# The Use Of Digital Signal Processing in Satellite Communication

by

Jonathan Richard Bramwell.

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# The Use Of Digital Signal Processing in Satellite Communication by Jonathan Richard Bramwell.

#### Abstract

The recent emphasis on Information Technology has increased the need for methods of data communications with a greater interest in the areas of Satellite communications. Data communications over a satellite can be easily achieved by the use of excessive power and bandwidth but efficient management of the satellite resource requires more elegant means of transmission. The optimum modulator and demodulator can be described by mathematical expressions to represent the physical processes that are required to transmit and receive a signal. Digital Signal Processing circuits can be use to implement these mathematical functions and once correctly designed are not susceptible to variations in accuracy and hence can maintain an accurate representation of the mathematical model.

This thesis documents an investigation into the algorithms and techniques that can be used in the digital implementation of a Satellite Data Modem. The technique used for carrier phase recovery and data decoding is a major variation on a method proposed by Viterbi and Viterbi and relies on Phase Estimation instead of the more common carrier regeneration techniques. A computer simulation of this algorithm and its performance is described and the overall performance of the simulation is compared to theoretical analysis and experimental performance of a Multi-Data Rate Satellite Modem covering data rates in the range 16 Ksymbol/sec to 256 Ksymbol/sec in both the BPSK and QPSK data formats.

#### Introduction.

The recent emphasis on Information Technology has increased the need for methods of data communications with a greater interest in the areas of Satellite communications. communications over a satellite can be easily achieved by the use of excessive power and bandwidth but efficient management of the satellite resource requires more elegant means of transmission. Many methods have been devised and the principles are outlined in several good communications text book <3,5,6,9,10,13> along with the theoretical solutions for solving the problems that communications bring i.e. Narrow bandwidths and high phase noise, Low signal power, large frequency errors, noise, etc. However, many solutions are theoretically possible but practically beyond, or at the edge of, analogue technology and so difficult to implement. Until recently the modulation and demodulation of all signals relied on use of analogue circuitry to generate the modulated signal and to demodulate the received signal. The optimum modulator can be described by a mathematical expression to represent the physical processes that are required to modulate and transmit a signal, Similarly the demodulator may be represented by a similar set mathematical expressions. However, the use of analogue components to implement these mathematical expressions the modulation and demodulation processes is only an approximation of the mathematical process required hence a revision is required of the mathematical model. This results in the model now being non-optimum. The major cause of this effect is due to the individual components only approximating to a required function, i.e. multiplier, adder, integrator etc. Often these approximations are perfectly valid over a range of interest but require much development work to implement the function correctly and difficulty in maintaining accuracy. With the increase in

processing speeds now available in Large Scale Integration (LSI) and Very Large Scale Integration (VLSI) digital circuits the use of analogue components is no longer only viable alternative. The use of digital circuits can implement these mathematical functions precisely with only limitations being set by the sampling frequency and the required signal to quantization noise at the the number of the bits within representation. It may also enable functions to be implemented that are almost impossible to create using analogue techniques ,i.e. close approximations to Non causal filters. The digital implementation is also, correctly designed, not susceptible to variations accuracy and hence can maintain an accurate representation of the mathematical model.

This thesis documents an investigation into the algorithms and techniques that can be used in the implementation of a Satellite Data Modem. The research into the design of such a modem was funded and initiated by the Department of Trade and Industry (DTI) and will be taken into production with the collaboration of Telemetrix Research Ltd, of Tewkesbury, Gloucestershire, UK. specification for the modem was laid down by the DTI and is given in Appendix A. The basic requirement was digital modem that could employ Binary Phase Shift Keying (BPSK) or Quadrature Phase Shift Keying (QPSK) with absolute decoding over a range of data rates from Ksymbols/sec to 256 Ksymbols/sec with an extension up 4.096 Msymbols/sec. These data rates were required to quickly switchable over the entire range. As a first in devising the best Digital Signal Processing (DSP) algorithms the mathematical models of the transmitting and receiving functions need to be described for different signalling formats. This will then enable the modulator and demodulator to be implemented in Digital hardware. This

algorithm and hardware examination is divided into sections documenting the modulator and the demodulator, sub-sections on digital demodulation, filtering, decoding and carrier phase recovery. The technique used for carrier phase recovery and data decoding is a major variation on a method proposed by Viterbi and Viterbi <26> but correcting all the errors and problems imposed by the Viterbi's technique. These new proposals are thought to be unique and have been patented <19>. A computer simulation of this algorithm and its performance is described and the overall performance of the simulation is compared to theoretical analysis and the experimental performance. The experimental results were obtained over a satellite link using the Intelsat 5A F11 satellite with the collaboration of British Telecomm International (BTI), Goonhilly Downs, Cornwall.

Suitable methods for modelling the signal to be transmitted and received are described below. Methods for digitally demodulating a signal ,either of a continuous nature (FM video signal), or of a discrete nature (BPSK/QPSK) are proposed.

# 2. Mathematical Modelling

# 2.1. Introduction to Mathematical Modelling of a Signal.

A mathematical model is a representation of a physical process. This model must be known at both the transmitter and receiver to enable the signal to be correctly modulated and demodulated. One model that is commonly used throughout communications systems is that of the Complex Envelope Representation.

# 2.1.1. The Complex Envelope Representation.

Any bandpass waveform can be represented in the form <6>:-

$$v(t) = Re[g(t).e^{j\omega c.t}]$$
 (Eq2.1.1.a)

where g(t) is the complex envelope of v(t)

$$g(t) = x(t) + j.y(t)$$
 (Eq2.1.1.b)

$$x(t) = A(t)Cos \Phi(t)$$
 (Eq2.1.1.c)

$$y(t) = A(t)Sin \Phi(t)$$
 (Eq2.1.1.d)

$$\Phi(t) = \tan^{-1}(y(t)/x(t))$$
 (Eq2.1.1.e)

with the  $tan^{-1}(.)$  function extended over four quadrants.

Where  $\omega c = 2.\pi$ . Fc., Fc is the carrier frequency of the bandpass signal and A(t) is the magnitude of the signal x(t), y(t), A(t) and  $\Phi(t)$  are all real baseband signals, while g(t) is a complex baseband signal.

By substitution , the bandpass waveform can therefore be fully represented by:-

 $v(t) = A(t)\cos \Phi(t).\cos \omega ct - A(t)\sin \Phi(t).\sin \omega ct$ 

(Eq2.1.1.f)

Often the x(t)= A(t) Cos  $\Phi(t)$  is called the In-phase component and y(t) = A(t).Sin  $\Phi(t)$  the Quadrature component. This model is also sometimes called the Quadrature Model.

The power of this model is considerable, not just in the representation of a bandpass signal from a baseband signal but also in the facts that if v(t) is deterministic then x(t),y(t),A(t), and  $\Phi(t)$  are also deterministic. It is similarly true if v(t) is a stochastic process, i.e. representing bandpass noise, then x(t),y(t),A(t) and  $\Phi(t)$  represent baseband noise and are similarly stochastic. As an example this model will be used to represent a Frequency Modulated (FM) Signal.

# 2.2. The FM Representation.

A FM signal can be represented by <5>:-

$$r(t) = A.Cos\{ \omega ct + K \begin{cases} t \\ m(t)dt + \theta(t) \end{cases}$$

$$(Eq2.2.a) .$$

where m(t) is the modulating signal, K is a constant proportional to the modulation index of the FM signal, and  $\theta(t)$  is an initial phase error at the receiver, which for simplicity is firstly consider to be zero.

Let 
$$K \int_{-\infty}^{\tau} m(t)dt = \Phi(t)$$
 (Eq2.2.b)

therefore

$$r(t)=A.\cos\{\omega ct + \Phi(t)\}\$$
 (Eq2.2.c)

by simple trigonometry this becomes:

$$r(t)=A.[\cos \Phi(t).\cos \omega ct - \sin \Phi(t).\sin \omega ct]$$
 (Eq2.2.d)

This can be clearly seen to be in the form of the complex envelope representation hence the components  $A.Cos\Phi(t)$  and  $A.Sin\Phi(t)$  are both baseband in nature and with a carrier frequency of  $\omega_c/2\pi$ . The object of the demodulator is to recover the modulating signal m(t).

If r(t) is able to be multiplied by Cos ct, which assumes a perfect phase reference, then the result is given by :-

$$r_{\rm I}({\sf t}) = {\sf A}\{{\sf Cos}\ \Phi({\sf t}).{\sf Cos}\ \omega{\sf ct}$$

$$- {\sf Sin}\ \Phi({\sf t}).{\sf Sin}\ \omega{\sf ct}\ \}.{\sf Cos}\ \omega{\sf ct}$$

$$= {\sf A}.\{ {\sf Cos}(\ \omega{\sf ct}\ +\ \Phi({\sf t})\}.{\sf Cos}\ \omega{\sf ct}$$

$$= {\sf A}.\{ {\sf Cos}(\ 2\omega{\sf ct}\ +\ \Phi({\sf t}))\ +\ {\sf Cos}\ \Phi({\sf t})\}$$

$$= ({\sf Eq2.2.e})$$

Low pass filtering to remove high order frequency components and normalising gives:-

$$r_{\tau}(t) = A.\cos \Phi(t)$$
 (Eq2.2.f)

Similarly if r(t) is multiplied by  $Sin \omega ct$  and filtered, the Quadrature component is obtained:-

$$r_{O}(t) = A.\sin \Phi(t)$$
 (Eq2.2.g)

The practical implementation of this process can be seen in fig 2.2.a.

From these two components it is possible to determine  $\Phi(t)$ :-

Defining

$$\Phi(t) = \Gamma^{-1} \left[ \frac{r_{Q}(t)}{r_{I}(t)} \right]$$
(Eq2.2.h)

Where

$$\Gamma^{-1}(.) = \underbrace{[1+\text{sign}(r_{Q}(t))]}_{2} \Phi'(t) + [1-\text{sign}(r_{I}(t))](\pi/2)$$

$$+ \underbrace{[1-\text{sign}(r_{Q}(t))]}_{2} \Phi'(t) - [1-\text{sign}(r_{I}(t))](\pi/2)$$

(Eq2.2.i)

and

$$\Phi'(t) = \operatorname{Tan}^{-1} \left[ \frac{r_{Q}(t)}{r_{I}(t)} \right]$$
(Eq2.2.j)

Sign(.) is the signature function defined as:-

$$sign(x) = \begin{bmatrix} 1 & for x \Rightarrow 0 \\ -1 & for x < 0 \end{bmatrix}$$

since 
$$\Phi(t) = K \begin{bmatrix} \tau \\ m(t)dt \\ -\infty \end{bmatrix}$$

$$m(t) = \underbrace{1.d\Phi(t)}_{K. dt}$$
 (Eq2.2.k)

and hence it is possible to resolve the value of m(t). It should be noted at this point that it can be shown that even if the phase reference contains an error then the effect in the receiver is removed by the differentiation to produce the same result as Eq 2.2.k above.

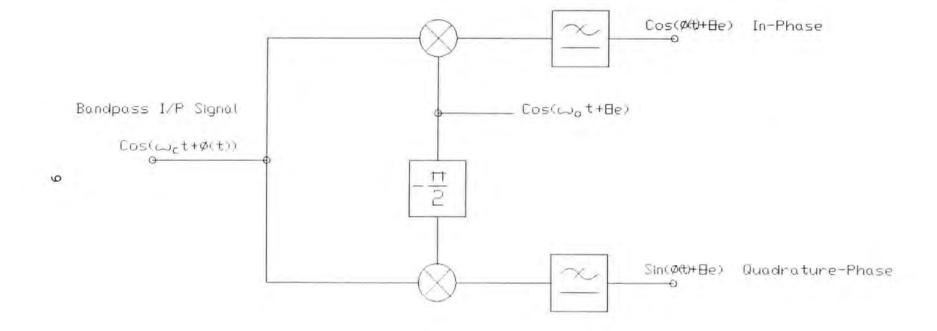


Fig 2.2.a Quadrature Down-Conversion Implementation

# 2.3. Frequency Spectra.

Considering Eq2.2.d it can be shown that this transforms into a frequency spectra consisting of both positive and negative frequencies around 0 Hz with a real component only as previously defined in Eq2.1.1.a and hence is more clearly described by :-

$$r(t) = A.\left[\begin{array}{c} e^{j(\omega ct + \Phi(t))} + e^{j(-\omega ct - \Phi(t))} \\ \hline 2 \end{array}\right]$$
(Eq2.3.a)

This can be expressed in diagrammatic form as in fig 2.3.a. When down-converted to baseband by a local oscillator with a perfect phase reference of Cos  $\omega$ ct the resultant before Low pass filtering is given by:-

$$r_{I}(t) = \underbrace{A \left[ e^{j(2\omega ct + \Phi(t))} + e^{-j(2\omega ct + \Phi(t))} \right]}_{4}$$

$$+ \underbrace{A \left[ e^{j\Phi(t)} + e^{-j\Phi(t)} \right]}_{4}$$
(Eq2.3.b)

This is shown in fig 2.3.b. Similarly with down-conversion using a quadrature local oscillator of Sin ct the resultant spectra is given by:-

$$r_{Q}(t) = A \left[ e^{j(2\omega ct + \Phi(t))} - e^{-j(2\omega ct + \Phi(t))} \right]$$

$$- A \left[ e^{j\Phi(t)} + e^{-j\Phi(t)} \right]$$

$$4j$$

$$4j$$

$$4j$$

$$(Eq2.3.c)$$

and can be seen in Fig 2.3.c.

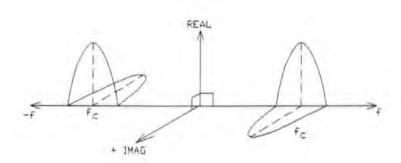
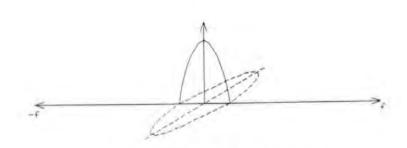


Fig 2.3.a Bandpass Frequency spectra



Baseband Real Component

Fig 2.3.b Frequency spectra for In-phase Channel

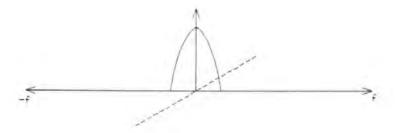


Fig 2.3.c Frequency Spectra For Quadrature Phase Channel

# 2.4. Processing of Quadrature Baseband Components.

Consider the digital implementation of a demodulator for the FM example above. As a practical example the signal be demodulated is a 30 MHz bandwidth, FM modulated TV signal transmitted over a KU band satellite link such Eutelsat F1 or Intelsat V F22. The signal is received from the satellite by a parabolic antenna (dish) of typically 1.2 metres diameter in the frequency range 10.95 to 11.7 GHz. The low noise amplifier and down-converter, amplify and convert the signal down to a 1st IF of approximately 1 GHz. A typical spectrum is shown in fig 2.4.a. Further analogue circuitry down-converts to a 2nd IF of 70 MHz, while also providing frequency selectivity to reduce spectrum to that of the wanted signal only. This signal at a suitable stage to input to a down-converter prior to the digital demodulator. operation of the frequency conversion is standard and will not be elaborated on further.

After frequency conversion to baseband, as described above, the signals must be low pass filtered. implementation the filters are implemented by the use analogue components. The bandpass signal was 30 Mhz but baseband this is reduced to 15 Mhz. Before digital processing can take place, the choice of sampling rate must take into account the bandwidth of the baseband analogue signal. Sampling theorem states that any continuous signal will be fully represented by a sequence of samples provided that the sampling frequency is at least twice the highest frequency present <6>. If this is not the case, then aliasing occurs and the resulting spectra is corrupted as shown in Fig 2.4.b. This implies that the received quadrature signals must be sampled at a rate of at least 30 Mhz. However the frequency ,at which the signal has

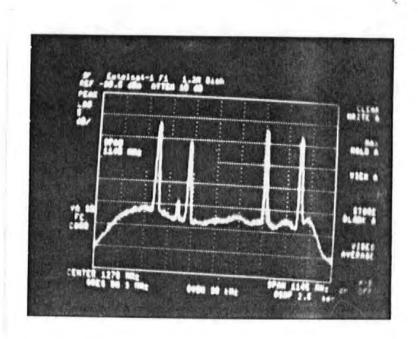
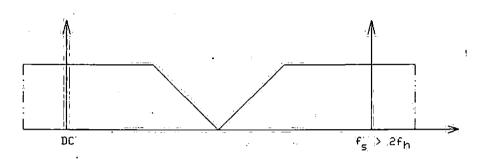


Fig 2.4.a Typical Received Spectrum for EutelSat F1

significant spectral components above -20 dB, extends to 17 MHz and therefore aliasing will occur unless sampled least at 35 MHz. As this is beyond the range of the digital components to operate, the baseband signals are filtered to 12.5 Mhz 3dB bandwidth with a 15 Mhz stopband, i.e. more than 30 dB attenuation at 15 MHz, using a 7th Order Elliptic filter as shown in fig 2.4.c. Therefore sampling can occur at 30 Mhz. This causes some degradation saturated colour performance by attenuating the wide deviation signals that these colours produce, although this degradation is tolerable in practice. One effect this attenuation is that the signal can now drop below the FM threshold, in these regions, when operating close to SNR threshold. This results in 'theshold events' or 'noise spikes' in the received picture . The demodulator must recover the modulating video signal and to achieve this two separate processes are required, as shown in the block diagram fig 2.4.d. The first process is to obtain the phase decoding the of the vector  $\Phi(t)$ . This is achieved by sampled Phase and Quadrature channels into a Phase angle by the use a Programmable Read Only Memory (PROM). The incoming baseband channels are each sampled at 30 MHz multiplexing two A/D converters sampling at 15MHz produce two 6 bit sample streams. The total number is 2<sup>12</sup> combinations for both channels, 12 bits, which can easily be accommodated in a single PROM. PROM would therefore be programmed with an algorithm to convert a 12 bit address to a 8 bit output which proportional to the phase of the vector. The algorithm used is therefore that of the extended  $Tan^{-1}$  function ( $\Gamma^{-1}(.)$ ), as previously described in Eq 2.2.h. The output is now a representation of the phase vector represented by the two quadrature channels. In the quadrature model analysis it was shown that to fully demodulate the received signal into the original modulating video signal, differentiation must take place. From the output phasor map, fig 2.4.e, it can



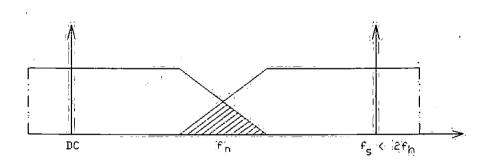
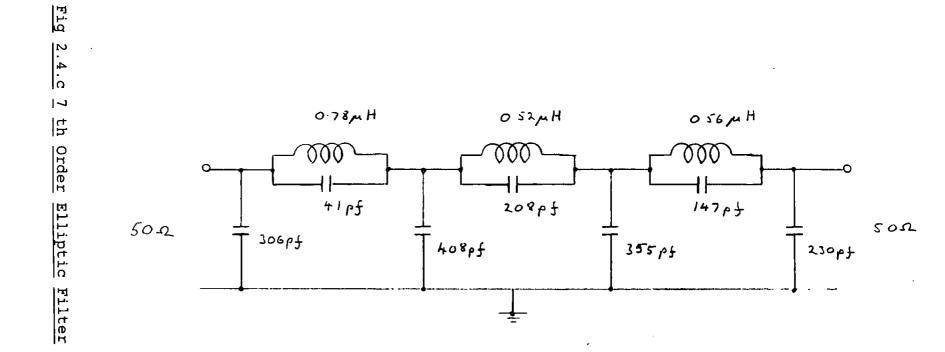


Fig 2.4.b Aliasing Frequency Spectra due to sampling frequency too low



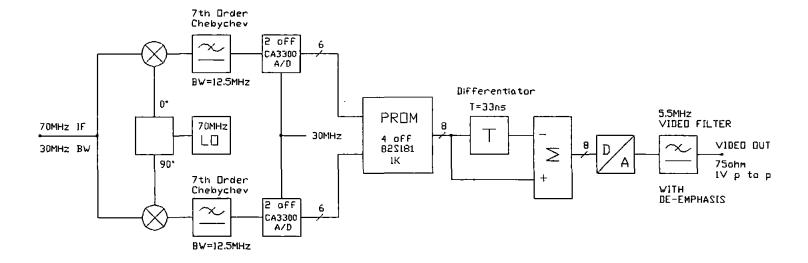


Fig 2.4.d Demodulation of an FM signal using Quadrature Down Conversion

be seen that the vector is represented as being a positive increasing value to a maximum of +180 degrees in an -clockwise direction and a negative increasing value to maximum of -180 degrees in the clockwise direction. difference value is obtained between two successive vector values, and in each case the 'shortest route' be taken. This is fully explained in a later section but obtained by interpretation can be sampling theory. Ιf rotating phasor of period a represented by two quadrature components is according to sampling theory, this sampling must take place at a frequency of  $2/\tau$ . Hence if the first sample occurs O degrees then the next sample occurs at the 180 point. If the period is less the  $\tau$  then the phasor difference will be less than 180 degrees. Since this is the case and we have defined the maximum phasor difference be 180 degrees by the sampling theorem then the phasor only have followed a path around the unit circle which less than 180 degrees. This is termed the "shortest route". The calculation can be performed by signed magnitude subtraction modulo 360 degrees fig 2.4.f. This shortest route subtraction can be more easily expressed a 2's Complement form of subtraction modulo 360. the differentiator the output is fed to digital a analogue converter. This reproduces the sampled analogue signal which because of its sample nature has frequency spectra existing around multiples of the sample frequency. These must be removed by low pass filtering fully implement the equivalent of the analoque FM demodulator. The analogue signal is then de-empasised and buffered to drive the  $75\Omega$  load of the video monitor. by the use of the above processes the FM signal has demodulated digitally. This approach has been fully explored experimentally as a first stage to this project and the results and conclusions can be found described detail in reference <21>.

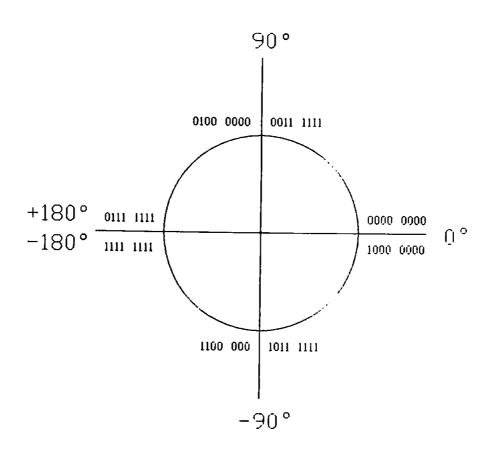


Fig 2.4.e Output Phase Map for Extended Tan Function (r-1(.)) With Sign/ Magnitude Representation

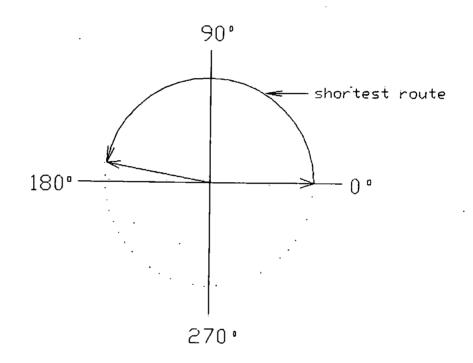


Fig 2.4.f Example of a 'Shortest Route' Calculation around the Unit Circle

# 3. A Discrete Time Version of the Digital Demodulator for Data Transmission.

In the previous section the digital demodulator was used to implement the discrete reception of a continuously changing time signal i.e analogue, without any loss of definition. A configuration will now be considered where a modulated signal is demodulated. From equation 2.1.1.f, should be noted that the phase angle  $\Phi(t)$  is a continuous variable with time, as is the magnitude A(t). Even if is not the case, and the phase and amplitude only change at discrete instants in time, the complex envelope model still be used to model the bandpass waveform. Ιf the In-phase and Quadrature components the 2 represent a vector dimensional axis of Eucilidean space, diagram can be constructed. A simple constellation whereby the amplitude is constant at unity and the phase can on any one of four equispaced values of 45,135,225,315 degrees can be represented on the space diagram as in Fig 3.a. This is a representation for Quadrature Phase Shift Keying. If the amplitude takes on any one of two values well as the four phase value then a form of Quadrature Amplitude Modulation is described, as shown in Fig Both these signals can be easily decoded by the demodulator already described from the ratios of the and quadrature channel values by changing the decoder function incorporated into the decode PROM. Many forms signal constellation can therefore be demodulated by the of the same digital demodulator technique by programming appropriate decode PROM's. However sampled discrete system the function of symbol synchronization and carrier phase lock have also carried out. These subjects will be dealt with in a section but first some basic principles of Binary Shift Keying (BPSK) are considered in connection with its spectrum, spectral shaping by means of filtering and effects of noise at the receiver.

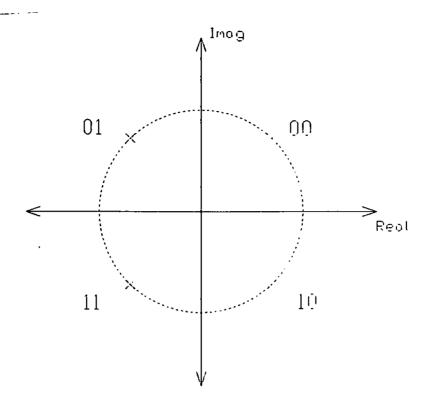


Fig 3.a Space Diagram Constellation for QPSK

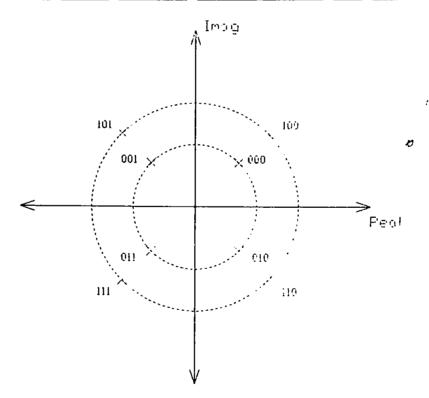


Fig 3.b Space Diagram Constellation for Quadrature
Amplitude Modulation

### 3.1. The Maximum Likelihood Demodulator.

For a completely known signal in Additive White Gaussian Noise it is possible to implement a demodulator which minimizes the probability of making an decision error between the observed received signal r(t), and the transmitted signal s(t). Consider an M'ary signalling system with transmitted signal waveform  $s_m(t)$  given by:-

$$s_{m}(t) = Re[u_{m}(t). e^{(j2.\pi.f.t)}]$$
 (Eq3.1.a)  
 $m = 1,2,..M$ 

where  $u_m(t)$  represent the low-pass equivalent signal waveforms. The M signals have signal energies individually defined by <13>:-

$$E_{m} = \int_{0}^{\tau} s(t)^{2} dt$$

$$= \frac{1}{2} \int_{0}^{\tau} |u_{m}(t)|^{2} dt$$
(Eq3.1.c)

The transmission of this signal through a channel results in the received signal being attenuated by a factor 'a' , delayed by ' $T_0$ ' and corrupted by Additive White Gaussian Noise (AWGN), represented by n(t) which is the complex representation of frequency shifted bandpass noise. This results in the received signal r(t) being represented by:-

$$r(t) = Re[\{\alpha.u_m(t-T_0)e^{(-j2\pi fT_0)} + n(t)\}e^{(j2\pi ft)}]$$
(Eq3.1.d)

the factor  $e^{\left(-j2\pi fT}_{0}\right)}$  represents a constant phase delay between the transmitted signal and the received signal. Assuming that the demodulator is synchronized to the

transmitter the dependance of the received signal on 't' can be eliminated. This results in the the received signal being expressed in the equivalent lowpass form:-

$$r(t) = Re[a.u_m(t)e^{-j\theta}+n(t)]$$
 (Eq3.1.e)

where  $\theta=2\pi fT_0$  radians. The demodulator must therefore observe the signal for a time t such that 0< t< T and decide from this observation which of the M signal has been transmitted. It is desirable for the probability of an error in this decision to be a minimum. This occurs if the demodulator selects the signal with the largest posterior probability i.e. it computes the probability of signal 'm' being transmitted given the signal r(t) is received, during the observation interval. This can be expressed as:-

$$p(m|r(t), 0 < t < T) m=1,2,..M$$
 (Eq3.1.f)

It can be shown (Proakis <13>) that for a set of M signals, of equal likely a-priori probability equal to 1/M, with AWGN the demodulator must compute the M decision variables:-

$$D_n = Re[e^{(j\theta)} \int_0^T r(t).u_n^*(t)dt] - \alpha.E$$
  
 $0 \qquad n=1,2..M$   
 $(Eq3.1.g)$ 

where  $u_n^*(t)$  = is complex conjugate of the variable  $u_n(t)$  and decide in favour of the largest  $D_n$ , and hence signal m. If however, the signalling waveforms are of equal energy then the  $\alpha.E$  term is a constant and can be neglected in the computation and hence becomes:-

$$D_{n} = Re[e^{(j\theta)} \begin{cases} T \\ r(t).u_{n}^{*}(t)dt \end{cases}$$
(Eq3.1.h)

For a Quadrature Amplitude Modulated signal, u(t) is given by:-

$$n=\infty$$

$$u(t) = \Sigma \text{ In. } g(t-nT) \qquad (Eq3.1.i)$$

$$n=0$$

where  $I_n = I_{nr} + jI_{ni}$ , and  $I_{nr}$  and  $I_{ni}$  are two information carrying symbols which can take on any one of k states. If  $I_{nr}$  and  $I_{ni}$  can only take on the value +/-1, then this is equivalent to Quadrature Phase Shift Keying (QPSK). If the  $I_{ni}$  symbol is set to zero then Binary Phase Shift Keying results. The function g(t) represents the low-pass pulse shaping function and is one factor that restricts the bandwidth of the transmitted signal. The transmitted signal s(t) therefore becomes:-

$$s_m(t) = Re[g(t). e^{(j2\pi ft + \theta_d + L)}]$$
 (Eq3.1.j)

$$\theta_{d} = \operatorname{Tan}^{-1}(I_{ni}/I_{nr})$$
 adjusted for a full 360 degrees.

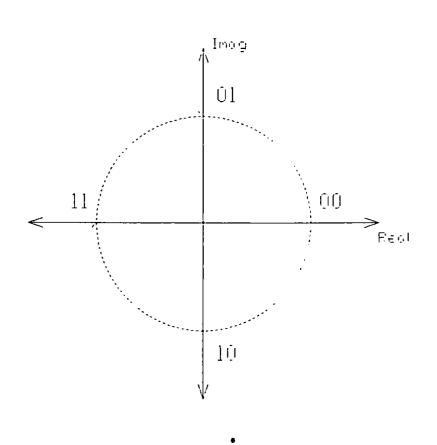
$$\theta_d = \Gamma^{-1}(I_{ni}/I_{nr})$$

for  $I_{nr}$ ,  $I_{ni}$  = +/- 1 for QPSK, and  $I_{nr}$  =+/- 1,  $I_{ni}$  = 0 for BPSK. L is a phase offset on the resultant constellation, an example of which can be seen in fig 3.1.a. Assuming g(t) is real then :-

$$s_{m}(t) = g(t).\{Cos (2\pi ft + \theta_{d} + L)\}$$
 (Eq3.1.k)

by simple trigonometry :-

$$s_{m}(t) = g(t)\{A_{p}.Cos\ 2\pi ft + A_{q}.Sin\ 2\pi ft\}$$
 (Eq3.1.1)



where

$$A_{p} = Cos(\theta_{d} + L)$$

$$A_{q} = Sin(\theta_{d} + L)$$

hence the transmitted signal can be constructed from the addition of two quadrature carriers individually modulated by the shaped information stream  $I_{ni}$  and  $I_{nr}$ .

Maximum Likelihood Demodulation of this transmitted signal in the presence of noise results in the computation of the decision variable Dm, by substitution of equation 3.1.j. into 3.1.h produces:-

$$D_n = e^{(j\theta)} \int_{0}^{T} r(t).g^{*}(t)e^{(-j\theta}d + L) dt$$
(Eq3.1.m)

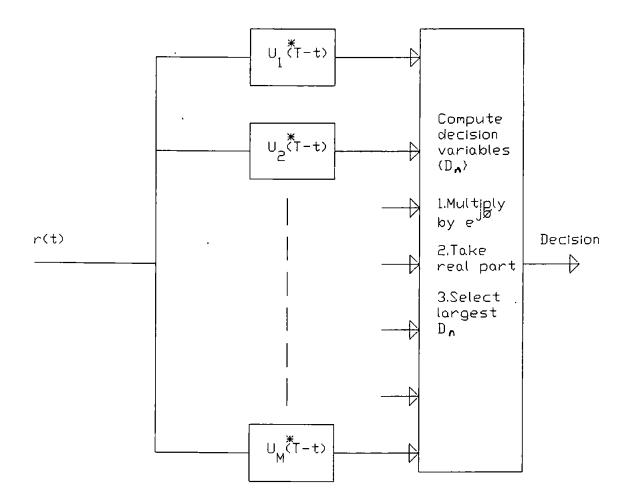
The exponent under the integral is independent of the integration variable and hence can be factored out of the decision variable.

$$D = e^{(j\theta)} \int_{0}^{T} r(t) \cdot g^{*}(t) dt$$
(Eq 3.1.n)

This can be implemented as a single matched filter or cross correlator. The resultant vector D can be phase processed to obtain a received phasor  $\theta_{\rm rd}$  which is then compared against the set of transmitted phasors produced by  $\{s_{\rm m}(t)\}$ .

The optimum demodulator must therefore compute this complex decision variable D from the received signal r(t) during the interval O<t<T, convert from a complex to polar form and compare the resultant phase against a set of possible transmitted phasor. This can be achieved by a system as shown in fig 3.1.b. The main objective of the research has

been to implement the above processes with increased accuracy in both the transmitter and receiver, compared to previous methods while carefully shaping the transmit spectrum by the correct selection of the function g(t).



Matched Filter Demodulator

Fig 3.1.b Optimum Demodulator Implementation

## 3.2. Binary Phase Shift Keying.

If we consider a binary random waveform in a non return to zero format (NRZ) such that a logical 0 is represented by a -1, and a logical 1 by a +1, the space diagram can displayed as two points 180 degrees apart Fig 3.2.a. For an analysis of this waveform we can consider it as a series of impulses convolved with a rectangular period + and - T/2 (where response of T is the period) and amplitude of value 1. As the impulse is random ( or pseudo-random) it's frequency spectrum ostensibly uniformly flat over the bandwidth of interest to and of normalized amplitude equal 1. hence convolution of the two time responses, now represented the multiplication of the two frequency responses, produces a power spectrum identical to that of a rectangular impulse response. From the Fourier transform this is found to that of the Sinc function as shown in Fig 3.2.b

$$V(f) = T (Sin \pi fT)$$

$$(\pi fT)$$
(Eq3.2.a)

by observation of fig 3.2.b it can be seen that the spectra of the BPSK signal has major components >-50dB out as as 100 times the symbol rate (single sided spectrum) 99% of the power is contained within 20 times the symbol rate (double sided spectrum) <6>. Hence this means very large bandwidths would be required to transmit whole BPSK spectrum without loss or distortion and makes the transmission of a NRZ format undesirable. overcome this restriction the spectrum of the NRZ introduces stream is shaped by filtering. This new problems. Filtering of the signal with little care produces Inter-Symbol Interference produced by the convolved impulse

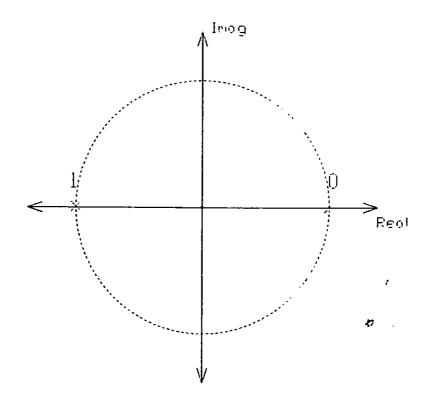


Fig 3.2.a Space Diagram for a BPSK signal

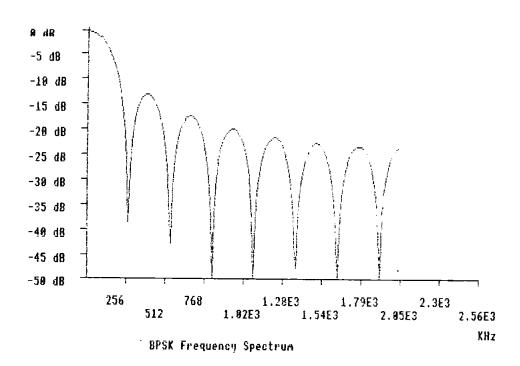


Fig 3.2.b Frequency Response for an Unfiltered BPSK Signal

responses of the NRZ pulses and the filter. This is manifest in the form of impulse response tails adding to the main lobe at the sampling instant resulting in a closure of the Data Eye an example of which is shown in Fig. 3.2.c.

(

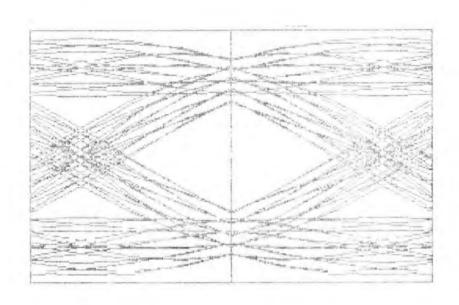


Fig 3.2.c Example of a Data Eye Diagram with Inter-Symbol Interference

#### 3.3. Nyquist Filter Criteria

Nyquist <1> proposed that to overcome this problem the spectrum of a filter must conform to a specific function related to the symbol rate, 2fo:-

$$H(f) = \begin{bmatrix} 1+Y(f) & f < fo \\ Y(f) & fo < f < 2fo \\ 0 & f > 2fo \end{bmatrix}$$
(Eq3.3.a)

Where Y(f) is a real function that is even symmetric about f=0 i.e

$$Y(-f) = Y(f)$$
 f < 2fo (Eq3.3.b)

and odd symmetric about f=fo such that:

$$Y(-f+fo) = -Y(f+fo) \quad f < fo \quad (eq3.3.c)$$

there is no ISI if the symbol rate is 2fo. A simple example of this symmetry can be seen in fig 3.3.a, but a commonly used form of the Nyquist Filter is that of the Raised Cosine Filter.

#### 3.4. Raised Cosine Roll-off Filters

The family of Raised Cosine Roll-off filters is defined by:-

$$X(f) = \begin{bmatrix} 1 & 0 < f < (1-\beta)/2T \\ 1/2(1-\sin(\pi(f-1/2T)/\beta)) & (1-\beta)/2T < f < (1+\beta)/2T \\ 0 & f > (1+\beta)/2T \\ & (Eq3.4.a) \end{bmatrix}$$

with the time response x(t) being given by:-

$$x(t) = \frac{\sin \pi t/T}{\pi t/T} \frac{\cos \beta \pi t/T}{1 - (2\beta t/T)^2}$$
(Eq3.4.b)

The roll-off factor  $\beta$  has a range from 0 to 1 and is often called the percentage roll-off of the filter i.e. 0% 100%. In all cases the zero crossings occur at the rate period. The Raised Cosine filters have a symmetrical time response around t=0 and hence have a constant response, i.e a zero imaginary component. It can be from fig 3.4.a that the 0% filter is equivalent to that a rectangular frequency response and represents the minimum bandwidth that can be used to transmit a signal of symbol rate 2fo symbols/sec without degradation. This produces a sinc function time response which although it complies with the Nyquist filter criteria can produce implementation If the problems and therefore produces worse ISI. timing at the receiver is not exact the data eye is sampled away from the point of zero ISI. Due to the overshoots that the sinc function produces the increased and hence the recovered signal is degraded . the percentage roll-off is increased the impulse tails reduce more rapidly and hence the amount of ISI be reduced by the use of a higher percentage roll-off impulse response. Hence symbol timing must be more accurate for low percentage roll-off factors. An analogue approach to the frequency response is hard to practically realize since the filters are usually minimum phase filters causal impulse responses of very long duration difficult to phase equalize. Hence by the appropriate choice of roll-off factor we can trade ISI, complexity of symbol timing recovery, and filter realization problems, for increases in transmit bandwidth.

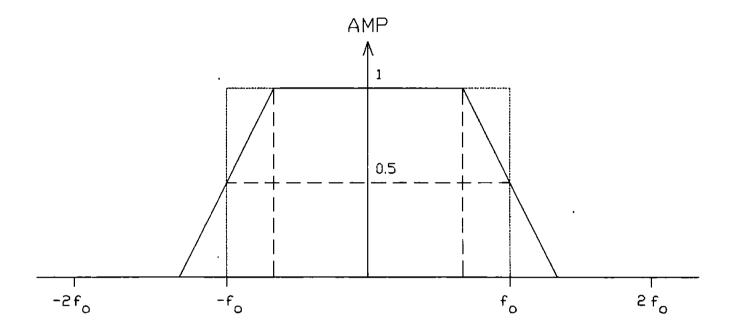


Fig 3.3.a Simple Example of a Nyquist Filter Frequency Spectrum

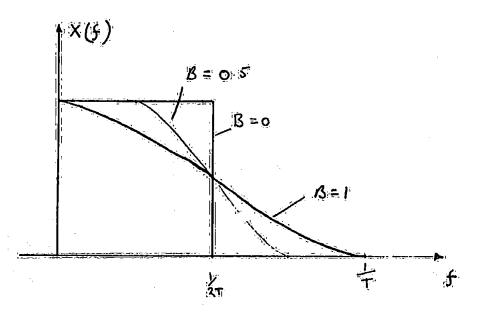


Fig 3.4.a Family of Raised Cosine Filter Frequency Responses

#### 3.5. Matched Receive Filters

In the case of digitally derived signals where the transmitted waveform is known and easily defined it long been known <6> that it is possible to filter received signal in such a way that, in the presence of additive white gaussian noise, the output signal can maximized against the noise. These Matched Filters the filter impulse response to be the 'mirror image' of the transmitted time signal. If we consider a Raised filter impulse response its mirror image is also a cosine filter impulse response due to its inherent symmetry and hence its zero phase response. Hence the matched filter for a Raised Cosine filter is in itself a Raised Cosine filter. However the spectral response of the channel is now that of a (Raised Cosine Filter) which no longer exhibits zero crossings at the sampling instant. We therefore require a set of filters that exhibit an overall response of a Raised cosine filter while being matched at receiver. Lucky, Salz and Weldon <7> have shown that optimum solution is that the transmitter and filters are designed such that their overall response is:

$$H_{R}(f).H_{1}(f).H_{2}(f) = (H_{N}(f))^{1/2}$$
 (Eq3.5.a)

Where subscript N indicates Nyquist filter, R receiver filter and 1 & 2 any other filters in receiver processing. This filter response is repeated in the transmitter. Therefore to have a Root Raised cosine Filter in both the transmitter and the receiver preserves the overall Nyquist frequency response and the Matched filter criteria.

#### 3.6. Design and Development of Multi-Rate Data Modem

# 3.6.1. Introduction to Design Requirements.

It has previously been shown that a digital implementation of a phase demodulator can be used to detect a variable phase signal in a continuous format with the output from the phase decode PROM being an exact representation of the received vector relative to the receiver local oscillator. It has been postulated that this could be extended to discrete binary signal format by the use of a symbol timing recovery function. It has also been shown that one optimum form of filtering in a binary signalling channel for both transmitter and receiver are that of Root Raised cosine filters which can simultaneously comply with both Nyquist filter and Matched filter criteria. This in the design for the data modem to become that in 3.6.1.a. Due to the digital nature of the proposed system, it is envisaged that by a simple re-configuration of modem, data rates ranging from 16Ksymbols/sec 256ksymbols/sec can be achieved. To obtain minimum degradation through the system, all filters must be accurate in both the time and frequency domains. Due to the symmetry of the root raised cosine filter impulse response, the theoretical filter is non causal and difficult realize using standard LC networks, or active filters.

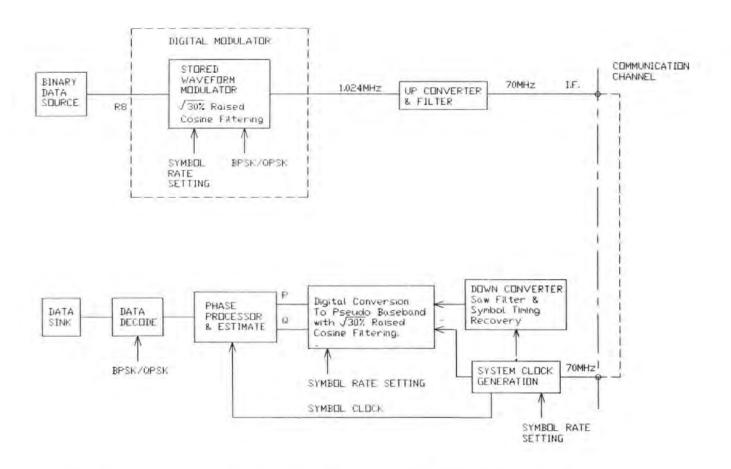


Fig 3.6.1.a Overall System Design for Multi-Data Rate Modem

#### 3.7. Multi-Rate Modem Modulator.

In the discussion so far attention has concentrated on the receiver aspect although it has been proposed that a Root Raised Cosine filter should be used at the transmitter for efficient spectral shaping. The theory and implementation behind the modulator will now be explored.

#### 3.7.1. The Modulator; A Brief Overview.

Consider a previously scrambled, hence pseudo-random data stream being presented to a modulator where by it will be converted into a QPSK signal format and fed to frequency conversion circuitry on a 1.024MHz First IF carrier. The conventional approach has been described by Feher <9>,Couch <6>,Proakis <13> and many other authors with spectral shaping either taking place in the baseband channels, or at the carrier frequency, using analogue filters. The basic block diagram can be seen in fig 3.7.1.a. The incoming data sequence is multiplexed into two data sequence at half the incoming data rate. These two parallel data sequences of NRZ pulses are then filtered for efficient spectral shaping before modulating onto a IF carrier in quadrature.

