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$3₃$ The behaviour of fibre-reinforced composites subjected to a soft ⁴ impact-loading: An experimental and numerical study

7 Haibao Liu ^a, Jun Liu ^a, Cihan Kaboglu ^a, Jin Zhou ^b, Xiangshao Kong ^c, Bamber R.K. Blackman ^a, 8 Anthony J. Kinloch^{a,*}, John P. Dear^{a,*}

⁹ a Department of Mechanical Engineering, Imperial College London, South Kensington Campus, London SW7 2AZ, UK
10 b School of Mechanical Engineering, Yi'an Jigotong University, Yi'an 710049, People's Penublic of China

^b School of Mechanical Engineering, Xi'an Jiaotong University, Xi'an 710049, People's Republic of China
11 f Departments of Naval Architecture. Ocean and Structural Engineering. School of Transportation. Wuha

^c Departments of Naval Architecture, Ocean and Structural Engineering, School of Transportation, Wuhan University of Technology, Wuhan, Hubei 430063, 12 People's Republic of China

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ABSTRACT

The present paper presents experimental and numerical studies on the behaviour of com- 28 posite laminates subject to impact loading by soft projectiles to represent the impact of a 29 small bird or hail-stone. In this research, gas-gun experiments are performed to study 30 woven carbon-fibre reinforced poly (ether-ether ketone) (CF/PEEK) composites subjected 31 to an impact by soft-gelatine projectiles. In addition, woven carbon-fibre reinforced epoxy 32 (CF/epoxy) composite specimens are also evaluated using gelatine projectiles to investigate 33 the effect of the matrix system on the impact response of the composites. A high-speed 34 camera is employed to capture the deformation of the projectiles and a three- 35 dimensional (3D) Digital Image Correlation (DIC) system is used to record the deformation 36 of the impacted composite specimens. A Finite Element (FE) model is developed to simu- 37 late the impact by a soft projectile on the composite specimens. Good agreement is shown 38 between the predictions from using the FE model and the experimental results. 39

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44 1. Introduction

 With their increasing application in load-bearing structures, polymer-matrix fibre-reinforced composite materials have attracted much attention from both academia and industry. With an appropriate lay-up, such composites can possess excel- lent in-plane properties [\[1–5\]](#page-17-0). However, the effect of impact loading, e.g. by a high-velocity soft-impact, on the residual through-thickness properties is still a key safety concern for composite structures [\[6–9\].](#page-17-0) With this in mind, gas-gun impact experiments have been widely used to evaluate the reliability of composite structures and components. Indeed, a number of researchers have investigated the behaviour of composites subjected to impact loading by soft-body projectiles.

 For example, Heimbs and Bergmann [\[10\]](#page-17-0) conducted an experimental study on the response of composite specimens under high-velocity impact loading by soft-body gelatine projectiles. In their experiments, the composites were subjected to tensile or compressive loading before the impact experiments, to represent the loading conditions of aircraft structures when subjected to foreign-object impact by a soft body. The effect of pre-load was to modify the force-displacement response, and related stiffness of the panel, with a subsequent increase of damage. Zbrowski [\[11\]](#page-17-0) performed soft-body impact tests on the elements of a composite tail-plane component using a gas-gun system. The soft projectile was again

⇑ Corresponding authors. E-mail address: j.dear@imperial.ac.uk (J.P. Dear).

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EFA 104448 No. of Pages 19, Model 3G

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

 made of gelatine. The head-on and off-centre collisions on elements of the tail-plane were studied using two high-speed cameras to record the interaction between the projectile and the composite component. Damage inspection of the tested components showed that the head-on collision significantly damaged the vertical tail-plane, but the off-centre collision caused only minor permanent deformation and, importantly, did not damage the leading edge of the component. Johnson and Holzapfel [\[12\]](#page-17-0) employed finite element (FE) analysis codes to simulate the soft impact on the composite shell structures. The intralaminar and interlaminar damage models were developed and implemented in commercial explicit FE codes. The developed composites failure models and code were applied to simulate soft impact on idealised aerostructures. The predic- tive capability of the developed models were discussed for capturing the loading response of composite aircraft structures subjected to deformable soft body impact.

 In the present research, the results from a fundamental experimental and numerical study on the impact behaviour of composite laminates subjected to a soft-body impact are presented. For the experimental studies, a well-defined manufacturing process, which is easy to perform and control, is developed for the preparation of the gelatine projectiles. These gelatine projectiles are subsequently employed to perform gas-gun impact tests on the composite laminates which act as the target specimens. A thermoplastic polymer-matrix composite (i.e. a reinforced poly (ether-ether ketone) (CF/PEEK) composite) and a thermoset polymer-matrix composite (i.e. a carbon-fibre reinforced epoxy (CF/epoxy) composite) are stud- ied and compared to investigate the effect of the matrix system on the impact response. A high-speed camera is employed to capture the deformation and flow of the gelatine projectiles during the test and the deformations undergone by the compos- ite specimens are recorded using a three-dimensional (3D) Digital Image Correlation (DIC) system. For the numerical studies, a FE model is developed, using the 'Abaqus/Explicit 2017' software code, to model the soft impact on the composites. The model implemented in the FE code for predicting the initiation of intralaminar damage in the fibre-reinforced composites is based upon the Hashin damage approach [\[13–15\],](#page-17-0) which has a higher computational efficiency than other possible 78 sub-routine damage $\{\circ\varphi\}$ ls, and for predicting the initiation of interlaminar damage is based upon the Abaqus in-built cohe- sive solution $[15-17]$ The evolution of the damage during the impact event is then also predicted by implementing damage evolution laws in the FE code as a sub-routine. The interlaminar damage evolution law is based on a linear-softening mate- rial model embedded into a bilinear cohesive law. The soft-gelatine projectile is modelled using the Smoothed Particle Hydrodynamics (SPH) technique [\[18\].](#page-18-0) The modelling results, including predictions of (a) the deformation and flow of the projectile, (b) the deformation of the impacted composite and (c) the location and extent of the damage suffered by the com- posite, are then compared with the corresponding experimental results. In this paper, the focus of the research presented, has been to study soft impact on woven carbon fibre composites employing PEEK and epoxy as matrix materials and develop SPH models to describe the impact process and damage generated.

