Electrolytic Conductance & Ionic Association of Potassium, Tetraphenylarsoniurn & Tetraphenylphosphonium Picrates in Methanol- Water Mixtures

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Electrolytic conductances of potassium picrate (KPi), tetraphenylarsonium picrate (Ph.AsPi) and tetraphenylphosphonium picrate (Ph._IPPi) have been determined at 25° C in methanol-water mixtures containing approximately 60, 70, 80, 90 and 100 wt $\frac{6}{6}$ methanol. In all the cases, limiting equivalent conductances, Λ_0 , and ion-pair association constants have been derived using the Shedlovsky function. For three of the solute-solvent systems, it is also possible to obtain results by Fuoss' parametric analysis. Using the present and the literature data, a comparison has been made between the conductance parameters derived from the Fuoss-1974 parametric analysis and those from earlier conductance functions. Also reported are the values of λ_0 , Walden products and Stokes radii for the single ions in 100% and 64.0% methanol. Variation of the Stokes radii with solvent composition is discussed in terms of structural and solvation effects.

M UCH work in our laboratory has been done on the determination of transfer free energies of electrolytes containing tetraphenylarsonium $(Ph₄As⁺)$, tetraphenylphosphonium $(Ph₄P⁺)$ triiso amyl-n-butylammonium $(TAB⁺)$ and tetraphenylborate $(BPH₄)$ as reference ions. The free energies for the transfer of an electrolyte from a reference medium (usually water) to other media are usually expressed in the form of transfer activity coefficients (medium effects)! and calculated from thermodynamic solubility products in water and in the nonaqueous solvent of interest. In solvents where ion pairing is appreciable it is necessary to determine the degree of ionic association before a solubility product can be eavluated from solubility data. Therefore, the primary objective of the present study is to determine the degree of ionic association for the title electrolytes in those methanol-water solvents where it is expected to be appreciable. Earlier communications from this laboratory reported analogous conductance studies for these and other electrolytes in ethanol-water solvents^{2,3}. Another objective of the present study is to gain additional insight into the magnitude of ion size parameters and limiting transference numbers of the ions and the manner in which they vary with the solvent medium in the methanol-water system.

Potassium picrate has been included in this study as a convenient bridge for the correlation of the properties of the reference ions and the picrate ion with those of the more common ions and also because its conductance parameters in methanol could be compared with literature values.

Materials and Methods

The preparation and purification of potassium picrate' (KPi) and of tetraphenylarsonium picrate $(Ph₄ AsPi)$ and tetraphenylphosphonium picrate $(Ph₄)$ PPi ³ as well as the purification of methanol⁴ have been described earlier. The method of preparing methanol-water mixtures of accurately known composition was analogous to that of preparing ethanol-water mixtures². Deionized water with a specific conductance of the order of 3×10^{-7} mho cm^{-1} was used.

The apparatus and procedure for conductance measurements were essentially the same as previously described", except that a Wayne-Kerr model B-224 bridge was used. Temperature stability in the 25.00°C bath was improved by circulating water at 25.00°C through the coils. The conductance cell, filled with slightly platinized platinum electrodes, has a cell constant of $0.0095422 + 0.000018$ as determined from measurements with 0.03-0.07 *M* aqueous KCI solutions using the equation of Chiu and Fuoss. Preparation and transfer of solutions involving anhydrous methanol were carried out in a dry box.

Results

Table I summarizes the relevant physical properties of the methanol-water solvents actually employed. The wt $\%$ methanol (designated as *w*), was obtained from the measured solvent density, *do,* by extrapola-

