

Kinematic characteristics of hollow ball under different braking conditions

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Received 9 November 2017; accepted 16 November 2017

DOI <https://doi.org/10.21595/vp.2017.19391>



Abstract. The purpose of this article is to evaluate smart fluids influence on braking properties for spherical piezo actuator and to determine the functions for rheological experimental graphs of chosen smart fluids. Braking action and motion are modeled using numerical method, which can also be called a stepped approximation. It can be done using Excel program, which can be found in typical Microsoft Office suite.

Keywords: braking characteristics, electrorheological fluid (ERF), magnetorheological fluid (MRF), approximation.

1. Introduction

The piezoelectric actuator is an extraordinary device that is capable to ensure high displacement accuracy, short response time and high force generation [1]. This actuator has very wide application region such as an ultra-precision component machining, tunable optical devices, biomedicine, robotics and so on [1-3]. In order to keep a high precision displacement resolution, a position sensor should be used. This enables us to evaluate and correct a displacement error [3]. Smart fluids (ERF and MRF) can be used to shorten the braking time and path of movable link [4].

2. Experimental data

The structural scheme of theoretical model is created using real experimental model (Fig. 1). A hollow ball (No. 1) in theoretical model (Fig. 2) is considered as a full-standard, despite that a hollow ball in experimental model is cut. Its outside radius is 30 mm, wall thickness 1.5 mm and it is made of steel. According to that, the full ball moment of inertia I (Eq. (1)) is equal to $73 \cdot 10^{-6} \text{ kg} \cdot \text{m}^2$. The inside radius of piezo tube (No. 3) is 19.5 mm. The surface of the ball after a contact with a smart fluid (No. 4) becomes greasy. A sliding friction coefficient goes down, if the greasy surface comes over the zone of 3 contact points (No. 2). These points are made of epoxy resin that are located at 120° angle distance about tube longitudinal axis. Seeking to prevent from the coefficient reduction, the angular displacement of the ball must be constrained and the radius R of the contact zone with a smart fluid has to be small enough. The horizontal projection of concave electrode (No. 5) is circle, which radius is 7.5 mm:

$$I = 0,4(R_1)^2 \cdot \frac{4}{3} \pi (R_1)^3 \rho - 0,4(R_1 - t_1)^2 \cdot \frac{4}{3} \pi (R_1 - t_1)^3 \rho, \quad (1)$$

$$A = \pi R^2, \quad (2)$$

$$\gamma_0 = \omega_0 \cdot \frac{R_1}{t}, \quad (3)$$

where R_1 – the outside radius of the ball; t_1 – the wall thickness of the ball; ρ – the density of steel, which is 7850 kg/m^3 ; R – the radius of electrode horizontal projection; t – the layer thickness of smart fluid, which is 0.5 mm.

The concave surface of the electrode is considered as flat, which contact area A (Eq. (2)) is $1.77 \cdot 10^{-4} \text{ m}^2$. These initial angular speeds of the ball ω_0 are: 0.2; 0.6 and 1 rad/s. According to this, the initial shear rates of smart fluid γ_0 (Eq. (3)) are: 12, 36 and 60 s^{-1} .

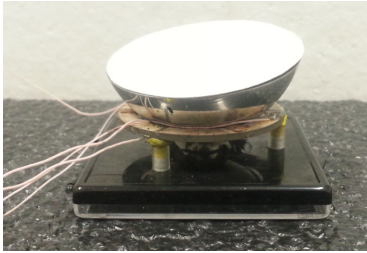


Fig. 1. Experimental model

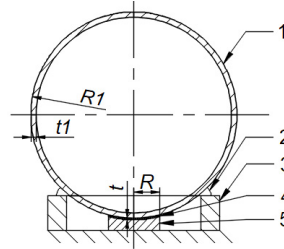


Fig. 2. The structural scheme of theoretical model

3. Determination of ERF theoretical characteristics

To model the braking process electrorheological fluid LID 3354 s is chosen, which experimental and functional graphs are shown in Figs. 3 and 4 [5, 6]. Despite that a linear function is recommended to use for the dependence of ERF yield stress τ_Y versus electric field strength [5], but a quadratic function (Eq. (4)) is chosen in order to get similar forms of the graphs. A sample function of second degree (Eq. (5)) is used to approximate experimental dependence of ERF viscosity μ versus electric field strength [5]. ERF viscosity value is considered to be permanent, when speed gradient changes:

$$\tau_Y(E) = 0,4 \cdot E^2 + 0,45 \cdot E, \tag{4}$$

$$\mu(E) = \mu_0 - C_\mu \cdot E^2 = 0,11 - 2 \cdot 10^{-8} \cdot (10^3 \cdot E)^2, \tag{5}$$

$$T(E) = 2/E, \tag{6}$$

where E – electric field strength; μ_0 – initial ERF viscosity, when E is equal to 0; C_μ – the constant of ERF viscosity function; T – the response time of smart fluid.

The average speed of ERF polarized particles is going up, until anisotropic structural block is created, when electric field strength is rising. This means, that the response time T changes in accordance to E , when the layer thickness of the fluid is constant [5]. A parabolic function (Eq. (6)) is chosen to model the mentioned dependence (Fig. 5). Despite that, the nominal value of exterior electric field strength can be reached almost instantly, but in theoretical model is considered that the field strength is changing linearly till nominal value is reached over response time period.

GER fluid, which performance is explained by giant electrorheological effect, can be used in order to get higher values of yield stress [7].

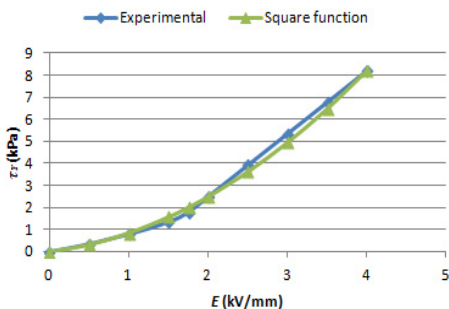


Fig. 3. ERF yield stress graphs

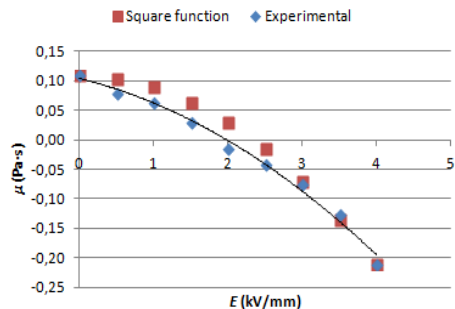


Fig. 4. ERF viscosity graphs

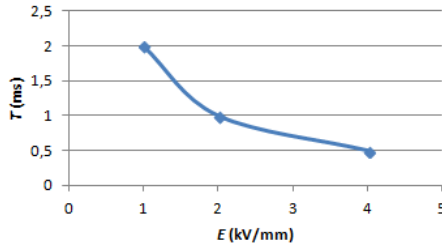


Fig. 5. ERF response time graph

4. Determination of MRF theoretical characteristics

To model the braking process magnetorheological fluid 140CG is chosen. After the investigation of theoretical shear models [8] and MRF viscosity characteristic (Fig. 6) [9], Bingham model is selected. MRF shear because of viscosity τ_μ (Eq. 7) doesn't depend on the strength of magnetic field and almost linearly depends on shear rate. This means, that MRF viscosity value can be assumed as a constant.

MRF yield stress τ_Y is depended on the strength of magnetic field, which experimental graph (Fig. 7) is approximated with quadratic function (Eq. (8)). Using the newest references about MRF [10] the dependence of response time versus magnetic field strength is created using parabolic function (Eq. (9)):

$$\tau_\mu(\gamma) = 0,02 + 0,0005 \cdot \gamma, \quad (7)$$

$$\tau_Y(H) = -0,0012 \cdot H^2 + 0,55 \cdot H, \quad (8)$$

$$T(H) = 500/H, \quad (9)$$

where H – magnetic field strength.

