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# 1 Urban Wind: Characterization of Useful Gust and Energy Capture

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- 7

# 8 Abstract

9 Small-scale wind turbine operations within the urban environment are exposed to high levels of gusts and turbulence compared to flows over less rough surfaces. There is therefore a need for such systems to not 10 11 only cope with, but to thrive under such fluctuating flow conditions. This paper addresses the potential importance of gust tracking technologies within the urban environment via the analysis of the additional 12 13 energy present in the gusty wind resource using high resolution measurements at two urban roof-top 14 locations. Results demonstrate significant additional energy present in the gusty wind resource at high 15 temporal resolution. This energy is usually under-represented by the use of mean wind speeds in 16 quantifying the power in the wind over longer averaging times. The results support the promise of 17 capturing a portion of this extra energy through gust tracking solutions. The sensitivity of this "additional" wind energy to averaging time interval is also explored, providing useful information for the 18 19 design of gust tracking or dynamic control algorithms for small-scale turbines. Relationships between 20 turbulence intensity and excess energy available are drawn. Thus, an analytical model is proposed which 21 may prove useful in predicting the excess energy available across wide areas from, for example, boundary 22 layer turbulence models.

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Keywords: urban wind; small-scale vertical-axis wind turbine; turbulence intensity; excess energy
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# 28 1. Introduction

Rising uncertainties over the future of oil and gas markets and increasing awareness of anthropogenic contributions to climate change have stimulated the quest for sustainable energy resources with lower  $CO_2$  emissions than traditional fossil fuel sources. In 2008, the UK government set legally binding targets for achieving an 80%  $CO_2$  reduction by 2050 compared to the 1990 baseline [1]. One attractive option for helping to achieve this target is increasing the usage of small-scale, decentralised and low-carbon energy sources, known as micro-generation. This would encourage energy generation close to the point of usage thereby reducing transmission losses. The UK government demonstrated its commitment to micro36 generation with the introduction of the feed-in-tariff (FIT) system in 2010 [2]. The FIT system guarantees 37 a fixed financial return for every kWh of renewable electricity generated. Investment in micro-generation 38 has therefore become financially attractive, although only if income generated can outweigh initial 39 installation and maintenance costs over the lifetime of the installation. The efficiency of the installation 40 must therefore be optimal for the available local energy resource in order to maximise energy and 41 financial returns.

42

43 Wind energy is currently enjoying the status of a commercially proven and cost effective technology with 44 significant recent increases in annual global installed capacity [3, 4]. The expansion of this industry into 45 rural areas has occasionally been met with public disapproval. However, the smaller and quieter wind 46 energy systems that have been developed for use in urban and rural areas may be less subject to these 47 concerns. These small-scale wind turbines can easily blend into the city through either the incorporation 48 of building mounted turbines in high rise city centres, or ground mounted turbines in semi-urban regions. 49 This would lessen the losses experienced within the electricity supply system [5], as well as creating 50 greater public awareness of renewable energy options. It is estimated that the installed capacity of 51 micro/small-scale wind turbines in the UK could reach 1.3GW by 2020 [6] if appropriate incentives and 52 policies are put in place.

53

54 Urban and semi-urban wind environments are characterised by rapidly fluctuating, turbulent winds. This 55 results from various factors including high surface roughness, the interaction between incoming flows and complex local building structures, and atmospheric instabilities caused by local heat sources [7]. The 56 57 resulting complex, gusty urban wind rapidly changes in both magnitude and direction over a range of 58 length and time-scales which may vary according to incoming wind direction and therefore upwind 59 roughness characteristics. Roughness also strongly influences mean wind speeds and the urban surface is 60 expected to slow down the mean wind close to the surface due to frictional and form drag effects [7]. 61 These complex characteristics of urban wind resource have strong consequences on energy generation. 62 McIntosh et al [8] for example, highlighted the inability of rural-specific turbine rotor designs in tracking the high fluctuations inherent in the gusty urban wind resource. However, there exists a significant 63 amount of energy stored within the higher frequency components of these gusts (as illustrated in the 64 micrometeorological region in Figure 1). Hence the possible extraction of this energy through advanced 65 66 turbine controls may partially offset the penalty of wind turbines operating in the reduced mean wind 67 speeds experienced close to urban surfaces.

68

Small-scale wind turbines fall into two major groups; Horizontal Axis Wind Turbines (HAWT) and
 Vertical Axis Wind Turbines (VAWT). HAWT designs have been greatly developed over recent years,

71 but are not necessarily fundamentally aerodynamically superior to VAWTs [10]. Their efficiency is 72 highly dependent on wind direction (yawing). Small-scale HAWTs may suffer higher performance degradation in gustier (urban) operating environments due to yaw misalignment with a  $cos^2$  dependence 73 74 on the relative wind angle [11]. This can result in increased use of control power due to yaw corrections in rapidly fluctuating conditions, potentially decreasing the overall efficiency of the turbine system. 75 76 VAWTs on the other hand have the ability to handle rapid changes in wind direction and operate at lower 77 tip speed ratios, resulting in reduced noise emissions. VAWTs therefore seem a potentially good choice 78 of configuration for the urban environment. However, they suffer from issues such narrower operating 79 ranges (e.g. higher cut-in wind speeds than HAWTS), lower peak efficiencies and low starting torques. 80 Many of these issues can be addressed through turbine controls [12, 13]. However, designing effective 81 controls relies on a detailed understanding of the nature of the available wind-resource in order to cope 82 with rapid changes in wind speed and the generation of rapid torques changes [14].

83

84 High temporal resolution monitoring of wind speeds within urban regions is not widespread, potentially 85 leading to higher levels of uncertainty in the assessment of wind turbine performance in urban areas [15]. 86 Computational models of air flows over cities could potentially provide additional information on wind 87 characteristics and may have the advantage of providing wide spatial coverage compared to a limited number of measurement sites [7, 16]. Hence it is of interest to determine whether outputs from such 88 89 models e.g. mean wind speeds and turbulence levels, could be used to assist in the prior assessment of 90 turbine performance and in turbine system design. For this reason, this study focuses on the assessment of 91 turbulence characteristics within urban areas and how measures of turbulence may be used to determine 92 how much energy is available to a well-controlled turbine.

93

94 The primary objective of the work is the characterization of typical urban wind resource based on high 95 resolution anemometer measurements at two urban roof-top locations considered as potential turbine 96 mounting sites. The additional energy resource available within high frequency gusts is quantified and is 97 linked to standard measures of turbulence such as turbulence intensity. We highlight the effect of 98 averaging time on the available wind power and demonstrate that the frequency of raw data must be well 99 matched to potential turbine response times in order to make accurate assessments of the excess energy 100 available to a particular turbine within gusts. By assessing the relationship between turbulence intensities 101 and the excess energy available within a built environment, we propose an analytical model for predicting 102 the excess energy and/or the total kinetic energy available at a potential turbine site. Section 2 introduces 103 the concepts of gust tracking and gust efficiency and their importance to turbine operation. Section 3 104 presents methods for the characterization of additional energy available within urban wind such as the 105 gust energy coefficient (GEC), and excess energy content (EEC), along with a brief description of the

selected urban sites for analysis and data processing methods. Section 4.1 presents results obtained from the two approaches in evaluating the additional energy available at these urban sites. The effects of averaging/turbine response time on potential turbine power output are discussed in Section 4.2. Here, relationships are drawn between turbulence intensity and excess energy content, and an analytical model for predicting *EEC* values within an urban environment is proposed. Finally the main conclusions are presented in Section 5.

