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# Contact Force Estimation in the Railway Vehicle Wheel-Rail Interface

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**Abstract:** Increased patronage of railways in the UK in the past 20 years has put demands on rolling stock to operate at peak availability with reduced time available for maintenance. One possible tool to enable this is the use of real time fault detection and diagnosis on board railway vehicles to detect faulty components and provide information about the current running condition of the system. This paper discusses the development of one such technique for the estimation of creep forces of the wheel-rail contact. Real time knowledge of which could be used to predict wear of the wheel tread and rail head, predict the formation of rolling contact fatigue, and identify any areas of low adhesion present on the network. The paper covers development of a full vehicle nonlinear contact mechanics model, development of the Kalman-Bucy filter estimation technique and how the technique will be developed and validated in the future.

*Keywords:* Accelerometers, Fault Diagnosis/Detection, Kalman Filters, Nonlinear Systems, Railways, Vehicle Dynamics

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## 1. INTRODUCTION

The railway industry in the United Kingdom has seen something of a renaissance in the past 20 years with annual increases in passenger numbers and tonnage of freight hauled, putting demands on rolling stock to be available for a greater proportion of the time. This results in a reduction in maintenance availability and a requirement to better understand the current running conditions so that timetables can be tailored to the peak operating capability of the current rolling stock.

A key tool in improving the capability of the system is the use of condition monitoring systems on board railway vehicles to detect faults and estimate running conditions in real time. The railway industry is starting the transition to this philosophy with systems such as the Bombardier ORBITA, Bombardier (2010). In academia many condition monitoring schemes have been investigated, such as: condition monitoring of suspension components, Li et al. (2006); wheel-rail profile estimation, Ward et al. (2010a); wheel speed measurement, Mei and Li (2008) and creep force detection, Charles et al. (2008).

This paper highlights development of an estimation technique to determine, in real time, the creep forces of the wheel rail interface. Estimation of these forces has potentially many benefits as currently this can only be measured with specially instrumented trains, the technology from which would be prohibitively expensive to install on all service vehicles. Creep forces fundamentally provide the guidance mechanism of the wheelset system by dissipating energy in the contact area, Wickens (2003). As such creep forces and moments are a key part of the mechanism for wheel and rail head wear, the generation of rolling contact fatigue of the rail head and the amount of adhesion that

is present for traction and braking. Force estimation in real time on each vehicle on the network will provide information by which it is possible to detect: the wear of the system to provide more targeted maintenance regimes; and areas of low adhesion so that mitigation such as rail head cleaning and treatment could be better deployed, Vasic et al. (2003). This paper is focused upon the estimation of creep forces, detection of the issues highlighted using the data provided by estimation is the subject of on-going research.

A number of ideas have been proposed to detect the running condition of the wheel-rail interface that use low cost inertial sensing mounted on the vehicle and advanced processing, such as: multiple Kalman filters to estimate creep coefficients, Hussain and Mei (2010); inverse modelling for the estimation of creep forces, Xia et al. (2008); and as first proposed in Charles et al. (2008) and further developed here, a Kalman-Bucy filter estimation of linearised creep forces, initially aimed at detecting local adhesion conditions. This paper therefore covers the nonlinear contact mechanics modelling of a full bodied vehicle, with two bogies and four wheelset. It then covers the Kalman-Bucy filtering estimation technique, with preliminary simulation results shown. Finally it discusses how the technique will be developed in the future and plans for experimental validation.

## 2. SYSTEM MODEL

Previous studies into creep force estimation have looked at a half vehicle models only, Charles et al. (2008), Ward et al. (2010b), where just one bogie system is considered, with the vehicle body constrained in yaw. This model has been sufficient for formative theoretical studies, however it demonstrated some discrepancies in the observability

of various creep forces at different parts on the vehicle system, with the estimated lateral creep force of the trailing wheelset giving best correlation to the modelled creep force. Therefore this study is looking into the best candidate creep forces for detection on a more representative system.

The current study considers a vehicle model with a full length body no longer constrained in yaw, plus two bogies with the accompanying four wheelsets, Figure 1. As with previous studies this model only considers the lateral and yaw directions, as the longitudinal and vertical effects can be satisfactorily neglected, Wickens (2003).

