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B. P. Abbott

R. Abbott

T. D. Abbott

F. Acernese

K. Ackley

See next page for additional authors

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Authors

B. P. Abbott, R. Abbott, T. D. Abbott, F. Acernese, K. Ackley, C. Adams, T. Adams, P. Addesso, R. X. Adhikari, V. B. Adya, C. Affeldt, M. Afrough, B. Agarwal, M. Agathos, K. Agatsuma, N. Aggarwal, O. D. Aguiar, L. Aiello, A. Ain, P. Ajith, B. Allen, G. Allen, A. Allocca, P. A. Altin, A. Amato, A. Ananyeva, S. B. Anderson, W. G. Anderson, S. V. Angelova, and S. Antier

A Search for Tensor, Vector, and Scalar Polarizations in the Stochastic Gravitational-Wave Background

- B. P. Abbott,¹ R. Abbott,¹ T. D. Abbott,² F. Acernese,^{3,4} K. Ackley,^{5,6} C. Adams,⁷ T. Adams,⁸ P. Addesso,⁹ R. X. Adhikari,¹ V. B. Adya,¹⁰ C. Affeldt,¹⁰ M. Afrough,¹¹ B. Agarwal,¹² M. Agathos,¹³ K. Agatsuma,¹⁴ N. Aggarwal,¹⁵ O. D. Aguiar,¹⁶ L. Aiello,^{17,18} A. Ain,¹⁹ P. Ajith,²⁰ B. Allen,^{10,21,22} G. Allen,¹² A. Allocca,^{23,24} P. A. Altin,²⁵ A. Amato,²⁶ A. Ananyeva,¹ S. B. Anderson,¹ W. G. Anderson,²¹ S. V. Angelova,²⁷ S. Antier,²⁸ S. Appert,¹ K. Arai,¹ M. C. Araya,¹ J. S. Areeda,²⁹ N. Arnaud,^{28,30} S. Ascenzi,^{31,32} G. Ashton,¹⁰ M. Ast,³³ S. M. Aston,⁷ P. Astone,³⁴ D. V. Atallah,³⁵ P. Aufmuth,²² C. Aulbert,¹⁰ K. AultONeal,³⁶ C. Austin,² A. Avila-Alvarez,²⁹ S. Babak,³⁷ P. Bacon,³⁸ M. K. M. Bader,¹⁴ S. Bae,³⁹ P. T. Baker,⁴⁰ F. Baldaccini,^{41,42} G. Ballardin,³⁰ S. W. Ballmer,⁴³ S. Banagiri,⁴⁴ J. C. Barayoga,¹ S. E. Barclay,⁴⁵ B. C. Barish,¹ D. Barker,⁴⁶ K. Barkett,⁴⁷ F. Barone,^{3,4} B. Barr,⁴⁵ L. Barsotti,¹⁵ M. Barsuglia,³⁸ D. Barta,⁴⁸ J. Bartlett,⁴⁶ I. Bartos,^{49,5} R. Bassiri,⁵⁰ A. Basti,^{23,24} J. C. Batch,⁴⁶ M. Bawaj,^{51,42} J. C. Bayley,⁴⁵ M. Bazzan,^{52,53} B. Bécsy,⁵⁴ C. Beer,¹⁰ M. Bejger,⁵⁵ I. Belahcene,²⁸ A. S. Bell,⁴⁵ B. K. Berger,¹ G. Bergmann,¹⁰ J. J. Bero,⁵⁶ C. P. L. Berry,⁵⁷ D. Bersanetti,⁵⁸ A. Bertolini,¹⁴ J. Betzwieser,⁷ S. Bhagwat,⁴³ R. Bhandare,⁵⁹ I. A. Bilenko,⁶⁰ G. Billingsley,¹ C. R. Billman,⁵ J. Birch,⁷ R. Birney,⁶¹ O. Birnholtz,¹⁰ S. Biscans,^{1,15} S. Biscoveanu,^{62,6} A. Bisht,²² M. Bitossi,^{30,24} C. Biwer,⁴³ M. A. Bizouard,²⁸ J. K. Blackburn,¹ J. Blackman,⁴⁷ C. D. Blair,^{1,63} D. G. Blair,⁶³ R. M. Blair,⁴⁶ S. Bloemen,⁶⁴ O. Bock,¹⁰ N. Bode,¹⁰ M. Boer,⁶⁵ G. Bogaert,⁶⁵ A. Bohe,³⁷ F. Bondu,⁶⁶ E. Bonilla,⁵⁰ R. Bonnand,⁸ B. A. Boom,¹⁴ R. Bork,¹ V. Boschi,^{30,24} S. Bose,^{67,19} K. Bossie,⁷ Y. Bouffanais,³⁸ A. Bozzi,³⁰ C. Bradaschia,²⁴ P. R. Brady,²¹ M. Branchesi,^{17,18} J. E. Brau,⁶⁸ T. Briant,⁶⁹ A. Brillet,⁶⁵ M. Brinkmann,¹⁰ V. Brisson,²⁸ P. Brockill,²¹ J. E. Broida,⁷⁰ A. F. Brooks,¹ D. A. Brown,⁴³ D. D. Brown,⁷¹ S. Brunett,¹ C. C. Buchanan,² A. Buikema,¹⁵ T. Bulik,⁷² H. J. Bulten,^{73,14} A. Buonanno,^{37,74} D. Buskulic,⁸ C. Buy,³⁸ R. L. Byer,⁵⁰ M. Cabero,¹⁰ L. Cadonati,⁷⁵ G. Cagnoli,^{26,76} C. Cahillane,¹ J. Calderón Bustillo,⁷⁵ T. A. Callister,¹ E. Calloni,^{77,4} J. B. Camp,⁷⁸ M. Canepa,^{79,58} P. Canizares,⁶⁴ K. C. Cannon,⁸⁰ H. Cao,⁷¹ J. Cao,⁸¹ C. D. Capano,¹⁰ E. Capocasa,³⁸ F. Carbognani,³⁰ S. Caride,⁸² M. F. Carney,⁸³ J. Casanueva Diaz,²⁸ C. Casentini,^{31,32} S. Caudill,^{21,14} M. Cavaglià,¹¹ F. Cavalier,²⁸ R. Cavalieri,³⁰ G. Cella,²⁴ C. B. Cepeda,¹ P. Cerdá-Durán,⁸⁴ G. Cerretani,^{23,24} E. Cesarini,^{85,32} S. J. Chamberlin,⁶² M. Chan,⁴⁵ S. Chao,⁸⁶ P. Charlton,⁸⁷ E. Chase,⁸⁸ E. Chassande-Mottin,³⁸ D. Chatterjee,²¹ B. D. Cheeseboro,⁴⁰ H. Y. Chen,⁸⁹ X. Chen,⁶³ Y. Chen,⁴⁷ H.