

We are IntechOpen, the world's leading publisher of Open Access books Built by scientists, for scientists

4,800

Open access books available

122,000

International authors and editors

135M

Downloads

Our authors are among the

154

Countries delivered to

TOP 1%

most cited scientists

12.2%

Contributors from top 500 universities



WEB OF SCIENCE™

Selection of our books indexed in the Book Citation Index
in Web of Science™ Core Collection (BKCI)

Interested in publishing with us?
Contact book.department@intechopen.com

Numbers displayed above are based on latest data collected.

For more information visit www.intechopen.com



Trajectory Generation for Mobile Manipulators

Foudil Abdessemed and Salima Djebrani
*Batna University, Department of Electronics,
Algeria*

1. Introduction

Mobile robot navigation has stood as an open and challenging problem over decades. Despite the number of significant results obtained in this field, people still look for better solutions. Some mobile robots are subject to constraints of rolling without slipping and thus belong to non-holonomic systems. Mobile robots also are subject to navigate in environments cluttered with obstacles. Now, in case the mobile robot presents a non-holonomic constraint, the problem consists of finding a path taking into account constraints imposed both by the obstacles and the non-holonomic constraints. Since non-holonomy make path planning more difficult, many techniques have been proposed to plan and generate paths. May be the most popular is the method of potential field (Khatib, 1986). However, this method may present some problems such as sticking to local minima. Moreover, the kinematic constraint is the other problem that can face trajectory planning. This can make time derivatives of some configuration variables non-integrable and hence, a collision free path in the configuration space not achievable by steering control.. Some researchers worked to find feasible path using different methodologies (Sundar & Shiller, 1997), (Laumond et al, 1994), (Reeds & Shepp, 1990). To deal with obstacles, some researchers decomposed the dynamic motion to static paths and velocity-planning problem (Murray et al, 1994), (Tilbury et al, 1995). In the work of (Qu et al, 2004), the authors treated the problem as a family of curves where the optimal path is found by adjusting a certain polynomial parameter. This idea was raised in many references including (Kant & Zucker, 1988) and (Murray & Sastry, 1993), where trajectories are represented by sinusoidal, polynomial or piecewise constant functions. In our recent work, and based on intelligent control, we proposed a fuzzy control methodology to navigate a mobile robot in a cluttered environment with the aim to reach the goal while avoiding static and/or dynamic obstacles (Abdessemed et al, 2004). Concerning robot arm path planning and trajectory generation, considerable efforts have been devoted to make these mechanical systems succeeding in their tasks. If we consider a robot arm with n -joints that move independently, the robot's configuration can be described by a 3-dimensional coordinate: (x_e, y_e, z_e) for the location of the end effector. These coordinates characterize the workspace representation, since they represent exactly the same coordinates of the object it intends to manipulate or to avoid. Although the workspace is well suited for collision avoidance, it happens that we are still

facing some other problems. In fact the task is usually expressed in the workspace coordinates and the question is how to map this space into configuration space. This problem finds its solution in the inverse kinematics. However, calculating the inverse kinematics is hard, and the problem becomes much harder if the robot has many DOFs. Moreover, for a particular workspace coordinates, many distinct configurations are possible. The other problem that may arise when using configuration space is the presence of obstacles. Within the scope of all these problems, many methods to path planning emerged. Among the techniques found in the literature, we state the cell decomposition methods (Russel & Norvig, 1995), Skeletonization methods (e.g. Voronoi graph (Okabe et al, 2000)), potential field. Due to some problems of the applied techniques already mentioned, such as local minima and uncertainties, probabilistic and robust methods have been explored. Demonstration of robustness of fuzzy logic and genetic algorithm encouraged many researchers to use these concepts for path planning and obstacle avoidance. We note that robust methods assume a bounded amount of uncertainties and do not assign any probabilities to values. The robots could replace good number of specific machine tools and could continue to supplant the man in a lot of complex tasks. In spite of all, the robot manipulators on fixed base have a lot of limitations. This is why like a man who has the faculty to move to achieve some tasks at different places or to do continuous tasks requiring a work of the arm during the displacement, the mobile manipulators have been considered. Mobile manipulators received particular attentions these last decades (Zhao et al, 1994); (Pin & Culioli, 1992); (Pin et al, 1996); (Lee & Cho, 1997); (Seraji, 1995). This is mainly due to their analytic problems and their various applications. A mobile manipulator consists of an arm fixed on a mobile platform. Such a configuration leads us toward a kinematically redundant system. Although we can construct non redundant mobile manipulators but, there are some good reasons to make us thinking of these systems as for example: increasing the working space of the arm, avoiding static or dynamic obstacles or, to avoid the robot singularities. From these observations, which allow to increase the working space by the mobility of the platform that a number of applications have been appeared. When these systems are devoted to indoor tasks, they are often equipped with wheels. The arrangement of the wheels and their actuation device determine the holonomic or non-holonomic nature of its locomotion system (Campion et al, 1996). Whereas some wheeled mobile manipulators built from an omni-directional platform are holonomic. Extensive research efforts have led people to plan the collision free paths for mobile manipulators. Many techniques have been proposed for path planning and trajectory generation. A desired task is usually specified in the work space. The first type has been a subject of our previous work [Abdessemed *et al*] where as the second type considers the plat form to be holonomic [Djebrani *et al*]. However, trajectory following control is easily performed in the joint space. Therefore, it is essential to obtain the desired joint space trajectory given the desired Cartesian space trajectory. This is accomplished using the inverse kinematics transformation. Controlling such systems is hard and the problem is more difficult to solve in case where the mobile platform contains some non-holonomic kinematical constraints. However, one should know that such a constraint does not decrease the configuration space reachable by the mobile platform but decreases the velocity space. Therefore, the mobile platform moves only along trajectories having a certain shape. On the other hand, if we choose a holonomic platform, the control would be much easier. In fact, A holonomic platform robot is an omni-directional robot whose mechanical structure enables it to change its displacement at any direction, without waiting

for the reconfiguration of its rolling parts. One of the consequences of the omnidirectionality is that the orientation of a robot becomes independent of the trajectory performed, provided that each "wheel" of the robot has the 3 degrees of mobility (2 translations and 1 rotation). In this book chapter, we try to see the two case studies, namely a holonomic and a non-holonomic mobile manipulator. The approach presented describes the development of the complete kinematic representation of a mobile manipulator. In this case, we present the analysis of the whole mechanical system constituted of a mobile platform over which a robot manipulator is mounted, forming thus the mobile manipulator (Fig. 1); the arm and the mobile platform are considered as a unique system. In this part of analysis, the mobile manipulator is considered as a unique entity. In order to have an overall study, we consider the two types of mobile platforms. The mobility introduced by the mobile platform is exploited to solve problems like collision avoidance and joints saturations. The results obtained demonstrate the effectiveness of the approaches for simple situations as well as for complex situations when obstacles are encountered.

2. Mobile manipulator with non-holonomic platform

2.1 Analysis

In this case a mobile manipulator with non-holonomic platform is viewed. Figure. 2 shows the four main reference axes: The stationary reference axis, the reference axis attached to the mobile platform, the reference axis attached to the base of the robot manipulator, and finally the reference axis attached to the end point of the effector. The homogeneous matrix found by a successive multiplication of the three homogeneous sub matrices can obtain the position and the orientation of the terminal point of the end effector with respect to the stationary reference axis:

$$T_e^o = T_p^o \cdot T_m^p \cdot T_e^m \quad | \quad (1)$$

Such that the matrix T_p^o is determined by a certain matrix $A(q)$, T_m^p is a fixed matrix and T_e^m is determined by the joint variable vector $\theta = [\theta_1, \theta_2, \dots, \theta_{n_m}]^T$, n_m represents the degree of freedom of the arm manipulator.

