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# DEVELOPMENT OF AN INTERACTIVE COMPUTER GRAPHICS 

## SYSTEM WITH APPLICATION TO DATA FITTING

## BY

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## DECLARATION


#### Abstract

I declare that the following thesis is a record of research work carried out by me, and that the thesis is of my own composition. I also certify that neither the thesis nor the original work contained herein has been submitted to this or any other institute for a degree.


To My Family

## ACKNOWLEDGMENTS

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## Chapter 1

INTRODUCTION

The first important manifestation of computer graphics was at M.I.T. in 1963, when Ivan Sutherland demonstrated his SKETCHPAD system on the TX2 computer at Lincoln Laboratory. In this demonstration a cathode-ray tube was used in such a way that it generated geometric figures and by using a light-pen, the figures on the screen could be drawn and manipulated. Although he was preceded by some earlier graphics hardware development (e.g. WHIRLWIND 1, 1950), it was Sutherland who made the breakthrough in man-machine communication, to the extent of interacting with a computer by means other than bits, numbers or the omnipresent punched card. Following this work Project MAC was initiated at M.I.T. in early 1964, involving the use of time-shared terminals and later the display consoles. During the same period, General Motors were developing their system DAC-1 (Design Augmented by Computer), which involved the use of CRT displays: these subsequently became the prototype of the IBM 2250 display.

The concepts of the computer-driven display, light-pen interaction with the CRT trace, and time-sharing are adequate to make up the technology of on-1ine computer graphics for drawing or drafting. In the famous M.I.T. SKETCHPAD, a drawing was constructed of entities or 'instances' which could be manipulated and reproduced on the screen. This demonstrated that the computer had an 'understanding' of the picture, could make calculations based on it, and display the result. This concept is the basis for the extension of computer graphics into several application areas such as computer-aided design, artificial intelligence and information retrieval. For example, interactive graphics displays can be used as a powerful tool in the computer-aided design of products and systems. In many cases such displays provide an ideal interface between man and machine; the designer can exercise
insight and judgement, while the computer undertakes involved calculations and analyses at high speed.

In general terms, computer graphics means images generated by computer, while interactive computer graphics means that the human must be involved with the computer through these images. The scope of computer graphics usage can vary in the level of sophistication involved, and may be classified as follows:-
(i) Historically, conventional batch-processing computer system first produced graphic output only via line printers, incremental graph plotters, video displays, etc. These are relatively expensive resources and graphic output is usually off-lined into a faster peripheral (typically magnetic tape) and consequently driving the plotter as a background job.
(ii) The introduction of time-sharing systems has made possible the idea of interactive computing. Thus, conversational input typically at a teletype terminal can be made to initiate computer output, and in particular, graphics output on a plotter or CRT. This is effectively 'semi-interactive graphics', since the process is interactive but no graphical input is involved.
(iii) The appearance of storage tube displays allowing a graphical input capability (e.g. by means of cross-hair cursor), has made it possible to build systems which enable the user to incorporate graphical interaction. However, this type of system still lacks the selective erasure capability which allows dynamic interaction. Such systems could be designated as 'static interactive graphics'. A wide range of scientific
applications which do not require dynamic interaction can utilize such systems, if a well-designed graphic interface and suitable interactive techniques are used.
(iv) The use of a refreshable display and some input device (e.g. light-pen), allows change of the picture in dynamic fashion in real time. It is often desirable to remove part of the picture or change its position, thus requiring a highly interactive graphics capability; this implies an intelligent terminal with its own display processor and input capability. With an increase in size and sophistication of the display processor, the graphics sub-system can become independent of the host computer, including its communication front-end. Thus it is possible for some graphics systems to be used as stand-alone configurations (for relatively small applications).
(v) With more general interactive graphics systems where further computing resources are needed, the display system would be linked to a large machine which would provide the extra facilities to run more extensive graphics problems. This may require the computer to understand the picture which the user has drawn on the screen. That is, the computer must have a useful knowledge of the topology or the connectivity of the picture as well as the coordinates of and storage significant points and elements. The programminglphilosophy required for this level of sophistication is necessarily more involved.

Computer graphics, computer-based pictorial information processing, has appealed to computer designers and users since the early days. Both hardware and software developments have continued to improve graphical facilities, but the progress has been relatively slow. A - number of quite sophisticated systems have been designed and built, but at a cost that makes them uneconomical for many users, and simply not available to most. As yet less attention has been given to the development of simple and relatively cheap systems, though the feasibility of such systems have been explored in recent years. At the same time, the need for graphics as a medium of information interchange has grown tremendously. With this increasing demand for computer graphics, terminal costs have reduced, allowing a wider use of terminals for this purpose. Consequently the need for improved software techniques for graphics has become apparent.

Therefore, interactive computer graphics has changed considerably over the past few years from an expensive, dedicated activity restricted to a privileged few users to a relatively low-cost, time-shared activity available to many users in most scientific/technical environments.

The aim of this work is to provide a graphical facility which is relatively low-cost both in regard to capital cost and run time overheads, and making efficient use of the available computing resources. The system must be generally available, general-purpose, portable, powerful and easily augmented by application programs in selected areas. The display terminal available in the early stages of development was the storage tube (Tektronix 4010). This display requires less software and processor power for its support than does a refreshable display. Admittedly, such a display limits the interaction and animation capabilities of the system but for the average application programmer
such restrictions are not serious. The basic graphic software package provided is made accessible to Fortran programmers while circumventing some of the limitations of the language for graphics applications.

This work was also aimed at the possible exploitation of some scientific application areas, in particular the use of man-machine interaction in data-fitting problems as a starting point for many more applications. Data-fitting is an area in which a batch processing environment is especially frustrating, because intermediate results and graphs of results provide additional insight and are needed in order to proceed intelligently.

The work reported in this thesis is organized into two parts. Part I presents a review study of the existing graphics facilities in terms of hardware and software (Chapter 2), interactive input techniques (Chapter 3) and the organization of graphics output processes and application data structures (Chapter 4). Finally, in Part I, a full account is presented concerning the development and implementation of the basic graphics software package LIGHT. Part II contains a detailed discussion of the implementation of several application programs which employ the basic graphics software developed in Part I. The applications cover the following problem areas:
(1) Interpolatory Data Fitting - IDF
(2) Interactive Contour Tracing - ICT
(3) Triangular Mesh Generation - TMG

Finally, full program listings of the basic software and the application modules are given in the Appendices accompanying this thesis.

