

A THEORETICAL MODEL FOR WIDE-BAND IR-ABSORPTION MOLECULAR SPECTRA AT ANY PRESSURE: FICTION OR REALITY?

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Plan

- 1 Outline of the needs
- 2 Non-Markovian **E**nergy-**C**orrected **S**udden approach
- 3 Applications to high-density IR spectra
- 4 Applications to CO₂ IR spectra at low densities
- 5 Conclusions & perspectives

1

Outline of the needs

Mars



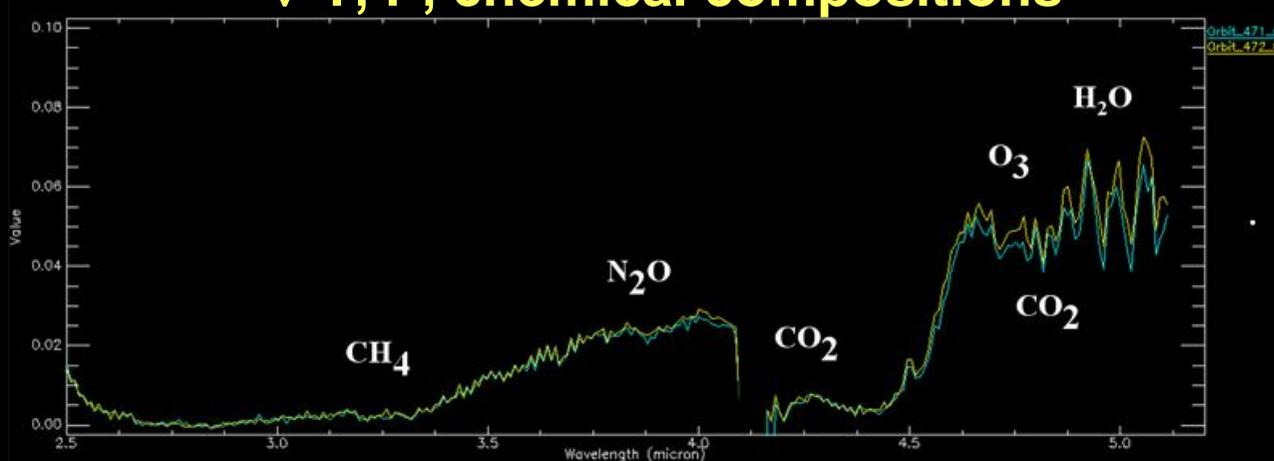
Earth



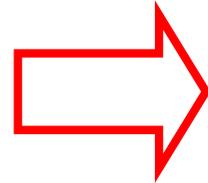
Venus



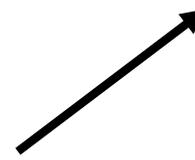
∇ T, P, chemical compositions



Absorption coefficient as a function of frequency
for each spectroscopically active molecule



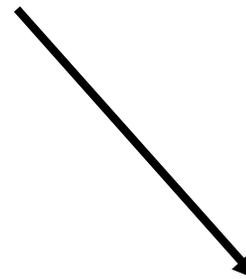
Atmospheric radiative transfer codes



Retrieval of geophysical parameters (temperature, humidity,...)



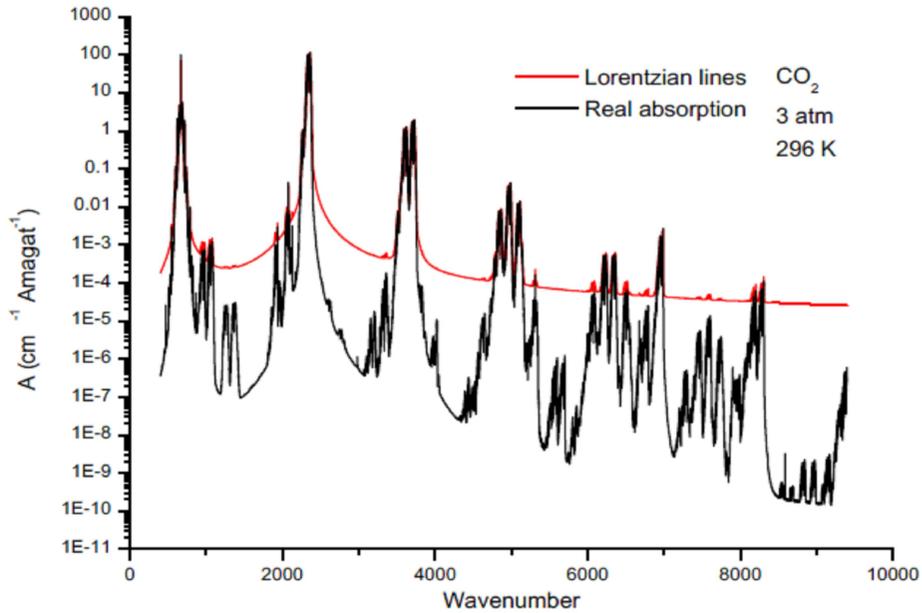
Weather/climate models



Optimization of solar photovoltaic systems

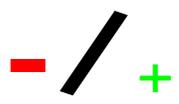
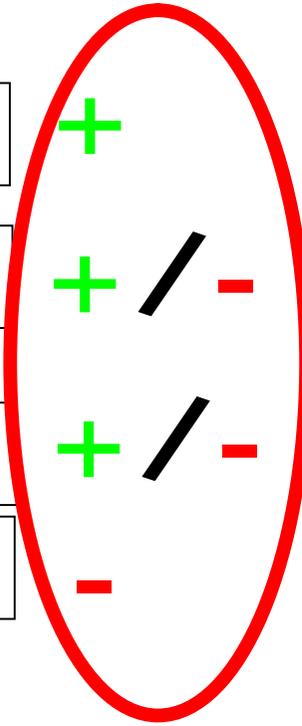
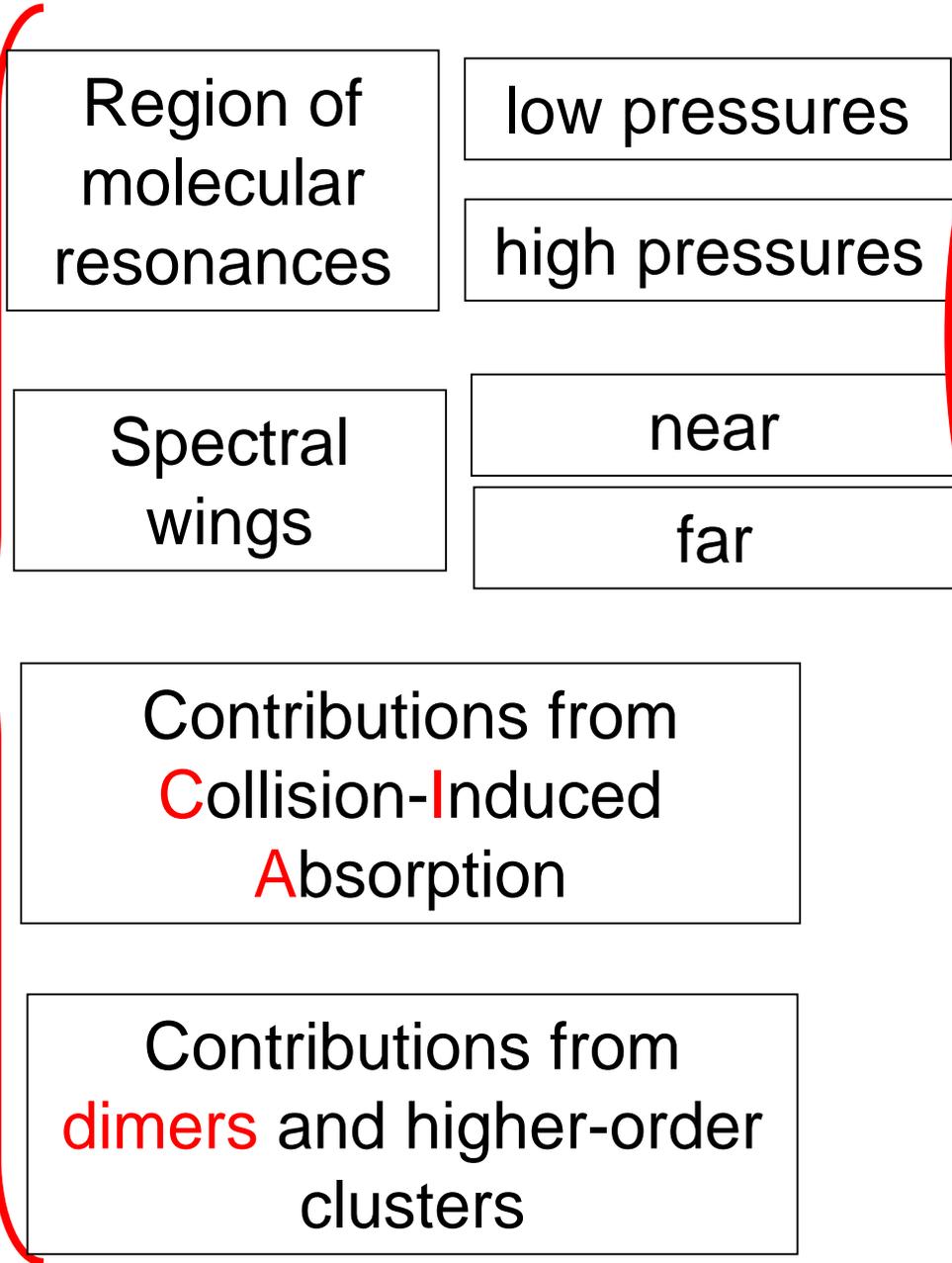
...

