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## **Predicting Acceptable Wait Times for Patrons at Transit Bus Stops by Time of Day**

Stephen Arhin

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# Predicting Acceptable Wait Times for Patrons at Transit Bus Stops by Time of Day

Stephen Arhin, PhD



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REPORT 19-30

# **PREDICTING ACCEPTABLE WAIT TIMES FOR PATRONS AT TRANSIT BUS STOPS BY TIME OF DAY**

Stephen Arhin, PhD

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## EXECUTIVE SUMMARY

The time spent waiting by bus patrons at bus stops is a primary measure for assessing the reliability of transit services. Uncertainty associated with waiting affects bus patrons' perception of quality of the service provided. Studies on bus wait times have therefore been of interest to transit service agencies and officials in a bid to gain more insight into improving quality of service.

This report presents the findings of a study conducted to determine patrons' maximum and minimum acceptable wait times at bus stops in Washington, DC and to develop prediction models for providing decision-makers with additional tools for improving patronage. The research relied primarily on a combination of field surveys and video-based data collection efforts. Field surveys were conducted to obtain patrons' suggested acceptable wait times at bus stops, while video-based data collection was used to obtain bus operational characteristics.

A total of 3,388 bus patrons were surveyed, at 71 selected bus stops. Additionally, operational data was extracted via video playback for 2,070 bus arrival events on 226 routes. Data was collected for AM peak (7:00 AM -9:30 AM), PM peak (4:00 PM- 6:30 PM) and mid-day periods (10:00 AM – 2:30 PM) over a nine-month duration, from May 2018 through January 2019.

The following are the summary results of the survey conducted at the bus stops:

- The least reported acceptable wait time beyond the scheduled bus arrival time was 1 minute.
- The highest reported acceptable wait time beyond the scheduled bus arrival time was 20 minutes.
- The mean of the reported maximum acceptable wait time for female patrons was 8.5 minutes. The mean of the reported maximum acceptable wait time for male patrons was 8 minutes.
- The modal acceptable wait time, reported by approximately 33% of the patrons, was 5 minutes.
- In decreasing order, the mean of the maximum acceptable wait times of patrons categorized by ethnicity were as follows: African American (8.5 minutes), Asian (8.4 minutes), Hispanic (8.3 minutes), and White (7.0 minutes).
- Patrons are willing to wait longer in warmer temperatures.
- Patrons are willing to wait longer at bus stops with longer headways.

Tables 1 and 2 present some data about the acceptable wait times and alternate mode choices of bus patrons.

**Table 1. Averages of Reported Acceptable Wait Times**

	Category	Avg. Max. Acceptable Wait Time (Minutes)	Avg. Min. Acceptable Wait Time (Minutes)
Time of Day	AM	7.0	2.5
	MID	10.5	4.0
	PM	7.5	3.0
Presence of Shelter	Without shelter	7.5	3.0
	With shelter	9.0	3.0
Gender	Male	8.5	3.0
	Female	8.0	3.0
Ethnicity	White	7.0	2.0
	Black	8.5	3.0
	Hispanic	8.3	3.0
	Asian	8.4	3.5
	Other	8.5	3.0
Knowledge of Bus Arrival Time	No	10.5	4.0
	Yes	7.0	2.5
Ward	1	8.0	3.0
	2	8.0	3.0
	3	7.0	3.0
	4	8.5	3.0
	5	8.0	3.0
	6	8.5	3.0
	7	9.0	4.0
	8	10.0	3.5
Quadrant	NE	8.0	3.0
	NW	7.0	3.0
	SE	10.0	3.0
	SW	9.0	3.5

**Table 2. Preferred Alternate Mode Choice of Bus Patrons**

Alternate Mode of Transportation	Percentage of Patrons (%)
Train	40
Ride Share	35
Bike	11
Walk	10
Other	4

Regression analyses were conducted to develop models to predict the maximum acceptable wait time of patrons based on factors including temperature, presence of shelter at the bus stops, average headway of buses, and patrons' knowledge of bus arrival times. The models were developed for A.M., P.M., and mid-day periods. The F Statistics for all three models were determined to be statistically significant with  $p$ -values  $<0.001$  at a 5% significance level. The models had values (percentage of variance explained) of 64%, 79% and 82%.

Although female patrons generally had lower maximum acceptable wait times than male patrons, the difference was not statistically significant. However, the mean differences between the maximum acceptable wait times of patrons grouped by ethnicity were determined to be statistically significant at a 5% significance level. The study revealed that White patrons had significantly lower maximum acceptable wait times than did patrons of other ethnic groups.

## I. INTRODUCTION

Urban areas typically have access to several transportation modes, including bus transit. Transit buses offer short-distance transportation between bus stops on different routes, mostly in dense urban areas. Transit agencies strive to keep patrons satisfied by improving the punctuality of bus arrivals at bus stops and by reducing wait times. Bus transit travel time and wait times are two of the critical factors that influence patrons' decision whether to use buses or to use another mode of transportation. If transit buses arrive at scheduled times, patrons are less likely to have the need to find alternative modes of transportation. However, if buses are chronically late at bus stops, patrons may feel that the bus system is unreliable and may seek alternative modes of transportation.

Henderson (1972) conducted a survey which showed that patrons waiting at a bus stop perceive wait time to be three times more bothersome than the time spent riding on the bus. Consequently, wait times are more likely than transit times to lead travelers to change from using buses to using another transportation mode. It is therefore necessary to be able to predict the maximum acceptable wait time of patrons in order to optimize bus headways, bus dwell times and the adequate spread of bus stops along a route.

This study aimed at modeling patrons' maximum acceptable wait times at bus stops in Washington, DC as functions of various predictor variables, in order to provide decision-makers with new tools for increasing ridership.



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## II. LITERATURE REVIEW

This section presents the finding of the review of literature on wait time of bus patrons. The review focuses on the patrons' perception of waiting as well as the on factors that may influence bus patrons' wait times. Previous models developed to predict wait time are also examined.

### PERCEIVED AND ACTUAL WAITING TIMES

Several studies have determined that waiting at bus stops is one of the most onerous components for riders of using bus transit services. A survey on bus user preferences was conducted in Australia, and found that among factors such as vehicle quality, trip quality and information quality, waiting time was the top most concern of patrons. A study reported that the time patrons spend waiting at a bus stop is perceived to be more burdensome than the same amount of time spent in-vehicle. The study further attributed the discomfort experienced by patrons to the uncertainty associated with waiting. The inconsistencies in waiting times can lead to large variabilities in travel time. Waiting time was found to be a statistically significant factor in explaining travel time variability. Also, several studies have sought to develop models to quantify waiting time of patrons at bus stops.

The literature has also revealed that perceived wait time of passengers differ from their actual wait times. Bus patrons subjectively overestimate their actual wait times and place more value on this perceived wait time than on any other investigated component of their trip. Perceived wait times tend to have a greater influence on rider discomfort and preference towards bus services than do actual wait times. A study was conducted to estimate the relationship between perceived and actual waiting times of patrons at bus stops on the campus of Ohio State University. The mean difference between the perceived and actual waiting time of passengers was estimated to be 0.84 minutes. A valuation of wait time and service headway among some public transport users in the United Kingdom found that patrons perceive one minute of waiting at a bus stop to be equivalent to 4.4 minutes of in-vehicle time. An earlier study conducted in the United States, found one minute of wait time to be perceived as equivalent to 8.4 minutes of in-vehicle time for a 30-minute journey and equivalent to 13 minutes for a 45 minutes journey.

Passenger perception of bus service performance and the effect of the perception on ridership were measured in a study conducted in Nanjing, China. An exploratory factor analysis found that, of the factors investigated, wait time was the most negatively perceived. A similar study in Nanjing, China determined that when wait times exceed passengers' tolerance; they tend to associate "long wait" as the primary service attribute. Thus, perceived wait times negatively influenced the overall transit service satisfaction. Another study investigated passenger wait time perceptions in Athens, Greece and concluded that on average, perceived wait times are 1.5 times higher than actual wait times. Previously, it had also been found that the disparity depended on whether passengers made a conscious decision to wait, or whether the wait was imposed on them by transit agencies; when imposed by the transit system, wait times were overestimated on average by a factor of two.

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## **FACTORS AFFECTING WAIT TIME PERCEPTION**

The perception of passage of time is highly subjective and depends on the innate characteristics of the individual. Thus, different individuals under the similar conditions and with similar demographic traits may nevertheless still perceive the passage of time differently. Nevertheless, several studies have identified certain key external factors that predictably influence the perceived wait times of bus patrons. These include bus stop features and surroundings, trip purpose, period of day, transit service attributes, weather and patrons' demographics. The following sections discuss these factors.

### **Bus Stop features and surroundings**

Bus stop features such as shelter, the presence of a bench, lighting, and the presence of security affect the perceived wait times of patrons. A study showed that transit users in Grenoble, France overestimated their actual wait times at bus stops where light and heat/ventilation were absent. Lesser estimates were recorded where adequate lighting and ventilation were present. Lighting, music, and aesthetics have also been found to influence the perceptions of waiting time, with transit users of a Dutch railway service generally preferring bright lighting, calming music and warm colors. A study was conducted to compare transit riders' actual and self-reported waiting times at 36 bus stations in the cities of Minneapolis and St. Paul in Minnesota, and concluded that wait times at bus stops without amenities such as shelter and benches are perceived to be about 1.3 times longer than they actually are; they also found that females who waited at insecure bus stops for more than 10 minutes overestimated their waiting times by a larger amount than did their male counterparts. Moreover, passengers were found to be more reluctant to wait at transfer stations without available amenities such as shelter and bench than stations with amenities. Bus stop or station amenities not only reduce perceived wait time but also have the potential of making additional actual wait times of transit users more bearable; a study revealed that commuters in Naples, Italy were willing to accept an additional 7 minutes of waiting time to use a new rail line with improved stations.

Studies conducted in California have found that passengers prefer short and predictable wait times in a safe environment, while the attractiveness of bus infrastructure did not really matter.

The availability of real-time arrival and departure information at bus stops also affects the perceived wait times of patrons. The addition of real-time departure information signs to bus and streetcar stops in London reduced perceived waiting times by more than 20%, and the reduction in perceived wait time was estimated to be equivalent to reducing headways from 10 to 8 minutes. A study also found that the availability of real-time arrival information reduced the ratio of perceived wait time to actual wait time.<sup>14</sup> It is recommended that the provision of real-time arrival information by transit services would reduce uncertainty and perceived waiting time.

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## **Period of day**

The time of day has been determined to affect bus patron's perception of wait times at bus stops. A study revealed that although perceived and actual wait times are longer during the afternoon than the evening and morning, the ratio of perceived to actual wait times is highest during the morning—perhaps due to riders' anxiety about getting to work on time—with patrons tending to overestimate their waits by a factor of 1.74 during the morning, by a factor of 1.63 during the evening and by a factor of 1.41 during the afternoon.<sup>9</sup> Another study conducted in Harbin, China also revealed that the period of the day to be a statistically significant predictor of waiting time.

## **Trip purpose**

Possible trip purposes include education, entertainment, shopping, returning home, and “personal”. Among these, patrons travelling to work are most likely to overestimate their waiting times by a factor of about 1.53.<sup>9</sup> A study showed that trip purpose is a significant predictor of perceived wait time, also finding that passengers traveling for work purposes overestimated their waiting time the most.<sup>19</sup>

## **Transit Service frequency and reliability**

A study conducted to identify the effects on waiting times of transit users of service frequency and reliability determined that, buses' strict adherence to their schedule allows transit users to coordinate their arrivals with those of the bus, resulting in average wait times that are less than half the scheduled headway. Uncertainty regarding the arrival times of buses due to unreliability therefore increases both the actual and the perceived wait time of transit users.

## **Patrons' demographics**

Psarros et al. (2011) found that male patrons tend to overestimate their wait times on average by a factor of 1.61, while female patrons who overestimate their wait times on average by a factor of 1.52.<sup>9</sup> However, Gurmu and Fan and Feng et al.<sup>19</sup> did not find a statistically significant effect of gender on wait time.

## **WAIT TIME AS A MEASURE OF TRANSIT SERVICE RELIABILITY**

In assessing the reliability of transit services, transit agencies and officials have, among other indicators, used passenger wait times as a performance measure. A study concluded that passengers' perception of transit service quality are affected by uncertainty in wait times. Wait time is considered an appropriate measure of service reliability for high frequency routes where the arrival of passengers is random. For low frequency services, it was shown that passengers usually synchronize their arrival time at bus stops with the arrival of buses, thus minimizing wait times.

In a study, waiting cost functions, which took into account headway and service reliability, were developed. The study further found that, by analyzing the behavior of passengers,

the cost of waiting could be broken down into two components: the actual mean time spent waiting and the “potential waiting time”, a measure of the additional time passengers have to budget for waiting, defined as the 95<sup>th</sup> percentile waiting time. Potential waiting time was found to be very sensitive to service reliability; therefore, by minimizing the waiting cost function, service reliability can be improved. A similar conclusion was reached in a study, which analyzed the service reliability of a high frequency bus line in Helsinki, using AVL and APC data. It was found that passengers assessed the reliability of bus services mainly in terms of additional waiting and travel time, and suggested that reduction in wait and travel times would increase passenger satisfaction and thereby lead to increases in patronage.

## RELATIONSHIP BETWEEN WAITING TIME AND HEADWAY

Several studies have sought to establish the relationship between headway and waiting times of passengers. One of the earliest studies which developed a model for estimating the average wait time of passengers was conducted by Welding.<sup>23</sup> That study focused (among other issues) on passengers wait times for bus services with short headways. It concluded that the average waiting time of passengers who randomly arrive at a boarding point is lowest when the service is perfectly regular. The following model to estimate average wait time was suggested:

$$\textit{Average wait time} = \frac{\sum h_i^2}{2 \sum h_i}$$

where  $h_i$  = headway (in seconds).

A study of the behavior of passengers of a bus network in Stuttgart, Germany found that passengers' arrival at a bus stop is schedule-dependent when headways exceed 8 minutes; most passengers synchronize their arrivals with those of the buses, reducing the time spent waiting.

Further, a study conducted in Leeds, England, developed a model to estimate waiting times from headways, which they called “service intervals”, improving an earlier model developed by Holroyd and Scraggs. Flaherty and Mangan assumed that the arrival of passengers is random during mid-day periods, but not during the morning and evening peak periods. Mathematically, and modifying their notation for consistency in this paper, their model is expressed as:

$$\textit{Average waiting time} = 1.79 + 0.14h$$

Osuna and Newell developed a model which took into consideration the random arrival of passengers during the peak periods. The random waiting time  $w_r$  was related to the headway  $h$  by the relation:

$$w_r = \frac{h}{2} \left[ 1 + \left( \frac{\sigma}{h} \right)^2 \right]$$

where

$h$  = the bus headway

$\sigma$  = the standard deviation of bus headway.

A study analyzed passenger wait times and headways of buses in Manchester, England, and found a linear relationship between wait time and headway. The finding of the study also corroborated that of previous study, concluding that the arrival behavior of passengers is schedule-dependent when headways exceed 8 minutes. Another study used data from London, England, and found that passengers' arrival behavior was schedule-dependent for longer headways, but found that the threshold headway duration was 12 minutes.

When passenger arrival at bus stops is random and headways are perfectly regular, the average wait times of passengers is one-half of the headway. When headways are not regular, however, the expected wait time increases with the headway variance: a more general model for expected wait times is

$$\bar{w} = \frac{\bar{h}}{2} [1 + c_v(h)]$$

where  $\bar{w}$  is the average wait time,  $\bar{h}$  is the average headway, and  $c_v(h)$  is the coefficient of variation of headway. Note that even this more sophisticated model still assumes that passengers arrive at stops randomly, and won't be valid when this assumption fails.

Table 3 summarizes the above-discussed studies related to headway and passenger wait times.

**Table 3. Relationship between Waiting Time and Dwell Time**

Study	Location	Minimum Headway required for non-random arrival of passengers	Established Relationship between Wait Time and Headway
Welding (1957)	London	N/A	Linear
Weber (1966)	Stuttgart	8 minutes	-
O'Flaherty and Mangan (1970)	Leeds	5 minutes (Peak Periods) 12 minutes (Mid-day Periods)	Linear
Osuna and Newell (1972)	London	N/A	Linear
Seddon and May (1974)	Manchester	7.5 minutes	Quadratic
Joliffe and Hutchison (1974)	London	12 minutes	Linear
Cham (2006)	Massachusetts	N/A	Linear

## COMPONENTS OF WAITING TIME

Most studies have measured wait time as the time between the arrival of a passenger at the bus stop and the time they board the bus. However, it was argued in another study that this measure is inadequate as a measure of the “real cost” to passengers of waiting, and that a better measure of this cost should take into account four main components: platform waiting, potential waiting, schedule inconvenience, and synchronization cost, with the latter two applying specifically to bus services with long headways.<sup>24</sup>

### Platform waiting time

Platform waiting time is defined as the time between the passenger’s arrival at the bus stop and the time they board the bus; this component is the one which most other studies have simply referred to as “wait time.” When bus service is reliable, passengers can reduce their platform wait times by synchronizing their arrivals with bus arrivals.

### Potential waiting time

Potential waiting time is the additional time that passengers must be prepared to wait beyond the bus’s expected departure time, in order to reduce the risk of missing the bus to 5%. The potential waiting time is defined as the difference between the 95<sup>th</sup> percentile wait time and the mean wait time. Potential waiting time constitutes a genuine form of “waiting” because it is the mean amount of time by which the passenger will arrive to their destination earlier than expected—for example, by waiting to clock in at their workplace.

### Schedule inconvenience

Schedule inconvenience is defined as the difference between a passenger’s most-desired departure time and the best departure time available on the bus schedule. Like potential waiting time, this component can lead to waiting in the form of early arrival. Unlike potential waiting time, this component is predictable, and so less costly; its predictability means that passengers can more easily plan to use their earliness productively—for example, by planning to buy a coffee and a breakfast sandwich before work.

---

## **Synchronization cost**

This component of waiting cost measures the burden on passengers of having to adjust their schedule so as to conform to the service time table, quantified in terms of the “equivalent” number of minutes of wait time that they would find equally burdensome. This measure combines burdens including: the psychological stress of conforming to a timetable; the difference between actual arrival time at a bus stop and intended arrival time, necessary because people must always plan to arrive early if they want to guarantee arriving on time; and stress about missing the bus; and the full-headway wait time which occurs when a bus is missed. Furth and Muller suggest that these costs are all either constant or proportional to headway, and that overall synchronization cost, converted into psychologically equivalent minutes of in-vehicle time, be given by

## **WAIT TIME AND ALTERNATE MODE CHOICE**

When passengers wait longer than their threshold of willingness, they tend to begin considering other options of transportation mode. Long waits thus lead to decreases in user confidence and ultimately to reductions in ridership. A study revealed that high variation in waiting time for transit users was leading travelers to select different transportation modes. Travel time has always been known to be the lead factor in mode choice of commuters; however, reliability, which is influenced by the consistency of wait time, was also found to be a major factor in mode choice. In a study on passengers’ travel mode choice behavior when waiting at bus stations in Jinan, China, it was argued that passengers choose to end the waiting process and find a different mode choice when they reach a state of strong negative feelings due delay of bus arrivals. Other transportation mode options considered by passengers include transferring to another bus route, taking a taxi, and carpooling. Travel mode choice behavior was also determined to be a consumer choice attribute, which can vary across individuals. Thus, the individual characteristics of passengers determine their waiting time threshold and mode choice behaviors. Individual characteristics such as gender, level of education, occupation, and cultural differences influence the alternate modes of transport chosen by individuals once their acceptable waiting time has passed.

In a study aimed at modeling the choice behavior of passengers waiting on a subway platform where services have temporarily been suspended, it was found that some passengers preferred to wait for services to resume over choosing another mode choice with a shorter travel time. Another study conducted in Ghana examined the factors that influenced commuters travel mode choice, and concluded that safety, travel distance, transport fare, comfort and waiting time influenced commuters’ mode choice.

## **PASSENGER WAIT TIME DISTRIBUTION AND MODELING**

A number of studies have examined the distribution of passenger wait times and developed models to estimate wait time. Holroyd and Scraggs developed a model to predict wait time as a function of the distance between the bus stop and the destination, and found that the function was increasing. The wait time in their model was given by

$$\textit{Wait time} = 0.48d + 1.8$$

with wait time measured in minutes and distance  $d$  measured in kilometers. Distance was the only predictor variable that was considered. The correlation between wait time and distance, however, was not found to be statistically significant, at a 5% significance level.

Arrival distribution curves were developed based on data collected at 28 bus, tram and commuter rail stations in a study conducted in Zurich, Switzerland. The stations were served by scheduled public transits with headways ranging from 2.33 to 30 minutes. The observations were made on weekdays during the morning, evening and mid-day periods. The analysis of the results showed that both passenger arrivals and wait times have a logarithmic relationship with headway. It further concluded that passengers begin to arrive at stations near the scheduled departure times, even for very short headways. Another study fitted the arrival rate of passengers transferring from rail to buses to normal, exponential, lognormal and gamma distributions. The study concluded that the lognormal and gamma distributions had the best. A similar conclusions was reached in a study conducted in Beijing, China. In this study, passenger arrival times were fitted to extreme value, exponential, lognormal, gamma and normal distributions; it was found that the arrival time of passengers at bus stops connected to rail stations were best fitted with the lognormal distribution, while arrival time of passengers at bus stops not connected to rail stations were best fitted with the gamma distribution.

The distributions of actual passenger wait times and perceived wait times were developed based on data collected at bus stops in London, England. It was found that, the actual wait times of passengers followed the gamma distribution while the perceived wait time of passengers followed the lognormal distribution. In addition, multiple linear regression model were developed to predict perceived wait time of passengers based on data for 234 passengers surveyed at three bus stops in Harbin, China. Factors considered in the development of the model included gender, level of education, possession of a time device, presence of a companion, travel purpose, riding frequency, walking time, reserved waiting, waiting mood, waiting behavior, and time of day (morning or evening peak). The ANOVA results did not find statistically significant effects on perceived waiting time of gender, level of education, or walking time at a 5% significance level.<sup>19</sup> Their best-fitting multiple linear regression model for perceived wait time was

$$Y = 7.604 - 1.526X_{WT} - 1.474X_{WC} - 1.545X_{TP} + 1.054X_{RF} + 0.894X_{RW} - 0.027X_{RW} \\ - 1.104X_{BC} + 1.104X_{MA} + 2.866X_{MW}$$

where

$Y$  = perceived wait time

$X_{WT}$  = having a time device



$X_{WC}$  = presence of companion

$X_{TP}$  = Trip purpose

$X_{RF}$  = Riding frequency

$X_{RW}$  = Reserved waiting time

$X_{BC}$  = Waiting behavior

$X_{MA}$  = Waiting mood.

Beyond the regression models, other studies have used machine learning techniques to develop passenger wait time models. A study used artificial neural networks to develop passenger wait time models based on data collected on passengers using a high-speed train service in Beijing. The predictors used in the model were trip distance, transportation mode, travel time, familiarity with the service facility, and level of education. The Artificial Neural Network (ANN) model developed consisted of one input layer with 5 neurons, two hidden layers with 8 and 3 neurons respectively, and an output layer with a single neuron. The sigmoid function and purelin transfer function were used as the respective activation functions in the hidden and output layers. The model was trained with data set of 720 samples, and validated with a data set of 336 samples. The model developed predicted passenger wait time with an average error of 9.2%.

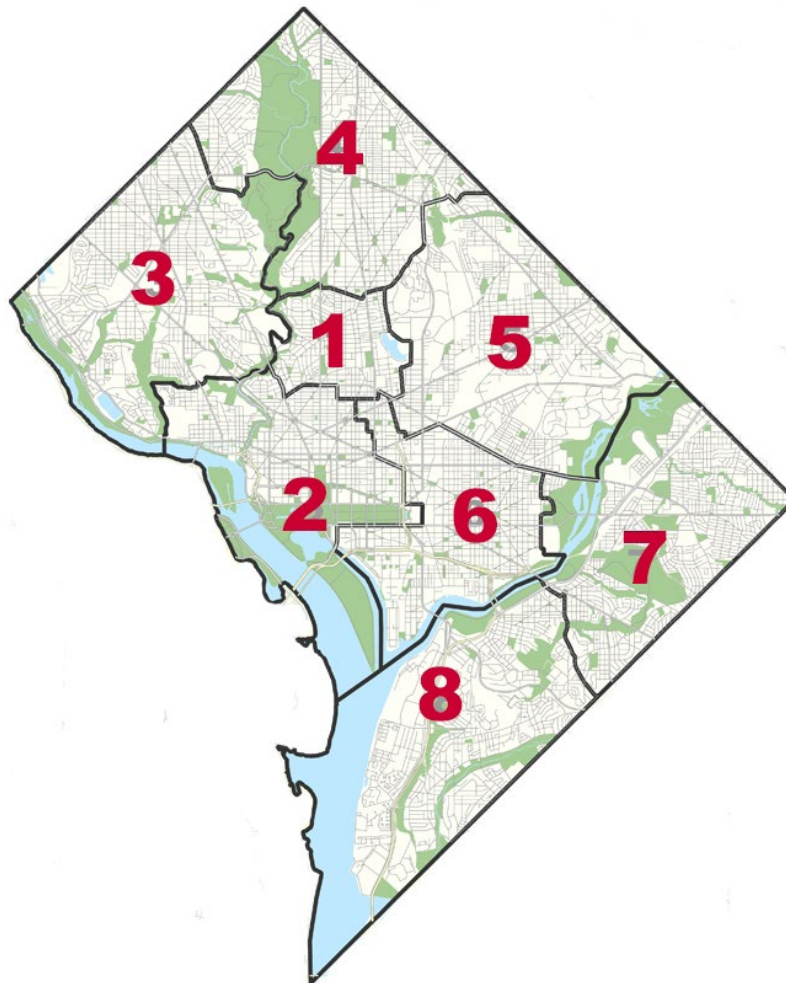
## **SUMMARY OF LITERATURE REVIEW**

The above review of the literature shows that the wait times of bus patrons generally follow lognormal and gamma distributions, and are impacted by several environmental and bus operational factors. It is also pointed out that when wait times exceed acceptable limits, patrons tend to consider other mode choices which provide comparatively efficient service. However, although several studies have sought to model both wait times and perception of wait times as functions of various predictor variables, none has sought to model the maximum acceptable wait time of patrons beyond the schedule arrival time of buses. This study therefore focuses on determining the average maximum wait time of patrons and on developing models for its prediction. Three different models were developed, for three different periods of the day: AM peak (7:00 AM -9:30 AM), PM Peak (4:00 PM- 6:30 PM) and mid-day (10:00 AM – 2:30 PM).

### III. RESEARCH METHODOLOGY

#### DESCRIPTION OF THE STUDY JURISDICTION

This research is based on data obtained in Washington, D.C. The city is divided into four quadrants of unequal area: Northwest (NW), Northeast (NE), Southeast (SE), and Southwest (SW). The city is also divided into eight Wards, which overlap the boundaries of the quadrants. As of 2017, the population of Washington, D.C. was approximately 694,000 with an annual growth rate of approximately 1.41%. The City is highly urbanized and is ranked as the sixth most congested city in the United States with each driver spending an average of 63 hours per year in traffic. The Washington Metropolitan Area Transit Authority (WMATA) is the agency that oversees the operations of Metrobus service in the jurisdiction. WMATA has a bus fleet of 1,595 buses that make more than 400,000 trips each week day. These buses serve about 11,500 bus stops and operate on 325 routes in Washington D.C., in portions of Maryland, and Northern Virginia, covering a total land area of about 1,500 square miles. Of the total number of bus stops, 2,556 (22.2%) have shelters, while the remainder do not. A map of Washington, D.C. showing the city divided into Wards is shown in Figure 1.



