

# Satellite or ground-based measurements for production of site specific hourly irradiance data: which is most accurate and where?

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## 1 Abstract

2 Site-specific satellite-derived hourly global horizontal irradiance is compared with that  
3 obtained from extrapolation and interpolation of values measured by ground-based weather  
4 stations. A national assessment of three satellite models and two ground-based techniques is  
5 described. A number of physiographic factors are examined to allow identification of the  
6 optimal resource. The chief influences are determined as: factors associated with latitude;  
7 terrain ruggedness; and weather station clustering/density. Whilst these factors act in  
8 combination, weather station density was found to be fundamental for a country like the UK,  
9 with its ever-changing weather. The decision between satellite and ground-based irradiance  
10 data based on accuracy is not straightforward. It depends on the exactitude of the selected  
11 satellite model and the concentration of pyranometric stations.

12 **Keywords:** global horizontal irradiance, national assessment of irradiance models, weather  
13 station density, kriging, satellite-derived irradiance, solar radiation.

## 14 1. Introduction

15 Solar radiation data has many applications, such as solar energy system performance and  
16 bankability assessment, building design of passive heating, cooling and daylighting elements,  
17 and resource assessment for agriculture and forestry. The most reliable i.e. lowest uncertainty  
18 source of solar radiation data is ground-based measurements by weather station networks  
19 and dedicated pyranometric stations (Sengupta et al., 2015). They measure the solar  
20 irradiance actually received at ground level, where solar systems are located. However, their  
21 reliability/uncertainty is conditional upon maintenance and calibration of the instruments.  
22 Pyranometer uncertainty must also be considered in the use of data.

23 This research investigates three methods to obtain solar radiation estimates for locations  
24 where it is not directly measured. The first is simply to allocate values from the single nearest  
25 measurement point. Here this method is termed “nearest neighbour extrapolation” (NNE) as  
26 in (Perez et al., 1997). Alternative names are “nearest neighbour interpolation”, “proximal  
27 interpolation” and “nearby station method”. The second method is to use an interpolation  
28 method based on the spatially weighted average of several neighbouring measurement  
29 locations. The third alternative approach is to model solar irradiance from cloud images  
30 captured by satellite. Like ground-based measurements, satellite data also has  
31 disadvantages. One shortcoming is lower accuracy at the specific weather location because  
32 the satellite data represents an area of the given pixel size, rather than an exact point.

33 There are no overall guidelines to direct the choice between ground-based or satellite  
34 irradiance data (Meteonorm, n.d.). This research sets out a data-informed methodology to aid  
35 the decision-making process and applies it to the UK as an example. It provides an extensive  
36 nationwide validation of these two solar irradiance data sources on an hourly basis. The case  
37 study area is the entire UK. This is a non-homogeneous region in terms of climate and  
38 topography and irradiance values vary significantly across the country.

39 Previous work has focused on distance from weather station as a deciding factor in the  
40 preferred choice of data source. As the distance between the point of measurement and  
41 location where data is required increases, the likelihood of divergence of weather conditions  
42 at the two sites also increases. In general, a distance decay effect may be observed, due to  
43 weather fronts and terrain. A theoretical distance is reached at which the decreasing accuracy  
44 of the ground-based data equals and then falls below the otherwise less accurate satellite-

45 modelled data. This cross-over or break-even distance was determined as 34 km for hourly  
46 averaged global horizontal irradiance (GHI) data in 1997 (Perez et al., 1997). This research is  
47 discussed in Appendix A.

48 This original work (Perez et al., 1997) referred to *nearest neighbour extrapolation* of ground  
49 data, whereas a number of well-known ground data sources (Meteonorm (Meteonorm, n.d.),  
50 PVGIS-classic (JRC, 2012)) use *geostatistical interpolation*. Interpolation techniques have  
51 been in existence for some time, but more powerful computers have enabled their widespread  
52 use and enhanced understanding. The last 20 years have seen considerable advances in  
53 satellite modelling also. Advances in networking and communication technology have led to  
54 increased availability of data of all types. In this context, this paper examines whether the  
55 historic break-even distance is still the best criterion on which to base a data source decision.

56 Other factors in the ground-based or satellite GHI data selection are: proximity to mountains  
57 and oceans; urbanisation (associated with high and changeable concentrations of aerosols  
58 and water vapour); high latitude; cloud cover (Hall and Hall, 2010; Perez et al., 2013; Suri and  
59 Cebecauer, 2014); and weather station density (Paulescu et al., 2013). The differences in  
60 accuracy of data derived from extrapolation/interpolation of ground-based sources and  
61 satellite-modelled data in these distinct regions have never (to the authors' knowledge) been  
62 quantified.

63 Both ground-based and satellite models are affected by orographic forcing when changes in  
64 elevation occur. When air is blown over mountains or hills, it is forced to rise. As it rises, it  
65 cools, becoming saturated with condensing water and forming a cloud, a phenomenon that is  
66 highly localised. Satellite models produce higher errors in coastal locations and are adversely  
67 affected by scattered cloud, especially at high latitudes (Perez et al., 2013). Broken cloud may  
68 mask the sun. Conversely, thin cloud close to the sun may enhance solar irradiance due to  
69 forward scattering (Yordanov et al, 2013). Current satellite instruments cannot distinguish  
70 small broken clouds from large thin cloud (Cebecauer et al., 2010).

71 Satellite values may also fail to distinguish clouds in the presence of bright surfaces e.g. snow  
72 or ice cover, and some types of vegetation. Interpolation of ground data is subject to edge  
73 effects. In the case of the UK, the coast is also the edge boundary of the weather station  
74 network and correlation might be expected. The temporal granularity of hourly weather station  
75 data is too coarse to reflect cloud movements. Thus, it is not at all clear which GHI data  
76 source provides the best accuracy in which geographic circumstance. This research will  
77 investigate this issue.

78 The accuracy of both ground-based and satellite-modelled GHI will be assessed in terms of  
79 root mean square error (RMSE) and mean bias error (MBE). The following comparisons will  
80 be made: (1) pair-wise comparison of weather station reading to nearest weather station  
81 value; (2) interpolated ground-measurement to nearest weather station record at various  
82 distances; and (3) interpolated ground versus satellite-derived values under differing  
83 geographic scenarios.

84 In the following, an assessment of solar irradiance models is carried out to direct the decision  
85 between the use of extrapolated/interpolated ground-measured or satellite-modelled  
86 irradiance data. First, the impact of distance to weather station is investigated, followed by the  
87 influence of other atmospheric and topographical factors as detailed above.

88 This paper is structured as follows. Section 2 describes the data employed and quality control  
89 procedures performed upon it. Calculation of distance decay errors is detailed. Section 3.1  
90 replicates former research with modern data. An investigation of the influence of distance on  
91 whether ground or satellite irradiance data is most accurate, is described. The previous  
92 research is then expanded upon and the results clearly visualised. Section 3.2 investigates  
93 the influence of atmospheric and topographic factors on whether ground or satellite irradiance  
94 data delivers the greater accuracy. These include locational and weather-related features.  
95 Finally, Section 4 summarises findings, interprets the results and offers conclusions.

## 96 2. Data and Methods

97 All data used is hourly global horizontal solar irradiance data for the complete year of 2014,  
98 unless otherwise stated. The case study area is the United Kingdom.

99 **2.1 Ground Data Description**

100 Ground-based solar irradiance measurements available as hourly averages are used from the  
101 UK Meteorological Office Integrated Data Archive System - MIDAS (UK Met Office, 2006).  
102 The UK Met Office currently has a network of over 80 automatic weather stations throughout  
103 the UK which observe irradiance as well as other meteorological conditions. Figure 1 and  
104 Figure 2 provide details of UK weather stations distribution. It may be seen that the  
105 distribution is somewhat uneven. 30% of the stations are clustered in the South East and  
106 Midlands i.e. approximately one-third of the weather stations are positioned in one-fifth of the  
107 nation. In other words, although stations are typically about 40 km apart, this can more than  
108 double, particularly in Wales and Scotland. The weather stations distance distribution has a  
109 small positive skew, with slightly more inter-station distances of less than 20 km and slightly  
110 fewer greater than 80 km.

111 The instruments at these stations are CM11/CMP11 (Kipp&Zonen) pyranometers, calibrated  
112 by reference to absolute cavity radiometers, traceable to the world radiation standard.  
113 Weather station sensors predominantly rely on rainfall for cleaning.

114

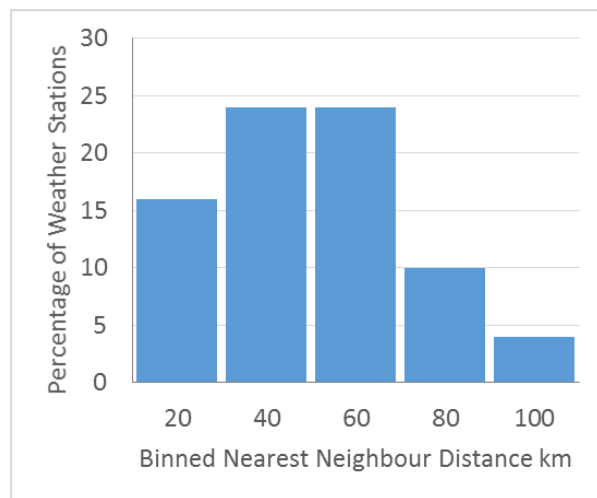


Figure 1: Map of Weather Stations Distribution

Figure 2: Histogram of Weather Stations Nearest Neighbour Distances

115

116 **2.2 Ground Data Methodology**

117 The UK Met Office apply quality control procedures to MIDAS data before release. Data  
118 inputs automatically undergo checks to ensure that they are correct and consistent with the  
119 surrounding data points on entry to the Meteorological Monitoring System. Observations are  
120 compared to location-dependant climatological extremes and previous records. The  
121 downloaded MIDAS data was then filtered to remove duplicates, flagged error values and  
122 values less than 0 W/m<sup>2</sup>. In addition, the following tests recommended by (Journée and  
123 Bertrand, 2011) were applied:

- 124 • The global horizontal solar radiation must be less than the extra-terrestrial value when  
125 the solar elevation angle is greater than 2 degrees.
- 126 • The global horizontal solar radiation must not exceed the European Solar Radiation  
127 Atlas clear sky value by more than 10% when the solar elevation angle is greater  
128 than 2 degrees.

129 It was determined that only 7 per 400,000 values were too high. This very small number of  
130 values was ignored.

131 The distance decay errors for nearest neighbour extrapolation and interpolation of data were  
132 calculated as follows. Firstly, the steps for NNE were: Take GHI values from two nearest  
133 neighbouring weather stations (1 and 2). Consider the value of station 2 to be unknown.

134 Accordingly, it becomes necessary to use the data from station 1. Validate the accuracy of  
135 station 1 data in these circumstances by comparing it to the real data from station 2. The  
136 distance decay is the distance between the two stations. This procedure is repeated for each  
137 closest weather station pair until all the data has been used. The RMSEs are plotted as a  
138 function of distance to nearest weather station. The NNE method is included in this research  
139 because this is the only method available to many GHI data users.

140 Secondly, interpolation distance decay errors were obtained. Interpolation takes the values  
141 from several weather stations surrounding the point of interest. These are input into a  
142 mathematical algorithm and weighted according to distance to the desired location to  
143 calculate a GHI value for the unknown site. This paper employs the kriging interpolation  
144 technique, detailed in Appendix B. The reduction in accuracy of interpolation due to distance  
145 decay is assessed by leave-one-out-cross-validation (LOOCV). This may be applied as  
146 follows: Interpolate with 79 weather stations and leave the 80<sup>th</sup> out. Compare the interpolated  
147 value obtained at the 80<sup>th</sup> station with the measured value from that site. (Calculate the  
148 RMSE). This is repeated for all stations (i.e. 80 times). Plot the RMSEs as a function of  
149 distance.

150 In this instance it is not sufficient to simply use the closest station distance to study loss of  
151 similarity between interpolated values with increasing distance. This is because GHI values  
152 from all weather stations are used in the kriging algorithm, not just those from closest to the  
153 location. Therefore, distance is obtained by re-using the kriging algorithm. The weather  
154 stations are treated individually. For each weather station, the distances to the other 79  
155 weather stations are calculated. These values are then interpolated to obtain a value for the  
156 weather station of interest. This is repeated for all stations. The average difference between  
157 the closest station distance and interpolated distance was 11 km, and the maximum 56 km,  
158 for the 79 weather stations.

