

Hindawi Publishing Corporation  
Scientifica  
Volume 2016, Article ID 6767538, 7 pages  
<http://dx.doi.org/10.1155/2016/6767538>



## Research Article

# Estimation of Surface Area and Volume of a Nematode from Morphometric Data

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Received 26 December 2015; Accepted 1 March 2016

Academic Editor: Alessandra Torina

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Nematode volume and surface area are usually based on the inappropriate assumption that the animal is cylindrical. While nematodes are approximately circular in cross section, the radius varies longitudinally. We use standard morphometric data to obtain improved estimates of volume and surface area based on (i) a geometrical approach and (ii) a Bézier representation of the nematode. These new estimators require only the morphometric data available from Cobb's ratios, but if fewer coordinates are available the geometric approach reduces to the standard estimates. Consequently, these new estimators are better than the standard alternatives.

## 1. Introduction

The physiological activities of nematodes, such as respiration or excretion/secretion, have been expressed on various bases, including wet or dry weight [1], protein [2], surface area [3], and nematode number [4]. Each of these has a distinct significance. Dry weight is indicative of the total amount of material comprising the nematode, including that which is metabolically inactive. Wet weight has the added complication that there is residual water outside the animal which is not related to its physical structure. Protein, commonly used by biochemists, depends on the specific assay employed, since protein properties and nonprotein contaminants interfere with the chemistry of each assay differently [5]. Surface area is especially relevant to transport studies [3, 6], but it is difficult to estimate. Nematode number is relatively easily estimated, but differences in the size of individuals can obscure the significance of the data reported.

Nematodes vary greatly in morphology between species [7–9] and life cycle stages, and the morphology of parasitic nematodes can depend on the host [10]. For example, *L<sub>3</sub> Teladorsagia circumcincta* essentially has a cylindrical body tapering to relatively pointed ends, the posterior tip being

more pointed than the anterior [8, 11]. Whereas the adult male, for example, is substantially larger and has a bursa at the posterior that is wider than rest of the body of the nematode, other species have a posterior reminiscent of a needle.

The morphometry of nematodes is often based on the length and width of the body [8, 12, 13] or of specific anatomical features [14]. Nematodes are frequently described as cylindrical; among many examples, Sims et al. [3, 6] estimated the surface area and volume of *Ascaris suum* and adult *Haemonchus contortus* from the length and width assuming the nematode to be cylindrical. Andrassy's [15] volume estimate is also based on that of a cylinder,

$$V_A \approx \frac{4}{5} \pi L \left( \frac{D}{2} \right)^2, \quad (1)$$

but includes a correction factor. Holovachov [16], citing the work of Tsalolikhin, estimated the volume of a nematode using

$$V_T = \frac{1}{24} \left[ \pi L (d^2 + dD + D^2) + \pi LD^2 \right], \quad (2)$$

where  $L$ ,  $D$ , and  $d$  are the length, maximum diameter, and labial region diameter, respectively. Of course, nematodes are

none of these shapes, so a means of representing the variety of morphologies that better describes the surface area and volume is required. Here we provide two complementary approaches to this problem based on common morphometric measurements.

## 2. Common Morphometric Measurements

The commonly used morphometric measurements [17–19] relate the distance between the anterior of the nematode and particular anatomical features ( $L_i$ ) and the diameter ( $D_i$ ) of the nematode at each point. While Cobb [19] described his approach as a “formula,” as Van Cleave [20] suggested, it is really just a short-hand notation for particular ratios. The specific anatomical points defined by Cobb [19] are the base of the pharynx or the buccal cavity ( $L_1$  and  $D_1$ ), the nerve ring ( $L_2$  and  $D_2$ ), the end of the oesophagus or base of the neck ( $L_3$  and  $D_3$ ), the vulva in females or middle of the nematode in males ( $L_4$  and  $D_4$ ), and at the anus ( $L_5$  and  $D_5$ ). Cobb [19] reports the overall length of the nematode ( $L$ ) and  $l_i$  ( $= L_i/L$ ) and  $d_i$  ( $= D_i/L$ ) as a percentage. While these values do not provide a complete description of the nematode, they do provide a means of generating the characteristic shape of the nematode as we describe here.

