

# Temperature Dependence of Material Properties and its Influence on the Thermal Distribution in Regeneratively Cooled Combustion Chamber Walls

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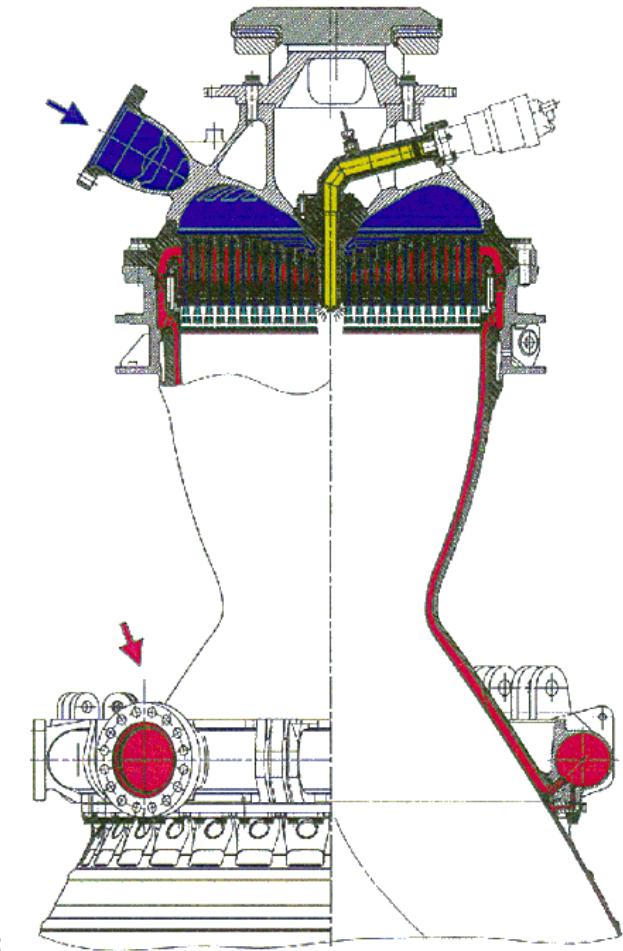
Institute of Space Propulsion

# conditions in regeneratively cooled LOX/GH<sub>2</sub>-engines

- ▶ hot gas temperature:  $\approx 3500 \text{ K}$
- ▶ pressure:  $\approx 11 \text{ MPa}$
- ▶ heat flux: up to  $80 \text{ MW/m}^2$
- ▶ LH<sub>2</sub>-temperature:
  - cooling channel inlet  $\approx 40 \text{ K}$
  - cooling channel outlet  $\approx 100 \text{ K}$
- ▶ wall structure temperature:
  - hot gas side  $\approx 400 - 800 \text{ K}$
  - cooling fluid side  $\approx 40 - 100 \text{ K}$

**hot gas wall temperature:  $\Delta T = 40 \text{ K} \approx 50\% \text{ life time}$**

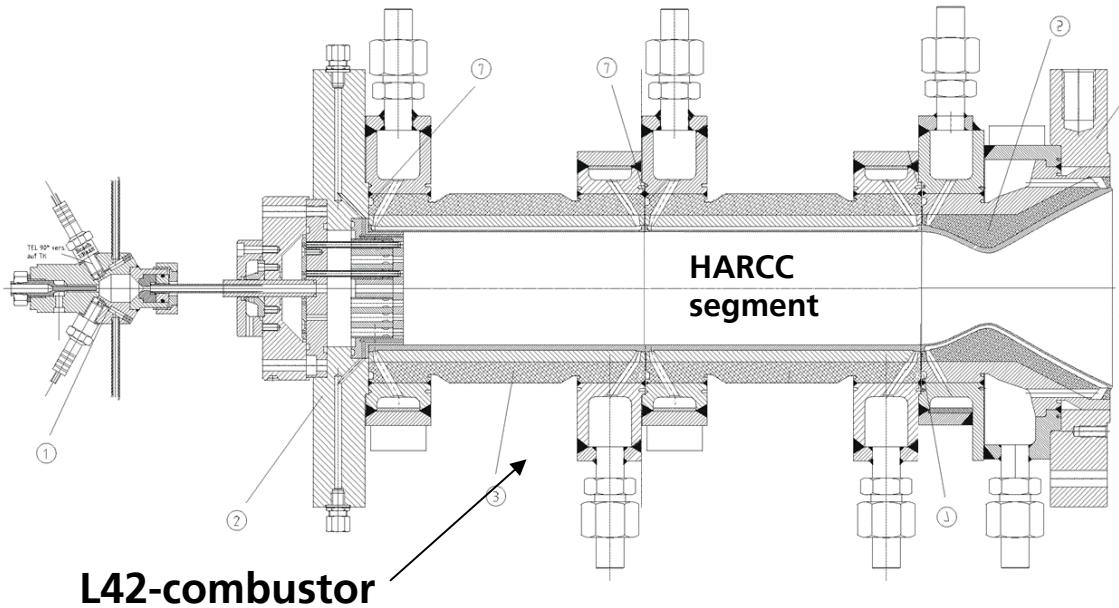
A. Fröhlich, M. Popp, G. Schmidt, D. Thelemann. Heat Transfer Characteristics of H<sub>2</sub>/O<sub>2</sub> Combustion Chambers, AIAA 93-1826, 29th Joint Propulsion Conference, Monterey, CA, 1993



# stratification in cooling channels with high aspect ratio

## HARCC-experiment

- ▶ P8 test bench
- ▶ LH<sub>2</sub>-cooled L42 combustor
- ▶ pressures up to  $P_c = 9 \text{ MPa}$
- ▶ heat fluxes up to  $40 \text{ MW/m}^2$
- ▶ variation of AR=1.7 ... 30



