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# Image Enhancement using Fuzzy Intensity Measure and Adaptive Clipping Histogram Equalization

Xiangyuan Zhu, Xiaoming Xiao, Tardi Tjahjadi, Zhihu Wu, Jin Tang\*

Abstract—Image enhancement aims at processing an input image so that the visual content of the output image is more pleasing or more useful for certain applications. Although histogram equalization is widely used in image enhancement due to its simplicity and effectiveness, it changes the mean brightness of the enhanced image, and introduces a high level of noise and distortion. To address these problems, this paper proposes image enhancement using fuzzy intensity measure and adaptive clipping histogram equalization (FIMHE). FIMHE uses fuzzy intensity measure to first segment the histogram of the original image, and then clip the histogram adaptively in order to prevent excessive image enhancement. Experiments on the Berkeley database and CVF-UGR-Image database show that FIMHE outperforms state-of-the-art histogram equalization based methods.

Index Terms—Image enhancement, histogram equalization, fuzzy intensity measure, adaptive clipping

#### I. Introduction

The aim of image enhancement is to bring out the hidden details in a low contrast image [1]. Image enhancement has been widely used in medical imaging [2], face recognition [3] and watermarking [4]. One image enhancement method, histogram equalization (HE), is widely used for contrast enhancement due to its simple operation and effectiveness. The main idea of HE is to flatten the probability density function (PDF) of the input image histogram and remap the grey levels to generate a processed image with improved contrast [5]. Although HE has many advantages, it significantly modifies the average brightness of the processed image with respect to the original image. It also introduces noise and intensity saturation effects which result in a loss of image details and make the appearance of the processed image unnatural.

In this paper, a new method is proposed to address the above-mentioned problems of HE, and verify the

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effectiveness of the method. These are achieved by using a fuzzy intensity measure for segmenting the original image histogram and adaptive clipping of the histogram to prevent excessive enhancement.

This paper is organized as follows. Section II reviews related methods. Section III presents the proposed method. Section IV analyzes the experimental results of the performance of the proposed method, and finally Section V concludes the paper.

#### II. RELATED WORK

Image enhancement algorithms based on the classical histogram equalization have been proposed to overcome the disadvantages of HE. The earliest improved algorithm is the brightness preserving bi-histogram equalization (BBHE) [6]. BBHE divides the histogram of an image into two parts based on the average brightness of the image, and then HE is applied to each part independently. Dualistic sub-image histogram equalization (DSIHE) [7] which is based on BBHE uses the median of the input image grey levels to divide the histogram. DSIHE is better than BBHE in maintaining the image brightness. The minimum mean brightness error bi-histogram equalization (MMBEBHE) [8] computes a minimum absolute value of the average luminance difference of the input image and uses each grey level as a splitting threshold until the minimum absolute mean brightness error is obtained.

Recursive mean-separate histogram equalization (RMSHE) [9] utilizes BBHE recursively, and the histogram of the input image is divided into  $2^r$  parts, where the user-defined scale r determines the recursive level, thus allowing brightness preservation from 0% to 100% [5]. Another algorithm similar to RMSHE is recursive sub-image histogram equalization (RSIHE) [10] which uses DSIHE instead of BBHE to divide the histogram. The common difficulty with RSMHE and RSIHE is in choosing the appropriate value of r.

Bi-histogram equalization with a plateau limit (BHEPL) [11] first divides an image histogram into two parts using the mean brightness of the image, and then clips the sub-histogram bins independently. A variant of BHEPL, bi-histogram equalization median plateau limit (BHEPL-D) [12], divides a histogram into two parts using the median of the image grey levels. BHEPL-D is better than BHEPL in maintaining the mean brightness while preserving the details of the image.

In modified histogram equalization (MHE) [13] the average value of the histogram is set as a limit to the

accumulation of histogram component bins. The method, exposure based sub image histogram equalization (ESIHE) [14], first clips the histogram bins and then divides the image into two parts using an exposure threshold. This method is effective in enhancing under-exposed images. More recently, bi-histogram equalization using two different plateau limits (BHE2PL) [15] uses two plateau limits to modify the sub-histograms. The method preserves the mean brightness while enhancing the contrast of the processed image.

Although many new methods have been proposed to solve the problem of image contrast enhancement while maintaining brightness, these methods can only achieve good enhancement under certain conditions and cannot achieve the best results on all evaluation metrics. In this paper, a method named fuzzy intensity measure and adaptive clipping histogram equalization (FIMHE) is proposed. The method increases the image contrast while preserving the original information of the image.

# III. PROPOSED METHOD

FIMHE consists of four steps: computation of fuzzy intensity measure, histogram segmentation, adaptive histogram clipping and equalization.

## A. Fuzzy Intensity Measure

The fuzzy intensity measure [16] is defined to distinguish the bright and dark regions in an image. The mean and standard deviation of the histogram intensity (or grey level) distribution, i.e., respectively

$$g_a = \frac{\sum_{m=0}^{L-1} m \times p(m)}{\sum_{m=0}^{L-1} p(m)}$$
 (1)

$$g_{d} = \left[ \frac{\sum_{m=0}^{L-1} \left[ (m - g_{a})^{2} p(m) \right]}{\sum_{m=0}^{L-1} p(m)} \right]^{1/2}$$
 (2)

are used to determine the non-homogeneous intensity distribution of the image. They are also used to define the

fuzzy intensity measure= 
$$\frac{g_d}{g_a}$$
 (3)

and

$$T = L \left[ \frac{g_d}{g_a} \right],\tag{4}$$

where m represents the intensity (or grey level) of the pixel at image coordinates (i, j), p(m) is the number of pixels in the histogram of the image, and L is the total number of grey levels in the image. The parameter T is used to cluster the image into bright and dark regions, where the dark and bright regions have grey level ranges of [0,T] and [T+1, L-1], respectively.

