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Supervision and Control Strategies of a 6 DOF Parallel Manipulator Using a Mechatronic Approach

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1. Introduction

Currently, the Stewart Platform is used in different engineering applications (machine tool technology, underwater research, entertainment, medical applications surgery, and others) due to its low mechatronic cost implementation as an alternative to conventional robots. The current trend of using parallel manipulators has created the need for developing open supervision and control architectures. This chapter presents the mathematical analysis, simulation, supervision and control implementation of a six degree of freedom (DOF) parallel manipulator known as the Stewart platform. The related studies are critically examined to ascertain the research trends in the field. An analytical study of the kinematics, dynamics and control of this manipulator covers the derivation of closed form expressions for the inverse Jacobian matrix of the mechanism and its time derivative, the evaluation of a numerical iterative scheme for forward kinematics on-line solving, the effects of various configurations of the unpowered joints due to angular velocities and accelerations of the links, and finally the Newton-Euler formulation for deriving the rigid body dynamic equations.

The contents of this chapter are organized as follows:

- Section II presents the features of a Stewart Platform manipulator, describing its spatial motion and applications.
- Section III covers the mathematical description, with the kinematics and dynamics modelling, and the actuator control using a mechatronic prototyping approach.
- Section IV details the control structure, and compares two different control strategies: the PID joint control structure and the Generalized Predictive Control (GPC). Both controllers structured in the polynomial RST form, as a generic framework for numerical control laws satisfying open architecture requirements.
- Section V describes the supervision and control architecture, particularly the spatial tracking error is analyzed for both controllers.

- Section VI provides time domain simulation results and performance comparison for several scenarios (linear and circular displacements, translational or rotational movements), using reconfigurable computing applied to a Stewart-Gough platform.
- Section VII presents the supervisory control and hardware interface implemented in a Labview™ environment.
- Finally, section VII presents the conclusions and contributions.

2. Stewart platform manipulator

The Stewart platform is a 6 DOF mechanism with two bodies connected by six extendable legs. The manipulation device is obtained from the generalisation of the proposed mechanism of a flight simulator presented in (Stewart, 1965)(Gough & Whitehall, 1962)(Karger, 2003)(Cappel, 1967). Its legs are connected through spherical joints at both ends, or a spherical joint at one end, and a universal joint at the other. The structure with spherical joints at both ends is the 6-SPS (spherical-prismatic-spherical) Stewart platform (Fig. 1), while the one, with an universal joint at the base and a spherical joint at the top is the 6-UPS (universal-prismatic-spherical) Stewart platform (Dasgupta, 1998)(Bessala, Philippe & Ouezdou, 1996).

The spatial movements of the six-axis parallel manipulator provide three translational and three rotational DOF of the movable plate, allowing position accuracy, stiffness and payload-to-weight ratio to exceed conventional serial manipulators performances. Due to these mechanical advantages, the Stewart platform manipulator is used in many applications such as flight simulators, parallel machine-tools, biped locomotion systems and surgery manipulators (Sugahara et al., 2005)(Wapler et al., 2003)(Wentlandt & Sastry, 1994).

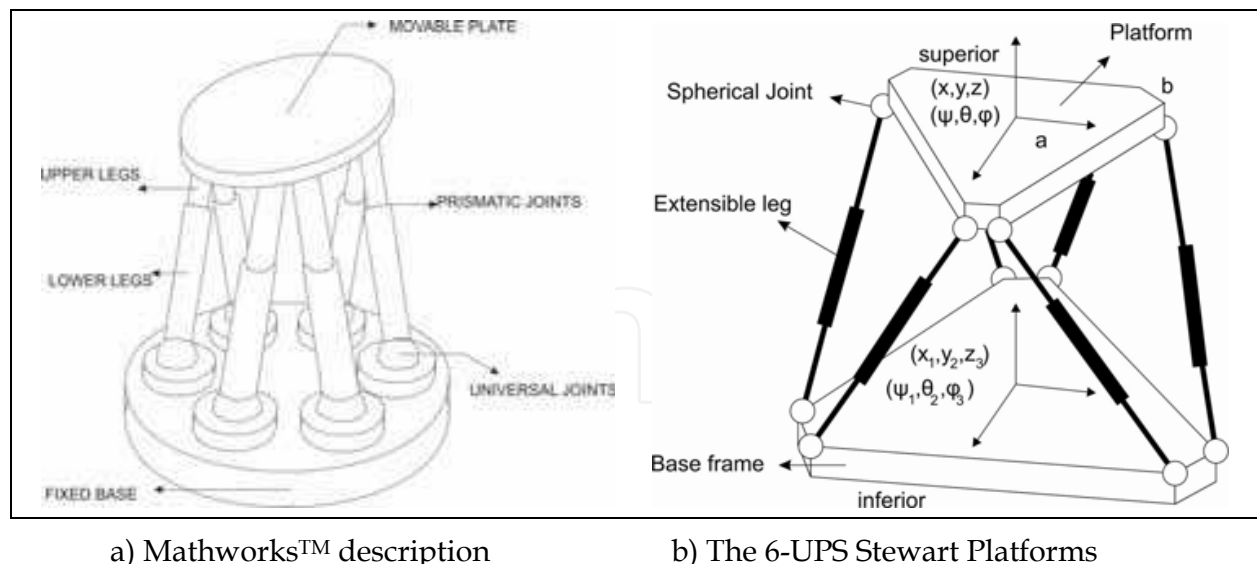


Fig. 1. Schematic Representation of the Stewart-Gough Platform.

3. Mathematical description

The mathematical model has to respond to a desired trajectory by actuating forces in order to properly move the mobile plate to the targeted position and orientation. For obtaining the

mathematical representation, a reference coordinated system for analyzing the manipulator is presented in Fig. 1.

3.1 Geometric model

Given the accomplishment of numerous tasks due to its configuration, the platform legs are identical kinematics chains whose motion varies accordingly to the tip of the joint used (Fasse & Gosselin, 1998)(Boney, 2003). Typically, the legs are designed with an upper and lower adjustable body, so each one has a variable length (Fig. 1). The geometrical model of a platform is expressed by its (X, Y, Z) position and the (ψ, θ, ϕ) orientation due to a fixed coordinate system linked at the base of the platform. The obtained function of this generalized coordinates (joints linear movements), is presented in (1).

X_i=f(L_i) (1)

where L_i=(L_1 L_2 ... L_6) are each joint linear position, X_i=(X Y Z ψ θ ϕ) the position-orientation vector of a point of the platform. Then the transformation matrix for rotations can be organised as Shown in (2), where, cψ: cos ψ, sψ: sin ψ

T(ψ,θ,ϕ)=rot(x,ϕ)rot(y,θ)rot(z,ψ) = [cϕ cθ | -cϕ sθ sψ - sϕ cψ | cϕ sθ cψ + sϕ sψ ; sϕ cθ | -sϕ sθ sψ + cϕ cψ | sϕ sθ cψ - cϕ sψ ; -sθ | cθ sψ | cθ cψ] (2)

where, θ = ATAN 2 [-n_z / (cϕ n_x + sϕ n_y)], ϕ = ATAN 2 [n_y / n_x], ψ = ATAN 2 [(sϕ a_x - cϕ a_y) / (-sϕ s_x + cϕ s_y)] and n=[n_x n_y n_z], s=[s_x s_y s_z], a=[a_x a_y a_z]: are the orthonormal vectors that describe the platform's orientation.

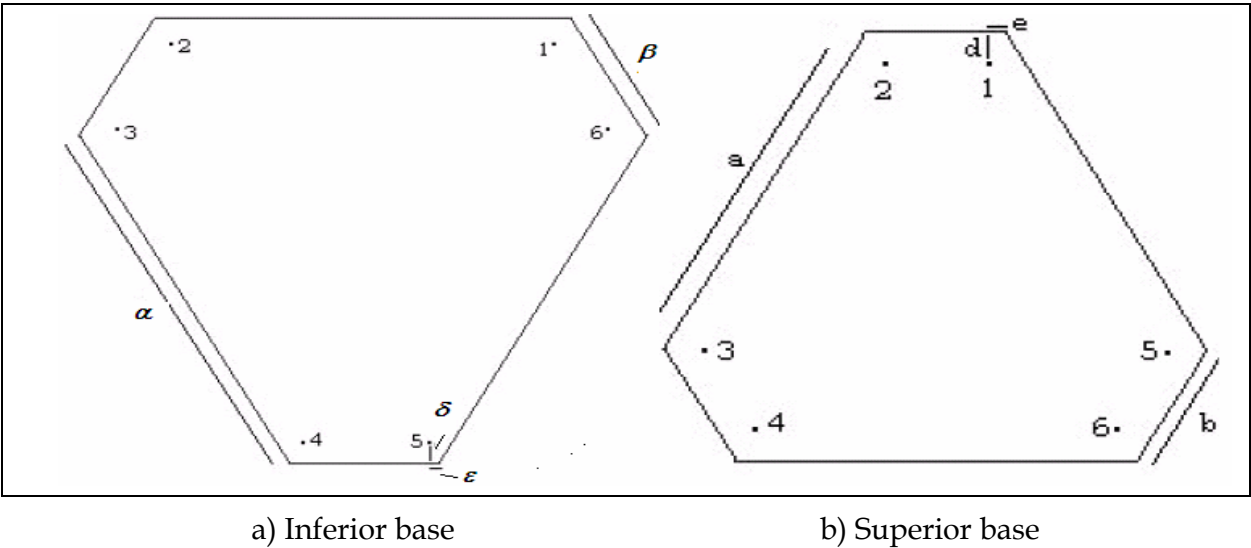


Fig. 2. Platform Geometric Model – Actuators reference points.

This transformation matrix allows changing each actuator's position into a new configuration in order to define the kinematics model as shown in Fig.2 (Kim, Chung & Youmt, 1997)(Li & Salcudean, 1997).

The points that define the upper base motion are located at the extremities of the six linear actuators fixed at the lower base of the platform. When assuming that the actuators have reached their final position and orientation, the problem is calculating the coordinates of the center of mass on the superior base, and the RPY orientation angles (roll, pitch and yaw).

The relative positions can be calculated from the position and orientation analysis (using the transformation matrix), leading to new ones within the platform's workspace.

The position vector for the actuator of the upper/lower base, P_i, P_s , is determined in relation to the fixed reference system at the center of mass of the inferior part as described in (3). The parameters $\alpha, \beta, \delta, \varepsilon, a, b, d, e$ are reported in Fig.2, where h represents the position of the center of mass of the upper base in its initial configuration, and each line of P_i, P_s represents the lower ($A_1 \dots A_6$) and superior ($B_1 \dots B_6$) coordinated extremities of the actuators.

$$P_i = \begin{bmatrix} A_i + \varepsilon & D_i - \delta & 0 \\ -A_i + \varepsilon & D_i - \delta & 0 \\ -A_i + \varepsilon + C_i & D_i - \delta + C_i & 0 \\ -B_i + \varepsilon & D_i + \delta & 0 \\ B_i + \varepsilon & -D_i + \delta & 0 \\ A_i - \varepsilon - C_i & D_i - \delta + C_i & 0 \end{bmatrix} \quad P_s = \begin{bmatrix} A_s + e & D_s - d & h \\ -A_s + e & D_s - d & h \\ -A_s + e + C_s & D_s - d + C_s & h \\ -B_s + e & D_s + d & h \\ B_s + e & -D_s + d & h \\ A_s - e - C_s & D_s - d + C_s & h \end{bmatrix} \quad (3)$$

where, $A_i = 0.5\alpha$, $A_s = 0.5b$, $B_i = 0.5\beta$, $B_s = 0.5a$, $C_i = 2(\varepsilon - B_i)\cos(t)$, $C_s = 2(e - B_s)\cos(t)$, $D_i = (A_i + B_i)\cos(t)$, $D_s = (A_s + B_s)\cos(t)$

Each actuator is associated to a position vector \underline{X}_i considering its inferior end and the value of the distension associated with the i th actuator. With the transformation matrix, \underline{X}_i^T is the new associated position vector for each upper position i th, obtained in (4).

$$\underline{X}_i = T(\psi, \theta, \varphi) \underline{X}_i^T \quad (4)$$

From the known position of the upper base, the coordinates of its extremities are calculated using the previous equations resulting in new ones, whose norm corresponds to the new size of the actuator. If X_0 is the reference point, then the difference between the current sizes and the target ones is the distension that must be imposed to each actuator in order to reach its new position as presented in (5)

$$\Delta L = \left| \underline{X}_i^T - \underline{X}_0 \right| - \left| \underline{X}_i - \underline{X}_0 \right| \quad (5)$$

Thus, the distance between the extremities is calculated using the transformation matrix and the known coordinates. The kinematic model of the platform receives the translation information in vector form and the rotation from a matrix with the RPY angles.

