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Optimized FFT Algorithm and its Application to Fast GPS Signal Acquisition

Lin Zhao, Shuaihe Gao, Jicheng Ding and Lishu Guo
*College of Automation,
Harbin Engineering University
China*

1. Introduction

The essence of GPS signal acquisition is a two-dimensional search process for the carrier Doppler and code phase, generally including correlator, signal capture device, and logic control module. The disposal efficiency of correlator would affect the capture speed of the whole acquisition process. Because of the corresponding relation between frequency-domain multiplication and time-domain convolution, the Discrete Fourier Transform (DFT) could be applied to play the role of the correlator, which is suitable to implement for computers (Akopian, 2005) (Van Nee & Coenen, 1991).

However, with the performance requirements of GPS receivers increasing, especially in the cold start and the long code acquisition, such as P code, the acquisition time should be furtherly reduced. Therefore, the fast discrete Fourier transform processing approach, that is, Fast Fourier Transform (FFT), is described, including radix-2, radix-4, split-radix algorithm, Winograd Fourier Transform Algorithm (WFTA) which is suitable for a small number of treatment points, and Prime Factor Algorithm (PFA) in which the treatment points should be the product of some prime factors.

According to the actual needs of GPS signal acquisition, an optimized FFT algorithm was put forward, which comprehensively utilize the advantages of different FFT algorithms. Applying optimized FFT algorithm to GPS signal acquisition, the results of simulations indicate that the improved processing could reduce the acquisition time significantly and improve the performance of GPS baseband processing.

2. Analysis on GPS signal acquisition

2.1 Basic characteristics of GPS L1 signal

There are three basic components in GPS signal: carrier waves, pseudo-random numbers (PRN) codes and navigation message (D code). Among them, the carrier waves are located at the L-band, including L1-band (1575.42MHz) which is with the most common application, L2-band (1227.6MHz) and L5-band (1176.45MHz). There are two basic types of PRN codes, the coarse/ acquisition (C/ A) code and the precise (P) code. The simplified structure of GPS L1 signal is shown in Fig. 1. The frequency of carrier wave is 1575.42MHz. The code rate of C/ A code and P code are 1.023MHz and 10.23MHz respectively. The data rate of D code is 50Hz.

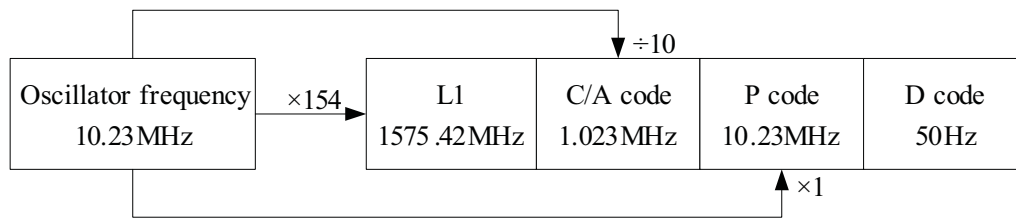


Fig. 1. The simplified structure of GPS L1 signal

C/A code is used to achieve spread spectrum of D code. Compound code $C/A \oplus D$ could be gained when the D code is spreading, and the code frequency is extended to 1.023MHz. Compound code $P \oplus D$ could be gained when the P code is spreading, and the code frequency is extended to 10.23MHz. And then multiply the spread spectrum signal with the L1 carrier wave to complete the modulation. Quaternary phase shift keying (QPSK) is applied in the modulation of L1 signal, where the in-phase carrier component $\cos(2\pi f_{L1}t + \theta_{L1})$ is modulated with compound code $C/A \oplus D$, and the orthogonal carrier components $\sin(2\pi f_{L1}t + \theta_{L1})$ is modulated with compound code $P \oplus D$, so the L1 signal transmitted by satellites could be expressed as:

$$s_{L1}(t) = \sqrt{2P_x}D(t)x(t) \cos(2\pi f_{L1}t + \theta_{L1}) + \sqrt{2P_y}D(t)y(t) \sin(2\pi f_{L1}t + \theta_{L1}) \quad (1)$$

Where P_x and P_y are powers of different signal components respectively, $D(t)$, $x(t)$ and $y(t)$ are D code, C/A code and P code of satellite respectively, f_{L1} is the frequency of carrier wave, and θ_{L1} is the initial phase.

The process of spread spectrum and modulation for GPS transmitted L1 signal could be shown in Fig. 2 (Kaplan, & Hegarty, 2006).

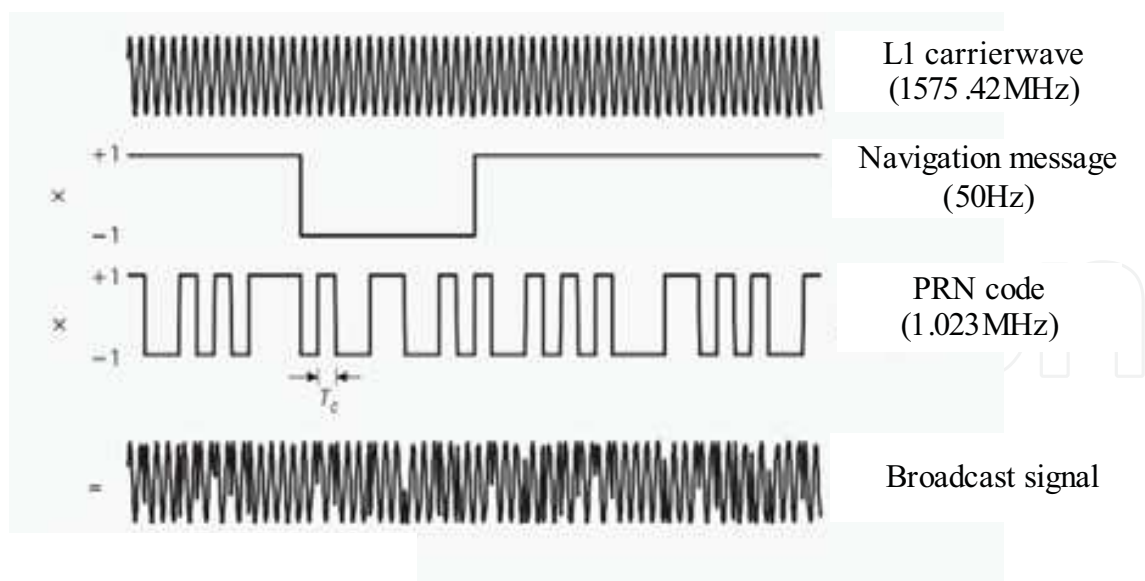


Fig. 2. The spread spectrum and modulation for GPS L1 signal

In fact, P code mainly used for the military, and is not open to civilian use, so the received L1 signal could be simplified to include carrier wave, C/A code and D code in the research of GPS C/A code acquisition.

