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# Isothermal variation of the entropy $(\Delta S_T)$ for the compound $Gd_5Ge_4$ under hydrostatic pressure

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In the present work, the isothermal variation of the entropy  $(\Delta S_T)$  for the compound Gd<sub>5</sub>Ge<sub>4</sub> was studied at different applied hydrostatic pressures (from 0 up to 0.58 GPa). In all pressure ranges, we observe the giant magnetocaloric effect. The  $\Delta S_T$  data for the compound Gd<sub>5</sub>Ge<sub>4</sub> at zero applied pressure present two peaks: the lowest temperature peak is due to irreversible processes and the highest temperature peak is due to magnetostructural transitions. Increasing the pressure, the lowest temperature peak displaces to lower temperatures and disappears. The magnitude of the other peak has a nonlinear behavior with pressure. Different protocols were used to obtain  $\Delta S_T$  at zero applied pressure and the results indicate that  $\Delta S_T$  strongly depends on the initial and final states of Gd<sub>5</sub>Ge<sub>4</sub> compound. We also present a *T-P* magnetic phase diagram built from the available magnetic data. © 2008 American Institute of Physics. [DOI: 10.1063/1.2980040]

## I. INTRODUCTION

The isothermal variation of the entropy  $(\Delta S_T)$  is one of the parameters that characterize the magnetocaloric effect (MCE) in the magnetic materials. MCE is an essential physical phenomenon for the magnetic refrigeration.<sup>1,2</sup> Since the discovery of the giant MCE (GMCE) in the compound Gd<sub>5</sub>Ge<sub>2</sub>Si<sub>2</sub> around room temperature,<sup>3</sup> the series Gd<sub>5</sub>(Ge<sub>1-x</sub>Si<sub>x</sub>)<sub>4</sub> has become the most studied family of magnetocaloric materials.

The compound Gd<sub>5</sub>Ge<sub>4</sub> was the first one of the family  $Gd_5(Ge_{1-x}Si_x)_4$  studied under different hydrostatic pressures by Magen et al.<sup>4</sup> in 2003. Besides the interesting linear thermal expansion results, these scientists also studied the magnetization in different pressures as a function of the temperature and magnetic field. In contrast with the magnetic behavior of the Ge rich compounds with  $0 < x \le 0.3$ , no ferromagnetic phase is observed in Gd<sub>5</sub>Ge<sub>4</sub> at zero magnetic field and down to the lowest measured temperature.<sup>5,6</sup> This compound orders antiferromagnetically below  $\sim 130$  K and has the type II orthorhombic structure [O(II)]. Induced by the magnetic field, there is a magnetostructural transition from the antiferromagnetic O(II) phase to the ferromagnetic phase, which has the type I orthorhombic structure [O(I)].<sup>7-10</sup> In the structure O(I) all subnanometers layers (slabs) are interconnected via partially covalent bonds among Ge and Si atoms, while none remain in the structure O(II). Magen *et al.*<sup>4</sup> showed that the effect of the hydrostatic pressure is similar to the one produced by the magnetic field, e.g., the pressure also induced the transition from the antiferromagnetic O(II) phase to the ferromagnetic O(I) phase.

In 1997, Pecharsky and Gschneidner<sup>11</sup> reported their re-

sults on the isothermal variation of the entropy as a function of the temperature for  $Gd_5Ge_4$  with zero applied pressure. The MCE curve presents two peaks, which were not discussed. In spite of the interesting results for this compound under hydrostatic pressures, there are no MCE studies for  $P \neq 0$ . The aim of the present work is to study the influence of the hydrostatic pressure on the magnetocaloric properties of the compound  $Gd_5Ge_4$ .

#### **II. EXPERIMENTAL PROCEDURES**

The compound  $Gd_5Ge_4$  was prepared using Gd, 99.99 wt % pure (metals and interstitial), and semiconductor grade Ge, 99.9999 wt % pure (metals and interstitial), by arc melting for three times to guarantee the sample homogeneity. The mass of the sample was 5 g and there was no relevant weight loss. The sample was qualitatively analyzed by metallography and a tiny amount of a second phase, probably Gd<sub>5</sub>Ge<sub>3</sub>, was observed.

The magnetization measurements under pressure were performed in a superconducting quantum interference device magnetometer (Quantum Design) in magnetic fields up to 70 kOe in the temperature range from 4 to 170 K. We have used a nonmagnetic Cu–Be clamp-type cell, able to work up to 1.2 GPa at 300 K. The sample was inserted in a Teflon® container filled with mineral oil. A piece of lead was used as a manometer and the pressures reported in this work were obtained at low temperatures.

The isothermal variation of the entropy  $(\Delta S_T)$  shown in Fig. 2 for the different pressures was calculated from the isothermal magnetization data. We have performed a usual protocol (now on called *Protocol 1*).

