Application of the THM to the investigation of reactions induced by unstable nuclei: the 18 F(p, α) 15 O case

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Abstract. The Trojan Horse Method is applied to the investigation of the 18 F(p, α) 15 O reaction, by extracting the quasi free contribution to the 2 H(18 F, α 15 O)n process. For the first time the method is applied to a reaction of astrophysical importance involving a radioactive nucleus. After investigating the reaction mechanism populating the α + 15 O + n exit channel, we could extract the 18 F(p, α) 15 O cross section and calculate the astrophysical factor over the 0 – 1 MeV energy interval. The possibility of exploring the cross section with no need of extrapolation allowed us to to point out the possible occurrence of a 7/2+ state at 126 keV, which would strongly influence the trend of the astrophysical factor at the energies of astrophysical interest. However, the low energy resolution prevents us to draw definite conclusions. Possible astrophysical consequences are also discussed, motivating further work on this reaction.

1 ¹⁸F in astrophysics

Classical novae are among the most energetic thermonuclear explosions in the Cosmos, releasing about 10^{44} erg. They occur in a binary system made up of a white dwarf and a less evolved companion. If matter is transferred from the less evolved star to the compact companion, it accumulates under degenerate conditions until the thermonuclear runaway is ignited. In the envelope temperatures in excess of 10^8 K are reached and nuclei undergo a sequence of proton captures producing β -unstable nuclei. Moreover, during these events about $10^{-3}-10^{-7}$ M_{\odot} are ejected into the interstellar medium, enriched in CNO and intermediatemass elements such as Ne, Na, Mg, Al (see [1–4] for recent reviews on classical novae).

The production of β -unstable nuclei suggests the possibility to observe both γ -ray emission due to the disintegration of short-lived radioactive species such as 13 N and 18 F and a late emission, due to medium-lived unstable nuclei such as 7 Be and 22 Na, determining the production of definite γ -lines from the de-excitation of excited states of their daughter nuclei. However, while classical novae have been observed in all wavelengths, from radio-waves to γ -rays with energies in excess of 100 MeV, they have been quite elusive in the $\sim 0.1-10$ MeV range, where the contribution of γ -rays from radioactive nuclei is expected.

In detail, the γ -ray spectrum should be dominated by an emission at energies ≤ 511 keV, originated by the an-

nihilation of positrons from 13 N and 18 F β^+ decay. The major contribution is predicted to come from 18 F, owing to its lifetime $T_{1/2} \sim 110$ s. This would allows 18 F to survive until the outer layers of the nova becomes transparent to γ -rays [3]. For this reason, the detection of the γ -lines from 18 F would help constraining models. However, only upper limits on the 18 F annihilation line have been set to date, leading to the establishment of a detectability distance, namely, the maximum distance of a classical nova for which the γ -line from 18 F can be observed. At present, the most stringent detectability distance of the 511 keV line has been set by the SPI spectrometer on board the space-borne γ -ray observatory INTEGRAL, \sim 3 kpc [5, 6].

Such constraint is strongly dependent on the predicted ¹⁸F abundances produced during novae outbursts. In turn, accurate modeling of the elemental yields are critically dependent on the cross sections of the production and destruction nuclear reactions entering ¹⁸F nucleosynthesis.

2 Present status of the 18 F(p, α) 15 O cross section measurements

Production of ¹⁸F in classical novae starts with the ¹⁶O(p, γ)¹⁷F reaction. Then, ¹⁸F is either produced by proton capture on ¹⁷F, through the ¹⁸Ne(β ⁺)¹⁸F chain, or following ¹⁷F β ⁺ decay by proton capture on the daughter ¹⁷O nucleus. Since the ¹⁸F half-life is quite large in comparison with the outburst timescale, it is primarily destroyed

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through proton-captures, the $^{18}F(p,\gamma)^{19}Ne$ and, chiefly, the $^{18}F(p,\alpha)^{15}O$ reaction, ~ 1000 times more efficient than the former [4]. However, the $^{18}F(p,\alpha)^{15}O$ reaction is the most uncertain process in ^{18}F production (and destruction) network, even if many direct and indirect measurements as well as theoretical studies (see, e.g. Ref.[7]) have focused on its investigation at astrophysical energies.