PART I

GRAPHICS SYSTEM

## Chapter 2

## A REVIEW OF FACILITIES FOR COMPUTER GRAPHICS

1. INTRODUCTION
2. GRAPHICS HARDWARE
2.1 Hardcopy Output Devices
2.2 Graphical Displays
2.3 Input Devices
2.4 Graphical Terminal Configurations
3. GRAPHICS SOFTWARE
3.1 Structure of Graphics Software
3.2 Features of a Typical Graphics Software Package

## 1. INTRODUCTION

A man-computer graphics system consists of the man (liveware), the hardware and the programming (software). In general, the hardware consists of a computer, a display driven by the computer, and input devices which permit the user to give instructions and data to the computer based on his evaluation of the picture (information) displayed on the screen. The programming consists of the basic system programs (e.g. UNIX system) and applications programs which permit the solution of specific problems. There is also the device interface software which enables the user's program to communicate with the display (e.g. LIGHT package, see Chapter 5).

It is immediately apparent that the hardware-programming system must be considered in its entirety, since all portions interact to provide the over all capability.

## 2. GRAPHICS HARDWARE

### 2.1 Hardcopy Output Devices

In an interactive terminal configuration some means of hardcopy production is usually useful and often essential. Here, we briefly mention the different types available:-
(i) Incremental Plotter

This is the most common graphical output hardcopy device. There are now two main types of incremental plotter: drum and flatbed. Paper on a drum plotter is supplied in a roll which is mounted at the rear of the device. The paper then passes over the drum and is either allowed to hang freely or, more usually, is wound onto a take-up spool. A pen attachment is mounted above the drum and can move across the width of the paper. The more advanced drum plotters
have multi-pen arrangements which are useful for plotting in several colours.

Flatbed plotters are available in the form of a horizontal table, or may be mounted at a fixed angle to the horizontal. The pen is suspended in a gantry arrangement which moves over the surface of the paper.

All digital plotting is accomplished by drawing straight lines in certain fixed directions. In the case of the drum plotter for example, movement of the drum alone can cause a line to be drawn in the direction of rotation of the drum, while movement of the pen alone can cause a line to be drawn at right angles to the direction of rotation of the drum.

In order to reduce the demand on the processor time of the central computer caused by.excessive data throughput, off-line plotting systems have been developed. A controller processes a simplified form of the plotter input (which has been stored on magnetic tape or disc), into the incremental steps required by the plotter. The main drawback of the incremental plotters is their low plotting speeds.

## (ii) Electrostatic Plotter

This is an alternative to incremental plotters. Here the output is not in the form of line vectors, but in the form of small dots. A dot may be 'drawn' only on a grid point and the distance between grid points is of the same order as the length of an incremental plotter step. The general arrangement of this plotter consists of dielectric coated plotting paper which passes over a writing head containing minute conducting styli which are
selectively able to deposit electrostatic charges on the paper. The positions of the charge deposits become visible on passing through a liquid toner suspension. Speeds of up to 1200 lines per minute are obtainable -- comparable to the speed of a lineprinter for a small or medium range computer configuration. It is possible with the addition of an interface to a storage tube, to produce hardcopy reproduction of the screen image on the plotter.

## (iii) Microfilm Recorder

This is another alternative to the incremental plotter but is commercially expensive. However, its speed makes it an economic proposition if vast quantities of output need to be produced.

The most powerful microfilm recorder currently available is the FR80 made by Information International Incorporated. Basically the FR80 consists of an IIIl5 computer which accepts data stored on magnetic tape and displays the result on a high precision CRT. Various cameras may be used to record the information displayed in hardcopy form, on 35 mm film, l6mm film or microfiche form.

### 2.2 Graphical Displays

Basically there are four types of graphical displays:-
(i) Direct view storage tube
(ii) Indirect view storage tube
(iii) Beam driven refresh display
(iv) Raster display

All the above types of displays rely on CRT-related technology for electron beam generation and control; details of this may be found in [1]. An electron beam, having struck a phosphor coated screen, will cause the phosophor to glow for a short period, the intensity
level falling as time increases. The length of time that the glow remains visible is termed the 'persistence' of the phosphor. In order to maintain the image on the screen for longer periods it must be redrawn and it is in the redrawing techniques that the differences between the above displays are to be found.

Storage tubes are so named because a representation of the screen image is stored in the form of an electric charge pattern which is continuously copied to the screen. The storage device is actually part of the display terminal. Refresh and raster display on the other hand need some form of external storage device (display file/buffer) from which to obtain the data to redraw the image.

Picture drawing on all types of display is accomplished by referencing a notional grid, precisely as is done on a plotter. Each grid point is addressable, though some may in effect lie outside the screen dimensions and are therefore never visible. The more visible points there are, the more accurate is the screen image, provided of course that the resolution obtainable by the focusing mechanism of the display is sufficient to enable adjacent points to be distinguishable by eye. Each type of display is now described more fully.
(i) Direct view storage tube (e.g. Tektronix 4010)

The writing beam is not focused directly into the screen, but onto a grid of fine wire situated immediately behind the screen and coated with dielectric, on which a pattern of charge is deposited and retained. This pattern is then effectively copied from the storage tube to the screen by a continuous flood of slow moving electrons. Selective erasure i.e. erasure of part of the image without erasure of the whole, is virtually impossible using the storage tube technique. Complete erasure of the screen is accomplished by applying a positive pulse of about half a second
duration to the storage grid. This has the side effect of producing a visible flash across the entire screen.
(ii) Indirect view storage tube (e.g. Princeton 801)

This is a variation on the previous storage technique and allows selective erasure. The image change is stored on a circular target which is about an inch in diameter and composed of a wafer of silicon and silicon oxide. The target is continuously scanned in a raster fashion by an electron beam to give the screen image. To remove part of the image, the target must be retraced in a special mode along those vectors not required. (iii) Beam driven refresh display (e.g. DEC GT42)

The alternative method of maintaining an image on the screen is to redraw the picture before it has faded. The persistence of the phosphor governs the rate at which the screen must be refreshed in order to avoid flicker. For most phosphors used in CRT's designed for interactive graphics, flicker will be avoided if the picture is refreshed 30 or more times per second. Maintaining this rate has two consequences:-
(a) high speed circuitry must be used to convert the digital signal received from the computer to the analogue signals required by the CRT.
(b) the data which describes the picture to be displayed must be readily accessible.

