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# Indoor Top- $k$ Keyword-aware Routing Query 

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#### Abstract

People have many activities indoors and there is an increasing demand of keyword-aware route planning for indoor venues. In this paper, we study the indoor top- $k$ keyword-aware routing query (IKRQ). Given two indoor points $s$ and $t$, an IKRQ returns $k s$-to- $t$ routes that do not exceed a given distance constraint but have optimal ranking scores integrating keyword relevance and spatial distance. It is challenging to efficiently compute the ranking scores and find the best yet diverse routes in a large indoor space with complex topology. We propose prime routes to diversify top- $k$ routes, devise mapping structures to organize indoor keywords and compute route keyword relevances, and derive pruning rules to reduce search space in routing. With these techniques, we design two search algorithms with different routing expansions. Experiments on synthetic and real data demonstrate the efficiency of our proposals.


## I. Introduction

Route planning is among the popular location-based services. Recently, it is increasingly in demand in various indoor venues such as shopping malls, railway stations and airports. As such venues accommodate significant parts of people's daily life, appropriate route planning can facilitate a huge number of people, especially when they have to go through a large and/or unfamiliar indoor environment.

Take Copenhagen Airport as an example. Suppose Jesper has just passed the security check for his flight to France. En route to his boarding gate, he wants to buy some Danish cookies, draw some euros in cash, and eat a bowl of noodle. He wants to reach the gate within 1.5 hours. His needs can be represented as an indoor routing query from a start point (security check) to a terminal point (his boarding gate). A desirable route should have a shop that sells cookies, an ATM or a bank that offers euros, and a restaurant offers noodles. The route should not be too long, i.e., the route distance should be less than a distance constraint. ${ }^{1}$

Indoor route planning is also applicable in other practical scenarios. For example, by specifying a request with keywords of "coffee" and "print", a person in an office can have a service robot to fetch a cup of coffee and a printout document in one single route. Moreover, in automatic warehouses of Amazon, JD.com and Alibaba, robots can make use of indoor routing with keywords to accomplish operational tasks, e.g., fetching or delivering particular products at particular locations.

In this paper, we formulate and study indoor top- $k$ keywordaware routing query (IKRQ). An IKRQ requires a start point

[^0]$s$, a terminal point $t$, a distance constraint $\Delta$, and a query keyword list $Q W$. It returns the $k$ best routes from $s$ to $t$ that are not longer than $\Delta$ and have highest ranking scores. A route score integrates the route's keyword relevance w.r.t. $Q W$ and its route distance, i.e., length from $s$ to $t$.

We differentiate two kinds of indoor keywords. An identity word (i-word) is the semantic name for an indoor partition ${ }^{2}$; a thematic word (t-word) further describes an i-word's partition. In the airport example above, the specific shop names, restaurant names, and ATM are i-words. T-words can be different things for different i -words. A shop's t -words can be the names of its goods. A restaurant's t-words can be the dishes on its menu. An ATM's t-words can be Danish krone, euro and Swedish krone that indicate available currencies in cash. This keyword differentiation makes more sense indoors than outdoors. When inside an indoor venue, people tend to visit a point-of-interest (POI) with a particular name, e.g., Apple or Samsung. In contrast, outdoor routing cannot benefit from venue names as they carry little semantics; neither can it work with keywords for indoor partitions as the partitions in the same venue are regarded as co-located in outdoor space.

An IKRQ is non-trivial due to several factors. First, it needs to define keyword relevance for routes w.r.t. query keywords, for which we need to consider both i-words and t-words in the indoor context. Second, it needs to integrate keyword relevance and spatial distance for ranking routes. A meaningful ranking score may be expensive to compute for routes with multiple hops. Third, it needs to search for routes in an indoor venue with a large number of partitions that form complex topology, which may result in a large search space for routing.

To resolve IKRQs, we develop a set of techniques. First, the concept of prime routes diversifies top- $k$ routes in the query result, and enables a particular pruning rule to reduce search space. Second, bi-directional mapping structures organize twolevel indoor keywords, which facilitates computing keyword relevances and ranking scores for routes that involve indoor partitions. Third, other pruning rules are derived based on the distance constraint and the bound of top- $k$ result. Fourth, two search algorithms are designed for routing, employing a topology-oriented expansion (ToE) and a keyword-oriented expansion (KoE), respectively. All proposed techniques are experimentally evaluated on synthetic and real data. The ex-

[^1]perimental results demonstrate the efficiency of our proposals and disclose the respective suitable settings for ToE and KoE .

We make the following contributions in this paper:

- We formulate indoor top- $k$ keyword-aware routing query (IKRQ). We also propose prime routes that diversify top$k$ results and reduce search space. (Section II)
- We propose a scheme to organize the indoor keywords, a method to compute keyword relevance for routes, and a ranking score for routes. (Section III)
- We derive a set of pruning rules for IKRQ search, and design a unified search framework with two algorithms that expand differently in routing. (Section IV)
- We conduct extensive experiments on synthetic and real data sets to evaluate our proposals. (Section V)
In addition, we review the related work in Section VI and conclude the paper in Section VII.


## II. Problem Formulation

## A. Preliminaries

Table I lists the frequently used notations.
TABLE I: Notations

| Symbol | Meaning |
| :--- | :--- |
| $v, d, p$ | partition, door, and point in an indoor space |
| $w_{i}, w_{t}$ | an identity word, a thematic word |
| $P W\left(v_{i}\right)$ | partition words of partition $v_{i}$ |
| $Q W$ | query keyword list |
| $K P\left(R_{i}\right)$ | sequence of key partitions on route $R_{i}$ |
| $R W\left(R_{i}\right)$ | route words of route $R_{i}$ |
| $\kappa\left(w_{Q}\right)$ | candidate i-word set of query keyword $w_{Q}$ |
| $\rho_{Q W}\left(R_{i}\right)$ | keyword relevance of route $R_{i}$ w.r.t. $Q W$ |
| $\psi\left(R_{i}\right)$ | ranking score of route $R_{i}$ |

A previous work [13] defines mappings that capture indoor topology. In particular, $D 2 P_{\sqsupset}\left(d_{i}\right)$ gives the set of partitions that one can enter through door $d_{i}$ and $D 2 P_{\sqsubset}\left(d_{j}\right)$ gives those that one can leave through door $d_{j}$. As a basic step, indoor routing needs to move from one door to another through their common partition. To this end, we have intra-partition door-to-door distance for two doors $d_{i}$ and $d_{j}$ as

$$
\delta_{d 2 d}\left(d_{i}, d_{j}\right)= \begin{cases}\left|d_{i}, d_{j}\right|_{E}, & \text { if } D 2 P_{\sqsupset}\left(d_{i}\right) \cap D 2 P_{\sqsubset}\left(d_{j}\right) \neq \varnothing ; \\ \infty, & \text { otherwise } .\end{cases}
$$

Here, $D 2 P_{\sqsupset}\left(d_{i}\right) \cap D 2 P_{\sqsubset}\left(d_{j}\right) \neq \varnothing$ means $d_{i}$ and $d_{j}$ are in the same partition that one can enter via $d_{i}$ and leave via $d_{j}$. In this case, we measure the Euclidean distance between $d_{i}$ and $d_{j}$. The case of $d_{i}=d_{j}$ is special. This happens when one needs to enter a partition due to its keyword relevance but then leave it from the same door for further routing. In this case, we set $\delta_{d 2 d}\left(d_{i}, d_{j}\right)$ to be the double of the longest non-loop distance one can reach inside the partition from the pertinent door. Note that $\delta_{d 2 d}$ simplifies the $f_{d 2 d}$ function [13] such that no partition is explicitly specified.

Moreover, the previous work [13] uses $v\left(p_{i}\right)$ to denote point $p_{i}$ 's host partition, $\mathrm{P} 2 D_{\sqsupset}\left(v_{k}\right)$ the set of enterable doors through which one can enter partition $v_{k}$, and $P 2 D_{\sqsubset}\left(v_{k}\right)$ the set of leaveable doors through which one can leave partition $v_{k}$. Still within a partition, we define point-to-door distance and door-to-point distance, respectively, as follows. Given a
door $d_{k}$, two points $p_{i}$ and $p_{j}$, we have

$$
\begin{aligned}
& \delta_{p t 2 d}\left(p_{i}, d_{k}\right)= \begin{cases}\left|p_{i}, d_{k}\right|_{E}, & \text { if } d_{k} \in P 2 D_{\sqsubset}\left(v\left(p_{i}\right)\right) ; \\
\infty, & \text { otherwise } .\end{cases} \\
& \delta_{d 2 p t}\left(d_{k}, p_{i}\right)= \begin{cases}\left|d_{k}, p_{j}\right|_{E}, & \text { if } d_{k} \in P 2 D_{\sqsupset}\left(v\left(p_{j}\right)\right) ; \\
\infty, & \text { otherwise }\end{cases}
\end{aligned}
$$

The two distances also facilitate indoor routing: $\delta_{p t 2 d}\left(p_{i}, d_{k}\right)$ is the intra-partition distance from point $p_{i}$ to door $d_{k}$ when one leaves the partition; $\delta_{d 2 p t}\left(d_{k}, p_{j}\right)$ is the intra-partition distance from door $d_{k}$ to point $p_{i}$ when one enters the partition.

We generalize doors and points to items represented by $x$. When the specific item types are unclear or not important, we use $\delta_{*}\left(x_{i}, x_{j}\right)$ to indicate one of $\delta_{d 2 d}, \delta_{d 2 p t}$ and $\delta_{p t 2 d}$.

## B. Principles and Definition of Routing Query

Definition 1 (Route and Route Distance). A route $R=$ $\left(x_{s}, d_{i}, \ldots, d_{n}, x_{t}\right)$ is a path through a sequence of doors from an item $x_{s}$ to an item $x_{t}$, where $x_{s}$ and $x_{t}$ can be a point or a door. Given routing request, $R$ is a complete route if $x_{s}$ and $x_{t}$ are the start and terminal points, respectively. Otherwise, we call it a partial route. A route $R$ 's route distance is $\delta(R)$ $=\delta_{*}\left(x_{s}, d_{i}\right)+\sum_{k=i}^{n-1} \delta_{*}\left(d_{k}, d_{k+1}\right)+\delta_{*}\left(d_{n}, x_{t}\right)$.


Fig. 1: An Example of Floorplan
Example 1. Referring to Fig. 1, one can start from $p_{s}$ in partition $v_{1}$, pass doors $d_{2}$ and $d_{5}$, and reach $p_{t}$ in partition $v_{5}$. The complete route is $R=\left(p_{s}, d_{2}, d_{5}, p_{t}\right)$, and a partial route is $R^{\star}=\left(p_{s}, d_{2}, d_{5}\right)$. Assuming $\delta_{p t 2 d}\left(p_{s}, d_{2}\right)=8.3 m, \delta_{d 2 d}\left(d_{2}, d_{5}\right)=$ 4.2m, and $\delta_{d 2 p t}\left(d_{5}, p_{t}\right)=6 m$, we have $\delta\left(R^{\star}\right)=\delta_{p t 2 d}\left(p_{s}, d_{2}\right)+$ $\delta_{d 2 d}\left(d_{2}, d_{5}\right)=12.5 \mathrm{~m}$ and $\delta(R)=18.5 \mathrm{~m}$.

