

ORIGINAL ARTICLE

Zero-dimensional polariton laser in a subwavelength grating-based vertical microcavity

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Semiconductor exciton–polaritons in planar microcavities form coherent two-dimensional condensates in non-equilibrium. However, the coupling of multiple lower-dimensional polariton quantum systems, which are critical for polaritonic quantum device applications and novel cavity-lattice physics, has been limited in conventional cavity structures. Here, we demonstrate full non-destructive confinement of polaritons using a hybrid cavity composed of a single-layer subwavelength grating mirror and a distributed Bragg reflector. Single-mode polariton lasing was observed at a chosen polarization. The incorporation of a designable slab mirror in a conventional vertical cavity, when operating in the strong-coupling regime, enables the confinement, control and coupling of polariton gasses in a scalable fashion. This approach may open the door to experimental implementations of polariton-based quantum photonic devices and coupled cavity quantum electrodynamic systems.

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INTRODUCTION

Semiconductor microcavity exciton–polaritons¹ have recently emerged as a unique, open system for studying non-equilibrium quantum order.^{2–4} Exciton–polaritons are formed *via* strong coupling between excitons and photons. Due to the excitonic component, the polaritons are massive, weakly interacting quasiparticles that feature strong nonlinearity and rich many-body physics.⁵ By mixing with the photon, polaritons have an effective mass that is 10^{-8} of the hydrogen atomic mass, and they are relatively insensitive to disorder or localization potentials in the active media. Hence, polaritons exhibit quantum coherence over macroscopic scales with high critical temperatures. Polaritons in quantum-well microcavities couple out of the cavity at a fixed rate while conserving the energy and in-plane wave-number, providing direct experimental access that is unavailable in typical many-body quantum systems. Hallmarks of non-equilibrium condensation and superfluidity have been widely observed in isolated two-dimensional (2D) polariton systems (Ref. 3 and the references therein).

Foundational work on 2D polariton systems has inspired theoretical schemes for polariton-based quantum circuits,^{6–8} quantum light sources^{9–12} and novel quantum phases.⁴ Experimental implementation of these schemes requires the control, confinement and coupling of polariton systems, which remain challenging in conventional microcavity structures. Important features of a versatile experimental platform based on polaritons include: first, well-defined zero-dimensional (0D) polaritons as building blocks of a coupled system; second,

the establishment (i.e., survival) of a non-equilibrium quantum phase in each 0D polariton cell, typically manifested as polariton lasing; third, controllable coupling among the 0D cells; fourth, individual addressability and control of each cell.

In conventional polariton cavities, the thick mirrors, consisting of distributed Bragg reflectors (DBRs), make it difficult for the polaritons to be confined or controlled beyond the perturbative regime. Most existing methods for controlling polaritons lead to a weak modulation potential that modifies the system's properties without reducing its dimensionality from 2D to 0D. Examples include weak confinement of excitons *via* mechanical strain¹³ and periodic modulation of the optical modes *via* surface patterning.^{14,15} Advanced techniques have been developed to embed apertures inside the cavity,^{16,17} which have led to 0D polariton cells, but polariton lasing has not been reported thus far. Alternatively, 0D polariton systems have also been produced *via* direct etching of the vertical cavity into pillars.^{18–21}

Using this method, two groups have recently achieved polariton lasing in pillars,^{22–24} thus satisfying the first two requirements. However, this approach requires destructive plasma etching throughout the 4- to 6- μm -tall cavity structure as well as the active media layers, which precludes coupling between separate pillars. It is also unclear whether further control of the polariton modes in each pillar would be possible.