The beam driven refresh display is a vector device which obtains its data for drawing the picture from a 'display file'. The display file is composed of 'display instructions', so named because their form bears a close resemblance to machine instructions. The set of instructions which may be used is called the 'display
instruction set', the size of the set depending on the hardware features of the display. For example, the DEC GT42 instruction set basically comprises

- set graphic mode
- Jump
- NO-OP
- Load status Register A
- Load status Register B
together with six data word formats that accompany the instructions:-
- character data format
- short vector mode
- long vector mode
- point data mode
- graph plot $\mathrm{X}(\mathrm{Y})$ mode
- relative point mode

For further details see reference [2].
The instructions in the display file are executed autonomously by the 'display processor unit' (DPU), and one such execution of all instructions in the display file is termed a 'refresh cycle'. The final instruction in the display file should be one of the two types:-
(a) an instruction to halt the DPU
(b) an instruction to direct the DPU to the first instruction of the display file.

By adopting method (a), the DPU may be synchronised to the internal clock of the host computer; a flag to restart the DPU is set when a timing signal (or clock interrupt) is received. Thus at the end of the refresh cycle there will be a pause before the next cycle is started, the refresh cycle plus the pause being termed a 'frame'. The number of frames per second is known as the 'refresh
rate' and by the above synchronisation technique the refresh rate may be maintained at a constant value provided that the relevant clock interrupt is not received before the DPU has finished its refresh cycle. If this happens then the refresh rate must be lowered with the possibility of picture flicker resulting. By adopting method (b), the refresh rate is not constant but varies according to the number of instructions in the display file. This procedure is not normally adopted as problems are caused if the display file manipulation is attempted while the DPU is executing instructions.
(iv) Raster Display

The sequential scan refresh display, or raster display, can use a standard domestic television monitor for its display screen. The screen elements, corresponding to grid points, are sequentially scanned, a double scan of alternate lines being adopted to reduce flicker. Data is stored for each element in the order required by the raster scan.

Finally, Table 2.1 presents a comparison of the various graphics display types discussed above, and Table 2.2 shows the hardware feature of the Tekronix 4010, DEC GT42 and Vector General. Table 2.3 presents an approximate cost of these hardware devices, circa 1976.

|  | (i) Direct view storage tube | (ii) Indirect view storage tube | (iii) Beam-driven refresh display | (iv) Raster scan refresh display |
| :---: | :---: | :---: | :---: | :---: |
| Picture drawing technique | Wire grid storage copied to screen | Raster scan of silicon target | Continuous retrace of display file | Raster scan from storage device or memory |
| Picture generation speed | Dependent on line speed | Dependent on line speed | Fast | Fast |
| Picture quality | Good | Poor | Good | Poor (at present) |
| Minimum line speed | 110 Baud | 110 Baud | 1 M Baud | 30 M Baud |
| Local memory requirements | None | None | 10 K bytes | 100 K bytes |
| Selective erasure | No | Yes | Yes | Yes |
| Time for complete erasures | 500 ms | 400 ms | 20 ms | 30 ms |
| Capacity limitation | Resolution | Resolution | Beam driven speed | Resolution |
| Intensity level | One only | Several | Several | Several |

TABLE 2.1: Comparison of Display Types

| . | Storage Tube |  | Display |
| :---: | :---: | :---: | :---: |
| Feature | Tektronix 4010 | GT42 | VG-3D3I |
| Lines: solid | Yes | Yes | Yes |
| long dash ----- | No | Yes | No |
| short dash -------- | No | Yes | Yes |
| Dotted ............ | No | No | Yes |
| chained - - - - - | No | Yes | Yes |
| Blinking: | No | Yes | Yes |
| Characters: normal set | 64 | 127 | 192 |
| rotation | No | No | Yes |
| italics | No | Yes | by rotation |
| Intensity levels: | 1 | 8 | 32 |
| Intensity modulations: | No | No | Yes |
| Transformation: rotation | No | No | 3D |
| translation | No | No | 3D |
| scaling | No | No | 3D |
| Windowing: | No | No | optional |
| Arc circle generator: | No | No | optional |

## DRUM PLOTTERS:

CIL Midas ( 34 cm ) . £2050
CIL Economist-1 (92 cm) £3750
FLATBED PLOTTERS:
Ferranti from $£ 27000$

## ELECTROSTATIC PLOTTERS:

Sintrom 800 ( 8.5 inch) plotter $£ 4300$
Sintrom 800A (8.5 inch) plotter/printer £4600

## MICROFILM PLOTTERS:

Ferranti
III FR80
from $£ 40,000$
\$210,000

DIRECT-VIEW STORAGE TUBES:
Tektronix 4010
from $£ 3300$
Tektronix 4010-1 (hard copy unit compatible) from $£ 3700$
Tektronix 4051 from $£ 5300$

INDIRECT-VIEW STORAGE TUBES:
Princeton 801 from $£ 8000$

## REFRESH DISPLAYS:

GT42
£12000
IMLAC ODS-4/DINO system
£15410
Vector General Series 3
from $£ 27400$
Vector General 3400
from $£ 45500$
CDC 777 Cybergrahpic terminal
£67100

TABLE 2.3: Approximate Costs of Hardware

### 2.3 Input Devices

For a display to be termed an interactive terminal it must have some means of permitting its user to input data. Without this facility the display is really an output only device. The various input devices currently available are:

- keyboard
- function buttons (switches)
- control dials
- joystick, tracker ball and mouse
- digitiser cursor
- tablet and stylus
- lightpen
- storage tube graphical cursor

More detail on these devices may be found in [1]. However, a detailed study of the associated programming techniques is presented in the next chapter.

### 2.4 Various Graphical Terminal Configurations

Numerous designs of graphics display terminal configurations are possible. This section presents some examples of these configurations based upon the tasks assigned to each part of the system. These tasks may be divided into the following categories as in [4]:
(a) Display file maintenance - (DFM) for refresh display only.
(b) Interactive demand servicing (IDS).
(c) Extensive numerical calculation (EC).

Examples of terminal configurations:-

## (i) storage tube terminal

The nature of the storage tube makes it particularly suitable for use as a remote terminal with no local processor. With this configuration (Fig.2.1), there is no provision for any computation to be done at the terminal site. A hardcopy unit at the terminal site would enable plots of the screen to be obtained in about ten seconds; this is therefore very useful additional equipment for such a terminal.
(ii) storage tube terminal with a small processor

This configuration (Fig.2.2), is the obvious enhancement to (i) providing some processing power at the terminal site. With appropriate software, the processor is able to cope with a limited amount of interactive demand servicing. A terminal providing just this system in one package is the Tektronix 4051. In addition to the standard Tektronix storage tube, this has a microprocessing unit for programming in Basic, $8 \mathrm{~K}-32 \mathrm{~K}$ bytes of memory and a cartridge tape unit. The Fortran version is the Tektronix 4081.