## P8 test bench →

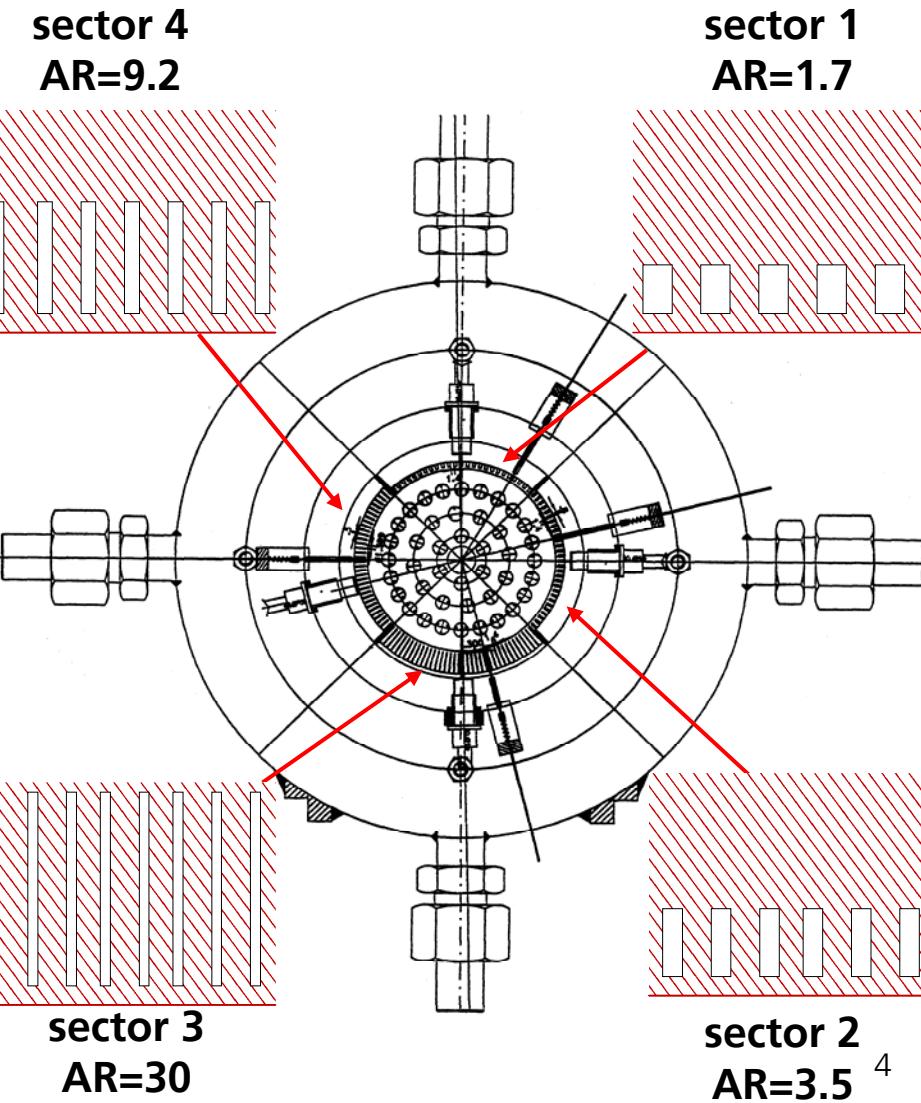
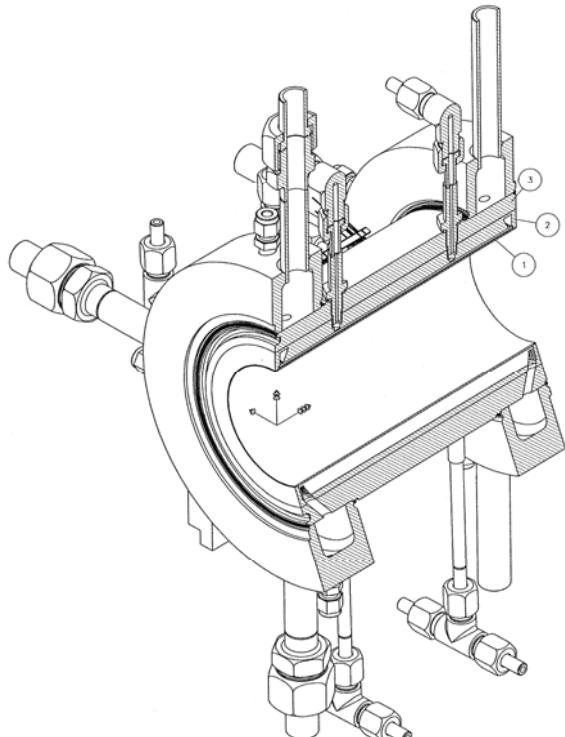
D. Suslov, A. Woschnak, J. Sender, M. Oschwald, Test specimen design and measurement technique for investigation of heat transfer processes in cooling channels of rocket engines under real thermal conditions, AIAA 2003-4613, 39th Joint Propulsion Conference, Huntsville, 2003

A. Woschnak, D. Suslov, M. Oschwald, Experimental and Numerical Investigations of Thermal Stratification Effects, AIAA 2003-4615, 39th Joint Propulsion Conference. Huntsville, 2003



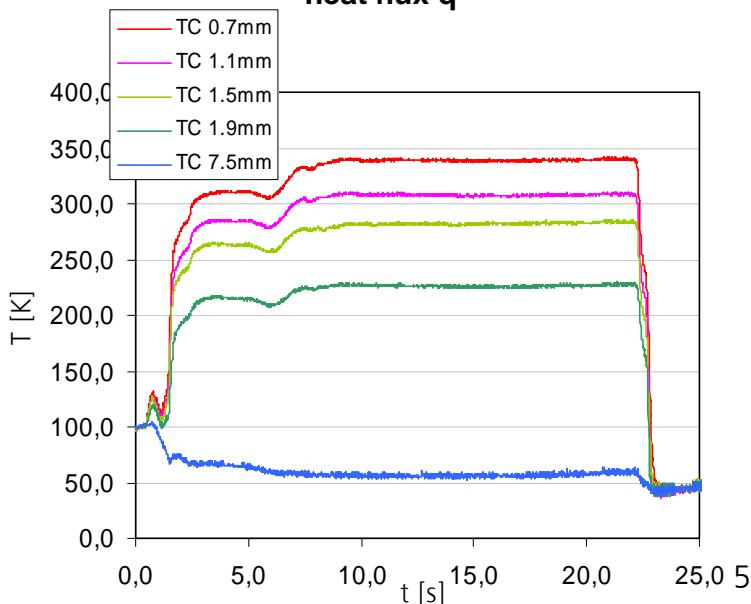
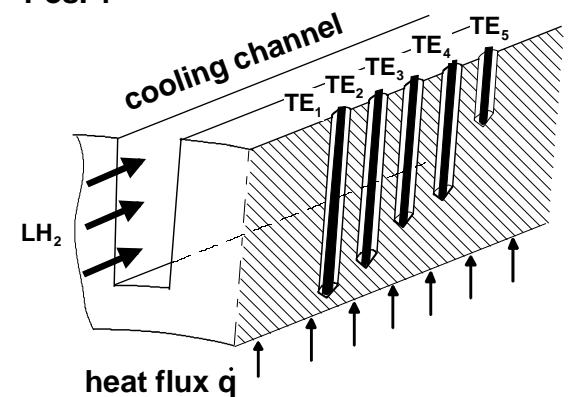
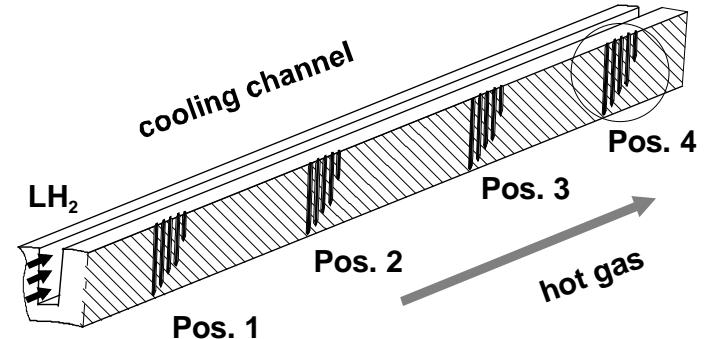
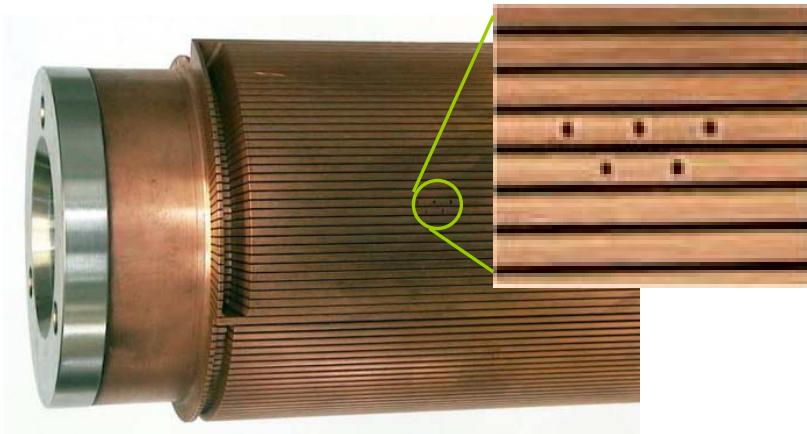
# HARCC geometries