Outline of the needs



Courtesy : N.N. Filippov

Absorption coefficients as functions of frequency



Outline of the needs

STANDARD APPROACH for allowed absorption

Niro et al., JQSRT 88, 483 (2004)

$$\alpha(\sigma) = \frac{8\pi^3}{3hc} \sigma n_1 (1 - e^{-\frac{hc\sigma}{kT}}) \frac{1}{\pi} \operatorname{Re} \sum_{k,k'} \rho_k d_k d_{k'} [i(\sigma - \sigma_k)] + n_2 [W]_{kk'}^{-1}$$

↑
absorption coefficient
at wavenumber σ

↑
Active-gas
density

↑
Rotational
populaton

↑
Dipole
matrix
element

↑
Isolated-
line
positions

↑
Bath-gas
density

↑
[W]_{kk'}⁻¹
Rotational
relaxation
matrix

Re $W_{kk'}$

Modelled by the Energy-Corrected Sudden approach
for «downward» transitions +
detailed-balance relation $\operatorname{Re}W_{kk'}\rho_k = \operatorname{Re}W_{k'k}\rho_{k'}$ for «upward» ones

Rotational
relaxation
matrix

Im $W_{kk'}$

One-parameter empirical modelling using the detailed balance

Re W_{kk}

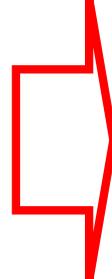
Calculated by sum rules $W_{kk} = -\sum_{k'} \frac{d_{k'}}{d_k} W_{k'k}$

In the 1st-
order impact
approx
6

Im W_{kk}

STANDARD APPROACH: PROBLEMS

1

ECS parameters fitted to experimental LW
 Sum rules for calculation of diag. elements } 

⇒ Recalculated LW ≠ experimental LW

« Renormalization procedure »

- 1) Lines sorted in decreasing intensity order
- 2) Expt LW imposed on the diagonal
- 3) Off-diagonal elements scaled to satisfy the detailed balance

2 Empirical modeling of Im W

3 Far spectral wings:
 break down of the impact approximation 

Empirical corrections to the Lorentzian shape:
 « χ -factors »

4 Far spectral wings: violation of the detailed balance

$$\Phi(-\omega) = \Phi(\omega) \exp(-\beta \hbar \omega)$$

Filippov & Tonkov, JCP 108, 3608 (1998)

5 One-sided sum rules → asymptotic behavior σ^{-3} in the far wing
 → negative intensities in low-frequency wing

General sum rules hold ONLY in the non-Markovian case

2 Non-Markovian Energy-Corrected Sudden approach

Symmetrized spectral density:

$$S^{(r)}(\sigma) = \frac{1}{\pi} \text{Re} \sum_{k, k'} A_k^{(r)} \left[i(\sigma - \sigma_k) + n_2 \Gamma^{(r)}(\sigma) \right]_{k, k'}^{-1} A_{k'}^{(r)}$$

r - rank of the coupling tensor

σ_k - proper frequencies of the free active molecule

n_2 - gas density

$A_k^{(r)}$ - intensities of separate lines $A_k^{(r)} = (-1)^{J_i} \sqrt{(2J_i + 1)(2J_f + 1)} \begin{pmatrix} J_i & r & J_f \\ 0 & 0 & 0 \end{pmatrix} \sqrt{\frac{\rho_i + \rho_f}{2}}$

$$\langle J_f \| C^{(r)} \| J_i \rangle$$

$$n_{if}$$

General form of the off-diagonal relaxation matrix elements:

$$\Gamma_{if, i'f'}^{(r)}(\sigma) = - \left[1 + \exp(-hc\sigma / kT) \right] / 2n_{if}n_{i'f'} \times \sum_L (2L + 1) F_{if, i'f'}^{Lr} \left[\rho_i \Phi_L(\sigma - \sigma_{f'i}) + \rho_{i'} \Phi_L(\sigma - \sigma_{f'i'}) \right]$$

2 Non-Markovian Energy-Corrected Sudden approach

Properties of the non-Markovian relaxation matrix

Symmetry (detailed balance):

$$\Gamma_{if,i'f'}^{(r)}(\sigma) = \Gamma_{i'f',if}^{(r)}(\sigma)$$

Time-reversal symmetry:

$$\Gamma_{if,i'f'}^{(r)}(\sigma) = \Gamma_{fi,f'i'}^{(r)*}(-\sigma)$$

Double-sided sum rules:

$$\sum_{i'f' \neq if} \Gamma_{if,i'f'}^{(r)}(\sigma) A_{i'f'}^{(r)} = \sum_{i'f' \neq if} A_{i'f'}^{(r)} \Gamma_{i'f',if}^{(r)}(\sigma) = -\Gamma_{if,if}^{(r)}(\sigma) A_{if}^{(r)}$$

Positive definition:

$$\sum_{if,i'f'} B_{if}^{(r)} \Gamma_{if,i'f'}^{(r)}(\sigma) B_{i'f'}^{(r)} \geq 0, \forall B^{(r)}$$

2 Non-Markovian Energy-Corrected Sudden approach

ECS modeling of the correlation function

Buldyreva & Bonamy, PRA 60, 370 (1999)

$$\text{Re } \Phi_L(\sigma) = \frac{2}{1 + \exp(-hc\sigma/kT)} \Phi_L^{class}(\sigma)$$

$$\Phi_L^{class}(\sigma) = Q_L' \Omega(\sigma)$$

$$\Omega(\sigma) = \left(1 + \frac{(2\pi\alpha b_c \sigma)^2}{12 n \bar{v}^2} \right)^{-n}, \quad n = 1 \text{ or } 2$$

Standard ECS parameters

- ECS-EP: $A(T), \alpha, \gamma, b_c$
- ECS-P : $A(T), \alpha, b_c$
- ECS-E : $A(T), \gamma, b_c$

Spectroscopy-independent

$$Q_L = \frac{A(T)}{[L(L+1)]^\alpha} \exp \left[-\gamma \frac{B}{kT} L(L+1) \right]$$