An interface is available which allows some direct storage tubes (Tektronix 4010) to behave as a refresh display. The intensity of the writing beam is reduced to prevent charge storage and is focused onto the screen; this is called 'write through only'. However, the performance of operation in this mode can not compete with the more expensive refresh displays.
(iii) low cost refresh display having its own processor and core memory

Because of the need to refresh the screen image many times a
second, some core memory is required at the terminal site (Fig.2.3.)
to hold the display file (or equivalent). In addition, the display


FIGURE 2.1: Storage Tube Configuration


FIGURE 2.2: Storage Tube and Small Processor Configuration
file must be updated when necessary and this is best done by providing a local processor, which can also be used for interactive demand servicing. This type of terminal is supplied as one package e.g. the DEC-GT42.
(iv) high cost refresh display with its own processor and core storage directly interfaced to a mini-computer

This, (Fig.2.4), provides a multi-user environment (e.g. Vector General 3400- PDP 11/45). The display's core and processor hold and maintain the display file. The minicomputer can be dedicated to interactive demand servicing. The extensive calculations which the minicomputer could not reasonably cope with would be sent down the link to the large computer for execution in batch mode.

## 3. GRAPHICS SOFTWARE

### 3.1 Structure of Graphics Software

In general there are three main and distinct 'layers' of software [5] in any interactive graphical computer program:(i) the lowest level, that 'closest' to the hardware is called 'basic' software and consists largely, for a given application, of a basic graphics package with its associated device drivers and may include some simple data-structuring and file handing routines. Parts of this basic software will of necessity, be written in machine dependent code; transfer of an application system from one host computer to another or from one graphical device to another will thus affect this layer of software more than any other.
(ii) The middle layer is known as 'general purpose' as this is normally written with a whole range of application areas in mind.


FIGURE 2.3: Low Cost Refresh System Configuration


FIGURE 2.4: High Cost Refresh System Configuration

Such general purpose routines are assembled from basic software building blocks. Examples, in this layer are routines for messages, menu display and removal, and routines for utility purposes such as clipping.
(iii) The top layer is the actual application program. This software is built on both of the bottom two layers. In other words, an application program will call basic routines directly or (usually) via the general purpose routines. To operate a given application program on a different computer, or a different graphical terminal or under a different operating system, few changes should be needed at this level in a well-designed, well-layered system.

A simplified schematic diagram of Fig. 2.5 shows a typical software package and the user program. Here we are considering the simple configuration of a mainframe computer driving a graphical display terminal. At the highest level there is the user program which calls routines in the display software package. Those routines of the package which are user-callable are known as 'frontend' routines, and these in turn call other routines which are not user callable and are therefore termed 'back-end' routines. At the lowest level there is the program known as the 'device driver' whose function is:-
(a) translate simple instructions from backend into low level instructions (i.e. machine code) which will drive the graphical terminal.
(b) handle communication between the computer and display terminal by sending instructions and data and (in the case of an interactive terminal) by receiving and interpreting data.


FIGURE 2.5: Simplified Schematic Diagram of a Typical Graphics Software

The device driver software communicates directly with the input/ output hardware of the computer and is of necessity written in assembly language.

### 3.2 Features of a Typical Graphics Software Package

### 3.2.1 Initialising the graphics package

The graphics software package must provide facilities for:
(i) device nomination
(ii) resetting to default values.
(i) Device nomination

Before any drawing can be made, the device has to be prepared for drawing or character generation. If the package was designed to operate under a 'closed' system, i.e. a dedicated computer and one screen, the device nomination may not be an explicit part of the package; switching on the system will prepare the device for calls from the graphics package. Nomination may involve clearing the device's display file (and hence clearing the screen for a refresh display) at the start of a run, but this is usually under the control of a further subroutine.
(ii) Resetting

All graphics packages will have various defaults to simplify initialisation, the number of these depending on the range of facilities offered by the package. For plotting packages, these are default axes, grid marks, curve resolution, maximum size of allowable plot etc. For display-oriented packages there will also be default settings for picture sensitivity, character size, brightness, window size etc. In some existing packages such as GINO-F [3] and GPGS [6] all default values are set in initialisation,
while other packages require, in addition to the setting of default values, various preparatory calls before drawing can commence. For example:
(a) Plotting package:

DISSPLA [7] requires a title, page border, definition of physical origin and subplot area, plus axes types and units.
(b) Other packages:

PICTURE SYSTEM [8] requires the refresh rate and the time interval between updating the display file to be specified as parameters to the initialising routine.

### 3.2.2 Picture generation

Picture generation routines form a large part of any graphics package. These routines are used to drive indirectly the drawing mechanism of the device through either assembly coded routines or structured display file. These routines form part of the 'frontend' of the graphics package. Calls to routines are interpreted by the graphics package into a series of calls to device driver routines which the application programmer is not allowed to (nor would wish to) access. In the case of a refresh device, the device driver may be a separately running program interpreting the structure of the current display file and regularly refreshing the screen with the current picture.

We can divide picture generation calls into three classes:
(i) Basic drawing routines

These are routines which translate directly into device driver calls, the most common of which is straight line drawing. Graphical devices normally allow such drawing action as MOVE,LINE,

DOT and character with the addition of different line types, intensities, pen sensitivity etc.

## (ii) Multiple drawing routines

Multiple drawing routines are those routines which are a kind of 'shorthand' for common objects, and replace a whole series of calls to the more basic picture generation routines. These are middle level routines provided by the package to simplify the work of the programmer at the expense of the size of the package.

## (iii) Complex drawing routines

These require much more preparation than multiple drawing routines either by the package or by the programmer. An example is CUPID [9] which has one complex drawing routine which plots a graph or histogram, and the axes with annotation. Every parameter (except the data file name) has a default value but can be altered by calls prior to PLOT.

Graphics packages are designed with different users in mind and for this reason provide fewer complex features and greater control over basic line drawing. For example GINO-F and PICTURE SYSTEM provide many more basic drawing routines than complex routines. On the other hand DISSPLA and PLOT-10 [10] are designed for plotting of graphical or other data under various systems of axes and does not demand the programmer to write code to draw the axes, tick marks, etc. Instead they provide subroutine calls to simplify the programming when the drawing follows a fixed format.

### 3.2.3 Picture administration

This involves the segmentation of pictures, the setting of picture parameters and picture manipulation.

