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## Half-Cycle-Pulse-Train Induced State Redistribution of Rydberg Atoms

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**Half-cycle-pulse-train induced state redistribution of Rydberg atoms**

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Population transfer between low-lying Rydberg states independent of the initial state is realized using a train of half-cycle pulses with pulse durations much shorter than the classical orbital period. We demonstrate experimentally the population transfer from initial states around  $n = 50$  with 10% of the population de-excited down to  $n < 40$  as well as up to the continuum. This is a demonstration of a state-independent de-excitation technique applicable to the currently produced state distribution of antihydrogen. The measured population transfer matches well to a model of the process for one-dimensional atoms.

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**I. INTRODUCTION**

The control of atoms in Rydberg states is important for many different applications, including the study of antihydrogen, the study of wave packets in Rydberg atoms, and the use of excitation blockades for quantum computing [1–3]. Precise tests of *CPT* using antihydrogen require trapped atoms in the ground state, but currently atoms are produced in a broad range of excited states. An effective means of de-excitation is thus required to ensure atoms reach the ground state and are trapped before annihilation on the trap walls. Stimulated de-excitation using narrow-band lasers is clearly infeasible due to the many thousands of states populated during three-body recombination. Hence, an alternative state-independent technique is required. Efficient de-excitation of antihydrogen atoms compatible with the techniques currently used to produce antihydrogen requires a scheme that meets several requirements. First, it must be capable of simultaneously de-exciting a range of states whose radius varies from  $0.5 \mu\text{m}$  to less than  $100 \text{ nm}$ ; this range is equivalent to states in no magnetic field with principal quantum numbers  $n$  between  $n < 35$  and  $n = 90$  [4]. Second, the current techniques to produce antihydrogen atoms result in a quasistatic production rate over at least several seconds; thus, a de-excitation scheme must not require a specific timing sequence. Finally, atoms with thermal velocities comparable to the  $1.2\text{K}$  production environment reach the walls of the trap enclosure in less than  $250 \mu\text{s}$ , which sets a limit for the required de-excitation rate.

Several groups have proposed schemes using trains of ultrashort unipolar electromagnetic pulses (half-cycle pulses or HCPs) to accomplish this de-excitation. When the length of the pulse is much shorter than the orbital period of the electron,  $\tau_{\text{orbit}} \propto n^3$ , these pulses effectively kick the electron, transferring momentum regardless of the initial state [5]. Depending on the phase of the kick relative to the electron's orbit, this momentum transfer can drive the atomic state either up toward the continuum or down toward the ground state. Hu and Collins solved the applicable time-dependent Schrödinger equation which predicts that a fixed repetition rate train of pulses should result in an oscillating population

distribution in number of HCPs with excursions from the initial state of greater than  $\Delta n = \pm 10$  [6]. Kopyciuk and Parzynski noted that, in a model system based on one-dimensional (1D) atoms, by changing the repetition rate of the HCPs during an experimental sequence, atoms can be driven either up or down in principal quantum by decreasing or increasing the repetition rate, respectively. Their model, however, does not predict the oscillatory phenomenon seen by Hu and Collins [7,8].

Experimentally, HCP trains have been demonstrated to coherently transfer Rydberg atoms between  $n$  states of 350 and 700 [9]. Because the orbital period for these atoms is on the order of tens of nanoseconds, electrical impulse generators are used to generate pulses with temporal widths less than the orbital period. However, this experimental technique cannot be extended to atoms with  $n < 100$  due to the much shorter pulse lengths required when the orbital periods are less than  $100 \text{ ps}$ . Single pulses to atoms in states comparable to those produced for antihydrogen study have been shown to cause population redistribution to nearby  $n$  and  $l$  states, but ionization occurs at high pulse amplitudes instead of inducing larger changes in quantum state [10,11]. These systems use amplified femtosecond lasers with repetition rates limited to less than around  $10 \text{ kHz}$  to produce HCPs; they thus cannot be extended to produce pulse trains to drive large changes within the lifetime of a Rydberg atom. Using adiabatic rapid passage through a series of microwave resonances has also been demonstrated as a technique to drive population transfers, but it requires specific knowledge of the dressed atomic states, which is difficult to determine in strong inhomogeneous magnetic fields such as those used to trap antihydrogen [12,13].

