



Observation of Spin-Dependent Charge Symmetry Breaking in ΛN Interaction: Gamma-Ray Spectroscopy of ${}^4_{\Lambda}\text{He}$

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The energy spacing between the spin-doublet bound state of ${}^4_{\Lambda}\text{He}(1^+, 0^+)$ was determined to be $1406 \pm 2 \pm 2$ keV, by measuring γ rays for the $1^+ \rightarrow 0^+$ transition with a high efficiency germanium detector array in coincidence with the ${}^4\text{He}(K^-, \pi^-){}^4_{\Lambda}\text{He}$ reaction at J-PARC. In comparison to the corresponding energy spacing in the mirror hypernucleus ${}^4_{\Lambda}\text{H}$, the present result clearly indicates the existence of charge symmetry breaking (CSB) in ΛN interaction. By combining the energy spacings with the known ground-state binding energies, it is also found that the CSB effect is large in the 0^+ ground state but is vanishingly small in the 1^+ excited state, demonstrating that the ΛN CSB interaction has spin dependence.

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Charge symmetry is a basic concept in nuclear physics which holds almost exactly for atomic nuclei. It should also hold in the ΛN interaction and Λ hypernuclei; the Λp and Λn interactions and the Λ binding energies (B_{Λ}) between a pair of mirror Λ hypernuclei such as ${}^4_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{He}$ should be identical under this symmetry.

In the NN interaction and ordinary nuclei, effects of charge symmetry breaking (CSB) have been observed, for example, in the ${}^3\text{H}$ and ${}^3\text{He}$ binding-energy difference of 70 keV and the nn and pp scattering length difference of $a_{nn} - a_{pp} = -1.5 \pm 0.5$ fm (both corrected for large Coulomb effects). In meson-exchange models, those effects are suggested to be explained by $\rho^0 - \omega$ mixing (see Ref. [1], for example).

On the other hand, there has been a long-standing puzzle in CSB for the ΛN interaction; the reported CSB effects are relatively large, having yet to be theoretically explained. Old experiments using emulsion techniques reported B_{Λ} of the ground states of ${}^4_{\Lambda}\text{H}(0^+)$ and ${}^4_{\Lambda}\text{He}(0^+)$ to be 2.04 ± 0.04 MeV and 2.39 ± 0.03 MeV, respectively [2], giving a B_{Λ} difference $\Delta B_{\Lambda}(0^+) = B_{\Lambda}({}^4_{\Lambda}\text{He}(0^+)) - B_{\Lambda}({}^4_{\Lambda}\text{H}(0^+)) = 0.35 \pm 0.05$ MeV. Theoretical efforts have been made since the 1960s [3] to account for the $\Delta B_{\Lambda}(0^+)$ value, but contemporary quantitative studies fail to give a $\Delta B_{\Lambda}(0^+)$ value larger than 100 keV; for example, a four-body $YNNN$ coupled-channel calculation with $Y = \Lambda$ and Σ using the widely accepted baryon-baryon interaction model (NSC97e) gives $\Delta B_{\Lambda}(0^+) \sim 70$ keV [4].

To resolve this problem, confirmation and improvement of experimental data on CSB are also necessary. Since systematic errors are not well evaluated in the old emulsion data for B_Λ , new data, ideally also gathered by different experimental methods, have been awaited. Recently, the π^- momentum in the ${}^4_\Lambda\text{H} \rightarrow {}^4\text{He} + \pi^-$ weak decay was precisely measured at MAMI-C [5], and the obtained value of $B_\Lambda({}^4_\Lambda\text{H}(0^+)) = 2.12 \pm 0.01(\text{stat}) \pm 0.09(\text{syst})$ MeV is consistent with the emulsion value.

