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## Statistical Representation Of A Hybrid Photovoltaic- Wind System for Controller Design

by

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| Date: | 29.07 .1995 |

Submitted in partial fulfillment of the requirements for the award of A Master of Philosophy of the Loughborough University of Technology.
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## 1. Introduction

This paper considers an autonomous, terrestrial energy supply plant applying renewable energy sources. It presents a mathematical model whose purpose is to gain an in-depth understanding of the impact of fluctuations of the wind speed and the intensity of the sun on the power supply of such an energy system. Results could then be used to design a controller that operates the system. The system with its four core elements is depicted in Fig. 1.1.


Fig. 1.1: Hybrid Energy System

They are a wind turbine, a photovoltaic array, a battery and a diesel engine. The controller receives data from these components and manages them. The electric energy generated by the system is provided for the user.

Combined Wind- PV- Diesel- systems do mainly compete with Diesel stand-alone systems, Wind- Diesel- systems and the connection to the mains. These island systems are typically
designed for a rated power of up to several 10 kW . They are supposed to operate on remote sites where a connection to the mains is not given.
(1) Diesel Stand- alone systems are the most common systems for decentral energy supply. Eventhough they are the cheapest option - as far as the investment costs are concerned - they might not be the best. And this is for three reasons. First, a diesel uses an energy source with a limited range. Second, the combustion of crude oil products causes ecological problems. Third, in remote areas the price for fossil fuels might be significantly higher than in urban areas, thus leading to a steep increase of the actual cost of a KWh . Moreover, in remote areas the required regular service might either not be asserted or costly.
(2) Wind- Diesel- systems are one option to cut down on the fossil fuel consumption. Since the renewable energy supply (i.e. wind speed) fluctuates considerably, a diesel generator is necessary to ensure high reliability. As high wind speeds and high solar insolation are often complementary, it is supposed that the photovoltaic array may fill in the gap when the wind turbine does not produce enough energy and vice versa, thus justifying the additional investment of the photovoltaic array.
(3) Connection to the national grid, which is fed by conventional power plants. This option has to be ruled out for many a site such as islands far away from the mainland. Where possible at all however, the investment of the connection is likely to be fairly expensive as the costs for it increase with decreasing population density. Moreover, centrally fed mains with a large area extension are susceptible to faults.

Fig. 1.2 shows the system in more detail. It consists of a wind turbine and a photovoltaic array as the renewable energy sources, a battery as an energy storage unit and a fossil fuel generator (diesel engine) for backup in order to guarantee a power supply at all times. The battery is supposed to fill in short- term gaps in the energy supply by the renewable sources, thus smoothing the power supply function and reducing the number of diesel starts. Depending on the load that has to be supplied, the load might be directly connected to the DC- Bus or via a DC/AC- converter.


Fig. 1.2: Autonomous Wind- PV- System

Since both wind speed and solar intensity do vary considerably, the power supplied by the renewable energy sources will vary too. Therefore, the general problem in the performance of renewable energy systems is the matching of energy production and load. As far as the energy producing components, the PV array, the wind generator, the diesel and the battery, are concerned, it is assumed that standard components are used, thus restricting the controller to the interaction within the ensemble. The controller will therefore be in charge of the charging and discharging of the battery, the start-stop- policy for the fossil fuel generator, the maximum power tracking for the Photovoltaic array and its positioning. It is furthermore conceivable to switch on additional loads if there is a surplus energy in order to reduce the amount of dumped energy. These additional loads could produce storable goods as drinking or hot water. To assist the controller in its management data will be fed in from all components in regular time intervals. Hence, it will be informed of the current wind speed, current intensity of the sun, state of charge of the battery and the load demand.

The purpose of this paper is to provide a mathematical model that reflects this scenario and is able to support the controller in its decision making. The focus of this model is the mathematical formulation of the stochastic processes "wind speed" and "solar intensity". They can be transformed by applying simple models for the wind turbine and the photovoltaic array into the stochastic processes "wind turbine power" and "solar power". These algorithms allow to calculate time series, resulting in a short term prediction of the power supply, delivering data that can be used by the controller to decide on the best policy in order to minimize the operational costs of the system. The point that should be stressed here is that this model is a short term model which allows to plan ahead over time periods of the order of up to one hour by using hourly data from various sensors. This is supposed to enable the controller to operate the system in an efficient way. For the best sizing of the components, howeyer, it is necessary to consider meteorological data of the site in question over a longer period.

Physical aspects of the energy sources which the model is based on are discussed in chapter 2 , followed by the discussion of the energy converters (i.e. wind turbine, photovoltaic array, battery and diesel) in chapter 3 . The statistical methods are then taken further in chapter 4. It will focus on the probability distribution of the power supplied by the renewable energy sources, followed by a section on the generation of synthetic time series of the power supply, including both renewable energy sources and the battery. The last section of this chapter discusses first passage time problems. The first passage time is the expected time when the power surpasses a certain passage level for the first time. This is useful for instance in the event that the renewable energy sources do not provide enough energy to meet the demand. If it is expected that this will be the case for a longer time period it might be worth switching on the diesel. If not, the power might as well be supplied by the battery in order to avoid switching the diesel on and off too often. Here, the first passage time provides useful information. Chapter 5 , eventually, gives a summary by restating the main points.

The algorithms presented in this paper have been coded in $\mathrm{C}++$ for a Windows 3.1 environment using the Borland $\mathrm{C}++3.1$ compiler and the Borland Object Windows $\mathrm{C}++1.0$ library. The relevant graphs in this paper have been created using Word Perfect Presentation

[^0]to which a data interface is provided by the program. The mostly interactive program is described in the Appendix II, where a complete class reference and a description of global functions are given.

## 2. Energy Sources

### 2.1 Wind Energy

### 2.1.1 Wind Speed Power Spectrum - Empirical Results

The spectral density function of the horizontal wind speed is largely dependant on the location where the speed was monitored. The characteristics of different sites, however, reveal distinctive similarities. A generic spectrum ([19]) is shown in Fig. 2.1.


Fig. 2.1: Generic Wind Speed Spectrum

## (1) Micrometeorological range

The peak in the high frequency range is caused by fluctuations called atmospheric turbulence. The energy of the fluctuations is centered around a period of around 1 minute. They can be approximated by the Ornstein- Uhlenbeck process ([25]), a stochastic model process. The micrometeorological range will be discussed in more detail detail in 2.1.2.
(2) Spectral gap

A striking phenomenon of a typical wind speed spectrum is a spectral gap between time periods of 10 minutes and 2 hours ([19]).
(3) Macrometeorological range

Large- scale movements of air masses account for three peaks on the macrometeorological side of the spectrum. The relative maximum at a diurnal time period is due to different temperature gradients at day and night. This effect is likely to be more distinctive at coastal sites as the air temperature on shore decreases more rapidly during night time than off shore. Depressions and anti- cyclones usually occur with periods of about four days which explains the second maximum of the spectrum. Again the pattern here is that the peak will be more distinctive in oceanic climates rather than continental. The peak at the one- year period in contrast is likely to vary with the degree of latitude. It will vanish at sites in close proximity to the equator. Some aspects of the macrometeorological range will be discussed in more detail in chapter 2.1.3

The peak in the micrometeorological range allows a short term prediction of the wind speed. Here, "short term" indicates time periods that fall into the spectral gap, i.e. between 10 minutes and one hour. Within this short term model a constant average hourly wind speed and standard deviation are assumed. These macrometeorological, hourly data can be derived from measured data. So far, what is said here, only applies to the wind speed distribution. In chapter 2.2.4 it will be shown, however, that the solar power spectrum too, can be seperated into a short term and a long term range. Hence, it will follow the same pattern: For short term considerations a statistical model will be used, whereas hourly values for the beam intensity are taken from a data feeder. Usually, the data feeder will hold current data. For optimization purposes, however, it could as well hold historical data taken from a specific site over a week or a month.

### 2.1.2 Turbulence: The Micrometeorological Range

### 2.1.2.1 Definitions

Turbulence includes all fluctuations with frequencies higher than the quasi- steady mean wind speed variation. If we assume the mean wind speed to be constant over a sufficiently
short time period, $\bar{v}(t)=\bar{v}$, the wind speed of the fluctuation will be defined by ([19], 2.15)

$$
\begin{equation*}
v_{\lambda}(t)=v(t)-\bar{V}, \tag{2.1}
\end{equation*}
$$

the difference between the instantaneous wind speed $v(t)$ and the mean wind speed $\bar{v}$. The variance of the turbulence will then be

$$
\begin{equation*}
\operatorname{Var}(V)=\int_{-\infty}^{\infty}(v-\bar{v})^{2} f_{v}(v) \mathrm{d} v \tag{2.2}
\end{equation*}
$$

where $f_{v}(v)$ is the probability density function with respect to the wind speed $v$. The index $v$ signals that V is the random variable. It is worth noting that the argument of the variance operator in (2.2) is capital V. Throughout this paper random variables will be referred to by capital letters, their realizations by small ones ${ }^{1}$. Given n realizations of the instantenous speed, $v_{j}(j=1 . . n)$, the empirical variance of the turbulence can be estimated from

$$
\begin{equation*}
\sigma_{v}^{2}=\frac{1}{n-1} \sum_{j=1}^{n}\left(v_{j}-\bar{v}\right)^{2} \tag{2.3}
\end{equation*}
$$

The turbulence intensity is defined as the quotient ([19], 2.17)

$$
\begin{equation*}
I_{v}=\frac{\sigma_{v}}{\bar{v}} \tag{2.4}
\end{equation*}
$$

### 2.1.2.2 Turbulence and the Ornstein- Uhlenbeck Process

Wind fluctuations over a restricted time interval can be represented by the OrnsteinUhlenbeck process, which also describes the velocity of free particles in Brownian motion. The random variable related to the velocity will be called V. In order to condense and simplify the formulas involved let us introduce the normalizations of the time axis,

[^1]\[

$$
\begin{equation*}
\tau=\beta t \tag{2.5}
\end{equation*}
$$

\]

with the time constant $\beta_{v}$, and the normalization of $v$,

$$
\begin{equation*}
\xi(t)=\frac{v(t)-\bar{v}}{\sigma} \tag{2.6}
\end{equation*}
$$

with the deviation $\sigma$. Both parameters $\tau$ and $\xi$ are thus dimensionless and their significance will prove to be self- explanatory after the following remarks. The random variable that stands for the normalized process will be $\Xi$. It is beyond the scope of this paper to elaborate on the physical details of the Ornstein- Uhlenbeck process. The O.U. - process is a continuous time Markov process whose probability density function $\varrho(\xi, \tau)$ has to satisfy the Fokker- Planck equation, which has the form

$$
\begin{equation*}
\frac{\partial \varrho(\xi, \tau)}{\partial \tau}=\frac{\partial^{2} \mathrm{e}(\xi, \tau)}{\partial \xi^{2}}+\frac{\partial}{\partial \xi}[\xi \varrho(\xi, \tau)] \tag{2.7}
\end{equation*}
$$

in the special case of the O.U. - process. The value $\varrho(\xi, \tau) \mathrm{d} \xi$ is the probability that, at time $\tau$, the wind speed lies in the interval $[\xi, \xi+d \xi]$ subjected to an initial condition $\varrho(\xi, 0)=h(\xi)$ at time $\tau=0$. A solution will be given later.
It may be noted that a discrete realization of an Ornstein- Uhienbeck process is the Ehrenfest model of diffusion ([14], p.343), which can be interpreted as a diffusion with a central force. That is a random walk in which the probability of a step in one direction varies with the position.

## (i) Power Spectrum and Autocorrelation Function

The power spectrum of the Ornstein- Uhlenbeck process as a function of the angular frequency $\omega$,

$$
\begin{equation*}
S_{\xi \xi}(\omega)=\frac{2}{\omega^{2}+\beta^{2}} \tag{2.8}
\end{equation*}
$$

is Lorenzian with the corresponding autocorrelation function ${ }^{2}$

$$
\begin{equation*}
R_{\xi \xi}(\tau)=\exp (-|\tau|) \tag{2.9}
\end{equation*}
$$

Please bear in mind that $\tau$ in (2.9) is normalized via (2.5). In the frame of the description of wind turbulence it is sometimes referred to as Dryden spectrum. For the sake of simplicity we will usually refer to the autocorrelation function (2.9) via the short hand $r=R_{\xi \xi}(\tau)$ or in its unnormalized form $r_{v}=R_{\xi \xi}\left(\beta_{v} t\right)$.

## (ii) The Probability Density Function

The probability density function $\varrho(\xi, \tau)$ is the solution of the Fokker- Planck equation (2.7). In this section we assume boundary conditions to satisfiy $\varrho(\infty, \tau)=\varrho(-\infty, \tau)=0$. These are two physically sensible conditions to avoid infinite wind speeds. In the first step the special initial condition $\varrho(\xi, 0)=\delta\left(\xi-\xi_{0}\right)$ is considered. In this case, $\varrho(\xi, \tau)=\varrho\left(\xi, \tau ; \xi_{0}\right)$, is the probability density under the condition that a wind speed $\xi_{0}$ has been observed at time $\tau=$ 0 . The solution is ([20], eq.3.40) given by

$$
\begin{equation*}
\varrho\left(\xi, \tau ; \xi_{0}\right)=\frac{1}{\sqrt{2 \pi\left(1-r^{2}\right)}} \exp \left[-\frac{1}{2} \frac{\left(\xi-\xi_{0} r\right)^{2}}{1-r^{2}}\right] \tag{2.10}
\end{equation*}
$$

This is identical to the probability density function of a bivariate standard normal probability density function with correlation coefficient r (compare with equation 6.23). In fact, $\varrho\left(\xi, \tau ; \xi_{0}\right)$ can be thought of as a Gaussian curve whose peak wanders with $\tau$ towards $\xi=0$ while becoming broader. Other methods of solving the Fokker-Planck equation are discussed for example in [34]. Actually, (2.10) can be interpreted as Green's function of the given boundary problem. Consequently, the probability density function for any initial condition $\varrho(\xi, 0)=h(\xi)$ can be obtained by convoluting Green's function with the initial condition:

$$
\begin{equation*}
\varrho(\xi, \tau)=<\varrho\left(\xi, \tau ; \xi_{0}\right)|h(\xi)\rangle=\int_{-\infty}^{\infty} \varrho\left(\xi, \tau ; \xi_{0}\right) h\left(\xi_{0}\right) d \xi_{0} \tag{2.11}
\end{equation*}
$$

[^2]Equation (2.11) is actually generally valid: Green's function gives the solution of a boundary value problem for the special initial condition $h(\xi)=\delta\left(\xi-\xi_{0}\right)$. The system response for another initial condition can then easily evaluated via the convolution integral. Hence, Green's function depends on both the partial differential equation and the boundary values. It is worth pointing out that are different types of Green functions, depending on the type of differential equation and on the formulation of the boundary conditions, thus restricting the generality of (2.11). In this paper, however, we only come across the type described above.

We might as well expand $\varrho\left(\xi, \tau ; \xi_{0}\right)$ as (using a generating formula in [26], p.252)

$$
\begin{equation*}
G_{1}\left(\xi, \xi_{0}, \tau\right)=\frac{1}{\sqrt{2 \pi}} \sum_{n=0}^{\infty}\left[\frac{H_{n}\left(\frac{\xi_{0}}{\sqrt{2}}\right) H_{n}\left(\frac{\xi}{\sqrt{2}}\right)}{2^{n} n!} e^{-a \tau} e^{-\frac{\xi^{2}}{2}}\right] \tag{2.12}
\end{equation*}
$$

where $H_{n}$ is the Hermitian polynom ([26], p. 249). The dependencies revealed by this formula are characteristic for diffusion processes: The time $\tau$ appears as a linear term in the exponent, a fact that makes clear that the process is irreversible, as it does not produce the same values for negative times. In contrast, solutions of the well known wave equation, where a second time derivative occurs, are invariant under time reversal.

## (iii) Equilibrium Distribution

The equilibrium distribution,

$$
\begin{equation*}
\varrho(\xi)=\lim _{\tau \rightarrow \infty} \varrho\left(\xi, \tau ; \xi_{0}\right)=\frac{1}{\sqrt{2 \pi}} \exp \left(-\frac{1}{2} \xi^{2}\right) \tag{2.13}
\end{equation*}
$$

is simply the standard normal distribution (equation 6.20). Bearing the normalization in mind we conclude that the stationary process V is normally distributed with variance $\sigma^{2}$ and mean wind speed $\overline{\mathrm{v}}$. If $\Phi(\mathrm{x})$ denotes the Gaussian distribution function (equation 6.20) the underlying distribution function is simply $\mathrm{F}_{\xi}(\xi)=\Phi(\xi)$. Hence, the expected time fraction $\tau_{e x}$ when the wind speed $\xi(\tau)$ exceeds a given value $\xi_{e x}$ can be determined by

$$
\begin{equation*}
\tau_{e x}=p\left(\Xi>\xi_{e x}\right)=\Phi\left(-\xi_{e x}\right) \tag{2.14}
\end{equation*}
$$

where p stands for "probability for".

## (iv) Level Crossing

The level crossing analysis of the O.U.- process gives an answer to the question of how frequently a stochastic process crosses a given level. The situation is illustrated in Fig. 2.2 for the normalized process $\Xi$.


Fig. 2.2 Level Crossing

We will for the moment set $\xi_{\mathrm{r}}=0$, thus reducing the problem to a zero crossing problem. The probability $p_{0}\left(\tau_{0}\right)$ that the zero level will be crossed by the process $\Xi$ in the time interval $\tau \in\left[0, \tau_{0}\right]$ at least once when only crossings from negative to positive values count (dots in Fig. 2.2), is equal to

$$
\begin{equation*}
p_{0}(\tau)=\frac{1}{2} p(Z(\tau)<0) \quad, Z(\tau)=\frac{\Xi(0)}{\Xi(\tau)} \tag{2.15}
\end{equation*}
$$

In (2.15) the random variable $Z$ could as well be the product $Z(\tau)=\Xi(0) \Xi(\tau)$ as it is only the change in sign of $\Xi$ from time 0 to $\tau$ which is of interest here. We prefer the quotient as in (2.15) since the necessary integration (compare with equations 6.12) is straightforward. The factor $1 / 2$ in front of $p_{0}$ stems from the fact that only a half of the crossings are from a state below to a state above $\xi_{r}$. The distribution function $F_{z}(z)$ of the quotient $Z$ of two normal processes is given by ([30], eq. 6.46)

$$
\begin{equation*}
F_{z}(z)=\frac{1}{2}+\frac{1}{\pi} \arctan \frac{z-r}{\sqrt{1-r^{2}}} \tag{2.16}
\end{equation*}
$$

with autocorrelation coefficient r (2.9), thus resulting in a zero crossing probability (now writing $\tau$ instead of $\tau_{0}$ )

$$
\begin{equation*}
p_{0}(\tau)=\frac{1}{2} F(0)=\frac{1}{2 \pi} \arccos (r(\tau)) \tag{2.17}
\end{equation*}
$$

Extending the theory to any $\xi_{\mathrm{r}}$ the crossing probability will be ([30], 11.119)

$$
\begin{equation*}
p_{\xi}(\tau)=p_{0}(\tau) \exp \left(-\frac{\xi_{r}^{2}}{2}\right) \tag{2.18}
\end{equation*}
$$

Different approaches are presented in [30] (p. 345) and [25] (p. 346) reaching at the same results.

## (v) Linear Prediction

Linear prediction gives an estimate for a future value $\xi(\tau+\lambda)$ of the O.U. - process, represented by the random variable $\Xi$, as a multiple of the instantaneous value $\boldsymbol{\xi}(\tau)$. The estimator can be obtained by evaluating the Yule- Walker- equations ([30], eq. 13.6) and it is

$$
\begin{equation*}
\hat{\xi}(\tau+\lambda)=e^{-\lambda} \xi(\tau) \tag{2.19}
\end{equation*}
$$

where $\hat{\xi}$ denotes the estimator of $\xi$. This reflects the fact that the process drifts towards the mean value at a rate proportional to the distance from the mean. Although it is a very simple method of prediction it will not be used in this paper as it can not be applied to time series
or first passage times.

## (vi) First Passage Time Problem

Suppose we want to determine the expected time $\bar{\tau}_{1}$ the O.U. - process needs to reach the state $\xi_{1}$ from the initial state $\xi_{0}$ at $\tau=0$. The situation, which is called a first passage time problem, is illustrated in Fig. 2.3.


Fig. 2.3 First Passage Time Problem

Until further notice we will assume $\xi_{1}>\xi_{0}$. Mathematically speaking we wish to calculate the distribution function $\mathrm{F}_{\mathrm{T} 1}(\tau)$ of the random variable $\mathrm{T}_{1}$ that stands for the time the process crosses the line $\xi_{1}$ for the first time after having started at level $\xi_{0} . \mathrm{F}_{\mathrm{T}}(\tau)$ can be expressed by the conditional probability

$$
\begin{equation*}
F_{T r}(\tau)=p\left(T_{1} \leq \tau\right)=p\left(\xi, \xi_{0}, \tau \mid \Xi(t)<\xi_{1} \forall t \in(0, \tau)\right) \tag{2.20}
\end{equation*}
$$

This problem can be solved in a very efficient way by examining the diffusion process in the
half space. Here, one boundary condition will be $\varrho\left(\xi_{1}, \tau\right)=0$, whereas the other remains in the infinite space, $Q(-\infty, \tau)=0$. Hence, the boundary $\xi_{1}$ acts as an absorbing wall. Particles reaching the $\xi_{1}$ - level for the first time will be removed and will not appear anymore in the half space $\xi^{\boldsymbol{\beta}}<\xi_{1}$. Green's function of this boundary problem is given by

$$
\begin{equation*}
G_{2}\left(\xi, \xi_{0}, \tau\right)=\frac{1}{\sqrt{2 \pi\left(1-r^{2}\right)}}\left[\exp \left(-\frac{1}{2} \frac{\left(\xi-\xi_{0} r\right)^{2}}{1-r^{2}}\right)-\exp \left(-\frac{1}{2} \frac{\left(\xi-\left(2 \xi_{1}-\xi_{0}\right) r\right)^{2}}{1-r^{2}}\right)\right] \tag{2.21}
\end{equation*}
$$



Fig. 2.4 Diffusion in the Half Space

The solution can be interpreted as the diffusion of two fields, punctual symmetric to the boundary $\xi=\xi_{1}$, where they compensate each other. (This way of calculating the first passage time has been applied to the Brownian process in [20] (p. 447) ). This is illustrated in Fig. 2.4. In the space $\xi<\xi_{1}$ is the original field while the sub space $\xi>\xi_{1}$ is occupied
by the imaginary field. As in (2.11) the solution for the special initial condition $\varrho(\xi, 0)=$ $\delta\left(\xi-\xi_{0}\right)$ is $\varrho(\xi, \tau)=\mathrm{G}_{2}\left(\xi_{0}, \xi_{0}, \tau\right)$. The number of particles left in the ensemble at time $\tau$ can consequently be obtained via integration

$$
\begin{equation*}
N\left(\xi_{1}, \tau\right)=\int_{-\infty}^{\xi_{1}} \varrho(\xi, \tau) d \xi=\Phi\left(\frac{\xi_{1}-\xi_{0} r}{\sqrt{1-r^{2}}}\right)-\Phi\left(\frac{\xi_{1}-\left(2 \xi_{1}-\xi_{0}\right) r}{\sqrt{1-r^{2}}}\right) \tag{2.22}
\end{equation*}
$$

The distribution function in question, $\mathrm{F}_{\mathrm{T} 1}(\tau)$, will then of course be

$$
\begin{equation*}
F_{T I}(\tau)=1-N\left(\xi_{0}, \tau\right) \tag{2.23}
\end{equation*}
$$

Applying (2.21) we obtain the distribution function of $T_{1}$,

$$
\begin{equation*}
F_{T r}(\tau)=\Phi\left(\frac{\xi_{0} r-\xi_{1}}{\sqrt{1-r^{2}}}\right)+\Phi\left(\frac{\xi_{1}-\left(2 \xi_{1}-\xi_{0}\right) r}{\sqrt{1-r^{2}}}\right) \tag{2.24}
\end{equation*}
$$

which conveys the limits $\mathrm{F}_{\mathrm{T} 1}(0)=\delta_{\xi_{0} \xi 1}\left(\delta\right.$ denotes the Kronecker symbol) and $\mathrm{F}_{\mathrm{T} 1}(\infty)=1$, as it has to be. The density function $\mathrm{f}_{\mathrm{Tl}}(\tau)$ with respect to $\tau$ will be attained via the time derivative, and it is

$$
\begin{align*}
f_{T r}(\tau)=\frac{r}{\sqrt{2 \pi}} \frac{1}{\left(1-r^{2}\right)^{\frac{3}{2}}}[ & \left(\xi_{1} r-\xi_{0}\right) \exp \left(-\frac{1}{2} \frac{\left(\xi_{0} r-\xi_{1}\right)^{2}}{1-r^{2}}\right)+ \\
& \left.\left(2 \xi_{1}-\xi_{0}-\xi_{1} r\right) \exp \left(-\frac{1}{2} \frac{\left(\xi_{1}-\left(2 \xi_{1}-\xi_{0}\right) r\right)^{2}}{1-r^{2}}\right)\right] \tag{2.25}
\end{align*}
$$

The expected transition time (average mean time for the process to get from $\xi_{0}$ to $\xi_{1}$ for $\xi_{1}$ $>\xi_{0}$ is

$$
\begin{equation*}
E[T]=\int_{0}^{\infty} t f_{T}(t) d t \tag{2.26}
\end{equation*}
$$

Looking at $\mathrm{f}_{\mathrm{T}}(\tau)$ it is obvious that the expected time exists as the integral (2.26) converges.

To simplify the numerical evaluation the substitution $r(\tau)=\exp \left(-\beta_{\mathrm{v}} \tau\right)$ helps to extract the representation

$$
\begin{align*}
E[T]= & \frac{-1}{\sqrt{2 \pi}}\left\{\operatorname { l i m } _ { \epsilon \rightarrow 0 } \int _ { \epsilon } ^ { 1 } \frac { \operatorname { l n } ( r ) } { ( 1 - r ^ { 2 } ) ^ { \frac { 3 } { 2 } } } \left[\left(\xi_{1} r-\xi_{0}\right) \exp \left(-\frac{1}{2} \frac{\left(\xi_{0} r-\xi_{1}\right)^{2}}{1-r^{2}}\right)+\right.\right. \\
& \left.\left.\left(2 \xi_{1}-\xi_{0}-\xi_{1} r\right) \exp \left(-\frac{1}{2} \frac{\left(\xi_{1}-\left(2 \xi_{1}-\xi_{0}\right) r\right)^{2}}{1-r^{2}}\right)\right] d r\right\} \tag{2.27}
\end{align*}
$$

The emergence of the small value $\epsilon$ is necessary as the integral is an improper one. It reminds one that the above proposed substitution is not permitted at the singularity $\mathrm{r}=0$. The results for $\xi_{0}>\xi_{1}$ are dual to the above results as the same Green function holds true. The number of particles left in the ensemble is accordingly

$$
\begin{equation*}
N\left(\xi_{1}, \tau\right)=\int_{\xi_{1}}^{\infty} \varrho(\xi, \tau) d \xi=-\int_{-\infty}^{\xi_{1}} \varrho(\xi, \tau) d \xi \tag{2.28}
\end{equation*}
$$

In analogy to the first case we denote the random variable that stands for the transition time with $T_{2}$. Its distribution function is

$$
\begin{equation*}
F_{T 2}(\tau)=2-F_{T \lambda}(\tau) \tag{2.29}
\end{equation*}
$$

and therefore the expected value $\mathrm{E}\left[\mathrm{T}_{2}\right]=-\mathrm{E}\left[\mathrm{T}_{1}\right]$. It is actually not only formally necessary to split up in two parts depending on the sign of $\left(\xi_{1}-\xi_{0}\right)$. The physical background of this is that diffusion processes are not time reversible. This finds its expression in the time derivative of only first order in the Fokker- Planck equation. In the case of wind speeds the very result was expected anyway. Suppose the wind speeds $\xi_{0}$ and $\xi_{1}$ are both positive. The equations developed here now say that it takes longer (on average) to get from a smaller $\boldsymbol{\xi}$ to a bigger one than in the opposite direction. Summarizing the results in a closed representation we can note the expected average transition time from $\boldsymbol{\xi}_{0}$ to $\boldsymbol{\xi}_{1}$

$$
\begin{equation*}
E[T]=\operatorname{sign}\left(\xi_{1}-\xi_{0}\right) E\left[T_{1}\right] \tag{2.30}
\end{equation*}
$$

by applying the well-known signum function.

A different approach to the expected average transition time has been carried out in [32] where Markov chains were used to determine the expected value. The technique described above is only applicable if the random variable is normal distributed, which is true in the case of wind speed fluctuations. For other distributions this method seems not to be feasible. The Markov- Chain- technique on the other hand is more general and adaptable to any type of distribution. We benefit from this in chapter 4.3 where two calculation techniques are presented, which are generally valid. As far as the wind speed distribution is concemed, however, the evaluation of integral (2.27) promises to be more efficient than the Markov-chain- algorithm. It can, however, not be extended to the wind turbine power. The analytical approach is therefore not further pursued.

## (vii) Two Sided Boundary Value Problem

Suppose we want to calculate the mean time $\tau_{\mathrm{b}}=\mathrm{E}\left[\mathrm{T}_{\mathrm{b}}\right]$ the O.U.- process $\Xi$ will stay within the boundaries $\xi_{1}<\xi_{0}<\xi_{2}$ starting at $\xi_{0}$ at $\tau=0$. The random variable that represents the time the process lasts within the band is denoted $\mathrm{T}_{\mathrm{b}}$.


Fig. 2.5 Two Sided First Passage Time Problem

The situation is shown in Fig. 2.5. Formally we can take the same way as before, assuming now two boundary conditions, $\varrho\left(\xi_{1}, \tau\right)=0$ and $\varrho\left(\xi_{2}, \tau\right)=0$, and the initial condition $\varrho(\xi, 0)$ $=\delta\left(\xi-\xi_{0}\right)$. Again, the problem will be solved by Green's function, $G_{3}\left(\xi_{3}, \xi_{0}, \tau\right)$. The expected transition time can then be computed by applying the same method as before. Green's function $\mathrm{G}_{3}$ however cannot be obtained as easily as in the case of a diffusion in the half space. The two-boundary values problem results in a discrete eigenvalue spectrum and Green's function is to be expected of the form

$$
\begin{equation*}
G_{3}\left(\xi, \xi_{0}, \tau\right)=\frac{2}{\xi_{2}-\xi_{1}} \sum_{n=1}^{\infty} \sin \left(n \pi \frac{\xi^{-}-\xi_{1}}{\xi_{2}-\xi_{1}}\right) \sin \left(n \pi \frac{\xi_{0}-\xi_{1}}{\xi_{2}-\xi_{1}}\right) \exp \left[-\tau \Theta_{n}\left(\xi_{,} \xi_{0}, \tau\right)\right] \tag{2.31}
\end{equation*}
$$

This statement satisfies both boundary conditions and the initial condition which can be easily verified by bearing the completeness of the sine-function

$$
\begin{equation*}
2 \sum_{n=1}^{\infty} \sin (n \pi \zeta) \sin \left(n \pi \zeta^{\prime}\right)=\delta\left(\zeta-\zeta^{\prime}\right) \tag{2.32}
\end{equation*}
$$

in the interval $\zeta \in(0,1)$ ( n integer) in mind. Obviously, this is not an efficient method of calculating the expected time. The methods discussed in chapter 4.3 , however, can be easily adapted to this problem.

### 2.1.2.3 The Kaimal Spectrum

Empirical results show that the Kaimal spectrum ([25], eq. 16.15)

$$
\begin{equation*}
S_{K I}(\omega)=\frac{c_{1} \sigma_{b}^{2}}{1+c_{2} \omega^{b}} \tag{2.33}
\end{equation*}
$$

with the coefficients

$$
\begin{align*}
c_{1} & =a \zeta \\
c_{2} & =a\left(\frac{\zeta}{2 \pi}\right)^{b} \\
b & =1.67 \\
a & =0.164  \tag{2.34}\\
\zeta & =\frac{L}{0.041 \bar{v}}
\end{align*}
$$

is a better representation of wind turbulence than the Dryden Spectrum (2.8). Its autocorrelation function

$$
\begin{equation*}
R_{K K}(t)=\frac{1}{\pi} \int_{0}^{\infty} S_{K}(\omega) \cos (\omega t) \mathrm{d} \omega \tag{2.35}
\end{equation*}
$$

can be obtained via Wiener- Chintchin transform (eq. 6.16), where the time axis is not normalized. This equation is used in order to determine the constants $\sigma_{v}^{2}$ and $\beta_{v}$ in the autocorrelation function of the O.U. - process, which is in the unnormalized form

$$
\begin{equation*}
R_{v}(t)=\sigma_{v}^{2} e^{\beta_{v} t} \quad, t>0 \tag{2.36}
\end{equation*}
$$

It is worth pointing out that the Kaimal spectrum was empirically found. The above developed theory however only holds for a Lorenzian spectrum with autocorrelation (2.35). In order to use the results of the statistical theory based on the Lorenzian spectrum we approximate its parameters $\sigma_{v}^{2}$ and $\beta_{v}$ as functions of the Kaimal parameter $\sigma_{1}^{2}$ and $\zeta$. As the autocorrelation function at $t=0$ represents the power of the process, both autocorrelation functions (2.36) and (2.35) have to return the same value at $t=0$, thus leading to the equation

$$
\begin{align*}
\sigma_{v}^{2} & =\frac{c_{1} \sigma_{k l}^{2}}{\pi} \int_{0}^{\infty} \frac{d \omega}{\left(1+c_{2} \omega^{b}\right)} d \omega \\
& =\frac{c_{1} \sigma_{k d}^{2}}{\pi b^{b} \sqrt{c_{2}}} \int_{0}^{\infty} \frac{d y}{y^{1-\frac{1}{b}}(1+y)} \tag{2.37}
\end{align*}
$$

The integrand in the second expression is not dependent on any parameters. This integral can be solved analytically ([8], 1.1.3.4), thus leading to the surprising result

$$
\begin{equation*}
\sigma_{v}^{2}=1.735 \sigma_{k d}^{2} \tag{2.38}
\end{equation*}
$$

To estimate the coefficient $\beta_{v}$, the autocorrelation of the Kaimal spectrum is to be calculated at another point $t$,

$$
\begin{equation*}
\beta_{v}=-\frac{1}{t} \ln \left[\frac{c_{1} \sigma_{L d}^{2}}{\pi \sigma_{v}^{2}} \int_{0}^{\infty} \frac{\cos (\omega t)}{1+c_{2} \omega^{b}} d \omega\right] \tag{2.39}
\end{equation*}
$$

The integral has to be numerically calculated for a given $t$ and $c_{2}$. In [25], p. 347 it is suggested to select $t=2 \mathrm{~s}$, as we are interested in short term fluctuations.

### 2.1.3 Macrometeorological Range

### 2.1.3.1 Mean Wind Speed Distribution

The horizontal hourly mean wind speed $\overline{\mathbf{v}}$ is said to be Weibull- distributed with the distribution function ([19], eq. 2.14)

$$
\begin{equation*}
F(\bar{V})=p(\bar{V} \leq \bar{v})=1-\exp \left[-\left(\frac{\bar{V}}{c}\right)^{k}\right] \tag{2.40}
\end{equation*}
$$

which can be adapted to a given wind site by varying the shape parameter $k$ and the scale parameter $c$. These parameters typically hover in the range of $k \in[1.7,2.5]$ and $c \in[1.15$, 1.18] respectively.

### 2.1.3.2 Mean Wind Speed Profiles

The horizontal wind speed varies with height. If the mean wind speed $\overline{\mathrm{v}}$ is monitored at height $\hat{z}$ the mean wind speed at height $z$ can be concluded from the formula ([19], eq. 2.5)

$$
\begin{aligned}
\frac{\bar{v}(z)}{\bar{v}(\hat{z})} & =\frac{\ln \left(\frac{z}{z_{0}}\right)+5.75 \frac{z}{h}}{\ln \left(\frac{\hat{z}}{z_{0}}\right)+5.75 \frac{\hat{z}}{h}} \\
h & =\frac{u_{*}}{6 f}
\end{aligned}
$$

Here, $h$ is the gradient height, $f$ the Coriolis parameter, $u_{*}$ the friction velocity and $z_{0}$ the roughness length. The Coriolis parameter depends on the location. It is $f=11.5 \mathrm{E}-5 \mathrm{~s}^{-1}$ for the UK. Values for $z_{0}$ are given in [19]. The friction velocity varies with surface roughness and with overall wind speed. If the friction velocity $u_{*}$ is unknown the simpler form ([19], eq. 2.4)

$$
\begin{equation*}
\frac{\bar{v}(z)}{\bar{V}(\bar{z})}=\frac{\ln \left(\frac{z}{Z_{0}}\right)}{\ln \left(\frac{\hat{z}}{z_{0}}\right)} \tag{2.42}
\end{equation*}
$$

may be applied.

### 2.2 Solar Energy

The intensity of the solar irradiation directly outside the earth's atmosphere is almost constant at around $1350 \mathrm{Wm}^{-2}$. Eventhough this value varies up to $\pm 3 \%$ due to eccentricities in the earth's orbit and fluctuating sunspots, it is stable enough to justify the name solar constant. On the earth's surface the peak solar intensity hovers around $1 \mathrm{kWm}^{-2}$ on a horizontal surface, provided the sun is at its apex on a sunny day. In case the latter conditions are not fullfilled, the solar radiation experienced on a surface will not be as big. In general, it will depend on the position of the sun and the clarity of the atmosphere. These geometrical aspects will be covered in 2.2.1. The actual solar power on a tilted surface as a function of the clearness of the sky and the geometry will be calculated in 2.2.2. Chapter 2.2.3 is devoted to a brief discussion of the optimum surface orientation. It is worth noting that the solar power evaluated in 2.2.2 is a value, averaged over a longer time period. These values are good to estimate the solar energy received over a whole year at a selected site. They are, however, not suitable for on-line control schemes. Though, the introduced terminology and techniques will form the starting-point for the discussion of the statistical characteristics of short term fluctuations in chapter 2.2.4.

### 2.2.1 Geometrical Aspects

### 2.2.1.1 Determination of the sun's position

The angle under which the sun is observed from a point on the earth's surface is affected by the earth's daily rotation, expressed by the solar hour angle, and the annual rotation of the tilted earth, expressed by the declination angle and the observer's latitude. The orientation of the sun can then phrased in terms of the solar altitude and azimuth.

## (i) The solar hour angle

The solar hour angle $\Omega$ expresses the daily rotation of the earth. As the earth rotates $360^{\circ}$ within 24 hours, every hour adds another $15^{\circ}$ to the solar hour angle. When the sun is in its highest point in the sky, the solar hour angle is zero ("Solar noon"). Angles before noon count negative, after noon positive. It is worth bearing in mind that the solar angle is not
identical with the local time. For a conversion from solar hour angle values to the local time the longitude of the site in question and the local standard time have to be considered.

## (ii) The declination angle

The declination angle $\delta$ is the angular position of the sun at solar noon with respect to the plane of the equator, and it varies because of the earth's tilt of $23.45^{\circ}$ from $-23.45^{\circ}$ to $+23.45^{\circ}$. Hence, the declination angle depends on the day of the year, $n \in[1,365]$, and it is ([9], eq. 3-8)

$$
\begin{equation*}
\delta=23.45\left(\frac{\pi}{180}\right) \sin \left[2 \pi \frac{284+n}{365}\right] \tag{2.43}
\end{equation*}
$$

on the northern hemisphere (in rad - not degrees). The declination angle reaches its peak at summer solistice and drops to its negative peak at winter solistice. It is converse on the southern hemisphere.

## (iii) The latitude

If the sun is observed from a site other than the equator, the observer's latitude $\theta$ has to be considered, as the sun's highest altitude decreases with $\theta$. The resulting solar-noon altitude angle is $\Omega_{\theta}=1 / 2 \pi-\theta+\delta$.
(iv) Solar altitude, azimuth and zenith angle


Fig. 2.6 Solar Altitude, Azimuth and Zenith Angle

The orientation of the sun in the sky can be phrased in terms of the solar altitude $\sigma$ and the azimuth angle of the sun $\alpha$. The altitude angle measures the angle between the line from the observer to the sun and the line to the horizon (compare Fig. 2.6). The solar azimuth angle gives the sun's angular distance from due south. An orientation to the East (as in Fig. 2.6) counts negative, West counts positive. Hence, azimuth angles from sunrise to solar noon are negative, while angles from solar noon to sunset are positive. The azimuth angle is obtained from ([9], eq. 3-4)

$$
\begin{equation*}
\sin \sigma=\sin \theta \sin \delta+\cos \theta \cos \delta \cos \Omega \tag{2.44}
\end{equation*}
$$

The altitude is calculated from ([9], eq. 3-5)

$$
\begin{equation*}
\sin \alpha=-\frac{\cos \delta \sin \Omega}{\cos \sigma} \tag{2.45}
\end{equation*}
$$

The complement of the solar altitude angle, the zenith angle, is defined as

$$
\begin{equation*}
\theta_{z}=\frac{\pi}{2}-\sigma \tag{2.46}
\end{equation*}
$$

### 2.2.1.2 Sunrise and sunset

As the solar altitude angle is restricted to values $\sigma \in\left[-90^{\circ}, 90^{\circ}\right]$ equation (2.45) is only valid for solar hour angles in the interval $\Omega \in\left[\Omega_{\mathrm{s}}, \Omega_{\mathrm{ss}}\right]$ where $\Omega_{\mathrm{st}}$ denotes the sunrise angle and $\Omega_{\mathrm{st}}$ the sunset angle. Substituting $\sigma= \pm 90^{\circ}$ into (2.45) leads to the sunrise angle $\Omega_{\mathrm{ss}, \mathrm{h}}=\Omega_{\mathrm{s}}$ and sunset angle $\Omega_{\mathrm{ss}, \mathrm{h}}=-\Omega_{\mathrm{s}}$ for horizontal surfaces, where

$$
\begin{equation*}
\mathbf{\Omega}_{s}=\arccos (-\tan \theta \tan \delta) \tag{2.47}
\end{equation*}
$$

For a tilted surface, however, equation (2.45) does not hold true.


Fig. 2.7 Tilted Surface

Suppose we have an array that is inclined to the horizontal by an angle $\beta$ (compare Fig. 2.7). The angle between the projection of the normal of the plane on the horizontal and South is $\alpha$, the azimuth angle as introduced above, so that $\alpha=0$ is due South, $\alpha>0$ an orientation towards the West and $\alpha<0$ an orientation towards the East. In contrast to the horizontal surface, the magnitudes of the solar angle for sunrise and sunset are not equal. They can be calculated by evaluating ([12], 2.2.15)

$$
\begin{align*}
& \mathbf{\Omega}_{s r}=-\min \left\{\boldsymbol{\Omega}_{s}, \arccos \left(\frac{-a b+\operatorname{sign}(\alpha) \sin (\alpha) \sin (\beta) \sqrt{a^{2}-b^{2}+1}}{a^{2}+\sin ^{2}(\alpha) \sin ^{2}(\beta)}\right)\right\} \\
& \mathbf{\Omega}_{s s}=\min \left\{\mathbf{\Omega}_{s}, \arccos \left(\frac{-a b-\operatorname{sign}(\alpha) \sin (\alpha) \sin (\beta) \sqrt{a^{2}-b^{2}+1}}{a^{2}+\sin ^{2}(\alpha) \sin ^{2}(\beta)}\right)\right\} \tag{2.48}
\end{align*}
$$

with the abbreviations

$$
\begin{align*}
& a=\cos \theta \cos \beta+\sin \theta \cos \alpha \sin \beta \\
& b=\tan \delta(\sin \theta \cos \beta-\cos \theta \cos \alpha \sin \beta) \tag{2.49}
\end{align*}
$$

In case the surface faces due south $(\beta=0)$, the magnitudes of sunset and sunrise angle will be the same. Substituting $\beta=0$ into (2.48) leads to a sunset angle

$$
\begin{equation*}
\mathbf{\Omega}_{s}=\min \left\{\mathbf{\Omega}_{s}, \arccos (-\tan (\theta-\beta) \tan \delta)\right\} \tag{2.50}
\end{equation*}
$$

### 2.2.2 Average Daily Solar Energy

Empirical solar radiation data is mostly data for horizontal surfaces. That is, the monthly average daily total radiation on a horizontal surface, H , is measured. If $\mathrm{H}_{0}$ denotes the monthly average daily total radiation directly outside the earth's atmosphere (i.e. the insolation that would be experienced without the earth's atmosphere), the clarity index K can be defined by

$$
\begin{equation*}
K^{\prime}=\frac{H}{H_{0}} \tag{2.51}
\end{equation*}
$$

which is the quotient of H and $\mathrm{H}_{0}$. This coefficient is based on measured data depending on the location and the month. The sunlight received by a horizontal surface can be divided into two parts. First, the direct beam radiation, which strikes the surface from one angle only directly from the sun. Second, the diffuse light, which is the proportion of light that is absorbed or scattered by air molecules, water vapor dust while passing the earth's atmosphere. Diffuse light approaches the horizontal surface from almost any angle. Hence, the monthly average daily total radiation on a horizontal surface can be written as a superposition of $\mathrm{H}_{\mathrm{b}}$, the direct or beam radiation, and $\mathrm{H}_{\mathrm{d}}$, the diffuse radiation:

$$
\begin{equation*}
H=H_{b}+H_{d} \tag{2.52}
\end{equation*}
$$

Light which approaches a tilted surface may as well be light reflected upon the ground (other than the array surface). The conversion of the monthly average daily energy on a horizontal surface, H , can be converted to the monthly average daily energy on a tilted surface, $\mathrm{H}_{\mathrm{T}}$ in two steps. This is in so far important as only values for the horizontal surface are available.

## (1) Estimating the diffuse light

Given an observed value of H , the diffuse radiation term in (2.52) can be separated by a specific correlation function. For latitudes $\theta$ between $43^{\circ} \mathrm{N}$ and $54^{\circ} \mathrm{N}$ the transformation ([29], eq. 3 )

$$
K_{d}= \begin{cases}1.557-1.84 K & , 0.35 \leq K \leq 0.75  \tag{2.53}\\ 0.177 & , K>0.75 \\ 1.0-0.249 K & , 0 \leq K<0.35\end{cases}
$$

is supposed to be accurate, where

$$
\begin{equation*}
K_{d}=\frac{H_{d}}{\boldsymbol{H}} . \tag{2.54}
\end{equation*}
$$

is called diffusion index in analogy to the clarity index defined in (2.51). For other latitudes similar formulas have been developed (for instance [17]). Having calculated the diffusion
term $H_{d}$, the beam radiation $H_{b}$ can be worked out from (2.52).

## (ii) Radiation on a tilted surface

The total hourly radiation on a titled surface is (the index T connotes "tilted")

$$
\begin{equation*}
H_{T}=H_{b T}+H_{d T}+H_{r T} \tag{2.55}
\end{equation*}
$$

It differs from (2.52) only in the additional term $H_{r}$, representing the reflected light. In the following we express these terms as functions of H , the hourly total radiation on a horizontal surface, and the introduced geometrical magnitudes.


Fig. 2.8 Radiation on a Tilted Surface

We will first deal with the direct radiation term. The normal component $\Phi_{\mathrm{bT}, \mathrm{n}}$ of the intensitiy $\Phi_{b}$ of the incoming light beam (compare with Fig. 2.8) on a tilted surface can be obtained from ([12], eq. 2.2.9, 2.2.10)

$$
\begin{equation*}
\Phi_{b T, n}=\Phi_{b} \cos \hat{v}_{T}=\Phi_{b m} \frac{\cos \hat{v}_{T}}{\cos \hat{v}_{z}} \tag{2.56}
\end{equation*}
$$

with

$$
\begin{equation*}
\cos \boldsymbol{v}_{T}=\sin \delta \sin (\theta-\beta)+\cos \delta \cos (\theta-\beta) \cos \Omega \tag{2.57}
\end{equation*}
$$

Here, $\Phi_{b a}$ is the normal component on the horizontal surface. Equation (2.56) is a good approximation unless large differences between $\boldsymbol{v}_{T}$ and $\hat{v}_{z}$ have to be considered. Otherwise the Bădescu- formula ([2], eq. 10) should be used. Let $R_{b}$ denote the ratio of the average daily beam radiation on a tilted surface to that on a horizontal surface,

$$
\begin{equation*}
\boldsymbol{R}_{b}=\frac{\boldsymbol{H}_{b T}}{\boldsymbol{H}_{b}} \tag{2.58}
\end{equation*}
$$

With the different solar hour angles for sunrise and sunset, (2.48) and (2.47), the ratio $\mathrm{R}_{\mathrm{b}}$ for any tilted surface with slope angle $\beta$ and azimuth angle $\alpha$ is obtained from ([12], eq. 2.2.14)

$$
\begin{align*}
R_{b} & =\frac{a\left(\Omega_{s s}-\Omega_{s s}\right)+b\left(\sin \left(\Omega_{s s}\right)-\sin \left(\Omega_{s r}\right)-c\left(\cos \left(\Omega_{s s}\right)-\cos \left(\Omega_{s s}\right)\right)\right.}{2\left(\cos \theta \cos \delta \sin \Omega_{s}+\Omega_{s} \sin \theta \sin \delta\right)} \\
a & =\sin \delta(\cos \beta \sin \theta-\cos \alpha \sin \beta \cos \theta)  \tag{2.59}\\
b & =\cos \delta(\cos \theta \cos \beta+\sin \theta \sin \beta \cos \alpha) \\
c & =\cos \delta \sin \beta \sin \alpha
\end{align*}
$$

In the preferrable situtation that the solar array is facing due south $(\alpha=0) R_{b}$ can be evaluated from the simpler representation (with $\Omega^{\prime}$ s as in (2.50))

$$
\begin{equation*}
R_{b}=\frac{\cos (\theta-\beta) \cos \delta \sin \Omega_{s}+\Omega_{s} \sin (\theta-\beta) \sin \delta}{\cos \theta \cos \delta \sin \Omega_{s}+\Omega_{s} \sin \theta \sin \delta} \tag{2.60}
\end{equation*}
$$

As far as the diffuse radiation on a tilted surface is concerned, an isotropic distribution of the diffuse radiation over the hemisphere is assumed. The diffusion term can be attained from ([12], eq. 3.23)

$$
\begin{equation*}
H_{d T}=H_{d} \frac{(1+\cos \beta)}{2} \tag{2.61}
\end{equation*}
$$

which takes into account that the tilted slope sees only a portion of the hemisphere. $\mathrm{H}_{\mathrm{d}}$ is the diffusion term of the horizontal surface.