### 159 *2.3 Satellite Irradiance Source*

160 Models which generate irradiance from satellite observations may be classified as physical  
161 (Miller et al., 2013) or hybrid (Perez et al., 2013). Hybrid models are also generally referred to  
162 as semi-empirical. Physical models utilise radiative transfer equations and require detailed  
163 information on the composition of the earth's atmosphere (e.g. cloud vertical distribution and  
164 optical properties, gridded aerosol properties and water vapour) as inputs. Obtaining data of  
165 sufficient quality for accurate results can be problematic. Hybrid models combine regression  
166 between satellite reflectance and corresponding ground measurements with a simplified  
167 radiative transfer algorithm.

168 Three models are investigated here. (1) CAMS (Schroedter-Homscheidt, 2016) utilises the  
169 Heliosat-4 physical model for satellite image-to-ground irradiance conversion. CAMS  
170 irradiance data is available at 15 minute, hourly, daily and monthly intervals. Hourly data only  
171 is analysed here, in order to be comparable with the ground-based MIDAS data. CAMS has a  
172 spatial resolution of 0.05° (5.6 km) and, in addition to satellite images, requires the following  
173 atmospheric data as inputs: aerosol properties, total column water vapour and ozone. These  
174 are obtained in the form of 3-hourly satellite-derived values and re-analysed via look-up tables  
175 to produce higher temporal resolution data, together with the shorter timeframe cloud satellite  
176 images. (2) SARAHE (Amillo et al., 2014) is a hybrid model, The data is available in hourly  
177 format. It has a spatial resolution of 0.05° and atmospheric input requirements similar to  
178 CAMS but uses long-term monthly modelled averages for the atmospheric data look-up  
179 tables. SARAHE data was available for 11 years (2005-2015). (3) Solargis (Cebecauer et al.,  
180 2010; Šuri and Cebecauer, 2012) also uses a hybrid approach. Solargis irradiance data is  
181 available at 15 minute, 30 minute, hourly, daily and monthly intervals. Again, hourly data only  
182 is analysed in this research. In addition to daily modelled values of atmospheric optical depth,  
183 water vapour and ozone (which are re-analysed to shorter time intervals), it includes snow  
184 index, snow depth, elevation and terrain shading in the model. Satellite elevation data is  
185 available at higher grid resolution, enabling Solargis to deliver a spatial resolution of 250 m.

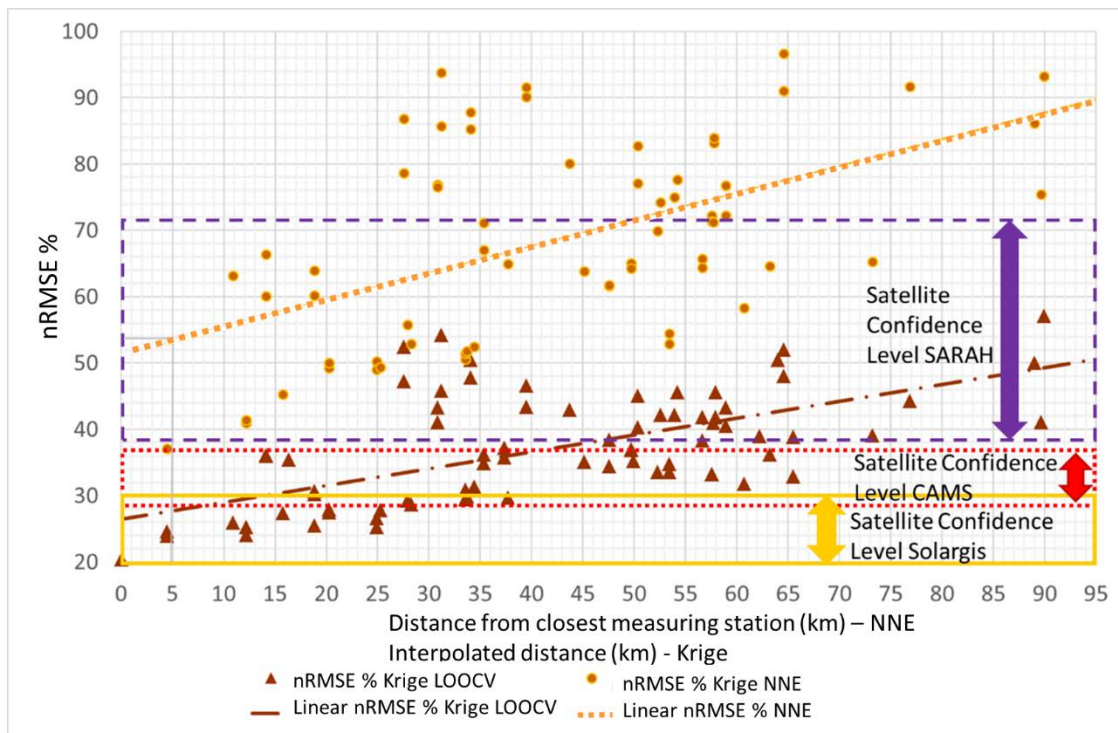
186 3. Results and Discussion

187 3.1 Influence of distance to weather station on ground or satellite irradiance  
188 data choice

189 3.1.1 Replication of earlier work

190 Initially, the example of (Perez et al., 1997) was replicated with modern data by plotting the  
191 nRMSE (normalised by mean of inputs) as a function of distance to produce a semi-  
192 variogram-like graph, illustrated in Figure 3. This same graph displays: (i) the nearest  
193 neighbour extrapolation nRMSE as a function of closest station distance; (ii) the kriging  
194 LOOCV nRMSE as a function of interpolated distance; and (iii) the satellite error level band  
195 for each of the three satellite models tested (CAMS, SARAH and Solargis). These satellite  
196 error ranges were taken from validation figures reported in the literature. Each model is  
197 compared to two UK BSRN stations, Lerwick and Camborne. Instruments at BSRN stations  
198 provide data of the highest available accuracy. Since these are at the UK's northern and  
199 southern extremities, nRMSE is considered to range between these values for the country as  
200 a whole.

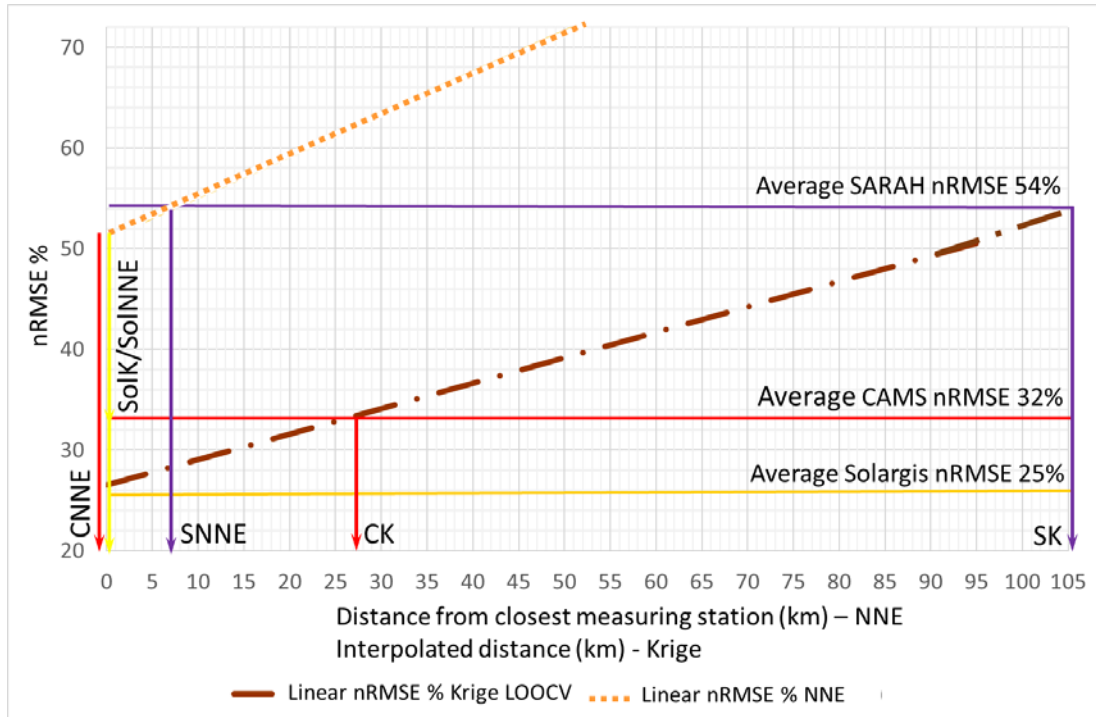
201 Similar to (Perez et al., 1997), the nRMSE is found to increase with distance. However, the  
202 points are widely distributed around the trendlines because of the variability of the UK's solar  
203 radiation field. The range of spread is almost twice as large in winter as in summer. Large  
204 NNE / interpolation errors still occur at short distances (large nugget) due to variable cloud  
205 cover. An alternative explanation for the spreading of points in Figure 3 is the possibility of  
206 poor ground data, for example, if the stations are not adequately maintained. This is the case  
207 with most networks of automatic weather stations in all countries, although the UK Met Office  
208 is a world-leading provider of weather information.



209

210 Figure 3: Satellite error relative to ground-based nearest neighbour extrapolation and kriging  
211 errors (including trends). Inter-station distances range from 600 m to 97 km.

212 Figure 4 is a simplified version of Figure 3, for ease of understanding. Trendlines only for  
213 nearest neighbour extrapolation nRMSE and kriging LOOCV nRMSE are marked (points  
214 removed). Satellite errors are shown as a single line for the average UK nRMSE % instead of  
215 a box for the nRMSE % range. (The satellite error average lines are placed at the halfway  
216 mark of the range boxes.) Break-even distances are labelled. The key to the labels is given in  
217 Table 1.



218

219 Figure 4: Satellite error relative to ground-based nearest neighbour extrapolation and kriging  
 220 trends.

221 It may be seen that modern data is far more plentiful than that available to researchers 20  
 222 years ago. Nonetheless, the inferences are less clear. Instead of one break-even distance,  
 223 there are six possibilities, one for each satellite model and NNE / kriging combination. In fact,  
 224 only three break-even distances exist in reality (Table 1). The CAMS and Solargis satellite  
 225 models are more accurate than NNE at all distances, on average. Solargis is also more  
 226 accurate than kriging at all distances, on average. This table suggests that for most  
 227 applications, NNE should not be used in the UK. Satellite data-derived data always delivers  
 228 results closer to reality beyond the break-even distance.

229 Table 1: Break-even distances for each satellite model and NNE / interpolation combination

Nearest Neighbour Extrapolation or Interpolation	Satellite Model	Distance in km of trendline at halfway interval of satellite confidence level box (average satellite model nRMSE)	Break-even distance label in Figure 4.
Nearest Neighbour Extrapolation	Solargis	0	SolNNE
	CAMS	0	CNNE
	SARAH	7	SNNE
Kriging	Solargis	0	SolK
	CAMS	27	CK
	SARAH	105	SK

230

231 Several deductions may be observed from Figures 3 and 4. First, it is apparent that, in  
 232 contrast to (Perez et al., 1997)' original work, kriging delivers a large improvement over  
 233 nearest neighbour extrapolation. This is because for the current work many more ground  
 234 station readings are available (80 plus as compared to 12 in 1997) and the sophisticated  
 235 kriging interpolation technique is employed, rather than (Perez et al., 1997)' simpler Inverse  
 236 Distance Weighting (IDW) interpolation. (IDW is necessary when data is sparse. Unlike  
 237 kriging, it does not calculate probability. Interpolation can only deliver accurate results with  
 238 more than 20-30 points (Huber, 2014).)

