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Life Prediction of Gas Turbine Materials

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1. Introduction

The advance of gas turbine engines and the increase in fuel efficiency over the past 50 years relies on the development of high temperature materials with the performance for the intended services. The cutaway view of an aero engine is shown in Fig. 1. During the service of an aero engine, a multitude of material damage such as foreign object damage, erosion, high cycle fatigue, low cycle fatigue, fretting, hot corrosion/oxidation, creep, and thermomechanical fatigue will be induced to the components ranging from fan/compressor sections up front to high pressure (HP) and low pressure (LP) turbine sections at the rear. The endurance of the gas turbine engine to high temperature is particularly marked by the creep resistance of HP turbine blade alloy. Figure 2 shows the trend of firing temperature and turbine blade alloy capability (Schilke, 2004). Nowadays, the state-of-the-art turbine blade alloys are single crystal Ni-base superalloys, which are composed of intermetallic γ' (Ni_3Al) precipitates in a solution-strengthened γ matrix, solidified in the [100] crystallographic direction. Turbine disc alloys are also mostly polycrystalline Ni-base superalloys, produced by wrought or powder metallurgy processes. Compressor materials can range from steels to titanium alloys, depending on the cost or weight-saving concerns in land and aero applications. Coatings are often applied to offer additional protection from thermal, erosive and corrosive attacks. In general, the advances in gas turbine materials are often made through thermomechanical treatments and/or compositional changes to suppress the failure modes found in previous services, since these materials inevitably incur service-induced degradation, given the hostile (hot and corrosive) operating environment. Therefore, the potential failure mechanisms and lifetimes of gas turbine materials are of great concern to the designers, and the hot-section components are mostly considered to be critical components from either safety or maintenance points of view.

Because of its importance, the methodology of life prediction has been under development for many decades (see reviews by Viswanathan, 1989; Wu et al., 2008). The early approaches were mainly empirically established through numerous material and component tests. However, as the firing temperatures are increased and the operating cycles become more complicated, the traditional approaches are too costly and time-consuming to keep up with the fast pace of product turn-around for commercial competition. The challenges in life prediction for gas turbine components indeed arise due to their severe operating conditions: high mechanical loads and temperatures in a high-speed corrosive/erosive gaseous environment. The combination of thermomechanical loads and a hostile environment may induce a multitude of material damages including low-cycle fatigue, creep, fretting and oxidation. Gas turbine designers need analytical methods to extrapolate the limited material

property data, often generated from laboratory testing, to estimate the component life for the design operating condition. Furthermore, the requirement of accurate and robust life prediction methods also comes along with the recent trend of prognosis and health management, where assessment of component health conditions with respect to the service history and prediction of the remaining useful life are needed in order to support automated mission and maintenance/logistics planning.

To establish a physics-based life prediction methodology, in this chapter, the fundamentals of high temperature deformation are first reviewed, and the respective constitutive models

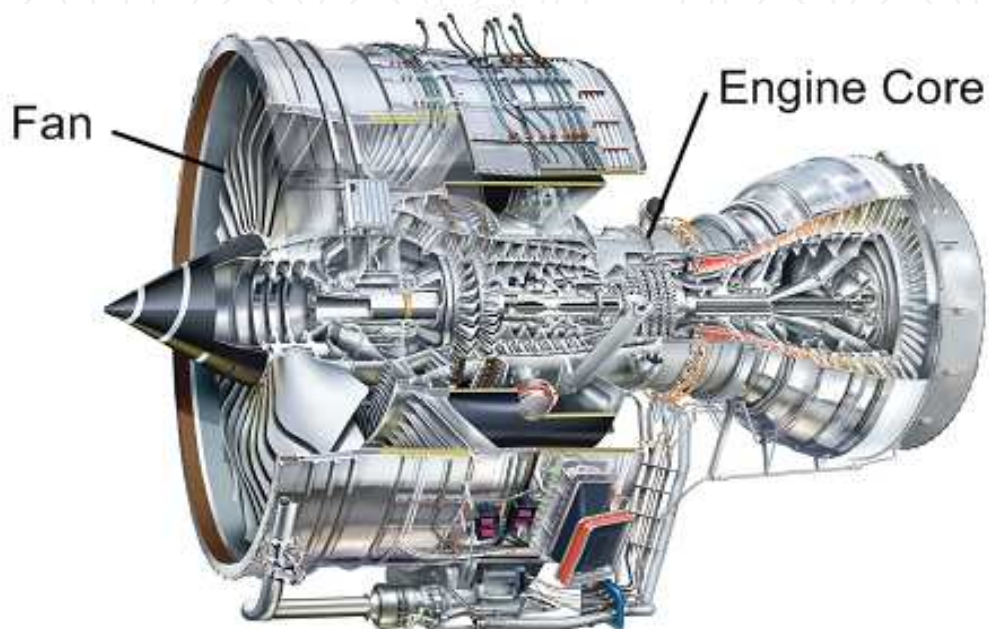


Fig. 1. Cutaway view of the Rolls-Royce Trent 900 turbofan engine used on the Airbus A380 family of aircraft (Trent 900 Optimised for the Airbus A380 Family, Rolls-Royce Plc, Derby UK, 2009).

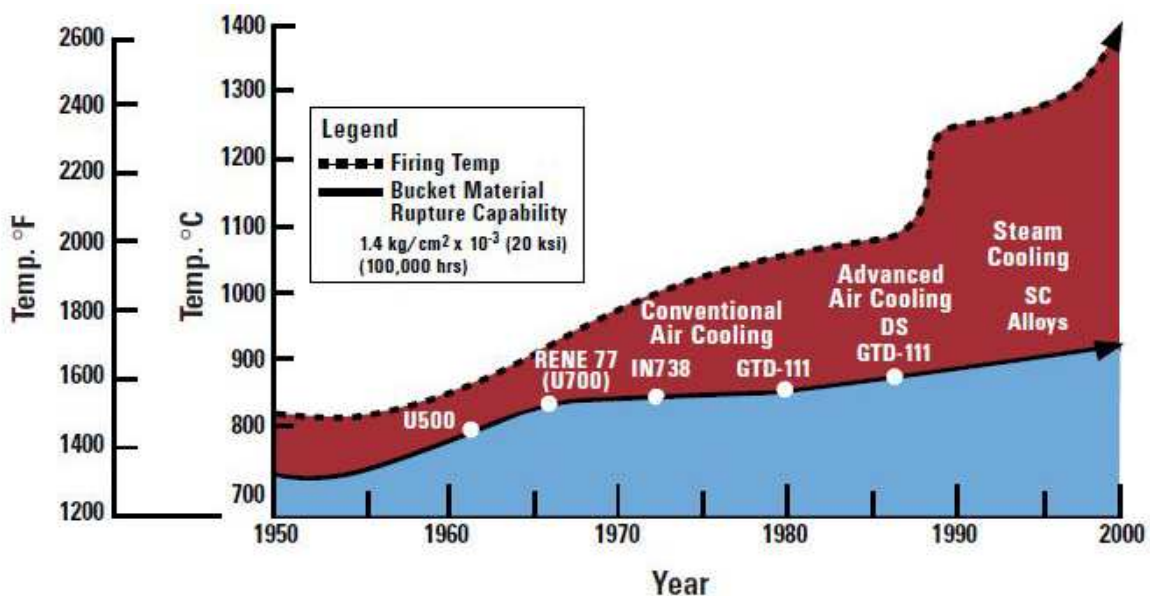


Fig. 2. Increase of firing temperature with respect to turbine blade alloys development (Schilke, 2004).

are introduced. Then, the evolution of material life by a combination of damage mechanisms is discussed with respect to general thermomechanical loading. Furthermore, crack growth problems and the damage tolerance approach are also discussed with the application of fracture mechanics principles.

2. Fundamentals of high temperature deformation

In general, for a polycrystalline material, deformation regimes can be summarized by a deformation map, following Frost and Ashby (Frost & Ashby, 1982), as shown schematically in Fig. 3. Elastic (E) and rate-independent plasticity (P) usually happens at low temperatures (i.e. $T < 0.3 T_m$, where T_m is the melting temperature). In the plasticity regime, the deformation mechanism is understood to be dislocation glide, shearing or looping around the obstacles along the path; and the material failure mechanism mainly occurs by alternating slip and slip reversal, leading to fatigue, except for ultimate tensile fracture and brittle fracture. As temperature increases, dislocations are freed by vacancy diffusion to get around the obstacles so that time-dependent deformation manifests. Time dependent deformation at elevated temperatures is basically assisted by two diffusion processes – grain boundary diffusion and lattice diffusion. The former process assists dislocation climb and glide along grain boundaries, resulting in grain boundary sliding (GBS), whereas the latter process assists dislocation climb and glide within the grain interior, resulting in intragranular deformation (ID) such as the power-law and power-law-breakdown.

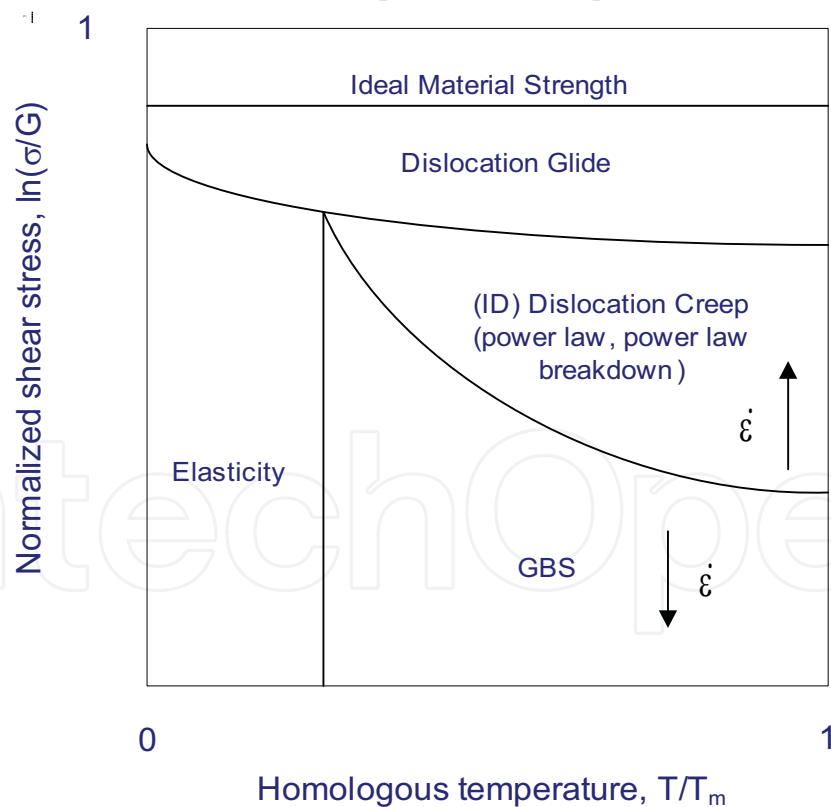


Fig. 3. A schematic deformation mechanism map.

In an attempt to describe inelastic deformation over the entire stress-temperature field, several unified constitutive laws have been proposed, e.g. Walker (1981), Chaboche & Galetaud (1986), and most recently, Dyson & McLean (2000). These constitutive models

employ a set of evolution rules for kinematic and isotropic hardening to describe the total viscoplastic response of the material, but do not necessarily differentiate whether the contribution comes from intragranular deformation mechanism or GBS, and hence have limitations in correlating with the transgranular, intergranular and/or mixed failure modes that commonly occur in gas turbine components. Therefore, a physics-based theoretical framework encompassing the above deformation and damage mechanisms is needed.

To that end, we proceed with the basic concept of strain decomposition that the total inelastic strain in a polycrystalline material can be considered to consist of intragranular strain ε_g and grain boundary sliding ε_{gbs} , as:

$$\varepsilon_{in} = \varepsilon_g + \varepsilon_{gbs} \quad (1)$$

The physics-based strain decomposition rule, Eq. (1), with the associated deformation mechanisms is the foundation for the development of an integrated creep-fatigue (ICF) modelling framework as outlined in the following sections (Wu et al. 2009).

2.1 Intragranular deformation

Intragranular deformation can be viewed as dislocation motion, which may occur by glide at low temperatures and climb plus glide at high temperatures, overcoming the energy barriers of the lattice. By the theory of deformation kinetics (Krausz & Eyring, 1975), the rate of the net dislocation movement can be formulated as a hyperbolic sine function of the applied stress (Wu & Krausz, 1994). In keeping consistency with the Prandtl-Reuss-Drucker theory of plasticity, the flow rule of intragranular strain, in tensor form, can be expressed as

$$\dot{\varepsilon}_g = \dot{p}_g \mathbf{n}_g \quad (2)$$

where \dot{p}_g is the plastic multiplier as defined by

$$\dot{p}_g = 2A(1 + Mp_g) \sinh(\psi) = \sqrt{\frac{2}{3} \dot{\varepsilon}_g : \dot{\varepsilon}_g} \quad (3)$$

where A is an Arrhenius-type rate constant, M is a dislocation multiplication factor, and \mathbf{n}_g is the flow direction as defined by

$$\mathbf{n}_g = \frac{3(\mathbf{s} - \boldsymbol{\chi}_g)}{2\sigma_g^{eq}} \quad (4)$$

where \mathbf{s} is the deviatoric stress tensor and $\boldsymbol{\chi}_g$ is the back stress tensor.

Note that the stress and temperature dependence of the plastic multiplier is described by a hyperbolic sine function, Eq. (3), with the evolution of activation energy ψ given by:

$$\dot{\psi} = \frac{V}{kT} \dot{\sigma}_g^{eq} \quad (5)$$

where V is the activation volume, k is the Boltzmann constant, and T is the absolute temperature in Kelvin. Eq. (3) covers both the power-law and the power-law-breakdown regimes in Fig. 3.

As intragranular deformation proceeds, a back stress may arise from competition between work hardening (dislocation pile-up and network formation) and recovery (dislocation climb) as:

$$\dot{\chi}_g = \frac{2}{3} H_g \dot{\epsilon}_g - \kappa \chi_g \quad (6)$$

where H_g is the work-hardening coefficient and κ is the climb rate (see detailed formulation later). Note that more complicated expressions that consider both hardening and dynamic/static recovery terms may need to be used to formulate the back stress with large deformation and microstructural changes, but to keep the simplicity for small-scale deformation (<1%), Eq. (6) is suffice, as demonstrated in the later examples.

The effective equivalent stress for intragranular deformation is given by

$$\sigma_g^{eq} = \sqrt{\frac{3}{2} (\mathbf{s} - \boldsymbol{\chi}_g) : (\mathbf{s} - \boldsymbol{\chi}_g)} \quad (7)$$

where the column (:) signifies tensor contraction.

2.2 Grain boundary sliding

Based on the grain boundary dislocation glide-climb mechanism in the presence of grain boundary precipitates (Wu & Koul, 1995; 1997), the governing flow equation for GBS can be expressed as

$$\dot{\boldsymbol{\epsilon}}_{gbs} = \dot{p}_{gbs} \mathbf{n}_{gbs} \quad (8)$$

with a GBS multiplier as defined by

$$\dot{p}_{gbs} = \varphi \frac{D\mu b}{kT} \left(\frac{b}{d}\right)^q \left(\frac{l+r}{b}\right)^{q-1} \frac{(\sigma_{gbs}^{eq}) (\sigma^{eq} - \sigma_{ic})}{\mu^2} \quad (9)$$

where D is the diffusion constant, μ is the shear modulus, and b is the Burgers vector, d is the grain size, r is the grain boundary precipitate size, l is the grain boundary precipitate spacing, and q is the index of grain boundary precipitate distribution morphology ($q = 1$ for clean boundary, $q = 2$ for discrete distribution, and $q = 3$ for a network distribution). The GBS flow direction is defined by

$$\mathbf{n}_{gbs} = \frac{3}{2} \frac{(\mathbf{s} - \boldsymbol{\chi}_{gbs})}{\sigma_{gbs}^{eq}} \quad (10)$$

The two equivalent stresses in Eq. (9) are given by

$$\sigma_{gbs}^{eq} = \sqrt{\frac{3}{2} (\mathbf{s} - \boldsymbol{\chi}_{gbs}) : (\mathbf{s} - \boldsymbol{\chi}_{gbs})} \quad (11)$$

and

$$\sigma^{eq} = \sqrt{\frac{3}{2} \mathbf{s} : \mathbf{s}} \quad (12)$$

The evolution of the grain boundary back stress in the presence of grain boundary precipitates is given by (Wu & Koul, 1995)

$$\dot{\chi}_{gbs} = \frac{2}{3} H_{gbs} \dot{\epsilon}_{gbs} - \kappa \chi_{gbs} \quad (13)$$

where H_{gbs} is the grain boundary work hardening coefficient, and κ is the dislocation climb rate as given by

$$\kappa = \frac{D\mu b (\sigma^{eq} - \sigma_{ic})}{kT \mu} \quad (14)$$

The equivalent stress for GBS, σ_{gbs}^{eq} , controls the grain boundary dislocation glide with a back stress χ_{gbs} . The other equivalent stress, σ^{eq} , controls grain boundary dislocation climb, once it surpass a threshold stress, σ_{ic} , that arises from the constraint of grain boundary precipitates. As shown in Eq. (9), the GBS multiplier is controlled by the grain boundary diffusion constant D and grain boundary microstructural features such as the grain size, the grain boundary precipitate size and spacing, and their morphology. The back stress formulation, Eq. (13), states the competition between dislocation glide, which causes grain boundary dislocation pile-up, and recovery by dislocation climb. Henceforth, Eq. (9) depicts the grain boundary plastic flow as a result of dislocation climb plus glide overcoming the microstructural obstacles present at the grain boundaries. Last but not least, GBS is also affected by the grain boundary waveform, as given by the factor ϕ (Wu & Koul, 1997):

$$\phi = \begin{cases} \frac{2}{1 + \left(\frac{2h}{\lambda}\right)^2} - 1 & \text{for triangular boundaries} \\ \frac{2}{\sqrt{1 + \left(\frac{\pi h}{\lambda}\right)^2}} - 1 & \text{for sinusoidal boundaries} \end{cases} \quad (15)$$

where λ is wavelength and h is the amplitude.

By solving all the components of inelasticity, the evolution of the stress tensor is governed by

$$\dot{\sigma} = \mathbf{C} : (\dot{\epsilon} - \dot{\epsilon}_{in}) \quad (16)$$

3. Deformation processes and constitutive models

3.1 Cyclic deformation and fatigue

It is commonly known that a metal subjected to repetitive or fluctuating stress will fail at a stress much lower than its ultimate strength. Failures occurring under cyclic loading are generally termed *fatigue*. The underlying mechanisms of fatigue is dislocation glide, leading to formation of persistent slip bands (PBS) and a dislocation network in the material. Persistent slip bands, when intersecting at the interface of material discontinuities (surface, grain boundaries or inclusions, etc.) result in intrusions/extrusions or dislocation pile-ups, inevitably leading to crack nucleation.

To describe the process of cyclic deformation, we start with tensile deformation as follows. For uniaxial strain-controlled loading, the deformation is constrained as:

$$\dot{\epsilon} = \frac{\dot{\sigma}}{E} + \dot{\epsilon}_p = \text{constant} \quad (17)$$

Substituting Eq. (3-7) into Eq. (17) (neglecting dislocation climb, i.e., $\kappa\chi_g \ll H\dot{\varepsilon}$; and multiplication, i.e., $M = 0$), we have the first-order differential equation of Ψ , as (Wu et al., 2001)

$$\dot{\Psi} = \frac{EV}{kT} \left[\dot{\varepsilon} - 2A \left(1 + \frac{H}{E} \right) \sinh \Psi \right] \quad (18)$$

which can be solved as

$$\left(\frac{e^{-\Psi} - a}{\chi e^{-\Psi} + b} \right) = \left(\frac{1-a}{\chi+b} \right) \exp \left\{ -\frac{VE\dot{\varepsilon}(t-t_0)\sqrt{1+\chi^2}}{kT} \right\} \quad (19)$$

where

$$\chi = \frac{2A}{\dot{\varepsilon}} \left(1 + \frac{H}{E} \right), \quad a = \frac{\sqrt{1+\chi^2} - 1}{\chi}, \quad b = \sqrt{1+\chi^2} + 1 \quad (20)$$

The initial time of plastic deformation is defined by

$$\Psi_0 = \frac{(\sigma - H\varepsilon_p^0 - \sigma_0)}{kT} = 0 \quad (21)$$

where ε_p^0 is the plastic strain accumulated from the prior deformation history, and σ_0 , as an integration constant, represents the initial lattice resistance to dislocation glide. At the first loading, $\varepsilon_p^0 = 0$. Since the deformation is purely elastic before the condition, Eq. (21), is met: $\sigma = E\dot{\varepsilon}t$, then $t_0 = \sigma_0/(E\dot{\varepsilon})$. Once the stress exceeds the initial lattice resistance in the material, i.e., $\sigma > \sigma_0$, plasticity commences. In this sense, σ_0 corresponds to the critical resolved shear stress by a Taylor factor.

From Eq. (20), we can obtain the stress-strain response as follows:

$$\sigma - H\varepsilon_p - \sigma_0 = -\frac{kT}{V} \ln \left(\frac{a + \omega(\varepsilon)b}{1 - \omega(\varepsilon)\chi} \right) \quad (22)$$

where, $\omega(\varepsilon)$ is a response function as defined by

$$\omega(\varepsilon) = \left(\frac{1-a}{\chi+b} \right) \exp \left\{ -\frac{V(E\varepsilon - \sigma_0)\sqrt{1+\chi^2}}{kT} \right\} \quad (23)$$

Eq. (22) basically describes the accumulation of plastic strain via the linear strain-hardening rule with dislocation glide as the dominant process and limited dislocation climb activities. It is applicable to high strain rate loading conditions, which are often encountered during engine start-up and shutdown or vibration conditions caused by mechanical and/or aerodynamic forces.

Based on the deformation kinetics, Eq. (22) describes the time and temperature dependence of high temperature deformation. As an example, the tensile behaviors of IN738LC at 750 °C, 850 °C and 950 °C are described using Eq. (22) and shown in Fig. 4, in comparison with the

experimental data. The strain rate dependence of the tensile behavior of this alloy at 950°C is also demonstrated in Fig. 5. The parameters for this material model are given in Table 1.

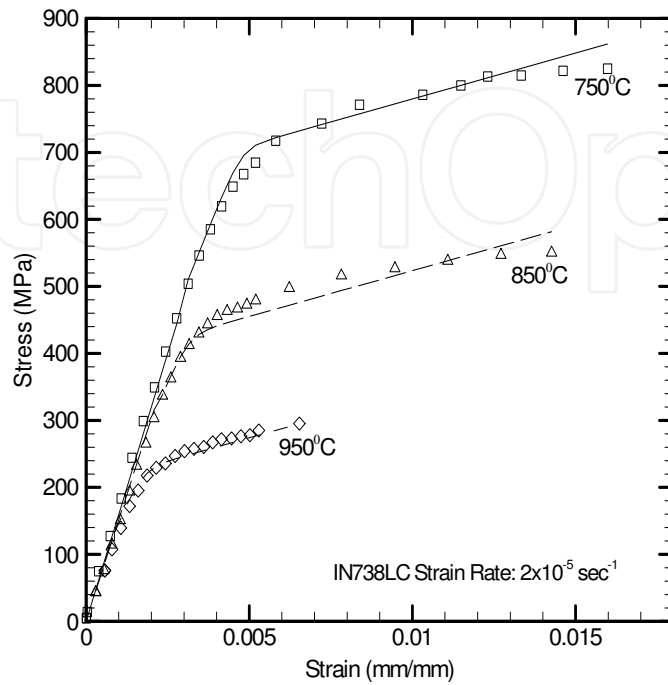


Fig. 4. Stress-strain curves for the IN738LC with the lines as described by Eq. (22).

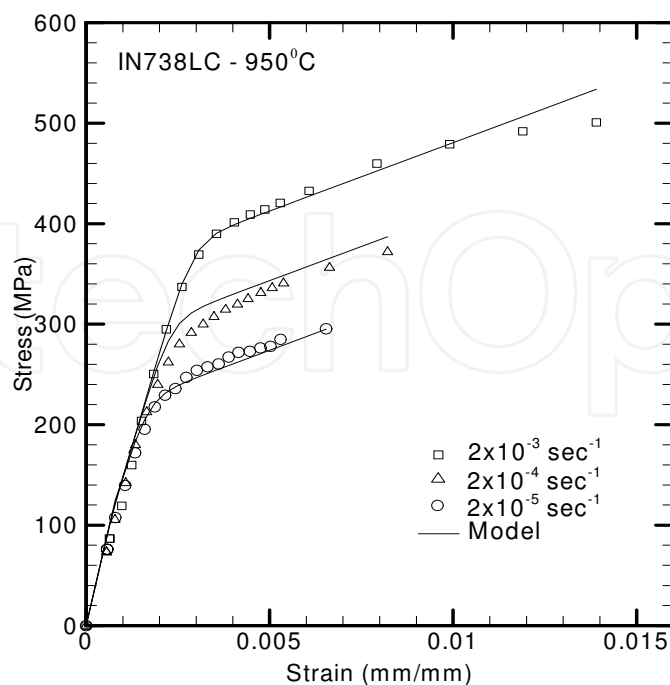


Fig. 5. Stress-strain responses of IN738LC to different loading strain rates at 950 °C.

Temperature (°C)	750	850	950
Initial lattice resistance, σ_0 (MPa)	540	285	110
Work Hardening Coefficient, H (MPa/mm/mm)	15000	13736	12478
Modulus of Elasticity, E (GPa)	175.5	151.4	137.0
Strain-Rate Constant, $A = A_0 \exp[-\Delta G_0^\ddagger / kT]$ (sec ⁻¹)	3.5×10^{-8}	1.56×10^{-7}	5.5×10^{-7}
Activation Constants			
Activation Volume, V (m ³)	3.977×10^{-22}		
Pre-exponential, A_0 (sec ⁻¹)	0.7		
Activation Energy, ΔG_0^\ddagger (J)	2.38×10^{-19}		

Table 1. Constitutive Model Parameters for IN738LC

This constitutive model has 6 parameters: E, H, V, σ_0 , A_0 and ΔG_0^\ddagger , which have defined physical meanings. The elastic modulus, E, the work-hardening coefficient, H and the initial activation stress σ_0 , are temperature-dependent. The activation parameters, V, A_0 and ΔG_0^\ddagger , are constants corresponding to a “constant microstructure”. As far as deformation in a lifing process is concerned, which usually occurs within a small deformation range of $\pm 1\%$, the description is mostly suffice. The present model, in the context of Eq. (22), also incorporates some microstructural effects via H and σ_0 . The significance will be further discussed later when dealing with fatigue life prediction. But before that, let us examine the cyclic deformation process as follows.

Under isothermal fully-reversed loading conditions, first, Eq. (22) describes the monotonic loading up to a specified strain. Upon load reversal at the maximum stress point, the material has $2\sigma_0 + H\varepsilon_p$ as the total stress barrier to yield in the reverse cycle. This process repeats as the cycling proceeds. As an example, the hysteresis loop of IN738LC is shown in Fig. 6. The solid line represents the model prediction with the parameters given in Table 1 (except $\sigma_0 = 40$ MPa for this coarser grained material). The model prediction is in very good agreement with the experimental data, except in the transition region from the elastic to the steady-state plastic regimes, which may be attributed to the model being calibrated to a finer-grained material.

As Eq. (22) implies, material deforms purely elastically when the stress is below σ_0 , but plasticity starts to accumulate just above that, which may still be well below the engineering yield surface defined at 0.2% offset. This means that the commencing of plastic flow may first occur at the microstructural level, even though the macroscopic behaviour still appears to be in the elastic regime. In this sense, σ_0 may correspond well to the fatigue endurance limit. Therefore, just by analyzing the tensile behaviour with Eq. (22), one may obtain an important parameter for fatigue life prediction.