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TABLE 4 - CONDUCTANCE OF Ph₄PPi IN METHANOL-WATER MIXTURES AT 25°C

100% Methanol

					90.0%	
Run_1		Run 2			Methanol	
10 ⁴ C	Λ	10° C	Λ	10^4 C	Λ	
1.7983 2.8839 4.0739 6.2779 7.1025 7.2977	82.67 81.46 80.46 78.84 78.35 78.27	1.2301 2.0150 4.1412 4.6975 5.0564	83.39 82.44 80.58 80.18 79.84	1.9897 2.4488 2.9150 4.2529 7.5417 7.7025	63.12 62.80 62.44 61.67 60.23 60.21	
80.2% Methanol		70.0% Methanol			60.1% Methanol	
2.3642 3.2507 4.4500 5.5009 6.3441	50.87 50.51 50.04 49.70 49.39	2.3681 2.8857 4.1581 4.9959 5.6451 5.9499	42.43 42.29 41.88 41.66 41.53 41.47	2.8550 3.6346 3.9198 4.3531 5.1526.	39.02 38.84 38.81 38.65 38.48	

tion from a large-scale graph of the literature values⁵ of d_0 versus wt $\%$ methanol. Similarly interpolated from literature data⁵ were the viscosity η_0 and the dielectric constant, *D,* for each of the mixtures. Tables 2-4 list the molar concentrations, C, and the equivalent conductances, Λ of the various electrolytes in different compositions of methanol-water mixture.

An attempt has been made to interpret all of our conductance data by means of the parametric analysis published by Fuoss⁶ using his computer programme for the calculation? of three parameters viz. the limiting equivalent conductance (Λ_0) , the ion-pair association constant, (K_A) and the distance parameter *(R)* the latter is the distance from the center of the cation of an ion pair within which a unique partner can be found for a paired ion. Unfortunately, the Fuoss parametric analysis gave results for only three of the solvent-electrolyte systems 'from the present study and for only three additional sets of conductance data reported earlier from this laboratory^{2,3}. It is significant that Fuoss' parametric analyses of our data was successful mostly for solutions in anhydrous alcohols, where the solvent correcti n to tc tal conductance was of the order of Sorrecti in to tetal conductance was of the order of
I ppt or less. In aqueous alcohol mixtures, where the solvent correction was of the order of 10-50 times greater, the precision of conductance data was undoubtedly reduced.

Consequently, values of Λ_0 and K_A for all the systems were derived using the Shedlovsky equation⁸:

$$
\frac{1}{\Lambda_2(z)} = \frac{K_A C \Lambda f^2 \pm S(z)}{\Lambda_0^2} + \frac{1}{\Lambda_0} \qquad \qquad ...(1)
$$

aExcluded from log K_A versus $1/D$ plots.

where f_{\pm} is the mean ionic activity coefficient estimated from the Debye-Hückel limiting law using successive approximations with respect to the degree of dissociation. The Shedlovsky function is defined as

$$
S_{(z)} = \{z/2 + [1 + (z/2)^{2}]^{1/2}\}^{2},
$$

where $z = S\Lambda_0^{-3/2}(C\Lambda)^{1/2}$ and $S = \alpha\Lambda_0 + \beta$

In the above expressions,

$$
\alpha = \frac{0.8204 \times 10^8}{(DT)^{3/2}}
$$
 and $\beta = \frac{82.501}{\eta (DT)^{1/2}}$

All calculations were carried out on an IBM 370/145- TABLE 5 - CONDUCTANCE PARAMETERS OBTAINED BY THE COMPUTER USING FORTRAN programmes. The con-
SHEDLOVSKY EQUATION
ductance parameters and constants obtained by the ductance parameters and constants obtained by the Shedlovsky equation are summarized in Table 5. A comparison of the Λ_0 and K_A values obtained by the Shedlovsky equation and by Fuoss' parametric analysis for the conductance data from this laboratory is shown in Table 6. In Table 7, a further comparison is made of Λ_0 and K_A values for KP in 100% methanol calculated by three different equations from the high precision data of Coplan and Fuoss⁹.

Discussion

Walden products and Stokes radii - It is evident from the comparative results in Tables 6 and 7 that the values of Λ ⁰ remain essentially the same regardless of the conductance function from which they are derived. Therefore, it is convenient to consider first any information obtainable from the Λ_0 's, as it should be virtually free of ambiguity. Table 5 lists the limiting co rductance, viscosity, and Walden products for the electrolytes. More informative, however, from the point of view of ionsolvent interactions are the Walden products of single ions, which can be calculated when limiting equivalent conductances forthe single ions are known. Stokes radii for the ions, R_s [,] can then be calculated from the relationship,

TABLE 6 - COMPARISON OF Λ_0 and K_A Values Obtained from the Shedlovsky Equation and via Fuoss Para-METRIC ANALYSIS[®]

[Data from this Laboratory]

 (a) Calculated from only four best points, omitting point 4.