2. The modelling approach

2.1. Modelling the response of the projectile

 The SPH approach [\[18\]](#page-18-0) was employed to model the behaviour of the gelatine projectile within the 'Abaqus/Explicit 2017' code, as discussed later. For the SPH method to capture the response of the soft-gelatine projectile upon impact of the com- posite, a constitutive law is required with suitable material properties employed for the gelatine projectile. The model used was originally developed for ballistic impact in metals and describes an isotropic elastic-plastic material subjected to rela- tively low pressures with an equation of state (EOS) describing the hydrodynamic pressure versus volume behaviour at high pressures. The linear Mie-Grüneisen EOS was employed to define the coupled equations for pressure and internal energy [\[15\].](#page-17-0) The most common form for this EOS is given by:

$$
p - p_H = \Gamma \rho (E_m - E_H) \tag{1}
$$

99 where p is the pressure which is defined as positive in compression. The Hugoniot pressure, p_{μ} , is a function only of the den-100 sity and can be ascertained from fitting to the experimental data. The parameters E_m and E_H are the internal energy per unit 101 mass and the specific energy per unit mass (i.e. the Hugoniot energy), respectively. The parameter, ρ , is the current density of 102 the gelatine projectile. The parameter, Γ , is the Grüneisen ratio and is defined by: 103

$$
\Gamma = \Gamma_0 \frac{\rho_0}{\rho} \tag{2}
$$

106 where Γ_0 is a material constant and ρ_0 is the reference density of the gelatine projectile. The specific energy per unit mass,
 E_H , is related to the Hugoniot pressure by: E_H , is related to the Hugoniot pressure by:

$$
E_H = \frac{p_H \eta}{2\rho_0} \tag{3}
$$

111 where $\eta = 1 - \rho_0/\rho$ and η is the nominal volumetric compressive strain. The elimination of Γ and E_H from the above equa-
112
113 tions yields:

$$
p = p_H \left(1 - \frac{\Gamma_0 \eta}{2} \right) + \Gamma_0 \rho_0 E_m \tag{4}
$$

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx 33

116 In the above equation, the pressure, p, is a function of the Hugoniot pressure, p_H , and the nominal volumetric compressive 117 strain, η . Once the relationship between p_H and η is defined, the pressure, p, can be expressed as a single-variable function. To 118 achieve this, the linear U_s versus U_p relationship was employed to fit the curve of the Hugoniot pressure versus the nominal 119 volumetric compressive strain. The term U_s is the shock-wave velocity. The term U_p is the particle velocity of the projectile 120 and the measured value of U_p was assigned to all the 8-node linear-brick (C3D8R) elements when the FE model was started, 121 as discussed in detail later. However, immediately after initial contact of the projectile with the composite, these elements 122 for the projectile were converted to continuum particle (PC3D) elements and the value of U_p assigned to the particle ele-123 ments was then continually updated based upon the loading conditions on the particles after the initial contact. Assuming 124 the usual linear U_s versus U_p relationship, then the Hugoniot pressure versus the nominal volumetric compressive strain 125 equation is given by: 126

128
$$
p_H = \frac{\rho_0 c_0^2 \eta}{(1 - s\eta)^2}
$$
 (5)

129 where the fitting coefficient, s, is the slope of the linear relationship between U_s and U_p : 130

$$
U_s = c_0 + sU_p \tag{6}
$$

 $\overline{\mathbf{c}}$

133 where c_0 is the reference speed of sound in the gelatine projectile. With the above assumptions, the relationship between the 134 pressure, p, and the nominal volumetric compressive strain, η may now be written as: 135

$$
p = \frac{\rho_0 c_0^2 \eta}{\left(1 - s\eta\right)^2} \left(1 - \frac{\Gamma_0 \eta}{2}\right) + \Gamma_0 \rho_0 E_m \tag{7}
$$

138 Thus, in the FE model, see below, Eqs. (5) and (6) were employed to define the parameters in the EOS for modelling the 139 gelatine projectile and Eq. (7) was used to predict the contact pressure between the gelatine projectile and the composite.

140 2.2. Modelling the response of the composites

141 2.2.1. The intralaminar damage model

 The model for predicting the initiation of any intralaminar damage was implemented within the 'Abaqus/Explicit 2017' FE 143 code, as discussed later, and was based upon Hashin's theory $[13–15]$. In Hashin's damage model, four different types of damage mechanisms, which arise from tensile fibre failure, compressive fibre failure, tensile matrix failure and compressive matrix failure, are employed to capture the initiation of intralaminar damage in the unidirectional-fibre sub-plies. The mate- rial coordinate system in the unidirectional-fibre sub-ply was defined as the 1-2-3 coordinate system, where the longitudinal fibre-direction is defined as the 11-direction and the transverse direction, perpendicular to the longitudinal fibre-direction, was defined as the 22-direction. The general forms of the damage criteria in Hashin's approach to model the initiation of the above four different types of damage are given as:

150

Tensile fibre failure
$$
(\hat{\sigma}_{11} \ge 0)
$$
: $F_f^t = \left(\frac{\hat{\sigma}_{11}}{X^T}\right)^2$ (8)

153

Compressive fibre failure $(\widehat{\sigma}_{11} < 0)$: $F_f^c = \left(\frac{\widehat{\sigma}_{11}}{X^c}\right)$ $\left(\widehat{\sigma}_{11}\right)^2$ 155 Compressive fibre failure $(\hat{\sigma}_{11} < 0)$: $F_f^c = (\frac{\hat{\sigma}_{11}}{\hat{\chi}^c})$ (9)

$$
156 \\
$$

159

161

Tensile matrix failure $(\widehat{\sigma}_{22} \ge 0) : \quad F_m^t = \left(\frac{\widehat{\sigma}_{22}}{Y^T}\right)$

