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# Improvements Quality of Kohonen Maps Using Dimension Reduction Methods 

Jiří Dvorský, Václav Snášel, Jana Kočíbová<br>VŠB - Technical University of Ostrava<br>Czech Republic

## 1. Introduction

The performance of Self Organizing Map (SOM) is always influenced by learn methods. The resultant quality of the SOM is also highly dependent onto the learning rate and the neighborhood function. In literature, there are plenty of studies to find a proper method to improve the quality of learning process of the SOM. They focus especially on convergence (Cottrell et al., 1998; Kohonen, 2001), the measure of the global topology preservation (Bauer et al., 1999) and, at an individual level, the sensitivity to parameters such as initialization, rate of decrease of neighborhood function, optimum learning rate etc. (de Bodt \& Cottrell, 2000; Mulier \& Cherkassky, 1995; Germen, 2005; Flanagan, 1996; 1994).
Although various disciplines use the SOM model in order to find solutions to broad spectrum of problems, however, there is not so much clue about the how the resultant maps are supposed to look after training.
Most articles are focused on the learning process of the SOM. The quality of the SOM is needed to measure in this process. The question is how to measure this quality. The distortion, or distortion measure, is certainly the most popular criterion for assessing the quality of the classification of the SOM (Kohonen, 2001; Rynkiewicz, 2006). Distortion measure provides an assessment of SOM properties with respect to the data and overcomes the absence of cost function in the SOM algorithm. Usually Mean Squared Error (MSE) is used to measure a distortion. The MSE is just a number without any dimension or scale, and may be hard to understand. What is the value of distortion is small enough? At what point should be the learning process terminated? Alternative approach for measurement of quality of learning process is the goal of our research.
In the SOM each neuron represents a set of input vectors. As the learning process continues, the set should be more and more stable, i.e. particular input vector should not move from one set to another in successive iteration in learning process. Movements, which still occur, can measure the quality of the learning process or quality of resultant SOM, if we decide to stop the learning.
Another idea is usage of a dimension reduction methods to capture most significant features of resultant SOM (Dvorský, 2007). At the beginning of the learning process, weights in the SOM are initialized with random values. In this case, there is no common, important feature in the SOM - the SOM contains only noise. How learning process continues, the map will learn significant features in the data. These features should be dominant, and if some approximation of the SOM is computed, these features must be preserved. In this moment, SVD or HOSVD, see sections 2.1 and 2.2, can be used to compute SOM approximation. In terms of

SVD, dominant features of the SOM will be represented as greater singular values. And vice versa, the small singular numbers will represent some noise in the SOM only. If small values are neglected, the approximated SOM will be very similar to the original one. In this way, quality of the SOM can be measured using data dimension reduction methods.

### 1.1 Notation of the SOM

In this chapter we will consider SOM as an array of neurons $\mathbf{m}_{\mathbf{i}}$, usually arranged in a low dimensionality grid (1D or 2D), the map, for ease of visualization. The grid may have several forms like rectangular, hexagonal. For each input vector $\mathbf{x}(t)$, neuron that best matches input vector is selected. This neuron is called Best Matching Unit (BMU). Then the weights of the BMU and its neighborhood will be adapted as follows:

$$
\begin{equation*}
\mathbf{m}_{i}(t+1)=\mathbf{m}_{i}(t)+\eta(t) h(t)\left(\mathbf{x}(t)-\mathbf{m}_{i}(t)\right), \quad \forall \mathbf{m}_{i} \tag{1}
\end{equation*}
$$

where $\eta, 0<\eta<1$ is the learning factor, which determines the speed of weight adaptation, and $h(t)$ is neighborhood size determining function.

