UNIVERSITY OF OSLO Department of Informatics

Master thesis

Assessment of Indoor Positioning System (IPS) technology

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Preface

The thesis is part of the fulfillment of my Masters degree at the Department of Informatics at the University of Oslo (IFI) and the University Graduate Center at Kjeller (UniK).

I would like to thank my supervisor Professor Knut Øvsthus for his help and guidance through out the work on this thesis, but also for making it possible for me and my fellow HiB students to achieve this Master's degree without having to leave Bergen ©. I would also like to thank Øystein Taskjelle and Espen D. Steine, which I have studied with the last five years, for good discussions and help whenever I got stuck.

Fulfilling this Master's degree is a big milestone for me personally, and I would never have made it without a big support from my family, especially my parents.

Summary

Indoor Positioning Systems (IPS) have lead to increased efficiency in many types of organizations and industries, and more and more companies embrace the new opportunities and functionality found in IPS solutions. Because of IPS's importance and usage potential in creating new services, there is a significant interest in the industry for IPS and Real Time Locating Systems (RTLS). The market potential for companies that develop and sell IPS and RTLS systems are thus predicted to be large in the coming years.

An IPS system may consist of only one technology, or be a hybrid of two or more technologies. Although the biggest difference between IPS systems are the technology they are based on, it is often the performance, usage, ease of deployment, cost, or a combination of these, that matters. Examples of technologies that are used in IPS systems and assessed in this thesis are Radio Frequency Identification (RFID), Wi-Fi, Ultrasound and Ultra-Wideband (UWB).

The technology assessment showed that UWB is probably the best technology for use in indoor positioning systems. Ultra-Wideband is however in its early phases and are therefore not regulated for use in all countries, for instance Norway. Wi-Fi is on the other hand a good choice for open indoor environments such as office or class rooms where some level of positioning error is accepted as long as the decreased performance is reflected in the price of the system. The testing program build in this thesis, including the proposed positioning methods, show that it is possible to create a low cost indoor positioning system by re-using the existing wireless network infrastructure and still achieve an acceptable level of accuracy.

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Chapter 1

Introduction

In this chapter, an introduction to the topic of this thesis is given in section 1.1 Indoor Positioning Systems (IPS), the motivation behind the thesis is explained in 1.2, problem description in 1.3, privacy concerns in 1.4, and demarcation of the problem description in 1.5. In the end, an overview of the report structure is found in 1.6.

1.1 Indoor Positioning Systems (IPS)

Indoor Positioning Systems (IPS) is a type of a Real-Time Locating System (RTLS). RTLS locates or track persons/assets in "real-time". Sometimes RTLS systems are also being referred to as *Local Positioning Systems* (LPS), or simply *Positioning Systems*. This thesis will focus on indoor positioning, and thus IPS. The development and use of IPS systems have increased radically in the last few years. More and more wireless technologies are being used, resulting in more feature rich systems capable of solving numerous big and small tasks in a company, factory or organization buildings. The big range of services the IPS systems can offer are mainly the reason for its extremely success and popularity in the recent years.

A IPS system consists of several steps, and the locating is not done in a single process. First *sensors* or *receivers/readers* receive signals from transmitting *devices* or *tags*. The sensors or receivers then sends the collected data values, to a central *locating engine* which calculates the approximate position of the device or asset using different algorithms/models. The collected data values could be either the Received Signal Strength Indication (RSSI), Time Difference of Arrival (TDoA) or the Angle of Arrival (AoA). How accurate the results are, depends on the technology used in the system. The calculated result is then sent from the locating engine in x and y coordinates (and z in 3D systems) to a *user interface*. The user interface is basically just an application where the calculated position is shown to the user on a map of the monitored area.

Although IPS is a type of RTLS, it is despite its name, usually not "real-time" in the true meaning. Real-time is when the system adjust itself whenever there is a change in the environment with a small or no delay, for instance when a person or an asset has changed its position. If a person on the move is being positioned, the position given to the user interface will often be slightly delayed in relation to the actual position because of the time it takes to collect data, calculate, and pass the information to the user interface. In real-life applications, this is not a problem since it is not often a true real-time system is actually needed. Therefore, most positioning systems on the market today do not perform "real" real-time positioning.

Furthermore, another challenge is the real-time vs long battery life "battle", since it is hard to fulfill them both. To get as close as possible to real-time, the device or tag have to transmit its position as often as possible, but this results in high power consumption and a low battery life. In reality, most IPS/RTLS tags contains a motion sensor which is used to differentiate transmitting intervals between when the asset/person is moving or not to save power. It's normal to use a transmitting interval of only a few seconds when the asset/person is moving, and several minutes when it's not. This enables a battery lifetime for up to 3 or 4 years before it needs to be changed.

1.2 Motivation

Indoor Positioning Systems (IPS) have lead to increased efficiency in many types of organizations and industries, and more and more companies embrace the new opportunities and functionality found in a IPS solution. IPS have many usage areas, and is for instance used in logistics, health care, critical/dangerous asset tracking, emergency services, personnel/visitor identification, security, and so on. They all rely on the IPS system to give them the highest possible efficiency, security and safety. This gives the technology behind the IPS systems is thus an ongoing process to always get the most out of the existing technology and solution.

Furthermore, because of IPS's importance and usage potential in offering new services,

there is a significant interest in the industry for IPS and RTLS systems. The market potential for companies that develop and sell RTLS systems are thus predicted to be large in the coming years. According to a forecast by IDTechEx, the global RTLS market will increase to \$2.58 Billion in 2019, while it was \$153 Million in 2009 [5].

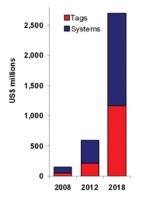


Figure 1.1: IDTechEx market forcast for Real-Time Locating Systems 2008-2018 [13]

IPS systems may consist of only one technology, or be a hybrid of two or more technologies. Although the biggest difference between IPS systems are the technology they are based on, it is often the performance, usage, ease of deployment, cost, or a combination of these, that matters.

1.3 Problem description

This thesis has been based on the following problem description:

"Assess technologies and methods used in Indoor Positioning Systems (IPS) and their applicability in different environments. Define the most important requirements for a indoor positioning system today, and select a technology to focus on based on these requirements. If possible, emphasis cheap technologies with acceptable accuracy. Test and evaluate different positioning methods real-time. Identify possible extensions of the assessed technology and methods."

1.4 Demarcation

The thesis will focus on the following technologies: Radio Frequency Identification (RFID), Wi-Fi, Ultrasound and Ultra-Wideband (UWB). Although there exist IPS systems that use other wireless technologies, like Infrared, Bluetooth and ZigBee, they are not by far as commercially available as the former mentioned technologies. Wi-Fi and RFID were chosen because of its wide deployment and low cost equipment. Ultrasound and UWB on the other hand was chosen because many see them as the "newcomers" in the indoor positioning arena, for its high potential to increase the performance of such systems.

In addition, the focus will be on open environments, typically class room and office environments.

1.5 Privacy concerns

Although positioning and localization systems offer new opportunities in terms of efficiencies, security and safety, it may also be seen as a threat to privacy. Specially when it is applied to persons, either directly, or on equipment worn by persons. The development of positioning systems have increased in the last years, with all sorts of technologies and functionality implemented. Positioning systems have resulted in a new market for localization services, and can be found in most part of our society today. Some examples are cell phone localization: AutoZeek¹ and mBuddy², localization of cars involved in a traffic accident: eCall, and indoor positioning systems used in different scenarios: dating, asset/patient/staff tracking at hospitals and passenger tracking in airports.

As a result, our society is more and more turning into a surveillance society. Localization, tracking and storage of personal data are hence regulated in most countries. In Norway it is *The Data Inspectorate* (in Norwegian: *Datatilsynet*) that have the mandate and task to control and regulate "..violation of persons right to privacy through the processing of personal data". They have, not surprisingly, been very skeptical[33] to the new localization and tracking services.

The most relevant statements I was able to find (at 03.05.2009) from The Data Inspec-

¹http://www.zeekit.no/

²http://www.mbuddy.no

torate concerning RTLS systems where an IPS system based on ultrasound, where it was used as a dating/friend-finding tool[7] at *Samfundet* in Trondheim. The goal was to be able to see where you're friends or possible partners were in the building. The Data Inspectorate thought there were no need to warn about this as long as the participants were given full information of what the collected data was going to be used for, and could get all its information deleted whenever he or she wanted it to be done.

In addition to the example above, I also found an statement were a new passenger tracking solution at airports[10] were proposed. The idea was that the passengers receive a RFID oblate to either keep on them, or to put on their luggage so the airport staff could be able to track either them or their luggage. The Data Inspectorate was very critical to this project, and called it a "...dramatically monitoring project", and didn't think the project would pass because of regulation restrictions. Further in the article, Gunnel Helmers which is a Senior Adviser in The Data Inspectorate, said that "..for it to be worth the loss of privacy, it must prove a very positive effect on the system". She claims that people with bad intentions will most likely find a way around the system anyway, resulting in a mass monitoring of a large group of innocent people.

Hence, for localization and tracking systems to be accepted, the persons involved have to know the systems purpose and operations, give its permission to be located/tracked, and the systems must prove a very positive effect on the system it's implemented in.

1.6 Structure of the report

The structure of the report are as follows; in section 2, *Theory and background*, the technologies assessed in this thesis are presented. In section 3, *Requirements*, the requirements for the technologies in this thesis is set, were section 4, *Technology assessment*, discuss the assessed technologies in relation to the requirements presented and choose a technology that the rest of the thesis focus on. Furthermore, in section 5, *Building a test program*, presents the testing program made to test the positioning methods and models presented in section 6, *Positioning methods and models*. Section 7, *Test setup*, presents the test area, equipment used and configuration. In the end, the test results and positioning methods are presented and evaluated in section 8, *Test results and evaluation*, and section 9 contains the *Conclusion* of the thesis. In addition, all the details around testing done in this thesis are found in appendix A, and logs from the positioning testing are found in appendix B.

Chapter 2

Theory and background

In this chapter, an technology overview of the assessed technologies in this thesis are given in 2.1. In addition, section 2.2 and 2.3 gives an overview of existing RTLS standards and methodologies.

2.1 Technology overview

2.1.1 Radio Frequency Identification (RFID)

RFID is a technology used to *identify* objects or assets by using RF. The objects or assets wear RFID tags which are then identified by a RFID reader. A RFID tag contains two parts; the antenna that receive and transmits RF signals, and a micro chip which stores and process information in addition to modulating and demodulating the RF signals. The antennas varies in size and shape, depending on the range and properties it shall have.

RFID tags are usually divided into either being *passive* or *active*, but are in fact two different technologies. Passive tags do not contain a battery, and are thus smaller in size. When a passive tag is read by a reader, the tags antenna induces enough power from the reader so the tag is able to transmit its reply. Passive tags is often used as bar codes in shops or on packages at logistics.

Active tags contain its own battery, and are hence bigger compared to passive tags, but have in addition greater memory and RF transmission range. Active tags are furthermore able to transmit at a higher effect than passive tags. This usually makes active tags more "trustworthy" to actually reach the reader with its reply in noisy areas. However, a drawback with active tags are the increase in price compared to passive tags.

When it comes to standards[23], The International Organization for Standardization (ISO) have created several standards for RFID to be used in different usage scenarios. In this context, the most relevant standards are the ISO 11784 and 1175 which defines how data is structured on the tag and the air interface protocol for tracking cattle. In addition, ISO 18046 and 18047 defines a standard for testing respectively the performance and the conformance of RFID tags and readers. Conformance is when the equipment are tested to determine whether an implemented system fulfills its requirements against the standard or not.

Because of its simple and mature technology, in addition to its many usage areas, RFID is therefore one of the most common used technologies in IPS systems. By knowing the location of the RFID reader, you also know the location of the asset or object that wear a RFID tag, since the transmission range is limited and the reader identifies the tags unique *number*. In IPS systems it is more common to use active tags, but some vendors offer passive tags. RFID is often used together with Wi-Fi in IPS systems to achieve higher *accuracy*, for example by using an *exciter*, sometimes called a *chokepoint*. Exciters are placed between rooms or floors, to achieve a 100% room level accuracy.

2.1.2 Wi-Fi

Wi-Fi is a trademark of the Wi-Fi Alliance¹, and refers to the IEEE 802.11 standard[14]. IEEE 802.11 was first published in 1997 and was the first wireless networking standard. Many extensions have been made since then and the original protocol is now obsolete. The standard are today the most widely adopted wireless technology in use. Most laptops and cell phones on the market today comes with an integrated IEEE 802.11 wireless interface card. Wireless LANs are mainly used for transmitting data, but it is also used for wireless Voice over IP (VoIP).

IEEE 802.11 uses *spread spectrum* techniques, which are different methods of generated electromagnetic energy in a particular bandwidth, spread in the frequency domain. This results in a signal with a wider bandwidth. IEEE 802.11 consist of many parts, describing different modulation techniques, security (802.11i) and more. The most important parts are *802.11a*, *802.11b*, *802.11g*, *and 802.11n*, which will be briefly explained below.

¹http://www.wi-fi.org/

First, IEEE 802.11a was first published in 1999, and was the first standard in the 802.11 "family" which supported a maximum data rate of 54 Mbit/s. 802.11a uses a modulation method called Orthogonal Frequency Division Multiplexing (OFDM). 802.11a operates in the 5 GHz band called Unlicensed National Information Infrastructure (U-NII).

Next, IEEE 802.11b was published in 1999, and uses the same data link layer as the original 802.11 standard. The high data rate for 802.11b (11 Mbit/s), compared to the original standard 802.11 (1-2 Mbit/s), made it widely accepted as the new standard for wireless technology. 802.11b uses a modulation technique called Complementary Code Keying (CCK), and operates in the 2.4 GHz Industrial, Scientific and Medical (ISM) band.

IEEE 802.11g was published in 2003, and it has a maximum theoretical data bit rate of 54 Mbit/s in the 2.4 GHz ISM band. This was only possible in the 5 GHz band (802.11a) before this standard were published. 802.11g is backwards compatible with 802.11b hardware, and are thus sharing many of the same characters and qualities. For a data rate of 1 and 2 Mbit/s, 802.11g uses DBPSK/DQPSK+DSSS for modulation, for 5.5 and 11 Mbit/s it uses CCK, and for data rates 6, 9, 12, 18, 24, 36, 48, and 54 Mbit/s it uses the same technique as 802.11a - OFDM. Even though 802.11b and 802.11g operate in the same frequency band, it is because of the modulation technique 802.11g have "copied" from 802.11a, that makes it achieve greater data rates.

The IEEE 802.11n standard have at the time this was written (09.05.2009) not yet been published. It is expected to be published in November 2009, and is significantly going to improve network throughput over wireless LANs with a theoretical data rate of up to 600 Mbps. This is possible by using a new method called Multiple In, Multiple Out (MIMO), which is going to be one of the big advantages with IEEE 802.11n.

The 802.11a/b/g standards are used differently in many countries because of regulations to the operating bands (2.4 and 5 Ghz). In Norway, The Norwegian Post and Telecommunications Authority² (NPT) is the regulator, and have allowed[30] use of these standards in the following frequencies; 2400-2483.5 MHz, 5150-5350 MHz and 5470-5725 MHz. This means in practice that you have a maximum of 3 non-overlapping channels in the 2.4 GHz band; for example channel 1, 6 and 11 for use with 802.11b/g. For the 5 GHz band there are 22[27] non-overlapping channels for use with the 802.11a standard. Without going into too much

²http://www.npt.no

details, the different frequency ranges mentioned above have some additional requirements in for instance, transmitting power and channel spacing.

Wi-Fi is, in addition to RFID, one of the most widely adopted technologies in IPS systems. IPS through Wi-Fi, is a simple way of re-using existing infrastructure, and the installation of such systems are often simple. Wi-Fi-IPS systems are often combined with the RFID technology to increase the accuracy.

2.1.3 Ultrasound

The term *Ultrasound* describes a vibration of cyclic sound pressure which are similar to sound waves, but with a frequency higher than the upper limit of human hearing. Although this limit varies from person to person, it is approximately between 10-20 kHz [3]. For any given person this threshold frequency decreases with increasing age. The study and applications of these vibrations are called *ultrasonics*. Some animals have a higher upper frequency limit than the human ear, and can thus hear ultrasound. Some examples are bats, cats, dogs, mice, and dolphins. Ultrasound frequencies just above the audible range share most of the same properties as human speech [12].

Ultrasound are today used in a wide range of applications, such as in *sonography*, at frequencies between 1-15 MHz. Sonography is used routinely during pregnancy to, among other things, determine the sex of the baby. Another common use of ultrasound is in range finding, called SONAR³, where an ultrasonic pulse is generated in a particular direction. SONAR works similar to RADAR⁴. Various industries use ultrasound, often in the range of 2 to 10 MHz, to either find flaws in materials or to measure the thickness of objects.