The last term in (2.55) is the reflected light portion. The energy of the reflected light is dependant on the ground's abilitiy to reflect, a property which may be represented by the albedo factor $\varrho$. The albedo usually ranges from 0.1 (asphalt paved roads) up to 0.9 (snow). Given the albedo, the diffusion term can be calculated from

$$
\begin{equation*}
H_{r T}=\varrho\left(H_{b}+H_{d}\right)\left(\frac{1-\cos \beta}{2}\right) \tag{2.62}
\end{equation*}
$$

Substituting equations (2.59), (2.61) and (2.62) into (2.55) results in the monthly daily total radiation on a tilted surface:

$$
\begin{equation*}
H_{T}=H_{b} R_{b}+H_{d} \frac{(1+\cos \beta)}{2}+\varrho\left(H_{b}+H_{d}\right) \frac{(1-\cos \beta)}{2} \tag{2.63}
\end{equation*}
$$

Finally, the ratio of monthly average daily total radiation on a tilted surface to that on a horizontal surface can be defined as

$$
\begin{equation*}
R=\frac{H_{T}}{H}=\left(1-K_{d}\right) R_{b}+K_{d}\left(\frac{1+\cos \beta}{2}\right)+\varrho\left(\frac{1-\cos \beta}{2}\right) \tag{2.64}
\end{equation*}
$$

At the end of this section it is worth pointing out that the calculus presented here applies to monthly averages. It is assumed that clouds are uniformly distributed over the sky. Drifting clouds are not considered in this technique.

### 2.2.3 Optimum Surface Orientation

Apparently, the maximum amount of direct-beam insolation is experienced by a surface whose normal is parrallel to the incoming light. In order to achieve this optimum orientation it must be possible to rotate the surface around two axes, namely the tilt and the azimuth angle, which requires two motors. Usually, the additional energy obtained by a two motor option is marginal and does not pay off. Hence, the second best option is to fix the surface, so that it faces due south and keep the slope angle flexible. In case that there is no
possibility to move the array at all, the surface would obtain the optimum amount of directbeam solar radiation over a year, if the tilt angle was equal to the site's latitude. Tilting the surface up, on the other hand, causes the diffuse light portion to decrease. The annual optimum surface at sites with humid climates is therefore about $10 \%-25 \%$ less than the latitude ([9]). The last statement is backed by an experimental investigation ([23]), in which a tilt angel of $30^{\circ}$ is suggested for a location at $48^{\circ}$ north.

### 2.2.4 Short- term Global Irradiance

### 2.2.4.1 Probability Density Function

Similar to the wind, the solar insolation is a stochastic process that reveals a distinctive short- term irradiance process, a phenomenon we might call turbulence by borrowing the word from the analysis of the wind. The short- term ( 5 minutes time average values) solar irradiance has been modelled in a paper by A. Skartveit ([40]). We will cite from this paper throughout this section unless otherwise specified. The objective is a probability density function with the same functionality as in the case of wind turbulence, now for the intrahour radiation. Again the pattern here is that we have a stochastic model of the radiation for a time period of an hour.
For the purpose of the short- term solar irradiance model the average root squared deviation

$$
\begin{equation*}
\sigma_{k}=\sqrt{\frac{\left(K_{j}-K_{j-1}\right)^{2}+\left(K_{j}-K_{f+1}\right)^{2}}{2}} \tag{2.65}
\end{equation*}
$$

will be defined. The coefficient $K_{j}$ is the clearneass index as defined in (2.51) at the hour with index j . The average root squared deviation is hence a weight function that takes into account the changes of the clearness index from the precedent hour to the hour in question and further on to the subsequent hour. Within the 5 minutes developmental sample the (i.e. for 5 minutes time average values) observed distribution of the intrahour standard deviation $\sigma_{\mathbf{k}}$ is Weibull- distributed with the density function

$$
\begin{equation*}
p(s)=\alpha \gamma(\alpha S)^{\gamma-1} \exp \left(-(\alpha s)^{\gamma}\right) \tag{2.66}
\end{equation*}
$$

corresponding distribution function

$$
\begin{equation*}
F(s)=1-\exp \left(-(\alpha s)^{y}\right) \tag{2.67}
\end{equation*}
$$

and the coefficients

$$
\begin{align*}
\alpha & =\Gamma\left(1+\frac{1}{\gamma}\right) \\
s & =\frac{\sigma_{t}}{\sigma^{*}}  \tag{2.68}\\
\sigma^{*} & =0.87 K^{2}(1-K)+0.39 \tilde{\sigma} \sqrt{K} \\
\gamma & =0.88+42\left(\sigma^{*}\right)^{2}
\end{align*}
$$

Here, $\Gamma(x)$ is the well known gamma function. The coefficient $\sigma_{k}$ must be estimated by chosing a random number $\zeta$, which is supposed to be evenly distributed between 0 and 1 , instead of $F(s)$. Then solve (2.67) for $s$,

$$
\begin{equation*}
s=\frac{1}{\alpha} \sqrt[r]{-\ln (1-\zeta)} \tag{2.69}
\end{equation*}
$$

and eventually determine $\sigma_{k}$ with (2.68). Given the hourly mean clearness index K (capital $K$ ) and the standard deviation $\sigma_{k}$, the distribution of short term $k$ - values (lower case $k$ ) is phrased in terms of a scaled clearness index $\mathbf{x}$,

$$
\begin{equation*}
x=\frac{k-k_{\min }}{k_{\max }-k_{\min }} \tag{2.70}
\end{equation*}
$$

and standard deviation $\sigma_{\mathrm{x}}$,

$$
\begin{equation*}
\sigma_{x}=\frac{\sigma_{k}}{k_{\max }-k_{\text {xim }}} \tag{2.71}
\end{equation*}
$$

The minimum and maximum values of k are given by the empirical formulas

$$
\begin{align*}
& k_{\min }=\max \left\{0,(K-0.03) \exp \left(-11 \sigma_{k}^{1.4}\right)-0.09\right\} \\
& k_{\max }=(K-1.5) \exp \left(-9 \sigma_{k}^{1.3}\right)+1.5 \tag{2.72}
\end{align*}
$$

The probability density function of the scaled index x is now described by a linear
combination of two Beta- distributions ${ }^{3}$. To clarify the following formalism we state the definition of the incomplete Beta- function ([41], def. 58:3:1)

$$
\begin{equation*}
B(\alpha, \beta, x)=\int_{0}^{x} t^{\alpha-1}(1-t)^{\beta-1} d t \quad, 0<x<1 \tag{2.73}
\end{equation*}
$$

and its normalized form ([41], def. 58:1:1)

$$
\begin{equation*}
I(\alpha, \beta, x)=\frac{B(\alpha, \beta, x)}{B(\alpha, \beta)} \quad, B(\alpha, \beta)=B(\alpha, \beta, 1) \tag{2.74}
\end{equation*}
$$

$\mathrm{B}(\alpha, \beta)$ is called Beta-function. Applying this notation the probability density function of the scaled index $x$ is

$$
\begin{equation*}
f_{x}(x)=w C_{1} t^{a_{1}-1}(1-x)^{h_{1}-1}+(1-w) C_{2} x^{a_{2}-1}(1-x)^{h_{2}-1} \tag{2.75}
\end{equation*}
$$

with the coefficients

$$
\begin{align*}
& a_{j}=\max \left\{1,\left(1-\kappa_{j}\right)\left(\frac{x_{j}}{\sigma_{j}}\right)^{2}-\kappa_{j}\right\} \\
& b_{j}=\max \left\{1, \frac{1-\kappa_{j}}{\sigma_{j}^{2}}\left(x_{j}\left(1-\kappa_{j}\right)-\sigma_{j}^{2}\right)\right\}  \tag{2.76}\\
& C_{j}=\left(B\left(a_{j}, b_{j}\right)\right)^{-1}
\end{align*}
$$

and

$$
\begin{equation*}
W=\frac{x_{2}-T}{x_{2}-x_{1}} \tag{2.77}
\end{equation*}
$$

with

[^3]\[

$$
\begin{align*}
& x_{1}=\hat{\mathbf{K}}\left(0.01+0.98 \exp \left(-60 \sigma_{t}^{3.3}\right)\right) \\
& x_{2}=(\hat{\mathbf{K}}-1)\left(0.01+0.98 \exp \left(-11 \sigma_{t}^{2}\right)\right)+1 \\
& \sigma_{1}^{2}=0.014  \tag{2.78}\\
& \sigma_{2}^{2}=0.006
\end{align*}
$$
\]

Here, $\hat{\mathrm{K}}$ is the hourly average clearness index normalized as in (2.70). The probability distribution function of the process X will then be written as

$$
\begin{equation*}
F_{x}(x)=w I\left(a_{1}, b_{1}, x\right)+(1-w) I\left(a_{2}, b_{2}, x\right) \tag{2.79}
\end{equation*}
$$

and consequently the distribution function of the short term k - values (clearness index) as ${ }^{4}$

$$
\begin{equation*}
F_{k}(k)=F_{x}\left(\frac{k-k_{\min }}{k_{\max }-k_{\min }}\right) \tag{2.80}
\end{equation*}
$$

At the end of this section, let us throw the main points into relief: Within a reasonable time interval, the clearness index $k$ is a stochastic process whose distribution function is described by $\mathrm{F}_{\mathbf{k}}(\mathrm{k})(2.80)$, which is a function of the hourly mean clearness index K and the standard deviation $\sigma_{k}$. In practice, the latter parameter can be estimated from previous observations (eq. (2.68)).

### 2.2.4.2 Conditional Probability

The objective of this subsection is to develop a technique to calculate the conditional distribution function $F_{x}\left(x(t) \mid X(0)=x_{0}\right)$ of $X(t)$ subject to the condition $X(0)=x_{0}$. We will often use the abbreviation $G_{x}(x)=F_{x}\left(x(t) \mid X(0)=x_{0}\right)$. For the purpose of this section we assume an autocorrelation coefficient in the form

$$
\begin{equation*}
r_{y}=r_{x}(t)=\exp \left(-\beta_{x} t\right) \tag{2.81}
\end{equation*}
$$

for the scaled clearness index x . At time $\mathrm{t}=0$ the conditional distribution function should
${ }^{4}$ Refer to chapter 6.2, for discussion of functions of random variables
yield $F_{x}\left(x(0) \mid X(0)=x_{0}\right)=s\left(x-x_{0}\right)^{5}$ and its probability density function $f_{x}\left(x(0) ; X(0)=x_{0}\right)$ $=\delta\left(x-x_{0}\right)$ since the probability to observe the process $X(t)$ at time $t=0$ in $x_{0}$ is equal to 1 . One way to work out the conditional probability would be to construct the joint probability density function $f_{x}(x(t), x(0))$ of the stochastic processes $X(t)$ and $X(0)$ from the given marginal distributions $F_{x}(x(t))$ and $F_{x}(x(0))$ and the autocorrelation coefficient. A technique to construct the joint probability density function from the marginal distributions is presented in [18]. Given the joint probability density function, the conditional probability density could be concluded from equation (6.14). In [18], the joint density function is known, which is not the case here. Hence, the problem is being solved in a different manner. First, the (nonconditional) distribution function $F_{x}(x)(2.79)$ will be approximated by a superposition of normal distributions with their peaks shifted along the $x$-axis. The expansion has the form

$$
\begin{equation*}
\hat{F}_{x}(x)=\sum_{q=1}^{Q} u_{q} v_{q}(x) \approx F_{x}(x) \tag{2.82}
\end{equation*}
$$

with the generating functions

$$
\begin{equation*}
v_{q}(x)=\Phi\left(\frac{x-\frac{q}{Q+1}}{\sigma_{q}}\right) \tag{2.83}
\end{equation*}
$$

In (2.82), $\mathrm{u}_{\mathrm{q}}$ are coefficients which will be subsequently determined. The generating functions $v_{q}(x)$ are normal distributions (definition equation (6.19)) along $x$ with their means centered at $x=0.5$ and equidistantly distributed. The standard variation coefficients $\sigma_{q}$ will be chosen as

$$
\begin{equation*}
\sigma_{q}=\frac{\varepsilon}{Q}\left[\max \left\{1, f_{x}\left(\frac{q}{Q+1}\right)\right\}+1\right] \tag{2.84}
\end{equation*}
$$

with a single coefficient $\epsilon$. The standard variation of each of the normal distributions will thus be smaller if $Q$ is larger or - in other words - if more functions are taken into account and hence the distance between two peaks becomes smaller. The division by $Q$ in (2.84) is

[^4]not imperative but intended to ensure that $\epsilon$ lies in the same order of magnitude irrespective of Q . The term in brackets in equation (2.84) is a number between 1 and 2 and has the following effect: Whenever the density function $f_{x}(x)$ is small (or the increments in $F_{x}(x)$ ) the variance of the normal distribution with its peak at this point will be smaller and vice versa. This correction term permits a more sensitive adaption in low- probability regions. The limitation of the correction term to values in the interval [1,2] seems to be appropriate to the range of $f_{x}(x)$. In order to optimize the approximation a least square problem is introduced with the merit function
\[

$$
\begin{equation*}
V\left(u_{q}\right)=\sum_{m=1}^{M}\left[\sum_{q=1}^{Q}\left(u_{q} v_{q}\left(\frac{m}{M+1}\right)\right)-F_{x}\left(\frac{m}{M+1}\right)\right]^{2} \tag{2.85}
\end{equation*}
$$

\]

as a function of the coefficients $u_{q}$. Here, we assume that $M$ trial points are taken into account. It is worth pointing out that the generating functions $v_{q}(x)$ do not form an orthogonal or complete function system. Therefore the choice of $\mathrm{Q}, \mathrm{M}$ and $\epsilon$ has to be carefully considered. As $\mathrm{F}_{\mathrm{x}}(\mathrm{x})$ is a superposition of two incomplete Beta- functions its derivative $f_{x}(x)$ may have up to 2 relative maxima over $x \in[0,1]$. Hence, $Q$ must be greater than 2, better 8 or 12 . Numerical results have shown that $Q>12$ is not beneficial. For a condensed representation we note the abbreviation

$$
\begin{equation*}
\alpha_{m q}=\Phi\left(\frac{\frac{m}{M+1}-\frac{q}{Q+1}}{\sigma_{q}}\right) \tag{2.86}
\end{equation*}
$$

To find the minimum of (2.85) its gradient with respect to $u_{q}$ is to be set equals 0 . Rearranging this condition yields

$$
\begin{equation*}
\sum_{m=1}^{M} \sum_{q=1}^{Q} u_{q} \alpha_{m q} \alpha_{m j}=\sum_{m=1}^{M} F_{s}\left(\frac{m}{M+1}\right) \alpha_{m j} \quad j=1 \ldots Q \tag{2.87}
\end{equation*}
$$

This is a system of linear equations, and we can arrange it into the matrix representation

$$
\begin{equation*}
A u=d \tag{2.88}
\end{equation*}
$$

with a symmetric coefficient matrix $\mathbf{A}$ and a right hand vector $\mathbf{d}$. The elements of $\mathbf{A}$ and $\mathbf{d}$
are

$$
\begin{align*}
d_{j} & =\sum_{m=1}^{M} F_{x}\left(\frac{m}{M+1}\right) \alpha_{m j} \\
A_{j j} & =\sum_{m=1}^{M} \alpha_{m l} \alpha_{m j} \tag{2.89}
\end{align*}
$$

Hence, solving (2.88) for $\mathbf{u}$ minimizes the merit function $V$ (2.85) with respect to the coefficients $\mathrm{u}_{\mathrm{q}}$ for a fixed standard deviation parameter $\epsilon$. The whole algorithm that considers $\epsilon$ as well is then as follow:

1. Set initial $\epsilon=0.4$
2. Calculate $\mathbf{u}$ from (2.88) and the merit function $V(2.85)$
3. Repeat step 2 for different values of $\epsilon$ until a minimum of V along the $\epsilon-$ axis has been found. The line search for $\epsilon$ is carried out in two steps: First, a bracket will be searched for, in which the minimum lies in. Second, a golden section search ${ }^{6}$ ([15]) follows to determine the minimum with a higher accuracy. High accuracy on the other hand is counterproductive to the computing time. Note that for each $\epsilon, 1 / 2 \mathrm{MQ}$ evaluations of $\Phi(x)$ are required. We will therefore quit the algorithm as soon as a V-value has been found which is below a specific value (e.g. 0.003). In case Q was selected as 5 and $V$ at the initial point $\epsilon=0.4$ is above $0.1, Q$ will be set to 8 and the algorithm restarted. Otherwise the algorithm will be aborted if the minimum of V has been determined to lay in an interval along the $\epsilon$ - axis which is smaller than 0.02 .
4. Function values of $F_{x}(x)$ can then be worked out from $\hat{F}_{x}(x)$ (eq. (2.82)).

The quality of the approximation can be checked by calculating the difference between the object function $\mathrm{F}_{\mathrm{x}}(\mathrm{x})((2.79)$ ) and its approximation (2.82),

$$
\begin{equation*}
\Delta(x)=F_{x}^{\prime}(x)-\hat{F}_{x}(x) \tag{2.90}
\end{equation*}
$$

[^5]In Fig. 2.9 $\Delta(x)$ has been calculated for typical values for $k, K_{0}$ and $\sigma_{\mathrm{k}}$. Here, the number of coefficients is set to $Q=8$, with the number of trials, $M$, as parameter. For $M=Q$ the trial points coincide with the peaks of the Gaussian functions. The figure of merit in this case was $\mathrm{V}=2.4 \mathrm{E}-30$. Increasing the number of trials to 16 does not improve the performance. It is actually quite the reverse. Hence, it is recommended to set $\mathrm{Q}=\mathrm{M}$.

In Fig. 2.10, $Q$ and $M$ have been simultaneously changed so that $Q=M$. Obviously, $Q=6$ is not sufficient as the maximum difference $\Delta$ is 0.159 for the chosen parameters of $k, K_{0}$ and $\sigma_{r}$.


Fig. 2.9 Quality of the Approximation


Fig. 2.10 Quality of the Approximation

For $\mathrm{Q}=12$, a maximum difference $\Delta$ of 0.001 has been observed. Larger Q - values will further improve the approximation. The associated calculation time, however, will increase as well, thus forcing to strike a balance between expenditure and accuracy. As the probability function is an empirical function, $\mathrm{Q}=12$ seems to be a good choice and will be used in all calculations carried out in this paper unless otherwise explicitly stated.

Having determined $u_{q}$ and $\epsilon$ the distribution function can now be worked out from (2.82). As the conditional distribution of a normal distributed random variable is known (with density function as in 6.23), the conditional distribution function of $X$ as the superposition of normal distributions can be easily concluded. It is

$$
\begin{equation*}
\hat{F}_{x}\left(x \mid X(0)=x_{0}\right)=\sum_{q=1}^{Q} u_{q} \Phi\left(\frac{x-\left(\frac{q}{Q+1}+\left(x_{0}-\frac{q}{Q+1}\right) r\right)}{\sigma_{q} \sqrt{1-r^{2}}}\right) \tag{2.91}
\end{equation*}
$$

which is the superposition of weighted, conditional normal distributions with autocorrelation coefficient $\mathrm{r}_{\mathrm{x}}$ (2.81). Equation (2.91) satisfies the stated initial conditions and it goes over
into (2.82) for $\mathrm{t} \rightarrow \infty$ when $\mathrm{r} \rightarrow 0$.

So far, statistical models for the short term behaviour of both wind speed and clearness index have been presented. We will continue this discussion in chapter 4.1, where the short term statistical models will be unified and extended to the total power supplied by the renewable energy sources. In order to include the power in the statistical theory, models for the wind generator and the photvoltaic array are needed. They will be the focus of the discussion in the following chapter 3.

### 2.3 Battery

### 2.3.1 Storage Technolgies

A storage unit in a hybrid wind- pv-system is used to deposit any surplus in the energy supplied by the renewable energy sources. In times, when the energy demand exceeds the available renewable energy, it is supposed to deliver the stored energy in order to avoid starting the fossil fuel generator. This could be for a short period of seconds as well as for a period of days. Out of all possible technologies the one should be selected, that fullfills the following criteria best:

- High charging- and recharging efficiency as well as a high storage efficiency
- Speed at which the storage system can be brought into in order to absorb or deliver energy.
- High lifetime expectancy
- High reliability
- Low cost
- Low ecologically harmful emission during both production and operation. Possibility of recycling after reaching the lifetime limit.
- Small size

In the following a brief outline of different storage technologies will be given and the above criteria will be addressed.

Mechanical storage systems reveal a high energy conversion efficiency. A drawback is their large size.

Chemical storage systems, in general, have a lower efficiency for energy conversion. The most prominent example for this category is the hydrogen production ([31]). Hydrogen is versatile in its application and an environment friendly storage medium. The costs, however, are considerably ( $\sim 1000 \mathrm{ECU} / \mathrm{kW}$ ).

Electrical storage systems, for instance in form of an electrolyte capacitor, are only suitable for the storage of energy for a few seconds.

Electrochemical storage systems (batteries) are systems where the chemical energy is translated into electric energy, which is produced when the chemicals in the system react with one another. Rechargeable systems allow the reverse process as well. Lead- Acid is the most commonly used battery type in PV applications due to its competitive price. NiCd batteries tend to have a higher energy density and may last longer in very cold areas. They are, however, more expensive [21].

For this paper a lead- acid battery has been chosen as energy storage system, which seems to be a good compromise between cost and life expectancy. Compare discussion in [21] and [7].

### 2.3.2 Lead- acid battery

### 2.3.2.1 Chemical Reaction

The energy stored in a battery is a chemical energy that is translated into electrical energy. The latter one is produced when the chemicals in the battery react with one another. Rechargeable batteries as the lead-acid battery allow the reverse process as well. In case of the lead- acid battery the chemical reaction can be written as ([37])

$$
\mathrm{Pb}+\mathrm{PbO}_{2}+\mathrm{H}_{2} \mathrm{SO}_{4} \Rightarrow 2 \mathrm{PbSO}_{4}+2 \mathrm{H}_{2} \mathrm{O} .
$$

The rate of the chemical reaction varies with

- state of charge,
- battery storage capacity,
- rate of charge and discharge,
- environmental temperature and
- the age and the shelf life of the battery.


### 2.3.2.2 State of Charge

The electric charge, $Q_{0}(t)$, in a battery can be thought of as the sum of the available charge
$Q_{1}(t)$ and the bound charge $Q_{2}(t)$. They all vary with the time. At the beginning, however, the electric charge $Q_{0}(0)=Q_{1,0}(t)+Q_{2,0}(t)=Q_{b}$ coincides with the battery storage capacity (i.e. the rated charge). The state of charge is defined as

$$
\begin{equation*}
\operatorname{SOC}(t)=\frac{Q_{1}(t)}{Q_{b}} \tag{2.92}
\end{equation*}
$$

the quotient of the residual capacity $Q_{1}(t)$ and the battery storage capacity. The depth of discharge, DOD, is then simply

$$
\begin{equation*}
D O D=1-S O C \tag{2.93}
\end{equation*}
$$



Fig. 2.11 Battery as a Two-Pole Device

If the battery is viewed as a two-pole electrical device (Fig. 2.11) with output current $I_{b}$ and voltage $V_{b}$ three states of the battery, dependant on the sign of $I_{b}$, can be defined as follows:
(1) $\mathrm{I}_{\mathrm{b}}<0$ : The battery will be charged.
(2) $\mathbf{I}_{b}=0$ : The battery will be exposed to an internal discharge, idle discharge. A typical value for self discharge is $0.1 \%$ per day ([42]).
(3) $I_{b}>0$ : The battery will be discharged.

In Fig. 2.12 the SOC is sketched for the three phases as a function of time.


## Fig. 2.12 State of Charge

Knowing the state of charge of the battery is very important for the energy management as it directly represents the energy that is available in the battery. As the battery charging or discharging current is in most cases not constants and varies according to changes in solar insolation and wind speed, a reliable state-of-charge determining on-line method is needed. For the purpose of this paper it is assumed that the state of charge can be determined. An on-line algorithm is described in [43] for instance.

### 2.3.2.3 Battery Modelling

The purpose of a battery model in this context is to provide a relationship between the state of charge, current and voltage. Below follows the brief discussion of three battery models. The first two, the Shepherd and the Salameh-Model, are electric models, the third is a
storage model. The electric models can be described in terms of an electric circuit with various elements. They permit us to calculate the voltage and the current. Given the electric current the available charge can be concluded from the differential

$$
\begin{equation*}
\frac{\partial Q}{\partial t}=\eta_{b} I \tag{2.94}
\end{equation*}
$$

where $\eta_{b}$ is a charge/ discharge efficiency factor.

## (i) The Shepherd Model

A simple electric model was devised by Shepherd ([38], [24]). The electric circuit is illustrated in Fig. 2.13.


Fig. 2.13 Battery Equivalent Circuit: Shepherd Model

It consists of a series of a resistance, $\mathrm{R}_{0}$, a fixed voltage, $\mathrm{V}_{0}$, and a charge dependant voltage, g DOD. The diodes are for directional purposes only, with the index ' $\mathbf{c}$ ' for 'charge' and ' d '
for 'discharge'. The discharge voltage is ([24], eq. 6)

$$
\begin{equation*}
V_{b}=V_{0, d}-g_{d} D O D+I_{b} R_{d} \tag{2.95}
\end{equation*}
$$

and the charge voltage accordingly with index ' $\mathbf{c}$ ' instead. The equation does not take into account the diodes which modify the model slightly at very low currents. The resistance $R_{b}$ is defined as ([24], eq. 7)

$$
\begin{equation*}
R_{d}=R_{0, d}\left(1+\frac{m_{d} D O D}{\frac{Q_{m, d}}{Q_{b}}-D O D}\right) \tag{2.96}
\end{equation*}
$$

Here, $\mathrm{m}_{\mathbb{d}}$ denotes a parameter describing the cell type, $\mathrm{R}_{0, \mathrm{~d}}$ the internal resistance at full charge and $Q_{m, d}$ a capacity paramter. Again, the same formula applies for charging the battery with index ' $\mathbf{c}$ '. In this form the model requires 5 parameters for each process, charging and discharging. This model can be easily extended to accommodate temperature dependancy by declaring parameters as functions of the temperature. Facinelli ([13], eq. 4a) assumes a quadratic relationship, whereas Khouzam ([24], eq. 9) employs linear functions.

## (ii) The Salameh Model

The Salameh Model ([37]) is a further development of the Shepherd model, as it takes internal discharge and overvoltage into account. The electric circuit is shown in Fig. 2.14.


Fig. 2.14 Battery Equivalent Circuit: Salameh Model

Again, the diodes are strictly for directional purposes and in this sense ideal. The battery capacity is $C_{b}$, the self discharge resistance $R_{p}$. Devices with index ' $o$ ' stem from the overvoltage circuit, whereas ' d ' and ' c ' denote 'discharge' and 'charge'. Although it seems to be a linear circuit - apart from the diodes - it is not. All devices are non- linear. The state of charge can therefore only be worked out in an iterative way.

## (iii) The Manwell Model

This model ([27]) places the emphasis on the electric charge. It assumes that the electric charge in a battery is either available or chemically bound. Charging and discharging causes a transfer of charge from one to the other 'container', though the sum of both may decrease with the time. According to the model the amount of available charge, $\mathrm{Q}_{1}(\mathrm{t})$, and bound charge, $\mathrm{Q}_{2}(\mathrm{t})$ at time t can be written as ([27], eq. 8,9 )

$$
\begin{align*}
& Q_{1}(t)=Q_{1,0}+\frac{\left(Q_{0} k c-I\right)\left(1-\mathrm{e}^{-\mathrm{kt}}\right)}{k}-\frac{I c\left(k t-1+\mathrm{e}^{-\mathrm{kt}}\right)}{k} \\
& Q_{2}(t)=Q_{2,0} \mathrm{e}-k t+Q_{0}(1-c)(1-\mathrm{e}-k t)-\frac{I(1-c)(k t-1+\mathrm{e}-k t)}{k} \tag{2.97}
\end{align*}
$$

with $\mathrm{Q}_{1,0}$ and $\mathrm{Q}_{2,0}$ denoting the charges at the beginning of the calculations. The sum of both
is denoted by $Q_{0}=Q_{1,0}+Q_{2,0}$. The parameter $k$ is a rate parameter. The width of the charge containers is described by c. Assuming a constant voltage the maximum discharge current is ([27], eq. 22)

$$
\begin{equation*}
I_{d \max }=\frac{k Q_{1,0} \mathrm{e}^{-\mathrm{kt}}+Q_{0} k c\left(1-\mathrm{e}^{-\mathrm{kt}}\right)}{1-\mathrm{e}^{-\mathrm{kt}}+c\left(k t-1+\mathrm{e}^{-\mathrm{kt}}\right)} \tag{2.98}
\end{equation*}
$$

The maximum charge current can be obtained from ([27], eq. 23)

$$
\begin{equation*}
I_{c \max }=\frac{-k c Q_{\max }+k Q_{1,0} \mathrm{e}^{-\mathrm{kt}}+Q_{0} k c\left(1-\mathrm{e}^{-\mathrm{kt}}\right)}{1-\mathrm{e}^{-\mathrm{kt}}+c\left(k t-1+\mathrm{e}^{-\mathrm{kt}}\right)} \tag{2.99}
\end{equation*}
$$

Here, $\mathrm{Q}_{\max }$ is the maximum battery capacity.
The model in this form does not take into account any temperature effects. For moderate temperatures, however, it procures accurate results. There are two major advantages of this model: First, it requires only 3 parameters, $\mathrm{Q}_{\max }, \mathrm{k}$ and c . In comparison, the Shepherd model requires 10 parameters, the Salameh model draws data from curves in order to determine its underlying non- linear elements. Second, the Manwell model is based on the electric charge, a fact that simplifies the determination of the state of charge. In the electric models, the state of charge has to be calculated by solving a differential equation. Hence, for the generation of time series of the state of charge in the section on time series, the Manwell model is used.

### 23.2.4 Lifetime Considerations

Depending on theoretical assumptions different statements can be made about the lifetime of a battery, which is measured in the number of cycles, $N$. The simplest relationship is ([22])

$$
\begin{equation*}
N D O D \approx \text { constant } \tag{2.100}
\end{equation*}
$$

as long as the battery is not overcharged or overdischarged. Other laws are similar and do in fact converge into above relationship under certain conditions. It is recommended ([11]) to operate the battery between $40 \%$ SOC and $80 \%-90 \%$ SOC. In [39] we have found some typical values concerning the lifetime:
$60 \%$ DOD $\quad 2000$ cycles
$30 \%$ DOD $\quad 4000$ cycles
$10 \%$ DOD $\quad 6000$ cycles

Summarising, it can be said that the charger/ discharger of the battery should be aware of the fact that an increased lifetime is only possible with a shallow depth of discharge.

### 2.4 Diesel Generator

With regard to the objective of this study just two facets of the operation of the diesel are of significance: Fuel consumption and life time, both of whom are covered in the following two sections.

### 2.4.1 Fuel Consumption and Efficiency

Fig. 2.15 illustrates a typical course of the fuel consumption as a function of the output power $P_{\text {Disel }}([28])$ as well as the corresponding normalized efficiency $\eta_{\text {Diesel }}$. Here, the power axis is conveniently normalized to the rated power $P_{\text {Diesel, }}$ and the fuel consumption $F\left(P_{\text {Diesel }}\right)$ is normalized to the consumption at the rated power, $\mathrm{F}\left(\mathrm{P}_{\text {Diseser }}\right)$. The graph gives rise to a linearization of the fuel consumption $\mathrm{F}\left(\mathrm{P}_{\text {Diksel }}\right)$,

$$
\begin{equation*}
F\left(P_{\text {Diesel }}\right)=F\left(P_{\text {Dlesel, }, r}\right)\left(f_{0}+f \frac{P_{\text {Dkesel }}}{P_{\text {Dlesel, }, r}}\right) \tag{2.101}
\end{equation*}
$$

with the dimension [volume/s]. Given the figures in [28] we have computed the linear regression coefficients to be $f_{0}=0.15$ and $f=0.81$. This data may serve as long as no specific data are given. Summarizing we can say that the diesel should always be operated above a certain minimum load in order to maintain efficiency.


Fig. 2.15 Fuel Consumption and Efficiency

### 2.4.2 Lifetime Considerations

Operating the diesel under light load causes the engine oil to foul, thus leading to an increasing wear and consequently higher maintenance costs and shorter life span. A model of a diesel engine bearing wear has been proposed ([10]). At this stage we can, however, not envisage an efficient way of including these results into the theory presented here. For now we will therefore just bear in mind that the recommended load ranges between $50 \%$ and $80 \%$ for prolonged operation ([11]). This conclusion falls significantly short of the expectations aroused by the heading as we are still not able to quantize the influence of the load or the frequency of start/ stop-cycles on the lifetime or the maintenance factor of the diesel.

## 3. Power Supply

### 3.1 Wind Turbine

In the study presented here we assume that the operation of a wind turbine is described by its power- speed curve. In absence of a specific characteristic a model curve as shown in Fig. 3.1 will be used ([16]) :


Fig. 3.1 P-v- Characteristic of a Wind Turbine

$$
P_{t u r b}(V)= \begin{cases}0 & V \leq V_{c f}  \tag{3.1}\\ P_{r}\left(\frac{V-V_{d}}{V_{r}-V_{d f}}\right)^{3} & V_{c t} \leq V \leq V_{r} \\ P_{r} & V_{r} \leq V \leq V_{c o} \\ 0 & V \geq V_{c o}\end{cases}
$$

Here, $P_{r}$ is the rated power of the wind turbine, which is the power supplied by the turbine at the rated wind speed $v_{r}$. The wind speeds $v_{c i}$ and $v_{c o}$ are called cut-in and cut-out speed respectively. They define the interval in which the wind generator is operated. If the turbine was operating at a wind speed below $v_{c i}$, the engine wear would be too big to operate in an efficient way. On the other side, the turbine is stopped in case of a wind speed above $\mathbf{v}_{\mathrm{co}}$. This is merely for economic reasons as an operation above $\mathrm{v}_{\mathrm{co}}$ would require a more expensive turbine. $P_{\text {turb }}$ is the power supplied by the turbine. The power that is actually available is further reduced by an efficiency factor $\eta_{w}$ :

$$
\begin{equation*}
P_{\text {Whad }}=\eta_{V} P_{T w r b} \tag{3.2}
\end{equation*}
$$

### 3.2 The Photovoltaic Array

### 3.2.1 The Equivalent Circuit

An equivalent circuit of a single diode model of a solar cell (index $j$ ) is drawn in Fig. 3.2. The current generated by the incoming light is $\mathrm{I}_{\mathrm{phj}}$ and will be discussed in chapter 3.2.4.


Fig. 3.2 Equivalent Circuit of a Solar Cell
$R_{p}$ and $R_{s}$ denote the parallel and the serial resistance. The diode is determined by its quality factor $A$ (usually in the range of $A \in[1,2]$ ) and reverse saturation current $\mathrm{I}_{0 \mathrm{j} \cdot}$. For an array of $N_{s}$ serial and $N_{p}$ parallel solar cells the I-U- characteristic is given by

$$
\begin{equation*}
I=I_{p h}-I_{0}\left[\exp \left(\frac{U+I R_{s}}{U_{T}}\right)-1\right]-\frac{U+I R_{s}}{R_{p}} \tag{3.3}
\end{equation*}
$$

where $\mathrm{U}_{\mathrm{T}}$ symbolizes the thermal voltage

$$
\begin{equation*}
U_{T}=\frac{A k T_{c e l}}{e} \tag{3.4}
\end{equation*}
$$

with elementary charge $e$ and cell temperature $T_{\text {cell }}$. The total series resistance $R_{s}$, photo current $\mathrm{I}_{\mathrm{pb}}$ and reverse saturation current $\mathrm{I}_{0}$ can be calculated from the values of the single cell via

$$
\begin{align*}
I_{p b} & =\boldsymbol{I}_{p b} \boldsymbol{N}_{p} \\
\boldsymbol{I}_{0} & =\boldsymbol{I}_{0,} \boldsymbol{N}_{p} \\
\boldsymbol{R}_{s} & =\boldsymbol{R}_{s,} \frac{\boldsymbol{N}_{s}}{\boldsymbol{N}_{\boldsymbol{p}}} \tag{3.5}
\end{align*}
$$

It is worth mentioning that $R_{p}$ and $R_{s}$ influence the characteristic in a significant way. Fig. 3.3 qualitatively sketches the impact of $R_{p}$ and $R_{s}$. The continuous curve represents the ideal array with $R_{s}=0$ and $R_{p} \rightarrow \infty$, whereas the dotted curves depict the effect of the impedances.


Fig. 3.3 I-U- Characteristic of a Solar Cell

### 3.2.2 PV Power Supply

The power supplied by the photovoltaic array, $P_{\text {sol }}$, is $P_{\text {sol }}=$ UI, where $I$ and $U$ have to satisfy
the characteristic (3.3). In order to find out the point ( $I_{m p}, U_{m p}$ ) for which the maximum power $P_{m p}=I_{m p} U_{m p}$ is supplied by the array, we will simplify the equivalent circuit by omitting the parallel resistance $\mathrm{R}_{\mathrm{p}}$ and we are then able to write the array voltage in the form

$$
\begin{equation*}
U=A U_{T} \ln \left[\frac{I_{p h}-I+I_{0}}{I_{0}}\right]-I R_{s} \tag{3.6}
\end{equation*}
$$

The current at the maximum power point can be assessed by setting the current derivation of the power to zero and it is ([24], eq. 19)

$$
\begin{equation*}
I_{p h}=I_{m p}+I_{0}\left[\exp \left(\frac{2 I_{m p} R_{s}}{A U_{T}}+\frac{I_{m p}}{I_{p h}-I_{m p}+I_{0}}\right)-1\right] \tag{3.7}
\end{equation*}
$$

Equation (3.7) has to be solved numerically for $\mathrm{I}_{\mathrm{mp}}$. $\mathrm{U}_{\mathrm{mp}}$ can be determined by evaluating (3.6). The maximum power will then be the product of both.


Fig. 3.4: Power characteristics of a solar cell

The diagrams in Fig. 3.4 demonstrate the dependency of the maximum power point as a function of the voltage (right hand side) and the photo current (left hand side). Having assumed typical values $\mathrm{R}_{3}=0.05 \Omega, \mathrm{AU}_{\mathrm{T}}=0.0737 \mathrm{~V}$ and $\mathrm{I}_{0}=4.5 \mathrm{~mA}$ we have calculated the maximum power point for given photo currents using the method described above. Some
values are presented in Tab. 3.1

| $\mathrm{I}_{\mathrm{p}}$ [A] | 0.0 | 1.25 | 1.875 | 2.5 | 3.125 | 3.75 | 5.0 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathrm{P}_{\mathrm{mp}}[\mathrm{W}]$ | 0.0 | 0.25 | 0.375 | 0.5 | 0.625 | 0.7 | 0.9 |

Tab. 3.1: Photo current versus maximum power

The values in Tab. 3.1 give rise to the presumption of a linear relation between $P_{m p}$ and $\mathrm{I}_{\mathrm{p}}$. Not quite. The linear approximation is only legitimate for sufficiently small photo currents. Towards larger values of $\mathrm{I}_{\mathrm{ph}}$ the power curve will significantly flatten out as outlined in Fig. 3.4.

In practice, a maximum power tracker may be inserted between the photovoltaic array and the load (i.e. the DC- bus) in order to ensure optimum operation. A maximum power tracking facility is an adjustable ratio DC to DC transformer which basically contains a parallel high frequency MOSFET switch. It provides a matching between the load and the photovoltaic array such that the solar cell is operated in the maximum power point. In general maximum power point trackers can be classified into step-down trackers ([36]) and step-up trackers ([35]). The first one drives a high voltage load from a low voltage PV array whereas the latter one operates vice versa.

It is, however, suggested ([23] p.434) that an MPP tracker does not pay off in case it requires additional hardware. Jantsch ([23]) reports a best fixed voltage system which yields an annual energy output of $98.4 \%$ of an MPP operated system.
For the purpose of this paper we assume that a reasonably good power tracker (with efficiency $\eta_{\text {mpl }}$ ) is in charge. The power delivered by the solar cell will then be reduced to

$$
\begin{equation*}
\boldsymbol{P}_{s o l}=\boldsymbol{\eta}_{m p t} \boldsymbol{P}_{m p} \tag{3.8}
\end{equation*}
$$

In case no MPP tracker was used, the factor $\eta_{\text {mpt }}$ would summarily cover the expected
losses, caused by the lack of an MPP tracker.

### 3.2.3 Temperature Dependency

Unlike the wind turbine the solar cell characteristics vary sensitively with the temperature. In general, the cell efficiency will decrease upon increasing temperature. The influence of the temperature can be included in equations (3.3) and (3.7) by applying ([24] eq. 16-18)

$$
\begin{array}{rlr}
I_{0}(T) & =I_{0}\left(T_{r}\right)\left(\frac{T}{T_{r}}\right)^{3} \exp \left(-b\left(\frac{1}{T}-\frac{1}{T_{r}}\right)\right) & \\
I_{p b}(T) & =I_{p b}\left(T_{r}\right)\left(1+a\left(t-T_{r}\right)\right) & a=5.7 E-4  \tag{3.9}\\
U_{T}(T) & =U_{T}\left(T_{r}\right) \frac{T}{T_{r}} &
\end{array}
$$

where $\mathrm{T}_{\mathrm{r}}$ is a reference temperature (usually $25^{\circ} \mathrm{C}$ ). If hourly mean temperature values throughout the year are given, we will employ (3.9). Otherwise, the values at reference point are used. However, calculations in this paper have been carried out without taking the temperature dependency into account.

### 3.2.4 Photo Current and Efficiency

Only a fraction of the energy of the incoming light can be converted into electric energy for several reasons:

- Photons with an energy $h v<\mathrm{E}_{\mathrm{g}}$ ( $\mathrm{E}_{\mathrm{g}}$ stands for the minimum band gap of the semi conductor) will not be absorbed.
- The surplus energy of absorbed photons will be thermalized, thus causing even a further reduction of the efficiency as temperature rises.
- Not every generated electron contributes to a voltage $\mathrm{eE}_{\mathrm{g}}$.
- Already absorbed electrons are likely to be recombined, especially if they are close to surfaces.
- Even if the light beam and the array surface were perpendicular a reflexion would be caused due to the different refraction indices of the air and the semi conductor.
For the purpose of this paper, however, we are content to introduce an efficiency factor $\zeta_{\text {sol }}$
that summarizes all the mentioned processes and assume a linear relationship

$$
\begin{equation*}
I_{p h}=A \zeta_{s a l} \Phi_{\perp} \tag{3.10}
\end{equation*}
$$

between the photo current and the product of the intensitiy of the perpendicular light $\phi_{\perp}$ and the active array area A (not to be confused with the diode factor A introduced previously). For a silicon solar cell, for example, it is $\zeta_{\text {sol }} \approx 0.28 \mathrm{AW}^{-1}$ ([9] p.73).

### 3.3 Combined Renewable Power

The renewable power supply consists of both the wind power (3.2) and the solar power (3.8). As far as the photovoltaic array is concemed, we assume a linear relationship between the maximum output power and the photo current (chapter 3.2.2). Taking (3.10) into account, a linear relationship between the solar power $P_{s o l}$ and the clearness index $k$ (see chapter 2.2),

$$
\begin{equation*}
P_{s a l}=\xi_{s o l} k \tag{3.11}
\end{equation*}
$$

can be concluded. The maximum power will be supplied by the photvoltaic array if the clearness index reaches its maximum. Suppose the maximum clearness index is $\mathrm{K}_{0}$. This coefficient can be used to normalize the solar power,

$$
\begin{equation*}
p_{s}=\min \left\{\frac{P_{s o l}}{\xi_{s o l} K_{0}}, 1\right\}=\min \left\{\frac{k}{K_{0}}, 1\right\} \tag{3.12}
\end{equation*}
$$

for simplification of further calculations. The $\min$ - operator is used to ensure that the normalized power is within the range $p_{s} \in[0,1]$. For a clearness index $k>K_{0}$ the power output will not increase as the system is in saturation. In the same manner, the wind turbine power (3.1), (3.2) is normalized to the rated power,

$$
\begin{equation*}
p_{\psi}=\frac{P_{w i n d}}{\eta_{r} P_{r}}=\frac{P_{\text {turb }}}{P_{r}} \tag{3.13}
\end{equation*}
$$

The total renewable power, $P_{\text {rea }}$, is $P_{\text {ren }}=P_{\text {wind }}+P_{\text {sol }}$. Its maximum $P_{\text {rea, max }}$ is reached when the wind turbine is operated in its rated power and the clearness index is $k=K_{0}$. Hence, the
maximum is $P_{\text {ren, max }}=\xi_{\text {sol }} K_{0}+\eta_{w} P_{r}$. Introducing the dimensionless parameter

$$
\begin{equation*}
\zeta=\frac{1}{1+\frac{\eta_{w} P_{r}}{\zeta_{s a l} K_{0}}} \tag{3.14}
\end{equation*}
$$

an elegant normalized expression for the total renewable power is given by

$$
\begin{equation*}
p_{\text {rea }}=\frac{P_{r e n}}{P_{\text {rea, max }}}=\zeta p_{s}+(1-\zeta) p_{\pi} \tag{3.15}
\end{equation*}
$$

The normalized parameters $p_{s}, p_{w}$ and $p_{\text {ren }}$ are dimensionless numbers in the interval $[0,1]$. In the next chapter we will resume the discussion from chapter 2 by extending the statistical models to the normalized renewable power.

## 4. Statistical System Modelling

The previous chapter was concerned with the modelling of the electric power supplied by the various components of the system. Assume for the moment that all components are linked together in one system. The output of the system, which is the total power, is obviously depependant on a huge variety of parameters, that can be categorised:

## (i) Fixed Parameters

Fixed parameters do not change their value during operation of the system. For example, the choice of a wind turbine determines cut-in, cut-out and rated wind speed. Once the wind turbine is chosen, they can not be altered.
(ii) Random Input Parameters

Random input parameters are the wind speed, $v$, the clearness index, $k$, and the external power demand, due to their very nature.
(iii) Derived Random Parameters

Derived random parameters are parameters that depend on the random input parameters. For instance, the mean wind speed.
(iv) Controller Dependant Parameters

These are parameters whose values are influenced by the controller. For instance, the state of charge of the battery falls into this category as the controller determines whether to charge or discharge the battery.
Please note that the parameter categories listed here are not mutually exclusive. The state of charge, for example, is both a derived random and a controller dependant parameter. The intention of the categotisation is much more to focus on the fact that, although concise models for the power supply have been developed, the behaviour of many a parameter is all but fixed. Due to the statistical nature of wind speed and clearness index, the whole system is a non- deterministic system, which can only be described employing statistical methods. There are several reasons for doing this.
First, it leads to a better appreciation of the influence of both the random input parameters and fixed parameters on the system.
Second, synthetic time series of the power output can be used for an off-line optimization of some of the fixed parameters. For instance, the fractional power factor (i.e. the ratio
between rated wind and rated solar power) could be optimized off-line for given (typical) wind and clearness index data taken at the site in question.
Third, statistical methods can be used to predict the power supplied by the renewable energy sources or the state of charge for given observations of the random input parameters and the state of charge. Again, this might be interesting for a better understanding of what is going on in the system. Though, there is another reason. As mentioned in the introduction (section 1), the main purpose of the controller in this hybrid system is to be in charge of the battery (charging, discharging or disconnecting) and the diesel (switch on and off). Statistical methods could be used to design the controller, which is not covered in this paper. For instance, various control policies could be compared off-line by generating time series. Later in this chapter, a very crude battery control policy is applied to generate time series of the state of charge. In this instance, the battery is being discharged (if possible) as soon as the renewable energy sources can not meet the power demand and it is always charged at times when there is a surplus. Other, more sophisticated policies can be easily implemented (or incorporated in the programme) as the important tools are developed here. The controller could, however, as well use statistical methods (e.g. first passage times) on-line and decide depending on those values. Hence, the methods developed here can be used at design stage as well as during operation.

This chapter is divided into three sections, of which the first is concerned with distribution functions. The second section covers the generation of synthetic time series of the power supplied by the renewable energy sources and the state of charge of the battery. The last section takes a deeper look at first passage time problems.

### 4.1 Distributions

The purpose of this section is to introduce the probability distribution functions of some stochastic processes that occur in the system. The first part is devoted to the wind speed. It is only included because the mathematical functions involved are simple, thus helping to appreciate the formalism and methods. The main emphasis however, is placed on the wind
turbine power and the photovoltaic array power. The discussion on distributions closes with the distribution of the joint renewable power, which is the sum of the power supplied by the wind turbine and the photovoltaic array.

### 4.1.1 Wind Speed Distribution

Let us first recall the conditional probability density function $f_{v}\left(v i v(0)=v_{0}\right)$ of the wind speed $v$ from equation (2.10), here in unnormalized form,

$$
\begin{equation*}
f_{V}\left(v \mid \nabla(0)=v_{0}\right)=\frac{1}{\sqrt{2 \pi \sigma_{V}^{2}\left(1-r_{v}^{2}\right)}} \exp \left[-\frac{1}{2}\left(\frac{v-\left(\bar{v}+\left(V_{0}-\bar{v}\right) r_{v}\right)}{\sigma_{V} \sqrt{\left(1-r_{v}^{2}\right)}}\right)^{2}\right] \tag{4.1}
\end{equation*}
$$

with the corresponding distribution function

$$
\begin{equation*}
F_{v}\left(v \mid v(0)=v_{0}\right)=\Phi\left(\frac{v-\left(\bar{v}+\left(v_{0}-\bar{v}\right) r_{v}\right)}{\sigma_{v} \sqrt{1-r_{v}^{2}}}\right) \tag{4.2}
\end{equation*}
$$

Fig. 4.1 and Fig. 4.2 depict the probability density and the corresponding distribution function of the wind speed fluctuations for a mean wind speed of $16 \mathrm{~m} / \mathrm{s}$ and three values for the standard deviation $\sigma_{v}$, where stationarity is assumed (I.e. $r_{v}=0.0$ ). For each graph 50 values have been calculated. Both pictures clearly display the influence of the standard variation. Increasing the standard deviation has the effect of increasing the probability for wind speed values that are further away from the mean.