**Figure 1. Map of the Washington, D.C.**

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## DATA COLLECTION

### Selection of Bus Stops

Bus operational data and patron survey data were collected at seventy-one selected bus stops in Washington, D.C. Both bus stops with shelter and bus stops without shelter were considered. The bus stops were selected based on the following criteria:

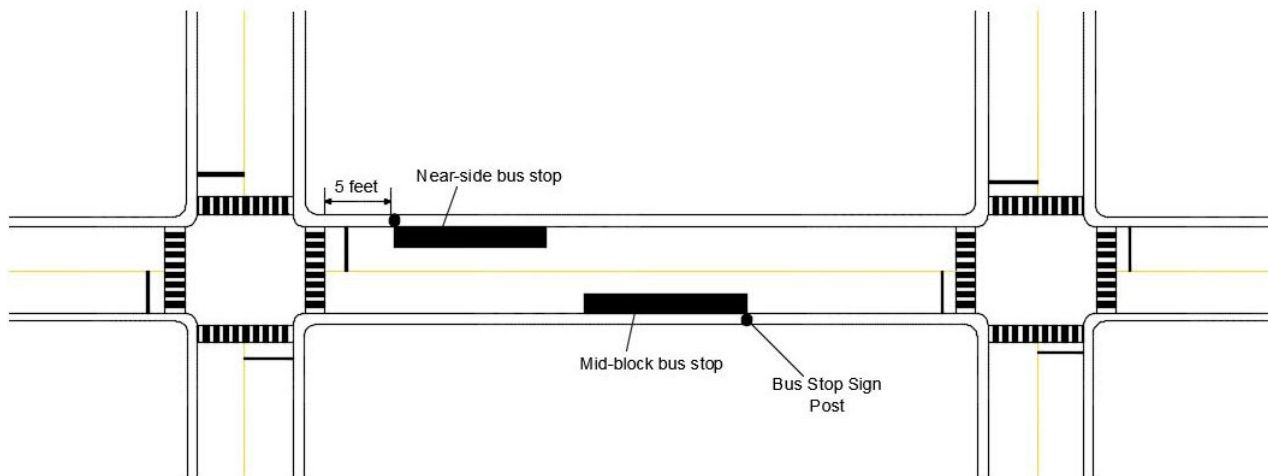
- Those on bus routes with longer headways: bus stops on routes with longer head ways were selected to ensure that data collection technicians were able to complete the survey of bus patrons before the arrival of a bus. Such bus stops were identified using the published time tables available on WMATA's website.
- Bus stops with high patronage: selection of bus stops with high patronage ensured that the required minimum number of patrons were surveyed at each bus stop.
- Proximity to metro rail station: bus stops in proximity to railways are viable locations to have access to bus patrons with variable characteristics. In addition, such locations usually have a high number of bus patrons waiting to board a bus.
- Roadway functional classification: bus stops on arterial and collector roads were selected for this study since they usually serve more than two bus lines.

### Bus Stop Characteristics

The bus stops selected for this study were categorized in relation to their location on the roadway and to the type of design.

#### *Bus Stop Placement and Location*

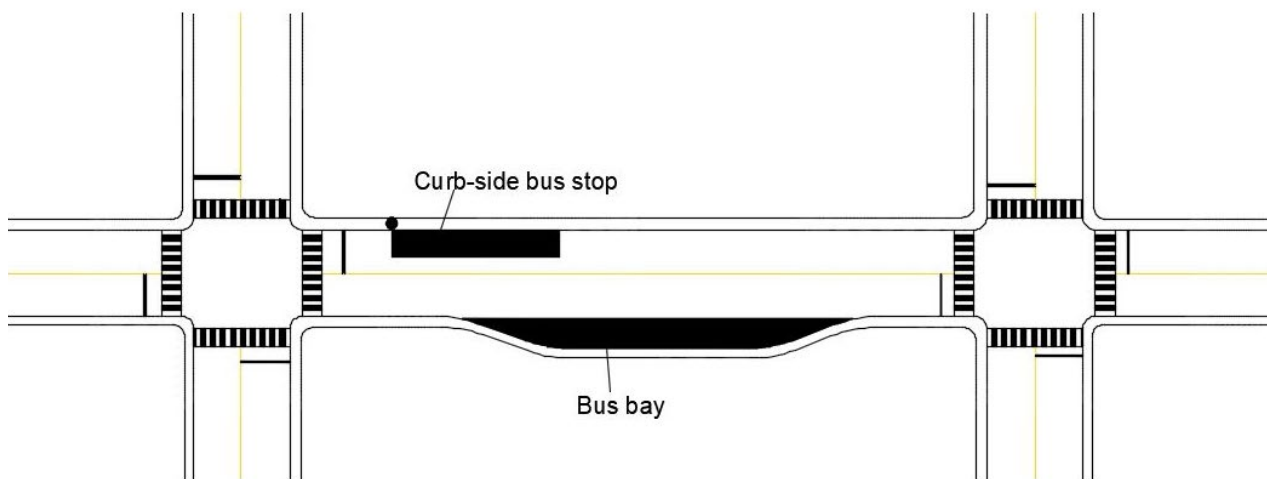
The WMATA Guidelines for the Design and Placement of Transit Stops defines bus stop locations relative to an intersection. Three types of location are specified: near-side (upstream) of the intersection; far-side (downstream) of the intersection; and mid-block (midway between intersections). Near-side bus stops are usually located at least 5 feet from the intersection, far-side bus stops are at least 50 feet from the intersection and midblock bus stops are positioned midway between two intersections. The selected bus stops for this study are comprised of only near-side and midblock bus stops, which are the predominant types of bus stops in Washington, D.C. Figure 2 depicts typical locations of near-side and mid-block bus stops used in this study.



**Figure 2. Near-side and Mid-block Bus Stop Locations**

### *Design Type*

Bus stops can be further categorized as being either curb-side bus stops or bus bays, depending on their position in relation to the travel lanes. Curb-side bus stops service patrons from a travel or a parking lane. Bus bays are constructed as insert into the curbs with tapered ends for acceleration and deceleration, and with reinforced concrete pavement. Figure 3 illustrates these two bus stop design types.



**Figure 3. Curb-side Bus Stop and Bus Bay**

### *Amenities*

Bus stops in Washington, D.C. vary in their possession of amenities such as sign posts, shelters, and information cases. The amenities are described as follows:

- *Bus stop sign post:* WMATA bus sign posts are usually red plaques mounted on the

top of white poles. The plaque provides the patron with information regarding route numbers, stop ID numbers, WMATA's web site address and a telephone number for patrons to call for assistance.

- *Information case*: this is a rectangular or cylindrical glass casing containing information such as system maps, neighborhood maps, and/or bus schedules.
- *Shelters*: these are covering structures that provide protection against weather for passengers waiting at a bus, together with a bench located in the shelter.

The primary bus stop amenity considered in this research was the presence or absence of a shelter.

A summary of the description of the 76 selected bus stops is presented in Appendix A. The information obtained include regarding bus stop ID, design type, placement, amenities, and service route numbers. Figures 4 to 6 present pictures of some bus stops at which data was collected.



**Figure 4. Curb-side Bus Stop with Shelter and Bench**



**Figure 5. Curbside Bus Stop without Shelter**



**Figure 6. Bus Bay with Shelter and Bench**

## **DATA COLLECTION**

Data collection at the selected bus stops was conducted over a nine-month duration from May 2018 through January 2019. Data was collected during the AM peak (7:00 AM–9:30 AM), PM peak (4:00 PM–6:30 PM) and mid-day periods (10:00 AM–2:30 PM). Two forms of data collection were performed: bus patrons were surveyed and bus operational data was collected. The data collection schedule was organized so as to maximize the number of survey participants and achieve a robust sample size.

### **Survey Data Collection**

Passengers waiting for the arrival of the next bus at the selected bus stops were randomly selected and interviewed during the morning, evening and mid-day periods on weekdays. The field technicians conducted the survey by use of electronic forms on computer tablets. However, where computer tablets were unavailable, paper questionnaires were used. The survey procedure was conducted as follows:

- i. Upon arrival at the bus stop, the interviewer first obtained the temperature at the bus stop location from the National Oceanic and Atmospheric Administration (NOAA) weather service website and recorded it in the designated field on the questionnaires accordingly. The date of survey and the name of the interviewer were also recorded.

- ii. The availability or unavailability of a bus shelter and the direction of travel (northbound, southbound, eastbound, westbound, southwest-bound or northeast-bound) the bus stop serves were then observed and recorded in their designated fields.
- iii. When a patron arrived at the bus stop, his/her arrival time and gender were recorded.
- iv. The field technician then approached the patron(s) and, if they were willing to participate, asked the following questions to complete the survey:
  - Whether the passenger was aware of the scheduled bus' arrival time.
  - At bus stops that serve more than one line, the patron was asked which route he/she intended to take. Where the bus stop served only one line, such information was simply obtained from the bus stop sign post.
  - The patron's minimum acceptable wait time beyond the bus scheduled arrival time for which the patron is willing to wait.
  - The maximum acceptable wait time beyond which the patron would consider an alternative transportation mode.
  - What alternate mode(s) of transportation the patron would consider if the bus was delayed beyond their maximum acceptable wait time.
- v. The bus line(s) that serve the bus stop were recorded.


Table 4 summarizes the variables collected from each bus stop and patron, as well as operational characteristics obtained during the survey, and their associated abbreviations used in the analysis.

**Table 4. Summary of Collected Data and Associated Variable Names**

Variable	Abbreviation
<i>Bus Stop Characteristics</i>	
Bus stop number	B#.
Bus stop type	BT
Temperature	T
Availability of shelter	S
Direction of travel	D
<i>Passenger Characteristics</i>	
Patron arrival time	PAT
Patron ethnicity	E
Route number	R#.
Knowledge of bus arrival time	KBAT
Minimum acceptable wait time	MiAWT
Maximum wait time	MAWT
Alternate mode of transport	AMT
<i>Operational Characteristics</i>	
Bus arrival time	AT
Bus departure time	DT



A total of 3,388 patrons were surveyed over the period of the study. In the event that the minimum number of responses was not obtained during a particular peak period due to inclement weather or low patron turnout, additional patrons were surveyed on the same day and period the following week. The survey questionnaire is presented in Figure 7. Figure 8 presents a photograph of a patron being surveyed at one of the selected study locations.




## Acceptable Wait Time Survey

**Interviewer Name:**

**Date :**



**Temperature:**


  

### Bus

**Bus Route :**

**Bus #:**

**Time :**



**Bus Direction of Travel :**

NB  
  SB  
  EB  
  WB

**Bus Stop has:**

Shelter  
  Bench  
  Both  
  None

### Patron

**Gender :**


Female  
  Male

**Ethnicity:**

White  
  African American  
  Hispanic  
 Asian  
 Other

**Passenger Arrival time at bus stop:**



**Knowledge of Bus Arrival**

Yes  
 No

**Minimum Acceptable wait time beyond Scheduled Arrival Time (minutes):**

**Maximum Wait Time beyond which you would consider alternative transportation mode**

**What alternative mode of transportation would you consider if the bus is delayed beyond your maximum wait time?**

**Figure 7. Survey Form**



**Figure 8. Patron Surveyed at a Selected Bus Stop**

### **Bus Operational Data**

Bus operational data was collected at each of the 78 selected bus stops. The data was collected by installing video recording cameras at the bus stops. The video recordings took place on weekdays, over a 12-hour duration from 6:30 AM to 6:30 PM. The following data was obtained of each bus arrival event via video playback:

- i. Bus arrival time: a bus was determined to have arrived at a bus stop when it came to a complete stop for boarding and alighting of passengers.
- ii. Bus departure time: a bus was determined to have departed a bus stop when the last passenger had either boarded or alighted the bus and the doors were shut.

A total of 2,070 bus arrival events on 226 routes were extracted, computed and compiled in an EXCEL spreadsheet for further analysis. Figure 9 presents a photograph of one of the video cameras mounted at a selected bus stop.



**Figure 9. Video Camera Installed at a Selected Bus Stop**

From the collected data, bus arrival and departure times were used to compute headway by finding the difference between the arrival time of a bus and that of the preceding bus on the same route. Therefore, headway was computed as:

$$H_A = AT_B - AT_A$$

where  $H_A$  is the actual bus headway,  $AT_A$  is the arrival time of bus A, and  $AT_B$  is the arrival time of bus B.

## DATA ANALYSIS

### Descriptive Statistics

The frequencies, mean, median, and standard deviation were computed for the bus stop characteristics, passenger characteristics and bus operational characteristics, for each bus stop.

### Model Development

#### *Regression Analysis*

To investigate the relationship between the maximum acceptable waiting time and variables such as average headway, knowledge of bus arrival time, presence of shelter, and temperature at the bus stops, multiple linear regression analyses were conducted. The regression models were developed for A.M. peak, mid-day off-peak, and P.M. peak periods, indexed as 1, 2, and 3 respectively. The multiple regression models for maximum acceptable wait time take the following form:

$$MAWT_i = \beta_{0i} + T\beta_{1i} + AH\beta_{2i} + KBAT\beta_{3i} + PS\beta_{4i} + \varepsilon$$

where

*MAWT* = Maximum Acceptable wait time

*AH* = Average Headway

*T* = Temperature

*KBAT* = Knowledge of Bus Arrival Time

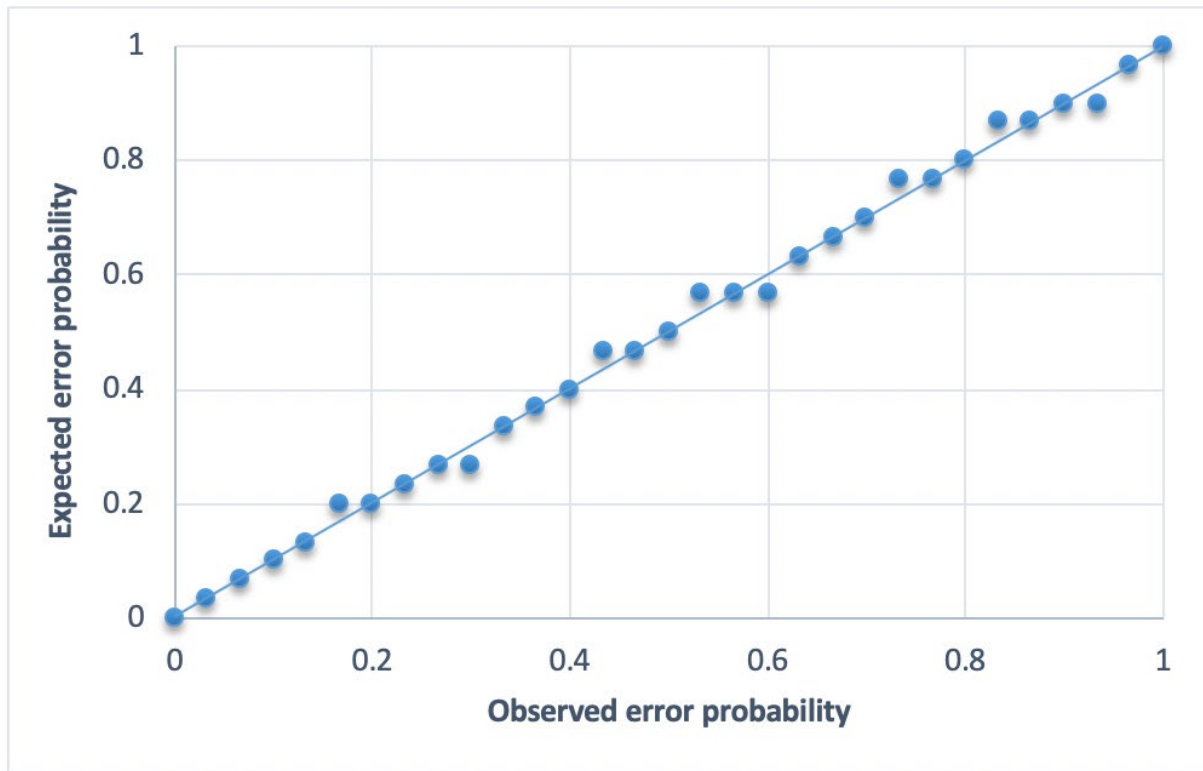
*PS* = Presence of Shelter

*MAWT* is the dependent variable while *T*, *AH*, *KBAT* and *PS* are the independent variables. The constants  $\beta_{ki}$  are the regression coefficients, with an associated approximately normally distributed error of  $\varepsilon$  with mean of zero and variance of  $\sigma^2$ , denoted as [ $\varepsilon \sim N(0, \sigma^2)$ ] and indexed as  $k = 0, 1, 2, 3, 4$  for the first, second, third, fourth and fifth regression coefficients respectively.

The variables were tested to ensure that they satisfied the assumptions of normality of errors, no multicollinearity, and homoscedasticity required for the soundness of multiple regression.

### *Normality of errors*

A sound multiple regression model requires that the errors or residual terms are randomly distributed. Therefore, the residuals should approximate the random errors that establish the relationship between the explanatory variables and the response variables. The normality of errors assumption is tested using a normal probability plot. The observed cumulative probabilities of the standardized residuals are plotted against the expected cumulative probabilities of the standardized residuals. If the errors are normally distributed, the plotted points will approximate a straight diagonal line as shown in Figure 10.



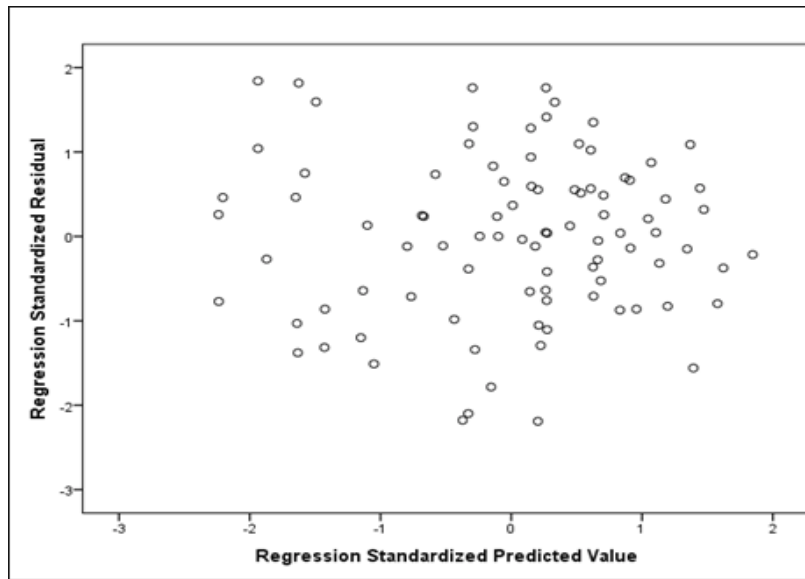
**Figure 10. Example Normal Probability Plot**

### *Multicollinearity*

Multicollinearity is a state of high intercorrelations among the independent variables. If present in a data set, statistical inferences made from the data may not be valid. In addition, multicollinearity may cause the regression coefficients to not be estimated precisely, and the standard errors to be increased. Overall, it reduces the degree of confidence of the resulting model. Multicollinearity is tested using a correlation matrix and Variance Inflation Factor (VIF) (the ratio of the variance of the model with multiple variables to the variance of the model with one variable). Usually, correlation between variables which are higher than 0.5 are considered highly correlated. Also, multicollinearity is considered to be present when the VIF of a variable is greater than 10.<sup>[54]</sup>

### *Homoscedacity*

Homoscedacity is the condition where the residual term is the same across all values of the independent variables. Violations of this condition, termed heteroscedacity, cause significance tests of the regression coefficients and estimations of confidence intervals to be inaccurate. The test for homoscedacity is conducted by observing the scatter plot of the regression standardized residuals against the predicted values. An even distribution about the zero line, as shown in Figure 11, indicates that the assumption of homoscedacity is met.



**Figure 11. Example Scatter Plot showing Homoscedacity**

### **Model Evaluation**

The multiple regression models were evaluated using the  $p$ -values of the F statistics,  $R^2$ , and adjusted  $R^2$ . These evaluating tool are used to assess the performance of the models.

#### *F-test*

The F-test evaluates the null hypothesis that, for the population from which a sample was drawn, all regression coefficients are equal to zero, against the alternative hypothesis that at least one regression coefficient is not. Thus, the F-test determines whether the proposed relationship between the response variable and the set of predictors is statistically significant. The F-test is conducted by taking the ratio

$$F \text{ statistic} = \frac{MSM}{MSE}$$

where MSM is the mean of squares for model and MSE is the mean of squares for the error. The statistical significance of the F statistic is then determined using the  $p$ -value. The significance level for this study was set at 5%.

***R<sup>2</sup>(Coefficient of Determination)***

The coefficient of determination,  $R^2$ , is a measure of the goodness-of-fit of a model. It is defined as the percentage of the variance of the dependent variable that can be explained by the model. R-squared is expressed mathematically as:

$$R^2 = \frac{SST - SSE}{SST}$$

where  $SST$  = Sum of Squares Total (sum of the squares of the difference of the dependent variable and its mean)

$SSE$  = Sum of Squares of Error (sum of the squares of the difference of the predicted dependent variable from actual values of the data)

Generally, increases as predictors are added to the model. However, this increase does not always result in the actual improvement of the model, as this could also be an indication of overfitting of the model. To remedy this effect, an adjusted  $R^2$  is also used to assess the model.

***Adjusted R<sup>2</sup>***

Like,  $R^2$ ,  $R^2_{adjusted}$  is a measure of the percentage of total variance in the dependent variable that is explained by the model. Unlike  $R^2$ ,  $R^2_{adjusted}$  takes into account the model's degrees of freedom, paying a penalty when too many predictor variables are added;  $R^2_{adjusted}$  will decrease as independent variables are added, if the increase in model fit is not enough to make up for the loss of degrees of freedom. It is given by

$$R^2_{adjusted} = 1 - \frac{MSE}{MST}$$

where  $MSE$  = Mean of Squares Total

$MST$  = Mean of Squares for Error

***Model Testing***

Model testing is the process of determining if the regression model provides acceptable explanation of variations in the data. The proposed prediction model was tested using the Kolmogorov-Smirnov (K-S), used to determine whether data follows a specified distribution; in this case it was used to check the normality assumption required by ANOVA. A random sample (the variable whose normality is being tested)  $x_1, x_2, \dots, x_m$  is taken from a population and is compared to the hypothesized distribution function to determine if the random sample's distribution is equal to the hypothesized distribution,

$$H_0: F_{1,n}(x_i) = F_{2,n}(x_2);$$

for all  $x$ , where  $F_{1,n}$  and  $F_{2,n}$  are empirical cumulative distribution functions of the observed and predicted datasets. The  $K$ -S test calculates a test statistic  $D$ , defined as

$$D_{n,n'} = \sup_x |F_{1,n}(x) - F_{2,n}(x)|$$

where,  $\sup$  is the supremum function. The null hypothesis is rejected at significance level  $\alpha$  if

$$D_{n,n'} > c(\alpha) \sqrt{\frac{n+n'}{nn'}}$$

where,  $n$  and  $n'$  are the sample sizes of the respective samples. For each  $\alpha$  level, Table 5 presents the critical,  $c$  value ( $\alpha$ ).

**Table 5. Critical Values of ( $\alpha$ )**

$c(\alpha)$	$\alpha$
1.22	0.10
1.36	0.05
1.48	0.025
1.63	0.01
1.73	0.005
1.95	0.001

### *Hypothesis Testing*

The test statistic used in this study for the comparison is the mean. The hypotheses that there is a significant difference in the average MAWT of passengers based on their gender and ethnicity was also tested, at a 5% significance level.

### *Difference in AWT Based on Gender*

The null hypothesis for this test was that there is no effect of a patron's gender on their MAWT, and the alternative hypothesis was that there is an effect:

$$H_0: X_1 = X_2$$

$$H_A: X_1 \neq X_2$$

where

$X_1$  = mean MAWT of female patrons

$X_2$  = mean MAWT of male patrons



*Difference in AWT Based on Ethnicity*

The null hypothesis was that there is no effect of a patron's ethnicity on their MAWT, and the alternative hypothesis was that there is an effect:

$$H_o: Y_1 = Y_2 = Y_3 = Y_4 = Y_5$$

$$H_A: \sim (Y_1 = Y_2 = Y_3 = Y_4 = Y_5)$$

where,  $Y_1$  = mean MAWT of Black/African American patrons

$Y_2$  = mean MAWT of White patrons

$Y_3$  = mean MAWT of Hispanic patrons

$Y_4$  = mean MAWT of Asian patrons

$Y_5$  = mean MAWT of Other ethnicity patrons

A preliminary analysis of the data to test for the parametric assumptions of normality and equality of variance using the Shapiro-Wilk and Levine Test respectively indicated a statistically significant violation of these assumptions. Because the assumption of normality did not hold, non-parametric tests were needed in order to test for statistically significant differences in MAWT of passengers. A non-parametric Wilcoxon rank-sum test was used to test for an effect of gender, and a non-parametric Kruskal-Wallis test was used to test for an effect of ethnicity.

*Wilcoxon rank-sum Test*

The Wilcoxon rank-sum test is a statistical analysis used to determine whether two independent samples were drawn from the same distribution; it is commonly thought of as a non-parametric alternative to the two-sample t-test, which tests for whether two samples' means significantly differ. This method tests the null hypothesis by comparing the ranks of the observations of the two groups of variables to decide whether or not the difference between the mean ranks are statistically significant. The statistical significance of the Wilcoxon rank-sum test statistic  $W_s$  is determined as follows;

$$\bar{W}_s = \frac{n_1(n_1 + n_2 + 1)}{2}$$

The Standard Error of the test statistic is then computed as,

$$SE_{\bar{W}_s} = \sqrt{\frac{n_1 n_2 (n_1 + n_2 + 1)}{12}}$$

Further, the z score of the test statistic,  $W_s$  is computed as,

$$z = \frac{W_s - \overline{W_s}}{SE_{\overline{W_s}}}$$

where,

$W_s$  = Wilcoxon rank-sum test statistics

$\overline{W_s}$  = the mean of the test statistics

$SE_{\overline{W_s}}$  = standard error of the test statistic

$n_1$  = sample size of the male patrons

$n_2$  = sample size of female patrons

Z = z score of the test statistic

A z score values greater than 1.96 corresponds to a p-value below 0.05; thus, at a 5% significance level, z scores greater than 1.96 are deemed statistically significant.

### *Kruskal-Wallis Test*

The Kruskal-Wallis Test is used to determine whether two or more independently drawn samples were drawn from the same distribution; a statistically significant result on this test suggests that at least one sample may have been drawn from a different distribution. This method compares the ranks of the observations of three or more groups of a variable to decide whether or not the difference between the mean ranks are statistically significant. The statistical significance of the Kruskal-Wallis test statistic, is determined as follows;

$$H = \frac{12}{N(N+1)} \sum_{i=1}^k \frac{R_i^2}{n_i} - 3(N+1)$$

where,

$H$  = Kruskal-Wallis test statistics

$N$  = total sample size

$R_i$  = the sum of ranks for group i

$N_i$  = the sample size of group i

The H statistic is then compared to a critical value,  $H_c$ , which approximates the chi-square distribution, for the same number of degrees of freedom. If H is higher than  $H_c$ , then the result is statistically significant and we reject the null hypothesis.

## IV. RESULTS

### SURVEY RESULTS

This section presents an overview of the results of the surveys conducted at the selected bus stops.