In the recent years, Ultrasound Identification (USID) have been used to automatically locate or track objects and assets in a given area indoor. Tracking and locating is done by having inexpensive badges/tags attached to objects or assets, which transmits an unique sound usually between 35-45 kHz to receivers (microphones) nearby. Based on this sound, the system can locate the asset or object. Sound is usually measured in *Pascal (Pa)*, but is often written as *Decibel (dB)* in relation to a standardized pressure of 20 µPa. Propagation speed of sound through air is approximately 340 m/s, but this varies with the air pressure,

³Sound Navigation And Ranging

⁴Radio Detection And Ranging

temperature and humidity [12]. A USID system typically uses a pressure up to 115 dB, because of several noise sources in the ultrasound specter [12]. Ultrasound waves reflects very easily, and this is one of the reasons ultrasound is used in IPS systems.

2.1.4 Ultra-Wideband (UWB)

Ultra-Wideband (UWB), sometimes called an *Impulse Radio*, is an unconventional type of radio technology for transmitting information at very low energy levels by using a large portion (>500 MHz) of the radio spectrum. This makes UWB good for short-range high-bandwidth communications. UWB transmits short pulses with sharp transitions, without carrier (baseband). A conventional radio is modulating a carrier giving a narrow spectral peak[35]. The difference between normal radio and UWB is shown in the figures[35] below:



Figure 2.1: Time and frequency use of a conventional radio

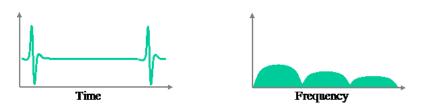


Figure 2.2: Time and frequency use for a UWB radio

UWB differs from narrowband (NB) and spread spectrum (SS) RF technologies, such as Bluetooth and WLAN, because of the wider bandwidth usage. This makes UWB able to transmit more data in a given period of time than traditional technologies, although the energy output is less. An overview of energy output versus frequency range are shown in figure 2.3 [15]. UWB has a potential data rate proportional to the bandwidth of the channel, and the logarithm of the signal-to-noise ratio⁵.

 $^{^5 \}mathrm{Shannon's}$ Law

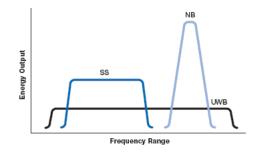


Figure 2.3: Narrowband (NB), spread spectrum (SS) and Ultra-Wideband (UWB) signal concepts

In 2002 IEEE authorized a PAR⁶ which goal was to agree on an personal area network (WPAN) UWB standard[11]. IEEE 802.15.3a Task Group (TG3a) were launched, and started out with 23 proposals for the physical layer (PHY) for UWB. They managed to consolidate the number of proposals into two, but then the process stopped. The task group was divided in half between these two proposals and each camp formed its own consortia, which was the WiMedia Alliance and the UWB Forum. WiMedia Alliance supported the MultiBand OFDM (MB-OFDM) UWB proposal, while the UWB Forum supported Direct Sequence UWB (DS-UWB).

⁶Project Authorization Request

INF5960

	MB-OFDM	DS-UWB
Bands	3-13	2
Bandwidths	3 x 528-13 x 528 MHz	$1.5~\mathrm{and}~3.6~\mathrm{GHz}$
Frequency ranges	3.1-10.6 GHz	3.1 - 5.15 and
		$5.825-10.6 { m GHz}$
Modulation	OFDM-QPSK	M-BOK, QPSK
Mod. efficiency 10^3 BER	$6.8~\mathrm{dB}$	4.1-6.8 dB
Error correction	Convolutional	Convolutional and
		Reed-Solomon codes
Margin at 10 m	$6~\mathrm{dB}$ at 110 Mbps	$6~\mathrm{dB}$ at 112 Mbps
Margin at 4 m	11 dB at $200 Mbps$	$11~\mathrm{dB}$ at $224~\mathrm{Mbps}$
Margin at 4 m	$6~\mathrm{dB}$ at 480 Mbps	$6~\mathrm{dB}$ at 448 Mbps

Table 2.1: The two UWB proposals [32]

Since none of the two proposals could get the needed majority of votes needed, the task group were dissolved in January 2006 after 3 years with a jammed process. As a result, there wont be a IEEE UWB standard, at least not known at the time of writing (28.04.2009). This is not the first time there has been similar problems in IEEE task groups (TG). The same thing happened with Bluetooth for example. The task groups of 802.11g and 802.11n had similar differences but managed to agree in the end. As a result of the IEEE 802.15.3a task group resolution, WiMedia Alliance and UWB Forum continued to work further with their proposal, and tried to promote their proposal for use in UWB products. In 2007, WiMedia Alliances UWB proposal was adopted as ECMA⁷ International standards, called ECMA-368 and ECMA-369:

- ECMA-368 High Rate Ultra Wideband PHY and MAC Standard[16]
- ECMA-369 MAC-PHY Interface for ECMA-368[17]

The 3^{rd} edition of the standards were published in December 2008. Shortly after the ECMA-368 and ECMA-369 standards were published for the first time, ISO/IEC adopted the stan-

⁷European Computer Manufacturers Association - http://www.ecma-international.org/

dards, as ISO/IEC 26907[21] and 26908[22] respectfully.

In Norway, NPT have not yet regulated use of UWB technology (as of 28.04.2009), and there are only a few documents published by NPT concerning UWB. In 2004 they published a document describing the *Strategic Goals for Frequency Management*[29] in the future, and here UWB had its own section. They basically conclude that they will await EU regulations of UWB, in addition to the results of CEPT⁸ and ETSI's⁹ standardization work for UWB in Europe. In 2009, NPT published an *Action Plan 2009*[31], describing what they will focus on in 2009-2011. In this document they stated that they would work for the introduction of UWB in Norway, "...without creating harmful interference to other radio systems".

In Europe, the work of regulating UWB have come further than in Norway, although the regulations are not finished and is still an ongoing progress[6] by CEPT/ECC after a mandate by the European Commission (EC). So far, the regulation work have concentrated on indoor use of UWB equipment. They want to minimize the outdoor use because of the risk for interference. For indoor use, they have regulated different power density throughput and different mitigation techniques in the frequency range 3.4 - 4.8 GHz and 8.5 - 9.0 GHz. It is expected that this frequency range will be expanded as the ongoing regulation work proceeds.

In USA, FCC^{10} have regulated a greater use of high power density throughput than Europe, on a wider range of frequencies. UWB can in the USA be used in the frequency range of 3.1 - 10.6 GHz.

UWB technology can enable a wide variety of WPAN applications [15] because of its high bandwidth possibilities at short range, such as ad-hoc connectivity between mobile devices or replacing the USB cable with high-speed wireless universal serial bus (WUSB) connectivity for PCs, printers and external storage devices. Because of its performance properties, UWB have also been adopted for use in IPS systems.

⁸European Conference of Postal and Telecommunications Administration

 $^{^9\}mathrm{European}$ Telecommunications Standards Institute

¹⁰Federal Communications Commission

2.2 Real-Time Locating System (RTLS) standards

IPS is as earlier mentioned a type of a RTLS system, and since there are no available standards at the moment only for IPS, the RTLS standards are presented instead. They share most of the same properties, and the biggest difference is that RTLS systems includes outdoor positioning while IPS are obviously only for indoor use. The standardization work for RTLS systems are still in its early phases, and the standards that have been published so far only explains lightly the basic issues of an RTLS system. These standards have been published by ISO/IEC, which is the International Organization for Standardization¹¹ and the International Electrotechnical Commission¹². Here is a list of the published RTLS/locating standards so far:

- ISO/IEC FDIS 19762-5[18] Information technology AIDC techniques Harmonized vocabulary, Part 5 Locating systems
- ISO/IEC 24730-1[19] Information technology real-time locating systems (RTLS) Part
 1: Application Program Interface (API)
- ISO/IEC 24730-2[20] Information technology real-time locating systems (RTLS) Part
 2: 2,4 GHz Air interface protocol (WhereNet/Zebra approach).

ISO/IEC FDIS 19762-5 addresses the vocabulary used concerning RTLS systems. According to this standard, a RTLS system is a combination of hardware and software that is used to *continuously* determine and provide the real-time position of assets and resources equipped with devices designed to operate with systems. Hence, the current layout of this ISO/IEC standardization by definition does not cover all types of discontinuous locating systems, like simple passive RFID concepts.

ISO/IEC 24730 are divided into two parts which respectfully defines two air interface protocols in part two and a single application program interface (API) for RTLS in part one. Part one open up for 3rd party software developing. The API enables the possibility to retrieve location data and other information from the systems that support this standard.

¹¹http://www.iso.org

¹²http://www.iec.ch

The API uses well known XML-based standards including XML¹³ and SOAP¹⁴. SOAP is a protocol for exchanging XML-based messages over computer networks.

The second part describes as mentioned an air-interface protocol for RTLS systems. The air-interface protocol are divided into three sections[24]. One addresses the tag-reader air-interface at 2.4 GHz and defines a location system providing x and y coordinates. The second section describes the air interface for low-frequency devices known as exciters, roughly around 120-125 kHz. Exciters are usually placed outside doors to provide 100% room or floor accuracy. And the third section describes a third interface, known as an On/Off Key (OOK). The OOK enables an active 2.4 GHz RTLS tag to communicate with a simple hand held reader. The system is designed for good coexistence with other wireless services in the 2.45 GHz ISM band, and is based on a system from *Zebra WhereNet*.

Part 3 was supposed to standardize Air Interface at 433 MHz (RFID systems) for use in RTLS, and in part 4 the goal was to incorporate Global Locating Systems into RTLS, but both projects are withdrawn[2].

Part 5 is still under development, but refers to the standardized communication according to IEEE 802.15.4a Chirp Spread Spectrum (CSS). CCS is a spread spectrum technique that uses wideband linear frequency modulated chirp pulses to encode information¹⁵. It was originally designed to compete with Ultra-Wideband (UWB) for precision ranging and low-rate wireless networks in the 2.45 GHz band, but is no longer actively being considered by IEEE for standardization in the area of precision ranging.

2.3 Real-Time Locating System (RTLS) methodologies

There exists a numerous methodologies for retrieving values that can be used in a locating engine to calculate a person or an assets position. Only the most widely used methodologies will be explained.

¹³eXtensible Markup Language

¹⁴Service Oriented Architecture Protocol

¹⁵IEEE Computer Society, (August 31, 2007). IEEE Standard 802.15.4a-2007

2.3.1 Received Signal Strength Indication (RSSI)

The Received Signal Strength Indication (RSSI) method measures the signal strength from a tag or device to several sensors or receivers. It then determines the tag/device position based on the measured RSSI values from at least 3 sensors/receivers.

This can be done using either a *fixed* mode or by creating a *mesh* of the area. In fixed mode, the measured RSSI values are converted into a distance measurement using a fixed path loss model. The path loss model shows the expected path loss in signal strength at a given distance, shown in dBm, which is in relation to 1mW. The distance is then used in a trilateration algorithm to determine the correct position between three or more receivers. Because a classic path loss model does not take walls and other obstacles into consideration, fixed mode may not be the most accurate mode available. There exist however more advanced methods which try to take this into account to some degree.

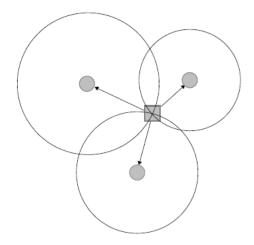


Figure 2.4: Trilateration [9]

One of the problems with trilateration are when the conversion between RSSI value to distance is inaccurate. The RSSI from each AP is turned into a distance, and used as the circles radius in the trilateration. In reality, the same RSSI value may be measured at different distances from the AP because of walls and other obstructions in the environment. This will obviously result in an inaccurate trilateration result. An example of uneven distribution of RSSI values are shown in figure 2.5.

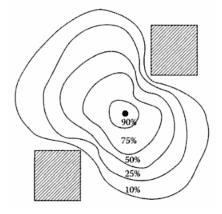


Figure 2.5: RSSI pattern example because of interference from obstructions and other sources

When using a mesh, the area you want to locate assets or devices in are distributed into a grid. Before it may be used, an "offline" phase has to be performed by using multiple tags as reference tags which are placed on the pre-defined grid. For the remainder parts of this thesis, a tag is defined as a small Wi-Fi unit which transmits small beacons packets to access point in range. Next, the RSSI values are measured at each point, for each receiver in range. Since you know the exact position of each reference tag, the real position is fed to the system along with the measured RSSI values, creating a *RF fingerprint*. Since the location engine only need to compare a tag or device's measured RSSI value with its database, mesh should in theory give a higher accuracy then fixed mode, specially in environments with a lot of obstacles. The size of the grid determines how accurate the resulting position will be. A small grid should give better accuracy, but it is also more time consuming. RSSI is usually used for indoor positioning.

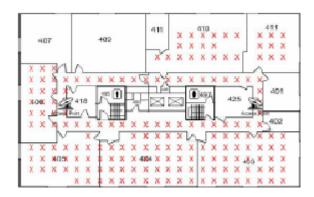


Figure 2.6: Example of an area where RF fingerprinting is used [28]

2.3.2 Time Difference of Arrival (TDoA)

Time Difference of Arrival (TDoA) use, like the name indicate, the time difference between the arrival of the transmitting tag signal to the various receivers. To be able to find the difference in arrival times, the receivers need to record the time when the signal arrived. The recorded times are then forwarded to the locating engine which calculates the difference in arrival time. The time difference is then transformed through an algorithm to provide an approximately distance from each tag which is used to find the estimated position of the tag. The TDoA method could be seen as the intersection of hyperbolas (hyperboloids in 3D), and mathematically the tag is located at the intersection of 3 hyperbolas in a 2D plane, and at the intersection of 4 hyperboloids in a 3D space [9].

TDoA is usually used in RTLS systems for outdoor tracking or localization, because it require the tag or device to be in Line of Sight (LoS) to the receivers. Time synchronization is a problem with TDoA. Since the locating engine compare the difference of time arrival from each receiver, it is very important that all the receiver clocks are synchronized. According to [26], the system will be 30 cm less accurate, for *each* nano second in synchronization difference, between the receiver clocks. TDoA works best with no obstacles, and is thus usually used outdoor.

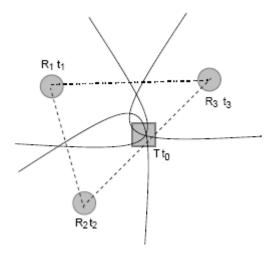


Figure 2.7: The Time Difference of Arrival (TDoA) method [9]

2.3.3 Time of Arrival (ToA)

The Time of Arrival (ToA) method, sometimes called Time of Flight (ToF), is a method based on the measurement of the propagation delay of the radio signal between a transmitter (tag/device) and one or more receivers (readers/sensors). The propagation delay is basically the amount of time it takes for a radio signal to travel from a source tag (TX) to its destination reader (RX) [9]. It can be calculated using $t_1 - t_0$, and figure 2.8 shows the basic principle of ToA. After all receivers in range have calculated its ToA, the ToA values are converted into distance by multiplying the propagation time $(t_1 - t_0)$ with the propagation speed of the signal. The distance values are then being used for trilateration. Trilateration requires data from at least three receivers to work.



Figure 2.8: The Time of Arrival (ToA) method [9]

Since ToA and TDoA share many similarities, they also share the time synchronization problem. To be able to get the highest possible accuracy when using this method, it is very important that the calculated propagation delays are comparable. To achieve time synchronization with precision up to a nanosecond would be very costly, and would result in a very high cost [9] for the RTLS system.

2.3.4 Angle of Arrival (AoA)

The Angle of Arrival (AoA) method determines the direction of a RF signal propagation received from a tag at a receiver (reader). This is possible by using direction sensitive antennas on the receivers [9]. The AoA value is determined by measuring the angle between the received signal and a pre-defined direction, for instance north. This is illustrated by the readers R1, R2 and tag T in figure 2.9.

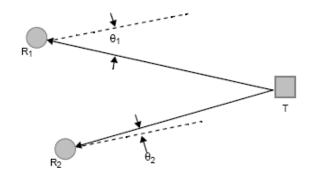


Figure 2.9: The Angle of Arrival (AoA) method. [9]

According to [9], taking measurements using this method often requires a complex set of between 4 and 12 antenna arrays situated in a horizontal line at all cell site locations. The accuracy of this method increases with the number of antennas used, but is also a more time consuming and costly process.

Chapter 3

Requirements

There are several challenges surrounding IPS systems. The technologies explained in section 2 have different pros and cons, depending on the intended use. Some usage areas have greater demands to the systems than others, and thus the underlying technology. In this chapter, several requirements are defined, based on the goal that an IPS system should be cheap, widely adopted and regulated, but still offer a good coverage and tracking accuracy to some degree. The importance of each requirement is dependent on the systems intended use and environment, which in this thesis are people or asset localization in office/class room environments. Some of the requirements have direct or indirectly relation to one or more of the other requirements.