Using the topological mappings introduced in Section II-A, we can easily obtain the partitions that a route $R$ passes. For example, given $R^{\star}=\left(p_{s}, d_{2}, d_{5}\right)$ we know that $R^{\star}$ passes $v_{1}$ between $\left(p_{s}, d_{2}\right)$ and $v_{2}$ between $\left(d_{2}, d_{5}\right)$. Before we formulate our indoor routing query, we discuss two principles of indoor route search.
Principle of Regularity. Traditional outdoor routing algorithms [1], [7], [11], [23] usually exclude loops in a route. This regularization avoids endless route searching. However, a regular route in indoor space can have a loop of doors within onehop. Referring to Fig. 1, anyone who needs to visit partition $v_{10}$ must enter and then leave $d_{15}$, the only accessible door of $v_{10}$. Accordingly, the principle of regularity disqualifies a route that contains one or more doors between two identical doors. For example, partial route $\left(d_{13}, d_{14}, d_{14}, d_{13}\right)$ is not allowed,
because of the doors between the two appearances of door $d_{13}$. This partial route means that one starts from $d_{13}$, passes $v_{7}$ twice and returns to $d_{13}$ again.
Principle of Diversity. The idea of diversifying top- $k$ results [14] inspires us to avoid homogeneous routes in our indoor routing. Back to the example in Fig. 1, suppose a user wants routes from $p_{s}$ to $p_{t}$ while covering two keywords oppo and costa. Several possible routes are listed in Table II. For ease of reading, we insert between each two consecutive route items the partition that connects the two items.

| $R_{1}$ | $\left(p_{s} \xrightarrow{v_{1}} d_{2} \xrightarrow{v_{2}} d_{6} \xrightarrow{v_{3}} d_{7} \xrightarrow{v_{5}} p_{t}\right)$ |
| :---: | :---: |
| $R_{2}$ | $\left(p_{s} \stackrel{\nu_{1}}{ } d_{2} \xrightarrow{\nu_{2}} d_{5} \stackrel{{ }_{5}}{ }{ }_{4}{ }_{7}{ }^{\nu_{3}} d_{7} \xrightarrow{v_{5}} p_{t}\right)$ |
| $R_{3}$ | $\left(p_{s} \xrightarrow{v_{1}} d_{2} \xrightarrow{\nu_{2}} d_{5} \xrightarrow{\nu_{5}} d_{9} \xrightarrow{\nu_{6}} d_{9} \xrightarrow{\nu_{5}} d_{7} \xrightarrow{\nu_{3}} d_{7} \xrightarrow{v_{5}} p_{t}\right)$ |
| $R_{4}$ | $\left(p_{s} \xrightarrow{v_{1}} d_{3} \xrightarrow{\nu_{5}} d_{5} \xrightarrow{\nu_{2}} d_{5} \xrightarrow{\nu_{5}} d_{7} \xrightarrow{\nu_{3}} d_{7} \xrightarrow{\nu_{5}} p_{t}\right)$ |

We use key partition to refer to a partition that covers the start point $p_{s}$, the terminal point $p_{t}$, or a subset of query keywords. We use $K P(\cdot)$ to denote the sequence of key partitions on a route. In Table II, we can find $K P\left(R_{1}\right)=K P\left(R_{2}\right)$ $=K P\left(R_{3}\right)=K P\left(R_{4}\right)=\left\langle v_{1}, v_{2}, v_{3}, v_{5}\right\rangle$, where the four partitions correspond to $p_{s}$, oppo, costa, and $p_{t}$, respectively. Routes $R_{1}$ to $R_{4}$ have the same start and terminal points, and they pass the four key partitions in the same order with different partial routes in between. Consequently, they are homogeneous but some of them have more complicated routing forms. To this end, we have the following two definitions.

Definition 2 (Homogeneous Routes). Two routes $R_{i}$ and $R_{j}$ are homogeneous routes if $R_{i}$.head $=R_{j}$.head, $R_{i}$. tail $=R_{j}$.tail, and $K P\left(R_{i}\right)=K P\left(R_{j}\right)$.

Definition 3 (Prime Route). Suppose $H R$ is a complete set of homogeneous routes for a routing query, we say a route $R_{i} \in H R$ is prime against $R_{j} \in H R$ if $\delta\left(R_{i}\right)<\delta\left(R_{j}\right) . R_{i}$ is a prime route if $R_{i}$ is prime against all other routes in HR.

By the concept of the prime route, we integrate the diversity principle into our routing query such that only prime routes should be included to ensure the diversity of search results.

Example 2. Assuming $R_{1}$ to $R_{4}$ in Table II are the only four regular routes from $p_{s}$ to $p_{t}$ having the sequence of key partitions $\left\langle v_{1}, v_{2}, v_{3}, v_{5}\right\rangle$. Referring to the geometric depiction of Fig. 1, we have $\delta\left(R_{3}\right)>\delta\left(R_{4}\right)>\delta\left(R_{2}\right)>\delta\left(R_{1}\right)$ and thus $R_{1}$ is the prime route among them. Consequently, only $R_{1}$ should be considered for the routing results.

Our study concentrates on finding qualified routes without exhaustive search. We define our research problem as follows.

Problem 1 (Indoor Top- $k$ Keyword-aware Routing Query). Given a start point $p_{s}$, a terminal point $p_{t}$, a distance constraint $\Delta$, and a query keyword list $Q W$, an indoor top$k$ keyword-aware routing query $\operatorname{IKRQ}\left(p_{s}, p_{t}, \Delta, Q W, k\right)$ returns $k$ regular and prime routes from $p_{s}$ to $p_{t}$ in a $k$-set $\Theta$ such that $\forall R \in \Theta, \delta(R) \leq \Delta$ and $\Psi(R, \Delta, Q W) \geq \Psi\left(R^{\prime}, \Delta, Q W\right)$ for any route $R^{\prime} \notin \Theta$ from $p_{s}$ to $p_{t}$ with $\delta\left(R^{\prime}\right) \leq \Delta$.

Above, $\Psi(R, \Delta, Q W)$ captures the ranking score for a route $R$, which takes into account both spatial distance and keyword relevance for $R$ and a given routing query. We proceed to detail the design of our ranking mechanism for routes.

## III. Ranking Relevant Routes for IKRQ

## A. Organization of Indoor Space Keywords

We differentiate two types of keywords associated with indoor partitions. An identity word (i-word) identifies the specific name of a partition, while a thematic word ( t -word) [4] refers to a tag relevant to that partition. A partition can relate to one i-word only but a set of $t$-words. For a specific indoor venue, i-words can be obtained from floor map or the like, and t -words can be extracted from the semantic descriptions of the indoor partitions or those of the corresponding i-words. For example, i-words in a mall are shop names like starbucks and zara and function area names like frontdesk and toilet. Meanwhile, a shop zara can be associated with many t-words such as pants, sweater and coat.

Given an indoor venue, we organize its i-words and t-words in two disjoint sets. If a word is in the i -word set $W_{i}$, it is excluded from the t -word set $W_{t}$ to keep the two keyword sets distinct. Given the full set $V$ of partitions in an indoor venue, a P2I mapping $\operatorname{P2I}\left(v_{k}\right)$ maps a partition $v_{k} \in V$ to its associated i-word $w_{i} \in W_{i}$, and an I2P mapping $I 2 P\left(w_{i}\right)$ maps an i-word $w_{i} \in W_{i}$ to a set of relevant partitions. Moreover, an I2T mapping $\operatorname{I2T}\left(w_{i}\right)$ maps an i-word $w_{i} \in W_{i}$ to a set of relevant t-words, and a T2I mapping $T 2 I\left(w_{t}\right)$ maps a t-word $w_{t} \in W_{t}$ to a set of relevant i-words.

In our setting, we maintain P2I as a many-to-one mapping and I2P as a one-to-many mapping such that an i-word can be associated to different partitions while a partition can only be identified by one i-word. For example, there may be five cashiers in a mall that are distributed in different partitions, but all these partitions are identified by an i-word cashier. Moreover, we maintain I2T and T2I as two many-tomany mappings, meaning that one i-word can be associated to multiple t -words and vice versa. For a partition $v_{k}$, we define its partition words $P W\left(v_{k}\right)$ as $\left\{P 2 I\left(v_{k}\right), \operatorname{I2T}\left(P 2 I\left(v_{k}\right)\right)\right\}$ that consists of an i-word $w_{i}=P 2 I\left(v_{i}\right)$ and a set of t -words relevant to $w_{i}$ as indicated by I2T mapping. For simplicity of presentation, we assume two partitions with the same i-word have the same set of $t$-words.

Example 3. Fig. 2 illustrates parts of the indoor space keyword mappings for the example in Fig. 1. Partition $v_{3}$ is mapped to an i-word costa via the P2I mapping. Reversely, we can use the I2P mapping to find that the $i$-word apple is associated with partition $v_{10}$. According to the I2T and T2I mappings, $t$-words laptop and smartphone are relevant to the $i$-word apple, and the $i$-word costa is relevant to $t$-words coffee and mocha. Moreover, $v_{3}$ 's partition words $P W\left(v_{3}\right)=$ $\{$ costa,$\{$ coffee, mocha,$\ldots\}\}$.

In our organization, i -words act as the pivot between partitions and t -words, as the vocabulary of i -words is much smaller than that of t -words, making the mappings between i-words

| P2I mapping: partition $\rightarrow i$-word $(\mathrm{n}: 1)$ I2T mapping: $i$-word $\rightarrow t$-word (m:n) |
| :--- |
| Partition |
| $v_{12}$ |
| $v_{3}$ |
| $v_{7}$ |
| $v_{10}$ |
| $\cdots$ |

Fig. 2: Indoor Space Keyword Mappings
and partitions more concise. Using the mappings described above, we are able to quantify the keyword relevance between query keywords and routes.

## B. Keyword Relevance between Query Keywords and Routes

Given a query keyword list $Q W$, we convert each query word $w_{Q}$ in $Q W$ into a set of candidate i-words for facilitating a matching between query words and partitions (and therefore routes). If a query word $w_{Q}$ is an i-word, we use the word itself as a candidate. If $w_{Q}$ is a $t$-word, we use the T2I mapping to obtain a set of relevant i-words that are called direct matching i-words. However, only using direct matching iwords may lead to a very sparse candidate set. As each iword is associated with a set of $t$-words that can be regarded as word features, we can measure the similarity between each direct matching i -word and other i -words, and retrieve those i words that is highly similar to the direct matching i-words. We called such i-words indirect matching i-words. For example, in Fig. 2, suppose a query word is laptop and we can find a direct matching i-word apple. Next, for apple we find another i-word samsung that shares some t-words with apple, e.g., both contain t -word smartphone. In this sense, samsung is similar to apple, and samsung can be obtained as an indirect matching i-word of laptop. By considering indirect matching i-words, we offer users more choices in routing.
Definition 4 (Candidate I-word Set). Given a query keyword $w_{Q} \in Q W$, its candidate i-word set $\kappa\left(w_{Q}\right)$ is a set of entries each of which is in form of $\left(w_{i}, s\right)$, a pair of a matching $i$-word $w_{i}$ and the similarity score $s$ between $w_{Q}$ and $w_{i}$. Two cases are discussed in deriving $\kappa\left(w_{Q}\right)$.