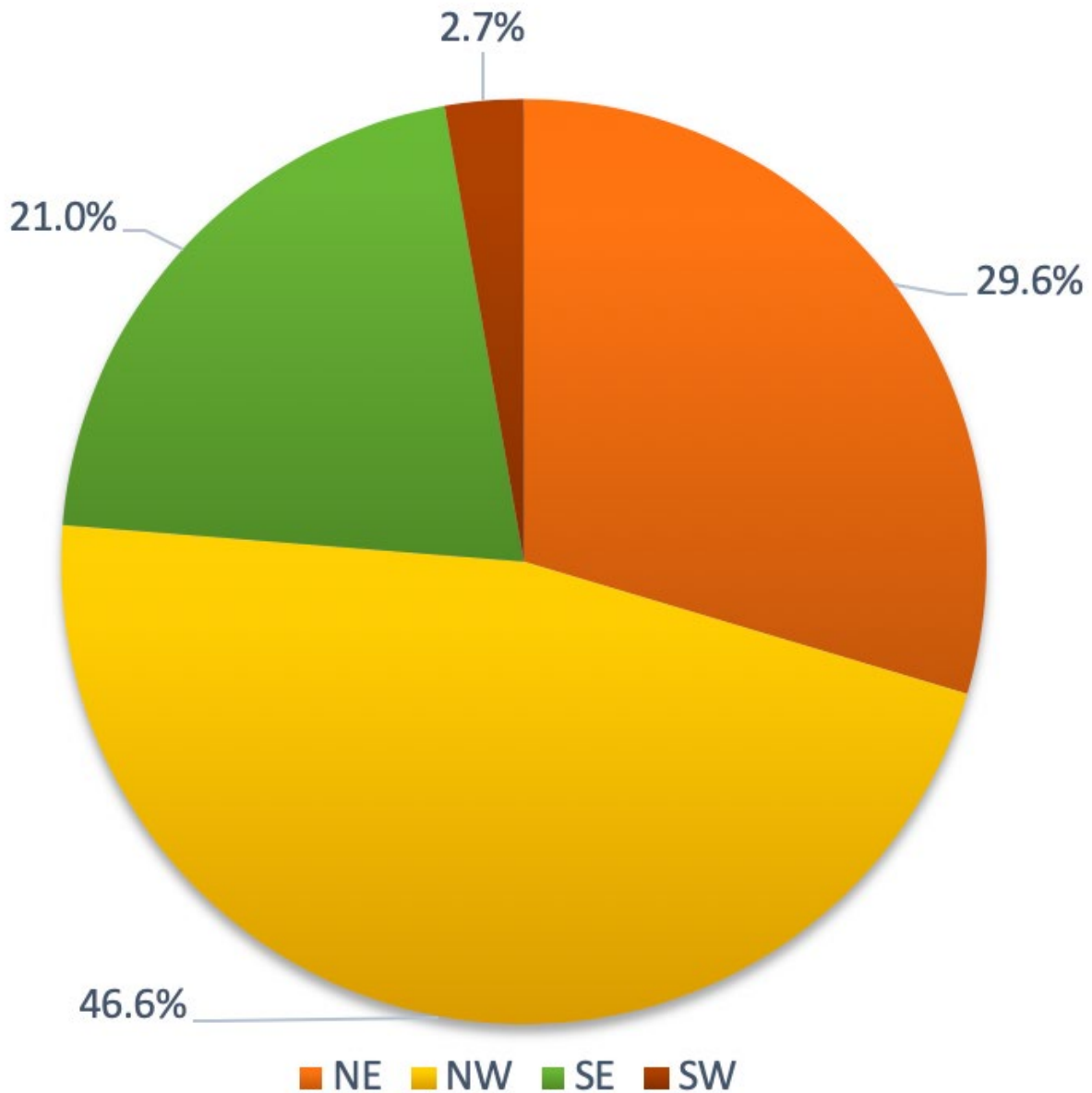
#### Summary Survey Statistics

Table 6 presents a summary of the characteristics of patrons and locations surveyed in this study. Figure 12 represents the percentage of surveys conducted by quadrant.

**Table 6. Survey Statistics Quick Facts**

Total # of patrons surveyed	3,388
Total # of females	1,753
Total # of males	1,635
Total # of White patrons	778
Total # of Black patrons	771
Total # of Hispanic patrons	747
Total # of Asian patrons	545
Total # of "Other" patrons	546
Total # of Locations surveyed	76
Total # of Locations with Shelter	40
Total # of Locations without Shelter	31

Table 6 shows that majority of the patrons that were surveyed were females. Most of the patrons that participated in the survey were White, followed by Black and Hispanic patrons. Most of the surveyed bus stops were located in the North-West (NW) quadrant of the Washington, D.C; as a result, 46.6% of the surveys were conducted in the NW quadrant.



**Figure 12. Percentage of Surveys per Quadrant**

### **Survey Statistics and Trends**

This section presents the descriptive statistics for the surveys conducted at 76 selected bus stops in Washington, D.C. The patrons' characteristics analyzed included gender, ethnicity, arrival time to the bus stop, knowledge of the bus arrival time to the bus stop, minimum and maximum acceptable wait time and choice of alternative mode of transportation. The location characteristics included: presence of bench at bus stop, quadrant, ward and weather temperature.

---

The analysis focused on following:

- *Time*: patron's time of arrival at the bus stop and time of the day;
- *Location*: survey location identified by pre-defined areas such as Ward, Quadrant, and bus stop type;
- *Patron's Characteristics*: gender, ethnicity and patron's knowledge of bus arrival time;
- *Patron's alternate mode*: a patron's next-most-preferred mode of transportation;
- *Environmental Factors*: temperature

### *Time*

The tables and figures in this section present the frequencies and distributions of patron's minimum and maximum acceptable wait times, categorized by day of the week and by time of day. The highlighted cells represent the modal choices.

#### *Acceptable Wait Times by Time of the Day*

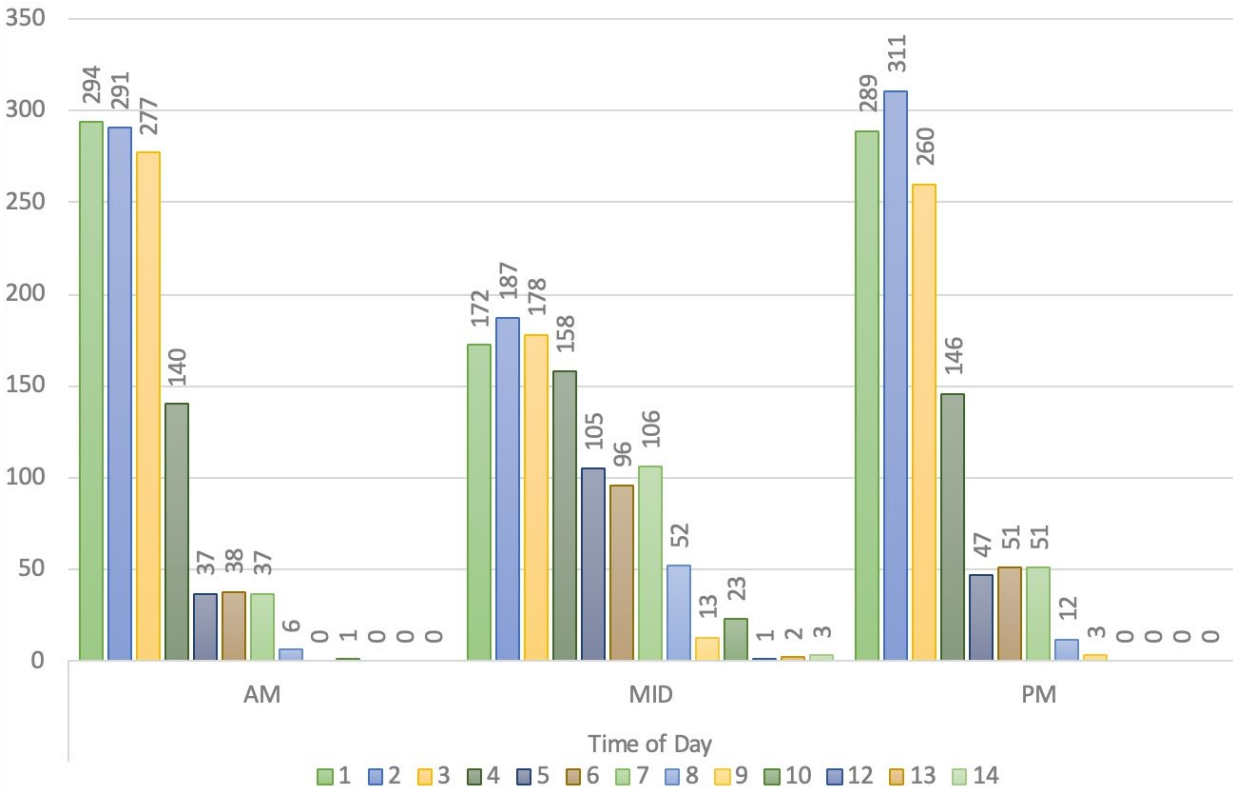
Tables 7 and 8 present the minimum and maximum acceptable wait times for patrons by time of the day. From the Table 7, it can be seen that the modal minimum acceptable wait time for the morning period was 1 minute, while the modal minimum acceptable wait time was 2 minutes during the mid-day and evening periods. Also, the modal maximum acceptable wait time during morning, mid-day and afternoon periods were 7 minutes, 10 minutes and 5 minutes respectively.

Figures 13 and 14 show patrons' choices for minimum and maximum acceptable wait times categorized by time of day. Figure 15 presents the summary of minimum and maximum acceptable wait times by time of the day.

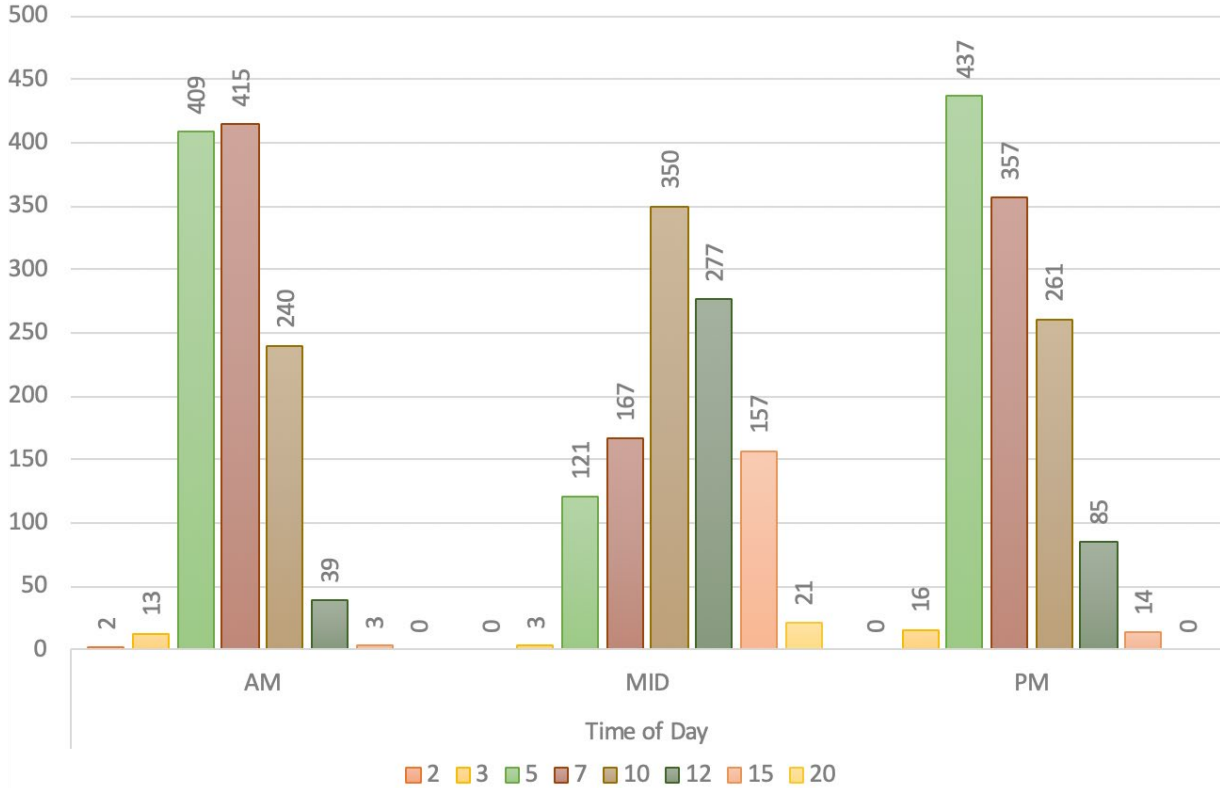
Figure 13 shows that patrons chose shorter acceptable wait times during the morning and afternoon periods. Similarly, Figure 14 shows that maximum acceptable wait times were also lower during the morning and afternoon periods. From Figure 15, it can be observed that most patrons were most likely to wait a longer period of time during the mid-day period, followed by the morning and afternoon periods, respectively.

Table 7. Patrons' Acceptable Wait Times by Time of the Day

	# Minutes	Time of Day		
		AM	MID	PM
Min. AWT	1	294	172	289
	2	291	187	311
	3	277	178	260
	4	140	158	146
	5	37	105	47
	6	38	96	51
	7	37	106	51
	8	6	52	12
	9	0	13	3
	10	1	23	0
	12	0	1	0
	13	0	2	0
	14	0	3	0
	2	2	0	0
Max. AWT	3	13	3	16
	5	409	121	437
	7	415	167	357
	10	240	350	261
	12	39	277	85
	15	3	157	14
	20	0	21	0



**Figure 13. Patrons' Minimum Acceptable Wait Times by Time of the Day**



**Figure 14. Patrons' Maximum Acceptable Wait Times by Time of the Day**



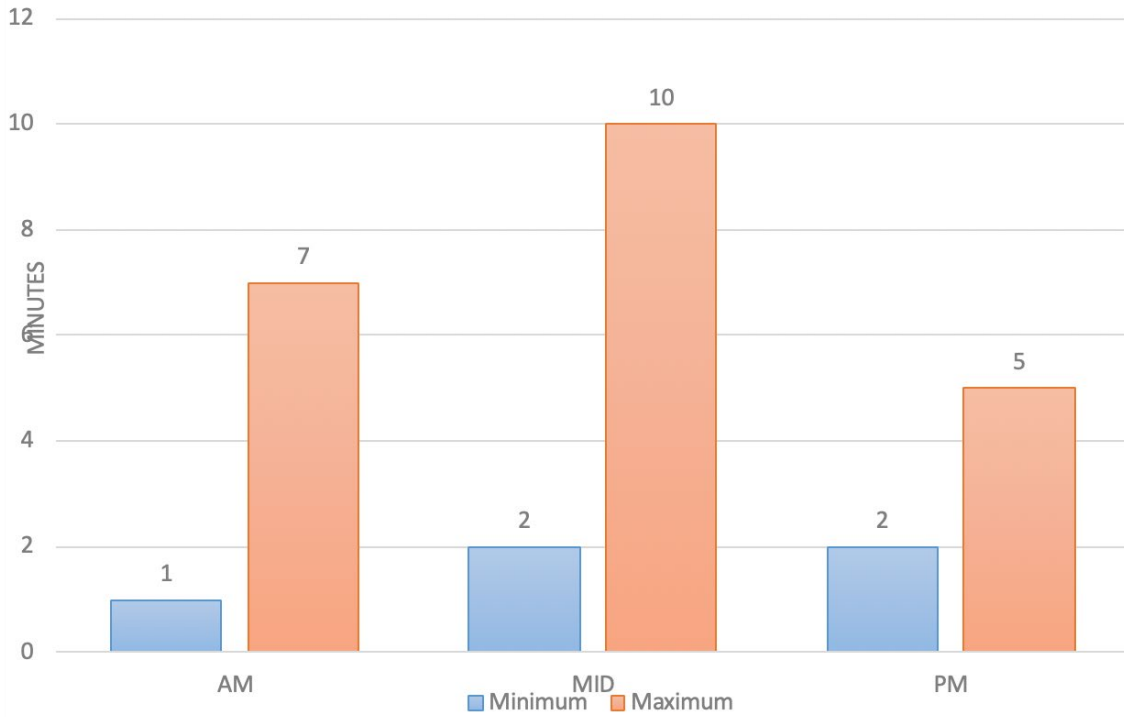


Figure 15. Patrons' Acceptable Wait Times by Time of the Day

Table 8. Relationship between Minimum and Maximum Acceptable Wait Times by Time of the Day

Min AWT	Time of Day / Max. AWT																				
	AM							MID							PM						
	2	3	5	7	10	12	15	2	3	5	7	10	12	15	2	3	5	7	10	12	15
1	2	9	131	103	42	7	0	2	39	30	48	33	19	1	4	149	92	33	8	3	2
2	0	4	135	108	36	8	0	1	38	46	44	46	12	0	12	156	85	46	9	3	0
3	0	0	143	101	30	3	0	0	44	44	44	27	17	2	0	132	85	31	11	1	0
4	0	0	0	103	33	4	0	0	0	47	55	38	14	4	0	0	95	39	12	0	0
5	0	0	0	0	34	3	0	0	0	0	50	37	18	0	0	0	0	35	12	0	0
6	0	0	0	0	33	4	1	0	0	0	55	29	12	0	0	0	0	40	11	0	0
7	0	0	0	0	32	4	1	0	0	0	54	34	15	3	0	0	0	37	13	1	0
8	0	0	0	0	0	6	0	0	0	0	0	33	17	2	0	0	0	0	9	3	0
9	0	0	0	0	0	0	0	0	0	0	0	0	12	1	0	0	0	0	0	3	0
10	0	0	0	0	0	0	1	0	0	0	0	0	21	2	0	0	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0
13	0	0	0	0	0	0	0	0	0	0	0	0	0	2	0	0	0	0	0	0	0
14	0	0	0	0	0	0	0	0	0	0	0	0	0	3	0	0	0	0	0	0	0

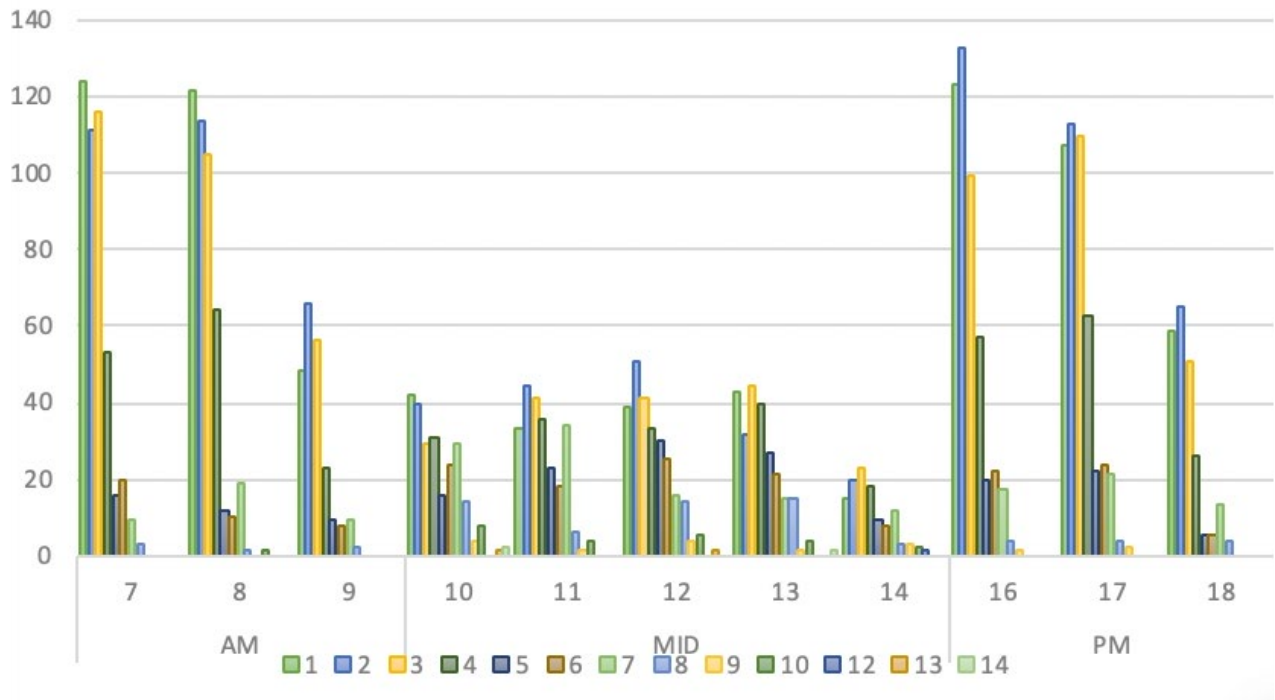
From Table 8, it can be observed that patrons tended to indicate shorter acceptable wait times during the afternoon and morning periods than during the mid-day period (between 4 and 7 minutes).

### Acceptable Wait Times by Hour of the Day

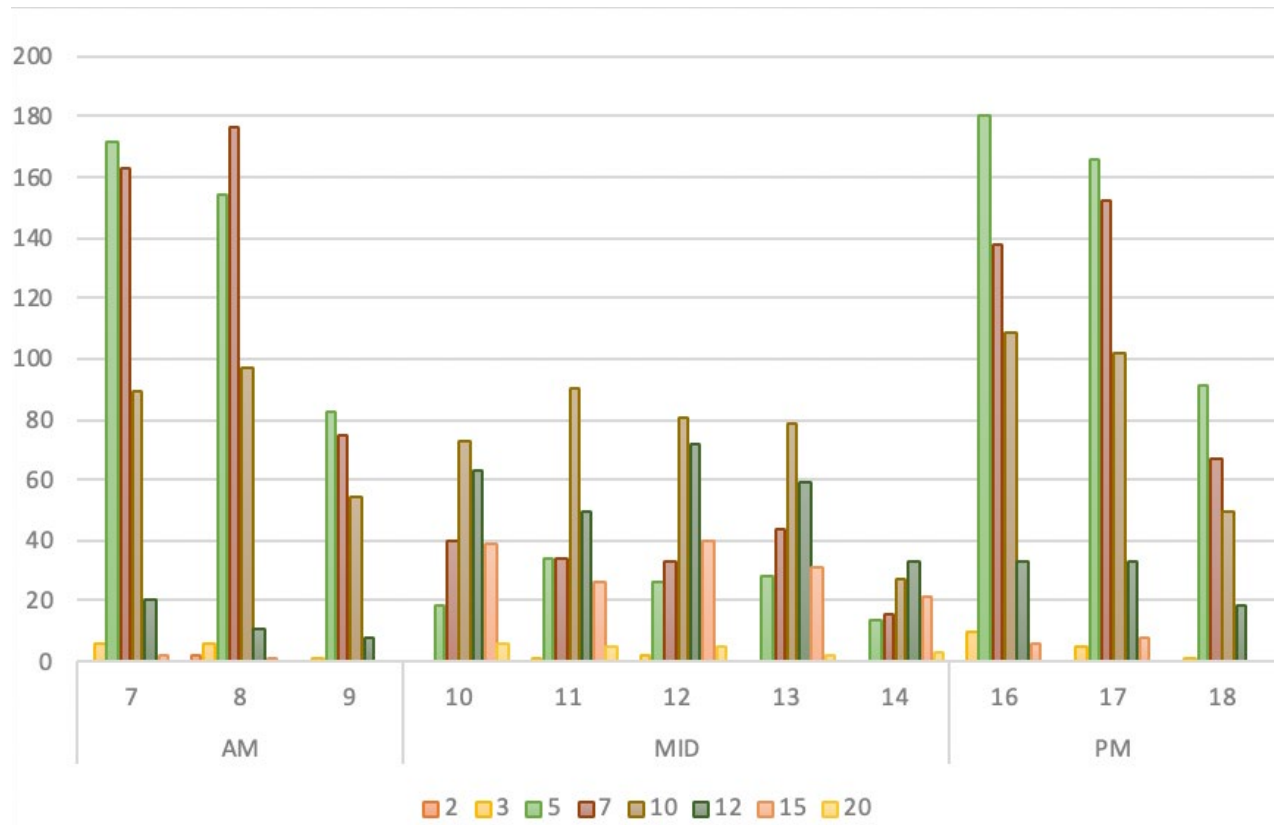
Table 9 along with Figures 16 through 18 present the minimum and maximum acceptable wait times for patrons by hour of the day. From the table, the highest number of patrons chose 1 minute as the minimum acceptable wait time at 7:00 AM, 8:00 AM and 4:00 PM, while 5 minutes was the maximum acceptable wait time for patrons at 4:00 PM.

**Table 9. Patrons' Acceptable Wait Times by Hour of the Day**

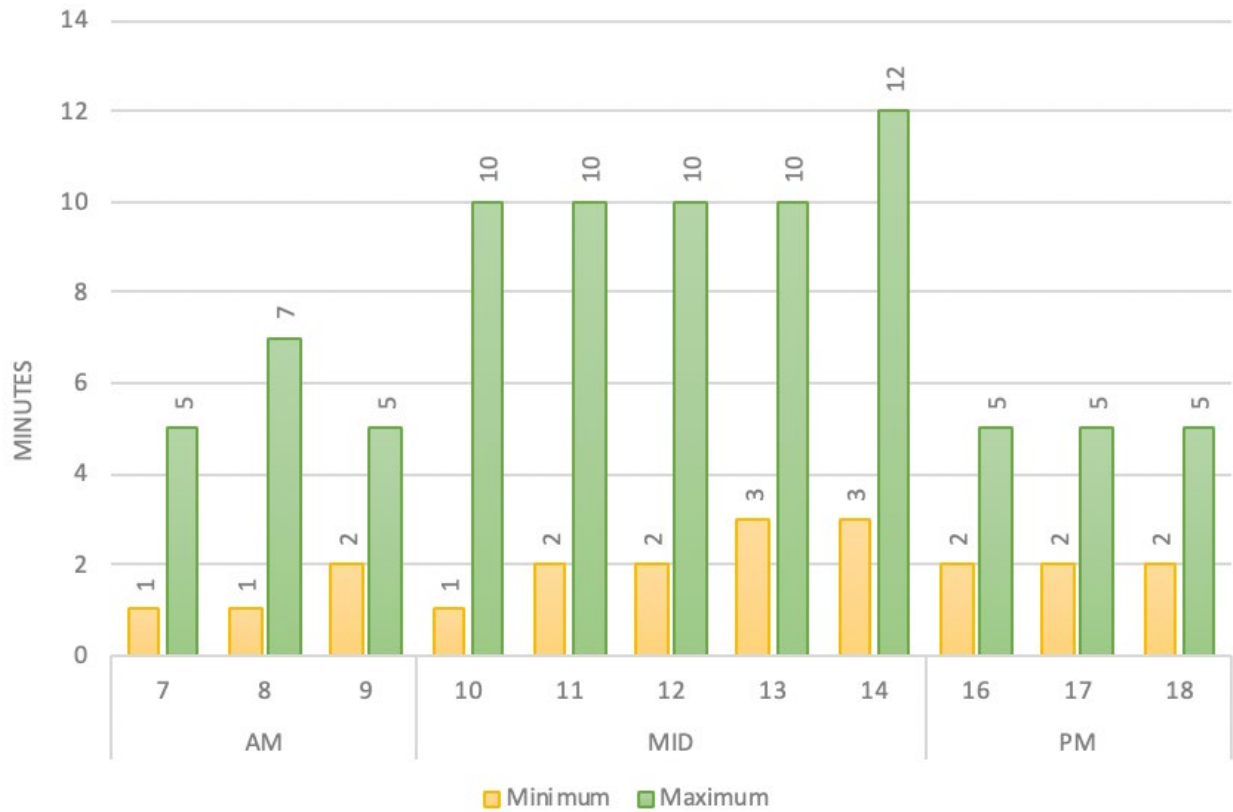
	# Minutes	AM			MID				PM			
		7	8	9	10	11	12	13	14	16	17	18
Min AWT	1	124	122	48	42	33	39	43	15	123	107	59
	2	111	114	66	40	44	51	32	20	133	113	65
	3	116	105	56	29	41	41	44	23	99	110	51
	4	53	64	23	31	36	33	40	18	57	63	26
	5	16	12	9	16	23	30	27	9	20	22	5
	6	20	10	8	24	18	25	21	8	22	24	5
	7	9	19	9	29	34	16	15	12	17	21	13
	8	3	1	2	14	6	14	15	3	4	4	4
	9	0	0	0	4	1	4	1	3	1	2	0
	10	0	1	0	8	4	5	4	2	0	0	0
	12	0	0	0	0	0	0	0	1	0	0	0
	13	0	0	0	1	0	1	0	0	0	0	0
	14	0	0	0	2	0	0	1	0	0	0	0
	Max AWT	2	0	2	0	0	0	0	0	0	0	0
3		6	6	1	0	1	2	0	0	10	5	1
5		172	154	83	19	34	26	28	14	180	166	91
7		163	177	75	40	34	33	44	16	138	152	67
10		89	97	54	73	90	81	79	27	109	102	50
12		20	11	8	63	50	72	59	33	33	33	19
15		2	1	0	39	26	40	31	21	6	8	0
20	0	0	0	6	5	5	2	3	0	0	0	



**Figure 16. Minimum Acceptable Wait Times by Hour of the Day**



**Figure 17. Maximum Acceptable Wait Times by Hour of the Day**



**Figure 18. Patrons' Acceptable Wait Times by Hour of the Day**

### *Location*

The tables and figures in this section present the frequencies of patron's acceptable wait times by Quadrant, Ward and bus stop type. The highlighted cells are the modal choices.

