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# A FUZZY EPQ MODEL FOR NON-INSTANTANEOUS DETERIORATING ITEMS WHERE PRODUCTION DEPENDS ON DEMAND WHICH IS PROPORTIONAL TO POPULATION, SELLING PRICE AS WELL AS ADVERTISEMENT

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#### **ABSTRACT**

The inventory system has been drawing more intrigue because this system deals with the decision that minimizes the total average cost or maximizes the total average profit. For any farm, the demand for any items depends upon population, selling price and frequency of advertisement etc. Most of the model, it is assumed that deterioration of any item in inventory starts from the beginning of their production. But in reality, many goods are maintaining their good quality or original condition for some time. So, price discount is availed for defective items. Our target is to calculate the total optimal cost and the optimal inventory level for this inventory model in a crisp and fuzzy environment. Here Holding cost taken as constant and no-shortages are allowed. The cost parameters are considered as Triangular Fuzzy Numbers and to defuzzify the model Signed Distance Method is applied. A numerical example of the optimal solution is given to clarify the model. The changes of different parameters effect on the optimal total cost are presented and sensitivity analysis is given.

**Keywords**: EPQ Inventory, Non-Instantaneous Deterioration, Demand dependent Production, Defuzzification, Signed Distance Method





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#### 1. INTRODUCTION

In an EPQ inventory, it is important to control quality. Most of the models of the inventory control system are formulated with the assumption that all produced items are of good quality. But in reality, for any production company to produce all good quality products is impossible. On the other hand, due to the different phenomenon, there are so many goods which deteriorate after their lifetime. In such situation price discount are common practices by the supplier that encourages the customer to purchase defective and deteriorated items other than regular purchase. So the effect of deterioration and defective items cannot be ignored in inventory models.

Most inventory models considered the request rate to be either stock needy or consistent or time-subordinate. It has been observed that decrease in the cost of the item for the most part positively affects request of the item. It becomes a necessity to make a proper strategy to maintain the inventory economically.

Ghare et al. (1963) developed an inventory model for the exponentially decaying inventory system. These types of models were extended and improved by Misra (1975). The investigators generally have taken the demand as constant. In reality, demand always depends on selling price of an item, population of that area, deterioration, the frequency of advertisement of the product etc. As time advanced, a few researchers created inventory models with deteriorating items, shortage items, demand patterns, cost patterns, items order cycles and their combinations.

Bhunia et al. (2014) derived a deterministic inventory model where deteriorated items demand depends upon selling price of items and the frequency of advertisement. Ghoreishi et al. (2014) researched on an inventory model for non-instantaneous deteriorating items with partial backlogging, permissible delay in payments, inflation- and selling price-dependent demand and customer returns. On the other hand, to reduce the cost, an intelligent businessman or a production company always produce products depends on demand.

Without any ambiguity, many inventory model based on different kinds of vulnerabilities are classically modelled using the approaches from the probability hypothesis. Some of the business fit such conditions, yet applying these models as they may be, for the most part, prompts incorrect choices. Here fuzzy inventory models



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fulfil that gap. We can get more exact outcomes for inventory problems, rather than

the conventional likelihood hypothesis by using fuzzy set theory.

It was presented by Zadeh (1965) whose research work has been receiving considerable attention from investigators in production and inventory system. Bellmann et al. (1970) proposed a scientific model on decision making in fuzzy condition. Later, Dubois et al. (1978) defined some operations on fuzzy numbers. Zimmermann (1985) made an attempt to use the fuzzy sets in operation research. Syed et al. (2007) investigated a fuzzy inventory model without shortages using signed

distance method.

Dutta et al. (2012) contributed on fuzzy inventory model without shortage using trapezoidal fuzzy number. Maragatham et al. (2014) researched on a fuzzy inventory model for deteriorating items with price-dependent demand. Islam and Biswas (2017) studied on a fuzzy inventory model having exponential demand with weibull distribution for non-instantaneous deterioration, shortages under partially backlogging and time dependent holding cost.

1.1. Motivation & Contribution of Study

In the proposed model, we have shown a fuzzy deterministic stock model for non-instantaneous deteriorating things with production proportional to demand and variable demand pattern depends on population, selling price and frequency of advertisement which is variables or constants according to any real-life situation. Here

we treated those as constants.

So, any production company produces any items according to demand. On the other hand, defection and deterioration occur for any production. In such situation price discount is a common phenomenon. The inventory parameters are taken as the triangular fuzzy number. Signed distance method is used to defuzzify the model. The goal for finding the solution for minimizing the total cost has been derived. To the author's best of knowledge such type of model has not yet been discussed in the inventory literature.

inventory incrature.

2. DEFINITIONS AND FUZZY PRELIMINARIES

**Definition 2.1:** A fuzzy set  $\widetilde{A}$  is a universe of discourse X is defined as the following set of pairs  $\widetilde{A} = \{(x, \mu_{\widetilde{A}}(x): x \in X\}$ . Where  $\mu_{\widetilde{A}}(x) \to [0,1]$  is a mapping called

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the membership function of the set  $\widetilde{A}$  and  $\mu_{\widetilde{A}}(x)$  is called the membership value or degree of membership of  $x \in X$  in the fuzzy set  $\widetilde{A}$ . The larger  $\mu_{\widetilde{A}}(x)$  is stronger the grade of membership form in  $\widetilde{A}$ .

**Definition 2.2:** A fuzzy set  $\widetilde{A}$  of the universe of discourse X is convex if and only if for all  $x_1, x_2 \in X$ ,  $\mu_{\widetilde{A}}(\lambda x_1 + (1 - \lambda)x_2) \ge \min[\mu_{\widetilde{A}}(x_1), \mu_{\widetilde{A}}(x_2)]$  when  $0 \le \lambda \le 1$ .

**Definition 2.3:** A fuzzy set  $\widetilde{A}$  of the universe of discourse X is called normal fuzzy set implying that there exists at least one  $x \in X$  such that  $\mu_{\widetilde{A}}(x) = 1$ .

**Definition 2.4:** The  $\alpha$  – cut of  $\widetilde{A}$  is defined as a crisp set  $A_{\alpha}$ ={x :  $\mu_{\widetilde{A}}(x) \geq \alpha$ , x  $\in$  X where  $\alpha \in [0,1]$ .  $A_{\alpha}$  is a non-empty bounded closed interval contained in X and it can be denoted by  $A_{\alpha} = [A_L(\alpha), A_R(\alpha)]$ . Where  $A_L(\alpha)$  and  $A_R(\alpha)$  are the lower and upper bounds of the closed interval respectively.

**Definition 2.5:** A fuzzy number is a fuzzy set in the universe of discourse X that is both convex and normal. The following figure (3) shows a fuzzy number  $\widetilde{A}$ .

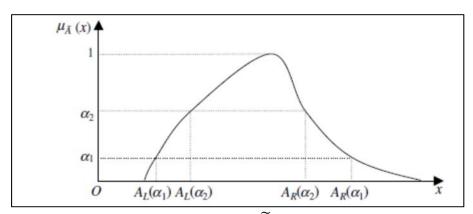


Figure 1: Fuzzy number  $\widetilde{A}$  With  $\alpha$ -cuts.

Above figure-1, shows a fuzzy number  $\widetilde{A}$  with  $\alpha$ -cuts  $A_{\alpha_1} = [A_L(\alpha_1), A_R(\alpha_1)],$   $A_{\alpha_2} = [A_L(\alpha_2), A_R(\alpha_2)].$  It is seen that if  $\alpha_2 \geq \alpha_1$  then  $A_L(\alpha_2) \geq A_L(\alpha_1)$  and  $A_R(\alpha_2) \geq A_R(\alpha_1).$ 

**Definition 2.6:** The function principle is used for the operation for Addition, Subtraction, Multiplication and Division of fuzzy numbers. Suppose  $\widetilde{A}=(a_1,a_2,a_3)$  and  $\widetilde{B}=(b_1,\,b_2,\,b_3)$  are two triangular fuzzy numbers. Then\_



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- (i) Addition:  $\widetilde{A} + \widetilde{B} = (a_1 + b_1, a_2 + b_2, a_3 + b_3)$ , where  $a_1, a_2, a_3; b_1, b_2, b_3$  are any real numbers.
- (ii) Subtraction:  $\widetilde{A}$   $\widetilde{B}$  =  $(a_1 b_1, a_2 b_2, a_3 b_3)$ , where  $a_1, a_2, a_3; b_1, b_2, b_3$  are any real numbers.
- (iii) Multiplication:  $\widetilde{A} \times \widetilde{B} = (a_1b_1, a_2b_2, a_3b_3)$ , where  $a_1, a_2, a_3$ ;  $b_1, b_2, b_3$  are all non-zero positive real numbers.
- (iv) Division:  $\frac{\widetilde{A}}{\widetilde{B}} = (\frac{a_1}{b_3}, \frac{a_2}{b_2}, \frac{a_3}{b_1})$ , where  $b_1$ ,  $b_2$ ,  $b_3$  are all non-zero positive real numbers.
- (v) Scalar Multiplication: For any real number K,

$$K\widetilde{A} = (Ka_1, Ka_2, Ka_3)$$
, Where  $K \ge 0$ ,  $K\widetilde{A} = (Ka_3, Ka_2, Ka_1)$  Where  $K < 0$ ,

**Definition 2.7:** The  $\alpha$  – cut of  $\widetilde{A}$  is defined by  $A_{\alpha} = \{x : \mu_{\widetilde{A}}(x) = \alpha, \alpha \geq 0\}$ .