112

#### 113 2. Background

114 Gusts are defined as sudden fluctuations in wind speed which may contain within them wind speeds as 115 high as 30-50% above the average [14]. An example of the gusty nature of real world urban wind speeds 116 is illustrated in Figure 2. It is shown that the wind speed varies greatly between 0.4 ms<sup>-1</sup> and 14.5 ms<sup>-1</sup> 117 within a very short time period. Abrupt changes are experienced between points 1 and 2 (a jump in speed from 2.7 ms<sup>-1</sup> to 13.2 ms<sup>-1</sup> in  $\leq$  20 s) and points 3 and 4 (a jump from 2.8 ms<sup>-1</sup> to 14.5 ms<sup>-1</sup> in  $\leq$  40s). 118 These sudden rises and drops in wind speed, contrast with observations from coastal/open sea terrain [17] 119 120 or rural terrain [18]. They result from increased turbulent drag caused by the high terrain roughness 121 present within urban environments [19], rapid changes in flow direction around buildings/structures, and 122 the formation of vortices [20] leading to regions of both flow acceleration and stagnation. These vortices 123 can be influenced by various factors ranging from the effect of building area density to the substantial 124 influence of roof heights and shapes on the flow structure within the urban environment [21]. All else 125 being equal, Bertenyi et al [22] suggest that a turbine system could experience a 60% loss or gain in 126 power generation if relocated from a coastal/open sea site to an urban environment.

127

Thus, it is important that controls utilised within turbines to be sited within the urban environment allow gust tracking which ensures that the system not only copes with, but thrives in this complex urban wind resource. The aim of these technologies is to try to maintain the turbine operation within its region of peak aerodynamic efficiency [22] and thus to maximise energy extraction as wind speeds fluctuate. The efficiency of a wind system is commonly characterised by its power coefficient [3, 23, 24] and is given as:

$$C_p = \frac{P_T}{P},\tag{1}$$

134 where *P* is the available wind power and  $P_T$  is the power generated by the wind turbine system.

135

Figure 3 presents a power coefficient  $(C_p)$  curve for the vertical axis QR5 wind turbine model as a function of non-dimensional tip speed ratio  $\lambda$ , as measured in a full-scale wind tunnel test by Quiet Revolution [25].  $\lambda$  is defined as the ratio between the rotational speed of the tip of the turbine blade and the actual velocity of the wind [26]. Although the power curve shown in Figure 3 is defined for steady flow conditions, the shape of performance curves in unsteady winds has been shown to be similar [8]. Hence the figure serves to illustrate the region of tip speed ratios at which maximum aerodynamic efficiency and therefore peak power can be achieved. Under real world gusts, it is quite possible for the turbine to move from operating at point 1 (peak power) to points 2, 3 or 4 over short time-scales (seconds) if the rotational speed of the turbine is not adjusted.

145

146 For better performance in a gusty wind resource, the turbine's rotational speed needs to be constantly and 147 precisely adjusted in order to enable the turbine system to operate at its peak aerodynamic efficiency (as 148 shown by  $C_{pmax}$  in Figure 3). Failure to do so could result in a significant loss in aerodynamic power, 149 especially in situations where the turbine experiences a large gust and its tip speed ratio falls into the 150 region of deep stall [8]. Here, the energy losses and low aerodynamic torque experienced may not be 151 sufficient to allow acceleration back to the turbine's correct speed. Tracking such gusts and avoiding 152 deep stall involves specific design considerations. These include low turbine inertia, real-time operating 153 conditions (as in the case of feedback controls), and a power electronics architecture which allows for 154 active control [27].

155

156 While studying flow across buildings/structures in urban environments, Cook [28] observed structure-157 generated turbulence which resulted in the power spectral density containing an additional peak at higher 158 frequency (i.e.  $\geq 0.1$  Hz) than typical boundary layer turbulence. The scale of this peak was influenced by 159 the size and shape of inherent urban structures and the frequency range of its fluctuations varied across 160 different sites. Ideally, gust tracking designs would be able to capture all the power contained within this 161 additional peak up to very high frequencies. However, cost limitations may prevent the design of turbines 162 and control architectures which are able to capture this full range of frequencies. In addition, where wind 163 data is used as input to feedback control models it is usually filtered to remove fast transients which could 164 de-stabilise the selected control model (e.g. simple proportional control [8]). It is therefore of interest to 165 consider different cut-off frequencies which may represent different levels of turbine responsiveness and 166 to evaluate the extent of excess energy which may be captured for the different cut-offs. The upper limit 167 of the frequency range (cut-off frequency  $F_C$ ) selected is represented in this paper as the gust frequency 168  $(F_G)$ .

169

The simplest and most popular method of cut-off frequency selection is made by using a low pass filter toextract the lowest frequency components of the wind input. This represents the gust frequency at which

the maximum amount of filtering retains a targeted percentage of the power content in the turbulent wind

173 within a given period. The targeted power content percentage tends to vary with different small-scale 174 wind turbine manufacturers as a result of their different design objectives (e.g. 99% below  $F_c \approx 0.1$  Hz 175 [8], 98% below  $F_c \approx 0.5$  Hz [29]). The selection of different cut-off frequencies tends to affect the 176 performance of the controller as well as the turbine output variables. However, the choice of employing a 177 wind turbine system with little or no gust tracking control within the urban environment would entail the 178 system operating at a much lower  $F_c$ . This results from the system's time lag which depends on the 179 turbine inertia, controller and aerodynamic response.

