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Wheat Growth Monitoring and Yield Estimation based on Multi-Rotor Unmanned Aerial Vehicle

Zhaopeng Fu

Nanjing Agricultural University, 2018801234@njau.edu.cn

Jie Jang

Nanjing Agricultural University, 2019201009@njau.edu.cn

Yang Gao

Nanjing Agricultural University, 2018101164@njau.edu.cn

Brian Krienke

University of Nebraska - Lincoln, krienke.brian@unl.edu

Meng Wang

Nanjing Agricultural University, 2018101016@njau.edu.cn

See next page for additional authors

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Authors

Zhaopeng Fu, Jie Jang, Yang Gao, Brian Krienke, Meng Wang, Kaitai Zhong, Qiang Cao, Yongchao Tian, Yan Zhu, Weixing Cao, and Xiaojun Liu

Article

Wheat Growth Monitoring and Yield Estimation based on Multi-Rotor Unmanned Aerial Vehicle

Zhaopeng Fu ¹, Jie Jiang ¹, Yang Gao ¹, Brian Krienke ², Meng Wang ¹, Kaitai Zhong ¹, Qiang Cao ¹ , Yongchao Tian ¹, Yan Zhu ¹ , Weixing Cao ¹ and Xiaojun Liu ^{1,*} 

¹ National Engineering and Technology Center for Information Agriculture, Key Laboratory for Crop System Analysis and Decision Making, Ministry of Agriculture, Jiangsu Key Laboratory for Information Agriculture, Jiangsu Collaborative Innovation Center for Modern Crop Production, Nanjing Agricultural University, 1 Weigang Road, Nanjing 210095, China; 2018801234@njau.edu.cn (Z.F.); 2019201009@njau.edu.cn (J.J.); 2018101164@njau.edu.cn (Y.G.); 2018101016@njau.edu.cn (M.W.); 2018101007@njau.edu.cn (K.Z.); qiangcao@njau.edu.cn (Q.C.); yctian@njau.edu.cn (Y.T.); yanzhu@njau.edu.cn (Y.Z.); caow@njau.edu.cn (W.C.)

² Department of Agronomy and Horticulture, University of Nebraska-Lincoln, Lincoln, NE 68583, USA; krienke.brian@unl.edu

* Correspondence: liuxj@njau.edu.cn; Tel.: +86-25-8439-6804; Fax: +86-25-8439-6672

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Abstract: Leaf area index (LAI) and leaf dry matter (LDM) are important indices of crop growth. Real-time, nondestructive monitoring of crop growth is instructive for the diagnosis of crop growth and prediction of grain yield. Unmanned aerial vehicle (UAV)-based remote sensing is widely used in precision agriculture due to its unique advantages in flexibility and resolution. This study was carried out on wheat trials treated with different nitrogen levels and seeding densities in three regions of Jiangsu Province in 2018–2019. Canopy spectral images were collected by the UAV equipped with a multi-spectral camera during key wheat growth stages. To verify the results of the UAV images, the LAI, LDM, and yield data were obtained by destructive sampling. We extracted the wheat canopy reflectance and selected the best vegetation index for monitoring growth and predicting yield. Simple linear regression (LR), multiple linear regression (MLR), stepwise multiple linear regression (SMLR), partial least squares regression (PLSR), artificial neural network (ANN), and random forest (RF) modeling methods were used to construct a model for wheat yield estimation. The results show that the multi-spectral camera mounted on the multi-rotor UAV has a broad application prospect in crop growth index monitoring and yield estimation. The vegetation index combined with the red edge band and the near-infrared band was significantly correlated with LAI and LDM. Machine learning methods (i.e., PLSR, ANN, and RF) performed better for predicting wheat yield. The RF model constructed by normalized difference vegetation index (NDVI) at the jointing stage, heading stage, flowering stage, and filling stage was the optimal wheat yield estimation model in this study, with an R^2 of 0.78 and relative root mean square error (RRMSE) of 0.1030. The results provide a theoretical basis for monitoring crop growth with a multi-rotor UAV platform and explore a technical method for improving the precision of yield estimation.

Keywords: UAV multispectral image; leaf area index; leaf dry matter; grain yield; estimation; wheat; machine learning

1. Introduction

Remote sensing platforms for crop growth monitoring and yield estimation mainly include ground, low altitude (unmanned aerial vehicle, UAV), and high altitude (satellite, aerospace). Ground remote sensing, such as analytical spectral devices (ASD), has the characteristics of easy use, multiple bands,

and high resolution, but it is time-consuming, labor-intensive, and has low operation efficiency for monitoring over a wide area. High-altitude remote sensing, such as MODIS and Landsat satellites, is suitable for large-scale monitoring, but has a low resolution, a long return period, and is susceptible to weather [1]. UAVs have developed rapidly since the end of the 20th century. With the improvement of agricultural remote sensing, UAV remote sensing has been quickly applied to practice [2]. Field growth information acquired based on UAV platforms mainly includes vegetation coverage monitoring, growth monitoring, and yield estimation. UAVs used to acquire field information are divided into fixed-wing UAVs and multi-rotor UAVs. Multi-rotor UAV can adjust the flight elevation as needed, making them convenient and flexible to fly, while improving the efficiency and accuracy. To some extent, UAVs have overcome the deficiencies of ground remote sensing and high-altitude remote sensing, providing strong support for crop information monitoring technology of precision agriculture [3].

Varieties of sensors are widely used in crop canopy-scale spectral monitoring by handheld or airborne means. Developed by the National Information Agriculture Engineering Technology Center, the portable multi-spectral growth monitoring diagnostic instrument CGMD302 can quickly measure the spectral reflectivity of a crop canopy at 720 and 810 nm; this instrument has already been applied to monitor the growth of rice, wheat, and other crops [4]. GreenSeeker, a handheld active spectrometer developed by Trimble Navigation Limited, has two fixed bands of red light and near-infrared, which can construct normalized difference vegetation index (NDVI) and ratio Vegetation Index (RVI), and be applied in the growth monitoring of rice, wheat, corn, and other crops [5,6]. These hand-held sensors have fewer wavebands, building a limited spectral index; this makes it difficult to determine fields with partial vegetation index saturation in the late growth period of crops. With the development of UAV technology, an increasing number of sensors have been mounted and applied in UAV remote sensing. For example, Yang et al. [7] adopted rotor-UAVs equipped with a digital camera and multi-spectral camera thermal imager to assist wheat breeding, including the acquisition of crop lodging area, leaf area index (LAI), and canopy temperature in a plot. Tian et al. [8] used the imaging spectral sensor mounted on an eight-rotor UAV to obtain the hyperspectral image data of farmland for an inversion estimation of cotton LAI. Zhao et al. [9] used an eight-rotor UAV mounted imaging hyperspectral sensor to obtain images of key growth periods of soybean and accurately estimate soybean yield. Many other studies have been conducted on crop growth monitoring and yield estimation based on UAV remote sensing [10–12]. However, due to the limitations of the UAV platform and sensor technology, the pre-processing of remote sensing images is not yet straightforward, leaving room for improvement of the accuracy of monitoring and estimation models.

LAI and leaf dry matter (LDM) are important physiological parameters to describe the growth model of crops, as well as important indexes to reflect the growth status of crops [13]. Many studies have been conducted on the spectral data monitoring the growth indicators, such as LAI, based on UAV platforms. For example, Córcoles et al. [14] analyzed the correlation between LAI and canopy coverage with three models based on the quadrotor UAV platform equipped with a digital camera. Gao et al. [15] used a multi-rotor UAV with a mounted imaging spectral sensor to obtain spectral data of wheat at various growth stages and analyzed its correlation with LAI. Aasen et al. [16] used a UAV to carry hyperspectral cameras to test different varieties to prove the feasibility of LAI monitoring in the context of precision agriculture.