The B_Λ difference for the excited 1^+ states provides additional important information on the spin dependent CSB effect from which the origin of CSB can be studied. The B_Λ values for the 1^+ state are obtained via the $1^+ \rightarrow 0^+$ γ -ray transition energies. The ${}^4_\Lambda\text{H}$ γ ray was measured three times, and the ${}^4_\Lambda\text{H}(1^+, 0^+)$ energy spacing was determined to be 1.09 ± 0.02 MeV as the weighted average of these three measurements (1.09 ± 0.03 MeV [6], 1.04 ± 0.04 MeV [7], and 1.114 ± 0.030 MeV [8]), as shown in Fig. 1 (on the left). On the other hand, observation of the ${}^4_\Lambda\text{He}$ γ ray was reported only once by an experiment with stopped K^- absorption on a ${}^7\text{Li}$ target, which claimed the $(1^+, 0^+)$ energy spacing to be 1.15 ± 0.04 MeV [7]. This result suggests a significantly large CSB effect also in the 1^+ state with $\Delta B_\Lambda(1^+) = 0.29 \pm 0.06$ MeV. However, this ${}^4_\Lambda\text{He}$ γ -ray spectrum is statistically insufficient, and identification of the ${}^4_\Lambda\text{He}$ hyperfragment through high energy γ rays attributed to the ${}^4_\Lambda\text{He} \rightarrow {}^4\text{He} + \pi^0$ weak decay seems to be ambiguous.

In order to clarify this situation, we performed a γ -ray spectroscopic experiment for ${}^4_\Lambda\text{He}$ at J-PARC [9], in which the 1^+ excited state of ${}^4_\Lambda\text{He}$ was directly produced via the ${}^4\text{He}(K^-, \pi^-)$ reaction with a 1.5 GeV/ c K^- beam, and γ rays were measured using germanium (Ge) detectors with

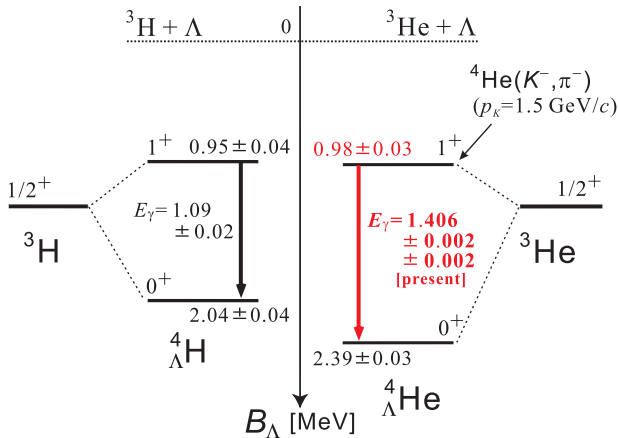


FIG. 1 (color online). Level schemes of the mirror hypernuclei, ${}^4_\Lambda\text{H}$ and ${}^4_\Lambda\text{He}$. Λ binding energies (B_Λ) of ${}^4_\Lambda\text{H}(0^+)$ and ${}^4_\Lambda\text{He}(0^+)$ are taken from past emulsion experiments [2]. $B_\Lambda({}^4_\Lambda\text{He}(1^+))$ and $B_\Lambda({}^4_\Lambda\text{H}(1^+))$ are obtained using the present data and past γ -ray data [6–8], respectively. Recently, $B_\Lambda({}^4_\Lambda\text{H}(0^+)) = 2.12 \pm 0.01(\text{stat}) \pm 0.09(\text{syst})$ MeV was obtained with an independent technique [5].

an energy resolution one order of magnitude better than that of the NaI counters used in all of the previous ${}^4_\Lambda\text{H}$ and ${}^4_\Lambda\text{He}$ γ -ray experiments. In this Letter, we present the result which clearly supersedes the previously claimed γ -ray transition energy and firmly establishes the level scheme of ${}^4_\Lambda\text{He}$, as shown in Fig. 1 (on the right).