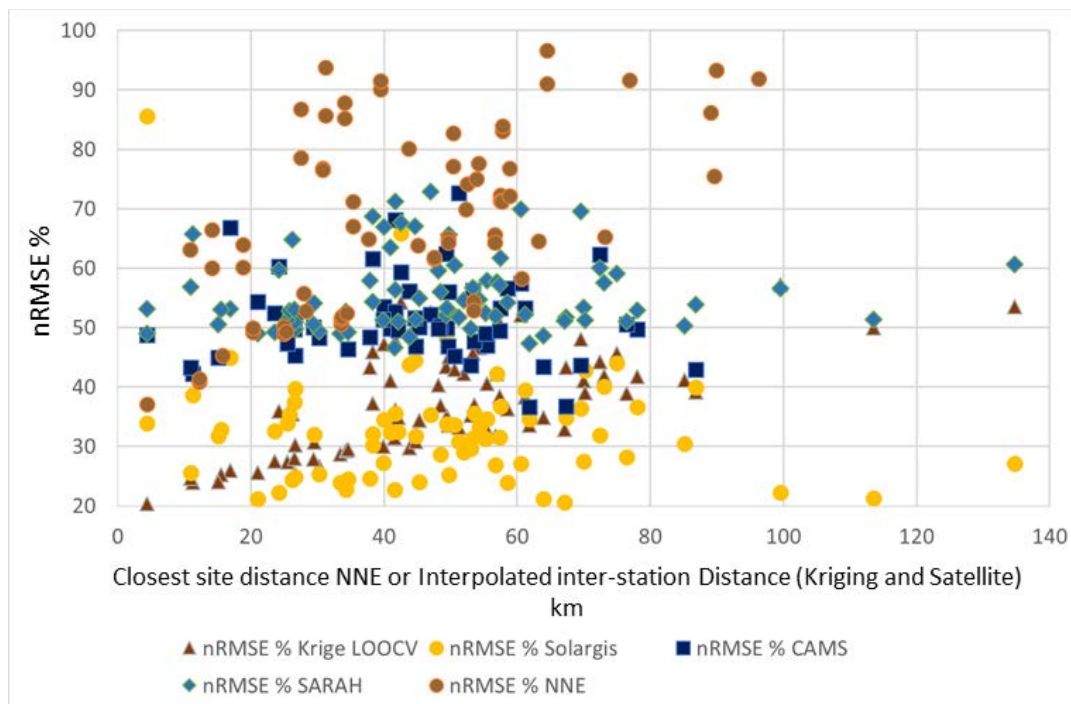


239 Second, satellite models generally perform better than nearest neighbour extrapolation. The  
 240 exception is the SARAH model at very low distances. Third, more satellite models are  
 241 available and the break-even distance is dependent on the model chosen. Fourth, the satellite  
 242 models have a wide confidence level because they are extensively validated at 80 or more  
 243 independent weather stations. ((Perez et al., 1997) had just one station available to them for  
 244 both parameterisation and evaluation.) Fifth, the break-even distances obtained are  
 245 influenced by the number of data points used, especially at the lower end of the distance  
 246 scale. Finally, the break-even distances are difficult to extract accurately off the graph due to  
 247 level of variation in the data.

### 248 3.1.2 Expansion of earlier work

249 With the benefit of modern computing power, the development of the internet, increased  
 250 availability of data and an extra 20 years' research into satellite modelling and kriging  
 251 techniques, it is possible to expand on the original work of (Perez et al., 1997). The data from  
 252 many more weather stations is available to the current researchers. In addition, MIDAS data  
 253 is entirely independent of ground-based data used for parameterisation of satellite models.  
 254 BSRN data is used for this purpose (BSRN, n.d.). The quantity of data also ensures the  
 255 independent validation of the kriging technique because leave-one-out-cross-validation is  
 256 possible. But perhaps the most significant step forward is the ability to compare NNE / kriging  
 257 nRMSE with satellite errors at over 80 weather stations (Figure 5). The 1997 authors had only  
 258 one weather station to calculate satellite error.

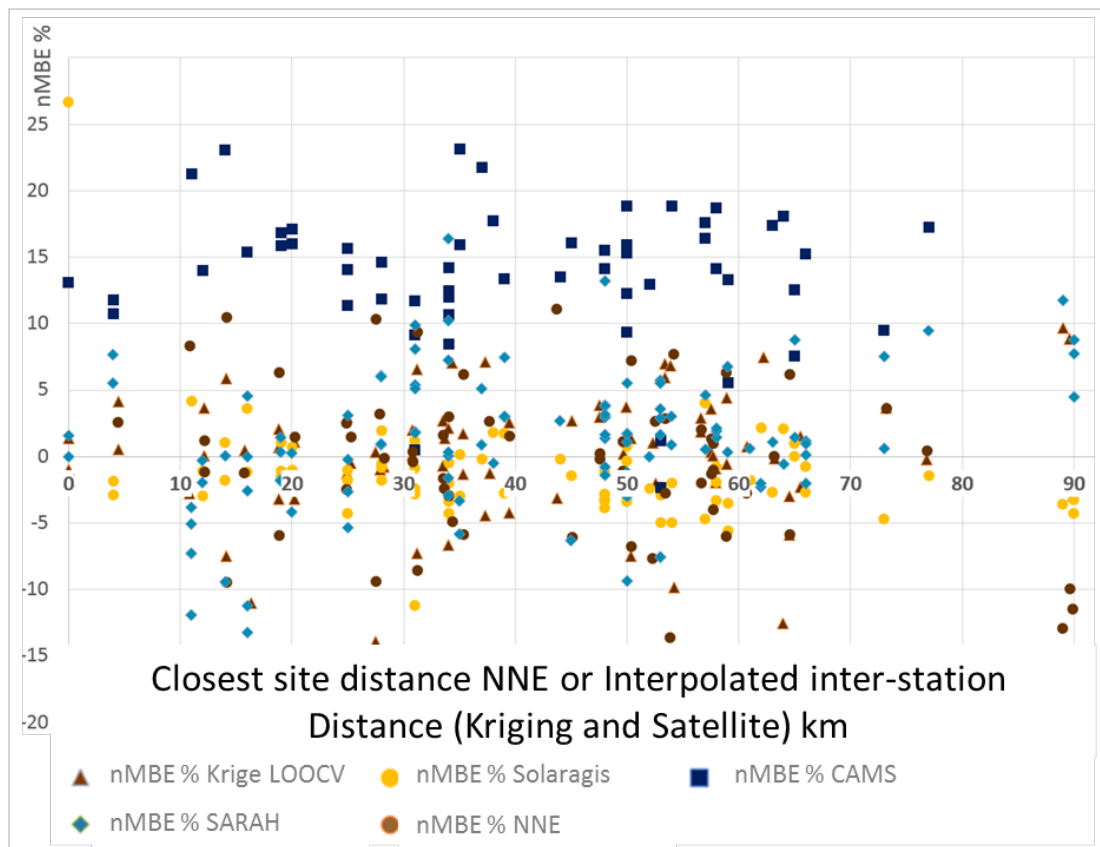
259 In contrast to Figures 3 and 4 which compare ground-based data to satellite confidence  
 260 intervals, Figure 5 compares extrapolated and kriged data errors at each weather station to  
 261 individual hourly satellite errors calculated for each same weather station. The nRMSE values  
 262 are calculated as follows. At each one of the 80 weather stations the pyranometric solar  
 263 irradiance value for all daylight hours in 2014 (5,116 hours) was obtained. The difference  
 264 between the measured irradiance value for every hour and the value provided by each of the  
 265 models (NNE, kriging and the three satellite-derived) was calculated. RMSEs were computed  
 266 from this, and then the nRMSE, normalised by the mean of inputs. The average nRMSE of all  
 267 the daylight hours at each weather station was calculated. The outliers in the Solargis data  
 268 arise as follows. The weather station at a distance of 4km is Heathrow. This is known to be  
 269 subject to reflections from passing aircraft and heat from the tarmac. The outlier at 42 km is in  
 270 the Scottish Highlands where the mountains and latitude are problematic for satellite data.



271

272 Figure 5: Satellite, NNE and kriging nRMSE at each weather station, plotted as a function of  
 273 increasing inter-station distance

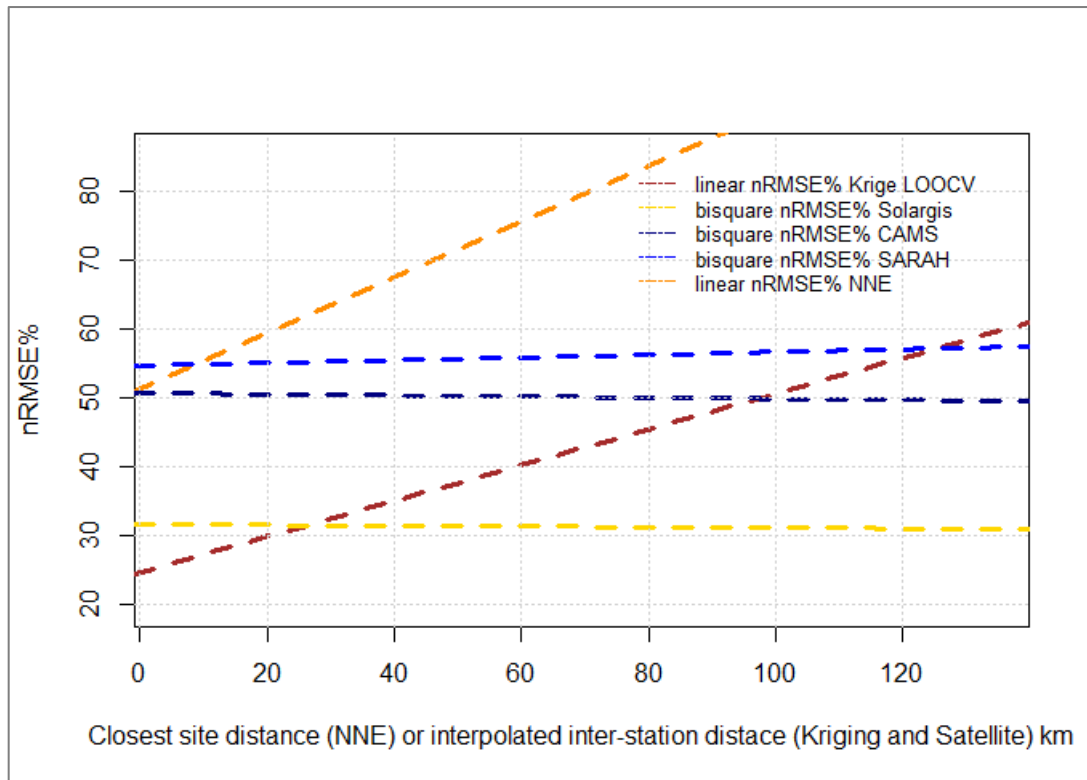
274 Figure 6 is similar to Figure 5, except that nMBE is compared to distance, rather than  
 275 nRMSE. It may be seen that the CAMS product exhibits positive bias, i.e. overestimation for  
 276 all stations. This has been reported several times e.g. (Copernicus, 2016). An empirical  
 277 CAMS radiation bias correction is available post-2017 (Copernicus, 2017). This reduces the  
 278 CAMS nMBE for UK weather stations to the same range as the other satellite models.



279

280 Figure 6: Satellite, NNE and kriging nMBE at each weather station, plotted as a function of  
 281 increasing inter-station distance





282

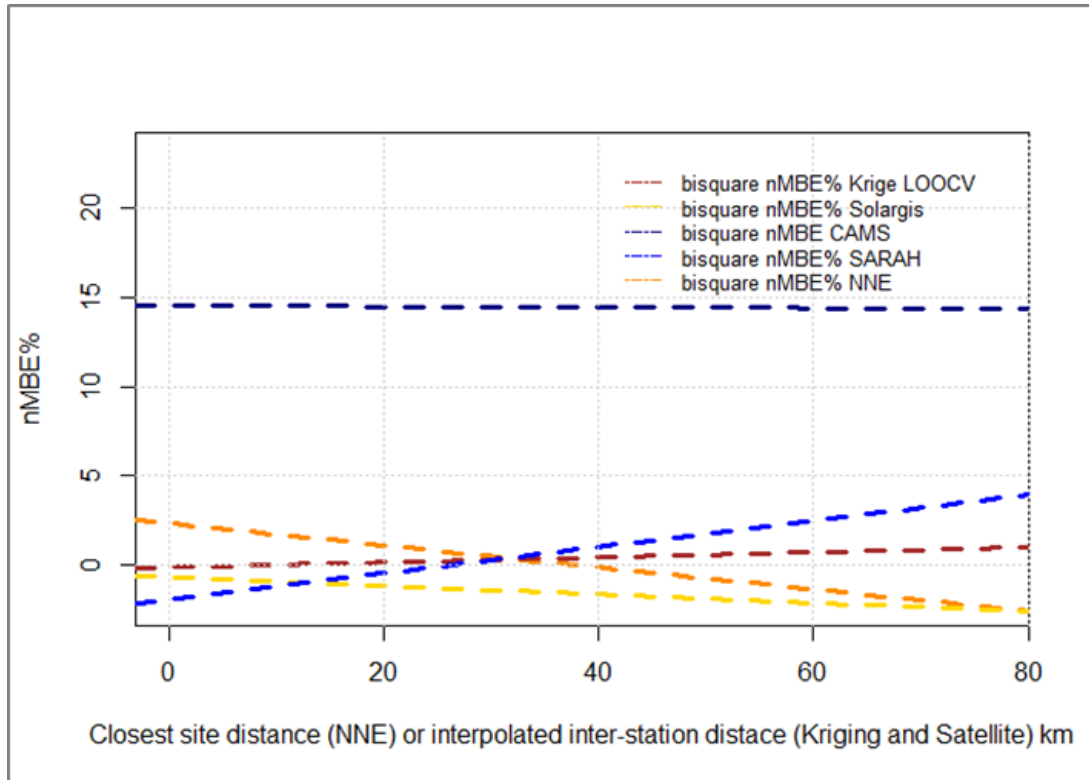
283 Figure 7: Trendlines of satellite, NNE and kriging nRMSE at each weather station, plotted as  
 284 a function of increasing inter-station distance (km). Robust regression used to remove  
 285 influence of outliers (Ripley, 2002).