Tanaka and Mura (Tanaka & Mura, 1981) have given a theoretical treatment for fatigue crack nucleation in terms of dislocation pile-ups. Fig. 7 shows a schematic of crack nucleation by a) vacancy dipole, which leads to intrusion; b) interstitial dipole which leads to extrusion, or c) tripole that corresponds to an intrusion-extrusion pair. They obtained the following crack nucleation formula:

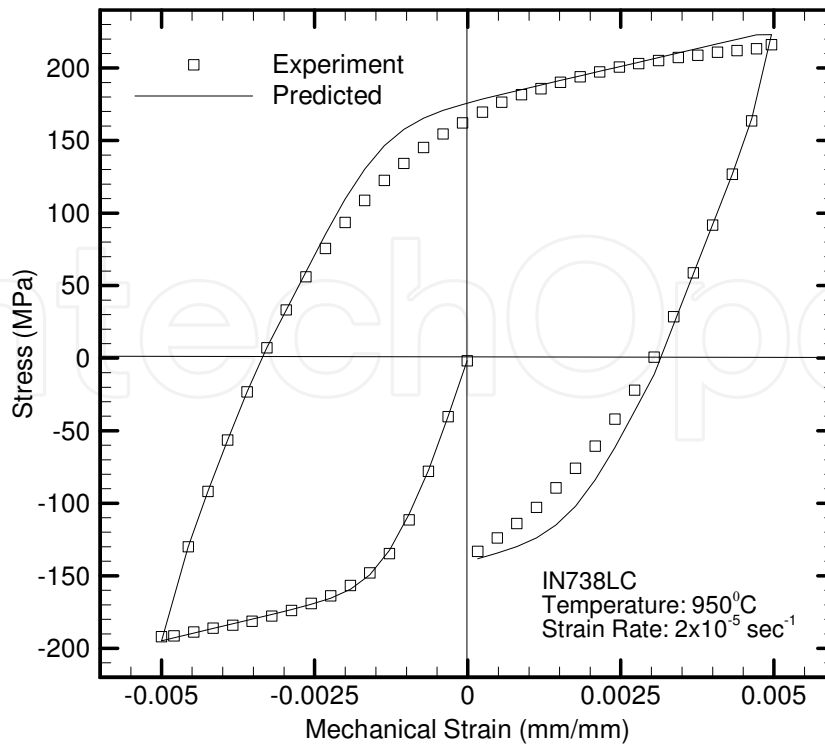


Fig. 6. Hysteresis loop of IN738LC at 950°C.

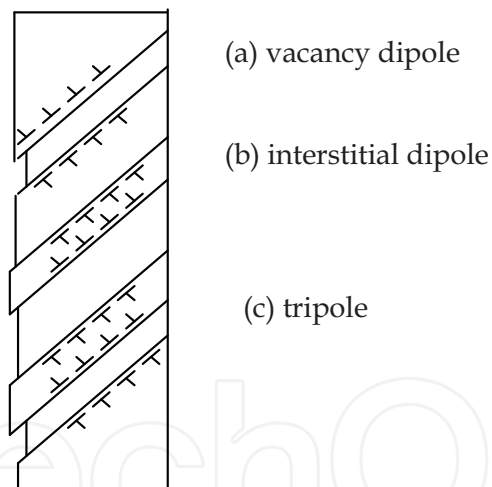


Fig. 7. Dislocation pile-ups by (a) vacancy dipoles (intrusion), (b) interstitial dipoles (extrusion) and (c) tripoles (intrusion-extrusion pair).

$$N_c = \frac{4(1-\nu)w_s}{\mu b} \frac{1}{\Delta\gamma^2} \quad (24)$$

where $\Delta\gamma$ is the plastic shear strain range.

Under strain-controlled cycling conditions, $\Delta\varepsilon_p = \Delta\varepsilon - \Delta\sigma/E$, Eq. (24) can also be written in the following form:

$$\frac{1}{N} = C\varepsilon_p^2 = C\left(\Delta\varepsilon - \frac{\Delta\sigma}{E}\right)^2 \quad (25)$$

Fig. 8 shows the prediction of Eq. (25) with $C = 0.009$ for fully-reversed low cycle fatigue of IN738 at 400°C, in comparison with the experimental data (Fleury & Ha, 2001). The flow stress σ is obtained from Eq. (22). Since the tensile behaviour of IN738 exhibits no significant temperature dependence below 700°C, the material properties at 750°C, as listed in Table 1, are used for the evaluation. Apparently, according to Eq. (25), the material's fatigue life approaches infinity when the total strain $\varepsilon \rightarrow \sigma_0/E$. In this case, the predicted endurance limit σ_0/E is approximately 0.4, which agrees well with the experimental observation. As shown in Fig. 8, when the fatigue life is correlated with the plastic strain range, the relationship is represented by a straight line in the log-log scale, as established by Coffin (1954) and Manson (1954), through numerous experimental observations on metals and alloys. When the fatigue life is correlated with the total strain range, the relationship becomes nonlinear.

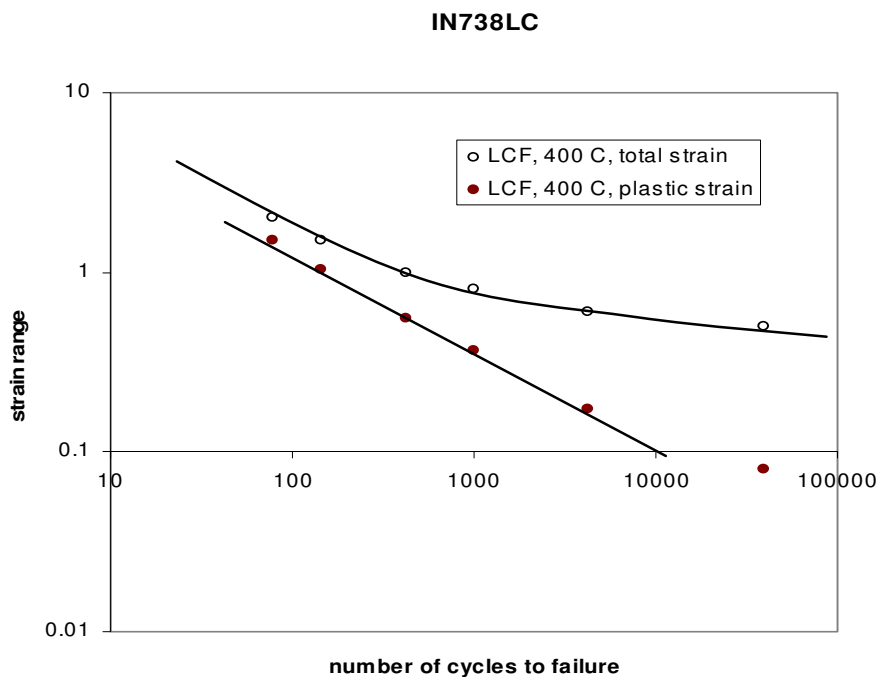


Fig. 8. LCF life of IN738 in terms of plastic and total strain (%).

The nonlinear total-strain-based fatigue life equation is often written as:

$$\Delta\varepsilon_p = \varepsilon'_f N_f^c + \frac{\sigma'_f}{E} N_f^b \quad (26)$$

where c , b , ε'_f and σ'_f are empirical constants.

Eq. (26) has been extensively used by engineers analyzing fatigue data. To establish the relationship, one needs to conduct strain-controlled cyclic tests with appreciable plastic deformation, and also stress controlled cyclic tests when plasticity is not measurable. Arbitrarily, failure cycles less than 10^4 has been termed *low cycle fatigue* (LCF), and above that *high cycle fatigue* (HCF). Laboratory LCF data are usually used to estimate the life of component with stress concentration features such as notches and holes, since it is believed that with the constraint of the surrounding elastic material, the local deformation behaviour is leaning more towards strain-controlled condition; whereas HCF data are usually used to

assess the component life under elastic stresses. For gas turbine engine components, an LCF cycle may represent major loading cycles such as engine start up -shutdown. HCF, on the other hand, occurs under low-amplitude cyclic stresses where deformation is primarily elastic. HCF failures are usually associated with vibration-induced stresses due to mistune or other geometrical damage that change the vibration characteristics of the component. It can become a life-threatening mode of failure especially when it is superimposed on LCF induced cracks. Under these conditions, components vibrate with high frequencies that can reach thousands of cycles per second, and hence exhaust its fatigue life after a short period of time.

Eq. (25) can also be extrapolated to HCF under stress controlled fatigue conditions. When the applied stress is well below the engineering yield point, the logarithm term in Eq. (22) is nearly zero such that the plastic strain can be approximated by

$$\varepsilon_p \approx \frac{\sigma - \sigma_0}{H} \quad (27)$$

and Eq. (25) can be rewritten as

$$\sigma = \sigma_0 + H(BN)^{-1/2} \quad (28)$$

Fig. 9 shows the S-N relationship of Ti-6Al-4V described with Eq. (28). In summary, it has been shown that Eq. (25) can be used for both LCF and HCF regimes with the material constitutive law, Eq. (22). It can potentially simplify the fatigue analysis by calibrating with a few cyclic tests in either LCF or HCF regime.

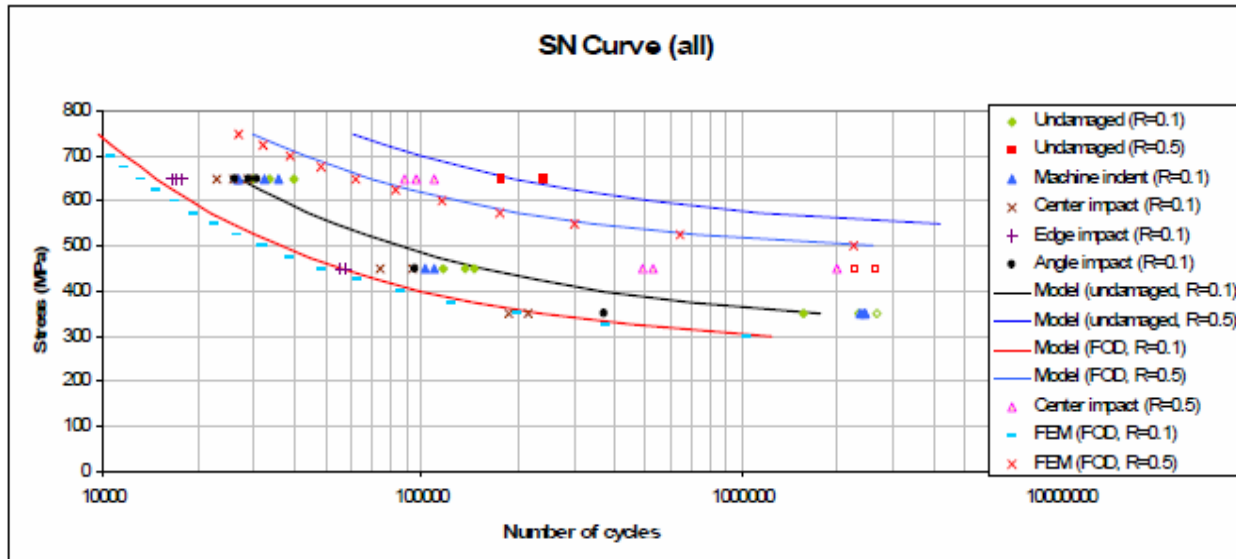


Fig. 9. S-N curves of Ti6Al4V under pristine and foreign object damaged conditions (Wu, 2009a).

3.2 Thermomechanical fatigue

Advanced turbine blades and vanes often employ a sophisticated cooling scheme, in order to survive at high firing temperatures. During engine start up and shutdown, these components experience thermal-mechanical cyclic loads, which can have a severer impact

on the life of the material than isothermal conditions. Thermomechanical fatigue (TMF) refers to the fatigue behaviour of a material under simultaneously thermal and mechanical loads. For laboratory studies, usually simple TMF cycles are employed: i) the in-phase (IP) cycle, which has a 0° phase angle between thermal and mechanical loads; ii) the out-of-phase (OP) cycle, which has a 180° phase angle; and iii) the diamond phase (DP) cycle, which has a phase angle in between; as schematically shown in Fig. 10. The OP and IP cycles represent two extreme conditions, where the maximum stress is reached at the “hot” end of IP and the “cold” end of OP temperature cycle. A more sophisticated engine cycle is shown in Fig. 11, which consists of a half diamond-phase cycle, a thermal excursion from T_{mean} to T_{max} , and a hold period at the maximum load.

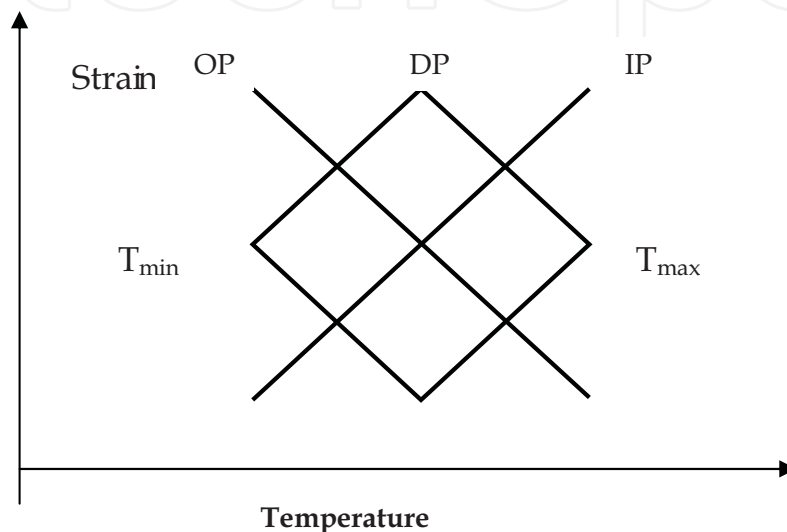


Fig. 10. Temperature-strain cycles for different TMF tests.

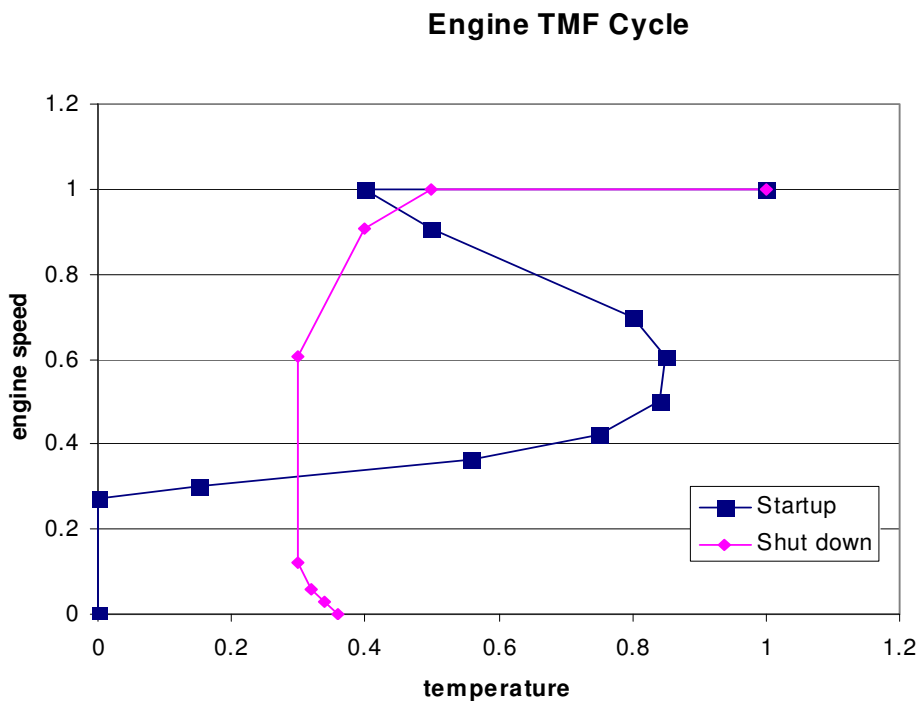


Fig. 11. An engine TMF cycle.

During TMF, the total strain (ε_{tot}) is the sum of thermal and mechanical strain components:

$$\varepsilon_{tot} = \varepsilon_{th} + \varepsilon_{mech} = \alpha(T - T_0) + \varepsilon_{mech} \quad (29)$$

where ε_{th} is the thermal strain, T_0 is the reference temperature, T is the current temperature, and α is the thermal expansion coefficient. The mechanical strain (ε_{mech}) in general can be considered as the sum of the elastic and inelastic strain components.

The damage accumulation and interactions during TMF can be very complex, because it usually involves fatigue, oxidation and creep in some combination. In extreme cases, the combined effects of temperature and stress could just induce one dominant damage mode, for example, it is generally believed that the IP cycle produces predominantly creep damage, while the OP cycle induces oxide-scale cracking (Sehitoglu, 1992). However, under general TMF conditions, the combined damage mechanisms and their interactions can be complicated. Many factors such as the maximum and minimum temperature, thermal and mechanical strain ranges, the phasing between temperature and strain, the strain rate, dwell time, and environment can all influence TMF life. It is almost a formidable task to characterize these effects completely by experimental approaches such as those adopted for LCF and HCF assessments. Therefore, physics based models are needed to describe the complex damage processes under TMF loading. In this section, the cyclic thermomechanical deformation behaviour is described. Interactions with oxidation and creep under general TMF conditions will be discussed later.

For TMF, we assume that the evolution of the energy, Ψ , undergoes a series of infinitesimal isothermal steps, for each i -th step, the energy state evolves from Ψ_{i-1} to Ψ_i over the time interval $\Delta t_i = t_i - t_{i-1}$ at a constant temperature T_i . Then, Eq. (18) can be integrated into the form:

$$\ln \left(\frac{e^{-\Psi} - a}{\chi e^{-\Psi} + b} \right) \Bigg|_{\Psi_{i-1}}^{\Psi_i} = - \frac{VE\dot{\varepsilon}\sqrt{1+\chi^2}}{kT_i} \Delta t_i \quad (i=1,2,\dots) \quad (30)$$

Summing up all these infinitesimal steps, we have:

$$\sum_{i=1}^N \ln \left(\frac{e^{-\Psi} - a}{\chi e^{-\Psi} + b} \right) \Bigg|_{\Psi_{i-1}}^{\Psi_i} = - \sum_{i=1}^N \frac{VE\dot{\varepsilon}\sqrt{1+\chi^2}}{kT_i} \Delta t_i \quad (31)$$

Let $N \rightarrow \infty$, the left-hand side of Eq. (31) will be equal to the logarithmic difference between the final state and the initial state, and the right-hand side is an integration of the temperature-dependent terms over the loading period. After mathematical rearrangement, we have:

$$\left(\frac{e^{-\Psi} - a}{\chi e^{-\Psi} + b} \right) = \left(\frac{1-a}{\chi+b} \right) \exp \left\{ - \int_{t_0}^t \frac{V\mu\dot{\gamma}\sqrt{1+\chi^2}}{kT} dt \right\} \quad (32)$$

where t_0 is the time to reach the elastic limit, or in other words, for plastic flow to commence, as defined by Eq. (21).

Let

$$\omega(t) = \left(\frac{1-a}{\chi+b} \right) \exp \left\{ - \int_{t_0}^t \frac{VE\dot{\varepsilon}\sqrt{1+\chi^2}}{kT} dt \right\} \quad (33)$$

and assume that within the temperature range of TMF, the variation of E is moderate such that it can be represented by its average E_m , and $\sqrt{1+\chi^2} \approx 1$ since χ is usually small, the ω function can be evaluated as,

$$\omega = \left(\frac{1-a}{\chi+b} \right) \exp \left\{ \mp \frac{VE_m\Delta\varepsilon\sqrt{1+\chi^2}}{k\Delta T} \ln \frac{T}{T_0} \right\} \quad (34)$$

where $\Delta T = T_{\max} - T_{\min}$ is the temperature range, $\Delta\varepsilon$ is the total strain range, the $-/+$ sign is used for the temperature rising or declining halves of the cycle, respectively, and T_0 denotes the temperature point at which the stress reaches the elastic limit, which can be determined based on the thermomechanical cycle profile, i.e., the $T - \varepsilon$ relationship.

Then, Eq. (32) can be rewritten into the stress vs. strain function, similar to Eq. (22), as

$$\sigma - H\varepsilon_p - \sigma_0 = - \frac{kT}{V} \ln \left(\frac{a + \omega b}{1 - \omega\chi} \right) \quad (35)$$

The stress-strain response of the coarse-grained IN738LC under an out-of-phase thermomechanical fatigue condition is predicted using Eq. (35), as shown in Figure 2.10, with the parameter values given in Table 2.1 but with a reduced $\sigma_0 = 40\text{MPa}$ for the coarse-grained ($d \sim 5\text{mm}$) material. The predicted hysteresis loop is in good agreement with the experimentally measured response.

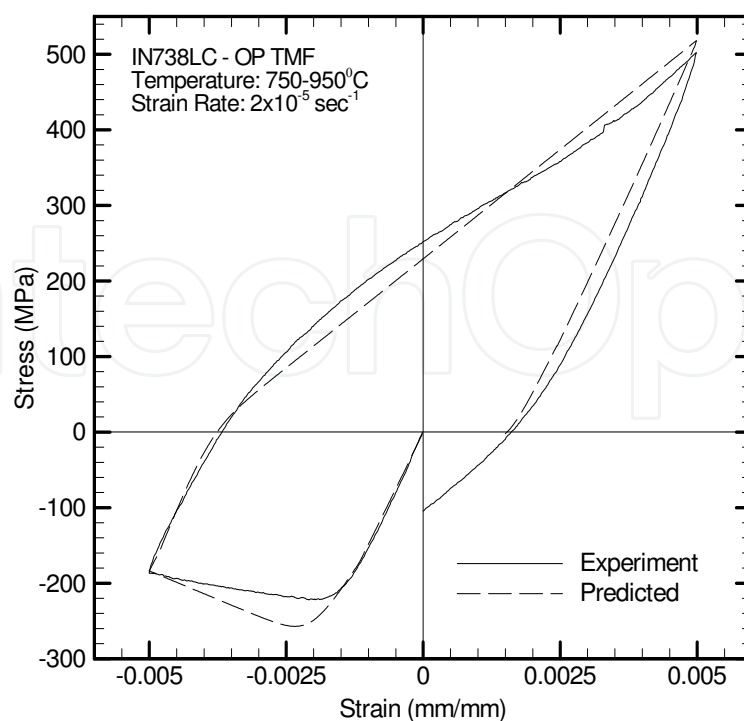


Fig. 12. Stress-strain response of IN738LC (coarse-grain) during an OP-TMF cycle.

3.3 Creep

Creep is a mode of inelastic material deformation occurring under sustained loading at high temperatures, usually above $0.3 T_m$ (T_m is the material's melting point). Creep can be one of the critical factors determining the integrity of components at elevated temperatures. In gas turbine engines, especially in hot sections, components such as turbine blades are subjected to sustained loads (centrifugal force and pressure) at high temperatures during the operation. Creep of a turbine blade can also cause dimensional changes that either reduce its aerodynamic efficiency or lead to elongation that rubs the engine casing, which may induce additional vibration and noise. Furthermore, creep damage may interact with fatigue that leads to significant reduction in the service life of the component.

Creep mechanisms have been extensively reviewed (Frost & Ashby, 1982; Ashby & Dyson, 1985; Wu & Koul, 1996). It is generally understood that the creep rate has different stress dependence by different mechanisms. Nevertheless, the steady-state creep rate (or the minimum creep rate) is often expressed in a Norton-Bailey form, as

$$\dot{\epsilon} = A_0 \exp\left(\frac{Q}{RT}\right) \sigma^n \quad (36)$$

where Q is the activation energy, T is the absolute temperature, R is the universal gas constant, and A_0 and n are empirical constants.

Traditionally, creep damage assessment has been mainly based on the minimum creep rate and the Larson-Miller plot, taking into consideration the temperature compensated rate property as exhibited in Eq. (36). Fig. 13 shows the Larson-Miller plot for Astroloy. In general, the stress vs. Larson-Miller parameter relationship is nonlinear due to the multiple creep mechanisms involved, and therefore, it is merely an experimental correlation rather than a physics-based model. Extrapolation to predict the long term creep life using Larson-Miller parameter has to be based on extensive testing. For component life prediction, it needs a constitutive law of creep to describe the stress relaxation and redistribution with time as creep deformation proceeds.

It has been known that creep deformation is a continuous physical process, where a decreasing creep rate regime (transient creep: primary plus secondary) is followed by an accelerating creep rate regime (tertiary creep) beyond a minimum creep rate. Wu & Koul (1996) have proposed a creep-curve model, based on the decomposition of the total inelastic strain into grain boundary sliding and intragranular deformation, as expressed in Eq. (1), and concluded that grain boundary sliding is primarily responsible for the transient creep behaviour, while the tertiary creep evolves mostly intragranular deformation with dislocation multiplication.

Under uniaxial loading condition, the solution of Eq. (8)-(14) has the form (Wu & Koul, 1995)

$$\epsilon_{gbs} = \epsilon_0 + \phi \dot{\epsilon}_{ss} t + \frac{\sigma}{\beta^2 H_{gbs}} \left[1 - \exp\left(-\frac{\beta^2 \phi H_{gbs} \dot{\epsilon}_{ss} t}{\sigma(\beta - 1)}\right) \right] \quad (37)$$

where β is a microstructure parameter, and

$$\dot{\epsilon}_{ss} = \phi(1 - \beta^{-1}) \frac{D\mu b}{kT} \left(\frac{b}{d}\right)^q \left(\frac{l+r}{b}\right)^{q-1} \frac{\sigma(\sigma - \sigma_{ic})}{\mu^2} \quad (38)$$

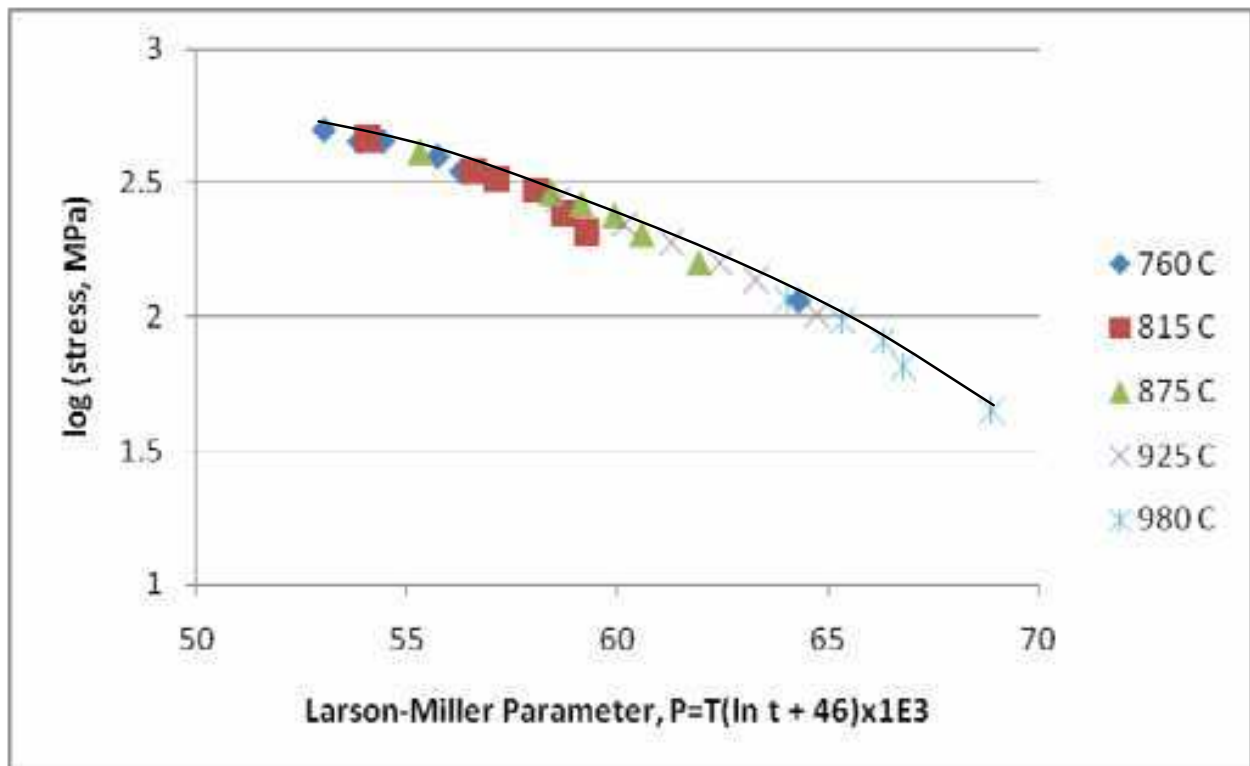


Fig. 13. The Larson -Miller plot for Astroloy.