The J-PARC E13 experiment was carried out at the K1.8 beam line in the J-PARC Hadron Experimental Facility [10]. The ${}^4\text{He}(K^-, \pi^-)$ reaction was used to produce ${}^4_\Lambda\text{He}(1^+)$, which was populated via the spin-flip amplitude of the $K^- + n \rightarrow \Lambda + \pi^-$ process. A beam momentum of 1.5 GeV/ c was chosen considering the elementary cross section of the spin-flip Λ production and the available beam intensity. A 2.8 g/ cm^2 -thick liquid ${}^4\text{He}$ target was irradiated with a total of 2.3×10^{10} kaons. A K^- beam ($K^-/\pi^- = 2 \sim 3$) was delivered to the target with a typical intensity of 3×10^5 over a 2.1 s duration of the beam spill occurring every 6 s. Incident K^- and outgoing π^- mesons were particle identified and momentum analyzed by the beam line spectrometer and the Superconducting Kaon Spectrometer (SKS) [11], respectively. In addition, γ rays were detected by a Ge detector array (Hyperball-J) surrounding the target. Through a coincidence measurement between these spectrometer systems and Hyperball-J, γ rays from hypernuclei were measured. The detector system surrounding the target is shown in Fig. 2.

The detector setting in SKS was configured for γ -ray spectroscopic experiments via the (K^-, π^-) reaction (SksMinus). SksMinus had a large acceptance (~ 100 msr) for detecting the outgoing pions in the laboratory scattering angle range of $\theta_{K\pi} = 0^\circ - 20^\circ$. The

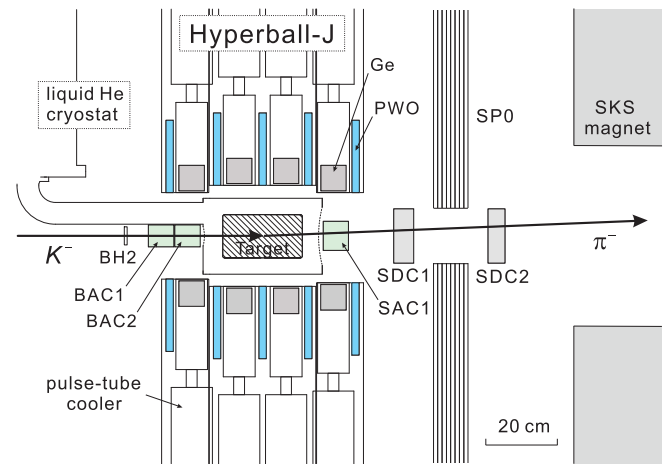


FIG. 2 (color online). A schematic view of the experimental setup around the liquid ${}^4\text{He}$ target (side view). SKS is a superconducting dipole magnet (2.5 T); BH2 is a plastic scintillation counter hodoscope; BAC1,2 and SAC1 are aerogel Čerenkov counters with $n = 1.03$; SDC1,2 are drift chambers. SP0 is an electromagnetic shower counter to tag high energy photons from π^0 decay. Hyperball-J consists of 27 Ge detectors, each surrounded by PWO counters for background suppression.

(K^-, π^-) reaction events were identified with threshold-type aerogel Čerenkov counters at the trigger level and by time of flight in the off-line analysis. The ${}^4_\Lambda\text{He}$ mass was calculated as the missing mass of the ${}^4\text{He}(K^-, \pi^-)$ reaction. A detailed description of the spectrometer system and of the analysis procedure for calculating missing mass will be reported elsewhere.

Hyperball-J is a newly developed Ge detector array for hypernuclear γ -ray spectroscopy [12]. The array can be used in high intensity hadron beam conditions by introducing mechanical cooling of the Ge detectors [13]. The array consisted of 27 Ge detectors in total, equipped with PbWO_4 (PWO) counters surrounding each Ge crystal to suppress background events such as Compton scattering and high energy photons from π^0 decay. The Ge detectors were of the coaxial type with a 60% relative efficiency. The Ge crystals covered a solid angle of $0.24 \times 4\pi$ sr in total, with the source point at the center. The total absolute photopeak efficiency was $\sim 4\%$ for 1 MeV γ rays when taking account of self-absorption in the target material. Energy calibration was performed over the 0.6–2.6 MeV range, by using data taken with Thorium-series γ rays in the period without the beam spill. The systematic error in the energy calibration was estimated to be 0.5 keV for that energy region. The energy resolution was 5 keV (FWHM) at 1.4 MeV after summing up data for all the detectors. The resolution was slightly worse during the beam spill period.