- If $w_{Q}$ is an $i$-word, the matching $i$-word can only be $w_{Q}$ itself with the similarity score 1, i.e., $\kappa\left(w_{Q}\right)=\left\{\left(w_{Q}, 1\right)\right\}$.
- If $w_{Q}$ is a t-word, the matching $i$-word(s) should include
- each direct matching $i$-word $w_{i}^{\prime} \in T 2 I\left(w_{Q}\right)$ with the similarity score 1 , denoted as $\left(w_{i}^{\prime}, 1\right)$.
- each indirect matching i-word $w_{i}^{\prime \prime}$ such that $\operatorname{I2T}\left(w_{i}^{\prime \prime}\right) \cap$ $\bigcup_{w_{i} \in T 2 I\left(w_{Q}\right)} I 2 T\left(w_{i}\right) \neq \varnothing$, where $\bigcup_{w_{i} \in T 2 I\left(w_{Q}\right)} I 2 T\left(w_{i}\right)$ is the union set of the $t$-words of each $i$-word in $T 2 I\left(w_{Q}\right)$. In such a case, the similarity is measured in the form of Jaccard Similarity as $s\left(w_{i}^{\prime \prime}\right)=\frac{\left|I 2 T\left(w_{i}^{\prime \prime}\right) \cap \bigcup_{w_{i} \in T I I\left(w_{Q}\right)} I 2 T\left(w_{i}\right)\right|}{\left|I 2 T\left(w_{i}^{\prime \prime}\right) \cup \bigcup_{w_{i} \in T I I\left(w_{Q}\right)^{I}} I 2 T\left(w_{i}\right)\right|}$.
To avoid long tails, we only keep the entries whose similarity scores are greater than a certain threshold $\tau$ in $\kappa\left(w_{Q}\right)$. We use $\kappa\left(w_{Q}\right) . W_{i}$ to denote the set of matching i-words in $\kappa\left(w_{Q}\right)$.
Example 4. Corresponding to Fig. 2, some partitions and their partition words are listed below.

| partition | i-word | t-words |
| :---: | :---: | :---: |
| $v_{3}$ | costa | \{coffee, drinks, macha $\}$ |
| $v_{10}$ | apple | \{phone, mac, laptop, watch $\}$ |
| $v_{7}$ | starbucks | \{coffee, macha, latte, drinks $\}$ |
| $v_{12}$ | samsung | \{phone, laptop, earphone $\}$ |

Given a query keyword list $Q W=\langle$ latte, apple $\rangle$, we set $\tau=0.5$. As keyword latte is a $t$-word, we have T2I(latte) $=\{$ starbucks $\}$. Thus, (starbucks, 1) is included as a candidate $i$-word since starbucks is a direct matching of latte. Furthermore, as i-word costa that is not a direct matching of latte, we have $s($ costa $)=\frac{\mid I 2 T(\text { costa }) \cap \cup_{w_{i} \in T 2 I I(\text { latte })} I 2 T\left(w_{i}\right) \mid}{\mid I 2 T(\text { costa }) \cup \cup_{w_{i} \in T I I(\text { latte })} I 2 T\left(w_{i}\right) \mid}$. Since I2T $($ costa $)=\{$ coffee, drinks, macha $\}$ and $\bigcup_{w_{i} \in T 2 I(\text { latte })} I 2 T\left(w_{i}\right)$ $=\{$ coffee, drinks, macha, latte $\}$, we have $s($ costa $)=3 / 4=0.75$. Likewise, we have $s($ apple $)=s($ samsung $)=0$. Consequently, $\kappa($ latte $)=\{($ starbucks, 1$),($ costa, 0.75$)\}$ and $\kappa($ latte $) . W_{i}=$ $\{$ starbucks, costa $\}$. As the other keyword apple is an i-word, we have $\kappa($ apple $)=\{($ apple, 1$)\}$ and $\kappa($ apple $) \cdot W_{i}=\{$ apple $\}$.

Finally, we can convert the original query keyword list to a list of candidate $i$-word sets: $\mathbf{K}(Q W)=\langle\kappa($ latte $), \kappa($ apple $)\rangle=$ $\langle\{($ starbucks, 1$),($ costa, 0.75$)\},\{($ apple, 1$)\}\rangle$.

On the other hand, given an item $x$ on a route $R$, we use an operator $v_{*}(x)$ to obtain its relevant partitions. If $x$ is a door, we obtain all the partitions that one can leave through door $x$, i.e., $v_{*}(x)=D 2 P_{\sqsubset}(x)$. Otherwise, $x$ is a point and we obtain the partition that contains point $x$, i.e., $v_{*}(x)=v(x)$. Accordingly, we look at i-words in a route.
Definition 5 (Route Words). Given $R=\left(x_{s}, d_{i}, \ldots, d_{n}, x_{t}\right)$, its route words are the union of all its relevant partitions' associated $i$-words, computed as $R W(R)=\bigcup_{x \in R} P W\left(v_{*}(x)\right) \cdot w_{i}$.
Example 5. Referring to the route $R=\left(p_{s}, d_{3}, p_{t}\right)$ in Fig. 1 , for point $p_{s}$, we have $P W\left(v\left(p_{s}\right)\right) \cdot w_{i}=P W\left(v_{1}\right) \cdot w_{i}=\{$ zara $\}$. Likewise, we have $P W\left(v\left(p_{t}\right)\right) \cdot w_{i}=\varnothing$. For door $d_{3}$, we have $P W\left(D 2 P_{\sqsubset}\left(d_{3}\right)\right) \cdot w_{i}=P W\left(v_{1}\right) \cdot w_{i} \cup P W\left(v_{5}\right) \cdot w_{i}=\{z a r a\} \cup \varnothing$ $=\{$ zara $\}$. Consequently, we have $R W(R)=\{$ zara $\}$.

Next, route $R$ 's keyword relevance is defined as follows.
Definition 6 (Keyword Relevance). Given a query keyword list $Q W$, a route R's keyword relevance w.r.t. $Q W$ is

$$
\rho_{Q W}(R)=\left\{\begin{array}{l}
0, \quad \text { if } N_{Q W}(R)=0 ; \\
N_{Q W}(R)+\frac{\sum_{w_{Q} \in Q W}\left(\max _{w_{i}^{\prime} \in \mathrm{M}\left(w_{Q}, R\right)} s\left(w_{i}^{\prime}\right)\right)}{N_{Q W}(R)}, \quad \text { otherwise. }
\end{array}\right.
$$

Above, $N_{Q W}(R)$ is the number of $R$ 's route words that are relevant to query words in $Q W$, and $\mathrm{M}\left(w_{Q}, R\right)=\kappa\left(w_{Q}\right) \cdot W_{i} \cap$ $R W(R)$ denotes the set of $w_{Q}$ 's matching i-words on $R$. When the context is clear, we use $\rho(R)$ to denote the keyword relevance. Also, $\rho(R)$ is positive if there is at least one query keyword covered by $R$ (i.e., $N_{Q W}(R)>0$ ). In such a case, the left part of the summation indicates the number of query keywords that $R$ covers, and the right part measures the average of each covered keyword $w_{Q}$ 's maximum similarity score with its matching i-words on $R$ (i.e., $\mathrm{M}\left(w_{Q}, R\right)$ ). In the best case, all keywords in $Q W$ can match an i-word on $R$ with similarity score 1 . Thus, the range of $\rho(R)$ is $0 \cup(1,|Q W|+1]$.

The computation complexity of $\rho(R)$ is $O(m n)$, where $m$ is $|Q W|$ and $n$ is the number of i-words in a route $R$.

Example 6. Referring to Fig. 1, we have two routes $R_{1}=$ $\left(p_{s}, d_{2}, d_{5}, d_{7}, d_{7}, p_{t}\right)$ and $R_{2}=\left(d_{15}, d_{15}, d_{14}, d_{13}, d_{7}, d_{6}\right)$ and a query keyword list $Q W=\{$ latte, apple $\}$. For route $R_{1}$, we have $R W\left(R_{1}\right)=\{$ zara,oppo, costa $\}$, and $\kappa($ latte $) . W_{i} \cap R W\left(R_{1}\right)=$ $\{$ costa $\}$ with similarity score 0.75 and $\kappa($ apple $) . W_{i} \cap R W\left(R_{1}\right)$ $=\varnothing$, thus $\rho\left(R_{1}\right)=1+\frac{0.75}{1}=1.75$.

For route $R_{2}$, we have $R W\left(R_{2}\right)=\{$ apple, starbucks, costa $\}$, $\kappa($ latte $) . W_{i} \cap R W\left(R_{2}\right)=\{$ starbucks, costa $\}$, and $\kappa($ apple $) . W_{i} \cap$ $R W\left(R_{2}\right)=\{$ apple $\}$. Consider the two candidate $i$-words of query keyword latte, we select i-word starbucks with the maximum similarity score as $s($ starbucks $)=1>s($ costa $)=$ 0.75. Consequently, $\rho\left(R_{2}\right)=2+\frac{1+1}{2}=3$.

## C. Ranking Score for Routes

Definition 7 (Ranking Score). Given a query $\operatorname{IKRQ}\left(p_{s}, p_{t}, \Delta\right.$, $Q W, k$ ) and a route $R$ from $p_{s}$ to $p_{t}$, the ranking score of $R$ is computed as a linear combination of the normalized scores of keyword relevance and spatial relevance as follows.

$$
\begin{equation*}
\psi(R, \Delta, Q W)=\alpha \cdot \frac{\rho(R)}{|Q W|+1}+(1-\alpha) \cdot\left(\frac{\Delta-\delta(R)}{\Delta}\right) \tag{1}
\end{equation*}
$$

We use $\psi(R)$ for simplicity when the context is clear. Our ranking score can be flexibly customized by the tradeoff parameter $\alpha \in[0,1]$ according to specific application needs [2], [6], [12], [20]. For example, a shopper in a mall may prefer the routes covering the query keywords as much as possible for the sake of shopping, and the requirement for walking distance can be less important. In this case, a large $\alpha$ can boost the keyword score. In contrast, passengers in airports are often more sensitive to distance constraints and would accept some query keywords missing. Thus, a small $\alpha$ can be used to emphasize the distance. The effect of $\alpha$ is studied experimentally.

## IV. Search Algorithms for IKRQ

A naive idea for our routing works as follows. We iteratively find candidate partial routes from the start point, validate them using the distance constraint and the two principles (Section II-B), and expand them through doors. After all complete routes have been seen, we return the $k$ routes with the highest ranking scores. This method is inefficient as it finds all complete routes through expensive expansions. To improve the efficiency, we can identify unpromising route branches and avoid expanding to them, which is enabled by pruning rules.

## A. Pruning Rules for Expansion

Our pruning rules use the skeleton distance [22] as the lower bound indoor distance for two indoor items $x_{i}$ and $x_{j}$.
$\left|x_{i}, x_{j}\right|_{L}=\left\{\begin{array}{l}\left|x_{i}, x_{j}\right|_{E}, \quad \text { if } x_{i} \text { and } x_{j} \text { are on the same floor; } \\ \min _{s d_{i} \in S D\left(x_{i}\right), s d_{j} \in S D\left(x_{j}\right)}\left(\left|x_{i}, s d_{i}\right|_{E}+\delta_{s 2 s}\left(s d_{i}, s d_{j}\right)+\right. \\ \left.\left|s d_{j}, x_{j}\right|_{E}\right), \quad \text { otherwise. }\end{array}\right.$

Specifically, $\left|x_{i}, x_{j}\right|_{L}$ is the Euclidean distance if $x_{i}$ and $x_{j}$ are on the same floor. Otherwise, one needs to go through a number of staircase doors (e.g., $s d_{i} \in S D\left(x_{i}\right)$ ) to reach $x_{j}$ from $x_{i}$, and there can be multiple such paths. In this case, $\left|x_{i}, x_{j}\right|_{L}$ is the shortest path distance among all such paths.

