

1 The gravitationally consistent sea-level fingerprint of
2 future terrestrial ice loss

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6 We solve the sea-level equation to investigate the pattern of the gravita-
7 tionally self-consistent sea-level variations (fingerprints) corresponding to
8 modeled scenarios of future terrestrial ice melt. These were obtained from
9 separate ice dynamics and surface mass balance models for the Greenland
10 and Antarctic ice sheets and by a regionalized mass balance model for glaciers
11 and ice caps. For our mid-range scenario, the ice melt component of total
12 sea-level change attains its largest amplitude in the equatorial oceans, where
13 we predict a cumulative sea-level rise of ~ 25 cm and rates of change close
14 to 3 mm/yr from ice melt alone by 2100. According to our modeling, in low-
15 elevation densely populated coastal zones, the gravitationally consistent sea-
16 level variations due to continental ice loss will range between 60 and 144 %
17 of the global mean. This includes the effects of glacial-isostatic adjustment,
18 which mostly contributes across the lateral forebulge regions in North Amer-
19 ica. While the mid range ocean-averaged elastic-gravitational sea-level vari-
20 ations compare with those associated with thermal expansion and ocean cir-
21 culation, their combination shows a complex regional pattern, where the for-
22 mer component dominates in the Equatorial Pacific Ocean and the latter in
23 the Arctic Ocean.

1. Introduction

24 The non-uniform effect of terrestrial ice melt (TIM) on relative sea level (RSL) was
25 recognised over a century ago [Woodward, 1888]. The modern theory [Farrell and Clark,
26 1976] has been further developed more recently to include, for example, changes in Earth
27 rotation and shoreline migration [Milne and Mitrovica, 1998] and is generally termed
28 the sea level equation (SLE). This equation has been used to investigate the impact of
29 idealised melt scenarios for Greenland and Antarctica [Mitrovica *et al.*, 2001] and to
30 examine the RSL pattern resulting from observed recent TIM [Bamber and Riva, 2010].
31 This latter study found that maxima occurred at low latitudes, in the Western Pacific in
32 particular, and had a marked zonal gradient driven, primarily, by the dominant sources
33 in both polar regions. To date, however, the SLE has not been used to examine the RSL
34 pattern resulting from prognostic predictions of future land ice melting, nor to examine
35 the relative importance of TIM and steric effects regionally.

36 Here, we combine predictions from numerical models for the evolution of the Greenland
37 (GrIS) and Antarctic (AIS) ice sheets with a regionalized model for glaciers and ice caps
38 to investigate the gravitationally consistent signature of future TIM based on the A1B
39 SRES scenario and the ECHAM-5 GCM [Meehl *et al.*, 2007]. Steric and ocean dynamic
40 processes are also non-uniformly distributed and we examine the relative importance of
41 these with respect to TIM, using the same GCM and greenhouse gas forcing.

2. Data processing and methods

42 For the Greenland and Antarctic ice sheets, volume changes are caused by both ice
43 dynamics and surface mass balance (SMB). SMB is driven by accumulation and surface

44 melting in Greenland and just the former in Antarctica. These fields were obtained from
45 two regional climate models (RCMs): MAR for Greenland [Fettweis *et al.*, 2007] and
46 RACMO for Antarctica [Lenaerts *et al.*, 2012]. Both were forced by the ECHAM5 GCM
47 under scenario A1–B. Annual SMB anomalies were calculated with respect to the baseline
48 period 1989–2008, and regridded to a spatial resolution of 1° . The period 1992–2000 was
49 appended to the scenarios using re-analysis data (ERA-Interim for Greenland, ERA-40
50 for Antarctica) and downscaled using the same RCMs. Ice dynamics, represented as
51 grounding line flux anomalies with respect to a reference year, were taken from ice sheet
52 model simulations forced by the same RCMs. SMB and ice dynamics sources are shown
53 in Fig. 1.

