-adjust its size and shape depending on the conditions. By the capabilities above, robots have the emergent capability to maximize adaptability to operate in uncertain environments. Thirdly, the coordinated navigation of multiple robots in an equilateral triangle formation reduces a potential traffic jam and stragglers.

(a) adaptive navigation problem


Fig. 1. Concept of adaptive navigation by autonomous mobile robot swarms
Consequently, the proposed adaptive navigation provides a cost-effective way to allow for an increase in efficiency and autonomy of group navigation in a highly cluttered environment. What is important from a practical standpoint is that the swarm flocking is considered as a good ad hoc networking model whose connectivity must be maintained while moving. In particular, maintaining the uniform distance enables the model to optimize efficient energy consumption in routing protocols (Fowler, 2001)(Lyengar et al., 2005). This networking model can potentially be used in application examples such as exploration and search-and-rescue. This navigation can be further applied to swarms of unmanned vehicles and sensors performing autonomous operations such as capturing and transporting toxic and hazardous substances. We describe our algorithm in detail, and perform extensive simulations to demonstrate that a swarm of robots can navigate toward a specified destination while adapting to unknown environmental conditions in a scalable manner.
The rest of this paper is organized as follows. Section 2 introduces a brief description of research related to swarming and flocking and sheds light on our motivation. Section 3 presents the robot model and the formal definitions of the adaptive navigation problem. Section 4 describes the fundamental motion control of each robot locally interacting with
their neighboring robots, leading to forming an equilateral triangle lattice. Section 5 gives the solution scheme of the adaptive navigation. Section 6 demonstrates the validity and applicability of the proposed scheme through extensive simulations. Section 7 draws conclusions.

## 2. Background

Wireless network-enabled mobile robotic sensors have been increasingly popular over the recent years (Yicka et al., 2008). Such robotic sensors dispersing themselves into an area can be used for search-and-rescue and exploration applications by filling the area of interest and/or establishing an ad hoc network. To achieve a desired level of self-deployment of robotic sensors, many prior studies have attempted to use decentralized approaches in selfconfiguration (Lee \& Chong, 2009)(Shucker et al., 2008)(Spears et al., 2004), pattern generation (Lee \& Chong, 2009-b)(Ikemoto et al., 2005), and navigation (Gu \& Hu, 2010)(Lee \& Chong, 2008)(Olfati-Saber, 2006). In particular, we have witnessed a great interest in distributed navigation control that enables a large number of robots to navigate from an initial position toward a desired destination without human intervention.
Recently, many navigation control studies have been reported in the field of swarm robotics, where the decentralized navigation controls are mainly based on interactions between individual robots mostly inspired by evidence from biological systems (e.g., fish schools or bird flocks) or natural phenomena (e.g., liquid diffusion). The navigation control can be further divided into biological emergence (Folino \& Spezzano, 2002)(Reynolds, 1987), behavior-based (Lee \& Chong, 2008)(Ogren \& Leonard, 2005)(Balch \& Hybinette, 2000), and virtual physics-based (Esposito \& Dunbar, 2006)(Zarzhitsky et al., 2005)(Spears et al., 2006) approaches. Specifically, the behavior-based and virtual physics-based approaches are related to the use of such physical phenomena as gravitational forces (Zarzhitsky et al., 2005)(Spears et al., 2006) and potential fields (Esposito \& Dunbar, 2006). Those works mostly use some sort of force balance between inter-individual interactions exerting an attractive or repulsive force on each other. This is mainly because the force-based interaction rules are considered simple yet effective, and provide an intuitive understanding on individual behavior. However, the computation of relative velocities or accelerations between robots is needed to obtain the magnitude of the interacting force.
Regarding the aspect of calculating the movement position of each robot, accuracy and computational efficiency issues have been attracted. In practice, many works on robot swarms use sensor-rich information and explicit means of communication. Note that if any means of communication would be employed, robots need to identify with each other or use a global coordinate or positioning system (Correll et al., 2000)(Lam \& Liu, 2006)(Nembrini et al., 2002). In this paper, we attempt to achieve adaptive navigation without taking advantage of rich computational capabilities and communication. This will allow us to develop robot systems in simple, robust, and non-costly ways. A subset of this work was reported in (Lee \& Chong, 2008) which provided mobile robot swarms with basic navigation and adaptation capabilities. The main objective of this paper is to present a completely new and general adaptive navigation coordination scheme assuming a more complicated arena with dead-end passageways. Specifically, we highlight the simplicity and intuition of the self-escape capability without incorporating a combination of sophisticated algorithms.