The selected events were those in which a Ge detector was hit within a typical time gate of 50 ns, and corresponding PWO counters had no hit during the 50 ns coincidence period. In the (K^-, π^-) reaction at 1.5 GeV/c, produced hypernuclei have recoil velocities (β) of 0.03–0.10, which lead to a stopping time longer than 20 ps in the target material. The ${}^4_\Lambda\text{He}(1^+ \rightarrow 0^+)$ M1 transition with an energy of ~ 1 MeV is estimated to have a lifetime of ~ 0.1 ps, assuming weak coupling between the core nucleus and the Λ [14]. Therefore, the γ -ray peak shape is expected to be Doppler broadened. We applied an event-by-event correction to the γ -ray energy by using the measured recoil momentum of ${}^4_\Lambda\text{He}$, the reaction vertex position, and the position of the Ge detector. It is noted that the Doppler-shift correction leaves 0.1% uncertainty in the measured γ -ray energy, where the dominant contribution comes from uncertainties (± 5 mm) associated with positions of the Hyperball-J apparatus with respect to the magnetic spectrometer systems. Details of the analysis procedures are almost the same as the previous hypernuclear γ -ray spectroscopic experiments [15].

Figure 3 shows the missing mass spectrum for ${}^4_\Lambda\text{He}$ as a function of the excitation energy, E_{ex} . Events with scattering angles ($\theta_{K\pi}$) larger than 3.5° were selected to reduce the background due to beam $K^- \rightarrow \pi^- + \pi^0$ events which kinematically overlap with hypernuclear production events at $\theta_{K\pi} = 0^\circ\text{--}3^\circ$. The background spectrum associated with materials other than liquid helium, as well as with K^- beam

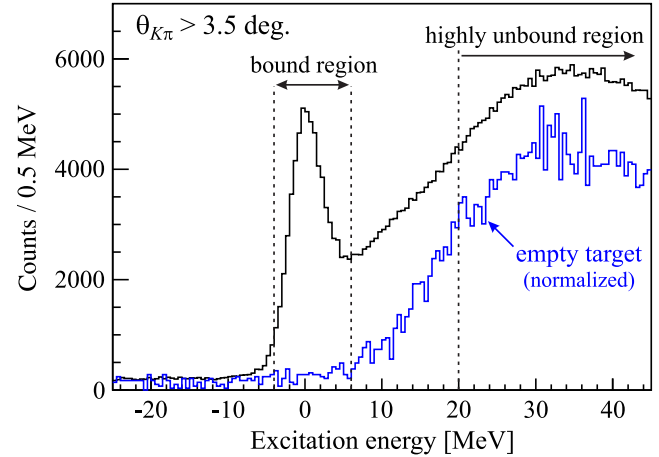


FIG. 3 (color online). The missing mass spectrum for the ${}^4\text{He}(K^-, \pi^-){}^4_\Lambda\text{He}$ kinematics plotted as a function of the excitation energy, E_{ex} , where events with scattering angles ($\theta_{K\pi}$) larger than 3.5° are selected. Black and blue lines show a spectrum with and without liquid helium, respectively.

decay events, was obtained with the empty target vessel, as shown together in Fig. 3; it is evident that the observed peak originates from the ${}^4\text{He}(K^-, \pi^-)$ reaction. According to a theoretical calculation, the ${}^4_\Lambda\text{He}(0^+)$ ground state is predicted to be predominantly populated, while the ${}^4_\Lambda\text{He}(1^+)$ excited state is produced at a lower rate [$\sim 1/4$ of ${}^4_\Lambda\text{He}(0^+)$] [16]. Therefore, the obtained peak is composed of ${}^4_\Lambda\text{He}(0^+)$ with a small contribution from ${}^4_\Lambda\text{He}(1^+)$, and the peak width of 5 MeV (FWHM) approximately corresponds to the missing mass resolution. The energy region for bound ${}^4_\Lambda\text{He}$ is $E_{\text{ex}} = 0\text{--}2.39$ MeV (see Fig. 1). Thus, the region of $-4 < E_{\text{ex}} < +6$ MeV was chosen for event selection of the ${}^4_\Lambda\text{He}$ bound state that is allowed for γ decay.

