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*Published in:*

VISIGRAPP 2019 - Proceedings of the 14th International Joint Conference on Computer Vision, Imaging and Computer Graphics Theory and Applications

*DOI (link to publication from Publisher):*

[10.5220/0007444208840891](https://doi.org/10.5220/0007444208840891)

*Publication date:*

2019

*Document Version*

Early version, also known as pre-print

[Link to publication from Aalborg University](#)

*Citation for published version (APA):*

Nikolov, I. A., & Madsen, C. B. (2019). Performance Characterization of Absolute Scale Computation for 3D Structure from Motion Reconstruction. In A. Kerren, C. Hurter, & J. Braz (Eds.), *VISIGRAPP 2019 - Proceedings of the 14th International Joint Conference on Computer Vision, Imaging and Computer Graphics Theory and Applications* (Vol. 5, pp. 884-891). SCITEPRESS Digital Library. <https://doi.org/10.5220/0007444208840891>

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# Performance Characterization of Absolute Scale Computation for 3D Structure from Motion Reconstruction

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Keywords: scaling, 3D reconstruction, structure from motion (SfM), GPS, robustness

Abstract: Structure from Motion (SfM) 3D reconstruction of objects and environments has become a go-to process, when detailed digitization and visualization is needed in the energy and production industry, medicine, culture and media. A successful reconstruction must properly capture the 3D information and it must scale everything to the correct scale. SfM has an inherent ambivalence to the scale of the scanned objects, so additional data is needed. In this paper we propose a lightweight solution for computation of absolute scale of 3D reconstructions by using only a real-time kinematic (RTK) GPS, in comparison to other custom solutions, which require multiple sensor fusion. Additionally, our solution estimates the noise sensitivity of the calculated scale, depending on the precision of the positioning sensor. We first test our solution with synthetic data to find how the results depend on changes to the capturing setup. We then test our pipeline using real world data, against the built-in solutions used in two state-of-the-art reconstruction software. We show that our solution gives better results, than both state-of-the-art solutions.

## 1 INTRODUCTION

### 1.1 Object 3D Reconstruction

With the emergence of more and more powerful CPU and GPUs, SfM software solutions have become widespread and easier to use. This gives both more specialized industry, medicine and culture preservation users the possibility to quickly capture objects and environments. Due to the nature of SfM, to create a detailed reconstruction of both object and texture, users need only a camera and the software. This gives SfM solutions the edge, compared to other low-cost 3D reconstruction solutions, like the ones based on time-of-flight (Corti et al., 2016), structured light (Sarbolandi et al., 2015) or stereo cameras (Sarker et al., 2017). These solutions require appropriate hardware, together with the specialized software, which gives them a larger overhead, for users to get into. Examples of 3D reconstruction using these methods are extensively benchmarked by (Jamaluddin et al., 2017), (Schöning and Heidemann, 2016).

### 1.2 State of the Art

An important requirement for the state of the art SfM software is for it to be both versatile and robust.

This is especially true for images taken in environments with varying conditions and containing objects with different shapes and sizes. Many of the state of the art SfM solutions fall in the category of open-source software like OpenSfM (VisualSfM, 2011), COLMAP (Schonberger, 2016), etc. Other SfM solutions are developed as part of commercial products like ContextCapture (Bentley, 2016), PhotoScan (Agisoft, 2010) and RealityCapture (CapturingReality, 2016). All of these solutions contain a whole processing pipeline going from the input images to a dense point cloud and mesh. One drawback that SfM has, is the ambiguity of the scale of the reconstructed object. The 2D information extracted from images, does not allow determining of the absolute scale of the scanned object. For obtaining this essential information, additional information is needed from the user or from external sensors.

This is why the programs also contain different built-in solutions for scaling the final model. In most cases these solutions are either using markers or manual distance measurement. This works only when there is access to the reconstructed objects or surfaces. This means that they are unfeasible for scanning structures with drones or scanning hard to reach or dangerous places. Another method is using the GPS positions for finding the absolute scale of the