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54 For Antarctica, from an ensemble of 81 model runs, two simulations were selected: a
55 “mid-range” (MR) scenario contributing ~ 7 cm of mean sea-level rise (SLR) by 2100,
56 and a “high-end” (HE) scenario contributing ~ 30 cm. Only volume changes of ice above
57 floatation (i.e. contributing to SLR) are taken into account here. Antarctica is divided
58 into 15 major drainage basins, and in each basin the volume change is evenly distributed
59 over all 1° grid cells with an average velocity Rignot *et al.* [2011a] over 50 m yr^{-1} . For
60 Greenland, flow-line model simulations were carried out for three outlet glaciers: Jakob-
61 shavn isbræ, Petermann and Helheim glaciers and upscaled to obtain total volume changes
62 due to calving for three sectors of the GrIS following a previous approach [Price *et al.*,
63 2011]. For the MR scenario the model was calibrated against present-day observations.
64 To obtain the HE scenario, the bedrock data, an important source of uncertainty, was per-
65 turbed by its two-sigma error estimate and perturbed model parameters were prescribed.

66 Within each sector, volume changes are distributed evenly over all grid cells with average
67 velocity [Moon *et al.*, 2012] over 100 m yr^{-1} . We assume the ice sheets were close to bal-
68 ance until about 1992 [Rignot *et al.*, 2011b], when we prescribe the calving flux anomalies
69 to be zero, and interpolate linearly between 1992 and the initial scenario values in 2001.
70 For Greenland, volume changes in the MR and HE scenarios contribute ~ 4 and ~ 6 cm
71 SLR by 2100, respectively.

72 Volume changes for glaciers and ice caps (GIC) (Fig. 1c) are derived from a regionalized
73 glacier mass balance model that uses temperature and precipitation anomalies for 19
74 glacierized sectors globally. The same GCM forcing was used as for the ice sheets and
75 steric response. The sensitivities of the regional glacier responses were calibrated using
76 automatic weather station data for 80 benchmark glaciers [Giesen and Oerlemans, 2012].
77 As for Greenland, for the MR and HE scenarios, a calibrated version and a version with
78 perturbed parameters were used, respectively. For peripheral GIC around the ice sheets,
79 we used the GIC results solely and masked out overlapping ice sheet model regions.

80 Using the Fortran code SELEN [Spada and Stocchi, 2007], the SLE is solved in two steps.
81 In the first step, we only account for the ice sources described in Fig. 1 and we assume
82 an elastic rheology (the time scale is small compared with the Maxwell mantle relaxation
83 time). The time series shown in Fig. 1 were smoothed by a 10-year running average
84 for each grid cell, integrated in time, and converted to decadal averaged volumes. In
85 the second step, we account for the effects of the glacio-isostatic adjustment (GIA) of the
86 Earth to the melting of late-Pleistocene ice sheets. Here the SLE is solved using a Maxwell
87 visco-elastic rheology and employing, in particular, model ICE-5G(VM2) [Peltier, 2004].

88 In the short time window considered, the GIA component evolves at a constant rate. In
89 both steps, we solve the SLE iteratively to a maximum harmonic degree 128 by the pseudo-
90 spectral method, including rotational effects on sea-level change [Milne and Mitrovica,
91 1998]. In all simulations, the solution of the SLE is expressed in terms of RSL. The
92 variation of “absolute” sea-level, which would be observed by satellite altimetry, is $RSL +$
93 U , where U is vertical displacement of the solid surface of the Earth.

3. Results

94 Fig. 2 shows the TIM component of RSL expected for the year 2100, relative to 1992, F2
95 for the MR (a) and HE (b) scenarios (see Fig. 1). The maps show a somewhat complex
96 pattern but they clearly indicate that a SLR is expected almost everywhere, except in
97 the near field of areas of large TIM: predominantly Greenland and West Antarctica. The
98 geometry of the RSL variation is a consequence of the elastic regional uplift caused by ice
99 un-loading and the decreased gravitational force between the depleting ice and the sur-
100 rounding ocean. With increasing distance, the amplitude of vertical deformation decreases
101 and SLR dominates the global pattern, reaching values in excess of the eustatic amplitude
102 generally at latitudes below about 30° (the eustatic SLR represents the spatially uniform
103 response for a rigid, non-self-gravitating Earth, and is obtained by ocean-averaging the
104 fingerprints). The RSL patterns in Fig. 2 qualitatively agree with Mitrovica *et al.* [2001],
105 who considered sea-level fingerprints corresponding to geometrically simple, idealised ice
106 sources. The global pattern is, however, fairly insensitive to the localised distribution of
107 ice loss except in the near field of the sources [Bamber and Riva, 2010; Spada *et al.*, 2012].