This is the dividing up of a picture into segments and this is only useful when the graphics package stores the picture represented by lines and characters in some form of file. The segments may be required for identification or to be used for building up complex pictures in a similar manner to the usage of subroutines in Fortran. Segments are used to obviate the necessity to regenerate the complete picture when only one part is changed. The normal usage of this form of segmentation is with the refresh device in which a lightpen is used to identify some part of the whole picture. But it can also be used with a storage-tube device where identification is made with the cursor (requiring a search of the display file to locate the picture from the coordinates). GINO-F offers the facility of storing a picture segment either on discs or in local arrays to be recalled when required.
(ii) Picture Parameters

These are used by graphics packages to give sections of code hardware options such as picture intensity, lightpen sensitivity etc. When picture segmentation is provided it is usual for each segment to have a header containing the segment name (or number) together with various picture parameters.

Packages that provide for altering these parameters contain a varying number of routines. For example, GINO-F has a routine a different for each type of parameter while DISSPLA provides $h$ routine: for each parameter setting.
(iii) Picture Manipulation

This is concerned with the display file and thus applies to display file based packages e.g. Picture Book [11]. Manipulation
usually involves deleting and copying of pictures, changing the position of a picture, etc.

### 3.2.4 Transformation

Transformation facilities provided by various packages could be divided into three categories:
(i) Linear Transformation
(ii) Windowing Transformation
(iii) Perspective Projection.

## (i) Linear Transformation

The four primitive transformations that are applied to an object in two or three-dimension are translation, scaling, rotation and shear. These transformations are applied to the coordinates of all points and end-points of lines forming the object. The basis of these transformations is the $4 \times 4$ transformation matrix using homogeneous coordinates. A typical package would usually provide routines to update the current transformation matrix, using these primitive transformations and producing more complex transformations.

## (ii) Windowing Transformation

This is concerned with the mapping of the picture (object) coordinates into the physical screen coordinates. One could assume if all picture drawing would remain within the limit of the screen, a large amount of coordinate checking could be removed from many graphics packages. But when a linear transformation is applied, for example, on an existing picture on the screen, it is very likely that the transformed picture will have some of its lines transformed off the screen. Hence, there is a need to clip the lines to a rectangular area or a 'window' and then project the
clipped picture on to the display 'viewport'. Thus, a windowing transformation has two phases, firstly to determine if a line exceeds a window boundary, and secondly to calculate the cut-off point. Routines such as clipping and viewing are usually provided to facilitate these operations. Both would define how much of the picture should be visible and where the visible portion should be placed on the screen. Finally there is often the necessity for zooming into a detailed part of a picture or placing several viewports on one screen.

## (iii) Perspective Projection

The combination of a perspective transformation with a projection is often called a perspective projection. It represents a transformation from three space to two space. Some packages, for example GINO-F and PICTURE SYSTEM, provide the programmer with transformation routines such as these, for greater control of viewing of three-dimensional objects projected onto the plane of the display screen.

## Chapter 3

## InTERACTIVE INPUT AND RELATED PROGRAMMING METHODOLOGY

1. INTRODUCTION
2. THE MAN-MACHINE DIALOGUE
3. INTERACTIVE INPUT SOFTWARE
3.1 Layers of input software
3.2 Interactive input facilities
3.3 Application program and Interactive input
4. INTERACTIVE INPUT DEVICES
4.1 Keyboard
4.2 Cross-hair cursor
4.3 Lightpen

## 1. INTRODUCTION

The organization of interactive input is probably the most important factor in the design of an interactive graphics program. Well planned man-machine communication is vital if the program is to be successfully used.

In this chapter we develop and apply the philosophies underlying graphical input techniques [12]. Initially, an attempt is made to formulate conceptually the mechanics of man-machine interaction and the different processes involved in the communication process. Then, the practicality of these concepts is exploited in the field of software techniques for interactive input, so that a better understanding of the nature of man-machine interaction is obtained and subsequently used in the development and design of interactive computer graphics systems. These techniques would provide facilities in the basic graphics packages for application programmers or could be used directly in the application programs. This area has received considerable attention in various contexts [13], [14].

Finally, a number of common input devices are examined separately, and the different programming techniques that may be used with such interactive input devices are highlighted. Most of these techniques have been incorporated in the design of the interpolatory data fitting packages in Chapter 6.

## 2. THE MAN-MACHINE DIALOGUE

The combination of man and machine can leave design decisions to man and calculation to the machine (computer). The main distinction between 'design decisions' and 'calculation' is that the latter are readily programmed and the former are not, being a function of
experience etc. The sharing of the work seems useful in many areas of design and is efficiently achieved when the man-machine interface is well-defined.

Ross [15] pointed out that the fundamental mechanics of communication involve the transfer of 'atomic' components such as characters or numbers. Therefore to convey an idea or a meaning from one body to another requires (1) a process of analysis through semantic, syntactic and lexical phases to define the stream of atomic components, (2) the transfer of these components through a suitable medium, and (3) a process of synthesis to reassemble the idea or meaning through lexical, syntactic and semantic phases. These phases retain their identity even though the rate of interaction may vary. In a telephone conversation where the atomic components are the sound syllables, the sentences are short and the rate of interaction is relatively high. Telegrams typically contain a single whole message or request, a letter typically consists of a series of requests, or pieces of information. Batch input to a computer corresponds to a letter. ATeletype input command compares to a telegram and 'interactive graphics' compares to telephonic or face to face dialogue. Therefore, conceptually we may recognise that there are three distinct levels at which interaction could take place in an interactive graphics system:
(i) Lexical Level:- corresponds to interactive facilities in the basic graphics package.
(ii) Syntactic Level:- corresponds to command languages in general.
(iii) Semantic Level:- corresponds typically to application programs.

Each level of processing of computer input and output corresponds to processes of synthesis and analysis respectively. Corresponding processes of analysis and synthesis occur in the brain of the operator. Fig. 3.1 illustrates these ideas, and Fig. 3.2 relates these to the different levels of program code used in a man-machine dialogue.


FIGURE 3.1: Man-Computer Communication Processes


FIGURE 3.2: Man-Computer Communication Processes and Program Code

## 3. INTERACTIVE INPUT SOFTWARE

Interactive graphics adds new dimensions to the more general conceptual framework of man-machine communication. A variety of schemes for interactive graphics are available today. The following discussion describes the basic principles and requirements of interactive input.

### 3.1 Layers of Input Software

Figure 3.3 shows how input software can be divided conceptually into three distinct layers corresponding to the three communication levels mentioned previously.