## B. Histogram segmentation

The original histogram is first divided into two parts with grey levels in the ranges of [0,T] and [T+1,L-1]. Denote  $N_{L1}$  and  $N_{L2}$  as the total numbers of pixels in the grey level ranges  $[0,T_l]$  and  $[T_l+1,T]$ , respectively. Denote  $N_{U1}$  and  $N_{U2}$  as the total numbers of pixels in the grey level ranges  $[T+1,T_n]$  and  $[T_n+1,L-1]$ , respectively.  $T_n$ 

and  $T_u$  are grey levels that equally divide the grey level ranges [0,T] and [T+1,L-1] such that the number of pixels in the grey level ranges  $[0,T_i]$  is equal to the number of pixels in  $[T_1+1,T]$ . Similarly for  $[T+1,T_n]$  and  $[T_{u}+1, L-1]$ . Thus,

$$N_{I1} = N_{I2} \,, \tag{5}$$

$$N_{U1} = N_{U2} \,. \tag{6}$$

Finally, the input histogram is divided into four parts with grey level ranges of  $[0,T_1]$ ,  $[T_1+1,T]$ ,  $[T+1,T_n]$  and  $[T_{..}+1, L-1]$ .

# C. Adaptive Histogram Clipping

Histogram bins clipping is introduced to prevent over-enhancement of local image areas. To limit the enhancement rate, it is necessary to limit the first derivative of the histogram or the histogram itself [11]. Clipping is performed if the histogram bins are greater than some threshold. For better enhancement, we introduce an adaptive method to clip the histogram. Specifically, the median of the occurring intensity of each of the corresponding sub-histogram are computed as

$$T_{L1}^{m} = median[h(k)], for 0 \le k \le T_{l}, (7)$$

$$T_{1,2}^m = median[h(k)], for T_1 < k \le T,$$
 (8)

$$T_{L1}^{m} = median[h(k)], \qquad for \quad T_{l} < k \le T, \qquad (8)$$

$$T_{U1}^{m} = median[h(k)], \qquad for \quad T < k \le T_{u}, \qquad (9)$$

$$T_{U2}^{m} = median[h(k)], for T_{u} < k < L-1, (10)$$

where h(k) is the number of pixels with grey level k. The average number of grey level occurrences of each sub-histogram are computed as:

$$T_{L1}^{a} = \frac{1}{T_{L} + 1} \sum_{k=0}^{T_{L}} h(k)$$
 (11)

$$T_{L2}^{a} = \frac{1}{T - T_{L}} \sum_{k=T,+1}^{T} h(k)$$
 (12)

$$T_{U1}^{a} = \frac{1}{T - T} \sum_{i=T}^{T_{u}} h(k)$$
 (13)

$$T_{U2}^{a} = \frac{1}{L - T_{u} - 1} \sum_{k=T_{u}+1}^{L-1} h(k) .$$
 (14)

The clipping thresholds of the four sub-histograms are adaptively determined as follows:

$$T_{L1} = \begin{cases} T_{L1}^{m} & \text{if } T_{L1}^{m} > 0\\ T_{L1}^{a} & \text{elsewhere} \end{cases}$$
 (15)

$$T_{L2} = \begin{cases} T_{L2}^{m} & \text{if } T_{L2}^{m} > 0\\ T_{L2}^{a} & \text{elsewhere} \end{cases}$$
 (16)

$$T_{U1} = \begin{cases} T_{U1}^{m} & \text{if } T_{U1}^{m} > 0\\ T_{U1}^{a} & \text{elsewhere} \end{cases}$$
 (17)

$$T_{U2} = \begin{cases} T_{U2}^{m} & \text{if } T_{U2}^{m} > 0\\ T_{U2}^{a} & \text{elsewhere} \end{cases}$$
 (18)

Finally, using the clipping each sub-histogram is clipped as follows

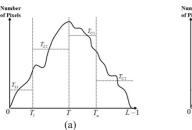
$$h_{L1}^{N}(k) = \begin{cases} h_{L1}(k) & \text{if } h_{L1}(k) \le T_{L1} \\ T_{L1} & \text{elsewhere} \end{cases}$$
 (19)

$$h_{L2}^{N}(k) = \begin{cases} h_{L2}(k) & \text{if } h_{L2}(k) \le T_{L2} \\ T_{L2} & \text{elsewhere} \end{cases}$$
 (20)

$$h_{U1}^{N}(k) = \begin{cases} h_{U1}(k) & \text{if } h_{U1}(k) \le T_{U1} \\ T_{U1} & \text{elsewhere} \end{cases}$$
 (21)

$$h_{U2}^{N}(k) = \begin{cases} h_{U2}(k) & \text{if } h_{U2}(k) \le T_{U2} \\ T_{U2} & \text{elsewhere} \end{cases}, \qquad (22)$$

where  $h_{L1}^N$ ,  $h_{L2}^N$ ,  $h_{U1}^N$ ,  $h_{U2}^N$  are the number of pixels corresponding to the grey level of each clipped sub-histogram, respectively. The clipping of histograms is illustrated in Figure 1.



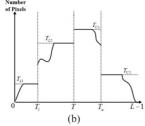


Fig. 1. Clipping of a histogram: (a) Original histogram and (b) the histogram after clipping.

## D. Equalization

After segmentation and clipping, four new sub-histograms are obtained. Histogram equalization is then applied to each sub-histogram as follows. Denote  $N_{L1}^{new}$ ,  $N_{L2}^{new}$ ,  $N_{U1}^{new}$  and  $N_{U2}^{new}$  as the total number of pixels in the new sub-histograms L1, L2, U1 and U2, respectively. The PDF of the corresponding sub-histograms are

$$P_{L1}(k) = \frac{h_{L1}^{N}(k)}{N_{L1}^{new}}, \quad for \ 0 \le k \le T_{l}$$
 (23)

$$P_{L2}(k) = \frac{h_{L2}^{N}(k)}{N_{L2}^{new}}, \quad for \ T_{l+1} < k \le T$$
 (24)

$$P_{U1}(k) = \frac{h_{U1}^{N}(k)}{N_{U1}^{new}}, \quad for \ T < k \le T_u$$
 (25)

$$P_{U2}(k) = \frac{h_{U2}^{N}(k)}{N_{U2}^{new}}, \quad for \, T_u < k < L.$$
 (26)