In this paper we report on an experimental demonstration of a technique that meets all of the requirements for efficient de-excitation. A photoconductive switch with  $82 \text{ MHz}$  repetition rate produces a train of primarily unipolar pulses with pulse widths on the order of  $1 \text{ ps}$  and amplitudes greater than  $500 \text{ V/cm}$ , allowing for the manipulation of atoms with  $n > 20$  through impulsive kicks from these pulses. By applying thousands of pulses within the radiative lifetime of an atom ( $\Gamma \sim 100 \mu\text{s}$  for  $n \sim 40$ ), greater than 10% of the initial population in  $n = 52$  can be driven to  $n = 40$ . Because radiative lifetimes scale strongly with  $n$  ( $\Gamma_{\text{rad}} \propto n^5 / \log n$ ), this reduction in  $n$  results in a factor-of-4 reduction in lifetime [14]. The population transfer follows the predictions of the 1D model system used in the theoretical work but, instead of a

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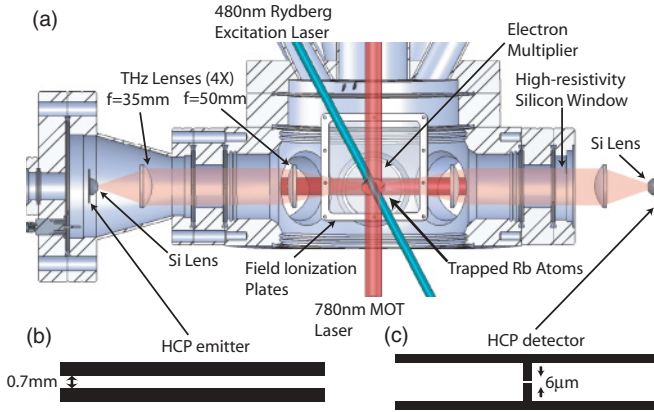


FIG. 1. (Color online) Schematic of the apparatus. Atoms trapped in the center of the magneto-optical trap (MOT) are excited to a Rydberg state, interact with a train of half-cycle pulses (HCPs) generated by the emitter antenna on the left side, and then are detected by field ionization from the field plates surrounding the central trapping region. The emitter and photoconductive detector geometries are shown in (b) and (c), respectively.

coherent transfer from each pulse, the population decoheres after each pulse.

## II. APPARATUS

Figure 1(a) shows the primary apparatus used in this experiment. Approximately  $3 \times 10^8$   $^{85}\text{Rb}$  atoms are trapped in a 4-mm-diam cloud in the center of a dispenser-loaded magneto-optical trap. The combination of the primary cooling laser at 780 nm and a tunable 480-nm optical parametric oscillator (OPO) producing 2-mJ, 10-ns-long pulses with linewidth of  $4 \text{ cm}^{-1}$  excite 1 in  $10^4$  atoms in two steps from the  $5S$  ground state to Rydberg  $nS$  or  $nD$  states. Field plates of 80% transparent stainless steel mesh separated by 2.2 cm can be biased producing an electric field that field ionizes the Rydberg atoms. An electron multiplier detects these ionized electrons. By applying a linear ramped field in time the entire field ionization distribution can be mapped out in a single shot. This field typically ramps from 0 to 700 V/cm in 10  $\mu\text{s}$ .

HCPs are generated within the vacuum system using a photoconductive switch fabricated on a semi-insulating GaAs wafer with microfabrication techniques [15]. SI-GaAs is a slow photoconductive switch with a carrier lifetime of more than 100 ps, a characteristic which is necessary for producing HCPs, which is discussed later. The semiconductor wafers used here are cut along the  $\langle 100 \rangle$  direction and have a resistivity of  $10^7 \Omega \text{ m}$ . Aluminum strip lines with a gap of 700  $\mu\text{m}$  for biasing the switch are directly deposited on GaAs using electron-beam evaporation to a thickness of between 0.5 and 0.8  $\mu\text{m}$ . Figure 1(b) shows the basic geometry. A similar wafer is used as a detector but, instead of a stripline antenna, a dipole antenna with a gap of 6  $\mu\text{m}$  is fabricated on the detector as shown in Fig. 1(c). A femtosecond Ti:sapphire oscillator with a maximum pulse width of 100 fs illuminates the emitter and detectors. This mode-locked laser operates around a center wavelength of 810 nm with a repetition rate of 82 MHz. An average laser power as high as 450 mW focused to a spot size of 50  $\mu\text{m}$  was used to pump the emitter.