## 3. Problem statement

### 3.1 Robot model and notations



Fig. 2. Illustration of definition and notation
In this work, we consider a swarm of mobile robots denoted by $r_{1}, \cdots, r_{n}$. It is assumed that an initial distribution of all robots is arbitrary and their positions are distinct. Each robot autonomously moves on a two-dimensional plane. Robots have no leader and no identifiers. They do not share any common coordinate system. Due to a limited observation range, each robot can detect the positions of other robots only within its line-of-sight. In addition, robots are not allowed to communicate explicitly with each other.
Next, as illustrated in Fig. 2-(a), let's consider a robot $r_{i}$ with local coordinate system $\vec{r}_{x, i}$ and $\vec{r}_{y, i}$. The robot's heading direction $\vec{r}_{y, i}$ is defined as the vertical axis of $r_{i}{ }^{\prime} s$ coordinate system. It is straightforward to determine the horizontal axis $\overrightarrow{\mathrm{r}}_{\mathrm{x}, \mathrm{i}}$ by rotating $\overrightarrow{\mathrm{r}}_{\mathrm{y}, \mathrm{i}} 90$ degrees clockwise. The position of $r_{i}$ is denoted by $p_{i}$. Note that $p_{i}$ is $(0,0)$ with respect to $r_{i}{ }^{\prime} s$ local coordinate system. The line segment $\overline{\mathrm{p}_{\mathrm{i}} \mathrm{p}_{\mathrm{j}}}$ is defined as a straight line between $p_{i}$ and $p_{j}$ occupied by another robot $r_{j}$. The distance between $p_{i}$ and $p_{j}$ is defined as $\operatorname{dist}\left(p_{i}, p_{j}\right)$. In particular, the desired inter-robot distance between $r_{i}$ and $r_{j}$ is denoted by $d_{u}$. Moreover, ang $\left(\overrightarrow{\mathrm{m}}_{\mathrm{i}}, \overrightarrow{\mathrm{n}}_{\mathrm{i}}\right)$ denote the angle between two arbitrary vectors $\overrightarrow{\mathrm{m}}_{\mathrm{i}}$ and $\overrightarrow{\mathrm{n}}_{\mathrm{i}}$.
As shown in Fig. 2-(b), $r_{i}$ detects the positions $p_{j}, p_{k}$ and $p_{l}$ of other robots located within its sensing boundary SB , yielding a set of the positions $\mathrm{O}_{\mathrm{i}}\left(=\left\{\mathrm{p}_{\mathrm{j}}, \mathrm{p}_{\mathrm{k}}, \mathrm{p}_{\mathrm{l}}\right\}\right)$ with respect to its local coordinate system. When $r_{i}$ selects two robots $r_{n 1}$ and $r_{n 2}$ within its SB, we call $r_{n 1}$ and $r_{n 2}$ the neighbors of $r_{i}$, and their position set $\left\{p_{n 1}, p_{n 2}\right\}$ is denoted by $N_{i}$ as illustrated in Fig. 2-(c). Given $p_{i}$ and $N_{i}$, a set of three distinct positions $\left\{p_{i}, p_{n 1}, p_{n 2}\right\}$ with respect to $r_{i}$ is called the triangular configuration $T_{\mathrm{i}}$, namely $\left\{\mathrm{p}_{\mathrm{i}}, \mathrm{p}_{\mathrm{n} 1}, \mathrm{p}_{\mathrm{n} 2}\right\}$. We further define the equilateral triangular configuration, denote by $\mathbb{E}_{i}$, as the configuration that all distances between any two of $p_{i}$, $\mathrm{p}_{\mathrm{n} 1}$ and $\mathrm{p}_{\mathrm{n} 2}$ of $\mathbb{T}_{\mathrm{i}}$ are equal to $\mathrm{d}_{\mathrm{u}}$.

### 3.2 Problem definition

It is known that the local geometric shape of schools of tuna represents a diamond shape (Stocker, 1999), whereby tuna exhibit their adaptive behavior while maintaining the local shape. Similarly, the local interaction in this work is to generate $\mathbb{E}_{i}$ from $\mathbb{T}_{\mathrm{i}}$. Formally, the local interaction is to have $r_{i}$ maintain $d_{u}$ with $N_{i}$ at each time toward forming $\mathbb{R}_{i}$. Now, we can
address the coordination problem of adaptive navigation of robot swarms based on the local interaction as follows:
Given $r_{1}, \cdots, r_{n}$ located at arbitrarily distinct positions, how to enable the robots to autonomously travel through unknown territories using only local information in order to reach a destination?
It is assumed that the unknown environment to be navigated by a swarm of robots includes obstacles and dead-end passageways. Next, we advocate that adaptive flocking can be achieved by solving the following four constituent sub-problems.

- Problem-1(Maintenance): Given robots located at arbitrarily distinct positions, how to enable them to navigate with $\mathbb{E}_{\mathrm{i}}$.
- Problem-2(Partition): Given that an obstacle is detected, how to enable a swarm to split into multiple smaller swarms to avoid the obstacle.
- Problem-3(Unification): Given that multiple swarms exist in close proximity, how to enable them to merge into a single swarm.
- Problem-4(Escape): Given some robots trapped in a dead-end passageway, how to enable them to escape from the area.


## 4. Geometric local interaction scheme

This section explains the local interaction among three neighboring robots. As presented in ALGORITHM-1, the algorithm consists of a function $\varphi_{\text {interaction }}$ whose arguments are $p_{i}$ and $\mathrm{N}_{\mathrm{i}}$ at each activation.

```
constant }\mp@subsup{d}{u}{}:=\mathrm{ uniform distance
FUNCTION }\mp@subsup{\varphi}{\mathrm{ interaction ( }{\mp@subsup{p}{n1}{},\mp@subsup{p}{n2}{}},\mp@subsup{p}{i}{})}{\mathrm{ )}
1(poc, 的,y) := centroid (p
2 }\phi:=\mp@code{angle between \overline{pmp pr2 and r's local horizontal axis}
3 p}\mp@subsup{p}{0,s}{}:=\mp@subsup{p}{0,s}{}+\mp@subsup{d}{u}{}\operatorname{cos}(\phi+\pi/2)/\sqrt{}{3
```



```
5 p\mp@subsup{p}{0t}{\prime}:= (p
```

Algorithm 1. Local Interaction (code executed by the robot $r_{i}$ at point $p_{i}$ )


Fig. 3. Illustration of the local interaction algorithm

### 4.1 Local interaction algorithm

Let's consider a robot $r_{i}$ and its two neighbors $r_{n 1}$ and $r_{n 2}$ located within $r_{i}{ }^{\prime} s$ SB. As shown in Fig. 3, three robots are configured into $\mathbb{T}_{i}$ whose vertices are $p_{i}, p_{n 1}$ and $p_{n 2}$, respectively.