 $\langle \hat{\sigma}_{22} \rangle^2$ Tensile matrix failure $(\hat{\sigma}_{22} \ge 0)$: $F_m' = \left(\frac{\sigma_{22}}{Y^T}\right)$ (10)

Compressive matrix failure
$$
(\hat{\sigma}_{22} < 0)
$$
: $F_m^c = \left(\frac{\hat{\sigma}_{22}}{2S^T}\right)^2 + \left[\left(\frac{Y^c}{2S^T}\right)^2 - 1\right] \frac{\hat{\sigma}_{22}}{Y^c} + \left(\frac{\hat{\tau}_{12}}{S^L}\right)^2$ (11)

162 In the above equations, the indices on the terms F_f^t , F_f^c , F_m^t and F_m^c represent the four types of damage of tensile fibre fail-163 ure, compressive fibre failure, tensile matrix failure and compressive matrix failure, respectively, and failure is predicted to 164 occur when $F \ge 1$. The parameters, X^T and X^C denote the tensile and compressive strengths in the longitudinal fibre-165 direction, respectively. The terms Y^T and Y^C are the tensile and compressive strengths in the transverse direction, respec-166 tively; S^L and $S^T = Y^C/2$ denote the shear strengths in the longitudinal and transverse directions to the fibres, respectively; 167 and the term $\hat{\sigma}_{11}$, $\hat{\sigma}_{22}$ and $\hat{\tau}_{12}$ are components of the effective stress tensor, $\hat{\sigma}$, that are used to evaluate the above criteria.
168 The compressive matrix failure criterion emploved is based o The compressive matrix failure criterion employed is based on a quadratic expression which incorporates stress interactions 169 and this can be traced back to the von Mises yield criteria.

18 February 2020

173

4 H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

170 Corresponding to the damage initiation mechanisms defined in Hashin's criteria, four damage parameters, d_f^t , d_f^c , d_m^t and 171 d_m^c , were implemented in the damage evolution model. A general form of the damage variable for a particular damage ini-172 tiation mechanism is given by $[15]$:

$$
d = \frac{e^f(\varepsilon - \varepsilon^0)}{\varepsilon(\varepsilon^f - \varepsilon^0)}\tag{12}
$$

176 where $d = d_f^t$ represents fibre tension and $\alpha = d_f^c$ represents fibre compression failure, $d = d_m^t$ represents matrix tension 177 failure and $d = d_m^c$ represents matrix tailure, respectively. The strain, ε , is the equivalent strain in the composite ply. The 178 strain values, ε^0 and ε^f , are the equivalent strains corresponding to the initiation of failure and final failure, respectively. 179 For fibre tension or fibre compression failure, the terms ε , \bigodot and ε' are assigned to be $\varepsilon = \varepsilon_{11}$, $\varepsilon^0 = \varepsilon_{11}^0$ and $\varepsilon' = \varepsilon_{11}^0$, respec-180 tively. For tensile or compressive matrix failure, the terms $\epsilon, \epsilon^{\sigma}$ and ϵ^f are assigned to be $\epsilon = \epsilon_{22}$, $\epsilon^0 = \epsilon_{22}^0$ and $\epsilon^f = \epsilon_{22}^f$, respec-181 tively. In the damage evolution model, the values of the initial failure strains, ε^0 , are equal to the strain values corresponding 182 to damage initiation, which may be directly obtained from the computation via implementing Eqs. (8) to (11) , respectively. 183 The final failure strains may be determined from a knowledge of the tensile, $G_{lc}|_{ft}$, and compressive, $G_{lc}|_{fc}$, intralaminar ply 184 fracture energies in the longitudinal fibre-direction, and the tensile, $G_{lc}|_{mt}$, and compressive, $G_{lc}|_{mc}$, interlaminar ply fracture 185 energies in the transverse to the fibre-direction.

186 Three damage variables, d_f , d_m and d_s , which reflect fibre damage, matrix damage and shear damage, respectively, were 187 derived from the damage parameters, d_f^t , d_f^c , d_m^t and d_m^c , as follows:

$$
190 \tFor fibre damage: \t df = \begin{cases} d_f^t & \hat{\sigma}_{11} \\ d_f^c & \hat{\sigma}_{11} \end{cases} \tbinom{\sum_{i=1}^{n} d_i^c}{\sum_{i=1}^{n} d_i^c}
$$
 (13)

$$
\text{For matrix damage:} \quad d_m = \begin{cases} d_m^t & \hat{\sigma}_{22} \\ d_m^c, & \hat{\sigma}_{22} \end{cases} \tag{14}
$$

194

205

$$
\text{For shear damage}: \quad d_s = 1 - \left(1 - d_f^t\right) \left(1 - d_f^c\right) \left(1 - d_m^c\right) \left(1 - d_m^c\right) \tag{15}
$$

197 During the evolution of damage, the derived damage variables, d_f , d_m and d_s , were employed to update the stiffness 198 matrix of the composite ply and to compute the degraded stresses that were acting. For more details, refer to the Abaqus 199 2017 documentation [\[15\]](#page-17-0).

200 2.2.2. The interlaminar damage model

201 The initiation of any interlaminar damage in the composite laminates was captured by using a quadratic-stress criterion, 202 which was implemented within the FE code, as discussed later, and is given by $[15-17]$: 203

$$
\left(\frac{\langle t_{33}\rangle}{t_{33}^0}\right)^2 + \left(\frac{t_{31}}{t_{31}^0}\right)^2 + \left(\frac{t_{32}}{t_{32}^0}\right)^2 \ge 1\tag{16}
$$

206 where t_i (i = 33, 31, 32) represent the current normal and shear stresses, and t_i^0 (i = 33, 31, 32) represent the normal and 207 shear cohesive-law strengths, when the separation is either purely normal (i.e. the 33) direction to the interface, or purely 208 in the first shear (i.e. 31), or the second shear (i.e. 32) directions, respectively. The interlaminar damage is assumed to initiate 209 when the above quadratic interaction function, involving the ratios of the stresses, reaches a value of one. Thus, employing 210 Eq. (16), the value of the displacement, δ^o , at the initiation of damage may be deduced.

