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Truncation Artifact Correction for Micro-CT Scanners

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Truncation Artifact Correction for Micro-CT Scanners

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Abstract

The work included in this project is framed on one of the lines of research carried out at the Laboratorio de Imagen Médica de la Unidad de Medicina y Cirugía Experimental (UMCE) of Hospital General Universitario Gregorio Marañón and the Bioengineering and Aerospace Department of Universidad Carlos III de Madrid. Its goal is to design, develop and evaluate new data acquisition systems, processing and reconstruction of multimodal images for application in preclinical research. Inside this research line, an x-ray computed tomography (micro-CT add on) system of high resolution has been designed for small animal. Nowadays, computed tomography (CT) is one of the techniques most widely used to obtain anatomical information from living subjects. Different artifacts from different nature usually degrade the qualitative and quantitative analysis of these images. This creates the urgent need of developing algorithms to compensate and/or reduce these artifacts.

The general objective of the present thesis is to implement a method for compensating truncation artifact in the micro-CT add-on scanner for small animal developed at Hospital Universitario Gregorio Marañón. This artifact appears due to the acquisition of incomplete x-ray projections when part of the sample, especially obese rats, lies outside the field of view. As a result of these data inconsistencies, bright shading artifacts and quantification errors in the images may appear after the reconstruction process.

First of all, truncation artifact in the high resolution micro-CT add-on scanner was studied. Then, after a review of the proposed methods in the literature, the optimal approach for the micro-CT add-on was selected, based on a sinogram extrapolation technique developed by Ohnesorge et al [1]. This method consists on a symmetric mirroring extrapolation of the truncated projections that guarantees continuity at the truncation point. It includes a sine shaping effect that ensures a smooth attenuation signal drop. Truncation artifact correction method has been validated in simulated and real studies. Results show an overall significant reduction of truncation artifact. This algorithm has been adapted and implemented in the reconstruction interface of the preclinical high-resolution micro-CT scanner, which is manufactured by SEDECAL S.L. and commercialized worldwide.

Key words:

X-ray, CT, micro-CT, artifact, truncation

Resumen

El trabajo de este proyecto se encuadra dentro de una línea de investigación que se desarrolla en el Laboratorio de Imagen Médica de la Unidad de Medicina y Cirugía Experimental (UMCE) del Hospital General Universitario Gregorio Marañón y el Departamento de Bioingeniería e Ingeniería Aeroespacial de la Universidad Carlos III de Madrid. Su objetivo es diseñar, desarrollar y evaluar nuevos sistemas de adquisición de datos, procesamiento y reconstrucción de imágenes multi-modales para aplicaciones en investigación preclínica. Dentro de esta línea de investigación se ha desarrollado un tomógrafo de rayos X de alta resolución para pequeños animales (micro-TAC add-on). Actualmente, la tomografía axial computarizada es una de las técnicas más ampliamente utilizadas para la obtención de información anatómica *in vivo*. Existe una serie de artefactos de distinta naturaleza en este tipo de imágenes que generalmente degradan y dificultan el análisis cualitativo y cuantitativo de las imágenes, dando lugar a una necesidad imperante de desarrollar algoritmos de corrección y/o reducción de estos artefactos.

El objetivo general del presente proyecto es la implementación de un algoritmo para la corrección del artefacto de truncamiento en el escáner micro-TAC add-on desarrollado en el Hospital Universitario Gregorio Marañón. Este artefacto aparece debido a la adquisición de proyecciones incompletas cuando parte de la muestra, especialmente ratas obesas, se extiende fuera del campo de visión. Estas inconsistencias en los datos obtenidos pueden dar lugar a la aparición de bandas brillantes y errores en la cuantificación de las imágenes después del proceso de reconstrucción.

En primer lugar, se ha estudiado el artefacto de truncamiento en el escáner micro-TAC add-on de alta resolución. Seguidamente, se ha llevado a cabo una revisión de los métodos propuestos en la bibliografía, seleccionando una estrategia óptima para el micro-TAC add-on bajo estudio: una técnica de extrapolación del sinograma publicado por Ohnesorge et al [1]. Este método consiste en una extrapolación de espejo simétrico de las proyecciones truncadas que garantiza la continuidad en el punto de truncamiento. Incluye el modelado de una senoide que asegura una caída de señal en los valores de atenuación suave. Este método ha sido validado en estudios simulados y reales. Los resultados muestran una clara reducción del artefacto de truncamiento. El resultado de este proyecto ha sido incorporado en la interfaz de reconstrucción del escáner pre-clínico micro-TAC add-on de alta resolución fabricado por SEDECAL S.A. y comercializado por todo el mundo.

Palabras clave:

Rayos x, TAC, micro-TAC, artefacto, truncamiento



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Content

1. Introduction to Medical Imaging	1
1. 1. Fundamentals of X-ray Imaging	2
1. 2. Image Reconstruction	5
1. 3. Artifacts in CT	8
2. Motivation, Context and Objectives	17
2. 1. Context.....	18
2. 2. Objectives and Key Milestones	25
2. 3. Outline of the Document	25
3. Study of Truncation Artifact	27
4. Correction of Truncation Artifact	31
4. 1. Bibliography Review of Truncation Correction Methods.....	31
4. 2. Selected Correction Method	33
5. Results	45
5. 1. Quantitative Analysis	45
5. 2. Real Truncated Rat Acquisitions	48
5. 3. Implementation	49
6. Discussion and Conclusions	52
Annex A - FBP	55
Annex B - ACT	57
Annex C - HDR	59
Annex D - Macro	61
References	63
Glossary	65

Image Index

Figure 1 – (a) Medical imaging techniques according to their energy. Two different scales are shown, from top to bottom: according to wavelength (m) and photon energy; (b) Comparison between radiation type, its corresponding wavelength and an approximate scale of wavelength with objects (Suetens, 2008). 1

Figure 2 - Scheme representing the different components of an x-ray scanner (Jan, 2006)..... 2

Figure 3 – (left) X-ray chest projection with overlaying information; (b) vertebral column and head x-ray projection..... 2

Figure 4 – (left) Three orthogonal directions of the medical imaging of the human body; (right) A, B and C axial, sagittal and coronal views respectively of a CT study (Fuji Synapse). 3

Figure 5– (a) parallel beam geometry; (b) fan beam geometry; (c) cone beam geometry. (Hsieh, 2009) 4

Figure 6 – Basic example illustrates the concept of projection..... 5

Figure 7 – Basic example illustrates the concept of backprojection. Upper image corresponds to the original image. Image on the left is obtained by backprojecting for $\Theta=0^\circ$. Image on the right is the added sum of the backprojected images obtained for $\Theta=0^\circ$ and $\Theta=90^\circ$. Resulting image is not exactly the same as the original one. However, pixel value distribution is maintained..... 6

Figure 8 – Original image (top) consists of a single point. In the bottom part, images resulting from backprojection of 3, 6 and 360 degrees respectively are shown. In the last case, image on the right, it can be observed how the point edges are smoother than in the other ones. 6

Figure 9– Scheme of the different steps in the FBP and the filter effect..... 7

Figure 10 – (a) CT Axial section of a homogeneous cylinder without beam hardening in which the yellow line represents the profile across the red line, (b) same axial section with beam hardening, in which the cupping artifact can be observed; (c) axial section of brain CT without beam hardening, (d) same axial section of brain CT with beam hardening artifact; difference between these two images is highlight with the red arrow (Barret et al, 2004)..... 9

Figure 11 - Axial (left) and coronal (right) images showing streaking artifact due to photon starvation (Barret et al, 2004)..... 10

Figure 12 – a) Sagittal section of a chest CT showing motion artifact due to cardiac motion (Department of Radiology, Vancouver General Hospital, University of British Columbia/Canada; b) and c) Pediatric phantom, simulating a non-sedated baby. b) Shows poor image quality due to motion while in c) motion artifacts have been significantly reduced by the use of rapid scanning. (Siemens AG)..... 10

Figure 13 – CT image showing the appearance of artifact caused by metallic artifacts (Barret et al, 2004). 11

Figure 14 – Scheme showing different detector misalignments (Abella et al, 2012). 12

Figure 15 – (left) Reconstructed image without geometric misalignment; (right) reconstructed image with horizontal detector displacement (Sun et al, 2006) 12

Figure 16 – (left) Formation of ring artifact when detector is out of calibration (right) Axial section of a brain CT image. Red arrow indicates the presence of ring artifact (Barret et al, 2004). 13

Figure 17 – Different ellipse reconstructions for different values of K (number of projections) and N (number of rays in each projection): Kak, 1988..... 14

Figure 18 – CT image showing truncation artifact (bright shading) because of patient diameter (70 cm) was bigger than field of view (50 cm of diameter). 15

Figure 19 – Sagittal, coronal and axial sections (left, middle and right, respectively) of a PET/CT rat study. Red arrow points out a myocardial infarction. 17

Figure 20 – Axial view of a CT study of a rat where the arrows indicate the truncation artifact. 18

Figure 21 - (left) Argus PET/CT multimodal scanner with cover, (middle) VrPET multimodal scanner without geometric misalignment; (right) FMT-CT..... 19

Figure 22 – Illustration of the cone beam geometry formed by the x- ray source and the detector 20

Figure 23 – Scheme showing how certain thickness of different attenuation coefficients influences the x-ray beam (Hsieh, 2009)..... 21

Figure 24 – (a) Raw data; (b) Flood image without object placed in the field of view; (c) Dark image; (d) Raw data after undergoing aforementioned corrections of gain and dead pixels; (e) Attenuation image after applying the logarithm to (d)..... 22

Figure 25 – (left) Options available on MMWKS, by clicking on ACQ the window in the middle appears on the screen; (middle) Example of console acquisition interface options offered to the user, by clicking on “CT_ACQ” the window on the right appears and acquisition parameters can be selected. 23

Figure 26 – (left) Options available on MMWKS, by clicking on RECON the window in the middle appears on the screen; (middle) Example of Console Reconstruction interface options, by clicling on CT RECON the image on the right opens. With BROWSE option a certain study can be selected, in this example a rat CT, and corrections can be applied before reconstruction. 24

Figure 27 – Example of MMWKS interface showing a mouse CT after reconstruction..... 24

Figure 28 – (left) CT scheme showing an object (red cube) that lies outside the FOV; (right) A, complete projection of a mouse CT study. B, truncated projection of a rat CT study. 27

Figure 29 – (left) Complete projection of a mouse CT study, (right) complete profile along yellow line plotted in the projection on the left. 27

Figure 30 – (left) Truncated projection of a mouse CT study, (right) truncated profile along yellow line plotted in the projection on the left. 28

Figure 31 – Effect of the filtering step: (left) homogeneous frequency distribution at the edges, (right) high frequencies have been enhanced in the truncated image. 28

Figure 32 – Reconstructed CT image showing truncation artifact (bright circular shading) combined with streaking (Mawlawi et al, 2006)..... 29

Figure 33 – Illustration of projection truncation in a phantom. (a) Original projection without truncation. (b) Simulated moderate level of projection truncation. (c) Simulated severe level of projection truncation (Hsieh, 2009)..... 29

Figure 34 – Top row shows the different fields of view, second row shows the corresponding sinograms, third row shows filtered sonograms and bottom row shows FBP reconstructions. Fist column (A) corresponds to a complete FOV acquisition, second column (B) Corresponds to a limited FOV in which the sinogram outside the FOV is set to zero, resulting in bright shading artifact. Finally, third column (C) presents a limited FOV, with the sinogram outside the field of view set to the end values. In this way, discontinuities are prevented, avoiding the bright rim (Boas 2012). 31

Figure 35 – Top image shows a truncated sinogram, bottom image shows the correcting sinogram form by sine completing curves (Ohnesorge et al, 2000). 32

Figure 36 – Top image shows a truncated sinogram, bottom image shows the correcting sinogram form by sine completing curves (Chityala et al, 2005). 32

Figure 37 – Profile showing an original truncated projection profile with extension according to Next value at the sides pre-set to zero..... 33

Figure 38 – (left) “symmetric mirroring” extrapolation (back dashed line) at the left side is performed around point SA (red dashed line) and (right) symmetric mirroring extrapolation (back dashed line) at the right side is performed around point SE (red dashed line). Back dashed lines denoted by $wSAk'$ and $wSEk'$ indicate the sine shaping effect (Ohnesorge et al, 2000)..... 35

Figure 39 – Comparison of profiles without truncated correction (top), with extrapolation without sine shaping, where the effect of low Next could not be overcome (middle) and with extrapolation with sine (bottom) using the implemented code. 36

Figure 40 – (left) Extrapolated projection profile with smooth transition to zero values; (right) Effect of the filtering step showing a homogeneous distribution. 36

Figure 41– Flow chart of the simplified algorithm. Circles correspond to functions and squares to Boolean operators. 37

Figure 42 – Truncated projections of a rat CT which have been extrapolated with extensions of 20, 30 and 40 pixels at each side, from left to right, respectively. Profiles plot along the yellow lines are shown in Figure 43. 39

Figure 43 – Comparison performed in ImageJ between extrapolated profiles drawn in Figure 42 with different extension values at the sides (in pixels). From top to bottom Next=20, Next=30 and Next=40, respectively. Red and blue circles indicate the extrapolation performed at the left and right edges, respectively. 39

Figure 44 – (left) complete original projection of a cylinder phantom CT, yellow lines indicate the boundaries for truncation; (right) truncated projection after cropping the original projection 90 pixels at each side. 41

Figure 45 – Axial sections of a cylinder phantom CT (left) Original projection without truncation, the image has been manually cropped after reconstruction (90 pixels at each side); (middle) Reconstructed data without truncation correction..... 41

Figure 46 – (left) Original mouse projection data; (middle) Mouse projection data with induced truncation of 140 pixels at each side; (right) mouse projection data with induced truncation of 160 pixels at each side. It can be observe how the loss of signal with 160 pixels is much more aggressive in the protruded mass than with 140. 42

Figure 47 – Axial sections of mouse CT (left) Original projection without truncation, the image has been manually cropped after reconstruction (160 pixels at each side); (right) Reconstructed data without truncation correction..... 42

Figure 48 – Axial sections of mouse CT showing the line across which profiles have been drawn. (left) Original image; (right) Image with artifact. 43

Figure 49 – Axial sections of a rat CT extending outside the Field Of View without algorithm correction..... 43

Figure 50 – Axial sections of a cylinder phantom CT (left) Original projection without truncation, (middle) Reconstructed data without truncation correction; (right) Reconstructed data with truncation correction. 45

Figure 51 – Axial sections of mouse CT (left) Original projection without truncation, the image has been manually cropped after reconstruction (160 pixels at each side); (middle) Reconstructed data without truncation correction; (right) Reconstructed data with truncation correction. 46

Figure 52 – Axial sections of mouse CT showing the line across which profiles have been drawn. (left) Original image; (middle) Image with artifact; (right) Corrected Image. 47

Figure 53 – Comparison of profiles drawn along the yellow lines. 47

Figure 54 – Axial sections of a rat CT extending outside the Field Of View: (left) Reconstructed data without truncation correction; (right) Reconstructed data with truncation correction. 48

Figure 55 – (left) Console interface options offered to the user, by clicking on “RECON” reconstruction options appear on the screen (middle); by clicking on CT_RECON Console Reconstruction window appears, offering the user the choice to select different correction methods. Truncation option appears highlighted in a red circle. Rat Projections from two different angles are shown. 49

Figure 56 – Upper row: sagittal, coronal and axial views respectively of a truncated CT image with truncation correction. Lower row: truncated CT image without truncation correction. 50

Table Index

<i>Table 1– Available CTF files features according to binning value</i>	<i>22</i>
<i>Table 2 – Scheme showing the correspondence between binning value, projection size and Next value needed to extrapolate and correct truncated projections.</i>	<i>39</i>
<i>Table 3 – Analysis of the Region of Interest (ROI) of the cylinder Recovery of mean CT value in % has been done by comparing the corrected image with the image with artifact.</i>	<i>45</i>
<i>Table 4 – Analysis of the Regions of Interest (ROI) of mouse acquisitions. ROI 1 has an area equal to 396 pixels while ROI 2 has an area of 568 pixels. Blue numbers are key indicators of the correction algorithm performance.</i>	<i>46</i>
<i>Table 5 – Analysis of the Regions of Interest (ROI) drawn in rat acquisitions. ROI 1 has area equal to 1444 pixels while ROI 2 has an area of 1008 pixels. Red numbers are key indicators of the correction algorithm.....</i>	<i>48</i>



Introduction

1. Introduction to Medical Imaging

Medical image is the representation of the spatial distribution of one or more chemical or physical properties of the organism, which are the origin of contrast. Medical image acquisition involves the irradiation of the sample with certain energy. Depending on the type of energy involved, different acquisition techniques are classified into modalities [2]. X rays and γ rays are forms of electromagnetic radiation. The former is the incident radiation corresponding to radiography and Computed Tomography (CT) images, while the latter gives rise to nuclear imaging (Scintigraphy, Positron Emission Tomography, PET, and Single Photon Emission Computed Tomography, SPECT). In Magnetic Resonance Imaging (MRI) the incident energy are radio frequency waves. Ultrasound Imaging (US) uses mechanical energy, in form of ultrasound waves. Figure 1 shows a scheme of the different energies.

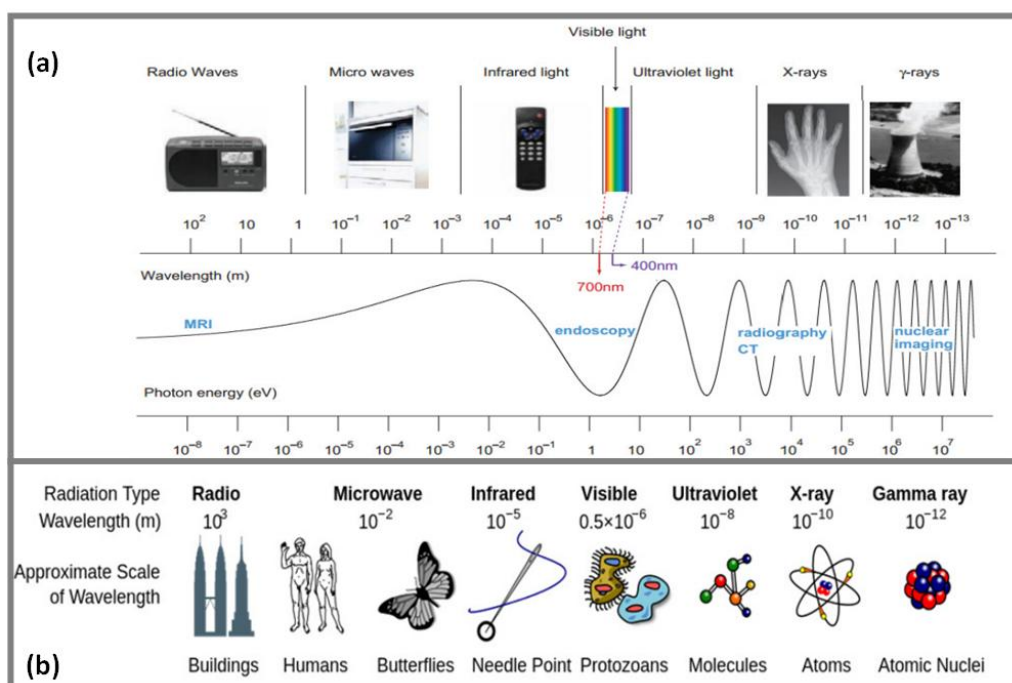


Figure 1 – (a) Medical imaging techniques according to their energy. Two different scales are shown, from top to bottom: according to wavelength (m) and photon energy; (b) Comparison between radiation type, its corresponding wavelength and an approximate scale of wavelength with objects (Suetens, 2008).

X-rays are forms of ionizing radiation. Because of its high energy they are able to eject an electron from an atom, leading to chemical reaction in an organism. High ionization dose may induce damage to the patient. Therefore, carefully planning of the radiation needed for the study is needed.

1. 1. Fundamentals of X-ray Imaging

The basic principle behind x-ray image formation in radiography (2D) is that the x-ray beam goes through the sample, suffer different attenuation according to the traversed tissues and finally reach the detector, where the information about the accumulated attenuation is recorded in a projection [3].

Figure 2 illustrates the different components of an x ray scanner. Diffuse radiation is emitted from the x-ray tube. A primary collimator focuses the beam ensuring the rays follow the desired trajectory. Pre-patient filter cancels out low radiation dose that will otherwise remain in the patient body (blue Region of Interest) without reaching the detector. As some scattered radiation (deviated rays) may occur, an anti-scatter grid is placed before the detector so as to limit the *incoming* x-ray direction. Finally, the attenuated x-ray beam lands on the detector and is recorded in a projection, as illustrated in Figure 3, [3]. From thorax image superposition of ribs, lungs and heart is quite evident.