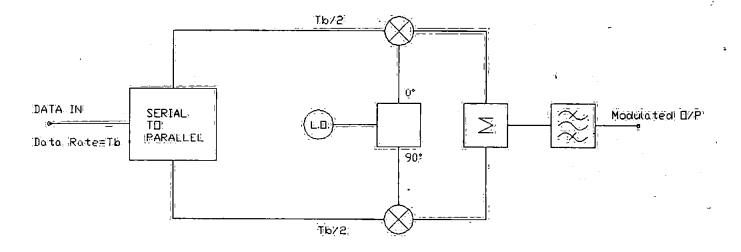


Fig 3.7.1.a Typical QPSK Modulation Method

### 3.7.2. Background to Digital Filters.

Consider a simple system as shown in fig 3.7.2.a. The input waveform x(t) with spectrum X(f) is filtered by the filter with transfer function H(f) to produce an output waveform Y(t) of spectrum Y(f) <8>. This can be expressed as :

$$Y(f) = H(f).X(f)$$
 (Eq3.7.2.a)

If we consider the same system in the time domain we obtain:-

$$y(t) = x(t)*h(t)$$
 (Eq3.7.2.b)

where \* represents the convolution of two time responses and h(t) the impulse response of the filter H(f).i.e.

$$y(t) = \int_{-\infty}^{\infty} h(T) \cdot x(t-T) dT$$
(Eq3.7.2.c)

Using the sampling theorem and by sampling at least twice the highest frequency the discrete time representation becomes:-

$$y(kT) = \sum_{n=-\infty}^{\infty} h(nT).x((k-n)T)$$

$$n = -\infty$$
 (Eq3.7.2.d)

hence if this mathematical function can be performed on the sampled data sequence the output sample data is effectively filtered. This function can therefore be modelled in digital hardware and repeated to any degree of accuracy required.

$$X(f)$$
  $H(f)$   $Y(f)$   $X(t)$   $Y(t)$ 

Fig 3.7.2.a Simple Linear Time Invariant Filter System

### 3.7.3. Digital Transmit Filters.

In the transmitter the incoming data pulses are of the NRZ format and hence only ascribe to two values +1 and -1. The convolution process is therefore limited to:

$$y(kT) = \sum_{n=-\infty}^{\infty} h(nT) \cdot x((k-n)T)$$

$$(Eq3.7.3.a)$$

where x(iT)=+1 or -1,k=0 to  $\infty$  and can be approximated by Eq3.7.3.b for a finite length of h(nT).

$$y(kT) = \sum_{n=0}^{N} h(nT).x((k-n)T)$$
 $n=0$ 
(Eq3.7.3.b)

hence only a limited number of coefficient multiplications and additions need to take place. Consider the data sequence not as a series of NRZ pulses but as a series of pseudo-random impulses with a flat normalized spectral response. The output spectrum from any filter is therefore defined by the filter spectrum only and hence its response. The digital filter now consist of the convolution of two impulse responses. This can be considered as in 3.7.3.a for a filter impulse response which is only significant over 6 symbol periods for a Root 30% cosine roll-off filter ( Appendix B ). In the centre of sequence the tails from all the filter impulse responses converge. For this region of interest it is possible to define the intermediate results for any input sequence 6 symbols i.e. calculate the convolution results and them in memory. If the sampling rate of the filter response has been correctly chosen with a 6 symbol word it is possible to store all combinations of results in a PROM. Since the two quadrature channels are both filtered by the same frequency response it is possible to use the same information for both channels. However care must

taken such that the time sample chosen by each channel corresponds to the correct filter response and that no phase shifts exist between channels.

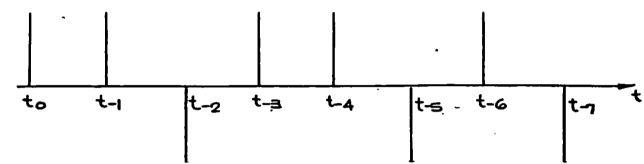
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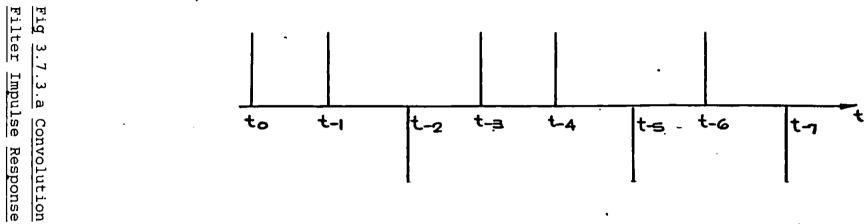
Data

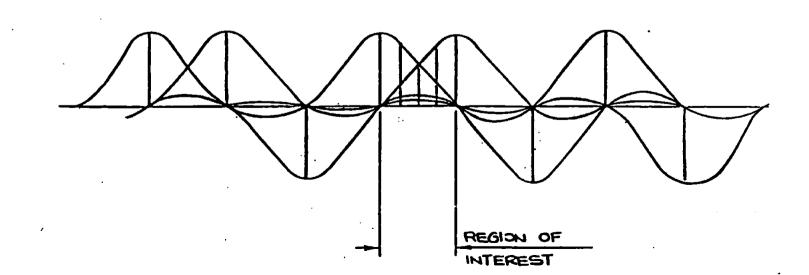
Impulse

Stream

with







#### 3.7.4. Digital Up-conversion to First IF.

Consider a sequence of 4.096MHz samples, of infinitesimal pulse width, output from the above digital filter PROM, fig 3.7.4.a and a carrier frequency of 1.024MHz is to be used. The sampled In-Phase carrier waveform can be consider to be as in fig 3.7.4.b. If these two waveforms are multiplied together the result is as in fig 3.7.4.c i.e. a 4.096MHz sample stream with alternate samples equal to zero. another sample stream is multiplied by the quadrature carrier as shown in fig 3.7.4.b the resultant is as in fig 3.7.4.d. It can be clearly seen that again 4.096MHz sample stream results, with alternate equal to zero. For the corresponding positions In-phase channel when the quadrature channel is zero In-phase is non-zero and vice versa. The output modulated carrier signal therefore consists of the In-phase quadrature channels added together which can be implemented by simply multiplexing the two channels. With the of the phase offset, L, for the data constellation, modulated carrier signal can be synthesised within the Prom and hence carrying out both with the filter and modulator functions. The complete modulator circuit becomes that fig 3.7.4.e. For a BPSK signal format the incoming data only diverted to the In-phase channel and the quadrature channel output is set to zero. Other data rates can accommodated by scaling the number of samples per symbol or the sampling rate. Scaling of the sampling rate causes IF output frequency to change but this can be adjusted by the use of frequency synthesisers in the analogue frequency up and down converters.

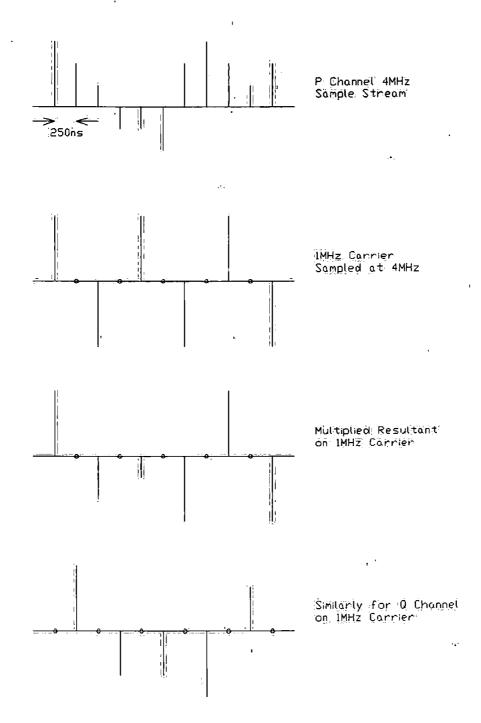


Fig 3.7.4.a/b/c/d An Example of the Quadrature Modulation Process in a Sampled Data System

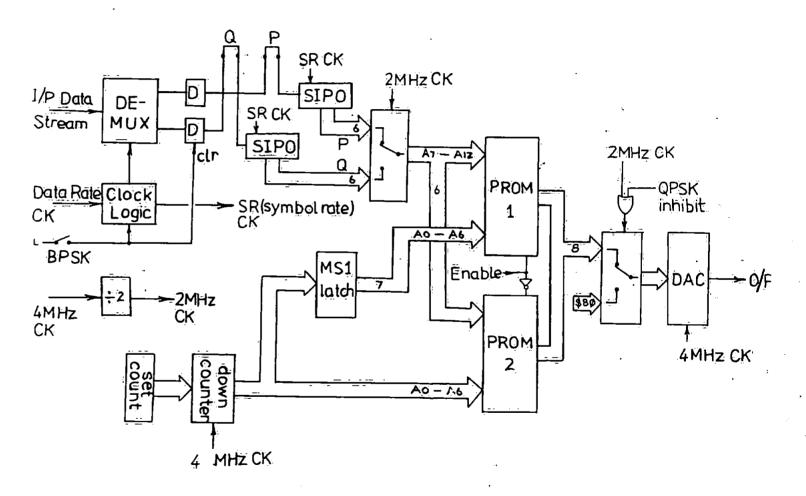


Fig 3.7.4.e Digital Modulator System Diagram

# 3.7.5. Effects of Sinc Function on Modulated Signal Frequency Spectra

The Modulator is designed to produce a shaped bandpass frequency response that conforms to the root 30% Raised Cosine spectrum. In the example given above the samples are of infinitesimal pulse width, as this width is increased a Sinc function, in the frequency domain corresponding to the pulse width, is superimposed over the desired frequency response. The response is therefore degraded by the effect of the sample and hold function produced by the DAC. output sample rate is set at 4.096MHz and will therefore produce a (SIN (X))/X (Sinc function) response around 0 with a first null at 4.096MHz. This response multiplies the required raised cosine response and a degraded frequency response is the result. This sinc function and its 3.7.5.a. The effect of this can be seen in fig slope across the passband is to create cross interference. In the region of interest that the cosine response passband extends i.e.+/- 128KHz 1.024MHz for a 256Ksymbol/sec data rate then the across the passband is 0.5dB. This could be removed by a number of different techniques:-

- 1) Increasing the sample rate to carrier frequency ratio throughout the system.
- 2) Equalise the asymmetry by the use of a digital equalization filter.
- 3) Decrease the hold time of the DAC by inserting a zero sample between each calculated output sample i.e. increase the output sample rate.
- 4) Consider the effect of the asymmetry to be negligible over the frequency range of interest.

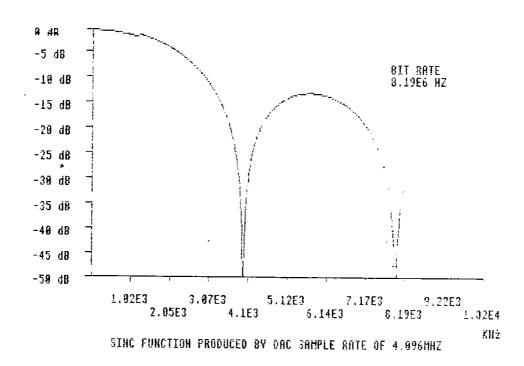


Fig 3.7.5.a Effect of Sampling on Output Frequency Response

Solution 4 was considered the most appropriate for this investigation with solution 3 favoured over 1 and 2 as this required a minimal amount of hardware. Solution 1 will increases the memory size of the PROM's to cover the required symbol rate range while also increasing the operating speed with solution 2 increasing the complexity of the modulator.

#### 3.8. Multi-Rate Digital Demodulator.

From the previous discussions of the modulator it can postulated that a demodulator can be based on a similar concept. The digital demodulator proposed consists of input signal on a minimum carrier frequency of being digitally converted to baseband in quadrature then digitally filtered. Sample rate reduction will be used to enable Root 30% raised cosine filters to be implemented practically while covering a symbol rate span of 16Ksymbols/sec to 256Ksymbols/sec. The final output rate from these filters is four times the symbol rate. From these four samples per symbol, one of the samples must extracted as the peak sample instant corresponding to zero ISI (when in conjunction with a matched transmitter filter) and the center of the data eye where the SNR is a maximum. A coherent Carrier phase reference with the 1MHz IF is also required to enable data to be correctly decoded from the received phase angle. To enable both of these processes occur the symbol timing must be recovered and a carrier reference established.

### 3.8.1. System Implementation.

initial bandlimiting of the received signal to prevent aliasing prior to sampling and digitizing, is obtained by the use of a SAW filter having a symmetrical impulse response and hence good phase linearity, minimal group delay variations. The incoming signal, the range 52-88MHZ, is first up-converted to 200MHz, frequency being mainly dependent on the availability then bandlimited 700 SAW filters and KHz bandwidth. The bandlimited signal is then down converted to a 1.024MHz minimum carrier frequency before being digitally sampled by a 6 bit Analogue to Digital converter giving a mean-squared signal to quantization noise ratio of 31dB <5>. This is considered to sufficiently below the noise floor of the received bandpass signal under normal operating conditions, approximately 4 dB SNR in 700 KHz for a 256 Kbit/sec signal with Eb/No of 8 dB, to produce no degradation. At higher signal to noise ratios the degradation will limit the final performance the system but due to the steepness of the theoretical error curves at high signal to noise this degradation will be insignificant. The sampling takes place at a 4.096MHz rate to fulfil sampling theorem requirements and symbol clock. synchronization with the In practice was found that a choice of sampling rate of two or three times the carrier frequency caused aliasing due to spectrum extending out to 1.8 MHz for the particular SAW filter used. This sampled signal is then digitally mixed to baseband before filtering.

#### 3.8.2. Digital Quadrature Down-Conversion

method used for down-conversion to baseband is obtained by a similar argument as in the modulator. Assume that the incoming signal is on a carrier locked to a quarter of the sampling frequency. Down converting with sampled 'local oscillator', synchronous with sampling frequency such that the sampling points occur the 0,90,180,270 degree points, produces alternate zero samples in the Phase and quadrature baseband channels. This can be implemented by the multiplication of sample pairs by 1.024MHz local oscillator i.e. which implemented by complementing -1 is samples, demultiplexing these samples into the phase and quadrature a zero value sample channels, and adding opposite channel while one channel is being enabled. zero term would normally be a product of the mixing process. The addition of the alternate zero term into channel when the data sample is diverted into the other channel results in two baseband 4.096MHz sample streams and allows sampling to occur at half the rate that would normally be required for the 4.096 MHz sample rates per channel while maintaining the correct mathematical model.

#### 3.8.3. Receiver Digital Filter Design

The digital filter design problem is similar to that of the modulator, however, now the filtered sample sequence is multi-level, i.e. 64 level for 6 bit A/D. If the concept of the pre-stored response is to be used the size of memory device required becomes prohibitive ( in the order of  $2^{36}$  ) and a new approach is undertaken.

#### 3.8.3.1. Choice of Raised Cosine Roll-off Factor.

The roll-off factor for the overall channel spectrum was chosen to be 0.3 or 30%. This figure is a compromise between minimum channel bandwidth requirements and timing jitter tolerances on the symbol timing recovery circuitry giving rise to ISI. Higher roll-off factors i.e. 50%, produce wider bandwidths but a higher timing jitter can be tolerated before the ISI significantly degrades the data eye.

## 3.8.3.2. Basic Digital Filter Implementation.

The Root 30% Raised Cosine Filter that is required for the receiver is linear phase and must hence be of a Finite Impulse Response Design (FIR), fig 3.8.3.2.a. Here delayed input samples are multiplied by the appropriate coefficients and the results summed to produce convolved output. The digital hardware implementation of a FIR filter can be undertaken in a variety of ways, Parallel multiplication and addition fiq 3.8.3.2 b, parallel multiplication and serial addition fig 3.8.3.2.c, cascaded multiplication addition parallel and fiq 3.8.3.2.d. The format used in the designed filters was shown in fig 3.8.3.2.e and can be termed a Direct Form FIR Filter with Serial multiplication and Addition. incoming sample stream is stored along a delay line, length 15T , which is constructed of 6 bit latches, sample rate  $f_{si} = 1/T$ . If the frequency at the input response of the filter is restricted to  $f_{si}/8$ , frequency components higher than 1/8 input sample rate are attenuated more than 20 dBs, then it is possible to sub-sample the output of the filter at  $f_{si}/4$ . This causes the filter response to repeat around the output frequency and the aliasing point now occurs at 1/8th of the input

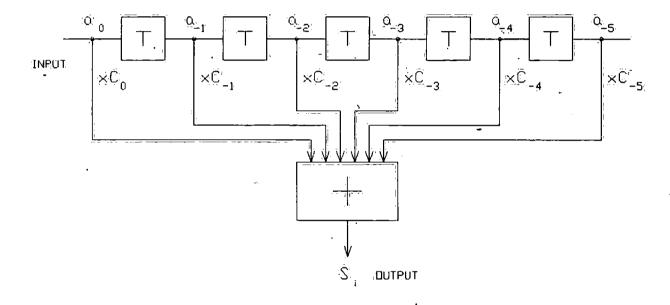


Fig 3.8.3.2.a Finite Impulse Response Filter Function
Diagram

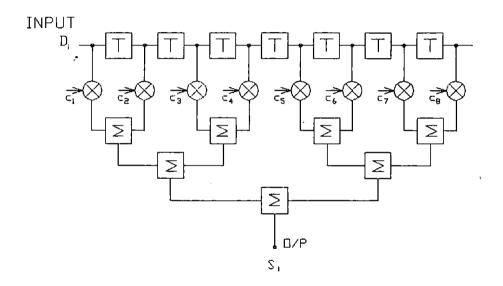


Fig 3.8.3.2.b FIR Filter Implementation with Parallel Multiplication and Addition

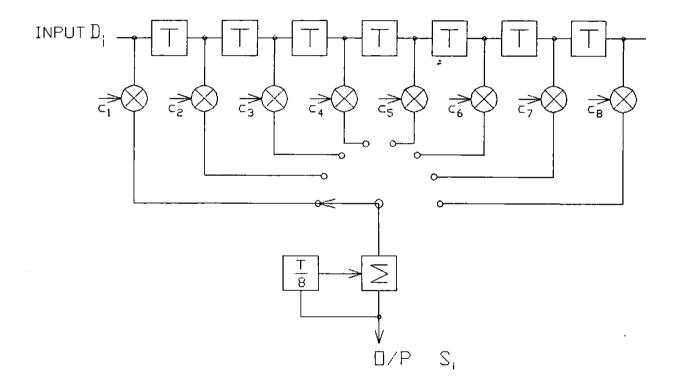


Fig 3.8.3.2.c FIR Filter Implementation with Parallel Multiplication and Serial Addition

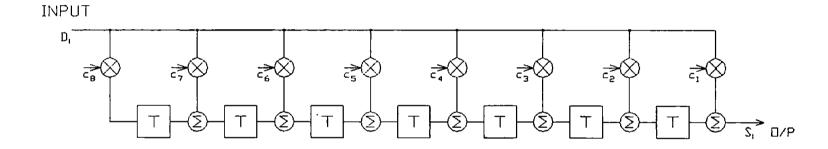


Fig 3.8.3.2.d FIR Filter Implementation with Parallel Multiplication and Cascaded Addition

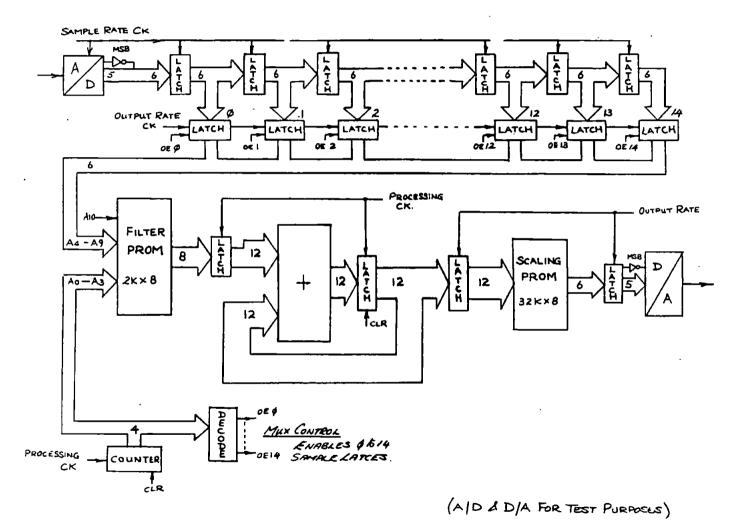


Fig 3.8.3.2.e FIR Filter Implementation used in Demodulator Filters

sample frequency. As the output sample rate is reduced by a factor of 4:1 then the redundant samples need not calculated. This increases the time available to carry the convolution process since only one in four of the input samples takes place in the convolution and hence allows high input rates to be practical. The selection of a set of input samples is dependant on the phase relationship between the input and output sampling signals. Any of sets will create the required frequency response but since we require the central maximum sample, ie the centre of the data eye at the output of the filter, selection of these sample sets is critical. The required set of samples taken from the delay line and latched onto a set of buffers during one input clock sample. This transfer to the buffers takes place at the output sample clock rate. The correct selection of input sample sets is required to enable correct final impulse response. Adjustment is provided changing the phase reference of the output/transfer clock with respect to the input sample clock. Once the required set of samples is present on the latches the convolution takes place. This is carried out by multiplexing the latched samples onto the PROM address lines, along with a number representing the effective coefficient that sample is multiplied. The PROM is pre-programmed with the answers to the multiplication of the coefficient in form of the algorithm:-

$$R(A(i,j)) = i \times C_j$$
(Eq3.8.3.2.a)

where R(A(i,j) = result from address A(i,j) given by:-

$$A(i,j) = i' \times 16 + j$$
 (Eq3.8.3.2.b)

j=coefficient number =0..15 i=sign/magnitude equivalent sample value of a 6 bit 2's complement input value, with equivalent maximum ,i, equal to +/-1. Hence A(i,j) can be represented by 10 bits. The output from the PROM is a bit representation also in 2's complement format scaled a maximum of +/- 1. The resulting products are accumulated the coefficient number count 0 to 14, coefficients. On count 16 the data is output to a PROM and the accumulator cleared. A new set of samples is now transferred to the multiplex latches. accumulator can in these 15 additions in theory produce maximum 12 bit result. The coefficients are not all at maximum of 1, as they are a sampled version of the root 30% Raised Cosine filter impulse response, and consequently maximum never reached. Also for is coefficients corresponding to different data accumulated maximum result will correspondingly change. enable this output to be adjusted for maximum signal quantizing noise the Scaling PROM allows the maximum input value to be adjusted to produce a maximum L bit value. This is performed by the PROM being pre-programmed with the algorithm:-

$$R(A(j)) = \underbrace{j' \times N}_{\text{Maximum input value}}$$
(Eq3.8.3.2.c)

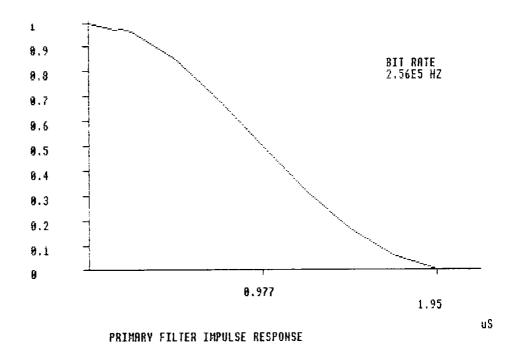
where maximum input value is magnitude of maximum value, j'=sign/magnitude equivalent of 2's complement input value j,  $N=2^{L-1}$ , where L= number of bits in output word, i.e. 6 bit output. This acts as a gain in the system, while also allowing the number of bits representing the output to remain at a manageable size. The error of re-scaling to the L bit output is therefore minimized and is only dependant on the output word size. The maximum error is therefore half a LSB but the signal is maximized to the maximum word length and hence preserving the signal to quantizing noise

ratio. This method also allows for increased flexibility in the usage of the basic filter design. Since the overall convolution technique relies on the coefficients multiplication i.e. the desired impulse response being multiplied by the incoming samples, the rate at which convolution takes place results in the scaling frequency response obtained from the filter. This therefore has the flexibility to change the scaling of frequency response by changing the processing rate of filter. It is also possible to switch from a 15 coefficient convolution to a 7 coefficient convolution, by changing the multiplexing buffer addressing system (coefficient pointer) and stored coefficient multiplication results in the use of a larger PROM this can be achieved by simple address selection. For a 15 coefficient filter 4 bit will be required for the coefficient pointer and with a bit input word then a total of 10 bits is required for the multiplication. Hence a minimum memory size of 1Kbytes another set of coefficients required. The addition of led to the choice of Signetics 82S191BN 2Kbyte 45 nSec enabling the filter to Proms with access times of produce a multiplication and addition result in 61nS i.e. a maximum clock frequency of 16.384MHz.

# 3.8.3.3 <u>Multi-Symbol</u> <u>Rate</u> <u>Receive</u> <u>Filter</u>.

Consider the 16Ksymbol/sec case: the incoming stream is highly over sampled but cannot be reduced sample rate due to aliasing constraints imposed by the SAW filter. One alternative is to change SAW filters. can be very expensive for a large number of symbol rates. A better alternative was proposed and implemented. bandlimiting filters known as primary filters reduce the bandwidth of the 4MHz sample stream such that sample rate can take place as previously described reduction Sub-sampling of the output data producing a decimation in

time. The lowpass primary filters are cascaded in series to reduce the bandwidth of the received signal and sampling rate until it is at a practical bandwidth and sample rate to allow the final shaping of the frequency response to take place. Each primary filter contains same impulse response coefficients, but due to different sample rates used, produces scaled frequency responses. The used for the primary filters frequency response computer optimization trading passband obtained by a response flatness and stopband attenuation against impulse length. The impulse and frequency responses of the primary filters can be seen in fig 3.8.3.3.a/b. The lower data rate the greater the number of primary filters must be used to reduce the bandwidth to a manageable level for pulse shaping.



 $\underline{\texttt{Fig}} \ \underline{\texttt{3.8.3.3.a}} \ \underline{\texttt{Impulse}} \ \underline{\texttt{Response}} \ \underline{\texttt{of}} \ \underline{\texttt{Primary}} \ \underline{\texttt{Filters}}$ 

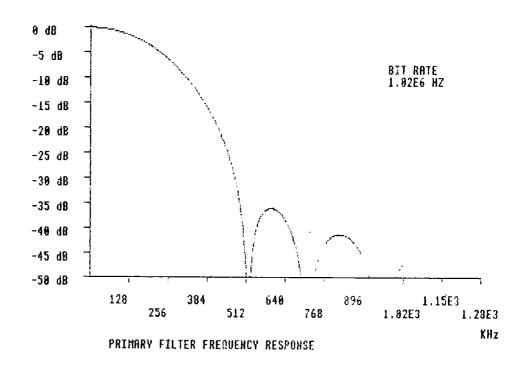


Fig 3.8.3.3.b Frequency Response of Primary Filters

#### 3.8.3.4 Shaping Filter

The final filter is designed to equalize the frequency response of the primary filters and provide the shaping to obtain the overall root 30% Raised Filter. The required frequency response of the filter can be seen in fig 3.8.3.4.a. To enable this to achieved with a target of the frequency sidelobes being greater than 30 dB down, the impulse response of the filter is arranged such that alternate sample coefficients are set to zero. This enables the long impulse response of the equalizing filter to be convolved while only using coefficients. The introduction of the zero terms results in the frequency response of the filter repeating around half of the output rate, i.e. twice the symbol rate since the sample rate is effectively reduced by a factor of 2 but narrow sample width. The spectrum of the signal to this filter must therefore be greater than 30 down over this frequency range otherwise the noise power at the output will increased. To facilitate these zero samples in the convolution process the input samples are into the multiplex buffers with a 2T delay between line for the final samples. This results in the delay filter being 31T samples long. The final output rate four times that of the symbol rate and allows the to be correctly shaped for conformity to the overall raised cosine response. The selection of Filters for a multi-data rate Receiver from 16 Ksymbol/sec to Ksymbol/sec can be seen in table 3.8.3.4.a

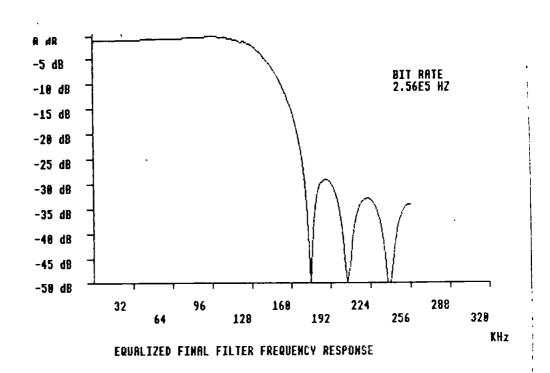


Fig 3.8.3.4.a Frequency Response of Shaping Filter

_	,
_	

Symbol	Filte	r 1 *			Filte	r 2			Filte	r 3			Filte	r 4			Filte	er 5	
	I/P	O/P	Co	BW	I/P	0/P (	o I	ВW	I/P	O/P	Co	BW	I/P	O/P	Co	BW	I/P	O/P	Co
	rate	rate		Hz	rate	rate		Hz	rate	rate		Hz	rate	rate		Hz	rate	rate	
16K	4M	2M	7	1M	2 <b>M</b>	512K	15	256K	512K	128K	15	64K	128K	64K	7	32K	64K	64K	15
32K	4M	1M	15	512K	1M	256K	15	128K	256K	128K	15	32K	BYPAS	S			128K	128K	15
64K	4M	2M	7	1M	2M	512K	15	256K	512K	256K	15	64K	BYPAS	s			256K	256K	15
128K	4M	1M	15	512K	1M	512K	15	128K	BYPAS	S			BYPAS	s			512K	512K	15
256K	4M	2M	7	1M	2M	1M	15	256K	BYPAS	ss			BYPAS	s			1M	1M	15

<sup>\*</sup> Requires switchable coefficient and scaling proms

Table 3.8.3.4.a Filters Required for a Multi-Data
Rate Receiver from 16 Ksymbol/sec to 256
Ksymbol/sec

# 3.8.3.5 Frequency Spectra Due to Decimation in Time

Considering the sampled bandpass frequency spectra at the 1.024MHz input, the spectral shape to the components is defined by the SAW filter and will be distributed across the frequency spectrum as in fig 3.8.3.5.a. If the required signal is 256 Ksymbols/sec, three filtering operations are required with decimations in time from 4 MHz to 2 MHz to 1 MHz. Care must be taken to remember that the bandpass spectra repeats around the sampling frequency, and at multiples of the sampling frequency.

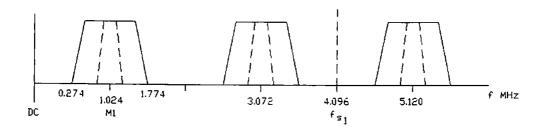


Fig 3.8.3.5.a Sample Bandpass Frequency Spectrum at A/D Input.

down converting this signal to baseband by mixing with a 1.024MHz 'Local Oscillator' results in fig 3.8.3.5.b.

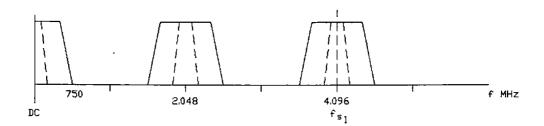


Fig 3.8.3.5.b. Down-Converted Spectra

Filtering this signal by the 1st primary filter with 7 active coefficients would produce the frequency spectra of fig 3.8.3.5.c. However this signal is sub sampled before it is generated at the output of the filter and hence the spectra now repeat around 2.048 MHz as in fig 3.8.3.5.d. The spectra response of the wanted signal is shown dotted within the filter response.

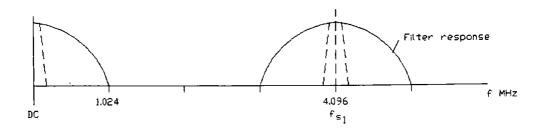


Fig 3.8.3.5.c Output from Primary Filter Before Sub Sampling Occurs.

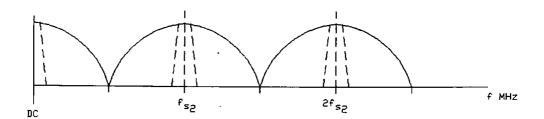


Fig 3.8.3.5.d Output from First Primary Filter After Sub-sampling.

The signal is the filtered again by a 2nd Primary Filter with 15 active coefficients producing the frequency spectra of fig 3.8.3.5.e before sub sampling at 1 MHz occurs.

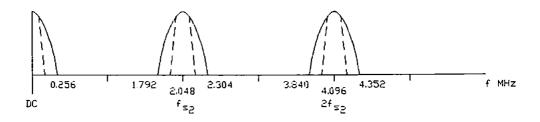


Fig 3.8.3.5.e Output from 2nd Primary Filter Before Sub-sampling at 1MHz Occurs.

The signal is then sub-sampled an again the frequency spectra repeats around the new sampling frequency of 1MHz as in fig 3.8.3.5.f.

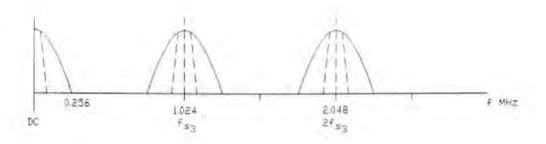


Fig 3.8.3.5.f Output from 2nd Primary Filter after Sub-sampling at 1 MHz.

The signal is now of sufficiently low bandwidth and sample frequency that it is possible to obtain a root 30% Raised Cosine frequency response filter within the constraints of the 15 active coefficients. To obtain good stopband performance, approximately -30 dB, coefficients are used with alternate coefficients This results in the filter frequency response repeating around half the sample rate. i.e. 512 KHz. is because the 15 non zero coefficients can be classed having been extracted from a continuous time response by a sampling signal of 512KHz but with a hold time of a 1.024 MHz sample. This results in the sinc function produced by the hold having its first null at 1.024 MHz but with the signal repeating around the sample rate of 512 KHZ. As all significant energy at this point has been removed by

previous filters this does not cause a problem. The final frequency spectra produced by the filters can be seen in fig 3.8.3.5.g.

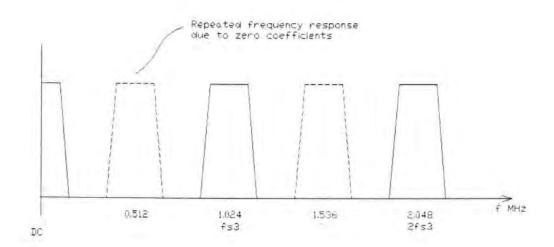


Fig 3.8.3.5.g Final Output from Shaping Filter, the Required Signal Response Being Shown by the Dotted Line.

# 3.8.4 Symbol Timing Recovery

In satellite data transmissions it is usual to scramble the transmitted data <9>. This is not for security reasons but to randomize the incoming data sequence, breaking up long sequences of '0's and '1's , and hence reducing the production of discrete spectral lines. This randomization aids symbol timing by breaking up long data sequences with little timing content, but the scrambling process itself can introduce limited sequences of 1's and 0's depending on the length and format of the scrambling technique used. Symbol timing recovery is not simply achieved and many methods have been produced <10> which often rely non-linear methods. The method that was adopted is that the Delay-Multiplier <11> which was implemented at the 200MHz IF of the SAW filter output, as shown in fig 3.8.4.a. The optimum delay was found to be Td=0 and represents a squaring function enhancing the envelope variations of the filtered waveform. This has been shown by Gardner <22> maximize the recovered symbol timing component for Nyquist pulses. The effect of the squaring function is to spread the received spectrum over twice its bandwidth. low-pass equivalent spectrum of the data signal exists from 0 to 1/2T Hz then the equivalent low-pass resultant spectrum from the squaring function extends to roughly to 1/T Hz. However a signal component is now produced at the symbol rate. The amplitude of this component has oscillatory behaviour depending on the delay time with maximum amplitude occurring at Td=0 <11>. An expression for the signal to noise ratio of the recovered component for

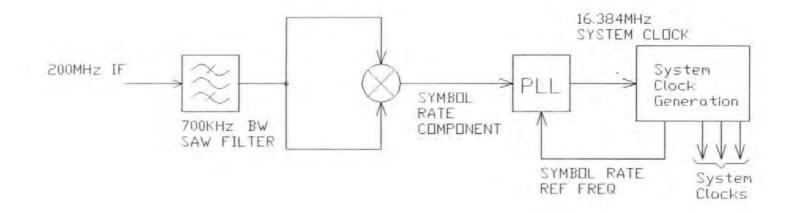


Fig 3.8.4.a Symbol Timing Recovery Circuit using Delay and Multiply Method, Td=0

QPSK is given by Palmer et al <14> for Nyquist pulses as :-

$$S/N = \underbrace{u. r.Eb.Rs}_{4.No.Bn}$$
 (Eq3.8.4.a)

where u is the squaring loss given by u= 1/(1+(No/2Eb)), Rs = symbol rate, r is the roll-off factor and Bn = noise bandwidth of the second filter of bandwidth B. This function can be normalized to the signal to noise ratio per Hz and hence for a symbol rate of 256Ksymbols/sec and 30% Raised cosine filters, the spectral density for specified Eb/No can be found ,Table 3.8.4.a.

Received signal Eb/No dB	Recovered Symbol timing component SNR dBHz
10	52.6
8	50.5
6	48.3
4	46.0
2	43.6

Table 3.8.4.a Eb/No Against Recovered Symbol Timing Component

These results do not include the self noise due to ISI. We require for low ISI and low degradation in BER a rms timing jitter phase variation of less than 22 degrees <9> for rectangular pulses. The 30% Raised cosine impulse response shape therefore requires more accurate symbol timing sampling to obtain near zero ISI. This ISI results in a reduction in eye height. This reduction is not caused by the main pulse lobe since its shape is nearly constant over the family of curves but by the the zero crossing point no longer being zero at the sampling instant. Another

consideration in this system is that the 'local oscillator' and the master system clocks are also regenerated from this recovered symbol clock. The variance on the symbol clock must therefore be kept to a minimum as the symbol clock is multiplied in the regeneration of the local oscillator and hence its variance also increases by a similar factor. The theoretical timing error variance in radians squared obtain is given by Palmer et al <14> as,

$$\sigma^2 = 1/(2S/N),$$
(Eq3.8.4.b)

examples of which are shown in Table 3.8.4.b.

SNR	Recovered	Symbol clock Phase
dB	variance rad <sup>2</sup>	RMS Phase deviation degrees
10 15 20 25	0.05	12.8
15	0.016	7.2
20	0.005	4.1
25	0.001	2.3

Table 3.8.4.b Received SNR Compared with Recovered Carrier Phase Variance

These results do not include the jitter caused by self-noise due to ISI if any. Hence for a worst case of a 16 Ksymbol/sec data rate the ratio of symbol rate to carrier of 1.024MHz is 1:64. hence if the carrier requires a phase deviation of say 5 degrees then the symbol clock deviation is required to be 0.078 degrees and would require a symbol clock SNR of 54 dB indicating a noise bandwidth in the symbol timing recovery system in the order of 1Hz for a 10 dB Eb/No signal. Hence the recovered symbol timing rms

phase deviation must be kept to a minimum by the correct choice of output filtering. The recovered symbol rate frequency component is then locked to a reference symbol rate frequency, obtained by dividing down the master system clock, by a Phase Locked Loop. The voltage controlled oscillator (vco) of the loop is centred at 16.384 MHz and generates the master system clock. Division of this clock produces all clocking components for the system. As the symbol rate reference is obtained from this master clock, and the Phase lock loop always locks with the same phase reference, all the system clocks can be maintained with the correct reference to each other. The symbol rate reference is capable of phase correction by 16 MHZ clock (61nS) to correctly select the initial A/D centre. The symbol reference with respect to the symbol rate reference can also be adjusted to correctly sub-sample the final shaping filter outputs.

# 3.9 Algorithm Development.

Throughout the design of the system, the algorithms used in the research and development of the digital modem have been implemented in Hardware and Software to produce a totally integrated system and meet the required specifications. This modelling and algorithm investigation was carried out using number of personal computers. investigations where carried out using a BBC Micro Computer and later on an IBM PC-AT. This required the production a number of algorithms to model the various functions software and enable the results to be extracted and used in the hardware implementation. The operation of each model will be discussed later but a general appreciation of the operation of the models will be considered.

As an example we will consider the algorithm to calculate the data that is to produce the transmitted waveform. This algorithm must perform a number of functions:-

- i) Generate all possible 6 symbol data patterns and calculate intermediate sample values from the convolution of the symbol stream with the transmitter filter impulse response.
- ii) Calculate the Transmit filter Impulse response from the Frequency response or vice versa.
- iii) Modulate the Intermediate samples onto the 1st IF carrier.

These functions could be implemented in one large computer program but due to memory restrictions this was segmented into a number of smaller programs that could be progressively used to create the final set of data. This required that intermediate data from the various programs was saved to disk before being used in the next program. This produces a simple format for the saved data and hence enabled data to be passed from algorithm to algorithm without any problems. This system of modelling could be further enhanced to produce a complete system simulation allowing functions to added or removed as desired.

# 3.9.1. Transmitter Algorithms.

As previously discussed, the transmitter must convert a stream of binary NRZ pulses and spectrally shape these in such a way that the overall response of the satellite channel conforms to Nyquist filter criteria. This is achieved by baseband filtering with Root 30% raised cosine filters for each channel data stream and then modulating this filtered symbol stream in quadrature onto the 1st IF

carrier as previously discussed in section 3.7.3. This is all performed by a look-up table implemented within a PROM. To enable this to take place as required the PROM must be programmed with the correct information. This required the development of a number of algorithms.

# 3.9.1.1. Raised Cosine Frequency Response and Impulse Response Generation.

This is obtained by the calculation of sample values from either the closed form time expression or transformation of the Frequency expression for the Raised Cosine Filter <13>. The Time domain response of the Raised Cosine function is given by :-

$$x(n\tau) = \frac{\sin \pi n\tau/T}{\cos \pi n\tau/T\beta}$$

$$\pi n\tau/T \qquad (1-(2\beta n\tau/T)^2)$$

$$(Eq3.9.1.1.a)$$

where  $\tau = 1/f_s$ ,  $T = k\tau$ , n = 0 to Nk and N is the number of symbol periods over which the single sided impulse response exists.

The Frequency domain response given by:-

$$X(nf') = \begin{bmatrix} 1 & 0 < nf' < (1-\beta)/2T \\ 1/2(1-\sin(\pi(nf'-1/2T)/\beta)) & (1-\beta)/2T < nf' < (1+\beta)/2T \\ 0 & nf' > (1+\beta)/2T \end{cases}$$
(Eq3.9.1.1.b)

Where  $f' = 1/N\tau$ , n = 0 to N-1 and N is the transform size. The Root raised cosine is obtained by taking the square root of the raised cosine frequency response values. The impulse response can then be obtained by taking the Inverse Discrete Fourier Transform IDFT of the result.

# 3.9.1.2. A Discrete Fourier Transform and the Inverse Discrete Fourier Transform

The DFT and IDFT algorithms were obtain from <5> and modified to save processing time. This saving in processing time was only viable since the time response was always symmetrical, hence the imaginary part of the complex result is always zero, and that the impulse response was generally quite short with respect to the total number of transform samples. Since the remaining samples are all zero then these contribute nothing by completing the remaining processing. This reduced the processing time by reducing the generality of the transforms and enabled a result to be obtained after say M\*N multiplications and additions, where M << N and M is the required number of output samples and N is the N point DFT, instead of N\*N for the DFT or Nlog<sub>2</sub> N for the FFT.

Hence where

$$M < log_2 N$$
 (Eq3.9.1.2.a)

then this form may be processed quicker than the FFT. This was not necessarily always the case but the simplicity of the program also increases the confidence in the final result. The DFT algorithm therefore became:-

$$F(iW) = \sum_{k=0}^{N-1} f(kT).Cos 2\pi ikT/NT$$

$$(Eq3.9.1.2.b)$$

for i = 0 to M-1

and the IDFT becomes

$$f(iT) = 1 \sum_{k=0}^{N-1} F(kW) \cdot Cos \ 2\pi i kT/NT$$

$$---k=0$$

$$N \qquad (Eq3.9.1.2.c)$$

for i = 0 to M-1

These programs were developed and integrated with the other software packages to enable any symmetrical sequence of real samples to be converted from the time domain to the frequency domain and vice versa.

#### 3.9.1.3. Convolution of Data Impulse Response.

This is required to take the data impulse stream of 6 data bits, convert to an input data address, and calculate the convolved output for all intermediate samples and their appropriate PROM addresses.

$$I_n = S_D * h(T)$$

for n = 0 to N-1, where N= sample rate/symbol rate and where h(T) is the impulse response of the transmit filter sampled at the sampling rate i.e. 4.096MHz.

 $\mathbf{S}_{D}$  is the sequence of impulses at period  $\tau_{\mathbf{S}}$  = symbol period given by the data word D

$$D = d_5 2^5 + d_4 2^4 + d_3 2^3 + d_2 2^2 + d_1 2^1 + d_0 2^0$$

and  $d_0 = lsb$ 

(Eq3.9.1.3.a)

such that

$$s_D = d_5^2 z^5 + d_4^2 z^4 + d_3^2 z^3 + d_2^2 z^2 + d_1^2 z^1 + d_0^2 z^0$$
(Eq3.9.1.3.b)

and

with the address location given by:-

$$A(D,n) = D \times N + n$$

(Eq3.9.1.3.d)

The resulting data can be modulated onto a carrier frequency 1/4 of the output sample rate by the inversion of alternate pairs of data samples. A pair consist of one P channel sample and one Q channel sample and forms one half cycle of the quadrature carrier output waveform. This enables the P and Q channels to use the same PROM but the data each channel accesses is offset by one sample period from the other, i.e. the P channel accesses even addresses while the Q channel accesses only the odd addresses.

# 3.9.1.4. Plotting of Eye Diagram, Impulse Response, and Frequency Response.

Software routines were produced to depict graphical results for data outputs. This reduced the probability of an undetected major error in the calculations since all the sampled data represents analogue processes which through experience can be evaluated more easily than tables of numbers.

#### 3.9.2. Receiver Algorithms.

The receiver algorithms and software can capitalise on the programs already developed for the transmitter in that the Raised Cosine, DFT/IDFT, and Plot programs can all be utilised in the receiver designs.

#### 3.9.2.1. The Primary Decimation Filters.

The primary filter perform two function:-

- a) Bandwidth reduction
- b) Output sample rate reduction.

The bandwidth reduction is obtained by choosing a series of coefficients that produce a sharp roll-off while preserving the signal passband, linear phase and short impulse response. This can be obtained by using a successive approximation technique whereby an initial frequency response is converted back and forth between its time frequency responses reducing undesired effects until all criteria are met. This technique resulted in an impulse response as previously seen in fig 3.8.3.3.a and frequency response in fig 3.8.3.3.b. This impulse response can be implemented using 15 coefficients but it should be noted that the frequency response has a small degradation at 3dB point of the signal. This can be equalized by tailoring the combine response of the Primary and Shaping filters produce the root 30% raised cosine response required. frequency response now forms a null at 1/8th of the sample rate the output can be sub-sampled down to a minimum rate of 1/4 the input sample rate.

# 3.9.2.2. The Shaping and Equalization Filters.

From the frequency response of the primary filters, X(W), and the required frequency response of Root 30% Raised Cosine Filters, Y(W), it is possible to calculate the required frequency response of the shaping filter, H(W) by:-

$$H(W) = \frac{Y(W)}{X(W)}$$
 (Eq3.9.2.2.a)

By the use of the IDFT, the time response and hence the coefficients can be found. Software routines were developed for all these manipulations. This results in the frequency response and time response of the shaping filter being as in fig 3.9.2.2.a and fig 3.9.2.2.b respectively.