Equation (37-38) is derived from the grain boundary dislocation glide plus climb mechanism. It states that the transient creep is a grain boundary sliding phenomenon that consists of a primary stage and a steady-state stage. It is influenced mostly by grain boundary microstructure and morphology, thus emphasizing the importance of grain boundary engineering in alloy design. According to Eq. (37), the true steady-state creep occurs at a rate as described by Eq. (38) only after an infinitely long time. Practically, a quasi-steady-state may be observed relatively soon after creep deformation starts, since the primary strain is reached as an exponential function of time. However, how long the quasi-steady-state will last depends on the time to the onset of tertiary creep, which is controlled by damage accumulation in both grain interior and along grain boundaries, such as dislocation multiplication, precipitate coarsening and cavity nucleation and growth. These processes may eventually take over and lead to an acceleration in the creep rate. Tertiary creep phenomena will be discussed later. Presently, we will discuss the important characteristics of transient creep before the commencing of tertiary creep.

First of all, the present model predicts a primary strain, as defined by

$$\varepsilon_{tr}^p = \frac{\sigma}{\beta^2 H_{gbs}} \quad (39)$$

It states that the primary strain is proportional to the applied stress σ divided by the work hardening coefficient H_{gbs} . This relationship may provide guidance for grain boundary engineering to lower the primary strain in alloy applications. Practically, the primary strain can be attained ~99 percent when the exponential term reaches 4.6, which defines the primary time as follows.

$$t_{tr}^p = 4.6 \frac{(\beta - 1)\sigma}{\beta^2 H \dot{\epsilon}_m} \quad (40)$$

Second of all, the present model predicts that ideally the GBS strain rate has a stress-dependence to the 2nd power. However, the apparent stress dependence may change since the presence of grain boundary precipitates can induce a back stress, σ_{ic} . For example, creep data on Nimonic 115 (Furrillo et al., 1979) can be correlated with Eq. (38), as shown in Fig. 14.

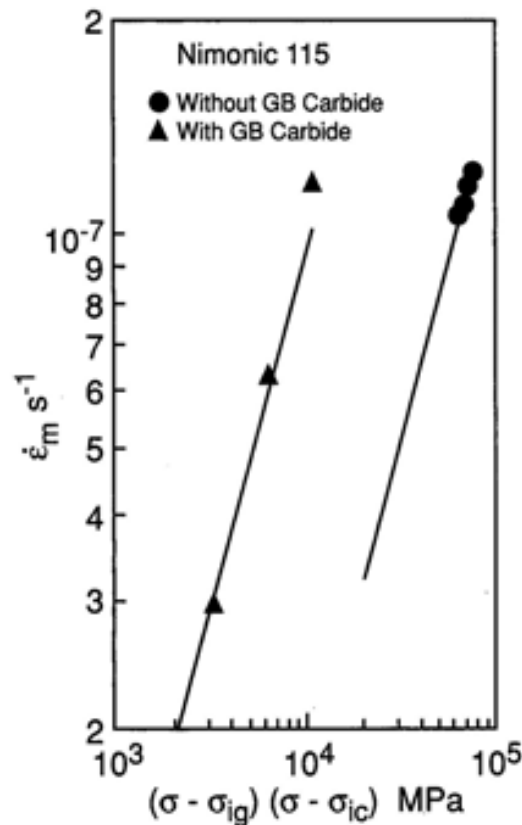


Fig. 14. The minimum creep rate correlation for Nimonic 115 (Wu and Koul, 1995).

The creep data generated by Castillo et al. (1988) on new and service exposed IN738LC turbine blade materials have also been analyzed with Eq. (37-38). Fig. 15 shows the creep curves obtained using Eq. (37) with the parameters as given in Table 2. In addition, creep curves of Alloy 718 and IN738 with planar and wavy grain boundaries are shown in Fig. 16 and Fig. 17, respectively. The descriptions have been made using Eq. (37) with the microstructure parameter and the wave factor ϕ , Eq. (15), given in Table 3. It should be noted that Eq. (37) in its present form does not include a damage parameter, and therefore only applicable to the point before tertiary creep commences. The coupling of GBS with grain boundary cavitation and/or oxidation will be discussed later.

Material Condition	Test Temperature	ϵ_0 (%)	β	H (GPa)	$\dot{\epsilon}_m$ (10^{-9} s^{-1})
New	954 °C	0.1	1.313	18.0	2.0
14159 hrs.	954 °C	0.45	1.13	30.0	3.05

Table 2. Creep Curve Parameters for IN738LC under Stress of 90MPa

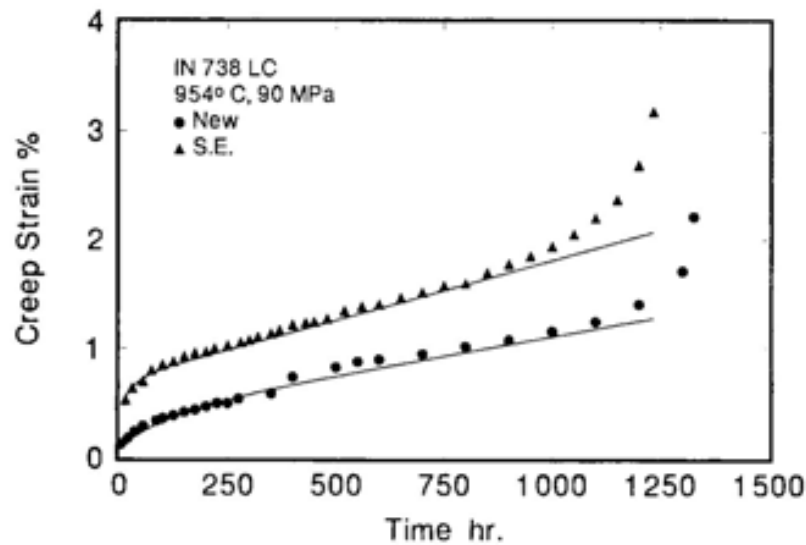


Fig. 15. Creep curves of new and service-exposed IN738LC as predicted by Eq. (37) (Wu & Koul, 1995).

Materials & Test Conditions	Grain Boundary	H (GPa)	β	ϕ	$\dot{\epsilon}_m$ (hr ⁻¹)
Alloy 718 $\sigma = 590$ MPa T = 650 °C	(planar) h = 0 $\lambda = d$ (triangular) h = 2 μm $\lambda = 10 \mu\text{m}$	204.6	1.78	1.0	0.00233
IN738LC $\sigma = 586$ MPa T = 760 °C	(planar) h = 0 $\lambda = d$ (sinusoidal) h = 5 μm $\lambda = 15 \mu\text{m}$	106.5	1.13	1.0	0.0397
		106.5	1.13	0.38	0.0152

Table 3. Microstructure and Creep Curve Parameters of Alloy 718

Intragranular deformation has been discussed in the previous section. It can be inferred from Eq. (2)-(7) that at constant stress, deformation would stop by work-hardening due to pile-up of gliding dislocations unless dislocation climb helps the dislocations to bypass the obstacle. Thus, it is reasonable to assume that during constant-stress creep, a steady-state of back stress is attained soon upon loading such that the intragranular strain rate $\dot{\epsilon}_i = \text{const}$. This means that the primary creep mechanism of intragranular deformation is negligible, which is often the case as observed in single crystal materials (Carry & Strudel, 1977, 1978). The tertiary creep strain then may accumulate with dislocation climb and multiplication as (Wu & Koul, 1996):

$$\dot{\epsilon}_g = (1 + M\epsilon_g)\dot{\epsilon}_i \quad (41)$$

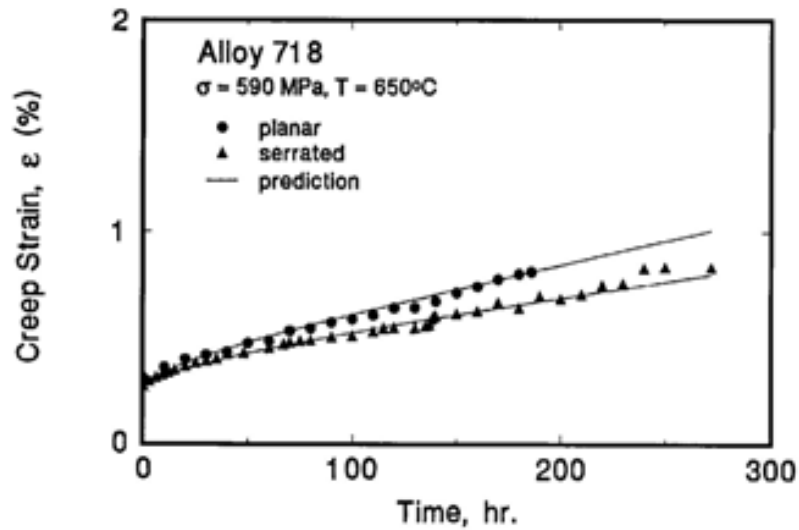


Fig. 16. Creep curves of Alloy 718 with planar and triangular wave grain boundaries, as predicted by Eq. (37) (Wu & Koul, 1997).

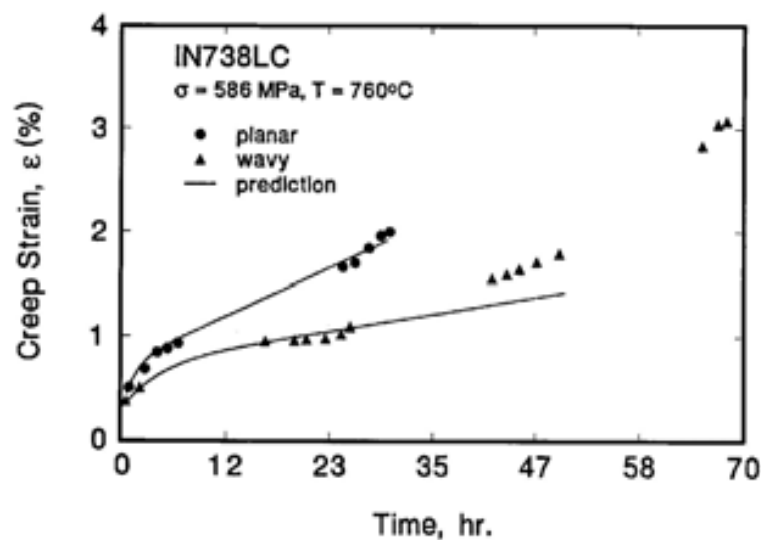


Fig. 17. Creep curves of IN738LC with planar and sinusoidal wave grain boundaries, as predicted by Eq. (37) (Wu & Koul, 1997).

where M is the normalized dislocation multiplication factor. The integration of Eq (41) leads to the following strain-time relation:

$$\varepsilon_s = \frac{1}{M} [\exp(M\dot{\varepsilon}_i t) - 1] \quad (42)$$

Then, adding the strain contributions from Eq. (37) and (42) together, according to Eq. (1), we obtain the total creep strain as

$$\varepsilon = \varepsilon_0 + \phi \dot{\varepsilon}_{ss} t + \frac{\sigma}{\beta^2 H} \left[1 - \exp\left(-\frac{\beta^2 \phi H \dot{\varepsilon}_{ss} t}{\sigma(\beta - 1)}\right) \right] \frac{1}{M} [\exp(M\dot{\varepsilon}_i t) - 1] \quad (43)$$

Using Eq. (43), the creep behaviour of IN738LC with and without grain boundary serration are re-analyzed with additional parameters $M = 14.3$ and $\dot{\epsilon}_i = 0.0035 \text{ h}^{-1}$, the results are shown in Fig. 18. The agreement with experimental observation is corroborated with the physical rationale that the two IN738LC materials have nearly the same intragranular microstructure in terms of γ' precipitate size and volume fraction but different grain boundary morphology.

During tertiary creep, intragranular deformation may overshadow GBS by the mere amount of strain accumulation, but grain boundary damage may still occur under stress, which limits the creep rupture life, as indeed most creep rupture occurs intergranularly in polycrystalline materials. Wu & Koul (1996) have summarized the grain boundary damage accumulation processes via cavitation and oxidation.

Continuous cavity nucleation and growth has been described by (Raj & Ashby, 1975):

$$A(t) = \rho_c(t)\pi r_c^2 + 2\pi \int_0^t \int_0^t r(t-\zeta)\dot{r}(t-\zeta)\dot{\rho}_c(\tau)d\zeta d\tau \quad (44)$$

where r_c is the critical nucleation radius, $\rho_c(t)$ is the void density and $r(t)$ is the cavity radius at time t .

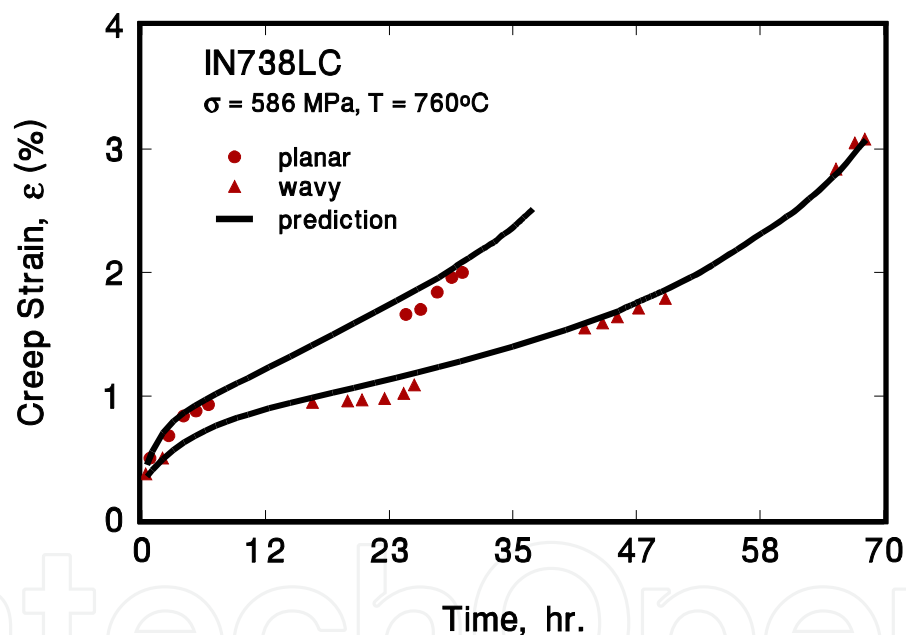


Fig. 18. Creep curves for IN738LC with planar and serrated grain boundaries, as predicted by Eq. (43) (Wu & Koul, 1996).

As a first approximation, we assume a constant cavity density and only consider the growth of these cavities, the cavity growth rate is approximately equal to $\dot{r} = \dot{\epsilon}_{ss}d$ (note that it is the GBS deformation component that dominates the steady-state creep rate in this case). If we define the creep damage parameter as $\omega = A/\pi d^2$, and the rupture time is reached at $\omega = \omega_{cr}$, then $t_r \propto 1/\dot{\epsilon}_{ss}$. The creep behaviour of wrought Alloy 718 with planar (the SHT material) and triangular-wave (the MHT material) grain boundaries at 650 °C under stress of 593 MPa were reported (Chang et al., 1992), as shown in Fig. 19. The average rupture time of the SHT material was 450 hours. The grain boundary wave factor ϕ for the MHT material is 0.7 with $h = 2 \mu\text{m}$ and $\lambda = 10 \mu\text{m}$ (Table 3). Based on the above consideration, the creep life of the

MHT material is estimated to be $t_{rMHT} = t_{rSHT}/\phi = 642$ hours under the given test condition, which is very close to the experimental observation. This proves that indeed the transient creep and creep life is limited by GBS.

Another mechanism for grain boundary damage is gaseous environmental attack – normally at high temperatures – oxidation. Suppose that oxygen penetrates the material inward through a parabolic law until the oxide scale is broken by deformation, the rate of oxide cracking can be expressed as

$$\left. \frac{dx}{dt} \right|_{ox} = \left(\frac{2D\dot{\epsilon}_{gbs}}{\epsilon^*} \right)^{\frac{1}{2}} \quad (45)$$

where x is the oxide crack length, D is a diffusion constant, and ϵ^* is the fracture strain of the oxide.

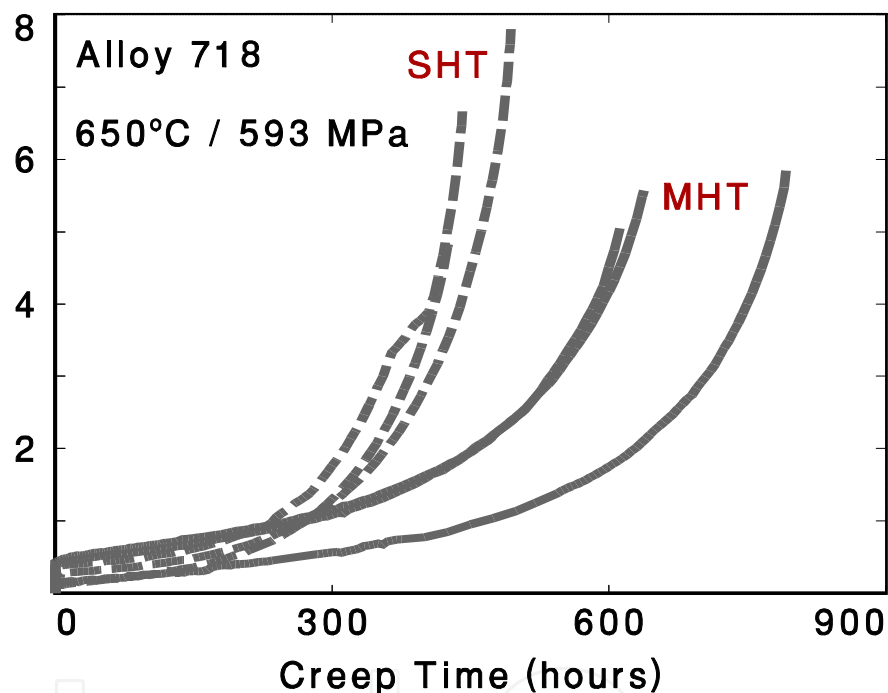
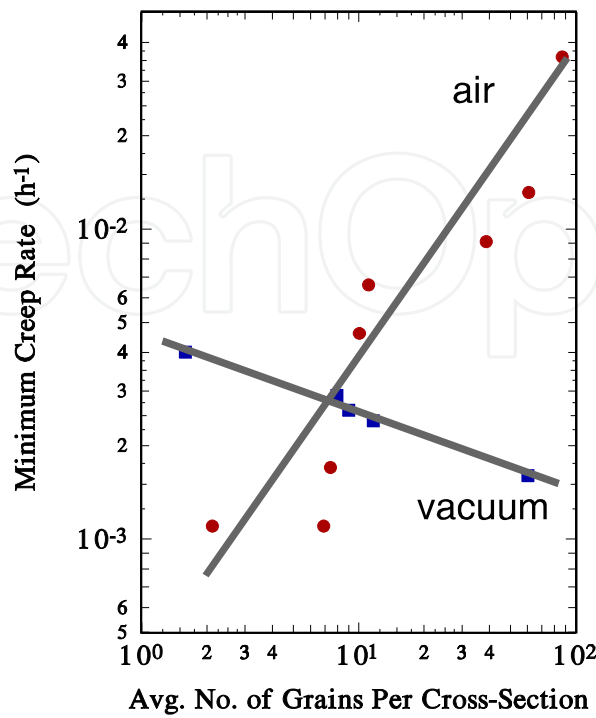


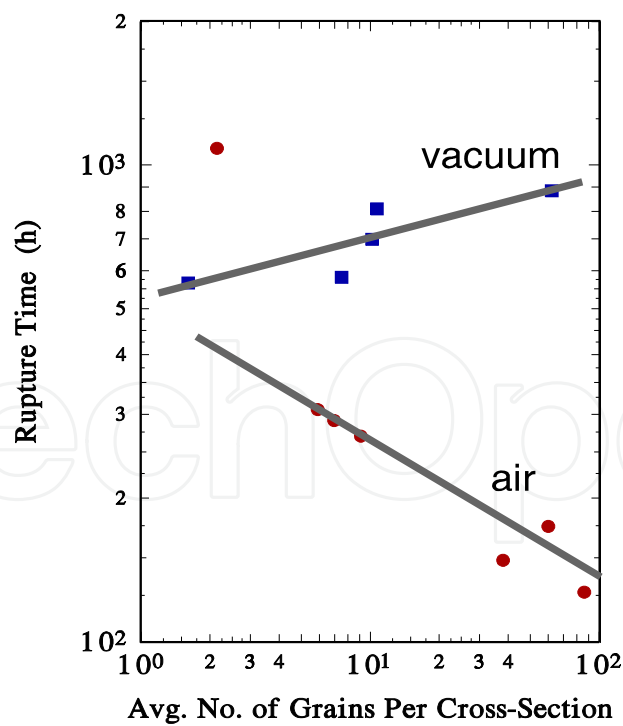
Fig. 19. Creep curves for standard and damage tolerant microstructures of Alloy 718 (Chang et al. 1992).

Sessions et al. (1977) studied the creep-oxidation interaction in Udimet 700. By re-plotting their data on the log-log scale as shown in Fig. 20, we can see that the creep rate in air increases and the rupture time decreases with the number of grains per cross-section. The air-tested creep rate increases linearly with the number of grains per cross section, and hence it follows the relationship of $\dot{\epsilon}_{min} \propto 1/d$, but the life is inversely proportional to \sqrt{d} , which implies a GBS phenomenon, as predicted by Eq. (45). Suppose that GBS occur at nearly a constant rate for most of the material's creep life, when the oxide crack reaches a critical length, then Eq. (45) would lead to $t_r \propto 1/\sqrt{\dot{\epsilon}_{min}}$. Therefore, we would expect that $t_r \propto \sqrt{d}$. In Fig. 20, the rupture time decreases with the number of grains per cross-section with a power of $-1/2$. This observation can be directly translated to the above statement, considering that the number of grains per cross-section is inversely proportional to the grain

size d for fixed specimen geometry. Therefore, Eq. (45) is suitable for describing the oxidation damage during creep.



(a)



(b)

Fig. 20. (a) Minimum creep rate data and (b) rupture life data for Udimet 700 at 927°C and 172 MPa, in air and vacuum.

To overcome the weakness of grain boundaries which are susceptible to cavitation and oxidation, advanced turbine blade and vane alloys are made from directionally-solidified (DS) and single crystal (SX) N-base superalloys, which are generally casted in the $\langle 001 \rangle$ crystal direction with the lowest modulus and hence the best tolerance to thermal fatigue. With the removal of grain boundaries, the creep behaviour of DS and SX alloys is therefore mainly a result of intragranular deformation. The majority of the creep life of DS and SX Ni-base superalloys is spent in the tertiary stage with a creep ductility in the order of 20~30%. Therefore, Eq. (42) is appropriate to describe the creep behaviour of such alloys, or in other words, ignore grain boundary sliding (GBS) from Eq. (43).

Now, let

$$\dot{\epsilon}_i = A_0 \exp\left(-\frac{\Delta G}{kT}\right) \sinh\left(\frac{V(\sigma - \sigma_0)}{kT}\right) \quad (46)$$

where A_0 is the pre-exponential constant, ΔG is the activation energy, V is the activation volume, σ_0 is the back stress, k ($=1.38 \times 10^{-23} \text{ J}\cdot\text{K}^{-1}$) is the Boltzmann constant, and T is the absolute temperature.

The creep behaviors of CM247LC, a DS alloy, at various stresses and temperatures are described with Eq. (42) and (46), with the parameters given in Table 4, as shown in Fig. 21. The model agrees well with the experimental creep behavior of CM247LC. The creep data at 225MPa/950°C (Satyanarayana et al., 2008), 560MPa/840°C (DeMestral et al., 1996), and 180MPa/1030°C (Kolbe et al., 1999) were used for calibration of the model to determine the parameter values of the model. One creep curve was calculated to predict the creep rupture response at 186MPa/982°C with an observed life of 120 hr. The model prediction is very close to the experimental observation. Using the same approach, the model can also be applied to SX alloys.

In summary, by the deformation decomposition rule, Eq. (1), the total creep strain is equal to the sum of intragranular strain and GBS strain. A schematic creep curve is shown in Fig. 22 by adding the two components. It should be recognized that the total (observed) secondary or minimum creep rate consists of both GBS and intragranular contributions with varying degrees, depending on the material's microstructure, the applied stress and temperature. Therefore, creep life assessment based on the measured minimum creep rates may be erroneous by extrapolating short-term test data for long-term lifetime prediction, since most short-term creep tests conducted at high stresses would induce a large amount of intragranular deformation that over shadows the true failure mechanism at grain boundaries. There are other creep-curve equations, the most similar one to Eq. (43) is the θ -projection method proposed by Evans & Wilshire (1985) as

$$\epsilon = \theta_1(1 - e^{-\theta_2 t}) + \theta_3(e^{\theta_4} - 1) \quad (47)$$

The θ -projection is purely empirical and mostly suitable for short-term creep tests where the secondary creep period is very short. Eq. (43), on the other hand, represents the total contribution from physical deformation mechanisms—GBS plus intragranular dislocation multiplication and climb, which can be linked to intergranular and transgranular crack propagation, leading to rupture. For DS and SX alloys, GBS diminishes and the intragranular deformation component dominates. Thus, Eq. (43) provides a holistic description of creep for complex engineering alloys.