3.1 Performance and reliability

3.1.1 Tracking accuracy

Depending on the intended use of a localization system, tracking accuracy may be one of the most important factors, and is thus a big challenge if there is a demand for high accuracy. The tracking accuracy differs from 15 cm to 10+ meters, depending on the technology used. However, the actual precision error in meters are not as important as the ability to determine what room the tag is in, and this are usually called *room separation* accuracy. Room separation accuracy is the likelihood of being in the room the system displays you in. If you are close to walls, the system may think you are on the other side of the wall (or on another floor), resulting in an unintended system behavior.

Requirement: Based on the intended use of a IPS system in this thesis, tracking accuracy should be at least within 5 meters, with room separation if possible. In other words, first the correct room should be chosen, and then the estimated accuracy should be no longer then five meters apart from the real position.

3.1.2 Coverage

Highest possible coverage area for each reader/receiver is important, since it indirectly have significance to another requirement which will be discussed later; *Cost.* Higher coverage from each receiver does also make the deployment easier, since you need less receivers and thus less cabling and configuration. With a small coverage area on the other hand, each receiver is more likely to receive signals from transmitting tags, and hence in theory increase the accuracy. This is because there will be more reference points to determine the location of the tag.

Requirement: In this thesis, coverage should be large enough so there wont be any need for multiple receivers in each room. If there are small office rooms right next to each other, the receiver should be able to handle more than one room.

3.1.3 Reliable transmission and interference

In positioning, it's very important for the location engine to get the best available measurements, at any time, so it is able to calculate a tags position based on the best data available. Interference may lead to lost packets, which can contain "good" measurements which again decrease the quality (accuracy) of the calculated position. With a high refresh rate in the user interface, lost packets may also result in a longer delay before the user interface can show the new tags position.

The uncertainty in reliable transmission comes from the physical medium used: wireless. The wireless medium have many advantages, like for instance in this context making positioning possible, but does also have some drawbacks since it are a shared medium. To cope with these issues, many technologies have built-in techniques to make sure that two parties do not transmit at the same time (for example *Clear Channel Assessment* (CCA) in Wi-Fi), to avoid possible interference. Interference are still a problem, since this only works for parties connected to the same receiver. A lot of consumer equipment like wireless phones, PC equipment and microwave ovens use the same frequencies as many IPS systems, and they can easily interfere with transmitting tags. It is hard, if not impossible, to remove the interference challenge completely, as long as a wireless medium is being used. In most cases a 100% reliable transmission are not required, the solution is thus to try and minimize the risk for interference instead.

Requirement: There should not be a major risk for interference, and if there are, it should not result in a dropped packet limit above 5% of all packets sent.

3.1.4 Fault tolerance

Fault tolerance is another reliability challenge when using IPS. What happens if a receiver in a given area stops working, and are no longer functioning properly? Usually the receivers overlap each other to some degree, hence the only problem is that the localization accuracy has decreased, but not all technologies works through walls. In areas where there are only one receiver, a worst case scenario could be that a person or asset wearing a tag are no longer able to be positioned, for instance in case of an emergency. Fault tolerance is hence an important design consideration and requirement in IPS.

Requirement: To be able to support a good fault tolerance, multiple receivers need to be able see the tag at any given position.

3.2 Regulations

All wireless technologies transmit and receive on one or more frequencies, occupying the frequencies in use in a given area. Since frequencies are a resource with limited capacity, it needs to be regulated by each country. Without regulations, wireless systems would have performed badly since the likelihood of interfering with other systems using the same frequency band would drastically increase. Although everyone agrees that frequencies should be regulated, it is done differently in each country. Also, regulations of new technologies in some countries are delayed compared to others because they want to see what other countries do first. *Requirement:* The chosen technology should be widely adopted by all countries, especially in Norway, and by that legal to use.

3.3 Standards

Standards make regulation across borders and 3rd party product development easier. It is also easier to combine IPS systems/technologies when they support common standards. There exists numerous standardization organizations across the world. The largest organizations are Federal Communications Commission (FCC) in USA, and ISO/IEC in Europe.

Requirement: There should exist widely adopted standards for the technology.

3.4 Cost

Since IPS systems use different technologies, they also vary in price. Lets take receivers for example, in addition to the price itself for each entity, the number of devices needed plays a significant role in the total price. Like pointed out in the *Coverage* section; the number of receiver devices needed depends on the coverage area by each receiver, which again affects the total price of the system.

The level of accuracy dies also play a significant role in the total price. First of all, different technologies achieve different accuracy, and are thus priced there after. Second of all, it can be more costly to deploy a IPS system where you want the highest possible accuracy, because you have to spend a lot of time calibrating the system for optimal use that environment. Some systems are easier to deploy than others (i.e. ultrasound versus Wi-Fi) since it don't need a frequency planning and a thorough calibration beforehand. This does also affect the total cost of the system.

Requirement: It is hard to set an exact cost limit for an IPS system, since cost is very relative, it is also depended on the budget you have, the intended use, and so forth. Cost is therefore in this context discussed in a high level perspective. For example, new technologies are often more expensive than widely adopted technologies that have been on the market for

a long time, but does not necessary give more value in relation to its performance. Therefor, the exact price difference is not relative in this thesis, but the technology gets a plus if the equipment is cheap.

3.5 Requirement summary

A summary overview of all the requirements defined above is shown in table 3.1. In section 4 *Technology assessment*, all the requirements in the table will be compared to all technologies presented in section 2.1 *Technology overview*. The technology that satisfies most of the requirements will be the chosen technology for the remainder parts of the thesis.

Туре	Requirement
Tracking accuracy	5m accuracy, and room separation
Coverage	Receivers need to cover at least 1 room. More is better.
Reliable trans. and int.	Maximum 5% dropped packets
Fault tolerance	More than 1 receiver needs to see the tag all the time
Regulations	Regulated in Norway
Standards	Widely adopted standards
Cost	Cheap equipment

Table 3.1: Requirement summary overview

Chapter 4

Technology assessment

In this chapter, the technologies that was briefly explained in section 2.1 (*Technology overview*) will be assessed in relation to the requirements in section 3 (*Requirements*).

4.1 Radio Frequency Identification (RFID)

RFID is used at small distances to identify people or assets leaving or entering a room/floor, often called an *exciter* or *chokepoint*. The tracking accuracy is therefore limited to room or floor positioning, and not where you are in that room or floor. While the positioning accuracy in meters decreases linearly with the size of the room, the room separation accuracy on the other hand is always 100%, independently of room size. A RFID IPS system alone would not fulfill the requirement set for tracking accuracy in this thesis.

Coverage is limited in an RFID system since its only purpose is to track a small area. Usual coverage area for a RFID receiver is approximately 20cm to 3-5m. It does therefore not meet the coverage requirement.

Depending on the system, RFID may operate at many different frequencies. AeroScouts¹ RFID solution for instance operates at 125 kHz[1] where there are low chance for interference. Because of its low range, the RFID system is not likely to cause interference for other receivers. RFID does therefore meet the interference requirement set.

The fault tolerance is none existing in RFID systems. If a receiver is not able to perform its task for some reason, people or assets entering or leaving the room would not be identified.

¹http://www.aeroscout.com

This would result in a wrong position for the person or asset on the user interface. The fault tolerance requirement is therefore not met.

RFID is not regulated in EU or Norway, but is still legal to use as long as its not interfering with existing equipment. This is mainly due to RFID's short range and coverage. However, [4] indicates that RFID needs to be regulated in the future as the technology and use of the technology evolves.

There exists numerous standards for RFID, depending on the usage, and the most important ones are briefly mentioned in section 2.1.1 (RFID). The huge number of different standardizations may however be a drawback for RFID, since it may result in different vendors using different standards. Despite this, RFID meets the standardization requirement set in section 3.3.

Although RFID is a widely adopted technology and the cost per product continues to decrease, it do require a lot of receivers to be deployed in the positioning area. Since all the doors in an area needs to have a receiver, the total amount of receivers may result in a high cost. In addition, cabling must be done to each door to connect the receivers to a centralized engine.

4.2 Wi-Fi

IPS systems based on the Wi-Fi technology usually achieves an tracking accuracy between 3-10m, depending on the environment and the positioning method used. In fixed mode, the accuracy depends on good models that reflects the environment the system are positioning in. This is clearly a difficult task and the accuracy are suffering from this. If a mesh map of the environment is created, with RSSI fingerprints of the entire environment with approximately 1m separation, it is possible to get a tracking accuracy as low as 3m (at average). Wi-Fi does not however guarantee room or floor separation. This can be solved by combining Wi-Fi with RFID, or by creating methods that increase the floor separation accuracy by using math logic. Wi-Fi is almost fulfilling the accuracy requirement.

Depending on the transmitted effect and the environment, the coverage in Wi-Fi systems are very good. According to the Wi-Fi Alliance², the Wi-Fi range in a office/light industrial setting is approximately 30-45m at 11 Mbps. This meets the coverage requirement.

²http://www.wi-fi.org/

Interference is one of the biggest challenges with Wi-Fi. The reason is mainly due to the frequency band the technology operates in, the ISM band. IEEE 802.11a does however not use this frequency band, but the use of IEEE 802.11b/g is far superior than the usage of 802.11a. Like mentioned in section 2.2 (Wi-Fi), the ISM band are also being used by other wireless equipment and can be used by anyone. This can cause interference that may affect the system significantly. Interference can to some degree be dealt with by doing a thorough channel planning in the environment you are operating in, but its impossible to control it completely. Wi-Fi does not satisfy the interference requirement completely.

Since coverage in Wi-Fi systems are very good, there may be overlap between Wi-Fi access points (AP) which gives a fault tolerance at an acceptable level. A tag needs to be in range of 3 or more AP's to be able to be positioned, but because of the good range from each AP this number may be 4 or more. This makes the Wi-Fi IPS system still able to position a tag even if one AP should fail. Based on this, the fault tolerance requirement is satisfied.

Wi-Fi is furthermore regulated for use in Norway in the ISM frequency band as mentioned above. This meet the requirement set.

Moving on to the standard requirement. IEEE 802.11 is the widely adopted standard for Wi-Fi and is a trademark from the Wi-Fi Alliance for hardware vendors, but it supports the standard by the IEEE organization. This requirement is therefore satisfied.

Wi-Fi is one of the most widely adopted technology around the world, which have resulted in cheap hardware. Since Wi-Fi AP's also have good coverage, there is no need for having AP's in all the small rooms. In addition, since most companies already have a wireless network infrastructure already in place, it is one of the cheapest technologies to use in a IPS system.

4.3 Ultrasound

Tracking accuracy in a ultrasound system is limited to room separation, and not where you are in the room. The reason for this is because the sound wave sent by the tag doesn't penetrate walls, so the only receiver that will hear the sound wave is the receiver in the same room as the tag. This means that ultrasound only satisfy parts of the tracking accuracy requirement.

The coverage area for each receiver is like stated above, the room the receiver is in, and nothing more. In theory, a receiver would be able to pick up a sound wave if it was penetrated through a wall, but this is usually not the case with ultrasound. This is however, also one of the advantages with an ultrasound system, depending on the intended use. In this context it does not satisfy the coverage requirement.

The main challenges in ultrasound communication are the large Doppler shifts, reverberation and background noise [12]. Doppler shift happens when the tag is moving at a given velocity relative to the receiver, and results in a small change in the wavelength. Reverberation is the lingering of sound in a room, once the source of the sound has stopped producing[12]. Background noise in a room may be everything from mechanic machines, normal conversations or music, to tinkling keys and slamming doors. They can all affect the transmission of sound waves, but the risk is not high. This satisfy the interference requirement.

The fault tolerance is the same in a ultrasound system as in a RFID system. Since the system depends on one reader in each room/area, the system will position the person or asset incorrectly if a receiver fails. This does not meet the requirement set.

Ultrasound are only sound waves that propagates through the air, and are therefore not regulated, at least to the authors knowledge. In addition, there exist no standards for ultrasound.

Since ultrasound is only sound, the main components you need are a microphone (receiver) and a speaker (tag), which is very cheap to make. Cabling are still needed to all the receivers, since an ultrasound IPS system is a centralized system, but it is still a cheap technology to use in an IPS system.

4.4 Ultra-Wideband (UWB)

Ultra-Wideband (UWB) is a new technology in IPS context, and there are not many commercial available products at the market. Ubisense³ and Timedomain⁴ were two of the first vendors of such products, and according to them an UWB system may provide an accuracy between 15-30cm at best. This definitely meets the accuracy requirement set.

The coverage area for UWB is limited by output power regulations, but are still able to reach approximately 50m despite its low power output. This is mainly because its unique strength to penetrate walls and objects. The coverage requirement is therefore satisfied.

UWB performs very good against interference because it uses short pulses as small as

³http://www.ubisense.com

⁴http://www.timedomain.com

2ns, which makes the wavelength less than 60cm. This makes the pulse arrive at its destination before it can self-interference with itself. In addition, UWB are thus resistant against multipath delays of more than one wavelength. UWB meets the reliable transmission and interference requirement.

The fault tolerance for UWB is similar to Wi-Fi. Because of a good coverage, and 5-10% overlap from other receivers, tag positioning should still be possible. The fault tolerance requirement is therefore met.

UWB may be a big interference source for other systems since it uses a wide range of the frequency spectrum (3.1-10.6 GHz), which are already regulated for other use. As a result, use of UWB has been prohibited in most countries. As explained in section 2.4, USA with FCC were the first to regulate and allow use of UWB systems. Norway have not yet regulated UWB, and it is therefore illegal to use in Norway at the time being (28.04.2009).

Providing a standard for UWB has been a difficult task, and because of disagreement in the work for a common IEEE standard there are now two proposals, each provided and supported by different vendors. The standardization process for UWB will continue, and it is very likely that a new standard is going to be available in the future. UWB does only partly satisfy this requirement since the standardization process its still in its early stages.

Since the UWB technology is very new in IPS context, the available products are thus priced there after. In other words, UWB IPS systems are very costly and is going to stay that way until the technology and products get more mature.

4.5 Choice of technology

RFID is a simple technology, that makes up an easy and cheap IPS system, but this is also the drawback. The technology doesn't achieve high enough "score" when comparing it to the requirements in section 3.

Ultrasound satisfy almost the same requirements as RFID, and vice versa. Ultrasound is also an inexpensive technology, but is only able to achieve room level separation accuracy.

UWB have the best tracking accuracy, but the lack of regulations and standards, in addition to a high cost, makes it not mature enough for use at the time being. UWB will however, clearly be the technology for the future when the missing pieces have been sorted out. Based on the requirement set in section 3, the technology that satisfied most of the requirements are Wi-Fi. Wi-Fi is therefore the chosen technology for the remaining parts of this thesis. It is also easier to obtain Wi-Fi equipment for testing purposes than the other technologies assessed. This have also affected the technology decision.

It is inspirational to see that it's possible to make an IPS system that re-use existing wireless infrastructures to also perform positioning tasks. Although Wi-Fi offer inexpensive hardware to IPS systems, it is not the technology with the highest accuracy. This is mainly because RSSI was never intended to be used in this context. RF fingerprinting increase the accuracy compared to fixed mode, but since it is a time consuming (and costly) process to build a fingerprint map, some of the point with cheap hardware disappear. The goal is to build a test program that uses "fixed" RSSI models and positioning methods that performs close to the accuracy given by RF fingerprinting methods (3-5m), but with limited deployment costs. To be able to test RSSI models and positioning methods, a testing program is needed.

Chapter 5

Building a test program

A test platform needs to be built before RSSI models and positioning methods/techniques can be implemented and tested. Originally, the plan was to code a small program on top of AeroScout's API, since we have an AeroScout system available at school. It quickly turned out however, that the API was only able to give (x, y) coordinates, and not the actual RSSI values. The coordinates have already been calculated by RSSI algorithms/models implemented by AeroScout, and it was therefore not possible to do the testing I wanted. As a result, I decided to build a positioning program from scratch where I could do the testing I wanted.

In this chapter, an explanation is given on how the RSSI values were retrieved before a positioning program could be build in section 3.1 (*How to get RSSI values*). In the next section, the positioning program is presented in section 3.2 (*About the framework*), and the different logic and math used to calculate a tags coordinate by the results from the RSSI models are presented in section 3.3 (*Implemented positioning logic*).

5.1 How to get RSSI values

Except for minor programming challenges in the making of the test program, the biggest challenge was by far how to retrieve RSSI values into the program. Of course, without RSSI values positioning would not be possible, and the program would have had no function. Finding a solution to this problem were very time consuming and took a huge part of the total amount of time spent on the entire thesis. The original goal was to be able to locate all devices with a Wi-Fi adapter. The first plan was to use SNMP¹ to retrieve the RSSI values from the AP's. It was however soon clear that the only SNMP MIB² available on the AP's used in this thesis, were only able to pass the RSSI for the associated clients to each AP, and not all devices/clients in range. Since each client is only able to associate to one AP at a time, trilateration would be impossible. This could however be solved by making a script that turns the radio on/off on all AP's except one, and then change the AP that is on with a five second interval. This would make the clients automatically connect to the AP that is on, as long as the same SSID is used. This solution would first of all be very inaccurate, since it would take a long time before the program has enough RSSI values to perform one position estimation. Second, this would destroy the possibility to use AP's for other tasks at the same time, like Internet or network sharing. The latter is an important point, since making existing equipment to perform more than one task is one of the main reasons for using Wi-Fi in this thesis.