211 The evolution of interlaminar damage during the impact event was modelled using a linear-softening material model 212 embedded into a bilinear surface cohesive law, where the traction is plotted versus the displacement, δ . This was imple-213 mented as a sub-routine in the FE code $[15-17]$. This embedded interface element requires a value of the interlaminar frac-214 ture energy, G_c , and this represents the area under the bilinear cohesive $\langle \hat{w} \rangle$ The energy-based Benzeggagh-Kenane (B-K) 215 [\[15\]](#page-17-0) criterion for Mixed-mode propagation was used to derive a value G_c for the growth of the delamination between the 216 composite plies, as given by: 217

$$
G_c = G_{lc} + (G_{llc} - G_{lc}) \left[\frac{G_{ll}}{G_l + G_{ll}} \right]^{\eta}
$$
\n
$$
(17)
$$

220 where G_{Ic} is the Mode I (opening tensile) interlaminar facture energy, G_{Ilc} is the Mode II (in-plane shear) interlaminar facture 221 energy and η is the B-K Mixed-mode interaction exponent, which may all be experimentally measured. The parameters G_l 222 and G_{II} are the current Mode I and Mode II energy-release rates, respectively, as calculated from the FE code. Complete frac-223 ture of the interface element was assumed to occur, and delamination results, when the cohesive traction vanishes at the end

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx \sim 5

224 of the degradation step. That is when the displacement, δ , of the interface element, as determined in the FE code, attains the 225 criterion: 226

228 $\delta \geq \delta^f$ (18)

229 $\;\;\;\;$ where δ^f is the displacement of the interface element at failure.

230 3. The projectiles and composites

231 3.1. The projectiles

 A well-defined process, which is relatively simple and controllable, has been developed for preparing the soft-gelatine projectiles to a uniform standard. The ingredients used to prepare these projectiles were gelatine powder and distilled water. The gelatine powder was supplied by Honeywell Specialty, Germany. The detailed procedure, to manufacture the gelatine projectiles, is presented in Table 1. The gelatine projectiles had a nominal diameter of 23 mm and a nominal length of $-$ 45 mm. The photograph of a typical gelatine projectile is given in [Fig. 1](#page-5-0) and [Table 2](#page-5-0) shows the dimensions of the gelatine projectiles [\[18\].](#page-18-0) Due to their relatively low hardness, the gelatine projectiles initially tended to deform during the launching event from the gas-gun. To eliminate this problem, a plastic sabot was developed to maintain the shape of the gelatine pro- jectile during the acceleration phase of the impact tests. The unassembled and assembled projectile-sabot system is shown in [Fig. 2](#page-6-0).

241 3.2. Composite specimens

242 A woven T300 carbon-fibre reinforced PEEK composite and a woven T300 carbon-fibre reinforced 'Toray 3631' epoxy 243 composite were studied. The woven carbon-fibre ply possessed a $[0-90^\circ]$ architecture. These materials were supplied by 244 Haufler Composites, Germany. An Out-of-Autoclave (OOA) manufacturing route was employed to consolidate the CF/PEEK 245 prepregs and an autoclave was used to cure the CF/epoxy prepregs. Diagrams of the processing schedules for the CF/PEEK 246 prepregs and the CF/epoxy prepregs are shown in [Fig. 3a](#page-6-0) and b, respectively. Composite target test specimens were 247 machined from the composite panels using a diamond saw and a floor-standing drill. The lay-up employed for the woven 248 CF/PEEK and woven CF/epoxy composites was $[0-90^\circ]_{4s}$ and the nominal thickness of the manufactured specimens was 249 2 mm. The geometry of the composite target test specimens for the impact tests is given in [Fig. 4](#page-6-0). [Table 3](#page-7-0) gives all the dimen-250 sions of the specimens, where H and W are the specimen height and width, respectively. The length, d_3 , defines the size of the 251 DIC pattern area. The length, d_1 , defines the distance between the sample edge and the centre line of the holes and d_2 defines 252 the distance between each of the holes. The radius of each hole is R. For the DIC measurement, the specimens were first 253 painted on the rear-face using a white matt paint and then 'speckled' using a paintbrush to form the matt-black pattern.

254 4. Experimental investigations

255 4.1. The gas-gun experiments

 A helium-propellant gas-gun, which has a four-litre pressure vessel and a three-metre-long barrel, was employed to accelerate the projectiles in the impact tests. The velocity of the projectile was adjusted by changing the pressure of the ves- sel. The incident velocity of the projectiles was measured using two pairs of infrared sensors located at the end of the barrel. A new projectile and a new sabot were employed for each impact test. The schematic of the experimental set-up for the gas- gun experiments is shown in [Fig. 5.](#page-7-0) During the experiments, the composite target specimen was fixed by a specimen support and this consisted of two main components: one component being the 20 mm thick steel supporting plate, which had a

Table 1

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

Fig. 1. The photograph of a gelatine projectile.

262 70 mm \times 70 mm cut-out and the other component was the 15 mm thick steel clamping plate, which also had an opening of 263 70 mm \times 70 mm. 70 mm \times 70 mm.

4.2. Digital Image Correlation (DIC) measurements

 A 3D DIC system was used to measure the deformation of the rear-face of the specimens during impact loading. Two 'Phantom Miro M/R/LC310' high-speed cameras, supplied by Vision Research Phantom, USA, were employed. A pair of iden- tical 'Nikon' lenses, with a fixed focal length of 50 mm, supplied by Nikon, UK, were used with these two cameras. During the tests, the recording rate of these two cameras was set at 40,000 frames per second and they were triggered simultaneously by the signal generated from the infrared sensors. To achieve the brightness required for the high-speed DIC measurements, two bright-light sources, which were only turned on a few seconds before the gas-gun was fired, were employed to illumi- nate the rear-face of the composite specimens, which were painted with matt white paints and speckled using black dots. 272 The area of interest for the DIC measurement was 60 mm \times 60 mm. It should be noted that the DIC technique only records 273 surface displacements and strains but this is useful in recording the overall displacemen surface displacements and strains but this is useful in recording the overall displacement response of the panel before dam-age and can detect surface damage when it occurs.

