

# Hybrid Photonic Crystal Fiber Sensing of High Hydrostatic Pressure

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## ABSTRACT

The opto-mechanical response of Hybrid Photonic Crystal Fiber (HPCF) with Ge-doped inclusions is numerically modeled for high hydrostatic pressure sensing purpose. A typical photonic crystal fiber (PCF) consists of a silica solid-core and a cladding with a hexagonal lattice of air-holes. The HPCF is similar to the regular PCF, but a horizontal line of air-holes is substituted by solid high index rods of Ge-doped silica. The optical guidance in HPCFs is supported combining two physical effects: the modified total internal reflection and the photonic bandgap. In such fibers, the Ge-doped inclusions induce residual birefringence. In our analysis, we evaluate the susceptibility of the phase modal birefringence and group birefringence to hydrostatic pressure. The analyses were performed at a photonic bandgap with central wavelength near to 1350 nm. The polarimetric pressure sensitivity is about 10 rad/MPa x m at  $\lambda = 1175$  nm.

**Keywords:** Fiber Optic Sensor, Pressure Sensor, Birefringence, Photonic Bandgap, Photonic Crystal Fiber, Microstructured Optical Fiber

## 1. INTRODUCTION

Hybrid Photonic Crystal Fiber (HPCF) is a novel type of photonic crystal fiber (PCF) that supports optical guidance by two physical effects: the modified total internal reflection (mTIR) and photonic bandgap (PBG) [1-4]. The HPCF is composed of air-holes and Germanium-doped silica rods disposed around an undoped silica core. The air-holes are arranged in a hexagonal lattice as in index-guiding PCFs, whereas the high-index rods replace a single row of air holes along one of the PCF axes. The Figure 1 shows the geometric design of HPCF, where along y-axis the core has a higher refractive index than the effective refractive index of the cladding, so along this axis light can be guided by the mTIR effect from two half-spaces of microstructured silica. On the other hand, along the x-axis mTIR is not possible, since the cladding rods have a higher index than the core. In this case, confinement only occurs in restricted bands of wavelength (photonic bandgaps).

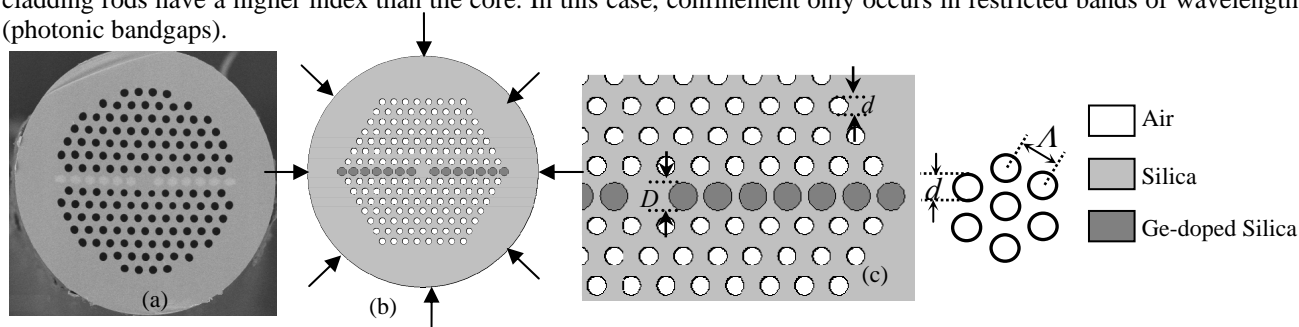


Figure 1. Hybrid photonic crystal fiber design. (a) Fabricated HPCF. (b) HPCF geometric model and applied hydrostatic pressure. (c) Main geometric parameters of the microstructure. The HPCF geometric parameters are:  $D = 6.38 \mu\text{m}$ ,  $d = 4.34 \mu\text{m}$  and  $\Lambda = 8 \mu\text{m}$ .

## 2. MODELLING METHOD

The numerical analyses were realized by a weakly coupled scheme to model the opto-mechanical response of HPCF. The residual induced stress, caused by the different thermal expansion coefficients of silica and Ge-doped silica, and the mechanical displacements consequence of the hydrostatic applied pressure are considered in the plane strain approximation. From the displacements is possible to determine the distribution of the normal stresses in the cross

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section of the fiber, and by the elasto-optic effect, that couples the mechanical stress to the optical index of refraction, is possible to evaluate the anisotropic profile of refractive indexes in the silica and the Ge-doped regions. From the new refractive indexes profiles we evaluate the optical propagation characteristics by the modal analyses based on the solution of full vectorial Helmholtz equation. In the opto-mechanical coupled analysis it was used a commercial finite element program (COMSOL). To the stress calculations were used Lagrange type finite elements and to the optical modal analyses were used vector finite elements (edge elements). An anisotropic cylindrical Perfectly Matched Layer (PML) was used as the domain truncation technique in the optical analyses.