108 The dominant localised sources of loss in both scenarios are West Antarctic calving and
109 the GrIS (Fig. 1). Although the integrated GIC response is similar in magnitude to the
110 AIS and larger than the GrIS, it is spread over a large part of the Earth's surface and
111 has, therefore, a smaller localised effect on RSL. This explains, in Fig. 2, the large sea-
112 level fall predicted off the Antarctic Peninsula, which, according to our computations, will
113 be subject to uplift rates as large as ~ 5 mm/yr in response to ice un-loading, and in the
114 region surrounding Greenland and the Svalbard archipelago. The sea-level fingerprints of
115 Fig. 2 are characterized by a distinct zonal pattern with a strong equatorial symmetry,
116 which reflects the dipole pattern of the major concentrations of TIM in Fig. 1. For both
117 scenarios, the largest increases are expected in the equatorial oceans where SLR exceeds
118 the eustatic value shown by green contours. In these regions the maxima are around 25%
119 greater than eustatic. This RSL pattern is broadly similar to the present-day fingerprint
120 due to TIM [Bamber and Riva, 2010].

121 Maps of the rates of sea-level variation expected for the year 2100, shown in Fig. S1,
122 have a similar pattern to the cumulative RSL of Fig. 2. At this epoch, maximum values
123 of ~ 3 and ~ 8 mm/yr are predicted at equatorial latitudes for the MR and HE scenarios,
124 respectively, in the same regions that experience the maximum amount of cumulative sea-
125 level (Fig. 2). However, according to our projections in Fig. 1, rates of this amplitude
126 can be considered as representative only of the second half of the 21st Century, at which
127 point there is an acceleration in ice loss from both the AIS and GIC (during previous
128 decades, these rates should be reduced by a factor of ~ 2). The spatially averaged rate of
129 sea-level rise for the MR scenario is ~ 3 mm/yr (not including steric effects). The TIM

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130 rates significantly exceed the (GIA-corrected) instrumental observations of SLR since
131 1880 (1.8 ± 0.1 mm/yr) [Douglas, 1997].

132 A cursory inspection of Fig. 2 indicates that the cumulative RSL along European coast-
133 lines does not exceed the eustatic value (this is also observed for the trends in Fig. S1).
134 This results specifically from mass loss from the GrIS and other Arctic GICs. However,
135 the rate is close to eustatic in north America, and largely above in Southeast Asia and
136 Africa. In Fig. S2 we consider RSL projections at specific locations of interest along the
137 coastlines (tide gauges and cities in low-elevation coastal zones).

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4. Discussion and conclusions

138 Here, the focus has been on the gravitationally consistent fingerprint of future terrestrial
139 ice loss. For the melting scenarios used, the patterns of SLR are fixed and will only
140 change significantly if the relative contributions of the AIS and Arctic ice masses change
141 significantly. The pattern is a consequence of localised elastic uplift and changes to the
142 geoid as a consequence of mass redistribution. Thermal expansion and ocean circulation
143 also have a non-uniform impact on the pattern of SLR [Yin *et al.*, 2010]. For convenience,
144 we will refer to these as the ocean response. It is, therefore, interesting to consider the
145 relative importance of oceanic and TIM effects on the future pattern of SLR and to see
146 where these effects may be compounded or possibly compensating. Slangen *et al.* [2012]
147 combined GCM model ensemble oceanic and TIM signatures using data from the IPCC
148 AR4 simulations but with a crude estimate of future TIM, resulting in the ocean response
149 being the main source of SLR. As is the case here, their TIM fluxes were not coupled to
150 the AOGCM simulations.