180

181 The cut-off frequency has been used in this paper to define the characteristic gust frequency, with  $F_{c}$ 182 employed in averaging the wind input data. A snap shot of the effects of filtering data was shown in Figure 2 with an  $F_c$  of 0.1 Hz. The averaging time duration  $(T_c = 1/F_c)$  is an important factor in gust 183 184 tracking, with the influence of short fluctuations on the turbine operation of a given turbine dependent on 185 the magnitude of the  $T_c$  used in averaging the incoming wind speed, turbine RPM and power.  $T_c$ 186 therefore varies with different turbine sizes and control models. The analysis of turbulence data at the 187 potential mounting site therefore needs to reflect these characteristics if the excess energy available is to 188 be properly assessed. Various turbine control techniques have been addressed in literature with the 189 optimum power/torque tracking technique a popular control strategy in achieving optimum power 190 generation [30]. For most control techniques, to run the turbine optimally requires obtaining the  $C_p - \lambda$ 191 dependency of the specific turbine and/or the wind speed in calculating the desired rotor speed needed to 192 vary the generator speed [31]. The difficulty and high cost of accurate measurement of urban wind and 193 the uncertainties surrounding the application of the turbine manufacturer's  $C_p - \lambda$  curve at different 194 turbine sites give rise to errors which will strongly influence the turbine controls. Maximum power point 195 tracking (MPPT) algorithms have been employed in various ways to circumvent these errors but will add 196 to the overall cost of the system [32-34]. In order to evaluate the performance of VAWTs in unsteady 197 winds and the cost effectiveness of control methods, the total energy available to the turbine needs to be 198 estimated and it is here that the current work is focussed.

199

#### 200

## 3. Methodology and Data Processing

Whilst there are a number of sources of UK wind resource information available with varying degrees of resolution (e.g. that available from the UK Met Office [35]), high frequency datasets for urban environments (cities, towns, etc.) are much scarcer since data sets acquired for weather forecasting purposes tend to be sited as far as possible in regions of uninterrupted flows. Freely available sources of wind resource data such as the Numerical Objective Analysis of Boundary Layer (NOABL) database contain wind speeds that do not account for the influence of the urban area upon the wind and in general tend to represent long term mean wind speeds [36]. Given the complex nature of the urban wind resource, 208 for a more effective urban wind assessment, specific high resolution measured wind data are required at 209 above roof heights which may be typical of roof-top mounted turbines. Limited research data sets are 210 available for this purpose and based on the availability of data, two sites were selected for this study. The 211 first is on the roof of the Houldsworth Building at the University of Leeds, and the second is that of the 212 Whitworth Meteorological Observatory of the University of Manchester (both within the United 213 Kingdom). The areas around both of these sites are densely populated and characterized by a large 214 number of buildings and structures. Nevertheless, both of these sites well exceed the local mean building 215 heights (11.9m for Leeds and 14.2m for Manchester based on a 250 x 250 m average) and therefore could 216 be considered as possible turbine mounting locations [37].

217

218 3.1 Site description and instrumentation

## 219 3.1.1 University of Leeds, Houldsworth Building

The first wind dataset was collected at a location within the University of Leeds Campus (in this paper referred to as Unileeds), Leeds, UK. This data was captured at a sampling frequency of 10 Hz using two sonic anemometers (Research-Grade Gill Scientific Instruments model R3-50) located at two different mast heights of 6 m and 10 m, on the top of the Houldsworth building (roof height approximately 24 m; Latitude: 53.809963°, Longitude: -1.5574005°). In the results section, height 1 (H1) at the Unileeds site represents data collected at mast height of 10 m, whilst height 2 (H2) represents data collected at a mast height of 6 m above the roof top.

227

### 228 3.1.2 Whitworth Meteorological Observatory, Manchester

The second wind data set was obtained from a sonic anemometer (Gill Windmaster Pro Sonic
Anemometer) at a sampling frequency of 20 Hz. This was mounted on a 5 m mast located on the roof-top
of the George Kenyon building on the University of Manchester South campus (also known as the
Whitworth Meteorological Observatory site with a building height of 49 m; Latitude: 53.467371°,
Longitude: -2.232006°). The wind data obtained for this study was averaged at a sampling frequency of
1 Hz.

235

### 236 *3.2 Scope of data collected and analysis*

The wind data used within this study were collected at the respective sites between the years 2009 and 2011, with a year-long dataset for each site selected for analysis within this paper. It should be pointed out that these are not entirely overlapping due to gaps within the available datasets. The quoted resolution of the Gill sonics is 0.01 ms<sup>-1</sup> with accuracies of <1.5%. Quality assurance of the data, involving the handling of data outliers, was carried out within previous studies and a description of this process can be found in Balogun et al. [38]. The mean wind direction ( $\theta$ ) and longitudinal free-stream wind speed (V) upstream of the rotor are derived from the horizontal wind components, u (x-direction) and v (y-direction) as follows:

$$\theta = \tan^{-1}(v/u), \qquad (2)$$

$$V = u\cos\theta + v\sin\theta, \qquad (3)$$

247 while the standard deviation of the longitudinal wind speed is given as

$$\sigma = \sqrt{\frac{1}{T} \sum_{i=1}^{T} (V_i - \bar{V})^2},$$
(4)

(4)

248 where  $\overline{V}$  is the mean wind speed, and T defines the sample time period.

249

The high resolution wind data, collected from each sonic anemometer, was averaged at a sample frequency of 1 Hz where necessary in order to remove the very fast transients and parsed into contiguous minute bursts, which is consistent with wind energy industry certification standards [39].

253

In a turbine system, the longitudinal wind speed is directed along the hub, while in characterising the degree of turbulence in a burst, the standard parameter of Turbulence Intensity (*T. I.*) is employed [40]. This is defined as the standard deviation of the fluctuating components of the wind speed normalised by the mean wind speed for over the chosen averaging period:

$$T.I.(\%) = \frac{\sigma}{\overline{V}} \times 100\%$$

258

Since *T*. *I*. is sensitive to the averaging period, it should only be compared for equivalent burst durations.The average power available in the wind is calculated by:

$$P = \frac{1}{2}\rho A \overline{V}^3 , \qquad (5)$$

where  $\rho$  is the air density and *A* is the cross sectional area in which the air is flowing through. However, there may exist additional energy within shorter frequencies in gusty conditions (as shown in Figure 1), which is usually lost (or under-reported) due to the use of the mean wind velocity measurements in calculating the wind power over a given period. This additional energy can be defined by two parameters; the Gust Energy Coefficient (*GEC*) [22] and the Excess Energy Content (*EEC*). The *GEC* is defined as the ratio of the integral energy inherent in the wind over a given period of time to the assumed energy by only considering the mean of the wind speed within the same period:

$$GEC = \frac{\int_0^T V^3 \, \mathrm{dt}}{\bar{V}^3 \cdot T} \, .$$

269

(6)

The *EEC*, which is closely related to the *GEC*, is defined as the excess energy (expressed as a percentage of the total integral energy) contained within transient fluctuation about the mean over a given burst period:

273

$$EEC(\%) = (GEC - 1) \times 100\%$$
. (7)

The values of *GEC* and *EEC* are sensitive to the length of the burst periods chosen in this paper to be 10mins in length (i.e. T = 10 mins). This is based on the fact that a spectral "gap" appears around this frequency as illustrated in Figure 1, and is consistent with industry-based standard approaches for certification [39].

278

#### 279 3.3 Assumptions

The effect of wind direction on the turbine (VAWT) performance within an urban environment was assumed to be negligible [27]. It is also assumed that in an idealised steady wind environment, the *GEC* and *EEC* would be 1.0 and 0% respectively [22]. This indicates that the total integral energy within the sample time period is reflected by the energy derived by employing the mean wind speed within the same sample time period.

