

## Multiband hairpin-line bandpass filters by using metamaterial complimentary split ring resonator

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### ABSTRACT

Telecommunication systems for the new generation have greatly stimulated the demand for multi-band bandpass filters with compact dimensions, low insertion loss, robust, low cost and less complex design. In this paper, a compact multi-band bandpass filter, with the fractional bandwidth of 40% and 20% at resonant frequency 3.5 and 5.5 GHz respectively with the response of Chebyshev passband ripple of 0.1 dB is presented. This bandpass filter is suitable for WiMAX application. The design is based on the hairpin-line configuration and metamaterial of complimentary split ring resonator structure. The hairpin-line is used for the compact structure design and easy to fabricate because it has open-circuited ends that require no grounding. While the complimentary split ring resonator structure is easy to design and can provide multi-band without affecting of size and performance of the filter. The simulated results show the dual-band bandpass response with the insertion loss is 0 dB and high attenuation at stopband. The proposed filter provides a compact, low insertion loss, and less complex structure design that are promising candidates in order to meet the demands of the new generation of communication systems.

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## 1. INTRODUCTION

The development of the telecommunication systems have enhanced the requirement for more sophisticated devices in order to meet the demands of the new generation of communication systems. In recent years, most of the wireless communication systems require a multifunctional device that can be operated in two or more frequency bands, small size, compact, robust and low cost. For example, the WiMAX applications that can be operate dual frequency band which are 3.5 GHz and 5.5 GHz. In the wireless systems, transmitter-receiver or transceiver is an important device that transmits and receives the modulated signal through a transmission medium. Multi-band transceiver components, such as multi-band bandpass filter, amplifier and oscillator are key devices to reduce the cost and the size of a multi-standard wireless system. In this paper, a multi-band bandpass filter has been proposed. The challenges to circuit designers designing a multiband bandpass filter are to achieve a small size and low insertion loss simultaneously. The previous researchers, the structure of multi-band filters design very complexly because have too many components inside and high insertion loss [1-4].

The hairpin-line band-pass filter is one of the most popular microstrip filter configurations used for the compact structure. This design is easy to fabricate because it has open-circuited ends that require no grounding. This design is obtained by folding the resonators of parallel-coupled into a “U” shape. This configuration will reduce the length of the conventional parallel-coupled band-pass filter. The examples

of previous work that using hairpin-line and interdigital configuration to design a compact filter have been reported in [5-7]. The size of the filter is 82.04 mm x 48.50 mm and has a more compacted structure compare to the conventional parallel-coupled method [6]. In addition, the hairpin filter can greatly improve the frequency selectivity compared with parallel-coupled structure [7].

Recently, many researchers have been attracted by a new type of artificial materials called as metamaterials. The metamaterials are a material engineered to have electromagnetic properties that are not found in nature [8-10]. The metamaterials have effective negative permittivity ( $\epsilon$ ) and negative permeability ( $\mu$ ) which was theoretically investigated by a Russian scientist Veselago [11]. In RF and microwave engineering, in order to obtain properties not present in the conventional material, the metamaterial transmission lines have been proposed. Metamaterial transmission line is an artificial line consisting of a host line such as a microstrip and coplanar waveguide (CPW) loaded with reactive elements such as inductances, capacitance or resonator [12-13]. Metamaterials are implemented with a split ring resonator (SRR) and complementary split ring resonator (CSRR) [14-16]. The advantages of CSRRs and SRRs are to reduce circuit dimension because the dimension of these resonators is much smaller than the signal wavelength at resonance. The previous researchers have been proved that by using metamaterial of CSRR can provide a compact design and without affecting the performance of filters [17-19].

In this paper, the metamaterials of CSRR have been studied to be used as a band-pass or band-stop filter. Then the CSRRs structure is combined with the hairpin-line bandpass filter to produce multi-band frequency responses. A proposed multi-band bandpass filter has provided compact size, less complex design with low insertion loss and high attenuation at stopband.

## 2. FILTER DESIGN

The proposed multi-band filter is designed in the following steps. The first step is to design a wide bandpass filter covering the frequency from 3.5 to 6.5 GHz by using hairpin-line configuration. The second step is to design a bandstop and bandpass filter at frequency 5 GHz based on CSRR configuration. The third step is to integrate the hairpin-line filters with the CSRR bandstop filter to result in a dual-band bandpass filter. This will be explained in details in the following.

### 2.1. Hairpin-line filter design

The conventional wideband hairpin-line bandpass filter was designed at a resonant frequency of 5 GHz, fractional bandwidth of 66%, 5 poles design, and the response of Chebyshev with passband ripple of 0.1 dB. The rogers RT6006 is used as substrate with a dielectric constant 6.15. The hairpin structure was designed by using copper as conducting element with thickness,  $t$  is 0.035 mm.