286

287 Figure 7 again shows NNE / kriged and satellite nRMSE at each weather station but in the  
 288 form of trendlines, for ease of interpretation. Some interesting information may be gained from  
 289 Figure 7. The nRMSE of the NNE and kriging techniques rise steeply with increasing distance  
 290 to weather station, whereas the nRMSE of all the satellite models have flat trends. This is as  
 291 expected because the satellite data is not connected with the weather stations data. Again,  
 292 kriging outperforms NNE and satellite models are more accurate than NNE. (The exception is  
 293 SARAH which breaks even with NNE at 10 km.) The key difference between the initial work  
 294 with satellite confidence levels (Figure 3) and nRMSE at individual weather stations (Figure 6)  
 295 is the break-even distances obtained. These may be read from Figure 6 where the trendlines  
 296 cross. It may be seen that kriging breaks even with the SARAH model at 125 km and with  
 297 CAMS at 97 km. The furthest UK inter-station distance is 97 km and no point in the UK is  
 298 more than 113 km from the sea (Haran, 2003). In the context of the UK, these distances are  
 299 therefore not useful. (They could serve as guide to the applicability of SARAH and CAMS  
 300 data in larger or landlocked countries.) Kriging breaks even with Solargis at 25 km. This is in  
 301 agreement with other independent studies, which have shown Solargis to be the most  
 302 accurate of the satellite products they tested (Ineichen, 2014, 2011).

303 So, of the six possible break-even distances, only one (25 km with Solargis) applies to  
 304 conditions in the UK. (These conditions comprise ground data availability and impact of  
 305 weather on satellite models.) Kriging of ground-measured data provides higher accuracy than  
 306 the other satellite models (CAMS and SARAH) at all distances from weather stations.

307 Figure 8 repeats the analysis performed in Figure 7 but uses nMBE as a measure of error. All  
 308 nMBE values are within the range of pyranometer error ( $\pm 5\%$ ), with the exception of CAMS,  
 309 which has now been corrected to this range, as noted above.



310

311 Figure 8: Trendlines of satellite, NNE and kriging nMBE at each weather station, plotted as a  
 312 function of increasing inter-station distance (km). Robust regression used to remove influence  
 313 of outliers (Ripley, 2002).

314

### 315 3.1.3 Application of break-even distance to the ground / satellite data 316 decision

317 Having determined a break-even distance for kriging and satellite data in the UK, it is now  
 318 possible to visualise it. The appropriateness of break-even distance to the decision between  
 319 use of interpolated ground-measured or satellite-derived irradiance data will also be reviewed.

320 Figure 9 draws the areas in the UK which are within 25 km of a weather station. The concept  
 321 of break-even distance suggests that kriged data should be used inside the 25 km circles and  
 322 Solargis data outside. (Note: the map would be a single colour for SARA and CAMS  
 323 because the break-even for kriging is so large the areas run into each other. Kriging  
 324 outperforms SARA and CAMS for the whole of the UK.) Figure 9 implies that kriging delivers  
 325 greater accuracy in 56% of the UK and Solargis is more accurate in 44%.

326 It is important not to forget that the 25 km obtained is actually the *average* break even  
 327 distance. The actual break-even is different for each station and it is somewhat misleading to  
 328 generally apply the average. Figure 10 indicates that for two-thirds of weather stations,  
 329 Solargis is more accurate than kriging at the station. That is, in these locations, a zero break  
 330 even distance should apply. Evidently, a different method of comparing kriging and Solargis  
 331 errors is required.

332

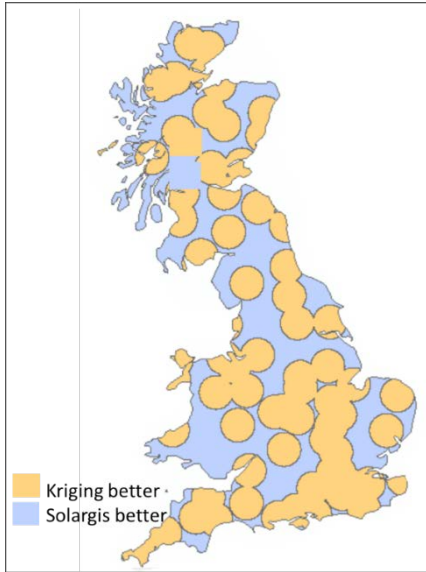


Figure 9: Map of 25 km average break-even distance between kriging and Solargis

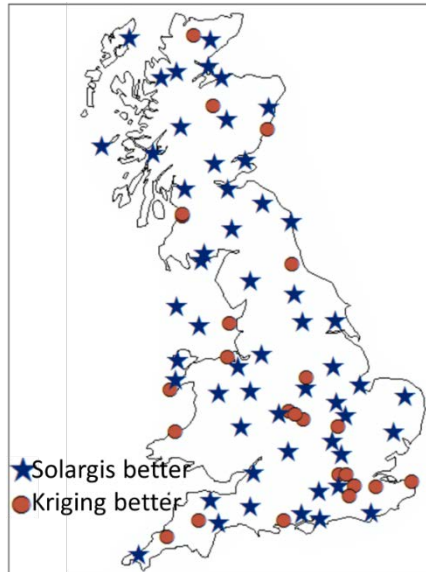


Figure 10: Map of weather stations showing whether the nRMSE of kriging or of Solargis delivers greater accuracy

333 Figure 11 displays the result of a two-stage process. The nRMSE of kriging and Solargis at  
 334 each weather station are interpolated. These two maps are then compared. If the interpolated  
 335 nRMSE of Solargis for a given pixel is less, Solargis is considered to be the best choice of  
 336 irradiance data for that pixel. Likewise, if the interpolated nRMSE of kriging for a given pixel  
 337 is less, kriging is considered to be the best choice of irradiance data for that pixel. This process  
 338 is repeated for the nMBE in Figure 12.

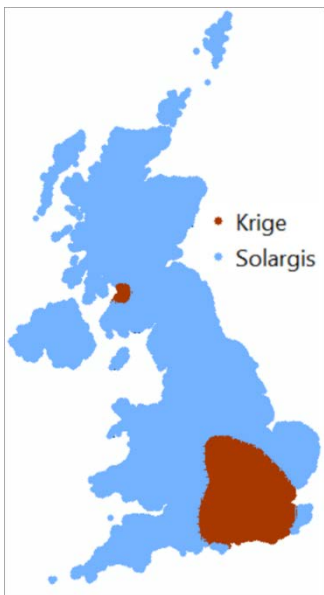


Figure 11: Areas of the UK where either kriging or Solargis offer highest accuracy, in accordance with their interpolated nRMSE

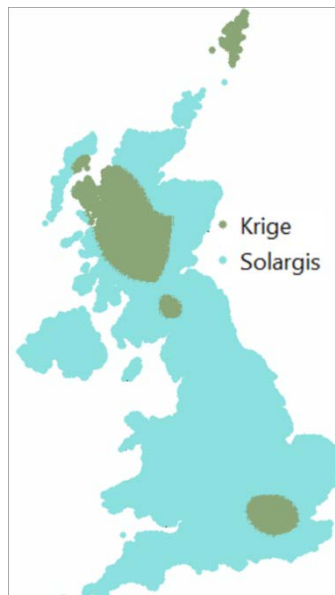


Figure 12: Areas of the UK where either kriging or Solargis offer highest accuracy, in accordance with their interpolated nMBE

339 It may be seen that there is a slight correlation between the interpolated errors in Figures 11  
 340 and 12 and the break-even distances in Figure 9 in the southeast of the country. Average  
 341 break-even is an approximate template for selection of the irradiance data source. Figures 11  
 342 and 12 suggest that kriging is most accurate where weather stations cluster in the centre and  
 343 southeast. Solargis is less accurate in the north, in terms of nMBE. This could be due to  
 344 increasing latitude or due to this being a mountainous region. These factors, together with  
 345 other geographic influences, are investigated in 3.2. In contrast to the break-even technique

346 in Figure 9, interpolation of nRMSE (Figure 10) reveals that, in reality, kriging is more  
 347 accurate than Solargis in just 14% of the UK.

### 348 3.1.4 Pyranometer Uncertainty

349 Figures 5 and 7 show that Solargis is the most accurate source of irradiance data, of those  
 350 tested, followed by kriging. Solargis outperforms kriging at two-thirds of weather stations (Fig.  
 351 10). Yet the mean difference between the two approaches is low: 32 kWh/m<sup>2</sup> or 4%. This  
 352 section briefly investigates whether the differences are large enough to be outside the bounds  
 353 of pyranometer uncertainty. (A more detailed investigation will be the subject of further  
 354 research.)

355  
 356 Uncertainty varies with the environment and instrumentation set-up (Strobel et al., 2009).  
 357 Instrumentation 1 in (Strobel et al., 2009) is equivalent to the MIDAS data sensors. The  
 358 uncertainty boundaries modelled for Instrumentation 1 for Northern Europe by (Strobel et al.,  
 359 2009) were applied to one year of kriged MIDAS data. It was found that kriged values and  
 360 those of the Solargis satellite model only agreed within the range of pyranometer uncertainty  
 361 for 17% of daylight hours in 2014. This limited correlation did not correspond to any particular  
 362 irradiance values, date or time. Thus, Solargis seems genuinely the best model for the  
 363 majority of the UK. Differences cannot be explained by bounds of measurement uncertainty.

### 364 3.2 Influence of atmospheric and topographic factors on ground or satellite 365 irradiance data choice

366 The following criteria were compared to nRMSE of the three satellite models and of the kriged  
 367 data: latitude; mean sea level pressure; distance to coast; clearness index and precipitation  
 368 (as representatives of cloudiness); urbanisation; cloud cover; landform; and weather station  
 369 distribution. The results are summarised in Figure 23 and Tables 2 and 3.

370

371 Table 2: Influence of Distance to Weather Station, Atmospheric and Topographic Factors on  
 372 Irradiance Models

RELATIONSHIP	R SQUARED			
	Solargis	Krige	CAMS	SARAH
MSLP against nRMSE % **	0.00	0.52	0.01	0.45
Air Mass against nRMSE %	0.00	0.53	0.00	0.48
Latitude against nRMSE %	0.00	0.50	0.00	0.40
Distance to Weather Station against nRMSE %	0.00	0.47	0.00	0.00
Total Cloud against nRMSE %	0.02	0.38	0.09	0.46
no. stations in 100 km grid sq against nRMSE %	0.00	0.33	0.00	0.00
Kt against nRMSE %	0.12	0.20	0.07	0.46
Precipitation against nRMSE %	0.00	0.15	0.08	0.14
Std Slope against nRMSE %	0.05	0.13	0.05	0.05
Relative Humidity against nRMSE %	0.05	0.12	0.01	0.00
Distance to Coast against nRMSE %	0.01	0.06	0.01	0.01
AMSL against nRMSE % *	0.05	0.06	0.08	0.07
Azimuth against nRMSE %	0.03	0.03	0.03	0.00
Hillshade against nRMSE %	0.03	0.02	0.00	0.01
no. stations in 45 km radius against nRMSE %	0.00	0.02	0.00	0.00
* Altitude above mean sea level				
** Mean sea level pressure				