The cumulative density functions (CDF) of the corresponding sub-histograms are

$$C_{L1}(k) = \sum_{i=0}^{k} P_{L1}(k), \text{ for } 0 \le k \le T_i$$
 (27)

$$C_{L2}(k) = \sum_{T,l}^{k} P_{L2}(k), \text{ for } T_l < k \le T$$
 (28)

$$C_{U1}(k) = \sum_{T+1}^{k} P_{U1}(k), \text{ for } T < k \le T_u$$
 (29)

$$C_{U2}(k) = \sum_{T=1}^{k} P_{U2}(k), \text{ for } T_u < k < L.$$
 (30)

The next step of FIMHE is to equalize each sub-histogram using the transfer function

$$f(k) = \begin{cases} T_{l} \times [C_{l1}(k) - 0.5 \times P_{l1}(k)] & \text{for } 0 \le k \le T_{l} \\ (T - T_{l} - 1) \times [C_{l2}(k) - 0.5 \times P_{l2}(k)] + T_{l} + 1 & \text{for } T_{l} < k \le T \\ (T_{u} - T - 1) \times [C_{U1}(k) - 0.5 \times P_{U1}(k)] + T + 1 & \text{for } T < k \le T_{u} \\ (L - T_{u} - 2) \times [C_{U2}(k) - 0.5 \times P_{U2}(k)] + T_{u} + 1 & \text{for } T_{u} < k < L \end{cases}, (31)$$

where f(k) denotes the new grey levels of each sub-histogram after equalization. The enhanced image is generated from the combined four sub-histograms.

#### IV. EXPERIMENTS

We performed qualitative and quantitative evaluations of the results of image enhancement, i.e., we evaluated FIMHE from the visual perspective of human perception and computed some quantitative assessments. We chose BBHE [6], DSIHE [7], RSIHE [10] (r=2), BHEPL [11], BHEPL-D [12], MHE [13] and ESIHE [14] for comparison because they are all based on a histogram segmentation, histogram modification or histogram clipping. We used the following four quantitative evaluation indices to evaluate the quality of the enhanced images: Shannon entropy (Entropy) [17]-[18], peak signal to noise ratio (PSNR) [19]-[22], absolute mean brightness error (AMBE) [23]-[26] and structural similarity index (SSIM) [27]-[33].

Entropy is an index that can be used to determine the richness of image details and has been widely used in the evaluation of image quality. Entropy can be defined as:

$$Entropy = -\sum_{k=0}^{L-1} p(k) \log_2 p(k) , \qquad (32)$$

where p(k) is the PDF of an image histogram. A larger entropy indicates richer information. For comparison, we also compute the percentage of information entropy, i.e.,

$$Entropy\% = \frac{Entropy_{outputimage}}{Entropy_{inputimage}} \times 100\%.$$
 (33)

PSNR measures image distortion or noise level and is defined as:

$$PSNR = 10\log_{10}\left[\frac{(L-1)^2}{MSE}\right],$$
 (34)

where the mean squared error (MSE) [34]-[36] is given by

$$MSE = \frac{1}{M \times N} \sum_{i=1}^{M} \sum_{j=1}^{N} |X(i,j) - Y(i,j)|^{2}.$$
 (35)

X(i, j) and Y(i, j) are respectively the grey level of the original image and enhanced image at coordinates (i, j).

AMBE utilizes the absolute value of the difference in the mean brightness of the original image and the enhanced image, i.e.,

$$AMBE = |E(X) - E(Y)|, \tag{36}$$

where

$$E(X) = \frac{1}{M \times N} \sum_{i} \sum_{j} X(i, j)$$
 (37)

$$E(Y) = \frac{1}{M \times N} \sum_{i} \sum_{j} Y(i, j) . \tag{38}$$

It is used to evaluate the change in brightness before and after image enhancement. Ideally, the mean brightness of the enhanced image should be equal to the mean brightness of the input image, in which case the value of AMBE is zero [37].

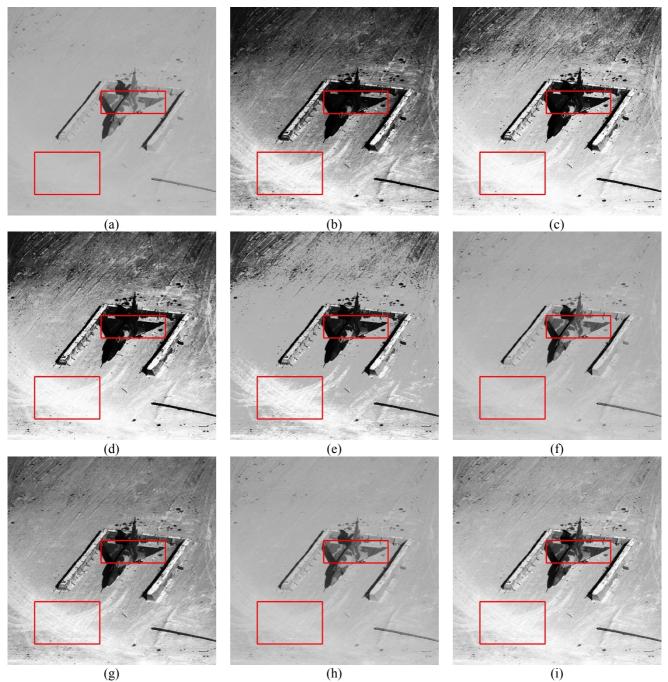


Fig. 2. Plane. (a) Original image. From (b) to (i): enhanced images using BBHE, DSIHE, RSIHE, BHEPL, BHEPL-D, MHE, ESIHE, and the proposed method, respectively.

SSIM combines correlation distortion, image brightness distortion and contrast distortion to determine the degree of distortion, i.e.,

$$SSIM(x,y) = \frac{(2\mu_x \mu_y + C_1)(2\sigma_{xy} + C_2)}{(\mu_x^2 + \mu_y^2 + C_1)(\sigma_x^2 + \sigma_y^2 + C_2)},$$
 (39)

where  $\mu_x$  and  $\mu_y$  are respectively the average brightness of the original image and the enhanced image;  $\sigma_x$  and  $\sigma_y$  are respectively the standard deviation of the original image and the enhanced image;  $\sigma_{xy}$  is the square root of the covariance of the original image and the enhanced image; and  $C_1$  and  $C_2$  are constants. The range of SSIM is [0, 1]. In order to get a better-enhanced image, the value of SSIM should be larger. The larger the value the smaller is the image distortion.