The more commonly used de Man indices [17–19] are the ratio of the length to the greatest diameter ( $a$ ), the ratio of the length to the length of the oesophagus ( $b$ ), the ratio of the length to the length of the tail ( $c$ ), and the ratio of tail length to radius at the anus ( $c'$ ). These are usually supplemented with other measurements, but what is reported varies considerably. Of course, some of Cobb's ratios can be expressed in terms of the de Man indices:

$$\begin{aligned} l_3 &= b^{-1}, \\ d_4 &\approx 2a^{-1}, \\ l_5 &= 1 - c^{-1}, \\ d_5 &= \frac{2c}{c'} \end{aligned} \quad (3)$$

and in some cases other measurements make it possible to calculate more of Cobb's ratios. Interestingly, some authors confuse de Man indices with Cobb's ratios [22, 23].

While Cobb's ratios are more comprehensive than the de Man indices and they are still used [24–27], the latter are in more widespread use. Fracker [28] suggested that Cobb had never substantiated the consistency of his ratios and pointed out that it is sometimes difficult to identify some of the required anatomical features. Such problems may represent an impediment to the use of Cobb's ratios for taxonomic purposes, but there is no such barrier to their use in modeling the geometry of a nematode. In fact, providing the measurement points that are distributed appropriately, it may not matter particularly that they are made consistently. However, the inadequacy of the de Man indices is indicated by the frequency with which they are supplemented by other measurements.

## 3. A Simple Geometric Model

For each nematode the volume ( $v$ ) can be thought of comprising the volumes of the head ( $v_H$ ), core ( $v_C$ ), and tail ( $v_T$ ),

$$v = v_H + v_C + v_T \quad (4)$$

and a surface area  $a_s$  made up of the surface areas of the sides of the head ( $a_{sH}$ ), core ( $a_{sC}$ ), and tail ( $a_{sT}$ ),

$$a_s = a_{sH} + a_{sC} + a_{sT}. \quad (5)$$

The surface area of the ends of the core must match the surface area of the base of the head and of the tail as appropriate. Of course, the length of these geometrical elements must sum to the length of the nematode.

While nematodes are often treated as cylindrical, a slight elaboration of this geometrical model is helpful. The frustum of a cone has a volume and surface area given by

$$v = \frac{\pi h}{3} (r_1^2 + r_1 r_2 + r_2^2), \quad (6)$$

$$a_s = \pi (r_1 + r_2) \sqrt{(r_1 - r_2)^2 + h^2} + \pi (r_1^2 + r_2^2), \quad (7)$$

respectively, where  $r_1$  and  $r_2$  are the radii of the base and the top of the frustum (so  $r_1 \geq r_2$ ) and  $h$  is the height. It is easy to see that if  $r_2 = r_1$ , then the expressions reduce to those for the volume and surface area of a cylinder. On the other hand, if  $r_2 = 0$ , they reduce to those of a cone. In two dimensions, as a nematode appears under the microscope, the perimeter and area of the projection of the frustum are

$$p = 2(r_1 + r_2) + 2\sqrt{(r_1 - r_2)^2 + h^2}, \quad (8)$$

$$a = (r_1 + r_2)h, \quad (9)$$

respectively. Applying these expressions to nematode morphology provides a flexible and simple geometrical approach that would incorporate both the standard cylindrical model and Tsalolikhin's estimator (2).

The structure defined by Cobb's ratios can be viewed as the sum of six separate geometrical elements:

$$v = \sum_{i=1}^6 v_i, \quad (10)$$

corresponding to those defined by the coordinates implicit in the ratios. The surface area is the sum of the corresponding surface areas less twice the surface area of circles corresponding to the interfaces between these elements:

$$a_s = \sum_{i=1}^6 a_{s_i} - 2\pi (r_{12}^2 + r_{23}^2 + r_{34}^2 + r_{45}^2), \quad (11)$$

similarly for the projected area ( $a$ ) and the perimeter ( $p$ ).

As a cone and a cylinder are simply particular cases of the frustum of a cone (10)-(11), the corresponding expressions for  $a$  and  $p$  can be written:

$$p = 2 \left( r_0 + r_n + \sum_{i=0}^{n-1} \sqrt{(r_{i+1} - r_i)^2 + (l_{i+1} - l_i)^2} \right), \quad (12)$$

$$a = \sum_{i=0}^{n-1} (r_i + r_{i+1}) (l_{i+1} - l_i), \quad (13)$$

$$a_s = \pi \left( r_0^2 + r_n^2 + \sum_{i=0}^{n-1} (r_i + r_{i+1}) \sqrt{(r_{i+1} - r_i)^2 + (l_{i+1} - l_i)^2} \right), \quad (14)$$

$$v = \frac{\pi}{3} \sum_{i=0}^{n-1} (r_i^2 + r_i r_{i+1} + r_{i+1}^2) (l_{i+1} - l_i). \quad (15)$$