The analyzed HPCF has high index inclusions of Ge-doped silica that causes residual stress and induced birefringence during the fabrication process. To model the residual stress is necessary to know the mechanical properties of Ge-doped silica that depends of the GeO<sub>2</sub> concentration. In this study we considered Ge-doped rods with parabolic profile of refractive index. The main mechanical and optical properties of Ge-doped silica as function of the GeO<sub>2</sub> concentration are [5-17]:

$$N_{dop} = (1 - X_{mol}) \cdot N_{SiO_2} + X_{mol} \cdot N_{GeO_2}, \quad (1)$$

$$N_{dop}(r) = N_{dop}^{max} \cdot \left[ 1 - 2 \cdot \Delta_N (r/a)^2 \right]^{1/2}, \quad \text{with} \quad \Delta_N = \left\{ \left( N_{dop}^{max} \right)^2 - N_{SiO_2}^2 / 2 \cdot \left( N_{dop}^{max} \right)^2 \right\}, \quad (2)$$

$$X_{mol}(r) = (N_{dop}(r) - N_{SiO_2}) / (N_{GeO_2} - N_{SiO_2}), \quad (3)$$

$$\alpha_{dop} = \alpha_{SiO_2} + \alpha_{GeO_2} \cdot X_{mol}, \quad (4)$$

$$\alpha_{dop}(r) = \alpha_{dop}^{max} \cdot \left[ 1 - 2 \cdot \Delta_T (r/a)^2 \right]^{1/2}, \quad \text{with} \quad \Delta_T = \left\{ \left( \alpha_{dop}^{max} \right)^2 - \alpha_{SiO_2}^2 / 2 \cdot \left( \alpha_{dop}^{max} \right)^2 \right\}, \quad (5)$$

$$T_{ann}^{dop}(r) = T_{ann}^{SiO_2} - 1000 \cdot X_{mol}(r), \quad (6)$$

$$E_{dop}(r) = (1 - 0.8 \cdot X_{mol}(r)) \cdot E_{SiO_2}, \quad (7)$$

$$\nu_{dop}(r) = (1 - 0.50 \cdot X_{mol}(r)) \cdot \nu_{SiO_2}, \quad (8)$$

where  $N$  represent the refractive index to the materials SiO<sub>2</sub> or GeO<sub>2</sub>,  $N_{SiO_2}$  is evaluated by the Sellmeier equation,  $N_{dop}$  is the refractive index of Ge-doped silica,  $N_{dop}^{max} = 1.023 N_{SiO_2}$ ,  $X_{mol}$  is the molar fraction of GeO<sub>2</sub>,  $\alpha_{SiO_2} = 5.5 \cdot 10^{-7}$  and  $\alpha_{GeO_2} = 1.04 \cdot 10^{-5}$  are the thermal expansion coefficients of silica and GeO<sub>2</sub>,  $T_{ann}$  is the annealing point,  $T_{ann}^{SiO_2} = 1130 \text{ }^\circ\text{C}$ ,  $E$  is the Young's module,  $E_{SiO_2} = 72.5 \text{ GPa}$  and  $E_{GeO_2} = 43.3 \text{ GPa}$ ,  $\nu$  is the Poisson ratio,  $\nu_{SiO_2} = 0.165$  and  $\nu_{GeO_2} = 0.197$ .

Taken into account the elasto-optic effect is possible to represent the refractive index changed by the stresses as:

$$N_1 = N + C_1 \sigma_1 + C_2 (\sigma_2 - \sigma_3), \quad N_2 = N + C_1 \sigma_2 + C_2 (\sigma_1 - \sigma_3), \quad N_3 = N + C_1 \sigma_3 + C_2 (\sigma_1 - \sigma_2), \quad (9)$$

where  $N$  is the refractive index of not stressed material (silica or Ge-doped silica),  $C_1$  and  $C_2$  are the stress-optic coefficients and  $\sigma_1$ ,  $\sigma_2$  and  $\sigma_3$  are the principal components of the induced stress. For PCFs, considering the uniformity of the glass composition, the axial stress  $\sigma_3 = 0$ . The principal stress components can be evaluated by  $\sigma_{1,2} = 0.5 \left\{ (\sigma_x + \sigma_y) \pm \left[ (\sigma_x - \sigma_y)^2 + 4 \tau_{x,y}^2 \right]^{1/2} \right\}$ , however the contribution of shear stress  $\tau_{x,y}$  is relatively small in the core region and its neighborhood and it will be neglected in this work ( $N_1 \equiv N_x$ ,  $N_2 \equiv N_y$ , and  $N_3 \equiv N_z$ ).

