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Coupled-cavity terahertz quantum cascade lasers for single mode operation

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We demonstrate the operation of coupled-cavity terahertz frequency quantum-cascade lasers composed of two sub-cavities separated by an air gap realized by optical lithography and dry etching. This geometry allows stable, single mode operation with typical side mode suppression ratios in the 30–40 dB range. We employ a transfer matrix method to model the mode selection mechanism. The obtained results are in good agreement with the measurements and allow prediction of the operating frequency. © 2014 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4884056>]

Laser diodes exploiting the coupled-cavity (CC) geometry where two sub-cavities are separated by an air gap were first demonstrated in the 1980s as a means for achieving single mode operation, alternative to distributed Bragg reflectors (DBRs) or distributed feedback (DFB) lasers.^{1–8} The attractiveness of this approach resides in its inherent fabrication simplicity with, however, an important limitation given by the need to control the width of the air gap between the two sections with sub-wavelength precision in order to obtain single mode-operation with a high side mode suppression ratio (SMR). In this work, we show that the CC technique can be successfully implemented to obtain single mode emission for a quantum cascade laser (QCLs) operating in the terahertz (THz) frequency range. Compared to the near-IR, the two orders of magnitude increase in wavelength considerably relaxes the difficulty in controlling the gap size and could help this technique to become a viable alternative to DFB resonators.^{9–13} Indeed, we report single mode operation in continuous wave (CW) with a SMR larger than 30 dB regardless of the pump current or operating temperature.

The QCL used in this work is based on the bound-to-continuum design active region, embedded in a single plasmon waveguide, described in Ref. 14. As shown schematically in Fig. 1(a), the two-section cavity consists of two waveguides, of lengths L_1 and L_2 , coupled by an air gap realized by Inductively Coupled Plasma (ICP) etching. As an example, in Fig. 1(b), we show an optical microscope image of a 4 μm -wide air gap, etched to a depth of $\sim 15 \mu\text{m}$, and penetrating the whole QCL active region.¹⁴ To evaluate the effect of the gap on the guided mode, we used a 2-D finite difference frequency-domain (FDFD) code developed according to Ref. 15. Two examples of the results obtained are displayed in Figs. 1(c) and 1(d), for gaps of width 6 μm , and 20 μm , respectively, the gap depth being kept constant at 15 μm . Here, the pre-computed waveguide fundamental mode is injected at position $z = z_1$, and the resulting squared electric field distributions are shown in a logarithmic color scale (to

avoid reflections from the boundaries of the computational domain, we employed perfectly matched layers as discussed in Ref. 15). It is clear that, as the gap width is increased from 6 μm to 20 μm , an increasing amount of energy is scattered towards the substrate, exciting higher order modes. From the point of view of laser operation, this power is therefore lost. In order to quantify such losses, we repeated the same simulation for different gap widths, evaluating the fraction of power that remains in the fundamental mode past the gap (at position $z = z_2$ in Figs. 1(c) and 1(d)). This was obtained by projecting the field at $z = z_2$ onto the pre-computed fundamental guided mode, and by computing the power carried by that component (for the exact implementation see Ref. 16). As shown in Fig. 2, the fraction of transmitted power is observed to decrease rapidly to below 40% as the gap is increased from 0 to 20 μm . To limit the scattering losses, we