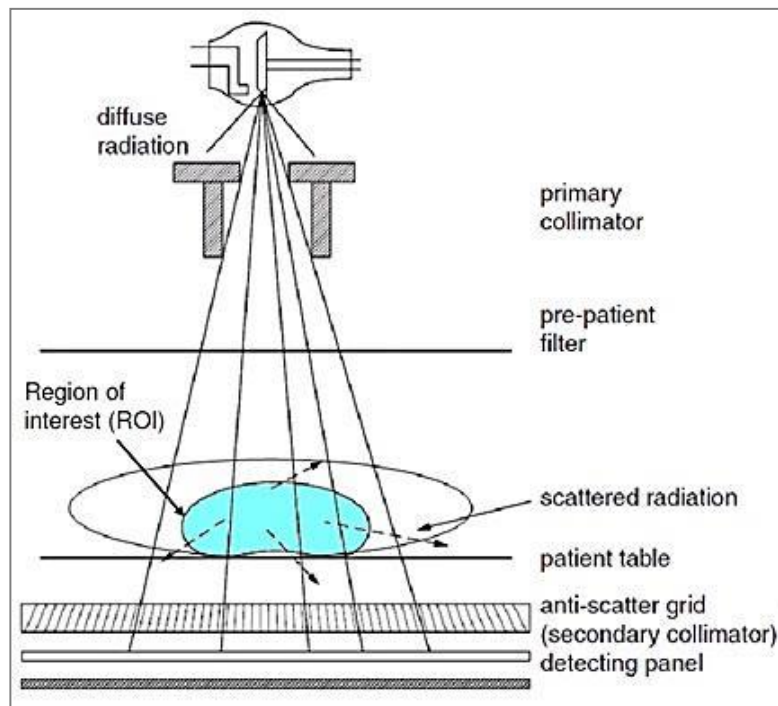


Figure 2 - Scheme representing the different components of an x-ray scanner (Jan, 2006).



Figure 3 – (left) X-ray chest projection with overlaying information; (b) vertebral column and head x-ray projection.

However, the problem with this technique is that all the anatomical information in 3D is collapsed into a projection (2D). Depth information is lost as there is no way of knowing the attenuation coefficient of a certain structure located above or below in space. It was latent the need of finding a new geometric configuration for the acquisition: rotating the source from different angles around the sample, so that information is obtained from every angle. In such a way, a 3D image (Tomography) was generated from 2D (Radiography) projection data, getting rid of overlaying object information. *Tomography* is derived from the Greek word *tomos* (to cut) and *graphos* (image).

Figure 4 shows the three orthogonal directions, in which “cuts” are performed. Different gray levels in each projection are related to the x ray attenuating properties of the tissues, which directly depend on mass density and atomic number [4]. Gray levels close to white color correspond to high density areas, that is, places where there is higher x-ray photons absorption, gray areas with soft tissues, medium density, and dark areas with the lowest possible density (air). As such, the differences in density between soft tissues are not remarkable and maximum contrast differences are achieved with bone and air [4].

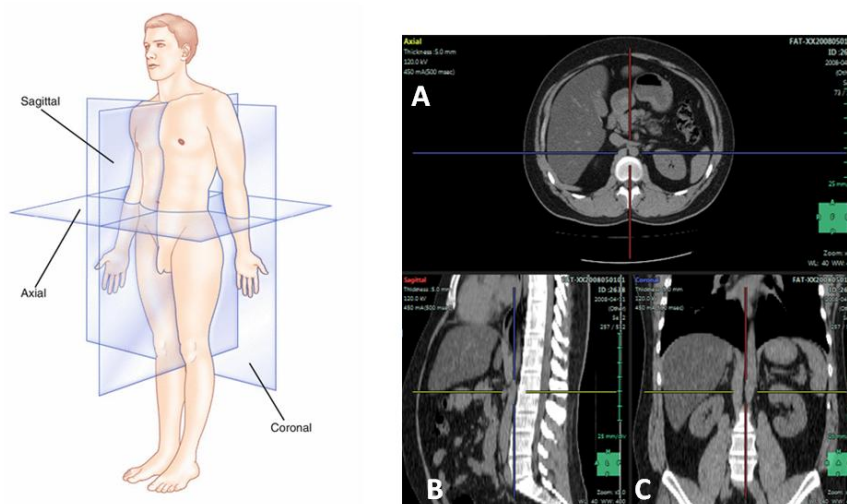


Figure 4 – (left) Three orthogonal directions of the medical imaging of the human body; (right) A, B and C axial, sagittal and coronal views respectively of a CT study (Fuji Synapse).

The mathematical foundation of computed tomography (CT) was first derived by Radon in 1917. However, it was not until the development of modern computers that the technique became at all viable. The original breakthrough was made by G. N. Hounsfield of EMI Laboratories in 1972, showing a practical method for generating cross-sectional images of the head [5]. Since then, CT has experienced tremendous growth in recent years, in terms both of basic technology and new clinical applications [4]. This technique provide with valuable 3D information for diagnosis, having both an excellent spatial resolution and, in the most recent scanners, a fast acquisition.

According to the detector shape, there are three possible configurations: parallel beam, fan beam and cone beam geometry (Figure 5, [4]). Parallel beam refers to a punctual source that moves in small increments parallel to the detector elements. In fan beam geometry the x-rays are equally spaced (landing on a detector line) or equiangular spaced (landing on a circular line detector). Finally, in cone beam geometry, the detector is flat and the x-rays describe a cone shape.

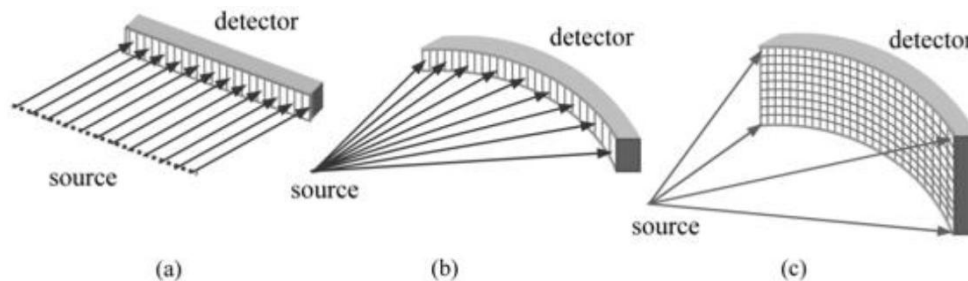


Figure 5– (a) *parallel beam geometry*; (b) *fan beam geometry*; (c) *cone beam geometry*. (Hsieh, 2009)

The most common units for CT data representation are Hounsfield Units (HU) or CT number. It consists on a re-scaling of gray values according to two known tissue values: air (-1000 HU) and water (- 1000). Soft tissues (including fat, muscle, and other body tissues) have CT numbers range from -100 HU to 60HU. Bones are more attenuated and have CT numbers from 250 HU to over 1000 HU. In such a way, impact of non-idealities of the acquisition process is reduced and small differences between tissue types are enhanced [4].

CT number or HU is defined by:

$$CT_{number} = \frac{\mu - \mu_{water}}{\mu} \cdot 1000 \quad (1)$$

1. 1. 1. Projection

Data recorded on the detector is known as *projection*. A simple example is presented here so as to illustrate the concept of projection.

Figure 6 shows how a projection is obtained, according to different attenuation coefficients (μ) in a parallel beam geometry configuration. Projection for projection angle $\Theta=0^\circ$ would be the sum of the attenuation coefficients along the different horizontal ray trajectories. Each projection recorded data represents the total attenuation traversed by an x-ray and t axis represents the distance of from the x-ray to the object center of coordinates. Information from a single projection angle is not enough to know the exact distribution of the four different attenuation values in the image. If a projection is performed at angle $\Theta=90^\circ$, additional attenuation information along the vertical axis will be obtained. For solving this simple example only two rays for two different projection angles are needed: they form a system of four equations with four unknowns. However, in a real case, number of unknowns is higher and a lot of projections (recorded data) are needed to as to accurately reconstruct an object.

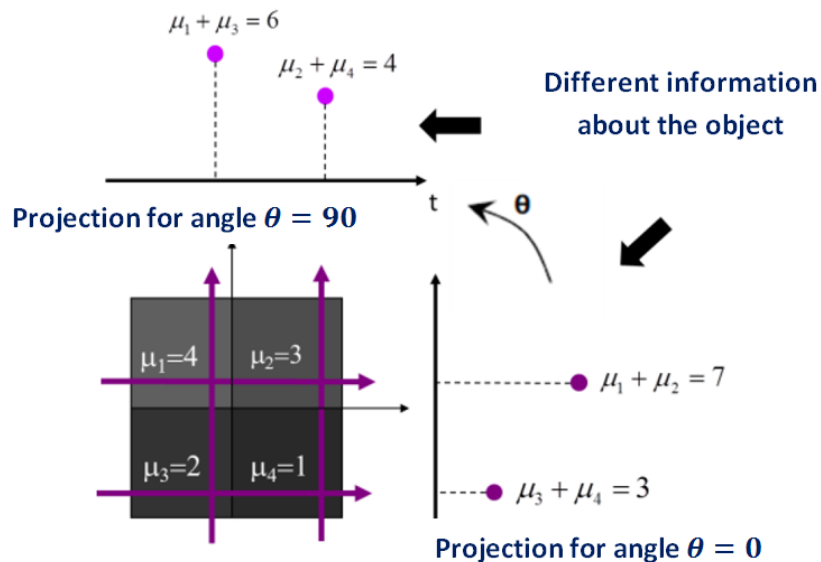


Figure 6 – Basic example illustrates the concept of projection.

1. 2. Image Reconstruction

The central idea of tomography is the reconstruction of a volume from raw projection data (line integrals) of the volume itself. There are different reconstruction methods that can be grouped into two categories, analytical or iterative, according to the mathematical base they use for going from projections to the original data set.

Analytical techniques are based on the Central Slice Theorem [6] and are divided into two categories, direct methods: Fourier based or Filtered Backprojection (FBP) based. Iterative techniques solve systems of equations until convergence to the solution and allow including more exhaustive models of the acquisition process. The reason for this is that, in contrast to analytical techniques, iterative methods are not restricted to the system geometry. FBP method is explained here, due to its relevance for the present project. A brief description of FDK reconstruction (named after Feldkamp, David and Kreis), similar to FBP, is also included.

1. 2. 1. Filtered Backprojection (FBP)

Filtered Backprojection method is based on the Central Slice Theorem [6] and it is divided into two steps: filtration and backprojection. Figure 7 clarifies the concept of backprojection, following with the example presented in Figure 6. Backprojected image for angle $\Theta=0$ degrees is obtained replicating attenuation values recorded by the horizontal rays. In the same way, backprojected image is obtained for $\Theta=90^\circ$. Final backprojected image will be the sum of backprojected images for each angle.

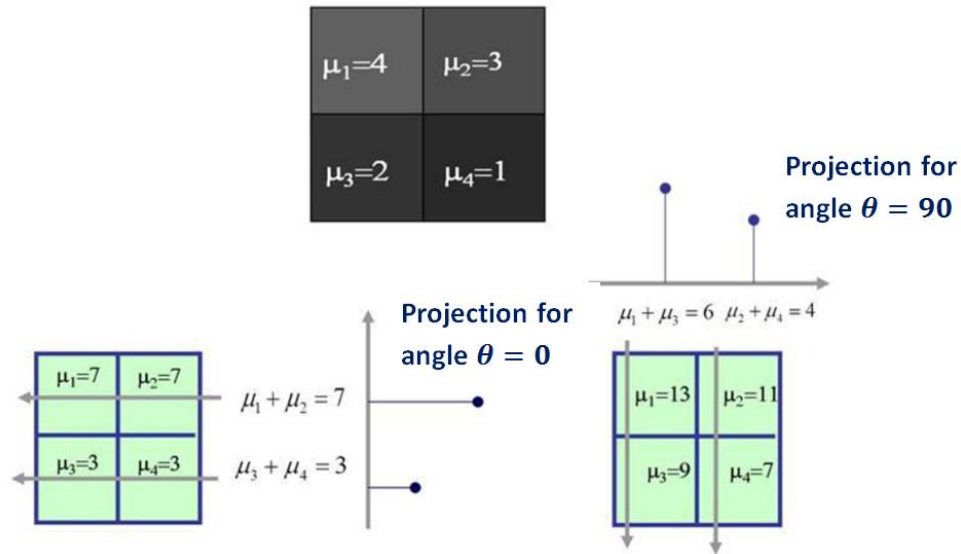


Figure 7 – Basic example illustrates the concept of backprojection. Upper image corresponds to the original image. Image on the left is obtained by backprojecting for $\theta=0^\circ$. Image on the right is the added sum of the backprojected images obtained for $\theta=0^\circ$ and $\theta=90^\circ$. Resulting image is not exactly the same as the original one. However, pixel value distribution is maintained.

As stated before, in a real case (with more pixels), more projections are needed to recover the original object. Figure 8 illustrates resulting images from different backprojection angles. They are a blurred version of the original image, due to the high low frequency component present in the backprojected image. Therefore, in order to completely recover the original image, the filtering step is needed in the reconstruction process.

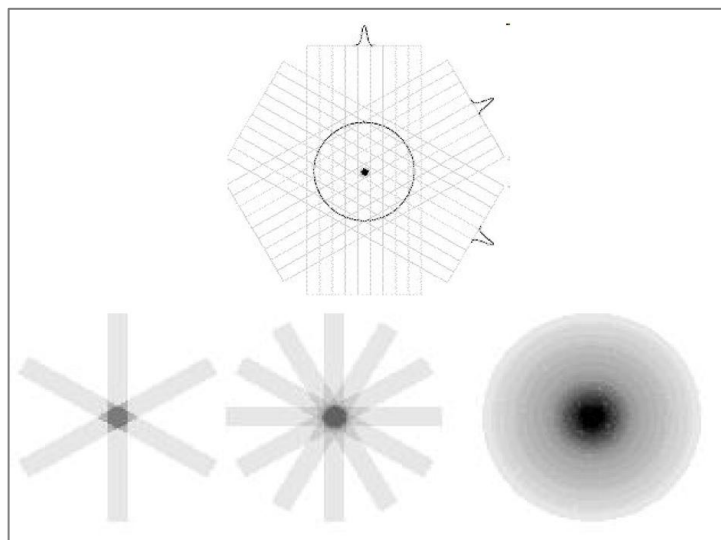


Figure 8 – Original image (top) consists of a single point. In the bottom part, images resulting from backprojection of 3, 6 and 360 degrees respectively are shown. In the last case, image on the right, it can be observed how the point edges are smoother than in the other ones.

Projections can be measured for Θ ranging from 0 to 2π . Stacking all these projections results in a 2D data set called sinogram.

Filter influence on the final image is illustrated in Figure 9. Starting from the sinogram, a direct backprojection without filtering will result on a blurred image, in which the low frequency component in the image is really high. However, if a ramp filter is applied to the initial sinogram, high frequencies are enhanced, while keeping low frequencies. This yields better reconstruction results, in which the low sampling densities in high components have been compensated.

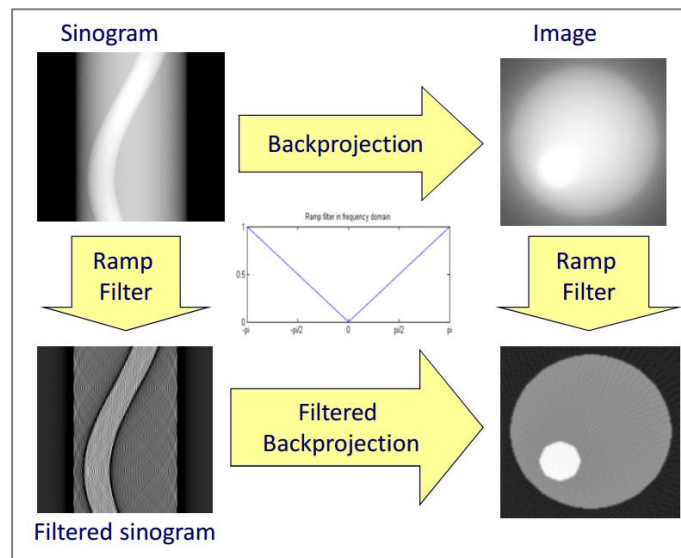


Figure 9– Scheme of the different steps in the FBP and the filter effect

Formal Definition of FBP

Given the sinogram $p(r, \theta)$, the question is how to reconstruct the distribution of attenuation coefficients $\mu(x, y)$, or generically, the function $f(x, y)$. Intuitively, one could think of the following procedure. For a particular line (r, θ) , assign the value $p(r, \theta)$ to all points (x, y) along that line. Repeat this (i.e. integrate) for θ ranging from 0 to π [2]. This procedure is defined by:

$$f(x, y) = \int_0^\pi p(x \cdot \cos\theta + y \cdot \sin\theta, \theta) d\theta \quad (2)$$

Derivation of this equation is included in Annex A.

1. 2. 2. FDK Reconstruction

FDK is a reconstruction algorithm designed for cone beam geometry scanners. It was proposed by Feldkamp, David and Kreis in 1984 [7].

In this method, reconstruction problem is studied as a FBP, but introducing a third (axial) coordinate in such a way that all rays can be considered starting from transformations in the system of reference.

Complete mathematical derivation that can be seen in [6], yields the following equation:

$$f(\mathbf{u}, \mathbf{v}, \mathbf{z}) = \frac{1}{2} \int_0^{2\pi} \frac{D_{FO}}{(D_{FO}-v)^2} \int_{-\infty}^{\infty} R_{\beta}(s, \mathbf{z}) h\left(\frac{D_{FO}}{D_{FO}-v} - s\right) \frac{D_{FO}}{\sqrt{D_{FO}^2 + z^2 + u^2}} ds d\beta \quad (3)$$

It represents the convolution of the projections R_{β} and the spatial version of the ramp filter previously mentioned for FBP. In addition, projections are weighted twice. First weighting, $\frac{D_{FO}}{\sqrt{D_{FO}^2 + z^2 + u^2}}$, appears because of the coordinate change. It compensates the oblique path rays describe in cone beam geometry. The second weighting, $\frac{D_{FO}}{(D_{FO}-v)^2}$, depends on the distance of the point to be reconstructed to the source.

In cone beam with circular trajectory, projections from every angle have information coming from different planes. In fact, only in the central slice correct data are obtained and FBP can be applied. Therefore, this is the only slice that can be reconstructed without uncertainty. Uncertainties are bigger as we go farther away from the center, which is known as cone beam artifact.

1. 3. Artifacts in CT

1.3.1. Introduction

The systematic discrepancy between real attenuation coefficients and the reconstructed values in the CT image is known as **CT artifact** and can be recognized in the reconstructed image in the form of undesirable lines, shadows, rings or other effects [4]. CT images are inherently more prone to artifacts than conventional radiographs because the image is reconstructed from approximately a million independent detector measurements [8]. Moreover, the reconstruction technique assumes the consistency of all acquired values, reflecting every acquisition error in the reconstructed image.

The sources of artifacts can be classified in four categories [8]: (1) physics-based artifacts, which result from the physical processes involved in the acquisition of CT data; (2) patient-based artifacts, which are caused by such factors as patient movement or the presence of metallic materials in or on the patient; (3) scanner- based artifacts, which result from imperfections in scanner function; and (4) artifacts produced by the image reconstruction process.

1.3.2. Physics-Based Artifacts

Beam Hardening

There are two factors that intervene in beam hardening origin: attenuation coefficients dependency on energy and the polyenergetic nature of the x-ray source beam. Beam Hardening is the process whereby the average energy of the x-ray beam increases when traversing an increasing thickness of material (the beam “hardens”), because less energy photons are preferentially absorbed (x-ray photons are attenuated more per unit thickness than higher energy photons. This is a direct consequence of the energy-dependence of attenuation coefficients, which are higher at lower energies. Because of this, x-ray travelling in different trajectories across an object, will emerge with different spectra, giving rise to data inconsistencies that result in reconstruction artifacts [9].

There are two common types of artifact can result from beam hardening effect: so-called cupping artifacts and the appearance of dark bands or streaks between dense objects of an image with heterogeneous volumes. These effects are illustrated on Figure 10, [8].

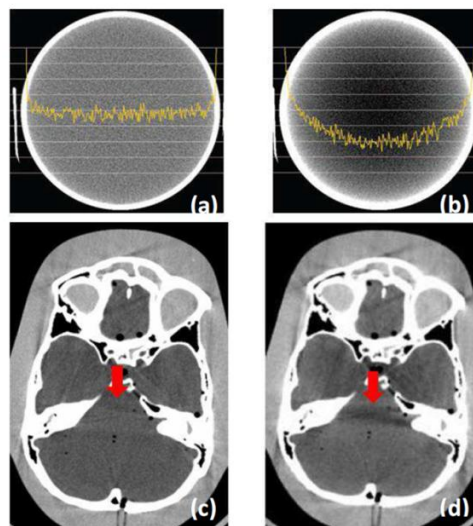


Figure 10 – (a) CT Axial section of a homogeneous cylinder without beam hardening in which the yellow line represents the profile across the red line, (b) same axial section with beam hardening, in which the cupping artifact can be observed; (c) axial section of brain CT without beam hardening, (d) same axial section of brain CT with beam hardening artifact; difference between these two images is highlight with the red arrow (Barret et al, 2004).