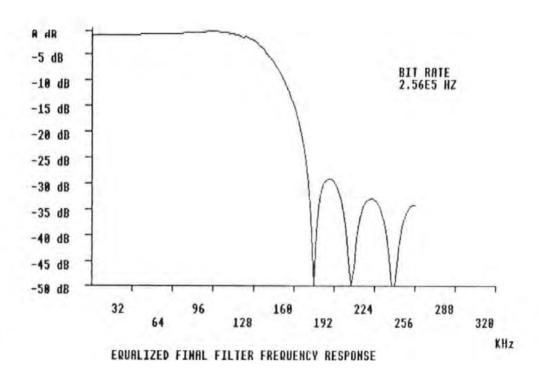


Fig 3.9.2.2.a Frequency Response of Final Shaping Filter with Equalisation.

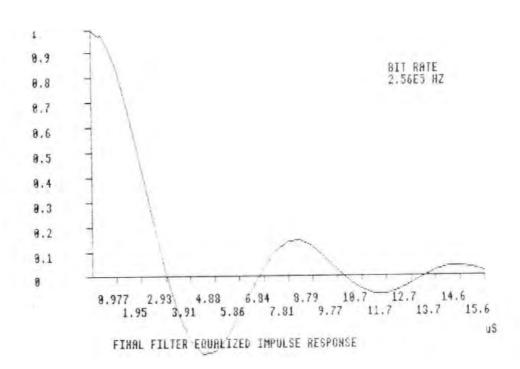


Fig 3.9.2.2.b Time Response of Final Shaping Filter with Equalisation.

# 3.9.2.2.1 Coefficient Multiplication in Digital Filter

The coefficients obtained for the received filters are not used directly but as a function in calculating a multiplication table to be stored in a PROM. This enables a fast calculation time only dependent on the access time of the PROM (less than 60ns). Each coefficient can be multiplied by all possible input sample words and hence for a 6 bit input word and 15 coefficients, a 1kbyte Prom is required, 2 x 16 = 1024.

This Look-up table can be produced by the function:-

$$M(i) = D' \times h(i)$$
 (Eq3.9.2.2.1.a)

where D' = sign magnitude representation of the 2's complement data word D = 0 ...63 for a 6 bit word.

h(i) = i th Coefficient value i=0 ...J-1 , and J= total number of coefficients. The address location for the multiplication result M(i) is given by:-

$$A_{M}(D,i) = D \times J + i$$
 (Eq3.9.2.2.1.b)

where  $J = 2^k$  and k=4. A 2Kbyte Signetics 82S191 PROM was used and allowed for two filter responses to be resident within the same PROM.

# 3.9.2.3. Data Decode Prom

The Data decode PROM must take samples from the P and Q channels at the centre of each symbol and perform the conversion from rectangular coordinates to Polar coordinates. This can be easily achieved by the pre-programming of two PROMS, to convert to phase and amplitude respectively.

$$\Phi_{a}(PQ) = \Gamma^{-1}(Qn/Pn) + x$$
(Eq3.9.2.3.a)

where  $\Phi_a$  (PQ) is the output phase value  $\Phi$  for address a(PQ), P,Q are the sample values for the centre of the symbol period of the P and Q channels nth sample respectively. The use of channel sign/ magnitude arithmetic allows the  $\Gamma$ -1(.) function as defined in Eq2.2.1 to be decoded for the full  $2\pi$  radians. The function x=0,  $\pi/4$  for BPSK and QPSK respectively rotates the space diagram at the output of the  $\Gamma$ -1(.) function such that the phase angles at the centre of the symbol are decoded onto the  $0,\pi/2,\pi,3\pi/2,2\pi$  axis for QPSK, and  $0,\pi$  axis for BPSK if the transmitter is locked to the receiver. The address conforms to the algorithm, for 6 bit sample values:-

$$a(PQ) = N.Pn + Qn$$
  $P,Q=0..N-1$  (Eq3.9.2.3.b)

 $N=2^k$ , and k=6.

The algorithm to produce the conversion to amplitude values is given by:-

$$A_{a}(P,Q) = \sqrt{(P_{n}^{2} + Q_{n}^{2})}$$
(Eq3.9.2.3.c)

with the address location for the result given by Eq3.9.2.3.b.

# 4. Introduction to Carrier Phase Estimation

The classical solution for the demodulation of PSK information involves the setting up of a local reference signal to synchronously demodulate the received signal from its intermediate frequency. For a BPSK or QPSK signal this can be simply achieved by the use of a quadrature down conversion process. The reference signal is mixed in quadrature with the received signal such that the products produce no cross channel interference between quadrature channels. Hence a phase reference must created that maintains a  $n.\pi/2$  radian phase offset (where n=0,1,2,3,4) to the received signal. This must maintained to an accuracy, in the presence of noise, of less than 0.5 radians deviation <23>, so that a major degradation in the system performance does not occur. Examples of phase error and Eb/No degradation can be seen in Table 4. This is classically achieved by the use of a PLL technique such as the Costas loop <24>, or one of the many other schemes that have evolved <10>. The Costas loop is particularly well suited to a quadrature down conversion system since most of the components required for its construction already exist for the demodulation of the data. If this technique is used in the digital demodulator already described the digital filter outputs would be used to provide phase information to a Voltage controlled local oscillator to maintain the reference phase relationship with the received signal. This produces a major problem. Due to the nature of the digital filters a long time delay is introduced into the loop. The effect of this time delay is as described by Develet <25>, and produces false lock conditions with a greatly reduced frequency acquisition range, due to a reduced loop bandwidth to stabilize the loop . The use of a sweeping additive acquisition signal can alleviate the reduction in acquisition range but false locks can still occur and would have to be detected and corrected. This system would also have the problem that if the signal became unlocked then the acquisition sequence would have to be reinitialized, hence losing data for this period. An alternative to the Costas loop method such as the xN mod  $2\pi$  method <10> also suffers from similar acquisition problems due to the narrow bandwidths of filters (or PLL) required to achieve the degree of accuracy required in the reference signal phase variance.

In general, an ideal carrier recovery system should be able to achieve three major goals:-

- 1) A wide frequency acquisition range.
- 2) Small reference phase variance.
- 3) A continuous acquisition mode.

A fourth point that is desirable in this digital system is that the incoming carrier frequency, I.F. must be maintained to be synchronous to the digital system clocks and the symbol rate clocks to allow for the simplified method of down conversion already described. Synchronism with the system clocks could be achieved by one of the above methods but unless these are also synchronous with the symbol rate the symbol information will slip past the system clocks and some method of estimating the centre of each symbol would be required. This could be achieved by an interpolation filter and represents an increase in the number of samples/symbol which have previously been reduced and hence is not the desired solution.

Several systems were investigated both experimentally and by the computer simulation in order to find a system that overcame all the above problems. The preferred system only required synchronization with the symbol rate frequency, while the carrier IF could be close to but not locked to system clocks. This resulted in a novel carrier recovery system that is not phased locked. Instead a Phase Estimator

operates on a changing phase, tracking the phase changes they occur. Phase variations are produced by a frequency offset from nominal, and phase noise contributions from all the frequency sources in the link. The process can also provide digital information of frequency offset errors that these may be corrected for example by a microprocessor to synchronously change frequency, without causing any major phase jumps, to the corrected frequency. A similar phase processor has been proposed by Viterbi and Viterbi <26> and simulated by Mcverry <27>. However, this required the use of complex arithmetic and was prone to cycle slipping due to noise at low Eb/No. The major cause of cycle slipping is the small number of symbols averaged over to achieve fast acquisition times and mistakes in tracking the transitions from one quadrant to the next. reference above the use of differential encoding and decoding reduces the effects of cycle slipping so that it is not a limiting factor. The need for maximum satellite power efficiency has now placed emphasis on absolute phase encoding so the cycle slip performance is important. reduce cycle slips the number of averaging samples must increased and an algorithm is needed to correctly detect the quadrant boundaries. One such algorithm is used in the method described by Tomlinson and Bramwell <21> and also does not require the use of Complex arithmetic as representation is converted representation with only the phase angle being processed. This results in a simplification of the hardware required and by the use of modulo arithmetic and Infinite Impulse Response Filters the acquisition time can be easily traded against cycle slipping performance at given values of Eb/No.

Eb/No dB	Regenerated Carrier SNR dB	Degradation from Theoretical dB
7	5	3.6
	10	1.5
	20	0.18
	30	0.02
6	5	3.0
	10	1.19
	20	0.13
	30	0.01
5	5	2.48
	10	0.95
	20	0.11
	30	0.01

Table 4.a Degradation from Theoretical Due to Noisy
Phase Reference

# 4.1. Phase Incoherent PSK Detection

In previous discussions on the operation of the digital receiver it has been assumed that the incoming signal has been forced to be synchronous to the system clock frequencies allowing the use of the digital frequency translation technique described in section 3. This results in a precise phase relationship being maintained between the received signal's I.F. centre frequency and the system clock i.e. Local oscillator. The case is now considered where this is not true, where the signal is not phase locked but where the I.F. frequency is close to the reference signal and assuming no noise component is present for simplicity. It can be shown that the signal, at the symbol centre, after filtering of high order frequency components can be represented by:-

#### P. channel output

$$R_{p}(t) = P \cos(\Phi(t)-\phi) - Q \sin(\Phi(t)-\phi) \qquad (Eq4.1.a)$$

Q. Channel output

$$R_{q}(t) = P \sin(\Phi(t)-\phi) + Q \cos(\Phi(t)-\phi)$$
 (Eq4.1.b)

where  $\Phi(t)$  is the time varying phase produced by the frequency offset , $\phi$  is initial reference phase offset,and P and Q represent the data signal for a QPSK system. In the synchronous case, assuming  $\phi$ = 0 and  $\Phi(t)$ = 0 then:-

P. Channel, 
$$R_p(t) = P$$
 (Eq4.1.c)

Q. Channel, 
$$R_q(t) = Q$$
 (Eq4.1.d)

as expected. The significance of the equations 4.1.a and 4.1.b can be best obtained by an examination of the Argand

diagram that they produce. This can be seen in fig 4.1.a. As the value of  $\Phi(t)$  changes with time the carrier phasor rotates with reference to the receiver phasor axis set up by the receiver local oscillator. This results in the phase angle of the transmitted symbol set rotating with the phasor  $\Phi(t)$  mod  $2\pi$ . It is necessary to be able to calculate this rotation of  $\Phi(t)$  on a symbol to symbol basis and correct for this rotation when decoding the data signal to convert from a phase incoherent system to that of phase coherent. This rotation can be made easier to manipulate by converting the rectangular format of eq4.1.a and eq4.1.b to that of a Polar format and hence become:-

$$A^2 = R_p(t)^2 + R_q(t)^2$$
 (Eq4.1.e)

$$\Phi'(t) = \Gamma^{-1} (R_q(t)/R_p(t))$$
 (Eq4.1.f)

where  $\Phi'(t) = \Phi(t) - \emptyset$ . If it is assumed that the P and Q data are both constant at +1 then the function  $\Phi'(t)$  represents a linear ramp over the range 0 to  $\infty$  mod  $2\pi$  where the rate of change of phase with time  $d\Phi'(t)/dt$ , the slope, is proportional to the frequency difference between the I.F. and the local oscillator fig 4.1.b. The addition of data to the signal results in values  $\Phi'(t)$  constructed of the basic ramp caused by the frequency error,  $\Phi(t)$ , and the data phase change  $\emptyset_d(nT)$ . Hence to obtain any estimate of  $\Phi(t)$  the data must first be removed.

$$\Phi'(t) = \Phi(t) + \phi_{\mathbf{d}}(nT) - \phi \qquad (Eq4.1.g)$$

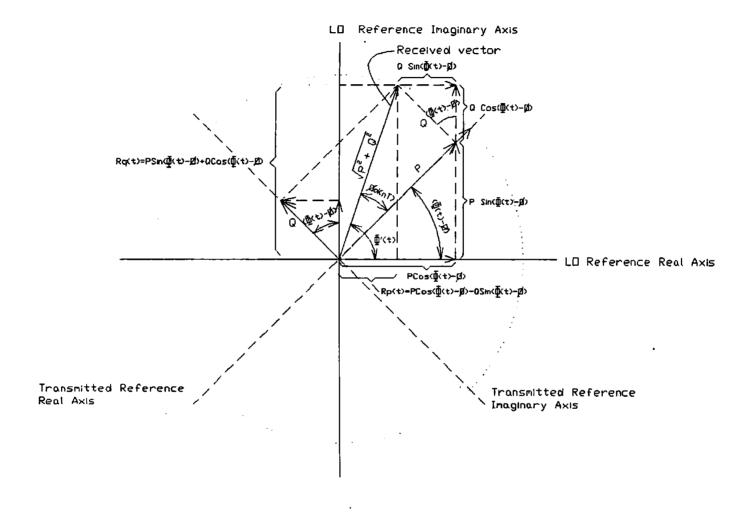


Fig 4.1.a Argand Diagram of Received Vectors Against Local Oscillator Reference.

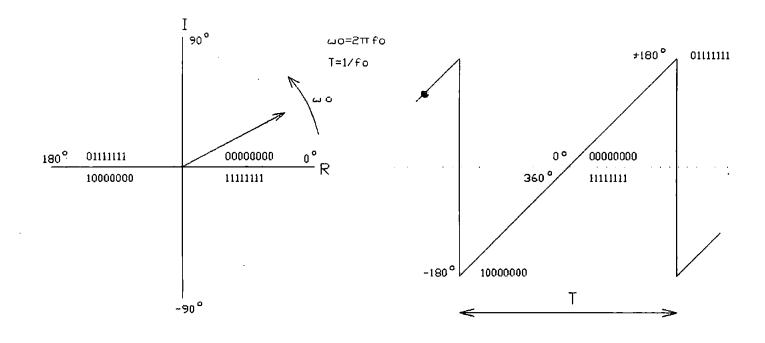


Fig 4.1.b Linear Representation of Frequency Offset as Changing Phase with Time.

### 4.2. Data Removal

Assume that available at the output of the  $\Gamma^{-1}(.)$  function there is an estimate available of  $\Phi(t)$ ,  $\widehat{\Phi}(t)$ . If this is subtracted from  $\Phi'(t)$  then letting  $\phi = -\pi/4$  the result is :-

$$p(t) = (\Phi'(t) - \hat{\Phi}(t)) \mod 2\pi$$
 (Eq4.2.a)
$$= (\Phi(t) + \phi_{\hat{d}}(nT) + \pi/4 - \hat{\Phi}(t)) \mod 2\pi$$
 (Eq4.2.b)
$$= (e(t) + \phi_{\hat{d}}(t) + \pi/4) \mod 2\pi$$
 (Eq4.2.c)

where e(t) represents the error between the actual value of  $\Phi(t)$  and the estimated value  $\Phi(t)$ . If QPSK data is considered where the data is defined by phase angles  $\phi_d(nT)$ , at the centre of the symbol of  $m.\pi/2$ , for m=0..4, then data can be removed by the use of a x4 mod  $2\pi$  function. Division by 4 now results in p'(t) being restricted to a  $+/-\pi/4$  range with the usual phase ambiguity. (Similarly in BPSK but with a x 2 mod  $2\pi$  function.)

where n= 4

for m=0..4, n=4 n.m. $\pi/2$  mod  $2\pi = 0$ , and  $n\pi/4 = \pi$  hence

$$p'(t) = e(t) + \pi/4 \mod \pi/2$$
 (Eq4.2.d)

It has therefore been possible to produce an error signal with which to control the estimate of  $\Phi$  (t). Filtering by a function h(t) and then integrating results in an ideally linearized phase lock loop as shown by Jaffe and Rechtin <28> with the acquisition time dependent on the time constant of the integrator and the loop filter h(t). However if the phase estimate deviates from the received phase by  $\pm \pi/4$  then an ambiguity arises and the loop will not function correctly and fall out of lock. Large frequency errors can not be corrected by the processing loop. However, a supplementary frequency tracking loop can be used to correct major frequency errors. The system is therefore in lock or out of lock, lock being indicated by the phase estimate following the received phasor, i.e. with a error signal tending to zero, with only the usual ambiguity of n.m/4 for QPSK n=0..4, or similarly  $\pi/2$  for BPSK.

### 4.3. Phase Processor

Consider a system as in fig 4.3.a, where the data has been removed from the rotating phasor  $\Phi(t)$  and obtain a value p'(t) representing the error between the rotating phase  $\Phi(t)$  and the estimated value  $\Phi(t)$ . Addition of p'(t) to the phase estimate now results in a value for the rotating phase  $\Phi(t)$  since:-

$$p'(t) = (e(t) + \pi/4) \mod \pi/2$$
 (Eq4.3.a)

if 
$$|e(t)| < \pi/4$$
 then  
 $p'(t) = e(t) + \pi/4 \mod \pi/2$   
 $p'(t) = (\Phi(t) - \widehat{\Phi}(t) + \pi/4) \mod \pi/2$ 

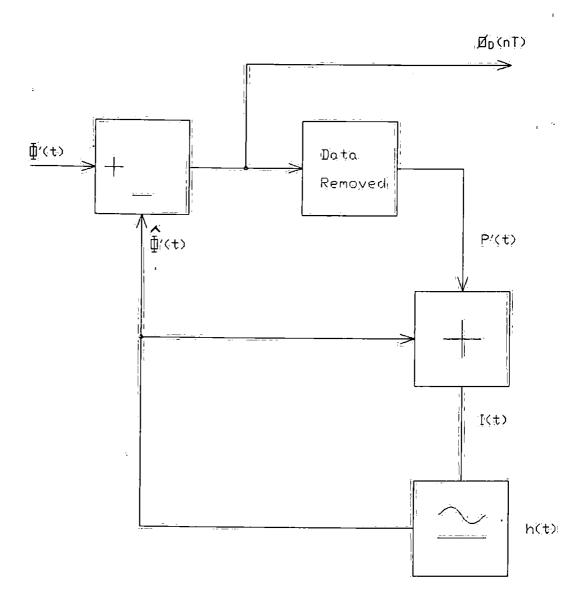


Fig 4.3 a Basic Phase Processor Block Diagram

hence

$$\hat{\Phi} (t) + p'(t) = (\hat{\Phi} (t) + \Phi(t) - \hat{\Phi} (t) + \pi/4) \mod \pi/2$$

$$= (\Phi(t) + \pi/4) \mod \pi/2$$
(Eq4.3.b)

The phase estimating loop is now only dependent on the filter time constant and not the integrator as before. If this is considered with a noise component Eq4.2.c then becomes:-

$$p(t) = (e(t) + \phi_d(nT) + \phi_n + \pi/4) \mod 2\pi$$
 (Eq4.3.c)

where  $\phi_n$  = phase noise, with zero mean, and bi-variate gaussian distribution, and variance  $\sigma^2$ . and Eq4.3.b becomes:-

$$\Phi_{n}(t) = \Phi(t) + p'(t)$$

$$= (\Phi(t) + \rho_{n} + \pi/4) \mod \pi/2 \qquad (Eq4.3.d)$$

i.e. phase,  $\Phi(t)+\phi_n$ , is limited to  $\pm\pi/4$  but variations greater than  $\pi/4$  re-enter at 0 or  $\pi/2$ . This is represented as a sawtooth waveform with amplitude 0 to  $\pi/2$  and repeating four times for every revolution of the received phasor. The rotating phasor has therefore been recovered with phase noise variance superimposed. We wish to obtain the expected value of  $\widehat{\Phi}_n(t)$ . Hence :-

$$E[\widehat{\Phi}_{n}(t)] = E[(\Phi(t) + \emptyset_{n} + \pi/4) \mod \pi/2]$$
 
$$(Eq4.3.e)$$
 
$$= E[\Phi(t) \mod \pi/2] + E[\emptyset_{n} \mod \pi/2]$$
 
$$+ E[\pi/4 \mod \pi/2]$$
 and 
$$E[\emptyset_{n}(t)] = 0 \text{ therefore } E[\emptyset_{n}(t) \mod \pi/4] = 0$$

$$E[\widehat{\Phi}_{n}(t)] = E[\Phi(t) \mod \pi/2] + \pi/4 \qquad (Eq4.3.f)$$

The expected or mean value being defined as:-

$$E[x] = \int_{-\infty}^{\infty} xp(x)dx \qquad (Eq4.3.g)$$

where p(x) is the probability of x .

The expected value of  $E[\widehat{\Phi}_n(t)]$  is therefore the mean of the signal  $\Phi(t) \mod \pi/2 + \pi/4$ . If the function  $\widehat{\Phi}_n(t)$  is filtered by a filter with impulse response h(t) the output becomes:-

$$y(t) = \widehat{\Phi}_{n}(t) * h(t)$$

where  $\widehat{\Phi}_n(t) = \widehat{\Phi}(t) + \emptyset_n(t)$  and  $\emptyset_n(t)$  is a sampled function of a stationary stochastic process .

$$y(t) = 1.$$

$$\int_{-\infty}^{\infty} \Phi_{n}(\omega) . H(\omega) e^{j\omega t} d\omega$$

$$Y(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \hat{\Phi}_{n}(t) e^{-j\omega t} dt. H(\omega) e^{j\omega t} d\omega$$

$$y(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \left[ \hat{\Phi}(t) + \phi_{n}(t) \right] e^{-j\omega t} dt H(\omega) e^{j\omega t} d\omega$$

$$y(t) = 1 \int_{-\infty}^{\infty} \left[ \int_{-\infty}^{\infty} (t)e^{-j\omega t} dt + \int_{-\infty}^{\infty} \phi_n(t)e^{-j\omega t} dt \right] H(\omega)e^{j\omega t} d\omega$$

let  $\hat{\Phi}$  (t) be a constant =  $\Phi$ 

$$y(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \left[ \Phi \left[ e^{-j\omega t} dt + \int_{-\infty}^{\infty} \rho_{n}(t)e^{-j\omega t} dt \right] H(\omega)e^{j\omega t} d\omega \right]$$

now

$$\int_{-\infty}^{\infty} \phi_{n}(t)e^{-j\omega t} dt = \phi_{n}(\omega)$$

therefore

fore
$$y(t) = 1 \int_{-\infty}^{\infty} [2\pi\delta(\omega)\Phi + \phi_{n}(\omega)]H(\omega)e^{j\omega t}d\omega$$

$$y(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} 2\pi\delta(\omega) \Phi H(\omega) e^{j\omega t} d\omega + \frac{1}{2\pi} \int_{-\infty}^{\infty} (\omega) H(\omega) e^{j\omega t} d\omega$$

as the bandwidth of  $H(\Omega)$  tends to 0 then

$$\frac{1}{2\pi} \int_{-\infty}^{\infty} \phi_{n}(\omega) H(\omega) e^{j\omega t} d\omega \text{ tends to } 0$$

where  $\Phi\delta(0)$  represents a dirac impulse at DC of height  $\Phi$  and H(0) represents the DC gain function of the filter. If H(0)=1 then the output value of the filter :-

 $y(t) = \Phi \qquad (Eq4.3.h)$ 

If the bandwidth of  $H(\omega)$  does not tend to zero then value of  $\Phi$  is degraded by the inclusion of the noise term. If  $\widehat{\Phi}$  (t) is not constant then  $\Phi(\omega)$  has a finite bandwidth and again the mean value is degraded. Eq 4.3.h shows it is possible to recover the value of  $\Phi(t)$  from a plus data phase signal. Practically the filter function does not reduce the bandwidth to zero and hence the component of the noise is not reduced to zero but close to it, depending on the bandwidth of the filter. This manifests itself as a random variation around the the rotating phasor. The use of the filter introduces a time delay Τd into the process. This effectively means that the estimated value of  $\Phi_n(t)$ the value of the rotating phasor by Td. If the phasor's rate of change is slow compared to Td then has little effect. However as the rate of changes increases then the estimated value  $\Phi_n(t)$  has an increasing phase error difference with  $\Phi(t)$  and the estimation will then become ambiguous as this phase error increase radians for QPSK or  $\pi/2$  for BPSK. This can be overcome by projecting the phase estimate over the delay time Td. requires a knowledge of both the time delay Td and the estimate of the rate of change of  $\Phi(t)$ i.e. the slope the frequency offset. The phase ramp or possible offset frequency range for the mean phase system alone therefore occurs when the phase delay around the phase filter loop is less than  $\pi/M$ :-

### 4.4. Frequency Offset Calculation

At the output of the  $\Gamma^{-1}(.)$  function, for a received M'ary signal plus noise with a frequency offset, it has been shown that by the subtraction of an estimated phase, data removal and filtering that it is possible to update that phase estimate. If an output is taken from the  $\Gamma^{-1}(.)$  function in parallel to this, and the data phase changes are removed from it by the use of a xM mod  $2\pi$  function, a M. $\Phi_n(t)$  phase output can be obtained, where  $\Phi_n(t) = \Phi(t) + \phi_n$ . Against time on a linear scale this can be represented as a ramp with period T=1/Mfo where fo is the offset frequency, over a phase change of 0 to  $2\pi$  radians; 0 and  $2\pi$  positions are the same as the function is mod  $2\pi$  and can be represented on a unit circle. It is required that an estimate for the rate of change of phase is to be found,  $d\Phi_n(t)/dt$ .

$$\frac{d\Phi_{n}(t)}{dT} = \frac{\Phi_{n}(t) - \Phi_{n}(t-T)}{T}$$
(Eq4.4.a)

Due to the effect of noise on the phasor,  $\Phi_n(t)$ , there is a probability density distribution about the  $\Phi(t)$ . One method of obtaining the most accurate value of  $d\Phi_n(t)/dt$  is by the evaluation of the sum of least squares error <29>.

The least square error slope, m, can be shown to be given by :-

$$m = \frac{\{n(\Phi(n)-\Phi(1))+ (n-1)(\Phi(n-1)-\Phi(2))+(n-2)(\Phi(n-2)-\Phi(3))+\dots\}}{2(n^2+(n-1)^2+(n-2)^2+\dots)}$$

(Eq 4.4.b)

n=(N-1)/2 where N=total Odd number of samples.

Hence by sampling  $\Phi_n(t)$  at regular points it is possible to calculate the best slope passing through these points. With the calculation of this slope value it is now possible evaluate a projected value m.X, where m.X is defined in Εq 4.7.3.2.b for the rate of change of  $\Phi(t)$  of the delay time of the mean filter.i.e. Calculation of expected value  $\Phi(t)$ . By the addition of this projected slope value it now possible to compensate for any known constant time delays within the system and estimate a value of  $\Phi$  (t) which is very close to that of the incoming rotating phasor. The final system model becomes that of fig 4.4.a. The advantage of placing the slope detection outside of the main loop is that once the slope has been correctly deduced then this aids the locking of the mean loop. If the slope detector is within the loop unless the system is locked the the projected slope can enhance the error in the estimated value and the system may never acquire lock.

### 4.4.1 Phase Estimator Recovered Phase Deviation

By analysis of the Final Phase estimator diagram as shown in Fig 4.4.a it can be shown that the deviation on the Estimated Carrier Phase can be given by:-

$$\sigma_{\rm T}^2 = \frac{2.(m'.M)^2.\sigma_{\rm n}^2}{L_{\rm f}} + 2\sigma_{\rm T}^2 + \sigma_{\rm n}^2$$
(Eq 4.4.1.a)

where  $\sigma_{\overline{T}}$  = the estimated carrier Phase,  $\sigma_{\overline{n}}$  = the phase

deviation due to AWGN, m'= frequency offset slope multiplier, M = M'ary PSK (2 or 4) and  $L_f$  and  $L_p$  the number of symbols over which the frequency and Phase means are averaged over. i.e 16 for Phase coefficient = 15/16 and 128 for Frequency coefficient = 127/128.

This can be shown to be:-

$$\sigma_{T}^{2} = \sigma_{n}^{2} \left[ \frac{2 \cdot (M \cdot m')^{2} \cdot L_{p} + L_{f}}{L_{f}(L_{p} + 2)} \right]$$
(Eq 4.4.1.b)

For  $L_{p} = 16$ ,  $L_{f} = 128$ ,  $m' = 0.547$ , and  $M = 4$  for QPSK
$$\sigma_{T} = 0.3\sigma_{n}$$
For BPSK  $m' = 1.094$ ,  $M = 2$ 

$$\sigma_{T} = 0.3\sigma_{n}$$

This is the same as for QPSK and is due to m'M being equal for BPSK and QPSK as expected. For an input signal to noise of 7 dB Eb/No for BPSK a Phase deviation (1 $\sigma$ ) is equal to 19.5 degrees. The expected Phase estimator deviation is therefore 5.8 degrees.

# 4.5. Conversion from Phase Incoherent to a Phase Coherent System

With the system as described above in lock the error between the estimated value  $\Phi$  (t) and  $\Phi$ (t) the rotating phasor is small. Neglecting the phase ambiguity created by the data removal process, the resultant value p(t) consists of the phase data information plus noise. Since the Amplitude of the phase data sample is known it is now possible to convert from the present polar representation to that of a rectangular representation by the use of the functions:-

 $|\mathbf{P}| = |\mathbf{A}| \cdot (\cos p(\mathbf{t}))$   $|(\mathbf{E}\mathbf{q}\mathbf{4}, \mathbf{5}, \mathbf{a})|$   $|(\mathbf{E}\mathbf{q}\mathbf{4}, \mathbf{5}, \mathbf{b})|$ 

where P and Q are the data signals as before. Hence the Phase incoherently received signal has been transformed and processed to produce a phase coherent result. The ambiguity in the absolute phase must be resolved by the usual methods, i.e Differential encoding, use of an FEC codec, or the transmission of a unique word.

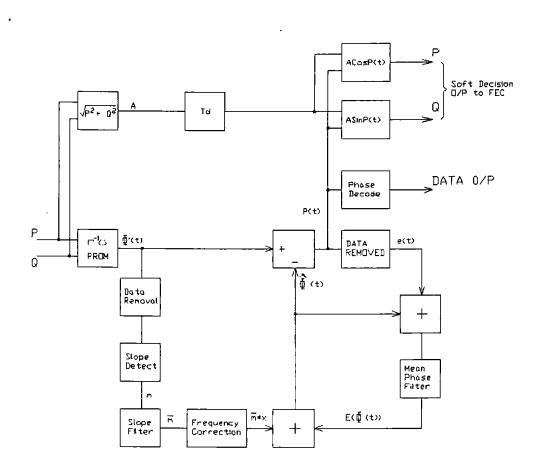


Fig 4.4.a Final System Diagram for Phase Estimator

### 4.6. Phase Estimator Mathematics

The operation of the Phase estimator has already been described, however the mathematics associated with filtering operation must be considered. The arithmetic that is used relate to values constrained within 0 and  $2\pi$ , i.e. a circular function, and not to values in the theoretical range of  $-\infty$  to  $+\infty$  as is usually the case in filtering. Let us consider the unit circle as in fiq 4.6.a, diagram is marked with degrees and quadrants represent the path taken by a rotating phasor. Consider point P1 on the circle. If we add to P1 another point which also lies on the circle the resultant Pr will also lie on the circle and can be represented by the formula:-

Pr= P1 + P2 mod 360

(Eq4.6.a)

The function mod 360 confines the result to lie on circle. Hence the addition of two points can be achieved. To perform a subtraction around the another factor must be known. If we consider points P1 P2 again and tried to calculate the difference phasors we can obtain two results. One if the difference is taken along the route P2->90->P1 and another if the is taken along P2->180->270->360->P1. Hence the filter must be able to distinguish which is the preferred route. sampling theory it is known that a signal must be at least at twice its highest frequency for the signal The be preserved without aliasing. frequency rotational the circle represents is the speed around inverse of the time taken for one complete revolution hence twice this frequency indicates that the circle be correctly sampled at points 180 degrees apart. If is now the case it can be simply seen that it shortest route that produces the correct result.

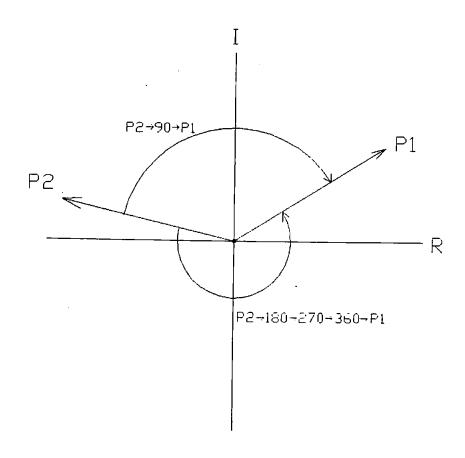


Fig 4.6.a "Shortest Route" Subtraction Around the Unit Circle

It is necessary to establish the arithmetic rules which always allows this to be the case. This can be achieved by the use of Complementary Arithmetic, for example consider the case of P1=32 degrees and P2 =211 degrees, the difference between the two points, minimum distance is 179 degrees.

$$Pr = P2 - P1$$

(Eq4.6.b)

In complementary arithmetic this could be calculated as

$$Pr = P2+(360-P1) \mod 360$$

(Eq4.6.c)

ie

 $Pr = 211 + (360 - 32) \mod 360$ 

 $= 211+328 \mod 360$ 

 $= 539 \mod 360$ 

= 179

If P2 is increased to 213 degrees then the result becomes 181 degrees which in complementary form represent -179 degrees, hence it is possible to distinguish the direction of the minimum distance as well as its magnitude. The function Pr, eq4.6.b can be simply represented in digital circuitry by the use of 2's Complement arithmetic and the modulo function accomplished by allowing the overflow of adders not to be acknowledged.

### 4.7. Implementation of the Phase Estimator.

The phase estimator requires in its implementation a number of algorithms which will be considered individually.

## 4.7.1. The $\Gamma^{-1}(.)$ Function

The conversion from rectangular to polar coordinates is achieved by the use of two PROMs. These are pre-programmed with algorithms to convert the sign magnitude quadrature signals to a Amplitude and Phasor representation. The  $\Gamma^{-1}$  information is a look-up table which conforms to the algorithm :-

$$\Phi_{a}(PQ) = \Gamma^{-1}(Qn/Pn) + x$$
 (Eq4.7.1.a)

where  $\Phi_a(PQ)$  is the output phase value  $\Phi$  for address a(PQ), P,Q are the sample values for the centre of the symbol period of the P and Q channels nth sample respectively. The function  $x=0,\pi/4$  for BPSK and QPSK respectively, equivalently rotates the space diagram at the output of the  $\Gamma$ -1 function such that the symbol centre phase angles are decoded onto the  $0,\pi/2,\pi,3\pi/2,2\pi$  axis for QPSK, and  $0,\pi$  axis for BPSK if the transmitter is locked to the receiver. This allows the xM MOD  $2\pi$  function to fold all phase errors around the 0 radian axis. The address conforms to the algorithm, for the two 6 bit sample values:-

$$a(PQ) = 64.Pn + Qn$$
 P,Q=0..63, (Eq4.7.1.b)

Hence a minimum 12 bit address prom is required for each data format with a 8 bit output word. This gives an output accuracy of 1.41 degrees and a error deviation of 0.26 degrees (table 4.7.1.a). Increasing the output word width

has very little effect on the overall performance of the system since this is already approximately 48dB S/Nquant and the system is limited by the quantization of the input to the  $\Gamma^{-1}(.)$  function. However the accuracy, and monotonicity of the output signal can be improved by the use of 7 bit Channel words at the address inputs (as shown in table 4.7.1.b).

n Bits Output Quantization	Phase error deviation in degrees
3 4 5 6 7	8.14 4.12 2.06 1.04 0.52
8	0.26

Table 4.7.1.a The Effects of Output Quantization on Phase in Rectangular to Polar Conversion

n Bits Input Quantization	Phase Error True Output	Deviation in degrees 8 bit Quantized output
4	8.94	8.94
5	4.06	4.06
6	3.07	3.08
7	1.25	1.28
8	0.37	0.45

Table 4.7.1.b The Effects of Input Quantization on Phase Output in Rectangular to Polar Conversion

It can also be seen from the table 4.7.1.a and 4.7.1.b that the total output phase deviation  $\sigma_{qo}$  conforms to the rules of power wise addition:-

$$\sigma_{qo}^2 = \sigma_{iq}^2 + \sigma_{oq}^2 \qquad (Eq4.7.c)$$

where  $\sigma_{iq}$  = phase error deviation due to input quantization

and  $\sigma_{\rm oq}$  = phase error deviation due to output quantization. Hence an overall 16 kbyte PROM could provide the decoding of the  $\Gamma^{-1}(.)$  for both BPSK and QPSK without any major increase in cost whilst producing a reduction in phase error variance which is additive to the noise created variance. The transformation to an amplitude function can be similarly performed using a PROM look-up table pre-programmed with the algorithm:-

$$A_a(PQ) = \sqrt{(Pn^2 + Qn^2)}$$
(Eq4.7.1.d)

the address a(PQ) being given by Eq4.7.1.b as before.

The 8 bit output words from the  $\Gamma^{-1}(.)$  PROM are in 2's Complement form to minimise the hardware for the processor implementation. The block diagram for the processor now being as in fig 4.7.1.a, and all values of degrees are scaled to an 8 bit representation of 256 levels or quanta, given by:

where  $m=2^n$ , n=8 bits, and deg is in the range 0 to 360 degrees. The output from the  $\Gamma^{-1}(.)$  PROM, at the data Symbol rate is fed into the Mean Estimator and the Slope Estimator and the operations carried out in parallel.

### 4.7.2. Mean Estimator.

The mean estimate is obtained following a number of sub-processes as described below.

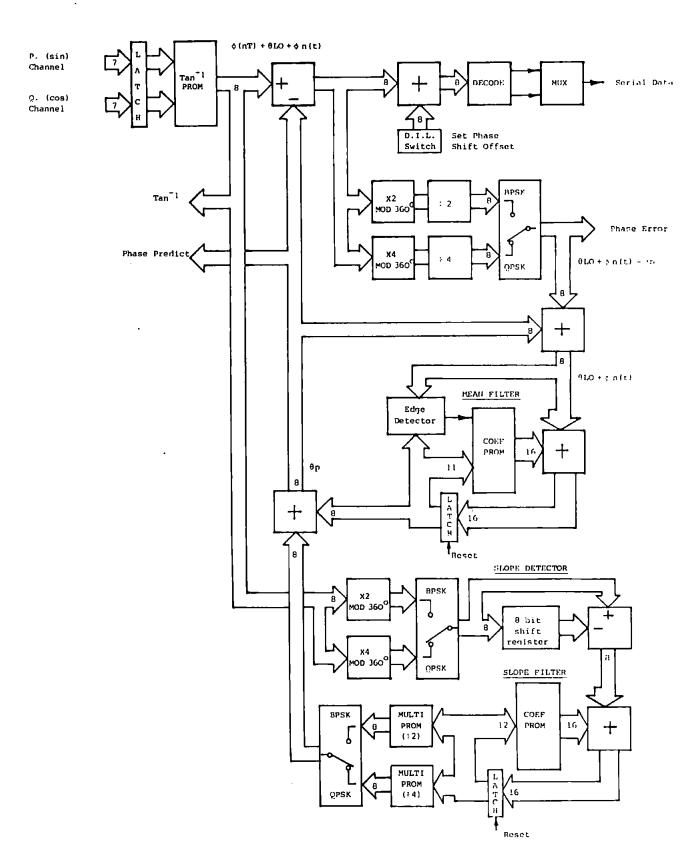


Fig 4.7.1.a Block Diagram of the Digital Phase Processor Implementation

### 4.7.2.1. Subtraction of Current Phase Estimate $\hat{\Phi}$ (nT).

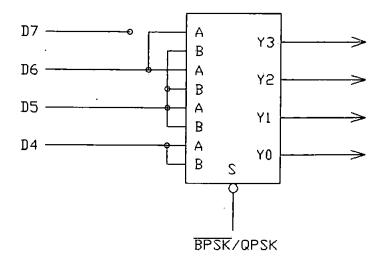
The first operation is the subtraction of the current phase estimate  $\widehat{\Phi}$  (nT), from the output of the  $\Gamma^{-1}(.)$  PROM,  $\Phi'(nT)$ . This is achieved by the use of 2's complement arithmetic. The subtrahend,  $\widehat{\Phi}$  (nT), is first complemented and then added to  $\Phi'(nT)$  in an 8 bit adder formed from 2 off 74F283 I.C.s. The complementation is performed by inverting the sample word and adding one, the addition being performed as a 'carry-in' to the adders. The output is allowed to overflow if required fulfilling the requirements of the circular function.

### 4.7.2.2. Data Symbol Removal.

Data is removed by the use of the xM mod 2π operation, where M= 2,4 for BPSK and QPSK respectively. This is simply carried out for a 2's Complement number by the shifting of the data  $\log_2 M$  bits to the left, i.e. multiplying by M. Bits that are shifted into position 9, MSB+1 are lost and bits shifted into position 0, the LSB are set to zero. The 8 bit output now represents the phase scale (+/-180) x M degrees so to readjust to the correct scale the result must be divided by M. This is done by bit shifting the word back to the right with the MSB's tied to MSB-1 for BPSK and MSB to MSB-1 and MSB-2 for QPSK. This can be implemented by the use of a selector IC 74F157 as in fig 4.7.2.2.a

### 4.7.2.3. Re-Addition of $\hat{\Phi}$ (nT)

This is achieved by the use of 2 off 74F283 adders. The 8 bit words being added together without the use of overflows to perform the circular function addition. The output is still an 8 bit word.



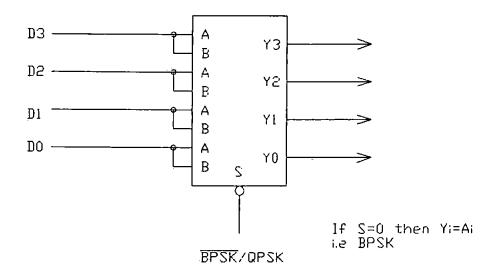


Fig 4:7.2.2.a Implementation of Data Removal From Received Phasor

### 4.7.2.4. Mean Filter

The mean filter is required to filter the rotating without the filtering of the transition created by the operator. The operation of the filter will be described later. The filter is of the Infinite Response Type ,IIR, and consists of an 8 bit input word and bit output word. To maintain the accuracy calculation and allow for the changing of to coefficients the is carried out with filter addition bits resolution. The input word of 8 bits is adjusted to 16 bit addition by the connecting the MSB's together. Shifting the position of this 8 bit input word relative to the bit feedback word allows the maximum attainable value ,with reference to the input word, to change by factors of This therefore allows the coefficient K to be changed by factors of 2 and hence allows the bandwidth the filter to be simply changed. The accumulator answer stored as a 16 bit word. The storage is performed by 2 74F374 latches, strobing the data when it has settled to correct value. These latches also provide the one period time delay of the filter. Enough bits, economically viable while preserving the accuracy of to the coefficient multiplying filter, are fed back where the input address representation is multiplied by the coefficient. This is at present 11 bits in the filter with 1 bit representing a transform condition modify the accumulator history. This bit effectively coefficient lookup table to one which accumulator data complemented before the coefficient multiplication was performed. The use of 2 off 2732 byte PROMs is therefore required. Two PROMs are used in parallel to obtain a 16 bit output, with one PROM containing the High byte information and the other the byte information. It is this 16 bit word that is fed adders.The output to the is taken from the

value stored on the latches and is adjusted back down to 8 bit representation by dividing this stored value by the coefficient denominator, m where K = m-1/m. By careful choice of m and K this can be a simple bit shift right operation, with zero entering the MSB positions. The 8 bit output word from this filter is now ready to be compensated for the frequency offset by the projected Slope Estimate.

### 4.7.3. Slope Estimation

Slope estimation or frequency offset estimation is performed by a number of sub processes as described below.

### 4.7.3.1. Data Removal

Data is removed from the  $\Gamma^{-1}(.)$  output value  $\Phi'(nT)$  by the same principle as in the Mean Filter section 4.7.2.2. The output is processed in the xM state to increase accuracy in the estimation process.

### 4.7.3.2. Slope Calculation.

Although it has been shown that the optimum fit to a series of points can be achieved on a least squares principle, the performance benefit of such a scheme is at a considerable cost in complexity and is therefore questionable. Another factor for consideration is that each increase in the accuracy of the 'fit' requires more points, increasing cost, and complexity. A simpler method is to take a first case approximation of the least squares approach given in Eq4.4.b and the calculation reduces to:-

$$m (nT) = \Phi'(nT) - \Phi'((n-k)T)$$

k

(Eq4.7.3.2.a)

where n & k are integers. Careful choice of k can produce a simple solution, i.e let  $k=2^L$  , L=0,1,2.. and this is

easily implemented in hardware. Filtering of this function can therefore be used to to limit the bandwidth of such signal to optimize the estimated value. The filter performed by an IIR filter of similar design as before but since it is the difference between phasor samples that being taken the transition does no longer exist. The IIR filter therefore requires no transition detection and bits of the accumulator result can be used to access the multiplied resultant of the 16 bit output. Shifting of input word relative to this 16 bit word also allows coefficient changes to be implemented as before. The output from the accumulator must then be scaled and projected forward in time to compensate for all time introduced around the mean estimator by :-

$$\delta\Phi(nT) = m(nT).T td$$

(Eq4.7.3.2.b)

 $T_{td} = T_d + 2T + 0.5T$ , the total time delay in Mean Estimator path; T is the delay due to the Mean Estimate filter; 2T is the extra delays in the Mean Estimator due to the digital logic timing constraints in this case; 0.5T allows calculations of the value to the centre of the next sample period with k = the number of samples over which the difference is taken and M compensates for the xM factor. This is implemented by the use of a scaling PROM using 12 bit input addresses with the output given by the representation of the input address value being multiplied by the factor  $d\Phi(nT)/dk$  and adjusted to qive an output. The 8 bit output word can now be added to the Mean Estimate to obtain the compensated phase estimate  $\Phi$  ((n-1)T).