2 Non-Markovian Energy-Corrected Sudden approach

Modifications for IR absorption bands

$$r = 1$$

Buldyreva & Daneshvar, JCP 139, 164107 (2013)

Linear molecule with a bending mode $(\nu_1 \nu_2^l \nu_3)$
can be considered as a symmetric top with $K \equiv l$

IOSA: Green, JCP 70, 816 (1979); JCP 90, 3603 (1989)

(I) Isolated-line intensities

$$A_k^{(r)} = (-1)^{J_i+l_f} \sqrt{(2J_i+1)(2J_f+1)} \begin{pmatrix} J_i & r & J_f \\ l_i & l_f-l_i & -l_f \end{pmatrix} \sqrt{\frac{\rho_i + \rho_f}{2}}$$

(II) Relaxation matrix

$$F_{if,if'}^{Lr} = (-1)^{r+l_i+l_f} \begin{pmatrix} J'_i & L & J_i \\ -l_i & 0 & l_i \end{pmatrix} \begin{pmatrix} J_f & L & J'_f \\ l_f & 0 & -l_f \end{pmatrix} \begin{Bmatrix} J_i & J_f & r \\ J'_f & J'_i & L \end{Bmatrix}$$

2 Non-Markovian Energy-Corrected Sudden approach

(III) Vibration-rotation interactions:

(A) Isolated-line intensities: Correction via Herman-Wallis factors

$$F(m) = (1 + a_1 m + a_2 m^2 + a_3 m^3)^2 \quad P\text{- \& } R\text{-}$$

$$F(m) = (1 + b_2 m^2)^2 \quad Q\text{-}$$

$$m = -J \quad (P); \quad m = J \quad (Q); \quad m = J + 1 \quad (R)$$

$$A_k^{(1)} \rightarrow A_k^{(1)HW} = A_k^{(1)} \sqrt{F(m)}$$

Coriolis interactions between vibrational levels:

Hartmann et al., JCP 110, 7733 (1999)

- If sum rules are restricted to one band, unperturbed dipole elements should be used
- Modifications of rel. matr. for Coriolis effects have no influence on the absorption shape

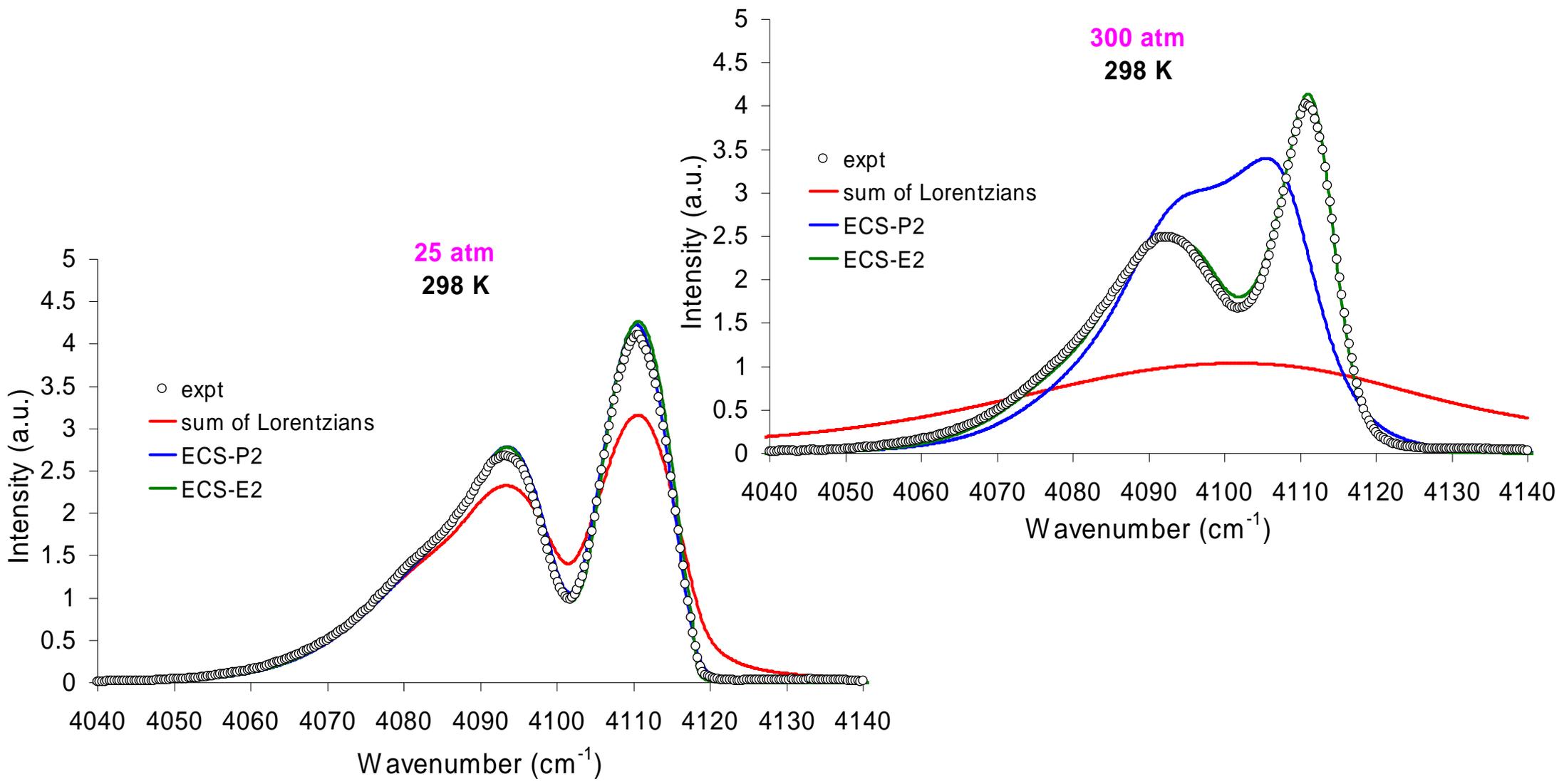
(B) Relaxation matrix modeling:

$$A_k^{(1)}$$

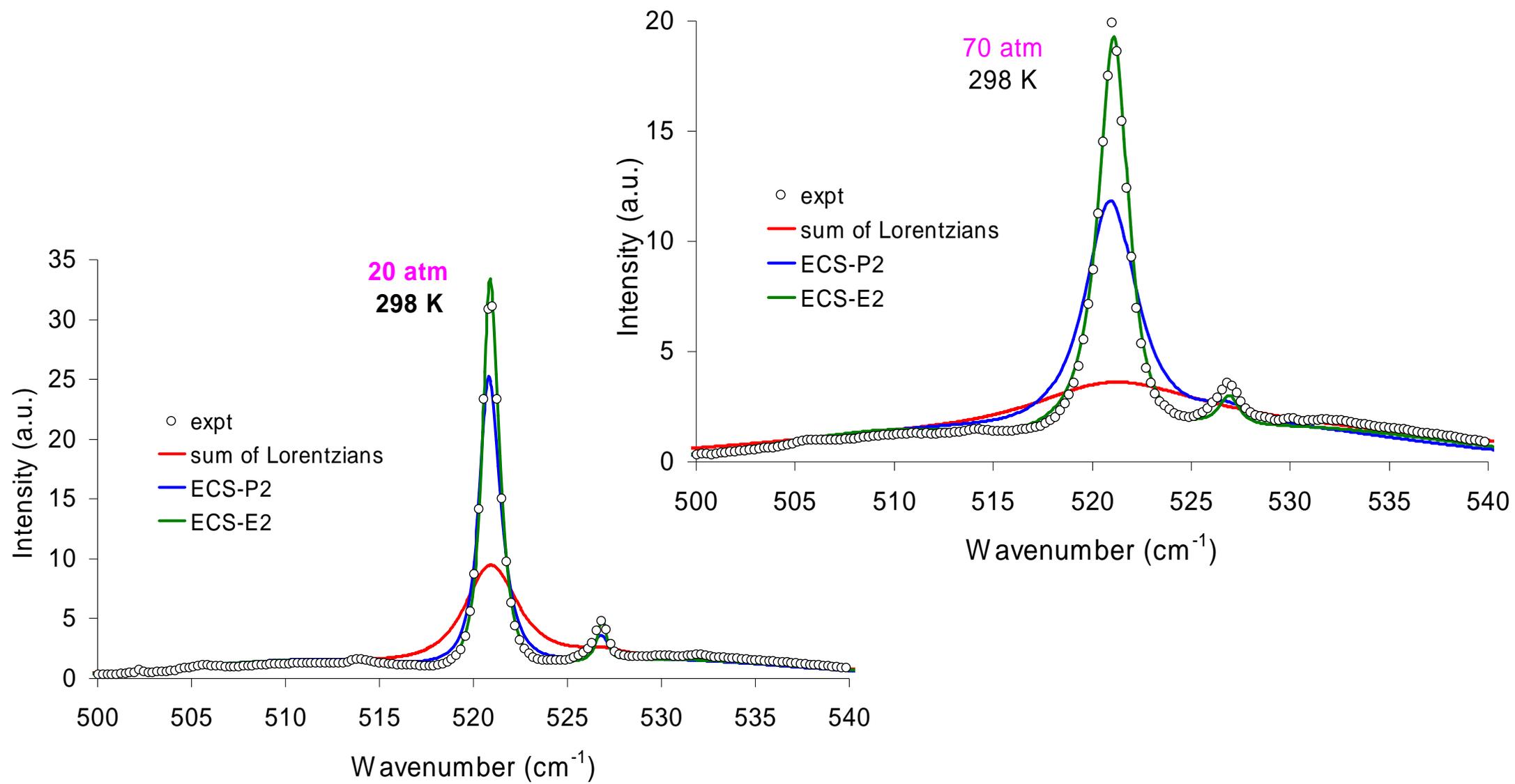
CO₂: Effective correction allowed for diagonal elements

