

1 Calibration Model Maintenance in Melamine Resin Production:
2 Integrating Drift Detection, Smart Sample Selection and Model
3 Adaptation

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10 **Abstract**

The physico-chemical properties of Melamine Formaldehyde (MF) based thermosets are largely influenced by the degree of polymerization (DP) in the underlying resin. On-line supervision of the turbidity point by means of vibrational spectroscopy has recently emerged as a promising technique to monitor the DP of MF resins. However, spectroscopic determination of the DP relies on chemometric models, which are usually sensitive to *drifts* caused by instrumental and/or sample-associated changes occurring over time. In order to detect the time point when *drifts* start causing prediction bias, we here explore a universal drift detector based on a faded version of the Page-Hinkley (PH) statistic, which we test in three data streams from an industrial MF resin production process. We employ *committee disagreement* (CD), computed as the variance of model predictions from an ensemble of partial least squares (PLS) models, as a measure for sample-wise prediction uncertainty and use the PH statistic to detect changes in this quantity. We further explore supervised and unsupervised strategies for (semi-)automatic model adaptation upon detection of a drift. For the former, manual reference measurements are requested whenever statistical thresholds on Hotelling's T^2 and/or Q -Residuals are violated. Models are subsequently re-calibrated using weighted partial least squares in order to increase the influence of newer samples, which increases the flexibility when adapting to new (drifted) states. Unsupervised model adaptation is carried out exploiting the dual antecedent-consequent structure of a recently developed fuzzy systems variant

of PLS termed FLEXFIS-PLS. In particular, antecedent parts are updated while maintaining the internal structure of the local linear predictors (i.e. the consequents). We found improved drift detection capability of the CD compared to Hotelling's T^2 and Q -Residuals when used in combination with the proposed PH test. Furthermore, we found that active selection of samples by active learning (AL) used for subsequent model adaptation is advantageous compared to passive (random) selection in case that a drift leads to persistent prediction bias allowing more rapid adaptation at lower reference measurement rates. Fully unsupervised adaptation using FLEXFIS-PLS could improve predictive accuracy significantly for light drifts but was not able to fully compensate for prediction bias in case of significant lack of fit w.r.t. the latent variable space.

11 *Keywords:* ensembled PLS, drift detection, committee disagreement, active learning, calibration
12 model maintenance by adaptation, weighted learning, melamine formaldehyde resin

13 **1. Introduction**

14 *1.1. Motivation and State-of-the-Art*

15 Melamine formaldehyde (MF) is an important class of thermosetting polymers, which have
16 found wide industrial application as coating and adhesive materials owing to their high thermal-
17 and chemical stability and physical resistance [1]. The properties of MF are largely determined
18 by the curing behavior and the degree of polymerization and cross-linking of the final product
19 [2]. It is therefore of pivotal interest to supervise the degree of polymerization (DP) during MF
20 resin production and to determine the optimal time point when the polymerization reaction should
21 be stopped. The water tolerance method and determination of free melamine concentration by
22 liquid chromatography (LC) are well established and widely used to assess the DP of MF resins
23 but produce significant cost in terms of material and human resources [3][4]. In addition, the
24 delay between sample collection and retrieval of the critical process information harbors the risk
25 of missing the optimal time point when the reaction has reached the desired DP [5]. In practice,
26 MF condensation processes are therefore often run below the theoretically possible speed in order
27 to minimize this risk at the expense of suboptimal allocation of resources.

28 Non-destructive estimation of free melamine content in MF resins by vibrational spectroscopy
29 has been demonstrated previously and holds promise for high-frequency in-line monitoring of MF
30 condensation [3]. Pawlicek *et al.* have recently established an online monitoring and control system
31 for MF resins based on Fourier-transform near infrared (FT-NIR) spectroscopy and demonstrated
32 the feasibility of accurate spectroscopic estimation of the turbidity point during the condensation
33 process [4]. However, it is widely appreciated that chemometric models, usually required for spec-
34 troscopic estimation of critical process parameters, often have a limited time-span during which
35 they deliver reliable predictions on new samples (e.g. spectra) and thus need regular supervision
36 and maintenance [6]. The breakdown of model reliability might occur either due to instrumen-
37 tal changes, changes in environmental conditions during spectra acquisition or changes in sample
38 composition (e.g. due to changing raw material composition) [7]. In any case, the relation between
39 FT-NIR spectra and the target values eventually gets altered by such *drifts*, which might ultimately
40 lead to prediction bias.

41 Maintenance of chemometric models can be roughly divided in two tasks: i) Detection of the
42 time point when any drift starts causing prediction bias (i.e. drift detection) and ii) model adap-
43 tation once a drift has been detected. Timely detection of drifts is crucial to avoid cost-intensive
44 manufacturing errors, defective production or even complete shutdown of the process [8]. Re-
45 calibration of chemometric models according to a static schedule using regularly collected refer-
46 ence measurements could eventually compensate for the occurrence of drifts to some extent, but
47 requires time-intensive modeling/validation cycles and disproportional efforts in terms of refer-
48 ence analytics. We have therefore recently proposed a self-adaptive calibration modelling strategy
49 employing non-linear fuzzy PLS models in order to automate off-line re-calibration and valida-
50 tion [5]. However, despite implicit drift handling [9], full supervised model adaptation employed
51 in [5] and [10] [11] require a high number of reference measurements and is thus of little prac-
52 tical relevance. In an attempt to reduce the amount of reference measurements Cernuda *et al.*
53 [12] proposed an active learning (AL) based approach to request (manual) reference measurements
54 for new samples when the corresponding spectra violate upper control limits for Hotelling's T^2

55 statistic or Q -residuals. Therein, the authors employed a sliding window approach featuring user-
56 defined thresholding of the rate at which reference measurement should be conducted. However,
57 despite dramatic reduction of reference measurements, the method performs permanent sample
58 selection and model re-calibration which may lead to superfluous reference measurements. In ad-
59 dition, employing a fixed window size might be problematic as large windows typically lack the
60 ability to keep pace with the dynamics induced by the drift while important sources of process
61 variability might be disregarded when using small ones. Other works on self-adaptive (evolving)
62 chemometric models have been proposed in [10] [11], but also require the full knowledge of target
63 measurements and are thus not applicable in our context. Active learning for off-line chemometric
64 calibration has been proposed in [13] [14]. However, these approaches are not directly applicable
65 for online model adaptation. For this reason, we here combine active learning along with explicit
66 drift detection: Initially trained chemometric models are updated according to a complete on-line,
67 single-pass active learning concept only once a drift has been detected. In addition, we also explore
68 unsupervised model adaptation exploiting the dual antecedent-consequent structure of the recently
69 proposed fuzzy systems variant of PLS (FLEXFIS-PLS) in order to reduce prediction bias.

70 1.2. Summary of Our Approach

71 We use linear and non-linear versions of (ensembled) partial least squares (PLS) in order to
72 establish initial calibration models for the determination of the turbidity point of MF resin during
73 polymerization. For the latter we use a previously described fuzzy-inference based PLS variant
74 termed FLEXFIS-PLS [15] to account for eventual non-linearities with the additional possibility
75 to update initially trained models in an unsupervised fashion. A novel type of drift detector based
76 on a faded version of the Page-Hinkley (PH) statistic [16] is introduced in order to determine the
77 time point when predictions start becoming unreliable and the model adaptation engine should be
78 turned on. In particular, we compute sample-wise prediction uncertainty as the variance of predic-
79 tions from an ensemble of PLS models, i.e. the *committee disagreement (CD)*, and incrementally
80 re-estimate the distribution of the PH statistic on the CD at every time instance [17]. This yields
81 adaptive control limits that are used to decide if a change has occurred. Model updates are triggered

82 only once these adaptive control limits are violated for the first time, which is an essential differ-
83 ence to the previous work in [12], where calibration models are *permanently* updated over sliding
84 windows.

