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Article

Sub-Transmission Network Expansion Planning Considering Regional Energy Systems: A Bi-Level Approach

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Abstract: In order to facilitate the transformation of the existing generation and transmission networks' structure into a scalable and competitive grid structure, this paper introduced regional energy systems (RGESs) that have the role of aggregating distributed energy resources (DERs) and flexible loads. The economic justification for the expansion of sub-transmission networks in the presence of regional energy systems was also investigated. To achieve this goal, multi-criteria optimization solutions were employed to find techno-economic solutions. While solving the proposed multi-criteria optimization problem, a Pareto front was determined to show the tradeoff between the criteria examined. In addition, fuzzy satisfying and the max-min method were used for finding equilibrium point. In order to demonstrate the performance and effectiveness of the proposed model, a realistic sub-transmission system in Guilan Province, Iran, was used as a test system and the results were compared to those from a traditional sub-transmission expansion planning model.

Keywords: fuzzy satisfying method; multi-criteria optimization; regional energy system; sub-transmission expansion planning

1. Introduction

In recent years, in order to increase efficiency; facilitate the use of renewable energy resources (RERs) and resolve environmental concerns; attract private sector participation; and use the potential of demand side management, the planning of moving power systems towards smart grid structures has been initiated [1]. Therefore, developing a reliable, economic, and scalable electric power system structure which also supports distributed controllability feature is a necessity. Traditionally, regional electric companies (RECs), which were responsible for the operation and expansion planning of sub-transmission systems, purchased electricity from large generation companies, and subsequently, delivered it to sub-transmission level consumers while paying all costs associated with power losses, lines, and substations expansion. This process was time consuming as it could create environmental and legal barriers. That method can be improved by utilizing regional energy systems (RGESs). RGESs, like multi-microgrids at the distribution voltage level, are aggregate systems that can increase the scalability, controllability, and competitiveness of power systems at the sub-transmission voltage level. Utilizing RGESs with the ability to supply regional loads is a suitable choice for upgrading energy efficiency, decreasing sub-transmission expansion costs, and reducing congestion on transmission lines and main sub-transmission feeders.

1.1. Literature Review

So far, an extensive amount of research has been reported on the optimal expansion planning of transmission and sub-transmission grids [2,3]. Some studies have only considered traditional expansion planning with or without considering distributed generation (DG) units [4–9], and others have focused on the expansion of aggregated systems regardless of the expansion of the generation and transmission networks [10,11]. However, an integration of different sectors, including power generation firms, service providers, transmission firms, and aggregated systems can be taken into account in restructured power systems [12–16]. The authors in [16] proposed an approach that investigates the utilization of an aggregate system in the network and addresses the effect of the system on generation/transmission expansion planning (GEP/TEP) considering uncertainties. The research has mainly considered the minimization of the total operation, investment, and load shedding costs for RGENs. The economic expansion planning of a sub-transmission grid and regional virtual power plant was investigated in [17] with the aim of minimizing the sub-transmission system's cost. In the same work, the expansion planning problem was formulated in a centralized format in which the benefits of the regional players are neglected.

However, in practice, the investors in generation companies, transmission companies, and RGENs make expansion planning decisions based on profits [18–20]. Optimal GEP and TEP problems are also addressed in [21,22], respectively, considering the role of demand response (DR) aggregators. A model for congestion and investment reduction is proposed in [23], while a security-based co-planning of transmission line expansion and energy storage facilities is introduced in [24]. Likewise, a bi-objective model for grid expansion planning with the integration of microgrid aggregators is proposed in [25].

Additionally, different solution methods like multi-criteria optimization techniques have been developed to solve the multi-criteria expansion planning problems [26,27]. With two conflicting objectives, considered in the optimization process, it is impossible to get a single solution that can optimize both objectives simultaneously. A general method to solve this issue is to employ multi-criteria decision analysis method to determine a final solution from the Pareto frontier. A multi-objective approach for placement of multiple DGs in the radial distribution system is presented in [28]. Reference [29] stated that NSGA-II and MOPSO are the modern, random optimization methods that are able to find the Pareto frontier. Multi-objective PSO (MOPSO) was used for a distributed energy system integrated with energy storage in [30].

1.2. Contribution of this Paper

Although an extensive amount of research has been reported on the optimal expansion planning of transmission and sub-transmission grids, not much work has been carried out on developing a competitive and scalable model for the economic expansion planning of sub-transmission grids, considering integrated energy systems. In this paper, while introducing regional energy entities at the sub-transmission level, the new concept of a bi-level planning process is proposed, which is very helpful for the optimal planning of energy systems with cost-profit components. Furthermore, depending on technical and environmental constraints (such as legal barriers for new sub-transmission installations and emission limitations), conditional decision-making can be applied. Fuzzy, multi-criteria particle swarm optimization with a Pareto solution is proposed to solve the problem we examine.

The major contributions of this paper include:

- Introducing RGEN as a scalable and competitive player in the sub-transmission expansion planning model. In a feed-in-tariff market space, the investors of RGEN and owners of REC are able to make optimal decisions;
- Establishing a bi-level fuzzy multi-criteria optimization method to capture the interaction between RGEN and REC for sub-transmission expansion planning;
- Determining an archive of non-dominated solutions (Pareto front) that enables conditional decision-making according to the limitations of a network, such as environmental or legal barriers in lines and substations installation.

1.3. Paper's Structure

The structure of the rest of the research is as follows. The problem statement together with the required definition is introduced in Section 2. The problem formulation is given in Section 3. The solution procedure is explained in Section 4. Numerical studies, including the case study and the discussion of the results, are detailed in Section 5. Conclusions and further developments are discussed in Section 6.

2. Problem Statement and Definition

This study's aim was optimally determining the expansion plan of both RGES's internal resources, such as DGs and flexible loads, and traditional sub-transmission systems (i.e., lines and substations' expansion planning). The owner of the traditional sub-transmission network (i.e., REC) and the owner of RGES can both be either private or governmental. Figure 1 illustrates the proposed schematic diagram of an integrated sub-transmission network with a single RGES.

An RGES aims at profit maximization with respect to the network and other relevant constraints, while an REC aims at minimizing traditional expansion and operation costs. These objectives yield a multi-criteria optimization problem, which is detailed in the next sections.