### *Acceptable Wait Times by Quadrant*

This section presents the patrons' minimum and maximum acceptable wait times, organized by Quadrant. The summary of the acceptable wait times by quadrant is presented in Table 10 and shown in Figures 19 through 21. From the table and figures, it can be seen that the modal acceptable wait time in the NW and the SE quadrants was 1 minute, while the modal acceptable wait times for the NE and SW quadrants were 2 and 3 minutes respectively. The modal maximum acceptable wait time was 5 minutes for the NW and NE quadrants, and 7 minutes for the SE and SW quadrants.

Table 10. Patrons' Acceptable Wait Times by Quadrant

	# Minutes	Quadrant			
		NE	NW	SE	SW
Min AWT	1	3	374	165	20
	2	251	373	148	17
	3	208	335	151	21
	4	131	214	88	11
	5	62	68	50	9
	6	63	74	43	5
	7	72	79	35	8
	8	15	39	15	1
	9	1	10	5	0
	10	3	10	10	1
	12	0	0	1	0
	13	0	2	0	0
	14	1	2	0	0
	Max AWT	2	1	0	1
3		13	13	6	0
5		309	468	176	14
7		253	460	194	32
10		296	340	185	30
12		88	202	98	13
15		41	82	47	4
	20	2	15	4	0

Note: NW=Northwest, NE=Northeast, SE=Southeast, SW=Southwest, BR=Border

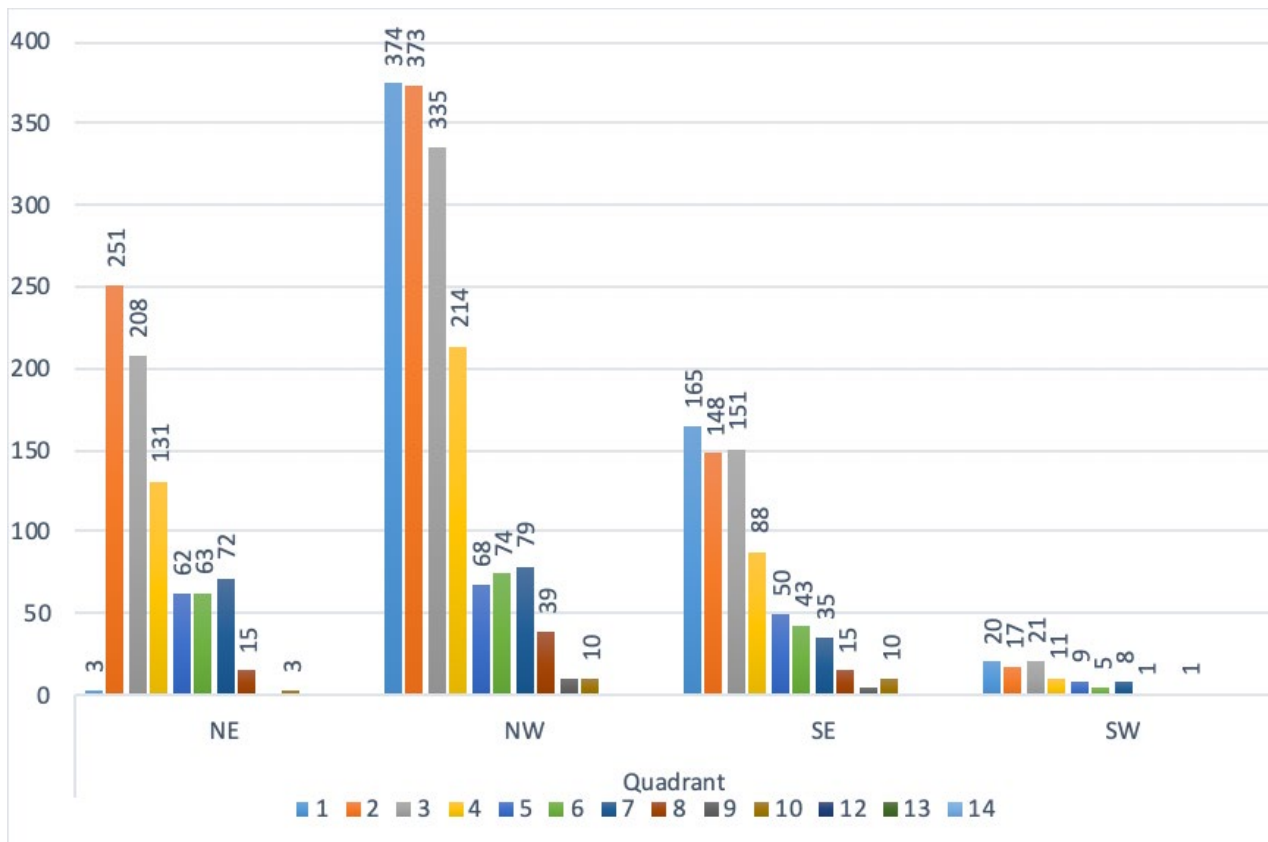


Figure 19. Patrons' Minimum Acceptable Wait Times by Quadrant

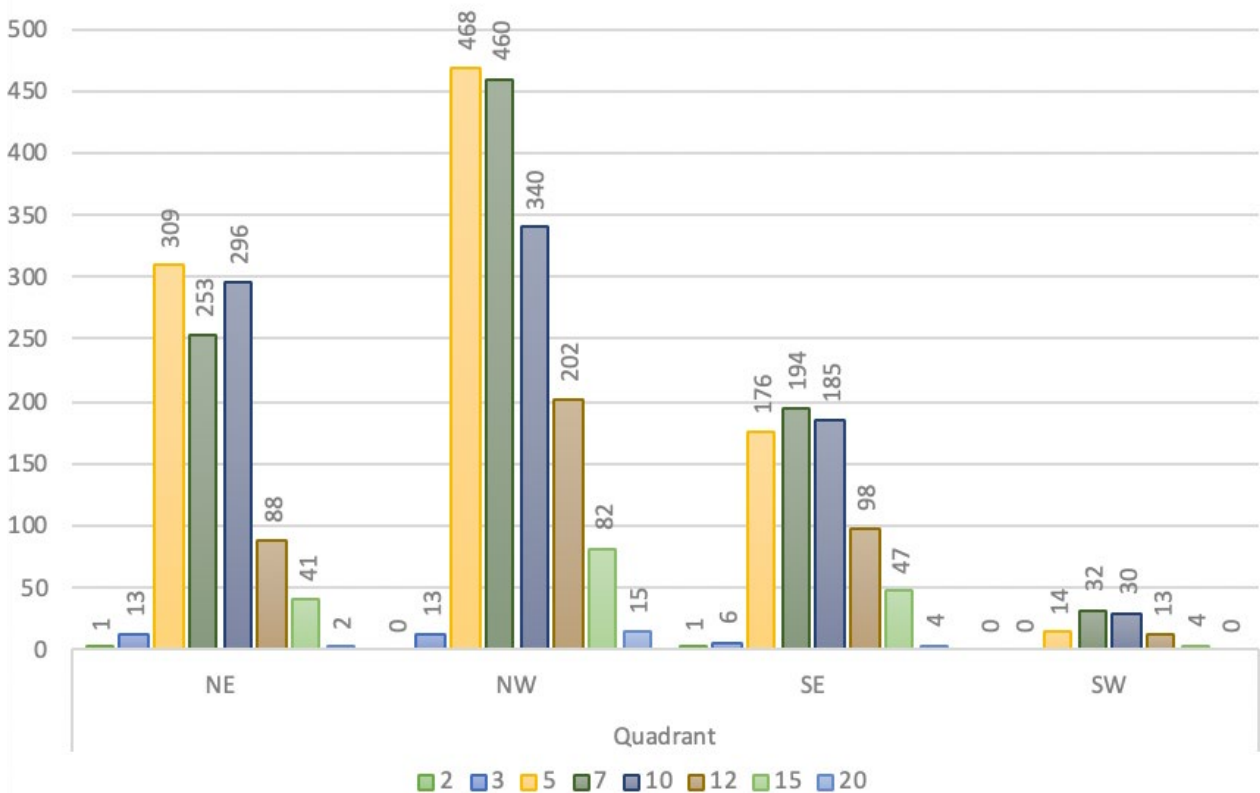
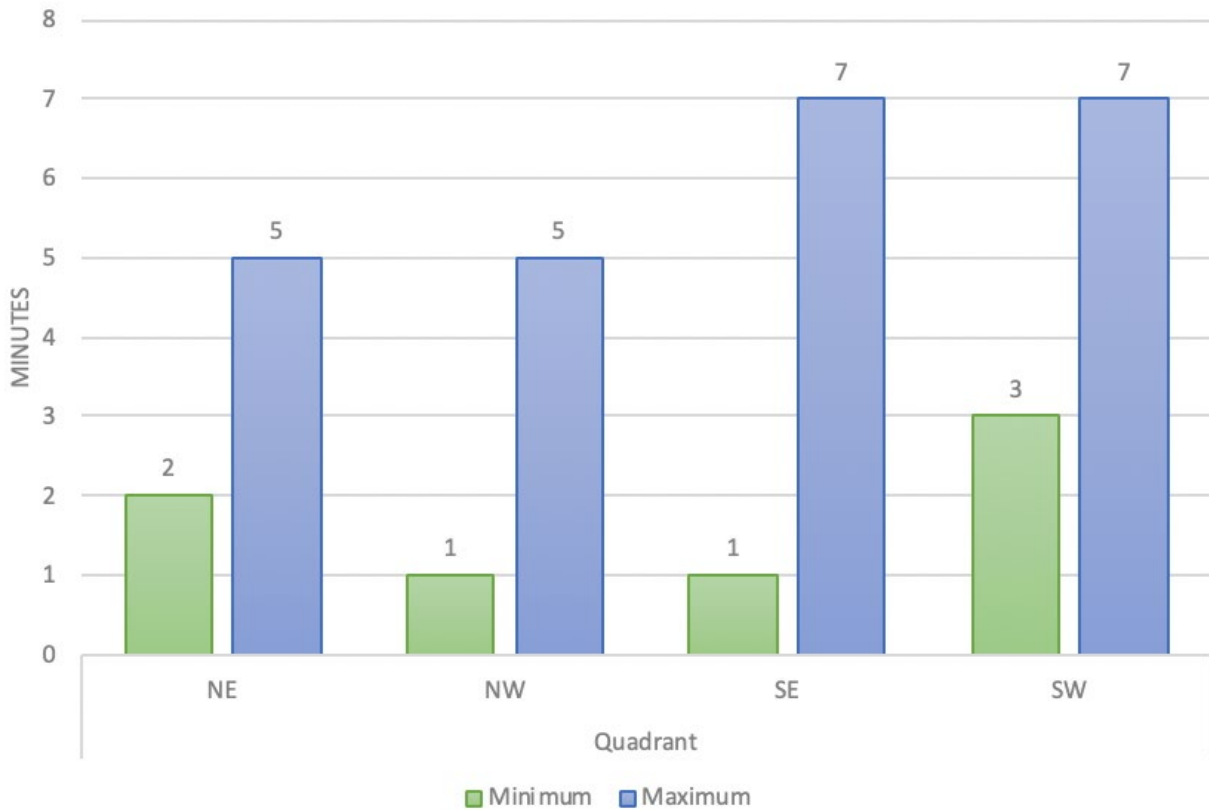


Figure 20. Patrons' Maximum Acceptable Wait Times by Quadrant



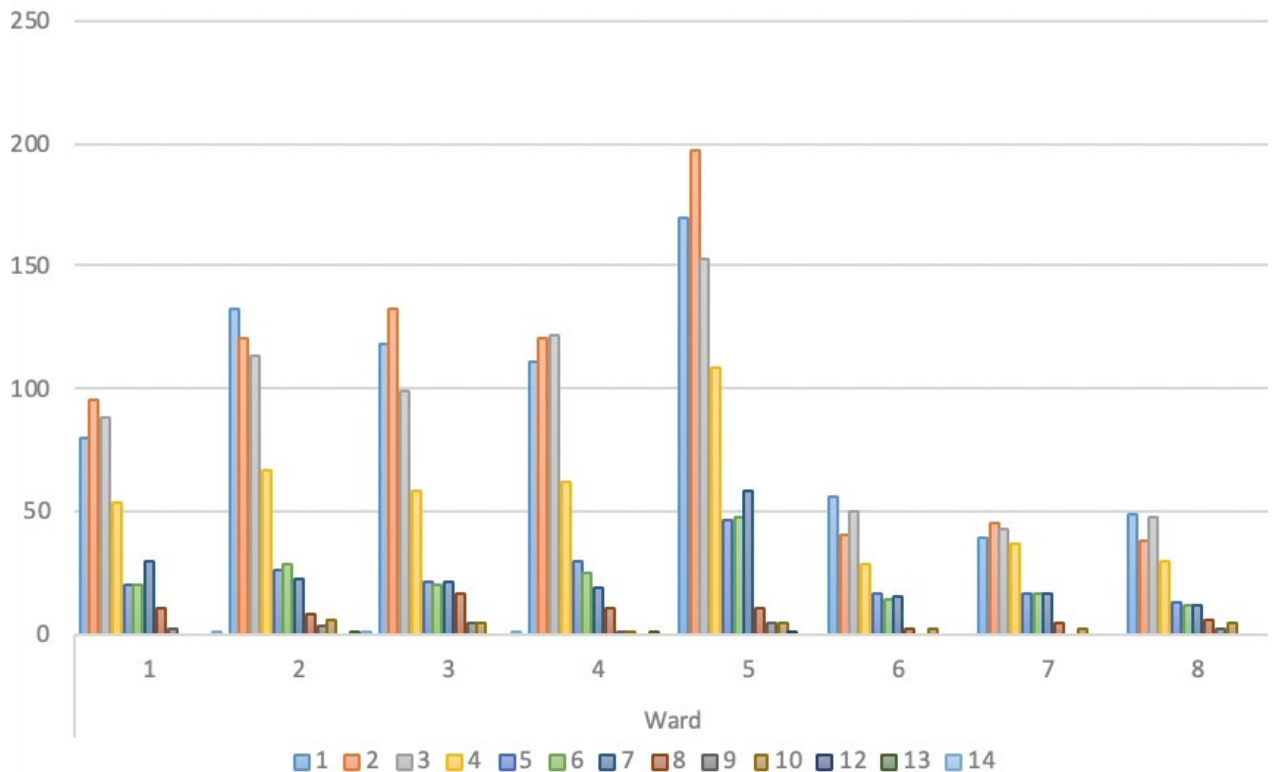
**Figure 21. Patrons' Acceptable Wait Times by Quadrant**

#### *Acceptable Wait Times by Ward*

This section presents the patrons' minimum and maximum acceptable wait times reported in each Ward. Table 11 and Figures 22 through 24 present the summaries of the acceptable wait times by ward. From the table and figures, it can be seen that the modal acceptable wait time was 2 minutes for Wards 1, 3, 5 and 7, and 1 minute for Wards 2, 6 and 8. The modal maximum acceptable wait time was 7 minutes for patrons in Wards 1, 5, 6, 7 and 8.

**Table 11. Patrons' Acceptable Wait Times by Ward**

	# Minutes	Ward							
		1	2	3	4	5	6	7	8
Min AWT	1	80	133	118	111	169	56	39	49
	2	95	120	133	121	197	40	45	38
	3	88	113	99	122	153	50	43	47
	4	53	67	58	62	109	28	37	30
	5	20	26	21	30	46	17	16	13
	6	20	29	20	25	48	14	17	12
	7	30	23	21	19	58	15	16	12
	8	11	8	17	11	11	2	4	6
	9	2	3	4	1	4	0	0	2
	10	0	6	4	1	5	2	2	4
	12	0	0	0	0	1	0	0	0
	13	0	1	0	1	0	0	0	0
	14	1	1	1	0	0	0	0	0
	Max AWT	2	0	1	0	0	1	0	0
3		12	5	5	4	6	0	0	0
5		86	180	204	125	266	41	20	45
7		140	142	101	151	190	79	75	61
10		95	108	75	139	237	71	70	56
12		55	49	78	62	57	28	42	30
15		11	41	27	18	41	5	12	19
20	1	4	6	5	3	0	0	2	



**Figure 22. Patrons' Minimum Acceptable Wait Times by Ward**



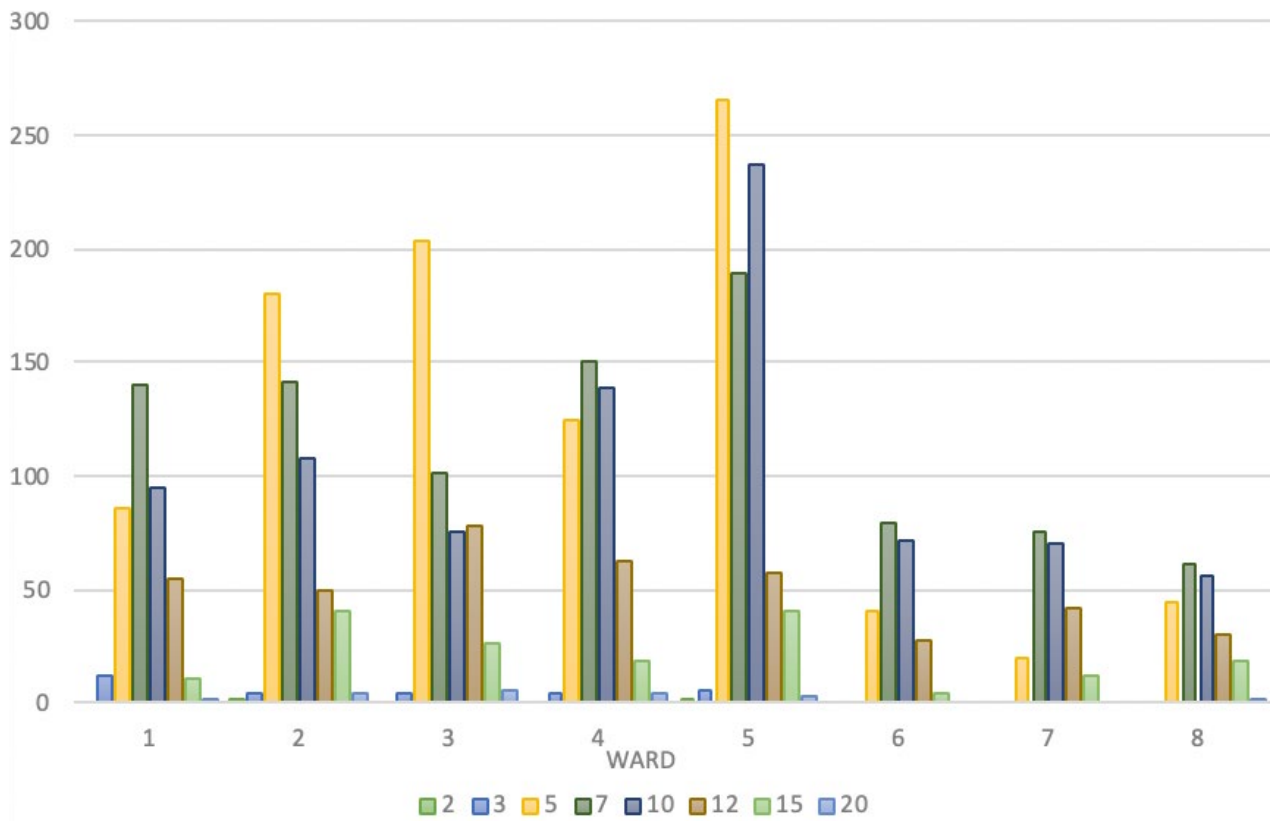


Figure 23. Patrons' Maximum Acceptable Wait Times by Ward

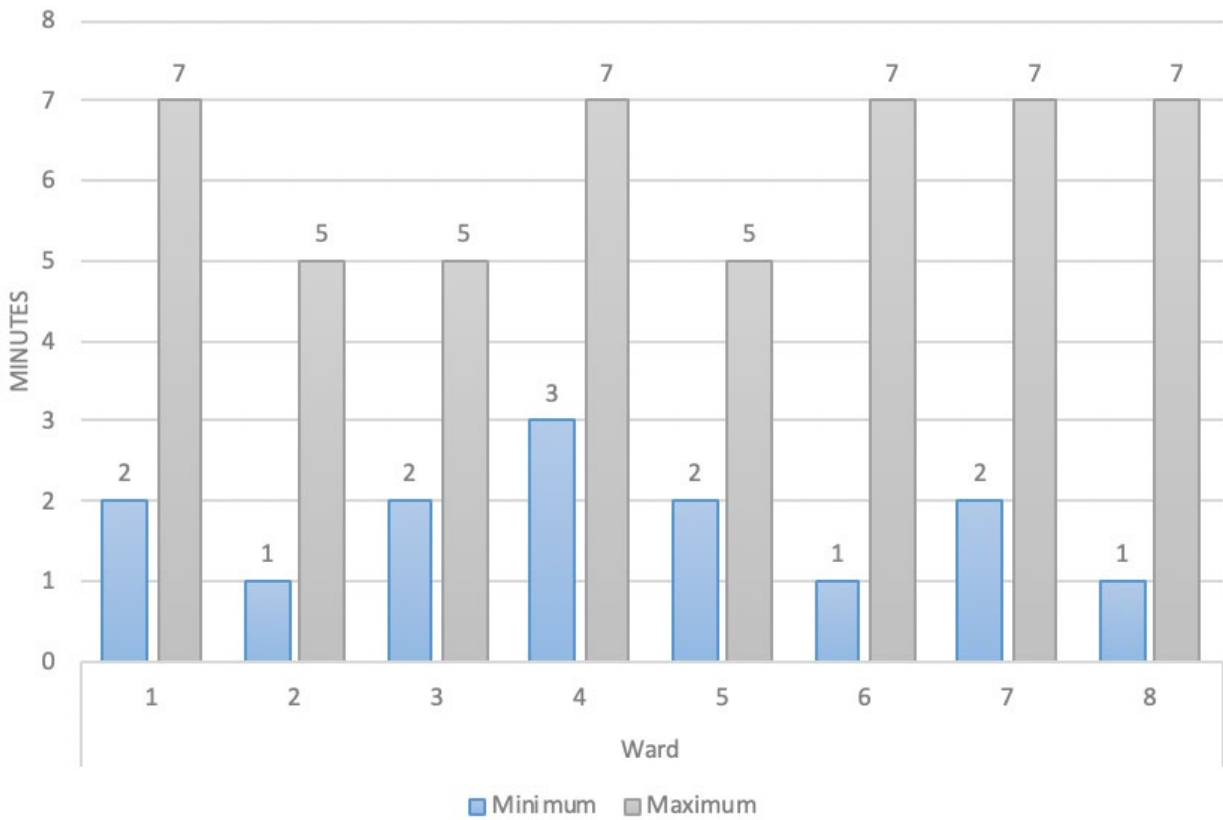


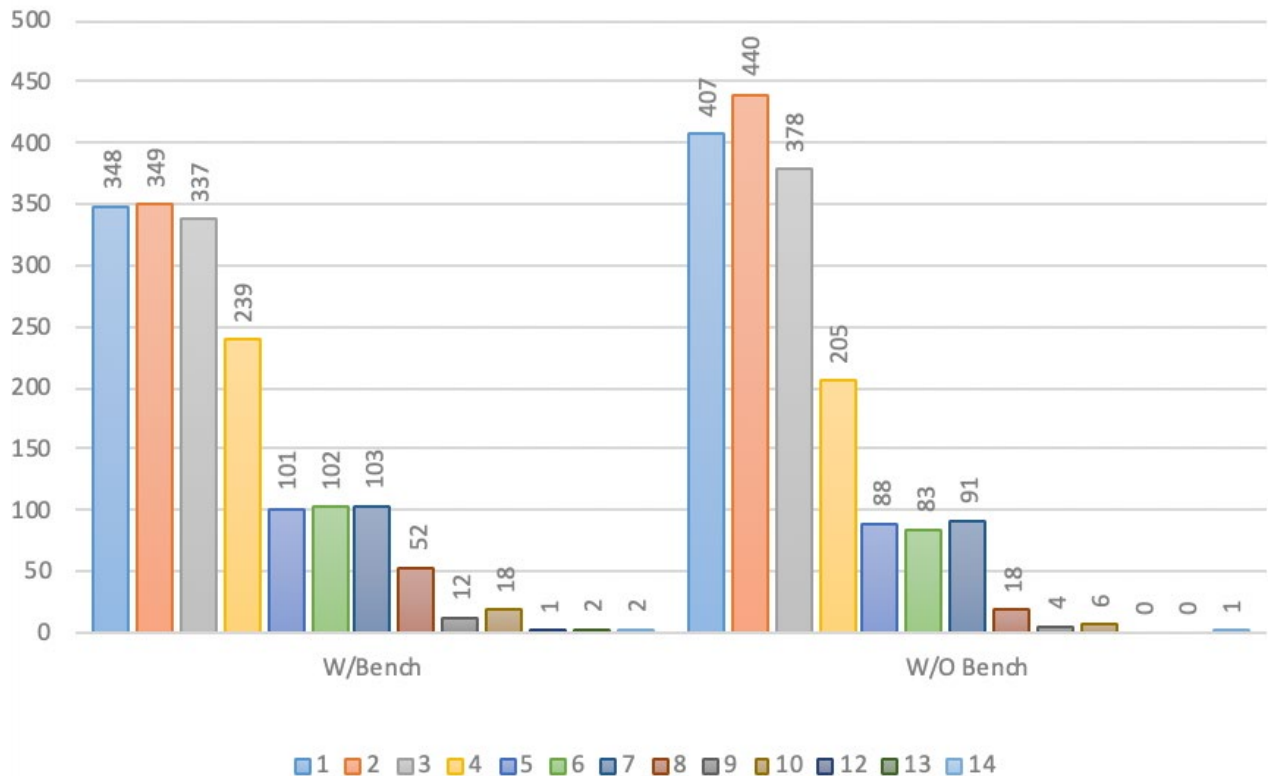
Figure 24. Patrons' Acceptable Wait Times by Ward

### *Acceptable Wait Times by Bus Stop Type*

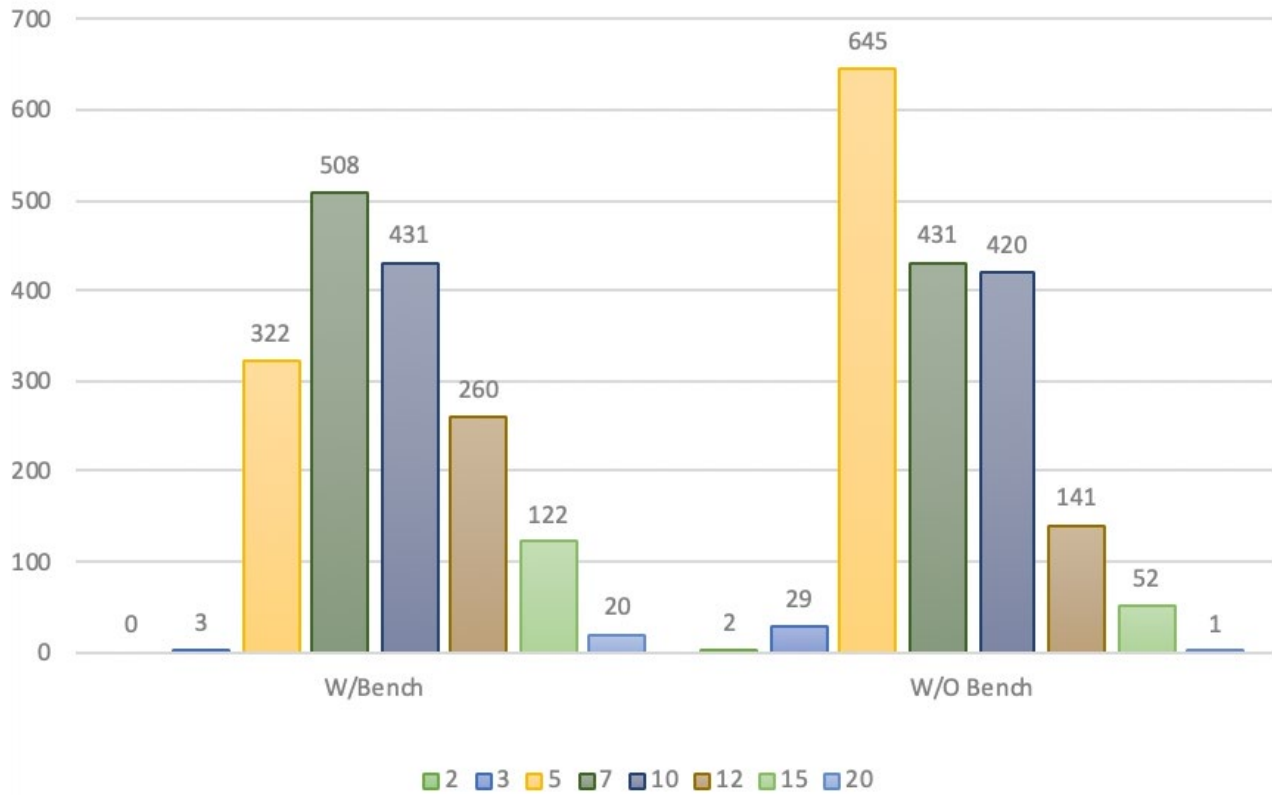
The minimum and maximum acceptable wait times were reported by bus stop type in this section. Table 12 and Figures 25 through 27 present the summary of the acceptable wait times by bus stop type. From the table and figures, it can be seen that the modal maximum acceptable wait time was lower for patrons at bus stops without a bench (5 minutes) than for those at bus stops with a bench (7 minutes).