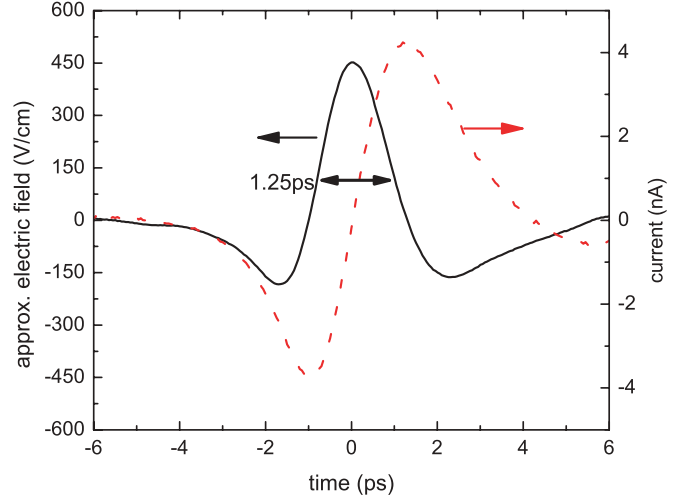


FIG. 2. (Color online) HCP waveform for a biasing electric field of 2 kV/cm. The dashed line shows the measured current from the photoconductive detector while the solid line is the derivative of the current, which is proportional to the radiated electric field.

To compensate for the strongly diverging nature of the emitted HCP radiation, a combination of a 10-mm-diam hemispherical silicon lens located on the back of the emitter wafer along with a pair of plano-convex lenses is used to refocus the pulses at the center of the trapped atom cloud. The two lenses have focal lengths of 35 and 50 mm and are respectively composed of TPX (polymethylpentene) and high-density polyethylene, which are both transparent in the terahertz region. They are placed such that all frequencies are refocused at the center of the trapped atoms. An identical sequence of lenses directs and refocuses the outgoing pulses on the photoconductive detector located outside the vacuum system. A high-resistivity Si window allows the HCPs to exit the UHV system.

Figure 2 shows typical HCPs with a temporal full width at half maximum of approximately 1 ps and a peak field of greater than 500 V/cm produced by our setup. The fast excitation of carriers in the GaAs wafer due to the pump pulse coupled with the strong-bias electric field results in a sudden current surge. Since in the dipole approximation the far-field radiation is proportional to the time derivative of the current, this current surge produces a strong positive pulse while the long carrier lifetime causes a slow decay in the current leading to a long negative tail. After propagation in free space, the strong divergence of the low-frequency components of the pulse as well as the Gouy phase induced by focusing converts this pulse into the symmetric pulse shown in Fig. 2.

The pulses are detected using the inverse technique in which the HCP electric field is used to induce a current within the detector. The measured current density is then given by  $j = e\mu \int_{-\infty}^{\infty} E_{\text{HCP}}(t)n(t)dt$ , where  $e$  is the charge of the carriers,  $\mu$  is the carrier mobility, and  $n(t)$  is the carrier density. For a semiconductor like SI-GaAs with a long carrier lifetime,  $n(t)$  can be approximated by a step function at time  $\tau$ , corresponding to the arrival of the probe pulse, so this equation reduces to  $j(\tau) \propto \int_{\tau}^{\infty} E_{\text{HCP}}(t - \tau)dt$  or equivalently the electric field of the HCP is proportional to the derivative of the measured current. Using the simplifying assumption

that the carrier mobility at terahertz frequencies is the same as that at dc frequencies, and accounting for both the exponential decay in carrier density caused by the approximately 300-ps carrier lifetime of SI-GaAs and the reflection losses at the interface between the detector and free space, the current induced by a known dc biasing field is used to calibrate the detector. This calibration has been checked by comparing this detected signal with an electro-optic detector with a known absolute calibration.