First, $r_{i}$ finds the centroid of the triangle $\Delta p_{i} p_{n 1} p_{n 2}$, denoted by $p_{c t}$, with respect to its local coordinate system, and measures the angle $\phi$ between the line $\overline{\mathrm{p}_{\mathrm{n} 1} \mathrm{p}_{\mathrm{n} 2}}$ connecting the neighbors and $\vec{r}_{x, i}$ ( $r_{i}^{\prime}$ s horizontal axis). Using $p_{c t}$ and $\phi, r_{i}$ calculates the next movement point $\mathrm{p}_{\mathrm{ti}}$. Each robot computes $\mathrm{p}_{\mathrm{ti}}$ by its current observation of neighboring robots. Intuitively, under ALGORITHM-1, $\mathrm{r}_{\mathrm{i}}$ may maintain $\mathrm{d}_{\mathrm{u}}$ with its two neighbors at each time. In other words, each robot attempts to form an isosceles triangle for $N_{i}$ at each time, and by repeatedly running ALGORITHM-1, three robots configure themselves into $\mathbb{E}_{\mathrm{i}}$ (Lee \& Chong, 2009).

### 4.2 Motion control

As illustrated in Fig. 4-(b), let's consider the circumscribed circle of an equilateral triangle whose center is $p_{c t}$ of $\Delta p_{i} p_{n 1} p_{n 2}$ and radius $d_{r}$ is $d_{u} / \sqrt{3}$. Under the local interaction, the positions of each robot are determined by controlling the distance $\mathrm{d}_{\mathrm{i}}$ from $\mathrm{p}_{\mathrm{ct}}$ and the internal angle $\alpha_{\mathrm{i}}$ (see Fig. 4-(a)). First, the distance is controlled by the following equation

$$
\begin{equation*}
\dot{d}_{\mathrm{i}}(\mathrm{t})=-\mathrm{a}\left(\mathrm{~d}_{\mathrm{i}}(\mathrm{t})-\mathrm{d}_{\mathrm{r}}\right), \tag{1}
\end{equation*}
$$

Where $a$ is a positive constant. Indeed, the solution of (1) is $d_{i}(t)=\left|d_{i}(0)\right| e^{-a t}+d_{r}$ that converges exponentially to $d_{r}$ as $t$ approaches infinity. Secondly, the internal angle is controlled by the following equation

$$
\begin{equation*}
\dot{\alpha}_{\mathrm{i}}(\mathrm{t})=\mathrm{k}\left(\beta_{\mathrm{i}}(\mathrm{t})-\gamma_{\mathrm{i}}(\mathrm{t})-2 \alpha_{\mathrm{i}}(\mathrm{t})\right), \tag{2}
\end{equation*}
$$


(a) control parameters range $\mathrm{d}_{\mathrm{i}}$ and bearing $\alpha_{i}$

(b) desired equilateral triangle $\mathbb{E}_{i}$

Fig. 4. Two control parameter of local interaction
where k is a positive number. Because the total internal angle of a triangle is $180^{\circ}$, (2) can be rewritten as

$$
\begin{equation*}
\dot{\alpha}_{\mathrm{i}}(\mathrm{t})=\mathrm{k}^{\prime}\left(60^{\circ}-\alpha_{\mathrm{i}}(\mathrm{t})\right), \tag{3}
\end{equation*}
$$

where $\mathrm{k}^{\prime}$ is 3 k . Likewise, the solution of (3) is $\alpha_{i}(\mathrm{t})=\left|\alpha_{\mathrm{i}}(0)\right| \mathrm{e}^{-\mathrm{k}^{\prime} \mathrm{t}}+60^{\circ}$ that converges exponentially to $60^{\circ}$ as $t$ approaches infinity.
Note that (1) and (3) imply that the trajectory of $\mathrm{r}_{\mathrm{i}}$ converges to $\mathrm{d}_{\mathrm{r}}$ and $60^{\circ}$, an equilibrium state as termed $\left[\begin{array}{ll}d_{r} & 60^{\circ}\end{array}\right]^{\mathrm{T}}$ shown in Fig. 4-(b). This also implies that three robots eventually
form $\mathbb{E}_{\mathrm{i}}$. In order to prove the convergence of the local interaction, we apply Lyapunov's stability theory (Slotine \& Li, 1991). Lyapunov's stability theorem states that if there exists a scalar function $\mathrm{v}(\mathrm{x})$ of the state x with continuous first order derivatives such that $\mathrm{v}(\mathrm{x})$ is positive definite, $\mathrm{v}^{\prime}(\mathrm{x})$ is negative definite, and $\mathrm{v}(\mathrm{x}) \rightarrow \infty$ as $\|\mathrm{x}\| \rightarrow \infty$, then the equilibrium at the origin is asymptotically stable. Now, the desired configuration can be regarded as one that minimizes the energy level of a Lyapunov function.
Consider the following scalar function of the state $\mathrm{x}=\left[\mathrm{d}_{\mathrm{i}}(\mathrm{t}) \quad \alpha_{\mathrm{i}}(\mathrm{t})\right]^{\mathrm{T}}$ with continuous first order derivatives:

$$
\begin{equation*}
\mathrm{f}_{\mathrm{l}, \mathrm{i}}=\frac{1}{2}\left(\mathrm{~d}_{\mathrm{i}}-\mathrm{d}_{\mathrm{r}}\right)^{2}+\frac{1}{2}\left(60^{\circ}-\alpha_{\mathrm{i}}\right)^{2} . \tag{4}
\end{equation*}
$$