With the lower bound distance, we derive the following pruning rules for a query $\operatorname{IKRQ}\left(p_{s}, p_{t}, \Delta, Q W, k\right)$.
Pruning Rule 1. A partial route $R^{\star}=\left(p_{s}, d_{i}, \ldots, d_{n}\right)$ in the searching can be pruned if $\delta\left(R^{\star}\right)+\left|d_{n}, p_{t}\right|_{L}>\Delta$.

Pruning Rule 2. A door $d_{n}$ can be pruned out of the search if $\left|p_{s}, d_{n}\right|_{L}+\left|d_{n}, p_{t}\right|_{L}>\Delta$.

Pruning Rule 3. An indoor partition $v_{i}$ can be pruned out of the search if its lower bound distance $\delta\left(p_{s}, v_{i}, p_{t}\right)=$

$$
\min _{d_{i} \in P 2 D_{\sqsupset}\left(v_{i}\right), d_{j} \in P 2 D_{\sqsubset}\left(v_{i}\right)}\left(\left|p_{s}, d_{i}\right|_{L}+\delta_{d 2 d}\left(d_{i}, d_{j}\right)+\left|d_{j}, p_{t}\right|_{L}\right)>\Delta .
$$

Example 7. Referring to Fig. 1, suppose we need to route from $p_{s}$ to $p_{t}$ with the distance constraint $\Delta=16 m$, and we have obtained a partial route $R^{\star}=\left(p_{s}, d_{2}, d_{5}\right)$ whose distance is $12.5 \mathrm{~m} . R^{\star}$ can be pruned according to Pruning Rule 1, since $\delta\left(R^{\star}\right)+\left|d_{5}, p_{t}\right|_{E}=12.5 m+6 m>\Delta=16 m$. Also, suppose that $\left|p_{s}, d_{6}\right|_{E}+\left|d_{6}, p_{t}\right|_{E}=13 m+5 m>\Delta=16 m$, door $d_{6}$ can be discarded according to Pruning Rule 2. Take a close look at partition $v_{3}$ whose only two doors are $d_{6}$ and $d_{7}$, and $\left|p_{s}, d_{6}\right|_{E}+\left|d_{6}, d_{7}\right|_{E}+\left|d_{7}, p_{t}\right|_{E}=13 m+4.5 m+1 m>\Delta=$ 16m, v3 can also be discarded according to Pruning Rule 3.

Furthermore, we derive the upper bound of the ranking score to enable the following pruning rule.
Pruning Rule 4. Given the current $k$-th highest ranking score $\psi_{k}$ among the seen complete routes, a partial route $R^{\star}=$ $\left(p_{s}, d_{i}, \ldots, d_{n}\right)$ can be pruned if its upper bound ranking score $\psi_{U}\left(R^{\star}\right)=\alpha \cdot 1+(1-\alpha)\left(1-\left(\delta\left(R^{\star}\right)+\left|d_{n}, p_{t}\right|_{L}\right) / \Delta\right) \leq \psi_{k}$.

In Pruning Rule 4, we upper bound a partial route's final ranking score by an overestimate of its keyword and spatial scores. The former is overestimated to 1 as a full coverage of query keywords and the latter is computed based on the lower bound indoor distance to $p_{t}$ (i.e., $\delta\left(R^{\star}\right)+\left|d_{n}, p_{t}\right|_{L}$ ). This pruning rule enables the $k$ bound pruning, i.e., we can discard a partial route if its upper bound ranking score is not higher than the $k$-th best score among the routes already obtained.

Furthermore, recall that only a prime route should be returned among all homogeneous routes (see the diversity principle in Section II-B). To this end, we have the following lemma and a corresponding pruning rule.

Lemma 1. Given a query $\operatorname{IKRQ}\left(p_{s}, p_{t}, \Delta, Q W, k\right)$, if route $R=\left(p_{s}, d_{i}, \ldots, d_{n}, p_{t}\right)$ is a returned prime route, each of its partial route $R^{\star}=\left(p_{s}, \ldots, d_{k}\right)(i \leq k \leq n)$ is also a prime route. Proof. Without loss of generality, we represent $R$ 's remaining route that continues with $R^{\star}$ as $R^{\vdash}=\left(d_{k}, \ldots, p_{t}\right)$. We prove the lemma by contradiction. Suppose that $R^{\star}$ is not a prime route and $R^{\star^{\prime}}$ is $R^{\star}$ 's homogeneous route such that $\delta\left(R^{\star^{\prime}}\right)<\delta\left(R^{\star}\right)$ and $K P\left(R^{\star^{\prime}}\right)=K P\left(R^{\star}\right)$. According to Definition 2, we have $R^{\star^{\prime}}$.tail $=R^{\star}$.tail $=d_{k}$. By
concatenating $R^{\star^{\prime}}$ and $R^{\vdash}$ at $d_{k}$, we can obtain a complete route $R^{\prime}$ from $p_{s}$ to $p_{t}$. Moreover, we have its sequence of key partitions $K P\left(R^{\prime}\right)=\operatorname{concat}\left(K P\left(R^{\star^{\prime}}\right), K P\left(R^{\vdash}\right)\right)=$ concat $\left(K P\left(R^{\star}\right), K P\left(R^{\vdash}\right)\right)=K P(R)$. According to Definitions 2 and 3, we find $R^{\prime}$ is a homogeneous route of $R$ and is prime against $R$. Thus, $R$ cannot be a prime route.

According to Lemma 1, a partial route cannot be a prime route if the search has already found a homogeneous route that is prime against it. This enables the following pruning rule.

Pruning Rule 5. A partial route $R^{\star}=\left(p_{s}, d_{i}, \ldots, d_{n}\right)$ in the search can be pruned if the search has already obtained a route $R^{\star^{\prime}}$ from $p_{s}$ to $d_{n}$ that is prime against $R^{\star}$.

Combining the definition of the prime route with the regularity principle in Section II-B, we have the following lemma.
Lemma 2. Given a route $R$ returned by the $\operatorname{IKRQ}\left(p_{s}, p_{t}, \Delta\right.$, $Q W, k), R$ can have a loop of two consecutive identical doors $\left(d_{k}, d_{k}\right)$ only if the loop passes a key partition that covers at least one query keyword in $Q W$.
Proof. (Sketch) We prove it by contradiction. Suppose that $R=\left(p_{s}, \ldots, d_{k}, d_{k}, \ldots, p_{t}\right)$ contains a loop $\left(d_{k}, d_{k}\right)$ that does not pass any key partition. According to Definition 3, there must be a homogeneous route $R^{\prime}=\left(p_{s}, \ldots, d_{k}, \ldots, p_{t}\right)$ of $R$ and $R^{\prime}$ is prime against $R$ in that $K P\left(R^{\prime}\right)=K P(R)$ and $\delta\left(R^{\prime}\right)<$ $\delta(R)$. This violates the diversity principle.

Example 8. Suppose $\operatorname{IKRQ(} p_{s}, p_{t}, 25 m$, \{latte, apple\}, 1) is issued in the setting shown in Fig. 1, the parameter $\alpha$ is 0.2, and the search has obtained a complete route $R_{1}=\left(p_{s}, d_{2}, d_{6}, d_{7}, p_{t}\right)$ whose distance is 20 m . According to Example 6, we have $R_{1}$ 's keyword relevance is 1.75 and its ranking score is $0.2 \cdot \frac{1.75}{3}+0.8 \cdot \frac{25-20}{25}=0.277$ according to Equation 1. Thus, the current kbound is updated to 0.277. Next, the search expands to a route $R_{2}^{\star}=\left(p_{s}, d_{2}, d_{5}, d_{7}, d_{7}\right)$ whose distance is 22.5 m and lower bound distance to $p_{t}$ is $22.5 m+\left|d_{7}, p_{t}\right|_{E}=22.5 m+1 m=23.5 m$. According to Pruning Rule 4, $R_{2}^{\star}$ 's ranking score is upper-bounded by $0.2 \cdot 1+0.8 \cdot \frac{25-23.5}{25}=0.248$. So $R_{2}^{\star}$ should be pruned as its upper bound ranking score is smaller than the current kbound.

Suppose that two partial routes have been obtained between $p_{s}$ and $d_{5}$, namely $R_{3}^{\star}=\left(p_{s}, d_{2}, d_{5}\right)$ and $R_{4}^{\star}=\left(p_{s}, d_{3}, d_{5}, d_{5}\right)$. Both routes pass a key partition $v_{2}$ (its $i$-word oppo is an indirect matching of apple) and we have $\delta\left(R_{3}^{\star}\right)=12.5 \mathrm{~m}$ and $\delta\left(R_{4}^{\star}\right)$ $=23.2 \mathrm{~m}$. Currently, $R_{3}^{\star}$ is prime against $R_{4}^{\star}$ and therefore $R_{4}^{\star}$ should be pruned according to Pruning Rule 5. Moreover, according to Lemma 2, when the search has expanded to a door $d_{9}$, the next hop cannot be $d_{9}$ again as neither of its relevant partitions ( $v_{5}$ and $v_{6}$ ) covers a query keyword.

## B. Overall Search Framework

Based on the above pruning rules and lemmas, we formalize our overall framework in Algorithm 1. A priority queue Q (initialized in line 1) is used to control the order of route expansion. The local information of the current expansion is kept in a five-tuple $\operatorname{stamp} S(v, R, \delta, \rho, \psi)$, where $R$ is a route that has been expanded to a door or the terminal point so far,

```
Algorithm 1 IKRQ_Search \(\left(p_{s}, p_{t}, \Delta, Q W, k\right)\)
    initialize priority queue Q
    set of all candidate i-words \(W_{c i} \leftarrow \bigcup_{w_{Q} \in Q W} \kappa\left(w_{Q}\right) \cdot W_{i}\)
    \(P \leftarrow\left(\cup_{w_{Q} \in Q W} I 2 P\left(\kappa\left(w_{Q}\right) . W_{i}\right)\right) \backslash v\left(p_{s}\right) \cup v\left(p_{t}\right)\)
    door sets \(D_{n} \leftarrow \varnothing, D_{f} \leftarrow \varnothing\)
    kbound \(\leftarrow 0\)
    initialize hashtable \(\mathrm{H}_{\text {prime }}\)
    \(R_{0} \leftarrow\left(p_{s}\right)\)
    \(S_{0} \leftarrow\left(v\left(p_{s}\right), R_{0}, 0, \rho\left(R_{0}\right), \psi\left(R_{0}\right)\right)\)
    Q.push \(\left(S_{0}\right)\)
    while \(Q\) is not empty do
        \(S_{i} \leftarrow \mathrm{Q} \cdot p o p()\)
        \(E S \leftarrow \operatorname{find}\left(S_{i}\right) \quad \triangleright\) find the next valid stamps
        for each \(S_{j} \in E S\) do
            connect \(\left(S_{j}\right) \quad \triangleright\) connect each valid stamp to terminal
    return current top- \(k\) results
```

$v$ is the last partition that $R$ reaches, and $\delta, \rho, \psi$ are $R$ 's route distance, keyword relevance, and ranking score, respectively. The architecture of our search algorithms is depicted in Fig. 3.