Another solution to retrieve RSSI from clients, is to make a software that needs to be installed on all the clients, which measure how the clients "sees" all the AP's. The RSSI values are then passed to the location engine/server. The first problem with this solution, is that every AP needs to have different SSID's. If not, the client only stores the AP with the best signal strength for the given SSID. The second problem is the need for installing software on all the clients. It is also unsure how accurate this solution would have been, since for example a PC with Windows operating system displays the RSSI values in % and not dBm. The values are therefore needed to be converted, and I was unable to find an accurate conversion method in my research.

I decided to use tags from AeroScout, which we already had available at school, since they worked fine in AeroScout's own Wi-Fi positioning solution. The tags do not associate with any AP, but transmit beacon packets at given intervals depending on the tag is in motion or not. The beacon packet is transmitted to the multicast address 010c.cc00.0000. All AP's were configured to listen to this multicast address, measure the RSSI from the received packet and forward a 39 bytes packet to the location server running the positioning framework at port 12091. There were no documentation of the data packet format available at the web, to my knowledge. AeroScout didn't want to help either, and said it was because they had a

¹Simple Network Management Protocol

²Management Information Base

company policy to not reveal this kind of information. This gave me a big challenge; what byte(s) contain the RSSI value? I had to try and find it out myself. First, I captured a lot of packets coming from the AP's using *Wireshark*.

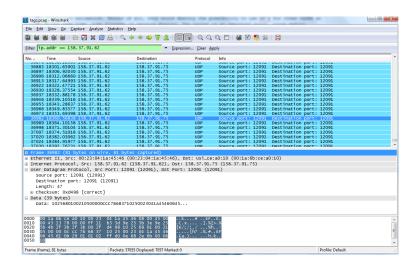


Figure 5.1: Packets containing RSSI values from AP's captured in Wireshark

It was easy to find the correct bytes for the tags MAC-address in the packet, but it turned out to be a lot harder to find the RSSI value. The data part was copied from several packets to a text file, to compare and find the bytes that change in relation to changes in distance between the tag and AP. This test decreased the unknown bytes from 39 to 5 bytes, as shown in figure 5.2.

> 10:be;68:01:00:21:05:00:00:0c:cc:7b:68:37:10:be:00:23:04:1a:45:46:06:02:61:0b:2c:01:01:02:ff: (c:91:6b:08:06:00:06:00

> 10:ef:68:01:00:21:05:00:00:0e:ee:7b:68:37:10:ef:00:23:04:1a:45:46:06:45:61:0b:29:01:01:02:ff: (b:94:53:4b:c4:00:06:00

10:d1:68:01:00:21:05:00:00:0c:cc:7b:68:37:10:d1:00:23:04:1a:45:46:06:02:61:0b:29:01:01:02:ff: cc:95:9a:0b:20:00:06:00

10:1b:68:01:00:21:05:00:00:0c:cc:7b:68:37:10:1b:00:23:04:1a:45:46:06:45:61:0b:29:01:01:02:ff:

Figure 5.2: WDS packet analysis in search for the correct RSSI byte

All the 5 bytes changed when the distance between the tag and AP changed. Hence, to be able to narrow it down more, I build a program that searched for similarities between 100+packets in the mentioned 5 bytes. The program searched after values in both % (18 to 100) and dBm^3 (-10 to -94), since I didn't know the correct RSSI value format. I also didn't know if I were looking for 7 or 8 bits. 7 bits are needed to represent the numbers mentioned, but 8 bits are needed to represent a signed number. The big question was also, how is that signed value represented in bits, if the RSSI value is in dBm? Sometimes the first bit represents an unsigned (0) or a signed (1) value, but the most common method is to use a method called *Two's complement*. All these formats and methods where coded into the "RSSI-finder" program and after a while it found similarities in the first byte using all 8 bits, with the dBm number range and the two's complement method for binary operations. Figure 5.3 shows a screenshot of the breakthrough.

convert hex to	eb:8f:f7:72:09	dc:91:6b:08:06	db:94:53:4b:c4	ce:95:9a:0b:2a	d9:c4:e7:0f:5a	cf:5f:c6:b9:96	
binary	111010111000111 111110111011100 1000001001	110111001001000 101101011000010 0000000110	110110111001010 001010011010010 1111000100	110011101001010 110011010000010 1100101010	110110011100010 011100111000011 110101101	110011110101111 111000110101110 0110010110	
Number of bits 8	-21	-36	-37	-50	-39	-49	[%
1	-41			-99			+
Minimum value [%]	- <u>82</u> -164	-142	- <u>146</u> -36	- <u>198</u> -140	-153	-195	
10	-72	-55	-71	-23	:100	-11	
Maximum value [%]	-143	-110	- <u>142</u> -27	-46	-200	- <u>21</u> -41	
100	-57	-184	-54	-140 -23 -46 -91 -182 -107	-30	-81	
	-113	-111	-108	-10/	-60	-161	
convert unsigned binary to decimal	-193	-187	175	-213 -170	-237	-129	
	-129	-117	-94	-84 -167	-217	-2	
	2	-211	-118	-77	-100		
	35	-166	-236	-154	-199	-15	
	.9	-149	-173	-102	-25	-58	
	-18	-42	-90	-204	-50	-115	
	-143 262 457 1122 1122 1122 1122 1122 1122 1122 11	-168	-102	-48	-200	-203	
	-137	-80	-204 -151	-96	-144	- <u>149</u> -41	
Number of bits 8	-36	-62	-46	-126	-61	-82	
Minimum value [dBm]	-142	-124	-91	-251	-121 -241	-164	
-94	-28	-240	-105	-234	-226	-141	
Maximum value (dBm)	-06	-224	-209	-212	-195	-26	
-10	- <u>142</u> -28 -56 -56 -112 -224 -191 -126 -252	21122 2232 2355 2355 2355 2357 2357 2357 23	2月18日 第二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十二十	777 154 51 102 204 205 205 205 205 205 205 205 205			
-10	-126	-255	-130	-54	-42	-155	
convert signed	-252	-253	-30	-107	-83	-53	

Figure 5.3: Finally, the RSSI value "revealed" itself in the 8 first bits using two's complement

5.2 About the test program

Building the positioning program from scratch took a lot more time than first expected, but were at the same time a nice learning process. The total amount of code lines in the program are approximately 4500 and were written in Microsoft Visual C# (2008). Visual C# were chosen because it's the programming language I am most experienced with.

The program can be divided into three main phases: the configuration and calibration phase, the positioning phase, and the data collection phase. The configuration and calibration phase is where the user enters all the data needed to find a tags position. In step 1, the user enters the IP address for all the available access points. A scan is then performed to find any

³Effect in decibel (dB) in relation to milliwatt (mW)

available tags to locate. The user then selects the tag it want to locate, as shown in figure 5.4:

About guration locess Points	Access Points - Step 1 Next >	Positioning model - Ster	0 2 < Back Next >	Map Configuration - Step 3	< Ba
os. methods	Add Access Points and choose client to locate	Choose and configure a RSSI method / m		- Configure a floor map	< Da
lap alibrate	Access Point IP address: Add Remove	ITU Indoor Propagation Model	Info: The log-distance path loss model	Add map and preview:	Brow
ns tor	IP address MAC address Status	Log-distance path loss model Measurement fitration Border check	is a radio propagation model that predicts the path loss a signal encounters inside a building or		
	158.37.91.61 0023.041a.3855 Connected 158.37.91.62 0023.041a.4546 Connected 158.37.91.63 0023.041a.45ab Connected 158.37.91.64 0023.041a.375c Connected	Wall check Wall attenuation Speed filtration Statistical position estimation	densely populated areas over distance.		
	Connect	Parameters		T T	Ĩ
	Select a tag to locate:				
	MAC address RSSI [dBm] Connected to AP	Tx 19 dBm		Rotate map: 0 degrees	Calibra
	000c.cc7b.4694 -62 158.37.91.64	Gain Tx 0 dBi	Antenna Gain transmitter	Listate map:	Map confid
	-54 158.37.91.61 -53 158.37.91.62	Gain Rx 2.2 dBi	Antenna Gain receiver Reference distance	Refresh rate: 1 second 👻	map coring
	-62 158.37.91.63			Hondarridio.	
		N 2 Wavelength 0.122 m	Path Loss exponent Frequency wavelength		
		PL(d_0) 67.6 dBm	Average PL at distance d 0		

Figure 5.4: Selecting access points to use and tag to locate

In step 2, the user selects the RSSI model and positioning methods it want to use. Most of the methods requires data input from the user. A RSSI model is required to be able to convert RSSI values to distance. Positioning methods are used to increase the accuracy, but are not required for the program to work. RSSI models and positioning methods are explained in detail in section 6, *Positioning methods and models*. Figure 5.5 show the configuration step 2:

ile About				r	
Configuration Access Points Pos. methods	Access Points - Step 1 - Add Access Points and choose client to locate Next >	Positioning model - Step - Choose and configure a RSSI method / m		Map Configuration - Step 3 -Configure a floor map	< Back
Map Calibrate	Access Point IP address:	Available methods and models	Info:		-
Logs	Add Remove	👿 Log-distance path loss model	The log-distance path loss model	Add map and preview:	Browse
Graphs	IP address MAC address Status	Measurement filtration	is a radio propagation model that predicts the path loss a signal		
Locator	158 37 91 61 0023 041a 3855 Connected	Wall check	encounters inside a building or densely populated areas over		
	158.37.91.62 0023.041a.4546 Connected	Wall attenuation	distance.		
	158.37.91.63 0023.041a.45ab Connected	Statistical position estimation			
	158.37.91.64 0023.041a.375c Connected				
	Connect	Parameters			
	Select a tag to locate:	Tx 19 dBm	Transmitted power		
	MAC address RSSI [dBm] Connected to AP	Gain Tx 0 dB	Antenna Gain transmitter	Rotate map: 0 degrees 👻	Calibrate
	000c.cc7b.4694 -62 158.37.91.64	Gain Rx 2.2 dBi	Antenna Gain receiver		
	-54 158.37.91.61 -53 158.37.91.62	d 0 1m	Reference distance	Refresh rate: 1 second -	
	-62 158.37.91.63	n 2	Path Loss exponent		
		Wavelength 0.122 m	Frequency wavelength		
		PL(d 0) 67.6 dBm	Average PL at distance d 0		
		PL(d_0) 62.2 dBm	"Best" PL at distance d 0		Locate

Figure 5.5: Select and configure positioning methods to use

In step 3, a map of the tracking area is being selected as shown in figure 5.6. Before the system can start locating the tag, the map needs to be calibrated. This is done by clicking

the *Calibrate* button, and the calibration form is shown in figure 5.7. Calibration is done by first drawing the borders on the map where you don't want the tag to be located outside. Secondly, the user tells the program where the walls are by drawing lines over the walls. Thirdly, a reference length is drawn on the map, and the real length is entered by the user. Fourth, drag and drop each entry in the AP table to the map at their given positions. Save the calibration settings by clicking the *Save* button and choose the wanted positioning refresh rate. The maximum is 1 second. The configuration and calibration phase is now ended and it is now possible to find the tags position.

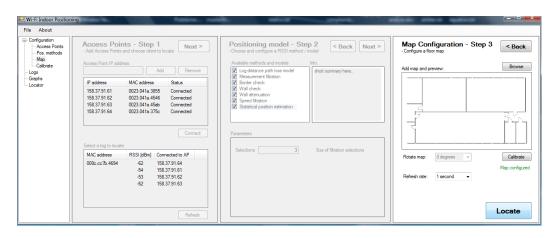


Figure 5.6: Selecting a map of the testing area

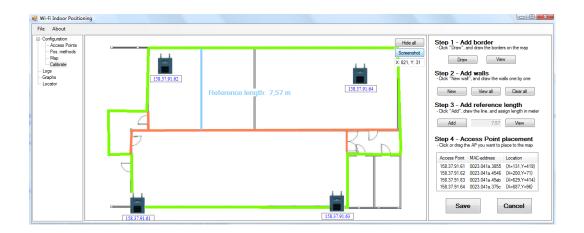


Figure 5.7: Calibrating/configuring the map

In the positioning phase, the selected tag is being positioned "real-time" at the configured refresh rate, by the chosen RSSI model and positioning methods. The user may *Stop* and

Resume the positioning at any time, or save a screen shot of a given moment. An example of this phase is shown in figure 5.8 below.

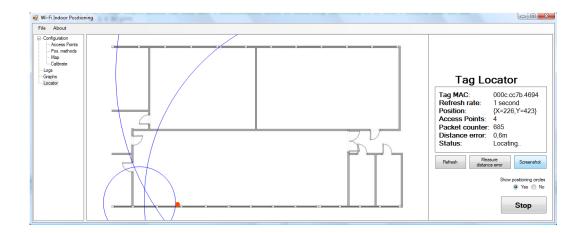


Figure 5.8: Example of the *Locator* screen, with positioning circles turned on

After the positioning phase is over, it's time to collect the data needed to evaluate the RSSI model and positioning methods used. All the configuration, calibration and positioning data are available in the *Logs* section. Measurements counter, error distances and other positioning data can be shown as graphs by clicking on *Graphs*. An example of the *Graphs* page is shown in figure 5.9.

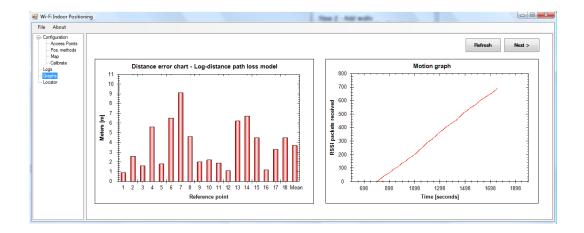


Figure 5.9: Example of the *Graphs* screen

5.3 Implemented trilateration logic

Next, when the program has received enough RSSI values, it passes the values on to the RSSI model. After the RSSI model have calculated the distance from each AP to the tag, trilateration is performed to estimate the tags position. In theory it is pretty straight forward, but in reality you also have some exceptions that needs to be handled.

First, the calculated distance between each AP and tag is used as the radius in a circle surrounding the AP. By comparing two and two "AP circles", we find the intersection points - if any. If the RSSI model is inaccurate, the two circles may not intersect. In these cases, a virtual line between the center of the first circle, and the center of the second circle is drawn. The line intersect with both circles, and the center point between the first intersection and the second intersection is selected, as shown in figure 5.10b.

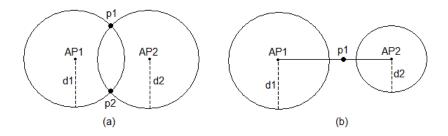


Figure 5.10: Example of two intersecting circles in (a), and no intersection points in (b)

The same process is repeated for all possible combinations of the AP's that was in the tags range. Ideally, at least three intersection points should overlap each other, and thus "reveal" the tags position, but no RSSI model is that accurate. In "real-life" the distance between the closest intersection points will vary, and thus not overlap. Estimating the mean position (\bar{X}, \bar{Y}) between the closest intersection points is thus the best solution to find the tags position:

$$\bar{X} = \sum_{i=1} X_{Pi} \qquad \bar{Y} = \sum_{i=1} Y_{Pi}$$
 (5.1)

42

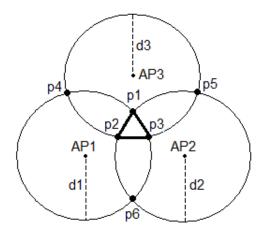


Figure 5.11: Trilateration example with three access points

Chapter 6

Positioning methods and models

In this chapter, different RSSI models and positioning methods are discussed. The positioning methods try to increase the accuracy of the RSSI model. First, the RSSI model *Log-distance path loss model* is discussed in section 6.1. Then, different positioning methods are proposed in section 6.2-6.7, ending with a summary in section 6.8.

6.1 Log-distance path loss model

The *log-distance path loss* model is a radio propagation model that predicts the path loss a signal encounters in a given environment over distance. Propagation models such as this one show that the average received signal strength decreases logarithmically with distance[8]. Since the received signal strength is measured by the AP's, the model is able to predict an approximate distance by comparing the received signal strength with the transmitted signal minus the predicted signal loss.