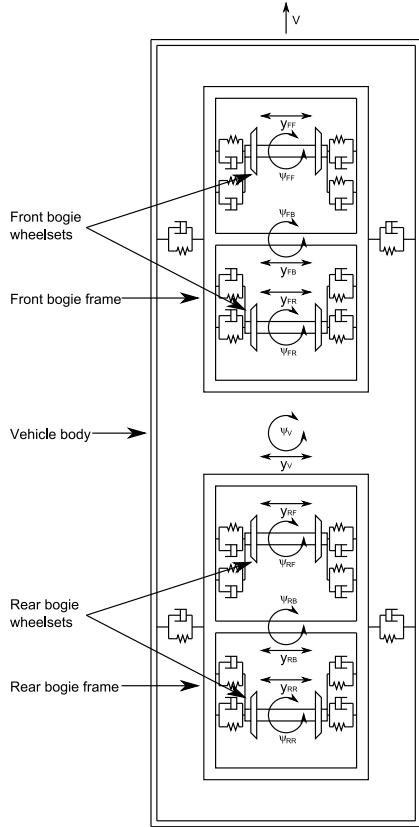


Fig. 1. Vehicle system plan view model

A detailed description of the development of railway vehicle dynamics can be found in Garg and Dukkipati (1984), with the rigid body dynamics for the simulation model given below by equations 1 to 14. These equations encompass lateral and yaw dynamics for the four wheelsets, two bogies and the vehicle body.

$$m_{FF}\ddot{y}_{FF} = F_{LyFF} + F_{RyFF} + F_{syFF} + F_{gFF} \quad (1)$$

$$I_{FF}\ddot{\psi}_{FF} = F_{LyFF}R_{LxFF} - F_{LxFF}R_{LyFF} + F_{RyFF}R_{RxFF} - F_{RxFF}R_{RyFF} + M_{s\psi FF} + M_{gFF} \quad (2)$$

$$m_{FR}\ddot{y}_{FR} = F_{LyFR} + F_{RyFR} + F_{syFR} + F_{gFR} \quad (3)$$

$$I_{FR}\ddot{\psi}_{FR} = F_{LyFR}R_{LxFR} - F_{LxFR}R_{LyFR} + F_{RyFR}R_{RxFR} - F_{RxFR}R_{RyFR} + M_{s\psi FR} + M_{gFR} \quad (4)$$

$$m_{RF}\ddot{y}_{RF} = F_{LyRF} + F_{RyRF} + F_{syRF} + F_{gRF} \quad (5)$$

$$I_{RF}\ddot{\psi}_{RF} = F_{LyRF}R_{LxRF} - F_{LxRF}R_{LyRF} + F_{RyRF}R_{RxRF} - F_{RxRF}R_{RyRF} + M_{s\psi RF} + M_{gRF} \quad (6)$$

$$m_{RR}\ddot{y}_{RR} = F_{LyRR} + F_{RyRR} + F_{syRR} + F_{gRR} \quad (7)$$

$$I_{RR}\ddot{\psi}_{RR} = F_{LyRR}R_{LxRR} - F_{LxRR}R_{LyRR} + F_{RyRR}R_{RxRR} - F_{RxRR}R_{RyRR} + M_{s\psi RR} + M_{gRR} \quad (8)$$

$$m_{FB}\ddot{y}_{FB} = -(F_{syFF} + F_{syFR} + F_{syVF}) \quad (9)$$

$$I_{FB}\ddot{\psi}_{FB} = -(M_{s\psi FF} + M_{s\psi FR} + M_{s\psi VF} + L(F_{syFF} - F_{syFR})) \quad (10)$$

$$m_{RB}\ddot{y}_{RB} = -(F_{syRF} + F_{syRR} + F_{syVR}) \quad (11)$$

$$I_{RB}\ddot{\psi}_{RB} = -(M_{s\psi RF} + M_{s\psi RR} + M_{s\psi VR} + L(F_{syRF} - F_{syRR})) \quad (12)$$