### 4.7.4. Conversion from Polar to Rectangular Representation.

Having removed the rotating phasor by the subtraction the instantaneous phase estimate the resultant signal represents the phase positions of the data plus a noise component. Since the Amplitude of this phasor is also known is possible to back to reconvert а rectangular representation by the use of the functions given eq4.7.4.a/b. These can be implemented by the use of PROMs pre-programmed to form a look-up table containing the functions:-

$$Pn(A,\Phi) = An. Cos \Phi n$$
(Eq4.7.4.a)

$$Qn(A,\Phi) = An. Sin \Phi n$$
(Eq4.7.4.b)

where  $Pn(A,\Phi)$  and  $Qn(A,\Phi)$  are the Amplitude values of the P and Q data samples at the nth instant given by the address created by the functions A and  $\Phi$ , such that

Address(A,
$$\Phi$$
) = 256.A +  $\Phi$  (Eq4.7.4.c)

This indicates that a 14 bit address line is required and hence a memory space of 16 Kbytes. This will then give a soft decision output with 256 levels. This is considerably than the accuracy normally required for a decision FEC decoder. It has been shown that there is only a 0.25 dB degradation in performance if only 3 bit (8 quantization of the soft decision output is used compared to the unquantized output <30>. However, the interface to such a decoder could possibly be of an analogue nature and hence conversion form Digital to analogue may be required. Accuracy can be preserved and at minimal extra cost since 8 bits PROMs. are readily available from the

### 4.8. An IIR Filter Filtering a Circular Function

The circular function representation although being limited to the range 0-360 degrees by the MOD operator is in representing a continuous linear slope, proportional to the frequency offset, stretching to infinity . It is only need to represent this as a finite number that reduces to a saw tooth waveform produced by the MOD operator. Ιt is required that the rotating phasor is filtered to remove phase variations due to noise but that the this waveform in the preserved. Ιf we simply filter conventional manner then the bandwidth of the filter cause the transition point at 0/360 degrees to be from a sharp transition to that of a gentle transition with the introduction of a smoothing of the waveform. This would not occur if the waveform was a continuous slope infinity and hence the output waveform from such a function would be incorrect. We must therefore modify filter function such that the 0 and 360 degree points are classed as the same point and hence no smoothing of the transition occurs, only the reduction in Phase variations caused by noise. To achieve the slope, transition edge must be detected whenever it occurs, not just once per cycle since noise can cause the phasor to oscillate around any point and hence the transition can occur many times unpredictably. Careful attention to the signal processing carried out here is important otherwise unnecessary cycle slip events will be introduced. With detection of this transition point the history of the slope must be modified such that it appears that the information that is contained within the memory of the filter now comes from a continuous line and not the sawtooth ramp. requirement to modify the history of the waveform stored by the filter must be able to be achieved on an instant instant basis and the most suitable form of filter for this type of operation is that of a digital single

recursive, Infinite Impulse Response filter or IIR filter. Other forms are not ruled out but can have enormous complexity with little apparent benefit. This is as depicted in fig 4.8.a, the small signal (1  $\sigma$  phase error <45 deg ) transfer function of such a filter being given by:-

$$H(Z) = \frac{1}{1 - K.Z^{-1}}$$

$$Substituting \qquad Z^{-1} = e^{-j\omega T} \quad Eq \quad 4.31 \quad becomes: -1$$

$$|H(W)|^2 = \frac{1}{1 - K^2 - 2.K.\cos \omega T} \quad (Eq4.8.b)$$

where  $\omega$  = angular frequency, T = sample rate of IIR filter (equal to the modem symbol rate), and K = feedback coefficient of the form K= (m-1)/m. By varying the value of the coefficient K it is therefore possible to adjust the frequency response of the filter as shown in fig 4.8.b, and can be shown (Appendix C) to have a constant time delay, Td, for any filter coefficient K of:-

$$Td = \frac{-K.T}{1 - K}$$
 (Eq4.8.c)

Hence with Td constant it is possible to correctly calculate the projection factor for the slope coefficient. From Eq4.3.i ,this therefore gives a maximum mean phase filter tracking range for QPSK at 256Ksymbols/sec of less than 1032 Hz. The large signal response due to frequent transition errors will be quite different from the above due to the non linear nature of the filter arithmetic. However this condition only pertains to SNR values i.e. -1 dB, much less than the operating point i.e 2 dB and hence the small signal transfer function can be regarded as valid for the range of interest.

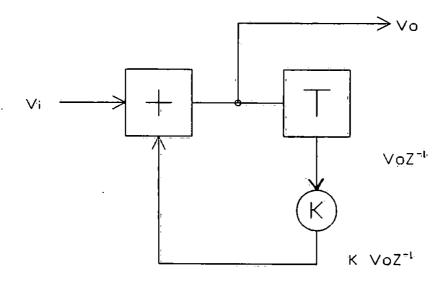
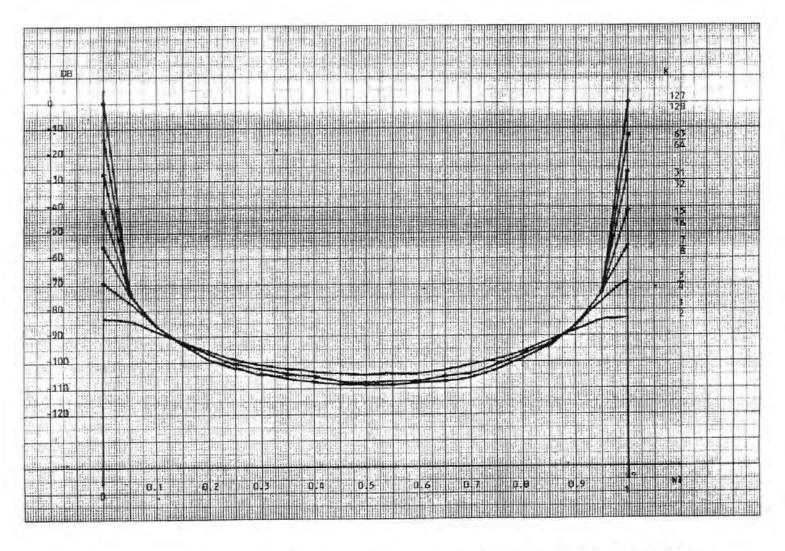


Fig 4.8.a Single Pole IIR Filter



 $\underline{\text{Fig}}$  4.8.b Frequency Response of Single Pole IIR Filter for Values of Coefficient K

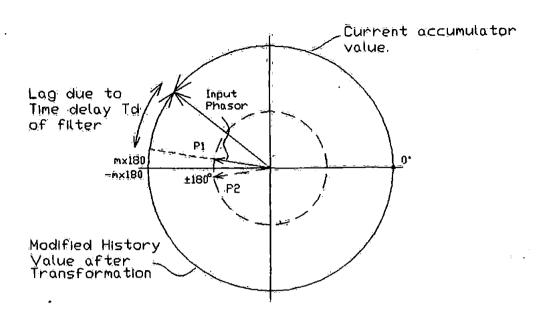
#### 4.8.1. Transition Transformation.

To enable the filter to operate without smoothing of the sawtooth waveform generated by the MOD function it must be possible to detect the fact that a transition is occurring and modify the accumulator result in such a manner this appears to change the history of the input function such that no transition appears to occur. Once the transition has been detected the modification of accumulator must take place. Consider the circle of 4.8.1.a the inner circle represents the sample values of the rotating phasor that are permissible and the outer circle the accumulator values which will tend to a maximum value of m times the maximum input value for an infinite series addition. For convenience the transition transferred to the +/- 180 degree point and hence maximum value for the accumulator is  $+/-m \times 180$ . accumulator value will also lag the rotating phasor by the time delay Td. Hence if the phasor was approaching the degree point in a positive direction i.e. anticlockwise. Then the accumulator value would be lagging behind it but also approaching m.180 from a positive direction. As the transition is reached and the phasor becomes negative the accumulator value, which is positive, must be transformed to appear to the new sample that the phasor has approaching from more negative values but still positive. This can be achieved by the transformation:-

$$A(nT) = \begin{bmatrix} A(nT) - m.360 & for 0 = < A(nT) = < m.180 \\ A(nT) + m.360 & 0 > A(nT) > -m.180 \\ (Eq4.8.1.a) & ... \end{bmatrix}$$

The algorithm which detects whether the history and input signal are on opposite sides of a transition boundary is defined as:-

Ed = 
$$(V_0/m)z^{-1} - V_1$$
 (Eq4.8.1.b)



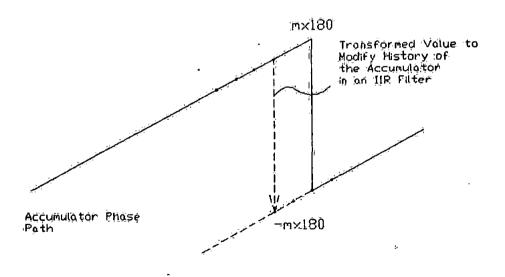


Fig 4.8.1.a Transition Detection Around the Unit

This can therefore be used to create a 'History Modifier' which modifies the 'sense' of the filter history dependent on the Edge detection function Ed such that:-

If Ed > 180 then C=1 if Ed <-180 then C=-1 Else C=0

By the use of this transformation with the detection of the transition area the it is now possible to low pass filter the rotating phasor as if the transition did not occur. Considering the following conditions:-

I/P = Vi in range +/- 180

Multiplication Coefficient K = 
$$(m-1/m)$$

O/P = Vo in range +/- Ma , where Ma =  $m \times Vi_{max}$ 

The single pole IIR Filter is defined by :-

$$Vo = Vi + K(Vo + C.Ma)Z^{-1}$$
 (Eq4.8.1.c)

$$Vo = \frac{Vi + K.C.Ma z^{-1}}{1-Kz^{-1}}$$
(Eq4.8.1.d)

where C is the History Modifier.

### 4.8.1.1. Digital Implementation of Transition Detection

The 2's Complement numbering system being used throughout the phase processor allows the performing of addition subtraction conforming to the rules of the function and implementation of the sign magnitude arithmetic by considering the operation of overflow The detection circuit is required to detect the transition created by the MOD operator. To detect this transition is only required that the difference is taken between an input sample value and the appropriately scaled accumulator detect if to the sample value has passed transition while the accumulator has not. This undertaken on a sign magnitude basis and is defined by equation eq4.8.1.b. The magnitude, if greater than 180 degrees, suggests that a transition has been reached while the sign indicates the direction that the phasor has moved, i.e. from the second quadrant to the third or vice Noise will corrupt this decision but the probability of noise sample causing a change of 180 degrees, without transition being present, is less than 2.2 e-7 Eb/No. It is the following of these transitions which allow the filtered phase output in a xM MOD 360 degree format i.e 4 times the carrier phase change/symbol for QPSK, to be converted to the linear ramp representing the change/symbol of the nominal carrier. Without monitoring of the transitions the phase estimate will cycle slip in relation to the received carrier phase and produce errors in the demodulation of the data. This is to the squaring circuit used for the recovery of a signal in BPSK. The output is twice the carrier frequency and hence must be filtered and divided by 2 before use the local oscillator. If this division by 2 is undertaken in the presence of noise cycle slips could occur and hence the recovered data would be in error.

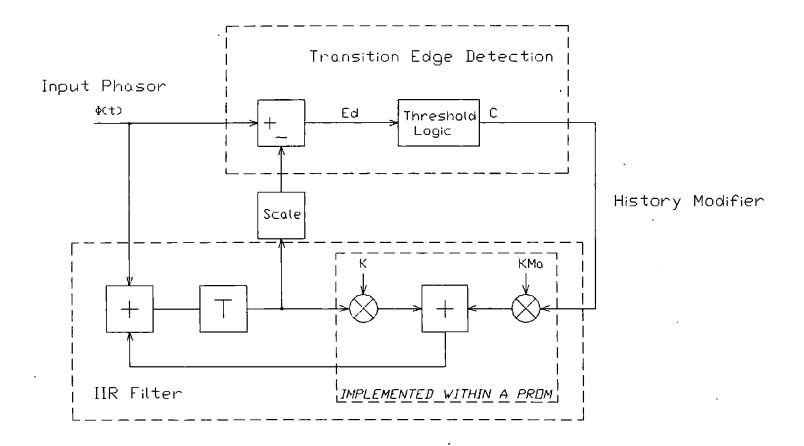


Fig 4.8.1.1.a <u>Transition</u> <u>Detection Circuit used in</u>
Phase <u>Processor</u>

### 4.8.2. Digital Implementation of the IIR Filter.

The IIR filter is implemented using a 16 bit accumulator with the Time delay being combined into a 16 bit latch to strobe the data once the result is stable. The output from the latch is then fed back to a 12 bit PROM which acts as a coefficient multiplier and also provides the transformation of the accumulator result. These results are pre-programmed into a look-up table with the following memory map, table 4.8.2.a. With the address given by:-

 $Address = H.2048 + Acczmn1 \qquad (Eq 4.8.2.a)$ 

where H=0 for C=1 and H=1 for C=-1. The value of 'Multin' is the decimal representation in sign/ magnitude form of the 2's complement accumulator delayed by 1 symbol period and truncated to an 11 bit address word, Acczmn1, and hence '2048' is the maximum number of values required. In the Off line calculation process for the lookup table, this word is converted from 2's complement to sign magnitude, multiplied by the coefficient and history modified as required. It is then reconverted from a sign magnitude representation to a 2's complement representation in a 16 bit wide word, the two bytes being stored as a High byte and a Low byte answer for the same input address.

I/P address	Operation
FFF	multin= -1024 to -1,
C00	output=(multin +2048)x K
BFF	multin = 0 to 1023
800	output = (multin-2048)x K
7FF	multin = -1024 to -1
400	output = multin x K
3FF	multin = 0 to 1023
000	output = multin x K

This memory map can be extended for greater accuracy by the use of larger PROMs and the appropriate scaling of the input address representation and adjustment factor. It should be noted that whatever the number of bits used to represent specific results that the answer is a scaled representation of 0 to 360 degrees ,or multiples of 0 to 360 degrees. Care must be taken to ensure that the correct representation is maintained. One method of arranging this is to enter and leave the filter as 8 bits but maintain all calculations within the filter at 16 bits. Hence a 12 representation in decimal scaled to a 16 bit word will have a maximum of 65520 (  $4095x2^{16-12}$ ) and 1 bit increments of the 12 bit word will produce 16 increments of the 16 representation. The output, from the filter, is taken the latched accumulator value and scaled to 8 bits by shifting right. This can only be performed accurately because the coefficient K is of the form K=(m-1)/m, where  $m=2^L$ , and L=0,1,2,... This results in a series of possible

coefficients of 1/2, 3/4, 7/8, 15/16, 31/32, 63/64, etc. Practical values range 15/16 to 127/128 and these have been found to be the most appropriate for the phase estimator to date.

### 4.9. Computer Simulation of Phase Estimator.

#### 4.9.1. Introduction

To investigate the performance of the Phase Estimator and to allow for a degree of optimization to take place the operation of the Phase Estimator was simulated by Computer. The computer used was an IBM PC-AT , Containing 512 Kbytes of RAM and a Mathematical Co- Processor to increase the speed of floating point calculations. The Simulation was written in the Pascal language implemented by Prospero Software Ltd. The Pro Pascal compiler complies with all the requirements of ISO 7185, level 0 with extensions for string handling, double-precision floating point arithmetic, random access files and separate segment compilation. The compiler is a true compiler generating native machine execution code <31>.

The simulation consists of a number of parts:-

- 1) The generation of Phase noise statistics .
- The use of these statistics to evaluate the performance of the Simulated Phase Estimator.
- 3) The Display of the Phase noise statistics and the Estimated Phase statistics as Probability Density Functions.

#### 4.9.2. Generation of Phase Noise Statistics

To evaluate the performance of the Phase Estimator the effect of the received noise on the filtered and quadrature down converted signal must be examined so that an accurate model of this noise can be produced while also being able to relate it to the standard measurement for data signals of Eb/No, the ratio of energy per bit to the noise spectral density. To enable this to be carried out the effect of the quadrature Matched Filters on the received noise power must be assessed. To enable the same data to be used for all forms of M'ary PSK the input signal to the quadrature down-converter is expressed as a value of Es/No, where Es is the energy per symbol. The bit energy can be related to the symbol energy by:-

$$Eb = Es /S$$

(Eq4.9.2.a)

where S = number of bits per symbol. It can be shown that the output SNR from each matched filter at the correct sampling point, is equal to 2Es/No.

P channel

signal energy 
$$o/p = Es.Cos^2 \phi(t)$$

(Eq4.9.2.b)

noise density o/p = No/2

Q channel

signal energy 
$$o/p = Es.Sin^2 \phi(t)$$

(Eq4.9.2.c)

noise density o/p = No/2

Therefore:-

total Signal energy = 
$$Es.Cos^2 \phi(t) + Es.Sin^2 \phi(t)$$
  
=  $Es(Cos^2 \phi(t) + Sin^2 \phi(t))$   
=  $Es$ 

total Noise density = No/2 + No/2 = No

Therefore combined Signal to noise = Es/No (Eq4.9.2.d)

Hence the energy per symbol, per filter is increase by a factor of 2, due to the matched filtering but the combined output SNR for the two quadrature filter outputs remains constant at Es/No. With this information it is now possible to numerically calculate the probability density function of the Phase noise, correctly scaled to the input Es/No value. This makes use of the independent quadrature noise components and their individual Gaussian PDF's, by the use of a rectangular to polar conversion.

# 4.9.2.1. Probability Density Function of White Gaussian Noise

Consider the time representation of bandpass Gaussian noise <5>, if the bandwidth of the noise is small compared with that of the centre frequency it is possible to represent the noise components as phasors and hence in the form:-

$$n(t) = n_{c}(t) \cos W_{c} t - n_{s}(t) \sin W_{c} t$$
(Eq4.9.2.1.a)

and it can be shown that this representation can be

extended to low pass noise and that the mean-squared value of n(t) equals the mean-squared value of the cosine noise term and equals that of the mean-squared sine noise term, i.e.

$$\overline{n^2}(t) = \overline{n_c}^2(t) = \overline{n_s}^2(t)$$
 (Eq4.9.2.1.b)

From Eq4.9.2.1a the mean-squared value of bandpass noise is given by:-

$$n^{2}(t) = \frac{n_{c}^{2}(t)}{2} + \frac{n_{s}^{2}(t)}{2}$$
 (Eq4.9.2.1.c)

Hence the noise is equally divided between the phase and quadrature channels and can be represented in phasor form as in fig 4.9.2.1.a. If this quadrature phasor is added to the signal phasor, assuming the signal phasor is 0 degrees, or that all data has been folded onto the 0 degree axis by a linear process, then the resultant deviation from 0 degrees is the phase noise error. If the deviation from nominal is calculated for a series of sample values of no and no taken from the Gaussian distribution, and the probability of this deviation occurring, the probability density function of phase error can be found.

Since the pdf of each of the noise components is an independent gaussian random variable, the probability of an event taking place which is dependent on two statistically independent functions is given by:-

$$P(A,B) = P(A).P(B)$$
 (Eq4.9.2.1.d)

Hence for any  $x_i, x_j$ , where  $x_i$  = i th sample of  $n_s(t)$  ,  $x_j$  = jth sample of  $n_s(t)$  :-

$$\phi(i,j) = \Gamma^{-1} \left[ \frac{x_i}{A + x_j} \right]$$
(Eq4.9.2.1.e)

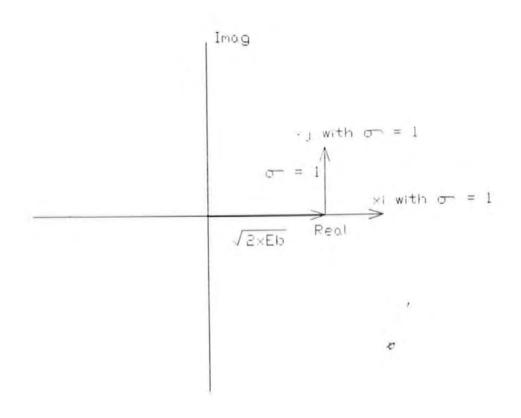


Fig 4.9.2.1.a Phasor Representation of Quadrature
Noise Components

where A= rms signal Amplitude. The probability of  $\phi(i,j)$  occurring :-

$$P(\emptyset(i,j)) = P(x_i).P(x_j)$$
 (Eq4.9.2.1.f)

and the probability of  $\emptyset=x$  is given by the summation of all values of  $P(x_i).P(x_i)$  producing the result  $\emptyset=x:-$ 

$$P(\emptyset=x) = \sum_{i} \sum_{j} P(xi).P(xj) | | \emptyset=x$$
 (Eq4.9.2.1.g)

If this is carried out over the range of  $x=-\pi$  to  $\pi$  the pdf of the phase error due to noise can be evaluated. It is therefore required that the Pdf of the noise samples  $x_i, x_j$  can be individually calculated and scaled for a particular value of Es/No. The probability of a sample x is given by the formula <5>:-

$$p(x) = \frac{e^{-(x-m)^{2}/2\sigma^{2}}}{\sqrt{(2\pi)\sigma}}$$
 (Eq4.9.2.1.h)

where  $m,\sigma^2$  are the mean and variance respectively. The factor  $1/\sqrt{(2\pi)}\sigma$  is to produce unit area under the curve. The function given in equation 4.9.2.1.h can be numerically evaluated by representing sample values of x in terms of  $\sigma$ , (since white gaussian noise m=0), and normalizing  $\sigma=1$ . After calculating for a range of x say from  $x=-5\sigma$  to  $+5\sigma$ , the cumulative distribution should tend to unity. However this is not the case due to its finite number of samples and hence the function must be scaled by the inverse of this cumulative value i.e.

$$x=5\sigma$$
 $x=5\sigma$ 
 $x=-5\sigma$ 
 $x=-5\sigma$ 
 $e^{-x^2/2\sigma^2}$ 
(Eq4.9.2.1.i)

and

C= 1/F(x) (Eq4.9.2.1.j)

Hence equation 4.9.2.1.h becomes:-
$$p(x) = \frac{e^{-x^2/2\sigma^2}}{c}$$
(Eq4.9.2.1.k)

The probability of a 50 event occurring is 1E-11 and a 60 event is 2E-16. A 5o event range is therefore considered to cover the range of probabilities of interest. It is possible to calculate the therefore now probabilities of samples  $x_{i}, x_{j}$  occurring and hence the probability of them occurring together by the use equation 4.9.2.1.f. It is now required that the value ø(i,j) be calculated for a particular value of Es/No. For this to be achieved the value of Es must be considered in terms of  $\sigma$ . If a value of Es/No, the signal to noise ratio of a symbol phasor, is given as x dB then this can converted to a power ratio and split into its quadrature components. Scaling by a factor of 2, for each quadrature channel, allows o to be maintained equal to unity. Hence the value of ø(i,j) can be calculated correctly scaled for values of Es/No and hence evaluated for Eb/No.

By the use of these techniques the pdf of  $\emptyset(i,j)$  can be evaluated over the range  $-\pi$  to  $+\pi$ . To obtain an accurate representation of this pdf it is necessary to evaluate a large number of points and to enable this to be economically achieved within the confines of the computer memory the a Histogram of the pdf is calculated. This results in all values of  $\emptyset(i,j)$  that fall within certain cells to be summed together. The cell width defines the accuracy to which an error function can be calculated, and the number of event results within a cell improves the accuracy of the probability calculation for that cell. It was found that a cell size of 0.5 degrees and a noise step range from 50 to -50 in 0.030 steps produce a accurate

answer when compared to standard error function tables. The results obtained are stored on disc and can be called from other programs to enable the results to be plotted or the simulation of the Phase Estimator evaluated.

#### 4.9.3. Phase Estimator Simulation.

To evaluate the performance of the phase estimator a computer simulation was produced that simulated operation of the hardware design but with the added flexibility of allowing changes in various functions to performed. The simulation is constructed within a shell of menus which allow the flexible functions of the simulation to be initialized. The menus include various trapping functions and error counting facilities. The phase noise samples are obtained from the pdf of the phase error for the particular noise level under investigation. The pdf of the SNR of interest is read from the disk and stored as array. This array is then adjusted and weighted such that uniformly distributed sampling of the array produces noise samples of random deviations with an overall distribution given by the initial pdf. This is achieved by having the area under the pdf being equal to unity. By the generation of a set of Uniformly Distributed Number's (UDN's), i.e numbers with uniform distribustion, between zero and unity it is possible to integrate the pdf of the noise to a point where the integral is equal to the UDN. The histogram cell in which this point rests therefore gives the appropriate phase noise point. This can reproduce the correct variate distribution without inhibiting the possibility of low probability samples. This is only the case over a large number of samples and hence the simulation must run for long period of time and be monitored such that it can be determined when the result has settled to an accurate enough value. Jeruchim <18> provides a confidence estimation on the Bit Error Rate and suggests that for BER of 10 K for a 99% confidence to achieve a small

deviation in BER,  $10^{k+2}$  bits must be observed. Hence for an error rate of 1  $\times 10^{-6}$  , an observation of 1  $\times 10^{8}$  bits is required. This of course requires a large amount of computational power and time. However the area of interest is more towards that of low Eb/No's and hence high error rates. This is therefore not a significant limitation. Once the noise samples can be created and distributed, according to the original pdf, then the simulation can add these noise samples, when required, to a set of samples which describe the operation of the signal, i.e. whether the simulation is operating on a coherent or incoherent signal. The Phase Processor simulation then manipulates these samples and decodes the results into phase angles. The phase results that are produced can be displayed and stored to enable errors or cycle slips to be evaluated. An error count can also be performed from the simulation and hence the BER calculated. The simulation also stores the estimated phase  $\widehat{\Phi}$  (t) and this can be evaluated as variance of the estimated value to the rotating phasor value  $\Phi(t)$ . This result is also stored on Disk to allow plots to be produced of this variation. The operation of the Phase Estimator Simulation is not included in this account but a full program listing can be seen in Appendix D.

### 4.9.4. Display of Phase Error Statistic

The results obtained of the phase estimate errors and the actual phase values used by the simulation are stored to disk to allow for post- processing along with the calculated phase error distribution. This post-processing is mainly to allow the result obtained to displayed in a fashion which can be readily understood i.e. in a graphical form. Let us consider the phase noise pdf as calculated. The Phase estimate results can be processed in a similar

fashion. The Plot program is again menu driven and allowing the plot requirements to be initialized. This can include magnification of the plot, multiple or single plots and filtering of the distribution.

## 4.9.4.1. General Description of Pdf Distribution Plot Program

The results of the phase noise pdf calculation are stored to disk with a heading consisting of a number indicating the length of the file, the cell width in degrees, and the standard deviation of the pdf. It is this information which is first read back into the plot program to enable the program to correctly plot the graph. This is followed by the reading into an internal array of the data describing the pdf. With this information all available to the program the pdf is plotted to scale and annotated with the rest of the data.

### 4.9.4.2. Smoothing Function

Due to the random sampled nature of the results if these are plotted directly the graphical result is is not always clear. To improve the display the data can be filtered by a function operating over a number of samples. This is achieved by the use of an algorithm which representing a single pole, IIR filter response with coefficient K in the form :-

K= m-1/m

(Eq4.9.4.2.a)

where m=1,2,3...10. and

$$Y(i) = Y(i-1).K + X(i)$$

m
(Eq4.9.4.2.b)

where Y(i) is the filtered output sample and X(i) is the current input sample.

#### 4.9.4.2.1. Magnification

In the x1 magnification mode the pdf displayed covers the range from - 180 to 180 degrees. This is often too large a range for large values of Eb/No i.e.Eb/No >8dB and hence it is desirable to magnify the plot. The range can therefore be expanded by an expansion factor in the sequence 1,2,3,5,10. Since the mean is always zero this occurs around the 0 degree point and hence expands the range of peak distribution. An example of the output from the Plot program can be seen in fig 4,9.4.2.1.a.

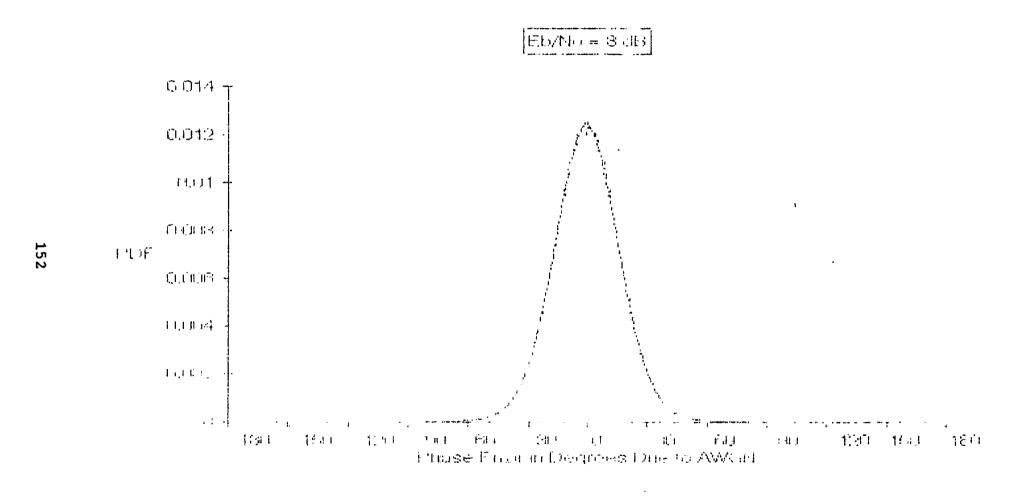


Fig 4.9.4.2.1.a Example of Plotted Phase Deviation due to AWGN

#### 5. Results

The results will be documented in two major sections:-

- a) The computer simulation results and predictions.
  - b) The experimental results.

These two main sections will then be broken down into sub-sections governing the various attributes of the implementation performance.

#### 5.1. Computer Simulation of Carrier Estimation

#### 5.1.1. Noise Statistics

The accuracy of the phase noise statistics was ascertained by the calculation of Probabilities of Error for a BPSK signal and compared to theoretical. For a BPSK signal to be in error the phase noise must be greater than 90 degrees. The probability of the phase being greater than 90 degrees is therefore the summation of the area under the curve from 90 to 180 degrees and -90 to -180 degrees. By comparison of this result with theoretical it is possible to evaluate the accuracy of the simulated noise distribution. It is therefore possible to choose the required number of samples that have to be calculated to produce an accurate phase distribution. The number of samples used in the calculation is governed by the noise step size. The evaluation of the noise step size can be seen in Table 5.1.1.

BPSK at Eb/No = 8 dB					dB	Probability of		Error*= 1.909072 x10		
						. of Samples		-/	% error	
1σ						121		8.133E-5	57	
0	.50					441		6.056E-5	68	
0	.30					1179		2.351E-4	-23	
0	.10					10201		1.836E-4	3.8	
0	.050	J				40401		1.9306E-4	-1.1	
0	.030	7				111779		1.8648E-4	2.3	
BPSK	at	Eb/No	=	90	iв	Probability	of	Error* = 3.3	62664 x10	
0	. 050	J				40401		3.41817E-5	-1.6	
0	.030	7				111779		3.44983E-5		
BPSK	at	Eb/No	=	3	dB	Probability	of	Error*= 2.287841 x10 <sup>-2</sup>		
	. 050					40401		2.36409E-2	A	
0	.030	7				111779		2.27417E-2	0.6	
0	.020	J				251001		2.31075E-2		
BPSK	at	Eb/No	=	5	dB	Probability	of	Error* = 5.9	53867 x10	
0	.050	7				40401		5.66557E-3	4.8	
	.030					111779		6.04744E-3		
BPSK	at	Eb/No	=	60	B	Probability	of	Error*= 2.3	8829 x10 <sup>-3</sup>	
	. 050					40401		2.31450E-3		
	. 030							2.41674E-3		

Table 5.1.1 Comparison of Accuracy of Noise Statistics

From the above calculation it was decided that a noise step size of 0.03 gave an accurate answer with an error on average of 0.5%. The time taken to calculate the noise sample using the IBM-AT at 6 MHZ Clocking and with Mathematical Co-processor was approximately 20 minutes per Eb/No point. To increase the number of sample points was considered unnecessary when comparing the trade off between accuracy and processor time. A selection of phase noise statistics obtained by the simulation can be seen in fig 5.1.1.a and it can be seen that the phase noise distribution is a bi-variate gaussian distribution . If consider various SNR then the distributions can be seen agree with those results obtained by Prokais <13> by evaluation of the joint probability density function.

# 5.1.2. Performance of Phase Estimator with AWGN, Frequency offset= 0 HZ.

The simulation was designed to enable a number of variables that an operating modem would encounter to be set up on initialization. ie.data rates, signal type, (BPSK, Signal to noise ratios, frequency offsets, phase and frequency filter coefficient, number of bits in the filter implementation etc. This results in a very large number of combinations to test the simulation under all conditions and would imply a considerable time being spent. This time can be considerably reduced by limiting the number of variables and performing initial tests to obtain an understanding of the appropriate areas of interest. can result in a decision directed test plan and hence reduce the number of variables to a manageable level. initial tests will therefore consist of simulations of BPSK and QPSK with zero frequency error over a range of SNR's with varying coefficients on the phase and frequency filters. The data rate is fixed at 256Ksymbols/sec and all other data rate performances can be scaled as appropriate. The number of bits in the filter implementations is set at 16. This will enable an optimum choice of phase and frequency coefficients to be selected. The key to the figures indicates the value of phase and frequency coefficients used, ie. p15f127 indicates a phase coefficient of 15/16 and a frequency coefficient of 127/128. A BPSK signal will first be considered.

#### 5.1.2.1. BPSK Performance for Varying Coefficients

Initial simulation conditions:-

- i) Type = BPSK
- ii) Symbol rate = 256Ksymbols/sec
- iii) Eb/No 3dB to 7 dB
- iv) Number of filter feedback bits = 16
- v) Frequency offset = 0 Hz

Consider fig 5.1.2.1.a and fig 5.1.2.1.b. It can be seen that the performance predicted by the simulation is close to theoretical and in some instants is better theoretical! This cannot be the case but it is within factor of 2 in BER,, which is generally considered reasonable uncertainty <18>. Expressed as an error from theoretical in dB's gives a worst case indication of approximately 0.5 dBs. The simulation time of simulation needs to be increased to obtain a more accurate answer if required. As this is only an experiment to ascertain the general operation of the phase estimator then this accuracy to within 0.5 dB is considered satisfactory and further accuracy is not required. Practically, measurement within 0.5 dB at low signal to noise ratios is difficult and requires very accurate measurement and long time averaging. One hypothesis that can be inferred from these performance figures is that the estimator will operate close to theory and at Eb/No's of 3dB's and

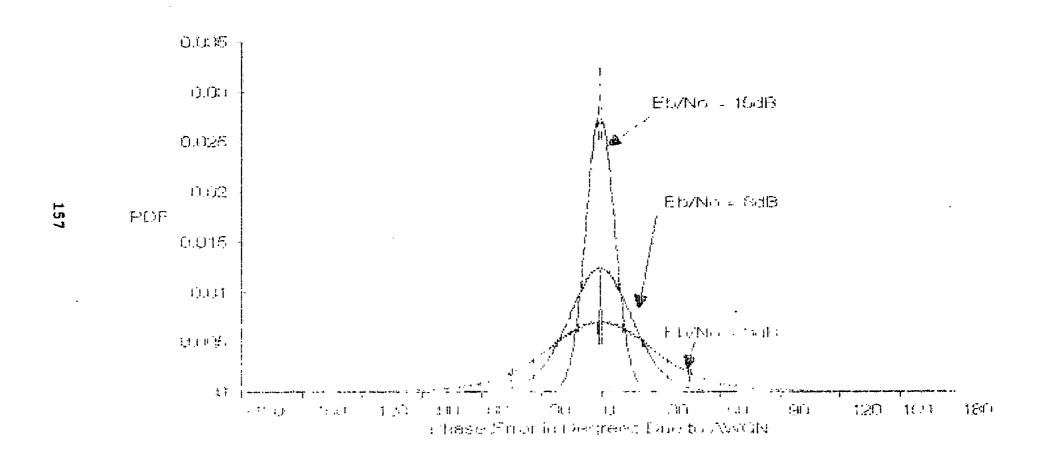
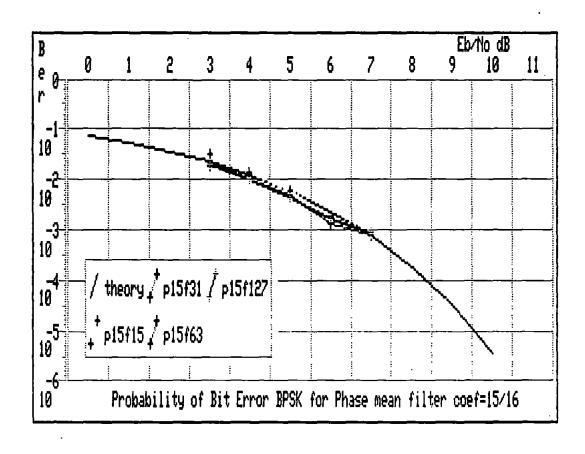
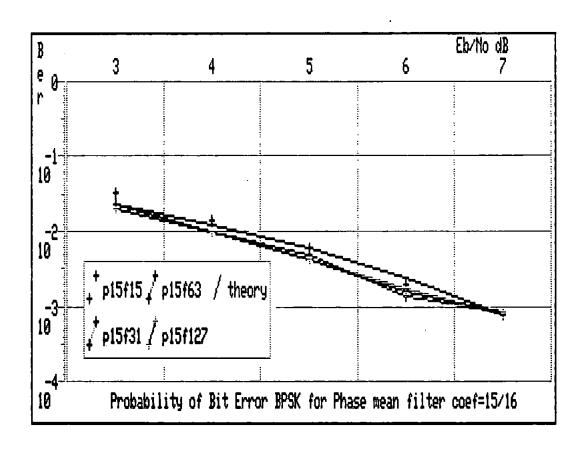


Fig 5.1.1.a Simulated Phase Deviations PDF produced by AWGN Source



 $\frac{\text{Fig}}{\text{Performance}} \frac{5.1.2.1.a}{\text{for f}} \frac{\text{Simulated}}{\text{offset}} = \frac{0}{2} \frac{\text{Hz}}{\text{Fig}}$ 



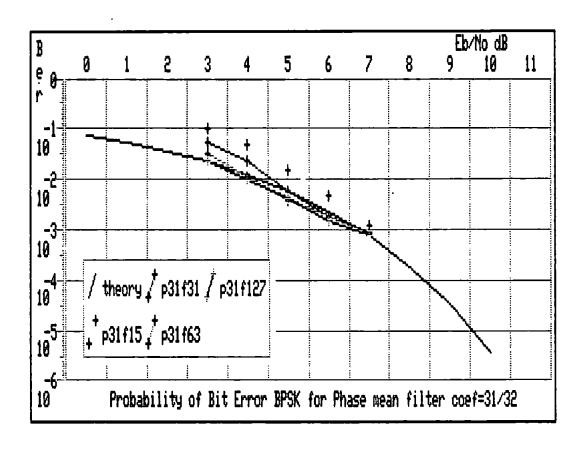
greater. We cannot draw any conclusions as to the required phase and frequency coefficients.

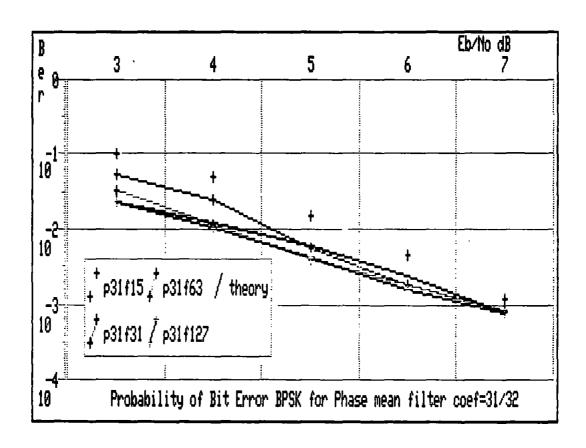
If we now consider fig 5.1.2.1.c and fig 5.1.2.1.d more can inferred as the the nature of the coefficient requirements. If we consider p31f15 then the frequency estimate is filtered less than the phase estimate and such is less accurate. Since this frequency estimate used to project the mean phase estimate then an inaccuracy in this calculation will increase the likelihood of error in the phase estimate  $\widehat{\Phi}$  (t) and hence the performance degraded by approximately 1.5dB. As the frequency estimate coefficient is increased then the degradation becomes less until again the curve lies close to that theoretical. This implies that the greater the accuracy the frequency estimate the better the performance of the Phase estimator. If we now consider fig 5.1.2.1.e the phase coefficient has been increased to 63/64 and again values of frequency coefficient produce a degradation performance. It must also be remembered that as the phase mean filter coefficient increases, the delay time around the feedback loop also increases and hence the projection increases. This results in any small errors frequency estimate being magnified degrading the and Considering fig performance. 5.1.2.1.f the phase coefficient is now 127/128 and even with a large frequency filter coefficient the degradation is considerable. The conclusions that must be drawn from these simulation results are :-

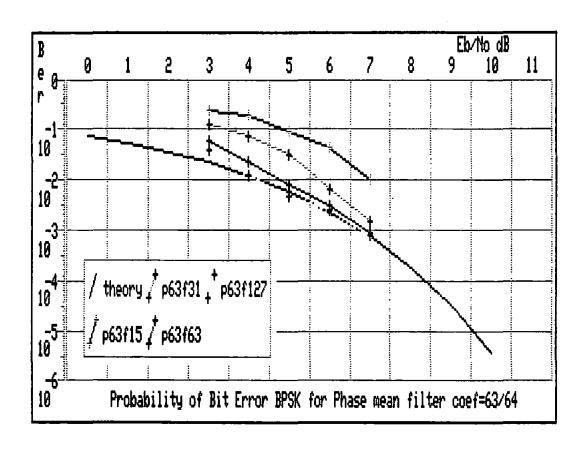
- a) The phase mean filter coefficient must be kept low to reduce the projection time.
- b) The phase mean filter coefficient must not be too low otherwise the noise performance is impaired.

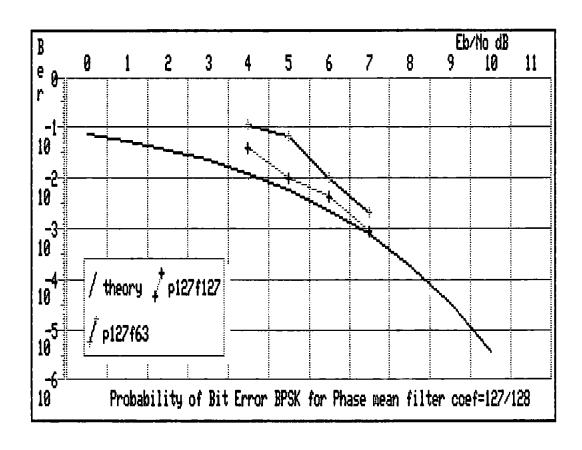
- c) The frequency filter coefficient must be close enough to unity such that an accurate frequency estimate is obtained. When projecting the phase this estimate must not degrade the overall performance. However if the frequency filter coefficient is to unity then the acquisition time of the phase estimator ie. for the frequency the time taken estimate to be valid , increases. It may therefore be necessary to trade acquisition time for estimator performance.
- d) Near unity frequency filter coefficients may also reduce the frequency following ability of any rapid short term frequency variations.

From these conclusions the best choice of phase mean filter coefficient is 15/16 with a frequency filter coefficient of 127/128. This performance can be seen in Fig 5.1.2.1.b.







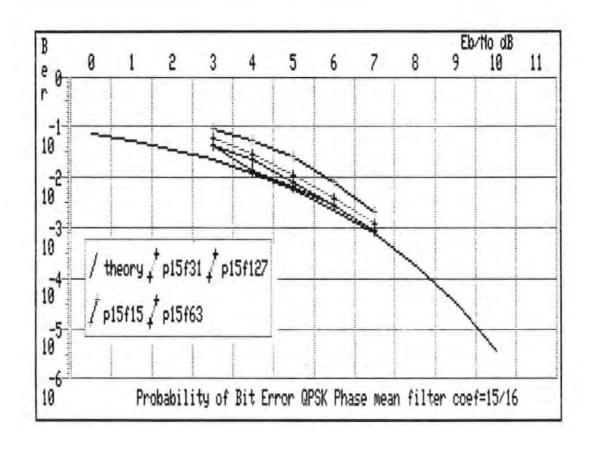


#### 5.1.2.2. QPSK Performance for Varying Coefficients

Initial simulation conditions:-

- i) Type = QPSK
- ii) Symbol rate = 256Ksymbols/sec
- iii) Eb/No 3dB to 7 dB
- iv) Number of filter feedback bits = 16
- v) Frequency offset = 0 Hz

If we consider figures 5.1.2.2.a through to 5.1.2.2.f then it can clearly be seen that the same arguments apply for the QPSK signal as for the BPSK signal. The phase estimator operates from an Eb/No of 3dB's or greater with the optimum performance coming from a small phase mean filter coefficient of 15/16 and a frequency filter coefficient of 127/128.