**Table 12. Patrons' Acceptable Wait Times by Bus Stop Type**

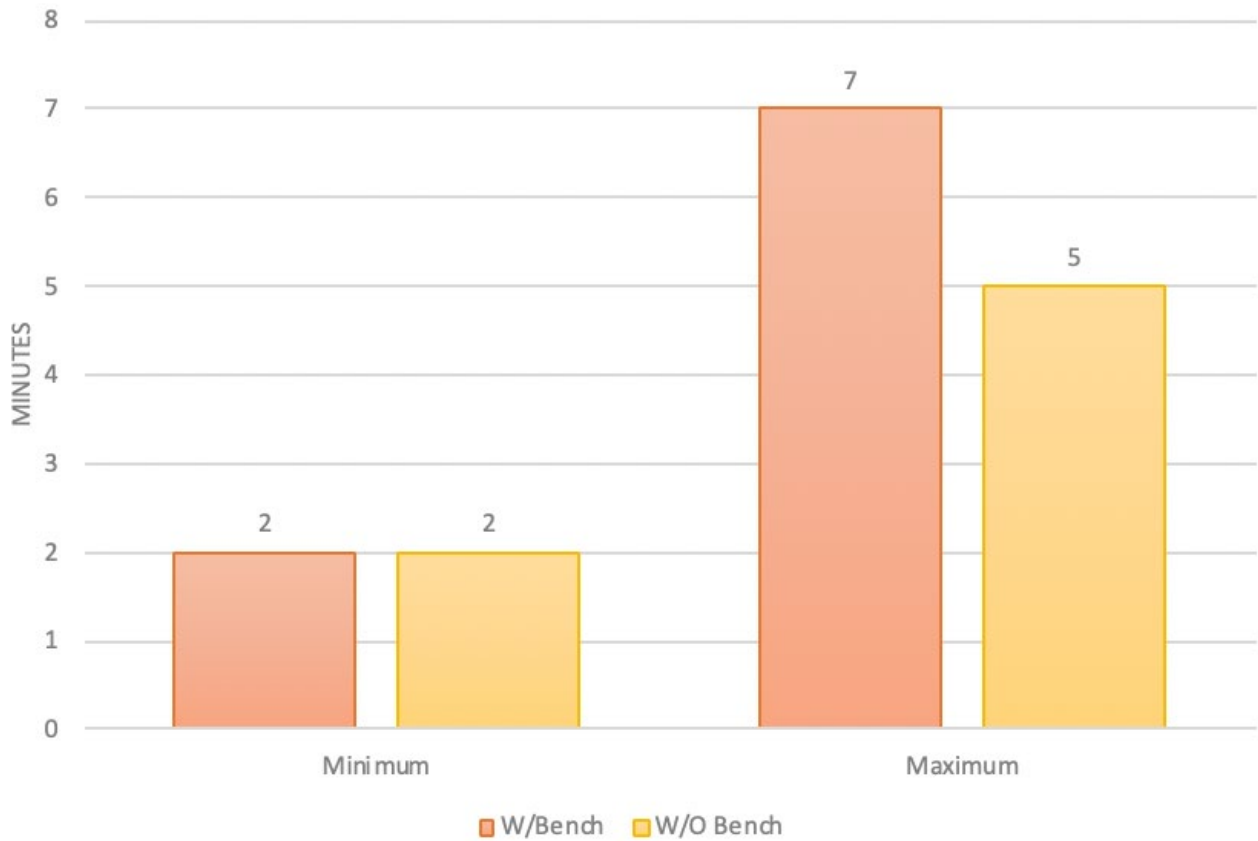
	# Minutes	Presence of Bench	
		Yes	No
Min AWT	1	348	407
	2	<b>349</b>	<b>440</b>
	3	337	378
	4	239	205
	5	101	88
	6	102	83
	7	103	91
	8	52	18
	9	12	4
	10	18	6
	12	1	0
	13	2	0
	14	2	1
	Max AWT	2	0
3		3	29
5		322	<b>645</b>
7		<b>508</b>	431
10		431	420
12		260	141
15		122	52
20	20	1	



**Figure 25. Patrons' Minimum Acceptable Wait Times by Bus Stop Type**



**Figure 26. Patrons' Maximum Acceptable Wait Times by Ward**



**Figure 27. Patrons' Acceptable Wait Times by Presence of Bench**

### Patrons' Characteristics

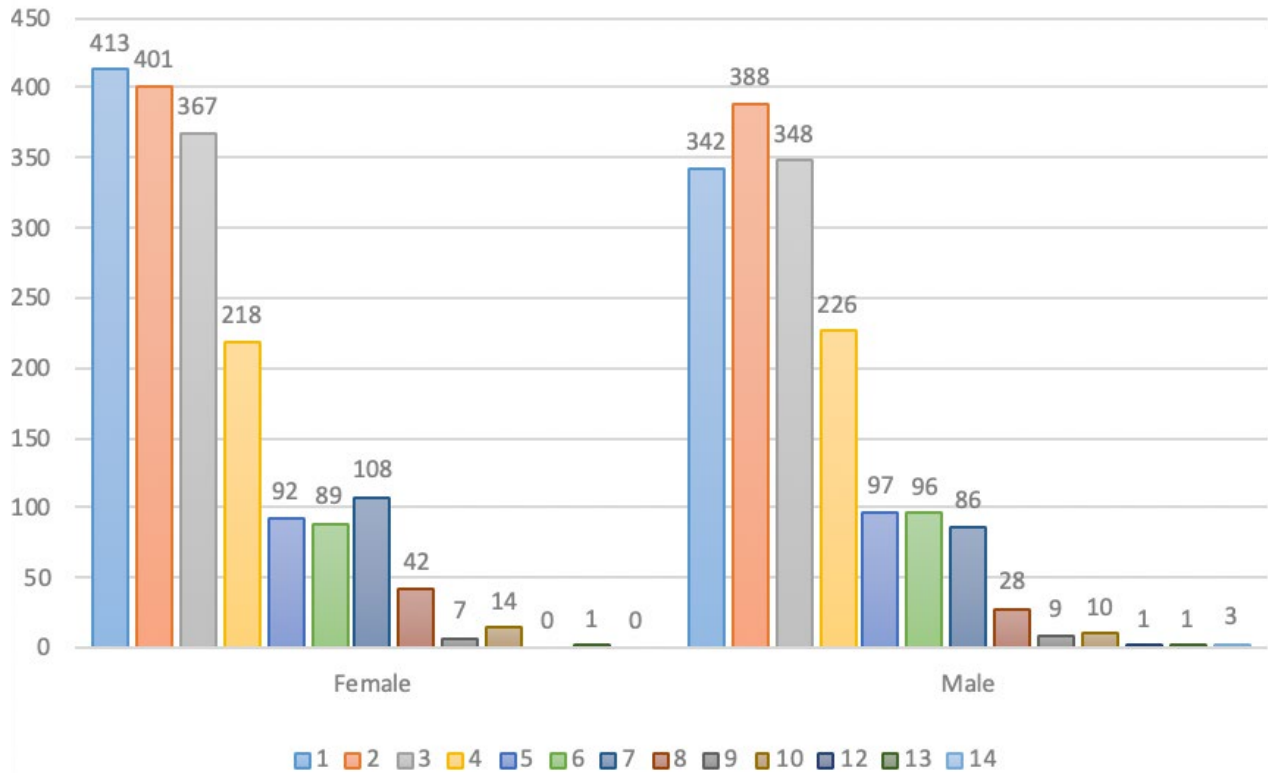
The tables and figures in this section present the frequencies of acceptable wait times categorized by gender, ethnicity and knowledge of bus arrival time.

#### Acceptable Wait Times by Gender

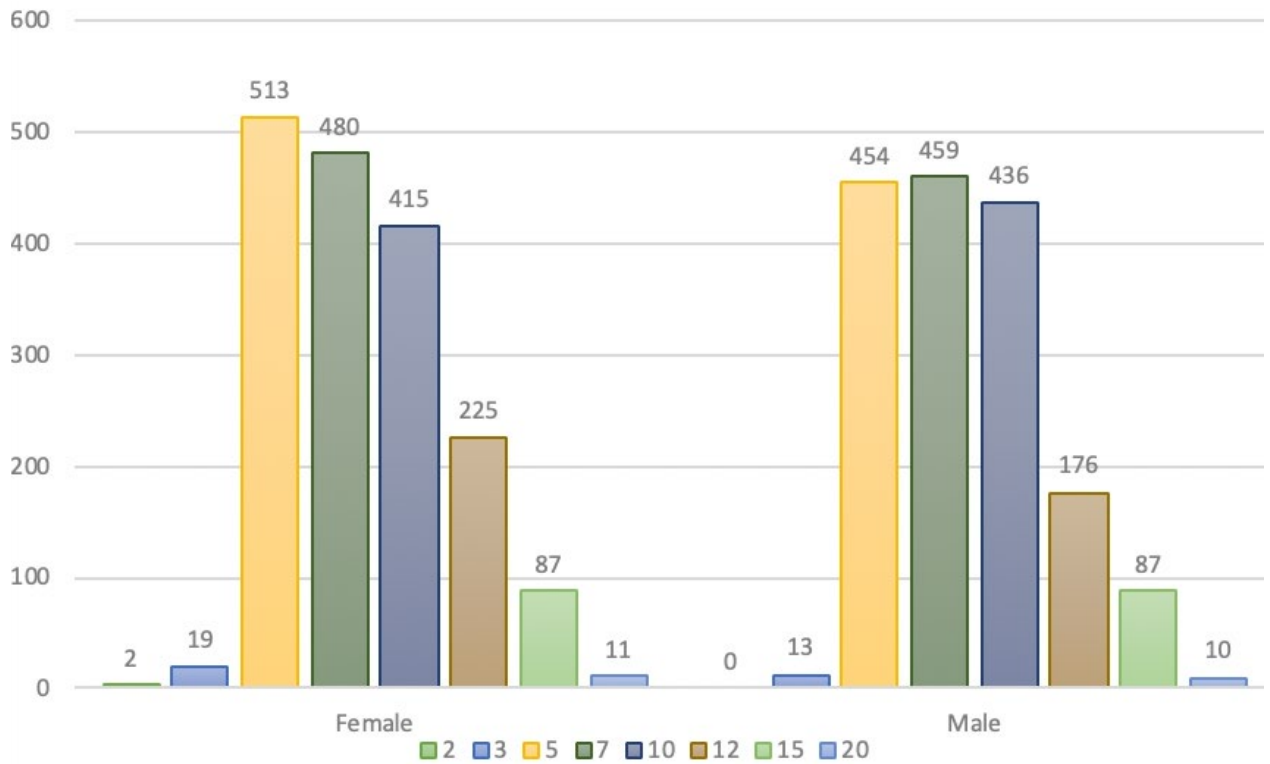
This section presents the minimum and maximum acceptable wait times by gender. The summary of the acceptable wait times by gender is presented in Table 13 and shown in Figures 28 through 30. From the table and figures, it can be seen that the modal maximum wait time was 5 minutes for female patrons, and 7 minutes for male patrons. From Figure 30, it can be observed that male patrons were more willing to wait for longer periods of time than female patrons.

**Table 13. Patrons' Acceptable Wait Times by Gender**

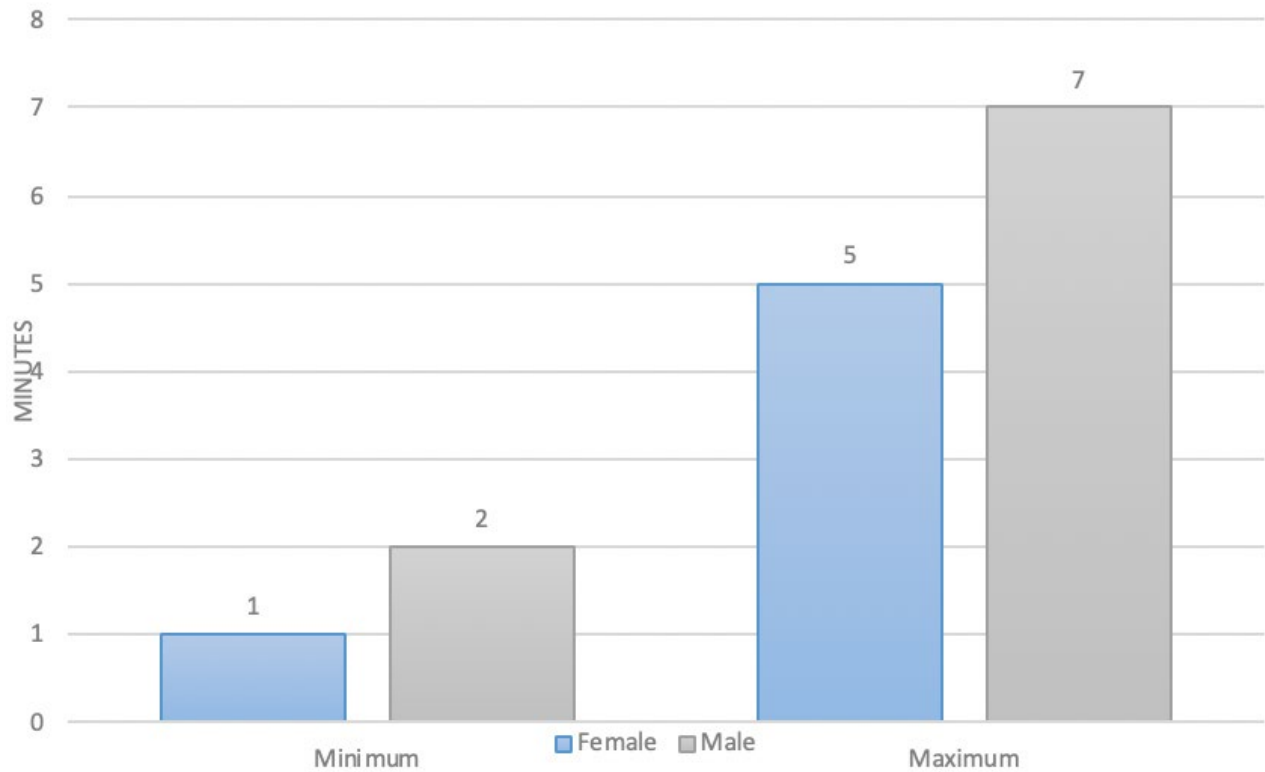
	# Minutes	Gender	
		Female	Male
Min AWT	1	413	342
	2	401	388
	3	367	348
	4	218	226
	5	92	97
	6	89	96
	7	108	86
	8	42	28
	9	7	9
	10	14	10
	12	0	1
	13	1	1
	14	0	3
	Max AWT	2	2
3		19	13
5		513	454
7		480	459
10		415	436
12		225	176
	15	87	87
	20	11	10



**Figure 28. Patrons' Minimum Acceptable Wait Times by Gender**



**Figure 29. Patrons' Maximum Acceptable Wait Times by Gender**



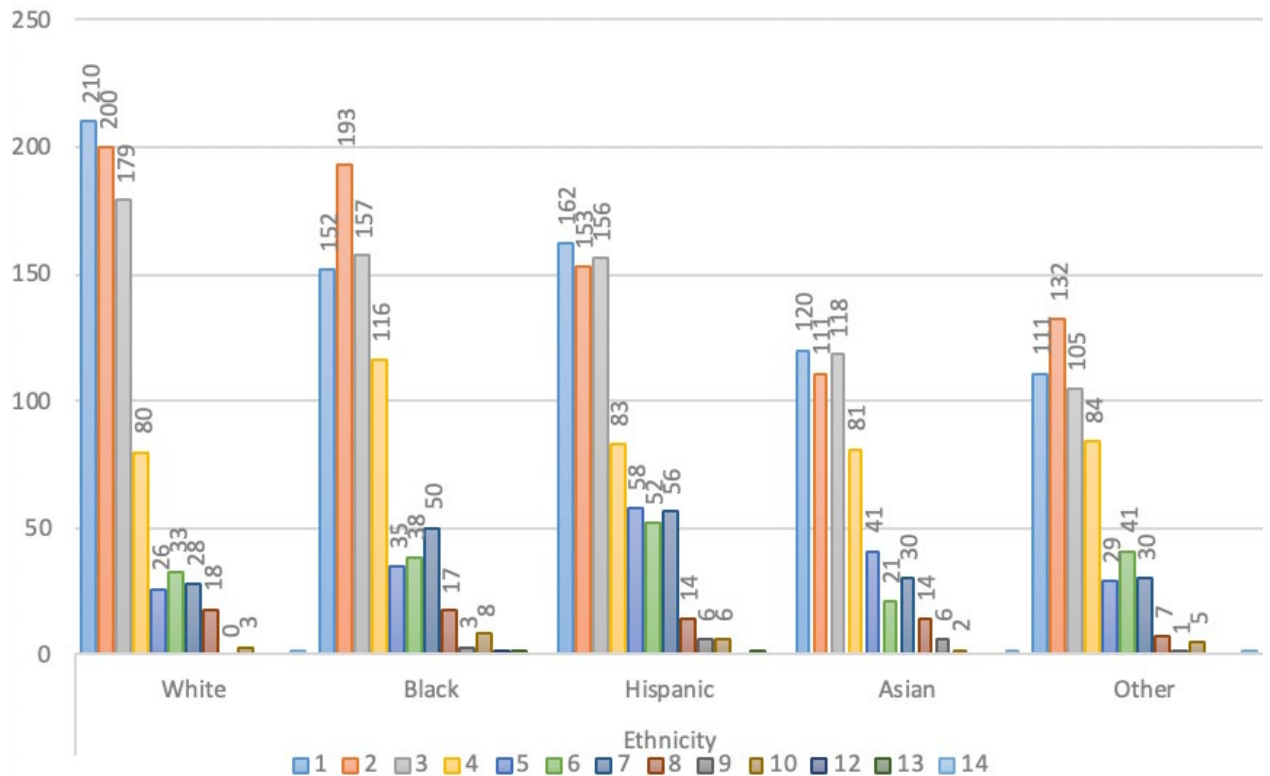
**Figure 30. Patrons' Acceptable Wait Times by Gender**

### *Acceptable Wait Times by Ethnicity*

The minimum and maximum acceptable wait times by ethnicity are presented in this section. The summary of the acceptable wait times by ethnicity is presented in Table 14 and shown in Figures 31 through 33. From the table and figures, it can be seen that the modal acceptable wait times ranged from 1 to 2, for all ethnicities. The modal maximum acceptable wait time was 5 minutes for white patrons, 7 minutes for Black and Asian patrons, and 10 minutes for Hispanic patrons and patrons whose ethnicities were listed as "Other."

**Table 14. Patrons' Acceptable Wait Times by Ethnicity**

	# Minutes	Ethnicity				
		White	Black	Hispanic	Asian	Other
Min AWT	1	210	152	162	120	111
	2	200	193	153	111	132
	3	179	157	156	118	105
	4	80	116	83	81	84
	5	26	35	58	41	29
	6	33	38	52	21	41
	7	28	50	56	30	30
	8	18	17	14	14	7
	9	0	3	6	6	1
	10	3	8	6	2	5
	12	0	1	0	0	0
	13	0	1	1	0	0
	14	1	0	0	1	1
	Max AWT	2	0	0	1	0
3		12	5	9	2	4
5		379	185	187	118	98
7		152	266	174	195	152
10		114	176	233	136	192
12		86	93	98	59	65
20		5	6	3	4	3



**Figure 31. Patrons' Minimum Acceptable Wait Times by Ethnicity**



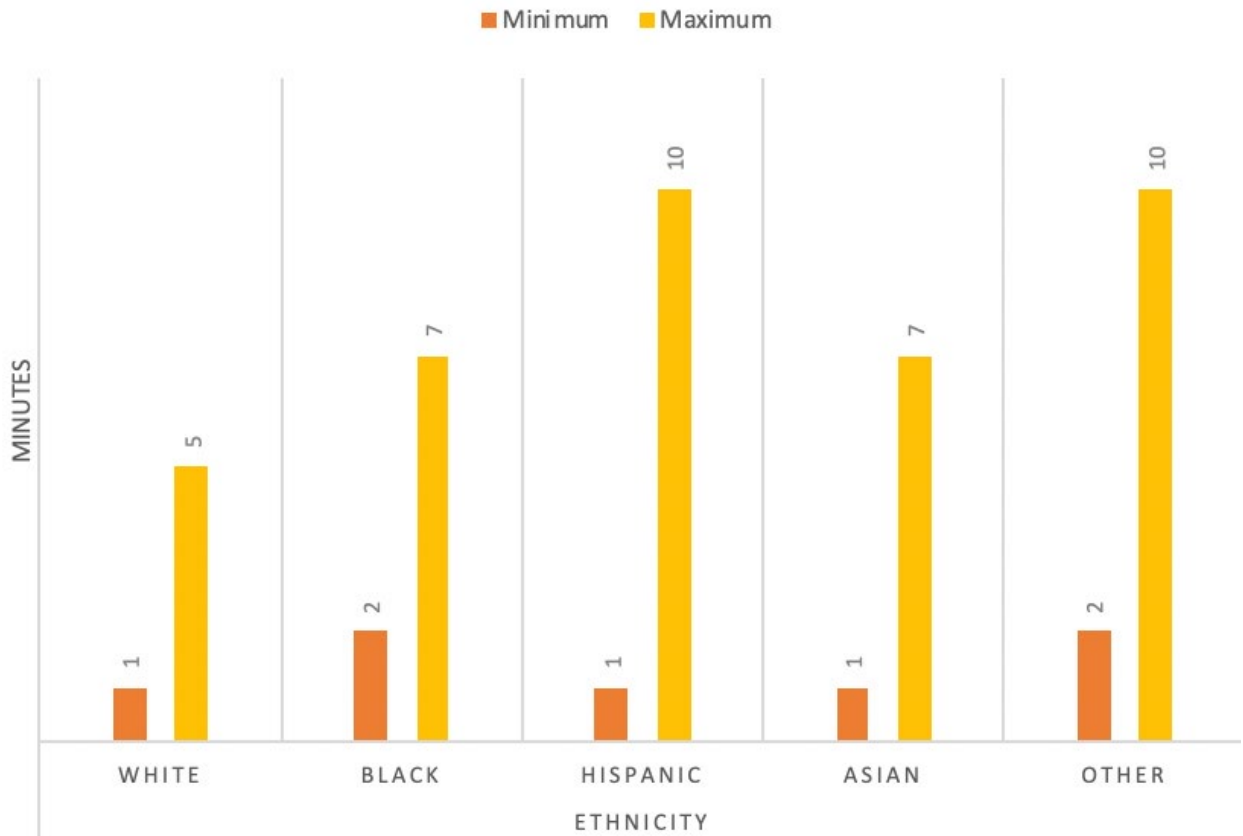


Figure 32. Patrons' Maximum Acceptable Wait Times by Ethnicity

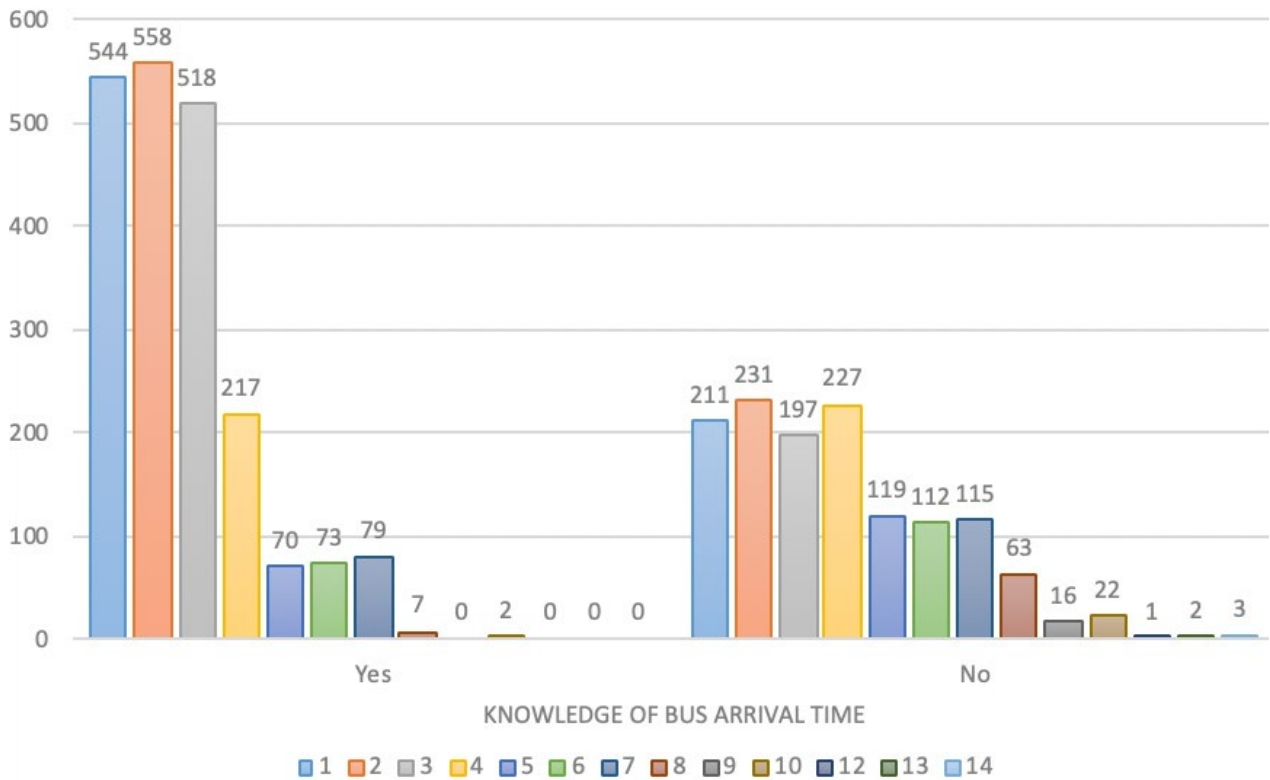


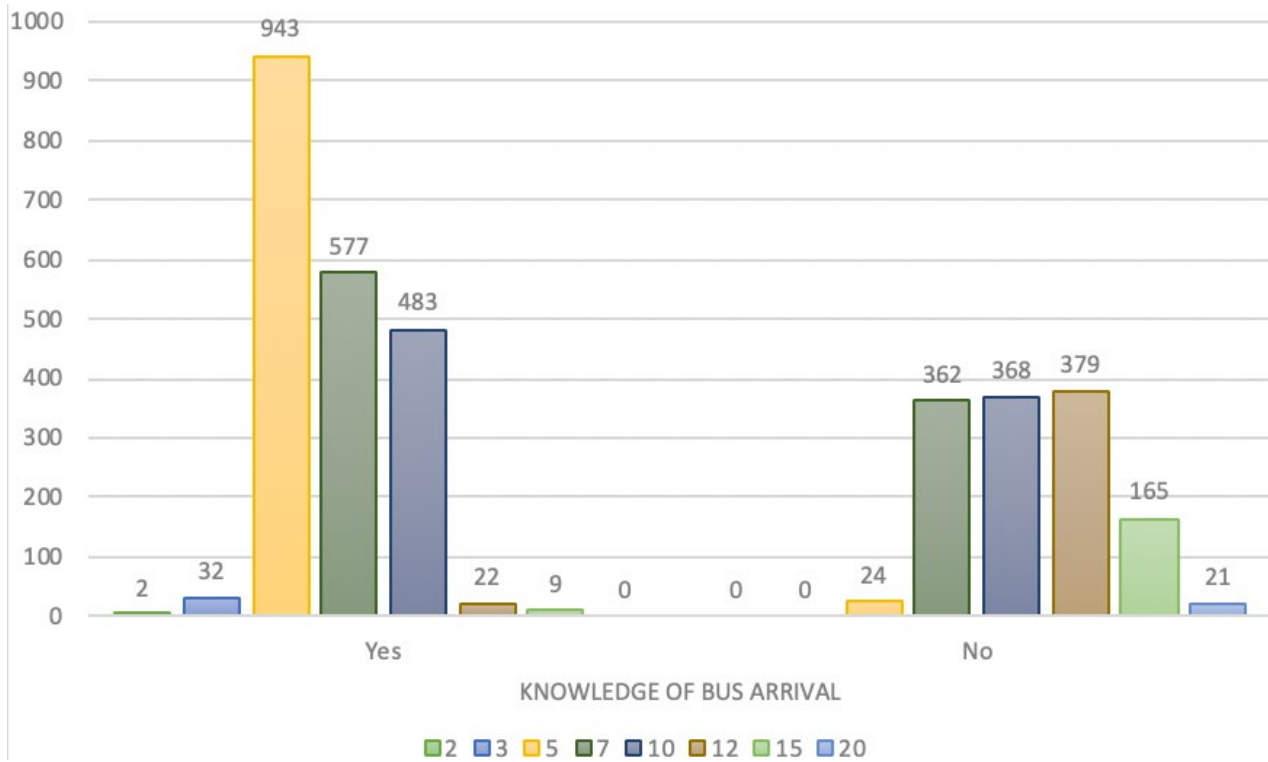
Figure 33. Patrons' Acceptable Wait Times by Ethnicity