12

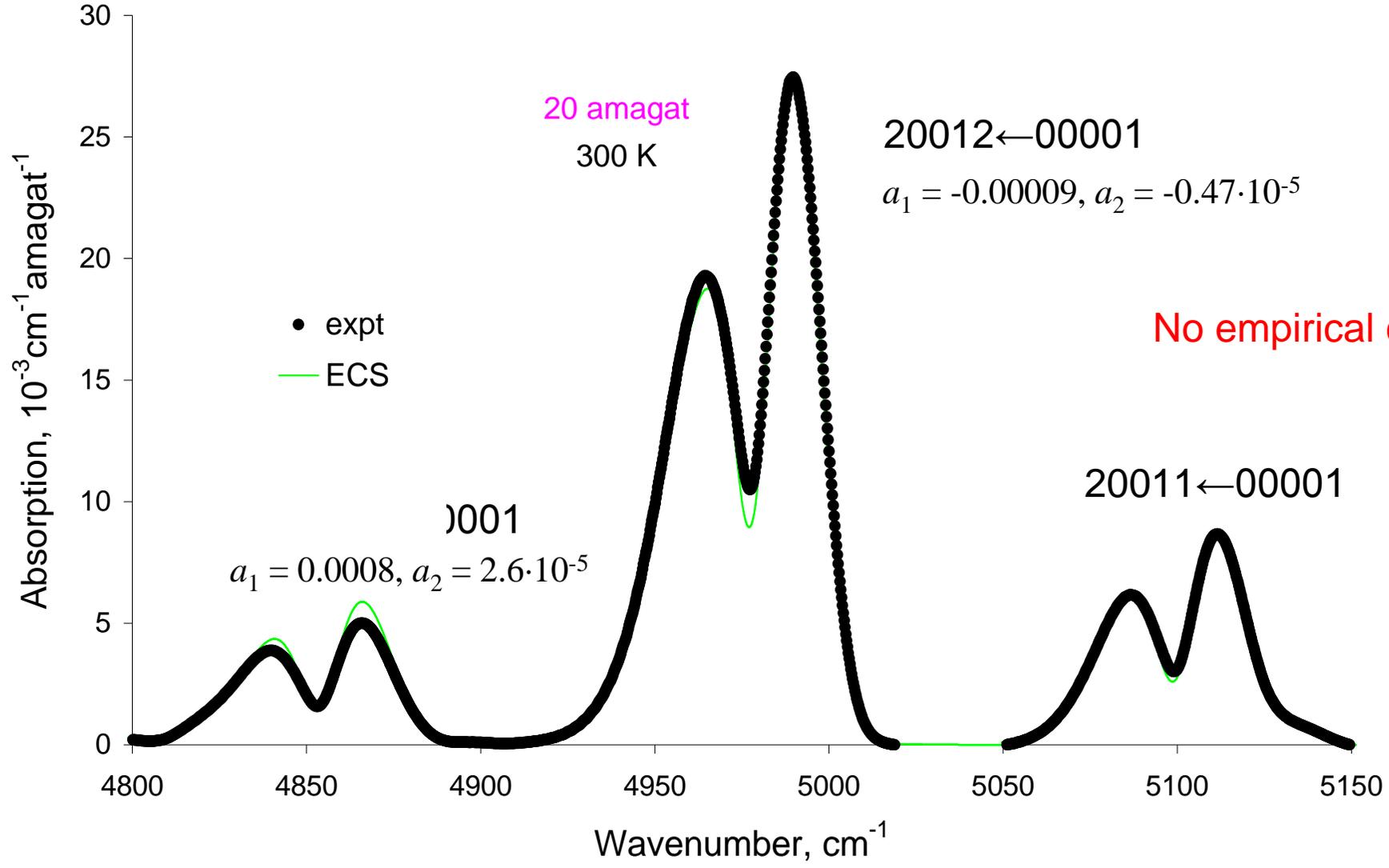
OCS-He $2\nu_3$



OCS-He ν_2

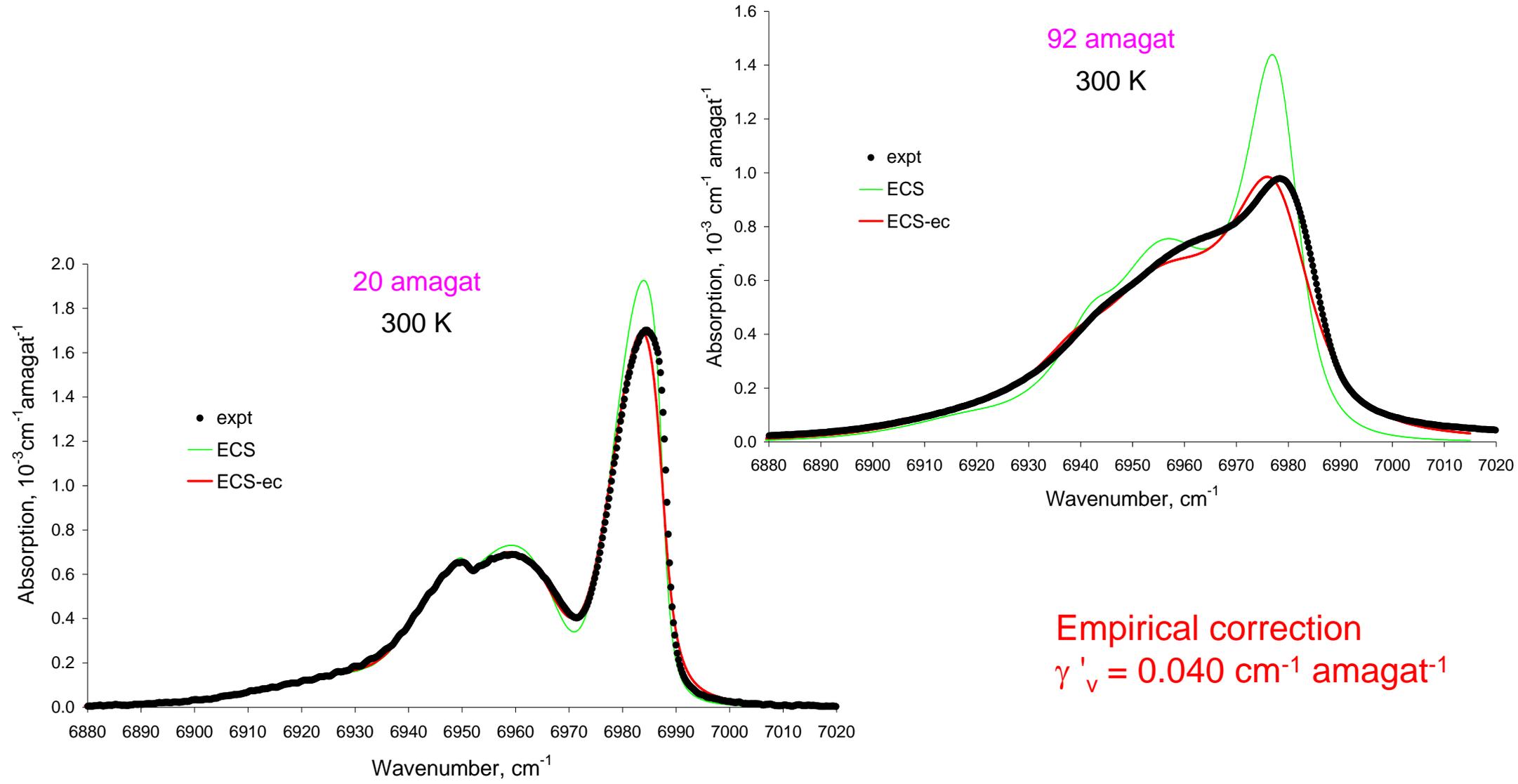


Applications to high-density IR spectra



Filippov et al., PCCP 15, 13826 (2013)

CO₂-CO₂ 3v₃



$a_1 = -0.000215$

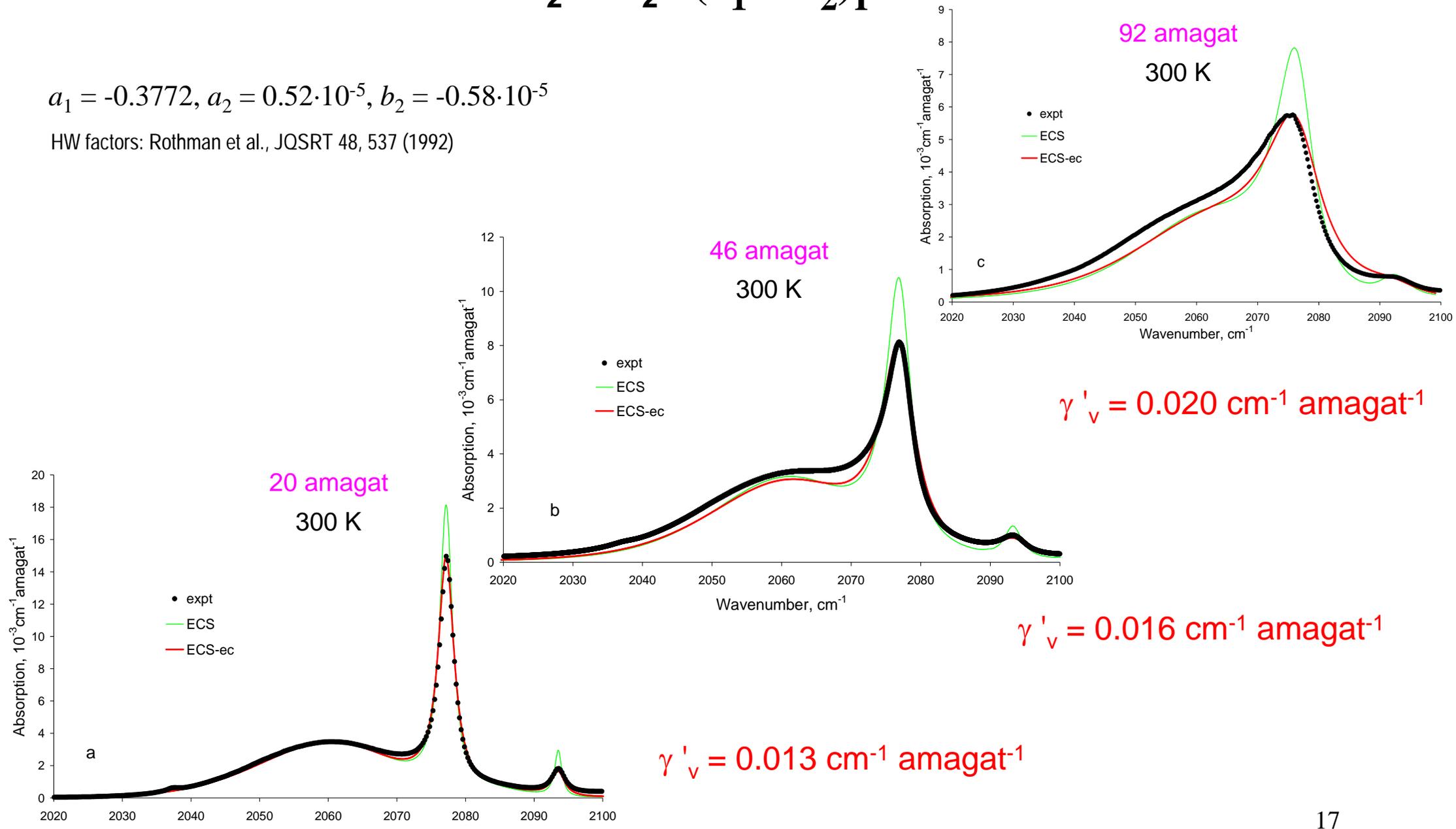
HW factors: Rothman et al., JQSRT 48, 537 (1992)

Filippov et al., PCCP 15, 13826 (2013)

CO₂-CO₂ (ν₁ + ν₂)_I

$a_1 = -0.3772, a_2 = 0.52 \cdot 10^{-5}, b_2 = -0.58 \cdot 10^{-5}$

HW factors: Rothman et al., JQSRT 48, 537 (1992)