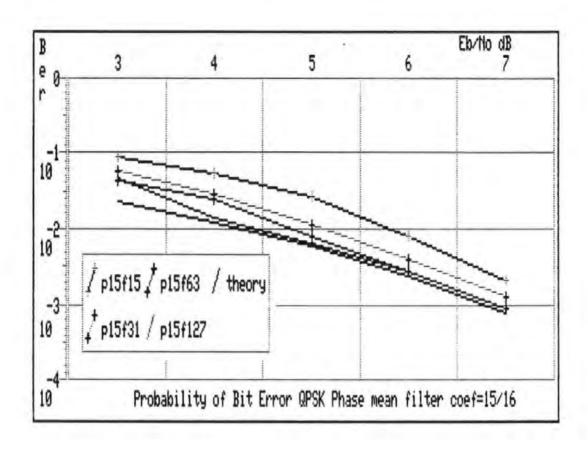
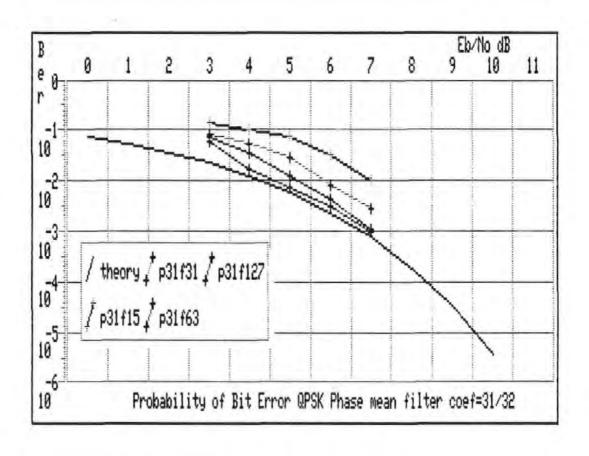
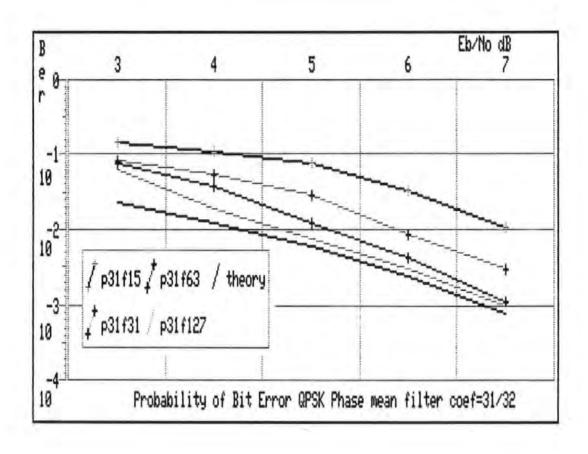
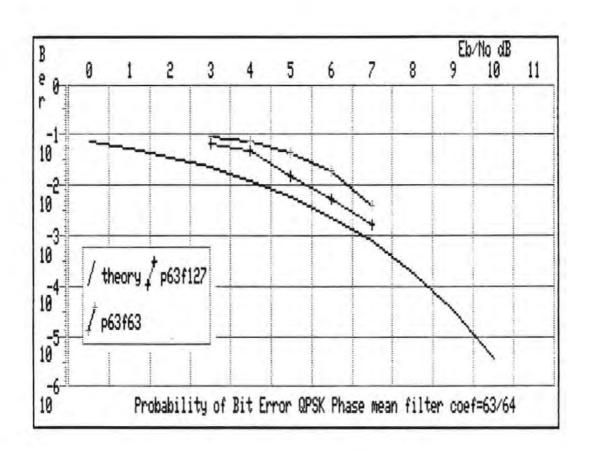
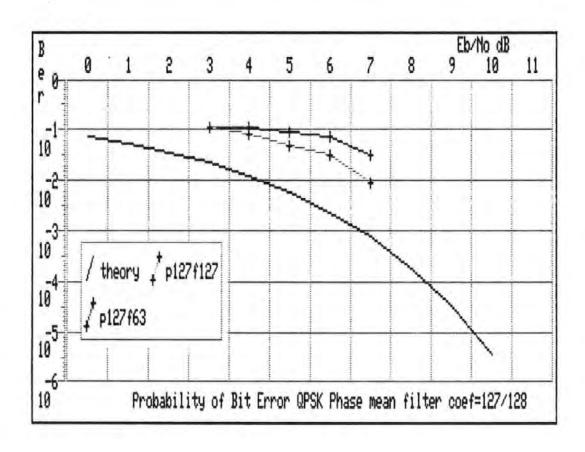


Fig 5.1.2.2.b Simulated QPSK Phase Estimator Performance for  $f_{offset} = 0$  Hz









#### 5.1.3. Performance Against Noise with a Frequency Offset.

Initial simulation conditions:-

- i) Type = BPSK and QPSK
- ii) Symbol rate = 256Ksymbols/sec
- iii) Eb/No 3dB to 7 dB
- iv) Number of filter feedback bits = 16
- v) Frequency offset = 1000 Hz, 2000 Hz, 3000 Hz
- vi) Phase Mean filter coefficient 15/16
- vii) Frequency filter = 127/128

If we consider fig 5.1.3.a the results for simulation performance can be seen. In this figure the 3 Khz performance degradation is minimal even with frequency offset. If we consider the QPSK case as in fiq 5.1.3.b then it can be seen that as the frequency increases then the degradation in performance becomes pronounced. This can be explained by an understanding the data removal process in both the phase mean and To remove the data from frequency estimation algorithms. the rotating phasor the phase is multiplied by 2 mod for BPSK and 4 mod 360 for QPSK. This results in a of the phasor diagram into +/- 90 degrees and degrees respectively. It can easily now be seen that the QPSK format an instantaneous phase change from nominal of only +/- 45 degree would result in an error, whereas for BPSK an instantaneous change of +/- 90 degrees is required. With the change in format the accuracy of the projecting calculation also effects the overall performance as in the estimated phase can be considered to be noise like and hence add to the phase deviation produced by the in a powerwise manner. The effect of the multiplication process is therefore to enhance the overall phase variance of the processed phasor. Hence as the frequency offset becomes greater and the loop becomes more stressed, the probability of this error occurring for a QPSK arises at a higher Eb/No than for a BPSK signal.

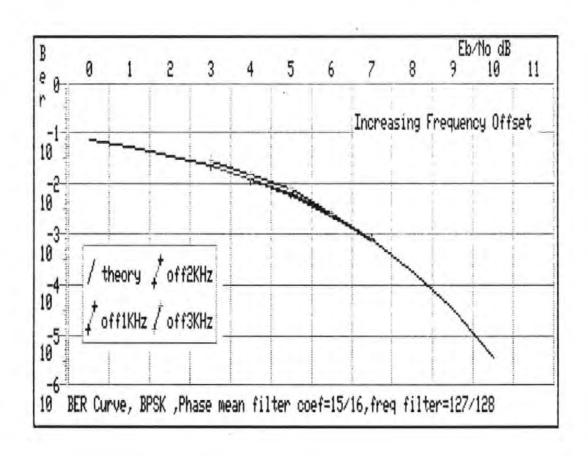


Fig 5.1.3.a Simulated BPSK Phase Estimator Performance for  $f_{offset} = 1000$ , 2000, 3000 Hz

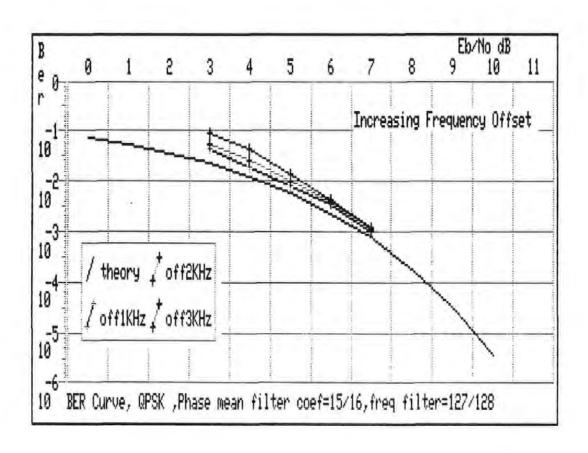


Fig 5.1.3.b Simulated QPSK Phase Estimator Performance for  $f_{offset} = 1000$ , 2000, 3000 Hz

# 5.1.4. Cycle Slip Probability

If we examine the predicted phase value  $\widehat{\Phi}$  (t) obtained from the simulation, for varying values of Eb/no, we can that the rms phase error deviation for the stimulated signal has undergone a signal to noise improvement relation to the received signal. However, a cycle slip will occur if the predicted phase crosses a decision boundary which in the case of QPSK is +/- 45 degrees and +/degrees for BPSK. The received signal incorporates a error deviation produced by the AWG noise  $(\sigma)$  for a Eq4.4.1.b it Es/No. From can be seen that the phase estimate has equal output phase deviation for both BPSK and QPSK for a given set of coefficients and input noise deviation. However since cycle slips occur for an estimator error of greater than 45 degrees in QPSK but 90 degrees BPSK, then for a given input phase deviation, set by input Es/No value, the probability of a cycle slip is for BPSK then for QPSK ie. BPSK operates to a Es/No 3 lower than QPSK before cycle slips will occur. By analysis of the plots produced from the simulation it can be that the bi-variate distribution fits that produced by the the predicted phase. By using the bi-variate distribution simulated by the Phase Noise simulation program ( Noise1-1 ) and the simulated estimated phase sigma value from Estimator simulation program ( Est1-18 ) an evaluation the probability of the phase estimate crossing a decision boundary, the probability of a cycle slip, calculated. A table of AWGN Phase deviation can be seen in Table 5.1.4.a for variation in Eb/No. This is then used evaluation of cycle slip probability for frequency offsets from nominal, which increases the in the loop, and varying Eb/No, the results of which can be seen in Tables 5.1.4.b for BPSK and Table 5.1.4.c for QPSK.

Es/No dB	sigma degrees	prob>45	prob>90
3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19	33.6 29.0 26.0 22.8 19.4 17.0 14.9 13.2 11.7 10.3 9.2 8.2 7.3 6.5 5.7 5.1 4.6	1.50e-1 1.08e-1 7.22e-2 4.44e-2 2.55e-2 1.2e-2 4.96e-3 1.6e-3 3.66e-4 6.34e-5 7.10e-6 2.56e-7 <1e-8 <1e-8 <1e-8	2.30e-2 1.26e-2 6.00e-3 2.29e-3 7.65e-4 1.86e-4 3.45e-5 3.38e-6 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8 <1e-8

 $\frac{\texttt{Table}}{\texttt{Varying}} \, \frac{\texttt{5.1.4.a}}{\texttt{Eb/No.}} \, \frac{\texttt{Phase}}{\texttt{Deviation}} \, \, \frac{\texttt{(1\sigma)}}{\texttt{produced}} \, \, \frac{\texttt{by AWGN}}{\texttt{AWGN}} \, \, \underline{\texttt{at}}$ 

Eb/No dB	F offset KHZ	Estimator Phase dev.	Probability of Cycle Slip/symbol
3 4 5 6 7	3 3 3 3 3	15.3 10.6 8.0 6.2 4.9	3.4e-5 <1e-8 <1e-8 <1e-8 <1e-8
3 4 5 6 7	2 2 2 2 2 2	12.0 9.4 7.4 5.7 4.7	<3.3e-6 <1e-8 <1e-8 <1e-8 <1e-8
3 4 5 6 7	1 1 1 1	9.6 7.6 6.4 5.3 4.6	<1e-8 <1e-8 <1e-8 <1e-8 <1e-8

Table 5.1.4.b Cycle Slip Probability Against Eb/No for BPSK Signals

Eb/No dB	F offset KHZ	Estimator Phase dev.	Probability of Cycle Slip/symbol
3 4 5 6 7	3 3 3 3 3	17.8 13.0 7.3 4.8 3.7	1.2e-2 1.6e-3 <1e-8 <1e-8 <1e-8
3 4 5 6 7	2 2 2 2 2 2	15.0 10.6 6.2 4.6 3.6	4.9e-3 6.3e-5 <1e-8 <1e-8 <1e-8

# $\underline{5.1.5.}$ Quantization $\underline{\text{Effects}}$ $\underline{\text{due}}$ to $\underline{\text{Feedback}}$ $\underline{\text{Bits}}$ in $\underline{\text{the}}$ $\underline{\text{IIR}}$ $\underline{\text{Filters}}$ .

In the Phase mean and Frequency estimate filters the number of Bits used in the feedback path of the IIR filter governs the accuracy of the filter and the minimum residual error that can occur. For example ,consider a IIR filter that is impulsed momentarily. This impulse circulates around the filter, being multiplied by the coefficient and added to the input. Since the input is now zero and the coefficient is less than unity ( to remain stable) the impulse declines at a rate set by the coefficient. Due to the finite number of bits, that are used in the feedback path, a point will be reached where the coefficient multiplied by the Z<sup>-1</sup> value is still equal to the Z<sup>-1</sup> value i.e.:-

$$| v_q z^{-1} | \text{quant} = | k. v_q z^{-1} | \text{quant}$$
 (Eq5.1.5.a)

This results in the output value of the filter not being able to be reduced any further to zero and this is termed the residual error. This also results in a rounding error in the coefficient multiplier output which can be analysed as noise and is often called 'roundoff noise' <8>. We therefore need to ascertain at what level the number of bits in the filter path effect the performance of the system. This was performed for simulation conditions:-

- i) Type = BPSK
- ii) Symbol rate = 256Ksymbols/sec
- iii) Eb/No 3dB to 7 dB
- iv) Number of filter feedback bits = 12,15
- v) Frequency offset = 3000 Hz
- vi) Phase Mean filter coefficient 15/16
- vii) Frequency filter = 127/128

The results of this simulation run can be seen 5.1.5.a. It can clearly be seen that a reduction of bits from 16 bits to 15 bits has a minimal effect of performance, with only a reduction to 12 bit causing degradation of approximately 1 dB at an Eb/No of 3dB's. Since the implementation of anything over 8 bits requires the use of two PROMs to perform the multiplication, 16 bits are readily available for feeding the addition circuit. However to create a lookup table with a 16 bit requires a Eprom size of 64Kbytes per prom. This is now not excessive with currently available PROMs and implemented, but due to lack of space on the original 256Ksymbol/sec modem the number of feedback bits was limited to 12 bits for the frequency filter and 11 bits for the phase mean.

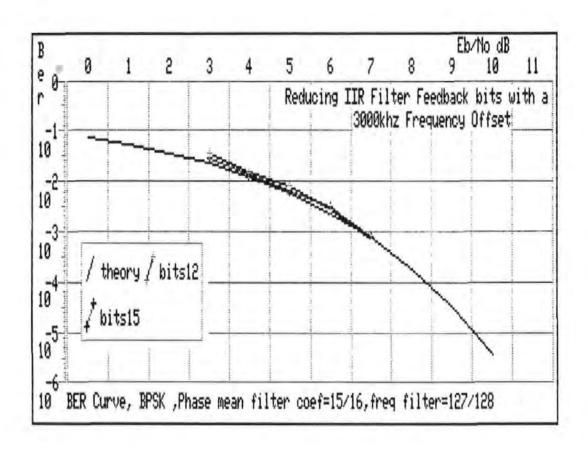


Fig 5.1.5.a Performance Variations due to Feedback Quantization in the Phase Estimator.

## 5.2. Experimental Performance of Modem System

The complete modem can be seen in fig 5.2.a and consists of a 19 inch, 6U Eurocard rack comprising of 11 boards.

#### 5.2.1. Modulator

The hardware configuration for the modulator can be seen in fig 5.2.1.a. This is a single 6U eurocard 220mm in depth. The modulator takes as its input binary data, at levels, and outputs a spectrally shaped quadrature on an IF of 1.024MHz. This is folllowed by an up conversion to 200 MHz where the converted image components are removed by a Surface Acoustic Wave (SAW) filter before converting to a standard IF of 70 MHz. It can therefore be seen modulator can made very compact while be producing the required performance. The spectral and up conversion to the first intermediate frequency are produced by the data stored in the PROM and can hence be easily changed. Firstly, consider the spectral shaping of a raised cosine filter with a signal by a 30% output. By impulsing the modulator with single bits of data it is possible to view the impulse response of the raised cosine filters. This can be seen in fig 5.2.1.b. This is shown for a 256 Ksymbol/sec filter. It can be that the response passes through the zero crossing symbol period intervals. The impulse response lasts for symbol periods with only a very small ripple outside main response. This results in the frequency response seen in fig 5.2.1.c. It can be seen that the 6dB (i.e. half amplitude) occurs at the half symbol rate point, 128 KHz. with the first frequency sidelobe approximately 30dB's down. It is these sidelobes that caused by the truncation of the impulse response to symbols. The data eye that this filter will produce can be seen in fig 5.2.1.d. .

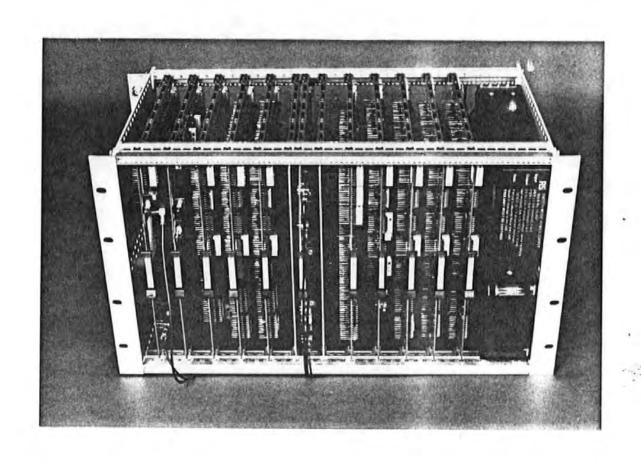


Fig 5.2.a Complete Digital Modem System

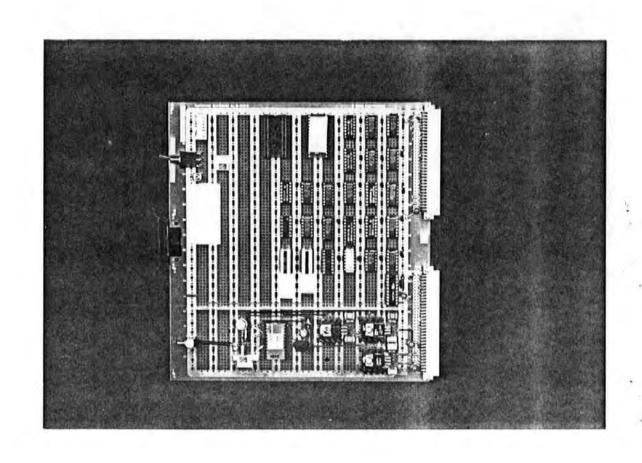


Fig 5.2.1.a Multi-Data Rate Modulator 16 Ksymbol/sec to 256 Ksymbol/sec BPSK and QPSK Formats.

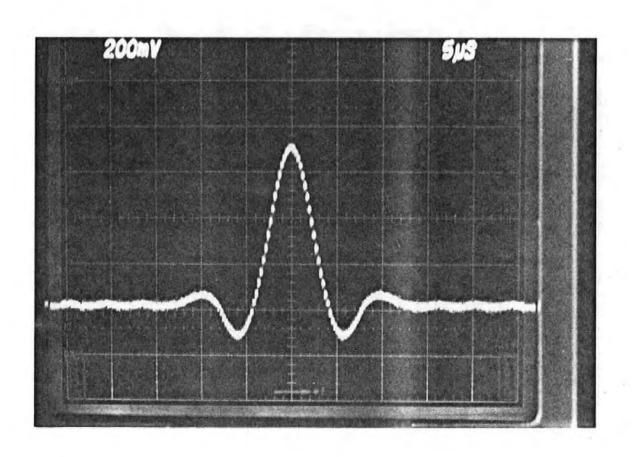


Fig 5.2.1.b 30% Raised Cosine Filter Impulse Response (no Carrier) for 256 Ksymbol/sec Filter.

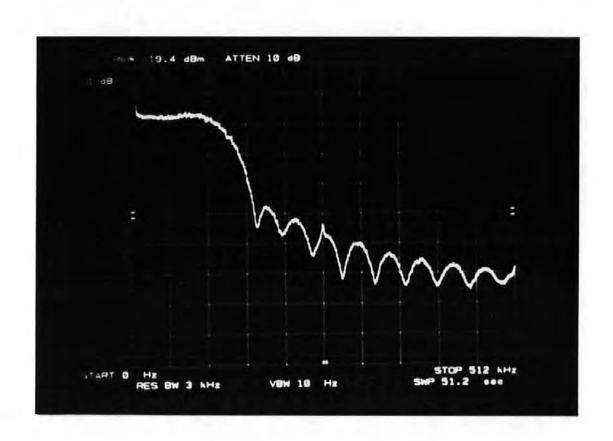


Fig 5.2.1.c 30% Raised Cosine Filter Frequency
Response (no Carrier) for 256 Ksymbol/sec Filter.



Fig 5.2.1.d Data Eye Generated by 256 Ksymbol/sec Data Stream Passing Through a Digital 30% Raised Cosine Filter

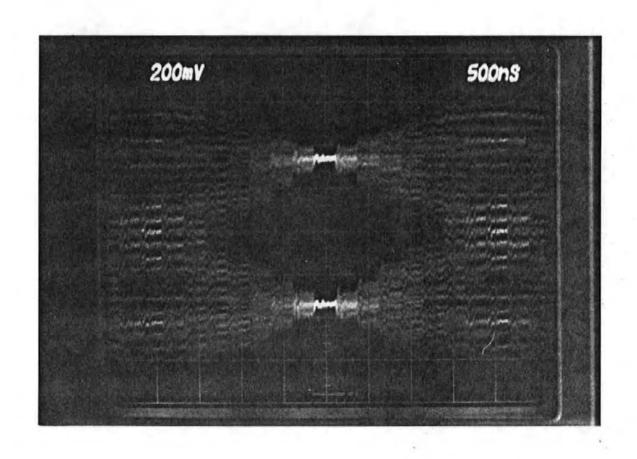


Fig 5.2.1.d Data Eye Generated by 256 Ksymbol/sec Data Stream Passing Through a Digital 30% Raised Cosine Filter

Due to the symmetrical impulse response, with the crossings all occurring at the symbol period rate, the data eye is fully open with all transitions passing through points. To achieve this with an analogue technique would be Now consider the case where the virtually impossible. modulator is producing a root 30% raised cosine response and being modulated onto a 1.024MHz IF. If the modulator is impulsed the result will be a carrier component onto will be modulated the filter impulse response. Hence if observe the output of the modulator we should see a superimposed with a impulse. of reversals Ιn channel format alternate samples, i.e. the quadrature zero component will samples, are hence a zero and observed. This can be seen in fig 5.2.1.e for the response and the data eye in fig 5.2.1.f. The data eye no longer fully open as some transitions do not now through the zero crossing at the symbol periods. since the receiver filters will be matched to this response response then the open eye can be recovered. The spectral for BPSK can be seen in fig 5.2.1.g and this conforms to root 30% raised cosine signal. The frequency sidelobes approximately 30 dB down on the centre frequency with half power point i.e. 3dB now occurring at the half Considering the rate points i.e. <u>+</u> 128 KHz. frequency response for the QPSK signal format the are shown in fig 5.2.1.h,i,j. It can clearly be seen the time response no longer has a zero component since quadrature channel now conveys data. The effect of this an increase of 3 dBs in the spectral response, due to orthoganality of the signals, but with all other spectral features remaining the same. The spectral response can compared to the computer plot in fig 5.2.1.k.

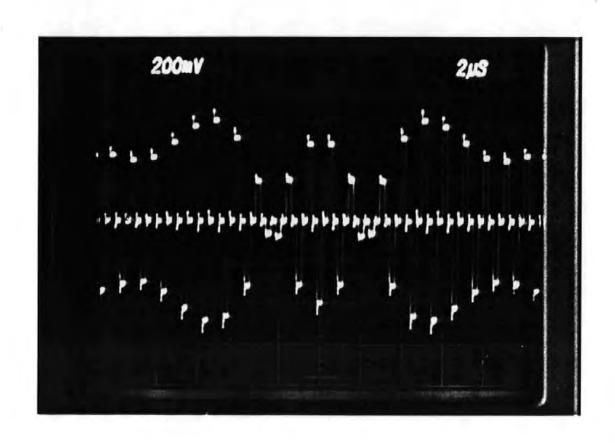


Fig 5.2.1.e BPSK Modulated Root 30% Raised Cosine Filter Impulse Response

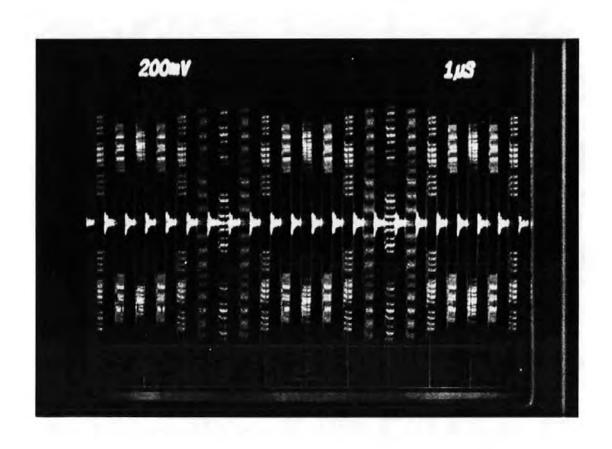


Fig 5.2.1.f Data Eye Generated by BPSK Root 30% Raised Cosine Filter After Modulation

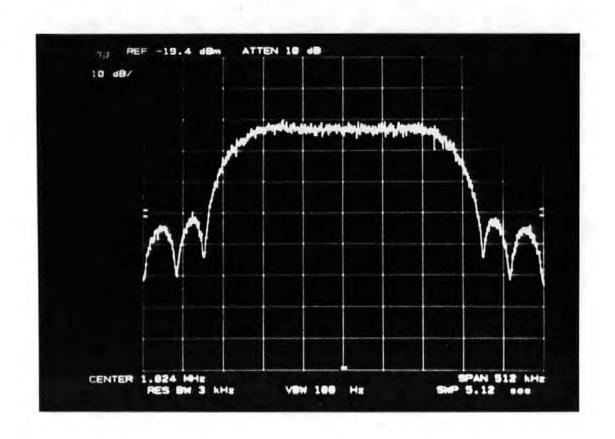


Fig 5.2.1.g BPSK Spectral Response with Root 30% Raised Cosine Filter at 1.024 MHz IF.

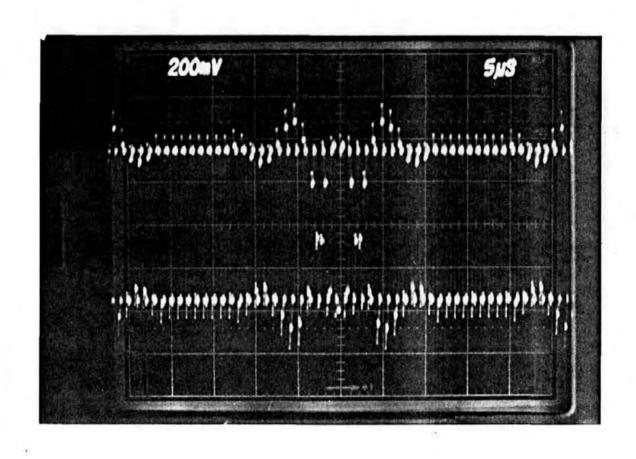


Fig 5.2.1.h QPSK Modulated Root 30% Raised Cosine Filters Impulse Response

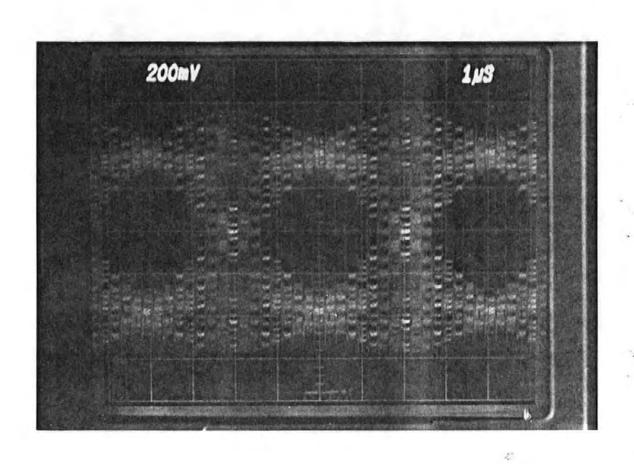


Fig 5.2.1.i Data Eye Generated by QPSK Root 30% Raised Cosine Filters After Modulation

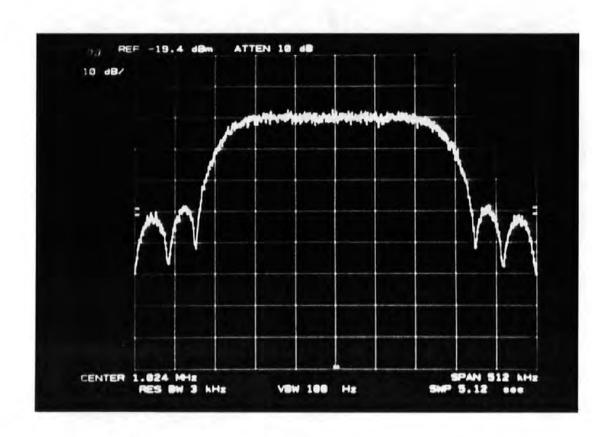


Fig 5.2.1.j QPSK Spectral Response with Root 30% Raised Cosine Filters at 1.024 MHz IF.

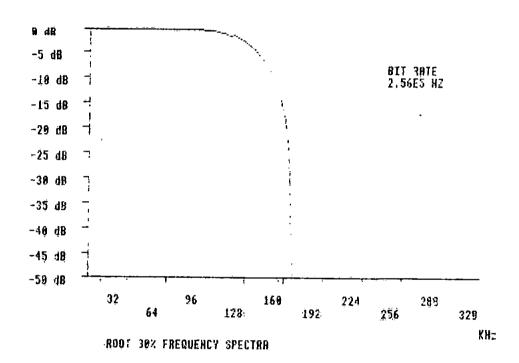
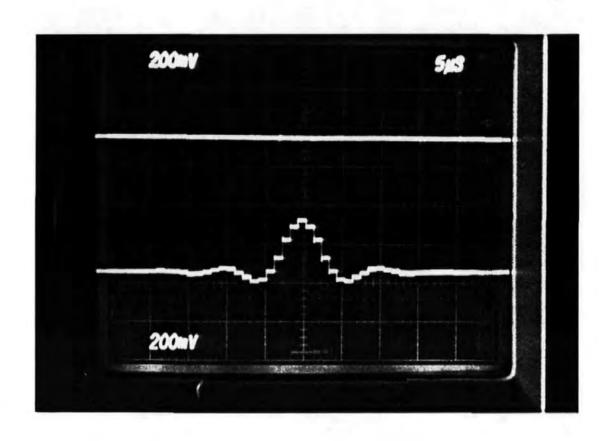


Fig 5.2.1.k Computer Plot of Root 30% Raised Cosine
Filter Frequency Response

## 5.2.2. Demodulator

## 5.2.2.1. Matched Filter Performance

To evaluate the results of the demodulator we will evaluate the performance of the quadrature down conversion 30% and spectral shaping to produce the full roll-off raised cosine filter. This is shown for a 256Ksymbol/sec signal originated by the signalling rate with a root 30% raised cosine on a 1.024MHz IF. This received by the demodulator and is down converted filtered. The Modulator and demodulator clocks are taken as synchronous and no timing recovery is required. The is only passed over the analogue IF interface at 1.024MHz not effected by any analoque such is other components. We will first consider the overall response for an impulse in a single channel. The output the matched filter can be response of seen 5.2.2.1.a. It can be seen that the output sample rate now 4 samples /symbol period and the zero crossings take place at the symbol rate. The Upper trace is the quadrature channel and it can be seen that no quadrature interference occurs. The time response for a BPSK stream can be seen in fig 5.2.2.1.b; it should be that at the centre of the data eye that the eye takes only two major levels with a one quanta variation either side. This would be very difficult to achieve by the use of analogue techniques. The QPSK result can be seen in 5.2.2.1.c. Now considering the frequency domain fiq 5.2.2.1.d it can be seen that the spectral shape of the filter output conforms to that of the 30% raised cosine function when compared to the computer plot with stop band frequency components approximately 40dB down. Α filter board can be seen in fig 5.2.2.1.e. The number filters required per channel is dependent on the rate and hence the system size can be considerable if large range of data rates is required.



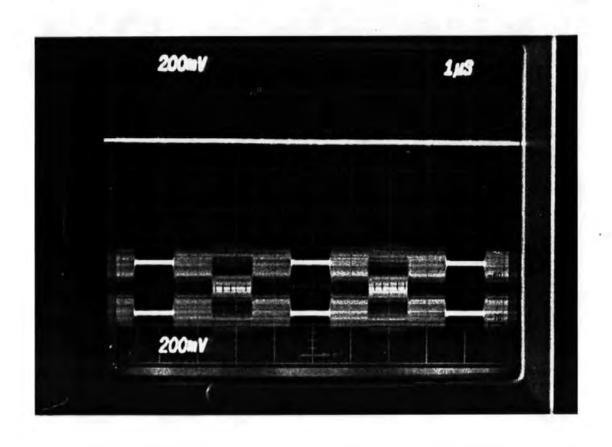


Fig 5.2.2.1.b Matched Filter Output for a Root 30% Raised Cosine Shaped Input BPSK Data Stream

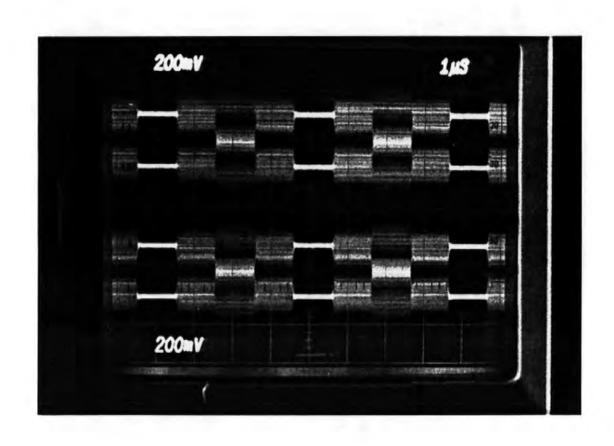


Fig 5.2.2.1.c Matched Filter Output Responses for Root

30% Raised Cosine Shaped QPSK Data Stream Input

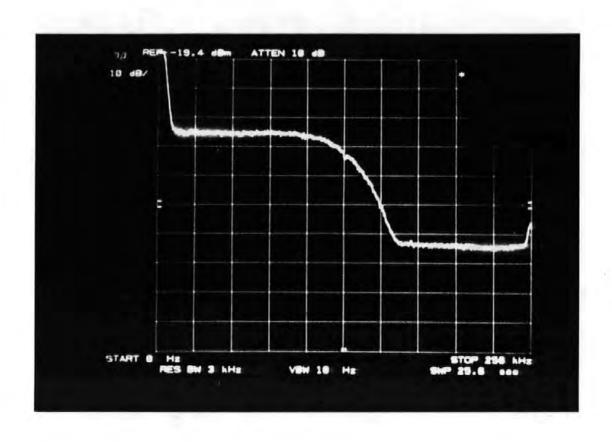
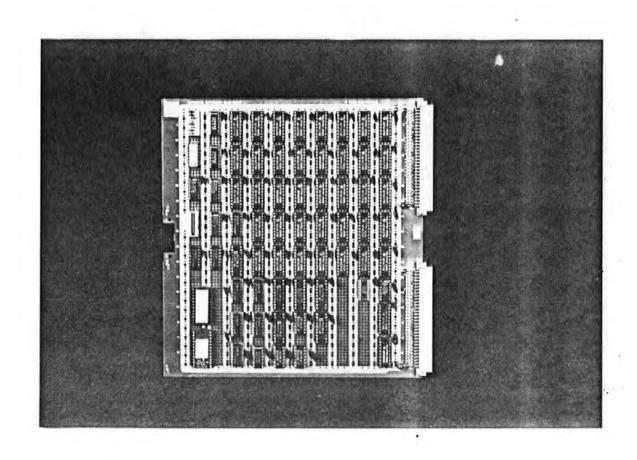


Fig 5.2.2.1.d Matched Filter Output Frequency Spectra
Producing an Overall 30% Raised Cosine Response



 $\underline{\text{Fig}}\ \underline{\text{5.2.2.1.e}}\ \underline{\text{A}}\ \underline{\text{Single}}\ \underline{\text{Digital}}\ \underline{\text{Filter}}\ \underline{\text{Board}}$ 

#### 5.2.2.2. Phase Estimator

The performance of the phase estimator is best considered by an evaluation of the bits error rate of the overall However, by the use of Digital to Analogue converters it is possible to monitor the outputs produced at various points throughout the algorithms. A selection of outputs from the phase estimator circuitry can be seen fig 5.2.2.2 to c. Performance estimations a are very difficult to evaluate in this situation as the performance relies on the variance of the phase estimate and hence the variance would have to be measured to give an performance indication and this could only be achieved off line monitoring and post processing, for which the equipment was not available and hence no attempt is made at this point. Let us consider the output from the  $\Gamma^{-1}(.)$ PROM with a synchronously demodulated signal such that there is no frequency, phase or symbol timing error. BPSK case phase output will be the representing 180 degree phase differences. This can seen in fig 5.2.2.2.a. The slew from one level to is due to the switching time of the Digital to Analogue Converter (DAC) being used for this output. For the signal the output will be four phase levels 90 apart. The analogue representation can be 5.2.2.2.b. However, it can be seen that the 5 levels are This is due to the output being 0,90,180,270,360 axis with 0 and just less than 360 degrees although next to each other on the unit circle are being represented by 00 and FF on the digital output which is the two extremes of the DAC ranges. If a carrier signal of approximately 1.024MHz is fed into the demodulator, with no modulating data, it is possible for the phase estimator lock onto this carrier and display the phase varying output. This can be seen in fig 5.2.2.2.c. the bottom trace being the output from the  $\Gamma^{-1}(.)$  PROM and the upper trace being the phase estimate

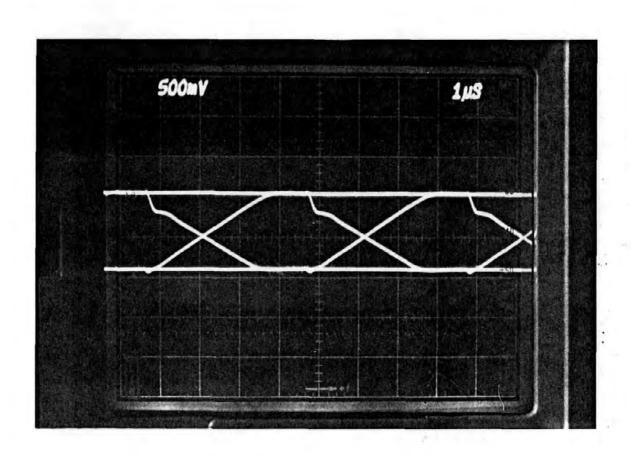


Fig 5.2.2.2 Synchronous BPSK Phase Output from Decode PROM Representing 0,180 Degrees

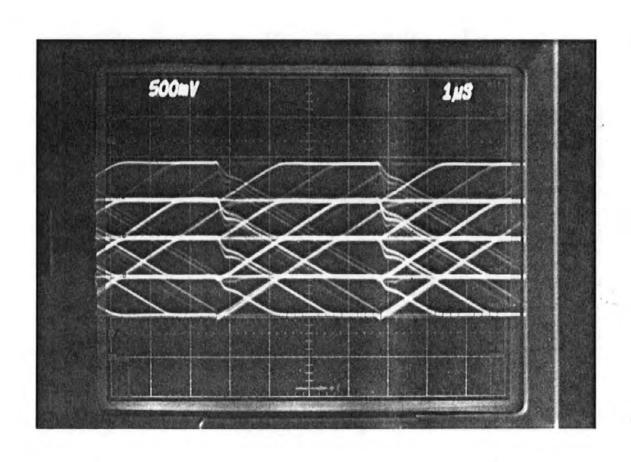


Fig 5.2.2.2.b Synchronous QPSK Phase Output from Decode PROM Representing 0,90,180,-90 Degrees

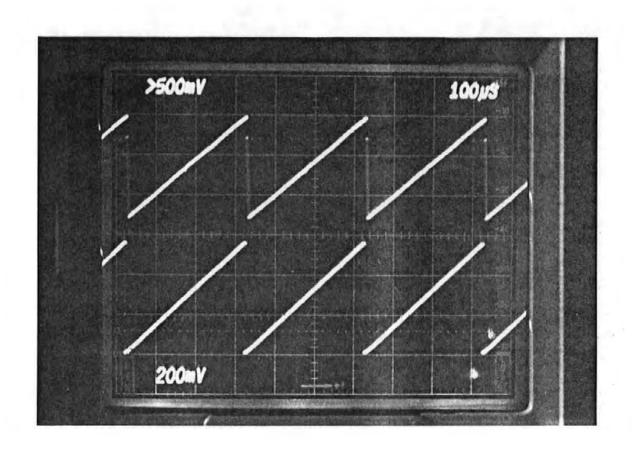


Fig 5.2.2.2.c Phase Estimator (top trace) Locked to a Rotating Phasor Produced by Phase Decoding the Received Carrier Signal by the  $\Gamma^{-1}(.)$  Decode PROM Output

from the phase estimator algorithm. In this case the Phase estimator has locked with zero phase error but this could be at 0, 180 degrees for BPSK or 0, 90, 180, 270, for QPSK. The period of the sawtooth waveform is the time required for the phase to change by 360 degrees and hence the slope of the waveform i.e. the rate of change of phase, is the frequency offset from the effective system 'local oscillator'. The Phase Estimator hardware can be seen in fig 5.2.2.2.d.

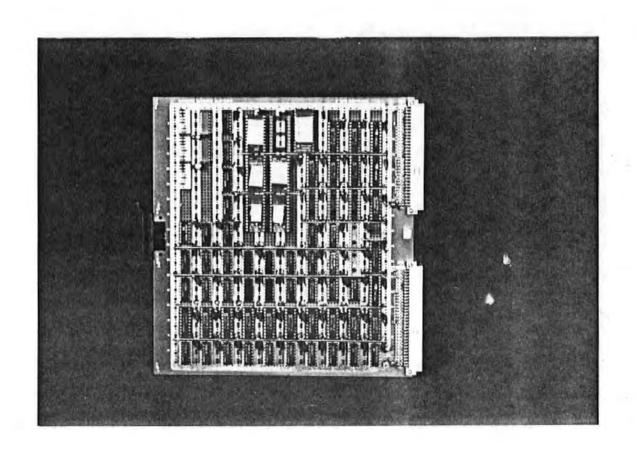


Fig 5.2.2.d Phase Estimator Hardware

#### 5.3 Trials Results

Satellite trials where carried out on the digital modem system on the 22-23 May 1986 at Goonhilly Downs, Cornwall, Uk with the help and collaboration of British Telecomm International. Due to the limitation of the number of in the frequency filter causing performance degradations the test was limited to using only the phase mean estimate. This could only be achieved by keeping the frequency offset from nominal at the digital IF to a minimum. The Test setup fo the signal path can be seen in fig 5.3.a. The satellite used was Intelsat 5A flight 11 at 27.5 degrees West. signal could also be routed via a 'Test Translator' tests when the satellite was unavailable and for more controlled experiments. The signal was provided to the up-conversion equipment at a 70 Mhz IF frequency and obtain from the down conversion equipment at a 70 MHZ IF. to noise ratio was obtained by removing the modulating signal from the transmitter and measuring the carrier power using an HP 8566A spectrum analyser. The noise power was also calculated in a 1 Hz bandwidth by the HP 8566A by away from measuring the noise power the Corroborating measurements where also made by the use of power Meter and a Calibrated Filter. This value of Carrier to Noise in 1Hz was then converted to Eb/No by the Formula:-

Eb/No = C/No - 
$$10\log_{10}$$
 data rate dB (Eq5.3a)

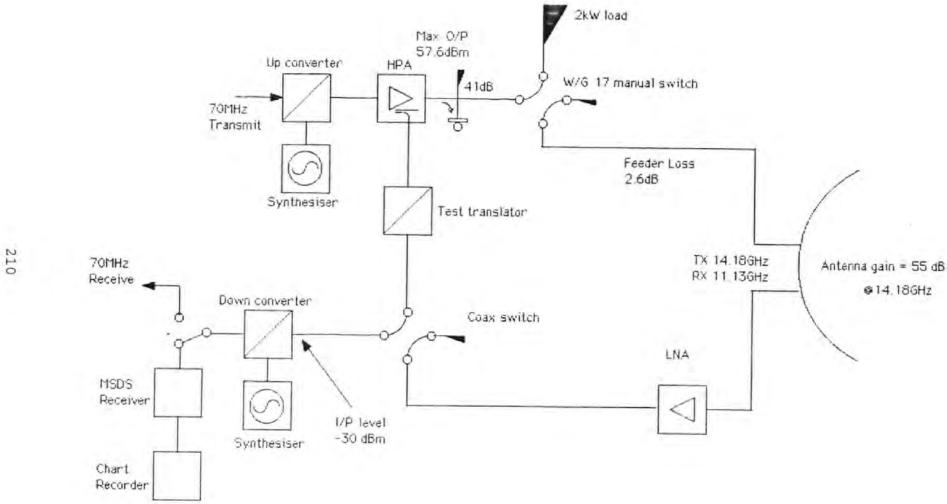


Fig 5.3.a Signal Path Arrangement for Satellite Trials

# 5.3.1 Experiments Carried Out Over a Simulated Satellite Link

To enable the performance of the modem to be evaluated, and not the degradations caused by the satellite or up/down link equipment, tests where performed taking measurements at various stages in the system to ascertain the optimum method for the satellite trials tests. Considering fig 5.3.1.b and c a series of test were performed for BPSK and QPSK using the test translator to simulate the satellite link. Measurements where taken with the system in:-

- i) A back to back mode via the 70 MHz IF interface.
- ii) Back to Back via the Test translator.
- ii) Back to back via the test translator and the HPA at 8dB backoff and 1 dB backoff.

If we first consider BPSK it can be seen in fig 5.3.1.b, that the modem via the 70MHZ interface has a degradation from theoretical of 0.7 dB over the range of Eb/No from 0 dB to 11 dB. This degradation is within the system as the degradation becomes less at low Eb/No. This occurs as system becomes of less significance in relation the received noise and hence the effect of the internal system noise is reduced at low SNR.

Introduction of the test translator results in a further degradation of 0.1 dB ,fig 5.3.1.c and the HPA with 8dB backoff a further 0.2 dB, fig 5.3.1.d. With the HPA at 1 dB backoff the degradation from theoretical is now 1.8dB, fig 5.3.1.e. This is due to the satellite TWT (test Translator) now becoming non-linear and introducing AM-PM and PM-PM products, ie any amplitude modulation present on the signal is converted to phase modulation and any phase modulation is enhanced.

