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Estudio termodinámico de  
sistemas ricos en CO<sub>2</sub> en  
condiciones de interés para la  
tecnología CCS

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Tesis Doctoral

ESTUDIO TERMODINÁMICO DE  
SISTEMAS RICOS EN CO<sub>2</sub> EN  
CONDICIONES DE INTERÉS PARA LA  
TECNOLOGÍA CCS

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DEPARTAMENTO DE QUÍMICA FÍSICA

**TESIS DOCTORAL**

**ESTUDIO TERMODINÁMICO DE  
SISTEMAS RICOS EN CO<sub>2</sub> EN  
CONDICIONES DE INTERÉS PARA LA  
TECNOLOGÍA CCS**

**CLARA RIVAS ALONSO**  
ZARAGOZA 2017



*A mis padres, Ángeles y Miguel,  
por su amor, su apoyo y su constante lección de vida,  
no podría contar con dos mejores maestros.*

*A mi "hada madrina", Ángeles Vielba,  
por su infinito amor incondicional y libre.*

*A la memoria de mi abuela, Esteli Llana,  
una pequeña castellana  
de sabiduría innata a la que tanto añoro.*



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**ESTA TESIS DOCTORAL HA SIDO ESCRITA EN LA MODALIDAD DE COMPENDIO DE TRABAJOS PREVIAMENTE PUBLICADOS Y SU ESTRUCTURA, RECOGIDA EN EL ÍNDICE, SE AJUSTA A LA NORMATIVA VIGENTE. LAS PUBLICACIONES PRESENTADAS SON LAS SIGUIENTES:**

- ❖ Inmaculada Velasco, Clara Rivas, José F. Martínez-López, Sofía T. Blanco, Santos Otín and Manuela Artal. **Accurate Values of Some Thermodynamic Properties for Carbon Dioxide, Ethane, Propane and Some Binary Mixtures.** *Journal of Physical Chemistry B.* 2011, 115, 8216-8230.
- ❖ Sofía, T. Blanco, Clara Rivas, Javier Fernández, Manuela Artal and Inmaculada Velasco. **Influence of Methane in CO<sub>2</sub> Transport and Storage for CCS Technology.** *Environmental Science & Technology.* 2012, 46, 13016-13023.
- ❖ Clara Rivas, Sofía T. Blanco, Javier Fernández, Manuela Artal, Inmaculada Velasco. **Influence of methane and carbon monoxide in the volumetric behaviour of the anthropogenic CO<sub>2</sub>: Experimental data and modelling in the critical region.** *International Journal of Greenhouse Gas Control.* 2013, 18, 264-276.
- ❖ Sofía T. Blanco, Clara Rivas, Ramón Bravo, Javier Fernández, Manuela Artal and Inmaculada Velasco. **Discussion of the Influence of CO and CH<sub>4</sub> in CO<sub>2</sub> Transport, Injection and Storage for CCS Technology.** *Environmental Science & Technology.* 2014, 48, 10984-10992.
- ❖ Clara Rivas, Beatriz Gimeno, Ramón Bravo, Manuela Artal, Javier Fernández, Sofía Teresa Blanco, María Inmaculada Velasco. **Thermodynamic properties of a CO<sub>2</sub>-rich mixture (CO<sub>2</sub>+CH<sub>3</sub>OH) in conditions of interest for carbon dioxide capture and storage technology and other applications.** *Journal of Chemical Thermodynamics.* 2016, 98, 272-281.





## INFORME DIRECTORES

### AUTORIZACIÓN PRESENTACIÓN DE TESIS DOCTORAL EN MODALIDAD DE COMPENDIO DE PUBLICACIONES

D<sup>ª</sup> MANUELA ARTAL LERÍN, Profesora Titular del Departamento de Química Física de la Universidad de Zaragoza y D<sup>ª</sup> SOFÍA TERESA BLANCO ARIÑO, Profesora Titular del Departamento de Química Física de la Universidad de Zaragoza,

#### AUTORIZAN

La presentación en la modalidad de compendio de publicaciones de la siguiente memoria de Tesis Doctoral titulada:

“Estudio termodinámico de sistemas ricos en CO<sub>2</sub> en condiciones de interés para la tecnología CCS”, presentada por D<sup>ª</sup> CLARA RIVAS ALONSO para optar al Grado de Doctor por la Universidad de Zaragoza, y

#### HACEN CONSTAR

Que ha sido realizada bajo su dirección en el Departamento de Química Física (Facultad de Ciencias) de la Universidad de Zaragoza.

Y para que conste a los efectos oportunos expiden la presente autorización

En Zaragoza, a 23 de Marzo de 2017

Fdo.: Manuela Artal Lerín

Fdo.: Sofía T. Blanco Ariño



## INFORME MOTIVADO DE LA COMISIÓN ACADÉMICA DE DOCTORADO

D<sup>ª</sup> MARÍA INMACULADA VELASCO ALBILLOS, Presidente de la Comisión Académica de Doctorado del Programa de Doctorado de Química Física de la Universidad de Zaragoza,

### **CERTIFICA:**

Que el trabajo correspondiente a la presente Memoria titulada:

“Estudio termodinámico de sistemas ricos en CO<sub>2</sub> en condiciones de interés para la tecnología CCS”

Ha sido realizada en dicho Departamento por D<sup>ª</sup> Clara Rivas Alonso bajo la dirección de las Dras. D<sup>ª</sup> Manuela Artal Lerín y D<sup>ª</sup> Sofía Teresa Blanco Ariño, para optar al grado de Doctor.

En Zaragoza, a 29 de Marzo de 2017

Fdo.: M<sup>ª</sup> Inmaculada Velasco Albillos





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# INTRODUCCIÓN



## 1. INTRODUCCIÓN

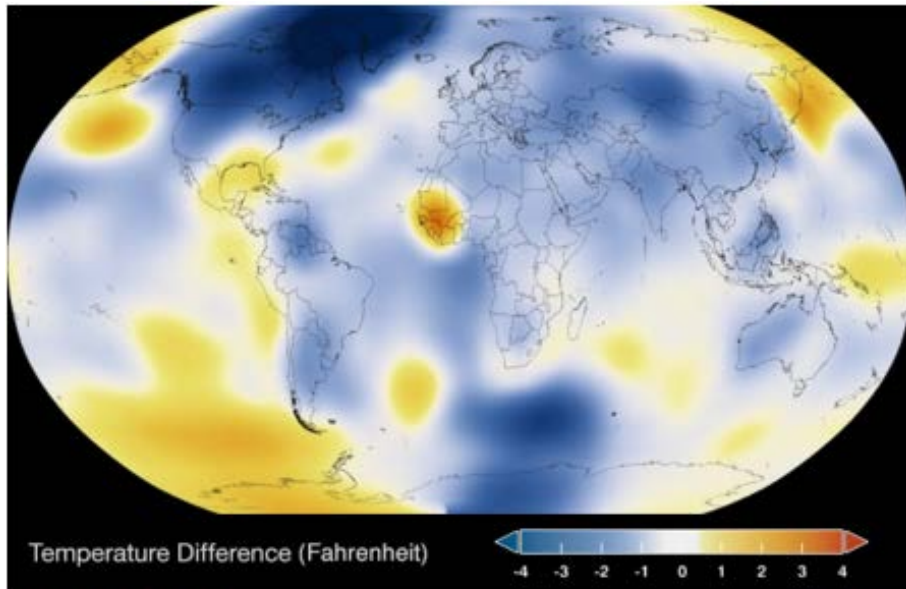
Uno de los mecanismos que posibilitan la vida en la Tierra es el efecto invernadero. Parte de la radiación emitida por el Sol que llega a nuestro planeta es reflejada por los gases atmosféricos y devuelta al espacio exterior, pero la mayoría penetra en la propia atmósfera. Una fracción es absorbida por los propios gases y la otra por la superficie terrestre. Asimismo, la Tierra emite radiación infrarroja que es a su vez reflejada, absorbida o transmitida por ciertos gases atmosféricos. La fracción de radiación absorbida por tales gases contribuye al denominado efecto invernadero, que posibilita mantener la temperatura media del planeta en márgenes muy uniformes y compatibles con las formas actuales de vida. El aumento en la concentración de esos compuestos participativos, denominados GEI –gases de efecto invernadero- ocasiona una mayor opacidad infrarroja de la atmósfera, con lo que se produce un efecto invernadero intensificado. Si los niveles de estos compuestos ascienden demasiado, un calentamiento excesivo puede trastornar las pautas naturales del clima. Las concentraciones de GEI tales como dióxido de carbono, metano y óxido nitroso han aumentado, sobre todo, por la utilización de combustibles fósiles, la deforestación y otras actividades humanas, promovidas por el crecimiento económico y demográfico y son en la actualidad muy superiores a los valores preindustriales.

El potencial de calentamiento ambiental, PCA, más conocido en su terminología inglesa como GWP (Global Warming Potential) es el calentamiento que produce la liberación de un kilogramo de un gas de efecto invernadero en relación con el causado por un kilogramo de CO<sub>2</sub> en un periodo de 100 años. Si bien el CO<sub>2</sub> es el GEI que menos potencial de calentamiento atmosférico tiene, 1 frente a 21 el metano, 310 el óxido nitroso y hasta 23900 el hexafluoruro de azufre,<sup>65</sup> la cantidad de CO<sub>2</sub> emitida a la atmósfera es mucho mayor que la de cualquier otro gas, lo que hace que el porcentaje del efecto invernadero debido al CO<sub>2</sub> sea, con diferencia el mayor de todos.

Este efecto tiene como consecuencia un aumento de la temperatura terrestre y del nivel de los océanos e incide directamente sobre el calentamiento global y el cambio climático. En las Figuras 1a) y 1b) se observa el cambio en la temperatura del globo terráqueo desde 1884 hasta 2015.<sup>40</sup>

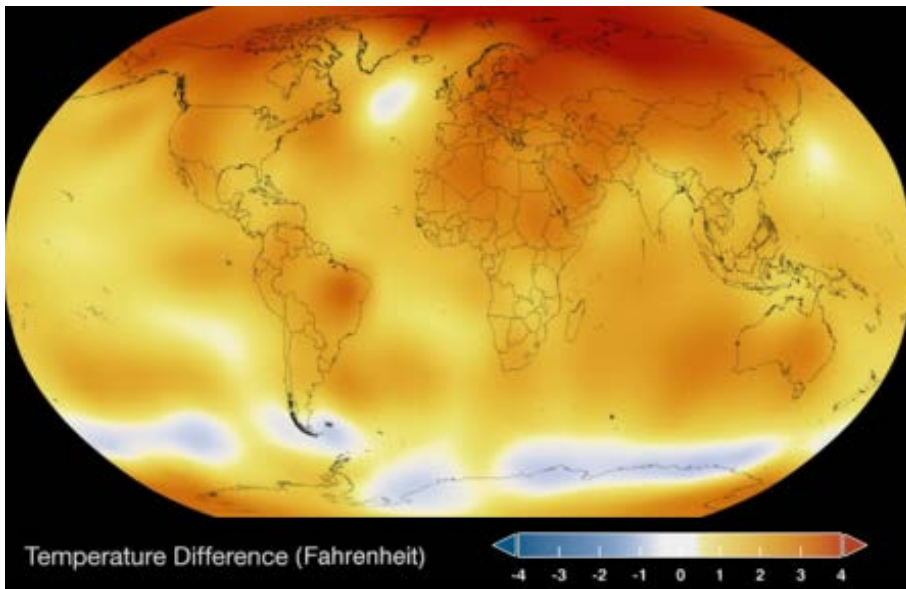
Así pues, la reducción de las emisiones de CO<sub>2</sub> producido por actividades humanas, CO<sub>2</sub> antropogénico, es un tema de vital importancia que atañe a todos los seres vivos del planeta.

a)



1884 2015

b)



1884 2015

Figura 1. Imágenes de las emisiones de gases en la Tierra a) en 1884, b) en 2015.<sup>40</sup>

Una de las estrategias más efectivas para reducir las emisiones de CO<sub>2</sub> atmosférico es la tecnología CCS (Carbon Capture and Storage). Esta tecnología consiste en la captura, acondicionamiento, transporte, inyección y almacenamiento geológico del CO<sub>2</sub> producido por la actividad humana, más del 95% del cual procede del sector energético. Esta tecnología se menciona de forma explícita en las Estrategias Europeas 2020 y 2050<sup>29, 30</sup> como uno de los métodos que debe contribuir a alcanzar el objetivo de reducir las emisiones europeas de GEI en un 80-95% para 2050. También se cita en la “Estrategia Española de Ciencia y Tecnología y de Innovación 2013-2020”.<sup>27</sup>

En agosto de 2013 el Global CCS Institute tenía identificados 65 proyectos CCS a gran escala en diversas etapas de desarrollo, de los cuales se ha estimado que 19 estén operativos en la actualidad.<sup>92</sup> Estos 19 proyectos suman una capacidad de almacenamiento de 38,5 millones de toneladas por año (Mtpa), muy lejana de las 7.000 Mtpa que se pretenden alcanzar para el año 2050.

Bajo el “27th Framework Programme (FP7)” de la Comisión Europea, la tecnología CCS se convirtió en un tema prioritario en la investigación energética dentro de la Unión Europea, con aproximadamente 160 millones de euros destinados como inversión para proyectos de investigación. Parte de estos proyectos incluyen la reducción de costes en la captura del CO<sub>2</sub>, evaluación de riesgos y peligros asociados al transporte del CO<sub>2</sub>, ampliación de la tecnología CCS a lo largo de las redes de cada país, y aseguramiento de la seguridad y eficacia del almacenamiento geológico.

La captura del CO<sub>2</sub> se puede lograr por postcombustión, precombustión u oxidación. Su acondicionamiento tras la captura, puede llevarse a cabo mediante deshidratación, separación de gases no condensables y/o licuefacción, compresión y bombeo. El transporte se realiza generalmente por tubería, y el CO<sub>2</sub> antropogénico finalmente se inyecta y se almacena en yacimientos de petróleo o de gas en explotación o agotados, yacimientos mineros agotados o formaciones salinas profundas (Figura 2).

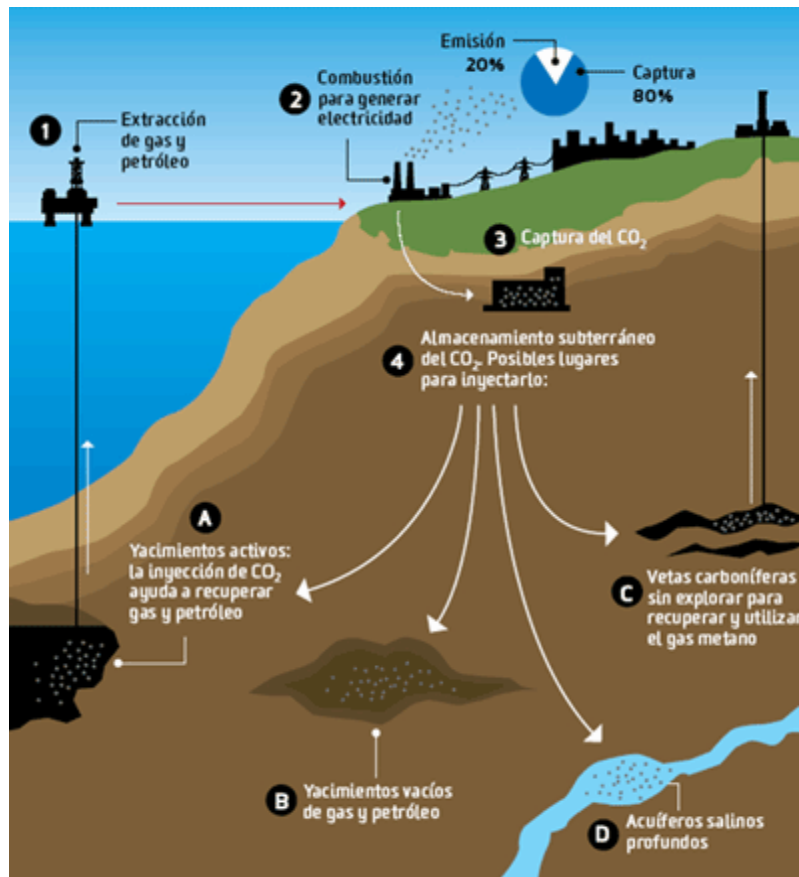


Figura 2. Representación de la emisión de CO<sub>2</sub> en una central eléctrica, su captura y su almacenamiento subterráneo en formaciones geológicas.

El diagrama de fases del CO<sub>2</sub> puro muestra como a temperaturas y presiones por encima de su punto crítico ( $P_c = 7.383 \text{ MPa}$ ,  $T_c = 304.21 \text{ K}$ ), las fases gas y líquido son indistinguibles y existe una única fase presente. Dicha fase, conocida como supercrítica, exhibe valores de viscosidad y densidad intermedios entre los de un líquido y un gas. La forma más económica y eficiente de transportar el CO<sub>2</sub> por tubería es hacerlo en condiciones de  $T$  y  $P$  en las que este compuesto se encuentra en fase densa (por encima de  $P_c$  y por debajo de  $T_c$ ) o supercrítica. Esto es debido a que el volumen ocupado por el CO<sub>2</sub> bajo condiciones supercríticas es unas 350 veces menor que el que ocupa en fase gaseosa y además su viscosidad es menor que la de los líquidos.

Sin embargo, el CO<sub>2</sub> transportado no es puro, proviene de muchas posibles fuentes, tales como centrales eléctricas de carbón, refinerías, reformado de asfalto, plantas de gas o de acero y cementeras. Por ello, el flujo de CO<sub>2</sub> contiene diversas impurezas, tales como: N<sub>2</sub>, O<sub>2</sub>, Ar, CH<sub>4</sub>, CO, SO<sub>x</sub>, NO<sub>x</sub>, H<sub>2</sub>S, H<sub>2</sub>, etc., en diferentes concentraciones. El aumento de la pureza del CO<sub>2</sub> evita posibles riesgos como por ejemplo la corrosión de las tuberías, y dependiendo de las impurezas que se eliminan, mejora el almacenamiento pero aumenta considerablemente el coste de la captura y del acondicionamiento.

La presencia y el tipo de impurezas afectan a las propiedades químico físicas del fluido, y como consecuencia al diseño y a la operación de los equipos necesarios en la tecnología CC.<sup>63</sup>. Además, en las diferentes etapas de la tecnología se cubren rangos de presión y temperatura muy amplios, ya que se transporta y se almacena en fase densa y/o supercrítica. En consecuencia, las propiedades químico físicas de la corriente de CO<sub>2</sub> antropogénico difieren de forma importante según su procedencia, y se modifican de forma más importante aún durante el proceso.

La presencia de impurezas en el CO<sub>2</sub> modifica la posición del punto crítico con respecto al CO<sub>2</sub> puro y la línea del equilibrio líquido-vapor (ELV) se transforma en una envolvente de fases que rodea a la región de coexistencia de las fases líquido y vapor (Figura 3), así la composición del fluido condiciona el valor de la presión mínima necesaria para asegurar el transporte en fase densa o supercrítica. Una de las características de los fluidos supercríticos en la región cercana al punto crítico es la gran variación en los valores de densidad,  $\rho$ , y de compresibilidad isotérmica,  $\kappa_T$ , cuando se producen pequeños cambios en la presión, temperatura y composición. Todas estas propiedades termodinámicas, influyen en varios parámetros que afectan a los procesos de transporte<sup>98</sup>: diámetro de tubería, caída de presión, velocidad de erosión, capacidad de las estaciones de recompresión, etc; y a los procesos de inyección y almacenamiento: parámetro de solubilidad, capacidad de almacenamiento, velocidad de ascensión de la pluma en acuíferos salinos y flujo de permeación.<sup>23</sup>

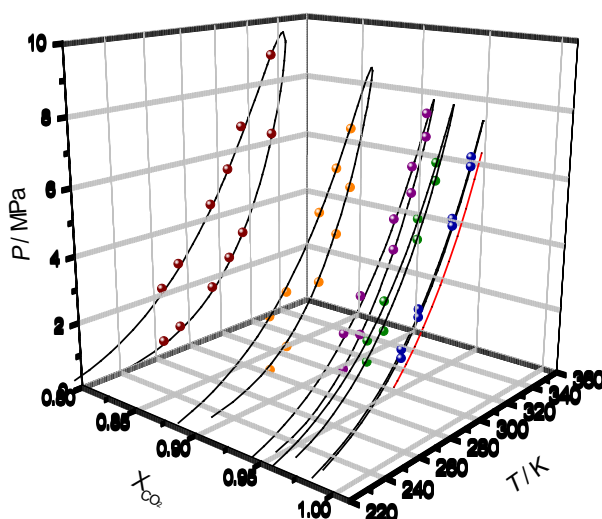


Figura 3. Presión de vapor del CO<sub>2</sub> puro (línea roja) y envolventes de fase de mezclas CO<sub>2</sub>+SO<sub>2</sub> con diferentes valores de fracción molar de CO<sub>2</sub>,  $x_{CO_2}$  (puntos: valores experimentales; líneas: calculados con PC-SAFT)<sup>35</sup>

Además del conocimiento de las propiedades volumétricas y del equilibrio líquido vapor del fluido a transportar y almacenar, la determinación de la velocidad del sonido,  $c$ , también es de gran interés puesto que permite durante la fase de transporte: i) conocer la distribución de tamaños de las burbujas en el líquido;<sup>56</sup> ii) detectar fugas;<sup>66, 69, 90, 104</sup> y

iii) estudiar la propagación de fracturas, puesto que depende de la relación entre la velocidad de la onda de presurización,  $v_p$  (directamente relacionada con  $c$ ) y la velocidad de fractura,  $v_f$ : si  $v_p > v_f$ , la fractura se detendrá y si  $v_p < v_f$ , se propagará hasta encontrar algún impedimento mecánico.<sup>5,26</sup> Asimismo, durante la fase de almacenamiento el conocimiento de  $c$  es necesario para: i) estudiar fugas en los almacenamientos<sup>10,56</sup> ii) realizar estudios sísmicos iii) optimizar procesos EOR; y iv) monitorizar el comportamiento de la pluma.<sup>54,87</sup>

En esta Tesis se estudian dos impurezas no condensables que puede contener el CO<sub>2</sub> antropogénico: el metano y el monóxido de carbono. El primero proviene, entre otros, de procesos derivados de la eliminación de los gases ácidos (H<sub>2</sub>S y/o CO<sub>2</sub>) en el gas natural y el CO, es habitual de procesos como la producción de petróleo. Tanto este compuesto como el metano pueden ser subproductos de la captura de pre-combustión en centrales energéticas.

Existe un vacío legal en lo referente al rango de composiciones permitido en el CO<sub>2</sub> antropogénico. Como consecuencia, el estudio experimental de los sistemas CO<sub>2</sub> + impurezas y la modelización termodinámica de los mismos cobra importancia a la hora de entender como su composición afecta a su comportamiento con el objeto de rentabilizar la tecnología asegurando al mismo tiempo la seguridad de la misma.

También hay poca definición en lo que respecta al cálculo económico del proceso dado que ninguno de los modelos utilizados en la actualidad tienen en cuenta el impacto de las impurezas en los diferentes parámetros de diseño. Además, la escasez de datos experimentales, en especial de propiedades volumétricas bajo las condiciones relevantes para la tecnología CCS, tiene como consecuencia que no haya todavía un modelo termodinámico validado en los rangos de la tecnología para predecir el comportamiento del fluido transportado y almacenado. Los modelos más comunes, basados en ecuaciones de estado, EoS, de distinta naturaleza, deberían comprobarse con datos experimentales de las mezclas en las condiciones en las que se produce el transporte y almacenamiento del CO<sub>2</sub> antropogénico.

Los trabajos que conforman esta Tesis recogen la puesta a punto de dos instalaciones experimentales, una para la medida de la densidad y otra para la determinación de velocidades del sonido, tanto en fluidos puros como en mezclas. Asimismo, proporcionan datos experimentales presión-densidad-temperatura-composición,  $P - \rho - T - x_{\text{CO}_2}$  y del ELV de los sistemas CO<sub>2</sub>+CH<sub>4</sub> y CO<sub>2</sub>+CO en composiciones, presiones y temperaturas de interés para la tecnología CCS. Estos datos nos permiten comprobar la capacidad predictiva de las EoS PR,<sup>75</sup> PC-SAFT<sup>36</sup> y GERG-2008<sup>50</sup> en los rangos estudiados en este trabajo mediante la comparación de los valores de las propiedades volumétricas y del ELV con los calculados con estas ecuaciones. A través del concepto de función de Krichevskii y de la teoría de Kirdwood-Buff se muestra el estudio teórico realizado sobre las interacciones existentes entre CO<sub>2</sub>/CH<sub>4</sub> ó CO cerca del punto



crítico. Por último, mediante los valores experimentales de densidad y ELV y los calculados de viscosidad, se determina la influencia del CO y del CH<sub>4</sub> sobre diversos parámetros que afectan al transporte, inyección y almacenamiento en la tecnología CCS. El análisis de estos parámetros es necesario para la construcción y operación seguras de los ceoductos, así como, para el almacenamiento fiable del CO<sub>2</sub> antropogénico a largo plazo en formaciones geológicas.



A decorative graphic featuring a dark blue rectangular border. Inside the border, the word "OBJETIVOS" is written in a bold, dark blue, sans-serif font. The text is centered and overlaid on a 3D-rendered molecular model consisting of three spheres: a large light gray sphere in the center, and two smaller light red spheres on either side, connected by thin lines. The spheres have a soft shadow cast beneath them.

# OBJETIVOS



## 2. OBJETIVOS

La adquisición y el mantenimiento de las instalaciones experimentales utilizadas en esta Tesis Doctoral, así como los trabajos realizados fueron financiados con los siguientes proyectos de investigación:

- CTQ2005-02213: "Equilibrio de fases a altas presiones de mezclas binarias y multicomponentes de fluidos petrolíferos y compuestos alternativos a las CFC".
- CTQ2008-02037: "Determinación de velocidades del sonido a altas presiones en fluidos petrolíferos y compuestos alternativos a los CFC; obtención de propiedades termodinámicas derivadas y modelización con EOS y RNA".
- UZ2008-CIE-02: "Obtención de propiedades derivadas de la velocidad del sonido en fluidos puros y gases".
- INF2008-CIE-05. "Mejora de una instalación de medida de velocidades del sonido a alta presión".
- CONVENIO CAIXA-DGA 2009: "Reducción de las emisiones de CO<sub>2</sub>: Determinación y predicción de las condiciones químico-físicas idóneas en el transporte y almacenamiento de CO<sub>2</sub>".
- CTQ2011-24875: Avances en la investigación para reducir las emisiones de gases de efecto invernadero: dióxido de carbono y refrigerante con alto potencial de calentamiento global".
- UZ2012-CIE-13: "Avances en la investigación para reducir las emisiones de gases de efecto invernadero: CO<sub>2</sub> y refrigerantes con alto potencial de calentamiento global (GWP)".

Los objetivos del presente trabajo han sido los siguientes.

1. Puesta a punto de una instalación de tubo vibrante para la determinación, en un amplio rango de presión y temperatura, de propiedades volumétricas para fluidos puros y mezclas.
2. Calibrado y puesta a punto de una instalación para la medida de velocidades del sonido en un amplio rango de presión y temperatura, en fluidos puros y mezclas.

3. Estudio experimental volumétrico y del equilibrio líquido-vapor de los sistemas  $\text{CO}_2+\text{CH}_4$  y  $\text{CO}_2+\text{CO}$ . Cálculo de incertidumbres. Determinación de propiedades derivadas y de sus precisiones.
4. Modelización de los sistemas  $\text{CO}_2+\text{CH}_4$  y  $\text{CO}_2+\text{CO}$  mediante Ecuaciones de Estado Cúbicas (PR)<sup>75</sup> y no cúbicas (PC-SAFT<sup>36</sup>, GERG-2008<sup>50</sup>).
5. Estudio estructural de los sistemas  $\text{CO}_2+\text{CH}_4$  y  $\text{CO}_2+\text{CO}$  en la región crítica a partir de la determinación de sus propiedades volumétricas a dilución infinita.
6. Estudio de la influencia de  $\text{CH}_4$  y  $\text{CO}$  en el transporte, inyección y almacenamiento del  $\text{CO}_2$  antropogénico en la tecnología CCS mediante el cálculo de parámetros característicos de dichos procesos a partir de las propiedades determinadas experimentalmente.



**APORTACIONES DEL  
DOCTORANDO**





### 3. APORTACIONES DEL DOCTORANDO

A continuación se describen las aportaciones realizadas por el doctorando para el desarrollo del presente trabajo y por tanto para la consecución de los objetivos concretos.

#### OBJETIVO 1

**Puesta a punto de una instalación de tubo vibrante para la determinación, en un amplio rango de presión y temperatura, de propiedades volumétricas para fluidos puros y mezclas.**

La instalación de tubo vibrante permite trabajar de forma dinámica asegurando que el sistema se encuentre en cada instante en cuasi-equilibrio termodinámico. Para ello, es necesario mantener un régimen cuasi-estático mediante la utilización del flujo óptimo del fluido de medida. El primer trabajo realizado fue determinar el valor óptimo de flujo necesario para realizar correctamente las medidas experimentales.

Se realizaron diferentes pruebas para optimizar el proceso de reducción de datos ya que el sistema de adquisición de datos de la instalación permite disponer de un gran número de ellos pero deben reducirse para facilitar cálculos posteriores.

Antes de elaborar el procedimiento operativo idóneo y de calcular la precisión de las variables determinadas, es necesario calibrar los diferentes equipos que las miden. Se realizó el calibrado de los dos medidores de presión. Una empresa externa calibró el sensor de temperatura.

La propiedad que determinan los equipos basados en el método del tubo vibrante es el periodo de vibración del tubo,  $\tau$ , función de la densidad del fluido confinado en él. Por ello es necesario calibrar la célula de medida en todo el rango de temperaturas y de presiones usando un fluido de referencia; en nuestro caso,  $\text{CO}_2$ .

Se verificó el calibrado y procedimiento operacional determinando la densidad de etano y propano y comparando los valores obtenidos con los calculados a partir de sus correspondientes EoS de referencia.

Debido al elevado número de puntos experimentales  $P - \rho - T$  que se obtienen en esta instalación, es posible calcular diferentes propiedades derivadas de la densidad tales como: compresibilidad isotérmica,  $\kappa_T$ , expansividad isóbara,  $\alpha_p$ , presión interna,  $\pi_i$ , y

coeficiente de temperatura,  $(\partial\pi_i/\partial T)$ . Se obtuvieron los valores de estas propiedades para CO<sub>2</sub> y etano así como su precisión.

Se elaboró el procedimiento experimental para mezclas binarias realizando las modificaciones necesarias con respecto al procedimiento para compuestos puros.

La consecución del objetivo 1 se recoge en el Artículo: *J. of Physical Chemistry B*, 2011, 115, 8216.

## OBJETIVO 2

**Calibrado y puesta a punto de una instalación para la medida de velocidades del sonido, en un amplio rango de presión y temperatura, para fluidos puros y mezclas.**

El método de medida de esta instalación está basado en la relación existente entre la longitud que recorren los ecos de un pulso ultrasónico y el desfase que se produce entre ellos. Para determinar dicha longitud es necesario realizar el calibrado a una presión y temperatura utilizando un fluido de referencia con una EoS precisa. En este caso, se utilizó agua MiliQ desgasificada a  $T = 298.12$  K y  $P = 1.00$  MPa. Dado que las calibraciones de los medidores de presión y temperatura estaban vigentes, no fue necesario recalibrarlos.

Se verificó la calibración y se determinó la precisión en la medida de velocidades del sonido de líquidos puros mediante la comparación de los valores experimentales obtenidos para el agua en un amplio rango de  $P$  y  $T$  con los proporcionados por la EoS.

Debido a que la instalación estaba diseñada únicamente para la medida de la velocidad del sonido en líquidos, hubo que modificarla para trabajar con gases comprimidos y comprobar su precisión en esas condiciones. Para ello, se determinó  $c$  en etano a ocho temperaturas y a presiones hasta 175 MPa y se compararon los datos con los proporcionados por la EoS de referencia de este compuesto.

A partir de los datos experimentales ( $P - \rho - T$  y  $P - c - T$ ) obtenidos para etano se calculó la compresibilidad isentrópica,  $\kappa_S$ , y la capacidad calorífica a presión constante,  $C_p$ . Su precisión se calculó, asimismo, por comparación con los valores proporcionados por su EoS de referencia.

Se puso a punto la instalación de medida de velocidades del sonido para mezclas que contienen gases comprimidos suficientemente densos. Se estableció el procedimiento experimental para la preparación y medida de estas mezclas y se determinó la incertidumbre en los valores experimentales de velocidad del sonido del sistema gas

comprimido+líquido, CO<sub>2</sub>+CH<sub>3</sub>OH. Las composiciones de las mezclas y las condiciones de trabajo se eligieron para que incluyeran las habituales de la tecnología CCS.

La consecución del objetivo 2 se recoge en los Artículos: *J. of Physical Chemistry B*, 2011, 115, 8216, y *J. of Chemical Thermodynamics*, 2016, 98, 272-281.

### OBJETIVO 3

**Estudio experimental de los sistemas CO<sub>2</sub>+CH<sub>4</sub> y CO<sub>2</sub>+CO. Cálculo de incertidumbres. Determinación de propiedades derivadas y de sus precisiones.**

Se determinó la densidad de los sistemas: CO<sub>2</sub>+CH<sub>4</sub> (6 composiciones; 9 temperaturas) y CO<sub>2</sub>+CO (5 composiciones; 10 temperaturas) a presiones desde 0.1 a 20 MPa. Se calculó, mediante la Ley de Propagación de Errores, la incertidumbre expandida en la determinación de la densidad,  $U(\rho)$ .

A partir de los datos experimentales ( $P - \rho - T - x_{CO_2}$ ) se calcularon las siguientes propiedades y sus respectivas incertidumbres: puntos de rocío y de burbuja, y densidades de las fases en equilibrio, ( $P_r - \rho_V; P_b - \rho_L$ ); compresibilidad isotérmica,  $\kappa_T$ ; expansividad isóbara,  $\alpha_P$ ; presión interna,  $\pi_i$ ; volúmenes molares de exceso,  $V_m^E$ ; y volúmenes parciales molares,  $\bar{V}_2$ .

Por último, se realizó una búsqueda bibliográfica de todas las propiedades, experimentales y calculadas, y se compararon con los datos obtenidos en este trabajo.

La consecución del objetivo 3 se recoge en los artículos: *Environmental Science & Technology*. 2012, 46, 13016; *International Journal of Greenhouse Gas Control*. 2013, 264; y *Environmental Science & Technology*. 2014, 48, 10984.

### OBJETIVO 4

**Modelización de los sistemas CO<sub>2</sub>+CH<sub>4</sub> y CO<sub>2</sub>+CO mediante Ecuaciones de Estado cúbicas (PR) y no cúbicas (PC-SAFT, GERG-2008).**

Se modelizaron los sistemas CO<sub>2</sub>+CH<sub>4</sub> y CO<sub>2</sub>+CO con tres Ecuaciones de Estado: Peng-Robinson, de gran aplicabilidad en ingeniería por su simplicidad; GERG-2008, muy precisa pero compleja de implementar; y PC-SAFT, con características intermedias entre las anteriores. Se obtuvieron los parámetros de interacción binaria cuando fue necesario, y se calcularon las desviaciones medias relativas de todas las propiedades volumétricas y del equilibrio líquido vapor:

La consecución del artículo 4 se recoge en los artículos: *Environmental Science & Technology*. 2012, 46, 13016; *International Journal of Greenhouse Gas Control*. 2013, 264; y *Environmental Science & Technology*. 2014, 48, 10984.

## OBJETIVO 5

Estudio estructural de los sistemas  $\text{CO}_2+\text{CH}_4$  y  $\text{CO}_2+\text{CO}$  en la región crítica a partir de la determinación de sus propiedades volumétricas a dilución infinita.

Se determinó la naturaleza de las interacciones entre las moléculas de disolvente,  $\text{CO}_2$ , y las de soluto,  $\text{CH}_4$  o  $\text{CO}$ , a 304.21 y 308.15 K utilizando el concepto de Función de Krichevskii y de la inversión de la Teoría de Kirkwood-Buff. Para ello, se calculó el volumen molar parcial del soluto a dilución infinita,  $\bar{V}_2^\infty$ , el número de coordinación de exceso,  $N_{exc}^\infty$  y el tamaño del clúster,  $N_1^{exc}$ .

La consecución del objetivo 5 se recoge en el artículo: *International Journal of Greenhouse Gas Control*. 2013, 264.

## OBJETIVO 6

Estudio de la influencia de  $\text{CH}_4$  y  $\text{CO}$  en el transporte, inyección y almacenamiento del  $\text{CO}_2$  antropogénico en la tecnología CCS mediante el cálculo de parámetros característicos de dichos procesos a partir de las propiedades determinadas experimentalmente.

Se identificaron, mediante el estudio de la bibliografía existente, los parámetros característicos de las etapas de transporte, inyección y almacenamiento, así como los procedimientos de cálculo idóneos para cada uno. A partir de los datos ( $P - \rho - T x_{\text{CO}_2}$ ;  $P_r - P_b$ ) obtenidos en parte de las composiciones estudiadas y los de viscosidad calculados, se obtuvieron diferentes parámetros para las distintas etapas de la tecnología CCS.

- Transporte: Presión mínima de operación,  $P_{min}$ ; Perfil de presión a lo largo de la tubería,  $P(d)$ ; Distancia máxima de presurización,  $L$ ; Capacidad de las estaciones de represurización,  $W$ ; y Diámetro interno de la tubería,  $D$ .
- Inyección y almacenamiento: Parámetro de solubilidad,  $\delta$ ; Capacidad de almacenamiento normalizada,  $M/M_0$ ; Velocidad de ascenso normalizada en acuíferos salinos,  $v/v_0$ ; y Flujo de permeación normalizado,  $\dot{M}/\dot{M}_0$ .

La consecución del objetivo 6 se recoge en los artículos: *Environmental Science & Technology*. 2012, 46, 13016; *International Journal of Greenhouse Gas Control*. 2013, 264; y *Environmental Science & Technology*. 2014, 48, 10984.



**METODOLOGÍA**



## 4. METODOLOGÍA

### 4.1. INSTALACIONES Y PROCEDIMIENTOS

#### A) PROPIEDADES VOLUMÉTRICAS Y EQUILIBRIO LÍQUIDO VAPOR

##### A.1.) Instalación para la determinación de medidas experimentales.

###### i. Descripción de la instalación

En la Figura 4 se muestra un esquema de la instalación que se ha empleado para determinar los datos presión – densidad – temperatura,  $P - \rho - T$ , de fluidos puros y sus mezclas en las regiones subcrítica, crítica y supercrítica.

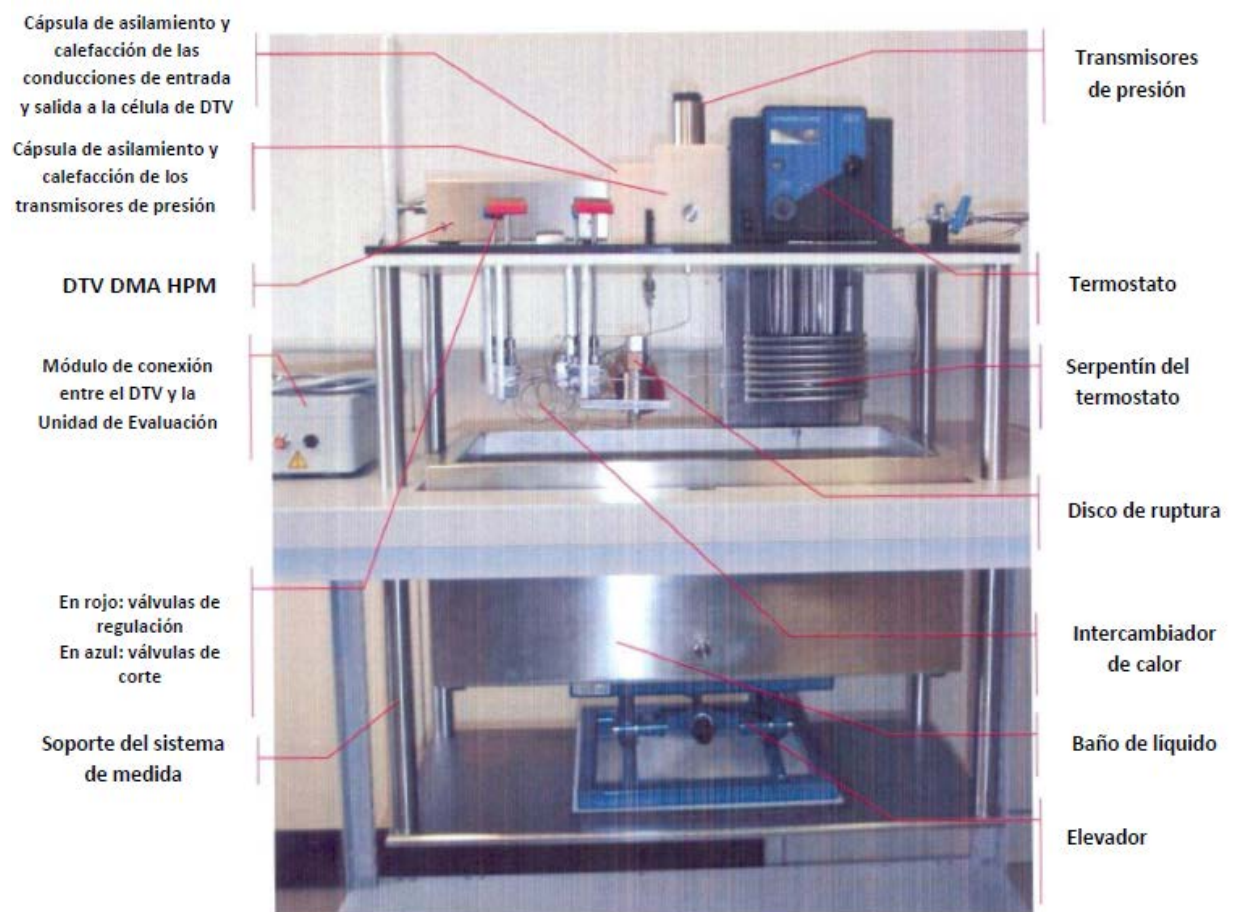


Figura 4. Instalación experimental para la determinación de datos  $P - \rho - T$  de fluidos puros y sus mezclas.

La instalación, que fue diseñada por ARMINES y el Laboratoire de Thermodynamique des Equilibres entre Phases de l'École Nationale Supérieure des Mines de Paris en Francia, permite obtener datos  $P - \rho - T$  de fluidos puros y mezclas en un rango de temperaturas desde 253 a 423 K y desde presión atmosférica hasta 70 MPa.

Su componente principal es una célula de Densimetría de Tubo Vibrante (DTV) AntonPaar KG, modelo DMA HPM, conectada a una unidad de evaluación mPDS 2000V3 que recoge datos de forma continua. La instalación se completa con las conducciones de entrada y de salida a la célula, diferentes módulos de regulación y corte y el sistema de termostatación. Este último consiste en un doble recubrimiento del densímetro de tubo vibrante que permite la regulación térmica mediante un baño externo (Fischer Bioblock, Cryo-polystat 71 modelo C85408). La temperatura del resto del circuito está regulada por otro baño (misma marca y modelo) en un valor ligeramente diferente que permite evitar que la primera burbuja de gas (medidas en fase condensada) o primera gota de líquido (medidas en fase gaseosa) se originen fuera de la célula de medida.

La presión se mide mediante dos transductores de presión regulados térmicamente (GE Infraestructura modelo PTX 611); uno de ellos se utiliza para presiones hasta 6 MPa y el otro hasta 70 MPa.

## ii. Procedimiento y calibración

El procedimiento experimental comienza con la limpieza de la instalación que consiste en hacer circular una corriente de nitrógeno a 0.2-0.3 MPa durante dos horas a lo largo de toda la instalación y después hacer vacío durante 4 horas. El fluido a estudiar se introduce mediante una célula de carga de volumen variable (Figuras 5(a) y 5(b)) fabricada en Hastelloy que se conecta a una bomba manual de alta presión que permite alcanzar presiones de hasta 100 MPa. El paso del fluido desde la célula a la bomba se lleva a cabo por compresión con He. Cuando el fluido es una mezcla, ésta se prepara en la célula de carga por diferencia de pesada introduciendo los fluidos en orden de menor a mayor presión de vapor. Para ello se emplea un comparador de masas (Sartorius, modelo CCE2004) que tiene una capacidad máxima de pesada de 2500 g, cuya legibilidad es de 0.0001 g y la repetibilidad es de 0.0002 g.

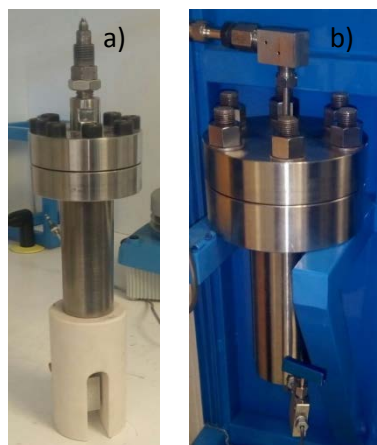


Figura 5. Células de volumen variable (a) Pequeña (0.05 l) y (b) Grande ( 0.51 l) .



Cuando se determinan densidades en condiciones críticas o supercríticas, donde no hay cambio de fase, la medida del periodo de vibración es descendente, partiendo de la presión máxima de medida y adquiriendo datos en todo el rango de presión para una temperatura dada hasta alcanzar la presión atmosférica. Dado que a la temperatura crítica de un fluido (o en su cercanía), pequeñas variaciones de presión suponen grandes cambios en la densidad, se realizaron pruebas en diferentes condiciones para optimizar la medida de estas isotermas.

Si a la temperatura de trabajo el fluido presenta cambio de fase, isotermas subcríticas, las medidas de densidad se realizan en dos tramos: uno ascendente en el que las medidas se toman desde presión de vacío hasta la presión de vapor (en el caso de los fluidos puros) o hasta la presión de rocío (en mezclas); y otro descendente, en el que se parte desde la presión máxima de medida para cada isoterma hasta la presión de vapor (en el caso de fluidos puros) o hasta la presión de burbuja (para el caso de las mezclas).

La adquisición de medidas  $P - \tau - T$  a una temperatura dada puede llegar hasta los 5000 puntos. Este es un número demasiado elevado para su posterior tratamiento, por ello es necesario descartar parte de estos puntos de forma que las isotermas son reducidas a un número alrededor de 1500.

Los límites del ELV a una temperatura determinada (presión de vapor de compuestos puros y presiones de rocío y de burbuja en mezclas), se determinan gráficamente, mediante el método de las tangentes (Figura 6). En este método las medidas precedentes y posteriores a los puntos del límite del ELV se ajustan mediante dos ecuaciones lineales; el punto de cruce de ambas corresponde a los puntos de rocío o de burbuja, según la medida corresponda a la fase vapor o a la líquida respectivamente.

En todos los casos, para asegurar el equilibrio a través de transformaciones cuasi-estáticas, los flujos de fluido se ajustan convenientemente hasta una velocidad óptima de  $0.005 \text{ MPas}^{-1}$ .

Presión /MPa

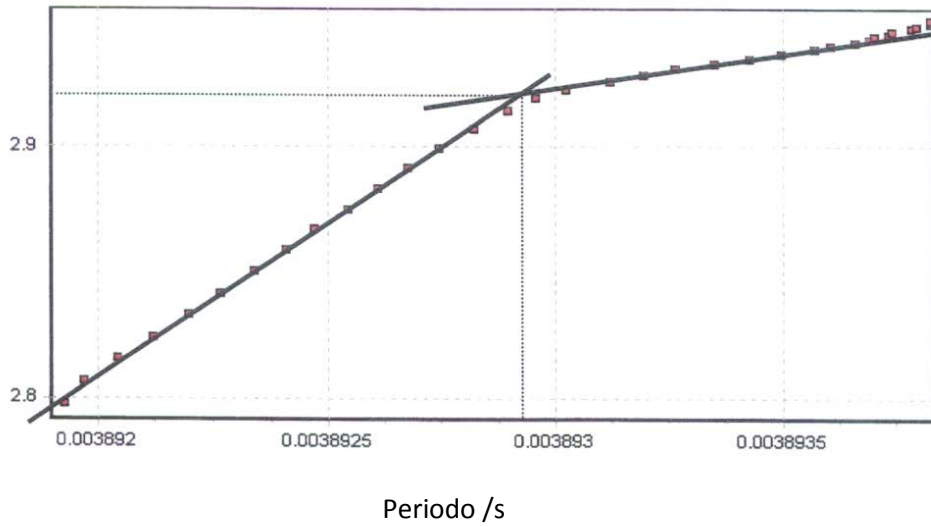


Figura 6. Determinación del punto de rocío de un fluido por el método de las tangentes.

El principio de medida de los densímetros de tubo vibrante se basa en la dependencia del periodo de oscilación del tubo en U situado en su interior con la masa conjunta del propio tubo y del fluido que circula por él. El comportamiento del tubo vibrante puede ser modelado como un sistema de amortiguador masa-resorte.<sup>48</sup>

El periodo de oscilación o vibración,  $\tau(s)$ , viene dado por la siguiente expresión:

$$\tau(s) = 2\pi \sqrt{\frac{M_0 + V\rho}{D}} \quad (\text{Ec. 1})$$

Donde

- $M_0$  masa del tubo en U vacío (kg)
- $V$  volumen del tubo vibrante ( $\text{m}^3$ )
- $\rho$  densidad del fluido que circula por el interior del tubo en U ( $\text{kg}\cdot\text{m}^{-3}$ )
- $D$  constante de muelle (N/m)

A partir de la ecuación anterior, sustituyendo la constante mecánica, se llega a la ecuación clásica para densímetros de tubo vibrante:

$$\rho = A\tau^2 - B \quad (\text{Ec. 2})$$

Los parámetros A y B pueden obtenerse mediante un calibrado utilizando fluidos de densidad conocida y midiendo el periodo de oscilación provocado por ellos. Sin embargo, en este trabajo hemos preferido utilizar como modelo de calibrado el desarrollado por Bouchot y Richon<sup>12</sup> Path Mechanical Calibration Model, FPMC; el objetivo del mismo es limitar la influencia del método de calibrado en la determinación de la densidad a partir de las medidas del periodo de vibración. El modelo busca relaciones para las dependencias de la presión y la temperatura que tengan consideraciones realistas, de forma que representen el comportamiento del material del tubo vibrante ante la deformación y la tensión.

Así, la ecuación que relaciona la densidad del fluido en unas condiciones dadas,  $\rho(T, P)$ , con el periodo de oscilación del tubo vibrante,  $\tau$ , es:

$$\rho(T, P) = \frac{M_0}{L_{00}} \cdot \left[ \frac{1}{\pi r_i^2} \exp\left(\int \alpha(T) dT + \gamma_T P\right) \right] \left[ \left( \frac{\Delta r^4}{\Delta r_0^4} \right) \exp(-3\gamma_T P) \left( \frac{\tau^2}{\tau_0^2} \right) - 1 \right] \quad (\text{Ec. 3})$$

Donde

$T$	Temperatura en el interior del tubo vibrante
$P$	Presión en el interior del tubo vibrante
$M_0$	Masa en el vacío del tubo vibrante
$L_{00}$	Longitud del tubo vibrante en el vacío a 273.15 K
$\alpha(T)$	Coefficiente de dilatación lineal
$\gamma_T$	Coefficiente de expansión del tubo vibrante a la temperatura $T$
$r_i$	Radio interno del tubo vibrante a la temperatura $T$ y la presión $P$
$\Delta r$	Diferencia entre el radio interno y el externo del tubo vibrante a la temperatura $T$ y la presión $P$
$\Delta r_0$	Diferencia entre el radio interno y el externo del tubo vibrante a la temperatura $T$ y a vacío
$\tau$	Periodo de vibración del tubo vibrante a la temperatura $T$ y la presión $P$
$\tau_0$	Periodo de vibración del tubo vibrante a la temperatura $T$ en el vacío

En el modelo FPMC, se usa un único fluido de referencia para obtener los valores de las constantes  $M_0/L_{00}$  y  $\gamma_T$ .

Se eligió el CO<sub>2</sub> como fluido de calibración por poder adquirirse con elevada pureza (99.998% molar), por presentar valores de densidad similares a los fluidos estudiados en esta Tesis y disponer de una EoS precisa que permite calcular valores de densidad de referencia en todo el rango de medida. La EoS utilizada fue la de Span y Wagner<sup>89</sup> que tiene un rango de aplicabilidad de hasta 800 MPa y 1000 K y con una incertidumbre

estimada en el cálculo de la densidad de  $u(\rho) = \pm 0.03\% - \pm 0.05\%$ . La calibración se llevó a cabo a once temperaturas (253.15, 273.15, 293.15,  $T_c(\text{CO}_2) = 304.21$ , 308.15, 313.15, 333.15, 353.15, 373.15, 393.15 y 423.15K) y desde presión atmosférica hasta 70 MPa, estudiando así tres estados del fluido: subcrítico, crítico y supercrítico.

Las desviaciones medias relativas (Anexo I Ecuación A.I) al comparar las densidades experimentales obtenidas en el calibrado y las calculadas con la EoS<sup>89</sup> fueron:  $MRD(\rho) = 0.09\%$  si se incluyen las medidas en la región crítica y  $MRD(\rho) = 0.07\%$  si se excluye esta región.

Los transductores fueron calibrados en los laboratorios de nuestro grupo de investigación utilizando un calibrador Wika CPH 6000 con una precisión de 0.025% en toda la escala. Las precisiones expresadas como incertidumbres para los medidores son  $u(P) = \pm 0.015$  MPa para el medidor de hasta 6 MPa y  $u(P) = \pm 0.0175$  MPa para el medidor de 6 hasta 70 MPa.

Las sondas de temperatura fueron calibradas por el Centro Español de Metrología, CEM, siguiendo el procedimiento CEM-PT-4.2-40. La incertidumbre en su medida es  $u(T) = \pm 0.006$ K.

### iii. Precisión

#### Compuestos puros

Con el objetivo de calcular la **precisión** de la instalación en la medida de densidades de compuestos puros se realizaron medidas de densidad de etano (99.995% molar) a nueve temperaturas, incluyendo la temperatura crítica del etano, en el rango desde 253.15 hasta 423.15 K y desde presión atmosférica hasta 70 MPa. Las ecuaciones de referencia utilizadas fueron la de Buecker y Wagner<sup>13</sup> para la región desde 0.1 a 30 MPa y la de Friend et al.<sup>31</sup> para presiones desde 30 hasta 70 MPa. En la Figura 7 se muestran las desviaciones obtenidas en la densidad para el etano con respecto a las EoS de referencia empleadas. El valor promedio de  $MRD(\rho)$  para el etano en el rango de temperaturas estudiado es de 0.13%.

Para comprobar la calidad de las medidas en las regiones con mayor dificultad experimental (cercanías del punto crítico), se realizaron medidas  $P - \rho - T$  para el propano (99.95 % molar) a las temperaturas:  $T = T_c(\text{C}_3\text{H}_8) = 369.82$ , 373.15, 393.15 y 423.15K y desde presión atmosférica hasta 20 MPa. Se compararon los datos obtenidos con los que proporciona la EoS de referencia de este compuesto<sup>58</sup> obteniéndose un valor promedio:  $MRD(\rho) = 0.20\%$ .

Con el objetivo de determinar la **repetibilidad** en la medida de la densidad, se midió la densidad del dióxido de carbono a 273.15, 304.21 y 353.15 K desde presión atmosférica

hasta 70 MPa. Cada isoterma se midió tres veces y se calculó la desviación estándar relativa (Anexo I, Ecuación A.II):  $\bar{S}_\rho^r = 0.05\%$  y  $\bar{S}_p^r = 0.3\%$ . El último valor corresponde a la repetibilidad en la región crítica extendida que comprende:  $0.6 \rho_C < \rho < 1.4 \rho_C$ ;  $0.98 T_C < T < 1.2 T_C$ .

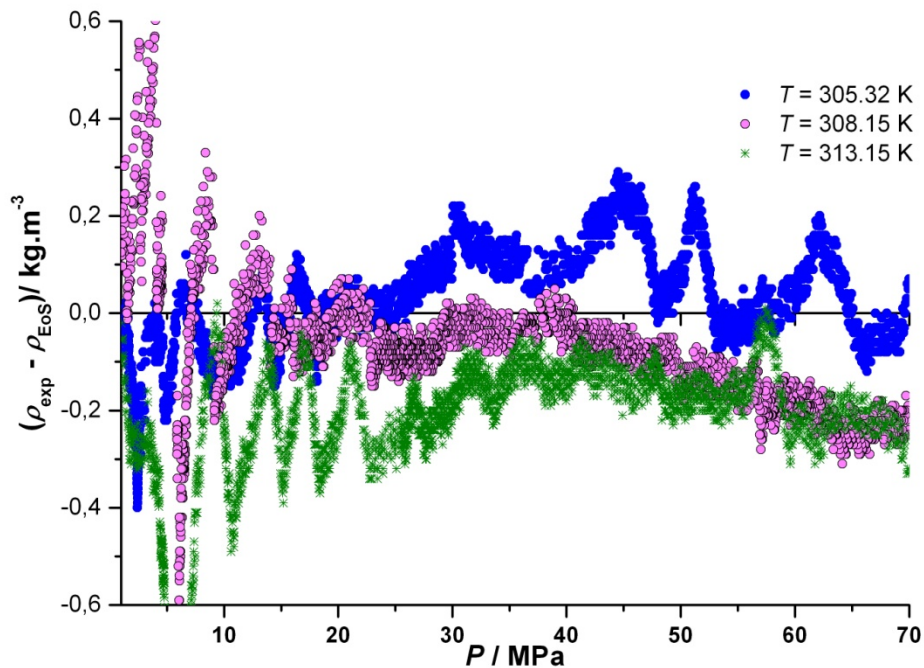


Figura 7. Desviaciones absolutas entre datos experimentales de densidad para etano a distintas temperaturas y las de referencia a partir de las EoS de Buecker y Wagner<sup>13</sup> y de Friend et al.<sup>31</sup>

### Mezclas

Para desarrollar un método óptimo de determinación de densidades de mezclas binarias y evaluar la precisión de las mismas, se estudiaron a  $T = 308.15$  K dos mezclas de  $\text{CO}_2 + \text{C}_2\text{H}_6$  de diferente composición y en distinto rango de presión, comprobando así la influencia de dichas variables sobre la precisión. Cada una de las isothermas se midió dos veces para determinar la repetibilidad expresada como desviación estándar relativa (Anexo I Ecuación A.II). Las mezclas estudiadas fueron  $x_{\text{CO}_2} = 0.4999$  hasta 20 MPa y  $x_{\text{CO}_2} = 0.9540$  hasta 70 MPa y los valores encontrados fueron  $\bar{S}_\rho^r = 0.13\%$  y  $0.06\%$ , respectivamente.

## A.2.) Cálculo de propiedades derivadas

A partir de los datos  $P - \rho - T$  obtenidos experimentalmente para  $\text{CO}_2$  y  $\text{C}_2\text{H}_6$ , se ha evaluado el efecto de la presión y la temperatura en su densidad a través de la compresibilidad isotérmica,  $\kappa_T$ , y la expansividad térmica isobárica,  $\alpha_P$ . Además, se ha calculado la presión interna,  $\pi_i$ , propiedad relacionada con el orden molecular en el fluido. Las ecuaciones usadas han sido:

$$\kappa_T = \left(\frac{1}{\rho}\right) \left(\frac{\partial \rho}{\partial P}\right)_T \quad (\text{Ec. 4})$$

$$\alpha_P = - \left(\frac{1}{\rho}\right) \left(\frac{\partial \rho}{\partial T}\right)_P \quad (\text{Ec. 5})$$

$$\pi_i = \left(\frac{\partial U}{\partial V}\right)_T = T \left(\frac{\partial P}{\partial T}\right)_V - P = T \left(\frac{\alpha_P}{\kappa_T}\right) - P \quad (\text{Ec. 6})$$

Los valores calculados se han comparado con los proporcionados por las respectivas EoS<sup>13,31,50</sup> obteniendo las siguientes desviaciones medias relativas (Anexo I Ecuación A.1):

$$MRD_{\text{CO}_2} (\kappa_T) < 1.2 \% ; \quad MRD_{\text{CO}_2} (\alpha_P) < 5.0 \% ; \quad MRD_{\text{CO}_2} (\pi_i) < 7.0 \%$$

$$MRD_{\text{C}_2\text{H}_6} (\kappa_T) < 1.2 \% ; \quad MRD_{\text{C}_2\text{H}_6} (\alpha_P) < 7.4 \% ; \quad MRD_{\text{C}_2\text{H}_6} (\pi_i) < 8.0 \%$$

La dependencia de  $\kappa_T$  y  $\alpha_P$  para el  $\text{CO}_2$  y el etano respecto a la temperatura y la presión es bastante similar (Figuras 8 y 9). En el punto crítico, la altísima sensibilidad de la densidad con pequeñas variaciones de presión o temperatura hace que  $\kappa_T, \alpha_P \rightarrow \infty$ <sup>94</sup> y supone que los valores de ambas propiedades en esa región sean similares a los de la fase líquida. Por otro lado, se puede apreciar que la presión interna en el dióxido de carbono es mucho mayor que la del etano (Figura 10). Esto se puede explicar por la existencia de un momento cuadrupolar importante derivado de la deficiencia electrónica en la molécula de  $\text{CO}_2$ .

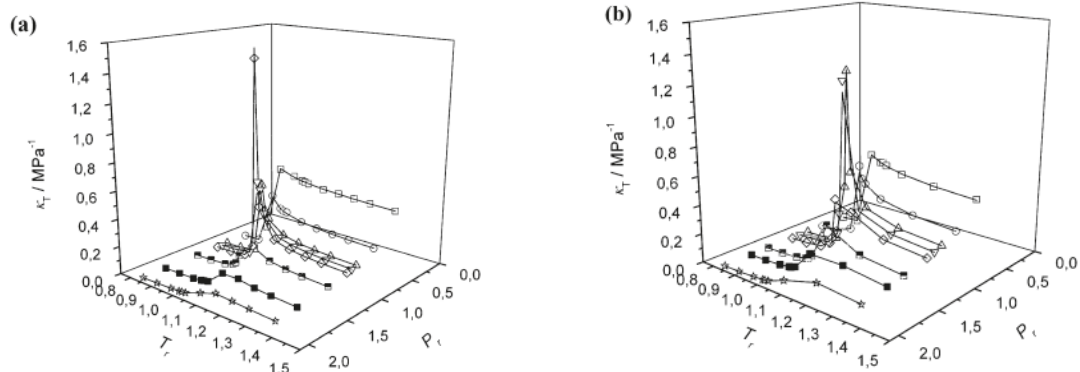


Figura 8. Representación de  $P_r - \kappa_T - T_r$  para (a) dióxido de carbono (b) etano; (símbolos) valores experimentales y (líneas) EoS.

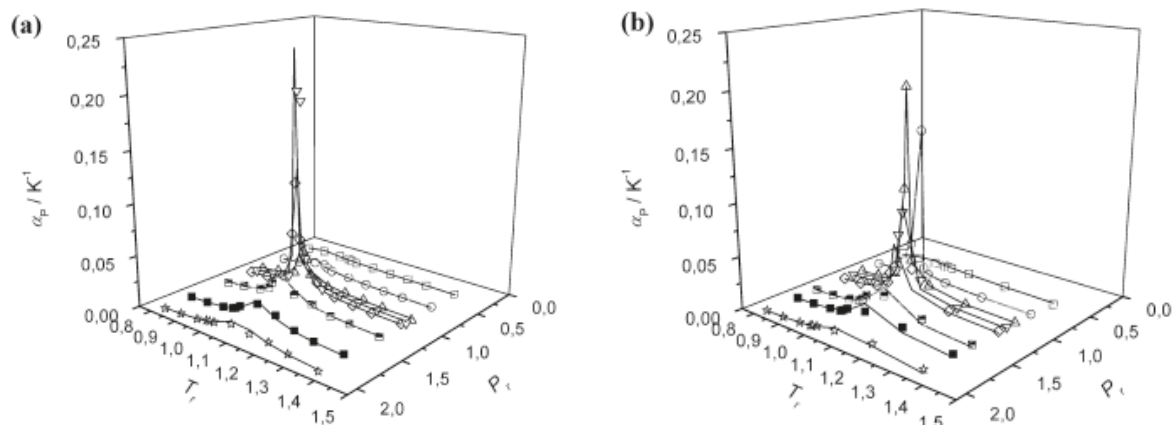


Figura 9. Representación de  $P_r - \alpha_P - T_r$  para (a) dióxido de carbono y (b) etano; (símbolos) valores experimentales y EoS (líneas).

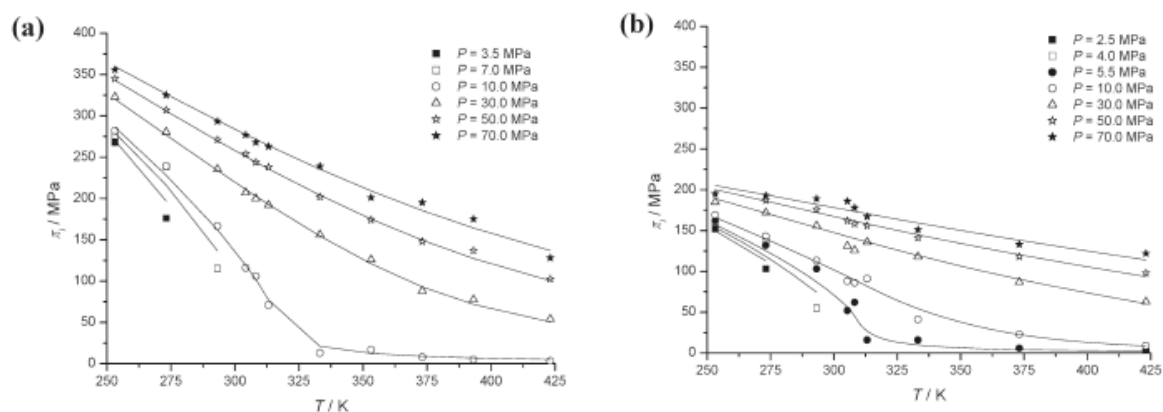


Figura 10. Representación de la presión interna,  $\pi_i$ , frente a la temperatura,  $T$ , para (a) dióxido de carbono ( $P_c = 7.383$  MPa y  $T_c = 304.21$  K) y (b) etano ( $P_c = 4.882$  MPa y  $T_c = 305.32$  K); valores experimentales (símbolos) y EoS (líneas).

## B) VELOCIDAD DEL SONIDO

### B.1.) Instalación para la determinación de medidas experimentales

#### i. Descripción de la instalación

La instalación experimental para la determinación de velocidades del sonido,  $c$ , se muestra en la Figura 11. Esta instalación, fabricada en el Imperial College de Londres, se basa en el método descrito en la bibliografía<sup>8,19</sup> que emplea un sistema de pulso ultrasónico de 5 MHz para obtener medidas de velocidades del sonido en líquidos. Sus componentes principales son: (1) bomba de presión manual, (2) entrada de fluido, (3) bomba de recirculación, (4) transductor de presión, (5) célula de presión, (6) baño de líquidos para la regulación de temperatura, (7) osciloscopio, (8) sonda de temperatura de platino, (9) línea de venteo, (10) unidad de evaluación y adquisición de datos y (11) línea de limpieza y vacío.

La instalación experimental permite la determinación de  $c$  en un amplio rango de temperaturas y presiones:  $T = 253.15 - 473.15$  K y  $P = 0.1 - 200$  MPa:

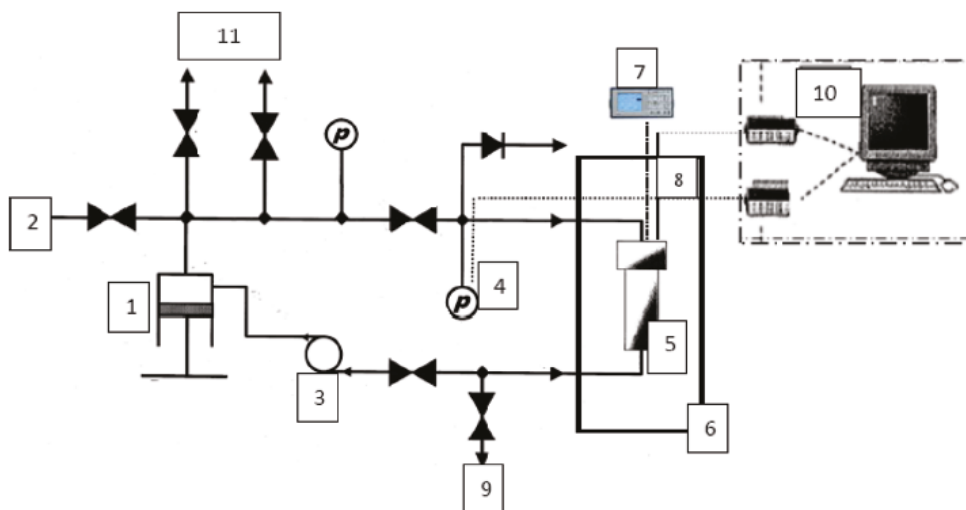


Figura 11. Esquema de la instalación experimental para la determinación de velocidades del sonido.

