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## Femtosecond Filamentation in Temperature Controlled Noble Gas

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### 1. Introduction

Intense few to monocycle pulses are the mJ or sub-mJ ultrashort pulses which have one to two optical periods (800 nm corresponding to 2.67 fs). They play more and more important roles in today's scientific and technological research fields, such as time-resolved measurements of electron dynamics in atoms and molecules, high-order harmonics and isolate attosecond pulse generation. To date, the major way of achieving intense few to monocycle pulses is to compress the spectra broadened through hollow fiber filled with noble gases or filamentation.

Combined with the technique of noble gas-filled hollow fiber and feedback phase compression, Yamashita group has achieved the shortest pulse duration 2.6 fs in the visible light range (Yamashita et al., 2006; Yamane et al., 2003; Matsubara et al., 2007). However, due to the damage at the entrance of the fiber, self-focusing and gas breakdown, the pulse energy in a gas-filled hollow fiber is limited to  $\mu\text{J}$  level. In addition, the loss in the hollow fiber also contributes to the low efficiency. Spectrum broadening through filamentation was presented as one of the extremely simple technique to generate intense few to monocycle pulses (Hauri et al. 2004; Hauri et al., 2005; Zair et al., 2007). In addition, the pulse self-compression can be realized in the filamentation (Couairon et al., 2006; Couairon et al., 2005). However, the competition of the multi-filament (Shen, 1984; Bergé et al., 2004; Vidal & Johnston, 1996; Braun et al., 1995; Skupin et al., 2004; Hosseini et al., 2004) when the peak power is several times above the critical power introduces instability between the filaments and restricts the achievement of high quality ultrashort intense pulses. The spectrum broadening through hollow fiber with a gradient pressure seems to be an efficient way to overcome the breakdown at the entrance of the fiber, and preserve the spatial and spectral qualities of the pulses with final energy of multi-mJ (Suda et al., 2005; Sung et al., 2006), but

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it is difficult to realize in the filamentation, because differential pumping does not only result in a large consumption of expensive noble gases, but also in a gas flow that disturbs the spatial beam stability and the spectral characteristics.

In this Chapter, we present a novel technique that could have the same effect as gradient pressure scheme to produce controllable nonlinear refraction index: the gradient temperature in a sealed tube filled with noble gas (Song et al., 2008a; Song et al., 2008b; Cao et al., 2009). That is, in practice, to heat the entrance and cool the exit end of the tube, so a temperature gradient can be formed along the tube. The gas pressure in this sealed tube reaches equilibrium but the gas density is gradually increased along the tube. This gradient temperature should have the similar effect as that of gradient pressure, because these two schemes both have increasing gas density distribution along the propagation of the pulse. Therefore, the incident pulse will be allowed to have a higher energy because the lower gas density at the entrance. The spectrum broadening will go on along the tube because the increasing gas density will compensate the decreasing peak power due to loss and dispersion. The ideas of gradient pressure and gradient temperature schemes are shown in Fig. 1. In the gradient pressure case the gas flow has disturbance to the system which will affect the stability and quality of the output beam while in the gradient temperature case the gas reaches equilibrium to avoid the disadvantages of the gradient pressure. Theoretical and experimental results will be shown in section 3 and 4 respectively to illustrate and prove the feasibility and effectiveness of the gradient temperature scheme and a final conclusion will be drawn in section 5 of this Chapter. Before we show the results we shall simply make some efforts on the filamentation and dynamics in filamentation in the section below.

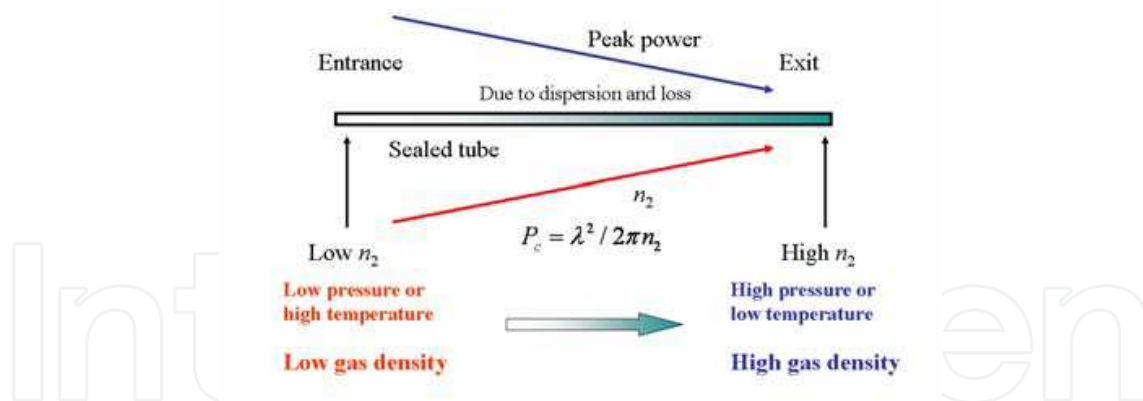


Fig. 1. Illustration of the gradient pressure and gradient temperature technique.

## 2. Theoretical model of dynamics in filamentation

Filamentation is a well-known phenomenon of the propagation of intense laser pulses in any kinds of Kerr media (gases, liquids, and transparent solid materials) under certain conditions. It is the result of the balance between the self-focusing due to the nonlinear refractive index of the medium dependence on the intensity and the defocusing due to the formation of the plasma and beam diffraction when a sufficient intense ultrashort laser

pulse propagates in the transparent medium. A single filament always occurs when the incident pulse with a peak power between one and a few times  $P_c$  where  $P_c$  is the critical power values of self-focusing. For a CW Gaussian beam, the self-focusing critical power is expressed by (Marburger, 1975):

$$P_c = \lambda_0^2 / 2\pi n_0 n_2 \quad (1)$$

where  $\lambda_0$  is the wavelength in vacuum,  $n_0$  and  $n_2$  are the linear and nonlinear refraction index of the medium. However, when the laser peak power is much higher than the self-focusing critical power, the incident beam typically breaks into several long and narrow filaments, a phenomenon known as multiple filamentation (MF). Multiple filamentation is an unstable state because there is the interaction among the filaments (Shen, 1984; Bergé et al., 2004; Vidal & Johnston, 1996; Braun et al., 1995; Skupin et al., 2004; Hosseini et al., 2004), which limits the energy that each filament can carry.

## 2.1 Model equations

In order to describe the dynamic of filamentation, a 3D extended nonlinear Schrödinger equation coupled with the electron density equation are usually employed. The extended nonlinear Schrödinger equation for the electric field envelop  $\varepsilon(r, t, z)$  in a reference frame ( $t = t_{\text{lab}} - z/v_g$ ) moving at the group velocity  $v_g$  can be written as,

$$\begin{aligned} \partial \varepsilon / \partial z = & i(\partial^2 \varepsilon / \partial r^2 + \partial \varepsilon / \partial r / r) / 2k_0 n_0 - ik''(\partial^2 \varepsilon / \partial t^2) / 2 \\ & + ik_0 n_2 |\varepsilon|^2 \varepsilon - ik_0 \rho \varepsilon / 2n_0 \rho_c - \sigma \rho \varepsilon / 2 - U_i W(I)(\rho_{nt} - \rho) \varepsilon / 2I \end{aligned} \quad (2)$$

where the evolution of the electron density  $\rho$  follows the equation,

$$\partial \rho / \partial t = W(I)(\rho_{nt} - \rho) + \sigma \rho |\varepsilon|^2 / U_i \quad (3)$$

where the terms on the right-hand side of Eq. (2) describe transverse beam diffraction, GVD, nonlinear self-focusing, absorption and defocusing due to the electron density  $\rho$ , and absorption by photo-ionization; the terms on the right-hand side of Eq. (3) are the generation of the plasma by photon ionization (involving multiphoton ionization and tunnel ionization) and avalanche (multiplication of the electrons in the laser field). In Eqs. (2) and (3),  $k_0$  is the wave number in vacuum,  $k''$  the second order dispersive coefficient,  $\rho_c$  the critical plasma density above which the plasma becomes opaque,  $\rho_{nt}$  the neutral atom density,  $\sigma$  the cross-section for inverse bremsstrahlung,  $U_i$  the ionization potential,  $I = \varepsilon \varepsilon^*$  the laser intensity and  $W(I)$  the photoionization rate. Equations (2) and (3) can be solved simultaneously by the split-step method (Agrawal, 2007). The photoionization rate from Keldysh theory (Keldysh, 1965) can be calculated by the PPT (Perelemov-Popov-Terent'ev) model (Perelemov et al., 1966) which reduced to tunnelling (Ammosov et al., 1966) or multiphoton ionization models under certain conditions. An initial collimated Gaussian beam following a lens read as:

$$\varepsilon(r, t, 0) = \varepsilon_g \exp(-r^2 / w_0^2 - t^2 / t_0^2 - ikr^2 / 2f) \quad (4)$$

where  $\varepsilon_g$  is the peak amplitude of the incident electric field,  $k = n_0 k_0$  the wave number in the medium,  $f$  the focal length of the lens,  $t_0$  and  $w_0$  are the half temporal width and the spatial radius of the  $1/e^2$  intensity (for), respectively.

## 2.2 Description of ionization

Plasma generation and plasma defocusing are important dynamics in the filamentation formation. It is very important to construct the ionization model to describe the propagation of the intense pulse in filamentation. That is, how to calculate the parameter  $W(l)$  in Eq. (3). Optical-field-ionization (OFI) covers both the multiphoton and tunnel regimes which we usually use the adiabaticity parameter  $\gamma$  to distinguish with. For an atom with ionization potential  $U_i$  in a linearly polarized laser field with frequency  $\omega_0$  and peak electric field  $E$ ,  $\gamma$  is defined as:

$$\gamma = \omega_0 \sqrt{2mU_i} / eE \quad (5)$$

where  $e$  is the electron charge and  $m$  the electron mass. OFI occurs in the tunnel regime when  $\gamma \ll 1$  and in the multiphoton regime when  $\gamma \gg 1$ .