2.2 Signal acquisition in GPS receiver

The original GPS signal, which is interfered and attenuated in the transmission path, is gained by the receiver antenna. Radio Frequency (RF) front-end completes the frequency conversion and analog-digital conversion for the weak signal, where the high frequency analog signal is transformed into Intermediate Frequency (IF) digital signal which is beneficial to computer processing. The coarse and precision estimates of carrier Doppler frequency shift and PRN code phase are achieved by acquisition and tracking in the baseband processing, and then despreading and then demodulation of navigation message should be completed. Actually it is the opposite process of spreading and modulation mentioned above. Position calculation could be realized by adequate information gained by baseband module (Michael, & Dierendonck, 1999). The workflow of typical GPS software receiver is shown in Fig. 3.

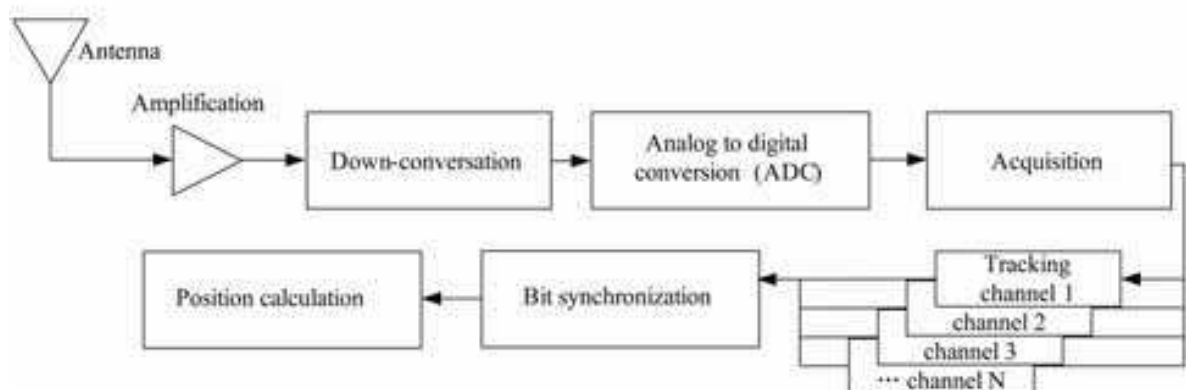


Fig. 3. The workflow of GPS receiver

As a part of baseband signal processing in GPS receiver, the main aim of signal acquisition is to find visible satellites, and estimate their C/ A code phase and carrier Doppler frequency shift respectively. The essence of GPS signal capture is a two-dimensional search process for the carrier Doppler and code phase. The PRN code phase and carrier Doppler frequency could be considered respectively. As shown in Fig. 4, each C/ A code contains 1023 code elements, and search step with one code element would be commonly selected. In high dynamic environment, the Doppler frequency ranges from -10kHz to +10kHz, and 1kHz search step is generally selected.

In the above search process, once the code phase and the carrier Doppler frequency shift generated by local oscillator are close to the receiving code phase and Doppler frequency shift, there will be a correlation peak for the randomness of C/ A code. Generally, the code phase error is less than half a symbol, and the Doppler frequency shift error is within [-500Hz, 500Hz]. At this time, the code phase and carrier Doppler frequency parameters which the peak point corresponds could be the acquisition results, and then the baseband processing enters the second stage, signal tracking.

When the predetermined frequency points are tested one by one in time-domain, the large computation would cause great time-consuming, unless there are a lot of hardware resources as the supplement. Fortunately, we can use another method to get all results the 1023 possible code phases corresponding for each frequency point, which is the acquisition method based on FFT.

3. GPS signal acquisition method based on FFT

Processing speed is constrained in the traditional acquisition method based on time domain, so the acquisition method based on Fourier transform is always used in current software receiver (Li, Zhang, Li, & Zhang, 2008).

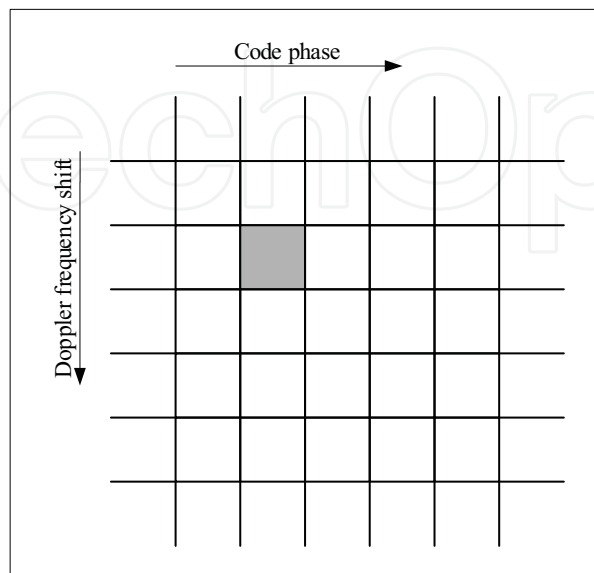


Fig. 4. Two-dimensional search for Doppler frequency shift and C/A code phase

3.1 Corresponding relation between frequency-domain and time-domain

Using circular correlation theory, convert the correlation of received signal and local generated signal in the time-domain to spectrum multiplying in the frequency-domain (Akopian, 2005) (Van Nee & Coenen, 1991). Assumed $c(\tau)$ is the circulating moving local code, N is the number of corresponding sampling points, the output of correlator would be expressed as:

$$y(t) = \sum_{\tau=0}^{N-1} s_{IF}(t)c(t+\tau) \quad (2)$$

Do discrete Fourier transform (DFT) of $y(t)$,

$$Y(k) = \sum_{\tau=0}^{N-1} \sum_{t=0}^{N-1} s_{IF}(t)c(t+\tau)e^{-2\pi jk\tau/N} \quad (3)$$

And then, $Y(k)$ could be transformed to

$$Y(k) = \sum_{t=0}^{N-1} s_{IF}(t) \left(\sum_{\tau=0}^{N-1} c(t+\tau)e^{-2\pi j(t+\tau)k/N} \right) e^{2\pi jtk/N} \quad (4)$$

If $S(k)$ and $C(k)$ are DFT forms of $x(t)$ and $c(\tau)$,

$$Y(k) = C(k) \sum_{t=0}^{N-1} s_{IF}(t)e^{2\pi jtk/N} = C(k) \times S(k)^{-1} \quad (5)$$

As the local code $c(\tau)$ is real signal, the complex conjugates of $S(k)$ and $C(k)$ could be expressed by $S^*(k)$ and $C^*(k)$ respectively. The amplitude output is

$$|Y(k)| = |S^*(k) \times C(k)| = |S(k) \times C^*(k)| \quad (6)$$

According to the correlation of original signal and local code, adjudicate the relevant results. The number of visible satellites, and the estimation of code phase and Doppler frequency shift could be drawn. So the process of signal acquisition based on FFT could be expressed as follows:

$$Y(k) = f_{IFFT}(f_{FFT}(s(k)) \times f_{FFT}^*(c(k))) \quad (7)$$

Where f_{IFFT} is the inverse fast Fourier transform (IFFT) operation, f_{FFT} is the FFT operation, and f_{FFT}^* is the conjugate form of f_{FFT} .