A_0 (hr ⁻¹)	ΔG (J)	V (m ³)	σ_0 (MPa)	M
4.22×10^{12}	6.896×10^{-19}	2.063×10^{-28}	0	400

Table 4. Activation Parameters for the CM247LC Creep Model

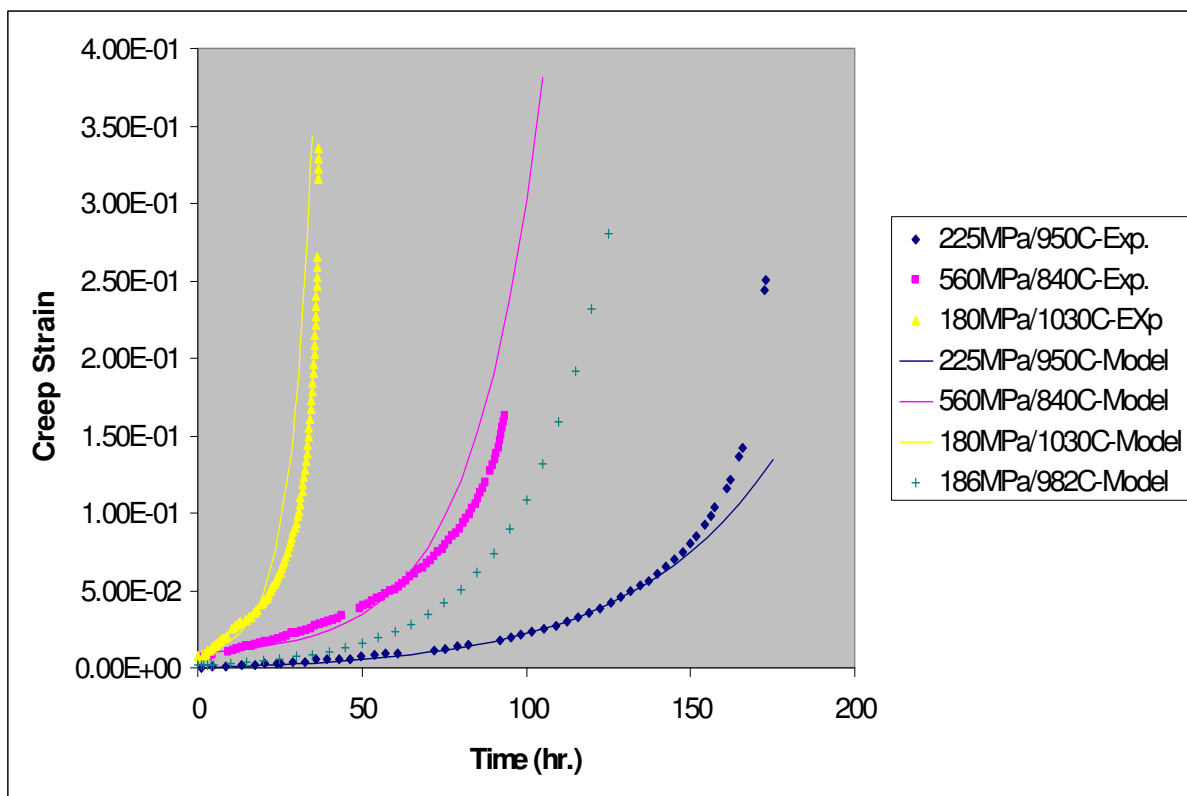


Fig. 21. Experimental and model creep curves of CM247LC.

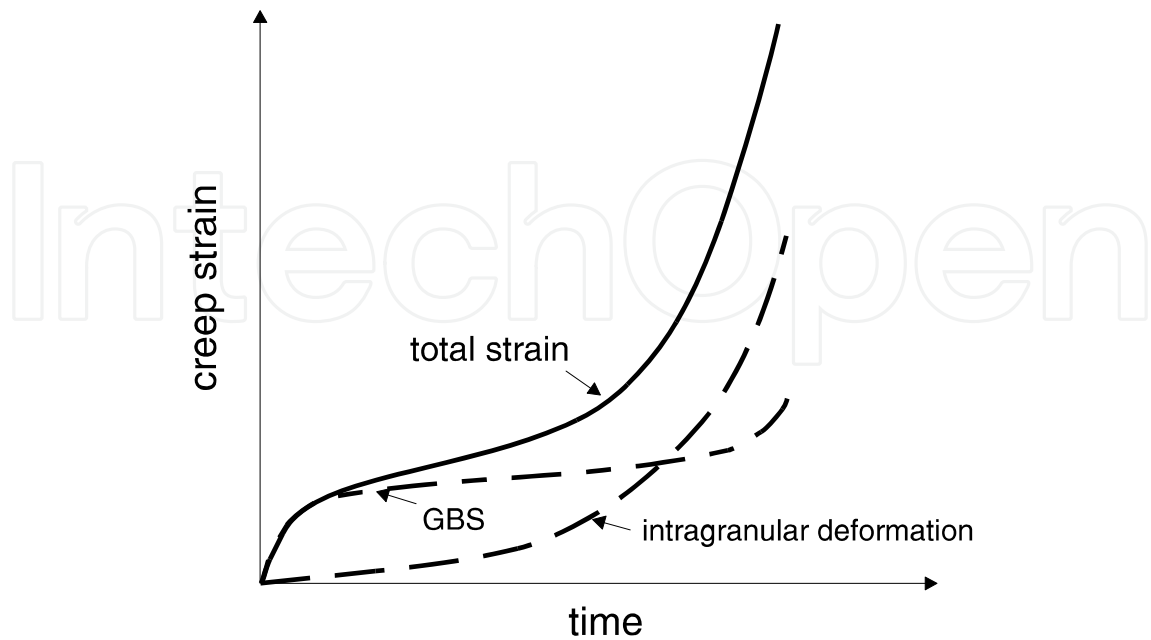


Fig. 22. Schematics of creep curves representing GBS strain, intragranular strain and the total creep strain

4. Evolution of material life under thermomechanical loading

A gas turbine engine component generally experiences thermomechanical loading during start-up/shutdown (cyclic) and cruise (steady holds) which cause thermomechanical creep-fatigue damage to the material. Researchers have been trying to develop more descriptive, more accurate, and more efficient analytical models for the dwell/creep-fatigue phenomena, in order to understand the creep-fatigue interaction for component life prediction. Existing TMF models can be largely categorized into the following three groups: 1) the linear damage accumulation model (Neu & Sehitoglu, 1989; Sehitoglu, 1992), 2) the damage-rate model (Miller, 1993), and 3) the strain-range partitioning (SRP) method (Halford et al., 1977). Recently, a holistic model of dwell/creep-fatigue has been presented (Wu, 2009b), which describes the processes of surface /subsurface crack nucleation, propagation of the dominant crack and its coalescence with internal creep cavitation damage, leading to the final fracture.

4.1 The generic TMF model

For generality, let us consider a polycrystalline material. Under thermomechanical fatigue (TMF) loading, multiple forms of damage may develop: an oxide scale forms at the material surface; cavitation develops inside the material, and fatigue damage may proceed in the form of persistent slip bands (PSB), as shown schematically in Fig. 23. Cracks may first initiate at surface flaws via intrusion/extrusion of PSB. Oxidation also occurs first at the material surface or at existing crack surfaces or a crack tip. Oxidation damage penetrates the material inwardly through diffusion processes. Subsurface cracks may also initiate at manufacturing flaws such as pores or inclusions, but they will quickly break through the surface and become surface cracks. In the mean time, creep cavities or wedge cracks may develop in the material interior, particularly along grain or interface boundaries. The life evolution process in a metallic material at high temperatures can be envisaged as nucleation of surface cracks by fatigue and/or oxidation, and inward propagation of the dominant crack, coalescing with internal cavities or cracks along its path, leading to final rupture.

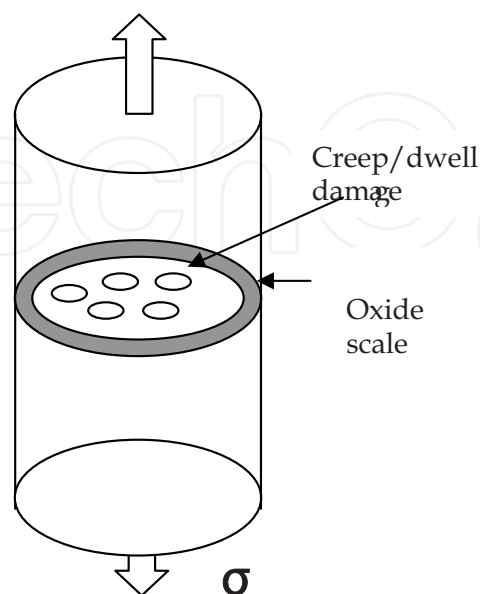


Fig. 23. A schematic of damage development in a material cross-section.

Fatigue damage can be regarded as accumulation of irreversible slip offsets on preferred slip systems. These slip offsets may occur at the surface of grains or grain boundaries or interface boundaries, which act as nuclei for cracks. Restricted slip reversal ahead of the crack tip is also recognized as the basic mechanism of transgranular fatigue crack propagation (Wu et al., 1993). Therefore, in a holistic sense, we can use the term da/dN to represent both the rate of accumulation of irreversible slip offsets leading to crack nucleation as well as the fatigue crack growth rate, bearing in mind that the functional dependencies of da/dN on the loading parameters are different for crack nucleation and crack growth.

On the other hand, creep damage may develop in the forms of cavities and/or wedge cracks (Baik & Raj, 1982). Cavity growth has been recognized as a diffusion phenomenon, whereas wedge cracking is a result of dislocation pile-up, also called Zener-Stroh-Koehler (ZSK) crack. The coalescence of creep/dwell damage with a propagating fatigue crack will result in a total damage accumulation rate as expressed by

$$\frac{da}{dN} = \left(\frac{da}{dN} \right)_f + \frac{l_c + l_z}{\Delta N} \quad (48)$$

where l_c is the collective cavity size per grain boundary facet, l_z is the ZSK crack size, ΔN is the number of cycles during which the fatigue crack propagates between two cavities or between two ZSK cracks separated by an average distance of λ ($\lambda \sim$ grain size or grain boundary precipitate spacing). Note that usually creep cavitation occurs at a high temperature and ZSK cracks occur at a relatively low temperature. These two types of damage usually do not occur at the same time. Here they are added together as competitive mechanisms over the entire temperature range from ambient temperature to near melting temperature.

Assume that during the period of ΔN , the dominant crack only propagates by pure fatigue, i.e., $da/dN \sim \lambda/\Delta N$, then we can rewrite Eq. (48), as

$$\frac{da}{dN} = \left(1 + \frac{l_c + l_z}{\lambda} \right) \left(\frac{da}{dN} \right)_f \quad (49)$$

With environmental effects such as oxidation contributing to propagation of the dominant crack in a cycle-by-cycle manner, the total crack growth rate is

$$\frac{da}{dN} = \left(1 + \frac{l_c + l_z}{\lambda} \right) \left\{ \left(\frac{da}{dN} \right)_f + \left(\frac{da}{dN} \right)_{env} \right\} \quad (50)$$

4.2 Cold-dwell fatigue

Cold-dwell fatigue usually refers to fatigue with hold-times at ambient temperatures, and it could cause significant low cycle fatigue (LCF) life reduction, particularly pronounced in high strength titanium alloys such as IMI 685, IMI 829 and IMI 834, and Ti6242. Dwell fatigue of titanium alloys is often accompanied with faceted fracture along the basal planes of the α phase, as seen in Fig. 24.

It has been perceived that the faceted fracture of α grains is driven by dislocation pile-up (Bache et al., 1997). Wu & Au (2007) have treated the problem in terms of the kinetics of Zener-Stroh-Koehler crack formation.

First of all, it should be recognized that the rate of dislocation pile-up accumulation is the net result of dislocation arriving by glide and leaving by climb in a unit time, which can be expressed as

$$\frac{dn}{dt} = \rho vs - \kappa n \quad (51)$$

where ρ is the dislocation density, v is the dislocation glide velocity, s is the slip band width, κ is the rate of dislocation climb, and n is the number of dislocations in a pile-up at time t .

According to the Orowan relationship, $\dot{\gamma}_p = \rho bv$ ($s \approx b$), Eq. (51) can be rewritten as

$$\frac{dn}{dt} = \dot{\gamma}_p - \kappa n \quad (52)$$

The number of dislocations in a pile-up at a steady-state can be obtained by integration of Eq. (52), as

$$n = \frac{\dot{\gamma}_p}{\kappa} [1 - \exp(-\kappa t)] \quad (53)$$

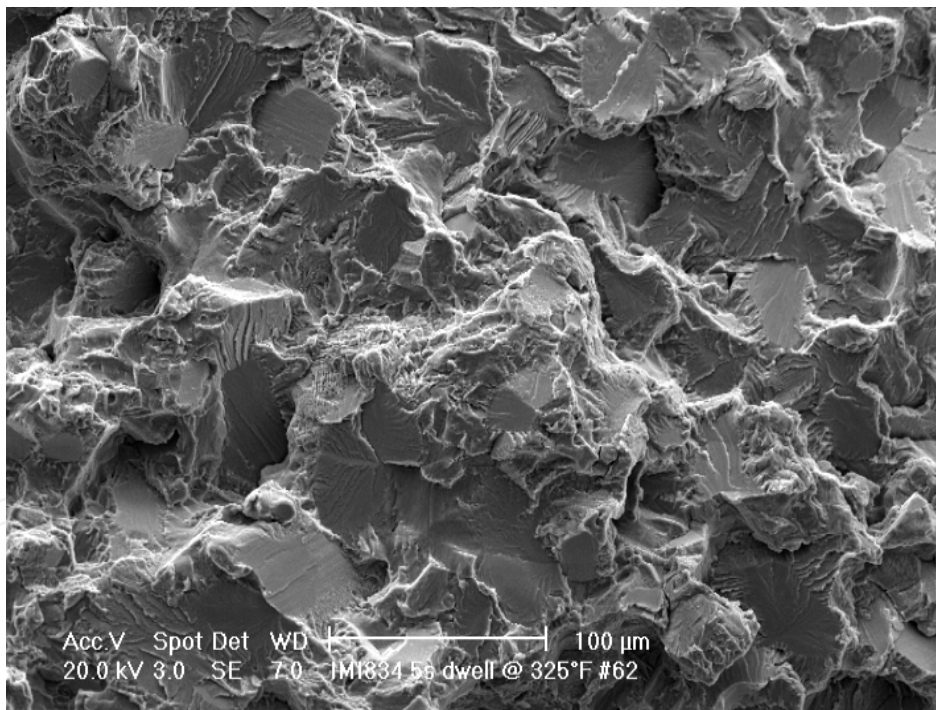


Fig. 24. A SEM micrograph of the fracture surface of IMI 834 failed by dwell fatigue

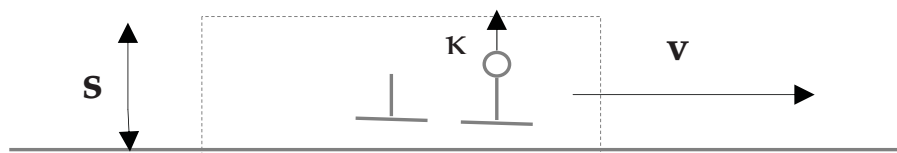


Fig. 25. Schematic of the kinetic process of dislocation pile-up.

Note that the energy release rate of a ZSK crack in an anisotropic material is given by (Wu, 2005)

$$G = \frac{1}{2} K_i F_{ij}^{-1} K_j = \frac{b_T^{(i)} F_{ij} b_T^{(j)}}{8\pi a} \quad (54)$$

where F_{ij} is an elastic matrix for anisotropic materials ($F_{11} = F_{22} = \mu/(1-\nu)$, $F_{33} = \mu$, μ —shear modulus, for isotropic materials), and $b_T = nb$ is the total Burgers vector in the pile-up group. Considering an average slip band angle of 45° , the dislocation pile-up may create a mix-mode I-II crack, by the Griffith's criteria:

$$\frac{\bar{F}_{22} b_T^2}{8\pi a} = 4w_s \quad (55)$$

where w_s is the surface energy, and $\bar{F}_{22} = (F_{11} + F_{22})/2$ is the average modulus. From Eq. (55), we can find the crack size $l (=2a)$ as

$$l = \frac{\bar{F}_{22} n^2 b^2}{16\pi w_s} \quad (56)$$

Substituting Eq. (53) into Eq. (56), we obtain

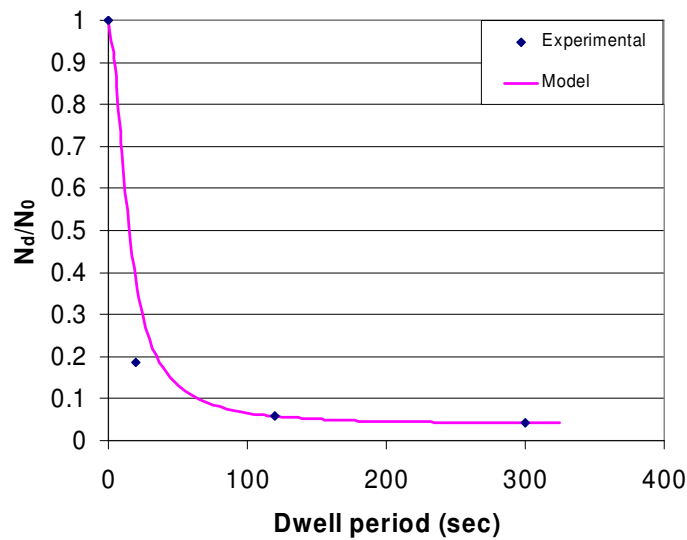
$$l_z = \frac{\bar{F}_{22} b^2}{16\pi w_s} \left(\frac{\dot{\gamma}}{\kappa} \right)^2 [1 - \exp(-\kappa\tau)]^2 \quad (57)$$

For constant amplitude fatigue with a constant holding period, substituting Eq. (57) into (49) and neglecting cavity formation, the integration of Eq. (49) leads to

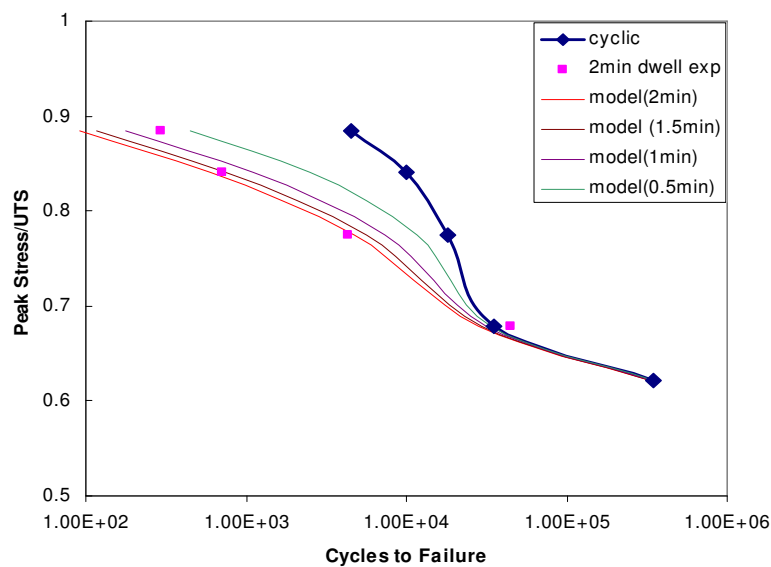
$$N = \frac{N_f}{\left(1 + \frac{\bar{F}_{22} b^2}{16\pi\lambda w_s} \left(\frac{\dot{\gamma}}{\kappa} \right)^2 [1 - \exp(-\kappa\tau)]^2 \right)} \quad (58)$$

Equation (58) shows that the fatigue life is knocked down by a factor greater than one, when a dwell period is imposed on fatigue loading. This “knock down” factor depends on the material properties such as elastic constants, surface energy, and microstructure (λ), and most importantly it is controlled by the ratio of dislocation glide velocity to the climb rate in the material. This means that, if damage occurs in the form of dislocation pile-up, the dwell-effect will be more detrimental when the ratio of dislocation glide to climb is large, particularly in materials with fewer active slip systems at low temperatures. As temperature increases, climb will overwhelm glide such that dislocation pile-up can hardly form, and hence the dwell damage becomes minimal, but cavities may start to grow. Basically, this is the essence of “cold dwell” vs. “hot creep”.

Bache et al. (1997) studied IMI834 and plotted the dwell fatigue life as function of dwell time and stress as shown in Figure 26 (a) and (b), respectively. The model, Eq. (58), describes the experimental behaviour very well. It shows that the dwell sensitivity, in terms of the ratio of dwell-fatigue life to the pure fatigue life, indeed follows an exponential function. Hence, given the pure fatigue life as the baseline, dwell fatigue life can be predicted, as shown in Figure 26 (b), in the form of S-N curves.



(a)



(b)

Fig. 26. Comparison of Eq. (58) with the experimental data on IMI 834 (Bache et al., 1997): a) normalized dwell fatigue life as a function of dwell time, b) S-N curves with different dwell times.

4.3 Creep-Fatigue

Creep-fatigue interaction refers to the effect of cyclic-hold interactions at high temperatures where creep damage can be significant. The simplest and hitherto the most popular way to count for the total accumulated damage is to combine Miner and Robinson's rules (Miner, 1945; Robinson, 1952), as

$$\sum \frac{N_i}{N_{fi}} + \sum \frac{t_j}{t_{rj}} = 1 \quad (59)$$

where N_{fi} is the pure fatigue life at the i th cyclic stress or strain amplitude, and t_{ij} is the creep rupture life at the j th holding stress level. The linear summation rule, as straightforward as it may be, is purely empirical and based on no physical mechanism. It does not differentiate the time spent under stress-control or strain-control conditions, or in tension or compression whatsoever, which causes different material response as stress relaxation vs. strain relaxation (creep). Many experimental investigations have shown that the fatigue life fraction vs. creep life fraction does not obey a linear relationship, as prescribed by Eq. (59), as cited by Viswanathan (1989).

Other creep-fatigue models were also proposed such as the frequency modified equation (Coffin, 1969), the hysteresis energy model (Ostergren, 1976), and the strain range partitioning (SRP) approach (Halford et al., 1977). Instead of modifying empirical equations with empirical factors accounting for the frequency effect, the SRP method tried to rationalize the complex creep-fatigue phenomena with the partition of four components in the total inelastic strain range: 1) plastic strain reversed by plasticity, $\Delta\varepsilon_{pp}$; 2) creep strain reversed by creep, $\Delta\varepsilon_{cc}$; 3) plastic strain reversed by creep, $\Delta\varepsilon_{pc}$; and 4) creep strain reversed by plasticity, $\Delta\varepsilon_{cp}$. A schematic of the occurrence of these strain components is shown in Fig. 27. Then, the total failure life is expressed as

$$\frac{1}{N} = \frac{F_{pp}}{N_{pp}} + \frac{F_{cc}}{N_{cc}} + \frac{F_{pc}}{N_{pc}} + \frac{F_{cp}}{N_{cp}} \quad (60a)$$

where

$$N_{ij} = D_{ij} \Delta\varepsilon_{ij}^{c_{ij}} \quad (60b)$$

F_{ij} is the fraction of the named strain component, and N_{ij} is the number of cycles to failure if the entire inelastic strain is comprised of the named strain only, where D_{ij} and c_{ij} are the Manson-Coffin constants. The problem of this approach with respect to life prediction is that the actual partition of these strain components is difficult to determine within the total strain range imparted to the component by a random loading cycle.

Considering physically that the total inelastic strain, ε_{inv} is comprised of intragranular deformation, ε_g , and grain boundary sliding (GBS), ε_{gbs} , as given by Eq. (1), we further assume that under cyclic-time hold conditions:

1. The intragranular deformation, when proceeds in a cyclic manner, leads to transgranular damage accumulation, such as persistent slip bands and fatigue cracking, and therefore, it is equivalent to the pp strain under cyclic conditions.
2. For short-period holds, cc, pc and cp types of inelastic strains are contributed mainly from GBS during the transient creep, since purely tertiary creep would never start upon short cycle repeats. GBS contributes to intergranular fracture.

When GBS operates, the accumulation of grain boundary damage, either in the form of cavity nucleation and growth or as grain boundary cracks, is proportional to the GBS displacement, such that

$$l_c = \varepsilon_{gbs} d \quad (61)$$

where d is the grain size.

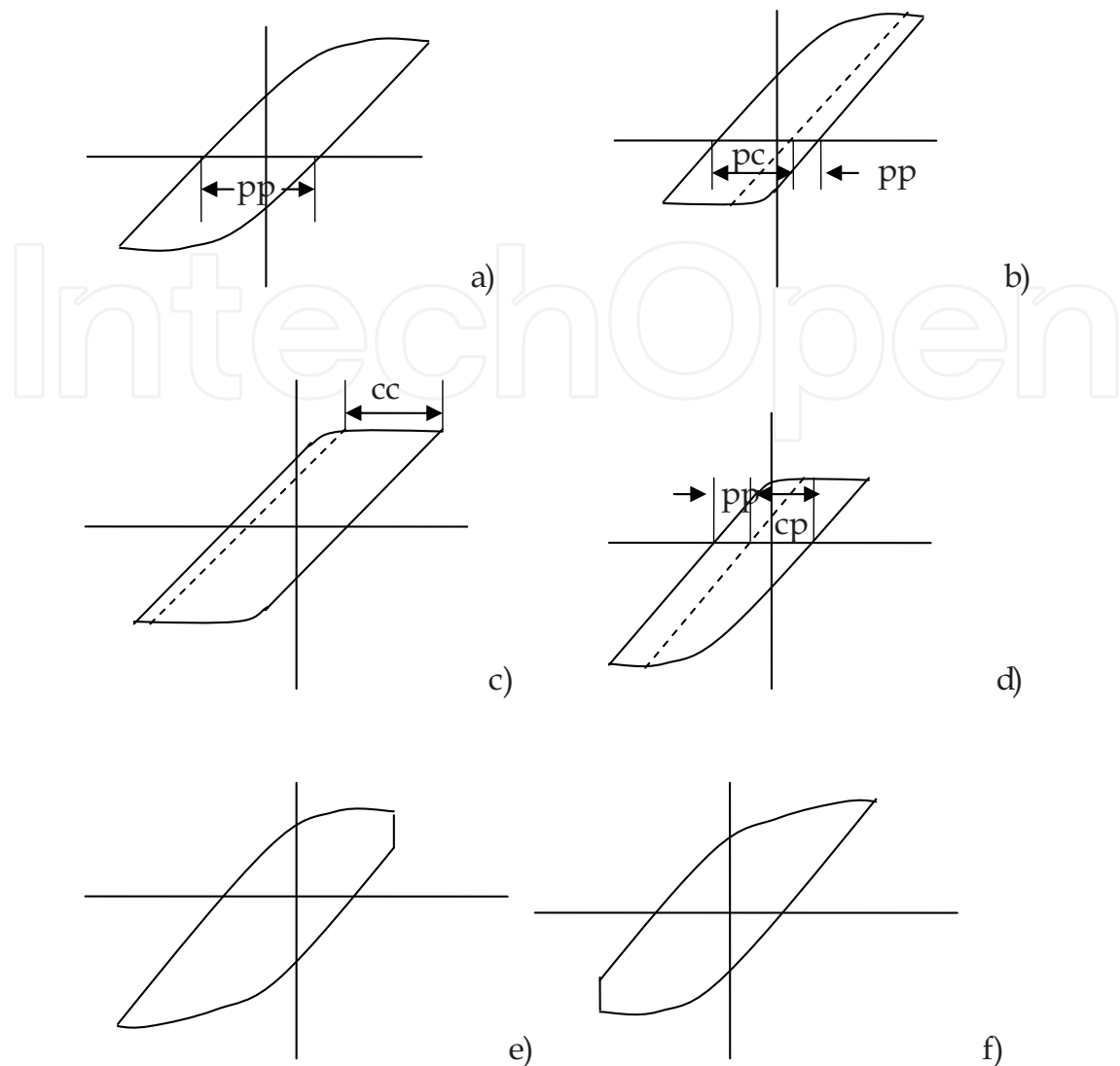


Fig. 27. The SRP cycle profiles: a) High Rate Strain Cycle (HRSC) – constant ramping in tension and compression; b) Compressive Cyclic Creep Rupture (CCCR) – ramped to a predetermined stress with compressive creep hold; reversed ramping to equal tensile strain; c) Balanced Cyclic Creep Rupture (BCCR) – creep holds in tension and compression at constant load until specific strain reached; d) Tensile Cyclic Creep Rupture (TCCR) – opposite cycle to CCCR with tensile hold; e) Tensile Hold Strain Cycle (THSC) – ramped to specific strain, stress relaxation followed by reversed ramping to equal compressive strain; f) Compressive Hold Strain Cycle (CHSC) – opposite to THSC with compressive stress relaxation.