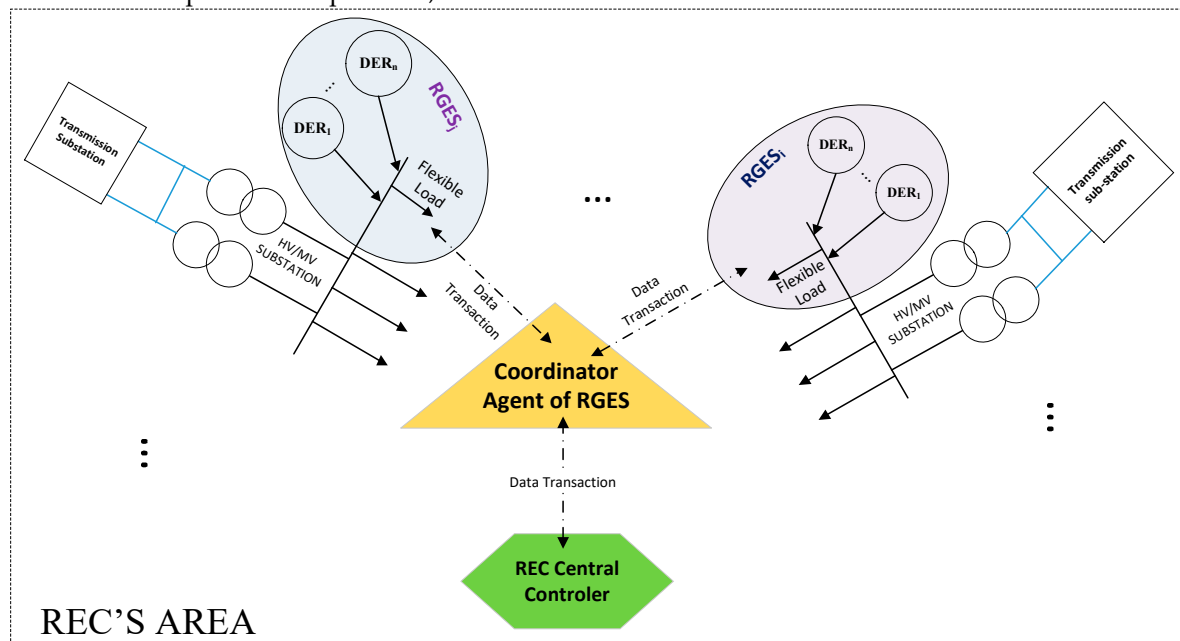


Figure 1. Schematic diagram of the integrated sub-transmission grid we propose, with a single regional energy system (RGES).

2.1. Regional Energy System (RGES)

The superiority of integrated energy systems over distributed generation sources is their greater controllability and visibility; they have a central coordinating agent and can facilitate the restructuring of the electricity industry from a centralized to a networked state. They can also, as an integrator of flexible loads, prevent the non-economic extension of the generation and sub-transmission networks over short periods of peak load. In the meantime, they can encourage small-cap private-equity partnerships to invest in the electricity industry. The RGES proposed in this study is configured as an energy network in a specific geographic region that is able to host a variety of renewable and non-renewable energy sources as well as flexible loads, representing a controllable entity in the power system. An RGES can be actively involved in the expansion planning of sub-transmission networks by investing in capacity addition and/or installation of new internal DERs. An investor in RGES can be a single entity or a number of private shareholders. An agent is referred to a coalition participant seeking to maximize the profit of the RGES.

2.2. Regional Electric Company (REC)

This paper assumes that RECs are responsible for supplying electricity for sub-transmission level consumers in a particular geographic region. They are also responsible for the expansion planning and operation of substations and lines at the sub-transmission and transmission voltage levels. Traditionally, they purchase electricity produced by large power plants and deliver it to the sub-transmission load centers. Therefore, in the traditional grid, their costs include the cost of purchasing energy from the upstream grid, the cost of energy losses, and costs incurred by substations and lines expansion planning programs. In the method we propose, in addition to purchasing power from upstream plants, REC can also purchase required energy from RGEN's resources. Here, it is also assumed that the costs of purchasing energy from upstream power plants and RGEN's resources are based on regulated tariffs. The purpose of REC is to minimize the related cost function.

3. Problem Formulation

3.1. First-Level Objective Function

At the first level, to get a maximized profit, RGEN determines the optimal sizing and sitting of the resources in the local area considering time duration, the amount of load in each sub-transmission load center, the investments and operation costs of resources, the feed-in-tariff rate, the guaranteed purchase time, and geographic variables, such as irradiation and wind characteristics and flexible load behaviors. In fact, knowing the forecasted load in each load point in the planning horizon, an RGEN is able to determine optimal site and size of its own resources in all sub-transmission substations (candidate site) to maximize its utility function according to Equation (1). Revenues include the present value of the energy sales to REC during the guaranteed purchase period, the energy sale to an REC after the guaranteed purchase period, and the salvaged revenue described in Equations (4)–(6). RGEN's costs include the present value of operation and investment costs, which are described by Equations (7) and (8).

$$OF_{RGEN} = \text{Max}\{I - C\}, \tag{1}$$

$$I = I_{TG} + I_{ATG} + I_{SAL}, \tag{2}$$

$$C = C_{OC} + C_{INV}, \tag{3}$$

$$I_{TG} = \sum_{i=1}^{N_{TS}} \sum_{k=1}^K \sum_{t=1}^T \sum_{\tau=t}^{t+TG_k} (1+ir)^{-\tau} \sum_{n=1}^{N_{LD}} P_{t\tau n}^{k_i} \times \Pi_{\tau n}^k \times T_{n\tau}, \tag{4}$$

$$I_{ATG} = \sum_{i=1}^{N_{TS}} \sum_{k=1}^K \sum_{t=1}^T \sum_{\tau=TG_{kt}+1}^{LF_k} (1+ir)^{-\tau} \sum_{n=1}^{N_{LD}} P_{t\tau n}^{k_i} \times \Pi_{\tau n}^k \times T_{n\tau} \tag{5}$$

$$I_{SAL} = \sum_{i=1}^{N_{TS}} \sum_{k=1}^K \sum_{t=1}^T (1+ir)^{-(t+LF_k)} \times SAL_{k_i} \tag{6}$$

$$C_{OC} = \sum_{i=1}^{N_{TS}} \sum_{k=1}^K \sum_{t=1}^T \sum_{\tau=1}^{LF_{kt}} (1+ir)^{-\tau} \sum_{n=1}^{N_{LD}} OC_{k_{it\tau}}, \tag{7}$$

$$C_{INV} = \sum_{t=1}^T (1+ir)^{-t} \sum_{i=1}^{N_{TS}} \sum_{k=1}^K IC_{k_{it}}. \tag{8}$$

3.1.1. Constraints of RGEN

- Operational Constraint of RGEN's Resources

The generation of each unit within the RGEN must be less than its nominal capacity.

$$0 \leq P_{kn}^{RGEN} \leq P_{kMax}^{RGEN} ; k = 1, 2, \dots, K ; n = 1, 2, \dots, N_{LD}, \tag{9}$$

where P_{kj}^{RGEN} and S_{kj}^{RGEN} are the generated power and nominal power of the kth resource of each RGEN in the nth level of the load duration curve (LDC) (MW), respectively. In this study, flexible loads have been also considered to be RGEN resources, so the same constraint as in Equation (9) was applied to show the range in which responsive loads could react.