Fig. 4.1 Wind Speed Probability Density Function


Fig. 4.2 Wind Speed Distribution Function

### 4.1.2 Wind Turbine Power Distribution

If we consider the random variable to be the input of the wind turbine characteristic (3.1) the distribution function of the normalized wind power $p_{w}$ (eq. 3.13) can be expressed in terms of $F_{v}\left(v \mid v_{0}\right)^{7}$ (eq. (4.2)),

$$
F_{p w}\left(p_{w} \mid V_{0}\right)= \begin{cases}0 & p_{\varpi}<0  \tag{4.3}\\ F_{v}\left(v_{d}+\sqrt[3]{p_{w}}\left(v_{r}-v_{d}\right) \mid v_{0}\right)-F_{v}\left(v_{\infty} \mid v_{0}\right)+1 & 0 \leq p_{\varpi} \leq 1 \\ 1 & p_{\varpi}>1\end{cases}
$$

Here, the short hand $\mathrm{F}_{\mathrm{pw}}\left(\mathrm{p}_{\mathrm{w}} \mid \mathrm{V}(0)=\mathrm{v}_{0}\right)=\mathrm{F}_{\mathrm{pw}}\left(\mathrm{p}_{\mathrm{w}} \mid \mathrm{v}_{0}\right)$ is used. Most conditional distribution functions in this paper are referred to by this notation. The wind power probability density function is attained by derivation:

Since the wind turbine $P(v)$ characteristic (eq. 3.1) is not differentiable at $v=v_{r}$ and $v=v_{c o}$, the distribution function $\mathrm{F}_{\mathrm{pw}}(\mathrm{v})$ reveals discontinuities at $\mathrm{p}_{\mathrm{w}}=0$ and $\mathrm{p}_{\mathrm{w}}=1$. This explains the emergence of the Dirac- function in the probability density function. In order to avoid these computational problems connected with the Dirac function, the power scale will be discretized,

$$
\begin{equation*}
p_{w, n}=\frac{n-1}{N-1} \quad, n=1 \ldots N \tag{4.5}
\end{equation*}
$$

where N power levels are allowed. As the power is now a discrete random variable, its distribution function will be a stair function with the distinct values

[^6]\[

$$
\begin{equation*}
G_{p \varpi}\left(n \mid v_{0}\right)=F_{p \varpi}\left(\left.\frac{n-1}{N-1} \right\rvert\, v_{0}\right) \tag{4.6}
\end{equation*}
$$

\]

The probability density function will now be replaced by a discrete probabilty function with values

$$
g_{p w}\left(n \mid V_{0}\right)= \begin{cases}G_{p w}\left(1 \mid V_{0}\right) & n=1  \tag{4.7}\\ G_{p w}\left(n \mid V_{0}\right)-G_{p w}\left(n-1 \mid V_{0}\right) & n=2 \ldots N\end{cases}
$$

The value $g_{p w}\left(n_{i} v_{0}\right)$ is the probability that - at time $t$ - a power output $p_{w} \in\left[p_{w, R-1}, p_{w, \Omega}\right]$ may be observed under the condition that the wind speed was $v(0)=v_{0}$ at time $t=0$. Summing up all $\mathrm{g}_{\mathrm{wp}}\left(\mathrm{n} \mid \mathrm{v}_{0}\right)$ over n yields 1.
The discussion of the functions $g_{p w}\left(n_{\mid} v_{0}\right)$ and $G_{p w}\left(n \mid v_{0}\right)$ is conducted in two parts. First, we restrict ourselves to the stationary case. This is when the correlation coefficient r marches towards 1 . Hence, the initial value has no influence on the stationary distribution.

### 4.1.2.1 Stationary Distribution

Fig. 4.3 shows probability functions $g_{p w}\left(n_{\mid} \mid v_{0}\right)$ for four different mean wind speeds as functions of the normalized power with $N=51$ (4.5). For the rated wind speed, cut-in speed, cut-out speed and the standard variation $\sigma_{\mathrm{v}}$ typical values have been assumed. These constant parameters are displayed above each diagram. In Fig. 4.3 the values for $p_{s}=1$ are omitted because of their magnitude. The curve with $\bar{v}=18 \mathrm{~m} / \mathrm{s}$ for instance has a high probability for maximum power 1 eventhough it is not explicitly displayed. A better representation is therefore Fig. 4.4 where the corresponding distribution functions $\mathrm{G}_{\mathrm{pw}}\left(\mathrm{n} \mid \mathrm{v}_{0}\right)$ are depicted. For a mean wind speed that is well below the rated wind speed ( $\bar{v}=12 \mathrm{~m} / \mathrm{s}$ in comparison to $\mathbf{v}_{\mathrm{r}}$ $=16 \mathrm{~m} / \mathrm{s}$ ) the shape of the probability function of the wind turbine power is almost the same as the one for the wind speed itself as the maximum power ( $\mathrm{p}=1$ ) is very unlikely. Increasing the wind speed increases the probability for maximum power which causes the distribution function to jump to 1 at $p=1$. Mathematically, this is due to the fact that the probability function is not zero at $\mathrm{p}=1$. Physically, the reason for this is that a whole
continuum of wind speed values do cause the same power, the maximum power (eq. 3.1).


Fig. 4.3 Wind Turbine Power: Stationary Distribution


Fig. 4.4 Wind Turbine Power: Stationary Distribution

In Fig. 4.5 the probability function is shown for different rated wind speeds. It makes clear that the variation of the rated wind speed is on a par with the variation of the mean wind speed. The set of curves is almost identical to the set in Fig. 4.3.


Fig. 4.5 Wind Turbine Power: Stationary Distribution

Eventually, Fig. 4.6 shows the influence of the standard variation $\sigma_{v}$. For comparison, the curve with $\sigma_{v}=1 \mathrm{~m} / \mathrm{s}$ is included in Fig. 4.5. As expected the probability curve becomes flatter while increasing the standard variation. A significant aspect is the increased probability at zero power in the $\sigma_{v}=4 \mathrm{~m} / \mathrm{s}$ curve. This is forced by the cut-out wind speed below which the turbine power is zero, eventhough the wind speed is not. Again, the values at $\mathrm{p}=1$ are omitted for the sake of a reasonable scale.


Fig. 4.6 Wind Turbine Power: Stationary Distribution

Fig. 4.7 shows the corresponding distribution functions including the jumps at $\mathrm{p}=1$. Note that the height of the jump at $p=1$ is equal to the probability that the system delivers maximum power.


Fig. 4.7 Wind Turbine Power: Stationary Distribution

### 4.1.2.2 Conditional Distribution

Having examined the stationary case light is now shed on the conditional probability distribution. Fig. 4.8 illustrates the impact of the time on the probability function. The initial wind speed was chosen to be $12 \mathrm{~m} / \mathrm{s}$, well below the mean wind speed. At time $\mathrm{t}=0$ the wind speed is known. Hence, the probability for one particular power value is one. As time goes by the range broadens and its peak moves towards the peak which corresponds to the mean wind speed. In fact, the stationary solution for this particular setting is included in Fig. 4.3. The graphical representation of $g_{p w}\left(n_{\mid} \mid v_{0}\right)$ in Fig. 4.8 emphasizes the fact that the power scale is discretized. It is worth pointing out that the time scale is not necessarily a typical one. Throughout the paper the time always appears in the product $\beta$ t in the autocorrelation function. By chosing a different $\beta$ the time scale will vary accordingly. For the calculations of the probability distributions an arbitrary value $\beta_{\mathrm{w}}=0.5 \mathrm{~s}^{-1}$ is assumed. Different values, however, do not affect the results.


Fig. 4.8 Wind Turbine Power: Conditional Distribution

In Fig. 4.9 the probability function is shown for a set of initial wind speeds at one particular time $t=0.2 \mathrm{~s}$. For cross reference, the curve with initial wind speed $v(0)=12 \mathrm{~m} / \mathrm{s}$ is also included in Fig. 4.8. Bearing in mind that both the rated wind speed and the mean wind speed are $16 \mathrm{~m} / \mathrm{s}$ it is clear why the curve with initial wind speed $v(0)=18 \mathrm{~m} / \mathrm{s}$ is virtually zero anywhere except at maximum power $\mathrm{p}=1$.

$$
\beta_{\mathrm{w}}=0.5, \mathrm{v}_{\mathrm{p}}=16 \mathrm{~m} / \mathrm{s}, v_{\operatorname{mean}}=16 \mathrm{~m} / \mathrm{s}, v_{\mathrm{d}}=2.8 \mathrm{~m} / \mathrm{s}, \mathrm{v}_{\infty}=24 \mathrm{~m} / \mathrm{s}, \sigma_{\mathrm{v}}=1 \mathrm{~m} / \mathrm{s}, \mathrm{t}=0.2 \mathrm{~s}
$$



Fig. 4.9 Wind Turbine Power: Conditional Distribution

The corresponding distribution functions $\mathrm{G}_{\mathrm{pw}}\left(\mathrm{n}_{\mathrm{I}} \mid \mathrm{v}_{0}\right)$ are depicted in Fig. 4.10.

$$
\beta_{\mathrm{w}}=0.5, v_{\mathrm{s}}=16 \mathrm{~m} / \mathrm{s}, v_{\mathrm{mexa}}=16 \mathrm{~m} / \mathrm{s}, v_{\mathrm{ft}}=2.8 \mathrm{~m} / \mathrm{s}, \mathrm{v}_{\mathrm{m}}=24 \mathrm{~m} / \mathrm{s}, \sigma_{\mathrm{v}}=1 \mathrm{~m} / \mathrm{s}, \mathrm{t}=0.2 \mathrm{~s}
$$



Fig. 4.10 Wind Turbine Power: Conditional Distribution

Fig. 4.11 displays curves with different mean wind speeds for an initial wind speed $v_{0}=$ $12 \mathrm{~m} / \mathrm{s}$ at time $\mathrm{t}=0.5 \mathrm{~s}$. This is the same setting as in Fig. 4.3. That means that the curves in Fig. 4.11 move to Fig. 4.3 for $t \rightarrow \infty$. The interpretation is simple. Under higher mean wind speeds the system moves more quickly to higher power values than under lower mean wind speeds.


Fig. 4.11 Wind Turbine Power: Conditional Distribution

### 4.1.3 PV Array Power Distribution

### 4.1.3.1 Stationary Distribution

In analogy to chapter 4.1.2 the normalized solar power scale (3.12) will be discretized by

$$
\begin{equation*}
p_{s, n}=\frac{n-1}{N-1} \quad, n=1 \ldots N \tag{4.8}
\end{equation*}
$$

With the normalizations (4.8) and (2.70) and assuming the linear relationship (3.12), the
stationary distribution function $\mathrm{F}_{\mathrm{ps}}(\mathrm{n})$ can be phrased in terms of the distribution function $F_{x}(x)$ (eq. 2.79),

$$
\begin{equation*}
G_{p s}(n)=F_{x}\left(\frac{K_{0} \frac{n-1}{N-1}-k_{\min }}{k_{\max }-k_{\min }}\right) \tag{4.9}
\end{equation*}
$$

Similar to (4.7), a stationary probability function can be obtained from

$$
g_{p s}(n)= \begin{cases}G_{p s}(1) & n=1  \tag{4.10}\\ G_{p s}(n)-G_{p s}(n-1) & n>1\end{cases}
$$

The stationary probability function $\mathrm{g}_{\mathrm{ps}}(\mathrm{n})$ is shown in Fig. 4.12 for 3 different clearness indexes and a constant standard variation $\sigma_{\mathrm{k}}$. Again, the power is divided up into $\mathrm{N}=51$ values. The maximum (normalized) clearness index $\mathrm{K}_{0}=1.3$ is assumed. Fig. 4.12 reveals that the probability function has in general two maxima due to the superposition of 2 betadistributions. A higher clearness index moves both maxima towards maximum power. At the same time the peak of the low power maximum decreases in favor of the high power maximum.


Fig. 4.12 PV Array Power: Stationary Distribution

This becomes even clearer in Fig. 4.13, where the corresponding distribution functions $G_{p s}(n)$ are drawn. This is an interesting result. Obviously, the system has two preferential points, neither of whom is the average. Hence, it is expected that the solar power sometimes may change rather abruptly by jumping from one to the other peak. In fact, this can be seen in the discussion of time series in chapter 4.2 .


Fig. 4.13 PV Array Power: Stationary Distribution

In the graph depicting the distribution functions, the curves with higher clearness index are below the ones with a smaller $k$. Remember that any distribution function $F(x)$ returns the probability that the system is in a state less than or equal $\mathbf{x}$.
The impact of the standard variation $\sigma_{k}$ is illustrated in Fig. 4.14 and Fig. 4.15. In the event of a small standard deviation $\sigma_{\mathbf{k}}$ the probability function is very much centered having one peak only. Larger values cause the two peaks that are mentioned earlier to seperate and drift apart towards minimum and maximum power respectively.


Fig. 4.14 PV Array Power: Stationary Distribution


Fig. 4.15 PV Array Power: Stationary Distribution

The matching distribution functions in Fig. 4.15 disclose yet another pecularity. The power
at which the distribution function is 0.5 is independent of the standard deviation. This power point is only a function of k and $\mathrm{K}_{0}$. Hence, $\sigma_{\mathrm{k}}$ has an impact on the weighting and not on the average.


Fig. 4.16 PV Array Power: Stationary Distribution

In Fig. 4.16 curves are drawn with the maximum cleamess index $\mathrm{K}_{0}$ as parameter. This parameter was introduced in (3.12) to normalize the power scale. It specifies the clearness index above which the maximum power is attained. In general, a larger $K_{0}$ permits higher power values and broadens the shape of the probability function. It has, however, no effect on the qualitative course of the curve.

### 4.1.3.2 Conditional Distribution

In analogy to the previous section the discrete, conditional distribution function $\hat{\mathrm{G}}_{\mathrm{ps}}\left(\mathrm{n} \mid \mathrm{k}_{0}\right)$ of the solar power can be phrased in terms of the approximating conditional distribution function $F_{x}(x)$ (eq. 2.91):

$$
\begin{equation*}
\hat{G}_{p o}\left(n \mid k_{0}\right)=\hat{F}_{x}\left(\left.\frac{K_{0} \frac{n-1}{N-1}-k_{\min }}{k_{\max }-k_{\min }} \right\rvert\, \frac{k-k_{\min }}{k_{\max }-k_{\min }}\right) \tag{4.11}
\end{equation*}
$$

Similar to (4.10) the discrete, conditional probability function can be obtained from

$$
\hat{g}_{p s}\left(n \mid k_{0}\right)= \begin{cases}\hat{G}_{p s}\left(1 \mid k_{0}\right) & n=1  \tag{4.12}\\ \hat{G}_{p o}\left(n \mid k_{0}\right)-\hat{G}_{p p}\left(n-1 \mid k_{0}\right) & n>1\end{cases}
$$

Please note that the hat on $\hat{\mathrm{g}}_{\mathrm{ps}, \mathrm{n}}$ signals that the normal distribution expansion (2.82) is applied. For large time values $t \rightarrow \infty, \hat{\mathrm{G}}_{\mathrm{ps,n}}$ represents the unconditional distribution function as the autocorrelation coefficient $\mathrm{r}_{\mathrm{x}}$ touches zero.


Fig. 4.17 PV Array Power: Conditional Distribution

In Fig. 4.17 an initial clearness index $\mathrm{k}(0)=0.1$ is assumed. The diagram shows the conditional probability function at 4 different times. Again, at time $t=0$ the probability to observe the power value that corresponds to $\mathrm{k}(0)$ is 1 . Later, the main bulk of the probability
function moves on to higher power values.
Another interesting feature is the variation of the initial value $\mathrm{k}(0)$ as displayed in Fig. 4.18. It is no accident that the three curves have the same shape. It can be concluded from the conditional distribution function (2.91) that

$$
\begin{equation*}
\hat{F}_{2}\left(x \mid x_{1}\right)=\hat{F}_{2}\left(\left(x_{1}-x_{0}\right) r+x \mid x_{1}\right) \tag{4.13}
\end{equation*}
$$

Hence, any variation of the initial clearness index can be translated into a shift along the clearness index axis. It finds its manifestation in Fig. 4.18.


Fig. 4.18 PV Array Power: Conditional Distribution

### 4.1.4 Combined Power Distribution

Given the conditional probability functions for the wind turbine power (eq. (4.7)) and the solar power (eq. (4.12)), the total renewable power $p_{\text {ren }}$ (eq. 3.15) can be obtained via
convolution ${ }^{8}$ if the stochastic processes of the wind speed and the clearness index are thought to be independent. Precedent to that let us denote the probability functions of $\left(\zeta p_{s}\right)$ and (1$\left.\zeta \mathrm{p}_{\mathrm{s}}\right)$,

$$
\begin{equation*}
h_{p s}(n)=\hat{g}_{p s}\left(\left.\frac{n}{\zeta} \right\rvert\, k_{0}\right) \quad, \quad h_{p w}(n)=g_{p w}\left(\left.\frac{n}{1-\zeta} \right\rvert\, v_{0}\right) \quad, \quad n=1 \ldots N \tag{4.14}
\end{equation*}
$$

before we can write the discrete probability function $g_{\text {prea }}\left(n_{i} v_{0}, k_{0}\right)$ subject to the initial conditions $v(0)=v_{0}$ for the wind speed and $k(0)=k_{0}$ for the clearness index,

$$
\begin{equation*}
g_{P_{\text {ren }}}\left(n \mid v_{0}, k_{0}\right)=\sum_{j=1}^{N} h_{p w}(J) \operatorname{hps}(n-j) \quad, \quad n=1 \ldots N \tag{4.15}
\end{equation*}
$$

The calculation of the convolution can be considerably speeded up by using the distribution functions rather than the probability functions. Hence, we define

$$
H_{p w}(i)= \begin{cases}0 & i<1  \tag{4.16}\\ G_{p w}\left(\left.\frac{i}{1-\zeta} \right\rvert\, V_{0}\right) & 1 \leq i \leq N \\ 1 & i>N\end{cases}
$$

and

$$
H_{p s}(\lambda)= \begin{cases}0 & i<1  \tag{4.17}\\ \hat{G}_{p s}\left(\left.\frac{i}{\zeta} \right\rvert\, k_{0}\right) & 1 \leq i \leq N \\ 1 & j>N\end{cases}
$$

leading to

$$
\begin{gather*}
h_{p s}(J)=H_{p s}(J)-H_{p s}(j-1) \\
h_{p w}(J)=H_{p w}(J)-H_{p w}(j-1) \tag{4.18}
\end{gather*}
$$

[^7]Now, the $\mathrm{H}_{\mathrm{ps}}$ and $\mathrm{H}_{\mathrm{pw}}$ values can be stored in vectors prior to the calculation of the convolution sum (4.15).

The stationary probability function is depicted in Fig. 4.19 with the fractional power factor $\zeta$ as paramter. In case of $\zeta=0.0$ only the wind turbine is used and the corresponding curve coincides with the $\overline{\mathrm{v}}=16 \mathrm{~m} / \mathrm{s}-$ curve in Fig. 4.3. On the other hand $\zeta=1.0$ signifies that the wind turbine is switched off with the resulting curve being the one in Fig. 4.19. The remnant two curves clearly mark the transition from one extreme to the other.


Fig. 4.19 PV Array Power: Conditional Distribution

As far as the conditional distribution is concerned, two scenarios are displayed for one specific time with $\zeta$ as parameter. First, in Fig. 4.20 a sudden wind speed slump (initial wind speed $v_{0}=8 \mathrm{~m} / \mathrm{s}$ in relation to a mean wind speed $\overline{\mathrm{v}}=16 \mathrm{~m} / \mathrm{s}$ ) is assumed. It is no surprise that a higher proportion of solar energy (greater $\zeta$ ) causes the probability function at time $t$ $=0.1 \mathrm{~s}$ to have its peak at higher power values than in the wind turbine - only case.
The second scenario, as shown in Fig. 4.21, assumes a clearness index slump (initial clearness index $\mathrm{k}_{0}=0.1$ and mean value $\mathrm{k}=0.7$ ).
Both scenarios demonstrate that a hybrid energy system is able to offset or at least restrain
the effect of fluctuations, thus stabilizing the system. This discussion is continued in the chapter on time series where the same parameter settings will be encountered.


Fig. 4.20 Joint Renewable Power: Wind Speed Slump


Fig. 4.21 Joint Renewable Power: Clearness Index Slump

### 4.2 Time Series

### 4.2.1 A General Time Series Algorithm

The purpose of this section is to present an algorithm to calculate synthetic time series of any stochastic process. It is applied to the processes discussed above in the following part.

Before defining the algorithm the framework has to be set out. First, let $F_{\xi}\left(\xi, \Delta t \mid \omega_{0}\right)$ denote the conditional distribution function with respect to the random variable $\xi$ at time $\Delta t$ subject to the initial value $\omega_{0}$. Here, $\xi$ and $\omega$ are vectors. In the framework of this paper they usually have one component, which corresponds either to the wind speed or the clearness index. Only in the case of the joint renewable power both components are needed. A function $\Xi(\xi)=\omega$ translates a given $\xi$ into an initial vector. It is assumed that the inverse function $\Xi^{-1}(\omega)$ exists. Often, it is not the random variable $\xi$ that is the desired magnitude. Therefore, a function $\psi=\Psi(\xi)$ is assumed that maps the vector $\xi$ to a scalar variable $\psi$. Finally, a random number generator ${ }^{9}$ is assumed that produces the random realizations, $\boldsymbol{\xi}$. This random number generator is a functional of the underlying conditional distribution function $F\left(\xi, \Delta t ; \omega_{0}\right)$, where $\Delta t$ is the desired time step and $\omega_{0}$ the set of initial values. Hence, it can be written as

$$
\begin{equation*}
\xi=\varrho\left[F_{\xi}\left(\xi, \Delta t \mid \omega_{0}\right)\right] \tag{4.19}
\end{equation*}
$$

Given this preliminary, the algorithm to generate time series with values $\psi_{j}$ and a time step $\Delta t$ between any two values can now be formulated.
(1) Denote the set of initial values as $\omega_{0}$. Calculate the first value of the time series from $\psi_{0}=\Psi\left[\Xi^{-1}\left(\omega_{0}\right)\right]$.
(2) $\operatorname{Set} \mathrm{j}=1$
(3) Initialize the random number generator with the current time. Link it to the underlying conditional distribution function. Set all initial values and the time step.
(4) Determine the next random vector $\xi_{j}=e\left[F_{\xi}\left(\xi, \Delta t: \omega_{j-1}\right)\right]$

[^8](5) Calculate set of initial values for next call: $\omega_{j}=\Xi\left(\xi_{j}\right)$
(6) Calculate next output value $\psi_{j}=\Psi\left(\xi_{j}\right)$
(7) Update $\mathbf{j}=\mathbf{j}+1$
(8) If enough values have been calculated go back to step (3) to generate next value. Otherwise continue at (9).
(9) End of algorithm.

Each value is generated successively in step (4) by taking the last set of realizations, $\boldsymbol{\xi}$, as initial values of the conditional distribution that governs the random number generator in the following call. Hence, each time the generator is being called the underlying distribution function might be different. At first glance, this algorithm might appear to be a bit nebulous. It will, however, gain substance in the following section. The reason for the general approach is that it allows an elegant implementation, independent of a specific distribution function ${ }^{10}$ or requirements.

### 4.2.2 Case Study

### 4.2.2.1 Wind Speed Time Series

In case of wind speed time series the vectors have only one component, the wind speed, $\boldsymbol{\xi}$ $=\omega=\mathrm{v}$ which coincides with the desired output magnitude, $\Psi(\xi)=\xi$. The underlying, conditional distribution function (4.2) is the well- known normal distribution ${ }^{11}$. Time series have been calculated for two parameter settings, the same as for the distribution functions in Fig. 4.1. In Fig. 4.22 three series are shown that have been generated using the same parameters. Fig. 4.23 shows three series based on the same parameters as in Fig. 4.22, except the standard variation being twice the previous value. The graphs clearly speak for themselves.

[^9]

Fig. 4.22 Wind Speed Time Series


Fig. 4.23 Wind Speed Time Series

### 4.2.2.2 Wind Turbine Power Time Series

Again, the underlying stochastic process is the wind speed. Therefore the same random generator can be used as before in the case of wind speed time series. The difference is the output function $\Psi(\xi)$ which is now the wind turbine P-v- characteristic (3.1), normalized by (3.13). The diagrams in Fig. 4.25, Fig. 4.24 and Fig. 4.26 show normalized power time series for different mean wind speeds.
In Fig. 4.24 the mean wind speed ( $\bar{v}=14 \mathrm{~m} / \mathrm{s}$ ) is below the rated wind speed ( $\mathrm{v}_{\mathrm{r}}=16 \mathrm{~m} / \mathrm{s}$ ) and the power slowly picks up. Concluding from the diagram it takes around 8 s to pass the power level $\mathrm{p}=0.6$ for the first time.


Fig. 4.24 Wind Turbine Power Time Series


Fig. 4.25 Wind Turbine Power Time Series


Fig. 4.26 Wind Turbine Power Time Series

In Fig. 4.25 and Fig. 4.26 the power will pick up a lot faster due to higher mean wind speeds of $16 \mathrm{~m} / \mathrm{s}$ and $18 \mathrm{~m} / \mathrm{s}$ respectively. A guess for the first passage time based on the graphs is 2 s and 3 s . Obviously, these are only very crude estimations of the first passage time and methods to calculate it are actually the center of discussion in the next chapter. We will, however, get back to these graphs in order to relate the results to single time series.

### 4.2.2.3 PV Array Power Time Series

The conditional distribution function to be applied to photovoltaic power time series is $\hat{\mathrm{G}}_{\mathrm{ps}}\left(\mathrm{n} \mid \mathrm{k}_{0}\right)$ from equation (4.11). The discrete power level $\mathrm{n} \in[1, N]$ can be identified with n $=\xi$, whereas the initial condition is $\mathrm{k}_{0}=\omega_{0}$. As a result of this the functions $\Xi$ and $\Psi$ are set to be

$$
\begin{align*}
& \Xi(n)=K_{0} \frac{n-1}{N-1} \\
& \Psi(n)=\frac{n-1}{N-1} \tag{4.20}
\end{align*}
$$

taking into account the normalization of the solar power (3.12) and the discretization (4.8). The time series values, produced from $\Psi(n)$, represent the normalized, discrete power. The random number generator used is described in chapter 6.6.3.
In Fig. 4.27 three time series have been recorded for a clearness index $\mathrm{k}=0.29$ and a standard deviation $\sigma_{k}=0.08$. Once it has picked up the power stays within the range of the peak of the stationary probability function (as depicted in Fig. 4.16) which has only one peak for this particular parameter setting.
In contrast, Fig. 4.28 displays 3 time series with clearness index $\mathrm{k}=0.7$, standard deviation $\sigma_{\mathrm{k}}=0.35$ and otherwise identical parameters. The data in Fig. 4.12 is consistent with two peaks in the distribution.
The three time series in Fig. 4.29 correspond to the probability functions in Fig. 4.16 whose peaks match closely to the values of the time series.


Fig. 4.27 PV Array Power Time Series


Fig. 4.28 PV Array Power Time Series


Fig. 4.29 PV Array Power Time Series

### 4.2.2.4 Joint Renewable Power Time Series

In case of joint renewable power time series the vectors $\xi$ and $\omega$ hold two components. The first is identical to the wind power case, the second to the solar power case. The two underlying stochastic processes are treated completely separate throughout, including two random number generators. They are only brought together in the output function $\Psi(\xi)$ which coincides with the normalized expression for the total renewable power (3.15). The following diagrams, Fig. 4.30 and Fig. 4.31, take up the scenarios from last chapter, namely Fig. 4.20 and Fig. 4.21. They illustrate - what was already predicted then - that a combination of two renewable energy sources stabilizes the system and smoothens the output.


Fig. 4.30 Wind Speed Slump


Fig. 4.31 Clearness Index Slump

### 4.2.2.5 State of Charge Time Series

In case of time series tracking the state of charge of the battery, the joint renewable time series generator is being used. Given the joint renewable power at each time step, the state of charge can be calculated. Using the Manwell battery model, the state of charge can be determined as follow:
(i) Prior to the initialisation of the time series generator the amount of available charge at the beginning, $Q_{10}$, and the amount of bound charge at the beginning, $Q_{20}$, have to be specified.
(ii) In order to simplify calculations it has been assumed that the power demand, $\mathrm{P}_{\mathrm{ex}}$ (the power to be delivered), is constant throughout the time series generation.
(iii) Assume the time series algorithm generates a value that represents the joint renewable power, $P_{r a n}$. Compare $P_{r n n}$ with the power demand $P_{c x}$. If ( $P_{r a n}>P_{\mathrm{ex}}$ ) go to step (iv). Charging the battery.
If $\left(P_{\mathrm{ran}}=\mathrm{P}_{\mathrm{z}}\right)$ continue with next time step.
If $\left(P_{r e n}<P_{u}\right)$ go to step (v). Discharging the battery.
(iv) Charging the battery:

First, calculate the maximum (negative) charge current, $\mathrm{I}_{\mathrm{cmax}}$, according to equation (2.99). Second, calculate the actual charge current, $I_{c}$, from

$$
\begin{equation*}
I_{c}=\frac{P_{r e n}-P_{a r}}{V} \tag{4.21}
\end{equation*}
$$

Here, V is the constant voltage with which the battery is charge. Now set $\mathrm{I}_{c}=\mathrm{I}_{\mathrm{cmax}}$ if $\mathrm{I}_{c}<\mathrm{I}_{\mathrm{c} \text { max }}$. In this case a surplus energy of $\Delta \mathrm{P}=\mathrm{P}_{\text {ra }}-\mathrm{P}_{\mathrm{d}}-\mathrm{V}_{\mathrm{c} \text { max }}$ cannot be used to charge the battery and has to be dumped. With the given value of $I_{c}=I$ calculated $Q_{1}$ and $Q_{2}$ with the help of equation (2.97).
(v) Discharging the battery:

First calculate the (positive) maximum discharge current using equation (2.98). The demanded current is

$$
\begin{equation*}
I_{d}=\frac{P_{r e n}-P_{e x}}{V} \tag{4.22}
\end{equation*}
$$

Set $I_{d}=I_{d, \max }$ if $I_{d}>I_{d \max }$. In this case the power delivered by both the renewable energy sources and the battery is not enough to meet the power demand $P_{\text {ex }}$. The power deficit $\Delta P=P_{\text {ren }}-P_{e x}-V_{I_{\text {max }}}$ has to be covered by the diesel engine. As in (iv) calculate $Q_{1}$ and $Q_{2}$ from equation (2.97), the state of charge from equation (2.92) and continue by fetching the next time series value.

Fig. 4.32, Fig. 4.33 and Fig. 4.34 illustrate the course of the state of charge for various scenarios. For all calculations the following values for the battery parameters have been assumed: $\mathrm{k}=0.5 \mathrm{~s}^{-1}, \mathrm{c}=1.0, \mathrm{Q}_{\max }=193.6 \mathrm{Ah}, \mathrm{V}=11.5 \mathrm{~V}$. The rated (maximum) joint renewable power has been assumed to be $P_{\text {ren, max }}=7 \mathrm{~kW}$ (compare discussion in section 3.3. In Fig. 4.32 and Fig. 4.33 the assumed power demand is $P_{e x}=5 \mathrm{~kW}$. Please note that both scenarios, wind speed slump and clearness index slump, correspond to the already examined cases in section 4.1.4 (on distributions) and in section 4.2.2.4 (on joint renewable power time series). The wind speed slump causes the battery to be discharged in order to meet the power demand. With increasing wind speed, however, the battery can be re-charged again after some time. For $\zeta=0$ (wind turbine only) the battery is going to be discharged deeper than for $\zeta>0$ (joint wind turbine and photovoltaic array).

The underlying scenario in Fig. 4.34 is identical to Fig. 4.33 except that the power demand is only $P_{c x}=3.5 \mathrm{~kW}$. Here, the depth of discharge caused by the wind speed slump is only marginal and the battery can be charge after a very short period.


Fig. 4.32 State of Charge: Wind Speed Slump


Fig. 4.33 State of Charge: Clearness Index Slump


Fig. 4.34 State of Charge: Wind Speed Slump

### 4.3 First Passage Time

The first passage time problem was already solved for the wind speed in chapter 2.1.2.2. This was an analytical solution and it was pointed out that the same way is not viable for more difficult stochastic processes. The coverage of probability distributions and time series gives way to two further algorithms which are the focus of this chapter. Their differences and similarities are highlighted in section 4.3.3.

### 4.3.1 Time Series Approach

As mentioned above the first passage time is the expected time $T_{f p}$ that elapses until a stochastic process reaches a passage level for the first time subject to an initial observation. In general, the first passage time is a function of the passage level $x_{p}$, the initial value $x_{0}$ and the underlying conditional distribution function $F\left(x, t \mid x_{0}\right)$. The idea behind a time series approach to the first passage time problem is to follow up a time series and record the time when the passage level is hit for the first time. For the simplicity of the calculations involved it is assumed that the initial value is always less than or equal to the passage level. The algorithm to calculate the first passage time is as follows:
(1) Specify the initial value $X_{0}$, the passage level $X_{p}$ and the time step $\Delta t$ that is inherent in the time series.
(2) Initialize the random number generator with the appropriate probability distribution.
(3) Set $\mathrm{n}=0$ ( n being the counter of time series taken into account)
(4) Set $T=0$ ( $T$ being the sum of first passage times from the individual time series.)
(5) Set $t=0$ ( $t$ being the time scale in one time series) and reset the time series calculator.
(6) Set $\mathrm{j}=0$ ( j being the counter of the number of generated time series values)
(7) Generate next time series value $x$. Set $j=j+1$.
(8) If $\left(x>x_{p}\right)$ go to (12)
(9) The process has not yet passed the specified passage level: Update time $t=t+\Delta t$.
(10) If $(\mathrm{j}>1000$ ) exit the procedure with error message. This is just a safety measure in order to prevent a possible deadlock. The number 1000 is merely a suggestion which seems to be realistic. In the program this limit can be interactively specified by the
user.
(11) Repeat steps from (7).
(12) The process has passed the specified passage level: Add $T=T+t$ and update $n=n$ +1 .
(13) If ( $\mathrm{n}<\mathrm{N}_{\mathrm{T}}$ ) start with new time series from step (5). $\mathrm{N}_{\mathrm{T}}$ is the number of time series taken into account. Obviously, a large $\mathbf{N}_{\mathrm{T}}$ stabilizes the result but causes the calculation time to increase. Numerical results (section 4.3.1.1) suggest that numbers between 10 and 20 already procure reasonably good results.
(14) The first passge time is the average, $T_{\mathrm{fp}}=T / N_{T}$.

This algorithm is illustrated and discussed in several examples in the following sub- sections.

### 4.3.1.1 Time Series Approach: Wind Speed

Applying the algorithm described above the first passage time has been calculated for the same parameter setting as in the time series in Fig. 4.22 and Fig. 4.23. It is displayed for an initial value of $v(0)=8 \mathrm{~m} / \mathrm{s}$ as a function of the wind speed passage level $v_{p}$ in Fig. 4.32. Hence, it shows the expected time it takes to encounter a wind speed $v_{p}$ or greater for the first time subject to an initial observation of $v(0)$. Not surprisingly, the first passage time is shorter if the standard variation is smaller. In Fig. 4.35 the first passage time is plotted as a function of the initial wind speed assuming a passage level $\mathrm{v}_{\mathrm{p}}=\overrightarrow{\mathrm{v}}=16 \mathrm{~m} / \mathrm{s}$. In both diagrams the number of time series taken into account, $\mathrm{N}_{t}$ was set to 20.


Fig. 4.35 Time Series Method - Wind Speed


Fig. 4.36 Time Series Method - Wind Speed

Fig. 4.37 depicts first passage times over the wind speed passage level for different values of $N_{r}$ For $N_{t}=5$ the variations are fairly significant, though even there the trend is distinct. The curves get smoother for greater values of $\mathrm{N}_{\mathrm{t}}$. The improvement stemming from an increase in $\mathrm{N}_{\mathrm{t}}=10$ to 20 , however, seems not to be worth twice the computing time.


Fig. 4.37 Influence of Number of Time Series

### 4.3.1.2 Time Series Approach: Wind Turbine Power

Results for the wind turbine power are illustrated in Fig. 4.38 and Fig. 4.39. They correspond to the time series displayed in Fig. 4.24, Fig. 4.25 and Fig. 4.26. Fig. 4.38 depicts the first passage time as a function of the specified passage level of the normalized wind turbine power, whereas Fig. 4.39 captures the first passage time as a function of the initial wind speed, assuming a constant power passage level $p_{p}=0.8$. Both diagrams clearly demonstrate that the first passage time rises immensly in the event of low mean wind speeds.


Fig. 4.38 Time Series Method - Wind Turbine Power


Fig. 4.39 Time Series Method - Wind Turbine Power

### 4.3.1.3 Time Series Approach: PV Array Power

The first passage time as a function of the passage level of the photovoltaic array power is illustrated in Fig. 4.40 and Fig. 4.41. Here, Fig. 4.40 corresponds to time series diagram Fig. 4.28, while Fig. 4.41 corresponds to Fig. 4.27. Note that the first passage time is the expected average time. It does not give any clue towards the variance. For instance, looking at the time series realizations Fig. 4.27 a large variance of the first passage time is expected which is due to the two peaks in the underlying distribution function. The first passage time algorithm, however, only yields the average time.


Fig. 4.40 Time Series Method - PV Array Power


Fig. 4.41 Time Series Method - PV Array Power

### 4.3.1.4 Time Series Approach: Joint Renewable Power

The first passage time as a function of the passage level of the joint renewable power is depicted in Fig. 4.42 and Fig. 4.43. Fig. 4.42 simulates a slump in the wind speed with an initial wind speed of $v(0)=8 \mathrm{~m} / \mathrm{s}$. This scenario is identical to 4.30 . Greater $\zeta$ - values, signifying a higher proportion of solar energy, reduce the first passage time considerably. For $\zeta=0.75$ the impact of the wind speed slump is almost insignificant. Fig. 4.43 on the other hand simulates a solar energy slump, corresponding to 4.31 . In relation to Fig. 4.42 solar energy and wind energy are just swapped. The qualitative results are the same.


Fig. 4.42 First Passage Time: Wind Speed Slump


Fig. 4.43 First Passage Time - Clearness Index Slump

### 4.3.2 Markov Chain Approach

In this section a technique is presented to work out the expected first passage time of a stochastic process using Markov chains, as mentioned in the first discussion of the first passage time problem in chapter 2.1.2.2. A Markov chain ([20]) is a discrete-value, discretetime Markov process. A Markov process on the other hand is a stochastic process for which the conditional probability density function at any time and for any given number k of previous observations, depends only on the most recent observation:

$$
\begin{equation*}
f_{x}\left(x \mid X\left(t_{1}\right)=x_{1}, X\left(t_{2}\right)=x_{2}, \ldots, X\left(t_{k}\right)=x_{k}\right)=f_{x}\left(x \mid X\left(t_{1}\right)=x_{1}\right), t_{1}>t_{2}>\ldots>t_{k} \tag{4.23}
\end{equation*}
$$

Hence, the evolution of the process can be phrased in terms of the so-called transition probability

$$
\begin{equation*}
g_{n m}(j)=p\left(X_{j}=n: X_{j-1}=m\right) \tag{4.24}
\end{equation*}
$$

This is the probability that the process X changes from value m to n within the time interval $[j-1, j]$. If $p_{j}(k)$ denotes the probability $p\left(X_{j}=n\right)$ all probabilities can be put into a vector

$$
P(j)=\left[\begin{array}{lll}
p_{1}(j) & \ldots & p_{N}(j) \tag{4.25}
\end{array}\right]^{T}
$$

with N components (for N possible values of X ). The progress of the process can then be expressed in matrix representation

$$
\begin{equation*}
P(j)=G(j) P(j-1) \tag{4.26}
\end{equation*}
$$

where $G(j)$ is the transition matrix with elements $g_{\mathrm{m}}(\mathrm{j})$ as defined above. The algorithm whose description follows has been inspired by an algorithm proposed by Paynter ([32]), which has been further developed in the frame of this paper.
The algorithm exploits the same idea that stood behind the analytical approach in 2.1.2.2. Assume the output of the stochastic process to be representable by a whole number in the closed interval $[1, \mathrm{~N}]$. Hence, there are only N different states to observe. Assume further that q is the passage level in question, where q is too a whole number, $\mathrm{q} \in[1, \mathrm{~N}]$. Back in chapter 2.1.2.2 a system was thought of being filled with particles. Particles that reach level
$q$ were taken out of the ensemble. In this context, the same can be achieved by introducing an ( $\mathrm{N}+1 \times \mathrm{N}+1$ ) - matrix G with the elements ( $\mathrm{n}, \mathrm{m} \in[1, \mathrm{~N}+1]$ )

$$
g_{n m}= \begin{cases}0 & \left\{\begin{array}{l}
m>q, n \neq N+1 \\
m \leq q, n=N+1
\end{array}\right.  \tag{4.27}\\
1 & m>q, n=N+1 \\
p_{n m} & \text { otherwise }\end{cases}
$$

where $\mathrm{p}_{\mathrm{nm}}$ is the corresponding transition probability. Hence, the transition matrix looks like

$$
G=\left[\begin{array}{ccccccc}
p_{11} & p_{12} & - & p_{1 q} & 0 & - & 0  \tag{4.28}\\
\vdots & & & \vdots & \vdots & & \vdots \\
p_{N 1} & p_{N 2} & - & p_{N q} & 0 & \cdots & 0 \\
0 & 0 & - & 0 & 1 & - & 1
\end{array}\right]
$$

Below the passage level, G of (4.28) is identical to the transition matrix of the stochastic process in question. Only difference: Once a particle has passed q , the transition probability for returning is zero and it will end up in state ( $\mathrm{N}+1$ ). After applying (4.26) over and over all particles will eventually be in state $(\mathrm{N}+1), \mathrm{P}(\mathrm{N}+1)=1$.
Assume now an initial state $\mathrm{u}, \mathrm{u}<\mathrm{q}$. The initial probability vector $\mathrm{P}(0)$ has therefore the components $\mathrm{p}_{\mathrm{j}}=\delta_{\mathrm{ju}}$, where $\delta$ is the Kronecker symbol,

$$
\delta_{i j}= \begin{cases}0 & i \neq j  \tag{4.29}\\ 1 & i=j\end{cases}
$$

The probability that at time k the system is in one of the states above the passage level is simply

$$
\begin{equation*}
C(k)=\sum_{j=q+1}^{N+1} p_{f}(k) \tag{4.30}
\end{equation*}
$$

$\mathrm{C}(0)$ is zero as it is assumed that $\mathrm{u}<\mathrm{q}$. The next value, $\mathrm{C}(1)$ is the probability that the passage level has been passed after the first time step. As a result, the associated first passage time - after one time step - is $T_{f p}(1)=1 * \Delta t * C(1)$. After the second time step the volume above q will have increased by $\Delta \mathrm{C}=[\mathrm{C}(2)-\mathrm{C}(1)]$, which can be interpreted as the
probability for passing q during the second time step. The resulting passage time is

$$
\begin{equation*}
T_{p p}(2)=\Delta t[2(1-C(1)) \Delta C]+T_{p p}(1) \tag{4.31}
\end{equation*}
$$

The term ( $1-\mathrm{C}(1)$ ) in (4.31) is the probability that the system has not passed q within the first time step. This makes both events ('passing $q$ in time step 1 ' and 'passing $q$ in time step 2) exclusive so that the probabilities can be added up, leading to (4.31). This can be continued until $\mathrm{C}(\mathrm{k})$ is 1 or very close to 1 . This technique can be put into a more general algorithm:
(1) Specify $N$, the number of discrete levels of the underlying stochastic process.
(2) Specify q , the passage level, $\mathrm{q} \in[1, \mathrm{~N}]$. Calculate the transition matrix G of the enlarged system (4.28) given a time step $\Delta t$.
(3) Specify $u$, the initial value, $u<q$.
(4) Specify $\mathrm{N}_{\mathrm{i}}$, the maximum number of iterations permitted and $\delta$, the stop criterion, $\delta$ < 1.0
(5) $\quad$ Set counter $\mathrm{j}=1$
(6) Set initial probability vector $\mathrm{P}(0)$ with components $\mathrm{p}_{\mathrm{j}}=\delta_{\mathrm{ju}}$.
(7) Initialize coefficients $\mathrm{C}(0)=0.0, \mathrm{ET}(0)=0.0, \gamma=1.0$
(8) Matrix multiplication $P(j)=G * P(j-1)$
(9) Calculate $\mathrm{C}(\mathrm{j})$ from (4.30).
(10) Calculate $\Delta C=C(j)-C(j-1)$
(11) Calculate $\operatorname{ET}(\mathrm{j})=\mathrm{j} * \boldsymbol{\gamma} * \Delta \mathrm{C}+\mathrm{ET}(\mathrm{j}-1)$
$E T(j)$ is the normalized first passage time that accumulates the results of the preceding time steps. Multiplied by the time step $\Delta t$ is the real first passage time. It is denoted ET to make clear this is the formula for the expected time T , the first passage time.
(12) Increment $\mathrm{j}=\mathrm{j}+1$
(13) If (1.0-C(j) < $\delta$ ) go to step (16). Otherwise, stop criterion not met. Continue with step (14).
(14) If ( $\mathrm{j}>\mathrm{N}_{\mathrm{i}}$ ) return with an error message. The maximum number of iterations has been reached. This is just to make sure that a deadlock can not occur.
(15) If (j $\leq N_{i}$ ) repeat iteration from step (8).
(15) If ( $\mathrm{j} \leq \mathrm{N}_{\mathrm{i}}$ ) repeat iteration from step (8).
(16) The first passage time $T_{f p}$ is $T_{f \mathrm{f}}=E T(j) * \Delta t$.

This algorithm can be seen as a template for any stochastic process. What is left to specify from case to case is the initial value, the passage level and the underlying distribution. And this is actually the main difficulty associated with this algorithm as it requires to calculate the transition matrix. This is discussed in detail in the following sections on the particular stochastic processes, i.e. wind speed, wind power and solar power.

### 4.3.2.1 Markov Chain Approach: Wind Speed

In order to apply the above algorithm to the wind speed, the wind speed scale has to be discretized. Assume that $M$ classes $C_{i}(i=1 \ldots M)$ along the wind speed axis are defined by the wind speed intervals $C_{i} \in\left[v_{i-1}, v_{i}\right]$. As the normal distribution is used to describe the wind speed fluctuations, the extreme values $v_{0}$ and $v_{M}$ are $\pm \infty$. For the values in between the relationship

$$
\begin{equation*}
V_{n}=\sigma_{v} u\left[2 \frac{n-1}{M-2}-1\right]+\bar{v} \quad, n=1 \ldots M-1 \quad, u=4.753 \tag{4.32}
\end{equation*}
$$

is proposed. Here, $\sigma_{v}$ is the standard deviation and $\bar{v}$ the average wind speed. The factor $u$ $=4.753$ was chosen so that $\Phi\left(v_{1}\right)=10^{-6}$. The choice is however, an arbitrary one. For the reverse direction, calculating a discrete level $n$ from a given speed $v$, the formula

$$
\begin{equation*}
n=\min _{t=1 . \ldots M}\left\{i \mid v_{t} \geq v\right\} \tag{4.33}
\end{equation*}
$$

can be applied. It says that n is the minimum index for which $\mathrm{v}_{\mathrm{i}} \geq \mathrm{v}$. Recalling the wind speed distribution function (4.2) allows to calculate the probability that the wind speed is at time $t$ - within class number i subject to the condition $v(0)=v_{0}$. It is

$$
\begin{equation*}
p_{n}\left(v_{0}\right)=F_{v}\left(v_{n} \mid v_{0}\right)-F_{V}\left(V_{n-1} \mid v_{0}\right) \tag{4.34}
\end{equation*}
$$

class $m$ to class $n$, where both classes are a whole range of wind speeds rather than just one value as the initial value in (4.34). Therefore, $p_{n}\left(v_{0}\right)$ has to be integrated over all $v_{0}$ values in class m and divided by the probability that it is in class m in the first place, that is

$$
\begin{equation*}
g_{n m}=\frac{\int_{v_{m-1}}^{v_{m}} p_{n}\left(V_{0}\right) \mathrm{d} v_{0}}{\Phi\left(\frac{v_{m}-\bar{v}}{\sigma_{v}}\right)-\Phi\left(\frac{v_{m-1}-\bar{v}}{\sigma_{v}}\right)} \tag{4.35}
\end{equation*}
$$

(4.35) can not be analytically integrated, thus requiring a large amount of computing time. Instead, the following transition probability is suggested:

$$
\begin{equation*}
g_{n m}=\beta_{m} \exp \left[-\frac{u^{2}\left(\left(\frac{2(n-1)}{M-1}-1\right)-\left(\frac{2(m-1)}{M-1}-1\right)\right)^{2}}{2\left(1-r^{2}\right)}\right] \tag{4.36}
\end{equation*}
$$

The coefficients $\beta_{\mathrm{m}}$ can be obtained from the normalization condition

$$
\begin{equation*}
\sum_{n} g_{n m}=1 \tag{4.37}
\end{equation*}
$$

The transition probability $\mathrm{g}_{\mathrm{nm}}$ as in (4.36) has the same charactefistic as the probability density function (4.1), namely the $\exp \left(-x^{2}\right)$ functionality. In fact, (4.36) can be obtained from (4.1) by substituting

$$
\begin{equation*}
v=\sigma_{v} u\left(\frac{2(n-1)}{M-1}-1\right)+\bar{v} \tag{4.38}
\end{equation*}
$$

for $v$ and $v_{0}$ and replacing the factor in front of the exp by $\beta_{m}$. The process is stationary when the correlation coefficient is zero and the transition probability simply becomes a probability for class $n$ irrespective of $m$.
Given the transition probability $\mathrm{g}_{\mathrm{am}}(4.36)$ and the conversions from wind speed to discrete numbers and vice versa, (4.32) and (4.33), the first passage time of wind speed fluctuations can be calculated by following the above Markov chain algorithm. Results for a mean wind
can be calculated by following the above Markov chain algorithm. Results for a mean wind speed of $16 \mathrm{~m} / \mathrm{s}$ are shown in Fig. 4.44 and Fig. 4.45 , where $\mathrm{M}=20$ classes were taken into account. In Fig. 4.44, where an initial wind speed of $12 \mathrm{~m} / \mathrm{s}$ was assumed, two curves for different standard variations are drawn as functions of the passage level of the wind speed. Fig. 4.45 depicts the first passage time as a function of the initial wind speed assuming a passage level of $16.0 \mathrm{~m} / \mathrm{s}$.

In Fig. 4.46 the Markov Chain and the Time Series approach are compared by applying them to the same parameter setting. Although the methods are very different the results are not inconsistent.


Fig. 4.44 Markov Chain Method - Wind Speed


Fig. 4.45 Markov Chain Method: Wind Speed


Fig. 4.46 Time Series versus Markov Chain Approach

The discussion of comparison is continued at the end of this chapter. But before that the stochastic processes of the wind power and the solar power are subjected to the Markov Chain approach. Unlike the wind speed these processes have already been discretized in chapter 4.1 , thus making life a lot easier.

### 4.3.2.2 Markov Chain Approach: Wind Turbine Power

The power scale in the conditional distribution of the wind turbine power is already discretized in (4.5). The initial value, $v_{0}$, in (4.6) however is not. In order to use it for the Markov chain algorithm, $\mathrm{v}_{0}$ in (4.6) has to be derived from a given initial power level m . As the power - wind- characteristic (3.1) is not a strictly monotonic function the wind speed can not always be concluded from a power value. If the power is zero valid wind speed values are $v<v_{c i}$ and $v>v_{c o}$; if it is 1 valid wind speed values are between $v_{r}$ and $v_{c 0}$. In order to circumvent this problem the following mapping between wind speed values v and discrete power levels $m$ is assumed:

$$
v(m)= \begin{cases}\min \left\{v_{d i}, \bar{v}\right\} & m=1  \tag{4.39}\\ v_{d t}+\left(v_{r}-v_{c t}\right) \sqrt[3]{\frac{m-1}{M-1}} & m=2 \ldots M-1 \\ \max \left\{v_{r}, \min \left\{v, v_{c o}\right\}\right\} & m=M\end{cases}
$$

That means, if $\mathrm{m}=1$ (power is zero) the wind speed is assumed to be $\mathrm{v}_{\mathrm{ci}}$ unless the mean wind speed $\overline{\mathrm{v}}$ is less. In case of $\mathrm{m}=\mathrm{M}$, which corresponds to maximum power $\mathrm{p}=1$, the formula returns a wind speed equal to the mean wind speed, though not below the rated wind speed $\mathrm{v}_{\mathrm{r}}$ or above cut- out speed $\mathrm{v}_{\mathrm{co}}$. The result can directly be inserted in (4.7), thus leading to the desired transition probability $\mathrm{g}_{\mathrm{nm}}$. Results are illustrated in Fig. 4.47 and Fig. 4.48 for a variety of mean wind speed values. Qualitatively, the results match Fig. 4.38 and Fig. 4.39 where the first passage time is calculated using the time series algorithm.