Rapid and non-destructive estimation of crop yield is an important part of agricultural remote sensing. Remote sensing technology has been widely used in crop growth monitoring and yield estimation. The development of UAV remote sensing provides a new means [17,18]. Zhu et al. [19] used a UAV remote sensing platform equipped with a multi-spectral camera to obtain the image data of wheat at the jointing stage, heading stage, and filling stage, and constructed nine linear models of different vegetation indexes and measured yields using the least square method. Gong et al. [20] used a multi-spectral camera mounted on a multi-rotor UAV to obtain images of the early flowering period of rapeseed and used a normalized vegetation index to predict yield. Yu et al. [21] developed a dual-camera high-throughput phenotype (HTP) platform on a UAV that collected multispectral

data from multiple growth periods to improve the accuracy of soybean yield estimates. At present, the research process of crop canopy spectral image data obtained by using UAV platform equipped with multiple sensors for crop yield estimation has been preliminarily defined, so more studies focus on the selection of the vegetation index and the improvement of the precision of the yield estimation model.

In this study, a multi-rotor UAV platform equipped with a multi-spectral camera was used to obtain canopy spectral data of wheat in multiple growth periods, and a variety of parametric or non-parametric modeling methods were integrated to monitor the main growth indicators (LAI and LDM) and predict grain yield. Therefore, the objectives of this study were: (1) to evaluate the potential of multi-spectral information obtained from a multi-rotor UAV for crop monitoring; (2) to invert the LAI and LDM of a crop and predict the yield by integrating spectral information with agronomic parameters; and (3) to compare and evaluate the estimation accuracy of various parametric regression methods and non-parametric regression methods. The results from this study will provide a reference for further research on UAV monitoring applied to wheat.

2. Materials and Methods

2.1. Experimental Design

In this study, field experiments were carried out in two consecutive years (2018–2019) at the experimental station located in Suining (117°54'E, 33°57'N), Xinghua (119°53'E, 33°05'N), and Kunshan (120°53'E, 31°29'N) (Figure 1), Jiangsu Province, China. The experimental area is located in the Yangtze River Reaches plain, with an average altitude of less than 50 m. Winter wheat is grown at one harvest per year within rice-wheat rotation production system. We selected Yangmai-23 to sow in Xinghua, Yangmai-15 in Kunshan and Xumai-33 in Suining. These wheat varieties are suitable for local growing environment. The treatments involved different N rates and seeding densities. Specific details of the treatments are provided in Table 1. N fertilizer (urea) containing 46% N was applied before sowing and at the stem elongation stage at rate of 50% and 50% of total N.

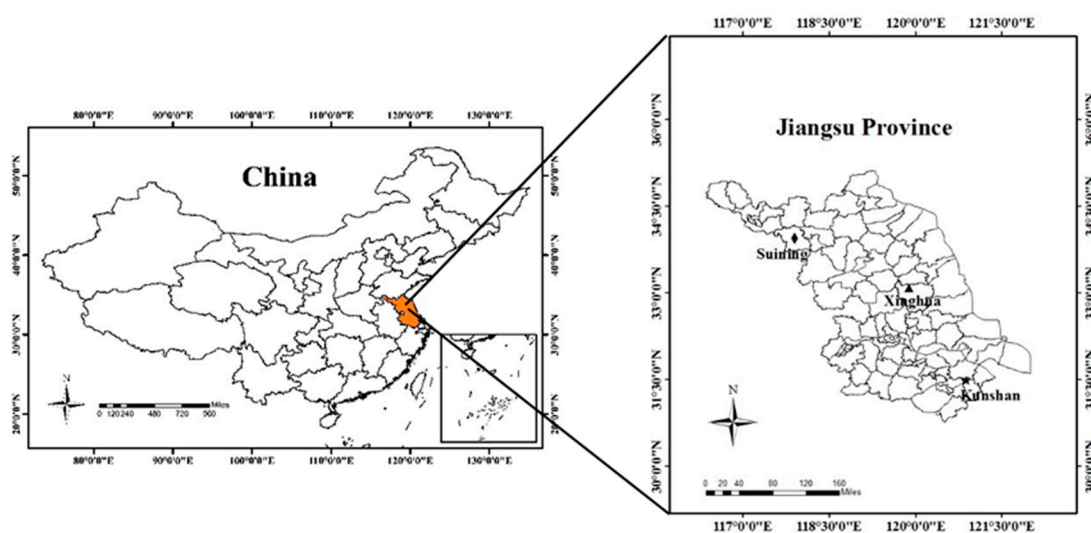


Figure 1. A map illustrating the study site. Wheat experiments were carried out at the Suining, Xinghua, and Kunshan Experimental Stations in Jiangsu Province, China in 2018–2019.

Table 1. Basic information about experimental design and data acquisition.

Experiment and Place	Cultivars and Season	Nitrogen Rates (kg ha ⁻¹)	Seeding Densities (Million Seedlings ha ⁻¹)	Plot Size	Sampling Stages
Exp.1	Yangmai-23	N0 (0)	D1 (1.2)	30 m ²	Tillering (6 March 2019)
Xinghua	2018–2019	N1 (180)	D2 (1.8)	5 m × 6 m	Jointing (12 March 2019)
		N2 (240)	D3 (2.4)	90 plots	Booting (4 April 2019)
		N3 (300)			Flowering (20 Apr 2019)
					Filling (9 May 2019)
Exp.2	Yangmai-15	N0 (0)	D1 (1.2)	24.5 m ²	Tillering (4 March 2019)
Kunshan	2018–2019	N1 (180)	D2 (1.8)	5.5 m × 4.5 m	Jointing (14 March 2019)
		N2 (270)	D3 (2.4)	84 plots	Booting (30 March 2019)
					Flowering (17 April 2019)
					Filling (5 May 2019)
Exp.3	Xumai-33	N0 (0)	D1 (1.5)	20 m ²	Tillering (7 March 2019)
Suining	2018–2019	N1 (180)	D2 (2.5)	4 m × 5 m	Jointing (13 March 2019)
		N2 (240)	D3 (3.5)	108 plots	Booting (8 April 2019)
		N3 (300)			Flowering (24 April 2019)
					Filling (15 May 2019)

2.2. Field Data Acquisition

All field data acquisition was synchronized with sampling dates (Table 1).

To measure the LAI, 30 individual wheat plants were selected from each plot and separated by organs (stem, leaf, and spike). The leaf area was measured using a portable li-3000c leaf area meter (Li-Cor., Lincoln, NE, USA), and the LAI of the population was measured by the number of plants and tillers per square meter.

To measure the LDM, 30 individual wheat plants were selected from each plot and separated by organs (stem, leaf, and spike). The green leaves were first placed in an oven at 105 °C for 30 min, and then dried at 80 °C for more than 48 h until a constant weight was obtained. Finally, dry matter was weighed.

To measure the grain yield, at the maturity stage, 1 m² plants were taken from the unsampled areas of each plot to calculate the number of panicles per unit land area, and 30 plants were taken for seed testing indoors to calculate the number of grains per spike, thousand grain weight, and percentage of seed set. In each plot, plants in an area of 1 m² were harvested twice for threshing and measuring yield.

2.3. Acquisition of UAV Images

This experiment used a six-rotor UAV (DJI M600Pro, Shenzhen, CHN) with a multi-spectral camera (Airphen, Hiphen, FR) to obtain image data at an altitude of 50 m above the wheat canopy (spatial resolution was 4.7 cm, focal length was 8 mm, heading overlap was 85%, sideways overlap was 90%, flight speed was 2 m/s). The acquisition of UAV images was synchronized with field sampling time (Table 1). We used the software DJI GS PRO (<https://www.dji.com/cn/ground-station-pro/>) to pre-plan the route and monitor the UAV's flight. The multi-spectral camera was composed of six channels with a resolution of 1280 × 960 and wavelengths of 450, 530, 675, 730, and 850 nm. Radiometric correction images are taken of standard reflectors on the ground before each flight. The camera is set to take photos automatically, taking photos at an interval of a second, and the image is saved as TIFF format. The flights were conducted in clear, cloudless and calm weather between 11 am and 1 pm.

2.4. Processing of UAV Images

When the UAV is equipped with multi-spectral sensors for crop monitoring, it is vulnerable to adverse weather factors, such as cloud cover, wind, and rain, which will result in the reduction of image data quality and increase the difficulty of later data analysis. Therefore, the preprocessing of

UAV images is very important for formal processing and analysis. Common UAV image preprocessing includes radiometric correction, image mosaic, geometric correction, and image cropping.