Log-distance path loss model is based on the *Friis free-space equation*[25], which gives the received power in free-space at distance d, with transmission power P_{tx} , antenna gain (G_t and G_r) at transmitter and receiver side, and with wavelength λ . The Friis free-space equation:

$$P_{rcvd}(d) = \frac{P_{tx} \cdot G_t \cdot G_r \cdot \lambda^2}{(4\pi)^2 \cdot d^2 \cdot L} = \frac{P_{tx} \cdot G_t \cdot G_r \cdot \lambda^2}{(4\pi)^2 \cdot d_0^2 \cdot L} \cdot \left(\frac{d_0}{d}\right)^2 = P_{rcvd}(d_0) \cdot \left(\frac{d_0}{d}\right)^2$$
(6.1)

Distance d has to be bigger than d_0 , since d_0 is a reference distance depending on the antenna technology. The exponential value 2 is for free space, so by changing the parameter

to n the model is slightly generalized and ready for use in other environments. Parameter n is also called the *path-loss exponent*, and typically varies between 2 and 6, where 2 is in free space and 6 are in obstructed building scenarios. An overview of different n values is found in table 6.1 [34].

$$P_{rcvd}(d) = P_{rcvd}(d_0) \cdot \left(\frac{d_0}{d}\right)^n \tag{6.2}$$

Environment	Path Loss Exponent, n
Free space	2
Urban area cellular radio	2.7 to 3.5
Shadowed urban cellular radio	3 to 5
In building line-of sight	1.6 to 1.8
Obstructed in building	4 to 6
Obstructed in factories	2 to 3

Table 6.1: Path loss exponents for different environments

Friis free-space equation shows that the received power depends on the frequency and distance among other things. The higher the frequency the lower received power, and visa versa. The longer distance, the lower received power since the radiated power would have to cover a larger area.

Since the path loss is defined as the ratio of the radiated power to the received power $\frac{P_{tx}}{P_{rcvd}(d)}$, the equation can be expressed in decibel as shown below [25], which is the log-distance path loss model.

$$PL(d)[dB] = PL(d_0)[dB] + 10nlog_1 0\left(\frac{d_0}{d}\right)$$
(6.3)

The predicted distance between a tag and AP is found by calculating the actual path loss, and is then inserted as PL(d)[dB] in the log-distance path loss model. The loss in dB at reference length d0 ($PL(d_0)[dB]$) have to be calculated first. The actual path loss is found by calculating a link budget, where the transmitted signal including antenna gain from both sides are compared with the received signal (RSSI) at the AP.

$$d = d_0 \cdot 10 \left(\frac{P_{tx} - P_{rx} + G_{tx} + G_{rx} - PL(d_0)}{10n} \right)$$
(6.4)

Log-distance path loss model is a very simple model, and the only value that reflects possible obstructions in the environment are the path loss exponent n. Instead of predicting the loss in a given environment, the path loss exponent n is often "tuned" in beforehand to the right value to represent the path loss in the given environment. The model gives however, some level of accuracy in open environments. Several positioning methods will be made and used together with this model to try and increase the accuracy.

6.2 Measurement filtration method

When using RSSI values as input parameter in positioning models, one of the challenges is the big fluctuations in the received values, even at small changes in the tags position. Sometimes, the tag doesn't even have to move for the RSSI value to change. Changes in the environment has just enough impact on the measured RSSI value as the changes in the tags own position. Changes in the environment could be door being closed, people walking around or interference. The program receives therefore a lot of RSSI measurements that do not give a good picture of the real change in the tags position. This results in a lot of position estimation based on false data. Hence, the program need to have some sort of logic to filter out poor RSSI measurements before the program passes the values on to the RSSI models.

Therefor, a method named *measurement filtration* were created, which saves the last RSSI measurements from each AP in a table. Two options are available. The program can be told to always use the best RSSI measurement in this table, or the mean value. When a new measurement is available, delete the oldest one and put the new measurement in the table. The table size differs from when the tag is in motion or not. When the tag is in motion, the AP receives a new packet every second and is able to measure the RSSI every second. If the table were too big (i.e. 50+ measurements) and the tag were in motion, the RSSI values gets "old" very fast, and old measurements do not give a good picture of the new position. When the tag is not moving, the refresh rate of RSSI values are 10 seconds, and the best possible measurement available in a long time frame should be used since its not moving. Interference

does usually result in worse RSSI values than expected, and not better. It is possible to get better measurements than you should because of interference, but my own measurements (see appendix A) shows that this is rare. The best RSSI value would therefore often give the best picture of the tags position. Both the mean and "best" filtration option available in this method would also make the RSSI fluctuations less visible to the user while the tag is not in motion. The table size is set to 3 measurements when the tag is in motion, and dynamically increasing to ∞ when it is not in motion, by looking the time difference between the last two received measurements.

6.3 Wall attenuation method

Since the log-distance path loss model do not take into account signal attenuation for walls, a method named *wall attenuation* were created. The method performs two tasks; first the method finds the AP with the highest ("best") RSSI value, and adds the wall attenuation to the RSSI measurement from the other AP's that is entered into the testing program. The reason for this is that the system do not know where the tag is, and thus not know how many walls there are between the tag and the AP. Since there usually are only one AP in each room, it assumes that the AP with the highest RSSI value is in that room in this first phase, and the AP in this room do not add any attenuation. This will not always be true, but some assumptions must be made to add wall attenuation to the measurements. The goal in the first step is not to estimate the correct position, but to increase the probability to estimate a position in the correct room.

After the first step, trilateration is then performed to estimate the tags room and position in that room. In step two of the wall attenuation method, the exact number of walls between the estimated position and each AP are counted. If there were more readers in the same room as the tag, the attenuation added in step one is removed. If there are more than one wall between the tag and AP, more attenuation is added in relation to the counted number of walls. Trilateration is once again performed after this step, and the estimated position should hopefully be more accurate.

6.4 Border check method

Although the *measurement filtration* method minimizes the significance of the worst RSSI measurements, there are cases where even the best RSSI measurement is not a good one. In other words, the best or mean RSSI measurement(s) may not always represent the correct signal loss, and the given distance from the tag to the access point. In a trilateration process, this would result in an in-accurate position estimation even when the two other measurements are correct. Hence, to try and correct this, a method named *border check* were created. The method performs two different tasks, and is thus a two-step phase. The first phase checks each estimated distance from each AP with the longest possible distance on the map. If the estimated distance is longer, it is changed to the max distance. After the first phase are done for all AP's, trilateration is then performed.

After the estimated position is known, the second phase determines whether the position is inside or outside the border drawn in the map calibration. Since the border drawn can be seen as a polygon, a method in computational geometry called *Point-In-Polygon* (PIP) is used. A polygon is defined as a plane figure that is bounded by a closed path, composed of a finite sequence of straight line segments. Point-In-Polygon checks whether a given point in the plane is inside or outside the border of the closed polygon. This is done by counting how many borders that needs to be crossed between a point entirely on the border of the map or figure, and to the position we want to check. If the number is un-even (1,3,5, etc.), the point is inside the border/polygon and the function returns *true*. If the counted number is even, (2, 4, 6, etc.) the point is outside the border/polygon and the function returns *false*. A Point-In-Polygon example is shown in figure 6.1. If the function returns false, a new function measures the closest point inside the border/polygon, from the estimated position point. The tags estimated position is then replaced with the new estimated position *inside* the border.

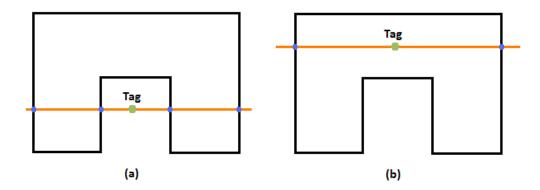


Figure 6.1: Point-In-Polygon examples: (a) is outside and (b) is inside, because of the straight lines even and un-even intersections with the border

6.5 Speed filtration

Although the impact of some of the big fluctuations in RSSI measurements are reduced by earlier methods, there are still situations where the tag is in motion and the estimated tags position vary greatly from estimation to estimation. Although it has only gone 1-2 seconds since the last estimation, it is possible that the next estimated position is far away from the last position. Obviously, one of the positions are wrong, since it is limited how fast an human being can move in a short time frame. To try and encounter this challenge, a method called *speed filtration* were created. The method assumes that the person wearing the tag moves at an average walking speed for humans, which is 1.33 m/s, plus an error margin of 10%. In other words, if the distance between the new position estimation is for instance 8m away from the current position, and it has only gone 3 seconds since the current position were estimated, the method rejects the new position estimation and keeps the current one. In the next position estimation, the time frame between the current position and the new estimation is bigger, and the method is thus allowing a bigger distance away from the current position. It is possible to change the allowed walking speed in the test program to a higher or lower value.

6.6 Statistical position estimation

To reduce the fluctuations furthermore, a *statistical position estimation* method were created. The method is similar to the *measurement filtration* method, but tries to increase the accuracy and reduce the fluctuations more by adding the estimated position to a table which includes the last three estimated positions, and then calculate the mean position based on this table. This may sometimes "destroy" correctly estimated positions by adding the mean values of a series of position estimations, but it will at the same time avoid big fluctuations which is the main goal.

6.7 Wall check method

Furthermore, the tags position can also be checked for being in the middle of a wall on the map. Walls are entered in the map calibration phase by drawing straight lines where there are walls. Since the drawn lines have only two points, the same Point-In-Polygon method as used in *border check* cannot be used directly. Therefor, the lines are converted into a polygon by calculating four corner points out of the start and end point of the wall line with a wall width of 3 points away from each point. For example, if a point is drawn from (10,10) to (50,10), the new corner points are respectively (10,7), (10,13), (50,7) and (50,13). The x-values would have changed instead if the wall line were vertically. The same Point-In-Polygon method as used in the *border check* method, can now be used after the line to polygon conversion. The method determines whether the tags estimated point is in a wall or not, and returns true if it is. If true is returned, a new function calculates the closest point in either of the room the wall separates, and changes the tags estimated position to this new position. If false, the tags already estimated position is kept.

6.8 Positioning method summary

This section will give an overview of all the mentioned positioning methods in the order they appear in the program. Some of the methods performs different tasks depending on when they are called, and are thus in use several times in just one position estimation. The first thing that happens in the program is a socket listening on port 12091 waiting for packets containing RSSI measurements. Next, the positioning methods appear in the order shown in figure 6.2:

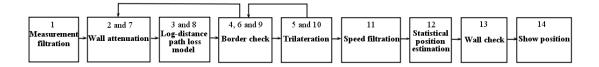


Figure 6.2: Positioning steps overview

In short, step 1 performs a measurement filtration, step 2 adds wall attenuation to some AP's the first time it is run. Step 3 calculates the distance according to the measured path loss. Then, the border check method in step 4 checks the estimated distance length the first time it is run, and reduce it if it is outside the border. In step 5 the tags position is estimated using trilateration. The position is then sent back to the border check method in step 6, and moved inside the border if it is outside. The border check method does then send the same (or changed) position to the wall attenuation method in step 7 which determines the correct number of walls between the estimated room of the tag and all the AP's, and are then adjusting the attenuation if necessary. In step 8 the adjusted RSSI values are sent back to the log-distance model which again estimates the distance. Moreover, the first process in the border check method is run again in step 9, and in step 10 the last trilateration process is performed and we have a new estimated tag position. Furthermore, in step 11, the newly estimated position is compared to the last approved position estimation, to see if the distance is too far away compared to the time frame between the estimations. If the position estimation is approved, step 12 calculates a mean position based on this position and the last three approved positions. Furthermore, step 13 checks to see if the final position is estimated to be on top of a wall on the map. It is moved outside the wall if it is. Lastly, step 14 shows the estimated position on the screen to the user.

A more thorough and detailed summary of these steps are found in a later chapter when the positioning methods are being evaluated.

Chapter 7

Test setup

In this chapter, a presentation of the test area is found in section 7.1, *Test area*, overview of the *equipment and hardware used* is found in section 7.2, furthermore are the *configuration* of the equipment and testing program found in respectively section 7.3 and 7.4.

7.1 Test area

All the testing are being performed in a test area with size 28,5m x 14,5m which contains one classroom, two labs and two hallways at the Bergen University College. Some of the rooms are separated by wooden walls, and some of the walls have areas with brick/concrete. All the rooms have wooden doors. Furthermore, each room has several big windows along side one of the sides. In addition, each room has been given a number, so its easier to understand which room is which before they are explained further:

Room type	Room number
Classroom	2
Labs	3 and 4
Hallways	1 and 5

Table 7.1: Room number overview

The classroom contain normal classroom interior like desks. The two labs have in addition to desks, also some cabinets. Especially the lab in room 3 on the map, which have cabinets along side the entire wall between room 3 and 4, in addition to three iron cabinets placed in the middle of the room with two meters separation. All other cabinets are composed of tree materials. The two hallways are just open spaces with no interior. It is expected that the signal loss in room 3 will be slightly higher because of all the obstacles in the middle of the room compared to the other rooms.

Furthermore, the testing area is limited in size because there were only 4 AP's available. Figure 7.1 shows a map of the test area, with room numbers.

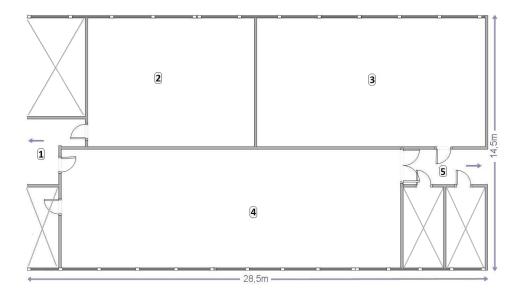


Figure 7.1: Overview of the testing area, 3rd floor, wing E at Bergen University College

The rooms marked with an X, are not part of the testing area. The arrows on the map indicates that the hallway continues in the given direction, but thats neither part of the testing area.

In addition, an important aspect that may affect the measurements done later are the possible sources of interference in the testing environment. Since the ISM frequency band is used, which are open for all to use, it is impossible to remove all these sources. Figure 7.2 shows all the broadcasting wireless networks in the testing area. A Lenovo program called *ThinkVantage Access Connections* were used.

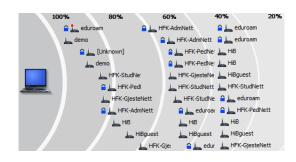


Figure 7.2: Overview of wireless networks in the testing area, seen by *ThinkVantage Access* Conn.

All the testing were done late in the evening in an attempt to reduce the surrounding wireless networks impact on the results. Hence, its likely that the only interference from these wireless networks are the broadcasted SSID¹ beacons which are transmitted at given intervals. Furthermore, there are to my knowledge, no other equipment in the testing area which occupies the same frequency band at the time of the testing.

7.2 Equipment and hardware used

An overview of the equipment and hardware used in the testing will be given in this section. First, four Cisco 1242AG Access Points were used as seen in figure 7.3, with two omnidirectional antennas at each AP with a 2.2 dBi gain.



Figure 7.3: Cicso 1232AG Access Point and 2.2 dBi omni-directional antenna

Furthermore, an 8-port Cisco Catalyst 2940 switch as seen in figure 7.4 were used to connect the AP's and the location server together, with a port speed of 100 Mbits/s.

¹Service Set Identifier



Figure 7.4: Cicso Catalyst 2940 switch

In addition, a Wi-Fi tag from AeroScout were used in the testing, which are named AeroScout T2 Tag.



Figure 7.5: AeroScout T2

Some of the technical tag specifications are shown in table 7.2.

	Dimensions	Weight	Radio	Transm. power	Compliant stand.
T2	62mm x 40mm x 17mm	$35\mathrm{g}$	2.4 GHz	$19 \mathrm{~dBm}$	IEEE 802.11b

Table 7.2: Aeroscout T2 and T3 tag specifications

Furthermore, in order to be able to configure the tags, *AeroScout Tag Activator* as seen on figure 7.6 had to be used in addition to the corresponding software *AeroScout Tag Manager*.



Figure 7.6: AeroScout Tag Activator

Lastly, a location server where the positioning framework were running was also used. The server were a Lenovo Thinkpad T61 running on Windows Vista 32-bits version with Service Pack 2 installed. The laptop had 2 GB memory (RAM) and a 2.20 GHz Intel Core 2 Duo processor (CPU).

7.3 Hardware configuration

The four Access Points were configured according to the IP address and frequency channel as stated in table 7.3, in addition to the CLI² commands below.

dot11 lbs rssitest multicast address 010c.cc00.0000 server address 158.37.91.75 port 12091 packet-type short channel-match interface Dot11Radio 0

²Command Line Interface

IP-address	Subnetmask	MAC-address	Channel
158.37.91.61	255.255.255.128	0023.041a.3855	1
158.37.91.62	255.255.255.128	0023.041a.4546	6
158.37.91.63	255.255.255.128	0023.041a.45ab	11
158.37.91.64	255.255.255.128	0023.041a.375c	1

Table 7.3: Frequency channel configuration on each AP

The CLI commands makes the AP listen to multicast mac-address 010c.cc00.0000 for tag-packets, and then forward the RSSI value to the location engine/server.

Only minimal configuration were done on the switch, and nothing that would affect the measurement performance. The only change done on the location server were the IP address settings which was configured to 158.37.91.75 with subnet mask 255.255.255.128. Global addresses were used since the network were connected to a UNINETT³ network which used global addresses in this range.

Moreover, the tag used in the testing were configured to transmit packets at a 1 second interval while it were in motion, and 10 seconds interval when not. The tag were also configured to transmit packets to the multicast address mentioned above, *010c.cc00.0000* at three different frequency channels: 1, 6 and 11. In addition, the packet format used were WDS, transmission power 19 dBm and a 1 Mbps data rate.