The residual stress and the applied hydrostatic pressure change the isotropic materials to non-homogeneous anisotropic materials leading to a material birefringence distribution. As a consequence of material birefringence, the two linearly polarized fundamental optical modes (FM<sub>x</sub> and FM<sub>y</sub>) present phase birefringence (B<sub>p</sub>). The material birefringence, the phase birefringence, and the group birefringence (B<sub>g</sub>) can be defined by:

$$B_m = (C_1 - C_2) \cdot (\sigma_x - \sigma_y), \quad B_p = n_{eff_x} - n_{eff_y}, \quad B_g = B_p - \lambda (dB_p / d\lambda), \quad (11)$$

where  $n_{eff}$  is the effective index of fundamental optical modes.

### 3. RESULTS

The Figures 2(a) and 2(b) present the material birefringence, induced by residual stress and applied pressure, near the fiber's core in the x and y-axis, respectively. Figures 2(c)-2(d) show the material birefringence induced by the residual stress ( $P = 0$  bar) and induced by both the residual stress and the hydrostatic applied pressure ( $P = 500$  bar), respectively. The effect of applying hydrostatic pressure is to decrease  $B_m$  in x direction, but in the y-axis the pattern of  $B_m$  is modified increasing its value in the center core and decreasing near the space between two air-holes above and below the core. The differential effect of pressure over  $B_m$  will affect differently the  $FM_x$  and  $FM_y$  modes.

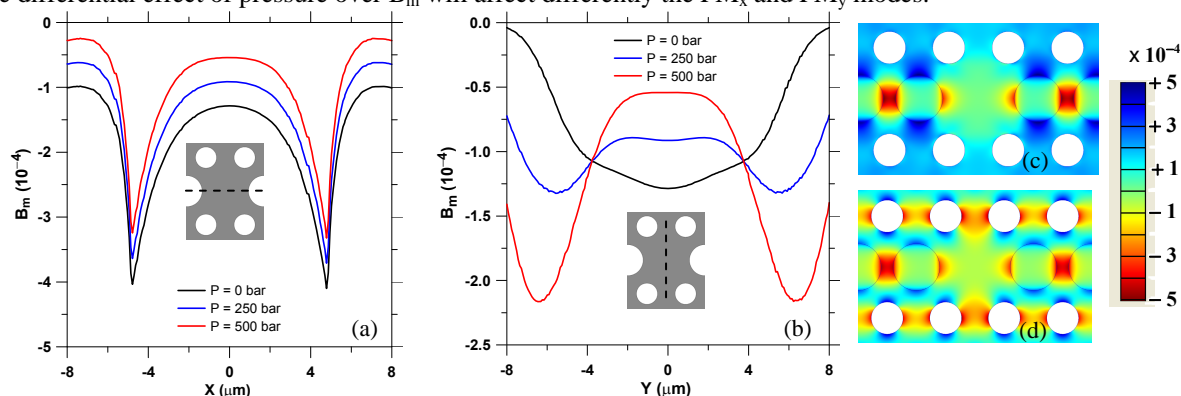


Figure 2. Material birefringence near the fiber's core for  $P = 0, 250$  and  $500$  bar. (a)  $B_m$  along the x-axis. (b)  $B_m$  along the y-axis.

The Figure 3(a) presents the spectral transmission at the bandgap with central wavelength  $\sim 1350$  nm and  $n_{eff}$  for both  $FM_x$  and  $FM_y$  modes. The Figure 3(b) shows the confinement losses at the left edge of bandgap for  $P = 0$  and  $500$  bar. Figure 3(c) presents a typical distribution of modal optical energy in the HPCF. Without applied pressure the HPCF has a polarimetric extinction ratio (PER) of about 50 dB at  $\lambda = 1160$  nm, useful for single mode single polarization applications. The bandgap position can be shifted adjusting the Ge-doped rods diameters [4]. Applying hydrostatic pressure (500 bar) leads to drastically decrease the polarimetric extinction ratio from 50 dB to about 15 dB at 1160 nm.