3.2 GPS signal acquisition based on FFT

The signal received by antenna would go through amplification, mixing, filtering, and analog-digital conversion in RF front-end, and its output is the IF digital signal. The local carrier wave numerical controlled oscillator (NCO) would generate two-way mutually orthogonal signal $\sin(\omega t)$ and $\cos(\omega t)$, which would be utilized to multiply the IF digital signal respectively. As shown in Fig. 5, the value of branch I and branch Q are regarded as real part and imaginary part respectively. Construct a new complex sequence with the form of

$$x(n) = I(n) + jQ(n) \quad (8)$$

Do FFT of this new sequence, and do FFT of the local generated C/A codes at the same time. Then complex multiplications are carried out between these two FFT values. After correlation, IFFT operations are carried out for it. Calculate the modulus of IFFT results one by one, and find the maximum value, which is shown in Fig. 6. Comparing the maximum value and the pre-set threshold, if the maximum value is less than the threshold, it means there is no effective signal. But if the maximum value is higher than the threshold, it means the acquisition is successful, and the received signal code phase and Doppler frequency shift would appear in the location of peak.

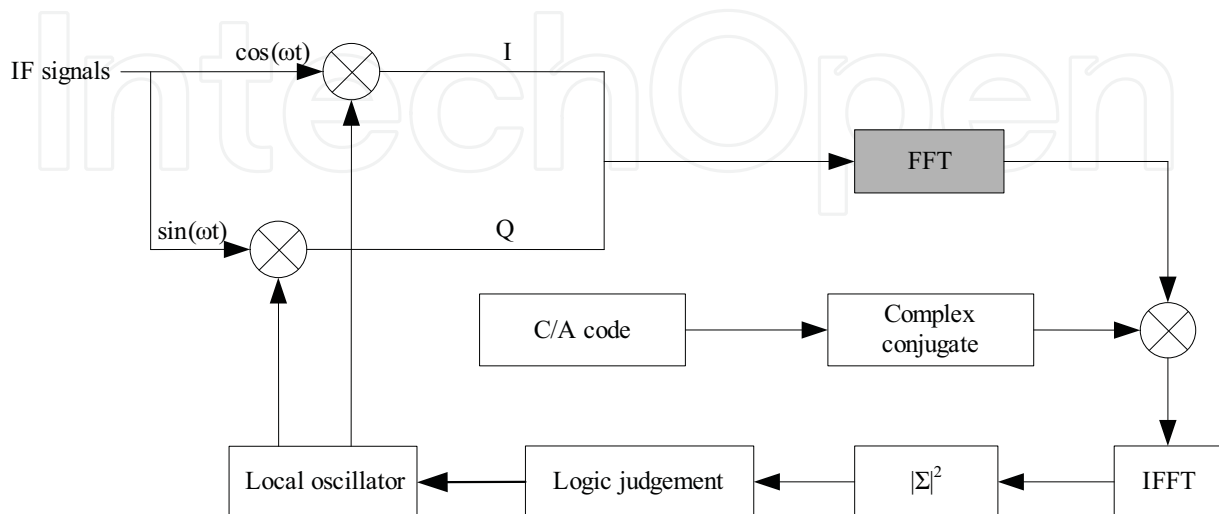


Fig. 5. Signal acquisition process based on FFT

The corresponding C/A code and Doppler phase shift could be obtained in the same time, so it is obviously that the FFT operations play a crucial role in the acquisition, especially in the quick acquisition for high dynamic environments. The efficiency of FFT computation would determine the capture speed and whole performance of the receiver.

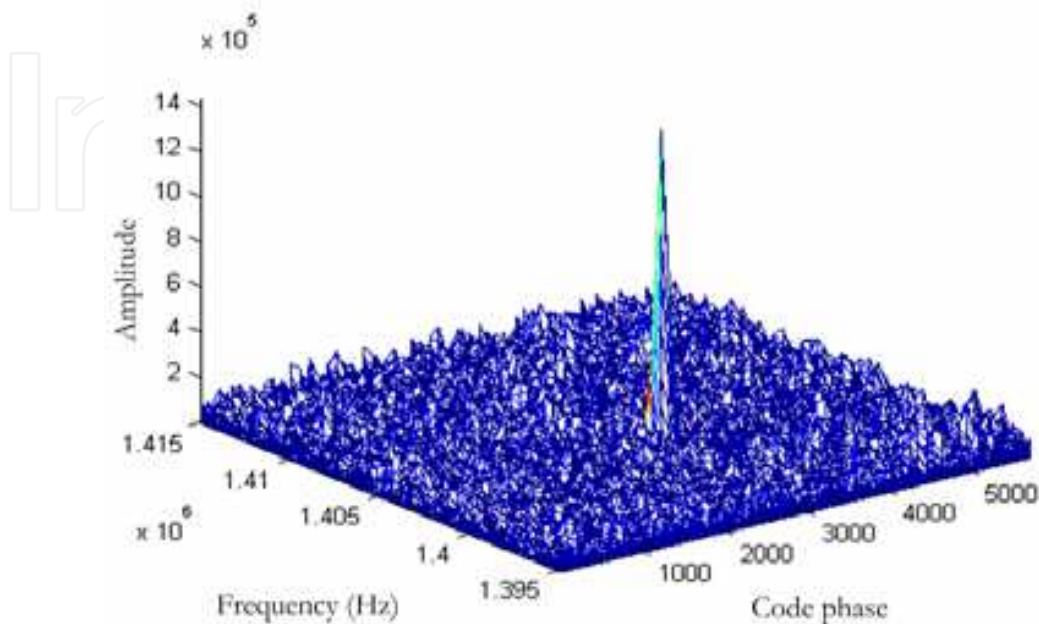


Fig. 6. The peak of signal acquisition (PRN=13)

4. Description on FFT algorithms

DFT of $x(n)$ could be defined as:

$$X(k) = \sum_{n=0}^{N-1} x(n)W_N^{nk} \quad (9)$$

According to the definition of equation (9), its computation of complex multiplication is N^2 , and its computation of complex addition is $N(N-1)$, whose operation is quite large. To calculate DFT rapidly, FFT algorithms came into being in nearly half a century with the purpose to reduce the calculation of DFT (Duhamel, & Vetterli, 1990).