85 We investigate different strategies for incremental updates of initially trained chemometric
86 models: i) Active learning in single-pass on-line mode based on violation of the well-known
87 Hotelling's T^2 - and Q -residual limits followed by automatic model re-calibration involving adap-
88 tive training set re-weighting (giving newer samples higher emphasis) and ii) unsupervised adapta-
89 tion of non-linear FLEXFIS-PLS models involving incremental adaptation of antecedents, which
90 affects only the position and spreads of the underlying fuzzy rules while maintaining the local linear
91 input-output relationships in the consequents. The rest of the paper is organized as follows: Sec-
92 tion 2 provides a brief description of the melamine resin production process and spectroscopic data
93 acquisition. Section 3 develops the theory behind PLS (3.2.1) and its non-linear variant FLEXFIS-
94 PLS (3.2.2) followed by a description of how these models are used for (un-) supervised model
95 adaptation in section 3.3. Active sample selection in single-pass mode is introduced in section
96 3.3.2. A novel drift detector combining committee disagreement and a modified variant of the
97 Page-Hinkley test is presented in section 3.4. Section 4 describes the experimental setup including
98 subsections describing data pre-treatment, model parametrization and method evaluation. A com-
99 parison of the proposed drift detector and different state-of-the-art (SoA) model diagnostic tools
100 (sample-specific standard errors, Hotelling's T^2 and Q -residuals) is presented in section 5 followed
101 by an evaluation of the proposed strategies for (automated) model adaptation (Sections 5.2 and
102 5.3). Conclusion are drawn in Section 6.

103 **2. Description of the Process and Data Acquisition**

104 The applied FT-NIR process spectrometer is a commercially available device (i-RED Infracot
105 Systeme, Austria). It is connected with three immersion probes through fiber optic equipment and
106 has been previously implemented at the MF resin production plant allowing parallel monitoring of
107 three reactors [18]. The optics of the spectrometer contain a monolithic Michelson interferometer

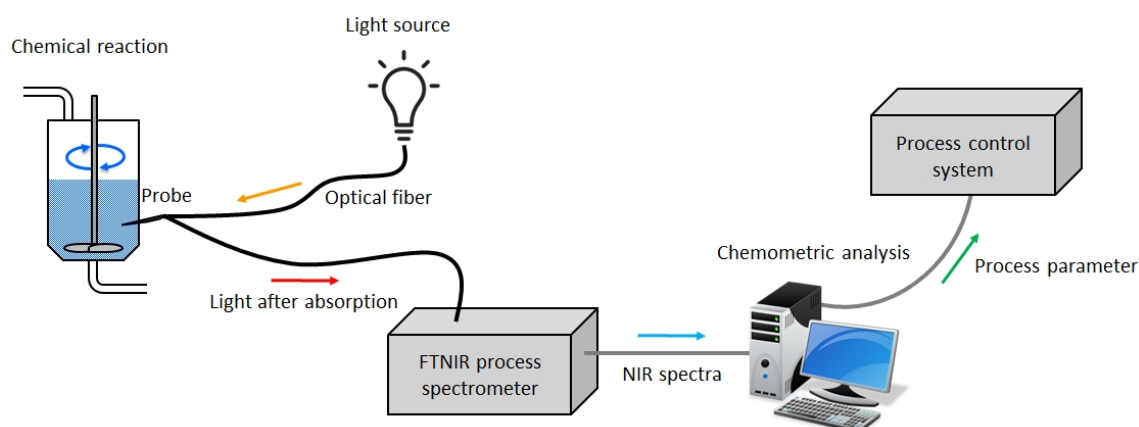


Figure 1: Scheme of the data acquisition process and its components in inter-communication with the chemical reactor

108 which is robust with respect to temperature changes [19] and uses a semiconductor reference laser.
 109 The resolution and the measurement rate of the instrument are configurable. The programmable
 110 logic controller, used for reading data acquired by sensors and controlling actuators, employs a
 111 field-bus interface using the CANopen protocol. Unlike conventional PLCs it supports large data
 112 structures like infrared spectra. Furthermore, it provides mechanisms for storing measurement data
 113 permanently to the 'process control system'.

114 A schematic overview of the data acquisition process and its interconnecting components at the
 115 process in the loop and in communication with the chemical reactor is visualized in Figure 1. A
 116 halogen light source provides infra-red light to a Hellma transmission probe (optical path length: 1
 117 mm) immersed directly into the resin inside the reactor. Despite accumulation of (solid) MF resin
 118 on the immersion probe at low temperatures, polymerisation can be adequately monitored during
 119 the critical phase of the process (i.e. towards the end of the reaction). An optical fiber (length:
 120 2×0.25 m), using quartz glass as fiber material (fiber type: AS600/660IRAN), is connected to the
 121 light source (halogen lamp) connecting the probe with the spectrometer. Its maximal and minimal
 122 immersion depth is 690 mm and 30 mm, respectively. The outer diameter is 25 mm and the pipe
 123 length of the probe is 700 mm. The temperature range of the product lies between 5°C and 260°C
 124 and the pressure range between 1 and 35 bar. The spectral range of the current setup expands from

125 820 nm to 2857 nm yielding spectra comprising a total of 2753 variables. The final spectra are
126 calculated as the average of 80 single shot interferograms, acquired during *ca.* 8 seconds.

127 During the condensation process, FT-NIR spectra and several process parameters (e.g. tem-
128 perature and pressure) are continuously collected from the process control system in real-time via
129 CANopen and permanently stored in a separate data server. Three consecutive spectra are recorded
130 within a few seconds and averaged in order to reduce the noise effect in single measurements. The
131 averaged spectra are then used for prediction and (eventual) model updates if necessary. The pre-
132 dicted values (i.e. turbidity points) are provided in real-time to the process control system. The
133 optimal endpoint of a batch is automatically determined based on prediction of the DP without
134 human intervention. In a second stage, the resin solution is cured using defined heat and pressure
135 yielding highly cross-linked MF resins.

136 **3. Theory**

137 *3.1. Notation*

138 Scalars are denoted by italic symbols (e.g. x or V). Lowercase and uppercase boldface symbols
139 denote column vectors (\mathbf{t}) and matrices (\mathbf{X}), respectively. Unless explicitly stated, vectors are
140 column vectors and superscripted symbols T and $^{-1}$ indicate the transpose and inverse, respectively
141 of a vector or matrix. Vertical concatenation of column vectors is indicated using comma notation
142 (e.g. $\mathbf{T} = [\mathbf{t}_1, \dots, \mathbf{t}_A]$). $\mathbb{E}[x]$ denotes the expected value of a random variable x .

143 *3.2. Chemometric Models*

144 *3.2.1. PLS and ensemble PLS*

Partial least squares (PLS) is aimed at finding a set of orthogonal direction vectors $\mathbf{w}_a \in \mathbb{R}^{K \times 1}$ for $a \in \{1, \dots, A\}$ such that projection of a matrix $\mathbf{X} \in \mathbb{R}^{N \times K}$ (of N samples and K covariates) on \mathbf{w}_a – termed scores \mathbf{t}_a – have maximal covariance with some target vector $\mathbf{y} \in \mathbb{R}^{N \times 1}$.

Formally,

$$\begin{aligned} \mathbf{w}_a &= \arg \max_{\mathbf{w}} \text{cov}(\mathbf{X}\mathbf{w}, \mathbf{y}) \\ \text{s.t. } \|\mathbf{w}_i\| &= 1 \text{ and } \mathbf{w}_i^T \mathbf{X}^T \mathbf{X} \mathbf{w}_i = 0 \text{ for } 1 \leq i \leq a. \end{aligned} \quad (1)$$

145 In the second step of PLS, \mathbf{y} is regressed on these new latent variables $\mathbf{T} = [\mathbf{t}_1, \dots, \mathbf{t}_A]$. Since
 146 usually $A \ll K$ sufficiently captures most of the variance in \mathbf{y} and the scores \mathbf{t}_a are mutually or-
 147 thogonal, $\mathbf{T}^T \mathbf{T}$ has full (column) rank and can thus be safely inverted circumventing the usual pitfall
 148 of least squares regression when coping with fat data matrices and/or highly correlated variables
 149 (which is usually the case for spectroscopic data). For a comprehensive introduction on PLS, we
 150 refer to [20] and for its application within an ensemble modelling scheme to [21]. We will exploit
 151 the latter by generating bootstrap samples from the calibration data [22]. In particular, for a given
 152 data set \mathbf{X} containing N samples, we randomly draw N samples with replacement and store them
 153 in a separate matrix \mathbf{X}_1 (termed one bag) — this procedure is repeated B times, yielding B bags
 154 $\mathbf{X}_1, \dots, \mathbf{X}_B$ each containing N samples. For each of the bags $\mathbf{X}_1, \dots, \mathbf{X}_B$, a separate PLS regression
 155 (PLSR) model is trained. During the prediction phase, the average prediction over all models is
 156 calculated to obtain the prediction \hat{y}_i on the i -th test sample, i.e.

