

Modified AES cipher round and key schedule

Edjie M. De Los Reyes¹, Dr. Ariel M. Sison², Dr. Ruji P. Medina³

^{1,3}Technological Institute of the Philippines, Philippines

²Emilio Aguinaldo College, Philippines

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ABSTRACT

In this paper, Advanced Encryption Standard was modified to address the low diffusion rate at the early rounds by adding additional primitive operations such as exclusive OR and modulo arithmetic in the cipher round. Furthermore, byte substitution and round constant addition were appended to the key schedule algorithm. The modified AES was tested against the standard AES by means of avalanche effect and frequency test to measure the diffusion and confusion characteristics respectively. The results of the avalanche effect evaluation show that there was an average increase in diffusion of 61.98% in round 1, 14.79% in round 2 and 13.87% in round 3. Consequently, the results of the frequency test demonstrated an improvement in the randomness of the ciphertext since the average difference between the number of ones to zeros is reduced from 11.6 to 6.4 along with better-computed p-values. The results clearly show that the modified AES has improved diffusion and confusion properties and the ciphertext can still be successfully decrypted and recover back the original plaintext.

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Corresponding Author:

Edjie M. De Los Reyes,
Technological Institute of the Philippines,
Quezon City, Philippines.
Email: emdelosreyes@tsu.edu.ph

1. INTRODUCTION

Development of information technology has immensely influenced the change in communication from conventional to digital means [1]-[3], this improvement in communication lead to confidentiality issues especially during the transit of information from source to its intended recipient [4], [5].

Information hiding and cryptography are the most common approach in providing information security [6], [7]. Steganography is a method of information hiding where it uses digital media as a cover to conceal information. However, once the pattern is known the information can be easily recovered [8], [9].

Cryptography is used to secure any form of communication system [10]-[12] by scrambling the information so that only the intended recipient can access it. Cryptography uses two general schemes: hashing and encryption. The cryptographic encryption scheme is classified into asymmetric and symmetric. The Advanced Encryption Standard (AES) is a symmetric block encryption defined by the Federal Information Processing Standards (FIPS) issued by the National Institute of Standards and Technology (NIST) of the United States of America (USA) and is currently the standard for encryption.

The AES algorithm, founded on the design of Belgian cryptographers Joan Daemen and Vincent Rijmen became the standard for encryption starting 2002 [13]. The algorithm has a data block length of 128 bits with variable key sizes of 128-bit (called AES-128), 192-bit (AES-192), and 256-bit (AES-256). The number of rounds to complete the process of encryption depends on the key size: 10 rounds for AES-128; 12 rounds for AES-192; and 14 rounds for AES-256 [14]. AES has different advantages such as security, flexibility, and ease of implementation.

Although AES is secured there is still room for improvement, especially in its diffusion property [15], [16] as it was observed that diffusion rate is quite slow in the early rounds [17], [18]. This paper introduced

two modifications to the standard AES to improve the diffusion property and as well as its confusion property. First modification is in the AES key schedule, additional permutation operations are used in the cipher key before it is expanded and second is in the AES cipher round where additional key permutation operations were introduced between states to achieve faster diffusion rates and better randomness of encrypted data.

2. RESEARCH METHOD

The two modifications to the standard AES are in (1) the key schedule algorithm and (2) the cipher round algorithm.

The key scheduling algorithm of AES is modified by introducing an additional byte substitution process and round constant addition through XOR prior to the generation of the subkeys: to prevent the cipher key bits from being used directly [19]. These modifications in the key scheduling algorithm are shown in Figure 1.