Photon Starvation

Photon starvation occurs when too few photons reach the detector. As a result, strong streaks appear through paths of high x-ray attenuation, where a lot of photons have been absorbed, and there is a decrease in the Signal to Noise Ratio (SNR), Figure 11. The reconstruction process has the effect of greatly magnifying the noise, resulting in horizontal streaks in the image [8]. This photon starvation artifact phenomenon occurs frequently when a pelvis or shoulder is scanned with thin slices [10].



Figure 11 - Axial (left) and coronal (right) images showing streaking artifact due to photon starvation (Barret et al, 2004).

There are two approaches aiming at reducing this artifact: Tube Current Modulation and Adaptive Filtration. The former implies the application of a higher x-ray tube current, so as to increase the probability that photons can traverse through the body and reach the detector, while the latter is based on the use of an adaptive filtration algorithm that will smooth the attenuation in the damaged areas before reconstruction.

1.3.3. Patient-based Artifacts

Patient Motion

Data inconsistencies appear when the patient moves during the scan, either voluntarily or involuntarily. The first one refers usually to respiratory motion, while the latter comprises peristalsis and cardiac motion (as can be seen in Figure 12 - left). Various methods can be used to reduce patient motion, such as instructing a patient to hold his or her breath or by means of sedation (eg, pediatric patients, Figure 12 – middle and right).

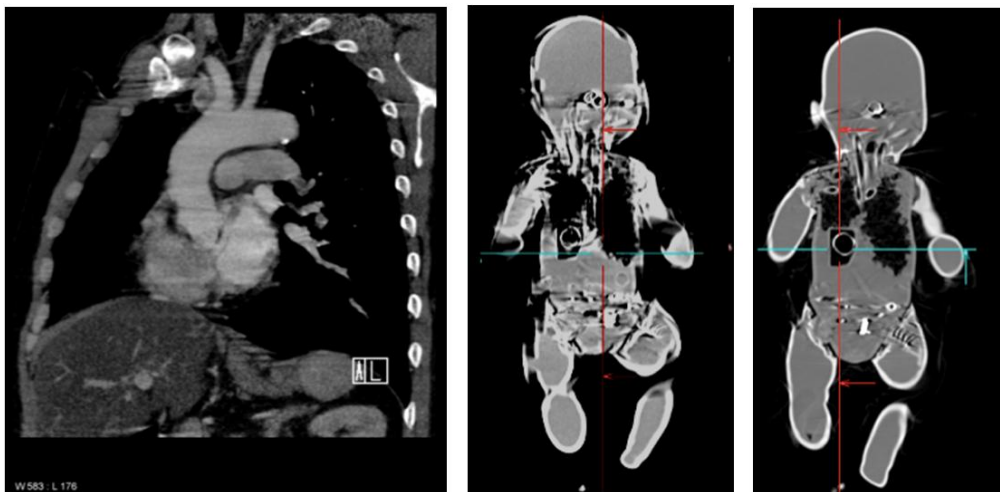


Figure 12 – a) Sagittal section of a chest CT showing motion artifact due to cardiac motion (Department of Radiology, Vancouver General Hospital, University of British Columbia/Canada; b) and c) Pediatric phantom, simulating a non-sedated baby. b) Shows poor image quality due to motion while in c) motion artifacts have been significantly reduced by the use of rapid scanning. (Siemens AG)

However, there are some preventive measures the operator can take into account to minimize this kind of artifact during the acquisition: the use of positioning aids to avoid voluntary movement or setting a scan time as short as possible to decrease discrepancies between different projections. Additionally, there are special built-in features on some scanners that use software correction by automatically applying reduced weighting to the beginning and end views, reducing their contribution to the final image [8].

Metallic Materials

Depending on the shape and density of the metal objects, such as dental prosthesis or hip implant, the appearance of this type of artifact can vary significantly (see Figure 13). They occur because the density of the metal is beyond the normal range that can be handled by the computer, resulting in incomplete attenuation profiles [8]. Nowadays there are post-processing methods for correcting the images although details in the tissue that surrounds the implant are not completely recovered [11].

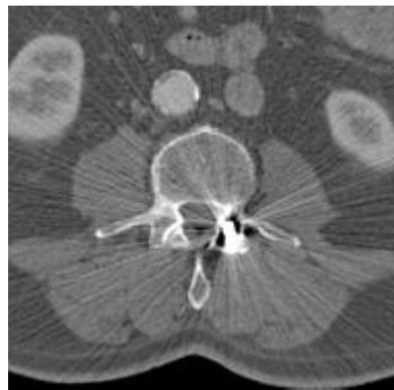


Figure 13 – CT image showing the appearance of artifact caused by metallic artifacts (Barret et al, 2004).

1.3.4. Scanner-Based Artifacts

Mechanical Artifacts

The following geometric misalignments can appear in the detector because of variations with respect to its ideal position in the scanner, giving rise to mechanical artifacts, as is shown in Figure 14, [12]: (a) Vertical and horizontal displacement of the detector; (b) rotation of the detector with respect to the z axis, parallel to detector plane columns; (c) detector tilt towards the x ray source around u axis; (d) skew of the detector in its plane, being coincident to the primary beam.

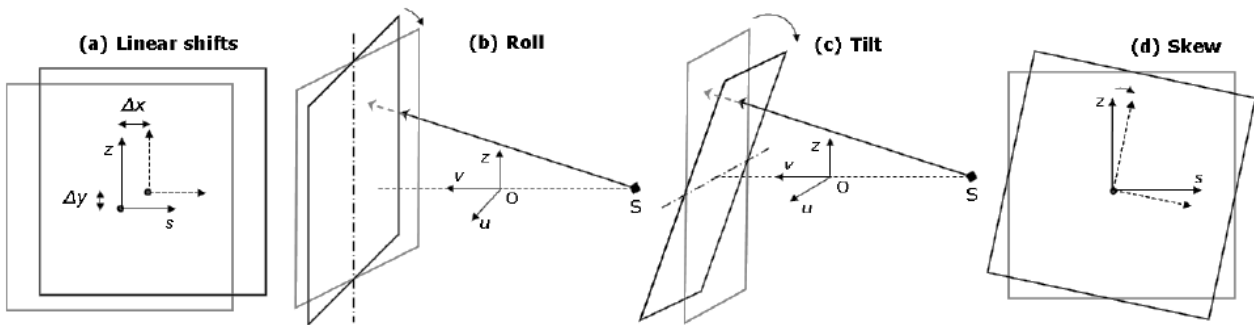


Figure 14 – Scheme showing different detector misalignments (Abella et al, 2012).

Depending on the geometric misalignment, different artifacts appear in the reconstructed image. Figure 15 illustrates the artifact formed in a CT image acquisition by a detector whose plane is horizontally shifted.

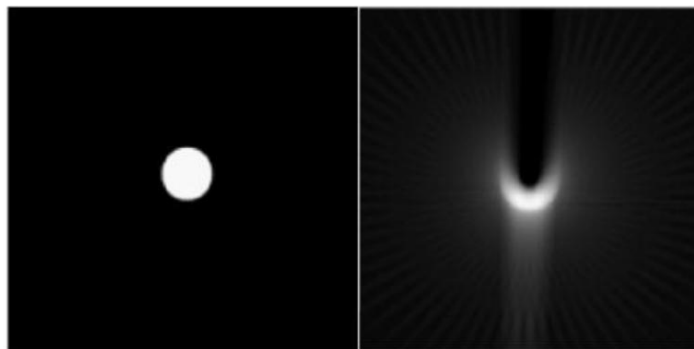


Figure 15 – (left) Reconstructed image without geometric misalignment; (right) reconstructed image with horizontal detector displacement (Sun et al, 2006).

Ring Artifacts

If one of the detectors is out of calibration on a third generation (rotating x-ray tube and detector assembly) scanner, the detector will give a consistently erroneous reading at each angular view (see Figure 16 – left, [8]), resulting in a circular artifact after reconstruction process, as can be observed in Figure 16-right, [8], [12]. This artifact can impair the diagnostic value of an image, and this is particularly likely when central detectors are affected, creating a dark smudge at the center of the image.

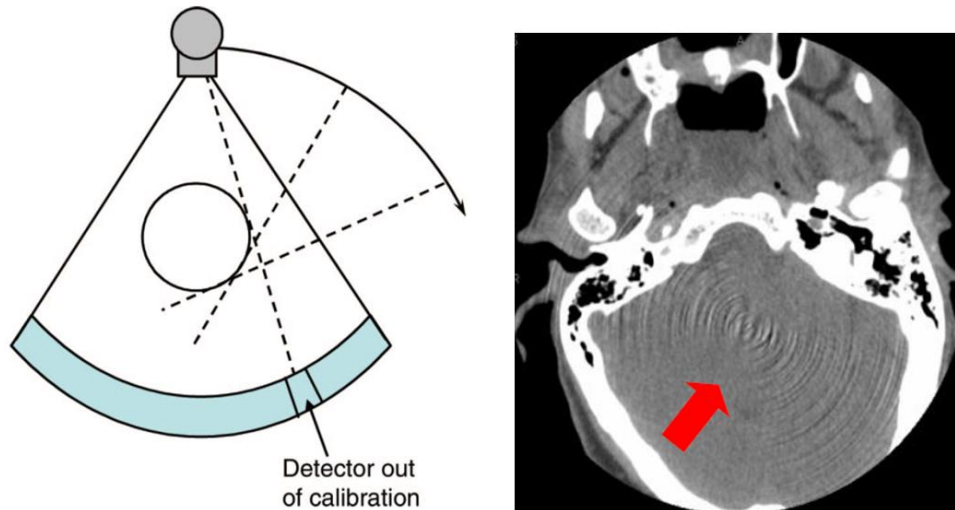


Figure 16 – (left) Formation of ring artifact when detector is out of calibration (right) Axial section of a brain CT image. Red arrow indicates the presence of ring artifact (Barret et al, 2004).

These artifacts are the result of discrepancies in the different detector gains. Corrections can be made by recalibration of detectors, repairing services or by implementing compensating algorithms that will be applied during the reconstruction of the acquired projections.

1.3.5. Reconstruction Artifacts

Number of Projections and Samples

In the data acquisition, there are two key factors that influence image reconstruction: number of samples in each projection and number of projections. A small number in any of those two parameters produces different kinds of artifacts in the image, ranging from Gibbs phenomena to streaks and bands and Moiré effect.

Aliasing artifact appears with a high number of projections (K) and a low number of samples (N). It can be prevented by increasing the number of detector samples or increasing the beam width (at the expense of spatial resolution). With a small number of views or projections, alternating dark and bright streaks will show up in the image, due to the lack of data in the angular dimension (see Figure 17, [6]).

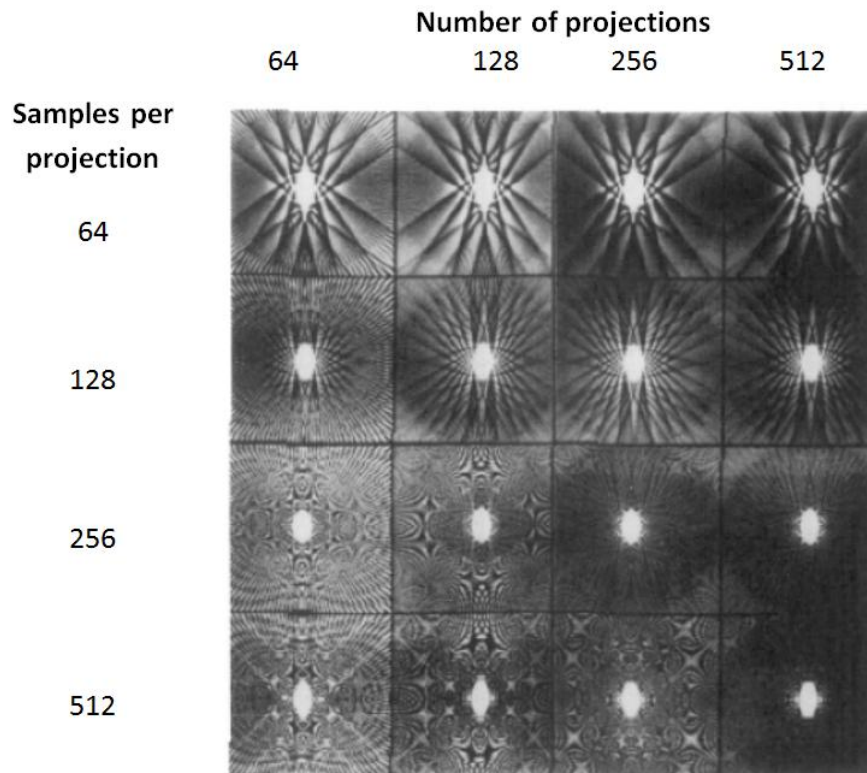


Figure 17 – Different ellipse reconstructions for different values of K (number of projections) and N (number of rays in each projection): Kak, 1988.

Projection number should be slightly higher than number of samples or number of rays in each projection (in case of parallel beam geometry) and its relation is determined by the following relationship [4]:

$$\frac{K}{N} \approx \frac{\pi}{2} \quad (4)$$

Incomplete Projections

A projection can be truncated when part of the object lies outside the scan field of view either because the object is too big to fit in size of the scan field of view (FOV) or because the patient was not centered properly. If the acquired data is reconstructed with an analytical method, such as FBP, problems arise in the filtering step. The reason for this is that 1D Fast Fourier Transform (FFT, based on the Central Slice Theorem [6]) of the projections will have components enhanced in the high frequencies due to discontinuities in the projections. As a result, the truncated reconstructed projections produce bright shading artifacts near the edge of the image (Figure 18).

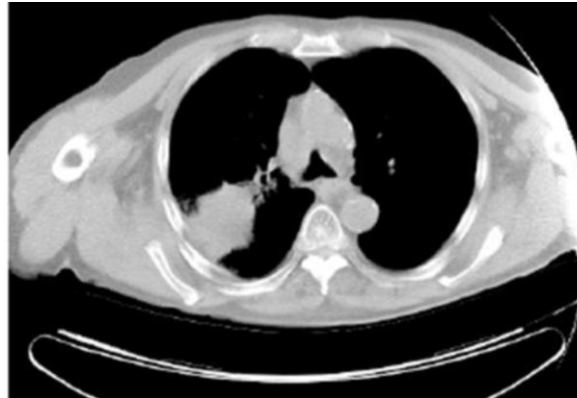


Figure 18 – CT image showing truncation artifact (bright shading) because of patient diameter (70 cm) was bigger than field of view (50 cm of diameter).

One approach to combating projection truncation is prevention by carefully center the patient in the scan FOV. However there are some cases in which this is unavoidable, especially in obese patients. Currently, different methods that try to correct the discrepancies caused by this artifacts are being implementing.

Motivation, Context and Objectives

2. Motivation, Context and Objectives

During the last decades, the numbers of animal models of human disease have largely increased. For the development of a drug or a medical procedure to treat a certain disease, there are some steps that must be followed: experimental design, in vitro testing and in vivo experimentation [13]. The last step in a drug commercialization implies the use of individuals to test the systemic effect of the drug, that is, the whole body's response to it. As the use of humans for the first testing of the medicament is not safe enough to guarantee the integrity of the patients, animals must be used until it is guaranteed that the drug is ready to be tried in humans. The main consideration to have in mind when drugs have to be tested is to have an organism as similar as possible to a human. Vertebrate animals are the best option because of their proximity in the evolutionary tree. Rats and mice are the most used animals for in vivo tests because they share most of the anatomy and its physiological functions. As both animals and humans share pathological features, the diseases that these organisms suffer are also similar.

Furthermore, use of small animals in preclinical imaging has become pivotal. Preclinical imaging for small animal refers to the in vivo visualization for research purposes. It embraces four common imaging modalities: Computed Tomography (CT), Nuclear Imaging (PET and SPECT), Magnetic Resonance Imaging (MRI) and Optical Imaging [14]. Different anatomical or functional information is obtained according to the modality selected.

Micro-CT is the most widely used anatomical imaging for small animal because of its high resolution and ease of integration in combined designs, especially in nuclear medicine scanners (PET and SPECT) [15]. This allows performing combined studies that are inherently registered (with aligned features of interest). In Figure 19 shows coronal, sagittal and axial sections of a combined PET/CT study. It can be observed how the functional image makes use of the anatomical image for having a reliable location reference.

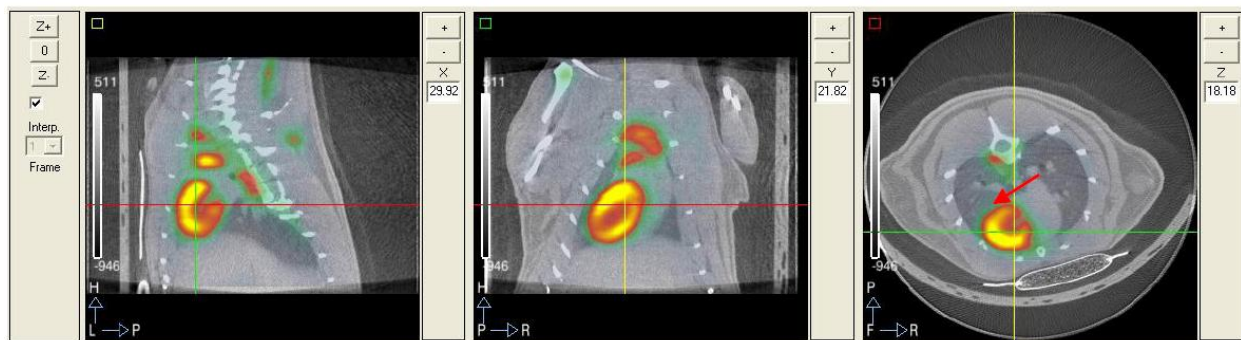


Figure 19 – Sagittal, coronal and axial sections (left, middle and right, respectively) of a PET/CT rat study. Red arrow points out a myocardial infarction.

Most of the micro-CT scanners available for small animal provide a limited field of view (FOV) required for the acquisition of certain samples. Some of the samples that are usually compromised include big rats (such as obese rats or rats in which a tumor growth has been induced) that extend outside the FOV, resulting in incomplete projections.

As a result of these data inconsistencies, bright shading artifacts may appear after the reconstruction process (see Figure 20). Therefore, truncated projections degrade the quantitative analysis of CT data. On account of this, it is necessary to correct truncation artifacts so as to obtain good image quality for diagnosis and research.

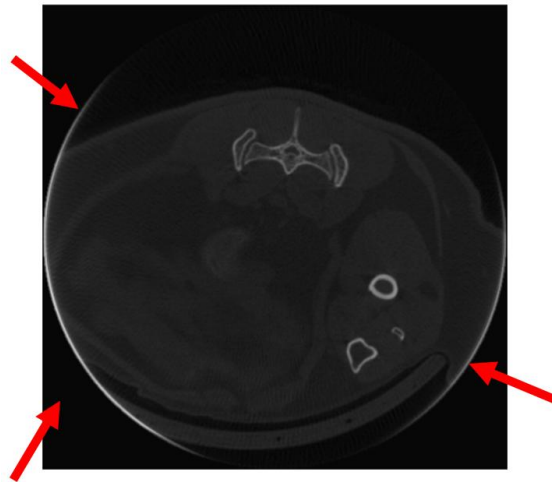


Figure 20 – Axial view of a CT study of a rat where the arrows indicate the truncation artifact.

2. 1. Context

The work of this project is framed on one of the lines of research carried out at the Laboratorio de Imagen Médica de la Unidad de Medicina y Cirugía Experimental (UMCE) of Hospital General Universitario Gregorio Marañón and the Departamento de Bioingeniería e Ingeniería Aeroespacial of Universidad Carlos III de Madrid. Its objective is to design, develop and evaluate new data acquisition systems, processing and reconstruction of multimodal images for application in preclinical research. According to this research stream, an x-ray tomography system (micro-CT add-on) of high resolution has been designed for small animal [15]. Given the aforementioned problems with limited FOV in micro-CT scanners, a correction algorithm for truncation artifact has been developed. It will be integrated into the preclinical high-resolution micro-CT add-on scanner manufactured and distributed worldwide by the Sociedad Española de Electromedicina y Calidad S.A. (SEDECAL, Madrid, Spain).

2. 1. 1. Target System

This section describes the system under study. This equipment has been designed for being integrated with nuclear imaging systems, such as PET and SPECT and optical systems by SEDECAL S.A. (see Figure 21). Therefore, this system will be referred as micro-CT *add-on*.