Each experimental run is synchronized relative to a laser pulse from the OPO, which provides the excitation to a given Rydberg state. The trapping quadrupole magnetic field is turned off 3 ms before the pulse, allowing all resulting eddy currents to dissipate prior to the excitation and ensuring minimal interference from the quadrupole field. The photoconductive switch's bias field is switched on  $5 \mu\text{s}$  prior to the pulse, allowing it to stabilize prior to any Rydberg atom excitation. This approach eliminates any effects from lower amplitude pulses being emitted as the field is being raised to the full value. Approximately 30,000 atoms are excited to a Rydberg state at time  $t = 0$ . After a variable time between 0 and  $150 \mu\text{s}$ , the HCP biasing field is turned off with a fall time of 30 ns. The final state distribution is measured by applying a  $10\text{-}\mu\text{s}$ -long ionizing field ramp at a fixed time of  $150 \mu\text{s}$  after the excitation pulse. Fixing the ionization field ramp in time relative to the excitation pulse ensures that no effects due to radiative decay or transitions induced by blackbody radiation are convolved into the measured state distribution because the only change between experimental runs is the length of time the HCPs are applied. Figures 3(e) and 3(f) show the measured normalized distribution for a fixed number of HCPs as the delay between the Rydberg excitation laser pulse and the ionization ramp is varied. At long delay times there is a small decrease in the number of atoms ionized at high fields, as expected, due to these states having reduced lifetimes; but at a delay of  $150 \mu\text{s}$  used for all of our other data, there is a negligible effect on the overall state distribution.

### III. RESULTS AND DISCUSSION

Figure 3(a) shows the normalized state distribution measured as a function of the number of HCPs. Initially all atoms ionize near  $80 \text{ V/cm}$  as set by the excitation wavelength and resulting state. As impulsive kicks are applied to this initial distribution, the population spreads out in a diffusive manner. During this process some atoms are lost due to field ionization by the small static  $1 \text{ V/cm}$  clearing field or from radiative decay to states that are not ionized by the maximum field of  $700 \text{ V/cm}$  applied during the detection ramp. To map between ionizing electric field and the approximate principal quantum number distribution shown in Fig. 3(c), we use the electric field at which the electron is no longer classically bound. In atomic units this field is  $F = \frac{A}{n^4}$ . Here  $A = 1/16$  for adiabatic ionization or  $A = 1/9$  for red-shifted Stark states that diabatically ionize, which we employ for data analysis from now on [16]. Justification for the choice of red-shifted Stark states is shown in Fig. 4. Figure 4(a) shows a field ionization trace after 1600 HCPs have been applied to the population. More than 10 peaks corresponding to discrete atomic states are clearly visible. Figure 4(b) plots these peak positions versus