*Protocol 1.* Before each isotherm, the magnetic field is removed, the temperature is stabilized, and an isothermal

magnetization curve is measured increasing the magnetic field until 50 kOe. The subsequent temperatures of the isotherms are always higher than the previous temperature. To obtain  $\Delta S_T$  data presented in Fig. 7, we have used other three different protocols for Gd<sub>5</sub>Ge<sub>4</sub> compound at zero applied pressure.

*Protocol 2.* Before each isothermal magnetization curve, the magnetic field was removed, the sample was heated up to 80 K, and after that cooled down to the temperature in which we would perform the measurement from 0 up to 50 kOe (similar to the protocol proposed in Ref. 12). The subsequent temperatures of the isotherms are always higher than the previous temperature.

*Protocol 3.* Before each isofield magnetization curve, the magnetic field was removed, the sample was heated up to 80 K, and after that cooled down to 4 K. Isofields were measured by increasing the temperature at fixed magnetic fields from 0 up to 50 kOe.

*Protocol 4.* Before each isofield magnetization curve, 50 kOe magnetic field was applied at 4 K (initial temperature of measurement) and after that the magnetic field was reduced to the magnetic field of interest. Isofields were measured by increasing the temperature at fixed magnetic fields from 0 up to 50 kOe.

To calculate  $\Delta S_T$  from isothermal magnetization data, we have used the following relation:

$$\Delta S_T(T)_{\Delta H} = \frac{1}{2\,\delta T} \left( \,\delta M_1 \,\delta H_1 + 2 \sum_{k=2}^{n-1} \,\delta M_k \,\delta H_k + \,\delta M_n \,\delta H_n \right), \tag{1}$$

which was discussed elsewhere.<sup>13,14</sup> To calculate  $\Delta S_T$  isofield magnetization data, we have used the following relation:

$$\Delta S_T(T_k)_{\Delta H} = \sum_{i,j} \frac{1}{2} \left[ \left( \frac{\partial M_i}{\partial T_k} \right)_{H_i} + \left( \frac{\partial M_j}{\partial T_k} \right)_{H_j} \right] \Delta H_{ij}, \quad j = i$$
  
+ 1. (2)

In the relation (2),  $M_i$  and  $M_j$  are the experimental values of the magnetization at applied magnetic fields  $H_i$  and  $H_j$ , respectively, and temperature  $T_k$ ;  $\Delta H_{ij}=H_j-H_i$  is the magnetic field step, which can be variable from 0 up to 50 kOe.

## **III. RESULTS AND DISCUSSION**

In Fig. 1, we show the magnetization as a function of the temperature for the compound  $Gd_5Ge_4$  at different hydrostatic pressures. With zero applied pressure, the feature of the magnetization is similar to those reported previously in the literature.<sup>4,7</sup> At 0.03 GPa, no significant change was observed in the magnetization curves, so it was omitted in the Fig. 1. Increasing the pressure, we note that a first-order magneto-structural transition appears, and the transition is displaced to higher temperatures, as it was reported elsewhere.<sup>4</sup> Our data show that the displacement of the transition temperature is  $dT_t/dP \cong 45$  K/GPa, in good agreement with Magen *et al.*,<sup>4</sup> who determined  $dT_t/dP \cong 49$  K/GPa from their magnetization data. The inset of Fig. 1 shows in detail the  $M \times T$  curves around the Néel temperature at different pressures. Considering the experimental errors, we do not observe any



FIG. 1. Magnetization as a function of the temperature for the compound  $Gd_5Ge_4$  at external magnetic field of 200 Oe and different applied hydrostatic pressures. The magnetization was measured heating up and cooling down. The inset shows details around Néel temperature.

displacement of the Néel temperature (~128 K) with the increasing hydrostatic pressure. It is not in agreement with Magen *et al.*,<sup>4</sup> who obtained the rate  $dT_N/dP \cong 7$  K/GPa.

In Fig. 2, we present the results of MCE, isothermal variation of the entropy  $(\Delta S_T)$ , for the compound Gd<sub>5</sub>Ge<sub>4</sub> at different hydrostatic pressures and magnetic field variation from 0 to 50 kOe. It is worth noticing the existence of two peaks in MCE data, even for the sample with zero applied pressure. Data for zero applied pressure are in good agreement with that reported by Pecharsky and Gschneidner.<sup>11</sup> The highest temperature peak (43 K) is related to the magnetostructural transitions observed in  $M \times T$  curves, such as that reported in Fig. 2 of Ref. 5. The lowest temperature peak (11 K) is originated from a partial reversibility that Gd<sub>5</sub>Ge<sub>4</sub> compound presents and can be better understood when we analyze the isotherms of Fig. 3.