## Fig. 4.47 Markov Chain Method - Wind Turbine Power



Fig. 4.48 Markov Chain Method - Wind Turbine Power

First passage times calculated via the Markov chain algorithm are, however, significantly
shorter. This is illustrated in a direct comparison in Fig. 4.49. Here, identical initial conditions apply to both curves. Obviously, the transition matrix $G$ allows the process to advance quicker than expected. Why is this discrepency? First, the time series approach tracks the wind speed, not the wind turbine power. As mentioned above, wind speed values can be uniquely translated into power values, but not the other way round. Second, the Markov chain method uses a discrete wind turbine power distribution, whereas the time series approach applies the continuous wind speed distribution - two different distribution types and two different underlying stochastic processes. The comparison of both algorithms is continued in section 4.3.3.


Fig. 4.49 First Passage Time - Wind Turbine Power

### 4.3.2.3 Markov Chain Approach: PV Array Power

The fluctuations of the photovoltaic power is governed by the conditional distribution (4.12), which can be used in the Markov chain algorithm without further alterations as the mapping between the cleamess index k and the normalized power is linear. Fig. 4.50 illustrates a
comparison between time series approach and Markov chain approach by using identical initial conditions. For the distribution of the PV power $M=20$ discretization were taken into account. Fig. 4.50 shows a good agreement between both algorithms. Unlike in the case of the wind power both algorithms do employ the same distribution formula.


Fig. 4.50 Time Series versus Markov Chain Approach

### 4.3.3 Time Series versus Markov Chains - A Comparison

The time series algorithm monitors the meteorological data, wind speed and clearness index, as it goes along and translates them into power values. To use this algorithm these parameters need to be given. The Markov Chain algorithm on the other hand, does not need meteorological data as it is tracking the power. Hence, if wind speed or clearness index are not monitored only the Markov chain algorithm can be used to estimate the first passage time. However, in the case of the wind turbine ambiguities occur as both minimum and maximum power could be caused by a wide range of wind speed values, causing the Markov
chain algorithm to be less accurate than the time series approach. For the stochastic processes 'wind speed' and 'PV array power' both algorithms procure similar results. For the values used in the examples the time series algorithm proved, in general, to be faster than the Markov chain algorithm - with the exception of PV array calculations. The Markov chain algorithm initially calculates the whole transition matrix G. It is not being recalculated throughout the algorithm. Only matrix multiplications on $G$ are carried out once $G$ is established. The time series algorithm has to return to the conditional distribution each time a random number is generated. As a result of this the Markov chain algorithm is advantegous whenever the evaluation of the conditional distribution function is time consuming, as it is in the case of the PV array power.

Finally, both algorithms calculate the first passage time successively by moving along the time axis. In contrast, the analytical method requires the evaluation of an integral or differential equation. It follows from this observation that the time series method is also based on the assumption of a Markov process. Hence, both methods assume the same physical processes. The difference is a mathematical one. Whereas the "Markov chain" method uses theoretical transition probabilities, the time series method uses a random number generator.

## 5. Summary

This paper centers on an autonomous energy supply plant that consists of a wind turbine, a photovoltaic array, a battery unit and a fossil fuel engine. The purpose was to develop and examine statistical models that describe the system and the influence of various parameters, such as the wind speed and the light intensity, on it.
This has been achieved in three steps. First, the energy sources involved have been discussed in chapter 2. It has been shown that the short term wind speed turbulence can be described by the Ornstein- Uhlenbeck process. Likewise, the short term fluctuations of the solar clearness index can be expressed in terms of mathematical functions. The third energy source is the battery unit, which may be charged in the event of a surplus energy or discharged if necessary. Three models for a lead- acid battery have been discussed: Two electric models and one based on the electric charges. For the purpose of this paper the latter one has been selected. Finally, a brief section has been devoted to the fossil fuel engine.

In the second step the power supply by this system has been modelled. For the wind turbine a simple power- wind speed characteristic has been used. As far as the photovoltaic array is concerned it has been shown that it is reasonable to assume a linear relationship between the clearness index and the power supplied by the array.

Eventually, in the third step the results of the first two steps have been used to extract distribution functions which describe the stochastic processes "Wind Turbine Power", "Photovoltaic Array Power", "Combined Renewable Power" and the "State of Charge" of the battery.

The distribution functions have been used to generate synthetic time series and calculate first passage time values. Having written a programme it has been possible to calculate and illustrate the distribution functions, time series and first passage time values for a variety of parameters and scenarios. By this way it has been demonstrated that the usage of both wind turbine and photovoltaic array do stabilize the power supply function if there is either a wind speed slump or a clearness index slump. Moreover, the programme has permitted the comparison of two different algorithms to calculate the first passage time. The graphical presentation of distribution functions, time series and first passage time functions has helped to gain a deeper understanding of the stochastic processes involved in the system. In the

[^10]introduction to the statistical system modelling it has been pointed out that the algorithms developed here can be used to design a controller that operates the system more efficiently. It has been stated that the time series algorithms can be used for both off-line optimization of some of the fixed parameters (such as the ratio between rated wind and photovoltaic array power) and on- line operation.

Finally, it is the author's pleasure to thank Dr. David Infield for many discussions, ideas, references and fruitful suggestions and Jonathan Cauldwell for his support.

## 6. Appendix I: Statistics

This appendix introduces the terminology and outlines some of the statistical methods used in this paper. These are in particular the concepts of the distribution functions and the autocorrelation function of a stochastic process.

### 6.1 Probability Distribution Functions

### 6.1.1 Continuous Distribution

A random variable is a transformation that maps the outcome of a random experiment to a real number. This real number is often referred to as a realization of X . The distribution function $\mathrm{F}(\mathrm{x})$ of a random variable X is the (theoretical) probability that the actual realization of the experiment will be less or equal the value $x$. Hence it can be written as

$$
\begin{equation*}
F(x)=p(X \leq x) \tag{6.1}
\end{equation*}
$$

From (6.1) it can be concluded that $F(x)$ is monotonic and it is $F(-\infty)=0$ and $F(\infty)=1$. Its first derivative,

$$
\begin{equation*}
f(x)=\frac{\partial F(x)}{\partial x} \tag{6.2}
\end{equation*}
$$

is called the probability density function. In case the probability density function is known, the corresponding distribution function can be evaluated via the integral

$$
\begin{equation*}
F(x)=\int_{-\infty}^{x} f(\xi) \mathrm{d} \xi \tag{6.3}
\end{equation*}
$$

The same principles apply to two- dimensional distributions: Two random variables X and Y constitute the joint distribution function

$$
\begin{equation*}
F(x, y)=p(X \leq x, Y \leq y)=\int_{-\infty}^{x} \int_{-\infty}^{y} f(\xi, \eta) \mathrm{d} \eta \mathrm{~d} \xi \tag{6.4}
\end{equation*}
$$

with the joint probability density function $f(x, y)$. In case the two random variables $X$ and $Y$ are statistically independent, the joint distribution function will just be the product of the two one- dimensional distribution functions $F_{X}(x)$ and $F_{Y}(y), F(x, y)=F_{X}(x) F_{Y}(y)$.

### 6.1.2 Discrete Distribution

Often, the number of possible realizations of a random experiment is finite, as for example in the case of a dice. In this case the theoretical probability for one particular realization $\mathrm{x}_{\mathrm{i}}$ with index i will be written as $\mathrm{p}_{\mathrm{i}}$. In this instance the distribution function has the shape of a stair function,

$$
\begin{equation*}
F(x)=\sum_{j=-\infty}^{\infty} p_{t} s\left(x-x_{j}\right) \tag{6.5}
\end{equation*}
$$

where $s\left(x-x_{i}\right)$ stands for the unit step function

$$
s\left(x-x_{0}\right)= \begin{cases}0, & x<x_{0}  \tag{6.6}\\ 1, & x \geq x_{0}\end{cases}
$$

The corresponding probability density function will then be a series of weighted delta functions:

$$
\begin{equation*}
f(x)=\sum_{j=-\infty}^{\infty} p_{f} \delta\left(x-x_{j}\right) \tag{6.7}
\end{equation*}
$$

For both numerical and graphical reasons the occurence of the delta function is often inconvenient. In this paper we have mostly calculated the probabilities $p_{i}$, depicted them in various graphics over the i - axis and called the p ( i ) relationship probability function in contrast to the proper probability density function. From a given distribution function $\mathrm{F}(\mathrm{x})$ the single event probabilities $p_{i}$ can be calculated via the relation $p_{i}=F\left(x_{i}\right)-F\left(x_{i-1}\right)$, which makes it very easy to switch from distribution to probability function and vice versa. As a result the distribution function $\mathrm{F}(\mathrm{x})$ too has only a finite number of values and can therefore be written as

$$
\begin{equation*}
F_{f}=\sum_{j=1}^{1} p_{j}, \sum_{j=1}^{\Lambda} p_{j}=1 \quad, i=1 \ldots \Lambda \tag{6.8}
\end{equation*}
$$

where $\Lambda$ denotes the number of discrete levels.

### 6.2 Functions of Random Variables

Assume a random variable X with distribution function $\mathrm{F}(\mathrm{x})$ and corresponding density function $f(x)$, whose realizations are channelled through a system with an input- output characteristic function $\mathrm{H}(\mathrm{x})$. The output can be described by a random variable Y with distribution function $G(y)$. For the sake of simplicity we will only mention two special cases. First, it is assumed that $\mathrm{H}(\mathrm{x})$ is strictly monotonic in the interval $\mathrm{x} \in[\mathrm{a}, \mathrm{b}) . \mathrm{H}(\mathrm{x})$ is constant in the interval $[b, c]$ and zero below $a$ and above $b$, continuous at both $a$ and $b$. At first glance, these restrictions seem to be purely arbitrary. They reflect, however, exactly the course of the characteristic of the wind turbine (3.1). The distribution function of the output will then be

$$
G(y)= \begin{cases}0 & , y<H(a)  \tag{6.9}\\ F(x(y))+F(c)-F(b) & , H(a) \leq y \leq H(b) \\ 1 & , y>H(b)\end{cases}
$$

where $\mathrm{x}(\mathrm{y})$ denotes the inverse function of $\mathrm{H}(\mathrm{x})$ in the interval $[\mathrm{a}, \mathrm{b})$. In the second special case we assume a linear transform $\mathrm{H}(\mathrm{x})=\alpha \mathrm{x}+\beta$. Here, the distribution function is simply

$$
\begin{equation*}
G(y)=F\left(\frac{y-\beta}{\alpha}\right) \tag{6.10}
\end{equation*}
$$

with the corresponding probability density function

$$
\begin{equation*}
g(y)=\frac{1}{|\alpha|} f\left(\frac{y-\beta}{\alpha}\right) \tag{6.11}
\end{equation*}
$$

Such a linear transform of a random variable is the input- output characteristic of the
photovoltaic array (see chapter 2.2.4).
Now consider a function $Z=g(X, Y)$ of two random variables $X$ and $Y$. The random variables can be described by the joint probability density function $f(x, y)$. Here, we will be noting the density function $\mathrm{f}_{\mathrm{z}}(\mathrm{z})$ of the new random variable Z for three special cases, all of which occur in this paper.

Sum: $\quad Z=X+Y \quad F(z)=\int_{-\infty}^{\infty} f(x, z-x) \mathrm{d} x$
Product: $Z=X Y \quad F(z)=\int_{-\infty}^{\infty} f\left(x, \frac{z}{x}\right) \frac{1}{|x|} \mathrm{d} x$
Quotient: $Z=\frac{X}{Y} \quad F(z)=\int_{-\infty}^{\infty} \boldsymbol{x} f(z x, x) \mathrm{d} x$

The expression for the sum can be considerably simplified if statistical independence of X and Y is presumed. By this way the density function of Z can be concluded without knowledge of the joint probability density, just by evaluating the convolution integral

$$
\begin{equation*}
f_{z}(z)=\int_{-\infty}^{\infty} f_{x}(x) f_{y}(z-x) \mathrm{d} x \tag{6.13}
\end{equation*}
$$

where $f_{x}(x)$ and $f_{y}(y)$ are the density functions corresponding to $X$ and $Y$. With the help of this relationship we were able to formulate a distribution of the sum of both wind and solar power in chapter 4.1.4.

### 6.3 Conditional Distributions

A conditional distribution in the context of this paper is a distribution of a random variable subject to a specific condition. Often this condition is an observation of the underlying stochastic process at another time. A conditional distribution function is written in the form $F(y \mid X=x)$, which signifies the distribution of the random variable $Y$ under the condition that another random variable $X$ maps onto its realization $x$. Given the joint probability
distribution function $f_{x y}(x, y)$ of two random variables $X$ and $Y$ and the probability density function of $Y, f_{y}(y)$ the conditional probability density function $f_{x}(x ; Y=y)$ can be calculated from

$$
\begin{equation*}
f_{x}(x \mid Y=y)=\frac{f_{x y}(x, y)}{f_{y}(y)} \tag{6.14}
\end{equation*}
$$

### 6.4 The Autocorrelation Function

A stochastic process is a time dependant process which can be described by a probability distribution function $F(x)$ and the autocorrelation function $R_{x x}(\tau)$. The latter is a measure for the correlation between the realizations of the random variable at time zero and time $\tau$. An autocorrelation function value of zero signifies that the realization at time $\tau$ is not in any way dependant on the value of the realization at time zero. Assuming the stochastic process to be stationary (the statistical characteristics such as mean value and variance are time independent) and ergodic ${ }^{12}$ the autocorrelation function can be worked out from

$$
\begin{equation*}
R_{x x}(\tau)=\lim _{T \rightarrow \infty} \frac{1}{2 T} \int_{-T}^{T} x(t) x(t+\tau) \mathrm{d} t \tag{6.15}
\end{equation*}
$$

with $x(t)$ being a realization of the process over the time $t$. If $x(t)$ represents an energy variable the autocorrelation function $R_{x x}(0)$ at $\tau=0$ can be interpreted as the average process power. This characteristic brings about the Wiener- Chintchin transform from the autocorrelation function $R_{x x}(\tau)$ to the corresponding power spectrum $S_{x x}(\omega)$, which is formally on a par with the Fourier transform,

[^11]\[

$$
\begin{align*}
& S_{x x}(\omega)=\int_{-\infty}^{\infty} R_{x r}(\tau) \mathrm{e}^{-\mathrm{f} \omega \tau} \mathrm{~d} \tau \\
& R_{y r}(\tau)=\frac{1}{2 \pi} \int_{-\infty}^{\infty} S_{x x}(\omega) \mathrm{e}^{\mathrm{i} \omega \tau} \mathrm{~d} \tau \tag{6.16}
\end{align*}
$$
\]

The double index $x x$ is there to remind one of the random variable $X$ that stands behind the stochastic process.

For the description of time discrete processes the same concepts apply. Only the results have to be adjusted accordingly. Given a series of observations $x_{i}(i \in \mathbb{N})$ taken at in constant time intervals T , the autocorrelation coefficients

$$
\begin{equation*}
R_{j}=\lim _{N \rightarrow \infty} \frac{1}{N} \sum_{i=0}^{N-1} x_{i-j} x_{j} \tag{6.17}
\end{equation*}
$$

converges towards the proper autocorrelation function $R_{x x}(j T)$, presumed stationarity and ergodicity. In full analogy to the Fourier transform (6.16) in the time continuous case, here the discrete Fourier transform will yield the power spectrum:

$$
\begin{align*}
S_{x r}(\omega) & =\sum_{k=-\infty}^{\infty} R_{k} \mathrm{e}^{-i k \omega T} \\
R_{k} & =\frac{T}{2 \pi} \int_{0}^{\frac{2 \pi}{T}} S_{k r}(\omega) \mathrm{e}^{i k \omega T} \mathrm{~d} \omega \tag{6.18}
\end{align*}
$$

The inverse transform, however, is not part of the discrete Fourier transform as the power spectrum has not been discreteized.

### 6.5 Normal Distribution and Normal Process

### 6.5.1 Normal Distribution

The so called standard normal distribution or Gaussian distribution is a distribution defined by the probability density function

$$
\begin{equation*}
f(x)=\frac{1}{\sqrt{2 \pi} \sigma} \exp \left(-\frac{1}{2} \frac{(x-a)^{2}}{\sigma^{2}}\right) \tag{6.19}
\end{equation*}
$$

Its mean value is $a$, its standard variation $\sigma$. For the special case of $a=0, \sigma=1$ the distribution is called standard normal or Gaussian distribution and the corresponding distribution function is defined by ([1], def. 26.2.2)

$$
\begin{equation*}
\Phi(x)=\frac{1}{\sqrt{2 \pi}} \int_{-\infty}^{x} \exp \left(-\frac{1}{2} \xi^{2}\right) d \xi \tag{6.20}
\end{equation*}
$$

The distribution function of a normal distribution is then

$$
\begin{equation*}
F(x)=\Phi\left(\frac{x-a}{\sigma}\right) \tag{6.21}
\end{equation*}
$$

The probability density function of two- dimensional or bivariate normal distribution for two identical distributed random variables X and Y with zero mean, standard variation $\sigma$ and correlation coefficient $r$ is given by

$$
\begin{equation*}
f_{x y}(x, y)=\frac{1}{2 \pi \sigma^{2} \sqrt{1-r^{2}}} \exp \left[-\frac{1}{2\left(1-r^{2}\right)}\left(\frac{x^{2}+y^{2}-2 r x y}{\sigma^{2}}\right)\right] \tag{6.22}
\end{equation*}
$$

where the correlation coefficient is defined via the covariance $v_{x y}, r=v_{x y} / \sigma^{2}$.

### 6.5.2 Normal Process

A stochastic process $X(t)$ is called normal if the random variables $X\left(t_{1}\right), X\left(t_{2}\right)$... belong to a multi- dimensional normal distribution. The probability density of $X(t)$ under the condition of a given observation $x_{0}$ at time $t=0$ can be calculated via (6.14) and (6.22) and it is

$$
\begin{equation*}
f\left(x \mid x_{0}\right)=\frac{1}{\sqrt{2 \pi} \sigma} \exp \left(-\frac{1}{2} \frac{\left(x-x_{0} r\right)^{2}}{1-r^{2}}\right) \tag{6.23}
\end{equation*}
$$

The corresponding distribution function can be expressed in terms of the Gaussian distribution (6.12),

$$
\begin{equation*}
F\left(x \mid x_{0}\right)=\Phi\left(\frac{x-x_{0} r}{\sqrt{1-\sigma^{2}}}\right) \tag{6.24}
\end{equation*}
$$

Hence, its mean value is the product $\mathrm{rx}_{0}$ and time dependant if r is a function of t .

### 6.6 Random Numbers

This section discusses random number generators that are able to retrieve numbers drawn from a given distribution. In fact, they are algorithms that return a number each time they are called upon. As they all have a period after which they will repeat the same sequence of numbers, the numbers are called pseudo random. Thanks to long periods the numbers appear however to be random. The Kolmogorov- Smirnov- test ([33], p.623) may be applied to check whether the empirical distribution of a stochastic process matches a theoretical distribution function. Its measure is the maximum value of the absolute difference between the theoretical distribution function and the empirical distribution function of a given sample of numbers. The Kolmogorov- Smirnov test is, however strictly not applicable to check the performance of a random number generator. The following sections discuss random generators for several distribution functions. For more details on their implementation and typical results of the corresponding Kolmogorov- Smirnov- tests refer to section 7.1.2.2.

### 6.6.1 Uniform Deviates

A uniform deviate is a random number drawn from a uniform distribution. It is assumed to return numbers that are evenly distributed over the open interval $(0,1)$. Throughout this chapter we will dencte a uniform deviate with $\check{\mathrm{u}} \in(0,1)$. In the following chapters it will be discussed how a uniform deviate can be used in order to generate random numbers drawn from a normal distribution (chapter 6.2) or any discrete distribution (chapter 6.6.3). They are necessary to produce synthetic time series of the wind speed and clearness index fluctuations.

### 6.6.2 Transformation Method and Normal Deviates

Assume random numbers are to be generated, drawn from a distribution that can be described by its probability density function $f(x)$ or the corresponding distribution function $F(x)$. Given a uniform deviate $u$ (uniformly distributed in ( 0,1 ) a random number $y$ of some arbitrary distribution $F(x)$ can be generated via the inverse function of $F(x)$,

$$
\begin{equation*}
y(u)=F^{-1}(u) \tag{6.25}
\end{equation*}
$$

This method is, however, not always feasible and depends on whether $\mathrm{F}^{-1}(\mathrm{x})$ can be evaluated or not.

A normal deviate is a random number y , drawn from a normal distribution with mean $\mathrm{x}_{\text {mean }}$ and standard deviation $\sigma^{2}$. If $x_{\text {mean }}=0$ and $\sigma=1$, the numbers may be called standard normal deviates. They will be denoted with $y_{s}$. The corresponding distribution function is the standard normal distribution (defined in equation (6.20). There are many methods to generate standard normal deviates using uniform deviates $u(0<u<1)$, two of which will be discussed briefly. The first method applies (6.25) directly. For the inverse of $F(x)$ an approximation has been used ([1], eq. 26.2.22). Thanks to the symmetry of the normal distribution,

$$
\begin{equation*}
\Phi(x)=1-\Phi(-x) \tag{6.26}
\end{equation*}
$$

the random number $y_{s}$ may be worked out from the relationship

$$
y_{s}=F^{-1}(u) \approx\left\{\begin{array}{cc}
\frac{a_{0}+a_{1} t}{1+b_{1} t+b_{2} t^{2}}-t, t=\sqrt{\ln \left(\frac{1}{u^{2}}\right)} & , 0<u \leq \frac{1}{2}  \tag{6.27}\\
-F^{-1}(1-u) & , \frac{1}{2}<u<1
\end{array}\right.
$$

with the coefficients $\mathrm{a}_{0}=2.30753, \mathrm{a}_{1}=0.27061, \mathrm{~b}_{1}=0.99229$ and $\mathrm{b}_{2}=0.04481$. The second method is the Box-Muller ([33], p.289f) method. Given two uniform deviates $u_{1}, u_{2} \in(0,1)$ and applying the transfer methods for two variables, it can be shown the the two parameters $y_{1}$ and $y_{2}$,

$$
\begin{align*}
& y_{1}=\sqrt{-2 \ln x} \cos \left(2 \pi x_{2}\right) \\
& y_{2}=\sqrt{-2 \ln x} \sin \left(2 \pi x_{2}\right) \tag{6.28}
\end{align*}
$$

are both independently distributed according to the standard normal distribution $\Phi(\mathbf{x})$. Both methods require one uniform deviate for each normal deviate. The Box-Muller method, however, requires less computing time. It was therefore the one that has been implemented in the project. Having determined a standard normal deviate $y_{s}$, it can be easily transferred to a normal deviate $y$ by computing

$$
\begin{equation*}
y=\sigma y_{s}+x_{\text {mean }} \tag{6.29}
\end{equation*}
$$

### 6.6.3 Deviates of Discrete Distributions

As shown above, discrete distributions can be described by the distribution coefficents $F_{i}$ (6.8). Given a uniform deviate $u \in(0,1)$ a random number $y$ of the discrete distribution can be obtained via

$$
\begin{equation*}
y=\left\{i \mid\left(F_{i} \geq u, F_{i+1} \leq u\right)\right\} \tag{6.30}
\end{equation*}
$$

This means that $y$ returns the $i$ for which $F_{i} \geq u$ and $F_{i+1} \leq u$ is. Hence, this is in fact the transformation method for discrete distributions.

## 7. Appendix II: Programme Documentation

### 7.1 Functional Specification

### 7.1.1 Getting Started

A programme has been written that carries out all the calculations described in this paper. It runs on a Windows 3.1 environment. The executable file is called owrenw.exe. In order to run it successfully the dynamically linked library bwcc.dll has to be accessible during runtime. To make sure that Windows is able to find it, it has to be in one of the following directories:

- In the same directory as owrenew.exe,
- In the Windows system directory
- In a directory that is included in the environment variable PATH.

The file owrenew.dlg contains user preferences and chosen parameters of the last session. It should reside in the same directory as owrenew.exe. It is not necessary to run the programme, but will be automatically created upon exiting the programme to Windows. After starting the programme a new window will appear on the screen, which is the main window of the application. Its main features are a menu bar to select further actions and a white board for graphical display. It is best to click with the mouse on the top right hand corner button to maximise the main window. The programme can be exited via Alt-D-X or by double clicking the top left hand corner. The programme has a Windows icon associated with it that can be included by using the Windows Setup utility.

### 7.1.2 Programme Description

In this section all menu options are described along with the dialog windows they will cause to open. There are 5 main items on the menu bar:

- Distributions: For all calculations of probability distribution functions.
- Applications: For random number generators, time series and the first passage time problems.
- Options: Setting up usere preferences and parameters.
- Export: Exporting data to Word Perfect Presentation.
- Help: The on-line help feature is not implemented.


### 7.1.2.1 Distributions

## (i) Wind Speed Distribution

The dialog window "Wind Speed Distribution" prepares for the calculations of the stationary probability density function of short term wind speed fluctuations as described in section 4.1.1. It permits to select either the calculation of the probability density function or the corresponding distribution function. Moreover, it asks for four parameters to be specified:

- $\quad$ Mean wind speed: This is the mean wind speed $\overline{\mathrm{v}}$ (equation 4.1 ) in $\mathrm{m} / \mathrm{s}$.
- Minimum wind speed: This is only for display purposes. The first value to be calculated will be $\mathrm{v}=$ minimum wind speed.
- Maximum wind speed: This is the last value to be calculated.
- Number of evaluations: Number of points to be calculated within the open interval [minimum wind speed, maximum wind speed].

Other parameters such as the wind speed standard deviation should be specified in the Settings dialog window (see below). Once all parameters are set, press the OK button of the "Wind Speed Distribution" window. The dialog window disappears and a new Calculations dialog window appears on the screen. Press OK to start calculations. The progress of the calculations can be monitored by looking at the Calculations window where the elapsed time and some other bits of information are depicted. Press OK (or ENTER) once the calculations are finished in order to continue. The calculated points are now shown in a graph in the main window.

## (ii) Wind Power Distribution

The dialog window "Wind Power Distribution" prepares for the calculation of distribution functions of the wind turbine power (section 4.1.2). It allows to choose between probability density function and distribution function as well as between stationary and conditional distribution. Parameters to be specified prior to continuation are:

- Mean wind speed: Same as in (i)
- Steps on power axis: This is the number of discrete levels along the power scale. See equation (4.5) in section 4.1.2.
- Time tau [s]: The time $\tau$ for which the distribution function is to be calculated. It appears in the autocorrelation coefficient $r_{v}$ in equations (4.1) and (4.2). It is only to be specified if the conditional function is chosen.
- Initial wind speed: The initial wind speed $v_{0}$ in equations (4.3) and (4.4) in the case of a conditional distribution. This field is grey and cannot be selectec if the stationary distribution is selected.

Again, other parameters may be specified in the Settings window. Once having pressed the OK button the procedure is identical to (i).

## (iii) Solar Power Distribution

This is the dialog window for the calculations described in section 4.1.3. Again, it gives the option to choose between probability density function and distribution function. Furthermore, the user has to select one of the following options:

- Analytical Distribution: This denotes the distribution function (4.9) using the Betafunction and not the approximation via Gaussian functions. It is for stationary distributions only.
- Approximation: This is now the distribution function (4.11) employing the approximation, though only for stationar distributions.
- Conditional Distribution: This is the conditional distribution (4.11), (4.12) for which an initial clearness index $k$ has to be specified.
- Quality of Approximation: Having selected this option the difference between the analytical solution and its approximation is calcualted (equation 2.90).
Parameters can be entered too:
- $\quad$ Average hourly clearness index $k$ : See discussion in section 2.2.4.1.
- $\quad$ Standard deviation $\sigma_{k}:$ See discussion in section 2.2.4.1.
- $\quad$ Steps on power axis: See above (ii).
- Time tau [s]: See above (ii).
- Initial clearness index $\mathbf{k}$ : This field can only be entered if the conditional
distribution is to be calculated.
- Number of trial points: This is variable M in equation (2.85), an optimization variable - not necessary if stationary distribution is to be calculated. For reasonable values refer to discussion in section 2.2.4.2.
- Number of coefficients: This is variable $Q$ in equation (2.85) and is not necessary for stationary distributions. Again, for reasonable values refer to section 2.2.4.2.
Furthermore, the user can tick the Bypass option. If a distribution is to be calculated that is based on the approximating formula, various optimisation parameters have to be determined prior to evaluating the distribution formula (2.82). The calculated optimisation parameters are stored in a file <solar.dat>. In case the same input parameters hold true the next time the approximation is used, the optimisation parameters are read from the file rather than repeating the same calculation - though only the Bypass - option is selected. In order to save time make sure the option is always selected. In case the input parameters don not match with the parameters on the file the optimisation calculation will be carried out anyway.


## (iv) Joint Renewable Distribution

Here is the dialog box for the calculation of combined power distributions as outlined in section 4.1.4. The layout of the window is very similar to the other distribution dialog windows giving the user the option to select between the joint density function (stationary) and the joint conditional distribution as defined by equation (4.15). The only additional parameter is the fractional power factor $\zeta$ (equation (3.15)).

### 7.1.2.2 Applications

## (i) Random Numbers

This dialog box and the corresponding calculations have been implemented in order to check the quality of random numbers generating algorithms as discussed in section 6.6. The user can choose one distribution type and enter relevant distribution parameters. Upon pressing the OK button, the programme will generate N (as specified in the input field Number of trials) random numbers and calculate the sample's mean value and variance. Moreover, it
will carry out a Kolmogorov- Smirnov test and print out the test result. The number of classes necessary for the test can be inserted in the input field Number of classes. For more details on the implementation of the Kolmogorov- Smirnov test and the significance of the test result see [33], page 623ff. Tests can be repeated by pressing the Retry button.

- Uniform distribution: In order to generate uniform deviates the random number generator of the C - standard library is used, whose period length is guaranteed to be $2^{32}$ ([5], rand()). The expected theoretical mean value of a distribution which is uniformly distributed in $[0,1]$ is 0.5 , its variance is $1 / 12=0.08333$. A typical result is mean 0.5163 and variance 0.08501 with $N=100$ trials. As mentioned in section 6 the uniform deviates are used to generate other random numbers, such as normal deviates.
- Normal distribution: The generator of random numbers taken from a standard normal distribution with zero mean and variance 1 is implemented using the BoxMuller method (see section 6.6.2). A typical result (for $\mathrm{N}=100$ ) is mean 0.04730 and variance 1.04078 . Normal deviates are used in all time series calculations that include the wind speed distribution.
Beta distribution: This random number generator is implemented by employing the rejection method for continuous distributions (compare [33], p.290). It is, however, never used for time series calculations. It is here more for development purposes and is now obsolete.
- Binomial distribution: Binomial deviates are generated using the rejection method as introduced in section 6.6.3. Although the binomial distribution is not required in the time series calculations of this paper it has been implemented here to confirm the rejection method using a well known discrete distribution. The binomial distribution depends on two parameters, n and p . Here, n is the number of trials and p the probability that an event occurs. The theoretical mean is $n p$, its variance $n p(1-\mathrm{p})$. As the binomial distribution is a discrete distribution, the Komogorov- Smirnov test is not applicable. Though, test results of the mean value and the variance suggest that the implemented method is reliable. It is used for all time series calculations involving discrete distributions.


## (ii) Time Series

The dialog window "Time Series" prepares for the generation of time series as discussed in section 4.2. The window is divided into three parts. First, the user can select one of the following time series:

- Wind Speed: Wind speed time series as outlined in section 4.2.2.1.
- Wind Power: Wind turbine power time series as outlined in section 4.2.2.2.
- $\quad$ Solar Power: Photovoltaic array power time series as outlined in section 4.2.2.3.
- Combined Renewable: Joint renewable power time series as outlined in section 4.2.2.4.
- Battery: State of Charge: State of charge time series as outlined in section 4.2.2.5.
- Power Deficit: Here, the programme generates a time series of the joint renewable power and tracks the state of charge of the battery. It then compares the power supplied by the renewable energies and the battery with the power demand. If the power demand is greater, hence if there is a power deficit it will go into the power deficit time series. If there is no deficit, the time series value will be zero. A power surplus is not recorded.
Second, the user has to enter initial values (dependend on the chosen type of time series):
- Initial wind speed [m/s]: Field only visible if selected time series use the wind.
- Initial clearness index $\mathbf{k}(\mathbf{0})$ : Field only visible for calculations including the PV array.
- Available charge Q10: Field only visible for calculations which need the battery.
- Bound charge Q20: Field only visible for calculations which need the battery.

Third, there are two input fields that are applicable to all time series calculations:

- Time step [s]: This is the implied time interval between two time series values and corresponds to $\Delta t$ in section 4.2.1.
- Number of points: Number of time series values to be generated in one calculation.


## (iii) First Passage Time Problems

The dialog window "First Passage Time Problems" refers to the calculations in section 4.3. First, the user selects the underlying, physical process: Wind speed, wind turbine power, solar power or joint renewable power. Second, he selects the method to be used, which is
either Time Series Approach (see section 4.3.1) or Markov Chain Approach (see section 4.3.2). Third, he can select a calculation technique:

- Calculate one passage time value only: For a given initial value and a chosen passage level the programme computes the first passage time.
- Passage time as function of initial value: For a given, fixed passage level the programme computes a series of first passage times. The first value to be calculated assumes the value entered into one of the initial value fields as initial value. The last value to be calculated assumes the initial value to be identical to the passage level. The total number of values to be calculated is specified in the input field Number of values.
- Passage time as function of passage level: For a given, fixed initial value (or a set of initial values in the case of joint renewable power) the programme computes a series of first passage times. The first value to be calculated assumes the passage level to be identical to the initial value. The last value to be calculated assumes the passage level to be the value entered into one of the passage level input fields. Again, the total number of values to be calculated is specified in the input field Number of values.

Fourth, there are some additional input fields, which may not be visible, depending on the selection of the process, the method and the calculation technique.

- Underlying time step: Only applicable if time series approach is selected. It has the same significance as in the Time series dialog window above.
- Initial wind speed: Initial wind speed in [m/s].
- Initial clearness index: Initial clearness index $\mathrm{k}(0)$.
- Initial power: Initial, normalised power $\in[0,1]$.
- Wind speed level: Passage level for the wind speed in $[\mathrm{m} / \mathrm{s}]$.
- Clearness index level: Passage level for the clearness index $k$.
- Power level: Passage level of the normalised power $\in[0,1]$.


### 7.1.2.3 Options

(i) Settings

In the "Settings" dialog window the user can enter parameters of physical relevance. Values entered here are used by the calculations unless altered in another dialog window. However, if a parameter of the Settings window is altered in another dialog box, it will be updated in the Settins window as well, so that there is never an ambiguity which value might be used in calculations as it is always the value last seen be the user.

- $\quad$ Cut-in wind speed: See section 3.1.
- Cut-out wind speed: See section 3.1.
- $\quad$ Rated wind speed: See section 3.1.
- Mean wind speed: See section 2.1.
- Wind standard deviation: See equation (2.3).
- Auto correlation coefficient $\beta \mathbf{w}$ : Wind speed autocorrelation coefficient $\beta_{\mathrm{v}}$ (see equation (2.9) and discussion below it).
- Max clearness index K 0 : This is parameter $\mathrm{K}_{0}$ in equation (3.14).
- Hourly clearness index k : This is the hourly average clearness index k as introduced in section 2.2.4.1.
- Standard variation $\sigma \mathbf{k}$ : Standard variation of the hourly cleamess index $\mathbf{k}$, as defined in equation (2.65).
- Auto correlation coefficient $\beta \mathrm{s}$ : Autocorrelation coefficient $\beta_{\mathrm{x}}$ of the normalised clearness index x , as defined in equation (2.81).
- Fractional power factor zeta: Definition in equation (3.14).
- Battery: Factor k: All battery parameters refer to the Manwell model in section 2.3.2.3 part (iii).
- Battery: Factor $\mathbf{c}$ : see factor k above.
- Battery: Qmax [Ah]: This is the battery capacity $\mathrm{Q}_{\mathrm{b}}$ as discussed in section 2.3.2.2. Please note that the value to be entered should be in Ampère hours.
- Battery: Voltage [V]: This is the (constant) battery voltage. See discussion of Manwell model in section 2.3.2.3 part (iii).
- Nominal Renewable Power [W]: The combined (non normalised), maximum renewable power in Watt, as defined in equation (3.15). Hence, this is the total installed power. This parameter is only used for state of charge time series.
- Power Demand [W]: This is the power demand $\mathrm{P}_{\mathrm{ex}}$ as in section 4.2.2.5.
(ii) Maths

In the "Maths" dialog box the user can specify some mathematical parameters:

## Solar Power: Approximation of Distribution

- Number of coefficients: See discussion of Solar Power Distribution window.
- Number of trial points: See discussion of Solar Power Distribution window.


## First Passage Time Problem

- Number of time series: Number of time series taken into account while calculating the first passage time using the time series approach. Refer to discussion in section 4.3.1.
- Max number of iterations: (Time series approach) See discussion of time series approach algorithm in section 4.3.1, point (10).
- Max number of iterations: (Markov chain approach) See discussion of Markov chain approach algorithm in section 4.3.2, point (14).
- Stopping criterion: Stopping criterion in Markov chain approach to first passage times. See discussion of algorithm in section 4.3.2, point (13).
- Number of grid points: This parameter is a software development parameter and is now without any significance.


## Process Discretization

- Number of classes: For discrete distributions that are discretised along the power axis. Refer to equations (4.5) or (4.8).
(iii) Directories

In the "Directories" window the user can specify the location of dialog or user files.

- Solar Data: The optimisation parameters for the approximation of the PV array power distribution are stored in the file with the name specified here. Please refer to the discussion on the bypass option in the Solar Power Distribution window.
- Dialog Data: This is a software development field which is now not used at all.
(iv) Display

In the "Display" dialog window the user is given a variety of options for display purposes.

- Auto display of graphics: If this option is ticked, the graph of the last calculation
will be automatically rebuilt after the display of other dialog windows. If the option is switched off, the graph is shown right after the calculation but is not being shown once another dialog box has been opened.
- Accumulate data series: If this option is switched on, up to 4 data series are accumulated and shown in the graph at the same time (in different colours). If the option is switched off only one data series is shown in the graph.
- Ask for legend text: If this option is switched on, the programme asks the user for a legend text to be associated with a curve. The legend text does not appear on the screen. It is, however, exported to Word Perfect Presentation. See discussion on the dialog window Export Data.


## (v) Export Data

The "Export Data" dialog window prepares for the export of the data of the most recently calculated data series to a file. If the option "accumulate data series" is switched on the data of all curves in the latest accumulation are exported. The format of this export file is data compatible with import requirements for Word Perfect Presentation diagrams. Hence, data calculated here can be exported to diagrams in Word Perfect Presentation. All diagrams in this paper have been produced using this technique.

- New file: Save data to a new file. If file already exists, its content will be overwritten.
- Attach data to file: Append data of last curve to the end of the specified file.
- File name: Name of the file the data should be sent to. If no pathname is specified, the current working directory is assumed.


### 7.1.2.4 Help

The on-line help is not implemented.

### 7.1.3 Bugs and Errors

The programme is designed in way so that it is unlikely to crash. Every input field (i.e. fields into which the user can type) are thoroughly checked. Messages do appear if the format is wrong. For instance if the user types a word where a number is expected. Moreover, messages do warn the user if the programme thinks some input parameters are out of range. For instance, if the user enters 1.2 into a normalized parameter field that expects only numbers between 0 and 1 , or if the cut-in wind speed is greater than the cut-out wind speed. In these instances the user can choose to abort the intended action or to ignore it. It is strongly recommended that the user never ignores the warning as this may result in severe errors. Remember that warnings are given for a reason. The option to ignore is implemented for software development purposes only.
Most internal errors should be captured before a crash and an error message is printed out on the screen while the programme is suspended. Although these errors are not damaging, they are not intended to occur. As at print time no situation is known of where such an error occurred.

It may happen that after some time that the headline in the graphs is displayed in a small font rather than a big font. This is due to the limited number of font resources in Windows. The problem has been recognised but not fixed. It has, however, no impact on anything else. If a user cannot live without the big font, he is advised to quit Windows and start Windows again. Other bugs are not known.

### 7.2 Technical Design

In this section the design of the programme is discussed. It is written in $\mathrm{C}++$, using the Borland $\mathrm{C}++3.1$ compiler for Windows. It uses the standard $\mathrm{C} / \mathrm{C}++$ library, Borland Class library and the Object Windows C++ library. Readers who are not familiar with $\mathrm{C}++$, object oriented programming and Object Windows C++ may find this section difficult to understand. Object Windows C++ ([3], [4]) is a class library that is used for all windows in the programme. The next paragraph gives an overview of the files that make up the source code. It is followed by a discussion of the main programme and an outline of the implementation philosophy. Although the number of classes and functions may seem at first
glance hard to swallow, the concept is simple and the structure logical. After the introduction into the programme idea section 7.3 gives a complete class reference, discussing all classes and their public and protected members. Section 7.4 describes all global functions. From there it should be no problem to undeerstand the source code.

### 7.2.1 The File Structure

### 7.2.1.1 Header Files

Header files in C/C++ (extension .h) are there to define classes and constants, declare global functions and data types and define macros. Every class, structure, function or data type is defined in a header file. A listing of all header files is printed in section 7.5 of this paper. The header files can be grouped as follows:

## (i) General Purpose C- Functions

These header files define constants and functions that can be considered as an extension of the standard C- library.
<boolwin.h> Definition of Boolean constants TRUE, FALSE, YES, NO, OK and some mathematical constants.
<cstring.h> Definition of functions on C - strings.
<error.h> Definition of an error handler.

## (ii) Mathematical functions and classes

These header files define mathematical functions and objects. They are not project specific. Among the classes are an implementation of a vector class, matrix class and a class that represents functions of one variable.
<diffcalc.h> Definition of the class obifunc which is the implementation of a function of one variable.
<mathfunc.h> Declaration of mathematical functions.
<vectors.h> Definition of the classes VECTOR and MATRIX.

## (iii) Windows

These header files define all objects that are inherited from Object Windows C++ classes.
Hence, the prefix 'ow'. These objects are usually windows or dialog boxes used in the project.
<owcalc.h> Definition of all window objects on which calculations are carried out.
<owdialg.h> Definition of all dialog windows.
<owlappl.h> Definition of general purpose dialog windows or input fields in dialog boxes.
<owparam.h> Definition of the structure Param. This structure acts as in interface between dialog windows and calculation related classes. Definition of class Graph which acts as an interface between calculations and the graphic window TGraph.
<owplot.h> Definition of graphic related classes.
<owrenew.h> Definition of the graphic window, TRenewPlot, the main window, TMainWindow, and the main application, TRenewApp.
<owres.h> Definition of all constants used for the windows resources.
<owstat.h> Definition of abstract calculation windows classes.

## (iv) Project Objects

These header files define all mathematical objects that are directly project related.
<distrib.h> Definition of classes in the context of distribution functions: E.g. the implementation of a discrete distribution or a continuous distribution.
<joint.h> Definition of the class ProbJointPower, the implementation of the joint renewable power distribution.
<passage.h> Definition of first passage time problem related classes.
<random.h> Definition of random number generator related classes.
<series.h> Definition of time series related classes.
<solar.h> Definition of classes that deal with the photovoltaic array and the distribution of the PV array power.
<wind.h> Definition of wind and wind power related classes.

### 7.2.1.2 Source Files

Source files (extension *.cpp) contain the code for the functions (or class member functions) defined in the header files. There is usually a mapping between header files and source files. E.g. the code for functions defined in wind.h can be found in wind.cpp. There are just two exceptions to this rule. First, there is no source file boolwin.cpp as the header boolwin. $h$ does not define any functions. Second, the functions contained in the source file linalg.cpp are defined in the header file mathfunc.h. A listing of the source file owrenew.cpp is included in section 7.5.2. The listing of other source files is not included in this paper in order to avoid overloading. The complete source code, though, is shipped together with the executable file. Readers interested in the complete source code are referred to the disk.

### 7.2.1.3 Resource File

Another important file is the resource file owres.c which contains data for the layout of the dialog windows, such as coordinates and other attributes. The resource file owres.rc has been created using Borland Resource Workshop ([6]). Some of the resources, such as input fields or dialog windows are given uinque identity numbers. These constants are defined in the header file owres. $h$ which is included by the resource file and other source files.

### 7.2.1.4 Other Files

The file owrenew.def is to be included in the project file. It contains text that serves as information but is otherwise not important. The library file bwcc.lib is included in the project file owrenew.prj as well. This is the library that renders the dialog windows the 'Borland' look rather than the 'Microsoft' look. As mentioned earlier the file bwcc.dll should be accessible at runtime for the same reason. The programme does not work without. Finally, the project file owrenew.prj contains all files to be compiled and linked. It is a software development tool.

### 7.2.2 The Programme Structure

The main routine of the programme is located in owrenew.cpp right at the end (see listing in section 7.5.2). It is a typical Object Windows C++ routine. Readers who are not familiar with Object Windows C++ should first read the programming handbook ([3]).
In the main routine two classes are initialised, param and GraphData. Their significance is mentioned later. Then, an instance of the class TRenewApp is created, which is inherited from the Object Windows C++ class TApplication. The application is run. Upon exit of the application the objects param and GraphData are deleted. Now what exaclty happens in TRenewApp?

Basically, it initialises the main window, class TMainWindow (inherited from Object Windows C++ class TWindow), which is the window that is visible on the screen and contains the menu bar. Now, the programme works in the main window and waits for commands, such as a selection of one of the menus. Generally, every window is actually represented by a class. All events that happen in a window (such as the selection of a menu item or if the user presses a button) are handled in the corresponding class. Hence, actions in the main window are handled in TMainWindow. Have a look at the definition of TMainWindow in the header file owrenew.h. For instance, there is a function CMWindSpeed ()$=\left[C M \_\right.$FIRST +cm WindSpeed $]$. This function is carried out as soon as the event 'cmWindSpeed' occurs. This particular event occurs as soon as the menu item 'Wind Speed Distribution' in 'Distributions' is selected. The function CMWindSpeed (see listing of owrenew.cpp in section 7.5.2) opens the dialog window 'Wind speed dialog', which is represented by the class TSpeedDialog, which is inherited from the Object Windows C++ class TDialog. It is defined in the header file owdialg.h. Now execution is transferred to the instantiation of TSpeedDialog. Here, the user can enter some parameters. If he presses the Cancel button the programme goes back to the main window. Otherwise it transfers execution to the next window, TWindSpeedObject, defined in header file owcalc.h. This is the calculation window. If the user presses the OK button the calculations are carried out by calling the member function workOutValues(). If the user selects OK after the termination of the calculations execution goes back one window to TSpeedDialog and from there to the main window TMainWindow. All the other menu items are handled in a similar way. On top of the main window lays a graphic window, TRenewPlot, which is inherited from TPlot and the Object Windows C++ class TWindow. Every time the execution returns from
the calculation window to the main window, the graphical window checks whether it has to draw a graph. TRenewPlot is defined in owrenew.h as well. It receives the data for the curves (i.e. the data of the last calculations) via the variable GraphData (definition in header owparam.h). The data calculated in TWindSpeedObject for instance are stored in GraphData and can be picked up by the graphic window TRenewPlot when it has to draw itself.
There is another interface variable worth mentioning. It is param, which is of type Param as defined in owparam.h. Every time a dialog window is initiated the default data for its input fields or radio buttons are taken from param. In fact, in the case of the dialog class TSpeedDialog, the appropriate data from param are loaded into an instance of a class TTransSpeedDlg (defined in owdialg.h) via its member function setParameter(). Then data are transferred to the dialog TSpeedDialog and appear on the screen. The user is now given the opportunity to overwrite the parameters in the input fields. If he chooses 'OK' at the end, the buffer TTransSpeedDlg is updated with the new data. So, if he opens the same dialog again, the input fields are now filled with the new data. Otherwise, if he chooses 'Cancel' the buffer is not being updated, which is indeed the functionality of a cancellation. All actions are implemented in a similar way. Look at Fig. 7.1. Every dialog window that appears upon selection of a menu item in the main window is directly inherited from the base class TDialog. E.g. TSettingsDialog is the class corresponding to the settings dialog window. Every dialog class is given a parameter buffer class as described above. E.g. the buffer that corresponds to TSettingsDialog is TTransSettingsDlg. All calculations are carried out on the calculation window which is itself a dialog window. If a calculation is to be carried out that produces only one value, hence a graphical display is not possible, the class to be used is directly inherited from TStatusWindow. E.g. the class TPassageTime, when only one first passage time value at a time is to be calculated. If a whole curve is to be computed, the class to be used is inherited from TMultiValObject. E.g. TWindSpeedObject. In all classes with postfix 'Object' calculations are carried out. That means that their member functions initialise the mathematical objects. There are no mathematics involved in classes with postfixes 'Dialog', Dlg' or 'Window'.

This paragraph was intended to give an overview of the principles of the programme. All classes and their member functions as well as all global functions are listed and discussed in the following sections ordered by header files. Especially the class reference is - together
with the source code - a very thorough documentation of the programme.


Fig. 7.1: Class Structure of Windows Objects

### 7.3 Class Reference

In this section a complete class reference is given. The first part consists of a list of all classes together with a short description and the header file it is defined in. In the second part the classes are discussed in more detail discussing all constructors, protected and public data elements, member functions and operators.