## 2. Methods of Dimension Reduction

Since our approach is based on SVD and HOSVD techniques, we first briefly review matrix SVD and then introduce tensor and the HOSVD technique. In this chapter, tensors are denoted by calligraphic upper-case letters $(\mathcal{A}, \mathcal{B}, \ldots)$, matrices by uppercase letters $(A, B, \ldots)$, vectors by bold lower case letters $(\mathbf{a}, \mathbf{b}, \ldots)$, and scalars by lower case letters $(a, b, \ldots)$.

### 2.1 Singular Value Decomposition

Singular value decomposition (SVD) is well known because of its application in information retrieval - Latent semantic indexing (LSI) (Berry \& Browne, 1999; Berry et al., 1995). SVD is especially suitable in its variant for sparse matrices (Larsen, 1998).

Theorem 2.1 (Singular value decomposition) Let $A$ is an $n \times m$ rank-r matrix. Be $\sigma_{1} \geq \cdots \geq \sigma_{r}$ eigenvalues of a matrix $\sqrt{A A^{T}}$. Then there exist orthogonal matrices $U=\left(\mathbf{u}_{1}, \ldots, \mathbf{u}_{r}\right)$ and $V=$ $\left(\mathbf{v}_{1}, \ldots, \mathbf{v}_{r}\right)$, whose column vectors are orthonormal, and a diagonal matrix $\Sigma=\operatorname{diag}\left(\sigma_{1}, \ldots, \sigma_{r}\right)$. The decomposition $A=U \Sigma V^{T}$ is called singular value decomposition of matrix $A$ and numbers $\sigma_{1}, \ldots, \sigma_{r}$ are singular values of the matrix $A$. Columns of $U$ (or $V$ ) are called left (or right) singular vectors of matrix $A$.

Now we have a decomposition of original matrix $A$. It is not needed to say, that the left and right singular vectors are not sparse. We have at most $r$ nonzero singular numbers, where rank $r$ is the smaller of the two matrix dimensions. Luckily, because the singular values usually fall quickly, we can take only $k$ greatest singular values and corresponding singular vector coordinates and create a $k$-reduced singular decomposition of $A$.

Definition 2.1 Let us have $k, 0<k<r$ and singular value decomposition of $A$

$$
A=U \Sigma V^{T}=\left(U_{k} U_{0}\right)\left(\begin{array}{cc}
\Sigma_{k} & 0 \\
0 & \Sigma_{0}
\end{array}\right)\binom{V_{k}^{T}}{V_{0}^{T}}
$$

We call $A_{k}=U_{k} \Sigma_{k} V_{k}^{T}$ a $k$-reduced singular value decomposition (rank- $k$ SVD).


Fig. 1. rank-k Singular Value Decomposition

For an illustration of rank- $k$ SVD see Figure 1, the gray areas determine first $k$ coordinates from singular vectors, which are being used.

Theorem 2.2 (Eckart-Young) Among all $n \times m$ matrices $C$ of rank at most $k A_{k}$ is the one, that minimizes $\left\|A_{k}-A\right\|_{F}^{2}=\sum_{i, j}\left(A_{i, j}-C_{w, j}\right)^{2}$.

Because rank- $k$ SVD is the best rank- $k$ approximation of original matrix $A$, any other decomposition will increase the sum of squares of matrix $A-A_{k}$.
SVD rank- $k$ approximation of original matrix $A$ can be understood in several ways. In information retrieval, matrix $A$ represents term-document matrix, and a latent semantics is obtained using rank- $k$ approximation of original matrix $A$. From another point of view rank- $k$ approximation can be viewed as elimination of noise from data represents in matrix $A$.
The SVD is computed by a batch $O\left(n m^{2}+n^{2} m+m^{3}\right)$ time algorithm (Golub \& Loan, 1996), that is unfeasible for large datasets, but for our case this algorithm is fully adequate.

Note 2.1 From now on, we will assume rank-k singular value decomposition when speaking about SVD.