- Limitation of RGEN Capacity

To enable the transfer of power generated by RGEN's internal resource in single-event mode for the sub-transmission transformer of each substation, the maximum power generated by RGEN that is fed to the sub-transmission network has to be limited to certain percentage according to Equation (10) [7]:

$$S_{RGENi} \leq 0.5S_i^{TS,max} + L_{min}, \tag{10}$$

where $S_i^{TS,max}$ is the maximum transformer capacity of each sub-transmission substation determined in the expansion planning phase and L_{min} is the minimum annual forecasted load in the planning horizon.

3.2. Second-Level Objective Function

At the second level, based on the results of sizing and sitting of RGEN's internal resources, REC applies load flow to get the amount of power required to be imported from the upstream network to satisfy the power balance constraint. It also determines energy loss cost and the costs related to the substation and lines' expansion planning programs; and the cost function of the REC is ultimately determined. So, the objective function of REC is to minimize the total cost of REC subject to different constraints. This cost function can be considered as the combination of cost elements according to Equation (11):

$$OF_{REC} = Min\{SLLC + UGEC + SSEC + SLEC + RGESEC\} \tag{11}$$

In Equation (11), the economic assessment is made based on five terms, considering their current net values. SLLC is the transmission and sub-transmission lines' losses obtained by Equation (12):

$$SLLC = \sum_{t=1}^T (1+ir)^{-t} \left[\sum_{i=1}^{N_{TS}} \sum_{j=1}^{N_{SS}} \sum_{n=1}^{N_{LD}} T_n \times LC \times L_{ij}^{SL} \times R_{ij}^{SL} \times I_{jn}^2 + \sum_{j=1, j \neq j'}^{N_{SS}} \sum_{j'=1, j' \neq j}^{N_{SS}} \sum_{n=1}^{N_{LD}} T_n \times LC \times L_{jj'}^{SL} \times R_{jj'}^{SL} \times I_{jn}^2 \right] \tag{12}$$

The power losses in service transformers were neglected in this study as they are relatively low compared to the line losses.

UGEC is the cost of power purchased from the utility (i.e., transmission network) that can be calculated based on Equation (13). Generally, it is the REC who pays for the energy imported from the transmission network, which changes over the time based on the load duration curve (LDC). That cost is normally higher in peak hours and lower in other time intervals. The cost of providing energy by the transmission network is given by Equation (13):

$$UGEC = \sum_{t=1}^T (1+ir)^{-t} \sum_{i=1}^{N_{TS}} \sum_{n=1}^{N_{LD}} P_{int}^G \times T_{nt} \times \pi_{int}^G \tag{13}$$

SSEC is the transmission and sub-transmission substation expansion cost obtained by Equation (14):

$$SSEC = \sum_{t=1}^T (1+ir)^{-t} \sum_{i=1}^{N_{TS}} \alpha_{it}^{TS} \times EC_{TS,i}(S_{TS,it}^{old}, S_{TS,it}^{new}) + \sum_{t=1}^T (1+ir)^{-t} \sum_{j=1}^{N_{SS}} \alpha_{jt}^{SS} \times EC_{SS,j}(S_{SS,jt}^{old}, S_{SS,jt}^{new}) \quad (14)$$

SLEC is the expansion cost for sub-transmission lines, as stated in Equation (15):

$$SLEC = \sum_{t=1}^T (1+ir)^{-t} \sum_{i=1}^{N_{TS}} \sum_{j=1}^{N_{SS}} \alpha_{ijt}^{SL} \times EC_{TSL,ijt}(S_{TSL,ijt}^{old}, S_{TSL,ijt}^{new}) + \sum_{t=1}^T (1+ir)^{-t} \sum_{j=1, j' \neq j}^{N_{SS}} \sum_{j'=1, j' \neq j}^{N_{SS}} \alpha_{jj't}^{TSL} \times EC_{SL,jj't}(S_{SL,jj't}^{old}, S_{SL,jj't}^{new}) \quad (15)$$

RGEESEC is the cost of energy provision paid by the REC to the RGES given by Equation (16):

$$RGEESEC = \sum_{j=1}^{N_{SS}} \sum_{k=1}^K \sum_{t=1}^T \sum_{\tau=1}^{TG_{kt}} (1+ir)^{-\tau} \sum_{n=1}^{N_{LD}} P_{t\tau n}^{kj} \times \Pi_{\tau n}^k \times T_{n\tau} \quad (16)$$

Once the total number of guaranteed purchase years is over, the energy produced by RGES's units (including DERs and services offered by flexible loads/DR programs) is no longer priced on feed-in-tariff basis but according to upstream network tariffs.

3.2.1. REC Constraints

- Line Loading Constraints

The loading of transmission and sub-transmission lines must be lower than their thermal capacity, as formulated in Equations (17) and (18):

$$|I_{ij}^{TSL}| \leq 0.8 |I_{ij,max}^{TSL}| ; \forall i \in \{1, 2, \dots, N_{TS}\}, \forall j \in \{1, 2, \dots, N_{SS}\} \quad (17)$$

$$|I_{jj'}^{SL}| \leq 0.8 |I_{jj',max}^{SL}| ; \forall j \in \{1, 2, \dots, N_{SS}\}, \forall j' \in \{1, 2, \dots, N_{SS}\}, j \neq j' \quad (18)$$

In this paper, it is assumed that maximum permitted current of each transmission and sub-transmission line is 80% of lines thermal capacity [7].

- Sub-Transmission Substations Constraints

The loading of sub-transmission substations must be lower than their thermal capacity, as given in Equation (19):

$$\sum_{j=1}^{N_{LP}} \gamma_{ij}^{LP} S_j^{LP} \leq (1-rf_i) \times S_i^{SS,max} ; \forall i \in \{1, 2, \dots, N_{SS}\} \quad (19)$$

According to Equation (19), the allocated load to each substation is lower than the capacity of that substation. However, considering the reserve factor results in a higher network reliability.