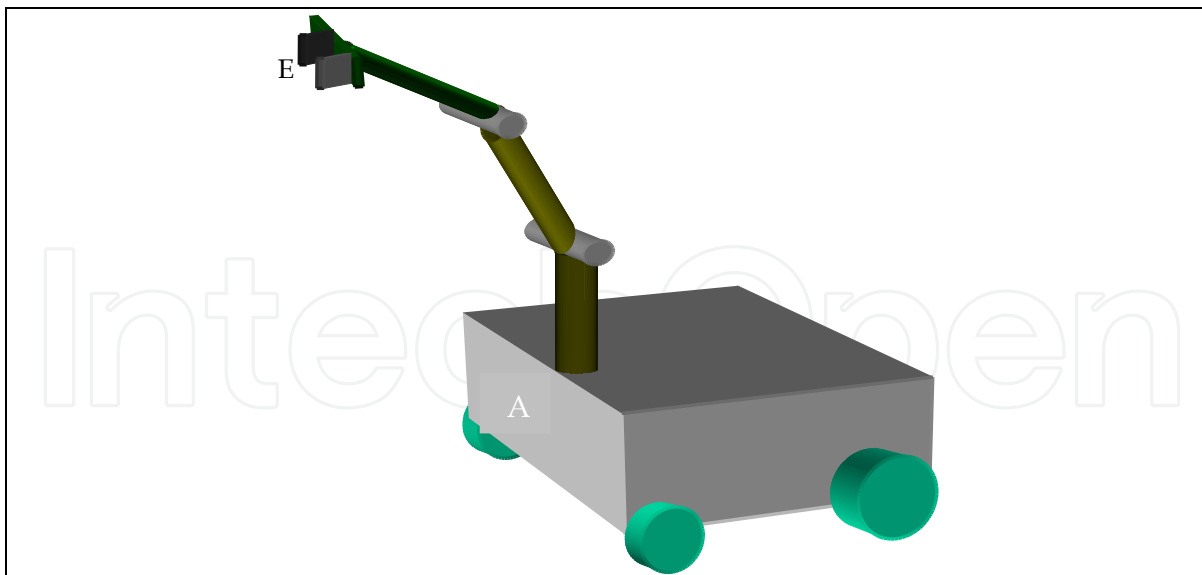


Fig. 1. Mobile Manipulator appearance

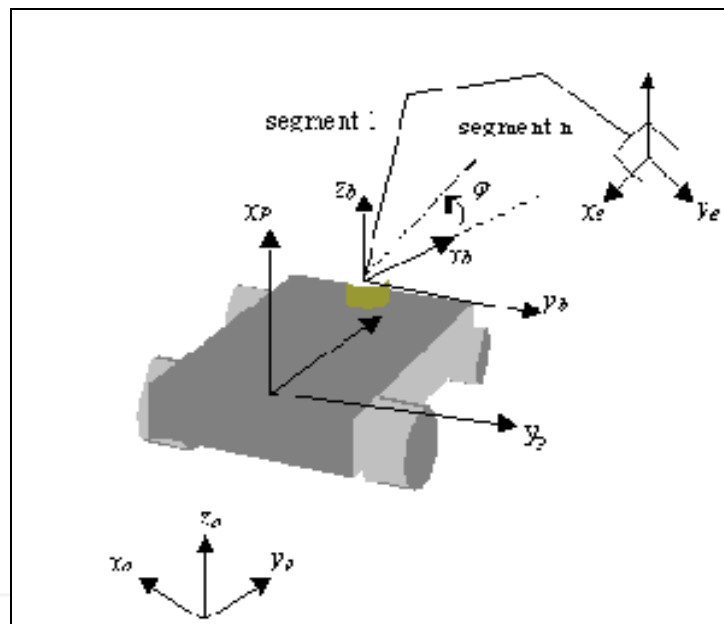


Fig. 2. Mobile Manipulator features

The equations of the geometric model are found to be:

$$\begin{aligned}
 x_e &= x_A + \cos(\theta_1 + \varphi)(l_2 \cos\theta_2 + l_3 \cos(\theta_2 + \theta_3)) \\
 y_e &= y_A + \sin(\theta_1 + \varphi)(l_2 \cos\theta_2 + l_3 \cos(\theta_2 + \theta_3)) \\
 z_e &= l_1 - l_2 \sin\theta_2 - l_3 \sin(\theta_2 + \theta_3)
 \end{aligned} \tag{2}$$

(x_A, y_A, φ) represent the mobile platform coordinates and its orientation in the world frame. $(\theta_1, \theta_2, \theta_3)$ are the three angles of the arm, and l_1, l_2 and l_3 its lengths. (x_e, y_e, z_e) are the coordinates of the end effector in the world frame. As we can see, the position vector

$X_e = (x_e, y_e, z_e)$ of the end effector E with respect to the world coordinate W is a non-linear function of the configuration vector: $q = (p^T, \theta^T)^T \in \mathfrak{R}^n$, ($n=3+n_m$). Now, if the vector X_e^d is the vector of the wanted task then

$$X_e = X_e^d = f(q) \quad (3)$$

If we derive this equation, we get the kinematic equation of the model

$$\dot{X}_e = J_m(q) \cdot \dot{q} \quad (4)$$

where $J_m(q)$ is the $m \times n$ Jacobienne matrix of the mobile manipulator. This equation represents a holonomic kinematic constraint since it can be written as

$$H(q) = 0 \quad (5)$$

If the mobile platform is non holonomic and without slip, then the following kinematic constraint is true:

$$A(p) \cdot \dot{p} = 0 \quad (6)$$

such that :

$$\dot{p} = \begin{bmatrix} \dot{x}_A \\ \dot{y}_A \\ \dot{\phi} \end{bmatrix}^T = \begin{bmatrix} \dot{X}_A \\ \dot{\phi} \end{bmatrix}^T \quad (7)$$

Equivalently, we can write the non-holonomic constraint (5) as:

$$J_v(q) \dot{q} = 0 \quad (8)$$

where: $J_v(q) = [A(p) \quad 0]$

\dot{q} cannot be eliminated by integration to give $\frac{d(J_v(q))}{dq} = 0$, this means that the system is non holonomic. Equations (4) and (8) are combined to give the differential kinematic model of the system including the mobile platform and the robot manipulator [1].

$$\begin{bmatrix} J_v(q) \\ \dots \\ J_m(q) \end{bmatrix} \dot{q} = \begin{bmatrix} 0 \\ \dots \\ \dot{X}_e \end{bmatrix} \quad (9)$$

Such that, $q = (p^T, \theta^T) = (x_A, y_A, \phi, \theta_1, \theta_2, \theta_3)^T$. In a compact form, equation (9) can be written as:

$$J(q) \dot{q} = \dot{X} \quad (10)$$

where:

$$J(q) = \begin{bmatrix} J_v(q) \\ \dots \\ J_m(q) \end{bmatrix}, \quad \dot{X} = \begin{bmatrix} 0 & \dots & \dot{X}_e \end{bmatrix}^T$$

If we assume that the speed of the end-effector is \dot{X}_d , we need then to solve the following differential equation:

$$J(q)\dot{q} = \dot{X}_d \quad (11)$$

The term redundancy designates the determination of admissible control signal for this redundant system. However, the system being undetermined, it is necessary to use some criteria that allow determining one of the infinite solutions of the problem. according to (Liégeois, 1997), the general formulation of the inverse kinematics is expressed by the following equation

$$\dot{q} = J^\# \dot{X}_d + (I - J^\# J)z \quad (12)$$

Where, $J^\#$ is the generalized inverse of the Jacobian matrix. The first term of the equation (12) represents the particular solution used to achieve the desired velocity of the end effector, and the term $(I - J^\# J)$ is an operator of projection that projects an arbitrary vector into the null space of J . Therefore, the term $(I - J^\# J)z$ is the general solution of the homogeneous equation:

$$J\dot{q} = 0 \quad (13)$$

The homogeneous solution contributes only in a motion within the joint space of the mechanical system named the self-motion. In order to find the optimal solutions, let us mention the techniques most commonly used for serial-chain redundant arms:

- Minimization of joint velocities

$$C_v = \dot{q}^T \dot{q} \quad (14)$$

- Minimization of joint acceleration

$$C_a = \ddot{q}^T \ddot{q} \quad (15)$$

- Minimization of kinetic energy

$$C_e = \dot{q}^T H \dot{q} \quad (16)$$

- Minimization of joint torques

$$C_t = \tau^T \tau \quad (17)$$

Some of these techniques can present some problems as: nonzero joint velocities corresponding to zero end-effector velocities, and instability of the motion. Otherwise, if the mobile manipulator is brought to evolve in an environment cluttered of obstacles, then the goal consists to find the solutions to the problem that must take them into consideration, consequently, one can write the relation as a certain function f such that, $\dot{q} = f(q, \dot{x}, \text{obstacles})$

2.2 Geometric solution with no obstacles

For this redundant system the matrix J is of dimension $m \times n$, with $m < n$. We seek a solution to equation (12), which guarantees a minimum value for the norm, in addition to a number of solutions in the null space of J . The solutions in the null space can be used to optimize some tasks as for example: to avoid some obstacles or to warn saturations of the joints. However, it is not recommended in practice to use directly the solution with minimal norm. Indeed, to avoid big velocities values, one can impose a weighting matrix

$W_v = \text{diag}\{w_a, w_b\}$ for the linear and angular velocities, in order to minimize the sum of their norms: $\|\dot{p}\|_{w_a} + \|\dot{\theta}\|_{w_b}$.

such that:

$$W = \begin{bmatrix} w_1 & 0 & \dots & 0 \\ 0 & w_2 & & 0 \\ \vdots & \vdots & \ddots & 0 \\ 0 & 0 & \dots & w_n \end{bmatrix}, \quad \text{where:} \quad w_i = \frac{b_i}{b_{\max}}, \quad \text{such that:}$$

$$b_i = (q_i)_{\max} - (q_i)_{\min} \quad \text{and} \quad b_{\max} = \max\{b_1, b_2, \dots, b_n\}$$

Thus, the optimal solution is the one that optimises the norm defined by the following expression:

$$\dot{q}^T W \dot{q} \quad (18)$$

While noticing that the matrix W is diagonal, it could be split into two diagonal matrices such that:

$$W = W_o^T W_o \quad (19)$$

In this case the norm could be written as :

$$\dot{q}^T W \dot{q} = \dot{q}^T W_o^T W_o \dot{q} = \|W_o \dot{q}\|^2 \quad (20)$$

and relation (11) becomes:

$$\dot{x}_d = JW_0^{-1}W_0\dot{q} \quad (21)$$

To find \dot{q} , one should solve equation (21), which minimizes the norm (18). The problem becomes an optimization problem, where we consider JW_0^{-1} as a system matrix and the product $W_0\dot{q}$ as the vector whose norm is to be minimized; the solution is thus:

$$\dot{q} = W^{-1}J^T(JW^{-1}J^T)^{-1}\dot{x}_d + Hz \quad (22)$$

knowing that:

$$H = W_0^{-1} - W^{-1}J^T(JW^{-1}J^T)^{-1}JW_0 \quad (23)$$

The first term of the equation (22), represent the optimal solution and the second term the homogeneous solution. The vector z is an arbitrary vector that is projected by the matrix H in the null space of J . It can be used to prevent saturation of the manipulator joints or to avoid unforeseen obstacles. To correct any drift of the trajectory of the space of the task, we introduce the error that measures the difference between the wanted vector and the one measured to yield:

$$\dot{q} = W^{-1}J^T(JW^{-1}J^T)^{-1}\left[\dot{x}_d + K(x_d - x)\right] + Hz \quad (24)$$

However, if we try to solve the equation (24), one can fall on a problem of numeric instability. To overcome this problem, we propose to use the singular value decomposition as a solution. This algorithm is a stable numerical procedure based on the decomposition theorem.