### 2.2 Tensors and HOSVD

A tensor is a higher order generalization of a vector (first order tensor) and a matrix (second order tensor). Higher order tensors are also called multidimensional matrices or multi-way arrays. The order of a tensor $\mathcal{A} \in \mathbb{R}^{I_{1} \times I_{2} \times \cdots \times I_{N}}$ is $N$. Elements of $\mathcal{A}$ are denoted as $a_{i_{1} \cdots i_{n} \cdots i_{N}}$ where $1 \leq i_{n} \leq I_{n}$. In tensor terminology, matrix column vectors are referred to as mode- 1 vectors and row vectors as mode- 2 vectors. The mode- $n$ vectors of an $N$-th order tensor $\mathcal{A}$ are the $I_{n}$-dimensional vectors obtained from $\mathcal{A}$ by varying the index $i_{n}$ and keeping the other indices fixed, that is the column vectors of $n$-mode matrix unfolding $\mathcal{A}_{(n)} \in R^{I_{n} \times\left(I_{1} I_{2} \cdots I_{n-1} I_{n+1} \cdots I_{N}\right)}$ of tensor $\mathcal{A}$. See (De Lathauwer et al., 2000) for details on matrix unfoldings of a tensor.
The $n$-mode product of a tensor $\mathcal{A} \in \mathbb{R}^{I_{1} \times I_{2} \times \cdots \times I_{N}}$ by a matrix $M \in \mathbb{R}^{J_{n} \times I_{n}}$ is an $I_{1} \times I_{2} \times \cdots \times$ $I_{n-1} \times J_{n} \times I_{n+1} \times \cdots \times I_{N}$-tensor of which the entries are given by

$$
\begin{equation*}
(\mathcal{A} \times n M)_{i_{1} \cdots i_{n-1} j_{n} i_{n+1} \cdots i_{N}}=\sum_{i_{n}} a_{i_{1} \cdots i_{n-1} i_{n} i_{n+1} \cdots i_{N}} m_{j_{n} i_{n}} \tag{2}
\end{equation*}
$$

Note that the $n$-mode product of a tensor and a matrix is a generalization of the product of two matrices. It can be expressed in terms of matrix unfolding:

$$
\begin{equation*}
B_{(n)}=M A_{(n)} \tag{3}
\end{equation*}
$$


where $B_{(n)}$ is the $n$-mode unfolding of tensor $\mathcal{B}=\mathcal{A} \times{ }_{n} M$.
In terms of $n$-mode products, the matrix SVD can be rewritten as $F=S \times{ }_{1} V^{(1)} \times_{2} V^{(2)}$. By extension, High order singular value decomposition (HOSVD) is a generalization of matrix SVD: every $I_{1} \times I_{2} \times \cdots \times I_{N}$ tensor $\mathcal{A}$ can be written as the $n$-mode product (De Lathauwer et al., 2000):

$$
\begin{equation*}
\mathcal{A}=S \times_{1} V^{(1)} \times_{2} V^{(2)} \cdots \times_{N} V^{(N)} \tag{4}
\end{equation*}
$$

HOSVD is illustrated in Figure 2 for $N=3$. $V_{n}$ contains the orthonormal vectors (called $n$ mode singular vectors) spanning the column space of the matrix $A_{(n)}$ (n-mode matrix unfolding of tensor $\mathcal{A}$ ). $\mathcal{S}$ is called core tensor. Instead of being pseudodiagonal (nonzero elements only occur when the indices satisfy $\left.i_{1}=i_{2}=\cdots=i_{N}\right), \mathcal{S}$ has the property of all-orthogonality. That is, two subtensors $\mathcal{S}_{i_{n}}=\alpha$ and $\mathcal{S}_{i_{n}}=\beta$ are orthogonal for all possible values of $n, \alpha$ and $\beta$ subject to $\alpha \neq \beta$. At the same time, the Frobenius-norms $\sigma_{i}^{n}=\left\|\mathcal{S}_{i_{n}=i}\right\|$ are $n$-mode singular values of $\mathcal{A}$ and are in decreasing order: $\sigma_{1}^{n} \geq \sigma_{2}^{n} \geq \cdots \geq \sigma_{I_{n}}^{n} \geq 0 \mathcal{S}$ is in general a full tensor and governs the interactions among $V_{n}$.