Fig. 3: Architecture of the IKRQ Search Algorithms
The initialization (lines 1-6) obtains a set $W_{c i}$ of all candidate i-words w.r.t. query keyword list $Q W$ (line 2), and computes a set $P$ of all key partitions covering at least one keyword in $Q W$ (line 3). We exclude the partition $v\left(p_{s}\right)$ from $P$ and add the partition $v\left(p_{t}\right)$ to $P$ to regularize the route search. Sets $D_{f}$ and $D_{n}$ hold the doors already explored (line 4). Doors in $D_{f}$ are filtered by Pruning Rule 2, whereas those in $D_{n}$ are not. Subsequent routing skips doors in $D_{f}$, and exempts doors in $D_{n}$ from repeated checks by Pruning Rule 2. We initialize the kbound for Pruning Rule 4 (line 5), and a hashtable $\mathrm{H}_{\text {prime }}$ to store the route temporarily prime against others for Pruning Rule 5 (line 6). The algorithm then performs the expansion iteratively (lines 7-14). It generates an initiate route $\left(p_{s}\right)$ and its corresponding stamp $S_{0}$ (lines 7-8). Next, it pushes $S_{0}$ into Q and iterates on Q until all stamps have been expanded to $p_{t}$ (lines 9-14). The search follows a find-and-connect paradigm. That is, in each iteration, it fetches a stamp $S_{i}$ with the highest ranking score from $Q$ (line 11), expands the current stamp to find a set $E S$ of valid stamps based on the pruning rules (calling function find() in line 12), and attempts to connect each valid stamp in $E S$ to the destination if some condition is met (calling function connect () in line 14). The top- $k$ results are returned when Q is empty (lines 10 and 15).

Given a valid stamp $S_{i}$, we propose two versions of strategies to find the next valid stamps. One is based on the indoor topology information and the other is based on the query keywords. The search algorithms using the two different strategies are called topology-oriented expansion (ToE) and keyword-
oriented expansion (KoE), respectively. Function find() is instantiated as ToE_find() and KoE_find(), respectively.

## C. Topology-oriented Expansion (ToE)

The idea of find() in ToE is to reach all accessible doors from the current door based on indoor topology. We formalize this strategy in Algorithm 2. In particular, line 1 initializes a set $E S$ to save the valid stamps to be found, and line 2 obtains the current stamp $S_{i}$ and the current door $d_{k}$ from the tail of the corresponding route $R_{i}$. To determine if $S_{i}$ is a temporary prime route that does not need to be pruned (c.f. Pruning Rule 5), ToE calls a function prime_check() to compare $S_{i}$ 's route $R_{i}$ to its homogeneous routes already recorded in a global hashtable $\mathrm{H}_{\text {prime }}$ (line 3).

```
Algorithm 2 ToE_find (Stamp \(S_{i}\) )
    set \(E S \leftarrow \varnothing\)
    \(\left(v_{i}, R_{i}, \delta_{i}, \rho_{i}, \psi_{i}\right) \leftarrow S_{i} ; d_{k} \leftarrow R_{i}\).tail
    if prime_check \(\left(S_{i}, \mathrm{H}_{\text {prime }}\right)\) is false then return \(\triangleright\) Pruning Rule 5
    for each \(d_{l}\) in \(P 2 D_{\sqsubset}\left(v_{i}\right) \backslash D_{f}\) do
        if \(d_{l} \in R_{i}\) and \(d_{l} \neq R_{i}\).tail then continue \(\quad \triangleright\) regularity check
        if \(d_{l} \notin D_{n}\) then \(\quad \triangleright\) Pruning Rule 2
            if \(\left|p_{s}, d_{l}\right|_{L}+\left|d_{l}, p_{t}\right|_{L}>\Delta\) then
                \(D_{f} \leftarrow D_{f} \cup d_{l} ;\) continue
            else
                \(D_{n} \leftarrow D_{n} \cup d_{l}\)
        \(v_{j} \leftarrow D 2 P_{\sqsupset}\left(d_{l}\right) \backslash v_{i}\)
        if \(d_{k}==d_{l}\) and \(P W\left(v_{i}\right) \cdot w_{i} \notin W_{c i}\) then
            continue \(\quad \triangleright\) regularity check based on Lemma 2
        if \(\delta_{i}+\delta_{d 2 d}\left(d_{k}, d_{l}\right)>\Delta\) then continue \(\triangleright\) distance constraint check
        \(\delta_{L B} \leftarrow \delta_{i}+\delta_{d 2 d}\left(d_{k}, d_{l}\right)+\left|d_{l}, p_{t}\right| L\)
        if \(\delta_{L B}>\Delta\) then continue \(\quad \triangleright\) Pruning Rule 1
        \(\psi_{U B} \leftarrow \alpha \cdot 1+(1-\alpha)\left(1-\delta_{L B} / \Delta\right)\)
        if \(\psi_{U B} \leq\) kbound then continue \(\quad \triangleright\) Pruning Rule 4
        \(R_{j} \leftarrow\) append \(d_{l}\) to \(R_{i}\)
        \(S_{j} \leftarrow\left(v_{j}, R_{j}, \delta\left(R_{j}\right), \rho\left(R_{j}\right), \psi\left(R_{j}\right)\right)\)
        prime_update \(\left(S_{j}, \mathrm{H}_{\text {prime }}\right)\)
        add \(S_{j}\) to \(E S\)
    return \(E S\)
```

The function prime_check() is detailed in Algorithm 3. First, the key for identifying $R_{i}$ 's homogeneous routes is formed as $\left(R_{i} \cdot t a i l, K P\left(R_{i}\right)\right)$, a pair of $R_{i}$ 's tail door and $R_{i}$ 's sequence of key partitions ${ }^{3}$ (line 2). The function returns true if the shortest distance among all homogeneous routes in $\mathrm{H}_{\text {prime }}$ does not exist or is greater than $R_{i}$ 's distance $\delta_{i}$. Otherwise, it returns false to indicate that $R_{i}$ is not the temporary prime route and should be pruned.

```
Algorithm 3 prime_check (Stamp \(S_{i}\), Hashtable \(\mathrm{H}_{\text {prime }}\) )
    \(\left(v_{i}, R_{i}, \delta_{i}, \rho_{i}, \psi_{i}\right) \leftarrow S_{i}\)
    key \(\leftarrow\left(R_{i} . t a i l, K P\left(R_{i}\right)\right)\)
    if \(\mathrm{H}_{\text {prime }}[k e y]=\varnothing\) or \(\mathrm{H}_{\text {prime }}[k e y]>\delta_{i}\) then return true else return false
```

Back to line 4 in Algorithm 2, ToE tests on each leavable door $d_{l}$ of $R_{i}$ 's last reached partition $v_{i}$. It excludes those doors in the global set $D_{f}$ that have been pruned by Pruning Rule 2. Before applying Pruning Rule 2, line 5 performs a regularity check. Specifically, if $d_{l}$ has been visited by $R_{i}$ before ( $d_{l} \in R_{i}$ ),

[^2]it can be the next door only when $R_{i}$ 's last visited door is also $d_{l}$ (a loop within one-hop in regularity principle). Hence, $d_{l}$ should be pruned if $d_{l} \neq R_{i}$.tail. Afterwards, ToE examines $d_{l}$ based on Pruning Rule 2. Specifically, if $d_{l}$ is not in $D_{n}$ (line 6), ToE computes the lower bound distance w.r.t. $d_{l}$ (line 7). If it exceeds $\Delta$, ToE adds it to $D_{f}$ to make sure it is not processed in subsequent routing. Otherwise, ToE adds it to $D_{n}$.

Next, ToE performs checks according to the query principles and pruning rules. Particularly, lines 11-13 check the regularity for two identical doors according to Lemma 2, in which $v_{j}$ is the partition that connects the $d_{k}$ and $d_{l}$ on the route. Line 14 checks the distance constraint for the route to be expanded to $d_{l}$, and lines $15-16$ further derive its lower bound and verify it according to Pruning Rule 1. In the end, ToE uses Pruning Rule 4 to remove the expansion whose derived upper bound ranking score cannot exceed the kbound of the search (lines 17-18). Once the check is done, ToE validates the expansion to $d_{l}$ by appending $d_{l}$ to the end of $R_{j}$ and generating the corresponding stamp $S_{j}$ (lines 19-20). Moreover, it calls function prime_update() to update the temporary prime route with $S_{j}$ (line 19). When each accessible door $d_{l}$ has been explored, ToE_find() returns the set $E S$ that contains all valid stamps.

Algorithm 4 formalizes the function prime_update(). The hash key generation is the same as its counterpart of prime_check(). Their difference is that prime_update puts the distance of the route $R_{i}$ into $\mathrm{H}_{\text {prime }}$ if $R_{i}$ is currently prime against its homogeneous routes.

```
Algorithm 4 prime_update (Stamp \(S_{i}\), Hashtable \(\mathrm{H}_{\text {prime }}\) )
    \(\left(v_{i}, R_{i}, \delta_{i}, \rho_{i}, \psi_{i}\right) \leftarrow S_{i}\)
    key \(\leftarrow\left(R_{i}\right.\). tail,\(\left.K P\left(R_{i}\right)\right)\)
    if \(\mathrm{H}_{\text {prime }}[k e y]=\varnothing\) or \(\mathrm{H}_{\text {prime }}[k e y]>\delta_{i}\) then \(\mathrm{H}_{\text {prime }}[k e y] \leftarrow \delta_{i}\)
```

We proceed to present how to connect each valid stamp returned by ToE_find(). The process is formalized in Algorithm 5. For stamp $S_{j}$ to be connected, we first determine if it has reached the same partition of the terminal point $p_{t}$ (line 2). If so, we immediately connect the end of the corresponding route $R_{j}$ to $p_{t}$ and check if the resulting route $R_{f}$ meets the query conditions (lines 3-5). If so, we add $R_{f}$ to the top- $k$ results and update the current kbound (lines 6-7). Otherwise, we explore how $S_{j}$ can be further processed (lines 8-19). Here we call prime_check() again to verify if $S_{j}$ holds the temporary prime route (lines $9-10$ ). Afterwards, we check if the current route $R_{j}$ has already covered all the query keywords (line 11). If so, there is no necessary to reach any other key partitions. Therefore, we immediately connect the end of $R_{j}$ to $p_{t}$ by finding a shortest regular route ${ }^{4}$, and obtain a final stamp $S_{f}$ (lines 12-14). Afterwards, we add the qualified route $R_{f}$ to the top- $k$ results and update the current kbound (lines $15-$ 17). If $R_{j}$ does not cover all the query keywords, we push $S_{j}$ into the queue for further expansion (lines 18-19). Lines $2-$ 17 in Algorithm 5 utilize a heuristic rule that the current