La célula de ultrasonidos se muestra en la Figura 12a). Sus principales elementos son: dos reflectores (2) y un transductor piezoeléctrico (5) fijado por medio de dos discos (4) usados como contactos eléctricos (6). La célula está introducida en una celda para altas presiones fabricada con una aleación de níquel y cromo, Nimonic80 A, que permite trabajar hasta 200 MPa (Figura 12b)). La celda tiene  $50 \text{ cm}^3$  de volumen interno, una conexión de entrada para introducir el fluido de medida y el cable del transductor, y una



de salida. La resistencia de platino del termómetro se introduce por un orificio de la celda en la parte superior.

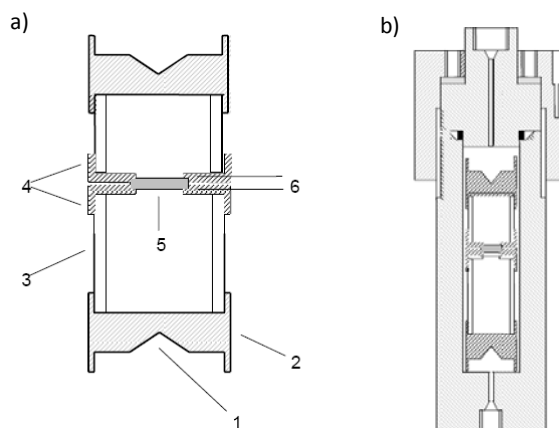


Figura 12. a) La célula de ultrasonidos, cavidad cónica (1), reflector (2), tubo de cuarzo (3), anillos de fijación de acero inoxidable (4), transductor piezoeléctrico (5), cables eléctricos (6). b) Celda para altas presiones.

Para presurizar el fluido de medida se utiliza una bomba manual de jeringa de 12 cm<sup>3</sup> de capacidad. La presión se mide con un transductor de presión de la marca Paroscientific con una incertidumbre  $u(P) = 0.02$  MPa.

La instalación está diseñada para trabajar con líquidos aunque también pueden utilizarse gases comprimidos siempre y cuando su densidad sea lo suficientemente alta. En este caso, los gases son introducidos con una bomba ISCO que se conecta a la entrada de la instalación; el gas, se comprime en la bomba ISCO y una vez licuado se transvasa a la bomba manual de la instalación. De esta manera es posible introducir la masa de fluido necesaria para alcanzar 200 MPa.

La celda de alta presión, con la celda de ultrasonidos en su interior, está inmersa en un baño termostatizado de unos 6.5 l de capacidad (FLUKE modelo 6020). Para temperaturas de trabajo inferiores a 293.15 K se utiliza un baño adicional (GRANT modelo GR150) que se regula a una temperatura de 20 K por debajo del baño principal. El fluido del baño es un aceite de silicona que puede ser utilizado en el rango completo de temperatura. La temperatura se mide con un termómetro calibrado por comparación con una resistencia estándar de platino previamente calibrada por el UK National Physics Laboratory. La incertidumbre en la medida de la temperatura,  $u(T)$ , es 0.015 K.

## ii. Procedimiento y calibración

El transductor piezoeléctrico de la célula de ultrasonidos es excitado con un tono de cinco ciclos generado a 5 MHz con una amplitud de 20 V entre picos. Esto provoca que el transductor emita pulsos acústicos simultáneamente en direcciones opuestas. La señal

que atraviesa el transductor se digitaliza mediante un osciloscopio digital. En la Figura 13a) se puede ver la señal de excitación del generador y otros dos tonos más pequeños que se corresponden con los primeros ecos provenientes de cada reflector.

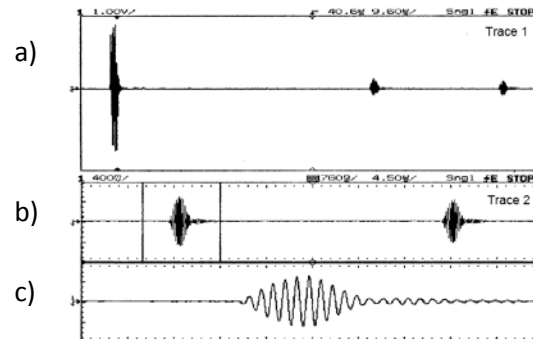


Figura 13. a) Pulso de excitación y ecos de respuesta emitidos; b) ampliación de los ecos; c) ampliación del primer eco.

En la Figura 13b) se muestran con más detalle los dos ecos donde se puede ver que su forma es prácticamente la misma. Si el tiempo en el que aparece un pico determinado de la señal del primer eco es  $t_1$  (se puede elegir el primer pico o el más alto), el tiempo en el que aparece el mismo pico en el segundo eco es  $t_2$  y la distancia entre los picos de los ecos es  $\Delta L$ , la velocidad del sonido,  $c$ , se obtiene como:

$$c = 2\Delta L/\Delta t \quad (\text{Ec.7})$$

Donde  $\Delta t = (t_2 - t_1)$ . La ventaja de este método es que al utilizar la diferencia entre los tiempos correspondientes a los dos ecos, los errores debidos a la difracción o a retrasos en la señal electrónica se reducen e incluso se eliminan.

La distancia  $\Delta L$  se determina mediante la calibración con un fluido dado a  $P_0$  y  $T_0$ . La variación de  $\Delta L$  con la temperatura,  $T$ , y la presión,  $P$ , se calcula mediante la siguiente ecuación:

$$\Delta L(T, P) = \Delta L(T_0, P_0) \left\{ 1 + \alpha(T - T_0) - \frac{1}{3} \kappa_T (P - P_0) \right\} \quad (\text{Ec.8})$$

Donde

- $\alpha$  es la dilatación térmica del cuarzo, que se asume independiente de  $T$  y de  $P$
- $\kappa_T$  es la compresibilidad isotérmica media del cuarzo a presiones entre  $P_0$  y  $P$ , que se calcula con la siguiente ecuación:

$$\kappa_T/\text{MPa}^{-1} = \{107820 + 36(T/\text{K} - 273.15) - 17.1 P/\text{MPa}\} \quad (\text{Ec.9})$$

El término de la compresibilidad isotérmica supone el 0.18% del valor de  $\Delta L$ , a 200 MPa y 423.15 K, mientras que el de la dilatación térmica no supera el 0.01% en el rango de temperatura estudiado.

La instalación experimental se calibró con agua desionizada (Milli Q) y desgasificada a 298.12 K y 1 MPa. Se determinó el desfase en el tiempo que tienen los dos ecos producidos en el fluido de calibración por un pulso ultrasónico a 5MHz, que fue de 13.245  $\mu$ s. Bajo estas condiciones de presión y de temperatura, el valor de la velocidad del sonido según la EoS IAPWS-95<sup>101</sup> es 1498.13  $\text{m s}^{-1}$ , de forma que el valor de la longitud de la celda calculado fue  $L_0=19.84 \times 10^{-3}$  m.

iii. Precisión en fluidos puros.

### Líquidos

Se midió la velocidad del sonido del agua desionizada en un rango de temperaturas desde 280.13 hasta 463.26 K a presiones comprendidas entre 1.0 y 190.0 MPa, obteniendo un valor de repetibilidad en la medida de  $c$  de  $\pm 0.02 \text{ ms}^{-1}$ .

Los valores experimentales obtenidos para el agua se compararon con los de la EoS de referencia de Wagner y Pruss<sup>101</sup>, que tiene una incertidumbre en la región líquida para  $c$  desde  $\pm 0.03$  a  $\pm 0.2\%$  y se calculó la  $MRD(c)$  siendo inferior a 0.06% para este fluido. Los valores obtenidos en este trabajo son similares a los de la literatura<sup>22,45,51,52,76,78,79,93,94,100</sup> determinados con sistemas de pulso ultrasónico que operan en la mayor parte de los casos hasta presiones más bajas que las alcanzadas en este trabajo.

### Fluidos comprimidos

Con el objetivo de verificar el adecuado funcionamiento de la instalación con gases comprimidos y obtener la precisión en la determinación de  $c$  para este tipo de sistemas, se midió  $c$  en etano puro ( $\geq 99.995$  % molar) en un rango de temperatura entre 273.19 y 423.21 K a presiones desde 3.93 hasta 170.0 MPa. Este rango de presiones cubre un amplio intervalo (entre 36.8 y 170.0 MPa) para el cual no existen valores de velocidades del sonido en la bibliografía.<sup>1,17,28,57,74,78,91,94</sup>

Se compararon los valores de  $c$  experimentales con los calculados con la EoS de referencia de Buecker y Wagner<sup>13</sup>. Las desviaciones encontradas fueron mayores que para el agua: 0.05% a  $T = 333.15$  K hasta 0.16% a  $T = 273.15$  K. La mayor desviación de las medidas con respecto a la EoS puede deberse al amplio rango de velocidades del sonido medido para este fluido (de 538.15 a 1774.91  $\text{ms}^{-1}$ ) en comparación con el rango de medida para el agua (de 1432.81 a 1845.40  $\text{ms}^{-1}$ ) y/o a la imprecisión de la EoS debido a la escasez de datos experimentales en la bibliografía. En las Figuras 14a) y b) se representan valores experimentales  $P - c - T$  para el agua y para el etano respectivamente, así como los valores calculados con las EoS de referencia<sup>13,101</sup>.

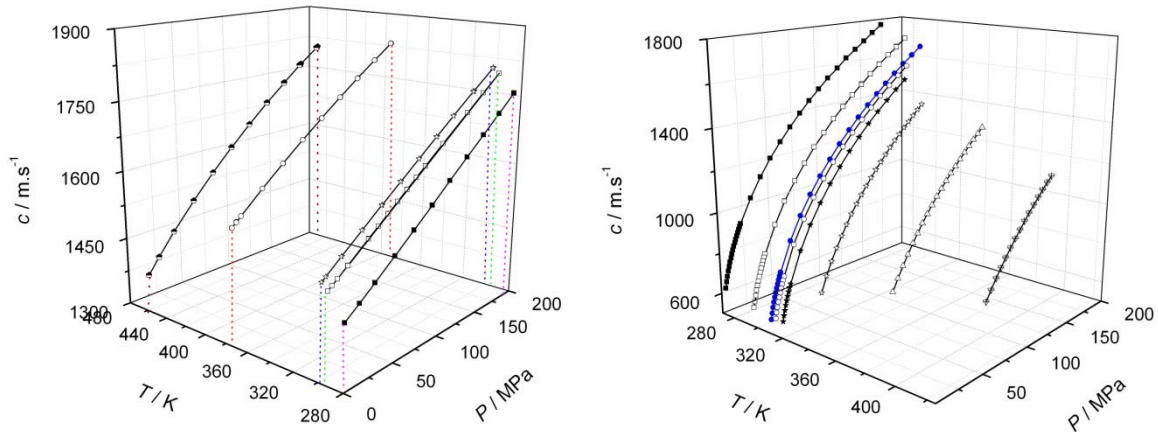


Figura 14. Representación  $P - c - T$  para (a) agua y (b) etano a varias presiones y temperaturas; valores experimentales (símbolos) y EoS (líneas). La isoterma crítica para el etano está representada por puntos azules.

- iv. Puesta a punto de la instalación para mezclas. Velocidad del sonido en el sistema  $\text{CO}_2 + \text{CH}_3\text{OH}$ .

La puesta a punto de la instalación para la medida de velocidades del sonido se llevó a cabo para mezclas gas comprimido + líquido. Se eligió el sistema  $\text{CO}_2 + \text{CH}_3\text{OH}$  porque el metanol puede estar presente en el  $\text{CO}_2$  antropogénico transportado y almacenado debido a su utilización para prevenir hidratos o como producto residual del proceso de secado del ceoducto. Se utilizaron  $\text{CO}_2$  y metanol de pureza del 99.998 y 99.93 % molar, respectivamente. Se estudiaron las mezclas de composición  $x_{\text{CO}_2} = 0.7534, 0.8502, 0.9250, 0.9700$  y  $0.9803$  a  $T = 263.15, 298.15$  y  $323.15$  K y presiones hasta 195 MPa. De la mezcla con  $x_{\text{CO}_2} = 0.9700$  se determinaron además las isothermas a  $273.15, 283.15, 293.15, 304.21$  y  $313.15$  K.

Las mezclas  $\text{CO}_2 + \text{metanol}$  se prepararon en una célula de volumen variable proporcionada por Top Industrie S.A.S., con un volumen máximo de 0.51 L y una presión máxima de 30 MPa (Figura 5.b). Después de introducir el metanol en la célula previamente evacuada, se inyectó el  $\text{CO}_2$  mediante una bomba de jeringa ISCO modelo 260D, que trabaja hasta 50 MPa. La mezcla se trasvasó a una bomba ISCO empujando el émbolo de la célula con un gas inerte y de ella a la bomba manual incluida en la instalación. La combinación de ambas bombas permitió cargar la masa suficiente para alcanzar la presión máxima de trabajo. La homogeneidad de la mezcla se aseguró mediante agitación tanto en la célula de volumen variable como en cada una de las bombas (ISCO, manual y de recirculación en el interior de la instalación).

Las masas de los distintos componentes se determinaron por pesadas sucesivas en un comparador de masas Sartorius modelo CCE 2004. La fracción molar del componente que se introduce en primer lugar,  $x_1$ , se determinó mediante la relación:

$$x_1 = \left[ \frac{(m_2 - m_1)}{M_1} \right] / \left[ \frac{(m_3 - m_2)}{M_2} + \frac{(m_2 - m_1)}{M_1} \right] \quad (\text{Ec.10})$$

Donde  $m_1$  es la masa del matraz o de la célula a vacío,  $m_2$  es la masa tras la introducción del primer componente,  $m_3$  tras la introducción del segundo componente,  $M_1$  es la masa molar del componente que se introduce en primer lugar y  $M_2$  la del que se introduce en segundo lugar. El cálculo de las incertidumbres se realizó a partir de la Ley de Propagación de errores.

Así, la incertidumbre estándar en la fracción molar,  $u_x$ , se calculó con la ecuación:

$$u_x^2 = [(\partial x/\partial m_1)u_m]^2 + [(\partial x/\partial m_2)u_m]^2 + [(\partial x/\partial m_3)u_m]^2 \quad (\text{Ec.11})$$

Donde  $u_m$  es la incertidumbre en la pesada, que fue tomada como  $\pm 2 \times 10^{-4}$  g. El valor obtenido para  $u_x$  fue de  $\pm 2 \cdot 10^{-6}$ .

La ecuación usada para el cálculo de la incertidumbre estándar de las medidas experimentales de  $c$ ,  $u_c$ , es:

$$u_c^2 = [(\partial c/\partial T)_P u_T]^2 + [(\partial c/\partial P)_T u_P]^2 + [(\partial c/\partial x)u_x]^2 + (u_c^*)^2 \quad (\text{Ec.12})$$

Donde  $u_P = 0.02$  MPa y  $u_T = 0.015$  K.

$u_c^*$  es la incertidumbre estándar de repetibilidad (Lin, 2014). Para determinar su valor, se prepararon dos mezclas de composición  $x_{\text{CO}_2} = 0.9250$ . Para cada una, se midieron dos isotermas a las siguientes temperaturas: 263.15, 298.15 y 323.15 K. Las desviaciones entre los valores de  $c$  a cada  $T$  para cada una de las mezclas se representan en la Figura 15. El valor determinado para  $u_c^*(c)$  fue  $5.3 \cdot 10^{-4} \cdot c$ .

Para obtener las contribuciones a la incertidumbre estándar debidas a las incertidumbres en la medida de la presión y de la temperatura se correlacionaron los valores experimentales de  $c$  mediante las siguientes ecuaciones:

$$(p - p^\#)/\text{MPa} = \sum_{i=1}^3 \sum_{j=0}^2 a_{ij} \{(c - c^\#)/(m \cdot s^{-1})\}^i (T/\text{K})^{-j} \quad (\text{Ec.13})$$

Donde  $c^\#$  es la velocidad del sonido a  $p = p^\#$ , la cual se correlaciona como función de la temperatura mediante la siguiente ecuación:

$$c^\#/(m \cdot s^{-1}) = \sum_{j=0}^2 b_j (T/\text{K})^j \quad (\text{Ec.14})$$

Para determinar la contribución en  $u_c$  de la incertidumbre en la composición se utilizaron las medidas de  $c$  de todas las mezclas  $\text{CO}_2 + \text{CH}_3\text{OH}$  obtenidas a 263.15, 298.15 y 323.15 K. Tanto esta contribución como las debidas a las incertidumbres en las medidas de  $P$  y  $T$ , respectivamente, resultan muy inferiores a  $u_c^*$ , por lo que la incertidumbre relativa estimada en la medida de  $c$  para el sistema  $\text{CO}_2 + \text{CH}_3\text{OH}$  fue  $u(c) = 5.9 \cdot 10^{-4} \cdot c$ . Este valor se encuentra dentro del rango de incertidumbres

estándar obtenido por otros autores utilizando un aparato similar tanto para mezclas líquidas como mezclas binarias de gases comprimidos<sup>8,19,64</sup>.

La Figura 16 muestra la evolución de  $c$  con la presión a las temperaturas de trabajo para la composición  $x_{\text{CO}_2} = 0.9700$  siendo el comportamiento el mismo para todas las composiciones:

$$\downarrow T, \uparrow P \Rightarrow c \uparrow$$

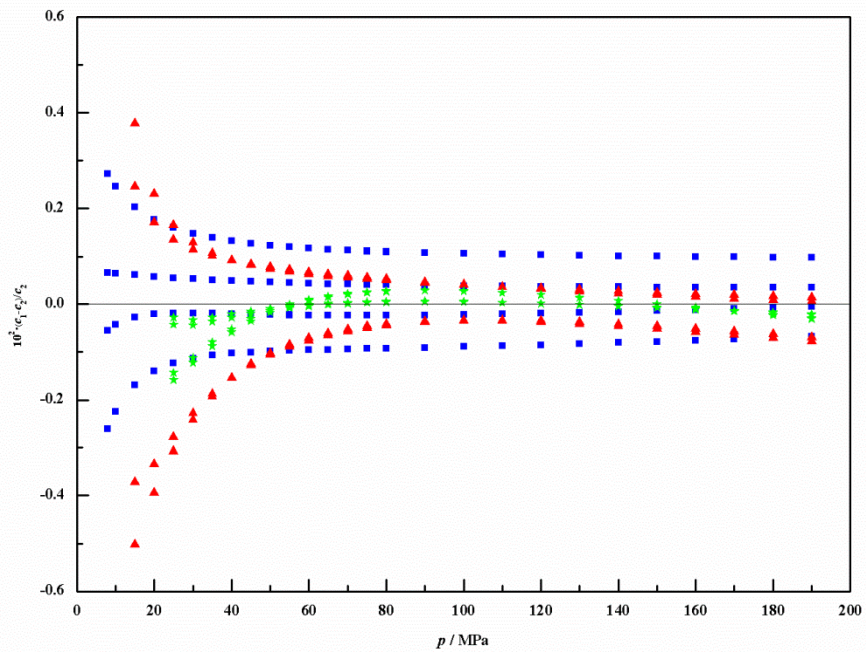


Figura 15. Desviaciones entre los valores de  $c$  para dos mezclas  $\text{CO}_2 + \text{CH}_3\text{OH}$  con  $x_{\text{CO}_2} = 0.9250$ , a tres temperaturas,  $T$ , frente a presión,  $P$ . Cada mezcla se midió dos veces a cada temperatura.  $\blacksquare$ ,  $T = 263.15 \text{ K}$ ;  $\blacktriangle$ ,  $T = 298.15 \text{ K}$ ;  $\star$ ,  $T = 323.15 \text{ K}$ .

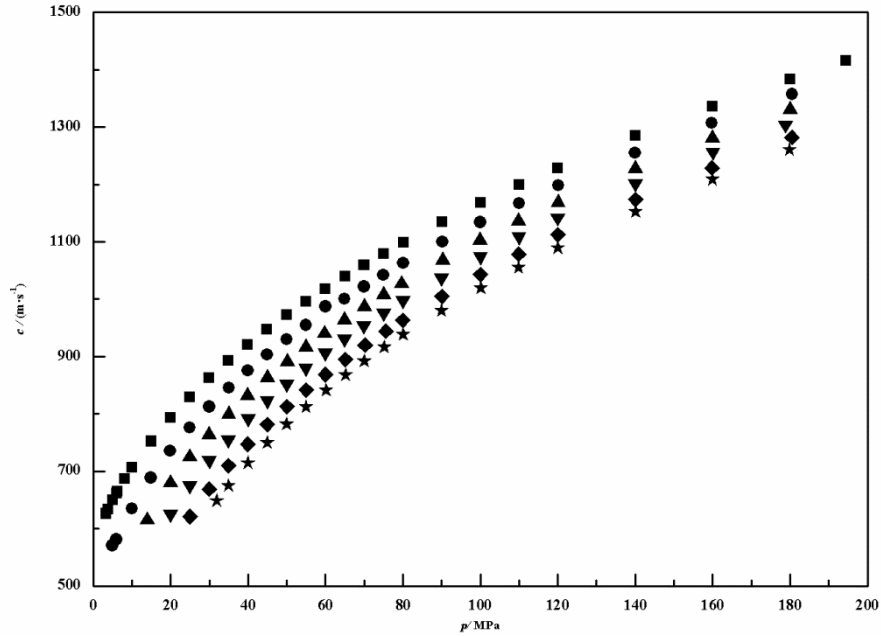


Figura 16. Velocidades del sonido experimentales,  $c$ , para la mezcla  $\text{CO}_2 + \text{CH}_3\text{OH}$  con  $x_{\text{CO}_2} = 0.9700$  a varias temperaturas,  $T$ : ■,  $T = 263.15 \text{ K}$ ; ●,  $T = 273.15 \text{ K}$ ; ▲,  $T = 283.15 \text{ K}$ ; ▼,  $T = 293.15 \text{ K}$ ; ◆,  $T = 304.21 \text{ K}$ ; ★,  $T = 313.15 \text{ K}$ .

## B.2.) Cálculo de propiedades derivadas

- Compresibilidad isentrópica,  $\kappa_S$ , y capacidad calorífica isobárica,  $C_P$ .

Con los valores de  $c$  y  $\rho$  determinados experimentalmente para el etano y los calculados  $\kappa_T$  y  $\alpha_P$  se han obtenido  $\kappa_S$  y  $C_P$  a partir de las siguientes ecuaciones:

$$\kappa_S = \frac{1}{\rho c^2} \quad (\text{Ec. 15})$$

$$C_P = \frac{\alpha^2 T}{\rho(\kappa_T - \kappa_S)} \quad (\text{Ec.16})$$

Los valores de estas propiedades se han comparado con los obtenidos con la EoS de referencia de Buecker<sup>13</sup>. Las desviaciones obtenidas fueron  $MRD(\kappa_S) = 0.19 \%$  y  $MRD(C_P) = 3 \%$ .

En la Figura 17 se representan los valores calculados de  $C_P$  junto con los predichos por la EoS.<sup>13</sup>

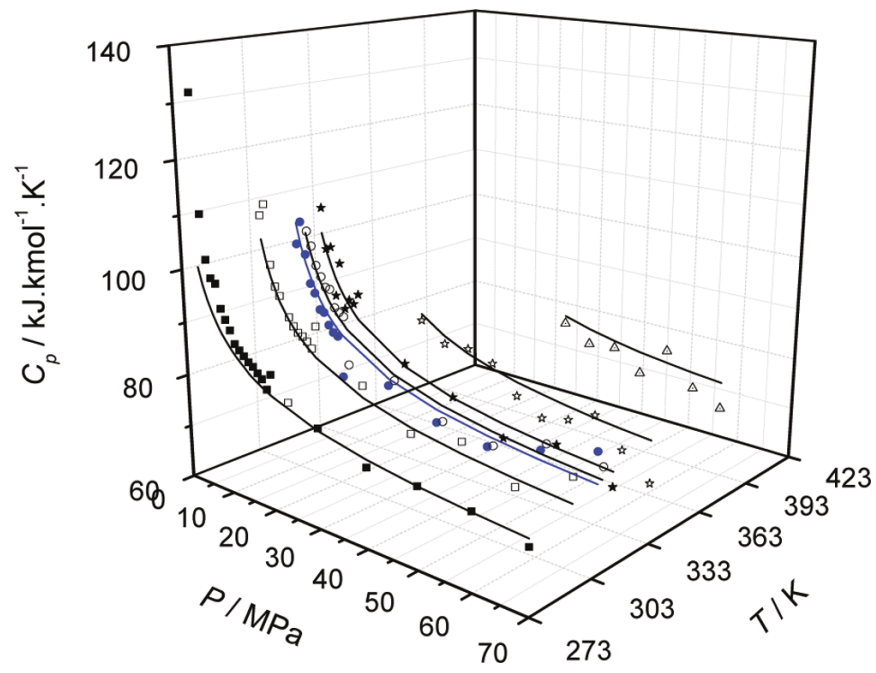


Figura 17. Representación  $P - C_p - T$  para el etano a varias presiones y temperaturas; valores calculados a partir de los  $c$  experimentales (símbolos) y EoS (líneas). La isoterma crítica para el etano está representada por puntos azules.



## 4.2. ESTUDIO DEL COMPORTAMIENTO VOLUMÉTRICO Y DEL ELV DE LAS MEZCLAS CO<sub>2</sub>+CH<sub>4</sub> Y CO<sub>2</sub>+CO RICAS EN CO<sub>2</sub>.

La determinación experimental de estas propiedades para los sistemas CO<sub>2</sub>+CH<sub>4</sub> y CO<sub>2</sub>+CO se ha realizado utilizando la instalación y el procedimiento experimental descritos en el apartado 4.1 de esta memoria.

Los valores experimentales del equilibrio de fase y de densidad, son necesarios para evaluar cuantitativamente la influencia de la presencia de CH<sub>4</sub> y CO en el CO<sub>2</sub> antropogénico y poder validar Ecuaciones de Estado que permitan predecir el comportamiento de estas mezclas en diferentes condiciones. Si bien en la literatura hemos encontrado datos experimentales  $P - \rho - T - x_{\text{CO}_2}$  y ELV para la mezcla CO<sub>2</sub>+CH<sub>4</sub><sup>21,67,102</sup>, las condiciones y composiciones de trabajo no son las de interés para la tecnología CCS. Para la mezcla CO<sub>2</sub>+CO los datos encontrados en la literatura son mucho más escasos, la mayor parte de los estudios se basan en modelos predictivos y no cubren los rangos de interés para la tecnología CCS.

Las impurezas que provienen de los gases de emisiones industriales condicionan la composición del fluido a almacenar, y por tanto deben tenerse en cuenta para el correcto diseño y operación de la tecnología CCS. El CH<sub>4</sub> es un compuesto habitualmente emitido en las industrias relacionadas con los sectores de agricultura, cerámica y gestión de residuos y el CO con los procesos de post-combustión. Ambos compuestos son altamente tóxicos con una influencia elevada en el efecto invernadero. Las composiciones estudiadas en este trabajo incluyen las recogidas en los registros oficiales de emisiones de España, Unión Europea y Estados Unidos<sup>2,3,82</sup>. Los rangos de  $P$  y  $T$  elegidos tienen en cuenta las presiones y temperaturas estimadas en el interior de las tuberías de CO<sub>2</sub><sup>62</sup> y en los lugares de almacenamiento geológico<sup>6</sup>.

### A) PROPIEDADES VOLUMÉTRICAS Y EQUILIBRIO LÍQUIDO VAPOR

En la Tabla 1 se resumen las mezclas estudiadas para los dos sistemas así como la concentración, presión y temperatura de trabajo.

Tabla 1 Composiciones, temperaturas y presiones objeto de estudio en este apartado. (En azul: estudiado para la mezcla CO<sub>2</sub>+CH<sub>4</sub>; en gris: estudiado para la mezcla CO<sub>2</sub>+CO; en blanco: no estudiado)

		<i>P</i> = 0.1 – 20 MPa										
<i>x</i> <sub>CO<sub>2</sub></sub>		<i>T</i> = 253.15 K	<i>T</i> = 263.15 K	<i>T</i> = 273.15 K	<i>T</i> = 283.15 K	<i>T</i> = 293.15 K	<i>T</i> = 298.15 K	<i>T</i> = 304.21K	<i>T</i> = 308.15K	<i>T</i> = 323.15K	<i>T</i> = 333.15K	<i>T</i> = 343.15K
0.8525	CO <sub>2</sub> +CH <sub>4</sub>											
-	CO <sub>2</sub> +CO											
0.9719	CO <sub>2</sub> +CH <sub>4</sub>											
0.9700	CO <sub>2</sub> +CO											
0.9809	CO <sub>2</sub> +CH <sub>4</sub>											
0.9810	CO <sub>2</sub> +CO											
0.9902	CO <sub>2</sub> +CH <sub>4</sub>											
0.9902	CO <sub>2</sub> +CO											
0.9932	CO <sub>2</sub> +CH <sub>4</sub>											
0.9930	CO <sub>2</sub> +CO											
0.9961	CO <sub>2</sub> +CH <sub>4</sub>											
0.9960	CO <sub>2</sub> +CO											

Se han determinado un total de 104 isothermas  $P - \rho - T - x_{\text{CO}_2}$  con una incertidumbre expandida ( $k = 2$ ) en la densidad (Anexo I, Ecuación A.V):  $U(\rho) = 0.35\text{-}0.80 \text{ kg}\cdot\text{m}^{-3}$ .

A modo de ejemplo, en las Figuras 18a) y b) se muestran las densidades experimentales para  $x_{\text{CO}_2} \cong 0.97$  para ambos sistemas a las temperaturas y presiones de trabajo. Como es de esperar, la densidad de las mezclas en las isothermas supercríticas es una línea continua cuya pendiente es máxima a la temperatura crítica y disminuye a medida que ésta aumenta.

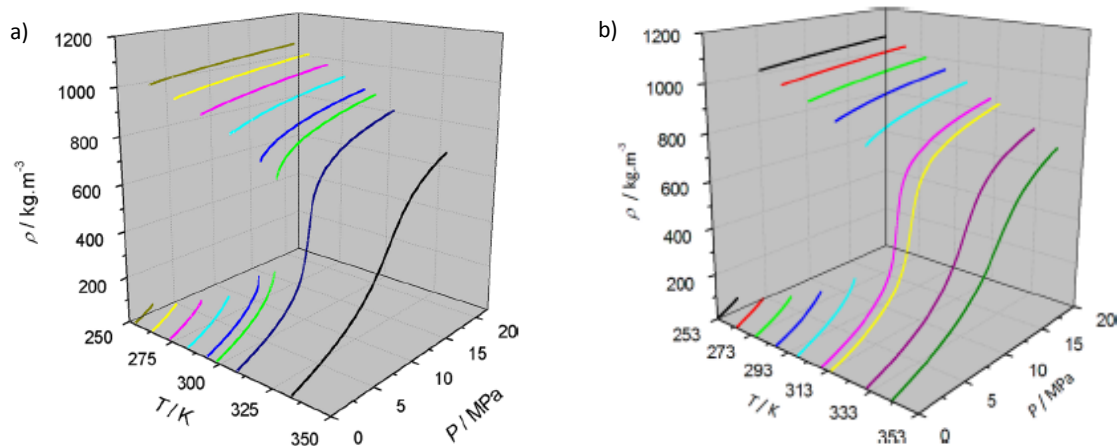


Figura 18. Densidades experimentales,  $\rho$ , para las mezclas a)  $\text{CO}_2+\text{CH}_4$  con  $x_{\text{CO}_2} = 0.9719$  y b)  $\text{CO}_2+\text{CO}$  con  $x_{\text{CO}_2} = 0.9700$ .

La región del equilibrio líquido vapor aparece delimitada por las discontinuidades de las isothermas subcríticas y sus puntos se pueden calcular como se ha descrito en la sección 4.1.A.1. La Figura 19 muestra las presiones de rocío y de burbuja experimentales y las densidades de las fases en equilibrio para tres mezclas  $\text{CO}_2+\text{CH}_4$ . Las envolventes de fase para las cinco mezclas  $\text{CO}_2+\text{CO}$  así como la línea de saturación del  $\text{CO}_2$  puro se encuentran recogidas en la Figura 20. Todos los resultados fueron consistentes con los encontrados en la bibliografía<sup>21,67,102</sup>

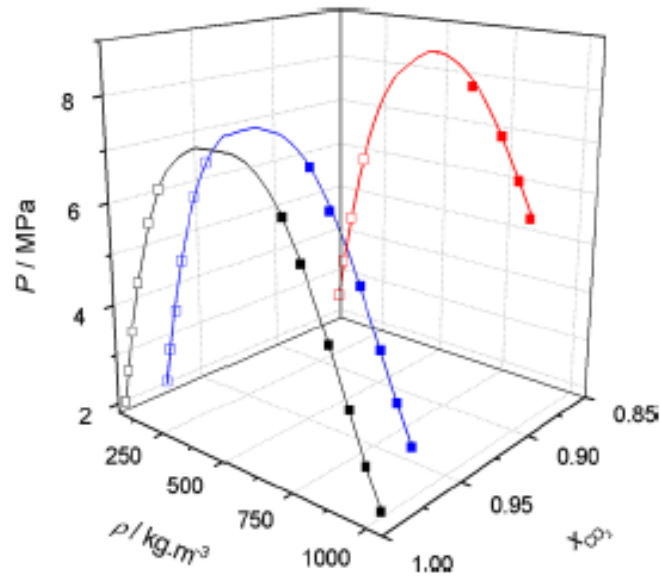


Figura 19. Presiones experimentales de rocío,  $P_r$ , (símbolos en blanco) de burbuja,  $P_b$ , (símbolos sólidos) y  $\rho_V, \rho_L$  del equilibrio de fases para las mezclas  $\text{CO}_2+\text{CH}_4$  con  $x_{\text{CO}_2}=0.8525$  (rojo),  $x_{\text{CO}_2}=0.9719$  (azul) y  $x_{\text{CO}_2}=0.9961$  (negro).

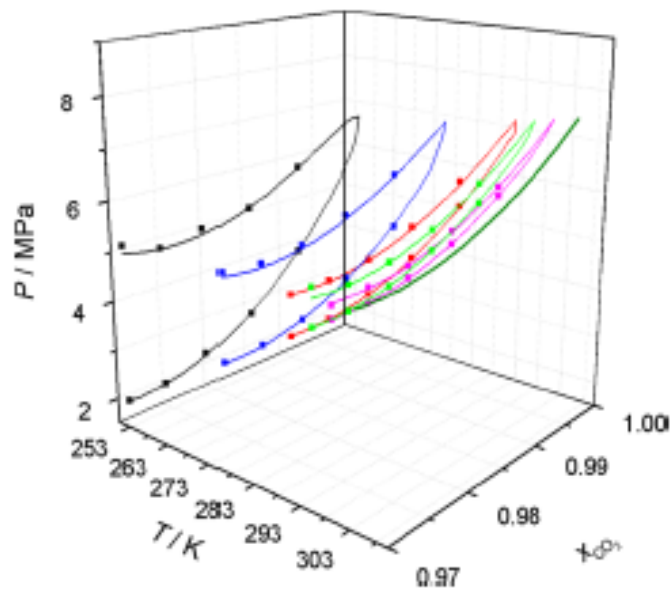


Figura 20. Presión de vapor de  $\text{CO}_2$ <sup>59</sup> (verde oliva) y envolventes de fase experimentales para las mezclas  $\text{CO}_2+\text{CO}$  con  $x_{\text{CO}_2}=0.9700$  (negro),  $x_{\text{CO}_2}=0.9810$  (azul),  $x_{\text{CO}_2}=0.9902$  (rojo),  $x_{\text{CO}_2}=0.9930$  (verde) y  $x_{\text{CO}_2}=0.9960$  (rosa).

De especial interés es el comportamiento volumétrico que presentan los sistemas en la región crítica. Por ello, también se han calculado los volúmenes molares de exceso,  $V_m^E$ , y los volúmenes parciales molares,  $\bar{V}_i$  de ambos sistemas a  $T = T_c(\text{CO}_2) = 304.21$  y  $308.15$  K:

$$V_m^E = V_{mezcla} - V_1 - V_2 = \frac{x_1 M_1 + x_2 M_2}{\rho_{mezcla}} - \frac{x_1 M_1}{\rho_1} - \frac{x_2 M_2}{\rho_2} \quad (\text{Ec.17})$$

$$\bar{V}_2 = V_m + (1 - x_2) \left( \frac{\partial V_m}{\partial x_2} \right)_{P,T} \quad (\text{Ec. 18})$$

Donde los subíndices 1 y 2, hacen referencia al disolvente (CO<sub>2</sub>) y al soluto (CH<sub>4</sub> o CO);  $M$  es la masa molar;  $V_m$  y  $\rho$  son el volumen molar y la densidad, respectivamente, a la temperatura,  $T$ , y presión,  $P$ .

Las incertidumbres expandidas en el cálculo de ambas propiedades (Anexo 1, Ecuación A.V) fueron:  $U(V_m^E) = 0.1 - 1 \text{ cm}^3 \cdot \text{mol}^{-1}$  y  $U(\bar{V}_2) = 3 - 85 \text{ cm}^3 \text{mol}^{-1}$ .

En la Figura 21 se recoge el  $V_m^E$  para ambos sistemas a las dos temperaturas y a las composiciones  $x_{\text{CO}_2} \cong 0.971$  y  $x_{\text{CO}_2} \cong 0.993$ ; dichas mezclas son supercríticas en esas condiciones.  $V_m^E$  depende fuertemente de la presión y de la composición, lo que indica un comportamiento alejado de la idealidad. Se observa un máximo para el volumen molar de exceso en función de la presión, y la disminución de su valor a medida que aumenta la temperatura y la fracción molar de CO<sub>2</sub>. El  $V_m^E$  es mayor para el sistema CO<sub>2</sub>+ CO que para CO<sub>2</sub>+CH<sub>4</sub>, lo que supone que la sustitución de una molécula de CO<sub>2</sub> por otra de CO produce una mayor perturbación en el sistema que en el caso de CH<sub>4</sub>. Esto puede deberse al mayor valor del momento dipolar de la molécula de CO ( $\mu_{\text{CO}} = 0.122 \text{ D}$ ) frente a  $\mu_{\text{CO}_2} = \mu_{\text{CH}_4} = 0$ , al tamaño de los componentes o a ambos factores.

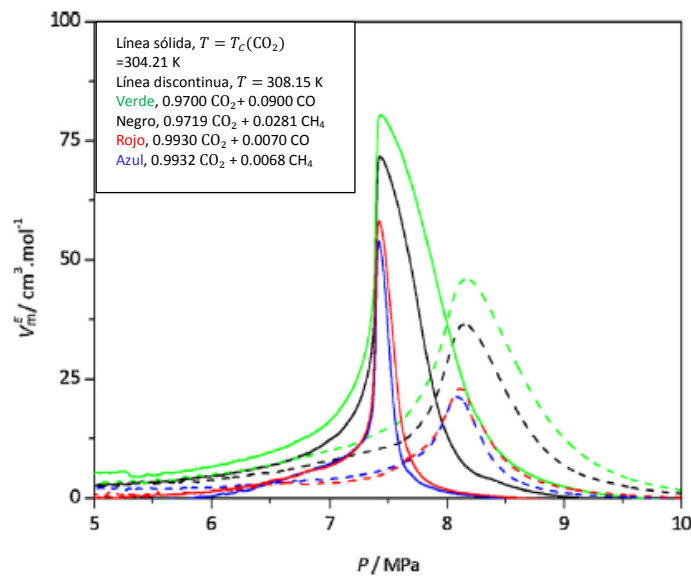


Figura 21. Representación  $V_m^E - P$  para los sistemas estudiados a  $T = T_c(\text{CO}_2) = 304.21 \text{ K}$  y  $T = 308.15 \text{ K}$ , para las composiciones  $x_{\text{CO}_2} \cong 0.971$  y  $x_{\text{CO}_2} \cong 0.993$ .

La Figura 22 muestra los volúmenes molares parciales del soluto,  $\bar{V}_2$ , para las cinco composiciones estudiadas de ambos sistemas, a las dos temperaturas y a las

presiones  $P = P_c(\text{CO}_2) = 7.383$  y  $8.000$  MPa. Para ambos sistemas se observa un comportamiento similar. A  $7.383$  MPa,  $\bar{V}_2$  disminuye al aumentar la concentración de soluto a ambas temperaturas de trabajo, con una pendiente mucho más pronunciada a  $308.15$  K. Sin embargo, a la presión supercrítica,  $8.000$  MPa,  $\bar{V}_2$  aumenta al aumentar la concentración del soluto a  $304.21$  K y disminuye a  $308.15$  K.

De nuevo, los valores de  $(\partial\bar{V}_2/\partial x_2)$  indican que el sistema  $\text{CO}_2+\text{CO}$  muestra una mayor desviación de la idealidad que el  $\text{CO}_2+\text{CH}_4$ .

Los valores de  $\bar{V}_2$  calculados en este trabajo para la mezcla  $\{0.9961 \text{ CO}_2+0.0039 \text{ CH}_4\}$  a  $308.15$  K se han comparado con los publicados por Zhang y colaboradores<sup>103</sup>, observándose buena concordancia, especialmente en la región densa. La desviación media relativa en el punto correspondiente al máximo valor de  $\bar{V}_2$  es  $\text{MRD}_{\bar{V}_2} < 6\%$ .

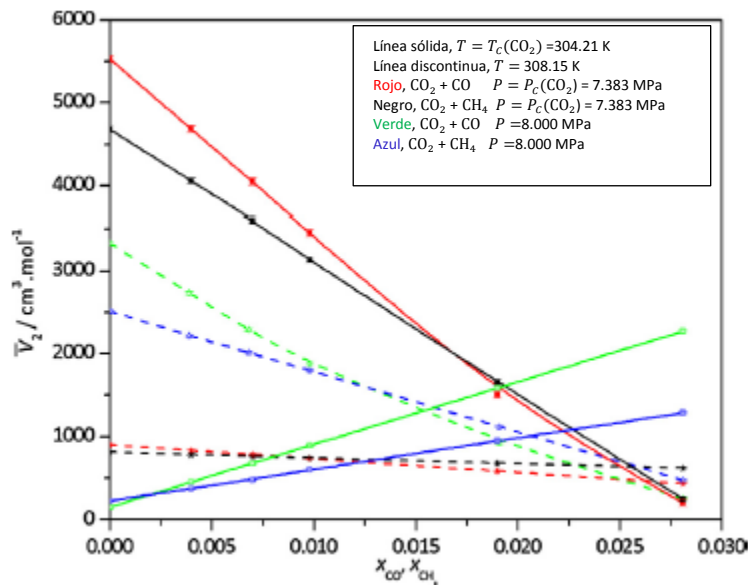


Figura 22. Representación de volumen parcial molar del soluto,  $\bar{V}_2$  frente a la fracción molar  $x_{\text{CO}_2}, x_{\text{CH}_4}$ , para los sistemas estudiados a  $P = 7.383$  y  $8.000$  MPa a  $T = 304.21$  y  $308.15$  K.

## B) PROPIEDADES DERIVADAS DE LA DENSIDAD

A partir de los datos experimentales  $P - \rho - T - x_{\text{CO}_2}$  se han calculado los valores de compresibilidad isotérmica,  $\kappa_T$ , expansividad térmica isobárica,  $\alpha_P$ , y presión interna,  $\pi_i$ , (Ecuaciones 4, 5 y 6) en todas las condiciones estudiadas.

En la Tabla 2 se recogen algunos de los datos calculados a  $304.21$  K para las mezclas  $\text{CO}_2+\text{CO}$  y  $\text{CO}_2+\text{CH}_4$  con  $x_{\text{CO}_2} = 0.993$ . Se observa que la dependencia de la compresibilidad isotérmica con la presión es similar para ambos sistemas, y la tendencia para  $\alpha_P$  es similar a la de la compresibilidad isotérmica.

Los valores de presión interna son mayores para la mezcla CO<sub>2</sub>+CO que para la mezcla CO+CH<sub>4</sub> aumentando en ambos casos al aumentar la presión del sistema.

Tabla 2. Valores de  $\kappa_T$ ,  $\alpha_P$ , y  $\pi_i$  para CO<sub>2</sub>+CO y CO<sub>2</sub>+CH<sub>4</sub> a 304.21 K para  $x_{CO_2}=0.993$ .

$P$ /MPa	$\kappa_T$ /MPa <sup>-1</sup>		$\alpha_P$ /K <sup>-1</sup>		$\pi_i$ /MPa	
	CH <sub>4</sub>	CO	CH <sub>4</sub>	CO	CH <sub>4</sub>	CO
8	$2.72 \cdot 10^{-1}$	-	$2.0 \cdot 10^{-2}$	-	14	-
9	$3.02 \cdot 10^{-1}$	$6.12 \cdot 10^{-2}$	$3.3 \cdot 10^{-2}$	$1.9 \cdot 10^{-2}$	25	85
10	$2.47 \cdot 10^{-1}$	$3.74 \cdot 10^{-2}$	$3.7 \cdot 10^{-2}$	$1.4 \cdot 10^{-2}$	36	104
11	$1.50 \cdot 10^{-1}$	$2.76 \cdot 10^{-2}$	$2.9 \cdot 10^{-2}$	$1.4 \cdot 10^{-2}$	48	143
12	$8.70 \cdot 10^{-2}$	$2.26 \cdot 10^{-2}$	$2.2 \cdot 10^{-2}$	$1.1 \cdot 10^{-2}$	63	136
13	$5.99 \cdot 10^{-2}$	$1.82 \cdot 10^{-2}$	$1.7 \cdot 10^{-2}$	$8.9 \cdot 10^{-3}$	72	136
14	$4.36 \cdot 10^{-2}$	$1.53 \cdot 10^{-2}$	$1.4 \cdot 10^{-2}$	$8.5 \cdot 10^{-3}$	82	155
15	$3.37 \cdot 10^{-2}$	$1.38 \cdot 10^{-2}$	$1.2 \cdot 10^{-2}$	$7.7 \cdot 10^{-3}$	91	155
16	$2.77 \cdot 10^{-2}$	$1.24 \cdot 10^{-2}$	$1.0 \cdot 10^{-2}$	$7.3 \cdot 10^{-3}$	98	163
17	$2.30 \cdot 10^{-2}$	$1.12 \cdot 10^{-2}$	$9.3 \cdot 10^{-3}$	$6.6 \cdot 10^{-3}$	106	162
18	$2.04 \cdot 10^{-2}$	$1.02 \cdot 10^{-2}$	$8.4 \cdot 10^{-3}$	$6.5 \cdot 10^{-3}$	107	176
19	$1.76 \cdot 10^{-2}$	$9.12 \cdot 10^{-3}$	$7.7 \cdot 10^{-3}$	$5.9 \cdot 10^{-3}$	115	178
20	$1.54 \cdot 10^{-2}$	$7.81 \cdot 10^{-3}$	$7.2 \cdot 10^{-3}$	$5.6 \cdot 10^{-3}$	122	198

### C) MODELIZACIÓN

#### a. Ecuación de Estado Peng-Robinson<sup>75</sup>

Las ecuaciones cúbicas son las ecuaciones de estado más sencillas que predicen la existencia del punto crítico y proporcionan una representación cuantitativa del ELV. Generalmente, predicen de forma razonable el comportamiento de fases de los sistemas binarios mientras que la modelización de la densidad requiere la introducción de un factor de corrección; sin embargo, su simplicidad las hace preferibles en muchas aplicaciones de ingeniería.

Para compuestos puros, solo se requiere para su aplicación las coordenadas del punto crítico ( $P_c, T_c, V_c$ ) y el valor del factor acéntrico,  $\omega$ . En el caso de mezclas, se introduce un parámetro de interacción binaria,  $k_{ij}$ . En este trabajo, hemos usado la formulación original que incluye las reglas de mezclas clásicas de van der Waals. Las ecuaciones son:

$$P = \frac{RT}{V-b} - \frac{a\alpha(T_r, \omega)}{V(V+b)+b(V-b)} \quad (\text{Ec. 19})$$

$$a = 0.45724 \frac{RT_c^{2.5}}{P_c} \quad (\text{Ec. 20})$$

$$b = 0.07780 \frac{RT_c}{P_c} \quad (\text{Ec. 21})$$

$$\alpha(T_r, \omega) = [1 + m(1 - T_r^{0.5})]^2; \quad (\text{Ec. 22})$$

$$m = 0.37464 - 1.54226\omega - 0.26992\omega^2 \quad (\text{Ec. 23})$$

$$a = \sum_i \sum_j x_i x_j a_{ij}; \quad b = \sum_i \sum_j x_i x_j b_{ij} \quad (\text{Ec. 24})$$

$$a_{ij} = \sqrt{a_i a_j} (1 - k_{ij}); \quad b_{ij} = \frac{1}{2} (b_i + b_j) \quad (\text{Ec. 25})$$

#### b. Ecuación de Estado GERG-2008<sup>50</sup>

Se trata de una ecuación de estado basada en una aproximación multifluido donde la energía de Helmholtz adimensional se divide en dos contribuciones: mezcla ideal,  $\tilde{a}_i^{id}$  y parte residual,  $\tilde{a}_i^{res}$ .

$$\tilde{a} = \tilde{a}^{id} + \tilde{a}^{res} = \sum_{i=1}^N x_i [\tilde{a}_i^{id} + \ln x_i] + \sum_{i=1}^N x_i \tilde{a}_i^{res} + \Delta \tilde{a}^{res} \quad (\text{Ec. 26})$$

Donde  $i$  hace referencia a la sustancia pura y  $\Delta \tilde{a}^{res}$  es la función de partición.

Fue desarrollada inicialmente como EoS de referencia para las mezclas de Gas Natural y, por lo general, ofrece mejores resultados que otras EoS. Sin embargo, es limitada en cuanto a su aplicación, costosa en cuanto al tiempo computacional que necesita<sup>41</sup> y no está validada en las condiciones de presión, temperatura y composición características en la Tecnología CCS.

#### c. Ecuación de Estado PC-SAFT<sup>36,37</sup>

En este modelo, basado en teorías de perturbación, el fluido de referencia se denomina fluido de cadena rígida. Las fuerzas de interacción atractivas entre moléculas se expresan a través de diferentes contribuciones, por lo que la energía de Helmholtz,  $\tilde{a}$ , se escribe como suma de las contribuciones siguientes: una para el gas ideal,  $\tilde{a}^{id}$ , un término de cadena rígida,  $\tilde{a}^{hc}$ , una contribución debida a la atracción dispersiva,  $\tilde{a}^{dis}$ , y varios términos relacionados con la asociación de las moléculas,  $\tilde{a}^{asoc}$ , e interacciones dipolo-dipolo,  $\tilde{a}^{DD}$ , cuadrupolo-cuadrupolo,  $\tilde{a}^{QQ}$  y dipolo-cuadrupolo,  $\tilde{a}^{QD}$ :

$$\tilde{a} = \tilde{a}^{id} + \tilde{a}^{hc} + \tilde{a}^{dis} + \tilde{a}^{asoc} + \tilde{a}^{DD} + \tilde{a}^{QQ} + \tilde{a}^{QD} \quad (\text{Ec. 27})$$



En este trabajo, no hemos tenido en cuenta las contribuciones polares y de asociación por lo que:

$$\tilde{a} = \tilde{a}^{id} + \tilde{a}^{hc} + \tilde{a}^{dis} \quad (\text{Ec. 28})$$

Los compuestos puros están caracterizados por tres parámetros geométricos: el número de segmento,  $m$ , el diámetro de segmento,  $\sigma$  y el parámetro de energía de segmento,  $\varepsilon$ . Si se obtienen a partir de presiones de vapor y de densidades líquidas, estos parámetros proporcionan una representación precisa tanto de las propiedades volumétricas como del ELV de las mezclas, sin embargo, sobreestiman los valores de las propiedades críticas. Con el objetivo de describir la región crítica, distintos autores<sup>11,16,33,34</sup> los reajustan incluyendo en la función objetivo sus puntos críticos. En esta Tesis se ha aplicado el modelo de dos maneras: utilizando parámetros de compuestos puros originales y reajustados. Además en ambos casos, hemos introducido traslación volumétrica para representar mejor la densidad en un intervalo amplio de presión.

Para las mezclas, se han aplicado las reglas de Lorentz-Berthelot donde el parámetro de interacción binaria,  $k_{ij}$ , corrige el término de dispersión de las moléculas:

$$\varepsilon_{ij} = \sqrt{\varepsilon_i \varepsilon_j} (1 - k_{ij}); \sigma_{ij} = \frac{1}{2} (\sigma_i + \sigma_j) \quad (\text{Ec. 29})$$

En la Tabla 3 se muestran los parámetros utilizados para la modelización. En la Tabla 4 se resume el estudio comparativo entre nuestros datos y los obtenidos con las diferentes EoS, en términos de  $MRD_x$  (Anexo I Ecuación A.I). En la región crítica de ambos sistemas, dada su complejidad, se hizo la modelización con PC-SAFT con parámetros originales y reajustados. En la Figura 23 se presentan las desviaciones obtenidas para la densidad en todo el rango de presiones.

**Tabla 3. Parámetros usados para la modelización de los sistemas CO<sub>2</sub>+CH<sub>4</sub> y CO<sub>2</sub>+CO con PR y PC-SAFT EoS**

Parámetro	CO <sub>2</sub>	CH <sub>4</sub>	CO
$T_C / K$	304.21 <sup>32</sup>	190.56 <sup>53</sup>	132.86 <sup>53</sup>
$P_C / MPa$	7.383 <sup>32</sup>	4.599 <sup>53</sup>	3.494 <sup>53</sup>
$\omega$	0.224 <sup>53</sup>	0.011 <sup>53</sup>	0.066 <sup>53</sup>
$m$	2.0730 <sup>36</sup> /2.1276 <sup>11</sup>	1.0000 <sup>36</sup> /1.0039 <sup>**</sup>	1.3097 <sup>36</sup> /1.3063 <sup>**</sup>
$\sigma / \text{Å}$	2.7852 <sup>36</sup> /2.8251 <sup>11</sup>	3.7039 <sup>36</sup> /3.7126 <sup>**</sup>	3.2507 <sup>36</sup> /3.2565 <sup>**</sup>
$\varepsilon / K$	169.21 <sup>36</sup> /163.76 <sup>11</sup>	150.03 <sup>36</sup> /149.11 <sup>**</sup>	92.15 <sup>36</sup> /91.48 <sup>**</sup>
$\Delta v_C (PR \text{ EoS}) / (10^{-3} \text{ m}^3 \text{ kg}^{-1})$	0	0	0
$\Delta v_C (PC - SAFT \text{ EoS}) / (10^{-3} \text{ m}^3 \text{ kg}^{-1})$	0.02 <sup>*</sup>	0 <sup>*</sup>	-0.10 <sup>*</sup>
-----			
$k_{ij} (PR \text{ EoS})$	CO <sub>2</sub> +CH <sub>4</sub> = 0.12 <sup>53</sup>		CO <sub>2</sub> +CO = 0.205
$k_{ij} (PC - SAFT \text{ EoS})$	CO <sub>2</sub> +CH <sub>4</sub> = 0.07 <sup>*</sup> /0.05 <sup>**</sup>		CO <sub>2</sub> +CO = 0.12 <sup>*</sup> /0 <sup>**</sup>

\*PC-SAFT modelo original (Este trabajo)

\*\*PC-SAFT modelo reajustado (Este trabajo)

Tabla 4. Desviaciones relativas promedio con respecto a las tres EoS de referencia para,  $P_r$ ,  $P_b$ ,  $\rho_V$ ,  $\rho_L$  y densidades,  $\rho$ , para regiones distintas a la crítica, para las mezclas  $\text{CO}_2+\text{CH}_4$  y  $\text{CO}_2+\text{CO}$ .

	$\text{CO}_2 + \text{CH}_4$			$\text{CO}_2 + \text{CO}$		
	PR	PC-SAFT	GERG-2008	PR	PC-SAFT	GERG-2008
	EoS	EoS	EoS	EoS	EoS	EoS
$MRD_{P_b}/\%$	0.69	1.7	0.18	1.9	1.6	1.3
$MRD_{P_r}/\%$	0.48	1.7	0.13	0.47	1.4	0.38
$MRD_{\rho_L}/\%$	4.5	1.8	0.24	3.8	0.39	0.45
$MRD_{\rho_V}$ / $\%$	1.5	5.8	0.66	1.8	4.3	1.4
$MRD_{\rho}^a/\%$	2.3	1.1	0.28	2.9	1.2	0.73
$MRD_{\rho}^b/\%$	3.6	1.7*/2.8**	0.40	3.2	1.5*/2.7**	1.1

<sup>a</sup>  $T \neq 304.21$  y  $308.15$  K

<sup>b</sup>  $T = 304.21$  y  $308.15$  K

\*PC-SAFT modelo original (Este trabajo)

\*\* PC-SAFT modelo reajustado (Este trabajo)

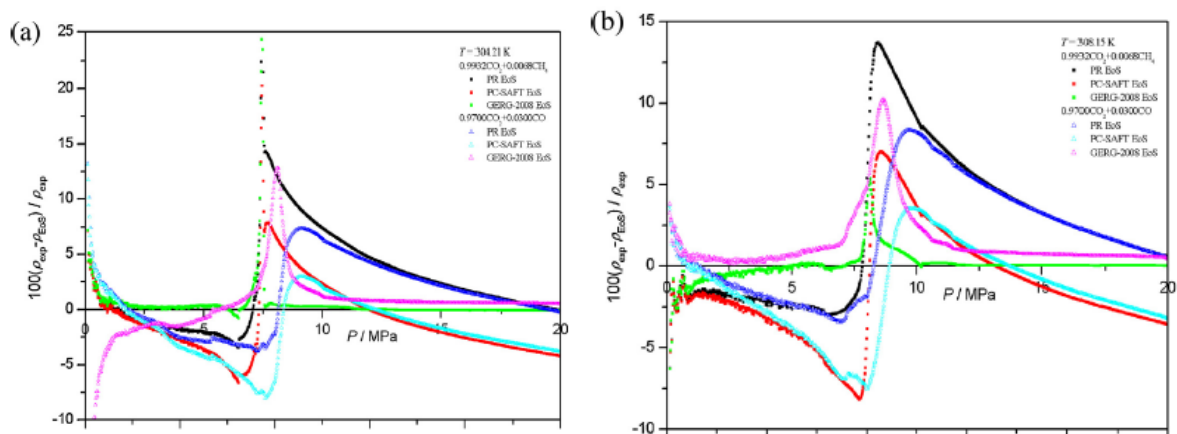


Figura 23. Desviación estándar relativa entre las densidades determinadas experimentalmente y los valores calculados utilizando diferentes EoS para distintas mezclas estudiadas en este trabajo. (a)  $T = 304.21$  K y (b)  $T = 308.15$  K.

A pesar de su simplicidad, la concordancia de la EoS PR con los datos experimentales es buena a presiones por debajo de la presión crítica para ambos sistemas y aceptable a presiones mayores.

La modelización con PC-SAFT utilizando los parámetros originales para los compuestos puros predice un estado subcrítico erróneo para nuestras mezclas ya que experimentalmente observamos un estado supercrítico. Sin embargo, las predicciones fuera de la región crítica son buenas. Por otro lado, si se utilizan los parámetros reajustados utilizando los puntos críticos para los compuestos puros, el modelo predice las regiones crítica y supercrítica de manera más precisa aunque las desviaciones fuera de estas regiones son mayores.

La comparación entre nuestros datos experimentales y los calculados con la EoS GERG-2008 es muy buena para ambos sistemas siendo las desviaciones menores para el sistema CO<sub>2</sub>+CH<sub>4</sub>. Esto podría deberse a que la ecuación está implementada con un gran número de datos experimentales para estas mezclas.

La EoS GERG-2008 es la ecuación que mejor representa nuestros resultados aunque presenta problemas al extenderla a mezclas de compuestos que no se encuentran en su base de datos. PC-SAFT presenta desviaciones ligeramente mayores que GERG-2008 pero su uso puede extenderse fácilmente a mezclas multicomponentes. Por último, PR puede también ser adecuada dependiendo de las presiones de trabajo y de la precisión requerida.

## D) ESTUDIO ESTRUCTURAL

La eficiencia y la selectividad de los procesos de almacenamiento están influenciados por el tipo de interacciones entre el CO<sub>2</sub> y las moléculas presentes en el reservorio, y por tanto, por su afinidad. En esta sección se determina la naturaleza de las interacciones entre las moléculas de disolvente, CO<sub>2</sub> y las de soluto, CH<sub>4</sub> o CO a través del estudio volumétrico de disoluciones infinitamente diluidas, IDS, para los sistemas CO<sub>2</sub>+CH<sub>4</sub> y CO<sub>2</sub>+CO en condiciones cercanas a la temperatura crítica del CO<sub>2</sub>. Se usarán el concepto de Función de Krichevskii y la Teoría de Kirkwood-Buff.<sup>43,46</sup>

El comportamiento termodinámico de una disolución puede ser descrito a través del efecto que produce sustituir, de forma isoterma e isocora, una molécula de disolvente por una de soluto a dilución infinita<sup>42,60</sup>. Cuando las condiciones de estudio coinciden con las críticas del disolvente se define el *parámetro de Krichevskii*,  $A_{K_r} = (\partial P / \partial x_2)_{T_c, V_c}^{\infty}$  y si no coinciden, la *función de Krichevskii*,  $J = (\partial P / \partial x_2)_{T, V}^{\infty}$ .

Por lo tanto,  $J$  estará relacionada con magnitudes termodinámicas de la mezcla. Se puede deducir<sup>11</sup>:

$$\bar{V}_2^{\infty} = \rho_1^{0-1} [1 + \kappa_T^0 J] \quad (\text{Ec. 30})$$

Donde los superíndices 0 y  $\infty$  denotan componente puro y dilución infinita, respectivamente;  $\rho_1^0$  es la densidad del disolvente puro y  $\kappa_{T,1}^0$  su compresibilidad isotérmica.

Por otro lado, se puede establecer una relación entre la función de Krichevskii,  $J$ , con las propiedades estructurales del fluido a través de la llamada Inversión de la Teoría de Kirkwood-Buff, desarrollada por Ben-Naim en 1978.<sup>9</sup> En ella, las propiedades termodinámicas determinadas experimentalmente son utilizadas para calcular las integrales de Kirkwood-Buff (KBI),  $G_{ij} = \int_0^\infty [g_{ij}(r) - 1] 4\pi r^2 dr$ , lo que permite conocer el entorno local de cada especie en el sistema multicomponente.  $g_{ij}(r)$  es la función de correlación de pares para las especies  $i$  y  $j$ , también llamada función de distribución radial, que representa la probabilidad de encontrar la partícula  $i$  a una distancia  $r$  de la partícula  $j$ .

Alternativamente, se puede trabajar en términos de la Función Integral de Correlación Directa (DCFI),  $C_{ij} = \int c_{ij} dr$ , donde  $c_{ij}$  (función de correlación directa) representa la correlación debida únicamente a las fuerzas de interacción existentes entre dos partículas  $i$  y  $j$  en un sistema de N-2 partículas.

Para una mezcla binaria en condiciones de dilución infinita,  $x_2 \rightarrow 0$ , las ecuaciones de Kirkwood-Buff se simplifican<sup>18, 55</sup>:

$$\rho_1^0 RT \kappa_T^0 = 1 + \rho_1^0 G_{11}^0 \quad (\text{Ec. 31}) \quad (\kappa_T^0)^{-1} = \rho_1^0 RT (1 - C_{11}^0) \quad (\text{Ec. 32})$$

$$\rho_1^0 \bar{V}_2^\infty = 1 + \rho_1^0 (G_{11}^0 - G_{12}^\infty) \quad (\text{Ec. 33}) \quad \rho_1^0 \bar{V}_2^\infty = \rho_1^0 RT \kappa_T^0 (1 - C_{12}^\infty) \quad (\text{Ec. 34})$$

$$J \kappa_T^0 = \rho_1^0 (G_{11}^0 - G_{12}^\infty) \quad (\text{Ec. 35}) \quad J = \rho_1^0 RT (C_{11}^0 - C_{12}^\infty) \quad (\text{Ec. 36})$$

Como se puede apreciar en la Ecuación 35, el reordenamiento del disolvente alrededor del soluto en la IDS, en relación a la estructura del disolvente puro, no viene dado por la fortaleza de la interacción entre las moléculas de disolvente y las del soluto sino por la asimetría intermolecular y la diferencia existente entre las interacciones disolvente-disolvente (1-1) y las disolvente-soluto (1-2). Todo ello permite valorar la idealidad de la mezcla.

El estudio se completa con el cálculo del número de coordinación de exceso,  $N_{exc}^\infty$ , y el tamaño de clúster,  $N_1^{exc}$ . El primero se define como la diferencia entre el número de moléculas de disolvente que rodean a una molécula de soluto en condiciones de dilución infinita y el número de moléculas de disolvente alrededor de otra igual. El segundo,  $N_1^{exc}$ , indica la afinidad que presentan las moléculas de disolvente por una molécula de soluto en las cercanías del punto crítico del solvente.

$$N_{exc}^{\infty} = 4\pi\rho \int_0^r [g_{12}(r) - g_{11}(r)]r^2 dr = -\kappa_T^0 \left( \frac{\partial P}{\partial x_2} \right)_{T,V}^{\infty} \quad (\text{Ec. 37})$$

$$N_1^{exc} = 4\pi\rho \int_0^r [g_{12}(r) - 1]r^2 dr = \rho_1^0 RT \kappa_T^0 (1 - A_{\kappa_r}^*) \quad (\text{Ec. 38})$$

Donde  $A_{\kappa_r}^* = \frac{A_{\kappa_r}}{\rho_1^0 RT}$

Cuando se dispone de datos volumétricos a dilución infinita, los valores de la función de Krichevskii (incluidos el parámetro de Krichevskii,  $A_{\kappa_r}$ ) se calculan a partir de las pendientes de las isoterma-isocoras  $P - x_2$  cuando  $x_2 \rightarrow 0$  (Figura 24).

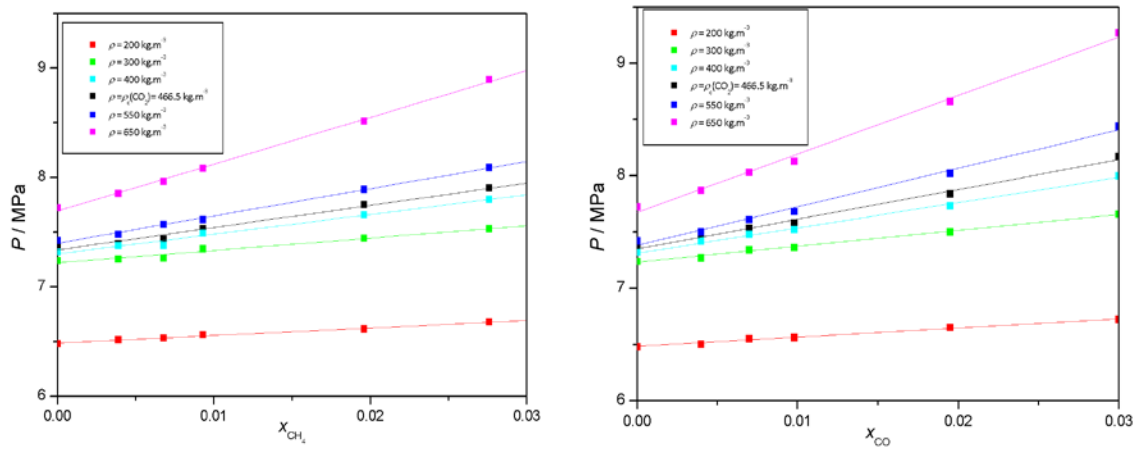


Figura 24. Datos  $P - x_{CH_4}/x_{CO}$  de mezclas diluidas (a)  $CO_2 + CH_4$  y (b)  $CO_2 + CO$ , para varias isocoras a  $T = 304.21$  K.

La Figura 25 muestra la diferencia de comportamiento de ambos sistemas en condiciones de dilución infinita, a la temperatura de 304.21 K, a través de la comparación de sus valores de  $J$ . Así, sustituir una molécula de  $CO_2$  por una de  $CO$  o de  $CH_4$  en el dióxido de carbono puro supone en ambos casos un aumento de presión del sistema, siendo más acusado en el caso del  $CO$  que del  $CH_4$ .

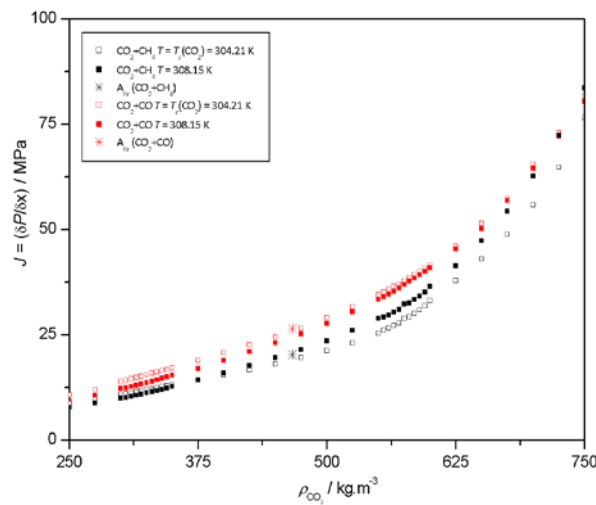


Figura 25. Función de Krichevskii,  $J$ , frente a densidad del disolvente puro,  $\rho_{CO_2}$  para los sistemas  $CO_2 + CO$  y  $CO_2 + CH_4$  a  $T = 304.21$  K y  $T = 308.15$  K.