Clearly, (12)–(15) can be extended easily to more than  $n = 6$  distinct geometric elements to obtain the natural expressions:

$$P = \lim_{n \rightarrow \infty} p = 2 \left( r_0 + r_n + \int_0^L ds \right), \quad (16)$$

$$A = \lim_{n \rightarrow \infty} a = \int_0^L (2r + dr) dl = 2 \int_0^L r dl, \quad (17)$$

$$S = \lim_{n \rightarrow \infty} a_s = \pi \left( r_0^2 + r_n^2 + \int_0^L (2r + dr) ds \right) \\ = \pi \left( r_0^2 + r_n^2 + 2 \int_0^L r ds \right), \quad (18)$$

$$V = \lim_{n \rightarrow \infty} v = \pi \int_0^L r^2 dl, \quad (19)$$

since  $\int dr dl = 0$ . Here,  $ds$  and  $dl$  are line elements taken along the surface and midline, respectively, of the nematode and  $r$  varies along the length of the nematode. In effect, Robinson [29] used a discrete version of (19) in his calculations.

#### 4. Least Squares Estimates of the Bézier Representation

*4.1. Bézier Curve Background.* The Bézier curve associated with  $n + 1$  points  $P_0, P_1, \dots, P_n$  is given by

$$\mathbf{C}(t) = \sum_{i=0}^n \mathbf{P}_i B_{i,n}(t), \quad (20)$$

where  $t \in [0, 1]$  and  $B_{i,n}(t)$  is a Bernstein polynomial given by

$$B_{i,n}(t) = \binom{n}{i} t^i (1-t)^{n-i}. \quad (21)$$

Of course, (20) can be written as  $\mathbf{C} = \mathbf{B}\mathbf{P}$  and if  $\mathbf{P}$  is known, then (20) can be used to calculate the Bézier curve. The least squares estimate of  $\mathbf{P}$  is

$$\mathbf{P} = (\mathbf{B}'\mathbf{B})^{-1} \mathbf{B}'\mathbf{C} \quad (22)$$

[30], where  $\mathbf{C}$  is a matrix containing the coordinates of the morphometric data and, if necessary to adjust for the importance of particular morphometric coordinates, this can be rewritten as

$$\mathbf{P} = (\mathbf{B}'\mathbf{W}\mathbf{B})^{-1} \mathbf{B}'\mathbf{W}\mathbf{C}, \quad (23)$$

where  $\mathbf{W}$  is a diagonal matrix of weights.

The parametric representation of the nematode in  $\mathbf{C}(t)$  can be used to provide an estimate of  $P$ ,  $A$ ,  $S$ , and  $V$  using well known expressions [31]:

$$P = 2 \int_{\alpha}^{\beta} \sqrt{\left(\frac{dy}{dt}\right)^2 + \left(\frac{dx}{dt}\right)^2} dt, \\ A = 2 \int_{\alpha}^{\beta} y(t) \frac{dx}{dt} dt, \quad (24)$$

$$S = 4\pi \int_{\alpha}^{\beta} y(t) \sqrt{\left(\frac{dy}{dt}\right)^2 + \left(\frac{dx}{dt}\right)^2} dt,$$

$$V = \pi \int_{\alpha}^{\beta} (y(t))^2 \frac{dx}{dt} dt.$$

In implementing these calculations it is useful to recall that the derivative of the Bernstein polynomial (21) is

$$\frac{d}{dt} B_{i,n}(t) = n(B_{i-1,n-1}(t) - B_{i,n-1}(t)), \quad (25)$$

so that the derivative of (20) is

$$\frac{d}{dt} \mathbf{C}(t) = n \sum_{i=0}^n \mathbf{P}_i (B_{i-1,n-1}(t) - B_{i,n-1}(t)). \quad (26)$$

*4.2. Application to Nematode Morphology.* As an explicit numerical example, the morphometric data provide 5 coordinates defined as a fraction of the length of the nematode which we supplement with two coordinates (0, 0) and (1, 0), so in (21)  $n = 6$ ,  $i = 0, 1, \dots, 6$ , and  $t = 0, 1/6, 2/6, \dots, 6/6$ . From this