Theorem

Given a matrix A of size $m \times n$, it can be written as a product of three matrices as:

$$A_{m \times n} = U_{m \times m} \cdot \Sigma_{m \times n} \cdot V_{n \times m}^T$$

The matrices U et V are orthogonal matrices and Σ is a diagonal matrix for which the elements on the diagonal are the singular values of the A matrix.

If one applies this theorem to the matrix:

$$A = JW_0^{-1} \quad (25)$$

Then

$$JW_0^{-1} = U\Sigma\Sigma^T \quad (26)$$

In this case, the complete solution becomes:

$$\dot{q} = W_0^{-1} V \Sigma^+ U^T [\dot{X}_d + K(X_d - X)] + W_0^{-1} [I - V \Sigma^+ \Sigma V^T] z \quad (27)$$

Where $\Sigma^+ = \Sigma^T (\Sigma \Sigma^T)^{-1}$. The complete solution makes intervene also the matrix H representing the projection of an arbitrary vector z in the null space of the Jacobian matrix J .

2.3 Geometric solution with obstacle avoidance

Now, if we consider a smooth function $g(q)$, representing a certain criterion to be minimized, then the vector z of the general solution given by equation (22) can be defined as follows:

$$z = -\nabla g(q) \quad (28)$$

where $\nabla g(q) = \left(\frac{\partial g}{\partial q} \right)^T$ is the gradient of g , and the homogeneous solution is obtained by

projecting z in the null space of J . However, we can use any function as far as it can be reduced to an expression that involves only terms of generalized joint variables. The method of the gradient is of a very vast use because it allows an easy incorporation of the different performance criteria in the control algorithm. This technique is used in our case to satisfy two objectives; first avoiding obstacles and second avoiding joint limits. Thus, the vector z is composed of two terms:

$$z = z_1 + z_2 \quad (29)$$

where $z_1 = -\beta \frac{\partial V_1}{\partial q}$ and $z_2 = -\beta_2 \frac{\partial V_2}{\partial q}$. V_1 is the potential associated with the joint limits such that: and V_2 is the potential associated with the obstacle presence.

$$V_1(q) = \frac{1}{2} \left(q - \frac{\bar{q} + \underline{q}}{2} \right)^T \left(q - \frac{\bar{q} + \underline{q}}{2} \right) \quad (30)$$

\bar{q}_i and \underline{q}_i represent respectively the upper and lower joint limits. Whereas V_2 is the potential associated with the obstacle presence such that:

$$V_2 = \sum_{i=1}^{\eta} V_{2i} \quad (31)$$

Such that

$$V_{2i} = \begin{cases} \frac{1}{2} k_1 \left(\frac{1}{d_i(x)} - \frac{1}{d_0} \right)^2 & d \leq d_0 \\ 0 & d > d_0 \end{cases} \quad (32)$$

k_1 denotes some adjusting coefficient, d and d_0 represent respectively the distance of a certain point on the robot to the obstacle and the minimal security distance.

2.4 Simulation results

A series of simulation were conducted in order to illustrate the performance of the method. Fig. 3, shows the terminal point of the end-effector following a reference trajectory in a free obstacle environment in the case where we consider the whole system as unique. In this case, one notes, according to Fig. 4, that the mobile platform follows a non-deformable trajectory in the x-y plane. The curves presented in Figs. 5, 6, 7 and 8 shows the evolution of the corresponding mobile manipulator joints. However, if an obstacle is put on the path of the mobile platform then, one can see that the mobile platform succeeds in getting around the obstacle while maintaining the terminal point on the reference trajectory; this is depicted in Fig. 9, and the new trajectory of the mobile platform in the x-y plane is clearly shown in Fig. 10. The curves presented in Figs. 11, 12, 13 and 14 show the evolution of the new corresponding mobile manipulator joints.

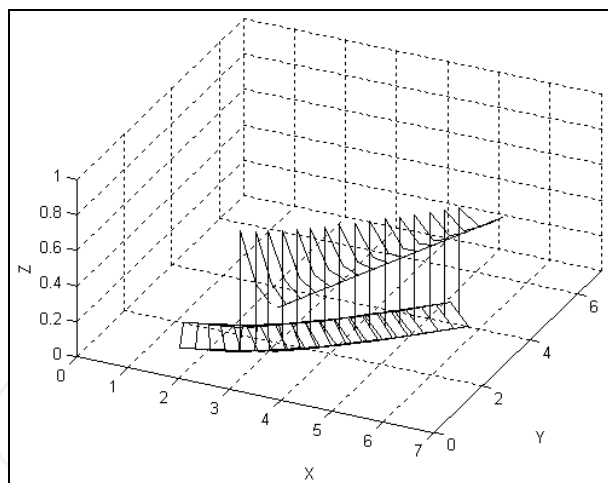


Fig.3. A 3D-view of the arm and the mobile platform evolutions in an obstacle free space.

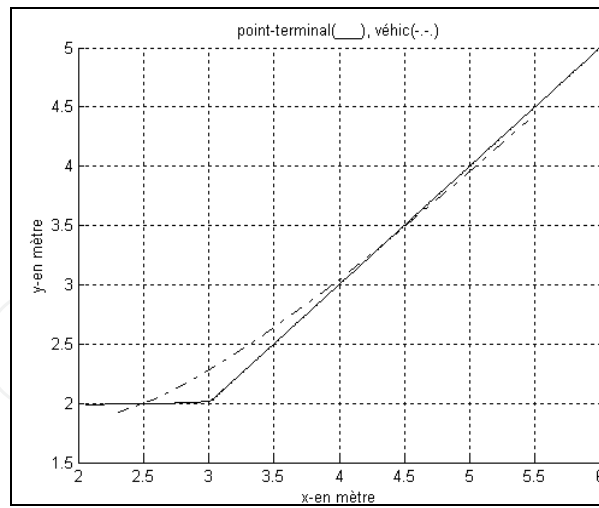


Fig. 4. End-effector and mobile platform trajectories in the x-y plane with no obstacles.