### Acceptable Wait Times by Knowledge of Bus Arrival Time

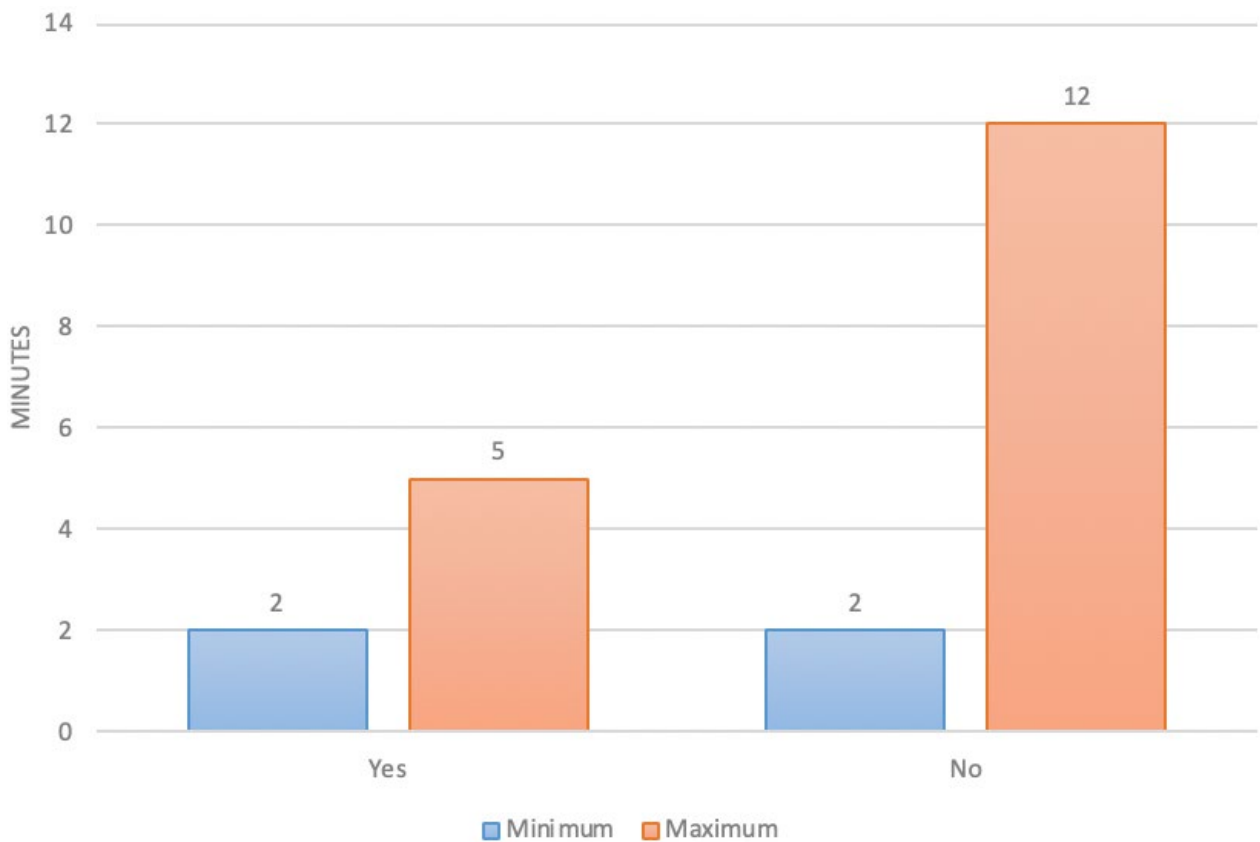
The minimum and maximum acceptable wait times by knowledge of bus arrival time are presented in this section. The summary of the acceptable wait times by knowledge of bus arrival time is presented in Table 15 (the heavily shaded cells are the modal choices and the lightly shaded ones are the runners-up) and shown in Figures 34 through 36. From the table and figures, it can be seen that the modal acceptable wait time for patrons that did not know the bus arrival time was 2 minutes, with 4 minutes being the second most common answer; in contrast, for patrons who did know the time when the bus was supposed to arrive, while the modal time was again 2 minutes, the second most common answer was only 1 minute. Similarly, the modal maximum acceptable wait time was 12 minutes for patrons who knew the bus arrival time was, but only 5 minutes for patrons that did not know the planned bus arrival time.

**Table 15. Patrons' Acceptable Wait Times by Knowledge of Bus Arrival Time**

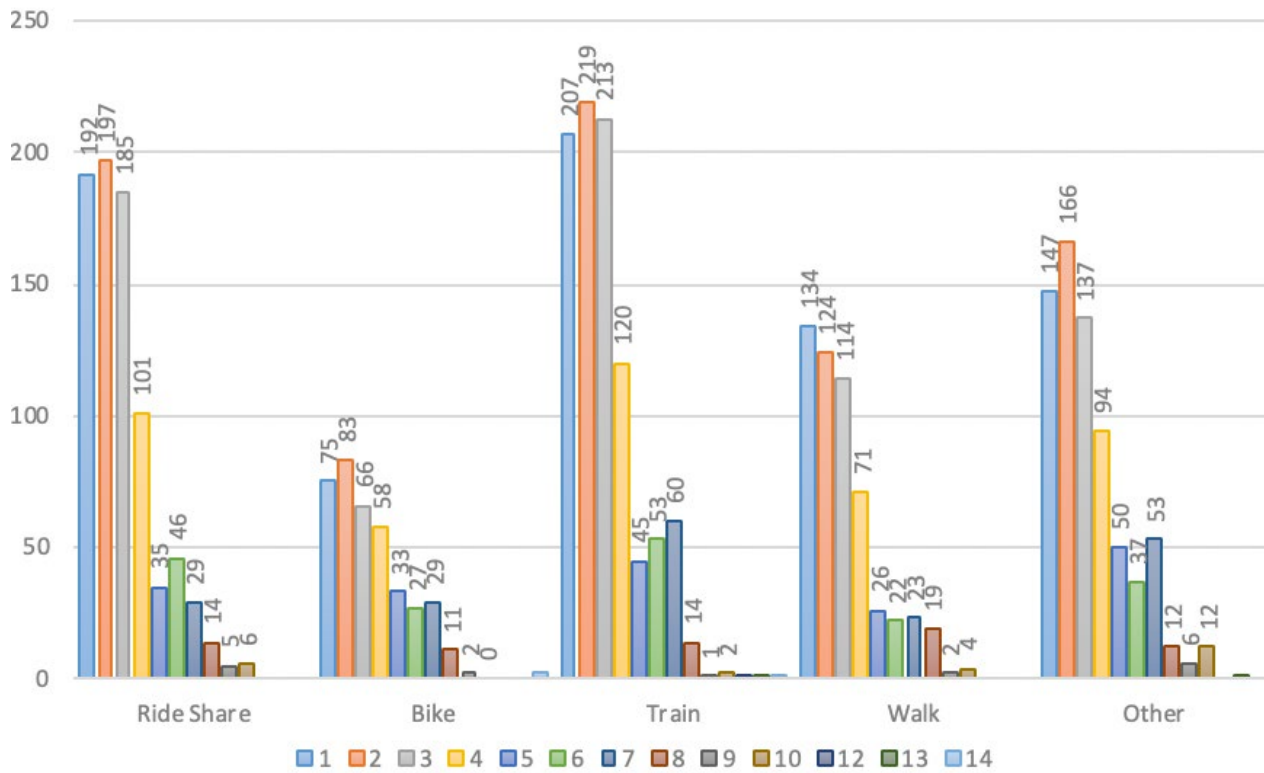
	# Minutes	Knowledge of Bus Arrival Time	
		Yes	No
Min AWT	1	544	211
	2	<b>558</b>	<b>231</b>
	3	518	197
	4	217	227
	5	70	119
	6	73	112
	7	79	115
	8	7	63
	9	0	16
	10	2	22
	12	0	1
	13	0	2
	14	0	3
	Max AWT	2	2
3		32	0
5		<b>943</b>	24
7		577	362
10		483	368
12		22	<b>379</b>
	15	9	165
	20	0	21



**Figure 34. Patrons' Minimum Acceptable Wait Times by Knowledge of Bus Arrival Time**



**Figure 35. Patrons' Maximum Acceptable Wait Times by Knowledge of Bus Arrival Time**



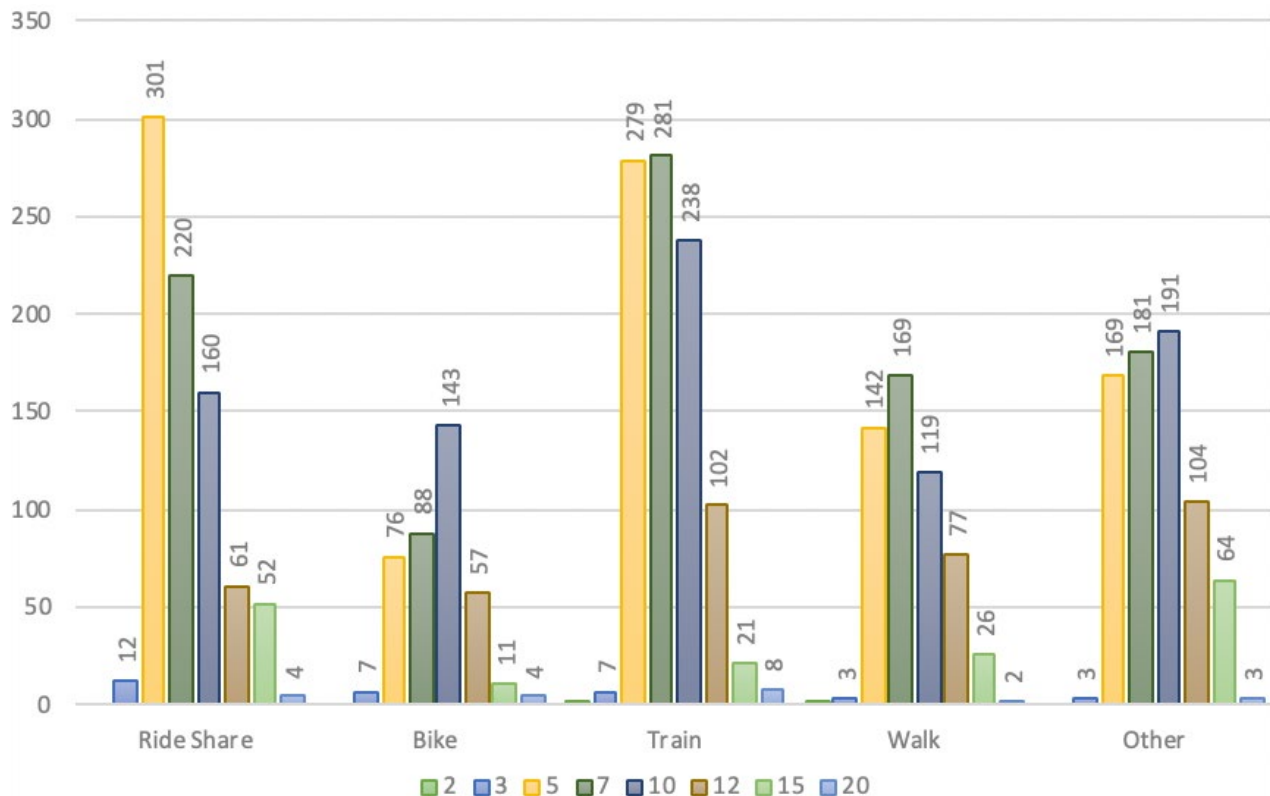
**Figure 36. Patrons’ Acceptable Wait Time by Knowledge of Bus Arrival Time**

*Acceptable Wait Times by Choice of Alternative Transportation Mode*

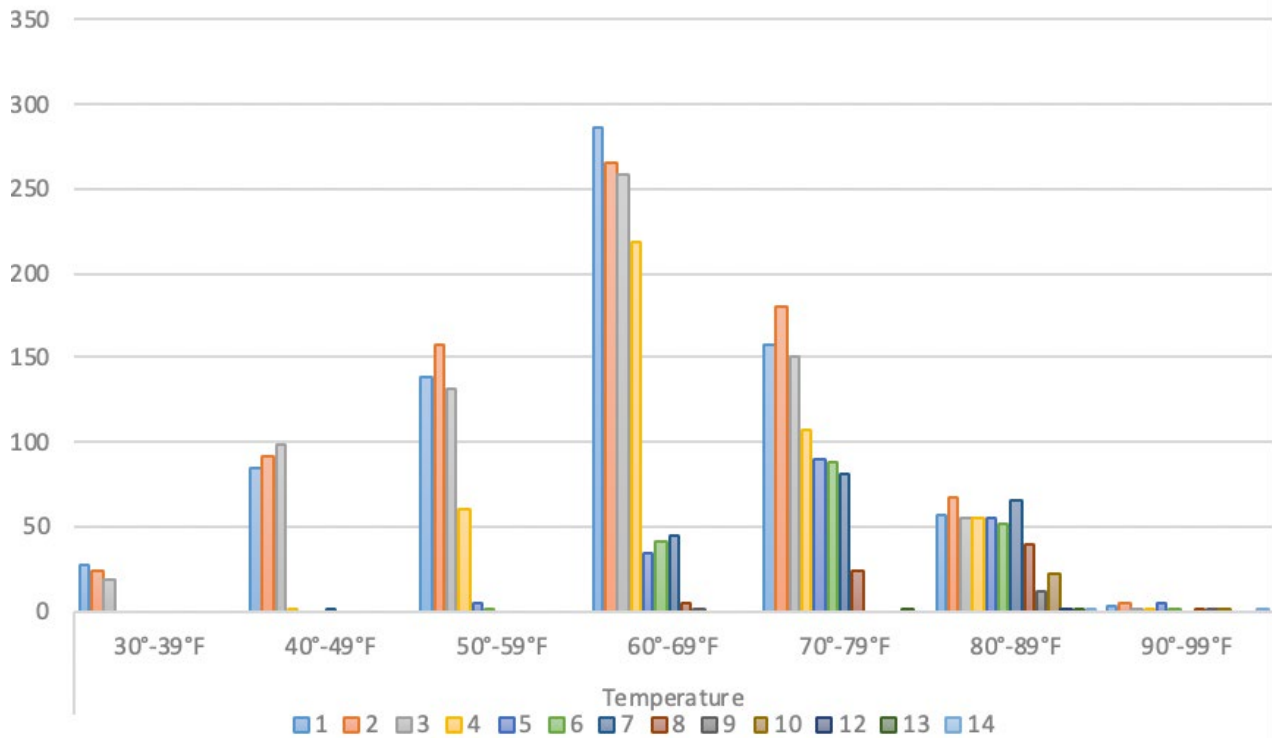
This section presents the minimum and maximum acceptable wait times by choice of alternative mode of transportation. The summary of the acceptable wait times by choice of alternative mode of transportation is presented in Table 16 and shown in Figures 37 through 39. From the table and figures, it can be seen that most patrons chose train and rideshare as their alternative mode of transportation after waiting between 2 and 7 minutes.

**Table 16. Patrons' Acceptable Wait Times by Knowledge of Bus Arrival Time**

	# Minutes	Alternative Mode of Transportation				
		Ride Share	Bike	Train	Walk	Other
Min AWT	1	192	75	207	134	147
	2	197	83	219	124	166
	3	185	66	213	114	137
	4	101	58	120	71	94
	5	35	33	45	26	50
	6	46	27	53	22	37
	7	29	29	60	23	53
	8	14	11	14	19	12
	9	5	2	1	2	6
	10	6	0	2	4	12
	12	0	0	1	0	0
	13	0	0	1	0	1
	14	0	2	1	0	0
	2	0	0	1	1	0
Max AWT	3	12	7	7	3	3
	5	301	76	279	142	169
	7	220	88	281	169	181
	10	160	143	238	119	191
	12	61	57	102	77	104
	15	52	11	21	26	64
	20	4	4	8	2	3



**Figure 37. Patrons' Minimum Acceptable Wait Times by Alternative Mode of Transportation Choice**



**Figure 38. Patrons' Maximum Acceptable Wait Times by Alternative Mode of Transportation Choice**

*Environmental Factors*

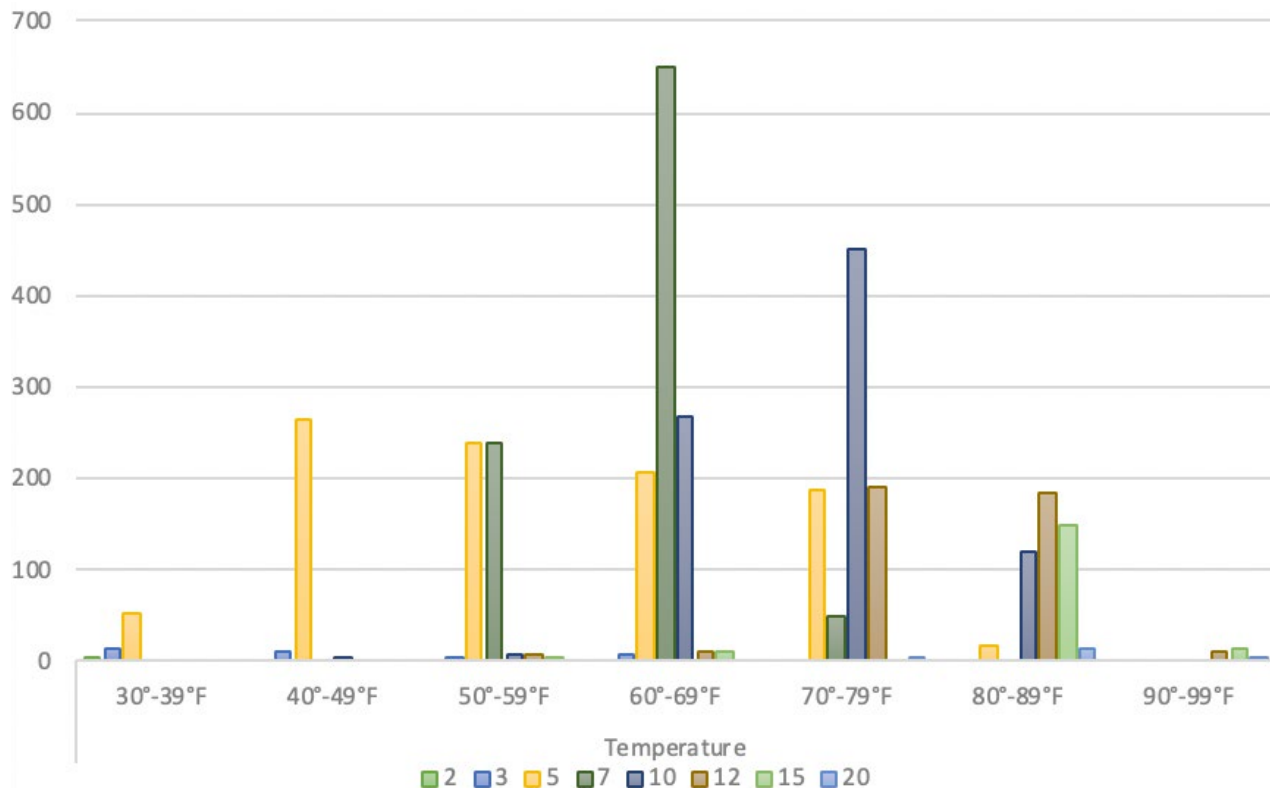
This section presents the frequencies of acceptable wait times by temperature at the time of the survey.

*Acceptable Wait Times by Temperature*

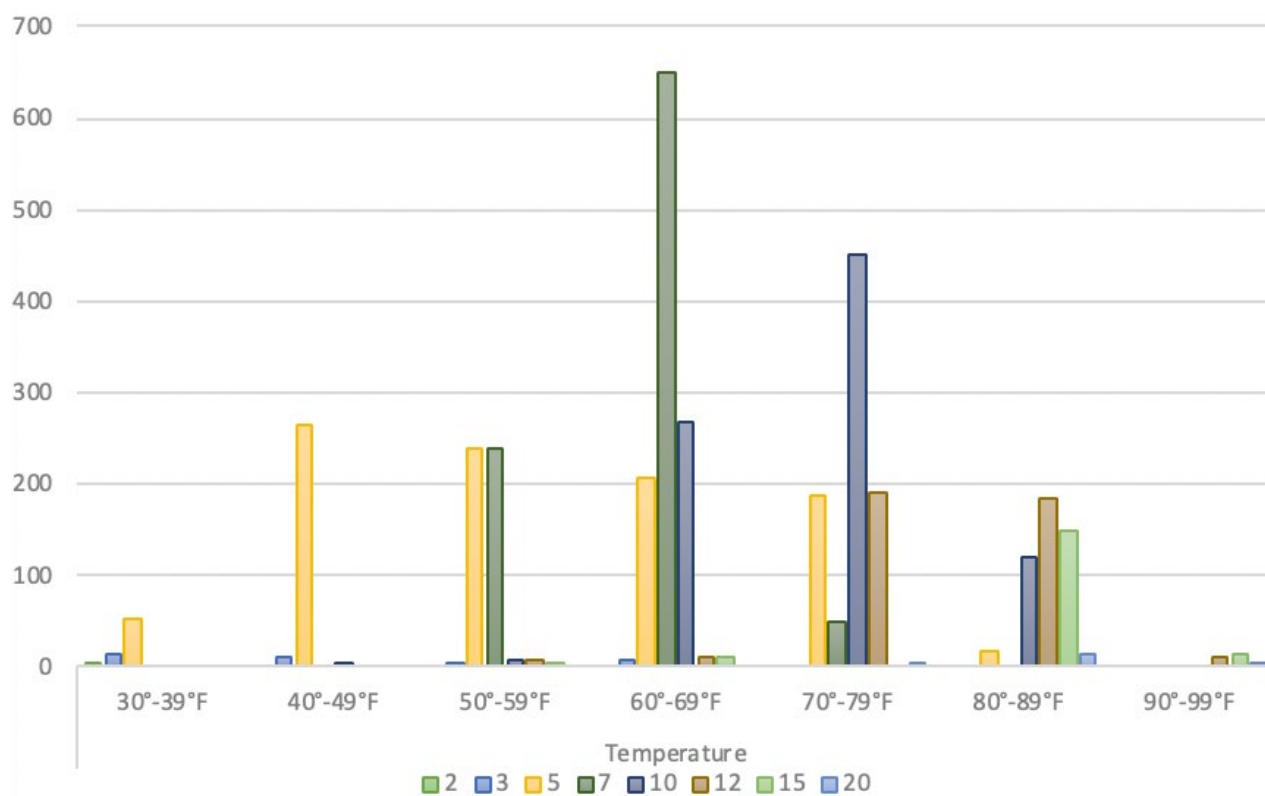
Table 17 and Figures 39 through 41 present the summary of responses of preferred minimum and maximum acceptable wait times by the temperature at the time of the survey. From the table, it can be observed that patrons were tended to choose longer maximum acceptable wait times as the temperature increased.