## A. Qualitative Evaluation

In order to analyze the quality of the enhanced image from visual effects, we selected six groups of images "Plane", "Photographer", "House", "Fish", "Couple" and "U2" which are commonly used in image quality assessment. The obvious changes in the enhanced images are denoted with red boxes in Figures 2 - 7.

For the first image "Plane" in Figure 2(a), we note that the texture features of the original image are blurred and many details are obscured. As can be seen in the rest of Figure 2, the results of BBHE and RSIHE are obviously over enhanced and have a poor performance. Although MHE has enhanced the texture slightly, the enhanced image is too dark on the wing and the foreground. The image content of the result of our proposed method is the most abundant and has a smooth texture.

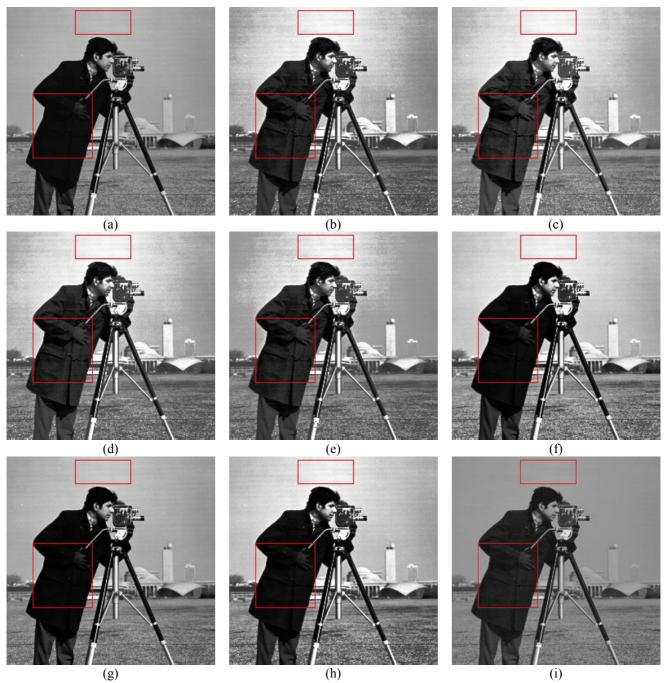


Fig. 3. Photographer. (a) Original image. From (b) to (i): enhanced images using BBHE, DSIHE, RSIHE, BHEPL, BHEPL-D, MHE, ESIHE, and the proposed method, respectively.

Figure 3(a) shows the image "Photographer" which is too dark for the image details to be clearly visible. The rest of Figure 3 shows that using DSIHE and BHEPL resulted in a saturation effect that makes the enhanced image greatly different in brightness from the original image. The result of the proposed method has a more natural look compared with those of the other methods, and the brightness is the most similar to the original image. It can also be observed from the man's clothes that the details of the original image are well preserved and has the minimum image degradation.

For the image "House" shown in Figure 4(a), DSIHE and RSIHE introduced a high level of noise and caused serious image distortion. Unlike the proposed method, the other methods produced excessive enhancement to the window, and resulted in a loss of image details. The proposed method not only resulted in the most abundant image details, the average brightness of the enhanced image is the

most similar to the original image.

For the image "Fish" shown Figure 5(a), the proposed method resulted in the most natural image with its brightness basically the same as the original image. The enhanced image has the clearest outline and most vivid details especially when compared with the result of BHEPL, which looks unnaturally artistic. It also has the richest details in the image while minimizing the noise level.

Figure 6(a) shows the image "Couple" which is too dark for the image details to be clearly visible. Using DSIHE and MHE resulted in a saturation effect that makes the enhanced image greatly different from the original image in brightness. The result of the proposed method has a more natural look compared with those of the other methods, and the brightness is the most similar to that in the original image. It can also be observed from the mural and the



Fig. 4. House. (a) Original image. From (b) to (i): enhanced images using BBHE, DSIHE, RSIHE, BHEPL-D, MHE, ESIHE, and the proposed method, respectively.

man's pants in the enhanced image that the details of the original image are well preserved and has the minimum image degradation.

For the image "U2" shown in Figure 7(a), DSIHE and ESIHE introduced a high level of noise and caused serious image distortion. Unlike the proposed method, other methods produced excessive enhancement to the left wing, and resulted in a loss of image details. The proposed method not only resulted in the most abundant image details, the average brightness of the image is the most similar to the original image.

Histogram equalization refers to processing an input image by mapping the input into an output image to effectively utilize the dynamic range such that each grey level has an equal number of pixels in the output, i.e., the grey level distribution is evenly spread out. Therefore, it is desirable for the equalized output image to have a flat grey

level distribution. However, it should be noted that this process should not change the overall shape of the input histogram so as to preserve the image content.

Figure 8 shows the histograms of the test images after applying eight HE-based image enhancement algorithms. The original histogram is stretched to both ends of the grey scale. As can be seen from the figure, each algorithm has improved the histogram of the original image, i.e., the histogram are more spread out. However, most algorithms greatly change the shape of the original histogram, e.g., DSIHE, RSIHE, and ESIHE. This means that the original information of the image has been changed, resulting in a large difference in visual appearance between the original and enhanced images. The histogram of the image processed by FIMHE has greatly flattened grey-level distribution. This algorithm stretches the original histogram to both ends of the grey scale while maintaining the shape

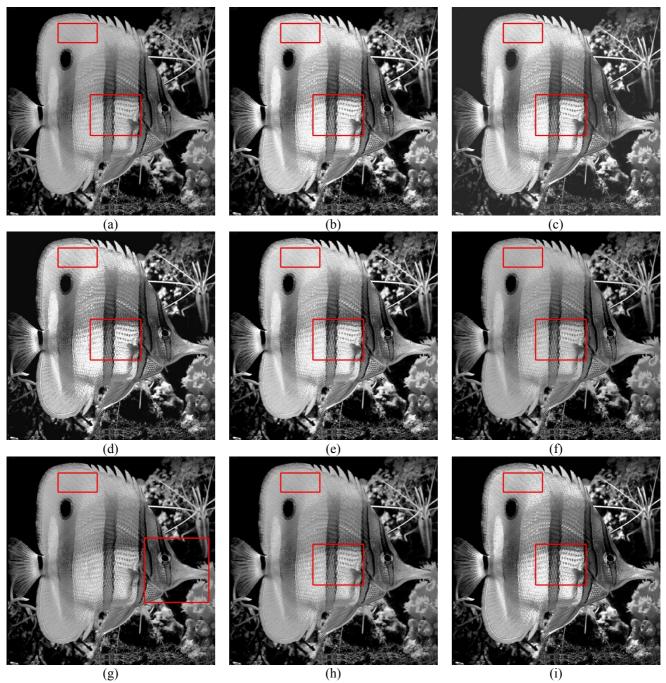


Fig. 5. Fish. (a) Original image. From (b) to (i): enhanced images using BBHE, DSIHE, RSIHE, BHEPL, BHEPL-D, MHE, ESIHE, and the proposed method, respectively.

of the original histogram. It thus preserves the image details and produces visual experience most similar to that of the original image.