Each annulus represents a piece of code and each circle represents an interface. The user (operator) is considered to be at the centre acting on the 'physical input device'. Input involves action by the user, terminal and the interactive program.
(i) User - a physical operation, such as the press of a 'key' on a keyboard, or placing of a lightpen over a picture element.
(ii) Terminal - the 'prompting' of the operator prior to his physical action; the delivery of all the data of input operations to the program, e.g. a character, a picture part plus $x, y$ coordinate; and 'echoing' the input data subsequently.
(iii) Interactive program - the organization of prompting, echoing and the processing of the input received.

### 3.2 Interactive Input Facilities

Consider a program which needs some data value at a point from the user before continuing execution. For example:


FIGURE 3.3: Interfaces and Layers of Input Software

1. characters
2. picture segment number
3. $x, y$ coordinate pairs

Input such as these are considered to be delivered by 'functional input devices' which are conceptually more convenient for programmers. The actual input data (such as a picture segment or coordinate pair) are placed in an agreed format in a global or common area (e.g. COMMON in Fortran). Ideally functional input devices are characterised by having:
(i) an identifying number such as $1,2,3, \ldots \ldots$ etc.
(ii) a value or set of values generated by user action, with an associated location or locations in the 'common' block where the value(s) would be placed.
(iii) an associated physical device or devices such as keyboard key, lightpen, or cross-hair cursor, from which the input actually arrives; including a 'trigger' which actually causes the dispatch of the input data.
(iv) a prompt to the user to announce the program's readiness for functional input.
(v) an echo to the user to announce the recognition of his input. Therefore, from these characteristics, one may conclude that interactive input programming facilities should include the following actions:-
(a) attach physical devices to functional devices and specify triggers;
(b) activate the required functional input devices;
(c) broadcast the various prompts associated with (b);
(d) send an echo to the user to confirm his input;
(e) request and wait for an event;
(f) read data from input devices.

These facilities have been variously combined in basic graphics packages
into a set of high level procedures. Some facilities are unavaiable in some packages, particular activities having been selected and fixed into the low level code of the device driver or even incorporated into the hardware of the physical input devices themselves (e.g. Tektronix 4010 cross-hairs cursor).
(a) attachment of physical devices to functional devices and specification of 'triggers':

Attachment needs to be largely by default. For example:-

| Type | Functional Devices |  | Physical Devices |  | Trigger |
| :---: | :--- | :--- | :--- | :--- | :--- |
| 1 | Single character | Key on keyboard |  | Key itself |  |
| 2 | Picture segment number | Lightpen |  | Sensing light |  |
| 3 | $x, y$ pair | Cross-hair cursor |  | Pressing a key |  |

The implementation of attachments requires 'mapping', which is usually performed within device drivers, e.g. within a keyboard driver, keys are mapped to characters. Mapping however may occur in a higher level code, e.g. keyboard driver characters could be mapped into integers, reals and valid character strings, which have been defined within the driver or in data which is fed to it via an application program. This mapping can be seen to be a process of lexical analysis. Physical devices produce 'atomic components' of input, or 'lexical tokens' (see Fig.3.3), or single characters or single picture segment numbers. The mapping programs convert this stream of lexical tokens into syntactic tokens or words. Each operable physical device must be considered as an indivisible entity. This notion is important if we are to design high performance man-machine operations into an application, and manage the human factors properly. This is by no means always possible with currently manufacturerd hardware and available basic graphics packages. For example, a light pen is not necessarily just one physical device as
many assume; it is usually two - a light pen sensor plus some kind of switch - each supplying an atomic component of input and each being separately attachable or specifiable as triggers: Mapping programs may be local to an installation or an application area. They may involve trivial one-to-one mappings such as keyboard keys to characters; or one-to-many such as keyboard keys to sets of characters, $x, y$ pairs; or many-to-one as shown below:-

|  | Physical Devi | Functional Devices |
| :---: | :---: | :---: |
| 1:1 | Keyboard keys | Characters |
|  |  | Characters |
| 1:many | Keyboard keys | $x, y$ pair |



Specification of triggers is not usually provided for by basic graphics packages. It is the kind of thing that has usually been seen as a characteristic of the physical device and often brought to the functional level without option. For example, the cursor input routine in LIGHT (see Chapter 5) is a direct mapping of thumbwheels to an $x, y$ pair with a particular trigger pre-specified.
(b) Activation of functional devices:

Activation of a functional input device will, through the physical attachments, activate a set of physical devices. These physical devices should then be highlighted in some way for the user.
(c) and (d) Broadcast of prompts and echoes:

Bleeps and Blinks from an interactive terminal are an essential part
of effective communication. As skill develops, direct response to prompts become less observable, indeed anticipation becomes more and more noticeable with experienced users. However, the right bleeps and blinks will then become an integral part of the continued success of the dialogue. Referring back to (b) above the activation of the physical device may be highlighted by prompts such as:

- a pair of cross-hairs on the display screen
- a bell on a keyboard

The operation of a device may be confirmed by echoes such as a small marker on the display screen .... etc.

Successful operation of physical devices is recognisable by the terminal user on a separate level from the successful acceptance of the input by the software at the functional level. The feel of the terminal device is an important aspect of user acceptability apart from the confidence that the program is operating correctly.
(e) Request and wait for event:

It should be noted that an event as far as the user is concerned is physical, e.g. the pressing of a key, or the turn of the thumbwheel (on the Tektronix 4010). An event as far as the program is concerned, is all that happens between passing control over to the user and control being returned to the application program on an acceptable trigger.
(f) Read data from input devices:

Input data is placed in a common area which acts as a functional input device buffer.

### 3.3 Application Program and Interactive Input

The semantic process of interpreting the meaning of communication from the user is performed in the code of the application program. The
syntactic processes of synthesising a sentence from words and analysing a sentence into words are often coded as an integral part of an application program. This usually takes the form of a 'command language'. Thus, the user of an interactive program must be provided with a set of commands by which to control the execution path of an application program. This approach induces modular program design and simplifies program overlay control. These commands must fulfil two requirements: they should control which processes are activated, and they should contain the data associated with these processes. Thus, it is generally advisable to define with precision the range of commands that the program will accept, and to define the form or syntax of each command. By doing so, we have defined a command language, the language 'spoken' by the user as he operates the interactive program. As he addresses the computer in this way, the computer addresses him, by means of displays and printed messages; thus a dialogue is maintained. Fig. 3.4 shows diagramatically the conceptual relationship between the command language and the application program modules. These commands may be presented on the display in the form of menus (tables), so that at any time the user can see what commands are available to him. He can then point at a specific command by the use of a device such as a lightpen or cross-hair cursor, and this is conveyed to the application program for interpretation. A menu may comprise one part which corresponds to the main modules of the application program, and a second part providing command options such as 'zoom'.