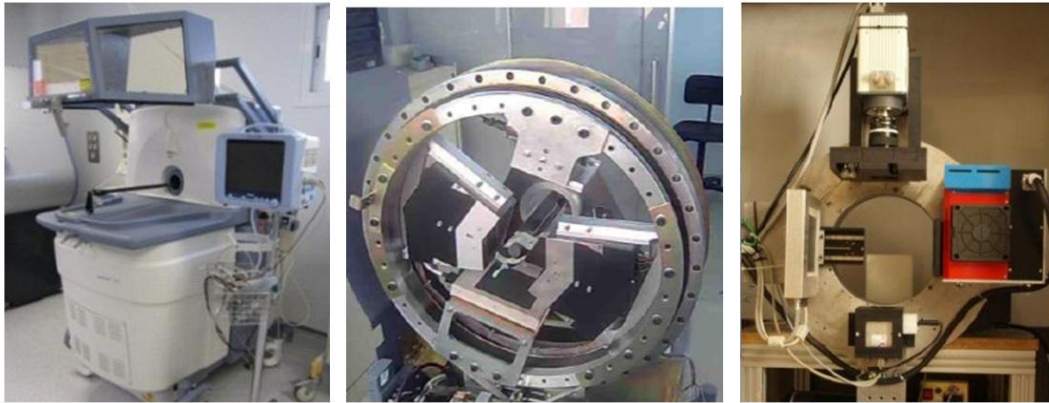


Figure 21 - (left) Argus PET/CT multimodal scanner with cover, (middle) VrPET multimodal scanner without geometric misalignment; (right) FMT-CT.

The system is composed of an x-ray tube and a detector over a rotating gantry. The bed where the sample is placed is located between them. Thanks to the movement of the rotating gantry the source and detector rotate counterclockwise around the sample so as to acquire projections from different angles. The x-ray tube (serie 5000 Apogee, Oxford Instruments) consists of a tungsten anode, a beryllium window of 126 μm and a focal spot of 46.5 μm x 49.1 μm . It works from 0 to 50 keV with maximum power of 50W according to the manufacturer specifications.

The key parameters of the system to take into consideration for the development of the project are:

- **Magnification Factor:** relationship between real object size and object size seen in the detector.

$$M = \frac{D_{SO} + D_{OD}}{D_{SO}} = 1.6 \quad (5)$$

Where D_{SO} is the distance between source and the origin of coordinates and D_{OD} is the distance between the origin of coordinates and the detector (see Figure 22 for detailed description)

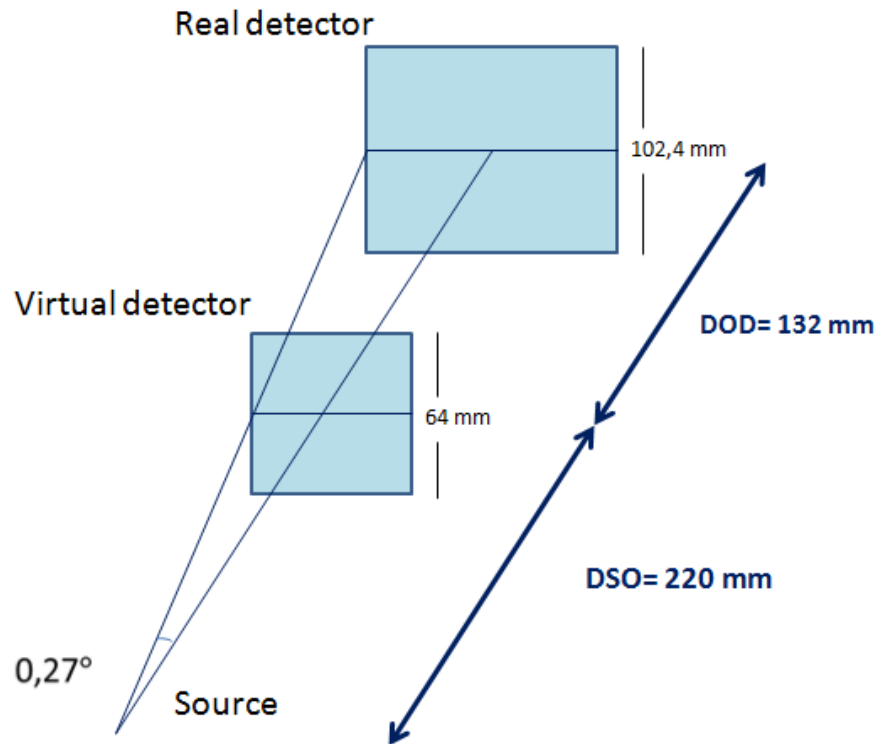


Figure 22 – Illustration of the cone beam geometry formed by the x- ray source and the detector

- **Spatial Resolution:** it depends on two different components, one due to the intrinsic resolution of the detector and another one due to x-ray source focal size. Magnification factor influences over both of them, changing their relative weighting when calculating resolution. The higher resolution that can be achieved in this micro-CT add-on is $50 \mu\text{m}$ on the detector [15].
- **Field of View (FOV):** it defines the diameter of the object volume that can be reconstructed. It will be limited by detector size and distance from the origin of coordinates to source and detector. It is calculated as follows:

$$FOV = \frac{T_d}{M} = 71,5 \text{ mm} \quad (6)$$

Where T_d refers to detector height

X-Ray Image Generation in the Detector

X-ray photons are emitted from a source, traverse the sample suffering different attenuation (as illustrated in Figure 23, [4]) and finally reach the detector, obtaining a projection.

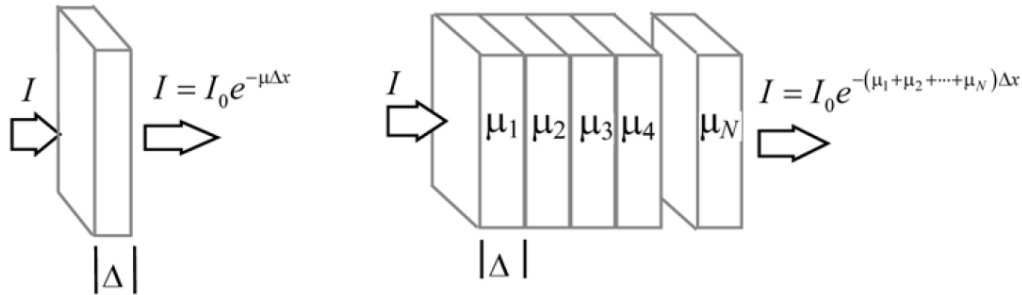


Figure 23 – Scheme showing how certain thickness of different attenuation coefficients influences the x-ray beam (Hsieh, 2009).

The number of photons that reach the detector (N_o) after traversing the sample is registered in the detector and related to the number of incident photons through the following expression:

$$N_o = N_i \cdot e^{-\int \mu(x) dx} + N_{dark} \quad (7)$$

Where $\mu(x)$ corresponds to the lineal attenuation coefficient at a certain point and N_{dark} to the intensity that is detected when the x-ray source is switched off, also known as “dark current”.

$$\int \mu(x) dx = -\ln \left(\frac{N_o - N_{dark}}{N_i} \right) \quad (8)$$

N_i will be obtained by performing an acquisition without the sample but with the x-ray source on. The same parameters as in the previous acquisition should be maintained. This acquisition is usually known as flood image (N_{flood}) and is described in the following equation:

$$N_{flood} = N_i \cdot e^{-\int 0 dx} + N_{dark} \quad (9)$$

Substituting N_i from equation (9) into (8) yields the value of the linear attenuation integral (10), where different detector gains (N_{flood}) and dark current N_{dark} have been adjusted:

$$\int \mu(x) dx = -\ln \frac{N_o - N_{dark}}{N_{flood} - N_{dark}} \quad (10)$$

Detector may have pixels that are not working properly and not receiving the incoming signal. As such, they are usually called “dead pixels”. Before acquisition, calibration is needed to correct their effect. For this, it is necessary to find the exact position of those pixels and to interpolate them with the neighboring pixels.

Figure 24 shows the different intermediate images generated in the acquisition process.

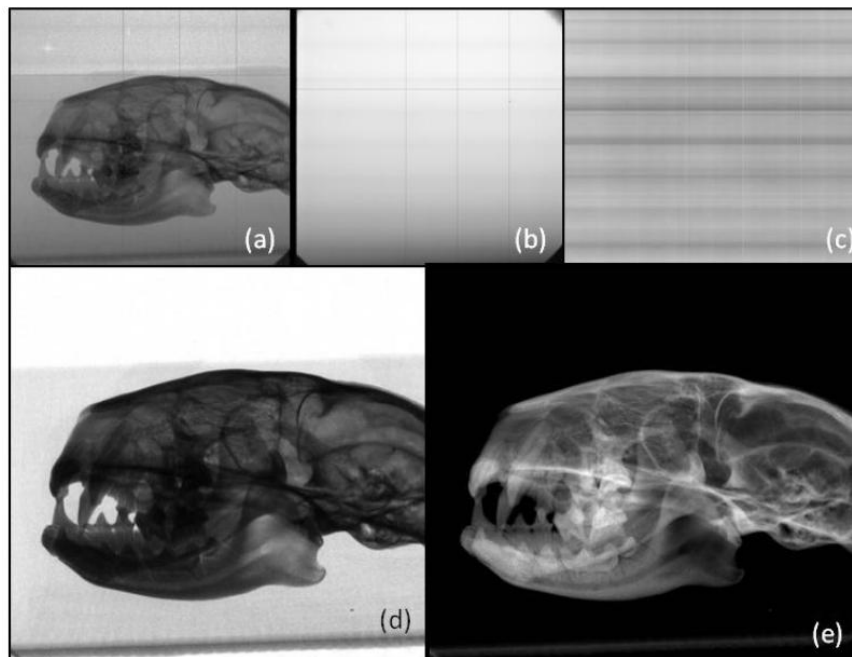


Figure 24 – (a) Raw data; (b) Flood image without object placed in the field of view; (c) Dark image; (d) Raw data after undergoing aforementioned corrections of gain and dead pixels; (e) Attenuation image after applying the logarithm to (d).

Each acquisition consist of a header document with ‘ACT’ extension (an example of ACT document has been included in Annex B) and several files with projection data with extension ‘CTF’. The former contains the necessary information concerning the parameters that were used to perform the study, such as size and number of projections. The latter, projection data, is stored in files and codified with 16 bits unsigned (unsigned integer or uint) in the corresponding ‘CTF’. The total number of ‘CTF’ files created depends on two parameters: binning and number of projections (angular positions) that were used for the acquisition. Binning value can be modified by the user and is related with the pixel size in the detector (50x50 μm) and the pixel size in the projection, that is, 50-binning x 50-binning μm . Table 1 summarizes how different binning values are related to changes in pixel size, projection size and number of projections.

Binning	Pixel size (μm)	Projection size (pixels)	Number of projections per ‘CTF’ file
1	50	2400x2400	30
2	100	1200x1200	90
4	200	600x600	180

Table 1– Available CTF files features according to binning value

Image Reconstruction and Visualization

The micro-CT add on is equipped with a user PC where there is a multimodal workstation or console (**MMWKS**, [16]) and the multi-bed reconstruction software *Mangoose* [12], based on the analytical method FDK [7]. Console shows image gray values in HU units, and the scanner is previously calibrated.

Console aims at providing a friendly interface where user can modify and specify certain acquisition parameters. Three different options are available when running the console, ACQ, RECON and TIMING (as shown in Figure 25). ACQ corresponds to acquisition of projections for a certain study. RECON refers to the reconstruction of raw projection data. TIMING option is used to time each procedure. By clicking on ACQ, and then in CT_ACQ, the window shown in Figure 25 – right appears on the screen.

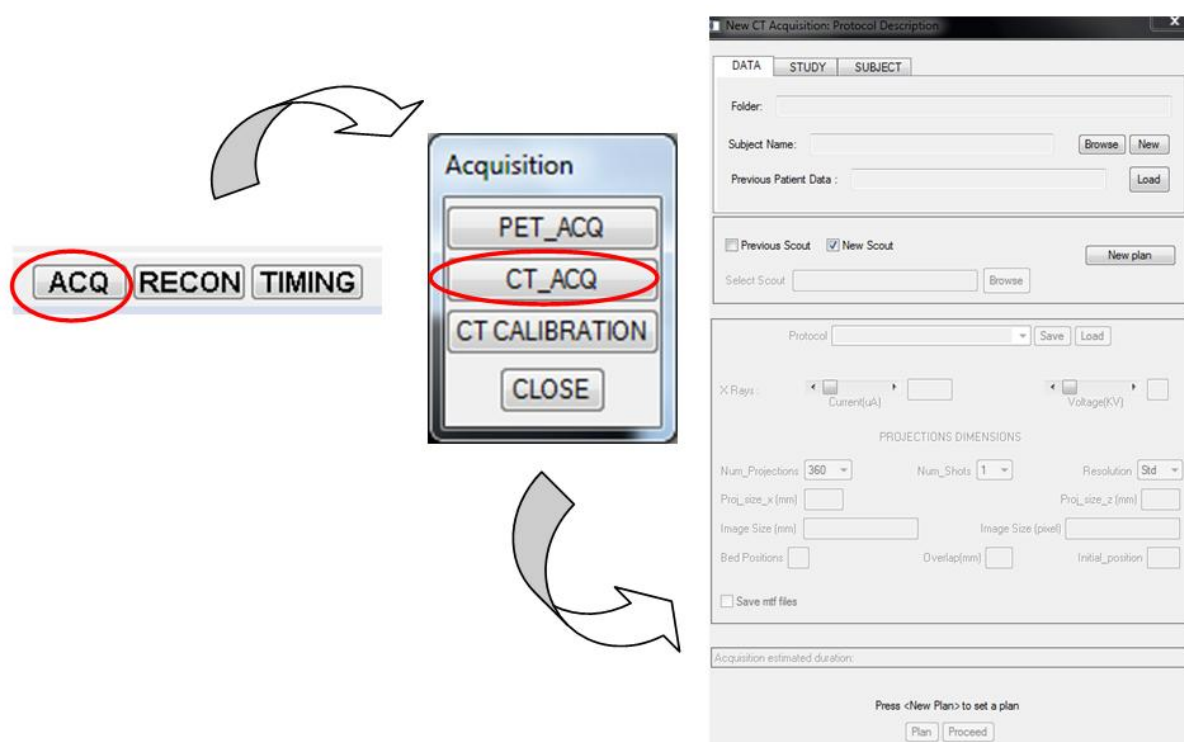


Figure 25 – (left) Options available on MMWKS, by clicking on ACQ the window in the middle appears on the screen; (middle) Example of console acquisition interface options offered to the user, by clicking on “CT_ACQ” the window on the right appears and acquisition parameters can be selected.

Reconstruction can be launched according to specific needs, such as correcting for beam hardening effect and reducing ring artifact. Reconstruction process creates two new extension files: a header with extension ‘HDR’ and a file with the reconstructed data with extension ‘IMG’. The header stores subject data and some acquisition parameters, such as projection size and voltage of the x-ray source (an example of HDR document has been included in Annex C). By clicking on RECON, and then CT_RECON the window shown in Figure 26– right appears on the screen.

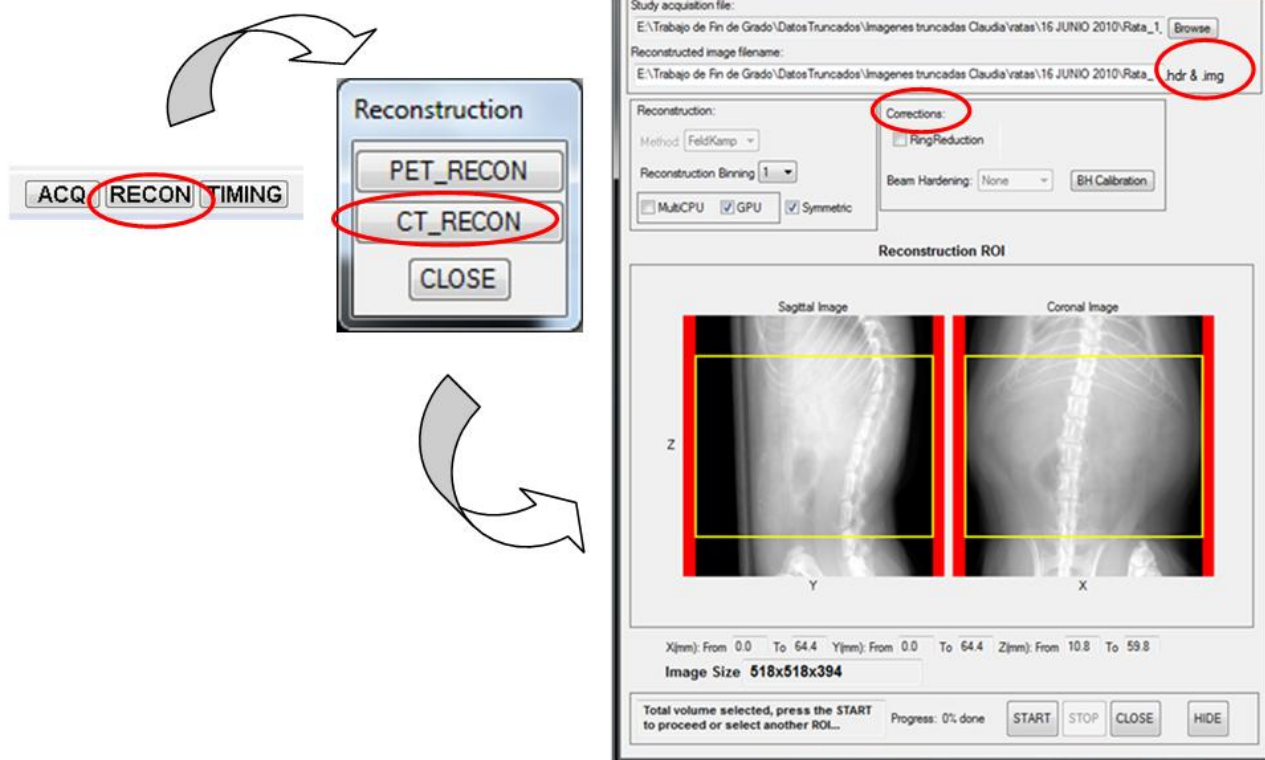


Figure 26 – (left) Options available on MMWKS, by clicking on RECON the window in the middle appears on the screen; (middle) Example of Console Reconstruction interface options, by clicking on CT RECON the image on the right opens. With BROWSE option a certain study can be selected, in this example a rat CT, and corrections can be applied before reconstruction.

Furthermore, additional features of the console include, apart from visualization and handling, segmentation, registration and analysis of the reconstructed images (Figure 27).

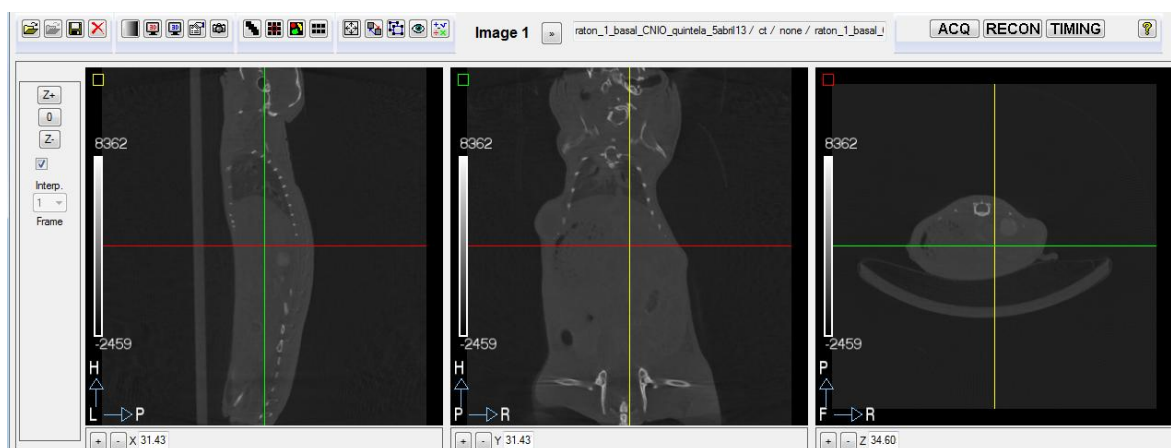


Figure 27 – Example of MMWKS interface showing a mouse CT after reconstruction

2. 2. Objectives and Key Milestones

The goal of this project is to develop a truncation artifact correction algorithm and to integrate it into the micro-CT add-on scanner available at Hospital Universitario Gregorio Marañón.

This project has a clear task division, including the following milestones:

1. Study of the target system: micro-CT add-on scanner for small animal imaging.
2. Study of truncation artifact in the aforementioned scanner.
3. Bibliography review of methods for truncation artifact correction. Implementation of the selected algorithm for truncation artifact correction according to the scanner needs.
4. Method evaluation and results.
5. Implementation of the correction method into the reconstruction interface of the target system and assessment of the complete software.