Under cyclic creep conditions as imposed by strain controlled cycles, l_c can be stabilized once the entire hysteresis behavior is stabilized. Therefore, again under constant amplitude cycling conditions, Eq. (49) can be integrated to (in this case, neglecting dislocation pile-ups, i.e., let $l_z = 0$):

$$N = \frac{N_f}{1 + \frac{\varepsilon_{gbs} d}{\lambda}} \quad (62)$$

As discussed in section 3.1, the pure LCF life, N_f , is correlated to $\Delta\varepsilon_g$ through Eq. (25), as:

$$\Delta\varepsilon_g = CN_f^{-1/2} \quad (63)$$

which can be established by HRSC tests.

For application of Eq. (62) to the asymmetrical creep-fatigue interaction tests such as CCCR, TCCR, THSC and CHSC, it should be recognized that, due to reversed plasticity, each individual grain is fatigued by the entire inelastic strain range, but GBS contributes to the effect of additional intergranular fracture. Since GBS operates in shear, it may produce grain boundary damage during either uniaxial tension or compression. Table 5 summarizes the strain partitioning of $\Delta\varepsilon_g$ and $\Delta\varepsilon_{gbs}$ for the different creep-fatigue interaction tests.

We take the data from a NASA contract report (Romannoski, 1982) and re-establish the strain partitioning rule, according to Eq. (1), as outlined in Table 5, the creep-fatigue interaction can be described by Eq. (62) for Rene 80 (in high vacuum) and IN100 (coated) as shown in Table 6 and 7, in comparison with the experimental data. For the bulk failure of these two materials under the test conditions, environmental effects can be neglected. The results are also shown in Fig. 28 and Fig. 29, respectively.

Test Type	$\Delta\varepsilon_g$	$\Delta\varepsilon_{gbs}$
HSRC	pp	0
CCCR	pp+pc	pc
TCCR	cp+cp	cp
BCCR	pp	cc
THSC	pp+cp+cc	$\Delta\sigma/E^*$
CHSC	pp+pc+cc	$\Delta\sigma/E^*$

*Note that $\Delta\sigma$ is the range of stress drop during stress relaxation in this test.

Table 5. The Strain Partitioning Concept

Spec. ID	Test	$\Delta\varepsilon_g$	$\Delta\varepsilon_{gbs}$	N_f	N	Exp.
74-U-pp-13	HRSC	0.605	0	175	175	145
21U-pp-8	HRSC	0.322	0	617	617	642
41U-pp-10	HRSC	0.179	0	1997	1997	1410
22U-pp-9	HRSC	0.026	0	94675	94675	163533
42U-pp-11	HRSC	0.051	0	24606	24606	217620
92U-pc-13	CCCR	0.554	0.46	209	45	41
28U-pc-9	CCCR	0.378	0.283	448	137	149
91U-pc-12	CCCR	0.257	0.209	969	363	356
98U-pc-16	CCCR	0.258	0.183	961	390	396
29U-pc-10	CCCR	0.204	0.164	1538	665	1415
112U-cp-11	TCCR	0.385	0.308	432	125	101
86U-cp-9	TCCR	0.289	0.306	766	222	147
30U-cp-5	TCCR	0.289	0.254	766	253	193
31U-cp-6	TCCR	0.208	0.202	1479	565	530
36U-cp-7	TCCR	0.111	0.092	5194	2992	3705

Table 6. Rene 80 at 871°C ($C=0.08$, $d/\lambda=8$)

Spec. ID	Test	$\Delta\varepsilon_g$	$\Delta\varepsilon_{gbs}$	N_f	N	Exp.
7	HRSC	0.129	0	796	796	635
6	HRSC	0.121	0	905	905	900
1	HRSC	0.138	0	696	696	1260
2	HRSC	0.086	0	1792	1792	2120
3	HRSC	0.059	0	3806	3806	3670
4	HRSC	0.05	0	5300	5300	9460
5	HRSC	0.031	0	13788	13788	12210
10	HRSC	0.026	0	19601	19601	17340
8	HRSC	0.028	0	16901	16901	27260
11	HRSC	0.014	0	67602	67602	48320
N12	CHSC	0.196	0.03375	345	128	250
N10	CHSC	0.105	0.02	1202	601	764
N9	CHSC	0.102	0.019375	1274	647	944
39	THSC	0.18	0.026875	409	174	239
N8	THSC	0.08	0.016875	2070	1123	1495
54	BCCR	0.09	0.168	1636	174	159
N5	BCCR	0.085	0.16	1834	204	200
56	BCCR	0.054	0.11	4544	699	383

Table. 7. IN 100(Coated) at 900°C ($C=0.0364$, $d/\lambda=50$)

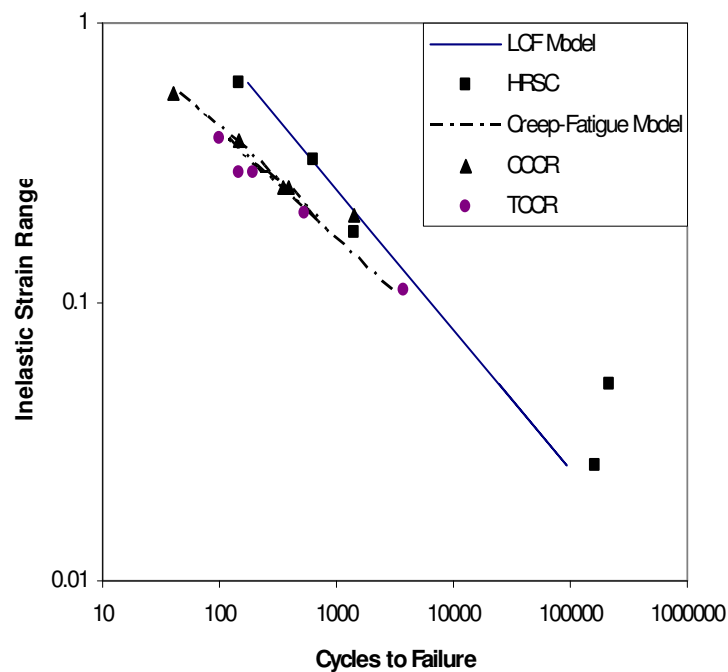


Fig. 28. Comparisons of Eq. (62-63) with experimental data for Rene 80 at 871°C

It has been shown that Eq. (62-63) can describe well the creep-fatigue interaction in complicated loading cycles. The advantage of this physics-based strain decomposition model is that, once calibrated with coupon data, it can be applied to component life prediction with ε_g and ε_{gbs} values evaluated from the constitutive model as presented in section 2. Mathematically, it unifies the SRP concept with the physical meaning that $\Delta\varepsilon_g$ represents the intragranular damage and $\Delta\varepsilon_{gbs}$ contributes to the intergranular fracture, thus it provides a complete description for the mix mode fracture.

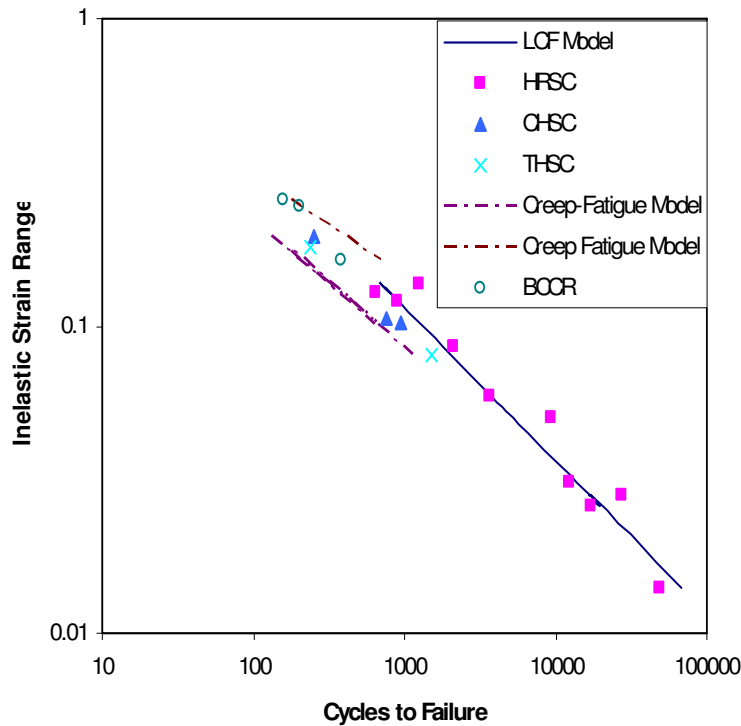


Fig. 29. Comparisons of Eq. (62-63) with experimental data for IN 100 (coated) at 1000°C.

4.4 Fatigue-Oxidation

When gas turbine components operate in a hot gas environment, an oxide scale typically forms on the material surface. This layer of oxide will be forced to deform compatibly with the substrate until it breaks, which may lead to premature crack nucleation. The stresses in both the substrate and oxide scale can be determined, by deformation compatibility:

$$\frac{\sigma_{ox}}{E_{ox}} + \alpha_{ox}(T - T_o) = \frac{\sigma_s}{E_s} + \alpha_s(T - T_o) \tag{64}$$

and, by the force equilibrium

$$\sigma_{ox}f + (1 - f)\sigma_s = \sigma \tag{65}$$

where σ_{ox} is the stress in the oxide scale, E_{ox} is the elastic modulus and α_{ox} is the thermal expansion coefficient of the oxide scale ($\sim 8\mu\text{m/mK}$ for Al_2O_3), σ_s is the stress in the substrate, E_s is the elastic modulus and α_s is the thermal expansion coefficient of the substrate material ($\sim 14\mu\text{m/mK}$ for Ni base superalloys), and f is the volume fraction of the oxide scale, T_o is the reference temperature at which the oxide formation is stress free. From the above relations, we can deduce that

$$\sigma_{ox} = \frac{E_{ox}}{fE_{ox} + (1 - f)E_s} [\sigma + (1 - f)E_s(\alpha_s - \alpha_{ox})(T - T_o)] \tag{66}$$

In Ni-base superalloys, the oxide, e.g., Al_2O_3 , may form with a negligible volume fraction, i.e., $f \ll 1$, but usually has a higher modulus than the substrate. Therefore, according to Eq.

(66), oxides act as stress raisers at the surface (multiplied by E_{ox}/E_s). During a TMF cycle, the oxidation stress may change with temperature.

Suppose the oxide growth follows a parabolic relation, as

$$h = \sqrt{2kt} \quad (67)$$

Neglecting other damage, i.e., $l_c = l_z = 0$, then, from Eq. (50), the fatigue-oxidation interaction results in the crack growth rate as:

$$\frac{da}{dN} = \left[\left(\frac{da}{dN} \right)_f + h_c \right] \quad (68)$$

where h_c is the critical penetration length.

If we normalize the crack length with the critical crack length, a_{cr} , Eq. (68) should become

$$\frac{d\phi}{dN} = \left[\left(\frac{d\phi}{dN} \right)_f + \frac{h_c}{a_{cr}} \right] \quad (69)$$

where a_{cr} is defined by

$$a_{cr} = \frac{1}{\pi} \left(\frac{K_{IC}}{Y\sigma} \right)^2 \quad (70)$$

K_{IC} is the material fracture toughness, Y is the crack configuration factor.

Consider, for example, IN738, the pure mechanical fatigue component has been described by Eq. (25) in section 3.1. With oxidation kinetics as described by Eq. (69) and the diffusion constant given by Neu & Sehitoglu (1989), the life prediction for IN738 LCF at 900°C LCF is shown in Fig. 30. Here, for simplicity, the shape factor Y is assumed to be unity and the fracture toughness is 60 MPa \sqrt{m} . The prediction agrees well with the experimental data. As the comparison shows, the high temperature effect on LCF and TMF life of IN738 can largely be attributed to oxidation. Some OP and DP TMF data are also shown in Fig. 30, these data fall closer to the line representing the oxidation-fatigue interaction.

4.5 Summary

A nonlinear creep/dwell-fatigue-oxidation interaction model is derived based on nucleation and propagation of a surface fatigue crack, with the assistance of oxidation, and its coalescence with creep/dwell damages (cavities or wedge cracks) along its path inside the material.

The model has been shown to be successful in correlating both “cold” dwell-fatigue and “hot” creep-fatigue, as long as the respective damage accumulation processes are described based on the relevant deformation mechanism. In cold dwell, the damage is envisaged as dislocation pile-up, leading to formation of ZSK cracks. In hot creep, the damage accumulation is related to grain boundary sliding. Particularly, for creep-fatigue interaction, the model reconciles the SRP concept. Therefore, it provides a unified approach to deal with dwell/creep-fatigue interactions.

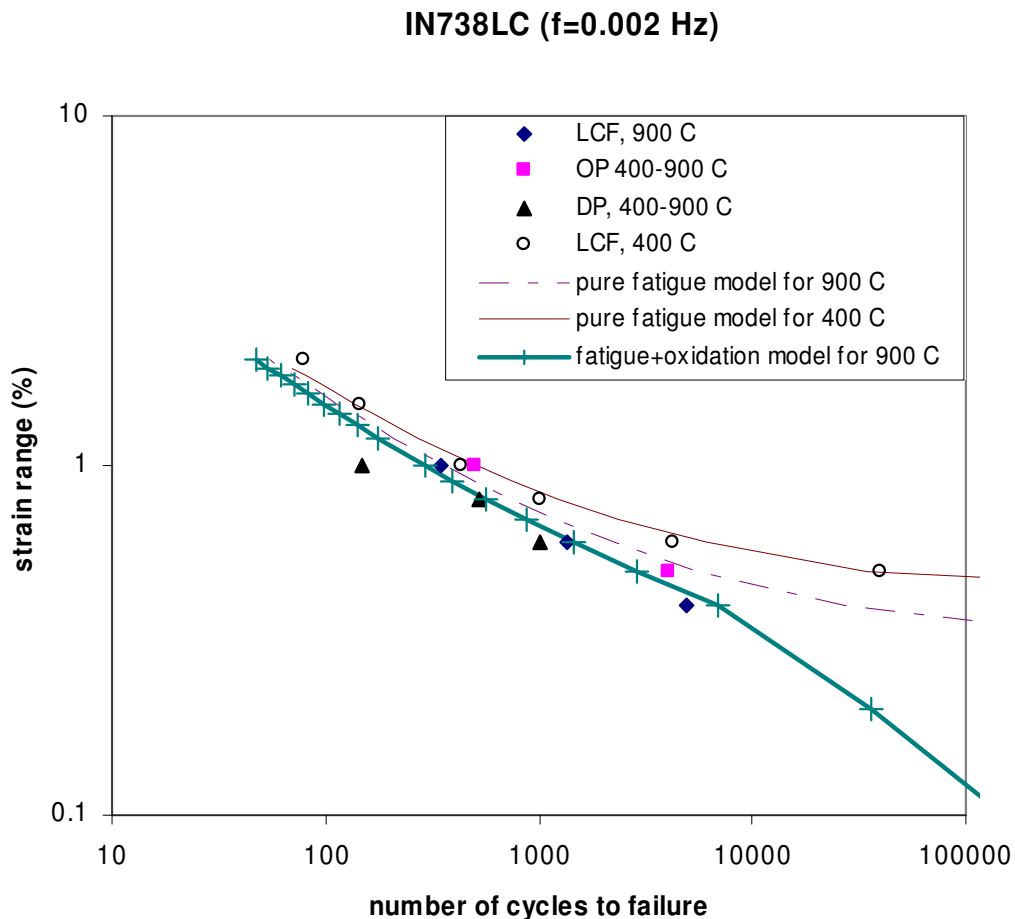


Fig. 30. Fatigue-oxidation interaction vs. pure fatigue in IN738 at high temperatures.

5. Macroscopic crack growth and damage tolerance

The previous section deals with the material life evolution under a nominal stress when the material damage state does not alter the stress distribution in a component macroscopically. This is usually called the *crack initiation life* with an engineering definition (e.g. $a < 0.03'$) acknowledging the minimum detection limit of non-destructive inspection (NDI). When the damage state presents itself as a macroscopic crack, then fracture mechanics concepts have to be used to characterize the stress-field ahead of the crack tip and the subsequent crack growth processes. Macroscopic crack growth is usually the last stage of damage accumulation leading to catastrophic fracture of components. Understanding the crack growth process is a priori for accurate prediction of crack growth life, which is very important for ensuring structural integrity of critical gas turbine components such as discs. While focusing simplified methodologies for engineering application, this section will also treat the subject with considerations of the fundamental crack growth mechanisms and deformation kinetics, keeping consistent with that discussed in the previous sections. The microstructural damage processes that contribute to crack growth always involve certain deformation mechanisms with the influence of environmental effects. Therefore, to break through the curtain of phenomenological description, one needs to relate the observed behavior to the controlling physical mechanism, using physics based crack growth models for accurate life prediction.

5.1 Fundamentals of fracture mechanics

Fracture mechanics is the theory to describe the stress problems of cracks in continuum solids. The solution is obtained by solving the stress equilibrium and strain compatibility equations with given boundary conditions and the appropriate constitutive equations (such as Hooke's law for elasticity or some power-law for plasticity). Then, the parameter derived from the crack-tip stress field or energy is used to characterize the fracture processes in engineering materials. Depending on the material and the applied condition, fracture mechanics are categorized into i) linear elastic fracture mechanics; and ii) non-linear fracture mechanics, as briefly introduced in the following.

5.1.1 Linear-Elastic Fracture Mechanics

Linear-elastic fracture mechanics (LEFM) has been developed for crack problems in elastic continua, based on the theory of elasticity. For engineering practices, it is meant to be applied to fracture of materials under the so-called *small-scale yielding* condition, that is, the crack length is much longer than the plastic zone developed ahead of the crack tip. Details of LEFM may be seen in the book—*Fracture Mechanics: Fundamentals and Applications* (Anderson, 2005).

In general, fracture, i.e., opening of the crack, may proceed in three distinguished modes: I) the opening mode, II) the in-plane shearing mode, and III) the out-of-plane shearing mode, as schematically shown in Fig. 31. In most practical cases, however, crack growth mostly proceeds macroscopically in mode I, perpendicular to the maximum principal stress.

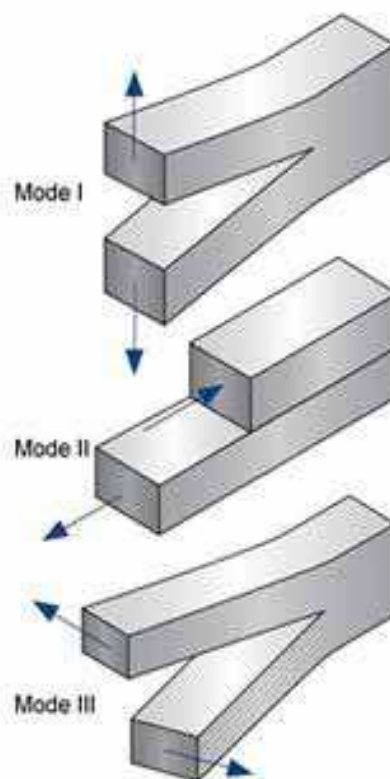


Fig. 31. A schematic of crack opening modes.

In a two dimensional (2D) crack configuration, the mode-I stress field ahead of the crack-tip (in the coordinate systems as shown in Fig. 32, where r is the distance from the crack-tip and θ is the position angle) can be expressed as

$$\sigma_{ij} = \frac{K_I}{\sqrt{2\pi r}} f_{ij}(\theta) \quad (71)$$

where K_I is the (mode-I) stress intensity factor, and $f_{ij}(\theta)$ is an angular function. For a 2D crack of length $2a$, the stress intensity factor is given by

$$K_I = Y\sigma\sqrt{\pi a} \quad (71)$$

where σ is the nominal applied stress and Y is the component geometry factor.

For a crack of elliptical shape with a short axis $2a$ and long axis $2c$, the stress intensity factor is given by

$$K_I = Y\sigma\sqrt{\frac{\pi a}{Q}} \quad (72a)$$

where

$$Q = 1 + 1.46\left(\frac{a}{c}\right)^{1.65} \quad (72b)$$

which is an approximation of the elliptical integral of the second kind to the 2nd power.

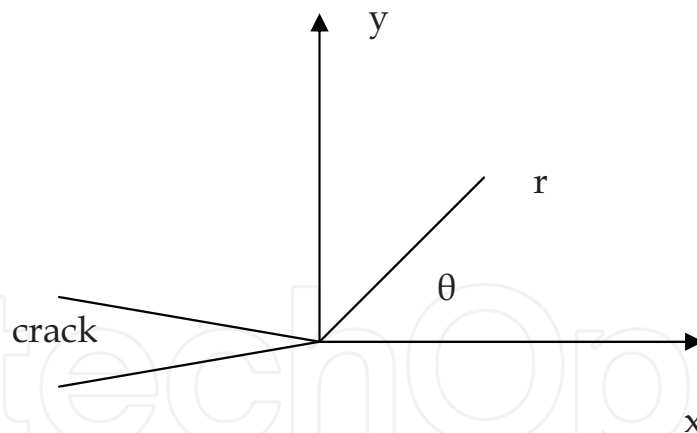


Fig. 32. The crack-tip coordinate.

K-solutions for various standard configurations have been summarized in handbooks (e.g. Tada et al. 2000). Newman & Raju (1983) have also provided numerical solutions for elliptical cracks in some standard 3D bodies. But, in most cases for cracks in engineering components, the solution is sought numerically using finite element methods, meshing for the particular component-crack geometry, which can be quite tedious and time consuming. An alternative method to extract stress intensity factors is the weight function method (Bueckner, 1970; Rice, 1972). Based on the reciprocal theorem of elasticity, this method can be used to evaluate the stress intensity factor by integrating the stress distribution with a weight function over the crack plane for an elastic body under an arbitrary loading, as:

$$K = \int_0^a \sigma(x)m(x,a)dx \quad (73)$$

where, $\sigma(x)$ is the stress distribution as induced by the remote traction T in the uncracked body, as illustrated in Fig. 33, and $m(x,a)$ is the weight function for the body. This method is rather attractive for engineering applications, since the stress distribution $\sigma(x)$ on the presumed crack plane can be readily determined using the finite element method for an engineering component, but the question is how to determine the weight function for the body?

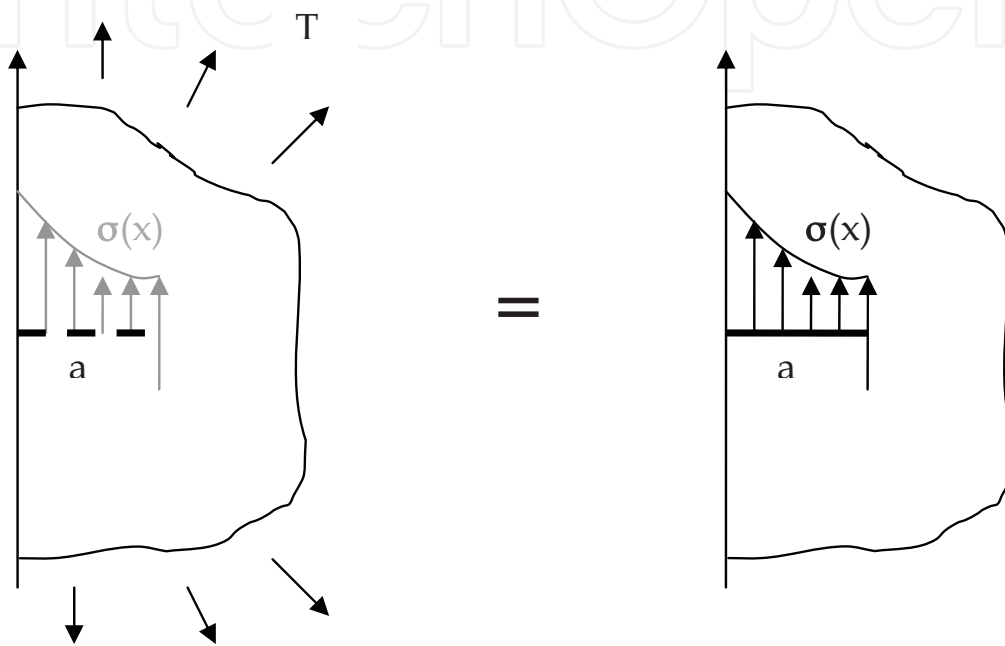


Fig. 33. Schematic illustration of the weight function method: a) stress distribution induced in the uncracked body subjected to an arbitrary remote traction T , and b) the same stress distribution loaded on the crack surface.

For two dimensional (2D) cracks, the weight function method can be generally expressed as (Bueckner, 1978; Rice, 1985)

$$K_{P'} = \iint \sigma(P(x,y))m(P,P')dA_P \quad (73)$$

where P is the integration point, P' is the crack-front point where the stress intensity factor is to be evaluated, and $m(P, P')$ is the weight function. An example for an embedded elliptical crack in an infinite solid was given by Wang et al. (1998):

$$m(x,y;P') = \frac{\sqrt{2s}}{\pi^{3/2}l^2} \sqrt{1 - \frac{s}{8\rho_1} - \frac{s}{8\rho_2} - \frac{s}{8\rho_3} - \frac{s}{8\rho_4}} \quad (74)$$

where s is the shortest distance from P to the crack front, ρ_i ($i = 1, 2, 3, 4$) are the distances between point C , where the extension of the shortest distance line intersects the major axis of ellipse, and the four points on the crack front that connects to point C with lines intersecting perpendicularly to crack front, as shown in Fig. 34.

In elastic materials or under small-scale yielding conditions, the J-integral and the stress intensity factor can be related as:

$$J = \frac{K^2}{E} \quad (78)$$

5.2 Fatigue crack growth

Fatigue crack growth phenomena have been an important subject of study, particularly because of the structural integrity airworthiness requirements. The fatigue crack growth law or model is a cornerstone of the so-called damage tolerance design, which will be elaborated later. This section concentrates on fatigue crack growth mechanism and its rate equation. Fatigue crack growth mostly proceeds in a transgranular mode, following a power-law relationship with the cycle stress intensity factor range, ΔK , as first observed by Paris (Paris, 1963):

$$\frac{da}{dN} = C(\Delta K)^n, \quad (79)$$

where C and n are empirical constants.

It has been recognized that the alternating slip and slip reversal process is mostly responsible for fatigue crack nucleation and propagation (Neumann, 1974; Laird & Smith, 1982), which has been summarized as the restricted slip reversibility (RSR) concept, as schematically show in (Fong & Thomas, 1988). Based on the RSR concept and the deformation kinetics, Wu et al. (1993) have derived a transgranular fatigue crack growth rate equation as

$$\frac{da}{dN} = \frac{(\alpha_f V_r - \alpha_r V_f)}{12\pi(1-R)V_f V_r H} (\Delta K - \Delta K_{th}) \left(\frac{\Delta K}{\sigma_y} \right)^2, \quad (80)$$

where

$$\Delta K_{th} = \frac{(1-R)H V_f V_r}{\alpha_f V_r - \alpha_r V_f} \left[\frac{1}{H} \left(\tau_{of} - \tau_{or} + \frac{\Delta G_f^\ddagger}{V_f} - \frac{\Delta G_r^\ddagger}{V_r} \right) - \ln \frac{\left(\frac{V_f H \dot{\gamma}_{of}}{2f \alpha_f \Delta K} \right)^{\frac{kT}{V_f H}}}{\left(\frac{V_r H \dot{\gamma}_{or}}{2f \alpha_r \Delta K} \right)^{\frac{kT}{V_r H}}} \right]. \quad (81)$$

where $\dot{\gamma}_0$ is a pre-exponential strain rate constant, ΔG^\ddagger is the activation energy, V is the activation volume, τ_0 is the slip resistance of the lattice, H is the work-hardening coefficient, α is the fracture work factor, k is the Boltzmann constant, T is the absolute temperature, f is the frequency, and the subscripts "f" and "r" refer slip-forward and reversal, respectively.