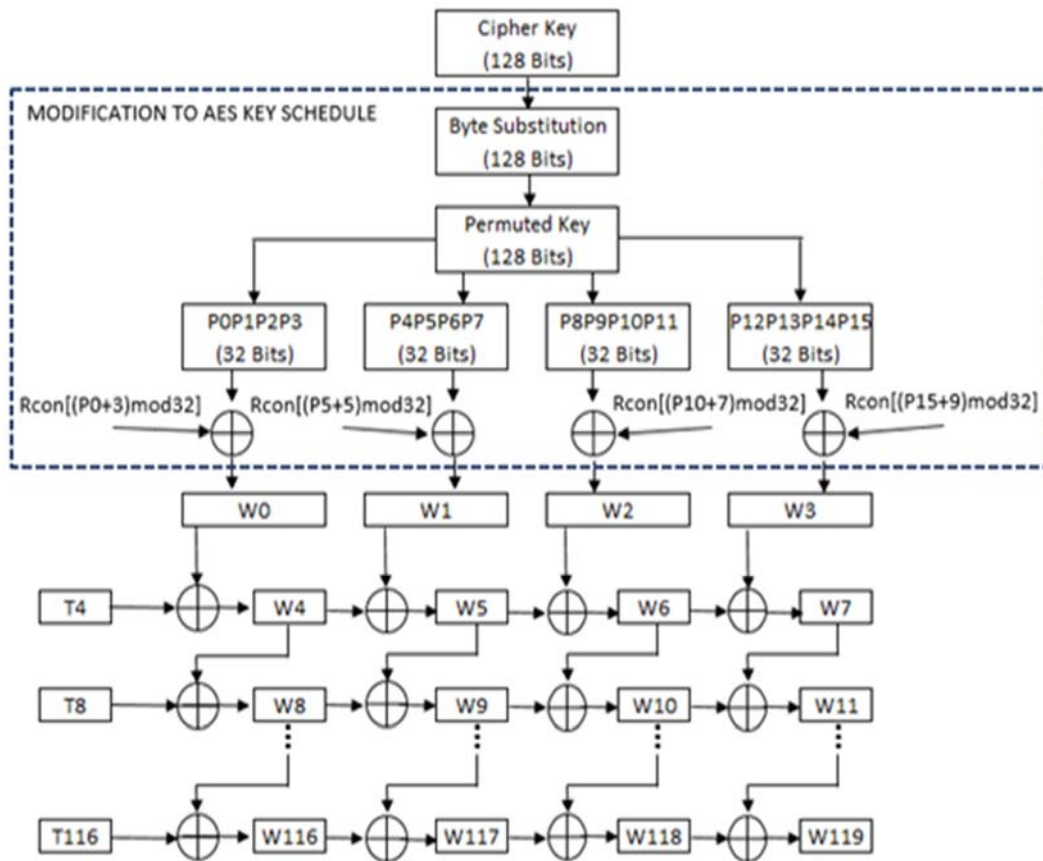


Figure 1. Modified AES Key Schedule

The standard S-box of the AES is used in the additional byte substitution process to provide additional obscurity to the cipher key since part of the design of the S-box is nonlinearity [20]. Furthermore, the output of the substitution herein referred to as permuted key (P), is then divided into four words where each word consists of 32 bits in length and each word is XORed with a value taken from the round constant of AES.

The round constant to be used will depend on the value of a specific byte of a word. The round constant is utilized to remove any symmetries in the cipher key [20]. Lastly, the succeeding stages in the key schedule algorithm are the same as the standard AES except for the number of iterations needed to generate all the required subkeys. The key schedule for both the encryption and decryption processes of the modified AES are the same.

Subsequently, the modifications to the cipher round algorithm of the AES in the encryption cycle are shown in Figure 2.

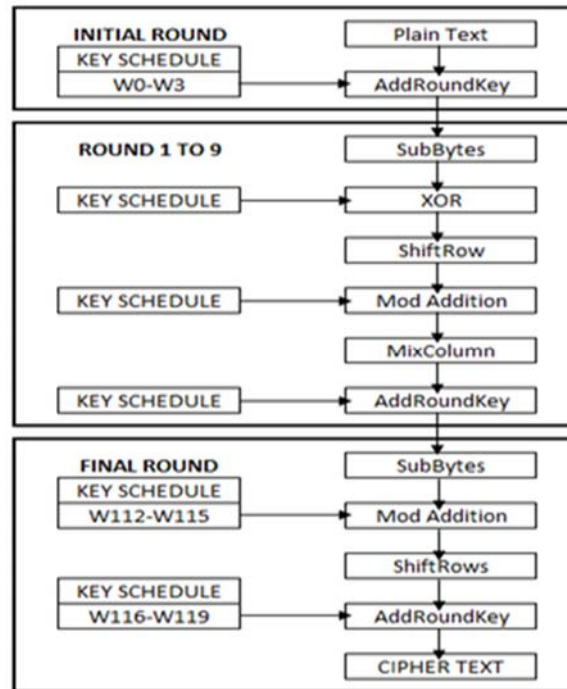


Figure 2. Modified AES Cipher Round - Encryption

The modifications to the AES cipher round are inclusions of XOR key permutation after the SubBytes operation and Modulo Addition key permutation after the ShiftRow operation from rounds one to nine. In the final round of the encryption, round ten, modulo addition is added after the SubBytes operation. The XOR operation is the same as the original add round key function, while modulo addition in the encryption process is a byte operation using the (1):