Since Cooley and Tukey proposed FFT algorithm, the new algorithms have emerged constantly. In general, there are two basic directions. One is that the length of sequence equals to an integral power of 2, with the form of $N = 2^l$, such as radix-2 algorithm, radix-4 algorithm and split-radix algorithm. The other is that the number of points does not equal to an integer power of 2, with the form of $N \neq 2^l$, which is represented by a class of Winograd algorithm, such as prime factor algorithm and WFTA algorithm (Burrus, & Eschenbacher, 1981).

But the basic idea of various FFT algorithms is to divide the long sequence to short sequences successively, and then make full use of the periodicity, symmetry and reducibility of rotation factors to decompose DFT with a large number N into DFT with a combination of small number of points to reduce the computation. The property of the rotation factor W_N^{km} is as follows:

- Periodicity :

$$W_N^{(k+N)m} = W_N^{k(m+N)} = W_N^{km} \quad (10)$$

- Symmetry :

$$W_N^{mk+N/2} = -W_N^{mk} \quad (11)$$

$$(W_N^{km})^* = W_N^{-mk} \quad (12)$$

- Reducibility :

$$W_N^{mk} = W_{nN}^{nmk} \quad (13)$$

$$W_N^{mk} = W_{N/n}^{mk/n} \quad (14)$$

Where N/n is an integer.

4.1 Radix-2 FFT algorithm

Radix-2 FFT algorithm is commonly used, which is described in detail in the literatures (Jones, & Watson, 1990) (Sundararajan, 2003). Its basic requirement is the length of the sequence N should satisfy $N = 2^l$, where l is an integer. If N could not satisfy $N = 2^l$, zero-padding method is always applied. There are two categories in radix-2 FFT algorithm: one is to decompose the time sequence $x(n)$ (n is time label) successively which is called decimation-in-time algorithm, and the other one is to decompose the Fourier transform sequence $X(k)$ (k is frequency label) which is called decimation-in-frequency algorithm. To some extent these two algorithms are consistent, so only decimation-in-time algorithm would be described in detail here.

Divide the sequence $x(n)$ with the length $N = 2^l$ into two groups according to parity,

$$x(n) \Rightarrow \begin{cases} x_1(r) = x(2r) \\ x_2(r) = x(2r + 1) \end{cases} \quad (15)$$

Where $n = 0, 1, \dots, N/2 - 1$. Therefore, DFT could be transformed into

$$X(k) = DFT(x(n)) = \sum_{n=0}^{N-1} x(n)W_N^{nk} \quad (16)$$

Separate according to its parity,

$$X(k) = \sum_{r=0}^{N/2-1} x(2r)W_N^{2rk} + \sum_{r=0}^{N/2-1} x(2r + 1)W_N^{(2r+1)k} \quad (17)$$

Simplify,

$$X(k) = \sum_{n=0}^{N-1} x_1(n)W_{N/2}^{rk} + W_N^k \sum_{n=0}^{N-1} x_2(n)W_{N/2}^{rk} \quad (18)$$

If there exist

$$X_1(k) = \sum_{r=0}^{N/2-1} x(2r)W_{N/2}^{rk} = \sum_{r=0}^{N/2-1} x_1(n)W_{N/2}^{nk} \quad (19)$$

$$X_2(k) = \sum_{r=0}^{N/2-1} x(2r+1)W_{N/2}^{rk} = \sum_{r=0}^{N/2-1} x_2(n)W_{N/2}^{nk} \quad (20)$$

Where $k = 0, 1, \dots, N/2 - 1$. And

$$X(k) = X_1(k) + W_N^k X_2(k) \quad (21)$$

Utilize the property of rotating factor, and formula (22), (23), (24) and (25) could be got.

$$X_1(k + N/2) = X_1(k) \quad (22)$$

$$X_2(k + N/2) = X_2(k) \quad (23)$$

$$X(k) = X_1(k) + W_N^k X_2(k) \quad (24)$$

$$X(k + N/2) = X_1(k + N/2) + W_N^{k+N/2} X_2(k + N/2) = X_1(k) - W_N^k X_2(k) \quad (25)$$

In the process of decimation-in-time radix-2 FFT, the N points DFT needs to convert to two groups with even and odd serial numbers, and each group has $N/2$ points. Then the periodicity, symmetry and reducibility would be used. The operations of formula (24) and (25) could be described by butterfly unit as shown in Fig. 7. The transmission coefficient $+1$ and -1 in the figure means the multiplication with $+W_N^k$ and $-W_N^k$.

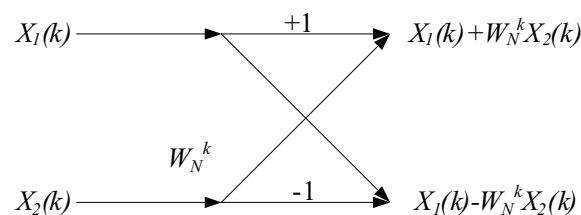


Fig. 7. Butterfly operation in decimation-in-time

Supposed that $N = 2^3 = 8$, now the decomposition process could be shown in Fig. 8.

Obviously, each butterfly operation requires one complex multiplication and two complex additions. If N points DFT is divided into two $N/2$ points DFT, calculating each $N/2$ points DFT directly, its computation of complex multiplication and complex addition are $N/2$ and $(N/2 - 1)N/2$ respectively. So these two $N/2$ points DFT requires $N^2/2$ complex multiplications and $(N/2 - 1)N$ complex additions. Considering the existing $N/2$ butterfly operations in synthesis of N points DFT, there would be $N/2$ complex multiplications and N complex additions. So the calculation of complex multiplication would be reduced to $N^2/2 + N/2 \approx N^2/2$, and the calculation of complex multiplication would be reduced to $N(N/2 - 1) + N \approx N^2/2$ with the first step decomposition. Therefore, when N equals to the integer power of 2, there would be $N \log_2 N/2$ complex multiplications and $N \log_2 N$ complex additions.