285

#### 286 4. Results and Discussion

#### 287 4.1 Effect of T.I. on power and EEC

288 Since T.I. is a more commonly presented statistic describing the level of turbulence in urban areas, it is 289 first interesting to evaluate whether a relationship exists between T.I. and available excess energy. The 290 monthly average wind speed values for the two sites analysed are shown in the bottom pane of Figure 4. The minimum monthly average wind speed value of 2.1 ms<sup>-1</sup> was observed in December, while the 291 maximum monthly average wind speed value of 5 ms<sup>-1</sup> was observed in May, both at the Manchester site. 292 The yearly average wind speeds were found to be 3.3 ms<sup>-1</sup>, 2.8 ms<sup>-1</sup> and 3.5 ms<sup>-1</sup> at the Unileeds (H1 and 293 294 H2) and Manchester sites respectively, with the longer term (5years) average values being somewhat higher at 3.74 ms<sup>-1</sup>, 3.15 ms<sup>-1</sup> and 3.66 ms<sup>-1</sup> at each site respectively. Therefore, the sites used in this 295 296 paper can be considered to possess a low to medium quality wind potential. In the top pane of Figure 4, 297 two methods of calculating the power density are shown. The dashed lines correspond to the use of 10 298 minute averages of wind speeds for the power calculations and the solid lines correspond to the average 299 power calculations at 1 s intervals. The solid line therefore represents the maximum power available if all 300 the energy in the high frequency gusts was to be captured by the turbine. There is clearly a marked 301 difference between these two methods, particularly for the Manchester site which exhibits the highest 302 turbulence intensities for most of the year. Of the two Leeds sites, H2 was shown to exhibit higher turbulence intensities, which is perhaps expected since this mast height is closer to the roof than H1. In addition to generally higher turbulence intensities, higher average wind power is also observed all year round at the Manchester site (excluding the months of November and December) mostly likely due to the fact that it is a tall building (49 m) compared to the local mean building height (14.2 m). If the additional energy in the high frequency gusts was able to be captured at this type of site, it may become viable for turbine siting. In section 4.2, we assess how much of this energy may be captured for different turbine response times as represented by  $T_C$ .

310

311 Based on the assertion that the output variables of a VAWT are not affected by rapid changes in wind 312 direction typical of an urban environment [27], it is relevant to investigate the degree to which the power 313 output is influenced by T. *I*. at the sites analysed. Methods for estimating the potential energy capture at a 314 specific site by incorporating a measure of turbulence (e.g. T.I.) are used by some experts within the wind 315 industry [41]. In addition, T.I. is likely to be a model output when using, for example, computational 316 fluid dynamics, CFD [42, 43] to investigate potential turbine sites. It is therefore useful to investigate how 317 excess energy varies with T. I. thus facilitating the use of such CFD models in the design of gust tracking 318 solutions.

319

A measure of the influence of *T*. *I*. can be highlighted by binning the wind power curve according to different turbulence intensity bands, as shown in Figure 5. This is a common approach employed by most practitioners within the wind industry and provides relevant information as to the turbulence level at which maximum power is observed and beyond which a decline is noticed in the power curve. It is important to note that power curves produced by identical turbines at different sites may lead to different results due to their strong dependence on the local *T*. *I*. distribution, thereby making measured power curves limited in terms of being comparable and transferrable [44].

327

328 Figure 5 highlights this point, by first showing how different the calculated power curves can be 329 depending on whether 1 s or 10 minute averages in wind speed are assumed. Also shown is the increase 330 in power (at 1 s) with increasing T.I. at both sites with a net reduction in power experienced below T.I.331 values of 50% at Unileeds (H1 and H2) and Manchester respectively compared to the average power 332 available over all frequencies. The monotonic increase in power with increasing T. I. bands suggests the 333 potential of the turbine extracting at least a portion of the additional energy observed within these gusty 334 wind resource sites. Implementing fast response controls however, will entail additional capital costs, and 335 hence the level of turbulence experienced at proposed installation sites may give useful information for 336 appropriate turbine design by answering the question: how much excess energy is there worth capturing? 337

338

339 Figure 6 shows frequency plots for each site for different bins relating to T.I. It therefore provides 340 relevant information as to the level to which enhanced energy extraction is required within both sites. At 341 the selected sites, the T.I. is almost never less than 10% and is most frequently between 30-40%. A 342 turbine which was able to effectively capture the high frequency energy under such conditions would be 343 able to access an average of over 30% more power than would be estimated using the mean wind speed 344 alone under these conditions as suggested in Table 1. For coastal, open country and rural sites where T.I. 345 is more frequently below 20% [22, 45], the average additional excess energy would be much lower (of the 346 order of 10%).

347

348 In a different approach, the EEC, as defined in Section 3.2, quantifies the "excess" energy present in the 349 gusty wind resource. Results from both sites show a yearly average additional energy of 35.3%, 50% and 350 53.4% at the Unileeds (H1 and H2) and Manchester sites respectively, for a response time of 1 s. An 351 illustration of the EEC at the two sites for a year's wind input is shown in Figure 7 and Figure 8, with 352 Unileeds (H2) and the Manchester sites showing significantly higher values of EEC. These sites are 6 and 353 5 m above the roof respectively compared to 10 m for H1, and both sites showed higher T.I. values 354 throughout the year than H1 (see Figure 4). Figure 8 shows a strong dependence of excess energy on wind 355 speeds as seen in previous studies [22]. A summary of the mean value of EEC at various sites from both 356 previous and the present studies, categorised according to different levels of terrain roughness, is shown 357 in Table 2. The low turbulence sites (i.e. coastal sites) suggest a minor margin of 3.3% of excess energy 358 while the high turbulence sites (i.e. urban environments) suggest a significant margin of above 23% of 359 excess energy available. What is clear from the current work is that in addition to the local roughness 360 parameters, for roof mounted sites it is also important to consider the height above roof when estimating 361 excess energy available.

362

Thus, from the results presented so far in Section 4.1, the two approaches used in evaluating the available "excess" energy at both sites highlight the presence of a sizeable quantity of additional energy in the gusty urban wind. This could assuage the uncertainties involved in urban wind assessment as well as encouraging gust tracking solutions.

367

## 368 4.2 Effect of $T_c$ on Power and EEC

The average wind speed across the two sites in a year was observed to be greater than 3.1 ms<sup>-1</sup> and the potential maximum cut off frequency ( $F_c$ ) likely to be less than 1 Hz (corresponding to the maximum resolvable response frequency of the turbine). Thus, dimensional reasoning, as shown in Equation 9, dictates that the minimum length scale ( $L_u$ ) corresponding to the characteristic maximum gust frequency 373 ( $F_G$ ) employed in this study is approximately larger in magnitude than the diameter of a small-scale 374 VAWT turbine (e.g. the QR5 with diameter – 3.1 m [27]).

$$L_u = \frac{\overline{V}}{F_c} > D_T$$

(8)

376 where  $D_T$  is the diameter of the turbine.