-P. Cheng,⁵ H. Chia,⁵ A. Chincarini,⁵⁸ A. Chiummo,³⁰ T. Chmiel,⁸³ H. S. Cho,⁹⁰ M. Cho,⁷⁴ J. H. Chow,²⁵ N. Christensen,^{70,65} Q. Chu,⁶³ A. J. K. Chua,¹³ S. Chua,⁶⁹ A. K. W. Chung,⁹¹ S. Chung,⁶³ G. Ciani,^{5,52,53} R. Ciolfi,^{92,93} C. E. Cirelli,⁵⁰ A. Cirone,^{79,58} F. Clara,⁴⁶ J. A. Clark,⁷⁵ P. Clearwater,⁹⁴ F. Cleva,⁶⁵ C. Cocchieri,¹¹ E. Coccia,^{17,18} P.-F. Cohadon,⁶⁹ D. Cohen,²⁸ A. Colla,^{95,34} C. G. Collette,⁹⁶ L. R. Cominsky,⁹⁷ M. Constancio Jr.,¹⁶ L. Conti,⁵³ S. J. Cooper,⁵⁷ P. Corban,⁷ T. R. Corbitt,² I. Cordero-Carrión,⁹⁸ K. R. Corley,⁴⁹ N. Cornish,⁹⁹ A. Corsi,⁸² S. Cortese,³⁰ C. A. Costa,¹⁶ E. Coughlin,⁷⁰ M. W. Coughlin,^{70,1} S. B. Coughlin,⁸⁸ J.-P. Coulon,⁶⁵ S. T. Countryman,⁴⁹ P. Couvares,¹ P. B. Covas,¹⁰⁰ E. E. Cowan,⁷⁵ D. M. Coward,⁶³ M. J. Cowart,⁷ D. C. Coyne,¹ R. Coyne,⁸² J. D. E. Creighton,²¹ T. D. Creighton,¹⁰¹ J. Cripe,² S. G. Crowder,¹⁰² T. J. Cullen,^{29,2} A. Cumming,⁴⁵ L. Cunningham,⁴⁵ E. Cuoco,³⁰ T. Dal Canton,⁷⁸ G. Dálya,⁵⁴ S. L. Danilishin,^{22,10} S. D'Antonio,³² K. Danzmann,^{22,10} A. Dasgupta,¹⁰³ C. F. Da Silva Costa,⁵ V. Dattilo,³⁰ I. Dave,⁵⁹ M. Davier,²⁸ D. Davis,⁴³ E. J. Daw,¹⁰⁴ B. Day,⁷⁵ S. De,⁴³ D. DeBra,⁵⁰ J. Degallaix,²⁶ M. De Laurentis,^{17,4} S. Deléglise,⁶⁹ W. Del Pozzo,^{57,23,24} N. Demos,¹⁵ T. Denker,¹⁰ T. Dent,¹⁰ R. De Pietri,^{105,106} V. Dergachev,³⁷ R. De Rosa,^{77,4} R. T. DeRosa,⁷ C. De Rossi,^{26,30} R. DeSalvo,¹⁰⁷ O. de Varona,¹⁰ J. Devenson,²⁷ S. Dhurandhar,¹⁹ M. C. Díaz,¹⁰¹ L. Di Fiore,⁴ M. Di Giovanni,^{108,93} T. Di Girolamo,^{49,77,4} A. Di Lieto,^{23,24} S. Di Pace,^{95,34} I. Di Palma,^{95,34} F. Di Renzo,^{23,24} Z. Doctor,⁸⁹ V. Dolique,²⁶ F. Donovan,¹⁵ K. L. Dooley,¹¹ S. Doravari,¹⁰ I. Dorrington,³⁵ R. Douglas,⁴⁵ M. Dovale Álvarez,⁵⁷ T. P. Downes,²¹ M. Drago,¹⁰ C. Dreissigacker,¹⁰ J. C. Driggers,⁴⁶ Z. Du,⁸¹ M. Ducrot,⁸ P. Dupej,⁴⁵ S. E. Dwyer,⁴⁶ T. B. Edo,¹⁰⁴ M. C. Edwards,⁷⁰ A. Effler,⁷ H.-B. Eggenstein,^{37,10} P. Ehrens,¹ J. Eichholz,¹ S. S. Eikenberry,⁵ R. A. Eisenstein,¹⁵ R. C. Essick,¹⁵ D. Estevez,⁸ Z. B. Etienne,⁴⁰ T. Etzel,¹ M. Evans,¹⁵ T. M. Evans,⁷ M. Factourovich,⁴⁹ V. Fafone,^{31,32,17} H. Fair,⁴³ S. Fairhurst,³⁵ X. Fan,⁸¹ S. Farinon,⁵⁸ B. Farr,⁸⁹ W. M. Farr,⁵⁷ E. J. Fauchon-Jones,³⁵ M. Favata,¹⁰⁹ M. Fays,³⁵ C. Fee,⁸³ H. Fehrmann,¹⁰ J. Feicht,¹ M. M. Fejer,⁵⁰ A. Fernandez-Galiana,¹⁵ I. Ferrante,^{23,24} E. C. Ferreira,¹⁶ F. Ferrini,³⁰ F. Fidecaro,^{23,24} D. Finstad,⁴³ I. Fiori,³⁰ D. Fiorucci,³⁸ M. Fishbach,⁸⁹ R. P. Fisher,⁴³ M. Fitz-Axen,⁴⁴ R. Flaminio,^{26,110} M. Fletcher,⁴⁵ H. Fong,¹¹¹ J. A. Font,^{84,112} P. W. F. Forsyth,²⁵ S. S. Forsyth,⁷⁵ J.-D. Fournier,⁶⁵ S. Frasca,^{95,34} F. Frasconi,²⁴ Z. Frei,⁵⁴ A. Freise,⁵⁷ R. Frey,⁶⁸ V. Frey,²⁸ E. M. Fries,¹ P. Fritschel,¹⁵ V. V. Frolov,⁷ P. Fulda,⁵ M. Fyffe,⁷ H. Gabbard,⁴⁵ B. U. Gadre,¹⁹ S. M. Gaebel,⁵⁷ J. R. Gair,¹¹³ L. Gammaitoni,⁴¹ M. R. Ganija,⁷¹ S. G. Gaonkar,¹⁹ C. Garcia-Quiros,¹⁰⁰ F. Garufi,^{77,4} B. Gateley,⁴⁶ S. Gaudio,³⁶ G. Gaur,¹¹⁴ V. Gayathri,¹¹⁵ N. Gehrels*,⁷⁸ G. Gemme,⁵⁸ E. Genin,³⁰ A. Gennai,²⁴ D. George,¹² J. George,⁵⁹ L. Gergely,¹¹⁶ V. Germain,⁸ S. Ghonge,⁷⁵ Abhirup Ghosh,²⁰ Archisman Ghosh,^{20,14} S. Ghosh,^{64,14,21} J. A. Giaime,^{2,7} K. D. Giardina,⁷ A. Giazotto,²⁴