An important facility that is sometimes overlooked in the design of an interactive system, is a backup or recovery procedure. User mistakes as well as program errors can cause extraordinary damage to data files. Because repairs can be costly in user and computer time, it is often wise to provide a fail-safe option which enables the user to backup to a point prior to the accident.


FIGURE 3.4: Relationship Between Command Language and Application Program Modules

## 4. INTERACTIVE INPUT DEVICES

The discussion here is concerned with some common input devices and the role that each may play in an interactive environment.

### 4.1 Keyboard

All interactive graphical terminals have a non-graphical input available through an ordinary keyboard similar to the teletype keyboard. All character sets may be expected to include a Fortran character set. Some terminals have keys which are purely 'local', and depression of these does not send any data to the device driver, e.g. the Tektronix 4010 'Page' key erases the current display from the screen. Several types of keyboard usage are possible:
(i) The most obvious use is probably for direct input in response to program input statement:

```
e.g. READ(KEYBRD,10)FILNAM ...... requires text
    READ (KEYBRD,20)X ...... requires a numerical value
```

where KEYBRD is the channel number for the keyboard of the graphical terminal. Experience has shown that the keyboard is the best device for input of 'precise numerical values'. Techniques such as
'thermometer' (see virtual devices later), although conceptually more sophisticated, offer no particular advantages over the keyboard when the required input is in the form of known and precise values. Keyboard input is also used to good effect to input any 'character information' which cannot be predetermined -- examples here are file names or headings for plotted output. It is usual to precede the input by an output message which tells the user that the machine is now ready for his input and advises him on the nature of input that is expected.
(ii) Another direct use of keyboard input is as a means of identifying picture parts on the screen. If a name is displayed next to each
picture segment, the user may identify parts of the model simply by typing the appropriate name. This technique has particular significance in storage-tube graphics.
(iii) Selected keyboard characters can also be used effectively as cursor terminators/triggers on storage-tube systems. The display software package will usually pass to the application program details about the cursor terminating characters used (e.g. using ASCII or some other code) and this may be used as a switch to control the program. Display of the cursor is usually a sufficient prompt to the user that the input is required.
(iv) The keyboard input of groups of characters (to be interpreted as command mnemonics, say) is well known to anyone who has used a computer interactively for purposes such as text editing or file manipulation (e.g. under Unix operation system on the PDP 11/40). Input prompt characters such as "\#" or "/" both orientate the user and signify that input is awaited.

Finally, application systems which use the keyboard almost exclusively as the input device have often been ergonomically preferable as the user does not have to 'grope' from one input device to another. The 'one device' input philosophy preserves a useful 'tactile continuity'. A disadvantage, however, is the need for a (sometimes considerable) user manual and the associated difficulties of user training.

### 4.2 Cross-hair Cursor

(i) The cursor can be used directly for input of screen coordinates. For example when zooming part of a picture displayed on the screen, a corner of the zoomed window could be indicated by the cursor. Other similar functions which require qualitative judgement (e.g. re-positioning of picture parts) can make direct use of cursor coordinate input.
(ii) Coordinate input can be used for simple picture part identification; but this is fast in operation and easy to organise only in particular circumstances. In the case of a menu, for example, it is easy to define a simple rectangular region inside which the cursor must be if it is to identify a menu option. The identification is simplified when the menu items are horizontal. A set of subroutines for such menu operations are included, for example, in LIGHT.
(iii) Input coordinates can be scaled and combined to produce values for such things as rotation angles, dimensions, etc. This usage may require the display of a scale or dial on which the cursor is positioned. The value associated with the current cursor position (or one of its coordinates) may be displayed alongside. This simply provides visual feedback and it can be usefully termed a 'virtual device'.

### 4.3 Lightpen

In hardware operations the lightpen simply generates an interrupt when it sees light, but for its application a wide variety of software techniques have been developed.
(i) By means of suitable software (usually employing tracking cross) a lightpen can be used to generate position data and thus be used as a cursor.
(ii) The lightpen is used to identify pictures on the screen. The popular use for this is the identification of menu options (lightbuttons). The identification of pictures by lightpen is a powerful technique that is easy to organise; the programmer normally chooses the identifying numbers given to separate pictures in the display file so that they may be rapidly identified later in his program. (iii) Very powerful use of the lightpen relates to virtual devices. A
whole range of virtual devices can be coded using a lightpen as the actual input device. A favourite device for generating numbers, for example; is the 'light potentiometer' or 'thermometer' device, which is in essence a scale on which the pen/cross can be positioned. Other devices exist which are usually designed to generate one input value at a time, the need varying from one application area to another. Within engineering design, for example, the user may wish to do some airthmetic calculation, so a 'virtual calculator' in the form of a pocket calculator keyboard is displayed on the screen and is used in the ordinary way with the lightpen replacing the human finger.

To end this section on interactive input devices, it is important to mention that before any input is allowed, sufficient prompts should be given to the user to signify the form of input expected of him. Such prompts take the form of instructional or other messages or a command option menu. The interactive input should be in some way echoed so that the operator knows it has been accepted. For many major or irreversible operations it is advisable to require first a choice from a CONFIRM/REJECT menu. This reminds the user of the import of his accidently destroying a file structure or erasing a picture from the screen.

## Chapter 4

## GRAPHICS SYSTEM AND DATA STRUCTURE ORGANISATION

1. INTRODUCTION
2. GRAPHICS INPUT/OUTPUT PROCESSES OF AN APPLICATION PROGRAM
3. GRAPHICS OUTPUT PROCESS
4. DATA STRUCTURE FOR INTERACTIVE GRAPHICS
4.1 Basic Requirements
4.2 Simple array representation
4.3 Compound data structure

## 1. INTRODUCTION

The following describes the processes and data essential to a graphics application program with particular reference to the organization of the graphic output process, both for refresh and storage tube display systems. The importance of the graphics application program data structure is also described in some detail.

## 2. GRAPHICS INPUT/OUTPUT PROCESSES OF AN APPLICATION PROGRAM

A simplified sketch of the processes and data necessary to the operation of an application program is shown in Figure 4.1.