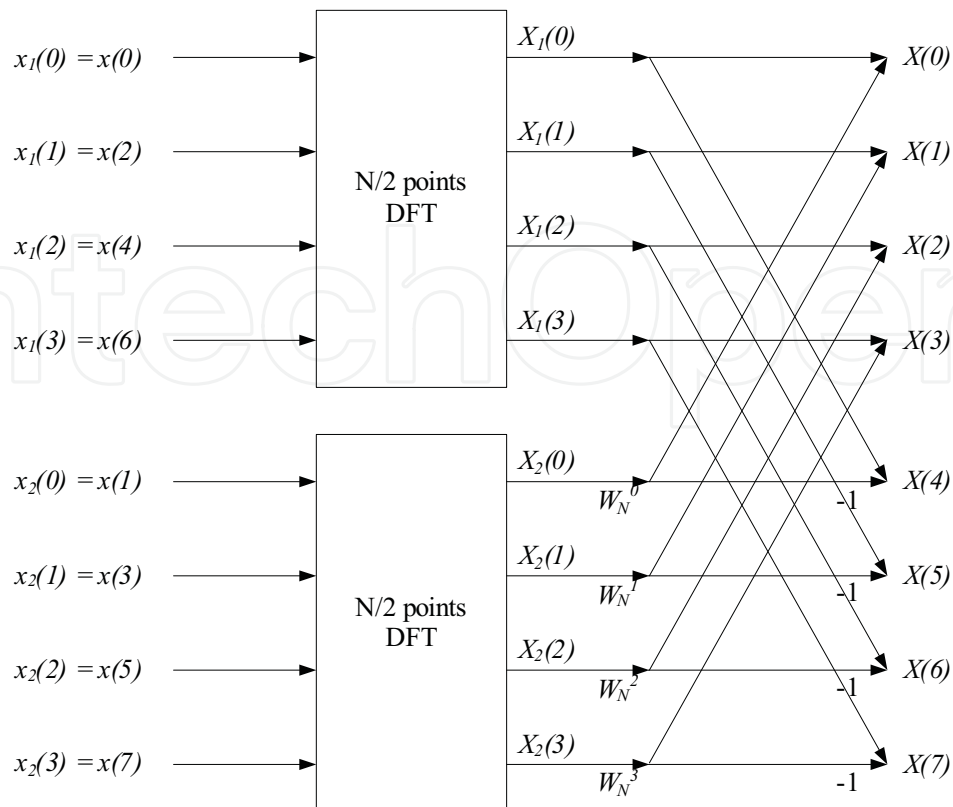


Fig. 8. Decomposition process of radix-2 FFT

4.2 Radix-4 FFT algorithm

Similar to the thought of radix-2 FFT, basic requirement of radix-4 FFT is the length of sequence N should satisfy $N = 4^l$, and it has been described in detail in the literatures (Jones, & Watson, 1990) (Sundararajan, 2003). It is worth to mention that each separate 4 points DFT would not require multiplication, and complex multiplication only appears in multiplying rotation factors operation. Rotation factor $W_N^0 = 1$, which need no multiplying, so each 4 points needs three multiplying rotation factors. And each step has $N/4$ 4 points DFT, so there would be $3N/4$ complex multiplications in each step. For N equals to 4^l , having l steps, the whole calculations of complex multiplications is

$$\frac{3}{4}N(l - 1) = \frac{3}{4}N((\log_2 N)/2 - 1) \approx \frac{3}{8}N \log_2 N \quad (26)$$

There is no multiplying rotation factor in first step operation. Compared to the calculation of radix-2 FFT, the multiplications operation is much less. The number of butterfly unit is the same, so the calculation of complex additions in radix-4 FFT is $N \log_2 N$, which equals to the calculation of radix-2 FFT.

4.3 Split-radix FFT algorithm

Split-radix FFT algorithm was proposed in 1984, whose basic idea is to use radix-2 FFT algorithm in even-number DFT, and use radix-4 FFT algorithm in odd-number DFT (Jones, & Watson, 1990) (Sundararajan, 2003).

Radix-2 algorithm is applied to process the DFT of even numbers, and then the DFT of even sample points could be:

$$X(2k) = \sum_{n=0}^{N/2-1} [x(n) + x(n + N/2)W_{N/2}^{nk}] \quad (27)$$

Where $k = 0, 1, \dots, N/2 - 1$. DFT of these points could be obtained by calculating the DFT of $N/2$ points without using any additional multiplication.

Similarly, radix-4 algorithm is applied to process the DFT of odd serial numbers. It is that rotation factor W_N^n should be multiplied for calculating the DFT of $\{X(2k + 1)\}$. For these sample points, the efficiency would be improved to use radix-4 decomposition, because the multiplication of 4 points butterfly operation is the least. Applying radix-4 decimation-in-frequency algorithm to calculate the DFT of odd sample points, the following $N/4$ points DFT could be obtained.

$$X(4k + 1) = \sum_{n=0}^{N/4-1} [(x(n) - x(n + N/2)) - j(x(n + N/4) - x(n + 3N/4))]W_N^n W_{N/4}^{kn} \quad (28)$$

$$X(4k + 3) = \sum_{n=0}^{N/4-1} [(x(n) - x(n + N/2)) + j(x(n + N/4) - x(n + 3N/4))]W_N^{3n} W_{N/4}^{kn} \quad (29)$$

So the N points DFT could be decomposed to one $N/2$ points DFT with no rotation factor and two $N/4$ points DFT with rotation factor. Use this strategy repeatedly until there is no decomposition.

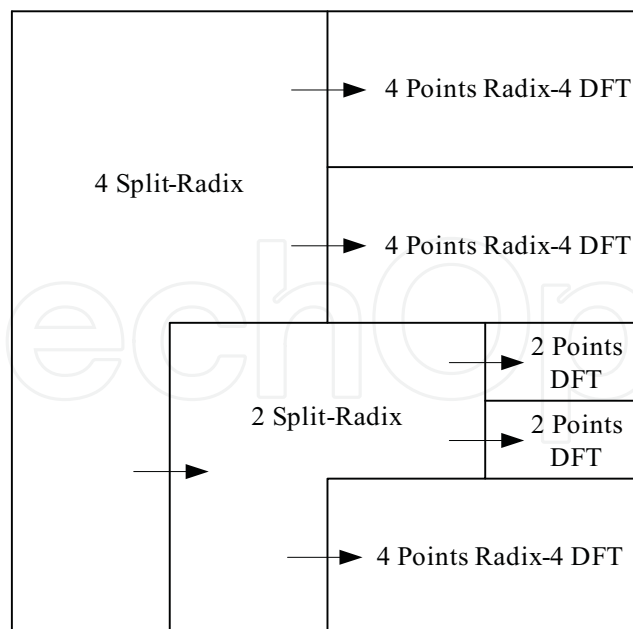


Fig. 9. 16 points DFT utilizing split-radix FFT

Taking $N = 4^2 = 16$ for example, there would be four split radices in the first step decomposition for $X(k)$. There would be two split radices in the second step decomposition

for $X_1(k)$, including a 4 points DFT utilizing radix-4 FFT and two 2 points DFT utilizing radix-2 FFT. And the second step decomposition for $X_2(k)$ and $X_3(k)$ are both 4 points DFT utilizing radix-2 FFT. The decomposition could be shown in Fig. 9.

Considering the efficiency and application conditions for radix-4 and radix-2 algorithm comprehensively, split-radix algorithm is one of the most ideal methods to process the DFT with the length of $N = 2^l$ (Lin, Mao, Tsao, Chang, & Huang, 2006) (Mao, Lin, Tseng, Tsao, & Chang, 2007) (Nagaraj, Andrew, & Chris, 2009).