³The national research network in Norway

ransmission Parameters	
Message Repetitions:	1 •
Message Repetitions Interval [msec]:	512 👻
Transmission Power [dBm]:	19 👻
Signal Detect Threshold [dBm]:	-70
Transmit Diversity Sequence [Po	stamble]
Data Rate (Mbps):	1
Data Frame Format:	WDS -
Destination Address for the transmissi	ion of Tag location messages:
IBSS/WDS	01 0C CC 00 00 00
CCX	01 40 96 00 00 03
erial Interface Configuration	
Serial Baud Rate (bps):	19200 -

Figure 7.7: The tag configuration done on both tags in AeroScout Tag Manager

7.4 Configuring the test program

After the hardware had been set up correctly and configured, the testing program had to be configured. The path loss model and some of the positioning methods have different parameters that need to be set in order to function properly. In the path loss model, the middle frequency of the ISM band were chosen as the frequency which is 2 442 Mhz (0,122m in wavelength). In addition, $PL(d_0)$ were found by doing RSSI measurements at the reference distance (d_0) 1m, and then the actual path loss at this distance were calculated. Two values of $PL(d_0)$ where found; 55.2 dBm if the "Best" option is selected in the measurement filtration method, and 60.9 dBm if the mean value is used. Finding the correct $PL(d_0)$ were harder than expected. I had several AeroScout T2 tags available in the pre-phase of the testing, and although they in theory were supposed to be similar, the path loss at 1m varied greatly. Two of the tags had a difference in loss at the same reference distance of about 10 dBm. All the tags had one thing in common, they all had much bigger path loss than expected if you compare it to the theoretically measured path loss by Friis free space equation. Some increase in loss were obviously expected, but not 15 dBm more than the mentioned Friis free space equation. More details about the measurements can be found in appendix A.1. Moreover, parameter n, which is the path loss exponent was set to 2 which is the value for free space since the point was to make methods that takes attenuation of walls and other obstacles into account to try and increase the accuracy.

Furthermore, in the measurement filtration method the "best" RSSI value option was chosen because it gave the most accurate results in the pre-testing. Both the packet and position memory in the measurement filtration method and the statistical position estimation method were set to 3. Lastly, the wall attenuation method had to be configured, and after measuring the mean attenuation for all the walls in the environment, a wall attenuation of 4.4 dB were used. Details about the wall attenuation measurements can be viewed in more detail in appendix A.3.

Model or method	Parameter	Value
	T_x	19 dBm
	G_{tx}	0
	G_{rx}	2.2 dBi
Log distance path loss	d_0	$1\mathrm{m}$
Log-distance path loss	n	2
	λ	$0.122\mathrm{m}$
	$PL(d_0)$ - "Best"	55.2
	$\operatorname{PL}(d_0)$ - Mean	60.9
Measurement filtr.	Packet memory	3
Measurement mtr.	Filtration method	Use the "best" RSSI value
Wall attenuation	Mix of wood/concrete	4.4 dB
Speed filtration	Average walking speed	1.33 m/s
Statistical pos. estima.	Position memory	3

An overview of the propagation model and positioning method parameters are shown in table 7.4.

Table 7.4: Model and method parameters used in the testing

In the end, before the testing could take place, the map of the test area had to be configured/calibrated. The result can be seen in figure 7.8. The four Cisco AP's were placed in the test area as shown in figure 7.8, at 2,5m in height. It may seem like the two access points at the bottom is placed outside the room, but it is the center point of the AP icon on the map that matters. Furthermore, the border of the testing area is in green color, the walls in orange, and the reference length in a light blue color. While doing the wall measurements, one of the measurements showed that there where no or only minimal attenuation between one of the rooms. This is a thin wooden wall, and adding an attenuation of 4.4 dB to this wall would therefore give a wrong picture of the environment. The testing program were unfortunately not scaled for differentiated wall attenuations, and the wall was therefore not added into the program.

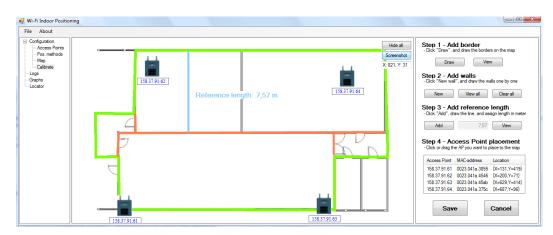


Figure 7.8: Map calibration in the testing program

Chapter 8

Test results and evaluation

8.1 Test results

The positioning tests were performed at 18 pre-defined reference positions and the mean position estimation from each reference point were used to calculate the distance error. Figure 8.1 shows the 18 reference points in blue circles which were the tags real positions, and the estimated positions of the tag are shown in red circles.

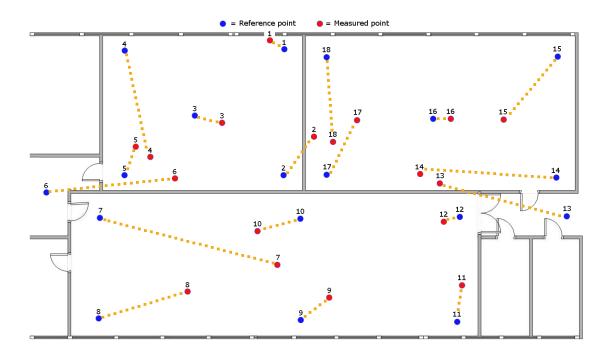
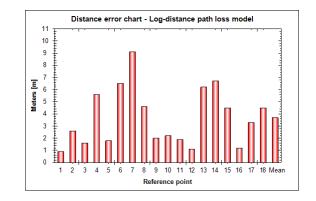


Figure 8.1: Measurement results



Furthermore, by looking at the position number in figure 8.1, the exact mean distance error at the given position can be found in figure 8.2 below.

Figure 8.2: Distance error on each measurement point

In addition to the mean distance errors on each position, figure 8.2 does also present the mean distance error for *all* estimated tag positions in the last column. Moreover, all the estimated positions during the testing were recorded and are presented graphically in figure 8.3. All estimated positions are in addition also available in text format in appendix B.

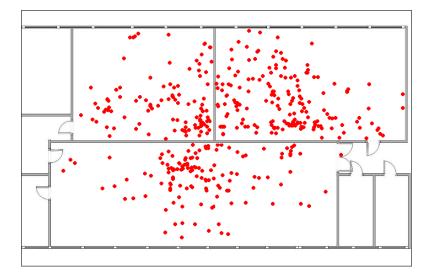


Figure 8.3: All estimated tag positions

It is important to note, that figure 8.3 are only showing position estimations that were "approved". In other words, all position estimations that were rejected by one of the positioning methods are not included. In addition, since equal RSSI values result in the same position estimation, they are obviously not visible on the map, since they are on top of each other.

8.2 Evaluation of the test results

The goal was to achieve a mean distance error of at least 3-5m according to the accuracy requirement set in section 3. The test results show that the mean distance error were 3.9m over the 18 different test positions. This satisfies most of the accuracy requirement. If one exclude the two test positions in the hallways, the mean distance error were 3.3m, which shows the big impact the two hallway positions had on the total mean distance error. The test results can furthermore be divided into showing the mean distance error for each room. This is shown in figure 8.4 below. The two hallways are excluded in this overview, since they as mentioned earlier only had one test position each.

							Mean:	Standard deviation:	Variance:
Ref. point	1	2	3	4	5				
Room 2	0,9	2,6	1,6	5,6	1,8		2,5	1,8	3,4
Ref. point	7	8	9	10	11	12			
Room 3	9,1	4,6	2	2,2	1,9	1,1	3,5	3,0	9,0
Ref. point	14	15	16	17	18				
Room 4	6,7	4,5	1,2	3,3	4,5		4,0	2,0	4,0

Figure 8.4: Distance error data for the three biggest rooms

The overview shows that the class room (number 2) and the big room (number 4) both achieves almost the same distance error as the mean distance error without the hallways, or better. The room with the highest distance error and one of the sources for the increased total mean distance error is the room up to the right on the map (number 3). This was as expected, since this room has more obstacles compared to the two other rooms, as explained earlier. It has many cabinets in wood along side one of the walls, in addition to several iron cabinets placed throughout the center of the room, from left to right. The two other rooms have only normal class room interior, like desks.

In addition, the accuracy requirement did also state that the system should be able to support room level separation, in other words at least manage to estimate the correct room for the tag. Test results show that this is achieved on 15 of the 18 test positions, resulting in a room separation accuracy of 83.3%, which is not enough.

Looking at the coverage requirement, the requirement was also just met to some degree. Wi-Fi is able to cover more than one (small) room, and you do not need more than one AP in a single room if the room is not too big. However, two AP's were used in the biggest room in the testing. This was not necessary, but was used since it were available and could increase the accuracy of the system. In addition, more than three AP's are required within range for the system to support some degree of fault tolerance. The fault tolerance requirement was therefore satisfied in the testing because of the extra AP used in the biggest room.

During the testing, there were some packet losses while the tag were in motion, but not greatly. Because of the frequency of packet transmissions (1s) when the tag is in motion, the system must lose several concurrent packet transmissions too stop functioning. This did not happen during the testing.

A total of 2000 RSSI measurements were performed under the testing. Many of the measurements were automatically performed while moving from one test position to another, so the actual number is less. The test results show that the difference between the smallest and biggest distance error were 8.2m. This is more than twice the mean distance error, and because of the wide range of distance error values, more test positions should have been tested, especially in the largest room. In addition, more measurements should have been made on the existing test positions to validate the existing distance errors, or to find a more accurate one.

Furthermore, an interesting "phenomenon" is visible by looking at the overview in figure 8.3 of all the estimated tag positions done in the testing. By drawing a line between the points furthest out, one can see that a "diamond" shaped figure becomes visible as shown in figure 8.5. This is in contrast to an expected rectangular shape since the test positions are placed rectangularly in the test area, with at least one test position close to each AP, which are placed at the map corners.

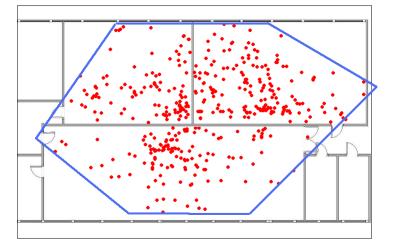


Figure 8.5: The estimated tag positions furthest out creates a "diamond" shape

There were unfortunately not enough time to investigate the reason for this further. However, it looks like the mean distance error are distributed in all directions when the tag is in the center of the map, but when the tag is close to one of the AP's, the distance error are usually in the direction away from the closest AP. It should be possible to make a positioning method that tries to solve this challenge by weighting the AP's close to the tag higher compared to the AP's farthest away.

8.3 Positioning methods evaluation

In order to evaluate and better understand the impact of each proposed positioning method to the tags final position estimation, several RSSI measurements were made at a fixed position, seen in figure 8.6. In this chapter, the measured RSSI values will be taken manually through the positioning methods before we end up with a position estimation. All the steps were shown earlier in ascending order in figure 6.2. To make it easier to have a "feel" with the numbers under way, all distance numbers are given in *meters*, instead of *points*, which are used in the testing program. The test map are 28.5m width with an height of 14.5m.

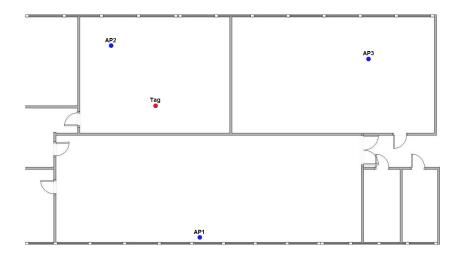


Figure 8.6: AP and tag positions in the test example

From the fixed position shown in the figure, all the AP's measured the RSSI from the tag 34 times each. All measurement details about this test example are going in appendix A.3. The same model and method configuration as used in the real testing are used in this example as well. This includes the calibration of the map with walls and borders. The only difference is the number of AP's used and the placement of these. Table 8.1 shows all the AP and tag coordinates.

	Coordinates (x,y)
AP1	(10.2 , 14.5)
AP2	(4.2, 2.2)
AP3	(21.2, 2.4)
Tag	(6.9 , 5.4)

Table 8.1: AP coordinates, in meters

After the RSSI measurements have been aggregated from each AP to the testing program, the *Measurement filtration* method is run. Since the "Best" option was used in the testing earlier, it will also be used in this example. When the tag is not in motion (as in this example), the method dynamically increase the memory table and remembers all the RSSI measurements done since the tag were last in motion. By looking at the table in appendix A.3, we see that the highest ("Best") RSSI for AP1 is -60 dBm, for AP2 it is -46 dBm and for AP3 it's -56 dBm. This is also shown in table 8.2 below.

	RSSI [dBm]
AP1	-60
AP2	-46
AP3	-56

Table 8.2: The highest RSSI value measured by each AP

Next, the *Wall attenuation* method adds attenuation (4.4 dB) for walls to the RSSI values, except the highest value, since its more likely that the AP with this value is in the same room as the tag. AP's in other rooms are expected to receive a more attenuated signal compared to the AP close to the tag. RSSI values after the first phase of this method is shown in table 8.3.

	RSSI, original [dBm]	RSSI, changed [dBm]
AP1	-60	-55.6
AP2	-46	-46
AP3	-56	-51.6

Table 8.3: RSSI values after Wall attenuation method

In the next step, the RSSI values are being converted to distance by the *Log-distance path loss* model. Table 8.4 shows the results, and the actual distance from each AP to the tag.

	Actual distance	Estimated distance
AP1	$9.6\mathrm{m}$	12.0m
AP2	4.3m	4.0m
AP3	14.8m	$7.6\mathrm{m}$

Table 8.4: Estimated and actual distances from AP's to tag

As the table shows, the estimated distances are a bit in-accurate, except AP2. This is however as expected in this phase, since AP2 is the only AP that is in the same room as the tag. Although the estimated distance from AP1 are 2.4m off compared to the real distance, the first phase of the wall attenuation method did actually improve the result. If the method hadn't added wall attenuation to AP1's RSSI value, the estimated distance would have been 20m instead. This would have been 10.4m off compared to the real distance. The method did on the other hand increase the estimation error on AP3's distance. This will however be fixed when the method is run again later.

Moving on to the next phase in the test program, the estimated distances are then verified in the first phase of the *Border check* method. This is only a rough check, that aims to adjust the worst error estimations. The method compares the estimated distances with the longest possible distance on the testing area. In this case, that is the diagonal on the map from the bottom left corner to AP3, which is 24m long. None of the estimated distances are this long, so the program just moves to the next phase which is the trilateration. The trilateration phase determines the mean position in relation to the distance from each AP's own position. Based on this, the trilateration process estimate the tags position to be (X=11.5,Y=1.1). As mentioned above, the tags real position is (6.9,5.4) which gives an in-accuracy/distance-error of 6.3m at this point. This is shown in figure 8.7.

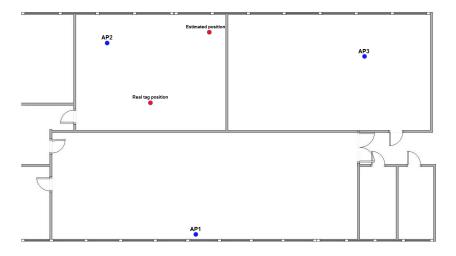


Figure 8.7: Temporary position estimation

The temporary position estimation is then sent to the *Border check* method for the second time. This time, the method checks weather the estimated position is inside our outside the border drawn in the map calibration process. In this example, the position is inside the border and nothing happens. Next, the second phase of the *Wall attenuation* method checks weather the first phase of this method added the correct amount of wall attenuation, to the right AP's. Counting the "correct" number of walls are now possible since the system didn't know the tags estimated room position in the first phase. By using the estimated position as starting point, the method counts the correct number of walls between the estimated position and each AP in range. If zero walls are counted, the method removes the added attenuation from the first phase, and if more than one are counted the method adds attenuation. In this example, one wall is counted between the estimated tag position and AP1, which is correct. Zero walls are found to AP2, which is also correct. In the end, zero walls are also counted between the tag and AP3. The reason for this is explained earlier. Wall measurements showed little attenuation between these rooms, and the wall between these rooms was therefore excluded in the map calibration process. The map calibration, which is also used in this example, may be seen again in figure 7.8. Since the first phase of the wall attenuation method added attenuation to the RSSI measurement done by AP3, it must be removed. Table 8.5 below shows the updated RSSI values.

	RSSI, original [dBm]	RSSI, before [dBm]	RSSI, now [dBm]
AP1	-60	-55.6	-55.6
AP2	-46	-46	-46
AP3	-56	-51.6	-56

Table 8.5: RSSI values after the second phase of the Wall attenuation method

Since one of the RSSI values changed, new distances have to be calculated using the logdistance path loss model again. Table 8.6 shows the new distances, in addition to the old distances and the actual distances for easy comparison.