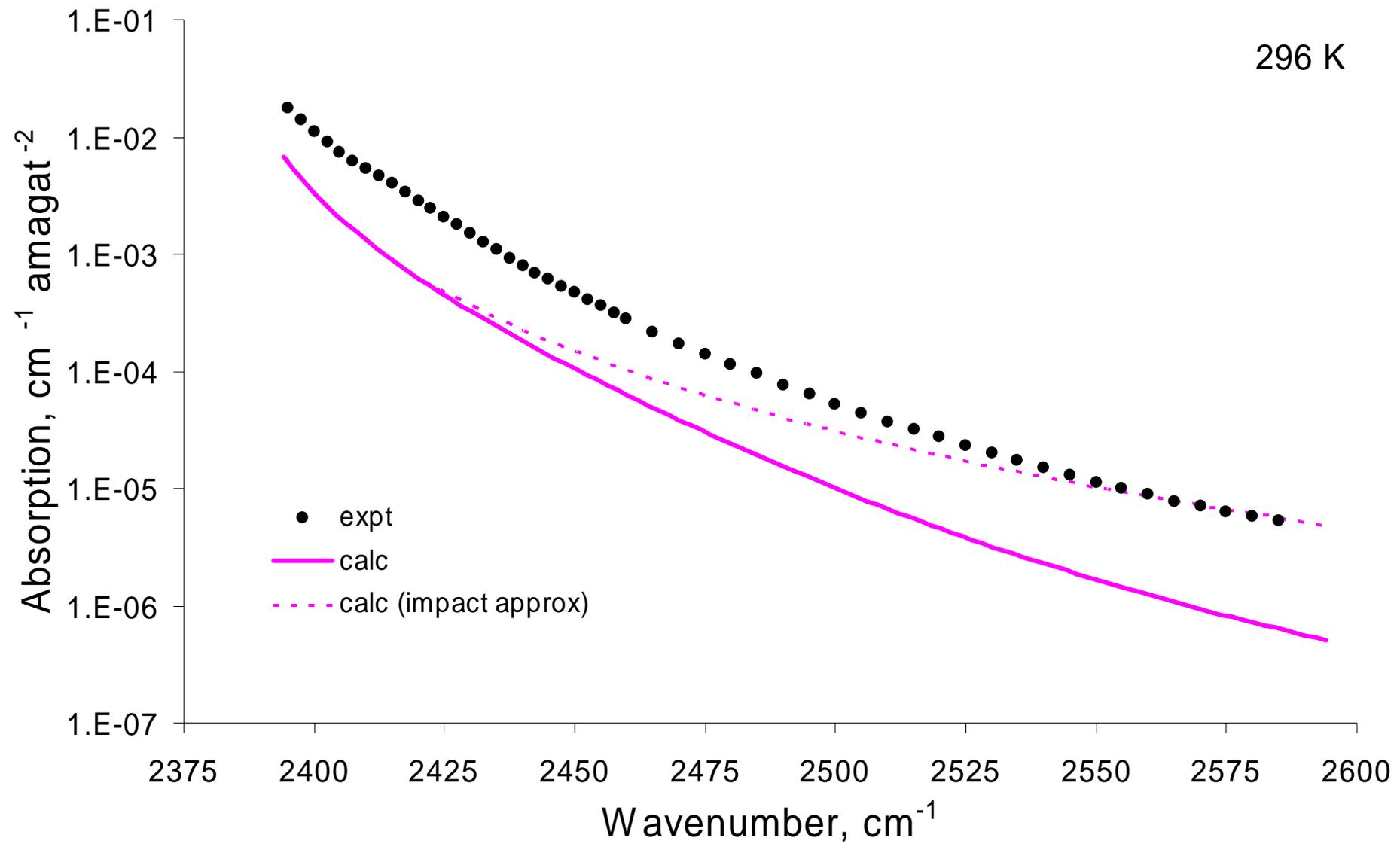


$\gamma'_v = 0.013 \text{ cm}^{-1} \text{ amagat}^{-1}$

$\gamma'_v = 0.016 \text{ cm}^{-1} \text{ amagat}^{-1}$

$\gamma'_v = 0.020 \text{ cm}^{-1} \text{ amagat}^{-1}$

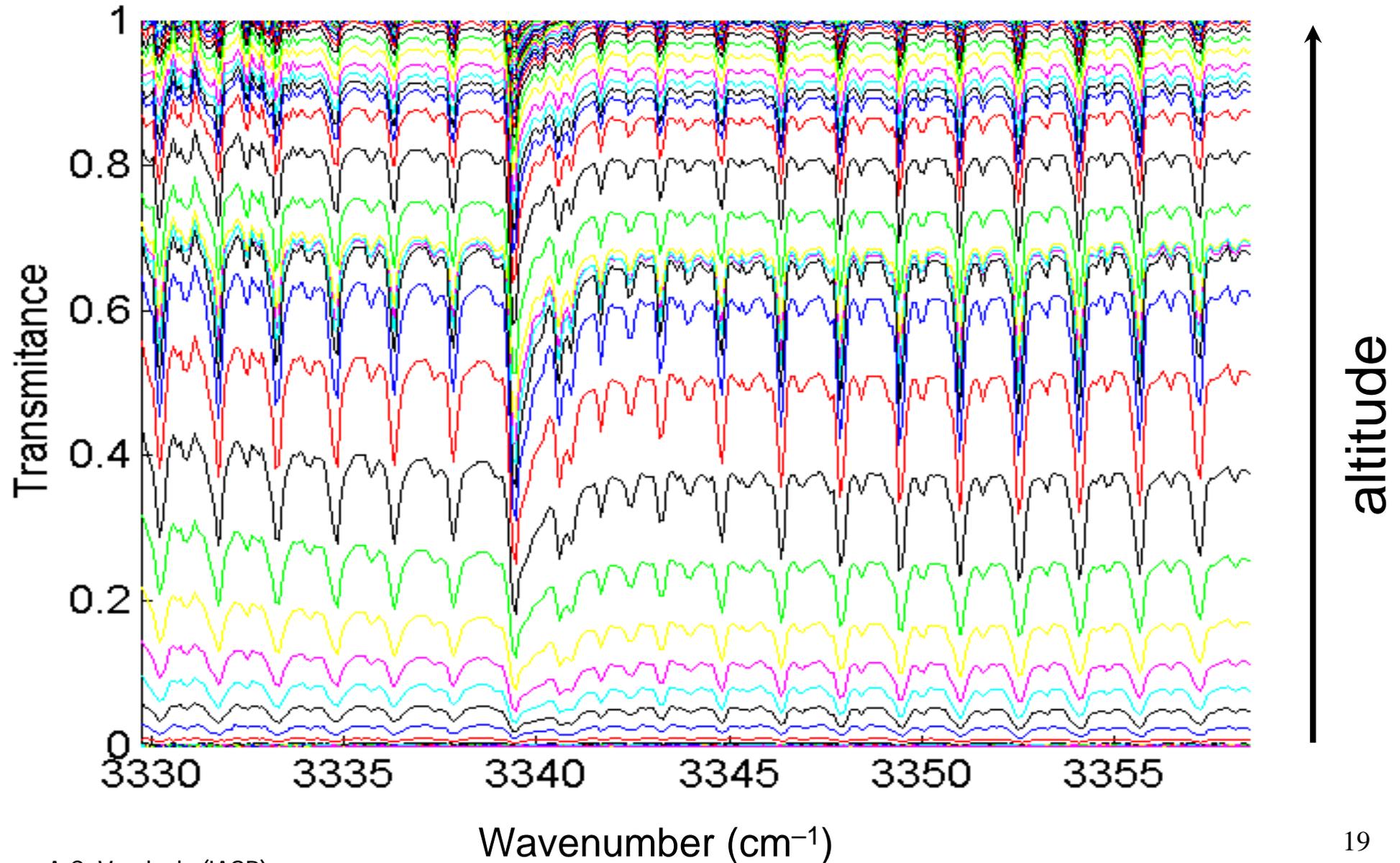
CO₂-CO₂ v₃ wing



Buldyreva & Daneshvar, JCP 139, 164107 (2013)