(b) Obtained by the SCAN method"?". *(c)* Calculated from the Fuoss-Onsager equation'! by the x-y method. TABLE 7 - COMPARISON OF CONDUCTANCE PARAMETERS FOR KPi IN 100% METHANOL OBTAINED BY DIFFERENT EQUATIONS

 D_{min} of C_{min} and D_{min}

TABLE 8 - LIMITING EQUIVALENT CONDUCTANCES, WALDEN PRODUCTS AND STOKES RADII OF SINGLE IONS

(a) $\eta_{04\cdot 0} = 1.338$ cp
(b) The limiting transference numbers of the cations refer to the picrates. (c) Λ_0 (KPi) $-\lambda_0$ (K⁺)
(d) Λ_0 (Ph₄AsPi) $-\lambda_0$ (Pi⁻)
(e) Λ_0 (Ph₄PPi) $-\lambda_0$ (Pi⁻)

 R_8 (in \AA) = $\frac{0.8194 \text{ Z}}{\Lambda_0 \eta_0}$ $...(2)$

where Z is the ionic charge.

Accurate values of λ_0 (+ are available for
100% methanol (= 52.38)¹² nd 64.0% methanol (50.0 mol %). Combining it with Λ_0 (KPi) = 99.32, which is an average of our own and literature data, yields λ_0 (Pi-) = 46.94. Values of λ_0 for
Ph₄As⁺ and Ph₄P⁺ ions are then obtained from the λ_0 's of the corresponding picrates determined
in this study. In 64.0% methanol, $\lambda_0(K^+)$ = 38.06 is obtained by combining Λ_0 (KCl) = 75.10 (ref. 13) and t_{+} (in KCl) = 0.5068 (ref. 14). The λ_0 's for other ions in 64.0% methanol are calculated by difference from those of the picrates interpolated from the results of the present study. The interpolated Λ_0 's are: KPi = 61.3; Ph₄AsPi = 39.7 and
Ph₄PPi = 41.5. All the parameters calculated for single ions, including transference numbers, Walden

products and Stokes radii (from Eq. 2) are compiled on Table 8.

Appreciable variation in the Walden product and therefore the Stokes radius of an ion as a function of the solvent is generally regarded as an index of specific ion-solvent interactions. including structural effects. A reasonable constancy of the above parameters in different solvents as well as an approximate agreement between crystallographic and Stokes radii is interpreted as indicative of absence of specific solvation effects. The data in Table 8 shows that the Stokes radii of the Ph₄As⁺ and Ph₄P⁺ ions differ little between 100% and 64.0% methanol ($R_B = 3.93$ and 3.72, respectively, for
Ph₄As⁺ and 3.83 and 3.35 for Ph₄P⁺). The van der
Waals' radii are estimated to be 4.30 (ref. 15) and 4.28 (ref. 16) for Ph_4As^+ and 4.28 for Ph_4P^+ (ref. 16). No conductance data are available for the Ph_aP+ and Ph₄As⁺ ions in water, but a comparison between methanol and water can be made for their structural analog, the tetraphenylborate anion. Thus, in
methanol, $\lambda_0(BPh_4^-) = 36.50$ (ref. 12) and in water, 19.69 (ref. 17), corresponding Stokes radii are 4.13 and 4.67 respectively. Similar values for
the Stokes radii of the BPh₄ ion were reported¹⁸ in acetonitrile (4.11) , nitrobenzene (4.12) and nitromethane (4.14) . The van der Waal's radius of the BPh₄ ion has been estimated^{15,16} to be 4.21. The small increase in the Stokes radius in water, relative to the van der Waals' radius, undoubtedly reflects the well-known hydrophobic structuremaking characteristic of bulky organic ions.

Evidently, the tetraphenyl ions, which form the basis for a number of extra thermodynamic assumptions requiring a relative 'ideality' with respect to solvation effects are indeed free of any major ionsolvent interactions that would be reflected in the variation of their Stokes radii.