The element values for Chebyshev function low-pass prototype filters was obtained from Table 1, given for a normalized low-pass cut-off frequency  $\Omega_c=1$ , are  $g_0 = g_6 = 1.0$ ,  $g_1 = g_5 = 1.1468$ ,  $g_2 = g_4 = 1.3712$  and  $g_3 = 1.9750$ . The physical dimensions of hairpin-line in Figure 2 are calculated by using the following formulas [20].

$$Q_{e1} = \frac{g_0 g_{01}}{FBW}, Q_{en} = \frac{g_n g_{01}}{FBW} \quad (1)$$

$$M_{i,i+1} = \frac{FBW}{\sqrt{g_i g_{i+1}}} \text{ for } i = 1 \text{ to } n - 1 \quad (2)$$

Table 1. Element values for Chebyshev lowpass prototype filters [20]

N	G1	G2	G3	G4	G5	G6
1	0.3052	1.0				
2	0.8431	0.6220	1.3554			
3	1.0316	1.1474	1.0316	1.0		
4	1.1088	1.3062	1.7704	0.8181	0.3554	
5	1.1468	1.3712	1.9750	1.3712	1.1468	1.0

Where  $Q_{e1}$  and  $Q_{en}$  are the external quality factors of the resonators at the input and output, and  $M_{(i,i+1)}$  are the coupling coefficients between the adjacent resonators. The hairpin resonators as shown in Figure 1 have a line width of 1 mm and a separation of 2 mm between the two arms.

A design equation is proposed for estimating the tapping point,  $t$  as shown below [20], in which  $Z_r$  is the impedance of the hairpin line,  $Z_o$  is the terminating impedance, and  $L$  is about  $\lambda_{go}/4$  long. Figure 2 shows all physical dimensions of hairpin-line bandpass filter operate at frequency 5 GHz.

$$t = \frac{2L}{\pi} \sin^{-1} \left( \sqrt{\frac{\pi Z_0/Z_r}{2 Q_e}} \right) \tag{3}$$

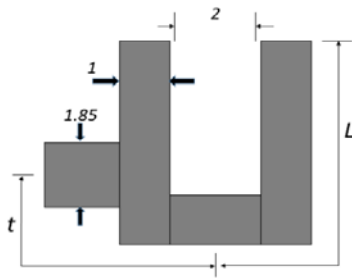


Figure 1. Hairpin resonator

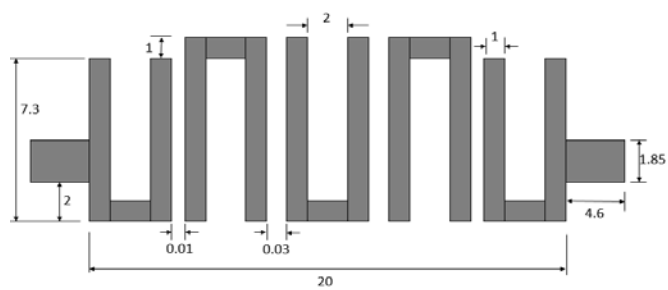


Figure 2. Geometry of hairpin-line structure at frequency 5 GHz

**2.2. Multi-band bandpass filter design**

The unit cell of CSRRs as shown in Figure 3 was designed at resonant frequency 5 GHz, using Rogers RT6006 as a substrate with a thickness of 1.27 mm, a relative permittivity of 6.15, and a loss tangent of 0.025. From the Figure 3, the conducting lines at top layer have a series gap and without a series gap.

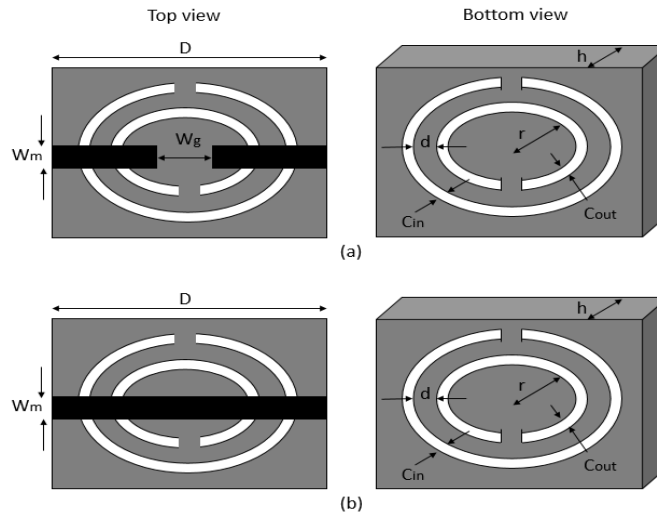


Figure 3. Unit cell of CSRRs with a series gap (a) and without series gap (b)

Table 2 shows all parameters of a unit cell CSRR in Figure 3. The values of the parameters are slightly different compared to the theoretical calculation to reach the design specification.