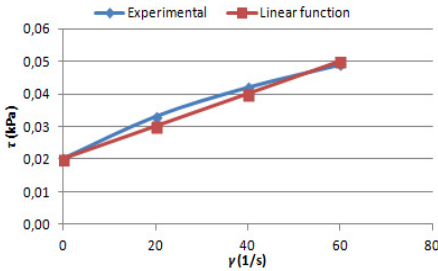


Fig. 6. MRF shear graphs because of viscosity

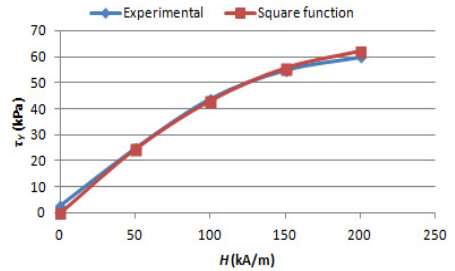


Fig. 7. MRF yield stress graphs

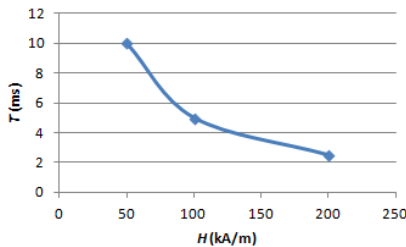


Fig. 8. MRF response time graph

5. Functional model of the stepped approximation

The equivalent shear stress τ of smart fluid is evaluated using an Eq. (10). The initial kinetic energy $E_{K,pr}$ of the ball is determined using an Eq. (11). The dependence of the friction coefficient

f versus a sliding speed is evaluated in Eq. (12). The negative work because of friction A_F is determined in Eq. (13) and negative work because of fluid shear A_R – in Eq. (14). The final value of ball kinetic energy E_K can be found using an Eq. (15). The model of the braking process is consisted of many time periods, when variable physical properties are recounted. The evaluation of the braking process is finished when the final value of the kinetic energy is equal to 0 Eq. (16). The total negative work after one time period shouldn't be bigger than 10 % of the initial kinetic energy in order to get quite accurate results of the stepped approximation. The estimation of important kinematic properties is presented in Eqs. (17-20):

$$\tau = \tau_Y + \tau_\mu = \tau_Y + \mu\gamma, \tag{10}$$

$$E_{K,pr} = I \frac{\omega_0^2}{2}, \tag{11}$$

$$f = f_0 - 2,5 \cdot 10^{-3} \omega R_1, \tag{12}$$

$$A_F = Nf\omega R_1 \Delta t, \tag{13}$$

$$A_R = \tau A \omega R_1 \Delta t, \tag{14}$$

$$E_K = E_{K,pr} - \sum A_F - \sum A_R, \tag{15}$$

$$E_K = 0, \tag{16}$$

$$\Delta s(t) = \Delta s(t - \Delta t \rightarrow t) = \omega(t - \Delta t) R_1 \Delta t, \tag{17}$$

$$s(t) = \sum_0^t \Delta s, \tag{18}$$

$$v(t) = v(t \rightarrow t + \Delta t) = R_1 \sqrt{\frac{2E_K(t)}{I}}, \tag{19}$$

$$a(t) = a(t - \Delta t \rightarrow t) = \frac{v(t) - v(t - \Delta t)}{\Delta t}, \tag{20}$$

where f_0 – a sliding friction coefficient, when the sliding speed is infinitesimal, which value is 0.3 [11]; N – the normal force in the friction zone, which is considered as permanent and equal to 1 N; Δt – a time period; $\Delta s(t)$ – a braking distance at the time period $t - \Delta t \rightarrow t$; $s(t)$ – a total braking distance till a time moment t ; $v(t)$ – a braking velocity at the time period $t \rightarrow t + \Delta t$; $a(t)$ – a braking acceleration at the time period $t - \Delta t \rightarrow t$.

6. Results

The essential properties of braking results using the chosen smart fluids are presented in Tables 1 and 2.

Table 1. The ball braking using ERF

ω_0 (rad/s)	0.2			0.6			1		
E (kV/mm)	0	2	4	0	2	4	0	2	4
Braking time (μ s)	1546	985	523	4911	2282	1059	8713	3646	1609
Braking distance (μ m)	5.04	3.67	2.18	48.79	25.31	12.51	146.96	65.73	30.25

Table 2. The ball braking using MRF

ω_0 (rad/s)	0.2			0.6			1		
H (kA/m)	0	100	200	0	100	200	0	100	200
Braking time (μ s)	1528	554	312	4827	1066	577	8517	1430	766
Braking distance (μ m)	4.97	2.16	1.26	47.85	12.97	7.15	143.20	29.41	15.91

The graphs of the ball sliding distance, velocity and acceleration are shown (Fig. 9-14) when electrorheological fluid LID 3354 s ($\omega_0 = 0.6$ rad/s and $E = 2$ kV/mm) and magnetorheological

fluid 140CG ($\omega_0 = 0.6 \text{ rad/s}$ and $H = 100 \text{ kA/m}$) are used.