151 Here, we use the ocean response signal from the ECHAM-5 A1-B simulation [Meehl *et*
152 *al.*, 2007] for consistency with the TIM forcing but it should be noted that this was not
153 done in a coupled experiment, which is beyond the scope of this study. Thus, the ocean
154 response is consistent with the greenhouse gas forcings used but not with the TIM fluxes
155 produced by the offline ice sheet and glacier models. For the HE scenario, in particular, the
156 ocean response would likely be significantly altered by our TIM fluxes in a fully coupled
157 experiment. For our MR scenario, the eustatic TIM contribution is 24 cm in terms of RSL,
158 which is a similar magnitude to the ocean response for ECHAM-5 A1B of 27 cm [Meehl *et*
159 *al.*, 2007]. For the HE scenario, the TIM contribution is 61 cm, which is \sim double the
160 ocean signal. Thus in the MR case there will be areas where the ocean response is larger
161 than TIM and vice versa but not for the HE scenario. The TIM and ocean fingerprints
162 are shown in Figs. 3 and 4, showing the total (TIM+ocean) contribution and the fraction
163 of the total SLR due to TIM for both scenarios, respectively. Here, the TIM contribution
164 is expressed in terms of RSL and does not include the GIA component of sea-level change
165 since its importance is limited to formerly glaciated areas and is not an important fraction
166 of the total SLR, even in the MR scenario (see Fig. S2). In Fig. 4, a fraction greater than
167 0.5 indicates that TIM is larger than the ocean response and vice versa.

168 From the results in Figs. 3 and 4, it is apparent that the Southern Ocean is dominated
169 by the TIM signal, even for the MR scenario because the ocean response is significantly
170 below the global mean but this is also an area where TIM is less than eustatic (Fig. 2)
171 and thus a region that experiences considerably less than the mean total SLR response of
172 48 cm (i.e. TIM plus ocean response, see Fig. 3). Across a large swathe of the Southern

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173 Ocean total SLR is close to zero and, in the vicinity of the Antarctic Peninsula, and West
174 Antarctica negative. Conversely the Arctic Ocean is a region where the ocean response
175 is greater than the global mean while TIM is less (Fig. 2). For the MR scenario this
176 results in a total SLR that is close to the global mean, except for the Chukchi Sea where
177 it reaches almost a factor two more at about 80 cm (Fig. 3). TIM dominates SLR across
178 the Equatorial Pacific Ocean and into a large part of the Indian Ocean, which are all areas
179 where the ocean response is close to, or less than, the global mean. The other region where
180 TIM dominates for the MR scenario is in the vicinity of the Kuroshio Current. For the HE
181 scenario, TIM is dominant everywhere except for a region around the Antarctic Peninsula,
182 West Antarctica and, surprisingly, the Arctic Ocean again. For reasons discussed above,
183 this conclusion is, however, tentative and should be confirmed using a coupled AOGCM
184 forced with the TIM fluxes used here.

185 Although the ocean response presented here is for just one model and one SRES scenario,
186 the pattern appears to be relatively robust across the ensemble of GCMS used in the
187 IPCC AR4 [Meehl *et al.*, 2007]. It is also the case, that even if the balance of ice loss
188 from the ice sheets changes within likely bounds, then the the areas experiencing the
189 largest SLR due to TIM will remain the same. Thus, we conclude that TIM will be of
190 critical importance to regional SLR in the Equatorial Pacific Ocean and, in particular,
191 around Western Australia, Oceania and the small Atolls and islands in this region. We
192 also conclude that SLR in the Arctic Ocean will be greater than the global mean and
193 dominated by ocean processes with relatively little impact from TIM.