$$\hat{y}_i = \frac{1}{B} \sum_{j=1}^B \hat{y}_i^{(j)}. \quad (2)$$

157 3.2.2. FLEXFIS-PLS (non-linear version of PLS)

158 We extend PLS to a non-linear version in order to be able to model any intrinsic non-linearity
 159 between latent features and reference measurements (i.e. turbidity points). In order to circumvent
 160 large-scale data matrices and/or extra (kernel) parameters as used in non-linear variants of PLS
 161 proposed in literature so far (such as in kernel-PLS [23]) and PLS variants employing non-linear
 162 modelling of the inner relationship between \mathbf{X} and \mathbf{y} [24] [25], we employ fuzzyfication of the latent
 163 variable space as previously described in [15] and [26], which allows capturing local data structures
 164 over the feature space – as exemplarily shown in Figure 2 for a simple two-dimensional example
 165 from a real-world process. Obviously, partitioning the data into two local regions and modelling

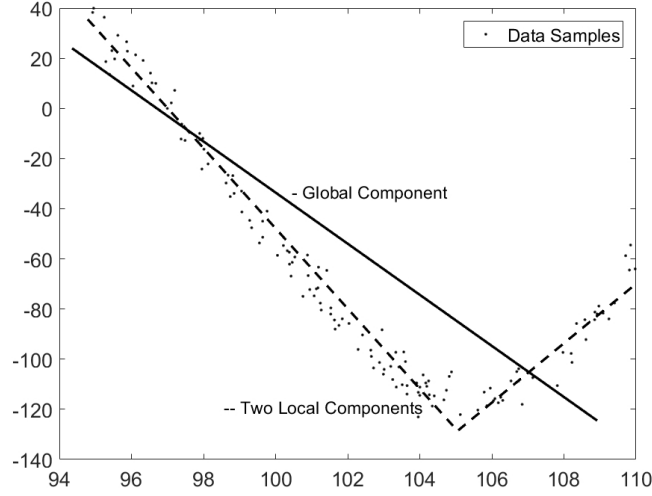


Figure 2: A two-dimensional example of local data clouds showing two components/trends (as dashed lines), which cannot be sufficiently resolved by a global, linear model (solid line).

166 the relationship between x and y for each region separately (dotted lines) is more appropriate than
 167 a global, linear model (solid line). The idea of our fuzzy modelling component is to obtain partial
 168 piece-wise linear predictors l_i for $i = 1, \dots, C$ local regions of the latent variable space:

$$l_i(\mathbf{t}) = \beta_{i0} + \beta_{i1}t_1 + \beta_{i2}t_2 + \dots + \beta_{iA}t_A, \quad (3)$$

169 amalgamated with multi-dimensional fuzzy rules defined through a multi-dimensional Gaussian
 170 kernel (implying ellipsoidal contours) to achieve smooth model outputs:

$$\hat{y} = \sum_{i=1}^C l_i(\mathbf{t})\Psi_i(\mathbf{t}) = \sum_{i=1}^C l_i(\mathbf{t}) \frac{\mu_i(\mathbf{t})}{\sum_{j=1}^C \mu_j(\mathbf{t})} \quad \mu_i(\mathbf{t}) = \exp\left(-\frac{1}{2}(\mathbf{t} - \mathbf{c}_i)^T \Sigma_i^{-1}(\mathbf{t} - \mathbf{c}_i)\right). \quad (4)$$

171 \mathbf{t} is the $A \times 1$ scores vector of a projected test sample, \mathbf{c}_i is the centroid of the i -th rule (i.e. the
 172 i -th local region of the latent variable space) and Σ_i^{-1} the corresponding local covariance matrix.
 173 This has some similarities with locally weighted regression [27], but produces a global, more inter-
 174 pretable model. For eliciting the optimal number of fuzzy rules (according to the non-linearity in
 175 the input-output relationship) and for synchronous estimation of the parameters in the antecedent

176 (i.e. $\mathbf{c}_i, \boldsymbol{\Sigma}_i^{-1}$) and consequent (i.e. $\boldsymbol{\beta}$) space, we employ a generalized evolving fuzzy systems learn-
 177 ing engine termed *Gen-Smart-EFS* [28]. A special case comes up when off-diagonal elements of
 178 the inverse covariance matrix $\boldsymbol{\Sigma}^{-1}$ are all set to 0 (ignoring the covariances between the inputs).
 179 In this case, axis-parallel fuzzy rules are triggered and the steps in the itemization above end up
 180 in the classical flexible fuzzy inference systems (FLEXFIS) approach [29], which we thus term
 181 *FLEXFIS-PLS*.

182 3.3. Model Adaptation

183 3.3.1. Update of PLS Models and Ensembles

184 For (ensemble) PLS models we propose a forgetting based weighting scheme in order to give
 185 new samples more emphasis during model re-calibration and outweigh older samples in the data
 186 stream. This leads to an increased flexibility when adapting to new 'drifted states'. In particular,
 187 we define a weighting function

$$\omega(i) = \lambda^{N-i}, \quad (5)$$

188 with λ being a forgetting factor typically set to a value between 0.9 and 1 (default 0.95), N is the
 189 number of labeled spectra in the actual calibration set (i.e. samples for which reference measure-
 190 ments are available) and $i \in \{1, \dots, N\}$ denotes time increments (from old to new). We normalize
 191 $\omega(i)$ such that $\sum_1^N \omega_i = N$ and define a $N \times N$ diagonal matrix \mathbf{G} with the i -th element being
 192 $g_{i,i} = \omega_i$. Finally, we solve the weighted PLS problem by replacing \mathbf{X} with $\mathbf{X}_G = \mathbf{G}\mathbf{X}$ in (1) when
 193 a new reference measurement becomes available.

194 3.3.2. Active Learning

195 For supervised model updates, a sample selection strategy becomes indispensable in order to
 196 keep measurement costs low. We here use violation of the critical limits of the well established
 197 Hotelling's T^2 and Q -Residual statistics as criterion to request reference measurements of incoming
 198 test samples as described previously in [12]. Hotelling's T^2 is proportional to the distance of a

199 projected sample to the training data centroid in the latent variable space. Per definition

$$T^2 = \sum_{j=1}^A \left(\frac{t_j}{\lambda_j} \right)^2, \quad (6)$$

200 where A denotes the total number of latent variables considered in the model and t_j denotes the
 201 score of a test spectrum when projected on the j -th loading vector \mathbf{p}_j with eigenvalue λ_j . Critical
 202 limits for T^2 are calculated by exploiting the relationship [30]

$$T^2 \sim \frac{A(K-1)}{K-A} F_{(A, K-A)}, \quad (7)$$

203 where A and K denote the number of LVs and number of original variables, respectively. $F(A, K -$
 204 $A)$ is the Fischer-Snedecor distribution with A and $K - A$ degrees of freedom in the numerator
 205 and denominator, respectively. In contrast to Hotelling's T^2 , which only considers the distance in
 206 the projected space, Q -Residuals are a measure of how well a test datum is represented by this
 207 subspace. Geometrically, they can be regarded as (orthogonal) distance between the datum in the
 208 original (high dimensional) space and its projection on A -dimensional latent feature space. For the
 209 i -th test datum

$$Q_i = \|\mathbf{x}_i - \mathbf{x}_i \mathbf{P}_A \mathbf{P}_A^T\|_F^2. \quad (8)$$

210 $\mathbf{P}_A \in \mathbb{R}^{K \times A}$ is the loadings matrix that projects x_i to the A dimensional latent feature space. Similar
 211 to Hotelling's T^2 , upper confidence bounds on Q -Residuals are often used in process monitoring in
 212 order to check whether spectra from incoming samples are well described by the model. We here
 213 used the Jackson-Mudholkar approximation [30]

$$Q_\alpha = \Phi_1 \left[\frac{c_\alpha \sqrt{2\Phi_2 h_0^2}}{\Phi_1} + 1 + \frac{\Phi_2 h_0 (h_0 - 1)}{\Phi_1^2} \right]^{1/h_0} \quad (9)$$