The experiment adopted the method of calibration boards for radiometric calibration to convert the image value into the image reflectivity through the reflectivity measured by the ground target; this reflected the surface reflectivity in real time [22]. The calibration board was obtained from Hiphen-Plant (<http://www.hiphen-plant.com/>), which has different reflectivity for different bands. The camera plug-in used was Agisoft Photoscan version 1.4.5 software (<https://www.agisoft.com/>), which completes the radiometric calibration of multi-spectral images. This step also includes the vignetting correction process, which can effectively eliminate the vignetting phenomenon caused by strong illumination conditions. Since the built-in plug-in of the multi-spectral camera was installed with the help of Agisoft Photoscan software, the image stitching process was also carried out using this software. First, the aerial image folder was imported into Agisoft Photoscan software. Redundant images during take-off and landing were deleted to reduce the processing capacity. The images were then graphically aligned, dense point clouds were built, and mesh and texture were generated. Finally, an orthographic high-resolution canopy image of the experimental field was obtained. To ensure the accuracy of the image, a method based on ground control point (GCP) was adopted for geometric correction. Customized standard plates were placed around the plot as the GCP (Figure 2). A high-precision GPS in the center of the GCP was obtained by real time kinematic (RTK). According to different field size and shape, we arranged different amount of GCP. 18 GCPs were arranged in Xinghua and Kunshan, and 16 GCPs were arranged in Suining. After the above pretreatment, the whole canopy multi-spectral image of the experimental field was obtained. The final precision of the orthomosaic image is 0.3 cm. The crop tool in ENVI software was used in the experiment to retain only part of the test area in the image to eliminate the influence of unnecessary roads and other features around the field. The region of interest (ROI) was manually circled in the plot (Figure 2) and the reflectivity data in the canopy spectral image was accurately extracted.

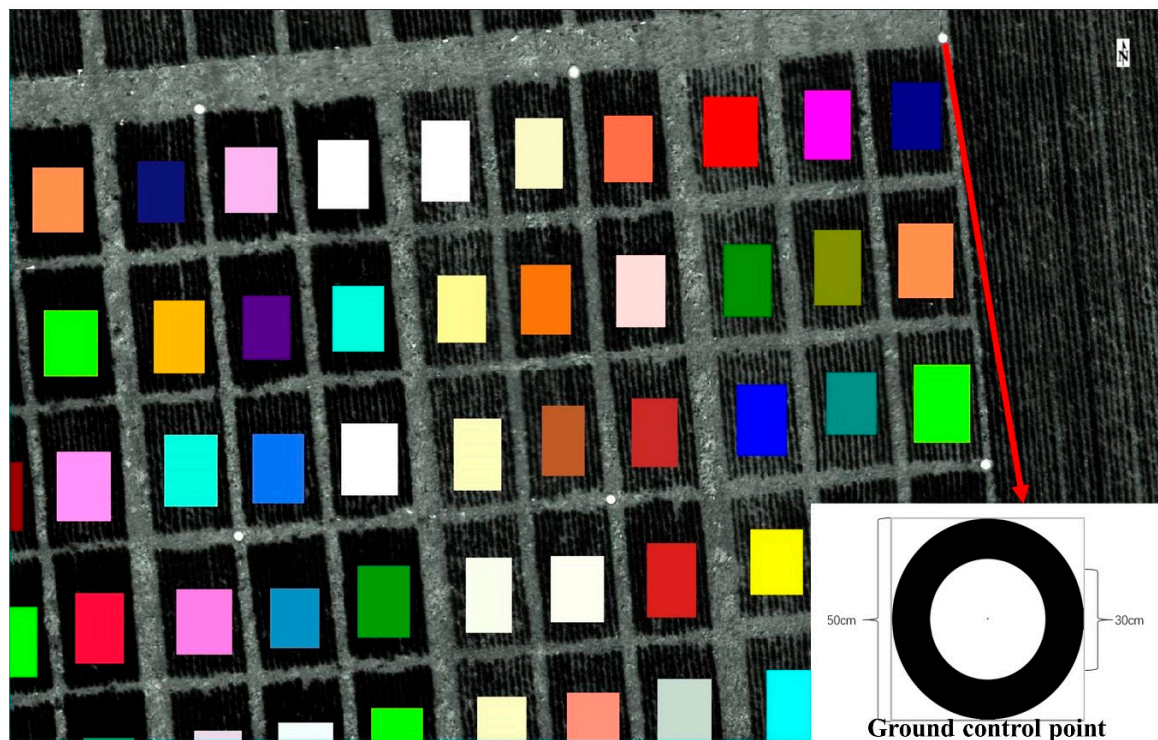


Figure 2. Region of interest and one of the ground control points.

2.5. Selection of Vegetation Index

After each flight, six multi-spectral image sets with wavelengths of 450, 530, 570, 675, 730, and 850 nm were generated. The six multispectral reflectivities in each sampling period were generated separately by the six multispectral image sets. The experiment extracted reflectivities of six bands from multi-spectral image and fitted vegetation index. The pre-processed reflectivity image was obtained. The reflectivity of each plot was obtained by averaging the total reflectivity of each plot, and then commonly used vegetation indices as described in Table 2 were fitted.

Table 2. Selected vegetation used for leaf area index, leaf dry matter, and yield estimation.

Vegetation Index	Formulation	Reference
GNDVI	$(\text{NIR} - \text{G})/(\text{NIR} + \text{G})$	[23]
NDVI	$(\text{NIR} - \text{R})/(\text{NIR} + \text{R})$	[24]
NDRE	$(\text{NIR} - \text{RE})/(\text{NIR} + \text{RE})$	[25]
RVI	NIR/R	[26]
CIRE	$(\text{NIR}/\text{RE}) - 1$	[27]
OSAVI	$(\text{NIR} - \text{R})/(\text{NIR} + \text{R} + 0.16)$	[28]
SAVI	$(1 + L) * (\text{NIR} - \text{R})/(\text{NIR} + \text{R} + L)$	[29]
CCCI	$(\text{NDRE} - \text{NDRE}_{\min})/(\text{NDRE}_{\max} - \text{NDRE}_{\min})$	[30]
RESAVI	$1.5 * (\text{NIR} - \text{RE})/(\text{NIR} + \text{RE} + 0.5)$	[31]

2.6. Modeling Methods and Validation

Quantitative remote sensing is to link agricultural remote sensing information with agricultural target parameters through modeling, which can be divided into three categories: physical model, statistical model, and semi-empirical model [32]. The statistical model is to make empirical statistical descriptions or conduct correlation analyses of a series of observation data and establish a regression model between remote sensing parameters and agricultural observation data. In addition to the commonly used parametric regression methods, various non-parametric regressions have become popular, including stepwise multiple regression (SMR), partial least squares regression (PLSR), artificial neural network (ANN), and support vector machine (SVM).

In this paper, multivariate modeling was used to explore the method of wheat yield estimation. In order to improve its estimation accuracy, we selected different modeling datasets from four perspectives. Six modeling methods including linear regression (LR), multiple linear regression (MLR), stepwise multiple linear regression (SMLR), partial least-squares regression (PLSR), artificial neural network (ANN), and random forest (RF). These modeling methods were used to explore the optimal wheat yield estimation model.

In this study, LR was used to construct the yield estimation model of vegetation indices and test the estimation accuracy. This was calculated as follows:

$$Y = kX + b \quad (1)$$

Y is the yield or predicted value (dependent variable) and X is the vegetation index or measured value (independent variable).

MLR is a regression analysis with two or more independent variables. Growth is often related to many factors, so MLR has more practical significance than LR. Based on the existing sample data, this study built an estimation model of MLR. This was calculated as follows:

$$Y = k_1X_1 + k_2X_2 + k_3X_3 + \dots + k_nX_n + b \quad (2)$$

where Y is yield, $X_1 \sim X_n$ is vegetation indices, and $k_1 \sim k_n$ is the coefficient of the corresponding independent variable.

In the MLR, the multiple correlation of variables will affect the estimation of parameters, leading to the decrease of the estimation accuracy. Therefore, this study also provided a solution for SMLR and PLSR to eliminate collinearity [33]. Typically, SMLR is used to eliminate unnecessary factors by stepwise regression, select significant factors, and obtain the optimal regression model [34]. Firstly, the variable with the maximum sum of squares of regression was selected from the optional variables, and then the variables were selected from the remaining optional variables to form the binary regression equation with the selected variables. This cycle was repeated so that only important variables were retained in the regression equation. The effect of collinearity could be reduced at this step.