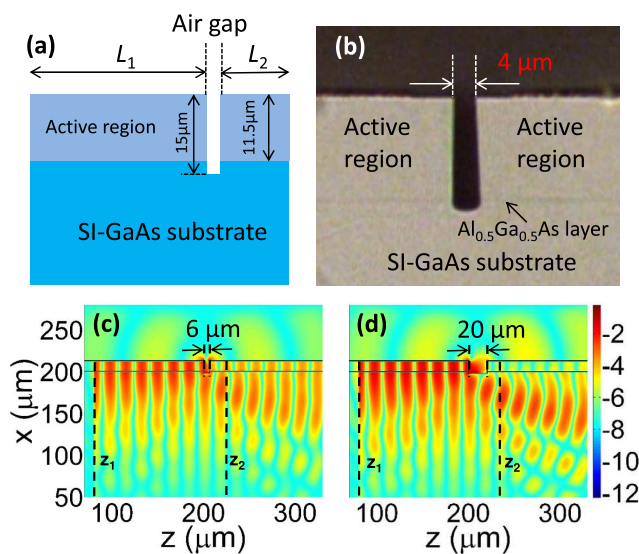


FIG. 1. (a) Schematic cross section of the CC QCL. (b) Optical microscope photograph of a 4 μm -wide air gap realized with ICP etching. The 11.5 μm thick active region is separated from the semi-insulating GaAs substrate by a 300 nm-thick $\text{Al}_{0.5}\text{Ga}_{0.5}\text{As}$ layer. This is visible in the photograph, as indicated by the black arrow. (c) FDFD simulation results for air gap widths of 6 μm (left) and 20 μm (right). The squared electric field component along the x-axis is shown in logarithmic color scale.

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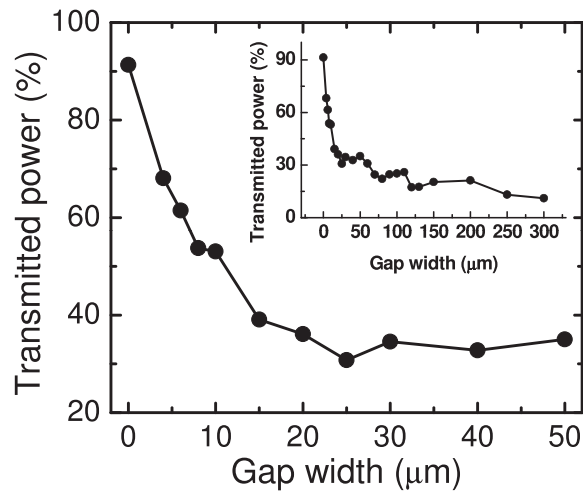


FIG. 2. Fraction of power transmitted in the fundamental mode through the air gap computed using an FDFD code for gap widths up to 50 μm . Inset. Same plot as main panel for gap widths up to 300 μm .

therefore used gap widths of 4 μm , 6 μm , and 8 μm for all the devices reported here.

To study the full CC device, we exploited an effective index, 1-D transfer matrix analysis described in detail in Ref. 17. The effective index in the waveguide sections was computed with COMSOL-Multiphysics, using the Drude conductivity in the doped layers and the GaAs bulk permittivity found in Ref. 18 at 2.5 THz.¹⁹ For the real part of the effective index inside the gap, we took a linear weighted sum of the material indices ($n=1$ for air and $n=3.6$ for the semi-insulating GaAs), with weights being derived from the FDFD simulations by computing the integral of the normalized field intensity at mid gap in each material. For the gap widths of 4 μm , 6 μm , and 8 μm used in this work, we obtain effective indexes of 2.8, 2.75, and 2.6, respectively. The imaginary part of the effective gap index was then determined in order to account for the scattering losses described in the previous paragraph (see Fig. 2). Once the effective indexes are computed, the CC device can be described analytically: interface matrices take into account the reflection and transmission coefficients at each interface, while propagation matrices describe the field propagation inside each section. By imposing the condition that there is no incoming light from outside the laser, one finally gets a complex propagation constant that provides the frequency of each longitudinal mode as well as its total losses.¹⁷

Figure 3 shows the total propagation losses (i.e., the sum of the material and radiative losses) as a function of the eigenmode frequency, obtained from the scattering matrix method for a selection of cavities with different widths of the air gap and lengths of the two cavities (we used material losses of 4 cm^{-1}). Results are presented corresponding to the lengths of the two cavities used experimentally (see below). The error bars account for the $\pm 3\text{ }\mu\text{m}$ uncertainty when measuring the cavity lengths. From Fig. 3, the spacing between two neighboring eigenfrequencies, although not constant, lies close to the free spectral range (FSR) of the long cavity ($\sim 20\text{ GHz}$).²¹ At the same time, in all cases, we observe a sizeable modulation of the losses with a quasi-periodicity close to the FSR of the short cavity