**Definition 2.8:** Among the various shapes of fuzzy number, triangular fuzzy number (TFN) is the most popular one.  $\widetilde{A}$  is represented by the triplet  $(a_1, a_2, a_3)$  and is defined by its continuous membership function where  $\mu_{\widetilde{A}}(x):X\to[0,1]$  is given by

$$\mu_{\widetilde{A}}(x) = f(x) = \begin{cases} 1 - \frac{a_2 - x}{a_2 - a_1}, & \text{for } a_1 \le x \le a_2 \\ 1, & \text{for } x = a_2 \\ 1 - \frac{x - a_1}{a_2 - a_1}, & \text{for } a_2 \le x \le a_3 \\ 0, & \text{for Otherwise} \end{cases}$$

**Definition 2.9:** The  $\alpha$ -level set of the triangular number  $\widetilde{A} = (a_1, a_2, a_3)$  is :

$$A_{\alpha} = \{x : \mu_{\widetilde{A}}(x) \ge \alpha\} = [A_{L}(\alpha), A_{R}(\alpha)].$$

Where 
$$A_L(\alpha) = a_1 + (a_2 - a_1)\alpha$$
,  $\alpha \in [0,1]$ , And  $A_R(\alpha) = a_3 - (a_3 - a_2)\alpha$ ,  $\alpha \in [0,1]$ .

We represent  $\widetilde{A} = (a_1, a_2, a_3) = \cup [A_L(\alpha), A_R(\alpha)]; 0 \le \alpha \le 1.$ 

**Definition 2.10**: Defuzzification of  $\widetilde{A}$  can be found by Signed Distance Method. If  $\widetilde{A}$  is a triangular fuzzy number then sign distance from  $\widetilde{A}$  to 0 is defined as:

$$d(\widetilde{A}, 0) = \frac{1}{2} \int_{0}^{1} [\{A_{L}(\alpha), A_{R}(\alpha)\}, 0] d\alpha$$



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Where,  $A_{\alpha}=[A_L(\alpha),A_R(\alpha)]$  and  $A_{\alpha}=[a_1+(a_2-a_1)\alpha,\ a_3-(a_3-a_2)\alpha],\alpha\in[0,1]$  is  $\alpha-{\rm cut}$  off fuzzy set  $\widetilde{A}$ , which is a close interval.

### 3. NOTATIONS AND ASSUMPTIONS:

This inventory model is produced based on the accompanying Assumptions and Notations which are utilized all through this paper in Crisp and Fuzzy Environment.

#### ❖ Notations:

- $\triangleright$  I(t): The inventory level at any time t, t ≥ 0.
- C<sub>1</sub>: The fixed operating cost of the inventory.
- > C<sub>2</sub>: The advertisement cost per advertisement.
- > lp: The production cost per unit per unit time.
- Tac: The total average cost per unit per cycle.
- $\triangleright$   $\widetilde{C_1}$ : The Fuzzy fixed operating cost of the inventory.
- $\triangleright$   $\widetilde{C_2}$ : Fuzzy advertisement cost per advertisement.
- Tac: Fuzzy total average cost per unit per cycle.
- >  $t_1$ : The production time when the quality of products in stock reaches maximum  $L_m$ ,  $t_1$ > 0.
- $\succ$  t<sub>2</sub>: The time duration where there is no production but deteriorating and end of t<sub>2</sub> the inventory level diminished gradually to zero, t<sub>2</sub>> 0.
- $\succ$  t<sub>1</sub> + t<sub>2</sub>: The length of cycle time, t<sub>1</sub> + t<sub>2</sub>> 0.

## **❖** Assumptions :

- Fig. The rate of non-instantaneous decay whenever any time t > 0 is time proportional,  $\theta(t) = \beta t$ ; where,  $\beta$  ( 0 <  $\beta$  < 1 ) is the scale parameter.
- The demand rate  $D(m, p, f) = \frac{mf}{p}$  is dependent on population (m), selling price (p) of an item and the frequency of advertisement (f), where m, p, f > 0.
- ightharpoonup Production rate  $K(k,m,p,a)=kD(m,p,f)=k\,rac{mf}{p},$  where k is a positive constant.
- ➤ Holding cost is h, a constant.



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- Lead time is zero or negligible.
- > The discounted rate d per unit per unit time.
- The Defective items rate r per time for each cycle.
- The horizontal planning takes place at an infinite rate.
- ➤ There is no replenishment or repair of deteriorating and defective items takes place in the given cycle.
- > The lead time is considered zero.

# 4. PRODUCTION INVENTORY MODEL IN CRISP ENVIRONMENT IS PRODUCED AS FOLLOW:

Let, the producer start to produce items at the start of each cycle when t=0 to satisfy the arriving demands in the inventory system. At the end of time  $t_1$ , the production stopped where number of r items are produced defective. We assume the inventory level reached to its highest level  $L_{\rm m}(>0)$  at end of  $t_1$ . During the time interval  $t_2$ , the inventory level diminishes owing to customer demand and deterioration and finally falls to zero at  $t=t_1+t_2$ . Figure – 2 delineates the inventory level of the proposed model.

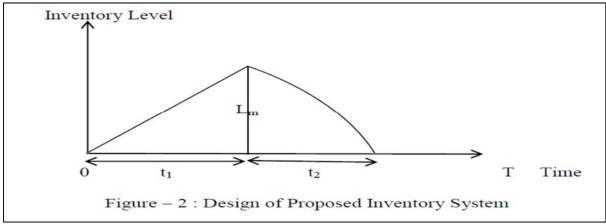


Figure 2: Design of Proposed Inventory System

The Inventory Level in  $t_1(0 \le t \le t_1)$ : The produced items during  $t_1$  would be depleted due to the instant demand as well as defective items. Under above assumption, during the period  $t_1$ , the inventory status of the system is given by the following differential equation-

$$\frac{dI_1(t)}{dt} = kD(m, p, f) - D(m, p, f) - r, \quad for \ (0 \le t \le t_1)$$
 (1)



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From the initial Condition  $I_1(0) = 0$  and  $I_1(t_1) = L_m$  get from above equation (1),

$$I_1(t) = \left(k \frac{mf}{p} - \frac{mf}{p} - r\right)t, \qquad for (0 \le t \le t_1)$$
 (2)

And 
$$L_m = \left(k \frac{mf}{p} - \frac{mf}{p} - r\right) t_1,$$
 (3)

The Inventory Level in  $t_2(t_2 \le t \le t_1 + t_2)$ : In this time, the inventory declines due to customers' demand and deterioration. Hence, the status of the inventory level during  $t_2$  is governed by the following Differential Equation,

$$\frac{dI_2(t)}{dt} + \beta I_2(t) = -D(m, p, f), \text{ for } (t_1 \le t \le t_1 + t_2)$$
(4)

From the boundary condition  $I_2(t_1 + t_2) = 0$  and dismissing the higher intensity of  $\beta$  and taking taking initial two terms of the exponential series, we get,

$$I_{2}(t) = \left[\frac{mf}{p}\right] \left[t_{1} + t_{2} - t + \beta \frac{t^{3}}{3} + \frac{\beta(t_{1} + t_{2})^{3}}{6} - \beta(t_{1} + t_{2}) \frac{t^{2}}{2}\right],$$
 (5)

According to above discussion, the following cost function can be derived.