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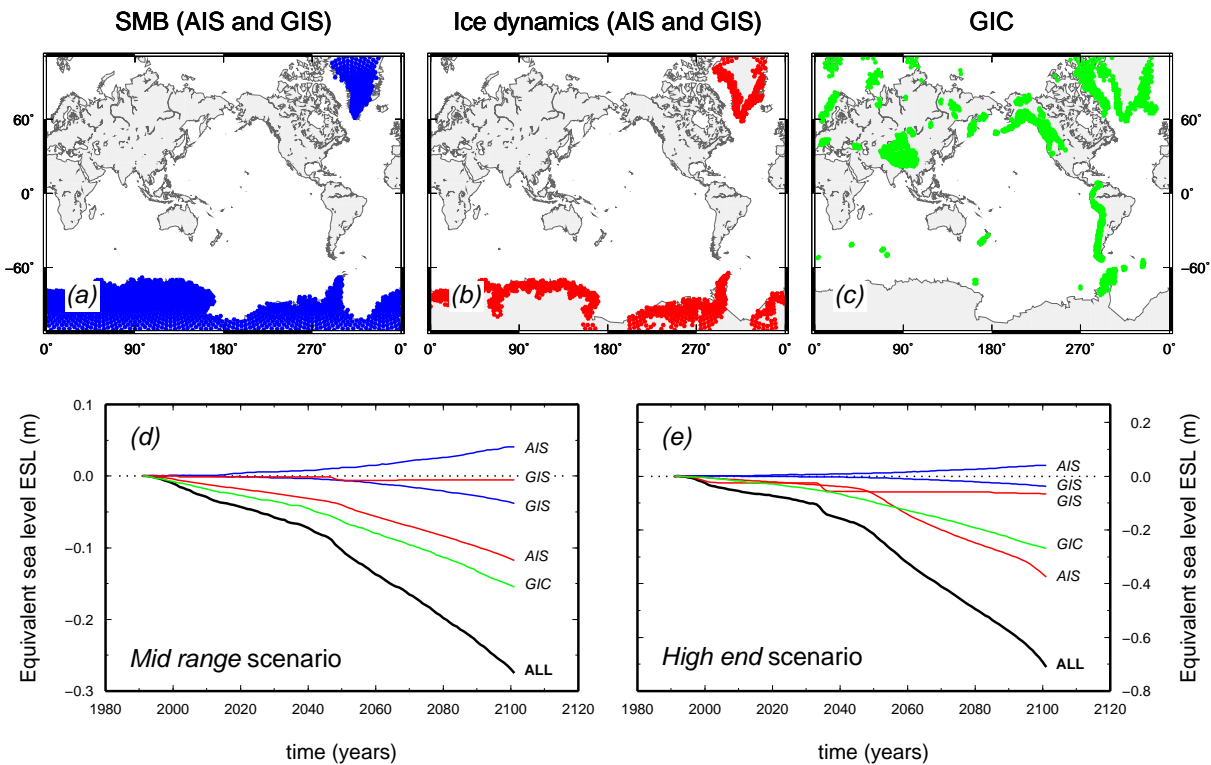


Figure 1. Top: spatial distributions of the ice sources used in this study: SMB (a), ice dynamics (b) and GICs (c). SMB and ice dynamics sources are further separated into AIS and GIS components. Bottom: time history of ESL (equivalent sea-level) since 1992, corresponding to the sources in (a–c), for the MR (d) and HE (e) scenarios, respectively. ALL curves show the total ESL variation.

