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1 Wild hummingbirds rely on landmarks not geometry when learning an array of flowers

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4 20 **Abstract** Rats, birds or fish trained to find a reward in one corner of a small enclosure, tend to
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7 21 learn the location of the reward using both nearby visual features and the geometric relationships
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9 22 of corners and walls. Because these studies are conducted under laboratory and thereby
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11 23 unnatural conditions, we sought to determine whether wild, free-living rufous hummingbirds
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14 24 (*Selasphorus rufus*) learning a single reward location within a rectangular array of flowers would
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16 25 similarly employ both nearby visual landmarks and the geometric relationships of the array.
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18 26 Once subjects had learned the location of the reward we used test probes in which one or two
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21 27 experimental landmarks were moved or removed in order to reveal how the birds remembered
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24 28 the reward location. The hummingbirds showed no evidence that they used the geometry of the
25
26 29 rectangular array of flowers to remember the reward. Rather, they used our experimental
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29 30 landmarks, and possibly nearby, natural landmarks, to orient and navigate to the reward. We
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31 31 believe this to be the first test of the use of rectangular geometry by wild animals and we
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33 32 recommend further studies be conducted in ecologically relevant conditions in order to help
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36 33 determine how and when animals form complex geometric representations of their local
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38 34 environments.
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43 36 Key Words: hummingbird, orientation, navigation, spatial memory, landmark, geometry
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40 **Introduction**

41 Orientation and navigation by vertebrates are often considered in the context of long distance
42 migrations (Guilford et al. 2011, Fuxjager et al. 2011). However, orientation and navigation are
43 common phenomena in animals' everyday lives as they defend territories, forage in their home
44 ranges, return to nests or burrows, etc. In many ways this latter expression of orientation and
45 navigation is more tractable and amenable to experimental manipulation than is the former and
46 numerous studies employing rats or pigeons have revealed the use of cues such as global
47 landmarks, local features and geometry of an enclosure for orientation. For example, Cheng
48 (1986) demonstrated that rats learned the food-rewarded corner of a small arena by encoding
49 both local visual features and the geometry of the arena.

50 Geometry in this context has a specific meaning. In Cheng's (1986) study, the rats
51 remembered not just the location of food relative to one or more features of the arena.
52 Significantly, they encoded and recalled aspects of the arena relative to each other; this is
53 considered a geometric representation of their environment. Specifically, the rewarded corner in
54 the arena had a short wall on one side and a longer wall on the other. When tested, the rats
55 demonstrated memory for this configuration by selecting the rotationally similar (diagonally
56 opposite) corner as often as they selected the correct corner.

57 Subsequent to Cheng's (1986) first reporting the use of arena geometry by rats, there
58 have been numerous studies investigating the extent to which animals use geometry vs. visual
59 cues when they learn and remember a reward location (recent reviews: Tommasi et al 2012,
60 Cheng et al. 2013). For example, Kelly and Spetch (2001) tested pigeons (*Columba livia*) in a
61 small rectangular room with identical visual features in each corner. With only the geometric
62 relationships between long and short walls available to indicate the rewarded corner, pigeons did

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4 63 indeed use the relative lengths of walls to find the reward. When mountain chickadees (*Poecile*
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6 64 *gambeli*) were tested in a similar rectangular arena with one wall painted blue (visual cue), birds
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9 65 trained with the reward close to the cue learned the cue and birds trained with the reward far
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11 66 from the visual cue learned arena geometry (Gray et al. 2005). In a follow-up experiment, wild-
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14 67 caught and hand-reared black-capped chickadees (*Poecile atricapillus*) tended to use geometry
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16 68 whereas wild-caught mountain chickadees tended to use the blue-wall cue (Batty et al. 2009).
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18
19 69 Kelly (2010), recognizing that geometry may be particularly salient when available only as the
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21 70 walls of a room, presented a rectangular array of four objects to Clark's nutcrackers (*Nucifraga*
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24 71 *columbiana*) in an arena with no reliable global landmarks. The birds learned the geometric
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26 72 relationships of the rectangular array only when a distinctive visual feature marked each object.