377

375

378 This means that frequencies,  $F_C$ , and/or their corresponding averaging time-scales,  $T_C$ , should be less than 379 1 Hz to be physically resolvable by the turbine. The estimated small-scale wind energy capture for an 380 urban site through a turbine will depend on the turbulence characteristics of the site (measured by T.I.) 381 and the response characteristics of the turbine system.  $T_c$  characterises the turbine delay in response due 382 to the difference in inertia of the turbine blades and generator (which will depend on turbine size and 383 weight) and the control system architecture [46]. Therefore a range of possible values for  $T_c$  could be 384 present for different systems. We present here two case studies and their effects on average available 385 power and EEC.

386

**Case 1 (Tb1)**: For the first case, the  $T_c$  employed ( $T_c = 10$  s) corresponds to the shortest averaging time for anticipated small-scale VAWT response characteristics as suggested in [46].

389

390 **Case 2 (Tb2)**: Case 2 represents a VAWT with a much higher system response time ( $T_c = 60$  s), where 391  $F_c \ll F_G$ . This corresponds to the averaging time used in measuring and subsequent data analysis for 392 wind turbines with rotor diameter less than 16m as described in the relevant standard, IEC 61400 – 12 – 1 393 (see Annex H of IEC 61400 – 12 – 1 [39]).

394

395 With the 10 s and 60 s averaging imposed at the two sites we examine the loss in average power and EEC 396 compared to a maximum response frequency of 1Hz, as shown in Figure 9. Tb1 and Tb2 experience a 397 lower average power loss at Unileeds (H1) as compared to other sites. This may be as a result of reduced 398 blockage and wake effects at the mast height of 10 m above roof at the Unileeds site, and the relatively 399 lower turbulence levels compared to sites nearer the roof (see Figure 4). At Unileeds (H1), Figure 9 400 suggests that Tb1 would experience a maximum loss of approximately 6.93% of the available average 401 wind power while Tb2 would experience a maximum power loss of 17.85%. Therefore, the probable 402 increase in cost of a faster responding control system may be easily offset by its potential to capture more 403 energy available in the gusts. A summary of the percentage gain in power available to Tb1 and Tb2 is 404 shown in Table 2. Regarding the *EEC* available at both sites, Figure 9 shows that increasing  $T_c$  tends to 405 reduce the possible additional energy available, with gust tracking solutions expected to have relatively 406 greater impact at lower mast heights, where T. I. levels are likely to be higher.

407 The turbulence spectrum and the location of the turbulent energy peaks will be site dependent and hence 408 large differences may be observed with the use of different time-resolution of the data  $(T_c)$  when

409 calculating *T*. *I*. at a given site. In addition, when trying to relate the excess energy that may be available

410 to a specific turbine, the use of an appropriate value of  $T_c$  is required in order to reflect the potential

411 response time of the turbine. Figure 10 demonstrates the impact of increasing  $T_c$  on average power, EEC

and *T.I.* at the Manchester site (in this case,  $T_C \approx 1/F_C$ ). Increasing  $T_C$  results in decreasing *T.I.* and decreasing average power and *EEC*, and vice versa. It is therefore interesting to explore whether, if appropriate averaging times are chosen whether a strong relationship exists between *T.I.* and *EEC*.

Such a relationship is demonstrated in Figure 11 where *EEC* is plotted against the equivalent binned values of *T*. *I*. for several values of  $T_C$ . The figure shows that all the data lie close to a best fit curve which was determined to be a cubic function using a least squares error approach within MATLAB's best fit tool. Thus, *EEC* values were approximated by an empirical relationship given by the following equation:

419

$$EEC = 0.00022T \cdot I \cdot {}^{3} + 0.019T \cdot I \cdot {}^{2} + 0.15T \cdot I \cdot -0.38$$
(9)

420

with a correlation coefficient value  $(R^2)$  of 0.9986. The coefficient was calculated based on the *EEC* values from site observations (as shown in Fig. 11), using MATLAB's fitting tool. The high correlation coefficient value  $(R^2)$  indicates a good agreement between *EEC* values from site observations and predicted values.

425

In assessing the performance of the *EEC* prediction model given in Equation 10, the mean absolutepercentage error (MAPE, as defined in Equation 11) was also used:

428

$$MAPE = 100 \times \frac{1}{n} \sum \frac{|EEC_{obs} - EEC_{pred}|}{|EEC_{obs}|}$$
(10)

429

430 where *n* is the number of data points,  $EEC_{obs}$  represent the *EEC* values obtained from observations and 431  $EEC_{pred}$  represent *EEC* values obtained from Equation 10.

432

Table 4 compares the MAPEs for the *EEC* model over the 3 test sites at different  $T_c$ s. Model results showed very low error values over the 3 test sites with the largest errors observed within the lowest *T.I.* bin (i.e. T.I. = 0 - 10%). This suggests that for the sites studied, the *EEC* available to a particular turbine could be estimated from knowledge of the turbulence intensities so long as the appropriate response time of the turbine was represented by the use of an appropriate value for  $T_c$  when calculating *T.I.* Testing the validity of such a model over wider regions will require employing further sets of field measurementsfrom urban sites as they become available.

#### 441 5. Conclusions

High temporal resolution wind measurements from 3 potential urban roof-top sites have demonstrated the gusty and turbulent nature of the urban wind resource and the potential advantages of utilising turbine control systems which are designed to capture the energy available in these gusts. Results demonstrated elevated available additional energy (high EEC) under conditions of higher T.I. values, suggesting that accurate modelling of turbulence intensities could inform calculations of the additional energy available if optimal gust tracking solutions were found. The levels of excess energy were determined not only by local roughness characteristics but also by the above roof elevation of the sites. For short mast roof-top applications, gust tracking could be particularly advantageous. Available power and EEC are shown to decrease with increasing averaging time  $(T_c)$  related to the response time of the VAWT, suggesting that faster system response times may be essential to capture the energy within the gusts. Twice the excess energy was available with a 10 s response compared to 60 s. Wind resource and energy systems assessment based on turbulence intensities was shown to vary with different values of  $T_c$  illustrating the importance of specifying the data resolution when quoting T.I. values and properly matching  $T_c$  to the expected response time of the proposed turbine. Finally, an analytical model for estimating the excess energy available at a potential urban site was proposed by assessing the relationship between T.I. and EEC.