PLSR can combine the basic functions of MLR, canonical correlation analysis, and principal component analysis. It can avoid non-normal distribution of data, eliminate multiple linearity between independent variables, and maintain the relationship between independent variables and dependent variables [35,36].

ANN simulates the biological neural network [37], including input layer, hidden layer and output layer [38]. Each layer can be regarded as composed of several logistic regression models, which receive information input from the previous layer and output the estimation results of the model to the next layer. Activation functions exist between the hidden layer and the output layer, mainly including the S function (sigmoid) and the double S function, which was adopted in this study [39]. ANN has strong fault-tolerance and adaptive learning ability, which is very suitable for modeling complex, non-linear systems and can be used for large-scale information processing.

RF is a learning method that integrates multiple decision trees, efficiently processing large-scale information with the ability to obtain a good fit and reduce noise [38,40]. RF uses bootstrap re-sampling to extract some samples from the original sample (N), sampling N times to form a training set, and making an estimation with the unsampled samples. According to the estimation of multiple decision trees, the final estimation result is obtained by voting [41]. In the model, NTREE and MTREE are the main parameter settings. NTREE specifies the number of decision trees contained in the RF, and MTREE specifies the number of variables in the node for the binary tree [38]. NTREE was set to 1000 and MTREE to two after the tuning in this study.

Based on the above experimental design, data acquisition and analysis, a flowchart (Figure 3) was made to better explain the research procedure.

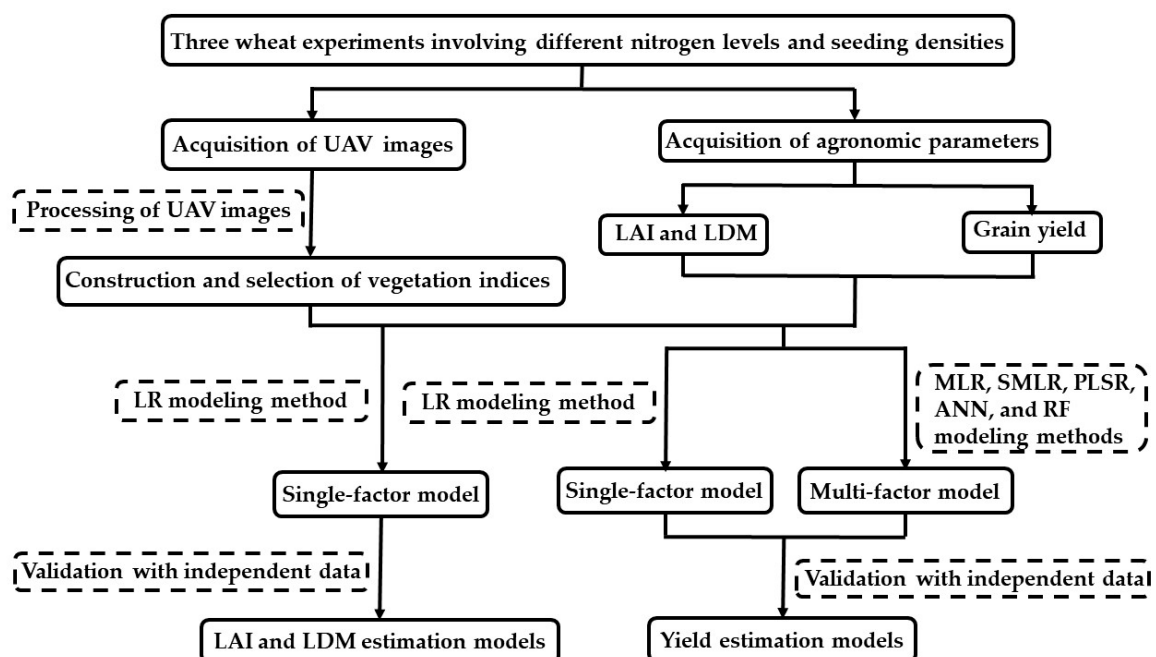


Figure 3. The flowchart of this study.

We introduced standard deviation (SD) and coefficient of variation (C.V.) to measure the dispersion degree of the total data. The greater the C.V., the more possibilities the total data contain. SD and C.V. were calculated as follows:

$$SD = \sqrt{\frac{1}{k-1} \sum_{i=1}^k (x_i - \bar{x})^2} \quad (3)$$

$$C.V. = \frac{SD}{Mean} \quad (4)$$

where \bar{x} is the mean of total samples and k is the number of samples.

UAV imaging data and agronomic parameters obtained from the experiment were used to establish the wheat growth index and yield estimation model. We chose two indexes, R^2 and relative root mean square error (RRMSE), to evaluate the performance of the model. Specifically, R^2 and RRMSE were calculated as follows:

$$R^2 = \frac{\sum_{i=1}^k (m - \bar{m})^2 (n - \bar{n})^2}{\sum_{i=1}^k (m - \bar{m})^2 \sum_{i=1}^k (n - \bar{n})^2} \quad (5)$$

$$RRMSE = \sqrt{\frac{1}{k} \sum_{i=1}^k (m - n)^2 / \bar{n}} \quad (6)$$

where m and n are estimated values and measured values, respectively, \bar{m} and \bar{n} are the average estimated values and measured values, respectively, and k is the number of samples. The method used to test the model in this study was independent data verification.

3. Results

3.1. Variations of Wheat Growth Indices and Yield

The experimental data is based on the whole, and different treatments (nitrogen levels and seeding densities) do not affect the results. In addition, different treatments can make the modeling data contain more possibilities, thus improving the universality of the model. Due to the differences between nitrogen levels and seeding densities, variations in the data were observed (Table 3). LDM in the dataset used for modeling had the largest variation, and its C.V. was 42.42%. LAI and yield had the next greatest variation, with variation coefficients of 37.81% and 30.10%, respectively. The dataset used for validation was similar to the dataset used for modeling, with the maximum variation of LDM, followed by LAI and yield. The C.V. for LDM, LAI, and yield was 45.32%, 40.31%, and 21.72%, respectively. LAI (0.6765–5.3046), LDM (2.2429 t/ha–23.4500 t/ha), and yield (1.3000 t/ha–8.5102 t/ha) showed variation, which covers most possible situations. Therefore, the dataset can support the development of reliable wheat growth index monitoring and yield estimation model.

Table 3. Descriptive statistics of wheat leaf area index (LAI), leaf dry matter (LDM), and yield of different cultivars and nitrogen levels.

Indicators	Sample Number	Min	Max	Mean	SD	C.V. (%)
Modeled dataset						
LAI	210	0.7524	4.9392	2.5707	0.9721	37.81
LDM (t/ha)	210	2.6224	23.4500	11.0954	4.7065	42.42
Yield (t/ha)	72	1.3000	8.5000	6.0011	1.8065	30.10
Validated dataset						
LAI	90	0.6765	5.3046	2.6112	1.0527	40.31
LDM (t/ha)	90	2.2429	21.8400	11.1606	5.0583	45.32
Yield (t/ha)	30	3.0920	8.5102	6.4665	1.4044	21.72

Note: Min is the minimum, Max is the maximum, Mean is the average value, SD is the standard deviation, and C.V. is the coefficient of variation.

3.2. LAI Estimation based on UAV Images

The regression relationship between vegetation indices calculated by multi-spectral data and LAI is shown in Figure 4. Different vegetation indices had different monitoring accuracy ($R^2 = 0.62\text{--}0.74$). The combination of the red band and the near-infrared band resulted in the best vegetation index, RESAVI, with its R^2 reaching 0.74.