$$S'x = (Sx + Bwx) \bmod 256 \quad (1)$$

Where $S'x$ is the new byte of the resulting state after modulo addition, Sx is a byte of the current state to undergo modulo addition, and Bwx is the respective byte of the subkey that is to be added with the current state matrix.

To elucidate the modified AES encryption process, let “a3bb37a0fcfbff36ec56b737529723d2” be the plaintext in hexadecimal format and the cipher key as “6d6e636b795f72656f7365797765745f”. The given strings are first translated into 4 by 4 state matrix, the state matrix is formed by taking 2 hexadecimal characters at a time from the given string and arranged from top to bottom then left to right as shown in Figure 3.

In the initial round of the modified AES, the plaintext is XORed (AddRoundKey) with the first subkey in the key schedule which is W0-W3. The result of the AddRoundKey is then passed to the SubBytes process for byte substitution using the standard AES S-box.

The SubBytes process is the start of a new round. The succeeding processes: the byte substitution, the added add round key using XOR operation, the shift row operation, the added add round key operation using modulo addition, the mix column and the add round key using an XOR operation will iterate until round 9.

The last AddRoundKey operation of round 9 is then passed through the SubBytes. In this process, a byte substitution takes place where each byte of the AddRoundKey state matrix is replaced with an equivalent value based on the AES S-box, producing the SubBytes state matrix of the final round. The SubBytes state matrix is then modulo added with the subkey W112-W115 of the key schedule followed by a ShiftRow operation. The ciphertext is finally derived from the AddRoundKey operation of the ShiftRow state matrix and the final subkey W116-W119.

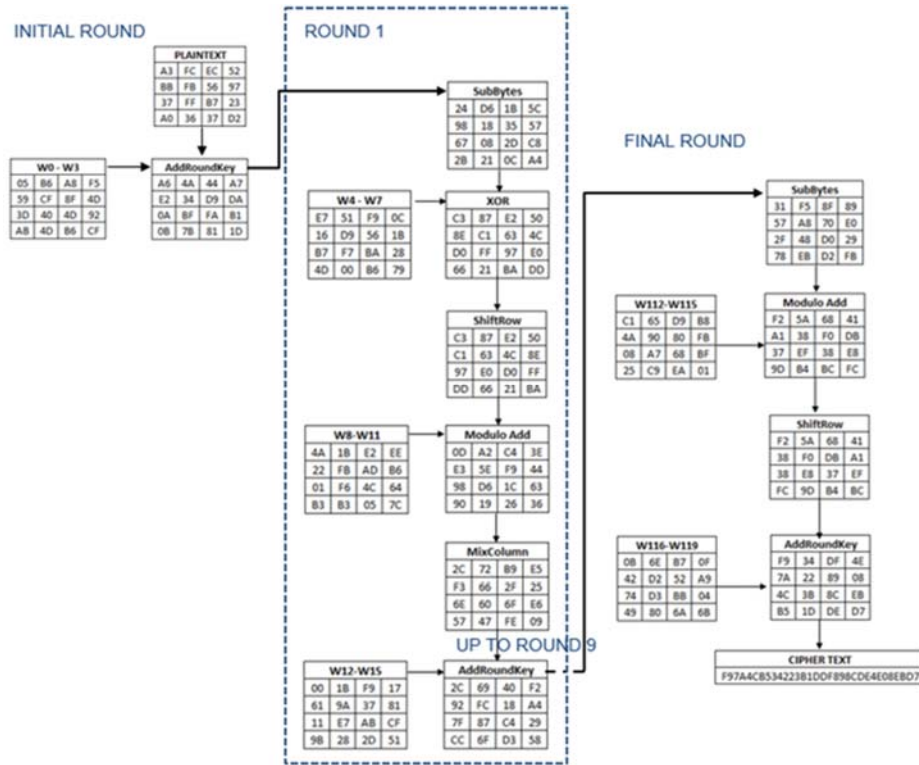


Figure 3. Illustrated Simulation of the Modified AES - Encryption Cycle

The decryption process will be the opposite of the encryption round where the different functions will be using their inverses: ShiftRow to Inverse ShiftRow, SubBytes to Inverse SubBytes, and MixColumns to Inverse MixColumns. While the modulo addition is changed to modulo subtraction and the formula used for modulo subtraction is shown in (2). The modified AES cipher round algorithm for decryption is shown in Figure 4.