## B. Quantitative Evaluation

Tables I to VI show the quantitative evaluation results on "Plane", "Photographer", "House", "Fish", "Couple" and "U2", respectively. The best test results are denoted in bold.

Table I shows that the proposed method, FIMHE, performs better on "Plane" than the other seven algorithms on all evaluation indices. In particular, its AMBE value is the smallest, i.e., the brightness of the original image is best preserved. Although the AMBE value of the image enhanced using BBHE is similar to that of FIMHE, it performs poorly on other indices.

Table II shows that FIMHE outperforms the other algorithms on "Photographer". Although its Entropy is

slightly smaller than the BHEPL-D, its PSNR and SSIM are maximum, i.e., the image information is abundant with minimal noise and artifacts. Although its Entropy is slightly smaller than that of the original image, FIMHE is still better than the other seven algorithms.

Table III shows that FIMHE is much better for Entropy and PSNR on "House". The brightness of the original image is preserved, and the introduction of noise is minimal, ensuring that the enhanced image can be used for televisions and digital cameras. The good effects of FIMHE can also be observed by comparing the details of the images shown in Figure 4.

Table IV shows the proposed method produces the largest SSIM value on "Fish" compared with other methods. This means that the distortion of the image is minimal, which gives the enhanced image a more natural look.

Table V shows that FIMHE is much better for PSNR and

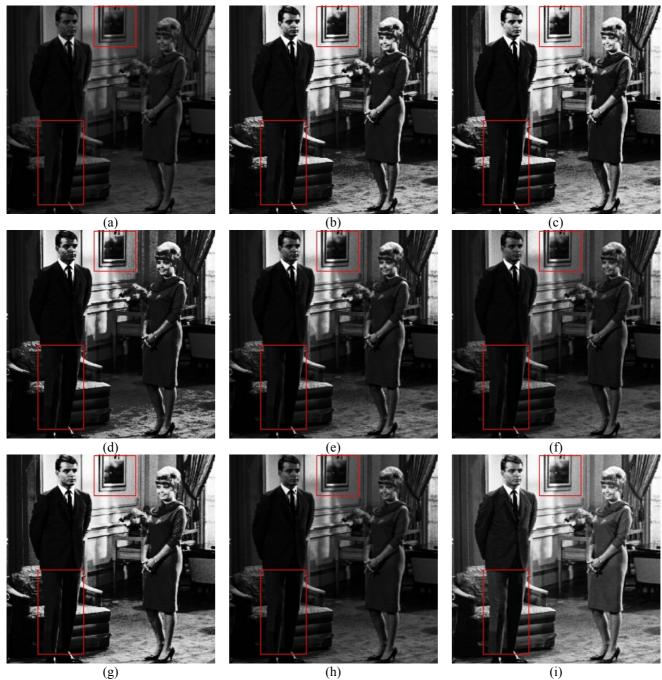


Fig. 6. Couple. (a) Original image. From (b) to (i): enhanced images using BBHE, DSIHE, RSIHE, BHEPL-D, MHE, ESIHE, and the proposed method, respectively.

AMBE on "Couple". The brightness of the original image is preserved, and the introduction of noise is minimal, ensuring that the enhanced image can be used for televisions and digital cameras.

Table VI shows the proposed method produces the largest SSIM and PSNR on "U2" (i.e., achieving the best performance) compared with the other methods. As can be seen from the maximum AMBE, it is closest to the brightness of the original image. Note also that the image processed by the proposed method achieves the highest (i.e., the best) value for SSIM and PSNR. This means that the distortion of the image is minimal, giving the enhanced image a more natural look.

The performance of FIMHE is more satisfactory than the other seven algorithms on "Plane", "Photographer", "House", "Fish", "Couple" and "U2".

In addition to these six test images, four objective evaluation functions (i.e., Entropy, PSNR, AMBE, and SSIM) were employed on different image databases to further verify the capabilities and performance of the proposed FIMHE.

Figure 9 shows the average test results for 400 images in the Berkeley database. It shows that FIMHE obtains the maximum average Entropy, i.e., the information of the original image is retained to the greatest degree, and the details are fully displayed. Its PSNR is the highest, i.e., the image contrast is well enhanced while introducing the smallest noise level. Its average AMBE is the smallest, i.e., the average brightness of the original image is best preserved. Finally, its SSIM being the highest indicates that the proposed method produces the minimum image distortion.

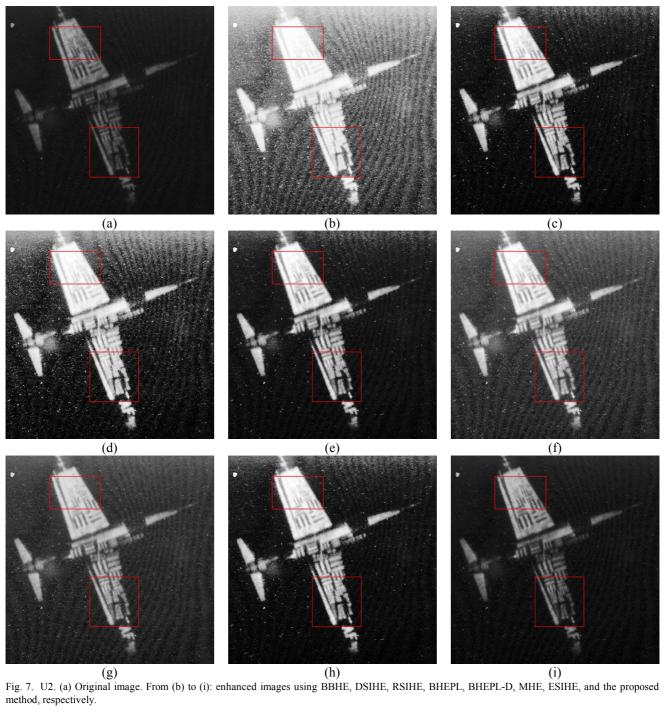


TABLE I
THE RESULT OF DIFFERENT ALGORITHMS ON THE IMAGE "PLANE"