In this work, we demonstrate a polariton system in an unconventional cavity that can fulfill all four requirements. The new cavity structure replaces the top DBR with a slab of photonic crystal (PC) (Figure 1), which enables confinement and control of the polariton modes by

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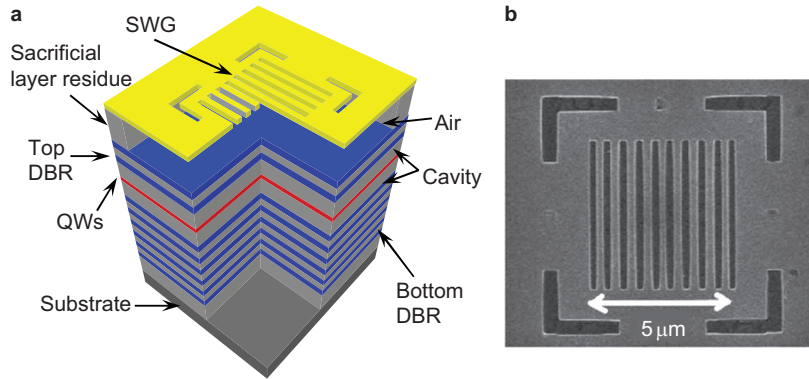


Figure 1 Examples of the hybrid cavity. (a) A schematic of a 0D hybrid cavity with a SWG mirror. (b) Top-view SEM image of a fabricated OD cavity with a SWG of $5\ \mu\text{m} \times 5\ \mu\text{m}$ in size. OD, zero-dimensional; SEM, scanning electron microscopy; SWG, subwavelength grating.

design.^{25–27} At the same time, there is no destructive interface in the active media layers or the main cavity layers; hence, coupling among multiple low-dimensional polariton cells is unhindered. Using this cavity system, we demonstrate 0D polariton lasing at a chosen polarization.

MATERIALS AND METHODS

A schematic of our hybrid cavity polariton device is shown in Figure 1a. To fabricate the device, we first grew the planar structure by molecular beam epitaxy on a GaAs substrate, consisting of 30 pairs of bottom DBR, an AlAs $\lambda/2$ cavity layer, 2.5 pairs of top DBR consisting of $\text{Al}_{0.15}\text{GaAs}/\text{AlAs}$, and an $\text{Al}_{0.85}\text{GaAs}$ sacrificial layer followed by an $\text{Al}_{0.15}\text{GaAs}$ top layer. There are 12 GaAs quantum wells distributed in the three central antinodes of the cavity. We created square gratings of $5\text{--}8\ \mu\text{m}$ in length (Figure 1b) on the top

layer *via* electron-beam lithography followed by a short plasma etching step. Hydrochloric acid chemical etching was then applied to remove the sacrificial layer, followed by critical point drying. The fabricated gratings are approximately 80 nm thick, with a period of approximately 520 nm and a duty cycle of approximately 40%, and are suspended over an air gap of approximately 300 nm. The gratings are optimized as a high-reflectance mirror for light polarized along the grating bar direction (transverse electric (TE)-polarization). Figure 1b shows a scanning electron microscopy image of the top view of one of the devices.

Optical measurements were performed to characterize the properties of the cavity system. For consistency, all data shown were taken on a device of $7.5\ \mu\text{m} \times 7.5\ \mu\text{m}$ in size. The sample was kept at $10\text{--}90\ \text{K}$ in a continuous flow liquid-helium cryostat. A pulsed Ti:sapphire laser