$$m_V\ddot{y}_V = F_{syVF} + F_{syVR} \quad (13)$$

$$I_V\ddot{\psi}_V = M_{s\psi VF} + M_{s\psi VR} \quad (14)$$

where  $F_{ijkl}$ ,  $R_{ijkl}$ ,  $M_{i\psi kl}$  are the forces (creep, gravitational and suspension), positions and moments,  $m_{kl}$  is the mass,  $I_{kl}$  is the moment of inertia,  $y_{kl}$  is the lateral position,  $\psi_{kl}$  is the yaw angle; where  $i = L$ (left),  $R$ (right),  $s$ (uspension);  $j = x$  (longitudinal),  $y$  (lateral);  $k = F$ (ront bogie),  $R$ (rear bogie),  $V$ (vehicle);  $l = F$ (ront wheelset),  $R$ (rear wheelset),  $B$ (ogie)

The accompanying suspension forces and moments (for small angles) for the primary and secondary suspension are given by equations 15 to 26.

$$F_{syFF} = k_{y1}y_{BF} + k_{y1}L\psi_{BF} - k_{y1}y_{FF} + f_{y1}\dot{y}_{BF} + f_{y1}L\dot{\psi}_{BF} - f_{y1}\dot{y}_{FF} \quad (15)$$

$$M_{s\psi FF} = k_{\psi 1}(\psi_{BF} - \psi_{FF}) + f_{\psi 1}(\dot{\psi}_{BF} - \dot{\psi}_{FF}) \quad (16)$$

$$F_{syFR} = k_{y1}y_{BF} - k_{y1}L\psi_{BF} - k_{y1}y_{FR} + f_{y1}\dot{y}_{BF} - f_{y1}L\dot{\psi}_{BF} - f_{y1}\dot{y}_{FR} \quad (17)$$

$$M_{s\psi FR} = k_{\psi 1}(\psi_{BF} - \psi_{FR}) + f_{\psi 1}(\dot{\psi}_{BF} - \dot{\psi}_{FR}) \quad (18)$$

$$F_{syRF} = k_{y1}y_{BR} + k_{y1}L\psi_{BR} - k_{y1}y_{RF} + f_{y1}\dot{y}_{BR} + f_{y1}L\dot{\psi}_{BR} - f_{y1}\dot{y}_{RF} \quad (19)$$

$$M_{s\psi RF} = k_{\psi 1}(\psi_{BR} - \psi_{RF}) + f_{\psi 1}(\dot{\psi}_{BR} - \dot{\psi}_{RF}) \quad (20)$$

$$F_{syRR} = k_{y1}y_{BR} - k_{y1}L\psi_{BR} - k_{y1}y_{RR} + f_{y1}\dot{y}_{BR} - f_{y1}L\dot{\psi}_{BR} - f_{y1}\dot{y}_{RR} \quad (21)$$

$$M_{s\psi RR} = k_{\psi 1}(\psi_{BR} - \psi_{RR}) + f_{\psi 1}(\dot{\psi}_{BR} - \dot{\psi}_{RR}) \quad (22)$$

$$F_{syVF} = -k_{y2}y_V - f_{y2}\dot{y}_V + k_{y2}y_{BF} + f_{y2}\dot{y}_{BF} - k_{y2}c\psi_V - f_{y2}c\dot{\psi}_V \quad (23)$$

$$M_{s\psi VF} = -k_{y2}c^2\psi_V - f_{y2}c^2\dot{\psi}_V + k_{y2}c y_V + f_{y2}c\dot{y}_V - k_{y2}c y_{BF} - f_{y2}c\dot{y}_{BF} \quad (24)$$

$$F_{syVR} = -k_{y2}y_V - f_{y2}\dot{y}_V + k_{y2}y_{BR} + f_{y2}\dot{y}_{BR} + k_{y2}c\psi_V + f_{y2}c\dot{\psi}_V \quad (25)$$

$$M_{s\psi VR} = -k_{y2}c^2\psi_V - f_{y2}c^2\dot{\psi}_V - k_{y2}c y_V - f_{y2}c\dot{y}_V - k_{y2}c y_{BR} - f_{y2}c\dot{y}_{BR} \quad (26)$$

where  $k_{mn}$  and  $f_{mn}$  are the suspension stiffness and damper coefficients; with  $m = y$ (lateral) or  $\psi$ (yaw);  $n = 1$ (primary suspension),  $2$ (secondary suspension).