P. Popolizio,³⁰ E. K. Porter,³⁸ A. Post,¹⁰ J. Powell,¹⁴⁸ J. Prasad,¹⁹ J. W. W. Pratt,³⁶ G. Pratten,¹⁰⁰ V. Predoi,³⁵ T. Prestegard,²¹ M. Prijatelj,¹⁰ M. Principe,⁹ S. Privitera,³⁷ G. A. Prodi,^{108,93} L. G. Prokhorov,⁶⁰ O. Puncken,¹⁰ M. Punturo,⁴² P. Puppo,³⁴ M. Pürer,³⁷ H. Qi,²¹ V. Quetschke,¹⁰¹ E. A. Quintero,¹ R. Quitzow-James,⁶⁸ F. J. Raab,⁴⁶ D. S. Rabeling,²⁵ H. Radkins,⁴⁶ P. Raffai,⁵⁴ S. Raja,⁵⁹ C. Rajan,⁵⁹ B. Rajbhandari,⁸² M. Rakhmanov,¹⁰¹ K. E. Ramirez,¹⁰¹ A. Ramos-Buades,¹⁰⁰ P. Rapagnani,^{95,34} V. Raymond,³⁷ M. Razzano,^{23,24} J. Read,²⁹ T. Regimbau,⁶⁵ L. Rei,⁵⁸ S. Reid,⁶¹ D. H. Reitze,^{1,5} W. Ren,¹² S. D. Reyes,⁴³ F. Ricci,^{95,34} P. M. Ricker,¹² S. Rieger,¹⁰ K. Riles,¹¹⁷ M. Rizzo,⁵⁶ N. A. Robertson,^{1,45} R. Robie,⁴⁵ F. Robinet,²⁸ A. Rocchi,³² L. Rolland,⁸ J. G. Rollins,¹ V. J. Roma,⁶⁸ J. D. Romano,¹⁰¹ R. Romano,^{3,4} C. L. Romel,⁴⁶ J. H. Romie,⁷ D. Rosińska,^{149,55} M. P. Ross,¹⁵⁰ S. Rowan,⁴⁵ A. Rüdiger,¹⁰ P. Ruggi,³⁰ G. Rutins,²⁷ K. Ryan,⁴⁶ S. Sachdev,¹ T. Sadecki,⁴⁶ L. Sadeghian,²¹ M. Sakellariadou,¹⁵¹ L. Salconi,³⁰ M. Saleem,¹¹⁵ F. Salemi,¹⁰ A. Samajdar,¹⁴² L. Sammut,⁶ L. M. Sampson,⁸⁸ E. J. Sanchez,¹ L. E. Sanchez,¹ N. Sanchis-Gual,⁸⁴ V. Sandberg,⁴⁶ J. R. Sanders,⁴³ B. Sassolas,²⁶ P. R. Saulson,⁴³ O. Sauter,¹¹⁷ R. L. Savage,⁴⁶ A. Sawadsky,³³ P. Schale,⁶⁸ M. Scheel,⁴⁷ J. Scheuer,⁸⁸ J. Schmidt,¹⁰ P. Schmidt,^{1,64} R. Schnabel,³³ R. M. S. Schofield,⁶⁸ A. Schönbeck,³³ E. Schreiber,¹⁰ D. Schuette,^{10,22} B. W. Schulte,¹⁰ B. F. Schutz,^{35,10} S. G. Schwalbe,³⁶ J. Scott,⁴⁵ S. M. Scott,²⁵ E. Seidel,¹² D. Sellers,⁷ A. S. Sengupta,¹⁵² D. Sentenac,³⁰ V. Sequino,^{31,32,17} A. Sergeev,¹²⁷ D. A. Shaddock,²⁵ T. J. Shaffer,⁴⁶ A. A. Shah,¹³⁶ M. S. Shahriar,⁸⁸ M. B. Shaner,¹⁰⁷ L. Shao,³⁷ B. Shapiro,⁵⁰ P. Shawhan,⁷⁴ A. Sheperd,²¹ D. H. Shoemaker,¹⁵ D. M. Shoemaker,⁷⁵ K. Siellez,⁷⁵ X. Siemens,²¹ M. Sieniawska,⁵⁵ D. Sigg,⁴⁶ A. D. Silva,¹⁶ L. P. Singer,⁷⁸ A. Singh,^{37,10,22} A. Singhal,^{17,34} A. M. Sintes,¹⁰⁰ B. J. J. Slagmolen,²⁵ B. Smith,⁷ J. R. Smith,²⁹ R. J. E. Smith,^{1,6} S. Somalia,¹⁵³ E. J. Son,¹³⁰ J. A. Sonnenberg,²¹ B. Sorazu,⁴⁵ F. Sorrentino,⁵⁸ T. Souradeep,¹⁹ A. P. Spencer,⁴⁵ A. K. Srivastava,¹⁰³ K. Staats,³⁶ A. Staley,⁴⁹ M. Steinke,¹⁰ J. Steinlechner,^{33,45} S. Steinlechner,³³ D. Steinmeyer,¹⁰ S. P. Stevenson,^{57,148} R. Stone,¹⁰¹ D. J. Stops,⁵⁷ K. A. Strain,⁴⁵ G. Stratta,^{120,121} S. E. Striglin,⁶⁰ A. Strunk,⁴⁶ R. Sturani,¹⁵⁴ A. L. Stuver,⁷ T. Z. Summerscales,¹⁵⁵ L. Sun,⁹⁴ S. Sunil,¹⁰³ J. Suresh,¹⁹ P. J. Sutton,³⁵ B. L. Swinkels,³⁰ M. J. Szczepańczyk,³⁶ M. Tacca,¹⁴ S. C. Tait,⁴⁵ C. Talbot,⁶ D. Talukder,⁶⁸ D. B. Tanner,⁵ D. Tao,⁷⁰ M. Tápai,¹¹⁶ A. Taracchini,³⁷ J. D. Tasson,⁷⁰ J. A. Taylor,¹³⁶ R. Taylor,¹ S. V. Tewari,¹⁴⁷ T. Theeg,¹⁰ F. Thies,¹⁰ E. G. Thomas,⁵⁷ M. Thomas,⁷ P. Thomas,⁴⁶ K. A. Thorne,⁷ E. Thrane,⁶ S. Tiwari,^{17,93} V. Tiwari,³⁵ K. V. Tokmakov,⁶¹ K. Toland,⁴⁵ M. Tonelli,^{23,24} Z. Tornasi,⁴⁵ A. Torres-Forné,⁸⁴ C. I. Torrie,¹ D. Töyrä,⁵⁷ F. Travasso,^{30,42} G. Traylor,⁷ J. Trinastic,⁵ M. C. Tringali,^{108,93} L. Trozzo,^{156,24} K. W. Tsang,¹⁴ M. Tse,¹⁵ R. Tso,¹ L. Tsukada,⁸⁰ D. Tsuna,⁸⁰ D. Tuyenbayev,¹⁰¹ K. Ueno,²¹ D. Ugolini,¹⁵⁷ C. S. Unnikrishnan,¹¹⁸ A. L. Urban,¹ S. A. Usman,³⁵ H. Vahlbruch,²² G. Vajente,¹ G. Valdes,² N. van Bakel,¹⁴ M. van Beuzekom,¹⁴ J. F. J. van den Brand,^{73,14} C. Van Den Broeck,^{14,158} D. C. Vander-Hyde,⁴³ L. van der Schaaf,¹⁴ J. V. van Heijningen,¹⁴ A. A. van Veggel,⁴⁵ M. Vardaro,^{52,53} V. Varma,⁴⁷ S. Vass,¹ M. Vasúth,⁴⁸ A. Vecchio,⁵⁷ G. Vedovato,⁵³ J. Veitch,⁴⁵ P. J. Veitch,⁷¹ K. Venkateswara,¹⁵⁰ G. Venugopalan,¹ D. Verkindt,⁸ F. Vetrano,^{120,121} A. Viceré,^{120,121} A. D. Viets,²¹ S. Vinciguerra,⁵⁷ D. J. Vine,²⁷ J.-Y. Vinet,⁶⁵ S. Vitale,¹⁵ T. Vo,⁴³ H. Vocca,^{41,42} C. Vorvick,⁴⁶ S. P. Vyatchanin,⁶⁰ A. R. Wade,¹ L. E. Wade,⁸³ M. Wade,⁸³ R. Walet,¹⁴ M. Walker,²⁹ L. Wallace,¹ S. Walsh,^{37,10,21} G. Wang,^{17,121} H. Wang,⁵⁷ J. Z. Wang,⁶² W. H. Wang,¹⁰¹ Y. F. Wang,⁹¹ R. L. Ward,²⁵ J. Warner,⁴⁶ M. Was,⁸ J. Watchi,⁹⁶ B. Weaver,⁴⁶ L.-W. Wei,^{10,22} M. Weinert,¹⁰ A. J. Weinstein,¹ R. Weiss,¹⁵ L. Wen,⁶³ E. K. Wessel,¹² P. Weßels,¹⁰ J. Westerweck,¹⁰ T. Westphal,¹⁰ K. Wette,²⁵ J. T. Whelan,⁵⁶ B. F. Whiting,⁵ C. Whittle,⁶ D. Wilken,¹⁰ D. Williams,⁴⁵ R. D. Williams,¹ A. R. Williamson,⁶⁴ J. L. Willis,^{1,159} B. Willke,^{22,10} M. H. Wimmer,¹⁰ W. Winkler,¹⁰ C. C. Wipf,¹ H. Wittel,^{10,22} G. Woan,⁴⁵ J. Woehler,¹⁰ J. Wofford,⁵⁶ K. W. K. Wong,⁹¹ J. Worden,⁴⁶ J. L. Wright,⁴⁵ D. S. Wu,¹⁰ D. M. Wysocki,⁵⁶ S. Xiao,¹ H. Yamamoto,¹ C. C. Yancey,⁷⁴ L. Yang,¹⁶⁰ M. J. Yap,²⁵ M. Yazback,⁵ Hang Yu,¹⁵ Haocun Yu,¹⁵ M. Yvert,⁸ A. Zadrożny,¹³¹ M. Zanolin,³⁶ T. Zelenova,³⁰ J.-P. Zendri,⁵³ M. Zevin,⁸⁸ L. Zhang,¹ M. Zhang,¹³⁹ T. Zhang,⁴⁵ Y.-H. Zhang,⁵⁶ C. Zhao,⁶³ M. Zhou,⁸⁸ Z. Zhou,⁸⁸ S. J. Zhu,^{37,10} X. J. Zhu,⁶ M. E. Zucker,^{1,15} and J. Zweizig¹