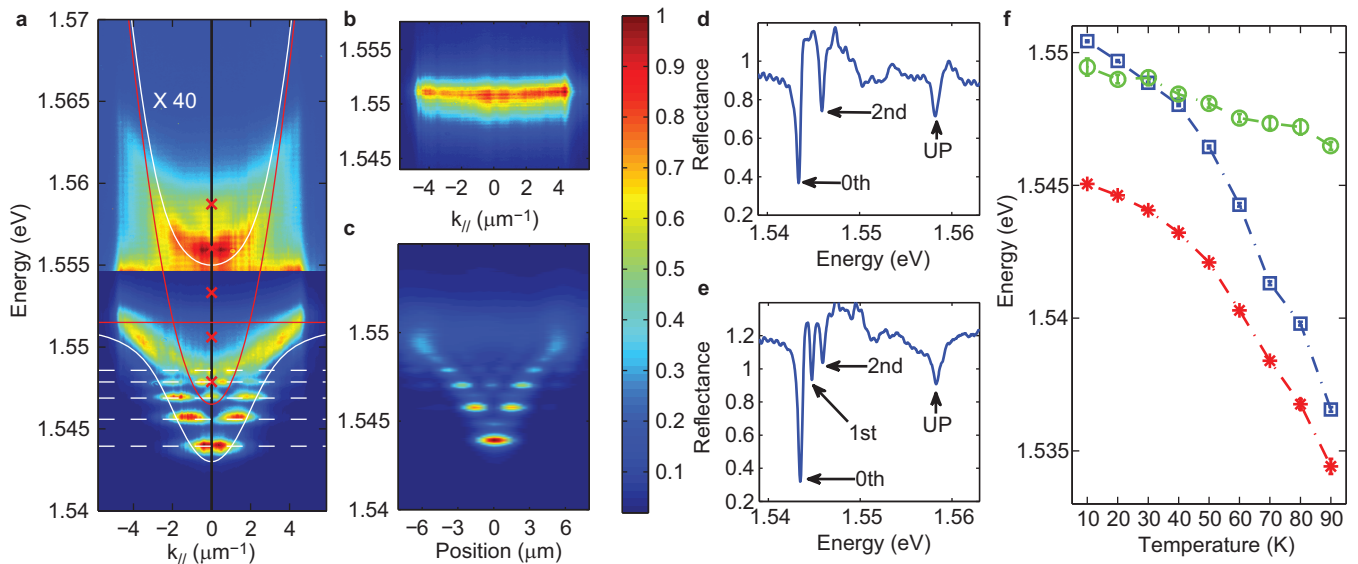


Figure 2 Spectral properties of a 0D polariton device. (a) Spectrally resolved momentum space image of the PL from a 0D cavity, which shows discrete LP modes and an UP mode. To clearly show the UP mode, the intensity of the upper panel is magnified by $40\times$ compared to the lower panel. The straight red line at 1.551 eV corresponds to the independently measured exciton energy. The other solid lines are the calculated dispersions of the LP, UP and uncoupled cavity. The white dashed lines and the crosses (X) mark the position of the calculated discrete LP and cavity energies, respectively. (b) Spectrally resolved momentum space images of the exciton PL, measured from the unprocessed part next to the SWG-DBR cavity. (c) Spectrally resolved real space image of the PL from the OD cavity, showing the spatial profile of the discrete LP modes. (d–e) Reflectance spectra of the OD cavity measured from (d) the normal direction and (e) 3.5° from the normal direction, both with an angular resolution of 0.27° . (f) Temperature dependence of the LP (stars), exciton (squares) and cavity resonances (circles). OD, zero-dimensional; DBR, distributed Bragg reflector; LP, lower polariton; PL, photoluminescence; SWG, subwavelength grating; UP, upper polariton.

at 740 nm was used as the excitation laser, with an 80-MHz repetition rate and a 100-fs pulse duration. The laser was focused to a spot size of approximately 2 μm in diameter on the device from the normal direction using an objective lens with a numerical aperture of 0.55. The photoluminescence signal was collected with the same objective lens, followed by real space or Fourier space imaging optics, and then sent to a 0.5-m spectrometer with an attached nitrogen-cooled charge-coupled device. The spectrally resolved real space and Fourier space distributions were measured by selecting a strip across the center of the Fourier space and real space distributions using the spectrometer's entrance slit. The resolution of the measurements was limited by the charge-coupled device pixel size to 0.3 μm^{-1} for Fourier space imaging and by the diffraction limit to 0.4 μm for real space imaging.