In contrast to tetraphenyl ions, the K^+ ion exhibits a considerable variation in its Walden products and Stokes radii with the solvent, λ_0^+ η_0 in 64.0% methanol being 44% greater than in 100% methanol. As a result, the Stokes radius of the K+ ion drops from a value of 2.88 in methanol to 1.61 in 64.0% methanol. In water, $\lambda_0(K^+) = 73.55$ so that using $\eta_{B_0} = 0.8903$ cp, the Walden product becomes 0.6548 and the Stokes radius 1.25, which is below the crystallographic radius of 1.33. The above variations can be interpreted in terms of the effect of the K^+ ion on the structure of solutions. In aqueous solutions, the K⁺ ion acts as a structurebreaker and the reason why its mobility is high relative to that of other solutes of comparable radii lies in the fact that a structure-breaking ion decreases the local viscosity by breaking some of the hydrogen bonds in the three-dimensional network of liquid water. No such effects are observed in nonaqueous solvents, which are generally less structured than water, and in those solvents the mobility of structurebreaking ions is not excessive.

Kay and Evans¹⁹ found that Walden products of structure-breaking ions in water decreased with increasing temperature and pressure. Since the effect of increased temperature and pressure is to

cause a partial breakdown of the three-dimensional water structure, it means that as the temperature or the pressure is increased the ions become less effective structure breakers and their mobility decreases¹⁹. There is evidence that addition of a nonaqueous solvent to water causes a breakdown in the water structure as well. This structure-breaking has been invoked to interpret the sharp increase in basicity, resulting in a basicity maximum, upon addition of ethanol, acetone or dioxane to water, as measured by the Hammett acidity function²⁰, H_0 . A similar pattern of basicity is reflected in the variation of the transfer activity coefficients for the proton, estimated in this laboratory for the entire range of ethanolwater^{21,22} and methanol-water²² solvents. The basicity maxima, which for the above alcohols occur in the region of 60-80 wt $\frac{\%}{\%}$, are believed to correspond to regions of minimum solvent structure and this is where one would expect the K⁺ ion to behave most 'ideally' on reference to Stokes law. Indeed, it might not be fortuitous that at 64.0% methano $R_8 = 1.61$, though there undoubtedly exists a methanol-water mixture where the correspondence to the crystallographic radius of 1.33 is even closer. As the solution becomes richer in methanol, solvation by methanol molecules gradually becomes a factor and the effectiveness of K^+ as a structure maker (in alcoholic media) is reflected in the gradual increase of the $R_{\rm g}$. A contributing cause to this is the dielectric relaxation effect, which may be partly responsible for increase in the Stokes radius of the picrate ion with increase in methanol content although specific solvation of the picrate ion by methanol molecules via strong dispersion interactions is well known²³ and is likely to be a factor here.

It was shown by Fuoss²⁴ and later by Zwanzig² that even in the absence of specific solvation, Walden products vary with the solvent dielectric constant due to the dielectric relaxation effect, which opposes the motion of ions. Fuoss derived a relationship between the Stokes radius in a real solvent of dielectric constant *D* and *R •••,* the hydrodynamic radius of an ion in a hypothetical solvent of infinite dielectric constant, where electrostatic forces would be reduced to $zero^{24}$:

$$
R_{\rm s}D = DR_{\infty} + B \qquad \qquad \ldots (3)
$$

Equation (3) was applied to our data by interpolating the values of ionic transference numbers, t_{+} and $t_$, for each solvent composition at which the Λ_0 s of the title electrolytes were determined and the Walden products and the Stokes radii of single ions were then calculated on their basis. Plots of *R.D* versus *D* are roughly linear for all the ions. R_{∞} values calculated by the method of least squares are: 3.53 (Ph_4As^+), 2.49 (Ph_4P^+) and for Pi^- 1.55 (from Ph_4 PPi), 1.59 (from Ph_4 AsPi) and 1.69 (from KPi). It is significant that Eq. (3) is inapplicable to the $K⁺$ ion, yielding a negative value of R_{∞} , which has no physical meaning. Evidently, structural and other solvation effects overwhelm the dielectric relaxation effect in this case. With the exception of the $Ph₄As⁺$ ion, the remaining ions have R_{\bullet} values much smaller than the ion sizes

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normally associated with them. This suggests that in methanol -water media, Eq. (3) cannot account fully even for the behaviour of the less solvated ions.