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29 73 Although these laboratory studies are carefully controlled and provide valuable insights
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31 74 into the orientation capabilities of animals, they are also highly artificial and lack ecological
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33 75 relevance. One solution to this concern has been to use more naturalistic tasks such as caching
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36 76 and recovery of food items by birds flying freely in an aviary (corvids: Kamil et al. 1999, parids:
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38 77 Krebs et al. 1990), or foraging by bees in large enclosures (Ohashi et al. 2007). Increasing
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41 78 ecological relevance involves animals in the wild, such as ants (Collett 2012) or ground squirrels
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43 79 (Vlasak 2006). One particularly tractable system is that of free-living territorial rufous
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46 80 hummingbirds (*Selasphorus rufus*), which forage at both natural and experimental flowers
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48 81 (Healy and Hurly 2013; Waser and McRobert 1992). Experimental incorporation of foraging
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51 82 behaviours, interspersed with activities such as territorial defense, courtship and predator
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53 83 avoidance, provides a realistic and ecologically relevant context for studies of orientation and
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56 84 navigation.
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4 85 Several studies of hummingbirds, rufous hummingbirds in particular, have demonstrated
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7 86 that they distinguish a rewarded flower from other nearby flowers primarily in terms of spatial
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9 87 location rather than the visual features of each flower (Hurly and Healy 2002, Miller et al. 1985).
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11 88 Spatial locations seem to be remembered relative to nearby objects (Healy and Hurly 1998,
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14 89 Hurly et al. 2010), a process that must, by definition, employ aspects of geometric
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16 90 representation. However, the identity and use of such natural landmarks remains elusive. One
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18 91 solution to this problem is to provide artificial flowers and conspicuous landmarks that can be
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20 92 systematically manipulated in order to assess how objects are combined and encoded to represent
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22 93 relevant information about the environment.

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26 94 Here we ask how wild, free-living hummingbirds presented with a four-flower
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28 95 rectangular array employ nearby visual cues and array geometry, and whether their use of these
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30 96 cues parallels the results from laboratory experiments conducted on a similar spatial scale. After
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32 97 the birds learned the location of the rewarded flower, we manipulated conspicuous nearby
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34 98 landmarks to determine whether the birds had incorporated these landmarks into their memory
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36 99 for the reward and whether they had also learned the geometry of the array. The strongest
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38 100 evidence for geometry would be if, in a test, the birds were to choose frequently the flower
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40 101 diagonally opposite to the rewarded flower.

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47 103 **Materials and Methods**

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50 104 The study was performed during June and July, 2007 – 2009 at the University of Lethbridge
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52 105 Westcastle Research Station (49°20.9'N, 114°24.6'W, 1400m elevation) in the front ranges of
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54 106 the Rocky Mountains in southwestern Alberta, Canada. The subjects were male rufous
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56 107 hummingbirds, each defending a territory surrounding a commercial hummingbird feeder
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4 108 containing 14% sucrose solution. Individual birds were with non-toxic ink on the breast feathers.

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7 109 Six subjects were studied in 2007, eight in 2008 and ten in 2009.

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9 110 Study sites were openings in the forest at least 200 m² in size and vegetated with green
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11 111 grass, forbs and shrubs less than 40 cm in height. Within the study sites were naturally occurring
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13 112 objects such as logs, rocks and soil disturbances, as well as clumps of vegetation of different
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15 113 shades of green. At medium distances were trees and forest edges, with ridges, mountains and
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17 114 sky visible at greater distances (Fig. 1). Experimental control of visual features on any of these
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19 115 scales was not possible.
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24 117 Experiment 1

25 118 Initial Training

26 119 A subject's feeder was removed during training and testing but was available at all other times.

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28 120 First, a subject was trained to feed on 25% sucrose from an artificial flower consisting of a vial
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30 121 that was taped to the top of a 62cm wooden dowel that projected visibly above the surrounding
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32 122 vegetation. The flower was then moved a few metres at a time away from the original feeder
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34 123 location until the bird flew directly to the flower each time it came to feed.
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44 125 Experimental Training

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46 126 We presented an array of four identical flowers in a rectangular pattern. One flower was
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48 127 randomly selected as the reward and this was cued by a conspicuous artificial landmark
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50 128 consisting of a red cube, constructed of cardboard and duct tape, atop a 62cm dowel. The cube
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52 129 was positioned outside of the array at an angle of 45° to the corner of the rectangle and at a
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54 130 distance of 5cm from the reward flower. Each of the remaining flowers was filled with water,
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4 131 which the hummingbirds find distasteful. A subject approached the array to feed and probed
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7 132 flowers until he found the reward, fed to satiation and then left. The flowers were then
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9 133 exchanged with each other to ensure that the bird could not learn the reward flower based upon
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11 134 its subtle visual features. The flower at the reward location was filled with sucrose and the
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14 135 others with water. Training occurred until the subject flew directly to the reward flower for 8
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16 136 consecutive feeding visits and at this point we conducted a Test Probe to assess what information
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19 137 the subject was employing to return to the reward flower. In all cases a choice was defined as
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21 138 the bird inserting its bill into a flower. Following the Test Probe the array was moved to a new
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24 139 orientation and location that did not overlap spatially with the previous array and a new series of
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26 140 training trials began.

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31 142 Test Probes32
33 143 During a Test Probe the array remained in the same location but the flowers were exchanged,
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36 144 each was filled with water and no flower was rewarded. A probe involved manipulation of the
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38 145 landmark in one of three ways (Fig. 2a):
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41 146 1) Diagonal – The landmark was moved to the diagonally opposite corner. A bird could use both
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43 147 landmark and geometric information to visit the flower now cued by the landmark.44
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46 148 2) Removal – The landmark was removed. A bird could use only geometric information about
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48 149 the long and short spacing of the flowers in the array and was expected to visit either the original
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50 150 location or the location diagonally opposite. It was also possible for the bird to use natural visual
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53 151 cues that were not under experimental control.
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4 152 3) Conflict – the landmark was shifted along the adjacent short side of the array to create a
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7 153 conflict between geometric information and the landmark. The bird was expected either to
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9 154 follow the landmark or to go to one of the two geometrically-correct flowers.