- Transmission Substations Constraints

The load of transmission substations must be lower than their thermal capacity, as provided in Equation (20):

$$\sum_{j=1}^{N_{SS}} \gamma_{ij}^{SS} S_i^{SS} \leq (1-rf_i) \times S_i^{TS,max} ; \forall i \in \{1, 2, \dots, N_{SS}\} \quad (20)$$

where γ_{ij}^{SS} is the binary variable set to 1 if the sub-transmission substation j is supplied from the i th transmission substation, and 0 otherwise.

- Power balance constraint

In each time interval and each LDC segment, the following demand-supply balance constraint must be met:

$$\sum_{k=1}^K P_k^{RGES} + Ptr = \sum_{j=1}^J P_{Load_j} + P_{Loss} \tag{21}$$

where P_k^{RGES} is the power generated by RGEN in each time and Ptr is transaction power with other networks.

4. Solution Procedure

4.1. Multiobjective Particle Swarm Optimization (MOPSO)

MOPSO was presented in 2004 by Coello et al. [32]. This algorithm is population-based, and uses a geographically-based approach to maintain diversity. As it introduces external archiving, crowding distance, and a mutation operator, MOPSO uses a measure of performance similar to the fitness value used by evolutionary algorithms, and the adjustments of individuals are analogous to the use of a crossover operator. The algorithm updates the velocity and the position of each particle according to global bests of particles gained from last iteration; and mutation is carried out among individuals. Regarding the performance evaluation of MOPSO, authors in [33] conducted a comparative study among several multi-criteria problem-solving algorithms. The quality of the Pareto sets (in terms of distance, distribution, and extent) was presented accordingly to analyze the performance of algorithms. It was shown that MOPSO multiplies the chances to keep individuals' changes and make it easier to maintain diversity compared to non-dominated sorting genetic algorithm II (NSGA-II). Additionally, the MOPSO method is faster at getting convergence compared to NSGA-II. Due to its design simplicity and effectiveness, MOPSO was also utilized in this study to solve the proposed bi-level optimization mode considering different technical constraints and regulatory frameworks. A typical MOPSO flowchart together with its building blocks and key functions are presented in [34,35].

4.2. Fuzzy Satisfying Method (FSM)

In this paper, a number of fuzzy sets were defined for all of the RGEN's profit functions and REC's costs we calculated according to Equations (22) and (23), respectively. It was assumed that maximum and minimum values of profit functions of RGEN (i.e., PF_i^{max} and PF_i^{min}) and cost functions (i.e., C_j^{max} and C_j^{min}) of REC could be predicted. When the individual's profit and cost range are taken into account, the membership function $\mu(PF)$ and $\mu(C)$ for each objective function can be determined by Equations (22) and (23) [36]:

$$\mu(PF_{RGES}) = \begin{cases} 0 & PF_{RGES} \leq PF_{RGES}^{min} \\ \frac{PF_{RGES} - PF_{RGES}^{min}}{PF_{RGES}^{max} - PF_{RGES}^{min}} & PF_{RGES}^{min} \leq PF_{RGES} \leq PF_{RGES}^{max} \\ 1 & PF_{RGES} \geq PF_{RGES}^{max} \end{cases} \tag{22}$$

$$\mu(PF_{REC}) = 1 - \mu(C_{REC}) \tag{23}$$

The minimum value for all membership functions of a specific set represents the optimal value of that set. A set with larger minimum value of membership functions is more favorable, since it satisfies more objective functions in terms of individual optimum values. In case of multiple objective functions, the optimal solution (i.e., the equilibrium) can be realized by Equation (24):

$$Max \psi = Max \{ \min (\mu(PF)_m) \} \quad m = 1, \dots, M, \tag{24}$$

where m is the MOPSO archive member's counter and M is the number of MOPSO archive members. According to Equation (24), an optimal plan for RGEN and REC would be a combination in which ψ has the highest value.

4.3. Solution Procedure Description

In the proposed bi-level and bi-objective sub-transmission expansion planning, considering an aggregated energy system, initially, RGEN obtains basic information, including estimations of different load levels in the planning horizon; the locations of load centers, current transmission, and sub-transmission lines; and substation information from the system operator. In this work, it was assumed that load centers are concentrated in the outgoing feeders of the sub-transmission substations. Additionally, sub-transmission and RGEN expansion planning were considered based on the anticipated peak load in the planning horizon. And, due to the short duration of peak load duration, for achieving economic planning, a percentage of the planning program is executed on the basis of flexible loads by RGEN. This paper assumes that 10% of the predicted peak load can be managed by flexible loads. In the first level of the proposed planning model, RGEN randomly distributes its internal resource capacity among the load centers. Due to operational constraints and considering the single contingency mode for the transformer capacity of sub-transmission substation, according to Equation (10), the maximum internal resource capacity of RGEN in each sub-transmission substation is considered to be half of the corresponding transformer capacity plus the minimum annual load of that substation. At the second level, according to the network constraint (Equations (17)–(21)) and the random sizing and siting of RGEN's internal resources, the REC applies a load flow program to quantify the amount of energy losses, the energy that must be purchased from the upstream network to maintain the power balance equation (Equation (21)), and the lines required and substation expansion planning. Afterwards, at the end of each iteration, OF_{RGEN} and OF_{REC} are calculated according to Equations (1) and (11) and are stored in the MOPSO archive. OF_{RGEN} and OF_{REC} are the RGEN's profit function and REC's cost function, respectively. This bi-level process is repeated until the termination criteria are met and non-dominated responses are stored in the archive. Finally, by using the fuzzy satisfying method (FSM), the equilibrium point of RGEN and sub-transmission expansion planning are determined.

Obviously, the higher the number of repetitions, the greater the likelihood of an optimal global response. Figure 2 shows the flowchart of the method.