214 with

$$\Phi_i = \sum_{j=A+1}^M \lambda_j^z, \text{ for } z = \{1, 2, 3\}, \quad M = \min(N, K) \quad (10)$$

215 and

$$h_0 = 1 - \frac{2\Phi_1 \Phi_3}{3\Phi_2^2}. \quad (11)$$

216 c_α is the standard normal deviate corresponding to the upper $(1-\alpha)$ quantile and α is typically set to
 217 0.95 or 0.99. As a lack of fit statistic, Q -Residuals tend to exceed these confidence limits if test data
 218 contain unmodelled information, which is usually indicative of a change in covariance structure
 219 (e.g. due to the presence of a new interferent). Combined together, a reference measurement for
 220 the i -th test sample is requested if

$$T_i^2 > T_\alpha^2 \text{ or } Q_i > Q_\alpha, \quad (12)$$

221 with T_α^2 and Q_α denoting the critical limits for Hotelling's T^2 and Q -Residuals calculated accord-
 222 ing to (7) and (9). α was systematically varied in order to investigate the relationship between
 223 critical limits, number of selected AL samples and resulting prediction error, (see Section 4.3). For
 224 ensemble PLS, a reference measurement was requested if either limit in (12) was violated for at
 225 least one of the models in the committee.

226 3.3.3. FLEXFIS-PLS Model Update in Unsupervised Mode

Unsupervised adaptation of FLEXFIS-PLS models is carried out by first determining the clos-
 est rule from a test spectrum in terms of the Mahalanobis distance to the corresponding rule's center
 in the latent variable space. The position of the winning rule

$$\mathbf{c}_{win} = \arg \min_{i=1, \dots, C} d(\mathbf{t}, \mathbf{c}_i) \quad (13)$$

227 is then updated according to

$$\mathbf{c}_{win}(N_{win} + 1) = \mathbf{c}_{win}(N_{win}) + \frac{\omega(\mathbf{t})}{\eta_{win}}(\mathbf{t} - \mathbf{c}_{win}(N_{win})). \quad (14)$$

228 \mathbf{t} denotes the scores vector obtained by projection (i.e. $\mathbf{t} = \mathbf{x}\mathbf{W}$), N_{win} denotes the support of the
 229 winning rule (i.e. the number of calibration samples contained in it), $\omega(\mathbf{t})$ is the weight assigned
 230 to the current sample according to (5) and η_{win} is the learning gain for the winning rule (i.e. $\frac{1}{N_{win}}$).
 231 Likewise, the spread of the winning rule (i.e. the variance σ_{win}^2 in each direction), is adapted
 232 through recursive variance update including rank-1 modification for increased stability [31]. where

233 the new contribution of the current sample to the variance, i.e. $(\mathbf{t} - \mathbf{c}_i(N_{win} + 1))^2$, is weighted by
 234 $\omega(\mathbf{t})$:

$$\sigma_{win}^2(N_{win} + 1) = \frac{N_{win}}{N_{win} + 1} \sigma_{win}^2(N_{win}) + \Delta c_{win}^2 + \frac{\omega(\mathbf{t})}{N_{win} + 1} (c_{win}(N_{win} + 1) - \mathbf{t})^2 \quad (15)$$

235 with $\Delta c_{win}^2 = (c_{win}(N_{win}) - c_{win}(N_{win} + 1))^2$, i.e. the difference between the updated and the old posi-
 236 tion of the cluster center (rank-1 modification [31]). In contrast to the original, fully (unweighted)
 237 supervised adaptation of FLEXFIS-PLS [15], the consequent parameters (i.e. the coefficients for
 238 the local linear predictors) are kept fixed (once estimated from an initial batch training set). Hence,
 239 only adaptation of the positions and spreads of the rule contours (defined though multivariate nor-
 240 mal distributions) is performed in order to account for changes in the input space.

241 3.4. Drift Detection

242 3.4.1. Test of Page and Hinkley

243 The test of Page-Hinkley (PH) is a cumulative sum based change detector of some normally
 244 distributed quality indicator θ [32] [33]. For a test datum, sampled at time point T , the PH statistic
 245 is defined as:

$$PH_T = S_T - \min_{0 \leq t \leq T} S_t \quad (16)$$

246 with

$$S_T = \sum_{t=1}^T (\theta_t - \bar{\theta}_{T-1} - \delta). \quad (17)$$

247 $\bar{\theta}_{T-1}$ is the average of all θ 's up to time point $T - 1$ and δ is the magnitude of the acceptable change
 248 in θ (usually set close to 0). A drift is detected if $PH_T > \lambda$. Lughofer *et al.* [16] adapted the test in
 249 the context of stream mining by introducing a fading factor $\alpha \in [0, 1]$ to outweigh older samples in
 250 the stream yielding

$$S_T = (\theta_T - \bar{\theta}_{T-1} - \delta) + \alpha S_{T-1}, \quad (18)$$

This faded version of the PH test is particularly useful if several drifts are present in a data stream
 [16]. In order to become independent from setting the threshold λ to a fixed value, we further

propose a modification involving incremental updates of mean and standard deviation of the PH statistic according to

$$\overline{\text{PH}}_T = T * \overline{\text{PH}}_{T-1} + \frac{1}{T+1} \text{PH}_T \quad (19)$$

and

$$\sigma_{\text{PH}_T} = (\overline{\text{PH}}_T - \overline{\text{PH}}_{T-1})^2 + \sqrt{\frac{T}{T+1} * \sigma_{\text{PH}_{T-1}}^2 + \frac{1}{T+1} (\overline{\text{PH}}_T - \text{PH}_T)^2}, \quad (20)$$

respectively and defining (pseudo-) statistical control limits at $\overline{\text{PH}}_t \pm 3\sigma_{\text{PH}_t}$ at each instance $t = \{1, \dots, T\}$. Violation of these limits indicates that a drift has occurred, i.e. whenever either

$$\text{PH}_T \geq \overline{\text{PH}}_{T-1} + 3\sigma_{\text{PH}_{T-1}} \quad (21)$$

in case that θ is increasing or

$$\text{PH}_T \leq \overline{\text{PH}}_{T-1} - 3\sigma_{\text{PH}_{T-1}}, \quad (22)$$

251 otherwise.

252 3.4.2. Committee Disagreement (CD)

253 In order to assess the quality θ of a prediction from a chemometric model we propose the
 254 committee disagreement degree (CD), which is computed as the variance among predictions from
 255 individual models of an ensemble trained on different subsets of the calibration set. For the i -th test
 256 spectrum

$$\text{CD}(x_i) = \frac{1}{B} \sum_{j=1}^B (V^{(j)}(x_i) - \bar{V}(x_i))^2, \quad (23)$$

257 where $V^{(j)}(x_i)$ denotes the prediction from the j -th model and $\bar{V}(x_i)$ is the average prediction on x_i
 258 among the B models in the committee. It can be shown that $\mathbb{E}[\text{CD}]$ is a lower bound for the squared
 259 generalization error of the committee and an increasing CD over time, on average, thus indicates
 260 that the error associated with model predictions is increasing [34]. Similar to Hotelling's T^2 and Q -
 261 Residuals, no target values are required to compute the CD, which is in contrast to other supervised

262 approaches for drift detection (based on model errors etc.) [35] [36] [37]. However, in contrast to
 263 these more traditional approaches to anomaly detection in chemometrics, the CD is based on actual
 264 predictions rather than on mere outlyingness with respect to the calibration samples or the latent
 265 variable subspace. This latter point is important since multivariate calibration models often tend
 266 to be capable of extrapolating considerably beyond the training samples and consequently may
 267 deliver accurate predictions despite significant violations of statistical control limits [6].