En las proximidades del punto crítico del disolvente puro,  $x_2 \rightarrow 0$ , la función de Krichevskii converge al parámetro de Krichevskii,  $J \xrightarrow{\alpha T=T_c} A_{Kr}$ , y la compresibilidad isotérmica del disolvente puro diverge,  $\kappa_T^0 \rightarrow +\infty$ . Por ello, en estas condiciones, las funciones termodinámicas y parámetros estructurales que dependen de  $\kappa_T^0$  también serán divergentes con un signo de divergencia que dependerá del signo del parámetro de Krichevskii,  $A_{Kr}$ ; para los sistemas estudiados en este trabajo,  $\rightarrow +\infty$ .

En la Tabla 5 se recogen los datos de los parámetros para los dos sistemas estudiados. Se puede observar que

- Los valores obtenidos de  $C_{ij}$  son superiores en la mezcla  $\text{CO}_2+\text{CH}_4$ , pero la gran asimetría del sistema  $\text{CO}_2+\text{CO}$  produce un cambio mayor en la estructura del disolvente, tal y como queda patente en sus valores mayores de  $(C_{11} - C_{12})$ .
- En ambos sistemas  $N_{exc}^\infty < 0$ . Es decir, la sustitución, en condiciones de dilución infinita a temperatura y volumen constantes, de una molécula de disolvente por una de soluto provoca una disminución en la densidad local (el número de coordinación) respecto a la existente en la mezcla ideal. La disminución es más acusada para el sistema  $\text{CO}_2+\text{CO}$ .
- La afinidad de las moléculas de  $\text{CO}_2$  por el soluto es mayor cuando éste es metano.

Tabla 5. Comparación entre los valores obtenidos para los sistemas  $\text{CO}_2 + \text{CO}$  y  $\text{CO}_2 + \text{CH}_4$  para varios parámetros estructurales y propiedades.

Parametro / Propiedad	T / K	Sistema	
		$\text{CO}_2 + \text{CH}_4$	$\text{CO}_2 + \text{CO}$
$A_{Kr} / \text{MPa}$	304.21	$20.383 \pm 0.004$	$26.418 \pm 0.005$
$A_{Kr}^*$	304.21	0.76	0.98
$(\bar{V}_2^\infty)_{max} / \text{cm}^3 \cdot \text{mol}^{-1}$	308.15	3300	3950
$(N_{exc}^\infty)_{min}$	308.15	-33	-38
$(N_1^{exc})_{max}$	308.15	11	3
$10^{-3}(C_{12})_{\rho_c} / \text{cm}^3 \cdot \text{mol}^{-1}$	308.15	0.020	0.006
$10^{-3}(C_{11} - C_{12})_{\rho_c} / \text{cm}^3 \cdot \text{mol}^{-1}$	308.15	0.072	0.085

Debenedetti y Mohamed<sup>20</sup> establecieron que dependiendo del signo de las divergencias de  $\bar{V}_2^\infty$ ,  $N_{exc}^\infty$  y  $N_1^{exc}$  las disoluciones infinitamente diluidas en las cercanías del punto crítico del disolvente puro presentan uno de estos tres tipos de comportamiento: atractivo, débilmente atractivo o repulsivo.

Para nuestros sistemas a  $T = T_c(\text{CO}_2)$  y  $\rho = \rho_c(\text{CO}_2)$ :

$$A_{\kappa_r} > 0; \quad \bar{V}_2^\infty \rightarrow +\infty; \quad N_{exc}^\infty \rightarrow -\infty; \quad 1 > A_{\kappa_r}^* > 0; \quad N_1^{exc} \rightarrow +\infty$$

Es decir, al añadir de forma isoterma e isóbara una molécula de soluto a la IDS, se produce un aumento de volumen y un enriquecimiento de disolvente alrededor del soluto para ambos sistemas, esto es, tienen un *comportamiento débilmente atractivo*.

## E) APLICACIÓN A LA TECNOLOGÍA CCS PARA LA REDUCCIÓN DE LAS EMISIONES DE CO<sub>2</sub>

La presencia y el tipo de impurezas que acompañan al CO<sub>2</sub> antropogénico influyen en sus propiedades termofísicas y en el comportamiento de éste y, como consecuencia, en el diseño y operación de las instalaciones de la tecnología CCS. Debido a los escasos datos experimentales relativos tanto a las impurezas objeto de esta Tesis como a otras, la mayor parte de los estudios de la bibliografía desarrollan simulaciones para predecir tanto el comportamiento termodinámico como los valores de los parámetros asociados con la tecnología CCS.

A partir de los valores experimentales de densidad y equilibrio líquido-vapor y de las propiedades derivadas obtenidas, así como de valores calculados de viscosidad, hemos cuantificado y comparado el efecto de la presencia de CO y CH<sub>4</sub> en parámetros seleccionados asociados con el transporte, la inyección y el almacenamiento del CO<sub>2</sub> antropogénico. La evaluación de estos parámetros es imprescindible para el diseño, construcción y operación de redes de tuberías de transporte y de equipos de inyección fiables y seguros, así como para el almacenamiento seguro a largo plazo.

### E.1.) Influencia del CH<sub>4</sub> y del CO en el transporte del CO<sub>2</sub> antropogénico por ceoducto

La presencia de impurezas en el CO<sub>2</sub> antropogénico incluso en pequeñas concentraciones, afecta en gran medida a la hidráulica de la tubería y a otros muchos aspectos de la operación y el diseño.<sup>86</sup> A partir de los datos experimentales presentados en este trabajo y de viscosidades calculadas con REFPROP<sup>59</sup> se obtienen valores de los siguientes parámetros: Flujo másico,  $m$ ; diámetro interno de la tubería,  $D$ ; velocidad de erosión,  $v_E$ ; número de Reynolds,  $R_e$ ; capacidad de las estaciones de represurización,  $W$ ; factor de fricción de Darcy-Weisbach,  $f$  y caída de presión por metro,  $\Delta P/L$ .

En la Tabla 6 se encuentran las ecuaciones utilizadas para el cálculo de estos parámetros y de otros necesarios en cálculos intermedios. Para ello se han utilizado valores

experimentales de densidad de este Trabajo y valores de viscosidad calculados con REFPROP 9.0.<sup>59</sup>

Los resultados obtenidos para los dos sistemas, CO<sub>2</sub>+CO y CO<sub>2</sub>+CH<sub>4</sub> se compararán entre sí y con los correspondientes al CO<sub>2</sub> puro.

Tabla 6. Resumen de ecuaciones para el cálculo de varios parámetros para el diseño de la tubería y su operación.<sup>25</sup>

Parámetros	Fórmula	Símbolos
Flujo másico	$m = \rho v A$	$m$ : flujo másico (kg·s <sup>-1</sup> ) $\rho$ : densidad del fluido (kg·m <sup>-3</sup> ) $v$ : velocidad del fluido (m·s <sup>-1</sup> ) $A$ : sección interna de la tubería (m <sup>2</sup> )
Diámetro interno de la tubería	$D = \left(\frac{4m}{v\rho}\right)^{1/2}$	$D$ : diámetro interno de la tubería (m) $m$ : flujo másico (kg·s <sup>-1</sup> ) $v$ : velocidad del fluido (m·s <sup>-1</sup> ) $\rho$ : densidad del fluido (kg·m <sup>-3</sup> )
Velocidad de erosión	$v_E = \frac{C}{\sqrt{\rho}}$	$v_E$ : velocidad de erosión (m·s <sup>-1</sup> ) $C$ : constante empírica $\rho$ : densidad del fluido (kg·m <sup>-3</sup> )
Número de Reynolds	$Re = \frac{\rho v D}{\mu}$	$Re$ : número de Reynolds $\rho$ : densidad del fluido (kg·m <sup>-3</sup> ) $v$ : velocidad del fluido (m·s <sup>-1</sup> ) $D$ : diámetro interno de la tubería (m) $\mu$ : viscosidad del fluido (Pa·s)
Capacidad de las estaciones de re-presurización	$W = \frac{m}{\rho} \cdot \frac{(P_{out} - P_{in})}{\eta_{booster}}$	$W$ : Capacidad de la estación de bombeo (MW) $m$ : flujo másico (kg·s <sup>-1</sup> ) $P_{out}$ : presión a la salida del compresor (MPa) $P_{in}$ : presión a la entrada del compresor (MPa) $\rho$ : densidad del fluido (kg·m <sup>-3</sup> ) $\eta_{booster}$ : rendimiento del compresor
Factor de fricción de Darcy-Weisbach	$f = \frac{1.325}{\left[\ln\left(\frac{e}{3.7D}\right) - \left(\frac{5.74}{Re^{0.9}}\right)\right]^2}$	$f$ : Factor de fricción de Darcy-Weisbach $e$ : altura aproximada (m) $D$ : diámetro interno de la tubería (m) $Re$ : número de Reynolds
Caída de presión por metro	$\frac{\Delta p}{L} = \frac{8fm^2}{\rho\pi^2 D^5}$	$(\Delta p/L)$ : caída de presión por metro (Pa·m <sup>-1</sup> ) $m$ : flujo másico (kg·s <sup>-1</sup> ) $\rho$ : densidad del fluido (kg·m <sup>-3</sup> ) $f$ : Factor de fricción de Darcy-Weisbach $D$ : diámetro interno de la tubería (m)



### E.1.1.1. Presión mínima de operación, $P_{min}$

La manera más rentable de transportar el CO<sub>2</sub> antropogénico es en estado supercrítico ( $P > P_c$  y  $T > T_c$ ) o estado denso ( $P > P_c$  y  $T < T_c$ ). Esto es debido a que, en esas condiciones, su viscosidad es menor que la del líquido y el volumen que ocupa es muy inferior al que ocuparía si estuviera en fase gas. A pesar de ello, algunos proyectos consideran el transporte en fase gas como alternativa cuando la longitud de la tubería y/o el flujo de masa son pequeños.

En cualquier caso, es importante evitar flujos bifásicos durante el transporte de fluidos por tuberías ya que originan<sup>47</sup>: (i) cavitación: producida por la implosión de la burbuja en la región bifásica, que genera ondas de choque que pueden causar roturas en la tubería; (ii) turbulencias causadas por las burbujas que obstaculizan el correcto funcionamiento de los compresores y las bombas; y (iii) pérdida en la capacidad de transporte.

En la bibliografía se han encontrado dos formas de operar distintas para transportar CO<sub>2</sub> antropogénico en fase densa:

- i) Mantener la presión de transporte por encima de un valor mínimo,  $P_{min}^{800}$ , que asegure una densidad del fluido transportado superior a  $800 \text{ kg}\cdot\text{m}^{-3}$ . En la Tabla 7 se recoge la presión mínima de operación para asegurar una densidad de  $800 \text{ kg}\cdot\text{m}^{-3}$ ,  $P_{min}^{800}$ , en el caso del CO<sub>2</sub> puro y de las mezclas CO<sub>2</sub>+CO a  $x_{\text{CO}_2} = 0.9902$  y  $x_{\text{CO}_2} = 0.9700$ .

No considerar las impurezas supondría un error de 62% en el valor de  $P_{min}^{800}$  en el caso de una mezcla CO<sub>2</sub>+CO con un 3% por mol de CO mientras que la misma cantidad de CH<sub>4</sub> daría lugar a un error de 27%.

- ii) Mantener la presión de transporte por encima de un valor mínimo,  $P_{min}$ , que corresponde a la presión de burbuja del fluido transportado. Las impurezas que acompañan al CO<sub>2</sub> antropogénico afectan significativamente a las características y localización de la región bifásica. Por ejemplo, si se transporta CO<sub>2</sub> puro a 283.15 K, la fase vapor aparecerá a la presión de saturación,  $P_{sat} = 4.50 \text{ MPa}$ . Sin embargo, si el fluido contiene un 3% de CH<sub>4</sub> por mol, la zona bifásica se encuentra comprendida entre  $P_b = 6.57$  y  $P_r = 4.72 \text{ MPa}$ . (Tabla 8 y Figura 26)

Para el CO<sub>2</sub> antropogénico transportado en fase densa o supercrítica, la literatura proporciona valores de  $P_{min}$  de 7.5-11 MPa y de 9-30 MPa de presión máxima de operación,  $P_{max}$ .

Tabla 7. Valores de presión mínima requeridos para obtener una densidad de  $800 \text{ kg}\cdot\text{m}^{-3}$  para varias temperaturas de transporte, al transportar  $\text{CO}_2$  puro o mezclas  $\text{CO}_2+\text{CO}$ .

$T_{tr}/\text{K}$	$P_{min}^{800} / \text{MPa}$		
	$\text{CO}_2$ puro	$x_{\text{CO}_2} = 0.9902$	$x_{\text{CO}_2} = 0.9700$
253.15	1.970	2.979	5.208
263.15	2.649	3.578	5.400
273.15	3.485	4.277	5.991
283.15	4.502	5.216	6.574
293.15	6.626	7.601	9.448
304.21	11.987	12.851	15.060
308.15	13.904	14.804	16.851
323.15	21.371	>20 MPa	>20 MPa
333.15	26.398	>20 MPa	>20 MPa
343.15	31.445	>20 MPa	>20 MPa

Tabla 8. Valores de presión de rocío y burbuja y densidades de la fase líquida y vapor para la mezcla  $\text{CO}_2+\text{CH}_4$  a varias temperaturas y composiciones.

$T$ /K	$P_r$ /MPa	$P_b$ /MPa	$\rho_L$ /kg·m <sup>-3</sup>	$\rho_V$ /kg·m <sup>-3</sup>	$P_r$ /MPa	$P_b$ /MPa	$\rho_L$ /kg·m <sup>-3</sup>	$\rho_V$ /kg·m <sup>-3</sup>
$x_{\text{CO}_2} = 0.9700$				$x_{\text{CO}_2} = 0.9810$				
253.15	2.070	5.208	1014.58	53.25	2.038	4.033	1021.71	53.66
263.15	2.770	5.400	966.00	74.40	2.741	4.477	970.42	73.19
273.15	3.680	5.991	909.35	102.10	3.577	5.087	916.50	101.98
283.15	4.720	6.574	840.50	141.71	4.695	5.905	850.08	137.92
293.15	6.080	7.465	752.15	207.60	5.912	6.871	758.54	202.01
$x_{\text{CO}_2} = 0.9902$				$x_{\text{CO}_2} = 0.9930$				
253.15	1.989	2.979	1026.86	52.45	1.988	2.978	1026.89	52.54
263.15	2.681	3.578	975.73	71.36	2.67	3.293	978.09	70.56
273.15	3.527	4.277	921.85	97.61	3.520	4.060	924.11	99.04
283.15	4.579	5.216	852.66	136.39	4.556	4.999	859.42	135.89
293.15	5.847	6.345	766.26	189.91	5.762	6.162	777.60	187.60
$x_{\text{CO}_2} = 0.9960$				$x_{\text{CO}_2} = 1 (\text{CO}_2 \text{ puro})$				
253.15	1.977	2.327	1031.12	52.46	1.9696*		1031.7	51.700
263.15	2.657	3.054	979.86	70.72	2.6487*		982.93	71.185
273.15	3.527	3.804	924.55	98.24	3.4851*		927.43	97.647
283.15	4.530	4.811	857.70	135.26	4.5022*		861.12	135.16
293.15	5.778	5.962	764.73	193.76	5.7291*		773.39	194.20

(\*) valores de  $P_{sat}$

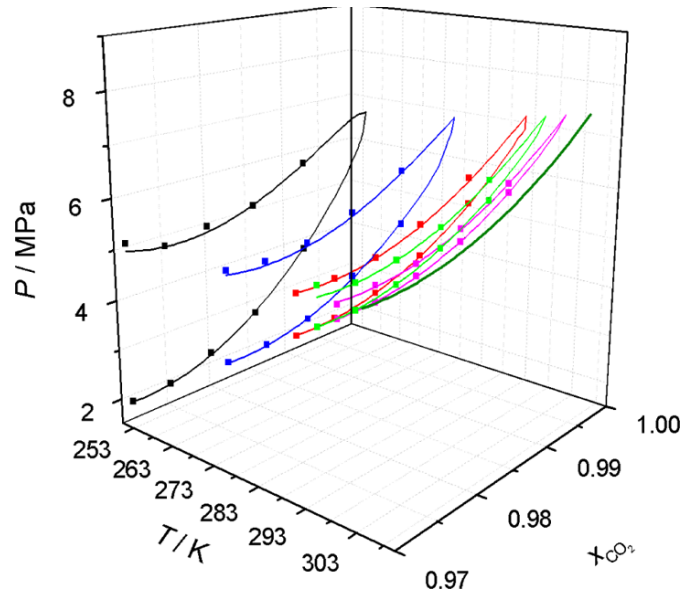


Figura 26. Presión de vapor para  $\text{CO}_2$ <sup>59</sup> (verde oliva) y envolventes de fase experimentales para las mezclas  $\text{CO}_2+\text{CO}$  con  $x_{\text{CO}_2} = 0.9700$  (negro),  $x_{\text{CO}_2} = 0.9810$  (azul),  $x_{\text{CO}_2} = 0.9902$  (rojo),  $x_{\text{CO}_2} = 0.9930$  (verde) y  $x_{\text{CO}_2} = 0.9960$  (rosa).

### E.1.2. Caída de presión a lo largo de la tubería, $P(d)$ .

La caída de presión está originada por la orografía del terreno y por el conjunto de fuerzas de fricción. Estas las ejercen tanto las paredes de la tubería sobre la capa de fluido que está en contacto con ellas como cada capa de fluido sobre las adyacentes. Como consecuencia, se produce una pérdida de energía en el sistema que se transforma en una disminución de la presión conforme el fluido va avanzando. Este factor es de gran importancia cuando se trata de transporte a grandes distancias.

La disminución en la densidad y en la viscosidad de la mezcla hace que la caída de presión aumente al aumentar la temperatura (Figura 27) y la concentración de impurezas no condensables, influyendo de forma muy similar el  $\text{CH}_4$  y el  $\text{CO}$ .

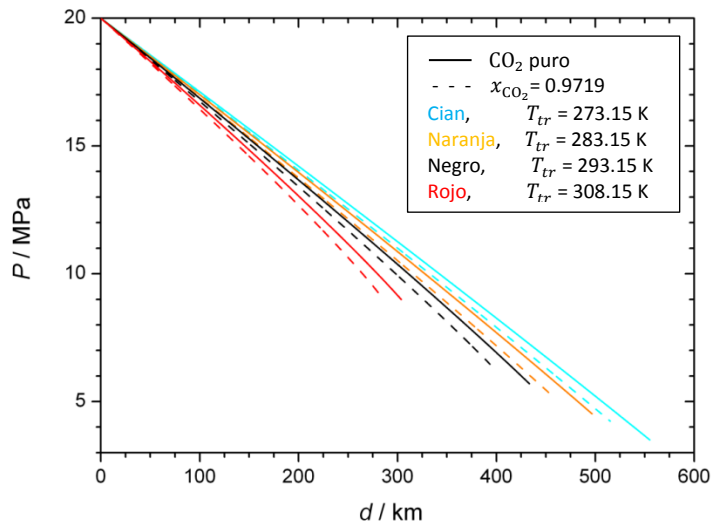


Figura 27. Comparación entre la caída de presión a lo largo de la tubería para  $\text{CO}_2$  puro (líneas sólidas) y las mezclas (a)  $\text{CO}_2+\text{CO}$  y (b)  $\text{CO}_2+\text{CH}_4$  (líneas discontinuas) a varias temperaturas de transporte,  $T_{tr}$ . Se ha utilizado para el cálculo: flujo másico  $m = 317 \text{ kg}\cdot\text{s}^{-1}$ , diámetro interno de la tubería  $D = 0.508 \text{ m}$  y coeficiente de rugosidad  $e = 4.6\cdot 10^{-5} \text{ m}$ , para una tubería con una presión inicial de 20.0 MPa.

Para una presión inicial  $P_{ini} = 20 \text{ MPa}$ , una distancia  $d = 250 \text{ km}$ , y una temperatura,  $T = 273.15 \text{ K}$ :

$$\text{CO}_2 \text{ puro} \Rightarrow P_{fin} = \mathbf{12.7 \text{ MPa}}$$

$$\text{CO}_2 + \text{CH}_4 / \text{CO} \quad (x_{\text{CO}_2} \cong 0.97) \Rightarrow P_{fin} = \mathbf{12.5 \text{ MPa}}$$

Para una presión inicial  $P_{ini} = 20 \text{ MPa}$ , una presión final,  $P_{fin} = 10 \text{ MPa}$ , y una temperatura,  $T = 308.15 \text{ K}$ :

$$\text{CO}_2 \text{ puro} \Rightarrow d = \mathbf{280 \text{ km}}$$

$$\text{CO}_2 + \text{CH}_4 / \text{CO} \quad (x_{\text{CO}_2} \cong 0.97) \Rightarrow d = \mathbf{262 \text{ km}}$$

La caída de presión junto con el diámetro de la tubería, la presión en su interior y las propiedades de transporte del fluido, determinan el lugar y el número de estaciones de bombeo o presurización necesarias para el transporte en fase densa. Así, para el diseño eficiente de la red de transporte se debe conseguir un compromiso entre el diámetro, la presión en el interior de la tubería y el número y la potencia de las estaciones de bombeo.

### E.1.3. Distancia máxima de represurización, $L$ .

La caída de presión anteriormente citada junto a la necesidad de garantizar una presión mínima de trabajo (E.1.1.) obliga a realizar operaciones de represurización cada cierta distancia. En la Figura 28 se muestra la distancia máxima de represurización,  $L$ , frente a la temperatura de transporte,  $T_{tr}$ , para el fluido transportado en tubería y unas

condiciones habituales de flujo másico,  $m$ , diámetro interno,  $D$  y coeficiente de rugosidad,  $e$ .

SET A se refiere a las condiciones que garantizan que la densidad del fluido transportado sea superior a  $800 \text{ kg}\cdot\text{m}^{-3}$  y SET B a las que garantizan que la presión en el interior de la tubería esté por encima de 9 MPa (valor promedio entre los límites inferior y superior del rango encontrado en la bibliografía para las  $P_{min}$  de transporte: 7.5-11 MPa).

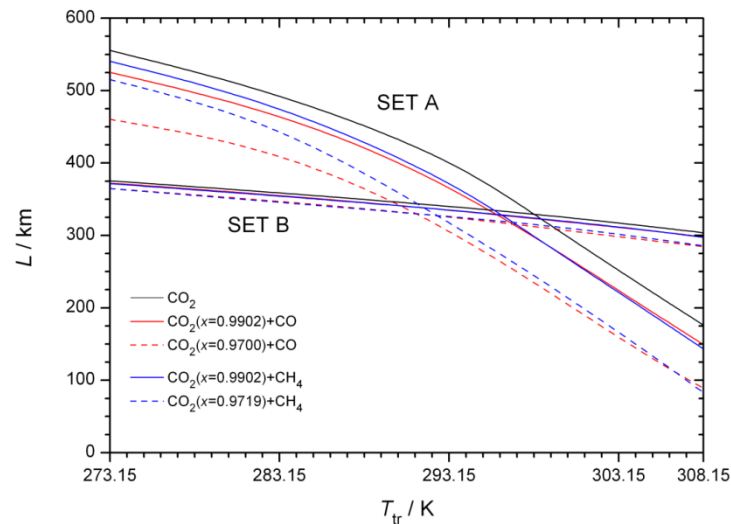


Figura 28. Distancias máximas de represurización,  $L$ , frente a temperaturas de transporte,  $T_{tr}$ , para  $\text{CO}_2$  puro y las mezclas  $\text{CO}_2+\text{CO}$  y  $\text{CO}_2+\text{CH}_4$ . Set A:  $L$  requerido para mantener la densidad del fluido por encima de  $800 \text{ kg}\cdot\text{m}^{-3}$ . Set B:  $L$  requerido para mantener la presión por encima de 9.0 MPa. Flujo másico elegido  $m = 317 \text{ kg}\cdot\text{s}^{-1}$ , diámetro interno de la tubería  $D = 0.508 \text{ m}$  y coeficiente de rugosidad  $e = 4.6 \times 10^{-5} \text{ m}$  para una tubería con una presión inicial de 20.0 MPa.

Se puede observar que cuando se trabaja con el objetivo de mantener la presión que garantice una densidad mínima,  $P_{min}^{800}$ , la distancia máxima de represurización,  $L$ , es más sensible al tipo y concentración de impurezas a bajas  $T$  y disminuye mucho al aumentar la temperatura de trabajo. Por otro lado,  $L$  apenas varía cuando se opera a  $P_{min} = 9.0$  MPa mostrando un comportamiento más estable.

Para las impurezas estudiadas dependiendo de la composición del fluido a  $T = 283.15 \text{ K}$ :

$$\text{SET A } ( P_{min}^{800} ) \quad \Rightarrow L = \mathbf{420-497} \text{ km}$$

$$\text{SET B } ( P_{min} = 9.0 \text{ MPa} ) \Rightarrow L = \mathbf{346-359} \text{ km}$$

#### E.1.4. Potencia de las estaciones de recompresión, $W$ .

Las presiones de entrada y de salida y el tipo de fluido a represurizar determinan la potencia requerida para las estaciones de recompresión,  $W$ . En la Figura 29 se observa la influencia que ejercen las impurezas (tipo y concentración) en  $W$  a una temperatura típica en la fase de transporte,  $T = 283.15 \text{ K}$ , y cuando la presión de salida es  $P_{m\acute{a}x} = 20$

MPa. El cálculo se muestra para las dos formas de operar que estamos considerando, la mejor opción dependerá del tipo de red de tuberías que se esté operando.

Para las impurezas estudiadas ( $x_{\text{CO}_2} = 0.9700 - 0.9960$ ) a  $T = 283.15 \text{ K}$  y dependiendo de la composición del fluido :

Represurización para densidad de  $800 \text{ kg}\cdot\text{m}^{-3}$   $\Rightarrow W = 7\text{-}7.9 \text{ MW}$

Represurización hasta  $9.0 \text{ MPa}$   $\Rightarrow W = 5.3\text{-}5.5 \text{ MW}$

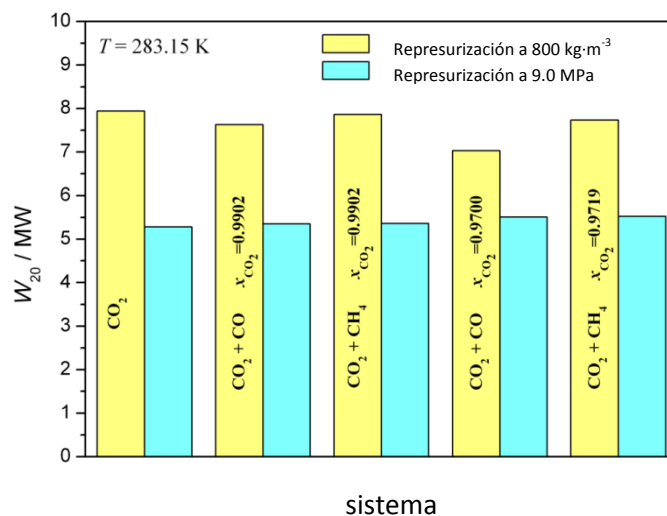


Figura 29. Máxima distancia de represurización,  $L$ , para  $\text{CO}_2$  puro y las mezclas  $\text{CO}_2+\text{CO}$  y  $\text{CO}_2+\text{CH}_4$  a  $T_{tr} = 283.15 \text{ K}$ . Amarillo:  $L$  para mantener la densidad del fluido por encima de  $800 \text{ kg}\cdot\text{m}^{-3}$ . Azul:  $L$  para mantener la presión por encima de  $9.0 \text{ MPa}$ . Flujo másico elegido  $m = 317 \cdot \text{kg}\cdot\text{s}^{-1}$ , diámetro interno de la tubería  $D = 0.508 \text{ m}$  y coeficiente de rugosidad  $e = 4.6 \cdot 10^{-5} \text{ m}$  para una tubería con una presión inicial de  $20.0 \text{ MPa}$ .

#### E.1.5. Diámetro interno de la tubería, $D$ .

El cálculo de este factor ha sido realizado para unas condiciones estándar de caída de presión y rugosidad y abarcando un rango de capacidad de aproximadamente  $10 \text{ Mt/año}$ . La Figura 30 muestra como para un diámetro determinado, el flujo másico transportado decrece a medida que la presión disminuye y la temperatura o la concentración de las impurezas aumentan.

En el caso más desfavorable (alta temperatura, alta concentración de impurezas y baja presión), la mayor diferencia entre el diámetro de la tubería calculado para el  $\text{CO}_2$  puro y las mezclas estudiadas, es de  $27 \text{ mm}$  (se corresponde con la mezcla  $\text{CO}_2+\text{CO}$  con  $x_{\text{CO}_2} = 0.9700$  a  $T = 308.15 \text{ K}$  y  $P = 9.0 \text{ MPa}$ ), lo que se traduce en un aumento de masa de tubería de  $11 \text{ toneladas}$  de acero por kilómetro de tubería.

$D$  (Mezcla  $\text{CO}_2 + \text{CO}$   $x_{\text{CO}_2} = 0.9700$ ) =  $D$  ( $\text{CO}_2$  puro) + **27 mm**  $\Rightarrow$  Aumento masa tubería standard = + **11 Tn/km**.

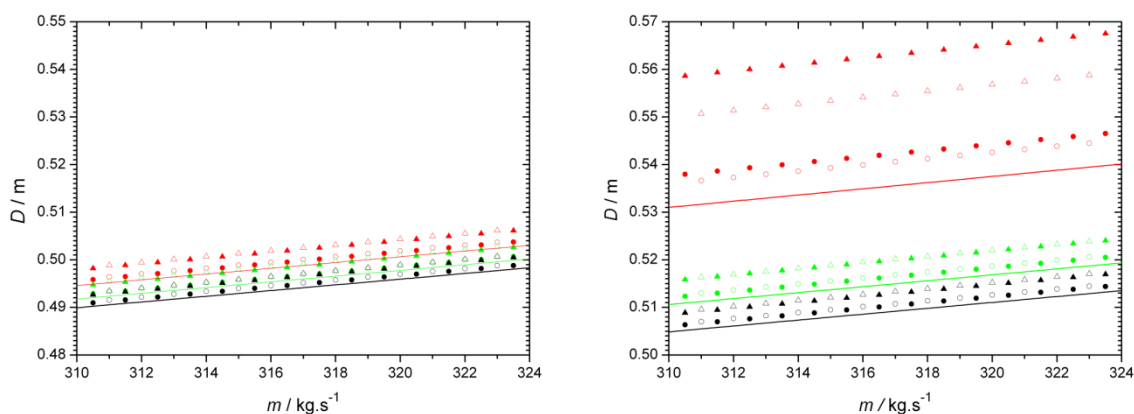


Figura 30. Diámetro interno de la tubería,  $D$ , frente a flujo másico (capacidad),  $m$ , para  $\text{CO}_2$  puro y las mezclas  $\text{CO}_2+\text{CO}$  y  $\text{CO}_2+\text{CH}_4$  a (a) 273.15 K y (b) 308.15 K a varias presiones,  $P$ . El coeficiente de rugosidad se ha fijado como  $e = 4.6 \cdot 10^{-5}$  m y se ha utilizado un valor promedio de caída de presión de  $33 \text{ Pa} \cdot \text{m}^{-1}$ . Rojo,  $P = 9.0 \text{ MPa}$ , Verde,  $P = 15.0 \text{ MPa}$ , Negro,  $P = 20.0 \text{ MPa}$ ; Líneas sólidas,  $\text{CO}_2$ ; Símbolos sólidos,  $\text{CO}_2+\text{CO}$ ; Símbolos en blanco,  $\text{CO}_2 + \text{CH}_4$ ; Círculos,  $x_{\text{CO}_2} \cong 0.99$ ; Triángulos,  $x_{\text{CO}_2} \cong 0.97$ .

## E.2.) Influencia del $\text{CH}_4$ Y $\text{CO}_2$ en la inyección y el del almacenamiento del $\text{CO}_2$ antropogénico.

El efecto de las impurezas en el  $\text{CO}_2$  almacenado depende del tipo de reservorio y de las interacciones entre el  $\text{CO}_2$  inyectado y las sustancias presentes previamente en el almacenamiento. En el caso del metano puede ser una impureza del  $\text{CO}_2$  antropogénico y estar también presente en el almacenamiento antes de la inyección.

Los parámetros seleccionados para evaluar la influencia de la presencia del  $\text{CO}$  y del  $\text{CH}_4$  en la inyección y almacenamiento, recogidos en la Tabla 9, son: parámetro de solubilidad,  $\delta$ , capacidad de almacenamiento,  $M$ , velocidad ascensional de la pluma en acuíferos salinos,  $v$ , y flujo de permeación,  $\dot{M}$ . En el caso de los tres últimos se han obtenido valores normalizados con respecto a los correspondientes al  $\text{CO}_2$  puro.

Tabla 9. Resumen de las ecuaciones de los parámetros empleados para evaluar la influencia de las impurezas en la inyección y el almacenamiento de CO<sub>2</sub> antropogénico.

Parámetros	Fórmula	Símbolos
Parámetro de solubilidad, $\delta$	$\delta = \left( \frac{-E(T)}{V(T,P)} \right)^{1/2}$ $\delta = \pi^{1/2}$ $\pi = \left( \frac{\partial U}{\partial V} \right)_T = T \left( \frac{\partial P}{\partial T} \right)_V - P = T \frac{\alpha_P}{\kappa_T} - P$	$(-E/V)$ : densidad de energía de cohesiva $\pi_i$ : presión interna $\alpha_P$ : expansividad isobárica $\kappa_T$ : compresibilidad isotérmica
Capacidad de almacenamiento normalizada, $M/M_0$	$\frac{M}{M_0} = \frac{\rho}{\rho_0 \left[ 1 + \sum_i \left( \frac{m_i}{m_0} \right) \right]}$	$m_i/m_0$ : relación de la masa de impureza $i$ con respecto a la masa de CO <sub>2</sub> en la mezcla $\rho$ y $\rho_0$ : densidad de la mezcla y del fluido puro respectivamente
Velocidad ascensional de la pluma normalizada, $v/v_0$	$\frac{v}{v_0} = \frac{F/(\rho\eta)}{F_0/(\rho_0\eta_0)} = \frac{(\rho_{salmuera} - \rho)(\rho_0\eta_0)}{(\rho_{salmuera} - \rho_0)(\rho\eta)}$	$m_i/m_0$ : relación de la masa de impureza $i$ con respecto a la masa de CO <sub>2</sub> en la mezcla $\rho$ y $\rho_0$ : densidad de la mezcla y del fluido puro respectivamente $\eta$ y $\eta_0$ : viscosidad de la mezcla y del fluido puro respectivamente $F$ y $F_0$ : fuerza de flotación de la mezcla y del fluido puro respectivamente $\rho_{salmuera}$ : densidad de la salmuera
Flujo de permeación normalizado, $\dot{M}/\dot{M}_0$	$\frac{\dot{M}}{\dot{M}_0} = \frac{\rho \left( \frac{\eta_0}{\eta} \right)}{\rho_0 \left[ 1 + \sum_i \left( \frac{m_i}{m_0} \right) \right]}$	$m_i/m_0$ : relación de la masa de impureza $i$ con respecto a la masa de CO <sub>2</sub> en la mezcla $\rho$ y $\rho_0$ : densidad de la mezcla y del fluido puro respectivamente $\eta$ y $\eta_0$ : viscosidad de la mezcla y del fluido puro respectivamente

### E.2.1. Parámetro de solubilidad, $\delta$

Debido a los valores de temperatura y presión en el interior de los reservorios, los fluidos confinados se encuentran en estado supercrítico y por tanto una de sus principales características es su gran capacidad de disolución.  $\delta$  ha sido ampliamente utilizado para predecir de manera semicuantitativa el comportamiento de mezclas líquidas<sup>7, 38, 39, 99</sup> y de fluidos supercríticos ligeramente polares.<sup>4</sup>



En este trabajo, hemos empleado el parámetro de solubilidad para estudiar las interacciones entre el fluido inyectado (considerado como el disolvente) y otras sustancias presentes en el reservorio. Los parámetros de solubilidad para CO<sub>2</sub> puro y para las mezclas de composición  $x_{\text{CO}_2} = 0.9902$  y  $x_{\text{CO}_2} = 0.9700$  correspondientes al sistema CO<sub>2</sub> + CO a tres temperaturas, se muestran en la Figura 31.

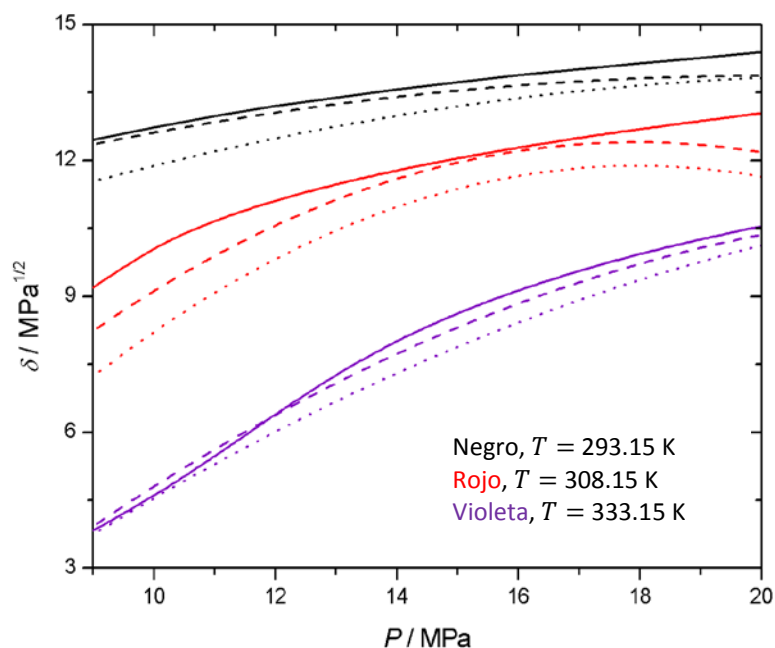


Figura 31. Parámetros de solubilidad,  $\delta$ , frente a presión para el CO<sub>2</sub> puro y la mezcla CO<sub>2</sub>+CO a varias temperaturas. Líneas sólidas, CO<sub>2</sub> puro; líneas discontinuas,  $x_{\text{CO}_2} = 0.9902$ ; líneas punteadas,  $x_{\text{CO}_2} = 0.9700$ .

Como se puede observar, la presencia de CO en el CO<sub>2</sub> antropogénico provoca una disminución de  $\delta$  en comparación con el CO<sub>2</sub> puro, reduciendo el poder de disolución del fluido y por lo tanto dificultando su captura. El mismo efecto se observa para el sistema CO<sub>2</sub>+CH<sub>4</sub>. Para las condiciones estudiadas en esta Tesis, el parámetro de solubilidad disminuye al aumentar la temperatura y disminuir la presión. Los valores obtenidos para el parámetro de solubilidad son consistentes con los encontrados en la literatura para la mezcla CO<sub>2</sub>+CO a 333.15K<sup>15</sup> aunque no son directamente comparables debido a las diferentes composiciones estudiadas.

Allada y colaboradores<sup>4</sup> sugieren que el parámetro de solubilidad es la clave determinante de la solubilidad en los disolventes supercríticos, y han sido capaces de unificar diversos comportamientos de los disolventes independientemente de la temperatura, la presión y de su naturaleza. Además, diferentes autores<sup>15</sup> apuntan a que la densidad es la propiedad que más influencia tiene en la capacidad de disolución de los fluidos densos.

La Figura 32 muestra  $\delta$  frente a  $\rho$  para CO<sub>2</sub> puro, seis mezclas de este trabajo y otras recogidas en la literatura.<sup>15</sup> El gráfico muestra una buena correlación  $\delta - \rho$  dentro del rango de densidad representado. Esto significa que sistemas con diferente  $T$  o  $P$  pero con la misma densidad, tendrán el mismo parámetro de solubilidad y que por lo tanto, la capacidad de solubilización del CO<sub>2</sub> inyectado puede ser conocida a partir de su densidad en las condiciones de almacenamiento.

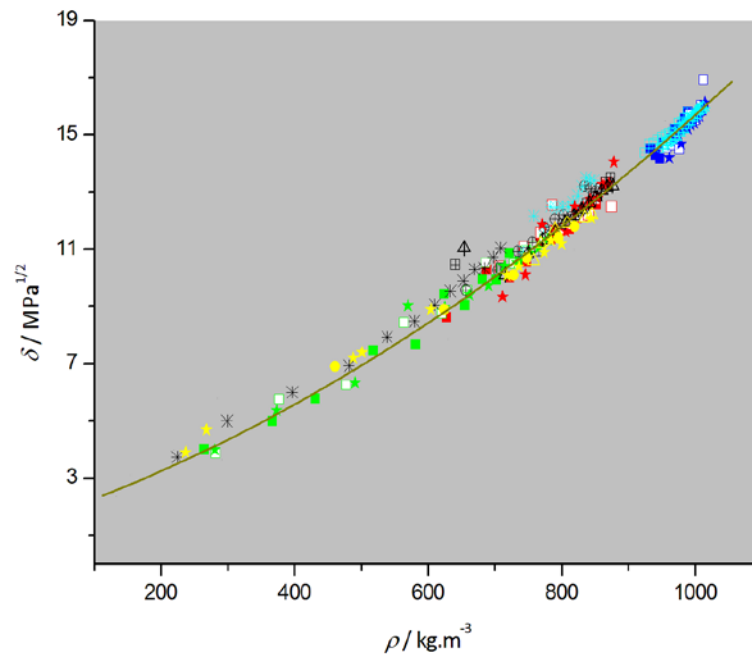


Figura 32. Parámetro de solubilidad,  $\delta$ , frente a densidad,  $\rho$ , para CO<sub>2</sub> puro (línea); mezclas CO<sub>2</sub>+CO con  $x_{\text{CO}_2}=0.9700$  (■),  $x_{\text{CO}_2}=0.9902$  (□) and  $x_{\text{CO}_2}=0.9930$  (★) a 273.15 K (azul), 304.21 K (rojo) and 323.15 K (verde); mezclas CO<sub>2</sub>+CH<sub>4</sub> con  $x_{\text{CO}_2}=0.8525$  (\*),  $x_{\text{CO}_2}=0.9719$  (⊕) y  $x_{\text{CO}_2}=0.9932$  (⊞) a 273.15 K (cian) y 304.21 K (negro); CO<sub>2</sub>+CO (▲), CO<sub>2</sub>+H<sub>2</sub> (●) y mezclas CO<sub>2</sub>+CO+H<sub>2</sub> (★)(amarillo).<sup>15</sup>

### E.2.2. Capacidad de almacenamiento normalizada, $M/M_0$

Este parámetro depende de la composición, temperatura y presión de manera que la presencia de impurezas no condensables reduce esta capacidad sobre todo si nos encontramos en unas condiciones cercanas a las críticas de la mezcla (Figura 33). Por ejemplo, una cantidad del 15% de CH<sub>4</sub> reduce  $M/M_0$  hasta aproximadamente 0.35 a 308.15 K y 8.5 MPa, lo que implica que un reservorio relativamente poco profundo no sería adecuado para almacenar corrientes con un alto nivel de este tipo de impurezas.

En la Figura 33 donde se representa  $M/M_0$  versus  $P$  a varias temperaturas para CO<sub>2</sub>+CO y CO<sub>2</sub>+CH<sub>4</sub> con  $x_{\text{CO}_2}=0.9700$ , se observa que la disminución máxima se obtiene cerca del punto crítico del CO<sub>2</sub> antropogénico ( $M/M_0 \cong 0.44$  para CO<sub>2</sub>+CO a 304.21 K y 7.5

MPa). Un aumento en la temperatura disminuye la magnitud del mínimo y lo desplaza a presiones mayores.

$$\text{CO}_2 + \text{CO} (x_{\text{CO}_2} \cong 0.97); T = 304.21 \text{ K}; P \cong 7.5 \text{ MPa} \quad \Rightarrow \left(\frac{M}{M_0}\right)_{\min} \cong \mathbf{0.44}$$

$$\text{CO}_2 + \text{CO} (x_{\text{CO}_2} \cong 0.97); T = 343.15 \text{ K}; P \cong 14.1 \text{ MPa} \quad \Rightarrow \left(\frac{M}{M_0}\right)_{\min} \cong \mathbf{0.89}$$

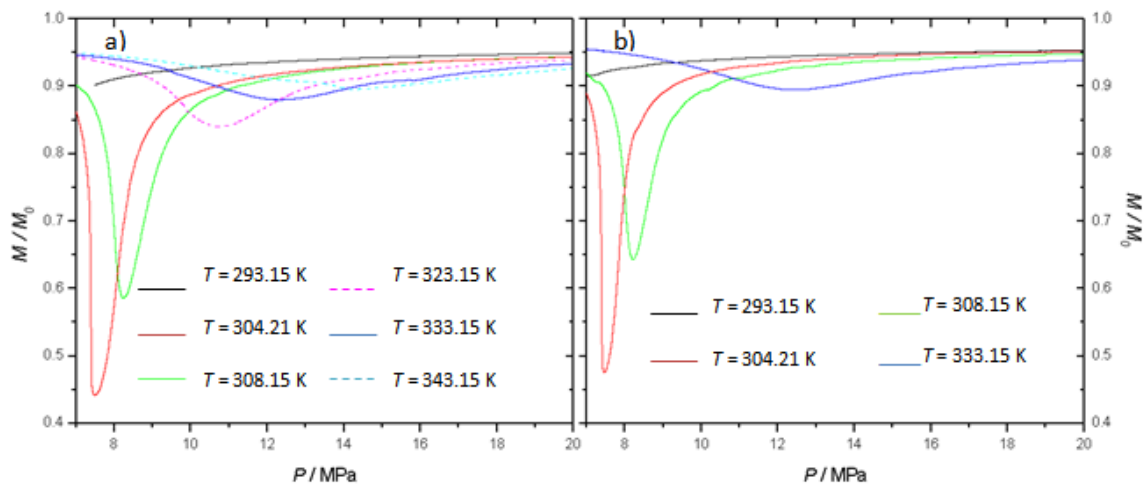


Figura 33. Capacidad normalizada de almacenamiento,  $M/M_0$ , frente a la presión a varias temperaturas para las mezclas (a)  $\text{CO}_2+\text{CO}$  ( $x_{\text{CO}_2} = 0.9700$ ) y (b)  $\text{CO}_2+\text{CH}_4$  ( $x_{\text{CO}_2} = 0.9719$ ).

A medida que la profundidad de inyección aumenta, la influencia del tipo de impureza en la capacidad de almacenamiento disminuye.

El CO afecta de manera más negativa que el  $\text{CH}_4$  a la masa de  $\text{CO}_2$  antropogénico que puede almacenarse, de forma que para la misma masa de fluido sería necesaria más presión para confinar el sistema  $\text{CO}_2+\text{CO}$  que el  $\text{CO}_2+\text{CH}_4$ . La eficiencia en el almacenamiento puede mejorarse si la presión de inyección se encuentra bastante por encima de los valores mínimos que se representan. Para el caso de reservorios cerrados, este valor de presión debe encontrarse dentro de los rangos de sobrepresiones permitidos. Para formaciones abiertas, una posible opción sería incrementar la profundidad de inyección en el almacenamiento.

### E.2.3. Velocidad ascensional de la pluma normalizada en acuíferos salinos, $v/v_0$

Si el reservorio es un acuífero salino, el fluido almacenado experimenta una fuerza de flotación ascendente que depende de la diferencia de densidades entre el fluido y la salmuera.<sup>88</sup> La velocidad con que se desplazará el fluido es directamente proporcional a la fuerza de flotación e inversamente proporcional a su viscosidad. A  $T \geq 304.21 \text{ K}$  (Figura 34)  $v/v_0$  presenta un máximo de mayor magnitud para la impureza CO.

$$\text{CO}_2 + \text{CO} (x_{\text{CO}_2} \cong 0.97); T = 304.21 \text{ K}; P \cong 7.5 \text{ MPa}; \rho_{\text{salmuera}} = 1025 \text{ kg}\cdot\text{m}^{-3} \Rightarrow$$

$$\left(\frac{v}{v_0}\right)_{\text{máx}} \cong 9.2$$

$$\text{CO}_2 + \text{CH}_4 (x_{\text{CO}_2} \cong 0.97); T = 304.21 \text{ K}; P \cong 7.5 \text{ MPa}; \rho_{\text{salmuera}} = 1025 \text{ kg}\cdot\text{m}^{-3} \Rightarrow$$

$$\left(\frac{v}{v_0}\right)_{\text{máx}} \cong 7.7$$

Los máximos para cada temperatura se encuentran a presiones dentro del rango de profundidades de los acuíferos salinos.<sup>71</sup> La presencia de CO o CH<sub>4</sub> conduce a un incremento en la velocidad ascendente de la pluma, lo que se hace significativo cerca del punto crítico del fluido, resultando por tanto en una disminución del contacto del CO<sub>2</sub> con la salina y por tanto en un descenso del poder de disolución. La propagación lateral de la pluma también disminuye y como consecuencia lo hace la cantidad de fluido atrapado en los poros de la roca. Estos efectos reducen la seguridad en el almacenamiento del CO<sub>2</sub> y cobran más importancia cerca de la roca de sellado, a profundidades menores aumentando el riesgo de posibles fugas. Un incremento en la densidad de la salmuera reduce tanto  $F/F_0$  como  $v/v_0$ . (Figura 34).

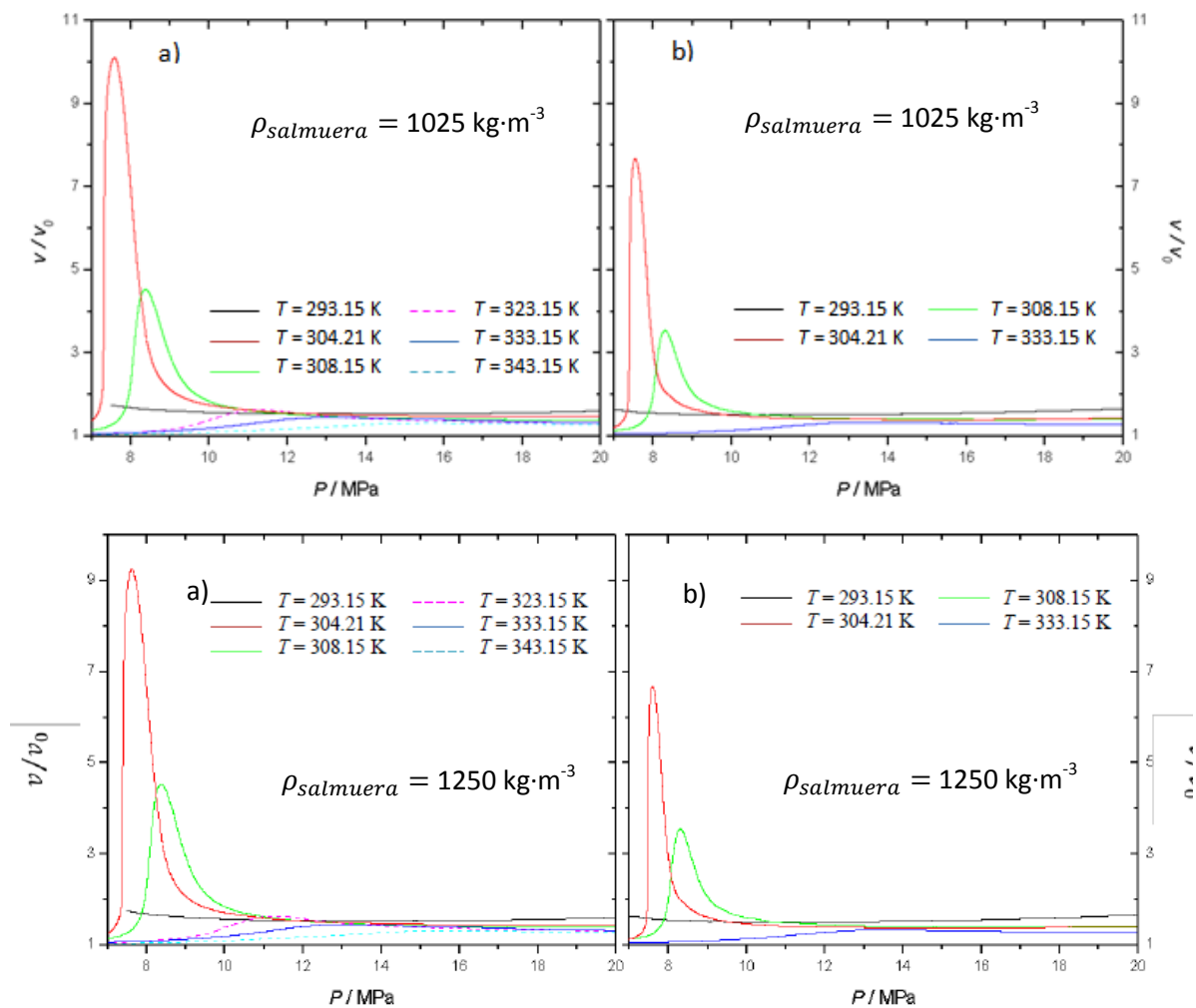


Figura 34. Velocidad ascensorial de la pluma normalizada,  $v/v_0$ , frente a la presión a varias temperaturas para las mezclas (a)  $\text{CO}_2 + \text{CO}$  ( $x_{\text{CO}_2} = 0.9700$ ) y (b)  $\text{CO}_2 + \text{CH}_4$  ( $x_{\text{CO}_2} = 0.9719$ )

#### E.2.4. Flujo de permeación normalizado, $\dot{M}/\dot{M}_0$

La inyectividad relativa de la corriente impura de CO<sub>2</sub> depende del efecto de las impurezas, de la temperatura, de la presión, de la densidad y la viscosidad.  $\dot{M}$  se ve reducida como resultado de una disminución de la densidad de estas mezclas en relación con el CO<sub>2</sub> puro; sin embargo, debido a la compensación por el aumento de la viscosidad, la reducción es menor que en la capacidad de almacenamiento discutida anteriormente. En los sistemas incluidos en este trabajo,  $\rho < \rho_0$  y  $\eta < \eta_0$  pero debido a los valores relativos de  $\rho/\rho_0$  y  $\eta_0/\eta$ , los valores obtenidos para  $\dot{M}/\dot{M}_0$  pueden ser mayores o menores que la unidad. Las mayores diferencias se encuentran en las proximidades del punto crítico y se observa que la influencia del CO es mayor que la del CH<sub>4</sub> para este parámetro (Figura 35).

$$\text{CO}_2 + \text{CO} (x_{\text{CO}_2} \cong 0.97); T = 304.21 \text{ K}; P \cong 8.0 \text{ MPa} \quad \Rightarrow \left(\frac{\dot{M}}{\dot{M}_0}\right)_{\text{máx}} \cong 1.25$$

$$\text{CO}_2 + \text{CH}_4 (x_{\text{CO}_2} \cong 0.97); T = 304.21 \text{ K}; P \cong 8.0 \text{ MPa} \quad \Rightarrow \left(\frac{\dot{M}}{\dot{M}_0}\right)_{\text{máx}} \cong 1.17$$

Al aumentar la presión el efecto de la temperatura disminuye tendiendo  $\dot{M}/\dot{M}_0$  a la unidad en el rango de temperatura estudiado.

Por otro lado, la presencia de impurezas no condensables en la etapa de inyección tiene como consecuencia la necesidad de incrementar la presión de cabeza debido a la disminución de la presión hidrostática en el pozo de inyección.<sup>85</sup>

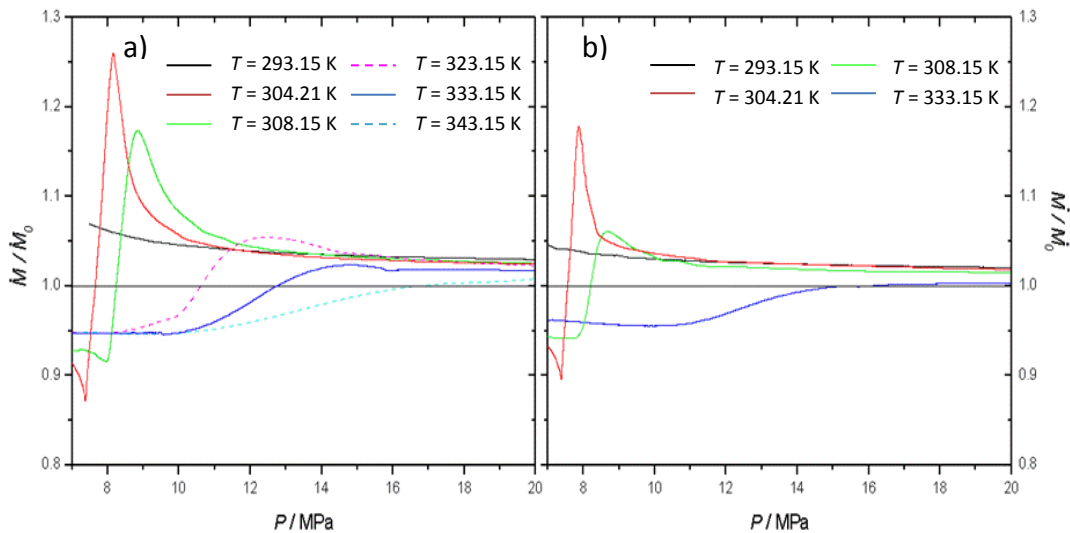


Figura 35. Flujo de permeación normalizado,  $\dot{M}/\dot{M}_0$ , frente a la presión a varias temperaturas para las mezclas (a) CO<sub>2</sub>+CO ( $x_{\text{CO}_2} = 0.9700$ ) y (b) CO<sub>2</sub>+CH<sub>4</sub> ( $x_{\text{CO}_2} = 0.9719$ ).



**CONCLUSIONES  
FINALES**







## 5. CONCLUSIONES FINALES

### 1.

Se ha elaborado el procedimiento para la determinación experimental de la densidad de fluidos puros y mezclas a diferentes presiones y temperaturas. Para ello, se ha utilizado CO<sub>2</sub>, etano y propano, y el sistema CO<sub>2</sub>+etano. La comparación de los valores obtenidos con los calculados usando las EoS de referencia así como con la bibliografía, confirma la calidad de las medidas experimentales. La precisión calculada en la medida de la densidad de compuestos puros, expresada como desviación relativa promedio, es  $MRD_{\rho} = 0.13\%$ . Para las mezclas binarias, las desviaciones obtenidas fueron  $MRD_{\rho} = 0.70\%$  para  $P=0.1-20$  MPa y  $MRD_{\rho} = 0.20\%$  en el rango hasta 70 MPa. La incertidumbre expandida ( $k = 2$ ) en la medida de la densidad y su repetibilidad para las mezclas estudiadas fueron:  $U(\rho) = 0.35-0.80$  kg·m<sup>-3</sup> y  $\bar{S}_{\rho}^r = 0.13\%$ , respectivamente.

Se calcularon para CO<sub>2</sub> y etano las propiedades derivadas de la densidad:  $\kappa_T$ ,  $\alpha_P$ , y  $\pi_i$ . La dependencia de las dos primeras con la temperatura y la presión es la esperada: los valores varían mucho en las cercanías del punto crítico, donde son divergentes, pero apenas cuando nos alejamos de él. Los valores de la presión interna para el CO<sub>2</sub> son más altos que los del etano, consecuencia del importante momento cuadrupolar que presenta el CO<sub>2</sub>.

### 2.

Se ha elaborado el procedimiento para la determinación experimental de la velocidad del sonido de fluidos puros (líquidos y gases comprimidos) a diferentes presiones y temperaturas. Se ha utilizado agua y etano y se ha calculado la precisión de las medidas comparando con las EoS de referencia para ambos fluidos. Las desviaciones obtenidas fueron:  $MRD_c(\text{H}_2\text{O}) = 0.06\%$  y  $MRD_c(\text{C}_2\text{H}_6) = 0.1\%$ .

A partir de los valores experimentales de velocidades del sonido y densidad se ha obtenido la compresibilidad isentrópica y la capacidad calorífica del etano. La desviación media relativa entre  $C_p$  calculada y la proporcionada por la EoS de referencia fue:  $MRD_{C_p}(\text{C}_2\text{H}_6) = 3\%$ .

Se ha puesto a punto la instalación para la medida de velocidades del sonido en mezclas mediante el estudio del sistema CO<sub>2</sub>+CH<sub>3</sub>OH con composiciones,

temperaturas y presiones elegidas para que incluyeran las condiciones de la tecnología CCS.

La incertidumbre estándar obtenida para este sistema es  $u_c=5.9 \cdot 10^{-4} \cdot c$ .

### 3.

Se han medido 54 isothermas  $P - \rho - T - x_{CO_2}$  para seis mezclas  $CO_2 + CH_4$  en los rangos de presión y temperatura que incluyen los estimados en el interior de las tuberías así como en los almacenamientos geológicos:  $x_{CO_2} \geq 0.85$ ;  $P = 0.1 - 20$  MPa;  $T = 253.15 - 333.15$  K. Para el sistema  $CO_2 + CO$ , se han determinado 50 isothermas  $P - \rho - T - x_{CO_2}$  correspondientes a cinco composiciones en los rangos:  $x_{CO_2} \geq 0.97$ ;  $P = 0.1 - 20$  MPa;  $T = 253.15 - 343.15$  K.

A partir de estos datos experimentales se han calculado: las presiones de rocío y de burbuja y las densidades de las fases en el ELV para cada mezcla a las temperaturas subcríticas,  $P_r - P_b - \rho_V - \rho_L$ ; propiedades derivadas,  $\alpha_p$ ,  $\kappa_T$  y  $\pi_i$ , para todas las isothermas; y los volúmenes molares de exceso,  $V_m^E$ , y volúmenes molares parciales,  $\bar{V}_i$ , en la región crítica.

Los valores obtenidos se han comparado con los escasos datos existentes en la bibliografía para estos sistemas en las condiciones estudiadas, encontrándose buenas concordancias en aquellos casos comparables.

### 4.

Se ha realizado la modelización de ambos sistemas con tres Ecuaciones de Estado de diferente tipo: (i) PR, ecuación cúbica; (ii) GERG-2008, ecuación basada en la aproximación multifluido; y (iii) PC-SAFT, ecuación basada en las teorías de la perturbación.

Las EoS se usaron en sus formulaciones originales pero en el caso de PC-SAFT, además se reajustaron los parámetros con el objetivo de mejorar la predicción en la zona crítica. De los resultados concluimos que las tres EoS predicen adecuadamente el comportamiento volumétrico y de fase de los sistemas  $CO_2 + CO$  y  $CO_2 + CH_4$  en las condiciones estudiadas. Las desviaciones promedio obtenidas fueron:

PR EoS:	$MRD_\rho < 3 \%$ ;	$MRD_{P_r, P_b} < 1 \%$ .
GERG-2008 EoS:	$MRD_\rho < 1 \%$ ;	$MRD_{P_r, P_b} < 2 \%$ .
PC-SAFT EoS:	$MRD_\rho < 2 \%$ ;	$MRD_{P_r, P_b} < 1 \%$ .

## 5.

Se ha realizado un estudio teórico de las interacciones entre las moléculas de  $\text{CO}_2$  y las moléculas de  $\text{CH}_4$  o  $\text{CO}$  utilizando el concepto de función de Krichevskii y la teoría de Kirkwood-Buff. Se calcularon diferentes parámetros que indican cómo se encuentran las moléculas dentro del sistema tales como: parámetro de Krichevskii,  $A_{Kr}$ ; volumen parcial molar a dilución infinita,  $\bar{V}_2^\infty$ ; tamaño de clúster,  $N_1^{exc}$  y número de coordinación de exceso,  $N_{exc}^\infty$ . El signo de estos parámetros permite concluir la afinidad de las moléculas soluto-solvente; así, en nuestros sistemas se observa un comportamiento débilmente atractivo.

## 6.

Se ha evaluado la influencia de las impurezas  $\text{CH}_4$  y  $\text{CO}$  en el transporte de  $\text{CO}_2$  por ceoducto a través de la cuantificación de la modificación de los límites del ELV y del cálculo de varios parámetros tales como: presión mínima operacional,  $P_{min}$ , caída de presión a lo largo de la tubería,  $P(d)$ , distancia máxima de represurización,  $L$ , potencia de las estaciones de recompresión,  $W$  y diámetro interno de la tubería,  $D$ .

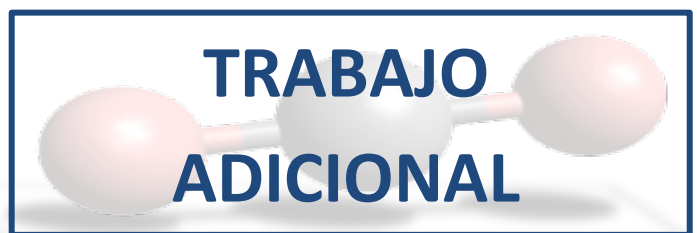
La presencia de las impurezas, ambos gases no-condensables, aumenta la presión de burbuja y, por lo tanto, la presión de trabajo mínima requerida para un óptimo transporte del fluido. Por otro lado, el efecto en los parámetros se hace más pronunciado al aumentar la temperatura y disminuir la presión.

Se ha evaluado la influencia de las impurezas  $\text{CH}_4$  y  $\text{CO}$  en las etapas de almacenamiento e inyección. Se ha calculado el parámetro de solubilidad,  $\delta$ , para  $\text{CO}_2 + \text{CO}$  y  $\text{CO}_2 + \text{CH}_4$  y comparado con el de otras mezclas observando que sistemas con diferente composición, temperatura o presión pero con la misma densidad, tienen el mismo parámetro de solubilidad y por lo tanto, la misma capacidad de solubilización del fluido inyectado. El valor obtenido para las mezclas es menor que el del  $\text{CO}_2$  puro por lo que su presencia dificultará la retención del mismo en el reservorio.

Además, se han calculado los parámetros normalizados (relativos a una corriente de  $\text{CO}_2$  puro) siguientes: capacidad de almacenamiento,  $M$ ; velocidad de ascenso de la pluma,  $v$ ; y flujo de permeación,  $\dot{M}$ . De los resultados se puede concluir que la presencia de estas impurezas es perjudicial ya que disminuye la capacidad de almacenamiento y aumenta el riesgo de fuga en los acuíferos salinos.

En todos los casos, se ha observado que el efecto producido por la presencia de  $\text{CO}$  en el  $\text{CO}_2$  antropogénico es mayor que el originado por el  $\text{CH}_4$ .





**TRABAJO  
ADICIONAL**



## 6. TRABAJO ADICIONAL Y PERSPECTIVAS DE FUTURO

Como continuación lógica del trabajo presentado se plantea la determinación experimental de la velocidad del sonido en mezclas de interés en la Tecnología CCS. Estos valores, junto a las propiedades descritas anteriormente, permitirán el cálculo de otras propiedades termodinámicas tales como la capacidad calorífica y el coeficiente de Joule-Thomson.

La determinación experimental de la velocidad del sonido del CO<sub>2</sub> en estado denso presenta serias dificultades, debido a que tiene un valor de tiempo de relajación vibracional,  $\tau$ , extraordinariamente alto, asociado a un elevado coeficiente de absorción del sonido,  $\alpha$ . La adición de pequeñas cantidades de un compuesto adecuado, agente dopante, con tiempo de relajación pequeño reduce considerablemente el  $\tau$  del sistema permitiendo la determinación de  $c$  en condiciones adecuadas. En nuestra investigación hemos optado por el metanol como dopante ya que es químicamente compatible con los componentes de la instalación, son conocidas sus propiedades como modificador en procesos de extracción supercrítica y se trata de un compuesto que puede aparecer como impureza en el CO<sub>2</sub> antropogénico (Proceso Rectisol) o ser añadido para favorecer la operatividad del proceso (agente desecante e inhibidor de la formación de hidratos).

### i) Velocidad del sonido en el CO<sub>2</sub> puro

A partir de las medidas experimentales (Sección 4.1.B) de  $c$  de las mezclas ricas en CO<sub>2</sub> ( $x_{\text{CO}_2} > 0.95$ ) y extrapolando a  $x_{\text{CO}_2} = 1$ , hemos estimado los valores de  $c$  para el CO<sub>2</sub> puro. Para disponer de valores de la velocidad del sonido a las mismas temperaturas y presiones en cada fracción molar, los valores de  $c$  experimentales de cada isopleta e isoterma se han ajustado al siguiente polinomio:

$$(P - P^\#) = \sum_{i=1}^3 a_i (c - c^\#)^i \quad (\text{Ec. 39})$$

Donde  $P^\# = 70$  MPa y  $c^\#$  es la velocidad del sonido a  $P = P^\#$ .