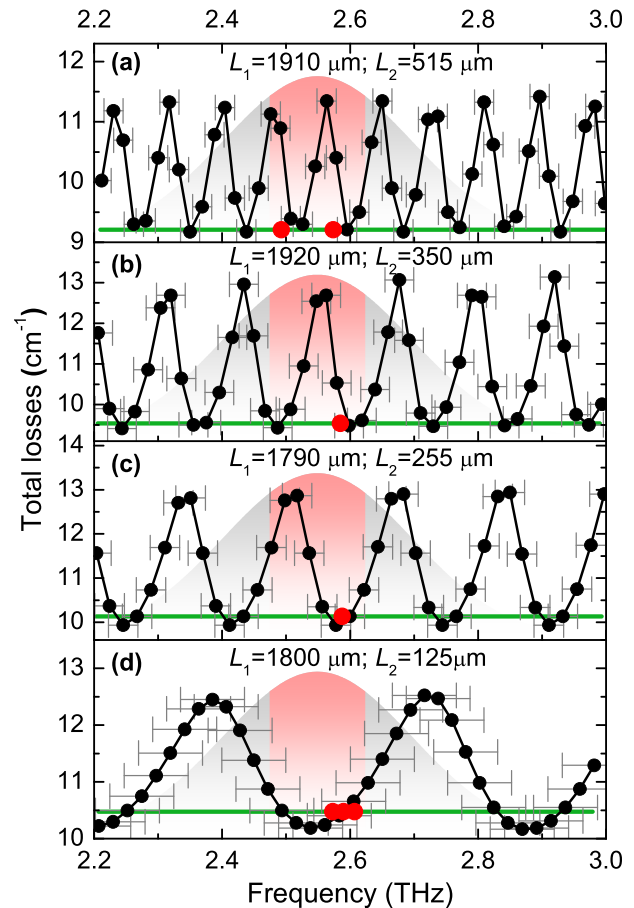


FIG. 3. Total propagation losses obtained from the scattering matrix method for the CC devices used in the experiment. The lengths of each cavity are shown. From top to bottom panel, the air gap widths are of 6 μm , 8 μm , 6 μm , and 4 μm , respectively. The error bars account for the $\pm 3\text{ }\mu\text{m}$ uncertainty in determining the cavity lengths. Horizontal green lines correspond to the total losses of a Fabry-Perot cavity of length $L_1 + L_2$. The red dots represent the experimental mode frequencies (see Figs. 4 and 5). For devices corresponding to panels (b) and (c), we obtained single mode emission. The shaded Gaussians represent schematically a gain curve of $\sim 350\text{ GHz}$ FWHM, centered at 2.55 THz (the curve has no relation with the y-axis scale). The red center part is 150 GHz wide and represents the lasing bandwidth centered at 2.55 THz as derived from Fig. 4(a). The value of the gain FWHM was taken from Ref. 20.

(315 GHz, 155 GHz, 115 GHz, and 80 GHz for cavity lengths of 125 μm , 255 μm , 350 μm , and 515 μm , respectively). In an effective mirror picture, this is produced by the etalon effect of the short cavity + air gap, which modulates the radiative losses of the long cavity.^{5,8} As a result, lasing action should occur in proximity to the loss minima, provided that these are not too far from the peak of the gain curve. To this end, to promote single mode operation, the distance between two loss minima should be somewhat larger than the typical lasing bandwidth (or gain peak).⁸ At the same time, however, increasing the separation between two minima/maxima will progressively reduce the curvature at the minimum of the loss curve, eventually leading to multimode operation when the loss difference between two neighboring eigenmodes is too small. For the active region used in this work, the typical lasing bandwidth of multimode Fabry-Perot cavity lasers can be up to 150 GHz (see Fig. 4(a));²¹ hence, the short cavity length should not significantly exceed 250 μm (FSR $\sim 155\text{ GHz}$) or be too much below this value. The