(LIGO Scientific Collaboration and Virgo Collaboration)

*Deceased, February 2017. †Deceased, November 2017. ‡Deceased, December 2016.

¹LIGO, California Institute of Technology, Pasadena, CA 91125, USA

²Louisiana State University, Baton Rouge, LA 70803, USA

³Università di Salerno, Fisciano, I-84084 Salerno, Italy

⁴INFN, Sezione di Napoli, Complesso Universitario di Monte S. Angelo, I-80126 Napoli, Italy

⁵University of Florida, Gainesville, FL 32611, USA

⁶OzGrav, School of Physics & Astronomy, Monash University, Clayton 3800, Victoria, Australia

⁷LIGO Livingston Observatory, Livingston, LA 70754, USA

⁸Laboratoire d'Annecy-le-Vieux de Physique des Particules (LAPP),

Université Savoie Mont Blanc, CNRS/IN2P3, F-74941 Annecy, France

⁹University of Sannio at Benevento, I-82100 Benevento,

Italy and INFN, Sezione di Napoli, I-80100 Napoli, Italy

¹⁰Max Planck Institute for Gravitational Physics (Albert Einstein Institute), D-30167 Hannover, Germany

- ¹¹*The University of Mississippi, University, MS 38677, USA*
- ¹²*NCSA, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA*
- ¹³*University of Cambridge, Cambridge CB2 1TN, United Kingdom*
- ¹⁴*Nikhef Science Park, 1098 XG Amsterdam, The Netherlands*
- ¹⁵*LIGO, Massachusetts Institute of Technology, Cambridge, MA 02139, USA*
- ¹⁶*Instituto Nacional de Pesquisas Espaciais, 12227-010 São José dos Campos, São Paulo, Brazil*
- ¹⁷*Gran Sasso Science Institute (GSSI), I-67100 L'Aquila, Italy*
- ¹⁸*INFN, Laboratori Nazionali del Gran Sasso, I-67100 Assergi, Italy*
- ¹⁹*Inter-University Centre for Astronomy and Astrophysics, Pune 411007, India*
- ²⁰*International Centre for Theoretical Sciences, Tata Institute of Fundamental Research, Bengaluru 560089, India*
- ²¹*University of Wisconsin-Milwaukee, Milwaukee, WI 53201, USA*
- ²²*Leibniz Universität Hannover, D-30167 Hannover, Germany*
- ²³*Università di Pisa, I-56127 Pisa, Italy*
- ²⁴*INFN, Sezione di Pisa, I-56127 Pisa, Italy*
- ²⁵*OzGrav, Australian National University, Canberra, Australian Capital Territory 0200, Australia*
- ²⁶*Laboratoire des Matériaux Avancés (LMA), CNRS/IN2P3, F-69622 Villeurbanne, France*
- ²⁷*SUPA, University of the West of Scotland, Paisley PA1 2BE, United Kingdom*
- ²⁸*LAL, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, F-91898 Orsay, France*
- ²⁹*California State University Fullerton, Fullerton, CA 92831, USA*
- ³⁰*European Gravitational Observatory (EGO), I-56021 Cascina, Pisa, Italy*
- ³¹*Università di Roma Tor Vergata, I-00133 Roma, Italy*
- ³²*INFN, Sezione di Roma Tor Vergata, I-00133 Roma, Italy*
- ³³*Universität Hamburg, D-22761 Hamburg, Germany*
- ³⁴*INFN, Sezione di Roma, I-00185 Roma, Italy*
- ³⁵*Cardiff University, Cardiff CF24 3AA, United Kingdom*
- ³⁶*Embry-Riddle Aeronautical University, Prescott, AZ 86301, USA*
- ³⁷*Max Planck Institute for Gravitational Physics (Albert Einstein Institute), D-14476 Potsdam-Golm, Germany*
- ³⁸*APC, AstroParticule et Cosmologie, Université Paris Diderot, CNRS/IN2P3, CEA/Irfu, Observatoire de Paris, Sorbonne Paris Cité, F-75205 Paris Cedex 13, France*
- ³⁹*Korea Institute of Science and Technology Information, Daejeon 34141, Korea*
- ⁴⁰*West Virginia University, Morgantown, WV 26506, USA*
- ⁴¹*Università di Perugia, I-06123 Perugia, Italy*
- ⁴²*INFN, Sezione di Perugia, I-06123 Perugia, Italy*
- ⁴³*Syracuse University, Syracuse, NY 13244, USA*
- ⁴⁴*University of Minnesota, Minneapolis, MN 55455, USA*
- ⁴⁵*SUPA, University of Glasgow, Glasgow G12 8QQ, United Kingdom*
- ⁴⁶*LIGO Hanford Observatory, Richland, WA 99352, USA*
- ⁴⁷*Caltech CaRT, Pasadena, CA 91125, USA*
- ⁴⁸*Wigner RCP, RMKI, H-1121 Budapest, Konkoly Thege Miklós út 29-33, Hungary*
- ⁴⁹*Columbia University, New York, NY 10027, USA*
- ⁵⁰*Stanford University, Stanford, CA 94305, USA*
- ⁵¹*Università di Camerino, Dipartimento di Fisica, I-62032 Camerino, Italy*
- ⁵²*Università di Padova, Dipartimento di Fisica e Astronomia, I-35131 Padova, Italy*
- ⁵³*INFN, Sezione di Padova, I-35131 Padova, Italy*
- ⁵⁴*Institute of Physics, Eötvös University, Pázmány P. s. 1/A, Budapest 1117, Hungary*
- ⁵⁵*Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, 00-716, Warsaw, Poland*
- ⁵⁶*Rochester Institute of Technology, Rochester, NY 14623, USA*
- ⁵⁷*University of Birmingham, Birmingham B15 2TT, United Kingdom*
- ⁵⁸*INFN, Sezione di Genova, I-16146 Genova, Italy*
- ⁵⁹*RRCAT, Indore MP 452013, India*
- ⁶⁰*Faculty of Physics, Lomonosov Moscow State University, Moscow 119991, Russia*
- ⁶¹*SUPA, University of Strathclyde, Glasgow G1 1XQ, United Kingdom*
- ⁶²*The Pennsylvania State University, University Park, PA 16802, USA*
- ⁶³*OzGrav, University of Western Australia, Crawley, Western Australia 6009, Australia*
- ⁶⁴*Department of Astrophysics/IMAPP, Radboud University Nijmegen, P.O. Box 9010, 6500 GL Nijmegen, The Netherlands*
- ⁶⁵*Artemis, Université Côte d'Azur, Observatoire Côte d'Azur, CNRS, CS 34229, F-06304 Nice Cedex 4, France*
- ⁶⁶*Institut FOTON, CNRS, Université de Rennes 1, F-35042 Rennes, France*
- ⁶⁷*Washington State University, Pullman, WA 99164, USA*
- ⁶⁸*University of Oregon, Eugene, OR 97403, USA*
- ⁶⁹*Laboratoire Kastler Brossel, UPMC-Sorbonne Universités, CNRS, ENS-PSL Research University, Collège de France, F-75005 Paris, France*
- ⁷⁰*Carleton College, Northfield, MN 55057, USA*
- ⁷¹*OzGrav, University of Adelaide, Adelaide, South Australia 5005, Australia*
- ⁷²*Astronomical Observatory Warsaw University, 00-478 Warsaw, Poland*