Association constants and ion-size parameters - In Table 6 a comparison is made between the values of association constants *KA* obtained by the Shedlovsky equation and by Fuoss' parametric analysis using the data from this laboratory. In order to ascertain that the above comparison is not distorted due to the relatively lower precision of our data, a similar comparison was made in Table 7 for the *KA* values derived by the two functions from the highprecision data of Coplan and Fuoss⁹. Excellent agreement is observed between the *KA* values for KPi in methanol obtained by us and in the former study⁹. It may be seen that K_A values calculated by Fuoss' parametric approach are always larger than those derived by the older Shedlovsky or Fuoss-Onsager functions. This is a consequence of a broader definition of ion pairing in the Fuoss parametric analysis⁶, where all ions that find a unique partner between the contact distance *a* and the distance parameter *R* are considered to be associated. *R* is the radius of a sphere centered at the cation of the ion-pair within which not only electrostatic attraction, but also other specific short-range interactions, both ion-ion and ion-solvent, take place. Beyond the' distance *R,* the solvent can be treated as a continuum. The above definition of *R* suggests that it should correspond closely to the distance of dielectric saturation, within which the solvent properties are modified by the ionic field. It is estimated that in methanol dielectric saturation extends to distances of up to 15\AA from the center of an ion²⁶ The agreement between this estimate and the *R* values of 14 and 16 for KPi in methanol (Table 7) is remarkable. The *R* values for methanol solutions obtained in this study are somewhat higher (21.5) and might reflect experimental errors. It is noteworthy that the increase in *KA'S* calculated by the Fuoss analysis" relative to the Shedlovsky function appears to vary with the dielectric constant of the solvent. Thus, for 60.1 % methanol *(D=51.55)* the increase is 76 %, for methanol *(D=* 32.64) the increase is \sim 30% and for ethanol ($D = 24.3$) it is only \sim 10% (Table 6). This may be illustrative of a phenomenon pointed out by Fuoss⁶ that K_A in solvents of lower dielectric constant is determined primarily by the contact distance *a* and is insensitive to the distance *R*. Thus, in solvents of lower dielectric constant, K_A can be adequately formulated by the classical Bjerrum theory⁶, where ions are considered paired within the distance from *a* to $e^2/2DkT$; in the latter *e* is electronic charge, *k* is the Boltzmann constant and *T* is absolute temperature.

The association constants obtained by the Shedlovsky function in this study have been analyzed by the classical relationship 2 :

$$
\log K_A = \log K_A^{\circ} + \frac{e^{\theta}}{2.203 \text{ a } DkT} \qquad ...(4)
$$

Plots of log K_A versus $1/D$ are approximately linear for Ph₄AsPi and Ph₄PPi, but exhibited a pronounced concave-down curvature for KPi at high

methanol contents, so that here a linear plot could be fitted only in the range of $60-90\%$ methanol. The values of the contact distance *a* (in A) obtained via Eq. (4) are 9.87 for Ph_4AsPi , 9.85 for Ph_4PPI and 2.84 for KPi. On the basis of our understanding of ion sizes, the first two values are much too high, unless we invoke the possibility of solvent-separated ion-pairs. The latter, however, must be weighed against the possibility that we may be dealing here with an artifact resulting from the shortcomings of the Shedlovsky function. On the other hand, the ion-size parameter for KPi is very reasonable. However, the relative magnitudes of the association constants of KPi and the picrates of the tetraphenyl ions are determined primarily by the pre-exponential term K_A° , which is 0.165 for KPi, 10.2 for Ph₄AsPi and 9.56 for Ph₄PPi. K_A° is determined to a large extent by the difference in the solvation energy of the free ions and the corresponding ion pairs'", The low value of K_A° for KPi relative to those for Ph₄PPi and Ph₄AsPi reflects the much greater solvation of the K⁺ ion as opposed to the Ph₄As⁺ and Ph₄P⁺ ions. Additionally, strong dispersion forces between the tetraphenyl cations and the picrate anion would tend to increase the $K_A s$ beyond their values predicted from coulombic considerations.

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