Keldysh's theory (Keldysh, 1965) and its subsequent developments (PPT model) (Perelomov et al., 1966) led to a general formula for OFI rates valid for any atom or ion with the orbital quantum number  $l$  and its projection  $m$  onto the quantization axis and charge state  $Z$ :

$$W(\omega_0, E) = \omega_{a.u.} \sqrt{6/\pi} |C_{n^*, l^*}|^2 f(l, m)(U_i / 2U_H) \times A_m(\omega_0, \gamma) (2E_0 / E \sqrt{1 + \gamma^2})^{2n^* - |m| - 3/2} \exp(-2E_0 g(\gamma) / 3E) \quad (6)$$

where  $U_H$  is the ionization potential of hydrogen,  $\omega_{a.u.}$  is defined by  $\gamma = 1$  from Eq. (5) for hydrogen or by  $\hbar \omega_{a.u.} = 2U_H$ :

$$\omega_{a.u.} = eE_H / \sqrt{2mU_H} \approx 4.1 \times 10^{16} \text{ s}^{-1} \quad (7)$$

$$E_H = e^5 m^2 / \hbar^4 (4\pi\epsilon_0)^3 \approx 5.14 \times 10^{11} \text{ V} / m \quad (8)$$

$$E_0 = E_H \times (U_i / U_H)^{3/2} \quad (9)$$

For a given atom, the dimensionless constant  $C_{n^*, l^*}$

$$|C_{n^*, l^*}|^2 = 2^{2n^*} / n^* \Gamma(n^* + l^* + 1) \Gamma(n^* - l^*) \quad (10)$$

is adapted from the formula well known for the hydrogen atom (Perelomov et al., 1966) by replacing the principal  $n$  and orbital  $l$  quantum numbers by their effective counterparts

$$n = Z(U_i / U_H)^{-1/2} \quad (11)$$

$$n^* = n - \delta l \quad (12)$$

$$l^* \approx n^* - 1 \quad (13)$$

respectively, and

$$\delta l = n - (U_i / U_H)^{-1/2} \quad (14)$$

is the quantum defect. Here  $\Gamma$  in Eq. (10) is the gamma function (Abramowitz & Stegun, 1972).

Other functions in Eq. (6) read as:

$$\begin{aligned} f(l, m) &= (2l + 1)!(l + |m|)! / 2^{|m|} (|m|)!(l - |m|)! \\ f(0, 0) &= 1 \end{aligned} \quad (15)$$

$$\begin{aligned} A_m(\omega_0, \gamma) &= 4\gamma^2 / \sqrt{3\pi} |m|! (1 + \gamma^2) \\ &\times \exp[-\alpha(k - v)] \Phi_m(\sqrt{\beta(k - v)}) \end{aligned} \quad (16)$$

$$\Phi_m(x) = x^{2|m|+1} / 2 \times \int_0^1 e^{-x^2 t} t^{|m|} / \sqrt{1 - t} dt \quad (17)$$

$$\beta(\gamma) = 2\gamma / \sqrt{1 + \gamma^2} \quad (18)$$

$$\alpha(\gamma) = 2[\sinh^{-1} \gamma - \gamma / \sqrt{1 + \gamma^2}] = \begin{cases} 2\gamma^3 / 3 & \text{when } \gamma \ll 1 \\ 2\log(2\gamma - 1) & \text{when } \gamma \gg 1 \end{cases} \quad (19)$$

$$\begin{aligned} \alpha(\gamma) &= 3 / 2\gamma \times [(1 + 1 / 2\gamma^2) \sinh^{-1} \gamma - \sqrt{1 + \gamma^2} / 2\gamma] \\ &= \begin{cases} 1 - \gamma^2 / 10 + 9\gamma^4 / 280 & \text{when } \gamma \ll 1 \\ 3 / 2\gamma \times (\log 2\gamma - 1 / 2) & \text{when } \gamma \gg 1 \end{cases} \end{aligned} \quad (20)$$

$$\begin{aligned} v &= U_i (1 + 1 / 2\gamma^2) / \hbar\omega_0 \\ v_0 &= U_i / \hbar\omega_0 \end{aligned} \quad (21)$$

Single ionization of atoms in the fundamental state with  $l = m = 0$ ,  $n^* = (U_i / U_H)^{-1/2}$  and  $|C_{n^*, l^*}|^2 = 2^{2n^*} / n^* \Gamma(2n^*)$  has explicit description for tunnel (ADK model) (Ammosov et al., 1986) and multiphoton limits.

When  $\gamma \ll 1$ , it is the tunnel ionization case where  $A_m(\omega_0, \gamma) \rightarrow 1$ , and we have

$$W(E) = \omega_{a.u.} \sqrt{6 / \pi} |C_{n^*, l^*}|^2 (U_i / 2U_H) (2E_0 / E)^{2n^* - 3/2} \exp(-2E_0 / 3E) \quad (22)$$

We can see from Eq. (22) that the probability of tunnel ionization is independent of the frequency of the wave.

When  $\gamma \gg 1$ , it is the multiphoton case, by taking into account only the term  $\kappa = K \equiv \text{mod}(v_0 + 1)$  in the series for  $A_m(\omega_0, \gamma)$ , and by using the relation  $v_0 = U_i / \hbar\omega_0 = E_0 / 2E\gamma$ , we have

$$\begin{aligned} W(\omega_0, E) &= \omega_{a.u.} (4^{2n^*} / \pi\sqrt{2}) |C_{n^*, l^*}|^2 (U_i / 2U_H) \\ &\times v_0^{2n^* + 2K - 3/2} e^{2K - v_0} \Phi_0(\sqrt{2(K - v_0)})(E / E_0)^{2K} \end{aligned} \quad (23)$$

We can rewrite Eq. (23) as

$$W(\omega_0, I) = \sigma_K I^K \quad (24)$$



where

$$W(\omega_0, E) = \omega_{a.u.} (4^{2n} / \pi\sqrt{2}) |C_{n,i}|^2 (U_i / 2U_H) \quad (25)$$

$$\times v_0^{2n+2K-3/2} e^{2K-v_0} \Phi_0(\sqrt{2(K-v_0)}) / I_0^K$$

$$I_0 = \varepsilon_0 n_0 c E_0^2 / 2 \quad (26)$$

where  $\varepsilon_0$  is the electric permittivity of free space,  $c$  is the speed of light in vacuum.

### 3. Simulation on gradient temperature (Song et al., 2008a; Song et al., 2008b)

#### 3.1 Model of simulation

In our simulation model, to simplify the calculation and hold the essential physical dynamic characteristics, we just only consider the fundamental mode (the spatial profile of which is not changing along propagation) of the coupled leaky modes propagating in the hollow fiber. We also neglect the interaction and energy transfer between the fundamental and high-order modes because the attenuation length of high-order modes is much smaller than that of the fundamental.

We use the standard nonlinear (1+1) dimension Schrödinger equation to simulate and analyze the evolution dynamic of the pulse propagation both in temporal and spectra domain. The nonlinear Schrödinger equation for the electric field envelope  $u(z, t)$  in a reference frame moving at the group velocity  $v_g$  takes the following form (assuming propagation along the  $z$  axis) (Agrawal, 2007):

$$\frac{\partial u}{\partial z} = -\frac{\alpha}{2} u + \frac{i\beta_2}{2} \frac{\partial^2 u}{\partial T^2} + i\gamma[|u|^2 u + \frac{i}{\omega_0} \frac{\partial}{\partial T} (|u|^2 u) - T_R u \frac{\partial |u|^2}{\partial T}] \quad (27)$$

The terms on the right hand side of the equation are the loss, second order dispersion, self-phase modulation, self-steepening and Raman scattering, respectively. Here  $c$  is the speed of light in vacuum,  $\omega_0$  the central angle frequency,  $\alpha$  the loss,  $\beta_2$  the GVD (group velocity dispersion) and  $T_R$  is related to the slope of the Raman gain spectrum. The nonlinear coefficient  $\gamma = n_2 \omega_0 / c A_{\text{eff}}$  where  $n_2$  is the nonlinear refractive index and  $A_{\text{eff}}$  the effective cross section area of the hollow fiber. Equation (27) and the parameters in the equation characterize propagation of the fundamental mode.

The initial envelop of the pulse is in the following form (Tempea & Brabec, 1998; Courtois et al., 2001), which is a simplification expression of Eq. (4):

$$u(0, t) = \sqrt{\frac{2P_{\text{in}}}{\pi w_0^2}} \exp\left(-\frac{t^2}{t_0^2}\right) \quad (28)$$

here  $P_{\text{in}}$  is the peak power of the incident pulse,  $w_0$  the spot size (for  $1/e^2$  intensity) of the fundamental beam (we assume that the beam focused on the entrance section of the hollow fiber matches the radius of the fundamental mode in our calculation mode),  $t_0$  the half temporal width at the  $1/e^2$  points of the pulse intensity distribution.

Equations (27) and (28) can be solved by the split-step Fourier method (Agrawal, 2007) in which the propagation is broken into consecutive steps of linear and nonlinear parts. The

linear part including loss and dispersion can be calculated in the spectrum domain by Fourier transform, while the nonlinear part which includes other terms on the right hand of Eq. (27) was solved in the time domain by Runge-Kutta method. The convergence of the solution can be easily checked by halving the step size to see if the calculation results are nearly unchanged.