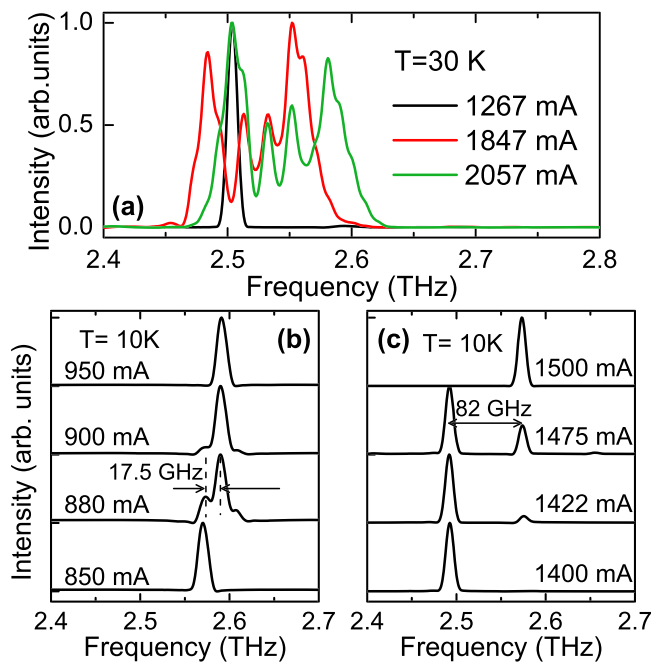


FIG. 4. (a) Measured emission spectra for a 4 mm-long, 160 μm -wide Fabry-Perot cavity ridge at different pump currents. The device was driven in CW at a heat sink temperature of 30 K. (b) Emission spectra in CW mode of the CC laser corresponding to Fig. 3(d). The ridge width is of 160 μm . (c) Emission spectra in CW mode of the CC laser corresponding to Fig. 3(a). The ridge width is of 220 μm .

lengths chosen in Fig. 3, with a long cavity length (L_1) of 1.8–1.9 mm, and short cavity lengths (L_2) equal to 515, 350, 255, and 125 μm should therefore provide an adequate set of devices to validate experimentally the mode selection mechanism.

Devices were first processed, using optical lithography and wet etching, into 160 μm and 220 μm -wide single plasmon waveguides. Air gaps (15 μm deep), with widths of 4 μm , 6 μm , and 8 μm , were then realized using ICP dry etching (Fig. 1(b)). Finally, the devices were cleaved to obtain sections of the desired lengths. For their characterization, devices were indium bonded to a copper holder that was subsequently screwed onto the cold head of a continuous flow liquid-helium cryostat. As pointed out in the previous paragraph, at high pump currents the typical lasing bandwidths of the bound-to-continuum active regions used in this work can extend up to ~ 150 GHz.^{14,21} To verify this we first fabricated conventional ridge cavity lasers, i.e., without air gap. A few representative emission spectra recorded at 30 K in CW operation are displayed in Fig. 4(a) for a 4 mm-long, 160 μm -wide ridge. Close to threshold (1260 mA) the emission is single mode but (as expected) at higher currents the emission becomes strongly multimode with a center frequency of 2.50–2.55 THz, and a maximum lasing bandwidth of ~ 150 GHz is observed close to the maximum emitted power.

Fig. 4(b) shows four representative spectra of a CC QCL with cavity lengths $L_1 = 1800$ μm and $L_2 = 125$ μm , (see Fig. 3(d) for the corresponding loss modulation). Spectra were collected with a FTIR spectrometer with a resolution of 7.5 GHz. The QCL was driven in CW mode at a heat sink temperature of 10 K, with the top metal contacts of the two sections shorted using wire-bonds, as was the case for all the