$$Sx = (S'x - Bwx) \text{ mod } 256 \tag{2}$$

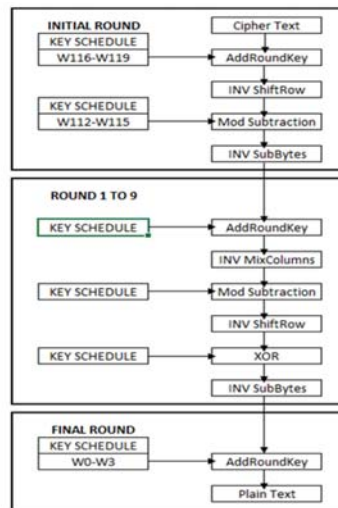


Figure 4. Modified AES Cipher Round - Decryption

An illustrative simulation of the decryption process is shown in Figure 5. The ciphertext input is XORed with the subkey W116-W119 of the modified AES key schedule, the key scheduling during decryption is also the inverse of the encryption key schedule, i.e. the first key schedule in the encryption cycle is the last key schedule in the decryption cycle.

The AddRoundKey state matrix is then applied with an inverse shift row operation and then modulo subtracted with the subkey W112-W115. The last operation in the initial round is an inverse byte substitution to the modulo subtraction state matrix.

The state matrix of the inverse SubBytes of the initial round is then XORed with the subkey W108-W111. The result of this step is the state matrix of the AddRoundKey and is then processed using the inverse mix column. These stages are repeated 9 times.

Subsequently, the state matrix of the inverse SubBytes of the ninth round is then XORed with W0-W3 subkey to recover back the original plaintext.