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603

#### **Figure Legends**

- 604 Figure 1: Frequency distribution of fluctuating wind energy within the internal sub-layer, adapted from Van Der
- 605 Hover [9]
- 606 Figure 2: Real world measured urban wind resource at a Manchester roof-top site illustrating a period with high
- fluctuations of the urban wind resource; the 1Hz data (dotted lines) and 0.1Hz data (solid lines).
- 608 Figure 3: Power coefficient for a QR5 VAWT model as a function of non-dimensional tip speed ratio, measured
- 609 under a full-scale wind tunnel test by Quiet Revolution highlighting the maximum power coefficient ( $C_{pmax}$ ) and
- 610 maximum tip speed ratio ( $\lambda_{max}$ ) (Adapted from [25]).
- 611 Figure 4: Average monthly power (top), T.I. (middle) and mean wind speed (bottom) values at the two sites for a
- one year data at a sampling frequency of 1 s (solid lines) and an averaging time of 10 mins (dotted lines).
- **Figure 5**: A comparison of the average power curve to power curves sorted by bands of *T.I.* for one year dataset
- bild parsed at 10 min bursts at (a) Unileeds (H1), (b) Unileeds(H2) and (c) Manchester sites.
- **Figure 6**: The *T*. *I*. distribution for a one year at both sites analysed, for which the power curves are plotted in Figure 616 5 at  $T_c = 1$  s.
- **617** Figure 7: Plot showing the average monthly *EEC* values at the two sites across the year at  $T_c = 1$  s.
- **618** Figure 8: *EEC* at  $T_c = 1$  s for a one year wind input at both sites (Unileeds (H1 and H2) and Manchester). Each
- point represents 10 min bursts, illustrating the expected potential contribution of gust tracking within both sites.
- 620 Figure 9: Effect of change in  $T_c$  on average *EEC* (left) and wind power (right) at Unileeds and Manchester 621 highlighting power and energy gain with decreasing averaging time.
- **Figure 10:** The relationship between average power, *EEC* and *T.I.* with averaging time for a year at the Manchester site demonstrated.
- **Figure 11:** The relationship between *EEC* and *T.I.* with averaging time at both sites
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Tables

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633

Sites	10 - 20%	20 - 30%	30 - 40%	40 - 50%	P <sub>1s</sub> P <sub>10mins</sub>	_
Unileeds(H1)	6.97	25.77	34.13	51.73	29.79	
Unileeds(H2)	8.04	18.64	32.36	60.01	33.63	
Manchester	16.57	25.63	28.54	49.55	28.83	

#### 635

**Table 1:** Percentage increase across the turbulence intensity bins from the Average Power  $(P_{10mins})$  calculated from

637 mean wind speed at 10 mins (as shown in the power plots in Figure 5)

638

SITE DESCRIPTION	<b>EEC</b> (%)	<i>z<sub>o</sub></i> (m)		
Coastal site	3.3	0.005		
Open country	16.1	0.05		
Semi Urban	22.7	0.2		
Urban	> 23	> 0.7		
Unileeds (H1)	35.3	1		
Unileeds (H2)	50	1		
Manchester	53.4	0.9		

639 Table 2: A summary of the *EEC* from some analysed turbine sites with their relative roughness heights (adapted

from [22]) and urban sites selected in this paper.

SITES	TURBINE CONFIGURATIONS					
	Tb1	Tb2				
Unileeds (H1)	6.93 %	17.85%				
Unileeds (H2)	10.68%	23.21 %				
Manchester	8.21 %	17.78%				

642 Table 3: Summary of percentage loss in power deduced from Tb1 and Tb2 operation from assumed maximum

643 operating frequency of 1Hz at both sites for a year

644

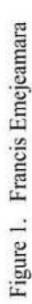
<sup>641</sup> 

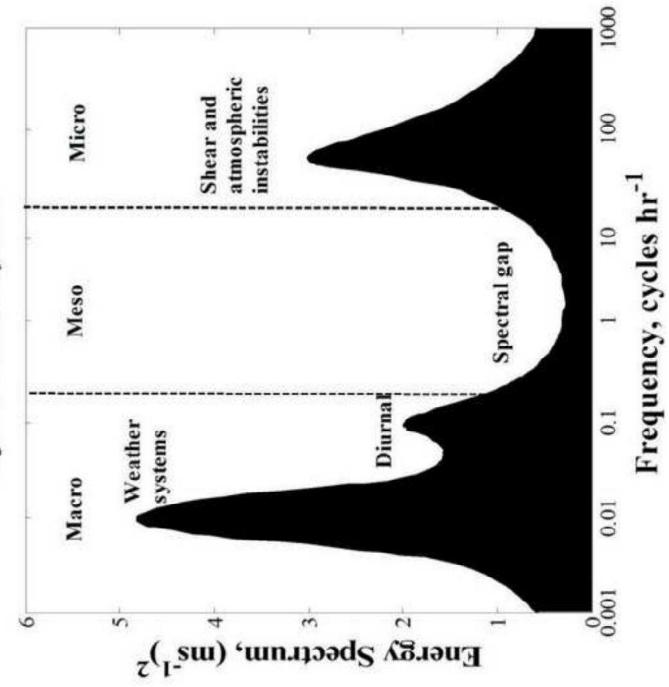
	Sites		MAPE for the different T. I. Bins (%)							
C		T.I. ranges	0-10	10-20	20-30	30-40	40-50	50-60	60-70	70-80
	Unileeds(H1)	•	8.740	1.035	2.634	0.866	1.447	1.196	0.261	1.611
1s	Unileeds(H2)		9.780	1.580	2.976	1.499	0.089	0.402	2.641	5.456
	Manchester		11.500	1.485	1.643	3.871	4.831	4.132	1.944	1.506
	Unileeds(H1)		8.719	1.429	2.803	1.386	0.349	0.354	1.006	2.507
10s	Unileeds(H2)		8.796	1.742	3.170	2.373	2.491	3.295	4.129	1.025
	Manchester		9.444	0.251	0.374	0.785	1.177	0.057	0.528	4.419
	Unileeds(H1)		8.141	1.626	2.863	2.141	0.835	0.083	3.854	1.777
60s	Unileeds(H2)		8.366	1.757	3.271	3.151	2.320	2.038	2.245	3.547
	Manchester		8.354	1.195	1.841	0.921	0.336	0.396	1.337	2.734

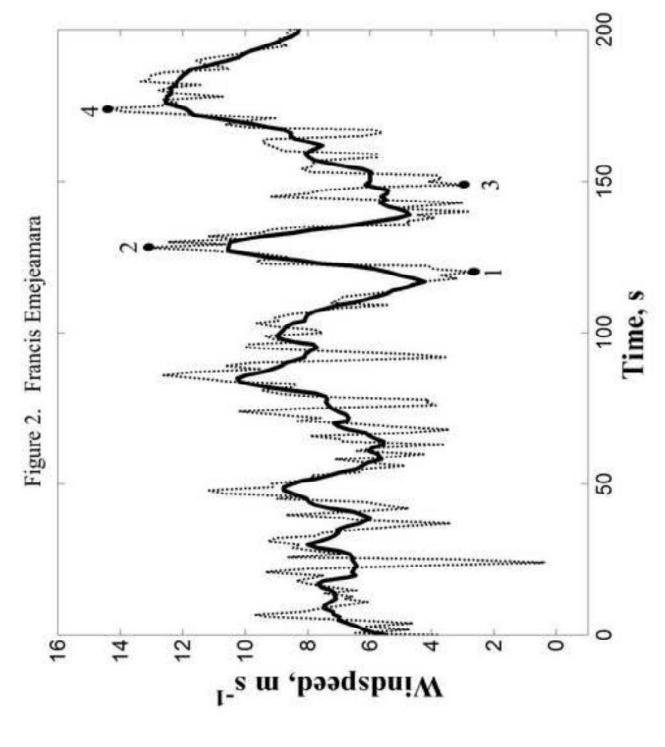


**Table 4:** Mean absolute percentage errors (%) compared over 3 test sites at different  $T_c$  using the *EEC* analytical model.