	Actual distance	Estimated distance - before	Estimated distance - now
AP1	$9.6\mathrm{m}$	12.0m	12.0m
AP2	4.3m	4.0m	4.0m
AP3	14.8m	7.6m	12.6m

Table 8.6: Estimated and actual distances from AP's to tag

The table shows that the distance from AP3 have been improved, which means the method fixed the error it did in the first phase the second time it was run. After the new distances have been calculated, the trilateration process estimate the new tag position, which is (8.5,2.5). The distance error is now 3.3m, compared to 6.3m in the first position estimation. The estimated tag position is now passed on to the next method which is the *Speed filtration* method. This method compares the estimated position against the last accepted position

estimation, and checks weather the distance between them are too far for a person to move in the given time frame between the two estimations. The estimated position is rejected if the method returns true. Which means that the previous estimated position is still valid. Since this example do not have a previous position estimation, the position is passed on to the next method. The *Statistical position estimation* aims to reduce the position estimating fluctuations even when the tag is not in motion. The estimated position is added to a table of the three last position estimations, and the mean position is returned. This is as said above the first position estimation, so this method have also neither influence on the final position estimation in this example.

The last method the estimated position is run through is the *Wall check* method. This is a very simple method, that only checks weather the estimated position is on top of a wall on the map. If the position is on top of a wall, the method changes the position to the closest position outside the wall.

None of the last methods did any changes to the temporary estimated position, so the final position and distance error are the same. A distance error of 3.3m are better than the mean distance error in the full scale testing earlier, and is the same as in the test if we compare it to the mean distance error without the hallways. This is a good result.

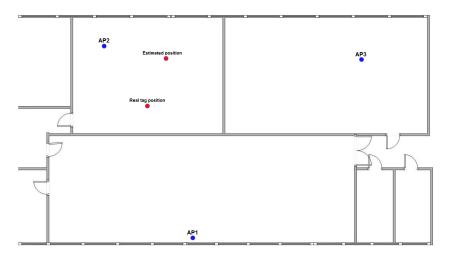


Figure 8.8: Final position estimation of tag

The final position estimation is shown graphically in figure 8.8.

Chapter 9

Conclusion

The assessment of different technologies used in indoor positioning systems showed that Ultra-Wideband is probably the best technology. Ultra-Wideband is however in its early phases and are therefore not regulated for use in all countries, for instance Norway. It is also the most expensive technology to use in an indoor positioning system at the time being, compared to the other assessed technologies.

Wi-Fi is on the other hand a good choice for open indoor environments such as office or class rooms where some level of positioning error is accepted as long as the decreased performance is reflected in the price of the system. The test results showed that it's difficult to make a positioning system based on Wi-Fi that is more accurate than 3m. However, the possibility to re-use the existing wireless network infrastructure makes the proposed system acceptable in relation to its potential low cost.

The test results also showed that most of the proposed positioning methods did improve the accuracy of the system. Some of the methods should however be edited to increase the level of accuracy. This are especially the *Wall attenuation* method and the *Border check* method.

9.1 Future work

The test results showed that the position estimations of the tag are less accurate in the room with the most obstacles. Therefore, a position method that try and take room obstacles into account should be investigated. This is not an easy task, and may not increase the accuracy since there also lie some significant uncertainty in how the position method is designed, in addition to the uncertainty in radio wave propagation. Still, it should be tested before a conclusion is made.

Furthermore, the testing also discovered significant position estimation fluctuations despite that the tag was not in motion. Two of the proposed position methods tried to encounter this problem, but didn't succeed 100%. Therefore, the proposed statistical method should be switched with an implementation of the non-linear version of the Kalman Filter, called Extended Kalman Filter (EKF).

In the end, testing different types of Wi-Fi tags should be performed, to give a better understanding of how big part of the positioning uncertainty that are related to the tags used, and how much is related to the Wi-Fi positioning system itself.

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Appendix A

Measurement data

A.1 Finding $PL(d_0)$

The first thing I measured were the path loss at the reference distance d_0 , which were set to 1m. The highest RSSI value achieved at this distance where -35 dBm, which gave a path loss of 55.2 dBm (= 19 - (-35) + 2.2). The mean RSSI value were -39.8 dBm which gave a path loss of 60.9 dBm. The standard deviation of all the PL(d_0) measurements were 4.05. All the measurements are shown below.

RSS	SI - 1	1m o	lista	nce	:																								Mean:	Standard deviation:	Highest value:
-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-46	-45	-45	-45	-45	-46	-46	-46	-45	-45	-41	-41	-39	-39	-38	-39	-38	-41			
-35	-34	-36	-36	-36	-36	-34	-36	-36	-36	-36	-36	-35	-34	-35	-34	-35	-34	-34	-35	-35	-42	-42	-42	-40	-37	-36	-35	-36			
-37	-37	-37	-37	-37	-43	-43	-37	-37	-37	-37	-38	-37	-37	-37	-37	-37	-37	-37	-37	-37	-39	-39	-38	-38	-38	-38	-39	-38			
-40	-43	-43	-40	-40	-40	-40	-40	-40	-40	-39	-40	-40	-44	-43	-39	-39	-44	-44	-40	-40	-41	-41	-41	-40	-37	-37	-36	-36			
-41	-41	-41	-40	-38	-38	-38	-39	-39	-40	-41	-41	-39	-39	-39	-38	-39	-39	-38	-41	-41	-38	-39	-39	-39	-38	-39	-41	-40	-39,7	4,0	-34,0
-35	-36	-41	-42	-42	-42	-36	-36	-41	-42	-42	-36	-36	-36	-36	-36	-36	-36	-42	-42	-36	-36	-36	-37	-36	-41	-42	-36	-36			
-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-45	-46	-45	-45	-45	-45	-45	-38	-38			
-35	-34	-34	-35	-36	-36	-36	-36	-35	-34	-34	-35	-34	-36	-36	-37	-34	-35	-34	-34	-35	-36	-34	-36	-37	-36	-36	-37	-40			
-36	-37	-37	-45	-41	-37	-38	-36	-38	-45	-53	-49	-39	-42	-38	-37	-38	-37	-37	-38	-43	-43	-37	-39	-37	-37	-37	-40	-41			
-36	-35	-36	-37	-43	-41	-40	-42	-40	-69	-44	-43	-42	-40	-43	-43	-43	-43	-43	-43	-39	-39	-43	-43	-43	-40	-40	-41	-39			

A.2 Measurements at different distances

In addition to the measurements above, I also made several measurements at 1 to 6m distance with another tag. The reason for this was because I wanted to see if they gave the same results, since they in theory are the same. All the RSSI values at the different distances is shown below, and clearly shows two things; at 1m the mean path loss value is approximately 4 dBm less than with the tag used in the positioning testing and $PL(d_0)$ measurements. The second thing we can see from the measurements is that the RSSI values do not decrease as the distance increases, as one would expect according to Friis free space loss equation. All details is found in the figure below.

										RSS	SI:							Mean:	Standard deviation:	Variance:	Highest value:	Estimated (In theory)
1m:	-30	-30	-37	-36	-29	-29	-36	-30	-29	-36	-29	-36	-36	-30	-37	-37	-36					
	-30	-36	-37	-54	-36	-36	-37	-37	-51	-36	-50	-36	-52	-37	-54	-37	-37	-36,94	7,13	50,91	-29	-19
2m:	-47	-47	-43	-43	-47	-48	-45	-44	-48	-44	-50	-50	-49	-47	-50	-50	-54					
	-46	-55	-46	-46	-46	-56	-58	-56	-55	-54	-46	-46	-55	-46	-53	-46	-50	-49,00	4,21	17,76	-43	-25
3m:	-53	-53	-39	-40	-40	-53	-41	-52	-52	-39	-41	-39	-52	-40	-52	-53	-47					
	-47	-46	-46	-46	-46	-46	-47	-46	-46	-46	-47	-47	-46	-47	-46	-46	-45	-46,24	4,44	19,70	-39	-28,5
4m:	-50	-49	-51	-49	-52	-52	-48	-49	-50	-49	-51	-51	-50	-49	-51	-50	-52					
	-52	-52	-52	-52	-58	-57	-59	-53	-52	-52	-56	-54	-53	-53	-53	-57	-56	-52,18	2,78	7,73	-48	-31
5m:	-57	-49	-58	-57	-57	-50	-49	-57	-48	-58	-57	-57	-48	-47	-49	-50	-47					
	-50	-53	-52	-47	-47	-47	-47	-47	-47	-47	-47	-52	-46	-50	-52	-47	-51	-50,71	4,09	16,76	-46	-33
6m:	-44	-43	-42	-43	-44	-44	-44	-42	-45	-44	-44	-42	-43	-42	-43	-43	-52					
	-50	-53	-50	-52	-52	-50	-52	-53	-53	-52	-53	-50	-52	-52	-52	-51	-53	-47,76	4,44	19,70	-42	-34,5

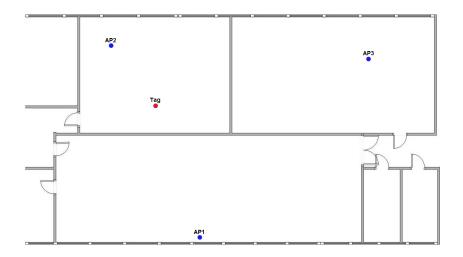
A.3 Wall attenuation measurements

One of the positioning methods described in the thesis tries to add wall attenuation to signals that penetrate walls. In order for this method to be as accurate as possible, several wall attenuation measurements were performed. The two tables below show respectively the RSSI measurement through one of the walls at the same reference distance as earlier (1m) and measurements from both sides of a wall. In the latter one, two AP's were used, one on each side of the wall, and the tag was on one of the sides. Interestingly enough, the measurements showed that there were no or just minimal signal loss through this wall.

	Wa	ll att	tenu	atio	n m	eası	ıren	nent	s, at	1m	dist	ance	e thr	oug	h fir	st w	all.	Mean:	Standard deviation:	Variance:	Highest value:	Estimated (In theory)
	-52	-45	-37	-39	-42	-42	-39	-43	-39	-41	-43	-42	-41	-38	-42	-43	-39					
	-42	-42	-39	-39	-39	-41	-40	-42	-41	-42	-39	-39	-39	-45	-40	-40	-51	-41,38	3,19	10,18	-37	-19
	Wa	ll att	tenu	atio	n m	eası	ıren	nent	s, tw	o A	P's o	lose	e to I	the v	wall			Mean:	Standard deviation:	Variance:	Highest value:	Estimated (In theory)
AP1	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20					
(with tag)	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20	-20,00	0,00	0,00	-20	-19
AP2	-21	-20	-24	-22	-20	-20	-20	-20	-20	-20	-20	-20	-22	-20	-20	-20	-20					
(through wall)	-20	-20	-20	-20	-20	-22	-20	-23	-20	-23	-20	-20	-20	-23	-20	-20	-20	-20,59	1,16	1,34	-20	-19

A.4 Measurements for positioning example

To be able to evaluate the proposed positioning methods in this thesis, several measurements were made on three AP's while the tag were not in motion on the same position on all measurements. Figure 8.6 shows the AP and tag placement on the map.



Furthermore, the table below shows the corresponding RSSI measurements done by each AP at this test setup.

	Mea	asur	eme	nts f	for p	osit	ioni	ng e	xan	ple	I.							Mean:	Standard deviation:	Variance:		Estimated (In theory)
AP1	-74	-64	-63	-68	-63	-65	-67	-73	-75	-61	-64	-70	-71	-71	-71	-66	-61					
(9,6m to tag)	-71	-68	-68	-67	-63	-66	-67	-67	-81	-64	-70	-60	-70	-76	-69	-68	-67	-67,91	4,60	21,17	-60	-38,7
AP2	-57	-51	-52	-50	-49	-46	-65	-56	-51	-51	-58	-56	-56	-53	-51	-58	-51					
(4,1m to tag)	-49	-54	-49	-52	-62	-49	-64	-56	-47	-57	-64	-57	-50	-52	-50	-56	-52	-53,85	4,88	23,83	-46	-31,3
AP3	-70	-68	-65	-59	-66	-68	-66	-72	-62	-63	-64	-59	-60	-66	-61	-65	-59					
(16,4m to tag)	-56	-67	-67	-60	-67	-67	-64	-64	-61	-64	-61	-67	-63	-65	-67	-63	-63	-64,09	3,51	12,33	-56	-43,3

Appendix B

Logs from the test program

All logs created by the test program during the positioning test presented in section 7.5 are shown in this chapter. The last part shows all the estimated tag positions, including the time stamp of the estimation.

General log:

20:25:37 Tag being located: 000c.cc7b.4694
20:25:37 Number of APs: 4
20:25:37 Refresh rate: 1 second
20:25:37 Map filename: hib-lab3.jpg

Configuration log:

20.20.21 Dorder coordinates.	20:26:24	Border	coordinates:
------------------------------	----------	--------	--------------

20:26:24	X = 153, Y = 29
20:26:24	X=157,Y=189
20:26:24	X = 59, Y = 190
20:26:24	X = 62, Y = 298
20:26:24	X = 117, Y = 297
20:26:24	X=116,Y=432
20:26:24	X = 654, Y = 426
20:26:24	X = 654, Y = 293
20:26:24	X=786,Y=295

20:26:24 X=781,Y=29

20:26:24 Wall coordinates:

20:26:24 X=422,Y=235 to X=782,Y=238

20:26:24 Reference coordinates:

20:26:24 X=464, Y=32 to X=463, Y=235, length: 7,57m

- 20:26:24 AP coordinates:
- 20:26:24 0023.041a.3855: X=132,Y=420
- 20:26:24 0023.041a.4546: X=208,Y=68
- 20:26:24 0023.041a.45ab: X=626,Y=414
- 20:26:24 0023.041a.375c: X=681,Y=79

Locator log - in the format [time stamp : X, Y coordinates]:

[6:X=410, Y=223][9:X=408, Y=265][13:X=430, Y=248][16:X=440, Y=223][18:X=437, Y=223][21:X=428,Y=236][23:X=435,Y=223][26:X=442,Y=223][28:X=440,Y=223][30:X=440,Y=248][38:X=440,Y=248][40:X=440,Y=248][42:X=440,Y=248][45:X=440,Y=248][47:X=40,Y=248][47:X=40,Y=248][47:X=40,Y=248][47:X=40,Y=248][47:X=40,Y=248][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=40,Y=40,Y=20][47:X=40,Y=20][47:X=40,Y=20][47:X=20][47:X=20][47:X=20[52:X=440,Y=248][54:X=440,Y=248][57:X=440,Y=248][59:X=440,Y=238][62:X=425,Y=248][59:X=440,Y=238][59:X=440,Y=238][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=440,Y=248][59:X=40,Y=248][50:X=40,Y=248][50:X=40,Y=248][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=40,Y=20][50:X=[131:X=433,Y=207][133:X=410,Y=213][136:X=397,Y=202][138:X=396,Y=212][141:X=363,Y=230][146:X=414,Y=230][148:X=393,Y=225][150:X=390,Y=205][153:X=397,Y=211][155:X=405,Y=219][161:X=396,Y=210][163:X=387,Y=220][165:X=368,Y=232][168:X=370,Y=233][170:X=424,Y=205][175:X=370,Y=224][177:X=398,Y=218][179:X=371,Y=240][182:X=399,Y=222][187:X=415,Y=213][191:X=413,Y=211][199:X=411,Y=205][201:X=409,Y=193][218:X=404,Y=170][222:X=396,Y=126][231:X=390,Y=97][241:X=408,Y=119][243:X=446,Y=164][261:X=427,Y=141][263:X=390,Y=97][268:X=539,Y=112][272:X=489,Y=96][274:X=539,Y=79][277:X=377,Y=113][280:X=395,Y=103][282:X=246,Y=148][284:X=222,Y=171][288:X=276,Y=174][289:X=375,Y=180][291:X=398,Y=233][293:X=367,Y=296][294:X=367,Y=296][296:X=379,Y=283][297:X=395,Y=269][298:X=395,Y=269][302:X=346,Y=324][305:X=346,Y=320][306:X=346,Y=307][307:X=347,Y=305][308:X=348,Y=306][311:X=382,Y=282][312:X=375,Y=270][313:X=325,Y=276][315:X=337,Y=271][316:X=343,Y=303] $[319:X=401,Y=308] \\ [320:X=381,Y=301] \\ [321:X=423,Y=297] \\ [322:X=417,Y=307] \\ [324:X=431,Y=336] \\ [323:X=417,Y=307] \\ [324:X=431,Y=336] \\ [323:X=417,Y=307] \\ [324:X=431,Y=306] \\ [324:X=431,Y=306] \\ [325:X=417,Y=307] \\ [325$ [327:X=482,Y=369][328:X=482,Y=369][330:X=482,Y=369][331:X=450,Y=346][332:X=386,Y=300][335:X=394,Y=303][336:X=507,Y=321][338:X=466,Y=314][339:X=499,Y=319][341:X=530,Y=215][343:X=533,Y=213][344:X=533,Y=213][346:X=533,Y=213][347:X=558,Y=97][349:X=558,Y=97]