Methods	Entropy	Entropy%	PSNR	AMBE	SSIM
Original image	4.938	-	-	-	-
BBHE	4.813	97.168	13.310	0.937	0.459
DSIHE	4.785	96.901	12.127	16.736	0.387
RSIHE	4.732	95.835	15.897	7.183	0.518
BHEPL	4.914	99.528	19.159	8.641	0.705
BHEPL-D	4.910	99.432	29.511	1.449	0.959
MHE	4.891	99.060	15.991	16.921	0.549
ESIHE	4.893	99.104	20.332	9.706	0.740
FIMHE	4.931	99.873	31.606	0.916	0.965

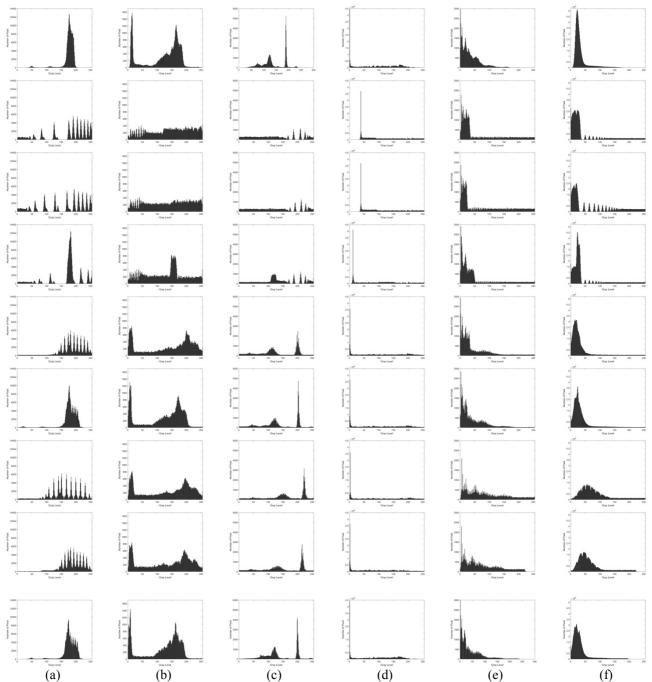


Fig. 8. Top row: Histogram of test image (a) Plane; (b) Photographer; (c) House; (d) Fish; (e) Couple; and (f) U2. From row 2 to bottom each row respectively shows the result of the images processed by BBHE, DSIHE, RSIHE, BHEPL, BHEPL-D, MHE, ESIHE and FIMHE.

TABLE II
THE RESULT OF DIFFERENT ALGORITHMS ON THE IMAGE "PHOTOGRAPHER"

Methods	Entropy	Entropy%	PSNR	AMBE	SSIM
Original image	7.019	-	-	-	-
BBHE	6.809	97.008	18.269	23.678	0.820
DSIHE	6.781	96.609	18.778	17.388	0.817
RSIHE	6.765	96.381	21.166	8.323	0.824
BHEPL	6.922	98.618	18.864	19.332	0.919
BHEPL-D	6.996	99.672	30.708	1.634	0.964
MHE	6.901	98.319	19.566	14.525	0.911
ESIHE	6.900	98.305	20.000	11.754	0.908
FIMHE	6.967	99.259	36.275	1.609	0.965

TABLE III
THE RESULT OF DIFFERENT ALGORITHMS ON THE IMAGE "HOUSE"

Methods	Entropy	Entropy%	PSNR	AMBE	SSIM
Original image	6.488	-	-	-	-
ВВНЕ	6.246	96.270	17.267	13.920	0.562
DSIHE	6.242	96.208	17.589	9.910	0.567
RSIHE	6.240	96.178	20.815	0.816	0.717
BHEPL	6.424	99.014	21.824	7.186	0.886
BHEPL-D	6.426	99.044	23.818	1.565	0.935
MHE	6.393	98.536	18.506	18.565	0.856
ESIHE	6.410	98.798	20.479	7.378	0.854
FIMHE	6.446	99.353	29.492	2.582	0.984

TABLE IV
THE RESULT OF DIFFERENT ALGORITHMS ON THE IMAGE "FISH"

Methods	Entropy	Entropy%	PSNR	AMBE	SSIM
Original image	6.451	-	-	-	-
BBHE	6.131	95.031	18.969	24.759	0.724
DSIHE	6.138	95.137	19.060	24.124	0.721
RSIHE	6.109	94.698	23.904	7.746	0.779
BHEPL	6.399	99.188	23.052	11.587	0.952
BHEPL-D	6.407	99.311	24.285	9.832	0.959
MHE	6.318	97.933	22.425	12.005	0.909
ESIHE	6.299	97.646	26.152	0.857	0.931
FIMHE	6.412	99.386	43.513	0.514	0.998

TABLE V
THE RESULT OF DIFFERENT ALGORITHMS ON THE IMAGE "COUPLE"

Methods	Entropy	Entropy%	PSNR	AMBE	SSIM
Original image	6.473	-	-	-	-
BBHE	6.306	97.413	13.265	32.275	0.693
DSIHE	6.267	96.807	11.667	42.987	0.620
RSIHE	6.339	97.924	15.699	19.435	0.802
BHEPL	6.373	98.444	18.598	15.058	0.879
BHEPL-D	6.412	99.052	22.268	10.915	0.930
MHE	6.410	99.022	11.681	53.587	0.489
ESIHE	6.410	99.019	14.422	38.979	0.614
FIMHE	6.440	99.490	23.759	8.686	0.950

 $\label{thm:condition} TABLE~VI\\ THE~RESULT~OF~DIFFERENT~ALGORITHMS~ON~THE~IMAGE~"U2"$ 