Figure 4 shows mass-gated γ -ray energy spectra. Figures 4(a) and 4(b) are the spectra without and with the Doppler-shift correction, respectively, when the highly unbound region ($E_{\text{ex}} > +20$ MeV) of ${}^4_\Lambda\text{He}$ is selected. Figure 4(c) is the spectrum without the Doppler-shift correction for the ${}^4_\Lambda\text{He}$ bound region. Only after the event-by-event Doppler-shift correction, the 1406-keV peak is clearly visible, as shown in Fig. 4(d). The peak at 1406 keV is assigned to the spin-flip M1 transition between the spin-doublet states, ${}^4_\Lambda\text{He}(1^+ \rightarrow 0^+)$, because no other state which emits γ rays is expected to be populated in the selected excitation energy region. This assignment is also consistent with the fact that the peak appears after the Doppler-shift correction.

Figure 5(a) shows simulated γ -ray peak shapes. The thin black line is for a γ ray emitted at rest, the dotted red line for a γ ray emitted immediately after the reaction where ${}^4_\Lambda\text{He}$ has a maximum β before slowing down in the target material, and the thick blue line for a γ ray with Doppler-shift correction applied to the dotted red line. The observed peak shape shown in Fig. 5(b) agrees with a simulated one to which the Doppler correction was applied, reflecting

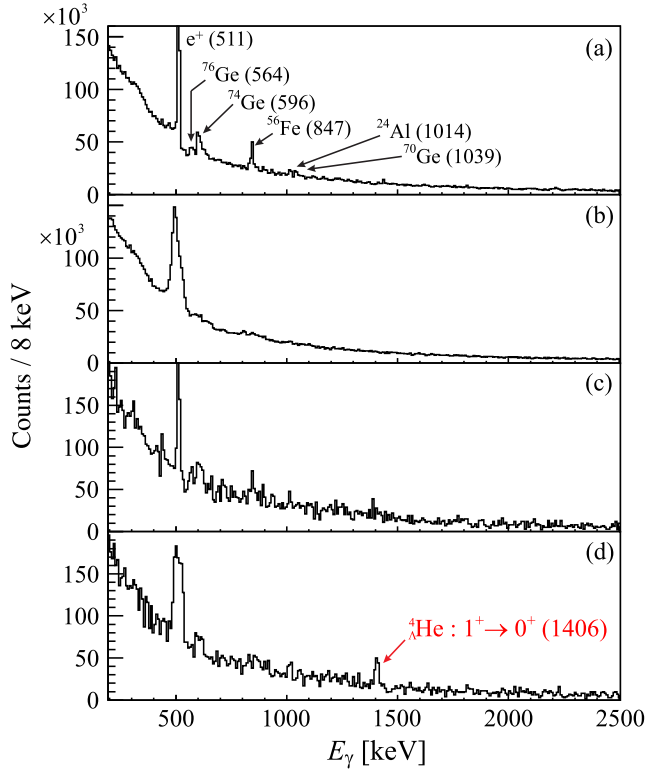


FIG. 4 (color online). γ -ray energy spectra measured by Hyperball-J in coincidence with the ${}^4\text{He}(K^-, \pi^-)$ reaction. Missing mass selections are applied to the highly unbound region ($E_{\text{ex}} > +20$ MeV) for (a) and (b), and to the ${}^4_{\Lambda}\text{He}$ bound region ($-4 < E_{\text{ex}} < +6$ MeV) for (c) and (d). An event-by-event Doppler correction is applied for (b) and (d). A single peak is observed in (d) attributed to the $M1(1^+ \rightarrow 0^+)$ transition.

ambiguities in the reconstructed vertex point and in the Ge detector positions. The peak fitting result for the Doppler-shift-corrected spectrum is presented in Fig. 5(b). The γ -ray energy and yield were extracted to be $1406 \pm 2(\text{stat}) \pm 2(\text{syst})$ keV and 95 ± 13 counts, respectively, with a peak significance of 7.4σ and a reduced χ^2 of 1.2. A dominant source of the systematic error comes from position inaccuracy of the reaction vertex and of the Ge detectors for correcting the Doppler shift. The peak energy varies less than 1 keV with different background functions used in the fitting. The obtained yield is consistent with an expected value based on a distorted-wave impulse approximation calculation [16] within a factor of 3.