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11 155 As they were free-living, the hummingbirds were not under our direct control, hence they
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14 156 determined the time interval between feeding visits (presumably based on hunger). Further, we
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16 157 could not physically disorient the birds as is done in laboratory tests by using a rotating turntable
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18 158 (e.g. Kelly 2010). However, during the ca. 10 minutes between visits to the array birds engaged
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21 159 in multiple activities: vigilance, preening, territorial chases, courtship displays (see Hurly et al.
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24 160 2001), hawking insects. Moreover, these multiple activities caused the birds to approach the
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26 161 array from different directions. Thus, the birds' natural behaviours in the wild considerably
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29 162 reduce the possibility that they found the reward through stereotypical approach paths, thus
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31 163 acting in a similar fashion to experimental disorientation used in the lab (e.g. by rotation,
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33 164 entering arena through different doors). Further, altering the experimental landmark by changing
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36 165 its normal relationship with other cues in the environment may also have acted as a surrogate for
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38 166 disorientation by creating conflicting information. A subject's choice during a Test Probe should
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41 167 reveal whether it was relying most on the experimental landmark, the geometry of the array, or
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43 168 other cues in the environment that were not under experimental control.

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47 48 170 Experimental Training Treatments

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51 171 In 2007, six subjects were trained with both Small Arrays (10x20cm) and Large Arrays
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53 172 (60x120cm) using a large landmark (see below) and for each array size they were tested with
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55 173 each Test Probe: Diagonal, Removal and Conflict. The order of Test Probes was selected
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58 174 randomly from an unbiased schedule. In 2008, eight subjects were trained under four conditions
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4 175 in which array size (Small vs. Large as above) was crossed with landmark size (Small: 5cm per
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7 176 side vs. Large: 10cm per side). The order of Test Probes was randomized as above.
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10 11 178 Experiment 2

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14 179 In 2009, we studied 10 territorial male rufous hummingbirds from the same population as

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16 180 Experiment 1. All training methods were the same, including the learning criterion of 8 first

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18 181 visits to the reward flower prior to Tests. The rectangular array was 50x100cm and the single

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21 182 reward flower was cued by two red cubes (10cm per side), one at 5cm (Near) and one at 100cm

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24 183 (Far) (Fig. 3a).
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27 28 185 Test Probes

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31 186 The Test Probes were: Remove Near, Remove Far, Remove Both, Conflict Near and Conflict Far

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33 187 (Fig. 3b). As with Experiment 1, each subject received each Test Probe only once, with the

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36 188 order of presentations selected randomly from an unbiased schedule.
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43 191 We analysed the choices birds made during Test Probes using G-tests (with William's correction

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46 192 G_{adj}), either comparing observed choices with the expectation of chance performance across the

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48 193 four flowers, or comparing choices between training treatments or Test Probes. When the

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51 194 sample size was smaller than 20 the expectation for any cell is less than the critical value of 5. In

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53 195 these cases we also employed randomization tests (R_p with 10,000 permutations) to determine

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55 196 the probability of occurrence of the observed and more extreme results, as recommended by

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58 197 Sokal and Rohlf (1995). We report the results of both G_{adj} and R_p . In every case the two tests
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4 198 were in agreement relative to the assessment of statistical significance ($\alpha = 0.05$). We report
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7 199 data as mean \pm SE.
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10 11 201 **Results**

12 13 14 202 Experiment 1

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19 204 The birds achieved the criterion of eight consecutive visits to the rewarded flower within $10.8 \pm$
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21 205 0.4 trials. Learning rate did not differ between years (2007, 11.2 ± 0.5 trials; 2008, 10.4 ± 0.5
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23 206 trials; $t = 1.405$, $df = 12$, $p = 0.185$), nor was it affected by Array Size or Landmark Size (Array:
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25 207 $F_{1,5} = 1.874$, $p = 0.229$; Landmark: $F_{1,5} = 0.241$, $p = 0.883$, Interaction: $F_{1,5} = 0.678$, $p = 0.448$).
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29 208 The mean inter-trial interval (9.8 ± 0.3 min) did not vary by year ($F_{1,12} = 1.278$, $p = 0.280$).
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31 209 Inter-trial intervals were not influenced by trial type (Training vs. Test), nor by Array Size or
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33 210 Landmark Size (all $F_{1,7} < 0.247$, all $p > 0.163$). Given that we found no differences between
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35 211 years in task acquisition or inter-trial intervals, we felt confident in combining data from 2007
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37 212 and 2008 in Experiment 1.
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42 43 214 Test Probes