Methods	Entropy	Entropy%	PSNR	AMBE	SSIM
Original image	5.650	-	-	-	-
BBHE	5.558	98.375	15.077	16.292	0.592
DSIHE	5.485	97.069	10.975	41.301	0.303
RSIHE	5.535	97.961	15.646	17.117	0.668
BHEPL	5.570	98.583	21.007	3.297	0.854
BHEPL-D	5.541	98.072	23.411	5.068	0.903
MHE	5.601	99.125	12.414	51.345	0.387
ESIHE	5.601	99.133	15.812	33.704	0.551
FIMHE	5.626	99.567	28.800	0.683	0.920

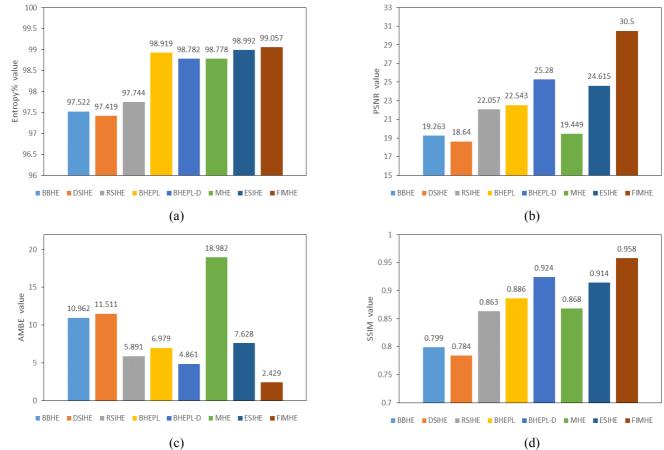


Fig. 9. Average result of (a) Entropy, (b) PSNR, (c) AMBE and (d) SSIM for the 400 images in the BERKELEY Database.

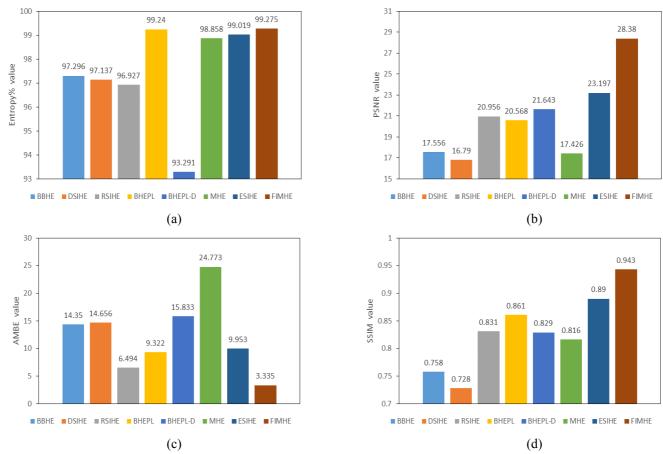


Fig. 10. Average result of (a) Entropy, (b) PSNR, (c) AMBE and (d) SSIM for the 86 images in the CVF-UGR-IMAGE Database.

Figure 10 shows the same conclusion on the CVF-UGR-Image database. Therefore, the proposed method is better than the state-of-the-art HE-based image enhancement methods.

## V. CONCLUSION

This paper proposes a HE-based enhancement algorithm, FIMHE, which combines fuzzy intensity measure, image segmentation and adaptive clipping of histogram bins to address over-enhancement and image distortion HE-based enhanced images. The algorithm not only enhances the contrast of the original image, but also preserves the original information in the image, making the enhanced image more natural in appearance. FIMHE avoids the problems of excessive enhancement, high level of noise and severe image distortion, which are present in images enhanced by other HE-based methods. When compared with the state-of-the-art HE-based contrast enhancement methods, FIMHE preserves the texture details and retains the overall content of the original image while providing sufficient contrast. The enhanced images also have the most natural appearance. The proposed algorithm is simple but effective for image contrast enhancement. It operates in real time, and has low requirements on equipment which reduces its operational cost. Therefore, it can be applied in real-time applications that require image enhancement while preserving the overall image content.

#### REFERENCES

- B. Gupta and T. K. Agarwal, "Linearly quantile separated weighted dynamic histogram equalization for contrast enhancement," *Comput Electr Eng.*, vol. 62, pp. 360-374, 2017.
- [2] Yashu Rajput et al., "Advanced Image Enhancement Based on Wavelet and Histogram Equalization for Medical Images," *IOSR J Elect Communl.*, vol. 2, no 6, pp. 12-16, 2012.
- [3] X. Tan and B. Triggs, "Enhanced Local Texture Feature Sets for Face Recognition under Difficult Lighting Conditions," *IEEE Trans. on Image Processing.*, vol. 19, no. 6, pp. 1635-1650, 2010.
- [4] J. Sang et al., "An image watermarking technique based on cascaded iterative Fourier transform," *Optik*, vol. 124, no. 20, pp. 4522-4525, 2013
- [5] J. R. Tang and N. A. Mat Isa, "Bi-histogram equalization using modified histogram bins," Appl Soft Comput., vol. 55, pp. 31-43, 2017.
- [6] Y.T. Kim, "Contrast enhancement using brightness preserving bi-histogram equalization." *IEEE Trans. Consum. Electron.*, vol. 43, no. 1, pp. 1-8, 1997.
- [7] Yu W, Qian C, and Baeomin Z, "Image enhancement based on equal area dualistic sub-image histogram equalization method," *IEEE Trans. Consum. Electron.*, vol. 45, no. 1, pp 68-75, 1999.
- [8] S.D. Chen and A.R. Ramli, "Minimum mean brightness error bi-histogram equalization in contrast enhancement," *IEEE Trans. Consum. Electron.*, vol. 49, no. 4, pp. 1310-1319, 2003.
- [9] S.D. Chen and A.R. Ramli, "Contrast enhancement using recursive mean-separate histogram equalization for scalable brightness preservation," *IEEE Trans. Consum. Electron.*, vol. 49, no. 4, pp. 1301-1309, 2003.
- [10] K.S. Sim and C.P. Tso, Y.Y. Tan, "Recursive sub-image histogram equalization applied to gray scale images," *Pattern Recogn Lett.*, vol. 28, no. 10, pp. 1209-1221, 2007.
- [11] C.H. Ooi and N.S.P. Kong, H. Ibrahim, "Bi-histogram equalization with a plateau limit for digital image enhancement," *IEEE Trans. Consum. Electron.*, vol. 55, no. 4, pp. 2072-2080, 2009.
- [12] C.H. Ooi and N.A. Mat Isa, "Adaptive contrast enhancement methods with brightness preserving," *IEEE Trans. Consum. Electron.*, vol. 56, no. 4, pp. 2543-2551, 2010.
- [13] M. Abdullah-Al-Wadud, "A modified histogram equalization for contrast enhancement preserving the small parts in images," Int J Comput Sci Net., vol. 12, no. 2, pp. 1-4, 2012.