Although the studies of filamentation in many gases have been focused by scientists and technologists (Akturk et al., 2007; Fuji et al., 2007; Dreiskemper & Botticher, 1995), argon (Ar) is the most frequency used gas for generation of ultrashort intense femtosecond pulses. In simulation in this chapter, we employ Ar as the medium to reveal the essence of gradient temperature technology.

The loss and waveguide dispersion relations of the hollow fiber can be expressed as (Marcatili & Schmeltzer, 1964):

$$\frac{\alpha}{2} = \left( \frac{2.405}{2\pi} \right)^2 \frac{\lambda^2}{2a^3} \frac{v^2 + 1}{(v^2 - 1)^{1/2}} \quad (29)$$

$$\beta_{\text{waveguide}} = \frac{2\pi}{\lambda} \left[ 1 - \frac{1}{2} \left( \frac{2.405\lambda}{2\pi a} \right)^2 \right] \quad (30)$$

where  $v$  is the refractive index ratio between the material of the hollow fiber (glass in our case) and the inner gas (argon in our case),  $\lambda = \lambda_0/n$ , the wavelength in the medium ( $\lambda_0$  the wavelength in vacuum),  $a$  the bore radius of the hollow fiber. The propagation constant  $\beta$  including contributions from both waveguide part (Eq. (30)) and material part:

$$\beta_{\text{material}} = \frac{\omega}{c} n \quad (31)$$

The relation between propagation constant  $\beta$  and  $m$  order dispersion coefficient  $\beta_m$  is:

$$\beta_m = \left( \frac{d^m \beta}{d\omega_m} \right)_{\omega=\omega_0} \quad (32)$$

For gases, the refractive index is a function of both temperature and pressure (Lehmeier, 1985):

$$n = \left( 2 \frac{n_0^2 - 1}{n_0^2 + 2} \frac{pT_0}{p_0T} + 1 \right)^{1/2} \left( 1 - \frac{n_0^2 - 1}{n_0^2 + 2} \frac{pT_0}{p_0T} \right)^{-1/2} \quad (33)$$

For argon, at the standard condition ( $T=273.15\text{K}$ ,  $p=1\text{atm}$ ), we have (Dalgarno & Kingston, 1960):

$$n_0^2 - 1 = 5.547 \times 10^{-4} \left( 1 + \frac{5.15 \times 10^5}{\lambda_0^2} + \frac{4.19 \times 10^{11}}{\lambda_0^4} + \frac{4.09 \times 10^{17}}{\lambda_0^6} + \frac{4.32 \times 10^{23}}{\lambda_0^8} \right) \quad (34)$$

In the above equations,  $p$  is the pressure,  $p_0$  the pressure at normal conditions (1 atm),  $T$  the temperature,  $T_0$  the temperature at normal conditions (273.15 K),  $n$  the refractive index of



the medium, and  $n_0$  the refractive index of the medium at normal conditions ( $T=273.15$  K,  $p=1$  atm). In Eq. (34), the unit of  $\lambda_0$  is  $\text{\AA}$  ( $10^{-10}$  m).

Before we do the simulations of the evolution of the pulse under gradient temperature, we first check the effect of the temperature on the hollow fiber and the medium (Ar as in our case) qualities such as loss, refractive index, etc. Figures 2 and 3 show the loss and refractive index as a function of the temperature. They all keep nearly constant during the interval from 300 K to 600 K. We can conclude that compared with room temperature, higher temperature does not introduce extra attenuation during the pulse propagation.

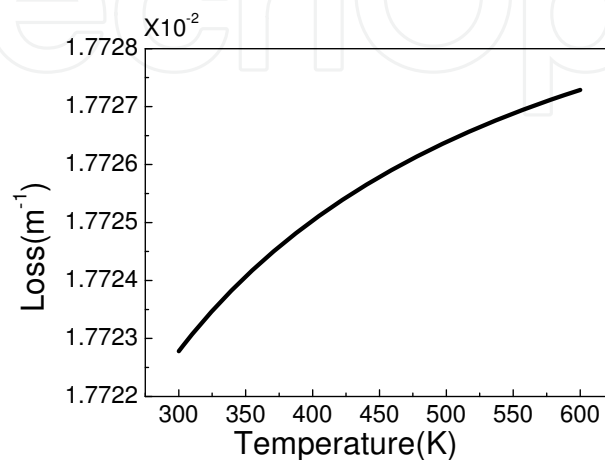


Fig. 2. Loss as a function of temperature for Ar in hollow fiber (bore diameter 500  $\mu\text{m}$ , pressure 1 atm).

To simplify and catch the essence physics process, we define a factor  $TF$  which represents the gas gradient temperature factor through the ideal gas equation:  $TF = pT_0/p_0T$ . It is obvious to see that the factor  $TF$  is proportional to the gas density (proportional to the gas pressure while inversely proportional to the gas temperature). When the gas pressure is 1 atm, the gradient factor  $TF$  is 1 for 300 K, and 0.5 for 600 K.

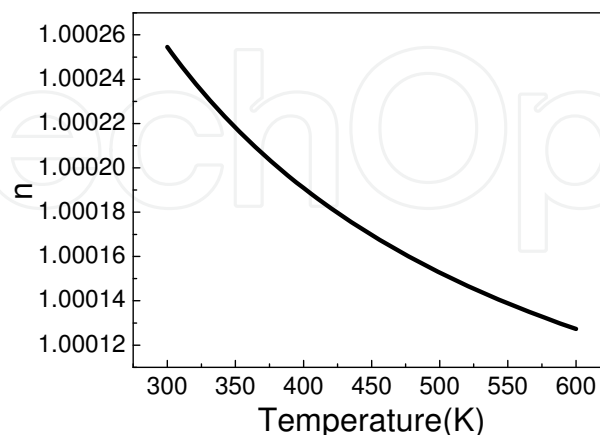


Fig. 3. Refractive index as a function of temperature for Ar at 1 atm.

The nonlinear refractive index and GVD are both proportional to the factor  $TF$  (Mlejnek et al., 1998):

$$n_2 = 4.9 \times 10^{-23} \times TF(\text{m}^2/\text{W}) \quad (35)$$

$$\beta_2 = 2.6 \times 10^{-29} \times TF(\text{s}^2/\text{m}) \quad (36)$$

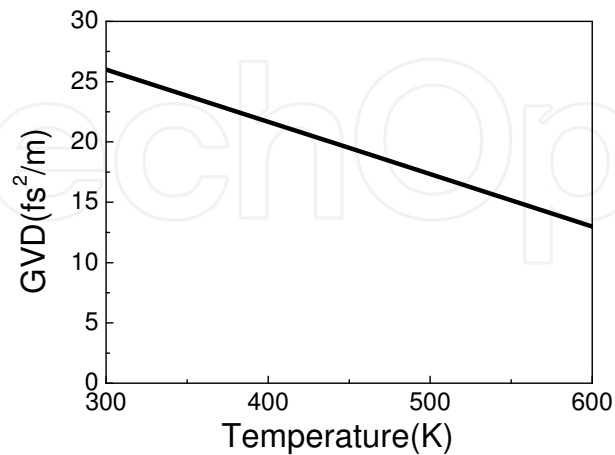


Fig. 4. GVD as a function of temperature (bore diameter 500  $\mu\text{m}$ , pressure 1 atm).

Now we can calculate the GVD and nonlinear refractive index by Eqs. (30)-(36). The results are shown in Figs. 4 and 5. As we can see from these figures, a higher temperature at 600 K decreases both the GVD and nonlinear refractive index  $n_2$  by a factor of 2 for the room temperature 300 K. The decreasing GVD gives the pulse a chance to slow down the pulse broadening in time domain; while the decreasing nonlinear refractive index increases the critical power for self-focusing  $P_c$  (see Eq. (1)). Therefore, at a higher temperature, the pulse broadening in time domain slows down and  $P_c$  is higher. If the tube is sealed and is locally heated at the entrance, and cooled at the exit end, the gas temperature gradient will be formed along the tube and so will the nonlinear refractive index.  $P_c$  at the hot side of the tube (entrance) will be higher than the cold end (exit end), like in the case of gradient pressure (see Fig. 1).

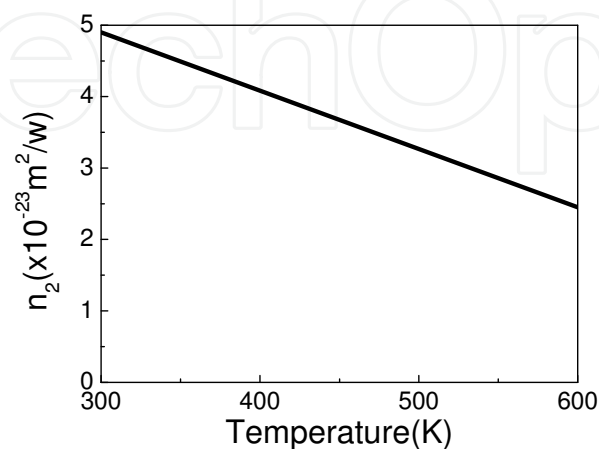


Fig. 5. Nonlinear refractive index as a function of temperature (pressure 1 atm).