4.4 PFA FFT

In the FFT calculation, the number of points N could not usually be approximated to the integer power of 2, where traditional radix-2, radix-4 and split-radix algorithms could not be used. PFA was proposed by Kolba and Park in 1977, which alleviates the conflict between computation and the structure of algorithm (Chu, & Burrus, 1982) (Liu, & Zhang, 1997). But when N equals to the product of a number of prime factors, that is $N = N_1 \times N_2 \dots \times N_i$, and most of them are odd items, its computational complexity would be slightly increased relative to the radix-2 FFT algorithm. Therefore the length of the decomposition factors should be better to be even, reducing the computations, whose basic idea is to transform one-dimensional DFT to two-dimensional or multi-dimensional small number of points DFT, and to get some superiors in calculation. However, it is provided that $N_1, N_2 \dots$ and N_i are prime to each other, so there could be only one even factor. Taking the whole efficiency of operation and computer resources cost into account, the application of PFA method in this section would be converted to the form of formula (30).

$$N = N_1 \times N_2 \quad (30)$$

Where N_1 and N_2 are prime factors to each other, and $N_1 = 2^m$, m is an integer.

4.5 WFTA FFT

The expression of DFT is:

$$X(k) = \sum_{n=0}^{N-1} x(n)W_N^{nk} \quad (31)$$

In the process of WFTA, the x and X in formula (31) could be expressed as the vector forms.

$$x = [x(0), x(1), \dots, x(N-1)]^T \quad (32)$$

$$X = [X(0), X(1), \dots, X(N-1)]^T \quad (33)$$

If D_N is a N -by- N matrix,

$$D_N(n, k) = [W_N^n k] \quad (34)$$

Where $n, k = 0, 1, \dots, N-1$. Here the DFT could be the matrix form of

$$X = D_N x \quad (35)$$

Winograd draw the decomposition of D_N , and

$$D_N = S_N C_N T_N \quad (36)$$

Where T_N is a J -by- N incidence matrix, S_N is a N -by- J incidence matrix, C_N a J -by- J diagonal matrix, J is a positive integer. According to different values of N , J is to be determined. Therefore,

$$X = S_N C_N T_N x \quad (37)$$

For the smaller number of points DFT, WFTA could obtain D_N by calculating S_N , C_N and T_N whose computations are less. When $N = 2, 3, 4, 5, 7, 8, 9, 16$, the results of DFT are defined as a smaller factor DFT, which were presented in the literatures (Winograd, 1976). It could be substituted to formula (36), and their computations could be shown in table 1, which is relatively less. For the larger number of points DFT, the structure and program are complex, which restrict the application of WFTA (Liu, & Zhang, 1997).

Length of sequence (N)	Multiplication computation	Addition computation
3	4	12
4	0	16
6	10	34
7	16	72
8	4	52
9	20	88
16	20	144

Table 1. The computation of smaller number of points DFT with WFTA

5. Optimized FFT algorithm for GPS signal acquisition

5.1 Preprocess for FFT

As for GPS receivers, the best sampling rate is an integer power of 2 (Jin, Wu, & Li, 2005), but actually the points in GPS receivers could not always meet the best sampling rate. So data pre-processing is needed. When $N \neq 2^l$, pretreatment would be used to transform the number of points satisfying $N = 2^l$, which includes following means (Zhao, Gao, & Hao, 2009).

1. Zeros-padding method

For arbitrary sampling rate f_s in RF front-end, the C/A code sequences are filled to the needed points. However, this process would change the cyclical properties of the C/A codes. Because of decreasing the correlation peak, the cross-correlation increases, and the signal to noise ratio (SNR) output diminishes, but it is easy to achieve.

2. Average correlation method

Divide the data into average packets, receive appropriate points and process FFT. This method could reduce the consumption of hardware resources, but also decrease the ratio of two peaks.

3. The linear interpolation method

If radix-2 FFT processing is applied, and linear interpolation methods are used, such as Lagrange interpolation algorithm, the input data would be interpolated to an integer power of 2.

4. Sinc interpolation method

First of all, apply Sinc filter interpolate the input data, and the original continuous signal would be recovered. Then it would be resampled with a new sampling frequency. The advantage is that the distortion of PRN code is smaller which makes receivers can still normally work in the low SNR environment, but the realization is complexity. Meanwhile, the volume of calculating is larger.

5. Double – Length Zero –Padding method

The method was proposed by Stockham in 1966, the main idea is to extend the calculation points from N to N_1 ,

$$N_1 = (2^k)_{min} \geq 2N - 1 \quad (38)$$

Where k is an integer. Add $N_1 - N$ zeros after the input data directly. The first N local C/ A codes and the final N local C/ A codes are in the same cycle. So fill $N_1 - 2N$ zeros in the intermediate and treat the extended data with FFT. The DFT of former N points is the required correlation results, and there is no loss of the correlation peak.

In the fast GPS signal acquisition process based on FFT, the commonly pretreatment is zeros-padding method.

5.2 Optimized FFT algorithm

As mentioned above, if the points of sequence meets $N = 2^l$, split-radix algorithm is one of the most effective approaches. In this article, an improved FFT method for the sequence with $N = 2^l$ points is proposed, which is called optimized FFT algorithm for integer power of 2 (OFFTI). Its specific operation is to maintain the split-radix algorithm until decomposed into the final 16 points DFT, and then utilize smaller points DFT with WFTA.

A smaller amount of zeros could be added to transform the type of $N \neq 2^l$ into the type of $N = 2^l$, and then OFFTI algorithm could be utilize. But for the sequence which could not be converted to the type of $N = 2^l$ with few zeros. The specific processing of this condition is as follows. Firstly, PFA is utilized to decompose $N = N_1 \times N_2$ points DFT to the nested form with N_1 ($N_1 = 2^m$) groups N_2 points DFT and N_2 groups N_1 points DFT. As each layer calculates relatively independence in the PFA method, so it will be still decomposed with PFA method in process of N_2 points DFT. Until decomposing to less points DFT, the WFTA would be considered. For $N_1 = 2^m$ points DFT, the OFFTI algorithm could be used. We call this method against the type not satisfying $N = 2^l$ OFFTN algorithm.

Taking GPS C/ A code acquisition for example, if the digital rate is 5MHz, there would be 5000 data points in 1msec data. Zeros-padding method is applied in the data preprocessing. According to the common radix-2 FFT, add zeros to 8192 points based on the 5000 data

points. Do $N=8192$ points DFT, and then discard the later 3192 points, which would bring extra computing and increase computation. Besides, there would be more errors brought in a certain extent. But if the OFFTN algorithm is used here, only several zeros should be added. Extending the points N to 5120 (45×5), the computation and errors would be much smaller than the traditional radix-2 FFT approach. The structure of the algorithm is shown in Fig. 10.