This analysis allows calculating each axes lengths so that the platform moves to the target position, so the required of each linear actuator k connected to the upper mobile base before and after movement is described in Eqs. 6 and 7.

$$L = \sqrt{\sum_{j=1}^3 (P_s^{kj} - P_i^{kj})^2} \quad \text{with} \quad k = 1, \dots, 6 \quad (6)$$

$$L + \Delta L = \sqrt{\sum_{j=1}^3 (T_j^{-1}(\psi, \theta, \phi) P_s^{kj} - P_i^{kj})^2} \quad (7)$$

The links of the platform are defined by:

$$A_i = [r_p \cos(\alpha_i), r_p \sin(\alpha_i), 0]^T = [A_{ix}, A_{iy}, A_{iz}]^T \quad \alpha_i = \frac{i\pi - a_p}{2} \quad \text{for } i=1,3,5 \quad \alpha_i = \alpha_{i-1} + a_p \quad \text{for } i=2,4,6 \quad (8)$$

And the links of the base by:

$$B_i = [r_b \cos(\beta_i), r_b \sin(\beta_i), 0]^T = [B_{ix}, B_{iy}, B_{iz}]^T \quad \beta_i = \frac{i\pi - a_b}{2} \quad \text{for } i=1,3,5 \quad \beta_i = \beta_{i-1} + a_b \quad \text{for } i=2,4,6 \quad (9)$$

Where r_p : radius of platform; r_b : radius of base; a_p : angle of platform and a_b : angle of base

3.2 Kinematic model

The Stewart Platform Manipulator changes its position and orientation as a function of its linear actuator's length. Fig. 3 shows the corresponding geometric model viewed from the top, where the bottom base geometry is formed by the B1 to B6 points, and the upper one by A1 to A6 points.

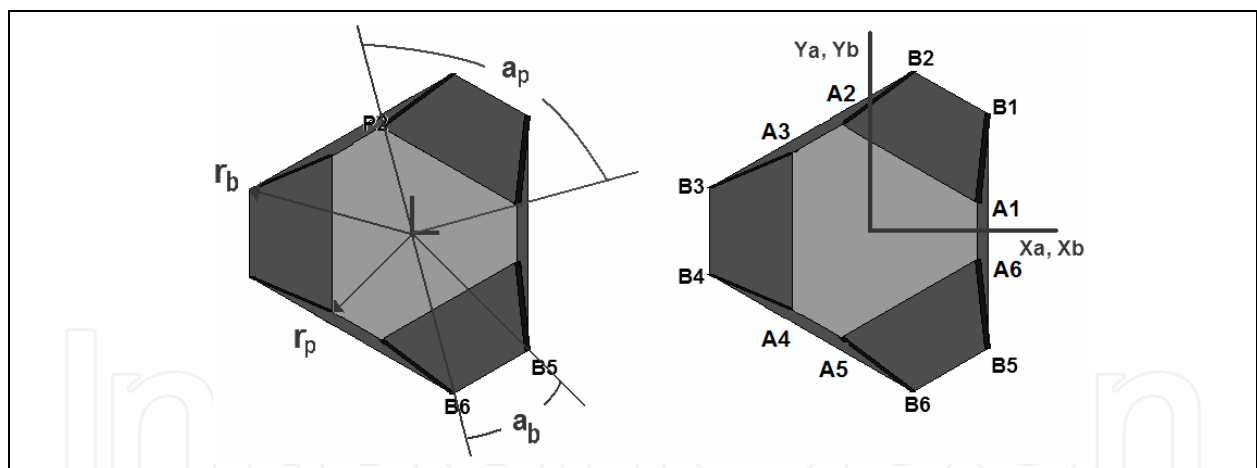


Fig. 3. Stewart Platform geometric model

3.3 Inverse kinematics

The inverse kinematics model of the manipulator expresses the joint linear motion as a position and orientation function due to the fixed coordinate system at the base of the platform (Wang, Gosselin & Cheng, 2002)(Zhang & Chen, 2007), as presented in Eq. 10:

$$l = f(x) \quad (10)$$

Where, $l = (l_1, l_2, l_3, l_4, l_5, l_6)$ is the linear position of the joints, $x = (X, Y, Z, \psi, \theta, \phi)$ is the position vector of the platform, X, Y, Z the cartesian position and ψ, θ, ϕ represents the orientation of

the platform. The reference systems are fixed to $A(u,v,w)$ and $B(x,y,z)$ at the base, as shown in Fig. 4.

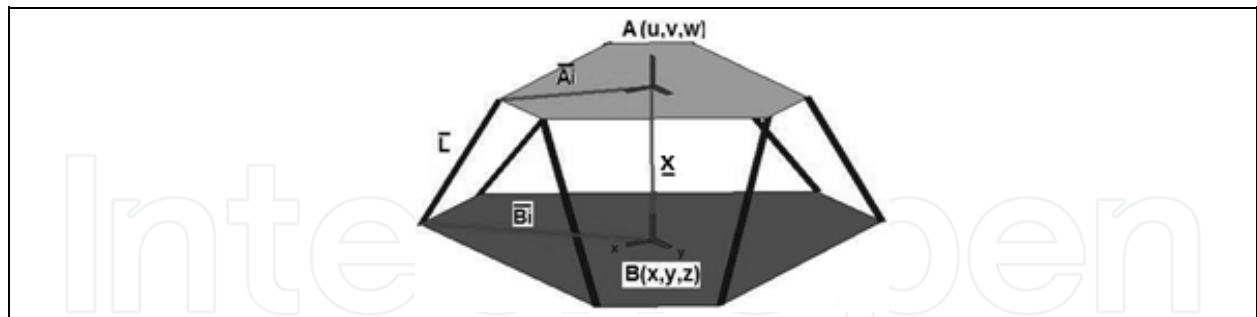


Fig. 4. Vector representation of the manipulator.

The transformation for the mobile platform's centroid to the base, is described by the position vector x and the rotation matrix ${}^B R_A$, where,

$${}^B R_A = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix} \quad (11)$$

The angular motions are expressed as Euler angle rotations in respect to x-axis, y-axis, and z-axis, i.e. roll, pitch and yaw, in sequence.

$${}^B R_A = \begin{bmatrix} c\psi c\phi & c\psi s\phi s\theta - s\psi c\theta & c\psi s\phi c\theta + s\psi s\phi c\theta \\ c\psi c\phi & s\psi s\phi s\theta + c\psi c\theta & s\psi s\phi c\theta - c\psi s\theta \\ -s\phi & c\phi c\theta & c\phi s\theta \end{bmatrix} \quad (12)$$

The vector-loop equation for the i th actuator of the manipulator is as follows:

$$l_i = {}^A R_B A_i + x - B_i \quad (13)$$

By substituting the terms for each actuator, (14) describes the platform motion in relation to its base.

$$l_i^2 = X^2 + Y^2 + Z^2 + r_p^2 + r_b^2 + 2(r_{11}A_{ix} + r_{12}A_{iy})(X - B_{ix}) + 2(r_{21}A_{ix} + r_{22}A_{iy})(Y - B_{iy}) + 2(r_{31}A_{ix} + r_{32}A_{iy})(Z - B_{iz}) - 2(XB_{ix} + YB_{iy} + ZB_{iz}) \quad (14)$$

3.4 Dynamics study

The dynamic equations are derived for the Stewart Platform with a universal joint at the base and a spherical joint at the top of each leg. For this study, it is assumed that there is no rotation allowed on any leg about its own axis, so the kinematics and dynamics for each one considers and calculates the constraining force over the spherical joint at its top.

Finally, the kinematics and dynamics of the platform are considered so the spherical joint forces from all the six legs complete the dynamic equations.

The motion control can be implemented on every joint considering the movements of each actuator (Guo & Li, 2006). Considering the coupling effects and to solve the trajectory

problem, the dynamic control takes the inputs of the system so the drive of each joint moves its links to the target position with the required speed.

The dynamic model of a 6-DOF platform can be calculated with the Euler-Lagrange formulation that expresses the generalized torque (Jaramillo et al, 2006)(Liu, Li and Li, 2000). The dynamic model is described by a set of differential equations called dynamic equations of motion as shown in (15).

$$\tau_i = J_i \ddot{L}_i + F_i \dot{L}_i + \Gamma_i \quad i = 1, \dots, 6 \quad (15)$$

where $\tau_i(t)$ is the generalized torque vector, $L_i(t)$ the generalized frame vector (linear joints), $J_i(t)$ the inertial matrix, $F_i(t)$ the non-linear forces (for example centrifugal) matrix, Γ_i the gravity force matrix.

3.5 Actuator model

Each joint is composed of a motor, a transmission system and an encoder and by considering DC motor (Ollero, Boverie & Goodal, 2005), its three classic equations are presented in Eq. 16

$$\begin{aligned} u(t) &= L_{mot} \frac{di(t)}{dt} + R_{mot} i(t) + K_E \frac{d\theta_m(t)}{dt} \\ T_m(t) &= J_{eq} \frac{d^2 \theta_m(t)}{dt^2} + B_{eq} \frac{d\theta_m(t)}{dt} = K_T i(t) \end{aligned} \quad (16)$$

where $T_m(t)$ is the torque, $\theta_m(t)$ the angular position of the motor axis, $i(t)$ the current, L_{mot}, R_{mot} respectively the inductance, resistance, J_{eq}, B_{eq} the inertia, friction of the axis load calculated on the motor side.

4. Control structure

A simulation environment allows implementing and testing advanced axis control strategies, such as Predictive Control, which is a well known structure for providing improved tracking performance. The purpose of the control structure is to obtain a model of the system that predicts the future system's behaviour, calculates the minimization of a quadratic cost function over a finite future horizon using future predicted errors. It also elaborates a sequence of future control values; only the first value is applied both on the system and the model, finally the repetition of the whole procedure at the next sampling period happens accordingly to the preceding horizon strategy (Li & Salcudean, 1997) (Nadimi, Bak & Izadi, 2006) (Remillard & Boukas, 2007) (Su et al, 2004).

4.1 Model

The Controlled Autoregressive Integrated Moving Average Model (CARIMA) form is used as numerical model for the system so the steady state error is cancelled due to a step input or disturbance by introducing an integral term in the controller (Clarke, Mohtadi & Tuffs,

1987). The predictive control law uses an external input-output representation form, given by the polynomial relation:

$$A(q^{-1})y(k) = B(q^{-1})u(k-1) + \frac{\xi(k)}{\Delta(q^{-1})} \quad (17)$$

where u is the control signal applied to the system, y the output of the system, $\Delta(q^{-1}) = 1 - q^{-1}$ the difference operator, A and B polynomials in the backward shift operator q^{-1} , of respective order n_a and n_b , ξ an uncorrelated zero-mean white noise.

4.2 Predictive equation

The predictive method requires the definition of an optimal j -step ahead predictor which is able to anticipate the behaviour of the process in the future over a finite horizon. From the input-output model, the polynomial predictor is designed under the following form:

$$\hat{y}(k+j) = \underbrace{F_j(q^{-1})y(k) + H_j(q^{-1})\Delta u(k-1)}_{\text{free response}} + \underbrace{G_j(q^{-1})\Delta u(k+j-1) + J_j(q^{-1})\xi(k+j)}_{\text{forced response}} \quad (18)$$

where F_j , G_j , H_j and J_j , unknown polynomials, corresponding to the expression of the past and of the future, are derived solving Diophantine equations, with unique solutions controller (Clarke, Mohtadi & Tuffs, 1987).

