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# Resonance Effect in Chatter Formation in Metal Cutting

A New Chatter Theory Based on Chip Serration  
Instability and System Response for Prediction of  
Chatter in End Milling

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**Impressum/Imprint (nur für Deutschland/only for Germany)**

Bibliografische Information der Deutschen Nationalbibliothek: Die Deutsche Nationalbibliothek verzeichnet diese Publikation in der Deutschen Nationalbibliografie; detaillierte bibliografische Daten sind im Internet über <http://dnb.d-nb.de> abrufbar.

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Coverbild: [www.ingimage.com](http://www.ingimage.com)

Verlag: LAP LAMBERT Academic Publishing GmbH & Co. KG  
Dudweiler Landstr. 99, 66123 Saarbrücken, Deutschland  
Telefon +49 681 3720-310, Telefax +49 681 3720-3109  
Email: [info@lap-publishing.com](mailto:info@lap-publishing.com)

Herstellung in Deutschland:  
Schaltungsdienst Lange o.H.G., Berlin  
Books on Demand GmbH, Norderstedt  
Reha GmbH, Saarbrücken  
Amazon Distribution GmbH, Leipzig  
ISBN: 978-3-8443-0447-3

**Imprint (only for USA, GB)**

Bibliographic information published by the Deutsche Nationalbibliothek: The Deutsche Nationalbibliothek lists this publication in the Deutsche Nationalbibliografie; detailed bibliographic data are available in the Internet at <http://dnb.d-nb.de>.

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Cover image: [www.ingimage.com](http://www.ingimage.com)

Publisher: LAP LAMBERT Academic Publishing GmbH & Co. KG  
Dudweiler Landstr. 99, 66123 Saarbrücken, Germany  
Phone +49 681 3720-310, Fax +49 681 3720-3109  
Email: [info@lap-publishing.com](mailto:info@lap-publishing.com)

Printed in the U.S.A.  
Printed in the U.K. by (see last page)  
ISBN: 978-3-8443-0447-3

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