This scalar function is always positive definite except $\mathrm{d}_{\mathrm{i}} \neq \mathrm{d}_{\mathrm{r}}$ and $\alpha_{\mathrm{i}} \neq 60$. The derivative of the scalar function is given by

$$
\begin{equation*}
\dot{\mathrm{f}}_{\mathrm{l}, \mathrm{i}}=-\left(\mathrm{d}_{\mathrm{i}}-\mathrm{d}_{\mathrm{r}}\right)^{2}-\left(60^{\circ}-\alpha_{\mathrm{i}}\right)^{2} \tag{5}
\end{equation*}
$$

which is obtained by differentiating $f_{l, i}$ to substitute for $\dot{d}_{i}$ and $\dot{\alpha}_{i}$. It is evident that (5) is negative definite and the scalar function $\mathrm{f}_{\mathrm{l}, \mathrm{i}}$ is radially unbounded since it tends to infinity as $\|x\| \rightarrow \infty$. Therefore, the equilibrium state is asymptotically stable, implying that $r_{i}$ reaches a vertex of $\mathbb{E}_{i}$. Further details on the convergence proof are given in (Lee \& Chong, 2009).


Fig. 5. Adaptive navigation algorithm flowchart

## 5. Adaptive navigation algorithm

As illustrated in Fig. 5, the input to the adaptive navigation algorithm at each time is $\mathrm{O}_{\mathrm{i}}$ and the arena border detected with respect to $r_{i}{ }^{\prime} s$ local coordinate system, and the output is $r_{i}{ }^{\prime} s$ next movement position. When $r_{i}$ observes the arena within its SB, depending on whether or not it can move forward, it either executes the partition function to avoid the obstacle or the escape function to break a stalemate. When $\mathrm{r}_{\mathrm{i}}$ faces no arena border but observes other
swarms, it executes the unification function. Otherwise, it basically performs the maintenance function to navigate toward a goal.

```
Function }\mp@subsup{\varphi}{\mathrm{ rrsel }}{}(\mp@subsup{O}{1,}{\prime},\mp@subsup{p}{i}{}
1 pon := min min (dist(pop)]
```



```
3 Output { {put, pu2}}}=\mp@subsup{N}{i}{}
```


## Algorithm 2. Neighbor Selection -1 (code executed by the robot $r_{i}$ at point $p_{i}$ )

The four functions above should determine two positions $\mathrm{p}_{\mathrm{n} 1}$ and $\mathrm{p}_{\mathrm{n} 2}$ occupied by two neighbors $r_{n 1}$ and $r_{n 2}$. These positions are the input arguments of ALGORITHM-1. Before explaining the four functions as individual solutions of each sub-problem, we introduce the neighbor selection algorithm commonly used in the four functions, enabling $r_{i}$ to select its neighbor robots. To form $\mathbb{T}_{\mathrm{i}}$, the first neighbor $\mathrm{r}_{\mathrm{n} 1}$ is selected as the one located the shortest distance away from $r_{i}$ as shown in Fig. 6-(a). When there exist two or more candidates $r_{n 1_{m}}$ and $r_{n 1_{n}}$ for $r_{n 1}, r_{i}$ arranges their positions $\mathrm{p}_{\mathrm{n} 1_{m}}=\left(\mathrm{x}_{\mathrm{n} 1_{\mathrm{m}}}, \mathrm{y}_{\mathrm{n} 1_{\mathrm{m}}}\right)$ and $\mathrm{p}_{\mathrm{n} 1_{\mathrm{n}}}=\left(\mathrm{x}_{\mathrm{n} 1_{\mathrm{n}}}, y_{n 1_{\mathrm{n}}}\right)$ with respect to $r_{i}$ 's local coordinate system. Then, $r_{i}$ uniquely determines its $r_{s 1}$ by sorting their positions in the following increasing order with respect to its local coordinate system: if $\left(\mathrm{p}_{\mathrm{n} 1_{\mathrm{m}}}<\mathrm{p}_{\mathrm{n} 1_{\mathrm{n}}}\right) \Leftrightarrow\left[\left(\mathrm{y}_{\mathrm{n} 1_{\mathrm{m}}}<\mathrm{y}_{\mathrm{n} 1_{\mathrm{n}}}\right) \vee\left\{\left(\mathrm{y}_{\mathrm{n} 1_{\mathrm{m}}}=\mathrm{y}_{\mathrm{n} 1_{\mathrm{n}}}\right) \wedge\left(\mathrm{x}_{\mathrm{n} 1_{\mathrm{m}}}<\mathrm{x}_{\mathrm{n} 1_{\mathrm{n}}}\right)\right\}\right]$ where the logic symbols $\vee$ and $\wedge$ indicate the logical conjunction and the logical disjunction, respectively. As presented in Fig. 6-(b), the second neighbor $r_{n 2}$ is selected such that the length of $\mathbb{T}_{i}$ 's perimeter is minimized as follows: $\min \left[\operatorname{dist}\left(\mathrm{p}_{\mathrm{n} 1}, \mathrm{p}_{\mathrm{n} 2}\right)+\operatorname{dist}\left(\mathrm{p}_{\mathrm{n} 2}, \mathrm{p}_{\mathrm{i}}\right)\right]$. In particular, when both $\mathrm{r}_{\mathrm{i}}$ and the neighbors are all aligned, if there are three or more robots in $\mathrm{O}_{\mathrm{i}}, \mathrm{r}_{\mathrm{n} 2}$ is re-selected such that $\mathrm{r}_{\mathrm{i}}$ is not located on the same line. Under ALGORITHM-2, $r_{i}$ is able to select its neighbors and then form $\mathbb{T}_{\mathrm{i}}$. Notice that the currently selected neighbors do not coincide with ones at the next time due to the assumption of anonymity. Using the current $O_{i}$ by $r_{i}, \mathbb{T}_{i}$ is newly formed at each time.