Direct measurements are very challenging because of the energy range of interest, below about 400 keV, where cross sections are vanishingly small, and because of the need of a radioactive beam, whose produced intensities seldom exceed 10⁶ ions per second. Direct measurements include the results of Ref.[8-13], focusing on the exploration of a broad 3/2⁺ resonance at about 700 keV in the center-of-mass system. A few measurements could reach astrophysical energies, measuring few points around 300 keV, where an additional resonance ($J^{\pi} = 3/2^{-}$) was observed [14, 15]. However, owing to poor energy resolution and large uncertainties, such measurements, though extremely complicated, could not set strong constraint on the trend of the cross section or, equivalently, of the astrophysical factor. The trend of the cross section is indeed very important to calculate the reaction rate, that is the input parameter of astrophysical calculations. Therefore, R-matrix was often used to extrapolate and interpolate the trend of the astrophysical factor; however, the occurrence of interfering resonances made it impossible to establish the behaviour of the astrophysical factor with the accuracy requested by astrophysical models.

With this respect, indirect techniques proved to be very helpful in the search of resonances at astrophysical energies, by performing the spectroscopy of ¹⁹Ne intermediate compound system or of its mirror nucleus ¹⁹F. Among others, the (d, p) reaction on ¹⁸F and the ¹⁵N – α elastic scattering were used to explore the ¹⁹F spectrum at energies corresponding to those of astrophysical interest (see [16] and [17], respectively). Similarly, p inelastic scattering off ¹⁹Ne was used to perform its spectroscopy [18], as well as the (d, n) transfer reaction on ¹⁸F [19] and the (p,d) neutron pickup on ²⁰Ne [20, 21]. These studies and charge symmetry considerations show that low-energy swave resonances are extremely influential, in particular the 3/2⁺ levels observed and/or predicted above and below the proton emission threshold (about 6.410 MeV) in ¹⁹Ne. This is due to the occurrence of a strong 3/2⁺ resonance at $E_{c.m.} = 665 \text{ keV}$ in the $^{18}\text{F}(p,\alpha)^{15}\text{O}$ astrophysical factor, possibly interfering with lower-lying 3/2⁺ state. The consequent interference pattern would strongly influence the trend of the astrophysical factor well within the energy window of astrophysical importance. Since this is presently the largest source of uncertainty affecting the $^{18}F(p,\alpha)^{15}O$ astrophysical factor, recently the 19 F(3 He, $t\gamma$) 19 Ne and the 19 F(3 He, t) 19 Ne reactions were studied aiming at determining the energies and proton widths of the predicted $3/2^{+19}$ Ne states (see [22] and [23], respectively).

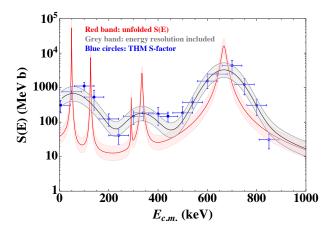


Figure 1. R-matrix analysis of the THM astrophysical factor (blu points), under the assumption of $J^{\pi} = 3/2^+$ for the 6460 keV ¹⁹Ne state as discussed in [25, 26]. The black line is the smoothed R-matrix calculation, accounting for a 53 keV energy spread (standard deviation), with parameters given in table 1. The red line is the corresponding deconvoluted astrophysical factor. The grey and the red bands show the uncertainty on the R-matrix analysis (standard deviation) due to the experimental errors affecting the THM S-factor.