RESULTS AND DISCUSSION

Strong coupling between the excitons and TE cavity modes was evident in the momentum space images of the emission from within the cavity, as shown in Figure 2a. Discrete lower polariton (LP) modes and a faint upper polariton (UP) branch were observed below and above the exciton energy, respectively, with dispersions distinct from that of the cavity photon (the red solid line). In contrast, the emission from outside the hybrid cavity region shows a flat, broad exciton band at the heavy hole exciton energy of $E_{exc}=1.551$ eV (Figure 2b). The energies of the polariton modes can be described as follows in the rotating wave approximation:

$$E_{UP,LP}(k) = \frac{1}{2} \left[E_{exc}(k) + E_{cav}(k) \pm \sqrt{(E_{exc}(k) - E_{cav}(k))^2 + 4\hbar^2\Omega^2} \right] \quad (1)$$

Here, k is the in-plane wavenumber, E_{cav} is the uncoupled cavity energy and $2\hbar\Omega$ is the exciton–photon coupling strength, corresponding to LP–UP splitting at zero exciton–photon detuning. Using Equation (1) and the measured $E_{exc}(k=0)=1.551$ eV, $E_{LP}(k=0)=1.543$ eV and $E_{UP}(k=0)=1.556$ eV, we obtain $E_{cav}(0)=1.548$ eV and $2\hbar\Omega=12$ meV.

The discrete LP modes show full three-dimensional confinement of the polaritons. The lateral size of the hybrid cavity is determined by the size of the high-reflectance subwavelength grating (SWG). Outside the SWG, there is no cavity resonance, and the excitons are eigen-excitations. Inside the SWG region, the TE-polarized cavity modes strongly couple to the excitons, leading to laterally confined TE-polarized polariton modes. The transverse magnetic (TM)-polarized excitons remain in the weak coupling regime. Because there is not a sharp lateral boundary at which the cavity mode disappears, we phenomenologically modeled the effective confinement potential as an infinite harmonic potential. The calculated energies of the LP modes are indicated by the dashed lines in Figure 2a, which agree very well with the measured LP resonances. For comparison, the confined cavity modes (crosses) and corresponding 2D dispersions of the LP, UP and cavity modes are also shown (solid lines).

The spatial profiles of the confined LP modes were also measured *via* spectrally resolved real space imaging, as shown in Figure 2c. The four lowest LP modes are well confined within the SWG region, while the higher excited states are spread outside and form a continuous band. The variances of the k -space and x -space wavefunctions along the detected direction are $\Delta k=0.85$ μm^{-1} and $\Delta x=1.01$ μm . Their product is $\Delta x \times \Delta k=0.86$, slightly larger than the uncertainty limit of 0.5, which may be due to the diffusion of the LPs.

The absorption spectra of the modes were obtained *via* reflectance measurements. The spectrum measured normal to the sample (Figure 2d) shows the three symmetric modes with the lowest mean in-plane wavenumber: the UP ground state, the LP ground state and

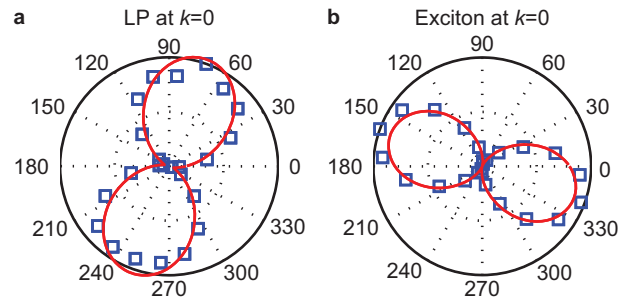


Figure 3 Polarizations of the polaritons and excitons in the hybrid-cavity polariton system. (a) Polar plots of the LP ground state intensity as a function of the angle of the linear polarization analyzer. The symbols represent the data. The solid lines fit to Equation (3), with a corresponding fitted linear degree of polarization of 91.9%. (b) Polar plot for the exciton emission intensity from within the SWG, corresponding to a fitted linear degree of polarization of 98.2%, with orthogonal polarization compared to (a). LP, lower polariton; SWG, subwavelength grating.

the second LP excited states. The spectral weights of the other polariton states are too small to be measured in reflectance. When measured at 3.5° from the sample normal, the first excited state of the LPs was also observed (Figure 2e).