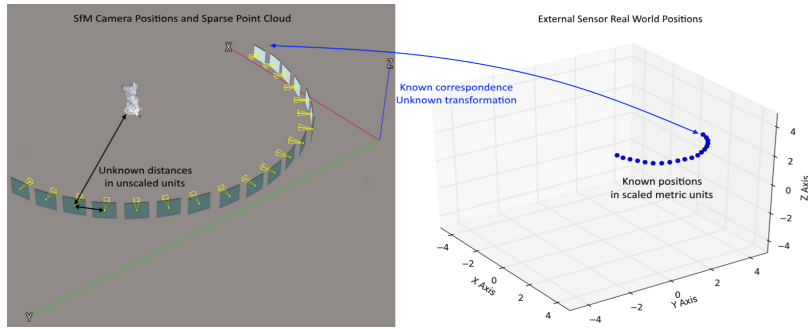


Figure 1: The two sets of corresponding points. On the left an output screen from 3D reconstruction program with the camera positions and a sparse point cloud, with unknown scale. On the right the same camera positions in a scaled real world metric units from an external sensor. Establishing the absolute scale of the reconstruction involves estimation the transformation, which will transfer the left set of points to the right.

object, but this way does not characterize the performance of the scaling and do not take into consideration external factors, which can influence the precision of the scaling.

### 1.3 Using External Sensor Data for Determining Scale and Noise Sensitivity

We propose a solution for determining the absolute scale for 3D SfM reconstructions using GPS positioning information, enhanced by RTK for a more precise estimation of the camera for each image taken. Others have proposed method for using GPS and RTK (Rabah et al., 2018), (Dugan, 2018) for georeferencing and enhancing the SfM reconstruction workflow, but they do not focus on the scale of the reconstructed objects. Our method is aimed at being used as part of a unmanned aerial vehicle (UAV) solution for scanning and 3D reconstruction of hard to reach surfaces and objects. It also works only with GPS data, in contrast with other methods using sensor fusion (Schöps et al., 2015). As the method is aimed for industrial and historical preservation use, not only is the absolute scale needed, but also calculating the uncertainty of said scale, as well as determining how capturing conditions and external factors might influence it. As an example, we show that when you have 3 captured horizontally spaced camera positions from the reconstruction process, a scaled distance of  $100mm$  on a reconstructed object can be with uncertainty of  $0.1mm$ . While the same scaled distance, when calculated from 18 captured horizontally spaced camera positions has uncertainty of  $0.007mm$ .

Our *main* contribution is this combination of estimating the absolute scale and its sensitivity to noise, which in the end gives both precise and robust results.

To test our approach, we first analyze the sensor

and determine its accuracy and precision. We then do a series of simulated test scenarios to get a baseline of the expected performance. Finally, we test the method in a real world testing scenario and compare results to the scaling results produced by the two 3D reconstruction programs - ContextCapture and PhotoScan. We demonstrate that our method gives better results than the state-of-the-art, while also providing a reliable uncertainty metric.

## 2 METHODOLOGY

### 2.1 SfM Pipeline

To understand the proposed workflow, the SfM pipeline needs to be first explored. SfM relies on information captured from multiple images around the scanned objects. Features are extracted from each image and matched. Normally algorithms like SIFT (Lowe, 2004), SURF (Bay et al., 2006) are used. From these matched points a sparse 3D point cloud can be triangulated using bundle adjustment (Triggs et al., 1999) and the camera positions can be back-projected. From these a dense point cloud and subsequent mesh can be created. The problem is that there is no information in 2D images alone on how big the scanned object is - is it a city or a model of a city? This is also reflected in the calculated camera positions.

### 2.2 Least-Squares Transformation Estimation

When capturing the images, the positions of the cameras can be saved in real world coordinates. The GPS-RTK can be directly positioned on the camera or on a drone carrying the camera. To calculate the real

world scale of the reconstruction, the transformation between the two sets of coordinates needs to be determined - the ones calculated by the SfM software and the ones given by the GPS-RTK. This is shown in Figure 1, where an output of SfM software is shown on the left side and the GPS-RTK points are shown on the right side.

Because there is clear a correspondence between the SfM camera positions and the GPS-RTK positions and the unknown transformation consists only of translation, rotation and uniform scaling, a simple least-squares estimation algorithm is considered. An implementation of the classical algorithm by (Umeyama, 1991) is chosen and customized for the needs of the paper. For the algorithm to work the two point sets need to have non-collinear points and no outliers.