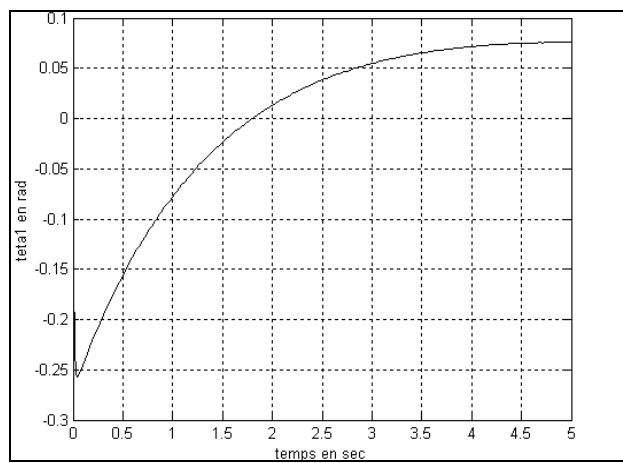


Fig. 5. Articulation θ_1 curve

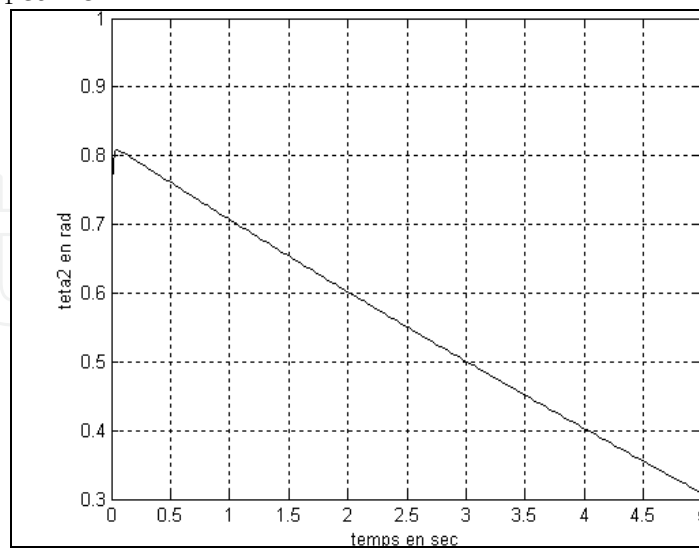


Fig.6. Articulation θ_2 curve

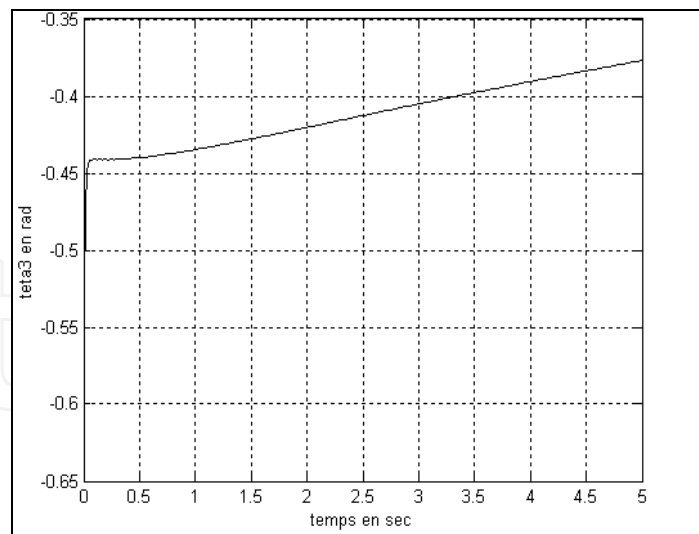
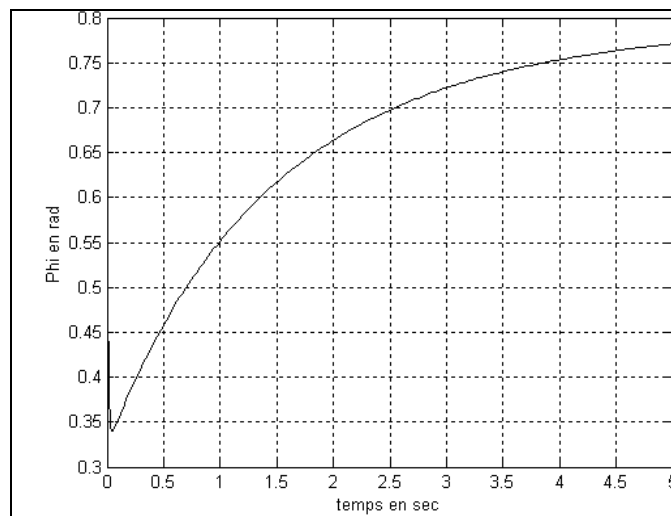
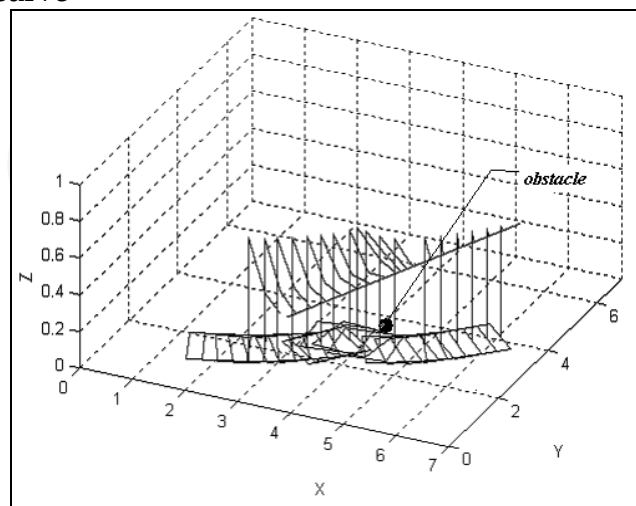
Fig. 7. Articulation θ_3 curveFig. 8. Articulation ϕ curve

Fig. 9. A 3D-View of the arm and the platform evolutions in presence of obstacles.

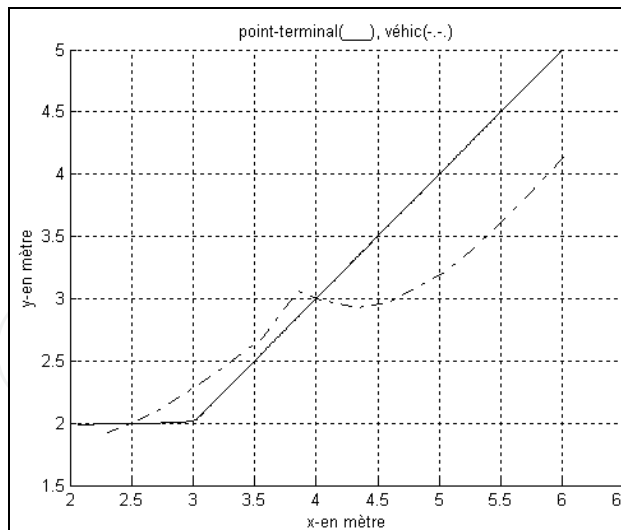


Fig. 10. End-effector and mobile platform trajectories in the x-y plane in presence of obstacles.

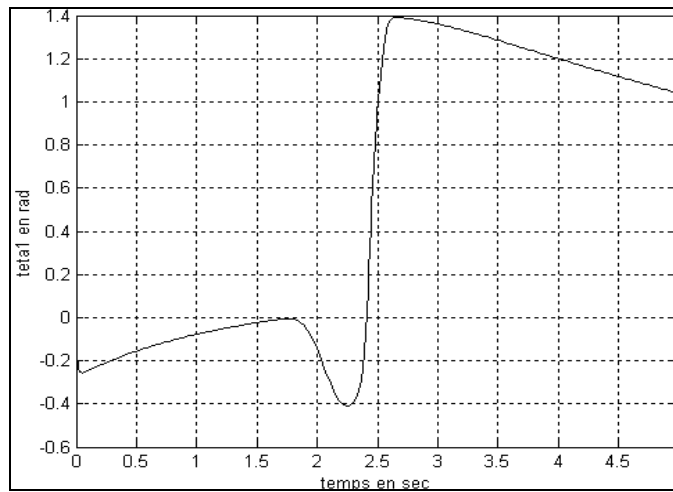


Fig. 11. Evolution curve of the joint θ_1

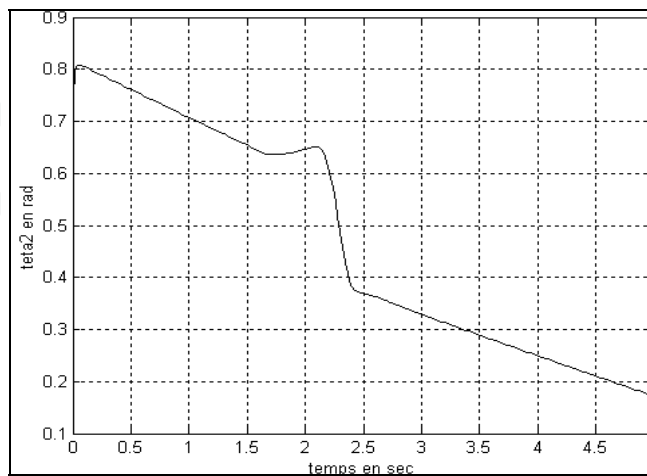


Fig. 12. Evolution curve of the joint θ_2

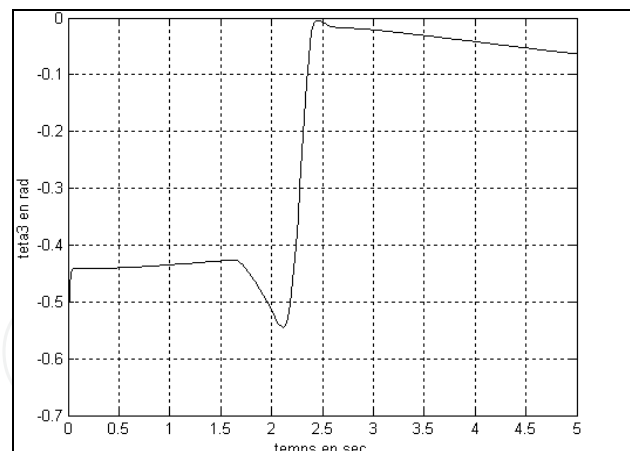


Fig. 13. Evolution curve of the joint θ_3

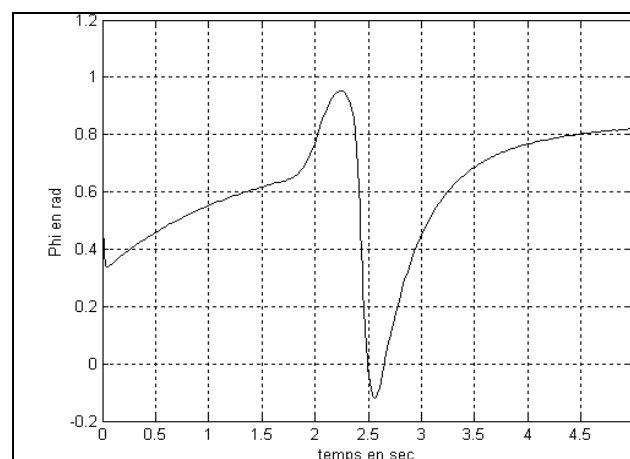


Fig. 14. Evolution curve of the joint φ

3. Mobile manipulator with holonomic platform

3.1. Analysis

The other type of mobile platforms that we intend to present in this section is the one with omnidirectional wheels. These particular types of wheels are used to develop a holonomic mobile robot. They enable the robot to move in any direction at any orientation. There is no need to change the orientation of the platform while moving in an arbitrary trajectory. The direction of the linear velocity is independent from the orientation of the mobile platform. We used the particular concept of a wheel formed with 2 truncated spheres intermechanically dependent developed in Mourioux and his colleagues, (Mourioux et al., 2006). Two parallel planes truncate each sphere. An axis enables each sphere to turn on it freely. This axis is maintained by a fork, which can rotate by using a DC motor. We consider here the mobile manipulator shown in Figure 15. The location of the platform is given by a vector $\xi_p = [x, y, \vartheta]^T$; which defines the position and the orientation of the platform in the fixed frame. The position of the point O_4 in the fixed frame is thus given by its Cartesian coordinates ξ_1 , ξ_2 , and ξ_3 .