268 3.4.3. Other quality metrics for assessing the quality of predictions

269 *Sample-Wise Prediction Uncertainty.* In order to estimate sample-wise prediction uncertainty, we
 270 here use the approximation proposed by Faber and Bro [38], i.e.

$$\sigma_{\text{PE}} \approx \sqrt{(1 + h_{\text{test}}) * \text{MSEC} - V_{\Delta y}}, \quad (24)$$

271 where $h_{\text{test}} = \mathbf{t}_{\text{test}}^T (\mathbf{T}^T \mathbf{T})^{-1} \mathbf{t}_{\text{test}}$ is the leverage of a test spectrum, $\mathbf{t}_{\text{test}} \in \mathbb{R}^{A \times 1}$ denotes the scores
 272 obtained by projection on the A latent variables retained in the model and $\mathbf{T} \in \mathbb{R}^{N \times A}$ is the scores
 273 matrix from the training samples. The mean squared error of calibration (MSEC) is obtained in the
 274 usual way and $V_{\Delta y}$ denotes the variance (uncertainty) of the reference measurements in the training
 275 set. The latter was set to 0 in all experiments since we were interested in how uncertainty changes
 276 (increases) when spectra become affected by potential drifts rather than estimating the uncertainty
 277 itself.

278 *Hotelling's T^2 and Q -Residuals.* Although T^2 and Q -Residuals (Section 3.3.2) are no direct mea-
 279 sures for the reliability of predictions from latent variable models they are widely used in chemo-
 280 metrics as a guide for practitioners to decide if normal operation conditions are violated. However,
 281 as stated by Wise *et al.* [6], multivariate calibration models are often capable to considerably ex-
 282 trapolate beyond the widely used 95% and 99% confidence limits, which is particularly true for
 283 the former. In case of high Q -residuals - usually indicative for the presence of a new source of
 284 variation that has not been accounted for in the calibration step (e.g. due to the presence of a new
 285 interferent) — prediction accuracy is affected only in case that the net analyte signal is affected.

Table 1: Dataset characteristics.

Scenario	# Variables	# Samples		# Drifts
		Cal	Test	
1	346	7521	1251	1
2	346	1442	129	3
3	346	2334	720	2

286 4. Experimental Setup

287 4.1. Dataset Characteristics and Data pre-treatment

288 Three drift effects were observed during the observation horizon, which are covered by three
 289 datasets further referred to as scenarios 1-3 (Table 1). All spectra were smoothed using the
 290 Savitzky-Golay algorithm (15 smoothing points, 0-th order polynomial) and subsequently nor-
 291 malized by the standard normal variate (SNV) normalization method applied to the entire spectral
 292 range comprising at total of 2753 variables. All models were calibrated using a combination of the
 293 following spectral ranges: 1599 – 1824 nm and 1434 – 1516 nm (Figure 3). These two spectral
 294 ranges include the carbon-hydrogen and especially the oxygen-hydrogen and water bands which
 295 typically change during the condensation process and are thus most suitable for process moni-
 296 toring. The selection of the relevant spectral ranges was performed manually based on chemical
 297 knowledge of experts at Metadynea Austria GmbH and RECENDT GmbH.

298 4.2. Model Parametrization

299 4.2.1. PLS

300 PLS models were fitted using PLS-Toolbox 8.2.1 (Eigenvector Research, Manson, WA, USA)
 301 and Matlab 2015a (Mathworks, Natick, MA, USA). The optimal complexity of PLS models was
 302 determined by 10-fold cross-validation (CV). To this end, the number of latent variables was varied
 303 between 1 and 15 and the root mean squared error of cross-validation (RMSECV) calculated in the
 304 usual way. Minimization of the CV error w.r.t the number of LVs often yields PLS models that are

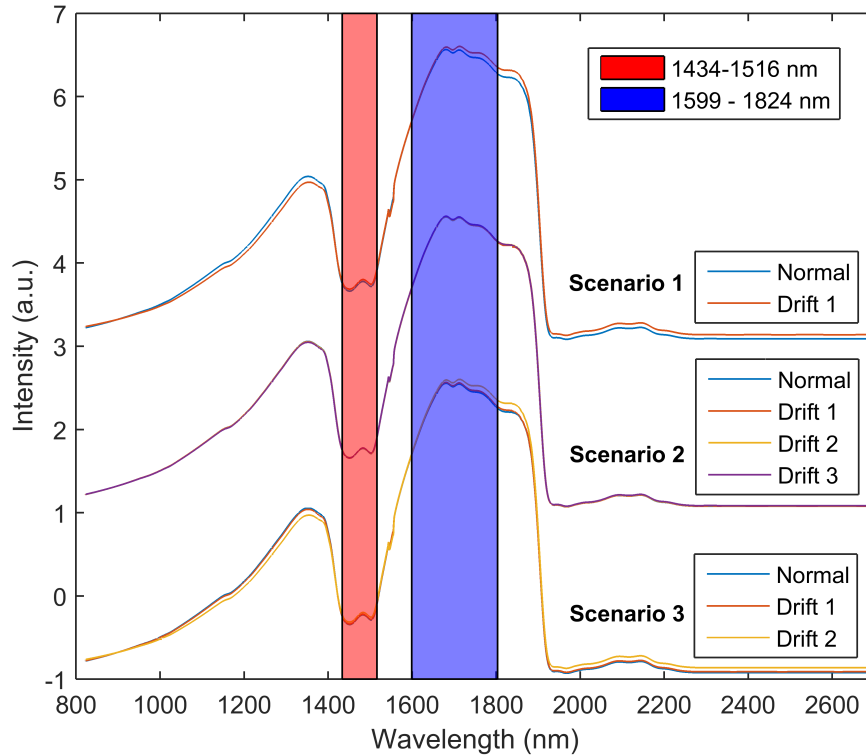


Figure 3: Representative FT-NIR spectra of Melamine Formaldehyde (MF) resin. Wavelength regions used for modelling the turbidity point are indicated. An average spectrum representing the normal condition and average spectra of drifted states are shown for each of the 3 investigated scenarios.

305 too complex. We therefore choose the optimal number of LVs by minimizing a penalized CV error
 306 criterion

$$\text{RMSECV}_{pen} = \text{RMSECV} \times \exp(0.05 \times \#\text{LVs}), \quad (25)$$

307 which includes a penalty for the number of latent variables (Figure 4). Ensemble PLS (ePLS)
 308 models were established by taking bootstrap samples from the pool of calibration data. The number
 309 of individual PLS models (i.e. committee members) was set to 20 in all experiments to achieve a
 310 fair comparison — based on several initial experiments, it turned out that this number is pretty
 311 insensitive for the results, anyway.

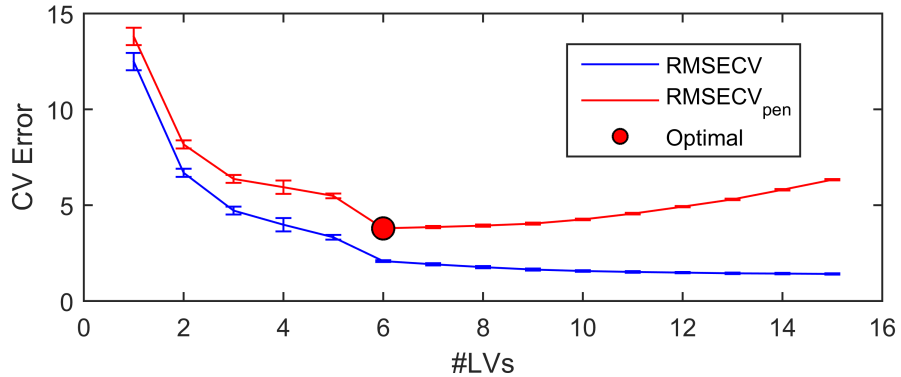


Figure 4: Model selection. The optimal model complexity in terms of number of latent variables (LV) is determined by minimizing (25) in order to penalize for inclusion of too many LVs.

312 4.2.2. FLEXFIS-PLS

313 In addition to the number of LVs, the number of fuzzy rules controlling the degree of non-
 314 linearity in the input-output relationship has to be tuned for FLEXFIS-PLS. To this end we set up
 315 the search grid for the number of LVs and fuzzy rules in the range between 1 and 15 for the former
 316 and 1-10 for the latter. Each parameter combination was evaluated by 10-fold CV and the resulting
 317 CV error penalized for complexity yielding a penalized CV error criterion (as an extension of the
 318 criterion in (25)):

$$\text{RMSECV}_{pen} = \text{RMSECV} \times \exp[0.05(\#\text{LVs} + \#\text{Fuzzy Rules})], \quad (26)$$

319 which was minimized in order to obtain the optimal parameter combination for the final model.
 320 The value of 0.05 in the exponential term is a default value we successfully used for various other
 321 applications and (spectroscopic) data in the past.