### 3.2 Spectrum broadening

As the incident pulse propagating along the hollow fiber filled with argon, the peak power of the pulse is continuously decreasing due to the dispersion and loss. However, the decreasing temperature along the fiber provides a gradually increasing nonlinear coefficient which partly compensates the decreasing peak power, the spectrum broadening can go on till the end of the tube. For the argon gas at atmospheric pressure and temperature of 600 K,  $P_c$  is 4.2 GW; while for the room temperature, 300 K, it is 2.1 GW, i.e. the critical power for 600 K is twice of that for 300 K. This means that the energy of the incident pulse will be allowed twice higher as that of the pulse under room temperature for the same pulse width. We did the simulation on the spectrum broadening for the uniform and gradient temperature cases in the hollow fiber. The bore diameter of the hollow fiber was 500  $\mu\text{m}$  and the length of the fiber was 60 cm. The temperature conditions are: condition 1: uniform room temperature ( $T = 300$  K); condition 2: temperature linearly decreasing from 600 K to 300 K along the hollow fiber; condition 3: temperature linearly decreases from 600 K to 300 K in the first half and increases from 300 K to 600 K in the second half of the fiber, i.e., the triangle temperature. The incident peak power of the pulses was set to be  $2P_c$  and the pressure was 0.2 atm, thus, for a 30 fs pulse, the incident pulse energy should be 0.6 mJ and 1.2 mJ, for room temperature 300 K (uniform case) and 600 K (gradient temperature case), respectively.

By solving Eq. (27) coupled with the initial condition in Eq. (28), we obtained the spectra and phases of the output pulses under the above three conditions, which are shown in Figs. 6 and 7. It is obvious that the output spectrum bandwidth of the pulse increases from 250 nm (about 675 nm to 925 nm, uniform temperature case) to 350 nm (about 625 nm to 975 nm, linear and triangle gradient temperature case). However, the triangle shaped gradient temperature does not seem to make visible difference from the linear gradient temperature case. We also plot the spectrum evolution of the triangle shaped temperature in Fig. 7(b). We can see that the spectrum starts to expand at about 20 cm and the profile collapses along the fiber. We will discuss on the spectrum broadening quantitatively in the following subsection.

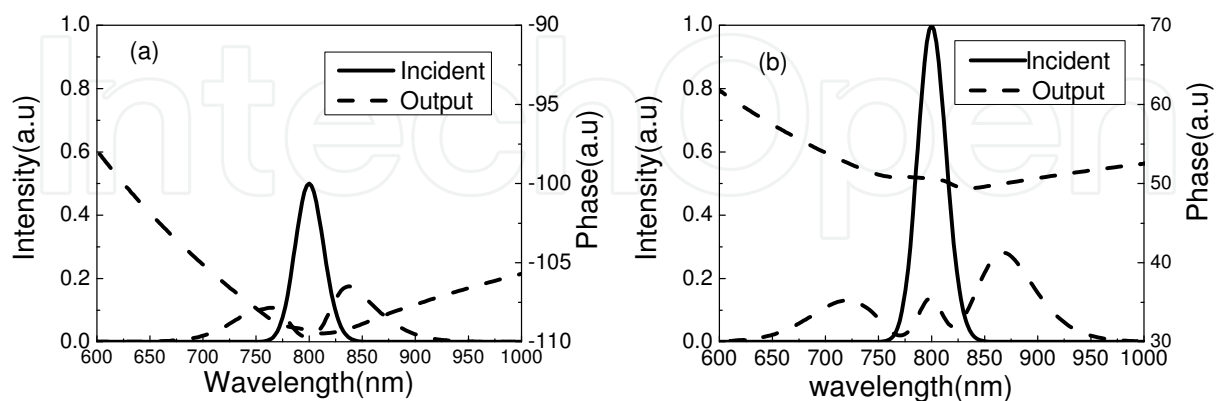


Fig. 6. Spectrum & phase for (a) uniform temperature (300 K), (b) linear gradient temperature (600 K to 300 K) and. Other conditions: bore diameter of the hollow fiber: 500  $\mu\text{m}$ , fiber length: 60 cm, filled argon gas pressure: 0.2 atm, incident pulse width: 30 fs, pulse energy: 0.63 mJ for the uniform case and 1.26 mJ for the gradient case.

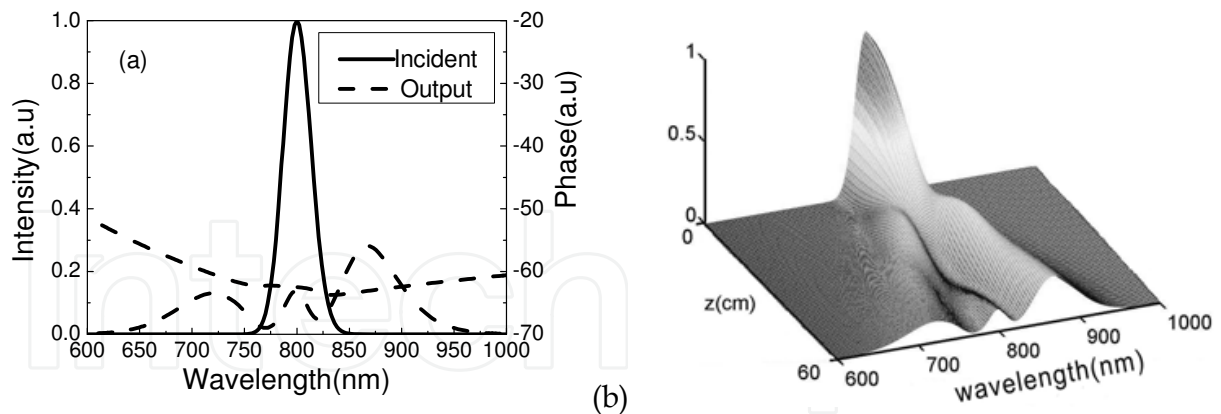


Fig. 7. (a) Spectrum & phase (b) Spectra evolution for triangle gradient temperature (600 K to 300 K to 600 K). Other conditions: bore diameter of the hollow fiber: 500  $\mu\text{m}$ , fiber length: 60 cm, argon gas pressure: 0.2 atm, incident pulse width: 30 fs, pulse energy: 1.26 mJ.

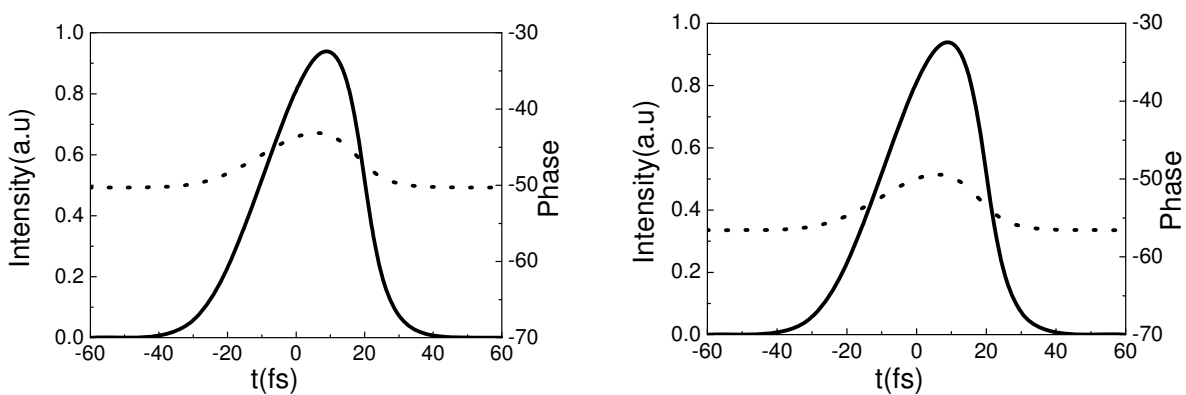


Fig. 8. Pulse profiles & phases for the (a) linear gradient and (b) triangle gradient temperature in Fig. 6 (b) and 7 (a).

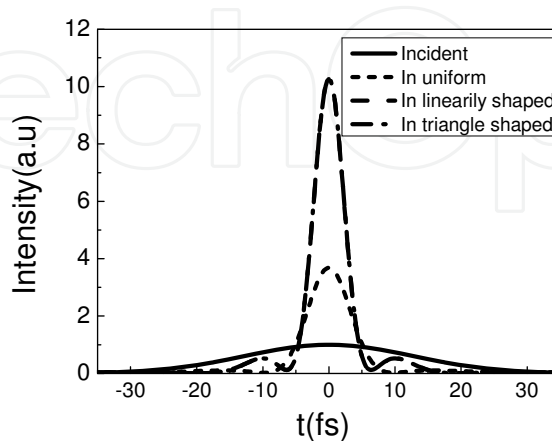


Fig. 9. Pulses profiles after ideal compression (spectra are shown in Figs. 6 and 7(a) respectively).

The output pulse profiles and phases of the linear and triangle gradient temperature are shown in Figs. 8(a) and 8(b) respectively. Still, we cannot see much difference between the linear and triangle cases for the output pulse. The transform limited pulse after ideal compression for the three conditions are shown in Fig. 9. The pulse width after ideal compression is 5 fs in the gradient temperature case (both linear and triangle gradient cases), which is 2/3 of pulse width in the uniform temperature case (7.5 fs). In addition, the pulse energy we can obtain in the gradient temperature scheme is twice higher as that in the uniform temperature scheme.

### 3.3 Discussions on spectrum broadening

When a pulse propagates through a Kerr medium whose length is  $L$ , the spectrum broadening  $S_p$  of the pulse is approximately determined by the integral below (Agrawal, 2007):

$$S_p = \int_0^L n_2(z)P(z)dz \quad (37)$$

where  $n_2(z)$  is the nonlinear refractive index at position  $z$ ,  $P(z)$  the peak power of the pulse at position  $z$ . We use Eq. (37) to discuss the spectrum broadening comparing with the simulation we did in the above subsection.