In mechanical fatigue, where the microstructure (grain size, precipitate size and shape) is stable and environmental effects are absent, α_f and α_r are of the same order of magnitude, and both forward and reverse slips occur by the same mechanism so that $\Delta G_f^\ddagger = \Delta G_r^\ddagger$, $V_f = V_r = V$, $\tau_{of} = \tau_{or}$ and $\dot{\gamma}_{of} = \dot{\gamma}_{or}$, and hence ΔK_{th} approaches zero, as $kT/VH \ll 1$. Therefore, for pure mechanical fatigue:

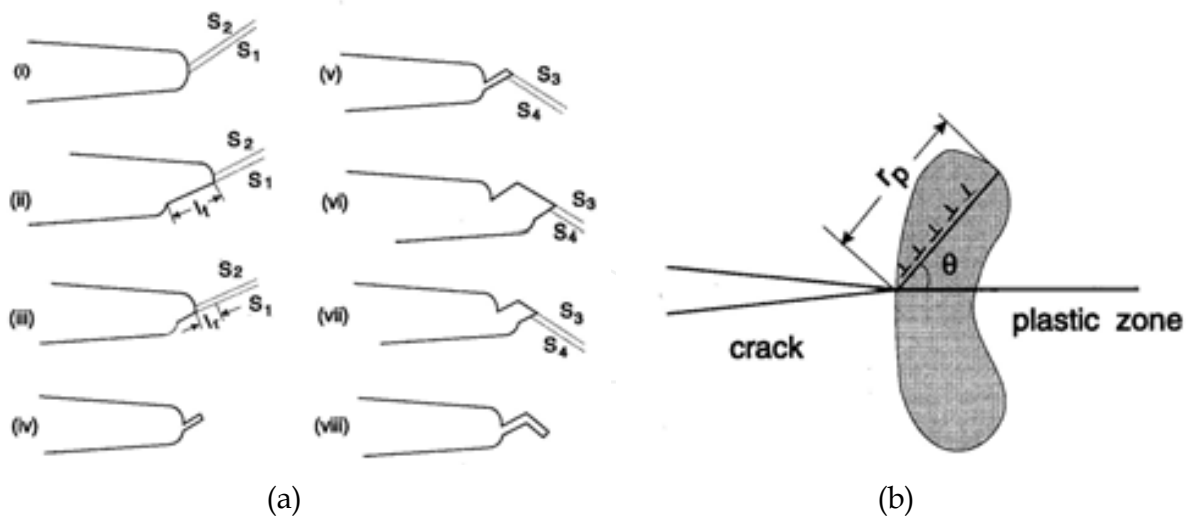


Fig. 35. (a) Schematics of fatigue crack growth by RSR: (i) Upon loading, slip systems on two favourably oriented slip planes S1 and S2 are activated. (ii) Forward slip occurs solely on S1 during the rising load cycle, producing a slip step of length l_f . (iii) During the decreasing load cycle, an increment of slip reversal l_r occurs on S1. (iv) A final slip reversal occurs on S2, producing a sharp crack tip. This process may be repeated over several load cycles (N) to produce a final crack length increment, $l_f - l_r$, after which a similar process may occur on another favourably oriented slip system variant along another pair of parallel slip planes, S3 and S4, as shown in the schematics (v) to (viii). (b) The RSR is confined within the plastic zone.

$$\frac{da}{dN} = \frac{(\alpha_f - \alpha_r)}{12\pi(1-R)VH\sigma_y^2} (\Delta K)^3 \quad (82)$$

Equation (82) takes the form of the Paris relationship with a physically defined proportional factor and a power law exponent of 3. This was indeed observed for fatigue crack growth rate data of a variety of alloys tested at room temperature in vacuum (Speidel, 1973), as shown in Fig. 36, where crack growth rate vs. ΔK relationship in a log-log plot exhibit a slope of 3 in the Paris regime. In addition, it was reported that $n = 3$ represents fatigue crack growth in ductile steels (Miline et al., 1988) and $n = 2.92$ in offshore steels (Smith & Cooper, 1989). Numerous experiments have also shown that the power law exponent of the Paris law falls within the range of 2.7~3.4 within the Paris regime. The power law exponent values found in these experiments are closer to 3 than 2 or 4, the values predicted by other models. Therefore, it may be fairly concluded that the RSR model is suitable for conventional materials where deformation is promoted by homogeneous slips.

Interestingly also, the RSR model shows that the fatigue crack growth rate depends on the materials' yield strength inversely to a power of 2, and it is also inversely proportional to the work-hardening coefficient. This implies the dependence on microstructure and temperature. For example, the yield strength depends on the grain size through the Hall-Petch relationship and it is also a function of temperature. Pure fatigue is essentially a "low temperature" phenomena occurring by the mechanism of dislocation glide, as depicted by the RSR model. The dependence of fatigue crack growth rate on yield strength was

demonstrated by Benson and Edmonds (1978) on 0.5Cr-0.5Mo-0.25V steel. A range of yield strength values, varying between 466 MPa and 834 MPa, were obtained using different heat treatment procedures. The work hardening coefficient, H , for each heat-treated material is estimated by dividing the difference between the ultimate tensile strength and the yield strength with the elongation, typically 13%. Then, the H -compensated crack growth rates at $\Delta K = 15.69 \text{ MPa}\sqrt{\text{m}}$, which is far above the fatigue threshold of this material, are plotted against σ_y^2 as shown in Fig. 37.

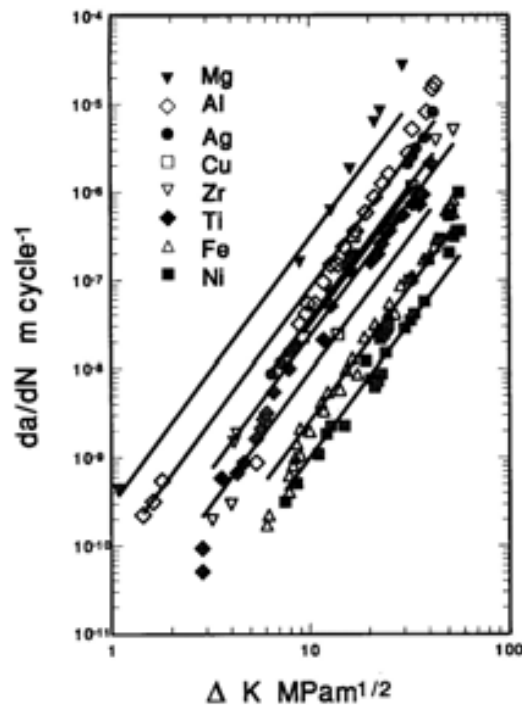


Fig. 36. Fatigue crack growth behaviours of a number of metals at room temperature in vacuum.

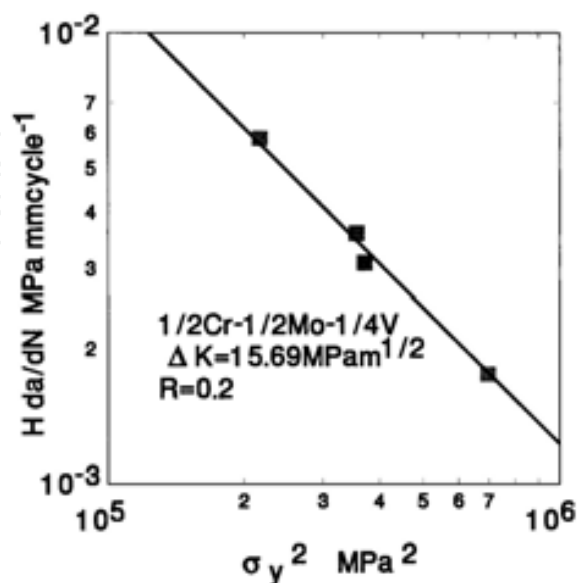


Fig. 37. H -compensated fatigue crack growth rate vs. σ_y^2 for 0.5Cr-0.5Mo-0.25V steel.

Equations (80)-(81) further predicts that the threshold in fatigue crack growth does not occur in the absence of microstructural change and environmental effects ahead of the crack tip such as in the case of pure mechanical fatigue. Some apparent thresholds ΔK_{th} does occur in coupon testing using load-decreasing procedures, due to crack closure, which will not be discussed further, since load shedding conditions are not particularly relevant to the service condition for fatigue crack growth to occur. According to Eq. (81), however, an intrinsic fatigue threshold may arise as a result of environmental interactions in a way if the environmental effects weaken the point obstacles after a new crack surface is exposed, leading to reduction of the activation barrier ΔG_{rr}^\ddagger and τ_{0r} , and/or increase of V_r upon slip reversal. Indeed, corrosion fatigue is a complex process and the detailed kinetics of the involved chemical processes need to be considered.

Another important phenomenon of fatigue is the behaviour of short cracks (Miller, K. J. & de los Rios, 1986). While the underlying physical mechanism is the same as discussed above, the complexity of the behaviour and the scatter reflects the interaction of the crack propagation kinetics with the microstructure, which should be addressed with a probabilistic approach and it is beyond the scope of this chapter. It is noteworthy though, that small crack growth behaviour is often observed to occur below the fatigue threshold established for a long crack, which indeed supports the predication of Eq. (82).

5.3 Creep crack growth

Creep crack growth resistance is also one of the important damage-tolerance properties required for materials being used for high temperature applications ($T \geq 0.3 T_m$, where T_m is the absolute melting temperature). Most creep crack growth tests have been conducted under constant load at high temperature in air, which is really a mixed creep-oxidation condition. Because of its apparent time-dependence, early studies on creep crack growth (CCG) mainly focused on correlating creep crack growth rates (CCGR) with some path-independent energy integrals $C(t)$ and C^* (the steady-state value of $C(t)$), which were good for creep-ductile materials such as Discaloy (Landes and Begley, 1976) and steels (Liu and Hsu, 1985). On the other hand, the stress intensity factor (K) has also been used to correlate CCGR, especially under small-scale creep deformation conditions and in the presence of environmental embrittlement effects, for high strength heat resistant alloys such as superalloys (Floreen, 1983; Sadananda & Shahinian, 1977).

Many mechanism based creep crack growth models have been proposed (e.g. Dimelfi & Nix, 1977; Vitek, 1978; Cocks & Ashby, 1982) and some general fracture mechanics treatments have also been given (Saxena, 1986; Riedel, 1989, Riedel, 1990), but these models did not sufficiently considered the contribution of grain boundary sliding, and therefore it is still lacking of a universal treatment to both creep-ductile and creep-brittle cases.

Considering the crack-tip stress relaxation by two deformation mechanisms – intragranular deformation and GBS, as schematically shown in Fig. 38, Xu et al. (1999) has derived a creep crack growth equation in the following form:

$$\frac{da}{dt} = \frac{d}{\lambda} \left[\frac{n+1}{n-p+1} \left(\frac{AI_n}{BI_p} \right)^{\frac{1}{n-1}} C(t) + (p+1) \left(\frac{1}{\sqrt{2\pi}} \right)^{\frac{2p}{p-1}} B^{\frac{1}{p-1}} K_I^{\frac{2}{p-1}} \left(\frac{C(t)}{I_n} \right)^{\frac{p^2-p-2}{p^2-1}} \right] \quad (83)$$

where n and p are power-law index, A and B are power-law constants, I_n and I_p are HRR field parameters associated with the HRR field of intragranular deformation and GBS, respectively; d is the grain size and λ is the critical GBS distance between cavities.

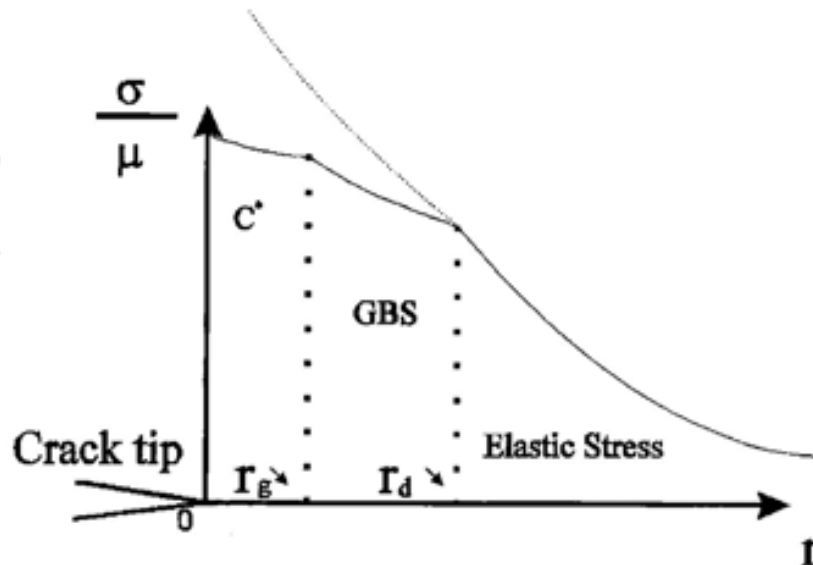


Fig. 38. A schematic of stress distribution in three zones ahead of a creep crack tip.

5.3.1 Creep-ductile cases

In creep ductile materials with small grain size, the creep zone may contain many grains, and therefore intragranular deformation plays a significant role in stress relaxation, while the contribution of GBS may be relatively small. For these cases, the first term in Eq. (83) dominates such that

$$\frac{da}{dt} = \frac{d}{\lambda} \frac{n+1}{n-p+1} \left(\frac{AI_n}{BI_p} \right)^{\frac{1}{n-1}} C(t) \quad (84)$$

This model basically agrees with that of Cocks & Ashby (1982).

5.3.2 Creep-brittle cases

In creep brittle materials (e.g., cast Ni-base superalloys) containing large grains, the role of intragranular deformation in crack-tip stress relaxation and creep crack growth will be limited. In that case, crack-tip deformation will mostly be concentrated in the grain boundary region, and therefore GBS plays a dominant role in the crack growth process. In such cases, the second term of Eq. (83) dominates, and particularly, considering that for pure GBS, $p = 2$, the rate equation reduces to:

$$\frac{da}{dt} = \frac{3}{4\pi^2} \frac{d}{\lambda} BK^2 \quad (85a)$$

The proportional constant B depends on grain boundary diffusion and microstructure, as discussed in section 2&3, as given by

$$B = \frac{D_{gb}\mu b}{kT} \left(\frac{b}{d}\right)^q \left(\frac{\lambda + h}{b}\right)^{q-1} \propto d^{-q} \quad (85b)$$

Creep crack growth behaviours on Udimet 520 at 540°C can be taken as an example to illustrate the application of Eq. (85) (Xu et al., 1999). The material was heat treated to obtain different grain sizes, all containing intragranular γ' but without any grain boundary $M_{23}C_6$ precipitates, and tested in argon and air. The test temperature was selected to ensure that no grain boundary precipitates formed during testing. Fractographic studies revealed that predominantly intergranular fracture and extensive crack tip branching occurred both in air and in argon, as shown in Fig. 39 (a) and (b) respectively. The metallurgical evidence suggests that GBS-controlled intergranular cracking and oxidation were the dominant damage mechanisms. No evidence of cavitation was found in any of the specimens. The test and material conditions satisfy the model's assumptions of the dominance of GBS.

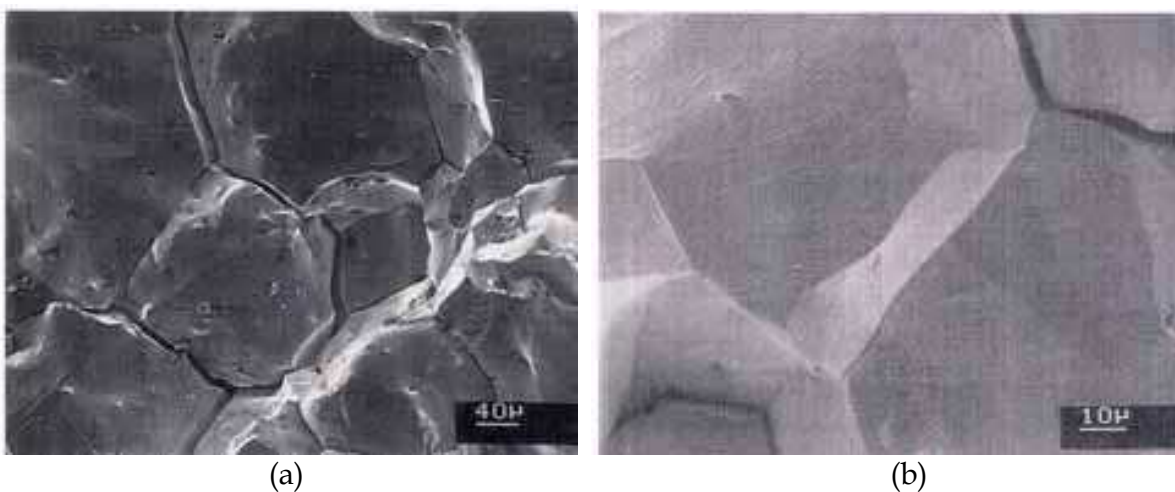


Fig. 39. SEM micrographs of the creep fracture surface of Udimet 520, (a) in air and (b) in argon, after Xu et al. (1999).

The CCGR in the argon environment, plotted in a double logarithm scale against the stress intensity factor K , exhibits a linear behaviour with the slope of 2, as shown in Fig. 40. For Udimet 520 with planar grain boundaries and no grain boundary precipitates, the stress index of GBS rate is 2 and hence, as predicted by Eq. (85), the creep crack growth rate exhibits a dependence on the stress intensity factor (K) to a power of 2. Other existing models fail to predict the K^2 dependence for creep crack growth in an inert or vacuum environment.

With regards to microstructure-dependence, the present creep crack growth model predicts that the creep crack growth rate depends inversely on the grain-size dependence to a power of q which can be related to grain boundary precipitate distribution morphology. For materials with planar and clean grain boundaries (no grain boundary precipitates, $q = 1$), it predicts no grain-size dependency. The data on Udimet 520 showed that the CCGR data were not sensitive to grain size variation over a grain size range of 235-464 μm , which corroborated the model prediction. For superalloys having received standard heat-treatments, where discrete grain boundary precipitates (e.g. $M_{23}C_6$ or δ phase) are present, the model predicts an inverse grain size dependence of creep crack growth rate. As reported in the literature, coarse grain size superalloys usually exhibit lower creep crack growth rates

(Floreen, 1983). For example, an inverse relation between CCGRs and grain size has been reported for Alloy 718 at 650°C (Liu et al. 1991). Stronger grain-size dependence is predicted by the model for materials with a continuous grain boundary precipitate network that may result from overaging or extended service exposure. However, no experimental work has been reported in this regard. But, it is a serious issue concerning aging gas turbine components.

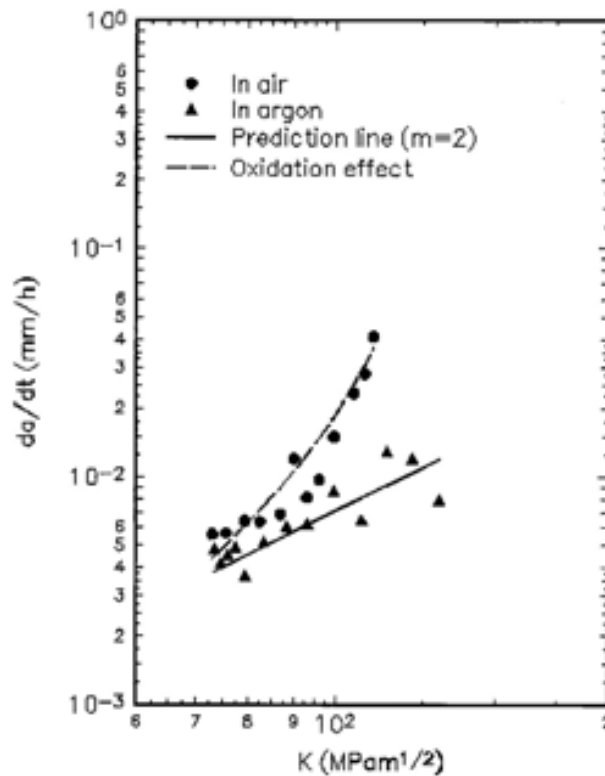


Fig. 40. Creep crack growth rate in Udimet 520 in argon and air at 540°C.

Considering environmental effect, as shown in Fig. 40, the creep crack growth rate in Udimet 520 tested in air exhibited an increasing power-dependence on K from 2 to a high value of 6.5 as K increases. This change in the K -dependence of creep crack growth rate with the environment, i.e. argon versus air, suggests that oxidation has a strong influence on the creep crack growth process.

The oxidation effects can be attributed to the reduction of the critical GBS distance λ to advance the crack in Eq. (85). An effective λ in the presence of oxide penetration may be equal to $\lambda_0 - X$, where λ_0 is the critical GBS distance in the absence of oxidation effects, and X is the penetrating oxide depth measured from the external oxide surface. As time t increases, oxides will penetrate deeper into the material and λ will be significantly reduced, and therefore the creep crack growth rate will increase. Taking the effect of oxidation into consideration, Eq. (85) takes the form

$$\frac{da}{dt} = \frac{3}{4\pi^2} \frac{d}{\lambda_0 - X} BK^2 \quad (86)$$

The curve for the creep crack growth rate in air was fitted to the test data by Xu et al. (1999) using a semi-empirical approach (Xu et al. 1999).

5.4 Creep-fatigue interaction in crack growth

Crack growth under creep-fatigue conditions is another important phenomenon affecting the structural integrity of gas turbine components, since evidently most of them operate under such conditions during the takeoff-cruise-landing cycle of the aircraft. The subject has been treated by Saxena et al. (1981) who proposed a linear summation model as:

$$\frac{da}{dN} = \left(\frac{da}{dN} \right)_f + C_5 \int_0^{t_h} \left[\frac{K^2(1-\nu^2)}{E(n+1)t} + C^* \right]^m dt \quad (87)$$

where t_h is the hold time; n is the creep law exponent, and $m \sim 1$ or $n/(n+1)$ (Cocks & Ashby, 1982), and C_5 is an empirical constant. Eq. (87) naturally reduces to a creep crack growth equation for long-term hold-times, and though it resolves into a K -dependence for short-term hold times but relates to no strong microstructural dependence, which is contrary to most experimental observations (e.g., Bain et al., 1988; Telesman et al. 2008).

Recall that, in section 4.1, we have developed a generic thermomechanical fatigue model with consideration of oxidation-creep-fatigue interactions, Eq. (50). Now, it is reasonable to consider that under creep-fatigue conditions, grain boundary sliding operates at a stress close to σ_y within the plastic zone, which is responsible for producing intergranular damage proportion to

$$l_c = d \int_0^{t_h} \varepsilon_{gbs} dt \quad (88)$$

Referring to Eq. (8) but omitting the mathematical detail of the integration, we shall propose for simplicity that

$$l_c \propto d^{1-q} \sigma_y^p t_h \quad (88)$$

Hence, substituting Eq. (88) into (50), we obtain:

$$\frac{da}{dN} = \left(1 + B \lambda^{-1} d^{1-q} \sigma_y^p t_h \right) \left\{ \left(\frac{da}{dN} \right)_f + \left(\frac{da}{dN} \right)_{env} \right\} \quad (89)$$

The creep-fatigue crack growth rates in Udimet 720 observed by Bain et al (1988) are shown in Fig. 41. It shows strong grain size dependence in the crack growth behaviour. Taking the fatigue crack growth rate at 427°C as the reference for each grain-size material respectively, this grain size dependence of creep-fatigue crack growth rate in Udimet 720 can be described using Eq. (89) with $q = 2.5688$, as shown in Fig. 42. Note that the yield strength of these materials were almost the same and there were grain boundary phases such as TiC, $Cr_{23}C_6$, and $(Cr, Mo, W)_3B_2$ present to form a discrete/almost continuous distribution such at $2 < q < 3$. The pure fatigue crack growth components (neglecting oxidation) in these materials were:

$$\begin{aligned} \frac{da}{dN} &= 6.432 \times 10^{-11} \Delta K^{3.72} && (ASTM0) \\ \frac{da}{dN} &= 1.6 \times 10^{-11} \Delta K^{3.72} && (ASTM3 - 8.5) \end{aligned} \quad (90)$$

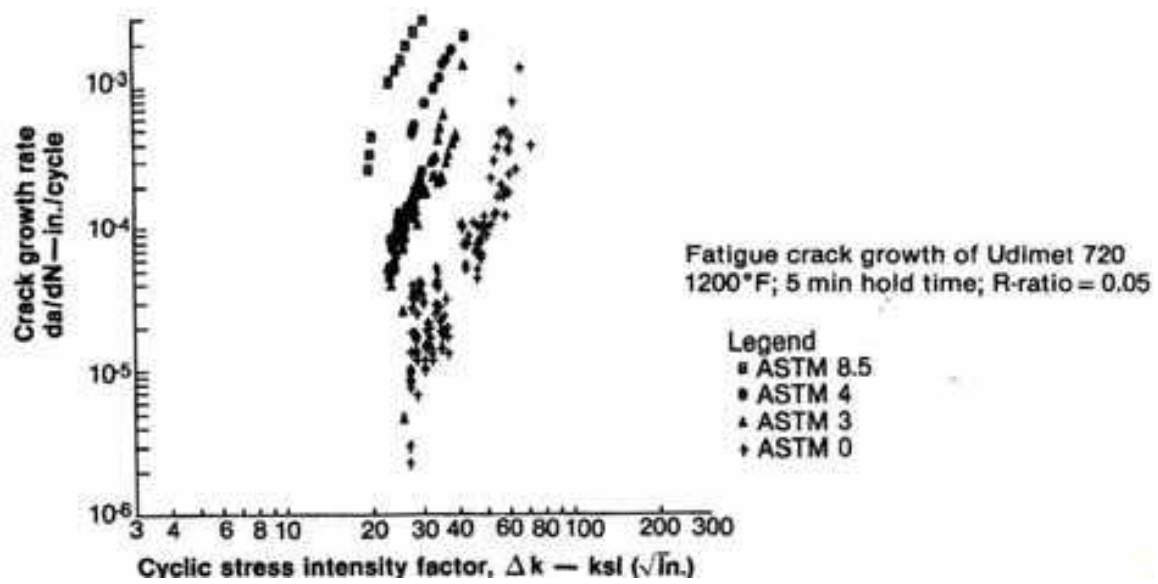


Fig. 41. Fatigue crack growth at 649°C with 5 min hold time at the maximum load (Bain et al., 1988).