322 4.3. Method Evaluation

323 *Performance Comparison.* The performance of calibration models with and without model adap-
 324 tation was compared by means of the global root mean squared error of prediction

$$\text{RMSEP}_{glob} = \sqrt{\frac{1}{N_t} \sum_{i=1}^{N_t} (\hat{y}_i - y_i)^2}, \quad (27)$$

325 where \hat{y}_i and y_i denote predicted and measured turbidity points and N_t is the number of test sam-
 326 ples used for evaluation. Since the analytical goal in melamine resin production is to accurately
 327 determine when condensation should be stopped, we also assessed the RMSEP locally in the region
 328 $y = [20, 40]$ close to the end point of the reaction, i.e.

$$\text{RMSEP}_{loc} = \sqrt{\frac{1}{N_{[20,40]}} \sum_{y \in [20,40]} (\hat{y}_i - y_i)^2}. \quad (28)$$

329 In order to systematically examine active learning, significance levels α in (12) were varied within
 330 the values $[0.999, 0.99, 0.95, 0.9, 0.75, 0.5]$ in order to change the frequency of reference measure-
 331 ments and model updates. In addition, active sample selection was compared to passive selection
 332 in terms of RMSEP improvements over static models. For the latter, equidistant sampling was used
 333 at the same rate as in active learning at a given α to allow direct comparison.

334 5. Results

335 5.1. Drift Detection

336 To study the merit of incrementally adapting control limits on the Page-Hinkley (PH) statistic,
 337 different model diagnostic measures including prediction uncertainty, Hotelling's T^2 , Q -Residuals
 338 and committee disagreement (CD) were tracked over time in 3 different drift scenarios (Figure 5).
 339 Since all of these quantities tend to increase as predictions become biased, only violation of the up-
 340 per control limit on the PH statistic was considered for drift detection; i.e., only equation (21) was
 341 used and shown as black-lined threshold in Figure 5. The top row in figure 5 shows the evolution of
 342 the residuals (i.e. absolute difference between measured and predicted turbidity points) produced
 343 by the corresponding chemometric models (without model adaptation). In the first scenario, con-
 344 siderable prediction bias is introduced around sample 650 with predictions for downstream samples
 345 becoming considerably shifted. In the second and third scenario, prediction bias is transient and
 346 the models deliver accurate predictions in between. In addition, predictions start drifting severely
 347 towards the end of the recordings for the latter. Analysis of the control charts based on the PH
 348 statistic revealed that prediction uncertainty ($\hat{\sigma}_{PE}$) and Hotelling's T^2 failed to report timely on the

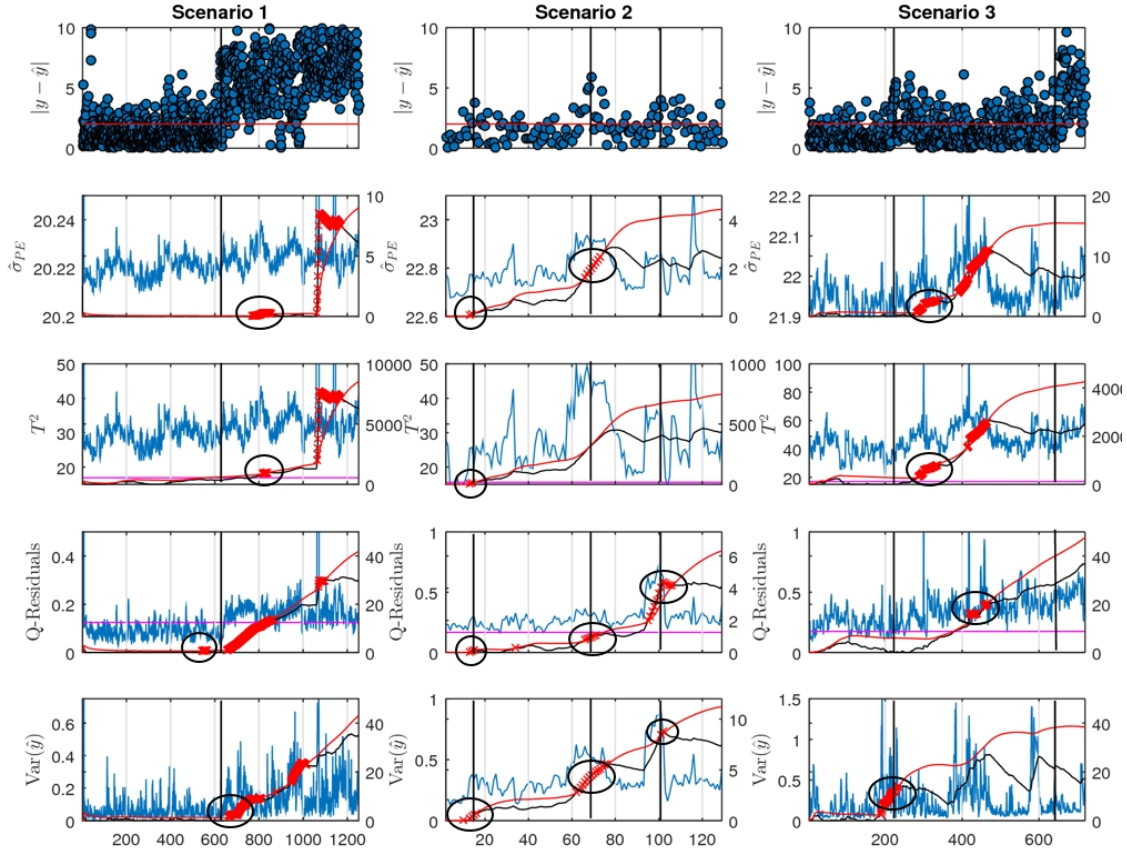


Figure 5: Drift detection by faded Page-Hinkley test using incrementally evolving control limits. Top row: Absolute difference between observed and predicted turbidity point temperatures for three independent test scenarios using static (SoA) calibration models. The horizontal line indicates the desired analytical accuracy of the model. Subsequent rows show evolution of corresponding model diagnostic measures for each scenario in the following order: $\hat{\sigma}_{PE}$: prediction uncertainty (24), T^2 : Hotelling's $T^2(6)$, Q -residuals (8), $\text{Var}(\hat{y})$: Committee disagreement (23). Blue lines indicate the raw data, evolution of the Page-Hinkley statistic and the corresponding upper threshold according to (21) are shown as black and red lines, respectively. Red crosses mark violations of the upper control limit by the the PH statistic. Solid ellipsoids mark those violations closest to real drifts, which are indicated by vertical lines and which have been determined by the experts from the company partner.

349 drift seen in scenario 1, whereas upper adaptive control limits were violated around the time point
 350 when the drift occurred for the Q -residuals and the committee disagreement. However, the former
 351 gave rise to an alarm fairly before the drift actually occurs, which is considered a false alarm. In

Table 2: Comparison of the performance of different drift detection methods based on four indicators, including our proposed CD (committee disagreement); bold font indicate best results over the four variants.