4.3 Cost function

The GPC strategy minimizes the weighted sum of the square predicted future errors and the square control signal increments:

$$J = \sum_{j=N_1}^{N_2} (\hat{y}(k+j) - w(k+j))^2 + \lambda \sum_{j=1}^{N_u} \Delta u(k+j-1)^2 \quad (19)$$

Assuming that $\Delta u(t+j) = 0$ for $j \geq N_u$. Four tuning parameters are required: N_1 , the minimum prediction horizon, N_2 the maximum prediction horizon, N_u the control horizon and λ the control-weighting factor.

4.4 Cost function minimization

The optimal j -step ahead predictor (20) is rewritten in matrix form:

$$\hat{\mathbf{y}} = \mathbf{G}\tilde{\mathbf{u}} + \mathbf{if}(q^{-1})y(t) + \mathbf{ih}(q^{-1})\Delta u(t-1) \quad (20)$$

ith:

$$\begin{aligned} \mathbf{if}(q^{-1}) &= \begin{bmatrix} F_{N_1}(q^{-1}) & \cdots & F_{N_2}(q^{-1}) \end{bmatrix}' & \tilde{\mathbf{u}} &= [\Delta u(t) \quad \cdots \quad \Delta u(t+N_u-1)]' \\ \mathbf{ih}(q^{-1}) &= \begin{bmatrix} H_{N_1}(q^{-1}) & \cdots & H_{N_2}(q^{-1}) \end{bmatrix}' & \hat{\mathbf{y}} &= [\hat{y}(t+N_1) \quad \cdots \quad \hat{y}(t+N_2)] \end{aligned} \quad (21)$$

$$\mathbf{G} = \begin{bmatrix} g_{N_1}^{N_1} & g_{N_1-1}^{N_1} & \cdots & \cdots \\ g_{N_1+1}^{N_1+1} & g_{N_1}^{N_1+1} & \cdots & \cdots \\ \cdots & \cdots & \cdots & \cdots \\ g_{N_2}^{N_2} & g_{N_2-1}^{N_2} & \cdots & g_{N_2-N_u+1}^{N_2} \end{bmatrix} \tag{22}$$

The future control sequence is then obtained by minimizing the criterion (23) (Clarke, Mohtadi and Tuffs, 1987):

$$\tilde{\mathbf{u}} = \mathbf{M} \left[\mathbf{w} - \mathbf{i}f(q^{-1})y(t) - \mathbf{i}h(q^{-1})\Delta u(t-1) \right] \tag{23}$$

with:

$$\mathbf{M} = \mathbf{Q} \mathbf{G}', N_u \times (N_2 - N_1 + 1), \mathbf{Q} = \left[\mathbf{G}'\mathbf{G} + \lambda \mathbf{I}_{N_u} \right]^{-1}, \mathbf{w} = \begin{bmatrix} w(t+N_1) & \cdots & w(t+N_2) \end{bmatrix} \tag{24}$$

4.5 RST form controller

The minimization of the previous cost function (Clarke, Mohtadi & Tuffs, 1987), results in the predictive controller derived in the RST form according to Fig. 5 and implemented through a differential equation in (25).

$$S(q^{-1})\Delta(q^{-1})u(t) = -R(q^{-1})y(t) + T(q)w(t) \tag{25}$$

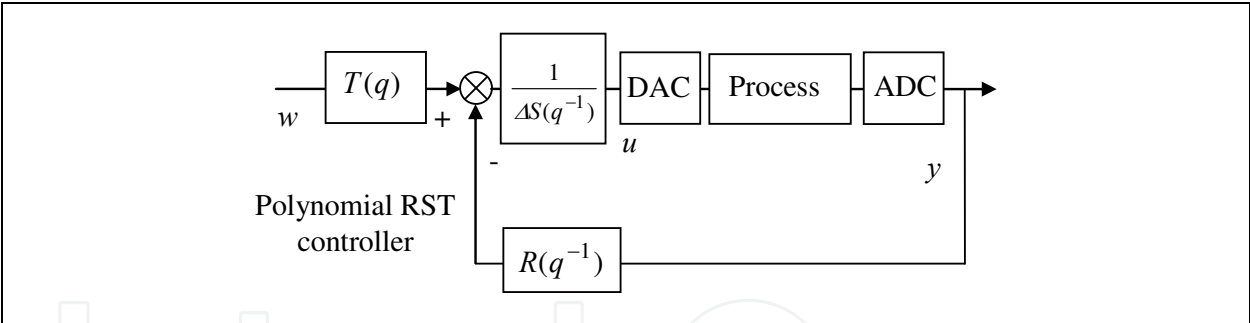


Fig. 5. GPC in a RST form.

The main feature of this RST controller is the non-causal form of the T polynomial, creating the anticipative effect of this control law.

4.6 Complete model implementation

Taking the x_r as the system's input trajectory the objective is to calculate the actuator's length l_r for each sampled position. Mechanism and actuator controller dynamic effects are considered over the six legs having as outputs their δ_{ld} and previous position x_{i-1} , this is done in order to calculate the current manipulator position x_o , x_f is determined by the length of the actuator l_o . Then these values are compared with the target position in order to estimate the error δ_l between the reference position x_r and the manipulator's position x_o after all the dynamics effects have been considered (Fig. 6 and Fig. 7) (Hunt, 1978)(Jaramillo et al, 2006) (Ghobakhloo, Egtesad & Azadi, 2006).

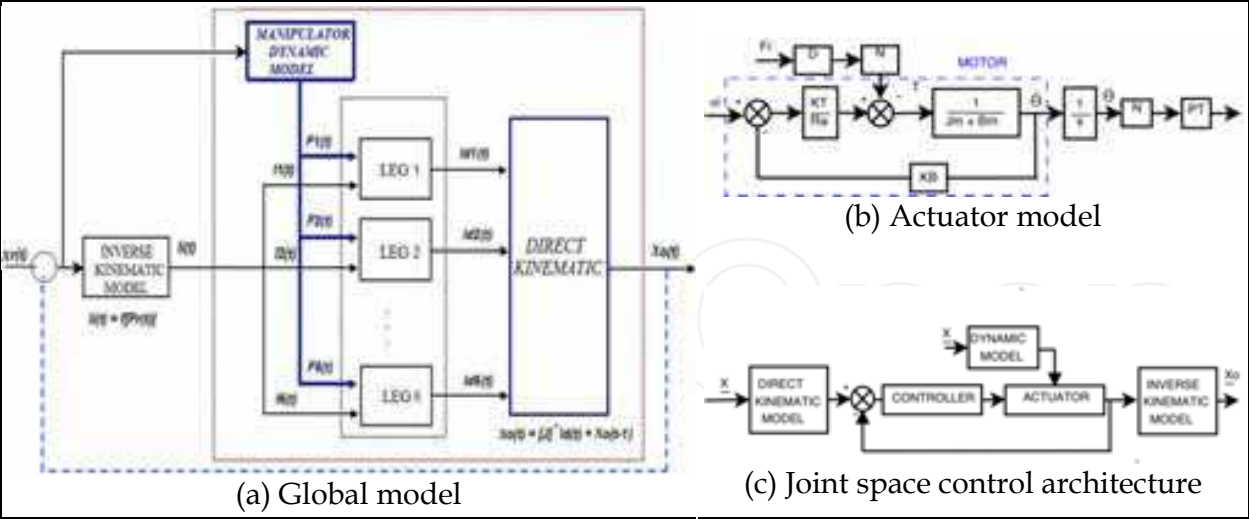


Fig. 6. Total system Model

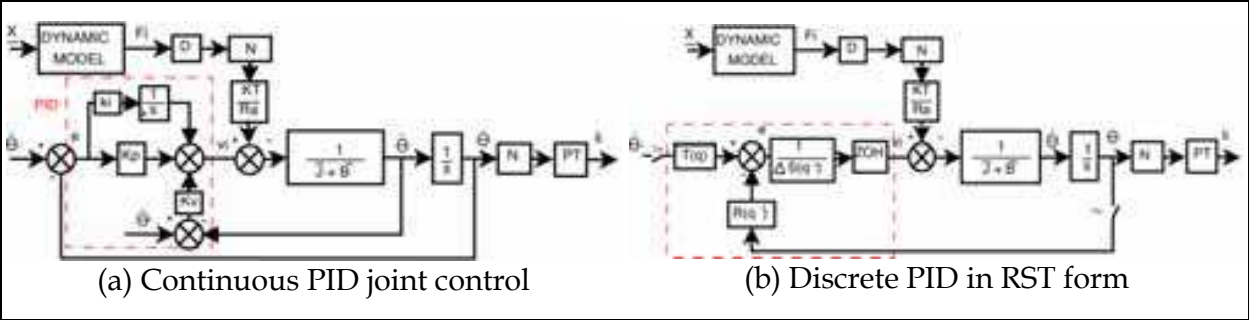


Fig. 7. Continuous and Discrete PID Controller.

$$\begin{aligned} \text{degree}\big(R(q^{-1})\big) &= \text{degree}\big(R(q^{-1})\big) \\ \text{degree}\big(S(q^{-1})\big) &= \text{degree}\big(B(q^{-1})\big) \\ \text{degree}\big(T(q)\big) &= N_2 \end{aligned} \tag{44}$$

The GPC has shown to be an effective strategy in many fields of applications, with good time-domain and frequency properties (small overshoot, improved tracking accuracy and disturbance rejection ability, good stability and robustness margins), is able to cope with important parameters variations.

5. Simulation

The modelling of the Parallel Manipulator leads to the design of a simulator adopting electric and mechanical libraries blocks using Simulink (Gosselin, Lavoie & Toutant, 1992). The main elements of the robotics joints are brushless DC motor drives, axis inertia, gears and control blocks. Other elements of the manipulator (including loads) are represented by three nonlinear models, one for each motor drive. The control system itself consists, essentially, in a cascade of control loops (for each axis). The inner speed and torque control loops are part of the drive model where only the position loop is explicitly modelled. In fact,

the position control of the manipulator can be implemented through the control feedback of each isolated joint (Cappel, 1967).
The developed simulator also includes a path generation module, providing the joints with axis trajectories as reference signal for controlling each of the parts (Jaramillo et al, 2006). Finally, a graphic interface is developed, showing the results of joint motion obtained through typical trajectories. The simulation software was implemented using Matlab ® and programmed with the equations of the Stewart Platform manipulator. This interface allows the input of the dynamic simulation parameters: mass and inertia of the mobile platform, actuator parameters and the gains of the PID controller. Fig. 8 shows a screen capture of the developed interface.