1. The Operating cost during the period 
$$[0, t_1 + t_2]$$
:  $C_1$  (6)

2. The Production cost during the period 
$$[0, t_1]$$
:  $lpk \frac{mf}{p} t_1 = klmf t_1$ , (7)

3. The Inventory Holding Cost during the period  $[0,t_1+t_2]: \int_0^{t_1} h I_1(t) dt + \int_{t_1}^{t_1+t_2} h I_2(t) dt$ 

Using equation (2) and (5), then integrating, we get from above the Holding Cost,

$$h\left(k\frac{mf}{p} - \frac{mf}{p} - r\right)\frac{t_1^2}{2} + h\frac{mf}{p}\left\{\frac{(t_1 + t_2)^2}{2} + \beta\frac{(t_1 + t_2)^4}{12} - t_1t_2 - \frac{t_1^2}{2} - \beta\frac{t_1^4}{12} - \frac{\beta(t_1 + t_2)^3}{6}t_1 + \beta(t_1 + t_2)\frac{t_1^3}{6}\right\}$$

$$(8)$$

4. The Deteriorating Cost during the period [  $t_1$ ,  $t_1+t_2$ ] :  $lp \int_{t_1}^{t_1+t_2} \beta t I_2(t) dt$ 

Using equation (5) and integrating, we get from above the Deteriorating Cost,

$$\beta \operatorname{lmf}\left[\frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2}t_2\right] \tag{9}$$

- 5. The Advertisement cost during the period  $[0, t_1 + t_2]$ :  $C_2f$  (10)
- 6. The Price Discount during the period [ $t_1$ ,  $t_1 + t_2$ ]:  $lpd \int_{t_1}^{t_1+t_2} \frac{mf}{p} dt$



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We get from above; Price Discount is 
$$ldmft_2$$
 (11)

Therefore the total average cost function per cycle:  $\frac{1}{(t_1+t_2)}$  [Operating Cost + Production Cost + Inventory Holding Cost + Deteriorating Cost + Advertisement Cost + Price Discount].

Hence the average net cost function is

$$\text{Tac } (t_1, t_2) = \frac{1}{(t_1 + t_2)} [C_1 + \text{klmft}_1 + \text{h} \left( \frac{\text{mf}}{p} - \frac{\text{mf}}{p} - r \right) \frac{t_1^2}{2} + \text{h} \frac{\text{mf}}{p} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{\beta(t_1 + t_2)^3}{6} t_1 + \beta(t_1 + t_2) \frac{t_1^3}{6} \right\} \\ + \beta \text{lmf} \left[ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right] + C_2 f + \text{ldmft}_2 \right],$$

$$(12)$$

Now, the necessary condition for the total average cost function of the system is minimize if equation (12) is satisfy,

$$\frac{\partial \operatorname{Tac}(t_1, t_2)}{\partial t_1} = 0, \tag{13}$$

And 
$$\frac{\partial \operatorname{Tac}(t_1, t_2)}{\partial t_2} = 0$$
, (14)

The solution, which might be called feasible solution of the problem, of the conditions (13) and (14) give the optimal solutions of  $t_1 = t_1^*$  and  $t_2 = t_2^*$  which minimize  $Tac(t_1, t_2) = Tac(t_1, t_2)^*$  provide they satisfy the sufficient conditions-

$$\frac{\partial^{2} \operatorname{Tac}\left(t_{1}, t_{2}\right)}{\partial t_{1}^{2}} \cdot \frac{\partial^{2} \operatorname{Tac}\left(t_{1}, t_{2}\right)}{\partial t_{2}^{2}} - \left(\frac{\partial^{2} \operatorname{Tac}\left(t_{1}, t_{2}\right)}{\partial t_{1} \partial t_{2}}\right)^{2} > 0, \tag{15}$$

And 
$$\frac{\partial^2 \text{Tac}(t_1, t_2)}{\partial t_1^2} > 0$$
 or,  $\frac{\partial^2 \text{Tac}(t_1, t_2)}{\partial t_2^2} > 0$ , (16)

However, it's difficult to solve the problem by inferring an explicit equation of the solutions from conditions (13) and (14). Therefore, we solve the optimal service level of  $t_1 = t_1^*$  and  $t_2 = t_2^*$  by using the software LINGO 17.0. Moreover, we also verify that the sufficient conditions of the optimality of the solutions of  $t_1 = t_1^*$  and  $t_2 = t_2^*$  are satisfied (i.e. inequalities (15) and (16)) under certain conditions.

# 5. THE PROPOSED INVENTORY MODEL IN FUZZY ENVIRONMENT IS PRODUCED AS FOLLOW:

Presently the above model will be produced in fuzzy Environment. Due to uncertainly, it is difficult to characterize every one of the parameters definitely. Let us



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assume that,  $\widetilde{C_1} = (C_1^1, C_1^2, C_1^3)$ ,  $\widetilde{h} = (h^1, h^2, h^3)$ ,  $\widetilde{p} = (p^1, p^2, p^3)$ ,  $\widetilde{C_2} = (C_2^1, C_2^2, C_2^3)$ , be Triangular Fuzzy Number in LR-form then the total average cost function of the system per unit time in fuzzy environment is given by-

$$\begin{split} &\operatorname{Tac}\, \widetilde{(t_1,\ t_2)} = \frac{1}{(t_1 + t_2)} [\widetilde{C_1} + \operatorname{klmft}_1 + \widetilde{h} \left( \operatorname{k} \frac{\operatorname{mf}}{\widetilde{p}} - \frac{\operatorname{mf}}{\widetilde{p}} - r \right) \frac{t_1^2}{2} + \widetilde{h} \, \frac{\operatorname{mf}}{\widetilde{p}} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{\beta(t_1 + t_2)^3}{6} t_1 + \beta(t_1 + t_2) \frac{t_1^3}{6} \right\} \\ &+ \beta \operatorname{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right\} \\ &+ \widetilde{C_2} f + \operatorname{ldmft_2} \right] \\ &\operatorname{Or,} \operatorname{Tac}\, \widetilde{(t_1,\ t_2)} = \frac{1}{(t_1 + t_2)} [(C_1^1, C_1^2, C_1^3) + \operatorname{klmft_1} + (h^1, h^2, h^3) \left( \operatorname{k} \frac{\operatorname{mf}}{(p^1, p^2, p^3)} - \frac{\operatorname{mf}}{(p^1, p^2, p^3)} - r \right) \frac{t_1^2}{2} \\ &+ (h^1, h^2, h^3) \frac{\operatorname{mf}}{(p^1, p^2, p^3)} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{\beta(t_1 + t_2)^3}{6} t_1 + \beta(t_1 + t_2) \frac{t_1^3}{6} \right\} \\ &+ \beta \operatorname{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^3}{2} t_2 \right\} + (C_2^1, C_2^2, C_2^3) f + \operatorname{ldmft_2} \right] = (U, V, W) \left( \operatorname{Say} \right) \end{aligned} \tag{17} \\ & \text{Where, } U = \frac{1}{(t_1 + t_2)} [C_1^1 + \operatorname{klmft_1} + h^1 \left( \operatorname{k} \frac{\operatorname{mf}}{p^1} - \frac{\operatorname{mf}}{p^1} - r \right) \frac{t_1^2}{2} + h^1 \frac{\operatorname{mf}}{p^1} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \frac{t_1^4}{2} - \frac{\beta(t_1 + t_2)^3}{6} t_1 + \beta(t_1 + t_2) \frac{t_1^3}{6} \right\} + \beta \operatorname{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right\} + C_2^1 f + \operatorname{ldmft_2} \right]; \\ & V = \frac{1}{(t_1 + t_2)} [C_1^2 + \operatorname{klmft_1} + h^2 \left( \operatorname{k} \frac{\operatorname{mf}}{p^2} - \frac{\operatorname{mf}}{p^2} - r \right) \frac{t_1^2}{2} + h^2 \frac{\operatorname{mf}}{p^2} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{\beta(t_1 + t_2)^3}{6} t_1 + \beta(t_1 + t_2) \frac{t_1^3}{6} \right\} + \beta \operatorname{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right\} + C_2^2 f + \operatorname{ldmft_2} \right]; \\ & V = \frac{1}{(t_1 + t_2)^3} \frac{h^2}{6} + h^2 \left( \operatorname{lmft_1} \right) \frac{h^2}{6} + \beta \operatorname{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right\} + C_2^2 f + \operatorname{ldmft_2} \right]; \\ & (t_1 + t_2)^3 \frac{h^2}{6} + h^2 \left( \operatorname{lmft_2} \right) \frac{h^2}{6} + \beta \operatorname{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^3}{2} \right\} + C_2^2 f + \operatorname{ldmft_2} \right]; \\ & (t_1 + t_2)^3 \frac{h^2}{6} + h^2 \left( \operatorname{lmft$$

$$\text{And, W} = \frac{1}{(t_1 + t_2)} [C_1^3 + \text{ klmft}_1 + \text{ h}^3 \left( \text{k} \frac{\text{mf}}{\text{p}^3} - \frac{\text{mf}}{\text{p}^3} - \text{r} \right) \frac{t_1^2}{2} + \text{h}^3 \frac{\text{mf}}{\text{p}^3} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} \right\} \\ = \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{\beta (t_1 + t_2)^3}{6} t_1 + \beta (t_1 + t_2) \frac{t_1^3}{6} \right\} + \beta \text{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right\} + C_2^3 f + \text{ldmft}_2 \right];$$