4.3. Damage inspection

 After the impact experiments, visual inspections were undertaken on the composite specimens and photographs were taken from the rear-faces of the post-impacted specimens. In general, the type of damage suffered by the composites on the rear-face could be categorised as: (a) no visible damage present, (b) cracking observed, (c) fracture having occurred, and (d) perforation (i.e. penetration of the projectile through the specimen) having occurred. The main difference between 'type (b) cracking' and 'type (c) fracture' is whether there was fibre breakage observed. For 'type (b) cracking' this was defined as when cracks were only observed in the matrix. However, for 'type (c) fracture', fibre failure was also observed. Schematics of these descriptions for status of the post-impacted composites are shown in [Fig. 6](#page-7-0).

5. Experimental results

5.1. Deformation of the gelatine projectile

 [Fig. 7](#page-7-0) shows the deformation of the gelatine projectile recorded by a high-speed camera during an impact with the CF/ PEEK composite specimen for an impact energy of 37 J. Within the resolvable time intervals, the time, t, corresponding to the 287 initial contact was defined as 0.0 ms, as shown in [Fig. 7c](#page-7-0). It was found that at the beginning of the impact event (i.e. t = 0.0 ms) the shape of the gelatine projectile was well preserved, which ensured that the gelatine projectile impacted

Table 2

Physical properties of the gelatine projectiles [\[18,36\].](#page-18-0)

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx 7

Fig. 2. Schematic of the disassembled (left) and assembled (right) projectile and sabot system.

Fig. 3. Processing schedules for: (a) the CF/PEEK prepregs and (b) the CF/epoxy prepregs.

Fig. 4. Schematic drawing of the composite specimens.

EFA 104448 No. of Pages 19, Model 3G

8 **B. Example 2018** H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

Table 3

Dimensions of the composite target test specimens.

Fig. 5. Schematic of the experimental set-up for the gas-gun impact tests.

Fig. 6. Schematics of the types of post-impact damage on the rear-face of the composites: (a) no visible damage, (b) cracking, (c) fracture, and (d) perforation.

Fig. 7. Deformation history of the gelatine projectile for a 37 J impact energy impacting the CF/PEEK composite.

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx \sim 9

289 the centre of the specimen and then deformed symmetrically. However, in [Fig. 7g](#page-7-0) for $t = 0.4$ ms, the gelatine projectile can 290 clearly be seen to be flowing freely after impact.

291 5.2. Effects of the impact energy of the gelatine projectile

 To study the effects of the impact energy on the response of the CF/PEEK composites subjected to soft impact-loading, these composites were impacted using gelatine projectiles fired at four different impact velocities, and hence with different impact energies. The testing configurations for investigating the effects of the impact energy on the impact response of the CF/PEEK specimens are given in Table 4.

296 5.2.1. Comparison of the Digital Image Correlation (DIC) results

 The 3D DIC system was employed to measure the major strain and out-of-plane (OOP) displacement on the rear-faces of the composites. The main DIC results obtained from the CF/PEEK composites, impacted by gelatine projectiles at different energy levels, are summarised in Table 5. (It should be noted that due to fracture of the rear-face during 'Test GCP-IV' when an energy level of 72 J was used, no accurate value for the maximum major strain could be obtained from the DIC results for this test.) As the impact energy is steadily increased, the maximum major strain and maximum OOP displacement both increased in value.

 [Figs. 8 and 9](#page-9-0) present the typical DIC results obtained from the CF/PEEK composite impacted by a gelatine projectile with impact energy of 37 J. [Fig. 8a](#page-9-0) shows the major strain maps, from which the evolution of the major strains along the horizon- tal mid-section, during the loading and unloading events, were also determined, [Fig. 8](#page-9-0)b. It should be noted that the total loading time for the DIC maps was 0.175 ms, during which time the major strain increased from 0.0 to 0.013. The average strain-rate, $\dot{\varepsilon}$, is given by: 308

$$
\dot{\varepsilon} = \frac{\Delta \varepsilon}{\Delta t} \tag{19}
$$

311 with $\Delta \varepsilon$ and Δt representing the strain and time increments, respectively. For the complete loading event, then $\Delta \varepsilon = 0.013$
312 and $\Delta t = 0.175$ ms which gives the average strain rate $\dot{\varepsilon}$ as 74.3 s⁻ 312 and $\Delta t = 0.175$ ms, which gives the average strain rate, ε , as 74.3 s⁻¹. (With respect to the numerical modelling studies dis-313 cussed below, it should be noted that at this value of strain rate then significant rate effects have not been previously 314 observed on the elastic and failure properties of such composites [\[20\]](#page-18-0).) The OOP displacement contours, corresponding to 315 different times during the impact tests, were also obtained from the DIC results and are shown in [Fig. 9a](#page-9-0) for an impact energy 316 of 37 J. Similarly, the OOP displacements along the horizontal mid-section, during the loading and unloading process of the 317 specimen, were also obtained and are shown in [Fig. 9b](#page-9-0).

318 5.2.2. Comparison of the post-impact damage

 Representative photographs taken of the rear-faces of two of the gelatine-impacted CF/PEEK specimens are shown in [Fig. 10,](#page-10-0) along with corresponding magnified images of the central area. In [Fig. 10](#page-10-0)a, where the CF/PEEK composite was impacted by a gelatine projectile with energy of 37 J, no visible damage was observed. The same observation, of no visible damage, was recorded for the CF/PEEK tests conducted at impact energy levels of 53 J and 64 J. In contrast, the CF/PEEK com- posite impacted using a gelatine projectile with an impact energy of 72 J has suffered 'type (c)' fracture damage, with crack-ing in the matrix mainly being confined to the central area of the specimen, as shown in [Fig. 10](#page-10-0)b. Further, obvious fibre

GCP-III Gelatine 20 ± 0.5 80 $\pm 2.5\%$ 64 $\pm 5\%$ GCP-IV Gelatine 20 ± 0.5 85 ± 2.5 $\%$ 72 ± 5%

Table 4

Main DIC results for the CF/PEEK composites impacted by the gelatine projectiles.