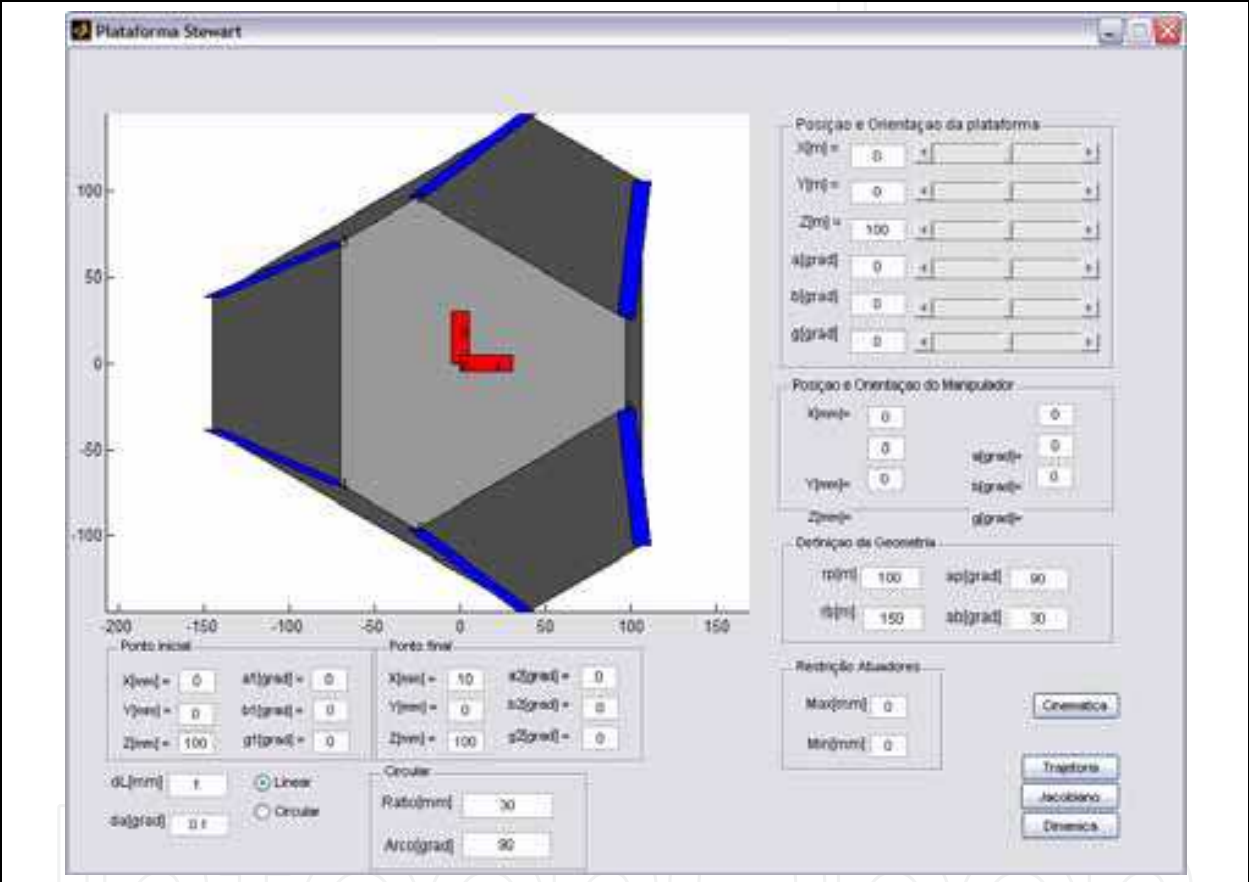


Fig. 8. Implemented simulation environment

In Fig. 9 the overall block diagram with the dynamic and control model (Fig. 3) implemented in Simulink is presented
The considered system used for supervision and control implementation includes 3 DC motors, a 1:100 gear box (N), a ball screw transmission (for joint 1 only) and incremental encoders (Table 1).The joint controllers are designed independently, resulting in three RST parameters, considering the same axis motor but with different inertia on the motor side due to different geometrical features for each one.
Four tuning parameters are required: N_1 the minimum prediction horizon, N_2 the maximum prediction horizon, N_u the control horizon and λ the control weighting factor. These are given in Table 2 have been chosen to provide good stability and robustness margins (Clarke, Mohtadi, & Tuffs, 1998).

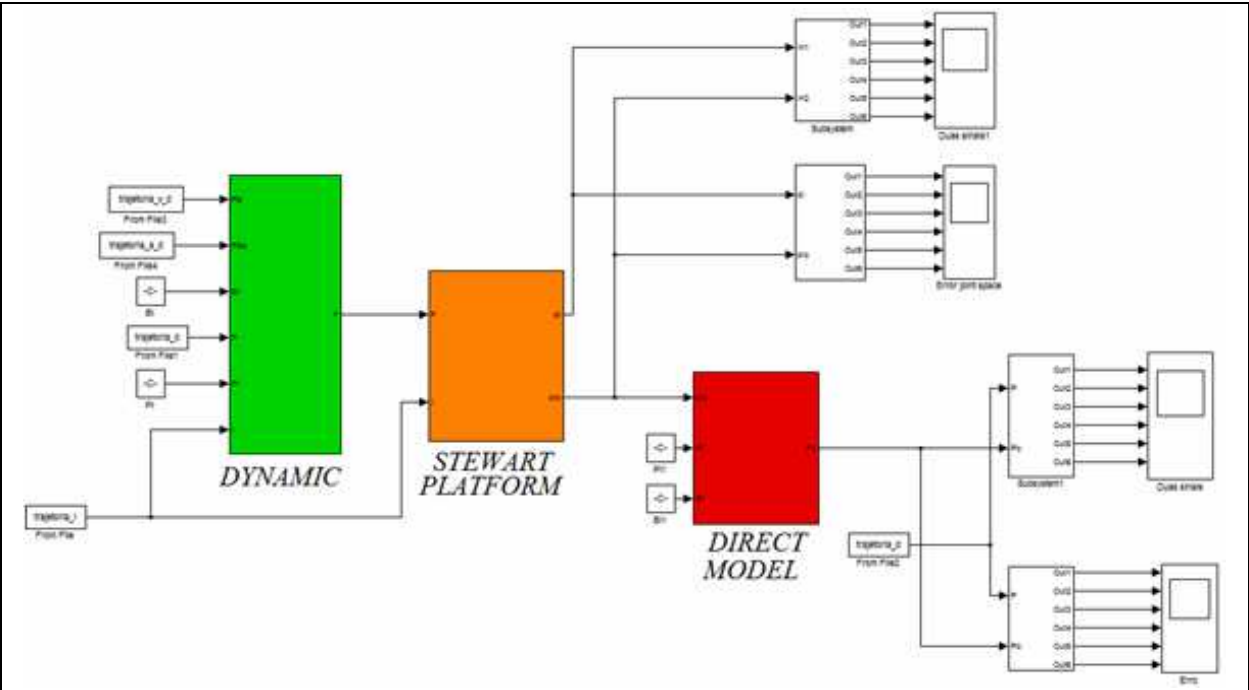


Fig. 9. Simulink Dynamic and control Model

Jm - Inertia (kgm ²)	0.71 10 ⁻³
Weight (kg)	8
Mechanical time constant (ms)	1.94
Voltage constant (V/rad/s)	0.807
Torque constant (Nm/ A)	1.33
L - Inductance (mH)	14.7
R - Resistance (Ω)	1.44

Table 1. Motor Parameters.

Joint	N ₁	N ₂	N _u	λ
1	1	8	1	92
2	1	8	1	107.3
3	1	8	1	126

Table 2. GPC tuning parameters for each joint.

5.1 Manipulator geometry variation: case study

The manipulator workspace and behaviour can be studied from the variation and simulation of various upper and bottom plate geometries, these configurations are presented in Fig. 10 with their corresponding geometry parameters. Once the geometry of each plate is chosen, motion to target positions can be simulated using the implemented path generator, Fig. 11 presents a circular path over a *xy* plane. An initial point of the circular trajectory on the *xy* plane is presented in Fig. 11.

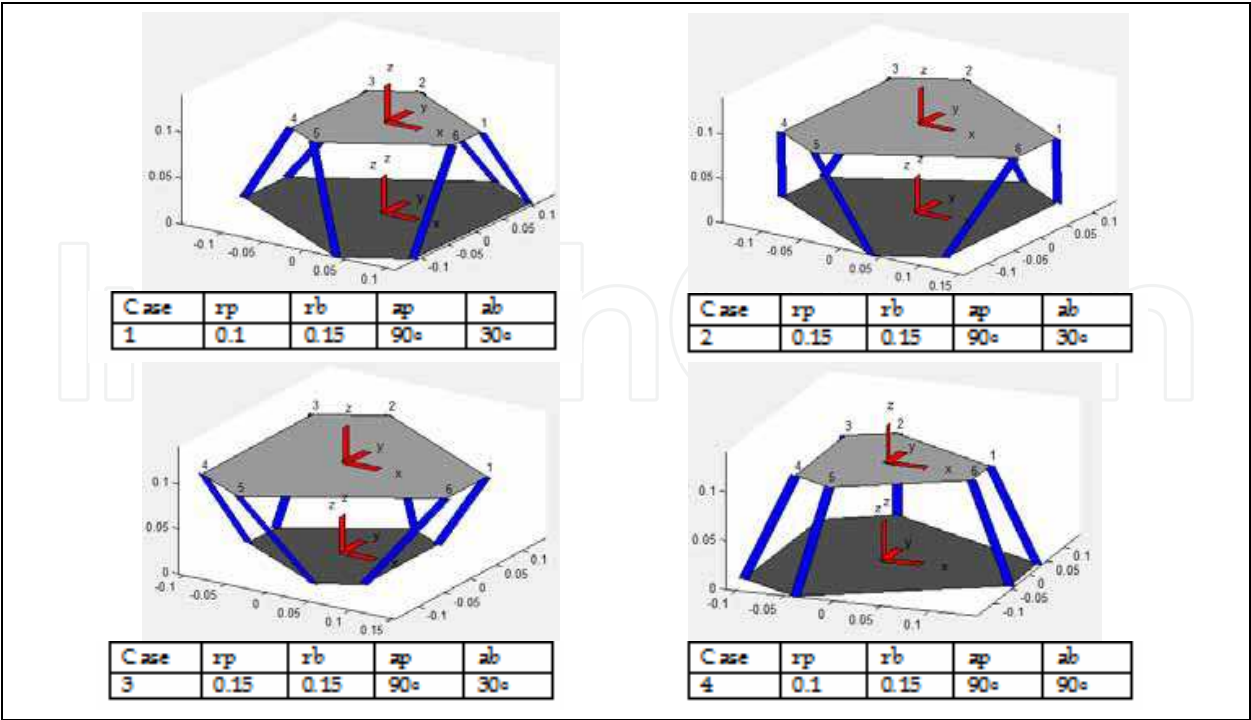


Fig. 10. Top and bottom implemented base geometries and parameters

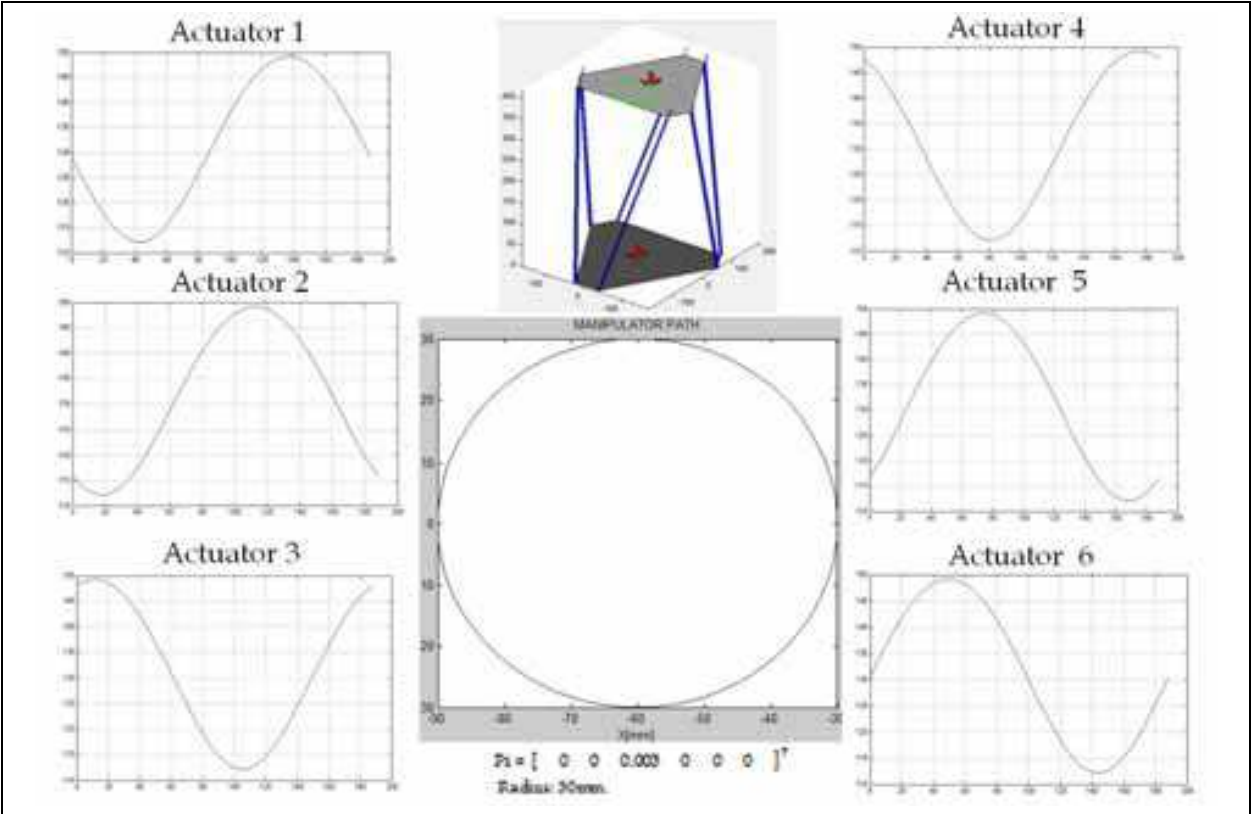


Fig. 11. Path Generator Results

The maximum velocity for this workspace trajectory is 2mm/s and the maximum acceleration is 0.1 mm/s² (Fig. 12).