- ⁷³VU University Amsterdam, 1081 HV Amsterdam, The Netherlands
⁷⁴University of Maryland, College Park, MD 20742, USA
⁷⁵School of Physics, Georgia Institute of Technology, Atlanta, GA 30332, USA
⁷⁶Université Claude Bernard Lyon 1, F-69622 Villeurbanne, France
⁷⁷Università di Napoli ‘Federico II,’ Complesso Universitario di Monte S.Angelo, I-80126 Napoli, Italy
⁷⁸NASA Goddard Space Flight Center, Greenbelt, MD 20771, USA
⁷⁹Dipartimento di Fisica, Università degli Studi di Genova, I-16146 Genova, Italy
⁸⁰RESCEU, University of Tokyo, Tokyo, 113-0033, Japan.
⁸¹Tsinghua University, Beijing 100084, China
⁸²Texas Tech University, Lubbock, TX 79409, USA
⁸³Kenyon College, Gambier, OH 43022, USA
⁸⁴Departamento de Astronomía y Astrofísica, Universitat de València, E-46100 Burjassot, València, Spain
⁸⁵Museo Storico della Fisica e Centro Studi e Ricerche Enrico Fermi, I-00184 Roma, Italy
⁸⁶National Tsing Hua University, Hsinchu City, 30013 Taiwan, Republic of China
⁸⁷Charles Sturt University, Wagga Wagga, New South Wales 2678, Australia
⁸⁸Center for Interdisciplinary Exploration & Research in Astrophysics (CIERA), Northwestern University, Evanston, IL 60208, USA
⁸⁹University of Chicago, Chicago, IL 60637, USA
⁹⁰Pusan National University, Busan 46241, Korea
⁹¹The Chinese University of Hong Kong, Shatin, NT, Hong Kong
⁹²INAF, Osservatorio Astronomico di Padova, I-35122 Padova, Italy
⁹³INFN, Trento Institute for Fundamental Physics and Applications, I-38123 Povo, Trento, Italy
⁹⁴OzGrav, University of Melbourne, Parkville, Victoria 3010, Australia
⁹⁵Università di Roma ‘La Sapienza,’ I-00185 Roma, Italy
⁹⁶Université Libre de Bruxelles, Brussels 1050, Belgium
⁹⁷Sonoma State University, Rohnert Park, CA 94928, USA
⁹⁸Departamento de Matemáticas, Universitat de València, E-46100 Burjassot, València, Spain
⁹⁹Montana State University, Bozeman, MT 59717, USA
¹⁰⁰Universitat de les Illes Balears, IAC3—IEEC, E-07122 Palma de Mallorca, Spain
¹⁰¹The University of Texas Rio Grande Valley, Brownsville, TX 78520, USA
¹⁰²Bellevue College, Bellevue, WA 98007, USA
¹⁰³Institute for Plasma Research, Bhat, Gandhinagar 382428, India
¹⁰⁴The University of Sheffield, Sheffield S10 2TN, United Kingdom
¹⁰⁵Dipartimento di Scienze Matematiche, Fisiche e Informatiche, Università di Parma, I-43124 Parma, Italy
¹⁰⁶INFN, Sezione di Milano Bicocca, Gruppo Collegato di Parma, I-43124 Parma, Italy
¹⁰⁷California State University, Los Angeles, 5151 State University Dr, Los Angeles, CA 90032, USA
¹⁰⁸Università di Trento, Dipartimento di Fisica, I-38123 Povo, Trento, Italy
¹⁰⁹Montclair State University, Montclair, NJ 07043, USA
¹¹⁰National Astronomical Observatory of Japan, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan
¹¹¹Canadian Institute for Theoretical Astrophysics, University of Toronto, Toronto, Ontario M5S 3H8, Canada
¹¹²Observatori Astronòmic, Universitat de València, E-46980 Paterna, València, Spain
¹¹³School of Mathematics, University of Edinburgh, Edinburgh EH9 3FD, United Kingdom
¹¹⁴University and Institute of Advanced Research, Koba Institutional Area, Gandhinagar Gujarat 382007, India
¹¹⁵IISER-TVM, CET Campus, Trivandrum Kerala 695016, India
¹¹⁶University of Szeged, Dóm tér 9, Szeged 6720, Hungary
¹¹⁷University of Michigan, Ann Arbor, MI 48109, USA
¹¹⁸Tata Institute of Fundamental Research, Mumbai 400005, India
¹¹⁹INAF, Osservatorio Astronomico di Capodimonte, I-80131, Napoli, Italy
¹²⁰Università degli Studi di Urbino ‘Carlo Bo,’ I-61029 Urbino, Italy
¹²¹INFN, Sezione di Firenze, I-50019 Sesto Fiorentino, Firenze, Italy
¹²²Physik-Institut, University of Zurich, Winterthurerstrasse 190, 8057 Zurich, Switzerland
¹²³American University, Washington, D.C. 20016, USA
¹²⁴University of Białystok, 15-424 Białystok, Poland
¹²⁵University of Southampton, Southampton SO17 1BJ, United Kingdom
¹²⁶University of Washington Bothell, 18115 Campus Way NE, Bothell, WA 98011, USA
¹²⁷Institute of Applied Physics, Nizhny Novgorod, 603950, Russia
¹²⁸Korea Astronomy and Space Science Institute, Daejeon 34055, Korea
¹²⁹Inje University Gimhae, South Gyeongsang 50834, Korea
¹³⁰National Institute for Mathematical Sciences, Daejeon 34047, Korea
¹³¹NCBJ, 05-400 Świerk-Otwock, Poland
¹³²Institute of Mathematics, Polish Academy of Sciences, 00656 Warsaw, Poland
¹³³Hillsdale College, Hillsdale, MI 49242, USA
¹³⁴Hanyang University, Seoul 04763, Korea
¹³⁵Seoul National University, Seoul 08826, Korea
¹³⁶NASA Marshall Space Flight Center, Huntsville, AL 35811, USA

- ¹³⁷*ESPCI, CNRS, F-75005 Paris, France*
- ¹³⁸*Southern University and A&M College, Baton Rouge, LA 70813, USA*
- ¹³⁹*College of William and Mary, Williamsburg, VA 23187, USA*
- ¹⁴⁰*Centre Scientifique de Monaco, 8 quai Antoine Ier, MC-98000, Monaco*
- ¹⁴¹*Indian Institute of Technology Madras, Chennai 600036, India*
- ¹⁴²*IISER-Kolkata, Mohanpur, West Bengal 741252, India*
- ¹⁴³*Whitman College, 345 Boyer Avenue, Walla Walla, WA 99362 USA*
- ¹⁴⁴*Indian Institute of Technology Bombay, Powai, Mumbai, Maharashtra 400076, India*
- ¹⁴⁵*Scuola Normale Superiore, Piazza dei Cavalieri 7, I-56126 Pisa, Italy*
- ¹⁴⁶*Université de Lyon, F-69361 Lyon, France*
- ¹⁴⁷*Hobart and William Smith Colleges, Geneva, NY 14456, USA*
- ¹⁴⁸*OzGrav, Swinburne University of Technology, Hawthorn VIC 3122, Australia*
- ¹⁴⁹*Janusz Gil Institute of Astronomy, University of Zielona Góra, 65-265 Zielona Góra, Poland*
- ¹⁵⁰*University of Washington, Seattle, WA 98195, USA*
- ¹⁵¹*King's College London, University of London, London WC2R 2LS, United Kingdom*
- ¹⁵²*Indian Institute of Technology, Gandhinagar Ahmedabad Gujarat 382424, India*
- ¹⁵³*Indian Institute of Technology Hyderabad, Sangareddy, Khandi, Telangana 502285, India*
- ¹⁵⁴*International Institute of Physics, Universidade Federal do Rio Grande do Norte, Natal RN 59078-970, Brazil*
- ¹⁵⁵*Andrews University, Berrien Springs, MI 49104, USA*
- ¹⁵⁶*Università di Siena, I-53100 Siena, Italy*
- ¹⁵⁷*Trinity University, San Antonio, TX 78212, USA*
- ¹⁵⁸*Van Swinderen Institute for Particle Physics and Gravity, University of Groningen, Nijenborgh 4, 9747 AG Groningen, The Netherlands*
- ¹⁵⁹*Abilene Christian University, Abilene, TX 79699, USA*
- ¹⁶⁰*Colorado State University, Fort Collins, CO 80523, USA*

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The detection of gravitational waves with Advanced LIGO and Advanced Virgo has enabled novel tests of general relativity, including direct study of the polarization of gravitational waves. While general relativity allows for only two tensor gravitational-wave polarizations, general metric theories can additionally predict two vector and two scalar polarizations. The polarization of gravitational waves is encoded in the spectral shape of the stochastic gravitational-wave background, formed by the superposition of cosmological and individually-unresolved astrophysical sources. Using data recorded by Advanced LIGO during its first observing run, we search for a stochastic background of generically-polarized gravitational waves. We find no evidence for a background of any polarization, and place the first direct bounds on the contributions of vector and scalar polarizations to the stochastic background. Under log-uniform priors for the energy in each polarization, we limit the energy-densities of tensor, vector, and scalar modes at 95% credibility to $\Omega_0^T < 5.6 \times 10^{-8}$, $\Omega_0^V < 6.4 \times 10^{-8}$, and $\Omega_0^S < 1.1 \times 10^{-7}$ at a reference frequency $f_0 = 25$ Hz.