**Table 17. Patrons' Acceptable Wait Times by Temperature**

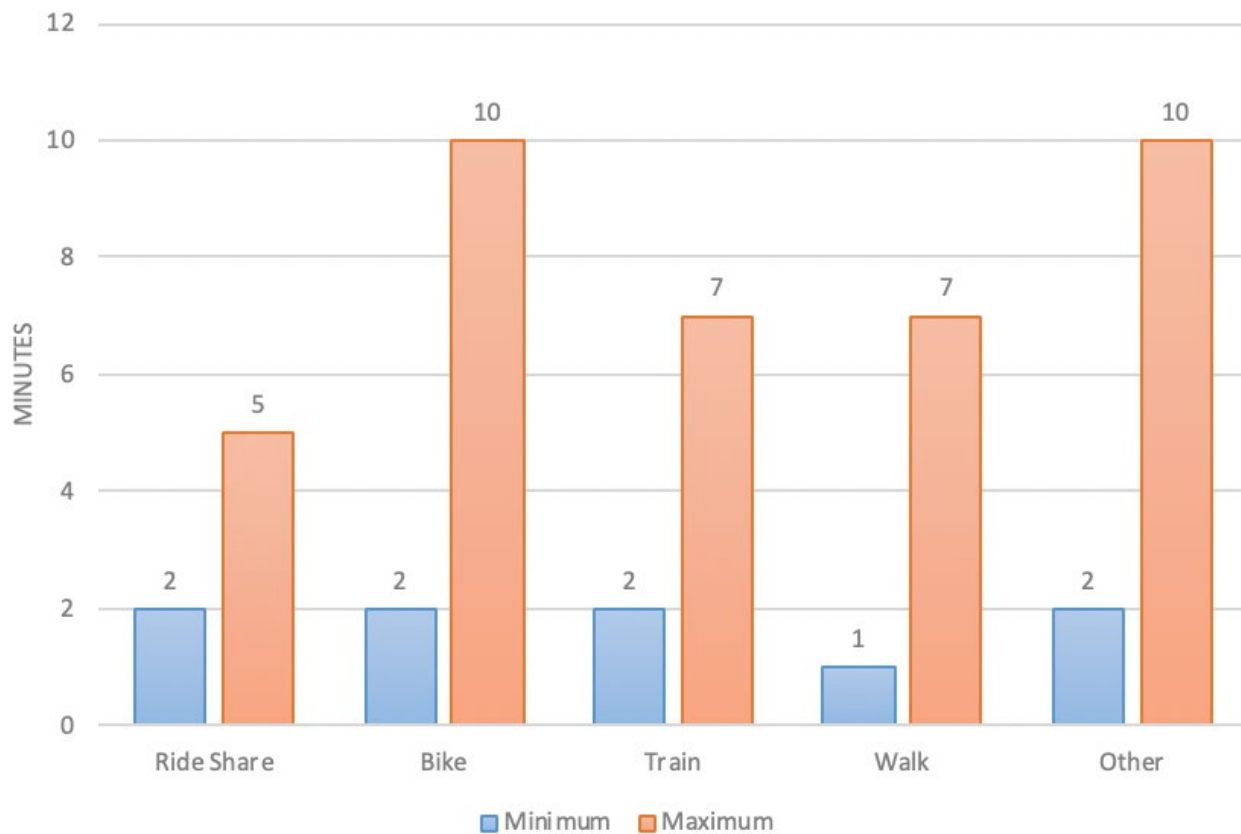
	# Minutes	Temperature						
		30°-39°F	40°-49°F	50°-59°F	60°-69°F	70°-79°F	80°-89°F	90°-99°F
Min AWT	1	27	85	139	287	157	57	3
	2	23	91	158	265	180	67	5
	3	18	99	131	258	151	56	2
	4	0	1	60	218	107	56	2
	5	0	0	5	34	90	56	4
	6	0	0	1	42	88	52	2
	7	0	1	0	45	82	66	0
	8	0	0	0	5	24	39	2
	9	0	0	0	2	0	12	2
	10	0	0	0	0	0	22	2
	12	0	0	0	0	0	1	0
	13	0	0	0	0	1	1	0
	14	0	0	0	0	0	2	1
	Max AWT	2	2	0	0	0	0	0
3		13	10	1	8	0	0	0
5		53	265	238	207	186	18	0
7		0	0	238	651	50	0	0
10		0	2	9	269	451	120	0
12		0	0	7	10	189	185	10
15		0	0	1	11	0	149	13
20	0	0	0	0	4	15	2	



**Figure 39. Patrons' Minimum Acceptable Wait Times by Temperature**



**Figure 40. Patrons' Maximum Acceptable Wait Times by Temperature**



**Figure 41. Patrons' Acceptable Wait Times by Alternative Mode of Transportation**



## REGRESSION ANALYSIS

This section presents results of the regression analyses to develop to predict the MAWT's of bus patrons. Three models were developed: one for the A.M. peak period (7:00 AM–9:30 AM), one for the mid-day off-peak period (10:00 AM–2:30 PM), and one for the P.M. peak period (4:00 PM–6:30 PM). The models were multiple linear regressions taking the form:

$$MAWT_i = \beta_{0i} + T\beta_{1i} + AH\beta_{2i} + KBAT\beta_{3i} + PS\beta_{4i} + \varepsilon$$

A 5% significance level was chosen for testing the models. The models were evaluated for statistical significance, using the p-values of the models' F statistics and a 5% significance level, and for goodness-of-fit, using both the  $R_2$  and the adjusted  $R_2$  values. Also, the statistical significance of the models' predictors were evaluated using the p-values of the predictors' t-statistics. The t-test for each regression coefficient tests the model against the null hypothesis that the true regression coefficient is zero. The F-test of overall significance for a regression model compares the fit of the regression with the fit of a null model with an intercept ( $\beta_{0i}$ ) but no predictor variables, that is, to a null model where all regression coefficients are zero.

In order to achieve the best-fitting linear relationship between the dependent variable, Maximum Acceptable Wait Time (MAWT), and transformations of the independent variables, Temperature (T), Average Headway (AH), Period of Day (PS), and Knowledge of Bus Arrival Time (KBAT), several curve estimations between the dependent variable and each independent variable were performed. The transformations were necessary to obtain the best relationship between the dependent and independent variable. The formulae used to transform each independent variable are shown in Table 18. Logistic and cubic transformations of AH and T respectively, resulted in the most favorable relationships with the MAWT while PS and KBAT remained untransformed. The summaries of the results of the regression analyses are presented in the following sections. The detailed results are attached as appendix A.

**Table 18. Data Transformation**

Variable	Transformed Variable	Selected Relationship with Dependent Variable	Transformation Formula
T	$T_{Tr}$	Cubic	$f_1(x) = x^3$
AH	$AH_{Tr}$	Logistic	$f_2(x) = \ln\left(\frac{1}{x}\right)$
KBAT	KBAT	Linear	$f_3(x) = x$
PS	PS	Linear	$f_4(x) = x$

### Wait Time Prediction Models for AM Peak Period

The results of the regression analyses for A.M. peak period are presented in Table 19. After transformation of the variables, the model took the form

$$MAWT_{A.M.} = \beta_{01} + (T)^3\beta_{11} + \ln\left(\frac{1}{AH}\right)\beta_{21} + KBAT\beta_{31} + PS\beta_{41}$$

The results showed that the fit of this regression model for the A.M. peak period was statistically significant, at a pre-chosen 5% significance level but with its F statistic actually corresponding to a very low p-value of <0.001. The effects of KBAT, PS and the transformed variables  $AH_{Tr}$  and  $T_{Tr}$  were determined to be statistically significant, again with a pre-chosen significance level of 5% but with very low p-values of <0.001. The best-fitting model, with an adjusted  $R^2$  value of 0.64, was determined to be

$$MAWT_{AM} = -0.40 + (1.07 \times 10^{-5})T^3 - 0.642 \ln\left(\frac{1}{AH}\right) - 2.22KBAT + 3.265PS$$

**Table 19. Results of the Regression Analyses for AM Peak Period**

MODEL SUMMARY			
R	R-Squared	Adjusted R-Squared	Standard Error
0.798	0.641	0.640	1.303
ANOVA SUMMARY			
Model	df	F	Sig
Regression	4	489.652	0.000
COEFFICIENTS			
Variable	Coefficients	t	Sig.
Constant	-0.400	-0.534	0.594
$T_{Tr}$	$1.233 \times 10^{-5}$	27.930	0.000
$AH_{Tr}$	-0.642	-5.652	0.000
KBAT	-2.220	-22.052	0.000
PS	3.265	30.988	0.000

### Wait Time Prediction Models for Mid-Day Period

The results of the regression analyses for Mid-day period are presented in Table 20. The model took the form

$$MAWT_{mid-day} = \beta_{01} + (T)^3\beta_{11} + \ln\left(\frac{1}{AH}\right)\beta_{21} + KBAT\beta_{31} + PS\beta_{41}$$

The results show that the fit of this model is statistically significant, at a pre-chosen 5% significance level but with its F statistic actually corresponding to a very low p-value of

<0.001. The effects of KBAT, PS and the transformed variables  $AH_{Tr}$  and  $T_{Tr}$  were determined to be statistically significant, also with a pre-chosen 5% significance level but actually with very low p-values of <0.001. The best-fitting model, with an adjusted  $R^2$  value of 0.821, was determined to be

$$MAWT_{Offpeak} = -2.678 + (1.37 \times 10^{-5})T^3 - 0.904 \ln\left(\frac{1}{AH}\right) - 1.048KBAT + 2.705PS$$

**Table 20. Results of the Regression Analyses for Mid-day Period**

MODEL SUMMARY			
R	R-Squared	Adjusted R-Squared	Standard Error
0.907	0.822	0.821	1.379
ANOVA SUMMARY			
Model	df	F	Sig.
Regression	4	1,258.751	0.000
COEFFICIENTS			
Variable	Coefficients	t	Sig.
Constant	-2.678	-3.087	0.002
$T_{Tr}$	$1.373 \times 10^{-5}$	34.806	0.000
$AH_{Tr}$	-0.904	-6.974	0.000
KBAT	-1.048	-9.273	0.000
PS	2.702	31.549	0.000

### Wait Time Prediction Models for P.M. Peak Period

The results of the regression analyses for P.M. peak period are presented in Table 21. After transformation of the variables the model took the form

$$MAWT_1 = \beta_{o1} + (T)^3 \beta_{11} + \ln\left(\frac{1}{AH}\right) \beta_{21} + KBAT \beta_{31} + PS \beta_{41}$$

The results show that the fit of this model is statistically significant, at a pre-chosen 5% significance level but with its F statistic actually corresponding to a very low p-value of <0.001. The effects of KBAT, PS and the transformed variables  $AH_{Tr}$  and  $T_{Tr}$  were determined to be statistically significant, also with a pre-chosen 5% significance level but actually with very low p-values of <0.001. The best-fitting model, with an adjusted  $R^2$  value of 0.793, was determined to be:

$$MAWT_{PM} = 1.372 + (1.37 \times 10^{-5})T - 0.326 \ln\left(\frac{1}{AH}\right) - 1.171KBAT + 2.074PS$$

**Table 21. Results of the Regression Analyses for P.M. Peak Period**

MODEL SUMMARY			
R	R-Squared	Adjusted R-Squared	Standard Error
0.891	0.793	0.793	1.134

ANOVA SUMMARY			
Model	df	F	Sig.
Regression	4	1,117.277	0.000

COEFFICIENTS			
Variable	Coefficients	t	Sig.
Constant	1.372	1.965	0.050
T <sub>Tr</sub>	1.174 x 10 <sup>-5</sup>	29.245	0.000
AH <sub>Tr</sub>	-0.326	-11.516	0.000
KBAT	-1.171	38.388	0.000
PS	2.074	-3.195	0.001

## MODEL TESTING

### Kolmogorov-Smirnov (K-S) Test

The results of the K-S tests for MAWT show that the maximum difference D between the cumulative distributions of the predicted and observed MAWTs, for all the models, was less than the critical value of 1.36 at a 5% level of significance. Thus, the distributions of predicted values and observed values do not significantly differ. The tables presenting the observed MAWT and the predicted MAWT are presented in Appendix B.

### Normality of Errors

The assumption of normality of errors was tested using the normal probability plot. The observed cumulative probabilities of the standardized residuals are plotted against the expected cumulative probabilities of the standardized residuals. Visual inspection of the plots, presented in Appendix B, for all models, shows the observed curve closely follows the diagonal of the plot, indicating that the errors are normally distributed.

### Multicollinearity

The test for multicollinearity showed that the VIF for all the variables in models were less than the maximum value of 10. Thus, multicollinearity was not present between the independent variables.

### Homoscedacity

Visual inspection of the residual plots of the three models (presented in appendix B) show an even distribution about the zero line, confirming the variance of the residuals of the

dependent variable is the same for all values of the independent variable.

Table 22 presents a summary of the models developed.

**Table 22. Summary of Results**

#	Peak Period	Model	R <sup>2</sup>
1	AM	$MAWT_{AM} = -0.40 + (1.07 \times 10^{-5})T^3 - 0.642 \ln\left(\frac{1}{AH}\right) - 2.22KBAT + 3.265PS$	0.645
2	MID	$MAWT_{Off} = -2.678 + (1.37 \times 10^{-5})T^3 - 0.904 \ln\left(\frac{1}{AH}\right) - 1.048KBAT + 2.705PS$	0.822
3	PM	$MAWT_{PM} = 1.372 + (1.37 \times 10^{-5})T^3 - 0.326 \ln\left(\frac{1}{AH}\right) - 1.171KBAT + 2.074PS$	0.798

## HYPOTHESIS TESTS

This section presents the results of the Wilcoxon rank-sum and Kruskal-Wallis tests for significant differences in the mean MAWT of bus patrons based on their gender and ethnicity respectively. The results were obtained by comparing the mean of the ranks of the MAWT of the patrons of each group of the independent variables. The z scores of the Wilcoxon W statistic and the Kruskal-Wallis H statistic were tested at a 5% significance level.

### Results of the Test for Significant Difference in Mean Rank of MAWT Based on Gender

Tables 23 and 24 present the results of the test for a significance difference in MAWT based on gender. The mean rank of female patrons was calculated to be 1,683.63 while the mean rank of male patrons was calculated to be 1,705.11, as shown in Table 23. The Wilcoxon W statistic was computed to be 2,949,722.00 as observed in Table 24. This statistic had a z score of -0.660, which was determined to be statistically non-significant at a 5% significance level (p= 0.509). Thus, the analysis found no statistically significant effect of passengers' gender on their MAWT.

**Table 23. Rankings by Gender**

Gender	N	Mean Rank	Sum of Ranks
Female	1752	1,683.63	2,949,722.00
Male	1635	1,705.11	2,787,856.00
<b>Total</b>	<b>3387</b>		

**Table 24. Wilcoxon Rank-Sum Test Statistics - Gender**

Test Statistic	Value
Wilcoxon W	2,949,722.00
Z	-0.660
Asymp. Sig. (2-tailed)	0.509

### Results of the Test for Significant Difference in Mean Rank of MAWT Based on Ethnicity

The results of the test for a significant difference in MAWT based on ethnicity are presented in Tables 25 and 26. As Table 25 shows, White patrons had the lowest mean rank of 1,365.61, while patrons of ethnicity “Other” had the highest mean rank of 1,895.57. The Kruskal-Wallis H statistic was calculated to be 131.91 as shown in Table 26. This statistic was determined to be statistically significant, at a pre-chosen 5% significance level but actually with a very low p-value <0.001. Thus, the analysis showed there are significant differences in the MAWT of patrons based on ethnicity.

**Table 25. Rankings by Gender**

Ethnicity	N	Mean Rank
White	778	1,365.61
Black	771	1,729.34
Hispanic	747	1,801.01
Asian	545	1,764.19
Other	546	1,895.57
<b>Total</b>	<b>3,387</b>	

**Table 26. Kruskal-Wallis Test Statistics - Ethnicity**

Test Statistic	Value
Kruskal-Wallis H	131.91
df	4
Asymp. Sig.	0.000

A post-hoc analysis was used to investigate the between-ethnicity differences in MAWT of patrons. Since the data did not meet the parametric assumptions of normality and homogeneity of variance, the Games-Howell post-hoc test was used for the analysis. The results of the analysis are shown in Table 27. The table shows the differences between the mean ranks MAWT for each ethnicity with that for each other ethnicity. The statistical significances of these differences are also presented in the table.

**Table 27. Results of Post-Hoc Test**

(I) Ethnicity	(J) Ethnicity	Difference of Mean Rank (I-J)	Std. Error	Sig.	95% Confidence Interval	
					Lower Bound	Upper Bound
<b>White</b>	Black	-0.950*	0.156	0.000	-1.38	-0.52
	Hispanic	-1.190*	0.158	0.000	-1.62	-0.76
	Asian	-1.044*	0.169	0.000	-1.51	-0.58
	Other	-1.430*	0.167	0.000	-1.89	-0.97
<b>Black</b>	White	0.950*	0.156	0.000	0.52	1.38
	Hispanic	-0.240	0.155	0.535	-0.66	0.18
	Asian	-0.094	0.167	0.980	-0.55	0.36
	Other	-0.480*	0.165	0.030	-0.93	-0.03
<b>Hispanic</b>	White	1.190*	0.158	0.000	0.76	1.62
	Black	0.240	0.155	0.535	-0.18	0.66
	Asian	0.145	0.169	0.911	-0.32	0.61
	Other	-0.240	0.167	0.602	-0.70	0.22
<b>Asian</b>	White	1.044*	0.169	0.000	0.58	1.51
	Black	0.094	0.167	0.980	-0.36	0.55
	Hispanic	-0.145	0.169	0.911	-0.61	0.32
	Other	-0.386	0.178	0.193	-0.87	0.10
<b>Other</b>	White	1.430*	0.167	0.000	0.97	1.89
	Black	0.480*	0.165	0.030	0.03	0.93
	Hispanic	0.240	0.167	0.602	-0.22	0.70
	Other	0.386	0.178	0.193	-0.10	0.87

\*The mean difference is significant at the 0.05 level.

The results show that there were statistically significant differences in MAWT rank between White patrons and patrons of all other ethnic groups, at a pre-chosen 5% significance level but with a very low p-value of <0.001, with White patrons having the lowest mean MAWT rank.

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## V. DISCUSSION

The research aimed at developing regression models for predicting the maximum acceptable wait times of bus patrons based on the weather condition (temperature), average headway of buses, patrons' knowledge of bus arrival times and the presence of shelter at the bus stops. Previous literature has shown that the actual wait times of patrons at bus stops differed from their perceived wait times, and that perceived wait time tend to matter more for dictating rider discomfort and preference towards bus services than do actual wait times. The factors that were found to affect the actual wait times of patrons included bus stop features and surroundings, period of day, the purpose of trip, and the patrons' demographics. The wait time of bus patrons has also been used by transit agencies and officials as a measure of transit service reliability; this was especially the case in jurisdictions with high frequency services, where the arrival of passengers is random, and the average wait time approximates half the headway. Although most studies define "wait time" simply as the time spent waiting at the bus stop, a study argued that a better measure of the real cost to patrons of waiting for buses would take into account four components: platform waiting time; potential waiting time; scheduled inconvenience; and synchronization cost. The review of literature also revealed that when wait times exceed acceptable limits, patrons tend to consider other mode choices. The alternate mode choice of passengers ranges from transferring to another bus route to other travel modes such as taxis and carpooling. Actual wait times have been reported in previous literature to follow the lognormal and gamma distributions.

The data used in this study was obtained by surveying 3,388 bus patrons at 71 selected bus stops in Washington, D.C. over an eight-month period. Data obtained from patrons included their ethnicity, gender, minimum and maximum acceptable wait times, alternate transportation mode choice, and knowledge of bus arrival times. Additionally, data on the operational characteristic of the buses were obtained via video playback of video recordings of cameras installed at the selected bus stop. The data extracted from the video recordings included the bus arrival and departure times; the headway of each bus route was then computed from these metrics. In addition, information and conditions at each bus stop at the time of each survey was recorded, including bus stop ID number, bus direction of travel, the availability of shelter and the temperature at the bus stop at the time of survey.

The results of the analysis of the survey data obtained confirmed some of the findings in previous literature and also provided new insight about the acceptable wait time of bus patrons. Analysis of the maximum acceptable wait times of patrons showed lognormal distribution, as was reported for actual wait times in previous literature (Guo et al, 2011). Most patrons' acceptable wait times ranged from 5 to 15 minutes. The mean maximum acceptable wait time of patrons during the mid-day period was found to be higher than during the A.M. and P.M peak periods, was recorded occurred during the A.M. peak period, which may be explained by the fact that most patrons during the A.M. are probably commuting to work and need to arrive on time. The mean acceptable wait times of patrons waiting at bus stops with shelter was approximately 28% higher than mean acceptable wait times of patrons at bus stops without shelter, a value close to the 30% previously reported by Fan et al. (2016). However, with regards to gender, the mean maximum acceptable wait times of male and female patrons was approximately equal, suggesting



that the gender of a patron may not influence their waiting tolerance level. In terms of race, White patrons reported the lowest mean maximum acceptable wait time; Black and “Other” ethnicity patrons recorded the highest mean maximum acceptable wait time; and Hispanic and Asian patrons had approximately the same, intermediate, mean maximum acceptable wait times. Bus patrons who had knowledge of the arrival time of the bus were observed to have lower acceptable wait times than those who had no knowledge of the arrival time, thus tending to be less tolerant when buses do not arrival as scheduled. About 40% of the patrons surveyed considered using a train as an alternate transportation mode while about 35% considered using a ridesharing service. Patrons at bus stops close to train stations mostly preferred using a train. Also, 10% preferred to walk to their destination if it is within a walking distance. In addition, 11% of the patrons preferred to use a bicycle.

Statistical analyses of the data were conducted in order to develop predictive models for acceptable wait times based on weather condition (temperature) and average headway of buses. Also, statistically significant differences in the average maximum acceptable wait times of patrons based on gender and ethnicity were investigated. The analyses were conducted at a 5% significance level, although many of the significant p-values turned out to be considerably lower than this. Regression models were developed for the A.M. peak, mid-day off-peak, and P.M. peak periods. All the models were found to fit the data with statistically significant F statistics (with very low p-values <0.001). In addition, the effects of temperature, average headways, presence of shelter, and knowledge of bus arrival time of all the models were determined to be statistically significant (with very low p-values <0.001). In general, the maximum acceptable wait of passengers also tend to increase as temperature increased. The maximum acceptable wait times of patrons increase with increasing bus headway. Moreover, patrons who are aware of the arrival times of buses had shorter maximum acceptable wait times. In addition, at bus stops with shelter, patrons are more likely to wait longer. The Kolmogorov-Smirnov tests showed that the effects of all the models’ regression coefficients were statistically significant at a 5% significance level. The models had values (percentage of variance explained) of 64%, 79%, and 82%.

The results of the Wilcoxon rank-sum test showed that the difference in the acceptable wait times of patrons based on the gender was not statistically significant ( $p$ -values = 0.509). In contrast, the Kruskal-Wallis test did show at least one statistically significant difference in the mean acceptable wait times of patrons based on ethnicity, reporting a statistically significant H statistic of 15.544 ( $p$ -value=0.000). A post-hoc analysis then revealed that there is a statistically significant difference of the acceptable wait times between White patrons and all other ethnicities.

## **VI. CONCLUSIONS AND RECOMMENDATIONS**

The models developed in this research are potentially useful tools that transit agencies could use to improve bus scheduling and operations in order to ultimately retain and improve ridership. It is recommended that future research explore the use of machine learning and artificial intelligence techniques to predict the wait time of patrons and also incorporate other factors such as average dwell time of buses.

## APPENDIX A

#	Bus Stop Name	Route #	Bus Stop ID	Direction of Travel	Design Type	Placement	Shelter
1	4th St and Butternut St, NW	54 62 63	1002825	SWB	Curb-Side	Intersection	No
2	4th St and Rhode Island Ave, NE	G8	1003928	WB	Curb-Side	Intersection	No
3	5th St and Whittier St, NW	62 63	1002794	SB	Curb-Side	Intersection	No
4	7th St and Constitution Ave, NW	16C 30N 30S 32 36 74	1000846	NB	Curb-Side	Mid- Block	No
5	7th St and Franklin St, NE	G8	1001928	NB	Curb-Side	Intersection	No
6	7th St and Maryland Ave, SW	74 A9	1000694	NB	Curb-Side	Mid- Block	Yes
7	7th St and S St, NW	70	1001602	SB	Curb-Side	Mid- Block	Yes
8	8th St and D St, SE	90 92	1000656	NB	Curb-Side	Intersection	Yes
9	8th St and D St, SE	90 92	1000664	EB	Curb-Side	Mid- Block	No
10	10th St and Pennsylvania Ave, NW	63 64 S2 S4	1003432	NB	Curb-Side	Intersection	Yes
11	11th St and U St, NW	90 92	1001678	SB	Curb-Side	Intersection	Yes
12	12th St and Michigan St, NE	80	1002286	SB	Curb-Side	Mid- Block	No
13	12th St and Monroe St, NE	H8 H9	1003928	EB	Curb-Side	Mid- Block	Yes
14	12th St and Pennsylvania Ave, NW	30N 30S 32 33 36 37 39 A9	1000981	NWB	Curb-Side	Mid- Block	Yes
15	12th St and Quincy St, NE	80	1002259	NB	Curb-Side	Mid- Block	Yes

#	Bus Stop Name	Route #	Bus Stop ID	Direction of Travel	Design Type	Placement	Shelter
16	14th St and Harvard St, NW	52 54	1003040	SB	Curb-Side	Intersection	Yes
17	14th St and Randolph St, NW	52 54	1002276	SB	Curb-Side	Intersection	No
18	23rd St and I St, NW	31 32 36 39 H1 L1 X1	1001168	NB	Curb-Side	Intersection	Yes
19	40th St and Albemarle St, NW	H2 H3 H4 M4	1002492	SB	Curb-Side	Mid- Block	Yes
20	Alabama Ave and 9th St, SE	W1 W4	1000150	EB	Curb-Side	Intersection	no
21	Alabama Ave and 24th St, SE	30S 32 92 V7 W4 W8	1000225	WB	Curb-Side	Mid- Block	Yes
22	Alabama Ave and Stanton Rd, SE	91 V7 W1 W2 W3 W4	1000189	SWB	Curb-Side	Mid- Block	No
23	Alabama Ave and Stanton Rd, SE	92 V7 W1 W2 W3 W4	1000189	WB	Curb-Side	Mid- Block	Yes
24	Benning Rd and 39th St, NE	V7 V8	1000959	EB	Curb-Side	Mid- Block	Yes
25	Calvert St and Connecticut Ave, NW	96	1001846	WB	Curb-Side	Intersection	No
26	Cathedral Ave and Woodley Rd, NW	96	1002017	WB	Curb-Side	Mid- Block	No
27	Connecticut Ave and Calvert St, NW	L1	1001826	SB	Curb-Side	Intersection	Yes
28	Connecticut Ave and Q St, NW	42			Curb-Side	Intersection	Yes

#	Bus Stop Name	Route #	Bus Stop ID	Direction of Travel	Design Type	Placement	Shelter
29	Connecticut Ave and Tilden St, NW	H2 L1 L2	1002331	SEB	Curb-Side	Intersection	Yes
30	Connecticut Ave and Tilden St, NW	D32 H2 L1 L2	1002312	NB	Curb-Side	Intersection	No
31	E Capitol St and 40th St, NE	96 97	1000817	WB	Curb-Side	Intersection	No
32	E Capitol St and 46th St, SE	96 97 U5 U6	1000769	EB	Curb-Side	Mid- Block	Yes
33	Eastern Ave and Walnut Ave, NW	F1 K2	2001137	NWB	Curb-Side	Intersection	No
34	F St and Benning Rd	V7 W4 V8	1000599	NWB	Curb-Side	Intersection	Yes
35	Florida Ave and Georgia Ave, NW	90 92 96	1001653	WB	Curb-Side	Intersection	Yes
36	Florida Ave and N St, NE	D51 90 92 X3	1001378	SEB	Curb-Side	Intersection	No
37	Georgia Ave and Lamont St, NW	70	1002068	NB	Curb-Side	Intersection	No
38	Georgia Ave and Dahlia St, NW	70	1002836	SB	Curb-Side	Intersection	No
39	Georgia Ave and Upshur St, NW	60 62 63 70	1002335	NB	Curb-Side	Intersection	Yes
40	Georgia Ave and V St, NW	70	1001709	SB	Curb-Side	Mid- Block	No
41	H St and 18th St, NW	30N 30S 32 33 36	1001148	EB	Curb-Side	Intersection	No