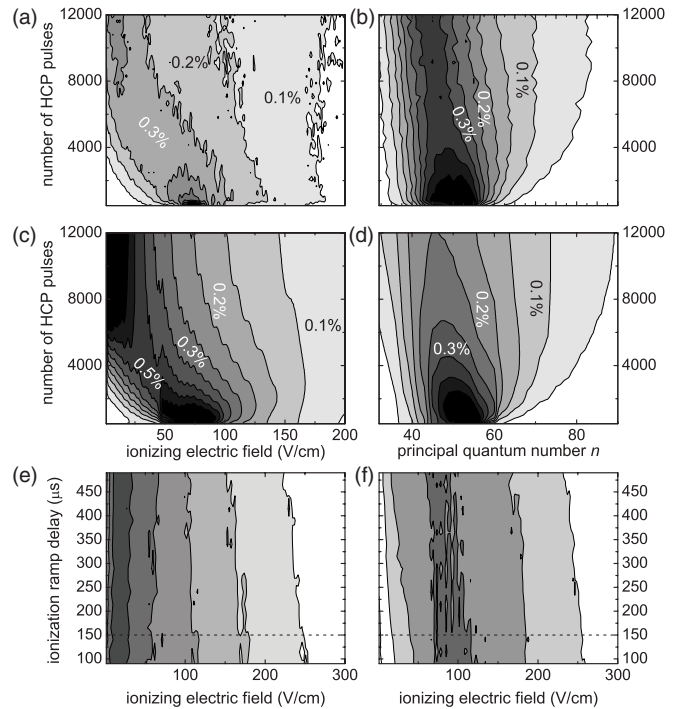


FIG. 3. Left plots: Normalized fraction of the atomic population that ionizes at a specific electric field as a function of the number of applied HCPs. Plot (a) shows experimental data and plot (c) shows the calculated values for the 1D model with a momentum transferred per pulse of  $q = 7.9 \times 10^{-5}$  in atomic units. Right plots: Atomic state distribution based on conversion from measured ionizing field using the expected fields for red-shifted Stark states. Plot (b) shows the experimental data while plot (d) shows data calculated using the 1D model. Bottom plots: Evolution of the state distribution in time after (e) 6500 or (f) 2400 HCPs are applied. The evolution is measured by delaying the ionizing ramp relative to the initial Rydberg excitation pulse. The dashed lines show the ionization ramp delay of  $150 \mu\text{s}$  used for all other plots.

the best-fit principal quantum number and corresponds closely to a distribution from red-shifted Stark states. The inset shows a comparison to the expected distribution if we assume  $nD$  states have been produced, which does not agree as well. The predominant excitation of red-shifted Stark states is due to the small electric field present during excitation [17]. Due to the large quantum defects of  $l \leq 2$  states in Rb, these optically accessible states are displaced at zero field from the Stark manifold of states with  $l > 2$ . While the first Stark manifold that an  $nS$  state encounters is the  $n - 3$  manifold with which there is only a small coupling due to the large difference in  $n$ , an  $nD$  state encounters the downhill, red-shifted state of the  $n - 1$  Stark manifold where there is a much larger coupling. At this point much of the  $D$  character is spread to these red-shifted states and it becomes possible to optically excite them when the electric field is high enough to have reached the first crossing,  $F \sim 1/3n^5$ .

Assuming the length of the HCP is short relative to the electron orbit time, the transition amplitude from initial state,  $i$ , to final state,  $f$ , due to an interaction with an HCP can be reduced to the inelastic form factor of the atom,  $T_{f,i} = \langle f | e^{-i\vec{q}\cdot\vec{r}} | i \rangle$ , where  $\vec{q}$  is the momentum transferred to the atom.



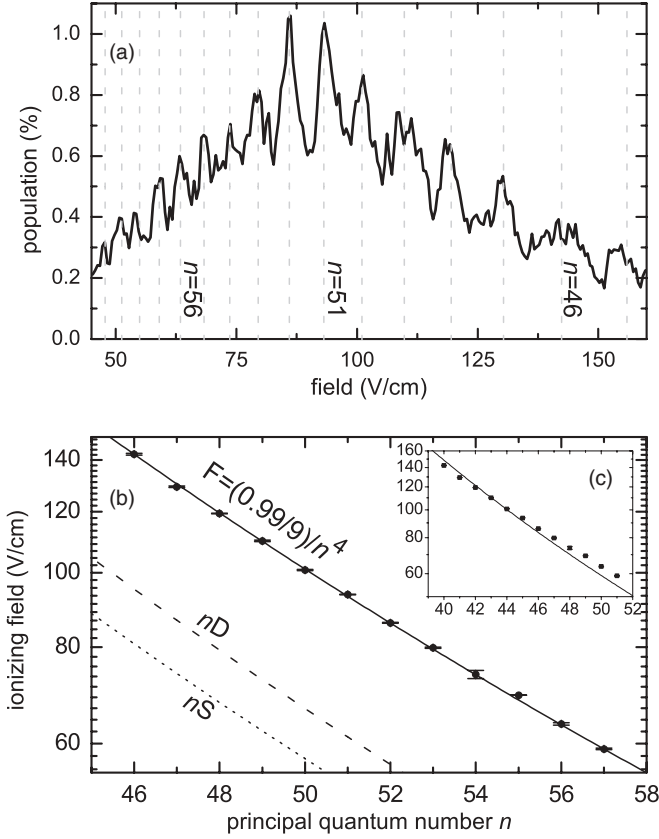


FIG. 4. (a) Field ionization trace showing peaks from populations in many different principal quantum numbers. Dashed lines are the calculated ionizing field for red Stark states. (b) Ionization peak locations versus principal quantum number. Note the close agreement to the red Stark state calculated value of  $F = (1/9)/n^4$ . The dashed and dotted lines show the expected ionization fields for  $nS$  and  $nD$  states, respectively, following adiabatic pathways toward ionization. (c) Similar fit assuming adiabatic ionization of  $nD$  states.