## CLASSES - OVERVIEW

| axis | Implementation of a coordinate axis | wplot.h> |
| :---: | :---: | :---: |
| BetaKgSTest | Kolmogorov- Smirnov test for Betadistribution | <random.h> |
| betaRand | Random number generator for betadistribution | <random.h> |
| ContCondSolApprox | Conditional distribution of the PV array power | <solar.h> |
| ContCondWindPower | Conditional distribution of the wind turbine power | <wind.h> |
| ContinuousDistribution | Continuous distribution | <distrib.h> |
| ContSolAppQual | Quality of approximation | <solar.h> |
| ContSolApprox | Distribution of the PV array power using approximation | <solar.h> |
| ContSolApproxX | Conditional distribution of the normalised clearness index x | <solar.h> |
| ContSolExact | Analytical solution of the PV array power distribution | <solar.h> |
| ContSolExactX | Analytical solution of the distribution of the normalised clearness index $x$. | <solar.h> |
| ContWindPower | Distribution of the wind turbine power | <wind.h> |
| DiscretDistribution | Implementation of a discrete distribution | <distrib.h> |
| discretRand | Generation of random numbers of any discrete distribution | <random.h> |
| DiscretRandomizer | Random number generator for discrete distributions | <distrib.h> |
| DiscretWindSpeed | Discrete distribution of wind speed fluctuations | <wind.h> |
| DiscSolApprox | $P V$ array power as a discrete distribution | <solar.h> |
| DiscretWindPower | Discrete distribution of wind turbine power fluctuations | <wind.h> |


| Graph | Interface between graphic window and calculations | <owparam.h> |
| :---: | :---: | :---: |
| JointPassageTimes | Object function for first passage times of joint renewable power fluctuations | <passage.h> |
| JointPowerTimeSeries | Joint renewable power time series | <series.h> |
| KgSTest | Abstract class of a KolmogorovSmimov test | <random.h> |
| MATRIX | Implementation of a matrix with real elements | <vectors.h> |
| MCPassageTime | First passage time using the Markov chain apporach | <passage.h> |
| MCWindSpeedPassageTime |  |  |
|  | First passage time of wind speed fluctuations using the Markov chain approach | <passage.h> |
| MCWindPowerPassageTime |  |  |
|  | First passage time of wind turbine power fluctuations using the Markov chain approach | <passage.h> |
| MCSolarPowerPassageTime |  |  |
|  | First passage time of PV array power fluctuations using the Markov chain approach | <passage.h> |
| MCJointPowerPassageTime |  |  |
|  | First passage time of joint renewable power fluctuations using the Markov chain approach | <passage.h> |
| MeritSol | Object to optimise the approximation used for the distribution of the PV array power. | <solar.h> |
| msgObjfunc | Function of one variable | <distrib.h> |
| NormKgSTest | Kolmogorov- Smirnov test for normal distribution | <random.h> |
| normRand | Generation of normal deviates | <random.h> |
| objfunc | Function of one variable | <diffcalc.h> |
| owObjfunc | Implementation of a function of one variable | <diffcalc.h> |
| pairvec | Double vector that stores $x$ - and $y$ values | <diffcalc.h> |
| Param | Structure that holds parameters for dialog windows | <owparam.h> |
| PassageTime | First Passage Time Object | <passage.h> |
| PassageTimes | First passage time problems in case more than one value is to be calculated. | <passage.h> |
| PassageTimesObject | Calculation of first passage times | <owcalc.h> |


| PowerDeficitTimeSeries | Time series of the power deficit | <series.h> |
| :---: | :---: | :---: |
| ProbCondSolApprox | Conditional distribution of the PV array power as statfunc object | <solar.h> |
| ProbCondWindPower | Conditional distribution - representing the wind turbine power - as statfunc object | <wind.h> |
| ProbJointPower | Joint renewable power probability function | <joint.h> |
| ProbSolAppQual | Quality of approximation as statfunc object | <solar.h> |
| ProbSolApprox | Solar distribution (using the approximation) as statfunc object | <solar.h> |
| ProbSolExact | Analytical solar distribution as statfunc object | <solar.h> |
| ProbWindPower | Stationary distribution - representing the wind turbine power - as statfunc object | <wind.h> |
| rejectRand | Generation of random numbers of any distribution | <random.h> |
| SolarPowerPassageTimes |  |  |
|  | Object function for first passage times of PV array power fluctuations | <passage.h> |
| SolarPowerTimeSeries | Solar power time series | <series.h> |
| SolarRandomizer | Random number generator for the distribution of the PV array power | <solar.h> |
| SolConstants | Store for clearness index distribution parameters. | <solar.h> |
| Speed | Wind speed fluctuations | <wind.h> |
| SpeedDens | Probability density function of wind speed fluctuations | <wind.h> |
| SpeedDist | Distribution function of wind speed fluctuations | <wind.h> |
| StateOfChargeTimeSeries |  |  |
|  | State of charge time series | <series.h> |
| statfunc | Implementation of a statistical function | <distrib.h> |
| TDirDialog | Dialog window Directories' | <owdialg.h> |
| TDisplayDialog | Dialog window 'Display Options' | <owdialg.h> |
| TDistributionObject | Calculation of wind power and PV array distributions | <owcalc.h> |
| TDoubleInput | Input field for a real number | <owlappl.h> |
| TDoubleInputI | Input field for a real number | <owlappl.h> |
| TExportDialog | Dialog window 'Export' | <owdialg.h> |
| TFpDialog | Dialog window 'First Passage Time Problems' | <owdialg.h> |
| TGraph | General purpose graphic window | <owplot.h> |
| TimeSeries | Time Series | <series.h> |
| TimeSeriesOne | Time series with only one initial value | <series.h> |


| TIntegerInput | Input field for an integer number | <owlappl.h> |
| :---: | :---: | :---: |
| TIntegerInputI | Input field for an integer number | <owlappl.h> |
| TJointDialog | Dialog window 'Joint Renewable |  |
|  | Distribution' | <owdialg.h> |
| TJointDistributionObject | Calculation of the joint renewable power distribution | <owcalc.h> |
| TMainWindow | Implementation of the main window | <owrenew.h> |
| TMathsDialog | Dialog window 'Mathematical Options' | <owdialg.h> |
| TMultiValObject | Calculation window for the computation of more than one value | <owstat.h> |
| TPassageTimeObject | Calculation of first passage time | <owcalc.h> |
| TPlot | Graphical representation of functions | <owplot.h> |
| TRenewApp | Main application | <owrenew.h> |
| TRenewPlot | Graphic window of project | <owrenw.h> |
| TSJointPassageTime | First passage time of joint renewable power fluctuations using the time series approach | <passage.h> |
| TSPassageTime | First passage time by time series approach | <passage.h> |
| TSSolarPowerPassageTim |  |  |
|  | First passage time of PV array power fluctuations using the time series approach | <passage.h> |
| TStatusWindow | Calculation window | <owstat.h> |
| TSWindSpeedPassageTim |  |  |
|  | First passage time for wind speed fluctuations using the time series approach | <passage.h> |
| TSWindPowerPassageTim |  |  |
|  | First passage time of wind turbine power fluctuations using the time series approach | <passage.h> |
| TRandDialog | Dialog window 'Random Numbers' | <owdialg.h> |
| TRandomObject | Random number generator calculations | <owcalc.h> |
| TSettingsDialog | Dialog window 'Settings' | <owdialg.h> |
| TSolarDialog | Dialog window 'Solar Power Distribution' | <owdialg.h> |
| TSpeedDialog | Dialog window 'Wind Speed Distribution' | <owdialg.h> |
| TTimeSeriesObject | Calculation of time series | <owcalc.h> |
| TTransDirDIg | Parameter transfer buffer for TDirDialog | <owdialg.h> |
| TTransDisplayDlg | Parameter transfer buffer for TDisplayDialog | <owdialg.h> |
| TTransExportDlg | Parameter transfer buffer for TExportDialog | <owdialg.h> |


| TTransFpDlg | Parameter transfer buffer for TFpDialog | <owdialg.h> |
| :---: | :---: | :---: |
| TTransJointDlg | Parameter transfer buffer for |  |
|  | TJointDialog | <owdialg.h> |
| TTransMathsDig | Parameter transfer buffer for |  |
|  | TMathsDialog | <owdialg.h> |
| TTransRandDlg | Parameter transfer buffer for |  |
|  | TRandDialog | <owdialg.h> |
| TTransSettingsDlg | Parameter transfer buffer for |  |
|  | TSettingsDialog | <owdialg.h> |
| TTransSolarDlg | Parameter transfer buffer for |  |
|  | TSolarDialog | <owdialg.h> |
| TTransSpeedDlg | Parameter transfer buffer for |  |
|  | TTransSpeedDlg | <owdialg.h> |
| TTransTsDlg | Parameter transfer buffer for |  |
|  | TTsDialog | <owdialg.h> |
| TTransWindDlg | Parameter transfer buffer for |  |
|  | TWindDialog | <owdialg.h> |
| TTsDialog | Dialog window 'Time Series' | <owdialg.h> |
| TYoMessage | Message window | <owlappl.h> |
| TYolnput | Dialog window with one input field | <owlappl.h> |
| TWindDialog | Dialog window 'Wind Power |  |
|  | Distribution' ${ }^{\text {' }}$ | <owdialg.h> |
| TWindSpeedObject | Calculation of the wind speed distribution | <owcalc.h> |
| UniKgSTest | Kolmogorov- Smirnov test for uniform distribution | <tandom.h> |
| uniRand | Generation of uniform deviates | <random.h> |
| uniRejectRand | Random number generator | <random.h> |
| VECTOR_ | Vector with real elements | <vectors.h> |
| WindPowerPassageTime |  |  |
|  | Object function for first passage times of wind turbine power fluctuations | <passage.h> |
| WindSpeedPassageTime |  |  |
|  | Object function for first passage times |  |
|  | of wind speed fluctuations | <passage.h> |
| WindSpeedTimeSeries | Wind speed time series | <series.h> |
| WindPowerTimeSeries | Wind power time series | <series.h> |

## CLASSES - REFERENCE

axis
<owplot.h>

Implementation of a coordinate axis within the diagram in the class TPlot.

## Constructors: <br> axis (HDC aDC, RECT* aCurRect); Initialising with window context aDC (see Object Windows C++ manual) and implied rectangular that represents the diagram.

Data elements: curRect

## Member functions:

setAxis

RECT* curRect; Rectangular that represents the diagram
void setAxis (int dir, int just, int coord, double mini, double maxi, const char* alpha, double ax, int n , int axlog, int axgrid, double dist, int mode);
Determination of the attributes of an axis:
dir Direction: HORIZ_DIR (horizontal), VERT_DIR (vertical)
just Text justification: LEFT_TEXT (left justification), RIGHT_TEXT (right jusstification), BOTTOM_TEXT (text below axis), TOP_TEXT (text above axis).
coord axis coordinate (relative to the rectangular)
mini start value of the axis
$\operatorname{maxi} \quad$ end value
text axis text
axle Distance between to marks (only for linea axis)
num For linear axis: Numbering only every num- th mark. For logarithmic axis: num $=1$ : Numbering of the $10-$ marks. num $=2$ : Numbering at 2 and 10 ; num $=3$ : at $2,5,10$; num $=4$ : at $2,3,5,10$.
axlog LIN (linear), LOG (logarithmic)
axgrid Draw a grid (YES or NO)
grid Grid distance (for linear axis only)
mode Presentation mode for the marks: IN_AXLE (axle points inwards), OUT_AXLE (axle points outwards), CENTER_AXLE (axle sit on the middle of the axis).
drawAxis void drawAxis (); draw axis with specified attributes

BetaKgSTest <random.h>

Kolmogorov- Smirnov test for Beta- distribution, derived from KgSTest.

## Constructors:

BetaKgSTest (int n, int r, double a, double b );
Construct test object for n classes, r trial points and distribution parameters a and b ,

Member functions:
theoretProb
initialize
double theoretProb (double x ); see $\mathrm{KgSTest}:$ :theoretProb.
void intiialize ( );
initialise randomizer with betaRand object.
betaRand <random.h>

Implementation of a random number generator for beta- distributed numbers. It is derived from uniRejectRand.

## Constructors:

betaRand (double alpha, double beta); Constructor with distribution parameters alpha and beta.

ContCondSolApprox
<solar.h>
Conditional distribution of the PV array power, derived from ContSolApprox. Only difference to the base class is setUp, where ContSolApprox::setCorrelation is called automatically.

Constructors:
ContCondSolApprox (); Default constructor
Member functions:
setUp
int setUp (TStatusWindow*, Param*);
see discussion above.

ContCondWindPower
<wind.h>
Conditional distribution of the wind turbine power. This class is derived from ContWindPower. Only difference is that ContWindPower::setCorrelation is called within

ContCondWindPower::setUp so that ContWindPower::F always returns the conditional distribution function if called from ContCondWindPower.

## Constructors:

ContCondWindPower (); call constructor of base class

## Member functions:

setUp int setUp (TStatusWindow*, Param*);
see discussion above.

ContinuousDistribution <distrib.h>

Abstract class that represents a continuous distribution. Again, this is a conditional distribution, subjected to the initial value initVal.

Constructors:
ContinuousDistribution (); Default Constructor

## Data elements:

 initValprotected: double initVal; implied initial value.

Member functions:
setInitVal

F
virtual int setUp (TStatusWindow*, Param*) $=0$;
Parameter setting function. Abstract function that must be overwritten in derived functions.
virtual void setInitVal (double x ); set initial value initVal.
virtual double F (double x ) $=0$;
Probability distribution function $\mathrm{F}(\mathrm{x})$. Abstract function that must be overwritten in derived functions.

## ContSolAppQual

<solar.h>
Quality of approximation, derived from class ContinuousDistribution.
Constructors:
ContSolAppQual (); Default Constructor

## Member functions:

```
F
virtual double F (double x );
Equation (2.90)
setUp
int setUp (TStatusWindow*, Param*);
```

ContSolApprox
<solar.h>

Distribution of the PV array power (using the approximation), derived from class ContinuousDistribution.

## Constructors:

ContSolApprox (); Default constructor

## Data elements:

 protected:| sol | MeritSol* sol; | pointer to the optimisation class |
| :--- | :--- | :--- |
| sc | SolConstants sc; | store of the distribution parameters |

## Member functions:

F
setUp
double F (double p); Equation (4.11), though with normalised p instead of integer n .
int setUp (TStatusWindow*, Param*);
Setting up the parameters. It is here that the optimisation is carried out by searching for the minimum of the merit function provided by sol. A golden search is carried out using objfunc::goldenSection. The calculations are implemented as described in 2.2.4.2
setCorrelation void setCorrelation (double time, double beta);
Unless setCorrelation is called the stationary distribution is being calculated.
setInitVal
void setInitVal (double initK);
Initialising the distribution with an average hourly clearness index $\mathrm{k}(0)$.

ContSolApproxX
<solar.h>
Conditional distribution of the normalised clearness index x , derived from ContSolApprox.

## Constructors:

ContSolApproxX (); Default Constructor
Member functions:
F
double F (double x );
Equation (2.91)

ContSolExact

Analytical solution of the PV array power distribution, derived from class ContinuousDistribution.

## Constructors:

ContSolExact ( ); Default constructor
Data elements:
protected:
solC $\quad$ SolConstants colC; Store of distribution parameters

Member functions:
protected:
Fx
double Fx (double x ); Equation (2.79)
public:
F double F (double p); Equation (4.9)
setUp int setUp (TStatusWindow*, Param*);

ContSolExactX
<solar.h>
Analytical solution of the distribution of the normalised clearness index $\mathbf{x}$, derived from ContSolExact.

Constructors:
ContSolExact ( ); Default Constructor

## Member functions:

F double F (double x); Equation (2.79)

ContWindPower
<wind.h>

Distribution of the wind turbine power. This class is derived from ContinuousDistribution.

## Constructors:

ContWindPower (); Default constructor
Data elements: protected:
r
double $r$;
autocorrelation function $r=\exp (-\beta t)$

## Member functions:

| F | double F (double p); $\quad$ Equation (4.3) |
| :--- | :--- |
| setUp | int setUp (TStatusWindow*, Param*); |

Parameter setting. Return OK if no error occurred.
setCorrelation void setCorrelation (double time, double beta);
Define autocorrelation function $\mathrm{r}=\exp (-$ beta * time)

DiscretDistribution
<distrib.h>
Abstract class of a discrete distribution. It actually is a conditional distribution with initial value (or call it conditional value) m .

Constructors:
DiscretDistribution ( int n ); Initialisation for n classes.

## Member functions:

setUp

$$
\text { virtual int setUp (TStatusWindow*, Param*) }=0 \text {; }
$$

Initialisation with parameters. Abstract function has to be overwritten in derived classes. Returns OK if no error occurred. Otherwise ERROR.

| gnm | virtual double gnm (int $n$, int $m$ ) $=0$; <br> returns the transition probability $\mathrm{g}_{\mathrm{m}}$ (probability for system to change from state $m$ to state $n$ in one step). Abstract class that has to be overwritten in derived classes. |
| :---: | :---: |
| Gn | virtual double Gn (int n ); <br> returns the probability that the system is in a state n or smaller provided the initial value is m . ( m can be set by function setM) I.e. the distribution function. The default return value is 1 . If another value is desired, Gn has to be overwritten. |
| setM | virtual void setM (int m); Set the initial value $m$ |
| getN | virtual void getN (double $p$ ) $=0$; <br> returns the class if the probability distribution value $p$ is given, provided $m$ is the initial value. In a way this is the inverse function to Gn. It is an abstract function and has to be overwritten in derived classes. |
| getClasses | int getClasses (); returns the number of classes |

discretRand
<random.h>
discretRand is immediately derived from uniRand. This class is designed for the case where
the probability distribution is of a discrete type and the probabilities $p_{j}(j=1 \ldots N)$ for the $N$ possible events j are given in a vector px .

## Constructor:

discretRand (VECTOR* x ); Initialization with vector x as described above.

## Member functions:

update
void update (void* xx);
Change distribution parameters (i.e. the probability vector px ) even after initialisation. It is: $\mathrm{px}=\left(\mathrm{VECTOR}{ }^{*}\right) \mathrm{xx}$;

DiscretRandomizer
<distrib.h>

Abstract class of a random number generator for discrete distributions, derived from class uniRand.

## Constructors:

DiscretRandomizer (); Default Constructor

## Data elements:

distribution
protected: DiscretDistribution* distribution;
Derived classes do have to install the desired distribution here. This is the distribution that governs the random number generator.

| Member functions: <br> setUp | virtual int setUp (TStatusWindow*, Param*) $=0 ;$ <br> Setting up parameters. Return OK if ok, otherwise ERROR. |
| :--- | :--- |
| setM | void setM (int m$) ;$ <br> set initial value m in distribution. See class DiscretDistribution. |
| getRandomNumber | double getRandomNumber ( ); <br> generates and returns next random number. |

## DiscretWindSpeed

<wind.h>

Discrete distribution of wind speed fluctuations as used in first passage time problems using the Markov chain approach. The class is derived from DiscretDistribution.

## Constructors:

DiscretWindSpeed (int $n$ ); calls constructor of base class
Member functions: gnm double gnm (int $n$, int m);
transition probability. See DiscretDistribution::gnm

| getN | int getN (double v); see DiscretDistribution::getN |
| :--- | :--- |
| setUp | int setUp (TStatusWindow*, Param*); |
|  | Parameter setting. Return OK if no error occurred. |

DiscSolApprox
<solar.h>

Implementation of adiscrete distribution that represents the PV array power. It is a class derived from DiscretDistribution.

## Constructors:

DiscSolApprox (int n ); Construct the class with n discretisation levels.

## Member functions:

setUp
gnm
Gn
setM
getN
int setUp (TStatusWindow*, Param*);
double gnm (int n , int m ); see DiscretDistribution:gnm
double GN (int n); see DiscretDistribution::Gn
void setM (int m); overwrites DiscretDistribution::setM
int getN (double x); see DiscretDistribution::getN•

DiscretWindPower
<wind.h>

Discrete distribution of wind turbine power fluctuations as used in first passage time problems using the Markov chain approach. The class is derived from DiscretDistribution.

## Constructors:

DiscretWindPower (int n ); calls constructor of base class

| Member functions: |  |
| :--- | :--- |
| gnm | double gnm (int n, int m); |
| Gn | transition probability. See DiscretDistribution::gnm |
| double Gn (int m); see DiscretDistribution::Gn |  |
| getN | int getN (double v); see DiscretDistribution::getN |
| setUp | int setUp (TStatusWindow*, Param*); |
|  | Parameter setting. Return OK if no error occurred. |

Graph
<owparam.h>
Interface between graphic window and calculations. Calculation objects store values here. They can be picked up by the graphic window, which is an instance of class TRenewPlot. It can store the function values of up to four curves.

## Constructors:

Graph ( ); Default constructor for 4 curves

## Data elements:

x
y
legend
scale
curveNo
$\min$
max
headline
subline
axtext

VECTOR x ; VECTOR y[4];
char legend [4][20];
double scale; int curveNo;
double min ;
double max; char headline[40]; char subline[50]; char axtext[40];
$\mathbf{x}$ - values
$y$ - values (up to 4 curves)
Legend text for the export to Word Perfect Presentation
Scaling factor for display purposes.
Number of sets of curve data currently stored. curveNo < 4.
Minimum value on $x$ - axis
Maximum value on x - axis
Headline of graph
Text below headline
Text below x - axis

Member functions:
setHeadline setSubline setAxtext
void setHeadline (char* text); define headline void setSubline (char* text); void setAxtext (char* text);
define line below headline define text belowe x - axis

## JointPassageTimes

<passage.h>
Object function for first passage times of joint renewable power fluctuations, derived from PassageTimes.

## Constructors:

WindSpeedPassageTimes (int select );
Constructor: If select $=0$ the data element passageTime is initialised with an instance of TSJointPowerPassageTime. Otherwise with MCJointPowerPassageTime.

Member functions:
SetUp int SetUp (TStatusWindow*, Param*); individual set-up of initial values and passage levels.

JointPowerTimeSeries
<series.h>
Implementation of joint renewable power time series, derived from TimeSeries.
Constructors:
JointPowerTimeSeries ();
Default constructor. Initialises a SolarPowerTimeSeries and a WindPowerTimeSeries object for the two underlying processes.

## Member functions:

protected:
getRandomNumber
public:
update
getOutput
setUserInit
getInitRandomVal
setUp
eval
double getRandomNumber ();
returns next random number from the implied random number generator.
void update (); see TimeSeries::update
double getOutput (); see TimeSeries::getOutput
void setUserInit (void*);
see TimeSeries::setUserInit
double getInitRandomVal ();
overwrites TimeSeriesOne::getInitRandomVal.
int setUp (TStatusWindow*, Param*);
Parameter setting
double eval (double);
return next time series value. the argument is not used.

KgSTest <random.h>

Abstract class of a Kolmogorov-Smirnov test.

## Constructors:

KgSTest (int n);

## Data elements:

protected:
size
k
mean
var
$\mathrm{x}, \mathrm{y}, \mathrm{r}$
randomizer

Member functions:
protected:
initialize
theoretProb

Construct a test with n trial points.
double size; number of trials. This is of type 'double' for data conversion reasons.
number of classes.
mean value of sample variance ov sample
Vectors holding the results.(r holding the generated numbers. $x$ and $y$ holding the theoretical distribution.) random number generator to be used in the test.
virtual void initialize ();
Per default this function does nothing. In derived classes, however, this is the place to initialise the random number generator randomizer.
virtual double theoretProb (double x ) $=0$;
This function has to be overwritten by derived classes. It has to return the theoretical probability for values smaller than or equals

| maxDistance | x. <br> double maxDistance (); |
| :---: | :---: |
|  | double maxDistance (); <br> This function calculates the maximum distance between |
| doValues | generated point and the theoretical distribution function. void doValues (); |
|  | generate the random numbers and pack them into vector r . |
| calcCumDist | void calcCumDist (); |
|  | internal function for the Kolmogorov-Smirnov test. |
| public: |  |
| doTest | double doTest (); |
|  | Carries out the Kolmogorov- Smirnov test and returns the te result. (See [33]). |
| getMean | double getMean (); Return the mean value of the sample |
| getVar | double getVar (); Return the variance of the sample |

MATRIX
<vectors.h>
typedef MATRIX_<int> typedef MATRIX_<double>

## Constructors:

MATRIX_(int n);
MATRIX_ (MATRIX_A);
MATRIX_ (int $m$, int $n$ );
Data members:

| col | int col; | Number of columns |
| :--- | :--- | :--- |
| row | int row; | Number of rows. |

## Member functions:

| col_to_vec | void col_to_vec (int i, VECTOR_<T>\& v); move values of the $i$-th column to vector $v$. |
| :---: | :---: |
| create | void create (int $m$, int $n$ ); <br> Allocation of memory on the heap for an $\mathrm{m} \times \mathrm{n}$ - matrix. |
| diag_to_vec | void diag_to_vec (VECTOR\& v); move diagonal elements to vector v . |
| maxval | T maxval (int\& i, int \& j ); returns the maximum value of the matrix. Indices see minval(). |
| minval | T minval (int\& i, int\& j); returns the minimum value of the matrix. Its indices are updated and passed by reference. |


| vec_to_col | void vec_to_col (int $\mathrm{i}, \mathrm{VECTOR}<\mathrm{T}>\& \mathrm{v}) ;$ <br> moves i-th column vector to vector v. |
| :--- | :--- |
| print | void print (ostream\& op); <br> Standard output to screen. |
| build | void build (istream\& ip); <br>  <br> Standard input via istream. |

## Operators:

| () | $\begin{aligned} & \mathbf{A ( \text { int } i )} \\ & \mathbf{A}(\text { int } i, \text { int } j \text { ) } \end{aligned}$ | Access to element $\mathrm{A}_{\mathrm{ii}}$ Access to element $\mathrm{A}_{\mathrm{ij}}$. |
| :---: | :---: | :---: |
| +, +=, -, -= | Matrix addition: | $\mathbf{A}+\mathbf{B}, \mathbf{A}-\mathbf{B}$ (A, B Matrices) |
| * | Multiply with number: Matrix multiplication: Multiply by vector: | $\begin{aligned} & \mathbf{B}=\mathbf{A} * \alpha, \mathbf{B}=\alpha * \mathbf{A}, \mathbf{A} *=\alpha \\ & \mathbf{C}=\mathbf{A} * \mathbf{B} \\ & \mathbf{v}=\mathbf{A} * \mathbf{u}, \mathbf{v}=\mathbf{u}^{\mathrm{T}} * \mathbf{A} \end{aligned}$ |
| 1 | Division by number $\alpha$ : | $\mathbf{A}=\mathbf{B} / \alpha ; \mathbf{A} /=\alpha ;$ |
| $=$ | $\mathbf{A}=\mathbf{B} ;$ |  |
| << | operator (ostream\& op, | MATRIX\& A); |
| >> | operator (istream\& ip, | MATRIX\& A); |

## MCPassageTime

Abstract class that calculates the first passage time using the Markov chain approach. It is derived from PassageTime.

Constructors:
MCPassageTime ( ); Default constructor

| Data elements: <br> protected: <br> classes |  |
| :--- | :--- |
|  | int classes; |
| distribution | Number of discretisation levels |
|  | DiscretDistribution* distribution; <br> Underlying discrete distribution that is used int the calculations. |

Member functions: protected:

Number of discretisation levels
DiscretDistribution* distribution;
Underlying discrete distribution that is used int the calculations.

| discretize | int discretize ( double x |
| :---: | :---: |
|  | Given an initial level $x$ (depending on the selection this could be a wind speed, clearness index or normalised power value) this function returns the class number the argument is in. It calls distribution->getN ( $x$ ). |
| public: |  |
| Eval | double Eval (double x); returns the first passage time (with non discretised passage level x ) using the Markov chain approach. |
| SetUp | virtual int SetUp (TStatusWindow*, Param*); |
|  | Parameter setting for Markov chain approach void setInitLevel (void*); |
|  | Assumes the argument to be double* and copies it into PassageTime::initLevel. |

MCWindSpeedPassageTime
<passage.h>
Object that calculates the first passage time of wind speed fluctuations using the Markov chain approach. It is derived from FPPassageTime.

Constructors:
MCWindSpeedPassageTime (); Default constructor
Member functions:
SetUp int SetUp (TStatusWindow*, Param*);
Setting the parameters and initialising distribution with an instance of DiscretWindSpeed.

MCWindPowerPassageTime
<passage.h>
Object that calculates the first passage time of wind turbine pwoer fluctuations using the Markov chain approach. It is derived from FPPassageTime.

Constructors:
MCWindPowerPassageTime (); Default constructor
Member functions:
SetUp
int SetUp (TStatusWindow*, Param*);
Setting the parameters and initialising distribution with an instance of DiscretWindPower.

Object that calculates the first passage time of PV arra power fluctuations using the Markov chain approach. It is derived from FPPassageTime.

## Constructors:

MCSolarPowerPassageTime (); Default constructor

## Member functions:

| SetUp | int SetUp (TStatusWindow*, Param*); |
| :--- | :--- |
| Setting the parameters and initialising distribution with an instance |  |

MCJointPowerPassageTime
<passage.h>
Object that calculates the first passage time of joint renewable pwoer fluctuations using the Markov chain approach. It is derived from FPPassageTime.

## Constructors:

MCJointPowerPassageTime (); Default constructor

## Member functions:

SetUp int SetUp (TStatusWindow*, Param*);
Setting the parameters.

## MeritSol

Object to optimise the approximation used for the distribution of the PV array power. It is derived form msgObjfunc.

Constructors:
MeritSol (SolConstants*, Param*);

## Data elements:

| psc | SolConstants* psc; | pointer to the distribution parameter store |
| :---: | :---: | :---: |
| initialx | double initialx; | initial normalised clearness index $\mathrm{x}_{0}$. |
| u | VECTOR u; | Coefficient vector. See equation (2.82). |
| sigma | VECTOR sigma; | See equation (2.84). |
| lambda | VECTOR lambda; | This is sigma / epsilon (see (2.84)) |
| Fxm | VECTOR Fxm; | Vector with distribution function values. Right hand side of (2.87). |
| QPlusOne | double QPlusOne; | Number of generating functions used +1 (see equation 2.87) |
| MPlusOne | double MPlusOne; | Number of trial points +1 |

## Member functions:

fx
Fx
Fp
FxApprox
FpApprox
setUp
double Eval (double x);
Calculates the merit function, equation (2.85).
double fx (double x); Equation (2.75)
double Fx (double x ); Equation (2.79)
double Fp (double p ); Distribution function in power values p . Compare equation (4.9)
double FxApprox (double $x$ ); Equation (2.82) double FpApprox (double p); as $F$ Approx but with power value p as argument. It is internally converted into a normalised clearness index x before calling FxApprox. int setUp ( ); Parameter initialisation

Operators:
The stream operators are used to save optimisation data to a file and retrieve it next time in order to save computing time.
friend ostream\& operator << (ostream\& outstr, MeritSol* v);
friend istream\& operator >> (istream\& instr, MeritSol* v);
msgObjfunc
<distrib.h>
Abstract class, derived from objfunc. It is an extension in that it can monitor the elapsed calculation time and then present messages.

## Constructors:

msgObjfunc ( );
Default constructor

Member functions:
enableTimeMsg
$\begin{array}{ll}\text { enableValueMsg } & \begin{array}{l}\text { void enableValueMsg (); } \\ \text { permit messages of the value of the calculation sent to the } \\ \text { message queue. }\end{array} \\ \text { setHandle } & \begin{array}{l}\text { void setHandle (); } \\ \text { set Windows handle. I.e. Handle of appropriate dialog window. } \\ \text { eval }\end{array} \\ \text { double eval (double); } \\ \text { Function from base class obifunc, here overwritten. } \\ \text { Eval } & \begin{array}{l}\text { double Eval (double) }=0 ; \\ \\ \text { Evaluation of object function. This abstract function has to be }\end{array}\end{array}$
overwritten in derived classes.
NormKgSTest $\quad$ <random.h>

Kolmogorov- Smirnov test for normal distribution, derived from KgSTest.

## Constructors:

NormKgSTest ( n ); Construct test object for n trial points.

| Member functions: <br> theoretProb <br> initialize | double theoretProb (double x ); <br> void intiialize ( ); <br> initialise randomizer with normRand object. |
| :--- | :--- |

normRand
normRand is derived from uniRand. It implements a random number generator, producing a series of numbers that are normal distributed with mean mean and standard deviation sigma. It implements the Box-Muller method (C.Press: Numerical recipes, 1992, p.289) drawing the uniform deviates from uniRand.

## Constructors:

normRand (); Initialization for standard normal deviates (i.e zero mean and unit standard variation.)
normRand (double mean, double sigma); Initialization with mean and sigma.

## Member functions:

getRandomNumber
update
virtual double getRandomNumber ();
returns the next random number. It overwrites the getRandomNumber function of uniRand.
void update (void* $x$ );
the first double value in x is interpreted as the mean value, the second as the variance. This gives the opportunity to change the parameters even after initialisation.
objfunc
<diffcalc.h>

Abstract class, which provides operations on functions of one variable.
Data members:
$x, y \quad$ VECTOR $x, y ; \quad x$ - and $y$ - values ( $y$ - values are the function values)

Member functions:
eval
bracketRoot

| goldenSection | double goldenSection (double ax, double bx, double cx , double fb , double tol, double\& xmin); <br> For the bracket of the minimum \{ $a x, b x, c x\}$ the function determines the minimum, xmin, and returns the value at xmin. The tolerance is tol. fb is the function value at bx . The algorithm uses the golden section search. |
| :---: | :---: |
| compEquiVal | void compEquiVal (double xmin, double xmax, int n); Function computes $n$ equidistant function values in the open interval [xmin, xmax]. The results are stored in $x$ and respectively. |

This class is derived from objfunc and extended by an info facility. This is useful if the underlying object function is evaluated N times and N is known before.

## Member functions:

| getPercentage | double getPercentage ( ); <br> returns the percentage of the number of evaluations carried out in <br> relation to the total number $N$ |
| :--- | :--- |
| prepForEquiVal | void prepForEquiVal (double xmin, double xmax, int $N$ ); <br> Preparation of the series of $N$ evaluations on the interval [xmin, <br> xmax]. |
| compEquiVal | void compEquiVal ( ); <br> Evaluation of the object function. Subsequent calls cause the <br> function to be evaluated at different $x$ - values - as stated in <br> prepForEquiVal ( ). The y - values are stored in vector $y$ in <br> objfunc. |

pairvec
<diffcalc.h>

## Constructors:

pairvec (int n ); $\quad$ initialises the class with $\mathrm{n}(\mathrm{x}, \mathrm{y})$ - pairs
pairvec ( );
initialises the class with size $=0$.

## Data members:

size
$\mathrm{x}, \mathrm{y}$

## Member functions:

```
create
move
move_down
swap
```


## Operators:

operator << (ostream\& op, pairvec\& v); $\gg \quad$ operator $\gg$ (istream\& ip, parivec\& v);

```
```

<<

```
<<
>>
>>
void create (int n );
Allocation of memory on the heap
void move (int \(\mathbf{i}\), int \(\mathbf{j}\) ); moves i -th element to j -th place void move_down (); moves all components one place down void swap (int \(i\), int j); Swap \(i\)-th and \(j\)-th elements.
```

Param

Structure that holds parameters for all dialog windows. It serves as an interface between dialog windows and calculation objects as both access it.
struct Param $\{$
double tau;
int eval;
int type;
int distSelect;

int filter;
int classes;

## // time

// number of function evaluations
int type;
int distSelect
$/ /=0$ (distribution) $=1$ (density)
// chosen distribution selection:
$/ /=0$ : Wind turbine power
// 1 : Conditional wind turbine power
// 2 : Exact Solar
// 3 : Approximated solar
// 4 : Approximated solar, conditional
// 5 : Quality of approximation

| int filter; | // filter of inspection windows |
| :---: | :--- |
| int classes; | // numer of discretisation levels in a discrete |

// Wind parameters:
double wivci;
double wivco;
double wiVr;
double wiVmean;
double wiVmin;
double wiVmax;
double wiSigma;
double wiBeta;
double wiInitV;
// cut- in speed
// cout- out speed
// rated wind speed
// mean wind speed
// minimum wind speed for wind speed distribution
// maximum wind speed for wind speed distribution
// variance of wind speed fluctuations
// wind autocorrelation coefficient
// initial wind speed
// Solar parameters: double solk; double solsigmak; double solk0; double solinitK; double solBeta; int soltrial; int solCoeff; int solBypass;
// average hourly clearness index $k$
// standard deviation of solar irradiation
// absolute maximum possible clearness index
// initial average hourly clearness index
// solar autocorrelation coefficient bsol
// number of trial points in normal approximation
// number of coefficients in normal approximation
// bypass of major calculations by retrieving
// old data
// Combined renewables parameters:

| double comZeta; | // fractional power factor zeta |
| :--- | :--- |
| double comInitP; | $/ /$ Initial p value (normalised power) |

// Random numbers dialog:

| double ranA; | // Parameter alpha for beta- distribution |
| :---: | :---: |
| double ranB; | // Parameter beta for beta- distribution |
| double ranp; | // parameter p for binomial distribution |
| double ranu; | // Parameter u for normal distribution (not used!l) |
| int ranclass; | // Number of classes for Kolmogorov- Smirnov test |
| int rantrial; | // Number of trials in Kolmogorov- Smirnoc test |
| int ranSelect; | // Last selection (i.e. distribution type) |

// Time series parameters:
double tsTimeStep; // Duration of a single time step
int tsPoints; // Length of a time series
int tsSelect; // Last selection (type of time series)
// First passage time parameters:
int fpTsTrial; // Number of time series taken into account
int fpTsMaxIt; // Max iterations in Time series mode
double fpMcStopCrit;// Stopping criterion in Markov chain mode
int fpMcMaxIt; // Max iterations in Markov chain mode
int fpMcGrid; // Markov chain mode: Grid Number $Q$
double fpPassV;
double fppassK;
double fppassp;
int fpNoVal;
// Passage level: Wind speed v
// Clearness index k
// Power level p

```
                                    // function-as-mode
    int fpSelectProcess; // Flags.
    int fpSelectMethod; // Markov chain - or time series approach
    int fpSelectCalc; // Calculation technique selected.
    // Battery parameters
    double batk; // Battery parameter k
    double batc; // Battery parameter c
    double batQMax; // Battery capacity
    double batv; // voltage
    double batQ10; // Initial available charge Q10
    double batQ20; // Initial bound charge, Q10 + Q20 <= 1.0
    // Denormalized system
    double sysPDemand; // Power demand
    double sysPRen; // Installed maximum renewable power
    // Display options
    int disAuto; // automatic re-drawing of graphics
    int disAccu; // accumulate data series when possible
    int disOldEval; // last eval
    int disOldType; // last window type
    double disOldVmin; // last minimum speed
    double disOldVmax; // last maximum speed
    int disFirstCurve; // = I if first curve, otherwise 0
    int disLegend; // =1 if legend desired, otherwise 0
};
```

PassageTime
<passage.h>
This is an abstract class that represents a first passage time calculator. It is derived from msgObjfunc. For a given passage level and initial value the first passage time is calculated in the function Eval, which has to be provided in derived classes.

## Constructors:

PassageTime ( ); Default Constructor
Data elements:
protected:
passLevel
initLeve
timeStep
Member functions:
protected:
SetUp
public:
setUp int setUp (TStatusWindow*, Param*);
Setup function that calls SetUp.
void setPassLevel (double newLevel); Sets the passage level to newLevel.
setInitLevel
double passLevel;
double initLevel;
double timeStep;
setPassLevel virtual void setInitLevel (void* initSet) $=0$;
passage level (speed, clearness index or power)
initial value (speed, clearness index or power, depending on selection)
time step (for time series approach only)

Sets initial level. As there could be not only one but two values that define the initial state (wind speed and clearness index in the case of joint renewable power) the new initial state, initSet is a void*. It has to be defined in derived classes.

PassageTimes
<passage.h>
Abstract class that is able to calculate more than one first passage time value in one set. Hence, it is derived from owObjfunc and has a PassageTime* object as data element.

## Constructors:

PassageTimes (); Default constructor

| Data elements: <br> protected: <br> selectCalc | int selectCalc; <br> noVal |
| :--- | :--- |
| int noVal;  <br> passageTime PassageTime* passageTime$\quad$see setUp. <br> see setUp. <br> Implied passage time <br> object |  |
| public: <br> minVal | double minVal; | | minimum value / start value (either |
| :--- |
| initial value or passage level depending |

## Member functions: protected:

SetUp
public:
setUp
eval
virtual int SetUp (TStatusWindow*, Param*) $=0$;
has to be overwritten by derived classes
int setUp (TStatusWindow*, Param* param); Parameter setup. selectCalc is initialised with param->fpSelectCalc (see Param::fpSelectCalc) and noVal with param->fpNoVal. double eval (double);
returns the first passage time as a function of either the initial value or the passage level depending on the selection, selectCalc.

Calculation window on which calculations of first passage times are carried out, derived from TMultiValObject. This class is to be used if the first passage time is to be calculated as a function of the initial value or the passage level and more than one value has to be
determined. All necessary functions are privately overwritten. See TMultiValObject.

## Constructors:

PassageTimesObject (PTWindowsObject AParent, LPSTR ATitle);

PowerDeficitTimeSeries <series.h>

Implementation of time series of the power deficit that may occur if the joint renewable power and the power delivered by the battery is not sufficient to meet the power demand. The class is immediately derived from StateOfChargeTimeSeries. The power difference can be picked up in the field StateOfChargeTimeSeries::deltaP.

## Constructors:

PowerDeficitTimeSeries (); Default constructor calls base class constructor

## Member functions:

eval
double eval (double); retums next time series value. Argument is not used.

Conditional distribution of the PV array power (using the approximation) embedded in a statfunc object. This is necessary to ensure that it can be easily used by dialog window classes. Moreover, the function statuinc::eval can calculate both the distribution function and the probability function.

## Constructors:

ProbCondSolApprox (); Constructor initialises statfunc::distribution with a ContCondSolApprox object.

ProbCondWindPower
<wind.h>
Conditional distribution - representing the wind turbine power - embedded in a statfunc object. This is necessary to ensure that it can be easily used by dialog window classes. Moreover, the function statfunc::eval can calculate both the distribution function and the probability function.

Constructors:
ProbCondWindPower (); Constructor initialises statuunc::distribution with a ContCondWindPower object.

Implementation of the probability function of the joint renewable power, derived from owObifunc.

## Constructors:

ProbJointPower (int n ); Construction for n different power levels.

| Member functions: <br> eval | double eval (double p ); <br> return probability for normalised power level p |
| :--- | :--- |
| setUp | int setUp (TStatusWindow*, Param*); |
|  | Setting up the parameters. |

## ProbSolAppQual

Quality of approximation embedded in a statfunc object. This is necessary to ensure that it can be easily used by dialog window classes. Moreover, the function statfunc::eval can calculate both the distribution function and the probability function.

Constructors:
ProbSolAppQual (); Constructor initialises statfunc::distribution with both a ContSolApprox and a ContSolExact object.

ProbSolApprox
<solar.h>

Distribution of the PV array power (using the approximation) embedded in a statfunc object. This is necessary to ensure that it can be easily used by dialog window classes. Moreover, the function statfunc::eval can calculate both the distribution function and the probability function.

Constructors:
ProbSolApprox (); Constructor initialises statfunc::distribution with a ContSolApprox object.

ProbSolExact
<solar.h>

Analytical solution of the distribution of the PV array power embedded in a statfunc object. This is necessary to ensure that it can be easily used by dialog window classes. Moreover, the function statfunc::eval can calculate both the distribution function and the probability function.

## Constructors:

ProbSolExact (); Constructor initialises statfunc::distribution with a ContSolExact object.

## ProbWindPower

Stationary distribution - representing the wind turbine power - embedded in a statfunc object. This is necessary to ensure that it can be easily used by dialog window classes. Moreover, the function statfunc::eval can calculate both the distribution function and the probability function.

Constructors:
ProbWindPower ( ); Constructor initialises statfunc::distribution with a ContWindPower object.
rejectRand
rejectRand is immediately derived from uniRand. It is a virtual base class for a random number generator applying the 'rejection method' (W. Press: Numerical recipes, 1992, p.290). Derived classes have to specify the comparison function, the original density function and the inverse distribution function.

Constructor:
rejectRand (); Default constructor

Member functions:
compFunc
origFunc $\quad$ virtual double origFunc (double) $=0$;
Original underlying probability density function. Has to be defined in derived classes. It is assumed that it takes only arguments in the interval [0,1].
invInteg $\quad$ virtual double invInteg (double) $=0$;
Inverse function of the normalized integral of the comparison function, returning only numbers in the interval [ 0,1$]$. Has to be defined in derived classes.
getRandomNumber virtual double getRandomNumber (); returns the next random number.

Object function for first passage times of PV array power fluctuations, derived from PassageTimes.

| Constructors: |  |
| :--- | :--- |
| WindSpeedPassageTimes (int select ); |  |
|  | Constructor: If select $=0$ the data element passa <br> initialised with an instance of TSSolarPowerPas <br> Otherwise with MCSolarPowerPassageTime. |
| Member functions: | int SetUp (TStatusWindow*, Param*); <br> SetUp |

SolarPower'TimeSeries
<series.h>

Implementation of PV array power time series, derived from TimeSeriesOne.
Constructors:
$\begin{array}{ll}\text { SolarPowerTimeSeries (); } & \begin{array}{l}\text { Default constructor. Initialises a SolarRandomizer } \\ \text { object as internal random number generator. }\end{array}\end{array}$
Member functions:
protected:
getRandomNumber double getRandomNumber ();
returns next random number from the implied random number generator.
public:
getOutput double getOutput ( ); see TimeSeries::getOutput
update
getInitRandomVal
setUp
void update ();
see
TimeSeries::update
double getInitRandomVal (); overwrites TimeSeriesOne::getInitRandomVal.
int setUp (TStatusWindow*, Param*);
Parameter setting

SolarRandomizer
<solar.h>

Random number generator for the distribution of the PV array power, derived from DiscretRandomizer.

Constructors:
SolarRandomizer ( ); Default Constructor

Member functions:
setUp

> int setUp (TStatusWindow*, Param*);

SolConstants
<solar.h>

Store for clearness index distribution parameters. Compare section 2.2.4.1
Constructors:
SolConstants (); Default constructor
Data elements:

|  | double w; | equation (2.77) |
| :---: | :---: | :---: |
| deltaKK0 | double deltaKK0; | ( $\mathrm{m}_{\max }-\mathrm{k}_{\min }$ )/ $\mathrm{K}_{0}$ (see section 2.2.4.1) |
| kminK0 | double kminK0; | $\mathrm{k}_{\text {min }} / \mathrm{K}_{0}$ (see section 2.2.4.1) |
| deltaK | double deltaK; | $\left(k_{\max }-\mathrm{k}_{\text {min }}\right)$ |
| kmin | double kmin; | $\mathrm{k}_{\text {min }}$ |
| correl | double correl; | correlation coefficient $\beta^{\text {x }}$. |
| a,b | VECTOR a,b; | equation (2.76) |
| Member functions: setUp | int setUp (Param*) |  |
|  | The function takes and calculates the | levant parameters off the Param structure of the data elements above. |
| xTok | void xTok (double | uble* k ); |
|  | Inverse functionalit | equation (2.70). |
| kTox | void kTox (double | uble* x ); |
|  | See equation (2.70) |  |

Speed <wind.h>

Abstract class that represents the distribution of wind speed fluctuations. The class is derived from owObjfunc.

Constructors:
Speed ();
Default constructor

## Data elements:

protected:

| vmean <br> vsigma | double vmean; <br> double vsigma; | mean wind speed <br> wind speed standard variation |
| :--- | :--- | :--- |
| Member functions:  <br> eval  <br> double eval (double v) $=0 ;$ see objfunc::eval |  |  |
| setUp | int setUp (Param*); | Parameter setting |

Probability density function of wind speed fluctuations. It is derived from Speed.
Constructors:
SpeedDens ( ); Default constructor

## Member functions: <br> eval

double eval (double v); Equation (4.2), but stationary only

SpeedDist
<wind.h>

Distribution function of wind speed fluctuations. It is derived from Speed.
Constructors:
SpeedDist (); Default constructor
Member functions:
eval double eval (double v); Equation (4.1), but stationary only

StateOfCharge'TimeSeries <series.h>
Implementation of time series of the state of charge of the battery, derived from TimeSeries.
Constructors:
StateOfChargeTimeSeries (); Default constructor. Initialises a JointPowerTimeSeries object for the underlying process.

## Data elements:

protected:
deltaP double deltaP;
difference between delivered and demanded power.

## Member functions:

protected:

| update | void update (); | see TimeSeries::update |
| :---: | :---: | :---: |
| getOutput | double getOutput ( ); | see TimeSeries::getOutput |
| public: |  |  |
| setUserInit | void setUserInit (void*); | see TimeSeries::setUserInit |
| setUp | int setUp (TStatusWindow*, Param*) |  |
|  | Parameter setting |  |
| eval | double eval (double); |  |
|  | return next time series value. the argu | ment is not used. |

Abstract class of a statistical function, derived from owObjfunc. It can be either a distribution or a probability density function.

Constructors:
statfunc ();
Data elements:
type protected: int type;
type is either 1 (distribution function) or 0 (probability density function).
protected: ContinuousDistribution* distribution;
Pointer to the implied distribution. Has to be set up in derived classes.

## Member functions:

eval
setUp
setType void setType (int aType);
specify function type. See data elemetn type for more details.
TDirDialog
double eval (double);
returns either the distribution or the probability density.
virtual int setUp (TStatusWindow*, Param*);
Parameter setting
<owdialg.h>

Implementation of the Directories' dialog window, derived from TDialog of the Object Windows $\mathrm{C}++$ library.

## Constructors:

TDirDialog (PTWindowsObject AParent, LPSTR ATitle);

TDisplayDialog
<owdialg.h>
Implementation of the 'Display Options' dialog window, derived from TDialog of the Object Windows C++ library.

## Constructors:

TDisplayDialog (PTWindowsObject AParent, LPSTR ATitle);

Calculation window on which calculations of both wind power and PV array power distributions are carried out, derived from TMultiValObject. All necessary functions are privately overwritten. See TMultiValObject.

## Constructors:

TDistributionObject (PTWindowsObject AParent, LPSTR ATitle);

## TDoubleInput

 <owlappl.h>Implementation of an input field in a dialog window that expects a real number. If the input is not valid a message window pops up and the dialog window cannot be closed. TDoubleInput is derived from the Object Windows C++ class TEdit.

## Constructors:

TDoubleInput (PTWindowsObject AParent, int ResourceId);

## Data elements:

x

## Member functions:

Transfer

CanClose
double $x$; Input value as a number and not text.
virtual WORD Transfer (void* DataPtr, WORD TransferFlag); Transfer and conversion from data element $x$ to the string in the input field. virtual BOOL CanClose ();
tries to convert string from input field to a double. If successful it returns OK. Otherwise ERROR.

TDoubleInputI

This class is derived from TDoubleInput. In addition it checks whether the value x lies in an interval [minVal, maxVal]. If not a message aMessage pops up.

Constructors:
TDoubleInputI (PTWindowsObject AParent, int ResourceId, const double aMinVal, const double aMaxVal, const char* aMessage);

Member functions:
CanClose virtual BOOL CanClose ( ); see TDoubleInput

Implementation of the 'Export' dialog window, derived from TDialog of the Object Windows C++ library.

Constructors:
TExportDialog (PTWindowsObject AParent, LPSTR ATitle);

TFpDialog
<owdialg.h>

Implementation of the 'First Passage Time Problems' dialog window, derived from TDialog of the Object Windows C++ library.