We need to also take into consideration the problem of the lever-arm offset between the GPS antenna and the camera (Daakir et al., 2016). As an initial calibration step the real-world distance between the two is measured and used as an additional input for the Least-Squares estimation algorithm.

$$a_i = T(b_i), \quad a_i \in A, \quad b_i \in B \quad (1)$$

$$T = \begin{bmatrix} sR_{11} & sR_{12} & sR_{13} & t_1 + x_{off} \\ sR_{21} & sR_{22} & sR_{23} & t_2 + y_{off} \\ sR_{31} & sR_{32} & sR_{33} & t_3 + z_{off} \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (2)$$

If the two point sets are  $A = [a_1, a_2, \dots, a_m]$ , for the known one and  $B = [b_1, b_2, \dots, b_m]$  for the unknown one, where each set is comprised of  $m$  number of points and each point has a  $x, y, z$  components. Then the transformation matrix  $T$  between the two needs to be calculated, such that it satisfies Equation 1. To do that, the sum of squared errors  $e^2$  shown in Equation 3 from (Umeyama, 1991), needs to be minimized, where  $s$  is the scale,  $R$  is the rotation and  $t$  is the translation component of the transformation matrix (Equation 2). The real world offset between the two sensors is given as  $x_{off}, y_{off}, z_{off}$  inputs.

$$e^2(R, t, s) = \frac{1}{m} \sum_{i=1}^m \|a_i - (sRb_i + t)\|^2 \quad (3)$$

To test out the algorithm's results, a synthetic point set of 18 points is created. The number of points is chosen such that it coincides with the tests, performed later. A new set of points is then created, by giving the point set, a random translation, rotation and scaling. The two sets are used in the least-square estimation algorithm. The result estimated transformation matrix is exactly the same as the one introduced

to the ground points to create the unknown ones. This is seen in Figure 2, where the estimated transformation matrix is used on the Utah teapot, to transform it to the coordinate's initial position, together with the unknown positions.

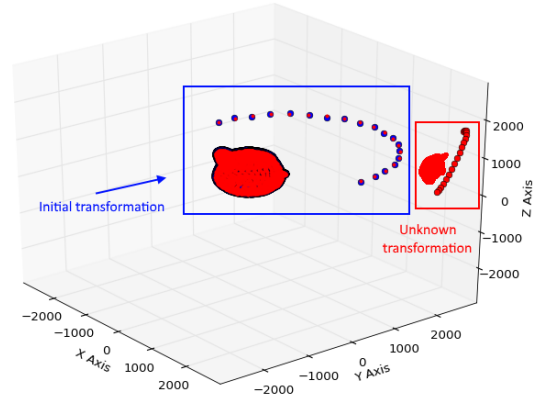


Figure 2: Visualization of the output of the least-squares transformation estimation algorithm. The initial position, orientation and scale are first transformed to "unknown" ones. The estimation algorithm is then used to find the transformation from the "unknown" one to the initial one. The Utah teapot is added for easier visualization

In the real world this is not the case, as measuring equipment is always a subject to additive noise. This needs to be taken into consideration, when using the least-squares estimation algorithm. This will transform Equation 3, where  $C = A + N$ , with  $A$  being the known locations and  $N = [n_1, n_2, \dots, n_m]$  is the added noise component, with each noise  $n_i = [n_x, n_y, n_z]^T$ . The next subsections will verify the sensor readings and model the noise.

### 2.3 Verifying Sensor Readings

For the paper the sensor provided by DJI (DJI, 2017) is used, as it has a very small margin of uncertainty in the positioning information - less than 0.02m in horizontal direction and 0.03m vertically, in good weather conditions. This precision needs to be verified, before using it. Because the sensor works only when attached to a drone controller, the whole platform is used for the test. The sensor is started and its readings are saved each second for a period of 5 minutes. The readings are taken when the whole platform is on the ground, to eliminate inconsistencies from the readings when the platform is in motion. The sensor is then manually moved to another location and the readings are again taken. The calculated position standard deviation for the first point is 0.0175m in horizontal direction and 0.0244m in height and for the

second point the standard deviations are  $0.0174m$  and  $0.0251m$  respectively. The values are thus in the interval given in the documentation by DJI. With the real world positioning uncertainty verified, the next step is to create a number of synthetic testing scenarios, where the uncertainty is used as a noise component. These scenarios are used to investigate aspects of how the GPS-RTK noise influences scale noise.

## 2.4 Synthetic Testing Scenarios

For the synthetic tests to be as close to a real world test, the point sets are setup as real SfM capturing positions. The tests are designed to determine the amount of camera positions needed and the amount of vertical camera bands. To gather enough variation in the calculated scale after the noise input in each of the tests, the least-squares estimation step is done a number of times, each time with a different sampling of noise input.