Table 2. Dimensions of unit cell CSRR

Parameters	Symbol	Value (mm)
Length of conducting line	D	8
Width of conducting line	W <sub>m</sub>	1
Length of series gap	W <sub>g</sub>	0.4
Inner radius of the first ring	r	1.26
Width of the first ring	C <sub>in</sub>	0.366
Width of the second ring	C <sub>out</sub>	0.364
Gap between the ring	d	0.4

## 2.2. Multi-band bandpass filter design

The multiband metamaterial hairpin-line bandpass filter was designed to resonate at 3.5 GHz and 5.5 GHz. Rogers RT6006 is used as a substrate with a thickness of 1.27 mm and a relative permittivity of 6.15. The filter specification is design to be 5 poles with the fractional bandwidth of 40% and 20% and using the response of Chebyshev with passband ripple 0.1 dB.

Figure 4 shows the proposed multiband bandpass filter configuration that combine wideband hairpin filter with three unit cell CSRR metamaterial. From the picture, the yellow color is a hairpin structure at the top layer and the red color is CSRRs at the ground plane. The conventional wideband hairpin-line bandpass filter and CSRR unit cell was designed to resonate at 5 GHz.

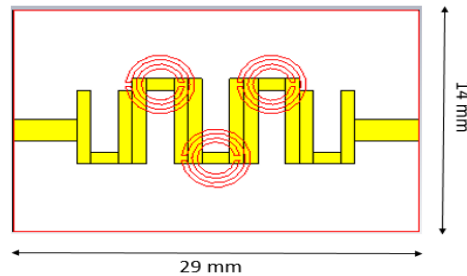


Figure 4. Multiband metamaterial hairpin-line bandpass filter

## 3. RESULTS AND DISCUSSION

Figure 5 shows the simulation results of the conventional wideband hairpin bandpass filter that simulate by using CST Software. It can be seen that the center frequency for hairpin filter is 5 GHz with bandwidth of 3.32 GHz. At the center frequency, the insertion loss,  $S_{21}$  is 0 dB and the attenuation loss at upper and lower cut off frequency are greater than -10 dB. Meanwhile, the return loss,  $S_{11}$  is less than -10 dB, so this wideband hairpin filter has good performances.

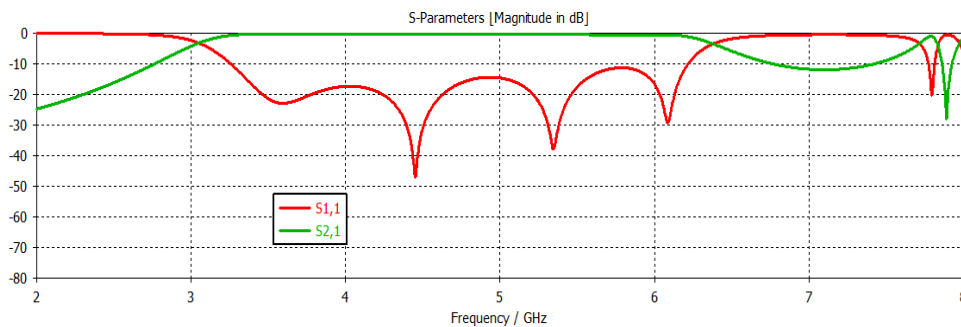


Figure 5. Simulation result of conventional hairpin filter

Figure 6 shows the simulation result of unit cell CSRR with a series gap and without a series gap. The s-parameter result shows the bandpass characteristic response of the CSRR with the series gap configuration at 5 GHz and the bandwidth is around 400 MHz as shown in Figure 6 (a). While, the CSRR without a series gap shown a bandstop characteristic at 5 GHz with bandwidth around 500 MHz as shown in Figure 6 (b). However, based on these results, the filter performances for single CSRR unit cell is not very good especially for bandpass filter because at the upper cut-off frequency the attenuation loss is lower. Thus, to solve this problem, three CSRRs unit cell is added in cascade to increase the attenuation loss at upper frequency.

Figure 7 shows the simulation results of multiband metamaterial hairpin bandpass filter. From the simulation results, the center frequency of passband is around 3.5 GHz at the first band and around 5.5 GHz for the second band. The insertion loss for the both passband is 0 dB. Moreover, the bandwidth at first band is around 1.9 GHz and 1.2 GHz for the second band. At the stop-band, the center frequency is 4.7 GHz with the bandwidth of 500 MHz. The return loss,  $S_{11}$  at first and second passband is less than -10 dB. Then, the

attenuation at stopband is very high at -50 dB and the attenuation at upper frequency at second passband has been increased to -20 dB compared to previous conventional hairpin filter. This show that we can design a dual band filter with improves performances by adding CSRRs metamaterial structure to conventional wideband hairpin filter.