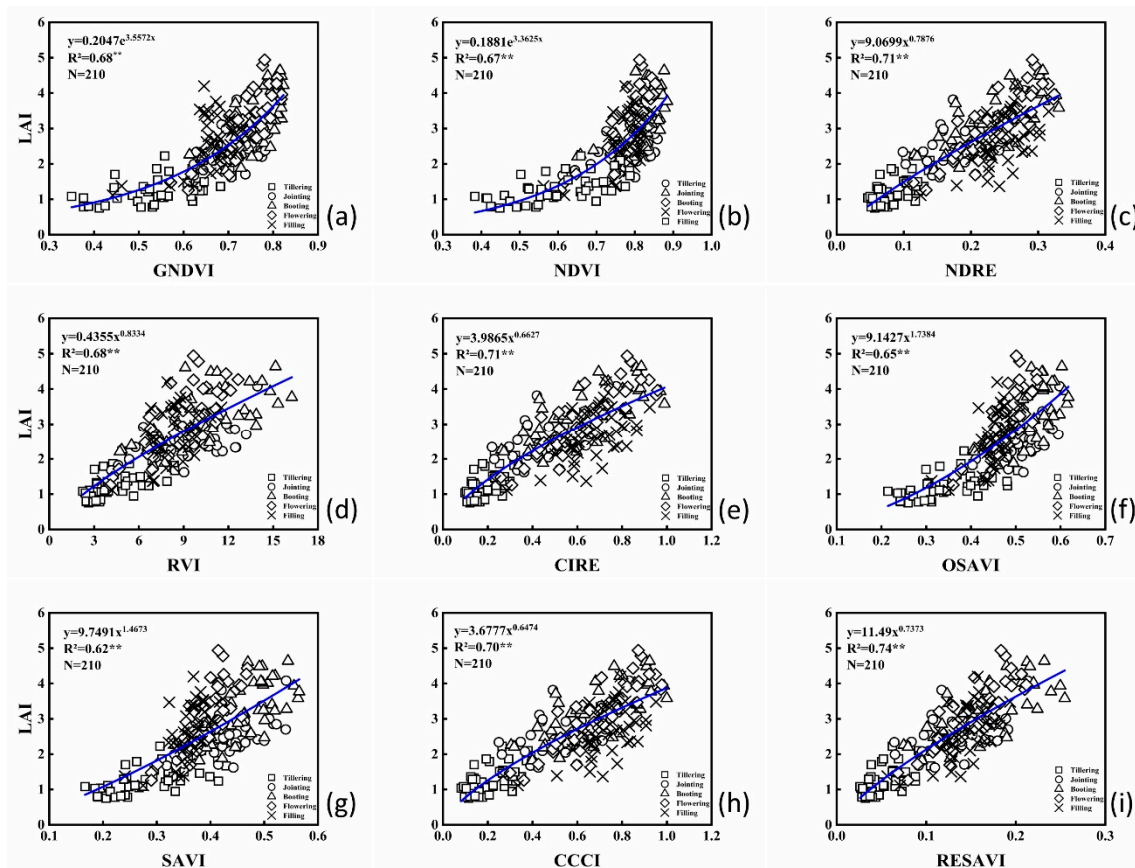


Figure 4. Leaf area index plotted against vegetation indices for the whole growth season of wheat: (a) GNDVI; (b) NDVI; (c) NDRE; (d) RVI; (e) CIRE; (f) OSAVI; (g) SAVI; (h) CCCI; (i) RESAVI.

According to the results of the model validation (Figure 5), the accuracy of different vegetation indexes is acceptable ($R^2 = 0.60\text{--}0.76$). RESAVI had the best accuracy for monitoring and estimation, with its R^2 reaching 0.76 and RRMSE reaching 0.1990. NDRE, CIRE, and CCCI also performed well, and their verified R^2 were all 0.74 (RRMSE = 0.2096–0.2126), indicating with good estimation accuracy.

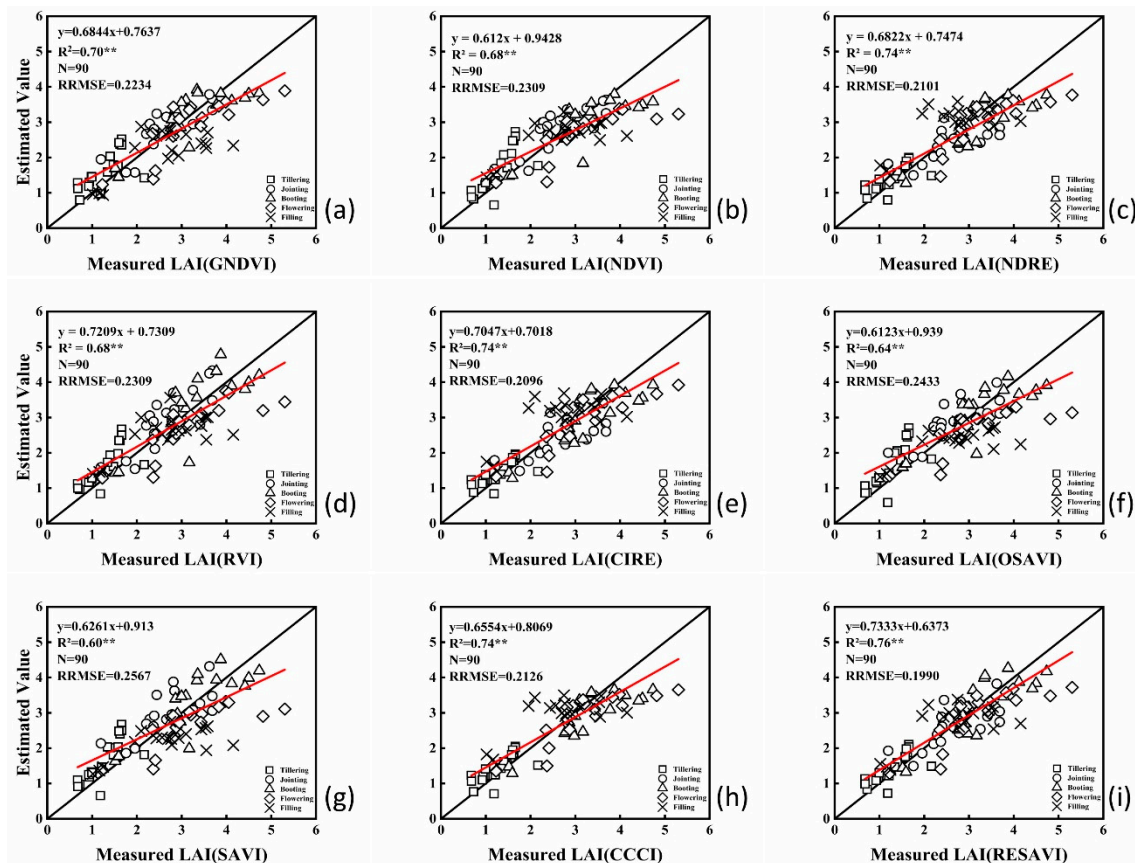


Figure 5. Validation of leaf area index (LAI) estimation models for the entire growth season of wheat: (a) GNDVI; (b) NDVI; (c) NDRE; (d) RVI; (e) CIRE; (f) OSAVI; (g) SAVI; (h) CCCI; (i) RESAVI.

Overall, the model with a better monitoring effect also had better estimation accuracy (such as NDRE). The model with a poor monitoring effect also had low accuracy in model validation (such as SAVI). The model constructed by RESAVI for LAI estimation was the optimal model, explaining 74% of the variability and had an R^2 of 0.76 and RRMSE of 0.1990.

3.3. LDM Estimation based on UAV Images

Regression relationships between vegetation indices calculated by multi-spectral data and LDM are shown in Figure 6. The accuracy of LDM monitoring constructed using different vegetation indices varies ($R^2 = 0.46$ – 0.74). The vegetation indices (NDRE, CIRE, CCCI, and RESAVI) of the red edge band and near-infrared band showed better performance ($R^2 \geq 0.7$). The effect of SAVI monitoring was poor, explaining a variation of 46%. The results were similar to those of LAI. The model constructed with CIRE was optimal, explaining 75% of the variability.