### 2.4.1 Number and sampling of image positions

The first synthetic test scenario looks at how the number of input camera positions affects the results of the scale factor. The least-squares estimation method requires at least two positions for estimation of the transformation. In the paper by (Nikolov and Madsen, 2016), a circular pattern of images is used, with the position of each image, changing by 20 degrees. This gave 18 images per circular pattern. For a simpler and easier image capture for the real world test scenarios described in the later sections, the circular pattern is changed to a semi-circular one, leaving the number of image positions to 18 again, giving a 10 degree separation between them. This gives the final testing interval - 3 to 18 positions. The minimum number of positions is set to 3, as at least 3 points are needed to estimate the 3D transformation. To test this we start with the full number of 18 positions going from 0 to 180 degrees. Then every time we lower the number of positions we do not just remove the last one, but we resample the left ones so they always cover the whole interval of 0 to 180 degrees, but have larger distance between them.

The synthetic test is done once without resampling, starting with 18 positions and removing positions, until only the first two are left. The second run of the test is done with removing and resampling the positions until only the 0 and 180 degree ones are left.

To model the positioning noise for each instance, a random sampling of the uncertainty values captured directly from the GPS-RTK. This of course introduces the problem that not enough data has been captured

for a more diverse modeling of the uncertainty. We will address this in the next subsection.

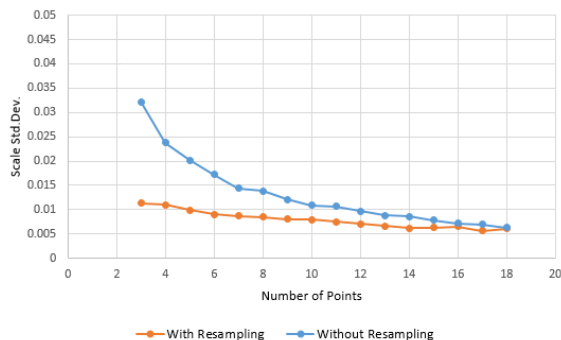


Figure 3: Results from the resampling versus no resampling synthetic test. Resampling the captured positions so the first and last one are always at 0 and 180 degrees, after removing positioning information drastically lowers the standard deviation of the calculated scale

The obtained results are shown in Figure 3. When resampling the positions, as points are removed the additional separation between points helps with lowering the calculated scale's error. This is especially evident up until 10 image positions. After that the two methods have comparable result standard deviations, which converge at 16 image positions. This shows that if not all image positions can be captured, it is better that the captured ones have maximum separation. In addition, the standard deviation settles at around 12 or 13 image positions.

### 2.4.2 Number of vertical bands

The second test scenario is designed to check how many vertical bands of images and image positions are needed. The previous test showed that worse scale uncertainty is achieved when no resampling of the points is present. This test will explore if better scale uncertainty can be achieved with more vertical separation between the positions, if no resampling is used. The work of (Nikolov and Madsen, 2016), shows that three bands of photos give the best possible reconstruction results. The paper however manually scales the output meshes, so no conclusions are given on how the scaling is affected by the bands. To test this we choose to test with one, two and three position bands respectively. This will determine if the additional spatial change between the positions in different bands, given to the least-squares estimator, will make a difference to the calculated scale factor.

The synthetic test is started with one band of vertical separation and 18 camera positions. The number of positions is reduced by one for each test until only 3 positions are left. The same is done for two and

Table 1: Change in the scale standard deviation when going from 1 to 2 bands and from 2 to 3 bands for the minimum and maximum number of tested point positions. The change from 2 to 3 bands is almost twice as small showing that the gained accuracy, is not enough to offset the larger amount of data, longer capturing time, etc.

Points	Difference	
	1 and 2 bands (%)	2 and 3 bands (%)
2	43.75	14.60
18	11.26	27.51

three vertical band tests. The estimated scale factor is calculated from each and standard deviation is calculated from all the possible results. The results are given in Figure 4.