A further confirmation of the strong-coupling regime is the temperature tuning of the resonances, as shown in Figure 2f. As the temperature increased, the LP and UP ground state energies were redshifted and were measured *via* k -space photoluminescence. The exciton energy was directly measured in the planar region outside the SWG. The shift of the cavity photon energy was obtained from the shift of the first low-energy side minimum of the stopband. Anticrossing of the LP and UP modes is evident. From the LP, exciton and cavity energies, we obtain a coupling strength of $2\hbar\Omega(T) \sim 10$ meV from 10 K to 80 K, showing that strong coupling persists to the liquid nitrogen temperature and higher.

Unlike planar DBRs, the grating breaks the in-plane rotational symmetry. As a result, the SWG mirrors can have high polarization selectivity. We optimized our SWG to have high reflectance for the TE mode and low reflectance for the orthogonal TM mode. Correspondingly, the polaritons are TE-polarized, while the TM-polarized excitons remain in the weak coupling regime. Figure 3 shows the photoluminescence intensity *vs.* the angle of linear polarization for the LPs and excitons at $k \sim 0$ within the SWG region, normalized by the maximum intensity. We fit the data with $I = A \cos(\theta - \phi)^2 + B$, where the fitting parameter ϕ depends on the orientation of the device, A corresponds to linearly polarized light, and B corresponds to a non-polarized background. Correspondingly, the degree of linear polarization is $\text{DOP} = (I_{\max} - I_{\min}) / (I_{\max} + I_{\min}) = A / (A + 2B)$. We obtained $A_{LP} = 1.04 \pm 0.04$, $B_{LP} = 0.05 \pm 0.01$, $\phi_{LP} = 71^\circ \pm 1^\circ$ and $\text{DOP} = 91.9\%$ for the LPs, confirming that the LPs are highly TE-polarized. For the excitons, we obtained $A_{exc} = 0.891 \pm 0.001$, $B_{exc} = 0.0081 \pm 0.0002$, $\phi_{exc} = 161^\circ \pm 1^\circ = \phi_{LP} + 90^\circ$ and $\text{DOP} = 98.2\%$, showing that the excitons are polarized orthogonal to the LPs. Such control of the polariton polarization has not been possible with conventional DBR–DBR cavities and is unique to the SWG-based cavity.

Finally, we show that polariton lasing was achieved in the 0D hybrid cavity. As shown in Figure 4a, the emission intensity I from the LP ground state increases sharply with the excitation power P at a threshold of $P_{th} \sim 5$ kW cm^{-2} , characteristic of the onset of lasing. Interestingly, the emission intensity I varies with P quadratically both below and well above the threshold, except at very low excitation densities. This result may arise because the energy separation between the discrete modes is larger