The  $\alpha-cuts,\ A_L(\alpha)$  and  $A_R(\alpha)$  of triangular fuzzy number Tac  $\widetilde{(\ t_1,\ t_2)}$  are given by-

$$\begin{split} A_L(\alpha) &= U + (V - U)\alpha = \frac{1}{(t_1 + t_2)} [C_1^1 + \ klmft_1 \ + \ h^1 \left( k \frac{mf}{p^1} - \frac{mf}{p^1} - r \right) \frac{t_1^2}{2} \ + \ h^1 \ \frac{mf}{p^1} \ \left\{ \frac{(t_1 + t_2)^2}{2} + \frac{h^2 \left( t_1 + t_2 \right)^2}{2} + \frac{h^2 \left( t_1 + t_2 \right)^2}{2} + \frac{h^2 \left( t_1 + t_2 \right)^2}{2} + \frac{h^2 \left( t_1 + t_2 \right)^3}{6} \right\} + \beta lmf \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right\} \ + \\ C_2^1 f + ldmft_2] + \frac{1}{(t_1 + t_2)} [(C_1^2 - C_1^1) + h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^1} - \frac{mf}{p^1} - r \right) \frac{t_1^2}{2} + \left( h^2 \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} + h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} + h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right\} \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} + h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} - h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} \right) \\ h^2 \frac{mf}{p^2} \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{mf}{p^2} \right) \\ h^2 \frac{mf$$

$$\text{And} \qquad A_R(\alpha) = W - (W - V)\alpha = \frac{1}{(t_1 + t_2)} \big[ C_1^3 + \text{ klmft}_1 \ + \ h^3 \left( k \frac{mf}{p^3} - \frac{mf}{p^3} - r \right) \frac{t_1^2}{2} \ + \\ h^3 \frac{mf}{p^3} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{\beta (t_1 + t_2)^3}{6} t_1 + \beta (t_1 + t_2) \frac{t_1^3}{6} \right\} +$$



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$$\begin{split} \beta lmf \{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \} + & C_2^3 f + ldmft_2 ] - \frac{1}{(t_1 + t_2)} [(C_1^3 - C_1^2) + h^3 \left( k \frac{mf}{p^3} - \frac{mf}{p^3} - r \right) \frac{t_1^2}{2} \\ - & h^2 \left( k \frac{mf}{p^2} - \frac{mf}{p^2} - r \right) \frac{t_1^2}{2} + (h^3 \frac{mf}{p^3} - h^2 \frac{mf}{p^2}) \\ & \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{t_1^2}{2} \right\} \\ & \frac{\beta (t_1 + t_2)^3}{6} t_1 + \beta (t_1 + t_2) \frac{t_1^3}{6} + (C_2^3 - C_2^2) f \right] \alpha \end{split}$$

We defuzzify the fuzzy average total cost function  $Tac\ (t_1,\ t_2)$  by Signed Distance Method as follows,

$$\begin{split} &\operatorname{Tac}_{sd} \widetilde{(t_1, t_2)} = \frac{1}{2(t_1 + t_2)} [C_1^1 + \operatorname{klmft}_1 + \operatorname{h}^1 \left( \operatorname{k} \frac{\operatorname{mf}}{\operatorname{p}^1} - \frac{\operatorname{mf}}{\operatorname{p}^1} - r \right) \frac{t_1^2}{2} + \operatorname{h}^1 \frac{\operatorname{mf}}{\operatorname{p}^1} \left\{ \frac{(t_1 + t_2)^2}{2} + \beta \frac{(t_1 + t_2)^4}{12} - t_1 t_2 - \frac{t_1^2}{2} - \beta \frac{t_1^4}{12} - \frac{\beta(t_1 + t_2)^3}{6} t_1 + \beta(t_1 + t_2) \frac{t_1^3}{6} \right\} + \beta \operatorname{lmf} \left\{ \frac{(t_1 + t_2)^3}{6} - \frac{t_1^3}{6} - \frac{t_1^2}{2} t_2 \right\} + C_2^1 f + \operatorname{ldmft}_2 \\ &+ \frac{1}{4(t_1 + t_2)} [(C_1^2 - C_1^1) + \operatorname{h}^2 \left( \operatorname{k} \frac{\operatorname{mf}}{\operatorname{p}^2} - \frac{\operatorname{mf}}{\operatorname{p}^2} - r \right) \frac{t_1^2}{2} - \operatorname{h}^1 \left( \operatorname{k} \frac{\operatorname{mf}}{\operatorname{p}^1} - \frac{\operatorname{mf}}{\operatorname{p}^1} - r \right) \frac{t_1^2}{2} + (\operatorname{h}^2 \frac{\operatorname{mf}}{\operatorname{p}^2} - \operatorname{h}^1 \frac{\operatorname{mf}}{\operatorname{p}^1}) \\ &+ \left( C_2^2 - C_2^1 \right) \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) + \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} + \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) + \operatorname{h}^3 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) + \operatorname{h}^3 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) + \operatorname{h}^3 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) + \operatorname{h}^3 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) + \operatorname{h}^3 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) + \operatorname{h}^3 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \frac{t_1^2}{2} \right) \right) \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \\ &+ \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \left( \operatorname{h}^2 \right) \right) \right) \right) \right) \right) \\ &+$$

Now, the necessary condition for the average total cost function of the system is minimize if equation (18) is satisfy,

$$\frac{\partial \operatorname{Tac}_{sd}(t_1, t_2)}{\partial t_1} = 0, \tag{19}$$

And 
$$\frac{\partial \operatorname{Tac}_{sd}(t_1, t_2)}{\partial t_2} = 0,$$
 (20)

The solution, which might be called feasible solution of the problem, of the conditions (19) and (20) give the optimal solutions of  $t_1 = t_1^*$  and  $t_2 = t_2^*$  which minimize  $Tac_{sd}(t_1, t_2) = Tac_{sd}(t_1, t_2)^*$  provide they satisfy the sufficient conditions-

$$\frac{\partial^{2} \operatorname{Tac}_{sd}(\widetilde{t}_{1}, t_{2})}{\partial t_{1}^{2}} \cdot \frac{\partial^{2} \operatorname{Tac}_{sd}(\widetilde{t}_{1}, t_{2})}{\partial t_{2}^{2}} - \left(\frac{\partial^{2} \operatorname{Tac}_{sd}(\widetilde{t}_{1}, t_{2})}{\partial t_{1} \partial t_{2}}\right)^{2} > 0$$
 (21)

And 
$$\frac{\partial^2 \operatorname{Tac}_{sd}(\widetilde{t_1}, t_2)}{\partial t_1^2} > 0$$
 Or,  $\frac{\partial^2 \operatorname{Tac}_{sd}(\widetilde{t_1}, t_2)}{\partial t_2^2} > 0$  (22)



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However, it's difficult to solve the problem by inferring an explicit equation of the solutions from conditions (19) and (20). Therefore, we solve the optimal service level  $t_1^*$  and the optimal cycle time  $t_1^* + t_2^*$  by using the software LINGO 16.0. Moreover, we also verify that the sufficient conditions of the optimality of the solutions  $t_1^*$  and  $t_2^*$  are satisfied (i.e. inequalities (21) and (22)) under certain conditions.