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45 215 When we combined data across the different array and landmark sizes it was evident that the
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47 216 three different Test Probes elicited significantly different patterns of choices (G-test of
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49 217 independence, $G_{adj} = 82.48$, $N = 129$, $p < 0.001$, Fig. 2b). Furthermore, choices within each Test
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51 218 Probe were significantly different from chance. In the Diagonal tests the birds' choices were
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53 219 concentrated on the flower diagonally opposite the reward and thus were consistent with the use
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55 220 of the landmark or geometry ($G_{adj} = 26.40$, $N = 43$, $p < 0.001$). In the Removal tests the birds'
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4 221 choices were mostly to the rewarded location ($G_{adj} = 22.99$, $N = 43$, $p < 0.001$), with no evidence
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6 222 that they used geometry. If birds had relied upon geometry then choices should have been
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8 223 divided equally between the reward location and the flower diagonally opposite; instead they
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10 224 were biased to the reward location (Binomial test, $p < 0.001$, $N = 29$, $R_p = 0.003$). Even
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12 225 examination of choices to the three less-preferred flowers showed no preference for the flower
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14 226 diagonally opposite the reward ($G_{adj} = 1.29$, $N = 17$, $p = 0.26$, $R_p = 0.27$). During the Conflict
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16 227 tests birds most frequently followed the landmark ($G_{adj} = 54.17$, $N = 43$, $p < 0.001$). Other
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18 228 choices were significantly in favour of the reward location with no evidence for geometry ($G_{adj} =$
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20 229 9.40 , $N = 13$, $p = 0.002$, $R_p = 0.001$).

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26 230 The sample sizes were insufficient to consider the effects of array size and landmark size
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28 231 simultaneously so we examined each separately (Fig. 2c, d). Birds exhibited significant non-
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30 232 random choices in 11 of the 12 Test Probe conditions. In the Diagonal and Removal tests, birds
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32 233 chose the original reward location most often when the array was large (Diagonal: $G_{adj} = 12.53$,
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34 234 $N = 43$, $p < 0.001$; Removal: $G_{adj} = 8.31$, $N = 43$, $p < 0.001$) but they did not do this in the
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36 235 Conflict tests ($G_{adj} = 6.57E-02$, $N = 43$, $p = 0.80$). Landmark size had a significant effect on
37
38 236 choices in Removal tests ($G_{adj} = 4.52$, $N = 31$, $p = 0.033$); birds returned to the reward location
39
40 237 most often when the landmark was small. There was no effect of landmark size in the Diagonal
41
42 238 ($G_{adj} = 2.52$, $N = 31$, $p = 0.11$) or Conflict ($G_{adj} = 1.48$, $N = 31$, $p = 0.22$) tests.

43 44 45 46 47 48 239 49 50 240 Experiment 2

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52 241 Results from Experiment 1 indicated that birds followed the experimental landmark but that they
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54 242 also used other cues to return to the reward location when the experimental landmark had been
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56 243 removed. We introduced a second conspicuous experimental landmark in Experiment 2 as an
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4 244 attempt to increase their attention to the experimental landmarks and to decrease their attention
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7 245 to other, natural landmarks in the environment.
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11 247 Training

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14 248 The number of trials required to reach criterion in Experiment 2 (11.8 ± 0.4) did not differ from
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16 249 Experiment 1 (10.8 ± 0.4 , $t = 1.570$, $df = 22$, $p = 0.131$). The mean inter-trial interval was $9.8 \pm$
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18 250 1.8 minutes.
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24 252 Test Probes

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26 253 When we removed only one landmark, the birds primarily chose the reward location in both
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28 254 Remove Near ($G_{adj} = 3.95$, $N = 10$, $p = 0.047$, $R_p = 0.019$) and Remove Far ($G_{adj} = 10.78$, $N =$
29
30 255 10, $p < 0.001$, $R_p < 0.001$) tests and these results did not differ from each other ($G_{adj} = 2.83$, $N =$
31
32 256 20, $p = 0.092$; Fig. 3b). However, removal of both landmarks seemed to disrupt orientation and
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35 257 choices did not differ from chance ($G_{adj} = 2.08$, $N = 10$, $p = 0.149$, $R_p = 0.236$). Choices differed
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37 258 significantly across the three types of removal tests ($G_{adj} = 6.73$, $N = 30$, $p = 0.009$) and in no test
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39 259 did birds prefer to use geometry.
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43 260 In Near Conflict tests most of the birds followed the landmark ($G_{adj} = 9.39$, $N = 10$, $p =$
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45 261 0.002, $R_p < 0.001$). In contrast, in the Far Conflict tests most of the birds chose the near
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47 262 landmark at the reward location ($G_{adj} = 9.39$, $N = 10$, $p = 0.002$, $R_p < 0.001$). These choice
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49 263 distributions differed significantly from each other ($G_{adj} = 7.23$, $N = 20$, $p = 0.007$; Fig. 3c).
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51 264 Birds never chose the flower diagonally opposite the reward location and thus we found no
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53 265 evidence for the use of geometry.
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4 **267 Discussion**