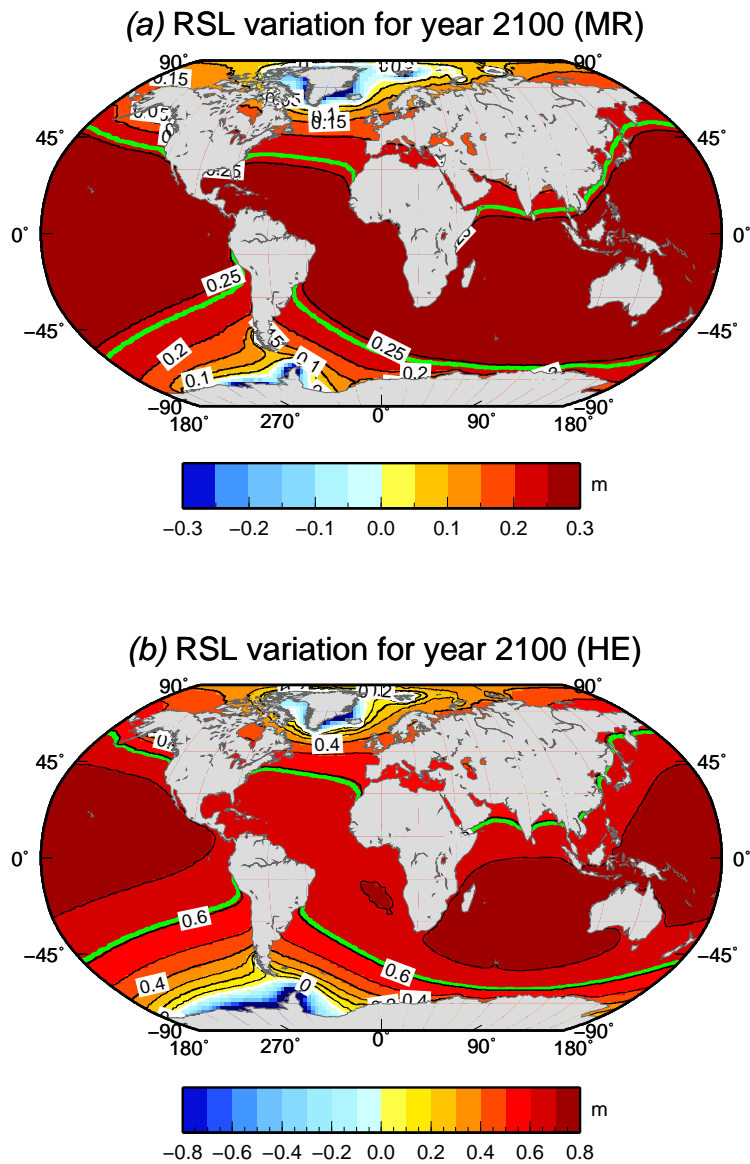


Figure 2. Fingerprint of the TIM RSL variation (m) for the year 2100 (relative to year 1992) pertaining to the MR (a) and HE scenarios (b). The green contour shows the ocean-averaged value (eustatic variation). The GIA component of sea-level change is not considered here.