## 3. SVD and HOSVD Approximation of SOM

### 3.1 BMU Movements

BMU is found for each training vector during learning process. As the SOM learns the structure of training set, the BMU of given training vector usually changes its position within the map. Movement of the BMU at the initial phase of learning process will be probably very rapid, and as the SOM converges to stable configuration the movement of the BMU will be very tight. The learning process could be stopped, when user specific maximal number of moved BMUs is reached.
In this way, the number of moved BMUs can be taken as alternative learning process quality measurement. The number of changes of BMUs' positions between successive iterations was considered as measure in our initial work. But this approach is not very helpful. Some movements of the BMU still remain.

### 3.2 SVD Approach

The second approach to measurement of BMU movement uses SVD decomposition of SOM. It is supposed, that movement of BMUs among original SOM and its rank- $k$ approximations will be very low, when stable configuration of the SOM is reached. To verify this hypothesis following experiment was performed:

1. The SOM $S$ is transformed to $r c \times m$ matrix $A$, where $r$ is the number of rows, $c$ is the number of columns of SOM $S$, and $m$ is the dimension of input.


Note 3.1 Each $\mathbf{m}_{i, j}(t)$ is $m$ dimensional vector.
2. Rank $k$ approximation $A_{k}$ of matrix $A$ is computed, $1 \leq k \leq m$.
3. SOM $S(k)$ is created from matrix $A_{k}$.
4. The $B M U_{S}$ for each training vector is computed with original SOM $S$.
5. The $B M U_{S}(k)$ is computed with rank $k$ approximation $S(k)$ for each training vector.
6. If $B M U_{S}$ is different from $B M U_{S}(k)$ the movement is encountered.

### 3.3 HOSVD Approach

The SOM forms usually 2D dimensional grid, each neuron is represented as $m$ dimensional vector, where $m$ is the dimension of input, training, vectors. From this point of view, SOM can be understood as 3-order tensor, and 3-dimensional HOSVD, see Figure 2, can be applied onto SOM. There is no need to form matrix by transformation of SOM. 3-order HOSVD can directly decompose SOM. It is expected that HOSVD preserves better relationships among neurons and structure of SOM.
Experiment similar as in SVD approach was performed:

1. The SOM $S$ is transformed to tensor $\mathcal{A} \in R^{r \times c \times m}$, where $r$ is the number of rows, $c$ is the number of columns of SOM $S$, and $m$ is the dimension of input.
2. $\mathcal{A}_{\left(k_{1}, k_{2}, k_{3}\right)}$ approximation of tensor $\mathcal{A}$ was computed. This approximation generalizes rank- $k$ approximation of matrix in SVD.
3. $\operatorname{SOM} S\left(k_{1}, k_{2}, k_{3}\right)$ is created from tensor $\mathcal{A}_{\left(k_{1}, k_{2}, k_{3}\right)}$.
4. The $B M U_{S}$ for each training vector is computed with original SOM $S$.
5. The $B M U_{S}\left(k_{1}, k_{2}, k_{3}\right)$ is computed with approximated SOM $S\left(k_{1}, k_{2}, k_{3}\right)$ for each training vector.
6. If $B M U_{S}$ is different from $B M U_{S}\left(k_{1}, k_{2}, k_{3}\right)$ the movement is encountered.