Constructors:
TFpDialog (PTWindowsObject AParent, LPSTR ATitle);

## Member functions:

virtual void WMInitDialog (RTMessage) = [WM_FIRST+WM_INITDIALOG];
Function is carried out upon initialisation of the window.
virtual void HandleOp0Msg (RTMessage) $=$ [WM_FIRST + idFpOp0];
Fanction is called upon selection of 'Wind Speed' option in the dialog window. If this option is selected input fields are made visible or invisible as appropriate. The id- constant is defined in owres. $h$.
virtual void HandleOplMsg (RTMessage) = [WM_FIRST + idFpOp1];
Function is called upon selection of 'Wind Power' option in the dialog window. See HandleOp0Msg above.
virtual void HandleOp2Msg (RTMessage) $=$ [WM_FIRST + idFpOp2];
Function is called upon selection of 'Solar Power' option in the dialog window. See HandleOp0Msg above.
virtual void HandleOp3Msg (RTMessage) $=$ [WM_FIRST + idFpOp3];
Function is called upon selection of 'Combined Renewable' option in the dialog window. See HandleOp0Msg above.
virtual void HandleOp4Msg (RTMessage) = [WM_FIRST + idFpOp4];
Function is called upon selection of Time Series Approach' option in the dialog window. See HandleOp0Msg above.
virtual void HandleOp5Msg (RTMessage) $=$ [WM_FIRST + idFpOp5];
Function is called upon selection of 'Markov Chain Approach' option in the dialog window. See HandleOp0Msg above.
virtual void HandleOp6Msg (RTMessage) $=[$ WM_FIRST + idFpOp6];
Function is called upon selection of 'Calculate one value only' option in the dialog window. See HandleOpOMsg above.
virtual void HandleOp7Msg (RTMessage) $=$ [WM_FIRST + idFpOp7];
Function is called upon selection of 'as function of initial value' option in the dialog window. See HandleOpOMsg above.
virtual void HandleOp8Msg (RTMessage) = [WM_FIRST + idFpOp8];
Function is called upon selection of 'as function of passage level' option in the dialog window. See HandleOpOMsg above.

TGraph
<owplot.h>
General purpose graphic window, derived from the Object Windows C++ class TWindow. It provides graphic resources such as a font, a pen and a brush. It offers functions to draw lines, write text or numbers.

Constructors:
TGraph (PWindowsObject AParent, LPSTR ATitle, PTModule AModule = NULL);
Data elements: (protected)

| logFont | LOGFONT logFont; | Font: Attributes |
| :---: | :---: | :---: |
| TheFont | HFONT TheFont; | Font: Resource (handle) |
| oldFont | HFONT oldFont; | Font: old resource (in order to go back to old font) |
| logPen | LOGPEN logPen; | Pen: Atrributes |
| ThePen | HPEN ThePen; | Pen: Resource handle |
| oldPen | HPEN oldPen; | Pen: old resource handle |
| logBrush | LOGBRUSH logBrush; | Brush: Attributes |
| TheBrush | HBRUSH TheBrush; | Brush: Resource handle |
| oldBrush | HBRUSH oldBrush; | Brush: old resource handle |
| backGround | COLORREF backGroun | d; Background color |
| DC | HDC DC; | Screen context. See [3] and [4] for |

## Member functions:

clearScreen
setTextHeight
setPenSize
setPenStyle
setPenColor
setBrushStyle
setBrushColor
setBrushHatch
setColor
open
void clearScreen (); clear the screen void setTextHeight (int n ); set text height void setPenSize (int n); void setPenStyle (int n); void setPenColor (COLORREF c); void setBrushStyle (int n); void setBrushColor (COLORREF c); set brush color void setBrushHatch (int n); void setColor (COLORREF c);
set pen width
set style of pen
set color of pen
set style of brush
set pattern of brush
set color of current resource
close
virtual void open (); open and initialise window virtual void close ( ); close window and delete all resources

Line void Line (int x 1 , int y 1 , int x 2 , int y 2 );
draw line from ( $\mathrm{x} 1, \mathrm{y} 1$ ) to $(\mathrm{x} 2, \mathrm{y} 2)$

| DoubleOut | void DoubleOut (double number, int dec, int $\mathbf{x}$, int $\mathbf{y}) ;$ <br> print out number starting at coordinate $(\mathrm{x}, \mathrm{y})$ with dec decimal <br> points. |
| :--- | :--- |
| IntegerOut | void IntegerOut (int number, int x, int y$) ;$ <br> print out number starting at coordinate ( $\mathrm{x}, \mathrm{y})$. |
| TextOut | void TextOut (char* text, int x, int y$) ;$ <br> print out text string text, starting at point ( $\mathrm{x}, \mathrm{y})$. |

TimeSeries <series.h>

Abstract class of a time series object, derived from owObifunc.

## Constructors:

TimeSeries ();
Default Constructor
Member functions: protected: update
virtual void update () $=0$;
Has to be defined in derived classes. It takes the output of the time series generator and channels it back to the initial values. This is the function $\Xi(\xi)$ in the time series algorithm point (5), section 4.2.1.
getOutput virtual double getOutput () $=0$;
Has to be defined in derived classes. It returns the desired output variable. This is the function $\Psi(\xi)$ in the time series algorithm point (6) in section 4.2.1.
public:
setUp
setUserInit
virtual int setUp (TStatusWindow*, Param*) $=0$;
Has to be defined in derived classes.
virtual void setUserInit (void* v) $=0$;
Has to be defined in derived classes. It sets initial value(s) as specified in $\mathbf{v}$. It could be an initial wind speed, initial clearness index or both.

TimeSeriesOne
Time series object, derived from TimeSeries. Though, it allows only one initial value, either wind speed or clearness index, but not both.

## Constructors:

TimeSeriesOne (); Default constructor
Data elements:
protected:
initUserVal
randomVal
outVal
double initUserVal; double randomVal; double outVal;
initial value as specified by the user current value of the underlying stochastic process output value

Member functions:
protected:
getInitRandomVal
getRandomNumber
virtual double getInitRandomVal (); returns initial value of underlying stochastic process
getRandomNumber virtual double getRandomNumber () $=0$; Has to be defined in derived classes. It has to return the next random number.
public:
eval double eval (double);
returns the next time series value. The argument is not used, though necessary as this object is derived from owObjfunc.
setUserInit void setUserInit (void*); see TimeSeries::setUserInit.

TIntegerInput <owlappl.h>

Implementation of an input field in a dialog window that expects an integer number. If the input is not valid a message window pops up and the dialog window cannot be closed. TIntegerInput is derived from the Object Windows C++ class TEdit.

## Constructors:

TIntegerInput (PTWindowsObject AParent, int ResourceId);
Data elements:
n
int $n$;
Input value as a number and not text.

Member functions:
Transfer

CanClose
virtual WORD Transfer (void* DataPtr, WORD TransferFlag); Transfer and conversion from data element $n$ to the string in the input field.
virtual BOOL CanClose ();
tries to convert string from input field to an integer. If successful it returns OK. Otherwise ERROR.

This class is derived from TIntegerInput. In addition it checks whether the value $x$ lies in an interval [minVal, maxVal]. If not a message aMessage pops up.

## Constructors:

TIntegerInputI (PTWindowsObject AParent, int ResourceId, const int aMinVal, const int aMaxVal, const char* aMessage);

Member functions:
CanClose virtual BOOL CanClose ();
see TDoubleInput

## TJointDialog

<owdialg.h>

Implementation of the 'Joint Renewable Distribution' dialog window, derived from TDialog of the Object Windows C++ library.

Constructors:
TJointDialog (PTWindowsObject AParent, LPSTR ATitle);

## Member functions:

virtual void WMInitDialog (RTMessage) $=$ [WM_FIRST+WM_INITDIALOG];
Function is carried out upon initialisation of the window.
virtual void HandleCondMsg (RTMessage) $=$ [WM_FIRST + idOpCond];
Function is called upon selection of 'Joint Conditional Function' option in the dialog window. If this option is selected input fields are made visible or invisible as appropriate. The id- constant is defined in owres. $h$.
virtual void HandleProbMsg (RTMessage) = [WM_FIRST + idOpProbDens];
Function is called upon selection of 'Joint Density Function' option in the dialog window. See HandleCondMsg above.

TJointDistributionObject
Calculation window on which calculations of joint renewable power distributions are carried out, derived from TMultiValObject. All necessary functions are privately overwritten. See TMultiValObject.

Constructors:
TJointDistributionObject (PTWindowsObject AParent, LPSTR ATitle);

## TMainWindow

<owrenew.h>
Implementation of the main window with the menu bar. It is derived from the Object Windows C++ class TWindow.

## Constructors:

TMainWindow (PTWindowsObject AParent, LPSTR ATitle);

| a elements: |  |  |
| :---: | :---: | :---: |
| TTransSettingsDlg | TransSettingsDlg; | Buffer for "Settings" window |
| TTransDirDlg | TransDirDlg; | Buffer for "Directories" window |
| TTransExportDlg | TransExportDlg; | Buffer for "Export" window |
| TTransDisplayDlg | TransDisplayDlg; | Buffer for "Display" window |
| TTransSpeedDlg | TransSpeedDlg; | Buffer for "Wind Speed Distributions" window |
| TTransWindDlg | TransWindDlg; | Buffer for "Wind Power Distribution" window |
| TTransSolarDlg | TransSolarDlg; | Buffer for "Solar Power Distribution" window |
| TTransJointDlg | TransJointDlg; | Buffer for "Joint Renewable Power Distribution" window |
| TTransRandDlg | TransRandDlg; | Buffer for "Random number" dialog window |
| TTransMathsDlg | TransMathsDlg; | Buffer for "Maths" window |
| TTransTsDlg | TransTsDlg; | Buffer for "Time Series" window |
| TTransFpDlg | TransFpDlg; | Buffer for "First Passage Time Problems" window |
| PTRenewPlot | testplot; | Graphic window that sits on top of the main window. |

## Member functions:

CanClose
virtual BOOL CanClose ();
Pops up a message window and asks whether the user really wants to quit. If 'Yes' the function returns YES. Otherwise NO.
virtual void CMWindSpeed (RTMessage) $=[$ CM_FIRST +cmWindSpeed$]$;
Function is called upon selection of "Wind speed distribution" menu item. It opens the appropriate dialog by initialising an instance of class TSpeedDialog.
virtual void CMSettings (RTMessage) $=$ [CM_FIRST + cmSettings];
Function is called upon selection of "Settings" menu item. It opens the appropriate dialog by initialising an instance of class TSettingsDialog.
virtual void CMMaths (RTMessage) $=$ [CM_FIRST + cmMaths];
Function is called upon selection of "Maths" menu item. It opens the appropriate dialog by initialising an instance of class

TMathsDialog.
virtual void CMWindPower (RTMessage) $=$ [CM_FIRST +cmWindPower$]$;
Function is called upon selection of "Wind Power Distribution" menu item. It opens the appropriate dialog by initialising an instance of class TWindDialog.
virtual void CMSolar (RTMessage) $=$ [CM_FIRST +cmSolar$]$;
Function is called upon selection of "Solar Power Distribution" menu item. It opens the appropriate dialog by initialising an instance of class TSolarDialog.
virtual void CMRenewable (RTMessage) = [CM_FIRST + cmRenewable];
Function is called upon selection of "Joint Renewable Distribution" menu item. It opens the appropriate dialog by initialising an instance of class TJointDialog.
virtual void CMExport (RTMessage) $=$ [CM_FIRST + cmExport $]$;
Function is called upon selection of "Export" menu item. It opens the appropriate dialog by initialising an instance of class TExportDialog.
virtual void CMDisplay (RTMessage) $=$ [CM_FIRST + cmDisplay $]$;
Function is called upon selection of "Display Options" menu item. It opens the appropriate dialog by initialising an instance of class TDisplayDialog.
virtual void CMHelp (RTMessage) $=$ [CM_FIRST + cmHelp];
Function is called upon selection of "Help" menu item. It pops up a message that this feature is not implemented.
virtual void CMDir (RTMessage) $=$ [CM_FIRST + cmDirectories $]$;
Function is called upon selection of "Directories" menu item. It opens the appropriate dialog by initialising an instance of class TDirDialog.
virtual void CMRandom (RTMessage) $=$ [CM_FIRST + cmRandom];
Function is called upon selection of "Random Numbers" menu item. It opens the appropriate dialog by initialising an instance of class TRandomDialog.
virtual void CMTimeSeries (RTMessage) $=$ [CM_FIRST + cmTimeSeries];
Function is called upon selection of "Time Series" menu item. It opens the appropriate dialog by initialising an instance of class TTsDialog.
virtual void CMFpt (RTMessage) $=[$ CM_FIRST + cmFirstPassage $]$;
Function is called upon selection of "First Passage Time Problems" menu item. It opens the appropriate dialog by initialising an instance of class TFpDialog.

## Operators:

Save dialog window data to a file and retrieving them in the next session by using the stream operators. They affect all data stored in the buffers with prefix 'Trans'.
friend ostream\& operator $\ll$ (ostream\&, RTMainWindow);
friend istream\& operator >> (istream\&, RTMainWindow);

TMathsDialog
<owdialg.h>
Implementation of the 'Mathematical Options' dialog window, derived from TDialog of the Object Windows C++ library.

Constructors:
TMathsDialog (PTWindowsObject AParent, LPSTR ATitle);

TMultiValObject
<owstat.h>

This class is derived from TStatusWindow. It is designed for the case that more than one value is to be calculated.

## Constructors:

TMultiValObject (PTWindowsObject AParent, LPSTR ATitle, int eval); initialise the class with eval being the number of function evaluations to be carried out.

| Member functions: protected: |  |
| :---: | :---: |
| workOutBasic | virtual int workOutBasic ( ) $=0$; |
|  | The function TStatusWindow::workOut has been split up here into two parts: First, calculations that have to be carried out prior to the evaluation of the first function value. This goes in here. virtual int workOutValues () $=0$; |
| workOutValues | This is the second part, where all values are calculated. The split is necessary as after workOutBasic the parameters are checked. In case they are pointless (return value of workOutBasic not OK) a message window will inform the user. Otherwise the programme |
|  | continues with the calculation of the function values in workOutValues. |
| areParametersOK | virtual int areParametersOK ( ) = 0; |
|  | This function is only called if the accumulation of curves in the diagram is desired. Here is the function to check that the current curve is compatible with the last calculations. |
| setOIdParameter | virtual void setOldParameter ( ) = 0; |
|  | This function is to be called after areParameterOK and is used by the next calculations for the same reason as stated in areParametersOK. |
| workOut | int workOut (); |
|  | overwrites TStatusWindow::workOut by splitting up into workOutBasic and workOutValues. |

calcValues
public:
calc
void calcValues (owObjfunc* func, double xmin, double xmax); The function carries out eval function evaluations on the object function func in the x - interval [ $x \mathrm{~min}, x \max$ ]. The number of evaluations is already specified in the constructor.
static void calc (owObjfunc* func, double xmin, double xmax, int N , TStatusWindow* window);
Static member function that carries out N function evaluations on func by using the status window window.

Calculation window on which the calculation of the first passage time is carried out provided only one value is required at the time, derived from TStatusWindow. If a whole curve of first passage time values (e.g. as a function of hte initial value) is required use class PassageTimesObject. All necessary functions are privately overwritten. See TStatusWindow.

## Constructors:

TPassageTimeObject (PTWindowsObject AParent, LPSTR ATitle);

Member functions:
workOut
writeRepl
protected: int workOut (); carry out the random number generator test. protected: void writeRepl (); write reply to parent StatusWindow into textline.

## TPlot

<owplot.h>
Graphical representation of functions. TPlot draws a complete coordinate system, with axes, grid lines, text and curves. It is derived from TGraph.

## Constructors:

TPlot (PTWindowsObject AParent, LPSTR ATtitle, PTModule AModule = NULL);

## Member functions:

public:

| plot | virtual void plot (); do nothing! This function has to be overwritten by derived classes. |
| :---: | :---: |
| draw | virtual void draw (); draw the whole diagram by calling plot. |
| Paint | virtual void Paint (HDC PaintDC, PAINTSTRUCT _FAR\& P); overwrites Paint from TWindow. See Object Windows C++ guide for more details. |
| setHeadLine | void setHeadLine (const char*); set headline |
| setSubLine | void setHeadLine (const char*); set line below headline |
| plotFactor | void plotFactor (double x ); |


double ygrid, const char* ytext);
Draw a linear coordinate system. Parameters as in axis: :setAxis.
Please note that setCoordinates has to be called prior to this
function.
void drawAutoLinCoord (double xmin, double xmax, VECTOR*
yval, const char* xtext, const char* ytext, int xaxgrid, int yaxgrid,
double scale int $\mathrm{n}=0$ );
Draw a linear coordinate system using drawLinCoord. Though,
before call setAutoCoord.
void drawCurve (VECTOR\& x, VECTOR\& y, DRA_MODE
draw_mode);
draw a curve with its x- and y- values in the diagram. draw_mode
is one of the following options:
PIXEL Do not connect two points
POLYGON Do connect subsequent points by a line
STEP Draw function as a staircase function
DIRAC Draw function as a Dirac function

TRenewApp <owrenew.h>
Main application, derived from Object Windows C++ class TApplication.
Constructors:
TRenewApp (LPSTR AName, HINSTANCE hInstance, HINSTANCE hPrevInstance, LPSTR lpCmdLine, int nCmdShow);

## Member functions:

InitMainWindow virtual void InitMainWindow ();
overwrites TApplication::InitMainWindow and intialises an instance of TMainWindow.

## TRenewPlot

Implementation of the graphic window that draws the diagrams. It is directly derived from TPlot. It is extended by the clear - flag. See data element below.

Constructors:
TRenewPlot (PTWindowObject AParent, LPSTR ATitle, PTModule AModule = NULL);
Data elements:
clear int clear; If clear is set to NO, the window draws the implied diagram. Otherwise the next call to Paint causes the window to be cleared.

Member functions:
Paint
plot
virtual void Paint (HDC PaintDC, PAINTSTRUC _FAR\& PaintInfo); calls TPlot::Paint if clear is YES. Otherwise it calls TPlot::draw. void plot ();
overwrites TPlot::plot. It draws the whole diagram given the curve data in GraphData which is an instance of class Graph.

Object that calculates the first passage time of joint renewable power fluctuations using the time series approach. It is derived from TSPassageTime.

## Constructors:

TSPassageTime (); Constructor that initialises a JointPowerTimeSeries object in place of timeSeries data element.

Member functions:
SetUp
int SetUp (TStatusWindow*, Param*);
Setting up the appropriate parameters.

TSPassageTime
Object that calculates the first passage time using the time series approach. It is directly derived from PassageTime.

Constructors:
TSPassageTime (); Default Constructor
Data elements:
protected:
timeSeries
TimeSeries* timeSeries;
Time series object to be used in the first passage time calculations.
Member functions:
protected:
SetUp
public:
Eval
setInitLevel
virtual int SetUp (TStatusWindow*, Param*);
see PassageTime::setUp.
double Eval (double x);
returns the first passage time where x is the passage level. It uses the time series timeSeries. Hence, derived classes need to initialise the time series they require. void setInitLevel (void*);
overwrites PassageTime::setInitLevel for time series approach objects. It calls TimeSeries::setUserInit

Object that calculates the first passage time of PV array power fluctuations using the time series approach. It is derived from TSPassageTime.

Constructors:
TSPassageTime (); Constructor that initialises a SolarPowerTimeSeries object in place of timeSeries data element.

Member functions:
SetUp
int SetUp (TStatusWindow*, Param*);
Setting up the appropriate parameters.

TStatusWindow
<owstat.h>

Window that pops up just before starting a calculation. Upon pressing the OK button the calculations are carried out. The status of the calculations can be observed by looking at the status lines in the window. It is derived from TDialog.

Constractors:
TStatusWindow (PTWindowsObject AParent, LPSTR ATitle);

## Data elements:

 tempstatic double temp;
This is a static data element. Calculation objects can write values in it that can be picked up by TStatusWindow.

## Member functions: protected: giveWarning

writeRepl
writeRep2
workOut
int giveWarning (char* message);
opens a window issuing a warning with text message. The user is given three options: OK, Ignore or Abort. Depending on his selection the return value is IDOK, IDIGNORE or IDABORT. virtual void writeRepl (); print out the first status line.
virtual void writeRep2 (); print out the second status line.
virtual int workOut () $=0$;
Abstract function that must be overwritten in derived classes. It carries out all the calculations. It returns OK if no error occurred.
virtual void WMInitDialog (RTMessage) = [WM_FIRST+WM_INITDIALOG];
Initialisation of the dialog window
virtual void Ok (RTMessage) = [ID_FIRST + IDOK];
Function that is called upon the selection of the OK button. It calls workOut to carry out the calculations.
virtual void Retry (RTMessage) = [ID_FIRST + IDRETRY];
Function that is called upon the selection of the Retry button. It is almost identical with Ok. Only that the Retry button can not always be selected.
virtual void TimeMsg (RTMessage) $=$ [WM_USER+WM_MSGOBJFUNC];
Function called upon a time message that is invoked in an instance of the class msgObifunc. Calculations should be carried out in this class, as it enables them to send time messages. TStatusWindow receives the time message and write then the elapsed time (since starting the calcualtions) to the status line.
public:
writeTime
isEnoughTime
writeStatus.
writeStatus2
void writeTime ();
write the time elapsed to the satus line
int isEnoughTime ();
in order to avoid writing to the screen too often this function can be asked prior to writing to the screen whether enough time has been elapsed since last writing. If so, it returns YES. Otherwise NO.
void writeStatus1 (char* text);
write text to first status line.
writeStatus2 void writeStatus2 (char* text);
write text to second status line in the dialog window.

TSWindSpeedPassageTime
<passage.h>

Object that calculates the first passage time of wind speed fluctuations using the time series approach. It is derived from TSPassageTime.

Constructors:
TSWindSpeedPassageTime (); Constructor that initialises a WindSpeedTimeSeries object in place of timeSeries data element.

Member functions:
SetUp int SetUp (TStatusWindow*, Param*);
Setting up the appropriate parameters.

TSWindPowerPassageTime
<passage.h>

Object that calculates the first passage time of wind turbine power fluctuations using the
time series approach. It is derived from TSPassageTime.
Constructors:
TSPassageTime ( ); Constructor that initialises a WindPowerTimeSeries object in place of timeSeries data element.

## Member functions:

SetUp
int SetUp (TStatusWindow*, Param*);
Setting up the appropriate parameters.

Implementation of the Random Numbers' dialog window, derived from TDialog of the Object Windows C++ library.

## Constructors:

TRandDialog (PTWindowsObject AParent, LPSTR ATitle);

## Member functions:

virtual void WMInitDialog (RTMessage) = [WM_FIRST+WM_INITDIALOG];
Function is carried out upon initialisation of the window.
virtual void HandleUniMsg (RTMessage) $=$ [WM_FIRST + idOpRandOpO];
Function is called upon selection of 'Uniform distribution' option in the dialog window. If this option is selected input fields are made visible or invisible as appropriate. The id- constant is defined in owres.h.
virtual void HandleNormMsg (RTMessage) $=$ [WM_FIRST $+\mathrm{idOpRandOp} 1]$;
Function is called upon selection of 'Normal distribution' option in the dialog window. See HandleUniMsg above.
virtual void HandleBetaMsg (RTMessage) $=$ [WM_FIRST + idOpRandOp2];
Function is called upon selection of 'Beta- distribution' option in the dialog window. See HandleUniMsg above.
virtual void HandleBiMsg (RTMessage) $=$ [WM_FIRST + idOpRandOp2];
Function is called upon selection of 'Binomial distribution' option in the dialog window. See HandleUniMsg above.

## TRandomObject

Calculation window on which the random number generators are tested, derived from TStatusWindow. All necessary functions are privately overwritten. See TStatusWindow.

Constructors:
TRandomObject (PTWindowsObject AParent, LPSTR ATitle);
Member functions:
workOut
protected: int workOut ( );
carry out the random number generator test.
writeRepl protected: void writeRep1 ();
write reply to parent StatusWindow into textline.

Implementation of the 'Settings' dialog window, derived from TDialog of the Object Windows C++ library.

Constructors:
TSettingsDialog (PTWindowsObject AParent, LPSTR ATitle);

TSolarDialog
<owdialg.h>
Implementation of the 'Solar Power Distribution' dialog window, derived from TDialog of the Object Windows C++ library.

## Constructors:

TSolarDialog (PTWindowsObject AParent, LPSTR ATitle);

## Member functions:

vittual void WMInitDialog (RTMessage) = [WM_FIRST+WM_INITDIALOG];
Function is carried out upon initialisation of the window.
virtual void HandleAnalytMsg (RTMessage) $=$ [WM_FIRST + idOpAnalyt];
Function is called upon selection of 'Analytical Function' option in the dialog window. If this option is selected input fields are made visible or invisible as appropriate. The id- constant is defined in owres. $h$.
virtual void HandleApproxMsg (RTMessage) $=$ [WM_FIRST + idOpApprox];
Function is called upon selection of 'Approximation' option in the dialog window. See HandleAnalytMsg above.
virtual void HandleCondMsg (RTMessage) = [WM_FIRST + idOpCond];
Function is called upon selection of 'Conditional Distribution' option in the dialog window. See HandleAnalytMsg above.
virtual void HandleQualMsg (RTMessage) $=[$ WM_FIRST + idOpQual];
Function is called upon selection of 'Quality of Approximation' option in the dialog window. See HandleAnalytMsg above.

TSpeedDialog
<owdialg.h>
Implementation of the 'Wind Speed Distribution' dialog window, derived from TDialog of the Object Windows C++ library.

Constructors:
TSpeedDialog (PTWindowsObject AParent, LPSTR ATitle);

TTimeSeriesObject
<owcalc.h>
Calculation window on which calculations of time series are carried out, derived from TMultiValObject. All necessary functions are privately overwritten. See TMultiValObject.

Constructors:
TTimeSeriesObject (PTWindowsObject AParent, LPSTR ATitle);

TTransDirDlg
<owdialg.h>
Parameter transfer buffer for TDirDialog. All input paramters in the dialog window appear here as data elements.

## Constructors:

TTransDirDlg ( ); Default Constructor
Data elements:
solFile char solFile[50]; file name of file for solar data
dlgFile char dlgFile[50];
file name of dialog file (not used in the programme!)

Operators:
friend ostream\& operator $\ll$ (ostream\&, TTransDirDlg\&);
friend istream\& operator $\gg$ (istream\&, TTransDirDlg\&);

TTransDisplayDlg
<owdialg.h>
Parameter transfer buffer for TDisplayDialog. All input paramters in the dialog window appear here as data elements.

## Constructors:

TTransDisplayDlg (); Default Constructor
Data elements:
opAuto $\quad$ WORD opAuto; Flag: Automatic display of graphs
opAccu WORD opAccu;
opLegend
WORD opLegend;

Flag: Accumulating data series
Flag: Ask for legend text

Member functions:
setParameter void setParameter ( );

Transfer above data elements to the corresponding fields in the global variable param.

Operators:<br>friend ostream\& operator << (ostream\&, TTransDisplayDlg\&); friend istream\& operator >> (istream\&, TTransDisplayDlg\&);

TTransExportDlg

Parameter transfer buffer for TExportDialog. All input paramters in the dialog window appear here as data elements.

## Constructors: <br> TTransExportDlg ( ); Default Constructor

Data elements:

| opNew | WORD opNew; | Flag: Export data to new file |
| :--- | :--- | :--- |
| opAttach | WORD opAttach; | Flag: Attach data to existing file |
| expFile | char expFile[50]; | Name of export file |

Member functions:
setParameter void setParameter ();
Transfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator $\ll$ (ostream\&, TTransExportDlg\&);
friend istream\& operator >> (istream\&, TTransExportDlg\&);

TTransFpDlg
<owdialg.h>

Parameter transfer buffer for TFpDialog. All input paramters in the dialog window appear here as data elements.

Constructors:
TTransFpDlg (); Default Constructor

## Data elements:

| fpOp0 | WORD fpOp0; | Flag: Wind Speed |
| :--- | :--- | :--- |
| fpOp1 | WORD fpOp1; | Flag: Wind turbine power time series |
| fpOp2 | WORD fpOp2; | Flag: PV array power time series |
| fpOp3 | WORD fpOp3; | Flag: Joint renewable power time series |
| fpOp4 | WORD fpOp4; | Flag: Time Series Approach |
| fpOp5 | WORD fpOp5; | Flag: Markov Chain Approach |


| fpOp6 | WORD fpOp6; | Flag: Calculate one value only |
| :---: | :---: | :---: |
| fpOp7 | WORD fpOp7; | Flag: Calculate first passage time as a function of the initial value |
| fpOp8 | WORD fpOp8; | Flag: Calculate first passage time as a function of the passage level |
| initV | double initV; | Initial wind speed |
| initK | double initK; | Initial average hourly clearness index $\mathrm{k}(0)$ |
| initP | double initP; | Initial, normalised power |
| passV | double passV; | wind speed passage level |
| passK | double passK; | clearness index passage level |
| passP | double passP; | power passage level |
| timeStep | double timeStep; | time step for time series approach only |
| noVal | int noVal; | number of values to be calculated if more than one value is required |

## Member functions:

setParameter
void setParameter ( );
Ttssfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator $\ll$ (ostream\&, TTransFpDlg\&);
friend istream\& operator >> (istream\&, TTransFpDlg\&);

## TTransJointDIg

<owdialg.h>
Parameter transfer buffer for TJointDialog. All input paramters in the dialog window appear here as data elements.

Constructors:
TTransJointDlg (); Default Constructor
Data elements:
opJointDens
opJointCond
vmean
initialv
clearness
initialK
tau
eval
zeta

WORD opJointDens; Flag: Joint density function (stationary) WORD opJointCond; Flag: Joint conditional density function double vmean; double initialv; double clearness; double initialK;
double tau; int eval; double zeta;

Average wind speed Initial wind speed Average hourly clearness index k Initial average hourly cleamess index $\mathrm{k}(0)$
Time tau (for conditional distribution)
Number of evaluations
Fractional power factor $\zeta$

## Member functions:

setParameter
void setParameter ();
Transfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator << (ostream\&, TTransJointDlg\&);
friend istream\& operator >> (istream\&, TTransJointDlg\&);

TTransMathsDIg <owdialg.h>

Parameter transfer buffer for TMathsDialog. All input paramters in the dialog window appear here as data elements.

## Constructors:

TTransMathsDlg (); Default Constructor

| Data elements: <br> solTrial | int solTrial; | number of trial points in optimisation of <br> approximated distribution function of PV <br> array power. |
| :--- | :--- | :--- |
| solCoeff | int solCoeff; | number of coefficients in approximated <br> distribution function of PV array power. <br> Number of time series taken into account <br> in first passage time calculations using <br> the time series approach. <br> Maximum number of iterations in the <br> time series approach algorithm for first |
| fpTsTrial | int fpTsTrial; | passage times |
| fpTsMaxIt | int fpTsMaxIt; | Stopping criterion in the Markov chain <br> approach algorithm. |
| fpMcStopCrit | int fpMcMaxIt; | Maximum number of iterations in the <br> Markov chain approach algorithm. |
| fpMcMaxIt | int fpMcGrid; | Mot in use. |
| fpMcGrid | int classes; | Number of discrete levels in a discrete <br> distribution. |

Member functions:
setParameter
void setParameter ();
Transfer above data elements to the corresponding fields in the global variable param.

Operators:
friend ostream\& operator << (ostream\&, TTransMathsDlg\&);
friend istream\& operator >> (istream\&, TTransMathsDlg\&);

Parameter transfer buffer for TRandDialog. All input paramters in the dialog window appear here as data elements.

## Constructors:

TTransRandDlg (); Default Constructor

## Data elements:

| ranOp0 | WORD ranOp0; | Flag: Uniform distribution |
| :--- | :--- | :--- |
| ranOp1 | WORD ranOp1; | Flag: Normal distribution |
| ranOp2 | WORD ranO2; | Flag: Beta- distribution |
| ranOp3 | WORD ranOp3; | Flag Binomial distribution |
| ranA | double ranA; | Parameter $\alpha$ for Beta- distribution |
| ranB | double ranB; | Parameter $\beta$ fro Beta- distribution |
| ranClass | int ranClass; | Number of classes for Kolmogorov- |
| ranTrial | int ranTrial; | Smirnov test |
|  |  | Number of random numbers to be <br> generated per set. |

## Member functions:

setParameter
void setParameter ();
Transfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator << (ostream\&, TTransRandDlg\&);
friend istream\& operator >> (istream\&, TTransRandDlg\&);

## TTransSettingsDlg

 <owdialg.h>Parameter transfer buffer for TSettingsDialog. All input paramters in the dialog window appear here as data elements.

## Constructors:

TTransSettingsDlg (); Default Constructor
Data elements:

| wiVci | double wiVci; | cut-in wind speed |
| :--- | :--- | :--- |
| wiVco | double wiVco; | cut-out wind speed |
| wiVr | double wiVr; | rated wind speed |
| wiVmean | double wiVmean; | mean wind speed |
| wiSigma | double wiSigma; | wind standard deviation $\sigma_{k}$ |
| wiBeta | double wiBeta; | autocorrelation coefficient of wind |

solK0
solSigmaK
solBeta double solBeta;
comZeta
batK
batc
batQMax
batV
sysPRen
sysPDemand
double solK0;
double solSigmaK;
double comZeta; double batK;
double batC;
double batQMax; double batV; double sysPRen; double sysPDemand;
turbulence $\beta_{v}$
max hourly clearness index $K_{0}$. standard deviation of the average hourly clearness index, $\sigma_{k}$. autocorrelation coefficient of the hourly clearness index, $\beta_{x}$ Fractional power factor $\zeta$
Battery factor $k$
Battery factor c
Battery Capacity
Battery voltage
Installed renewable power
Power demand

Member functions:
setParameter
void setParameter ();
Transfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator << (ostream\&, TTransSettingsDlg\&);
friend istream\& operator $\gg$ (istream\&, TTransSettingsDlg\&);

TTransSolarDlg
Parameter transfer buffer for TSolarDialog. All input paramters in the dialog window appear here as data elements.

Constructors:
TTransSolarDlg (); Default Constructor
Data elements:

| opProb | WORD opProb; | Flag: probability density function |
| :---: | :---: | :---: |
| opDist | WORD opDist; | Flag: distribution function |
| opAnalyt | WORD opAnalyt; | Flag: Analytical function |
| opApprox | WORD opApprox; | Flag: Approximation |
| opCond | WORD opCond; | Flag: conditional process |
| opQual | WORD opQual; | Flag: Quality of approximation |
| opBypass | WORD opBypass; | Flag: Bypass selected. |
| clearness | double clearness; | Average hourly clearness index |
| initialK | double initialK; | Initial average hourly clearness index $\mathrm{k}(0)$ |
| trial | int trial; | Number of trial points (for approximation only) |
| coeff | int coeff; | Number of coefficients in approximation |

of distribution function.
Member functions:
setParameter void setParameter ();
Transfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator << (ostream\&, TTransSolarDlg\&);
friend istream\& operator >> (istream\&, TTransSolarDlg\&);

TTransSpeedDlg <owdialg.h>

Parameter transfer buffer for TSpeedDialog. All input paramters in the dialog window appear here as data elements.

Constructors:
TTransSpeedDlg (); Default Constructor
Data elements:
opProb WORD opProb; Flag: Probability density function
opDist
vmean
vmin
vmax
eval

WORD opDist; double vmean; double vmin; double vmax; int eval;

Flag: Distribution function mean wind speed
Speed at which to start calculations Speed at which to finish calculations Number of evaluations required

## Member functions:

setParameter
void setParameter ();
Transfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator << (ostream\&, TTransSpeedDlg\&);
friend istream\& operator >> (istream\&, TTransSpeedDlg\&);

## TTransTsDlg

 <owdialg.h>Parameter transfer buffer for TTsDialog. All input paramters in the dialog window appear here as data elements.

Constructors:
TTransTsDlg ( ); Default Constructor

Data elements:
tsOp0
tsOp1
tsOp2
tsOp3
tsOp4
tsOp5
tsTimeStep
tsPoints
initV
initK
initQ10
initQ20
Member functions:
setParameter

WORD tsOp0; Flag: Wind speed time series
WORD tsOpl;
WORD tsOp2;
WORD tsOp3;
WORD tsOp4;
WORD tsOp5;
double tsTimeStep;
int tsPoints;
double initV;
double initK;
double initQ10;
double initQ20;

Flag: wind turbine power time series Flag: PV array power time series Flag: Joint renewable power time series
Flag: State of charge time series Flag: Power deficit time series Time step $\Delta t$ that is implicit in the time series
Number of points to be calculated
Initial wind speed
Initial average hourly clearness index $\mathrm{k}(0)$
Initial available charge $Q_{10}$ Intiial bound charge $\mathrm{Q}_{20}$
void setParameter ();
Ttssfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator $\ll$ (ostream\&, TTransTsDlg\&);
friend istream\& operator >> (istream\&, TTransTsDlg\&);

## TTransWindDlg

 <owdialg.h>Parameter transfer buffer for TWindDialog. All input paramters in the dialog window appear here as data elements.

## Constructors:

TTransWindDlg (); Default Constructor

## Data elements:

opProb
opDist
opStationary
opCond
vmean
eval
tau
initialv

WORD opProb;
WORD opDist;
WORD opStationary; WORD opCond; double vmean;
int eval;
double tau;
double initialv;

Flag: probability density function
Flag: distribution function
Flag: stationary process
Flag: conditional process mean wind speed
number of evaluations required time tau
initial wind speed

Member functions:
setParameter void setParameter ();

Transfer above data elements to the corresponding fields in the global variable param.

## Operators:

friend ostream\& operator << (ostream\&, TTransWindDlg\&);
friend istream\& operator >> (istream\&, TTransWindDlg\&);
TTsDialog <owdialg.h>

Implementation of the "Time Series' dialog window, derived from TDialog of the Object Windows C++ library.

Constructors:
TTsDialog (PTWindowsObject AParent, LPSTR ATitle);

| Member functions: |
| :--- |
| virtual void WMInitDialog (RTMessage) $=[$ WM_FIRST+WM_INITDIALOG]; |
| Function is carried out upon initialisation of the window. |
| virtual void HandleOp0Msg (RTMessage) $=$ [WM_FIRST + idTsOp0]; |
| Function is called upon selection of 'Wind Speed' option in the |
| dialog window. If this option is selected input fields are made |
| visible or invisible as appropriate. The id- constant is defined in |
| owres.h. |

virtual void HandleOplMsg (RTMessage) = [WM_FIRST + idTsOp1];
Function is called upon selection of 'Wind Power' option in the
dialog window. See HandleOpOMsg above.

TYoMessage
<owlappl.h>
Implementation of a message window with title ATitle, and four different actions that can be taken. See member functions. TYoMessage is derived from TDialog. Which event functions may be called depends on the resource ID the class was constructed with. E.g. it might be a
window with only a Yes and No button. In this instance the function CMIgnore could not be called as there is no Ignore button.

## Constructors:

TYoMessage (PTWindowsObject AParent, LPSTR ATitle, char* a Message);

```
Member functions:
virtual void WMInitDialog (RTMessage) = [WM_FIRST+WM_INITDIALOG];
virtual void CMYes (RTMessage) = [ID_FIRST + IDYES];
    Function called upon event 'CMYes'
virtual void CMNo (RTMessage) = [ID_FIRST + IDNO];
    Function called upon event 'CMNo'
virtual void CMIgnore (RTMessage) = [ID_FIRST + IDIGNORE];
    Function called upon event 'CMIgnore' (Ignore - button)
virtual void CMAbort (RTMessage) = [ID_FIRST + IDABORT];
    Function calles upon event 'CMAbort' (Abort - button)
```

TYoInput
<owlappl.h>

Implementation of a dialog window with one input field. It is derived from TDialog.

## Constructors:

TYoInput (PTWindowsObject AParent, LPSTR ATitle, char* title, char* input);
Data elements:
textBuffer char textBuffer[80]; Implied input string
Member functions:
virtual void WMInitDialog (RTMessage) $=$ [WM_FIRST + WM_INITDIALOG $]$;
Initialisation of the window.

## TWindDialog

<owdialg.h>

Implementation of the 'Wind Power Distribution' dialog window, derived from TDialog of the Object Windows C++ library.

## Constructors:

TWindDialog (PTWindowsObject AParent, LPSTR ATitle);
Member functions:
virtual void WMInitDialog (RTMessage) $=$ [WM_FIRST+WM_INITDIALOG];
Function is carried out upon initialisation of the window.
virtual void HandleCondMsg (RTMessage) $=$ [WM_FIRST + idOpCond];
Function is called upon selection of 'Conditional distribution'
option in the dialog window. If this option is selected the input fields for time tau and initial wind speed have to be made visible. The constant idOpCond is defined in owres.h.
virtual void HandleStatMsg (RTMessage) $=$ [WM_FIRST + idOpStationary];
Function is called upon selection of 'Stationary distribution' option in the dialog window. It makes the input fields for the time tau and the initial wind speed invisible. Compare with HandleCondMsg

TWindSpeedObject
<owcalc.h>

Calculation window on which calculations of wind speed distributions are carried out, derived from TMultiValObject. All necessary functions are privately overwritten. See TMultiValObject.

Constructors:
TWindSpeedObject (PTWindowsObject AParent, LPSTR ATitle);

UniKgSTest
<random.h>

Kolmogorov- Smirnov test for uniform distribution, derived from KgSTest.
Constructors:
UniKgSTest ( n ); Construct test object for n trial points.
Member functions:
theoretProb double theoretProb (double x ); see KgSTest::theoretProb. initialize void intiialize ( );
initialise randomizer with uniRand object.
uniRand
<random.h>
Random number generator. The numbers are drawn from a uniform distribution using the standard C - library function rand(). Before generating number for the first time the member function initialize ( ) should be called.

Constructor:
uniRand ()
Default constructor
Member functions:
initialize
void initialize ();
initializes the generator with the current time.
getRandomNumber virtual double getRandomNumber (); returns the next random number.

## uniRejectRand

<random.h>

Implementation of a random number generator using the rejection mehtod with a uniform distribution as comparison function for distributions with non zero values in the interval [ 0,1$]$. It is immediately derived from rejectRand.

## Constructors:

uniRejectRand (); Default constructor with unit ceiling.
uniRejectRand (double max);
Constructor with ceiling max.
VECTOR
<vectors.h>
Implementation of a vector with real number as elements. The class implements a huge variety of functions on vectors and operations.
typedef VECTOR_<int> IVECTOR;
typedef VECTOR_<double> VECTOR;
typedef VECTOR_<float> FVECTOR;

## Constructors:

| $\begin{aligned} & \text { VECTOR_(VECTOR_\& v); } \\ & \text { VECTOR_(int n); } \end{aligned}$ |  | Copy |
| :---: | :---: | :---: |
|  |  | Const |
| Data members: dim | int dim; | Dime |
| Member functions: add | void ad <br> add an | x); ment, $x$ |
| build | void bu Standar | (istream put vi |
| copy | VECTO returns |  |
| create | void cre allocate | (int n ) emory |
| del | void de <br> deletes <br> dimensi | n); ment by 1. |
| move_down | T move | wn () |


| move_up | T move_up (); moves up all components by 1 . Return element thath is no longer in the vector. |
| :---: | :---: |
| mul | friend MATRIX_mul (VECTOR_\& $u$, VECTOR_\& $v$ ); Vecor ultipliction $\mathbf{A}=\mathbf{u}^{\mathbf{T}}$ |
| print | void print (ostream\& op); Standard output on the stream. |
| search | int search ( T ); <br> Search for element $x$ in the vector. Return the index of the first element. If $x$ is not element of the vector, return 0 , otherwise its index. |
| set | void set ( T x); <br> Set all components on $\mathbf{x}$. |
| swap | void swap (int $i$, int $j$ ); <br> Swap the $i$-th and $j$-th element. |

## Operators:

| () | $\mathbf{v}$ (int i); Access to elemnt i (indices from 1 ...dim) |
| :---: | :---: |
| $+,+=,-,=$ | $\mathbf{v}+\mathbf{u}, \mathbf{v}+\mathrm{a}, \mathbf{v}-\mathbf{u}, \mathbf{v}-\mathrm{a}(\mathbf{u}, \mathbf{v}$, Vectors; a real number) <br> Note.: Addition or subtraction of a real number means all components are affected in the same way. |
| * | multply by number: $\quad \mathbf{u}=\alpha^{*} \mathbf{v}, \mathbf{u}=\mathbf{v}^{*} \alpha, \mathbf{v} *=\alpha$ multiply each component: $\quad \mathbf{u}=\mathbf{v} * \mathbf{w}$ |
| 1 | Divide by number $\alpha: \quad \mathbf{u}=\mathbf{v} / \alpha ; \mathbf{u} /=\alpha$; |
| = | Assignment. Works even if dimensions of both vectors befor assignment are not the same |
| = ! | $(\mathbf{u}==\mathbf{v})$ TRUE, if all components in $\mathbf{u}$ and $\mathbf{v}$ are identical. <br> $(\mathbf{u}!=\mathbf{v})$ TRUE, if at least two components of $\mathbf{u}$ and $\mathbf{v}$ are <br>  different. |
| <, < | $(\mathbf{u}<=\mathbf{v})$ TRUE, if all components of $\mathbf{u}$ are less than the components of $\mathbf{v}$. |
| >,>= | ( $\mathbf{u}>=\mathbf{v}$ ) TRUE, if all components of $\mathbf{u}$ are greater than the components of $\mathbf{v}$. |
| << | operator << (ostream\& op, VECTOR_<T>\&v); |
| >> | operator >> (istream\& ip, VECTOR_<T>\& v); |

Object function for first passage times of wind turbine pwoer fluctuations, derived from PassageTimes.

## Constructors:

WindSpeedPassageTimes ( int select );
Constructor: If select $=0$ the data element passageTime is initialised with an instance of TSWindPowerPassageTime. Otherwise with MCWindPowerPassageTime.

Member functions:
$\begin{array}{ll}\text { SetUp } & \begin{array}{l}\text { int SetUp (TStatusWindow*, Param*); } \\ \text { individual set-up of initial values and passage levels. }\end{array}\end{array}$

WindPowerTimeSeries
<series.h>

Implementation of wind turbine power time series, derived from class WindSpeedTimeSeries.
Constructors:
WindPowerTimeSeries (); calls the constructors of the base class.

| Member functions: <br> getWindPower | static double getWindPower (double v , double vci, double vco, <br> double vr); <br> return the wind turbine power for a given wind speed, v, cut-in <br> wind speed vci, cut-out wind speed, vco, and a rated wind speed, <br> vr. It uses equation (3.1). |
| :--- | :--- |
| getV | static double getV (double p, double vci, double vr); <br> Inverse function to getWindPower. It returns the wind speed for a <br> given power p, cut-in wind speed vci and rated wind speed, vr. It <br> uses the invertible part of (3.1) only. |
| getOutput | double getOutput (); see TimeSeries::getOutput <br> setUp |

WindSpeedPassageTimes <passage.h>
Object function for first passage times of wind speed fluctuations, derived from PassageTimes.

## Constructors:

WindSpeedPassageTimes (int select );
Constructor: If ele $t=0$ the data element pa ageTi $e$ is initialised with an instance of TSWindSpeedPassageTime. Otherwise with MCWindSpeedPassageTime.

Member functions:
SetUp
int SetUp (TStatusWindow*, Param*);
individual set-up of initial values and passage levels.

WindSpeedTimeSeries
<series.h>
Implementation of wind speed time series, derived from TimeSeriesOne.
Constructors:
WindSpeedTimeSeries (); Default constructor. Initialises uniRand object as internal random number generator.

Data elements:
protected:

| $\mathbf{r}$ | double r; | autocorrelation coefficient |
| :--- | :--- | :--- |
| sigma | double sigma; | wind speed standard deviation |

Member functions:
protected:
getRandomNumber
getOutput
public:
setUp
update
setCorrelation
double getRandomNumber ();
returns next random number from the implied random number generator.
double getOutput (); see TimeSeries::getOutput
int setUp (TStatusWindow*, Param*);
Parameter setting
void update ();
void setCorrelation (double r);
see TimeSeries::update
set correlation coefficient

### 7.4 Global Functions

This section discusses all global functions. They are listed in alphabetical order within the source files they are in.
<cstring.cpp>
String Functions
catDayName
<cstring.h>
Function: Concatenate full day name
Syntax: void catDayName (char* buffer, int day);
Purpose: Upon day the function concatenate the full day name ("Monday", ...) .day $=0$ points to "Sunday"
catDbl <cstring.h>

Function: Concatenate double number into string
Syntax: void catDbl (char* buffer, double x);
void catDbl (char* buffer, double x, int width);
Remark: see copyDbl ();
catDMY <cstring.h>
Function: Concatenate day, month and year
Syntax: void catDMY (char* buffer, int dd, int mm, int yy);
Remark: see catDMY ();
catEco
<cstring.h>
Function: Concatenate double number in economics format
Syntax: void catEco (char* buffer, double x);
void catEco (char* buffer, double x, int width);
Remark: see copyEco ();
catField <cstring.h>

Function: Concatenate a field to a string
Syntax: void catField (char* buffer, char* field, int width, int margin = RIGHT);
Remark: see copyField
catHMS
Function: Concatenate hour, minute, second
Syntax: void catHMS (char* buffer, int hh, int mm, int ss);
Remark: see catHMS ();
catInt
<cstring.h>
Function: Concatenate integer number into string
Syntax: void catInt (char* buffer, int x);
void catInt (char* buffer, int x, int width);
Remark: see copyInt ();
copyDble<cstring.h>
Function: Convert a double number into a string
Syntax: void copyDbl (char* buffer, double x);
void copyDbl (char* buffer, double x, double width);
Purpose: $\mathbf{x}$ will be converted into a string. In the second version, buffer will have the length width.
copyDMY <cstring.h>

Function: Convert day, month and year into a string
Syntax: void copyDMY (char* buffer, int dd, int mm, int yy =-1);
Purpose: Format of buffer will be: 12.07 .84 or 12.07 .1984 (if $\mathrm{yy}>0$ ) or 12.07 . (if $\mathrm{yy}<$ 0 ). $d d$ is the day, $m m$ the month (1.. 12) and $y y$ the year.
copyEco
Function: Convert a double number into economics format
Syntax: void copyEco (char* buffer, double x); void copyEco (char* buffer, double x, int width);

Purpose: $\quad \mathbf{x}$ will be converted into an economics format like $2.356,75$. In the second version, buffer will have the length width.

## copyField

<cstring.h>
Function: Copy a field into a string
Syntax: void copyField (char* buffer, char* field, int width, int margin = RIGHT);
Purpose: Copy field into buffer in a field of width bytes. The alignment will be either to the right margin ( margin $=$ RIGHT) or to the left ( margin $=$ LEFT)

## copyHex

<cstring.h>
Function: Copy hexadecimal umber into a string
Syntax: void copyHex (char* buffer, unsigned short $x$ );
Purpose: $\quad x$ will be converted into a string of the form 0x0A1E
copyHMS
<cstring.h>
Function: Convert hour, minute and second into a string
Syntax: void copyHMS (char* buffer, int hh, int mm, int ss = 60);
Purpose: Format of buffer will be: 07:12:42 (if ss $<60$ ) or 07:12 (if ss $==60$ ). $h h$ is the hour, $m m$ the minute and $s s$ the seconds.
copyInt
<cstring.h>
Function: Convert an integer into a string
Syntax: void copyInt (char* buffer, int x); void copyInt (char* buffer, int $x$, int width);

Purpose: $\quad \mathbf{x}$ will be converted into a string. In the second version, buffer will have the length width.
decodeString <cstring.h>

Function: Decoding a string from a file
Syntax: void decodeString (char* aString);
Purpose: Removing special characters for 'New Line', 'Space' and 'NULL'.
getDbl
<cstring.h>
Function: Convert a string into a double
Syntax: BOOL getDbl (char* buffer, double\& x);
Purpose: The function returns the converted x as output.
Return: ERROR if a format error occurred, otherwise OK
getInt <cstring.h>
Function: Convert a string into an integer
Syntax: BOOL getInt (char* buffer, int\& x );
Purpose: The function returns the converted x as output.
Return: ERROR if a format error occurred, otherwise OK

Function: Copy month and year into a string
Syntax: void getMonthAndYear (char* buffer, int month, int year);
Purpose: Copy int buffer "January 1994" depending on month and year.
getString <cstring.h>
Function: Get a string from a stream
Syntax: void getString (istream\& instr, char* aString);
Purpose: Copy next string of instr into aString (until 'Space' of New Line') Special characters for New Line' and 'Space' will be removed in aString. So not the NULL- character (char NULLSTRING). If $* a S t r i n g==$ NULLSTRING the actual string in the stream was NULL:
place
<cstring.h>
Function: Insertion of a string into another
Syntax: void place (char* buffer, char* text, int row, int col);
void place (char* buffer, double x , int row, int col, int width);
Purpose: Insertion of text into buffer in row number row, starting at column number col. The routine will fill in ' n ' and ' ' where necessary. The second version places a double number in a field of length width.
replace
<cstring.h>
Function: replace a character in a string by another
Syntax: void replace (char* buffer, char a, char b);
Purpose: Bytes in buffer that are equal to $a$ will be replaced by $b$.
splitDMY
<cstring.h>
Function: Conversion of a string into day, month and year
Syntax: void splitDMY (char* buffer, int\& day, int\& month, int\& year);
Purpose: Given buffer as input, the routine return day, month and year as output

## strToLower

<cstring.h>
Function: Convert string into lower case
Syntax: void strToLower (char* string);

Function: Convert string into upper case
Syntax: void strToUpper (char* string);
<linalg.cpp>
Linear Algebra
comp_inv
<mathfunc.h>
Function: calculates the inverse matrix
Syntax: BOOL comp_inv (MATRIX\& A);
Return: ERROR, if A singular; otherwise OK.