sector no.	width [mm]	height [mm]	aspect ratio	fin width [mm]
1	1.2	2.0	1.7	1.4
2	0.8	2.8	3.5	1.4
3	0.3	9.0	30	1.4
4	0.5	4.6	9.2	1.4



# temperature determination in wall structure with thermocouples

- ▶ measurements at 4 axial locations
  - $z=52\text{mm}, 85\text{mm}, 119\text{mm}, 152\text{mm}$  downstream duct entrance
- ▶ 5 radial positions
  - $0.7\text{mm}, 1.1\text{mm}, 1.5\text{mm}, 1.9\text{mm}, 7.5\text{mm}$  from hot gas side
- ▶ determination of surface temperature, heat flux and heat transfer coefficients by inverse method



# heat conduction / material properties

**instationary problem:**

$$\rho \frac{\partial(c_V T)}{\partial t} - \nabla \cdot (\lambda \nabla T) = 0$$

**stationary problem:**

$$-\nabla \cdot (\lambda \nabla T) = 0$$

**specific heat:**

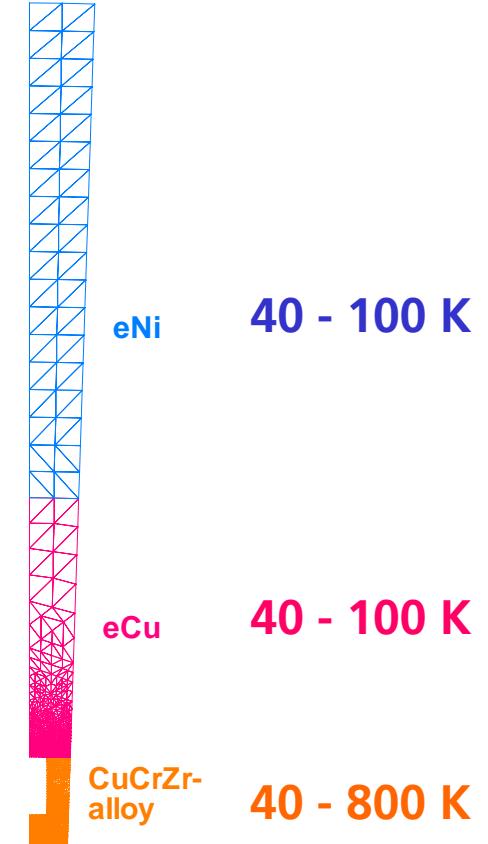
$$c_V \approx 25.9 \text{ J/mol/K}$$

(Dulong-Petit, ambient temperature)

**heat conductivity:**

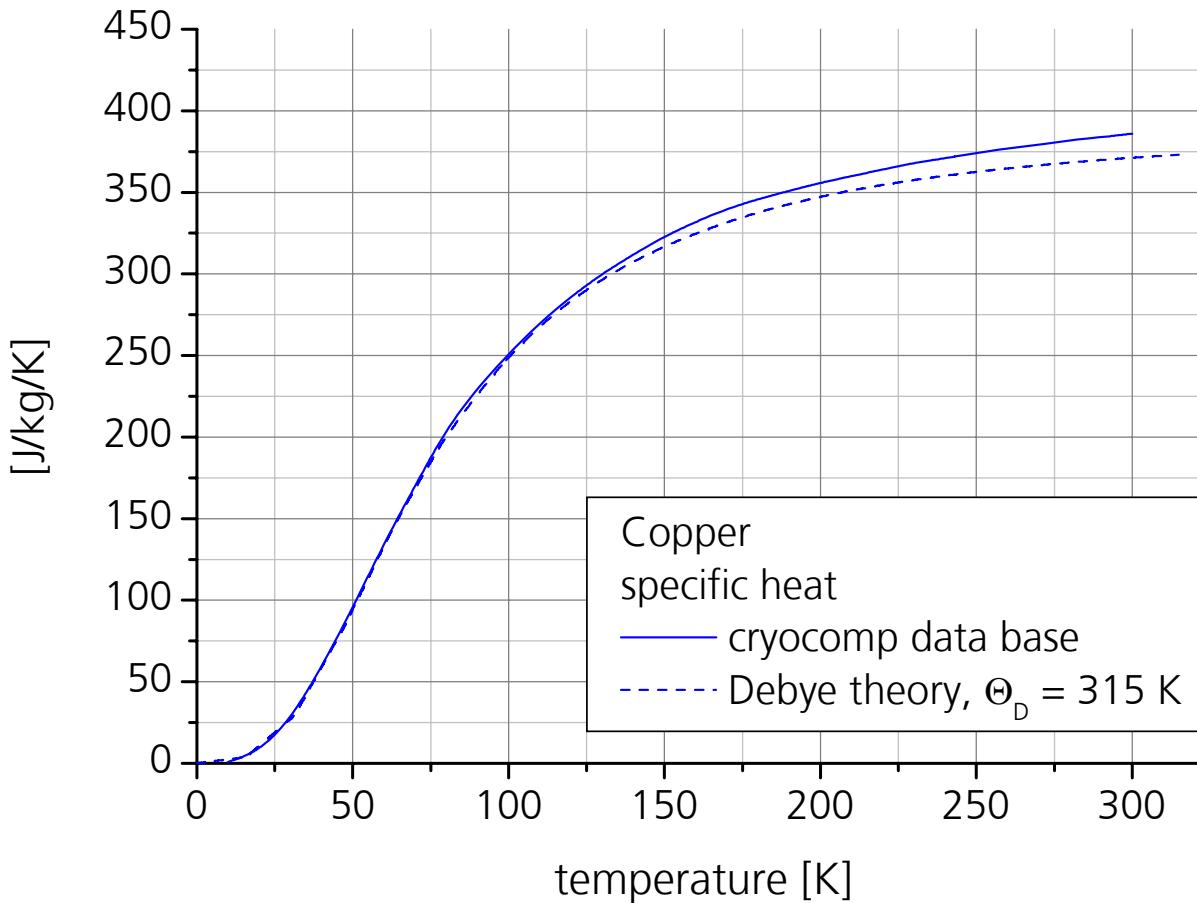
$$\lambda \approx 350 \text{ W/Km}$$

(typical Cu-alloy)