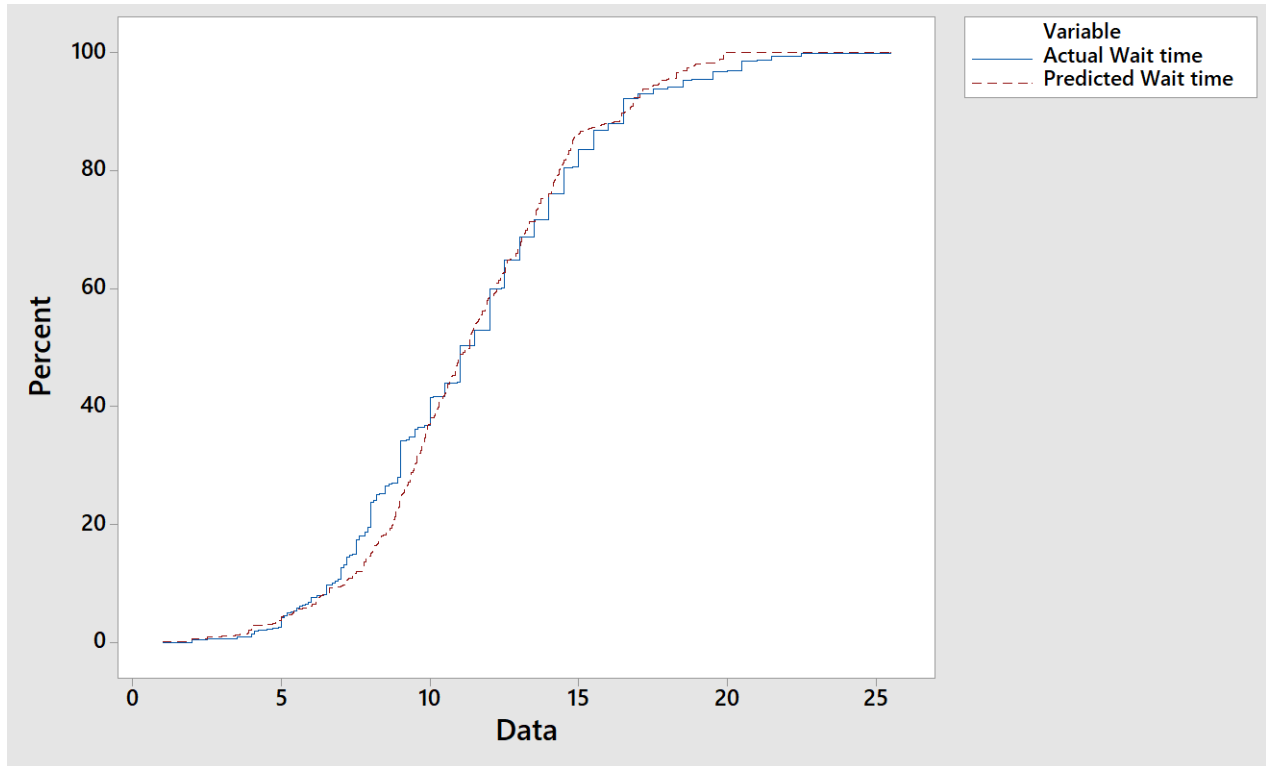
#	Bus Stop Name	Route #	Bus Stop ID	Direction of Travel	Design Type	Placement	Shelter	
42	Irving St and 13th St, NW	H1						
		H2						
		H3				Curb-Side	Intersection	No
		H4						
		H8						
43	Irving St and 14th St, NW	H1						
		H2						
		H3			EB	Curb-Side	Intersection	Yes
		H4						
		H8						
44	K St and North Capitol St, NE	D4	1003657	WB	Curb-Side	Mid- Block	No	
45	Kansas Ave and Allison St, NW	62	1002417	NB	Curb-Side	Intersection	Yes	
		63						
46	M St and Delaware Ave, SW	V1						
		P6	1000495	EB	Curb-Side	Intersection	Yes	
		74						
47	Malcom X Ave and Martin Luther King Ave, SE	W4	1000166	EB	Curb-Side	Intersection	No	
48	Martin Luther King Ave and Howard Pl, SE	90						
		A9						
		B2						
		P6	1000354	NEB	Curb-Side	Mid- Block	Yes	
		V2						
		W2						
		W3						
49	Martin Luther King Jr Ave and Pomeroy Rd, SE	W6						
		A2						
		A4						
		A6						
		A7	1000271	SB	Curb-Side	Intersection	no	
		A8						
50	Massachusetts Ave and 20th St, NW	W2						
		W3						
		D1						
		D4						
		D6	1001473	SB	Curb-Side	Mid- Block	no	
51	Massachusetts Ave and G St, NW	N2						
		N4						
		37						
51	Massachusetts Ave and G St, NW	80	1003323	SEB	Curb-Side	Intersection	Yes	
52	Minnesota Ave and E Capitol St, SE	U7						
		V2	1000761	SB	Curb-Side	Mid- Block	No	
		V4						

#	Bus Stop Name	Route #	Bus Stop ID	Direction of Travel	Design Type	Placement	Shelter
53	Minnesota Ave and Hunt Pl, NE	U4 U7 V2 V4	1001167	WB	Curb-Side	Intersection	No
54	Minnesota Ave and Nannie Helen Burroughs Ave, NE	U4 U7 V2 V4	1001189	WB	Curb-Side	Intersection	Yes
55	Minnesota Ave and S St, SE	B2 V2	1000435	SWB	Curb-Side	Intersection	Yes
56	Mississippi Ave and 10th Pl, SE	W2 W3	1000112	EB	Curb-Side	Intersection	No
57	Monroe St and 14th St, NE	G8	1002134	EB	Curb-Side	Intersection	No
58	Nannie Helen Burroughs Ave and 44th St, NE	V2 V4 X9	1003180	WB	Curb-Side	Intersection	Yes
59	New Hampshire Ave and Georgia Ave, NW	64 H8	1002981	EB	Curb-Side	Intersection	Yes
60	New Jersey Ave and Rhode Island Ave, NW	96 G2	1001583	NB	Curb-Side	Intersection	No
61	N Capitol St and H St, NE	80 D8 X1	1001120	NB	Curb-Side	Intersection	Yes
62	P St and 17th St, NW	G2	1001443	WB	Curb-Side	Intersection	Yes
63	Pennsylvania Avenue and 8th Street, SE	30N 30S 32 34 36 39 92	1000654	EB	Curb-Side	Intersection	Yes
64	Rhode Island Ave and 3rd St, NW	G8 G9	1001609	WB	Curb-Side	Intersection	No
65	Rhode Island Ave and 5th St, NE	D8 P6	1001754	EB	Curb-Side	Intersection	No
66	Riggs Rd and Chillum Pl, NE	K9 E4 R1 R2	1002643	NB	Curb-Side	Intersection	No

#	Bus Stop Name	Route #	Bus Stop ID	Direction of Travel	Design Type	Placement	Shelter
67	Riggs Rd and N Capitol St, NE	64 E4 K2 K6	1002584	NB	Curb-Side	Intersection	Yes
68	Sheriff Rd and 49th St, NE	U4	1001267	EB	Curb-Side	Intersection	No
69	S Dakota Ave and Delafield St, NE	H8	1002507	SB	Curb-Side	Intersection	Yes
70	South Dakota Ave and Farragut Pl, NE	80	1002537	SB	Curb-Side	Intersection	No
71	U St and 11th St, NW	90 92 96 X3	1001687	WB	Curb-Side	Intersection	No
72	Western Ave and 44th St, NW	N4	2000013	EB	Curb-Side	Intersection	No
73	Wheeler Rd and Savannah St, SE	A6 A7	1000132	SB	Curb-Side	Intersection	No
74	Wisconsin Ave and Jenifer St, NW	30N 30S 31 33 N2	1002646	SB	Curb-Side	Intersection	Yes
75	Wisconsin Ave and Tenley Cir, NW	30N 30S 31 33 N2		NWB	Curb-Side	Intersection	Yes
76	Wisconsin Ave and Van Ness St, NW	30N 30S 31 33 37 96 H3 H4	1002389	EB	Curb-Side	Intersection	Yes

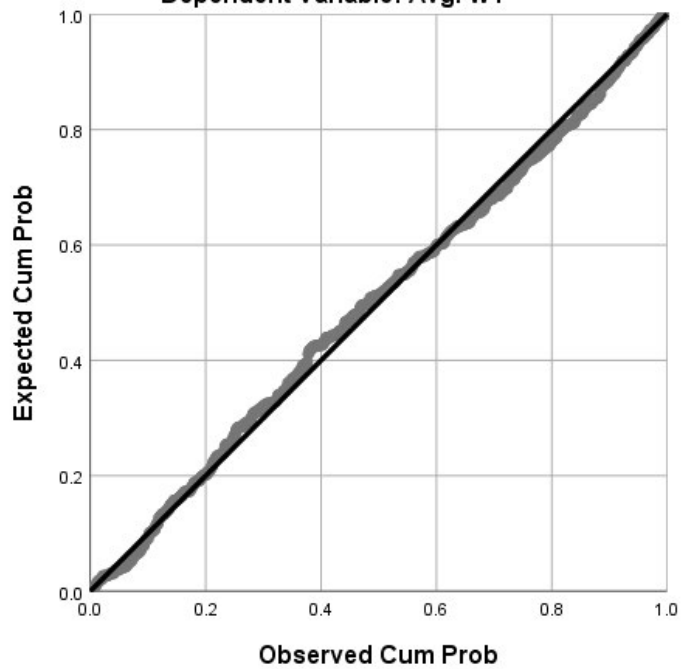
\*SWB – Southwest-bound, SB - Southbound, NWB – Northwest-bound, NB - Northbound, EB – Eastbound, WB – Westbound

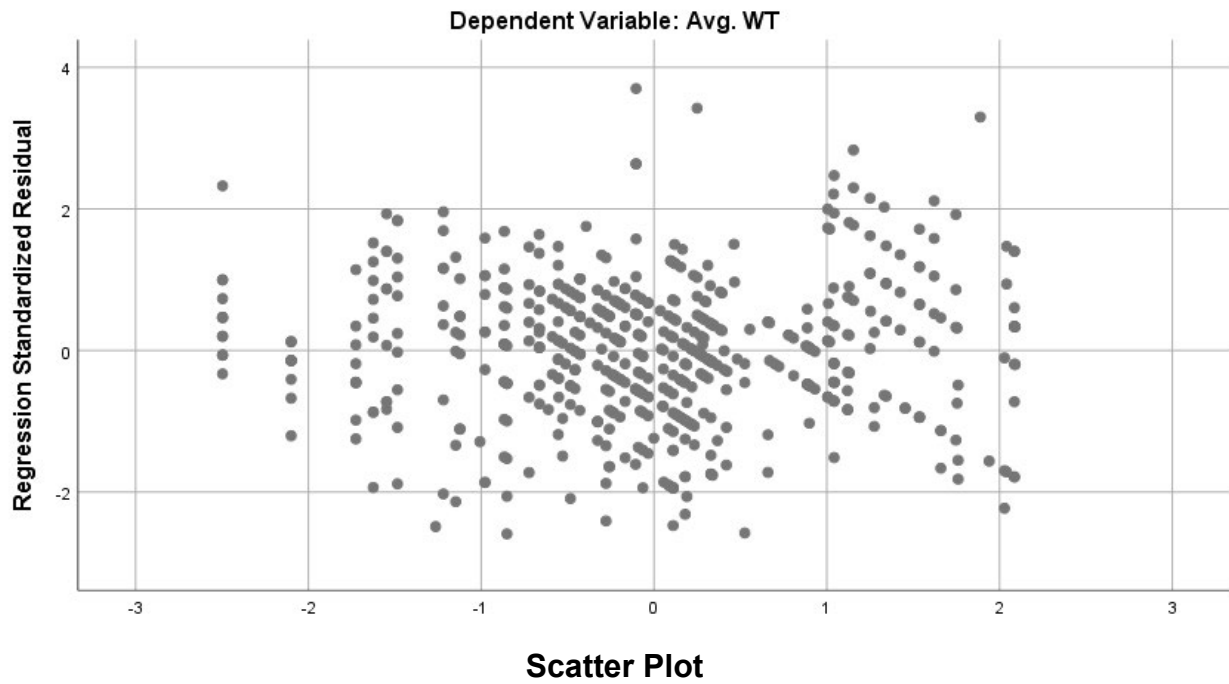


**AM PEAK MODEL TESTING****K-S Test for Model Accuracy**

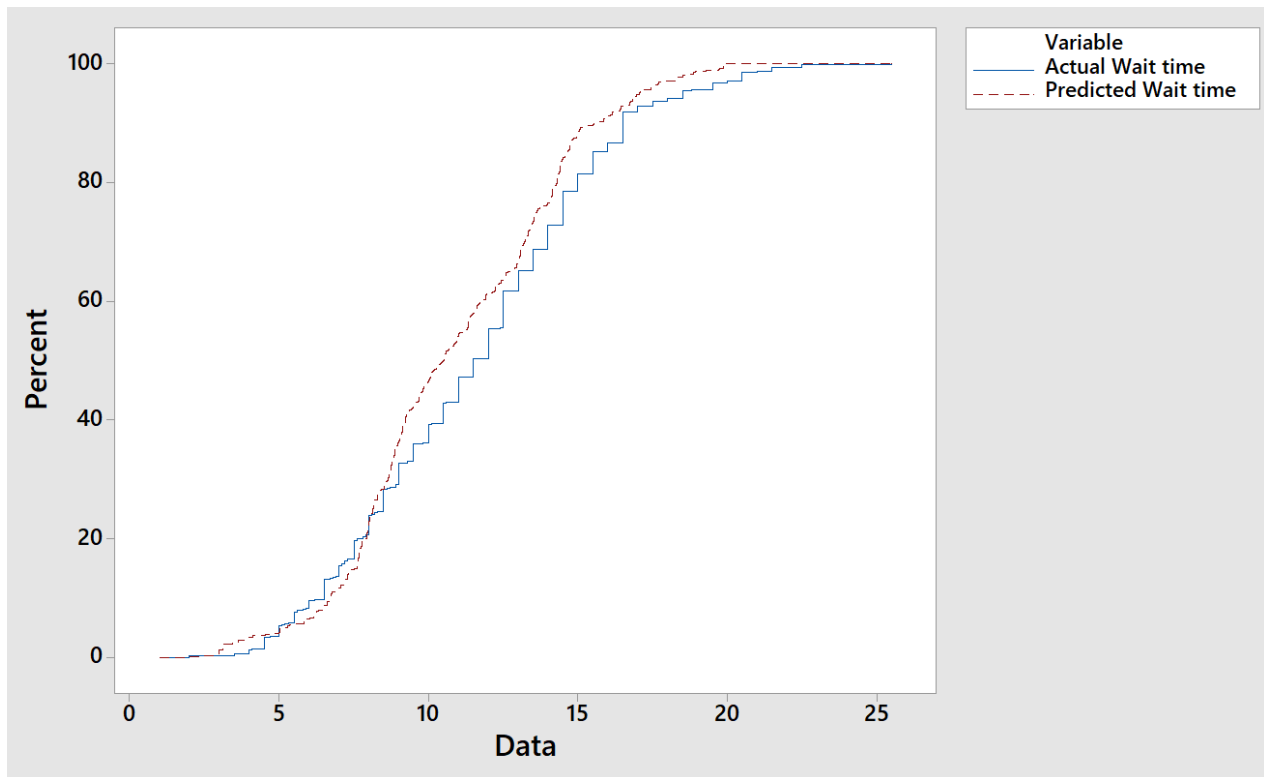
Normal P-P Plot of Regression Standardized Residual

Dependent Variable: Avg. WT

**Normal Probability Plot**

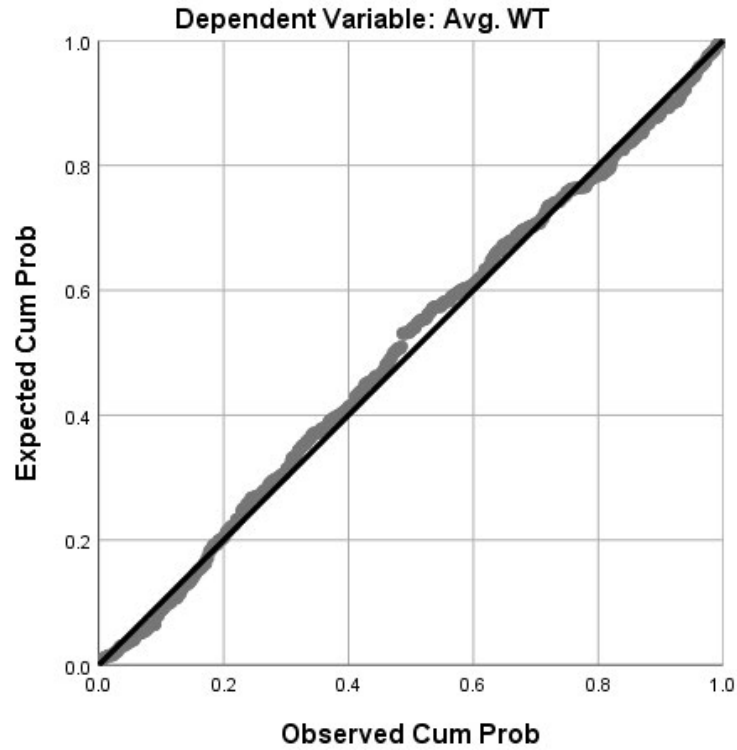


### MID PEAK MODEL TESTING

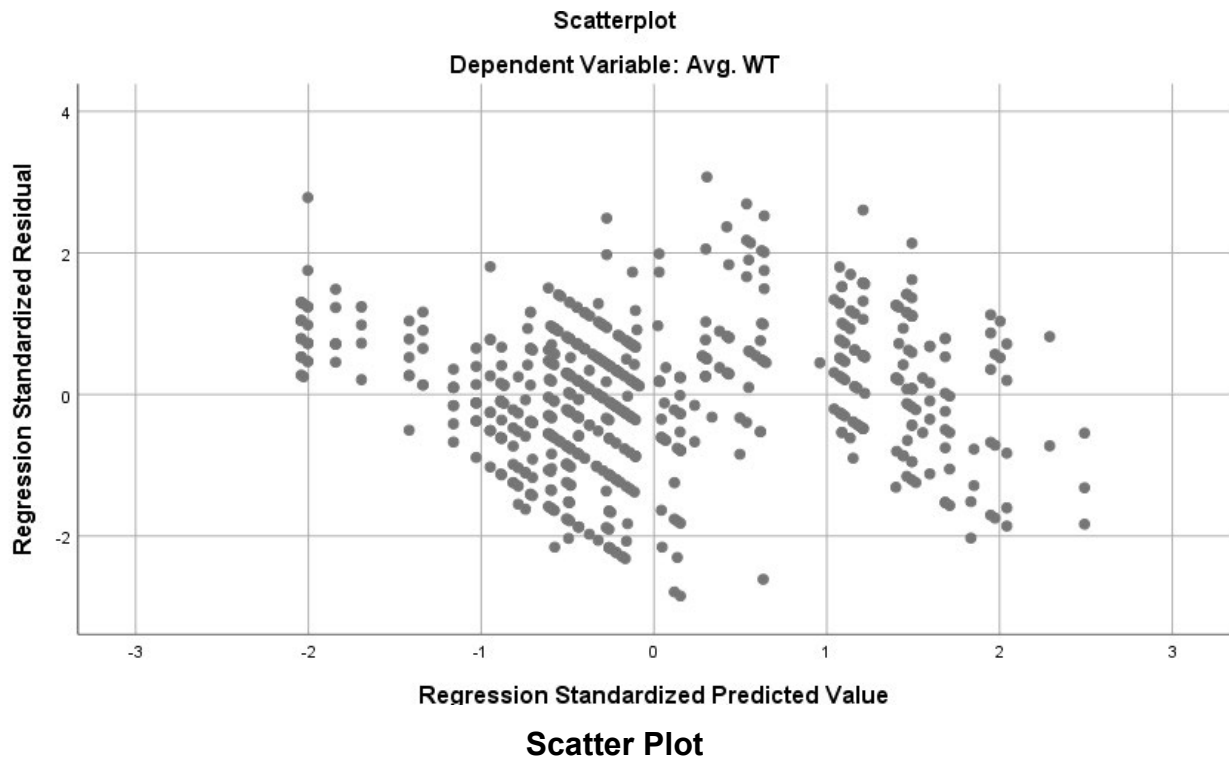


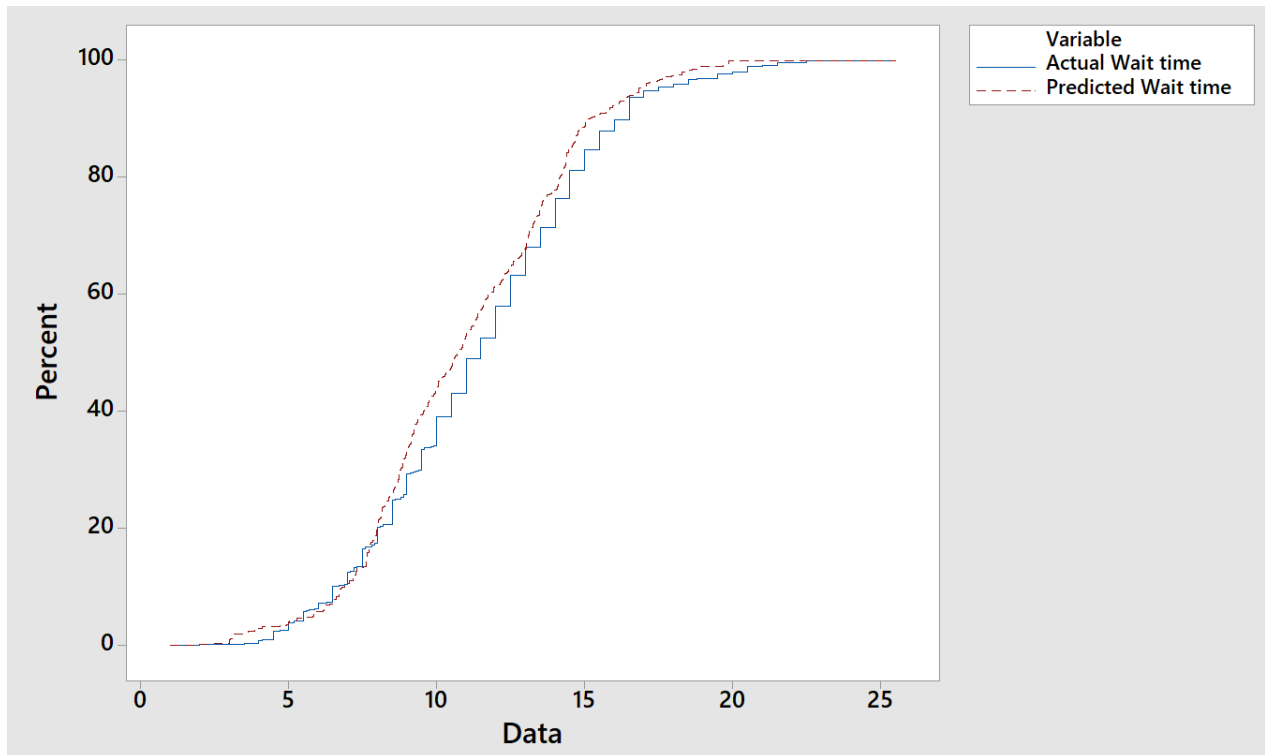
### K-S Test for Model Accuracy

Normal P-P Plot of Regression Standardized Residual

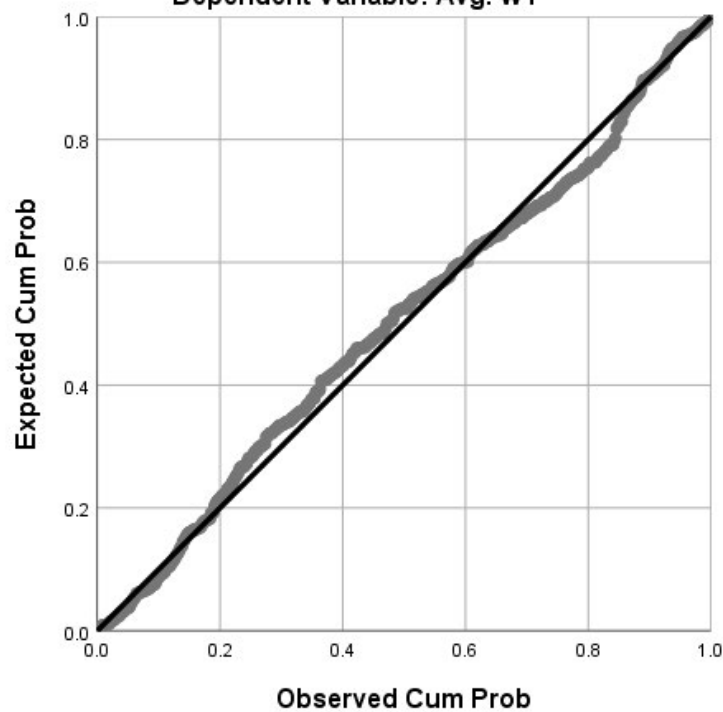


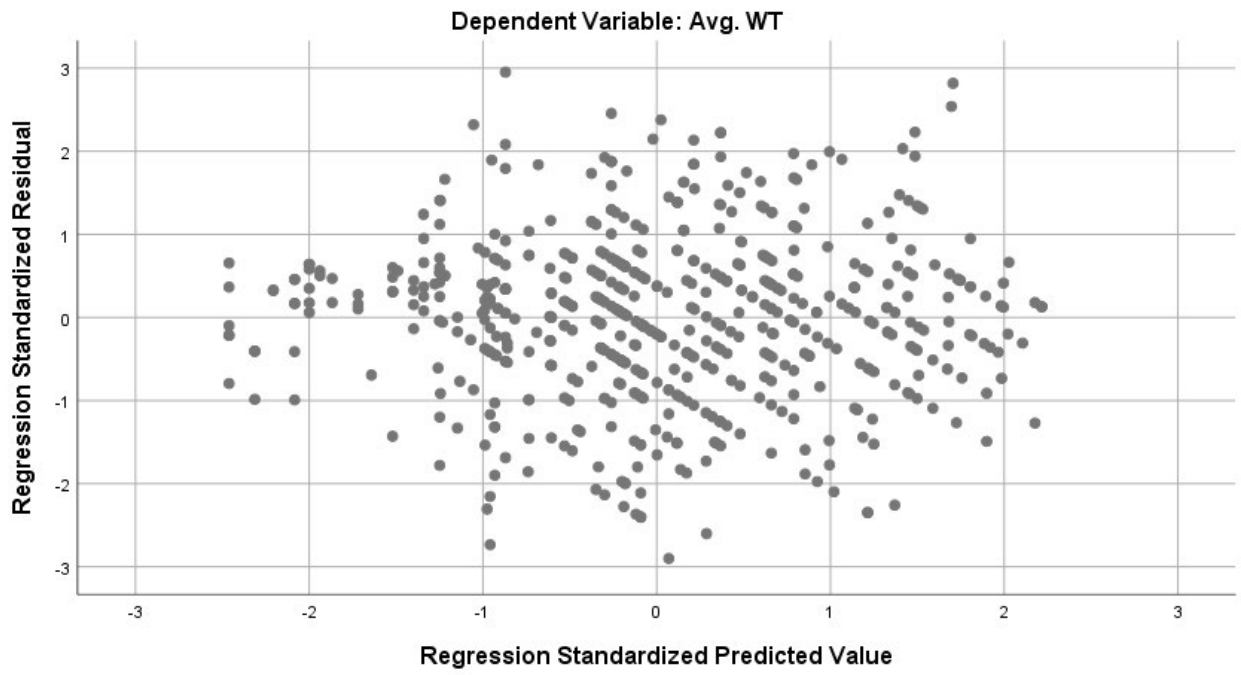
Normal Probability Plot



**PM PEAK MODEL TESTING****K-S Test for Model Accuracy****Normal P-P Plot of Regression Standardized Residual**

Dependent Variable: Avg. WT

**Normal Probability Plot**



Scatter Plot

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## ENDNOTE

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