Similarly, the highest inventory level per unit time in fuzzy environment is given by

$$\widetilde{L_m} = \left(k \frac{mf}{\widetilde{p}} - \frac{mf}{\widetilde{p}} - r\right) t_1 = \left(k \frac{mf}{(p_1, p_2, p_3)} - \frac{mf}{(p_1, p_2, p_3)} - r\right) t_1 \tag{23}$$

Defuzzified value of fuzzy number  $\widetilde{L_m}$  by using Signed Distance Method is given by-

$$(\widetilde{L_{m}})_{sd} = \frac{1}{2} \left( k \frac{mf}{p_{1}} - \frac{mf}{p_{1}} - r \right) t_{1} + \frac{1}{4} \left( (k \frac{mf}{p_{2}} - \frac{mf}{p_{2}} - r) - (k \frac{mf}{p_{1}} - \frac{mf}{p_{1}} - r) \right) t_{1} + \frac{1}{2} \left( k \frac{mf}{p_{3}} - \frac{mf}{p_{3}} - r \right) t_{1} - \frac{1}{4} \left( (k \frac{mf}{p_{3}} - \frac{mf}{p_{3}} - r) - (k \frac{mf}{p_{2}} - \frac{mf}{p_{2}} - r) \right) t_{1}$$

$$(24)$$

#### 6. NUMERICAL SOLUTION:

**VI (A):** A company produces cell-phones. The company wants to minimize the total expenditure. The demand of cell-phones dependent on population (m=2565) of that area, selling price (p) which is near about \$.11.6, never less than \$8.6 and above \$14.6. and the frequency of advertisement (f) is near about 6. Production rate is proportional (k=1.5 times) to demand as well as production cost (l=0.15 times) is proportional to selling price. At this situation, the fixed operating cost ( $C_1$ ) of the inventory system is near about \$175, never less than \$150 and above \$200. Similarly, the holding cost (k) of the inventory system is near about \$1.2, never less than \$0.84 and above \$1.56 and the advertisement cost ( $C_2$ ) of the inventory system is near about \$50, never less than \$25 and above \$75. The defective cell-phones per unit time are (r=1) cell-phones where price discount is avail \$(d=1) 1.3. Also it is observe that the deteriorating rate is (l=1) 0.01. Determine the Optimal value of l=10.01. Optimal value of l=11.02.

According to above input data, the solution of the crisp-model is furnishing bellow in table-1.



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Table 1: Output Result in crisp environment

|                  | Table 1: Gatpat Research energy environment |         |                  |               |  |  |  |
|------------------|---------------------------------------------|---------|------------------|---------------|--|--|--|
| t <sub>1</sub> * |                                             | $t_2^*$ | $Tac(t_1,t_2)^*$ | ${\rm L_m}^*$ |  |  |  |
| 0.9168 0.5023    |                                             | 0.5023  | 3816.822         | 484.7281      |  |  |  |

**VI (B):** As discussed in the above example if we assume the parameters in fuzzy sense as:  $\widetilde{C_1}$  = ( 150, 175, 200 ),  $\widetilde{p}$  = ( 8.6, 11.6, 14.6 ),  $\widetilde{C_2}$  = ( 25, 50, 75 ),  $\widetilde{h}$  = (0.84, 1.2, 1.56 ), where other parameters are unchanged. The solution of fuzzy model by Signed Distance Method is obtained bellow:

(1). When  $\widetilde{C_1}$ ,  $\widetilde{p}$ ,  $\widetilde{C_2}$  and  $\widetilde{h}$  are all Triangular fuzzy numbers then the solution is given bellow table:

Table 2: Output Result in fuzzy environment for case-1.

| $t_1^*$ | t <sub>2</sub> * | $Tac_{sd}(t_1,t_2)^*$ | ${\rm L_m}^*$ |
|---------|------------------|-----------------------|---------------|
| 0.9191  | 0.5040           | 3814.925              | 503.4081      |

(2). When  $\widetilde{C_1}$ ,  $\widetilde{p}$ , and  $\widetilde{C_2}$  are Triangular fuzzy numbers then the solution is given bellow table:

Table 3: Output Result in fuzzy environment for case-2.

| $t_1^*$ $t_2^*$ |        | $Tac_{sd}(t_1,t_2)^*$ | L <sub>m</sub> * |          |
|-----------------|--------|-----------------------|------------------|----------|
|                 | 0.9031 | 0.4924                | 3828.560         | 494.6113 |

(3). When  $\widetilde{C_1}$ , and  $\widetilde{p}$  are Triangular fuzzy numbers then the solution is given bellow table:

Table 4: Output Result in fuzzy environment for case-3.

|         | • • • • • • • • • • • • • • • • • • • |                       |               |
|---------|---------------------------------------|-----------------------|---------------|
| $t_1^*$ | t <sub>2</sub> *                      | $Tac_{sd}(t_1,t_2)^*$ | ${\rm L_m}^*$ |
| 0.9031  | 0.4924                                | 3828.560              | 494.6113      |

(4). When only  $\widetilde{C}_1$  is Triangular fuzzy numbers then the solution is given bellow table:

Table 5: Output Result in fuzzy environment for case-4.

| t <sub>1</sub> * | t <sub>2</sub> * | $Tac_{sd}(t_1,t_2)^*$ | L <sub>m</sub> * |
|------------------|------------------|-----------------------|------------------|
| 0.9168           | 0.5023           | 3816.822              | 484.7281         |

(5). When none of  $\widetilde{C_1}$ ,  $\widetilde{p}$ ,  $\widetilde{C_2}$  and  $\widetilde{h}$  is a Triangular fuzzy numbers then the solution is given bellow table:

Table 6: Output Result in fuzzy environment for case-5.

| t <sub>1</sub> * | t <sub>2</sub> * | $Tac_{sd}(t_1,t_2)^*$ | L <sub>m</sub> * |
|------------------|------------------|-----------------------|------------------|
| 0.9168           | 0.5023           | 3816.822              | 484.7281         |

Comparison of Optimal Solutions is given in Table-7:

| Model | Optimal value of t <sub>1</sub> | Optimal value of t <sub>2</sub> | Optimal value of Tac( $t_1, t_2$ ) | Optimal value of L <sub>m</sub> |
|-------|---------------------------------|---------------------------------|------------------------------------|---------------------------------|
| Crisp | 0.9168                          | 0.5023                          | 3816.822                           | 484.7281                        |
| Fuzzy | 0.9191                          | 0.5040                          | 3814.925                           | 503.4081                        |



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### 7. SENSITIVITY ANALYSIS

We currently analyse to sensitivity analysis of the optimal solution of the model for change system parameters  $C_1$ , k,  $C_2$ , m, f, h, p, d, l, r and  $\beta$  by -30%, -15%, +15%, +30% individually, keeping alternate parameters unaltered. The underlying information is taken from the above numerical illustration.