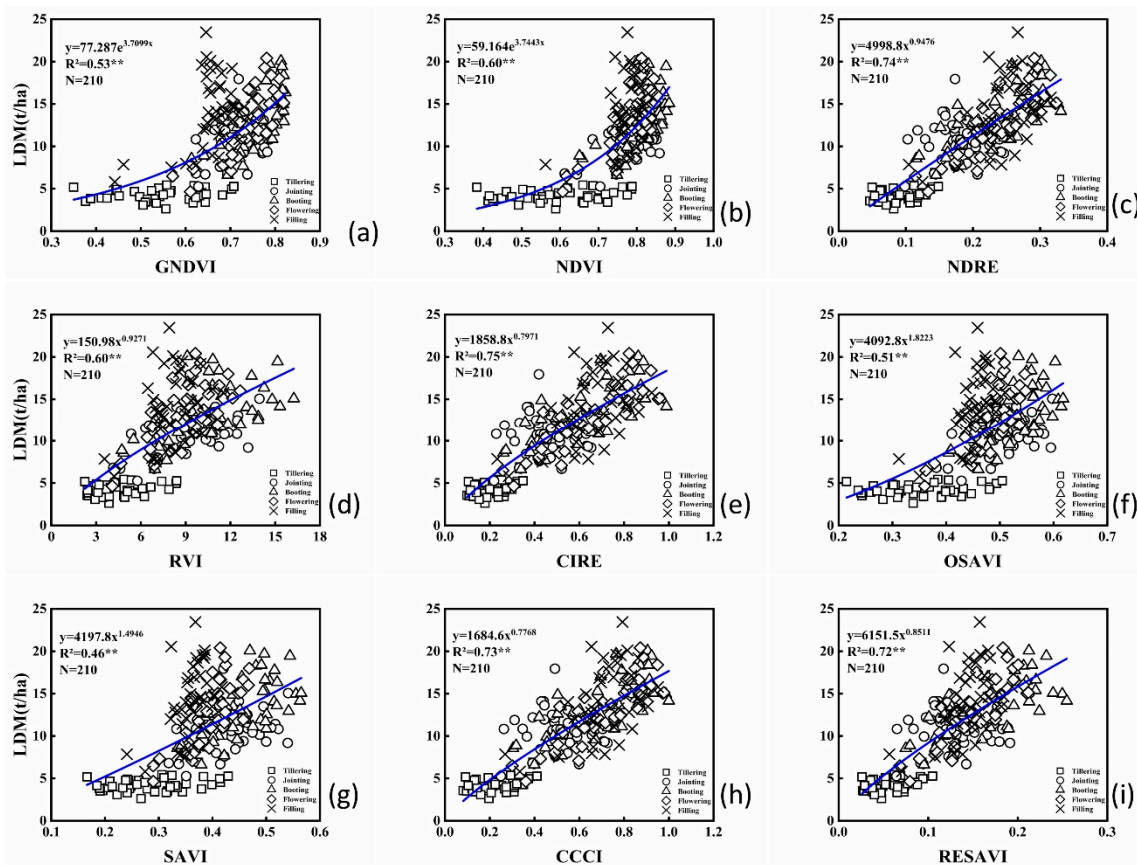


Figure 6. Leaf dry matter ($t\ ha^{-1}$) plotted against vegetation indices for the whole season: (a) GNDVI; (b) NDVI; (c) NDRE; (d) RVI; (e) CIRE; (f) OSAVI; (g) SAVI; (h) CCCI; (i) RESAVI.

The model built by each vegetation indices verified that R^2 ranged from 0.43 to 0.74 (Figure 7). The model with a higher R^2 verification had a lower RRMSE, meaning it had better estimation accuracy. Models constructed by NDRE, CIRE, and CCCI fit the data well and had an R^2 of 0.74, 0.73, and 0.74, respectively. As above, SAVI estimated the data poorly ($R^2 = 0.43$). NDRE was the optimal estimation model, explaining 74% of variability, with RRMSE of 0.2337.

Combined with the modeling and verification results, the models with better estimation results were all constructed with vegetation indices that utilized a combination of red edge band and near-infrared band images. NDRE had the largest verified R^2 , so it was the optimal wheat LDM estimation model.

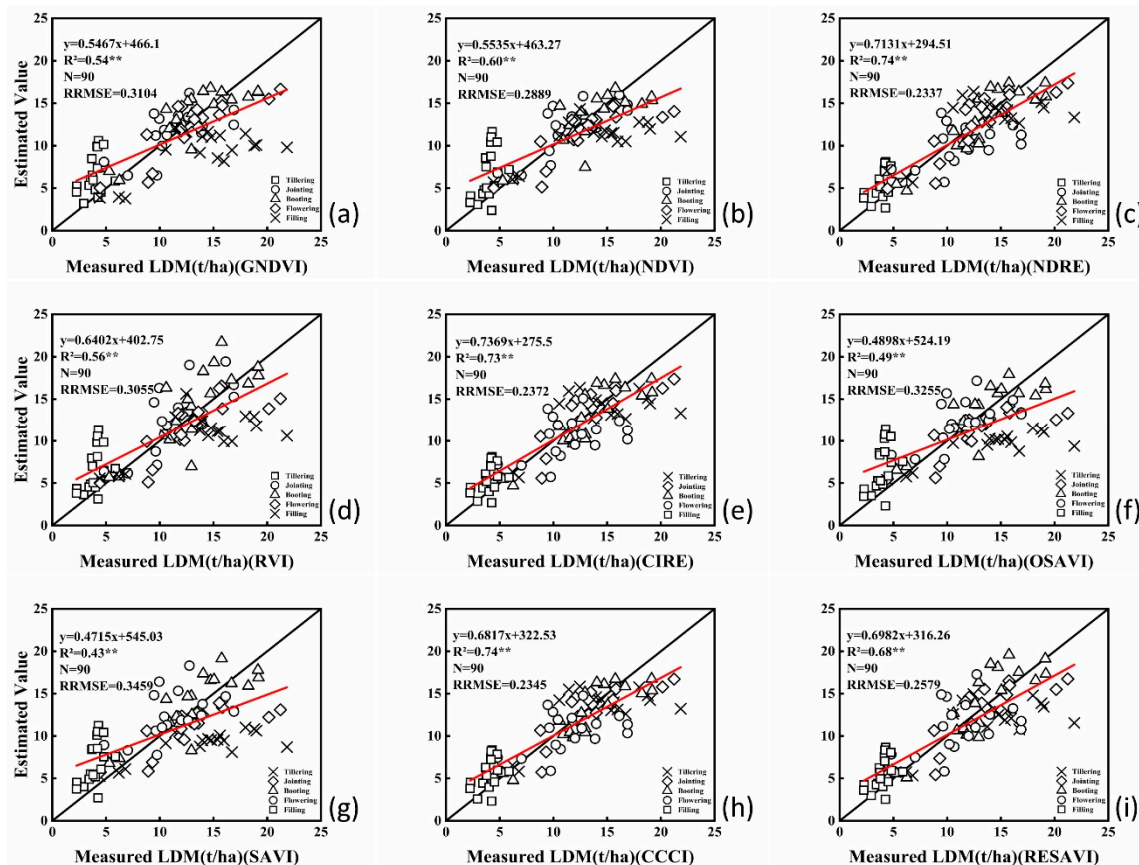


Figure 7. Validation of leaf dry matter (LDM) estimation models for the entire growth season of wheat: (a) GNDVI; (b) NDVI; (c) NDRE; (d) RVI; (e) CIRE; (f) OSAVI; (g) SAVI; (h) CCCI; (i) RESAVI.

3.4. Yield Estimation based on UAV Images

In this study, a multi-spectral camera mounted on a UAV was used to obtain image data of the wheat canopy at key growth stages. We extracted the reflectivities from the image data and calculated the required vegetation indices (Table 4). The yield predicted by the vegetation index at the tillering stage was poor. The determination coefficient between the vegetation index and yield at the jointing stage ranged from 0.3858 to 0.6328, among which NDVI was the best index, explaining a variation of 63.28%. NDVI at the booting stage ($R^2 = 0.5949$ – 0.7617) also had the best performance ($R^2 = 0.7617$). NDRE at the flowering stage ($R^2 = 0.6910$ – 0.7838) had the best performance ($R^2 = 0.7838$). CCCI at the filling stage ($R^2 = 0.4057$ – 0.6806) showed the best performance, with $R^2 = 0.6806$. In general, the vegetation indices of the booting stage, flowering stage, and filling stage were well fitted to the data. The yield estimation model of NDRE showed the best results.

Table 4. Determination coefficients between grain yield and different vegetation indices.