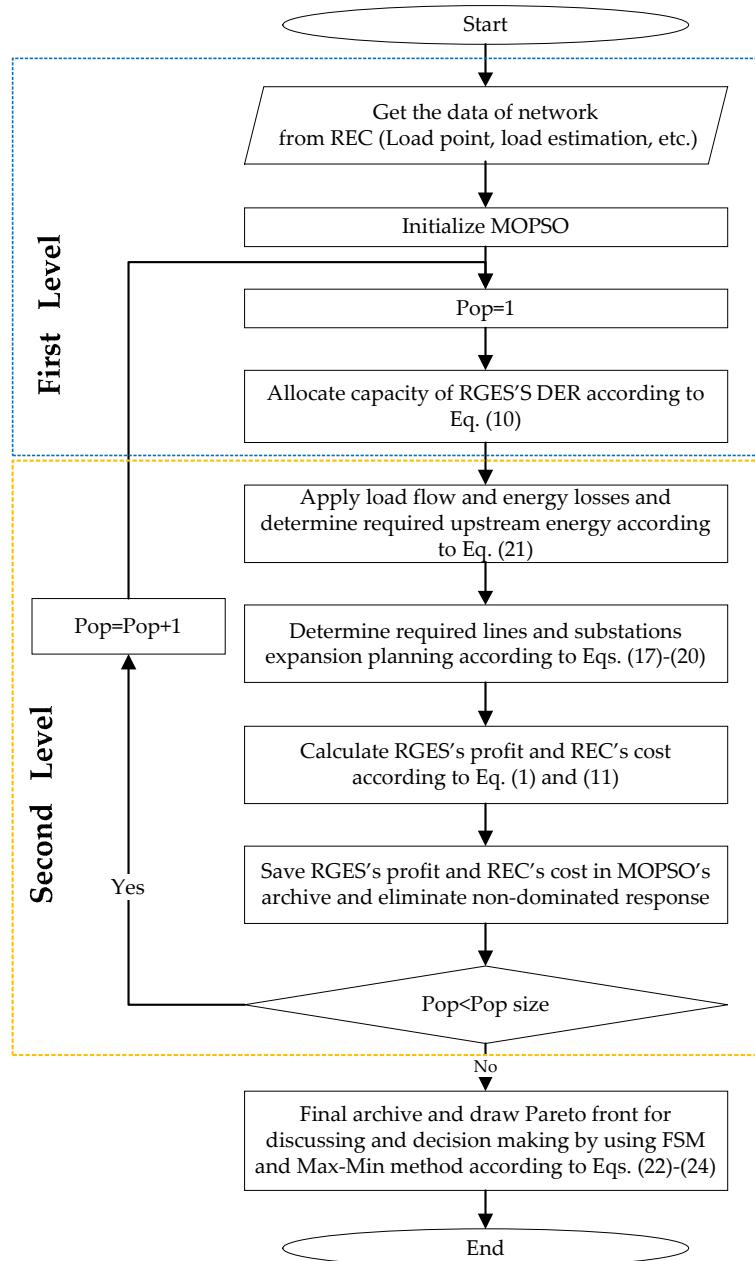


Figure 2. Flowchart of the proposed method.

5. Simulations and Test Results

5.1. Input Data

To investigate the effectiveness of the proposed method, the representative sub-transmission system of Guilan Regional Electrical Company located in north of Iran was used as a test case. This electrical network includes twenty-three 63/20 kV sub-transmission substations. In this research, it was assumed that all load points were located in the existing sub-transmission substations. The 63/20 kV substations are fed by five 230/63 kV transmission substations. The single line diagram of the case study is depicted in Figure 3 and its details are given in Appendices A and B.

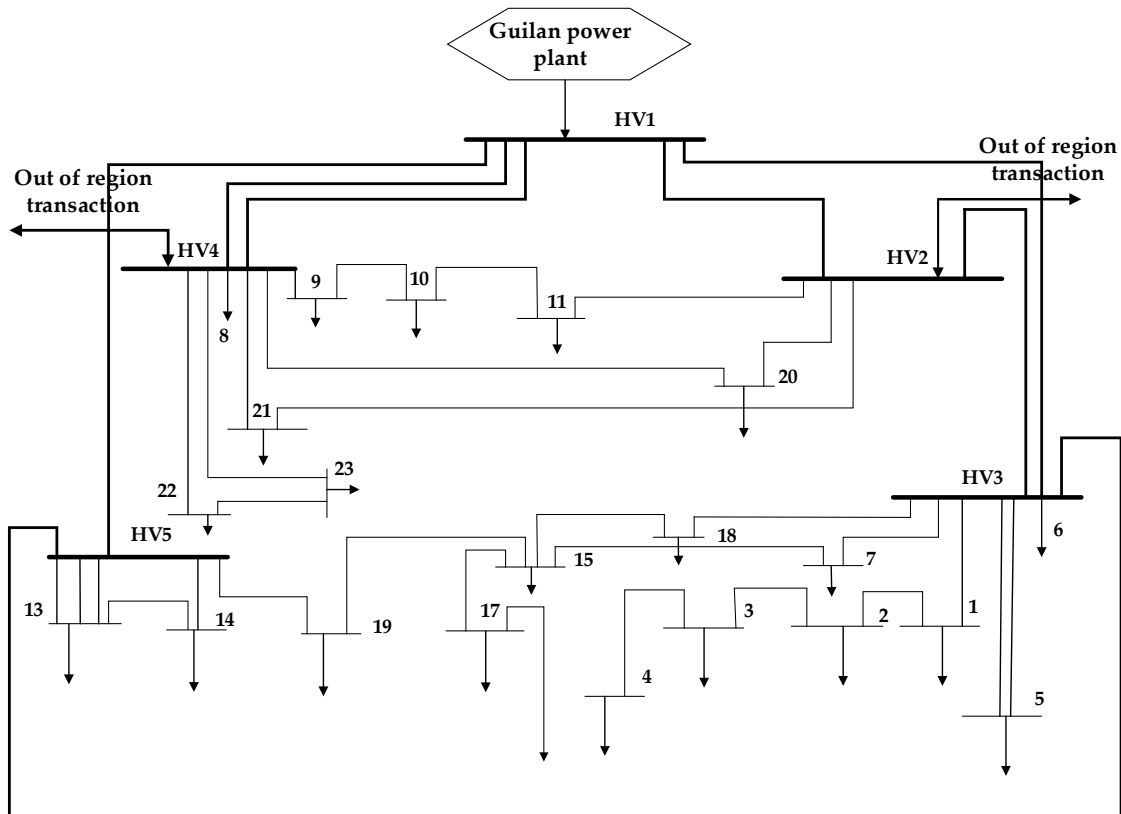


Figure 3. Single line of the case study.

The annual load growth in all levels of LDC was assumed to be 7%. Each sub-transmission line has a capacity of 50 MW. The reserve factors for the lines and substation were supposed 20% and 30%, respectively [36], and the maximum constructible circuits of the lines at the corridors are 4. The number of study years in the expansion planning problem was chosen to be 5. Other requisite information is provided in Table 1.

Table 1. Data requirements for the simulation [31].