**combustion chamber  
wall construction**

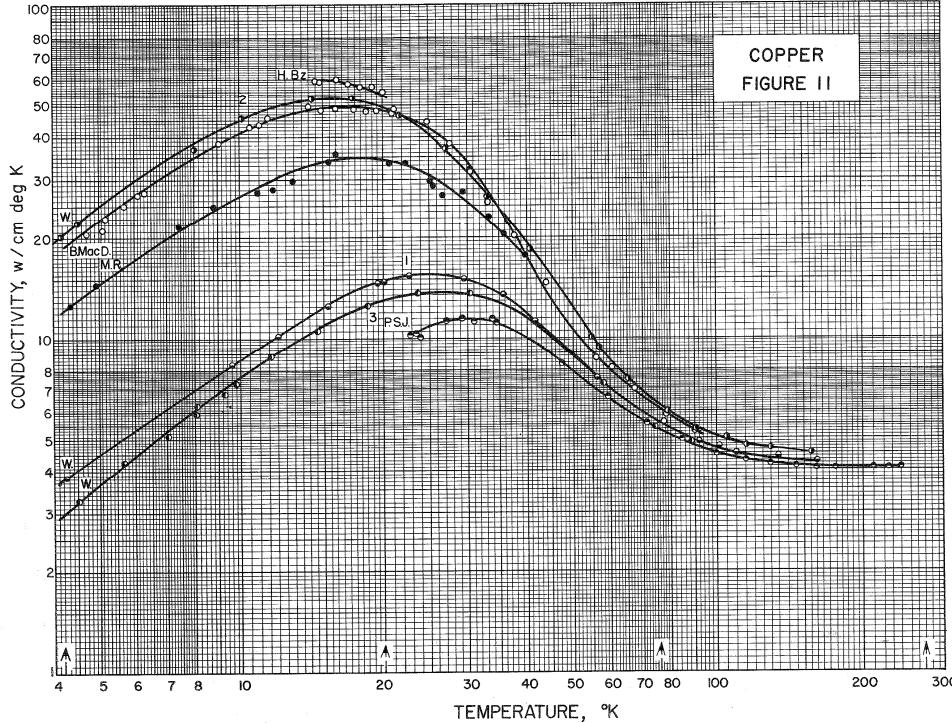
# Debye-theory of the specific heat



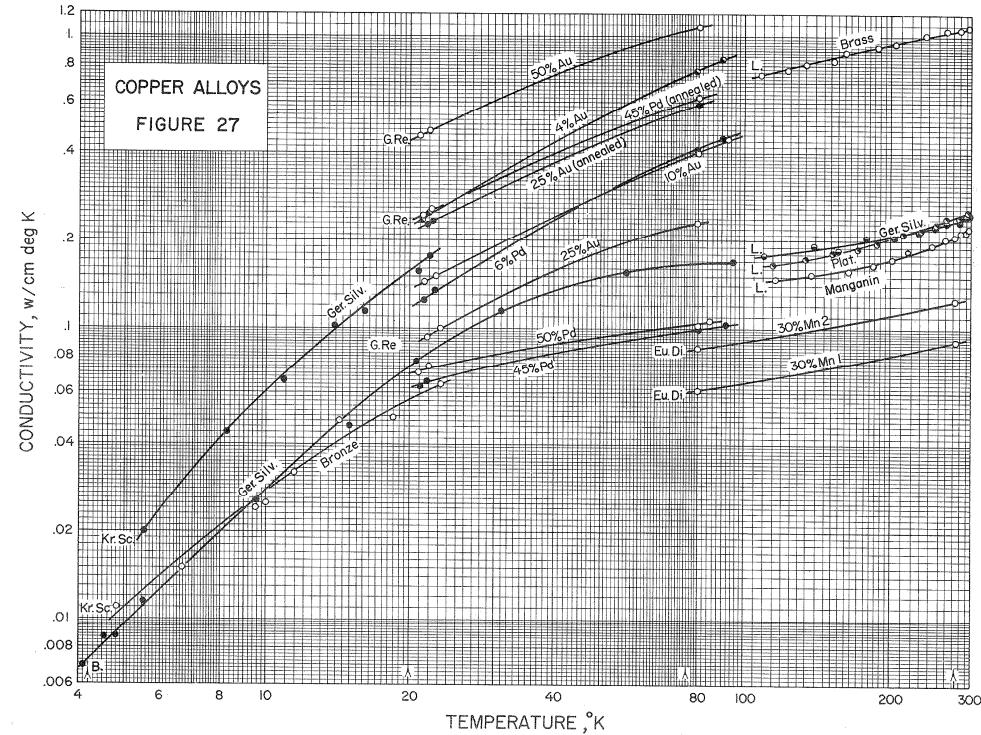
## Debey-theory

- ▶ quantum mechanics for low temperature behaviour
- ▶ high temperature limit:  
 $c_v = 3R$  (Dulong-Petit)
- ▶ low temperature limit:  
 $c_v \propto a \cdot (T / \Theta_D)^3$
- ▶ for copper:  $\Theta_D \approx 315$  K