## 4. Experimental Results

A number of experiments were carried out to prove our hypothesis. One of them is provided in this chapter. Parameters of used SOM $S$ are given in Table 1. The input data comes from experiments done by Kudelka et al. (Kudelka et al., 2006).

| Parameter | Value |
| :--- | :---: |
| \# of rows | 50 |
| \# of columns | 50 |
| SOM shape | toroid |
| input dimension | 10 |
| \# of input vectors | approx 25,000 |
| \# of iterations | 5000 |

Table 1. Experimental SOM $S$ parameters

### 4.1 Results of SVD Approach

The experimental results are summarized in following tables and graphs. Table 2 provides insight to learning process. Each rank- $k, 1 \leq k \leq 10$, approximation $S(k)$ of SOM $S$ is computed and number of moved BMUs are stored, moreover a distance of the movement.
In initial phase of learning process, there is no significant difference among $S(k)$ approximations. The number of moved BMUs varies from $99 \%$ to $26 \%$ in iteration 0 . Average distance of movement is also near constant, from 13.6 to 15.4.
There are significant difference among each $S(k)$ approximations after 4000 and 5000 iterations. $S(1)$ approximation has $76 \%$ of moved input vectors, but $S(8)$ resp. $S(9)$ has only $9 \%$ resp. $2.6 \%$ of moved input vectors after 5000 iterations. The average distance is also very small, only 2.4 resp. 3.
Although maximal distance of the movement remains very high in all phases of learning process, the average distance of BMUs movement decreases. Histograms of these distances can provide very useful information about learning. Figure 3(a) demonstrates initial state of SOM $S$. The distribution of distances is random; there are plenty of short movements and also a lot of long movement of BMUs. The charts 3(d) have different shape. Histogram of distances has strong hyperbolic shape, i.e. very short movements are predominate. Cumulative histogram shows, that movements of length 1 (less than $20 \%$ ) comprise slightly more than $80 \%$ of all movements for $S(8)$ resp. $S(9)$ approximations. These results coincide with the widely known "Pareto's 80/20 law". In other words, SOMs $S(8)$ resp. $S(9)$ are very close to original SOM $S$, consequently SOM $S$ after 5000 iterations completed contains very small amount of noise (compare $S(9)$ approximation after 500 iterations completed). We can conlude, that well trained SOM is resistant to SVD decomposition.
U-matrices (Ultsch, 1993) of experimental SOM $S$ and its approximations $S(k)$ are given in Figure 4. These figures show, that even $S(1)$ approximation is used, the main features, main structure, of original SOM is preserved. $S(2)$ resp. $S(3)$ approximation add more details to basic structure of $S(1)$ approximation. $S(8)$ resp. $S(9)$ approximations are not easily distinguishable from original SOM.

### 4.2 Results of HOSVD Approach

On the other hand performance of HOSVD approximation of SOM $S$ was disappointing. Umatrices of approximated SOM are very similar to SVD ones, see Figure 6. Also cumulative histograms 5 of BMUs' movements show very similar characteristics. But when absolute values are compared, there are very high differences, see Table 3 e.g. only 616 BMUs were moved after 5,000 iterations in rank-9 SVD approximation, which is only $2.63 \%$ of all input vectors. But in similar HOSVD approximation more than 9,000 BMUs were moved.

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## 5. Conclusion

Alternative approach of quality measurement of the SOM learning process was presented. This approach uses SVD decomposition of the SOM, and number of moved BMUs are counted among each consecutive rank-k approximations of original SOM. Our experiments show some properties of SVD decomposition of SOM. That is new and good.
On the other hand HOSVD cause some problems, because number of moved BMUs is very high. It seems that SOM is not true three dimensional object - the third dimension consisting of neurons is not relevant. We should check if this behavior is feature or bug of this method or if it is a matter of coincidence. This is new and quite disappointing.
Usage of Non-negative Matrix Factorization (Golub \& Loan, 1996) is our goal in future research. The second goal is application of presented method on the other type of neural network, such as Growing Neural Gas (Fritzke, 1994).