With an initial density matrix  $\rho(0)$  given by a statistical mixture of the measured initial-state distribution, the state distribution resulting after  $j$  pulses is given by

$$\rho(j) = (e^{-iHt_r} T)^j \rho(0) (T^\dagger e^{iHt_r})^j, \quad (1)$$

where  $t_r$  is the period of the pulse train and  $H = -1/2n^2$  is the unperturbed Hamiltonian of the system.

The applicable form factor has been analytically calculated for hydrogenic Stark states with parabolic quantum numbers  $n_1$ ,  $n_2$ ,  $m$ , and  $n = n_1 + n_2 + |m| + 1$ , where the atomic quantization axis and the HCP electric field polarization are parallel [18]. In this configuration the only applicable selection rule is  $\Delta m = 0$ . No simple analytical formula exists for when the quantization axis and the HCP electric field polarization are perpendicular. In the case of weak momentum transfer,  $T_{f,i} \sim \delta_{i,f} - iq_x \langle f|x|i \rangle$  and the applicable matrix elements are known [19]. In contrast to the parallel case, the selection rule for the magnetic quantum number is now  $\Delta m = \pm 1$ . As red-shifted Stark states are predominantly 1D atoms with the expectation value of the axial electron position much greater than the radial position, the interaction can be further simplified to that of 1D atoms interacting with an impulsive kick of given

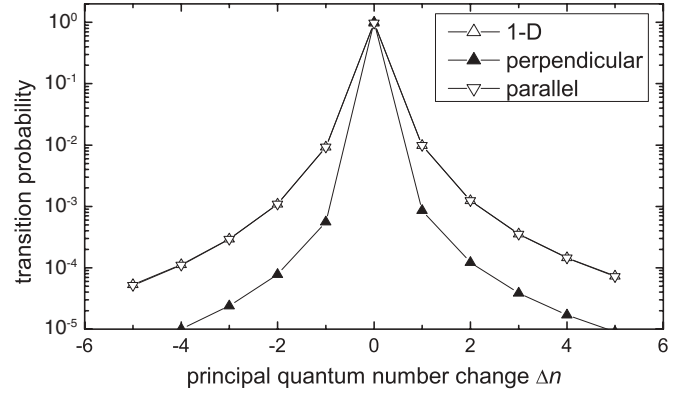


FIG. 5. Transition probability from  $n = 62$  to  $n = 62 + \Delta n$  for a momentum transfer of  $q = 7.9 \times 10^{-5}$ . The probabilities from the 1D model [Eq. (2)] and from 3D red-shifted Stark states with  $|m| \leq 5$  kicked by a pulse with electric field polarization along the quantization axis are almost the same. The probabilities from the same Stark states kicked instead by a pulse with electric field polarization perpendicular to the quantization axis are more than an order of magnitude lower.

momentum transfer,  $q$ . The transition amplitude for a single impulsive kick in the 1D approximation is given by [20]

$$\begin{aligned} T_{n',n} = & -\frac{z(\lambda - 2/n)^n (\lambda - 2/n')^{n'}}{\sqrt{nn'\lambda^{n+n'}}} \\ & \times \left[ \left( \frac{n-1}{\lambda - 2/n} + \frac{n'-1}{\lambda - 2/n'} - \frac{n+n'}{\lambda} \right) \right. \\ & \times F(-n+1, -n'+1, 2, z) - \frac{(n-1)(n'-1)}{2} \\ & \times \left( \frac{1}{\lambda - 2/n} + \frac{1}{\lambda - 2/n'} \right) \\ & \left. \times z F(-n+2, -n'+2, 3, z) \right], \quad (2) \end{aligned}$$

where  $n$  and  $n'$  are the initial and final principal quantum numbers,  $F(a, b, c, y)$  is the hypergeometric function,  $\lambda = n^{-1} + (n')^{-1} - iq$ , and  $z = -4n'n[(n-n')^2 + (qn'n)^2]^{-1}$ .