Indicator	Detection Capability	Sign. Delays (> 50 samples)	# of False Alarms
σ_{PE}	4 out of 6	2 times	2
T^2	3 out of 6	2 times	2
Q	4 out of 6	0 times	3
CD (ours)	5 out of 6	0 times	1

352 scenario 2, the PH statistic successfully indicated occurrence of a drift around sample No. 12 for all
353 investigated diagnostic measures. In addition, the drop in accuracy around sample 70 and 100 was
354 successfully reported by either Q -Residuals and the CD, but not by Hotelling’s T^2 . The behavior
355 of the diagnostic measures was most divergent for scenario 3 with the CD successfully reporting
356 on the increase in prediction error around sample 200. However, all variants failed to detect the
357 second drift towards the end of the stream in this scenario. In contrast, the PH statistic computed
358 from the Q -Residuals did not indicate unusual behavior of the model around sample 200 but viola-
359 tion of the control limit was given around sample 400, which however must be regarded as a false
360 alarm. In addition to violations around sample 400, Hotelling’s T^2 and $\hat{\sigma}_{PE}$ displayed violations
361 around 250 – slightly delayed with respect to the high errors seen around sample 200. Finally, we
362 observed that the PH statistic associated with CD (and to some extent also with the Q -Residuals)
363 *correctly* decreased as predictive accuracy increased again in case of the transient effects causing
364 prediction bias in scenario 2 and 3. In case of scenario 2, the third drift was solely detected by
365 the CD and the Q -Residuals. The overall performance over all six drift cases in the three streams
366 is summarized in Table 2, reflecting more clearly the out-performance of SoA indicators by our
367 proposed committee disagreement variant: the columns denote i) the detection capability in terms
368 of the number of drifts that were correctly detected, ii) the number of significant delays (> 50
369 samples) between drift and detection and iii) the number of false alarms that were triggered by
370 the corresponding model diagnostic measure. These numbers are calculated based on the fact that

371 the experts saw a significant delay in detecting a drift correctly in case of more than 25 samples.
372 Due to an implicit uncertainty of the experts about the exact location of a drift, there has been also
373 respected a tolerance of 25 samples before and after the vertical lines (indicating the most likely
374 drift positions defined by experts) when evaluating the drift detection performance. This means
375 that no false alarm is counted when a drift is detected up to 25 samples before, and no significant
376 delay is counted when a drift is detected up to 50 samples ($25 + 25$ — as indicated in the first row
377 of Table 2) after the expert-defined drift positions.

378 5.2. Active Learning (AL)

379 In order to guide adaptation of chemometric models when a drift has been detected, we first
380 investigated a previously described AL strategy that builds upon the idea to request reference mea-
381 surements for samples (spectra) that violate critical limits of Hotelling’s T^2 and/or Q -residuals. As
382 soon as the reference information is available, the calibration set is extended by this sample and the
383 model automatically re-calibrated using the techniques described in section 3.3. We here further
384 extended this approach by incorporating gradual forgetting of older samples and by placing more
385 emphasis on newer samples, which is in contrast to our previous sliding window approach that
386 eventually discards samples encoding important process variability. The automatic model update
387 engine is activated upon the first violation of the incrementally adapting threshold on the PH statis-
388 tic associated with the CD as it was the overall best measure for drift detection over all 3 scenarios.
389 Critical limits for Hotelling’s T^2 and Q -Residuals were systematically varied in order to control the
390 number of violations and thus the frequency at which reference measurement should be performed.
391 Figure 6 compares model adaptation based on active vs. passive (i.e. random) selection of sam-
392 ples in the 3 scenarios. We found that active sample selection performed favorably over random
393 selection in scenario 1. Thereby, accuracy could be significantly increased from RMSEP = 3.56
394 corresponding to the reference model (without adaptation) to an acceptable level (i.e. RMSEP be-
395 tween 1.9 and 2.5) when requesting reference measurements at a rate of 5 – 10% corresponding
396 to $\approx 30 - 60$ samples over the entire stream (Table 3). In contrast, active selection did not yield
397 consistently better results than passive selection in scenarios 2 and 3, which can be attributed to the

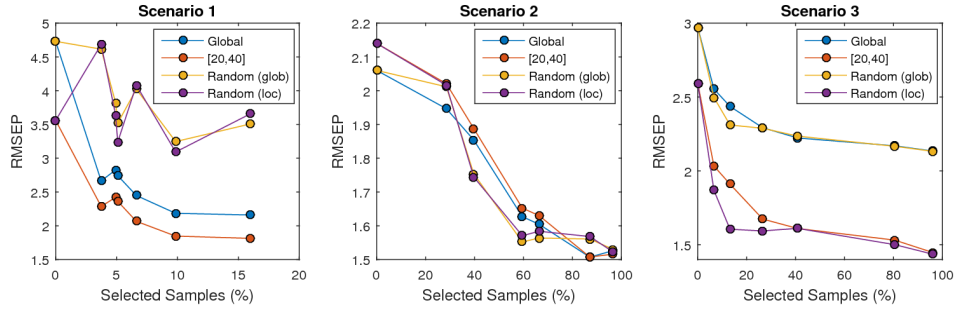


Figure 6: Active learning vs. random selection of samples for ensemble PLS. Global and local (i.e. in the turbidity point range of [20,40]) root mean squared errors of prediction are shown for sample selection by active learning and equidistant, random selection at the same sampling frequencies.

398 transient nature of the drifts in these scenarios. While the AL engine runs into danger of triggering
 399 re-calibration based on outlying samples leading to deterioration of predictive accuracy, equidis-
 400 tant (random) selection can be more robust with respect to putative outliers or transient drifts. This
 401 effect was most pronounced when the fraction of samples selected for model adaptation was small
 402 and flattens out as more re-calibration samples were included. Yet overall, accuracy could be kept
 403 within an acceptable range in scenarios 2 and 3 irrespective of how re-calibration samples were
 404 selected.

405 5.3. Unsupervised Model Adaptation

406 We recently introduced a fuzzy systems version of PLS (FLEXFIS-PLS) that performs parti-
 407 tioning of the latent variable space, similar to locally weighted regression, in order to model non-
 408 linear relationships between inputs and targets. Notably, the FLEXFIS-PLS architecture allows
 409 unsupervised adaptation of trained models in single-pass mode (i.e. without the need to re-evaluate
 410 the entire calibration set). To this end, the center and spread of the local region closest to the
 411 current sample is incrementally updated towards this sample. This in turn gradually changes the
 412 membership degree function in Equation (4) and thus the weighting of the local linear predictors
 413 during inference.

414 We first investigated if the static version of non-linear FLEXFIS-PLS can outperform ordinary,

415 linear ensemble PLS on the three scenarios (without adaptation). On the one hand, we found that
416 increasing the number of fuzzy rules beyond 1 did in general not increase accuracy of FLEXFIS-
417 PLS models (results not shown) indicating that the relationship between the LVs and the turbidity
418 point is highly linear. On the other hand ePLS and static FLEXFIS-PLS – which correspond
419 to ordinary PLS if the number of fuzzy rules is 1 – performed comparably except for scenario
420 1 where ePLS significantly outperformed static FLEXFIS-PLS. This finding is in line with an
421 improved bias-variance trade-off resulting from bagging as discussed in detail in [39]. We next
422 investigated the ability of the FLEXFIS-PLS architecture to adapt to the drifts through single-pass
423 updates of the models’ antecedents when the number of fuzzy rules was > 1 (Figure 7), termed
424 as unsupervised adaptation in Table 3 below. Similar to active learning, adaptation was initiated
425 by the first detection of a drift. However, in contrast to AL, all subsequent samples were used
426 for model adaptation without restriction. Overall, we found significant improvements in terms of
427 the RMSEP in scenario 2 and 3, while only the global error could be improved with respect to
428 the reference model (without adaptation) in scenario 1. This latter finding can be explained by the
429 abundance of low turbidity point samples (for which $y \ll 20$) in the first dataset due to the fact that
430 process monitoring was carried out manually after occurrence of the drift. We further found that the
431 ability to adapt to the drifts was strongly dependent on the number of fuzzy rules employed, which
432 corresponds to the non-linearity degree of the models. In scenario 2, two fuzzy rules yielded the
433 best performance, while 8 rules were optimal in scenario 3 (Table 3). Increasing the non-linearity
434 degree beyond the optimal value led to rapid increase of prediction errors, which can be attributed
435 to overfitting.

436 *5.4. Discussion and Overall Performance*

437 We here applied the Page-Hinkley test to detect changes in different model diagnostic quantities
438 associated with chemometric models in order to determine the time point when initially deployed
439 models should be adapted. In our extension, control limits are derived autonomously by incremen-
440 tal estimation of the mean and standard deviation of the PH statistic, which proved successful for
441 reliable detection of abrupt changes in prediction accuracy irrespective of the scale of the underly-

Table 3: Results summary. The (average) number of latent variables retained in the model, number of fuzzy rules employed for unsupervised model adaptation, local (i.e. in the turbidity point range of [20,40]) and global RMSEP for each method are shown. For active learning, RMSEP values refer to a frequency of $\approx 10\%$ reference measurements used for model adaptation.