# thermal conductivity at low temperatures



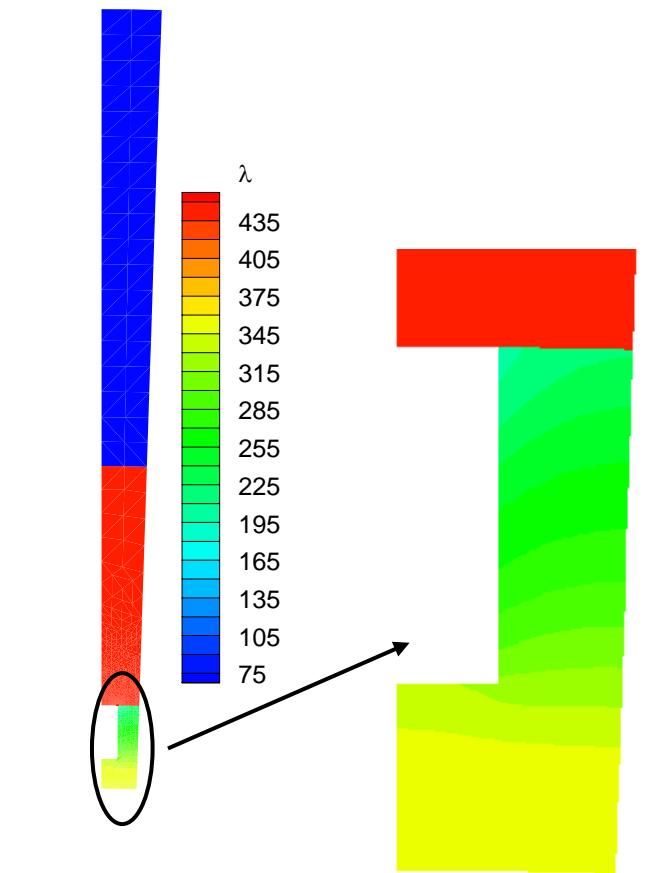
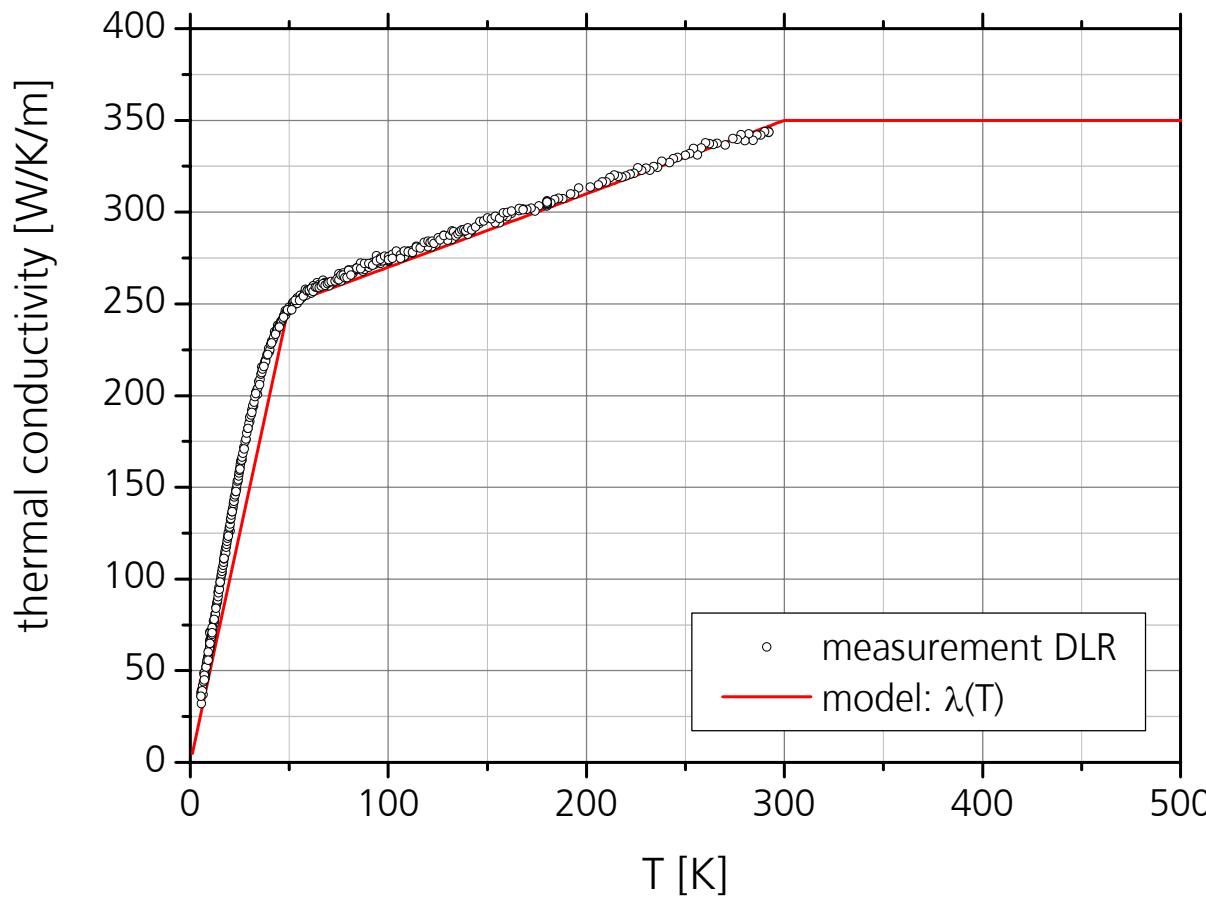
**pure copper**  
**maximum near 20 K**



**copper alloys**  
**phonon scattering at lattice imperfections:**  
**reduction of thermal conductivity**

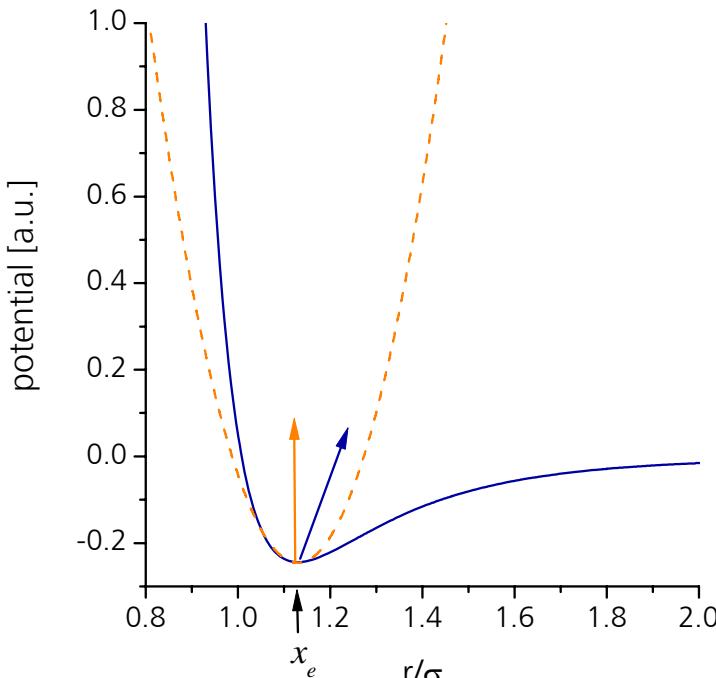
R.L. Powell and W. A. Blanpied, Thermal Conductivity of Metals and Alloys at Low Temperature, NBS Circular 556, 1954