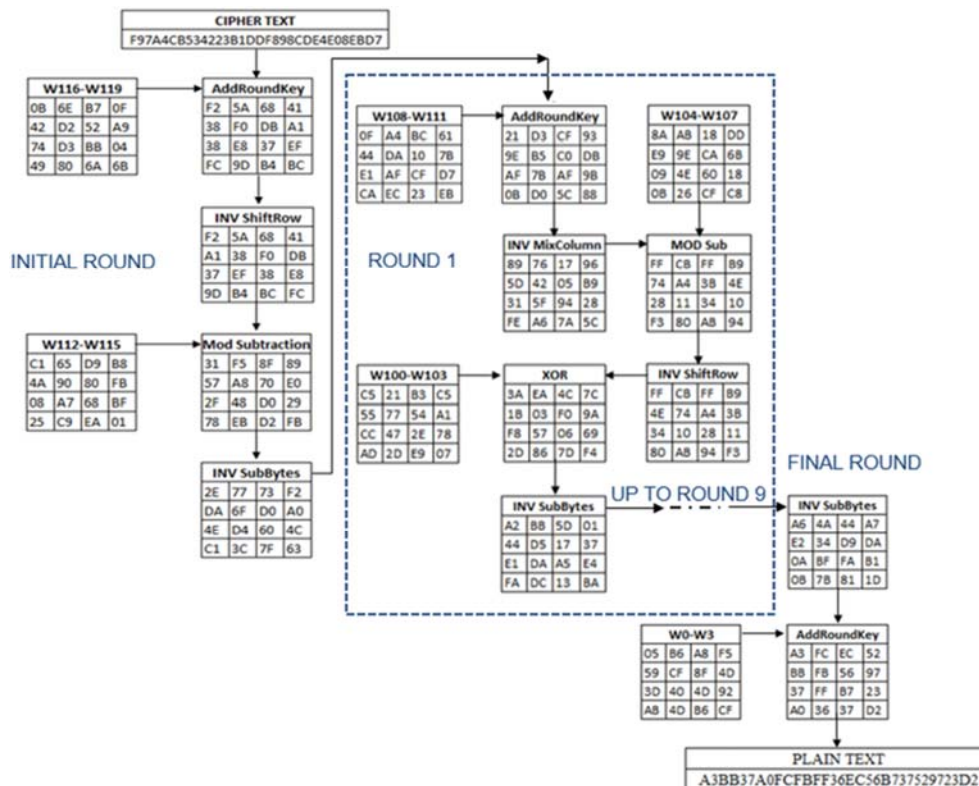


Figure 4. Illustrated Simulation of Modified AES Decryption Cycle

3. RESULTS AND ANALYSIS

The modifications to AES are tested using 10 different samples of plaintexts in hexadecimal format and to determine the performance of the modified AES in terms of its diffusion characteristics: the avalanche effect is employed. Hence, the status of one bit of the plaintext is changed (from bit 0 to bit 1 and vice versa) the highlighted hexadecimal character signifies this change in the bit status. The plaintexts are shown in Table 1.

The cipher key: 45654C65644D6F796A44736569655273 is used to encrypt the plaintexts enumerated in Table 1. The encrypted results of the standard AES for the 10 input samples of the original plaintexts and the plaintexts with one flipped bit are shown in Table 2. While the encrypted results for the modified AES are shown in Table 3.

The avalanche effect is computed by getting the summation of the number of bits that have changed between the encrypted plaintext and the ciphertext of the input with one bit flipped.

To demonstrate the effect of the modified AES cipher round and key schedule, the avalanche effect for the first 5 rounds of both the standard AES and the modified AES are taken and shown in Table 4.

Table 1. Input plaintexts

| Samples | Plaintexts | Plaintexts with One Bit Flipped |
|---------|----------------------------------|----------------------------------|
| 1 | 8CE0522352A3622E39D82E4E0C69459B | 8CE0522352A3622E19D82E4E0C69459B |
| 2 | B7FFDB3473357E17A08D8DDE34D614B9 | B7DFDB3473357E17A08D8DDE34D614B9 |
| 3 | AEF6A545B7B00CA10225CBE70EE25907 | AEF6A545B7B00CA14225CBE70EE25907 |
| 4 | 2A60EF8D9F0F6909612E7CE1734F33D6 | 2A60EF8D9F0F6929612E7CE1734F33D6 |
| 5 | B9A920481E1DC1705EB238D7C256665A | B9A920481E3DC1705EB238D7C256665A |
| 6 | AFDEAE30C1D4A939E89011467C11C955 | AFDEAE30C1D4A939689011467C11C955 |
| 7 | 0AE231D3CC3865DAB650465BE5A61D62 | 0AE231D3CC3865DAB650465BE5A61D63 |
| 8 | 6AAB3E2CE1EB488AEDE3E5C271E7B59D | 6AAB3E2CE1EB688AEDE3E5C271E7B59D |
| 9 | 5C484433CA71082A6544D0D923A5BC36 | 5CC84433CA71082A6544D0D923A5BC36 |
| 10 | F68545373518FE8658C8DF729DFCE965 | F68545353518FE8658C8DF729DFCE965 |

Table 2. Standard AES ciphertext results

| Samples | Encrypted Plaintexts | Encrypted Plaintexts with One Bit Flipped |
|---------|----------------------------------|---|
| 1 | 50796041DDC6C7748CD16621D03730BC | 95006CC37096C0D44D44ADBC3E717A5D |
| 2 | 1E44EFE4637CCAB5295BE522B38033FE | B5C1B3E66D0550C093167863ED4CA30 |
| 3 | 93737532CA9A374202A85A265879B2AD | 272A23CF82DA81096785FFE9EDD646F3 |
| 4 | E46E0D7E8740FBB9D6D765F7ECE61CED | EA62609CD436C42B97C15CA99B6509E9 |
| 5 | 27C24083CF405EA7D32FF5F5AF56DA2A | D35EA9DDF514FA899E02D4F422051050 |
| 6 | F7864F3BC4785C3F306B6C7735A8D632 | 8ABE1E0CAF227A539A0CCE4625D3B827 |
| 7 | 6D904E0F746CE9950BB4B7257706BC6F | 60DAAADCD8B9FA5F1EBD1718BCAF4521 |
| 8 | 6FBDBDBE2AAAF889FE7D9812C7765D82 | 5084EADE99F2869DD8678976FABAB47 |
| 9 | 0D39B23D5045A22AFB72DFE63427B7D7 | B90CBAC30B12037857DBA82023C30CCD |
| 10 | 78224BBB5F4061F92D463175F3BF4AFD | B06A2C1A27AFAB8F718B8463EB39F963 |