EFA 104448 No. of Pages 19, Model 3G

10 H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

Fig. 8. CF/PEEK composites impacted at a 37 J energy level: (a) the major strain maps and (b) the evolution of the major strain profiles (in intervals of 0.025 ms) during loading and unloading. (Inset picture, on right, shows a horizontal solid line where the profile section is taken.)

 (b)

Fig. 9. CF/PEEK composites impacted at a 37 J energy level: (a) the OOP displacement contours and (b) the evolution of the OOP displacement profiles (in intervals of 0.025 ms) during loading and unloading. (Inset picture, on right, shows a horizontal solid line where the profile section is taken.)

EFA 104448 No. of Pages 19, Model 3G

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx 11

Fig. 10. Photographs of the rear-faces of the CF/PEEK composites after impact: (a) for an energy of 37 J ('Test GCP-I') and (b) for an energy of 72 J ('Test GCP- IV).

325 breakage was observed in this CF/PEEK composite specimen. Thus, it can be concluded that there is a critical impact energy 326 between about 64 J and 72 J at which visible damage in the CF/PEEK composite is initiated.

327 5.3. Effects of the matrix system

 To study the effects of the employed matrix system on the impact response of the composite laminates, CF/epoxy com- posite specimens were also impacted, using a soft-gelatine projectile, at an energy level of 38 J. The details of the testing con- ditions are summarised in Table 6 and the results are shown in Table 7 and Fig. 11. As may be seen, the main effect of the matrix selected for the carbon-fibre composite is that the CF/PEEK composite ('Test GCP-I') impacted at an energy level of 37 J did not show any visible damage, whilst the CF/epoxy composite ('Test GCE-I') showed significant damage with 'type (b) cracking' being recorded.

Table 6

Gas-gun test conditions to study the effect of the matrix system.

Table 7

Results from the CF/PEEK and CF/Epoxy composites impacted by the gelatine projectiles.

Fig. 11. The rear-faces of the specimens after impact: (a) the CF/PEEK composite impacted at a 37 J energy level and (b) the CF/epoxy composite impacted at a 38 J energy level.

EFA 104448 No. of Pages 19, Model 3G

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

6. The Finite element (FE) model

6.1. Model definition

 As a discussed earlier, in order to model the soft-body impact on the composite test specimens a Finite-Element (FE) model was developed based upon a commercial software code, 'Abaqus/Explicit 2017'. Within the FE model, the gelatine pro- jectile was modelled using the Smoothed Particle Hydrodynamics (SPH) modelling technique [\[18\].](#page-18-0) As discussed earlier, the SPH method is a meshless Lagrangian technique where the solid FE mesh for the gelatine impactor is replaced by a set of discrete interacting particles. The gelatine projectile was first modelled using 8-node linear-brick (C3D8R) elements. How- ever, upon initial contact of the projectile with the composite target specimen, these elements were converted to continuum particle (PC3D) elements, see Fig. 12. The characteristic length for the PC3D elements was 0.5 mm, which was equivalent to half of the element size that was used for modelling the gelatine projectile with the CSD8R elements. The total mass of the projectile was equally distributed between all the 8-node linear-brick (C3D8R) elements or all the continuum particle (PC3D) elements. Turning to the modelling of the composite specimen, the damage theories discussed earlier [\[13–15\]](#page-17-0) were origi- nally developed for unidirectional fibre-reinforced composite plies. Hence, the $[0-90^\circ]$ woven carbon-fibre ply used for the CF/PEEK and CF/epoxy composites was represented as two unidirectional-fibre sub-plies, joined at right angles to the

Fig. 12. The FE model with PC3D elements.

Fig. 13. The creation of a single equivalent $[0^{\circ}$ -90° woven-fibre reinforced composite ply.

EFA 104448 No. of Pages 19, Model 3G

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx 13

 fibre direction. Thus, in the FE modelling, two unidirectional-fibre sub-plies were first created, with the thickness of each of the unidirectional-fibre sub-plies (i.e. 0.125 mm) being equal to half that of the thickness of the equivalent [0–90] woven- fibre composite ply (i.e. 0.25 mm). These two unidirectional-fibre sub-plies were placed at right angles and then joined using 351 'tie constraints', to form a single equivalent $[0-90^\circ]$ woven-fibre composite ply, which has the same in-plane properties as 352 the actual woven-fibre composite ply that was used in the composite specimens, see [Fig. 13](#page-11-0). The elements employed in the FE model for the composite target test specimens were 8-node quadrilateral in-plane general-purpose continuum shell 354 (SC8R) elements, with an element size of 1 mm \times 1 mm. The interfaces between the composite plies were modelled using
355 the cohesive surface law, which is again a built-in sub-routine within the 'Abagus/Explicit 2 the cohesive surface law, which is again a built-in sub-routine within the 'Abaqus/Explicit 2017' code $[22-24]$. The boundary conditions employed in the model were the same as those used in the gas-gun experiments. A general contact algorithm was used to govern the global contact in the numerical modelling and a friction coefficient of 0.2 was adopted for the global con-tact [\[25–27\].](#page-18-0)

359 6.2. Input parameters

 In order to use the SPH method for capturing the response of the soft-gelatine projectile, an equation of state (EOS) with 361 suitable input parameters, as shown in Eqs. (5) and (6) , is required for the modelling of the gelatine projectiles, see [Sec-](#page-1-0) [tion 2.1](#page-1-0). The input parameters required for the numerical modelling of the gelatine projectiles are shown in Table 8. For the composite specimen, it was defined using continuum shell elements and only the in-plane material properties are then required for the numerical modelling. However, the values of the cohesive stiffness, maximum cohesive strength and the various fracture energies do need to be inputted into the sub-routine which simulates the damage evolution in the compos- ite via a linear-softening material model embedded in a bilinear cohesive law. The relevant material properties of the CF/ PEEK and CF/epoxy composites required for the FE modelling studies may be found from the literature [\[28–35\]](#page-18-0) and are given in Table 9.