[^3]stamp should connect to the destination directly when a certain condition is met, i.e., it has reached the destination partition or covered all query keywords. As a result, the kbound and prime routes are updated as soon as possible, which in turn help to prune more aggressively.

```
Algorithm 5 connect (Stamp \(S_{j}\) )
    \(\left(v_{j}, R_{j}, \boldsymbol{\delta}\left(R_{j}\right), \boldsymbol{\rho}\left(R_{j}\right), \boldsymbol{\psi}\left(R_{j}\right)\right) \leftarrow S_{j}\)
    if \(v_{j}==v\left(p_{t}\right)\) then \(\triangleright\) reach a door in the same partition with \(p_{t}\)
        \(R_{f} \leftarrow\) append \(p_{t}\) to \(R_{j}\)
        \(S_{f} \leftarrow\left(v\left(p_{t}\right), R_{f}, \delta\left(R_{f}\right), \rho\left(R_{f}\right), \psi\left(R_{f}\right)\right)\)
        if \(\delta\left(R_{f}\right) \leq \Delta\) and \(\psi\left(R_{f}\right)>\) kbound and prime_check \(\left(S_{f}, \mathrm{H}_{\text {prime }}\right)\)
    is true then
                update top- \(k\) results and \(k\) bound with \(R_{f}\)
                prime_update( \(\left.S_{f}, \mathrm{H}_{\text {prime }}\right)\)
    else
        if prime_check \(\left(S_{j}, \mathrm{H}_{\text {prime }}\right)\) is false then
            continue
                \(\triangleright\) Pruning Rule 5
        if \(\rho\left(R_{j}\right)=|Q W|+1\) then \(\quad \triangleright\) all keywords has been covered
            find shortest regular route \(\left(d_{j}, d_{x}, \ldots, p_{t}\right) \quad \triangleright\) regularity check
            \(R_{f} \leftarrow\) append \(\left(d_{x}, \ldots, p_{t}\right)\) to \(R_{j}\)
            \(S_{f} \leftarrow\left(v\left(p_{t}\right), R_{f}, \delta\left(R_{f}\right), \rho\left(R_{f}\right), \psi\left(R_{f}\right)\right)\)
            if \(\delta\left(R_{f}\right) \leq \Delta\) and \(\psi\left(R_{f}\right)>k b o u n d\) and prime_check \(\left(S_{f}\right.\),
    \(\mathrm{H}_{\text {prime }}\) ) is true then
                                    update top- \(k\) results and \(k\) bound with \(R_{f}\)
                                    prime_update( \(\left.S_{f}, \mathrm{H}_{\text {prime }}\right)\)
        else
                            \(\triangleright\) can be further expanded
                Q.push \(\left(S_{j}\right)\)
```


## D. Keyword-oriented Expansion (KoE)

ToE always expands from the current door to the next enterable door within one hop. However, such one-hop expansions cannot guarantee covering some query keyword(s). An alternative is to focus on the query words that have not been covered by the current stamp, and directly expand to one of the key partitions that can cover some of those uncovered query words. This idea is called keyword-oriented expansion (KoE), and its finding strategy is formalized in Algorithm 6.

The processing on the current stamp $S_{i}$ (lines 1-3) is the same as the counterpart in Algorithm 2. It is noteworthy that here $v_{i}$ must be a key partition and $d_{k}$ must be an enterable door of $v_{i}$ since in each expansion KoE has to reach a key partition. Next, unlike ToE that iterates on each enterable door based on indoor topology, KoE searches for the candidate partitions relevant to the uncovered query keywords (lines $4-$ 7). Specifically, it copies the key partition set $P$ (initialized in line 2 of Algorithm 1) to a local set $P^{\prime}$ (line 4), iterates on each query word $w_{Q} \in Q W$, and checks if $w_{Q}$ has been covered by the current route $R_{i}$ in $S_{i}$ (lines 5-6). If so, its corresponding key partitions should be removed from $P^{\prime}$ (line 7). In line 6 , a case is handled separately. When the initial stamp $S_{0}$ is encountered $\left(d_{k}=p_{s}\right)$, we do not remove any partition from $P^{\prime}$. This ensures that no extra constraint on partitions is added.

Afterwards, KoE deals with each candidate partition $v_{j} \in P^{\prime}$ to find a route that can reach one of the enterable doors of $v_{j}$. For each candidate partition $v_{j}$, KoE derives the lower bound distance and checks it against Pruning Rule 3 (lines 9-10). If a partition $v_{j}$ should be pruned, it is excluded from the global set $P$ and never processed in subsequent expansions.

```
Algorithm 6 KoE_find (Stamp \(S_{i}\) )
    set \(E S \leftarrow \varnothing\)
    \(\left(v_{i}, R_{i}, \delta_{i}, \rho_{i}, \psi_{i}\right) \leftarrow S_{i} ; d_{k} \leftarrow R_{i}\). tail
    if prime_check \(\left(S_{i}, \mathrm{H}_{\text {prime }}\right)\) is false then return \(\triangleright\) Pruning Rule 5
    \(P^{\prime} \leftarrow P \quad \triangleright\) find candidate key partitions
    for \(w_{Q} \in Q W\) do
        if \(\kappa\left(w_{Q}\right) . W_{i} \cap R W\left(R_{i}\right) \neq \varnothing\) and \(d_{k} \neq p_{s}\) then
                \(P^{\prime} \leftarrow P^{\prime} \backslash I 2 P\left(\kappa\left(w_{Q}\right) \cdot W_{i}\right)\)
    for \(v_{j}\) in \(P^{\prime}\) do
        if \(\delta_{L B}\left(p_{s}, v_{j}, p_{t}\right)>\Delta\) then
            \(P \leftarrow P \backslash v_{j} ;\) continue \(\quad \triangleright\) Pruning Rule 3
        if \(\delta_{i}+\delta_{L B}\left(d_{k}, v_{j}, p_{t}\right)>\Delta\) then continue \(\triangleright\) distance constraint check
        for each \(d_{x} \in P 2 D_{\sqsubset}\left(v_{i}\right)\) and \(d_{l} \in P 2 D_{\sqsupset}\left(v_{j}\right)\) do
            find shortest regular route \(\left(d_{k}, d_{x}, \ldots, d_{l}\right) \quad \triangleright\) regularity check
            \(R_{j} \leftarrow\) append \(\left(d_{x}, \ldots, d_{l}\right)\) to \(R_{i}\)
            \(\delta_{L B} \leftarrow \delta\left(R_{j}\right)+\left|d_{l}, p_{t}\right|_{L}\)
                if \(\delta_{L B}>\Delta\) then continue \(\quad \triangleright\) Pruning Rule 1
                \(\psi_{U B} \leftarrow \alpha \cdot 1+(1-\alpha)\left(1-\delta_{L B} / \Delta\right)\)
                if \(\psi_{U B} \leq k\) bound then continue \(\quad \triangleright\) Pruning Rule 4
                \(S_{j} \leftarrow\left(v_{j}, R_{j}, \delta\left(R_{j}\right), \rho\left(R_{j}\right), \psi\left(R_{j}\right)\right)\)
                prime_update \(\left(S_{j}, \mathrm{H}_{\text {prime }}\right)\)
    return \(E S\)
```

Furthermore, KoE checks the distance constraint for the routes to be expanded to the doors of $v_{j}$, whose lower bound distance is computed as $\delta_{i}+\delta_{L B}\left(d_{k}, v_{j}, p_{t}\right)$ (line 11). Referring to Pruning Rule $3, \delta_{L B}\left(x_{s}, v_{i}, x_{t}\right)$ means the minimum indoor distance from $x_{s}$, through partition $v_{i}$, to $x_{t}$.
When $v_{j}$ becomes the next target partition to reach, KoE needs to find a route from the current door $d_{k}$ through a leavable door $d_{x}$ in current partition $v_{i}$ to an enterable door $d_{l}$ in the next partition $v_{j}$. For each such combination of $d_{k}$, $d_{x}$ and $d_{l}$, we may find a large number of qualified routes. However, the following lemma tells that we only need to consider the one with the shortest distance in the expansion.

Lemma 3. Given $R_{p}=\left(p_{s}, \ldots, d_{i}, d_{i+1}, \ldots, d_{j}, \ldots, p_{t}\right)$ as a prime route such that $d_{i}$ and $d_{j}$ refer to an enterable door of two consecutive key partitions $v_{m}$ and $v_{m+1} \in \operatorname{KP}\left(R_{p}\right)$, respectively, and $d_{i+1}$ refers to a leavable door of $v_{m} . R_{p}$ 's partial route $R_{p}^{\star}=\left(d_{i}, d_{i+1}, \ldots, d_{j}\right)$ must also be a prime route.

Proof. (Sketch) We prove it by contradiction. Suppose $R_{p}$ 's key partition sequence is $\left\langle v_{s}, \ldots, v_{e}\right\rangle$. We segment $R_{p}$ into three partial routes: $R_{p}^{\dashv}=\left(p_{s}, \ldots, d_{i}\right), R_{p}^{\star}=\left(d_{i}, d_{i+1}, \ldots, d_{j}\right)$, and $R_{p}^{\vdash}=\left(d_{j}, \ldots, p_{t}\right)$. Their key partition sequences are $\left\langle v_{s}, \ldots, v_{m-1}\right\rangle,\left\langle v_{m}\right\rangle,\left\langle v_{m+1}, v_{s}\right\rangle$, respectively. If $R_{p}^{\star}$ is not a prime route, there must be a route $R_{p}^{\star^{\prime}}$ having $\delta\left(R_{p}^{\star^{\prime}}\right)<\delta\left(R_{p}^{\star}\right)$ and $K P\left(R_{p}^{\star^{\prime}}\right)=K P\left(R_{p}^{\star}\right)=\left\langle v_{m}\right\rangle$. By concatenating $R_{p}^{-1}, R_{p}^{{ }^{\prime}}$, and $R_{p}^{\vdash}$, we get a route $R_{p}^{\prime}$ that has $K P\left(R_{p}^{\prime}\right)=K P\left(R_{p}\right)=\left\langle v_{s}, \ldots, v_{e}\right\rangle$ and $\delta\left(R_{p}^{\prime}\right)<\delta\left(R_{p}\right)$. Thus, $R_{p}$ is not a prime route.
Lemma 3 can be easily extended to the situation where global regularity needs to be considered for the whole route. Therefore, given any combination of $d_{k} \in P 2 D_{\sqsupset}\left(v_{i}\right), d_{x} \in$ $P 2 D_{\sqsubset}\left(v_{i}\right)$ and $d_{l} \in P 2 D_{\sqsupset}\left(v_{j}\right)$, we only need to find the shortest route $\left(d_{k}, d_{x}, \ldots, d_{l}\right)$ with a regularity check (lines $12-13$ in Algorithm 6). When each such route has been expanded to $d_{l}$, we generate a new route $R_{j}$ and check it based on Pruning Rule 1 and 4 (lines $14-18$ ). If those rules fail to prune
anything, we form a new stamp $S_{j}$ and call prime_update() (lines 19-20). When each candidate partition $v_{j}$ has been explored, KoE_find() returns the set $E S$ that contains all valid stamps. Recall that such stamps will be processed in the search framework (lines 13-14 in Algorithm 1) where the use of connect () is the same as that in the search of ToE.

## V. Experimental Studies

We experimentally evaluate $\mathrm{ToE}, \mathrm{KoE}$ and their variants. Table III lists all routing algorithms in comparison. Specifically, $\mathrm{ToE} \backslash \mathrm{D}$ and $\mathrm{KoE} \backslash \mathrm{D}$ involve no pruning rule based on the distance constraint $\Delta$, i.e., Pruning Rules 1,2 and 3. ToE $\backslash B$ and $\mathrm{KoE} \backslash \mathrm{B}$ skip the $k$ bound-based Pruning Rule 4. ToE $\backslash \mathrm{P}$ skips the prime-based Pruning Rule 5. This variant does not apply to KoE, since it is formulated based on prime routes. Instead, we design $\mathrm{KoE}^{*}$ that precomputes the shortest route between any two doors, which may speed up routing to the next key partition in KoE (line 13 in Algorithm 6). Note that such a route should be re-computed when the regularity check fails. All algorithms are implemented in Java and run on a PC with a 2.30 GHz Intel i5 CPU and 16 GB memory.