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7 268 In these experiments, wild, free-living male rufous hummingbirds learned the location of a single
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9 269 rewarded flower in a rectangular array of four flowers when one or two conspicuous
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11 270 experimental landmarks cued the reward. To determine what information the birds used to
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14 271 remember the location of the reward, we manipulated the landmarks in occasional Test Probes.
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16 272 In 18 of 20 comparisons the birds' first flower choices indicated significant patterns about where
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19 273 they expected the reward to be. It is clear that the birds attended to the experimental landmarks
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21 274 because they often followed the landmarks when they were moved to a different location in the
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24 275 array (Diagonal or Conflict). When we removed the landmarks the birds most often returned to
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26 276 the rewarded flower, which indicates that they also used cues from the environment over which
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29 277 we had no control. There was no evidence that the hummingbirds recognized or used the
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31 278 geometry of the rectangular array to remember the location of the rewarded flower. To our
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34 279 knowledge, this is the first test of the use of rectangular geometry by wild animals in the field
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36 280 and the results do not parallel those from numerous lab studies.

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38 281 The Diagonal test aligned geometric and landmark information and thus acted as a
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41 282 positive control demonstrating that the birds both responded to Test Probes and paid attention to
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43 283 the experimental landmarks. This test cannot however, distinguish between the use of landmarks
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46 284 vs. geometry. The Removal test was the condition in which we could best detect the use of
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48 285 geometry with the expectation of equal choices to the reward and the flower diagonally opposite
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51 286 the reward. Surprisingly, the birds chose the diagonally opposite flower least frequently, soundly
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53 287 rejecting the exclusive use of array geometry in this task. Finally, in the traditional test that is
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56 288 used to determine whether the landmark or geometry has the greater influence on learning the
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58 289 reward location, the Conflict test, the birds also failed to choose the flower specified by
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4 290 geometric cues. Additional cues that may have been used in conjunction with the geometry of
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7 291 the array are discussed below.
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9 292 Given the ubiquity of positive geometry results in the laboratory for various species, it is
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11 293 surprising and intriguing that we found no evidence that hummingbirds recognized the geometry
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14 294 of the rectangular array. To make sense of these results we must distinguish between two related
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16 295 but different questions, the first being whether hummingbirds can form geometric representations
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19 296 of our experimental flowers. The answer to this is yes: hummingbirds most certainly can learn
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21 297 and recognize the geometry of an array of artificial flowers. Healy and Hurly (1998) presented
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24 298 wild male rufous hummingbirds in this same population with an array of five artificial flowers
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26 299 arranged in a cross pattern and in which only the centre flower was rewarded. Once a bird
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29 300 learned which flower contained the reward, the array was translocated one flower-spacing unit
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31 301 such that upon return the bird's flower choice would indicate that it thought the reward should be
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33 302 in the flower currently in the actual spatial location previously occupied by the reward or that the
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36 303 reward should be in the centre of the array (relative position). When the arrays were composed
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38 304 of flowers with relatively wide spacing (80, 160, 320cm) the birds selected the flower in the
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41 305 absolute spatial location. In contrast, when flower spacing was relatively small (5, 10, 20 ,
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43 306 40cm) the birds selected the centre flower, indicating that they recognized geometric
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46 307 relationships between the flowers within the array. This effect of flower spacing on the use of
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48 308 geometric relationships between flowers was also obtained in more complex arrays of 16 flowers
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51 309 (Healy and Hurly 1998).
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53 310 Because wild hummingbirds can indeed recognize and use at least some aspects of the
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55 311 geometry of an array of flowers, a second question attains relevance: under what circumstances
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58 312 do wild foraging hummingbirds employ geometry? Healy and Hurly (1998) speculated that
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4 313 when presented with compact arrays, hummingbirds use non-rewarded flowers as landmarks to
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7 314 remember the rewarded flowers but when presented with dispersed arrays they use natural,
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9 315 nearby landmarks. From the previous data it seems reasonable to infer that these natural
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11 316 landmarks were generally less than 80 cm from the reward. The results of the current
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13
14 317 experiment are consistent with this inference. First, during the Diagonal tests in Experiment 1
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16 318 (Fig. 2c), the hummingbirds almost ignored the reward location when the array was small
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19 319 (10x20cm), but not when it was large (60x120cm), differences that are consistent with the 40 vs.
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21 320 80 cm spacing threshold reported by Healy and Hurly (1998). Second, when landmark size was
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24 321 manipulated (Fig. 2d) and birds experienced Removal tests, they returned less often to the reward
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26 322 location when the landmark had been large than when it had been small, suggesting differential
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29 323 attention between the experimental and natural landmarks. Third, in Experiment 2 the birds were
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31 324 influenced more strongly by the near (5cm) than by the far (100cm) landmark (Fig. 3c). Thus it
32
33 325 seems reasonable to hypothesize that wild hummingbirds remember the locations of one or more
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36 326 rewarded flowers in relation to the locations of nearby objects (landmarks) and that these
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39 327 landmarks can be other nearby flowers. It is notable that removal of both landmarks in
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41 328 Experiment 2 seriously disrupted choices, suggesting that the two experimental landmarks
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43 329 together played a significant role in memory for the reward location.