**B**

$$= \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{15625}{46656} & \frac{3125}{7776} & \frac{3125}{15552} & \frac{625}{11664} & \frac{125}{15552} & \frac{5}{7776} & \frac{1}{46656} \\ \frac{64}{729} & \frac{64}{243} & \frac{80}{243} & \frac{160}{729} & \frac{20}{243} & \frac{4}{243} & \frac{1}{729} \\ \frac{1}{64} & \frac{3}{32} & \frac{15}{64} & \frac{5}{16} & \frac{15}{64} & \frac{3}{32} & \frac{1}{64} \\ \frac{1}{729} & \frac{4}{243} & \frac{20}{243} & \frac{160}{729} & \frac{80}{243} & \frac{64}{243} & \frac{64}{729} \\ \frac{1}{46656} & \frac{5}{7776} & \frac{125}{15552} & \frac{625}{11664} & \frac{3125}{15552} & \frac{3125}{7776} & \frac{15625}{46656} \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \quad (27)$$

TABLE 1: Comparison of estimates of  $p$ ,  $a$ ,  $a_s$ , and  $v$  for *A. antarcticus* [21] obtained using the cylindrical, Andr assy (1), and Tsalolikhin (2) approximations [15, 16] and those reported here (12)–(15) and (24). The estimates from the B ezier representation were confirmed numerically using (24).

	$p$ or $P$ (m)	$a$ or $A$ (m <sup>2</sup> )	$a_s$ or $S$ (m <sup>2</sup> )	$v$ or $V$ (m <sup>3</sup> )
cylinder <sup>a</sup>	$1.229 \times 10^{-3}$	$8.64 \times 10^{-9}$	$2.75 \times 10^{-8}$	$9.77 \times 10^{-14}$
Andr�assy <sup>b</sup>	—	—	—	$7.82 \times 10^{-14}$
Tsalolikhin <sup>a</sup>	$1.188 \times 10^{-3}$	$5.04 \times 10^{-9}$	$1.58 \times 10^{-8}$	$3.98 \times 10^{-14}$
This work				
Geometrical	$1.204 \times 10^{-3}$	$7.13 \times 10^{-9}$	$2.24 \times 10^{-8}$	$7.15 \times 10^{-14}$
B�ezier	$1.208 \times 10^{-3}$	$7.54 \times 10^{-9}$	$2.26 \times 10^{-8}$	$7.40 \times 10^{-14}$

<sup>a</sup>The expressions for  $p$ ,  $a$ , and  $a_s$  for these two approaches are obvious and are not reproduced here.

<sup>b</sup>It is unclear how Andr assy’s approach can be applied to the estimation of  $p$ ,  $a$ , and  $a_s$ .

which we reproduce here because it applies to every case for which there are 7 morphometric coordinates. It is clear from (20) and  $\mathbf{B}$  that  $\mathbf{C}(0) = \mathbf{P}_0$  and  $\mathbf{C}(1)=\mathbf{P}_6$ . Cobb [21] gives morphometric data for *Aplectus antarcticus* from which, including the supplementary coordinates,

$$\mathbf{C}' = \frac{1}{100} \begin{pmatrix} 0 & 0.1 & 12.6 & 21 & 51 & 87 & 100 \\ 0 & 0.4 & 1.1 & 1.15 & 1.2 & 0.95 & 0 \end{pmatrix}, \quad (28)$$

$$\mathbf{P}' = \frac{1}{100} \begin{pmatrix} 6.743 \times 10^{-13} & -57.417 & 151.512 & -155.854 & 127.245 & 87.37 & 100 \\ 1.701 \times 10^{-14} & -1.543 & 5.829 & -3.422 & 3.969 & 0.722 & 5.088 \times 10^{-16} \end{pmatrix} \quad (29)$$

and writing (20) explicitly,

$$\begin{aligned} \mathbf{C}(t) &= \begin{pmatrix} x(t) \\ y(t) \end{pmatrix} \\ &= \mathbf{P}_0 (1-t)^6 + 6\mathbf{P}_1 (1-t)^5 t + 15\mathbf{P}_2 (1-t)^4 t^2 \\ &\quad + 20\mathbf{P}_3 (1-t)^3 t^3 + \dots + 15\mathbf{P}_4 (1-t)^2 t^4 \\ &\quad + 6\mathbf{P}_5 (1-t) t^5 + \mathbf{P}_6 t^6, \end{aligned} \quad (30)$$

where  $\mathbf{P}_i$  is the  $i$ th row of  $\mathbf{P}$ . As  $\mathbf{C}(t)$  is expressed in relative units it can be converted into dimensional form by multiplying by  $L$ .