In the present work, the γ -ray transition of ${}^4_{\Lambda}\text{He}(1^+ \rightarrow 0^+)$ was unambiguously observed, and the excitation energy of the ${}^4_{\Lambda}\text{He}(1^+)$ state was precisely determined to be $1.406 \pm 0.002 \pm 0.002$ MeV, by adding a nuclear recoil correction of 0.2 keV. By comparing it to the previously measured spacing of ${}^4_{\Lambda}\text{H}$ (1.09 ± 0.02 MeV), the existence of CSB in the ΛN interaction has been definitively confirmed. It is to be mentioned that two old experiments using stopped K^- on ${}^6\text{Li}$ and ${}^7\text{Li}$ targets had reported hints of unassigned γ -ray peaks at 1.42 ± 0.02 MeV [17]

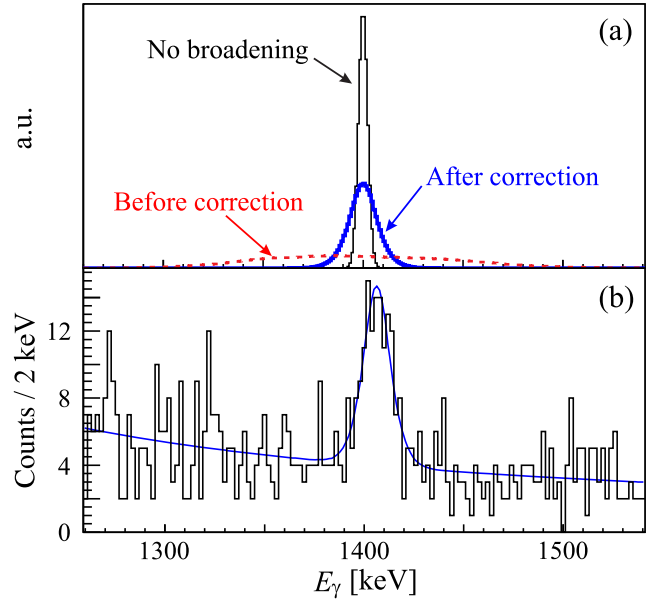


FIG. 5 (color online). (a) Simulated shapes of a 1.4 MeV γ -ray peak: the thin black line corresponds to a γ ray emitted at rest, the dotted red line to a γ ray emitted by the recoiling ${}^4_{\Lambda}\text{He}$. The thick blue line is the result of the Doppler-shift correction applied to the dotted one. (b) The fit of the simulated peak shape to the present data.

and 1.45 ± 0.05 MeV [6], respectively. It is presumed that those γ rays came from ${}^4_{\Lambda}\text{He}$ produced as a hyperfragment. By combining the emulsion data of $B_{\Lambda}({}^4_{\Lambda}\text{He}(0^+))$, the present result gives $B_{\Lambda}({}^4_{\Lambda}\text{He}(1^+)) = 0.98 \pm 0.03$ MeV, as shown in Fig. 1. By comparing it to $B_{\Lambda}({}^4_{\Lambda}\text{H}(1^+)) = 0.95 \pm 0.04$ MeV, obtained from the emulsion data of $B_{\Lambda}({}^4_{\Lambda}\text{H}(0^+))$ and the ${}^4_{\Lambda}\text{H}$ γ -ray data, the present result leads to $\Delta B_{\Lambda}(1^+) = B_{\Lambda}({}^4_{\Lambda}\text{He}(1^+)) - B_{\Lambda}({}^4_{\Lambda}\text{H}(1^+)) = 0.03 \pm 0.05$ MeV. Therefore, the CSB effect is strongly spin dependent, being at least one order of magnitude smaller in the 1^+ state than in the 0^+ state. This demonstrates that the underlying ΛN CSB interaction has spin dependence. Our finding suggests that Σ mixing in Λ hypernuclei is responsible for the CSB effect since the 1^+ state in ${}^4_{\Lambda}\text{H}/{}^4_{\Lambda}\text{He}$ receives a one order of magnitude smaller energy shift due to Λ - Σ mixing than the 0^+ state [18,19], which is caused by strong ΛN - ΣN interaction in the two-body spin-triplet channel.