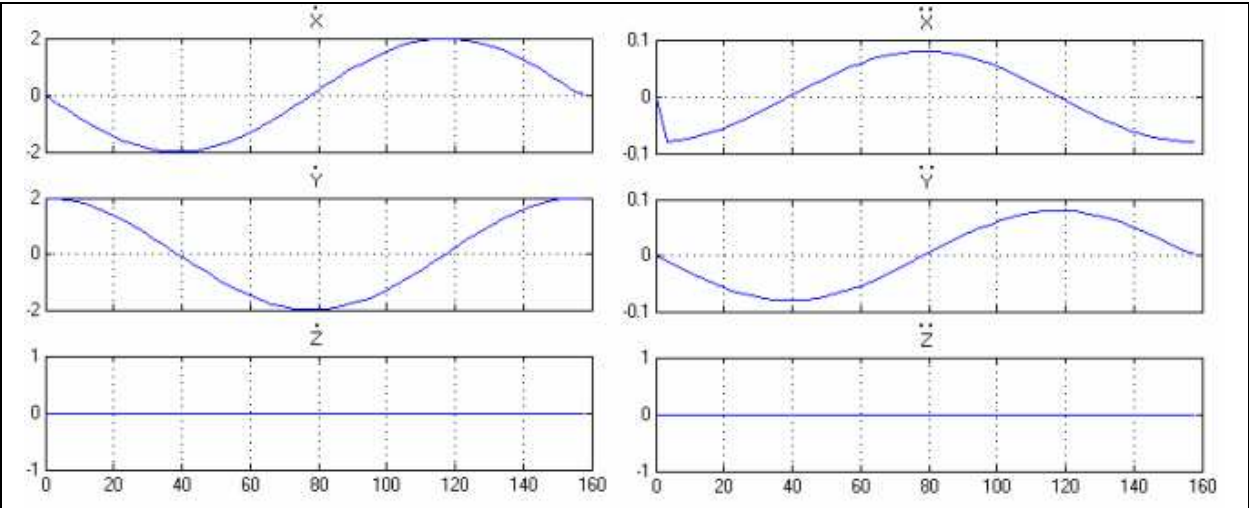


Fig. 12. a. workspace velocity b. workspace acceleration

The joint space trajectory corresponding to the target workspace path for each actuator $l_i(t)$ is obtained through the inverse kinematics model obtaining the trajectories trajectories presented in Fig. 13.

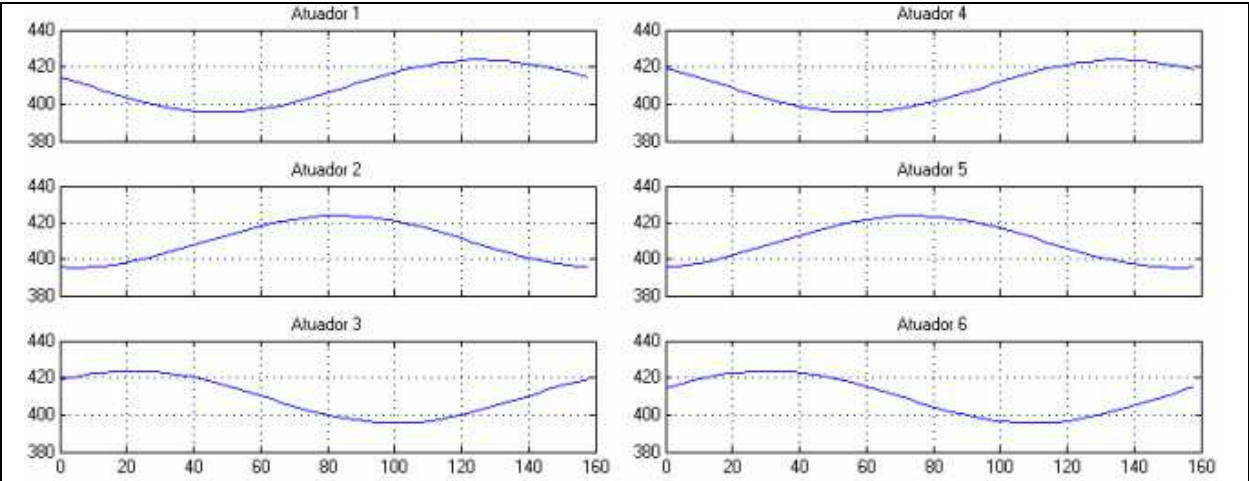


Fig. 13. Joint space trajectory

The singular configurations with various conditions along the trajectory are analyzed (Fig. 14), in this case, the variation of the singular number respect to the initial condition is 2.52%; with this small variation singular configurations are avoided, while in other cases changing the number of conditions results in higher singularities.

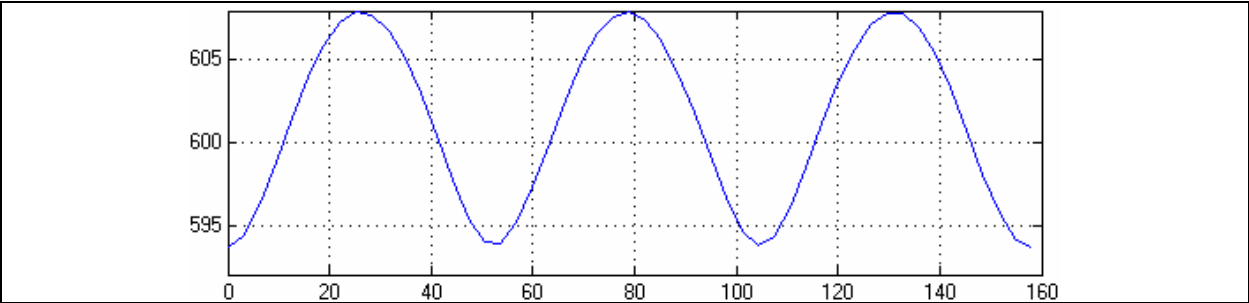


Fig. 14. Singular Analyses.

The constant workspace volume of the manipulator is also evaluated (Fig. 15). This useful characteristic helps to plan new workspace trajectories with constant orientation.

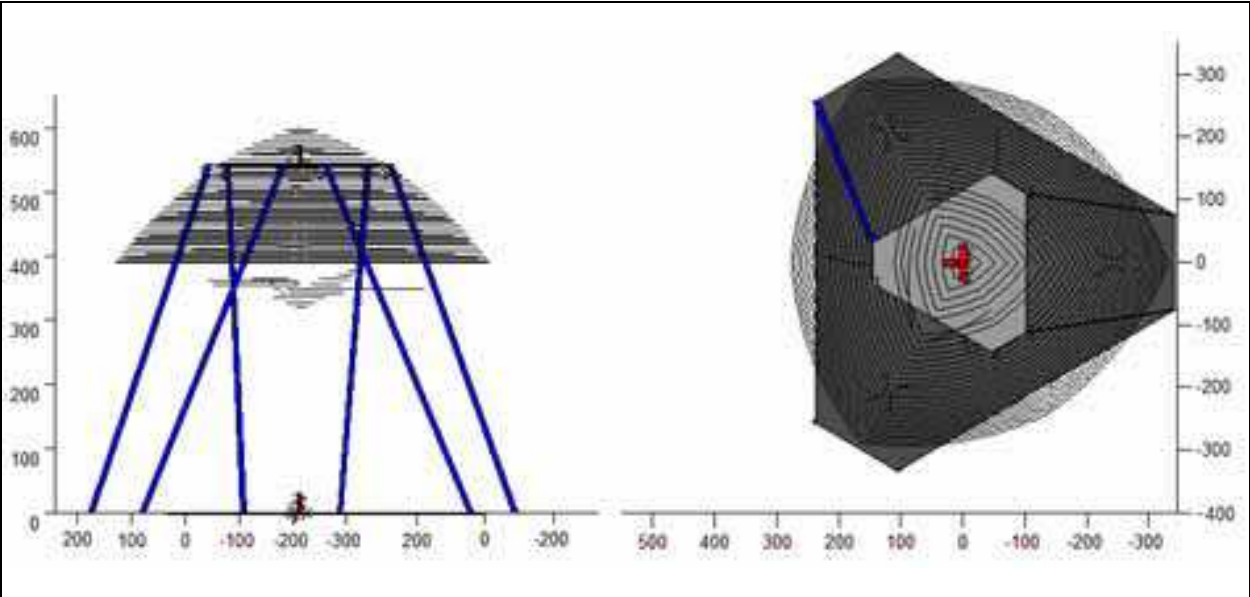


Fig. 15. Work space volume

5.2 Dynamics study

In order to perform the dynamic study and analyze the associated effects of various forces over the platform, the entire system has been modelled in a Simulink environment. The obtained model is composed of of one equation and four integration blocks for calculating velocity and position from the known acceleration. In addition, to simplify the implementation of the simulation, the platform initial conditions are declared through an initialization button. Finally a graph button allows the visualization of the results after simulation.

The simulation tests were performed using values defined in subsection 5.1, and also the initial position of the center of gravity of the following platform:

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$$\begin{aligned} T_o &= \begin{bmatrix} 0.1 & 0 & 0.395 \end{bmatrix} \text{ m} \\ \theta_o &= \begin{bmatrix} 0.1 & 0 & -0.2 \end{bmatrix} \text{ rad} \end{aligned}$$

The initial position of the 3D platform is presented in Fig. 16a, where a 50N constant force is applied on each arm for 0.5 s resulting in the position of the platform shown in Fig. 16b. During this movement the change of position, linear and angular velocities of the center of gravity is calculated and presented in Fig.17.

5.3 Control analysis

For joint space position control the PID controller is tuned with the following gains: $K_p=100$, $K_i=1$ and $k_d=1$. the $li(t)$ input and $ld(t)$ output joint space trajectory is presented in Fig. 18.