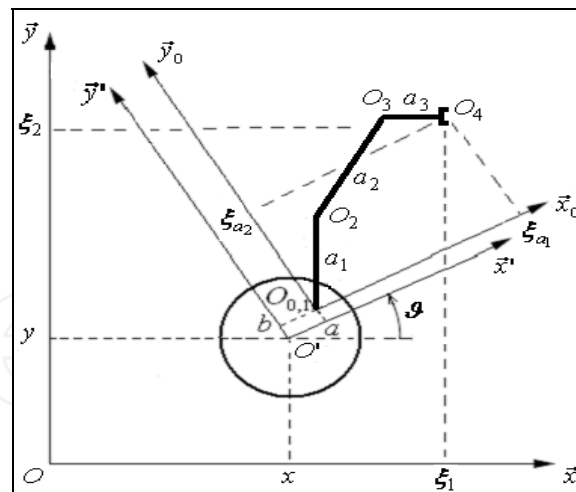


Fig. 15. Mobile manipulator with omni directional platform

3.2 Geometric solution with no obstacles

The control of the mobile manipulator is given by $u = [u_a^T, u_p^T]^T = [\dot{q}_{a1}, \dot{q}_{a2}, \dot{q}_{a3}, \dot{x}, \dot{y}, \dot{\theta}]^T$, with $u_a = \dot{q}_a = [\dot{q}_{a1}, \dot{q}_{a2}]^T$ being the control of the robotic arm and $u_p = [\dot{x}, \dot{y}, \dot{\theta}]^T$ the control of the platform. The degree of mobility of the mobile manipulator is $\delta_m = n_a + \delta_{mp} = 3 + 3 = 6$, with δ_{mp} the degree of mobility of the platform. According to Figure 16, the geometric model of this mobile manipulator is:

$$\begin{cases} \xi_1 = x + (a + C_1(a_3C_{23} + a_2C_2))C_g - (b + S_1(a_3C_{23} + a_2C_2))S_g \\ \xi_2 = y + (a + C_1(a_3C_{23} + a_2C_2))S_g + (b + S_1(a_3C_{23} + a_2C_2))C_g \\ \xi_3 = z + a_1 - a_2S_2 - a_3S_{23} \end{cases} \quad (33)$$

From (32), we get the instantaneous location kinematics model:

$$\dot{\xi} = J \cdot u \quad (34)$$

Where;

$$\dot{\xi} = \begin{bmatrix} \dot{\xi}_1 \\ \dot{\xi}_2 \\ \dot{\xi}_3 \end{bmatrix}, \text{ and } J = \begin{bmatrix} D_3 & D_2 & D_1 & 1 & 0 & D_9 \\ D_6 & D_5 & D_4 & 0 & 1 & D_{10} \\ 0 & D_8 & D_7 & 0 & 0 & 0 \end{bmatrix}$$

With the following intermediate variables:

$$\begin{aligned} C_{g1} &= \cos(\vartheta + q_{a1}), S_{g1} = \sin(\vartheta + q_{a1}), C_{12g} = \cos(q_{a1} + q_{a2} + \vartheta), S_{12g} = \sin(q_{a1} + q_{a2} + \vartheta), \\ D_1 &= -a_3C_{1g}S_{23}, D_2 = -a_2C_{1g}S_2 + D_1, D_3 = -a_2S_{1g}C_2 - a_3S_{1g}C_{23}, \\ D_4 &= -a_3S_{1g}S_{23}, D_5 = -a_2S_{1g}S_2 + D_4, D_6 = a_2C_{1g}C_2 + a_3C_{1g}C_{23}, \end{aligned}$$

$$D_7 = -a_3 C_{23}, \quad D_8 = -a_2 C_2 + D_7,$$

$$D_9 = -aS_g - bC_g + D_3, \quad D_{10} = aC_g - bS_g + D_6$$

The kinematic control problem is aimed to find the control vector $(u(t) | t \in [t_0, t_f])$ to achieve the desired operational motion $(\xi^*(t) | t \in [t_0, t_f])$ of the end effector in such a way that the error $e(t) = \xi^*(t) - \xi(t)$ approaches zero. Since the system is redundant ($m < \delta_m$), we set m_{add} additional tasks (Seraji, 1998) so that

$$\dot{\xi}_{\text{add}} = J_{\text{add}} \cdot u \quad (35)$$

J_{add} is a matrix of dimension $m_{\text{add}} \times \delta_m$. Also we want to regulate $\xi_{\text{add}}(t)$ to the velocities of the desired additional tasks $\xi_{\text{add}}^*(t)$. Equation (34) and (35) are combined to give the differential kinematics model

$$\dot{\xi}_t = J_t \cdot u \quad (36)$$

Such that: $J_t = \begin{bmatrix} J \\ J_{\text{add}} \end{bmatrix}$ and $\xi_t = \begin{bmatrix} \xi \\ \xi_{\text{add}} \end{bmatrix}$

The problem is now to regulate the actual value of ξ_t to $\xi_t^* = [\xi^*, \xi_{\text{add}}^*]^T$. Let $e_t = [e^T, e_{\text{add}}^T]^T = \xi_t^* - \xi_t$ with $e_{\text{add}} = \xi_{\text{add}}^* - \xi_{\text{add}}$. The matrix J_t is of dimension $(m + m_{\text{add}}) \times \delta_m$. Depending on the desired additional tasks this matrix is not necessarily square. If we suppose that J_t is of full rank and if $r = \text{rank}(J_t)$, then $r = \min(m + m_{\text{add}}) \times \delta_m$.

The control vector u is computed by solving the linear system $\dot{\xi}_t = J_t u$ (Bayle et al., 2002).

Now, if we consider only the position of the end effector, then $\xi = [\xi_1, \xi_2, \xi_3]^T$, i.e., $m=3$; and if $\xi_{\text{add}} = \xi_p = [x, y, \theta]^T$, i.e., $m_{\text{add}}=3$. In this case, we can determine the vector u such that

$$u = J_t^{-1} (\xi_d^* + W_t (\xi_d^* - \xi_t)) \quad (37)$$

Where W_t is an $(m + m_{\text{add}})$ -order definite positive matrix and $\xi_d^*(t) = \xi_t^*(t)$ denotes the desired motion.

3.3. Geometric solution with obstacles

Up to now we have supposed the path of the robot clear from any obstacles.. However, in case of presence of obstacles some modifications have to be done. In this case, we use an approach based on virtual impedance model (Arai & Ota, 1996). This model can be seen as an extension of the potential field concept (Khatib, 1986). This model determines the motion of a robot by means of a desired trajectory ξ_t^* modified by a sum of different forces. These forces consist of three parts: an attractive force named F_{target} , generated to attract the robot toward the objective, a repulsive force generated between the robot and the obstacles F_{obs} , and a third force generated between the platform and the carried arm manipulator F_{man} , (see Fig 16). In this work, only the first two forces are considered. The closed loop dynamical equation is expressed as equation (37).

$$M_d(\ddot{\xi}_t^* - \ddot{\xi}_t) + B_d(\dot{\xi}_t^* - \dot{\xi}_t) + K_d(\xi_t^* - \xi_t) = F_{ext} \quad (38)$$

Where F_{ext} represents all the forces exerted on the mobile robot, such that:

$$F_{ext} = F_{target} + \sum_i F_{obs} + F_{man} \quad (39)$$

From equation (37), we can derive the desired impedance Z_d such that:

$$Z_d = M_d s^2 + B_d s + K_d \quad (40)$$

Where M_d, B_d, K_d are diagonal positive definite desired mass, damping and spring effects. Equation (38) can be expressed in terms of the desired impedance and the trajectory tracking. Let e_d be a new signal error such that

$$e_d = (\xi_t^* - \xi_t) - \frac{F_{ext}}{Z_d} \quad (41)$$

If e_d approaches zero, then equation (38) is realized. The realized trajectory in equation (41)

can be seen as the sum of the desired trajectory ξ_t^* and the force correction $\frac{F_{ext}}{Z_d}$ to give

what we call the desired modification motion:

$$\xi_d^*(t) = \xi_t^*(t) + \frac{F_{ext}}{Z_d} \quad (42)$$

Note that $F_{ext} = 0$ in free motion.