 $[352:X=566,Y=180] [353:X=568,Y=221] [354:X=568,Y=221] [355:X=568,Y=221] [357:X=611,Y=224] \\ [361:X=659,Y=244] [364:X=667,Y=235] [366:X=692,Y=214] [368:X=696,Y=206] [371:X=713,Y=189] \\ [375:X=572,Y=169] [378:X=630,Y=192] [383:X=651,Y=206] [390:X=617,Y=213] [392:X=593,Y=216] \\ [422:X=555,Y=213] [452:X=573,Y=218] [454:X=610,Y=229] [456:X=539,Y=105] [458:X=539,Y=105] \\ [464:X=524,Y=320] [466:X=524,Y=320] [469:X=539,Y=236] [471:X=559,Y=217] [473:X=543,Y=183] \\ [480:X=531,Y=235] [483:X=552,Y=229] [488:X=546,Y=190] [491:X=572,Y=214] [502:X=584,Y=178] \\ [510:X=640,Y=207] [514:X=645,Y=208] [518:X=628,Y=159] [520:X=607,Y=64] [523:X=607,Y=64] \\ [527:X=607,Y=64] [530:X=434,Y=399] [532:X=434,Y=399] [535:X=434,Y=399] [537:X=537,Y=225] \\ [547:X=569,Y=174] [549:X=585,Y=216] [552:X=580,Y=217] [554:X=570,Y=221] [557:X=574,Y=198] \\ \end{tabular}$

 $[564:X=549,Y=126] [566:X=484,Y=70] [657:X=506,Y=78] [659:X=552,Y=94] [717:X=532,Y=177] \\ [720:X=497,Y=340] [721:X=497,Y=340] [722:X=497,Y=340] [724:X=497,Y=340] [727:X=497,Y=340] \\ [731:X=709,Y=246] [733:X=709,Y=246] [734:X=709,Y=246] [736:X=709,Y=246] [737:X=709,Y=246] \\ [740:X=616,Y=248] [741:X=455,Y=312] [743:X=427,Y=268] [744:X=395,Y=240] [745:X=437,Y=258] \\ [748:X=452,Y=327] [750:X=439,Y=316] [751:X=429,Y=357] [753:X=409,Y=346] [754:X=340,Y=342] \\ [757:X=259,Y=325] [758:X=259,Y=325] [760:X=259,Y=325] [761:X=259,Y=325] [763:X=236,Y=337] \\ [765:X=139,Y=308] [767:X=161,Y=293] [769:X=235,Y=227] [770:X=153,Y=287] [772:X=153,Y=287] \\ [780:X=293,Y=313] [787:X=304,Y=317] [790:X=337,Y=304] [791:X=337,Y=304] [792:X=337,Y=304] \\ [797:X=337,Y=304] [819:X=223,Y=192] [822:X=389,Y=29] [823:X=373,Y=34] [844:X=465,Y=184] \\ [847:X=465,Y=184] [850:X=348,Y=148] [852:X=227,Y=241] [854:X=221,Y=224] [856:X=205,Y=188] \\ [860:X=230,Y=194] [861:X=225,Y=186] [863:X=224,Y=174] [866:X=265,Y=52] [868:X=253,Y=93] \\ [878:X=274,Y=50] [880:X=280,Y=45] [906:X=324,Y=34] [908:X=413,Y=34] [909:X=504,Y=80] \\ [912:X=456,Y=76] [914:X=438,Y=154] [916:X=438,Y=154] [919:X=439,Y=142] [920:X=454,Y=144] \\ [912:X=456,Y=76] [914:X=454,Y=144] \\ [912:X=456,Y=76] [914:X=454,Y=144] \\ [912:X=456,Y=76] [914:X=454,Y=144] \\ [912:X=456,Y=76] [914$

[924:X=471,Y=149][925:X=471,Y=149][926:X=471,Y=149][930:X=337,Y=47][933:X=400,Y=85]

 $[948:X=405,Y=65] [950:X=415,Y=72] [952:X=416,Y=71] [955:X=426,Y=34] [957:X=432,Y=39] \\ [962:X=489,Y=40] [977:X=340,Y=142] [979:X=421,Y=117] [981:X=328,Y=146] [986:X=355,Y=145] \\ [989:X=339,Y=101] [990:X=339,Y=101] [991:X=339,Y=101] [995:X=303,Y=130] [997:X=324,Y=173] \\ [989:X=380,Y=101] [980:X=380,Y=101] [981:X=380,Y=101] [981:X=380,Y=130] [981:X=380,Y=130] \\ [988:X=380,Y=101] [988:X=380,Y=101] [988:X=380,Y=101] [988:X=380,Y=101] [988:X=380,Y=130] [988:X=380,Y=130] \\ [988:X=380,Y=101] [988:X=380,Y=101] [988:X=380,Y=101] \\ [988:X=380,Y=101] [988:X=380,Y=101] [988:X=380,Y=130] [988:X=380,Y=130] \\ [988:X=380,Y=101] [988:X=380,Y=101] [988:X=380,Y=130] [988:X=380,Y=130] \\ [988:X=380,Y=101] [988:X=380,Y=101] \\ [988:X=380,Y=100,Y=100] \\ [988:X=380,Y=100,Y=100,Y=100] \\ [988:X=380,Y=100,Y=100] \\ [988:X=380,Y=100,Y=100,Y=100] \\ [988:X=380,Y=100,Y=100,Y=100] \\ [988:X=380,Y=100,Y=100,Y=100,Y=100] \\ [988:X=380,Y=100,Y=100,Y=100,Y=100,Y=100] \\ [988:X=380,Y=100,$

 $[1001:X=303,Y=181] [1003:X=303,Y=184] [1006:X=299,Y=193] [1034:X=318,Y=183] \\ \label{eq:constraint}$

$$[1035:X=401,Y=181] [1038:X=386,Y=175] [1041:X=430,Y=181] [1046:X=420,Y=170] \\ \label{eq:eq:exact_star}$$

$$[1047:X=430,Y=150] [1052:X=431,Y=127] [1054:X=418,Y=99] [1055:X=426,Y=90] \\ [1056:X=426,Y=90] [1064:X=216,Y=195] [1085:X=283,Y=166] [1086:X=202,Y=214]$$

[1089:X=194,Y=210] [1090:X=173,Y=201] [1091:X=191,Y=149] [1093:X=191,Y=149] [1093:X=191,Y=140] [1093:X=191,Y=100] [1093:X=190] [1093:X=190]

[1097:X=246,Y=166][1099:X=350,Y=172][1102:X=357,Y=162][1106:X=346,Y=166]][1097:X=246,Y=166][1099:X=350,Y=172][1102:X=357,Y=162][1106:X=346,Y=166]][1099:X=350,Y=172][1102:X=357,Y=162][1106:X=346,Y=166]][1099:X=350,Y=172][1102:X=357,Y=162][1106:X=346,Y=166]][1099:X=350,Y=172][1102:X=357,Y=162][1106:X=346,Y=166]][1099:X=350,Y=172][1102:X=357,Y=162][1106:X=346,Y=166]][1099:X=350,Y=172][1102:X=357,Y=162][1106:X=346,Y=166]][1099:X=350,Y=172][1106:X=346,Y=166]][1106:X=346]][1106:X=34[1108:X=345,Y=165][1110:X=345,Y=163][1112:X=355,Y=178][1113:X=399,Y=189][1115:X=369,Y=215][1116:X=332,Y=247][1118:X=306,Y=189][1120:X=306,Y=189][1121:X=346,Y=210][1122:X=402,Y=194][1126:X=200,Y=179][1127:X=200,Y=179][1129:X=200,Y=179][1130:X=200,Y=179][1131:X=200,Y=179][1132:X=337,Y=171][1135:X=411,Y=142][1136:X=411,Y=142][1137:X=411,Y=142][1138:X=222,Y=172][1140:X=222,Y=172][1141:X=222,Y=172][1142:X=222,Y=172][1144:X=282,Y=218][1146: X = 213, Y = 342] [1148: X = 213, Y = 342] [1149: X = 213, Y = 342] [1159: X = 276, Y = 228] [1159: X = 276, Y = 228] [1159: X = 213, Y = 342] [1150: X = 213, Y = 342] [1150: X = 213, Y = 342] [1150: X = 213, Y =[1163:X=276,Y=228][1164:X=322,Y=283][1170:X=477,Y=280][1173:X=255,Y=205][1178:X=255,Y=205][1182:X=349,Y=231][1183:X=300,Y=238][1186:X=300,Y=238][1188:X=326,Y=293][1189:X=364,Y=424][1191:X=372,Y=341][1195:X=372,Y=341][1196:X=363,Y=376][1206:X=345,Y=279][1207:X=354,Y=305][1221:X=337,Y=311][1222:X=357,Y=293][1223:X=373,Y=294][1225:X=380,Y=302][1227:X=424,Y=371][1230:X=408,Y=341][1232:X=407,Y=325][1238:X=408,Y=327][1239:X=421,Y=373][1242:X=401,Y=367][1244:X=333,Y=414][1246:X=352,Y=398][1247:X=365,Y=396][1250:X=389,Y=398][1252:X=451,Y=417][1254:X=439,Y=415][1255:X=415,Y=411][1258:X=357,Y=358][1259:X=347,Y=369][1260:X=271,Y=360][1268:X=294,Y=356][1269:X=340,Y=332][1270:X=341,Y=345][1272:X=342,Y=334][1273:X=256,Y=362][1274:X=256,Y=362][1279:X=324,Y=332][1281:X=400,Y=322][1282:X=390,Y=318][1283:X=382,Y=339][1285:X=380,Y=337][1286:X=332,Y=383][1287:X=332,Y=383][1287:X=332,Y=383][1287:X=332,Y=383][1285:X=383,Y=383][1285:X=383,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=383][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=382,Y=382][1285:X=38[1288:X=332,Y=383][1291:X=359,Y=336][1292:X=388,Y=274][1294:X=391,Y=284][1296:X=456,Y=370][1301:X=434,Y=340][1302:X=422,Y=323][1304:X=413,Y=326][1305:X=379,Y=309][1308:X=374,Y=303][1310:X=363,Y=305][1313:X=364,Y=304][1315:X=361,Y=306][1320:X=363,Y=299][1322:X=368,Y=287][1324:X=369,Y=284][1325:X=407,Y=261][1327:X=418,Y=249][1328:X=477,Y=210][1329:X=502,Y=235][1330:X=499,Y=220][1332:X=586,Y=228][1335:X=564,Y=221][1337:X=585,Y=275][1338:X=591,Y=257][1339:X=611,Y=250][1340:X=611,Y=250][1341:X=574,Y=259][1343:X=510,Y=249][1344:X=510,Y=249][1345:X=569,Y=218][1347:X=536,Y=227][1348:X=535,Y=225][1350:X=535,Y=225][1351:X=535,Y=225][1360:X=550,Y=282]][1365:X=586,Y=371][1367:X=602,Y=375][1369:X=633,Y=348][1377:X=549,Y=334][1378:X=382,Y=307][1379:X=382,Y=307][1380:X=382,Y=307][1383:X=382,Y=307]

[1384:X=533,Y=371][1386:X=533,Y=371][1388:X=533,Y=371][1390:X=482,Y=278][1393:X=533,Y=157][1395:X=533,Y=156][1398:X=535,Y=156][1402:X=528,Y=146][1405:X=515,Y=126][1407:X=530,Y=120][1410:X=531,Y=162][1412:X=566,Y=275][1413:X=560,Y=264][1414:X=566,Y=278][1415:X=566,Y=278][1417:X=566,Y=278][140][1417:X=566,Y=278][1417[1419:X=569,Y=262][1422:X=567,Y=270][1424:X=576,Y=249][1429:X=506,Y=250][1431:X=376,Y=230][1432:X=504,Y=224][1434:X=504,Y=224][1435:X=429,Y=233][1436:X=383,Y=258][1438:X=383,Y=258][1440:X=422,Y=240][1443:X=475,Y=217][1444:X=527,Y=111][1446:X=527,Y=111][1447:X=527,Y=111][1448:X=471,Y=181] $[1450:X=488,Y=156] \\ [1451:X=488,Y=156] \\ [1452:X=467,Y=192] \\ [1454:X=551,Y=275] \\ [1452:X=467,Y=192] \\ [1454:X=551,Y=275] \\ [1451:X=488,Y=156] \\ [1451:X$ [1456:X=543,Y=226][1457:X=598,Y=248][1459:X=598,Y=248][1461:X=587,Y=223][1462:X=591,Y=224][1464:X=591,Y=224][1477:X=664,Y=220][1478:X=778,Y=188]][1480:X=778,Y=161][1481:X=777,Y=83][1482:X=777,Y=83][1486:X=777,Y=83][1489:X=777,Y=83][1490:X=777,Y=83][1491:X=777,Y=83][1494:X=714,Y=142][1496:X=446,Y=203][1498:X=466,Y=226][1500:X=487,Y=223][1503:X=481,Y=223][1505:X=412,Y=265][1513:X=430,Y=258][1514:X=467,Y=272][1516:X=451,Y=263][1517:X=476,Y=253][1518:X=476,Y=253][1521:X=662,Y=277][1522:X=662,Y=277][1526:X=563,Y=218][1528:X=556,Y=110][1530:X=557,Y=130][1531:X=562,Y=156][1563:X=525,Y=141][1564:X=451,Y=112][1567:X=457,Y=95][1568:X=469,Y=61][1569:X=549,Y=82][1571:X=534,Y=89][1573:X=598,Y=105][1578:X=618,Y=128][1581:X=673,Y=157][1583:X=673,Y=155][1586:X=675,Y=152][1591:X=649,Y=141][1593:X=598,Y=120][1594:X=599,Y=115][1600:X=575,Y=126][1603:X=596,Y=120][1604:X=611,Y=128][1606:X=596,Y=195][1607:X=602,Y=176][1609:X=599,Y=205][1611:X=625,Y=227][1612:X=613,Y=219][1615:X=740,Y=240][1616:X=697,Y=225][1617:X=735,Y=237][1619:X=730,Y=230][1620:X=720,Y=217][1623:X=720,Y=217][1625:X=496,Y=132][1652:X=563,Y=161][1653:X=468,Y=118][1654:X=463,Y=125][1656:X=431,Y=184][1658:X=447,Y=163][1661:X=467,Y=178][1663:X=463,Y=177][1666:X=461,Y=173][1688:X=488,Y=133][1690:X=542,Y=53][1696:X=542,Y=53][1697:X=500,Y=94][1699:X=354,Y=211][1700:X=354,Y=211][1701:X=354,Y=211][1702:X=354,Y=211][1703:X=354,Y=211][1705:X=354,Y=211][1706:X=448,Y=199][1709:X=575,Y=210][1711:X=625,Y=245][1714:X=644,Y=227][1716:X=732,Y=227][1719:X=544,Y=170][1720:X=544,Y=170][1722:X=636,Y=199][1723:X=588,Y=194]

[1725:X=588,Y=194][1727:X=599,Y=205][1728:X=576,Y=221][1730:X=508,Y=134][1731:X=521,Y=174][1733:X=531,Y=220][1734:X=531,Y=220][1736:X=531,Y=220][1737:X=484,Y=189][1738:X=443,Y=180][1740:X=443,Y=180][1741:X=580,Y=145][1742:X=536,Y=163][1744:X=584,Y=165][1745:X=587,Y=170][1747:X=589,Y=180][1748:X=592,Y=187][1749:X=619,Y=222][1751:X=612,Y=215][1752:X=623,Y=222][1754:X=567,Y=129][1769:X=580,Y=135][1790:X=552,Y=57][1797:X=556,Y=69] [1800:X=566,Y=93][1806:X=568,Y=105][1808:X=584,Y=149][1810:X=584,Y=153][1813:X=623,Y=201][1851:X=608,Y=194][1854:X=606,Y=198][1862:X=593,Y=211]] $[1864: X = 614, Y = 219] \\ [1866: X = 600, Y = 225] \\ [1868: X = 615, Y = 224] \\ [1869: X = 616, Y = 227] \\ [1869: X = 616, Y =$ [1870:X=632,Y=224][1871:X=632,Y=224][1873:X=632,Y=224][1874:X=583,Y=208][1876:X=521,Y=155][1877:X=521,Y=155][1879:X=533,Y=173][1880:X=575,Y=205][1882:X=575,Y=205][1883:X=482,Y=60][1885:X=482,Y=60][1890:X=482,Y=60][1892:X=474,Y=198][1893:X=387,Y=348][1895:X=381,Y=346][1896:X=401,Y=350][1898:X=403,Y=370][1899:X=418,Y=400][1903:X=418,Y=400][1904:X=418,Y=400][1905:X=190,Y=247][1908:X=262,Y=295][1910:X=154,Y=300][1913:X=134,Y=252][1915:X=162,Y=185][1918:X=64,Y=207][1920:X=66,Y=218][1923:X=72,Y=239][1925:X=105,Y=251][1927:X=88,Y=270][1930:X=162,Y=175][1935:X=65,Y=211][1936:X=162,Y=179][1937:X=162,Y=179][1938:X=162,Y=179][1943:X=313,Y=297][1966:X=274,Y=298][1975:X=471,Y=420][1978:X=162,Y=181][1980:X=211,Y=256][1983:X=162,Y=167]