Figure 5 compares the probability,  $|T_{f,i}|^2$ , of a transition for these three different cases from a red-shifted Stark state where  $n_1 = 0$  and  $|m| \leq 5$  to a final state with a given change in principal quantum number. Two points from this figure are important. First, the overall shape of the curve is similar for all three cases but the probability of a transition in the perpendicular kick case is approximately an order of magnitude lower. Since  $\Delta E = (2\mathbf{p}_0 \cdot \mathbf{q} + q^2)/2$ , where  $\mathbf{p}_0$  is the initial momentum and with perpendicular polarization  $\mathbf{p}_0 \cdot \mathbf{q} = 0$ , one would expect the reduction in energy transfer and thus transition amplitude when kicked in this configuration. Second, in the two three-dimensional (3D) cases, the transition amplitude is clustered around similar states. Hence, the likelihood of driving a transition away from red-shifted Stark states is many orders of magnitude lower. Given these results, the 1D model is expected to apply quite well apart from the correction in overall amplitude necessary for the perpendicular kick case because atoms that start in a primarily 1D state will stay in similar states.

Unless a fast decoherence term is added, this model shows interference effects and emphasizes eigenstates which have stationary phase at the frequency of the pulse train. This is not seen in the actual experimental data, suggesting that decoherence occurs on a time scale similar to the time between HCPs. This is a shorter time scale than for dephasing due to blackbody transitions or spontaneous emission. Also no dependence on density is observed, precluding a collisional process being responsible for the decoherence. The most probable reason for the fast decoherence is the fact that the polarization of the HCP is nearly perpendicular to the quantization axis set by the static external electric field. Each kick must change  $m$  by  $\pm 1$ , allowing for many more states to be populated, and small changes in the time between HCPs will result in dephasing between these states.

Figure 3(d) shows the results of applying the aforementioned 1D model to the initial-state distribution shown in Fig. 3(b) measured when no HCPs have been applied. The predicted ionizing field distribution shown in Fig. 3(c) is calculated by assigning an electric field distribution to each principal quantum number centered at the expected field for red-shifted Stark states with a width proportional to the distance between adjacent state field ionization center values.

To compare the model and experimental data in more detail, Fig. 6 shows the electric fields at which 10%, 50%, and 90% of the atoms have ionized for a series of different initial states. The agreement between the experimental data and the one free parameter model is quite good, especially for atoms in

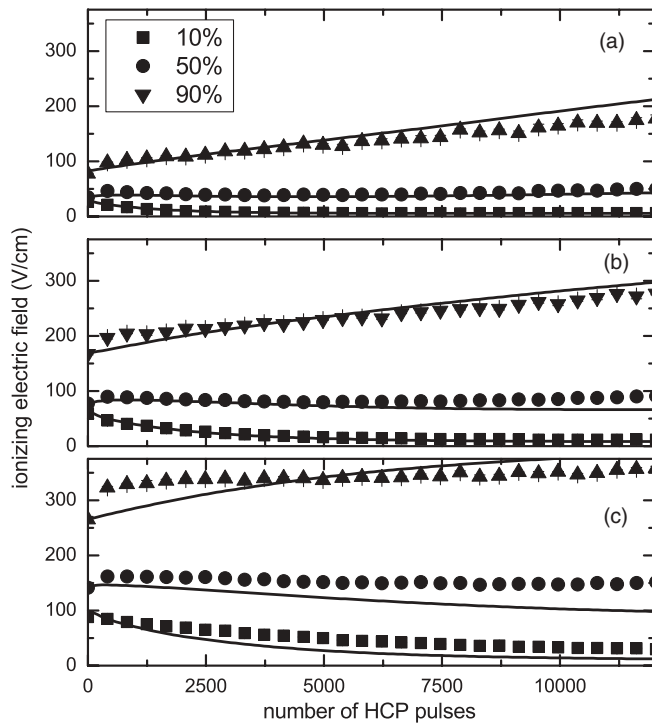


FIG. 6. Electric field for which the given percentage of the atomic ensemble has ionized as a function of the number of HCPs applied. The initial state of the atoms varies from (a)  $n = 62$  to (b)  $n = 52$  to (c)  $n = 46$ . Solid lines show the expected value from the 1D model with momentum transfer per pulse of  $q = 7.9 \times 10^{-5}$  in atomic units.