Creep forces fundamentally provide the guidance mechanism for the wheelsets. These forces are generated in reaction to the creeps (or slips) in the rolling contact of the wheel-rail interface in normal running, these are relative

velocities of the wheel and the rail in the contact area and are defined as

$$s_i = \frac{w_i}{V}, \quad i = x, y \quad (27)$$

where  $V$  is the forward velocity of the wheelset,  $w_i$  is the creep (slip) velocity in the relevant direction (where  $x$  is longitudinal direction and  $y$  is lateral direction), where this is defined as

$$w_i = V_w - V_r, \quad i = x, y \quad (28)$$

where  $V_w$  is the velocity of the wheel through the contact patch, and  $V_r$  is the velocity of the rail through the contact patch. Creep generation is a highly nonlinear process, however effects of hysteresis can be ignored due to this being a single direction rolling contact.

Normal practice for wheel-rail contact modelling is to linearise the creep forces generated in the model based upon Kalker coefficients, Kalker (1967). Due to the importance here of modelling the non-linear adhesion characteristics up to and beyond the creep saturation, use is made of the contact force model developed in Polach (2005). This is essentially a practical curve fitting mechanism, where the creep force (excluding spin effects) are calculated as

$$F = \frac{2Q\mu}{\pi} \left( \frac{\epsilon}{1 + \epsilon^2} + \arctan\epsilon \right) \quad (29)$$

where  $Q$  is the wheel load, with

$$\epsilon = \frac{2C\pi a^2 b}{3Q\mu} s \quad (30)$$

where  $C$  is the proportionality coefficient of the contact shear stiffness ( $N/m^3$ ). Kalker coefficients can be used for this purpose, where for the longitudinal direction

$$\epsilon_x = \frac{1}{4} \frac{G\pi abc_{11}}{Q\mu} s_x \quad (31)$$

where  $s_x$  is the longitudinal component of the total creep  $s$

$$s = \sqrt{s_x^2 + s_y^2} \quad (32)$$

The forces  $F_x$ ,  $F_y$  in the longitudinal and lateral directions are

$$F_i = F \frac{s_i}{s}, \quad i = x, y \quad (33)$$

and the adhesion coefficients

$$f_i = \frac{F_i}{Q}, \quad i = x, y \quad (34)$$

The friction coefficients rely upon the slip velocity, where

$$\mu = \mu_0 [(1 - A) e^{-Bw} + A] \quad (35)$$

$A$  is the ratio of limit friction coefficient at infinity slip velocity  $\mu_\infty$  to the maximum friction coefficient  $\mu_0$

$$A = \frac{\mu_\infty}{\mu_0} \quad (36)$$

For large creep applications the force is worked out using reduction factors,  $k_A$  in the area of adhesion and  $k_S$  in the area of slip, as

$$F = \frac{2Q\mu}{\pi} \left( \frac{k_A \epsilon}{1 + (k_A \epsilon)^2} + \arctan(k_S \epsilon) \right), \quad k_S \leq k_A \leq 1 \quad (37)$$

where

$$k = \frac{k_A + k_S}{2} \quad (38)$$

Experimentation has shown that, contrary to expectation from theoretical models such as that of Kalker, Kalker

(1967), the initial slope of the creep curve varies with different adhesion levels, Pearce and Rose (1985), Harrison and McCanney (2002). Four levels of adhesion are defined in this study as dry, wet, low and very low conditions. The accompanying constants are given in Table 1 and the creep curves are given in Figure 2. This varying slope means that different adhesion levels should be feasibly detected without the system becoming saturated. The effect of varying the adhesion levels on the running system is shown in Figure 3. This shows the sum of the lateral creep forces and gravitational stiffnesses for the rear bogies front wheelset and demonstrates that for the same system disturbance (i.e. the lateral position of the track), the creep forces generated reduces as the friction levels reduce, meaning that detection of changes of adhesion level is feasible in practice.