44
45 330 Such reliance upon landmarks (natural or experimental) is consistent with the results of
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47
48 331 past studies. Hummingbirds seem to remember rewards in terms of spatial locations (absolute or
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51 332 relative) rather than distinctive visual features of rewarded flowers but they will employ such
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53 333 visual features when spatial cues are made ineffective (Hurly and Healy 2002). Moreover, when
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55 334 Hurly et al. (2010) trained hummingbirds to feed from a single conspicuous rewarded flower and
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58 335 after several flights to the rewarded flower it was either removed or moved approximately 1.5m,
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4 336 birds returned to the original reward location. This demonstrated that they had not used the
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7 337 visual features of the flower as a distant beacon but rather as a visual cue only when they were
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9 338 very close to its location. It seems likely that the birds recognized the rewarded location using
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11 339 natural, nearby landmarks and recent evidence indicates that such learning of rewarded locations
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14 340 occurs with a single experience (Flores-Abreau et al. 2012).

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16 341 The methods and scale of our field study paralleled the methods and scale of a host of
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19 342 laboratory studies testing whether animals encode the geometric properties of rectangular
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21 343 enclosures or arrays of objects and then later use this information to reorient and return to a goal.
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24 344 The hummingbirds may have encoded geometry but they showed no evidence of using it to find
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26 345 the goal, even when the conspicuous landmarks were removed. Aside from following the
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29 346 experimental landmark, the birds' most common choice was the flower location that had been
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31 347 rewarded in training, for which they must have used other spatial cues. One possibility is that
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33 348 they navigated to the absolute spatial location of the goal flower by using visual landmarks in the
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36 349 environment that were not under experimental control. Objects conspicuous to the human eye,
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39 350 such as logs, rocks, soil disturbances and shrubs are obvious candidates. Consistent with this
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41 351 idea, rats tested in small rectangular enclosures generally avoided diagonal errors when they
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43 352 were permitted views of the surrounding environment (Margules and Gallistel 1988). The other
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46 353 possibility was that the birds encoded the flowers in the array as a group and then used some sort
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48 354 of directional cues to represent which one of the flowers was the reward (e.g. the flower closest
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51 355 to a landmark, the flower farthest north). Candidate directional cues include magnetic (Freire et
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53 356 al. 2005) or sun compass (Wiltschko et al. 1999), asymmetry in the panoramic view of the
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56 357 landscape such as a distant mountain (Wystrach et al. 2011), or even the slope of the ground
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58 358 (Nardi et al. 2010). Using natural visual landmarks, in addition to our experimental landmarks,
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4 359 requires the encoding of geometric properties such as sense, direction and distance. Similarly,
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7 360 using directional cues requires the encoding of, at the very least, distance relationships between
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9 361 the array elements and a compass direction. Thus, we can conclude only that our tests did not
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11 362 show that the hummingbirds placed high priority on using the geometry of the rectangular array
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14 363 to orient to the reward and that they used other cues instead. We consider the use of idiothetic
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16 364 mechanisms in this case to be unlikely because the minimum flight distance to the array was
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19 365 more than 10 times the maximum length of the array (1.2m). One final consideration is that it
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21 366 may require severe disorientation of the subjects to get them to reveal their use of geometry and
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24 367 such disorientation was not possible in this field study with free-living birds. However, unlike
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26 368 laboratory experiments in which the subjects sit in a holding cage during intervals between trials
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29 369 and tests, the wild hummingbirds spent the 10-minute intervals engaged in vigilance, territorial
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31 370 chases, courtship flights, capturing insects, etc. Thus, birds frequently approached the array from
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34 371 different directions between trials. These activities are very likely to have provided some degree
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36 372 of disorientation or interference with learned information.