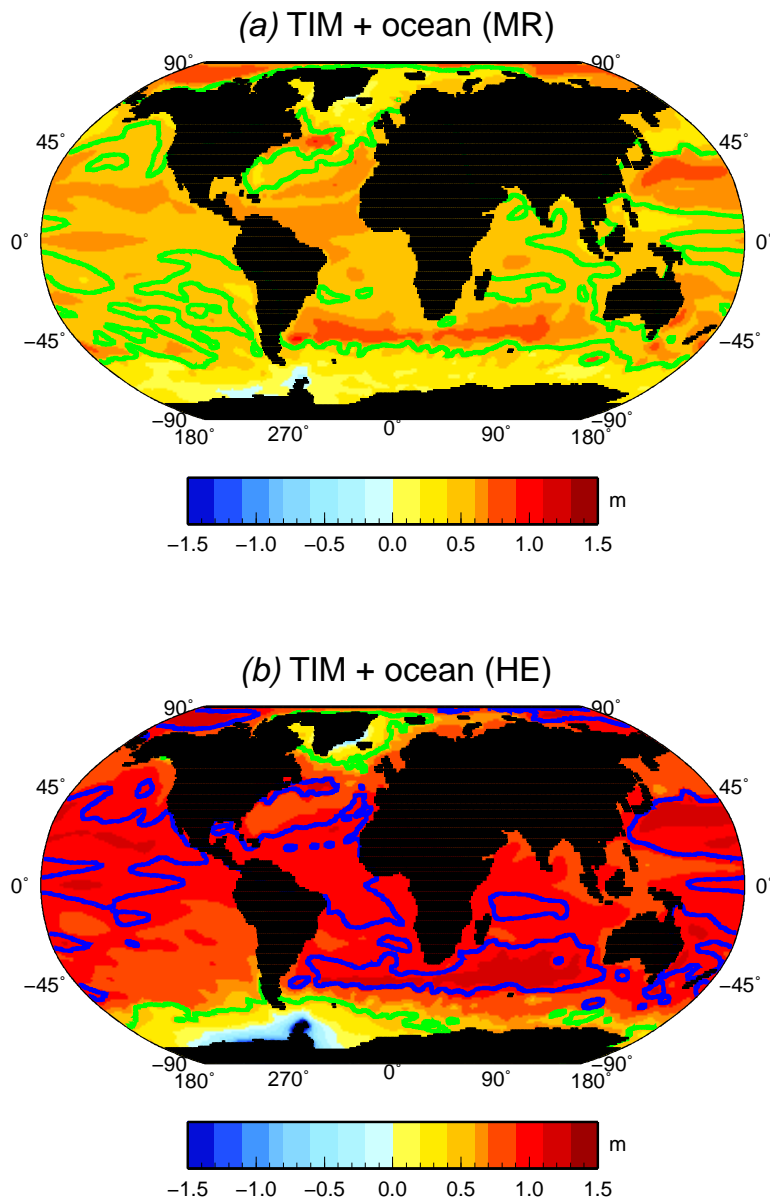


Figure 3. Total SLR (TIM plus ocean component) for the year 2100 and based on the MR (a) and HE scenarios (b), respectively. The green contour line corresponds to a SLR of 0.5 m; the blue one in (b) to a SLR of 1.0 m.

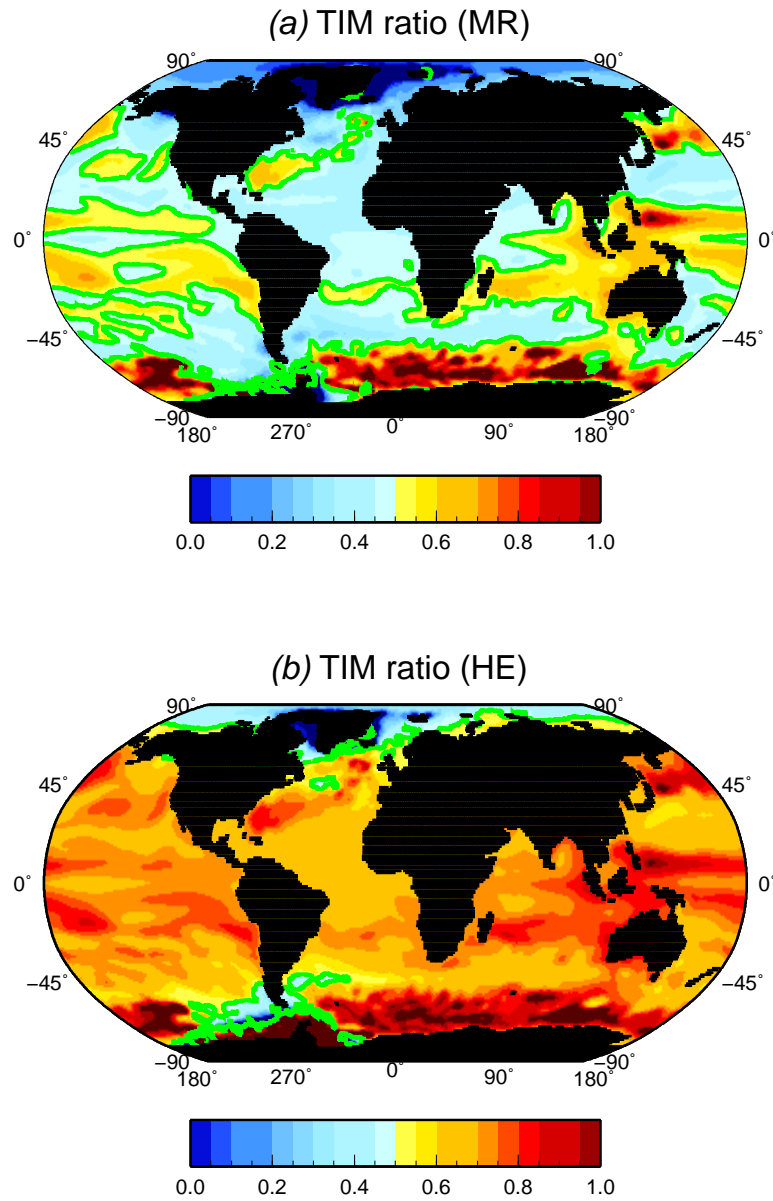


Figure 4. Ratio of the TIM component of total SLR expected for the year 2100 and based on the MR (top) and HE scenarios (bottom), respectively. The green contour line shows the a ratio of 0.5, where the contribution of TIM and ocean processes is equal.