Fig. 6. Illustration of the neighbour selection algorithm

### 5.1 Maintenance function

The first problem is how to maintain $\mathbb{E}_{i}$ with neighboring robots while navigating. As shown in Fig. 7-(a), $r_{i}$ adjusts its traveling direction $\vec{T}_{i}$ with respect to its local coordinate system and
computes $O_{i}$ at the time $t$. By rotating $\vec{T}_{i} 90$ degrees clockwise and counterclockwise, respectively, two vectors $\vec{T}_{i, c}$ and $\vec{T}_{i, a}$ are defined. Within $r_{i}{ }^{\prime} s S B$, an area of traveling direction $\mathrm{A}\left(\overrightarrow{\mathrm{T}}_{\mathrm{i}}\right)$ is defined as the area between $\overrightarrow{\mathrm{T}}_{\mathrm{i}, \mathrm{c}}$ and $\overrightarrow{\mathrm{T}}_{\mathrm{i}, \mathrm{a}}$ as illustrated in Fig. 7-(b). Under ALGORITHM-2, $r_{i}$ checks whether there exists a neighbor in $A\left(\vec{T}_{i}\right)$. If any robots exist within $A\left(\vec{T}_{i}\right)$, $r_{i}$ selects the first neighbor $r_{n 1}$ and defines its position $p_{n 1}$. Otherwise, $r_{i}$ spots a virtual point $p_{v}$ located some distance $d_{v}$ away from $p_{i}$ along $A\left(\vec{T}_{i}\right)$, which gives $p_{n 1}$. After determining $p_{n 1}, r_{n 2}$ is selected and its position $p_{n 2}$ is defined.

(a) traveling direction $\vec{T}_{i}$

(b) maintenance area $\mathrm{A}\left(\overrightarrow{\mathrm{T}}_{\mathrm{i}}\right)$

Fig. 7. Illustration of the maintenance function

### 5.2 Partition function



Fig. 8. Illustration of the partition function
When $r_{i}$ detects an obstacle that blocks its way to the destination, it is required to modify the direction toward the destination avoiding the obstacle. In this work, $r_{i}$ determines its direction by using the relative degree of attraction of individual passageways $s_{j}$, termed the favorite vector $\vec{f}_{j}$, whose magnitude is given:

$$
\begin{equation*}
\left|\overrightarrow{\mathrm{f}}_{\mathrm{j}}\right|=\left|\frac{\mathrm{w}_{\mathrm{j}}}{\mathrm{~d}_{\mathrm{j}}^{2}}\right| \tag{6}
\end{equation*}
$$

where $w_{j}$ and $d_{j}$ denote the width of $s_{j}$ and the distance between the center of $w_{j}$ and $p_{i}$, respectively. Note that if $r_{i}$ can not exactly measure $w_{j}$ beyond its $S B, w_{j}$ may be shortened. Now, $s_{j}$ can be represented by a set of favorite vectors $\left\{\vec{f}_{\mathrm{j}} \mid 1 \leq \mathrm{j} \leq \mathrm{m}\right\}$, and then $\mathrm{r}_{\mathrm{i}}$ selects the maximum magnitude of $\vec{f}_{j}$, denoted as $\left|\vec{f}_{j}\right|_{\text {max }}$. Similar to defining $A\left(\vec{T}_{i}\right)$ above, $r_{i}$ defines a maximum favorite area $A\left(\vec{f}_{\text {jmax }}\right)$ based on the direction of $\left|\vec{f}_{j}\right|_{\text {max }}$ within its SB. If neighbors are found in $A\left(\vec{f}_{j \text { max }}\right), r_{i}$ selects $r_{n 1}$ to define $p_{n 1}$. Otherwise, $r_{i}$ spots a virtual point $p_{v}$ located at $d_{v}$ in the direction of $\left|\vec{f}_{j}\right|_{\max }$ to define $p_{n 1}$. Finally, $r_{n 2}$ and its $r_{n 2}$ are determined under ALGORITHM-2.