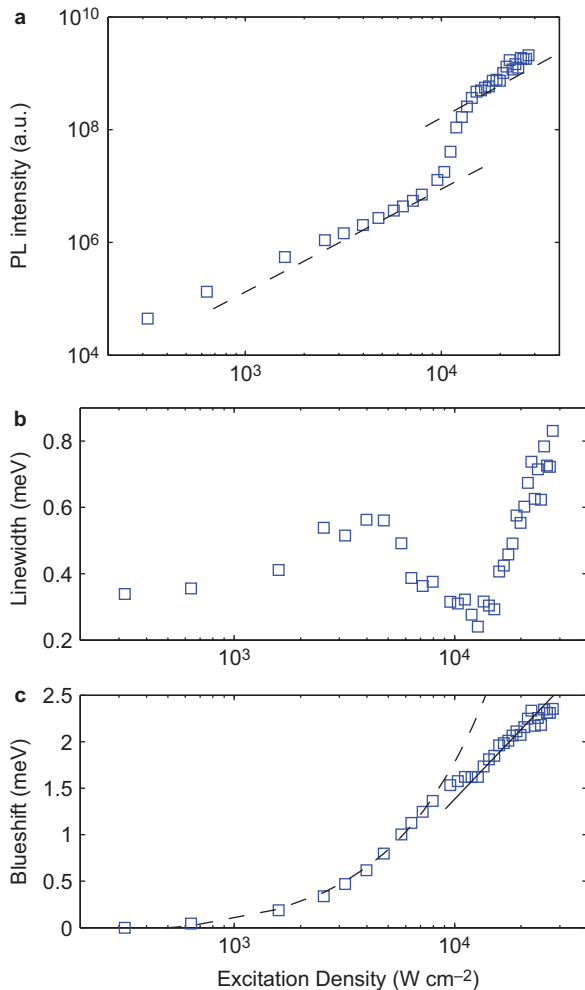


Figure 4 Lasing properties of the 0D polaritons. (a) Integrated intensity, (b) linewidth and (c) corresponding energy blueshift of the LP ground state vs. the excitation density. The dashed lines in (a) provide a comparison with quadratic dependence. The dashed lines in (c) display comparisons with the linear dependence below the threshold and logarithmic dependence above the threshold. OD, zero-dimensional; LP, lower polariton; PL, photoluminescence.

than $k_B T \sim 0.8$ meV. As a result, relaxation to the ground state through LP-phonon scattering is suppressed compared to LP-LP scattering.

Accompanying the transition, a sharp decrease in the LP ground state linewidth was measured. The minimum linewidth of 0.24 meV may be primarily limited by the intensity fluctuation of the pulsed excitation laser.²⁸ The LP energy increased continuously with the excitation density due to exciton-exciton interactions. The blueshift shows a linear dependence below the threshold, is suppressed near the threshold, and shows a logarithmic dependence above the threshold.^{22,29} The discrete energy levels are maintained across the threshold and remain distinct below the uncoupled cavity energy.

The establishment of polariton lasing confirms the quality of the 0D polariton system. The threshold density is smaller than or comparable to those measured in DBR-DBR pillar cavities.^{22,23} The linewidth reduction and blueshift are all within an order of magnitude of reported values in DBR-DBR planar or pillar microcavities.^{1,22,23} Unlike DBR-DBR cavities, however, the polariton lasing demonstrated herein occurs with a *a priori* defined polarization, independent of the excitation conditions.

CONCLUSIONS

In conclusion, we have demonstrated the first hybrid cavity incorporating a slab PC mirror, operating in the strong coupling regime and supporting polariton lasing. Three-dimensional confinement of the polaritons was achieved by using a finite size SWG, with the quantum wells and the main cavity layers untouched. Polariton lasing in the ground state was readily observed.

Unique to the hybrid SWG cavity, the LP is linearly polarized, while the orthogonally polarized exciton mode remains in the weak-coupling regime. The PL of the weakly coupled TM excitons provides direct access to the TE exciton reservoir, which has not been available in conventional III-As cavities. This approach can enable polarized polariton lasers^{30–34} and can simplify quantum photonic devices based on single-spin polaritons.^{10–12,35}

The integration of a slab PC mirror in a polariton system adds flexibility in controlling the fundamental properties of polaritons by design, including the dimensionality and polarization, as demonstrated in this work. The investigation of different PC designs will allow for further modifications of the polariton properties. Importantly, control of the polariton system was achieved without creating destructive interfaces in the active media or main cavity layer. Hence, extension of this single 0D polariton system to multiple close-placed systems would allow for the creation of controllably coupled polariton systems, while each 0D cell in the coupled system could be separately controlled and probed. The demonstrated hybrid-cavity polariton system may provide a scalable architecture for the experimental implementation of coupled lattice cavity systems.^{4,36}

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