The magnetization isotherms of Fig. 3 were measured from 4 to 26 K at intervals of 2 K and from 30 to 78 K at



FIG. 2. Isothermal variation in the entropy as a function of the temperature at different hydrostatic pressures. The curves were calculated from the magnetization isotherms from 0 up to 50 kOe.



FIG. 3. Magnetization isotherms measured with no applied pressure for the compound  $Gd_5Ge_4$ . From 4 to 26 K the isotherms were measured at intervals of 2 K and from 30 to 78 K at intervals of 4 K.

intervals of 4 K. The first two curves have typical ferromagnetic behavior. The next isotherms have the coexistence of ferromagnetic and antiferromagnetic phases even before the metamagnetic transitions, and the amount of the ferromagnetic phase decreases with the temperature, according to Ref. 5. At 10 K, we notice that the reversibility is partial, since the profile of the next isotherm (12 K) indicates that more ferromagnetic phase became antiferromagnetic in the demagnetizing process. These processes more and more reversible with increasing temperature provoke the large variation in the areas among the isotherms and consequently the MCE peak around 11 K, whose magnitude characterizes a GMCE.

With the application of hydrostatic pressure, the peak at 11 K displaces to lower temperatures and disappears. It is worth noticing that, as the lowest temperature peak disappears with the increasing applied pressure, positive values of  $\Delta S_T$  appear (Fig. 2). For 0.58 GPa, there are three measured/ calculated positive values and the largest one is out of any experimental errors. The origin of this inverted MCE is the crossing isotherms shown in the Fig. 4(b). However, these crossings are not induced by pressure, since they are also present in the 0 GPa data, but with zero applied pressure they are not enough to produce positive values of  $\Delta S_T$ .

The magnitude of the GMCE ( $\Delta S_T$ ) of the second peak decreases with pressure until 0.19 GPa. With subsequent increasing pressure until 0.58 GPa, the GMCE turns to increase almost reaching the value at zero applied pressure. This behavior is different from that observed for Gd<sub>5</sub>Ge<sub>2</sub>Si<sub>2</sub> compound<sup>15</sup> whose GMCE continuously decreases with hydrostatic pressure and stops being a giant effect. The peak temperature almost does not change until 0.19 GPa and displaces to higher temperatures above this pressure.

For applied pressure of 0.58 GPa, the sharp metamagnetic transitions disappear [Fig. 4(a)]. It could be an indication of disappearance of the first-order character of the transitions at this hydrostatic pressure, but the hysteresis in the  $M \times T$  data (Fig. 1) and the high peak value of  $\Delta S_T$  (Fig. 2) indicate the opposite.

Another important parameter to analyze magnetocaloric



FIG. 4. (a) Magnetization isotherms measured with applied pressure of 0.58 GPa for the compound  $Gd_5Ge_4$ . From 4 to 26 K the isotherms were measured at intervals of 2 K and from 30 to 78 K at intervals of 4 K. (b) Detailed isotherms from 4 to 14 K.

materials comparatively is the *refrigeration capacity* (q), which is given by <sup>16,17</sup>

$$q(\Delta T)_{\Delta H} = -\int_{T_1}^{T_2} \Delta S_T(T)_{\Delta H} dT,$$
(3)

where  $\Delta H$  is the variation in the magnetic field used to calculate  $\Delta S_T$ ,  $T_1$  is the temperature of the cold end of a refrigeration cycle,  $T_2$  is the temperature of the hot end, and  $\Delta T$  $=T_2-T_1$ . In fact, q is the area under  $\Delta S_T \times T$  curve and quantifies the maximum heat that can be transferred from the cold end ( $T_1$ ) to the hot end ( $T_2$ ). To compare different materials, we must often calculate q for a similar and convenient  $\Delta T$ .<sup>17,18</sup> Neglecting the errors in  $\Delta S_T$ , we plot the refrigeration capacity as a function of the pressure in Fig. 5. q was calculated with  $\Delta T$ =51 K around the highest temperature peak of each  $\Delta S_T$  curve. Considering a linear fit, we find that



FIG. 5. Refrigeration capacity as a function of the hydrostatic pressure calculated with 51 K around the peak temperature of the  $\Delta S_T \times T$  curves.

the refrigeration capacity increases with pressure at a rate of q/P=190 J kg<sup>-1</sup> GPa<sup>-1</sup>, varying from 600 J kg<sup>-1</sup> at 0 GPa up to 700 J kg<sup>-1</sup> at 0.58 GPa.