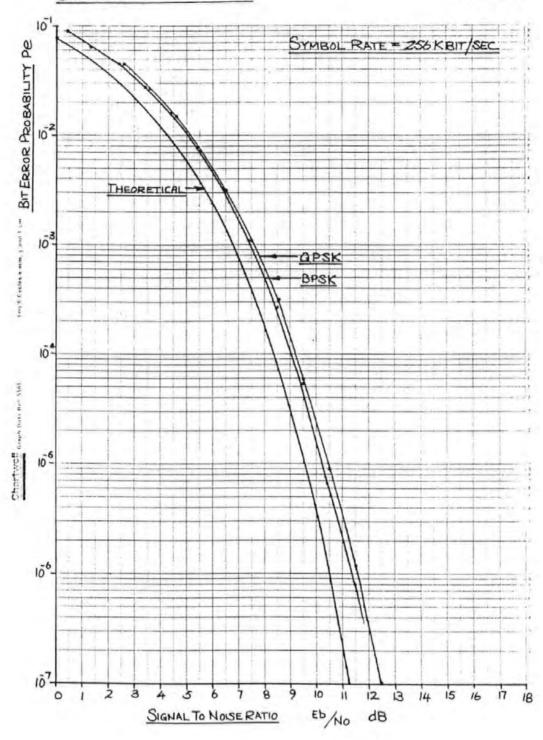


Fig 5.3.1.b 70MHz Interface Loop Back Test Results for BPSK and QPSK at 256 Ksymbol/sec

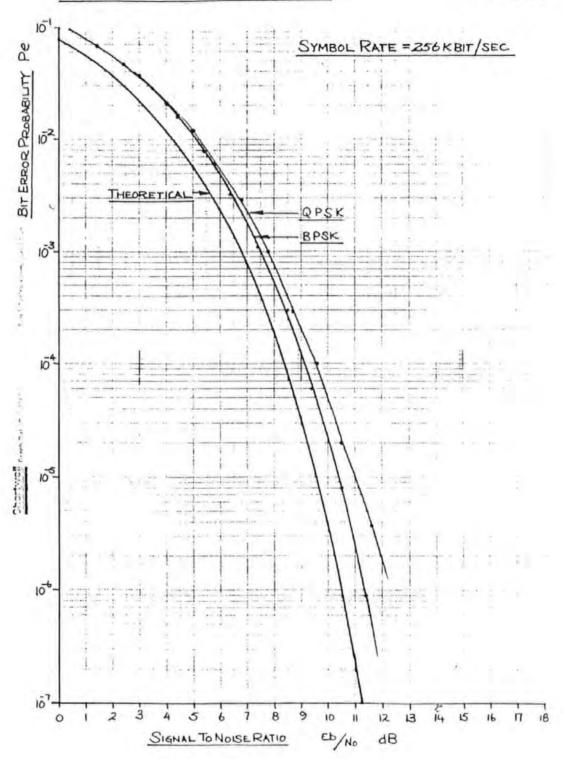


Fig 5.3.1.c Test Results for BPSK and QPSK at 256
Ksymbol/sec via Test Translator at 14GHz

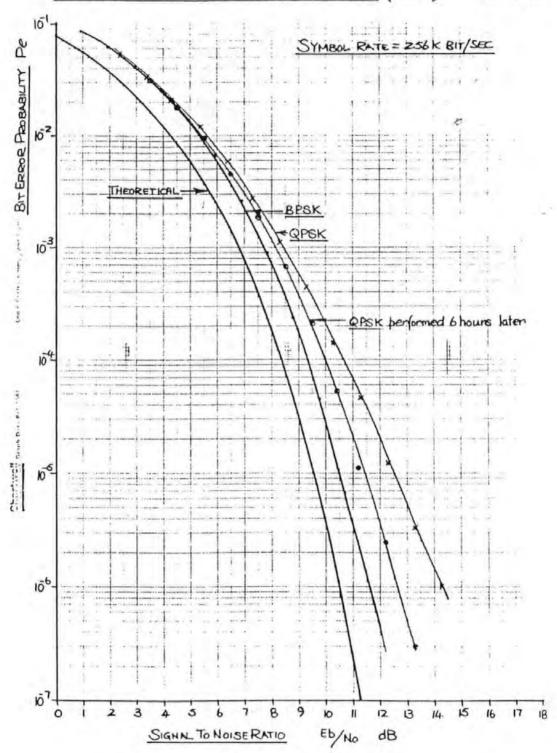


Fig 5.3.1.d Test Results for BPSK and QPSK at 256

Ksymbol/sec via Test Translator at 14GHz and HPA at

-8dB Backoff

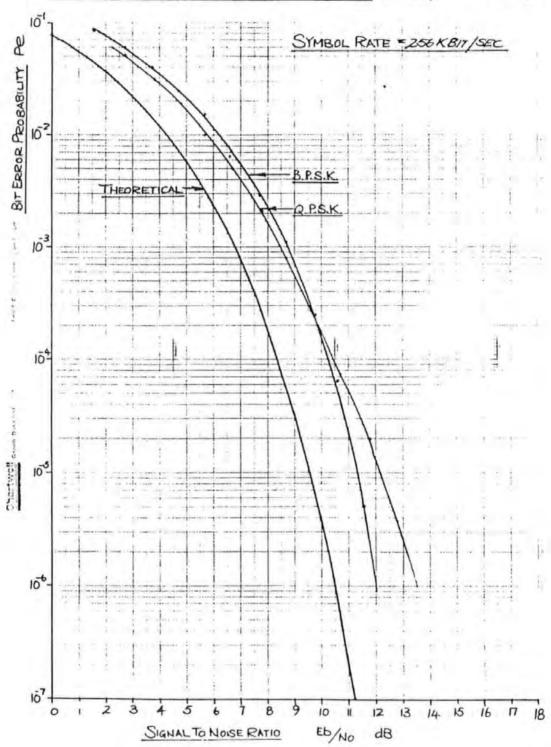


Fig 5.3.1.e Test Results for BPSK and QPSK at 256

Ksymbol/sec via Test Translator at 14GHz and HPA at

-1dB Backoff

is therefore no longer a measure of the performance but is now dependant on the Non-linearity the TWT. This area is therefore to be avoided for modem but this may not be the evaluation tests case operational environment. The results from the QPSK where similar, however the degradation from theoretical now between 0.8dB and 1dB over the range 3 dB to 12dB with greater degradation for the effects of the test translator and the HPA. This increased degradation is due reduced decision boundary which now occurs at +/degrees from the transmitted phase position compared with +/- 90 degrees for BPSK and is hence more susceptible phase noise . This also results in cycle slips occurring at a much higher value than in BPSK and hence the measured Eb/No is 3 dB's greater than for BPSK as discussed previously in section 5.1.4 and confirms the results of the simulation. Considering fig 5.3.1.f and g the relative degradation for each stage in the transmission reception sequence, over a simulated satellite link, can be worst for BPSK and QPSK respectively. The degradation between BPSK and QPSK can be found for the MHz interface, ie the Modem degradation from fig and is 0.2 dB at 11.5 dΒ Eb/No on top of a degradation from theoretical.



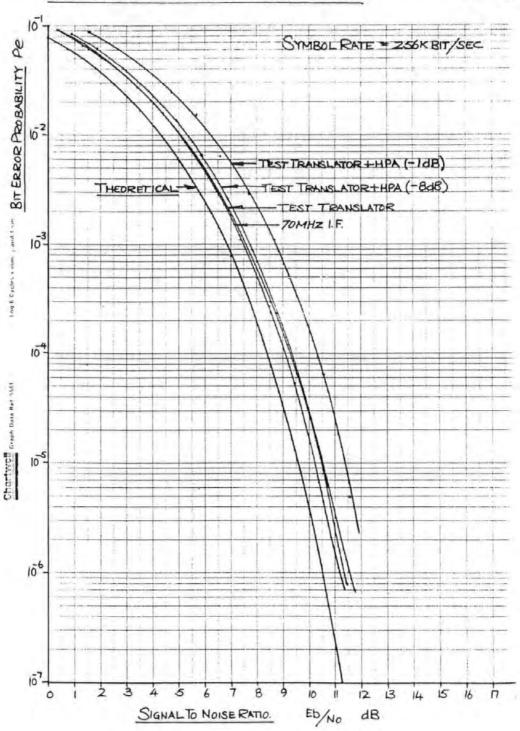


Fig 5.3.1.f BPSK Relative Degradations Throughout the Simulated Satellite Link



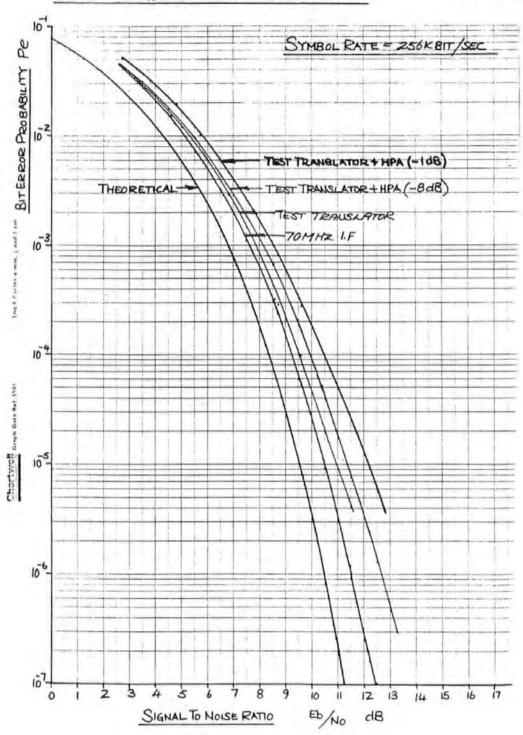


Fig 5.3.1.g QPSK Relative Degradations Throughout the Simulated Satellite Link

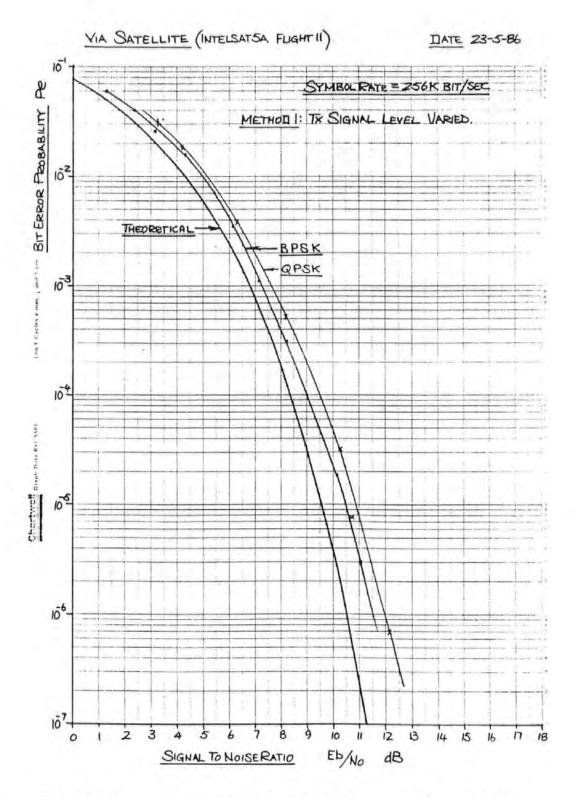
## 5.3.2 Experiments Over an Operational Satellite Link

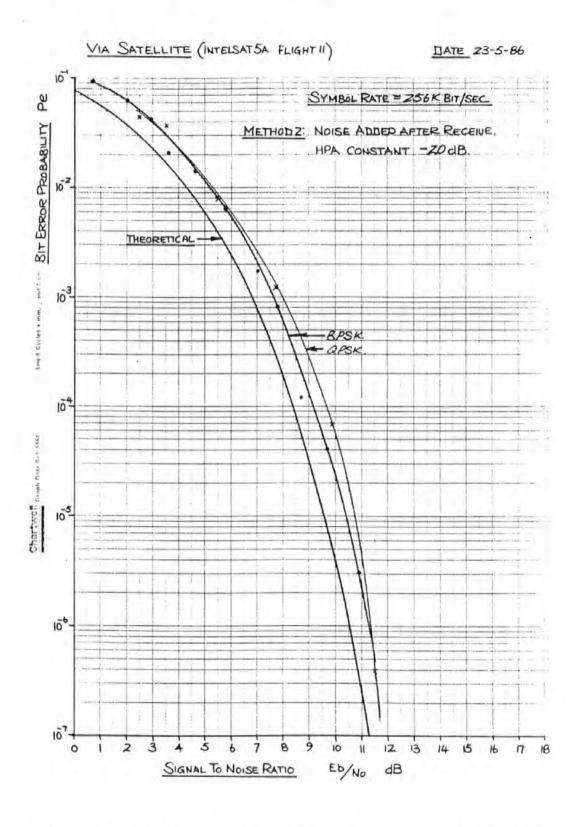
To investigate the effect of noise over a satellite link the signal to noise ratio i.e. Eb/No must be varied. This can be achieved by 2 methods.

- i) Varying the transmitted power level and keeping the satellite system noise floor constant.
- ii) Keeping the the transmitted power constant and increasing the additive noise.

Method 1 has the advantage of simplicity but this relies on the linearity of the satellite HPA and that the HPA does not approach saturation. The results from this method are shown in fig 5.3.2.a for BPSK and QPSK. It can be seen that the degradation from theoretical is no longer as constant as in the test translator results although the degradations has not increased by a great amount in either case.

Method 2 is slightly more difficult than method 1 as required a White Gaussian Noise source to be added to received signal before demodulation. The Noise source provided by BTI and added to the the received signal the use of a passive combiner. The satellite power effects 20 dB backoff to reduce the maintained at saturation. The results for BPSK and QPSK can be seen in fig 5.3.2.b. It can be seen that the BPSK results are similar to those obtained at 70 MHz with а degradation theoretical of 0.8 dB across the same Eb/No range. QPSK result has a sight divergence from theoretical with maximum degradation of 1.2 dB. The degradation is again thought to be phase noise related. Comparisons of the satellite degradation against 70 MHz IF can be seen in 5.3.2.c and d for BPSK and QPSK respectively.







23.5.86

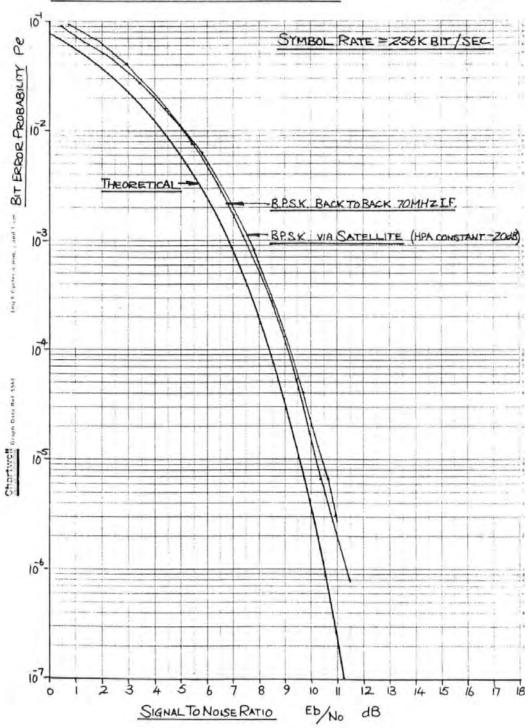


Fig 5.3.2.c Comparison of BPSK BER Curves for the 70 MHz Interface and Via the Satellite Link

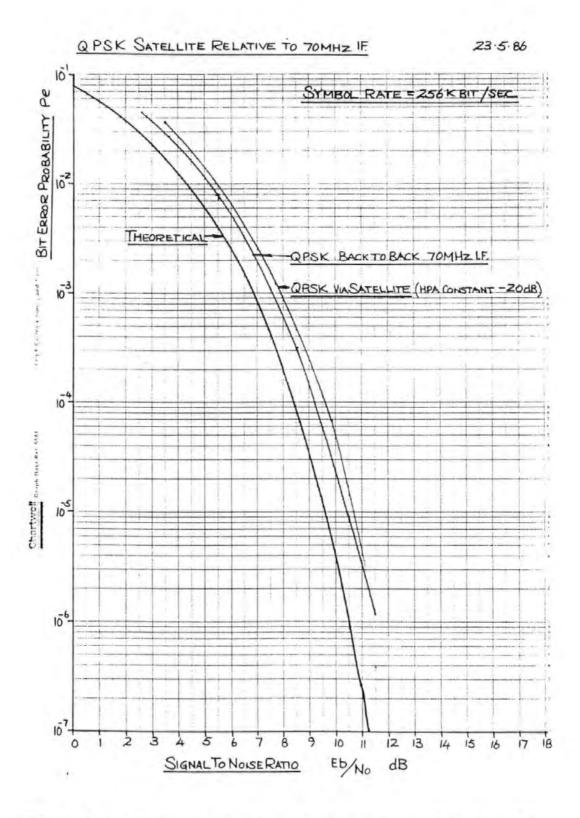


Fig 5.3.2.d Comparison of QPSK BER Curves for the 70

MHz Interface and Via the Satellite Link

## 6. Conclusions

The previous sections have documented the investigation into the possibility of a digital Modulator and Demodulator for any signal that can be modelled using the quadrature model. In section 2 it was suggested that this model be used as the basis for an implementation in hardware and resulted in the design of a Multi-data Phase Shift keying Modem capable of producing a BPSK modulated signal. During this investigation algorithm was hypothesized for the use of a Phase estimator to predict the received signal carrier phase instead phase lock loop system which produced acquisition and stability problems due to the effects time delays used in the digital filters. Phase estimator algorithm was first simulated by the use of an IBM computer with the algorithm implemented ATPascal. The results from this simulation indicated the need for a frequency and Phase correction algorithm and algorithm would operate over a maximum acquisition range at the symbol rate of 256 Ksymbol/sec. Α reduction in symbol rate will also reduce acquisition range on a pro-rata basis. The accuracy of filters used in the algorithm where also accessed with indication that a minimum feed-back path of 15 bits required to implement the filters without any degradation in the algorithm implementation.

It has also been shown that the degradation becomes less when the frequency estimate is averaged over more samples. Acquisition time could therefore be traded against performance since the greater the averaging time the greater the accuracy of the frequency estimate.

The Phase estimator then has a minimum acquisition time of:-

Min acq. time= 1 + 1 
$$\longrightarrow$$
 symbols  $1-K_p$   $1-K_f$ 

where K is the feedback coefficient of the phase filter and the frequency filter.  $\dot{}$ 

The effects of AWGN on cycle slip performance against frequency offset from nominal, for varying Eb/No also suggest that the more stressed the loop becomes due to frequency offset the higher the probability of cycle slip. This is due to the effects of calculating a phase mean estimate of a variable phase and noise component and then projecting this value forward in time to compensate for the frequency offset or rate of Change of Phase per symbol. This projection becomes more prone to error as the frequency offset increases. It is therefore desirable to try to minimise the frequency offset by some other method before phase tracking is used.

The digital implementation of the modem as also been shown to produce filter implementations of a very high accuracy for filter responses that are non causal and hence produce minimal degradation in received data eyes. The filters where implemented as Root 30% Raised Cosine Filters at both the transmitter and receiver to produce an overall channel response of a 30% Raised Cosine Filter. The complete digital implementation was evaluated in trials at British Telecomm International Earth Station Αt Goonhilly, Cornwall, over a satellite link and was shown to have a degradation from theoretical of 0.7dB for BPSK and 0.8 dBs

for QPSK with a cycle slip performance threshold of 0 dB Eb/No for BPSK and 3 dB for QPSK. The results of the simulation and experiments of the digital multi-data rate modem demonstrate that the use of digital techniques in the modulation and demodulation of a signal is possible and that high accuracy and small degradations from theoretical can be achieved. Although the implementation resulted in a large number of circuit boards and components the use of digital signal processing has some major advantages over that of analogue systems.

Firstly the individual logic elements may be combined by the use of Very large Scale Integration (VLSI) to reduce the number and size of logic elements used. This will also reduce the production costs.

Secondly, by using digital implementations once the correct system design is achieved, any reproductions of that system can be produced with the minimum of set up as opposed to analogue circuits which require individually setting up.

Thirdly the multi-data rate system has been designed enable a degree of flexibility to be established when using satellite communication system. The modem be configured to allow for the use of a single data rate or of a series of data rates dependent on power and availability of transponder bandwidth or as a customer desires. This can be achieved by the addition of digital filter boards required but with no other major changes to the system. One anomaly however is that for the lower the data rate required the greater the complexity of the receiver. Fig 6.a shows the complete data modem as configured for 256 Ksymbols/sec.

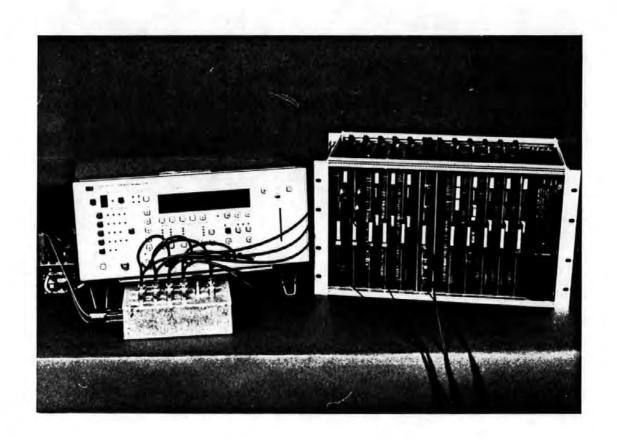


Fig 6.a The Complete Data Modem Configured for 256 Ksymbols/sec.

## 6.1. Further Investigations

As with all new concepts this dissertation has only scratched the surface of a large area for investigation. Although the digital modem system experimentally developed was successful in that it operated close to theory and for low Eb/No values the system design may not have been optimum from a cost point of view. With the Phase estimator the algorithm used was found to be very successful but no attempt has been made to find the optimum algorithm or the optimum hardware solution for this algorithm. However a few suggestions for areas of further investigation into the algorithms design concepts can be discussed.

## 6.1.1. Digital Implementation

The investigation has centred around the development algorithms to implement a Multi-data rate BPSK/QPSK 16Ksymbol/sec to 256 data rates the range in Ksymbols/sec. This range can be extended with present day technology to a symbol rate of 4.096 Msymbols/sec by increase in the parallelism used in the Modulator and the speed demodulator. The limiting factor is in multiplications and additions can be performed. This limited in this design by the access times of the bipolar proms used in the digital demodulator filters. The design uses a serial multiply and addition coefficients. This could be reduced to each prom performing a single multiplication with additions pipelined. result a throughput rate of 33MHz. Another in improvement in throughput rate can be achieved by calculating the sample at the centre of the data eye the final output of the matched filters and hence the throughput rate becomes equal to the symbol rate with the sampling rate equal to four times the symbol rate. This is approaching the state of the art in digital TTL compatible logic at the present time.

## 6.1.2. Phase Estimator

Further investigations can be performed to discover the optimum solution for the phase filter. It is presently implemented as a single pole IIR filter with History modification. Could the filter be implemented as an integrator, or as a FIR filter and would the performance increase warrant any extra complexity required?

The current arrangement of the phase estimator certain amount of feedback in the system design. the usual manifestations of results in acquisition cycle slip. i.e. If the system looses lock due to then the resultant cycle slip and acquisition time are loop bandwidth. dependant on the This can be reduced dependance on the phase filter only by the implementation of a feed forward system as shown in fig 6.1.2.a. In implementation the frequency estimate is used to correct the phase to within the range of the phase estimator before the phase is filtered and subtracted from the phase data signal. This algorithm relies on the use of filters and time delays to match the phase estimator output Another system that could with the received carrier phase. be implemented even with the long time delays multi-data rate filters requires the use of a frequency locked loop so that a frequency estimation signal from the  $\Gamma^{-1}(.)$  PROM after data removal differentiating and fed back to the 'local oscillator' correct for any frequency error. The time constant of be adjusted by changing the coefficient K, to achieve a stable system. This method shown in fig 6.1.2.b. Since the phase estimator is used to follow phase and coherently demodulate the the frequency estimate only has to appear stable such that a phase noise degradation is not superimposed

the incoming signal. Hence the delay around the loop can be much larger than is possible with a Phase locked loop system.

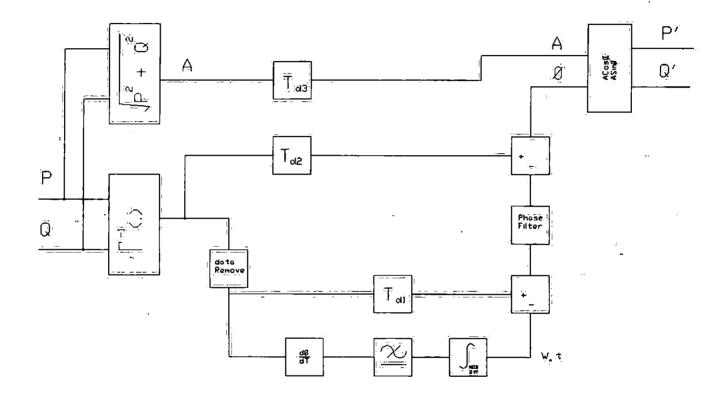


Fig 6.1.2.a Feed Forward Phase Estimator Algorithm

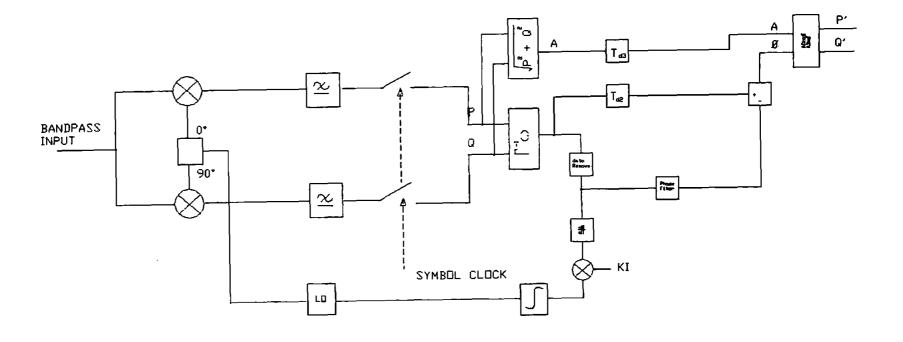


Fig 6.1.2.b Frequency Feedback Loop with Feed-Forward

Phase Processing, an Optimum Solution?

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I would like to thank the following people, who have helped in the research and presentation of this thesis.

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REAL TIME DIGITAL SIGNAL PROCESSING IN SATELLITE MODEMS.

M. Tomlinson and J.R. Bramwell

Department of Communications Engineering, Plymouth Polytechnic.

#### <u>Abstract</u>

This paper contains a brief overview of the ongoing research carried out at Plymouth Polytechnic and Telemetrix PLC, sponsored by the Department of Trade and Industry, sponsored into the use of digital signal processing (DSP) to provide accurate modelling of the channel transmit and receive filters, up and down conversion, carrier and symbol and down conversion, carrier and symbol timing recovery. Due to the digital nature of the modem, changes in configuration can easily be performed by micro-processor resulting in a User friendly Multi-Data rate modem operating over a range of 16kbits/sec to 4.096Mbits/sec. This, coupled with virtually zero ISI and optimal bandwidth shaping filters, produces a high performance system capable of operating close to theoretical predictions.

field of communications has enabled many

#### <u>Introduction.</u> The use of the quadrature model in the

forms of modulation to be developed, one of which is Quadrature Phase Shift Keying, QPSK. By the use of this model it is possible to convey twice as much data over a bandwidth limited channel but at the same symbol rate as Binary Phase Shift Keying. However with the Quadrature model the bandwidth and shape of the modulated signal is determined by the baseband filtering, if any. If Non-Return to Zero (NRZ) pulses are used i.e. no baseband filtering the bandwidth required would be considerable. Bandlimiting these pulses with little care results in the introduction of Inter-Symbol Interference (ISI) and hence a degradation of the Bit Error Rate results. However, Nyquist <1> proposed that ISI could be reduced by the use of a filter that conforms to a skew symmetric transfer function. One such family that conforms to this specification is that of the Raised Cosine function. This enables the 3dB bandwidth to be contained to half the symbol rate frequency fo. Furthermore there will be no spectral components beyond the frequency fo+fx, where fx is a percentage of fo. This results in the specification of a filter as a percentage roll-off factor, where 100% leads to spectral components out to the symbol rate, 2fo, and 0% has no spectral component above fo and is often termed a Brick Wall filter (fig 1). The penalty for this reduction in bandwidth is an increase in oscillatory tails of the impulse response. This results in a need for more accurate symbol timing recovery for zero ISI, and the need non-causal filters. Frequently only 100% Raised Cosine filters are used due to the difficulty in producing symmetrical impulse responses accurately enough to give zero ISI from analogue components. It has been proposed by the authors <7> that DSP can be used to increase performance in modem systems. This paper shows that the use of

DSP in a real time environment is a realistic proposal and can achieve any reasonable form of filter function that may be required to produce close to zero ISI at the receiver while confining the bandwidth. An added advantage of the digital approach is the easy switching of bandwidths enabling a Multi-Data Rate modem to be produced.

The Modulator, A Brief Overview. Consider a previously scrambled, hence pseudo-random data stream being presented to a modulator where by it will be converted into a QPSK signal format and transmitted to up-conversion circuitry on a 1.024MHz First IF carrier. The conventional approach would be as describe by Feher (2),Couch (3),Proakis (4) and many more, with spectral shaping either taking place in the baseband channels or at the carrier frequency using analogue methods. The basic diagram can be seen in fig 2. The incoming data sequence is multiplexed into two data sequence at half the incoming data rate. These two parallel data sequences or NRZ pulses can then be filtered for efficient spectral shaping before modulating onto a carrier in quadrature.

#### <u>Digital Transmit Filters.</u>

The roll-off factor for the overall channes spectrum is chosen to be 0.3 or 30%. This figure is a compromise between channel bandwidth requirements and jitter tolerances on the symbol recovery circuitry giving rise to ISI. Higher roll-off factors i.e. 50%, produce wider bandwidths but a higher jitter can be tolerated before ISI degrades the data eye. It was decided to implement Root 30% Raised Cosine Spectral responses in the both the transmitter and receiver to conform both to Nyquist Criteria and Match Filter criteria as proposed by Lucky, Salz, and Weldon, (\$>. In the transmitter the incoming data pulses are of the NRZ format and hence only ascribe to two values +1 and -1. The convolution process is therefore limited to (6>:

where  $\times$  (iT)= +1 or -1. In a digital system the impulse response of the filter must be truncated to allow for an economical implementation. The consequence of this is an increase in stopband side lobe power and hence a compromise must be reached. In this case the truncation was chosen to be at +/-3 symbol periods and results in a stopband 30 dB down at the 30% point. Hence the convolution can be approximated by:

$$y(kT) = \begin{cases} x & \text{th (nT).x((k-n)T)} \\ x & \text{th (nT).x((k-n)T)} \end{cases}$$

hence only a limited number of coefficient multiplications and additions need to take place, but there is still another saving that can be made. Consider the data sequence not as a series of NRZ pulses but as a series of pseudo-random impulses with output spectrum from any filter is therefore defined by the filter spectrum only and hence its impulse response. The digital filter now consist of the convolution of two impulse responses. can be considered as in fig 3 for a filter impulse response which is only significant over a symbol periods. In the centre of the sequence the tails from all the filter responses converge. For this region of interest it is possible to define the intermediate results for any input sequence of 6 symbols i.e. calculate the convolution results and store them in memory. If the sampling rate of the filter impulse response has been correctly chosen with a 6 symbol input word it is possible to store all combinations of results in a PROM. Due to the symmetry between the two quadrature channels it is also possible to use the same information for both channels, if not the same PROM. If the sample clock is therefore set at 4.096MHz then a 16Kbyte Prom would be required for a 16Ksymbol/sec symbol rate. By the use of extra PROMS or intermediate sampling more data rates could easily be accommodated.

Digital Up-conversion to First IF. Consider a sequence of 4.096MHz samples output from the above digital filter fig 4a and we require a carrier frequency 1.024MHz. The sampled In-Phase carrier waveform can be consider to be as in fig 4b. If these two waveforms are multiplied together the result is as in fig 4c i.e. a 4.096MHz sample stream with alternate samples equal to zero. If we consider another sample stream multiplied by the quadrature carrier to fig 4b the resultant is as in fig 4d and it can be clearly seen that again a 4.096MHz sample stream results with alternate samples equal to zero however for corresponding positions in the In-phase channel when the quadrature channel is zero the In-phase is non-zero and vice versa. The output quadrature carrier IF therefore consists of the In-phase and quadrature channels added together which in this implementation is simply a multiplexing of the two channels. By correct choice of the phase reference between the two channels the carrier can be implemented within the PROM and the complete modulator circuit becomes that of fig 5. For a BPSK signal format the incoming data is only diverted to the In-phase channel and the quadrature channel output is set to zero. The use of other data rates can be accommodated by scaling the clocking frequencies appropriately and hence the IF output frequency.

Multi-rate Digital Demodulator.
From the previous discussions of the modulator it is readily apparent that the demodulator may be based on the same concept i.e. the digital demodulator consist of an input signal on a minimum carrier frequency of 1.024MHz. This is digitally converted to baseband in quadrature and then digitally filtered and sample rate reduced to enable Root 30% raised cosine filters to be implemented practically while covering a span of symbol rate from 16Ksymbols/sec to

256Ksymbols/sec. The output sample rate from these filters is four times the symbol rate. From these four samples per symbol one of the samples must be extracted as the peak sample instant corresponding to zero ISI (when in conjunction with a matched transmitter filter) and the center of the data eye. Carrier phase reference with the IMHz IF must also be achieved to enable data to be decoded from the received Phase and Quadrature samples. To enable both of these processes to occur the symbol timing must be first recovered and then a carrier reference can be established.

Digital Filter Implementation.
The Root 30% Raised Cosine Filter that is required for the receiver must be linear phase to minimize group delay variations and must hence be of a Finite Impulse Response Design (FIR). The format used in the design filters was as shown in fig 6 and can be termed a Direct Form FIR Filter with Serial Addition. The convolution technique relies on the coefficients of multiplication i.e. the desired impulse response being multiplied by the incoming samples, the rate at which this convolution takes place results in the scaling of the frequency response obtained from the filter. It is therefore possible to change the scaling of the frequency response by

changing the processing rate of the filter.

<u>Practical Implementation.</u>
The initial bandlimiting of the received signal to prevent aliasing prior to digitizing, is obtained by the use of a SAW filter for phase linearity, producing minimal group delay variations. The incoming signal, in the range 52-88MHZ, is first up-converted to 200MHz, the frequency being mainly dependent on the availablity and cost of SAW filters and then bandlimited to a 700 KHz bandwidth. The bandlimited signal is then down converted to a 1.024MHz minimum carrier frequency before being digitally sampled. This sampling takes place at a 4.096MHz rate to fulfil sampling theorem requirements and allow synchronization with the symbol clock. In practice it was found that two or three times the carrier frequency did not fulfil requirements as the spectrum will extend to 1.8 MHz with the particular filter used. This sampled signal is then digital mixed to baseband before filtering. This reduces the requirement for closely phase equalized low pass filters before the sampling process can take place. The method used for down-conversion to baseband is obtained by a similar argument as in the modulator. Assume that the incoming signal is on a carrier locked to a quarter of the sampling frequency, down converting with a 'local oscillator' synchronous with the sampling frequency produces alternate zero value samples in the Phase and quadrature baseband channels. This can be modelled by the multiplication of sample pairs by 1.024MHz local oscillator i.e. +1 and -1 which is implemented by complementing samples. Demultiplexing of these samples into the phase and quadrature channels, with addition of a zero value sample in the opposite channel while one channel is being enabled, results in two baseband sample streams. The addition of alternate zero term into a channel when the data sample is diverted into the other channel allows sampling to occur at half

rate than would normally be required for the 4 MHz sample rates per channel. It is necessary to maintain the sample rate in each channel to enable the switching of data rates over the given range and reduces the effect of the sinc function imposed on the frequency spectrum by the rectangular sample pulses.

Multi-Symbol Rate Receive Filter.
Consider the 16Ksymbol/sec case: the incoming sample stream is highly over sampled but cannot be reduced in sample rate due to aliasing constraints imposed by the SAW filter. One alternative is to change SAW filters. This can be very expensive for a large number of symbol rates. Another alternative was proposed and implemented. The digital filters reduce the bandwidth of the 4MHz sample stream such that sample rate reduction can take place.i.e.. Sub-sampling of the output data. This is the approach taken which results in the use of switchable Primary filters. Each one containing the same impulse response coefficients but produce different bandwidth scaling due to the reduced input sample rates and hence processing rate. The lower the data rate the greater the number of primary filters that must be used to reduce the bandwidth to a managable level for pulse shaping. The final filter is designed to equalize the frequency response of the primary filters and provide the final shaping to obtain the overall root 30% Raised Cosine Filter. The symbol rate to allow a recognizable data eye to be monitored.

## <u>Carrier Reference Acquisition and Data</u> Decoding.

Decoding.
The receiver is required to make an optimum decision on the received signal at the centre of the data impulse only and hence as long as the decimation in time keeps the correct samples no degradation occurs. Accurate symbol timing is required and can be obtained from the phase and quadrature channel or from the input carrier IF signal. However this system requires that the sampling at the A/D input must be synchronous with the symbol timing signal and the input carrier frequency if an optimum decision is to be achieved. One method to allow both the symbol timing and the carrier frequency to be synchronized relies on phase locking the carrier with the system clocks synchronized to the symbol timing component. Another method using a digital approach allows the incoming carrier frequency to be close to that of the digital system down-conversion frequency but not locked to it in any form. If the frequency offset is not to great this signal can be processed by the filters to produce minimal degradation the impulse response . If the incoming carrier frequency is not synchronous then quadrature channel interference results. Due to the symmetry of the incoming signal the channel outputs become: -P channel

$$r(t) = P \cdot Cos(\emptyset(nT) - \theta) - Q \cdot Sin(\emptyset(nT) - \theta)$$
(3)

O channel

$$r(t) = P.Sin(\emptyset(nT)-8) + Q.Cos(\emptyset(nT)-8)$$
(4

8 is the initial phase offset of the system clocks with P and O representing channel information. If this symmetry did not exist then the cross channel components would be required to resolve the channel signals. From the final sub-sampled filter outputs the phase and quadrature samples are presented as addresses to the Decode PROM which is pre-programmed to translate them to a phase angle representation by Tan -1 (.) function extended over a full 360 degrees. This output can be viewed as a rotating phasor,  $\theta'(nT) = \theta(nT) - \theta$ , or as a slope representing the rate of change of phase modulo 360 degrees, superimposed with the transmitted data information. From this information it is now possible to remove the data from the phasor and by the use of an Estimator algorithm the rotating phasor position can be estimated for the next incoming phasor plus data sample, fig 7. After subtraction of the phase estimate the data is removed to give an error value. Addition of the phase estimate 0p(nT) to this error value leaves the instantaneous phase offset from the presumed reference phase plus any phase noise. The Phase noise is of a bi-variate Gaussian distribution produced by the effect of the quadrature noise components fig 8. This signal is now filtered to reduce the noise variance on the signal leaving the instantaneous mean phase position. If the rate of change of phase is too great the the mean phase lags the incoming phase due to the delays introduced by the filter. This eventually results in the mean phase output aliasing, not tracking the incoming phase rotation and the system falls out of lock. This can be extended by incorporating into the estimator frequency information that can also be extracted from the Tan-1 PROM projecting the instantaneous mean phase position to compensate for the high rate of change of phase i.e. frequency offset. If the amplitude information of the filter outputs is also extracted it is now possible to remove the rotating phase vector from the data phase information. This converts from a phasor amplitude representation back to a complex representation, and regenerate the correct P and Q channel data information with 0 (nT) = 0,70,180, 270 degrees, the usual 4 phase ambiguity for QPSK. This data is then available for soft decision decoding. A hard decision data symbol can also be extracted from the estimator circuit but due to the 4 phase ambiguity a set of 8 decoding maps are required ( for QPSK) to obtain the correct demodulated data output. The error rate performance of this system has been tested in a back to back mode fig 9, without cycle slipping, over an operating frequency range of 12 KHz. (Cycle slipping is very important for data modems operating with FEC at low Eb/No values). Due to the digital nature of this system bandwidths can be easily adjusted to produce any trade-offs that are required to optimize the system for a particular operating point. Another advantage of this Estimator is that it acquires 'lock' within a very short time period of 32 symbol periods or less depending on the filtering requirements used. This system has been tested by simulation, back to back testing and by satellite trials.

where 0(nT) is the varying phase component

due to the frequency offset of the carrier,

<u>Conclusions</u>
The use of DSP in the satellite Data modem area can be used to improve the accuracy with which filters can be constructed to enable the use of zero ISI filter functions. In addition to the reduction of bandwidth many more advantages and savings can be found in:

1) System setup, lack of filter equalization by hand or machine, once designed accurate reproduction can be simply achieved. 2) The use of VLSI can reduce the

modem costs.

3) Due to the use of Digital quadrature up and down conversion and a synchronous system both quadrature channels can be easily matched and phase quadrature maintained across the passband.

4) The complete system can maintain linear phase.

5) Data rates can be made switchable the range 16kbits/sec to for 256kbits/sec, for both QPSK and BPSK. A version that can operate from 50 bit/sec up to 4.096Mbits/sec QPSK is under development. These versions are being implemented using similar techniques but requires more parallel

processing to take place at the higher rates.

Along with the advantages produced by digital filtering the use of Phase estimation techniques to allow following of any phase reference errors between the carrier and the system local oscillator produces an increase in frequency range over which the system can operate compared with a more conventional approach. This also reduces the acquisition time of the system and is also flexible enough to allow optimum operating conditions to be set . It is envisaged that the modem will be micro-processor controlled to increase user friendliness and provide flexibility. VLSI custom chips will allow manufacturing problems to be eased, and costs reduced.

#### Acknowledgements.

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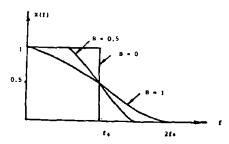


Fig 1 Frequency Response Shaping for Raised Cosine Filters.

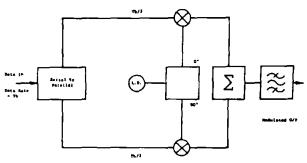
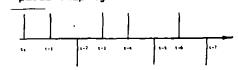


Fig 2 Basic QPSK Modulator for NRZ pulse Shaping



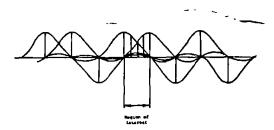


Fig 3 Impulse Response Summation

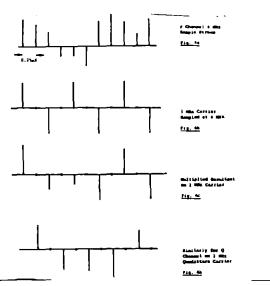


Fig 4 Frequency Conversion of Impulse Stream to Allow Channel Multiplexing

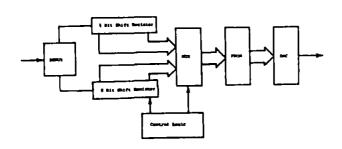
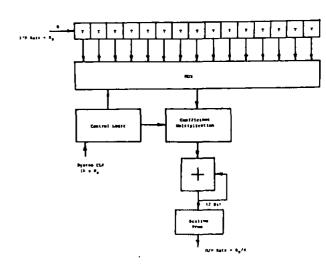


Fig 5 Digital OPSK/BPSK Modulator with Root Raised Cosine Filtering



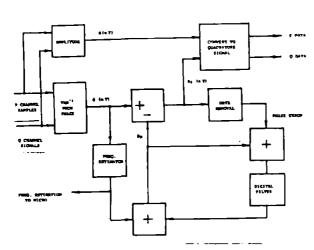


Fig 7 Simplified Phase Estimator
Architecture

Title\* Phise Poise Protability Distribution for 8 d3 (b/Mo at Tah-) Prox Output Size of press ries calculation \* 2.59 degrees

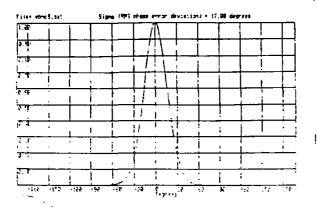


Fig 8 Phase Noise Probability Distribution from Tan-1 Prom

Fig 6 Basic Digital Receive Filter
Architecture

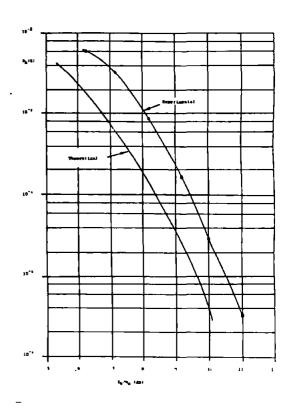


Fig 9 Bit Error rate Curve for BPSK -- at 256Kbit/sec

## Appendix A

Extract from specification of Multi-Data rate Modem produced by the DTI (later to become the British National Space Centre) June 1984.

Electrical

Modulation

BPSK and QPSK (capability for Absolute and Differential Decoding).

Data Rates

32Kbits/sec to 512Kbits/sec QPSK.
16Kbits/sec to 256Kbits/sec BPSK.

Mode of operation

Continuous.

Channel Spacing

1.41 x data rate

Channel Filter Response

The overall transmit and receive filter should be that of a 30% Raised Cosine Filter amplitude equalized for reasonably flat group delay. The Transmit channel filters shall be such as to produce a transmit energy mask as shown in figure A.1: the receive channel filter shall have the characteristics as shown in figure A.2. Group delay per symbol period for the received filter shall be as shown in figure A.3.

Cycle Skipping Performance

When operating at 6.6 dB Eb/No the observed cycle slip rate shall not exceed 1 slip per minute.

Bit Timing Integrity

Bit Error Rate due to clock slip events must be negligible compared to BER due to received noise.

Back to Back Performance

Eb/No for a given BER to be within 1.3 dB of Theoretical assuming perfect Nyquist filtering ( for BER  $10^{-3}$  to  $10^{-10}$ ).

Transmit Frequency

In the Range 52 to 88 MHz.

Receive Frequency

In the Range 52 to 88 MHz

Frequency uncertainty

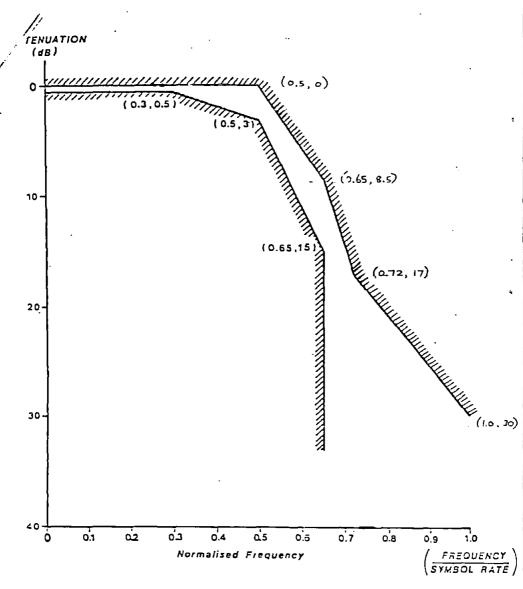
± 25 KHz

Acquisition Time

< 1sec

Lock Acquisition

Must acquire lock for Eb/No >4 dB.



The filter spectrum is symetrical about the centre frequency

Fig A.1 Transmit Filter Mask.

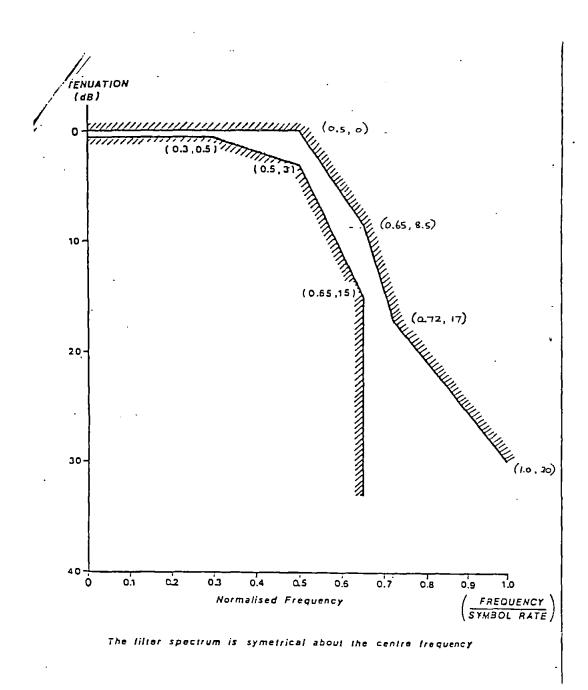


Fig A.2 Received Filter Mask.