373  
374

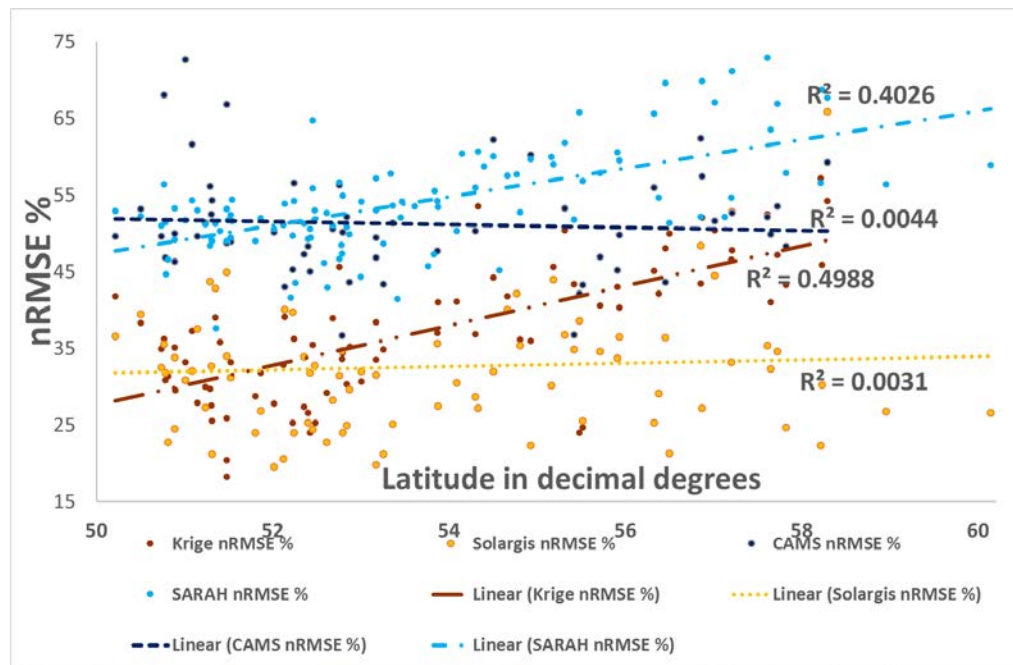
Table 3: Relationships between Geographic, Atmospheric and Topographic Factors in the UK

RELATIONSHIP	R SQUARED
Latitude against Kt	0.41
Longitude against Kt	0.09
AMSL against Kt *	0.06
Std Slope against Kt	0.00
Latitude against Air Mass	1.00
Latitude against MSLP **	0.91
Latitude against Total Cloud	0.17
Longitude against Total Cloud	0.14
Latitude against Relative Humidity	0.04
Latitude against no. stations in 45 km radius	0.11
Latitude against no. stations in 100 km grid sq.	0.10
Latitude against Distance to Weather Station	0.03
* Altitude above mean sea level	
** Mean sea level pressure	

375  
376  
377

3.2.1 Influence of Latitude, Coast, Precipitation, and Urbanisation

378 Figure 13 illustrates the relationship between nRMSE of irradiance model and latitude.



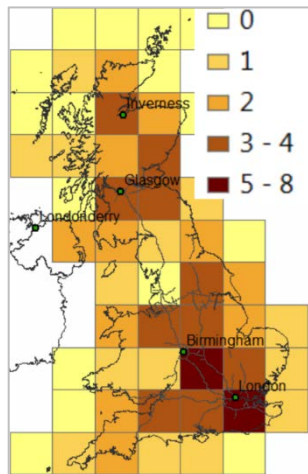
379  
380  
381

Figure 13: Trendlines of satellite and kriging nRMSE at each weather station, plotted as a function of latitude

382  
383  
384  
385

It may be seen that the performance of SARA and kriging vary with latitude, CAMS and Solargis much less so. Latitude is known to have a negative effect on satellite models, due to parallax. The more sophisticated CAMS and Solargis models handle this better. The apparent influence of latitude on the kriging model is probably a result of the north of the UK being

386 more mountainous and having fewer weather stations (see sections 3.2.2 and 3.2.3). These  
 387 factors cannot be separated in the UK. The statistical significance of decrease in number of  
 388 weather stations with latitude (Table 3) is slender. Distribution of stations can be explained by  
 389 population density and accessibility (Kilibarda et al., 2015), which in turn are influenced by  
 390 terrain. In the UK these tend to decrease northwards but the exceptions are the cities of  
 391 Glasgow and Edinburgh in southern Scotland. Figure 14 compares weather station  
 392 distribution in terms of count per Ordnance Survey 100 km grid square with major cities and  
 393 the motorway network.

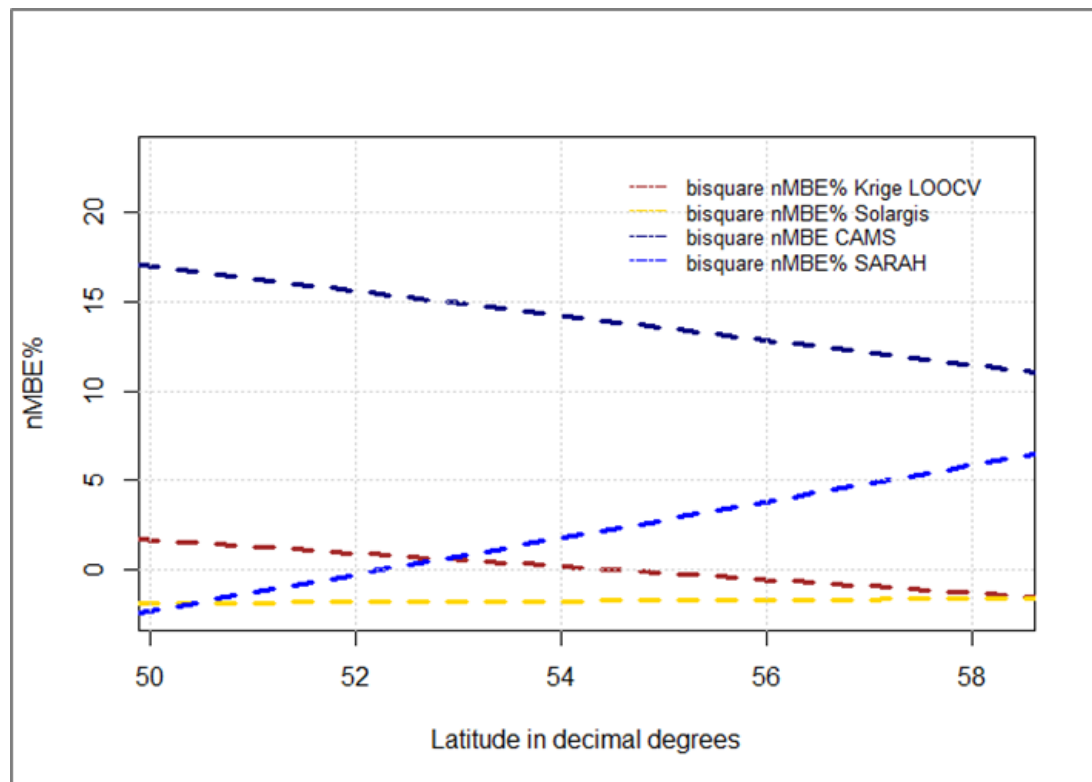


394

395 Figure 14: Count of weather stations per Ordnance Survey 100 km grid square

396

Figure 15 plots the relationship between nMBE of irradiance model and latitude.



397

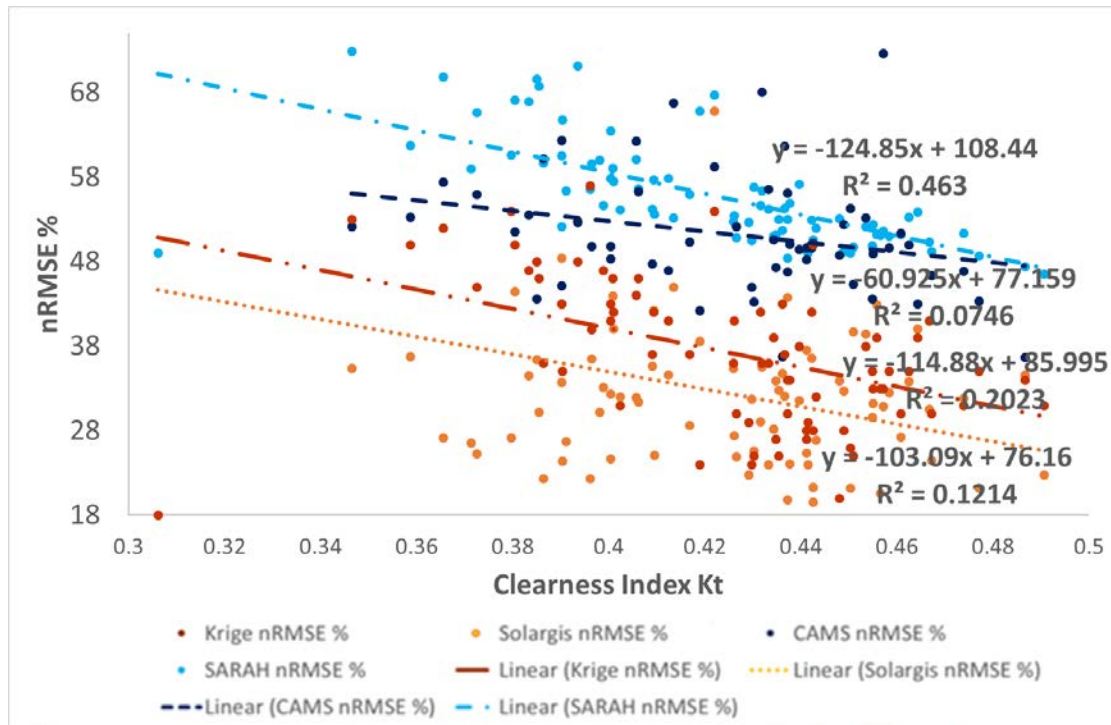
398 Figure 15: Trendlines of satellite and kriging nMBE at each weather station, plotted as a  
 399 function of latitude. Robust regression used to remove influence of outliers (Ripley, 2002)

400

With the exception of CAMS (now corrected), the nMBE of all irradiance models is within  
 401 pyranometer error. The unanticipated phenomenon of CAMS nMBE decreasing northwards in  
 402 the UK is in agreement with the map produced by (Wald, 2017).

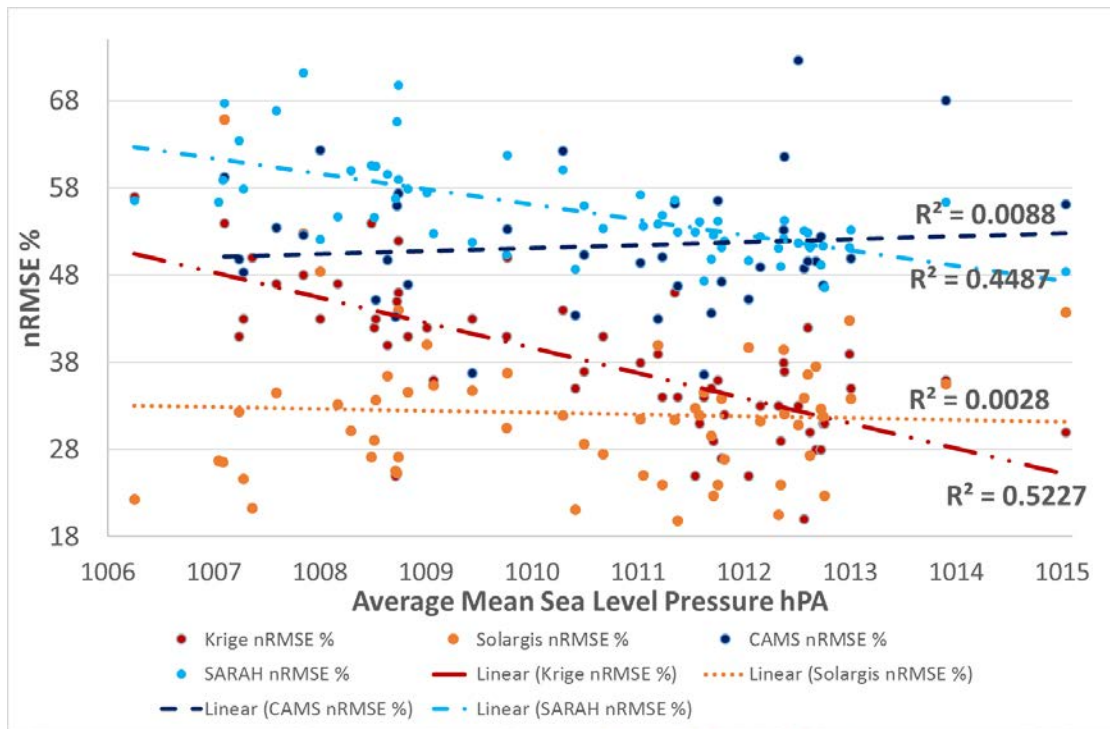


403 Higher latitudes may also be associated with increased cloud cover or cloud variability  
 404 (Wetherald and Manabe, 1986). In the UK, this was indeed found to be the case. A statistical  
 405 test showed an association between clearness index, Kt, (hourly GHI as a fraction of  
 406 extraterrestrial irradiance), and latitude ( $R^2 = 0.41$ ) A comparison of nRMSE with Kt found that  
 407 all models show increased accuracy with clearer skies (Figure 16). SARAH shows a greater  
 408 increase in accuracy with clearer skies than the other models.