First, this integral can approximately determinate the spectrum broadening quantitatively. If we take  $n_2(z)P(z)$  as a variable and set it equal everywhere along the medium, the nonlinear Schrödinger equation (Eq. (27)) is actually the same in every  $z$  of the medium. The result is that the final pulse temporal and spectral profiles (normalized with themselves) are the same, which means that they are only different with intensity.

Second, from the integral we can see that the spectrum broadening will not be much broader in the gradient temperature case than that in the uniform case. But from the energy point, we can see that the incident energy will be allowed twice higher than uniform temperature. This is a big priority of gradient temperature. Our intention is to achieve not only ultrashort but also intense pulses. The energy is also a main final object which we focus on.

Third, from the integral in Eq. (32) we can deduce that the spectrum broadening in triangle gradient will be almost the same as that in the linear gradient case. This is true and can be verified by our simulation results (see Figs. 6 (b) and 7 (a)). In fact, the difference of linear and triangle gradient scheme excluding real experimental conditions in simulation is small. Their different effects can be seen from experiments more obviously. Triangle gradient scheme's priority is that this design gives even better pulse compression, avoids cyclic compression stages, and therefore limits the energy loss as shown in Ref (Couairon et al., 2005). From ideal theoretical point, these two schemes have almost the same ability of spectrum broadening. From the experimental point, triangle scheme has priority to linear project and it is a little more complex. Although this experimental conclusion is obtained from gradient pressure scheme, we can expect the same results in gradient temperature case.

### 3.4 Ideal gradient line shape

In the above simulation, we set the input pulse peak power related to the critical self-focusing power  $P_c$ . Inversely, we can derive an ideal gradient shape for a giving pulse, which means that at every step of evolution, we change the temperature so as to make the

pulse's peak power equals to the critical power of self-focusing. Figure 10 shows the ideal gradient shape for a 30 fs, 0.1 mJ incident pulse. The  $TF$  differential increases along the fiber, which implies that the peak power of the pulse along the tube drops faster and faster during the evolution. If we can realize such a gradient temperature, we can avoid multi-filament formation everywhere along the tube. In fact, in the linear gradient shape case, a moderately increasing the length of the tube (corresponding to decreasing the slope of the linear line) or decreasing the peak power of the input pulse will avoid the self-focusing or filament formation everywhere along the tube and the result of the spectrum broadening is still much broader than the uniform temperature case.

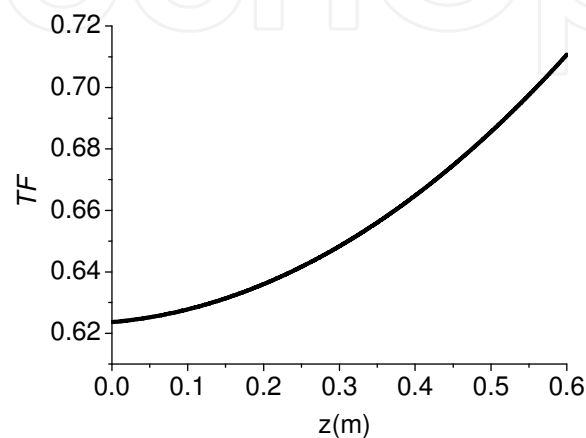


Fig. 10. Ideal gradient shape for 0.1mJ.

#### 4. Experimental results (Cao et al., 2009)

As we mentioned in the introduction, spectrum broadening through filamentation was one of the most extremely simple and robust techniques to generate intense few to monocycle pulses with less sensitivity to the experiment conditions. In real experiments, an aperture (Cook et al., 2005), rotating lens, anamorphic prisms, circular spatial phase mask (Pfeifer et al., 2006), periodic amplitude modulation of the transverse beam profile (Kandidov et al., 2005), introducing beam astigmatism (Fibich et al., 2004) or incident beam ellipticity (Dubietis et al., 2004) in the laser beam prior to focusing have been used to stabilize the pointing fluctuations of a single filament. In the previous section, we show the priority of the gradient temperature scheme by theoretical simulation. In this section, we will verify the robustness of this scheme by showing the experimental results.

We show our experimental setup in Fig. 11. The laser pulse was produced from a set of conventional chirped pulse amplification (CPA) Ti: sapphire laser system. This laser system produced linearly polarized pulses of 37 fs pulse at the central wavelength of 805 nm. The energy of the pulses was 2 mJ and the repetition rate was 1 kHz. The beam diameter of the pulses was 10 mm (at  $1/e^2$  of the peak intensity). In this experiment, four silver mirrors were used to couple the amplified pulses into the sealed silica tube, where M1, M2 and M3 were the plane mirrors and FM1 was a concave mirror with a 1.7 m radius of curvature. A hard aperture A1 as an attenuator and a beam profile shaper was inserted in front of the concave mirror FM1. The output pulse was focused by a concave mirror, FM2, into a pulse compression system consisting of two negative dispersion mirrors, CM1 and CM2. The negative dispersion mirrors were rectangles of size  $10 \times 30 \text{ mm}^2$ . Each reflection contributed



a GDD of  $50 \text{ fs}^2$  within wavelength area of  $680\sim 1100 \text{ nm}$ . The pulse after compression was reflected by plane mirrors, M4 and M5, then through a beam split mirror, BS1, into SPIDER. The Ar gas filled in the tube was controlled and monitored to be below the maximum pressure of 3 atm, because a higher gas pressure may blow up the windows of the tube. The focal point in the tube was measured as 47 cm from the input window. The spot size of the focused pulse was  $100 \mu\text{m}$ . To make a temperature gradient along the propagation of the pulse, a 20 cm heating length furnace was used to heat the tube. The 100 cm long high-temperature and high-gas-pressure resistance silica tube with the inner diameter of 25 mm was sealed off with two 1-mm thick fused silica Brewster windows. The tube was inserted into the transverse center of the furnace. Two ends of the tube were cooled by air. To avoid the expansion of the tube and make the furnace easy to move along the tube, between the external side of the tube and the internal side of the furnace, there was a 2 mm wide gap. The temperature of the furnace was controlled by a temperature controller between  $25 \text{ }^\circ\text{C}$  and  $500 \text{ }^\circ\text{C}$  with a  $\pm 5 \text{ }^\circ\text{C}$  precision. It should be noted that the temperature we mention in the following text in this section is the temperature at the longitude center of the furnace. With this configuration, the temperature at the heating point could be increased from  $25^\circ\text{C}$  to  $500^\circ\text{C}$  within 35 minutes. The above experimental setup is the same as that was used in broadening the spectrum through filamentation, expecting for the additional furnace. Therefore, an additional furnace and temperature controller are sufficiently easy to modify the traditional filamentation setup to our experimental setup.

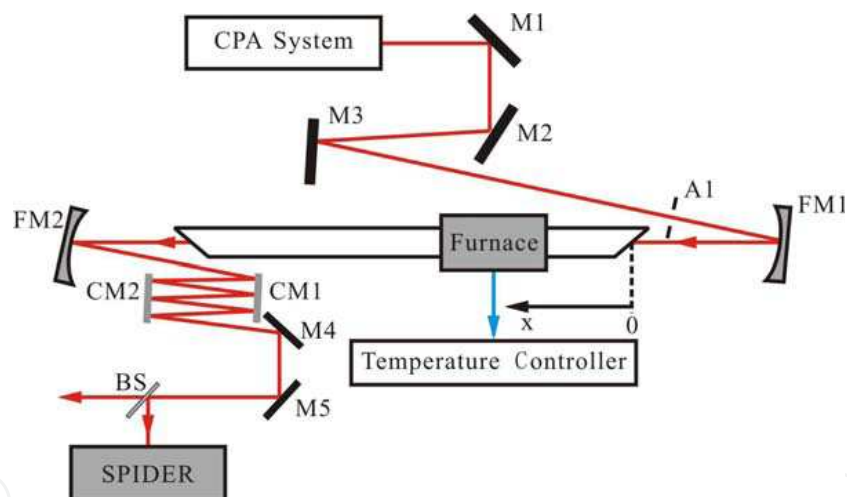


Fig. 11. The schematic of the experimental setup

To know the actual temperature distribution inside the tube, we inserted a thermistor and moved it along the tube to measure the temperature. The measured temperature distribution at a maximum central temperature of  $500^\circ\text{C}$  is shown in Fig. 12. The temperature rapidly drops down to the room temperature outside the furnace, so that the temperature distribution is of a triangular shape, with the temperature gradient of about  $2403 \text{ }^\circ\text{C}/\text{m}$ . According to our simulation results and discussions in the former section, the priority of the triangle gradient is that it gives an even better pulse compression, avoids cyclic compression stages, and limits the energy loss. As the temperature is distributed along the tube, there should be a gas flowing from the hot to the cool position. However, in the experiment, the temperature variation was a very slow process. We did not observe the instability caused by the gas turbulence. In general, the radial thermal distribution could

also cause thermal lensing effect. In our case, because the inner tube diameter was only 25 mm, the radial temperature difference between the wall and the center was measured to be only 2–3 °C, so that the thermal lensing effect could be neglected.

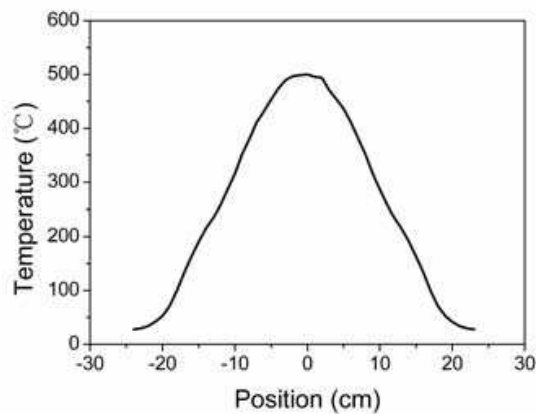


Fig. 12. Temperature distribution along the tube when the temperature at the furnace central (zero point at  $x$ -axis) is 500 °C.