Posteriormente, estos datos interpolados se han ajustado a una función cuadrática de la fracción molar:

$$c(x_{\text{CO}_2}) = c_0 + c_1(1 - x_{\text{CO}_2}) + c_2(1 - x_{\text{CO}_2})^2 \quad (\text{Ec. 40})$$

Donde  $c(x_{\text{CO}_2} = 1) = c_0$  es la velocidad del sonido en el  $\text{CO}_2$  puro. La incertidumbre standard relativa en el cálculo de  $c_0$  teniendo en cuenta el error experimental y el proveniente del análisis de regresión es  $u_r(c_0) = 0.14\%$ , muy inferior a la desviación que presenta la EoS de referencia en esta región<sup>89</sup>:  $MRD(c) = 2\%$ .

Los valores obtenidos (Figura 36) han sido comparados con los únicos datos experimentales que existen en el rango de presiones y temperaturas que cubren este trabajo,<sup>77</sup> con los obtenidos por Lin y Trusler<sup>64</sup> mediante extrapolación usando propano como dopante, y con los valores proporcionados por la EoS de referencia para el  $\text{CO}_2$  puro (Figura 37). Como puede observarse existe una gran concordancia, obteniendo unas desviaciones medias relativas:  $MRD(c) = 0.61, 0.28$  y  $0.42\%$ , respectivamente.

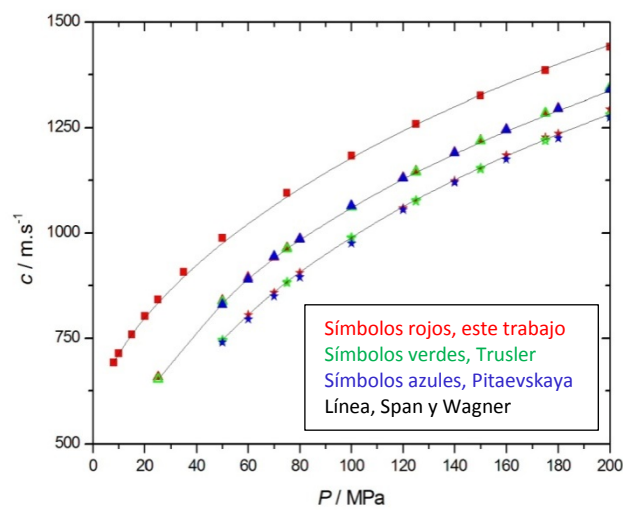


Figura 36. Velocidad del sonido,  $c$ , de  $\text{CO}_2$  puro frente a la presión,  $P$ , a varias temperaturas,  $T$ . ■,  $T = 263.15\text{ K}$ ; ▲,  $T = 298.15\text{ K}$ ; ★,  $T = 323.15\text{ K}$ .



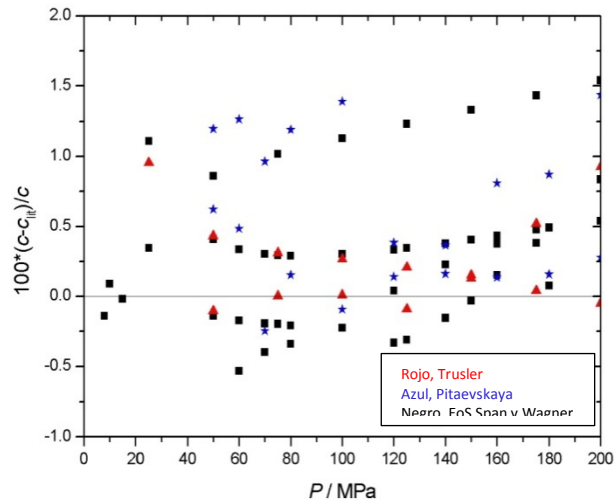


Figura 37. Comparación entre las velocidades del sonido para el  $\text{CO}_2$  puro obtenidas en este trabajo,  $c$ , y de la literatura,  $c_{lit}$ ,  $\blacktriangle$ , Trusler<sup>64</sup>;  $\star$ , Pitaevskaya<sup>77</sup>;  $\blacksquare$ , Span Wagner EoS<sup>89</sup>.

ii) Efecto del metanol como agente dopante.

Como hemos comentado en el apartado 4.1.B.1. de esta Memoria, las medidas acústicas son necesarias para un correcto estudio de riesgos durante la monitorización de los procesos de transporte y almacenamiento del  $\text{CO}_2$  antropogénico. Sin embargo, las especiales características del  $\text{CO}_2$  puro hacen que, en ciertas condiciones, sea imposible su determinación con fiabilidad. Añadir pequeñas cantidades de un compuesto adecuado puede posibilitar la determinación experimental de  $c$  al disminuir mucho el tiempo de relajación del fluido. Así, añadiendo únicamente un 1 % en mol, la señal experimental es nítida a la frecuencia de 5 MHz en un rango de presiones y temperatura considerable. Por otro lado, la pequeña variación observada de  $c$  con la concentración nos permitirá dopar el  $\text{CO}_2$  con más cantidad de metanol permitiéndonos un mayor rango de medida de  $c$  sin afectar apenas a su valor. En la Figura 38 se puede apreciar el error cometido al considerar las mezclas  $\text{CO}_2+\text{CH}_3\text{OH}$  como si fueran  $\text{CO}_2$  puro. Dopar hasta con un 5% en mol de metanol supone, en los rangos de  $P$  y  $T$  estudiados, una desviación media relativa del 0.40%, con una desviación máxima del 1.1%, de nuevo inferior a la incertidumbre de la propia EoS de referencia para el  $\text{CO}_2$ .

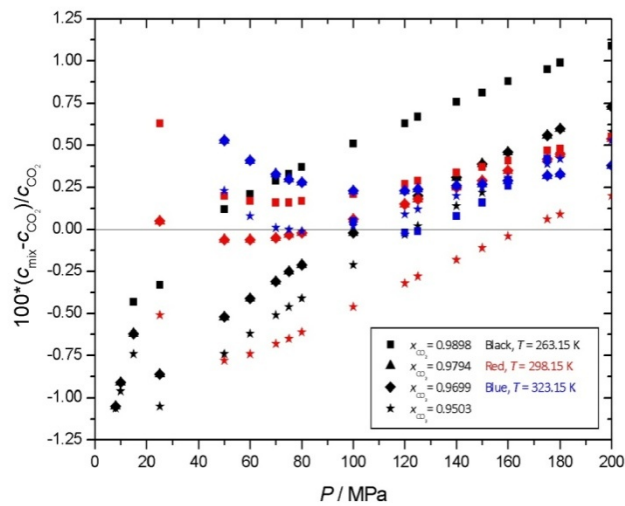


Figura 38. Comparación entre las mezclas de CO<sub>2</sub> estudiadas en este trabajo,  $c_{mix}$ , y las velocidades del sonido para el CO<sub>2</sub> puro a partir de la EoS de referencia,  $c_{CO_2}$ .

El trabajo adicional descrito ha permitido al grupo de investigación disponer en la actualidad de datos fiables de velocidades del sonido para los sistemas CO<sub>2</sub> + impurezas de interés para la tecnología CCS, mediante su dopaje con metanol. De otra forma, habría sido imposible abordar la investigación de una propiedad tan importante como es la velocidad del sonido dada la elevada concentración de CO<sub>2</sub> en los sistemas que han de ser estudiados.

**ANEXO**



## 7. ANEXO

### Desviación Media Relativa en la propiedad x

$$MRD(x) = \frac{100}{N} \sum_{i=1}^N \left| \frac{x_i^{exp} - x_i^{cal}}{x_i^{exp}} \right| \quad (\text{Ec. A.I})$$

Donde

- $x_i^{exp}$  Son los datos experimentales  
 $x_i^*$  Son los valores bibliográficos o los calculados  
 $N$  Es el número de puntos

### Desviación Estándar Media Relativa de la propiedad x

La desviación estándar media para la propiedad  $x$ ,  $\bar{S}_x^r$ , se ha calculado utilizando las siguientes ecuaciones:

$$\bar{S}_x^r = \frac{100}{N} \sum_{j=1}^N ({}_j S_x^r) \quad (\text{Ec. A.II})$$

Donde  $N$  es el número de puntos y  ${}_j S_x^r$  es la desviación estándar relativa en cada punto:

$${}_j S_x^r = \frac{{}_j S_x}{(1/n) \sum_{i=1}^n x_i^{exp}} \quad (\text{Ec. A.III})$$

Y  ${}_j S_x$  es la desviación estándar en cada punto:

$${}_j S_x = \sqrt{\frac{n \sum_{i=1}^n (x_i^{exp})^2 - \sum_{i=1}^n (x_i^{exp})^2}{n(n-1)}} \quad (\text{Ec. A.IV})$$

Siendo  $n$  el número de análisis para una  $T$  y  $P$  dadas.

### Incertidumbre

La incertidumbre expandida se ha calculado mediante las reglas de la ley de propagación de errores:

$$U(y) = ku_c(y) = k \left[ \sum_{i=1}^N \left( \frac{\partial f}{\partial x_i} \right)^2 u^2(x_i) \right]^{1/2} \quad (\text{Ec. A.V})$$

Donde

- $k$  Factor de cobertura ( $k = 2$  en este trabajo)

$u_c(y)$	Incertidumbre estándar combinada del valor estimado $y$
$N$	Número de puntos
$x_i$	Cada una de las variables de las que depende $y$
$(\partial f / \partial x_i)$	Coeficiente de sensibilidad de la variable de entrada $x_i$
$u^2(x_i)$	Cuadrado de la incertidumbre asociada a la variable de entrada $x_i$



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**APÉNDICE**



## 9. APÉNDICE

La normativa que regula la elaboración y defensa de Tesis Doctoral en la Universidad de Zaragoza indica que: *“Podrán optar por la presentación de tesis en la modalidad de compendio de publicaciones aquellos doctorandos que, previamente a la presentación de sus tesis y con la autorización expresa de su director o directores, tengan publicados o aceptados para su publicación, con fecha posterior a la del inicio de sus estudios de doctorado, un número mínimo de cuatro artículos con unidad temática, de los cuales tres habrán de estarlo en revistas científicas cuyo índice de impacto se encuentre incluido en la relación de revistas del Journal of Citation Reports”.*

Los artículos que recogen el trabajo realizado en esta tesis doctoral son cinco, todos ellos, se han publicado en revistas de conocido prestigio cuya temática, índice de impacto y posición (JCR) se indican a continuación.

Se presenta una copia de las 5 publicaciones y la renuncia de los co-autores no doctores a que estos trabajos puedan ser incluidos en otra tesis doctoral presentada en esta modalidad.

## 9.1. RELEVANCIA DE LAS PUBLICACIONES

### The Journal of Physical Chemistry B



Publicación Internacional que recoge estudios relacionados con macromoléculas, surfactantes, membranas, mecánica estadística y termodinámica. Los artículos experimentales que se admiten en esta publicación deben ir acompañados de modelización o simulación y de una profunda discusión.

El artículo publicado en esta revista es:

**Accurate Values of Some Thermodynamic Properties for Carbon Dioxide, Ethane, Propane, and Some Binary Mixtures.** *J. Phys. Chem. B*, **2011**, 115, 8216-8230.

Año de publicación: 2011

Categoría de JCR: Chemistry Physical: 32 de 130

Índice de Impacto: 3.696



Esta publicación recoge todo tipo de estudios relacionados con el medioambiente tales como modelización medioambiental, energía y medioambiente, procesos medioambientales, ecotoxicología y salud medioambiental humana.

Los artículos publicados en esta revista son:

**Influence of Methane in CO<sub>2</sub> Transport and Storage for CCS Technology.** *Environ. Sci. Technol.* **2012**, 46, 13016-13023.

Año de publicación: 2012

Categoría de JCR: Engineering, environmental: 2 de 42

Environmental, Science: 7 de 210

Índice de Impacto: 5.257

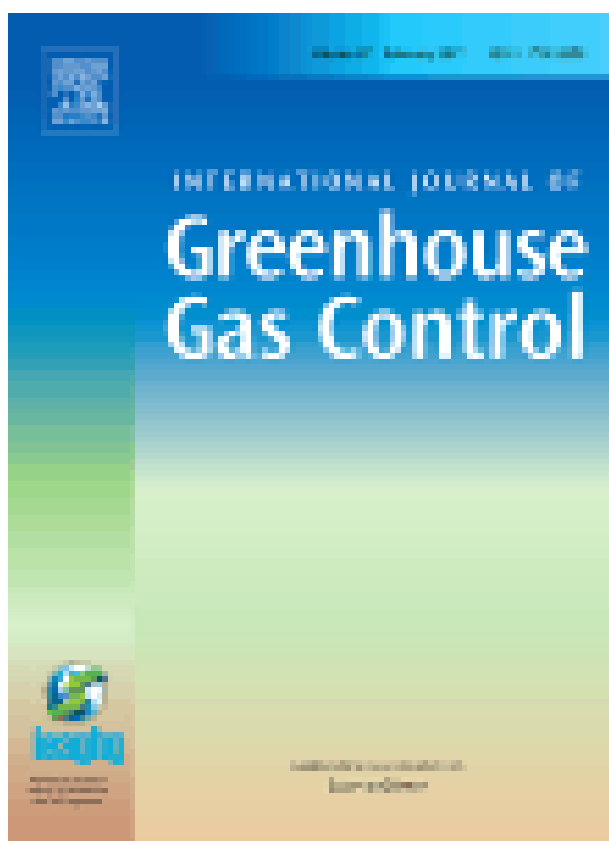
**Discussion of the Influence of CO and CH<sub>4</sub> in CO<sub>2</sub> Transport, Injection and Storage for CCS Technology.** *Environ. Sci. Technol.* **2014**, 48, 10984-10992.

Año de publicación: 2014

Categoría de JCR: Engineering, environmental: 3 de 47

Environmental, Science: 10 de 223

Índice de Impacto: 5.330



Esta publicación se centra en desarrollos científicos y de ingeniería enfocados al control de gases de efecto invernadero a través de su captura y almacenamiento en el sector energético y otras fuentes industriales. Entre los temas más comunes se encuentran la captura, transporte y almacenamiento geológico del CO<sub>2</sub> así como otras alternativas de almacenamiento.

El artículo publicado en esta revista es:

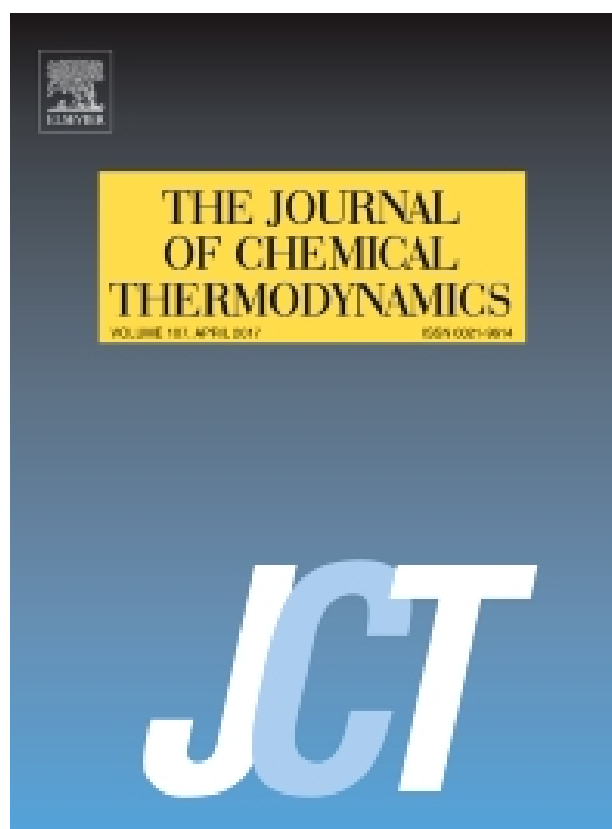
**Influence of methane and carbon monoxide in the volumetric behaviour of the anthropogenic CO<sub>2</sub>: Experimental data and modelling in the critical region.** *International Journal of Greenhouse Gas Control*, 2013, 18, 264-276.

Año de publicación: 2013

Categoría de JCR: Energy & Fuels: 16 de 83

Engineering, environmental: 8 de 46

Índice de Impacto: 3.821



Revista especializada en los equilibrios termodinámicos y propiedades de transporte de los sistemas químicos y publica trabajos relacionados con gases, líquidos, sólidos, polímeros, mezclas, disoluciones e interfaces. Los métodos experimentales deben describirse con suficiente detalle como para permitir una evaluación crítica de la exactitud de los resultados.

El artículo publicado en esta revista es:

**Thermodynamic properties of a CO<sub>2</sub>-rich mixture (CO<sub>2</sub>+CH<sub>3</sub>OH) in conditions of interest for carbon dioxide capture and storage technology and other applications.** *J. Chem. Thermodynamics*, **2016**, 98, 272-281.

Año de publicación: 2015

Categoría de JCR: Thermodynamics: 13 de 58

Índice de Impacto: 2.196

## **9.2. COPIA DE LOS TRABAJOS PUBLICADOS**

A continuación se adjuntan los cinco trabajos publicados, por orden de publicación.



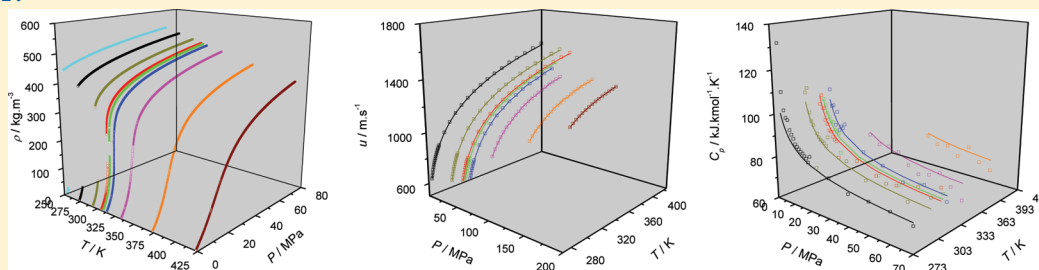
# Accurate Values of Some Thermodynamic Properties for Carbon Dioxide, Ethane, Propane, and Some Binary Mixtures

Inmaculada Velasco, Clara Rivas, José F. Martínez-López, Sofía T. Blanco, Santos Otín, and Manuela Artal\*

Departamento de Química Física, Facultad de Ciencias, Universidad de Zaragoza, 50009-Zaragoza, Spain

Supporting Information

## ABSTRACT:



Quasicontinuous  $P\rho T$  data of  $\text{CO}_2$ , ethane, propane, and the  $[\text{CO}_2 + \text{ethane}]$  mixture have been determined along subcritical, critical, and supercritical regions. These data have been used to develop the optimal experimental method and to determine the precision of the results obtained when using an Anton Paar DMA HPM vibrating-tube densimeter. A comparison with data from reference EoS and other authors confirm the quality of our experimental setup, its calibration, and testing. For pure compounds, the value of the mean relative deviation is  $\text{MRD}(\rho) = 0.05\%$  for the liquid phase and for the extended critical and supercritical region. For binary mixtures the mean relative deviation is  $\text{MRD}(\rho) = 0.70\%$  in the range up to 20 MPa and  $\text{MRD}(\rho) = 0.20\%$  in the range up to 70 MPa. The number of experimental points measured and their just quality have enable us to determine some derived properties with satisfactory precision; isothermal compressibilities,  $\kappa_T$ , have been calculated for  $\text{CO}_2$  and ethane ( $\text{MRD}(\kappa_T) = 1.5\%$ ), isobaric expansion coefficients,  $\alpha_p$ , and internal pressures,  $\pi_i$ , for  $\text{CO}_2$  ( $\text{MRD}(\alpha_p) = 5\%$  and  $\text{MRD}(\pi_i) = 7\%$ ) and ethane ( $\text{MRD}(\alpha_p) = 7.5\%$  and  $\text{MRD}(\pi_i) = 8\%$ ). An in-depth discussion is presented on the behavior of the properties obtained along subcritical, critical, and supercritical regions. In addition,  $PuT$  values have been determined for water and compressed ethane from 273.19 to 463.26 K up to pressures of 190.0 MPa, using a device based on a 5 MHz pulsed ultrasonic system ( $\text{MRD}(u) = 0.1\%$ ). With these data we have calibrated the apparatus and have verified the adequacy of the operation with normal liquids as well as with some compressed gases. From density and speed of sound data of ethane, isentropic compressibilities,  $\kappa_s$ , have been obtained, and from these and our values for  $\kappa_T$  and  $\alpha_p$ , isobaric heat capacities,  $C_p$ , have been calculated with  $\text{MRD}(C_p) = 3\%$ , which is within that of the EoS.

## INTRODUCTION

The aim of this paper will be to obtain the accurate values of some thermodynamic properties, such as density, speed of sound, and other derivative properties such as isothermal and isentropic compressibility, isobaric coefficient thermal expansion, and isobaric heat capacity. The systems studied here are mainly carbon dioxide and ethane. Experimental measurements of density and speed of sound of the systems under study have been used for calibration purposes, for the development of the experimental procedure and for the determination of precisions of the two different devices used to measure these two properties.

Good quality data in a very broad range of pressures and temperatures (subcritical, critical, and supercritical region), of pure compounds and mixtures is as important to a number of industries, as it is for the development of new and improved equations of state, and they are fundamental in the investigation of intermolecular interactions and dynamic properties of phases. The experimental data presented here will help to

improve the reference EoS for the fluids studied in the region of high pressure, where great deviations are obtained in their predicted properties.

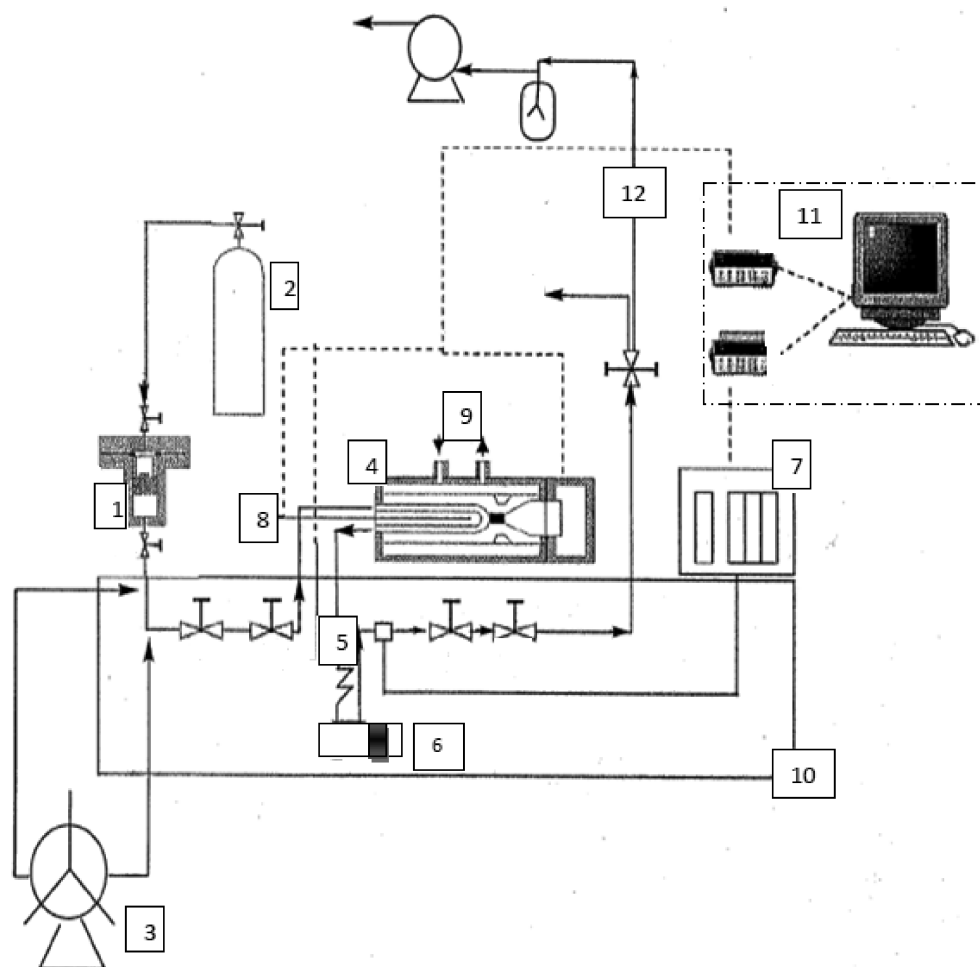
From the experimental densities obtained in this work, the most characteristic properties of supercritical fluids were studied. Their variable densities, which can be changed continuously over all values between that of the liquid and that of the gas, could be considered a bridge between the condensed phase and the gas phase.

Furthermore, as we have worked at several temperatures, among them, at temperatures moderately greater than the critical temperature, a broad range of densities were obtained with just small changes in pressure and temperature.

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**Figure 1.** Experimental setup to measure volumetric properties of pure and binary mixtures: (1) loading cell, (2) nitrogen, (3) manual pump, (4) densimeter, (5) vibrating tube output, (6) rupture disk, (7) thermoregulated pressure transducers, (8) platinum temperature probe, (9) externally connected liquid thermoregulated bath, (10) liquid bath, (11) evaluation unit and data acquisition, and (12) evacuation and vacuum line.

## EXPERIMENTAL SECTION

**Measurement of  $P\rho T$  Properties.** *Apparatus Description.* Figure 1 illustrates a schematic of the apparatus that we have used for the determination of  $P\rho T$  data of fluids in the subcritical, critical, and supercritical regions. The apparatus has been designed and built by ARMINES and the Laboratoire de Thermodynamique des Equilibres entre Phases de l'École Nationale Supérieure des Mines de Paris (France). It was designed for fast, reliable, and accurate generation of  $P\rho T$  data over the whole state surface of a fluid encompassing the liquid and vapor compressed phases, and the saturation curve in the (253 to 423) K temperature range, up to 70 MPa, for pure compounds and mixtures of defined compositions. The main component of the apparatus is an Anton Paar DMA HPM vibrating-tube densimeter. The measurement circuit contains the vibrating tube and its upstream and downstream tubing that are respectively the input and output ports of the fluid to be studied, and the regulating and shut-off valves. Increases or decreases in pressure are obtained through mass transfers with respect to the measurement circuit. To ensure equilibrium through quasi-static transformations, the corresponding flow rates have been kept sufficiently low (They are usually below  $0.005 \text{ MPa s}^{-1}$ ). Considering the vibration period as pseudo state variable, the  $P\tau T$  variables can describe the

$P\rho T$  state surface as long as calibration provides a direct relation between  $\tau$  and  $\rho$ .

The installation also includes an ensemble of devices and materials, like those for temperature regulation, particularly around the vibrating tube, and for measurements of pressures and temperatures.

The measurement circuit is composed of the DMA HPM external measuring cell, where the input tubing is connected to shut-off and regulating valves for compression of the vapor, and the output tubing is also connected to shut-off and regulating valves for decompression of liquid. Input and output tubing are thermo regulated by means of heating cartridges, and the remaining circuit sits in a thermo regulated liquid bath. At the circuit exit, a three-way shut-off valve allows the evacuation of the circuit by means of a vacuum pump before measurements and venting for liquid decompression after measurements. The circuit is connected to two pressure transducers for measuring pressures up to 6 and 70 MPa respectively.

The DMA HPM consists of the measuring cell and of an interface module. The interface module generates the period of oscillation, and measures the resulting period of oscillation and the cell temperature. The density measuring cell is connected to an evaluation unit mPDS 2000 V3 where the current oscillation period, measuring temperature and sample density are displayed.

Given that the apparatus is designed for quasi continuous data acquisition, the mPDS 2000 V3 Evaluation Unit is connected to an external computer with software written in LabVIEW to control the data acquisition.

The double envelop of the vibrating tube densimeter enables thermoregulation by an external liquid bath (Fischer Bioblock, Cryo-polystat 71 model C85408). The circuit is thermoregulated by a Fischer Bioblock Scientific Cryothermostat Variostat model C85775 and a liquid bath. In the case of measurements of condensed phases, the temperature of the vibrating tube is tuned to a value slightly lower than that of the measuring circuit. This ensures the initiation of the condensation to happen strictly within the tube. In the case of gas phase measurements, all of the external tubing is warmer than the vibrating tube to avoid local condensations alongside the measurement circuit.

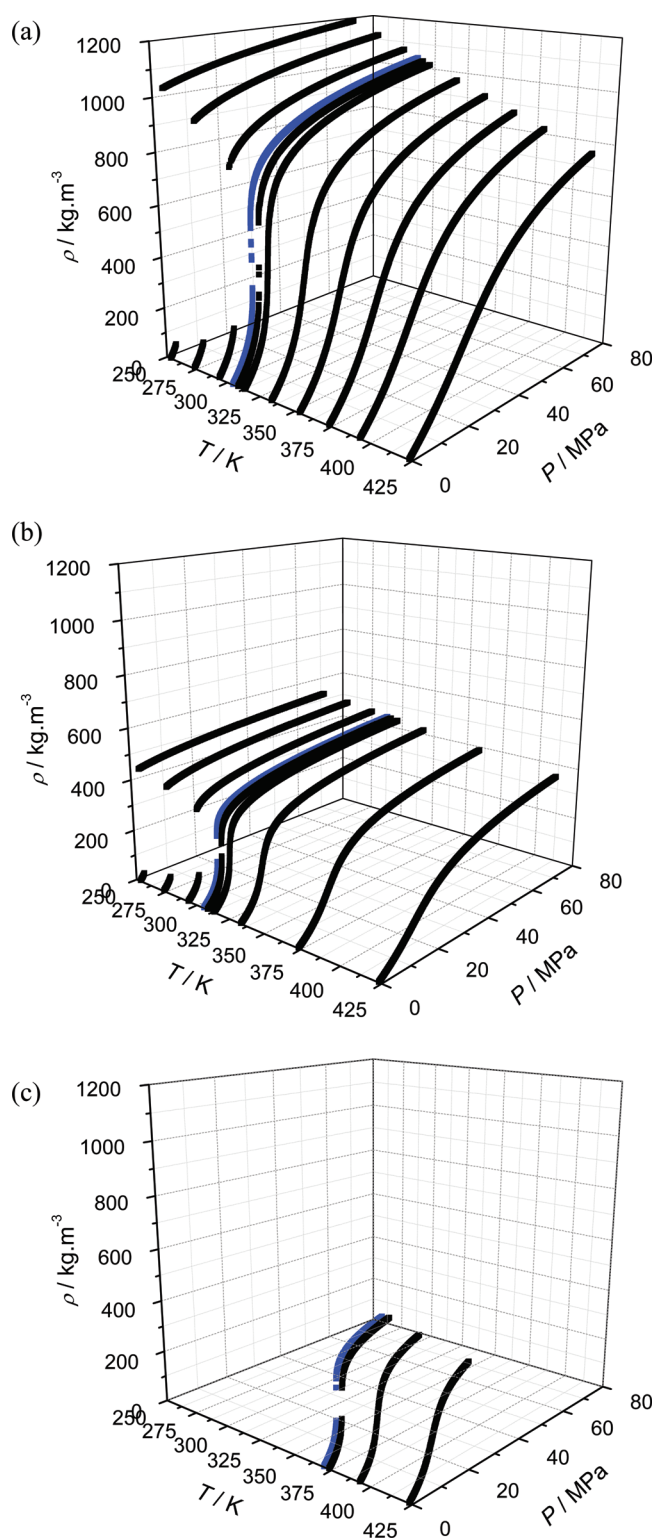
The temperature is measured by means of two 100 ohms platinum probes connected to Data Acquisition Unit Model 34970A from Agilent. One probe is located inside the wall of the vibrating tube and the other inside the liquid bath. The probes and the Data Acquisition Unit were calibrated by the Centro Español de Metrología, CEM, following the CEM-PT-4.2–40 procedure. The precision in the measurement of the temperature is  $\pm 0.006$  K.

The pressure is measured by means of two pressure transducers (GE Infrastructure model PTX 611) 6 and 70 MPa that are thermo regulated and connected to the measurement circuit and to a Data Acquisition Unit Model 34970A from Agilent. The pressure transducers were calibrated in our laboratories using a Wika CPH 6000 calibrator with an accuracy of 0.025% through the whole scale. The precisions observed in the measurement of pressure were 0.008 MPa for measurements up to 6 MPa and 0.001 MPa for measurements from 6 to 70 MPa.

A variable-volume cell is used for loading pure compounds and mixtures into the measurement circuit. The volume is modified thanks to a piston which separates the loaded fluids from pressurized nitrogen. The cell can be weighted on a mass comparator from Sartorius model CCE 2004, for maximum masses of 2500 g and repeatability better than 0.0002 g. Successive introductions of compounds allow the preparation of mixtures of accurately determined composition thanks to successive weighing of the cell (the components are introduced in order of increasing volatility). Mixtures are homogenized through efficient stirring and kept at pressures higher than their bubble pressures. The fluid is transmitted from the loading cell to the measurement circuit through a manual pump, made by Top Industrie, which makes it possible to achieve pressures up to 70 MPa inside the measurement circuit.

An isotherm consists of about 12000 density-pressure points, considered the raw data, which are evenly reduced to about 2000 points for easier handling in subsequent calculations. This large number of points makes quasi-continuous isotherms available along subcritical, critical and supercritical regions, and allows the accurate determination of the limits of vapor–liquid equilibrium.

**Calibration.** The measurement of density with a vibrating tube is not absolute; thus, the response of the instrument must be calibrated against fluids of known density. The reference fluid was carbon dioxide with a stated purity of 99.998% and the reference densities were calculated using the reference EoS.<sup>1</sup> The model of calibration used in this work is the Forced Path Mechanical Calibration model, FPMC, developed by Bouchot.<sup>2</sup> This includes realistic mechanical considerations and forces representing the stress and strain behavior of the tube material.



**Figure 2.** Experimental densities for (a) carbon dioxide, (b) ethane, and (c) propane at several pressures and temperatures. Critical isotherm for each compound is represented by blue dots.

The parameters determined from the calibrating operation were  $(M_0/L_{00})$  and  $\gamma_T$ ; both were found to be temperature dependent but pressure independent. Carbon dioxide was measured at 253.15, 273.15, 293.15,  $T_c(\text{CO}_2) = 304.21, 308.15, 313.15,$



Table 1. Deviations of Experimental Results for CO<sub>2</sub>, C<sub>2</sub>H<sub>6</sub>, and C<sub>3</sub>H<sub>8</sub> at Different Temperatures

T/K	CO <sub>2</sub>			C <sub>2</sub> H <sub>6</sub>			C <sub>3</sub> H <sub>8</sub>		
	no. points	MRD(%) $\rho$	MRD(%) $P$	no. points	MRD(%) $\rho$	MRD(%) $P$	no. points	MRD(%) $\rho$	MRD(%) $P$
253.15	1700	0.02		2090	0.10				
273.15	2450	0.02		2230	0.05				
293.15	2420	0.02		2310	0.09				
304.21 <sup>a</sup>	2980	0.06	0.07						
305.32 <sup>a</sup>				2530	0.13	0.14			
308.15	2320	0.07	0.61	2570	0.14	0.12			
313.15	2120	0.05	0.46	2570	0.13	0.20			
333.15	1810	0.12	0.17	2360	0.11	0.20			
353.15	1880	0.05	0.07						
369.82 <sup>a</sup>							1684	0.24	0.57
373.15	2290	0.04		2180	0.14		1841	0.30	0.16
393.15	2270	0.11					2110	0.18	0.15
423.15	2150	0.15		2100	0.25		1819	0.09	

<sup>a</sup> Critical temperature of different compounds. Extended critical region  $\Rightarrow 0.6\rho_c < \rho < 1.4\rho_c$ ;  $0.98T_c < T < 1.2T_c$ .

333.15, 353.15, 373.15, 393.15, and 423.15 K up to 70 MPa. The densities obtained from experimental measurements and FPMC model (Figure 2a) were compared with those from the reference EoS,<sup>1</sup> and the Mean Relative Deviation (MRD( $\rho$ ), eq. A.1) obtained is 0.09%, if the critical region is included, and 0.07%, if the critical region is excluded.

The values of MRD( $\rho$ ) obtained in this work for the calibration are comparable with those from the literature<sup>3–6</sup> as determined with an Anton Paar DMA HPM vibrating-tube densimeter, but unlike us, following discontinuous procedures of measurement and without considering the critical and vapor regions. As a consequence, the goal of our work is to get quasicontinuous  $P\rho T$  data along subcritical, critical, and supercritical regions of pure fluids and mixtures with adequate precisions and additionally, to be able to determine the limits of vapor–liquid equilibrium.

*Experimental Results and Precision for Pure Compounds.* With the aim to verify the calibration procedure detailed above, the densities of ethane (purity of 99.995%) and propane (purity of 99.95%) were obtained. Ethane was measured at 253.15, 273.15, 293.15,  $T_c(\text{C}_2\text{H}_6) = 305.32$ , 308.15, 313.15, 333.15, 373.15, and 423.15 K over the whole range of pressure, and propane was measured at  $T_c(\text{C}_3\text{H}_8) = 369.82$ , 373.15, 393.15, and 423.15 K, at pressures up to 20 MPa. These densities are shown in Figure 2, panels b and c, respectively. The measurements with propane were made along shorter ranges of temperature and pressure since our objective was to check only the regions with the most experimental difficulty: the critical isotherm and the supercritical region not far from the critical point. These fluids were chosen due to the fact that reference EoS exist for both in the literature, a fact that will allow us to establish comparisons with the experimental data obtained in the present study. In the case of ethane, the reference EoS used were: Buecker and Wagner,<sup>7</sup> for the region of 0.1 to 30 MPa, and Friend et al.,<sup>8</sup> for pressures from 30 to 70 MPa. Lemmon's<sup>9</sup> EoS was used for propane.

The densities obtained from experimental measurements and FPMC model for ethane and propane were compared with those from the reference EoS, and the precisions (MRD) calculated are presented in Table 1 together with those for carbon dioxide. In this table, values for MRD in density of subcritical isotherms are presented. For critical and supercritical isotherms, the values of

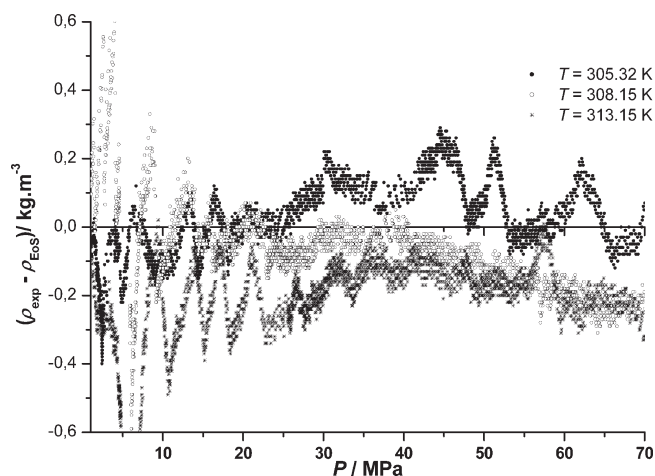
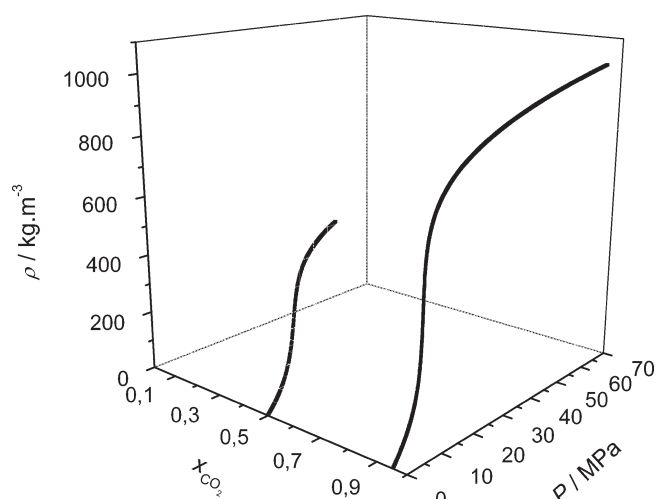


Figure 3. Absolute deviations between experimental density data of ethane at several temperatures and those from the reference EoS of Buecker and Wagner<sup>7</sup> and Friend et al.<sup>8</sup>

MRD are given in density for points outside the extended critical region, and in pressure within the extended critical region as the EoS criterion. The ranges of density and temperature of the extended critical region for each compound are given also in Table 1. The MRD( $\rho$ ) values obtained for the liquid phase of the systems studied by us, MRD( $\rho$ ) = 0.05%, are similar to those from literature.<sup>3–6</sup> However, if we calculate the deviation for all the phases, we found higher values of MRD( $\rho$ ). As an example, the absolute deviations ( $\rho_{\text{exp}} - \rho_{\text{EoS}}$ ) for ethane at three near critical temperatures are presented in Figure 3.

In order to determine the accuracy in the densities of pure compounds measured using our setup, the density of carbon dioxide was determined at 273.15, 304.21, and 353.15 K up to 70 MPa. Each isotherm was measured three times. The relative mean standard deviation,  $\overline{\sigma}_r$  (eq A.2) obtained was 0.05% in density and 0.3% in pressure. The later value is obtained within the extended critical region, which comprises densities from 200 to 680 kg/m<sup>3</sup> and temperatures from 298 to 365 K.



**Figure 4.** Experimental densities of  $\{\text{CO}_2 (1) + \text{C}_2\text{H}_6 (2)\}$  binary mixtures at  $T = 308.15 \text{ K}$  and several pressures..

**Experimental Results and Precision for Binary Mixtures.** To develop the optimal method for the determination of the densities of binary mixtures, and to evaluate the precision and accuracy in density results, the carbon dioxide + ethane system was studied at  $T = 308.15 \text{ K}$ , with  $x_{\text{CO}_2} = 0.4999$  up to 20 MPa and with  $x_{\text{CO}_2} = 0.9540$  up to 70 MPa, and the results were compared with those from the reference EoS.<sup>1</sup> The MRDs( $\rho$ ) obtained were 0.7% for the mixture with  $x_{\text{CO}_2} = 0.4999$  and 0.2% for  $x_{\text{CO}_2} = 0.9540$ . We have performed the precision study in two different ranges of pressure with the aim to observe the influence of high pressures on the precision obtained for density. These values of MRD( $\rho$ ) are comparable with those from experimental values used for EoS development. The mixtures are generated as explained above and each isotherm is measured twice times in order to determine the accuracy, expressed as the relative mean standard deviation,  $\overline{S}_\rho^r$ . The results are 0.13% for  $x_{\text{CO}_2} = 0.4999$  and 0.06% for  $x_{\text{CO}_2} = 0.9540$ . The experimental values of the density for both mixtures are shown in Figure 4.

**Measurement of Speed of Sound.** The apparatus, shown in Figure 5, is a complete system for making speed-of-sound measurements in homogeneous liquids with viscosities up to 100 mPa s and may also be suitable for compressed gases, provided that the density of the gas is sufficiently high. It works over a range of temperatures and pressures from 273.15 K up to 473.15 K and from atmospheric pressure to 200 MPa. The apparatus is based on the method and detailed design published previously<sup>10,11</sup> and employs a 5 MHz pulsed ultrasonic system that allows accurate measurements of the speed of sound in compressed fluids.

The device was tested with deionized (Milli Q) and degassed water. The temperature was controlled at 298.12 K for the purpose of instrument calibration. The measured delay time between the two echos at  $T = 298.12 \text{ K}$  and  $P = 1.00 \text{ MPa}$  was 13.245  $\mu\text{s}$ . Under those conditions of temperature and pressure, the value of the speed of sound from the IAPWS-95 EoS<sup>12</sup> is 1498.13  $\text{m s}^{-1}$ ; therefore, and the path length was calculated to be  $L_0 = 19.84 \times 10^{-3} \text{ m}$ . These calibration data were incorporated into the control program and then, the sound-speed of deionized and degassed water was measured at temperatures from 280.13 to 463.26 K at pressures from 1.0 to 190.0 MPa. The results obtained are represented in Figure 6a.

The repeatability (accuracy) of the  $u$ ,  $T$ ,  $p$ , quantities was  $\pm 0.02 \text{ ms}^{-1}$ ,  $\pm 0.005 \text{ K}$ , and  $\pm 0.005 \text{ MPa}$ , respectively. The experimental values of speed of sound obtained for water were compared with those from the reference EoS,<sup>12</sup> and the precision (MRD( $u$ )) obtained was better than 0.06%. The values of MRD( $u$ ) obtained in this work are comparable with those from the literature<sup>13–23</sup> determined with pulsed ultrasonic systems operating in most of the cases up to pressures lower than those reached in this work. Using the same technique, Gedanitz et al.<sup>24</sup> measured sound velocity in fluids up to 30 MPa in the temperature range between 250 and 350 K, and the deviations observed in their measurements are better than those given above.

In order to verify the adequate operation of the installation for some compressed gases, speeds of sound of pure ethane (purity of 99.995%) have been determined from 273.19 to 423.21 K at pressures up to 170.0 MPa. These data cover a wide range of pressures (from 36.8 to 170.0 MPa) for which we have not found ethane's speed of sound in the literature.<sup>17,25–31</sup> Experimental data and values for MRD obtained from comparison between our experimental speeds of sound for ethane and those calculated with the reference EoS<sup>7</sup> are presented in Table 2 and represented in Figure 6b. The MRD( $u$ ) values are higher than those calculated for water; this can be due to the wide range of speeds of sound measured for ethane (from 538.15 to 1774.91  $\text{ms}^{-1}$ ) in comparison with a relatively narrow range for water (from 1435.81 to 1845.40  $\text{ms}^{-1}$  only).

## DERIVED PROPERTIES AND DISCUSSION

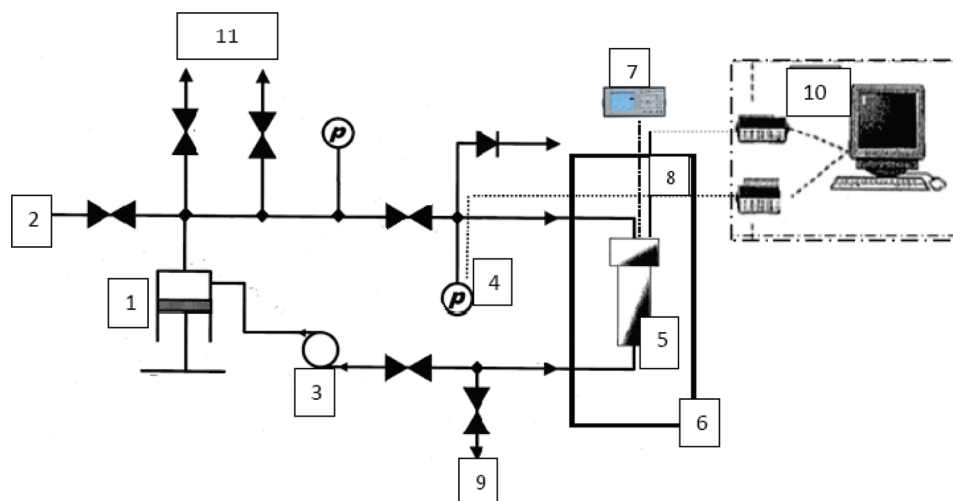
**Isothermal Compressibility.** From the  $P$ - $\rho$ - $T$  experimental values of  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$ , we have evaluated the effect of pressure on the density by means of the isothermal compressibility  $\kappa_T$ , defined as

$$\kappa_T = \left( \frac{1}{\rho} \right) \left( \frac{\partial \rho}{\partial P} \right)_T \quad (1)$$

We have compared our values with those obtained from their respective EoS.<sup>17,8</sup> The mean relative deviation, MRD( $\kappa_T$ ), is better than 1.5% over the entire pressure and temperature ranges. Some of our results are shown in Tables 3 and 4. In general, the value of the isothermal compressibility, as well as its dependence on temperature and pressure for both compounds is quite similar, as can be appreciated in Figure 7, panels a and b. The behavior of the isothermal compressibility over the pressure and temperature ranges studied is the following:

- The isothermal compressibility increases when the temperature increases, at pressures below the critical pressure in the liquid phase, but decreases slowly with the increase of temperature in the gas phase.
- If the pressure is slightly greater than the critical pressure,  $\kappa_T$  in the liquid phase will increase when temperature is increased until it reaches a maximum, near the critical temperature. After this maximum the value of the isothermal compressibility (of this supercritical phase), decreases slowly, showing higher values than those of the liquid phase.
- If the pressure is much greater than the critical pressure, the isothermal compressibility increases slowly with temperature along the isobar, showing values similar to those of the liquid phase.

In our current study, the behavior of the isothermal compressibility on the subcritical, critical and supercritical isotherms has



**Figure 5.** Experimental setup to measure speed of sound at high pressure of pure and binary mixtures: (1) pressure generator, (2) fluid inlet, (3) circulation pump, (4) pressure transducer, (5) pressure vessel, (6) liquid thermoregulated bath, (7) oscilloscope, (8) platinum temperature probe, (9) drain line, (10) evaluation unit and data acquisition, and (11) clean and vacuum line.

been verified. We have observed a discontinuity in the value of this property as the system approaches the liquid–vapor equilibrium. The liquid phase values for  $\kappa_T$  are  $10^{-2}$  or  $10^{-3}$  times those of the gas phase. At the critical isotherms (of  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$ ), we have verified the very high value of the compressibility of these fluids in the regions around their respective critical points. At the critical point, the very high susceptibility of the density to small variations of pressure generates strong density fluctuations at the microscopic level.<sup>32–34</sup> The presence of such microscopic density inhomogeneities has significant consequences for the structure of compressible supercritical solutions, when they're used as SCF solvents. At the critical point,  $\kappa_T \rightarrow \infty$ , but when the pressure is increased to about 10 MPa, the isothermal compressibility values are similar of those of the liquid phase.

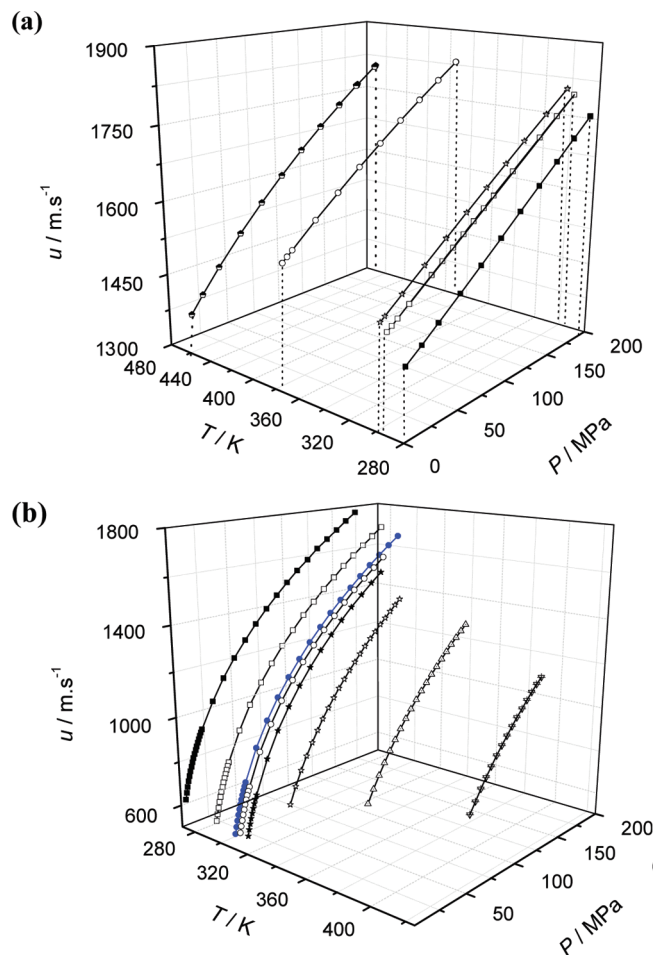
At 308.15 K, a supercritical temperature for both fluids, but still near their critical temperatures, the isothermal compressibility behavior is similar to the critical isotherms with the exception of the maximum value of the compressibility; in this case  $\kappa_T$  exhibits a finite value.

About 340 K, the maximum on  $\kappa_T$  disappears, and at even greater temperatures  $\kappa_T$  will always decrease as the pressure increases, reaching values similar to those of the liquid phase. In the condensed phases, we observed that when the temperature is increased, the compressibility of the compound increases, because the cohesion forces between molecules diminish, favoring the randomness of the molecular distribution and increasing the intermolecular distances. On the contrary, an increase in pressure has the opposite effect.

**Isobaric Thermal Expansivity.** From the  $P$ - $\rho$ - $T$  experimental values of  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$ , we have evaluated the effect of temperature on the density by means of the isobaric thermal expansivity,  $\alpha_p$ , defined as

$$\alpha_p = - \left( \frac{1}{\rho} \right) \left( \frac{\partial \rho}{\partial T} \right)_p \quad (2)$$

We have compared our values with those obtained from their respective EoS<sup>1,7,8</sup> and the mean relative deviation,  $\text{MRD}(\alpha_p)$ , is better than 5% for  $\text{CO}_2$  and better than 7.5% for  $\text{C}_2\text{H}_6$ , over the entire pressure and temperature ranges, as shown in Tables 3 and 4.



**Figure 6.**  $u$ - $T$ - $P$  representation for (a) water and (b) ethane at several pressures and temperatures; (symbols) experimental values and (lines) EoS. The critical isotherm for ethane is represented by blue dots.

The  $\text{MRD}(\alpha_p)$  for ethane is higher due to the small number of experimental isotherms in the same range of studied temperature.

Table 2. Speed of Sound Experimental Data,  $u$ , for  $C_2H_6$  at Several Pressures and Temperatures

$T = 273.15\text{ K}$		$T = 293.15\text{ K}$		$T = T_c(C_2H_6) = 305.32\text{ K}$		$T = 308.15\text{ K}$	
$P/\text{MPa}$	$u/\text{m s}^{-1}$	$P/\text{MPa}$	$u/\text{m s}^{-1}$	$P/\text{MPa}$	$u/\text{m s}^{-1}$	$P/\text{MPa}$	$u/\text{m s}^{-1}$
3.93	632.6	7.94	572.2	9.94	538.1	10.94	547.5
4.93	661.2	8.89	599.9	10.94	567.0	11.93	574.7
5.93	687.1	9.93	627.4	11.94	593.3	12.93	599.4
6.92	710.8	10.94	651.5	12.93	617.2	13.94	622.9
7.93	732.8	11.93	673.9	13.94	639.8	14.93	644.2
8.94	753.7	12.93	694.5	14.94	660.7	15.94	660.0
9.93	772.5	13.93	714.2	15.93	680.2	16.93	683.7
10.92	790.7	14.94	732.8	16.93	698.9	17.93	701.8
11.92	808.1	15.94	750.6	17.94	717.0	18.93	719.1
12.93	824.6	16.93	767.2	18.93	733.8	19.93	735.6
13.94	840.6	17.93	783.5	19.93	749.9	29.93	872.6
14.94	855.9	18.94	798.7	29.94	885.0	39.93	978.3
15.94	870.5	19.93	813.6	39.93	989.3	49.94	1066.5
16.94	884.7	29.94	939.4	49.93	1076.8	59.94	1142.9
17.93	898.6	39.94	1038.9	59.94	1152.7	69.93	1210.8
18.93	911.7	49.93	1123.0	69.93	1220.4	79.94	1272.5
19.94	924.5	59.93	1196.0	79.93	1281.8	89.94	1329.6
29.94	1035.8	69.93	1262.3	89.93	1338.4	99.94	1381.8
39.95	1127.0	79.94	1321.4	99.93	1390.7	109.94	1431.2
49.93	1205.0	89.94	1377.7	109.93	1439.8	119.94	1477.8
59.93	1274.1	99.93	1428.1	119.93	1486.1	129.91	1521.4
69.93	1336.2	109.93	1476.7	129.94	1529.7	139.95	1563.2
79.94	1393.5	119.97	1520.2	139.93	1571.3	149.93	1603.0
89.94	1446.4	129.93	1565.4	149.92	1610.7		
99.95	1495.2	139.94	1605.6	159.94	1648.5		
109.93	1541.2	140.02	1604.8	169.92	1684.5		
120.18	1584.1	149.94	1645.1				
130.14	1628.4	159.89	1679.8				
140.10	1665.9	169.92	1718.1				
149.96	1701.9						
159.86	1739.4						
169.94	1774.9						
MRD( $u$ ) = 0.16%		MRD( $u$ ) = 0.12%		MRD( $u$ ) = 0.12%		MRD( $u$ ) = 0.10%	
$T = 313.15\text{ K}$		$T = 333.15\text{ K}$		$T = 373.15\text{ K}$		$T = 423.15\text{ K}$	
$P/\text{MPa}$	$u/\text{m s}^{-1}$	$P/\text{MPa}$	$u/\text{m s}^{-1}$	$P/\text{MPa}$	$u/\text{m s}^{-1}$	$P/\text{MPa}$	$u/\text{m s}^{-1}$
11.94	543.0	24.94	703.0	39.94	767.4	54.84	807.8
12.93	569.9	29.93	772.5	44.92	819.2	59.87	849.7
13.93	593.5	34.92	833.1	49.94	867.2	65.01	889.8
14.93	616.2	39.92	887.0	54.93	911.2	69.96	926.6
15.93	637.4	44.94	936.2	59.94	952.3	74.83	960.4
16.93	657.3	49.94	981.1	64.93	990.9	79.91	994.9
17.93	676.2	54.93	1022.9	69.93	1027.6	84.91	1027.1
18.94	694.2	59.93	1061.9	74.94	1062.2	89.94	1057.7
19.96	711.3	64.93	1098.4	79.94	1095.0	94.93	1087.4
29.94	851.3	69.93	1133.2	84.93	1126.5	99.94	1115.5
39.94	959.3	74.93	1166.2	89.94	1156.5	104.94	1143.3
49.99	1048.9	79.93	1197.5	94.93	1185.4	109.94	1169.6
59.93	1126.0	84.93	1227.8	99.93	1213.3	114.93	1195.4
69.93	1194.8	89.94	1256.7	104.93	1240.1	119.93	1220.4
79.94	1257.0	94.93	1284.4	109.93	1266.1	124.93	1243.0



Table 2. Continued

T = 313.15 K		T = 333.15 K		T = 373.15 K		T = 423.15 K	
P/MPa	$u/m\ s^{-1}$	P/MPa	$u/m\ s^{-1}$	P/MPa	$u/m\ s^{-1}$	P/MPa	$u/m\ s^{-1}$
89.93	1314.3	99.93	1311.3	114.93	1291.1		
99.93	1367.4	104.93	1337.2	119.94	1315.5		
109.93	1416.2	109.94	1362.1	124.91	1339.1		
119.93	1461.7	114.93	1386.4	129.94	1361.9		
129.99	1505.9	119.94	1409.9	134.85	1384.2		
139.92	1546.7	124.94	1433.1				
		129.93	1455.2				
MRD( $u$ ) = 0.06%		MRD( $u$ ) = 0.05%		MRD( $u$ ) = 0.06%		MRD( $u$ ) = 0.13%	

Table 3. Isothermal Compressibility,  $\kappa_T$ , Isobaric Thermal Expansivity,  $\alpha_p$ , and Internal Pressure,  $\pi_i$ , for CO<sub>2</sub> at Several Pressures and Temperatures

P/MPa	$\kappa_T/MPa^{-1}$	$\alpha_p/K^{-1}$	$\pi_i/MPa$	$\kappa_T/MPa^{-1}$	$\alpha_p/K^{-1}$	$\pi_i/MPa$
T = 253.15 K						
0.2	5.10	$4.1 \times 10^{-3}$		4.90	$3.4 \times 10^{-3}$	
2.5	$4.48 \times 10^{-3}$	$4.4 \times 10^{-3}$	248	$4.65 \times 10^{-1}$	$5.6 \times 10^{-3}$	
5	$3.90 \times 10^{-3}$	$4.4 \times 10^{-3}$	281	$3.10 \times 10^{-1}$	$1.2 \times 10^{-2}$	
7	$3.66 \times 10^{-3}$	$4.1 \times 10^{-3}$	281	$5.45 \times 10^{-1}$	$3.5 \times 10^{-2}$	
7.5	$3.61 \times 10^{-3}$	$3.9 \times 10^{-3}$	267	$5.80 \times 10^{-1}$	$2.0 \times 10^{-1}$	41
10	$3.26 \times 10^{-3}$	$3.7 \times 10^{-3}$	282	$3.32 \times 10^{-2}$	$1.4 \times 10^{-2}$	116
20	$2.48 \times 10^{-3}$	$3.2 \times 10^{-3}$	310	$8.35 \times 10^{-3}$	$5.4 \times 10^{-3}$	177
30	$2.03 \times 10^{-3}$	$2.8 \times 10^{-3}$	323	$5.07 \times 10^{-3}$	$4.0 \times 10^{-3}$	207
40	$1.73 \times 10^{-3}$	$2.5 \times 10^{-3}$	334	$3.58 \times 10^{-3}$	$3.4 \times 10^{-3}$	247
50	$1.51 \times 10^{-3}$	$2.3 \times 10^{-3}$	345	$2.80 \times 10^{-3}$	$2.8 \times 10^{-3}$	254
60	$1.34 \times 10^{-3}$	$2.2 \times 10^{-3}$	353	$2.34 \times 10^{-3}$	$2.5 \times 10^{-3}$	265
70	$1.22 \times 10^{-3}$	$2.0 \times 10^{-3}$	356	$1.99 \times 10^{-3}$	$2.3 \times 10^{-3}$	277
T = 304.21 K						
T = 308.15 K						
0.2	5.00	$3.4 \times 10^{-3}$		5.30	$2.3 \times 10^{-3}$	
2.5	$4.60 \times 10^{-1}$	$5.0 \times 10^{-3}$		$4.15 \times 10^{-1}$	$3.0 \times 10^{-3}$	
5	$2.98 \times 10^{-1}$	$9.3 \times 10^{-3}$		$2.15 \times 10^{-1}$	$3.7 \times 10^{-3}$	
7	$3.60 \times 10^{-1}$	$2.8 \times 10^{-2}$		$1.58 \times 10^{-1}$	$1.9 \times 10^{-3}$	
7.5	$5.27 \times 10^{-1}$	$1.9 \times 10^{-1}$	20	$1.48 \times 10^{-1}$	$1.8 \times 10^{-3}$	4
10	$5.27 \times 10^{-2}$	$2.0 \times 10^{-2}$	106	$1.15 \times 10^{-1}$	$3.6 \times 10^{-3}$	4
20	$9.49 \times 10^{-3}$	$5.6 \times 10^{-3}$	163	$5.65 \times 10^{-2}$	$4.2 \times 10^{-3}$	3
30	$5.45 \times 10^{-3}$	$4.1 \times 10^{-3}$	200	$2.84 \times 10^{-2}$	$5.6 \times 10^{-3}$	12
40	$3.82 \times 10^{-3}$	$3.3 \times 10^{-3}$	227	$1.55 \times 10^{-2}$	$4.5 \times 10^{-3}$	54
50	$2.98 \times 10^{-3}$	$2.8 \times 10^{-3}$	244	$9.90 \times 10^{-3}$	$3.6 \times 10^{-3}$	82
60	$2.44 \times 10^{-3}$	$2.5 \times 10^{-3}$	259	$7.02 \times 10^{-3}$	$3.4 \times 10^{-3}$	103
70	$2.09 \times 10^{-3}$	$2.3 \times 10^{-3}$	268	$5.33 \times 10^{-3}$	$2.4 \times 10^{-3}$	121
MRD( $\kappa_T$ ) = 1.2%; MRD( $\alpha_p$ ) = 5%; MRD( $\pi_i$ ) = 7%						

Table 4. Isothermal Compressibility,  $\kappa_T$ , Isobaric Thermal Expansivity,  $\alpha_p$ , and Internal Pressure,  $\pi_i$ , for C<sub>2</sub>H<sub>6</sub> at Several Pressures and Temperatures

P/MPa	$\kappa_T/MPa^{-1}$	$\alpha_p/K^{-1}$	$\pi_i/MPa$	$\kappa_T/MPa^{-1}$	$\alpha_p/K^{-1}$	$\pi_i/MPa$
T = 253.15 K						
0.2	5.50	$4.5 \times 10^{-3}$		5.27	$4.2 \times 10^{-3}$	
2.5	$7.08 \times 10^{-3}$	$4.3 \times 10^{-3}$	152	$5.22 \times 10^{-1}$	$8.2 \times 10^{-3}$	
4	$6.37 \times 10^{-3}$	$4.1 \times 10^{-3}$	160	$5.50 \times 10^{-1}$	$1.4 \times 10^{-2}$	
5	$5.97 \times 10^{-3}$	$3.9 \times 10^{-3}$	161	$4.36 \times 10^{-1}$	$9.2 \times 10^{-2}$	59
5.5	$5.79 \times 10^{-3}$	$3.8 \times 10^{-3}$	162	$1.17 \times 10^{-1}$	$2.2 \times 10^{-2}$	52
10	$4.58 \times 10^{-3}$	$3.2 \times 10^{-3}$	169	$1.92 \times 10^{-2}$	$6.4 \times 10^{-3}$	92
20	$3.24 \times 10^{-3}$	$2.5 \times 10^{-3}$	178	$7.40 \times 10^{-3}$	$3.3 \times 10^{-3}$	118
30	$2.53 \times 10^{-3}$	$2.1 \times 10^{-3}$	185	$4.73 \times 10^{-3}$	$2.7 \times 10^{-3}$	142
40	$2.07 \times 10^{-3}$	$1.9 \times 10^{-3}$	192	$3.49 \times 10^{-3}$	$2.2 \times 10^{-3}$	152
50	$1.77 \times 10^{-3}$	$1.7 \times 10^{-3}$	195	$2.80 \times 10^{-3}$	$1.9 \times 10^{-3}$	162
60	$1.56 \times 10^{-3}$	$1.6 \times 10^{-3}$	193	$2.32 \times 10^{-3}$	$1.8 \times 10^{-3}$	174
70	$1.38 \times 10^{-3}$	$1.4 \times 10^{-3}$	195	$2.00 \times 10^{-3}$	$1.7 \times 10^{-3}$	186
T = 305.32 K						
T = 308.15 K						
0.2	5.10	$4.1 \times 10^{-3}$		5.40	$2.5 \times 10^{-3}$	
2.5	$5.22 \times 10^{-1}$	$6.8 \times 10^{-3}$		$4.26 \times 10^{-1}$	$3.5 \times 10^{-3}$	
4	$4.60 \times 10^{-1}$	$1.3 \times 10^{-2}$		$2.76 \times 10^{-1}$	$3.5 \times 10^{-3}$	
5	1.24	$1.8 \times 10^{-1}$	40	$2.27 \times 10^{-1}$	$4.0 \times 10^{-3}$	2
5.5	$2.66 \times 10^{-1}$	$5.8 \times 10^{-2}$	62	$2.09 \times 10^{-1}$	$4.3 \times 10^{-3}$	3
10	$2.18 \times 10^{-2}$	$6.8 \times 10^{-3}$	86	$1.21 \times 10^{-1}$	$5.5 \times 10^{-3}$	9
20	$7.74 \times 10^{-3}$	$3.4 \times 10^{-3}$	116	$4.05 \times 10^{-2}$	$5.7 \times 10^{-3}$	39
30	$4.89 \times 10^{-3}$	$2.7 \times 10^{-3}$	126	$1.68 \times 10^{-2}$	$3.7 \times 10^{-3}$	63
40	$3.57 \times 10^{-3}$	$2.2 \times 10^{-3}$	149	$9.47 \times 10^{-3}$	$2.8 \times 10^{-3}$	85
50	$2.83 \times 10^{-3}$	$1.9 \times 10^{-3}$	158	$6.55 \times 10^{-3}$	$2.3 \times 10^{-3}$	98
60	$2.35 \times 10^{-3}$	$1.8 \times 10^{-3}$	171	$4.86 \times 10^{-3}$	$2.0 \times 10^{-3}$	113
70	$2.04 \times 10^{-3}$	$1.6 \times 10^{-3}$	178	$3.89 \times 10^{-3}$	$1.8 \times 10^{-3}$	122
MRD( $\kappa_T$ ) = 1.2%; MRD( $\alpha_p$ ) = 7.4%; MRD( $\pi_i$ ) = 8%						

Again, the values of the isobaric thermal expansivity for both compounds, as well as its dependence on the temperature and pressure, are quite similar. They are shown in Figure 8, panels a and b. For both carbon dioxide and ethane, the values of  $\alpha_p$  are of the same order for the two phases, liquid and gas. The dependence on the temperature along the isobars for  $\alpha_p$  is the same as  $\kappa_T$ , throughout the range of pressures studied.