Parameter	Value	Parameter	Value
Interest rate (%)	5	Duration of night low -load(h)	1500
Number of planning years	5	Duration of day peak -load(h)	600
Annual growth rate of the guaranteed purchase (%)	7	Duration of day mid -load(h)	2260
Maximum allowed voltage drop	5	Duration of day low - load(h)	1000
Maximum RGEs's resources penetration (%)	50	Transmission electricity price in the peak -load level (\$/MWh)	50
Installation cost of DG units (\$/MW)	200,000	Transmission electricity price in the mid-load level (\$/MWh)	30
Operating cost of DG units (\$/MWh)	25	Transmission electricity price in the low-load level (\$/MWh)	20
RGEC electricity price in the peak-load level (\$/MWh)	60	Cost of DR in the peak-load level(\$/MWh)	80
RGEC electricity price in the mid-load level (\$/MWh)	35	Cost of DR in the mid-load level(\$/MWh)	40
RGEC electricity price in the low-load level (\$/MWh)	25	Cost of DR in the low-load level(\$/MWh)	30
Duration of night - peak load(h)	400	Penalty cost of load loss in sub-transmission (\$/MWh)	15.22
Duration of night - mid load(h)	3000		

To study the effects of RGEN on sub-transmission expansion planning, two different cases were considered as follows:

- Base case (traditional sub-transmission expansion planning method): There are no RGEN units installed in the local area and the load of the sub-transmission system is totally supplied by the transmission network. This case represents the traditional sub-transmission network model where there is no contribution from local energy sources. Additionally, the optimal expansion planning model for such a network should primarily consider OF_{REC} as an objective.
- Case 2 (the proposed method): In this case, for the base case network, instead of the traditional method, the bi-level approach proposed in this paper is utilized and the results are compared with the results of traditional method for validating the new approach.

In Tables 2 and 3, data requirements for the technical and economic evaluations of the sub-transmission expansion planning model and MOPSO parameters are provided, respectively. Real information of the test system we examined was used for both case studies.

Table 2. Technical and economic data used to create the sub-transmission expansion planning model [31].

Parameter	Value
Secondary voltage of sub-transmission substation (KV)	20
Cost of transformer capacity increment(\$/MVA)	12,500
Cost of each MV bay installation(with maximum capacity of 7 MW)(\$)	2850
Cost of each HV (63 kV) bay installation(with maximum capacity of 50 MVA) (\$)	285,000
Cost of 63 kV overhead line extension with 50 MVA capacity(\$/km)	80,000
Cost of 230 KV overhead line extension with 250 MVA capacity (\$/km)	200,000

Table 3. MOPSO Parameters.

Parameter	Value
Number of iterations	100
Number of population	200
Repository size	10
Inertia coefficient	0.5
Mutation rate	0.5
C1	1.5
C2	2

5.2. Discussion

Results of the optimal expansion planning in each case study are included in Table 4 in terms of different objectives and cost/benefit components. Obviously, incorporation of RGEN resources into the expansion planning model could not only decrease overall system losses, but also mitigate the costs of lines and substations expansion, and the energy purchased from the transmission network.

Table 4. Summary of the simulation results.

[Prices are in dollars]	OF_{REC} (*10 ⁶)	OF_{RGEN} (*10 ⁶)	Line cost (SLEC) (*10 ⁶)	Substation cost (SSEC) (*10 ⁶)	Loss cost (SLLC) (*10 ⁶)	(UGEC) (*10 ⁶)
Base case (Traditional)	1375	0	72	95	43	1150
Pareto (1)	1072	296	12	18.79	11.64	678.5
Pareto (2)	1350	784	4.98	9.74	10.33	343.3
Pareto (3)	1197	524	8.76	10.43	10.85	534
Pareto (4)	1170	481	5.63	10.49	11.18	558
Pareto (5)	1140	425	52.16	11.53	11.13	602

Pareto (6)	1327	743	4.78	9.55	10.31	399
Pareto (7)	1092	330	13	19.58	11.28	655.7
Pareto (8)	1309	714	4.98	9.18	10.6	420
Pareto (9)	1213	544	8.55	10.86	10.8	418
Pareto (10)	1156	442	8.56	18.60	10.91	569

It can be observed from simulation results that the main cost component in a traditional expansion plan (base case) relates to the UGEC (Figure 4). The results of the second case study are tabulated in the other rows of Table 4. By solving the proposed two-objective optimization problem using an MOPSO algorithm, a set of non-dominated solutions were found.

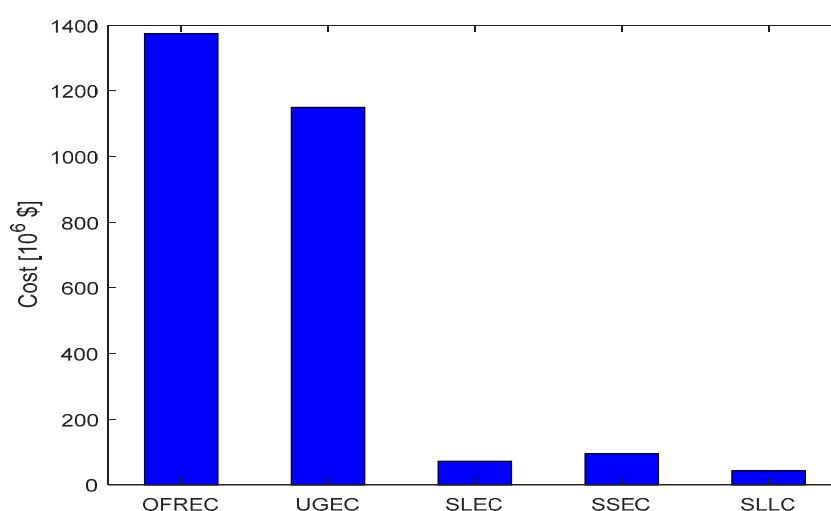


Figure 4. Traditional planning cost components.

The Pareto front of optimal solutions for the problem, which are stored in a finite-sized repository, is shown in Figure 5. As observed, the proposed multi-criteria optimization model yields a valid and well-distributed set of Pareto-optimal solutions, providing the system planers (e.g. REC and RGEs owners) various options to select an appropriate expansion plan according to economic and/or technical considerations. As an illustrative example, in Guilan Regional Electric Company's network, which is our real test case in this study, the total cost of a given expansion plans can be very different according to several factors, such as large-scale land acquisitions and leases, weather conditions, and legal considerations. These factors can push an expansion plan to a highly expensive and time-consuming point or even to the verge of infeasibility. Getting back to the results shown in Table 4, it is understood that, although the first point in the Pareto set, named Pareto (1) herein, involves the smallest cost for REC, it denotes the most extensive lines expansion plan, which enforces the least profit for the RGEs, accordingly. On the other hand, Pareto (2) shows a situation where the expansion plan results in a maximum OFRGEs for the RGEs and low SLEC and SSEC. In Pareto (2), SLLC is also a minimum that is good for the REC. Pareto (7) presents the maximum losses, lines and substations expansion costs, and least profit for the RGEs, which is not favorable for the RGEs and Guilan Regional Electric Company. In the next sub-section, fuzzy satisfying and the max-min method are used to determine the economic equilibrium point according to the Equations (22)–(24).