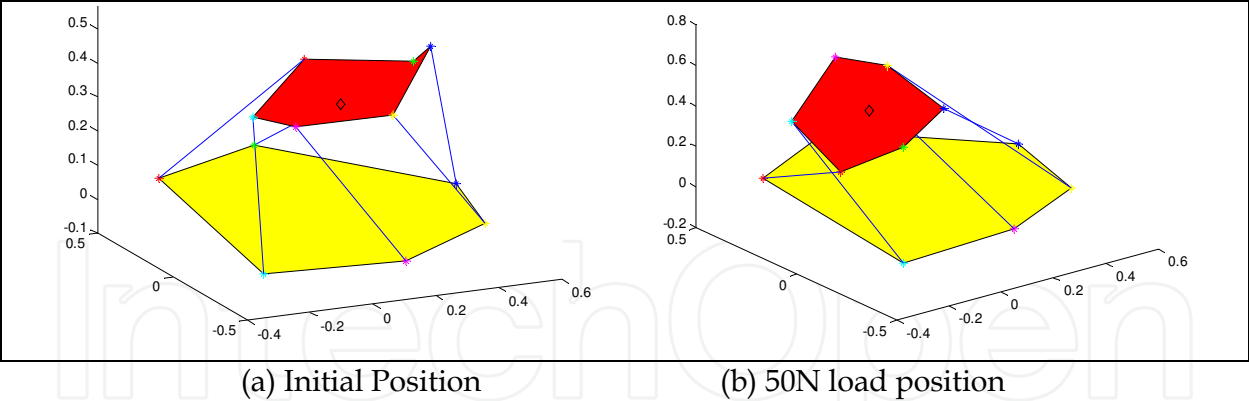


Fig. 16. Stewart Platform Positions

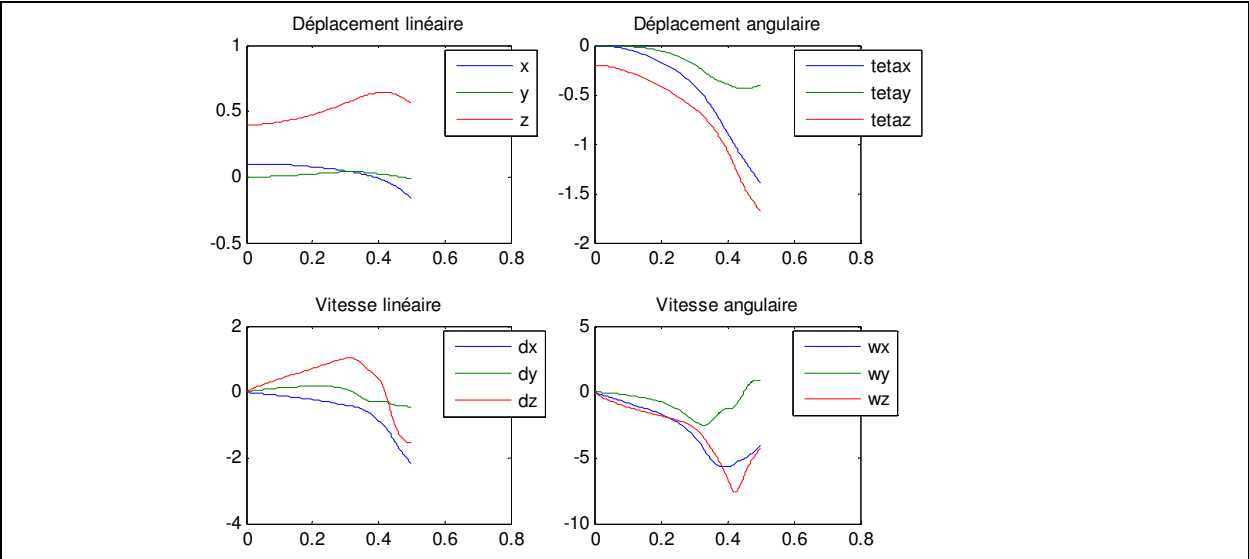


Fig. 17. Linear and angular displacement of of the center of gravity of the Stewart Platform.

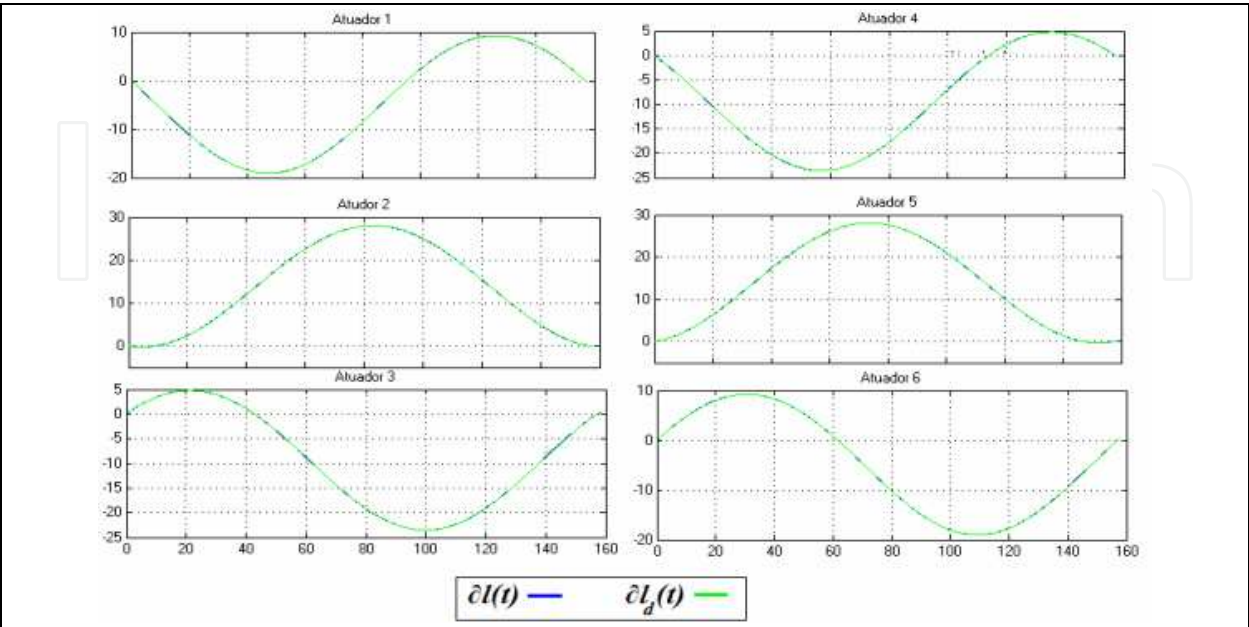


Fig. 18. Input and output joint space trajectory.

The maximum joint space error is 0.1 mm in all the actuators resulting in a maximum motion of 30 mm or 0.333%.

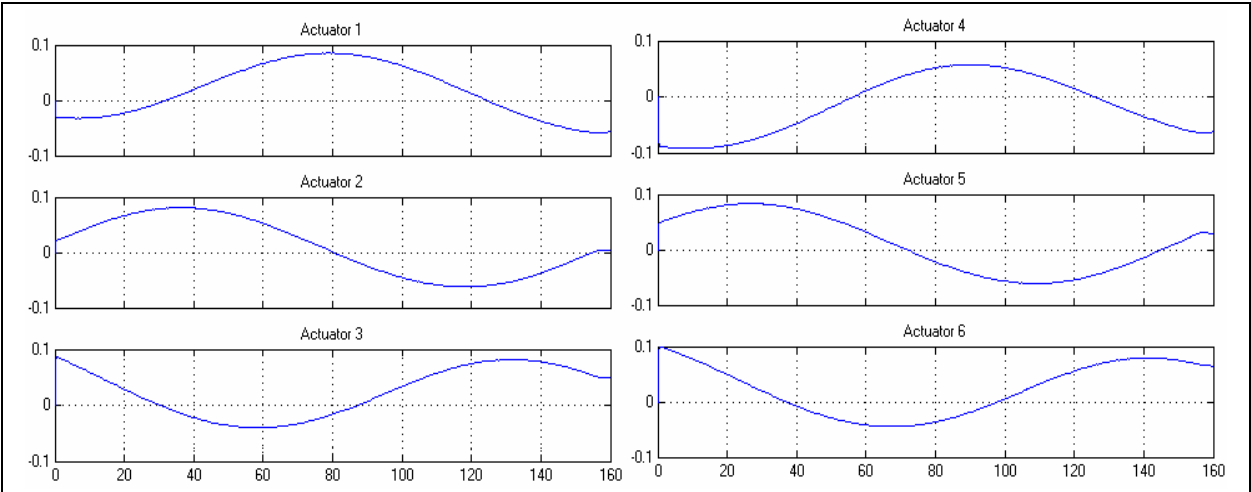


Fig. 19. Joint Space error

Applying the forward kinematics for calculating and comparing the workspace output x_0 is calculated and compared with the workspace input x_r .

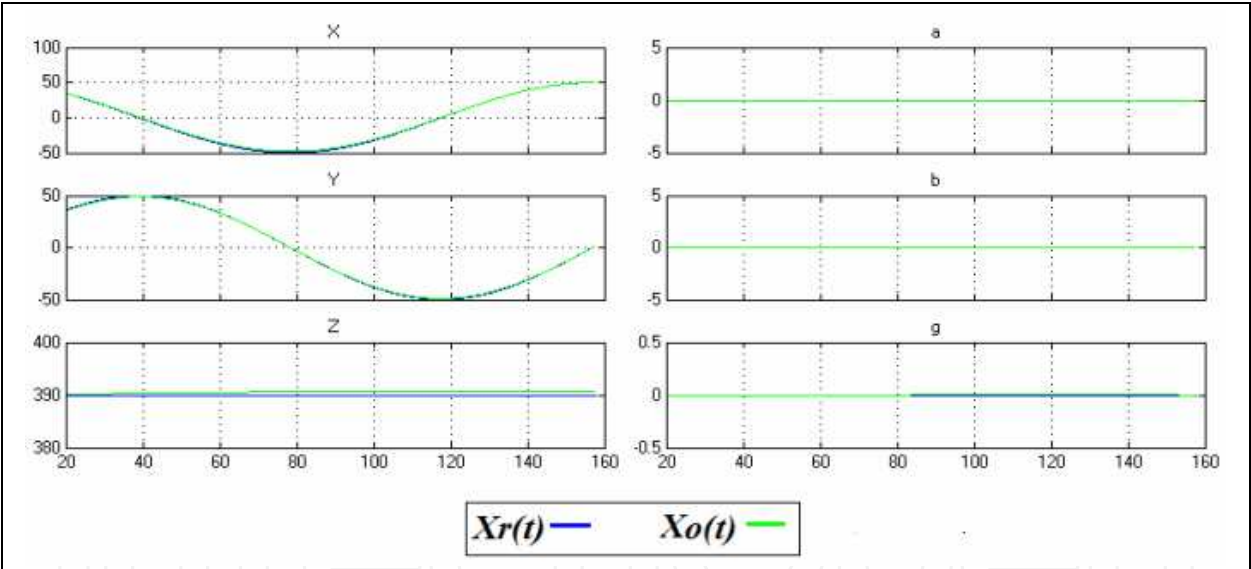


Fig. 20. Output and input workspace trajectory

The maximum work space error is 0.5 mm for a maximum linear motion of 390 mm in the z axis (Fig. 21).