# thermal conductivity of copper alloy for L42-combustor



**variation of thermal conductivity  
in wall with thermal field**

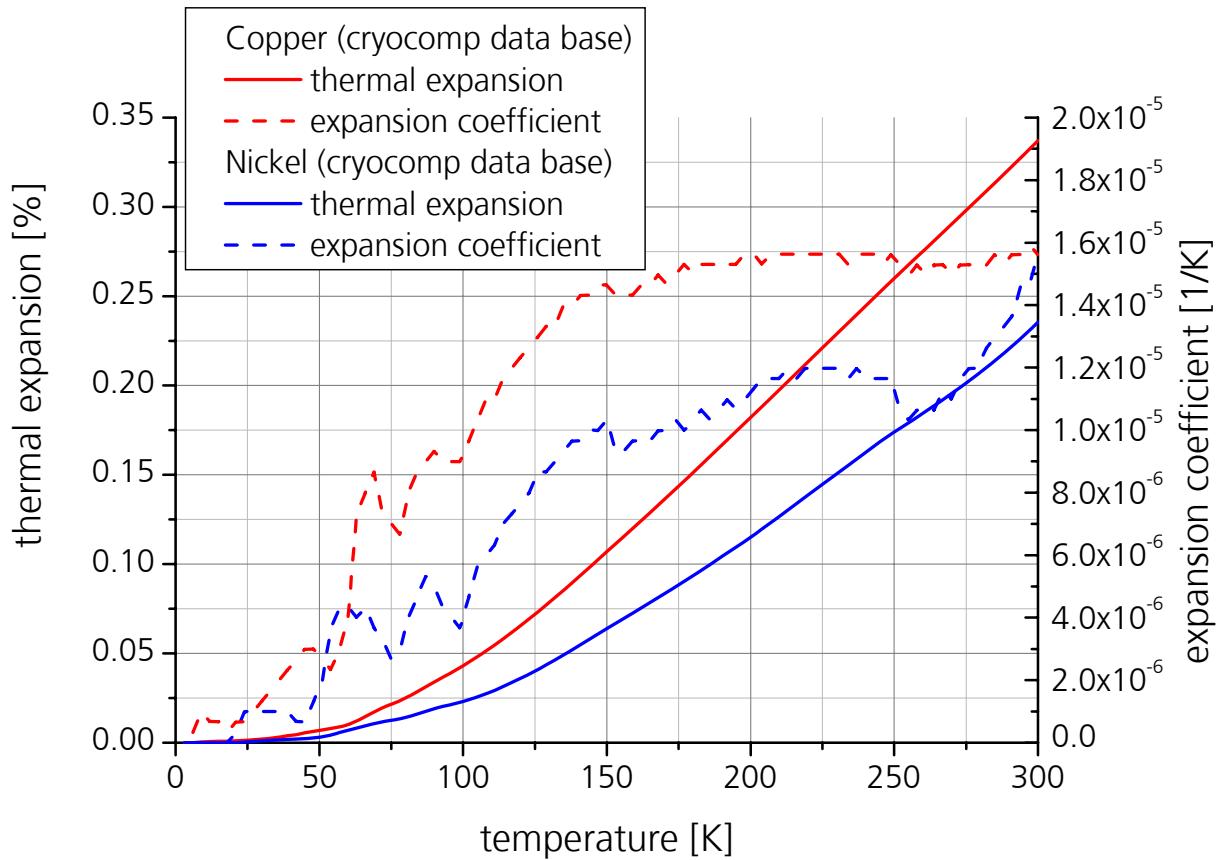
# thermal expansion coefficient



$$U(x) = cx^2 - gx^3 + \dots$$

$$\langle x \rangle = x_e + \frac{3g}{4c^2} k_B T$$

$$\alpha = \frac{1}{\langle x \rangle} \frac{d\langle x \rangle}{dT}$$



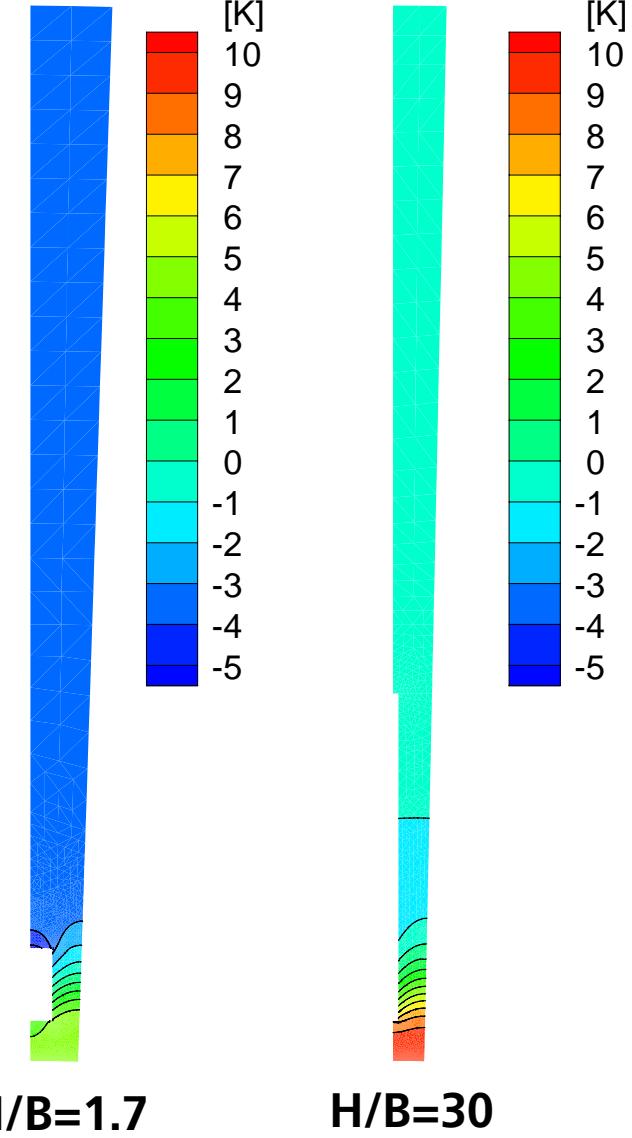
- ▶ thermal expansion due to anharmonicity of potential
- ▶ expansion coefficient vanishes at  $T=0$

$$\Delta T_w = T_v - T_c$$

## thermal field w/o and with temperature dependence of $\lambda$

- ▶ HARCC experiment, 52 mm downstream cooling fluid inlet

AR H/B	sector	$T_{H2}$	$T_w$ [K]		$\Delta T_w$ [K]
			$T_c$ $\lambda=\text{const.}$	$T_v$ $\lambda(T)$	
1.7	Q1	85	380.9	385.0	4.9
3.5	Q2	90	363.3	369.4	6.1
9.1	Q4	95	349.9	358.2	8.3
30	Q3	100	343.6	352.7	9.1

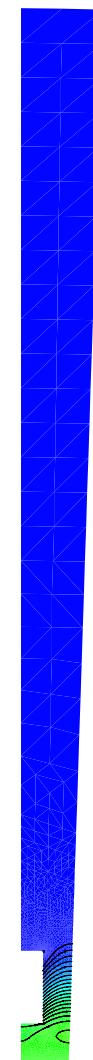


$$\Delta T_w = T_v - T_c$$

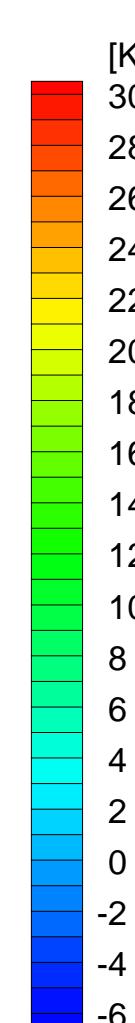
# thermal field w/o and with temperature dependence of $\lambda$