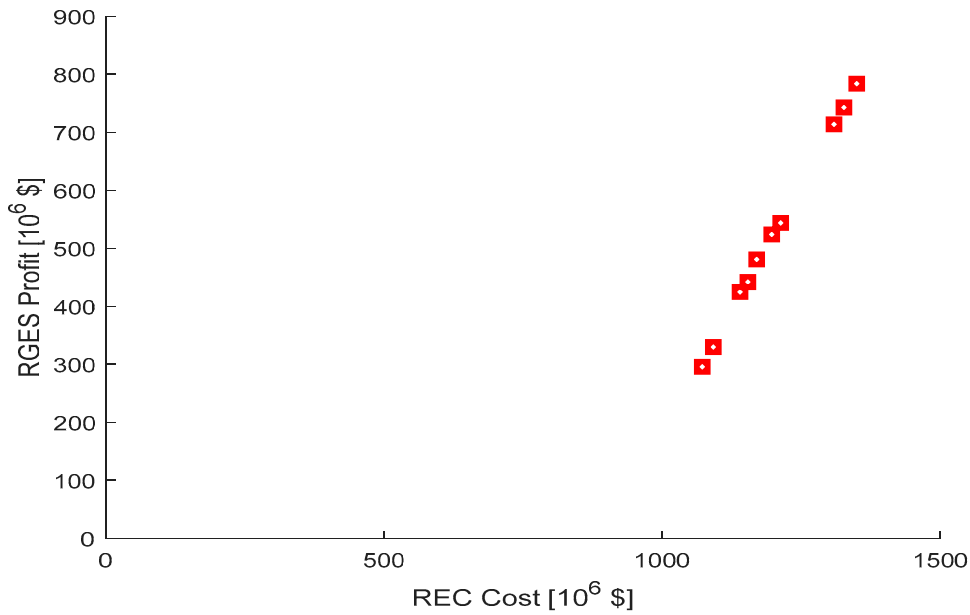


Figure 5. Pareto front diagram.

5.3. Applying the Fuzzy Satisfying Method for Evaluating MOPSO’s Archive

The simulation results of the traditional and proposed methods for sub-transmission expansion planning were analyzed in the previous subsection. In this subsection, apart from the constituent elements of the OF_{RGES} and OF_{REC} , the equilibrium point of investment in view point of RGES and REC’s investor were obtained using the FSM method described in Section 3.2. Using Equations (22) and (23), the fuzzy values of RGES profits and REC costs are provided in Tables 5 and 6.

Table 5. Membership value of Pareto (1) to Pareto (5).

	Pareto (1)	Pareto (2)	Pareto (3)	Pareto (4)	Pareto (5)
$(\mu(PF), \mu(C))$	(0.8, 0.37)	(0.1, 0.98)	(0.47, 0.65)	(0.54, 0.6)	0.63, 0.53)

Table 6. Membership value of Pareto (6) to Pareto (10).

	Pareto (6)	Pareto (7)	Pareto (8)	Pareto (9)	Pareto (10)
$(\mu(PF), \mu(C))$	(0.13, 0.93)	(0.75, 0.41)	(0.18, 0.89)	(0.43, 0.68)	(0.58, 0.55)

Using Equation (24), Pareto (10) is the equilibrium point for RGES and REC. However, as explained in Section 4.2, depending on the degree of importance of the OF_{RGES} and OF_{REC} components and other specific conditions of RGES and REC, another Pareto point could also be considered for expansion planning.

Figure 6 shows a comparison between the expansion costs of substations and lines, and the loss cost in the traditional expansion planning model and the proposed method (conducted for Pareto (10)). It was observed that a joint expansion planning model could decrease the costs of lines and substations’ expansions and losses by 88%, 80%, and 74%, respectively, in comparison with the traditional method.

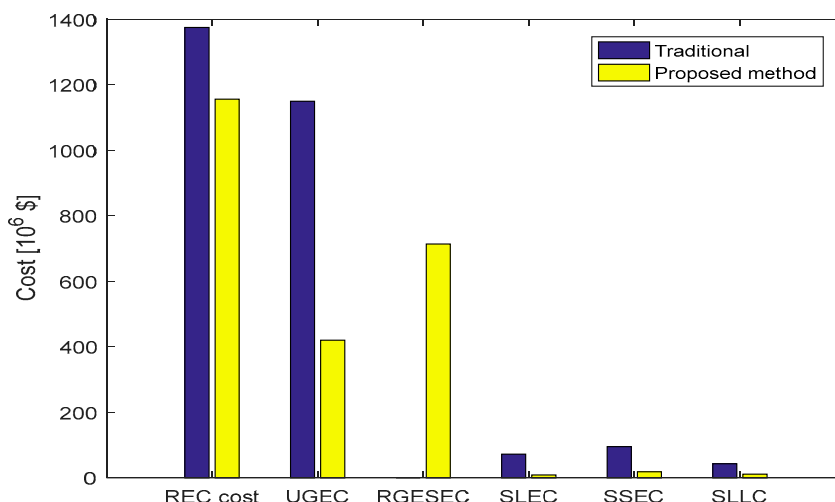


Figure 6. A comparison of the elements of the traditional and proposed methods.

6. Conclusions

The aim of this paper was to propose an efficient, bi-level expansion-planning method considering the regional energy system (RGES) at sub-transmission level. The RGES could not only participate in the sub-transmission grid expansion planning, but also contribute to energy provision services in the long term.

The proposed bi-level planning process with all system constraints was presented as an optimization model with two objectives, including different cost-profit components. Through a real test system and using computer simulations in two different approaches (traditional and proposed methods), the effectiveness of the approach we proposed was demonstrated. Results showed that expansion planning of sub-transmission grid considering RGES could significantly reduce power loss cost, costs of lines’ and substation expansions, and the total cost of a given REC while accruing profits for RGES. Additionally, given the relative importance of the RGES’s cost function elements, it is possible to decide the conditional decision making from non-dominated responses.

The extension of this work will mainly consider the effect of uncertainties, such as the impact of the uncertainty of renewable energy units of RGESs on making expansion plans. Contingency analysis in the presence of RGES will also be an aspect of future work.