Table 3. Modified AES ciphertext results

| Samples | Encrypted Plaintexts | Encrypted Plaintexts with One Bit Flipped |
|---------|----------------------------------|---|
| 1 | B3A29FB59A819F5BD6B9A041FBA7BE93 | F847568BA83F2E8B74E9B9E3C26E476C |
| 2 | 2F32B3FF51F1808E85A3E0441EEDD43D | 42BD8A1A90B0FA91096C3B8861820C1B |
| 3 | 65BB3DB5163CA56B388FA44518156F45 | 616C805C353F49F5FDBA163DD92BD668 |
| 4 | E68585DC6BBA52013EE676BE0AF2F10E | 946C0199AE2EB5241747DF154A05D50C |
| 5 | 2762D80CEBE87736C8AD29AE5C15D3AD | 59C287045E148A23C958AC78432985FA |
| 6 | BF20B2AAEAF5162BCB6A3736EEC56F75 | D3D9CCE19AAE704650C04DB4FB922880 |
| 7 | BA1E83967AF7699223F6DC125BF4C44D | 19D905B7B6FA9E2147AFA662767CFEBB |
| 8 | 18AA0019AF8B669EECE63AE57155CFE4 | D65DCD48AECE1E240A653CC5747B67FA |
| 9 | 09D8A5397E0D65C2FD8FE81517803275 | 89DC4B724D54307543E1B55C6DCEFC6C |
| 10 | 3E64BA827097E648CA387E16421A49B5 | 7C75DD0FC8F7408BD1F3C7713F706F5B |

Table 4. Avalanche effect for the first five rounds

| Samples | Round 1 | | Round 2 | | Round 3 | | Round 4 | | Round 5 | |
|---------|---------|-------|---------|-------|---------|-------|---------|-------|---------|-------|
| | S.AES | M.AES | S.AES | M.AES | S.AES | M.AES | S.AES | M.AES | S.AES | M.AES |
| 1 | 13 | 21 | 60 | 66 | 65 | 69 | 72 | 78 | 76 | 67 |
| 2 | 13 | 19 | 51 | 78 | 64 | 74 | 72 | 72 | 59 | 63 |
| 3 | 16 | 19 | 62 | 69 | 69 | 84 | 55 | 72 | 76 | 67 |
| 4 | 5 | 16 | 75 | 77 | 55 | 67 | 71 | 69 | 62 | 65 |
| 5 | 5 | 22 | 60 | 62 | 59 | 62 | 64 | 73 | 64 | 70 |
| 6 | 13 | 20 | 59 | 73 | 69 | 72 | 61 | 68 | 63 | 67 |
| 7 | 10 | 20 | 65 | 74 | 62 | 66 | 69 | 74 | 67 | 62 |
| 8 | 10 | 20 | 63 | 70 | 57 | 73 | 66 | 63 | 66 | 70 |
| 9 | 18 | 19 | 75 | 76 | 53 | 64 | 53 | 65 | 58 | 69 |
| 10 | 18 | 20 | 59 | 77 | 60 | 67 | 66 | 62 | 63 | 72 |

Based on these results, there is a significant increase in the avalanche effect of the modified AES cipher round and key schedule compared to the standard AES. In round 1, the average avalanche effect of the standard AES is 12.1 bits while the modified AES is 19.6 bits giving 61.98% improvement over the standard AES. Moreover, the modified AES has an improvement of 14.79% and 13.87% in round 2 and round 3 respectively. Consequently, an increase in the average results of the avalanche effect of the modified AES rivaled with the standard AES is evidently shown in Figure 6, the increase in avalanche effect also indicates an increase in security compared to the standard AES [21], [22]. The overall improvement of the modified AES in the avalanche effect over the standard AES is about 7%.