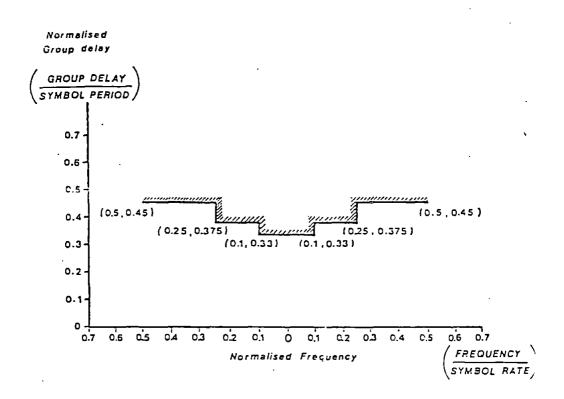


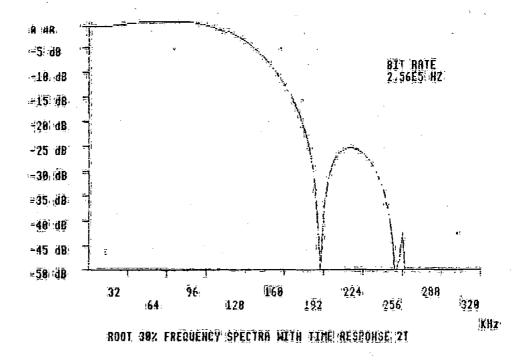
Fig A.3 Received Filter Group Delay per Symbol Period

## Appendix B

The Truncation of Root 30% Raised Cosine Impulse Response and it Effect in the Frequency Domain

design of the Raised Cosine filters factors can be traded to obtain the most elegant and convenient solution. These factors include the choice roll-off factor, truncation for the length response, size of filters required in terms of sections or Proms etc. Careful choice is required. the transmitter the length of example in the response is constrained by the size and access times economics of available Proms. The initial specification called for filters Root 30% raised cosine transmitter and receiver with a 30dB stopband at 1.4 rate hence the final filter arrangement the symbol required number conform to these conditions. For the implemented with a 4.096MHz data rates sampling to be frequency the size of prom required is 16Kbytes. This be economically implemented in 8Kbyte 2764 EPROMs but constrains the impulse response length to 6 symbol periods (double sided), but is this enough to fulfil the specification?

If an analysis is undertaken on a root 30% Raised Cosine impulse response it can be seen in fig B.1 that if the response is reduced to 2 symbol periods (single sided) the the frequency response obtained will have sidelobes to a level of -26dB. If the truncation is 3 symbol periods the sidelobe level is -29dB and if 4 symbol period the level is -32dB. The 3 symbol period truncation was chosen to be close match to the desired response for the research model without incurring the extra cost of the 4 symbol system.



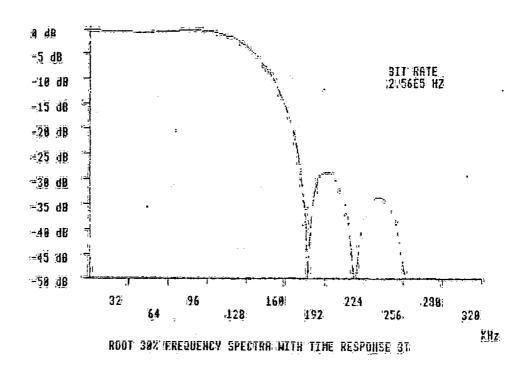
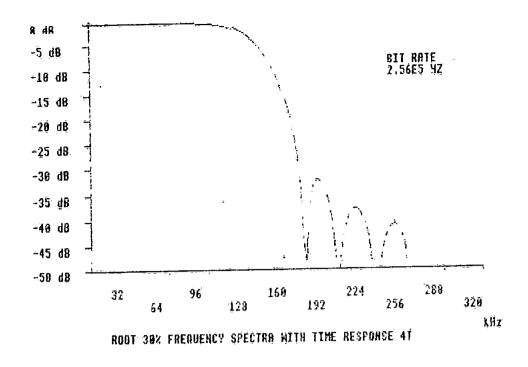


Fig B.1 Variations in Sidelobe Performance due to Impulse Response Truncation.



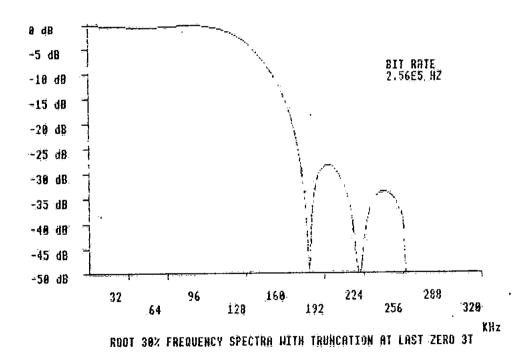


Fig B.1 Variations in Sidelobe Performance due to Impulse Response Truncation.

## Appendix C

# Infinite Impulse Response Single Pole Filter

The single pole filter can be defined by the equation:-

$$v_0 = v_{in} + K.v_0.z^{-1}$$
 (eq C.1)

where  $V_{O}$  = output , $V_{in}$  = input, K= feedback coefficient, Z is the Z transform.

Therefore

$$\frac{V_{o}}{V_{in}} = \frac{1}{1 - K.Z^{-1}}$$
 (eq C.2)

 $now z^{-1} = e^{-jwT}$ 

and eq C.2 becomes

$$\frac{V_{o}}{V_{in}} = \frac{1}{1 - K.Cos wT + jK.Sin wT}$$
(eq C.3)

Hence the magnitude response is given by:-

$$\begin{vmatrix} v_{o} \\ v_{in} \end{vmatrix}^{2} = \frac{1}{1 - 2.K.\cos wT + K^{2}}$$
(eq C.4)

and the phase difference output to input  $\theta_{lag}$  is given by:-

$$\theta_{\text{lag}} = \tan^{-1} \left[ \frac{-\text{ K.Sin wT}}{1-\text{ K.Cos wT}} \right]$$
(eq C.5)

if w << 1/T , wT<<1, Sin wT tends to wT, and Cos wT tends to 1

Therefore

$$\theta_{\text{lag}} = \tan^{-1} \left[ \frac{-\text{K.wT}}{-\text{K.wT}} \right]$$

(eq C.6)

and  $tan^{-1}(.)$  tends to (.)

hence

$$\theta_{\text{lag}}$$
 tends to  $\begin{bmatrix} - \text{K.wT} \\ \hline 1 - \text{K} \end{bmatrix}$  (eq C.7)

now  $\theta_{lag} = w.T_{d}$  where  $T_{d} = Time$  delay through filter and hence approximates to:

$$T_{d} = \begin{bmatrix} -K.T \\ \hline 1-K \end{bmatrix}$$
(eq C.8)

hence for a coefficient of K= 15/16

$$T_d = -15.T$$

## Appendix D

This appendix contains program listings for the programs used in the phase estimator simulation. The programs were written in Pascal and were compiled using The Propero Pascal Compiler.

## Program 1 Phase Deviation Due to AWGN

This program generates quadrature noise components for a normalised sigma deviation. The resulting noise PDF is of a bi-variate distribution and is stored as a Histogram with a selected phase cell width. The resulting histogram can be used to calculate the probability of a particular phase error due to AWGN occuring and hence the error function integrations. The following pages contain the program listing for Noise1-1.pas with appropriate comments. Due to the naming conventions used, whereby a meaningfull name is used for a function or procedure, the use of flow charts and line by line commenting is considered superfluous.

#### NOISE1-1.pas

phase\_noise\_statistics(input,output);
{ calculate statistical distribution and probabilities of
phase errors}

```
real=longreal;
                     choice=0..5;
               var ebno,noisestep,stepsize:real;
                   quit:string;
function antilog(x:real):real;
{calculates 10<sup>X</sup>}
begin
    antilog:= exp(x*2.302585093); \{ 2.3025= ln 10 \}
end;
function prob(x,propc:real):real;
{gaussian probability of x, scale for unit area by propc}
         var y:real;
begin
     y:=-1*sqr(x)/2; \{sigmasquared=1\}
     prob:=propc*exp(y)/sqrt(2*pi);
end;
procedure quitread(var quit:string);
[sets quit to yes to leave menu area]
begin
      quit:='yes'
end;
procedure proportionalConstant(var propc, stepsize,
                                     noisestep:real);
{calculates constant such that area under calculated curve = 1}
             var x,prob,y,sum:real;
                  n,i:integer;
```

```
begin
     n:=round(5/noisestep);
     sum:=0;
     for i:=-n to n do
       begin
           x:=i*noisestep;
           y:=(-1*sqr(x))/2; {sigmasquared =1}
           prob:= exp(y)/sqrt(2*pi);
           sum:=prob+sum;
       end;
     propc:= 1/sum;
     writeln('propc =',propc);
end;
procedure EboverNo(var rmsEbNo,ebno:real);
{ requests Eb/No ratio in dBs and converts to rms}
          var x:real;
begin
     x := ebno/10;
     x := antilog(x);
     x:=x*2;{ split into inphase and quadrature components
                                               keeping No =1}
     rmsEbNo:=sqrt(x);
end;
procedure clearhist(var thetahist:historarray;
                    var cellcount:intarray);
{clears historgram memory area ready for start of calculation}
         var h:integer;
```

```
begin
     for h:=-maxloc to maxloc do
      begin
       thetahist[h]:=0;
       cellcount[h]:=0;
      end;
end;
procedure add_to hist(etheta:longreal;probtheta:longreal;
                      stepsize:real;var thetahist:historarray;
                      var cellcount:intarray;
                      var listends:integer);
 {calculates historgram for radian stepsize of probability of
phase deviation}
         var number:integer;
             newprob, oldprob: longreal;
begin
     number:= round(etheta/stepsize);
     cellcount[number]:=cellcount[number]+1;
                             {increment cell count of cell number
     oldprob:= thetahist[number];
     newprob: = oldprob+probtheta;
     thetahist[number]:=newprob;
     if abs(number)>listends then listends:=number;
end;
procedure thetaerror(var thetahist:historarray;
                     var cellcount:intarray; rmsEbNo,propc,
                     stepsize, noisestep: real;
                     var listends:integer);
{calculate array of noise samples for all values of
                                                       noise
variations }
```

```
var n,i,j,location:integer;
                xi,xj,piby2,pmag,qmag,quadshift,
                probsum,probtheta:real;
                etheta:longreal;
begin
     n:= round(sqr(2*(5/noisestep)+1));
     writeln( 'Calculating ',n:7,' noise samples');
     piby2:=pi/2;
      n:=round(5/noisestep);
      probsum:=0;
      location:=0;
      for i:=-n to n do
       begin
          xi:= i*noisestep;
          for j:= -n to n do
           begin
            xj:=j*noisestep;
                 pmag:=rmsEbNo+ xi;
                 qmaq:= xj;
                 if pmag<>0 then
                 begin
                  etheta: =arctan(gmag/pmag);
                  if (pmag<0) and (qmag>0) then
                     etheta:=pi+etheta;
                  if (pmag<0) and (qmag=0) then etheta:=pi;
                  if (pmag<0) and (qmag<0) then
                  etheta:=-pi+etheta;
                 end
                 else
                  begin
                   if qmag=0 then etheta:=0;
                   if qmag>0 then etheta:=piby2;
                   if qmag<0 then etheta:= -piby2;
                  end;
```

```
probtheta:= prob(i*noisestep,propc)
                        * prob(j*noisestep,propc);
            add to hist(etheta, probtheta, stepsize,
                        thetahist, cellcount, listends);
            probsum:=probsum+probtheta;
            location:=location+1;
          end;
      end;
      writeln('probsum= ',probsum:10:5);
      listends:=listends-1;
end;
procedure averagephasevariance(thetahist:historarray;
                            listends:integer;
                            var sigma:real;stepsize:real);
{ calculates
                                                          of
              average phase variance
                                             from
                                                    sum
p(i)*error^2}
          var h:integer;
              etheta:real;
              sum:longreal;
begin
     sum:=0:
     for h:= -listends to listends do
       begin
         etheta:= h*stepsize;
         sum:= thetahist[h]*sqr(etheta)+sum;
       end;
     sigma:= sqrt(sum)*180/pi;
     writeln('RMS phase deviation = ',sigma:10:6,'
              degrees'); end;
procedure savedisc(thetahist:historarray;
                   cellcount:intarray;
                   listends:integer;
```

```
sigma, stepsize: real);
{ write data to disc as a text file}
       label 10;
       var outfile1:text;
           h:integer;
           sum:real;
           name:string;
begin
    writeln('entered save to disc');
     sum:=0:
  10:writeln('Name of file ( max 8 characters.dat)');
     readln(name);
     if length(name)>12 then goto 10;
     stepsize:=stepsize*180/pi;{convert to degrees}
     assign(outfile1, name);
     rewrite(outfile1);
     writeln(outfile1, listends, stepsize, sigma);
     for h:= -listends to listends do
       begin
       sum:=sum+thetahist[h];
         writeln(outfile1,thetahist[h]);
       end;
       writeln('Sum of Probabilities under curve = ',
               sum:6:4);
end;
procedure write_to_disc(thetahist:historarray;
                         cellcount:intarray;
                         listends:integer;
                         sigma,stepsize:real);
{ question of writing to disc statistical phasenoise data}
```

```
label 10,20;
        var ch:char;
begin
     10 : writeln('Save phase statistics to disc? (y/n) ');
          readln(ch);
          case ch of
           ''y':savedisc(thetahist,cellcount,listends,
                         sigma, stepsize);
            'Y':savedisc(thetahist,cellcount,listends,
                         sigma,stepsize);
            'n':goto 20;
            'N':goto 20;
            otherwise goto 10;
          end:
20:end;
procedure erfc(listends:integer;stepsize:real;
               thetahist: historarray);
{produces complimentary error function i.e probability of
error being greater than x}
         var h:integer;
             sum,etheta,x,xdeg:real;
begin
     stepsize:=stepsize*pi/180;[converts to rads]
     writeln('Enter prob(phase error >x degrees)');
     readln(xdeg);
     x:=xdeq*pi/180;
     sum:=0;{calculates complimentary errror function}
     for h:= -listends to listends do
      begin
       etheta:= h*stepsize;
       if abs(etheta)>=x then sum:= sum+thetahist[h];
```

```
{probability of etheta>x radians}
      end;
      writeln('probability of phase error >',xdeg:4:2,'
               degs = ',sum:15:12);
end;
procedure setnoisepower(var ebno:real);
begin
     write('Noise power required in dB ');
     readln(ebno);
end;
procedure setnoisestep(var noisestep:real);
         label 10;
begin
10: write('Noisestep size required (include leading zeros)
           in sigma ');
    readln(noisestep);
    if (noisestep<0) or (noisestep>5) then goto 10;
end;
procedure sethiststep(var stepsize:real);
          label 10;
begin
     write('Cell width stepsize in degrees (min =0.5 deg )
           ?');
    readln(stepsize);
    if stepsize<0.5 then goto 10;
    if stepsize>10 then
      writeln('Stepsize too large for accuracy');
end;
```

```
procedure computenoisestat(ebno,noisesteps,stepsize:real;
                            var listends:integer;
                                    thetahist:historarray);
                            var
{calculates Phase noise statistics in this procedure}
               var x,propc,sigma,probability,rmsEbNo:real;
                   h,n:integer;
                   cellcount:intarray;
begin
     stepsize:= stepsize*pi/180;{ converts to radians}
     proportionalConstant(propc, stepsize, noisestep);
     EboverNo(rmsEbNo,ebno);
     clearhist(thetahist,cellcount);
     thetaerror(thetahist,cellcount,rmsEbNo,propc,stepsize,
                noisestep, listends);
     averagephasevariance(thetahist, listends, sigma,
                          stepsize);
     write to disc(thetahist,cellcount,listends,sigma,
                          stepsize);
end;
procedure computegaussian(ebno,stepsize:real;
                            var listends:integer;
                                     thetahist:historarray);
{Caluculates Gaussian historgram in this procedure}
     label 10,20,30;
     var scale, sum, y, sigma,
         rmsEbNo, maxangle, etheta: real;
         h:integer;
```

```
ch:char;
         cellcount:intarray;{dummy}
begin
     sum:=1;
     clearhist(thetahist,cellcount);
    Eboverno(rmsEbNo, ebno);
     write('Enter value of sigma in degrees for which plot
           required ? ');
     readln(sigma); 30: write('Comparison plot ? (y/n) ');
     readln(ch);
     case ch of
     'y': goto 20;
     'Y': goto 20;
     'N':goto 10;
     'n':goto 10;
     otherwise goto 30;
     end;
10: write('Enter max phase angle to which plot is required
          ?');
    readln(maxangle);
    listends:=round(maxangle/stepsize);
20: scale:=1/sum;
    sum:=0;
    for h:=-listends to listends do
     begin
         etheta:=h*stepsize/sigma;
         y:=(-1*sgr(etheta))/2;
         thetahist[h]:=scale* 0.3989422*exp(y);
         sum:=sum+thetahist[h];
     end;
     if (sum>1.01) or (sum<0.99) then goto 20;
     write to disc(thetahist,cellcount,listends,sigma,
                   stepsize);
end;
procedure plot;
```

```
{calls Plot program }
begin
    chain('plotstat');
end;
procedure menu(var ebno,noisestep,stepsize:real;
              var quit:string);
{sets up menu for desired set of statistics}
  label 10,20;
  var value:choice;
      listends:integer;
      thetahist:historarray;
begin
   listends:=0;
10: writeln;
   writeln('**********************************);
   writeln('
                    PHASE NOISE PROBABILITY
   writeln('
                       version ',vers:6:2);
   writeln;
   writeln('1) Noise power is ',EbNo:6:1 ,' dB');
   writeln;
   writeln('2) Noise stepsize is ',noisestep:6:3,
             ' Sigma');
   writeln;
   writeln('3) Historgram cell width ', stepsize:6:3,
            'Degrees');
   writeln;
   writeln('4) Compute Phase noise statistics');
   writeln;
   writeln('5) Compute Gaussian Distribution');
```

```
writeln;
   writeln('6) Call Plot Program');
   writeln;
   writeln('7) Calculate ERFC ');
   writeln;
   writeln('0) End');
   writeln;
   write('ENTER ');
   readln(value);
   case value of
   0: quitread(quit);
   1: setnoisepower(ebno);
   2: setnoisestep(noisestep);
    3: sethiststep(stepsize);
    4: computenoisestat(ebno, noisestep, stepsize, listends,
                        thetahist);
    5: computegaussian(ebno,stepsize,listends,thetahist);
    6: plot;
    7: erfc(listends,stepsize,thetahist);
   otherwise goto 10;
    end;
    if quit='yes' then goto 20;
    goto 10;
  20:end;
procedure loaddefault(var ebno,noisestep,stepsize:real);
{loads default setting into menu }
begin
     ebno:= 0;
     noisestep:=0.03;
     stepsize:=0.5;
end;
{**** Main program starts here ****** }
```

```
begin {main program}
   quit:='no';
   loaddefault(ebno,noisestep,stepsize);
10:menu(ebno,noisestep,stepsize,quit);
   if quit='yes'then goto 20;
   goto 10;
20:end.
Phase Estimator Simulation Program
```

The phase estimator simulation program inputs noise statistic data from a series of files created by Noise1-1.pas for different Eb/No values. This values are take for integer steps in SNR. The program then simulates the behaviour of the phase estimator algorithm for a set of variables which can be selected via a set of menus. The resultant simulation output is stored to providing records of the setup conditions and performance evaluation for post processing. The following pages contain the program listing for Est1-18.pas which was used in the evaluation of the algorithm. As before flow diagrams and line by line commenting is considered superfluous.

#### EST1-18.pas

program Estimator(input,output);

{program allows reading of statistical data from files of different Eb/No. This program is for the analysis of the phase estimator using an IIR filter with single order coefficient selectable from , 15/16,31/32,63/64,127/128 . The Frequency information is now obtained outside the loop of the estimator and feeds forward to the predicted phase mean }

label 10,20;

```
const maxint=4194304;
        pi=3.14159263;
        nmax=128;
        m = 256;
        offset=0;
        ver=1.18;
  type sample= array[0..nmax] of real;
        intsample=array[0..nmax] of integer;
        intresults= array [0..nmax] of integer;
        intarray= array[-360..360] of integer;
        rlresults= array [0..nmax] of real;
       delayspace=array[0..32] of integer;
       samplearray= array[-360..360] of real;
       weightingarray=array [0..721,0..1] of real;
{ could be too small if noise stepsize<0.5 degrees}
       choice=1..6;
       timeseconds=0..60;
       results=record
                trap:string;
                elapsedarray:rlresults;
                anglearray: rlresults;
                binsample: intsample;
                datain:intsample;
                noiseimpulsearray:intresults;
                noiseyloarray:intresults;
                meanphasearray:intresults;
                projectslopearray:intresults;
                predphasearray:intresults;
                noise:sample;
                cerror:sample;
                dataoutarray:intresults;
                end:
       menurecord= record
                    ebno, esno: integer;
                    trapsprung:boolean;
```

```
trapcount:integer;
                  errate:real;
                  errcount:integer;
                  sigma:real;
                  fo:real;
                  fs:real;
                  runtime:real;
                  mag:real;
                  quantbits:integer;
                  datatype:string;
                  dstate:string;
                  nstate:string;
                  filter:string;
                  slope:string;
                  mean:string;
                  slopecoef:string;
                  meancoef:string;
                  coefinc:string;
                  bits:integer;
                  refstepsize:real;
                  reflistends:integer;
                  auto:string;
                end;
statrecord= record
             errormean:real;
             errordev:real;
             carriermean:real;
             carrierdev:real;
             end;
var value:choice;
    etheta, sigma, stepsize, maxy: real;
    ycord:samplearray;
    noise:sample;
```

```
esno, h, listends: integer;
           name,quit,sesno:string;
           readbefore:boolean;
           waittime:timeseconds;
           setup:menurecord;
                                                    external;
function rand:real;
function cstat:boolean;
                                                    external;
procedure time(var hours, minutes, seconds,
                                                    external;
                        hundreths:integer);
function convertdegtoqnt(x:integer):integer;
{converts degrees to quantized level number}
begin
     convertdegtoqnt:=x*m div 360;
end;
procedure wait(var waittime:timeseconds);
{waits for a set time period before returning}
        var hours, minutes, seconds, hundreths,
            starttime:integer;
begin
     time(hours, minutes, seconds, hundreths);
     starttime:=seconds;
     repeat
     time(hours, minutes, seconds, hundreths);
     until seconds>starttime+waittime;
end;
procedure quitread(var quit:string);
{sets quit variable to yes}
 begin
```

```
quit:='yes';
end;
procedure keypressed(var quit:string);
{sets acknowlegdement if key pressed}
       label 10,20;
       var value:choice;
begin
    quit:='no';
 10:writeln(' Key pressed :-');
   writeln;
   writeln(' 1) Continue ');
   writeln;
   writeln(' 0) Quit ');
    writeln;
    write(' ENTER ');
    readln(value);
    case value of
     0:quitread(quit);
     1:goto 20;
    otherwise goto 10;
    end;
20:end;
procedure clearcellcount(var cellcount:intarray);
{clears histogram array cells}
   var h:integer;
begin
     for h:=-360 to 360 do
     begin
     cellcount[h]:=0;
     end;
end;
```

```
procedure disksave(setup:menurecord;statresult:statrecord;
                   phaseresult:results);
{saves setup and results to disk}
        label 10;
        var filename:string;
            estimatorfile:text;
            h:integer;
begin
     str(setup.trapcount,filename);
     if setup.trapcount>99 then filename:='ZZ';
     filename:=concat('a:phdata',filename,'.dat');
     assign(estimatorfile, filename);
     rewrite(estimatorfile);
     writeln(estimatorfile,
         'Eb/No = ',setup.ebno:6,' dB,',
         ' Noise SD = ',setup.sigma:6:2,' degrees,',
         ' Add Noise ', setup.nstate, ', ',
         ' Add Data ',setup.dstate,'-',setup.datatype);
     writeln(estimatorfile,
        'Frequency offset ',setup.fo:6:3,' Hz,',
        ' Symbol rate = ',setup.fs:6:1,' KHz,',
        ' Filter is ', setup.filter);
     writeln(estimatorfile,
        'Sim time = ',setup.runtime:8:6,'sec,',
        ' Quantizing Bits = ',setup.quantbits,',',
       ' Magnitude of signal = ',setup.mag);
     writeln(estimatorfile,
       'Error count = ',setup.errcount,',',
       ' Error rate inclusive of this data block ',
                                    setup.errate:8:6);
     writeln(estimatorfile, 'Type of Trap is ',
             phaseresult.trap);
     writeln(estimatorfile, 'Mean is ', setup.mean,
                  ' Coefficient = ', setup.meancoef);
```

```
writeln(estimatorfile, 'Slope is ', setup.slope,
                   'Coefficient = ', setup.slopecoef);
    writeln(estimatorfile,'No. of Bit in IIR feedback is '
             , setup.bits);
    writeln(estimatorfile);
    writeln(estimatorfile, 'Elapsed':8, 'Data':5, 'angle':6,
             'bin':6, 'noise':5, 'offsetP':8, 'mean':5,
             'slope':6, 'thetaP':7, 'ModO/p':7, 'C/Est ':7,
                                                  'Data':6);
    writeln(estimatorfile,'sec':8,'degs':5,'degs':6,
             'qnt':5,'deq':5,'qnt':8,'qnt':5,'qnt':6,
             'qnt':7, 'qnt':7, 'degs':6);
     for h:=0 to nmax do
      begin
       writeln(estimatorfile,
       phaseresult.elapsedarray[h]:8:6,
       phaseresult.datain[h]:5,
       phaseresult.anglearray[h]:6:1,
       phaseresult.binsample[h]:5,
        phaseresult.noiseimpulsearray[h]:5,
        phaseresult.noiseyloarray[h]:8,
        phaseresult.meanphasearray[h]:5,
        phaseresult.projectslopearray[h]:6,
        phaseresult.predphasearray[h]:7,
        phaseresult.noise[h]:7:1,
        phaseresult.cerror[h]:6:1,
        phaseresult.dataoutarray[h]:6);
       end;
10: close(estimatorfile);
end;
procedure aver(n:integer;ransample:sample;var mean:real);
{calulates mean of integer samples}
           var h:integer;
               sum:real;
```

```
begin
    sum:=0;
     for h:= 0 to nmax do
       begin
        sum:= sum+ ransample[h];
       end;
     mean:=sum/(nmax+1);
end;
procedure variance(randsample:sample; var oldmean, mean,
                 sd:real);
{calculates variance of random input samples}
         var h,n:integer;
             sum,sigmasqrd,mean1:real;
begin
      n:=nmax;
      aver(n,randsample,mean);
               mean1:=oldmean; {uses current mean value}
      for h:=0 to nmax do
        begin
            sum:= sqr(randsample[h]-mean1)+sum;
        end;
     sigmasqrd:= sum/(nmax);
     sd:= sqrt(sigmasqrd);
end;
{These procedures are all used in the phase estimator
simulation }
function convert2scom(y, x:integer):integer;
{Converts sign magnitude to 2's complement notation}
```

```
begin
     if x<0 then
        convert2scom:= y+x
    else
        convert2scom:=x;
end;
function inverse2s(y, x:integer):integer;
{converts from 2's complement to sign magnitude}
begin
     if x<0 then writeln('ERROR in Inverse 2s complement');</pre>
     if x>=y div 2 then
        inverse2s:=x-y
     else
        inverse2s:=x;
end;
function subcyclic( augend,addend:integer):integer;
{performs 2s compliment subtraction on a circular
                                                       basis
ignoring overflows}
bégin
     subcyclic:= (augend+(m-addend)) mod m;
end;
function addcyclic( augend,addend:integer):integer;
{performs 2's complement addition on a circular
ignoring overflows}
begin
     addcyclic:=(augend+addend) mod m;
end;
function power(x,y:real):real;
```

```
{calculates x to power of y}
begin
    power:= exp(y*ln(x));
end;
function log(x:real):real;
{calculates log to base 10}
begin
     log:=ln(x)/ln(10);
end;
function divide2scom(y,x,denom:integer):integer;
{divides 2's complement number by denom}
begin
         x:=inverse2s(y,x);
         x:=x div denom;
         divide2scom:=convert2scom(y,x);
end;
procedure initializeloop(var startphase:real;
                          var predphase, avl, adl, dt, accum,
                              slopaccuminus1:integer;
                          var averphase, averslope,
                              slopedly:delayspace);
{initialize arrays and predicted phase}
          var h:integer;
```

```
begin
     startphase:=0;
     predphase:=0; {initial phase prediction value}
     accum:=0; {initial value of average accumulator}
     avl:=16;{ set length of averaging circuit}
     dt:=8 ;{set slope detect over 8 symbols}
     adl:=16;{ set slope averager to 16 symbols}
     slopaccuminus1:=0;{set slope average accumulator }
     for h:=0 to avl do [flush out to initialize averaging
                         space}
      begin
       averphase[h]:=0;
      end;
      for h:= 0 to adl do
                  { flush out averaging space for slope
                    detector}
       begin
         averslope[h]:=0;
       end:
       for h:= 0 to dt do
                  { flush out delay space for slope
                    detector}
        begin
          slopedly[h]:=0;
        end;
end;
procedure greaterthan180(var x:real);
{if x greater than 180 degrees converts to negative value}
begin
      if x<-180 then x:=360+x;
      if x>180 then x:=x-360;
end;
```

```
procedure modulus( s,y:real;var ans:real);
{produces modulo arithmetic}
          var multi:real;
begin
     multi:=trunc(s/y);
     ans:= s - (multi*y);
end;
procedure shiftintarray(var inputarray:delayspace;
                             length:integer);
{shifts data through array space}
          var h:integer;
begin
     for h:= length-1 downto 0 do
        begin
             inputarray[h+1]:=inputarray[h];
        end
end;
procedure setinsample(var phaseresult:results;
                      var worksample:sample) ;
{sets up a set of input samples}
         var h,y:integer;
             temp:real;
begin
     y := 360;
      for h:=0 to nmax do
       begin
```

```
phaseresult.noiseimpulsearray[h]:=round(worksample[h]);
   temp:=phaseresult.anglearray[h]+phaseresult.datain[h]
                     +worksample[h];
             modulus(temp,y,temp);
             greaterthan180(temp);
             worksample[h]:=temp;
       end;
 end;
procedure convert to m binary(inputsample:sample;
                               var binsample:intsample);
 (converts real input sample (simulated from prom output) to
m bit binary representation}
          var h:integer;
 begin
      for h:= 0 to nmax do
        begin
            binsample[h]:=round(inputsample[h]*m/360);
            if binsample[h]= 128 then binsample[h]:=-128;
        end
 end;
 procedure removedata(qsk, currentsample:integer;
                      var phaserr:integer);
                form incoming signal and calcultes
 {removes data
                                                        phase
 error of predicted value and local oscillator phase}
         var multi:integer;
 begin
      multi:=2+2*qsk;
      currentsample:=(currentsample*multi) mod m ;
      phaserr:= divide2scom(m,currentsample,multi);
 end;
```

```
procedure locate cell(cerror:real;var cellnumber:integer;
                      setup:menurecord);
{locates the cell number that a particular value to thete
resides in }
          var theta:real;
 begin
     theta:=cerror;
     if theta<0 then
      cellnumber:=round((theta+setup.refstepsize/2)
                       /setup.refstepsize)
      else
       cellnumber:=round((theta-setup.refstepsize/2)
                          /setup.refstepsize);
end;
procedure referrorplot(phaseresult:results;
                       setup:menurecord;
                                       cellcount:intarray);
{accumulates count of cells that theha falls
                                                    in for
calculation of estimated phase deviation}
        var h,cellnumber:integer;
begin
     for h :=0 to nmax do
      begin
       locate cell(phaseresult.cerror[h],cellnumber,setup);
       cellcount[cellnumber]:=cellcount[cellnumber]+1;
     end;
end;
procedure savedisc(cellcount:intarray;listends:integer;
                                  sigma,stepsize:real);
{ write data to disc as a text file}
```

```
var outfile1:text;
           h, number of samples: integer;
           etheta:real;
           name:string;
begin
     numberofsamples:=trunc(setup.fs*1e3*setup.runtime);
     str(setup.ebno,name);
     name:=concat('OP',setup.datatype,name,'.dat');
     assign(outfile1,name);
     rewrite(outfile1);
     writeln(outfile1, listends, stepsize, sigma);
     for h:= -listends to listends do
       begin
         writeln(outfile1,cellcount[h]/numberofsamples);
                                 {calculates probability}
       end;
end;
procedure refdatasave(cellcount:intarray;setup:menurecord;
                       statresult:statrecord);
{saves reference data to file }
begin
     savedisc(cellcount, setup.reflistends,
              statresult.carrierdev,
              setup.refstepsize);
end;
procedure saveresult(setup:menurecord;
                      statresult:statrecord; filename,
                      display,trap,ercount:string);
{Svaes results to disk}
     var outfile1:text;
begin
```

```
assign(outfile1, filename);
rewrite(outfile1);
writeln(outfile1);
 writeln(outfile1,'************** PHASE
         ESTIMATOR COMPUTE MENU**************
         ******* );
 writeln(outfile1, 'Eb/No = ',setup.ebno:5,' dB,',
          ' SIM time = ',setup.runtime:6:4,' sec,',
   ' Data = ',setup.dstate,',',' Type = ',
         setup.datatype);
 writeln(outfile1,'Noise = ',setup.nstate,',',
         ' Frequency offset ',setup.fo:10:1,' Hz,',
         ' Symbol rate = ',setup.fs:6:1,' Khz');
 writeln(outfile1,'Number of traps = ',
         setup.trapcount:4,',','
         Bit Error rate = ', setup.errate:10:6,',',
         ' Symbol Error Count = ', setup.errcount:4 );
  writeln(outfile1,'Slope detector is ', setup.slope,
             Mean filter output is ', setup.mean);
  writeln(outfile1,'Number of feedback bits in IIR= ',
           setup.bits:3);
  writeln(outfile1,'Slope Coefficient = ',
         setup.slopecoef,
          Mean Coefficient = ',setup.meancoef);
  writeln(outfile1,'Input noise mean = ',
         statresult.errormean:6:3 ,' deg',
   ' Input standard deviation = ',
        statresult.errordev:6:3,
   ' deq');
  writeln(outfile1,'******************
        **************************
  writeln(outfile1);
  writeln(outfile1,' 1) Number of quantizing bits ',
          setup.quantbits);
  writeln(outfile1);
```

```
writeln(outfile1,' 2) Magnitude of input signal
               (0-1) ', setup.mag:6:2);
       writeln(outfile1);
       writeln(outfile1,' 3) Display Estimator Run Time
                              Data ', display);
       writeln(outfile1);
       writeln(outfile1,'
                           4) Error Trap Data and save to
                              disk, Trap on ', trap);
       writeln(outfile1);
       writeln(outfile1,'
                           5) Error rate Count ',
               ercount);
       writeln(outfile1);
       writeln(outfile1,'
                           6) Compute');
       writeln(outfile1);
       writeln(outfile1,'
                           7) Auto compute');
       writeln(outfile1);
       writeln(outfile1,' 0) End');
       writeln(outfile1);
       close(outfile1);
end;
procedure iirfilter( x:integer; var filout,
                     accminus1:integer;
                     coef:string; setup:menurecord);
{IIR filter function using 16 bit arithmetic to simulate
constructed system}
{For 16 bit accumulator, 16 bit output from accum is
                                                         fed
back, as n bit prom address}
{plus 1 bit for complement signal}
         var acc, dif, multin, multout, augend, addend,
             shift:integer;
             difbits:real;
begin
     difbits:=16-setup.bits;
```

```
augend:=inverse2s(m,x);
     x:=augend;
     if coef= '15/16'then x:=x*16;
     if coef='31/32' then x:=x*8;
     if coef='63/64' then x:=x*4;
     if coef = '127/128' then x:=x*2;{converts 8 bit input}
                                      to}
                                   {faction of max i.e.+/-
                                    327681
     shift:=round(power(2,difbits));
    multin:= (accminus1 div shift)*shift;
                       { 16 bits rounded to n bit address}
     dif:= augend- (multin div 256);
             {converts to 8 bits from 16 bits for direction
              test}
     if dif>128 then
      multin:=65536+multin;
     if dif<-128 then
     multin:=-65536+multin;
      if coef='15/16'then multout:= 15*multin div 16;
      if coef='31/32' then multout:=31*multin div 32;
      if coef='63/64' then multout:= 63*multin div 64;
      if coef='127/128' then multout:= 127*multin div 128;
     addend:=multout; augend:=x;
     acc:=(augend+addend) ;{accum is 16 bits}
     accminus1:=acc;
     filout:=acc;
end;
procedure iirslopedet(noiseyslope,dt,qsk:integer;
                   var projectslope,slopaccuminus1:integer;
                   var slopedly:delayspace;
                       setup:menurecord);
{calculates the slope of the changing phase vector}
     var meanslope,slope:integer;
```

```
coef:string;
             multi:real;
begin
    coef:=setup.meancoef;
    slopedly[0]:= noiseyslope;
    slope:=subcyclic(slopedly[0],slopedly[dt]);
    iirfilter(slope, meanslope, slopaccuminus1,
             setup.slopecoef,setup);
                             {meanslope is 16 bit result}
   meanslope:=meanslope div 16;
     if meanslope<-m/2*16 then meanslope:= m*16+meanslope;
     if meanslope>((m/2*16)-1) then
         meanslope:=meanslope-(m*16);
     shiftintarray(slopedly,dt);
     if coef='15/16' then multi:=16.5;
     if coef='31/32' then multi:=32.5;
     if coef='63/64' then multi:=64.5;
     if coef='127/128' then multi:=128.5;
 projectslope:= round(multi*meanslope/(dt*16*(2+2*qsk)));
    {*16 converts to 8 bits from 12}
    projectslope:=convert2scom(m,projectslope);
end:
procedure sloperemovedata(qsk,inputvalue:integer;
                          var fourxslope:integer);
{removes data from input slope signal}
         var multi:integer;
begin
     multi:=2+2*qsk;
     fourxslope:=(inputvalue*multi) mod m;
end;
procedure freqdetect(inputvalue,qsk,dt:integer;
```

```
var pslope,slopaccuminus1:integer;
                    var slopedly:delayspace;
                    setup:menurecord);
{calculates frequency offset from nominal}
        var fourxslope:integer;
begin
     sloperemovedata(qsk,inputvalue,fourxslope);
     iirslopedet(fourxslope,dt,qsk,pslope,slopaccuminus1,
                 slopedly, setup);
end;
procedure errortrap(phaseresult:results;
                    var setup:menurecord;
                    loop:integer;var lastdata:integer;
                    var cycleslip,symerror:boolean);
{looks for errors and cycle slips in the decoded data}
        var h, trapointer, startdata, comparedata,
            datain:integer;
begin
      cycleslip:=false;
      symerror:=false;
      if phaseresult.datain[0]<0 then
        datain:=360+phaseresult.datain[0]
       else
        datain:=phaseresult.datain[0];
      datain:=convertdeqtoqnt(datain);
      h := 1;
      trapointer:=0;
      if loop=0 then
        startdata:= phaseresult.dataoutarray[0]-datain
```

```
startdata:=lastdata;
      while h<= nmax do
       begin
       if phaseresult.datain[h]<0 then
        datain:=360+phaseresult.datain[h]
       else
        datain:=phaseresult.datain[h];
      datain:=convertdegtoqnt(datain);
      comparedata:=phaseresult.dataoutarray[h]-datain;
      if comparedata<>startdata then
      begin
       setup.errcount:=setup.errcount+1;
       symerror:=true;
       trapointer:=trapointer+1;
       if trapointer>10 then trapointer:=10;
      end:
      if trapointer= 10 then
         begin
           startdata:=comparedata;
                  { if different values of data for 10 }
                  {samples then reset startdata to compare
                   data }
           cycleslip:=true;
         end:
       if comparedata=startdata then
       begin
        trapointer:=trapointer-1;
        if trapointer<0 then trapointer:=0;
       end;
         h := h+1;
    end;
    lastdata:=startdata;
end;
```

else

```
procedure phase estimate1(var phaseresult:results;
                   setup:menurecord;qsk:integer;
                   startphase:real;binsample:intsample;
                   display, trap, ercount: string;
                   avl,adl,dt,loop:integer;
                   var accum, slopaccuminus1, predphase,
                   numberoftraps, lastdata: integer;
                   var averphase, averslope,
                   slopedly:delayspace);
                                                         and
{uses binsamples to estimate
                                  the carrier phase
frequency error using IIR Filter with variable coefficient
+ frequency offset detection and projection, in parallel,
from difference samples taken over 8 symbol periods
averaged using an iir filter}
         label 10,20;
         var minuscarrier, promsample, noiseylophase, phaserr,
             projectslope, newsample, phasemean, mphaseout,
          dataout, noise impulse: integer;
             modcerror,h,erraccum:integer;
             angle, angle1, elapsedtime: real; begin
     if display='no' then goto 10;
       writeln('Elapsed':8, 'Data':5, 'angle':6, 'bin':4,
               'noise':5, 'offsetP':8, 'mean':5, 'slope':6,
               'thetaP':7,'ModO/p':7,'C/Est ':7,'Data':6);
       writeln('sec':8,'degs':5,'degs':6,'qnt':5,'deg':5,
               'qnt':8,'qnt':5,'qnt':6,'qnt':7,
               'qnt':7, 'deqs':6);
10: for h:=0 to nmax do
{ process binsamples in a sequential manner to obtain
output sequence}
     begin
```