409  
 410 Figure 16: Average hourly nRMSE % per site for 2014 as a function of average hourly  
 411 clearness index, Kt per site

412 Another factor linked to latitude in the UK is atmospheric pressure (mean sea level pressure)  
 413 ( $R^2 = 0.91$ ). Low pressure areas, formed between the tropical and polar air masses in the  
 414 Atlantic, approach the UK from southwest to northeast, due to the west to east direction of the  
 415 upper Polar Front Jet Stream. The correlation between nRMSE of irradiance model and mean  
 416 sea level pressure is shown in Figure 17. SARAH and kriging both show some negative  
 417 correlation with pressure. That is, the model errors decrease as the pressure increases. High  
 418 pressure reduces the formation of cloud, so these two models are performing better under  
 419 stable, clear conditions. This has already been seen with the clearness index. MSLP has little  
 420 influence on CAMS and Solargis nRMSE because these models are more resilient in the  
 421 presence of cloud.



422

423 Figure 17: Average hourly nRMSE % per site for 2014 as a function of average Mean Sea  
 424 Level Pressure per site

425 Plots of nRMSE % at weather station against distance to coast delivered flat trends in all  
 426 cases. Proximity to coast is known to impact satellite models. The UK is entirely coastal in  
 427 terms of coastal cloud formation and maritime aerosols, so no deductions are possible in this  
 428 case. Definitions of 'coastal' vary being between 80 and 100 km of shoreline (NOAA Office for  
 429 Coastal Management, 2016; Small and Nicholls, 2003). The furthest point from tidal water in  
 430 the UK is only 72 km away (Haran, 2003).

431 A weak association between precipitation and modelled irradiance values was detected. The  
 432 weakness of the association is due the fact that cloud cover in the UK frequently does not  
 433 result in rain. The connection between relative humidity and irradiance model errors was  
 434 likewise found to be slight. Aerosols must also be present for clouds to form (Appendix C).  
 435 Kriging does not account for cloudiness at all, whilst Solargis has several innovations which  
 436 improve its performance (GeoModelSolar, 2012).

437 An attempt to correlate RMSEs of modelled irradiances with rural urban classification  
 438 (DEFRA, 2013) proved inconclusive. This is probably due to the fact that no UK weather  
 439 station is more than 32 km from an urban area.

### 440 3.2.2 Cloud Cover

441 As noted in Section 3.2.1, higher latitudes may be subject to persistent cloudiness and the  
 442 frequent appearance of broken clouds. Hourly cloud cover and cloud type (measured in  
 443 oktas) from (UK Met Office, 2006) were analysed. The statistical relationship between  
 444 average hourly cloud cover and UK latitude is not strong ( $R^2 = 0.17$ , Table 3). The cloud cover  
 445 to longitude association is even less convincing ( $R^2 = 0.04$ ). This is probably because broken  
 446 cloud (5-6 oktas) prevails across the majority of the country 90% of the year. However,  
 447 interpolation of average hourly cloud cover for 2014 from 286 weather stations (Figure 18)  
 448 illustrates a visual link between cloud cover, latitude and longitude. Cloud amount increases  
 449 from the southeast to the northwest. Comparison of Figure 18 with the nRMSE % distributions  
 450 of the satellite and kriging algorithms in Figures 20 and 21 also suggests causality between  
 451 cloud cover and modelled irradiance error. This is especially clear in the cases of kriging and  
 452 SARA ( $R^2 = 0.38$  and  $0.46$  respectively, Table 2).

453



454

455 Figure 18: Map of interpolated average hourly cloud cover (2014)

456 A study of latitude and cloud type indicates a stronger relationship between medium cloud  
 457 and latitude than either low or high cloud (Table 4). The way the different clouds form may  
 458 explain this observation. Low clouds e.g. cumulus and stratocumulus clouds form over land  
 459 when the air is heated by the ground and rises. The air temperature drops and water vapour  
 460 condenses. This effect will occur nationwide. Low stratus cloud results from orographic  
 461 forcing, with presence of British mountains being linked to latitude. Mid-atlantic depressions  
 462 which track across the UK from southwest to northeast generate the following sequence of  
 463 cloud cover as they pass through: high, then medium and finally low. The cloud composition  
 464 on the weather fronts differs according to air stability and atmospheric temperature gradients  
 465 (AQA, n.d.).

466 Table 4: R Squared value for relationship between cloud types and latitude

RELATIONSHIP	R Squared
Latitude against Low Cloud	0.06
Latitude against Medium Cloud	0.13
Latitude against High Cloud	0.02

467

468 Comparison of cloud type and solar irradiance models reveals that all models are influenced  
 469 by low cloud to approximately the same extent (Table 5). Low cloud provides the largest  
 470 average contribution to overall cloud cover in the UK (average low cloud = 5 oktas, average  
 471 medium cloud = 2 oktas, average high cloud = 1 okta.) Solargis, kriging and SARAH are  
 472 influenced by low cloud rather than by medium or high cloud. Low level stratus cloud can  
 473 cover most of the sky, medium level altostratus allows more penetration of irradiance,  
 474 whereas high level cirrus is wispy (UCAR, 2012). CAMS shows a different pattern of cloud  
 475 type influence, possibly due to its more frequent aerosol optical depth input.

476 Table 5: R Squared value for relationship between cloud types and modelled irradiance errors

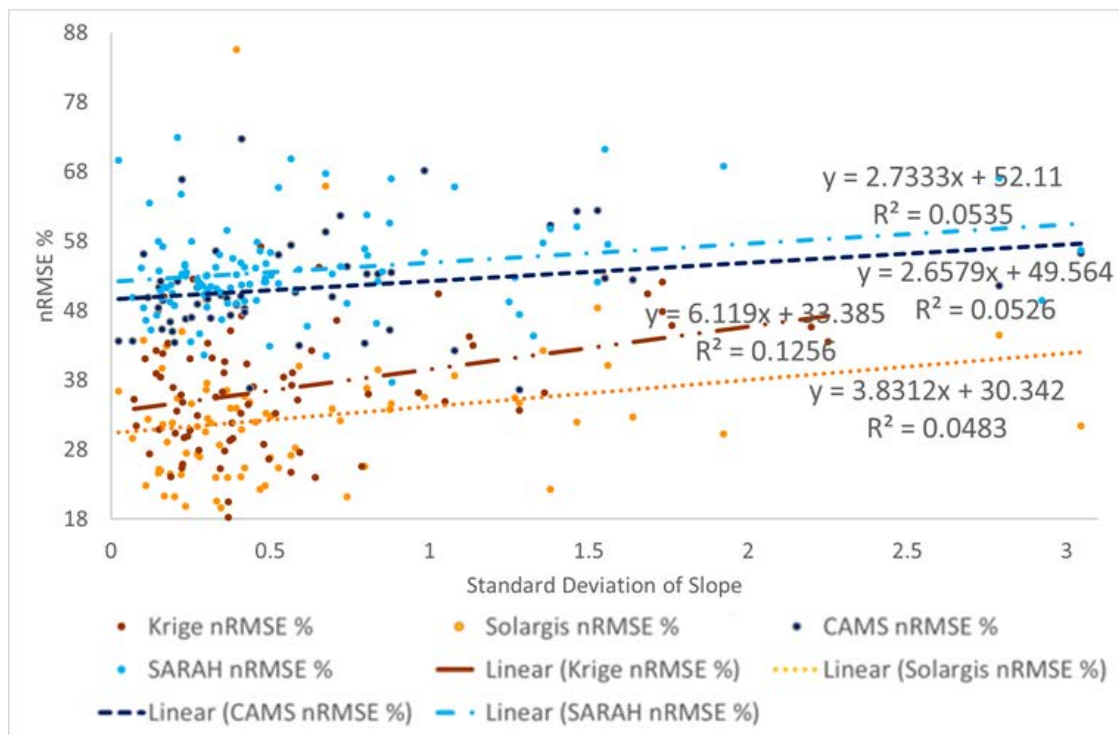
RELATIONSHIP	Solargis	Krige	CAMS	SARAH
Total Cloud against nRMSE %	0.02	0.38	0.09	0.46
Low Cloud against nRMSE %	0.27	0.31	0.36	0.3
Medium Cloud against nRMSE %	0	0	0.66	0.12
High Cloud against nRMSE %	0	0	0.54	0

477

478 3.2.3 Landform

479 Typical landforms include hills, mountains and plains. Landforms may be categorised by  
 480 several physical attributes; the ones of interest to this research are elevation (altitude above  
 481 mean sea level - AMSL) and change of elevation (or lack of). Change of elevation is  
 482 associated with slope, aspect and prominence (height above lowest contour line) i.e. terrain  
 483 ruggedness. AMSL in the UK is low, compared to most other European countries. Even so,  
 484 there are over 3,000 mountains in the U.K. with a minimum height of 2,000 feet (610 m),  
 485 There are also more than 16,000 “tumps” with a prominence of 30 m (Jackson et al., 2017).

486 A plot of nRMSE against AMSL revealed a weak relationship (slope of 0.02) for all models.  
 487 Therefore terrain ruggedness was investigated. There are several ways to quantify  
 488 topographic ruggedness (Cooley, 2016). Here standard deviation of slope is used because it  
 489 performs well at all scales and is conceptually simple (Grohmann et al., 2011). The slope data  
 490 used was the Shuttle Radar Topography Mission (SRTM) 90 m cell size digital elevation grid  
 491 (Pope, 2017). Figure 19 indicates that all models are disadvantaged by complex terrain.  
 492 Kriging is more impacted than the satellite models because it does not interpolate in the z  
 493 plane. This may also be seen in Table 6 which averages nRMSE % inside and outside of  
 494 Less Favoured Areas (LFA). These are EU-defined mountainous and hill farming areas (EU,  
 495 2013).



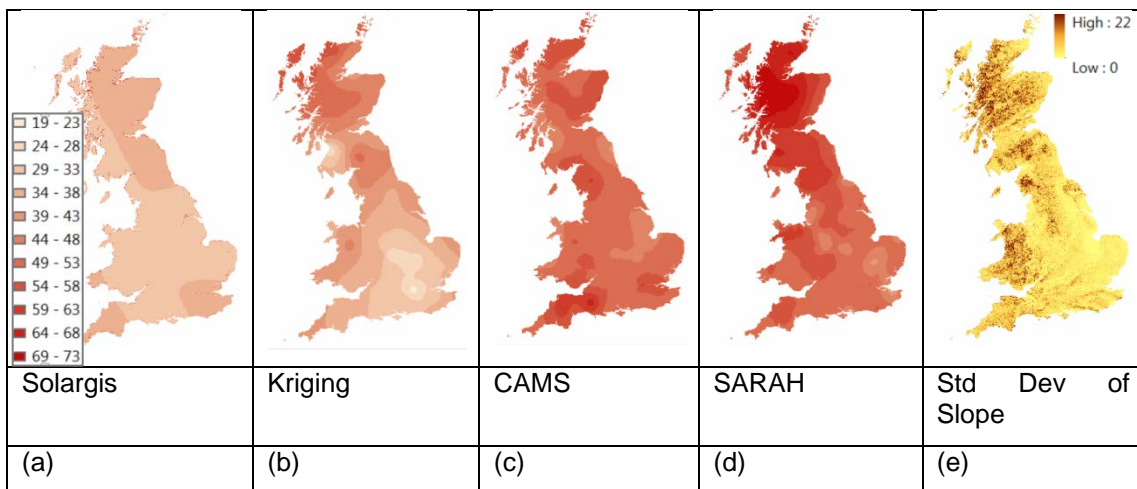
496  
 497 Figure 19: Trendlines of satellite and kriging nRMSE at each weather station, plotted as a  
 498 function of Standard Deviation of Slope

499  
 500 Table 6: Average nRMSE % inside and outside of Less Favoured (hill and mountain) Areas.  
 501

	Average nRMSE % in LFA	Average nRMSE % outside of LFA
Krige	44	34
Solargis	34	32
CAMS	54	50
SARAH	58	53

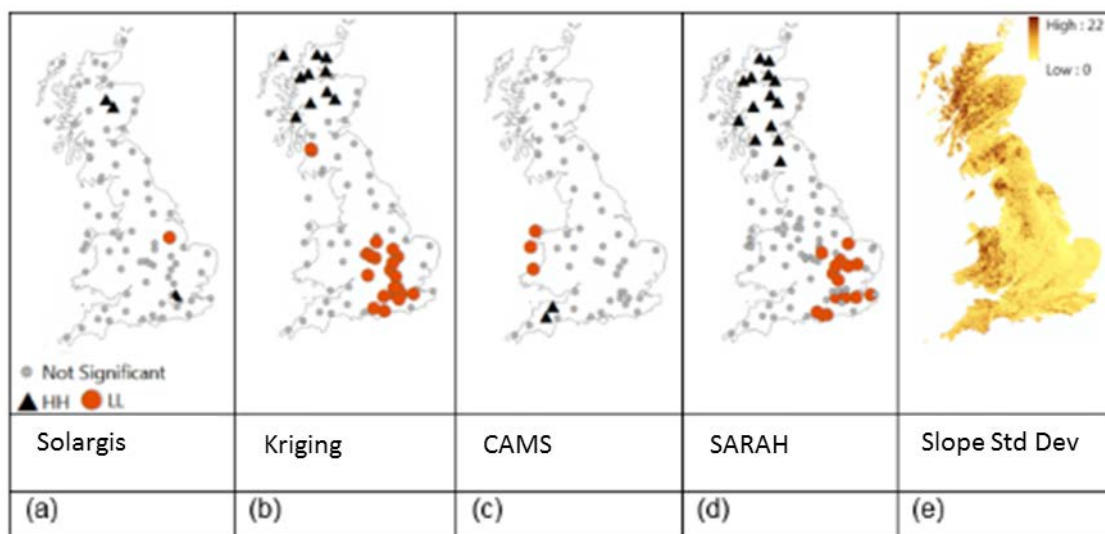
503 An investigation was carried out to establish the relationship between standard deviation of  
 504 slope and the clearness index. In theory, cloudiness should increase with terrain complexity  
 505 due to orographic forcing. In fact, the resultant graph based on UK data showed no link  
 506 between these variables (flat trend). A Kt/elevation plot was also non-conclusive. The  
 507 influence of terrain ruggedness on solar irradiance models in the UK must be due to another  
 508 associated factor. Hillshade was generated using ArcGIS software (ESRI, 2014). All the  
 509 models show a non-significant reduction in error as shadowing decreases. When azimuth was  
 510 studied, the kriging model nRMSE displayed a non-significant relationship. None of the  
 511 satellite models showed any correlation to azimuth. The connection between terrain and  
 512 irradiance appears to be complex and not easily explained with hourly data (Tables 2 and 3).