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Fig. 3. Frequency and cumulative frequency histograms of distances between $B M U_{S}$ and $B M U_{S}(k)$ for SOM $S$

(c) $k=2$ approximation
(d) $k=3$ approximation

(e) $k=8$ approximation

(f) $k=9$ approximation

Fig. 4. SVD rank-k approximations of final SOM $S$ (after 5000 iterations)


Fig. 5. Frequency and cumulative frequency histograms of distances between $B M U_{S}$ and $B M U_{S}\left(k_{1}, k_{2}, k_{3}\right)$ for SOM S
(a) Original SOM
(b) $k_{1}=5, k_{2}=5, k_{3}=1$ approximation

(c) $k_{1}=10, k_{2}=10, k_{3}=2$ approximation (d) $k_{1}=15, k_{2}=15, k_{3}=3$ approximation

(e) $k_{1}=40, k_{2}=40, k_{3}=8$ approximation (f) $k_{1}=45, k_{2}=44, k_{3}=9$ approximation

Fig. 6. $S\left(k_{1}, k_{2}, k_{3}\right)$ HOSVD approximations of final SOM $S$ (after 5000 iterations)

|  | Number of singular values $k$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 |  |
|  | 0 completed iterations |  |  |  |  |  |  |  |
| MSE | 0.784 | 0.74 | 0.712 | 0.64 | 0.614 | 0.57 | 0.536 | 0.5 |
| \# of moved BMUs | 23,381 | 22,570 | 18,053 | 15,897 | 14,963 | 12,326 | 11,031 | 10,65 |
| Moved BMUs [\%] | 99.825 | 96.362 | 77.077 | 67.872 | 63.884 | 52.626 | 47.097 | 45.48 |
| Max. distance | 25 | 25 | 25 | 25 | 25 | 25 | 25 |  |
| Average distance | 13.6 | 13.9 | 16.6 | 17.7 | 17.2 | 16.3 | 17 | 14.9 |
|  | 500 completed iterations |  |  |  |  |  |  |  |
| MSE | 0.603 | 0.456 | 0.366 | 0.303 | 0.244 | 0.209 | 0.172 | 0.13 |
| \# of moved BMUs | 22,000 | 19,805 | 18,468 | 16,496 | 13,823 | 11,681 | 9,788 | 7,14 |
| Moved BMUs [\%] | 93.929 | 84.557 | 78.849 | 70.43 | 59.017 | 49.872 | 41.79 | 30.51 |
| Max. distance | 25 | 25 | 25 | 25 | 25 | 25 | 25 |  |
| Average distance | 14.3 | 10 | 9.2 | 6.6 | 6.4 | 5.9 | 5.5 |  |
|  | 4000 completed iterations |  |  |  |  |  |  |  |
| MSE | 0.595 | 0.452 | 0.356 | 0.284 | 0.236 | 0.184 | 0.143 | . 0 |
| \# of moved BMUs | 20,643 | 16,252 | 13,698 | 11,964 | 9,353 | 8,185 | 4,907 | 3,92 |
| Moved BMUs [\%] | 88.135 | 69.388 | 58.483 | 51.08 | 39.933 | 34.946 | 20.95 | 16.75 |
| Max. distance | 25 | 25 | 25 | 25 | 25 | 25 | 25 |  |
| Average distance | 11.4 | 8 | 6.9 | 5.8 | 4.8 | 3.8 | 4.2 |  |
|  | 5000 completed iterations |  |  |  |  |  |  |  |
| MSE | 0.595 | 0.452 | 0.355 | 0.284 | 0.229 | 0.18 | 0.119 | 0.08 |
| \# of moved BMUs | 1,7748 | 10,760 | 7,555 | 6,868 | 5,058 | 3,781 | 2,564 | 2,12 |
| Moved BMUs [\%] | 75.775 | 45.94 | 32.256 | 29.323 | 21.595 | 16.143 | 10.947 | 9.07 |
| Max. distance | 25 | 25 | 25 | 25 | 25 | 25 | 25 |  |
| Average distance | 13.2 | 9.1 | 7.5 | 5.5 | 5 | 4 | 3.7 |  |