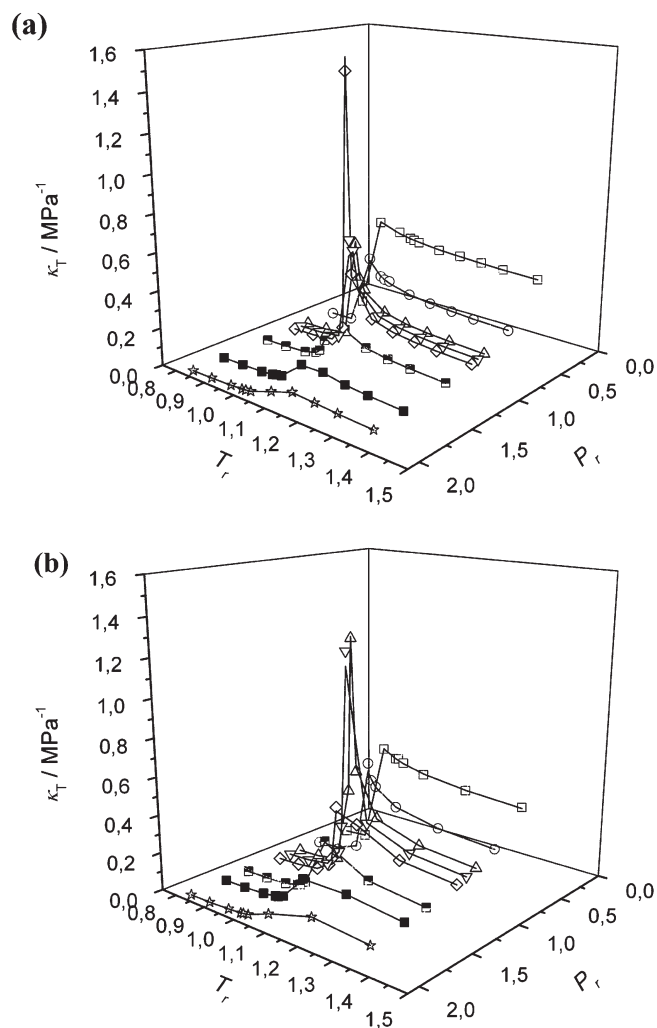
When the isobaric thermal expansivity,  $\alpha_p$ , was analyzed along the subcritical isotherms, it was found that it increases with pressure in the gas phase but decreases in the liquid phase, showing a small discontinuity upon reaching the VLE.

Also  $\alpha_p \rightarrow \infty$  at the critical point, and for both critical isotherms, the higher calculated value for  $\alpha_p$  were found near their respective critical pressures. Later,  $\alpha_p$  decreases slowly when pressure increases.

The behavior of the isobaric thermal expansivity, for the supercritical isotherms of both components, is quite similar to their respective critical isotherms, and with the exception of the maximum value of the expansivity  $\alpha_p$  is a finite value which decreases when the temperature is increased.

**Internal Pressure,  $\pi_i$ .** Internal pressure,  $\pi_i$ , was defined<sup>35</sup> as a macroscopic property used for estimating the dispersion element of cohesion of liquids and reflecting molecular ordering. Its role





**Figure 7.**  $\kappa_T$ – $T$ – $P$  representation for (a) carbon dioxide and (b) ethane; (symbols) experimental values and (lines) EoS.

in thermodynamics of liquid solutions was defined by Hildebrand. Internal pressure is understood to be a fundamental property used in the calculation of the energy of cavity formation.

The Internal pressure is closely related to different properties of liquids, such as ultrasonic velocity, free volume, viscosity, surface tension, and density.<sup>36</sup>

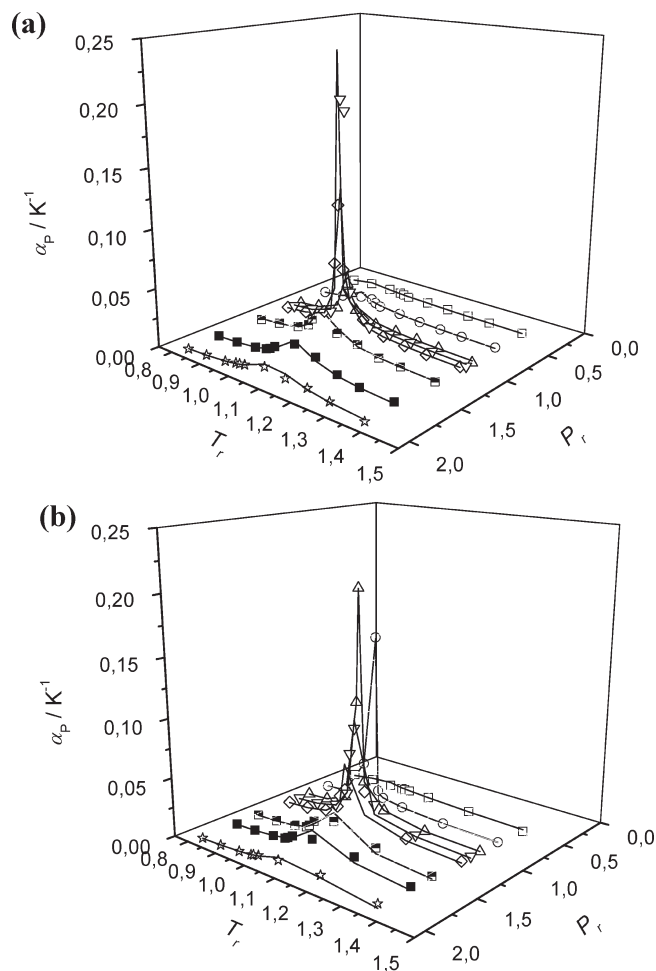
The precise meaning of the internal pressure is illustrated in the following thermodynamic relation:

$$\pi_i = \left( \frac{\partial U}{\partial V} \right)_T = T \left( \frac{\partial P}{\partial T} \right)_V - P \quad (3)$$

and combining eqs 1 and 2

$$\pi_i = T \left( \frac{\alpha_p}{\kappa_T} \right) - P \quad (4)$$

Some of the values obtained for the internal pressure at different pressures and temperatures, and their comparison with those calculated with the corresponding reference EoS<sup>1,7,8</sup> are presented in Tables 3 and 4; The mean relative deviation, MRD( $\pi_i$ ), obtained is 7% for CO<sub>2</sub> and 8% for C<sub>2</sub>H<sub>6</sub>, respectively. Supercritical fluids may be considered as high-density condensed matter, and one of their greatest advantage has been the possibility



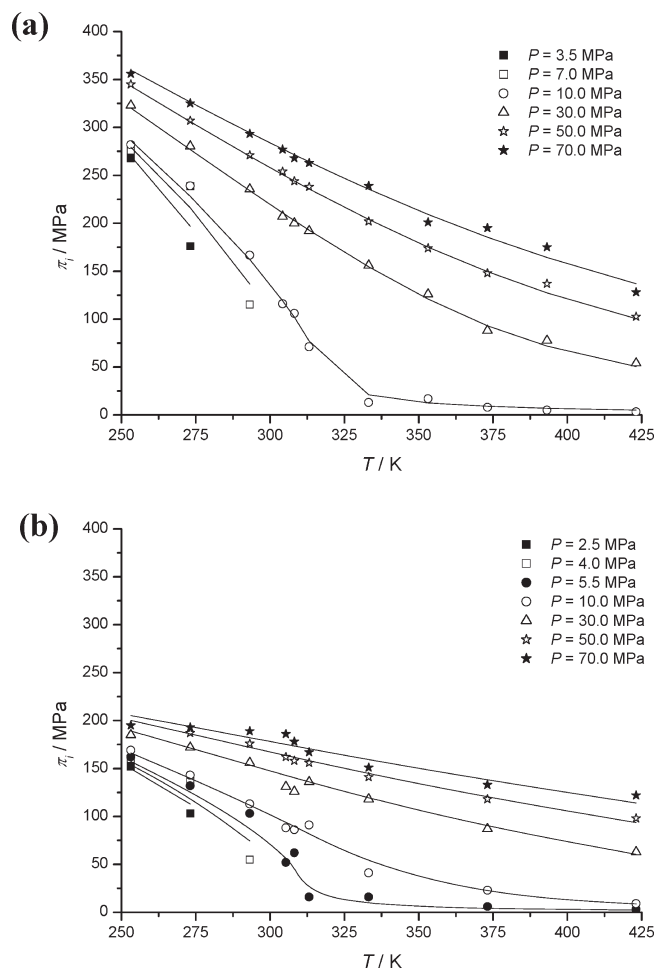
**Figure 8.**  $\alpha_p$ – $T$ – $P$  representation for (a) carbon dioxide and (b) ethane; (symbols) experimental values and (lines) EoS.

to be described far above their critical temperatures (around 100 K); in view of this we have enlarged the internal pressure study to the supercritical region.

The internal pressure for the CO<sub>2</sub> and C<sub>2</sub>H<sub>6</sub> decreases when temperature rises along isobars, Figure 9, panels a and b; this could mean that cohesive forces decrease when temperature increases. At the critical temperature, and above it, the internal pressure vanishes at the critical pressure or near it. On the other hand, the internal pressure increases when the pressure rises along isotherms, Figure 10, panels a and b.

The behavior of  $\kappa_T$  and  $\alpha_p$  for carbon dioxide and ethane is similar, but values of the internal pressure for these two compounds are quite different. Thus, in the liquid region, and through the whole range of temperatures and pressures studied, the  $\pi_i$  values for CO<sub>2</sub> are much higher than those for ethane, but these differences diminish at high temperatures in the supercritical region.

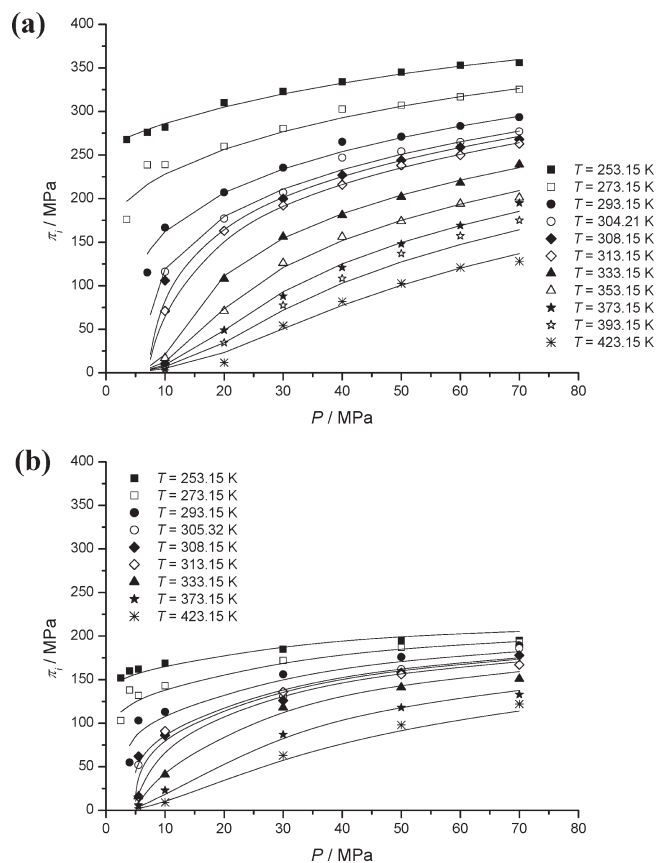
The internal pressure value for carbon dioxide is abnormally high if we compare it with that for ethane or propane. Although CO<sub>2</sub> has a zero dipole moment, the carbon atom in a CO<sub>2</sub> molecule is electron deficient, whereas the oxygen has two lone pairs of electrons; it is a charge-separated molecule with significant nonzero bond dipole moments. This charge separation results in a significant quadrupole moment; CO<sub>2</sub> is thus described as a quadrupolar solvent.<sup>37,38</sup>



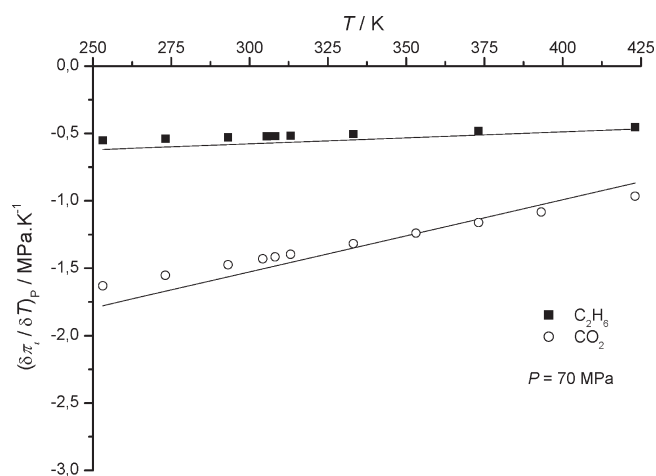
**Figure 9.** Representation of internal pressure,  $\pi_i$ , versus temperature,  $T$ , for (a) carbon dioxide ( $P_c = 7.383$  MPa,  $T_c = 304.21$  K) and (b) ethane ( $P_c = 4.882$  MPa,  $T_c = 305.32$  K); (symbols) experimental values and (lines) EoS.

Different authors have studied the microscopic structure of liquid and supercritical  $\text{CO}_2$ .<sup>39–50</sup> The aim of most of these papers was to determine the pair correlation function, and in some, an attempt was made to provide a qualitative description of local orientations. Different arrangements (parallel, cross-shaped, T-shaped, and chain-like arrangements) were identified, and different regions of the  $T$ – $P$  plane were mapped with varied orientational correlations: some of the authors matched the T-shaped arrangements with high density regions, others found parallel-arrangements in these areas. Generally, results from different authors are not in complete accordance. In our current study we have not been able to establish a direct correlation between the different arrangements and internal pressure.

Kartsev<sup>51</sup> indicates that the derivative  $(\partial\pi_i/\partial T)_P$  is related to the structural organization of the fluids. Thus, according to the sign of the slope of the  $\pi_i$  versus  $T$  curve, liquids can be classified into two structural groups: Those fluids being  $(\partial\pi_i/\partial T)_P < 0$ , namely, non- or weakly associate fluids, and those being  $(\partial\pi_i/\partial T)_P > 0$ , the associated fluids, which have molecules linked by hydrogen bonds. For the last group, as the degree and the stability of the association increases, the slope also increases. In our study,  $(\partial\pi_i/\partial T)_P$  are negative for both  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$ , and

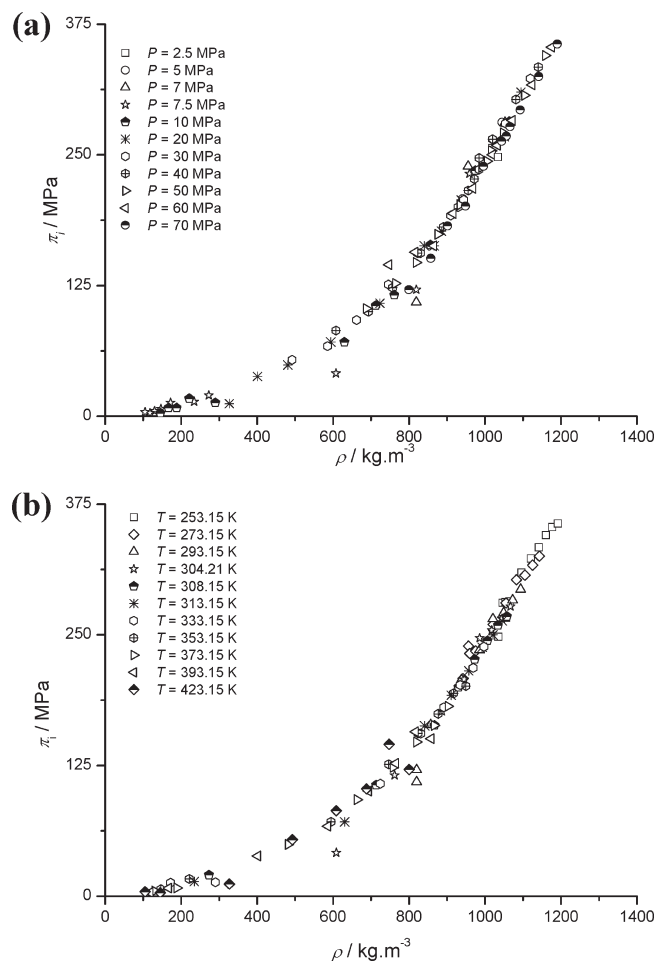


**Figure 10.** Representation of internal pressure,  $\pi_i$ , versus pressure,  $P$ , for (a) carbon dioxide ( $P_c = 7.383$  MPa,  $T_c = 304.21$  K) and (b) ethane ( $P_c = 4.882$  MPa,  $T_c = 305.32$  K); (symbols) experimental values and (lines) EoS.



**Figure 11.** Thermal coefficient,  $(\partial\pi_i/\partial T)_P$ , versus temperature,  $T$ , for  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$  compounds; (symbols) experimental values and (lines) EoS.

according to this classification, both fluids are weakly associated, with the  $\text{CO}_2$  showing a steeper slope than that of  $\text{C}_2\text{H}_6$ . This fact is due to the differences between the values of the dipole and quadrupole moments of these compounds.<sup>37,52,53</sup> Figure 11

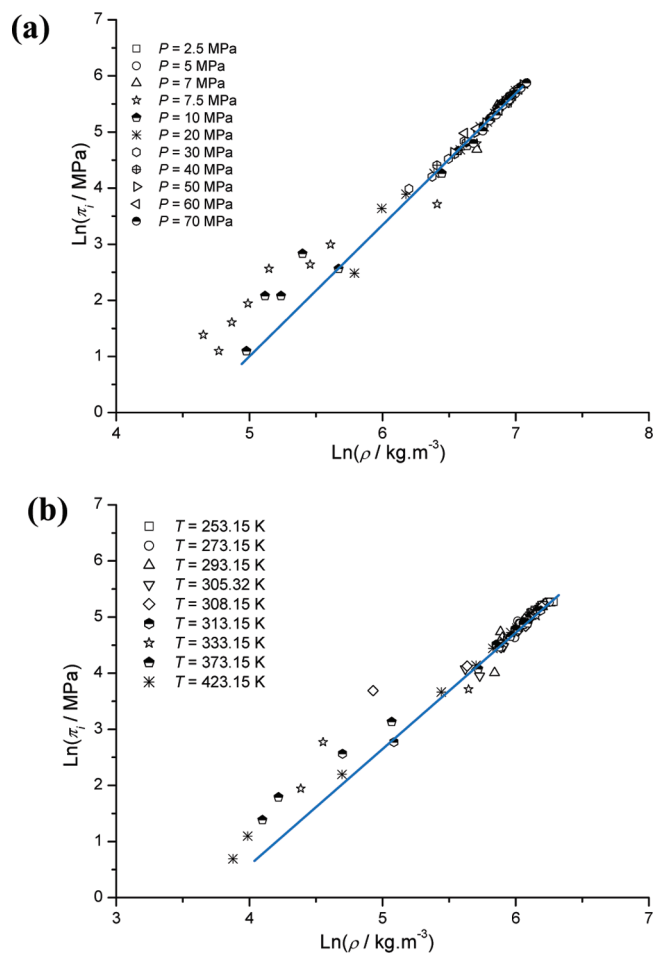


**Figure 12.** Representation of internal pressure,  $\pi_i$ , versus density,  $\rho$ , for  $\text{CO}_2$ ; (a) isobar and (b) isotherm.

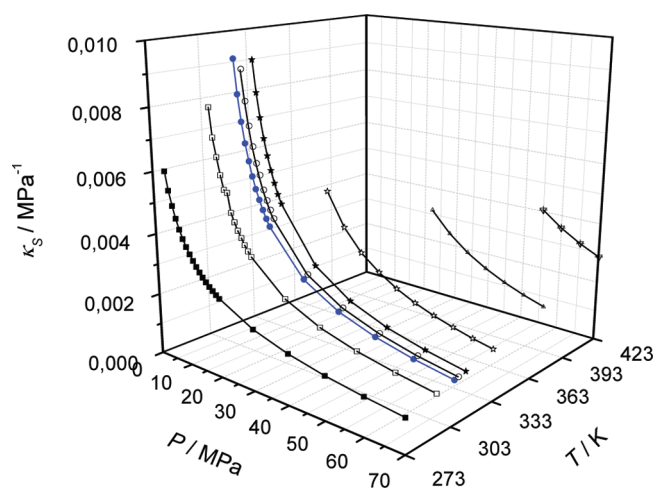
shows the variation of the internal pressure coefficient for  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$ , along the 70 MPa isobars.

Finally, the dependence of the internal pressure on the density was analyzed for both fluids. It has been found that as the density increases along an isobar, the internal pressures increase, and does so with the same slope that increases of the density with respect to internal pressure in an isotherm. This can be seen in Figure 12, panels a and b, where we have chosen to show the isobar and isotherm plots for  $\text{CO}_2$ . However the more surprising result is that different dense states with the same internal pressure values have very similar densities. Different dense states mean states with different pressure or/and temperature and a density equal or greater than the critical density. In Figure 13, panels a and b, we have represented  $\ln(\pi_i)$  versus  $\ln(\rho)$  for  $\text{CO}_2$  and  $\text{C}_2\text{H}_6$ , respectively. The observed deviations from linearity correspond with supercritical states ( $T > T_c$  and  $P > P_c$ ) of density smaller than the critical density.

We may thus conclude that the system's internal pressure is directly related to the density of the compound. The values of the internal pressure of the compound (at liquid or supercritical state) will be significant if it has a liquid-like density. On the other hand, if the compound is at its supercritical state, but its density is gas-like, the internal pressure will not be significant.



**Figure 13.** Representation of  $\ln(\pi_i) - \ln(\rho)$  for (a) carbon dioxide ( $P_c = 7.383$  MPa,  $T_c = 304.21$  K) and (b) ethane ( $P_c = 4.882$  MPa,  $T_c = 305.32$  K); (symbols) experimental values.



**Figure 14.**  $\kappa_s - P - T$  representation for ethane at several pressures and temperatures; (symbols) experimental values and (lines) EoS. The critical isotherm for ethane is represented by blue dots.

**Isentropic Compressibility,  $\kappa_s$ , and Isobaric Heat Capacity,  $C_p$ .** The isentropic compressibility,  $\kappa_s$ , for ethane has been

Table 5. Isentropic Compressibility,  $\kappa_s$ , and Isobaric Heat Capacity,  $C_p$ , for  $C_2H_6$  at Several Pressures and Temperatures

T = 273.15 K			T = 293.15 K		
P/MPa	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{K}^{-1}$	P/MPa	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{K}^{-1}$
3.93	$6.10 \times 10^{-3}$	132	7.94	$7.94 \times 10^{-3}$	109
4.93	$5.52 \times 10^{-3}$	111	8.89	$7.02 \times 10^{-3}$	112
5.93	$5.06 \times 10^{-3}$	103	9.93	$6.42 \times 10^{-3}$	101
6.92	$4.68 \times 10^{-3}$	100	10.94	$5.88 \times 10^{-3}$	97
7.93	$4.36 \times 10^{-3}$	99	11.93	$5.44 \times 10^{-3}$	95
8.94	$4.09 \times 10^{-3}$	95	12.93	$5.37 \times 10^{-3}$	75
9.93	$3.87 \times 10^{-3}$	93	13.93	$4.75 \times 10^{-3}$	92
10.92	$3.67 \times 10^{-3}$	91	14.94	$4.47 \times 10^{-3}$	90
11.92	$3.49 \times 10^{-3}$	89	15.94	$4.23 \times 10^{-3}$	89
12.93	$3.33 \times 10^{-3}$	88	16.93	$4.02 \times 10^{-3}$	89
13.94	$3.18 \times 10^{-3}$	87	17.93	$3.83 \times 10^{-3}$	88
14.94	$3.06 \times 10^{-3}$	86	18.94	$3.66 \times 10^{-3}$	87
15.94	$2.94 \times 10^{-3}$	86	19.93	$3.51 \times 10^{-3}$	91
16.94	$2.83 \times 10^{-3}$	85	29.94	$2.50 \times 10^{-3}$	83
17.93	$2.73 \times 10^{-3}$	84	39.94	$1.98 \times 10^{-3}$	77
18.93	$2.64 \times 10^{-3}$	82	49.93	$1.64 \times 10^{-3}$	79
19.94	$2.56 \times 10^{-3}$	85	59.93	$1.42 \times 10^{-3}$	74
29.94	$1.96 \times 10^{-3}$	79	69.93	$1.25 \times 10^{-3}$	79
39.95	$1.61 \times 10^{-3}$	75			
49.93	$1.38 \times 10^{-3}$	75			
59.93	$1.21 \times 10^{-3}$	74			
69.93	$1.08 \times 10^{-3}$	72			

T = 305.32 K			T = 308.15 K		
P/MPa	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{K}^{-1}$	P/MPa	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{K}^{-1}$
9.94	$9.37 \times 10^{-3}$	103	10.94	$9.04 \times 10^{-3}$	106
10.94	$8.29 \times 10^{-3}$	108	11.93	$8.07 \times 10^{-3}$	103
11.94	$7.45 \times 10^{-3}$	102	12.93	$7.31 \times 10^{-3}$	99
12.93	$6.80 \times 10^{-3}$	96	13.94	$6.68 \times 10^{-3}$	98
13.94	$6.25 \times 10^{-3}$	95	14.93	$6.17 \times 10^{-3}$	96
14.94	$5.79 \times 10^{-3}$	92	15.94	$5.81 \times 10^{-3}$	96
15.93	$5.41 \times 10^{-3}$	92	16.93	$5.37 \times 10^{-3}$	92
16.93	$5.08 \times 10^{-3}$	89	17.93	$5.05 \times 10^{-3}$	92
17.94	$4.78 \times 10^{-3}$	88	18.93	$4.76 \times 10^{-3}$	91
18.93	$4.53 \times 10^{-3}$	88	19.93	$4.52 \times 10^{-3}$	82
19.93	$4.30 \times 10^{-3}$	80	29.93	$3.02 \times 10^{-3}$	82
29.94	$2.92 \times 10^{-3}$	81	39.93	$2.30 \times 10^{-3}$	77
39.93	$2.24 \times 10^{-3}$	77	49.94	$1.88 \times 10^{-3}$	76
49.93	$1.83 \times 10^{-3}$	76	59.94	$1.59 \times 10^{-3}$	79
59.94	$1.56 \times 10^{-3}$	79	69.93	$1.39 \times 10^{-3}$	79
69.93	$1.36 \times 10^{-3}$	82			

T = 313.15 K			T = 333.15 K			T = 373.15 K		
P/MPa	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{K}^{-1}$	P/MPa	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{K}^{-1}$	P/MPa	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{K}^{-1}$
11.94	$9.31 \times 10^{-3}$	110	24.94	$5.18 \times 10^{-3}$	89	39.94	$4.38 \times 10^{-3}$	86
12.93	$8.31 \times 10^{-3}$	102	29.93	$4.13 \times 10^{-3}$	85	44.92	$3.73 \times 10^{-3}$	84
13.93	$7.54 \times 10^{-3}$	103	34.92	$3.45 \times 10^{-3}$	86	49.94	$3.24 \times 10^{-3}$	84
14.93	$6.90 \times 10^{-3}$	94	39.92	$2.97 \times 10^{-3}$	84	54.93	$2.87 \times 10^{-3}$	81
15.93	$6.37 \times 10^{-3}$	100	44.94	$2.61 \times 10^{-3}$	79	59.94	$2.58 \times 10^{-3}$	86
16.93	$5.93 \times 10^{-3}$	92	49.94	$2.33 \times 10^{-3}$	77	64.93	$2.34 \times 10^{-3}$	80
17.93	$5.54 \times 10^{-3}$	93	54.93	$2.11 \times 10^{-3}$	78	69.93	$2.14 \times 10^{-3}$	78

MRD( $\kappa_s$ ) = 0.19%; MRD( $C_p$ ) = 3%

Table 5. Continued

$T = 313.15 \text{ K}$			$T = 333.15 \text{ K}$			$T = 373.15 \text{ K}$		
$P/\text{MPa}$	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{ K}^{-1}$	$P/\text{MPa}$	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{ K}^{-1}$	$P/\text{MPa}$	$\kappa_s/\text{MPa}^{-1}$	$C_p/\text{kJ kmol}^{-1} \text{ K}^{-1}$
18.94	$5.21 \times 10^{-3}$	93	59.93	$1.93 \times 10^{-3}$	80			
19.96	$4.92 \times 10^{-3}$	95	64.93	$1.78 \times 10^{-3}$	75			
29.94	$3.22 \times 10^{-3}$	84	69.93	$1.65 \times 10^{-3}$	71			
39.94	$2.42 \times 10^{-3}$	81						
49.99	$1.96 \times 10^{-3}$	76						
59.93	$1.66 \times 10^{-3}$	78						
69.93	$1.44 \times 10^{-3}$	74						

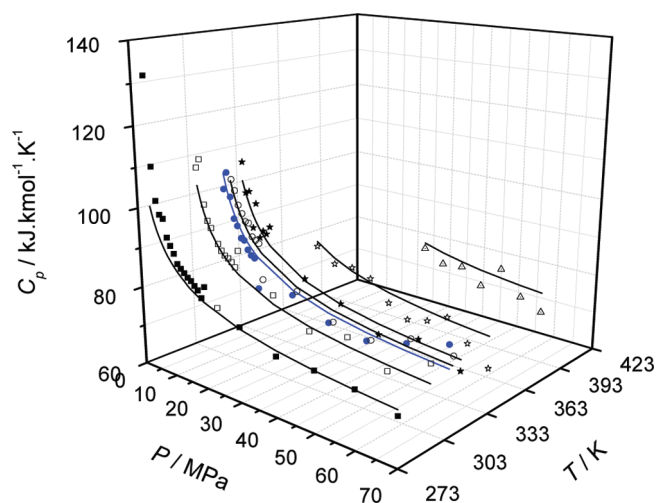


Figure 15.  $C_p$ – $P$ – $T$  representation for ethane at several pressures and temperatures; (symbols) experimental values and (lines) EoS. The critical isotherm for ethane is represented by blue dots.

obtained from our experimental density and speed of sound values using the following relationship:

$$\kappa_s = \frac{1}{\rho u^2} \quad (5)$$

The values for this property along with those from the EoS<sup>7</sup> are represented in Figure 14. In Table 5 are presented our  $\kappa_s$  data and the value for  $\text{MRD}(\kappa_s)$  obtained from comparison between our data with those obtained with the reference EoS.<sup>7</sup>

Finally, from our experimental density values,  $\rho$ , and those calculated for  $\kappa_T$ ,  $\alpha_p$ , and  $\kappa_s$  (eqs 1, 2, and 5), isobaric heat capacities,  $C_p$ , have been obtained for ethane, using the equation

$$C_p = \frac{\alpha^2 T}{\rho(\kappa_T - \kappa_s)} \quad (6)$$

These values along with those from EoS<sup>7</sup> are represented in Figure 15. Buecker and Wagner<sup>7</sup> highlight the scarcity and poor quality of experimental  $C_p$  data in the literature<sup>54–62</sup> and point out that it would be desirable to possess isobaric heat capacity data in the gas and also in the supercritical range up to high pressures. However, these requirements are probably unrealistic. In those regions, it may be more important to get good quality  $P\rho T$  and speed-of-sound data to fill the gaps mentioned above. The mean relative deviation,  $\text{MRD}(C_p)$ , between our values for  $C_p$  and those from EoS<sup>7</sup> is 3% (Table 5); this value is within that of the

EoS: the uncertainties in heat capacities range from 2% in the vapor and liquid regions below 450 K and 30 MPa, to 5% at high pressures.

## CONCLUSIONS

Quasi-continuous  $P\rho T$  data of  $\text{CO}_2$ , ethane, propane, and the  $[\text{CO}_2 + \text{ethane}]$  mixture have been measured throughout very broad temperature and pressure ranges. These data have been used to develop an optimal method and to determine the precision for the results obtained. A comparison with data from references EoS and other authors confirm the quality of our experimental setup, as well as its calibration and testing. The value of the mean relative deviation for pure compounds is  $\text{MRD}(\rho) = 0.13\%$  and  $\text{MRD}(P) = 0.17\%$  (in the extended critical region). For binary mixtures the value of the mean relative deviation is  $\text{MRD}(\rho) = 0.70\%$  in the range up to 20 MPa and  $\text{MRD}(\rho) = 0.20\%$  in the range up to 70 MPa. As a consequence, the great number of experimental points obtained and their quality has enabled us to determine some derived properties for  $\text{CO}_2$  and ethane with the following precision:  $\text{MRD}(\kappa_T) = 1.5\%$ ;  $\text{MRD}(\alpha_p) = 5\%$  for  $\text{CO}_2$  and  $\text{MRD}(\alpha_p) = 7.5\%$  for  $\text{C}_2\text{H}_6$ ;  $\text{MRD}(\pi_i) = 7\%$  for  $\text{CO}_2$  and  $\text{MRD}(\pi_i) = 8\%$  for  $\text{C}_2\text{H}_6$ .

The behavior of the isothermal compressibility on the subcritical, critical and supercritical isotherms has been studied, observing the disappearance of the  $\kappa_T$  maximum around 340 K. In the condensed phases it is observed that temperature and pressure have opposite effects.

The dependence of  $\alpha_p$  on temperature is the same as for  $\kappa_T$  in all range of pressures studied.

Since supercritical fluids may be regarded as high-density condensed matter, we have enlarged the internal pressure study to the supercritical region. In this paper, we have shown that although the values and behavior of  $\kappa_T$  and  $\alpha_p$  for  $\text{CO}_2$  and ethane are similar the internal pressures for these fluids are very different even though these differences minimize at high temperatures in the supercritical region. In fact, the values of internal pressure for  $\text{CO}_2$  are abnormally high in comparison with those for ethane, and their behavior with temperature, given by the temperature coefficient, shows a much steeper slope than that for ethane. This can be explained if we take into account the charge separation in the molecule of  $\text{CO}_2$ , which shows as a consequence a significant quadrupolar moment. Furthermore, the dependence of the internal pressure with density was analyzed. We have found that different dense states with the same internal pressure values possess very similar densities. Finally, we conclude that the system's internal pressure will be significant only if the supercritical fluid has density-like liquid.



Additionally,  $PuT$  values have been determined for water and ethane within a broad range of pressure and temperature, using a device based on a 5 MHz pulsed ultrasonic system. The precision of the experimental data obtained with this apparatus has been determined by comparison between our measured values of speed of sound and those from the reference EoS for water<sup>12</sup> and compressed ethane.<sup>7</sup> The values obtained, given as MRDs, are 0.06% for water and 0.1% for compressed ethane.

From speed of sound and density values, isentropic compressibilities,  $\kappa_s$ , have been obtained for ethane, and with these and our values of  $\rho$ ,  $\kappa_T$ , and  $\alpha_p$ , isobaric heat capacities,  $C_p$ , have been calculated and compared with those from EoS;<sup>7</sup> the MRD( $C_p$ ) obtained is 3%, which is acceptable since it is within that of the EoS.

## APPENDIX A

The mean relative deviation, MRD( $x$ ), is calculated as follows:

$$\text{MRD}(x) = \frac{100}{N} \sum_{i=1}^N \left| \frac{x_i^{\text{exp}} - x_i^{\text{cal}}}{x_i^{\text{exp}}} \right| \quad (\text{A.1})$$

where

- $x_i^{\text{exp}}$  experimental value of a point
- $x_i^{\text{cal}}$  calculated value for a point
- $N$  number of points

The relative mean standard deviation,  $\overline{S}_x^r$  is calculated

$$\overline{S}_x^r = \frac{100}{N_p} \sum_{j=1}^{N_p} ({}_j S_x^r) \quad (\text{A.2})$$

where the relative standard deviation by point is

$${}_j S_x^r = \frac{{}_j S_x}{\frac{1}{n} \sum_{i=1}^n x_i^{\text{exp}}} \quad (\text{A.3})$$

and the standard deviation by point is

$${}_j S_x = \sqrt{\frac{n \sum_{i=1}^n (x_i^{\text{exp}})^2 - \left( \sum_{i=1}^n x_i^{\text{exp}} \right)^2}{n(n-1)}} \quad (\text{A.4})$$

## ASSOCIATED CONTENT

**S** Supporting Information. Experimental values of  $P-\rho-T$  for pure CO<sub>2</sub>, ethane, propane, and binary mixtures [CO<sub>2</sub> + ethane]. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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## LIST OF SYMBOLS

$P$	pressure
$T$	temperature
$\rho$	density
$u$	sound-speed
$\kappa_T$	isothermal compressibility
$\alpha_p$	isobaric thermal expansivity
$\pi_i$	internal pressure
$\kappa_s$	isentropic compressibility
$C_p$	isobaric heat capacity
EoS	equation of state
MRD	mean relative deviation

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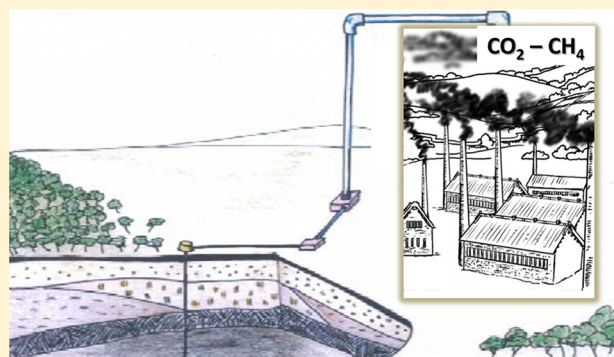
# Influence of Methane in CO<sub>2</sub> Transport and Storage for CCS Technology

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**S** Supporting Information

**ABSTRACT:** CO<sub>2</sub> Capture and Storage (CCS) is a good strategy to mitigate levels of atmospheric greenhouse gases. The type and quantity of impurities influence the properties and behavior of the anthropogenic CO<sub>2</sub>, and so must be considered in the design and operation of CCS technology facilities. Their study is necessary for CO<sub>2</sub> transport and storage, and to develop theoretical models for specific engineering applications to CCS technology. In this work we determined the influence of CH<sub>4</sub>, an important impurity of anthropogenic CO<sub>2</sub>, within different steps of CCS technology: transport, injection, and geological storage. For this, we obtained new pressure–density–temperature ( $P\rho T$ ) and vapor–liquid equilibrium (VLE) experimental data for six CO<sub>2</sub> + CH<sub>4</sub> mixtures at compositions which represent emissions from the main sources in the European Union and United States. The  $P$  and  $T$  ranges studied are within those estimated for CO<sub>2</sub> pipelines and geological storage sites. From these data we evaluated the minimal pressures for transport, regarding the density and pipeline's capacity requirements, and values for the solubility parameter of the mixtures, a factor which governs the solubility of substances present in the reservoir before injection. We concluded that the presence of CH<sub>4</sub> reduces the storage capacity and increases the buoyancy of the CO<sub>2</sub> plume, which diminishes the efficiency of solubility and residual trapping of CO<sub>2</sub>, and reduces the injectivity into geological formations.



## 1. INTRODUCTION

Carbon Dioxide Capture and Storage (CCS) is one of several effective strategies (along with energy efficiency, fuel switching, and use of renewable energy sources) to reduce greenhouse gas (GHG) levels in the atmosphere in the medium term.<sup>1–3</sup>

CCS is usually considered as a process consisting of four main separate steps: CO<sub>2</sub> capture, CO<sub>2</sub> conditioning, CO<sub>2</sub> transport, and CO<sub>2</sub> injection and storage.

CO<sub>2</sub> capture can be performed by different techniques (postcombustion, precombustion decarbonization, and oxyfuel combustion) and conditioned via dehydration, noncondensable gas separation and/or liquefaction, and compression/pumping.<sup>4–8</sup> Even though this work is not devoted to CO<sub>2</sub> conditioning and capture, the technologies used will determine the composition of the gas to be handled. It is also important to take into account that it seems that CO<sub>2</sub> purification after capture will be very expensive. Thus, for many of the separation technologies the expense of purification greatly increases for a higher degree of purity of gaseous mixture,<sup>6</sup> therefore, it is essential the study of CO<sub>2</sub> behavior with different impurities.<sup>9</sup> On the other hand, quality specifications for transport are not currently stated. The elaboration of the corresponding regulations will require studying the influence of impurities on the thermodynamic properties of the transported and stored fluid as well. This is precisely the aim of our current study.

For over 30 years now, and within the context of EOR (enhanced oil recovery) and EGR (enhanced gas recovery), long-distance CO<sub>2</sub> transport and injection technologies have been developed. Nevertheless, there are some important differences between these technologies and CCS since CO<sub>2</sub> captured from power stations and industrial sources may contain different proportions and/or types of impurities from those found in the sources of CO<sub>2</sub> usually used in EOR and EGR. The design and operation of a CO<sub>2</sub> + impurities managing system is complicated, due to the highly nonlinear thermodynamic properties of the fluid and because it is normally transported as a dense-fluid, for operational and economic reasons.<sup>10</sup> Since the Kyoto Summit, an international network with specific research programmes devoted to CCS technology has been established. One such scheme is the FP7 Cooperation Work Programme, which includes a topic entitled “Impact of the Quality of CO<sub>2</sub> on Transport and Storage” within the Energy Theme.<sup>11</sup>

Literature shows that the presence and type of impurities clearly influence the fluid's properties and behavior, and as a consequence the design and operation of CCS facilities.<sup>12</sup>

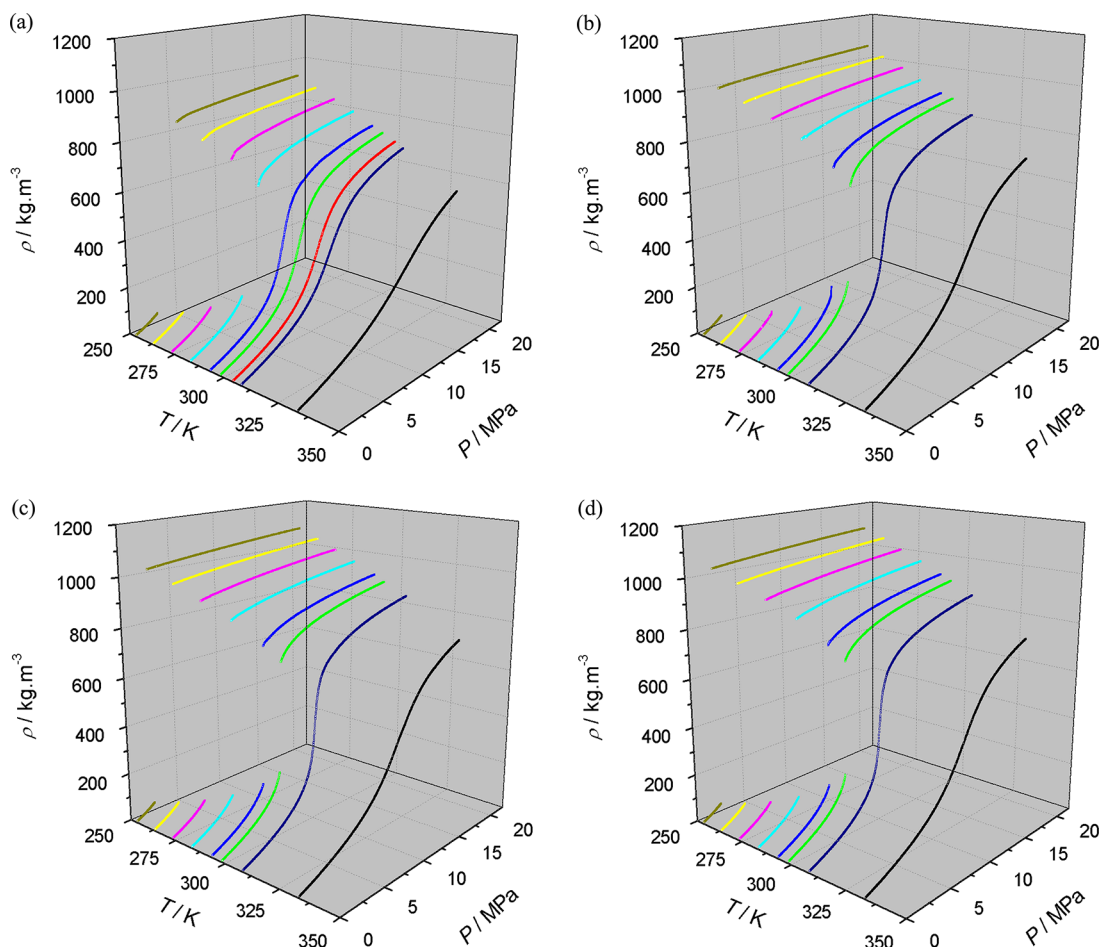
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**Figure 1.** Experimental densities,  $\rho$ , for  $\text{CO}_2 + \text{CH}_4$  mixtures with (a)  $x_{\text{CO}_2} = 0.8525$ ; (b)  $x_{\text{CO}_2} = 0.9719$ ; (c)  $x_{\text{CO}_2} = 0.9902$ , and (d)  $x_{\text{CO}_2} = 0.9961$  at several temperatures and pressures.

Knowledge of the thermodynamic properties of the  $\text{CO}_2 +$  impurities mixtures, especially pressure–volume–temperature–composition ( $PVTxy$ ) and vapor–liquid equilibrium (VLE), is therefore essential. This information will allow determination of composition specifications and purification requirements (if necessary) of the fluid in the different steps of this technology, and will enable design of efficient, safe, and economical processes.<sup>9</sup> These data are also necessary to develop reliable theoretical models for engineering applications, covering the large range of operative conditions (from atmospheric pressure to supercritical states) of multicomponent mixtures involved in CCS processes. Many equations of state (EoS), such as PR, RKS, SAFT, and GERG are available for thermodynamic calculations of  $\text{CO}_2$  mixtures, but none of them show any clear advantage in CCS applications for the calculations of all  $PVTxy$  properties, thus a reference EoS for CCS should be a future goal.<sup>9,13</sup>

This is the first work in a systematic study on binary mixtures of  $\text{CO}_2$  and the typical impurities found in industrial emissions. In this study we present reliable experimental data of pressure–density–temperature,  $P\rho T$ , and VLE, properties for mixtures of  $\text{CO}_2$  and  $\text{CH}_4$  at the compositions,  $P$ , and  $T$  ranges of interest for the transport and the storage in the CCS technologies.  $\text{CO}_2$  and  $\text{CH}_4$  are two of the six GHGs that have been targeted by the international community as causing global warming, being the environmental impact of methane emissions 21 times greater than that of carbon dioxide.<sup>1</sup> Our experimental data

were compared with those predicted by GERG EoS which is, among the above-mentioned, the most recommended by the NIST for  $\text{CO}_2 + \text{CH}_4$  mixtures and the most used for petroleum fluids and natural gas.<sup>14</sup>

From the  $P\rho T$  experimental values of  $\text{CO}_2 + \text{CH}_4$  mixtures, we evaluated the effect of impurities on several parameters related to transport, injection, and storage such as the minimal pressure for transport, the solubility parameter, the normalized storage capacity of the reservoir, the normalized rising velocity of the  $\text{CO}_2$  plume, and the normalized permeation flux.

## 2. EXPERIMENTAL SECTION

**Materials.** Carbon dioxide (wt % > 99.998) and methane (wt % > 99.995) were obtained from Air Liquide.

In Spain, compositions of the emissions from different industries are characterized and recorded by the Registro Estatal de Emisiones y Fuentes Contaminantes (PRTR España).<sup>15</sup> The highest content of methane (wt %  $\text{CH}_4 \approx 6.0\%$ ) is found in emissions from waste management (7% of the total of  $\text{CO}_2$  emitted in Spain in 2010). In addition to this, wt %  $\text{CH}_4$  varies from  $\approx 1.0\%$  for farming and livestock emissions to  $\approx 0.36\%$  for other industries such as ceramics production.<sup>15</sup> Having taken these figures into account, we chose six compositions ranging from 0.14% to 5.93% in wt % of  $\text{CH}_4$  allowing us to study representative industrial emissions in Spain. In this composition range the percentages of methane from emissions of the main sources of anthropogenic  $\text{CO}_2$  in

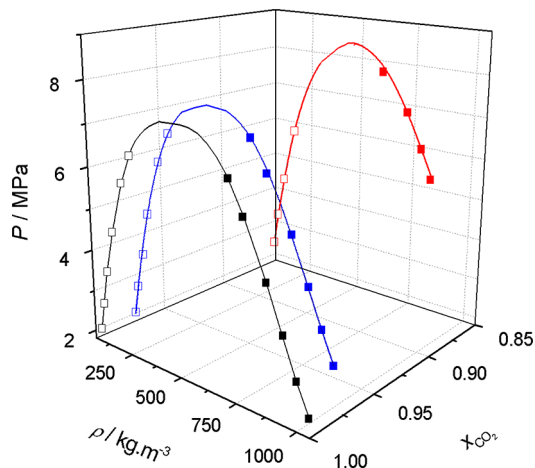
the EU and the U.S.<sup>16–19</sup> are included. The total emissions in Spain, EU, and U.S. contain wt % of CH<sub>4</sub> of 0.15%, 0.65%, and 0.55%, respectively. The mixtures were prepared by successive weighting of the components in a variable volume cell with a precision of 0.0002 g.

**Apparatus and Procedures.** The experimental setup used in this work for the determination of  $P\rho T$  data of CO<sub>2</sub> + CH<sub>4</sub> mixtures is the same as that described in a previous study.<sup>20</sup> It was designed for fast, reliable, and accurate generation of  $P\rho T$  data. Their quasi-continuous data acquisition along subcritical, critical, and supercritical regions (6000 points/isotherm evenly reduced to about 1000 points/isotherm for easier handling) allows the accurate determination of the limits of VLE and the calculation of derived properties from the experimental data.

The precision and accuracy in density results for mixtures were determined in a previous work;<sup>20</sup> the mean relative deviation, MRD ( $\rho$ ) = 0.7% and mean standard deviation,  $\bar{S}_\rho^r$  = 0.13% were obtained.

### 3. RESULTS AND DISCUSSION

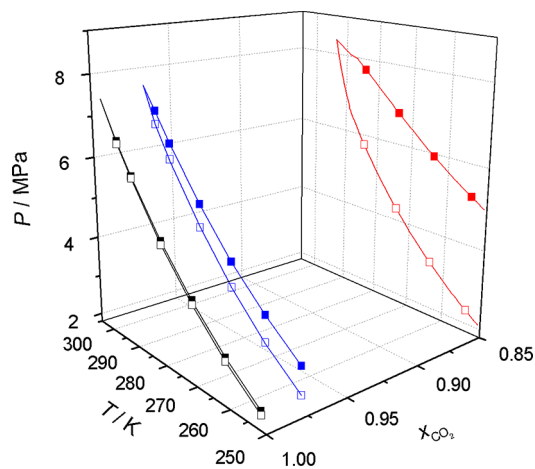
In this work we present 49 experimental  $P\rho T$  isotherms (containing a total of 49 000 points available in the Supporting



**Figure 2.** Experimental dew (blank symbols) and bubble (solid symbols) pressures,  $P_{dew}$  and  $P_{bubble}$ , and saturation densities,  $\rho_{sat}$  of the phases in equilibrium for CO<sub>2</sub> + CH<sub>4</sub> mixtures with  $x_{CO_2} = 0.8525$  (red),  $x_{CO_2} = 0.9719$  (blue), and  $x_{CO_2} = 0.9961$  (black).

Information) for six CO<sub>2</sub> + CH<sub>4</sub> mixtures (CO<sub>2</sub> mole fraction,  $x_{CO_2} = 0.8525, 0.9719, 0.9809, 0.9902, 0.9932,$  and  $0.9961$ ) from atmospheric pressure to 20 MPa, and at 253.15, 263.15, 273.15, 283.15, 293.15, 298.15, 308.15, and 333.15 K. In the case of the mixture with  $x_{CO_2} = 0.8525$  the isotherm at 304.21 K ( $T_c$  of CO<sub>2</sub>) is presented too. Properties were measured in  $P$  and  $T$  ranges which are within the estimated pressures and temperatures in CO<sub>2</sub> pipelines (7.5–20 MPa and 273–303 K)<sup>9</sup> and in geologic storage sites on the basis of a geothermic gradient<sup>21</sup> of 25 K/km and an average gradient of hydrostatic pressure of 10 MPa/km.

From these  $P\rho T$  experimental data we obtained the dew and bubble pressures,  $P_{dew}$  and  $P_{bubble}$ , and the densities of the phases in equilibrium ( $\rho_{sat}$ ) for each mixture at the corresponding subcritical temperatures, as well as the derivative properties  $\alpha_p$  (isobaric thermal expansivity),  $\kappa_T$  (isothermal compressibility), and  $\pi$  (internal pressure). Besides, we



**Figure 3.** Phase envelopes for CO<sub>2</sub> + CH<sub>4</sub> mixtures with  $x_{CO_2} = 0.8525$  (red),  $x_{CO_2} = 0.9719$  (blue), and  $x_{CO_2} = 0.9961$  (black). Open symbols, dew pressures,  $P_{dew}$ ; solid symbols, bubble pressures,  $P_{bubble}$ .

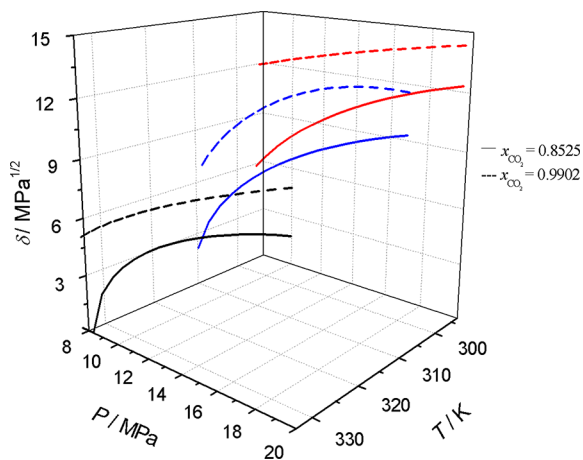
**Table 1.** Values of Minimal Compressing Pressure,  $P$ , Required to Obtain a Density of 800 kg/m<sup>3</sup> for Transport of Pure CO<sub>2</sub><sup>20</sup> or a CO<sub>2</sub> + CH<sub>4</sub> Mixture with  $x_{CO_2} = 0.9961$  or  $x_{CO_2} = 0.8525$

T (K)	P (MPa)		
	pure CO <sub>2</sub> <sup>14,20</sup>	$x_{CO_2} = 0.9961$	$x_{CO_2} = 0.8525$
253.15	1.970	2.094	5.233
263.15	2.649	2.758	6.031
273.15	3.485	3.626	12.859
283.15	4.502	4.700	18.951
293.15	6.626	7.014	>20
298.15	9.017	9.367	
304.21	11.987	12.359	
308.15	13.904	14.239	
333.15	26.398	>20	

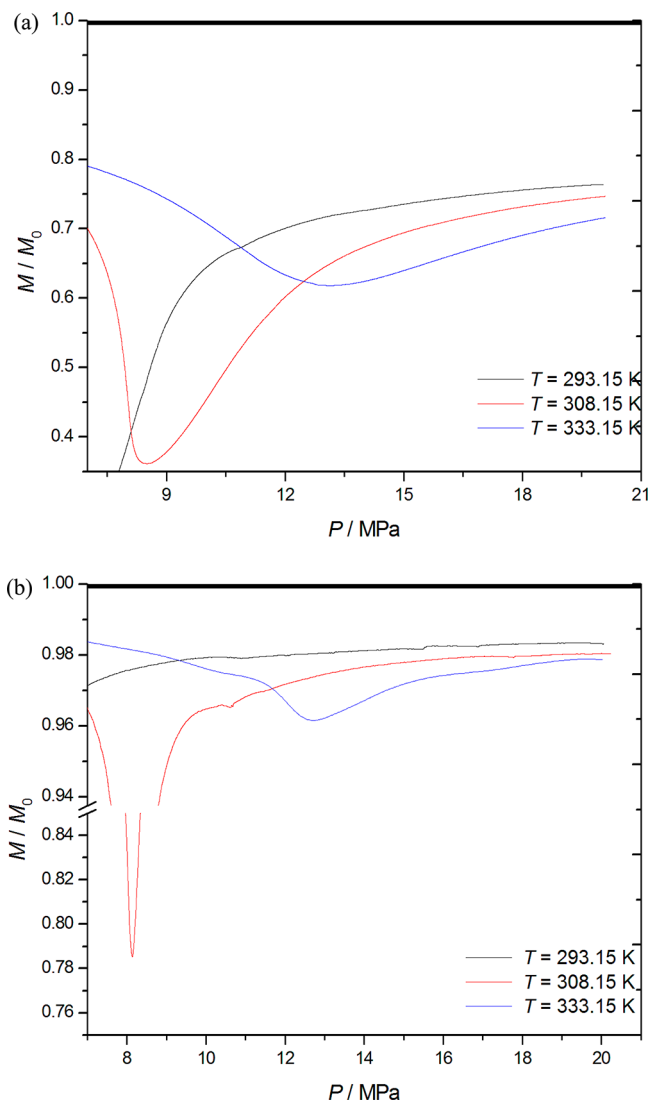
**Table 2.** Bubble Pressure Values,  $P_{bubble}$ , for Pure CO<sub>2</sub><sup>14</sup> and for CO<sub>2</sub> + CH<sub>4</sub> Mixtures with  $x_{CO_2} = 0.9961$  and  $x_{CO_2} = 0.8525$

T (K)	$P_{bubble}$ (MPa)		
	pure CO <sub>2</sub> <sup>14</sup>	$x_{CO_2} = 0.9961$	$x_{CO_2} = 0.8525$
253.15	1.9696	2.073	5.232
263.15	2.6487	2.753	6.031
273.15	3.4851	3.622	7.000
283.15	4.5022	4.608	7.741
293.15	5.7291	5.827	
298.15	6.4342	6.532	

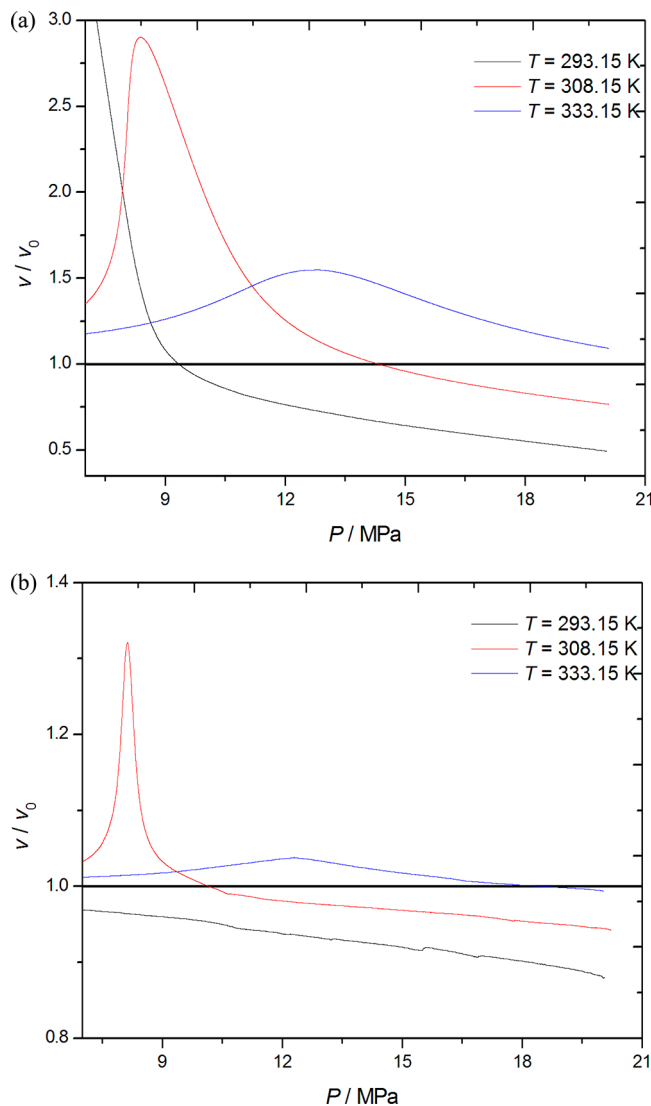
evaluated the minimal pressures for transport, regarding the density and pipeline’s capacity requirements, and the effect of impurities on the solubility parameter,  $\delta$ . This parameter will govern the interactions between the injected CO<sub>2</sub> and the substances previously present in the reservoir, such as methane itself among others. Last, we calculated, using our experimental data, values for other parameters related to storage such as the normalized storage capacity of the reservoir and the normalized rising velocity of the plume by means of the approach that Wang et al. used for other impurities.<sup>22</sup> Acting in this fashion, the experimental data will give realistic information about what



**Figure 4.** Solubility parameters,  $\delta$ , for  $\text{CO}_2 + \text{CH}_4$  mixtures with  $x_{\text{CO}_2} = 0.8525$  (continuous line);  $x_{\text{CO}_2} = 0.9902$  (dashed line) at 293.15 K (red), 308.15 K (blue), and 333.15 K (black).



**Figure 5.** Normalized  $\text{CO}_2$  storage capacity,  $M/M_0$ , for  $\text{CO}_2 + \text{CH}_4$  mixtures with (a)  $x_{\text{CO}_2} = 0.8525$  and (b)  $x_{\text{CO}_2} = 0.9902$  at 293.15, 308.15, and 333.15 K.

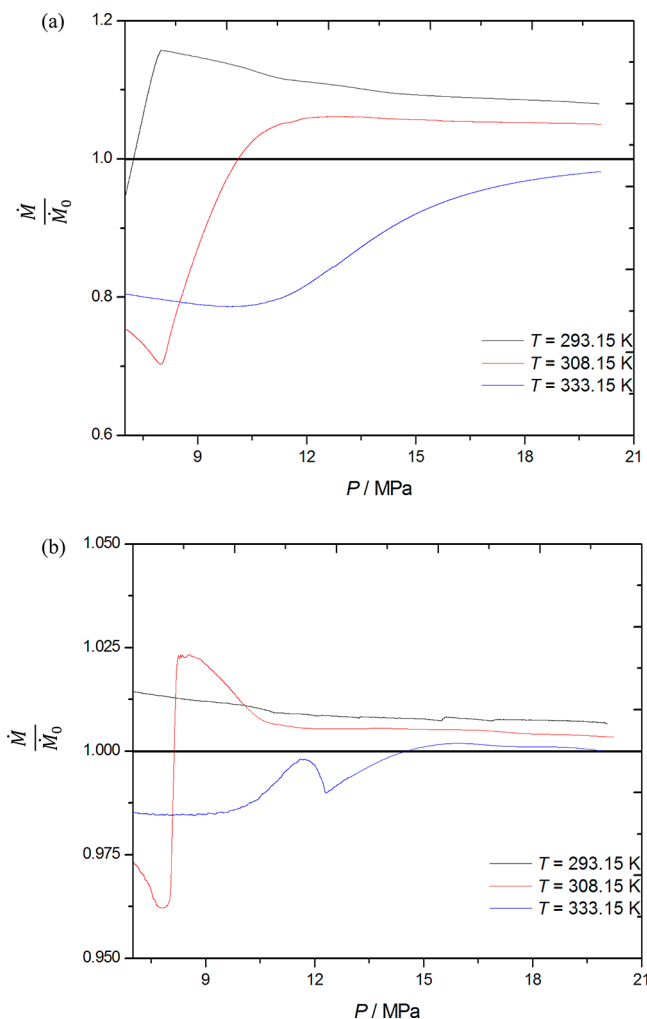


**Figure 6.** Normalized rising velocity of the plume,  $v/v_0$ , for  $\text{CO}_2 + \text{CH}_4$  mixtures with (a)  $x_{\text{CO}_2} = 0.8525$  and (b)  $x_{\text{CO}_2} = 0.9902$  at 293.15, 308.15, and 333.15 K.

is happening inside the reservoirs after injection of  $\text{CO}_2$ . The normalized permeation flux,<sup>22</sup> which provides a measure of the relative injectivity of the impure  $\text{CO}_2$  stream, has been also calculated from our data and the viscosity data from GERG EoS.<sup>14</sup>

Figure 1a, b, c, and d show the experimental densities for four of the six  $\text{CO}_2 + \text{CH}_4$  mixtures which include the whole range of composition studied. The representations corresponding to the rest of the mixtures are included in Figures S1a and S1b and the complete  $P\rho T$  experimental data are listed in Table S1, both in the Supporting Information. In these graphics, the density of the mixtures at subcritical temperatures shows a discontinuity in the liquid–vapor equilibrium zone which is limited by the dew point in the low pressure regions and by the bubble point in the high pressure regions. However, the representation at supercritical temperatures is a continuous line.

In Figures 2 and 3 the VLE properties are represented for the mixtures at  $x_{\text{CO}_2} = 0.8525, 0.9719,$  and  $0.9961$  (Figure 2, dew and bubble pressures and densities of the phases in equilibrium, hence the limits of the discontinuities in Figure 1 mentioned



**Figure 7.** Normalized permeation flux,  $\dot{M}/\dot{M}_0$ , for  $\text{CO}_2 + \text{CH}_4$  mixtures with (a)  $x_{\text{CO}_2} = 0.8525$  and (b)  $x_{\text{CO}_2} = 0.9902$  at 293.15, 308.15, and 333.15 K.

before; Figure 3, the corresponding  $P$ – $T$ – $x_{\text{CO}_2}$  projections). For the rest of the mixtures similar representations can be found in Figures S2 and S3, and the corresponding values in Table S2.

There are numerous publications on  $\text{CO}_2 + \text{CH}_4$  system in the literature, but not for the compositions and conditions of interest for CCS technology. We have found three publications which give values of density<sup>23</sup> and VLE properties<sup>24,25</sup> at conditions similar to ours (but not the same). Magee and Ely<sup>23</sup> give values for density of  $\text{CO}_2 + \text{CH}_4$  with  $x_{\text{CO}_2} = 0.98$  that are in good agreement with our data. Also, our value for bubble pressure at 293.15 K for this mixture agrees with that from these authors. Furthermore, we have found reasonable agreement between our pressures for VLE and those reported by Xu et al.<sup>24</sup> and Donnelly and Katz.<sup>25</sup>

Our experimental data for density and VLE have been compared with those predicted by GERG EoS.<sup>14</sup> The obtained deviations are  $\text{MRD}(\rho) = 0.28\%$ ,  $\text{MRD}(P_{\text{dew}}, P_{\text{bubble}}) = 0.15\%$ , and  $\text{MRD}(\rho_{\text{sat}}) = 0.45\%$ , which are within the margins of error given by the authors.

**Influence of Impurities in Transport.**  $\text{CO}_2$  is transported through pipelines over long distances as a dense-phase fluid at densities from 800 to 1000  $\text{kg}/\text{m}^3$ . To achieve this density

requirement at the different operating temperatures, the minimal transport pressure will depend on the composition of the  $\text{CO}_2$  transported. Table 1 shows the values of minimal compressing pressure required to obtain a density of 800  $\text{kg}/\text{m}^3$  if the fluid transported is pure  $\text{CO}_2$ ,<sup>14,20</sup> or if it is a  $\text{CO}_2 + \text{CH}_4$  mixture with  $x_{\text{CO}_2} = 0.8525$  or  $x_{\text{CO}_2} = 0.9961$  (from our experimental  $P\rho T$  data). As it can be seen, for the  $\text{CO}_2$  rich mixture the required values of pressure are slightly higher but similar to those for pure  $\text{CO}_2$  at 253.15 K. For a mixture characterized as the binary  $\text{CO}_2 + \text{CH}_4$  with  $x_{\text{CO}_2} = 0.8525$ , the minimal value of pressure required in the pipeline is almost three times that for pure  $\text{CO}_2$ , and this proportion increases as temperature increases, so that the required pressure at 283.15 K is more than four times the value for pure  $\text{CO}_2$ .

The presence of impurities in the transported fluid modifies the limits of VLE as well, and hence the value for the bubble pressure for a given temperature, as shown in Figure 2. In the transport by pipeline, the operating pressure cannot be lower than the bubble pressure of the fluid to avoid the presence of vapor phase which would diminish the pipeline's capacity. In Table 2 bubble pressure data for pure  $\text{CO}_2$ <sup>14</sup> and  $\text{CO}_2 + \text{CH}_4$  ( $x_{\text{CO}_2} = 0.8525$  and  $x_{\text{CO}_2} = 0.9961$ ) mixtures are listed for the subcritical temperatures studied. Although these bubble pressures are lower than those necessary to fulfill the density requirements, the conditions in which the fluid's pressure is lower than those values of pressure should be avoided in the different types of operations that take place in the transport network.