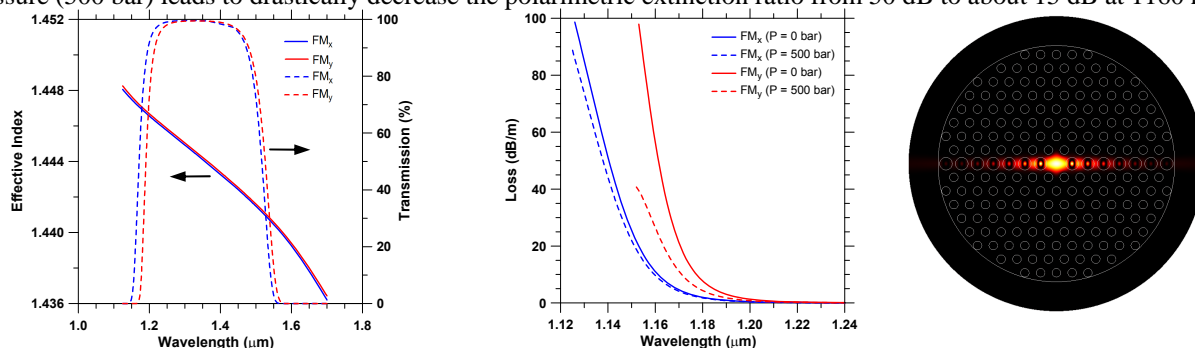


Figure 3. (a) Effective index of  $FM_x$  and  $FM_y$  modes and respective spectral transmission without applied pressure. (b) Confinement losses of fundamental modes near the left edge of bandgap considering  $P = 0$  and  $500$  bar. (c) Typical modal energy distribution of fundamental guided mode in HPCF.

Figure 4(a) presents the phase and group birefringence across the entire bandgap for  $P = 0$  bar. Figure 4(b) shows the  $B_p$  and  $B_g$  near the left edge of bandgap for  $P = 0$  and  $500$  bar, and Figure 4(c) presents the susceptibility of phase and group birefringences ( $dB_p/dP$ ) and ( $dB_g/dP$ ) to hydrostatic pressure near the left edge of the bandgap.  $B_p$  and  $B_g$  vary quickly in the bandgap edge and is almost constant in the center of the bandgap. The rapid variation in  $B_p$  and  $B_g$  allows to use it as a sensing parameter. The maximum susceptibility of  $B_p$  and  $B_g$  were  $dB_p/dP=1.10^{-6}$  (at  $\lambda=1135$  nm) and  $dB_g/dP=7.10^{-6}$  (at  $\lambda=1175$  nm), respectively.

### 4. CONCLUSION

For the first time the opto-mechanical response of a hybrid photonic crystal fiber was numerically investigated for hydrostatic pressure sensor application. The HPCF has a high polarimetric extinction ratio of  $\sim 50$  dB that is reduced to  $\sim 15$  dB at  $\lambda = 1160$  nm when submitted to hydrostatic pressure variation of 500 bar, this effect can also be used as a sensing parameter. On the other hand, the phase and group birefringences vary quickly at the edge of photonic bandgaps

and demonstrate the potential of HPCF as a pressure element sensor. The non-optimized HPCF design allows reaching a phase and grouping susceptibility to hydrostatic pressure of:  $dB_p/dP=1.10^{-6}$  (at  $\lambda=1135$  nm) and  $dB_g/dP=7.10^{-6}$  (at  $\lambda=1175$  nm), respectively.

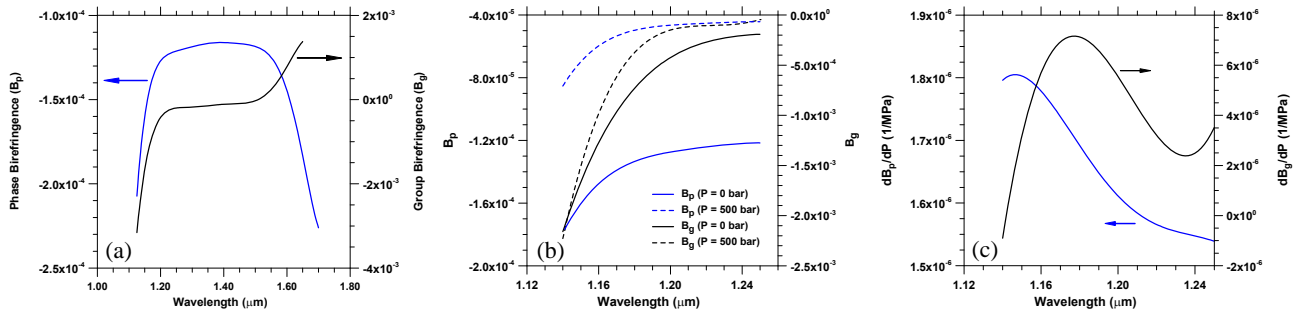


Figure 4. Phase and group birefringence, and the susceptibility of phase and group birefringence to hydrostatic pressure. (a) Phase and group birefringence in entire bandgap without pressure ( $P = 0$  bar). (b) Phase and group birefringence at the left edge of the bandgap considering hydrostatic pressure of 0 bar and 500 bar. (c) Susceptibility of phase and group birefringence at the left edge of the bandgap ( $\Delta P = 500$  bar).

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