Introduction – The direct detection of gravitational waves offers novel opportunities to test general relativity in previously unexplored regimes. Already, the compact binary mergers [1–5] observed by Advanced LIGO (the Laser Interferometer Gravitational Wave Observatory) [6, 7] and Advanced Virgo [8] have enabled improved limits on the graviton mass, experimental measurements of post-Newtonian parameters, and inference of the speed of gravitational waves, among other tests [3, 9–11].

Another central prediction of general relativity is the existence of only two gravitational-wave polarizations: the tensor plus and cross modes, with spatial strain tensors

$$\hat{e}_+ = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad \hat{e}_\times = \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad (1)$$

(assuming waves propagating in the $+\hat{z}$ direction). Generic metric theories of gravity, however, can allow for up to four additional polarizations: the x and y vector modes and the breathing and longitudinal scalar modes, with basis strain ten-

sors [12–14]

$$\begin{aligned} \hat{e}_x &= \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} & \hat{e}_y &= \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \\ \hat{e}_b &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix} & \hat{e}_l &= \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}. \end{aligned} \quad (2)$$

The observation of vector or scalar modes would be in direct conflict with general relativity, and so the direct measurement of gravitational-wave polarizations offers a promising avenue by which to test theories of gravity [14].

Recently, the Advanced LIGO-Virgo network has succeeded in making the first direct statement about the polarization of gravitational waves. The gravitational-wave signal GW170814, observed by both the Advanced LIGO and Virgo detectors, significantly favored a model assuming pure tensor polarization over models with pure vector or scalar polarizations [4, 15]. In general, however, the ability of the Advanced LIGO-Virgo network to study the polariza-

tion of gravitational-wave transients is limited by several factors. First, the LIGO-Hanford and LIGO-Livingston detectors are nearly co-oriented, preventing Advanced LIGO from sensitively measuring more than a single polarization mode [4, 9, 10, 15]. Second, at least five detectors are needed to fully characterize the five polarization degrees of freedom accessible to quadrupole detectors. Quadrupole detectors (those measuring differential arm motion) have degenerate responses to breathing and longitudinal modes, and can therefore measure only a single linear combination of scalar breathing and longitudinal polarizations [14–17].

Beyond compact binary mergers, another target for Advanced LIGO and Virgo is the stochastic gravitational-wave background. An astrophysical stochastic background is expected to arise from the population of distant compact binary mergers [18–23], core-collapse supernovae [24–26], and rapidly-rotating neutron stars [27–29]. In particular, the astrophysical background from compact binary mergers is likely to be detected by LIGO and Virgo at their design sensitivities [23]. A background of cosmological origin may also be present, due to cosmic strings [30, 31], inflation [32–35], and phase transitions in the early Universe [32, 33, 36–38].

Long duration gravitational-wave sources, like the stochastic background [39–42] or persistent signals from rotating neutron stars [43–45], offer a viable means of searching for non-standard gravitational-wave polarizations. Unlike gravitational-wave transients, which sample only a single point on the LIGO/Virgo antenna response patterns, long-duration signals contain information about many points on the antenna patterns. Long-duration signals therefore enable the direct measurement of gravitational-wave polarizations using the current generation of gravitational-wave detectors, without the need for additional detectors or an independent electromagnetic counterpart. The stochastic background is thus a valuable laboratory for polarization-based tests of general relativity [42].

In this Letter, we present the first direct search for vector and scalar polarizations in the stochastic gravitational-wave background. We analyze data recorded during Advanced LIGO’s first observing run (O1), which has previously been searched for both isotropic and anisotropic backgrounds of standard tensor polarizations [46, 47]. First, we describe the O1 data set and its initial processing. We then discuss the stochastic analysis, including the construction of Bayesian odds that indicate the non-detection of a generically-polarized stochastic background in our data. Finally, we present upper limits on the joint contributions of tensor, vector, and scalar polarizations to the stochastic gravitational-wave background. Additional details and results are presented in the Supplemental Materials, available online.

Data – We search Advanced LIGO data for evidence of a stochastic background, analyzing data recorded between September 18, 2015 15:00 UTC and January 12, 2016 16:00 UTC during LIGO’s O1 observing run. We do not include several days of O1 data recorded prior to September 18, but this has negligible impact on our results. We exclude

times containing the binary black hole signals GW150914 and GW151226, as well as the signal candidate LVT151012.

The initial data processing proceeds as in previous analyses [46, 48]. Time-domain strain measurements from the LIGO-Hanford and LIGO-Livingston detectors are down-sampled from 16384 Hz to 4096 Hz and divided into half-overlapping 192 second segments. Each time segment is then Hann-windowed, Fourier transformed, and high-pass filtered using a 16th order Butterworth filter with a knee frequency of 11 Hz. Finally, the strain data is coarse-grained to a frequency resolution of 0.03125 Hz and restricted to a frequency band from 20 – 1726 Hz. Within each segment, we compute the LIGO-Hanford and LIGO-Livingston strain auto-power spectral densities using Welch’s method [49].

Standard data quality cuts are performed in both the time and frequency domains to mitigate the effects of non-Gaussian instrumental and environmental noise [46, 47, 50]. In the time domain, 35% of data is discarded due to non-stationary detector noise, leaving 29.85 days of coincident observing time. In the frequency domain, an additional 21% of data is discarded to remove correlated narrowband features between LIGO-Hanford and LIGO-Livingston [46, 47, 50]. These narrowband correlations are due to a variety of sources, including injected calibration signals, power mains, and GPS timing systems. To estimate possible contamination due to terrestrial Schumann resonances [51–53], we additionally monitored coherence between magnetometers installed at both detectors. Schumann resonances were found to contribute negligibly to the stochastic measurement [46, 50].

We assume conservative 4.8% and 5.4% calibration uncertainties on the strain amplitude measured by LIGO-Hanford and LIGO-Livingston, respectively [54]. Phase calibration is a much smaller source of uncertainty and is therefore neglected [46, 55]. All results below are obtained after marginalization over amplitude uncertainties; see the Supplemental Materials for details.

Method – To search for a generically-polarized stochastic background, we will apply the methodology presented in Ref. [42]. This method is summarized below, and additional details are discussed in the Supplemental Materials.

The stochastic background may be detected in the form of a correlated signal between pairs of gravitational-wave detectors. We will assume that the stochastic background is stationary, isotropic, and Gaussian. For simplicity, we also assume that the background is uncorrelated between polarization modes. Finally, we assume that the tensor and vector contributions to the background are individually unpolarized (with equal contributions, for instance, from the tensor plus and cross modes). Certain theories may violate one or more of these assumptions. For example, the stochastic background is unlikely to remain strictly unpolarized in the presence of gravitational-wave birefringence, as in Chern-Simons gravity [58–60], while theories violating Lorentz invariance may yield a departure from isotropy [61, 62]. The violation of one or more of our assumptions would likely reduce our search’s sensitivity to the stochastic background.

Given the above assumptions, the expected cross-correlation between two detectors in the presence of a stochastic background is of the form [39–41, 56]

$$\langle \tilde{s}_1(f) \tilde{s}_2^*(f') \rangle = \frac{1}{2} \delta(f - f') \sum_A \Gamma_A(f) S_h^A(f). \quad (3)$$

Here, $S_h^A(f)$ is the one-sided gravitational-wave strain power spectral density of the net tensor ($A = T$), vector (V), and scalar (S) contributions to the stochastic background. The detectors' geometry is encoded in the overlap reduction functions $\Gamma_A(f)$, defined [39, 42, 56, 57]

$$\Gamma_A(f) = \frac{1}{8\pi} \sum_{a \in A} \int d\hat{n} F_1^a(\hat{n}) F_2^a(\hat{n}) e^{2\pi i f \hat{n} \cdot \Delta x / c}. \quad (4)$$

$F_I^a(\hat{n})$ is the antenna response function of detector I to signals of polarization a , Δx is the separation vector between detectors, and c is the speed of light. The integral is taken over all sky directions \hat{n} .