**Influence of Impurities in Storage and Injection.** There are different sites which are suitable candidates for geological storage: deep saline aquifers, depleted oil and gas fields, and nonexploitable coal seams.<sup>26</sup> The anthropogenic  $\text{CO}_2$ -trapping mechanism and the influence of impurities can be different according to the kind of reservoir. Inside the reservoirs, there will be interactions between the substances present before the injection and the injected anthropogenic  $\text{CO}_2$  ( $\text{CO}_2 + \text{impurities}$ ). Methane can be present in the reservoir before injection and as a component of anthropogenic  $\text{CO}_2$ . In the study on solvent–solute intermolecular forces, we propose the anthropogenic  $\text{CO}_2$  stream to be labeled as the solvent, and those substances present beforehand in the reservoir as solutes. The solvent will probably be in a supercritical state because of the conditions of temperature and pressure inside the reservoir. Fluid in this state presents two characteristic properties: a great ability to dissolve nonvolatile substances (several orders of magnitude greater than in the gas state), and a wide variability of this solvent's capacity with the operating conditions ( $T$ ,  $P$ ). The concept of solubility parameter, introduced by Hildebrand and Scott in 1950,<sup>27</sup> has been extensively used for more than sixty years to interpret and predict the thermodynamic behavior of liquid solutions in a semiquantitative way,<sup>28–31</sup> and has also been extended to nonpolar and slightly polar supercritical fluids.<sup>20,32</sup> The solubility parameter,  $\delta$ , was defined by Hildebrand and Scott as

$$\delta = \left( \frac{-E(T)}{V(T, P)} \right)^{1/2} \quad (1)$$

where  $-E$  is the cohesive energy and  $V$  is the molar volume of the liquid, with  $(-E/V)$  being the so-called “cohesive energy density”. Hansen<sup>28</sup> assumes the cohesive energy to be an



additive quantity composed of a dispersive (d), a polar (p), and a hydrogen-bond (h) contribution

$$E = E_d + E_p + E_h \quad (2)$$

and, therefore,

$$\delta^2 = \delta_d^2 + \delta_p^2 + \delta_h^2 \quad (3)$$

Bagley et al.<sup>30</sup> subdivide the solubility parameter in two parts:

$$\delta^2 = \delta_V^2 + \delta_R^2 \quad (4)$$

where  $\delta_V^2 = \delta_d^2 + \delta_p^2$  corresponds to the “physical” or “non-chemical” effects and is known as the “volume-dependent solubility (or cohesion) parameter”, which is defined by

$$\delta_V^2 = \pi \quad (5)$$

where  $\pi$  is the internal pressure. The other component,  $\delta_R$ , is a “residual” parameter, which results from “chemical” effects. Since hydrogen bonding is not present in our system, it seems appropriate to neglect the residual contribution and to use the internal pressure to estimate the solubility parameter<sup>31</sup>

$$\delta^2 = \delta_V^2 = \pi \quad (6)$$

which is a relationship between the solubility parameter and the internal pressure earlier used by Hildebrand and Scott.<sup>27</sup> Allada et al.<sup>32</sup> suggest that the solubility parameters are the determinant key of solubility of the solutes in supercritical solvents and that they apparently unify diverse behaviors of solvents regardless of kind,  $T$ , or  $P$ . In this work, we propose to apply this concept to stored anthropogenic CO<sub>2</sub>. Hence, in storage of anthropogenic CO<sub>2</sub>, the solubilization of substances present beforehand will depend on interactions between these solutes and the supercritical fluid, and as we have shown this behavior can be approximated if we know the values for internal pressure of the mixture which is injected for storage.

The internal pressure is defined as

$$\pi = \left( \frac{\partial U}{\partial V} \right)_T = T \left( \frac{\partial P}{\partial T} \right)_V - P \quad (7)$$

In this equation, we can write

$$\left( \frac{\partial P}{\partial T} \right)_V = - \left( \frac{1}{\rho} \right) \left( \frac{\partial \rho}{\partial T} \right)_P \frac{1}{\left( \frac{1}{\rho} \right) \left( \frac{\partial \rho}{\partial P} \right)_T} = \frac{\alpha_p}{\kappa_T} \quad (8)$$

where  $\alpha_p$  is the isobaric thermal expansivity and  $\kappa_T$  is the isothermal compressibility. We calculated  $\alpha_p$ ,  $\kappa_T$ , and  $\pi$  values (see Supporting Information) from our  $P\rho T$  experimental data. Solubility parameters are represented in Figure 4 for mixtures with  $x_{\text{CO}_2} = 0.8525$  and  $x_{\text{CO}_2} = 0.9902$  at 293.15, 308.15, and 333.15 K. As can be seen, the solubility parameters decrease as the methane mole fraction increases in the anthropogenic CO<sub>2</sub>. For each mole fraction studied, the greatest value of the parameter is obtained for the compressed liquid mixtures, and decreases as temperature increases and pressure decreases.

Noncondensable impurities, such as methane, will increase the compression pressure needed for injection and reduce the capacity of the storage sites because the density of the mixture will decrease. Wang, et al.<sup>22</sup> proposed the following expression for the storage capacity, expressed in mass, as a function of the density of the CO<sub>2</sub> stream:

$$\frac{M}{M_0} = \frac{\rho}{\rho_0 \left[ 1 + \sum_i \left( \frac{m_i}{m_0} \right) \right]} \quad (9)$$

where  $M$  and  $M_0$  denote, respectively, the mass of CO<sub>2</sub> in the mixture and in the pure CO<sub>2</sub> stream which occupies the same volume or its ratio per unit volume.  $\rho$  and  $\rho_0$  are the densities of the mixture and the pure CO<sub>2</sub> stream, and  $m_i/m_0$  is the ratio of the mass of impurity  $i$  to the mass of CO<sub>2</sub> in the mixture. The ratio  $M/M_0$  on the left-hand side of this relation represents a normalized storage capacity for CO<sub>2</sub>, i.e. the capacity for structural trapping of CO<sub>2</sub>. In the case of pure CO<sub>2</sub> (zero impurity effect) the ratio equals unity. The right-hand side is a function of temperature, pressure, and mixture composition and has been calculated from our  $P\rho T$  experimental data. Accordingly, the normalized storage capacity has been determined, and Figure 5a and b show the results for CO<sub>2</sub> + CH<sub>4</sub> mixtures with  $x_{\text{CO}_2} = 0.8525$  and  $x_{\text{CO}_2} = 0.9902$ , respectively, at three temperatures that can be found in storage at different depths: 293.15, 308.15, and 333.15 K. As can be observed, the presence of CH<sub>4</sub> negatively affects the mass of CO<sub>2</sub> which can be stored in a given reservoir. At a given temperature, for any reservoir, the lowest value of anthropogenic CO<sub>2</sub> stored (expressed by mass) corresponds to the richest methane mole fractions (Figure 5a). The deeper the location of the reservoir (higher values of  $T$  and  $P$ ) the greater is the mass of CO<sub>2</sub> which can be potentially stored. If we consider a depth from 1000 to 2000 m, the pressure of the injected CO<sub>2</sub> will range from 10 to 20 MPa, and the average temperature will be 333.15 K (for an average gradient of hydrostatic pressure of 10 MPa/km and a geothermic gradient<sup>21</sup> of 25 K/km). Under these conditions, the storage capacity can be reduced to a figure as low as 60% for the mixture with  $x_{\text{CO}_2} = 0.8525$  and 96% for the mixture with  $x_{\text{CO}_2} = 0.9902$  (Figure 5a and b).

In general, the presence of noncondensable impurities (i.e., methane) in anthropogenic CO<sub>2</sub> causes a decrease in the CO<sub>2</sub> storage capacity, with a minimum at a given  $P$  for each  $T$  (Figure 5a and b). As a consequence, the effect of pressure has to be taken into account in the estimation of the capacity of underground formations. To increase the efficiency of the storage, both the pressure of injection and the depth inside the reservoir should be combined. At a given depth ( $T = \text{constant}$ ), increasing the storage pressure well beyond the minimum pressure would improve the storage efficiency (Figure 5a and b). For closed reservoirs, this may be achieved by increasing the injection pressure within the allowable overpressure range; for open formations where overpressure may not be attainable, increasing the depth of injection and storage is the only option.

In deep saline aquifers, the presence of impurities affects parameters related to storage, such as the buoyancy and the rising velocity. The presence of light-impurity species, such as CH<sub>4</sub>, generates a greater buoyancy of the CO<sub>2</sub> plume, due to its lower density. For a given mass of the plume in a unit volume in contact with the site water, the buoyant force,  $F$ , can be expressed as

$$F = (\rho_{\text{H}_2\text{O}} - \rho)g \quad (10)$$

where  $\rho_{\text{H}_2\text{O}}$  and  $\rho$  are the densities of the water and the plume, respectively, and  $g$  is the gravitational acceleration. The effect of impurities on this force with reference to pure CO<sub>2</sub> may be given as

$$\frac{F}{F_0} = \frac{\rho_{\text{H}_2\text{O}} - \rho}{\rho_{\text{H}_2\text{O}} - \rho_0} \quad (11)$$

where  $F$  and  $F_0$  are the buoyant forces for the  $\text{CO}_2$  mixture and pure  $\text{CO}_2$ , respectively. The greater the difference between the densities of anthropogenic  $\text{CO}_2$  ( $\rho$ ) and pure  $\text{CO}_2$  ( $\rho_0$ ), the greater the change in the buoyancy will be. If impurities are noncondensable,  $\rho < \rho_0$ , the buoyancy increases, and this in turn will significantly increase the rising velocity of the plume,  $v$ . The rising velocity for the  $\text{CO}_2$  mixture,  $v$ , can be related to that of the pure  $\text{CO}_2$  stream,  $v_0$ , by<sup>22</sup>

$$\frac{v}{v_0} = \frac{F/(\rho\eta)}{F_0/(\rho_0\eta_0)} \quad (12)$$

where  $\eta$  is the viscosity of the  $\text{CO}_2$  impure stream and  $\eta_0$  is that of pure  $\text{CO}_2$ . In Figure 6, the relations  $v/v_0$  for  $\text{CO}_2 + \text{CH}_4$  with  $x_{\text{CO}_2} = 0.8525$  (Figure 6a) and  $x_{\text{CO}_2} = 0.9902$  (Figure 6b) at 293.15, 308.15, and 333.15 K, are represented against pressure. The values for the relations were calculated from our experimental  $P\rho T$  data and values for viscosity from GERG EoS.<sup>14</sup> For the two mixtures, the  $v/v_0$  relations present maxima at 308.15 and 333.15 K inside the pressure range represented in the figures. For the  $\text{CH}_4$ -richest mixture at 308.15 K, the rising velocity can reach nearly three times that of the pure  $\text{CO}_2$  plume. At 333.15 K, which would be the average temperature at depths from 1000 to 2000 m, the maxima, for the two compositions, are found exactly at pressures inside the ranges corresponding to those depths (10–20 MPa). For  $x_{\text{CO}_2} = 0.8525$ , the rising velocity of the fluid, at this temperature, can be more than 1.5 times that of the pure  $\text{CO}_2$  plume (Figure 6a), but for  $x_{\text{CO}_2} = 0.9902$  this relation diminishes to almost 1 (Figure 6b). An elevated rising velocity makes the time for  $\text{CO}_2$ –water contact in the reservoir shorten, with less dissolving effect. The lateral spreading of the plume will be diminished as well, and as a consequence the area for trapping  $\text{CO}_2$  in the rock's pores will decrease, with a reduction in the formation of a residual phase. When the plume makes contact with the cap rock layer and is retained under, it spreads laterally, but the contact with saline water happens only at the interface. Moreover, near the cap rock, at a lower depth, the pressure is lower than in the deeper region, and therefore the efficiency of both solubility and residual trapping will be lower. Therefore, the risk for leakage increases if pathways are available.

In relation to injection, to analyze the differences due to the type of the fluid injected, pure  $\text{CO}_2$  or anthropogenic  $\text{CO}_2$ , an expression based on Darcy's law can be used to calculate the permeation flux

$$\dot{M} = \frac{\rho k}{\eta} \nabla P \quad (13)$$

Where  $\dot{M}$  is the mass flow per unit area,  $\rho$  and  $\eta$  are the density and the viscosity, respectively, of the injected fluid,  $k$  is the rock permeability,  $\nabla$  is the gradient operator, and  $P$  is the pressure. Noncondensable impurities reduce the density of the  $\text{CO}_2$  stream, and the mass flux will decrease for the same pressure drop and viscosity. Additionally, impurities will also affect the viscosity of the fluid, and the mass flow will increase if the viscosity of the impure  $\text{CO}_2$  stream is lower than the viscosity of pure  $\text{CO}_2$ . Therefore, the decrease in density may be compensated by a corresponding decrease in viscosity. Both

density and viscosity are functions of temperature and pressure, and the rock permeability and pressure gradient vary for each particular site. Nevertheless, we may use the following relation for an estimation of the impurity effects under the same permeability and pressure drop conditions<sup>22</sup>

$$\frac{\dot{M}}{\dot{M}_0} = \frac{\rho\left(\frac{\eta_0}{\eta}\right)}{\rho_0\left[1 + \sum_i\left(\frac{m_i}{m_0}\right)\right]} \quad (14)$$

where  $\dot{M}$ ,  $\eta$ , and  $\rho$  are the mass flow per unit area, viscosity, and density of the anthropogenic  $\text{CO}_2$ , and  $\dot{M}_0$ ,  $\eta_0$ , and  $\rho_0$  those of the pure  $\text{CO}_2$ . The bracket in the denominator introduces a correction for impurities as in eq 9. Equation 14 represents a normalized permeation flux and allows estimating the relative injectivity of the impure  $\text{CO}_2$  stream.

We calculated the values of  $\dot{M}/\dot{M}_0$  for mixtures with  $x_{\text{CO}_2} = 0.8525$  and  $x_{\text{CO}_2} = 0.9902$  at 293.15, 308.15, and 333.15 K, using our experimental  $P\rho T$  data and calculated values for viscosity.<sup>14</sup> In Figure 7a and b, the values obtained for the relation are represented against pressure. It can be observed that for pressures from 10 to 20 MPa, the permeation flux at 293.15 and 308.15 K for the two mixtures is higher than that for pure  $\text{CO}_2$ . At 333.15 K the trend changes, and the permeation flux of the mixture poorest in  $\text{CO}_2$  is lower than that of pure  $\text{CO}_2$ , trending toward 1 as pressure increases; for the other mixture, the permeation flux is lower than 1 up to 14 MPa, and approximately equals 1 from this pressure.

## ■ ASSOCIATED CONTENT

### ● Supporting Information

$P$ - $\rho$ - $T$  experimental values for  $\text{CO}_2 + \text{CH}_4$  mixtures;  $\rho$ - $T$ - $P$  representations;  $P$ - $\rho_{\text{sat}}$ - $x_{\text{CO}_2}$  and  $P$ - $T$ - $x_{\text{CO}_2}$  values and representations of VLE;  $\kappa_T$ - $T$ - $P$ ,  $\alpha_P$ - $T$ - $P$ , and  $\pi$ - $P$ - $T$  values and representations. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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### Notes

The authors declare no competing financial interest.

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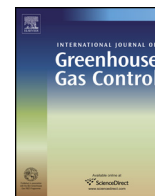
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# Influence of methane and carbon monoxide in the volumetric behaviour of the anthropogenic CO<sub>2</sub>: Experimental data and modelling in the critical region



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## ABSTRACT

Density measurements of the systems CO<sub>2</sub> + CH<sub>4</sub> at  $T=304.21$  K and CO<sub>2</sub> + CO at  $T=304.21$  and  $308.15$  K were carried out at pressures and compositions of interest in the process of transport and storage of CO<sub>2</sub> (CCS technology):  $P=0.1$  to 20 MPa, and  $x_{\text{CO}_2} \geq 0.97$ . From the experimental  $P-\rho-T-x_{\text{CO}_2}$  data, we have studied the dependence of the isothermal compressibility, the excess molar volume, and the partial molar volume of the solute with composition, pressure and temperature within the critical region. We have modelled the volumetric behaviour of these systems with Peng–Robinson, PC-SAFT and GERG Equations of State, thus validating these equations under the conditions considered. Furthermore, we have confirmed the weakly attractive behaviour of these systems by performing a study of the interactions between solvent molecules, CO<sub>2</sub>, and those of the solute, CO or CH<sub>4</sub>, using the Krichevskii Function concept and the Kirkwood–Buff Theory. Finally, we have quantified the influence of small amounts of CH<sub>4</sub> and CO in the transport of anthropogenic CO<sub>2</sub> through several normalized parameters, related to the design and operation of the fluid transport process.

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## 1. Introduction

Nowadays new technologies are being developed in order to reduce CO<sub>2</sub> emissions originated from industrial processes. For instance, CO<sub>2</sub> capture by algae and subsequent transformation into biomass in a process similar to photosynthesis (Ramachandriya et al., 2013); obtaining combustible materials or other high added value substances from its photocatalytic and electrochemical reduction (Ghasemi et al., 2013); purification and treatment of drinking water (Vo et al., 2013) and food preservation, (Al-Nehlawi et al., 2013). However, the technology that will furthest reduce carbon dioxide in the atmosphere is the capture, transport and storage of CO<sub>2</sub> (CCS technology). According to the International Energy Agency (IEA/CSLF, 2010), the contribution of this technology to atmospheric CO<sub>2</sub> reduction by 2050 is expected to be of the order of 20% and the reduction achieved by greater energy efficiency of 36% (horizon 2050). In CCS, anthropogenic CO<sub>2</sub> (CO<sub>2</sub> from human activity) is processed in order to increase its CO<sub>2</sub> content (to 85–99.5% CO<sub>2</sub>), then transported to a storage site and injected and stored in the chosen reservoir.

The phase diagram of a pure compound shows that at temperatures and pressures above its critical point (for pure CO<sub>2</sub>,  $P_c=7.383$  MPa,  $T_c=304.21$  K (Gil et al., 2008)), the gas and liquid phases are indistinguishable and there is only one phase present, known as a supercritical phase, which exhibits viscosity and density values intermediate between the values of liquids and gases. If we consider that the volume occupied by CO<sub>2</sub> under supercritical conditions is about 350 times smaller than that occupied in gas phase, and that the viscosity under these conditions is relatively small, the most economical means of transporting CO<sub>2</sub> through pipelines is going to be either as a supercritical fluid or as a dense fluid. The supercritical region lies above the critical temperature and pressure and the “dense phase region” is located above the critical pressure, but below the critical temperature.

However, the transported fluid is not pure CO<sub>2</sub>, as it contains other compounds derived from both the emission sources and the capture and conditioning processes. The presence of these “impurities” in CO<sub>2</sub> changes its thermodynamic properties: the position of the critical point is affected and the line of liquid–vapour equilibrium is transformed into a phase envelope, enclosing a two-phase region; thus fluid composition determines the minimum pressure necessary to ensure transport in supercritical or dense phase. There are different reasons why transport, and, in general, any operation should be avoided under two-phase flow in this technology (Knoope et al., 2013): (i) cavitation produced by bubble

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implosion in the two-phase region generates shock waves which may cause cracks in the pipeline; (ii) turbulence caused by the bubbles hinder the work of compressors and pumps; and (iii) two-phase flow reduces the quantity of fluid transported. In any case, multiphase flow conditions seem to be unavoidable at startup/failure modes. An equation of state, EoS, for solid CO<sub>2</sub> has been recently published (Trusler, 2011, 2012) that can be solved simultaneously with an equation for the fluid phases to obtain solid–vapour and solid–liquid equilibria, which can be of practical importance when calculating the discharge rate in the event of pipeline failure.

One of the characteristic properties of supercritical fluids in the region near the critical point is the wide variation caused in the density and compressibility values when small changes in pressure, temperature and composition occur. These properties, in turn, influence various parameters that affect the process of transport, having an impact on the overall economic cost of the facilities (ElementEnergy, 2010; Knoope et al., 2013): pipeline diameter, pressure drop, erosional velocity, capacity of the booster stations, etc. As for the injection and storage processes, the density variation due to the presence of impurities affects parameters such as injection flow, solubility parameter, storage capacity and rising velocity of the plume (Blanco et al., 2012).

The variety of emission sources, capture and conditioning processes as well as the storage reservoirs, can cause the composition of the stored fluid to be quite varied. In particular, CH<sub>4</sub> is a likely impurity in the CO<sub>2</sub> capturing process from natural gas sweetening, and is present in significant quantities in some reservoirs (reservoirs exhausted of coal and natural gas); CO is a likely impurity in processes from heavy oil production and upgrading, and both are expected impurities from power plants using pre-combustion capture. Additionally, there is a significant legislative gap regarding the range of compositions allowed in anthropogenic CO<sub>2</sub>. As a consequence, the experimental study and thermodynamic modelling of these systems have become important: we must understand how the composition of these systems affect their behaviour and make technology profitable while ensuring maximum safety.

Knoope et al., 2013 recognize a significant knowledge gap in the calculation of the economic costs of the process since none of the models used take into account the impact of impurities on the various design parameters. Moreover, the shortage of experimental data, especially of volumetric properties under conditions relevant to CCS technology, means that there is not a preferred thermodynamic model to predict the behaviour of the fluid to be transported and stored (Li et al., 2011a,b; Sánchez-Vicente et al., 2013). The most common models are based on the use of Equations of State of different nature: cubic (Peng–Robinson, Patel–Teja, etc.), those derived from statistical mechanics (SAFT versions, CPA, etc.) or multiparameter approaches (GERG). However, all of them should be validated with experimental data of mixtures, under conditions at which transportation and storage of anthropogenic CO<sub>2</sub> take place: compositions rich in carbon dioxide,  $x_{\text{CO}_2} > 0.85$ , and pressure and temperature values corresponding to the critical region.

It is also important to know the nature of the interactions between CO<sub>2</sub> molecules and those of compounds which may appear in the capture and storage processes, since they may alter the selectivity in the capturing process or induce additional phenomena during storage. This study can be performed from ab initio calculations (Liu and Wilcox, 2013), molecular dynamics (Lachet et al., 2012) and statistical mechanics (Blanco et al., 2009).

In our current work we have studied the volumetric behaviour of mixtures of carbon dioxide with small amounts of methane or carbon monoxide, at compositions, temperatures and pressures of interest in CCS technology (ElementEnergy, 2010; Li et al., 2011a; ENCAP Project, 2008; EEA, 2012; EPA, 2012):  $x_{\text{CO}_2} \geq 0.97$ ,  $T = 304.21$

and 308.15 K, and  $P = 0.1–20$  MPa. The CO<sub>2</sub> + CH<sub>4</sub> and CO<sub>2</sub> + CO systems have been modelled using three different Equations of State: PR (Peng and Robinson, 1976), EoS widely used in engineering for their acceptable results despite the simplicity in implementation; PC-SAFT (Gross and Sadowski, 2001, 2002), EoS nowadays used in various applications including the study of supercritical fluids; and GERG-2008 (Kunz and Wagner, 2012), EoS developed for mixtures containing natural gas components. The three EoS have been validated for these systems under the aforesaid conditions. We have performed a theoretical study of the interactions that occur between the molecules involved in these mixtures near the critical point of the solvent, showing the affinity of the solvent molecules, CO<sub>2</sub>, for the solute, CH<sub>4</sub> or CO. The study has been conducted using the Krichevskii function concept (Levelt Sengers, 1994; Japas et al., 1998) and the Kirkwood–Buff Theory (Kirkwood and Buff, 1951). Finally, we have calculated the effect of CH<sub>4</sub> and CO as impurities on various operating transport parameters in CCS technology, by comparing the physicochemical properties of the mixtures with those of pure CO<sub>2</sub>. This aspect has not been well studied in the literature. To this end, we have used equations which have been reviewed and widely accepted for modelling by the industrial and engineering community (ElementEnergy, 2010).

## 2. Materials and methods

### 2.1. Chemicals

Carbon dioxide (mole fraction > 99.998%), methane (mole fraction > 99.995%) and carbon monoxide (mole fraction > 99.997%) were obtained from Air Liquide and used without further purification.

### 2.2. Apparatus

Density measurements were carried out using an experimental setup described in a previous work (Velasco et al., 2011). The apparatus was designed and built by ARMINES and the Laboratoire de Thermodynamique des Equilibres entre Phases de l'École Nationale Supérieure des Mines de Paris (France) for fast, reliable and accurate generation of  $P\rho T$  data for pure compounds and mixtures over the whole state surface of a fluid encompassing the liquid and vapour compressed phases, and the saturation curve in the (253 to 423) K  $\pm$  0.006 K temperature range, up 70 MPa pressure with a precision of 0.025% FS.

The main component of the system is a vibrating tube densimeter Anton Paar DMA HPM which includes the measuring cell and an interface module. Increases or decreases in pressure inside the cell are obtained through mass transfers with respect to the measurement circuit. Connecting the unit to a mPDS 2000V3 evaluation unit allows quasi-continuous data acquisition. A schematic diagram is shown in Fig. S1 (Supporting Information).

### 2.3. Experimental procedure

A variable-volume cell is used for loading mixtures into the measurement circuit. Successive introduction of compounds allows the preparation of mixtures of accurately determined composition due to successive weighing of the cell on a mass comparator from Sartorius, model CCE 2004, with maximum masses of 2500 g and typical repeatability better than 0.0001 g. The components are introduced in order of increasing volatility and the mixture formed is homogenized through efficient stirring and kept at pressures higher than its bubble point pressure.

The fluid is transmitted from the loading cell to the measurement circuit through a manual pump, which makes it possible to achieve pressures up to 70 MPa inside the measurement circuit (in

this work, the maximum operating pressure was 20 MPa). When the fluid to be studied exhibits phase transition within the operating range of temperature and pressure, the density measurement is performed in two stages: (i) ascending from atmospheric pressure to the pressure corresponding to phase transition; and (ii) descending from the maximum operating pressure down to the pressure of the phase transition. However, when the fluid exhibits no phase transition, as is the case in this work, the measurement is only carried out with descending pressure.

Since we must ensure a quasi-static equilibrium, the pressure changes have been kept sufficiently low; they are usually below  $0.005 \text{ MPa s}^{-1}$ . Thus, each isotherm in the range of 0.1–20 MPa consists of about 4000 density–pressure points, which are evenly reduced to about 1000 points for easier handling in subsequent calculations. This large number of points makes quasi-continuous isotherms available along subcritical, critical and supercritical regions, and allows the accurate determination of density derivative properties.

#### 2.4. Calibration and uncertainty

The general principle of the vibrating tube densimeter is based on the application of the relation between the vibrating period of a one-dimensional resonator and its vibrating mass. This system has a transversal stiffness,  $K=K(T, P)$ , and is vibrating with a period,  $\tau$ , in an undamped harmonic way under the effect of a mechanical excitation. Considering the vibration period,  $\tau$ , as a pseudo state variable, the  $P\tau T$  variables can describe the  $P\rho T$  state surface as long as a calibration may provide a direct relation between  $\tau$  and  $\rho$  (Appendix A, Eqs. (A1) and (A2)). In this work, forced path mechanical calibration model, FPMC (Bouchot and Richon, 2001), has been used. This model includes realistic mechanical considerations and forces representing the stress and strain behaviour of the tube material.

In order to evaluate the precision in density results,  $\rho = \rho(\rho_{\text{ref}}, \tau, P, T)$ , uncertainty propagation law has been used (Appendix A, Eq. (A3)). The reference fluid to calibrate was pure  $\text{CO}_2$  and the estimated uncertainty in  $P$  and  $T$  were  $u(P) = \pm 0.008 \text{ MPa}$  and  $u(T) = \pm 0.006 \text{ K}$  (Velasco et al., 2011). From those and  $u(\rho_{\text{ref}}) = 0.03\%$  (Span and Wagner, 1996) and  $u(\tau) = \pm 2 \times 10^{-5} \text{ ms}$  (Bouchot and Richon, 2001), the expanded ( $k=2$ ) uncertainty in the density has been calculated for our mixtures:  $u(\rho) = 0.4\text{--}0.7 \text{ kg/m}^3$ . On the other hand, the repeatability of the density measurements for mixtures, expressed as relative mean standard deviation (Appendix A, Eqs. (A4)–(A6)), is  $\bar{S}_\rho^r = 0.13\%$  (Velasco et al., 2011).

### 3. Results

#### 3.1. Experimental density

$P$ – $\rho$ – $T$ – $x_{\text{CO}_2}$  measurements for  $\{\text{CO}_2 + \text{CH}_4\}$  ( $x_{\text{CO}_2} = 0.9719, 0.9809, 0.9902, 0.9932, 0.9961$ ) at  $T = 304.21 \text{ K}$  (critical temperature of pure  $\text{CO}_2$ , Gil et al., 2008) and  $\{\text{CO}_2 + \text{CO}\}$  ( $x_{\text{CO}_2} = 0.9700, 0.9810, 0.9902, 0.9930, 0.9960$ ) at  $T = 304.21$  and  $308.15 \text{ K}$  were carried out in the pressure range from 0.1 to 20 MPa.

Experimental results are shown in Fig. 1 for the  $\text{CO}_2 + \text{CH}_4$  system and Fig. 2 ( $T = 304.21 \text{ K}$ ) and 3 ( $T = 308.15 \text{ K}$ ) for  $\text{CO}_2 + \text{CO}$  mixtures. Full numerical data are included in Tables S1–S3 in the Supporting Information. As shown in Figs. 1–3, at the studied temperatures the densities of all mixtures change continuously with pressure, and an inflection point appears in the isotherms; that is, the systems are at a supercritical temperature for any composition, a fact which is consistent with literature data on critical locus of these systems (Donnelly and Katz, 1954; Bian et al., 1993; Ke et al., 2001): the critical temperatures of all mixtures under study

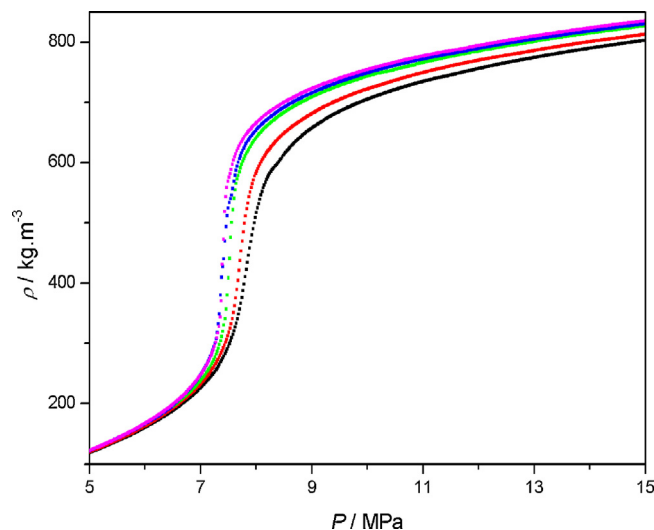


Fig. 1. Experimental densities,  $\rho$ , for  $\text{CO}_2 + \text{CH}_4$  mixtures at  $T = T_c(\text{CO}_2) = 304.21 \text{ K}$  and several pressures.

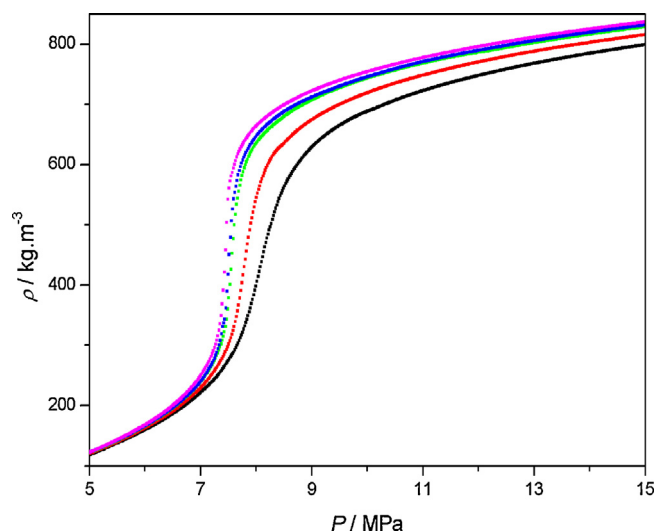


Fig. 2. Experimental densities,  $\rho$ , for  $\text{CO}_2 + \text{CO}$  mixtures at  $T = T_c(\text{CO}_2) = 304.21 \text{ K}$  and several pressures.

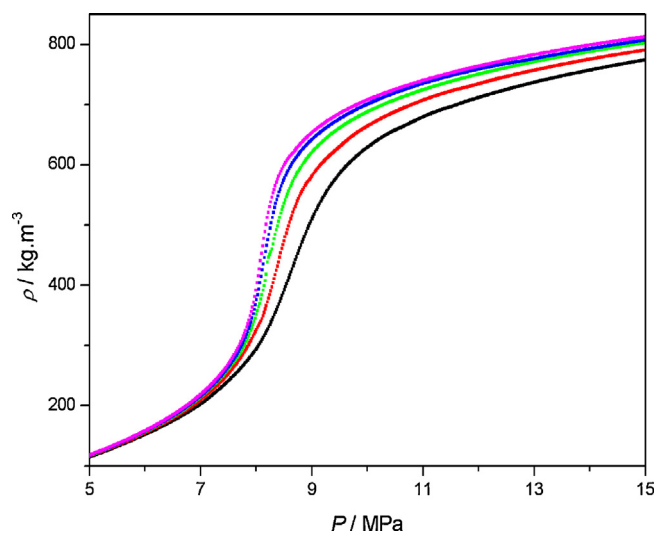


Fig. 3. Experimental densities,  $\rho$ , for  $\text{CO}_2 + \text{CO}$  mixtures at  $T = 308.15 \text{ K}$  and several pressures.

range from 302.6 K to 303.9 K. At the same temperature (304.21 K) the influence of the presence of CO on the density of the mixtures is higher than that of CH<sub>4</sub>. For a given system (CO<sub>2</sub> + CO or CO<sub>2</sub> + CH<sub>4</sub>), the influence of the presence of solute on the density of the mixtures is higher at 304.21 K ( $T_c$  of pure CO<sub>2</sub>) than at 308.15 K (for CO<sub>2</sub> + CH<sub>4</sub> at 308.15, see Blanco et al., 2012).

Table 1 lists literature references for the volumetric properties of the two systems as well as the  $T$ – $P$ – $x_{\text{CO}_2}$  ranges of each study. As can be seen, the system CO<sub>2</sub> + CH<sub>4</sub> has been widely studied, however there are only eight studies in which the values of temperature, pressure and composition are of interest in CCS technology, and solely the data published by Zhang et al. (2002) and Blanco et al. (2012) analyzed the region of infinite dilution, IDS, the region that has been studied in our current work. Our experimental data are consistent with those but not directly comparable since temperature do not match. We have carried out a comparison between the experimental density data from Blanco et al. (2012), used further in this study, for the mixture of composition  $x_{\text{CO}_2} = 0.9961$  and those published by Zhang et al. (2002) for the mixture  $x_{\text{CO}_2} = 0.997$ , both at  $T = 308.15$  K, obtaining a mean relative deviation (Appendix A, Eq. (A7)):  $\text{MRD}_\rho = 2.2\%$

For the CO<sub>2</sub> + CO system the extent of literature data is rather small. Mallu et al. (1987) and Cipollina et al. (2007) have studied its volumetric behaviour, and our experimental data are consistent with those but not directly comparable, since the compositions do not match.

### 3.2. Isothermal compressibility

From the  $P$ – $\rho$ – $T$ – $x_{\text{CO}_2}$  experimental values of the mixtures studied, we have evaluated the effect of pressure on density at the critical temperature of pure solvent,  $T = 304.21$  K, by means of the isothermal compressibility,  $\kappa_T$ , defined as:

$$\kappa_T = \left(\frac{1}{\rho}\right) \left(\frac{\partial \rho}{\partial P}\right)_T \quad (1)$$

Figs. 4 and 5 show the  $\kappa_T$ – $x_{\text{CO}_2}$ – $P$  representations for CO<sub>2</sub> + CH<sub>4</sub> and CO<sub>2</sub> + CO mixtures, respectively. It can be seen that the dependence of the isothermal compressibility on pressure and composition is similar for both systems: (i)  $\kappa_T$  varies with pressure, going through a maximum; (ii) the maximum value of  $\kappa_T$

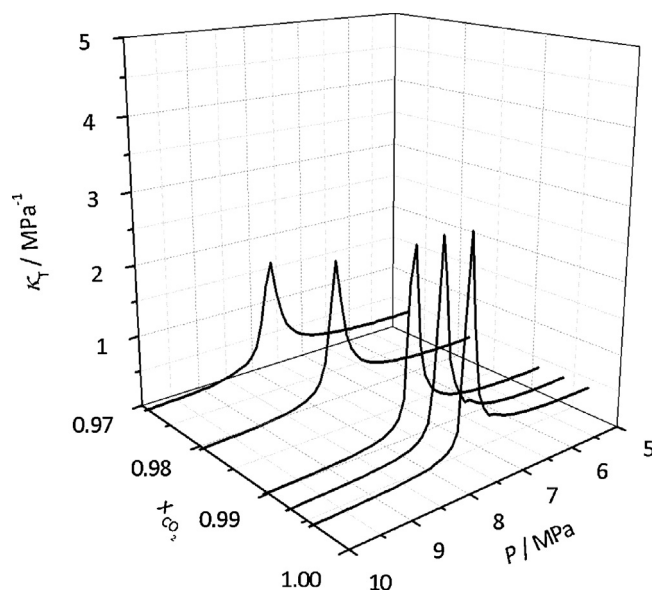


Fig. 4. The  $\kappa_T$ – $x_{\text{CO}_2}$ – $P$  representations for CO<sub>2</sub> + CH<sub>4</sub> mixtures at  $T = T_c(\text{CO}_2) = 304.21$  K.

increases as the composition of CO<sub>2</sub> goes up, since the critical temperature of the increasingly CO<sub>2</sub> rich mixture approaches the critical temperature of CO<sub>2</sub>; and (iii) the pressure at which the maximum in  $\kappa_T$  occurs decreases as the composition of CO<sub>2</sub> rises, since the critical pressures,  $P_c$ , of both systems decrease when  $x_{\text{CO}_2}$  increases (Donnelly and Katz, 1954; Bian et al., 1993; Ke et al., 2001). Moreover, when comparing the mixture compressibility for the two systems with the same concentration, we observe that if  $x_{\text{CO}_2} < 0.99$ , the maximum value for the isothermal compressibility of the CO<sub>2</sub> + CH<sub>4</sub> system is higher than that for CO<sub>2</sub> + CO and when  $x_{\text{CO}_2} > 0.99$ , this trend is reversed.

### 3.3. Excess molar volume and solute partial molar volume

From experimental data obtained in this work and literature experimental values for the CO<sub>2</sub> + CH<sub>4</sub> system at 308.15 K (Blanco

**Table 1**  
Summary of  $T$ – $P$ – $x_{\text{CO}_2}$  ranges of mixtures studied in this work.

System	No. points	Range $T$ (K)	Range $P$ (MPa)	Range $x_{\text{CO}_2}$	Reference
CO <sub>2</sub> + CH <sub>4</sub>	476	311–478	1.4–68.9	0.15–0.80	Reamer et al. (1944)
	28	293–453	4.1–19.3	0.20–0.80	Beer (1969)
	186	253–288	2.4–14.5	0.45–0.96	Arai et al. (1971)
	63	283–322	4.7–20.7	0.91	Simon et al. (1977)
	118	220–320	0.1–48.3	0.48	Esper (1987)
	91	225–400	2.1–35.8	0.98	Magée and Ely (1988)
	155	300–320	0.2–9.8	0.10–0.90	Brugge et al. (1989)
	28	289	0.03–6.7	0.1	Lemming (1989)
	64	323–398	0.1–6.5	0.482	Mallu and Viswanath (1990)
	298	270–350	0.2–28.4	0.31	Jaeschke and Humphreys (1991)
	149	279–308	3.7–6.4	0.10–0.48	Jaeschke et al. (1997)
	44	673	19.9–99.9	0.10–0.90	Seitz and Blencoe (1996)
	194	323–573	9.9–99.9	0.10–0.90	Seitz et al. (1996)
	228	225–350	1.8–69.5	0.10–0.90	Hwang et al. (1997)
	17	273–290	2.0–9.5	0.06–0.15	Glos et al. (2001)
	22	308	5.4–12.1	0.997	Zhang et al. (2002)
	324	233–373	0.2–20.7	0.08–0.15	Wöll and El Hawary (2003)
	315	250–400	1–20	0.20–0.60	Móndejar et al. (2012)
	49,000	253–333	0.1–20	0.85–0.996	Blanco et al. (2012)
	5000	304	0.1–20	0.97–0.996	This work
CO <sub>2</sub> + CO	75	323–423	0.1–6.5	0.57	Mallu et al. (1987)
	56	308–343	26.0–47.0	0.86–0.93	Cipollina et al. (2007)
	10,000	304–308	0.1–20	0.97–0.996	This work

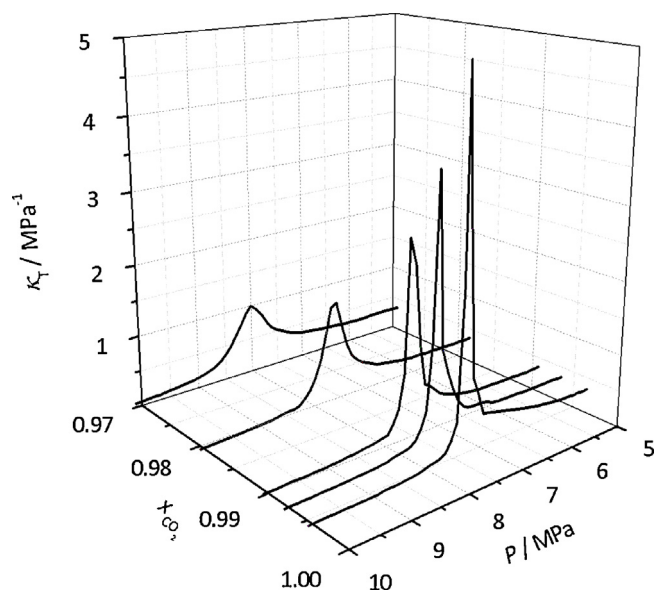


Fig. 5. The  $\kappa_T$ - $x_{\text{CO}_2}$ - $P$  representations for  $\text{CO}_2$ + $\text{CO}$  mixtures at  $T = T_c(\text{CO}_2) = 304.21$  K.

et al., 2012), we have calculated the excess molar volume of the mixture,  $V_m^E$ , using the following expression:

$$V_m^E = V_m - V_1 - V_2 = \frac{x_1 M_1 + x_2 M_2}{\rho_m} - \frac{x_1 M_1}{\rho_1} - \frac{x_2 M_2}{\rho_2} \quad (2)$$

where the subscripts 1, 2 and  $m$  refer to solvent ( $\text{CO}_2$ ), solute ( $\text{CH}_4$  or  $\text{CO}$ ), and mixture, respectively;  $M_i$  is the molar mass of each component  $i$  in the mixture, and  $V_i$ ,  $V_m$ ,  $\rho_i$  and  $\rho_m$  are the molar volume and the density for the pure compounds and the mixture at temperature  $T$  and pressure  $P$ .

Due to the small values of the densities of these mixtures at low pressures, we have calculated the expanded ( $k=2$ ) uncertainties in the excess molar volumes in the 5–20 MPa range. The rules of propagation of errors (Appendix A, Eq. (A3)) have been used, obtaining the values  $U(V_m^E)$  0.1–1  $\text{cm}^3 \cdot \text{mol}^{-1}$ .

Fig. 6 shows the trends in the excess molar volumes,  $V_m^E$ , with pressure and composition for two mixtures,  $x_{\text{CO}_2} \cong 0.971$  and  $x_{\text{CO}_2} \cong 0.993$ , of both systems at the two operating temperatures.

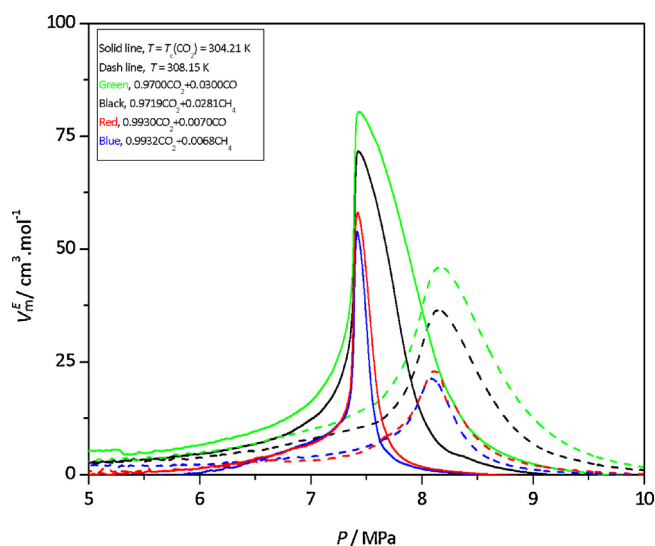


Fig. 6. The  $V_m^E$ - $P$  representation for studied systems at  $T = T_c(\text{CO}_2) = 304.21$  K and  $T = 308.15$  K,  $x_{\text{CO}_2} \cong 0.971$  and  $x_{\text{CO}_2} \cong 0.993$  mole fractions.

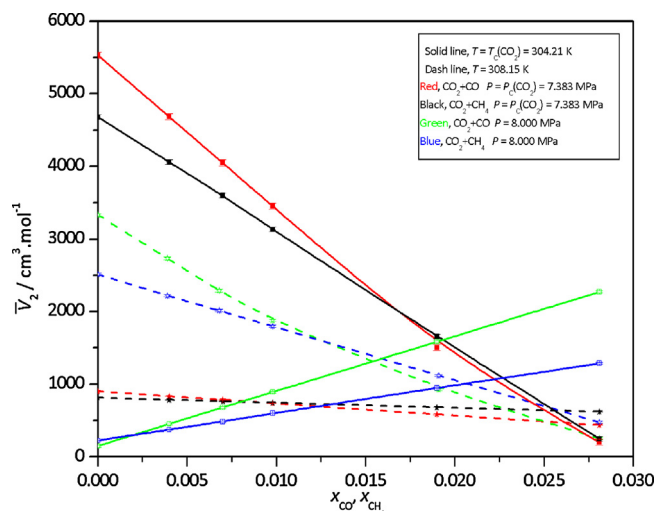


Fig. 7. Solute partial molar volume,  $\bar{V}_2$ , versus solute mole fraction,  $x_{\text{CH}_4}$ ,  $x_{\text{CO}}$ , for studied systems at  $P = 7.383$  and  $8.000$  MPa and at  $T = 304.21$  and  $T = 308.15$  K.

They are supercritical mixtures and we observe a peak in the excess molar volume:  $P \cong 7.41$  MPa at  $T = 304.21$  K and  $P \cong 8.15$  MPa at  $T = 308.15$  K. The value of the maximum for  $V_m^E$  decreases with increasing temperature and molar fraction of  $\text{CO}_2$ . Finally, the maxima in  $V_m^E$  for  $\text{CO}_2$ + $\text{CO}$  mixtures are higher than for mixtures  $\text{CO}_2$ + $\text{CH}_4$ , which means that the inclusion of a molecule of  $\text{CO}$  in pure  $\text{CO}_2$  disturbs the system to a further extent than when introducing a molecule of  $\text{CH}_4$ . This may be due to either the dipolar moments ( $\mu_{\text{CO}_2} = \mu_{\text{CH}_4} = 0$ ;  $\mu_{\text{CO}} = 0.122$  D), the sizes of the components of each system (the size difference between the molecules of  $\text{CO}_2$  and  $\text{CH}_4$  is smaller than that between  $\text{CO}_2$  and  $\text{CO}$ ), or both.

From the density data, the partial molar volume of the solute,  $\bar{V}_2$ , has been calculated for the five studied compositions of each system at temperatures of 304.21 and 308.15 K and selected pressures of 7.383 MPa (critical pressure of pure  $\text{CO}_2$ ) and 8.000 MPa (supercritical pressure). To this end we have used the following expression:

$$\bar{V}_2 = V_m + (1 - x_2) \left( \frac{\partial V_m}{\partial x_2} \right)_{P,T} \quad (3)$$

where the subscripts 2 and  $m$  refer to solute ( $\text{CH}_4$  or  $\text{CO}$ ) and mixture respectively, and  $V_m$  is the molar volume of the mixture at temperature  $T$  and pressure  $P$ .  $(\partial V_m / \partial x_2)_{P,T}$  values have been calculated from polynomial fittings of  $V_m$  vs.  $x_2$ ,  $V_m$  being the first term on the right hand side of Eq. (2).

The expanded ( $k=2$ ) uncertainty in  $\bar{V}_2$  have been calculated using the rules of propagation of errors (Appendix A, Eq. (A3)). The values are  $U(\bar{V}_2) = 3$ – $85$   $\text{cm}^3 \cdot \text{mol}^{-1}$ .

Fig. 7 shows trends in the partial molar volumes of the solute,  $\bar{V}_2$ , with solute concentration at the pressures and temperatures indicated above. A similar behaviour is observed for the two systems under study: at  $P = P_c(\text{CO}_2) = 7.383$  MPa,  $\bar{V}_2$  decreases with increasing solute concentration at both working temperatures, with a much smaller slope at 308.15 K. By contrast, at the supercritical pressure,  $P = 8.000$  MPa,  $\bar{V}_2$  increases with increasing solute concentration at  $T = 304.21$  K, and decreases at  $T = 308.15$  K.

We have compared (Fig. S2, Supporting Information) the values of  $\bar{V}_2$  calculated in this work for the  $\{0.9961\text{CO}_2 + 0.0039\text{CH}_4\}$  mixture with those calculated by Zhang et al. (2002) for the  $\{0.997\text{CO}_2 + 0.003\text{CH}_4\}$  mixture at 308.15 K, observing good agreement, especially in the dense region. The mean relative deviation, calculated with Eq. (A7) (Appendix A), at the point corresponding to the maximum value of  $\bar{V}_2$  is  $\text{MRD}_{\bar{V}_2} < 6\%$ .



**Table 2**  
Parameters used for modelling the systems studied in this work with PR and PC-SAFT EoS.

Pure compound parameter	CO <sub>2</sub>	CH <sub>4</sub>	CO
$T_c$ (K)	304.21 <sup>a</sup>	190.56 <sup>b</sup>	132.86 <sup>b</sup>
$P_c$ (MPa)	7.383 <sup>a</sup>	4.599 <sup>b</sup>	3.494 <sup>b</sup>
$\omega$	0.224 <sup>b</sup>	0.011 <sup>b</sup>	0.066 <sup>b</sup>
$m$	2.0730 <sup>c</sup> /2.1276 <sup>d</sup>	1.0000 <sup>c</sup> /1.0039 <sup>e</sup>	1.3097 <sup>c</sup> /1.3063 <sup>e</sup>
$\sigma$ (Å)	2.7852 <sup>c</sup> /2.8251 <sup>d</sup>	3.7039 <sup>c</sup> /3.7126 <sup>e</sup>	3.2507 <sup>c</sup> /3.2565 <sup>e</sup>
$\varepsilon$ (K)	169.21 <sup>c</sup> /163.76 <sup>d</sup>	150.03 <sup>c</sup> /149.11 <sup>e</sup>	92.15 <sup>c</sup> /91.48 <sup>e</sup>
$\Delta v_c$ (10 <sup>-3</sup> m <sup>3</sup> /kg)	0.02 <sup>f</sup> /0.17 <sup>d</sup>	–	–0.1 <sup>f</sup> /–0.1 <sup>e</sup>
Used in PR and PC-SAFT EoS: $T_c$ , critical temperature; $P_c$ , critical pressure; $\omega$ , acentric factor.			
Used in PC-SAFT EoS: $m$ , segment number; $\sigma$ , segment diameter; $\varepsilon$ , segment energy parameter; $\Delta v_c$ , volume shift.			
Binary interaction parameter, $k_{ij}$		CO <sub>2</sub> + CH <sub>4</sub>	CO <sub>2</sub> + CO
Peng–Robinson EoS		0.12 <sup>b</sup>	–0.15 <sup>g</sup>
PC-SAFT EoS		0.07 <sup>f</sup> /0.05 <sup>e</sup>	0.12 <sup>f</sup> /0 <sup>e</sup>

<sup>a</sup> Gil et al. (2008).<sup>b</sup> Laursen (2012).<sup>c</sup> PC-SAFT original model; Gross and Sadowski (2001).<sup>d</sup> PC-SAFT rescaled model; Blanco et al. (2009).<sup>e</sup> PC-SAFT rescaled model; this work.<sup>f</sup> PC-SAFT original model; this work.<sup>g</sup> Ke et al. (2001).

The strong dependence of  $V_m^E$  on pressure and composition (Fig. 6) demonstrates the non-ideality of the studied systems. However, the greater values of  $V_m^E$  and  $(\partial V_2/\partial x_2)$  exhibited by the CO<sub>2</sub> + CO system suggest that this system deviates from ideality further than CO<sub>2</sub> + CH<sub>4</sub>

#### 4. Modelling

Due to the variety of compositions that the transported and later stored fluid can present, as well as the pressure and temperature operational ranges within CCS technology, it is interesting to develop effective working tools which will allow to correctly predict the phase and volumetric behaviour of the fluid. To do this, our experimental  $P$ – $\rho$ – $T$  results have been compared, in terms of relative mean deviation,  $\text{MRD}_X$  (Appendix A, Eq. (A7)), with those

calculated using three different types of Equations of State, validating them for these experimental conditions.

**Peng–Robinson EOS** (Peng and Robinson, 1976). The cubic equations are the simplest EoS which predict the existence of a critical point and quantitative representation of VLE. Their simple structure, which requires little input information, make them popular for engineering applications.

The parameters used for the pure components, as well as the binary interaction parameter,  $k_{ij}$ , included in the mixing rule of a van der Waals fluid, are shown in Table 2. A comparison between our experimental data and those calculated with the PR EoS are shown in Table 3. Despite its simplicity, the agreement with experimental data is good at pressures below the critical pressure,  $\text{MRD}_\rho = 1.8\%$  for both systems, and acceptable at higher pressures:  $\text{MRD}_\rho(\text{CO}_2 + \text{CH}_4) = 4.4\%$  and  $\text{MRD}_\rho(\text{CO}_2 + \text{CO}) = 4.1\%$ .

**PC-SAFT EoS** (Gross and Sadowski, 2001, 2002). In this model, based on Wertheim's first order thermodynamic perturbation theory, the reference fluid is the hard-chain fluid. Attractive intermolecular forces are further separated into different contributions, so that the Helmholtz energy,  $a$ , is written as the sum of the ideal-gas contribution,  $a^{id}$ , a hard-chain term,  $a^{hc}$ , a contribution for the dispersive attraction,  $a^{dis}$ , and several terms for associating, dipolar and quadrupolar interactions. In this work, we have not taken into account the polar and association contributions, therefore the terms contributing to the Helmholtz energy are as follows:

$$a = a^{id} + a^{hc} + a^{dis} \quad (4)$$

For the non-polar pure compounds, three parameters are needed: the segment number,  $m$ , the segment diameter,  $\sigma$ , and the segment energy parameter,  $\varepsilon$ . These parameters provide an accurate representation for both volumetric and VLE properties if they are obtained from vapour pressures and liquid densities; however, they always overestimate the critical properties. In order to describe the critical region, different authors (Cismondi et al., 2005; Blanco et al., 2009; Gil et al., 2010, 2012) perform a rescaling of pure-compound parameters using their  $T_c$  and  $P_c$ . In this work we have applied PC-SAFT EoS to our systems with both options, using pure compounds parameters ( $m, \sigma, \varepsilon$ ) original and rescaled. Moreover, in both cases, we have adjusted the experimental density values of pure CO<sub>2</sub> and CO using volume shift,  $\Delta v_c$ .

The parameters used for the pure components, the mixing parameters and a comparison between our experimental data

**Table 3**  
Comparison between the experimental  $P$ – $\rho$ – $T$ – $x_{\text{CO}_2}$  data for the systems studied in this work and those calculated using PR, PC-SAFT and GERG EoS.

CO <sub>2</sub> + CH <sub>4</sub>	$\text{MRD}_\rho$ (%) $T = 304.21$ K			$\text{MRD}_\rho$ (%) $T = 308.15$ K		
	PR	PC-SAFT	GERG	PR	PC-SAFT	GERG
$x_{\text{CO}_2} = 0.9719$	3.4	1.4 <sup>b</sup> /2.6 <sup>c</sup>	0.5	3.4	1.4 <sup>b</sup> /2.6 <sup>c</sup>	0.4
$x_{\text{CO}_2} = 0.9809$	3.2	1.8 <sup>b</sup> /2.7 <sup>c</sup>	0.2	3.6	1.7 <sup>b</sup> /2.9 <sup>c</sup>	0.4
$x_{\text{CO}_2} = 0.9902$	3.4	1.7 <sup>b</sup> /2.8 <sup>c</sup>	0.4	3.6	2.0 <sup>b</sup> /3.0 <sup>c</sup>	0.3
$x_{\text{CO}_2} = 0.9932$	3.4	1.9 <sup>b</sup> /2.8 <sup>c</sup>	0.5	3.8	1.7 <sup>b</sup> /3.0 <sup>c</sup>	0.4
$x_{\text{CO}_2} = 0.9961$	3.4	1.8 <sup>b</sup> /2.8 <sup>c</sup>	0.3	3.8	1.7 <sup>b</sup> /2.8 <sup>c</sup>	0.4
$\text{MRD}_\rho$ (%)	3.4	1.7 <sup>b</sup> /2.7 <sup>c</sup>	0.4	3.7	1.7 <sup>b</sup> /2.9 <sup>c</sup>	0.4
CO <sub>2</sub> + CO	$\text{MRD}_\rho$ (%) $T = 304.21$ K			$\text{MRD}_\rho$ (%) $T = 308.15$ K		
	PR	PC-SAFT	GERG	PR	PC-SAFT	GERG
$x_{\text{CO}_2} = 0.9700$	2.8	1.5 <sup>b</sup> /2.6 <sup>c</sup>	1.8	3.1	1.3 <sup>b</sup> /2.4 <sup>c</sup>	1.5
$x_{\text{CO}_2} = 0.9810$	3.1	1.4 <sup>b</sup> /2.7 <sup>c</sup>	1.4	3.4	1.2 <sup>b</sup> /2.6 <sup>c</sup>	1.6
$x_{\text{CO}_2} = 0.9902$	3.4	1.4 <sup>b</sup> /2.8 <sup>c</sup>	1.1	3.4	1.4 <sup>b</sup> /2.7 <sup>c</sup>	0.7
$x_{\text{CO}_2} = 0.9930$	3.2	1.6 <sup>b</sup> /2.7 <sup>c</sup>	0.7	3.7	1.4 <sup>b</sup> /2.9 <sup>c</sup>	0.8
$x_{\text{CO}_2} = 0.9960$	3.4	1.7 <sup>b</sup> /2.7 <sup>c</sup>	0.8	3.6	1.5 <sup>b</sup> /2.8 <sup>c</sup>	0.7
$\text{MRD}_\rho$ (%)	3.2	1.5 <sup>b</sup> /2.7 <sup>c</sup>	1.1	3.4	1.4 <sup>b</sup> /2.7 <sup>c</sup>	1.1

<sup>a</sup> Experimental data from Blanco et al. (2012).<sup>b</sup> PC-SAFT original model.<sup>c</sup> PC-SAFT rescaled model.

and calculated values are found in Tables 2 and 3 respectively. When the original parameters for the pure compounds are used (Gross and Sadowski, 2001, 2002), the model predicts in the vicinity of the critical pressure,  $P_c$ , an erroneous subcritical state for many of our mixtures when in reality those are at supercritical conditions. Mean relative deviations in this region ( $P=7\text{--}9\text{ MPa}$ ) are  $\text{MRD}_\rho(\text{CO}_2 + \text{CH}_4) = 12.8\%$  and  $\text{MRD}_\rho(\text{CO}_2 + \text{CO}) = 8.1\%$ . However, the agreement outside the critical region is much better:  $\text{MRD}_\rho(\text{CO}_2 + \text{CH}_4) = 0.5\%$  and  $\text{MRD}_\rho(\text{CO}_2 + \text{CO}) = 0.8\%$ . On the other hand, if the parameters used are rescaled using the critical points of the pure compounds, the model predicts supercritical state for all mixtures and represents the critical region more accurately, with  $\text{MRD}_\rho(\text{CO}_2 + \text{CH}_4) = 5.7\%$  and  $\text{MRD}_\rho(\text{CO}_2 + \text{CO}) = 5.6\%$ , although the deviation for the remaining pressures is higher:  $\text{MRD}_\rho(\text{CO}_2 + \text{CH}_4) = 2.5\%$  and  $\text{MRD}_\rho(\text{CO}_2 + \text{CO}) = 2.4\%$ .

GERG EoS (Kunz and Wagner, 2012). International reference equation of state for natural gases based on a multi-fluid approximation. This approximation divides the Helmholtz energy formula into three terms: one term to account for ideal gas behaviour, a second term describing the contributions of pure substances and a third term for the departure function. This equation covers subcritical, critical and supercritical regions as well as liquid–vapour phase boundaries but its accuracy decreases when the GERG database contains few experimental data of the studied system. It should

also be noted that the uncertainty increases in both density and VLE calculations of  $\text{CO}_2$ -rich mixtures (Li et al., 2011a).

As can be seen from Table 3, a comparison between our experimental data and those calculated with the GERG EoS is very good for both systems; the deviation for  $\text{CO}_2 + \text{CH}_4$  is smaller, since the EoS developed for this system uses a larger number of experimental data, covering a wider range of pressures. However, for  $\text{CO}_2 + \text{CO}$ , the EoS GERG database only contains VLE data in the pressure range from 0.1 to 6 MPa. The deviations obtained are:  $\text{MRD}_\rho(\text{CO}_2 + \text{CH}_4) = 0.4\%$  and  $\text{MRD}_\rho(\text{CO}_2 + \text{CO}) = 1.0\%$ .

GERG EOS is the equation that best represents our experimental results, although its extension to mixtures with compounds not included in their database is complex. By contrast, PC-SAFT EoS offers slightly higher deviations than GERG, but its use can be extended easily to multicomponent mixtures. Finally, PR EoS may be adequate, depending on the working pressure and the accuracy required.

Fig. 8a and b depicts the relative deviations between the experimental densities and the values calculated using PR, PC-SAFT and GERG EoS for selected mixtures studied in this work (different solute, composition and temperature). Deviations are similar at both temperatures for pressure values removed from the critical, while in the near-critical zone the nearer the temperature (to the critical value) the higher the deviations.

## 5. Discussion

### 5.1. Study of the interaction $\text{CO}_2$ – impurity

The efficiency and selectivity of the capture processes are influenced by the type of interactions between the molecules present, that is, by their affinity. Moreover, once the fluid is stored,  $\text{CO}_2$  molecules can interact with other molecules present in the reservoir, consequently modifying the behaviour of the plume (Blanco et al., 2012). In this section we determine the nature of the interactions between solvent molecules,  $\text{CO}_2$ , and those of the solute,  $\text{CH}_4$  or  $\text{CO}$ , through a volumetric study in the critical region of infinitely dilute solutions, IDS, for systems  $\{\text{CO}_2(1) + \text{CH}_4(2)\}$  or  $\{\text{CO}_2(1) + \text{CO}(2)\}$ . We use the Krichevskii function concept (Levelt Sengers, 1994; Japas et al., 1998) and the Kirkwood–Buff Theory (Kirkwood and Buff, 1951).

#### 5.1.1. Krichevskii function

The Krichevskii function,  $J$ , represents the pressure change that occurs in a system when a molecule of solvent is replaced by one of the solute at constant  $T$  and  $V$  in IDS. When the conditions of  $T$  and  $V$  correspond to critical conditions for the pure solvent, the Krichevskii function,  $J$ , becomes the Krichevskii parameter,  $A_{\text{Kr}}$ :

$$J = \left( \frac{\partial P}{\partial x_2} \right)_{T, V}^{\infty} \quad (5)$$

$$A_{\text{Kr}} = \left( \frac{\partial P}{\partial x_2} \right)_{T_c, V_c}^{C, \infty} \quad (6)$$

According to Eqs. (5) and (6), given a number of volumetric data at infinite dilution, the values for the Krichevskii function (including the parameter  $A_{\text{Kr}}$ ) can be calculated from the slopes of the isotherms–isochores  $P$ – $x_2$  when  $x_2 \rightarrow 0$ .

Fig. 9a and b shows some experimental results on the  $P$ – $x_{\text{CH}_4}$  and  $P$ – $x_{\text{CO}}$  planes at  $T = 304.21\text{ K}$  for mixtures studied along various isochores, including the critical. The slopes of the  $P$ – $x_2$  graphs increase in both systems with increasing density, being greater when  $\text{CO}$  is the solute. The slopes along the critical isothermal–isochoric, the Krichevskii parameter, for our systems are shown in Table 4. In the literature we have found some values for the  $A_{\text{Kr}}(\text{CO}_2 + \text{CH}_4)$  parameter; the mean relative deviations between our results and the

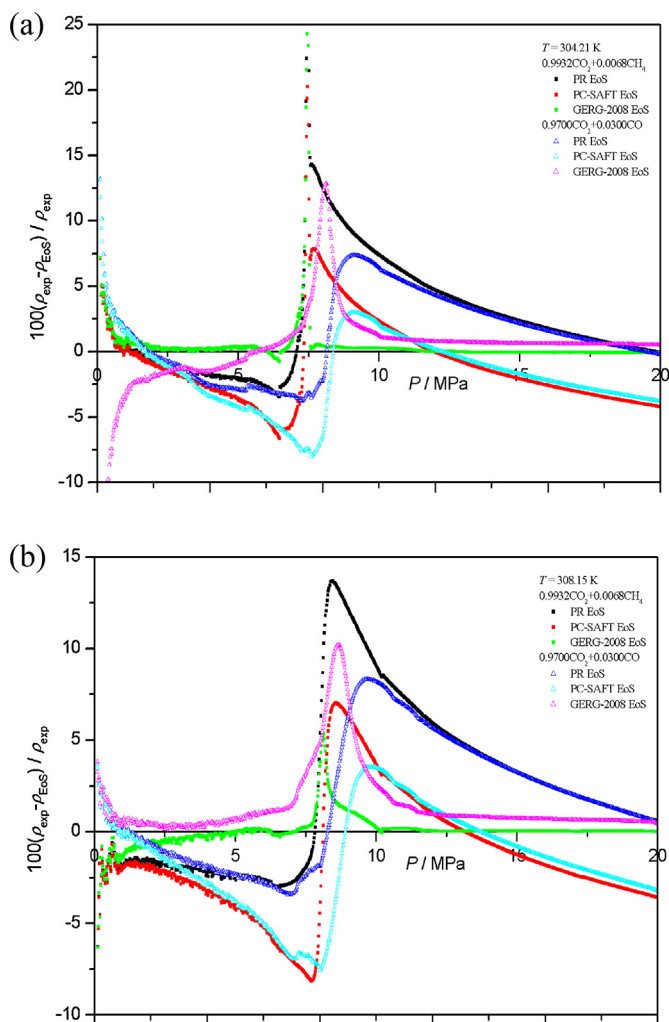


Fig. 8. Relative deviation between the experimental densities and the values calculated using different EoS for several mixtures studied in this work. (a)  $T = 304.21\text{ K}$ ; (b)  $T = 308.15\text{ K}$ .

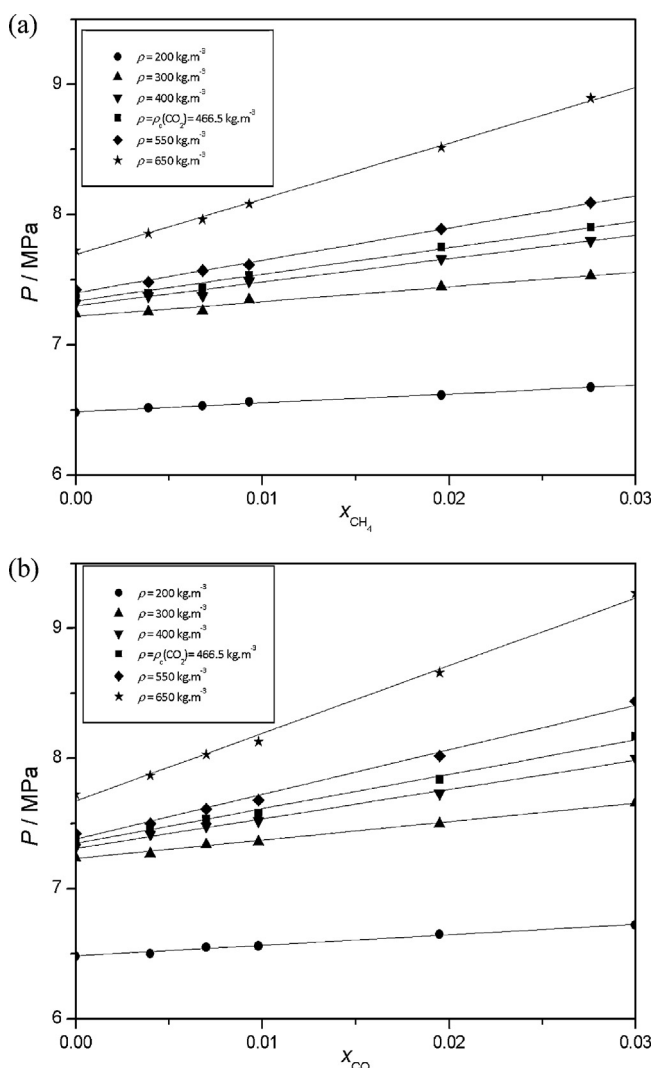
**Table 4**

Comparison between the values obtained for the CO<sub>2</sub>+CH<sub>4</sub> and CO<sub>2</sub>+CO systems for several structural parameters and properties: Krichevskii parameter,  $A_{Kr}$ ; reduced Krichevskii parameter,  $A_{Kr}^*$ ; maximum value of the partial molar volume of solute at infinite dilution at  $T=308.15$  K,  $(\bar{V}_2^\infty)_{max}$ ; minimum value of the excess solvent number at  $T=308.15$  K,  $(N_{exc}^\infty)_{min}$ ; cluster size at  $T=308.15$  K,  $(N_1^{exc})_{max}$ , and direct correlation function integrals,  $C_{ij}$  at  $\rho = \rho_c$  (CO<sub>2</sub>) and  $T=308.15$  K.