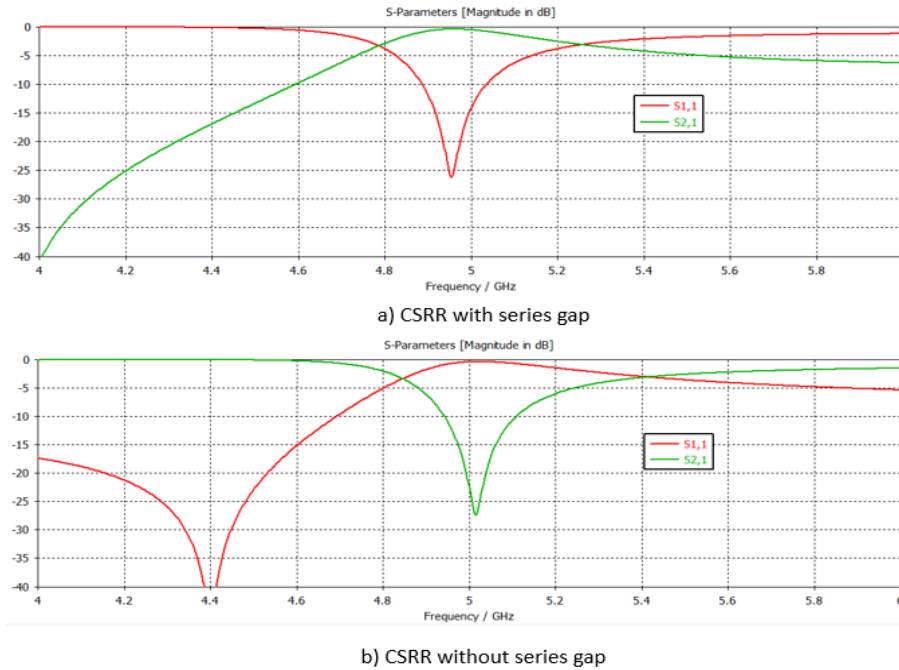


Figure 6. Simulation results of unit cell CSRR

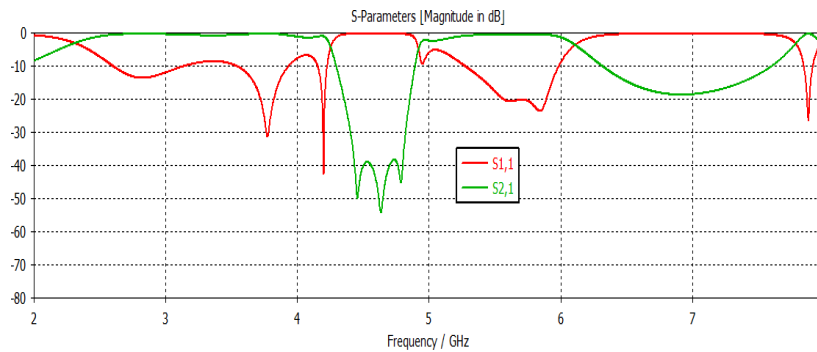


Figure 7. Simulation result of multiband metamaterial hairpin bandpass filter

Table 3 shows the comparison interms the performances and sizes of the proposed filter with the other reported designs. It can be seen that the size of the proposed filter is slightly bigger than the other filters but still can be considered compact. In addition, the performance of the proposed filter is much better than the other filters with lower insertion loss at desired passband as shown in Table 3.

Table 3. Comparison the proposed filter with the other reported

	f1 / insertion loss	f2 / insertion loss	Size
[3]	3.5 GHz / 2 dB	5.5 GHz / 2 dB	19mm × 16.65mm
[4]	3.5 GHz / 1.1 dB	5.75 GHz / 0.89 dB	19mm × 12mm
Proposed filter	3.5 GHz / 0 dB	5.5 GHz / 0 dB	29mm × 14mm

#### 4. CONCLUSION

In this paper, a unit cell CSRR operating at 5 GHz has been successfully designed and analyzed. From the results, it can be concluded that a unit cell CSRR with a series gap has the bandpass characteristic and a unit cell CSRR without a series gap has the bandstop characteristic. The result performances of single CSRR can be improved by adding more CSRRs unit cells in cascade. Finally, a multiband metamaterial hairpin bandpass filter operating at 3.5 and 5.5 GHz has been presented. The proposed multiband bandpass filter has better performances compared to the conventional hairpin filter design.

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