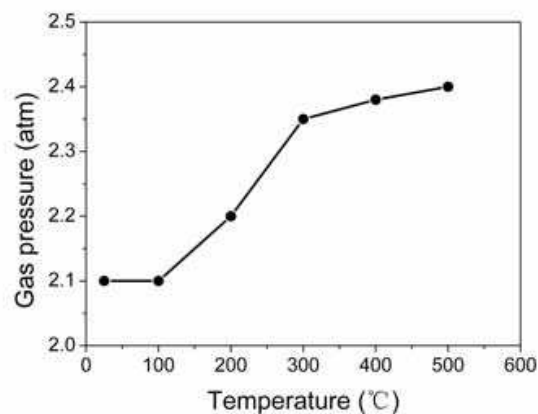


Fig. 13. Measured gas pressure as a function of the heated temperatures when the initial gas pressure is 2.1 atm

As for the sealed tube, the gas pressure in total should be uniform and increase with the temperature. The measured gas pressure as a function of the heated temperatures when the initial gas pressure is 2.1 atm is shown in Fig. 13. Generally speaking, the influence of the pressure and temperature should be separately examined. However, since we just wanted to investigate the filamentation process in a sealed tube with the change of the temperature, we did not attempt to separate the temperature and pressure effects in our experiment. Moreover, the pressure change within 100 °C was only a few percent. This small change does not introduce noticeable difference in the material parameters for argon gas such as GVD,  $n_2$ , and the average electron collision time.

#### 4.1 Filament controll and spectrum broadening by gradient temperature

To check the influence of the temperature, we changed the local temperature in the tube and measured the beam pattern and the broadened spectrum. The beam pattern was taken by an

ordinary digital camera looking at the surface of a white paper positioned at the plane orthogonal to the beam path and 3 m away from the exit window of the tube and the broadened spectrum was measured by a spectrometer (Ocean Optics, SD2000). When the furnace was turned off, the temperature was kept at room temperature 25 °C inside the tube, and the gas density was uniform along the tube. Pulses with energy of 1.2 mJ (32.4 GW peak power, about 6.5 times higher than the critical power at 2.1 atm) after the aperture A1 were coupled into the tube, and output pulse energy of the pulses was 1.1 mJ. A single filament began to appear at 3 cm before the focal point and the filament was about 40 cm long at 1.7 atm. By increasing the gas pressure to above 2.1 atm, the single filament broke into multiple filaments, as is shown in Fig. 14(a). The inserted picture is the output beam profile of the multi-filament in the far field, where three filament spots can be identified. The interactions among multi-filament result in shot-to-shot fluctuations in the filamentation pattern. As the temperature was increased to 200 °C, the gas pressure in the tube was increased to 2.2 atm, a little higher than that at 25 °C (see Fig. 13). Although the heated gas will flow to the cool end and be kept at the same temperature in a long term, the gas temperature of the exit end of the tube was found still 25 °C. When the furnace was increased to 200 °C, the multi-filament turned to become a single filament, as shown in Fig. 14(b). There was only one single filament that has a good beam profile. Further increasing the temperature to 300 °C or higher, the single filament collapsed and disappeared, as shown in Fig. 14(c). Although the gas pressure was also increased at the same time, the higher gas pressure was caused by the accelerated activity of the gas atoms, but not because of the increase of the number of the gas atoms. Gas atoms moved from the position of higher temperature to that of lower temperature, which resulted in that the gas density was lower at the entrance and higher at the end of the filament. Higher self-focusing critical power  $P_c$  induced by the higher gas



Fig. 14. Filament pattern at temperature of (a) 25 °C; (b) 200 °C; (c) 300 °C; (d) 25 °C. The inserted pattern in every picture is the output beam profile.

density was effective to avoid the occurrence of the multi or even single filamentation. Inversely, by decreasing the temperature from 300 °C to the initial room temperature 25 °C, multi-filament appeared gradually, which is shown in Fig. 14(d). It was almost the same as in the initial state (Fig. 14(a)) of our experiment.

At the temperate of 25 °C and input pulse energy of 1.2 mJ, we measured the output spectra at different gas pressure. The results are shown in Fig. 15. The output spectra toward the short wavelength became wider with the increase of gas pressure, which resulted from the increase of the number of the filled gas atoms. At the gas pressure of 2.1 atm, multi-filament was formed in the gas-filled tube.

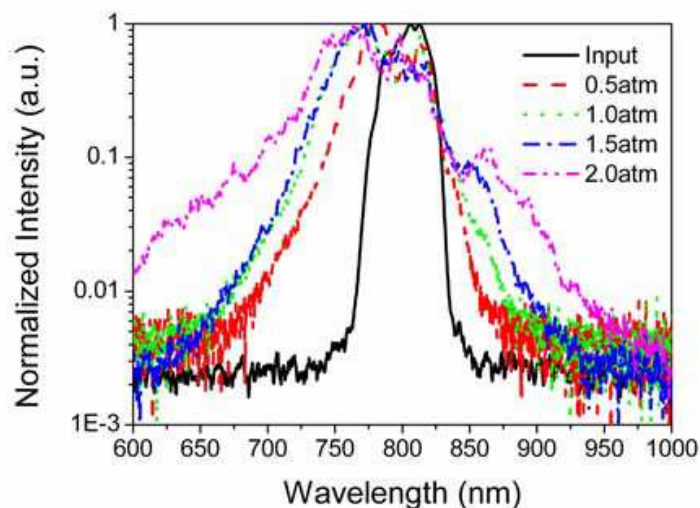


Fig. 15. Spectra at different gas pressures with the input pulse energy of 1.2 mJ and the heated temperature of 25 °C

Fig. 16 shows the evolution of output spectra at different temperatures of the entrance of the filament, when the gas pressure was 2.1 atm and incident pulse energy was 1.2 mJ. It can be seen that the spectral width was broadened to about twice as that of the incident spectrum. For a single filament at 200 °C, the spectrum broadening is due to an increasing phase contribution from ionization-induced spectrum broadening and interaction with the plasma. Whereas, in the case of non-filament at above 300 °C, the spectrum broadening is due to the dominant self-phase modulation (SPM) rooted from  $n_2$ , which becomes weak with the increase of the temperature. The further increasing of the temperature results only in a narrower broadened spectrum. When the filament disappears at high temperature, it means that the self-focusing critical power is high.

Therefore, we can increase the input pulse energy up to the new self-focusing critical power. The final results are shown in Fig. 17. At the temperature of 25 °C and incident pulse energy of 1.2 mJ, filament was formed at 2.1 atm, shown as the point A in Fig. 17. Then, when the temperature at the entrance of the filament was increased to 300 °C, the filament disappeared, shown as the point B in Fig. 17. After increasing the pulse energy from 1.2 mJ to 1.54 mJ at 300 °C, the filament appeared again, shown as the point C in Fig. 17. After increasing the temperature from 300 °C to 400 °C at 1.54 mJ, the filament disappeared again, shown as the point D in Fig. 17. It indicates that the filament can appear or disappear by increasing the temperature and input pulse energy in turn. Meanwhile, if the temperature

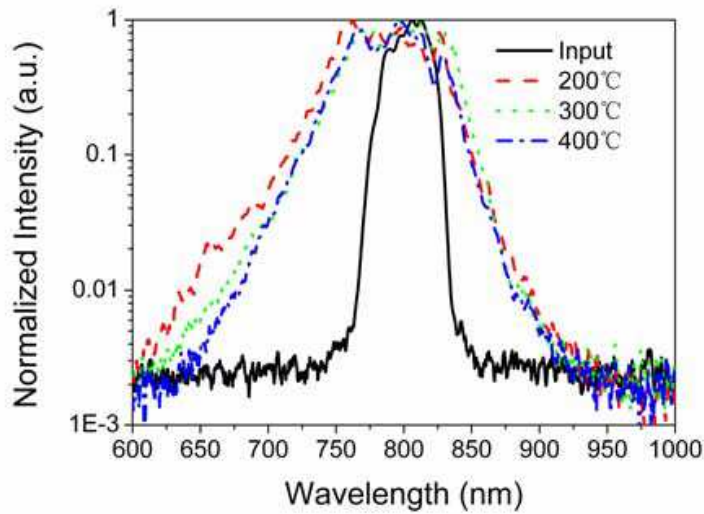


Fig. 16. Spectra at different temperatures with the input pulse energy of 1.2 mJ and the initial gas pressure of 2.1 atm

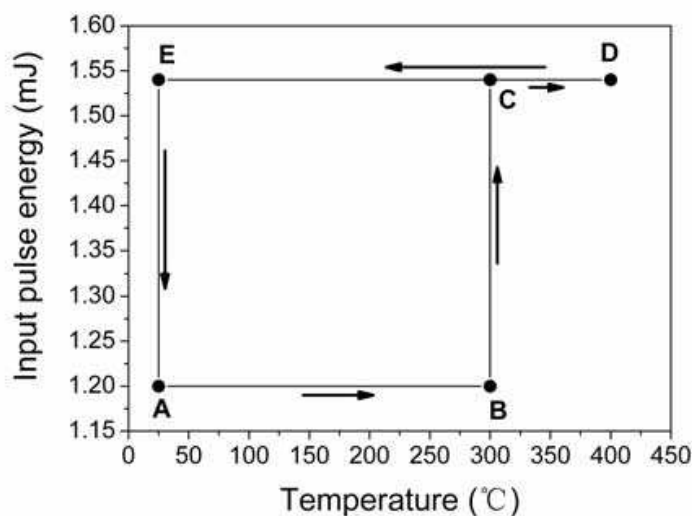


Fig. 17. The cycle between filament and no-filament by changing the temperature and input pulse energy in turn. Filament appears at points A, C, and E and disappears at points B and D.

was decreased to 25 °C at the incident pulse energy of 1.54 mJ, the filament also appeared, shown as the point E in Fig. 17, and further when the pulse energy was decreased to 1.20 mJ, the filament was the same as in the initial state. The above experimental results indicate that the filament can be controlled by adjusting the local self-focusing critical power by the temperature, although the broadened spectrum narrows with the increase of the temperature. More incident pulse energy can be allowed in the tube at the higher local temperature. The presented method is simple and feasible to operate with only a heating furnace, without continuing consumption of expensive gases comparing with the gradient pressure scheme.