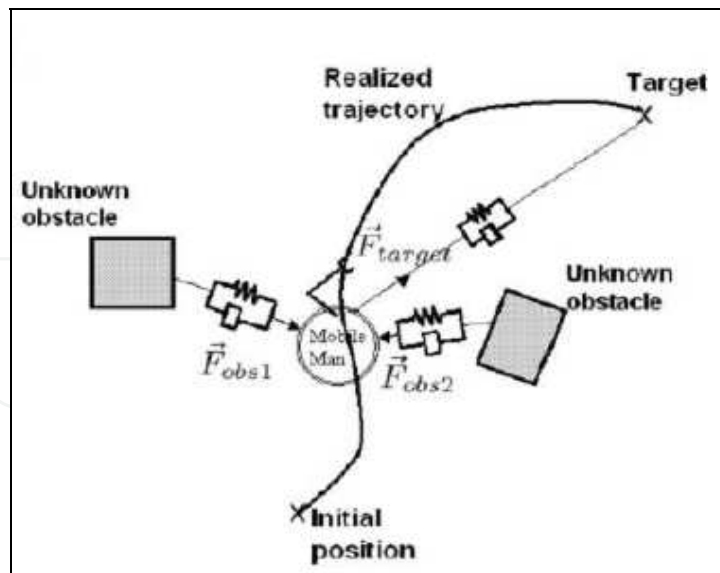


Fig. 16. Virtual impedance model for the mobile platform

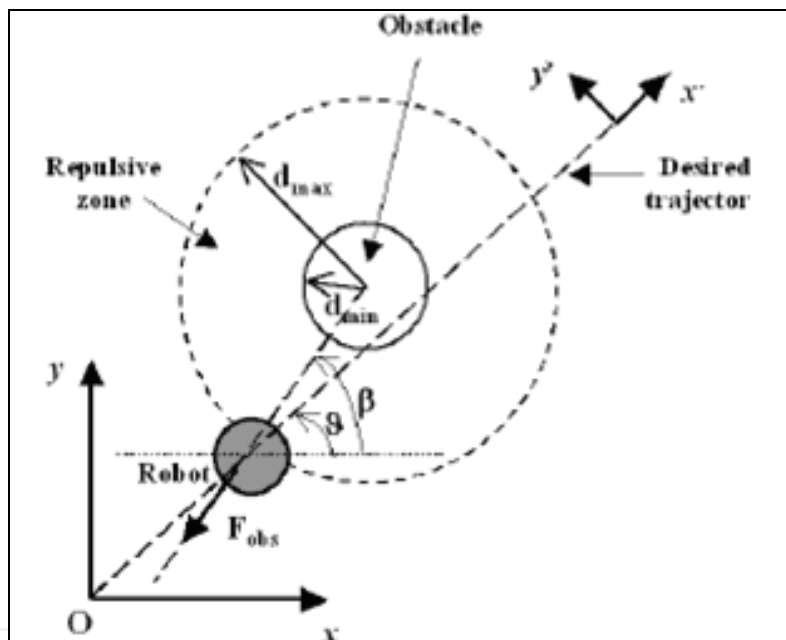


Fig. 17. Obstacle repulsion force

The magnitude F_{obs} is chosen to be (Borenstein & Koren, 1991):

$$F_{obs} = a_{obs} - b_{obs} \left(d(t) - d_{min} \right)^2$$
 where a_{obs} and b_{obs} are positive constants satisfying the

condition $a_{obs} = b_{obs} (d_{max} - d_{min})^2$, d_{max} is the maximum distance between the robot and the detected obstacle that causes a nonzero repulsive force, d_{min} represents the minimum distance accepted between the robot and the obstacle and $d(t)$ is the distance measured between the robot and the obstacle $d_{min} < d(t) < d_{max}$ (Fig. 17). Note that the bound d_{max} characterizes the repulsion zone. Which is inside the region where the repulsion force has a non-zero value. Desired interaction impedance is defined as the linear dynamic

relationship $Z_d = B_d s + K_d$ where B_d and K_d are positive constants simulating the damping and the spring effects, respectively, involved in the robot obstacle interaction inside the repulsion zone.

3.4 Simulation results

Simulations are conducted in order to show the performance of the proposed methodology. The numerical example supposes the lengths of the arm are such that $a_1 = 0.6$, $a_2 = 0.4$, $a_3 = 0.3$ and the initial configuration of the mobile manipulator is such that: $\xi_p = (0.1, 0.1, \pi/6)$ and $q_a = [\pi/4, -\pi/2, \pi/4]^T$. The end effector is supposed to track

the following straight-line trajectory $\xi^*(t) = [\xi_1^*(t), \xi_2^*(t), \xi_3^*(t)]^T = [0.1t, 0.1t, 1 + 0.1t]^T$;

Furthermore, we imposed the following additional tasks to the mobile platform $\dot{\xi}_p^*(t) = (x^*(t), y^*(t), \vartheta^*(t)) = (t, t, \pi/4)$. Fig. 18 shows the stance of the whole system when the end effector tracks the reference trajectory. The resulting trajectory of the end effector as well as that of the mobile platform is depicted in Fig. 19. Figures 20, 21, 22 and 23 describe the evolution of the angles of the arm and the orientation of the platform respectively. If the robot finds an obstacle at less than $d_{\max} = 1\text{m}$ the impedance control is activated, and the collision is avoided as it can be seen in Fig. 24.

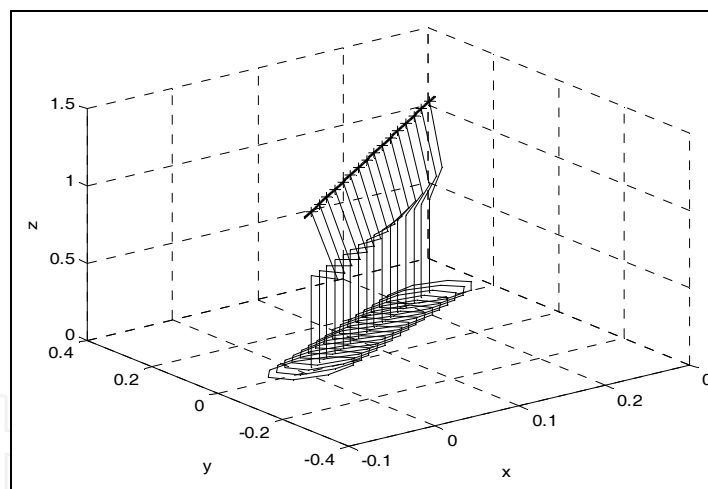


Fig. 18. A 3D-view of the arm and the mobile platform evolutions in an obstacle free space.

The resulted trajectories of the arm as well as of the mobile platform appear in Fig. 26. The corresponding curves showing the evolution of the angles of the arm and the orientation of the platform are depicted in Figs. 27, 28, 29 and 30 respectively.

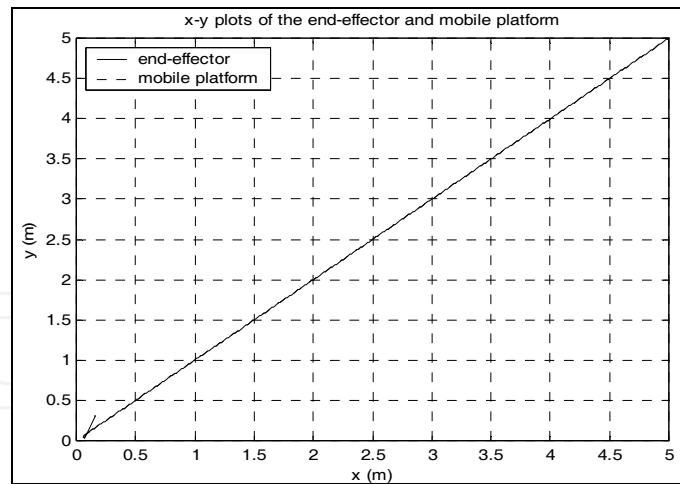


Fig. 19. End-effector and mobile platform trajectories in the x-y plane with no obstacles.