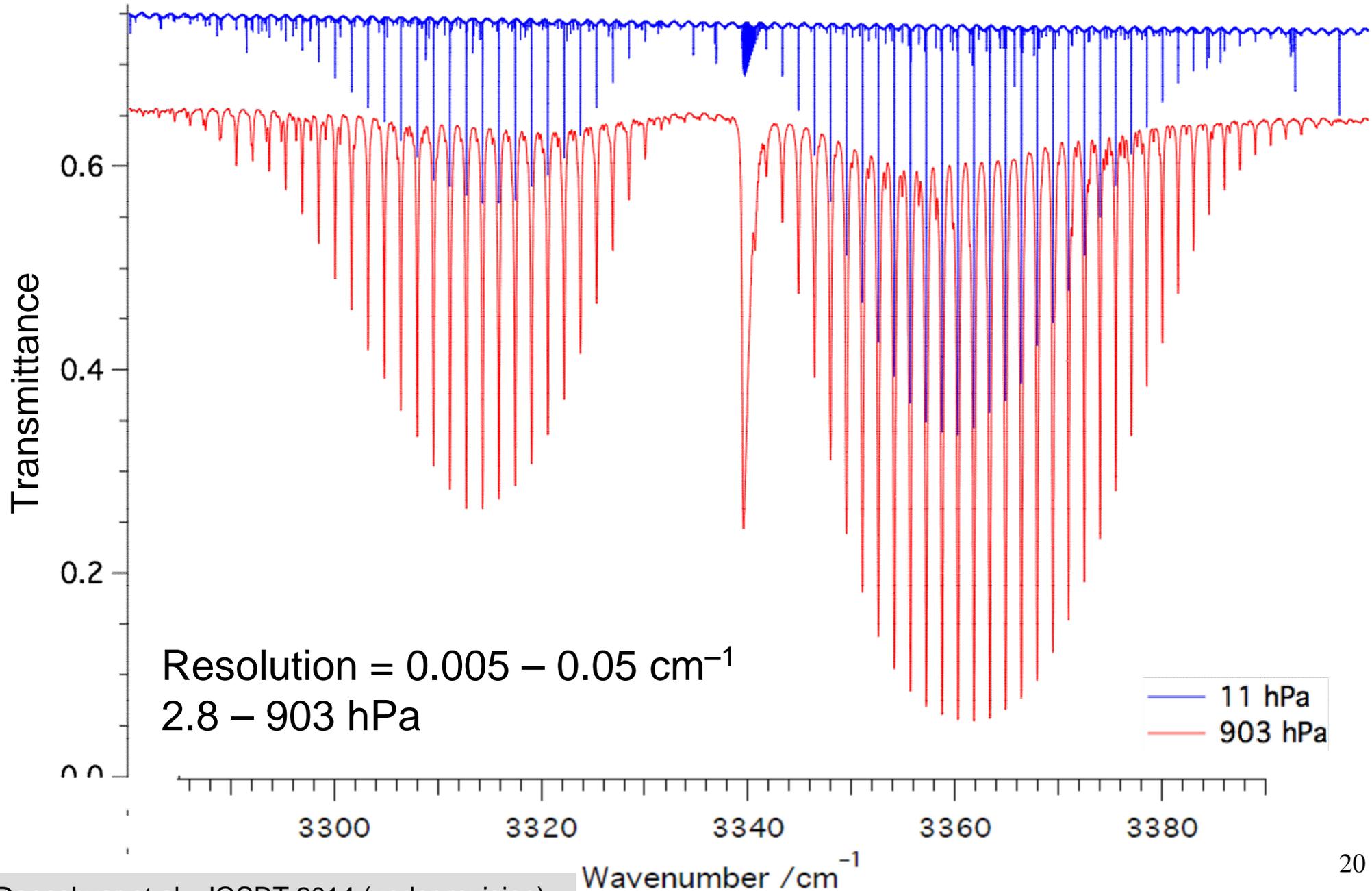
④ Applications to CO₂ IR spectra at low densities

SOIR spectra of the atmosphere of Venus (Venus Express)