- cooling fluid temperature: 50K

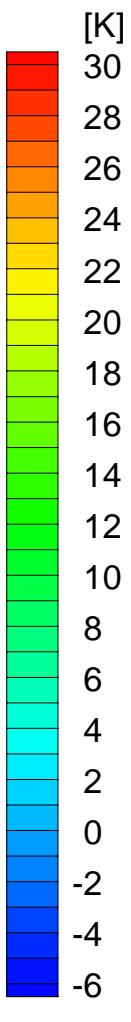
AR H/B	sector	$T_w$ [K]		$\Delta T_w$ [K]
		$T_c$ $\lambda=\text{const.}$	$T_v$ $\lambda(T)$	
1.7	Q1	349.0	361.3	12.3
3.5	Q2	326.6	345.7	19.1
9.1	Q4	308.3	334.6	26.3
30	Q3	297.3	327.0	29.7



H/B=1.7



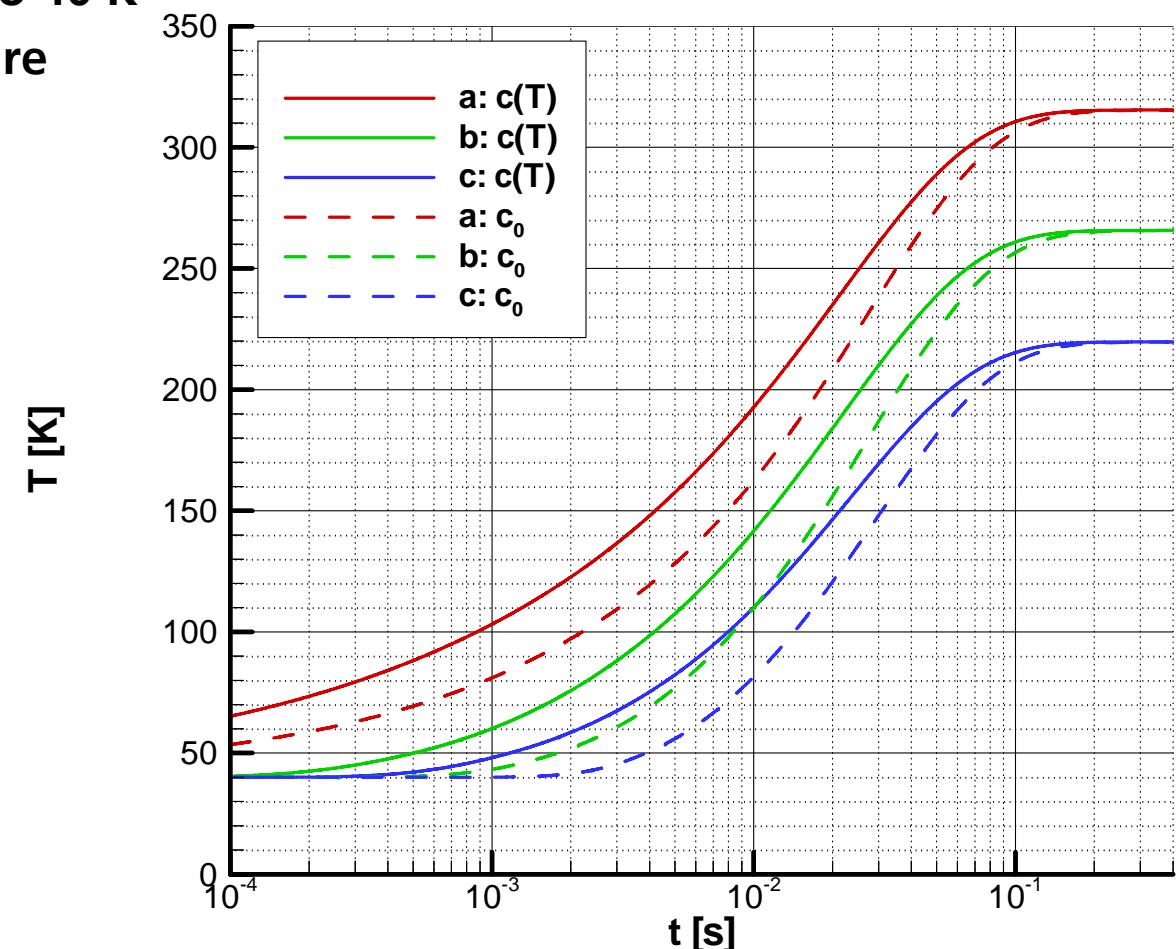
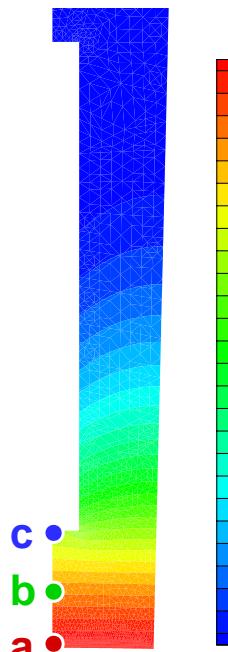
H/B=30



# transient thermal field: $c_v=c_0$ vs. $c_v=c_v(T)$

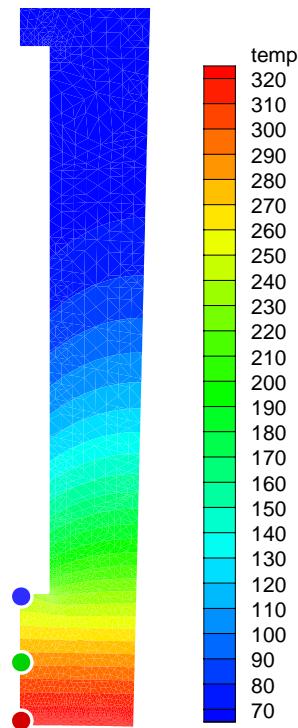
## wall temperatures

- ▶ pre-cooling of structure to 40 K
- ▶ instantaneous temperature increase at  $t=0$