2. 3. Outline of the Document

The present document is organized in 6 sections. Section 1 presents an introduction to x-ray imaging in general and in CT in particular, including a brief section for image reconstruction. It also presents a detailed description of the different CT artifacts that degrade image quality.

In Section 2 relevancy of CT scanners in preclinical application is described. Motivation and context justify the need of developing an algorithm for truncation correction in the micro-CT add-on. A detailed description of the target system is made. Key milestones of the project and outline of the document are listed.

In Section 3, Truncation artifact is studied, explaining the relevance of correcting these data inconsistencies.

In section 4, proposed methods in the literature are reviewed and the selected correction method is presented. Methodology for algorithm efficacy evaluation is explained.

In section 5, performance of the algorithm is evaluated through simulations and real raw truncated projections from the scanner.

In section 6, overall conclusions and limitations of the project are presented and future work lines are proposed.



Study of Truncation Artifact

3. Study of Truncation Artifact

Truncation artifact appears due to the acquisition of incomplete projections when part of the sample lies outside the field of view (FOV). This effect is illustrated in Figure 28 - left, where the blue cube fits inside the x-ray beam (grey area) while the red cube is bigger and the cone beam rays are unable to cover its whole surface. Therefore, the complete projection defining red cube shape will not be recorded by the detector, as part of it lies outside the scan FOV. Acquired data are thus abruptly discontinuous at the projection boundaries. Incomplete projections are likely to occur in the target system when working with obese rats, too big to fit inside the scanner, and even some studies that require positioning the bed in such a way that part of it lies outside the field of view. Figure 28 – right shows in (A) a complete projection of a mouse that perfectly fits inside the FOV and (B) a truncated projection of a rat body that extends beyond the scanner FOV.

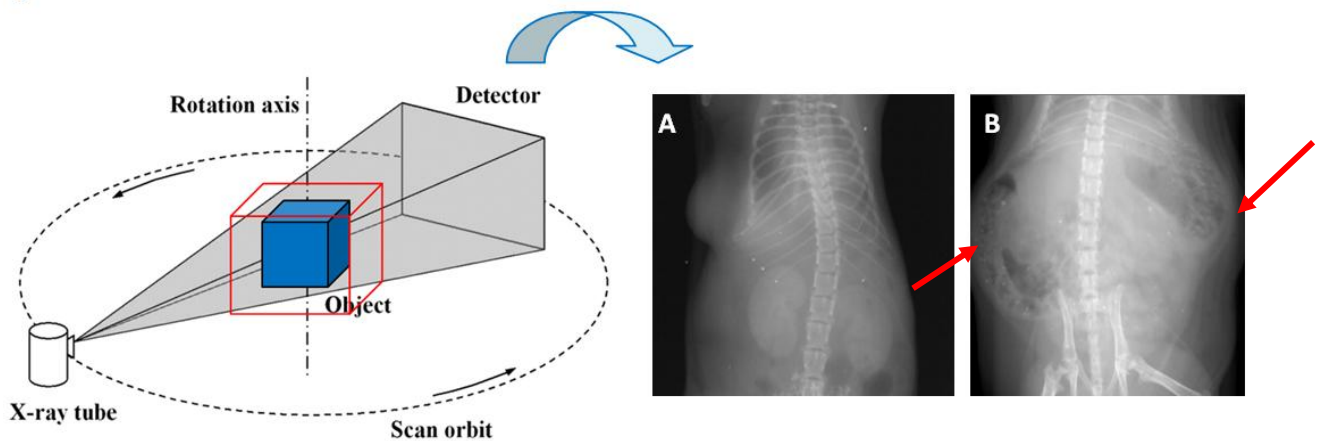


Figure 28 – (left) CT scheme showing an object (red cube) that lies outside the FOV; (right) A, complete projection of a mouse CT study. B, truncated projection of a rat CT study.

Figure 29 – left shows a complete mouse projection. Profile showed in Figure 29 – right was drawn along the yellow line in Figure 29 – left.

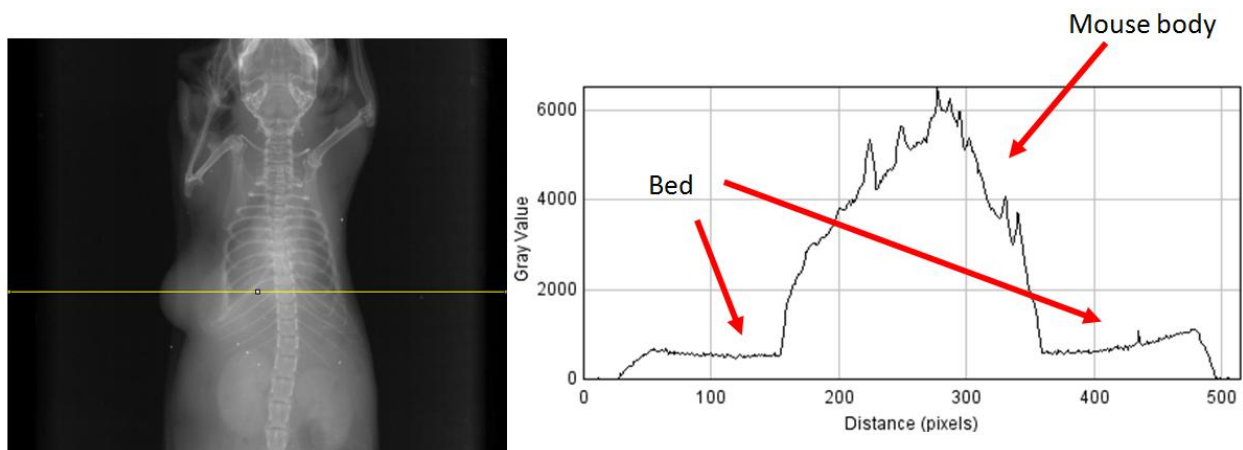


Figure 29 – (left) Complete projection of a mouse CT study, (right) complete profile along yellow line plotted in the projection on the left.

Figure 30 - left illustrates a truncated projection. Figure 30 – right shows the sudden loss of signal at both projection boundaries in the truncated profile drawn along the yellow line in Figure 30 – left.

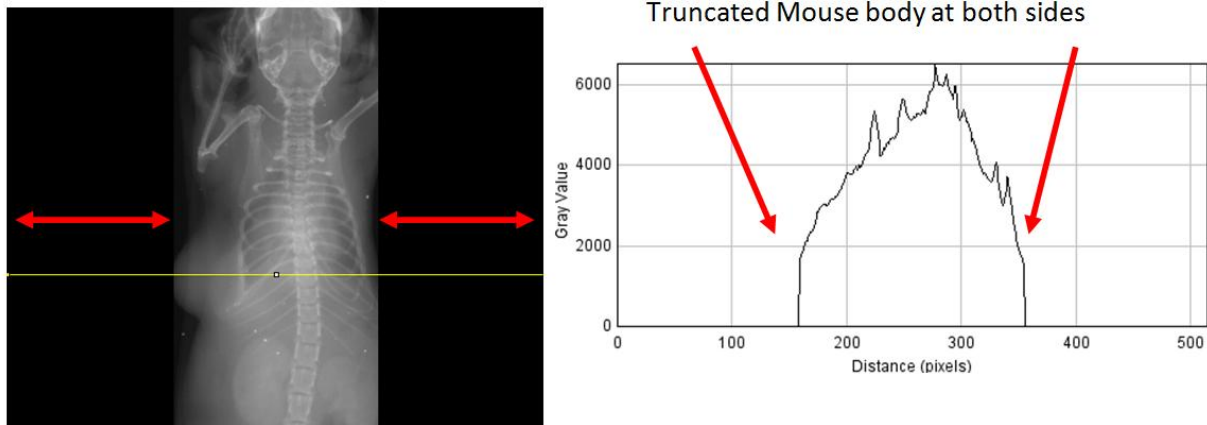


Figure 30 – (left) Truncated projection of a mouse CT study, (right) truncated profile along yellow line plotted in the projection on the left.

If the truncated data is reconstructed with an analytical method, such as (FBP), problems arise in the filtering step. The reason for this is that 1D FFT of the projections will have components enhanced in the high frequency components due to discontinuities in the projections. This creates sharp edges, and their effect will be amplified by the ramp filter in FBP (as shown in Figure 31 - right).

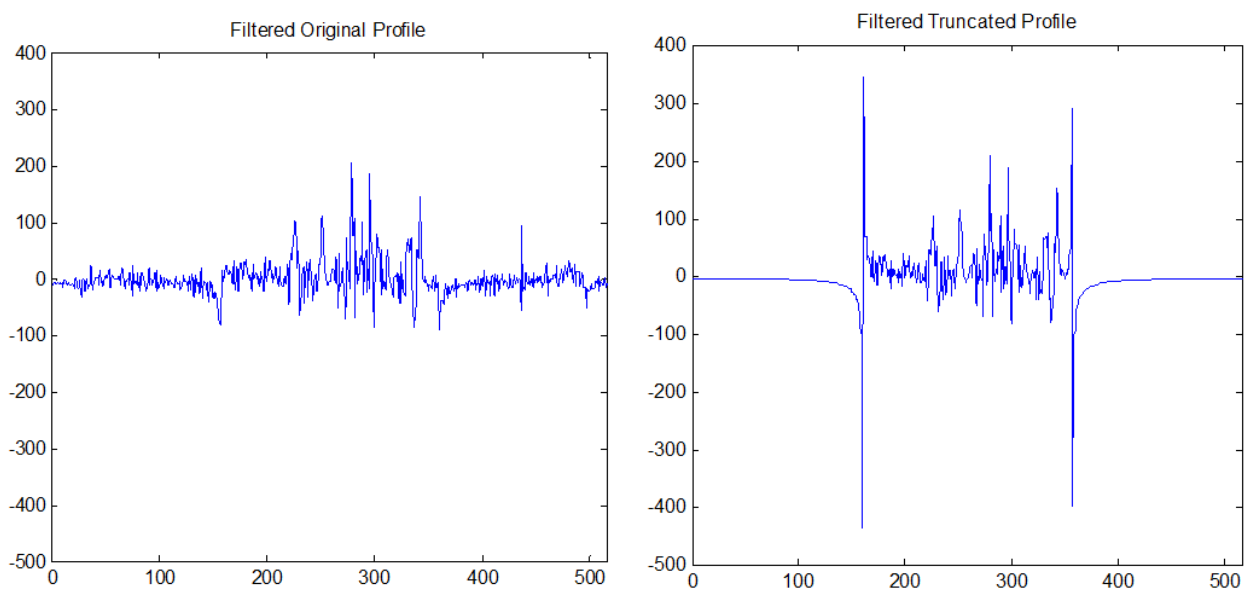


Figure 31 – Effect of the filtering step: (left) homogeneous frequency distribution at the edges, (right) high frequencies have been enhanced in the truncated image.

As a result of the high frequency component increment, reconstructed truncated projections may produce bright shading artifacts near the edge of the reconstructed image (Figure 32, [17]). In some cases, bright rim can be combined with characteristic streaking.



Figure 32 – Reconstructed CT image showing truncation artifact (bright circular shading) combined with streaking (Mawlawi et al, 2006).

Truncation artifact degrades the qualitative and quantitative analysis of the images. Figure 33 illustrates how the more an area (phantom portion) is truncated, the higher the artifact influences the resulting image, [4]. On account of this, correction algorithms are necessary to visualize the peripheral structures within the scan FOV [1]. In this way, misleading information and consequent misdiagnose of a CT study could be prevented.

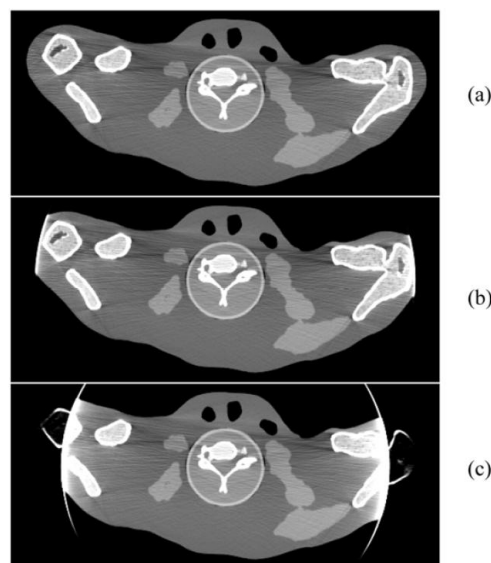


Figure 33 – Illustration of projection truncation in a phantom. (a) Original projection without truncation. (b) Simulated moderate level of projection truncation. (c) Simulated severe level of projection truncation (Hsieh, 2009).

One approach to reduce truncation artifact is by adequately positioning the sample in the scan FOV. However, as stated above, there are some cases in which this is unavoidable. It creates the need of developing algorithms for correcting the acquired data.

Correction of Truncation Artifact

4. Correction of Truncation Artifact

4. 1. Bibliography Review of Truncation Correction Methods

Various approaches have been proposed to reduce truncation artifact in cases where patients are too big to fit in the scanner FOV. Furthermore, special interest is placed in limited field of view CT (also known as interior CT), in which only a small region of interest inside the body (such as spine or tumors) is acquired, reducing patient dose. One way of doing this is by performing a complete low dose acquisition to complement the high dose Region of Interest (ROI) acquisition [18]. This option is not suitable for the problem in the micro-CT add-on when rats extend outside the field of view, making acquisition of complete low dose image impossible.

The proposed approaches to correct the truncation artifact are based on completing the projections, following different strategies. Figure 34, column C, shows a simple solution by setting the sinogram outside FOV to the end projection values and reconstruct the image using FBP, proposed by Boas et al in 2012 [19].

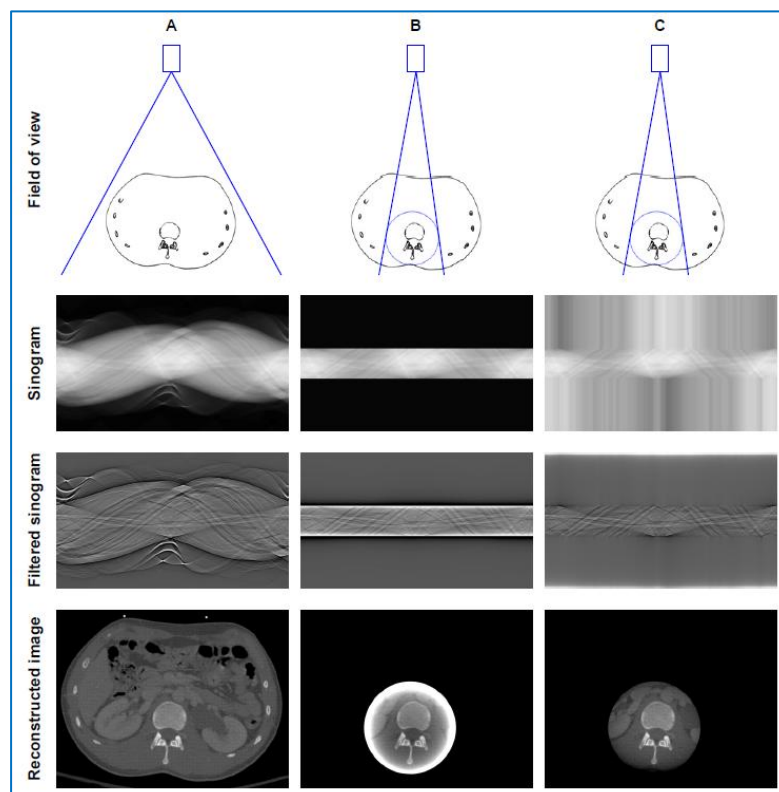


Figure 34 – Top row shows the different fields of view, second row shows the corresponding sinograms, third row shows filtered sonograms and bottom row shows FBP reconstructions. First column (A) corresponds to a complete FOV acquisition, second column (B) Corresponds to a limited FOV in which the sinogram outside the FOV is set to zero, resulting in bright shading artifact. Finally, third column (C) presents a limited FOV, with the sinogram outside the field of view set to the end values. In this way, discontinuities are prevented, avoiding the bright rim (Boas 2012).

Even though the aforementioned approach reduces to a high extend the bright rim of truncation, a small error still appears at the edge [19]. In order to minimize this uncertainty, Hsieh proposed in 2004 [20] an approach that makes use of the fact that the total attenuation of each ideal projection remains constant over the views. They use the magnitudes and slopes of the projection samples at the location of truncation to estimate water cylinders that can best fit to the projection data outside the FOV. The difficulty is how to estimate water cylinders to complete projection data. Ohnesorge et al 2000 [1] developed an extrapolation method that solves the problem of estimating the data outside the FOV: data outside projection boundaries is simulated with a symmetric mirroring extrapolation with respect to the truncated profile. Extrapolated pixels at projection sides define continuous intensity decay (see Figure 35).

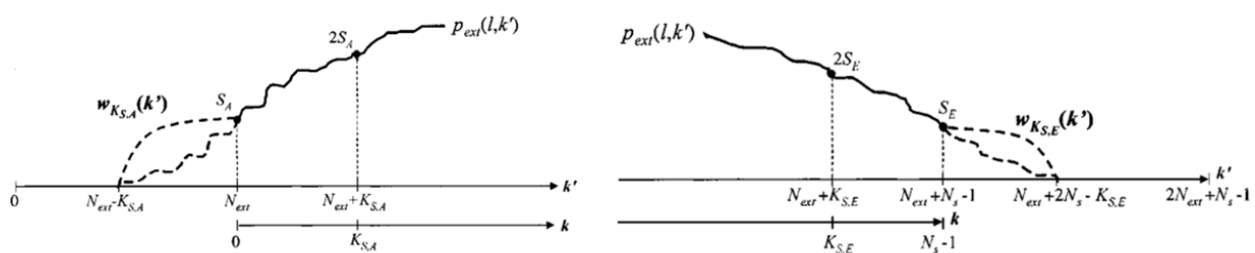


Figure 35 – Top image shows a truncated sinogram, bottom image shows the correcting sinogram form by sine completing curves (Ohnesorge et al, 2000).

A different approach is that presented by Chityala et al [21], who proposed an extrapolation technique that takes advantage of the fact that every feature in the object traces a sine curve in the sinogram. By completing the sine curves in a truncated sinogram, it is possible to obtain reconstruction comparable to full Field Of View. This effect is illustrated in Figure 36, [21]. However, this approach implies certain complexity for modeling sinogram curves.

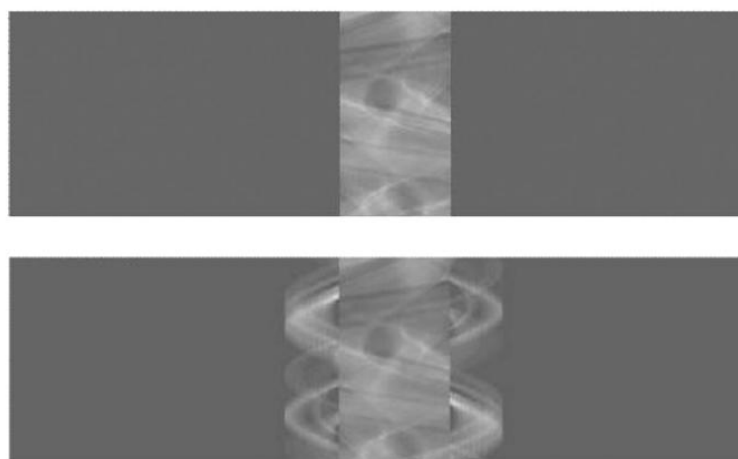


Figure 36 – Top image shows a truncated sinogram, bottom image shows the correcting sinogram form by sine completing curves (Chityala et al, 2005).

Finally, Wiegert et al presented in 2005 another technique for completing the sinogram, based on a priori knowledge. This is done by selecting a CT scan of a different patient/sample showing the same body region. 3D image registration is done so as to match both acquisitions. Then, reference data is used to complete the projections [22]. Although this approach is very attractive, it was not selected because of the problems common to registration of rats that would be in different positions and probably with different induced tumors.

Ohnesorge et al algorithm [1] has been selected as the optimal one for the micro-CT add-on because of its ease of implementation and efficiency in modeling smooth extrapolated profiles.

4. 2. Selected Correction Method

Method proposed by Ohnesorge et al aims at extrapolating the truncated projections at the edges with a smooth transition of the projection data to the baseline [1]. This extrapolation is performed before image reconstruction. Truncated projections are extended at the sides and values are assigned based on a “symmetric mirroring” extrapolation that is performed perpendicularly to the decaying profile. After the extrapolation procedure an appropriate weighting is applied to ensure a smooth transition to zero values. Moreover, noise properties are maintained in the extrapolated region [1].

To guarantee low computational effort, the first algorithm step identifies those projection lines where the scanned object extends beyond the field of view. If the values at the projection line edges are above a predefined threshold, S_{min} , that line will be extended at both edges (by a certain pixel distance, N_{ext}) in the radial direction, with the added pixels pre-set to zero, as shown in Figure 37. However, if the values at the edges do not exceed this threshold, projection will be extended at the sides, but data remain unaltered, as no extrapolation is performed [1].