Recently, Gal estimated the CSB effect [20] using a central-force ΛN - ΣN interaction (the D2 potential in Ref. [18]), in contrast to the widely used tensor-force dominated ΛN - ΣN interaction in the Nijmegen one-boson exchange models. His $\Delta B_{\Lambda}(1^+)$ values are in agreement with the present observation. Further theoretical studies may reveal not only the origin of the CSB effect but also the properties of Λ - Σ mixing in hypernuclei.

In summary, the J-PARC E13 experiment clearly identified a γ -ray transition from ${}^4_{\Lambda}\text{He}$ produced by the ${}^4\text{He}(K^-, \pi^-)$ reaction and determined the energy spacing

between the spin-doublet states ($1^+, 0^+$) to be $1406 \pm 2(\text{stat}) \pm 2(\text{syst})$ keV, which is apparently different from the ${}^4_\Lambda\text{H}$ spacing of 1.09 ± 0.02 MeV. Therefore, the existence of CSB in the ΛN interaction has been confirmed via γ -ray spectroscopy alone. Combined with the emulsion data of $B_\Lambda(0^+)$, the present result indicates a large spin dependence in the CSB effect, pronounced in the 0^+ state while vanishingly small in the 1^+ state. We believe that the present finding provides crucial information for understanding the ΛN - ΣN interaction and eventually baryon-baryon interactions.

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- [1] G. A. Miller, A. K. Opper, and E. J. Stephenson, *Annu. Rev. Nucl. Part. Sci.* **56**, 253 (2006).
- [2] M. Jurić *et al.*, *Nucl. Phys.* **B52**, 1 (1973).
- [3] R. H. Dalitz and F. Von Hippel, *Phys. Lett.* **10**, 153 (1964).
- [4] A. Nogga, H. Kamada, and W. Glöckle, *Phys. Rev. Lett.* **88**, 172501 (2002), and references therein.
- [5] A. Esser *et al.*, *Phys. Rev. Lett.* **114**, 232501 (2015).
- [6] M. Bedjidian, A. Filipkowski, J. Y. Grossiord, A. Guichard, M. Gusakov, S. Majewski, H. Piekarz, J. Piekarz, and J. R. Pizzi, *Phys. Lett.* **62B**, 467 (1976).
- [7] M. Bedjidian *et al.*, *Phys. Lett.* **83B**, 252 (1979).
- [8] A. Kawachi, Ph.D. thesis, University of Tokyo, 1997 (unpublished).
- [9] H. Tamura, M. Ukai, T. O. Yamamoto, and T. Koike, *Nucl. Phys.* **A881**, 310 (2012).
- [10] K. Agari *et al.*, *Prog. Theor. Exp. Phys.* (2012), 02B009.
- [11] T. Takahashi *et al.*, *Prog. Theor. Exp. Phys.* (2012), 02B010.
- [12] T. Koike *et al.*, in *Proceedings of the 9th International Conference on Hypernuclear and Strange Particle Physics (HYP2006), Mainz, Germany, 2006*, edited by J. Pochodzalla and T. Walcher (Springer, New York, 2007), p. 25.
- [13] T. Koike *et al.*, *Nucl. Instrum. Methods Phys. Res., Sect. A* **770**, 1 (2015).
- [14] R. Dalitz and A. Gal, *Ann. Phys. (N.Y.)* **116**, 167 (1978).
- [15] M. Ukai *et al.*, *Phys. Rev. C* **77**, 054315 (2008).
- [16] T. Harada (private communication).
- [17] A. Bamberger, M. A. Faessler, U. Lynen, H. Piekarz, J. Piekarz, J. Pniewski, B. Povh, H. G. Ritter, and v Soergel, *Nucl. Phys.* **B60**, 1 (1973).
- [18] Y. Akaishi, T. Harada, S. Shinmura, and K. S. Myint, *Phys. Rev. Lett.* **84**, 3539 (2000).
- [19] E. Hiyama, M. Kamimura, T. Motoba, T. Yamada, and Y. Yamamoto, *Phys. Rev. C* **65**, 011301 (2001).
- [20] A. Gal, *Phys. Lett. B* **744**, 352 (2015).