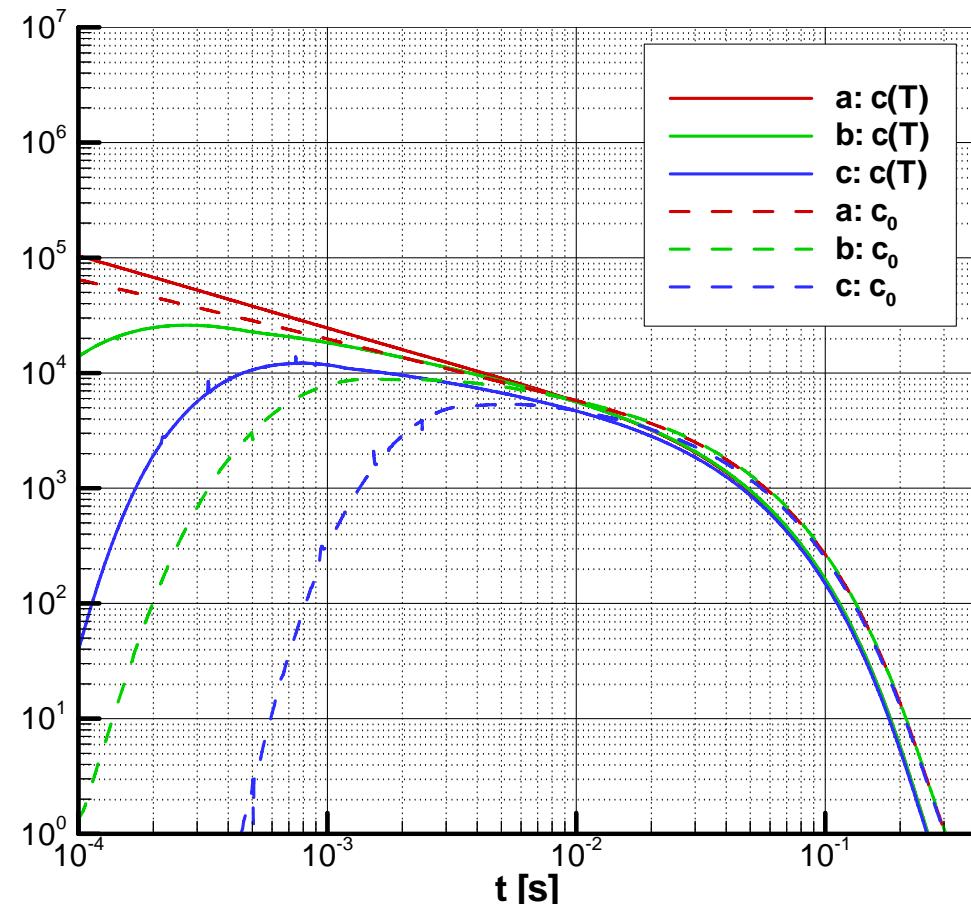


# transient thermal field: $c_v=c_0$ vs. $c_v=c_v(T)$

## temporal gradients

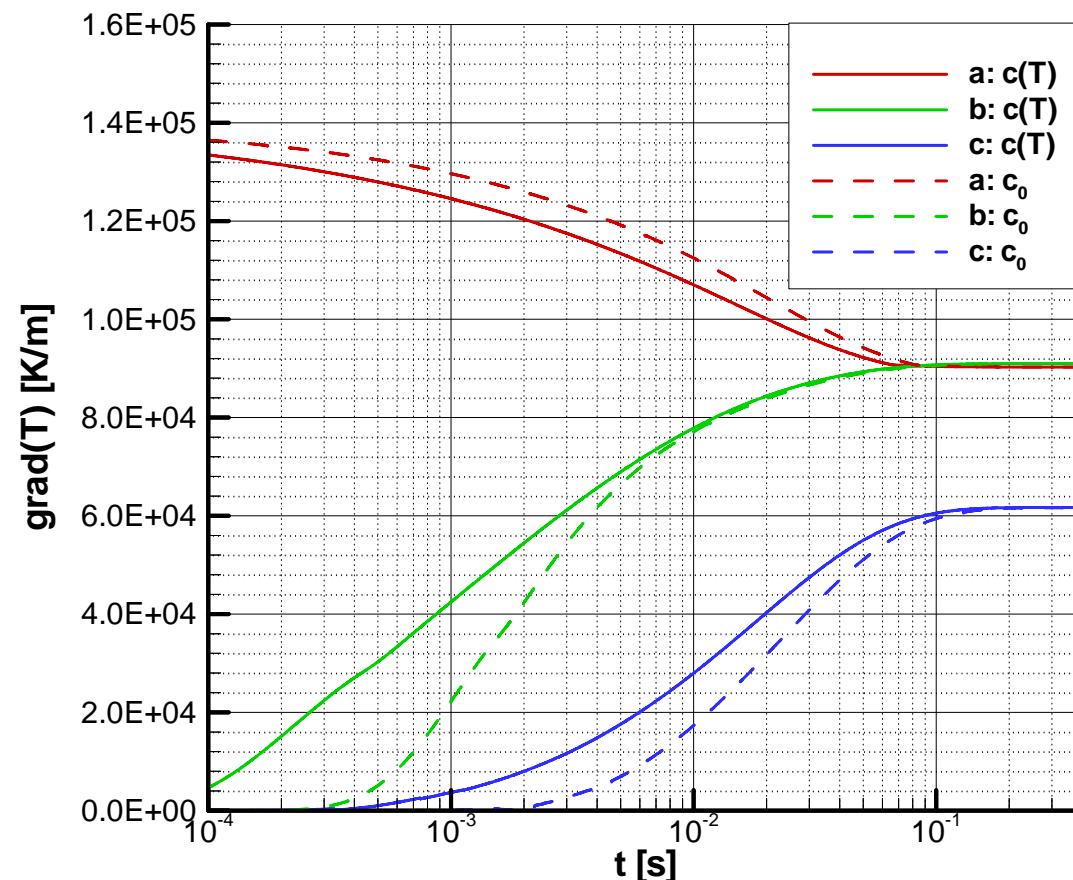
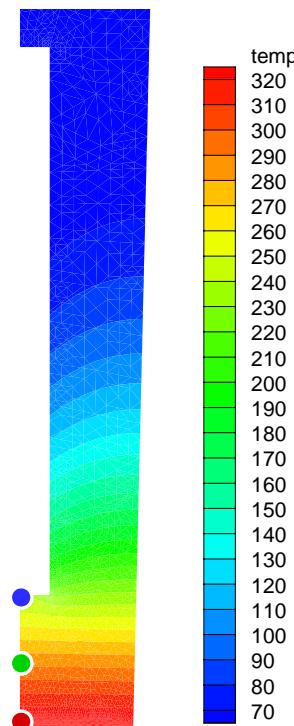


$dT/dt$  [K/s]



# transient thermal field: $c_v=c_0$ vs. $c_v=c_v(T)$

## spatial gradients



## summary

specific heat  $c_v$

thermal conductivity  $\lambda$

thermal expansion coefficient  $\alpha$

- ▶ show significant temperature dependence
- ▶  $c_v, \lambda, \alpha$  disappear at absolute zero

$\alpha \rightarrow 0$  for  $T \rightarrow 0$

- reduced thermal stress at low temperature

$c_v \rightarrow 0$  für  $T \rightarrow 0$

- only minor differences as compared with simulation results with  $c_v = \text{const.}$

$\lambda \rightarrow 0$  for  $T \rightarrow 0$

- increase of hot gas side wall temperature
- relevant level of increase at low cooling fluid temperature and high AR