#### 4.2 Self compression in temperature controlled filamentation

The filamentation of intense femtosecond laser pulses will lead to a remarkable pulse self-compression. The filamentation of ultrashort laser pulses is a balance between the beam self-focusing by the optical Kerr effect, beam defocusing due to the plasma, pulse self-steepening, and beam diffraction. The propagating pulse suffers significant reshaping in both time and space domain. This reshaping process will lead to the self compression of the intense femtosecond pulse. In this part, we investigate the self compression of the femtosecond pulse propagation in temperature controlled filamentation. We start from a 0.7 mJ incident pulse with 25 °C and 2 atm. In this condition, it could only form a very short filament at the focal point. The output pulse reduced from 35 fs to 23.5 fs due to self compression, with a Fourier transform limit of 16 fs (see Fig. 18).

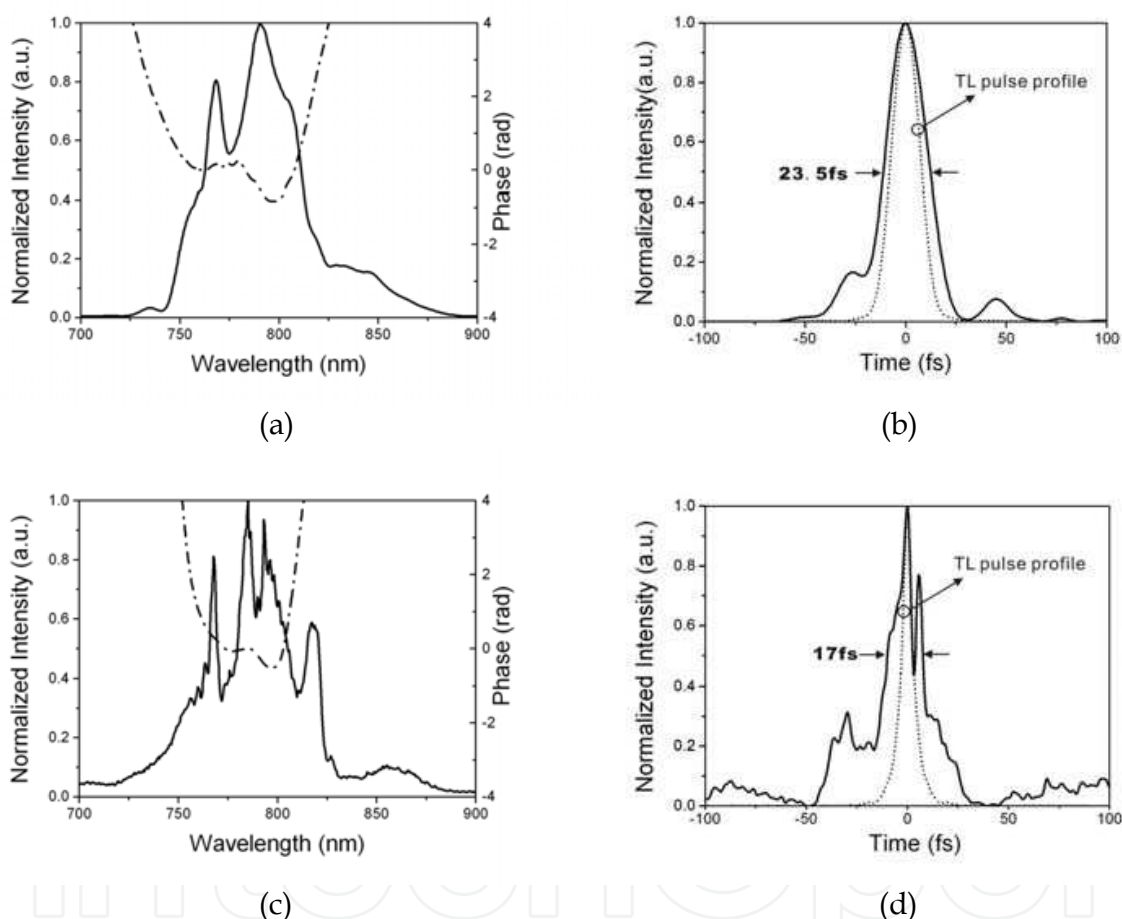


Fig. 18. The spectra and phases of (a) 0.7 mJ, (c) 0.8 mJ incident pulse at 25 °C. Pulse profiles after self compression and Fourier transform limit corresponding to (a) and (c) are shown in (b) and (d) respectively.

When the energy of incident pulse was 0.8 mJ, the pulse further reduced to 17 fs, with a Fourier transform limit of 5.5 fs. As the energy of input pulse was increased to 1.3 mJ, filament in the tube split to multifilaments at 5 cm after focal point, and the spots split and converged rapidly evidenced by far field observation. The transform of multifilaments to single filament can be controlled by temperature. We could observe remarkable multifilaments with pulse energy up to 1.7 mJ. When the temperature of heat center reached



170°C, multifilaments converged to single filament and at this temperature, multifilaments will reoccur if pulse energy increases to 2.7 mJ. When the temperature of heat center was 400°C, multifilaments shrunk to single filament again. We increased the temperature to 450°C, filamentation was not obvious and the pulse is self compressed to 19 fs with a Fourier transform limit of 14.5 fs (see Fig. 19). Filament disappeared as the temperature increases to 500 °C. The width of output pulse reduced to 24.5 fs and its transform limited pulse is 15 fs (see Fig. 19). The energy of the self compressed pulse increased by nearly 2 mJ compared to the case of 0.8 mJ (Fig. 19).

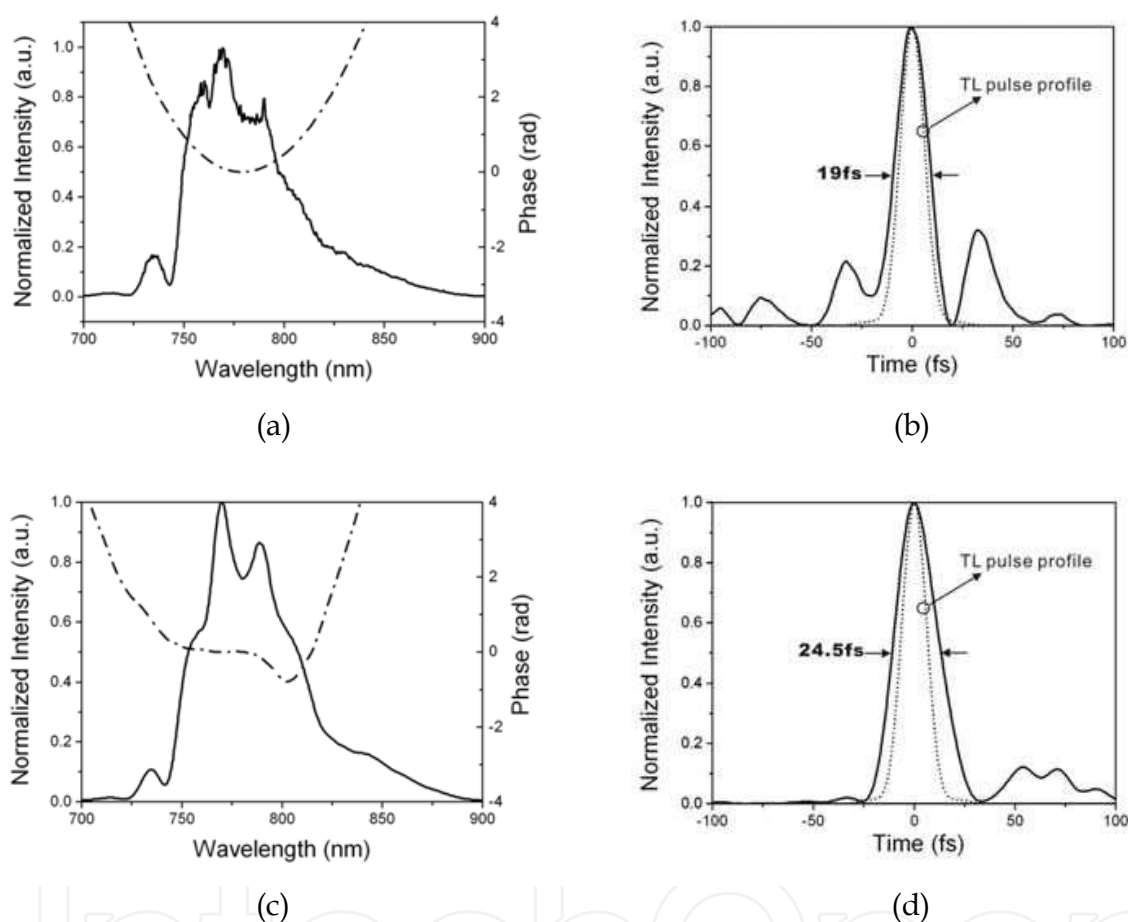


Fig. 19. The spectra and phases of (a) 450°C, (c) 500°C with 2.7 mJ incident pulse. Pulse profiles after self compression and Fourier transform limit corresponding to (a) and (c) are shown in (b) and (d) respectively.