Vegetation Index	Tillering Stage	Jointing Stage	Booting Stage	Flowering Stage	Filling Stage
GNDVI (850,570)	0.1139 **	0.5378 **	0.7199 **	0.7422 **	0.4057 **
NDVI (850,675)	0.1491 **	0.6328 **	0.7617 **	0.7661 **	0.5692 **
NDRE (850,730)	0.1757 **	0.4234 **	0.6841 **	0.7838 **	0.6804 **
RVI (850,675)	0.1433 **	0.4073 **	0.5949 **	0.6910 **	0.5394 **
CIRE (850,730)	0.1768 **	0.3858 **	0.6251 **	0.7455 **	0.6614 **
OSAVI (850,675)	0.1494 **	0.5770 **	0.7339 **	0.7698 **	0.5384 **
SAVI (850,675)	0.1486 **	0.5284 **	0.6779 **	0.7398 **	0.5045 **
CCCI (850,730)	0.1757 **	0.4234 **	0.6841 **	0.7837 **	0.6806 **
RESAVI (850,730)	0.1704 **	0.3882 **	0.6279 **	0.7527 **	0.6622 **

Note: ** indicates correlation significant at 0.01 level, the bold indicates the best correlation.

Grain yield is affected by multiple factors. Therefore, in addition to the traditional single-factor models, we also constructed multi-factor models to increase the accuracy and stability of the model. Using traditional linear methods may generate problems, such as collinearity, when constructing multi-factor models; therefore, we introduced several commonly used machine-learning methods for yield estimation. Table 4 shows the four methods of acquiring the modeling dataset, and adopt LR, MLR, SMLR, PLSR, ANN and RF for modeling and estimating. The relationships between the measured yield and estimated yield of the different models are shown in Table 5.

Table 5. Validation of yield estimation models with simple linear regression (LR), multiple linear regression (MLR), stepwise multiple linear regression (SMLR), artificial neural network (ANN), and random forest (RF).

Vegetation Indices for Modeling	LR	MLR	SMLR	PLSR	ANN	RF
NDRE (Flowering)	0.7000 ^a 0.1307 ^b	\	\	\	\	\
NDVI (Flowering), NDRE (Flowering), OSAVI (Flowering), CCCI (Flowering)	\	0.7490 ^a 0.1142 ^b	0.7490 ^a 0.1142 ^b	0.7542 ^a 0.1353 ^b	0.7701 ^a 0.1126 ^b	0.7606 ^a 0.1149 ^b
NDVI (Jointing), NDVI (Booting), NDVI (Flowering), NDVI (Filling)	\	0.7186 ^a 0.1163 ^b	0.7186 ^a 0.1163 ^b	0.7571 ^a 0.1343 ^b	0.7454 ^a 0.1100 ^b	0.7800 ^a 0.1030 ^b
NDVI (Jointing), NDVI (Booting), NDRE (Flowering), CCCI (Filling)	\	0.7572 ^a 0.1113 ^b	0.7308 ^a 0.1197 ^b	0.7667 ^a 0.1353 ^b	0.7582 ^a 0.1132 ^b	0.7602 ^a 0.1165 ^b

Note: ^a indicates the value of determination coefficient R^2 , ^b indicates the value of relative root mean-squared error (RRMSE). NDVI (Jointing) means normalized difference vegetation at the jointing stage, NDVI (Booting) means normalized difference vegetation at the booting stage, NDVI (Flowering) means normalized difference vegetation at the flowering stage, NDVI (Filling) means normalized difference vegetation at the filling stage, NDRE (Flowering) means normalized difference red edge at the flowering stage, OSAVI (Flowering) means optimized soil adjusted vegetation index at the flowering stage, CCCI (Flowering) means canopy chlorophyll content index at the flowering stage, and CCCI (Filling) means canopy chlorophyll content index at the filling stage.

The yield estimation model established by NDRE at the flowering stage explained 70% of the variation (RRMSE = 0.1307), meaning that it performed well (Table 5). Table 5 shows that the flowering stage was the best growth stage to build the yield estimation model. Therefore, NDVI ($R^2 = 0.7661$), NDRE ($R^2 = 0.7838$), OSAVI ($R^2 = 0.7698$), and CCCI ($R^2 = 0.7837$), which were the single-factor models with the highest R^2 in Table 4, were adopted to build the multi-factor estimation model for wheat yield (Table 5). This experiment randomly selected 72 datasets for modeling and 30 datasets for verification. Five methods including MLR, SMLR, PLSR, ANN, and RF were used to build the wheat yield estimation model. As shown in Table 5, PLSR, ANN, and RF performed better. The validation results of MLR and SMLR were similar (the factors of NDVI were excluded from SMLR modeling). The RRMSE of these five methods was maintained at a reasonable range of 0.1126–0.1353. In the yield estimation model, ANN was the optimal yield estimation model, explaining a variability of 77.01% with an RRMSE of 0.1126.

The overall performance of NDVI was the best; therefore, NDVI at jointing stage ($R^2 = 0.6328$), booting stage ($R^2 = 0.7617$), flowering stage ($R^2 = 0.7661$), and filling stage ($R^2 = 0.5692$) were used to construct the wheat yield estimation model. Modeling verification was carried out based on the same dataset mentioned above, and five modeling methods including MLR, SMLR, PLSR, ANN, and RF were also adopted for the comparative analysis (Table 5). The estimation accuracy of MLR and SMLR was similar to each other (factors were not excluded from SMLR modeling), and the results were similar to the multiple vegetation indices at a single growth stage. PLSR, ANN, and RF performed better than MLR and SMLR ($R^2 = 0.7454$ – 0.78). The RRMSE of different methods was maintained at a reasonable range of 0.1030–0.1343. RF was the optimal yield estimation model in this method, which explained 78% of the variation and the RRMSE was 0.1030.

As Table 5 shows, NDVI had the best performance at the jointing stage, explaining a variability of 63.28%. NDVI showed the best performance at the booting stage, explaining 76.17% of variability.

NDRE showed the best performance at flowering stage, explaining a variability of 78.38%. CCCI was the best vegetation index at the filling stage, explaining the variability of 68.06%. In terms of multiple vegetation indices at multiple growth stages, we chose NDVI at the jointing stage, NDVI at the booting stage, NDRE at the flowering stage, and CCCI at the filling stage to build an overall model of wheat yield estimation. Modeling validation was based on the same dataset and modeling method mentioned above (Table 5). The estimation accuracy of SMLR was quite different from that of MLR (NDVI at the booting stage and CCCI at the filling stage were excluded during SMLR modeling). PLSR, ANN, and RF still performed well, explaining a variation of 75.82% to 76.67%. The PLSR was the optimal yield estimation model because it had the largest R^2 in this method.

4. Discussion

Plants have spectral characteristics and can absorb, reflect, and radiate different spectra. UAV remote sensing technology used for agriculture can detect these spectral characteristics of plants. Light of different wavelengths has different effects on plant growth [42]. Image sensors mounted on UAVs are used to collect images of crops in different bands and extract different features [43,44]. The multi-spectral sensor we used (i.e., Airphen) is an imaging sensor. Unlike non-imaging sensors, such as GreenSeeker or RapidSCAN, Airphen collects image data from more spectral bands (6 bands) with a good spatial resolution (4.7 cm). Compared with hyperspectral sensors, Airphen is easier to operate and more convenient for data processing. In addition, Airphen is light enough to fit a UAV. We used a customized gimbal to stably connect the sensor to the multi-rotor UAV so that it can the UAV can fly more steadily and take clearer images. For small-scale crop monitoring tasks, multi-rotor UAVs have the advantages of low take-off and landing requirements, low cost, high flexibility, and high resolution compared with fixed-wing UAVs. Unlike high-altitude (satellite, aerospace) remote sensing, UAV remote sensing is convenient and can adjust through time and space as needed. In crop-scale monitoring, ground remote sensing is time-consuming and laborious with low efficiency. A comparison of different sensors and remote sensing platforms is shown in Table 6.

Table 6. Parameters comparison for different sensors and platforms.