3 Indirect measurement of the 18 F(p, α) 15 O cross section using the THM

Because of the ambiguities in the trend of the ${}^{18}F(p,\alpha){}^{15}O$ astrophysical factor at ultra-low energies, we decided the apply the Trojan Horse Method (THM) to its determination. Indeed, THM is an alternative and valuable approach to obtain the bare-nucleus cross section of a reaction induced by charged particles at energies lower than the Coulomb barrier, thanks to the use of suitable reactions with three particles in the exit channel. A recent review of the method is given in Ref.[24]. Here we recall that THM is based on the selection of the quasi-free reaction mechanism, namely, we single out the condition under which a cluster system (for instance, a deuteron), usually referred to as Trojan Horse nucleus, is used to transfer a participant cluster while the remaining cluster is emitted without influencing the participant-projectile interaction. In the case of the 18 F(p, α) 15 O reaction, we studied the 2 H(18 F, α 15 O)nthree-body reaction, the neutron being the spectator to the nuclear reaction of astrophysical interest. Since the energy of the incident ¹⁸F is chosen large enough to overcome the Coulomb barrier of the ¹⁸F-d interaction, the deuteron breakup takes place inside the nuclear field, so that Coulomb repulsion is greatly suppressed. Such energies, of the order of several AMeV, are usually much larger than those corresponding to the atomic degrees of freedom, so electron screening effects are also negligible. On the other hand, both the energy spent to break the Trojan Horse nucleus and intercluster motion make it possible to span the astrophysical energy region with a single beam

Two experiments were carried out, one at CNS-RIKEN (see [25] for more details) and one at the Texas A&M University [26]. Results are in agreement with each

other within uncertainties and their weighed average is shown as blue circles in figure 1. In the figure, vertical error bars account for statistical and normalization errors, while the horizontal error bar indicates the calculated energy resolution, strictly linked to the bin width used in the data analysis. More details can be found in the original works [25, 26]. We then performed an R-matrix analysis of the THM data, starting from the work [20] and modifying the parameters in order to best reproduce the THM S-factor. The adopted procedure is discussed at length in [27]. Here we remind that the best fit curve (shown as a black line in figure 1) is achieved by assuming the (++)(++) interference pattern, following to the notation in Fig. 3 of [20], excluding the 7 keV resonance corresponding to the 6.417 MeV state in ¹⁹Ne (see table 1) and inserting a 7/2+ state of ¹⁹Ne at 6.537 MeV, whose occurrence was already pointed out in [25, 26]. Also, to compare the calculated astrophysical factor with the experimental THM one, the effect of the energy resolution is taken into account, by smearing the theoretical curve to match the 53 keV (standard deviation) calculated energy resolution. A very good agreement is found between the fitted curve and the THM S-factor, as for 18 degrees of freedom, a reduced $\chi^2 = 1.5$ is obtained. The R-matrix astrophysical factor, devoid of effects due to energy resolution, is shown as a red line in figure 1. Finally grey and red bands are used to highlight the uncertainty affecting the R-matrix calculation, for the smeared and unfolded astrophysical factors respectively, taking into account the experimental uncertainties affecting THM data. Table 1 contains the resonance parameters leading to the best fit of the THM data.

To test the effect of the inclusion of the 6417 keV state, R-matrix calculations comprising and excluding such state were implemented. Inserting such a state with the resonance parameters of the literature [20] leads to a reduced $\chi^2 = 3.1$ for 18 degrees of freedom after smearing, two times larger than the calculation completed without its inclusion. This suggests that THM data tend to exclude it from the astrophysical factor. The reason of the increase of the reduced χ^2 is also apparent from the inspection of figure 1. The inclusion of the 6417 keV state would cause an increase of the R-matrix S-factor by a factor of more than 3 at 5 keV (from about 300 MeVb up to about 1000 MeVb), leading to a discrepancy of 5.5σ with respect to the THM astrophysical factor at the same energy. However, more work is necessary to definitely exclude such contribution as our conclusions are presently based on a single point. Yet, it is worth nothing that the THM result agrees with the lack of observation of the mirror state in the $^{15}N(\alpha, \alpha)^{15}N$ cross section [28].

The second important feature is the occurrence of the 6537 keV state reported in [25, 26]. This level, corresponding to a 126 keV resonance, was not included in the R-matrix calculation by [20]. However, its omission in the present R-matrix calculation would determine an increase in the reduced χ^2 to 1.8. Owing to the THM data energy resolution, the deviation of the calculated S-factor not including the 126 keV resonance from the experimental THM one is well below 5σ , so a new measurement

Table 1. Parameters of the R-matrix calculation (red line) in figure 1. Resonance energies, corresponding levels in ¹⁹Ne, spin-parities, Γ_p and Γ_α are reported, respectively. For the sub threshold state, the ANC is given instead of Γ_p . A complete discussion on the parameters can be found in [27] and in [20] and references therein.