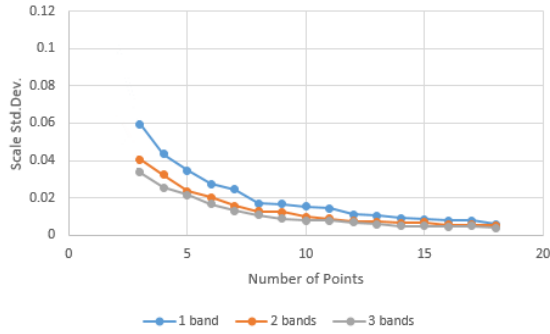


Figure 4: Results from capturing of positioning data from different number of vertical bands. More vertical bands help with the uncertainty of the scale. Both the larger number of points and the additional spatial information help with that.

As expected, the high standard deviation decreases as we introduce additional vertical positions in the form of more bands. This is both because of the larger number of points and additional vertical separation. If we look at the difference between the standard deviations of the calculated average scale we can see a relation between the number of bands and number of points. The data is given in Table 1. When more points are present in each band the gains won by going from one to two bands are not big, but if multiple bands need to be taken, then it will be much better to capture three. When less points are present in each band it is necessary to have as much bands as possible, so the benefits from the additional number of points and separation can be felt. To strike a balance between number of bands captured and scale precision gains, we choose to use two bands for the real world testing scenario for testing against the state of the art.

## 2.5 Covariance Propagating of Positioning Noise

The way the noise is introduced in these synthetic tests and the performance characterization of the scale calculation is found, can be cumbersome, as the test needs to be done a large number of times. A better solution to this is using covariance propagation (Haralick, 2000) of the noise. This will give the relation between the uncertainty in each GPS-RTK position and the uncertainty in the final calculated scale. The idea has been shown to give good results (Madsen, 1997), as long as there are independent input parameters, which are used in a function - no matter analytically or iteratively found, to calculate a set of output parameters. As each captured GPS-RTK position is used in the calculation of the scale factor through the least-square estimation, this means that we can express the transformation calculation as represented as  $s = f(C)$ , where  $s$  is the estimated scale and  $C$  is the GPS-RTK positioning set together with the introduced noise. We do not use the second positioning set  $B$  obtained from the SfM reconstruction, as an input parameter, as it is treated as a constant. We use the method demonstrated in (Madsen, 1997), for determining the covariance matrix of the input parameters. This of course need to be done for each of the three dimensions for each of the points. The standard deviation of the calculated scale will depend both on the standard deviation of the uncertainty of the measured GPS-RTK positions and the first derivative of the function. To find the standard deviation of the scale, the first order approximation needs to be done to the covariance matrix, as seen in Equation 4 and then used together with the dependence of the scale to the positions in all 3 dimensions, as given in Equation 5. Where  $\Delta$  is the covariance matrix of  $Q$  and is described as Equation 6, for each of its dimensions. Thus  $Q$  is a combined vector containing all the dimensional data for each position  $Q = [x_1, y_1, z_1, \dots, x_m, y_m, z_m]^{1 \times 3m}$

$$\Delta = \begin{bmatrix} \sigma_{x_1}^2 & 0 & 0 & \dots & 0 \\ 0 & \sigma_{y_1}^2 & 0 & \dots & 0 \\ 0 & 0 & \sigma_{z_1}^2 & \dots & 0 \\ \dots & \dots & \dots & \dots & \dots \\ 0 & \dots & \sigma_{x_m}^2 & 0 & 0 \\ 0 & \dots & 0 & \sigma_{y_m}^2 & 0 \\ 0 & \dots & 0 & 0 & \sigma_{z_m}^2 \end{bmatrix}_{3m \times 3m} \quad (4)$$

$$\sigma_s^2 = \frac{\partial s}{\partial Q} \Delta \frac{\partial s^T}{\partial Q} \quad (5)$$

$$\frac{\partial s}{\partial Q} = \left[ \frac{\partial s}{\partial x_1} \frac{\partial s}{\partial y_1} \frac{\partial s}{\partial z_1} \dots \frac{\partial s}{\partial x_i} \frac{\partial s}{\partial y_m} \frac{\partial s}{\partial z_m} \right] \quad (6)$$

To test if the iterative approach and the covariance propagation approach will yield the same results. Again the testing scenario of subsection 2.4.1 is used, both with and without resampled positioning data. The results can be seen in Figure 5. The two approaches achieve closely matched results for both positioning data types. The average difference between the calculated scale standard deviation from 3 to 18 points between the two approaches, without resampling positioning data is 12.07%, while with resampling the difference falls to 4.88%. In addition the covariance propagation approach follows a smoother overall curve of progression, meaning less chance for random noise in the estimated scale standard deviation. This also demonstrates that the covariance propagation method gives very accurate estimation of the standard deviation of the scale, while bypassing the assumptions about the nature of the uncertainty's distribution.