Model parameter	Dry	Wet	Low	Very Low
$k_A$	1.00	1.00	1.00	1.00
$k_S$	0.40	0.40	0.40	0.40
$\mu_0$	0.55	0.30	0.06	0.03
$A$	0.40	0.40	0.40	0.40
$B$	0.60	0.20	0.20	0.10

Table 1. Polach contact model parameters

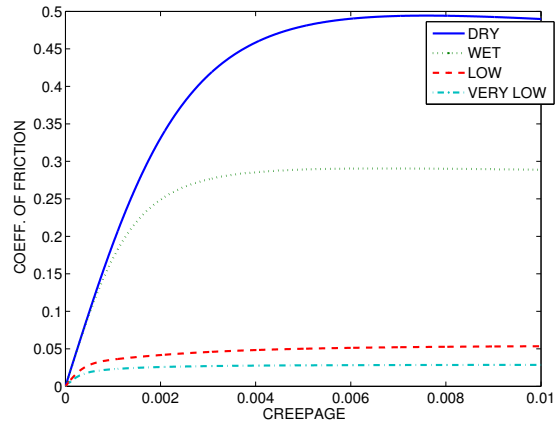


Fig. 2. Creep curves for varying adhesion conditions

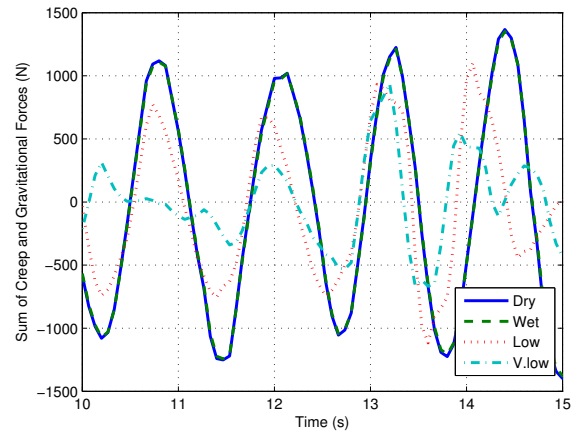


Fig. 3. Lateral creep forces for varying adhesion conditions



Parameter	Description	Value	Units
$f_{y1}$	primary lateral damper CoE	0	Ns/m
$f_{\psi 1}$	primary yaw damper CoE	0	Nms
$f_{y2}$	secondary lateral damper CoE	$0.06e^6$	Ns/m
$I_b$	bogie yaw inertia	3500	kgm <sup>2</sup>
$I_v$	vehicle yaw inertia	30000	kgm <sup>2</sup>
$I_w$	wheelset yaw inertia	700	kgm <sup>2</sup>
$k_{y1}$	primary lateral stiffness	$40e^6$	N/m
$k_{y2}$	secondary lateral stiffness	$0.1e^6$	N/m
$k_{\psi 1}$	primary yaw stiffness	$2.5e^6$	Nm
$m_b$	bogie mass	2500	kg
$m_v$	vehicle mass	1250	kg
$m_w$	wheelset mass	22000	kg
$y_{FF}$	front bogie, front wheelset displacement	-	m
$y_{FR}$	front bogie, rear wheelset displacement	-	m
$y_{RF}$	rear bogie, front wheelset displacement	-	m
$y_{RR}$	rear bogie, rear wheelset displacement	-	m
$\psi_{FF}$	front bogie, front wheelset yaw angle	-	rad
$\psi_{FR}$	front bogie, rear wheelset yaw angle	-	rad
$\psi_{RF}$	rear bogie, front wheelset yaw angle	-	rad
$\psi_{RR}$	rear bogie, rear wheelset yaw angle	-	rad