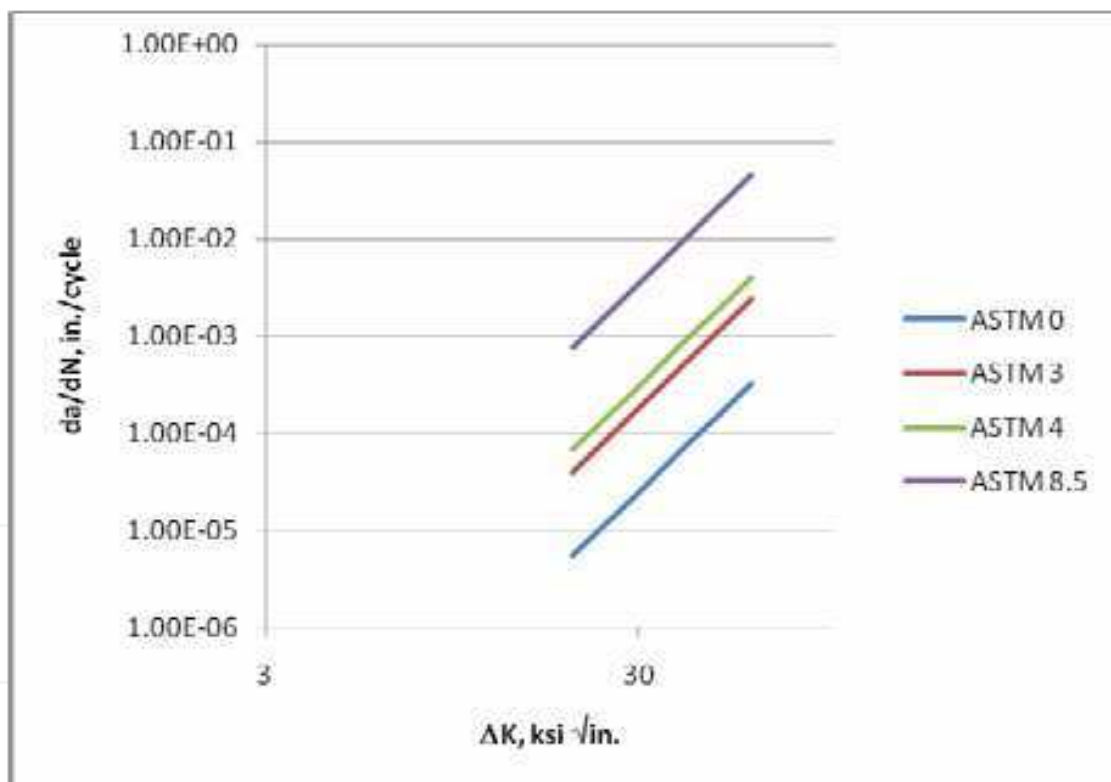


Fig. 42. The predicted Fatigue crack growth in Udmet 720 at 649°C with 5 min hold time.

Telesman et al. (2008) also observed strong microstructural dependence of the hold time fatigue crack growth rate in the LSHR P/M disk superalloy. Using heat treatments to control the grain size at constant but with different cooling rate and subsequent aging treatments to control the γ' size, they related the increased fatigue crack growth rate with the stress relaxation potential possessed in each microstructure with different (primary, secondary and tertiary) γ' sizes and distribution. This can also be explained qualitatively by

Eq. (89): stress relaxation would impart a lower grain boundary sliding rate, resulting in lesser grain boundary damage during the hold time and hence reducing the overall crack growth rate.

Finally, it should be pointed out that none of the above phenomena could be sufficiently addressed with Eq. (87). In general, the present model, Eq. (89), also presents the effect of creep damage in a multiplication factor, for every fatigue crack increment will induce coalescence with the creep damage accumulated ahead of the propagating fatigue crack.

5.4 Damage tolerance analysis

The damage-tolerance philosophy assumes materials or components entering into service have defects in their initial conditions. Then the component life is basically the life of crack propagation starting from an initial flaw, as:

$$N = \int_{a_0}^{a_f} \frac{da}{f(\Delta K)} \quad (91)$$

where a_0 is the initial crack size, a_f is the final crack size at fracture (or sometimes, a dysfunction crack size reduced by a safety factor), and the crack growth rate function $f(\Delta K)$ can be any of the aforementioned, particularly Eq. (79), (86) or (89), depending on the operating condition. In the simple case under pure mechanical fatigue condition, where the crack growth rate is expressed by the Paris law, Eq. (79), the damage tolerance life can be obtained by integration as

$$N = \int_{a_0}^{a_f} \frac{da}{C(\Delta K)^n} = \int_{a_0}^{a_f} \frac{da}{C(\Delta\sigma\sqrt{\pi})^n a^{\frac{n}{2}}} = \frac{1}{(\frac{n}{2}-1)C(\Delta\sigma\sqrt{\pi})^n} \left(\frac{1}{a_0^{\frac{n}{2}-1}} - \frac{1}{a_f^{\frac{n}{2}-1}} \right) \quad (92)$$

Using this philosophy, components need to be inspected before and during service. If no actual cracks are found, it is usually assumed that the initial crack size is equal to the non-destructive inspection (NDI) limit, and hence the crack propagation life marks the safe inspection interval (SII) on the maintenance schedule. Since crack propagation life is apparently sensitive to the initial crack size, an economical maintenance plan requires more advanced NDI techniques with accuracy and lower detection limits. Taking advantage of the damage tolerance properties, a component can repeatedly enter into service, as long as it passes NDI, regardless of whether the usage has exceeded the safe-life limit, and it will retire only after cracks are found. This is called retire for cause (ROC). By virtue of damage tolerance, life extension can be achieved on safe-life expired parts, as shown schematically in Figure 5.1. The damage tolerance approach is not only meant to be used as a basis for life extension, but more so to ensure the structural integrity of safety-critical structures and components to prevent catastrophic fracture, as it is required by the Aircraft Structural Integrity Program (ASIP) and Engine Structural Integrity Program (ENSIP) of the United State Air Force.

Due to the inherent properties of materials, detectable crack propagation periods are usually very short for most materials, and even more so for advanced materials such as intermetallic and ceramic materials, such that life management based on damage tolerance is totally unpractical (too many interruptions of service due to inspections, and therefore too costly). Besides, it is commonly recognized that damage accumulation spends most of its time

undetectable non-destructively, i.e., at the microstructural level and in the small (short) crack regime. Thus, new life management philosophy is required, which should put emphasis on the physics-based understanding of the continuous evolution of damage from crack nucleation, to short crack growth and long crack growth (to eventual failure), which will be called the holistic structural integrity process.

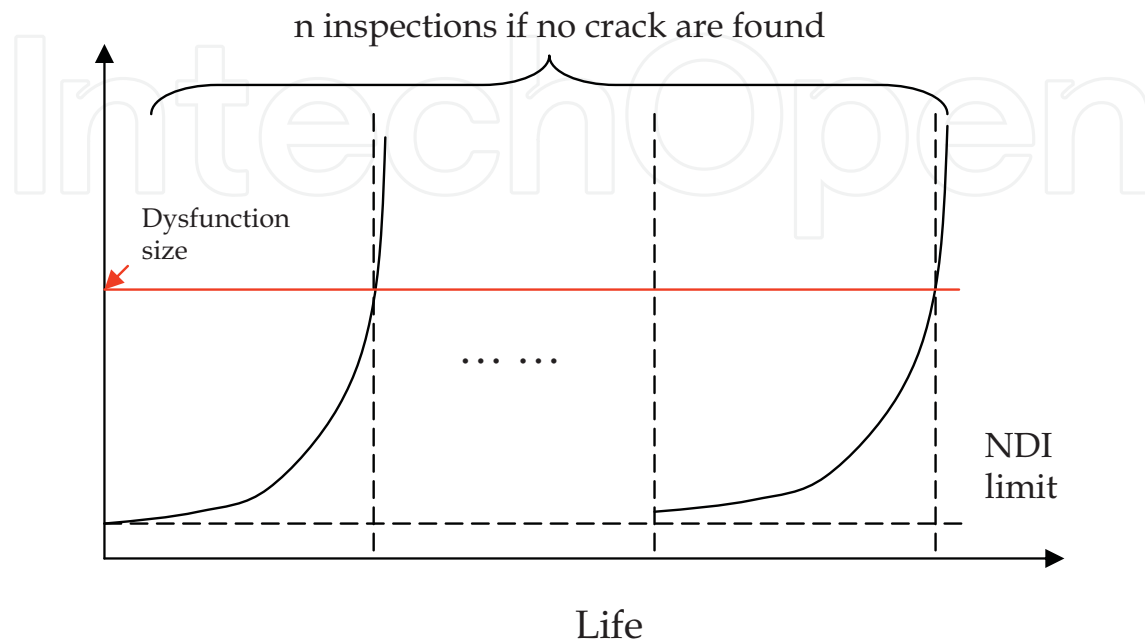


Fig. 43. Schematic of damage-tolerance life management.

6. Analyses of gas turbine components

This section demonstrates the application of the aforementioned models for two selected cases: (i) turbine blade creep and (ii) turbine blade crack growth, as follows.

6.1 Turbine blade creep

A turbine blade is modelled using the finite element method, as shown in Fig. 44. The blade was represented by a solid airfoil attached to a solid platform. Since the present analysis focused on the airfoil portion, the platform only serves as the elastic boundary condition. The temperature and pressure distribution induced by the hot gas impingement is obtained from fluid dynamics and pressure distribution analyses and is applied upon the blade as the boundary conditions as shown in Fig. 45 and Fig. 46, respectively. The turbine rotates at 13800 rpm.

The turbine blade material is assumed to creep by GBS only, obeying the following creep law:

$$\varepsilon_{gbs} = \varepsilon_0 + \phi \dot{\varepsilon}_{ss} t + \frac{\sigma}{\beta^2 H_{gbs}} \left[1 - \exp\left(-\frac{\beta^2 \phi H_{gbs} \dot{\varepsilon}_{ss} t}{\sigma(\beta - 1)}\right) \right] \quad (93)$$

where $E = 100000$ (MPa), $H_{gbs} = 25000$ (MPa), $\beta = 1.00925$, and

$$\dot{\varepsilon}_{ss} = 10^8 \exp\left(-4 - \frac{16000}{T}\right) \left(\frac{\sigma - 150}{E}\right)^2 \quad (94)$$

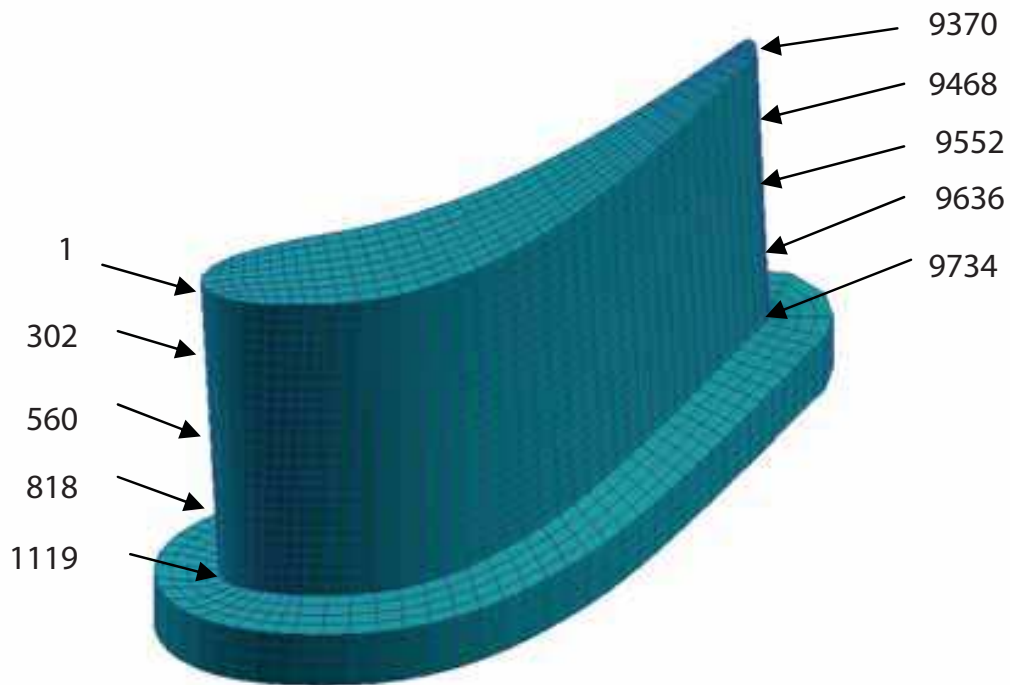


Fig. 44. FEM model of turbine blade. The numbers indicate some selected nodes. Numbers indicate the nodal points

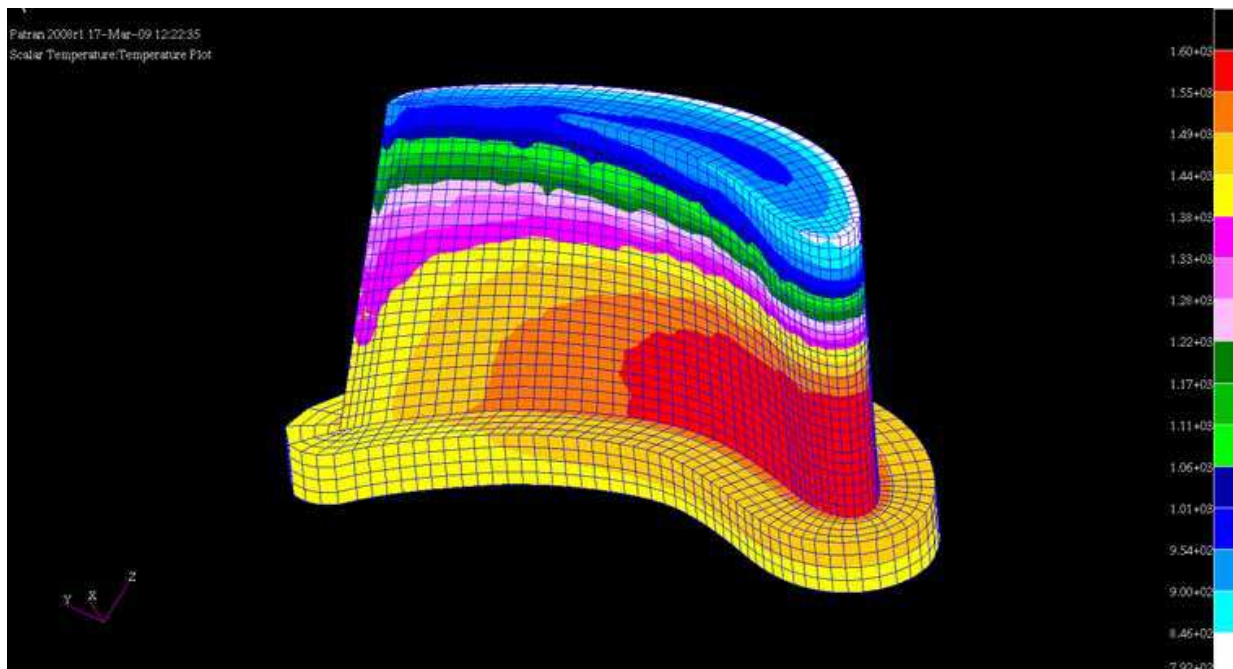


Fig. 45. Temperature profile in the blade

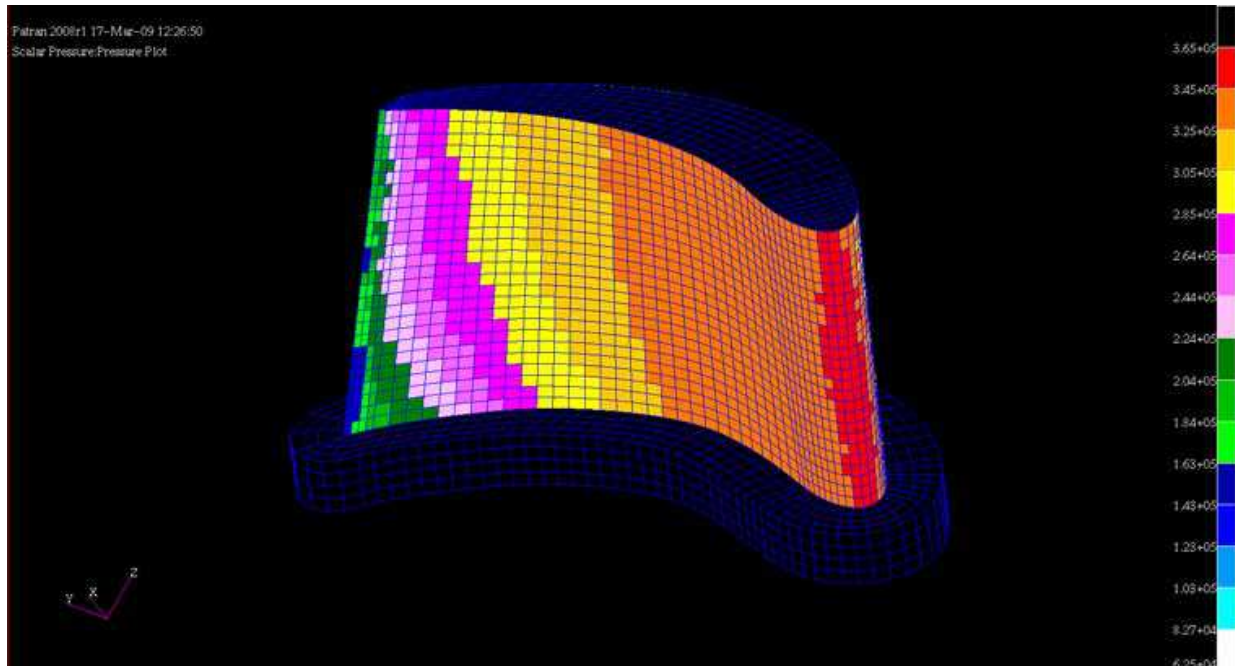
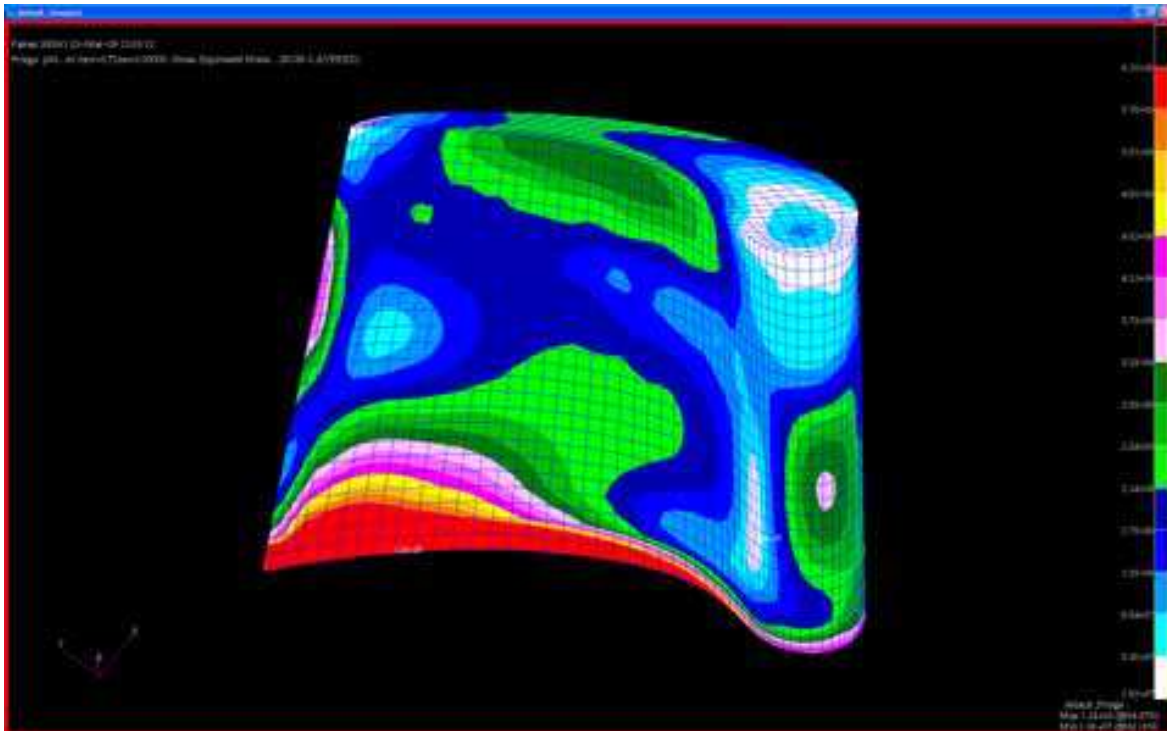
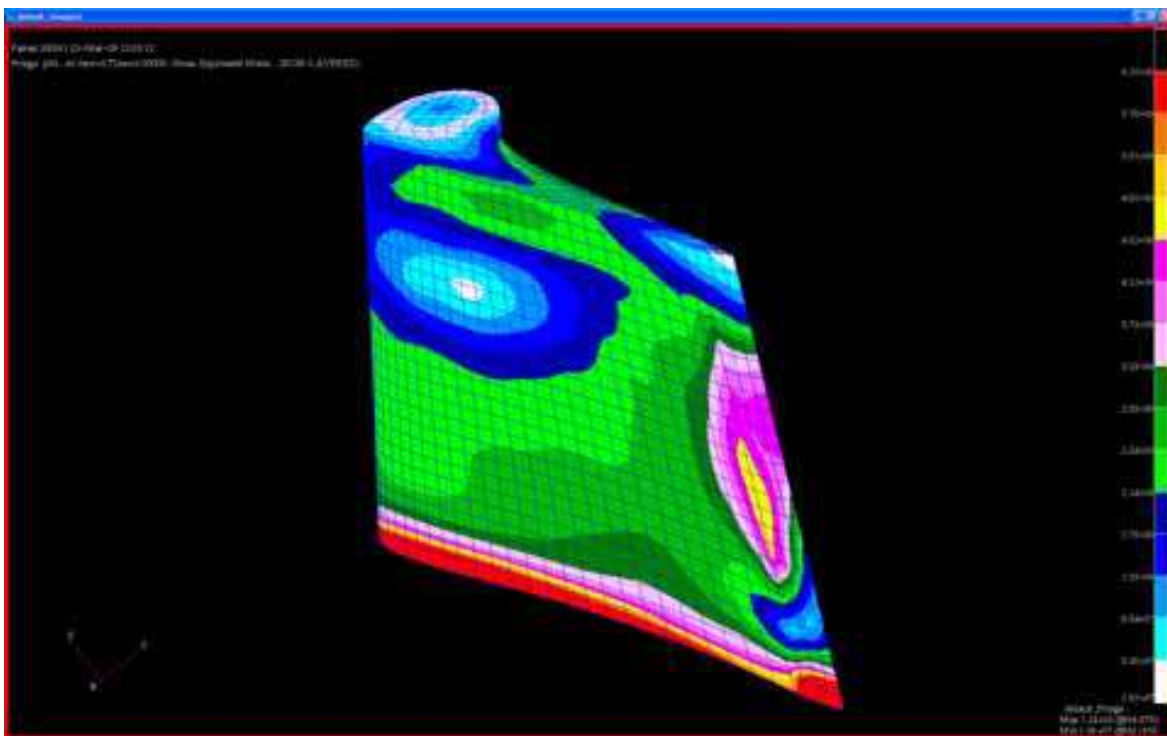


Fig. 46. Pressure profile as the boundary condition on the blade surface.

Creep simulation was conducted using MSC.Marc for 100 hours. The initial (at $t = 0$) and final ($t=100$ hours) von Mises stress distribution contours are shown in Fig. 47 and Fig. 48, respectively. The initial response of the blade is purely elastic, which results in a highly non-uniform stress distribution in the blade with particular stress concentrations at the mid-leading edge and mid-trailing edge and near the bottom attachment. After 100 hours, when creep deformation proceeds into a steady state, stress distribution became more uniform throughout the airfoil. Stress concentration remained at the bottom attachment, because, for simplicity of demonstration, the platform was assumed to deform only elastically. The final creep strain distribution contours are shown in Fig. 49. The creep strain accumulates the most where the initial elastic stress concentration appears, which then leads to stress relaxation. Creep deformation and stress relaxation curves at selected nodes along the leading/trailing edges (the nodal numbers are indicated in Fig. 44) are shown in Fig. 50 - Fig. 53, respectively. In both cases, the stress has dropped dramatically with the overall increment of the creep strain. Except those creep strain concentration regions, the majority of the airfoil, especially the upper half, practically remains in the elastic regime. The stress relaxation or "stress shakedown" in a component have a two-fold meaning on the life of the component: it may impact on the low cycle fatigue damage with a timely reduced stress, but on the other hand, it is also accompanied with an increase of creep damage in the material. From this analysis for this particular blade, it deems that the mid-leading edge and the bottom of trailing edge are critical locations. After 50 hours, creep deformation proceeds in steady state.

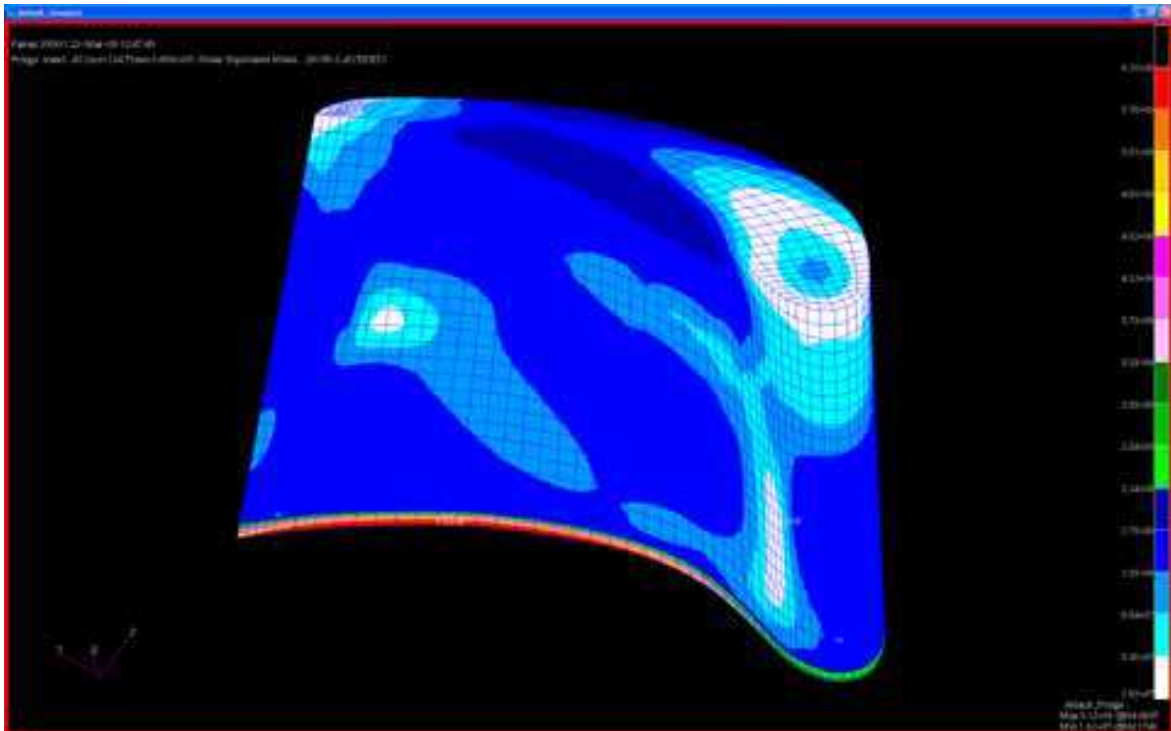


(a)

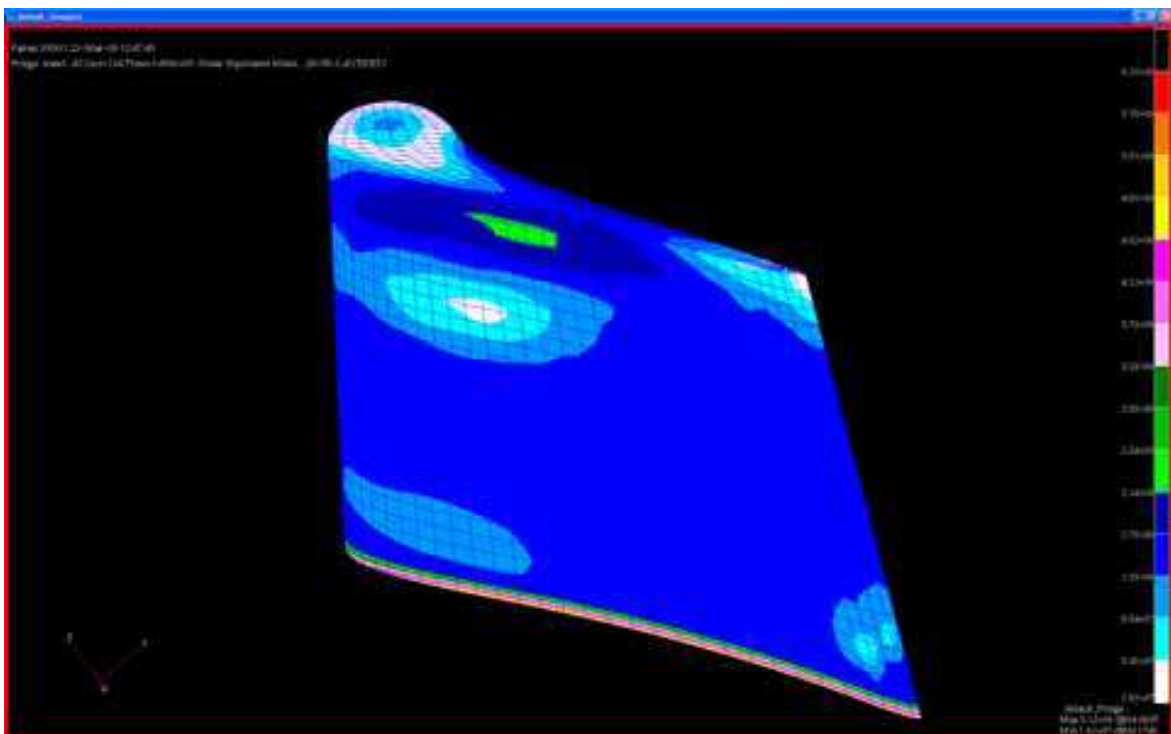


(b)

Fig. 47. Stress distribution at $t=0$: a) the pressure side, and b) the suction side.