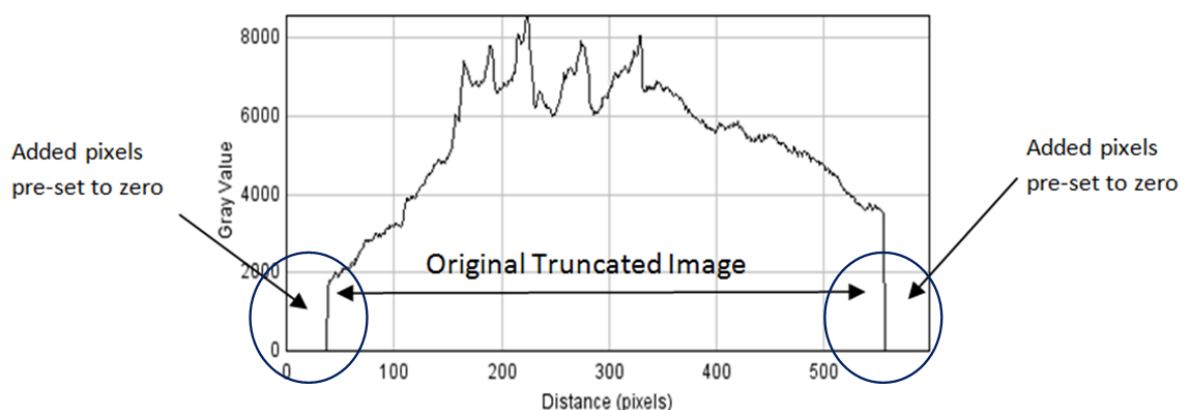


Figure 37 – Profile showing an original truncated projection profile with extension according to N_{ext} value at the sides pre-set to zero.

Let's consider a truncated projection $p(l, k)$ where:

$$\text{projection number } l = 0, 1, \dots, N_p - 1$$

with N_p : total number of projections for reconstruction of an image

$$\text{pixel number } k = 0, 1, \dots, N_s - 1$$

with N_s : total number of pixels in each projection (radial dimension)

Let $\widetilde{p}_{ext}(l, k)$ be the extended truncated projection, filled by zeroes at the sides, allocating in its center the original truncated projection; mathematically:

$$\widetilde{p}_{ext}(l, k) = \begin{cases} 0; & k' = 0, 1, \dots, N_{ext} - 1 \\ p(l, k' - N_{ext}); & k' = N_{ext}, N_{ext} + 1, \dots, N_{ext} + N_s - 1 \\ 0; & k' = N_{ext} + N_s, N_{ext} + N_s + 1, \dots, 2 \cdot N_{ext} + N_s - 1 \end{cases} \quad (11)$$

S_A and S_E (see Figure 38) denote the non-zero attenuation values at the projection edges, $p(l, k = 0)$ and $p(l, N_s - 1)$. These are the central points around which the "symmetric mirroring" extrapolation will be performed (as illustrated in the profiles of Figure 38 with the red dashed line) [1]. Small differences in profile value are calculated starting from S_A to the previous pixel position and subtracting to S_A those differences in the next pixel position (as illustrated in Equations 14 and 15) are extrapolation is perform. The process is repeated for S_E .

The extrapolation is done in the interval between the projection edges (S_A and S_E) and the first value that exceeds the double edge value ($2 \cdot S_A (= K_{S_A})$ and $2 \cdot S_E (= K_{S_E})$). The equations 14 and 15 yield the black dashed line that continues the black solid line profile in Figure 38, [1]. Also, the mirroring operation should not exceed the extrapolation range (fixed parameter, N_{ext}). Therefore, the indices K_{S_A} and K_{S_E} must be limited with:

$$K_{S_A} \leq N_{ext} \quad (12)$$

$$K_{S_E} \leq N_s - N_{ext} - 1 \quad (13)$$

Having these boundaries in mind, the extrapolation is calculated as follows:

For the left extended side:

$$\begin{aligned} \widetilde{p}_{ext}(l, N_{ext} - k) &= S_A - (p(l, k) - S_A) = 2 \cdot S_A - p(l, k) \\ \text{for } k &= 1, 2, \dots, \min(K_{S_A}, N_{ext}) \end{aligned} \quad (14)$$

For the right extended side:

$$\begin{aligned} \widetilde{p}_{ext}(l, 2 \cdot N_s + N_{ext} - 2 - k) &= S_E - (p(l, k) - S_E) = 2 \cdot S_E - p(l, k) \\ \text{for } k &= N_s - 2, N_s - 3, \dots, \max(K_{S_E}, N_s - 1 - N_{ext}) \end{aligned} \quad (15)$$

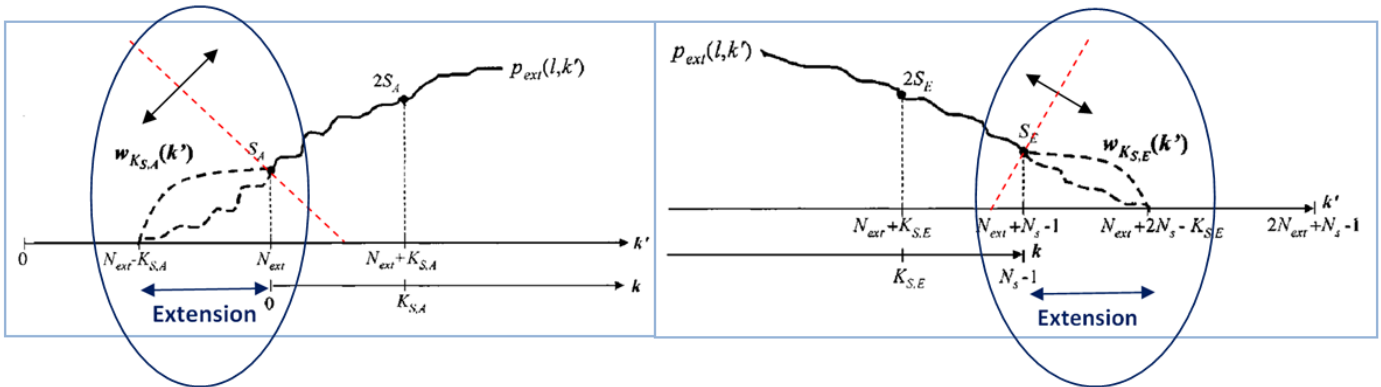


Figure 38 – (left) “symmetric mirroring” extrapolation (back dashed line) at the left side is performed around point S_A (red dashed line) and (right) symmetric mirroring extrapolation (back dashed line) at the right side is performed around point S_E (red dashed line). Back dashed lines denoted by $w_{S_A}(k')$ and $w_{S_E}(k')$ indicate the sine shaping effect (Ohnesorge et al, 2000).

Finally, the extrapolated projection $p_{ext}(l, k')$ is generated by multiplying $\widetilde{p}_{ext}(l, k)$ by a sine going from 0 to $\frac{\pi}{2}$ for the left edge and to $\frac{\pi}{2}$ to π for the right edge. This weighting (denoted by $w_{S_A}(k')$ and $w_{S_E}(k')$) is especially needed if the extrapolated data does not hit the base line after the mirroring operation, with occurs for low values of N_{ext} . Even more, the sine will be elevated to $\tau=0.75$ so smooth its shape, as proposed by Ohnesorge et al, [1]. This effect is illustrated in Figure 38 by the dashed line $w_{S_A}(k')$ and $w_{S_E}(k')$. Therefore, mathematically:

For the left extended side:

$$p_{ext}(l, k') = \widetilde{p}_{ext}(l, k) \cdot w_{S_A}(k') \quad (16)$$

for $k' = 0, 1, \dots, N_{ext} - 1$

For the right extended side:

$$p_{ext}(l, k') = \widetilde{p}_{ext}(l, k) \cdot w_{S_E}(k') \quad (17)$$

for $k' = N_S + N_{ext}, N_S + N_{ext} + 1, \dots, N_S + 2 \cdot N_{ext} - 1$

Figure 39 shows the effect of the sine shaping effect. The upper profile corresponds to a truncated projection that has been extended at the sides. The profile in the middle has been extrapolated without applying the sine. As a result, on the right side there is a sharp decrease in gray values (red circle, right) and on the left side extrapolation values do not reach zero value. Finally, the bottom profile corresponds to an extrapolation with the sine shaping effect: a smooth transition can be clearly observed at both sides (blue circles).

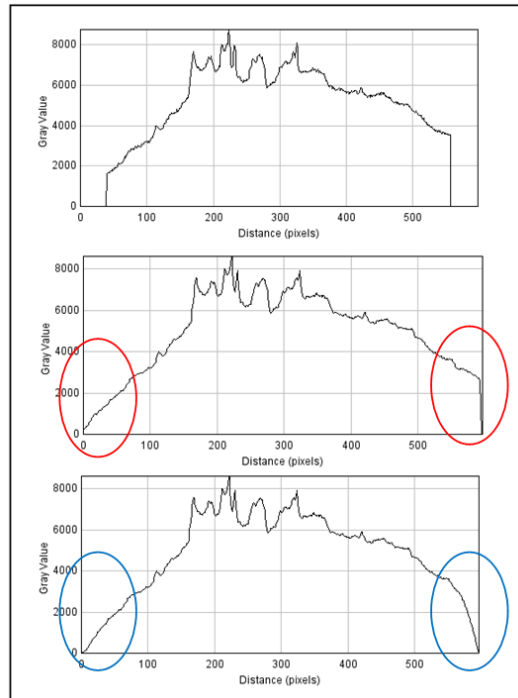


Figure 39 – Comparison of profiles without truncated correction (top), with extrapolation without sine shaping, where the effect of low N_{ext} could not be overcome (middle) and with extrapolation with sine (bottom) using the implemented code.

Figure 40 shows how projection profile and filtering effect should be after applying a truncation artifact correction algorithm. On the left, an extrapolated projection with smooth transition to zero values is shown. On the right, the filtered profile shows a homogeneous distribution.

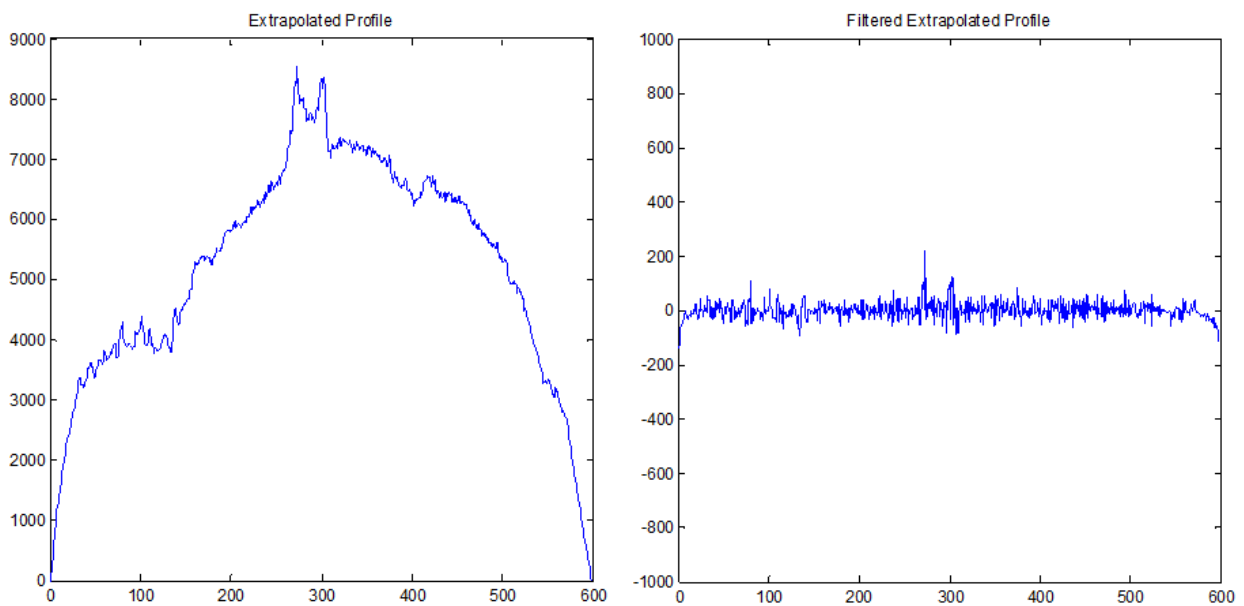


Figure 40 – (left) Extrapolated projection profile with smooth transition to zero values; (right) Effect of the filtering step showing a homogeneous distribution.

4. 2. 1. Implemented Algorithm

Algorithm was implemented in MATLAB 2013. Figure 41 illustrates a flow chart of the algorithm.

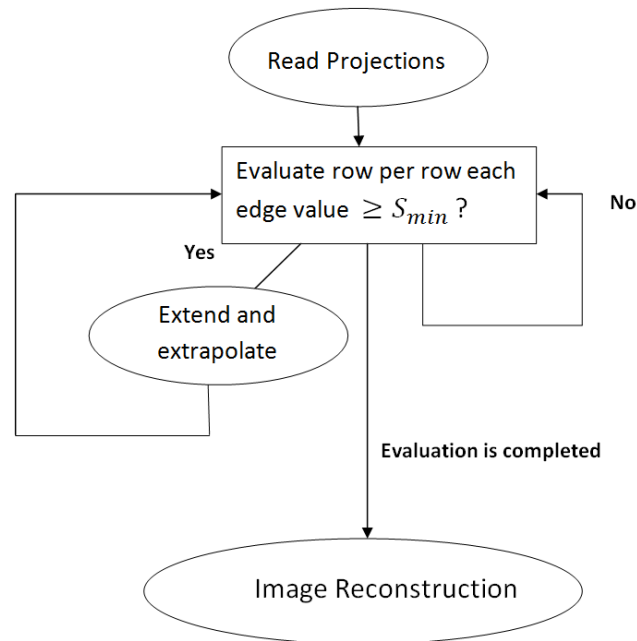


Figure 41– Flow chart of the simplified algorithm. Circles correspond to functions and squares to Boolean operators.

The implemented algorithm consists of the following functions:

Read Projections

The function “read_slice” loads all the projections stored in the acquired CTF files. Its input values are:

- *xSize*: radial dimension of each projection
- *ySize*: axial dimension of each projection
- *zSize*: number of projections stored in each CTF file.
- *Path*: directory from where the acquisitions are loaded
- *Name*: name of the loaded CTF files

It will give a single output, *tmp*, which stores the complete acquired projections.

Ohnesorge Extrapolation

The function “Ohnesorge_extrap” extends and extrapolates the projections whose edge values are above the minimum gray value defined by S_{min} . Its input values are the following:

- tmp : Acquired projections
- $binning$: according to projection binning value, parameter N_{ext} will be set.
- S_{min} : minimum value above which a projection is considered to be truncated. And therefore will be extended and extrapolated.

it gives as output the extrapolated (corrected) projections, p_{ext} . Finally, extrapolated projections are temporarily stored, so as to evaluate and quantify algorithm performance.

A careful study of two key parameters, S_{min} and N_{ext} , was made for algorithm implementation,:

- S_{min}

S_{min} is the minimum threshold that the edge attenuation values should have in a truncated projection so as to be considered for extension and further extrapolation. In case of severe truncation, S_{min} can be increased up to 1000 and still the algorithm will extrapolate every projection line. S_{min} was set to 50 (gray pixel value) for the target system. 50 is a number low enough to ensure every little sample (in the case of mouse usually starting at 500) and bed discontinuity (200) is modeled.

For each projection view, the algorithm will analyze line by line (row by row of the 2D projection data) whether both edges have suffered truncation or not. In the case that only one side has been truncated, the extrapolation will be performed just on that edge.

- N_{ext}

N_{ext} is the size (length) of the added pixels, pre-set to zero. The extension number corresponds to just one side; therefore, the total added pixels are $2 \cdot N_{ext}$. Ohnesorge et al [1] proposes a value of N_{ext} close to $\frac{N_S}{15}$. Most of the studies in the target system are made using binning 4, which have an N_S (total number of projection samples) around 512. Different N_{ext} values have been tested in rat and mice acquisitions: 20, 30 and 40 for projections obtained with binning 4. Figure 42 shows three different projections that have been extrapolated with $N_{ext} = 20$, $N_{ext} = 30$ and $N_{ext} = 40$, respectively. Figure 43 presents their corresponding profiles plotted along the yellow line. It can be observed how the signal drop is smoother with $N_{ext} = 40$. Moreover; difference in computational time was not significant. Therefore, for the implementation in the micro-CT scanner an extension value of 40 has been applied. This selected value (40 for binning 4) also matches with the reference one, proposed by Ohnesorge et al ($\frac{N_S}{15} \sim 36$), [1]

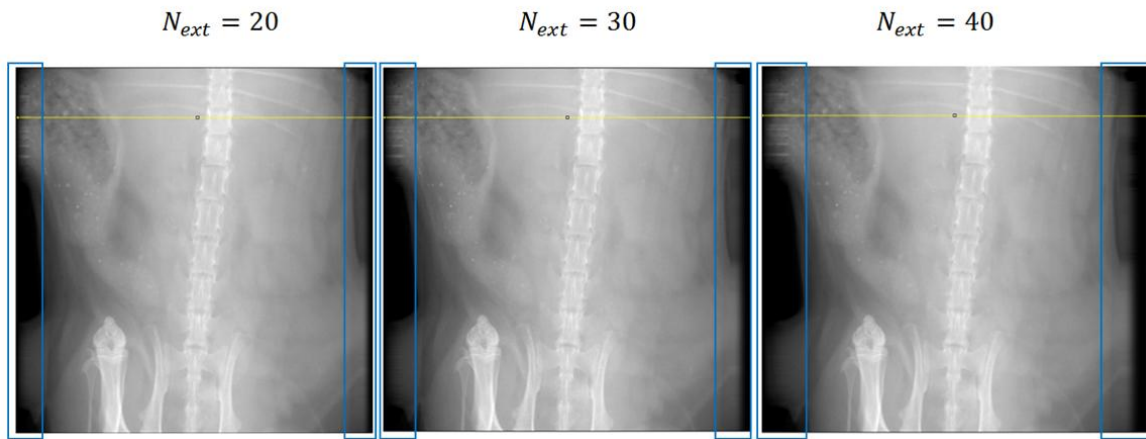


Figure 42 – Truncated projections of a rat CT which have been extrapolated with extensions of 20, 30 and 40 pixels at each side, from left to right, respectively. Profiles plot along the yellow lines are shown in Figure 43.

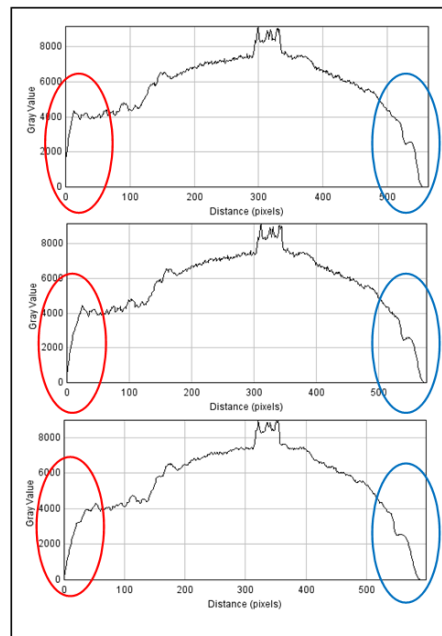


Figure 43 – Comparison performed in ImageJ between extrapolated profiles drawn in Figure 42 with different extension values at the sides (in pixels). From top to bottom $N_{ext}=20$, $N_{ext}=30$ and $N_{ext}=40$, respectively. Red and blue circles indicate the extrapolation performed at the left and right edges, respectively.

It should be noted that selected N_{ext} depends directly on binning value; Table 2 shows the values for all the binning configurations available in the scanner.

Binning	Pixel size (μm)	Projection size (pixels)	Next value (one projection side)
1	50	2400x2400	160
2	100	1200x1200	80
4	200	600x600	40

Table 2 – Scheme showing the correspondence between binning value, projection size and Next value needed to extrapolate and correct truncated projections.

4. 2. 2. Evaluation

Algorithm performance was evaluated through the following steps:

- Quantitative analysis of CT studies from the micro-CT scanner in which different amounts of truncation at the sides were induced.
- Analysis with real truncated data from the micro-CT scanner.

Quantitative Analysis

In order to assess the ability of the algorithm to reduce the truncation artifact, induced **truncations** were simulated in complete projections from the scanner (as can be seen in Figure 44 and Figure 46) and reconstruction was performed. This enabled the quantitative comparison of original complete data with truncated projections **with** and **without** the algorithm correction. Two different set of projections are used to illustrate the process: from a cylinder phantom study and from a mouse study.

So as to compare the different images, reconstructed images from no-truncated projections were crop in ImageJ **after** reconstruction. In such a way, they matched in size with the reconstructed images from truncated projections that, because of the missing information at the sides, were smaller in size.