Name	Category	Content	Example	Parameters contrast	Reference
Sensors	Imaging sensor	Hyperspectral camera	Cuber UHD185 Firefly imaging spectrometer of UAV	125 bands (450–950 nm), sensor resolution: 2 million pixels	[45]
		Multispectral camera	Airphen	6 bands (450 nm, 530 nm, 570 nm, 675 nm, 730 nm, 850 nm), 1280 × 960 pixels	This paper
	Non-imaging sensor	\	GreenSeeker	2 bands (656 nm, 774 nm), handheld	[6]
Platforms	Ground	\	Analytical spectral devices (ASD)	Wavelength range: 325–1075 nm, spectral resolution: 3 nm	[45]
	Low-altitude	Fixed-wing UAV	FW I	Endurance: 60 min, maximum speed: 17.5 m/s	[46]
		Multi-rotor UAV	DJI M600Pro	Endurance: 38 min, maximum speed: 18 m/s	This paper
High-altitude	Satellite	MODIS	Spatial Resolution: 250 m (bands 1–2), 500 m (bands 3–7), 1000 m (bands 8–36)	[47]	

LAI and LDM are the primary growth parameters of crops and they are closely related to yield formation. The traditional test method is destructive sampling, which it is time-consuming and laborious, and may suffer from human error. By means of remote sensing, lossless estimation of LAI and LDM can be achieved, which greatly improves the efficiency and prepares for the following yield estimation. In this study, the correlation between vegetation indices and growth parameters during the whole growth season of wheat was constructed. During the same growth stage, the difference

among N rates (0–300 kg·ha⁻¹) and seeding densities (1.2–3.5 million seedlings ha⁻¹) resulted in the synchronous change of growth parameters and vegetation indices. Vegetation indices can represent the growth status of different treatments to some extent, so they can be used to non-destructively estimate crop growth parameters. We adopted a simple regression method to analyze this single factor model. SR is one of the common modeling methods related to the correlation between vegetation indices and growth parameters. When building the relationship between vegetation indices and LAI, GNDVI and NDVI appeared to show a ‘saturation’ phenomenon [48], resulting in a poor fit with the dataset. The vegetation indices of the red edge band and near-infrared band (NDRE, CIRE, CCCI, and RESAVI) performed better, explaining a variability of 71%, 71%, 70%, and 74%, respectively. The LAI estimation model constructed by RESAVI was the optimal model in this study (Table 7). The results of the LDM estimation models are similar to that of LAI estimation models. Better vegetation indices (NDRE, CIRE, and CCCI) were also composed of a combination of red edge band and near-infrared band data, explaining 74%, 73%, and 74% of variation, respectively. The LDM estimation model constructed by CIRE was the optimal model in this study (Table 7). This is consistent with previous research results [49]. This may be because the red edge band and the near-infrared band are more sensitive and can better characterize the canopy growth dynamics.

Table 7. The optimal estimation model of LAI, LDM, and yield in this study.

The Optimal Estimation Model	Vegetation Index	Modeling Method	Modeling R ²	Verified R ²	RRMSE
LAI	RESAVI (All stages)	LR	0.74	0.74	0.1990
LDM	CIRE (All stages)	LR	0.75	0.75	0.2372
Yield	NDVI (Jointing)	RF	0.76	0.78	0.1030
	NDVI (Booting)				
	NDVI (Flowering)				
	NDVI (Filling)				

At present, the conventional method of wheat yield estimation by remote sensing is an empirical model, including a linear model and nonlinear model. Linear models are simple to calculate, but the formation of wheat yield is usually non-linear [50]. In this study, LR and MLR are linear models, but we also utilized nonlinear models, including SMLR, PLSR, ANN, and RF; among these nonlinear models, ANN and RF are machine-learning tools that have been developed more recently. In general, the nonlinear estimation model is better than the general linear estimation model in this study. It is possible that the linear method often has a problem of strong empirical characteristics and low accuracy [51]. The correlation between the vegetation index and yield from the booting stage to the filling stage was better than that at the early growth stage, and this is consistent with the research results of Zhu et al. [19]. Since the time of photographing and sampling was at the late filling stage, rather than at the early or middle stage, the correlation coefficient at the filling stage decreased. Wheat leaves began to age gradually at the late filling stage and were no longer suitable for modeling and analysis.

Considering the single factor to construct the yield estimation model, we selected the NDRE at the flowering stage, which performed best throughout the entire season, to establish the model using a simple regression method. We found that NDRE at the flowering stage was significantly correlated with yield. We can conclude that it is feasible to estimate wheat yield with sensitive vegetation indices, which is consistent with previous studies [17]. While considering the multiple factors used to construct the yield estimation model, we selected four vegetation indices with the best performance from different perspectives to establish the model by multiple multivariate modeling methods. In this study, the estimation accuracy of multi-factor estimation models was much higher than that of single-factor models. The multi-factor yield estimation model with the lowest R² value was the model constructed by NDVI at the jointing stage, NDVI at the booting stage, NDVI at the flowering stage, and NDVI at the filling stage. The methods used in this model with the lowest R² were MLR and SMLR, and they performed almost identically. Similar results were obtained in the model constructed

by NDVI, NDRE, OSAVI, and CCCI at the flowering stage. However, in the model constructed by NDVI at the jointing stage, NDVI at the booting stage, NDRE at the flowering stage, and CCCI at the filling stage, the MLR method was superior to SMLR. The difference between MLR and SMLR mainly depend on the number of exclusion factors in the modeling process of SMLR. Overall, the estimation accuracy of PLSR, ANN, and RF was better than MLR and SMLR. In the model constructed by NDVI at the jointing stage, NDVI at the booting stage, NDRE at the flowering stage, and CCCI at the filling stage, PLSR was the optimal the method with the highest R^2 (0.7667). ANN had the best performance in the model constructed by NDVI at the flowering stage, NDRE at the flowering stage, OSAVI at the flowering stage, and CCCI at the flowering stage, explaining 77.01% of the variation. In this paper, the optimal yield estimation model was constructed by NDVI at the jointing stage, NDVI at the booting stage, NDVI at the flowering stage, and NDVI at the filling stage, which adopted the RF method, explaining a variability of 78% (Table 7). Machine-learning methods (PLSR, ANN, and RF) have advantages for doing regression with non-linear correlation by avoiding multi-collinearity and eliminating interference factors, thus further improving the accuracy of the yield estimation model.

When establishing the single factor model, we only adopted the simple regression method because the single-factor model did not have the problem of multicollinearity or others, which appeared in multi-factor models. Different modeling methods may marginally improve model accuracy. For example, PLSR had a very similar result as the simple linear regression. In the exploration of the modeling methods of a multi-factor yield estimation model, some commonly used methods were adopted, including MLR, SMLR, PLSR, ANN, and RF. Recently, some popular modeling methods are expected to be tried in future further studies, such as support vector machine (SVM). A limitation of this study is the specific locality, using experimental results from Jiangsu Province, meaning that without the verification of different ecological points and further experiments, there may be a lack of universality in the findings.

5. Conclusions

This study explored the potential of multi-spectral camera mounted on a multi-rotor UAV for monitoring wheat growth indices. The results showed that the vegetation index composed of a red edge band and near-infrared band was significantly correlated with LAI and LDM. The optimal LAI estimation model was built by RESAVI, explaining 76% variation, with an RRMSE of 0.1990. The optimal LDM estimation model was built by NDRE, explaining 74% variation, with an RRMSE of 0.2337. We also analyzed and evaluated the yield estimation accuracy of LR, MLR, SMLR, PLSR, ANN, and RF. The results showed that the yield estimation model built by multiple factors is superior to the single factor, and the yield estimation model built by PLSR, ANN, and RF performed better than other models. In this experiment, the optimal yield estimation model was built by NDVI at the jointing stage, NDVI at the booting stage, NDVI at the flowering stage, and NDVI at the filling stage. The modeling method we used was RF, explaining 78% variation, with RRMSE of 0.1030. In summary, this study demonstrates the potential of using a multi-rotor UAV combined with the multi-spectral camera to monitor wheat growth parameters and estimate yield. A variety of linear and nonlinear modeling methods were used to explore the possibility of further improving the accuracy of yield estimation. The UAV sensing system in this study can provide reference and technical support for the management and decision-making of intensive farming at medium-scale cropping area, which performed more efficient than handheld sensors. This method should combine with satellite data to enlarge the application at large-scale agricultural area in future study.

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