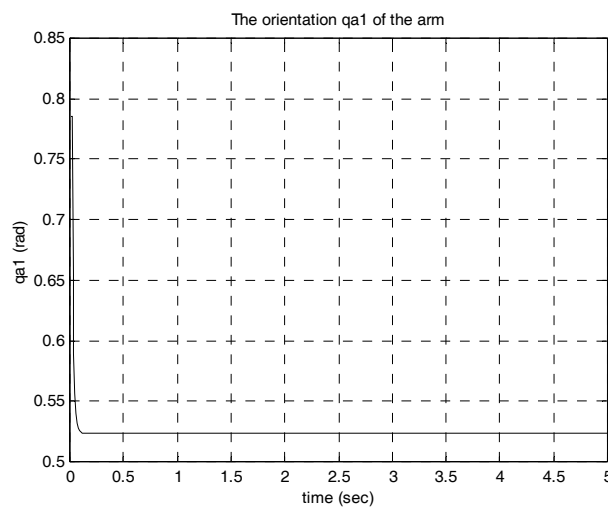


Fig. 20. Articulation q_{a1} curve

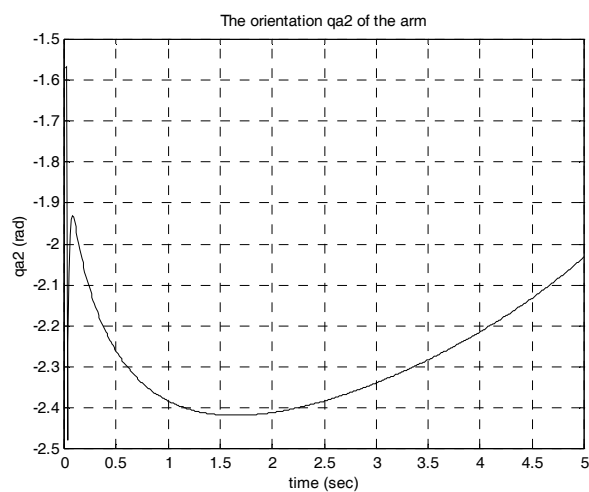


Fig.21. Articulation q_{a2} curve

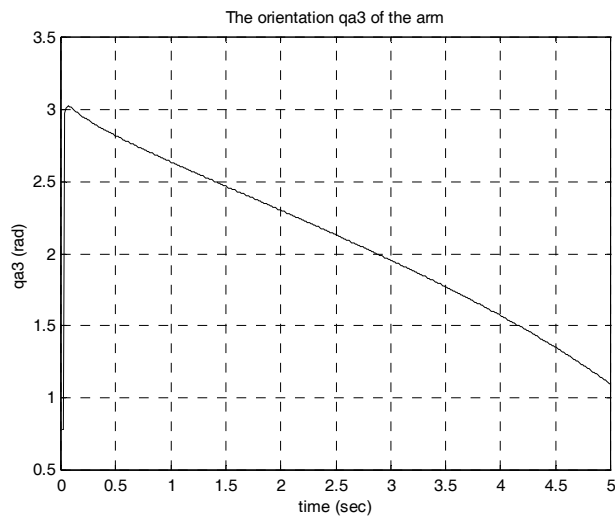


Fig. 22. Articulation q_{a3} curve

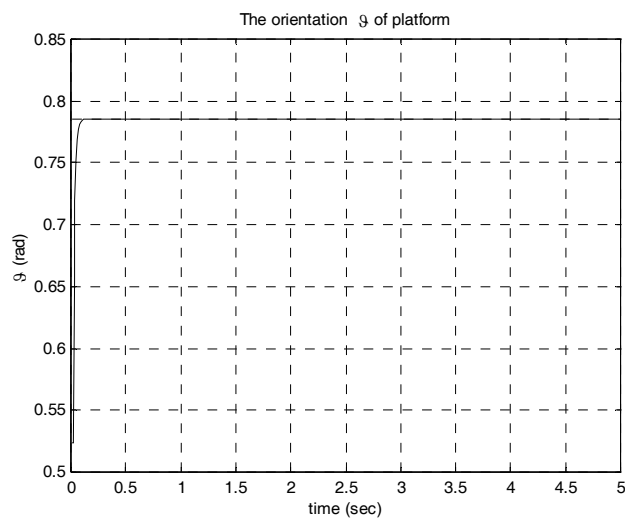


Fig. 23. Articulation ϑ curve

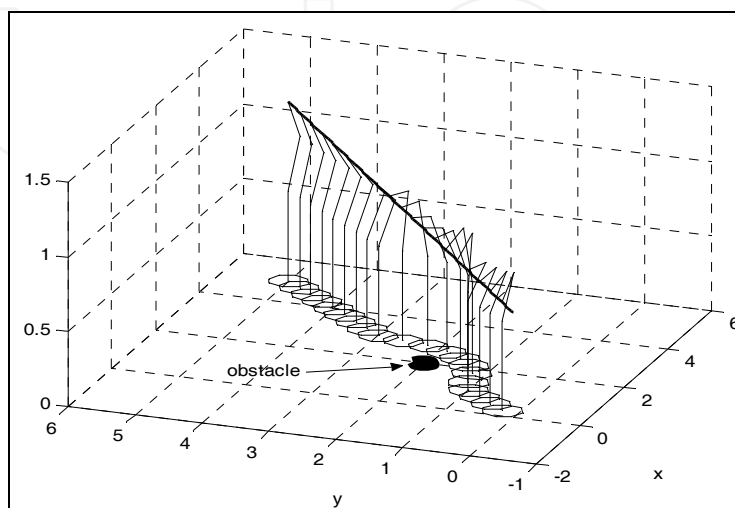


Fig. 24. A 3D-View of the arm and the platform evolutions in presence of obstacles

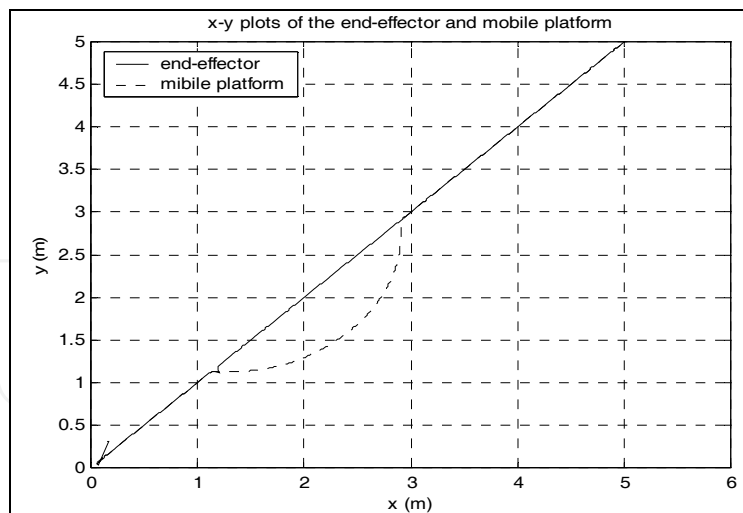


Fig. 25. End-effector and mobile platform trajectories in the x-y plane in presence of obstacles

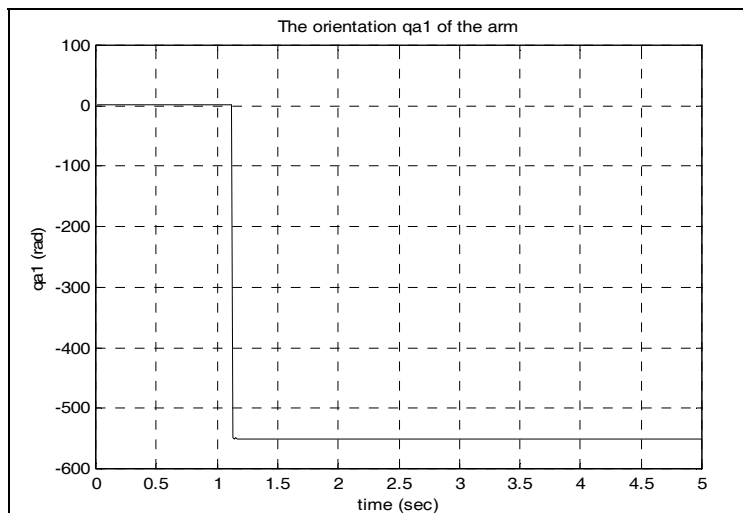


Fig. 26. Evolution curve of the joint 01

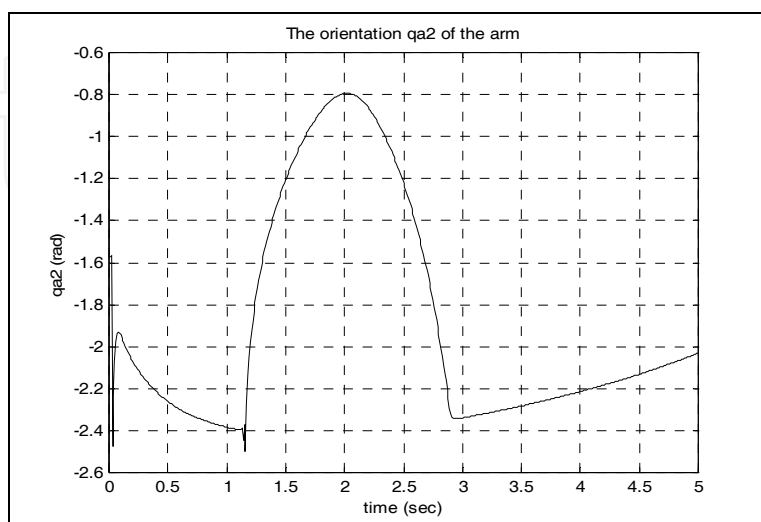
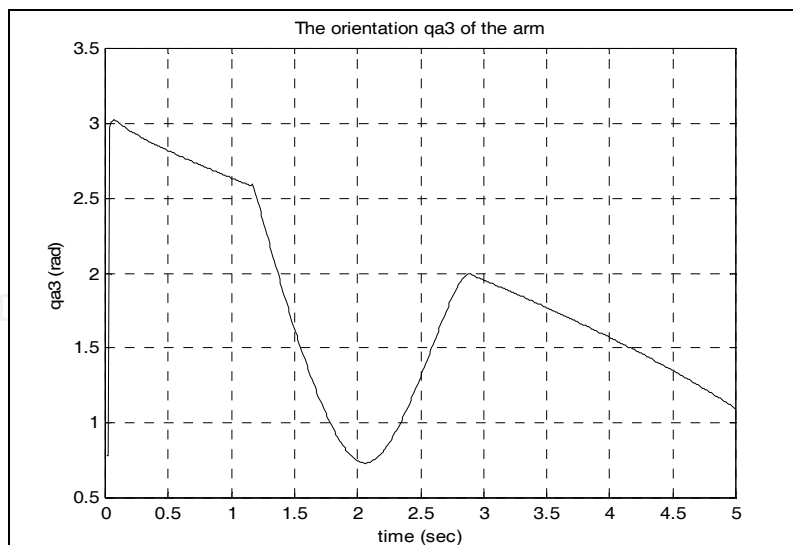
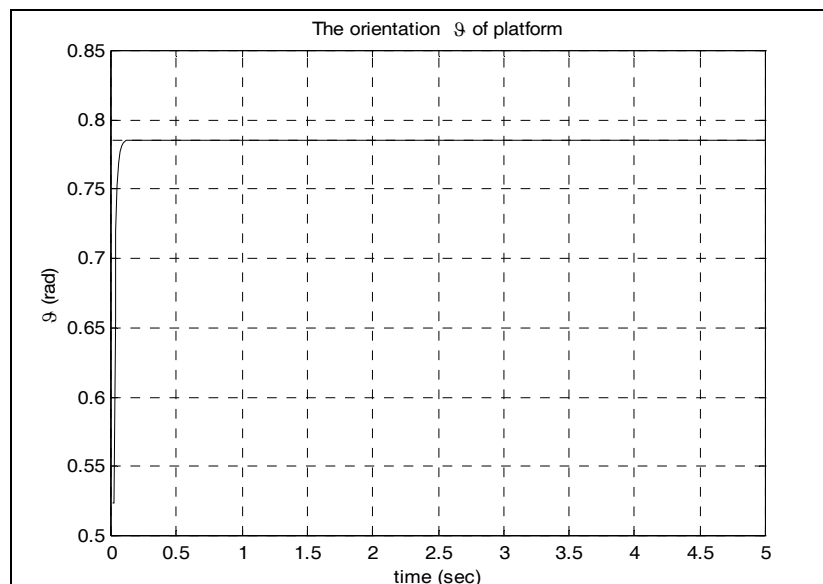


Fig. 27. Evolution curve of the joint 02

Fig. 28. Evolution curve of the joint θ_3 Fig. 29. Articulation ϑ curve

4. Conclusion

This work proposed two different methodologies to generating desired joint trajectories for both holonomic and non-holonomic mobile manipulators given prespecified operational tasks. The first part considers a non-holonomic platform where the generalized inverses in the resolution of a redundant system are used. The additional degrees of freedom are exploited to avoid unforeseen obstacles and joint limits. In the second part of the work a holonomic platform is used. In this case, the trajectory is generated using a reactive approach based on virtual impedance and additional tasks. When the robot task is about a stationary point, the mobile manipulator showed a good tracking for the manipulator. As perspective an estimate procedure must be conducted in order to estimate the contact forces and the unknown holonomic mobile manipulator parameters driving the system Computer

simulations have validated to show the effectiveness of the two approaches. The reference values obtained by the two methods can be used as inputs to controllers for real motion.