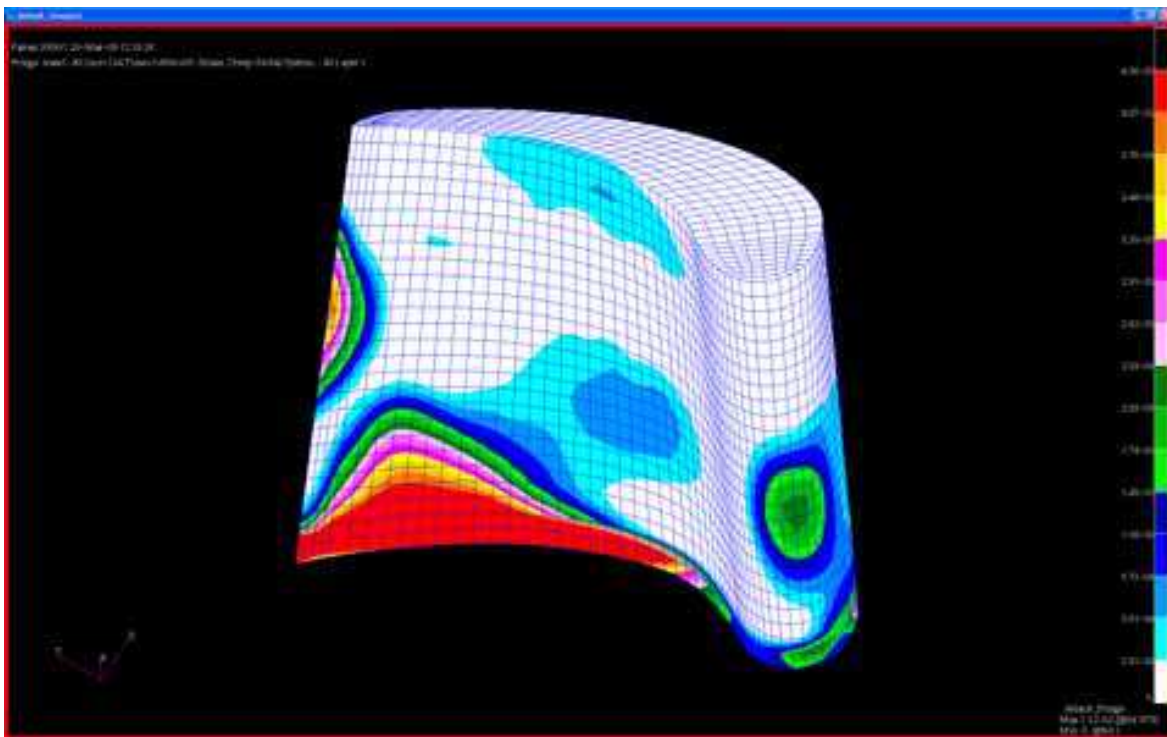


(a)

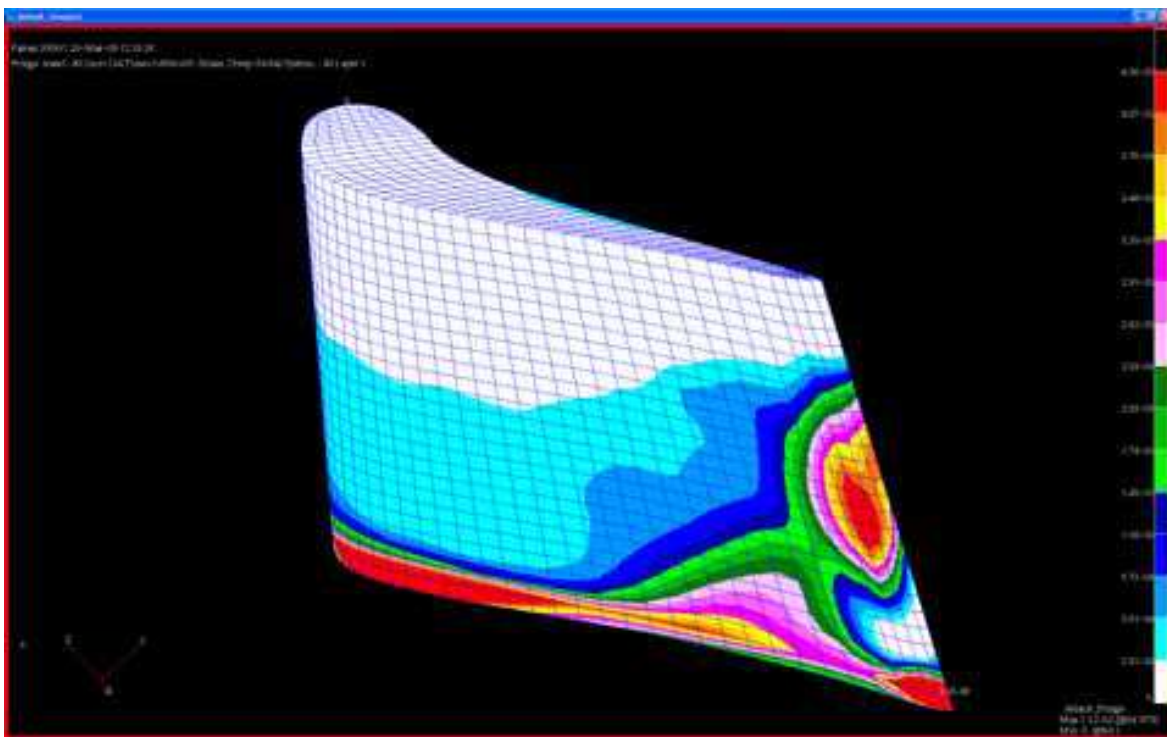


(b)

Fig. 48. Stress distribution at $t = 100$ hrs, a) the pressure side, and b) the suction side.



(a)



(b)

Fig. 49. Creep deformation of the blade after a 100 hr., a) the pressure side, and b) the suction side.

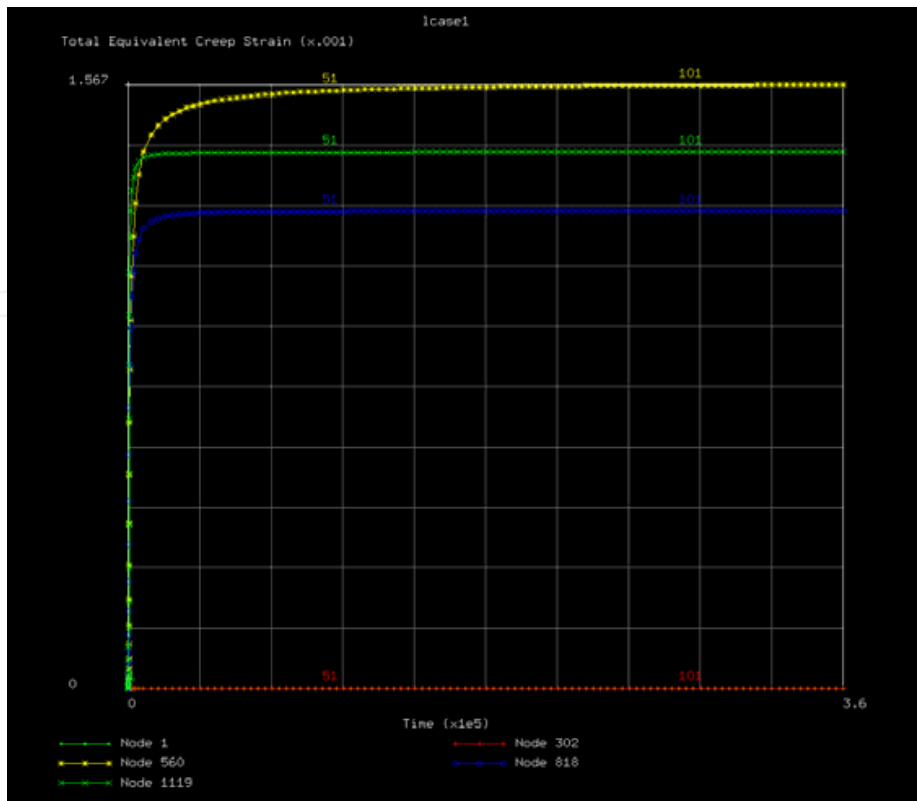


Fig. 50. Deformation history at selected nodes along the leading edge.

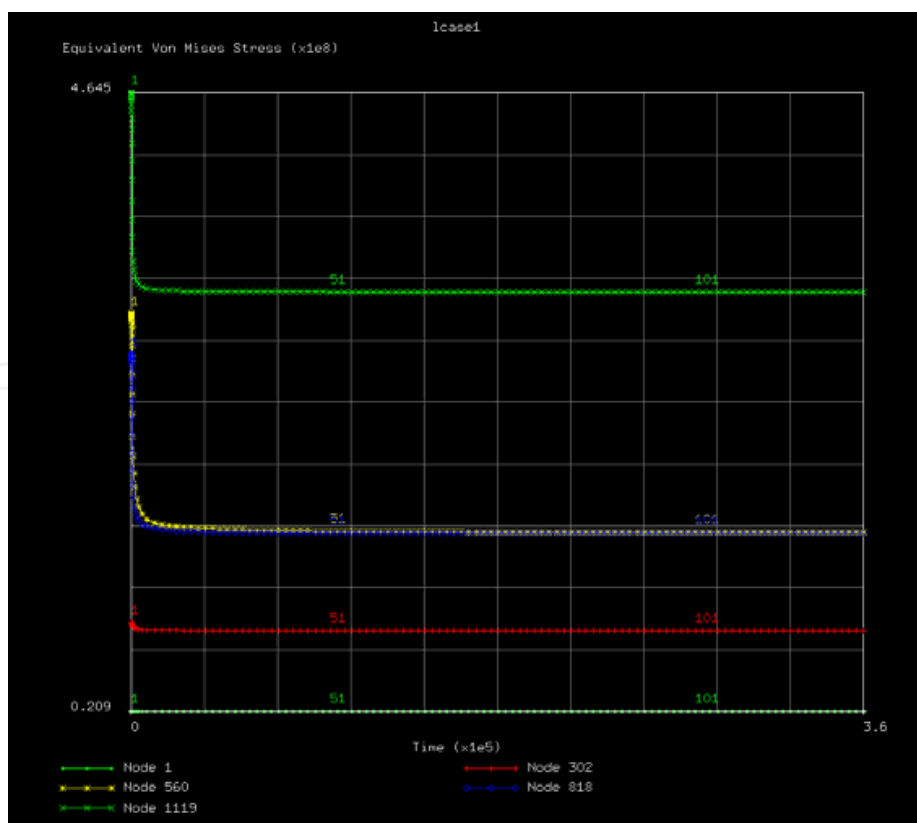


Fig. 51. Stress relaxation at selected nodes along the leading edge.

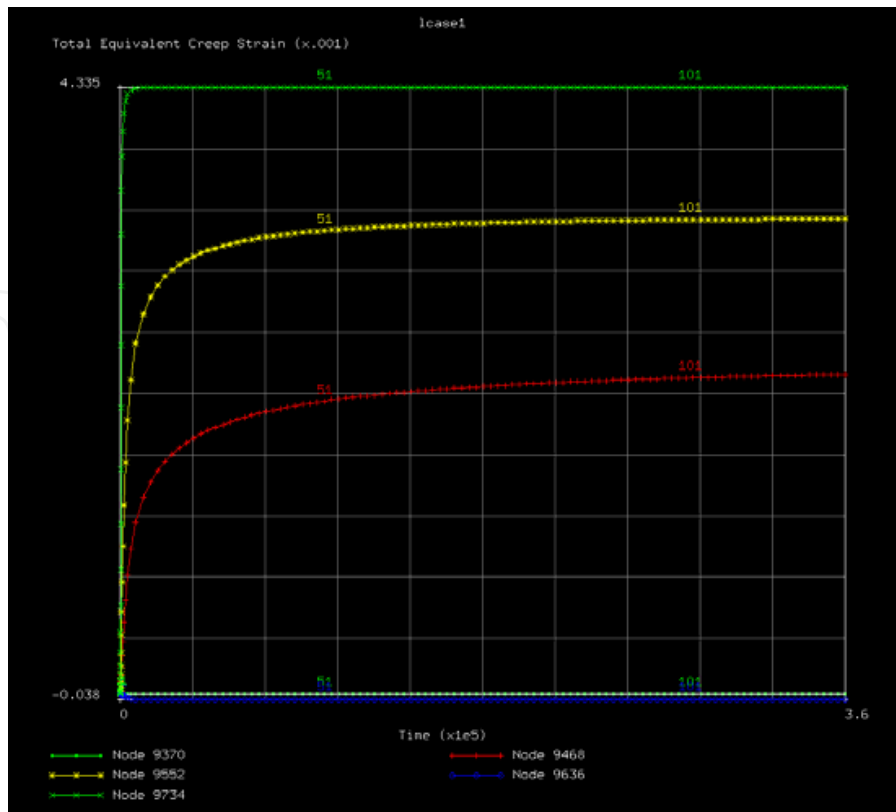


Fig. 52. Deformation history at selected nodes along the trailing edge.

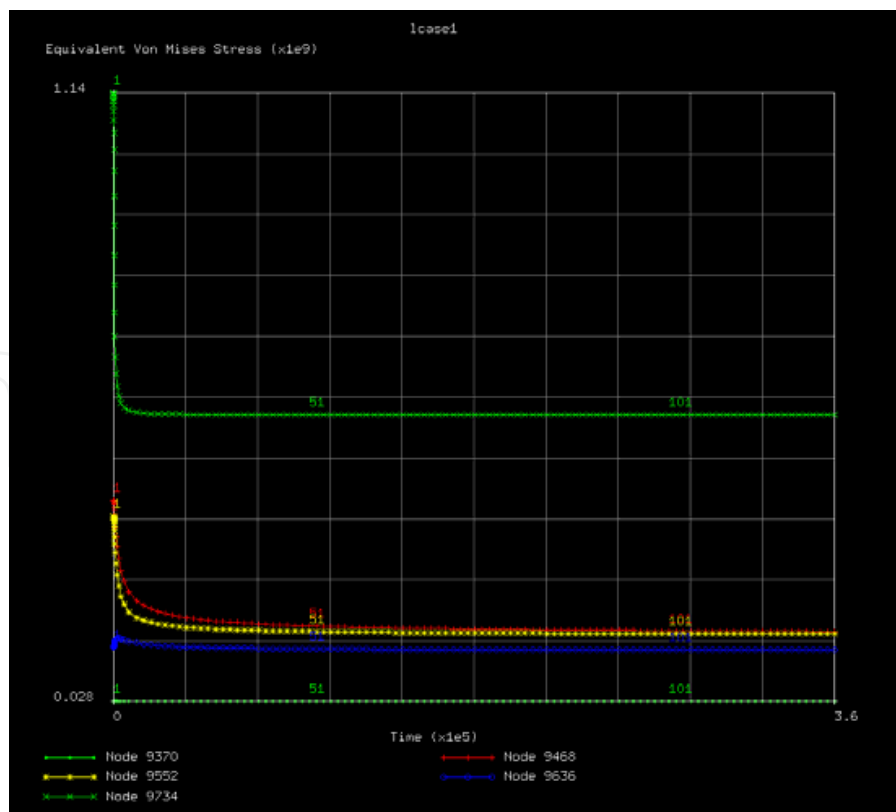


Fig. 53. Stress relaxation at selected nodes along the trailing edge.

6.2 Turbine Blade Crack Growth

Next we consider a turbine blade that experienced premature failure due to fatigue crack growth. A finite element model was created for the blade and the stress analysis was conducted with the consideration of centrifugal loading and the blade contact with the disc. The finite element mesh and the von Mises stress distribution in the blade is shown in Fig. 54.

An initial crack of semi-elliptical shape existed in the trough of the first serration on the pressure side (indicated by the arrow in Fig. 54). The principal stress over a quarter of the fir-tree root plane is shown in Fig. 55. Simulation of crack growth was conducted using the weight function method, Eq. (73-74) with appropriate boundary correction factors. The stress intensity factor results were then input into the integration for crack advancement based on the Paris-law of the material. The crack depth and aspect ratio as functions of the cycle number normalized to its failure are shown in Fig. 56. The crack depth increased monotonically. The crack aspect ratio increased initially, reached a constant value of 0.93, and then began to decline. This change reflected the fracture mechanics characteristic of the elliptical crack and the effect of stress distribution on the cracking plane in the component. When the crack was small, the stress over the crack was almost constant, the maximum stress intensity factor of the semi-elliptical crack occurred at the deepest crack front, which drove the crack toward a “circular” shape. However, when the crack became large, the stress distribution would have an effect. Since the stresses were relatively high at the notch root surface, then the stress intensity factor at the surface point began to accelerate, which then drove the crack to grow faster in the surface length direction. The variations of the stress intensity factors at both the surface and the deepest points are shown in Fig. 57.

The a) initial and b) final crack profiles as revealed by post-mortem examination of the fracture surface are shown in Fig. 58 (a) and (b), respectively. The results of the weight function method crack growth simulation are seen to agree with the observed crack growth profile on an actual component.

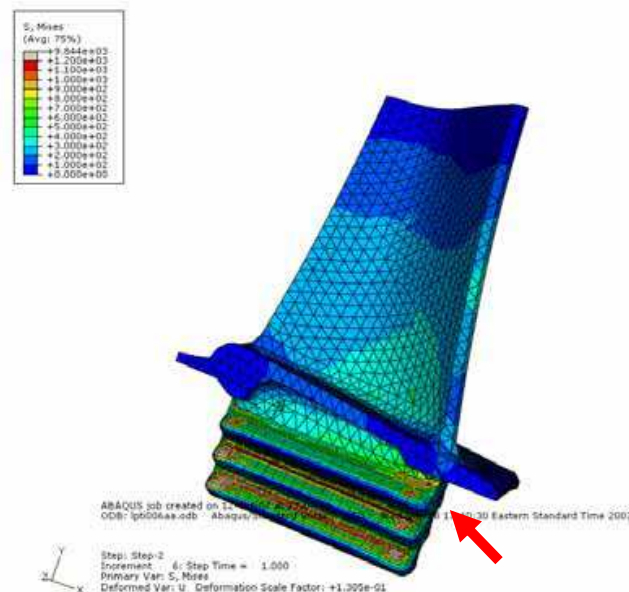


Fig. 54. The von Mises stress in a turbine blade. The arrow indicates where a crack would form.

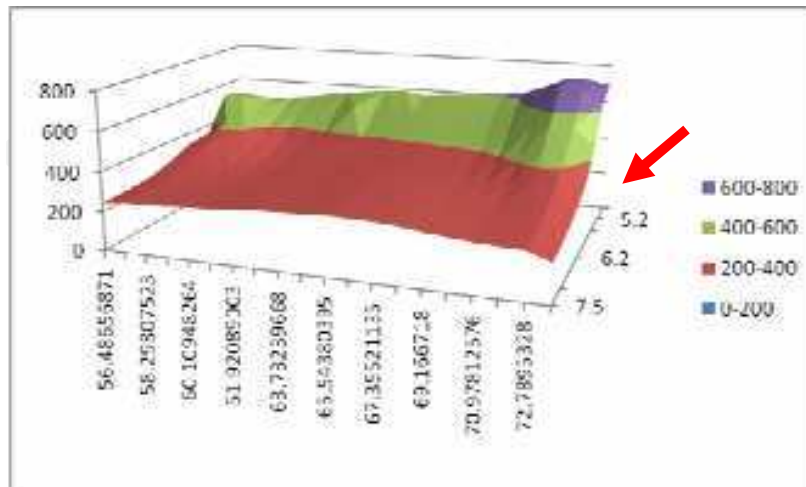


Fig. 55. Stress distribution (in unit of MPa) over a quarter of the fir-tree root plane (in unit of mm). The arrow indicates where the initial crack existed.

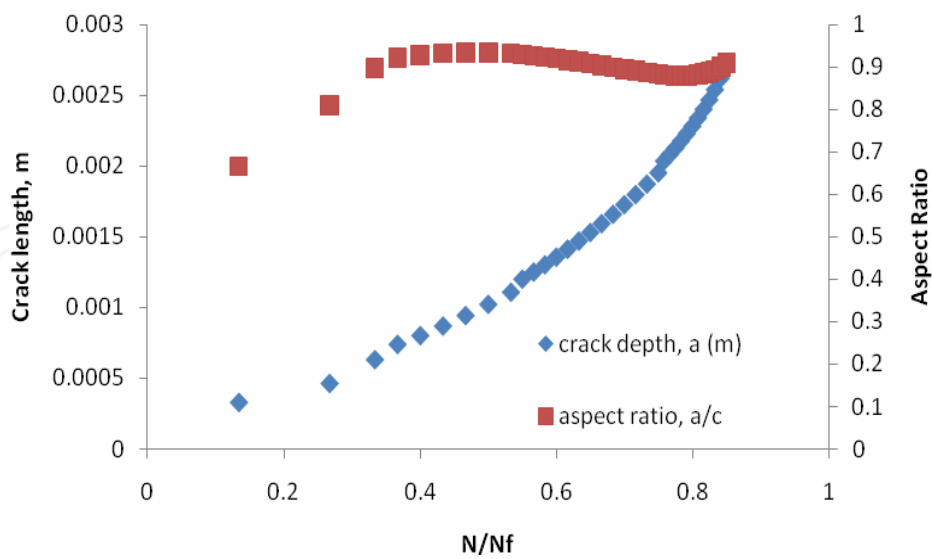


Fig. 56. Crack depth and aspect ratio as functions of the number of cycles.

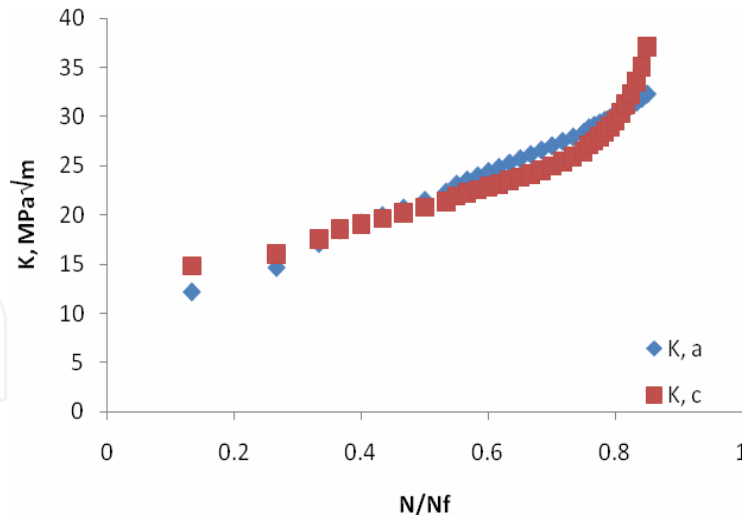
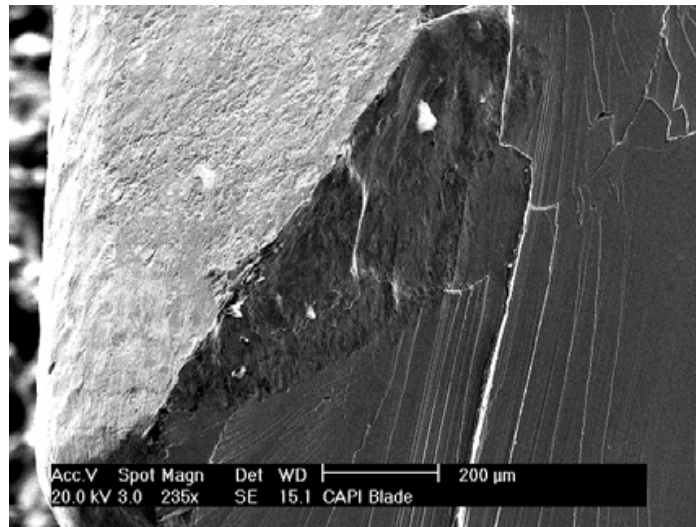


Fig. 57. Stress intensity factors at the surface and the deepest points.



(a)



(b)

Fig. 58. a) The initial crack profile, and b) the final crack profile.

7. Conclusion

In this chapter, a framework of integrated creep-fatigue (ICF) constitutive modelling is presented. The ICF model formulates deformation and damage accumulation in terms of two inelastic strain components—intragranular deformation (ID) and grain boundary sliding (GBS). This way, the model can reflect the microstructural (grain size, grain boundary morphology, grain boundary precipitates and intragranular precipitates) dependence of the deformation behaviour with respect to each deformation mechanism. As regards to damage accumulation in the form of crack nucleation and propagation, the decomposition rule founds the physical base to relate transgranular (fatigue) fracture to ID and intergranular cavitation (creep) damage to GBS for polycrystalline materials. From this premise, a general thermomechanical fatigue (TMF) model has been developed that involves creep-fatigue and oxidation-fatigue interactions.

The TMF damage accumulation model physically depicts the process of fatigue crack nucleation and propagation in coalescence with the creep/dwell damages (cavities or wedge cracks) distributed along its path inside the material. According to the present model, creep/dwell-fatigue interaction is nonlinear in nature. The model has been shown to successfully correlate both “cold” dwell-fatigue and “hot” creep-fatigue. In cold dwell, the damage is envisaged as dislocation pile-up, leading to formation of ZSK cracks. In hot creep, the damage accumulation is related to grain boundary sliding. Particularly, for creep-fatigue interaction, the model reconciles the SRP concept. Therefore, it provides a unified approach to deal with dwell/creep-fatigue interactions.

Similarly, a fatigue crack growth equation is presented based on the transgranular restricted slip reversal (RSR) mechanism, and a creep crack growth equation based on grain boundary sliding with stress relaxation ahead of the crack tip. Crack growth in creep-fatigue is also described within the same framework in association with fracture mechanics.

Overall, a physics-based holistic lifing approach has been developed; and when incorporated with the finite element method, it offers an integrated methodology for life prediction of gas turbine components, addressing a variety of failure modes under high temperature loading conditions.

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