Parameter/property	T (K)	System	
		CO <sub>2</sub> + CH <sub>4</sub>	CO <sub>2</sub> + CO
$A_{Kr}$ (MPa)	304.21	20.383 ± 0.004	26.418 ± 0.005
$A_{Kr}^*$	304.21	0.76	0.98
$(\bar{V}_2^\infty)_{max}$ (cm <sup>3</sup> /mol)	308.15	3300	3950
$(N_{exc}^\infty)_{min}$	308.15	-33	-38
$(N_1^{exc})_{max}$	308.15	11	3
$10^{-3}(C_{12})_{\rho_c}$ (cm <sup>3</sup> /mol)	308.15	0.020	0.006
$10^{-3}(C_{11} - C_{12})_{\rho_c}$ (cm <sup>3</sup> /mol)	308.15	0.072	0.085

literature are:  $MRD_{A_{Kr}} = 1.6\%$  (Furuja and Teja, 2000) and  $MRD_{A_{Kr}} = 8.0\%$  (Abdulagatov et al., 2007).

The values of the  $P$ - $x_2$  slopes on the rest of isochores allow us to complete the study of the behaviour of IDS when expanding it to other states different to the critical point. Fig. 10 shows the evolution of the Krichevskii function,  $J$ , with the density of the pure solvent,  $\rho_{CO_2}$ , at  $T=304.21$  and  $308.15$  K for the two systems under study. As can be seen,  $J$  is positive over the entire range of densities and its values are slightly higher and less sensitive to temperature for CO<sub>2</sub>+CO than for the CO<sub>2</sub>+CH<sub>4</sub> system.



**Fig. 9.** (a)  $P$ - $x_{CH_4}$  data for {CO<sub>2</sub> (1)+CH<sub>4</sub> (2)} dilute mixtures and (b)  $P$ - $x_{CO}$  data for {CO<sub>2</sub> (1)+CO (2)} dilute mixtures, for several isochores at  $T=304.21$  K.

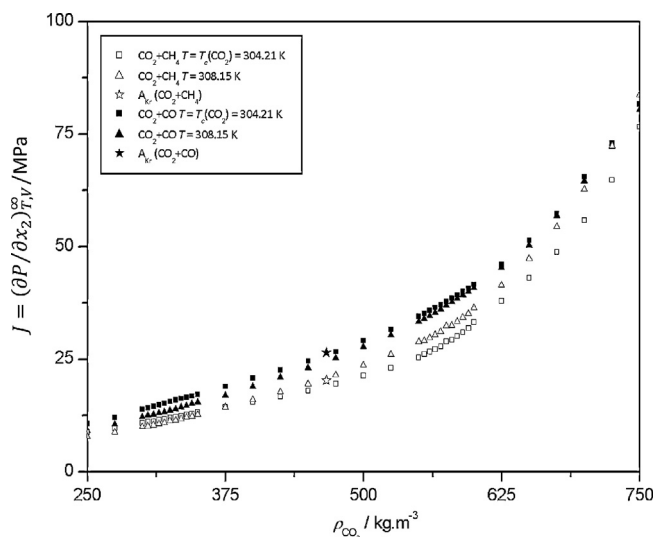
The partial molar volume of solute at infinite dilution,  $\bar{V}_2^\infty$ , can be expressed in terms of the Krichevskii function,  $J$  (Blanco et al., 2009):

$$\rho_1^0 \bar{V}_2^\infty = [1 + \kappa_T^0 J] \quad (7)$$

where the superscripts 0 and  $\infty$  denote pure component and infinite dilution, respectively, and  $\rho_1^0$  and  $\kappa_T^0$  are the density and the isothermal compressibility of the solvent.

In the vicinity of the critical point of the solvent,  $J \rightarrow A_{Kr}$  and the compressibility of the pure solvent,  $\kappa_T^0$ , is a divergent function ( $\kappa_T^0 \rightarrow +\infty$ ); therefore, under these conditions, the partial molar volume of the solute at infinite dilution will also be divergent  $\bar{V}_2^\infty \rightarrow +\infty$ , and the sign of the Krichevskii parameter will define the sign of such divergence. For the two mixtures studied in this work, the parameter  $A_{Kr} > 0$ , thus at the critical point of the solvent,  $\bar{V}_2^\infty \rightarrow +\infty$ . A representation of  $\bar{V}_2^\infty$  vs  $\rho_{CO_2}$  can be seen in Fig. S3 (Supporting Information). Table 4 shows the maximum values of  $\bar{V}_2^\infty$  exhibited by our systems at a temperature of 308.15 K; these peaks appear in the vicinity of the critical pressure ( $\cong 8$  MPa) and the value is higher for the CO<sub>2</sub>+CO mixture, which suggests that the substitution of a molecule of CO<sub>2</sub> by one of CO results in a bigger change in the volume of the system than if the replacing molecule were CH<sub>4</sub>.

The only value found in the literature for the partial molar volume at infinite dilution of the systems studied has been published by Abdulagatov et al. (2007) for the CO<sub>2</sub>+CH<sub>4</sub> system. These authors find a negative sign for the divergence of  $\bar{V}_2^\infty$ , which is not consistent with the positive sign of their own value of  $A_{Kr}$ .



**Fig. 10.** Krichevskii function,  $J$ , versus density of the pure solvent,  $\rho_{CO_2}$ , for the {CO<sub>2</sub> (1)+CH<sub>4</sub> (2)} and {CO<sub>2</sub> (1)+CO (2)} systems at  $T=304.21$  K and  $T=308.15$  K.

### 5.1.2. Structural properties

The study of a fluid structure can be conducted through the so-called inversion of the Kirkwood–Buff Theory (Kirkwood and Buff, 1951), developed by Ben-Naim in 1977. In it, measurements of thermodynamic properties are used to calculate Kirkwood–Buff integrals,  $G_{ij} = \int_0^\infty [g_{ij}(r) - 1] 4\pi r^2 dr$ , where  $g_{ij}(r)$  is the pair correlation function or radial distribution function for species  $i$  and  $j$ , and represents the probability of finding the particle  $i$  at a distance  $r$  of the particle  $j$ . Strictly speaking, the  $G_{ij}$  integrals are not molecular properties, however, they provide information about the species' local packing.

For a binary mixture at infinite dilution conditions,  $x_2 \rightarrow 0$ , the Kirkwood–Buff equations are simplified (Lee and Cochran, 1994; Chialvo and Cummings, 1995) to:

$$\rho_1^0 \bar{V}_2^\infty = 1 + \rho_1^0 (G_{11}^0 - G_{12}^\infty) \quad (8)$$

$$\rho_1^0 RT \kappa_T^0 = 1 + \rho_1^0 G_{11}^0 \quad (9)$$

Considering Eqs. (7) and (8):

$$J = \frac{\rho_1^0 (G_{11}^0 - G_{12}^\infty)}{\kappa_T^0} \quad (10)$$

Alternatively, the Kirkwood–Buff equations and the expression for the Krichevskii function can be written in terms of the direct correlation function integral (DCFI),  $C_{ij} = \int c_{ij} dr$  where  $c_{ij}$  represents the direct correlation due solely to the interaction forces exerted between two particles in a system of  $N-2$  particles.

$$\rho_1^0 \bar{V}_2^\infty = \rho_1^0 RT \kappa_T^0 (1 - C_{12}^\infty) \quad (11)$$

$$(\kappa_T^0)^{-1} = \rho_1^0 RT (1 - C_{11}^0) \quad (12)$$

$$J = \rho_1^0 RT (C_{11}^0 - C_{12}^\infty) \quad (13)$$

As can be seen in Eqs. (10) and (13),  $J$  represents the difference between solvent–solvent (1–1) and solvent–solute (1–2) interactions, making it possible to evaluate the ideality of the mixture: a value close to zero indicates that these interactions are very similar. The equations above show that, in IDS, the rearrangement of the solvent around the solute, in relation to the structure of the pure solvent, is not determined by the strength of the interaction between the molecules of solvent and solute, but defined by the intermolecular asymmetry. The values of the direct correlation function integrals,  $C_{ij}$ , for  $\text{CO}_2 + \text{CH}_4$  are higher than for  $\text{CO}_2 + \text{CO}$  (Table 4 shows one of them,  $(C_{12})_{\rho_c}$ ). However, the greater asymmetry of the second system causes a more extensive change in the structure of the solvent, as evidenced by higher values of  $(C_{11} - C_{12})$ ; a graphical representation is shown in Fig. S4 (Supporting Information).

$N_{12}^{\text{exc}}$  is defined as the excess number of solvent molecules around a solute molecule in the IDS, in relation to the number of solvent molecules around another solvent molecule. This parameter is related to the radial distribution functions for the interactions solvent–solute (1–2) and solvent–solvent (1–1) and consequently with the Krichevskii function:

$$\begin{aligned} N_{12}^{\text{exc}} &= (N_{12} - N_{11}) 4\pi \rho_1^0 \int_0^{R_{\text{shell}}} [g_{12}(r) - g_{11}(r)] r^2 dr \\ &= -\kappa_T^0 \left( \frac{\partial P}{\partial x_2} \right)_{T,V}^\infty \end{aligned} \quad (14)$$

where  $N_{12}$  represents the number of solvent molecules around a solute molecule and  $N_{11}$  indicates that each solvent molecule is surrounded by a box of  $N_{11}$  solvent molecules. If we consider the sign obtained for the Krichevskii function in our current work, we realize that the replacement of one molecule of solvent by another of solute, at constant volume and temperature, causes a decrease

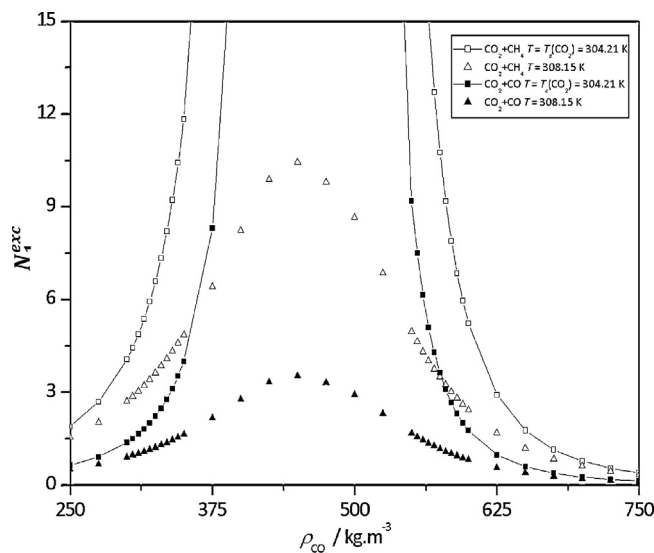


Fig. 11. Affinity of solvent molecules for a solute molecule (cluster size),  $N_1^{\text{exc}}$ , versus density of the pure solvent,  $\rho_{\text{CO}_2}$ , for the  $\{\text{CO}_2(1) + \text{CH}_4(2)\}$  and  $\{\text{CO}_2(1) + \text{CO}(2)\}$  systems at  $T = 304.21 \text{ K}$  and  $T = 308.15 \text{ K}$ .

in the local density of  $\text{CO}_2$  molecules around a molecule of solute in the IDS compared to that of pure  $\text{CO}_2$ , and the effect is greater for CO than for  $\text{CH}_4$ . A plot of  $N_1^{\text{exc}}$  vs  $\rho_{\text{CO}_2}$  is shown in Fig S5 (Supporting Information), and Table 4 lists the minimum values found for the excess coordination number,  $N_{12}^{\text{exc}}$ , of our systems at 308.15 K.

Moreover, the affinity of solvent molecules for a molecule of solute, or cluster size,  $N_1^{\text{exc}}$ , may be calculated from the properties of the pure solvent and from the so-called dimensionless Krichevskii parameter  $A_{\text{Kr}}^* = A_{\text{Kr}} / \rho_1^0 RT$ ,

$$N_1^{\text{exc}} = 4\pi \rho_1^0 \int_0^{R_{\text{shell}}} [g_{12}(r) - 1] r^2 dr = \rho_1^0 RT \kappa_T^0 (1 - A_{\text{Kr}}^*) \quad (15)$$

Fig. 11 shows the evolution of  $N_1^{\text{exc}}$  with the density of pure solvent for our systems: it becomes a divergent function at the solvent critical point,  $N_1^{\text{exc}} \rightarrow +\infty$ , and at 308.15 K, the maximum for the  $\text{CO}_2 + \text{CO}$  system is smaller in magnitude than that for  $\text{CO}_2 + \text{CH}_4$  (Table 4).

Finally, according to Wheeler's decorated lattice model (Wheeler, 1972), the behaviour of a near-critical system can be classified in terms of the solvent–solute interaction energy,  $\varepsilon_{12}$ , when adding a solute molecule to the solvent under isobaric and isothermal conditions: (i) attractive behaviour ( $\varepsilon_{12} \ll 0$ ) which results in a volume contraction and an enrichment of solvent around the solute ( $\bar{V}_2^\infty \rightarrow -\infty$ ,  $N_1^{\text{exc}} \rightarrow +\infty$ ); (ii) weakly attractive behaviour ( $\varepsilon_{12} < 0$ ), causing a volume expansion together with an enrichment in solvent ( $\bar{V}_2^\infty \rightarrow +\infty$ ,  $N_1^{\text{exc}} \rightarrow -\infty$ ); and (iii) repulsive behaviour ( $\varepsilon_{12} > 0$ ) that leads to a volumetric expansion and a decrease in solvent around the solute ( $\bar{V}_2^\infty \rightarrow +\infty$ ,  $N_1^{\text{exc}} \rightarrow -\infty$ ). Debenedetti and Mohamed in 1989 and Lee and Cochran in 1994 established that for IDS in the vicinity of the critical point, mixtures can be classified within the previous regimes depending on the sign of the Krichevskii parameter,  $A_{\text{Kr}}$ , the value of the dimensionless parameter,  $A_{\text{Kr}}^*$ , and the divergence signs for different properties:  $\bar{V}_2^\infty$ ,  $N_{12}^{\text{exc}}$ , and  $N_1^{\text{exc}}$ .

For the mixtures included in this study:

$$A_{\text{Kr}} > 0; \quad \bar{V}_2^\infty \rightarrow +\infty; \quad N_{12}^{\text{exc}} \rightarrow -\infty; \quad 1 > A_{\text{Kr}}^* > 0; \quad N_1^{\text{exc}} \rightarrow +\infty$$

Therefore we can conclude that both systems, near the solvent critical point, behave as weakly attractive mixtures. There are studies in the literature on the nature of the  $\text{CO}_2 + \text{CH}_4$  system based on Molecular Dynamics Simulation (Baglin et al., 2000; Skarmoutsos and Samios, 2006; Parris, 2010). Skarmoutsos and



Samios determined that this system shows repulsive behaviour with a value of the excess coordination number slightly negative,  $N_{exc}^{\infty} = -0.261$ . However, their calculations were performed under conditions of temperature and pressure away from the critical point:  $T = 323.15$  K and  $P = 9.94$  MPa.

## 5.2. Effect of impurities in the process design

Given that the technology for natural gas (NG) transport is well developed and that there are vast pipeline networks dedicated to this use, it would seem a possibility to use existing gas pipelines for CO<sub>2</sub> transport. However, the large differences between the behaviour of CH<sub>4</sub> (main component in NG) and that of CO<sub>2</sub> (main compound in CCS), in practice limit this use to transport in gas phase (ElementEnergy, 2010; Serpa et al., 2011). Therefore, it may become necessary to design a new pipeline network to transport CO<sub>2</sub> in dense or supercritical phase. Furthermore, the presence of impurities in the anthropogenic CO<sub>2</sub> stream, even in small proportions, can significantly modify the properties of the fluid to be transported, primarily the phase equilibrium, density and viscosity, which strongly affects pipeline hydraulics and many other aspects of pipeline design and operation (Seevam et al., 2008). In order to evaluate these effects the usual parameters related to transport have been used: mass flow,  $m$ , erosional velocity,  $v_E$ , pipeline inner diameter,  $D$ , Reynolds number,  $Re$ , Darcy–Weisbach friction factor,  $f$ , pressure drop per unit length  $\Delta P/L$ , and capacity of the booster stations,  $W$  (Table 5). To calculate them, models based on Bernoulli's law for incompressible flow, applied to full and turbulent flow in circular shaped pipelines, have been used. These models, relatively simple but pragmatic, have been reviewed and accepted by the industrial and engineering community (Vandeginste and Piessens, 2008; ElementEnergy 2010). To establish a comparison between the behaviour of the pure CO<sub>2</sub> stream and the stream containing impurities, normalized parameters have been defined,  $X/X_0$ , where  $X$  are the above mentioned parameters for the mixtures and  $X_0$  for pure CO<sub>2</sub>. Table S4 (Supporting Information) shows the equations for normalized parameters, as well as certain conditions that have been kept constant for both streams in the calculations. In this manner, the deviations from unity of the normalized parameters are due to the different compositions and, therefore, different properties of pure and anthropogenic CO<sub>2</sub> streams.

Conditions of composition ( $x_{CO_2} \cong 0.97$ ), pressure ( $P = 8.6$ – $20$  MPa) and temperature ( $T = 304.21$  and  $308.15$  K) used for the calculation are within customary in CCS technology (ElementEnergy, 2010, Li et al., 2011a; ENCAP Project, 2008; EEA,

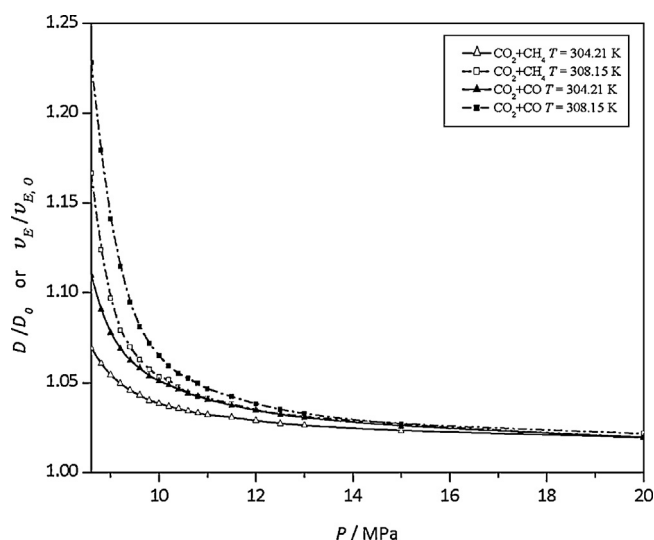


Fig. 12. Comparison of normalized pipeline inner diameter,  $D/D_0$ , (for a given mass flow and transport velocity) or erosional velocity,  $v_E/v_{E,0}$ , for mixtures CO<sub>2</sub> + CH<sub>4</sub> or +CO with  $x_{CO_2} \cong 0.97$ .

2012; EPA, 2012). The experimental values of the densities used in the calculation have been taken from this work, from Blanco et al. (2012) and from Velasco et al. (2011). The viscosities have been obtained from REFPROP 9.0 (Lemmon et al., 2010) by using the extended corresponding states (ECS) model developed by Klein et al. (1997).

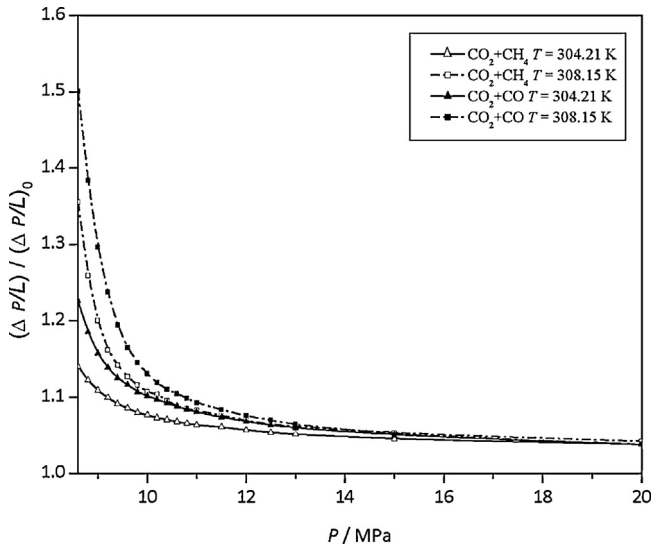
To obtain the friction factors,  $f$ , and the pressure drops per metre,  $\Delta P/L$ , standard values for pipeline inner diameter,  $D = 0.508$  m, and mass flow,  $m = 317$  kg/s (Serpa et al., 2011), and roughness height of commercial steel,  $e = 4.6 \times 10^{-5}$  m (Vandeginste and Piessens, 2008), have been used.

The results are shown in Table S5 (Supporting Information) and in Figs. 12 and 13, and S6–S9 (Supporting Information). As can be seen, the differences with respect to the behaviour of pure CO<sub>2</sub> are greater for CO<sub>2</sub> + CO than for CO<sub>2</sub> + CH<sub>4</sub> mixtures, in accordance with the conclusions drawn in Section 5.1 (the CO molecule provokes greater structural disruption than CH<sub>4</sub> in their respective mixtures with CO<sub>2</sub>). For both systems, the differences increase with increasing  $T$  and decreasing  $P$ . They became significant at pressures ranged from 8.6 to 10 MPa, but they are smaller than 10% above 15 MPa.

Table 5

Equation overview for the calculation of several parameters in pipeline design and operation (ElementEnergy, 2010).

Parameter	Formula	Symbols
Mass flow	$m = \rho \times v \times A$	$m$ = mass flow (kg/s); $\rho$ = fluid density (kg/m <sup>3</sup> ); $v$ = fluid velocity (m/s); $A$ = pipeline inner section (m <sup>2</sup> ).
Pipeline inner diameter sizing	$D = \left( \frac{4 \times m}{v \times \pi \times \rho} \right)^{1/2}$	$D$ = inner diameter (m); $m$ = mass flow (kg/s); $v$ = fluid velocity (m/s); $\rho$ = fluid density (kg/m <sup>3</sup> ).
Erosional velocity	$v_E = \frac{C}{\sqrt{\rho}}$	$v_E$ = erosional velocity (m/s); $C$ = empirical constant; $\rho$ = fluid density (kg/m <sup>3</sup> ).
Reynolds number	$Re = \frac{\rho \times v \times D}{\mu}$	$Re$ = Reynolds number; $\rho$ = fluid density (kg/m <sup>3</sup> ); $v$ = fluid velocity (m/s); $D$ = inner diameter (m); $\mu$ = fluid viscosity (Pa s).
Capacity of the booster stations	$W = \frac{m}{\rho} \times \frac{(P_{out} - P_{in})}{\eta_{booster}}$	$W$ = capacity of the booster station (MW); $m$ = mass flow (kg/s); $\rho$ = fluid density (kg/m <sup>3</sup> ); $P_{out}$ = booster outlet pressure (MPa); $P_{in}$ = booster inlet pressure (MPa); $\eta_{booster}$ = booster efficiency.
Darcy–Weisbach friction factor	$f = \frac{1.325}{[\ln(e/3.7 \times D) - (5.74/Re^{0.9})]^2}$	$f$ = Darcy–Weisbach friction factor; $e$ = roughness height (m); $D$ = inner diameter (m); $Re$ = Reynolds number.
Pressure drop per metre	$\frac{\Delta p}{L} = \frac{8 \times f \times m^2}{\rho \times \pi^2 \times D^5}$	$(\Delta P/L)$ = pressure drop per metre (Pa/m); $m$ = mass flow (kg/s); $\rho$ = fluid density (kg/m <sup>3</sup> ); $f$ = Darcy–Weisbach friction factor; $D$ = inner diameter (m).



**Fig. 13.** Comparison of normalized pressure drop per metre,  $(\Delta P/L)/(\Delta P/L)_0$ , for a mass flow of 317 kg/s (10 Mt/year), a pipeline inner diameter of 0.508 m (20 inch) and a roughness height of  $4.6 \times 10^{-5}$  m (0.00015 ft) for mixtures  $\text{CO}_2 + \text{CH}_4$  or  $+\text{CO}$  with  $x_{\text{CO}_2} \cong 0.97$ .

For a transport velocity and a pipeline inner diameter, the mass flow,  $m$ , is lower for mixtures than for pure  $\text{CO}_2$  ( $m/m_0 = 0.96\text{--}0.66$ , Fig. S8, Supporting Information), due to the lower density of the mixtures. Normalized Darcy–Weisbach friction factors,  $f/f_0$ , are also lower than 1 (0.995–0.999, Fig. S9, for the utilized pipeline inner diameter, mass flow and roughness height). The rest of the normalized parameters are greater than 1, which means that the corresponding values for the mixtures parameters are higher than those for pure  $\text{CO}_2$ . The higher deviations appear in the  $\text{CO}_2 + \text{CO}$  mixture at 308.15 K and 8.6 MPa, with  $Re/Re_0 = 1.75$  and  $(\Delta P/L)/(\Delta P/L)_0 = 1.50$ . Pressure drop per metre is higher for mixtures than for pure  $\text{CO}_2$  in all the cases studied, a fact which might require an increase in the number of boosters along the network, especially if transport is carried out at low pressures.

## 6. Conclusions

Density measurements of the  $\{\text{CO}_2 (1) + \text{CH}_4 (2)\}$  and  $\{\text{CO}_2 (1) + \text{CO} (2)\}$  systems were carried out under conditions of composition, pressure and temperature of interest in CCS technology:  $x_{\text{CO}_2} \geq 0.97$ ,  $P = 0.1\text{--}20$  MPa, and  $T = T_c(\text{CO}_2) = 304.21$  K for both systems and at  $T = 308.15$  K for the  $\text{CO}_2 + \text{CO}$  system. All  $P\text{--}\rho\text{--}T\text{--}x_{\text{CO}_2}$  data have been obtained using a vibrating-tube densimeter. The expanded ( $k=2$ ) uncertainty and the repeatability (mean relative standard deviation) of the density measurements for our mixtures have been calculated:  $U(\rho) = 0.4\text{--}0.7$  kg/m<sup>3</sup> and  $\bar{S}_\rho^r = 0.13\%$ . Other properties related to experimental data such as isothermal compressibility,  $\kappa_T$ , excess molar volume,  $V_m^E$ , and solute partial molar volume,  $\bar{V}_2$ , in the critical region ( $T = 304.21$  and 308.15 K and  $P = 5\text{--}10$  MPa) have been calculated as a function of pressure and composition.

The volumetric behaviour has been compared to literature data and it has been modelled with three Equations of State. The deviations obtained have been: Peng–Robinson,  $\text{MRD}_\rho \leq 3.5\%$ ; rescaled PC-SAFT,  $\text{MRD}_\rho \leq 2.8\%$ ; and GERG,  $\text{MRD}_\rho \leq 1.0\%$ . Thus the three EoS have been validated, for these binary systems, under CCS technology conditions.

Using the Krichevskii Function concept and the Kirkwood–Buff Theory, we have carried out a theoretical study of the interactions between  $\text{CO}_2$  and  $\text{CO}$ , or  $\text{CO}_2$  and  $\text{CH}_4$  molecules. To this end we have calculated: (i) the Krichevskii function,  $J$ , and the Krichevskii

parameter,  $A_{\text{Kr}}$ , which reflect the change experimented by the pressure when replacing a molecule of solvent by another of solute in infinitely dilute solutions, IDS, at constant  $T$  and  $V$ ; (ii) the partial molar volume of the solute at infinite dilution,  $\bar{V}_2^\infty$ ; (iii) the direct correlation function integrals,  $C_{ij}$ ; (iv) the excess coordination number,  $N_{exc}^\infty$ ; and (v) the affinity of the solvent per solute molecule, or cluster size,  $N_1^{exc}$ . From the sign of the Krichevskii parameter,  $A_{\text{Kr}}$ , its dimensionless counterpart,  $A_{\text{Kr}}^*$ , and the divergence signs for different structural properties in the systems studied ( $A_{\text{Kr}} > 0$ ;  $\bar{V}_2^\infty \rightarrow +\infty$ ;  $N_{exc}^\infty \rightarrow -\infty$ ;  $1 > A_{\text{Kr}}^* > 0$ ;  $N_1^{exc} \rightarrow +\infty$ ), we can conclude that these mixtures exhibit weakly attractive behaviour.

We have proven that the presence of impurities in  $\text{CO}_2$ , even in small proportions, modifies the properties of the mixtures. This results, in turn, in a modification of the parameters related to the design and operation in the process of fluid transport, depending on the nature of the mixture, the pressure and the temperature, and must be taken into account in the planning of CCS facilities. In this paper we have quantified the effect of small amounts of  $\text{CH}_4$  and  $\text{CO}$  in  $\text{CO}_2$  transport through various normalized parameters (related to their corresponding values when the fluid to be transported is pure  $\text{CO}_2$ ). The parameters studied were: pipeline inner diameter,  $D$ , erosional velocity,  $v_E$ , transport velocity,  $v$ , Reynolds number,  $Re$ , booster capacity,  $W$ , mass flow,  $m$ , Darcy–Weisbach friction factor,  $f$ , and pressure drop per metre,  $\Delta P/L$ . Differences with respect to pure  $\text{CO}_2$  increase with increasing temperature and decreasing pressure, becoming important (up to 75% in some cases) for  $8.6 \text{ MPa} < P < 10 \text{ MPa}$  (working operating pressures in transport), and converge to smaller values (less than 10%) for  $P > 15 \text{ MPa}$ .

We have observed, in all the properties studied in this work (volumetric, structural and operational for CCS technology), that the presence of  $\text{CO}$  as an impurity in anthropogenic  $\text{CO}_2$  produces a greater disruption in relation to pure  $\text{CO}_2$  than that of  $\text{CH}_4$ .

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## Appendix A.

### A.1. Relation between period, $\tau$ , and density, $\rho$

$$\rho(P, T) = \left( \frac{M_0}{V_i(P, T)} \right) \left[ \left( \frac{K(P, T)}{K_0(T)} \right) \left( \frac{\tau^2(P, T)}{\tau_0^2(T)} \right) - 1 \right] \quad (\text{A1})$$

$$\rho(P, T) = \rho_{\text{ref}}(P, T) \frac{(K(P, T)/K_0(T))(\tau^2(P, T) - \tau_0^2(T))}{(K(P, T)/K_0(T))(\tau_{\text{ref}}^2(P, T) - \tau_0^2(T))} \quad (\text{A2})$$

where  $\rho(P, T)$  is the density of the inner fluid to be determined at pressure  $P$  and temperature  $T$ ;  $\rho_{\text{ref}}(P, T)$  is the density of the reference fluid at pressure  $P$  and temperature  $T$ ;  $M_0$  is the mass of the vibrating tube under vacuum;  $V_i(P, T)$  is the internal volume of the vibrating tube at pressure  $P$  and temperature  $T$ ;  $K(P, T)$  is the transversal stiffness of the vibrating tube at pressure  $P$  and temperature  $T$ ;  $K_0(T)$  is the transversal stiffness under vacuum at temperature  $T$ ;  $\tau(P, T)$  is the period of the vibrating tube with inner fluid to be determined at pressure  $P$  and temperature  $T$ ;  $\tau_{\text{ref}}(P, T)$  is the period of the vibrating tube with reference fluid at pressure  $P$  and temperature  $T$ ;  $\tau_0(T)$  is the period under vacuum of the vibrating tube at temperature  $T$ .

## A.2. Uncertainty, $U(y)$

The expanded ( $k=2$ ) uncertainty in the density,  $\rho$ , excess molar volumes,  $V_m^E$ , and solute molar partial volumes,  $\bar{V}_2$ , have been calculated by the rules of error propagation law (JCGM 100, 2008):

$$U(y) = k u_c(y) = k \left[ \sum_{i=1}^N \left( \frac{\partial f}{\partial x_i} \right)^2 u^2(x_i) \right]^{1/2} \quad (\text{A3})$$

where  $k$  is the coverage factor;  $u_c(y)$  is the combined standard uncertainty of the estimated  $y$ ;  $x_i$  represent the input variables;  $(\partial f/\partial x_i)$  is the sensitivity coefficient of the input variable  $x_i$ ;  $u^2(x_i)$  is the variance of  $x_i$ .

## A.3. Relative mean standard deviation, $\bar{S}_x^r$ , and mean relative deviation, $MRD_x$

The relative mean standard deviation is calculated:

$$\bar{S}_x^r = \frac{100}{N} \sum_{j=1}^N (j S_x^r) \quad (\text{A4})$$

where  $j S_x^r$  is the relative standard deviation by point:

$$j S_x^r = \frac{j S_x}{(1/n) \sum_{i=1}^n x_i^{\text{exp}}} \quad (\text{A5})$$

and  $j S_x$  is the standard deviation by point:

$$j S_x = \sqrt{\frac{n \sum_{i=1}^n (x_i^{\text{exp}})^2 - \left( \sum_{i=1}^n x_i^{\text{exp}} \right)^2}{n(n-1)}} \quad (\text{A6})$$

The relative mean deviation is calculated:

$$MRD_x = \frac{100}{N} \sum_{i=1}^N \left| \frac{x_i^{\text{exp}} - x_i^*}{x_i^{\text{exp}}} \right| \quad (\text{A7})$$

where  $x_i^{\text{exp}}$  are experimental data;  $x_i^*$  are bibliographic or calculated values;  $N$  is the number of points;  $n$  is the number of analysis for given  $T$  and  $P$ .

## Appendix B. Supplementary data

Supplementary material related to this article can be found, in the online version, at doi:10.1016/j.ijggc.2013.07.019.

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# Discussion of the Influence of CO and CH<sub>4</sub> in CO<sub>2</sub> Transport, Injection, and Storage for CCS Technology

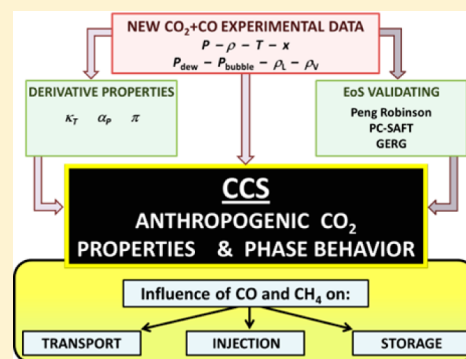
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## Supporting Information

**ABSTRACT:** This paper discusses the influence of the noncondensable impurities CO and CH<sub>4</sub> on Carbon Capture and Storage (CCS) technology. We calculated and drew conclusions about the impact of both impurities in the CO<sub>2</sub> on selected transport, injection, and storage parameters (pipeline pressure drop, storage capacity, etc.), whose analysis is necessary for the safe construction and operation of CO<sub>2</sub> pipelines and for the secure long-term geological storage of anthropogenic CO<sub>2</sub>. To calculate these parameters, it is necessary to acquire data on the volumetric properties and the vapor–liquid equilibrium of the fluid being subjected to CCS. In addition to literature data, we used new experimental data, which are presented here and were obtained for five mixtures of CO<sub>2</sub>+CO with compositions characteristic of the typical emissions of the E.U. and the U.S.A. Temperatures and pressures are based on relevant CO<sub>2</sub> pipeline and geological storage site values. From our experimental results, Peng–Robinson, PC-SAFT, and GERG Equations of State for were validated CO<sub>2</sub>+CO under the conditions of CCS. We conclude that the concentration of both impurities strongly affects the studied parameters, with CO being the most influential and problematic. The overall result of these negative effects is an increase in the difficulties, risks, and overall costs of CCS.



## 1. INTRODUCTION

Carbon Capture and Storage (CCS) technology is one of the most effective climate change mitigation strategies in the medium term. In 2013, the Global CCS Institute identified 65 large-scale CCS projects in various stages of development, of which only 19 will be operational by 2016.<sup>1</sup> The capture and storage capacity of these 19 projects is approximately 38.5 megatons per year, while the storage forecasts are more than 7 gigatons per year in 2050.<sup>2</sup>

The goal of CCS is to avoid the release to the atmosphere of anthropogenic CO<sub>2</sub> generated by industrial and energy-related sources. CO<sub>2</sub> is captured in individual producer facilities and subsequently conditioned, transported, and injected into an underground geological storage field.<sup>3–5</sup> CO<sub>2</sub> capture can be accomplished by different techniques: postcombustion, pre-combustion, and oxy-combustion. Conditioning can be carried out by dehydration, separation of noncondensable gases and/or liquefaction, and compression/pumping. Transport is usually performed by pipeline, and the anthropogenic CO<sub>2</sub> is finally injected and stored in depleted oil and gas fields, deep saline formations or deep unmineable coal seams.

The source of the CO<sub>2</sub> as well as the capture and conditioning processes used will determine the composition of the transported and stored CO<sub>2</sub>. High purification is technically possible but not economically viable.<sup>4</sup> In addition, recent literature focuses on the potential benefits and limitations of the combined capture (cocapture) and storage

of multiple gases (CO<sub>2</sub> and at least one other gas).<sup>6–9</sup> The presence of impurities in the fluid and the wide ranges of temperature, *T*, and pressure, *P*, involved in CCS cause the physicochemical properties of the current anthropogenic CO<sub>2</sub> to vary significantly according to its origin and to change significantly throughout the process.<sup>10–12</sup>

CO<sub>2</sub>QUEST<sup>13</sup> and Impacts<sup>14</sup> are two research projects of the seventh Framework Programme of the European Commission, among others, that are currently devoted to evaluating the impact of CO<sub>2</sub> quality on its transport and storage behavior. However, there is a shortage of experimental data on the mixtures of interest specific to this technology.<sup>15,16</sup>

This work is part of a study we are carrying out<sup>17–20</sup> on CO<sub>2</sub> systems containing noncondensable or condensable impurities, with the ultimate goal of validating equations of state, EoS, and obtaining interaction parameters, if necessary, from synthetic multicomponent mixtures with compositions representative of actual anthropogenic CO<sub>2</sub>. The first objective of this work was to quantify fundamental properties, such as volumetric and phase behavior, of mixtures of CO<sub>2</sub> with a noncondensable impurity, CO, using our experimental installations. CO is a highly toxic impurity whose presence is especially important in

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precombustion capture processes.<sup>11</sup> We present new and accurate pressure–density–temperature–composition,  $P\rho T x_{\text{CO}_2}$ , and vapor–liquid equilibrium, VLE, experimental data for five mixtures of  $\text{CO}_2+\text{CO}$  whose compositions, temperatures and pressures are within the range of interest applicable to CCS conditions.<sup>12,15,21–28</sup>

There are experimental studies in the literature on the volumetric properties<sup>20,29,30</sup> and the vapor–liquid equilibrium<sup>31</sup> of  $\text{CO}_2+\text{CO}$ , but none cover the range of interest for CCS technology to the extent of this work. Due to the scarce experimental data on this and other impurities, most of the studies performed simulations to predict both the thermodynamic behavior and the values of the parameters associated with transport, injection and storage.<sup>11,12,32–34</sup>

Using experimental data from this work for the  $\text{CO}_2+\text{CO}$  system, and from literature for pure  $\text{CO}_2$ ,<sup>18</sup>  $\text{CO}_2+\text{CH}_4$ ,<sup>19,20</sup> and  $\text{CO}_2+\text{CO}$ ,<sup>20</sup> we have quantified and compared the effect of the presence of CO and  $\text{CH}_4$  (another noncondensable impurity), evaluating several selected transport, injection and storage parameters.<sup>12,25,32</sup> The analysis of these parameters is necessary for the safe and reliable design, construction, and operation of  $\text{CO}_2$  pipelines and injection equipment, as well as the secure long-term geological storage of  $\text{CO}_2$ .

In addition, we validate with our experimental data three equations of state: Peng–Robinson (PR) EoS, widely used in industry;<sup>35</sup> GERG EoS, developed for natural gas;<sup>36</sup> and PC-SAFT EoS, one of the most used in this technology for the calculation of thermodynamic properties.<sup>37,38</sup> Given that there remains no one single equation whose characteristics are ideally suited for this technology, it is essential to have experimental data to draw realistic conclusions and to aid in the rational selection of the optimal equation.<sup>11,15,39,40</sup>

Because some impurities of anthropogenic  $\text{CO}_2$  are toxic, and  $\text{CO}_2$  itself is directly toxic in air when inhaled at concentrations above approximately 5%, the safe operation of  $\text{CO}_2$  pipelines is of paramount importance.<sup>41</sup> Due to the relatively high Joule–Thomson expansion coefficient of  $\text{CO}_2$  and its triple point coordinates, the rapid expansion of an accidental release may lead to solids formation following a pipeline rupture or puncture. In this regard, several publications devoted to the prediction of phase equilibria involving solids, either validating existing EoS or proposing new ones, are found in the literature.<sup>42–46</sup>

In summary, this work provides new experimental volumetric and VLE data of the system  $\text{CO}_2+\text{CO}$  at compositions, pressures, and temperatures of interest for CCS technology. Using these data, we validate several equations of state under CCS conditions.<sup>35–38</sup> From this work and literature experimental data,<sup>18–20</sup> we calculate and draw conclusions about the impact of both CO and  $\text{CH}_4$  impurities in the  $\text{CO}_2$  on selected engineering parameters related to the transport, injection, and geological storage of the  $\text{CO}_2$ .<sup>12,25,32</sup>

## 2. EXPERIMENTAL SECTION

**2.1. Materials.** Carbon dioxide (wt % > 99.998) and carbon monoxide (wt % > 99.997) were obtained from Air Liquide and used without further purification.

The  $\text{CO}_2+\text{CO}$  mixtures with a  $\text{CO}_2$  mole fraction,  $x_{\text{CO}_2}$ , from 0.9700 to 0.9960 were prepared by successive introduction of the components (in order of increasing volatility) into a variable-volume cell, which was weighed on a mass comparator with a precision of 0.0002 g.

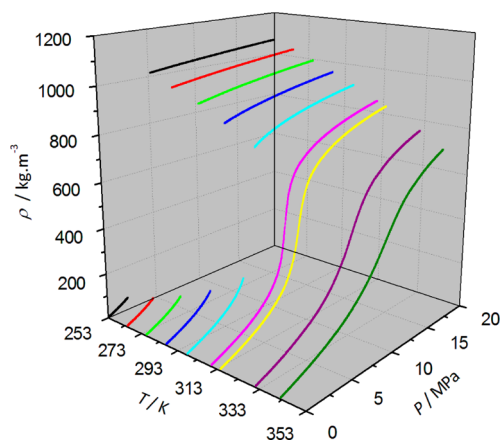
**2.2. Apparatus and Procedures.** The experimental setup used in this work for the determination of  $P\rho T$  data of  $\text{CO}_2+\text{CO}$  mixtures is the same as that described in a previous study.<sup>18</sup> Its main component is a vibrating tube densimeter Anton Paar HPM, which is connected to a MPDS 2000 V3 evaluation unit. The use of two thermostatic baths at two different temperatures ( $\Delta T \cong 0.3^\circ$ ), one for the densimeter and the other for the rest of the installation, assures that the first drop of liquid (at dew pressure,  $P_{\text{dew}}$ ) or the first vapor bubble (at bubble pressure,  $P_{\text{bubble}}$ ) is formed inside the vibrating tube. Moreover, the quasi continuous acquisition of  $P\rho T$  data (6000 points/isotherm evenly reduced to approximately 1000 points/isotherm for easier handling) allows the determination of the limits of VLE and the calculation of derivative properties, both with adequate accuracy. The temperature and pressure ranges are 253 to 423 K  $\pm$  0.006 K and from atmospheric pressure to 70 MPa with a precision of 0.025% FS, respectively.

The uncertainty propagation law was used<sup>47</sup> to evaluate the precision in the density of our mixtures; the expanded ( $k = 2$ ) uncertainty obtained is  $U(\rho) = 0.35\text{--}0.80 \text{ kg}\cdot\text{m}^{-3}$ . The repeatability of the density measurements for mixtures, expressed as the relative mean standard deviation, is  $\bar{S}_\rho^r = 0.13\%$ .<sup>18</sup>

## 3. RESULTS AND DISCUSSION

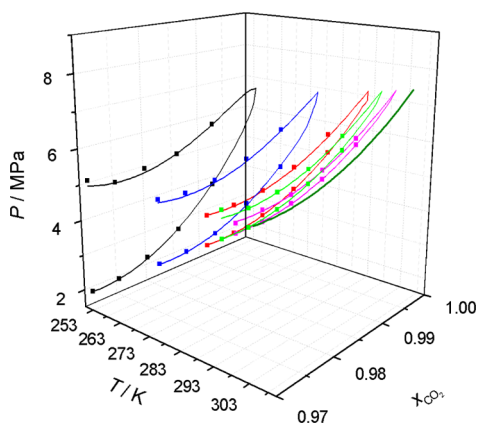
$P\rho T x_{\text{CO}_2}$  measurements for  $\text{CO}_2+\text{CO}$  mixtures ( $x_{\text{CO}_2} = 0.9700, 0.9810, 0.9902, 0.9930, \text{ and } 0.9960$ ) at  $T = 253.15, 263.15, 273.15, 283.15, 293.15, 323.15, 333.15, \text{ and } 343.15 \text{ K}$  were carried out in the pressure range from 0.1 to 20 MPa. The CO mole fractions of this work include the compositions of the typical emissions in the E.U. and the U.S.A., whose values range approximately from 0.007 to 0.030 and from 0.011 to 0.016, respectively.<sup>26,28</sup> The experiments were performed at  $T$  and  $P$  relevant to those in  $\text{CO}_2$  pipelines and in geologic storage sites (geothermic gradient = 25 K/km; hydrostatic pressure gradient = 10 MPa/km).<sup>15,21,22</sup>

In the Supporting Information, SI, Table S1 contains a total of 40 000  $P\rho T x_{\text{CO}_2}$  points. Figure 1 shows the experimental densities for the  $\text{CO}_2+\text{CO}$  mixture with  $x_{\text{CO}_2} = 0.9700$ ; analogous representations for the rest of the mixtures are included in SI Figure S1. In these figures, the density of the mixtures at supercritical temperatures is a continuous line



**Figure 1.** Experimental densities,  $\rho$ , for  $\text{CO}_2+\text{CO}$  mixtures with  $x_{\text{CO}_2} = 0.9700$  at several temperatures and pressures.

whose slope diminishes as  $T$  increases; the maximum slope is at the critical conditions of the mixture. This is consistent with the fact that the isothermal compressibility of the mixtures is maximum at the critical point and diminishes as  $T$  increases away from the critical value. The mixtures studied in this work have critical temperatures between 302.6 and 303.9 K.<sup>20</sup> The subcritical isotherms show a discontinuity in the VLE region, which is limited by  $P_{\text{dew}}$  and  $P_{\text{bubble}}$  (Figure 2); these values and those for the densities of the liquid and vapor phases in equilibrium,  $\rho_L$  and  $\rho_V$ , respectively, (Figure S2) are shown in Table S2 in the SI.



**Figure 2.** Vapor pressure of  $\text{CO}_2$ <sup>48</sup> (olive green) and experimental phase envelopes for  $\text{CO}_2+\text{CO}$  mixtures with  $x_{\text{CO}_2} = 0.9700$  (black),  $x_{\text{CO}_2} = 0.9810$  (blue),  $x_{\text{CO}_2} = 0.9902$  (red),  $x_{\text{CO}_2} = 0.9930$  (green), and  $x_{\text{CO}_2} = 0.9960$  (pink).

We have found studies in the literature on VLE<sup>31</sup> and the volumetric<sup>20,29,30</sup> behavior of  $\text{CO}_2+\text{CO}$ . The values taken from the VLE graphical representations of Kaminiishi and Toriumi do not agree with our experimental values or with the values predicted by the EoS used in this work. Our volumetric experimental data are consistent with those from literature, but cannot be directly compared because either the compositions<sup>29,30</sup> or the temperatures<sup>20</sup> do not match.

The composition of the anthropogenic  $\text{CO}_2$  and the temperature and pressure during its transport and storage will vary based on multiple factors: different regulations regarding quality requirements of the fluid, different emission sources and capture and conditioning processes, emission plants operating under variable external demands, operational depressurizations, and off-shore versus on-shore transport. Given the variability of the conditions involved in CCS technology, it becomes necessary to use a predictive tool, such as an EoS, to calculate the values of essential properties, such as density and phase equilibria, for the optimal design and operation of the facilities involved in CCS. However, none of the current EoS presents marked advantages over the others.<sup>11,15,39,40</sup> In this regard, we have compared, in terms of relative mean deviation,  $\text{MRD}_x$ , our experimental data for density and VLE with those calculated using three different types of equations of state: PR EoS,<sup>35</sup> GERG EoS,<sup>36</sup> and PC-SAFT EoS.<sup>37,38</sup>

The parameters used for the pure components in PR and PC-SAFT EoS, as well as the binary interaction parameter,  $k_{ij}$ , included in the mixing rule of a van der Waals fluid are shown in SI Table S3. The  $\text{MRD}_x$  values are tabulated in the SI (Tables S4 and S5). The  $\text{MRD}_\rho$  values obtained for  $\text{CO}_2+\text{CO}$

mixtures with  $x_{\text{CO}_2} = 0.9810$  and  $x_{\text{CO}_2} = 0.9930$  at 253.15 K (subcritical  $T$ ) and 343.15 K (supercritical  $T$ ) are represented in SI Figure S3. From the results obtained, it can be concluded that (i) the PR EoS provides a reasonable prediction of the volumetric behavior and a good representation of VLE despite its simplicity ( $\text{MRD}_\rho = 2.87\%$ ,  $\text{MRD}_{P_{\text{bubble}}} = 1.89\%$ ,  $\text{MRD}_{P_{\text{dew}}} = 0.47\%$ ); (ii) the GERG EoS is the equation that best represents our experimental density and VLE data ( $\text{MRD}_\rho = 0.73\%$ ,  $\text{MRD}_{P_{\text{bubble}}} = 1.30\%$ ,  $\text{MRD}_{P_{\text{dew}}} = 0.38\%$ ), although it requires substantial computation time<sup>39</sup> and its extension to mixtures containing compounds not included in its database is complex; and (iii) the PC-SAFT EoS adequately predicts  $P\rho T$  and VLE ( $\text{MRD}_\rho = 1.19\%$ ,  $\text{MRD}_{P_{\text{bubble}}} = 1.58\%$ ,  $\text{MRD}_{P_{\text{dew}}} = 1.45\%$ ) and can easily be extended to multicomponent mixtures.

**3.1. Influence of Impurities on Transport.** The presence of impurities in the anthropogenic  $\text{CO}_2$  greatly affects both the phase and the volumetric behaviors of the fluid, thereby modifying the parameters utilized in the design and operation of transport by pipeline. Some of these parameters will be discussed in this section: the minimum operational pressure,  $P_{\text{min}}$ ; the pressure profile along the pipeline,  $P(d)$ , where  $d$  is the distance; the maximum repressurization distance (maximum separation distance between boosters),  $L$ ; the booster stations power,  $W$ ; and the inner diameter of the pipeline,  $D$ . These, and other required parameters (Reynolds number, friction factor and pressure drop per meter), were calculated using the recommended equations<sup>25,32</sup> shown in SI Table S6. When fixed values were assumed for certain parameters in the calculations of others, it is indicated in the text and in the figure captions. The results for  $\text{CO}_2+\text{CO}$  were compared with those calculated for  $\text{CO}_2+\text{CH}_4$  mixtures and for pure  $\text{CO}_2$  under the same conditions. We used the phase equilibria and volumetric experimental data obtained from this work and from the literature.<sup>18–20</sup> Viscosity values were calculated using REFPROP 9.0.<sup>48</sup>

**3.1.1. Minimum Operational Pressure,  $P_{\text{min}}$ .** Although the transport by pipeline of anthropogenic  $\text{CO}_2$  in gaseous phase has been considered in several studies<sup>49,50</sup> and may be cost-effective for low mass flow rates and short distances,<sup>50</sup> it is most commonly transported in a supercritical or dense phase. In any case, it is important to avoid phase changes and two-phase flow during pipeline operation.

Transporting in a dense phase is achieved by setting  $P_{\text{min}}$  to always be higher than  $P_{\text{bubble}}$  of the transported fluid. The impurities accompanying the anthropogenic  $\text{CO}_2$  significantly influence the characteristics and location of the two-phase region. Thus, for pure  $\text{CO}_2$  transported at 283.15 K, the vapor phase appears at the saturation pressure  $P_{\text{sat}} = 4.50$  MPa (SI Table S2). However, if the fluid contains 3% by mole  $\text{CH}_4$ , then the vapor will appear at  $P_{\text{bubble}} = 5.85$  MPa, and it will coexist with the liquid until  $P_{\text{dew}} = 4.69$  MPa, below which there will be a single-phase gas.<sup>19</sup> If the impurity is 3% by mole  $\text{CO}$ , the two-phase flow would take place from 6.57 to 4.72 MPa ( $P_{\text{bubble}}$  and  $P_{\text{dew}}$ , respectively) (SI Table S2, Figure 2, and SI Figure S2).

Another issue to be considered when anthropogenic  $\text{CO}_2$  is transported in the dense phase is the possible proximity of the operational conditions to the critical point of the fluid. Under these conditions, density values change significantly with small changes in  $P$ ,  $T$ , or  $x_{\text{CO}_2}$  (e.g., compressibility will be very high,  $(\kappa_T)_{T,P} \rightarrow \infty$ ), which influences the transport parameters.



For the anthropogenic CO<sub>2</sub> transport pressure in a supercritical or dense phase, the literature provides ranges of 7.5–11 MPa for  $P_{\min}$  and 9–30 MPa for the maximum pressure,  $P_{\max}$ ; minimum values ensure dense or supercritical conditions for the fluid, and maximum values depend more on economic factors than technical ones.<sup>51</sup> Temperatures range from a lower limit, usually above  $-2\text{ }^{\circ}\text{C}$  (271 K), set by winter surrounding temperatures, and an upper limit, 30–44  $^{\circ}\text{C}$  (303–317 K), determined by the compressor station discharge temperature and the external pipeline coating material. Both onshore and offshore references have been considered.<sup>7,11,15,16,22,25,51–60</sup>

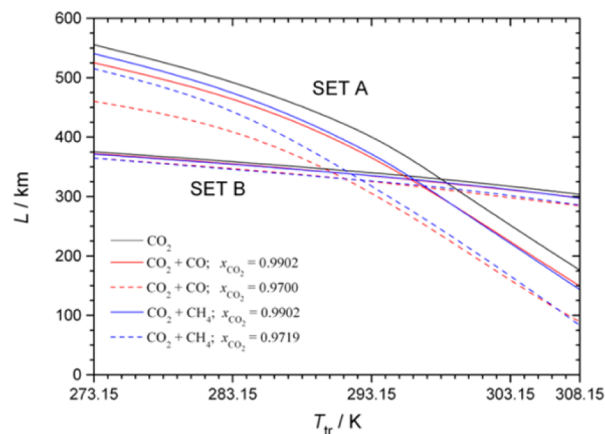
Some previous studies propose, instead of pressure ranges, a reference value of 800 kg/m<sup>3</sup> as the minimum density of the fluid during the transport.<sup>25,32</sup> SI Table S7 presents the minimum operational pressure needed to ensure this density value,  $P_{\min}^{800}$ , if the transported fluid is pure CO<sub>2</sub> or for CO<sub>2</sub>+CO mixtures with compositions  $x_{\text{CO}_2} = 0.9902$  and  $x_{\text{CO}_2} = 0.9700$ . Again, the impurities are very important; considering the fluid to be pure CO<sub>2</sub> can introduce an error of up to 62% in  $P_{\min}^{800}$  if the anthropogenic CO<sub>2</sub> is actually a mixture with 3% by mole CO. The same amount of CH<sub>4</sub> would lead to an error of up to 27%.<sup>19</sup>

We calculated the remaining mentioned parameters for the transport of pure CO<sub>2</sub>, CO<sub>2</sub>+CO, and CO<sub>2</sub>+CH<sub>4</sub> systems, both with  $x_{\text{CO}_2} \cong 0.99$  and  $x_{\text{CO}_2} \cong 0.97$ , between  $P_{\max} = 20.0$  MPa and  $P_{\min} = 9.0$  MPa (the average maximum and minimum literature values) and temperatures from 273.15 to 308.15 K. In addition, we calculated the  $L$  and  $W$  required to maintain the density of the fluid above 800 kg/m<sup>3</sup> during transport. In this case, the transport is considered to be between  $P_{\max} = 20.0$  MPa and the corresponding  $P_{\min}^{800}$  at each composition and transport temperature. The pressure profile,  $L$  and  $W$ , were all calculated for a mass flow,  $m$ , of 317 kg/s (10 Mt/year) in a  $D = 0.508$  m (20 in.) pipeline with a roughness height,  $e$ , of  $4.6 \times 10^{-5}$  m (0.00015 ft.).<sup>32,56</sup>

**3.1.2. Pressure Profile along the Pipeline,  $P(d)$ .** SI Figure S4 shows the influence of impurities on the pressure drop along a pipeline for these systems at various transport temperatures,  $T_{\text{tr}}$ , and a pipeline inlet pressure ( $P_{\max}$ ) of 20.0 MPa. The pressure drop increases with increasing temperature and (noncondensable) impurity concentration, due to the decrease in the density and the viscosity of the mixture (see SI Tables S1 and S6), and the presence of CO or CH<sub>4</sub> has a very similar influence on it. For example: in scenario of SI Figure S4, and for a distance,  $d$ , of 250 km, for pure CO<sub>2</sub> pressure drops from 20 MPa down to 12.7 MPa at 273.15 K, and to 11.2 MPa at 308.15 K; if the fluid is a mixture with  $x_{\text{CO}_2} \cong 0.97$ , then the pressure drops down to 12.5 MPa at 273.15 K and to 10.6 MPa at 308.15 K.

Pressure drop, itself related to the diameter of the pipeline, the inlet pressure and the properties of the transported fluid, determines the placement and number of pumping (booster) stations, if needed. However, most techno-economic models do not take into account pumping stations, or they include them with a simplified approach, resulting in a large uncertainty in their costs and placement.<sup>50,61</sup> To choose the most cost-effective option, the trade-offs between diameter, inlet pressure, and pumping stations must be considered.

**3.1.3. Maximum Repressurization Distance,  $L$ , and Booster Stations Power,  $W$ .** Figure 3 shows the maximum repressurization distance,  $L$ , versus the transport temperature,  $T_{\text{tr}}$ , for the



**Figure 3.** Maximum repressurization (pumping) distances,  $L$ , versus transport temperature,  $T_{\text{tr}}$ , for pure CO<sub>2</sub>, CO<sub>2</sub>+CO, and CO<sub>2</sub>+CH<sub>4</sub> mixtures. Set A:  $L$  required to maintain the density of the fluid above 800 kg/m<sup>3</sup>. Set B:  $L$  required to maintain the pressure above 9.0 MPa. Mass flow was taken to be  $m = 317$  kg/s, inner diameter of the pipeline  $D = 0.508$  m, and roughness height  $e = 4.6 \times 10^{-5}$  m. The pipeline inlet pressure was set at 20.0 MPa.

fluid transported by pipeline. Two sets of lines are represented: set A shows  $L$  required to maintain the density of the fluid above 800 kg/m<sup>3</sup>, and set B shows  $L$  required to maintain the pressure above 9.0 MPa. In both sets,  $L$  decreases as both  $T_{\text{tr}}$  and CO or CH<sub>4</sub> concentrations increase due to the increase in the pressure drop which in turn is due to the decrease in the density and the viscosity (SI Figure S4). In set A,  $L$  varies approximately 470 km between the represented ranges of composition, pressure and temperature. Moreover, at low  $T_{\text{tr}}$ , both the type of impurity (CO or CH<sub>4</sub>) and its concentration affect  $L$  strongly, whereas at high  $T_{\text{tr}}$ , only the concentration has an influence (CO<sub>2</sub>+CO and CO<sub>2</sub>+CH<sub>4</sub> systems exhibit a similar behavior). In set B, the variation of  $T_{\text{tr}}$  and CO or CH<sub>4</sub> concentration has a less pronounced effect on  $L$  (approximately 85 km).

SI Figure S5 shows an estimation of the booster power required to repressurize the fluid up to a booster outlet pressure  $P_{\text{out}} = P_{\max} = 20.0$  MPa,  $W_{20}$ , versus the transport temperature,  $T_{\text{tr}}$ . It was assumed that the fluid enters the booster at the inlet temperature,  $T_{\text{in}} = T_{\text{tr}}$ , and leaves it at the outlet temperature  $T_{\text{out}} = 38\text{ }^{\circ}\text{C}$  (311 K).<sup>11,25,51,54,60</sup> The average in–out values for each fluid density were used. Set A presents  $W_{20}$  required when the booster inlet pressure,  $P_{\text{in}}$ , is  $P_{\min}^{800}$  at  $T_{\text{in}}$ ; set B presents  $W_{20}$  when  $P_{\text{in}} = P_{\min}$  is 9.0 MPa. In set A, the variation of  $W_{20}$  with both  $T_{\text{tr}}$  and composition is similar to that found for  $L$  in the same set in Figure 3, and  $W_{20}$  varies within the represented range of composition,  $T$  and  $P$  by approximately 6.9 MW. In set B, the variation is the opposite: the higher the temperature or the impurity concentration, the higher  $W_{20}$  becomes, with  $\Delta W_{20} \cong 1.8$  MW.

Thus, at 283.15 K, a typical  $T_{\text{tr}}$ , one must repressurize at a maximum distance of  $\cong 420$ –497 km (depending on the composition of the fluid) to keep the density above 800 kg/m<sup>3</sup>, and the required booster power ranges from approximately 7.0 to 7.9 MW. However, to keep the pressure above 9.0 MPa, the repressurization distance varies from  $\cong 346$  to 359 km, and the booster power varies between  $\cong 5.3$  and 5.5 MW (Figure 3 and SI Figures S5, S6, and S7). The best operational options for a given network can be calculated. For instance, for a 400 km pipeline, no booster stations would be necessary to maintain



the density above 800 kg/m<sup>3</sup>; however, one booster would be required to maintain the pressure above 9.0 MPa.

**3.1.4. Pipeline Inner Diameter,  $D$ .** SI Figure S8 shows the inner diameter of a pipeline,  $D$ , versus its capacity (mass flow,  $m$ ) for the studied systems at several values for  $T$  and  $P$  under the transport conditions. The represented range of capacity was chosen to be approximately 317 kg/s (10.0 Mt/year). Diameters were iteratively calculated for each mass flow assuming an average pressure drop per meter of 33 Pa/m and a roughness height of the pipeline of  $4.6 \times 10^{-5}$  m.<sup>32</sup> The transported mass flow for a given diameter decreases as  $P$  decreases and as  $T$  increases or as impurity concentration rises. For identical mole fractions at low temperature and high pressure, the behaviors of the mixtures containing either CO or CH<sub>4</sub> are very similar. However, greater differences appear at high temperature, high concentration of impurities, and at low pressure. Within the represented capacities, the largest difference between the pipeline diameter calculated for pure CO<sub>2</sub> and those for the studied mixtures is 27 mm (corresponding to the CO<sub>2</sub>+CO system with  $x_{\text{CO}_2} = 0.9700$  at  $T = 308.15$  K and  $P = 9.0$  MPa, SI Figure S8e). The increase of 27 mm in the inner diameter means an increase of approximately 11 tons (approximately 5% of the total weight) of steel per km of pipeline (standard carbon steel pipeline, API SL X70, inner diameter 536 mm, wall thickness 16.5 mm,<sup>62</sup> and mass flow 317 kg/s).

### 3.2. Influence of Impurities on Storage and Injection.

In CO<sub>2</sub> storage, impurities have different effects depending on the type of reservoir and the interaction between the injected anthropogenic CO<sub>2</sub> and the substances present beforehand. The effects of CO on several parameters related to the storage and injection steps and the comparison with those of CH<sub>4</sub> are discussed below.

**3.2.1. Solubility Parameter,  $\delta$ .** Given the values of temperature and pressure inside the reservoirs, the fluid is in a supercritical state and therefore has one of the characteristic properties of this state, which is a large solvent capacity. The solubility parameter (eq 1)<sup>63</sup> has been extensively used to predict in a semiquantitative manner the behavior of liquid mixtures<sup>64–67</sup> and slightly polar supercritical fluids.<sup>18,68</sup> We utilized  $\delta$  to study the interactions between the injected fluid (considered as the solvent) and other substances in the reservoir.

$$\delta = \left( \frac{-E(T)}{V(T, P)} \right)^{1/2} \quad (1)$$

where  $(-E/V)$  is the so-called “cohesive energy density”. In this work, we used the internal pressure,  $\pi$ , to estimate the solubility parameter, thus applying the approach made by Hansen<sup>64</sup> and neglecting the small dipole moment of CO (0.12 D):<sup>69</sup>

$$\delta = \pi^{1/2} \quad (2)$$

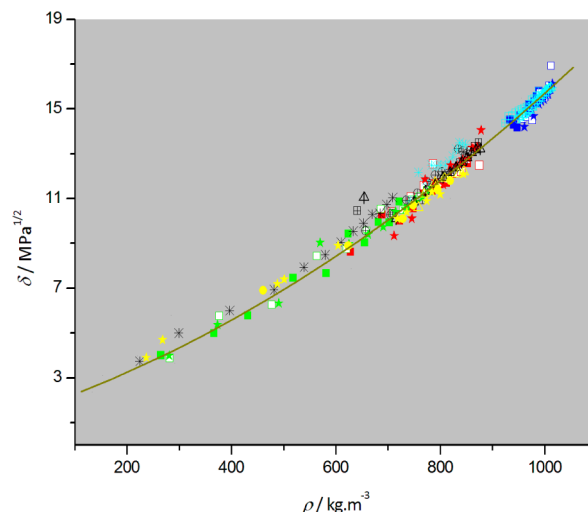
$$\pi = \left( \frac{\partial U}{\partial V} \right)_T = T \left( \frac{\partial P}{\partial T} \right)_V - P = T \frac{\alpha_p}{\kappa_T} - P \quad (3)$$

where  $\alpha_p$  is the isobaric thermal expansivity, and  $\kappa_T$  is the isothermal compressibility. We obtained values for  $\alpha_p$ ,  $\kappa_T$ , and  $\delta$  from the  $P\rho T x_{\text{CO}_2}$  measurements (SI Table S8), with the following MRD <sub>$x$</sub>  values calculated in relation to values from the best EoS, the GERG EoS, to reproduce our experimental values:<sup>36</sup> MRD <sub>$\alpha_p$</sub>  = 2.54%, MRD <sub>$\kappa_T$</sub>  = 1.47% and MRD <sub>$\delta$</sub>  = 1.59%

(subcritical temperatures, 253.15 K  $\leq T \leq$  293.15 K) and MRD <sub>$\alpha_p$</sub>  = 5.04%, MRD <sub>$\kappa_T$</sub>  = 4.27% and MRD <sub>$\delta$</sub>  = 3.04% (supercritical isotherms, 304.21 K  $\leq T \leq$  333.15 K).

Solubility parameters are represented in SI Figure S9 for pure CO<sub>2</sub> and CO<sub>2</sub>+CO mixtures with  $x_{\text{CO}_2} = 0.9902$  and  $x_{\text{CO}_2} = 0.9700$  at 293.15, 308.15, and 333.15 K. As seen, the presence of CO in the anthropogenic CO<sub>2</sub> causes  $\delta$  to diminish compared to pure CO<sub>2</sub>, reducing the solvent power of the fluid and consequently hindering fluid trapping. The same effect was already observed for the CO<sub>2</sub>+CH<sub>4</sub> system.<sup>19</sup> For the studied conditions, the solubility parameter decreases as temperature increases and pressure decreases. Our values for the solubility parameter are consistent with those from the literature for CO<sub>2</sub>+CO at 333.15 K,<sup>30</sup> but they are not directly comparable due to their different compositions.

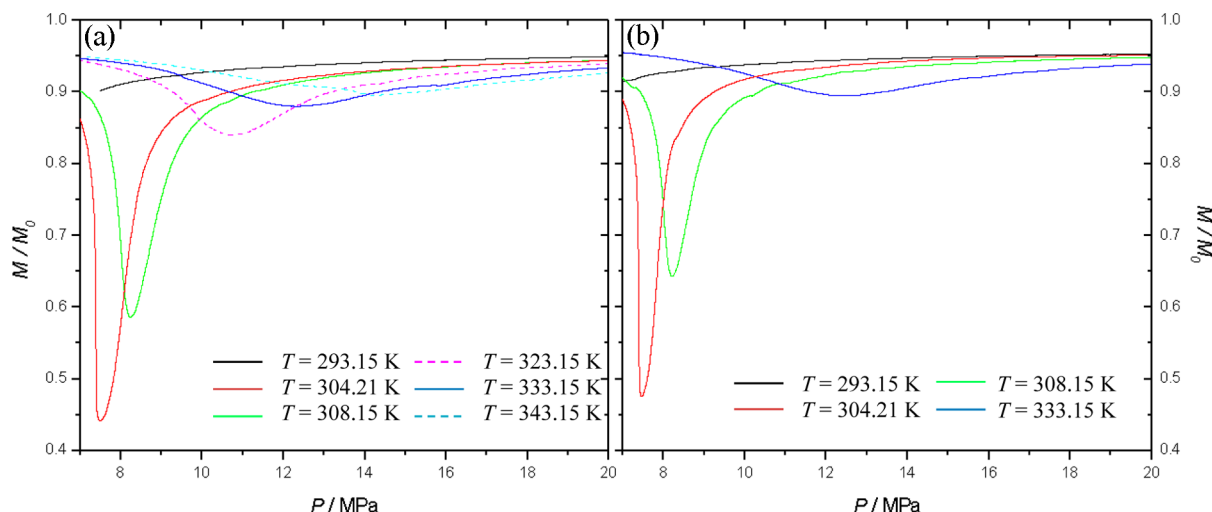
Allada et al.<sup>68</sup> suggest that the solubility parameter is the key determinant of solubility in supercritical solvents, and they were able to unify diverse behaviors of solvents regardless of  $T$ ,  $P$ , and their nature. Moreover, different authors<sup>18,30</sup> note that density has the strongest influence on the solvent capacity of dense fluids. Figure 4 shows  $\delta$  versus  $\rho$  for pure CO<sub>2</sub> and six



**Figure 4.** Solubility parameter,  $\delta$ , against density,  $\rho$ , for pure CO<sub>2</sub><sup>18</sup> (line); CO<sub>2</sub>+CO mixtures with  $x_{\text{CO}_2} = 0.9700$  (■),  $x_{\text{CO}_2} = 0.9902$  (□) and  $x_{\text{CO}_2} = 0.9930$  (★) at 273.15 K (blue), 304.21 K (red) and 323.15 K (green); CO<sub>2</sub>+CH<sub>4</sub> mixtures<sup>19</sup> with  $x_{\text{CO}_2} = 0.8525$  (\*),  $x_{\text{CO}_2} = 0.9719$  (⊕) and  $x_{\text{CO}_2} = 0.9932$  (⊞) at 273.15 K (cyan) and 304.21 K (black); and CO<sub>2</sub>+CO (▲), CO<sub>2</sub>+H<sub>2</sub> (●) and CO<sub>2</sub>+CO+H<sub>2</sub> (★) mixtures<sup>30</sup> (yellow).