Table 8: Sensitivity Analysis

| Parameters                                                     | Changed Value | *PCPV | t <sub>1</sub> *                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | t <sub>2</sub> *                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | $Tac(t_1,t_2)^*$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | ${\mathbb{L}_{m}}^*$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |
|----------------------------------------------------------------|---------------|-------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|                                                                | 122.5         | -30   | 0.8572                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.4795                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3778.723                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 453.2304                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 148.75        | -15   | 0.8572         0.4795         3778.723           0.8875         0.4911         3798.057           0.9168         0.5023         3816.822           0.9454         0.5132         3835.066           0.9731         0.5238         3852.839           0.0000         0.7685         4233.764           1.7367         0.1635         3268.603           0.9168         0.5023         3816.822           0.4117         0.6943         4121.946           0.0184         0.7681         4233.477           0.8123         0.4622         3750.002           0.8660         0.4828         3784.308           0.9168         0.5023         3816.822           0.9653         0.5208         3847.801           1.0115         0.5385         3877.443           1.1219         0.5797         2762.855           1.0329         0.5462         3155.231           0.9168         0.5023         3816.822           0.8459         0.4753         4337.446           0.7875         0.4529         4854.907           0.9975         0.5325         2707.156           0.9508         0.5150         3262.388 <td>469.2162</td> | 469.2162                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| $C_1 = 175$                                                    | 175           | 00    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | t <sub>2</sub> *         Tac(t <sub>1</sub> ,t <sub>2</sub> )*           0.4795         3778.723           0.4911         3798.057           0.5023         3816.822           0.5132         3835.066           0.5238         3852.839           0.7685         4233.764           0.1635         3268.603           0.5023         3816.822           0.6943         4121.946           0.7681         4233.477           0.4622         3750.002           0.4828         3784.308           0.5023         3816.822           0.5208         3847.801           0.5385         3877.443           0.5797         2762.855           0.5462         3155.231           0.5023         3816.822           0.4753         4337.446           0.4529         4854.907           0.5325         2707.156           0.5150         3262.388           0.5023         3816.822           0.4926         4370.720           0.4850         4924.238           0.6151         3709.147           0.5509         3765.363           0.5023         3816.822           0.4640 | 484.7281                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 201.25        | +15   | 0.9454                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5132                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3835.066                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 499.8058                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 227.5         | +30   | 0.9731                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5238                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3852.839                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 514.4838                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 0.98          | -30   | 0.0000                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.7685                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 4233.764                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 0.0000                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |
|                                                                | 1.19          | -15   | 1.7367                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.1635                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3268.603                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 434.3065                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| k = 1.4                                                        | 1.4           | 00    | 0.9168                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5023                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3816.822                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 484.7281                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 1.61          | +15   | 0.4117                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.6943                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 4121.946                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3 453.2304<br>7 469.2162<br>2 484.7281<br>6 499.8058<br>9 514.4838<br>4 0.0000<br>3 434.3065<br>2 484.7281<br>6 332.3405<br>7 19.0962<br>2 429.4780<br>8 457.8487<br>2 484.7281<br>1 510.3290<br>3 534.8182<br>5 414.5397<br>1 442.4768<br>2 484.7281<br>6 514.5294<br>7 541.6986<br>6 308.5458<br>8 426.9689<br>2 484.7281<br>0 542.0407<br>8 599.0377<br>7 562.4372<br>3 519.1984<br>2 484.7281<br>1 456.4212<br>3 432.6353<br>4 593.0900<br>0 531.7821<br>2 484.7281<br>9 446.3356<br>7 416.1339<br>4 71.7164<br>5 320.0902<br>2 484.7281<br>9 446.3356<br>7 416.1339<br>4 71.7164<br>5 320.0902<br>2 484.7281<br>9 446.3356<br>7 416.1339<br>4 71.7164<br>5 320.0902<br>2 484.7281<br>9 446.3356<br>7 416.1339                                                                                                                                                                                                                                                                  |
|                                                                | 1.82          | +30   | 0.0184                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.7681                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 4233.477                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 19.0962                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             |
|                                                                | 35            | -30   | 0.8123                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.4622                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3750.002                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 429.4780                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 42.5          | -15   | 0.8660                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.4828                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3784.308                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 453.2304<br>469.2162<br>484.7281<br>499.8058<br>514.4838<br>0.0000<br>434.3065<br>484.7281<br>332.3405<br>19.0962<br>429.4780<br>457.8487<br>484.7281<br>510.3290<br>534.8182<br>414.5397<br>442.4768<br>484.7281<br>514.5294<br>541.6986<br>308.5458<br>426.9689<br>484.7281<br>542.0407<br>599.0377<br>562.4372<br>519.1984<br>484.7281<br>456.4212<br>432.6353<br>593.0900<br>531.7821<br>484.7281<br>446.3356<br>416.1339<br>71.7164<br>320.0902<br>484.7281<br>592.7702<br>644.6292                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| $C_2 = 50$                                                     | 50            | 00    | 0.9168                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5023                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3816.822                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 57.5          | +15   | 0.9653                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5208                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3778.723         453.2           3798.057         469.2           3816.822         484.7           3835.066         499.8           3852.839         514.4           4233.764         0.00           3268.603         434.3           3816.822         484.7           4121.946         332.3           4233.477         19.09           3750.002         429.4           3784.308         457.8           3816.822         484.7           3847.801         510.3           3877.443         534.8           2762.855         414.5           3155.231         442.4           3816.822         484.7           4337.446         514.5           4454.907         541.6           2707.156         308.5           3262.388         426.9           3816.822         484.7           4370.720         542.0           4924.238         599.0           3709.147         562.4           3864.551         456.4           3909.253         432.6           3816.822         484.7           3771.299         446.3      < | 510.3290                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| $C_1 = 175$ $k = 1.4$                                          | 65            | +30   | 1.0115                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5385                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3877.443                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 534.8182                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 1795.5        | -30   | 1.1219                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 2762.855                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 2080.25       | -15   | 1.0329                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5462                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3155.231                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 442.4768                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| m=2565                                                         | 2565          | 00    | 0.9168                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5023                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3816.822                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 723         453.2304           057         469.2162           322         484.7281           066         499.8058           339         514.4838           764         0.0000           603         434.3065           322         484.7281           946         332.3405           477         19.0962           902         429.4780           308         457.8487           322         484.7281           301         510.3290           443         534.8182           355         414.5397           231         442.4768           322         484.7281           446         514.5294           907         541.6986           156         308.5458           388         426.9689           382         484.7281           720         542.0407           238         599.0377           147         562.4372           363         519.1984           322         484.7281           351         456.4212           253         432.6353           314         593.0900 |
| $C_1 = 175$ $k = 1.4$ $C_2 = 50$ $m = 2565$ $f = 6$ $p = 11.6$ | 2949.75       | +15   | 0.8459                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.4753                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 4337.446                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 514.5294                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 3334.5        | +30   | 0.7875                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 4854.907                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 541.6986                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 4.2           | -30   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| f = 6                                                          | 5.1           | -15   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 6             | 00    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| _                                                              | 6.9           | +15   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 7.8           | +30   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 0.84          | -30   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 1.02          | -15   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| h = 1.2                                                        | 1.2           | 00    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 1.38          | +15   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 1.56          | +30   | 0.8183                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.4328                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3909.253                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 432.6353                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 8.12          | -30   | 0.7844                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.4104                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3945.814                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 593.0900                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 9.86          | -15   | 0.8545                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 531.7821                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| p = 11.6                                                       | 11.6          | 00    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 13.35         | +15   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 446.3356                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 15.08         | +30   | 1.0244                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.5829                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3735.587                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 416.1339                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 0.91          | -30   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 1.105         | -15   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
| d = 1.3                                                        | 1.3           | 00    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 1.425         | +15   | 1.1212                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.3035                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3944.362                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 592.7702                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 1.69          | +30   | 1.2193                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.0642                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 4005.503                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 644.6292                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
|                                                                | 0.105         | -30   |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |
|                                                                | 0.1275        | -15   | 0.9363                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 0.4894                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 3343.782                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 495.0048                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |

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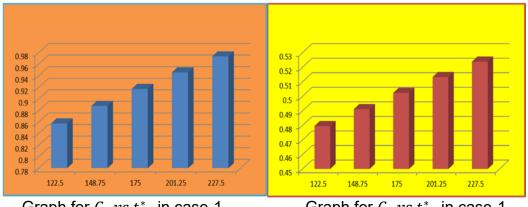
| l = 0.15       | 0.15   | 00  | 0.9168 | 0.5023 | 3816.822 | 484.7281 |
|----------------|--------|-----|--------|--------|----------|----------|
|                | 0.1725 | +15 | 0.8968 | 0.5150 | 4289.504 | 474.1139 |
|                | 0.195  | +30 | 0.8760 | 0.5274 | 4761.822 | 463.1572 |
|                | 1.4    | -30 | 0.9161 | 0.5024 | 3817.035 | 484.9041 |
|                | 1.7    | -15 | 0.9165 | 0.5024 | 3816.929 | 484.8161 |
| r = 2          | 2      | 00  | 0.9168 | 0.5023 | 3816.822 | 484.7281 |
|                | 2.3    | +15 | 0.9172 | 0.5022 | 3816.716 | 484.600  |
|                | 2.6    | +30 | 0.9176 | 0.5022 | 3816.609 | 484.5518 |
|                | 0.0070 | -30 | 0.9172 | 0.5048 | 3816.068 | 484.8918 |
|                | 0.0085 | -15 | 0.9170 | 0.5038 | 3816.446 | 484.8086 |
| $\beta = 0.01$ | 0.0100 | 00  | 0.9168 | 0.5023 | 3816.822 | 484.7281 |
|                | 0.0115 | +15 | 0.9167 | 0.5011 | 3817.197 | 484.6501 |
|                | 0.0130 | +30 | 0.9153 | 0.4865 | 3821.674 | 483.8837 |

\*PCPV = Percentage Change in Parameter Values.