6. Supervision and control architecture

The purpose of implementing a supervisory system over the platform is to permit an easy, fast adaptation and expansion of the system due to current technological trends, resulting in better portability and scalability of the system. Through the structure division in functional blocks, with very specific dedicated interfaces, the project implementation becomes more efficient. The rapid prototyping tools allow designing integrated environments for

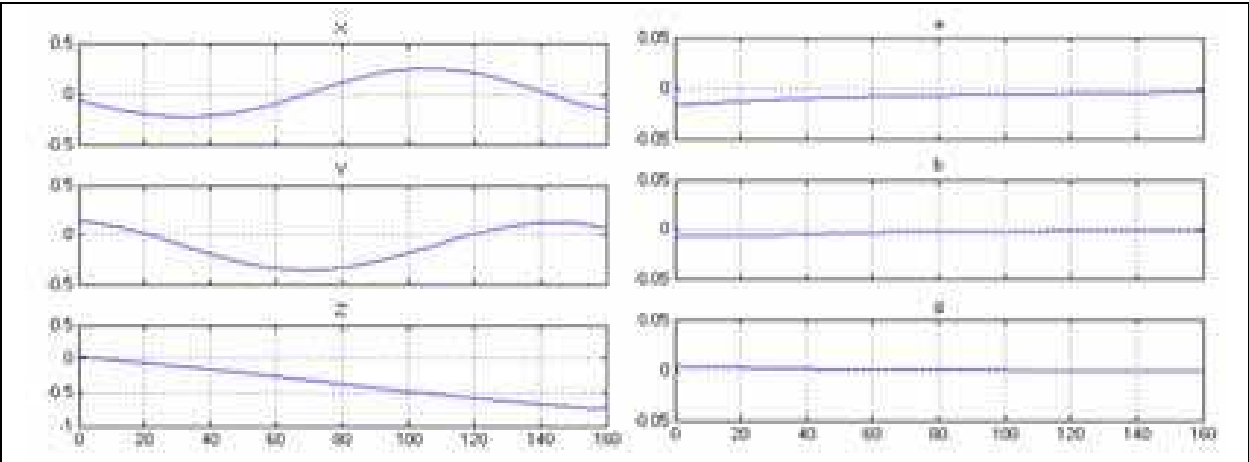
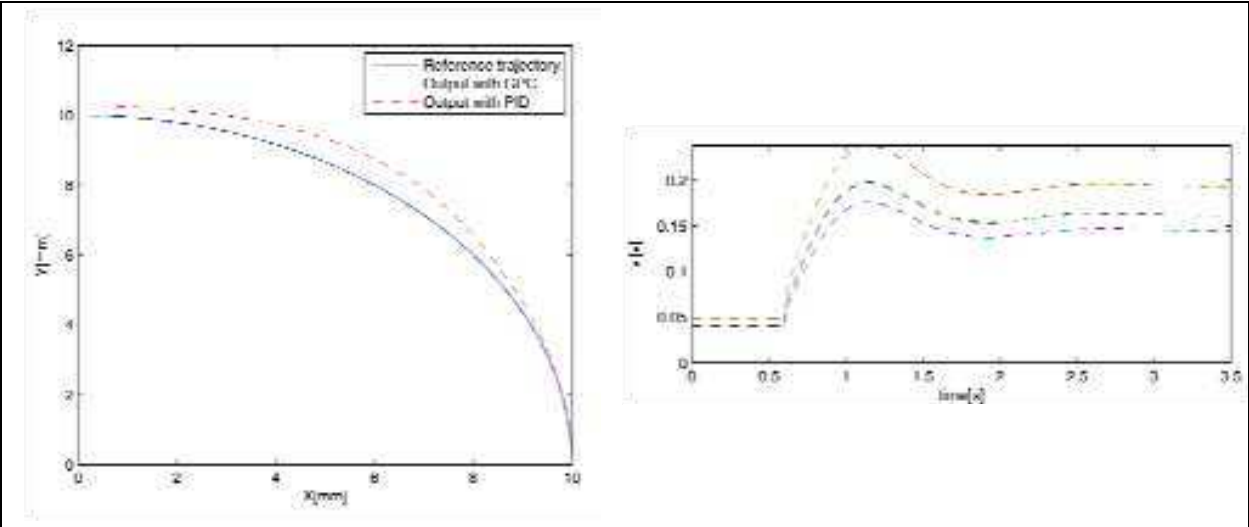


Fig. 21. Work space error



a) Tracking error

b) Disturbance reaction, PID

Fig. 22. Time domain simulation results, tracking error and disturbance reaction

modelling, simulating, and testing algorithm development, through components that simulates the dynamic models of the mechatronic systems; performs complex simulation of the overall system and environment; generates programming code for embedded robot control, and communicates with the platform for controlling it locally or remotely (McCallion, 1977).

The proposed control architecture is a set of implemented hardware and software modules emphasizing on rapid prototyping systems integrated to support the development of the platform tasks.

6.1 Control levels

In the supervisory control level, the supervision of a generic platform task can be achieved through the execution of global control strategies. This level also allows correcting the task execution according to the data obtained through the sensors. The embedded control level is dedicated for executing control strategies allowing locally decision making, with occasional corrections from the supervisory control level. The local control is restricted to local

strategies associated with the sensors and actuators data. The strategies in this level can be implemented under a rapid prototyping framework like FPGA, as described in Fig. 23.

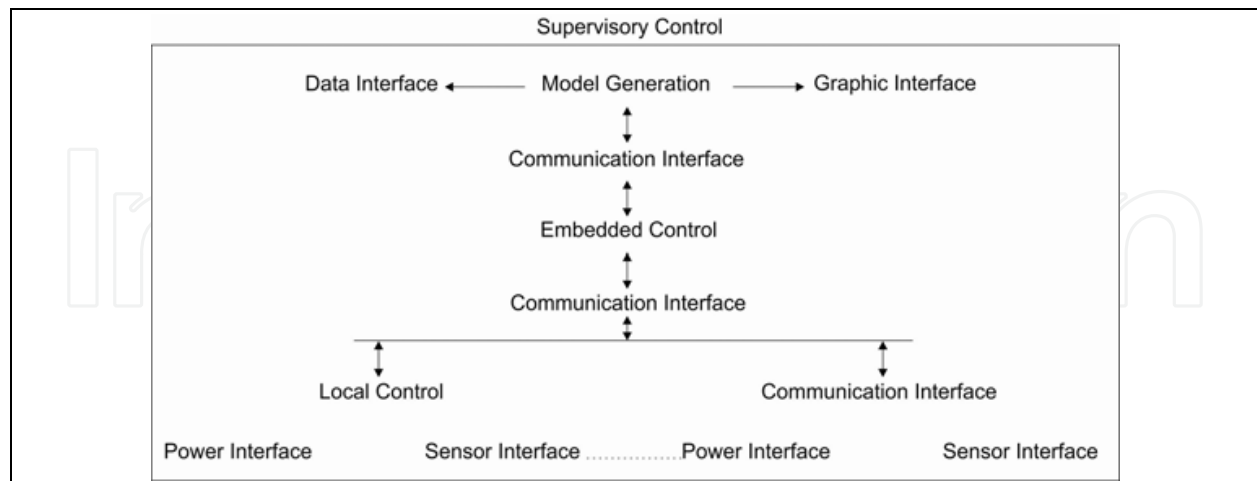


Fig. 23. Stewart-Gough Platform – Control Architecture.

6.2 Embedded level

At the embedded control level two main tasks are implemented: the command decoder and the logic control. The first task decodes commands received by the embedded communication interface (from supervisory control), allowing different actions to be executed according to the received data. The second task generates control signals to actuators' interfaces and receives signals from sensors' interfaces, both located at local control level, so control strategies are implemented in the logic control block.

The prototype uses a FPGA from Altera (Stratix II EP2S60) (Altera, 2008), the configware blocks were implemented in VHDL or Graphic language in the Altera's development platform Quartus II. The embedded control strategies in the logic control block were development using C++ language, in a system-on-a-programmable-chip (SOPC) environment or through the use of blocks implemented in reconfigurable hardware.

6.3 Position control using FPGA

The objective of the proposed controller is to control the linear actuators of the platform. It is able to process the digital signals from the encoders coupled to each linear actuator and the digital signals of the target trajectory. For example, a PID digital controller written in a RST form can be implemented in PLD, with the fitted gain parameters through external programming. The controller's output is a digital signal for the PWM power block. Various implementations of the digital PID (Proportional-Integrative-Derivative) controllers are implemented, and, consequently tuning parameters are necessary for fulfilling the different performance requirements, or to endure different levels of operating noise. A typical implementation of a PID controller can be achieved using a set of differential equations, as follows:

$$U[n] = P[n] + I[n] + D[n], \quad (45)$$

$$P[n] = Kp \cdot e[n], \quad (46)$$

$$I[n] = I[n - 1] + \frac{Kp \cdot Ts}{2 \cdot Ti} (e[n] - e[n - 1]) \tag{47}$$

$$D[n] = \frac{(pTs - 2)}{(pTs + 2)} \cdot D[n - 1] + \frac{2 \cdot Kp \cdot Td}{Ts \cdot (pTs + 2)} \cdot (e[n] - e[n - 1]) \tag{48}$$

where: $U[n]$ is the current control signal resultant, $P[n]$ the current proportional control signal, $I[n]$ the current integral control signal, $D[n]$ is composed of the proportional, derivative and integral parameters (K_p , T_d and T_i) where T_s is the sampling time, respectively. Also, $e[n]$ the current error sample, and finally, $e[n-1]$ the previous error sample. A register error block stores values of $e[n]$ and $e[n-1]$, and makes shift operations ($e[n-1] = e[n]$ and $u[n-1] = u[n]$). An output register block stores $u[n]$ and $u[n-1]$.

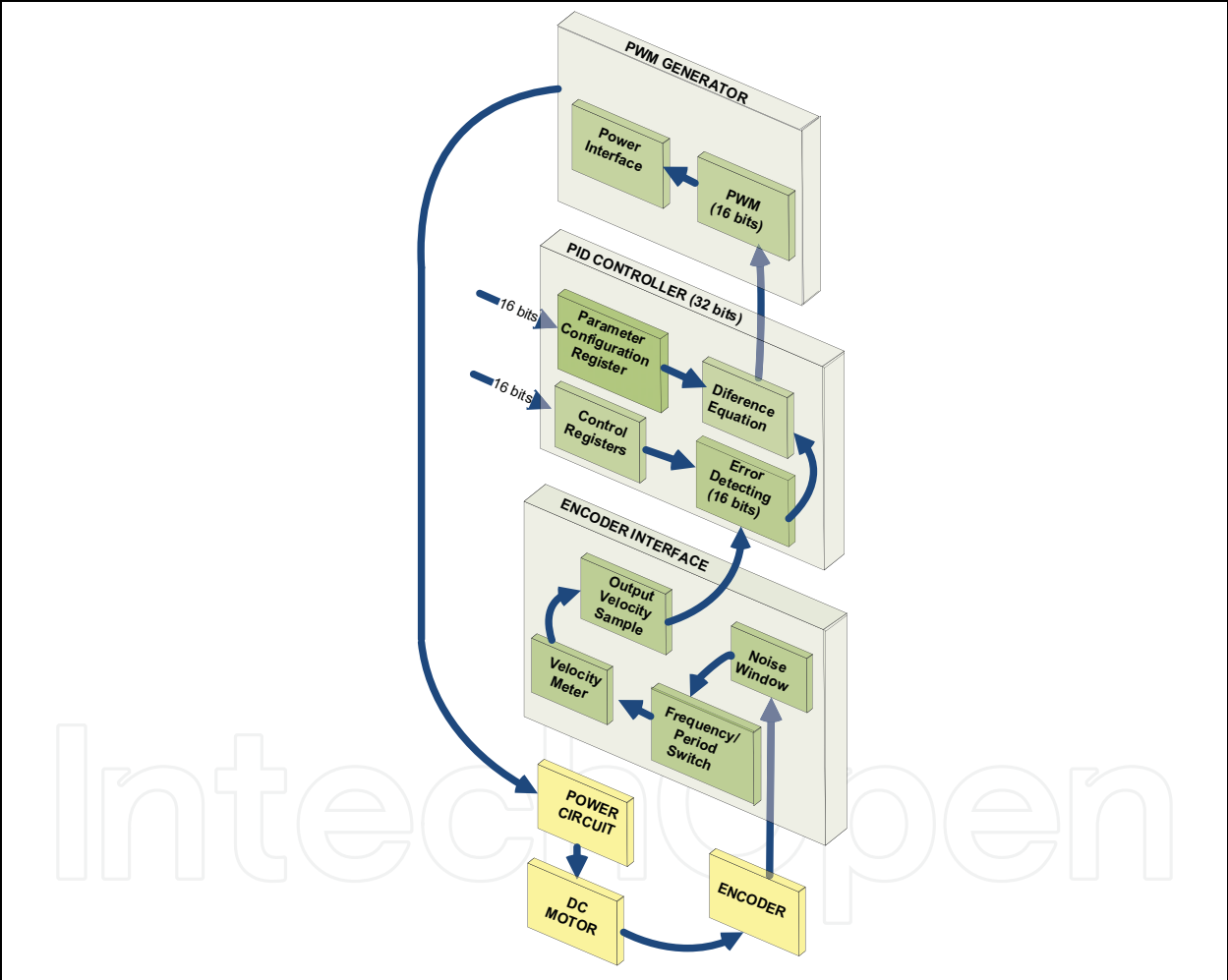


Fig. 24. Embedded DC motor control blocks.