angle1:=phaseresult.anglearray[h]\*m/360;

```
{convert to binary
                                       term
     phaseresult.cerror[h]:=angle1+(m-predphase);
modulus(phaseresult.cerror[h],m,phaseresult.cerror[h]);
     modcerror:=round(phaseresult.cerror[h]);
     removedata(qsk, modcerror, modcerror);
     phaseresult.cerror[h]:=modcerror;
   if phaseresult.cerror[h]>m/2-1 then
        phaseresult.cerror[h]:=phaseresult.cerror[h]-m;
  phaseresult.cerror[h]:=phaseresult.cerror[h]*360/256;
     promsample:=convert2scom(m,binsample[h]);
     if setup.slope='ON' then
      freqdetect(promsample, qsk, dt, projectslope,
                 slopaccuminus1, slopedly, setup)
     else
      projectslope:=0;
    minuscarrier:=subcyclic(promsample,predphase);
     removedata(qsk,minuscarrier,phaserr);
     phaserr:=convert2scom(m,phaserr);
     dataout:= subcyclic(minuscarrier,phaserr);
     noiseylophase:=addcyclic(phaserr,predphase);
     if setup.mean='ON' then
      iirfilter(noiseylophase,phasemean,accum,
                setup.meancoef,setup)
     else
      phasemean:=0;
     phasemean:= (phasemean div 256)
     if phasemean <- m/2 then phasemean:= m+phasemean;
     if phasemean>m/2 -1 then phasemean:=phasemean-m;
     phasemean:=convert2scom(m,phasemean);
     predphase:=addcyclic(projectslope,phasemean);
     mphaseout:= inverse2s(m,phasemean);
     noise[h]:=inverse2s(m,phaserr);
     elapsedtime:=(loop*(nmax+1)+(h+1))/(setup.fs*1e3);
     phaseresult.elapsedarray[h]:=elapsedtime;
     phaseresult.noiseyloarray[h]:=noiseylophase;
```

```
phaseresult.meanphasearray[h]:=mphaseout;
        phaseresult.projectslopearray[h]:=projectslope;
        phaseresult.predphasearray[h]:=predphase;
        phaseresult.dataoutarray[h]:= dataout;
        phaseresult.binsample[h]:=binsample[h];
   phaseresult.noise[h]:=noise[h];
        if display='no'then goto 20;
       writeln(elapsedtime:8:6,phaseresult.datain[h]:5,
             phaseresult.anglearray[h]:6:1,binsample[h]:5,
             phaseresult.noiseimpulsearray[h]:5,
             noiseylophase:8,mphaseout:5,projectslope:6,
             predphase:7,noise[h]:7:1,
             phaseresult.cerror[h]:6:1,dataout:6);
   20:end;
end;
procedure mean2scom(var meandif:delayspace;newsample,
                    len:integer;var phasemean:integer;
                    var accum:integer);
{returns a current mean value from a sample per sample
input}
         var differ,y:integer;
begin
     y:=len*m;
     meandif[0]:= newsample;
     differ:= subcyclic(meandif[0], meandif[len]);
     differ:= inverse2s(m,differ);
     differ:= convert2scom(y,differ);
                                {converts from 8bit to 12
                                 bit }
     accum:= (accum + differ) mod y;
     phasemean:= divide2scom(y,accum,len);
```

```
phasemean:= inverse2s(y,phasemean);
     phasemean:= convert2scom(m,phasemean);
     shiftintarray(meandif,len);
end;
procedure slopedet(noiseylophase,dt,avl,adl:integer;
                   var projectslope,slopaccum:integer;
                   var slopedly, averslope:delayspace);
     var meanslope,slope:integer;
begin
    slopedly[0]:= noiseylophase;
    slope:=subcyclic(slopedly[0],slopedly[dt]);
   mean2scom(averslope, slope, adl, meanslope, slopaccum);
    shiftintarray(slopedly,dt);
    meanslope:=inverse2s(m,meanslope);
    projectslope:= round((av1/2+0.5)/dt*meanslope);
    projectslope:=convert2scom(m,projectslope);
end;
procedure phase estimate2(qsk:integer;binsample:intsample;
                         var noise:sample;display,trap,
                             ercount:string;
                         avl,adl,dt:integer;
                    var accum,slopaccum,predphase:integer;
                     var averphase, averslope,
                         slopedly:delayspace);
                                                        and
{uses binsamples
                                  the carrier phase
                   to estimate
frequency error using mean phase by averaging + frequency
                                       in parallel,
offset detection
                    and projection,
                                                       from
difference
                     taken over
                                  8
                                      symbol periods
                                                        and
            samples
averaged}
```

```
label 10,20;
         var minuscarrier, promsample, noiseylophase, phaserr,
             projectslope, newsample, phasemean, mphaseout,
             dataout:integer;
             h:integer;
begin
     writeln('Entered phase estimator');
     if display='no' then goto 10;
       writeln('h':10,'binsample':10,'meanphase':10,
               'lophase':10, 'predicted':10, 'phaserr':10,
               'Data out':10);
 10: for h:=0 to nmax do
{ process binsamples in a sequential manner to obtain
output sequence}
     begin
        promsample:=convert2scom(m,binsample[h]);
        minuscarrier:=subcyclic(promsample,predphase);
        removedata(qsk,minuscarrier,phaserr);
        noiseylophase:=addcyclic(phaserr,predphase);
        mean2scom(averphase, noiseylophase, avl, phasemean,
                  accum);
        slopedet(noiseylophase, dt, avl, adl, projectslope,
                 slopaccum, slopedly, averslope);
        predphase:=addcyclic(projectslope,phasemean);
        mphaseout:= inverse2s(m,phasemean); .
        dataout:= subcyclic(minuscarrier,phaserr);
        noise[h]:=inverse2s(m,phaserr);
        if display='no'then goto 20;
        writeln(h:10,binsample[h]:10,mphaseout:10,
                noiseylophase:10, predphase:10,
                noise[h]:10:1, dataout:10);
   20:end
 end;
```

```
procedure phaselock(var phaseresult:results;
                         setup:menurecord;
                         worksample:sample;
                         startphase:real;qsk:integer;
                         display, trap, ercount: string;
                         avl,adl,dt,loop:integer;
                     var accum, slopaccuminus1, predphase,
                         numberoftraps, lastdata: integer;
                     var averphase, averslope,
                         slopedly:delayspace);
        var binsample:intsample;
            meandif:delayspace;
            ch:char;
            h:integer;
begin{phaselock main body}
    writeln('entered phaselock');
    startphase:=startphase*180/pi;{converts to degrees};
    setinsample(phaseresult,worksample);
    convert to m binary(worksample, binsample);
    writeln('converted to binary');
    if setup.filter='IIR' then
     phase estimate1(phaseresult, setup, qsk, startphase,
                      binsample, display, trap, ercount,
                      avl, adl, dt, loop, accum, slopaccuminus1,
                      predphase, number of traps, lastdata,
                      averphase, averslope, slopedly)
    else
     phase estimate2(qsk,binsample,noise,display,trap,
                      ercount, avl, adl, dt, accum,
                      slopaccuminus1, predphase, averphase,
                      averslope, slopedly);
end;
```

```
********
{set up menu procedures}
procedure readname(var name, quit:string);
{read file name}
begin
    write('File name= ');
    read(name);
    quit:='no';
end;
procedure readdata(name:string;var ycord:samplearray;
                  var maxy:real;var listends:integer;
                 var sigma,stepsize:real);
{read data of phase noise deviation from file}
      var h:integer;
          infile1:text;
begin
    assign(infile1, name);
    reset(infile1);
    readln(infile1, listends, stepsize, sigma);
    stepsize:=stepsize*pi/180;
    sigma:=sigma*pi/180;
    h:=-listends;
    while h<=listends do
      begin
        readln(infile1,ycord[h]);
        if ycord[h]>maxy then maxy:=ycord[h];
                {find maximum value for y}
        h:=h+1;
      end;
      close(infile1);
```

```
if h<> listends+1 then writeln('errror in reading
file');
end:
procedure readfile(var listends:integer;var sigma:real;
                   var stepsize:real;
                   var name,quit:string;
                   var ycord:samplearray;var maxy:real;
                   var readbefore:boolean;
                   var esno:integer);
{reads data from named file}
         label 10,20,30;
         var h:integer;
             inebno:real;
             checkok:boolean;
             ch:char;
begin
     Writeln('Symbol Energy Es/No dB required (integer
              values only)');
     readln(inebno);
     esno:=round(inebno);
     str(esno,name);
     name:=concat('ebno',name,'.dat');
10: checkok:=fstat(name);
     if checkok=false then
     begin
20: writeln('File not found :Enter file name (y/n)');
       readln(ch):
       case ch of
         'y': readname(name,quit);
         'Y': readname(name,quit);
         'n': quitread(quit);
         'N': quitread(quit);
```

```
otherwise goto 20;
         end;
        goto 10
      end;
      if quit='yes' then goto 30;
      readdata(name, ycord, maxy, listends, sigma, stepsize);
      readbefore:=true;
30:end;
procedure erfc(listends:integer;stepsize:real;
               ycord:samplearray);
{produces complimentary error function i.e probability of
error being greater than x}
         var h:integer;
             etheta, x, x1: real;
             sum,prob error:longreal;
begin
     writeln('Enter prob(phase error >x degrees)');
     readln(x);
     x1:= x*pi/180;
     sum:=0;{calculates complimentary errror function}
     for h:= -listends to listends do
      begin
       etheta:= h*stepsize;
       if abs(etheta)<=x1 then sum:= sum+ycord[h];
           {probability of etheta<x1 radians}</pre>
      end;
      prob error:=1-sum;
      writeln('Probability of phase error >',x:4:2,' deg =
              ',prob_error:15:10);
end;
```

```
procedure pseudorandom(qsk:integer;var iv:integer;var
                       random:intsample);
{from an initial set up value, iv, a pseudo random stream is
produced using 23 stage shift register}
      Type rnumber=array[1..23] of integer;
            shiftreg : rnumber;
      var
            i, ip, temp, h, j:integer;
            p:real;
begin
      {initialize shift register with start point}
      for h:= 23 downto 1 do { turns seed value into binary
                                form}
        begin
          shiftreg[h]:=0;
          p:= power(2,h);
          ip:=round(p);
            shiftreg[h]:=iv div ip;
            iv:=iv mod ip;
        end:
  for j:=0 to qsk do
  begin
   for i:= 0 to nmax do
    begin
      temp:=( shiftreg[18]+shiftreg[23]) mod 2;
      if j=0 then
        random[i]:=shiftreq[23]
      else
        random[i]:=random[i]+2*shiftreg[23];
      for h:= 22 downto 1 do
```

```
begin
             shiftreg[h+1]:=shiftreg[h];
         end;
     shiftreg[1]:=temp;
   end;
  end;
end;
procedure nodata(var data:intsample);
{clears data array}
   var h:integer;
begin
     for h:=0 to nmax do
      begin
        data[h]:=0;
end;
procedure nonoise(var worksample:sample);
{fills noise locations with zero}
       var h:integer;
begin
      for h:= 0 to nmax do
      begin
      worksample[h]:=0;
      end;
end;
procedure noiseset(ycord:samplearray;var worksample:sample;
```

```
var n,h:integer;
          sum,uniform:real;
begin
     for n:=0 to nmax do
     begin
      uniform:=round(1e9*rand)/1e9;
      if uniform=1 then uniform:=1-1e-9;
      sum:=0;
      h:=-listends;
      while h<=listends do
      begin
       sum:=sum+ycord[h];
       if sum>uniform then
       begin
        worksample[n]:=h*stepsize;
        h:=listends+1; {leave loop}
       end;
       h:=h+1;
      end;
     end;
end;
procedure denzero(num:integer;var ramp:real);
{set num if denominator zero}
begin
      if num=0 then ramp:=0;
      if num>0 then ramp:=pi/2;
      if num<0 then ramp:=-pi/2;
end;
```

listends:integer;stepsize:real);

```
procedure promerror(angle,ramp:real;
                    var sum:real;h:integer);
         var error,y:real;
{calculates error due to prom quantization}
begin
            y := 360;
            angle:=180*angle/pi;
            modulus(angle,y,angle);
            ramp:= 180*ramp/pi;{converts to degrees}
            if ramp<0 then ramp:= ramp+360;
            ramp:=round(ramp*m/360);{converts to
                                                         bit
                                                     m
binary}
            ramp:= ramp*360/m;{ converts back to real
                                                         for
error}
            error: =angle+(360-ramp);
            modulus(error,y,error);
            if error>180 then error:=error-360;
            sum:=sum+sqr(error);
end;
procedure frequencyoffset(var phaseresult:results;
                          fo,fs,mag:real;
                          quantsteps:integer;
                          var startphase,nextstartphase:real);
{allows frequency offset of carrier to be set and converts
to phase change/sample}
        label 10;
        var y,h,num,den:integer;
            sum,sigma,normf,angle,ramp,noisesam:real;
            waittime: timeseconds;
```

```
begin
         y:=360;
         normf:=fo/fs;
         sum:=0;
         if fo=0 then
         begin
           for h:=0 to nmax do
             begin
             phaseresult.anglearray[h]:=0;
             end;
          goto 10;
         end:
         for h:= 0 to nmax do
          begin.
            angle:= 2*pi*normf*h+startphase;
            num:=trunc(sin(angle)*mag*quantsteps);
            den:=trunc(cos(angle)*mag*quantsteps);
            if den=0 then
            denzero(num, ramp)
            else
             ramp:= arctan(num/den);
            if (num=0)and (den=0) then ramp:=0;
            if (num>=0) and (den<0) then ramp:= pi+ramp;
            if (num<0) and (den<0) then ramp:= -pi+ramp;
            promerror(angle, ramp, sum, h);
            {convert to degrees}
            ramp:= ramp*180/pi;
            modulus(ramp,y,ramp);
            phaseresult.anglearray[h]:=ramp;
         end;
     10: nextstartphase:=2*pi*normf*(nmax+1)+startphase;
         modulus(nextstartphase, 2*pi, nextstartphase);
         if nextstartphase>pi then
```

nextstartphase:=nextstartphase-(2\*pi);

writeln('Prom Sigma (standard deviation) from

sigma:=sgrt(sum/(nmax));

```
phase angle = ',sigma:6:2,'Degrees');
end;
procedure bpskdata(var phaseresult:results);
{set up data with random phase angles}
         var iv,h,qsk:integer;
             random:intsample;
begin
          qsk:=0;
          iv:=4197376;
          pseudorandom(qsk,iv,random);
          h := 0;
          while h<=nmax do
          begin
            case random[h] of
              0: phaseresult.datain[h]:=0;
              1: phaseresult.datain[h]:=180;
            end;
            h := h+1;
           end;
end;
procedure qpskdata(var phaseresult:results);
{set up qpsk random phase samples}
             var h,i,iv,qsk:integer;
                 random:intsample;
begin
              qsk:=1;
              iv:=4065273;
              pseudorandom(qsk,iv,random);
              h := 0;
              while h<=nmax do
                begin
```

```
case random[h] of
                    0:phaseresult.datain[h]:=0;
                    1:phaseresult.datain[h]:=90;
                    2:phaseresult.datain[h]:=180;
                     3:phaseresult.datain[h]:=-90;
                  end;
                  h := h+1;
                 end;
end;
procedure datayes(var qsk:integer;var phaseresult:results);
{creates data}
         var ch:char;
             i, iv: integer;
 begin
        case qsk of
          0:bpskdata(phaseresult);
          1:qpskdata(phaseresult);
          otherwise
            writeln('qsk=',qsk);
        end;
end;
procedure setoffset(var fo:real);
{sets offset frequency }
begin
    writeln('Enter frequency offset in Hz');
    readln(fo);
 end;
procedure setout(var out:string);
{set display output on or off}
begin
```

```
if out='ON' then out:='OFF'
     else
       out:='ON';
end;
procedure setcoef(var coef:string); {set coefficent value}
     var temp:string;
begin
     if coef='15/16' then
     temp:='31/32';
     if coef='31/32' then
     temp:='63/64';
     if coef='63/64' then
     temp:='127/128';
     if coef='127/128' then
     temp:='15/16';
     coef:=temp;
end;
procedure setbits( var number:integer);
{set number of bits in feedback variable}
     label 10;
begin
  10:write('Enter number of feedback address bits ');
     readln(number);
     if (number <1) or (number>16) then
      goto 10;
end;
procedure setiirmenu( var setup:menurecord);
```

```
{sets up iir filters in phase and slope processing
sections }
        label 10,20;
        var value:choice;
          quit:string;
begin
    quit:='no';
    setup.filter:='IIR';
10: writeln('****************************
              **************************
    writeln('*
                                 IIR Filters menu
             *');
    writeln('**************************
              ***********************************
    writeln;
    writeln(' 1) Slope output ',setup.slope);
    writeln;
    writeln(' 2) Slope Coefficient ',setup.slopecoef);
    writeln;
    writeln(' 3) Mean output ',setup.mean);
    writeln;
    writeln(' 4) Mean Coefficient ', setup.meancoef);
    writeln;
    writeln(' 5) Number of Address Bits for Feedback Word
             ',setup.bits);
    writeln;
    writeln(' 0) End');
    writeln;
    write(' ENTER ');
    readln(value);
    case value of
      0: quitread(quit);
      1: setout(setup.slope);
```

```
2: setcoef(setup.slopecoef);
      3: setout(setup.mean);
      4: setcoef(setup.meancoef);
      5: setbits(setup.bits);
      otherwise goto 10;
      end:
      if quit='yes' then goto 20;
      goto 10;
20:end;
procedure setfilter(var setup:menurecord);
{calls setup procedure for setting filter types}
      label 10,20;
      var value:choice;
          quit:string;
begin
      setiirmenu(setup);
      goto 20;{ skip this menu}
      quit:='no';
  10: writeln(' 1) IIR filter ');
      writeln;
      writeln(' 2) Averageing');
      writeln;
      writeln(' 0) End');
      writeln;
      write('ENTER ');
      readln(value);
      case value of
      0: quitread(quit);
      1: setiirmenu(setup);
      2: setup.filter:='Averaging';
      otherwise goto 10;
      end;
```

```
if quit='yes' then goto 20;
      goto 10;
20:end;
procedure setnoise(var nstate:string);
{sets state of noise samples}
begin
     if nstate='yes' then
     begin
       nstate:='no'
     end
    else
      nstate:='yes'
end;
procedure setdstate(var dstate:string);
{set state of data samples}
begin
     if dstate='no' then dstate:='yes'
     else
      dstate:='no';
end;
procedure setbpsk(var qsk:integer;var datatype:string);
{set type of PSK to BPSK}
begin
     qsk:=0;
     datatype:='BPSK';
end;
procedure setqpsk(var qsk:integer; var datatype:string);
{set type of PSK to QPSK}
```

```
begin
    qsk:=1;
     datatype:='QPSK';
end;
procedure setdata( var dstate, datatype:string; var
                   qsk:integer);
{calls setting of PSK type}
      label 10,20;
      var ch:char;
begin
     if dstate='yes ' then
     begin
      dstate:='no';
      goto 10;
     end
     else
     dstate:='yes';
   20: writeln('BPSK or QPSK (b/q/n) ?');
       readln(ch);
       case ch of
       'b':setbpsk(qsk,datatype);
       'B':setbpsk(qsk,datatype);
       'q':setqpsk(qsk,datatype);
       'Q':setqpsk(qsk,datatype);
       'n':setdstate(dstate);
       'N':setdstate(dstate);
       otherwise goto 20;
      end;
10: end;
procedure setsymbolrate(var fs:real);
{sets the symbol rate of the simulation}
       label 10;
```

```
begin
  10: write('Enter symbol rate in Khz ');
        readln(fs);
        if (fs<=0) then goto 10;
end;
procedure setruntime(var runtime:real);
{sets the simulated run time of the simulation}
     label 10;
begin
10 : write('Enter required simulated run time in seconds
');
     readln(runtime);
     if runtime<=0 then goto 10;
end;
procedure degnoise(var worksample:sample);
{converts from radian noise samples to degree noise
samples }
       var h:integer;
begin
     for h:= 0 to nmax do
      begin
       worksample[h]:=worksample[h]*180/pi;
       end;
end;
procedure maxmin(phaseresult:results);
{calculates maximum and minimum phase noise samples}
     var h:integer;
        max,min:real;
```

```
begin
     max:=-128; min:=127;
     for h:=0 to nmax do
     begin
     if max<phaseresult.noise[h] then</pre>
        max:= phaseresult.noise[h];
     if min>phaseresult.noise[h] then
        min:= phaseresult.noise[h]
     end:
     writeln('max phase error = ',max:5:1,' qnts');
     writeln('min phase error = ',min:5:1,' qnts' );
end;
procedure erroratio(loop:integer;var setup:menurecord);
{calculates error rate of simulation}
         var numberofsymbols,numberofbits:integer;
begin
     numberofsymbols:=(loop+1)*nmax;
     numberofsymbols:=(loop+1)*nmax;
     if setup.datatype='BPSK' then
       numberofbits:=numberofsymbols
     else
      numberofbits:=2*numberofsymbols;
      setup.errate:=setup.errcount/numberofbits;
end;
procedure sumvariance(var sd:real;oldsigma:real;
                      loop:integer);
{calculates current variance of complete simulation
                                                      after
new simulated block}
         var currentvar,oldvar,newvar:real;
begin
     currentvar:=sqr(sd);
     oldvar:=sqr(oldsigma);
     newvar:=(nmax*loop*oldvar+(nmax*currentvar))
```

```
/((loop+1)*nmax);
     sd:=sqrt(newvar);
end;
procedure resultstats(var statresult:statrecord;
                      var cellcount:intarray;
                      phaseresult:results;
                      loop, number of traps,
                      errcount:integer;
                      fs,errate:real);
{output statistical results to screen}
       var sd,sddeq,mean:real;
begin
      writeln('Elapsed time is ',
               (loop+1)*nmax/(fs*1e3):8:6,' sec');
      writeln('<<<<Phase error output statistics>>>>');
      maxmin(phaseresult);
      variance(phaseresult.noise, statresult.errormean,
               mean,sd);
      sddeg:= 360/m * sd;
      sumvariance(sddeg,statresult.errordev,loop);
      sd:=sddeq*m/360;
      writeln('Mean = ',mean:6:3,' qnts':5,' or ',
               mean*360/m :6:3, ' deg');
      writeln('Standard Deviation =',sd:6:3,' qnts':5,
              ' or ', sddeg:6:3,' degrees':8);
      statresult.errormean:=mean;
      statresult.errordev:=sddeg;
      writeln('<<<<Carrier Estimator statistics>>>>');
      variance(phaseresult.cerror, statresult.carriermean,
               mean,sd);
      mean:=(mean*nmax+statresult.carriermean*nmax*loop)
             /(nmax*(loop+1));
      referrorplot(phaseresult,setup,cellcount);
```

```
sumvariance(sd, statresult.carrierdev, loop);
      writeln('Mean = ',mean:6:3,' degrees':8);
      writeln('Standard Deviation = ',sd:6:3,' degrees':8);
      writeln('Number of Results trapped = ',
               numberoftraps);
      writeln('Bit Error Rate = ',errate:10:8);
      writeln('Symbol Error Count = ',errcount:6);
      writeln('************************
              ***************
      statresult.carriermean:=mean;
      statresult.carrierdev:=sd;
end;
procedure compute(var setup:menurecord;
                  var statresult:statrecord;
                  stepsize:real; display,trap,
                  ercount:string;
                  var quit:string;qsk:integer;
                  ycord:samplearray;
                  listends:integer);
{computes phase estimation simulation from here}
       label 10,30;
       var
              cellcount:intarray;
              worksample:sample;
              fs, startphase, next startphase, real quant bits,
              sigma1:real;
              predphase, avl, adl, dt, accum, slopaccuminus1,
              totalnumber, numberloops, loop, quantsteps,
              lastdata, presentcount:integer;
              averphase, averslope, slopedly: delayspace;
              noiseimpulsearray, noiseyloarray,
```

```
meanphasearray, projectslopearray,
              predphasearray, dataoutarray: intresults;
              anglearray, elapsedarray: rlresults;
              phaseresult:results;
              trapsprung, symerror, cycleslip,
              keypress:boolean;
begin
    writeln('Computing- Please wait');
    quit:='no';
    realquantbits:=setup.quantbits;
    quantsteps:=round( power(2,realquantbits-1));{single
                                                    sided }
    fs:=setup.fs*1e3;{converts to Hz}
    sigma1:=setup.sigma*180/pi;
    totalnumber:=trunc(setup.runtime*fs);
    statresult.carriermean:=0;
    statresult.carrierdev:=0;
    clearcellcount(cellcount);
    numberloops:=totalnumber div nmax;
    initializeloop(startphase,predphase,avl,adl,dt,accum,
             slopaccuminus1, averphase, averslope, slopedly);
    setup.errate:=0;
    setup.trapcount:=0;
    setup.errcount:=0;
    statresult.errormean:=0;
    statresult.errordev:=0;
    lastdata:=0; loop:=0;
    while loop<= numberloops-1 do
    begin
     keypress:=false;
     trapsprung:=false;
     if setup.nstate='no' then
      nonoise(worksample)
     else
      begin
```

```
noiseset(ycord,worksample,listends,stepsize);
      degnoise(worksample);
     end;
    writeln('Noise standard deviation (sigma) = ',
             sigma1:6:1, Degrees');
    frequencyoffset(phaseresult, setup.fo, fs, setup.mag,
             quantsteps, startphase, nextstartphase);
   if setup.dstate='no' then
   begin
     nodata(phaseresult.datain);
     goto 10;
    end
    else
     datayes(qsk,phaseresult);
10: writeln('*******************************
             *************
   writeln('Frequency offset = ',setup.fo:10:2,' Hz');
   writeln('Noise ',setup.nstate);
   writeln('Data ',setup.dstate,setup.datatype:6);
   phaselock(phaseresult, setup, worksample, startphase, qsk,
              display, trap, ercount, avl, adl, dt, loop, accum,
              slopaccuminus1,predphase,setup.trapcount,
              lastdata,averphase,averslope,slopedly);
   startphase:=nextstartphase;
    if ercount= 'no' then
    presentcount:=setup.errcount;
   errortrap(phaseresult, setup, loop, lastdata, cycleslip,
              symerror);
   if ercount='no' then setup.errcount:=presentcount;
   erroratio(loop,setup);
   writeln('Eb/No = ',setup.ebno:3,'dB', ' Simulation time
             = ', setup.runtime:6:4,' sec');
   writeln('Slope coefficient = ',setup.slopecoef,' Mean
             coefficient = ', setup.meancoef);
   resultstats(statresult,cellcount,phaseresult,loop,
            setup.trapcount, setup.errcount, setup.fs,
```

```
setup.errate);
    if trap= 'No' then goto 30;
    if (trap= 'Cycle slip') and (cycleslip=true) then
     trapsprung:=true;
    if (trap= 'Symbol error') and (symerror=true) then
     trapsprung:=true;
    setup.trapsprung:=trapsprung;
    if trapsprung=true then
    begin
      phaseresult.trap:=trap;
      disksave(setup, statresult, phaseresult);
       setup.trapcount:=setup.trapcount+1;
    end;
 30:loop:=loop+1;
    keypress:=cstat;
      if keypress=true then
        keypressed(quit);
      if quit='yes'then
       begin
        writeln('||||||| EXIT AT END OF NEXT BLOCK
                 !!!!!!!!!!!);
         loop := numberloops;
       end;
   end;
    refdatasave(cellcount, setup, statresult);
end;
procedure setststp(var value:integer);
{set up start and stop values for auto computation}
    label 10;
    var invalue:real;
begin
 10:write('Enter Eb/No ');
    readln(invalue);
```

```
value:=round(invalue);
    if (value<3) or (value>10) then goto 10;
end;
procedure setcoefinc(var coefinc:string);
{set up for auto coefficent increment}
begin
  if coefinc='no' then
    coefinc:='yes'
  else
   coefinc:='no';
end;
procedure run(var setup:menurecord;
              var statresult:statrecord;
              stepsize:real;
              display, trap, ercount, filename: string;
              qsk:integer;ycord:samplearray;listends,
              filenumber,start,stop:integer);
{runs program manually for one set up position}
       label 10,40;
       var h,slopecoefno:integer;
           runtime, fs:real;
           quit, name : string;
           checkok:boolean;
begin
     h:=start; quit:='no';
     while h<= stop do
     begin
      if setup.datatype='QPSK' then
         setup.esno:=h+3
```

```
else
     setup.esno:=h;
   str(setup.esno,name);
   name:=concat('ebno',name,'.dat');
   checkok:=fstat(name);
   if checkok=false then
    begin
      writeln('File ',name,' not found');
      h:=stop+1;
      quit:='yes';
    end;
    h:=h+1;
  end:
. if quit='yes' then goto 10;
 quit:='no';
  if setup.coefinc='yes' then
    slopecoefno:=1
  else
    slopecoefno:=4;
  while slopecoefno<=4 do
   begin
   h:=start;
   while h<= stop do
   begin
     if setup.datatype='QPSK' then
      setup.esno:=h+3
     else
     setup.esno:=h;
     str(setup.esno,name);
     name:=concat('ebno',name,'.dat');
     writeln('Reading data from file ',name);
     readdata(name, ycord, maxy, listends, sigma, stepsize);
     setup.sigma:=sigma;
     str(filenumber, filename);
     filename:=concat('R',filename,'.dat');
     fs:=setup.fs*1e3;
```

```
3: runtime:=(100/2.28e-2)/fs;
         4: runtime:=(100/1.25e-2)/fs;
         5: runtime: = (100/5.95e-3)/fs;
         6:runtime:=(100/2.38e-3)/fs;
         7: runtime: = (100/7.7e-4)/fs;
         8:runtime:=(100/1.91e-4)/fs;
         9:runtime:=(100/3.4e-5)/fs;
         10:runtime:=(100/3.8e-6)/fs;
         otherwise runtime:=0;
         end;
         setup.runtime:=runtime;
         compute(setup, statresult, stepsize, display, trap,
                  ercount, quit, qsk, ycord, listends);
         saveresult(setup, statresult, filename, display, trap,
                     ercount);
         filenumber:=filenumber+1;
         if quit='yes' then h:=stop;
         h:=h+1;
      end;
      if quit='yes' then
       begin
        slopecoefno:=5;
        goto 40;
       end;
      slopecoefno:=slopecoefno+1;
      setcoef(setup.slopecoef);
 40:end;
10:end;
procedure autocompute(var setup:menurecord;
                       var statresult:statrecord;
                           stepsize:real;
                           display, trap, ercount: string;
                           qsk:integer;ycord:samplearray;
```

case h of

```
listends:integer);
{automatically computes simulated runs over a range of
Eb/No}
         label 10,20;
         var filenumber,start,stop:integer;
             filename, quit: string;
             value:choice;
begin
    quit:='no';
     write('Enter initial file number (1-9999) ');
     readln(filenumber);
   str(filenumber,filename);
     filename:=concat('R',filename,'.dat');
     start:=3;
     stop:=7;
     setup.coefinc:='no';
10: writeln('Saving Files from ',filename);
    writeln;
     writeln(' 1) Start Eb/No (min 3dB) = ',start:4,' dB');
    writeln;
     writeln(' 2) Stop Eb/No (max 10dB) = ',stop:4,' dB');
     writeln;
     writeln(' 3) Increment Slope Coefficient Values
            ',setup.coefinc);
    writeln;
    writeln(' 4) Run');
    writeln;
     writeln(' 0) End ');
     writeln;
    write('ENTER ');
     readln(value);
     case value of
      0:quitread(quit);
```

```
1:setststp(start);
      2:setststp(stop);
      3:setcoefinc(setup.coefinc);
      4: run(setup, statresult, stepsize, display, trap, ercount,
        filename, qsk, ycord, listends, filenumber, start, stop);
     otherwise goto 10;
     end;
     if quit='yes' then goto 20;
     goto 10;
20: end;
procedure setquantbits(var quantbits:integer);
{sets number of quantizing bits}
    label 10;
    var realquantbits:real;
begin
10: Write('Enter number of quantizing bits required ');
     readln(realquantbits);
     quantbits:=round(realquantbits);
     if quantbits<1 then goto 10;
end;
procedure setmag(var mag:real);
{set magnitude of input signal}
    label 10;
begin
10: write('Enter magnitude of input signal ');
     read(mag);
     if mag<=0 then goto 10;
end;
```

```
procedure setdisplay(var display:string);
{set display on or off}
begin
   if display='no' then display:='yes'
     display:='no';
end;
procedure errortrapmenu(var trap:string);
{set error trap option}
  label 10;
  var value:choice;
begin
writeln;
    writeln('!!!!!!!!!INSERT DISK INTO DRIVE A - NOW
            !!!!!!!!!!!!!
    writeln;
    writeln(' 1) No trap ');
    writeln;
    writeln(' 2) Trap on cycle slip ');
    writeln;
    writeln(' 3) Trap on Symbol error');
    writeln;
    write(' ENTER ');
    readln(value);
    case value of
    1:trap:='No';
    2:trap:='Cycle slip';
    3:trap:='Symbol error';
    otherwise goto 10;
    end;
```

```
procedure seterrorcount(var ercount:string);
{set error count string}
begin
     if ercount='no' then
       ercount:='yes'
    else
      ercount:='no';
end;
procedure computemenu(var setup:menurecord;
                     var statresult:statrecord;
                     stepsize:real;
                     qsk:integer; ycord:samplearray;
                     listends:integer;
                             display,ercount,trap:string);
                     var
{setup menu for compute options}
      label 10,20;
      var value:choice;
begin
      quit:='no';
   10: writeln;
      writeln;
      writeln('************* PHASE ESTIMATOR COMPUTE
               MENU********* );
      writeln( 'Eb/No = ',setup.ebno:5,' dB,',' SIM time =
                ',setup.runtime:6:4,' sec,',
     ' Data = ',setup.dstate,',',' Type = ',
```

end;

```
setup.datatype);
writeln('Noise = ',setup.nstate,',',
' Frequency offset ',setup.fo:10:1,' Hz,',
' Symbol rate = ',setup.fs:6:1,' Khz');
writeln('Number of traps = ',setup.trapcount:4,',',
        ' Bit Error rate = ',
 setup.errate:10:6,',', ' Symbol Error Count =
  ',setup.errcount:4 );
writeln('Slope detector is ', setup.slope,'
                                             Mean
  filter output is ', setup.mean,
  ' Feedback bits in IIR = ',setup.bits:3);
writeln('Slope Coefficient = ',setup.slopecoef,
             Mean Coefficient = ',
        setup.meancoef);
writeln('Error noise mean = ',
        statresult.errormean*360/m:6:3 ,' deg',
   Error standard deviation = ',
 statresult.errordev:6:3, 'deg');
writeln('Sim. Noise S.D = ',
        setup.sigma*180/pi:6:3, ' deg',
 ' Est S.D = ',statresult.carrierdev :6:3,' deg');
writeln('***************************
        *********************
writeln(' 1) Number of quantizing bits ',
           setup.quantbits);
writeln;
writeln(' 2) Magnitude of input signal (0-1) ',
             setup.mag:6:2);
writeln;
writeln(' 3) Display Estimator Run Time Data ',
        display);
writeln;
writeln(' 4) Error Trap Data and save to disk,
           Trap on ', trap);
writeln:
writeln(' 5) Error rate Count ', ercount);
```

```
writeln(' 6) Compute');
        writeln;
        writeln(' 7) Auto compute');
        writeln;
        writeln(' 0) End');
        write('ENTER ');
        readln(value);
        case value of
        0: quitread(quit);
        1:setquantbits(setup.quantbits);
        2: setmag(setup.mag);
        3:setdisplay(display);
        4: Errortrapmenu(trap);
        5:seterrorcount(ercount);
        6:compute(setup, statresult, stepsize, display, trap,
          ercount, quit, qsk,ycord,listends);
        7:autocompute(setup, statresult, stepsize, display,
             trap,ercount,qsk,ycord,listends);
        otherwise goto 10;
        end;
        if quit='yes' then goto 20;
        goto 10;
     20:quit:='no';
end;
procedure estimatemenu(var setup:menurecord;ycord:samplearray;
                       var stepsize:real;
                       var qsk:integer;listends:integer);
       label 10,20;
       var value:choice;
           display, ercount, trap: string;
```

writeln;

```
statresult:statrecord;
```

begin

```
display:='no';
      trap:='no';
      ercount:='no';
      quit:='no';
      if setup.datatype='QPSK'then setup.ebno:=setup.esno-3
  10:
      else
       setup.ebno:=setup.esno;
      setup.errate:=0;
      setup.trapcount:=0;
      setup.errcount:=0;
      statresult.errormean:=0;
      statresult.errordev:=0;
      statresult.carrierdev:=0;
      statresult.carriermean:=0;
      writeln;
      writeln:
      writeln('*******PHASE ESTIMATOR MENU*******);
                          Eb/No = ',setup.ebno:5,'dB
      writeln('*
* ¹ );
                                                ',ver:6:2,'
      writeln('*
                               version
*');
      writeln('***********************************):
      writeln:
      writeln(' 1) Frequency offset ',setup.fo:10:1,'
Hz');
      writeln;
      writeln(' 2) Add noise ',setup.nstate);
      writeln;
      writeln(' 3) Add data ', setup.dstate,
setup.datatype:10);
      writeln;
      writeln(' 4) Filter is ',setup.filter);
      writeln;
```

```
writeln(' 5) Symbol Rate ',setup.fs :6:1,'KHz ');
       writeln;
       writeln(' 6) Simulated Run Time is ',
setup.runtime:10:6,' sec');
       writeln;
       writeln(' 7) Compute');
       writeln;
       writeln(' 0) End');
       writeln;
       write(' ENTER ');
       readln(value);
       case value of
       0: quitread(quit);
       1: setoffset(setup.fo);
       2: setnoise(setup.nstate);
       3: setdata(setup.dstate,setup.datatype,qsk);
       4: setfilter(setup);
       5: setsymbolrate(setup.fs);
       6: setruntime(setup.runtime);
       7: computemenu(setup, statresult, stepsize, qsk, ycord,
            listends, display, ercount, trap);
       otherwise goto 10;
       end;
       if quit='yes' then goto 20;
       goto 10;
20:end:
procedure callestimatemenu(listends:integer;stepsize,
                   sigma:real;ycord:samplearray;
                   var setup:menurecord);
         var qsk:integer;
begin
     setup.nstate:='no';
```

```
setup.dstate:='no';
    setup.datatype:='QPSK';
    qsk:=1;{set to qpsk}
    setup.fo:=0;
    setup.filter:='IIR';
    setup.fs:=256;{in kHz}
    setup.runtime:=3e-3;
    setup.quantbits:=6;
    setup.mag:=1;
    setup.slope:='ON';
    setup.mean:='ON';
    setup.slopecoef:='63/64';
    setup.meancoef:='31/32';
    setup.bits:=16;
    setup.sigma:=sigma;
    setup.refstepsize:=0.5;{ stepsize in degrees,min=0.5}
    setup.reflistends:=round(180/setup.refstepsize);
    estimatemenu(setup, ycord, stepsize, qsk, listends);
end;
procedure menu(var value:choice;var quit:string;
               sesno:string; var setup:menurecord);
{produces menu of choices}
begin
    quit:='no';
    Writeln;
    writeln;
    writeln('**********MENU***********');
    writeln('
                   Es/No = ', sesno);
    writeln('
                   version ',ver:6:2);
```

```
writeln;
     writeln('Please make slection');
     writeln;
     writeln;
     writeln(' 1) Readfile from disc.');
     writeln;
     writeln('
                2) Calculate Erfc.
                                     ');
     writeln;

 Phase Estimator performance.');

     writeln('
     writeln;
     writeln(' 0) End');
     writeln;
     write(' ENTER');
     readln(value);
end;
begin{main program}
     readbefore:=false;
     sesno:='NOT SET';
10:
     menu(value,quit,sesno,setup);
     if (readbefore=false) and ((value=2) or (value=3))
     then
      begin
       writeln('Warning:Must read from file first!!');
       waittime:=2;
       wait(waittime);
       goto 10;
     end
     else
       case value of
        1: readfile(listends, sigma, stepsize, name, quit,
           ycord, maxy, readbefore, esno);
        2:erfc(listends,stepsize,ycord);
        3:callestimatemenu(listends, stepsize, sigma, ycord,
            setup);
```

```
0: goto 20;
  otherwise goto 10;
end;
end;
setup.esno:=esno;
str(esno,sesno);
sesno:=concat(sesno,' dB');
case value of
    1:waittime:=0;
    2:waittime:=5;
    3:waittime:=0;
    0:waittime:=0;
end;
wait(waittime);
goto 10;
20:end.
```

## Plot Phase Statistics Program

This program reads data from the phase estimator simulation a .

the noise gemeration program to enable the PDF's of the phase variations to be plotted.

## Plot1-24.pas

```
program PlotPhaseStat(input,output);
{program reads data from named disc
                                          file and
                                                      plots
probability distribution of phase error}
       label 10,20;
       const ver= 1.24;
       type gsxint =0..32767;
            coord=real;
            plotarray=array[0..720] of coord;
            choice=0..10;
       var quit,magx:string;
           mag:integer;
              openworkstation(ident:gsxint);
procedure
                                                  external;
procedure
              closeworkstation;
                                                  external;
```

```
external;
procedure
              clearworkstation;
procedure setwindow(left,right,bottom,top:coord);
                                           external;
procedure setviewport(left, right, bottom, top:coord);
                                           external;
                                                    external;
procedure
              newpoly;
procedure polypoint(x,y:coord);
                                           external;
                                           external;
procedure drawpoly;
procedure clip;
                                           external;
procedure plotstring(x,y:coord;s:string); external;
                                                    external;
              stringheight(h:real);
procedure
procedure setgetmode(device, mode: gsxint); external;
procedure getstring(stringdev:gsxint;echo:boolean;
                                                    external;
                      characters:string);
    x,y:coord;var
procedure getvaluator(valdev:gsxint;var value:gsxint;
                      var terminator :char;
                      var status:gsxint); external;
procedure quitread(var quit:string);
begin
                                               quit:='yes';
     if
                quit='no'
                                   then
end;
procedure averageplot(var ycord:plotarray; var filend,
                       centreloc:integer;
                       var stepsize:real;var maxy:coord);
         label 10,20;
         var avecentre,centre,averend,averageover,i,h,
             n:integer;
             sum:real;
             averycord:plotarray;
begin
     averageover:=round(2/stepsize);
     if odd(averageover) = false then
       averageover:=averageover+1;
     stepsize:=averageover*stepsize;
     centre:= filend div 2;
     averend:=(filend+1) div averageover;
     avecentre:= (averend div 2);
     n:=avecentre;
     maxy:=0;
     h:=centre-(averageover div 2);
     while h<=filend do
        begin
        sum:=0;
        i:=0;
        while i<=averageover-1 do
          begin
          if h+i>filend then goto 10;
```

```
sum:=ycord[h+i]+sum;
            ycord[h+i]:=0;{clears ycord array}
10:
             i:=i+1;
        end:
        averycord[n]:=sum;
        h:=h+averageover;
        if averycord[n]>maxy then
        begin
          maxy:=averycord[n];
          centreloc:=n;
        end;
        n:=n+1;
     end;
     h:=centre- (averageover div 2)-1;
    {averages in negative direction starting from just
     below centre}
     n:=avecentre-1;
     while h>=0 do
        begin
        sum:=0;
        i := 0;
        while i<= averageover-1 do
          begin
          if h-i<0 then goto 20;
            sum:=ycord[h-i]+sum;
            ycord[h-i]:=0;
20:
             i := i+1;
         end;
        averycord[n]:=sum;
        h:=h-averageover;
        if averycord[n]>maxy then
         begin
          maxy:=averycord[n];
          centreloc:= n;
        end;
        n := n-1;
     end;
     for h:= 0 to averend do
       begin
       ycord[h]:=averycord[h];
       end;
       filend:=averend;
end;
procedure normalize(var ycord:plotarray;filend:integer;
                     var maxy:coord);
        var h:integer;
begin
    for h:= 0 to filend do
       ycord[h]:=ycord[h]/maxy;
   end;
```

```
maxy:=1; end;
procedure readfile(var filend,centreloc:integer;
                    var sigma:coord;
                    var stepsize:real;var name:string;
                          ycord:plotarray;var maxy:coord);
                    var
{reads data from named file}
         label 10:
         var listend,h:integer;
              checkok:boolean:
              infile1:text;
begin
  10:Writeln('File to be plotted ');
     readln(name):
      checkok:= checkfn(name);
     if checkok=false then goto 10;
     assign(infile1, name);
     reset(infile1);
readln(infile1, listend, stepsize, sigma);
     filend:= 2*listend;
     h:=0;
     while not eof(infile1) do
       begin
         readln(infile1,ycord[h]);
         if ycord[h]>maxy then
         begin
            maxy:=ycord[h];{find maximum value for y}
            centreloc:=h;
         end;
         h:=h+1;
       end;
      if h-1<> filend then
       writeln('errror in reading file');
      if stepsize<2 then
       averageplot(ycord, filend, centreloc, stepsize, maxy);
       writeln('max y =',maxy);
       normalize(ycord, filend, maxy);
end;
procedure
            datatostring(var
                                  result:string;indata:real);
{converts real data to string}
        var dataint,reslength,intlength:integer;
            intpart,fract:string;
begin
     dataint:=round(indata*100);
     str(dataint, result);
     reslength:=length(result);
      if reslength=1 then
      begin
         fract:=result;
```

```
result:=concat('0.0',fract);
      end:
     if reslength=2 then
      begin
      fract:=result;
      result:=concat('0.',fract);
      end;
      if reslength>=3 then
      begin
      intlength:=reslength-2;
       intpart:=copy(result,1,intlength);
       fract:= copy(result,intlength+1,2);
     result:=concat(intpart,'.',fract);
     end;
end;
procedure setscreen(maxy:coord; filend,mag:integer);
{sets up screen co-ordinates}
      var windowtop, windowright: coord;
begin
      windowtop:= 1.1*maxy;
      windowright:=1.1*filend/mag;
      setwindow(0,windowright,0,windowtop);
      setviewport(0,1,0,0.8);
end;
procedure draw_scale(maxy,sigma:coord;filend,centreloc,
                      mag:integer;stepsize:real);
{draw vertical scales on sceen}
           var x,centrex,y,stopx,starty,stopy:coord;
                prob:real;
                value,sprob:string;
                nmax, xsigscale, h, locbetweenline: integer;
begin
      stopx:= 1.1*filend/mag;
stopy:= 1.1*maxy;
      starty:=0.1*maxy;
      for h:=1 to 10 do
       begin
       newpoly;
        prob:= maxy*h/10;
          y:= starty+prob;
       polypoint(0,y); polypoint(stopx,y);
       drawpoly;
       datatostring(sprob,prob);
       sprob:=concat(sprob,' ');
       plotstring(1,y-maxy/40,sprob);
      end:
      centrex:= 1.1*centreloc;
      locbetweenline:=round(30/(stepsize*mag));
      nmax:= round(centrex/locbetweenline)-1;
```

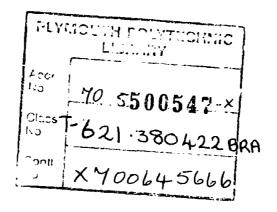
```
for h:=-nmax to nmax do
       begin
         x:=centrex+locbetweenline*h;
         newpoly;
         polypoint(x,starty); polypoint( x,stopy);
         drawpoly;
         xsigscale:=round(h*locbetweenline*stepsize);
         str(xsigscale, value);
         plotstring(x,starty-maxy/20,value);
      end;
      value:=' deg ',
      plotstring(0.5,0,value); end;
procedure draw axis(maxy, sigma: coord; filend, centreloc,
                    mag:integer;stepsize:real);
{draw axis for plot}
       var stopx,starty,stopy:coord;
begin
     starty:= 0.1*maxy;
     stopx:=1.1*filend/mag;
     newpoly;
     polypoint(0,starty);
                            polypoint(stopx,starty);
     stopy:=1.1*maxy;
     polypoint(stopx,stopy);
                                polypoint(0,stopy);
     polypoint(0,starty);
     drawpoly;
     draw scale(maxy, sigma, filend, centreloc, mag, stepsize);
end;
procedure draw data(ycord:plotarray;maxy:coord;
                     filend, mag, centreloc: integer);
{reads data in plot array and plots on workstation}
         var h,short:integer;
             oldx,oldy,startx,starty,x,y:coord;
begin
      h:=centreloc-(centreloc div mag);
      startx:=0.05*filend/mag;
      starty:=0.1*maxy;
      oldx:=startx;
      oldy:=starty;
      while h<filend/mag do
      begin
      short:=0;
       newpoly;
       polypoint(oldx,oldy);
       while short<10 do
         begin
            x:=h+startx;
            y:=ycord[h]+starty;
```

```
oldx:=x;
            oldy:=y;
             polypoint(x,y);
            short:=short+1;
            h := h+1;
             if h>= filend then short:=10;
        end;
         drawpoly;
       end; end;
procedure addtitle(name,title:string;siqma,stepsize:real);
{adds title to plot}
      var sigmas:string;
          Istepsize,isigma:integer;
          echo:boolean;
begin
    echo:=true;
    setwindow(0,1,0,1);
    setviewport(0,1,0.82,1);
title:=concat('Title = ',title);
    plotstring(0,0.8,title);
    datatostring(sigmas, sigma);
    sigmas:=concat('RMS phase error = ',sigmas,' degs');
    plotstring(0,0.5,sigmas);
    name:=concat('File=',name);
    plotstring(0,0.2,name);
end;
procedure plotfile(mag:integer);
       var sigma1,maxy:coord;
           ycord:plotarray;
           title, name: string;
           sigma, stepsize: real;
           filend, centreloc, h:integer;
begin
    openworkstation(1);
    clearworkstation;
    closeworkstation;
    maxy:=0;
    readfile(filend,centreloc,sigma,stepsize,name,ycord,-
             maxy);
    sigma1:= sigma/stepsize;
    writeln('Title ?');
    readln(title);
    openworkstation(1);
    clearworkstation;
    clip;
```

```
setscreen(maxy,filend,mag);
    draw axis(maxy, sigma1, filend, centreloc, mag, stepsize);
    draw data(ycord, maxy, filend, mag, centreloc);
    addtitle(name, title, sigma, stepsize);
end;
procedure plotsingle(mag:integer);
{plots single set of data to screen}
         label 10,20;
       var terminator:char;
           value, status: gsxint;
begin
        plotfile(mag);
     setviewport(0,1,0,1);
10:plotstring(0.8,0,'MENU ?');
        setgetmode(1,2);
        getvaluator(1, value, terminator, status);
        case terminator of
         'Y': goto 20;
         'y': goto 20;
         'n':quitread(quit);
          'N':quitread(quit);
         otherwise goto 10;
         end:
20:
      closeworkstation;
end;
procedure plotmulti;
{multiple plot program will go in here}
begin
 writeln('multiplot');
end;
procedure magnifx(var magx:string;var mag:integer);
{magnifies area of display around centre}
      var temp:string;
begin
    if magx= 'X1'then
     begin
      temp:='X2';
      mag:=2;
    end;
    if magx= 'X2'then
    begin
```

```
temp:='X3';
     mag:=3;
   end;
   if magx= 'X3'then
   begin
     temp:='X5';
     mag:=5;
   end;
   if magx= 'X5'then
   begin
     temp:='X10';
     mag:=10;
   end;
   if magx= 'X10'then
   begin
     temp:='X1';
     mag:=1;
   magx:=temp; end;
procedure menu(var magx,quit:string;mag:integer);
{menu for plot setup }
     label 10,20;
     var value :choice;
begin
     if quit='yes' then goto 20;
  10:writeln;
     writeln('
                  Plot Phase
                            Noise statistics');
     writeln('
                       version ',ver:6:2);
     writeln(' CGA version ');
     writeln;
     writeln('1) Plot single file');
     writeln;
     writeln('2) Plot Multiple files');
     writeln;
     writeln('3) Magnification X-axis ',magx);
     writeln;
     writeln('0) End ');
     writeln;
write( 'ENTER ');
     readln(value);
     case value of
     0:quitread(quit);
     1:plotsingle(mag);
     2:plotmulti;
     3:magnifx(magx,mag);
     otherwise goto 10;
     end;
```

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```
if quit='yes' then goto 20;
  goto 10; 20: end;

begin{main program}
    quit:='no';
    magx:='X1';
    mag:=1;

10: menu(magx,quit,mag);
    if quit='yes' then goto 20;
    goto

20:end.
```