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38 373 Cheng's (1986) original study demonstrating that rats encoded the geometry of a small
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41 374 room even when a distinctive visual feature, which could act as a beacon, cued the location of
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43 375 the reward, has spawned a substantial assortment of laboratory studies with other species that
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46 376 demonstrate similar results (e.g. fish: Brown et al. 2007, Sovrano et al. 2005; chicks: Chiandetti
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48 377 and Vallortigara 2008; pigeons: Kelly and Spetch 2001). These studies consistently show that
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51 378 the subjects can encode rectangular geometry but, unlike Cheng (1986), most indicate that when
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53 379 geometry and visual features are placed in conflict, features frequently play a greater role. Here
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55 380 we again face the issue of what specific question we are addressing; whether we wish to know
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4 381 that animals are capable of learning the geometry of small enclosures or whether we wish to
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7 382 know under what circumstances animals encode and rely upon geometry.
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9 383 Some evidence suggests that use of visual features vs. geometry is related to proximity.
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11 384 In both mountain chickadees (Gray et al. 2005) and goldfish (*Carassius auratus*) (Vargas et al.
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13 385 2011), visual features dominated geometry when subjects were trained with the feature proximal
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15 386 to the reward but no clear dominance of either cue occurred when subjects were trained with the
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17 387 feature distant from the reward. Thus, it is difficult to draw general conclusions about the overall
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19 388 influence of overshadowing or salience on the relative weighting of visual features and geometry
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21 389 because results seem specific to training conditions (Kelly et al. 1998, Brown et al. 2007).
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24 390 Although most laboratory studies have examined whether animals learn the geometry of
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26 391 enclosures, several have examined whether they learn the geometry of a rectangular array of
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28 392 discrete objects. Gibson et al. (2007) tested rats and Kelly (2010) tested Clark's nutcrackers. In
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30 393 both studies subjects did learn about the geometry of the array, but the array was moved between
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32 394 each training trial to make global cues in the room ineffective. Rats' learning was dominated by
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34 395 the unique features of the objects and they learned geometry best when the objects were made
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36 396 identical. In contrast, nutcrackers did not learn the location of the reward unless features were
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38 397 individually distinctive, and in learning the task they also acquired the geometry of the array. As
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40 398 with this hummingbird study, when the reward feature was placed in conflict with the geometry
41
42 399 of the array the nutcrackers followed the feature. A series of experiments with chicks (ca. 3-14
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44 400 days of age) indicate that the geometry of enclosures is encoded much more readily than is the
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46 401 geometry of an array of objects (e.g. Pecchia and Vallortigara 2010). Conversely, chicks could
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48 402 encode the geometry of a rectangular array of objects but only when their view of the array was
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50 403 carefully controlled (Pecchia and Vallortigara 2012). This finding suggests that view-matching
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4 404 is very important for young chicks and it would be interesting to determine whether it is
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7 405 necessary for older birds that have greater experience navigating in a complex environment. The
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9 406 issue is further complicated by evidence that view-matching is acquired during training whereas
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11 407 spontaneous reorientation in chicks employs geometric 3-dimensional properties of the enclosure
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14 408 (Lee et al. 2012a). Similarly, fish may spontaneously reorient by the geometry of walls but
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16 409 favour landmarks following training (Lee et al. 2012b), and they did not encode the geometry of
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19 410 the corners of an enclosure that were emphasized as objects rather than as the intersections of
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21 411 walls (Lee et al. 2013).

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24 412 As Kelly (2010) suggests, animals may regard the rectangular geometry of enclosures or
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26 413 edges differently than they regard the rectangular geometry of discrete objects (points).
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29 414 Certainly, animals in the laboratory frequently encode reward locations in terms of distance from
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31 415 a straight edge (Cheng and Sherry 1992, Gray et al. 2004). Alternatively, there may be
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33 416 something special about an animal being contained within an enclosure that makes the walls and
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36 417 corners particularly salient and which are then incorporated into a geometrical representation of
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39 418 the environment. Perhaps some of the objects within a rectangular array of discrete objects can
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41 419 be ignored or weighted less heavily than others, whereas the restrictive nature of a small
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43 420 enclosure forces animals to regard walls as extremely salient (Sutton 2009).

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46 421 Finally, the degree to which animals attend to rectangular geometry may relate to the
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48 422 degree to which the learning task is ecologically relevant or natural. In the least natural
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51 423 situations, small laboratory enclosures, animals readily learn rectangular geometry but in the
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53 424 most natural situation, four artificial flowers in a rectangular array in the field, our hummingbirds
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55 425 showed no evidence of having done so. It is interesting to note that in an intermediate situation,
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58 426 four objects in a large arena, Clark's nutcrackers did learn about geometry of an array but only
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4 427 when the objects were visually distinctive (Kelly 2010). Using fish, Sovrano et al. (2005)
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7 428 showed that subjects trained in a small tank were slightly better at geometry and tended to make
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9 429 errors about visual cues, whereas fish trained a large tank were more likely to make errors about
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12 430 geometry, supporting the idea that some aspects of containment might influence which objects
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14 431 are included in a cognitive spatial representation of the environment. Although containing
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16 432 animals in small rooms is highly artificial, the spatial scale is ecologically realistic. Although the
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19 433 territories of rufous hummingbirds are on the order of 1 ha and they must orient and navigate on
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21 434 that spatial scale, they also experience flowers separated by only a few centimetres and
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24 435 experiments with artificial flowers indicate that they discriminate between flowers separated by 5
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26 436 cm or less (Healy and Hurly 1998; Hurly and Healy 1996). Future research should focus on
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29 437 how and when animals form these complex spatial representations during their natural activities
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31 438 in the wild and what ontological and evolutionary conditions influence this process.