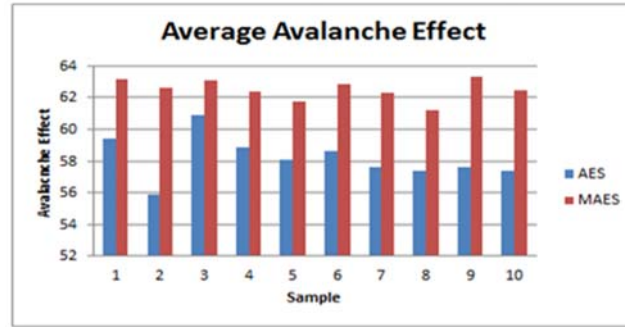


Figure 6. Comparison between Standard AES and Modified AES

To measure the confusion property of the modified AES, frequency test is utilized. The frequency test determines the randomness of a string by assessing the number of ones and zeros: when they are approximately the same in number then it indicates randomness [23]. The P -value in (3) will be used in determining whether a cryptographic result is either random or not.

$$P - value = \operatorname{erfc} \left(\frac{S_{obs}}{\sqrt{2}} \right) \quad (3)$$

The P -value is the probability of finding the observed results, under the null hypothesis of randomness [23], hence if the result of the P -value is <0.01 the null hypothesis is accepted meaning the cryptographic result is non-random. However, if the P -value is >0.01 then the cryptographic result is random.

The results of the frequency test of both the standard AES and the modified AES using the same input samples and key are shown in Table 5. The Ones and Zeros columns in the table represent the total number of ones and zeros respectively in the ciphertext string while the Sobs-column is the observed value.

Table 5. Frequency test results

| Samples | Ones | | Zeros | | Sobs | | p -value | |
|---------|-------|-------|-------|-------|-------|-------|------------|-------|
| | S.AES | M.AES | S.AES | M.AES | S.AES | M.AES | S.AES | M.AES |
| 1 | 58 | 72 | 70 | 56 | 1.061 | 1.414 | 0.289 | 0.157 |
| 2 | 67 | 65 | 61 | 63 | 0.530 | 0.177 | 0.596 | 0.860 |
| 3 | 60 | 64 | 68 | 64 | 0.707 | 0.000 | 0.480 | 1.000 |
| 4 | 76 | 66 | 52 | 62 | 2.121 | 0.354 | 0.034 | 0.724 |
| 5 | 68 | 66 | 60 | 62 | 0.707 | 0.354 | 0.480 | 0.724 |
| 6 | 69 | 73 | 59 | 55 | 0.884 | 1.591 | 0.377 | 0.112 |
| 7 | 67 | 68 | 61 | 60 | 0.530 | 0.707 | 0.596 | 0.480 |
| 8 | 74 | 65 | 54 | 63 | 1.768 | 0.177 | 0.077 | 0.860 |
| 9 | 69 | 62 | 59 | 66 | 0.884 | 0.354 | 0.377 | 0.724 |
| 10 | 70 | 59 | 58 | 69 | 1.061 | 0.884 | 0.289 | 0.377 |

Based on these frequency test results, all the encrypted texts for both standard AES and modified AES are random and henceforth non-linear since the computed p -values are higher than 0.01. However, it is noteworthy to point out that the distribution of ones and zeros have improved in the modified AES over the standard AES. The average difference between the distribution of 1's and 0's for the 10 samples are: 6.44 bits in the modified AES; 11.6 bits in the standard AES. Conversely, there are 7 instances where the modified AES is better than the standard AES in terms of computed p -values.

4. CONCLUSION

In cryptography, diffusion and confusion property indicates the strength of a cryptographic algorithm [24]. Based on the results, the modified AES cipher round and key schedule algorithm have shown an increased in the diffusion characteristics both in the early rounds and in the full rounds of encryption. This improvement is attributed to the introduction of additional key permutations in the cipher round using simple primitive operations such as exclusive OR and modulo arithmetic. Likewise, the confusion characteristics of the modified AES are enhanced based on the results of the frequency test. Moreover, the modified AES can be successfully

decrypted and recover back the original plaintext. However, though improvements were noted in the confusion property, there is still room for improvements.

For future works, the following may be considered, to introduce additional linear operations to improve further the confusion property and apply the modified AES cipher round and key schedule algorithm in securing confidential files. Additional study may be conducted to determine the effect of the added operations in terms of performance with respect to execution throughput of the modified AES.

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