Plotting  $y(t)$  against  $x(t)$  (30) yields the B ezier curve in the upper half of Figure 1(a). Since the nematode is symmetrical the lower boundary is just  $-y(t)$  against  $x(t)$ , which is also shown in Figure 1(a). At least two features of the form defined by (30) are inappropriate: at the anterior end the B ezier curve forms a pair of loops and at the posterior end  $dy/dx$  approaches zero. The former is a common feature of polynomial interpolation through more than a small number of points [32]. The latter is overcome by fitting a B ezier curve clockwise through the coordinates on both sides of the nematode (Figure 1(b)). This 13-coordinate extended representation is reasonable at the posterior, but the Runge effect is amplified at the anterior. However, it is clear from Figure 1(b) that the lower surface is better described than the upper surface. In fact all except the anterior supplementary

where the upper row of numbers represents the relative position along the length of the nematode and the lower row is the corresponding relative radius (note that Cobb [21] specifies the diameter rather than the radius). Substituting these into (22) yields estimates of the B ezier control points

coordinate are described well by the lower curve. This observation and the symmetry of the nematode prompted the use of that part of the curve from the anterior supplementary coordinate (1, 0) to the first of Cobb’s coordinates (0.001,  $-0.004$ ) to model both the upper and lower boundaries of the nematode (Figure 1(c)). The dotted line underneath Figure 1(c) indicates the portion of the B ezier curve that was used to generate the upper side of the nematode by reflection around the horizontal axis. The remainder of the anterior boundary was completed by linear interpolation from the anterior supplementary coordinate (0, 0) to (0.001, 0.004) and to (0.001,  $-0.004$ ).

## 5. Comparison of Estimates of $p$ , $a$ , $a_s$ , and $v$

The geometric and B ezier representations of *A. antarcticus* described here are bounded by the cylindrical model and they enclose Tsalolikhin’s model (2) completely (Figure 2). As (2) can be rewritten as

$$V_T = \frac{1}{2} \frac{\pi L}{3} \left[ \left( \frac{d^2 + dD + D^2}{4} \right) + \frac{D^2}{4} \right], \quad (31)$$

it is apparent that (2) represents an average of the volumes of a cone (diameter  $D$  and length  $L$ ) and a conical frustum (length  $L$ , diameters  $D$  and  $d$ ). Implicit in this geometrical approach is the assumption that  $D$  is located at the midpoint of a nematode which gets thinner towards blunt and pointed ends (presumably the anterior and posterior, resp.). Of course, this

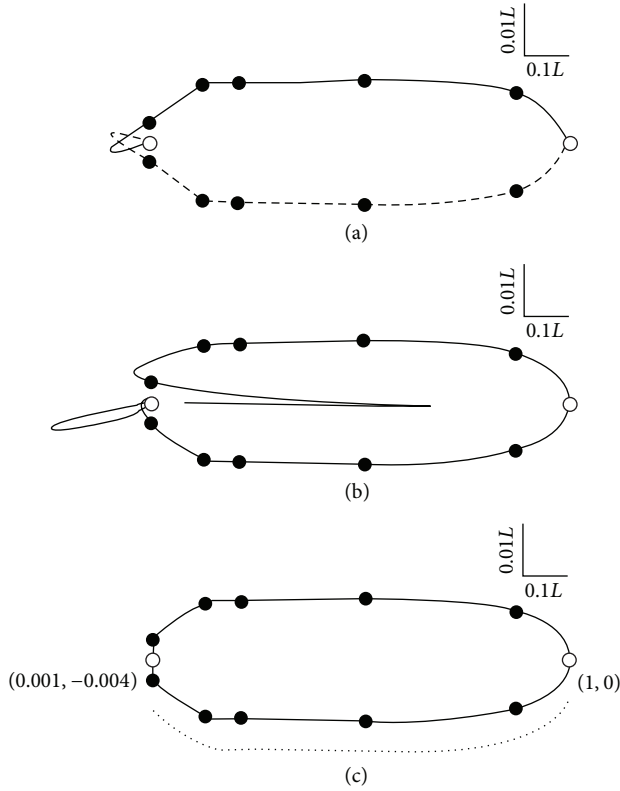


FIGURE 1: The development of the unweighted Bézier representation of *Aplectus antarcticus*. The morphometric data of Cobb [21] (●) and two supplementary coordinates (○, (0, 0) and (1, 0)) are shown. The 7-coordinate version of the unweighted Bézier representation (27)–(30) is the solid line in (a), which is reflected along the horizontal axis to give the dashed line in (a). The extended 13-coordinate Bézier representation in (b) is explained in the text, as is the edited extended representation (c) that is derived from it. The dotted line in (c) represents the region from (0.001, -0.004) to (1, 0) that is reflected about the horizontal axis to form the upper boundary. Note that the vertical and horizontal dimensions differ in scale by a factor of 10 relative to the overall length of the nematode ( $L = 0.6$  mm).

is equivalent to (15) for  $n = 2$ , which might be the case for reports of the de Man indices (3).