We will work not directly with $\Gamma_A(f)$, but rather with the *normalized* overlap reduction functions $\gamma_A(f) \propto \Gamma_A(f)/\Gamma_0$, where the constant Γ_0 is chosen such that $\gamma_T(f) = 1$ for co-located and co-oriented detectors. For Advanced LIGO, $\Gamma_0 = 1/5$, but in general its value will vary for other experiments like LISA and pulsar timing arrays [63]. The normalized overlap reduction functions for LIGO's Hanford-Livingston baseline are shown in Fig. 1. Because tensor, vector, and scalar modes each have distinct overlap reduction functions, the shape of a measured cross-correlation spectrum [Eq. (3)] will reflect the polarization content of the stochastic background [39, 42]. Of the three curves in Fig. 1, the scalar overlap reduction function is smallest in magnitude. This reflects the fact that the Advanced LIGO detectors have weaker geometrical responses to scalar-polarized gravitational waves than to tensor- and vector-polarized signals.

Conventionally, gravitational-wave backgrounds are parameterized by their energy-density spectra [56, 63]

$$\Omega(f) = \frac{1}{\rho_c} \frac{d\rho_{\text{GW}}}{d \ln f}, \quad (5)$$

where $d\rho_{\text{GW}}$ is the energy density in gravitational waves per logarithmic frequency interval $d \ln f$. We normalize Eq. (5) by $\rho_c = 3H_0^2 c^2 / 8\pi G$, the closure energy density of the Universe. Here, G is Newton's constant and H_0 is the Hubble constant; we take $H_0 = 68 \text{ km s}^{-1} \text{ Mpc}^{-1}$ [64]. The precise relationship between $\Omega(f)$ and $S_h(f)$ is theory-dependent. Under any theory obeying Isaacson's formula for the stress-energy of gravitational waves [65], the energy-density spectrum is related to $S_h(f)$ by [42, 56, 66]

$$\Omega(f) = \frac{2\pi^2}{3H_0^2} f^3 S_h(f). \quad (6)$$

Eq. (6) does not hold in general, however [66]. For ease of comparison with previous studies, we will instead take Eq.

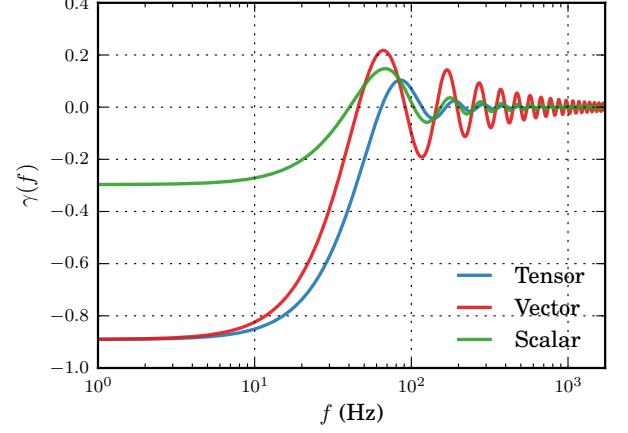


FIG. 1. Overlap reduction functions representing the Advanced LIGO network's sensitivity to stochastic backgrounds of tensor (blue), vector (red), and scalar-polarized (green) gravitational waves.

(6) as the *definition* of the canonical energy-density spectra $\Omega^A(f)$. The canonical energy-density spectra can be directly identified with true energy densities under any theory obeying Isaacson's formula. For other theories, $\Omega^A(f)$ can instead be understood simply as a function of the detector-frame observable $S_h^A(f)$.

Within each 192s time segment (indexed by i), we form an estimator of the visible cross-power between LIGO-Hanford and LIGO-Livingston:

$$\hat{C}_i(f) = \frac{1}{\Delta T} \frac{20\pi^2}{3H_0^2} f^3 \tilde{s}_{1,i}^*(f) \tilde{s}_{2,i}(f), \quad (7)$$

normalized such that the estimator's mean and variance are [42]

$$\langle \hat{C}_i(f) \rangle = \sum_A \gamma_A(f) \Omega^A(f) \quad (8)$$

and

$$\sigma_i^2(f) = \frac{1}{2\Delta T df} \left(\frac{10\pi^2}{3H_0^2} \right)^2 f^6 P_{1,i}(f) P_{2,i}(f), \quad (9)$$

respectively. Within Eqs. (7) and (9), ΔT is the segment duration, df the frequency bin-width, and $P_{I,i}(f)$ is the one-sided auto-power spectral density of detector I in time-segment i , defined by

$$\langle \tilde{s}_{I,i}^*(f) \tilde{s}_{I,i}(f') \rangle = \frac{1}{2} \delta(f - f') P_{I,i}(f). \quad (10)$$

The normalization of $\hat{C}(f)$ is chosen such that the contribution from each polarization appears symmetrically in Eq. (8); this choice differs by a factor of $\gamma_T(f)$ from the point estimate $\hat{Y}(f)$ typically used in stochastic analyses [42, 46, 48].

Finally, the cross-power estimators from each segment are optimally combined via a weighted sum to form a single cross-power spectrum for the O1 observing run,

$$\hat{C}(f) = \frac{\sum_i \hat{C}_i(f) \sigma_i^{-2}(f)}{\sum_i \sigma_i^{-2}(f)}, \quad (11)$$

with the corresponding variance

$$\sigma^{-2}(f) = \sum_i \sigma_i^{-2}(f). \quad (12)$$

Note that, unlike transient gravitational-wave searches, searches for the stochastic background are well-described by Gaussian statistics due to the large number of time-segments contributing to the final cross-power spectrum [67].

Given the measured cross-power spectrum $\hat{C}(f)$, we compute Bayesian evidences for various hypotheses describing the presence and polarization of a possible stochastic signal within our data. Evidences are computed using PyMultiNest [68], a Python interface to the nested sampling code MultiNest [69–73]. We consider several different hypotheses:

- Gaussian noise (N): No stochastic signal is present in our data, and the measured cross-power is due entirely to Gaussian noise.
- Signal (SIG): A stochastic background of any polarization(s) is present.
- Tensor-polarized (GR): The data contains a purely tensor-polarized stochastic signal, consistent with general relativity.
- Non-standard polarizations (NGR): The data contains a stochastic signal with vector and/or scalar contributions.

These evidences are combined to form two Bayesian odds [42]:

- Odds $\mathcal{O}_{\text{N}}^{\text{SIG}}$ for the presence of a stochastic signal relative to pure noise.
- Odds $\mathcal{O}_{\text{GR}}^{\text{NGR}}$ for the presence of non-standard polarizations versus ordinary tensor modes.

$\mathcal{O}_{\text{N}}^{\text{SIG}}$ quantifies evidence for the *detection* of a generically polarized stochastic background, and generally depends only on a background's total power, not its polarization content. $\mathcal{O}_{\text{GR}}^{\text{NGR}}$ indicates if the background's polarization is inconsistent with general relativity. In particular, the sensitivity of $\mathcal{O}_{\text{GR}}^{\text{NGR}}$ to non-standard polarizations is not significantly affected by the strength of any tensor polarization which may also be present [42]. See the Supplemental Materials for further details about our hypotheses and odds ratio construction, including the priors placed on these hypotheses and their parameters.

Results – Using the cross-power measured between LIGO-Hanford and LIGO-Livingston during Advanced LIGO's O1

TABLE I. 95% credible upper limits on the log-amplitudes of tensor, vector, and scalar modes in the stochastic background at reference frequency $f_0 = 25$ Hz. We assume an energy-density spectrum in which all three modes are present, and present limits following marginalization over the spectral index of each component [see Eq. (13)]. We show results for two different amplitude priors: a log-uniform prior ($dp/d\log \Omega_0 \propto 1$; top row) and a uniform prior ($dp/d\Omega_0 \propto 1$; bottom row). Additional parameter estimation results are shown in the Supplemental Materials.

Prior	$\log \Omega_0^T$	$\log \Omega_0^V$	$\log \Omega_0^S$	Ω_0^T	Ω_0^V	Ω_0^S
Log-Uniform	-7.25	-7.20	-6.96	5.6×10^{-8}	6.4×10^{-8}	1.1×10^{-7}
Uniform	-6.70	-6.59	-6.07	2.0×10^{-7}	2.5×10^{-7}	8.4×10^{-7}

observing run, we obtain odds $\ln \mathcal{O}_{\text{N}}^{\text{SIG}} = -0.53$ between Signal and Gaussian noise hypotheses, indicating a non-detection of the stochastic gravitational-wave background. Additionally, we find $\ln \mathcal{O}_{\text{GR}}^{\text{NGR}} = -0.25$, consistent with values expected in the presence of Gaussian noise [42]. (We will use ln and log to denote base- e and base-10 logarithms, respectively.)