369 6.3. Implementation of the model

 [Fig. 14](#page-13-0)a shows the flow chart of the main FE model and [Fig. 14b](#page-13-0) shows the sub-routine for the composite damage model. In the computation process a computation step was performed for every appropriate single element in the FE model. In the composite damage model, if any of the damage criteria are initiated, the model will then run the flow-path 'Yes', otherwise the flow-path 'No' will be taken. Note that the time associated with the impact event enters the FE model by the 'Model state' being equivalent to a 'step time'. The numerical model is stopped when the defined total time for the impact event has 375 expired.

Table 8

Input properties for the FE modelling of the soft-gelatine projectile [\[37–39\]](#page-18-0).

Table 9

Input properties for the FE modelling studies of the composite [\[28–35\].](#page-18-0)

Note:

 G_{lc} and G_{llc} are the Mode I and Mode II interlaminar fracture energies between two $[0-90^\circ]$ woven-fibre composite plies.

 $G_{lc}|_{\hbar}$ and $G_{lc}|_{\hbar}$ are the tensile and compressive ply fracture energies of the unidirectional-fibre sub-plies in the longitudinal fibre-direction.

 $G_{lc}|_{mt}$ and $G_{lc}|_{mc}$ are the tensile and compressive ply fracture energies of the unidirectional-fibre sub-plies in the transverse to fibre direction.
* These properties are for interlaminar failure between two of the

14 H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

Fig. 14. The implementation of the FE model showing schematically the flowcharts for one computation step for a single element: (a) the flowchart of the main model and (b) the flowchart of the sub-routine model for assessing the initiation and evolution of composite damage. Note that in (b) for the subroutine model the failure criteria for the initiation and evolution of damage are given by Eqs. [\(8\)–\(15\)](#page-2-0) for intralaminar damage and by Eq. [\(17\)](#page-3-0) for interlaminar damage.

376 7. Model validation and application

377 7.1. Validation of the model

378 7.1.1. The deformation of the gelatine projectile

 The deformation histories of the gelatine projectile obtained from the experimental studies and predicted using the FE model for an impact test conducted at an energy level of 37 J on the CF/PEEK composite (i.e. 'Test GCP-I') are compared in [Fig. 15](#page-14-0). The experimental results show that, after the initial contact with the composite specimen, the front of the gelatine projectile started to deform and flow to the periphery of the composite specimen. Correspondingly, the modelling results 383 show a similar phenomenon, as shown in [Fig. 15](#page-14-0)b. At a later stage of the impact event, see Fig. 15e, most of the gelatine pro- jectile has deformed, flowed and spread over the surface of the composite specimen, and again the modelling studies accu- rately capture this behaviour of the gelatine projectile. Thus, the comparison between the experimental and numerical modelling results reveal that the SPH model for the relatively soft-gelatine projectile can indeed reproduce the experimental behaviour of the soft-gelatine projectile used in the gas-gun impact experiments.

Fig. 15. Deformation of the gelatine projectile obtained from the experimental studies and as predicted from the numerical FE model for the CF/PEEK composites at an impact energy of 37 J.

Fig. 16. Comparison between the predicted and experimental results for the CF/PEEK composite at an impact energy of 37 J: (a) the maximum major strain and the out-of-plane (OOP) displacement and (b) the central OOP displacement versus time trace.

388 7.1.2. The CF/PEEK composites

 Based on the DIC results obtained from the experiment conducted at an impact energy of 37 J using the gelatine projectile (i.e. 'Test GCP-I'), the major strain and out-of-plane (OOP) displacement histories of the centre point for the rear-face of the composite test specimen can be extracted. The values of the maximum major strain and central OOP displacement predicted from the FE modelling studies are compared with the corresponding experimental results in Fig. 16a, and good agreement may be seen. To further confirm the accuracy of the numerical FE model, the predicted central OOP displacement versus time 394 trace was also compared with the corresponding experimental results, see Fig. 16b. It can be seen from these results that, although the modelling studies gave somewhat lower maximum values than the experimentally measured values, the gen- eral trend and overall response of the composites were predicted extremely well using the numerical FE model. The slightly lower prediction values may be due to curvature effects in the woven material which the model could not fully capture.

 The next step is to assess the capability of the numerical FE model that has been developed to predict the impact damage created in the composite by the impact event, and two impact energies levels of 37 J and 72 J were so modelled. The exper- imental and predicted extents of damage at these two energy levels, which resulted in the CF/PEEK composites, are shown in [Fig. 17a](#page-15-0) and b, respectively. (The 'DAMAGESHR' shown in the legend corresponds to the shear damage.) It was found that, at an energy level of 37 J, the prediction from the FE numerical modelling studies was that no visible impact damage would have been suffered by the composite specimen. This finding is in excellent agreement with the experimental results. When

 (a)

 (b)

Fig. 17. The experimentally measured and predicted degrees of damage resulting in the rear-face of the CF/PEEK composites at impact energies of (a) 37 | and (b) 72 J.

 an impact energy level of 72 J was modelled, failure was predicted to be present only in the central area of the CF/PEEK com-405 posite, as shown in Fig. 17b. The experimental results revealed that some damage had indeed occurred in this region of the composite. In addition, the extent of the damage, as determined from the post-impact experimental observations on this composite specimen, is accurately predicted by the numerical studies.