## det

 <mathfunc.h>Function: calculate the determinant of a matrix A
Syntax: double det (MATRIX\& A);
Remark: Algorithm by [33], p. 49
lineqsol <mathfunc.h>
Function: Solve the linear matrix equation $\mathbf{A x}=\mathbf{b}$
Syntax: BOOL lineqsol (MATRIX\& A, VECTOR\& $x$, VECTOR\& $b$ );
Return: ERROR, if equation cannot be solved. Otherwise OK.
luback <mathfunc.h>
Function: Back substitution
Syntax: BOOL ludecomp (MATRIX\& A, IVECTOR\& index, double* d);
Purpose: Successive calculation of the coefficients in the linear system. This function is used in lineqsol.
Return: ERROR, if matrix singular.
Remark: Algorithm by [33], p. 47
ludecomp
<mathfunc.h>
Function: L-U- decomposition of a matrix
Syntax: BOOL (MATRIX\& A, IVECTOR\& index, double* d);
Purpose: The given matrix A is replaced by its LU- decomposition. index is an output vector that record the row permutation effected by the partial pivoting. $d$ is an output as $\pm 1$ depending on whether the number of row interchanges was even or
odd. The routine is used in combination with luback to solve linear equations.
Return: • ERROR, if matrix singular.
Remark: Algorithm see [33], p. 46
<mathfunc.cpp>
Mathematical Functions
beta
<mathfunc.h>
Function: evaluates the first derivative of the unnormalized, incomplete Beta- function
Syntax: double beta (double $\alpha$, double $\beta$, double x );
Purpose: beta $(\alpha, \beta, x)=x^{\alpha-1}(1-x)^{\beta-1}$
Remark: Algorithm by [33], p. 226ff.
Beta
<mathfunc.h>
Function: evaluates the Beta- function
Syntax: double Beta (double x, double y);
double Beta (double $\alpha$, double $\beta$, double $x$ );
Purpose: The first version calculates the Beta- function, $B(\alpha, \beta)$. The second calculates the normalized, incomplete Beta- function $\mathrm{I}(\alpha, \beta, x)$
Remark: Algorithm by [33], p. 226ff.
bino <mathfunc.h>
Function: calculates the binomial coefficient ( $\left(\begin{array}{l}\text { 足 }\end{array}\right)$
Syntax: double bino (double n, double k);

## Bnp

<mathfunc.h>
Function: calculates the distribution function of the binomial distribution $B(n, p)$ at point $k$ Syntax: double Bnp (double n, double p, double k);

Purpose: $\quad \operatorname{Bnp}(n, p, k)=\sum\left({ }_{j}^{n}\right) p^{j}(1-p)^{n-j}(j=0 . . k)$
Remark: Algorithm by [33], p. 229
cot
<mathfunc.h>

Function: berechnet $\cot (x)$
Syntax: double cot(double $x$ );

## cube

<mathfunc.h>
Function: cubic function $\mathrm{x}^{3}$
Syntax: double cube (double $x$ );
erf
<mathfunc.h>
Function: calculates the error function $\operatorname{erf}(\mathbf{x})$
Syntax: double erf (double x);
Remark: Algorithm by [33], p. 220
erfc
<mathfunc.h>
Function: calculates the complementary error function erfc( $x$ )
Syntax: double erfc (double $x$ );
Remark: Algorithm by [33], p. 220
fact
<mathfunc.h>

Function: calculate the faculty n !
Syntax: double fact (double n);
Remark: Algorithm by [33], p. 215
Gamma
<mathfunc.h>
Function: calculate the Gamma function $\Gamma(x)$
Syntax: double Gamma (double x);
double Gamma (double a, double x );
Purpose: The first version calcualtes the Gamma function $\Gamma(x)$. The second calculates the normalised, incomplete Gamma function $\gamma(\alpha, x)=\gamma(\alpha, x) / \Gamma(\alpha)$.
Remark: Algorithm by [33], p. 213ff

## isinterval

<mathfunc.h>
Function: Interval test
Syntax: int isinterval (double x, double a, double b);
int isinterval (int $x$, int $a$, int $b$ );
Return: YES, if $x \in[a, b]$; else NO
Ingamma
<mathfunc.h>
Function: calculates the logarithm of the gamma function $\ln (\Gamma(x))$
Syntax: double Ingamma (double $x$ );
Purpose: This function is incorporated in the function Gamma to calculate the gamma

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| :--- | :--- | ---: |
|  | function. <br> Remark: <br> Algórithm by [33], p. 214 |  |
| phi |  | <mathfunc.h> |

Function: calculates the first derivative of the normal distribution, $\partial_{\mathrm{x}}\left[\phi\left((\mathrm{x}-\mathrm{a}) / \sigma^{2}\right)\right]$ with mean a and standard variation $\sigma$
Syntax: double phi (double x, double a, double var);
double phi (double $x$, double a, double $\sigma^{2}$, double $x(0)$, double $r$ );
Purpose: The first version calculates the function as stated above. The second version is the density function $f(X(t) \mid X(0)=x(0)$ ) of a conditional normal distribution with correlation coefficient r. (Equation 4.1)

PHI
<mathfunc.h>
Function: Calculate the normal distribution
Syntax: double PHI (double x);
double PHI (double x, double a, double var);
double PHI (double $x$, double a, double $\sigma^{2}$, double $x(0)$, double $r$ );
Purpose: PHI ( $x$ ) calculates the standard normal distribution. PHI ( $x, a, v a r$ ) calculates the normal distribution with mean a and variance var. PHI ( $\left.\mathrm{x}, \mathrm{a}, \mathrm{\sigma}^{2}, \mathrm{x}(0), \mathrm{r}\right)$ calculates the distribution function $F(x \mid X(0)=x(0))$ of a conditional distribution with correlation coefficient r. (Equation 4.2).
Remark: The function uses the functin Gamma (compare discussion of relationship between error function and $\Gamma$ - function in [33], p.220)

SIGN
<mathfunc.h>
Function: Signum- Function
Syntax: $\quad$ SIGN(x)
Return: -1 or 1
sqr
<mathfunc.h>
Function: Square function $\mathrm{x}^{2}$
Syntax: T sqr (Tx);
SWAP

Function: Swap two arguments
Syntax: void SWAP (double\& a,double\& b);
void SWAP (int\& a , int\& b );

Function: Data export to Word Perfect Presentation
Syntax: . BOOL exportData ( VECTOR\& data, char* fileName, int mode);
Purpose: The components of vector data are written to file fileName. Depending on mode data are appended to the file (mode $=$ ATTACH) or existing data in the file are overwritten with the new data (mode $=$ NEW). If the file does not exist the mode NEW is assumed.
Return: Return value is ERROR if specified file could not be opened. Otherwise OK.

### 7.5 Listings

### 7.5.1 Header Files

### 7.5.1.1 <boolwin.h>

```
/**************************************************************************/
/*** MOCulez BOOLTIN.B ***/
/***
    ***/
/*** consists of basic type deciarations and constants ***/
```


*ifndef BOOLWIN HEADER
\#define BOOLWIN_HEADER
\#include <windows.h>



## tendif

| /*** End of BooLwIN. |  |  |  |
| :---: | :---: | :---: | :---: |
|  |  |  |  |

### 7.5.1.2 <estring.h>

```
/***************************************************************************/
/*** ***/
/*** Module: CSTRING.H ***/
/***
/***************************************************************************/
#ifndef cstring mEADER
#define CSTRING_HEADER
#ifndef BOOLWIN HEADER
finclude <boolwin.h>
#endif
#include <iostream.h>
```



```
#define MAXSTRING }9
#define MAXTEXT 200
#define normString 40
```

\#define EMPTYSTRING '炎’ // Character No. 178
\#define sPACE $\quad$ ' $\ddagger$ ' // Character No. 157
\#define NULLSTRING $\quad \cdot \boldsymbol{A}, ~ / /$ Character No. 185
\#define NEW LINE ' $\quad$ ' // Character No. 220
\#define NEWPAGE
F' // Character No. 215

\#endif


### 7.5.1.3 <diffcalc.h>



```
#endif
#ifnder bOOLWIN HEADER
#include <boolwin.h>
#endif
/*** Type declarations *****************************************************/
typedef enum {
                    DETECT_EQUI,// determine search direction. Search at equidistant
points.
                    DETECT DYNA,// Search with dynamically increasing step width
                        DOWN_EQUUI, // search along points smaller than x0
                                DOWN-DYNA,
                                UP_EQ\UI, // search along points bigger than x0
                UP_DYNA,
} BRACKET_MODE;
typedef enum {
    POL_INT, // polynomial approximation interpolation
    RAT INT, // rational function approximation interpolation
    SPLINE // spline interpolation
} POL_MODE;
typedef enum {
    LIN,
    LOG
} REP_MODS; // representation mode: linear/ log.
/*** structure to store function values ***********************************/
class pairvec {
public :
```



```
};
inline ostream& operator << (ostream& outstr, pairvec& v)
    { return outstr << v.size <<, , << v.x <<, , << v.y; }
inline istream& operator >> (istream& instr, pairvec& v)
    { return instr >> V.size >> V.x >> V.y; }
/***************************************************************************/
/*** Abstract class of an object function **********************************/
/***************************************************************************/
class objfunc {
public:
\begin{tabular}{ll} 
VECTOR & \(x ;\) \\
VECTOR & \(y ;\)
\end{tabular}\(/ / / \bar{y}\)-values
            virtual double eval (double) = 0; // abstract function
/*** Minimization and roots *************************************************/
            BOOL bracketMin (double&, double&, double&, double&,
double&, double&, int ,
            double goldenSection (double, double, double, double,
                double ,double&);
/*** Determination of more than one function value *************************/
    void compEquival (double, double, int );
};
/*** Object function with facilities for Turbo Vision Objects ****************/
class owObjfunc : public objfunc {
    int k;
    int num;
    double d;
```

```
    double xmin;
public: : 
    double getPercentage (, );
    void prepForEquival (double, double, int);
};
fendif
/*** End of diffcalc.h ******************************************************/
```


### 7.5.1.4 <distrib.h>

```
/*************************************************************************************/
/*** ***/
/*** Module: DISTRIB.H ***/
/*** ***/
/*** Type Declarations for objects concerning distributions. ***/
/**t*****************************************t*t****************************/
#ifndef DISTRIB HEADER
#define DISTRIB_HEADER
#ifndef DIFFCALC HEADER
#include <diffcaIc.h>
#endif
#ifndef RANDOM HEADER
#include <randöm.h>
#endif
#ifndef OWPARAM HEADER
#include <owparam.h>
#endif
```

```
define WM MSGOBJTUNC 0x00
```

define WM MSGOBJTUNC 0x00
\#define DEÑSITY P 0x0000
\#define DEÑSITY P 0x0000
\#define DENSITY X 0x0004
\#define DENSITY X 0x0004
\#define DISTRIBÜTION 0x0001
\#define DISTRIBÜTION 0x0001
class TStatusWindow; // forward declaration
class TStatusWindow; // forward declaration
/***************************************************************************/
/*** Abstract class of a discrete distribution
******************/
/***********************************************************************************/
Class DiscretDistribution {
protected :
int classes;
int initM;
public:
DiscretDistribution ( int n ) : classes (n) { ; }
virtual %DiscretDistribution ( ) { ; }
virtual int setUp ( TStatusWindow*, Param* )=0;
virtual double gnm (int, int )}=0\mathrm{ ;
virtual double Gn ( int n ) { return 1; }
virtual void setM (intm) { initm=m; }
virtual int getN (double )=0;
int getClasses ( ) { return classes; }
};
/*******************************************************************************/
/*** Abstract class of a randomizer for discrete distributions *************/

```

```

class DiscretRandomizer : public uniRand {
protected :
DiscretDistribution* distribution;
public :

```
```

    DiscretRandomizer ( ) : uniRand ( ) { ; }
    virtual -DiscretRandomizer ( );
    virtual int setUp (TStatusWindow*, Param* ) = 0;
    void setM
    double getRandomNumber (
        (int );
    ;
/***************************************************************************/
/** Abstract class of a continuous distribution ******************/
/***************************************************************************/
class ContinuousDistribution {
protected :
double initVal;
public:
ContinuousDistribution ( ) { ; }
virtual ContinuousDistribution ( ) { ; }
virtual int setup (TStatusWindow*, Param* ) = 0;

```

```

};
/**************************************************************************/
/*** class statfunc *************************/

```

```

class statfunc : public owobjfunc {
double lastp;
double lastResult;
protected :
int type; // = 1 : distribution , = 0 : density
ContinuousDistribution* distribution;
public :
statfunc
virtual
double
virtual int
void
};

```


```

/*** class msgObjfunc *************************/
/********************************************************************************/
class msgObjfunc : public objfunc {
int permitTime;
int permitvalue;
HWND handle;
public:
msgObjfunc ( ) : permitTime (0), permitvalue (0) { ; }
void enableTimeMsg ( ) { permitTime = 1 ; }
void enablevalueMsg
void setHandle
(HWND aHandle) { permitValue = = 1; ; }
virtual double eval (double); (e) { handle m aHandle; }
virtual double eval (double);
virtual double Eval (double) = 0;
};

```

\section*{\#endif}
```

/*** End of distrib.h *****************************************************/

```

\subsection*{7.5.1.5 <error.h>}
```

/*****************************************************************************/
/*** MODUL : ERROR.H
***/
/*** ***/
/******************************************************************************/

```
```

\#ifndef ERROR HEADER
\#define ERROR_HEADER

```
/*** Declarations of global functions ***********************************/
void error_message (const char far* message, const chax far* modul);

\section*{\#endif}
```

/*** End Of ERROR.H *********************************************************/

```

\subsection*{7.5.1.6 <joint.h>}
```

/***************************************************************************/
/*** ***/
/*** Module: JOINT.H ***/
***/
/*** Ieader for joint power related objects ***/
/***************************************************************************/

```
\#ifnder JOINT HEADER
\#define JOINT_HEADER
*ifndef DISTRIB HEADER
(include <distrib.h>
tendif
\#ifndef WIND_HEADER
include <wind.h>
\#endif
fifndef SOLAR HEADER
\#include <solär.h>
\#endif

/*** Class ProbJointPower \(\quad * * * /\)

class ProbJointPower : public owobjfunc \(\{\)
    ContCondWindPower* windPower;
    ContCondSolApprox* solarPower;
    int num;
    VECTOR Gpw;
    VECTOR Gps;
    double gpw (int);
    double gps (int);
public :
    ProbJointPower (int \(n\) );
    virtual ProbJointPower ( );
    double eval ( double );
    int setup ( IStatusWindow*,Param*);
\};
\#endif


\subsection*{7.5.1.7 <mathfunc.h>}

```

/***Module\& MATHFUNC.B b ***/
***
***/
/*** consists of definitions and prototypes for mathematical functions ***/
/\#*t consists of definitions and prototypes for mathematical functions *t*//

```

\section*{*ifndef MATHFUNC header \\ *define MATHFUNC-hEADER \\ ifndef VECTORS_HEADER \\ *include <vector̄a.h> \\ \#endif \\ fifndef BOOLWIN HEADER \\ \#include <boolwin.h> \\ \#endif}
/**************************************************************************/
/*** Utility functions ***/
/************************************************************************/
void SWAP (double \&a, double \&b);
Void SWAP (int sa, int \&b);

BOOL isinterval (double \(x\), double \(a\), double b);
BOOL isinterval (int \(x\), int a int b);





Cumulative Bin. distribution
double cube (double x)
double erf (double); // erf(x)
double erfc (double); \(/ / \operatorname{erfc}(x)\)
double fact (double); // factorial
double Gamma (double); // gamma function
double Gamma (double, double ); // Incomplete gamma function
double
max (double, double);
\(\begin{array}{ll}\text { double min } & \text { (double, double); } \\ \text { double } & \text { phi }\end{array} \quad\) (double, double, double);
double phi (double, double, double, double, double); // cond; phi(x)
double PBI (double); //PBI(x)
double PHI (double, double, double); \(/ / \mathrm{phi}(\mathrm{x})\)
double PBI (double, double, double, double, double); // cond. Phi (x)
\begin{tabular}{ll} 
double \\
double & SIGN
\end{tabular}\(\quad\)\begin{tabular}{l} 
(double); \\
(double \(x\) );
\end{tabular}
\begin{tabular}{ll} 
double SIGN & (double X); \\
double & sqr
\end{tabular}

BOOL comp_inv (MATRIX\&); // Inverse
double det (MATRIX\&); //determinant
BOOL Iineqsol (MATRIX, VECTOR\&, VECTOR ); //Linear equation solver
BOOL Iudecomp (MATRIX\&, IVECTOR\&, double*); //LU- decomposition
void luback (MATRIX\&, IVECTOR\&, double*); //Backsubstitution
\#endif
/*** End of MATEFUNC.CPP ************************************************/

\subsection*{7.5.1.8 <owcalc.h>}
```

/******************************************************************************/
/*** Module: OWCALC.H ***/
/******************************************************************************/
/******************************************************************************)
/*** Object Windows C++: Calculations in the Windows inherited from ***/
/*** either TStatusWindow or TMuliValobject
***/
/*************************************************************************/

```
\#ifndef OWCALC HEADER
\# define OWCALC_HEADER
\#ifndef OWSTAT HEADER
\#include <owstät.h>
Fendif
\#ifndef WIND HEADER
finclude <wind.h>
tendif
*ifndef solar header
\#include <solar.h>
*endif
\#ifndef JOINT EEADER
\#include <joint.h>
\#endif
Fifndef RANDOM HEADER
\#include <random.h>
\#endif
\#ifndef SERTES HEADER
Finclude <seriës.h>
*ndif
\#ifndef PASSAGE HEADER
\#include <passaḡe.h>
fendif

CLASSDEF (TWindSpeedObject)
class TWindspeedobject : public TMultiValobject \{
private :
SpeedDens* f;
SpeedDist* F ;
int workOutBasic ( );
int workoutValues ();
int areParameterok ( );
void setoldparameter ();
public :
TWindSpeedObject (PTWindowsObject AParent, LPSTR ATitle);
virtual TWindSpeedObject ( ):
\};

CLASSDEF (TDistributionObject)
̄̄ass TDistributionObject : public TMultivalobject \{
private :
statfunc* distribution;
int workOutBasic ()
int workoutvalues ();
int areParameterok ();
void setoldParameter ();
public :
TDistributionObject (PTWindowsObject AParent, LPSTR ATitle);
virtual TTDistributionObject ();
\};

CLASSDEF (TJointDistributionObject)
class TJOintDistributionobject : public TMultiValobject \{
private :
ProbJointPower* jointPower;
int workOutBasic ();
int workOutValues ( );
int areparameterok ();
void setoldparameter ();
public :
TJointDistributionobject (PTWindowsObject AParent, LPSTR ATitle);
virtual "TJointDistributionObject ( );
\};
```

/*** TRandomObject ***********************************************************/
CLASSDEF (TRandomObject)
Class TRandomObject : public TStatusWindow {
KgSTest* kgSTest;
double test;
protected :
int workOut ( );
void writeRepl ( );
public:
TRandomobject (PTWindowsObject AParent, IPSTR ATitle);
virtual -TRandomObject ( );
};

```

_CLASSDEF (TTimeSeriesObject)
\(\bar{c}\) lass TTimeSeriesObject : public TMultivalobject \(\{\)
private:
    TimeSeries* timeSeries;
    int workOutBasic ();
    int workoutValues ();
    int areParameterok ();
    void setoldParameter ();
public :
        TrimeSeriesObject (PTWindowsObject AParent, LPSTR ATitle);
        virtual \(\sim_{\text {TTimeSeriesObject ( ) }}\)
\};

CLASSDEF (TPassageTimeObject)
Class TPassageTimeObject : public TStatusWindow \{
        passagetime* passagetime;
        double
            time;
protected :
        int workout ();
        void writerepl ();
public:
        TPassageTimeObject (PTWindowsObject AParent, LPSTR ATitle);
        virtual "TPassageTimeObject ( );
\};

    CLASSDEF (PassageTimesObject)
Class PassageTimesObject : public TMultiValobject \{
private :
    PassageTimes* passageTines;
        int workoutBasic ();
        int workoutValues ();
        int areparameterok ();
        void setoldParameter ();
public:
    PassagerimesObject (PTWindowsObject AParent, LPSTR ATitle);
    virtual "PassageTimesobject ( );
\};
\#endif


\subsection*{7.5.1.9 <owdialg.h>}
```

|***********t*************************************************************/
/*** Module: OFDIALG.B ***/
/*************************************************************************/

```
\begin{tabular}{|c|c|c|c|c|}
\hline \multicolumn{5}{|l|}{/*** Header for <owdialg.cpp> defines the dialog windows objects for ***/} \\
\hline \multicolumn{5}{|l|}{\multirow[t]{2}{*}{/*** this programme. All dialog wincows relate to Object Windows C++ ***/}} \\
\hline & & & & \\
\hline \multicolumn{5}{|l|}{/***} \\
\hline /*** & class TTransSettingsDlg & Settings Dialog: & Data & ***/ \\
\hline /*** & class TSettingsDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class TTransSpeedDlg & Wind speed Dialog: & Data & ***/ \\
\hline /*** & class TSpeedDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class TTransDirdig & Directories Dialog: & Data & ***/ \\
\hline /*** & class TDirdialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class TTransWindDlg & Wind Power Dialog: & Data & ***/ \\
\hline /*** & class TWindDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class TTransExportDlg & Export Data Dialog: & Data & ***/ \\
\hline /*** & class TExportdialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class TTransDisplayDlg & Display Options: & Data & ***/ \\
\hline 1*** & class TDisplayDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline 1*** & class TTransSolardlg & Solar Power Dialog: & Data & ***/ \\
\hline /*** & class TSolarDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class trransJointDlg & Joint Renewables: & Data & ***/ \\
\hline /*** & class TJointDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class TRandDialog & Random Numbers. & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** Window ***/} \\
\hline /*** & class TTransMathsDlg & Maths & Data & ***/ \\
\hline /*** & class TMathsDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** W**/} \\
\hline /*** & Class ITransTsDlg & Time series: & Data & ***/ \\
\hline /*** & class TTsDialog & & Window & ***/ \\
\hline \multicolumn{5}{|l|}{/*** ***/} \\
\hline /*** & class TTransFpDlg & First passage time: & Data & ***/ \\
\hline \multicolumn{5}{|l|}{\multirow[b]{2}{*}{/*** ***/}} \\
\hline & & & & \\
\hline /*** & *********************** & ******************* & *********** & ***/ \\
\hline
\end{tabular}
```

\#ifndef OWDIALG HEADER
\#define OWDIALG_HEADER
\#ifndef OMRES HEADER
\#include "owres.h"
\#endif
\#ifndef OWLAPPL HEADER
\#include "owlapp̄1.h"
\#endif
\#include <owl.h>
\#include <dialog.h>
\#include <iostream.h>
finclude <edit.h>
\#include <string.h>
\#include <radiobut.h>
/*** Settings Window ****************************************************************)
CLASSDEF (TSettingsDialog)
Class TSettingeDialog : public TDialog {
public :
TSettingsDialog (PTWindowsObject AParent, LPSTR ATitle);
};
class TTransSettingsDlg
public :
TTransSettingsDlg ( );
double wiVci; // cut-in wind speed

```
```

    double wiVco; // cut-out wind speed
    double wiVr; // rated wind speed
    double wiVmean; // mean wind speed
    double wiSigma; // standard variation of wind turbulence
    double wiBeta; // autocorrelation coefficient (wind)
    double solk0; // maximum clearness index
    double solk; // average hourly clearness index
    double solsigmak;// standard deviation of clearness index
    double solBeta; // autocorrealtion coefficient (solar)
    double comZeta; // fractional power factor
    couble batK; // Battery parameters
    double batc;
    double batQMax;
    double batV;
    double sysPRen; // Nominal renewable energy
    double sysPDemand; // Power Demand
    void setParameter ( );
    friend ostream& operator << (ostream&, TTransSettingsDlg&);
    friend istream& operator >> (istream&, TTransSettingsDlg&);
    };

```
/*** Wind Speed Dialog *************************************************/
CLASSDEF (TSpeedDialog)
Class TSpeodDialog : public TDialog \{
public:
    TSpeedDialog (PTWindowsObject AParent, LPSTR ATitle);
\};
Class TTransSpeedDIg \{
public:
    TTransSpeedDlg ( );
    WORD OpProb; //Flag: probability density function
    WORD opDist; // Flag: Distribution function
    double vmean; // mean wind speed
    double vmin; // minimum wind speed (for graph)
    double vmax; // maximum wind speed (for graph)
    int eval; // number of function evaluations
    void setparameter ();
    friend ostream\& operator << (ostream\&, TTransSpeedDlg\&);
    friend istream\& operator >> (istream\&, TTransSpeedDlg\&);
\};
/*** Directories Dialog **********************************************************)
    CLASSDEF (TDirDialog)
Class TDirDialog : public TDialog \(\{\)
public:
    TDirDialog (PTWindowsObject AParent, IPSTR ATitle);
\};
class TTransDirDlg \(\{\)
public:
    TTransDirDlg ( )
    char solpile[50]; // file name for solar data
    char dlgFile[50]; // file name for dialog data
    friend ostream\& operator << (ostream\&, TTransDirDlg\&);
    friend istream\& operator >> (istream\&, TTransDirDlg\&);
\};

    CLASSDEF (TWindDialog)
Class TWindDialog : public TDialog \(\{\)
    pTStatic textTau;
    prstatic textInitialv;
    PTDoubleInputI inTau;
    PTDoubleInputI inrnitialv;
    PTRadioButton radiocond;
    char buftaut 30\(]\);
    char bufInitialv́(30]:
public :
    TWindDialog (PTWindowsobject AParent, LPSTR ATitle);
    virtual void WMInitDialog (RTMessage) \(=\) [WM_FIRST+WM_INITDIALOG];
```

    virtual void BandleCondMsg (RTMessage) = [ID_PIRST + idopCond];
    virtual void HandleStatMsg (RTMessage) = [ID_FIRST + idOpStationary];
    };
class TTransWindDlg {
public :
TTransWindDlg ( );
WORD OpProb; // Flag: probability density function
WORD OpDist; // Flag: distribution function
WORD opStationary; // Flag: stationary process
WORD OpCond; // Flag: Conditional function
double vmean; // mean wind speed
int eval; // number of evaluations
double tau; // time tau
double initialv; // initial wind speed
void setParameter ();
friend ostream\& operator << (ostream\&, mTransWindDlg\&);
friend istream\& operator >> (istream\&, TTransWindDlg\&);
};
/*** Export Dialog **************************************************************)
CLASSDEF (TExportDialog)
class TExportDialog : public TDialog {
public:
TExportDialog (PTWindowsObject AParent, LPSTR ATitle);
};
class TTransExportDlg {
public:
TTransExportDlg ( );
WORD OpNew; // Flag: new file
WORD OpAttach; // Flag: attach to existing file
char expFile[501; // File name: Export file
void setparameter ();
friend ostream\& Operator << (Ostream\&, TTransExportDlg\&);
friend istream\& operator >> (istream\&, TTransExportDlg\&);
};
/*** Display Dialog *******************************************************/
CLASSDEF (TDisplayDialog)
class TDisplayDialog : public TDialog {
public:
TDisplayDialog (PTWindowsObject AParent, IPSTR ATitle);
};
class TTransDisplayDlg {
public:
TTransDisplayDlg ( );
WORD OpAuto; // Flag: Auto display of graphics
WORD OpAccu; // Flag: Accumulating data series
WORD opLegend;
void setParameter ();
friend ostream\& operator << (ostream\&, TTramsDisplayDlg\&);
friend istream\& operator >> (istream\&, TTransDisplayDlg\&);
};
/*** Solar Dialog **********************************************************/
CCASSDEF (TSOlarDialog)
\overline{class TSolarDialog : public TDialog {}}
PTDoubleInputI inTau;
PTDoubleInputI inInitialk;
PTIntegerInputI inTrial;
PTIntegerInputI incoeff;
pTCheckBox checkBypass;
PTStatic textTau;
PrStatic textInitialk;
prstatic textTrial;
PTStatic textcoeff;
prRadioButton radioAnalyt;
PTRadioButton radioApprox;
PTRadioButton radiocond;
PTRadioButton radioQual;

```
```

char buftau[30];
char bufinitialk[30];
char buftrial[30];
char bufCoeff[30];
void enableApprox ( );
void disableApprox ( );
void enablecond (;)
void disableCond ( );
protected :
virtual void WMInitDialog (RTMessage) = [WM_FIRST + WM_INITDIALOG];
virtual void HandleAnalytMgg (RTMessage) = [ID_FIRST + idOpAnalyt 1;
virtual void HandleApproxMsg (RTMessage) = [ID_PIRST + idOpApprox ];
virtual void HandleCondMsg (RTMessage) = [ID'FIRST + idopCond 1;
virtual void HandlequalMsg (RTMessage) = [ID_FIRST + idopqual ];
public :
TSolarDialog (PTWindowsObject AParent, LPSTR ATitle);
};
Class TTransSolarDlg {
public:
TTransSolarDIg ( );
WORD OpProb; / // Flag: probability density function
WORD OpDist; // Flag: Distribution function
WORD OpAnalyt; // Falg: Analytical solution
WORD OpApprox; // Flag: Approximation
WORD opCond; // Flag: Conditional function
WORD OpQual; // Flag: Quality
HORD OpBypass; // Flag: Bypass
double clearness; // Clearness index
double sigmak; // Standard variation of clearness index
int eval; // number of function evaluations
double tau; // time tau
double initialk; // intitial clearness index
int trial; // number of trial points
int coeff; // number of coefficients in approximation
void setParameter ();
friend ostream\& operator << (ostream\&, TTransSolarDlg\&);
friend istream\& operator >> (istream\&, TTransSolarDlg\&);
};
/*** Joint Renewable Dialog **************************************************/
CLASSDEF (TJOintDialog)
Class TJointDialog : public TDialog {
prDoubleInputI inTau;
PTDoubleInputI inInitialk;
pTDoubleInputI inInitialv;
PTStatic textTau;
Prstatic textInitialk;
pTStatic textInitialv;
char bufTau[30];
char bufInitialv[30];
char bufInitialk[30];
PTRadioButton radioCond;
void enablecond ();
void disableCond ();
protected :
virtual void WMInitDialog (RTMessage) = [WM FIRST + WM INITDIALOG];
virtual void EandleCondMsg (RTMessage) = [ID_FIRST + idOpCond ];
virtual void EandleProbMsg (RTMessage) = [ID_PIRST + idOpProbDens ];
public :
TJOintDialog (PTWindowsObject AParent, LPSTR ATitle);
};
class TTransJointDlg {
public :
TTransJointDIg ( );
WORD opJointDens;
WORD opJointCond;
double vmean;
double initialv;
double clearness;
double sigmaK;

```
```

    double initialk;
    double tau;
    int eval;
    double zeta;
    void setparameter ( );
    friend ostream& operator << (ostream&, TTransJointDlg&);
    friend istream& operator >> (istream&, TTransJointDlg&);
    };
/*** Random Numbers Dialog ************************************************/
CLASSDEF (TRandDialog)
class TRandDialog : public TDialog
PTStatic ranTextBeta;
PTStatic ranTextA;
PTStatic ranTextB;
pTStatic ranTextBi;
PTStatic ranTextP;
PTStatic ranTextclass;
PTDoubleInputI ranInputA;
PTDoubleInputI ranInputB;
PTDoubleInputI ranInputP;
PTIntegerInputI ranInputciass;
PTRadioButton ranRadiol;
PTRadioButton ranRadio2;
PTRadioButton ranRadio3;
char bufA[30];
char bufB[30];
char bufp[30]:
char bufclass[30];
void EideBeta ();
void UnHideBeta ();
void EideBi ();
void Un\#ideBi ();
void Eideclass ();
void UnHideclass( );
public :
TRandDialog (PTWindowsObject AParent, LPSTR ATitle);
virtual void WMInitDialog (RTMessage) = [WM_FIRST + WM_INITDIALOG];
virtual void HandleUniMgg (RTMessage) m [ID_FIRST + iakanOpol;
virtual void HandleNormMsg (RTMessage) = [ID_FIRST + idRanOp1];
virtual void EandleBetaMsg (RTMessage) = [ID_FIRST + idRanOp2];
virtual void HandleBiMsg (RTMessage) = [ID-FIRST + idRanOp3];
};
class TTransRandD1g {
public :
TTransRandDIg ( );
WORD ranOpO; // Flag: Uniform distribution
WORD ranOp1; // Flag: Normal distribution
WORD ranOp2; // Flag: Beta distribution
WORD ranOp3; // Flag: Binomial distribution
double ranA; // Input parameter: alpha
double ranB; // Input parameter: beta
double ranp; // Input parameter: p(binomial distr.)
int ranclass; // Number of classes in chi囬 test
int ranTrial; // Number of trials in chi⿱⿰习习⿱人从丶从匕年test
void setParameter ();
friend ostream\& Operator << (ostream\&, TTransRandDlg\&);
friend istream\& operator >> (istream\&, TTransRandDlg\&);
};
/*** Maths Dialog ***************************************************************
CLASSDEF (TMathsDialog)
class TMathsDialog : public TDialog {
public :
TMathsDialog (PTWindowsObject AParent, LPSTR ATitle);
};
class TTransMathsDlg {
public :
TTransMathsDlg ( );
int solrrial;

```
```

    int solCoeff;
    int fpTsTrial;
    int fpTsMaxIt;
    double fpMcStopCrit;
    int fpMcMaxIt;
    int fpMcGrid;
    int classes;
    void setParameter ( );
    friend ostream& operator << (ostream&, TTransMathsDIg&);
    friend istream& operator >> (istream&, TrransMathsDIg&);
    };
/*** Time Series Dialog ************************************************/
CLASSDEF (TTsDialog)
Class TTsDialog : public TDialog {
prstatic
tsTextInitV;
PTStatic tsTextInitR;
PTStatic taTextInitQio;
PTStatic tsTextInitQ20;
PTDoubleInputI tsInputInitv;
PTDoubleInputI tsInputInitk;
PTDOubleInputI tsInputInitolo;
PTDOubleInputI tsInputInitQ20;
PrRadioButton tsOpo;
PTRadioButton tsOp1;
ptRadioButton tsOp2;
PTRadioButton tsOp3;
PTRadioButton tsOp4;
PTRadioButton tsops;
char bufInitv[30];
char bufInitK[30];
char bufInitQ10[30];
char bufInitg20[30];
void HideV ();
void UnHidev ();
void Eidek ( );
void UnHideR (j;
void HideQ ();
void UnHideQ ();
public :
TTsDialog (PTWindowsObject AParent, LPSTR ATitle);
virtual void WMInitDialog (RTMessage) = [WM_FIRST + WM INITDIALOG];
virtual void EandleOpOMsg (RTMessage) =[IDFIRST + idFsOpO];
virtual void HandleoplMsg (RTMessage) = [ID_FIRST + idTsOpl];
virtual void Handleop2Msg (RTMessage)=[ID-FIRST + idTsOp2];
virtual void Eandleop3Msg (RTMessage) = [ID_FIRST + idTsOp3];
virtual void Handleop4Msg (RTMessage)=[ID_FIRST + idTsOp4];
virtual void \#andleop5Msg (RTMessage) = [ID_FIRST + idTsOp5];
};
class TTransTsDlg {
public:
TTransTsDIg ( );
WORD tsOpo; // Flag: Wind speed time series
WORD tsop1; // Flag: Wind power time series
WORD tsOp2; // Flag: Solar power time series
WORD tsOp3; // Flag: Combined power time series
WORD tsOp4; // Flag: State of charge
WORD tsOp5; // Flag: Power Deficit
double tsTimeStep;
int tsPoints;
double initV;
double initr;
double initglo;
double initQ20;
void setParameter ( );
friend ostream\& operator << (ostream\&, TTransTsDlg\&);
friend istream\& operator >> (istream\&, TTransTsDIg\&);
};
/*** First Passage Time Problems **********************************************
_CLASSDEF (TFpDialog)

```
```

class TFpDialog : public TDialog {
PTRadioButton fpOpo;
PTRadioButton EpOp1;
PrRadioButton
PTRadiobutton
prradiobutton
PTRadioButton
PTRadioButton
PTRadioButton
PTRadioButton
PTStatic
PTStatic
PTStatic
pTStatic
PTStatic
PTStatic
PTStatic
PTDoubIeInputI
pTDoubleInput
PTDoubIeInputI
PTDoubIeInputI
PTDoubleInput
pTDoubleInputI
PTIntegerInputI
char
char
char
char
char
char
bufPassP[30];
char boid bufNoVal[30];
void Eidevo ();
void UnHidevo ();
void EidekO ();
void UnHidek0 ();
void Gidepo ();
void UnHidepo ();
void HidePassV (
void UnHidepassV
void
void
void
void
void
void
public:
TFpDialog (PTWindowsObject AParent, LPSTR ATitle);
virtual void WMInitDiaiog (RTMessage) = [WM FIRST + WM INITDIALOG];
virtual void EandleOpomsg (RTMessage) =[ID_FIRST + idFpopO];
virtual void HandleOplMsg (RTMessage) = [IDFIRST + idFpOpl];
virtual void HandleOp2Msg (RTMessage) = [ID-FIRST + idFpOp2];
virtual void Eandleop3Msg (RTMeseage) =[ID_PIRST + idFpOp3];
virtual void HandleOp4Msg (RTMessage) = [ID_FIRST + idFpOp4];
virtual void \#andleop5Msg (RTMessage) = [ID_FIRST + idFpop5];
virtual void gandleOp6Msg (RTMessage) = [ID_PIRST + idFpOp6];
virtual void Handleop7Msg (RTMessage) = [ID_FIRST + idFpop7];
virtual void Eandleop8Msg (RTMessage) = [ID_FIRST + idFpOp8];
};
Class TTransFpDlg {
public:
TTransFpDlg ( );
HORD fpOpO;
WORD fpop1; ll/ Flag: Process: Wind Power
WORD fpop1; // Flag: Process: Wind Power
WORD fpOp3; // Flag: Process: Combined Power
WORD fpop4; // Flag: Method: Time series approach
WORD fpops; // Flag: Mehtod: Markov Chain approach
WORD fpOp6;
WORD fpOp7;
WORD fpops; // Flag: as function of passage levels
double initV; // Initial values
RD flopo;

```
```

    double initर;
    double initP;
    double passV; // Passage levels
    double passK;
    double pass?;
    double timeStep;
    int noval;
    void setParameter ( ):
    friend ostream& operator << (ostream&, TTransFpDIg&);
    friend istream& operator >> (istream&, TTransFpDlg&);
    };
fendif
/*** end of owdialg.h ******************************************************/

```

\subsection*{7.5.1.10 <owlappl.h>}
```

/***************************************************************************/
/*** MODUL : OWLAPPL.E 苴 ***/
/*** ***/
/***************************************************************************/ノ

```
\#ifndef OWLAPPL_HEADER
\#define OWLAPRL_HEADER
\#include <windows.h>
\#include <owl.h>
\#include <edit.h>
\#inciude <button.h>
/*** Constants ********************************************************/
\#define idOwlApplText 100
/*** Double Input ****************************************************/
CLASSDEF (TDoubleInput)
Class TDoubleInput : public TEdit \{
    BOOL validInput ( );
public :
    double x;
    TDoubleInput (PTWindowsObject AParent, int ResourceId);
    virtual WORD Transfer (void* Dataptr, WORD Transferflag):
    virtual bool canclose ( ):
\};
/*** Double Input in a specific interval ********************************/
CLASSDEF (TDoubleInputI)
c̄ass TDoubleInputI : public TDoubleInput \(\{\)
    double minval;
    double maxVal;
    char message[50];
public :
    TDoubleInputI (PTWindowsObject AParent, int ResourceId,
            const double aminval, const double aMaxVal, const char* amessage);
    virtual BOOL Canclose ( ):
\};

CLASSDEF (TIntegerInput)
Class TIntegerInput : public TEdit \{
    BOOL validInput ();
public :
    int \(n\);
    TIntegerInput (PTWindowsObject AParent, int ResourceId);
    virtual WORD Transfer (void* Dataptr, WORD Transferflag);
    virtual bOOL Canclose ();
\};
/*** Integer Input in a specific interval *****************************/
```

CLASSDEF (TIntegerInputI)
class TIntegerInputI : public TIntegerInput {
int minval;
int maxVal;
char message[50];
public :
TIntegerInputI (PTWindowsObject AParent, int ResourceId,
const int aMinVal, const int aMaxVal, const char* aMessage);
virtual BOOL CanClose ( ):
};
/*** Message Dialog *******************************************************/
CIASSDEF (TYoMessage)
class TYoMessage : public TDialog {
PTStatic statText;
char buffer[80];
public :
TYOMessage (PTWindowsObject AParent, LPSTR ATitle,char*);
virtual void WMInitDialog (RTMessage) = [WM_PIRST+WM INITDIALOG];
virtual void CMYes (RTMessage) = [ID_FIRST + IDYES];
virtual void CMNO (RTMessage) = [ID_FIRST + IDNO];
virtual void CMIqnore (RTMessage) = [ID FIRST + IDIGNORE];
virtual void cmabort (RTMessage) = [ID_FIRST + IDABORT ];
};
/*** InputDialog ***************************************************************/
CCASSDEF (TYOInput)
Class TYOInput : public TDialog (
PTEdit inputrine;
PTStatic statText;
public :
TYOInput (PTWindowsObject AParent, LPSTR ATitle,
char* title,char* input);
char textBuffer[80];
virtual void WMInitDialog (RTMessage) = [WM_FIRST+WM_INITDIALOG];
};

```
\#endif
/*** End of OWLAPPL. H ****************************************************/

\subsection*{7.5.1.11 <owparam.h>}
```

/******************************************************************************/
/*** Module: OWPARAM.H
***/
/****************************************************************************/
/**************************************************************************/
/*** Header for <owparam.h> defines the parameter structures that ***/
/*** serve as interfaces between windows objects and mathematical ***/
/*** objects.
/*** . N* ***
/*** struct Param Parameter ***/
/*** class Graph Graphic related data ***/
/******************************************************************************/
\#ifndef OWPARAM HEADER
\#define OWPARAM_HEADER
\#ifndef DIFFCALC HEADER
\#include <diffcaIc.h>
\#endif
*include <string.h>

```



```

    double batQ10; / // Q10 + Q20 <= 1.0
    // Denormalized system
    double sysPDemand;
    double sysPRen;
    // Display options
    int disAuto; // automatic re-drawing of graphics
    int disAccu; // accumulate data series when possible
    int disOldEval; // last eval
    int disoldType; // last window type
    double disoldVmin; // last minimum speed
    double disoldVmax; // last maximum speed
    int disFirstCurve; // = 1 if first curve, otherwise 0
    int disLegend; // = 1 if legend desired, otherwise 0
    };

```

```

/*** class Graph ***/
/***************************************************************************/
/*** Graphic related data *************************************************/
Class Graph {
public :
VECTOR x; // x - values
VECTOR Y[4]; // y - values
char legend[4][20]; // Legend for curves
double scale; // scaling factor
int option;
int curveNo; // number of curves in same graph
double min; // minimum on x- axis
double max; // maximum on x- axis
char headline[401;
char subline [50];
char axtext [40];
Graph (): curveNo(4) { ; }
void setHeadline (char* text) { strncpy (headline,text,39); }
void setSubline (char* text) { strncpy (subline ,text,49); }
void setAxtext (char* text) { strncpy (axtext ,text,39); }
};
\#endif
/*** ene of owparam.h *****************************************************/

```

\subsection*{7.5.1.12 <owplot.h>}

```

/*** MODUL : OWPLOT.H ***/
/*** ***/
/***************************************************************************/

```
*ifndef OWPLOT_HEADER
*define OWRLOT_HEADER
\#ifndef VECTORS HEADER
\#include <vectors.h>
*endif
*ifndef DIFFCALC HEADER
Finclude <diffcaIc.h>
\#endif
*include <fstream.h>
\#include <windows.h>
finclude <owl.h>
```

/*** Constants *************************************************************/
\#define TOP 100
\#define BOTTOM 101
\#define NEW 200
\#define ATTACH }20
\#define LIN
\#define PIXEL 0
\#define POLYGON 1
\#define STEP 2
\#ciefine DIRAC 3
fdefine IN AXLE 0
\de£ine OUT AXIR 1
\#define CENTER_AXIE 2
\#define TO_HORIZONTAS O
*define TO_VERTICAL 1
typedef unsigned int DRA MODE;
typedef unsigned int AXLE_MODE;
class axis;
/*** class TGraph ********************************************************/
CLASSDEF (TGraph)
Class TGraph : public TWindow {
protected :
LOGFONT logFont; // Font
HFONT TheFont;
HFONT oldFont;
LOGPEN logPen; // Pen
HPEN ThePen;
HPEN oldPen;
LOGERUSE logBrush; // Brush
HBRUSH TheBrush;
EBRUSH OldBrush;
COLORREF backGround; // Background Color
HDC DC;
public :
TGraph (PrWindowsObject AParent, LPSTR ATitle, PTModule AModule m NULL);
void clearScreen (int );
void setTextHeight (int n );
void setPensize (int n );

```

```

    void setPenColor (COLORREF COIOr);
    void setBrushColor (COLORREF color);
    void setBrushHatch (int n (coLORREP color);
    virtual void open ()
    virtual void close (int x1, int y1, int)
    Line (int x1, int y1, int x2, int y2 );
    void Doubleout (double number, int dec, int }x\mathrm{ , int }y\mathrm{ );
    void Integerort (int number, int x, int }Y\mathrm{ ()
    void Textout (char* text, int x, int y );
    };
/*** class TPlot *********************************F**********************/
CLAASSDEF (TPIOt)
class TPlot : public TGraph {
char headLine[50];
char subLine[60];
int curveNO; // curve number
double xquotlin, yquotlin, xquotlog, yquotlog;
int xlog, ylog;
double x min,x max,y_min,y_max;
axis* xbottom;
axis* xtop;
axis* yleft;

```
```

    axis* yright;
    RECT maxRect;
    protected :
RECT
public :
TPlot
TMlot (PTW.
virtual void plot ( ) { ; }
virtual void draw ();
virtual void Paint (EDC PaintDC, PAINTSTRUCT _PAR\& PaintInfo);
void setHeadrine (const char*);
void setSubLine (const char*);
void plotFactor (double factor);
protected :
void plotHeadLine ( );
void plotSubLine ();
void drawMargin ();
int xcoord (double x);
int ycoord (double x);
void . setCoordinates (double xmini,double xmaxi,double ymini,
double ymaxi);
double setAutoCoord (double xmini, double xmaxi, VECTOR* yval, int n=0);
void setAutoAxAttr (double\&,double\&,int\&,int\&,double\&,double\&);
void
drawUpperx
(int,int,int,int);
(double mini,double maxi,double axle,int num,
int log, const char* text,int axle mode);
void drawRighty
(double mini,double maxi,double axle,int num,
int log, const char* text,int axle mode);
void drawLowerx (double mini,double maxi, double axle,int num,
int log, int grid, double dist,const char* text,int axle_mode);
drawLefty (double mini,double maxi, double axle,int nüm,
int log, int grid, double dist,const char* text,int axle_mode);
void drawlincoord (double xaxle,int xnum,int xgrid,double xgriddist,
const char* xtext,double yaxle,int ynum,int ygrid,double
ygriddist, const char* ytext);
void drawLinCoord (int, const char*, int, const char*);
double drawAutoLinCoord (double xmini, double xmaxi, VECTOR* yval,
const char* xtext, const char* ytext, int xaxgrid, int yaxgrid,
double scale, int n=0);
void drawCurve (VECTOR\&,VECTOR\&, DRA_MODE draw_mode);
};
class axis { // Structure for description of an axis
int direction;// horizontal or vertical
int textjust; // text justification
int axle_mode;
int centercord;// central coordinate
int grid; // Grid ?
double min; // Minimam
double max; // Maximum
char text[501; // Axis text
double axle; // Distance between axles
int num; // draw numbers every num-th axle
double griddist; // grid distance for linear representation
int innlog; // linear or logarithmic representation
void logarith (int, int, const char*);
public:
RECT* curRect;
HDC DC;
axis (BDC aDC, RECT* aCurRect) { DC = aDC; curRect = aCurRect;}
void setAxis (int dir, int just, int cord, double mini, double maxi,
const char*
alpha,double ax,int n,int axlog,int axgrid,
mode);
void drawAxis (void);
};
/*** Function prototypes ***************************************************/
BOOL exportData (VECTOR\&, char*, int, char*, double);

```
\#endif
```

/*** End of OWPLOT.E *******************************************************/

```

\subsection*{7.5.1.13 <owrenew.h>}
```

/****************************************************************************/
/*** Module: OWRENEM.H
***/
/***************************************************************************/
/*****************************************************************************/
/*** Header of the main programme ***/
/*** ***/
/*** Definitions and declarations of: ***/
/*** class TRenewPlot (plot window) ***/
/*** class TMainWindow ***/
/*** class TRenewApp (application ***/
/*************************************************************************/

```

\section*{\#ifndef OWRENEW HEADER}
fdefine OWRENEW_HEADER
\#ifndef OWRES HEADER
include "owrēs.h"
Fendif
\#ifndef OWPLOT HEADER
\#include "owplōt.h"
\#endif
*ifndef OWLAPPL_HEADER
tinclude "owlapp̄I.h"
tendif
*ifndef owdialg header
\#include <owdiaIg.h>
*endif
\#include <owl.h>
tinclude <dialog.h>
finclude <iostream.h>
\#include <edit.h>
*include <string.h>
\#include <radiobut, h>
/*** Graphics Window **************************************************/
CLASSDEF (TRenewPlot)
c̄ass TRenewPlot : public TPlot \(\{\)
    int delta;
    int start;
    int end;
    HBRUSH brushPen,oBrushPen;
public :
    int clear;
        TRenewPlot (PTWindowsobject AParent, LPSTR ATitle, PTModule AModule \(=\) NULL);
    virtual void Paint (BDC PaintDC, PAINTSTRUCT FAR\& PaintInfo);
    void plot. ( );
\};
/*** Main Window ******************************************************/
CLASSDEF (TMainWindow)
class TMainWindow : public TWindow \{
    void calc (owobjfunc*, double, double);
public:
    TrransSettingsDlg TransSettingaDlg;
    TrransDirDlg
    TTransExportDlg
    TrransDisplaydig
    TTransSpeedDlg
    TTransWindDIg
    TTransSolardig
        Transsirdig;
        TransExportDlg;
        Transexportdig;
        TransSpeedDlg;
        TransWindDlg;
                                TransSolarDlg;
```