Moreover, In order to do a quantitative analysis, using ImageJ, same Regions of Interest (ROI) with circular shapes were drawn in homogeneous regions and analyzed in every image. To do so, straightforward macros were created [23]. A macro is a simple program that performs a series of ImageJ commands. One of them is included in Annex D for additional information: it opens the images, crops the original one, delineates the same Regions of Interest in the three different images and measures their areas and mean values. In such a way, it is ensured that the same regions are analyzed in every image.

Percentage of recovery from truncation artifact in mean CT values is calculated as follows:

$$\mathbf{Recovery} (\%) = \frac{\mathbf{Mean}_{corrected\ image} - \mathbf{Mean}_{image\ with\ artifact}}{\mathbf{Mean}_{image\ with\ artifact}} \cdot \mathbf{100} \quad (18)$$

- PHANTOM CYLINDER:

Phantom cylinder data consisted on 360 projections taken around 360 degrees, binning 4, radial size of 512 pixels and axial size of 512 pixels. Truncation width of 90 pixels at each side has been induced in the original complete projections from a phantom cylinder, as illustrated in Figure 44 by the yellow lines.

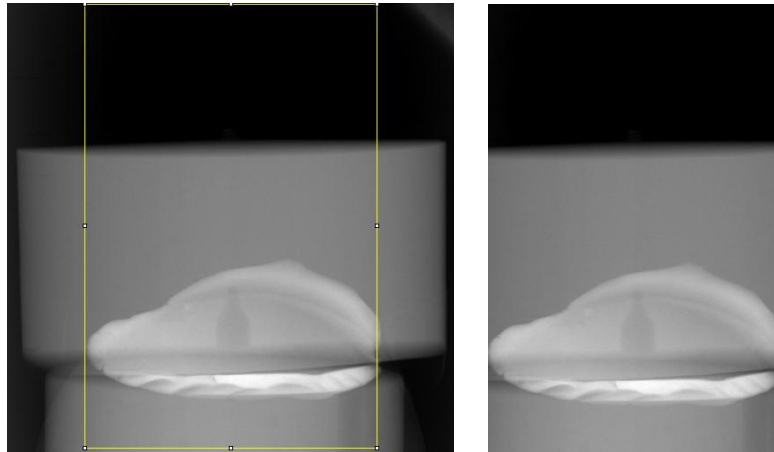


Figure 44 – (left) complete original projection of a cylinder phantom CT, yellow lines indicate the boundaries for truncation; (right) truncated projection after cropping the original projection 90 pixels at each side.

The main point to bear in mind with this phantom is that when inducing truncation at both edges through all the projections we would be creating a cylinder with smaller diameter.

The objective of this section is to evaluate how the algorithm behaves when working with a homogeneous media and how values of regions not too close to the edges vary with and without the algorithm with the presence of truncated data. Figure 45 shows the images to be analyzed with the reconstructed images corresponding ROI delineated by a yellow circle. Same ROI will be drawn after algorithm correction.

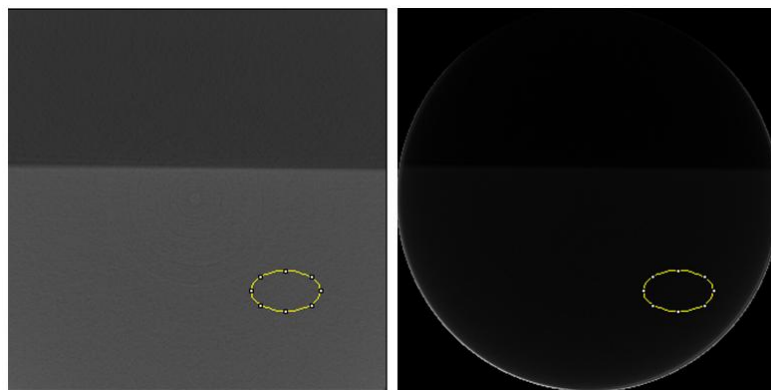


Figure 45 – Axial sections of a cylinder phantom CT (left) Original projection without truncation, the image has been manually cropped after reconstruction (90 pixels at each side); (middle) Reconstructed data without truncation correction.

- MICE ACQUISITIONS FROM THE SCANNER:

Mice data consisted on 360 projections taken around 360 degrees, binning 4, radial size of 516 pixels and axial size of 570 pixels. Different scenarios were analyzed so as to see how the algorithm

overcomes different amounts of truncation and subsequent loss of information: truncation of 140 pixels and of 160 pixels in the case of mice acquisitions. Figure 46 illustrates how truncation has been performed at the sides of each projection.

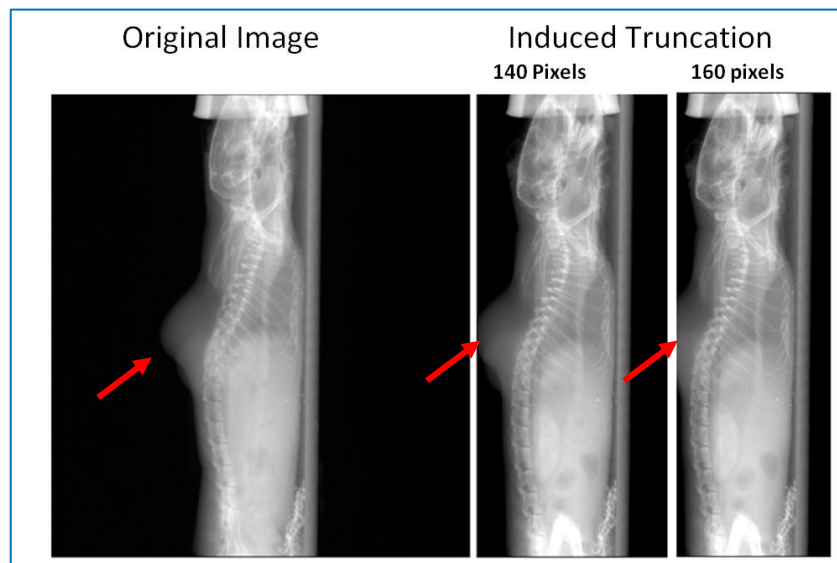


Figure 46 – (left) Original mouse projection data; (middle) Mouse projection data with induced truncation of 140 pixels at each side; (right) mouse projection data with induced truncation of 160 pixels at each side. It can be observe how the loss of signal with 160 pixels is much more aggressive in the protruded mass than with 140.

The exact ROIs corresponding to soft tissue are drawn in every image so as to ensure accuracy in the comparison (Figure 47 shows the ROIs in the image with induced truncation 140, but the same ROIs have been drawn for truncation value 160). One of them has been placed closer to the area where bright rim has been corrected. The other one has been placed in a farther region of homogeneous soft tissue.

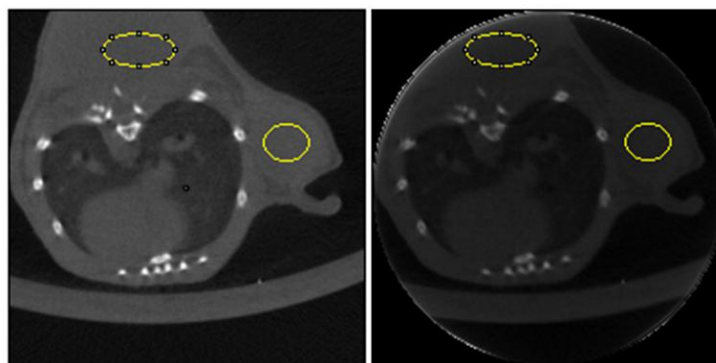


Figure 47 – Axial sections of mouse CT (left) Original projection without truncation, the image has been manually cropped after reconstruction (160 pixels at each side); (right) Reconstructed data without truncation correction.

Furthermore, a profile has been drawn across the bright rim so as to evaluate algorithm behavior when reducing the sharp transition, as indicated in Figure 48.

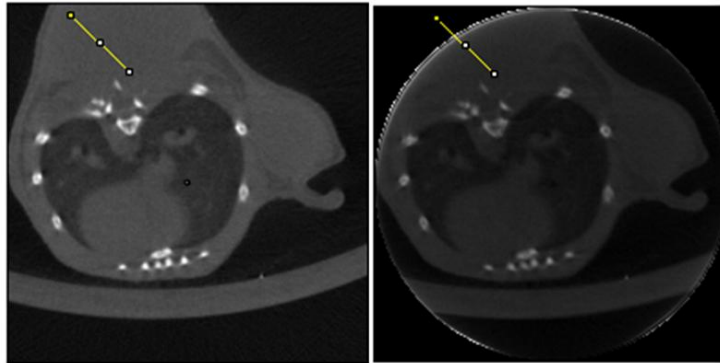


Figure 48 – Axial sections of mouse CT showing the line across which profiles have been drawn. (left) Original image; (right) Image with artifact.

Real Truncated Data from the Scanner

The final step in the algorithm evaluation consists on an evaluation of real truncated acquisitions from the micro-CT, as their body extended beyond the scan field of view. Comparison is done between the corrected Image (reconstructed image from truncated projections that have been corrected with the algorithm) and the image with artifact, which comes from the reconstruction of the truncated projections obtained during a real acquisition. As a result, it is not possible to obtain a quantitative comparison of how the image would have behaved without the artifact.

Two ROIs have been drawn: the first one (ROI 1) is located closed to the truncation edge, the second one (ROI 2) is placed a little more inward but still close to the image boundary. Rat body lying outside the field of view and with the ROIs already drawn can be observed in Figure 49.

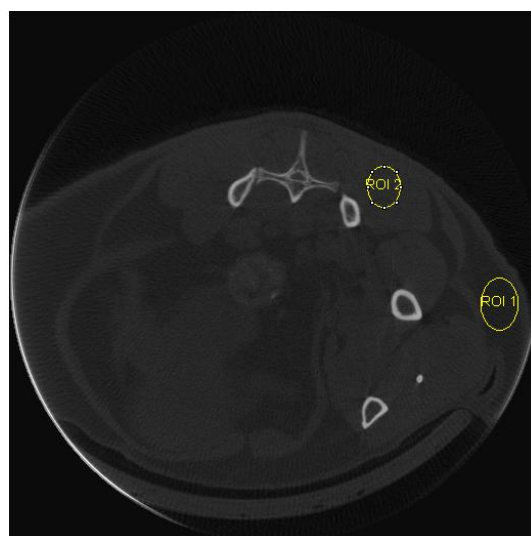


Figure 49 – Axial sections of a rat CT extending outside the Field Of View without algorithm correction.

Results

5. Results

5. 1. Quantitative Analysis

5. 1. 1. Cylinder Phantom – Induced Truncation

Figure 50 shows the results of the simulation, where corrected image appears on the right. Table 3 presents the results of the analysis of the ROI shown in Figure 50.

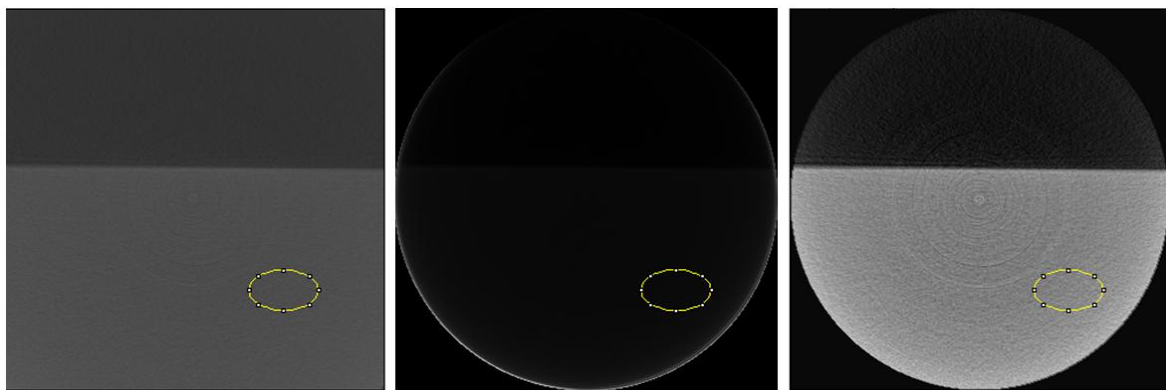


Figure 50 – Axial sections of a cylinder phantom CT (left) Original projection without truncation, (middle) Reconstructed data without truncation correction; (right) Reconstructed data with truncation correction.

BH_cylinder - Induced truncation of 90 pixels at projection boundaries

Mean Value	Original image	Image with artifact	Corrected Image	Recovery%
ROI 1	-326,504	300,453	127,041	57,71

Table 3 – Analysis of the Region of Interest (ROI) of the cylinder Recovery of mean CT value in % has been done by comparing the corrected image with the image with artifact.

5. 1. 2. Mice Acquisitions – Induced Truncation

Figure 51 shows the results of the simulation, where corrected image appears on the right. Table 4 presents the results of the analysis of the ROI shown in Figure 51.

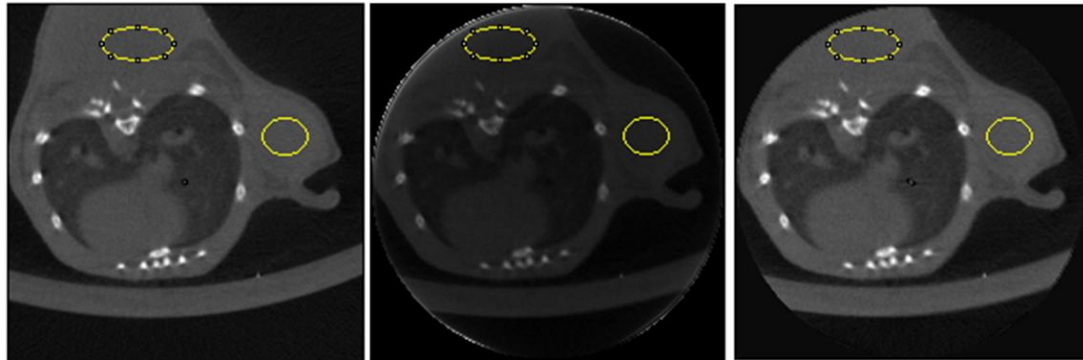


Figure 51 – Axial sections of mouse CT (left) Original projection without truncation, the image has been manually cropped after reconstruction (160 pixels at each side); (middle) Reconstructed data without truncation correction; (right) Reconstructed data with truncation correction.

Mouse_19_basal - Induced truncation of 140 pixels at projection boundaries				
Mean ROI values				
	Original Image	Image with Artifact	Corrected Image	Recovery%
ROI 1 (farther)	128,722	598,73	543,828	9,17
ROI 2 (closer)	92,451	587,537	499,507	14,98
Mouse_19_basal - Induced truncation of 160 pixels at projection boundaries				
	Original Image	Image with Artifact	Corrected Image	Recovery%
ROI 1 (farther)	128,722	690,402	574,005	16,86
ROI 2 (closer)	92,451	941,644	537,486	42,92

Table 4 – Analysis of the Regions of Interest (ROI) of mouse acquisitions. ROI 1 has an area equal to 396 pixels while ROI 2 has an area of 568 pixels. Blue numbers are key indicators of the correction algorithm performance.

Comparison between profiles (drawn in Figure 52) is shown in Figure 53. The smooth transition performed by the correction algorithm is observed.

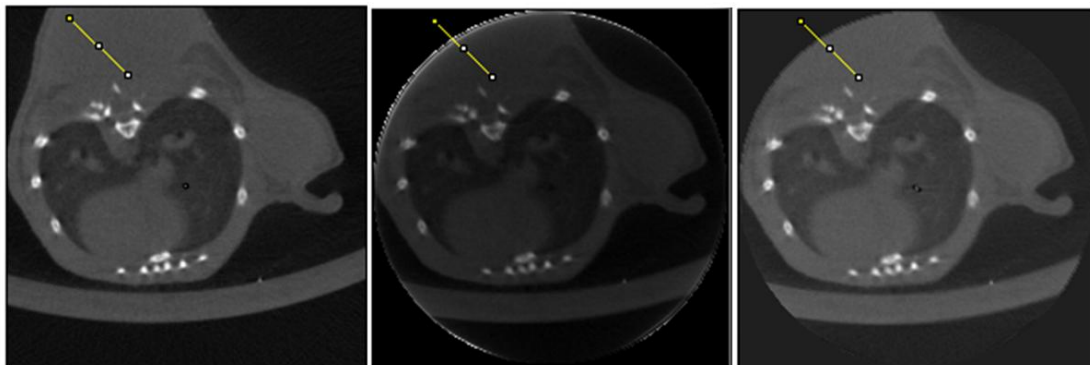


Figure 52 – Axial sections of mouse CT showing the line across which profiles have been drawn. (left) Original image; (middle) Image with artifact; (right) Corrected Image.

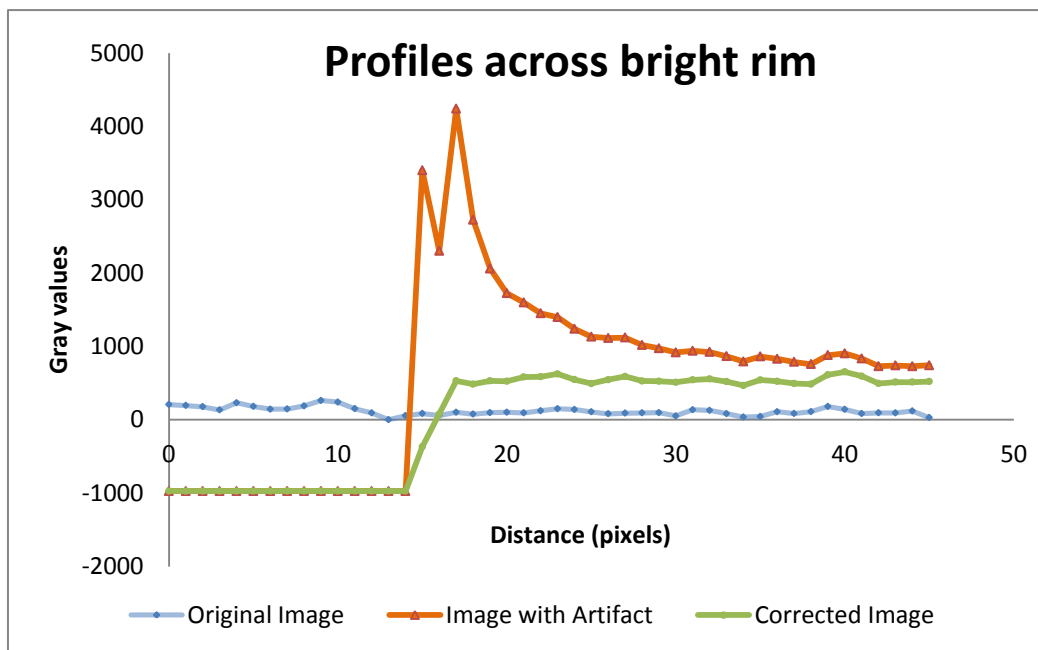


Figure 53 – Comparison of profiles drawn along the yellow lines.

5. 2. Real Truncated Rat Acquisitions

Figure 54 shows the results of the simulation, where corrected image appears on the right. Table 5 presents the results of the analysis of the ROIs shown in Figure 54.

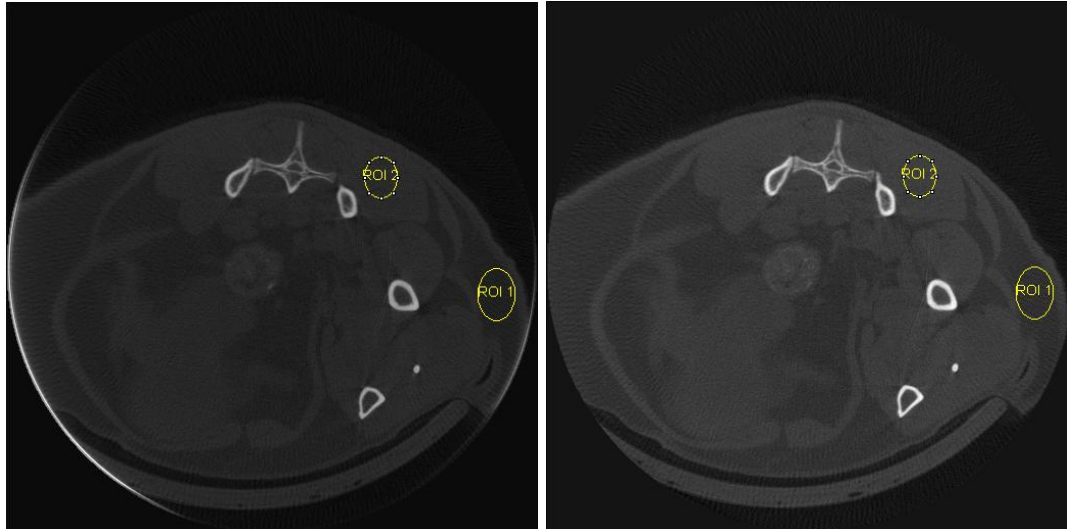


Figure 54 – Axial sections of a rat CT extending outside the Field Of View: (left) Reconstructed data without truncation correction; (right) Reconstructed data with truncation correction.