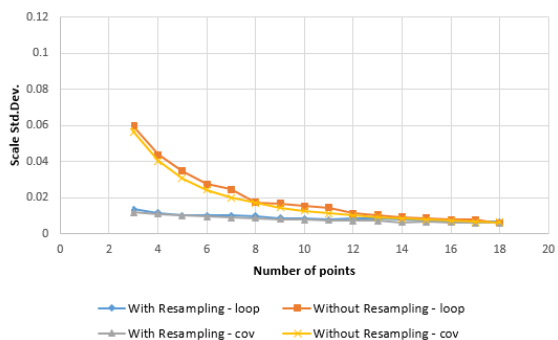


Figure 5: Comparing the iterations approach to the covariance propagation approach for calculating scale uncertainty from position uncertainty. The comparison is made for different number of input positions and a different way of resampling the positions

### 3 REAL WORLD TESTING

Two objects are chosen for the test. They can be seen in Figure 6. The objects are chosen because they represent two different 3D reconstruction use cases - the statue represents a digital heritage use case, while the wind turbine blade represents an industrial use case. Both cases require precise scale estimation.

For each of the two objects, two vertical bands of 18 images are taken in a semi-circle. The horizontal separation between the images is 10 degrees, while the vertical separation between bands is 20 degrees. The images are taken with a Canon 5Ds at maximum resolution 8688x5792. This camera is chosen, so enough information is captured from the objects and the chance of the 3D reconstruction failing



(a) Angel Statue (b) Blade Segment

Figure 6: Two test objects used for 3D reconstruction. Each represent different reconstruction challenges and reconstruction cases

or having errors is minimized.

The camera positions are manually determined with a laser range finder. This is done so that any possible random positioning accuracy fluctuations on the GPS-RTK, caused by weather conditions, pressure changes or environment effects are removed. A second reason for this is that this way the experiment can be done in an indoor environment, removing the possible illumination changes that can affect the final reconstruction.

For the reconstruction both PhotoScan and ContextCapture software is used. The two solutions have a number of built-in ways to scale a model - using point markers that the user directly adds to the model and have been measured beforehand, printing marker trackers and putting them around the scanned object and detecting them in the images, adding coordinates to the camera positions from GPS. For testing our proposed solution, we have chosen the method that is most relevant - adding camera positions, together with the images and using them to scale the object.

Because the built-in solutions do not have a measurement of the uncertainty of the scaling, the comparison will be done only on the basis of the calculated scaling factors. For comparing the calculated scale factors, the reconstructed objects will be scaled using these factors and the distance will be measured manually on the real world object and the scaled reconstruction.

As there are no ground truth scaled model to compare the scales from the three methods, a manual measuring of the objects is chosen. A number of parts of the two real world objects are measured with a caliper, which has a resolution of  $\pm 0.02mm$ , when measuring objects below 100mm. The reconstructed and scaled model are imported into CloudCompare (Girardeau-Montaut, 2003) for measuring the same parts. By measuring multiple parts of the models and averaging

the difference between the real world measurement and the scaled model measurement, the effects of the possible human errors, while manually measuring are minimized.

The obtained scaled models are given in Figure 6. Just by looking at the models, no observable difference can be seen. Table 2 contains the average measured distance errors from measuring ten different parts in the real world and on the reconstructed objects, as well as the standard deviation from the measurements. The results show that our proposed solution gives better results, because the mean error distance is the lowest compared to the other. Even if we factor in the manual repeated measurement error, shown as the standard deviation of the distance in the table, the results obtained by our method are better or the same as the build in solutions.