### 5.3 Unification function

In order to enable multiple swarms in close proximity to merge into a single swarm, $\mathrm{r}_{\mathrm{i}}$ adjusts $\vec{T}_{i}$ with respect to its local coordinate system and defines the position set of robots $D_{u}$ located within the range of $d_{u} . r_{i}$ computes ang $\left(\vec{T}_{i}, \overrightarrow{p_{i} p_{u}}\right)$, where $\overrightarrow{p_{i} p_{u}}$ is the vector starting from $p_{i}$ to a neighboring point $p_{u}$ in $D_{u}$, and defines a neighbor point $p_{\text {ref }}$ that gives the minimum ang $\left(\vec{T}_{i}, \overrightarrow{p_{i} p_{u}}\right)$ between $\vec{T}_{i}$ and $\overrightarrow{p_{i} p_{u}}$. If there exists $p_{u l}, r_{i}$ finds another neighbor point $p_{u m}$ using the same method starting from $\overrightarrow{p_{i} p_{u l}}$. Unless $p_{u l}$ exists, $r_{i}$ defines $p_{\text {ref }}$ as $p_{r n}$. Similarly, $r_{i}$ can decide a specific neighbor point $p_{\ln }$ while rotating 60 degrees counterclockwise from $\overrightarrow{\mathrm{p}_{i} \mathrm{p}_{\mathrm{ref}}}$. The two points, denoted as $\mathrm{p}_{\mathrm{rn}}$ and $\mathrm{p}_{\mathrm{ln}}$, are located at the farthest point in the right-hand or left-hand direction of $\overrightarrow{p_{i} p_{u}}$, respectively. Next, a unification area $A\left(U_{i}\right)$ is defined as the common area between $A\left(\vec{T}_{i}\right)$ in SB and the rest of the area in SB, where no element of $D_{u}$ exists. Then, $r_{i}$ defines a set of robots in $A\left(U_{i}\right)$ and selects the first neighbor $r_{n 1}$. In particular, the second neighbor position $p_{n 2}$ is defined such that the total distance from $p_{n 1}$ to $p_{i}$ can be minimized only through either $p_{r n}$ or $p_{\ln }$.


Fig. 9. Illustration of the unification function

### 5.4 Escape control

When $r_{i}$ detects an arena border within its SB as shown in Fig. 10-(a), it checks whether $\mathbb{T}_{i}$ is equal to $\mathbb{E}_{i}$. Neighboring robots should always be kept $d_{u}$ distance from $r_{i}$. Moreover, $r_{i}{ }^{\prime} s$ current position $p_{i}$ and its next movement position $p_{t i}$ remain unchanged for several time steps, $r_{i}$ will find itself trapped in a dead-end passageway. $r_{i}$ then attempts to find new neighbors within the area $A\left(E_{i}\right)$ to break the stalemate. Similar to the unification function, $r_{i}$ adjusts $\vec{T}_{i}$ with respect to its local coordinate system and defines the position set of robots $D_{e}$ located within SB. As shown in Fig. 10-(b), $r_{i}$ computes ang $\left(\overrightarrow{T_{i}}, \overrightarrow{p_{i} p_{e}}\right)$, where $\overrightarrow{p_{i} p_{u}}$ is the vector starting from $p_{i}$ to a neighboring point $p_{e}$ in $D_{e}$, and defines a neighbor point $r_{r e f}$ that gives the minimum ang $\left(\overrightarrow{\mathrm{T}}_{\mathrm{i}}, \overrightarrow{\mathrm{p}_{\mathrm{i}} \mathrm{p}_{\mathrm{e}}}\right)$ between $\overrightarrow{\mathrm{T}}_{\mathrm{i}}$ and $\overrightarrow{\mathrm{p}_{\mathrm{i}} \mathrm{p}_{\mathrm{u}}}$. While rotating 60 degrees clockwise and counterclockwise from $\overrightarrow{\mathrm{p}_{\mathrm{i}} \mathrm{p}_{\text {ref }}}$, respectively, $\mathrm{r}_{\mathrm{i}}$ can decide the specific neighbor points $\mathrm{p}_{\mathrm{ln}}$ and $p_{r n}$. Employing $p_{l n}$ and $p_{r n}$, the escape area $A\left(E_{i}\right)$ is defined. Then, $r_{i}$ adjusts a set of robots in $A\left(E_{i}\right)$ and selects the first neighbor $r_{n 1}$. In particular, the second neighbor position $p_{n 2}$ is determined under ALGORITHM-2.


Fig. 10. Illustration of the escape function

## 6. Simulation results and discussion

This section describes simulation results that tested the validity of our proposed adaptive navigation scheme. We consider that a swarm of robots attempts to navigate toward a stationary goal while exploring and adapting to unknown environmental conditions. In such an application scenario, the goal is assumed to be either a light or odor source that can only be detected by a limited number of robots. As mentioned in Section 3, the coordinated navigation is achieved without using any leader, identifiers, global coordinate system, and explicit communication. We set the range of SB to 2.5 times longer than $d_{u}$.
The first simulation demonstrates how a swarm of robots adaptively navigates in an environment populated with obstacles and dead-end passageway. In Fig. 11, the swarm navigates toward the goal located on the right hand side. On the way to the goal, some of the robots detect a triangular obstacle that forces the swarm split into two groups from 7 sec (Fig. 11-(c)). The rest of the robots that could not identify the obstacle just follow their neighbors moving ahead. After being split into two groups at 14 sec (Fig. 11-(d)), each group maintains their local geometric configuration while navigating. At 18 sec (Fig. 11-(e)), some
robots happen to enter a dead-end passageway. After they find themselves trapped, they attempt to escape from the passageway by just merging themselves into a neighboring group from 22 sec to 32 sec (from Figs. 11-(f)) to (k)). After 32 sec (Fig. 11-(k)), simulation result shows that two groups merge again completely. At 38 sec (Fig. 11-(l)), the robots successfully pass through the obstacles.