E_{res} (keV)	E_x (keV)	\mathbf{J}^{π}	Γ_p (keV)	Γ_{α} (keV)
-124	6286	1/2+	$83.5 \text{ fm}^{-1/2}$	11.6
7	6417	$3/2^{-}$	$1.6 \ 10^{-41}$	0.5
29	6440	$1/2^{-}$	$3.8 \ 10^{-19}$	220
49	6460	$3/2^{+}$	$2.3 \ 10^{-13}$	0.9
126	6537	$7/2^{+}$	$7.1 \ 10^{-8}$	1.5
291	6702	$5/2^{+}$	$2.4 \ 10^{-5}$	1.2
334	6745	$3/2^{-}$	$2.2 \ 10^{-3}$	5.2
665	7075	$3/2^{+}$	15.2	23.8
1461	7872	1/2+	55	347

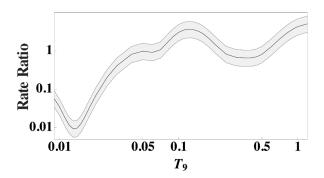


Figure 2. Ratio of the 18 F(p, α) 15 O reaction rate calculated using the deconvoluted THM S-factor (red band of figure 1) to the one reported in the JINA REACLIB database [30]. Uncertainties of the reaction rate are represented as a grey band.

with improved energy resolution is necessary to clarify its occurrence. This is a very important point since this resonance occurs at astrophysical energies, right in the position where the largest influence from interference between s-wave resonances is expected. Therefore, the presence of the 6537 keV is of significant astrophysical relevance, calling for further indirect high-resolution studies of the $^{18}\text{F}(\text{p},\alpha)^{15}\text{O}$ reaction using the THM. A more extended discussion on the R-matrix analysis can be found in [27].

4 Astrophysical consequences

Using standard equations (see, for instance, [29]), the reaction rate for the 18 F(p, α) 15 O reaction was calculated using

the best-fit R-matrix astrophysical factor, devoid of energy resolution effects (the red band in figure 1). The resulting reaction rate was then divided by the one listed in the JINA REACLIB database [30], for ease of comparison. In fact, as it is shown in [27], the reaction rate is exponentially decreasing with decreasing temperature. The ratio of the THM reaction rate to the REACLIB one is shown in figure 2 as a black line. The REACLIB rate is used for comparison since it is routinely used in novae modeling. The shaded area displays the uncertainty interval corresponding to the red band in figure 1. Temperature on the horizontal axis is given in units of 10⁹ K, namely $T_9 = T/10^9$ K. For $0.1 \lesssim T_9 \lesssim 0.5$, typical temperatures of novae nucleosynthesis, the THM reaction rate is about a factor of 2 on the average larger than the one in the REACLIB database [30], in agreement with the results by [20]. The effect of the missing 7 keV resonance causes a decrease of the reaction rate ratio below about $T_9 \sim 0.1$, outside the temperature range of astrophysical energies.

The THM reaction rate was then implemented into one-dimensional, hydrodynamic simulations of novae thermonuclear runaways using the SHIVA code [4, 31]. In particular, we tested the influence of the reaction rate for two models of 1.25 M_☉ oxygen-neon white dwarfs, accreting H-rich material from the stellar companion at a rate of $2 \times 10^{-10} \text{ M}_{\odot} \text{ yr}^{-1}$. By changing the $^{18}\text{F}(p,\alpha)^{15}\text{O}$ reaction rate only, using in one case the THM one and in the other the one listed in REACLIB, we found no change in the dynamical properties of the explosion. Conversely, important differences in the chemical composition of the ejected matter was found, revealing a decrease of the ¹⁸F supply for the THM case by a factor of ~ 2 . This would imply a reduction of the detectability distance of the 511 keV annihilation line by γ -ray satellites by a factor $\sim \sqrt{2}$. This may help explaining the present lack of observations of this γ -ray line.

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