Some of the blocks are described as follows: **Error Detecting** is used for comparing of the reference input and output velocity signals, allowing the generation of a proportional binary word to the error among the periods of the signs. The obtained output of this block is $U[n]$, **Difference Equation** implements the PID digital controller, using the gain parameters (K_p , T_s and T_i) contained in the control input registers. **Control Register** implements the control registers, responsible for the programming of several operational parameters, including the

gain parameters. **PWM and Power Interface** converts the binary word supplied by PID controller in a pattern of digital signs to control the PWM potency block.

The considered reconfiguration in the interface and logical block design eases testing, implementation and future updating, due to this, the development of systems based on reconfigurable computing present well-suited features for developing this kind of problem. The synchronized control of the actuator system can be easily achieved through the same PLD.

6.4 Prototyping environment

A simulation tool was developed for the 6 DOF parallel manipulator, including motor drives, gear boxes, kinematic and dynamic models, and design of the control system for three axes. Simulations described below consider trajectories issued from the path generation module. The model was tested first in Matlab-Simulink language and the final control hardware implementation was performed in visual programming using LabVIEW™ software (Fig. 25). This last one is used for communication purposes between the program and the control hardware of the prototype.

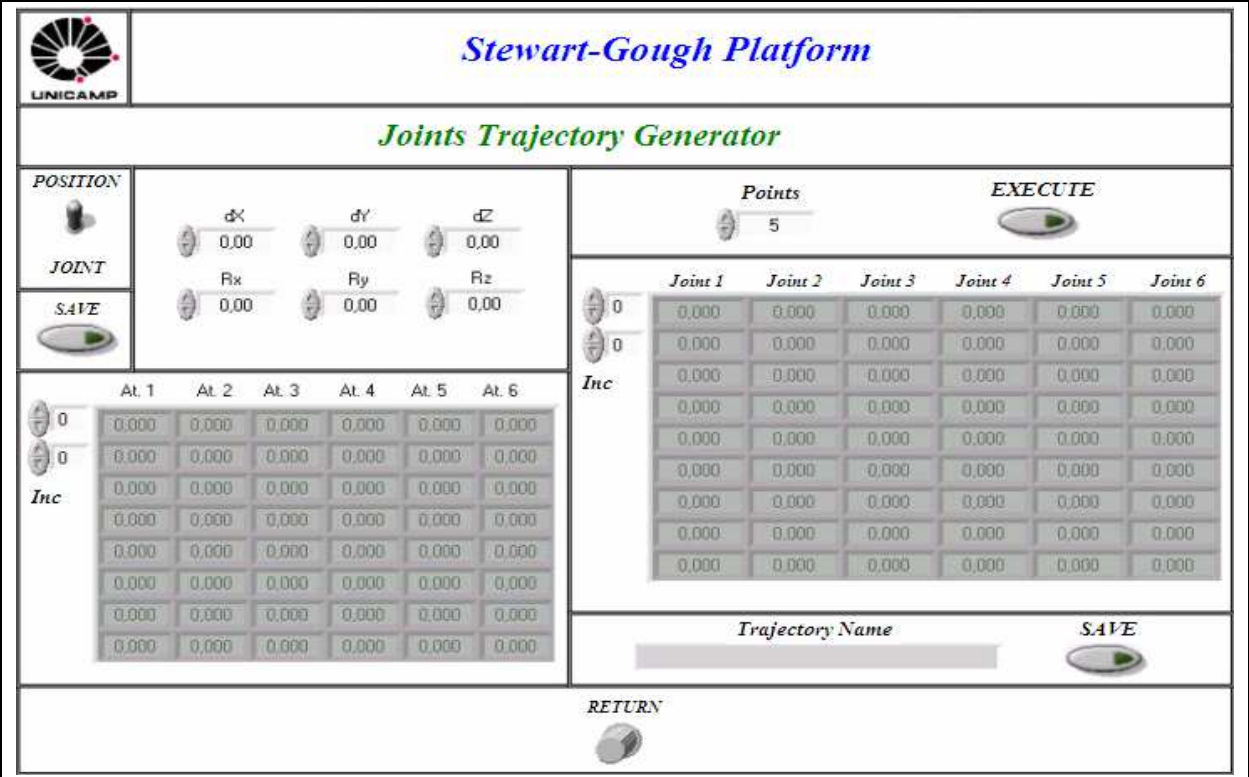
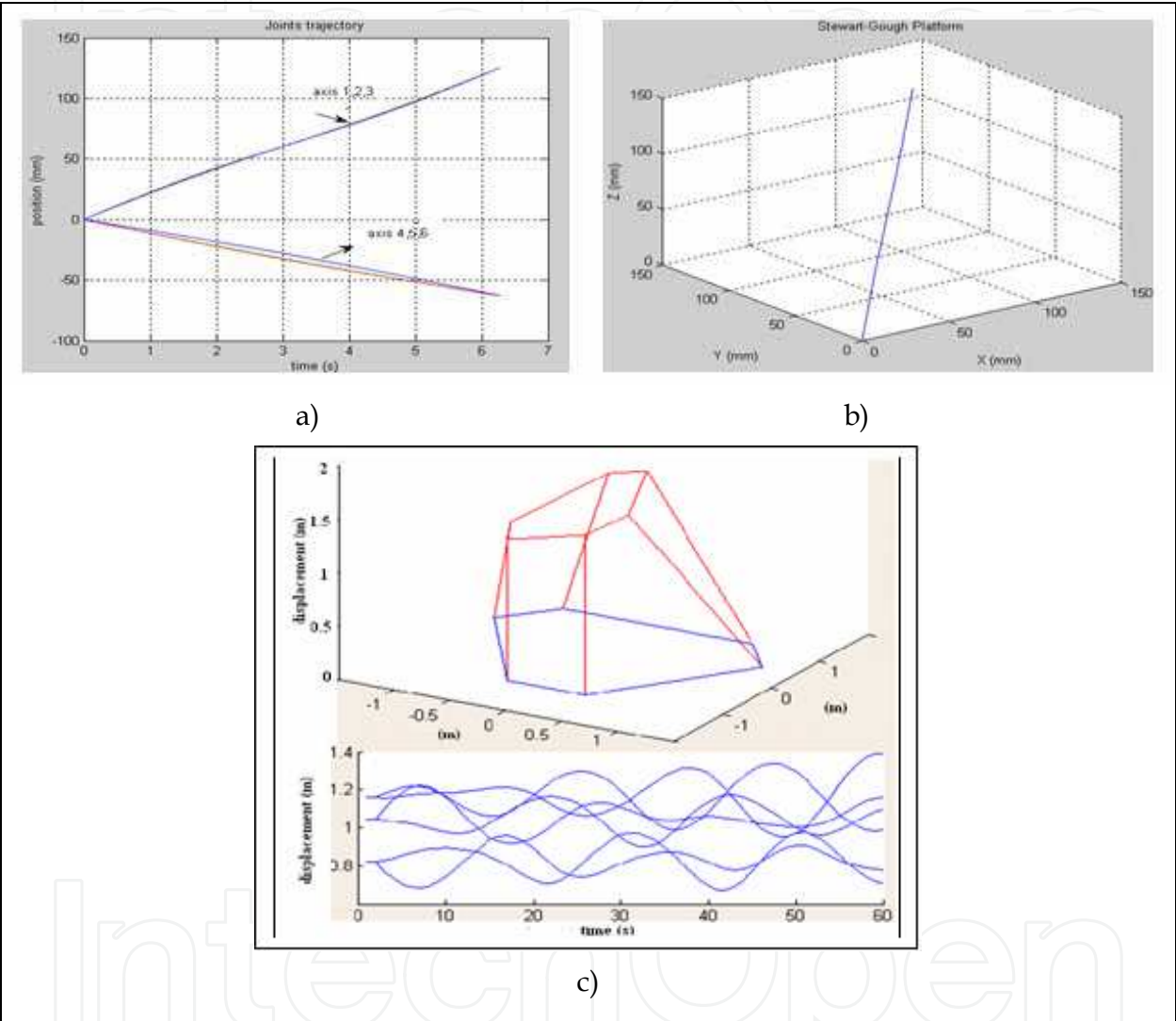


Fig. 25. Model implemented in LabVIEW™.

6.5 Experimental results

The development of a numerical algorithm [8], allows calculating the linear positions for a task defined with respect of the platform center in the Cartesian Space, contains the solution of the inverse kinematics through the use of recursive numerical methods based on the calculation of the kinematics model and of the inverse Jacobian matrix of the manipulator. This algorithm has been validated through different simulations, assessing the behavior of

the trajectory (joint coordinate). For this purpose the kinematics model of the platform was used with six linear joints. Fig. 26a shows the joints movements of each linear actuator and their displacement (45 degrees, approximately) of one point of the upper base of this platform obtained through the inverse kinematics model (Fig. 26b). Fig. 26c shows results of the proposed simulation, obtained with PID axis controllers implemented through FPGA, considering general sea movements and LABVIEW™ experimental platform.



a) Joints evolutions. b) Trajectory description. c) Joint motion

Fig. 26. Kinematics model - Simulation results.

7. Conclusions

This chapter presents the study of kinematics, dynamics and supervision and control of a Stewart-Gough platform, under a reconfigurable architecture concept, considering the division of the system in small functional blocks. This implementation consisted in merging knowledge acquired in multiple areas, and appears as a very promising design strategy for a better reconfiguration capability and portability.

This platform also becomes a powerful benchmark for many research activities, such as the validation of controllers and supervision strategies, model generation and data transmission protocols, among others. For example, the implementation of predictive controllers on this prototype may enable the test of this advanced control strategy under severe conditions of use.

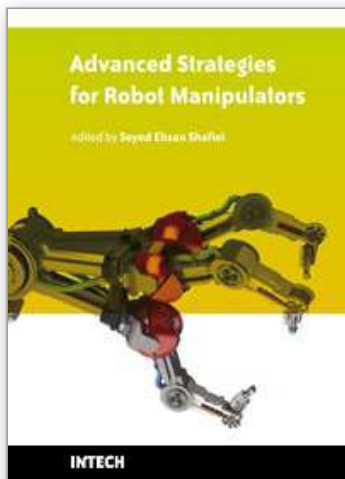
To simplify tests, implementation and future modifications, the use of rapid prototyping functions in the implementation of the interfaces and other logical blocks is emphasized in the proposed prototype. The control block, for example, can benefit of the characteristics of low consumption, high-speed operations, integration capacity, flexibility and simple programming. Some promising aspects of this architecture are:

- Flexibility, as there is a large variety of possible configurations in the implementation of solutions for several problems,
- It is a powerful tool for prototype design, allowing simple solution to control the several sensors and actuators usually present in this kind of projects,
- Possibility of modification of control strategies during operation of the platform,
- The open architecture of this platform enables the use for educational and researches activities.

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Advanced Strategies for Robot Manipulators

Edited by S. Ehsan Shafiei

ISBN 978-953-307-099-5

Hard cover, 428 pages

Publisher Sciyo

Published online 12, August, 2010

Published in print edition August, 2010

Amongst the robotic systems, robot manipulators have proven themselves to be of increasing importance and are widely adopted to substitute for human in repetitive and/or hazardous tasks. Modern manipulators are designed complicatedly and need to do more precise, crucial and critical tasks. So, the simple traditional control methods cannot be efficient, and advanced control strategies with considering special constraints are needed to establish. In spite of the fact that groundbreaking researches have been carried out in this realm until now, there are still many novel aspects which have to be explored.

How to reference

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Joao Mauricio Rosario, Didier Dumur, Alvaro Joffre Uribe Quevedo, Mariana Moretti and Fabian Lara (2010). Supervision and Control Strategies of a 6-DOF Parallel Manipulator Using a Mechatronic Approach, *Advanced Strategies for Robot Manipulators*, S. Ehsan Shafiei (Ed.), ISBN: 978-953-307-099-5, InTech, Available from: <http://www.intechopen.com/books/advanced-strategies-for-robot-manipulators/supervision-and-control-strategies-of-a-6-dof-parallel-manipulator-using-a-mechatronic-approach>

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