Single filament reoccured when the energy of incident pulse increased to 5.7 mJ, and the width of output pulse was 69 fs. Compared with multifilaments before heating, the pulse energy of self compression was increased nearly 4 mJ by heating the gas to 500 °C with overcoming the emergence of multifilaments.

We can define the self-compression ratio,  $S$ , as the ratio between the width of Fourier transform limit and that of self compression pulse which exhibits the condition of self compression without any dispersion compensation.  $S = 1$  is the ideal value (see table 1). Preliminary analysis shows that at the same temperature, high energy promotes self compression, but the self compression rate for high energy is low, which can approach the

ideal value after dispersion compensation. For the same energy, self compression rate differs slightly at different gradient temperature, which is higher at lower temperature.

Temperature (°C)	Pulse Energy (mJ)	Measured pulse width (fs)	Transform limited pulse width (fs)	S
25 (No Gradient)	0.7	23.5	16	0.6809
25 (No Gradient)	0.8	17	5.5	0.3235
450 (Gradient)	2.7	19	14.5	0.7632
500 (Gradient)	2.7	24.5	15	0.6122

Table 1. Self compression rate S at different energy and temperatre schemes.

#### 4.3 Pulse compression with dispersion compensation by chirp mirror after temperature controlled filamentation

To obtain intense ultrashort pulse, dispersion compensation is need after the filamentation. We started from a 2.4 mJ incident pulse under 25 °C and 2 atm condition, and we observed multifilaments. The width of spectrum was broaden 3 times of that of the incident pulse, and the transform limited pulse was 6 fs. The pulse compression was difficult under this condition because of the strong fluctuation caused by multifilaments. When we increased the temperature to 380 °C, the pressure in the tube was about 2.3 atm, and multifilaments gradually shrunk to a 35 cm long single filament, starting at 3 cm before the focal point. Figure 20 shows the narrowing of the pulse width due to high temperature.

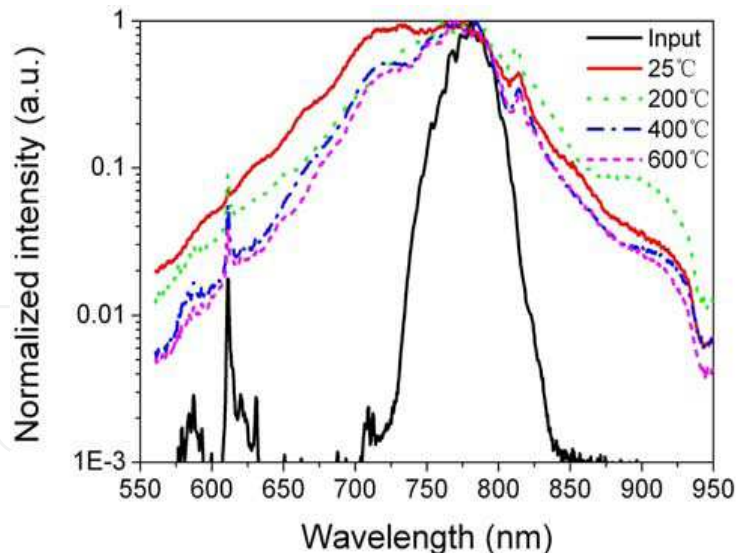


Fig. 20. Spectra of a 2.4 mJ incident pulse at 2 atm at different temperature.

In Fig. 21, we show the phases and spectrum of the pulse reflected by the chirp mirror for 6 and 8 bounces, measured by a SPIDER. We can see that after 3 bounces between the chirp mirror, the spectrum is not flat. While after 4 bounces, the spectrum becomes flat and the GDD turns from positive to negative. We can get a 1.6 mJ, 15 fs output pulse compared with 8 fs of transform limited,. Certainly the dispersion compensation is not complete and finely compensation is needed.

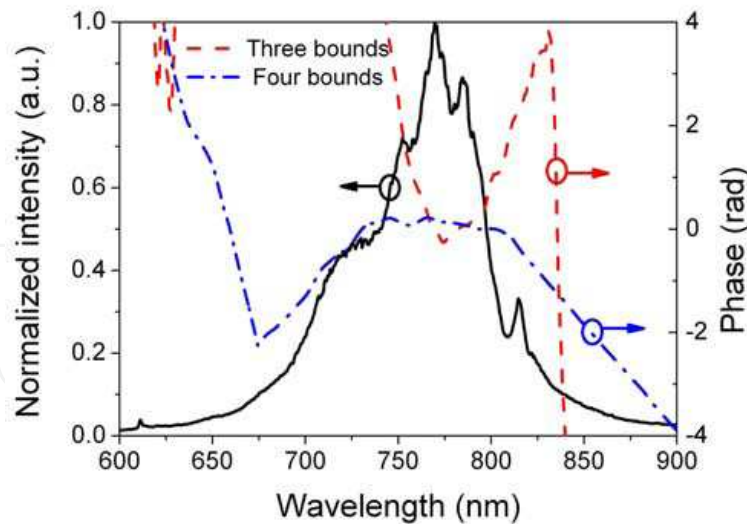


Fig. 21. Spectrum and phases for 3 and 4 bounces between chirp mirror.

## 5. Summary

In this chapter, a novel technology for generating intense few to monocycle light pulse was proposed and demonstrated. This technology has similar effect as the gradient pressure scheme while avoid the disadvantage of gas flow and consumption of expensive noble gases.

A model for simulation of the pulse evolution in a gradient temperature hollow fiber filled with argon gas has been established. The simulation results show that in the gradient temperature scheme, the incident pulse energy can be much higher than that of the uniform case, which is similar to the gradient pressure. In the gas of gradient temperature, the pulse spectra can be broadened more than that in the case of uniform temperature. Shorter pulses can be obtained after a further compression.

We also verified the effectiveness and feasibility of the scheme of gradient temperature. The entrance of the filament was heated by a furnace and the two ends of the tube were cooled with air, which resulted in the temperature gradient distribution along the tube. The presented method is easily done with only a furnace, without the large consumption of noble gas and turbulence. Although the temperature gradient is not linear, we observed that multiple filaments were shrunken into a single filament and then filament disappears by increasing the temperature to some degree, which indicates that the critical power increases with temperature due to the gas atoms squeezed to the other end of the tube where the temperature is lower. Also, the filament can appear and disappear by controlling the local temperature and incident pulse energy in turn. The spectrum of the exit pulses is not expanded so much in comparison with the case of the same pressure and the same pulse energy, because the total gas atoms number is unchanged in the sealed tube. However, higher pulse energy is allowed to incident into the tube and a round trip pass of the tube is expected to expand the spectrum further with self-compression.

The gradient temperature technique has a great advantage that the temperature is easier to control than gradient pressure by differential pumping. Another merit is that the gas in the tube is relatively steady without flow, which is very important for keeping the output spectra stable. Not long after heating the gas to a high temperature at part of the sealed tube,

the inner gas pressure will reach an equilibrium and the gas density in the tube will be gradient while the pressure in the tube will be equal everywhere. Because the pressure in the sealed tube is uniform, the convection and instabilities does not appear in our experiments. In contrast, in our experiment, the spectra and the light spot are very stable. For the pulse of same incident peak power, the spectra expansion in the gradient temperature is not as large as in the uniform temperature case. This is because the high temperature reduces the nonlinearity. However, because of this, a higher input energy can be sent through the tube, such that at the end of the tube, the peak power of the pulse is still high enough to expand the spectrum. This is the main reason that the transform limited pulse is shorter in gradient temperature tube than in the uniform temperature one. The drawback of the scheme is that the gas density difference cannot be as large as in the scheme using differential pumping. In addition, a big temperature difference may break the glass tube.

This technique offers one more degree of freedom to control the filamentation in a gas-filled tube for the intense monocycle pulse generation without gas consumption and turbulence and opens a new way for multi mJ level monocycle pulse generation through filamentation in the noble gas.

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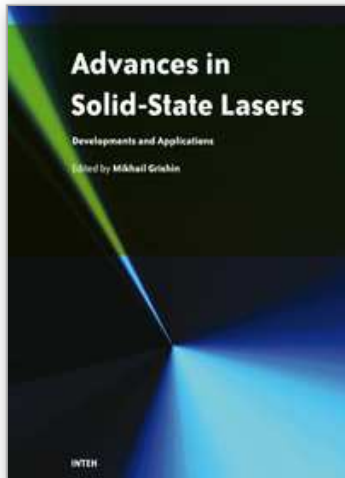
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## **Advances in Solid State Lasers Development and Applications**

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Invention of the solid-state laser has initiated the beginning of the laser era. Performance of solid-state lasers improved amazingly during five decades. Nowadays, solid-state lasers remain one of the most rapidly developing branches of laser science and become an increasingly important tool for modern technology. This book represents a selection of chapters exhibiting various investigation directions in the field of solid-state lasers and the cutting edge of related applications. The materials are contributed by leading researchers and each chapter represents a comprehensive study reflecting advances in modern laser physics. Considered topics are intended to meet the needs of both specialists in laser system design and those who use laser techniques in fundamental science and applied research. This book is the result of efforts of experts from different countries. I would like to acknowledge the authors for their contribution to the book. I also wish to acknowledge Vedran Kordic for indispensable technical assistance in the book preparation and publishing.

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