- [14] K. Singh and R. Kapoor, "Image enhancement using exposure based sub image histogram equalization," *Pattern Recogn Lett.*, vol. 36, no. 36, pp. 10-14, 2014.
- [15] P.B. Aquino-Morínigo et al., "Bi-histogram equalization using two plateau limits," *Signal Image Video P.*, vol. 11, no. 5, pp. 857-864, 2017
- [16] Hasikin K and N. A. M. Isa, "Adaptive fuzzy intensity measure enhancement technique for non-uniform illumination and low-contrast images," Signal Image Video P., vol. 9, no. 6, pp. 1419-1442, 2015.
- [17] K Singh, R Kapoor, and SK Sinha, "Enhancement of low exposure images via recursive histogram equalization algorithms," *Optik*, vol. 126, no. 20, pp. 2619-2625, 2015.
- [18] Y. Zhu and C. Huang, "An Adaptive Histogram Equalization Algorithm on the Image Gray Level Mapping," *Physics Procedia*, vol. 25, pp. 601–608, 2012.
- [19] K. Iqbal, R. Abdul Salam, A. Osman, and A. Zawawi Talib, "Underwater image enhancement using an integrated color model," *IAENG International Journal of Computer Science*, vol. 34, no. 2, pp. 239-244, 2007.
- [20] J.-C. Yoo and C. W. Ahn, "Image matching using peak signalto-noise ratio-based occlusion detection," *IET Image Process*, vol. 6, no. 5, pp. 483–495, 2012.
- [21] K. Liang, Y. Ma, Y. Xie, B. Zhou, and R. Wang, "A new adaptive contrast enhancement algorithm for infrared images based on double plateaus histogram equalization," *Infrared Phys Techn*, vol. 55, no. 4, pp. 309–315, 2012.
- [22] J. R. Tang and N. A. Mat Isa, "Adaptive Image Enhancement based on Bi-Histogram Equalization with a clipping limit," *Comput Electr Eng*, vol. 40, no. 8, pp. 86–103, 2014.
- [23] SD Chen and AR Ramli, "Minimum mean brightness error bi-histogram equalization in contrast enhancement," *IEEE Trans. Consum. Electron.*, vol. 49, no. 4, pp. 1310-1319, 2004.
- [24] N. Sengee and H. Choi, "A Novel Filter ed Bi-Histogram Equalization Method," *Journal of Korea Multimedia Society*, vol. 18, no. 6, pp. 691–700, 2015.
- [25] R. Aedla, G. Dwarakish, and D. V. Reddy, "Automatic Shoreline Detection and Change Detection Analysis of Netravati-GurpurRivermouth Using Histogram Equalization and AdaptiveTresholding Techniques," Aquatic Procedia, vol. 4, pp. 563–570, 2015
- [26] L. Maurya, P. K. Mahapatra, and A. Kumar, "A social spider optimized image fusion approach for contrast enhancement and brightness preservation," *Appl Soft Comput*, vol. 52, pp.575–592, 2017.
- [27] Z. Wang et al., "Image quality assessment: From error visibility to structural similarity," *IEEE Trans. Image Process.*, vol. 13, no. 4, pp. 600-612, 2004.
- [28] M. Hanmandlu, O. P. Verma, N. K. Kumar, and M. Kulkarni, "A novel optimal fuzzy system for color image enhancement using bacterial foraging," *IEEE T Instrum Meas*, vol. 58, no. 8, pp. 2867–2879, 2009.
- [29] S.-C. Huang, F.-C. Cheng, and Y.-S. Chiu, "Efcient contrast enhancement using adaptive gamma correction with weighting distribution," *IEEE T Image Process*, vol. 22, no. 3, pp. 1032–1041, 2013
- [30] Tan, Hui Li, "A Perceptually Relevant MSE-Based Image Quality Metric," *IEEE Transactions on Image Processing*, vol. 22, no. 11, pp. 4447-4459, 2013.
- [31] Qian, Jiansheng, "Image quality assessment based on multi-scale representation of structure," *Digital Signal Processing*, vol. 33, no. 3, pp. 125–133, 2014.
- [32] Brunet, Dominique, E. R. Vrscay, and Z. Wang, "On the Mathematical Properties of the Structural Similarity Index," *IEEE Transactions on Image Processing*, vol. 21, no. 4, pp. 1488–1499, 2012.
- [33] Han, G., and B. Lin, "Optimal sampling and reconstruction of undersampled atomic force microscope images using compressive sensing," *Ultramicroscopy*, vol. 633, no. 3, pp. 85–94, 2018.
- [34] D. Lee and S. Lim, "Improved structural similarity metric for the visible quality measurement of images," *J Electron Imaging.*, vol. 25, no. 6, pp. 063015, 2016.
- [35] Koloda, Ján, "Scalable Kernel-Based Minimum Mean Square Error Estimator for Accelerated Image Error Concealment," *IEEE Transactions on Broadcasting*, vol. 63, no. 1, pp. 59–70, 2017.
- [36] Contan C, Kirei B S, Topa M D, "Error-dependent step-size control of adaptive normalized least-mean-square filters used for nonlinear acoustic echo cancellation," Signal Image & Video Processingvol, vol. 10, no. 3, pp. 511–518, 2016.
- [37] J. R. Tang and N. A. M Isa, "Adaptive Image Enhancement based on Bi-Histogram Equalization with a clipping limit," *Comput Electr Eng.*, vol. 40, no. 8, pp. 86-103, 2014.



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