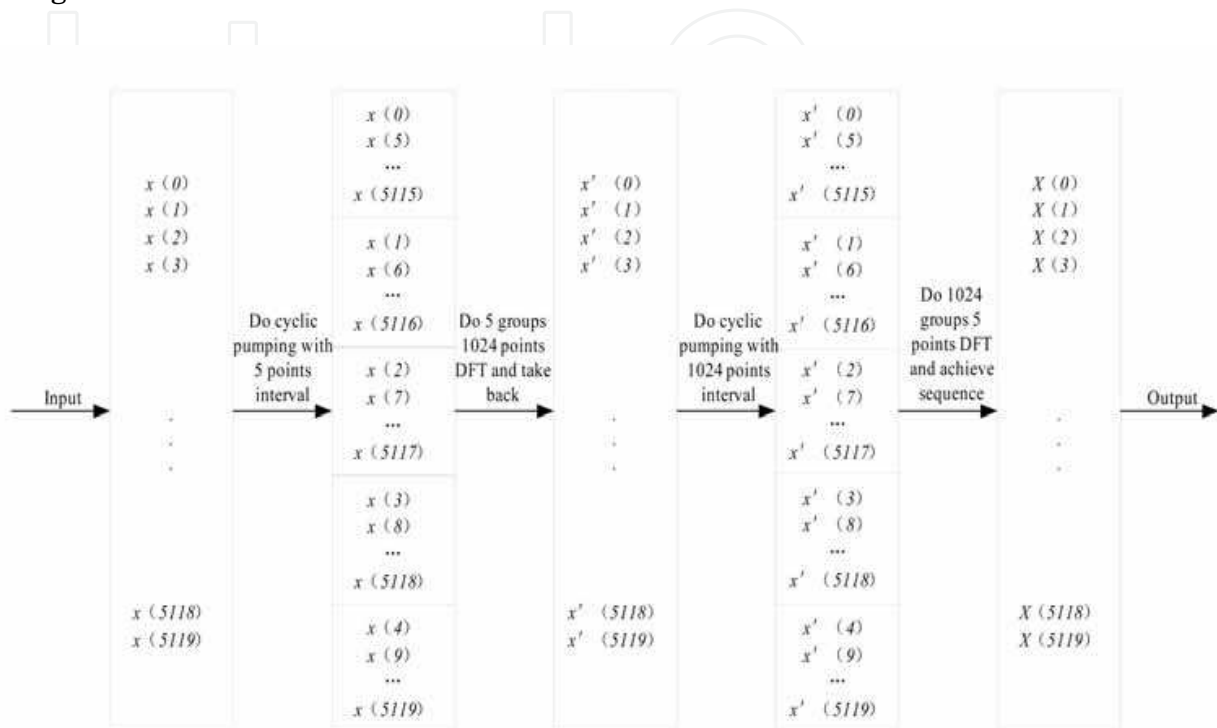


Fig. 10. The OFFTN structure of 5000 points

6. Improved acquisition method and simulation analysis

Apply the optimized methods mentioned above to GPS signal acquisition method based on FFT, the specific process is shown in Fig. 11.

The IF digital signal provided by GPS RF front-end is sent to baseband processing module, and then achieve pre-processing by few zeros padding. Multiply baseband signal with local generated carrier wave, and I channel signal is obtained. Multiply baseband signal with local generated carrier wave with 90° phase shift, and also Q channel signal is obtained. Then take the complex signal formed by I and Q channel signal to the FFT processing. Considering the character of the signal length, if N equals to the integer power of 2 approximately, OFFTI algorithm would be used, otherwise, OFFTN would be selected. The peak would generate by the correlation operations, and then compare it with the predetermined threshold. If the value is greater than the threshold, there would be GPS signal captured. Otherwise, no useful signal exists. Repeat the process until all of the available satellites are searched.

Signal acquisition base on radix-2 algorithm and the improved method are compared. As shown in Fig. 12, the correlation peaks have little difference for various methods and the acquisition results are mostly the same.