    TTransJointDlg TransJointDlg;
    TTransRandDlg
    TTransMathsDlg
    TTransTsDlg
    TTransFpDIg
    PTRenewPlot
    TMainWindow
    TransRandDlg;
    TransMathsDlg;
    TransTsDlg;
    TransFpDlg;
    testplot;
    (PTWindowsObject AParent, LPSTR ATitle);
    virtual TMainWindow ();
    virtual BOOL Canclose ( );
    virtual void CMWindSpeed (RTMessage) = [CM_PIRST + cmWindSpeed];
    virtual void CMSettings (RTMessage) = [CM_PIRST + cmSettings ];
    virtual void CMMaths (RTMessage) = [CM_FIRST + CmMaths];
    virtual void CMWindPower (RTMessage) = [CM_FIRST + cmWindPower];
    virtual void CMSolar (RTMessage) = [CM-FIRST + cmSolar];
    virtual void CMRenewable (RTMessage) = [CM_FIRST + cmRenewable];
    virtual void CMExport (RTMessage) = [CMFIRST + cmExport];
    virtual void CMDisplay (RTMessage) m [CM FIRST + cmDisplay];
    virtual void CMHelp (RTMessage) = [CM-FIRST + cm#elp];
    virtual void CMDir (RTMessage) = [CMMFIRST + CmDirectories];
    virtual void CMRandom (RTMessage) = [CM_FIRST + cmRandom];
    virtual void CMTimeSeries(RTMessage) = [CMFFIRST + cmTimeSeries];
    virtual void CMFpt (RTMessage) = [CM-FIRST + cmPirstPassage];
    virtual void GotwindowClass (WNDCLASS& WndClass);
    friend ostream& operator << (ostream&, RTMainWindow);
    friend istream& operator >> (istream&, RTMainWindow);
    };
/*** Application **********************************************************/
CLASSDEF (TRenewApp)
Class TRenewApp : public TApplication {
int choice;
public:
TRenewApp(LPSTR AName, HINSTANCE hInstance, HINSTANCE hPrevInstance,
LPSTR lpCmdLine, int nCmdShow)
: TApplication(AName, hInstance, hprevInstance, IpCmdLine, nCmdShow),
choice (0)
{ };
virtual void InitMainWindow();
};
*endif
/*** ene of owrenew.h **************************************************/

```

\subsection*{7.5.1.14 <owres.h>}
\begin{tabular}{|c|c|c|c|}
\hline /********************** & & & \\
\hline /********************** & ** & * & \\
\hline \#ifndef OWRES HEADER & & & \\
\hline /*** Constants ******** & ** & * & \\
\hline +define cmWindSpeed & 500 & & \\
\hline \#define cmSolar & 501 & & \\
\hline \# define cmRenewable & 502 & & \\
\hline *define cmSettings & 503 & & \\
\hline \#define cmMaths & 504 & & \\
\hline Fdefine cmExport & 505 & & \\
\hline \#define cmWindPower & 506 & & \\
\hline \#define cmilelp & 507 & & \\
\hline \#define cmDirectories & 510 & & \\
\hline \#define cmRandom & 512 & & \\
\hline \(\ddagger\) define cmTimeSeries & 513 & & \\
\hline \#define cmFirstPassage & 514 & & \\
\hline \(\ddagger\) define cmDisplay & 515 & & \\
\hline /*** ID. Constants & & & \\
\hline
\end{tabular}
\begin{tabular}{lc} 
// Parameter & \\
\#define idEval & 100 \\
\#define idTau & 101 \\
\#define idTextTau & 102 \\
\#define idStatusText & 103 \\
\#define idTimeText & 104 \\
\#define idReportText & 105 \\
\#define idclasses & 106
\end{tabular}

\section*{// Dialogs}
\begin{tabular}{ll} 
\#define & idOpProbDens \\
\#define idOpDist & 110 \\
\#define idopAnalyt & 111 \\
ild \\
\#define idopApprox & 113 \\
\#define idopcond & 114 \\
\#define idOpQual & 115 \\
\#define idOpStationary & 116
\end{tabular}
\begin{tabular}{ll} 
// Wind parameter & \\
\#define idWiVci & \\
\#define idWiVco & 120 \\
\#define idWiVr & 121 \\
\#define idWisigma & 122 \\
\#der \\
\#define idWiVmean & 123 \\
\#define idWiBeta & 124 \\
\#define idWiVmin & 125 \\
\#define idWiVmax & 127 \\
\#define idWiTextInitv & 127 \\
\#define idWiInitv & 129
\end{tabular}
\begin{tabular}{ll} 
// Solar parameter & \\
\#define idSolk & 140 \\
\#define idSolSigmak & 141 \\
\#define idSolko & 142 \\
\#define idSolBeta & 144 \\
idefine idSolInitk & 145 \\
\#define idSolTrial & 146 \\
\#define idSolcoeff & 147 \\
\#define idSolBypass & 148 \\
\#define idSolTextInitk & 149 \\
\#define idSolTextTrial & 150 \\
\#define idSolTextCoeff & 151
\end{tabular}
// Combined Renewables
\#define idcomZeta 160
\#define idComp 161
\begin{tabular}{ll} 
// Export Dialog & \\
\#define idExpAttach & 170 \\
\#define idExpNew & 171 \\
\#define idExpFile & 172 \\
// Directories dialog & \\
\#define idDlgFile & 180 \\
\#define idSolfile & 181
\end{tabular}
// Random Numbers Dialog
\#define idRanopo
190
\#define idRanopl 191
\#define idRanOp2 192
*define idRanop3 193
\#define idRanTexta 194
\#define idRanTextB 195
\#define idRanTextr 196
\#define idRanTextBeta 197
*define idranTextBi 198
\#define idRanInputa 199
Fdefine idRanInputB 200
\#define idRanInputP 201
\#define idRanTextclass 202
\#define idRanTrial 203
\#define idRanInputclass 205
Header Files


\subsection*{7.5.1.15 <owstat.h>}

/*** Module: OWSTAT.日
\(* * * /\)
```

/*************************************************************************/
/*************************************************************************/
/*** Object Windows C++: Calculations in the Status Window Environment ***/

```

\#ifndef OWSTAT_HEADER
*define owstat_header
ifndef DISTR BEADER
include <distrib.h>
endif
\#include <owl.h>
Finclude <dialog.h>
\#include <edit.h>
\#include <button.h>

    CLASSDEF (TStatusWindow)
Class TStatusWindow : public TDialog \{
private :
    PTStatic statusText1;
    PTStatic statusText2;
    PTStatic timeText;
    PTButton okButton;
    PTButton cancelButton;
    PTButton retryButton;
    double lastTime;
    double startTime;
    int mode;
    void starttimer ();
    double time ();
protected :
    int giveWarning
    virtual void writeRepl
    virtual void writeRep2
    virtual int workout
    virtual void WMInitDialog
    virtual void ok
    virtual void Retry
    virtual void TimeMsg
public :
    void writerime ( );
    int isEnoughtime ( ):
    static double temp;
void
writeStatus 1 (char* ;
    void writestatus2 (char* );
    TStatusWindow (PTWindowsObject AParent, LPSTR ATitle);
    virtual -TStatusWindow ( );
f;
/*** class TMultiValobject **********************************************/
CLASSDEF (TMultiValobject)
Class TMultiValobject : public TStatusWindow \{
    int eval;
    int isAccuDesired ( );
protected :
    virtual int workOutBasic ( ) \(=0\);
    virtual int workoutvalues ( ) = o;
    virtual int areParameterok ( ) \(=0\);
    virtual void setoldparameter ( ) =0;
    int workout
    void calcValues (owObjfunc*,double,double)
public :
    TMultiValobject (PTWindowsObject AParent, LPSTR ATitle,int):
    virtual TMultiValobject ( ) \{ ; \}
    static void calc (owobjfunc*, double, double,int,TStatusWindow*);
\};
\#endif
```

/*** end of owstat.h *******************************************************/

```

\subsection*{7.5.1.16 <passage.h>}
```

/*********************************************************************************/
/***
***/
/*** Module: PASSAGE.|
***/
/***
/*** Eeader for first pasaage time problems in the renewable energy ***/
/*** project owrenew.prj ***/
/********************************************************************************/
\#ifndef PASSAGE HEADER
\#define PASSAGE_HEADER
\#ifndef SERIES HEADER
*include <seriés.h>
\#endif
*ifndef VECTORS_HEADER
\#include <vectors.h>
\#endif
\#ifndef OWPARAM_HEADER
\#include <owparäm.h>
\#endif

```
class DiscretDistribution; // forward declaration
```

/***************************************************************************/
/*** Abstract class of a first passage time problem ************************/
/***************************************************************************/
class PassageTime : public msgobjfunc {
protected :
double passLevel; // passage level (power / speed)
double inituevel; // initial level (power / speed)
double timeStep; // time step
virtual int Setup (TStatusFindow*, Param*) = 0;
public:
PassageTime
virtual TPasaagemime
int setUp
void setpassLevel (double newLevel Param*};{ {assLevelmnewLevel; }
virtual void setInitLevel (void* ) =0;
};
/***************************************************************************/
/*** Abstract class for first passage time - time series approach **********/
/***************************************************************************/
class TSPassageTime public Passagerime {
private :
int repFactor; // number of time series taken into account
int maxIt; // maximum number of iterations
protected :
TimeSeries* timeSeries;
virtual int SetUp ( TStatusWindow*, Param* );
public:
TSPassageTime ( );
virtual ~rsPassageTime ( );
double Eval ( double );
void setInitLevel ( void* );
};
/***************************************************************************/
/*** Wind speed passage time - time series approach
******/
/***************************************************************************/

```
```

Class TSWindSpeedPassageTime : public TSPassageTime {
public :
TSWindSpeedPassageTime (TStatusWindow*, Param* );
};
/****************************************************************************/
/*** Wind power passage time - time series approach ******/
/*****************************************************************************/
class TSWindPowerPassageTime : public TSPassageTime {
public :
TSWindPowerPassageTime (TStatusWindow*, Param* );
};
/**********************************************************************************)
/*** Solar power passage time - time series approach ******/
/***************************************************************************************
Class TSSOlarPowerPassageTime : public TSPassageTime {
public :
TSSOlarPowerPassageTime (TStatusWindow*, Param* );
};
/*********************************************************************************)
/*** Joint renewable passage time - time series approach ******/
/********************************************************************************/
class TSJointPowerPassageTime : public TSPassageTime {
public:
TSJOintPowerPassageTime ( TStatusWindow*, Param*);
};
/*****************************************************************************/
/*** Abstract class for Markov chain approach ******/
/**************t************************************************************/
Class MCPassageTime : public PassageTime {
private :
MATRIX G; // Transition matrix
VECTOR P; // Probability vector
double stopCrit; // stopping criterion
int maxit; // maximum number of iterations
int discPassLevel; // discretized passage level
int discInitLevel; // discretized initial level
void updateg ( );
protected :
int classes; // number of discretization levels
DiscretDistribution* distribution;
int discretize (double );
public:
MCPassageTime ( );

```

```

    virtual int SetUp (lnitLevel ( TStatusWindow*, Param*);
    };
/*******************************************************************************/
/*** Class MCFindSpeedPassageTime ******/
/********t******************************t***********************************/
class MCWindSpeedPassageTime : public MCPassageTime {
public :
MCWindSpeedPassageTime ( ) : MCPassageTime ( ) { ; }
int SetUp (TStatusWindow*, Param*);
};
/**********************************************************************************/

```
```

/*** class MCWindPowerPassageTime ******/
/**************************************************************************************/

```
class MCWindPowerPassageTime : public MCPassageTime \{
public:
    MCWindPowerPassageTime ( ): MCPassageTime () \{; \}
    int SetUp ( TStatusWindow*, Param* );
\};
/***********************************************************************/
/*** Class MCSolarPowerPassageTime *****/
/************************************************************************/
Class MCSOlarPowerPassageTime : public MCPassageTime \{
public:
    MCSolarPowerPassageTime ( ) : MCPassageTime ( ) \{ ; \}
    int Setup ( TStatusWindow*, Param*);
\};
/*************************************************************************/
/*** cIass MCJOintPowerPassaceTime t****/

class MCJointPowerPassageTime : public MCPassageTime \(\{\)
public:
    MCJointPowerPassageTime ( ): MCPassageTime () \{ ; \}
    int SetUp (TStatuBWindow*, Param*);
;;
/*************************************************************************/
/*** Abstract class of a first passage time problem **********************/
\(/ * * *\) allowing to vary either the passage level or initial value. ***/
/***********************************************************************/
class Passagetimes : public owobjfunc \{
protected :
    \(\begin{array}{ll}\text { int } & \text { selectcalc; } \\ \text { int } & \text { noval; }\end{array}\)
    PassageTime* passageTime;
    virtual int SetUp ('TStatusWindow*, Param*) \(=0\);
public:
    double minval;
    double maxVal;
    Passagetimes ( )i
    virtual ~Passagerimes ( );
    int setUp (TStatusWindow*, Param*);
    double eval ( double );
\};
// Wind speed
class WindSpeedPassageTimes : public PassageTimes \{
public:
    WindSpeedPassageTimes ( int
int SetUp
(TStatusWindow*, Param* );
\};
// Wind power
class WindPowerPassageTimes : public PassageTimes \{
public:
    WindPowerPassageTimes (int );
    int SetUp (TStatusWindow*, Param*);
\};
// solar power
class SolarPowerPassageTimes : public PassageTimes \{
public:
    SolarPowerPassageTimes (int );
    int SetUp (TStatusWindow*, Param*);
\};
// Joint renewable power
class JointPowerPassagetimes : public PassageTimes \{
```

public:
JointPowerPassagerimes (int );
int SetUp (TStatusWindow*, Param*);
};

```
\#endif
/*** End of passage.h ***************************************************/

\subsection*{7.5.1.17 <random.h>}
```

/***************************************************************************/
/*** Module: RANDOM.E ***/
/*** ***/
/*** Definition of types and classes for random numbers ***/
/***************************************************************************/

```
\#ifindef RANDOM HEADER
\#define RANDOM_HEADER
*ifndef VECTORS HEADER
finclude <vectors.h>
\#emdif
\#ifndef MATHFUNC_HEADER
\#include <mathfuñe.h>
*endif
/*** Constanta ***********************************************************/
\#define NTAB 32
/*** Uniform deviates **************************************************/
class uniRand \{
public :
    uniRand
    virtual
    void
    virtual double
    virtual void
\};
/*** Gaussian deviates N(a, var) "*****************************************/
class normRand : public unikand \{
    double mean;
    double sigma;
    int iset;
    double gset;
public :
    normRand
    normRand
    virtual
    virtual double
    void
\}:
/*** Rejection method ***************************************************/
class rejectRand : public uniRand \{
public:
    rejectRand
    virtual double getRandomNumber ( )
protected :
    virtual double compFunc (double) \(=0\);
    virtual double origFunc (double) \(=0\);
    virtual double invinteg \(\quad\) (double) \(=0\);
\};
/*** Rejection method using a uniform distribution as comparison function */
/*** for distributions with non zero values in the interval [0,1] */
class unirejectrand : public rejectrand \{
```

private :
double ceiling;
public :
uniRejectRand ( ) { ceiling = 1; }
uniRejectRand (double max) { ceiling = max; }
protected :
virtual double compFunc (double) { return 1; }
virtual double invInteg (double y) { return y; }
};

```

```

class betaRand : public uniRejectRand {
private :
double alpha,beta,fact;
protected :
virtual double origFunc (double );
virtual double compFunc (double );
public :
betaRand
betaRand
};
/*** Discrete distributions using the rejection method ********************/
class discretRand : public uniRand {
private :
VECTOR* px;
double ceiling;
double getRandomNumber ( );
public :
discretRand ( vECTOR* ); ( void* );
};
l*******************************************************************************/
/*** Kolmogorov - Smirnov test ********************************************************)
/********************************************************************************/
/*** Abstract class for KGS test ******************************************/
Class RgSTest {
protected :
double size;
int k;
double mean;
double var;
VECTOR x,y,x;
uniRand* randomizer;
virtual void initialize ( ) { ; }
virtual double theoretprob (double x) = o;
void dovalues
double
void
public :
double doTest
double getMean ( );
double getvar (int (, );
RgSTest (int n);
};
/*** Rolmogorov- Smirnov Test for uniform distribution ********************/
Class UniKgSTest : public KgSTest {
public :
UniKgSTest (int n) : KgSTest (n) { ; }
double theoretprob (double x) { return (x); }
void initialize ( ) { randomizer = new uniRand ( ); }
};
/*** Kolmogorov- Smirnov Test for normal distribution *********************/
class NormKgSTest : public KgSTest {
public:
NormRgSTest (int n) : KgSTest (n) { ; }

```
```

    double theoretProb (double x) { return (PHI (x) ); }
    void initialize () { randomizer = new normRand ( ); }
    };
/*** Kolmogorov- Smirnov Teat for beta- distribution ***********************/
class BetakgSTest : public KgSTest {
double alpha, beta;
double classes;
public :
BetaRgSTest (int n, int r, double a, double b);
double theoretProb (double x);
void initialize ( ) { randomizer = new betaRand (alpha,beta); }
};
*endif
/*** End of RANDOM.H ******************************************************/

```

\subsection*{7.5.1.18 <series.h>}
```

/***************************************************************************/
/*** ***/
/*** Module: SERIES.E ***/
/*** ***/
/*** Eeader for time series objecta within the renewable energy ***/
/*** project owrenew.prj ***/
/***************************************************************************/
\#ifndef SERIES HEADER
\#define SERIES-HEADER
\#ifndef VECTORS HEADER
*include <vectors.h>
\#endif
\#ifndef DISTRIB EEADER
\#include <distrīb.h>
\#endif
*ifndef DIFFCALC HEADER
\#include <diffcalc.h>
\#endif
\#ffndef RANDOM HEADER
*include <randöm.h>
Gendif
\#ifndef OWPARAM HEADER
\#include <owparam.h>
*endif
\#ifndef SOLAR HEADER
*include <sol\overline{ar.h}>
*endif
/***************************************************************************/
/*** Abstract ciass of a time series ***************************************/

```

```

class TimeSeries : public OwObjfunc {
protected :
virtual void update ( ) = 0;
virtual double getOutput ( )}=
public :
TimeSeries
virtual
virtual int
virtual void
};

```
```

Class TimeSeriesOne : public TimeSeries {
protected :
double initUserVal;
double randomVal;
double outVal;
virtual double getInitRandomVal ( ) { return initUserVal; }
virtual double getRandomNumber ()=0;
public:
TimeSeriesOne ( )%
~TmeSeriesOne eval (年 )
double seval setUserInit (年 vouble (%)
};
/*********************************************************************************/
/*** Class of wind speed time series ****************************************/
/*******************************************************************************/
Class WindSpeedTimeSeries : public TimeSeriesOne {
double vmean; // mean wind speed
double effsigma; // effective standard variation
uniRand* randomizer;
protected :
double r; // autocorrelation coefficient
double sigma; // standard variation
double getRandóNumber ( ) { return (randomizer->getRandomNumber()); }
double getOutput ( ) { return randomVal; }
public :
int setUp (TStatusWindow*, Param* );
void update ( );
void setcorrelation ( double );
WindSpeedTimeSeries ( );
};
/**********************************************************************************/
/*** Wind power time series t***/
/***************************************************************************/

```
class WindPowerTimeSeries : public WindSpeedTineSeries \{
private :
    double vci,vco,vr;
public :
    WindpowerTimeSeries ( )
    static double getwindPower (double V, double Vci, double Vco, double Vr);
    static double getV (double p, double Vci, double Vr);
    \(\begin{array}{ll}\text { double getoutput } \\ \text { int setUp } & \text { ( TStatusWindow*, Parara* ); }\end{array}\)
\};

/*** Solar power time series ***/

class SolarPowerTimeSeries : public TimeSeriesOne \{
    double NMinusone;
    double RO;
    SolarRandómizer* randomizer;
    double getRandomNumber ( ) \{ return (randomizer->getRandomNumber()); \}
public :
    \(\begin{array}{ll}\text { SolarpowerTimeSeries } \\ \text { SolarPowerTimeSeries } & \text { ( } \\ \text { int }\end{array}\)
    int setup
    double getoutput
    double getInitRandomVal
    void update
\};

/*** Joint power time series

```

class JointPowerTimeSeries : public TimeSeries {
SolarPowerTimeSeries* solarPowerTimeSeries;
WindPowerTimeSeries* windPowerTimeSeries;
double zeta; // fractional power factor
public :
JointPowerTimeSeries
~JointPowerTimeSeries
void update
double getoutput
({);
ll
};

```
/***********************************************************************/
/*** State of charge time series

class StateOfChargeTimeSeries : public TimeSeries \{
    double batK,batc,batQMax,batV,batQ10,batQ20;
    double sysPRen, sysPDemand;
    double I, PNeed;
    double q1,q2;
    double kt;
    void calcrcharge ( ):
    void calcIDischarge \((\) ):
protected :
    JointPowerTimeSeries* jointPowerTimeSeries;
    double deltap;
    void update ( ):
    double getoutput \()\) ):
public :
    StateOfChargeTimeSeries ( );
    ~Stateof ChargetimeSeries ( );
    double eval ( double \(\quad\) int
    int setup (TStatusWindow*, Param*);
, void setUserInit ( void* );
r;
/************************************************************************/
/*** Power Deficit Time Serian
    ****/
/*************************************************************************/
Class PowerDeficitTimeSeries : public StateOfChargeTimeSeries \(\{\)
    double getoutput ( );
public :
    PowerDeficittimeSeries ( );
    double eval )
\};
\#endif


\subsection*{7.5.1.19 <solar.h>}
\begin{tabular}{|c|c|}
\hline /*** & \multirow[t]{2}{*}{Module: SOLAR.H} \\
\hline /*** & \\
\hline /*** & \\
\hline /*** & Header for sola \\
\hline ** & ************** \\
\hline
\end{tabular}
\#ifndef SOLAR_HEADER
idefine SOLAR_HEADER
\#ifndef DISTRIB_HEADER
\#include <distrib.h>
tendif
```

/***************************************************************************/
/*** Solar Power Constants ***/
/***************************************************************************/
class SolConstants {
public :
SolConstants ( );
SolConstants() { ; }
double w,deltakRO,kminko,deltak,kmin,correl;
VECTOR a,b;
int setup (Param* );
void xTok (double, double*);
void kTox (double, double*);
};
f***************************************************************************/
/*** The exact distribution (with beta functions) ***/
/***************************************************************************/
class ContSolExact : public ContinuousDistribution {
protected :
SolConstants solC;
double Fx (double );
public : ( )
ContSolExact ( ); {; {
double F ( double );
int setUp ( TStatusWindow*, Param*);
};
class ContSolExactX : public ContSolExact {
public:

```

```

    double F ( double );
    };
class ProbSolExact : public statfunc {
public:
ProbSolExact ( );
};

```

\(/ * * *\) Object class for solar power with leagt square method *****************/

class Meritsol : public msgobjfunc \{
    double alpha (int j, int \(k\) );
    double fp ( double p); // density function in \(p=j /(N-1)\)
    double merit \()\) ) // figure of merit
    int solcoeff;
    int solTrial;
    double solk;
    double solsigmak;
    MATRIX AA; // Coefficient matrix A
    MATRIX Alpha; // Coefficient matrix
    VECTOR d;
    // Coefficients of left gide of normal equations
    VECTOR C; // Coefficients of prob dens function
public:
    MeritSol (SolConstants*,Param*);
    Meritsol( ) \{; \}
    solconstants* psc;
    double initialx;
    VECTOR u;
    initial clearness index on \(x\) - scale
    // Coeff. vector of generating functions
    VECTOR sigma; // Standard deviation vector
    VECTOR Iambda; // Standard deviation vector / epsilon
    VECTOR FXT:
    double QPIusOne;
    double MPlusOne;
    // vector with distribution function values
    // number of generating functions used +1
    \(/ /\) number of trial points +1

```

/*********************************************************************************)
/*** Approximated Distribution
***/
/*************************************************************************************)
// Approximation of the solar diatribution
class ContSolApprox : public ContinuousDistribution {
protected :
MeritSol* sol;
SolConstants sc;
public :
ContSolApprox ( );
-ContSolApprox ( );
double F ( double
int setUp (TStatusWindow*, Param* );
void setcorrelation ( double time, double beta);
void setInitval ( double initk );
};
class ContSolApproxx : public ContSolApprox {
public :
ContSolApproxX
ContSolApproxx
double F
};
class ProbSolApprox : public statfunc {
public :
ProbSolApprox ( );
};
// Conditional distribution
class ContCondSolApprox : public ContSolApprox {
public :
ContCondSolApprox ( ) : ContSolApprox ( ) { ; }
int setUp ( TStatusWindow*, Param* );
};
class ProbCondSolApprox : public statfunc {
public:
ProbCondSolApprox ( );
};
// Qualityfunction
class ContSolAppQual : public ContinuousDistribution {
ContSolExact* exact;
ContSolApprox* approx;
public :
ContSolAppQual ( );
*ContSolAppoval
virtual double F
int setUp F ( double (TStatusWindow*, Param* );
};
class ProbSolAppQual : public statfunc {
public:
ProbSolAppQual ( );
};
/**********************************************************************************/
/*** Discrete Distribution

```

\section*{/************************************************************************/}
```

class DiscSolApprox : public DiscretDistribution {
private :
ContSolApprox* solApprox;
lowl
double NMinusOne;

```

\};
/**************************************************************************/
/*** Discrete Randomizer ***/
/***************************************************************************/
class SolarRandomizer : public DiscretRandomizer \{
public :
    SolarRandomizer ( );
    int setUp ( TStatusWindow*, Param*);
\};
tendif


\subsection*{7.5.1.20 <vectors.h>}
```

/***************************************************************************/
/*** Module: VECTORS.且
***/
/*** ***/
/*** consists of class definitions for vectors and arrays. ***/
/***************************t***********************************************/
ifndef VECTORS EEADER
*define VECTORS_HEADER
\#include <iostream.h>
*include <complex.h>
/*** The general class of a linear chain ***********************************/
template <class T> class CBAIN_ {
protected:
T* p;
int size;
public:
CHAIN (int n);
CHAIN (void);
CHAIN- (CHAIN_\& c);
-CHAIN () {if(-(size) delete p;}
int minchainindex (void);
int maxchainindex (void);
}
template <class T> class MATRIX_;
/*** The class of vectors **************************************************/
template <class T> class VECTOR_ : public CEAIN_<T> {
public:

```

VECTOR_
friend ostream\&
friend istream\&
friend int
friend int
friend int
friend int
friend int
friend int
friend vector_
friend
frientor MATRIX_<T>
void
void
void
void
void
void
int
T
T
void
VECTOR_<T>
void
\};
typedef VECTOR_<int>
typedef VECTOR_<double> DVETOR;
class VECTOR : public DVECTOR
public:
\begin{tabular}{|c|c|c|c|c|c|}
\hline VECTOR & & , & double> & & \\
\hline vector & int m & : VECTOR \({ }^{-}\)<doul & double> ( n ) & \{ ; \} & \\
\hline VECTOR & (VECTOR\& V) & : VECTOR \({ }^{-1}\) & double> (v) & \{; \} & \\
\hline VECTOR\& & & operator & (VECTOR\& & & ; \\
\hline friend & VECTOR & operator & (VECTOR\& a , & VECTOR\& & \\
\hline friend & VECTOR & operator + & (VECTOR\& \(u\), & doubla & \\
\hline friend & VECTOR\& & operator + + & (VECTOR\& u , & VECTOR\& & \\
\hline friend & VECTOR\& & operator +m & (VECTOR\& \({ }^{\text {a }}\), & double & \\
\hline friend & vector & operator & (VECTOR\& u , & VECTOR\& & \\
\hline friend & VECTOR & operator & (VECTOR\& u , & double & \\
\hline friend & VECTOR\& & operator & (VECTORE \({ }^{\text {a }}\), & VECTOR\& & \\
\hline friend & VECTOR\& & operator & (VECTORE \({ }^{\text {a }}\), & double & \\
\hline friend & VECTOR & operator & (VECTORE \(u\), & double & \\
\hline friend & VECTOR\& & operator & (VECTOR\& \(u\), & double & \\
\hline friend & VECTOR & operator & (double u, & VECTOR\& & \\
\hline friend & VECTOR & operator & (VECTOR\& \({ }^{\text {a, }}\) & VECTOR\& & \\
\hline friend & VECTOR & operator & (VECTORE A, & double & \\
\hline friend & vectora & operator /= & (VECTOR\& A, & double & \\
\hline friend & VECTOR & operator / & (VECTORE u , & VECTOR\& & \\
\hline friend & ostream\& & operator << & (ostream\& & VECTORE & \\
\hline friend & istream\& & operator >> & (istream\& & VECTOR\& & \(v\) \\
\hline
\end{tabular}
    frctor
    VECTOR
    double
    double
    double
    double
    double
    int
    double
    int maxindex
    static VECTOR cross (VECTOR \&u, VECTOR \&V);
    static double scalar (VECTOR \&u, VECTOR \&V);
\};
/*** The class of arrays *************************************************/
template <class \(T>\) class MATRIX_ : public CHAIN_<T> \{
public :
\begin{tabular}{|c|c|c|}
\hline int & row; // Zeile & \\
\hline int & col; // Spalte & \\
\hline MATRIX & ( Yoid int \({ }^{\text {) }}\) &  \\
\hline MATRIX_ & (int m, int \(n\) ) & CHAIN_<T> (m * \(n\) ) \{ row m m; col = n ; \\
\hline
\end{tabular}

```

{ row = A.row; coI = A.col;}
VECTOR_<T>
T\&
MATRIX_\&
friend- ostream\&
friend istream\&
void
void
void
void
T
void
void
};
typedef MATRIX_<int> IMATRIX;
typedef MATRIX_<double> DMATRIX;
class MATRIX : public DMATRIX {
public :

| MATRIX |  | ) : | MATRIX | x <ciouble> | ( ) $\{$ | ; $\}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| MATRIX | (int m, in | ( m ) : | MATRIX | x-<double> | (m,n) | ; $\}$ |
| MATRIX | (int n | ) | MATRIX | x <double> | (n) \{ | ; $\}$ |
| MATRIX | ( MATRIX\& | A ) : | MATRIX | X-<double> | (A) | , |
| MATRIX: |  | operator | = | (MATRIX\& |  | ; |
| friend | MATRIX | operator | + | (MATRIX\& ${ }^{\text {, }}$ | MATRIX\& | B ) |
| friend | MATRIX\& | operator | $r+=$ ( | (MATRIX\& A, | MATRIX\& | B ) |
| Eriend | MATRIX | - operator | г - | (MATRIXE A, | MATRIX\& | B ); |
| friend | MATRIX\& | operator | - = ( | (MATRIXE A, | MATRIXE | B ) |
| friend | MATRIX | operator | * ( | (MATRIX\& ${ }^{\text {, }}$ | double | $x$ ) |
| friend | MATRIX | operator | \% * ( | (double $x$, | MATRIX\& | A ) |
| friend | MATRIX\& | operator | r * = | (MATRIX\& ${ }^{\text {, }}$ | double | ; |
| friend | MATRIX | operator | - ( | (MATRIX\& A, | MATRIXE | B ) |
| friend | VECTOR | operator | \% ( | (MATRIX\& A, | VECTOR\& | $v$ ) |
| friend | VECTOR | operator | * | (VECTOR\& V, | MATRIX\& | A ) |
| friend | MATRIX | operator | r / | (MATRIX\& A, | double | $\mathbf{x}$ ) |
| friend | MATRIX\& | operator | r $/=$ 1 | (MATRIX\& A, | double | $x$ ) |
| friend | Ostream\& | operator | r $<$ | (ostreamk | MATRIX\& | A ) |
| friend | istream\& | operator | r >> | (istream\& | MATRIXE | A ) |
| void |  | identity |  | ( ); |  |  |
| double |  | trace |  | ( ) |  |  |
| MATRIX |  | transp |  | ( ) ; |  |  |

};
*endif
/*** End Of VECTORS.H ******************************************************/

```

\subsection*{7.5.1.21 <wind.h>}
```

/***************************************************************************/
/*** - . - ***/
/*** Module: WIND.H ****/
/*** ***/
/*** Header for wind related objects ***/
/***************************************************************************/
\#ifndef WIND HEADER
\#define WIND_HEADER
*ifmdef DIFFCALC HEADER
*include <diffcaIc.h>
*endif
\#ifndef DISTRIB HEADER
\#include <distrib.h>

```
```

\#endif
\#ifndef MATHFUNC hEADER
\#include <mathfunc.h>
\#endif
class WindSpeedTimeSeries; // Forward declaration
/****\#*********************************************************************/
/*** Continuous Wind Speed Distribution *************************************/
/**********************************************************************************/
class Speed : public owobjfunc {
protected :
double vmean;
double vaigma;
public:
Speed () { ; }
virtual doubie eval (double)=0;
int setUp (Param*);
};
class SpeedDist : public Speed {
public :
SpeedDist ( ) {; }
double eval (dóuble v) { return (PHI(v,vmean,vsigma));}
};
class SpeedDens : public Speed {
public:
SpeedDens () {; }
double eval (double v) { return (phi(v,vmean,vsigma));}
};
/*********************************************************************************/
/*** Discrete Wind Speed Distribution ****************************************/
/*****************************************************************************************)
Class DiscretWindSpeed : public DiscretDistribution {
private :
double uAlpha; // alpha quantile
double vmean; // mean wind speed
double sigma; // standard variation
double r;
// correlation
VECTOR points;
VECTOR beta;
double rawP ( int , int );
public:
DiscretWindSpeed (int n) : DiscretDistribution (n) { ; )
double gnm (int, int );
int getN (double );
int setUp ( TStatusWindow*, Param* );
};
/******************************************************************************/
/*** Continuous Wind turbine power distribution ****************************/
/*********************************************************************************/
class ContWindPower : public ContinuousDistribution {
private :
double ffvco,vci,vco,vr,vmean,sigmav;
double
protected :
double r
r ; // autocorrelation coefficient
public :
ContWindPower
virtual -ContWindPower ( ) { ; }
double F (double );
int setUp (TStatusWindow*, Param* );
void setCorrelation (double time, double beta);
};

```
```

/**************************************************************************/
/*** Continuous Conditional. Wind turbine power distribution ****************/
/*****************************************************************************/
class ContCondWindPower : public ContWindPower {
public:
ContCondWindPower ( ) : ContWindPower ( ) { ; }
int setUp (TStatusWindow*, Param*);
};
/***************************************************************************************
/*** Wind turbine power probability distributions ***************************/
/*******************************************************************************/
class ProbWindPower : public statfunc {
public :
ProbWindPower ( ):
};
class ProbCondWindPower : public statfunc {
public :
ProbCondWindPower ( );
};
/*******************************************************************************/
/*** Discrete Wind Power ******************/
/*****************************************************************************/
class DiscretWindPower : public DiscretDistribution {
private :
double vci,vco,vr,vmean;
ContWindPower* windPower:
WindSpeedTimeSeries* timeSeries;
double getPower ( int n);
public :
DiscretWindPower ( int n);
~DiscretWindPower ( in );
double gnm (int, int );
double Gn ( int );
int getN ( double . );
int setUp ( TStatusWindow*, Param* );
};
\#endif
/*** End of wind.h ***********************************************************/

```

\subsection*{7.5.2 Source Files}

\subsection*{7.5.2.1 <owrenew.cpp>}
```

/*************************************************************************/
/*** Renewable Energy Resources for Windows ***/
/*************************************************************************/
\#ifndef OWRENEH GEADER
\#include "owrenew.h"
*endif
\#ifndef OWPEOT_HEADER
\#include "owplot.h"
*endif
\#ifndef OWCALC HEADER
*include <owcaIc.h>
\#endif
*ifndef OWLAPPG HEADER
\#include <owlapp1.h>
tendif
\#ifndef OWPARAM_HEADER
髙include <owparam.h>
*endif
\#ifndef CSTRING HEADER
\#include <cstring.h>
\#endif
*include <owI.h>
*include <button.h>
*include <edit.h>
\#include <groupbox.h>
*include <radiobut.h>
*include <fstream.h>
\#define dlgFile "owrenew.dlg"
/*** Module global prototypes ********************************************/
void NoFeatureMessage (HWND);
/*** Global variables ****************************************************/
Param* param; // parameter
PTRenewApp App;
Graph* GraphData; // Graphic Data Interface
/*************************************************************************/
/*************************************************************************/

```
TRenewPlot : : TRenewPlot (PTWindowsobject AParent, LPSTR ATitle, PTModule AModule)
        : PPlot (AParent, ATitle, AModule)
i
    delta \(=\) (curRect.right - curRect. left);
    start = curRect.left ;
    end \(=\) start + delta;
    clear \(=\) YES;
\}
void TRenewPlot : : Paint (EDC dc, PAINTSTRUCT _FAR\& v) \{
    if (cleax m= YES
        TPlot : : Paint (de, v);
    else \{
        if (! param->disAuto)
            clear = YES;
```

        draw ( );
    }
    }

```
void TRenewPlot : : plot ( ) \{ // Display GraphData in a graph
    int
        setHeadíine (GraphData->headline);
        setSubLine (GraphData->subline);
    clearScreen ();
    plotHeadLine ();
    plotSubLine ( );
    drawMargin ();
    GraphData->scale = drawAutoLinCoord (GraphData->min, GraphData->max,
        GraphData->y, GraphData->axtextr" ",
        YES, YES,GraphData->scale, GraphData->CurveNo);
    for (i=0;i<=GraphData->curveNo;i++) \{
        drawCurve (GraphData->x,GraphData->y[i],GraphData->option);
        switch (i) \{
            case 0:
                setPenColor (RGB(255,0,0));
                break;
            case 1
                setPenColor (RGB(0,255,0));
                break:
            case 2 :
                setPenColor ( \(\operatorname{RGB}(0,0,255)\) );
                break;
            case 3 :
            default :
                setPenColor ( \(\operatorname{RGB}(0,0,0)\) );
                break;
        \(\}\)
    \}
    setPenColor \((\operatorname{RGB}(0,0,0))\);
\}
/***********************************************************************/
/*** Main Platform ***/

/*** class TMainWindow *************************************************/
TMainWindow :: TMainWindow (PTWindowsobject AParent, LPSTR ATitle)
        : TWindow(AParent, ATitle)
\{
    Attr.style |= WS MAXIMIZE | WS_VISIBLE;
    AssignMenu ("COMMANDS");
    testplot \(=\) new TRenewpiót (this, NULL);
\}
TMainWindow :: MMainWindow () \{
    delete testplot;
\}
void TMainWindow :: GetWindowClass (WNDCLASS\& WndClass) \{
    TWindow :: GetWindowClass (WndClass);
    WndClass.hbrBackground \(=\) (EBRUSH) COLOR_APPWORKSPACE+1;
-\}
BooL TMainwindow : : Canclose ()
\{
    BOOL retval;
    if (GetModule()->ExecDialog(new TYoMessage(this,"Question",
                "Do you want to quit to Windows?")) \(=\) = IDYES) \(\{\)
        fstream op;
        op.open (digFile, ios : : out);
        if (op)
            op << *this;
        op.close ();
        retval = True;
    \}
    else
```

        retval = False;
    return retval;
    }
void TMainWindow :: CMWindSpeed (RTMessage) {
int retval=GetModule()->ExecDialog (new TSpeedDialog(this,"SpeedDialog"));
if (retval =- IDOR) {
testplot->open ( );
testplot->clearscreen ( );
testplot->close ( );
TransSpeedDlg.setparameter ();
TransSettingsDlg.wiVmean = TransSpeedDlg.vmean;
if (GetModule()->ExecDialog(new TWindSpeedObject(this,"StatusWindow"))
== IDOK)
testplot->clear = NO;
}
}
void TMainWindow :: CMSettings (RTMessage) {
if (GetModule()->ExecDiaIog (new TSettingsDialog (this, "Settings"))m= IDOK) {
TransSettingsDlg.setParameter ( );
TransSpeedDIg.vmean = TransSettingsDlg.wiVmean;
TransWindDlg.vmean = TransSettingsDlg.wiVmean;
TransSolarDig.clearness = TransSettingsDlg.solk;
TransSolarDlg.sigmaK = TransSettingsDlg.solSigmak;
TransJointDlg.vmean = TransSettingsDlg.wiVmean;
TransJointDlg.sigmaK = TransSettingsDlg.solSigmaR;
TransJointDIg.clearness = TransSettingsDlg.solk;
}
}
void TMainWindow :: CMMaths (RTMessage) {
if (GetModule()->ExecDialog (new TMathsDialog (this, "Maths"))== IDOK) {
TransMathsDlg.setParameter ( );
TransSolarDlg.coeff = TransMathsDIg.solCoeff;
TransSolarDlg.trial = TransMathsDlg.solTrial;
}
}
void TMainWindow :: CMDir (RTMessage) {
GetModule()->ExecDialog (new TDirDialog (this,"Directories"));
}
void TMainWindow :: CMDisplay (RTMessage) {
if (GetModule()->ExecDialog (new TDisplayDialog (this,"Display"))== IDOK)
TransDisplayDlg.setParameter (.);
}
void TMainWindow : : CMRandom (RTMessage) {
if (GetModule()->ExecDialog (new TRandDialog (this,"RandomNumbers"))m=IDOR){
TransRandDlg.setParameter ( );
GetModule()->ExecDialog(new TRandomObject(this,"StatusWindow"));
}
}
void TMainWindow :: CMTimeSeries (RTMessage) {
if (GetModule()->ExecDialog (new TTsDialog (this,"TimeSeries"))=m=IDOK) {
TransTsDIg,setParameter ( );
TramsSettingsDlg.setParameter ();
TransMathsDig.setParameter ();
param->801Bypass m 1;
testplot->open ( );
testplot->clearScreen ( );
testplot->close ( );
if (GetModule()->ExecDialog(new MTimeSeriesObject(this,"StatusWindow"))
== IDOK) {
int IDOK) {i,j;
char buffer[80];
double }\quadx=(GraphData->y[0])(1):
for (i=0;i<=GraphData->curveNO;i+++)
for (j=1;j<=GraphData->x.dim;j++) {
if ((GraphData->Y[i])(j) != x)

```
```

                break;
                }
                i
                f (i>GraphData->curveNo && j > GraphData->x.dim) {
                    strcpy (buffex,"All data have same value: ");
            catDbl (buffer, x);
            GetModule()->ExecDialog(new TYoMessage(this,"Warning",
                    buffer));
                return;
            }
            else
            testplot->clear = NO;
        }
    }
    }
void TMainWindow :: CMFpt (RTMessage) {
if (GetModule()->ExecDialog (new TFpDialog (this,"FirstPassageTime"))==IDOK) {
TransSettingsDlg.setParameter ( );
TransMathsDIg.setParameter ( );
TransFpDlg.setparameter ( ):
param->solBypass = 1;
if (param->fpSelectCalcmm0) // compute one value only
GetModule()->ExecDialog(new TPassageTimeObject(this,"StatusWindow"));
else { // compute more values
testplot->open ( );
testplot->clearScreen ( );
testplot->close ( );
if (GetModule()->ExecDialog(new PassageTimesObject(this,"StatusWindow"))
\#= IDOR)
testplot->clear = NO;
}
}
}
void TMainWindow :: CMWindPower (RTMessage) {
if (GetModule()->ExecDialog (new TWindDialog (this, "WindPower")) == IDOK) {
testplot->open ( );
testplot->clearscreen ( );
testplot->close ( );
TransSettingsDlg.wivmean = TransWindDlg.vmean;
TransSettingsDlg.setParameter ();
TransWindDlg.setParameter ();
if (GetModule()->ExecDialog(new TDistributionObject(this,"StatusWindow"))
== IDOR)
testplot->clear = NO;
}
}
void TMainWindow :: CMSOIar (RTMessage) {
if (GetModule()->ExecDialog (new TSolarDialog (this, "SolarPower")) == IDOK) {
TransSettingsDlg.solR = TransSolarDlg.clearness;
TransSettingsDlg.solSigmak m TransSolarDlg.sigmaK;
TransMathsDIg.solCoeff = TransSolarDlg.coeff;
TransMathsDlg.solTrial = TransSolarDlg.trial;
TransSettingsDlg.setParameter ( );
TransSolarDlg.setParameter ( );
testplot->open ( );
testplot->clearscreen ( );
testplot->close ( );
if (GetModule()->ExecDialog(new TDistributionObject(this,"StatusWindow"))
\#m= IDOK)
testplot->clear = NO;
}
}
void TMainWindow :: CMRenewable (RTMessage) {
if (GetModule()->ExecDialog (new TJointDialog (this, "RenewablePower")) == IDOK)
{
TransSettingsDlg.solk = TransJointDlg.clearness;
TransSettingsDlg.solSigmaR = TransJointDlg.sigmak;
rransSettingsDlg.wivmean = TransJointDlg.vmean;

```
```

void TRenewApp::InitMainWindow()
{
TMainWindow* Main = new TMainWindow (NULL, Name);
MainWindow = Main;
fstream ip;
ip.open (dlgFile, ios :: in);
if (ip)
ip >> *Main;
ip.close ();
Main->TransSettingsDlg.eetParameter ();
Main->TransSpeedDlg.setParameter ();
Main->TransDisplayDlg.setParameter ();
}

```

```

/*** Main Programme ******************************************************/
/************************************************************************/
int pASCAI WinMain(HINSTANCE hInstance, HINSTANCE hPrevInstance,
LPSTR lpCmdJine, int nCmdShow)
{
TRenewApp RenewApp("Renewable Energy Short Term Prediction",
hInstance, hPrevInstance, lpCmdLine, nCmdShow);
param = new param ( );
param->disFirstCurve = YES;
App = \&RenewApp;
GraphData = new Graph ( );
RenewAgp.Run();
delete (param);
delete (GraphData);
return RenewApp.Status;
}
/*** end of file *********************************************************/

```
```

        TransSettingsDlg.comZeta = TransJointDlg.zeta;
        TransMathsDlg.setParameter ( );
        TransSettingsDlg.setParameter ( );
        TransJointDlg.setParameter ( ):
        param->solBypass = 1; // set solar bypass
        testplot->open ( );
        testplot->clearScreen ( );
        testplot->close ( );
        if (GetModule()->ExecDialog(new TJointDistributionObject(this,"StatusWindow"))
            == IDOR)
        testplot->clear = NO;
    }
    }
void TMainWindow :: CMExport (RTMessage) {
int errno = OK;
if (GetModule()->ExecDialog (new TExportDialog (this, "Export")) == IDOK) {
if (TransExportDlg.OpNew m= YRS)
errno = exportData (GraphData->x, TransExportDlg.expFile, NEW,"".
GraphData->scale);
if (errno) {
for (int i=0;i<=GraphData->curveNo;i++) {
if ((errno = exportData (GraphData->y[i],TransExportDlg.expFile,
ATTACH,GraphData->legend[i],GraphData->scale)) == ERROR)
break;
}
if
if (terrno)
GetModule()->ExecDialog(new TYoMessage(this,"Message",
"Could not open specified file"));
}
}
void TMainWindow :: CMEelp (RTMessage) {
GetModule()->ExecDialog(new TYoMessage(this,"Message",
"Feature not implemented"));
}
ostream\& operator << (ostream\& outstr, RTMainWindow v) {
outstr << V.TransSpeedDlg << '\n';
outstr << v.TransSettingaDlg << '\n';
outstr << v.TransExportDIg << '\n';
outstr << v.TransDirDlg << '\n';
outstr << V.TransWindDIg << '\n';
outstr << v.TransSolarDIg << '\n';
outstr << V.TransJointDlg << '\n';
outstr << V.TransRandDlg << '\n';
outstr << V.TransMathsDig << '\n';
outstr << v.TransTsDlg << '\n';
outstr << V.TransFpDlg << '\n';
outstr << v.TransDisplayDlg << '\n';
retura outstr;
}
istream\& operator >> (istream\& instr, RTMainWindow v) {
instr >> v.TransSpeedDlg
>> v.TransSettingsDlg
>> v.TransExportDlg
>> v.TransDirDlg
>> v.TransWindDIg
>> v.TransSolarDlg
>> V.TransJointDlg
>> v.TransRandDIg
>> V.TransMathsDig
>> V.TransTsDlg
>> v.TransFpDlg
>> V.TraneDisplayDlg;
return instr;
}
/*** Application ***************************************************************

```

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[^0]:    Introduction

[^1]:    ${ }^{1}$ Refer to chapter 6 for further discussion of random variables and distribution functions.

[^2]:    ${ }^{2}$ Refer to chapter 6 for a discussion of the relationship between autocorrelation function and power spectrum of a stochastic process.

[^3]:    ${ }^{3}$ A random variable $X$ is said to be beta- distributed with the parameters $\alpha$ and $\beta$ if the corresponding probability distribution function is $\mathrm{F}(\mathrm{x})=\mathrm{I}(\alpha, \beta, \mathrm{x})$.

[^4]:    ${ }^{5} s\left(x-x_{0}\right)$ denotes the unit step function with the step at $x=x_{0}$.

[^5]:    ${ }^{6}$ Golden section search is after the Fibonacci routine the most efficient routine to find a minimum of a function of one variable, when an initial bracketing of the minimum is given.

[^6]:    ${ }^{7}$ Refer to chapter 6.2, for a discussion of functions of random variables.

[^7]:    ${ }^{8}$ Refer to chapter 6.2 for more details

[^8]:    ${ }^{9}$ Refer to chapter 6.6 for a discussion of random number generators.

[^9]:    ${ }^{10}$ Refer to chapter 7 for more details on the implementation of random generators and time series calculators (class TimeSeries).
    ${ }^{11}$ Algorithms to retrieve normal deviates are described in chapter 6.6.2.

[^10]:    Summary

[^11]:    ${ }^{12}$ Assume a stochastic process as an output of an experiment. The output is $s_{i}(t)$ as a function of time. The experiment is repeated $N$ times ( $i=1 \ldots N$ ). Now, the values of $s_{i}\left(t_{k}\right)(N$ values) can be put together in a sample k . A stochastic process is called ergodic if the statistical values of any sample coincide with the ones of any time function. It is worth noting that it can not be proved that a stochastic process is ergodic or not. It is more a conceptual idea. Ergodicity is, however, usually assumed as it enables to evaluate the autocorrelation in the time domain without knowing the joint probability distribution.