Table 2. Parameters of SVD rank-k approximations of given SOM

|  | Approximation parameters ( $k_{1}, k_{2}, k_{3}$ ) |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $(5,5,1)$ | $(10,10,2)$ | $(15,15,3)$ | $(20,20,4)$ | $(25,25,5)$ | $(30,30,6)$ | $(35,35,7)$ |
|  | 0 completed iterations |  |  |  |  |  |  |
| MSE | 1.485 | 1.218 | 1.136 | 0.979 | 0.887 | 0.754 | 0.696 |
| \# of moved BMUs | 23,422 | 23,421 | 23,407 | 23,104 | 23,299 | 23,109 | 21,829 |
| Moved BMUs [\%] | 100 | 99.996 | 99.936 | 98.642 | 99.475 | 98.664 | 93.199 |
| Max. distance | 25 | 25 | 25 | 25 | 25 | 25 | 25 |
| Average distance | 18.4 | 14.6 | 16.3 | 16.7 | 15 | 15.9 | 15.9 |
|  | 4000 completed iterations |  |  |  |  |  |  |
| MSE | 0.595 | 0.452 | 0.356 | 0.285 | 0.237 | 0.184 | 0.143 |
| \# of moved BMUs | 23,404 | 23,304 | 22,722 | 21,671 | 20,141 | 18,890 | 17,265 |
| Moved BMUs [\%] | 99.923 | 99.496 | 97.011 | 92.524 | 85.992 | 80.651 | 73.713 |
| Max. distance | 25 | 25 | 25 | 25 | 25 | 25 | 25 |
| Average distance | 14.3 | 11 | 6.6 | 6.5 | 5 | 2.5 | 2.3 |
|  | 5000 completed iterations |  |  |  |  |  |  |
| MSE | 0.595 | 0.453 | 0.356 | 0.285 | 0.23 | 0.182 | 0.12 |
| \# of moved BMUs | 23,398 | 23,220 | 21,419 | 18,217 | 19,305 | 18,132 | 15,638 |
| Moved BMUs [\%] | 99.898 | 99.138 | 91.448 | 77.777 | 82.423 | 77.414 | 66.766 |
| Max. distance | 25 | 25 | 25 | 25 | 25 | 25 | 25 |
| Average distance | 14.6 | 13.7 | 8.6 | 6 | 3.4 | 2.2 | 1.8 |

Table 3. Parameters of $S\left(k_{1}, k_{2}, k_{3}\right)$ HOSVD approximations of given SOM $S$


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The Self－Organizing Map（SOM）is a neural network algorithm，which uses a competitive learning technique to train itself in an unsupervised manner．SOMs are different from other artificial neural networks in the sense that they use a neighborhood function to preserve the topological properties of the input space and they have been used to create an ordered representation of multi－dimensional data which simplifies complexity and reveals meaningful relationships．Prof．T．Kohonen in the early 1980s first established the relevant theory and explored possible applications of SOMs．Since then，a number of theoretical and practical applications of SOMs have been reported including clustering，prediction，data representation，classification，visualization，etc． This book was prompted by the desire to bring together some of the more recent theoretical and practical developments on SOMs and to provide the background for future developments in promising directions．The book comprises of 25 Chapters which can be categorized into three broad areas：methodology，visualization and practical applications．

## How to reference

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## InTech Europe

University Campus STeP Ri
Slavka Krautzeka 83／A
51000 Rijeka，Croatia
Phone：＋385（51） 770447
Fax：＋385（51） 686166
www．intechopen．com

## InTech China

Unit 405，Office Block，Hotel Equatorial Shanghai
No．65，Yan An Road（West），Shanghai，200040，China
中国上海市延安西路65号上海国际贵都大饭店办公楼405单元
Phone：＋86－21－62489820
Fax：＋86－21－62489821
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