With the available data, we are able to outline a *T-P* magnetic phase diagram for Gd<sub>5</sub>Ge<sub>4</sub>, which is represented in Fig. 6. This diagram was built from the heating curves of  $M \times T$  data. We can clearly distinguish four regions. One of them is the paramagnetic phase above 128 K. Below 128 K, there is an antiferromagnetic phase, whose lower limit in temperature is a region of phase coexistence. Since the  $M \times T$  curve at 0.03 GPa is almost identical to the one at 0 GPa, e.g., 0.03 GPa is not enough to induce ferromagnetic coupling, we can affirm that the antiferromagnetic phase exists at low temperatures and low hydrostatic pressures. At low temperatures, the upper limit in pressure for the antiferromagnetic phase is not well established, but it is at most 0.13 GPa, since Magen *et al.*<sup>4</sup> reported induction of ferromagnetic



FIG. 6. *T-P* magnetic phase diagram for the compound  $Gd_5Ge_4$  built from  $M \times T$  data (heating data). The solid lines are guides to the eyes and the dotted lines are supposed extensions of the experimental data.



FIG. 7. Isothermal variation in the entropy for  $Gd_5Ge_4$  compound at zero applied pressure obtained from four different protocols described in the Experimental procedures section. Protocols 1 and 2 used isothermal curves  $(M \times H)$  and protocols 3 and 4 used isofield curves  $(M \times H)$ .

phase at this pressure. From our data, at low temperatures and above 0.03 GPa, there is a ferromagnetic phase. According to the Ref. 4, this phase exists at low temperatures until 0.8 GPa at least. Increasing the temperature from the ferromagnetic phase, we achieve a region of coexistence between the ferromagnetic and antiferromagnetic phases, which was determined from the heating  $M \times T$  data.

Since the  $\Delta S_T$  peak at low temperature shown in Fig. 2 is due to irreversible processes at zero and low applied pressures, we performed other magnetization measurements (M  $\times H$  and  $M \times T$ ) at zero applied pressure with different procedures to verify the possible different  $\Delta S_T$  profiles. In Fig. 7, we present  $\Delta S_T$  results obtained from protocols 1–4 described in the Experimental procedures section. For the range of temperatures where there is partial or total irreversibility, below  $\sim 20$  K, it is easy to see that there are great divergences among  $\Delta S_T$  profiles for the four analyzed protocols. We also notice differences next to the highest temperature maxima around 45 K.  $\Delta S_T$  magnitudes for protocols 1 and 2 decrease faster than that for protocols 3 and 4. This can be partially explained by the relatively large  $\Delta T$  interval between the two consecutive isotherms, which have transitions around 50 kOe, used in the protocols 1 and 2, as shown in Fig. 3 (Protocol 1). Other contribution to these differences would be irreversible processes around the first-order transitions. Such differences are also observed in the MnAs compound<sup>19</sup> and probably in other magnetocaloric materials that present first-order transitions.

Based on  $M \times T$  data reported by Tang *et al.*,<sup>7</sup> we expect that Gd<sub>5</sub>Ge<sub>4</sub> presents a positive  $\Delta S_T$  at low temperatures. This way, the protocols 2 and 3 could be candidates to the protocol that best reflects the intrinsic properties of this compound. Nevertheless, magnetic refrigeration can use several thermodynamical cycles. If the initial and final states of processes are different in certain thermodynamical cycles,  $\Delta S_T$ 

nis article is copyrighted as indicated in the article. Reuse of AIP content is subject to the terms at: http://scitation.aip.org/termsconditions. Downloaded to J IP: 143 106 108 169 On: Wed. 17. Jun 2015 17:31:24 could have very different values. So, it is not obvious to indicate which is the correct protocol for calculating the iso-thermal variation in the entropy in the case of  $Gd_5Ge_4$  and probably other compounds that present first-order transitions.

#### **IV. CONCLUSIONS**

The MCE of the compound  $Gd_5Ge_4$  at zero applied pressure presents two peaks: the lowest temperature peak is due to irreversible processes and the highest temperature peak is due to magnetostructural transitions. Increasing the pressure, the lowest temperature peak displaces to lower temperatures and disappears, which is an indication that irreversibility disappears with applied pressure. The magnitude of the other peak decreases with pressure until 0.19 GPa. With subsequent increasing pressure until 0.58 GPa, the magnitude turns to increase almost reaching the value at zero applied pressure. In all pressure range, we observe GMCE, and the refrigeration capacity increases with the applied pressure.

From the available magnetic data, we built a T-P magnetic phase diagram for Gd<sub>5</sub>Ge<sub>4</sub>. Besides the magnetic single phase regions (paramagnetic, ferromagnetic, and antiferromagnetic), there is also a region in the diagram where ferromagnetic and antiferromagnetic phases coexist. The temperature range of coexistence increases with hydrostatic pressure.

 $\Delta S_T$  obtained from the different protocols at zero applied pressure present great divergences. These divergences are consistent with the fact that  $\Delta S$  depends on the initial and final states of the system.

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