Table 2. Model parameters

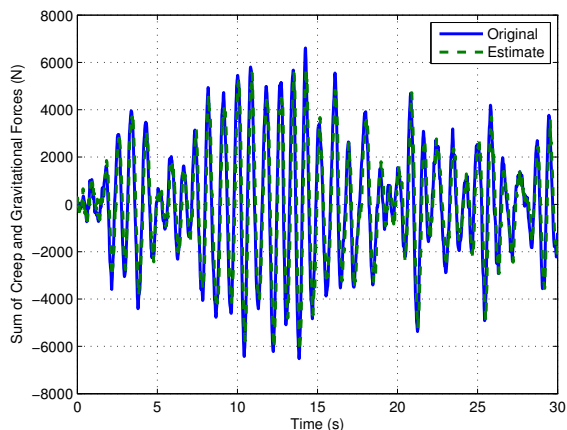


Fig. 4. Estimation of the lateral creep forces

Creep force/moment	Dry $R^2$ (%)	Wet $R^2$ (%)	Low $R^2$ (%)	V.Low $R^2$ (%)
$F_{FF}$	83.64	82.95	69.94	65.10
$F_{FR}$	85.12	84.90	79.26	73.44
$F_{RF}$	85.03	84.28	73.64	71.88
$F_{RR}$	85.13	85.14	72.76	65.35

Table 3. Lateral creep forces fit quality

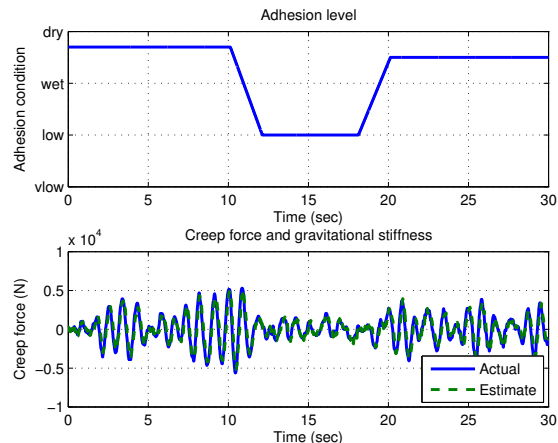


Fig. 5. Varying adhesion estimation

#### 4. FUTURE WORK

This study provides a strong theoretical background for a project on on-board detection of low adhesion which started in 2010, administered by the Rail Safety and Strategy Board (RSSB) with funding from the UK's Rail Industry Strategic Research Program. The project has several facets: further development of the data processing algorithms as shown here; how these estimates can be translated into a useful understanding of the adhesion condition; fundamental research into creep characteristics at low creep values using a scale roller rig; and validation of the techniques through data generated by a multi-bodied dynamic simulation package (such as VAMPIRE®) and data gathered from a full scale instrumented vehicle.

The intention is also to consider the force estimation technique for many other applications. This could be used for assessing the performance of railway vehicles in terms of the wheel and rail geometric and wear characteristics, perhaps as part of a homologation process. As mentioned earlier this is considered a simpler and cheaper alternative to the use of load measuring wheels which is the current practice. Beyond a homologation process, the technique if applied to a large number, or the majority of the vehicles on the network could be used to help in the prediction wear of the wheel tread, wear of the rail head and it could also be used predict the occurrence of rolling contact fatigue. These latter two points which consider the condition of the infrastructure would require extremely accurate coordination of the position of the vehicle on the network to the forces being estimated, and a study would also have to be generated as to how these forces relate the presence of patterns of wear and fatigue phenomena.

#### 5. CONCLUSIONS

This paper discussed development work of the creep force estimation technique around the wheel-rail interface. The primary aim of this research is to develop a real-time system for the estimation of creep forces that could be used to detect local adhesion conditions, and predict the wear generated on the vehicle and the rail infrastructure.

Firstly this paper discussed the development of a full vehicle body non-linear contact mechanics model of the lateral

and yaw dynamics of the system. This was performed as previous studies highlighted that some of the lateral creep forces and creep moments gave a better estimation than others, and this needed to be investigated in a more representative model of a rail vehicle system.

It then discussed the Kalman-Bucy filter method used to estimate the lateral creep forces and the yaw creep moments of the four wheelset in the model, and how these have given successful estimations in simulations.

Finally the future direction of the project was highlighted with further development potential of the algorithm given, and an explanation of the methods of validation that will be used, by data generated in multi-bodied dynamics simulation software and through track testing. Suggestions were also given for other applications of the creep force estimations.

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