513 Figure 20 illustrates the nRMSE % for each modelled irradiance value at each weather station  
 514 in interpolated format (for ease of interpretation). The nRMSE maps are compared to terrain  
 515 ruggedness in the form of a map of standard deviation of slope. It can be seen that kriging  
 516 and SARAH have high errors in areas of complex terrain (mountains) and lower errors in flat  
 517 regions, whereas Solargis is robust against topographic features.



518 Figure 20: Maps of interpolated nRMSE % of satellite and kriging algorithms compared to  
 519 map of Standard Deviation of Slope

520 Figure 21 investigates the degree to which errors at adjacent weather stations are similar for  
 521 each irradiance model. Anselin Local Moran's I index is calculated, mapped and compared to  
 522 the map of terrain ruggedness. Anselin Local Moran's I allows identification of spatial groups  
 523 of objects with features of the same magnitude (Anselin, 2010; Renard, 2017). This index  
 524 enables statistically significant groups with high (HH) and low (LL) error values to be  
 525 distinguished. Again, in the cases of kriging and SARAH, a link with terrain ruggedness is  
 526 detected.





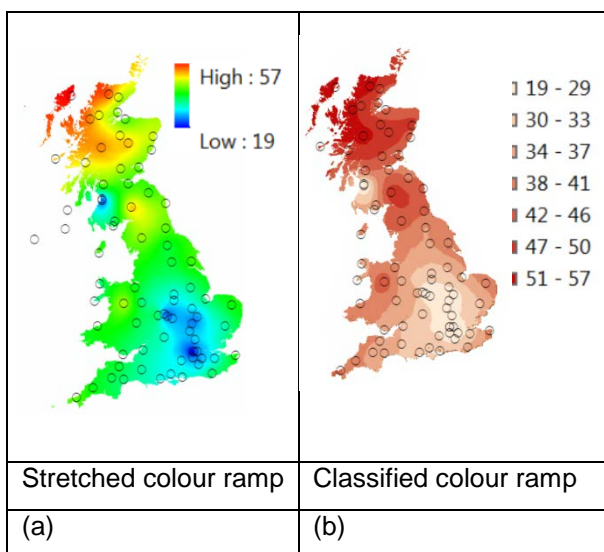
528 Figure 21: Maps of Anselin Local Moran's I index at each weather station for satellite and  
 529 kriging algorithms compared to map of Standard Deviation of Slope

530 There is another way in which terrain may influence solar irradiance. As altitude above mean  
 531 sea level (AMSL) increases, the atmosphere becomes thinner (less pressure). Thus the total  
 532 amount of water vapour the atmosphere can potentially hold is decreased and more solar  
 533 irradiance penetrates at higher altitudes. However, increases in daily totals of global  
 534 irradiance with altitude have been reported as 6-10% per 1000 m (Blumthaler et al, 1997).  
 535 The difference in ground height between the highest and lowest UK weather station is only  
 536 360 m. Therefore, altitude effect could only account for a small percentage of changes in the  
 537 UK solar irradiance data.

538 Absolute humidity (mass of water vapour in a unit volume of air kg/m<sup>3</sup>) was calculated from  
 539 MIDAS weather station values for relative humidity and temperature using the NOAA Moisture  
 540 Calculator (Padfield, 2013). The trend for water vapour to decrease with rising elevation in  
 541 the UK is slender ( $R^2 = 0.01$ ). When absolute humidity is compared to irradiance model  
 542 errors, no relationship was found for any of the satellite models (flat trends). This suggests  
 543 that they all address altitude effects well. In the case of kriging, nRMSE decreases with  
 544 increasing water vapour content ( $R^2 = 0.5$ ), in contrast to expectations. Also, plotting average  
 545 hourly global horizontal irradiance against weather station AMSL gave a slight anticorrelation  
 546 ( $R^2 = 0.02$ ). These last two statistics suggest that, in upland areas in the UK, the effect of  
 547 irradiance increasing with altitude is outweighed by cloud formation associated with rising  
 548 terrain.

549 **3.2.4 Weather Station Distribution**

550 Maps of interpolated nRMSE for the irradiance values from the kriging algorithm were  
 551 generated, with colour ramps optimised to the kriging error values (Figure 22). These were  
 552 overlaid with the location of weather stations. There is a clear visual link between clustering of  
 553 weather stations and low errors. (There is, of course, no relationship between clustering of  
 554 MIDAS stations and any of the satellite models because these do not utilise MIDAS data.)



555 Figure 22: Maps of interpolated nRMSE % of kriging algorithms overlaid with weather station  
 556 location

557 Several techniques were experimented with to ascertain how to quantify this link  
 558 mathematically. Weather station density and neighbour count in distance band gave the  
 559 simplest and most reliable results (Table 7).

560  
 561  
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 563  
 564



565  
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 567  
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 569

Table 7: Results of techniques quantifying weather station clustering

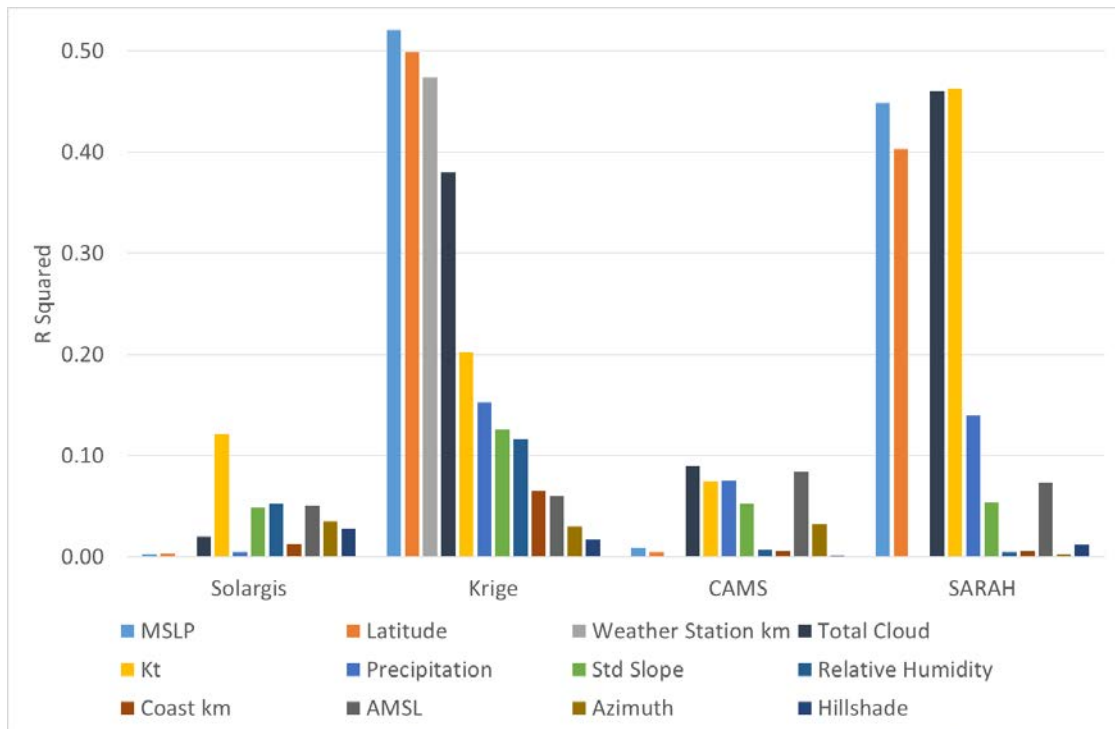
Weather Station Density		Neighbour Count in Distance Band	
Area	No. weather stations per 100 x 100 km grid square (10,000 km <sup>2</sup> )	No. neighbours within 100 km radius of each weather station	No. neighbours within 45 km radius of each weather station
All UK	3	2 (+ station itself = total of 3 in circular area)	n/a
Areas where kriging performs best (< 30 % nRMSE)	6	n/a	2 (+ station itself = total of 3 in circular area)

570

571 Looking at Figures 11 and 14, it is evident that kriging outperforms Solargis where there are  
 572 at least 6 weather stations per 10,000 km<sup>2</sup> grid square. Kriging outperforms CAMS and  
 573 SARAH throughout the UK i.e. where there is a weather station density of at least 3 weather  
 574 stations per 10,000 km<sup>2</sup> grid square. Three per 10,000 km<sup>2</sup> grid square is possibly achievable  
 575 for many national meteorological organisations, but perhaps not more than this. It is surmised  
 576 that this is the lowest weather station density for interpolation to surpass satellite model  
 577 accuracy. PVGIS Classic/Original PVGIS/PVGIS-3 (JRC, 2012a), computed from  
 578 interpolation of data from 566 ground meteorological stations throughout the European  
 579 Subcontinent, has a new version, PVGIS-4/PVGIS-CMSAF. PVGIS Classic has 2 weather  
 580 stations per 10,000 km<sup>2</sup> grid square. The new version is based on calculations from CMSAF  
 581 satellite images and its authors are convinced it is an improvement on PVGIS Classic in most  
 582 places (JRC, 2012b).

583 *3.2.5 Major topographic influences on ground or satellite irradiance data*  
 584 *choice*

585 These are presented in Table 2 and Figure 23.



586

587 Figure 23: Influence of Distance to Weather Station, Atmospheric and Topographic Factors  
588 on Irradiance Models

589 Reviewing sections 3.2.1 to 3.2.3 (with Table 2 and Figure 23), it is apparent that the SARAH  
590 model is affected by factors associated with latitude and cloudiness (MSLP, Total Cloud  
591 Cover and Kt), and to a lesser extent by terrain. Kriging accuracy is determined by: factors  
592 associated with latitude and cloudiness; weather station clustering; less strongly by terrain. In  
593 the cases of Solargis and CAMS, none of the factors tested heavily influence error  
594 distributions (Figure 23).

595 Thus, when deciding between ground-measured and satellite-derived irradiance values,  
596 terrain, latitudinal factors and weather station clustering are the factors which matter. Some  
597 satellite models treat problems due to latitude and terrain more successfully than others. The  
598 SARAH model is less accurate than the CAMS and Solargis models. SARAH uses long-term  
599 monthly modelled averages for atmospheric input data (Appendix C). These long-term  
600 monthly aerosol averages smooth daily fluctuations. CAMS and Solargis employ satellite-  
601 derived 3-hourly and daily calculated values respectively. Short-term calculated values have  
602 an additional advantage over satellite data in that any missing data is filled in (Cebecauer et  
603 al., 2011), suggesting that Solargis may have the most accurate atmospheric inputs.