32
33 439

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44
45
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48 445

49 50 446 **Ethical Standards**

51
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53 447 This research was conducted with the approval of the University of Lethbridge Animal Welfare
54
55 448 Committee, meeting the standards of the Canadian Council on Animal Care, and under permits
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57
58 449 from the Canadian Wildlife Service and Alberta Sustainable Resource Development.

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451 **Conflict of Interest**

452 None of the authors have conflicting financial relationships with any of the funding or approval
453 agencies associated with the research reported here.

454

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4 **550 Figure Captions**

5
6
7 **551 Fig. 1** An example of one of the study sites. Visual cues outside of experimental control were
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9 **552** available in the immediate area of the experimental array (see foreground), in the intermediate
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11 **553** distance (trees and forest edge), and in the far distance (ridges and mountains).
12
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14 **554**

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16 **555 Fig. 2** Experiment 1. a) Positions of flowers and the landmark during training. Note that the
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19 **556** relative position of the rewarded flower was assigned randomly. For convenience, the results are
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21 **557** presented as if the rewarded flower was always flower number 1. b) Choices to flowers during
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23
24 **558** the Test Probes for all data combined. c) Choices to flowers during Test Probes separated by
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26 **559** array size. d) Choices to flowers during Test Probes separated by landmark size. Asterisks
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28
29 **560** within an array identify significance levels for choices between flowers. Asterisks between
30
31 **561** arrays indicate significance levels for comparisons between arrays. ns not significant; * $p <$
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33 **562** 0.05; ** $p < 0.01$; *** $p < 0.001$
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36 **563**

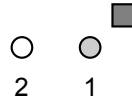
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38 **564 Fig. 3** Experiment 2. a) Positions of flowers and the two landmarks during training. b) Choices
39
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41 **565** to flowers during Test Probes in which landmarks were removed. c) Choices to flowers during
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43 **566** Test Probes in which landmarks were moved into conflict positions. Asterisks within an array
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45
46 **567** identify significance levels for choices between flowers. ns not significant; * $p < 0.05$; ** $p <$
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48 **568** 0.01; *** $p < 0.001$
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Figure
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Figure

a. Training Array

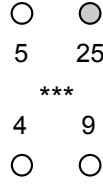


b. Combined Data

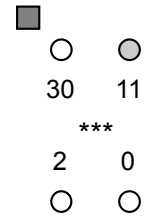
Diagonal



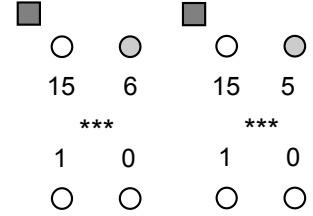
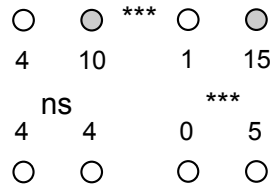
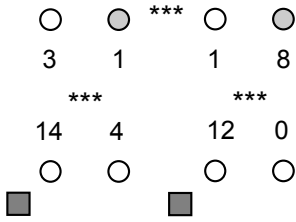
Remove



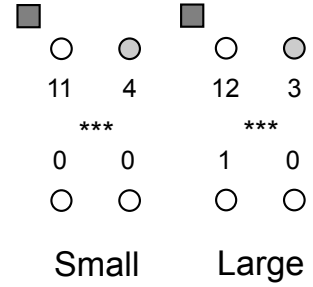
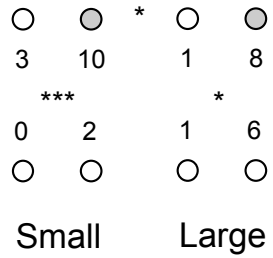
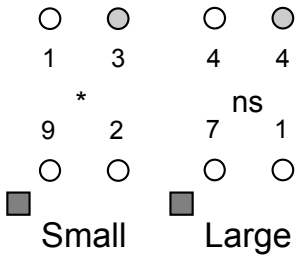
Conflict



c. Array Size

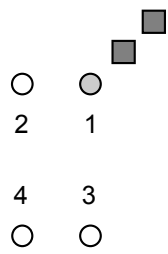


d. Landmark Size

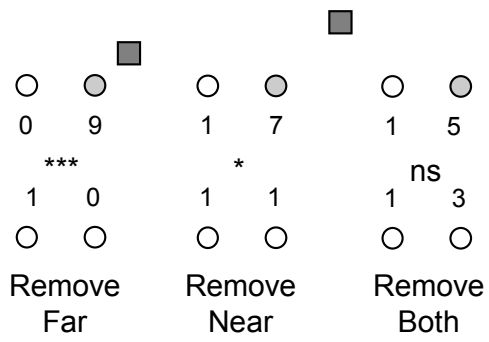


Figure

a.



b.



c.