Method		# LVs (# Fuzzy Rules)	RMSEP	
			local	global
Scenario 1	Static ePLS	9	3.56	4.73
	Unsupervised Adaptation	9 (1)	3.7	4.8
	Active Learning ($\approx 10\%$)	9	1.85	2.19
Scenario 2	Static ePLS	8	2.06	2.14
	Unsupervised Adaptation	8 (2)	2.01	2.10
	Active Learning ($\approx 10\%$)	8	2.07	2.05
Scenario 3	Static ePLS	8	2.62	3.00
	Unsupervised Adaptation	8 (8)	2.16	2.64
	Active Learning ($\approx 10\%$)	8	1.6	2.0

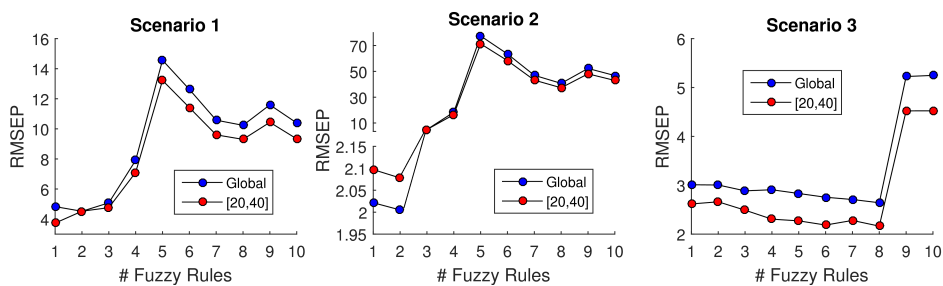


Figure 7: Unsupervised model adaptation by FLEXFIS-PLS. The change of global and local (i.e. in the turbidity temperature range of [20,40]) RMSEP vs. number of fuzzy rules is shown for scenarios 1-3. Data points where # Fuzzy Rules = 1 indicate the accuracy of FLEXFIS-PLS without adaptation.

442 ing diagnostic measure. This latter point is important since in real world applications, diagnostic
 443 measures often tend to violate (rigid) statistical thresholds without implications in terms of predic-
 444 tion bias. For instance, Hotelling’s T^2 was trending above the 95%-CI in all 3 scenarios most of
 445 the time while predictions were (mostly) fine. In addition, the most common diagnostic measures
 446 in chemometrics (i.e. T^2 and Q -Residuals) relate to some sort of similarity between test datum
 447 and calibration samples without taking into account the inference process. To this end we proposed
 448 the committee disagreement (CD) as a diagnostic measure, which takes this aspect into consider-
 449 ation. Notably, we found that the CD was the only quantity for which our drift detector gave an
 450 alarm when prediction bias significantly increased for the first time in all 3 investigated scenarios
 451 underpinning the importance of this aspect. Once a drift has been confirmed, active learning based
 452 on violations of Hotelling’s T^2 and Q -residuals proved successful to keep the overall accuracy of
 453 chemometric models within the analytical goal while at the same time minimizing the number of
 454 reference measurements required for adaptation. AL proved particularly successful when predic-
 455 tions from initial models became persistently biased (scenario 1). In case of transient drifts on the
 456 other hand (scenarios 2 and 3), AL could in fact not outperform random selection when using the
 457 same low number of samples (< 10%) for model adaptation. However, these results do not gener-
 458 ally lead us to conclude that AL is not suitable in case that a drift is only transient: The fact that
 459 adaptation based on AL did not significantly increase prediction bias compared to random sample

460 selection actually underpins the robustness and flexibility of AL in combination with automated
461 model re-calibration.

462 Regarding unsupervised model adaptation of the fuzzy rule-bases in FLEXFIS-PLS, our results
463 clearly demonstrate significant improvements in all scenarios (compared to static FLEXFIS-PLS
464 models). However, model adaptation could not appropriately compensate for the severe drift in
465 scenario 1, which can be attributed to the fact that a strong change in covariance structure occurred
466 in this scenario (indicated by the sudden increase of the Q -residuals around sample 660). In such
467 case, adaptation of the latent variable space based on additional (reference) measurements becomes
468 indispensable. For the lighter drifts (scenarios 2 and 3), unsupervised model adaptation could
469 significantly reduce the RMSEP of static models provided that model complexity (# Fuzzy Rules)
470 was appropriate. Yet, model selection by traditional cross-validation on the calibration data is of
471 little use for the determination of the optimal complexity since optimality largely depends on the
472 particular drift situation, which is not known beforehand. Future work on unsupervised model
473 adaptation should therefore address this dilemma in more detail.

474 Finally, in Table 4 we compare the overall performance of the calibration model maintenance
475 strategies in terms of their cost-benefit tradeoff including results based on sliding window SW-PLS
476 with and without active learning (but without explicit drift detection) as applied and compared be-
477 fore in [40] for exactly the same application scenario (the same production site). Notably, reference
478 sample selection by AL and subsequent model adaptation by re-calibration dramatically reduces the
479 overall error compared to the reference model (static ePLS). The improvements obtained through
480 i) using ensembles rather than single models, ii) calibration set reweighing rather than operating
481 on a sliding window and iii) explicit drift detection rather than continuous model adaptation are
482 basically negligible considering the RMSE only (i.e. 2.1 vs. 2.08). However, from a practical point
483 of view these extensions are able to massively reduce operational cost considering that AL might
484 request a reference measurement at any time keeping operators basically locked at the process line
485 when no implicit drift detection system is in place. On the other hand, in contrast to SW-PLS, the
486 proposed method does not discard calibration samples, which over the long term reduces the bur-

Table 4: Cost-benefit tradeoff for different modelling and model adaptation variants. The proposed methods are highlighted in bold font.

Method/Criterion	RMSE local/global	Additional Parameters	# Reference Measurements
Static ePLS	2.75/3.29	None	None
SW-PLS [40]	-/2.49	Window Size	≈ 12%
SW-PLS + AL [40]	-/2.1	Window Size	≈ 12%
ePLS + AL	1.84/2.08	None	8 – 10% after drift
FLEXFIS-PLS (unsuperv.)	2.09/2.37	None	None

den of reference analyses especially in case that input-output relationships are subject to frequent, short-term alterations. Finally, unsupervised model adaptation using FLEXFIS-PLS could improve accuracy slightly when compared to static ePLS over all scenarios. However, unsupervised adaptation makes sense only if the drifted state is still represented well enough by the original latent variables, which is clearly not the case for scenario 1.

6. Conclusion

Calibration model maintenance remains a hot, yet in our opinion undervalued, issue in chemometrics and process analytical technology and currently involves large manual efforts and expert knowledge. Robust detection of the time-point when either the process itself or the process monitoring system fails is the first critical step towards autonomous, fully integrated maintenance of process reliability. Along these lines we here found that the Page-Hinkley statistic is a useful, general purpose quantity for tracking model diagnostic measures over time. In order to increase usability and flexibility of the PH test we introduced the concept of adaptive control limits, which circumvents using predefined thresholds (that need to be set according to application and quality measure). Committee disagreement significantly outperformed SoA indicators in terms of detection capability, delay of detection and false alarms indicating that the model diagnostic tool set should be extended by measures taking into account not only the "outlyingness" of test samples but

504 also the inference process. Once detected, drifts have to be compensated in a principled way with
505 an emphasis on cost efficiency. Active learning in combination with automated model adaptation
506 could meet these requirements while being remarkably robust against transient drift effects (out-
507 liers). Finally, the combination between fuzzy models and PLS is appealing since it allows both,
508 fully unsupervised model adaptation and modelling non-linearity in the learning/mapping prob-
509 lem. Future work should focus on further integrating the here presented concepts. For instance,
510 combining active learning with unsupervised model adaptation (i.e. semi-supervised adaptation)
511 on the one hand and using the PH statistic to determine the time point when model adaptation can
512 be safely shut down.

513 **Acknowledgements**

514 Financial support was provided by the Austrian research funding association (FFG) under the
515 scope of the COMET program within the research project "Industrial Methods for Process Ana-
516 lytical Chemistry - From Measurement Technologies to Information Systems (imPACts)" (contract
517 #843546) and by the strategic economic- and research program "Innovative Upper Austria 2020"
518 of the province of Upper Austria. The third author was supported by the Basque Government
519 through the BERC 2014-2017 program, and by the Spanish Ministry of Economy and Compet-
520 itiveness MINECO through BCAM Severo Ochoa excellence accreditation SEV-2013-0323 and
521 through project TIN2017-82626-R. This publication reflects only the authors' views.

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