7.2. Application of the model

7.2.1. Predicting the deformation of the CF/PEEK and CF/epoxy composites

 To model the effects of the matrix system on the impact response of the composites, the central OOP displacement was predicted from the FE model for the CF/PEEK specimens impacted at a 37 J energy level and the CF/epoxy specimens 412 impacted at a 38 J energy level, as shown in Fig. 18a. The central OOP displacement versus time traces predicted for the CF/PEEK composite and for the CF/epoxy composite exhibited a very similar behaviour up to a peak value of the displace- ment followed by a gradual decrease. Fig. 18b shows a comparison of the maximum central OOP displacements predicted in the FE model for the CF/PEEK ('Test GCP-I' at 37 J) and the CF/epoxy ('Test GCE-I' at 38 J) composites. When impacted, the CF/epoxy composite ('Test GCE-I') is predicted from the FE modelling to undergo a maximum central OOP displacement of 3.9 mm, which is marginally higher than that of 3.7 mm for the CF/PEEK composite ('Test GCP-I'). These predicted values of the central OOP displacement for the two types of composite are also compared with the experimental results in [Table 10,](#page-16-0) where very good agreement may be seen between the experimental measurements and the FE modelling simulations. The out of plane displacement response for CF/PEEK and CF/epoxy are very similar as both composites have the same carbon fibres with similar volume fraction.

7.2.2. Predicting the post-impact damage of the composites

 A comparison of the post-impact damage in the composites obtained from the experiments and the FE numerical mod-elling results for the CF/PEEK and the CF/epoxy composites is shown in [Fig. 19a](#page-16-0) and 19b, respectively. It can be seen that the

Fig. 18. Predicted (a) central out-of-plane (OOP) displacement versus time trace and (b) the experimentally measured and predicted maximum OOP displacements for the CF/PEEK impacted at 37 J and the CF/epoxy impacted at 38 J.

18 February 2020

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx 17

Table 10

Comparison of the experimentally measured and the numerically predicted maximum central out-of-plane (OOP) displacement.

Fig. 19. Comparison of the damage obtained from the experiments and the FE modelling: (a) the CF/PEEK composite impacted at 37 J and (b) CF/epoxy composite impacted at 38 J.

 predicted results for the CF/PEEK did not show any damage, which agrees fully with the experimental observations. On the other hand, the modelling results for the CF/epoxy predicted that some centrally-located damage would occur, which was indeed observed in the experimental studies. The evolution of damage was observed by plotting the derived damage vari-428 able, d_s , which is dependent on fibre and matrix failure, d_f and d_m respectively, as defined by Eq. [\(15\).](#page-3-0) The damage observed in CF/epoxy on the rear face was mostly localised matrix and fibre failure at the centre of the panel. The amount of energy expended in damage of the composite sample for CF/PEEK and CF/epoxy was very small relative to the incident impact energy. Most of the incident impact energy is transformed into elastic energy in the specimen which is then dissipated in friction at the support fixtures and in intrinsic damping, as the specimen vibrates after impact. Of course, some of the inci-dent impact energy is dissipated in plastic flow of the projectile.

434 7.2.3. Predicting the contact pressure between the projectile and the composite

 The numerical FE model was also employed to predict the average contact pressure between the soft-gelatine projectile and the composite specimen by using Eq. [\(7\),](#page-2-0) see [Section 2.1](#page-1-0). This parameter could not be readily experimentally measured in the gas-gun experiments. The contact pressure versus time histories were obtained from the FE models for (a) the CF/PEEK composite impacted at an impact energy of 37 J and (b) the CF/epoxy impacted an impact energy of 38 J, and the results are 439 shown in Fig. 20a. It can be seen that the CF/PEEK and the CF/epoxy composites suffered a very similar average contact pres- sure history, with an initial short duration compressive phase giving rise to a relatively high initial contact pressure. The pre- dicted maximum average contact pressures for the CF/PEEK and the CF/epoxy impact tests, when the relatively soft-gelatine projectile was used, are 10.7 MPa and 9.8 MPa, respectively, as shown in Fig. 20b.

Fig. 20. Numerical predictions from the FE model for: (a) the average contact pressure versus time history and (b) the maximum average contact pressure. (For the CF/PEEK composite impacted at an energy of 37 J and (b) the CF/epoxy impacted an energy of 38 J.

EFA 104448 No. of Pages 19, Model 3G

H. Liu et al. / Engineering Failure Analysis xxx (xxxx) xxx

8. Conclusions

 This paper has focussed on experimental and numerical studies of the response of polymer-matrix fibre-reinforced com- posites under impact loading by a soft projectile. A simple but reliable technique was proposed for the preparation of the relatively soft-gelatine projectiles and a plastic sabot was employed to maintain the shape of the gelatine projectile upon being launched from the gas-gun. A high-speed camera was used to record the deformation of the projectile during the impact event. The recorded frames showed that the gelatine projectile behaved as a viscoelastic-plastic fluid. The gas-gun tests were firstly performed using woven carbon-fibre reinforced poly(ether-ether ketone) (CF/PEEK) composite specimens, using the gelatine projectiles, at four different impact energy levels. Secondly, to investigate the effects of the matrix system on the impact response of the composites, woven carbon-fibre reinforced epoxy (CF/epoxy) were impacted using the gelatine projectiles. The experimental results demonstrated that the CF/epoxy composite exhibited a lower impact resistance and suffered more impact damage, compared with the CF/PEEK composite, when struck by the gelatine projectiles using a similar impact energy.

 A finite-element (FE) numerical model was developed, which was based on the 'Abaqus/Explicit 2017' commercially- available software code, for predicting the behaviour of the projectile and the composite test specimen during the impact event. The FE numerical model has enabled (a) the deformation, (b) the initiation of damage, and (c) the evolution of such damage in the composite target specimens to be predicted, as well as the deformation and flow behaviour (and the contact pressure) of the projectile. The results from the numerical studies have been found to be in very good agreement with the experimental results.

 In terms of design, woven architectures are often employed on the outside of composite laminates to generate a hybrid architecture. Woven composites do not have the stiffness of an equivalent laminate carbon-fibre material but they have the advantage that delamination and interfacial cracking does not occur so readily as has been shown by the above modelling and experiments. CF/PEEK is a very attractive woven material as the threshold for damage is higher than an equivalent CF/ epoxy and this has also been confirmed by the modelling and experiments.

- Uncited references
- [\[19,21\].](#page-18-0)

Declaration of Competing Interest

 The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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