Table 2: Average distance error between measurements from the real world object and the reconstructed model, for the two tested objects - angel (A) and blade (B). The results are in *mm* and the comparison is made between our proposed solution (Paper) and the built-in scaling solutions in ContextCapture (CC) and PhotoScan (PS)

	Paper (mm)	CC (mm)	PS (mm)
A	<b>0.35 ± 0.063</b>	0.48 ± 0.069	1.04 ± 0.093
B	<b>0.18 ± 0.012</b>	0.23 ± 0.008	0.56 ± 0.009

$$\sigma_{metric}^2 = D_{SfM}^2 \cdot \sigma_s^2 \quad (7)$$

Furthermore the scale uncertainty in *mm* can be also easily measured through our proposed solution. We can take two random points from the unscaled measured object and calculate the Euclidean distance between them in unknown units -  $D_{SfM}$ . As we have calculated the scale uncertainty, denoted as  $\sigma_s$ , we can use Equation 7 as given in the book by (DeGroot and Schervish, 2012), to calculate scaled distance uncertainty  $\sigma_{metric}^2$  in the chosen metric. To demonstrate how this uncertainty can be useful, we recalculate the real world reconstruction's scale uncertainty, by using different number of position data - from 2 to 18. Each uncertainty is then used to find the metric uncertainty of the distance between the same two randomly chosen points. The results from the test can be seen in Figure 8. The calculated metric uncertainty decreases with the introduction of more and more point positions.

## 4 CONCLUSION AND FUTURE WORK

In our paper we presented a pipeline for computing the absolute scale of a 3D model reconstructed

using SfM. Our method relies on using external positioning information from a GPS-RTK sensor, which has an inherent uncertainty present in the provided data. We provide an analysis of this uncertainty and how it propagates to the calculated absolute scale and results in a scale uncertainty. Through a series of tests we demonstrated how changes to the number of positions used and their spatial relationship can also influence the scale uncertainty. We tested two ways to find the scale uncertainty - an iterative method and a mathematical covariance propagation of noise method.

Finally, we tested our proposed pipeline against the scaling solutions available in state of the art SfM software solutions - ContextCapture and PhotoScan. We demonstrate that we achieve better results, on top of providing more information about the scaling uncertainty.

As an extension to the current paper, we propose testing the pipeline using data captured through drone flights. This way the GPS-RTK positioning information can be tested in different weather and environment conditions. Additionally the testing on objects with different sizes will provide data on how the method scales with size and if the uncertainty depends on the size of the scanned object. Finally, different positioning systems would also be tested and modeled - both indoor and outdoor, to make the pipeline more versatile.

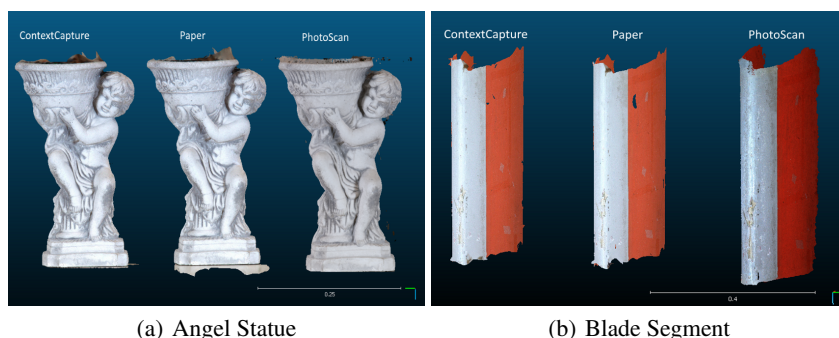
## ACKNOWLEDGEMENTS

This work is funded by the LER project no. EUDP 2015-I under the Danish national EUDP programme. This funding is gratefully acknowledged.

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(a) Angel Statue

(b) Blade Segment

Figure 7: Reconstructed and scaled model. The ContextCapture and PhotoScan reconstructions are scaled using the built-in solutions in the software. For our proposed solution(Paper), the unscaled ContextCapture reconstruction is used as basis. The brightness difference in the models is due to the different ways the programs normalize the texture color. In addition the model from PhotoScan reconstructed a larger portion of the blade and looks larger even though the scale is comparable.

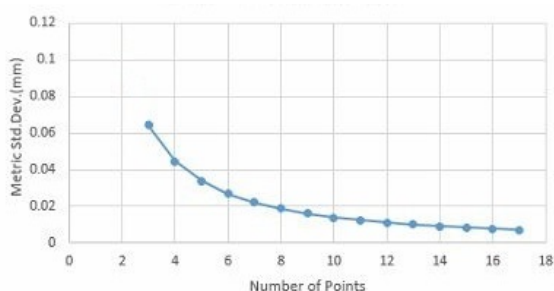


Figure 8: Correlation between the number of positions used to calculate the scale uncertainty and the metric uncertainty when measuring the real world distance between two points on a object

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