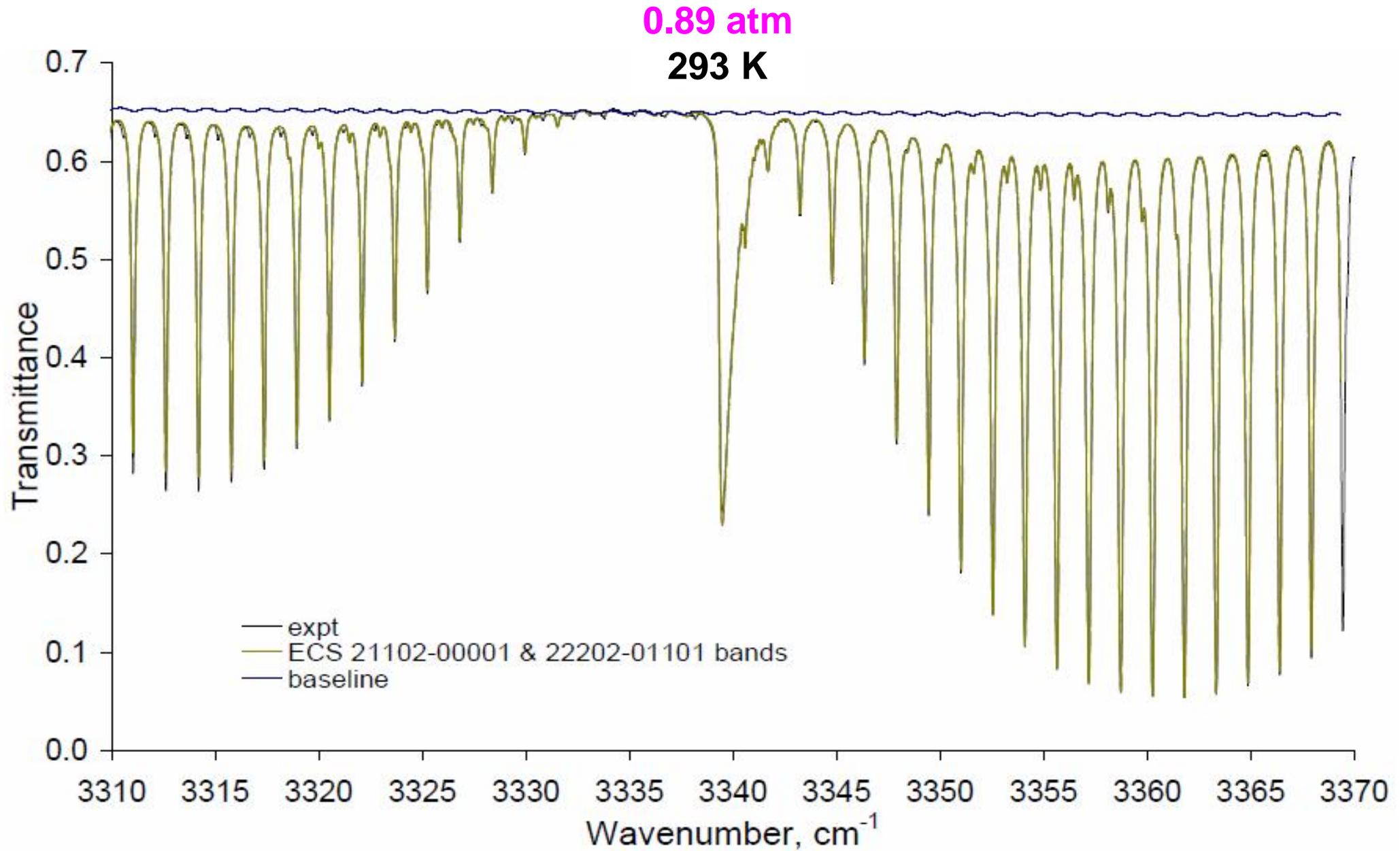


④ Applications to CO₂ IR spectra at low densities

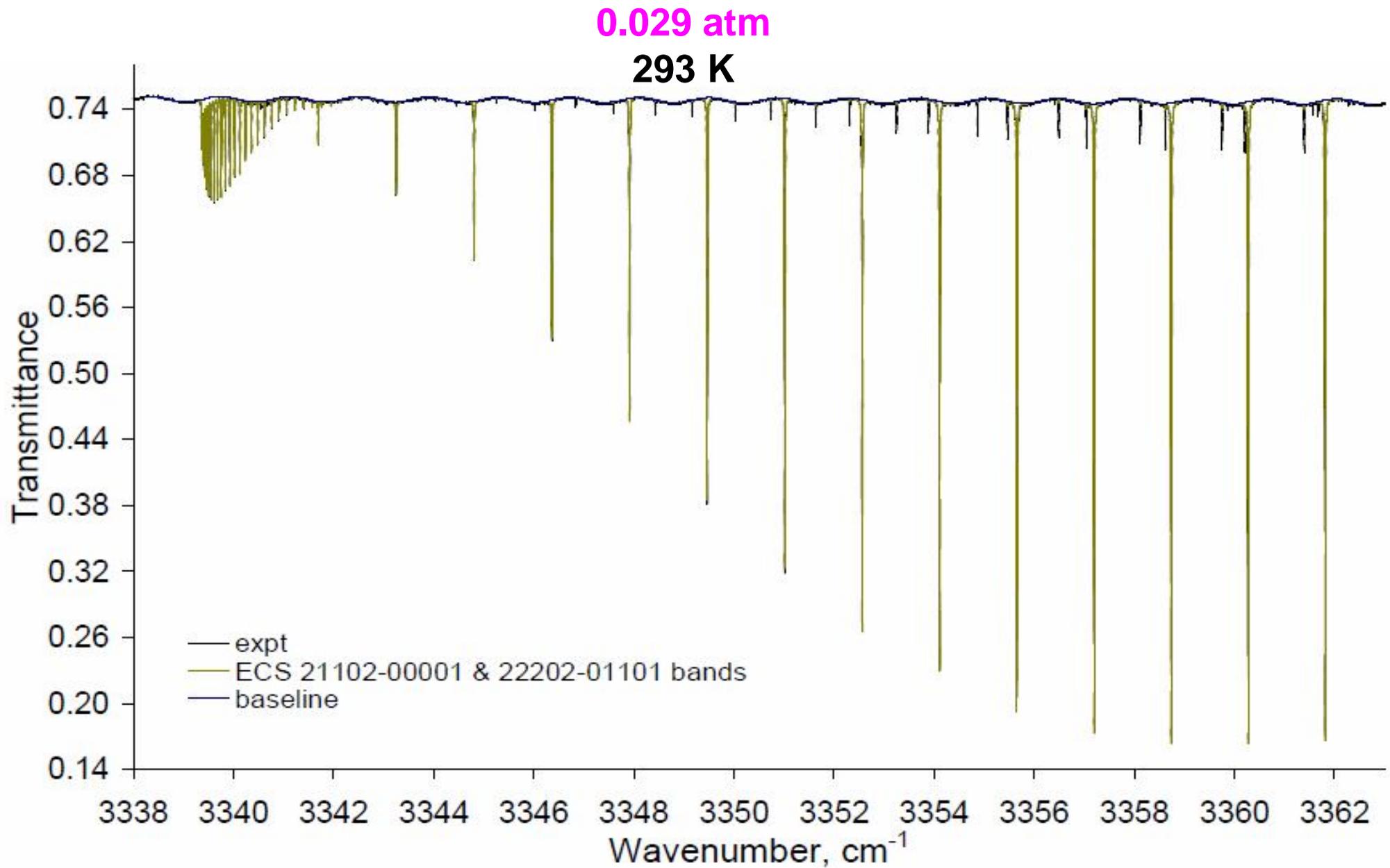
10 FTS spectra recorded (55 m, 293 K)



④ Applications to CO₂ IR spectra at low densities

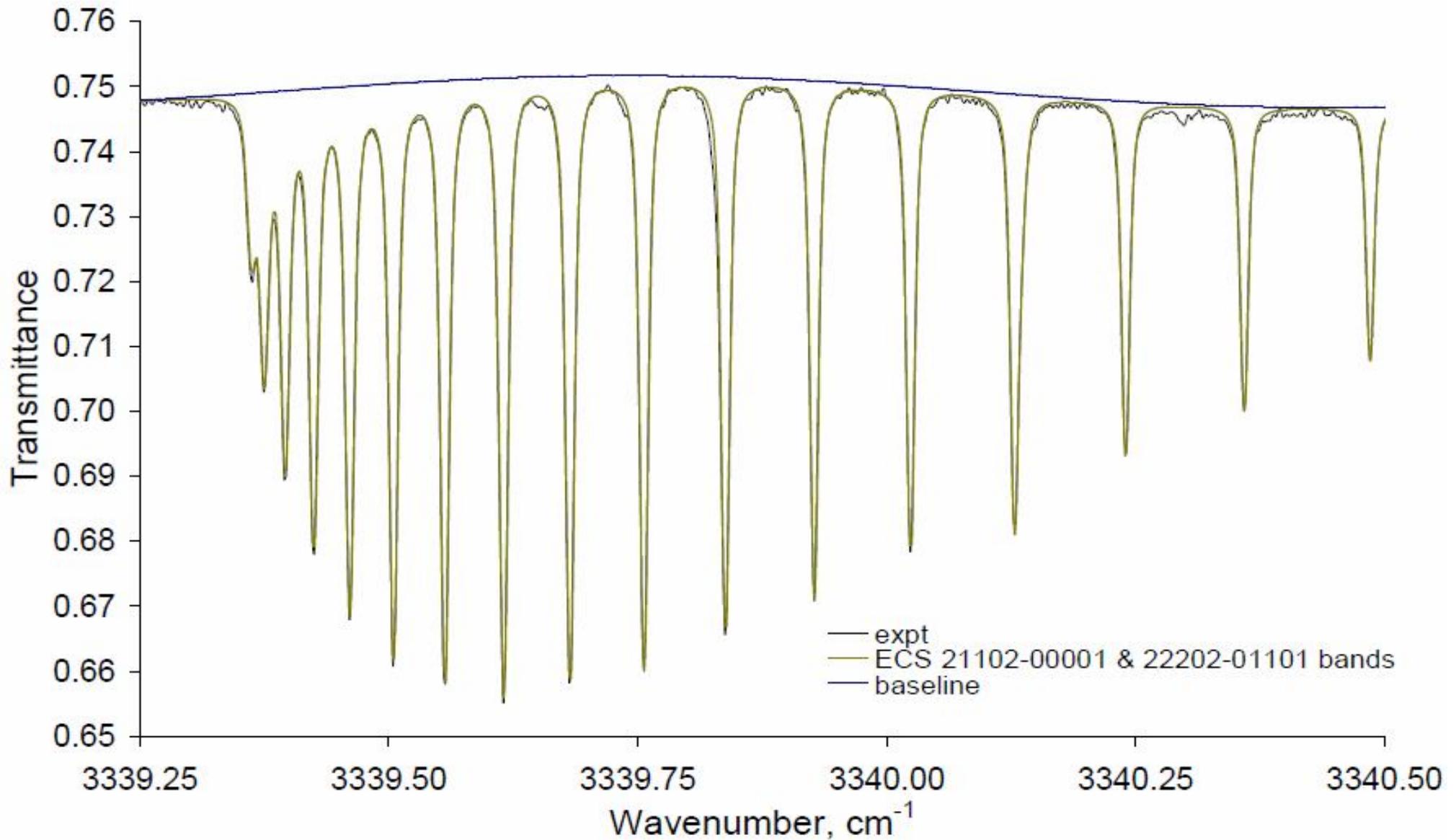


④ Applications to CO₂ IR spectra at low densities



④ Applications to CO₂ IR spectra at low densities

0.029 atm Q-branch zoom



Main results

- Immediate good agreement with expt OCS-He spectra up to 300 atm **without any additional fitting parameter**
- Satisfactory agreement for CO₂ up to nearly liquid phase **(+ 1 fitting parameter)**
- Excellent agreement with low-density expt CO₂ spectra down to 0.03 atm
- The model has **a universal character** (IR, Raman iso, aniso)

Further improvements/tests/applications

- Studies of extremely low pressures (narrowing effects)
- Modeling of $\text{Im } \Gamma$
- Studies of **far wings (non-Markovian effects)**
- Modeling of temperature dependences
- Calculations of correlation functions from *ab initio* PES
- Studies of other bands and other molecular systems