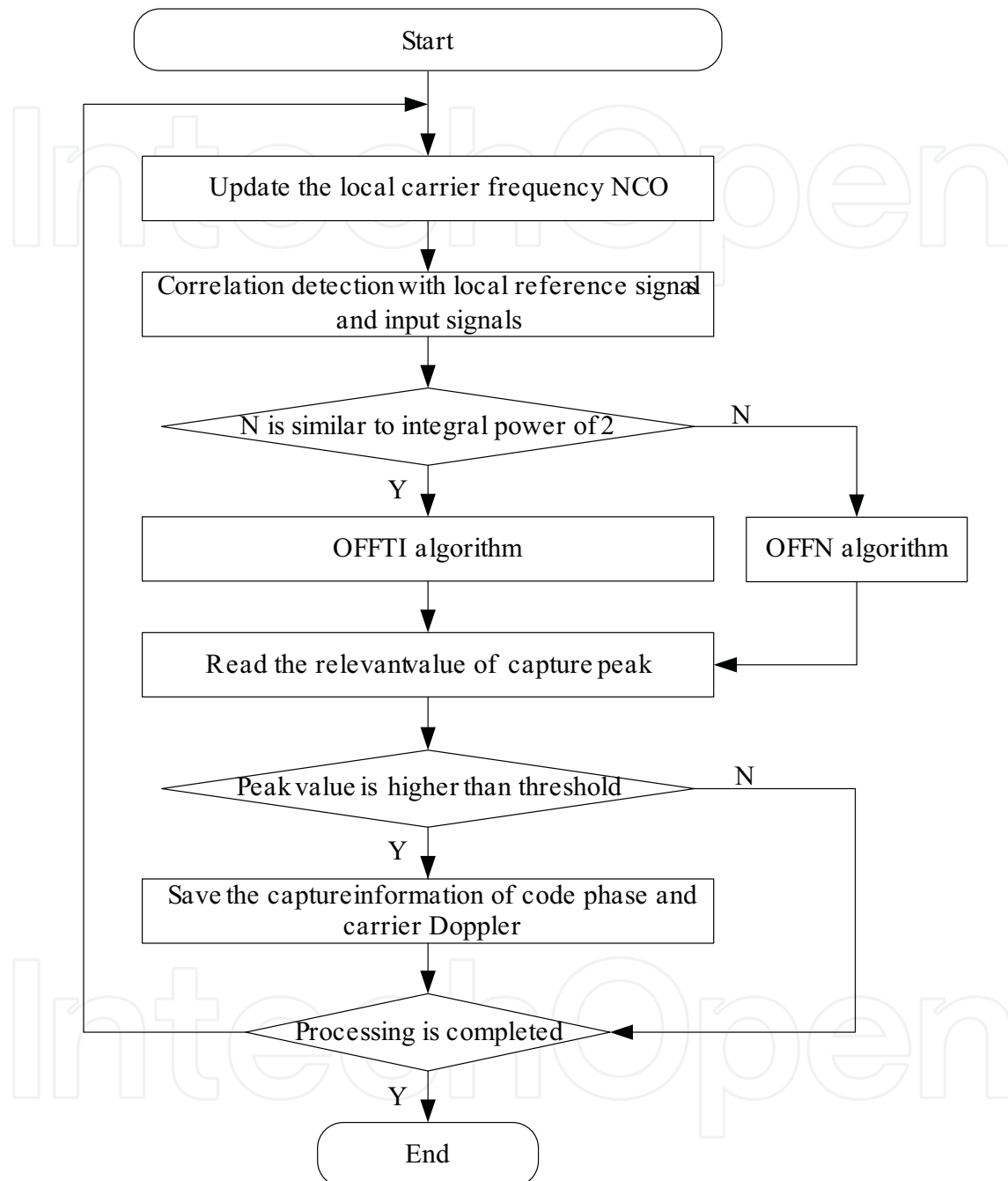
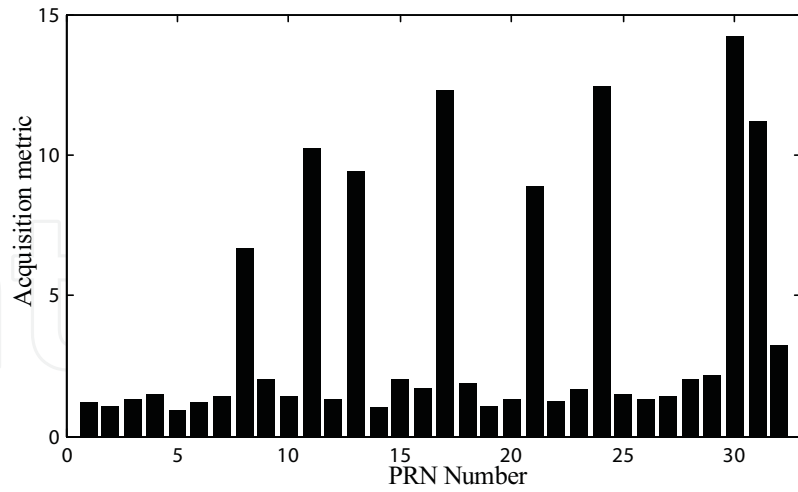
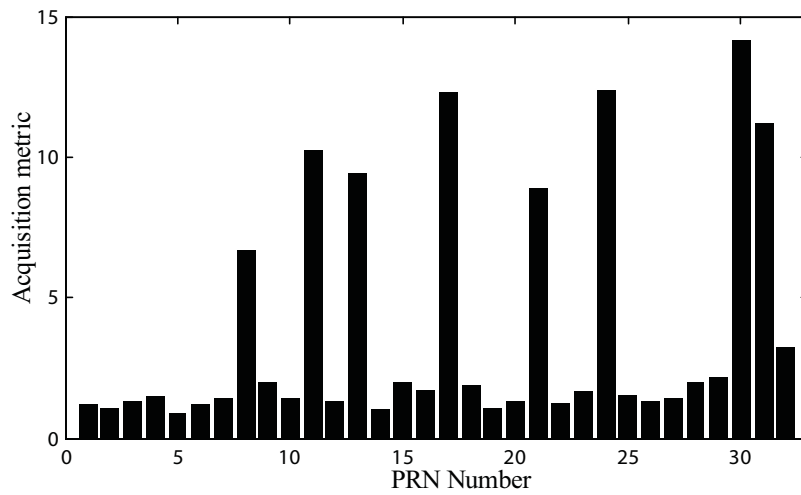


Fig. 11. GPS signal acquisition utilizing optimized FFT

To further verify the advantages of processing efficiency with utilizing optimized FFT, compare the signal acquisition time in various Doppler shifts. The results are shown in Fig. 13, which indicate the processing efficiency of improved method has a significant superiority to the traditional methods.



(a) Acquisition results utilizing radix-2 algorithm



(b) Acquisition results utilizing improved algorithm

Fig. 12. Acquisition results utilizing different algorithms

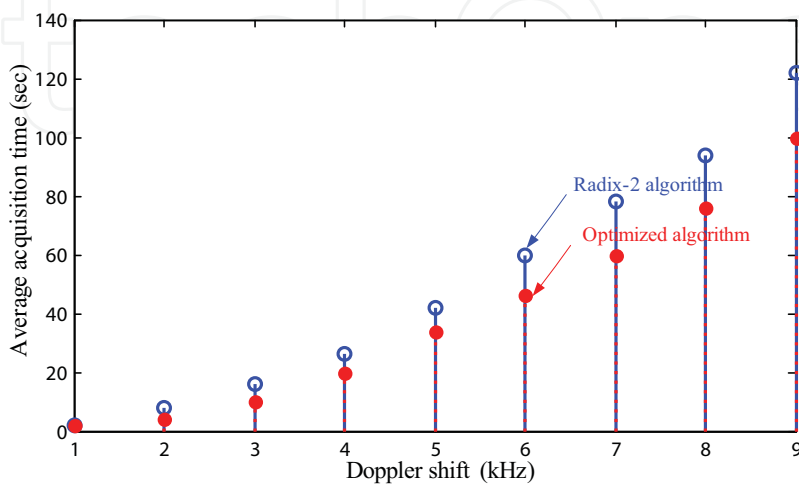


Fig. 13. Comparison of average acquisition time

7. Conclusion and future work

Apply an optimized FFT algorithm which integrates the traditional radix-2, radix-4, split-radix, PFA and WFTA to GPS C/ A code acquisition processing, and the primary results of simulation and experiment indicate that the optimized FFT algorithm could improve the average acquisition time and operation efficiency significantly. It is believed that this method could also be utilized in the long code acquisition, such as P code. Future work is to research and develop a more efficient and flexible processing platform to satisfy the demands of fast DFT calculation.

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This book aims to provide information about Fourier transform to those needing to use infrared spectroscopy, by explaining the fundamental aspects of the Fourier transform, and techniques for analyzing infrared data obtained for a wide number of materials. It summarizes the theory, instrumentation, methodology, techniques and application of FTIR spectroscopy, and improves the performance and quality of FTIR spectrophotometers.

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University Campus STeP Ri
Slavka Krautzeka 83/A
51000 Rijeka, Croatia
Phone: +385 (51) 770 447
Fax: +385 (51) 686 166
www.intechopen.com

InTech China

Unit 405, Office Block, Hotel Equatorial Shanghai
No.65, Yan An Road (West), Shanghai, 200040, China
中国上海市延安西路65号上海国际贵都大饭店办公楼405单元
Phone: +86-21-62489820
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