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Nomenclature

Sets			
T	Number of years in the planning horizon.	L_{ij}	The total length of sub-transmission line along the ij path (km)
N_{TS}	Number of transmission substations.	I_{ij}	Current flowing through the lines in ij path (A)
N_{SS}	Number of sub-transmission substations.	$T_{(t)}$	Time duration of each load level
N_{LD}	Number of load levels.	TG	The number of years electricity is purchased at a regulated tariff by the regional electric Company

K	Number of sources in a RGEs.	Π^G	Electricity price for energy purchasing from upstream utility (Transmission grid)
Indices		Π^k	Electricity price for energy purchasing from regional energy system's resources
t	Time index, $t = \{1, \dots, T\}$	$EC_{TS} (S_{TS}^{old}, S_{TS}^{new})$	The cost of upgrading the capacity of transmission substation j from S_{TS}^{old} to S_{TS}^{new}
i	Transmission subscript index, $i = \{1, \dots, N_{TS}\}$	$EC_{SS} (S_{SS}^{old}, S_{SS}^{new})$	The cost of upgrading the capacity of sub-transmission substation i from S_{SS}^{old} to S_{SS}^{new}
j, j'	Sub-transmission subscript indices, $j, j' = \{1, \dots, N_{SS}\}$	$EC_{SL} (S_{SL}^{old}, S_{SL}^{new})$	The cost of upgrading the capacity of sub-transmission line i from S_{SL}^{old} to S_{SL}^{new}
n	Time duration index, $n = \{1, 2, \dots, N_{LD}\}$	$EC_{TSL} (S_{TSL}^{old}, S_{TSL}^{new})$	The cost of upgrading the capacity of transmission line j from S_{TSL}^{old} to S_{TSL}^{new}
k	Energy source index in each regional energy system, $k = \{1, \dots, K\}$	Π^G	Electricity price for energy purchasing from upstream utility (Transmission grid)
τ	Guaranteed year subscript index, $\tau = \{1, \dots, T_G\}$	Π^k	Electricity price for energy purchasing from RGEs's resources
Pop	Population subscript index, $Pop = \{1, \dots, Popsiz\}$	rf	The reserve factor of substation which is a number between 0 up to 1
Parameters		LF_k	The life time of the k^{th} resource in a RGEs
ir	Interest rate	IC_k	Installation cost of the k^{th} source in a RGEs
OF_{RGEs}	RGEs's profit function	OC_k	Operation cost of the k^{th} source in a RGEs
I	RGEs's income	SAL_k	Salvage value of the k^{th} resource in a RGEs
C	RGEs's cost	P_{tr}	Total power transaction between considered region and other regions
IT_G	RGEs's revenue in the guaranteed purchase period	P_{RGEs}	Generated power by RGEs' s resources
I_{ATG}	RGEs's revenue after the guaranteed purchase period	S_j^{LP}	The power demand of the j^{th} load point
I_{SAL}	Salvage revenue	S_{TS}^{max}	Maximum transformer capacity of transmission substation
Coc	Operational cost	R_{ij}	The resistance of sub-transmission line along the ij path (Ohm/km)
C_{INV}	Investment cost	S^{SS}	Transformer capacity of sub-transmission substation
OF_{REC}	REC's cost function	SL	Sub-transmission Line
C_{SLLC}	Cost of transmission/sub-transmissions lines losses	Variables	
C_{UGEC}	Cost of the purchased power from the utility (i.e., transmission network),	P^G	Imported power from transmission grid into sub-transmission grid
C_{SSEC}	Cost of transmission/sub-transmission substations' expansion,	P^k	Purchased power from the k^{th} sources of RGEs
C_{SLEC}	Expansion cost of sub-transmission lines	P_{LOSS}	Purchased power from the k^{th} sources of RGEs
C_{RGESES}	Cost of energy provision paid by the REC to the RGEs	$\alpha^{SL}, \alpha^{TSL}, \alpha^{TS}, \alpha^{SS}, \gamma^{LP}, \gamma^{SS}$	Binary variables
LC	Loss cost factor (\$/MWh)		

Appendix A

Table A-1. Specification of substations and loads.

Substation (bus #)	Voltage level (kV)	Existing capacity (MVA)	Extendable capacity (MVA)	Peak-load in base year (MW)	Mid-load in base year (MW)	Low-load in base year (MW)
1	63/20	2*30	3*30	40	19	10
2	63/20	2*30+15	3*30	50	38	17
3	63/20	2*40	3*40	42	28	15
4	63/20	2*40	3*40	18	11	7
5	63/20	2*40	3*40	18	12	7
6	63/20	1*30	2*30	24	27	6
7	63/20	2*15	2*30	24	17	6
8	63/20	1*15	2*15	13	8	3
9	63/20	2*15	2*30	19	11	4.5
10	63/20	2*15	2*30	30	22	18
11	63/20	2*30	3*30	36	23	11
12	63/20	2*40	3*40	34	18	9.5
13	63/20	2*40	3*40	66	45	17
14	63/20	2*30	3*30	48	24	8
15	63/20	2*30+1*20	3*40	61	40	17
16	63/20	2*30	3*30	56	35	17
17	63/20	2*40	3*40	66.5	51	19
18	63/20	2*40	3*40	62	48	18
19	63/20	2*30	3*30	58	36	13
20	63/20	2*40	3*40	30	18	8
21	63/20	2*30	3*30	60	34	17
22	63/20	2*40	3*40	45	21	10

Appendix B

Table B-1. Specification of corridors.

Corridor	Length(km)	Capacity (MVA)	Extendable Capacity (MVA)	Corridor	Length(km)	Capacity (MVA)	Extendable Capacity (MVA)
HV3-1	19.55	1*50	2*50	HV5-13	2	3*50	4*50
1-2	9.83	1*50	2*50	13-14	10.2	1*50	2*50
2-3	4.2	1*50	2*50	HV4-22	9.1	1*50	2*50
3-4	7.2	1*50	2*50	HV4-23	11	1*50	2*50
HV3-5	13.36	2*50	3*50	22-23	9	1*50	2*50
HV3-18	10.5	1*50	2*50	HV4-21	11	1*50	2*50
HV3-7	5.79	1*50	2*50	HV4-9	2	1*50	2*50
7-15	5.5	1*50	2*50	HV4-20	6.3	1*50	2*50
18-15	3.9	1*50	2*50	9-10	4.5	1*50	2*50
15-17	4.8	1*50	2*50	10-11	5	1*50	2*50
15-19	9	1*50	2*50	HV2-11	1	1*50	2*50
HV5-19	8	1*50	2*50	HV2-21	11	1*50	2*50
HV5-14	7.8	1*50	2*50	HV2-20	12.5	1*50	2*50

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