TABLE III: Notations of Comparable Methods

| Modification | ToE family | KoE family |
| :--- | :---: | :---: |
| - | ToE | KoE |
| no distance-based Pruning Rules 1-3 | ToE $\backslash \mathrm{D}$ | KoE $\backslash \mathrm{D}$ |
| no kbound-based Pruning Rule 4 | ToE $\backslash \mathrm{B}$ | KoE $\backslash \mathrm{B}$ |
| no prime-based Pruning Rule 5 | ToE $\backslash \mathrm{P}$ | - |
| with precomputed shortest routes | - | $\mathrm{KoE}^{*}$ |

## A. Results on Synthetic Data

1) Settings: Indoor Space. Based on a real-world floorplan ${ }^{5}$, we generate a multi-floor indoor space where each floor takes $1368 \mathrm{~m} \times 1368 \mathrm{~m}$ with 96 rooms, 4 hallways, and 4 staircases. The irregular hallways are decomposed into smaller but regular partitions. As a result, we obtain 141 partitions and 220 doors on each floor. We duplicate the floorplan $3,5,7$, or 9 times to simulate different indoor spaces. The four staircases of each two adjacent floors are connected by stairways, each being 20 m long. In the default setting, we use a 5 -floor indoor space with 705 partitions and 1100 doors.
Indoor Keywords. We assign keywords to the 96 rooms on each floor as follows. We use Scrapy ${ }^{6}$ to crawl the online shop information from five shopping malls ${ }^{7}$ in Hong Kong, obtaining 2074 documents for 1225 shop brands. All the 1225 brand names are used as i-words. They are then fed into the RAKE algorithm [15] to extract corresponding keywords from the documents. Only 1120 i-words yield extracted keywords. For each such i-word, we use up to 60 extracted keywords with the highest TF-IDF values as its t-words. In total, we have 9195 t -words and each i-word corresponds to 16.6 t words on average. We randomly assign an i-word and all its t-words to each room. The indoor space keyword mappings are of approximately 4 MB and thus kept in main memory.
[^4]Queries. For a valid $\operatorname{IKRQ}\left(p_{s}, p_{t}, \Delta, Q W, k\right)$, the distance constraint $\Delta$ must be larger than the indoor distance $\delta_{s 2 t}$ between $p_{s}$ and $p_{t}$. Thus, we generate $p_{s}, p_{t}$, and $\Delta$ in the following steps. 1) We fix $\delta_{s 2 t}$ to a certain value and randomly select a point $p_{s}$ in the space. 2) We find a door $d^{\prime}$ whose distance to $p_{s}$ approximates $\delta_{s 2 t}$ based on the precomputed door-to-door matrix. 3) We expand from $d^{\prime}$ to find a random point $p_{t}$ whose distance to $p_{s}$ just meets $\delta_{s 2 t}$. 4) We generate $\Delta=\eta \cdot \delta_{s 2 t}$, where $\eta>1$ is a coefficient. Subsequently, we randomly select a set of keywords from the 1120 i -words and 9195 t -words to form $Q W$. A parameter $\beta$ controls the fraction of i-words in $Q W$. The query keyword set size $|Q W|$ is varied from 1 to 5 , as an analysis [21] discloses that nearly all map queries contain at most 5 keywords, and statistics ${ }^{8}$ show that 65 percent of web searchers use 1 or 2 keywords and over 94 percent of web searchers use at most 4 keywords. In addition, we also vary the tradeoff parameter $\alpha$ in the ranking score (c.f. Equation 1) and the similarity threshold $\tau$ (see Definition 4). Table IV gives the parameter settings with default values shown in bold. It is noteworthy that users do not have to specify all of these parameters. For example, users do not need to give i-words and t-words separately. Rather, they are recognized automatically in our implementation.
Performance Metrics. We generate ten query instances with random $Q W$ s for each parameter setting. We run each instance five times, and measure the average running time and average memory cost per run of a single query instance.

| TABLE IV: Parameter Settings |  |
| :---: | :---: |
| Parameters | Settings |
| $k$ | $1, \ldots, \mathbf{7}, \ldots, 11$ |
| $\|Q W\|$ | $1,2,3, \mathbf{4}, 5$ |
| $\beta(\%$ of i-words in $Q W)$ | $20 \%, 40 \%, \mathbf{6 0 \%}, 80 \%, 100 \%$ |
| $\delta_{s 2 t}($ meter $)$ | $1100,1300, \mathbf{1 5 0 0}, \ldots, 2100$ |
| $\eta$ | $1.4, \mathbf{1 . 6}, 1.8,2.0$ |
| $\alpha$ | $0.1,0.3, \mathbf{0 . 5}, 0.7,0.9$ |
| $\tau$ | $0.05, \mathbf{0 . 1}, 0.2,0.4$ |

2) Efficiency Studies: Performance Overview. We run each algorithm in the default setting and report the running time per query instance in Fig. 4. Among all, ToE and KoE perform the best because they make full use of all pruning rules. In general, ToE returns top-7 results within 117 ms while KoE needs about 133 ms . For $\mathrm{ToE} \backslash \mathrm{D}$ and $\mathrm{KoE} \backslash \mathrm{D}$, the distance-based pruning has a greater impact on their efficiency. Next, $\mathrm{ToE} \backslash \mathrm{B}$ and $\mathrm{KoE} \backslash \mathrm{B}$ are basically equal to their original counterparts, showing that the kbound pruning barely works in the default setting. The effect of parameter $k$ is studied shortly in the next set of experiments. Still in Fig. 4, the KoEbased algorithms fluctuate more on different query instances than KoE-based ones. This is because the expansion of KoE is highly related to the query words, and thus is easily influenced by the randomly generated $Q W$ s. In contrast, ToE's expansion is relatively stable because it always finds the next door according to indoor topology rather than $Q W \mathrm{~s}$.
$\mathrm{KoE}^{*}$ is much slower than others and it has a wider range of variations. This indicates that its precomputing does not pay

[^5]off. On the contrary, it needs to recompute indoor distances when a route regularity check fails and the recomputed results cannot be reused in a dynamic routing process. Fig. 4 omits the results of $\mathrm{ToE} \backslash \mathrm{P}$ as it is five to six orders of magnitude slower than the others. $\mathrm{ToE} \backslash \mathrm{P}$ increases the number of routes exponentially due to its absence of prime route-based pruning. As $\mathrm{ToE} \backslash \mathrm{P}$ and $\mathrm{KoE}^{*}$ perform poorly, we omit them in further comparisons but discuss them separately in Sections V-A3 and V-A4, respectively.


Fig. 4: Default parameters


Fig. 5: Running time vs. $k$

Effect of $k$. We investigate the effect of $k$ by varying it from 1 to 11. Referring to Fig. 5, the running time of each algorithm increases only slightly as $k$ increases. Each KoE variant outperforms its ToE counterpart. Moreover, ToE $\backslash \mathrm{D}$ and $\mathrm{KoE} \backslash \mathrm{D}$ are much slower than ToE and KoE , which again demonstrates the power of the distance-based pruning. Consistent with the default parameter tests, the gap between $\mathrm{ToE} \backslash \mathrm{B}(\mathrm{KoE} \backslash \mathrm{B})$ and $\mathrm{ToE}(\mathrm{KoE})$ is insignificant. Sometimes $\mathrm{ToE} \backslash \mathrm{B}$ is even faster than ToE. When $|Q W|$ is at its default of 4, the overestimated keyword relevances of some partial routes tend to be higher than the final keyword relevance of routes already obtained, making the $k$ bound less useful to prune those partial routes. Considering the extra $k$ bound maintenance costs, ToE can be slower than $\mathrm{ToE} \backslash \mathrm{B}$. Nevertheless, both ToE and KoE return the top- 11 routes within 150 ms .
Effect of $|Q W|$. We vary $|Q W|$ from 1 to 5 and report the running time and memory costs in Fig. 6 and 7, respectively. For all algorithms, both metrics increase when $|Q W|$ is larger. Referring to Fig. 6, all KoE-based algorithms slow down more rapidly than ToE counterparts. When there are more query words, it is more difficult for partial routes to achieve full coverage of query words and connect to the terminal quickly. Therefore, both ToE and KoE are slower when $|Q W|$ increases. Moreover, a larger $|Q W|$ leads to more candidate partitions and thus more keyword combinations are considered in KoE. As a result, KoE's running time grows faster than ToE. When $|Q W|$ increases to 5 , the maximum query keyword size, each KoE-based variant incurs more time than its ToE counterpart. Nevertheless, KoE can still return the top-7 routes within 300ms. Referring to Fig. 7, KoE family cost less memory than ToE family as KoE expansions are more aggressive, jumping directly from one key partition to another without caching intermediate results, whereas KoE has the lowest memory cost thanks to its efficient route pruning.
Effect of $\eta$. Referring to Fig. 8, when increasing $\eta$ from 1.6 to 2 , both ToE and $\mathrm{ToE} \backslash \mathrm{B}$ 's running time increase steadily since the distance constraint is larger. In contrast, ToE $\backslash \mathrm{D}$ is insensitive to $\eta$ as it does not use any distance-related pruning. On the other hand, KoE family's time costs only slightly increase with $\eta$, showing that they can work well with
larger or looser distance constraints. Referring to Fig. 9, when increasing $\eta$, the memory costs of ToE family increase while those of KoE family stay stable, which again demonstrates KoE family's insensitiveness to the distance constraint.