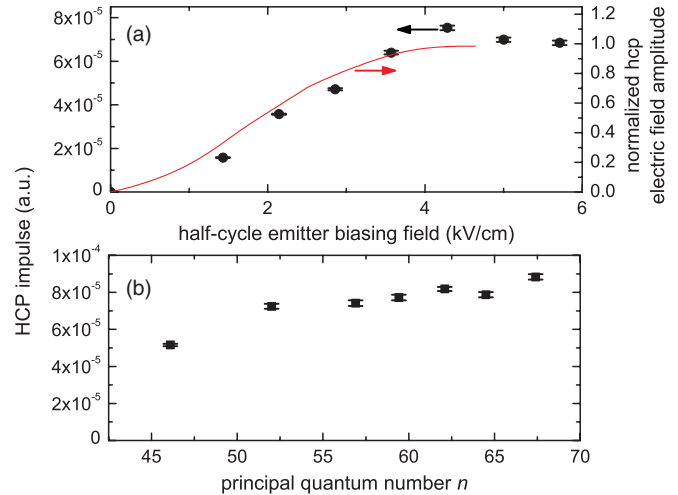


FIG. 7. (Color online) Best fit for the impulse in atomic units transferred by a single HCP to the 1D model described in the text. (a) The initial state of the atoms was held fixed at  $n = 62$  while the amplitude of the HCP was scanned. The solid line shows the measured amplitude of the HCP. (b) The HCP amplitude was held constant at a biasing field of 4.3 kV/cm while the initial atomic state was varied.

higher  $n$  states. The lack of agreement for lower  $n$  states, or equivalently populations that ionize at higher electric fields, in Fig. 6 is caused by a series of factors. First, at lower principal quantum numbers the 1D approximation, even for a red-shifted Stark state, begins to break down. Additionally, HCPs applied to atoms in these states are more likely to drive atoms to states for which the 1D approximation no longer applies. In addition, the width in electric field over which a state ionizes is proportional to the field at which it ionizes. Thus, for lower  $n$  states the width is much greater, resulting in a lower signal at a given field and increasing the sensitivity to noise and the exact details of how the conversion between state and ionizing field distributions is performed.

The maximum momentum transferred per pulse utilized in the model was calculated by a best fit to the data for the field at which 10% of the total population was ionized, including several initial-state distributions, as shown in Fig. 7(b). Averaging over these points, we find a calculated momentum transfer per pulse of  $q = 7.9 \times 10^{-5}$ . From Eq. (2) and this calculated momentum transfer, there is less than a 1% probability of an atom changing principal quantum number by  $\pm 1$  from the action of a single pulse for states near  $n \sim 50$  and a negligible probability to change by higher amounts. Consequently this model behaves as a diffusive process and the spreading of population density is expected. From the measured electric field of the HCP we expect a maximum momentum transferred by a single pulse of  $5 \times 10^{-4}$  in atomic units. This is a factor of 5 times more than the maximum calculated from the 1D model fit as shown in Fig. 7(b). However, correcting the calculated value for the reduced transition amplitudes when the HCP kicks the atom perpendicular to its quantization axis, we find  $q \sim 3 \times 10^{-4}$ , which is in close agreement.

#### IV. CONCLUSION

In summary, a train of HCPs produces large diffusive population transfers independent of the initial  $n$  state of the Rydberg atoms and operates regardless of the time structure creating Rydberg atoms. These trains are thus ideal for the control and efficient de-excitation of Rydberg antihydrogen atoms because they meet all of the previously discussed conditions required for compatibility with antihydrogen production. The ability to accurately model the population transfer demonstrated in this text, using analytical calculations of the inelastic form factor, will allow for the efficient development of enhanced protocols using, for example, chirped-pulse trains both to enhance the efficiency of the transfer and to drive atoms toward a desired final state. These protocols will depend on coherent population transfers and thus the rapid dephasing observed in our experiments must be reduced prior to their implementation.

Regardless of further developments, the population transfers demonstrated in this paper will greatly increase the

probability of trapping antihydrogen atoms. The 10% increase in  $l$ -mixed population with  $n \leq 40$  has a radiative lifetime that is a factor of 4 shorter than that of  $n = 52$ ; furthermore, during the 150  $\mu\text{s}$  that HCPs were applied, an additional 2% of the population reached the ground state. For antihydrogen applications, this reduction from greater than 4 ms to a 1-ms lifetime should increase the population that reaches the ground state before annihilation on a trap wall by more than an order of magnitude based on the current ATRAP experimental configuration [21].

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