#### 604 4. Conclusion

605 This research delivers a national assessment of which data source is most accurate for  
606 production of site specific hourly irradiance data: satellite-derived values or ground-based  
607 measurements. Furthermore, it explores the atmospheric and geographic conditions under  
608 which each solar radiation resource delivers the most accurate results. The models tested  
609 may be listed in decreasing order of accuracy as follows: Solargis, kriging of ground  
610 measurements, CAMS, SARAH and nearest neighbour extrapolation of ground  
611 measurements. The exception is where there are at least 6 weather stations per 10,000 km<sup>2</sup>  
612 grid square. In these circumstances, kriging outperforms Solargis.

613 It was noted that nearest neighbour extrapolation does not deliver accurate results. Choice of  
614 satellite model is influential. The decision is not between satellite-derived and ground-based  
615 data, but between *which* satellite model and *interpolation* of ground measurements.

616 All the irradiance models evaluated were affected by landform, SARAH and kriging also by  
617 latitude. In the UK these factors cannot be separated since topographic ruggedness increases  
618 with latitude. Generally, it is not the case that some models perform better under certain

619 terrestrial circumstances than others. Solargis has lower errors over the entire UK than  
620 CAMS, which is in turn is more accurate nationwide than SARA. Satellite model accuracy  
621 appears to be related to time resolution of atmospheric input data.

622 Regarding the satellite/interpolated values decision, break-even distance provided guidance,  
623 but it can be enhanced. Rather than distance from weather station, the number of neighbours  
624 in distance band or number of weather stations per 100 x 100 km grid square (weather station  
625 clustering/density), are more effective rules. These demonstrate a closer representation of  
626 reality. Of the datasets tested in this paper, kriging is more accurate than SARA and CAMS  
627 where there are at least 3 weather stations per 100 x 100 km grid square or 2 neighbours in a  
628 100 km distance band of each weather station. Kriging is more accurate than Solargis where  
629 there are at least 6 weather stations per 100 x 100 km grid square or 2 neighbours in a 45 km  
630 distance band of each weather station. Weather station density is key. It is conjectured that in  
631 countries with less variable climates and landscapes e.g. flat desert, greater interpolation  
632 accuracy may be achieved with fewer ground measurements. For instance, research using  
633 data from ten meteorological stations located in the south and centre of Tunisia (Loghmani  
634 and Timoumi, 2017) has found solar irradiance data may be accurately extrapolated for  
635 distances of 65 – 129 km.

636 Influence of station network density has been recognised in studies of rainfall and  
637 temperature (Hofstra et al., 2010; Yang et al., 2016) but not previously been investigated for  
638 solar irradiance.

639 The most recent developments in satellite-based modelling of solar irradiance combine long-  
640 term satellite values with short-term high-accuracy ground measurements. This technique of  
641 site adaptation enables the production of enhanced historical data for new sites e.g. solar  
642 farms with measurement facilities. Validation against independent data has shown impressive  
643 improvements in error values (Cebecauer and Suri, 2016; Polo et al., 2016; Ruiz-Arias, J.A.,  
644 Quesada-Ruiz, S., Fernández, E.F., Gueymard, 2015).

645 Satellite data itself will also improve with the launch of the Meteosat Third Generation series  
646 from 2021 onwards. The new satellites will provide images at high spatial resolutions, from 2  
647 km to 0.5 km, as well as higher quality aerosol data. The ability of satellite irradiance  
648 algorithms to handle broken cloud will be enhanced and more accurate data for the radiative  
649 transfer equations will become available. Thus, in future, it may be possible that satellite-  
650 derived irradiance values will match or exceed the accuracy of data interpolated from even  
651 the highest density station networks.

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701 [\\_correction\\_v1.pdf/1e3fa565-b616-4ded-9bcd-05841b3ba3ac](http://www.soda-pro.com/documents/10157/326332/CAMS72_2015SC2_note_201707_acceptance_bias_correction_v1.pdf/1e3fa565-b616-4ded-9bcd-05841b3ba3ac) (accessed 06/02/2018)

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### 832 **Appendix A: Discussion of (Perez et al., 1997)**

833 This work has been extensively referenced, having received over 176 citations to date  
834 (Google Scholar (Google, n.d.), January 2018). It received 61 citations in the 11-year period  
835 2000-2010 as opposed to the average of 8 in the engineering field (Times Higher Education,  
836 n.d.). Post-2010, with widening availability of satellite data, the citation rate increased,  
837 reaching as high as 19 per year. Citing journals were published in English, French,  
838 Portuguese and Spanish. Most were in the field of photovoltaics, but there has also been  
839 interest from agricultural, terrestrial and oceanic sciences.

840 Approximately one-third of all citations study satellite modelling of irradiance. However,  
841 utilisation has broadened, particularly in the last three years. There has been a particular  
842 focus on photovoltaic electricity production. Other uses include merging ground-based and  
843 satellite irradiance data, irradiance forecasting, solar panel soiling and grid impacts of PV.  
844 Inputs into other disciplines include leaf area index and evaporation.

845 Half of all case studies citing (Perez et al., 1997) are based in Europe. Just two have a global  
846 application, Africa/Arabia and South America each comprise 15%, whilst Asia and North  
847 America contribute 5% respectively. Thus, although the original work was based on USA  
848 data, it has mostly been applied in Europe.

849 Despite the great number of citations, only two groups of researchers have attempted to  
850 emulate (Perez et al., 1997) work. (Martins and Pereira, 2011) obtained a break-even  
851 distance of 60 km for daily solar irradiance data in Brazil. Recent work on daily global  
852 horizontal irradiance (GHI) found the accuracy of the SARAH satellite model surpassed that  
853 of ordinary kriging interpolation of ground-based measurements when the distance to the  
854 closest measurement station exceeded 20 – 30 km (Urraca et al., 2016). This suggests that  
855 modern satellite models ought to deliver a much shorter break-even distance for hourly GHI  
856 than (Perez et al., 1997) figure of 34 km.

### 857 **Appendix B: Description of kriging technique used in this research**

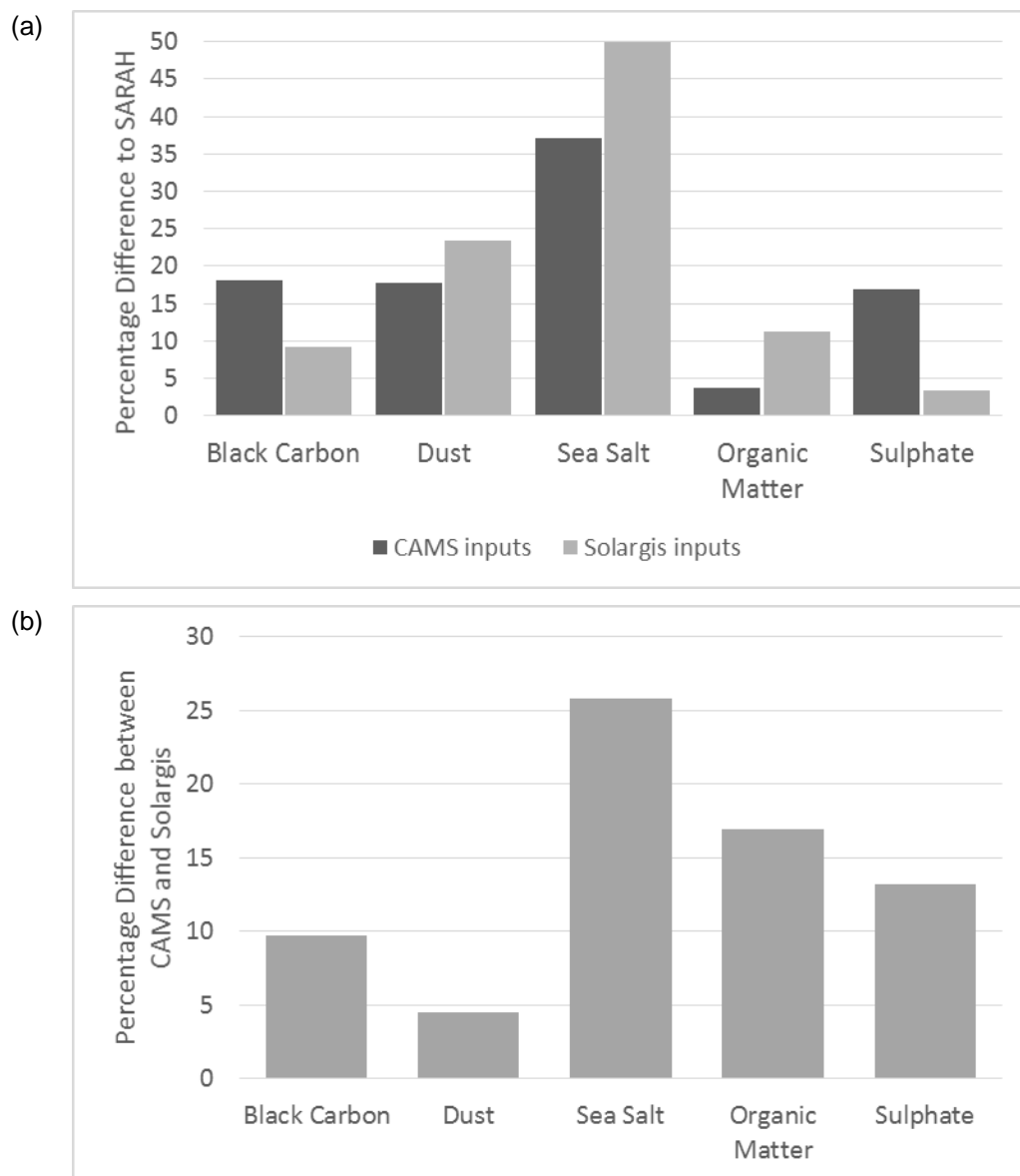
858 Kriging is widely used (Hofstra et al., 2008), suitable for data containing directional bias and  
859 provides error calculations. Specifically, ordinary kriging is used with an empirical semi-  
860 variogram. (The semi-variogram is a graph of the difference in value recorded at pairs of  
861 locations (the semi-variance) on the y-axis, plotted as a function of distance between them on  
862 the x-axis.) The semi-variogram model was selected as exponential, following an investigation  
863 of spatial autocorrelation, visual performance and cross-validation. Data from all the weather  
864 stations is utilised to calculate the end result. The empirical semi-variogram is fitted via the  
865 autofitVariogram technique from R software (Hiemstra, 2015). This obtains the sill and nugget  
866 from the semi-variance and the range from map size. (The sill is the value of semi-variance  
867 on the y-axis at which the exponential semi-variogram flattens. The nugget is the value at  
868 which the graph intersects its y-axis. Theoretically zero, the nugget value results from  
869 measurement errors, subsampling noise and fine-scale environmental variability. Additionally,  
870 it may include discontinuity of the data. In this instance, hourly solar radiation data may be  
871 discontinuous due to passing cloud. The range is the distance on the x-axis at which the  
872 model levels.) The R technique was chosen because of its ability to process the large quantity  
873 of data involved. The average nugget for all the hourly datasets is fairly large. This is caused  
874 by short-scale variability of irradiance in the UK. The country is located adjacent to the Afro-  
875 Eurasian land mass where several air masses converge. This causes the well-known  
876 changeability of the weather. (See (Palmer et al., 2017) for further explanation of selection of  
877 kriging and details of its application.)

878 The R Automap package provides automated kriging. Eighty semi-variograms (the number of  
879 weather stations) are computed for every hour for which data exists. That is 80 x number of  
880 daylight hours e.g. 5100 (12 x 365 plus extra dawn and dusk) = 408,000. Kriging took  
881 approximately 4 hours for one years' data using an i7 32 GB 8 core computer, using parallel  
882 computing and just-in-time compilation.

883 **Appendix C: Comparison of Atmospheric Input Data for Satellite Global Horizontal**  
884 **Irradiance Models**

885 The differences in aerosol optical depth input data between the satellite models is charted in  
886 Figure C.1. The data was obtained by the authors from the CAMS and CM-SAF download  
887 sites. It can be seen in Figure C.1(a) that Solargis is very different to SARA, CAMS less so.  
888 In Figure C.1(b) likewise, a substantial difference between CAMS and Solargis is visible. The  
889 differences are especially marked for sea salt, which is influential in the UK's maritime  
890 climate. SARA uses long-term monthly modelled averages for AODs, whereas Solargis  
891 employs daily calculated values. Long-term averages reduce variation in data, whilst higher  
892 temporal resolution calculated values fill gaps and reflect all changes, hence the disparity.  
893 CAMS takes satellite-derived 3-hourly AOD values which although shorter term, may still be  
894 subject to missing data.

895



897 Figure C.1: Percentage Difference between satellite model partial aerosol optical depths at  
 898 550 nm. Location: East Midlands of UK. Time period: January 2010. (a) Difference between  
 899 CAMS and Solargis partial AODs and those of SARAH. (b) Difference between CAMS and  
 900 Solargis partial AODs