5. References

- Khatib, O. (1986). Real-time obstacle avoidance for manipulators and mobile robots, *International Journal of Robotics Research*, 5(1):90-98.
- Sundar, S. & Shiller, Z. (1997). Optimal obstacle avoidance based on the Hamilton-Jacobi-Bellman equation, *IEEE Trans. on Robotics and Automation*, Vol. 13, pp. 305-310.
- Laumond, J. P., Jacobs, P. E., Taix, M., and Murray, R. M. (1994). A motion planner for nonholonomic mobile robots, *IEEE Trans. on Robotics and Automation*, Vol. 10, pp. 577-593.
- Reeds, J. A. and Shepp, R. A. (1990). Optimal paths for a car that goes both forward and backward, *Pacific J. Math.*, vol. 145, pp. 367-393.
- Murray, R. M.; Li, Z. & Sastry, S. S. (1994). A Mathematical Introduction to Robotic Manipulation. Boca Raton, FL: CRC Press.
- Tilbury, D.; Murray, R. M. & Sastry, S. S. (1995). Trajectory generation for the n-trailer problem using goursatnormal form, *IEEE Trans. Automat. Contr.*, vol. 40, pp. 802-819, May 1995.
- Abdessemed, F. Monacelli, E. & Benmahammed, K. (2008). Trajectory Generation In an Alternated and a Coordinated Motion Control Modes of a Mobile Manipulator, *AMSE journal, Modelling, Measurements and Control B*, Vol.77, No 1, pp 18-34.
- Djebrani, S. Benali, A. & Abdessemed, F. (2009). Force-position control of a holonomic mobile manipulator, 12 int. Conf. on Climbing & Walking Robots and the support technoligis for Mobile Machines Bogazaci Univ. Garanti Culture Center (North Campus).
- Qu, Z.; Wang, J. & Plaisted, C. E. (2004). A New Analytical Solution to Mobile Robot Trajectory Generation in the Presence of Moving Obstacles, *IEEE Tran. on Robotics*, Vol. 20, No. 6.
- Kant, K. & Zucker, S. W. (1988). Planning collision free trajectories in time varying environments: A two-level hierarchy, in *Proc. IEEE Int. Conf. Robotics and Automation*, Raleigh, NC, pp. 1644-1649.
- Murray, R. M. & Sastry, S. S. (1993). Nonholonomic motion planning: Steering using sinusoids, *IEEE Trans. Automat. Contr.*, vol. 38, pp. 700-716.
- Abdessemed, F.; Benmahammed, K. & Eric Monacelli (2004). A Fuzzy Based Reactive Controller for Non-Holonomic Mobile Robot, *Journal of Robotics and Autonomous Systms*, 47 (2004) 31-46.
- Russell, S. & Norvig, P. (2000). Artificial Intelligence: A Modern Approach, *Prentice Hall*, New Jersey, 1995
- A. Okabe, B. Boots, K. Sugihara and S.N. Chiu, Spatial Tessellations and Applications of Voronoi Diagrams, John Wiley & Sons, New York.
- Zhao, M.; Ansari, N. & Hou, E.S.H. (1994). Mobile manipulator path planning by a genetic algorithm, *Journal of Robotic Systems*, 11(3): 143-153.
- Pin, F. G. & Culioli, J. C. (1992). Optimal Positioning of Combined Mobile Platform-Manipulator systems for Material Handling Tasks, *Journal of intelligent and Robotic Systems*. 6: 165-182.

- Pin, F. G.; Morgansen, K. A.; Tulloch, F. A.; Hacker, C. J. & Gower, K. B. (1996). Motion Planning for Mobile Manipulators with a Non-Holonomic Constraint Using the FSP (Full Space Parameterization) Method, *Journal of Robotic Systems* 13(11), 723-736.
- Lee, J. K. & Cho, H. S. (1997). Mobile manipulator Motion Planning for Multiple Tasks Using Global Optimization Approach, *Journal of Intelligent and Robotic Systems*, 18: 169-190.
- Seraji, H. (1995) Configuration control of rover-mounted manipulators, *IEEE Int. Conf. on Robotics and Automation*, pp2261-2266.
- Campion, G.; Bastin, B. & D'Andrea-Novel. (1996). Structural proprieties and classification of kinematic and dynamic models of wheeled mobile robots. *IEEE Trans. on Robotics and Automation*, 2(1):47{62, February.
- Liegeois, A. (1997). Automatic supervisory control of the configuration and behavior of multibody mechanisms, *IEEE Trans. Syst. Man Cybernet.* 7, 842-868.
- Seraji, H. (1993). An on-line approach to coordinated mobility and manipulation, ICRA'93, pp. 28-35, May, 1993.
- Mourioux, G.; Novales, C.; Poisson, G. & Vieyres, P. (2006). Omni-directional robot with spherical orthogonal wheels: concepts and analyses, *IEEE International Conference on Robotics and Automation*, pp. 3374-3379.
- Seraji, H. (1998). A unified approach to motion control of mobile manipulators, *The International Journal of Robotics Research*, vol. 17, no. 2, pp. 107-118.
- Bayle, B.; Fourquet, J. Y.; Lamiroux, F. & Renaud, M. (2002). Kinematic control of wheeled mobile manipulators, *IEEE/RSJ International Conference on Intelligent Robots and Systems*, pp. 1572-1577.
- Arai, T. & Ota, J. (1996). Motion planning of multiple mobile robots using virtual impedance, *Journal of Robotics and Mechatronics*, vol. 8, no. 1, pp. 67-74.
- Borenstein, J. & Koren, Y. (1991). The vector field histogram fast obstacle avoidance for mobile robots, *IEEE Transactions on Robotics and Automation*, vol. 7, no. 3, pp. 278-288.

IntechOpen

IntechOpen

IntechOpen



Robot Manipulators Trends and Development

Edited by Agustin Jimenez and Basil M Al Hadithi

ISBN 978-953-307-073-5

Hard cover, 666 pages

Publisher InTech

Published online 01, March, 2010

Published in print edition March, 2010

This book presents the most recent research advances in robot manipulators. It offers a complete survey to the kinematic and dynamic modelling, simulation, computer vision, software engineering, optimization and design of control algorithms applied for robotic systems. It is devoted for a large scale of applications, such as manufacturing, manipulation, medicine and automation. Several control methods are included such as optimal, adaptive, robust, force, fuzzy and neural network control strategies. The trajectory planning is discussed in details for point-to-point and path motions control. The results in obtained in this book are expected to be of great interest for researchers, engineers, scientists and students, in engineering studies and industrial sectors related to robot modelling, design, control, and application. The book also details theoretical, mathematical and practical requirements for mathematicians and control engineers. It surveys recent techniques in modelling, computer simulation and implementation of advanced and intelligent controllers.

How to reference

In order to correctly reference this scholarly work, feel free to copy and paste the following:

Foudil Abdessemed and Salima Djebrani (2010). Trajectory Generation for Mobile Manipulators, Robot Manipulators Trends and Development, Agustin Jimenez and Basil M Al Hadithi (Ed.), ISBN: 978-953-307-073-5, InTech, Available from: <http://www.intechopen.com/books/robot-manipulators-trends-and-development/trajectory-generation-for-mobile-manipulators>

INTECH
open science | open minds

InTech Europe

University Campus STeP Ri
Slavka Krautzeka 83/A
51000 Rijeka, Croatia
Phone: +385 (51) 770 447
Fax: +385 (51) 686 166
www.intechopen.com

InTech China

Unit 405, Office Block, Hotel Equatorial Shanghai
No.65, Yan An Road (West), Shanghai, 200040, China
中国上海市延安西路65号上海国际贵都大饭店办公楼405单元
Phone: +86-21-62489820
Fax: +86-21-62489821

© 2010 The Author(s). Licensee IntechOpen. This chapter is distributed under the terms of the [Creative Commons Attribution-NonCommercial-ShareAlike-3.0 License](https://creativecommons.org/licenses/by-nc-sa/3.0/), which permits use, distribution and reproduction for non-commercial purposes, provided the original is properly cited and derivative works building on this content are distributed under the same license.

IntechOpen

IntechOpen