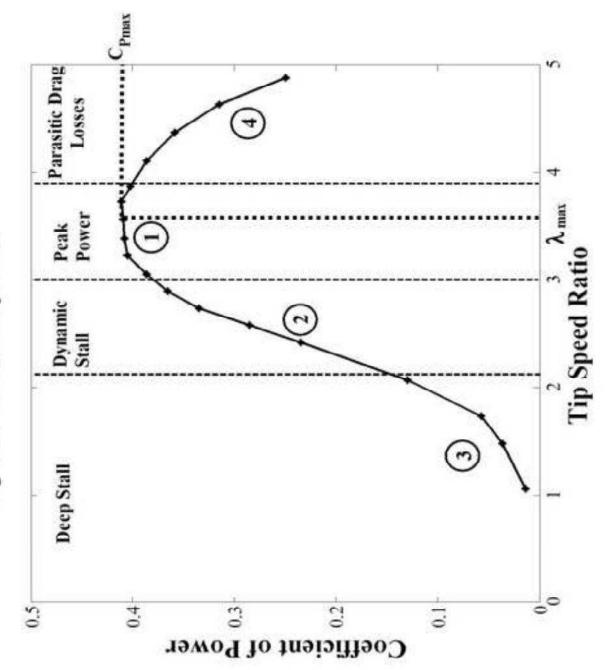
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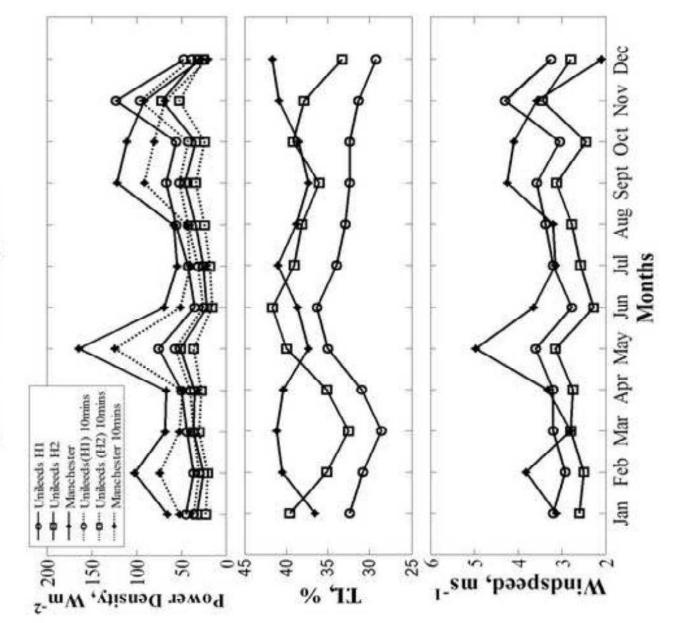