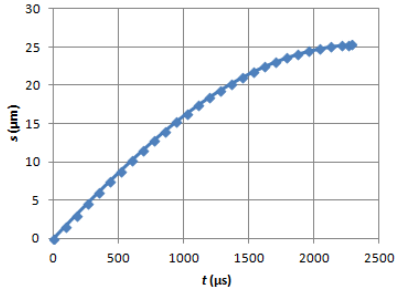


Fig. 9. Braking path graph using ERF

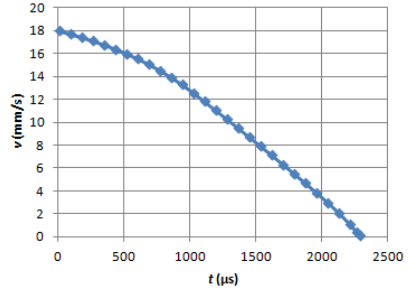


Fig. 10. Braking velocity graph using ERF

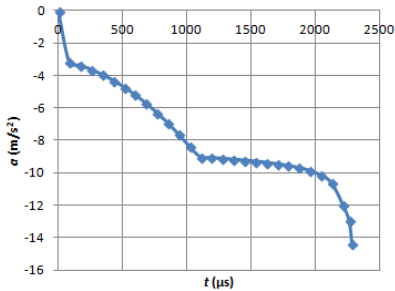


Fig. 11. Braking acceleration graph using ERF

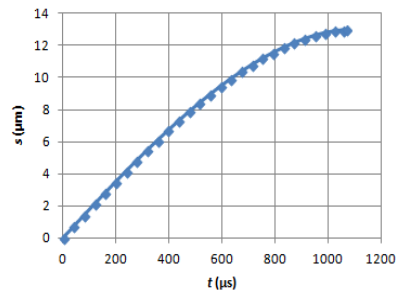


Fig. 12. Braking path graph using MRF

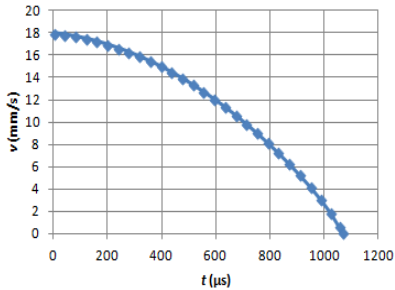


Fig. 13. Braking velocity graph using MRF

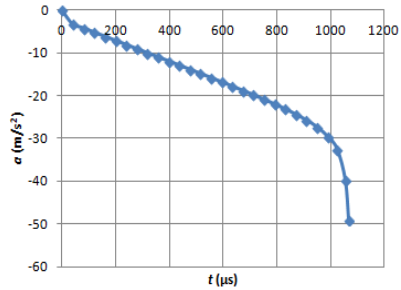


Fig. 14. Braking acceleration graph using MRF

7. Conclusions

The braking times are very similar to the response times of LID 3354 s, when an initial angular speed of the ball is the lowest, according to the table 1 data. When the speeds of the ball are greater, then the braking times are several times longer than the appropriate response times. The braking times and distances differs approximately from 3 ($\omega_0 = 0.2 \text{ rad/s}$) to 5 ($\omega_0 = 1 \text{ rad/s}$) times when the strength value of electric field varies from the lowest to the highest.

The braking times using MRF don't reach the appropriate response times, according to the Table 2. The braking times and distances differs approximately from 5 ($\omega_0 = 0.2 \text{ rad/s}$) to 10 ($\omega_0 = 1 \text{ rad/s}$) times when the strength value of magnetic field varies from the lowest to the highest.

Acknowledgement

The work was supported by the Research Council of Lithuania under the Project SmartTrunk, No. MIP-084/2015.

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