Next, we concentrate on comparing ToE and KoE.
Effect of $\beta$. Referring to Fig. 10, both algorithms speed up clearly when increasing the i -word faction $\beta$. As each t word may relate to more partitions than each i-word in our setting, a larger $\beta$ tends to exclude more t -words and thus more candidate partitions. Therefore, both algorithms return the results faster for queries with more i-words. Still, ToE outperforms KoE and the gap enlarges rapidly when varying $\beta$ from $60 \%$ to $20 \%$. That is because the candidate i-word set will be large with more t -words, which more affects KoE.
Effect of floor number. We vary the floor number to test the scalability of our algorithms. Referring to Fig. 11, ToE's time cost increases slowly but KoE deteriorates very fast when there are more floors. The distance between adjacent floors in our dataset is set to 20 m only, which means the distance between two points separated by several floors is still very small. Consequently, the distance constraint can hardly help exclude the candidate partitions several floors away. Thus, both search algorithms need to consider more candidates. Nevertheless, ToE can still finish within 250 ms when there are 9 floors. As ToE keeps the intermediate results at each step, its running time increases slower than KoE for more floors.
Effect of $\delta_{s 2 t}$. We vary the route distance $\delta_{s 2 t}$ with $\eta$ fixed to 1.6. Referring to Fig. 12, both algorithms slow down sightly with $\delta_{s 2 t}$ increased to 1900 m . When $\delta_{s 2 t}$ is small, ToE that expands based on topology can quickly find enough routes and return. However, when $p_{s}$ and $p_{t}$ are separated further, ToE needs to expand more partitions and thus costs more time. In contrast, KoE finds the next valid stamp based on keywords and is less affected by the increase of $\delta_{s 2 t}$.
Effect of $\alpha$ and $\tau$. With varying $\alpha$, all algorithms perform steadily with minor fluctuations only. This implies that our ranking score is robust and insensitive to $\alpha$. The experiments with varying $\tau$ show that our search algorithms are also insensitive to $\tau$. The Jaccard similarity in our keyword relevance is rather long-tailed. Very few indirect matching i-words are retrieved even $\tau$ is tuned to 0.05 . Thus our search algorithms stay stable. Due to page limit, we omit the result figures.
Summary. In general, KoE has better scalability when some distance-related parameters (e.g., $\eta$ and $\delta_{s 2 t}$ ) are enlarged. Conversely, ToE is more efficient when there are more query words. In addition, KoE always has a lower memory cost.
3) Effect of Precomputing in KoE: With others in default, we run KoE and $\mathrm{KoE}^{*}$ at different $\eta$ values. Referring to Fig. 13, KoE always outperforms $\mathrm{KoE}^{*}$ except when $\eta$ is as small as 1.2. A smaller $\eta$ leads to a tighter distance constraint, and KoE tends to directly connect to $p_{t}$ with the shortest distance regardless of covering query words. In such a case, the precomputed shortest routes between key partitions are useful. However, once the distance constraint becomes larger, more routing choices are included and the precomputed results become useless. This leads to a lot of recomputations that clearly


Fig. 6: Time vs. $|Q W|$


Fig. 11: Time vs. floor


Fig. 16: Homogeneous rate


Fig. 7: Memory vs. $|Q W|$


Fig. 12: Time vs. $\delta_{s 2 t}$


Fig. 17: Time vs. $|Q W|$


Fig. 8: Time vs. $\eta$


Fig. 13: Time of KoE*


Fig. 18: Memory vs. $|Q W|$


Fig. 9: Memory vs. $\eta$


Fig. 14: Memory of KoE*


Fig. 19: Time vs. $\eta$


Fig. 10: Time vs. $\beta$


Fig. 15: Time of ToE $\backslash \mathrm{P}$


Fig. 20: Homogeneous rate
jeopardize KoE*'s efficiency. As shown in Fig. 14, $\mathrm{KoE}^{*}$ 's memory cost is an order of magnitude higher than that of KoE as it uses precomputing. In summary, we find that KoE's on-the-fly search nature yields much more performance gains in both time and memory costs than $\mathrm{KoE}^{*}$ 's precomputing.
4) Effect of Prime Route-based Pruning: We compare ToE to $\mathrm{ToE} \backslash \mathrm{P}$ that does not employ the prime route-based pruning. Referring to Fig. 15, when increasing $\eta$ from 1.4 to 2, $\mathrm{ToE} \backslash \mathrm{P}$ slows down almost exponentially whereas ToE stays stable. As $\mathrm{ToE} \backslash \mathrm{P}$ never checks and prunes those non-prime routes during the search, its candidate routes can be extremely large even when a small $\eta$ is used. When $\eta$ increases to 2 , $\operatorname{ToE} \backslash \mathrm{P}$ is three orders of magnitude slower than ToE.

Without the prime concept, ToE $\backslash \mathrm{P}$ tends to return homogeneous routes. We measure the homogeneous rate as the fraction of homogeneous routes in the returned top- $k$ routes. The results w.r.t. different $k$ values are reported in Fig. 16. With a larger $k$, ToE $\backslash \mathrm{P}$ 's top- $k$ routes become homogeneous at a rapid pace. For $k \geq 3$, more than $60 \%$ of returned routes are homogenous, and the percentage grows up $92 \%$ when $k$ is 15 . Such top- $k$ results are barely interesting to users. Since ToE $\backslash P$ also runs fast as shown in Fig. 15, it is of great importance to perform the prime route-based pruning in our search.
5) Search Result Quality: We use a typical example to show that our IKRQ can find more reasonable and desirable routes in practice. Referring to Fig. 1, we have I2T $($ Apple $)=\{$ phone, mac, laptop, watch $\}$ and I2T(Samsung $)$ $=\{$ phone, laptop, earphone $\}$. Assuming $\alpha$ is 0.5 and $\tau$ is 0.1 , query ( $p_{1}, p_{2}, 100$, earphone, 2 ) returns routes $R_{1}=$ ( $p_{1}, d_{4}, d_{15}, d_{15}, p_{2}$ ) and $R_{2}=\left(p_{1}, d_{4}, d_{17}, d_{17}, p_{2}\right)$, although earphone is not in Apple's t-words in $R_{1}$. In particular, $\delta\left(R_{1}\right)$ $=10 m, \delta\left(R_{2}\right)=20 m, \rho\left(R_{1}\right)=1.667$ and $\rho\left(R_{2}\right)=2$, so $\psi\left(R_{1}\right)$ $=0.867$ and $\psi\left(R_{2}\right)=0.9$. Although $R_{3}=\left(p_{1}, d_{4}, p_{2}\right)$ has a shorter distance of 9.5 m , it lacks words similar with earphone
and is not returned with $\psi\left(R_{3}\right)=0.4525$. Apparently, Apple offers earphones. Its route $R_{1}$ will be excluded and users will miss useful choices if we use exact keyword matching.

## B. Results on Real Data

We collect a dataset with real indoor topology and keyword distributions from a seven-floor, $2700 \mathrm{~m} \times 2000 \mathrm{~m}$ shopping mall in Hangzhou, China. There are ten staircases in which each stairway roughly 20 m long. Among all the 639 stores, those of the same category, e.g., cosmetics and men's wear, are on the same floor(s). We extract the keywords from the store descriptions on the mall's website and obtain 5036 twords for 533 i -words (stores). There are 103 stores with no t-words but only one i-word. An i-word corresponds to 31 t words maximum and 9.4 ones on average. We use the same parameter settings as in Table IV, except that $\alpha$ is adjusted to 0.7 to suit the needs of keyword-awareness in shopping. Like on the synthetic data, we still generate 10 query instances for each parameter setting, run each instance 5 times, and measure the average cost per run for each query instance.

First, we vary $|Q W|$. Referring to Fig. 17, all algorithms but $\mathrm{ToE} \backslash \mathrm{D}$ moderately incur more time with increasing $|Q W|$. Those without distance-based pruning worsen rapidly, e.g., ToE $\backslash \mathrm{D}$ cannot return within 1 second when $|Q W|$ exceeds 3. Consistent with the results in synthetic data, KoE worsens faster than ToE as $|Q W|$ increases, and it becomes less efficient when $|Q W|=5$. In the real mall, shops of the same category are spatially adjacent, resulting in a dense distribution of the candidate partitions that refer to the same query keyword. When distance constraint is certain, KoE needs to consider more partition combinations that complicate the search. In contrast, ToE always expands based on topology and is less affected. As shown in Fig. 18, the memory cost of each algorithm increases moderately with a larger $|Q W|$. However, KoE is always the most space-efficient one.

Also, we study the effect of $\eta$ on running time. Referring to Fig. 19, when $\eta$ increases, i.e., the distance constraint is looser or larger, ToE family needs to access more doors and thus takes more time to return. With looser distance constraints, KoE gradually approaches $\mathrm{KoE} \backslash \mathrm{D}$. In this case, all KoE algorithms tend to cover more query words, and therefore they become similar in processing candidate partitions. In general, ToE and KoE can always return the results less than 500 ms , showing they are both efficient in finding routes in real applications.

Fig. 20 reports $T o E \backslash P$ 's homogeneous rate in the real data. Without the use of prime routes, $\mathrm{ToE} \backslash \mathrm{P}$ always returns homogeneous routes, not to mention its high running time.

## VI. Related Work

Indoor Routing and Path Finding. Goetz and Zipf [5] define a routing graph for indoor environments with obstacles. Lu et al. [13] design an indoor space model that facilitates shortest path finding. To speed up distance-aware indoor path finding, Shao et al. [17] design VIP-tree that enables more aggressive pruning. VIP-tree also supports indoor trip planning based on neighbour expansion [18]. Li et al. [10] construct indoor possible paths based on probabilistic location samples of moving objects and search for the most popular indoor semantic regions using the constructed paths. Costa et al. [3] propose context-aware indoor-outdoor path recommendation that minimizes the outdoor exposure and path distance. Li et al. [8] design vision-based mobile indoor navigation that helps blind and visually impaired people walk indoors. In contrast to our IKRQ, these works do not consider indoor semantic keywords. A recent work [16] studies indoor keyword-aware skyline route query that considers the number of covered keywords and route distances, whereas our IKRQ does not count keywords but use prime routes to exclude routes through the same partitions. Also, unlike work [16], our setting allows a partition to have more than one keyword.
Outdoor Keyword-aware Routing. Given a source $s$, a destination $e$, and a category set $C$, the trip planning query [9] finds the shortest $s$-to-e path that covers at least one object from each category in $C$, whereas the optimal sequenced route query [19] finds the shortest path covering all categories in a total order. Partial order is considered elsewhere [11]. The multi-approximate-keyword routing query [23] changes the strict category coverage to an approximate matching using edit distances between a keyword and a location. The geographical route search [7] finds routes whose length is within a threshold and keyword-dependent scores are highest. The keywordaware optimal routing [1] considers keyword coverage, route score, and travel cost budget. The optimal route search [24] finds one route whose word coverage is maximum within a budget constraint. The clue-based route search [25] supports an order of keywords to cover, and requires that the network distance from one matched keyword to next is within a corresponding user-specified limit. However, all these works fall short for indoor topology considered in our IKRQ queries. Also, none of them distinguishes identity and content words that carry different semantics. Moreover, most works do not
consider routing diversity, and works [1], [7], [9], [23], [24] are approximate solutions.

## VII. Conclusion and Future Work

Given two indoor points $s$ and $t$, indoor top- $k$ keywordaware routing query (IKRQ) finds $k s$-to- $t$ routes that have optimal ranking scores integrating keyword relevance and spatial distance constraint. We propose prime routes to increase result diversity, devise data structures for computing route keyword relevances, and derive pruning rules to reduce search space. Further, we design two IKRQ search algorithms that expand differently in routing. Experiments demonstrate the efficiency of our proposals and the performance characteristics of them.

For future work, we can use a soft distance constraint to support approximate routing. With indoor mobility data, it is possible to incorporate route popularity into routing. Also, it is useful to consider special entities like lifts in routing.
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[^0]:    ${ }^{1}$ A time constraint $T$, e.g., 1.5 hours, can easily be converted to a distance constraint $\Delta=V_{\max } \cdot T$, where $V_{\max }$ is the maximum indoor walking speed.

[^1]:    ${ }^{2}$ A partition is a basic indoor region with clear boundaries. Examples are rooms, staircases, and booths.

[^2]:    ${ }^{3}$ In our routing, all expanding routes have the same head item, i.e., $p_{s}$.

[^3]:    ${ }^{4}$ Note that a global regularity check is required when connecting $R_{j}$ to $p_{t}$.

[^4]:    ${ }^{5}$ deviantart.com/mjponso/art/Floor-Plan-for-a-Shopping-Mall-86396406
    ${ }^{6}$ https://scrapy.org/
    ${ }^{7}$ Refer to https://longaspire.github.io/s/hkdata.html for the details.

[^5]:    ${ }^{8}$ http://www.keyworddiscovery.com/keyword-stats.html