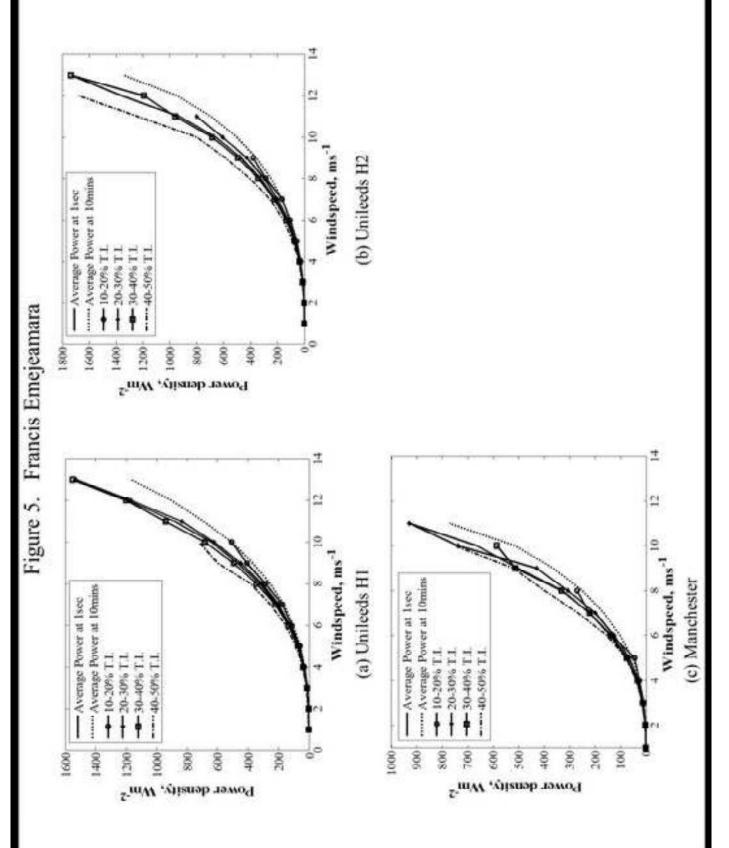






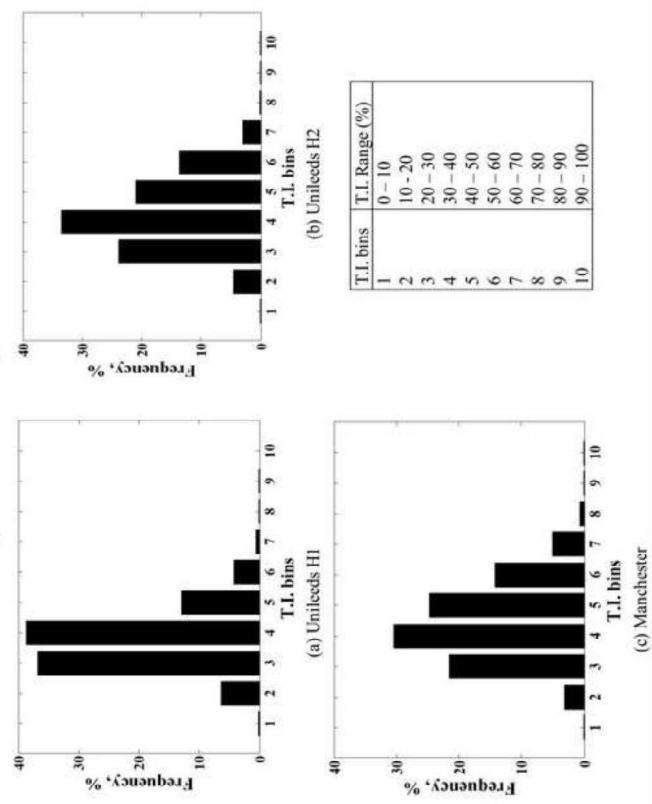
# Figure 4. Francis Emejeamara



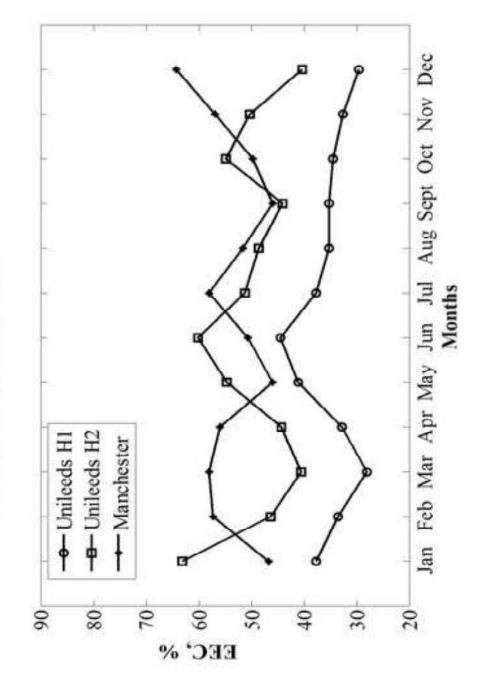




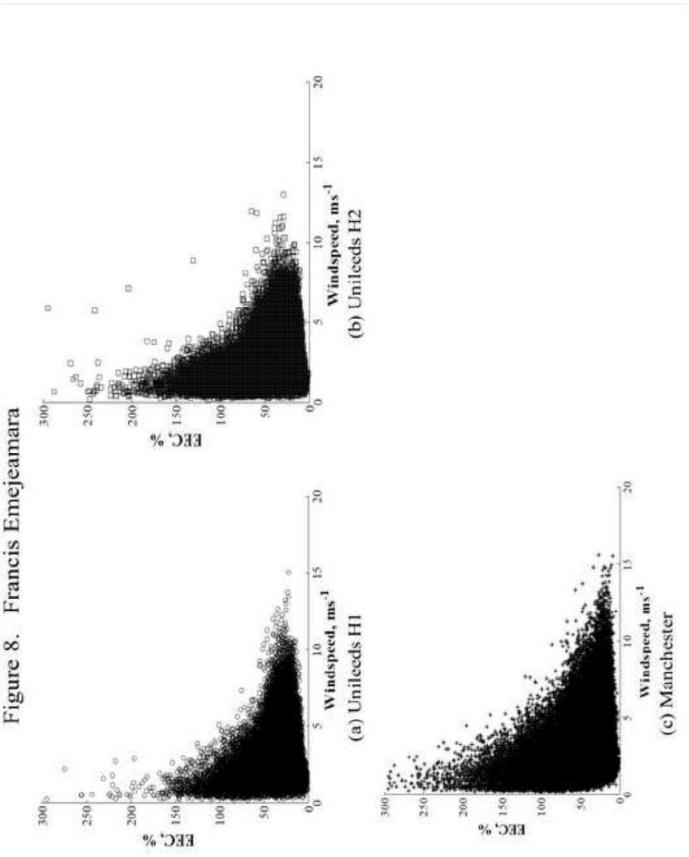




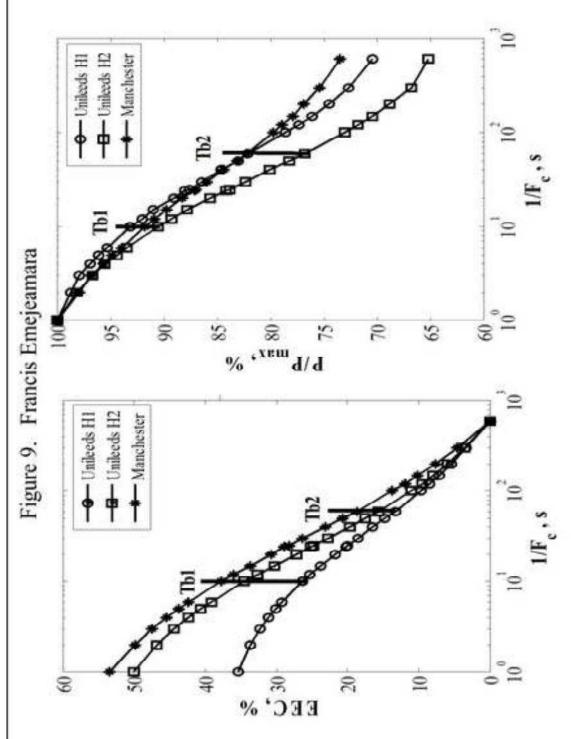












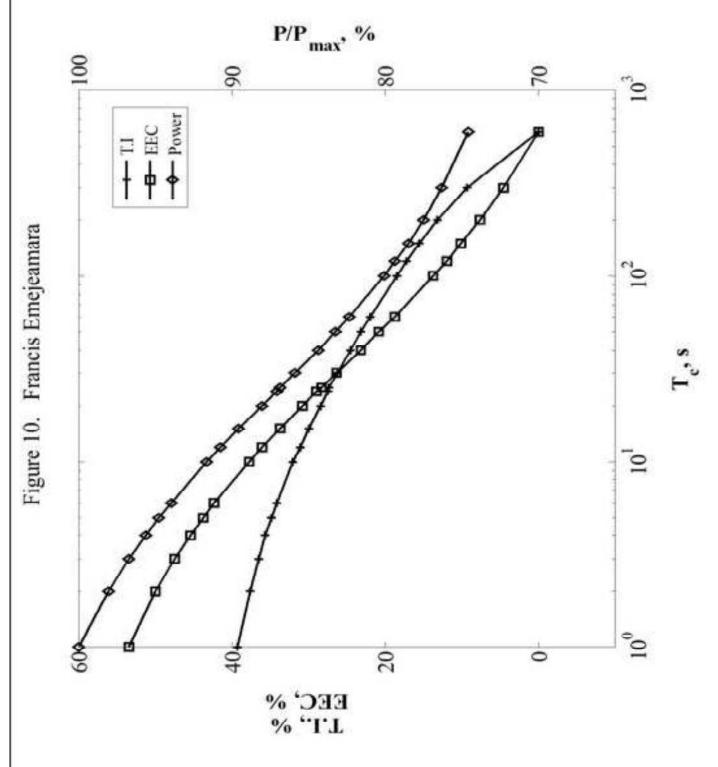


Figure 10 Click here to download high resolution image