Fig. 11. Simulation results of adaptive flocking toward a stationary goal ((a) $0 \mathrm{sec},(\mathrm{b}) 4 \mathrm{sec}$, (c) $7 \mathrm{sec},(\mathrm{d}) 14 \mathrm{sec},(\mathrm{e}) 18 \mathrm{sec},(\mathrm{f}) 22 \mathrm{sec},(\mathrm{g}) 23 \mathrm{sec},(\mathrm{h}) 24 \mathrm{sec},(\mathrm{i}) 28 \mathrm{sec},(\mathrm{j}) 29 \mathrm{sec},(\mathrm{k}) 32 \mathrm{sec},(\mathrm{l}) 38 \mathrm{sec})$

Fig. 12 shows the trajectories of individual robots in Fig. 11. We could confirm that the swarm was split into two groups due to the triangular obstacle located at coordinates $(0,0)$. If we take a close look at Figs. 11-(f) through (j) (from 22 sec to 29 sec ), the trapped ones escaped from the dead-end passageway located at coordinates ( $x, 200$ ). More important, after passing through the obstacles, all robots position themselves from each other at the desired interval $d_{u}$.


Fig. 12. Robot trajectory results for the simulation in Fig. 11
Next, the proposed adaptive navigation is evaluated in a more complicated environmental condition as presented in Fig. 13. On the way to the goal, some of the robots detect a rectangular obstacle that forces the swarm split into two groups in Fig. 13-(b). After passing through the obstacle in Fig. 13-(d), the lower group encounters another obstacle in Fig. 13(e), and split again into two smaller groups in Fig. 13-(g). Although several robots are trapped in a dead-end passageway, their local motions can enable them to escape from the dead-end passageway in Fig. 13-(i). This self-escape capability is expected to be usefully exploited for autonomous search and exploration tasks in disaster areas where robots have to remain connected to their ad hoc network. Finally, for a comparison of the adaptive navigation characteristics, three kinds of simulations are performed as shown in Figs. 14 through 16. All the simulation conditions are kept the same such as $d u$, the number of robots, and initial distribution. Fig. 14 shows the behavior of mobile robot swarms without the partition and escape functions. Here, a considerable number of robots are trapped in the dead-end passageway and other robots pass through an opening between the obstacle and the passageway by chance. As compared with Fig. 14, Fig. 15 shows more robots pass through the obstacles using the partition function. However, a certain number of robots remain trapped in the dead-end passageway because they have no self-escape function. Fig.

16 shows that all robots successfully pass through the obstacles using the proposed adaptive navigation scheme. It is evident that the partition and escape functions will provide swarms of robots with a simple yet efficient navigation method. In particular, self-escape is one of the most essential capabilities to complete tasks in obstacle-cluttered environments that require a sufficient number of simple robots.


Fig. 13. Simulation results of adaptive flocking toward a stationary goal ((a)0 sec,(b) 8 sec , (c) $10 \mathrm{sec},(\mathrm{d}) 14 \mathrm{sec},(\mathrm{e}) 18 \mathrm{sec},(\mathrm{f}) 22 \mathrm{sec},(\mathrm{g}) 25 \mathrm{sec},(\mathrm{h}) 27 \mathrm{sec},(\mathrm{i}) 31 \mathrm{sec},(\mathrm{j}) 36)$


Fig. 14. Simulation results for flocking without partition and escape functions


Fig. 15. Simulation results for flocking with only partition function


Fig. 16. Simulation results for flocking with the partition and escape functions

## 7. Conclusions

This paper was devoted to developing a new and general coordinated adaptive navigation scheme for large-scale mobile robot swarms adapting to geographically constrained environments. Our distributed solution approach was built on the following assumptions: anonymity, disagreement on common coordinate systems, no pre-selected leader, and no direct communication. The proposed adaptive navigation was largely composed of four functions, commonly relying on dynamic neighbor selection and local interaction. When each robot found itself what situation it was in, individual appropriate ranges for neighbor selection were defined within its limited sensing boundary and the robots properly selected their neighbors in the limited range. Through local interactions with the neighbors, each robot could maintain a uniform distance to its neighbors, and adapt their direction of heading and geometric shape. More specifically, under the proposed adaptive navigation, a group of robots could be trapped in a dead-end passage, but they merge with an adjacent group to emergently escape from the dead-end passage. Furthermore, we verified the effectiveness of the proposed strategy using our in-house simulator. The simulation results clearly demonstrated that the proposed algorithm is a simple yet robust approach to autonomous navigation of robot swarms in highlycluttered environments. Since our algorithm is local and completely scalable to any size, it is easily implementable on a wide variety of resource-constrained mobile robots and platforms. Our adaptive navigation control for mobile robot swarms is expected to be used in many applications ranging from examination and assessment of hazardous environments to domestic applications.