presented CC devices. For currents up to approximately 850 mA (the threshold current, not shown, is of 700 mA), single mode emission is observed centered at 2.57 THz. When the drive current approaches 900 mA, however, emission switches to multimode, as shown in Fig. 4(b) at $I = 880$ mA and 900 mA. For higher currents single mode emission is then recovered at 2.59 THz and maintained up to the maximum emitted power at 950 mA. As shown by the red dots in Fig. 3(d), the measured multimode spectrum lie, within the error of the frequency measurement, at the minimum of the loss curve between 2.5 and 2.6 THz.²² The mode separation is ~ 17.5 GHz, which, within the spectrometer resolution, is also in agreement with the computed mode spacing of ~ 22 GHz derived from the Fig. 3(d). For this CC device, the loss modulation curvature is therefore too weak to maintain single mode operation over the entire current operating range. Another situation where we observe multimode operation is displayed in Fig. 4(c), for $L_1 = 1900$ μm and $L_2 = 515$ μm (see Fig. 3(a) for the corresponding loss modulation plot). Again, between pump currents of 1400 mA and 1500 mA, two modes appear, at 2.490 THz and 2.574 THz. As shown by the red dots in Fig. 3(a), the frequencies of these two modes correspond to two computed loss minima, and their difference of 82 GHz is in excellent agreement with the computed value of ~ 84 GHz. In this case, despite the curvature being sufficiently strong to prevent the simultaneous lasing of neighbouring eigenmodes, two modes belonging to adjacent loss minima can be brought above threshold simultaneously since they fall within the ~ 150 GHz bandwidth.

Figure 5 shows the electrical and optical characteristics of a CC QCL with $L_1 = 1790$ μm and $L_2 = 255$ μm (see Fig. 3(c) for the computed loss modulation). In this case, single mode operation is achieved over the full operating current range (Fig. 5(b)). Indeed, as shown by the red dot in Fig. 3(c), the emission frequency of 2.588 ± 7.5 GHz is in very good agreement with the position of the loss minimum. Moreover, in this case, the distance between two loss minima

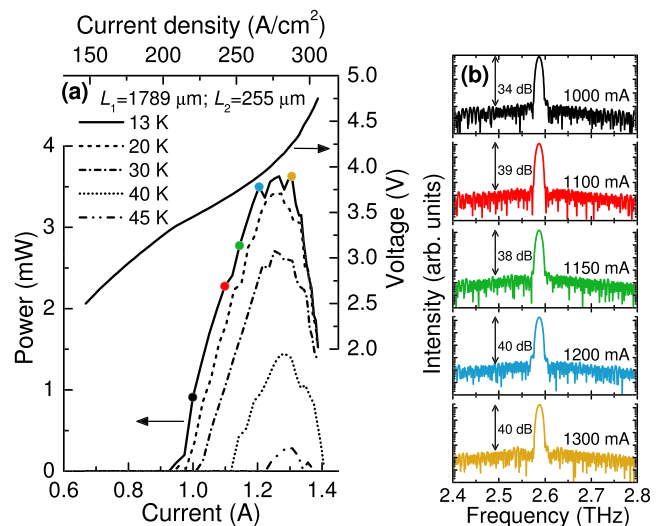


FIG. 5. (a) Voltage/current (right axis) and collected power/current (left axis) characteristics of the CC device corresponding to Fig. 3(c); the ridge width is of 220 μm . (b) Emission spectra at $T = 13$ K (see the colored dots in the left panel). All data were collected in CW mode.

is ~ 160 GHz, i.e., almost double compared to Fig. 3(a), preventing bi-mode oscillation. From Fig. 5(b), the achieved SMR is between 30 and 40 dB regardless of the operating current. This is comparable to the best results reported in the literature for edge or surface emitting THz QCLs.^{10–14,22,23} We have also verified (not shown) that single mode emission is maintained up to the maximum operating temperature of 45 K. Furthermore, we find essentially the same result (i.e., stable single mode oscillation with similar SMRs) for the device corresponding to Fig. 3(b) (spectra not shown). We therefore conclude that for a long cavity length of ~ 2 mm, single mode operation can be ensured by having short cavity lengths in the 250–350 μm range.