#### 8. OBSERVATIONS:

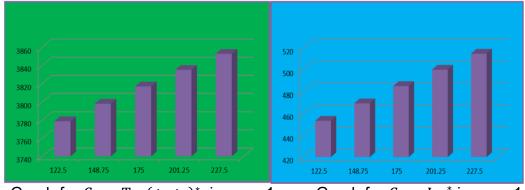
From the above table we can close the accompanying:

(1). From the above table, for increasing of  $C_1$ , the optimal value of  $t_1^*$  and  $t_2^*$  increase slowly. By this effect, the total average cost  $Tac(t_1,t_2)^*$  and the highest inventory level  $L_m^*$  increase slowly. Bellow the graph to illustrate these results:



Graph for  $C_1 vs t_1^*$  in case-1

Graph for  $C_1 vs t^*_2$  in case-1



Graph for  $C_1$  vs Tac( $t_1$ ,  $t_2$ )\* in case-1

Graph for  $C_1 vs L_m^*$  in case-1

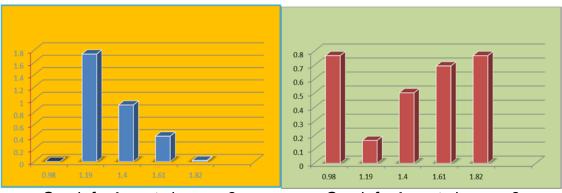
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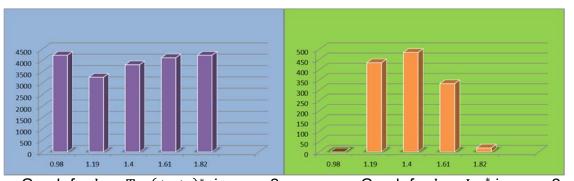
DOI: 10.14807/ijmp.v10i5.897

(2). From the above table, when k < 1 i.e. 0.98, the optimal value of  $t_1^*$  and the highest inventory level  $L_m^*$  become zero where the optimal value of  $t_2^*$  increase. With this effect the total average cost  $Tac(t_1,t_2)^*$  increase. Apart from this, for increasing of k, the optimal value of  $t_1^*$  decrease and the optimal value of  $t_2^*$  increase rapidly. By this effect, the total average cost  $Tac(t_1,t_2)^*$  increase and the highest inventory level  $L_m^*$  decrease rapidly. Bellow the graph to illustrate these results:



Graph for  $k vs t_1^*$  in case-2

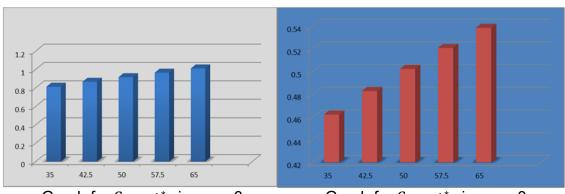
Graph for  $k vs t_2^*$  in case-2



Graph for k vs Tac( $t_1, t_2$ )\* in case-2

Graph for  $k vs L_{m}^{*}$  in case-2

(3). From the above table, for increasing of  $C_2$ , the optimal value of  $t_1^*$  and  $t_2^*$  increase slowly. By this effect, the total average cost  $Tac(t_1,t_2)^*$  increase slowly and the highest inventory level  $L_m^*$  increase rapidly. Bellow the graph to illustrate these results:



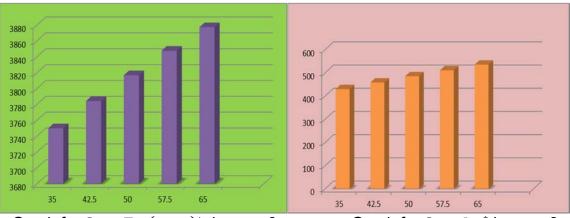
Graph for  $C_2 vs t_1^*$  in case-3

Graph for  $C_2 vs t^*_2$  in case-3

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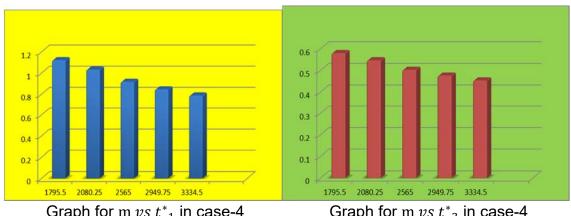
DOI: 10.14807/ijmp.v10i5.897



Graph for  $C_2$  vs  $Tac(t_1, t_2)^*$  in case-3

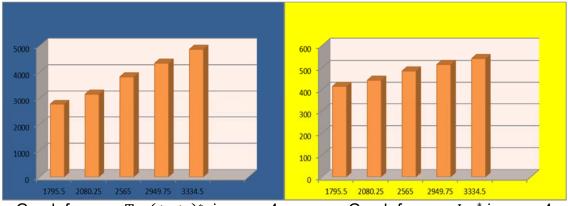
Graph for  $C_2 vs L_m^*$  in case-3

(4). From the above table, for increasing of m, the optimal value of  $t_1^*$  and  $t_2^*$  decrease slowly. By this effect, the total average cost  $Tac(t_1, t_2)^*$  and the highest inventory level  $L_{m}^{*}$  increase rapidly. Bellow the graph to illustrate these results:



Graph for m  $vs t_1^*$  in case-4

Graph for m vs  $t^*_2$  in case-4



Graph for m  $vs \operatorname{Tac}(t_1, t_2)^*$  in case-4

Graph for m vs L<sub>m</sub>\* in case-4

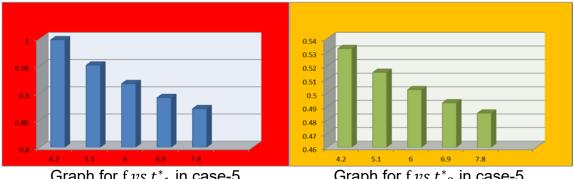
(5). From the above table, for increasing of f, the optimal value of  $t_1^*$  and  $t_2^*$ decrease slowly. By this effect, the total average cost  $Tac(t_1, t_2)^*$  and the highest inventory level  $L_m^{\ *}$  increase rapidly. Bellow the graph to illustrate these results:

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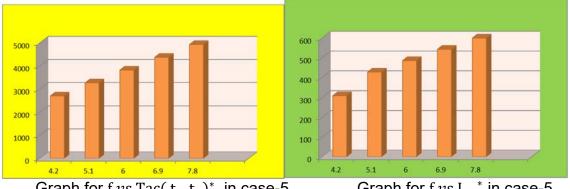
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Graph for f  $vs\ t^*_1$  in case-5

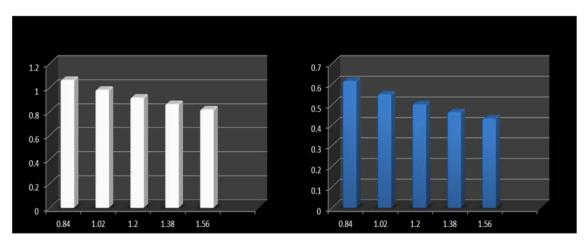
Graph for f  $vs\ t^*_2$  in case-5



Graph for f vs Tac( $t_1, t_2$ )\* in case-5

Graph for f vs  $L_m^*$  in case-5

(6) From the above table, for increasing of h, the optimal value of  $t_1^*$  and  $t_2^*$  decrease slowly. By this effect, the total average cost  $Tac(t_1,t_2)^*$  increase and the highest inventory level  ${\rm L_m}^{\ast}\,$  decrease slowly. Bellow the graph to illustrate these results:



Graph for h  $vs\ t^*_1$  in case-6

Graph for h vs  $t^*_2$  in case-6

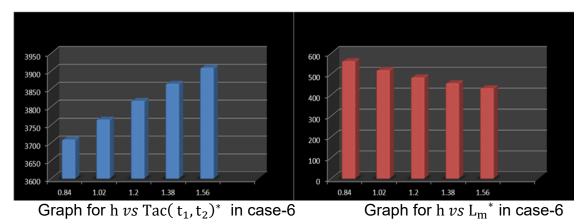


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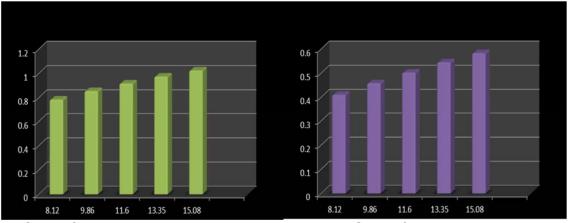
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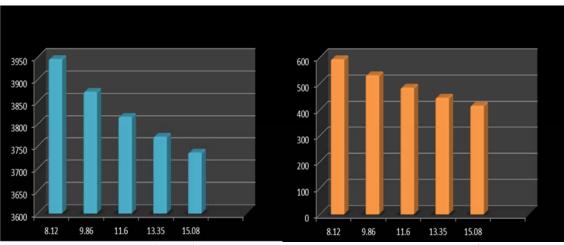