Rata_ZDF			
Mean ROI values			
	Image with Artifact	Corrected Image	Recovery %
ROI 1	-181,87	-219,383	20,63
ROI 2	106,025	76,495	27,85

Table 5 – Analysis of the Regions of Interest (ROI) drawn in rat acquisitions. ROI 1 has area equal to 1444 pixels while ROI 2 has an area of 1008 pixels. Red numbers are key indicators of the correction algorithm.

5. 3. Implementation

Complete truncation correction algorithm was adapted from MATLAB 2013 to IDL 8.3 and integrated inside the complete software of console **MMWKS [16]**. Before implementing the algorithm in IDL, reconstruction of the extrapolated (corrected) projections was made in MATLAB, using an Image Reconstruction Toolbox (IRT). The “Image Reconstruction Toolbox” is a collection of open source algorithms for imaging reconstruction. This software has been developed at the University of Michigan by Jeff Fessler and his students. Within this Toolbox, the analytical reconstruction method FDK (named after Feldkamp, Davis and Kress) has been used. A careful evaluation of CT reconstruction (CT_reconinterface.pro) work flow was made, so as to properly fit truncation artifact correction in the **MMWKS** library.

In addition to this, an interface is needed, so as to offer truncation correction option to laboratory technicians. Truncation artifact correction algorithm is designed to be applied just before undergoing reconstruction, as the extended projections will be the input to *Mongoose* [12] reconstruction software.

By clicking on RECON and CT_RECON the window shown in Figure 55 – right appears on the screen. It can be seen how inside “Corrections” section a specific option for Truncation has been implemented (bottom red oval). By clicking on “BROWSE” in the reconstruction interface, the user can select the file with extension “.ACT” of the acquired study to be reconstructed. Furthermore, as indicated by the upper red oval shown in Figure 55, every time that truncation correction is selected the HDR and IMG file names created after reconstruction are named with the suffix “_truncation”.

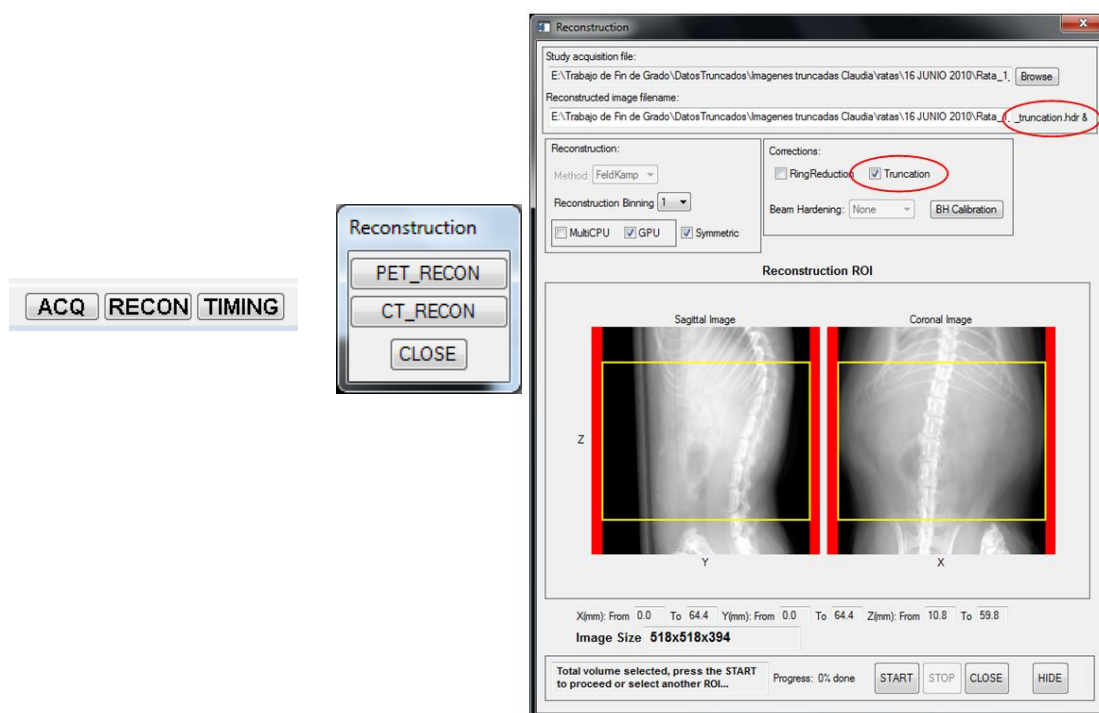


Figure 55 – (left) Console interface options offered to the user, by clicking on “RECON” reconstruction options appear on the screen (middle); by clicking on CT_RECON Console Reconstruction window appears, offering the user the choice to select different correction methods. Truncation option appears highlighted in a red circle. Rat Projections from two different angles are shown.

If the **MMWKS** [16] detects truncation option has been activated, the raw projections stored in CTF files are extended and extrapolated. Then, extrapolated projections are stored in temporal CTF files. When truncated option is activated, **MMWKS** calls *Mongoose* reconstruction software [12] with option **-d** modified so as to extend the radial dimension of the projections. Finally, when reconstruction process is completed, temporal files are deleted.

Figure 56 shows two reconstruction results with truncation correction and without truncation correction in the console.

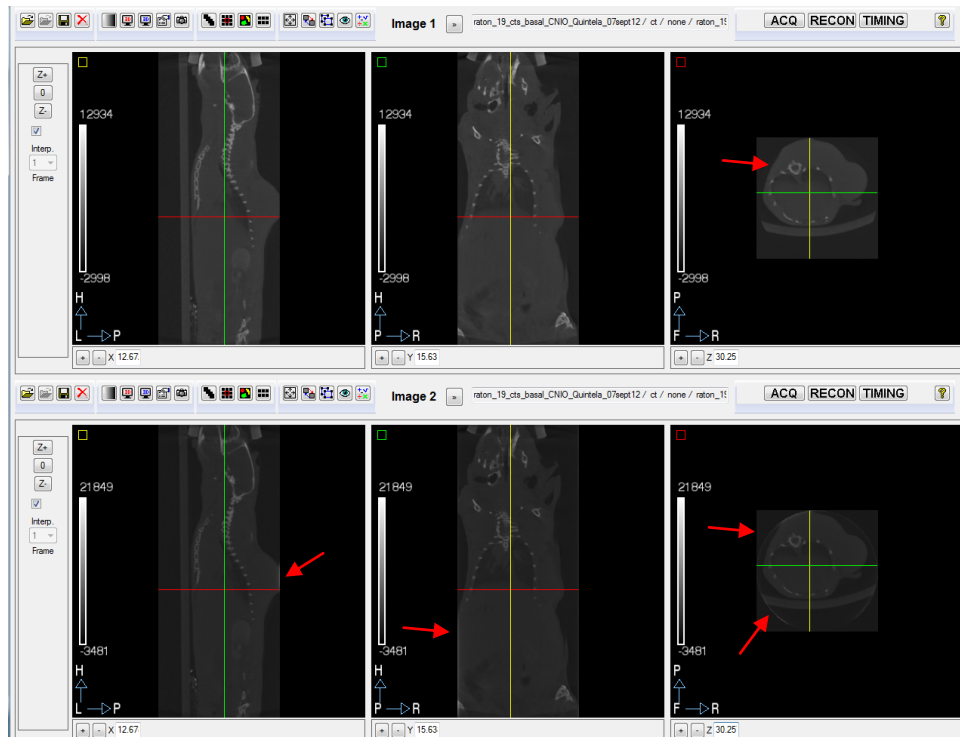


Figure 56 – Upper row: sagittal, coronal and axial views respectively of a truncated CT image with truncation correction. Lower row: truncated CT image without truncation correction.

Discussion and Conclusions

6. Discussion and Conclusions

The present Bachelor Thesis has been developed inside a line of research of high resolution scanners for preclinical application at the Hospital Universitario Gregorio Marañón. It has been focused in the development of an algorithm for correcting micro-CT artifacts produced by truncated or incomplete projections. These artifacts are usually characterized by bright shading and quantification errors.

After a review of the proposed methods in the literature, an optimal approach for the micro-CT add-on under study was selected, based on a sinogram extrapolation method published by Ohnesorge et al [1]. This method consists on a symmetric mirroring extrapolation of the truncated projections that guarantees continuity at the truncation point. It includes a sine shaping effect that ensures a smooth attenuation signal drop. Furthermore, noise properties in the extrapolated region are preserved.

Algorithm performance was assessed using real CT studies. Data of complete cylinder phantom and mice projections from the scanner was modified by simulating different amounts of induced truncation at the projection sides. In this way, original image from complete projections and truncated images with and without correction algorithm were compared. Cylinder results show overall significant recovery from truncation artifact: recovery of 58% in mean CT values. In mice results three different tendencies were observed. First, algorithm shows higher recovery in areas closer to the image boundaries (from 15% to 43% in images with induced truncation of 140 and 160 pixels, respectively) in contrast to farther areas (from 9% to 17% in images with induced truncation of 140 and 160 pixels, respectively). Second, the higher the induced truncation in the original image is, the more the algorithm recovers from the truncation artifact: from 15% in an image with induced truncation of 140 pixels to 43% in an image with induced truncation of 160 pixels (both of these values are obtained from a ROI closer to the image boundaries). Third, a profile drawn across the bright rim shows the smooth transition created by the algorithm; it tries to lower gray values down to the reference of the original image.

Finally, real truncated rat projections from the scanner were also analyzed. However, in this case there was no reference from complete projection data to compare with. Results show a recovery of 21 to 28%.

Therefore, the algorithm eliminates the characteristic bright rim and reduces, to some extent although not completely, the increment suffered by CT values in the presence of the artifact. Algorithm showed a problem when bones were truncated: their gray values were so high that there was not a significant smooth transition at the edges.

Future work lines will focus on overcoming the problems found in the developed method, especially to have a complete recovery of CT values. Implementation of some of the truncation correction methods proposed in the bibliography review will be done to study if they are able to overcome these algorithm limitations. Approach proposed by Wiegert et al (2004) is particularly attractive. It uses reference data previously obtained in the scanner so as to complete the missing parts in the projections [24].



Also, given that the micro-CT add-on is designed to be integrated with a PET scanner, it would be interesting to evaluate the impact of the truncation artifact on the PET values when using the CT image to correct for attenuation.

Annex A - FBP

According to the Central Slice Theorem, projection Fourier transforms fill points in space with a polar sampling. From the Central Slice Theorem, backprojection can be done with a polar coordinate system in the frequency domain. Starting from the equation analysis that relates the Radon Transform with the object Fourier transform, it can be observed that the inverse of the Radon transform can be converted into a backprojection of the previously filtered projections in the image space domain, which defines its name, Filtered Backprojection.

The equation that relates the distribution $f(x,y)$ with its 2D Fourier Transform $F(u,v)$ is the following:

$$f(x, y) = \iint_{-\infty-\infty}^{\infty\infty} F(u, v) \cdot e^{j2\pi(ux+vy)} dudv$$

For going from this coordinate system (u,v) to the polar coordinate system, the following change of variation is needed:

$$u = w \cdot \cos\theta$$

$$v = w \cdot \sin\theta$$

$$du \cdot dv = w \cdot dw \cdot d\theta$$

Therefore, applying this change of variables , yields:

$$f(x, y) = \iint_{0\ 0}^{2\pi\ \infty} F(w, \theta) e^{j2\pi(x\cos\theta+y\sin\theta)} w \cdot dw \cdot d\theta$$

Dividing this integral for $\theta \in [0,2\pi]$ in two parts:

$$\theta \in [0, \pi] \text{ and } \theta \in [\pi, 2\pi]$$

Yields:

$$f(x, y) = \iint_{0\ 0}^{\pi\ \infty} F(w, \theta) e^{j2\pi w(x\cos\theta+y\sin\theta)} w \cdot dw \cdot d\theta + \iint_{2\pi\ 0}^{2\pi\ \infty} F(w, \theta) e^{j2\pi w(x\cos\theta+y\sin\theta)} w \cdot dw \cdot d\theta$$

From Fourier Transform property:

$$F(w, \theta + \pi) = F(-w, \theta)$$

Finally:

$$f(x, y) = \int_0^\pi \int_{-\infty}^{\infty} F(w, \theta) \cdot |w| \cdot e^{j2\pi w t} dw \cdot d\theta$$

Taking into account that the Central Slice theorem can be substituted by the 2D transform of the distribution for a projection angle θ given by the 1D transform of the corresponding projection, yields:

$$f(x, y) = \int_0^\pi \int_{-\infty}^{\infty} S_\theta \cdot |w| \cdot e^{j2\pi w t} dw \cdot d\theta$$

Which can be simplified to:

$$p_\theta(t) = \int_{-\infty}^{\infty} S_\theta \cdot |w| \cdot e^{j2\pi w t} dw$$

This equation is the inverse Fourier transform of the product of two transforms. This product corresponds in the projection space with the convolution of the projection, $P_\theta(t)$, with a function whose Fourier transform is equal to a ramp function, $|w|$. Therefore, it is a filtered projection. Rearranging the terms yields:

$$f(x, y) = \int_0^\pi \mathbf{p}(x \cdot \cos\theta + y \cdot \sin\theta, \theta) d\theta$$

Annex B - ACT

raton_19_cts_basal_CNIO_Quintela_07sept12_07Sep2012_Acq003

Fri 07 Sep 2012 08:08:43 PM CEST

[Acquisition]

acq_code_version=4.20
base_filename="raton_19_cts_basal_CNIO_Quintela_07sept12_07Sep2012_Acq003"
Num_projections=360
Binning=4
Frames=8
Voltage=40.000000
Amperage=338.710022
Overlap=0.000000
Bed_positions=1
Al_filter=1.000000
Shutter_mode=0
Init_angle=0
Scan_Angle=360
Rot_direction=0
Init_bed_position=368.309998

[Output files]

Num_files=2
Util_pixels_Z=2400
Proj_size_axial=570
Util_pixels_Y=2400
Proj_size_radial=516
Projections_per_file=180

[Calibration]

file_detector_corrections="d_corrections_CT.txt"
File_flood="flood4bin"
file_dark="dark4bin"
file_hounsfield="hounsfield"
magnification_CT=1.641380
alfa_bed_error=-0.002857
beta_bed_error=0.000000
dz_bed_error=4.926110
D_so=226.000000

[PET/CT alignment]

offset_x=-0.901000
offset_y=0.232000
offset_z=-174.639008

[Info]

GENERAL DATA :=

original institution :=unknown



originating system :=unknown
contact person :=unknown
patient name :=raton_19_cts_basal_CNIO_Quintela_07sept12
patient ID :=
patient breed:=
patient dob:=
patient age:=
patient sex:=Other
patient weight (gr):=
patient size (cm):=
patient orientation :=Head_in
patient rotation :=Prone
study ID :=
study date :=7/9/2012
study time :=20:00:33
data description :=
process description:=
user comment=

Annex C - HDR

```
;INTERFILE -Grupo Imagen UMCE HGGMFri Sep 07 20:11:43 2012
INTERFILE :=
imaging modality:=ct
version of keys := 5.4
date of keys := 2006:22:10
acq code version:=4.20
reconstruction code version:=version: 3.2.0
GENERAL DATA :=
original institution:=unknown
originating system:=unknown
contact person := www.hggm.es/image
patient name:=raton_19_cts_basal_CNIO_Quintela_07sept12
patient id:=none
patient breed:=unknown
patient dob:=none
patient age:=unknown
patient sex:=Other
patient weight (gr):=0
patient size (cm):=unknown
patient orientation:=head_in
patient rotation:=prone
study id:=none
study date:=7/9/2012
study time:=20:00:33
data description:=none
process description:=Reconstructed CT
user comment:=none
name of data file:=raton_19_cts_basal_CNIO_Quintela_07sept12_07Sep2012_Acq003.img
IMAGE DATA :=
imagedata byte order:=littleendian
slice orientation:=
number format:=signed integer
number of bytes per pixel:=2
number of dimensions:=1
matrix size [1]:=516
matrix size [2]:=516
matrix size [3]:=570
scaling factor (mm/pixel) [1]:=0.121849
scaling factor (mm/pixel) [2]:=0.121849
scaling factor (mm/pixel) [3]:=0.121849
data compression := none
number of time frames:=1
offset [1]:=-0.901000
offset [2]:=0.232000
offset [3]:=193.671
gated data:=no
```

average cycle length (msec):=NA
cycletlength deviation (%):=NA
accepted deviation (%):=NA
CT IMAGE DATA:=
number of projections:=360
projection binning:=4
voltage (kv):=40.0000
amperage (ua):=338.710
start horizontal bed position (mm):=368.310
overlap (mm):=0.0
magnification factor:=1.64138
number of bed positions:=1
alum filter thickness (mm):=1.00000
projection size [1]:=516.000
projection size [2]:=516.000
projection size [3]:=570.000
number of shots:=8
beam hardening:=None
reconstruction binning:=1
method of reconstruction:=FeldKamp
type of interpolation:=Lineal
method of scatter correction:=NONE
axial correction:=Yes
vertical smooth:=NO
axial smooth:=NO
ring reduction:=NO
TEMPORAL STUDY :=
index nesting level := (time frame)
image duration (sec) [1] :=0.000000
image relative start time (sec) [1] :=0.000000
END OF INTERFILE :=

Annex D - Macro

// Open the reconstructed images in ImageJ

```
// Open Original Image
run("Raw...", "open=[E:\\Trabajo de Fin de Grado\\Rata micro-
CT\\raton_19_cts_basal_CNIO_Quintela_07sept12\\Acq003\\raton_19_cts_basal_CNIO_Quintela_0
7sept12_07Sep2012_Acq003.img] image=[16-bit Signed] width=516 height=516 offset=0
number=300 gap=0 little-endian");
```

```
// Crop manually the original image so that it matches in size with the truncated ones for the
ROI analysis
```

```
makeRectangle(161, 161, 196, 196);
run("Crop");
```

```
//Open the Truncated Image without Algorithm Correction
```

```
run("Raw...", "open=[E:\\Trabajo de Fin de Grado\\Rata micro-
CT\\raton_19_cts_basal_CNIO_Quintela_07sept12\\Acq003\\modif\\raton_19_cts_basal_CNIO_Qui
ntela_07sept12_07Sep2012_Acq003_ring.img] image=[16-bit Signed] width=196 height=196
offset=0 number=300 gap=0 little-endian");
```

```
//Open the Truncated Image with Algorithm Correction
```

```
run("Raw...", "open=[E:\\Trabajo de Fin de Grado\\Rata micro-
CT\\raton_19_cts_basal_CNIO_Quintela_07sept12\\Acq003\\modif\\raton_19_cts_basal_CNIO_Qui
ntela_07sept12_07Sep2012_Acq003_truncation.img] image=[16-bit Signed] width=196 height=196
offset=0 number=300 gap=0 little-endian");
```

// ROI Analysis:

```
//mouse reconstrcuted image with induced truncation of 160 pixels at each side:
```

```
//original Image:
```

```
selectWindow("raton_19_cts_basal_CNIO_Quintela_07sept12_07Sep2012_Acq003.img");
makeOval(140, 62, 25, 20);
run("Measure");
```

```
run("Add Selection...");
makeOval(51, 12, 40, 18);
run("Measure");
```

```
//Truncated Image without Algorithm Correction:
```

```
selectWindow("raton_19_cts_basal_CNIO_Quintela_07sept12_07Sep2012_Acq003_ring.img
");
```

```
makeOval(140, 62, 25, 20);
run("Measure");
```

```
run("Add Selection...");
makeOval(51, 12, 40, 18);
run("Measure");
```



```
//Truncated Image with Algorithm Correction:  
selectWindow("raton_19_cts_basal_CNIO_Quintela_07sept12_07Sep2012_Acq003_truncated  
on.img");  
makeOval(140, 62, 25, 20);  
run("Measure");  
  
run("Add Selection...");  
makeOval(51, 12, 40, 18);  
run("Measure");
```

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Glossary

CT: Computed Tomography

FBP: Filtered Backprojection

FDK: Feldkamp, David y Kreis

FFT: Fast Fourier Transform

FOV: Field of view

HU: Hounsfield Units

IDL: Interactive Data Language

LIM: Laboratorio de Imagen Médica

MATLAB: Matrix Laboratory

MMWKS: Multimodality workstation

MRI: Magnetic Resonance Imaging

PET: Positron Emission Tomography

ROI: Region of Interest

SEDECAL: Sociedad Española de Electromedicina y Calidad

SNR: Signal to Noise Ratio

SPECT: Single Photon Emission Tomography

TAC: Tomografía Axial Computarizada

UMCE: Unidad de Medicina y Cirugía Experimental.

US: Ultrasound