For the $L_1 = 1790 \mu\text{m}$ and $L_2 = 255 \mu\text{m}$ device, presented in Fig. 5, the maximum emitted power at a heat sink temperature of 13 K is in excess of 3.5 mW. The latter was measured with a calibrated THz power meter and was not corrected for the polyethylene window transmission coefficient ($\sim 70\%$). In general, for all tested CC devices, we found no significant degradation in performance compared to Fabry-Perot cavity devices, both in terms of threshold current and emitted power. To understand this further, it is instructive to compare the minima of the propagation losses in Fig. 3 with the losses of the bare Fabry-Perot cavities of the same lengths ($= L_1 + L_2$), displayed by the horizontal green lines. In all four cases, the latter slightly exceeds those of the CC lasers. This means that when the reflectivity of the short cavity etalon reaches a maximum, the corresponding decrease in radiative loss more than compensates for the additional scattering loss introduced by the air gap (see Figs. 1(c)–2). This effect can also be evaluated in the framework of an effective reflectivity approximation.⁸ For example, for the cavity lengths of Fig. 3(c), we obtain an effective reflectivity of the combined air gap + short cavity of 0.75, leading to a total mirror losses of 4 cm^{-1} , i.e., significantly less than the 6 cm^{-1} obtained for a Fabry-Perot cavity of the same total length (facet reflectivities of 0.3 on both sides).²⁴ This is the reason why for the gap widths used in this work (4 μm , 6 μm , and 8 μm) we observe no significant change of the threshold current when compared to Fabry-Perot devices. This is unlike the situation for the plasmon-waveguided DFB THz QCLs demonstrated to date.^{9,11} Indeed, these devices rely on loss coupled gratings patterned on the top laser metallization that inevitably introduce significant additional losses (the increase in waveguide losses can be up to $\sim 50\%$).^{9,11,25} In Fig. 6(a), we report the minimum of the total losses as a function of the gap width. As can be seen, the latter exceeds the losses of the Fabry-Perot cavity (solid green line) for gap widths larger than $\sim 20 \mu\text{m}$ (the cavity lengths are those of Fig. 3(c)).

In Fig. 6(b), we report the computed emission frequency as a function of the short cavity length. The former was extracted from the minimum of the computed loss curve, assuming that single mode operation is maintained. It can be seen that, in principle, it is possible to tune continuously the emission frequency by ~ 140 GHz by changing the short cavity length from 250 μm to 265 μm , yielding a tuning coefficient of $\sim 10 \text{ GHz}/\mu\text{m}$ (note that a change of gap width from 4 μm to 20 μm yields instead a maximum tuning of 30 GHz). A tuning of a few GHz can thus in principle be obtained using optical lithography. This is not the case for a THz

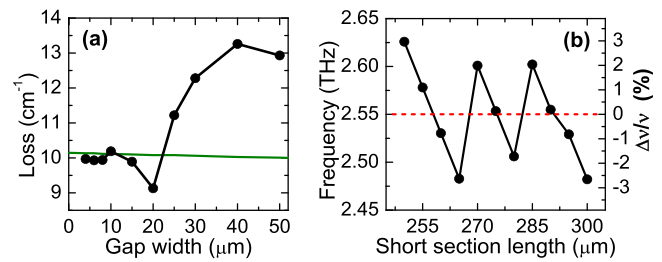


FIG. 6. (a) Total losses vs gap width for the CC device of Fig. 3(c). The black dots correspond to the minimum of the computed losses close to 2.55 THz. The solid green line represents the total losses of a Fabry-Perot device of the same total length. (b) Computed emission frequency as a function of short section length for the CC device of Fig. 3(c). The emission frequency is taken from the minimum of the computed losses close to 2.55 THz. The right axis represents the fractional frequency tuning from 2.55 THz (dashed red line).

QCL DFB laser, where the tuning coefficient at 2.5 THz is $\sim 100\text{--}200 \text{ GHz}/\mu\text{m}$.^{9–11,25} In practice, to control the emission frequency in the CC device precisely, one possibility would be to define a cavity length by lithography and then realize both facets by deep ICP etching into the substrate.

In conclusion, we have reported the operation of CC THz QCLs and shown that this geometry is capable of providing robust single mode emission with SMRs in the 30–40 dB range. Changing the short cavity length allows in principle a fine tuning of the emission frequency over ~ 100 GHz, making of this technique a promising alternative to DFB gratings. The radiative loss modulation induced by the CC scheme could also be used as a method to obtain integrated anti-reflection coatings at the QCL facets for the realization of THz amplifiers.^{20,26}

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