Given our non-detection, we place upper limits on the presence of tensor, vector, and scalar contributions to the stochastic background. To simultaneously constrain the properties of each polarization, we will restrict our analysis to a model assuming the presence of tensor, vector, and scalar-polarized signals (this is the TVS hypothesis in the notation of the Supplemental Materials). Under this hypothesis, we model the total canonical energy-density of the stochastic background as a sum of power laws:

$$\Omega(f) = \Omega_0^T \left(\frac{f}{f_0} \right)^{\alpha_T} + \Omega_0^V \left(\frac{f}{f_0} \right)^{\alpha_V} + \Omega_0^S \left(\frac{f}{f_0} \right)^{\alpha_S}. \quad (13)$$

Here, Ω_0^A is the amplitude of polarization A at a reference frequency f_0 , and α_A is the corresponding spectral index. We take $f_0 = 25$ Hz [46]. Standard tensor-polarized stochastic backgrounds are predicted to be well-described by power laws in the Advanced LIGO band. The expected astrophysical background from compact binary mergers, for instance, is well-modeled by a power law with $\alpha_T = 2/3$ [18–20, 74].

We will consider two different prior distributions for the background amplitudes: a log-uniform prior between $10^{-13} \leq \Omega_0^A \leq 10^{-5}$ and a uniform prior between $0 \leq \Omega_0^A \leq 10^{-5}$. The former (log-uniform) corresponds to the prior adopted in Ref. [42]. The latter (uniform) implicitly reproduces the maximum likelihood analysis used in previous studies, and is included to allow direct comparison to previous stochastic results [46, 48]. The upper amplitude bound (10^{-5}) is consistent with limits placed by Initial LIGO and Virgo [48]. In order to be normalizable, the log-uniform prior requires a non-zero lower bound; although parameter estimation results will depend on the specific choice of lower bound, in general this dependence is weak [44]. Our lower bound (10^{-13}) is chosen to encompass small energy densities well below the reach of LIGO and Virgo at design sensitivity [23, 46].

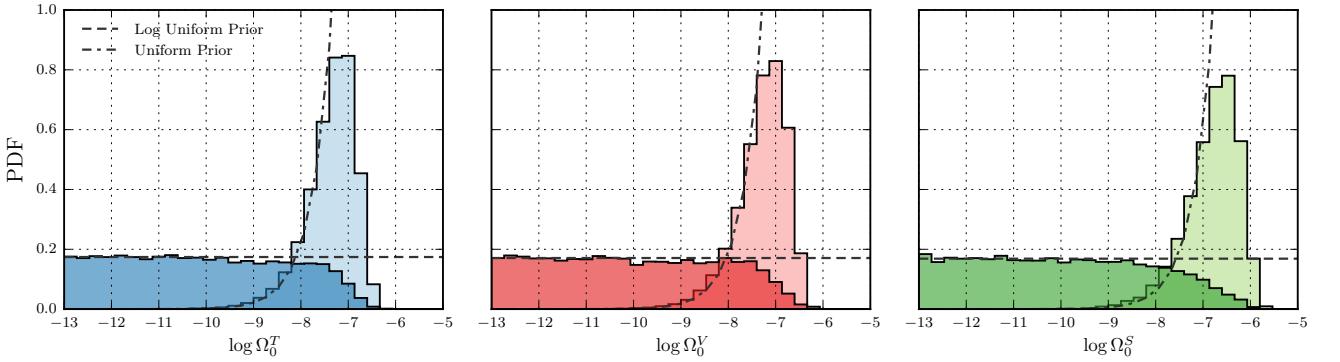


FIG. 2. Posteriors on the tensor (*left*), vector (*center*), and scalar (*right*) stochastic background amplitudes at reference frequency $f_0 = 25$ Hz. Within each subplot, dark posteriors show results obtained assuming log-uniform priors (dashed curves) on Ω_0^A , while light posteriors show results corresponding to uniform amplitude priors (dot-dashed curves). The prior curves shown here have been renormalized by constant factors to illustrate consistency with the posteriors below our measured upper limits. These posteriors correspond to the 95% credible upper limits listed in Table I. Relative to the log-uniform priors, the uniform amplitude priors preferentially weight loud stochastic signals and therefore yield more conservative upper limits.

Following Ref. [42], we take our spectral index priors to be $p(\alpha_A) \propto 1 - |\alpha_A|/\alpha_{\text{MAX}}$ for $|\alpha_A| \leq \alpha_{\text{MAX}}$ and $p(\alpha_A) = 0$ elsewhere. This prior preferentially weights flat energy-density spectra, penalizing spectra which are more steeply positively or negatively sloped in the Advanced LIGO band. We conservatively choose $\alpha_{\text{MAX}} = 8$, allowing for energy-density spectra significantly steeper than backgrounds predicted from known astrophysical sources (like compact binary mergers).

We perform parameter estimation using posterior samples obtained by PyMultiNest. Figure 2 shows posteriors on the tensor, vector, and scalar background amplitudes, under each choice of amplitude prior. The dashed and dot-dashed curves are proportional to the log-uniform and uniform amplitude priors, respectively; each prior curve has been renormalized by a constant factor to illustrate consistency between our priors and posteriors at small Ω_0^A . We can now place upper limits on the amplitude of each component at $f_0 = 25$ Hz. The 95% credible upper limits on the amplitude of each polarization are listed in Table I for each choice of prior (for convenience, we list limits in terms of both $\log \Omega_0^A$ and Ω_0^A). As no signal was detected, our posteriors on the spectral indices α_A are dominated by our prior. Full parameter estimation results, including posteriors on α_A , are given in the Supplemental Materials.

Care should be taken when comparing these upper limits to those obtained in previous analyses (e.g. Table I of Ref. [46]). Three important distinctions should be kept in mind. First, the amplitude posteriors in Fig. 2 (and hence the limits in Table I) are obtained after marginalization over spectral index. Previous analysis, on the other hand, typically assume specific fixed slopes or present exclusion curves in the $\Omega_0^T - \alpha_T$ plane [46]. Second, Bayesian upper limits may be strongly influenced by one's adopted prior. Uniform amplitude priors, for instance, preferentially weight larger signals and hence yield larger upper limits, while log-uniform priors support smaller

signal amplitudes, giving tighter limits. Finally, our results are obtained under a specific signal hypothesis allowing simultaneously for tensor, vector, and scalar polarizations. These limits are not generically identical to those that would be obtained if we allowed for tensor modes alone. In the Supplemental Materials, we have tabulated upper limits under a variety of signal hypotheses allowing for each unique combination of gravitational-wave polarizations (our results, though, do not vary considerably between hypotheses). We have additionally verified that, under the GR (tensor-only) hypothesis with delta-function priors on the background's spectral index, we recover upper limits identical to results previously published in Ref. [46].

Conclusion – The direct measurement of gravitational-wave polarizations may open the door to powerful new tests of gravity. Such measurements largely depend only on the geometry of a gravitational wave's strain and its direction of propagation, not on the details of any specific theory of gravity. Recently, the Advanced LIGO-Virgo observation of the binary black hole merger GW170814 has enabled the first direct study of gravitational-wave polarizations [4, 15]. While LIGO and Virgo are limited in their ability to discern the polarization of gravitational-wave transients, the future construction of additional detectors, like KAGRA [75, 76] and LIGO-India [77], will help to break existing degeneracies and allow for increasingly precise polarization measurements.

Long-duration signals offer further opportunities to study gravitational-wave polarizations. Detections of continuous sources like rotating neutron stars [44, 45] and the stochastic background [42] will offer the ability to directly measure and/or constrain gravitational-wave polarizations, even in the absence of additional detectors. In this Letter, we have conducted a search for a generically-polarized stochastic background of gravitational waves using data from Advanced LIGO's O1 observing run. Although we find no evidence for the presence of a background (of any polarization), we have

succeeded in placing the first direct upper limits (listed in Table I) on the contributions of vector and scalar modes to the stochastic background.

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