CO<sub>2</sub>+CO, CO<sub>2</sub>+CH<sub>4</sub>, CO<sub>2</sub>+H<sub>2</sub>, and CO<sub>2</sub>+CO+H<sub>2</sub> mixtures from this work and other literature.<sup>18–20,30</sup> The graphic shows a good  $\delta$ - $\rho$  correlation within the represented density range. This means that systems with different  $T$  and/or  $P$ , but with the same density, will have the same solubility parameter and, therefore, that the solubilization capacity of the injected CO<sub>2</sub> could be known from its density at storage conditions.

In the following, we compare the influence of two noncondensable impurities, CO or CH<sub>4</sub>, on the storage capacity,  $M$ , the rising velocity of the plume inside deep saline aquifers,  $v$ , and the permeation flux during injection,  $\dot{M}$ . For this purpose, we use normalized parameters,  $X/X_0$ , where  $X$  is the value corresponding to the CO<sub>2</sub>+CO or CO<sub>2</sub>+CH<sub>4</sub> systems and  $X_0$  corresponds to pure CO<sub>2</sub>. The studied  $T$  and  $P$  ranges are



**Figure 5.** Normalized storage capacity,  $M/M_0$ , versus pressure at several temperatures for (a)  $\text{CO}_2+\text{CO}$  ( $x_{\text{CO}_2} = 0.9700$ ) and (b)  $\text{CO}_2+\text{CH}_4$  ( $x_{\text{CO}_2} = 0.9719$ ) mixtures.

293.15 K – 343.15 K and 7 MPa–20 MPa, respectively, and are within the temperature and pressure ranges of the operating reservoirs in different scenarios.<sup>12,24</sup> The equations used are as follows:<sup>12,19</sup>

$$\frac{M}{M_0} = \frac{\rho}{\rho_0 \left[ 1 + \sum_i \left( \frac{m_i}{m_0} \right) \right]} \quad (4)$$

$$\frac{v}{v_0} = \frac{F/(\rho\eta)}{F_0/(\rho_0\eta_0)} = \frac{(\rho_{\text{br}} - \rho)(\rho_0\eta_0)}{(\rho_{\text{br}} - \rho_0)(\rho\eta)} \quad (5)$$

$$\frac{\dot{M}}{\dot{M}_0} = \frac{\rho \left( \frac{\eta_0}{\eta} \right)}{\rho_0 \left[ 1 + \sum_i \left( \frac{m_i}{m_0} \right) \right]} \quad (6)$$

where  $m_i/m_0$  is the ratio of the mass of impurity  $i$  to the mass of  $\text{CO}_2$  in the mixture;  $(\rho, \eta, F)$  and  $(\rho_0, \eta_0, F_0)$  are the density, the viscosity, and the buoyancy force of the mixture and the pure  $\text{CO}_2$  stream, respectively; and  $\rho_{\text{br}}$  is the density of the brine.

Density values were taken from experimental  $P\rho T x_{\text{CO}_2}$  data for pure  $\text{CO}_2$ ,<sup>18</sup>  $\text{CO}_2+\text{CO}$  (this work and literature values<sup>20</sup>), and  $\text{CO}_2+\text{CH}_4$ .<sup>19,20</sup> The values of  $1025 \text{ kg/m}^3$  and  $1250 \text{ kg/m}^3$ , representative of dilute and highly concentrated brines,<sup>70</sup> were used for  $\rho_{\text{br}}$ . Viscosity data were calculated as previously described.<sup>48</sup>

**3.2.2. Normalized Storage Capacity,  $M/M_0$ .** This parameter is dependent on composition,  $T$  and  $P$ . Streams with high concentrations of noncondensable impurities reduce the storage capacity by a large amount if  $T$  and  $P$  are near of the critical values of the mixture. For example, an impurity of 15% by mole  $\text{CH}_4$  reduces  $M/M_0$  to approximately 0.35 at 308.15 K and 8.5 MPa,<sup>19</sup> revealing that a relatively shallow site may not be appropriate for storing high impurity streams. Figure 5 shows  $M/M_0$  versus  $P$  at several  $T$  for the two systems with  $x_{\text{CO}_2} 0.97$ , the highest impurity concentration in this work. The maximum decrease appears near the critical point of anthropogenic  $\text{CO}_2$  ( $M/M_0 \cong 0.44$  for  $\text{CO}_2+\text{CO}$  at 304.21 K and 7.5 MPa). An increase in temperature shifts this maximum decrease to a higher pressure, and its magnitude decreases ( $M/M_0 \cong 0.89$  at 343.15 K and 14.1 MPa). Likewise, as the depth of

the geological formation increases, the influence of the type of impurity on storage capacity decreases. It can be seen that  $\text{CO}$  affects the mass of anthropogenic  $\text{CO}_2$  that can be stored in a reservoir more negatively than  $\text{CH}_4$  so that, for the same mass of fluid, it would be necessary to confine the  $\text{CO}_2+\text{CO}$  system at higher pressure than  $\text{CO}_2+\text{CH}_4$ . Storage efficiency can be improved if the injection pressure is well above the minimum values shown in these representations. In the case of closed reservoirs, this value for pressure has to be within the allowable overpressure range. For open formations, an option could be to increase the depth of storage, given that overpressure may not be attainable.

**3.2.3. Normalized Rising Velocity,  $v/v_0$ .** If the reservoir is a saline aquifer, then the stored fluid pushes up with a buoyancy force,  $F$ , which is given by the difference between its density and that of brine (eq 5). The speed of the plume,  $v$ , is directly proportional to the buoyancy force and inversely proportional to its viscosity. The presence of noncondensable impurities increases the rising velocity, although the values of the normalized parameter depend on temperature and pressure. The  $v/v_0$  relations, represented in SI, Figure S10 versus  $P$  at several  $T$  for the two systems with  $\rho_{\text{br}} = 1025 \text{ kg/m}^3$ , present maxima at  $T \geq 304.21 \text{ K}$ , which are higher for the  $\text{CO}_2+\text{CO}$  mixtures than for  $\text{CO}_2+\text{CH}_4$  (9.2 and 7.7 at 304.21 K, respectively). The maxima for each temperature are found at pressures inside the depth range corresponding to a saline aquifer.<sup>24</sup> The presence of  $\text{CO}$  or  $\text{CH}_4$  leads to an increase in the rising velocity of the plume, which is significant near the critical point of the fluid, resulting in the decrease of the  $\text{CO}_2$ –brine contact and therefore the solvent effect. The lateral spreading of the plume also decreases, and as a consequence, the amount of trapped fluid in the rock’s pores diminishes. These effects reduce the  $\text{CO}_2$  storage security and become even more important near the cap rock, at a lower depth (low pressure range of the representation where the highest peaks are found), and the risk of leakage could increase. An increase in the density of the brine reduces  $F/F_0$  and  $v/v_0$  (SI Figures S10 and S11).

**3.2.4. Normalized Permeation Flux,  $\dot{M}/\dot{M}_0$ .** The relative injectivity of the impure  $\text{CO}_2$  stream depends on the effect of impurities,  $T$  and  $P$ , on both the density and the viscosity.  $\dot{M}$  reduces as a result of the lower density of these mixtures in

relation to CO<sub>2</sub>; however, due to the compensation by increased viscosity, the reduction is smaller than that of the storage capacity discussed before. In the studied systems  $\rho < \rho_0$  and  $\eta < \eta_0$  and given the relative values of  $\rho/\rho_0$  and  $\eta_0/\eta$  in eq 6, the normalized permeation flux can be higher or lower than unity. Figure S12 shows that the largest differences from 1 appear in the vicinity of the critical point. At high pressures throughout the studied  $T$  range, the effect of temperature diminishes, and  $\dot{M}/\dot{M}_0$  tends to values approaching unity. It can be seen that the influence of CO is greater than that of CH<sub>4</sub> on this parameter. Another effect of noncondensable impurities, such as CO or CH<sub>4</sub>, on the injection step is the need to increase the headhole pressure as a consequence of the lower hydrostatic pressure of the injection well.<sup>71</sup>

From the obtained results for the three normalized storage and injection parameters, we verified the following trends with composition,  $T$  and  $P$ : (i) a high impurity composition modifies these parameters by a large amount; (ii) for the same composition, the highest deviations from pure CO<sub>2</sub> appear near the critical point of the mixture; (iii) as pressure increases, the influence of temperature becomes less important; (iv) as the pressure and temperature increase, the influence of the presence of impurities is attenuated; (v) the parameter most affected by impurities is the rising velocity over the entire studied ranges of  $T$  and  $P$ ; and (vi) CO has a greater effect than CH<sub>4</sub> on all the studied normalized parameters and becomes the most problematic of the two impurities.

In summary, the presence of the studied impurities, CO and CH<sub>4</sub>, leads to (i) a decrease in the interactions that enable CO<sub>2</sub> to become trapped inside the storage area; (ii) the need for greater storage capacity reservoirs and/or a larger number of sites to confine the same mass of fluid; (iii) an increased risk of leakage in saline aquifers; (iv) the need to increase the injection pressure; and (v) a need to increase the number of monitoring units to ensure a safe process. All these effects result in an increase in the overall cost of the process. Similar observations have been found in literature for other noncondensable impurities.<sup>12</sup>

## ■ ASSOCIATED CONTENT

### ● Supporting Information

Additional tables and figures regarding experimental data, derivative properties, EoS modeling and transport and storage parameters are presented. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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### Notes

The authors declare no competing financial interest.

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# Thermodynamic properties of a CO<sub>2</sub> – rich mixture (CO<sub>2</sub> + CH<sub>3</sub>OH) in conditions of interest for carbon dioxide capture and storage technology and other applications



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## ABSTRACT

Methanol can be an impurity in transported and stored anthropogenic CO<sub>2</sub> in carbon dioxide capture and storage technology; likewise, methanol is one of the most useful CO<sub>2</sub> modifiers for supercritical processes. Therefore reliable values of thermodynamic properties of CO<sub>2</sub> – rich mixtures CO<sub>2</sub> + CH<sub>3</sub>OH are needed. We measured the following properties of a (CO<sub>2</sub> + CH<sub>3</sub>OH) mixture with  $x_{\text{CO}_2} = 0.9700$  in dense phase at six temperatures from 263.15 K to 313.15 K:

- The speed of sound,  $c$ , up to 194.49 MPa, using a double-path pulse-echo method at 5 MHz, for which a repeatability study gave an overall standard uncertainty of  $c$ ,  $u(c) = 5.9 \times 10^{-4}c$ .
- The density,  $\rho$ , at pressures  $\leq 20.00$  MPa using a vibrating-tube densimeter with a standard uncertainty,  $u(\rho) = 0.4 \text{ kg/m}^{-3}$ .

Combining our  $c$  and  $\rho$  experimental values and the isobaric specific heat capacity,  $c_p$ , from the GERG equation of state (EoS), we calculated  $\rho$ ,  $c_p$ , the volume-dependent solubility parameter,  $\delta_V$ , and the Joule–Thomson coefficient,  $\mu_{JT}$ , at pressures  $\leq 195.0$  MPa. We are the first to report the adaptation for compressed gases of a calculation method based on numerical integration previously used only for liquids. The experimental and calculated values were compared with those from the PC-SAFT and GERG EoSs, allowing us to validate both EoSs to represent the experimental properties of the system under most conditions studied and the calculation method up to 195.0 MPa.

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## 1. Introduction

Carbon dioxide capture and storage (CCS) is considered one of the most important technologies to reduce the world's emissions of greenhouse gases. In the International Energy Agency's two-degree scenario (2DS), CCS is expected to help reduce global CO<sub>2</sub> emissions by storing approximately 7 gigatons per year by 2050 [1]. This amount is much greater than that used for enhanced oil and gas recovery purposes (approximately 50 megatons per year in the USA [2]). To optimize the process efficiency, the CO<sub>2</sub> will have to be transported from the capture plants to reservoirs predominantly in high-pressure pipelines [3].

CCS technology comprises three main steps: anthropogenic CO<sub>2</sub> capture, transport and storage. The design of each step is

influenced by the thermodynamic procedure used to model the fluid behaviour [3]. Whether using an existing procedure or developing a new one, experimental data on the physicochemical properties of CO<sub>2</sub> mixtures with the impurities typically present in anthropogenic CO<sub>2</sub> are needed in wider composition, temperature and pressure ranges than those associated with CCS technology [4]. However, the paucity of experimental values precludes the development of a reference model for this technology, especially an equation of state (EoS), which is one of the most critical future challenges [5].

To develop an EoS, the essential data are the volumetric properties (pressure–density–temperature,  $p$ – $\rho$ – $T$ ) and the vapor–liquid equilibrium, VLE, although reliable values for the speed of sound,  $c$ , and the isobaric specific heat capacity,  $c_p$  are necessary as well. Using acoustic results to formulate EoSs is particularly attractive given that the speed of sound can be measured with outstanding precision over wide temperature and pressure ranges.

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Furthermore, all the thermodynamic properties of a fluid can be obtained from speed of sound measurements by integrating the partial differential equations that relate  $c$  to other thermodynamic properties [6]. Currently, accurately measuring the speed of sound propagation in high-pressure fluids is one of the standard methods to precisely determine such fluids' thermophysical properties [7].

In practice, reliable  $p$ – $\rho$ – $T$  values, among others, are necessary to evaluate parameters related to transport, injection and storage [8]. Moreover, the speed of sound enables detection of the pressure drop along the pipeline and leaks, monitoring of changes in composition and the performance of seismic studies [9–11].

To estimate the temperature variations at various stages of the process, precise data from additional thermodynamic properties such as  $c_p$  and the Joule–Thomson coefficient,  $\mu_{JT}$ , are required [9,12]. The solubility parameter,  $\delta$ , provides information about the interactions between the injected fluid and other substances present in the storage reservoir.

All these properties are affected to a great extent by the nature and quantity of the impurities present in the anthropogenic  $\text{CO}_2$ , which, in turn, depend on the  $\text{CO}_2$  source and the capture and conditioning processes [5]. Although the main impurities are  $\text{N}_2$ ,  $\text{H}_2$ ,  $\text{O}_2$ ,  $\text{Ar}$ ,  $\text{SO}_2$ ,  $\text{NO}_x$ ,  $\text{CO}$  and water [4,13], methanol can be present in transported and injected anthropogenic  $\text{CO}_2$  because of its use as a hydrate inhibitor and as a residue from pipeline drying. Thus, quantification of the effect of this impurity on the thermodynamic properties that influence CCS processes is necessary.

Furthermore, supercritical  $\text{CO}_2$ ,  $\text{ScCO}_2$ , is the most widely used supercritical solvent in a broad range of applications, and methanol is one of the most common modifiers added to enhance the solvating power of  $\text{ScCO}_2$  to target polar species [14]. The solvent strength of a supercritical fluid solvent is related to its density, and it may be quantitatively represented by the solubility parameter [15]. In addition,  $c_p$  and  $\mu_{JT}$  of the  $(\text{CO}_2 + \text{CH}_3\text{OH})$  system acting as the mobile phase affect to resolution properties in supercritical fluid chromatography [16].

Density and VLE have been widely studied in the literature [17–37] for the  $(\text{CO}_2 + \text{CH}_3\text{OH})$  system, however we note that little information is available on its volumetric behaviour at  $T \leq 313$  K and at mole fractions of  $\text{CO}_2$ ,  $x_{\text{CO}_2}$ , greater than 0.75 [19–21,32,34]. Values of  $\delta$  have been obtained at  $T \geq 313$  K [14,38–40]; however, no numerical values for  $c$ ,  $c_p$  or  $\mu_{JT}$  are available in the literature.

The aim of this work was to conduct an extensive thermodynamic study of a  $\text{CO}_2$  – rich mixture with  $\text{CH}_3\text{OH}$  ( $x_{\text{CO}_2} = 0.9700$ ) under  $T$  and  $p$  conditions compatible with CCS and other applications. We therefore:

- (i) Adapted and used an experimental apparatus to measure accurately the speed of sound in mixtures containing sufficiently dense compressed gases. We also determined the uncertainty of the experimental speed of sound measurements for the  $(\text{CO}_2 + \text{CH}_3\text{OH})$  system.
- (ii) Experimentally measured the following properties for the  $(\text{CO}_2 + \text{CH}_3\text{OH})$  mixture with  $x_{\text{CO}_2} = 0.9700$ :
  - The speed of sound,  $p$ – $c$ – $T$ , between 263.16 K and 313.15 K and at pressures up to 194.49 MPa.
  - The density,  $p$ – $\rho$ – $T$ , from 263.15 K to 313.15 K and up to 20.00 MPa.
- (iii) Adapted and validated a calculation method to obtain  $\rho$  and  $c_p$  values and derived properties such as the volume-dependent solubility parameter,  $\delta_v$ , and  $\mu_{JT}$  for systems containing compressed gases at pressures up to 195.0 MPa. All properties were obtained for  $(\text{CO}_2 + \text{CH}_3\text{OH})$  with  $x_{\text{CO}_2} = 0.9700$  within the working temperature range.

Several authors [41–45] have used the same fundamental approach for liquid compounds; however, this work represents its first application to compressed gases.

- (iv) Compared either the experimental results or the calculated values of the aforementioned thermodynamic properties with two different formulation EoS: PC-SAFT [46,47] and GERG [48,49].

In summary, in this article we implement an experimental setup to measure  $c$  in mixtures containing compressed gases. We present the experimental results for the speed of sound (at pressures up to 194.49 MPa), and density (up to 20.00 MPa) for the  $(\text{CO}_2 + \text{CH}_3\text{OH})$  mixture ( $x_{\text{CO}_2} = 0.9700$ ); together, these results allow us to evaluate the predictive power of the PC-SAFT and GERG EoSs for these properties. From our  $c$  values and both our  $\rho$  and the GERG EoS  $c_p$  at a reference pressure, we calculate  $\rho$ ,  $c_p$ ,  $\delta_v$ , and  $\mu_{JT}$  for pressures up to 195.0 MPa. This method of calculating thermodynamic properties up to high pressures, which is applied here to compressed gases for the first time, is validated by comparing the results with the values obtained from the PC-SAFT and GERG EoSs.

## 2. Materials and methods

### 2.1. Chemicals

Methanol from Sigma–Aldrich (biotech. grade, mole fraction 0.9993) and carbon dioxide from Air Liquide (mole fraction >0.99998) were used without further purification. The details, including purities and sources of the materials used in this work are listed in Table 1.

### 2.2. Speed of sound data acquisition: experimental setup and procedure

To determine the speed of sound, we used a 5 MHz ultrasonic pulse device previously described for its application to pure fluids [50]. It was originally designed to work with liquids, and we demonstrated that it is also adequate for sufficiently dense compressed gases [50]. The device operates between 253 K and 473 K and from atmospheric pressure to 200 MPa, with standard uncertainties  $u(T) = 0.015$  K and  $u(p) = 0.02$  MPa, respectively.

The  $(\text{CO}_2 + \text{CH}_3\text{OH})$  mixtures were prepared in a variable-volume cell provided by Top Industrie S.A.S. with a maximum volume of 0.51 L and a maximum working pressure of 30 MPa. The cell was first evacuated, and methanol was the first component added to the evacuated cell. Next,  $\text{CO}_2$  was injected using an ISCO model-260D syringe pump for a chromatography instrument; this pump operates at pressures up to 50 MPa. After the mixture was prepared, it was transferred to a syringe pump by pushing the embolus of the cell with an inert gas. It was then transferred from the syringe pump to the experimental setup in several steps. This method allowed us to accumulate enough fluid mass to reach pressures as high as 195.0 MPa using the manual pump in the installation. The mixture was homogenized by stirring inside the

**Table 1**  
The sources and mole fraction purity of the materials used in this paper.

Chemical name	Source	Mole fraction purity	Purification method
Methanol	Sigma Aldrich	0.9993 <sup>a</sup>	None
Carbon dioxide	Air Liquide	>0.99998 <sup>a</sup>	None

<sup>a</sup> The mole fraction was given by the supplier.



variable-volume cell, the syringe pump and the manual pump; it was homogenized using a recirculation pump inside the setup.

The masses of the different components were determined by successive weighing in a mass comparator from Sartorius, model CCE 2004, with a repeatability better than 0.0002 g. The mole fraction of the component that was first introduced,  $x_1$ , was determined by the relation

$$x_1 = \left[ \frac{(m_2 - m_1)}{M_1} \right] / \left[ \frac{(m_3 - m_2)}{M_2} + \frac{(m_2 - m_1)}{M_1} \right] \quad (1)$$

where  $m_1$  is the empty cell mass,  $m_2$  and  $m_3$  are the masses after the first and second components were added, respectively, and  $M_1$  and  $M_2$  are the molar masses of the first and second components, respectively. The standard uncertainty in the mole fraction was calculated to be  $u(x) = 2 \times 10^{-6}$  using the following:

$$u^2(x) = [(\partial x / \partial m_1)u(m)]^2 + [(\partial x / \partial m_2)u(m)]^2 + [(\partial x / \partial m_3)u(m)]^2 \quad (2)$$

where  $u(m) = 2 \times 10^{-4}$  g is the uncertainty of the balance.

### 2.3. Volumetric data acquisition: experimental setup and procedure

The apparatus and the experimental procedure used to measure densities were previously described [8]. In this setup,  $T$  ranges from (263 to 473) K  $\pm$  0.006 K and  $p$  ranges between atmospheric pressure and 70 MPa with 0.025% FS precision. The main component is an Anton Paar DMA HPM vibrating-tube densimeter connected to an MPDS V3 evaluation unit.

### 3. Calculation method of thermodynamic properties up to high pressures

Various methods have been proposed in the literature to obtain other thermodynamic properties from the speed of sound [51], thus exploiting the high precision of its experimental determination. These methods use experimental values of  $c$  obtained at high pressures and several temperatures and  $\rho$  and  $c_p$  both at a reference pressure  $p^\#$  and as a function of temperature. From these data, calculated values of  $\rho$ , the isobaric thermal expansivity,  $\alpha_p$ , the isothermal compressibility,  $\kappa_T$ , and  $c_p$  are obtained as functions of pressure and temperature. In liquid systems  $p^\#$  is equal to atmospheric pressure [7,41–45,52,53]. The method we used is based on these studies, except that  $p^\#$  must be above atmospheric pressure to ensure that the fluid is in a dense phase along all working pressure and temperature ranges; thus,  $p^\#$  depends on the studied system. Moreover, at the chosen  $p^\#$  value, the experimental density  $\rho^\#$  obtained at  $p^\#$  must correlate well with  $T$ . In this method, the input thermodynamic properties are correlated using the following equations:

$$(p - p^\#) / \text{MPa} = \sum_{i=1}^3 \sum_{j=0}^2 a_{ij} \{ (c - c^\#) / (\text{m s}^{-1}) \}^i (T/K)^{-j} \quad (3)$$

$$c^\# / (\text{m s}^{-1}) = \sum_{j=0}^2 b_j (T/K)^j \quad (4)$$

$$c_p^\# / (\text{J kg}^{-1} \text{K}^{-1}) = \sum_{j=0}^3 c_j (T/K)^j \quad (5)$$

$$\rho^\# / (\text{kg m}^{-3}) = \sum_{j=0}^3 d_j (T/K)^j \quad (6)$$

The calculated thermodynamic properties of the system are obtained for a given composition up to high pressures by numerical integration of the following system of partial differential equations:

$$\left. \begin{aligned} c^{-2} &= (\partial \rho / \partial p)_T - (T / \rho^2 c_p) (\partial \rho / \partial T)_p^2 \\ (\partial c_p / \partial p)_T &= -(T / \rho^3) [2(\partial \rho / \partial T)_p^2 - \rho (\partial^2 \rho / \partial T^2)_p] \end{aligned} \right\} \quad (7)$$

The solution to the system (7) is obtained using the initial conditions  $\rho^\#(T)$  and  $c_p^\#(T)$  and a simple predictor–corrector algorithm [43] with step lengths  $\Delta p = 0.1$  MPa and  $\Delta T = 5$  K. The values of  $\rho^\#(T)$  were determined experimentally, whereas  $c_p^\#(T)$  values were calculated with the GERG EoS [48,49] using REFPROP 9.0 [54]. The values of  $\delta_V$  [55–57] and  $\mu_{JT}$  were calculated up to high pressures using the preceding and the following equations:

$$\delta_V^2 = \left( \frac{\partial U}{\partial V} \right)_T = T \left( \frac{\partial p}{\partial T} \right)_V - p = T \frac{\alpha_p}{\kappa_T} - p \quad (8)$$

$$\mu_{JT} = \left( \frac{\partial T}{\partial p} \right)_H = -\frac{1}{c_p} \left[ T \left( \frac{\partial p / \partial T \right)_V + V \right] = \frac{(T\alpha_p - 1)}{\rho c_p} \quad (9)$$

### 4. Equations of state

In this work, we compared both our experimental values ( $c$ ,  $\rho$ ), and the calculated values explained previously ( $\rho$ ,  $c_p$ ,  $\delta_V$ ,  $\mu_{JT}$ ) with data obtained from the PC-SAFT and the GERG EoS using VLXE [58] and REFPROP 9.0 [54] software, respectively.

#### 4.1. PC-SAFT EoS

The PC-SAFT EoS [46,47] describes the Helmholtz dimensionless energy,  $\tilde{a}$ , as the sum of several contributions: ideal gas ( $id$ ), hard chain ( $hc$ ), dispersive attraction ( $dis$ ), association ( $assoc$ ) and multipolar interactions (QQ: quadrupole–quadrupole, DD: dipole–dipole, QD: quadrupole–dipole).

$$\tilde{a} = \tilde{a}^{id} + \tilde{a}^{hc} + \tilde{a}^{dis} + \tilde{a}^{assoc} + (\tilde{a}^{QQ} + \tilde{a}^{DD} + \tilde{a}^{QD}) \quad (10)$$

In this model, three geometrical parameters are needed to describe the non-associated and non-polar pure components: the segment number,  $m$ ; the segment diameter,  $\sigma$ ; and the segment energy parameter,  $\varepsilon$ . Generally, these parameters are calculated from VLE and density data; however, in such cases the critical region is not correctly represented. An alternative is to recalculate the parameters from the pure compounds' critical temperatures and pressures [17].

The mixing parameters  $\sigma_{ij}$  and  $\varepsilon_{ij}$  are obtained from the Berthelot–Lorentz rules, which include an adjustable binary interaction parameter,  $k_{ij}$ :

$$\sigma_{ij} = \frac{1}{2}(\sigma_i + \sigma_j) \quad (11)$$

$$\varepsilon_{ij} = \sqrt{\varepsilon_i \varepsilon_j} (1 - k_{ij}) \quad (12)$$

where the subscripts  $i$  and  $j$  refer to each of the compounds present in the mixture.

When pure compounds exhibit association, two additional parameters are required: the association volume,  $\kappa^{A_i B_i}$ , and the association energy,  $\varepsilon^{A_i B_i}$ . These parameters can be obtained from experimental hydrogen-bonding enthalpies and entropies of the pure compounds or from molecular simulations. Moreover, an association scheme must be defined.

For mixtures of such compounds, the cross-association parameters,  $\kappa^{A_i B_j}$  and  $\varepsilon^{A_i B_j}$ , can be calculated using the following combination rules:

$$\kappa^{A_i B_j} = \sqrt{\kappa^{A_i B_i} \cdot \kappa^{A_j B_j}} \quad (13)$$



$$\varepsilon^{A_i B_j} = \frac{1}{2} (\varepsilon^{A_i B_i} + \varepsilon^{A_j B_j}) \quad (14)$$

The interactions present in the mixtures between a self-associated compound and another non-self-associated compound, which has either proton donor sites or proton acceptor sites (e.g., CO<sub>2</sub>), were named *induced association* by Kleiner and Sadowski [59]. In this case, they suggested a simple approach: the association energy parameter,  $\varepsilon^{A_i B_i}$ , of the non-self-associating compound is zero, and the association volume parameter,  $\kappa^{A_i B_i}$ , of this component is assumed to be equal to the value of the associating component in the mixture:

$$\kappa^{A_i B_j} = \kappa^{assoc.comp}, \quad \varepsilon^{A_i B_j} = \frac{\varepsilon^{assoc.comp}}{2} \quad (15)$$

A detailed explanation of this model applied to the (CO<sub>2</sub> + CH<sub>3</sub>OH) system is given in a previous work [17], where we studied the VLE and the critical region of this system. For this study, the geometrical parameters of the pure compounds were recalculated from their critical points, and a temperature-dependent binary interaction parameter,  $k_{ij}(T)$ , was introduced. For methanol, we used a 2B association scheme (i.e., two association sites: a one-electron donor and a one-electron acceptor). Because of the presence of specific interactions between the carbon atom of CO<sub>2</sub> and the oxygen atom of alcohol and CO<sub>2</sub>-alcohol hydrogen bonding, we treated this system as *induced association*. We then used  $\varepsilon^{A_i B_i} = 0$  and  $\kappa^{A_i B_i} = \kappa^{methanol}$  and a 2C association scheme (i.e., two negative sites that are active only when mixed with a molecule with at least one positive or neutral site) for CO<sub>2</sub>. Multipole interactions were not considered. This procedure is also that used in the present study.

Neither the PC-SAFT EoS nor cubic EoSs adequately predict density at moderate and high pressures. To enhance the precision in the density calculation, some authors have recalculated the geometrical parameters by introducing the density in the objective function and even varying it with pressure [60,61]. Similar to our earlier work [8], we chose to add the volume translation,  $\Delta v_c$ , for each pure component. We used a constant  $\Delta v_c$  value for all  $T$  to avoid unphysical results [62]. Because  $\Delta v_c$  depends on the value of the molar volume of the component,  $v$ , we here used a  $\Delta v_c$  value for CO<sub>2</sub> that differs from that used in previous works [8] because we extended the pressure range to 195.0 MPa.

In summary, in applying the PC-SAFT EoS to the (CO<sub>2</sub> + CH<sub>3</sub>OH) system, we used the same procedure as in our previous work [17] except that we added  $\Delta v_c$  to accurately predict the density. Thus, we used a minimum number of parameters (Table S1) to model the investigated thermodynamic properties (vapor-liquid equilibrium, critical locus, speed of sound and density).

#### 4.2. The GERG EoS

The GERG EoS [48,49] is based on a multi-fluid approximation where the dimensionless Helmholtz energy,  $\tilde{a}$ , is expressed as the sum of two contributions: an ideal-gas mixture (*id*) and a residual component (*res*):

$$\tilde{a} = \tilde{a}^{id} + \tilde{a}^{res} = \sum_{i=1}^N x_i [\tilde{a}^{id} + \ln x_i] + \sum_{i=1}^N x_i \tilde{a}^{res} + \Delta \tilde{a}^{res} \quad (16)$$

where the subscript  $i$  indicates the pure compound and  $\Delta \tilde{a}^{res}$  is the departure function. Initially, this EoS was developed as a reference EoS for natural gas mixtures, and it generally provides better results than other EoSs for systems whose components are implemented in the equation.

Although methanol is not one of the 21 compounds included in the Kunz and Wagner article [49], it has been implemented in the REFPROP 9.0 software; thus, we were able to use the equation to calculate the thermodynamic properties of the system under

investigation in the present work. The calculations are based in the reference EoS for CO<sub>2</sub> [63] and methanol [64] together with the GERG EoS mixture model. The predicted values are slightly more accurate than those from GERG EoS as published because the pure-component EoSs are more elaborate.

## 5. Results

### 5.1. Experimental results obtained using the newly implemented apparatus to measure the speed of sound in mixtures

The system (CO<sub>2</sub> + CH<sub>3</sub>OH) was studied to develop the experimental procedure for mixtures containing sufficiently dense compressed gases and to determine the uncertainty of the speed of sound measurements in those gases. The chosen compositions were  $x_{CO_2} = (0.7534, 0.8502, 0.9250 \text{ and } 0.9803)$  at nominal temperatures of 263.15 K, 298.15 K and 323.15 K and pressures from 6.00 MPa to 190.04 MPa. The  $p$ - $c$ - $T$  values used in this section are listed in Table S2.

The overall standard uncertainty of the experimental  $c$  measurements,  $u(c)$ , was calculated from the following equation [65]:

$$u^2(c) = \left[ (\partial c / \partial T)_{p,x} u(T) \right]^2 + \left[ (\partial c / \partial p)_{T,x} u(p) \right]^2 + \left[ (\partial c / \partial x)_{T,p} u(x) \right]^2 + (u^*(c))^2 \quad (17)$$

where  $u(T)$ ,  $u(p)$ , and  $u(x)$  are given in Section 2.2, and  $(\partial c / \partial T)_{p,x}$  and  $(\partial c / \partial p)_{T,x}$  were obtained from Eqs. (3) and (4). Correlated  $c$ - $x$  data for the four mixtures allowed us to evaluate  $(\partial c / \partial x)_{T,p}$ .

To determine the standard repeatability uncertainty,  $u^*(c)$ , two mixtures with  $x_{CO_2} = 0.9250$  were prepared. For each one, two isotherms were determined at each of the three temperatures (Table S2). The deviations between the  $c$  values of each isotherm for both mixtures are represented in Fig. 1. The value determined for  $u^*(c)$  was  $5.3 \times 10^{-4} \cdot c$ , and the overall standard uncertainty of  $c$  was  $u(c) = 5.9 \times 10^{-4} \cdot c$ . The last value lies within the range of standard uncertainties ( $3 \times 10^{-4} \cdot c$  to  $10 \times 10^{-4} \cdot c$ ) obtained by other authors using similar apparatus for liquid mixtures and binary mixtures of compressed gases [43,65,66].

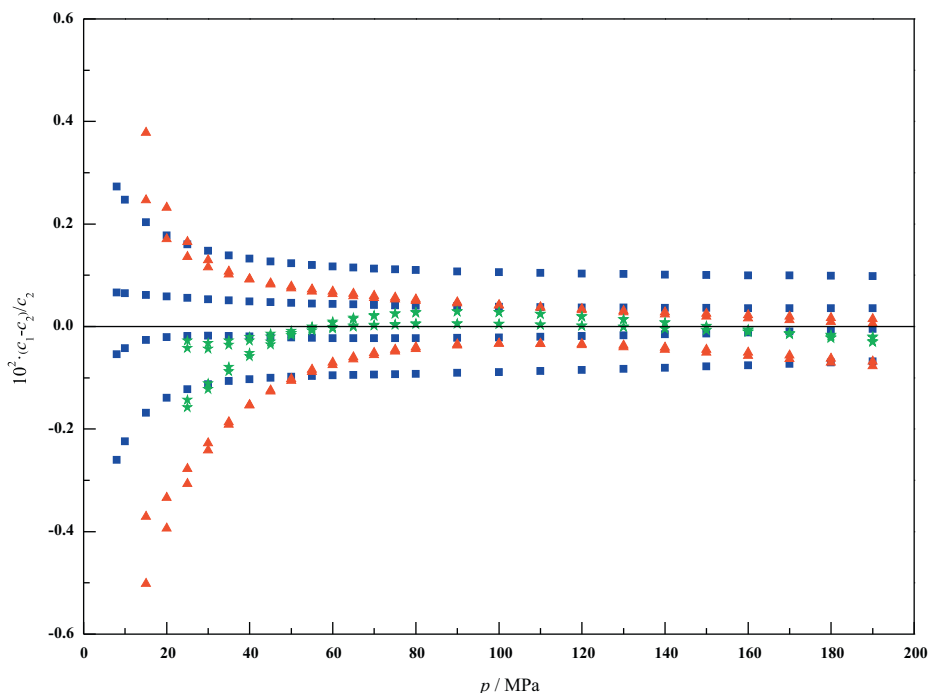
### 5.2. Experimental results for the mixture (CO<sub>2</sub> + CH<sub>3</sub>OH) ( $x_{CO_2} = 0.9700$ )

#### 5.2.1. Speed of sound

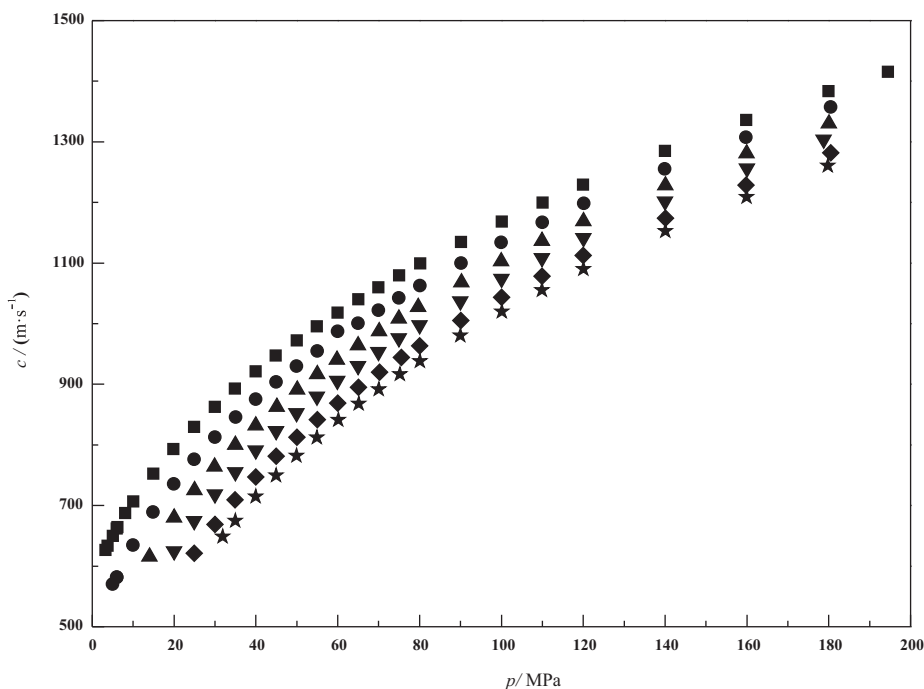
Experimental values  $p$ - $c$ - $T$  were measured along six isotherms at nominal temperatures = (263.15, 273.15, 283.15, 293.15, 304.21 and 313.15) K and at pressures from 3.28 MPa to 194.49 MPa (Fig. 2, Table S3). The standard uncertainty was  $u(c) = 5.9 \times 10^{-4} \cdot c$ , as previously indicated. The speed of sound increases as pressure increases and as temperature decreases. No values were found in the literature for this system.

#### 5.2.2. Density

The density was measured at the same nominal temperatures as the speed of sound and the pressure ranged from 4.00 MPa to 20.00 MPa. The experimentally determined density values of the six isotherms correspond to dense phase of the mixture. The isotherms at temperatures from 263.15 K to 304.21 K are subcritical and that at 313.15 K is supercritical. The standard uncertainty in the experimental determination of the density was  $u(\rho) = 0.4 \text{ kg m}^{-3}$ , which was obtained following the procedure described in the Supplementary material (S.M.) (pp S11). Similar to the speed of sound, values of  $\rho$  in the liquid phase of this mixture also increase with increasing pressure and with decreasing temperature (Fig. 3, Table S4).



**Fig. 1.** Deviations between the  $c$  values in two mixtures (1, 2)  $\text{CO}_2 + \text{CH}_3\text{OH}$  with  $x_{\text{CO}_2} = 0.9250$ , at three temperatures,  $T$ , and versus pressure,  $p$ . Each mixture was measured twice at each temperature. ■,  $T = 263.15$  K; ▲,  $T = 298.15$  K; and ★,  $T = 323.15$  K.

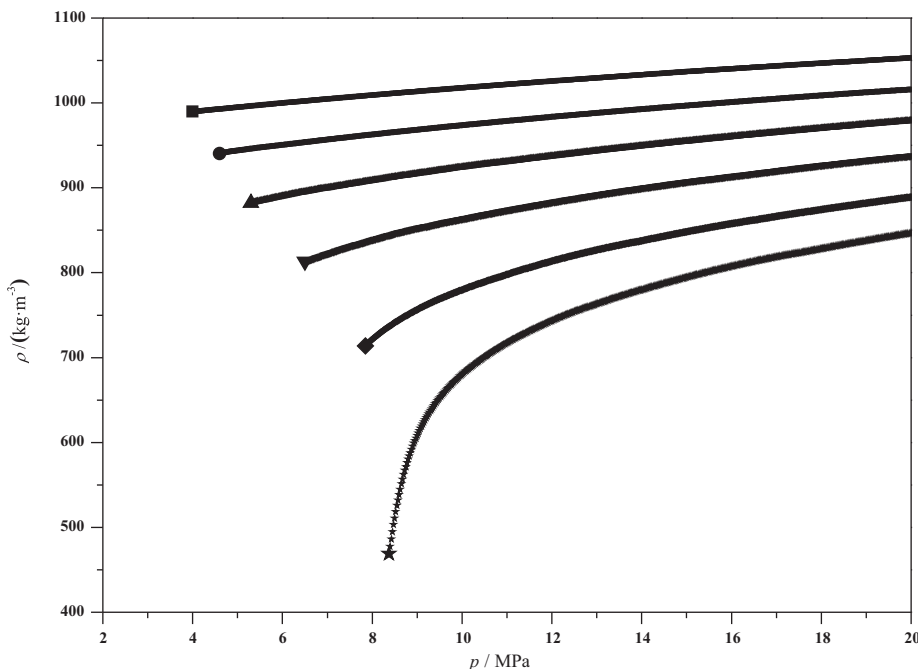


**Fig. 2.** Experimental speeds of sound,  $c$ , versus pressure,  $p$ , for  $\text{CO}_2 + \text{CH}_3\text{OH}$  with  $x_{\text{CO}_2} = 0.9700$  at several temperatures: ■,  $T = 263.15$  K; ●,  $T = 273.15$  K; ▲,  $T = 283.15$  K; ▼,  $T = 293.15$  K; ◆,  $T = 304.21$  K; ★,  $T = 313.15$  K.

Despite the abundance of density data in the literature, we could quantitatively compare our values only with those of Berger and Deye ( $x_{\text{CO}_2} = 0.9777$  at 313.15 K) [20] and Cao et al. ( $x_{\text{CO}_2} = 0.9657\text{--}0.9760$  at 313.15 K) [32], where the deviations  $\text{MRD}_\rho = 1.30\%$  and  $5.52\%$ , respectively. Our results are consistent with the remainder of the literature data at  $T \leq 313$  K and at  $x_{\text{CO}_2} > 0.75$  [19–21,32,34].

### 5.3. Results from the thermodynamic property calculation method for the mixture ( $\text{CO}_2 + \text{CH}_3\text{OH}$ ) ( $x_{\text{CO}_2} = 0.9700$ ) at high pressures

From our experimental  $p$ – $c$ – $T$  and our calculated  $c_p^\#$ – $T$  values (GERG EoS), we obtained  $\rho$ ,  $c_p$ ,  $\delta_V$  and  $\mu_{JT}$  for temperatures from 263.15 K to 313.15 K and for pressures up to 195.0 MPa using the aforementioned calculation method



**Fig. 3.** Experimental densities,  $\rho$ , versus pressure,  $p$ , for  $\text{CO}_2 + \text{CH}_3\text{OH}$  with  $x_{\text{CO}_2} = 0.9700$  at several temperatures:  $\blacksquare$ ,  $T = 263.15$  K;  $\bullet$ ,  $T = 273.15$  K;  $\blacktriangle$ ,  $T = 283.15$  K;  $\blacktriangledown$ ,  $T = 293.15$  K;  $\blacklozenge$ ,  $T = 304.21$  K;  $\star$ ,  $T = 313.15$  K.

(Table S5 and Fig. 4a–d). Eqs. (3)–(6) of this method were applied with  $p^\# = 14.0$  MPa and with the values of the parameters  $a_{ij}$ ,  $b_j$ ,  $c_j$  and  $d_j$  given in Table 2.

### 5.3.1. Density

Because we have experimental values for  $\rho$  for pressures up to 20.00 MPa and calculated values starting from 14.0 MPa, we compared the values in the overlapping range from 14.0 MPa to 20.0 MPa. The experimental and calculated values agreed well with an  $\text{MRD}_\rho = 0.075\%$ . We compared our calculated density values with the experimental values of Berger and Deye [20]; the deviation is  $\text{MRD}_\rho = 0.35\%$ . Our results are consistent with the experimental results of Maiwald et al. [34].

### 5.3.2. Isobaric specific heat capacity

The calculated values of this property vary between  $2734.6 \text{ J K}^{-1} \text{ kg}^{-1}$  (14.0 MPa, 313.15 K) and  $1551.6 \text{ J K}^{-1} \text{ kg}^{-1}$  (195.0 MPa, 313.15 K). The variation of  $c_p$  with pressure diminishes gradually as temperature decreases, showing a crossing region at approximately  $1865 \text{ J K}^{-1} \text{ kg}^{-1}$  and 35 MPa. No  $c_p$  values for the mixture studied were found in the literature.

### 5.3.3. Volume-dependent solubility parameter

The calculated values for the  $\delta_v$  increase as pressure increases and temperature decreases. We found values of the solubility parameter,  $\delta$ , in the literature for  $T \geq 313.15$  K [14,38–40], which cannot be compared with our  $\delta_v$  values because of the different effects included and the temperature or composition.

### 5.3.4. Joule–Thomson coefficient

The evolution of  $\mu_{JT}$  values with pressure and temperature is similar to that of  $c_p$ . The greatest variation with pressure is shown for the supercritical isotherm ( $0.82597 \text{ K MPa}^{-1}$  at 14.0 MPa and  $-0.33179 \text{ K MPa}^{-1}$  at 195.0 MPa) and the lowest variation corresponds to 263.15 K, which causes a crossing of all isotherms in the vicinity of  $-0.25 \text{ K MPa}^{-1}$  and 100 MPa. The Joule–Thomson

coefficient changes its sign for the five upper isotherms in the pressure range studied. No  $\mu_{JT}$  values were found in the literature.

## 6. Discussion

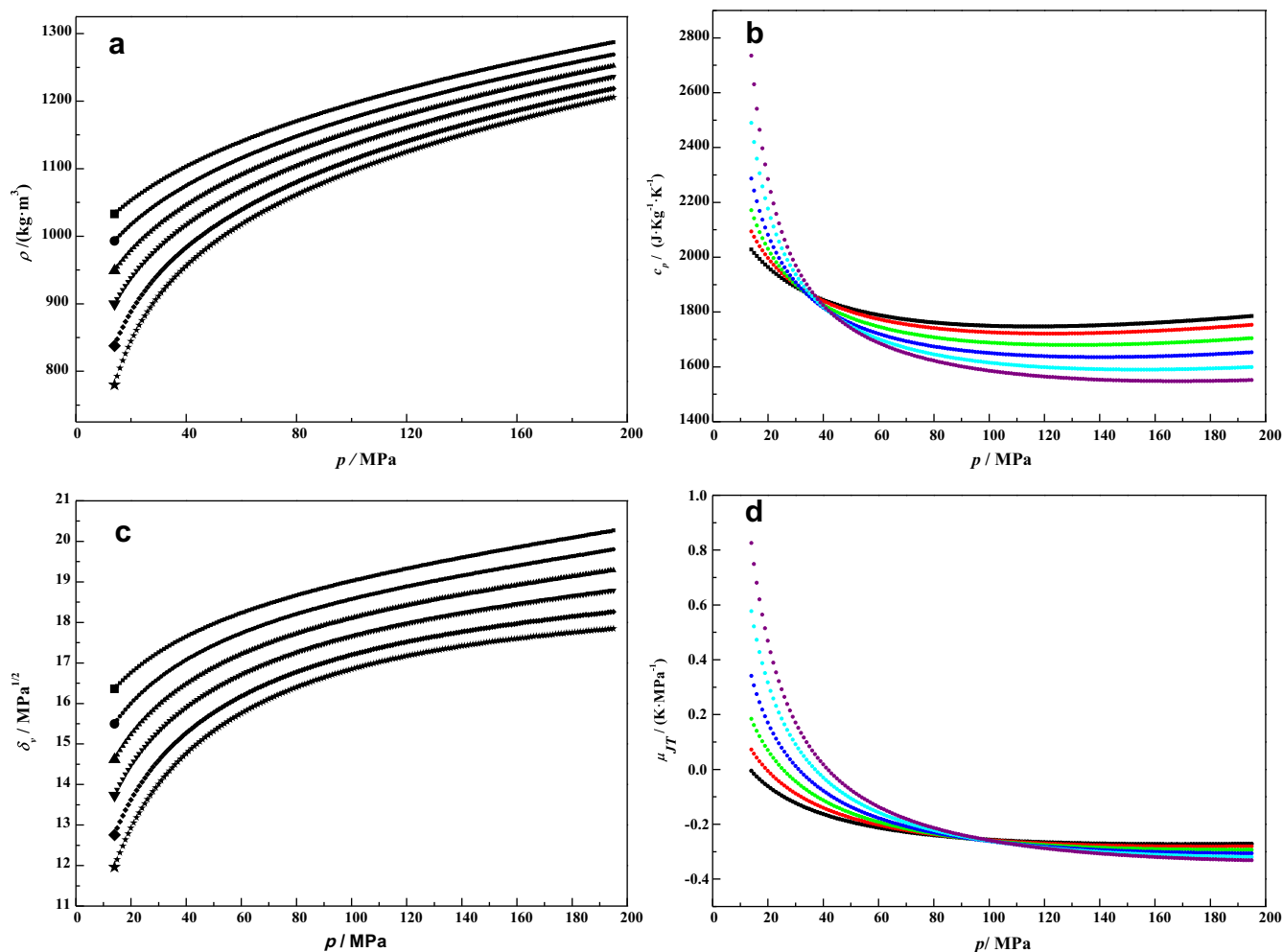
The repeatability and overall standard uncertainty results obtained in this work, together with the agreement with the data from the literature, allow us to use our experimental  $c$  and  $\rho$  values to evaluate whether the PC-SAFT and GERG EoSs properly predict the studied thermodynamic behaviour for  $(\text{CO}_2 + \text{CH}_3\text{OH})$ . If the two EoSs are successful, we will use both to validate the method for calculating  $\rho$ ,  $\delta_v$ ,  $c_p$  and  $\mu_{JT}$  up to 195.0 MPa.

### 6.1. Experimental results for $(\text{CO}_2 + \text{CH}_3\text{OH})$ ( $x_{\text{CO}_2} = 0.9700$ )

#### 6.1.1. Speed of sound ( $p \leq 194.49$ MPa; $263.16 \text{ K} \leq T \leq 313.15 \text{ K}$ )

We observed that the PC-SAFT EoS tends to underestimate the speed of sound when we compared the experimental and EoS results (Fig. S1); we also observed that the divergence increases with decreasing temperature. The calculated value of the average PC-SAFT EoS deviation for all isotherms is  $\overline{\text{MRD}}_c = 2.77\%$  (Table S6). The GERG EoS values of  $c$  are always greater than the experimental values, with the largest deviations at low pressures (Fig. S1). The average value of the GERG EoS deviations for all isotherms is slightly lower than that from the PC-SAFT EoS,  $\overline{\text{MRD}}_c = 2.65\%$  (Table S6).

To calculate the overall standard uncertainty in the speed of sound,  $u(c)$ , experimental values of  $c$  for four mixtures of  $(\text{CO}_2 + \text{CH}_3\text{OH})$  ( $0.7534 \leq x_{\text{CO}_2} \leq 0.9803$ ) were determined. All of them were modelled to investigate possible trends with respect to composition. The PC-SAFT EoS deviations are similar for all mixtures. However, the GERG EoS provides better results than the PC-SAFT EoS for the two  $\text{CO}_2$  – richest mixtures and significantly higher deviations with increasing values of  $x_{\text{CH}_3\text{OH}}$ . Thus, the GERG EoS



**Fig. 4.** (a) Calculated densities,  $\rho$ ; (b) calculated isobaric specific heat capacities,  $c_p$ ; (c) calculated volume-dependent solubility parameters,  $\delta_v$ ; (d) calculated Joule-Thomson coefficients,  $\mu_{JT}$ , versus pressure,  $p$ , for the mixture  $\text{CO}_2 + \text{CH}_3\text{OH}$  with  $x_{\text{CO}_2} = 0.9700$  at several temperatures; (a and c)  $\blacksquare$ ,  $T = 263.15$  K;  $\bullet$ ,  $T = 273.15$  K;  $\blacktriangle$ ,  $T = 283.15$  K;  $\blacktriangledown$ ,  $T = 293.15$  K;  $\blacklozenge$ ,  $T = 304.21$  K;  $\star$ ,  $T = 313.15$  K; (b and d)  $\bullet$ ,  $T = 263.15$  K;  $\color{red}\bullet$ ,  $T = 273.15$  K;  $\color{green}\bullet$ ,  $T = 283.15$  K;  $\color{blue}\bullet$ ,  $T = 293.15$  K;  $\color{cyan}\bullet$ ,  $T = 304.21$  K;  $\color{purple}\bullet$ ,  $T = 313.15$  K.

$\overline{MRD}_c$  is 1.88% for  $x_{\text{CO}_2} = 0.9803$  and 14.1% for  $x_{\text{CO}_2} = 0.7534$  (Table S7).

### 6.1.2. Density ( $p \leq 20.00$ MPa; $263.15$ K $\leq T \leq 313.15$ K)

Deviations in density values increase with increasing temperature and decreasing pressure for both EoSs (Fig. S2). The PC-SAFT EoS predicts that the density values will be lower than the experimental values for subcritical isotherms. For this EoS, the largest deviations are observed at  $T = 313.15$  K, near the critical point of the mixture ( $T_c \cong 310$  K [17]) (Fig. S2). The mean value of all PC-SAFT EoS deviations is  $\overline{MRD}_\rho = 3.96\%$  (Table S6). The GERG EoS overestimates  $\rho$  with a significantly lower  $\overline{MRD}_\rho = 0.58\%$ , although its deviation is more than double that of the PC-SAFT EoS at the supercritical temperature,  $(MRD_\rho)_{\text{max}} = 23\%$ . Density values from the literature [18–37] show similar or higher deviations with PC-SAFT EoS predictions than our experimental values and greater differences with GERG EoSs than our values (Table S8).

On the basis of the deviations between the experimental values and those calculated by each EoS for the two properties, we conclude that both equations are valid to represent the behaviour of this system under most of the studied conditions. However, we observed exceptions, such as the evaluation of the density near the critical point of the mixture, where the deviations were significant for both EoSs, and the GERG EoS's prediction for the speed of sound within mixtures with  $x_{\text{CO}_2} < 0.97$ .

The experimental results are a useful contribution to the body of scientific knowledge because no  $c$  values have been reported and because volumetric information at  $T \leq 313$  K and  $x_{\text{CO}_2} > 0.75$  is scarce. Accurate values for these properties are needed to evaluate several parameters related to transport, injection and storage in CCS technology and also for other applications. In addition, these values will allow the research community to develop and improve EoSs in the future.

## 6.2. Calculated results for ( $\text{CO}_2 + \text{CH}_3\text{OH}$ ) ( $x_{\text{CO}_2} = 0.9700$ ) up to 195.0 MPa

Given the satisfactory results obtained in the previous section, we will use both EoSs to discuss our results calculated from the experimental values at pressures up to 195.0 MPa. The calculated  $\rho$ ,  $c_p$ ,  $\delta_v$  and  $\mu_{JT}$  values are compared to those obtained from the PC-SAFT and GERG EoSs (Figs. S3–S6) at temperatures from 263.15 K to 313.15 K and at pressures from 14.0 MPa to 195.0 MPa. The deviations thus obtained are expressed as  $\overline{MRD}_x(\%)$  or AAD in Table S9.

### 6.2.1. Density

Fig. S3 shows the deviations between the calculated  $\rho$  values and those from both EoSs. Our obtained values are greater than the values obtained using the PC-SAFT EoS at pressures below

**Table 2**

Parameters in Eq. (3)–(6) for the correlation for the speed of sound, isobaric heat capacity, and density of CO<sub>2</sub> + CH<sub>3</sub>OH with  $x_{\text{CO}_2} = 0.9700$  and  $\overline{MRD}$  (%) values.

Parameters	Eq. (3)
$a_{10}$	$1.803588 \cdot 10^0$
$a_{11}$	$-1.057660 \cdot 10^3$
$a_{12}$	$1.613456 \cdot 10^5$
$a_{20}$	$-2.893926 \cdot 10^{-3}$
$a_{21}$	$1.590804 \cdot 10^0$
$a_{22}$	$-2.057073 \cdot 10^2$
$a_{30}$	$2.153084 \cdot 10^{-6}$
$a_{31}$	$-1.154812 \cdot 10^{-3}$
$a_{32}$	$1.601533 \cdot 10^{-1}$
$\overline{MRD}$ (%)	0.08
Parameters	Eq. (4)
$b_0$	$4.551011383 \cdot 10^3$
$b_1$	$-2.1725446 \cdot 10^1$
$b_2$	$2.7618 \cdot 10^{-3}$
$\overline{MRD}$ (%)	0.27
Parameters	Eq. (5)
$c_0$	$-8.2772910000 \cdot 10^4$
$c_1$	$9.35309155 \cdot 10^2$
$c_2$	$-3.460573 \cdot 10^0$
$c_3$	$4.297499 \cdot 10^{-3}$
$\overline{MRD}$ (%)	0.11
Parameters	Eq. (6)
$d_0$	$5.897805216 \cdot 10^3$
$d_1$	$-5.0584614 \cdot 10^1$
$d_2$	$0.188454 \cdot 10^0$
$d_3$	$-2.526272E \cdot 10^{-4}$
$\overline{MRD}$ (%)	0.02

$\overline{MRD}$  (%) =  $\frac{10^2}{N} \sum_{i=1}^N \left| \frac{x_i - x_{fit}}{x_i} \right|$   
 $x_i$ : experimental datum;  $x_{fit}$ : value obtained for that property at the same state point from the corresponding correlating equation;  $N$ : number of points.

(40–60) MPa, whereas they are lower at higher pressures; the average deviations obtained for each isotherm are nearly equal, and  $\overline{MRD}_\rho = 1.90\%$ . In relation to the GERG EoS, we obtain deviations no higher than 1%, with an average value  $\overline{MRD}_\rho = 0.46\%$ , where our calculated values are usually higher than the predicted values.

### 6.2.2. Isobaric specific heat capacity

A comparison of the calculated values with those from the two EoSs (Fig. S4) shows that calculated values are higher than the values predicted by the PC-SAFT EoS. The deviations are significant and generally increase with increasing pressure, with an average value of  $\overline{MRD}_{c_p} = 10.3\%$ . Deviations of the values calculated using the GERG EoS are much lower than those calculated using the PC-SAFT EoS, with an average value of  $\overline{MRD}_{c_p} = 2.47\%$ . The calculated crossing region for this property ( $c_p \cong 1865 \text{ J K}^{-1} \text{ kg}^{-1}$  and  $p \cong 35 \text{ MPa}$ ) agrees better with predictions from the GERG EoS ( $c_p \cong 1780 \text{ J K}^{-1} \text{ kg}^{-1}$  and  $p \cong 55 \text{ MPa}$ ) than with predictions from the PC-SAFT EoS ( $c_p \cong 1460 \text{ J K}^{-1} \text{ kg}^{-1}$  and  $p \cong 155 \text{ MPa}$ ).

### 6.2.3. Volume-dependent solubility parameter

In Fig. 5,  $\delta_V$  values are represented as a function of  $\rho$  for pure CO<sub>2</sub> [50], for the (CO<sub>2</sub> + CH<sub>3</sub>OH) mixture studied in this work and for six (CO<sub>2</sub> + CO), (CO<sub>2</sub> + CH<sub>4</sub>), (CO<sub>2</sub> + H<sub>2</sub>), (CO<sub>2</sub> + CO + H<sub>2</sub>), mixtures from the literature [8]. The graph shows a good  $\delta_V$ – $\rho$  correlation at densities less than  $\cong 1050 \text{ kg m}^{-3}$ , as shown in a previous study [8]. This result indicates that within this density range, different systems at various  $T$  or  $p$  conditions, but with the same density, will have the same  $\delta_V$ . For  $\rho > 1050 \text{ kg m}^{-3}$ , deviations

between the  $\delta_V$  values for the (CO<sub>2</sub> + CH<sub>3</sub>OH) mixture and those for pure CO<sub>2</sub> depend on  $T$ ; however, these deviations are not greater than those observed for other systems in other regions of the graph.

Our  $\delta_V$  values are lower than the values obtained from the PC-SAFT EoS within the full range of pressures, with larger deviations at both higher pressures and higher temperatures, with an  $\overline{MRD}_{\delta_V} = 3.28\%$ . The GERG deviations are smaller than those obtained from the PC-SAFT EoS, and their average value is  $\overline{MRD}_{\delta_V} = 1.60\%$ . Comparisons with both EoSs are shown in Fig. S5.

### 6.2.4. Joule–Thomson coefficient

Because the numerical values of this property were so small, deviations were expressed as AADs. The PC-SAFT EoS deviations are much larger than those from the GERG EoS, as shown in Fig. S6, which is reflected in the average values of  $\overline{AAD}_{\mu_{JT}} = 0.056 \text{ K MPa}^{-1}$  from the PC-SAFT EoS and  $\overline{AAD}_{\mu_{JT}} = 0.013 \text{ K MPa}^{-1}$  from the GERG EoS. The crossing region obtained from the calculation method ( $\mu_{JT} \cong -0.25 \text{ K MPa}^{-1}$  and  $p \cong 100 \text{ MPa}$ ) differs more from that predicted by the PC-SAFT EoS ( $\mu_{JT} \cong -0.43 \text{ K MPa}^{-1}$  and  $p \cong 220 \text{ MPa}$ ) than that from the GERG EoS ( $\mu_{JT} \cong -0.32 \text{ K MPa}^{-1}$  and  $p \cong 180 \text{ MPa}$ ).

We consider the results obtained adequate in the comparison between the calculated values of the four properties  $\rho$ ,  $c_p$ ,  $\delta_V$  and  $\mu_{JT}$  and the data provided by both EoSs, except for  $c_p$  and  $\mu_{JT}$  in relation to the PC-SAFT EoS.

## 7. Conclusions

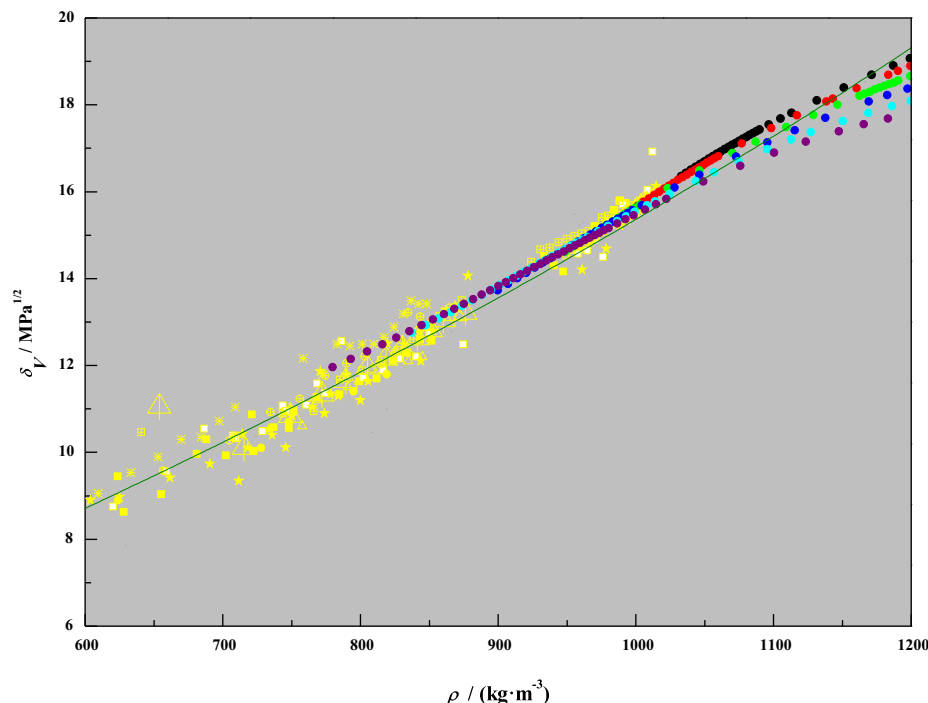
An ultrasonic pulse apparatus and the experimental procedure were adapted to measure the speed of sound in mixtures containing compressed gases, and  $c$  was measured for four (CO<sub>2</sub> + CH<sub>3</sub>OH) mixtures ( $x_{\text{CO}_2} = 0.7534, 0.8502, 0.9250$  and  $0.9803$ ) at nominal temperatures  $T = (263.15, 298.15, \text{ and } 323.15) \text{ K}$  and at pressures up to 190.04 MPa. The overall standard uncertainty of the experimental speed of sound was evaluated for the (CO<sub>2</sub> + CH<sub>3</sub>OH) system, where the contributions of temperature, pressure, composition and repeatability were taken into account. The value obtained,  $u_c = 5.9 \times 10^{-4} \cdot c$ , is within values reported in the literature.

The speed of sound was experimentally determined for the (CO<sub>2</sub> + CH<sub>3</sub>OH) mixture with  $x_{\text{CO}_2} = 0.9700$  at nominal  $T = (263.15, 273.15, 283.15, 293.15, 304.21 \text{ and } 313.15) \text{ K}$  and at pressures from 3.28 MPa to 194.49 MPa. The density of the mixture in the dense phase was measured at the same nominal temperatures, including five subcritical and one supercritical, and at pressures up to 20.00 MPa.

This system was modelled with two different formulation EoSs: PC-SAFT and GERG. From the obtained deviations, we conclude that both equations are valid to represent the studied experimental thermodynamic properties of the system except for in the critical region and, in the case of the GERG EoS, the speed of sound in the mixtures poorest in CO<sub>2</sub>.

Values of  $\rho$ ,  $c_p$ ,  $\delta_V$  and  $\mu_{JT}$  were calculated for the  $T$  range from 263.15 K to 313.15 K and from 14.0 MPa to 195.0 MPa for the (CO<sub>2</sub> + CH<sub>3</sub>OH) mixture with  $x_{\text{CO}_2} = 0.9700$ . For this calculation, we used a method based on numerical integration and previously used for liquid systems by adapting it for compressed gases. The values thus obtained were compared with those obtained from the PC-SAFT and GERG EoSs. The results of this comparison, together with the agreement between our experimental and calculated densities in the overlapping pressure range, validate the calculation method.





**Fig. 5.** Volume-dependent solubility parameter,  $\delta_V$ , versus density,  $\rho$ , for pure  $\text{CO}_2$  [50] (line);  $\text{CO}_2 + \text{CH}_3\text{OH}$  with  $x_{\text{CO}_2} = 0.9700$  at several temperatures: ●,  $T = 263.15 \text{ K}$ ; ●,  $T = 273.15 \text{ K}$ ; ●,  $T = 283.15 \text{ K}$ ; ●,  $T = 293.15 \text{ K}$ ; ●,  $T = 304.21 \text{ K}$ ; ●,  $T = 313.15 \text{ K}$ ;  $\text{CO}_2 + \text{CO}$ ,  $\text{CO}_2 + \text{CH}_4$ ,  $\text{CO}_2 + \text{H}_2$  and  $\text{CO}_2 + \text{CO} + \text{H}_2$  mixtures (yellow) [8]. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Therefore, we have achieved the aim of this work, which was to comprehensively study the thermodynamics of a  $\text{CO}_2$  – rich mixture of ( $\text{CO}_2 + \text{CH}_3\text{OH}$ ) at  $T$  and  $p$  conditions of interest for CCS technology and other applications. The results reported in this paper are a useful contribution to mitigate the lack of information in the literature on the thermodynamic behaviour of such mixtures. Acoustic, volumetric,  $c_p$  and  $\mu_{JT}$  data are important for the calculation of several parameters related to transport, injection and storage in CCS and for supercritical processes. In addition, these data will allow the future improvement, development and validation of new theoretical models for this technology. Neither of the two studied EoSs satisfactorily represents all the properties studied in this work, although the GERG EoS correctly predicts the system behaviour at high pressures.

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## Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.jct.2016.03.026>.

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