(7). From the above table, for increasing of p, the optimal value of  $t_1^*$  increase rapidly and the optimal value of  $t_2^*$  increase slowly. By this effect, the total average cost  $Tac(t_1,t_2)^*$  decrease slowly and the highest inventory level  $L_m^*$  decrease rapidly. Bellow the graph to illustrate these results:



Graph for p  $vs\ t_1^*$  in case-7

Graph for p  $vs\ t^*_2$  in case-7



Graph for p vs Tac( $t_1, t_2$ )\* in case-7

Graph for p  $vs L_{m}^{*}$  in case-7

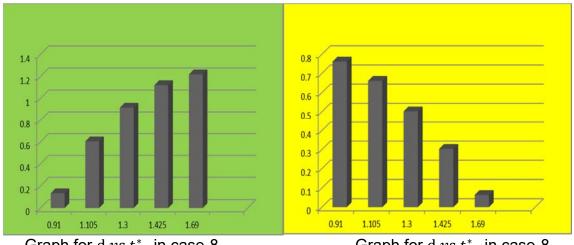
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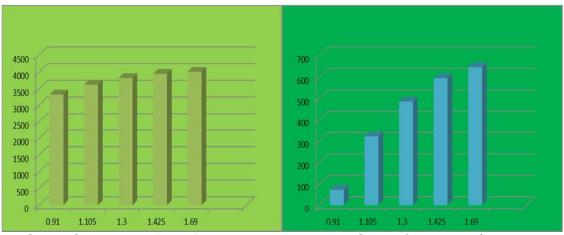
DOI: 10.14807/ijmp.v10i5.897

(8) From the above table, for increasing of d, the optimal value of  $t_1^*$  increase and the optimal value of  $t_2^*$  decrease rapidly. By this effect, the total average cost  $Tac(t_1,t_2)^*$  increase slowly and the highest inventory level  $L_m^*$  increase rapidly. Bellow the graph to illustrate these results:



Graph for d  $vs t_1^*$  in case-8

Graph for d  $vs t_2^*$  in case-8



Graph for d vs Tac( $t_1, t_2$ )\* in case-8

Graph for d vs  $L_{m}^{*}$  in case-8

(9) From the above table, for increasing of I, the optimal value of  $t_1^*$  decrease and  $t_2^*$  increase slowly. By this effect, the total average cost  $Tac(t_1,t_2)^*$  increase rapidly and the highest inventory level  $L_m^*$  decrease slowly. Bellow the graph to illustrate these results:

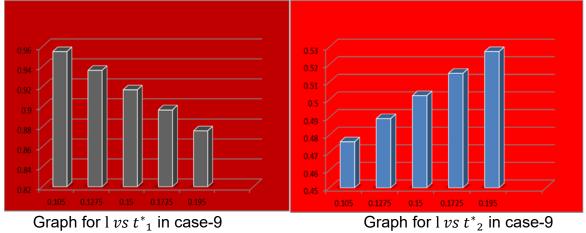


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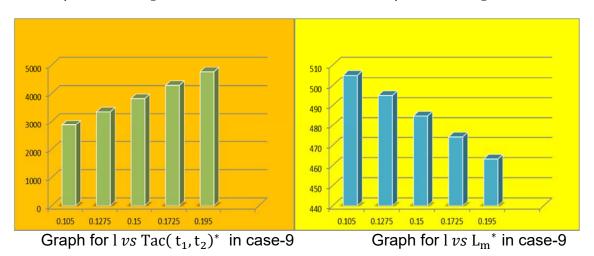
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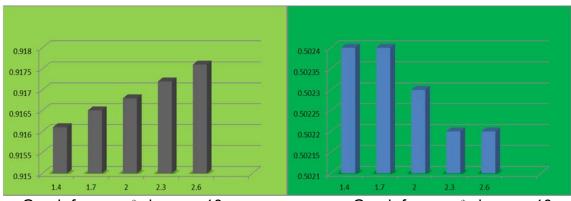
DOI: 10.14807/ijmp.v10i5.897



Graph for  $l vs t_2^*$  in case-9



(10) From the above table, for increasing of r, the optimal value of  $t_1^*$  increase and the optimal value of  $t_2^{\ast}$  decrease slightly. By this effect, the increment of the total average cost  $Tac(t_1, t_2)^*$  and the decrement of the highest inventory level  $L_m^*$  is negligible. Bellow the graph to illustrate these results:



Graph for  $r vs t_1^*$  in case-10

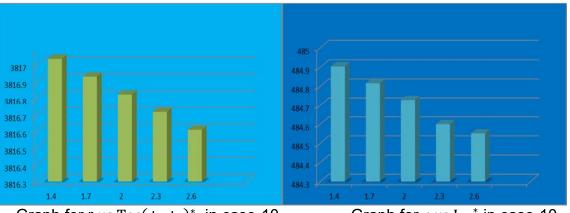
Graph for r vs  $t^*_2$  in case-10

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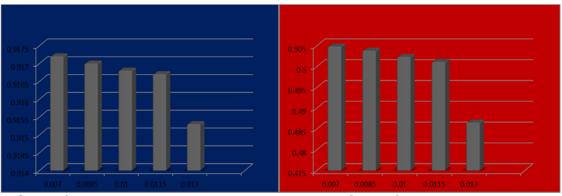
DOI: 10.14807/ijmp.v10i5.897



Graph for r vs Tac( $t_1, t_2$ )\* in case-10

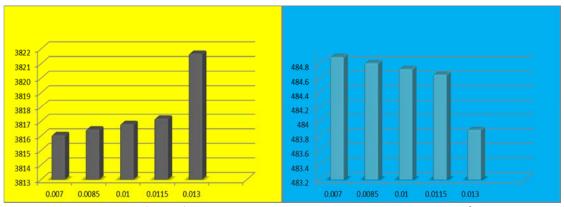
Graph for  $r vs L_m^*$  in case-10

(11) From the above table, for increasing of  $\beta$ , the decrement of the optimal value of  $t_1^*$  and  $t_2^*$  is negligible. By this effect, the increment of the total average cost  $Tac(t_1,t_2)^*$  is very slow and the decrement of the highest inventory level  $L_m^*$  is negligible. Bellow the graph to illustrate these results:



Graph for  $\beta vs t_1^*$  in case-11

Graph for  $\beta vs t_2^*$  in case-11



Graph for  $\beta$  vs Tac( $t_1, t_2$ )\* in case-11

Graph for  $\beta vs L_m^*$  in case-11

#### 9. CONCLUSIONS

In this article, we proposed a genuine E. P. Q. Inventory Model and gave solution along affectability examination approach. From the Table-9, it is indicates when deterioration, production cost, holding cost is lesser, average cost function of



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the system decreases. Whereas it also observed that lesser population lesser demand

and lesser selling price greater demand. Here, a crisp model is produced then it

changed to fuzzy model taking triangular fuzzy number and illuminated by Signed

Distance Method. Decision maker may get the ideal outcomes as per his desire

utilizing the result of this model. In future, the other sort of membership functions, for

example, Parabolic Fuzzy Number (pFN), Generalised Fuzzy Numbers, Piecewise

Linear Hyperbolic Fuzzy Number, Parabolic level Fuzzy Number (PfFN), Pentagonal

Fuzzy Number and so forth can be considered to build the membership function and

afterward that model can be effectively solved by Werner's Approach, Nearest Interval

Approximation, Geometric Programming (GP) strategy, Nearest Symmetric Triangular

Defuzzification (NSTD) technique, and so forth.

10. LIMITATIONS OF THE STUDY

This proposed model of the inventory system there are a few constraints, which

are as per the following:

1. The inventory system includes just a single thing and one stocking point.

2. The proposed model is restricted here on the grounds that shortages are not

permitted.

3. This stock model diminishes the business chance up, as it were, yet this

investigation does not ensure the end of business chance.

11. FUTURE SCOPE

In future, researchers can extend this model by taking allowable shortages, two

warehouse, stock dependent demand, permissible delay in payment, stochastic

demand and inflation. In furthere, the other sort of membership functions, for example,

Parabolic Fuzzy Number (pFN), Generalised Fuzzy Numbers, Piecewise Linear

Hyperbolic Fuzzy Number, Parabolic level Fuzzy Number (PfFN), Pentagonal Fuzzy

Number and so forth can be considered to build the membership function and

afterward that model can be effectively solved by Werner's Approach, Nearest Interval

Approximation, Geometric Programming (GP) strategy, Nearest Symmetric Triangular

Defuzzification (NSTD) technique, and so forth.

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