The geometrical model represents the convex hull of  $\mathbf{C}$  (Figure 2), which necessarily provides a minimum estimate of  $p$  and  $a$ . The overestimation inherent in the cylindrical estimate and the underestimation arising from Tsalolikhin's model (2) are clear (Figure 2). To quantify this, the coordinates for *A. antarcticus* (28) were used to calculate  $p$ ,  $a$ ,  $a_s$ , and  $v$  (or the corresponding values from the Bézier representation (24)) (Table 1). As would be expected from Figure 2, the Bézier and geometrical representations yield estimates that are similar and lie between those of the cylindrical and Tsalolikhin's (2) models. Arbitrarily taking the geometrical representation as a reference, the cylindrical approach yields a volume 36% larger and (2) yields a value that is 44% smaller (Table 1). Even the value obtained from Andrassy's equation is 9% larger than the geometrical estimate, whereas the Bézier estimate is only 3.5% larger (Table 1).

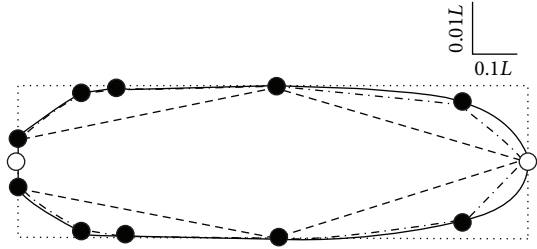


FIGURE 2: Comparison of the boundaries on which the estimates in Table 1 are based. The Bézier (—) and geometric (-----) representations are those we describe. The Tsalolikhin (----) and cylindrical (.....) approximations have been reported previously. The morphometric data for *A. antarcticus* reported by Cobb [21] (●) and two supplementary coordinates (○, (0, 0) and (1, 0)) are shown. The vertical and horizontal dimensions differ in scale by a factor of 10 relative to the overall length of the nematode ( $L = 0.6$  mm).

In the case of *A. antarcticus* the error in  $V_T$  arising just from the assumption that the point of greatest diameter is at  $L/2$  may be small. Nevertheless, it is instructive to consider a variant of (2) in which the weighting ( $\lambda$ ) between the conical posterior and an anterior conical frustum can be varied. To do this we write (2) as

$$\begin{aligned} V_T(\lambda) &= \frac{\pi L}{3} \left[ \lambda \left( \frac{d^2 + dD + D^2}{4} \right) + (1 - \lambda) \frac{D^2}{4} \right] \\ &= \frac{\pi L}{3} \left[ \lambda \left( \frac{d^2 + dD}{4} \right) + \frac{D^2}{4} \right], \end{aligned} \quad (32)$$

and the error arising from the midlength assumption is

$$\varepsilon_T = \frac{V_T - V_T(\lambda)}{V_T(\lambda)} = \frac{1}{2} \frac{1 - 2\lambda}{\lambda + D^2/(d^2 + dD)}. \quad (33)$$

Applying (33) to the values for *A. antarcticus*, in which the widest point is located at  $0.51L$  rather than  $0.5L$ , yields  $\varepsilon_T = -0.0036$ , so volume is only slightly underestimated, but Cobb [21] reports data for other species for which  $\lambda$  is larger. For example, for *Monhystera polaris*  $d = 1.5$ ,  $D = 3.4$ , and  $\lambda = 0.64$ , so  $\varepsilon_T = -0.063$  which would be a significant underestimate for some purposes, even without any consideration of the other coordinates Cobb [21] reports.

## 6. Conclusion

Estimates of nematode volume are usually made using the cylindrical, Andrassy, and Tsalolikhin approximations. The latter provides an underestimate and the others provide overestimates of nematode size, but they rely on a small number of coordinates. However, the more detailed data available from the Cobb ratios can be used to make better estimates based on the simple geometric or a Bézier approach that we describe. The cylindrical and Tsalolikhin approximations are particular cases of the more general geometric estimate that represents the minimum size of the nematode. The geometric estimate can be extended to incorporate more coordinate data. These approaches could easily be incorporated into appropriate image analysis software [33–36].



## Competing Interests

The authors declare that they have no competing interests.

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