## 8. References

Balch, T. \& Hybinette, M. (2000). Social potentials for scalable multi-robot formations, Proc. IEEE Int. Conf. Robotics and Automation, pp. 73-80, IEEE
Correll, N., Bachrach, J., Vickery, D., \& Rus, D. (2009). Ad-hoc wireless network coverage with networked robots that cannot localize, Proc. IEEE Int. Conf. Robotics and Automation, pp. 3878-3885, IEEE
Esposito, J. M. \& Dunbar, T. W. (2006). Maintaining wireless connectivity constraints for swarms in the presence of obstacles, Proc. IEEE Int. Conf. Robotics and Automation, pp. 946-951, IEEE
Folino, G. \& Spezzano, G. (2002). An adaptive flocking algorithm for spatial clustering, In: Parallel Problem Solving from Nature (LNCS), Yao, X., Burke, E., Lozano, J. A., Smith, J., Merelo-Guervos, J. J., Bullinaria, J. A., Rowe, J., Tino, P., Kaban, A., \& Schwefel, H.-P. (Ed.), Vol. 2439, 924-933, Springer Berlin, ISBN: 978-3-540-23092-2

Fowler, T. (2001). Mesh networks for broadband access, IEE Review, Vol. 47, No. 1, 17-22
Gu, D. \& Hu, H. (2010). Distributed minmax filter for tracking and flocking, Proc. IEEE/RSJ Int. Conf. Intelligent Robots and Systems, pp. 3562-3567, IEEE
Ikemoto, Y., Hasegawa, Y., Fukuda, T., \& Matsuda, K. (2005). Graduated spatial pattern formation of robot group, Information Science, Vol. 171, No. 4, 431-445
Lam, M. \& Liu, Y. (2006). ISOGIRD: an efficient algorithm for coverage enhancement in mobile sensor networks, Proc. IEEE/RSJ Int. Conf. Intelligent Robots and Systems, pp. 1458-1463, IEEE
Lee, G. \& Chong, N. Y. (2009). A geometric approach to deploying robot swarms, Annals of Mathematics and Artificial Intelligence, Vol. 52, No. 2 - 4, 257-280
Lee, G. \& Chong, N. Y. (2009-b). Decentralized formation control for small-scale robot teams with anonymity, Mechatronics, Vol. 19, No. 1, 85-105
Lee, G. \& Chong, N. Y. (2008). Adaptive flocking of robot swarms: algorithms and properties, IEICE Trans. Communications, Vol. E91-B, No. 9, 2848-2855
Lyengar, R., Kar, K., \& Banerjee, S. (2005). Low-coordination topologies for redundancy in sensor networks, Proc. 3rd Acm Int. Sym. Mobile Ad Hoc Networking and Computing, pp. 332-342, ACM
Nembrini, J., Winfield, A., \& Melhuish, C. (2002). Minimalist coherent swarming of wireless networked autonomous mobile robots, Proc. 7th Int. Conf. Simulation of Adaptive Behavior, pp. 373-382, IEEE
Olfati-Saber, R. (2006). Flocking for mult-agnet dynamic systems: algorithms and theory, IEEE Trans. Automatic Control, Vol. 51, No. 3, 401-420
Ogren, P. \& Leonard, N. E. (2005). A convergent dynamic window approach to obstacle avoidance, IEEE Trans. Robotics and Automation, Vol. 21, No. 2, 188-195
Stocker, C. W. (1987). Flocks, herds, and schools: a distributed behavioral model, Computer Graphics, Vol. 21, No. 4, 25-34
Sahin, E. (2005). Swarm robotics: from sources of inspiration to domains of application, In: Swarm Robotics (LNCS), Sahin, E \& Spears, W. M., (Ed.), Vol. 3342, 10-20, Springer Berlin, ISBN: 978-3-540-24296-3
Shucker, B., Murphey, T. D., \& Bennett, J. K. (2008). Convergence-preserving switching for topology-dependent decentralized systems, IEEE Trans. Robotics, Vol. 24, No. 6, 1405-1415

Slotine, J. E. \& Li,W. (1991). Applied nonlinear control, Prentice-Hall, ISBN: 0-13-040890-5
Spears, D., Kerr, W., \& Spears, W. M. (2006). Physics-based robot swarms for coverage problems, Int. Jour.Intelligent Control and Systems, Vol. 11, No. 3, 124-140
Spears, W. M., Spears, D., Hamann, J., \& Heil, R. (2004). Distributed, physics-based control of swarms of vehicles, Autonomous Robots, Vol. 17, No. 2 -3, 137-162
Stocker, S. (1999). Models for tuna school formation, Mathematical Biosciences, Vol. 156, No. 1-2, 167-190
Wilson, E. O. (1976). Sociobiology: the new synthesis, Harvard University Press, ISBN: 0-674-00089-7
Yicka, J., Mukherjeea, B., \& Ghosal, D. (2008). Wireless sensor network survey, Computer Networks, Vol. 52, No. 12, 2292-2330
Zarzhitsky, D., Spears, D., \& Spears, W. M. (2005). Distributed robotics approach to chemical plume tracing, Proc. IEEE/RSJ Int. Conf. Intelligent Robots and Systems, pp. 4034-4039, IEEE


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Robot navigation includes different interrelated activities such as perception－obtaining and interpreting sensory information；exploration－the strategy that guides the robot to select the next direction to go；mapping －the construction of a spatial representation by using the sensory information perceived；localization－the strategy to estimate the robot position within the spatial map；path planning－the strategy to find a path towards a goal location being optimal or not；and path execution，where motor actions are determined and adapted to environmental changes．This book integrates results from the research work of authors all over the world，addressing the abovementioned activities and analyzing the critical implications of dealing with dynamic environments．Different solutions providing adaptive navigation are taken from nature inspiration，and diverse applications are described in the context of an important field of study：social robotics．

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