The input handler processes interrupts from the input devices and provides the means for an application program to read data from these devices. The input routines receive data from the input handler, make appropriate changes to the application data structure and pass control to other routines. The non-input/output routines are those portions of the application program that do not directly involve input or output (i.e. computational routines). The output routines define the picture to be displayed, from the application data structure. Effectively they define how these data may be visualised for display purposes. The transformation and windowing routines are capable of scaling, rotating and translating graphic information generated by the output routines. These routines also clip the picture information against a rectangular boundary. A series of different transformations are combined into a compound transformation by concatenation. The display generator generally includes a vector generator and character generator, which convert the transformation and clipped information into signals suitable for the display's deflection systems.


FIGURE 4.1: Simplified Diagram of the Graphics Input/Output Processes

## 3. THE GRAPHIC OUTPUT PROCESS

If we now consider the output process in Figure 4.1 and assume that the output routines pass graphic data directly to the display screen via the transformation and windowing routines and the display generator, then if these routines are executed once, the picture that they define will flash onto the screen and disappear. But if we arrange for output routines to be executed repeatedly at a sufficiently high frequency the picture will be refreshed and will remain visible. The output routines then perform the function of a 'viewing algorithm' [1], presenting on the screen a continuous view of what is contained in the application data structure. Whenever the data structure is changed, the picture changes accordingly. If we wish to see a different representation of the data, we can substitute a different viewing algorithm by changing the output routine.

This concept of a 'viewing algorithm' is simple but difficult to implement [16]. The problem lies in ensuring that the output routines written by the application programmer execute rapidly enough to keep the picture from flickering. Unless the routines are extremely simple and the data structure quite small, flicker is bound to occur.

However, with storage tube displays, the problem is partly solved because of the inherent storage that cannot be selectively erased. This is known as a 'picture store' and consequently the output process would be modified as shown in Figure 4.2.

With a refresh display, however, it is desirable to provide some means for selectively erasing parts of the picture. This we can do by including a 'transformed display file', that contains results of each transformation process and two sub-processes, one


FIGURE 4.2: Storage Tube Output Process
to build or generate display file code, and the other to traverse the file for picture generation onto the display. The display file may be divided into any number of logically distinct segments (e.g. Picture Book on the GT42) that may be separately created and erased. This configuration of the output processes for refresh display is shown in Figure 4.3.

It is also possible to have a transformed display file with a storage tube system, but here the display file is not of course used to refresh the display. It can nevertheless perform a very useful function in permitting part of the picture to be changed without the need to transform the whole picture. Instead, just the altered segment is re-constructed, then the screen is cleared and the entire display file is re-transmitted.

Figures 4.2 and 4.3 show some part of the output process enclosed by dotted lines to indicate that these sub-processes may be performed by special hardware. In the case of the storage tube, the display generator, picture store and the display combine together in one hardware package, e.g. the Tektronix 4010.

The GT42 is an example of a programmable refresh display capable of maintaining a segmented display file. It has a small local processor PDP $11 / 10$ to control the display and a simple monitor Picture Book [11] to generate and manipulate the display file and pass back user input. A more advanced form of refresh display would also include a hardware transformation capability e.g. the Vector General.

In each of the above configurations, the application program communicates with the graphics system by means of function calls. Input functions pass data from the input devices to the program, while output functions add line and text to the display file, modify the transformation parameters and manipulate display file segments.


## 4. DATA STRUCTURE FOR INTERACTIVE GRAPHICS

### 4.1 Basic Requirements

The data structure in a computer graphics system is important for two reasons. Firstly, we make use of various kinds of data organisation, when a graphics system based on display files is built. For example, Picture Book [11] for the GT42 refresh display uses a segmented display file and is conceptually structured into chapters, pages and lines. The package also provides the user with a number of functions for manipulating this structure. This kind of structure must be relatively simple if a display processor is to be able to trace through the file. Secondly, any interactive graphics program must be capable of building and manipulating a database.

The design of such a database should be flexible, and allow searching, accessing and updating to be performed quickly. The degree of structuring used by the application program to describe a picture, depends purely on the application itself.

The picture may have no particular structure, in which case it is best described in terms of a set of point coordinates. In this case it may suffice to use a simple list of the $x, y$ coordinates of the end-points of the straight lines which make up the drawing. Examples of this sort of problem include contour lines and graph plotting. Most pictures, however, have a definite structure; points and lines which represent a separate object, for example, are more closely associated than other points and lines in the display. The most common way of structuring the points and lines in a display is to associate them into sets. The application program then deals, not with points and lines, but with sets; for example, when a transformation (such as rotation or scaling) is applied to a set, it is applied by implication to all the points and lines
which make up the set. Situations like this and others require various degrees of complexity to be employed in their data structures, resulting in systems with different degrees of interactive capability. Conventional arrays and vectors, although they are very simple to implement and easy to use, do not perform well in an interactive situation. The reason for this is that they are essentially static data structures, and do not expand or contract during a program's execution. From this we can see that one of the most important qualities to look for in a data structure for interactive use is its ability to change during execution i.e. a dynamic structure. Another important programming concept also relating to computer graphics involves the connectivity between different objects representing some geometric model.

The need to be able to identify, recall, and manipulate these objects requires a well structured data model (database), which is a convenient descriptive representation of the collection of objects on the screen. Each object in the model may be described by a data block (record). A data block consists of fixed number of contiguous storage words describing a particular entity or figure. Thus, geometric figures represented by data blocks may be selectively created, moved, copied and erased.

### 4.2 Simple Array Representation

Often we do not need data blocks to be completely flexible, so it is possible to use the concept of array representation of figure elements to serve as a display list. Assume that we are concerned with only straight line segments, and that we wish to use a systematic method of listing the lines for display or for certain basic operations. Two possible representations may be used as illustrated in Figure 4.4.

|  | XLINEN, |  | YLINE(, K) |  |
| :---: | :---: | :---: | :---: | :---: |
| LINE NUMBER | $\mathrm{K}=1$ | $\mathrm{K}=2$ | K=1 | $\mathrm{K}=2$ |
| N | x1 | x2 | Y1 | Y2 |
| 1 | - | - | - | - |
| 2 | - | - | - | - |
| 3 | - | - | - | - |
| nne |  |  |  |  |



FIGURE 4.4: Array Representation of Lines

### 4.3 COMPOUND DATA STRUCTURE

If the data blocks are not stored contiguously in memory, the procedure is more complicated. In this case, we use a list structure in which data blocks or records are chained (connected) together by pointers. A pointer, a word containing an address, is a means of linking one data block with others in the data model. Such a link list may logically connect data blocks which are physically scattered arbitrarily throughout memory. In this way the computer understands the relationship among the objects represented by the data blocks and the relationship between the objects and computation routines. A simple form of a link list representing a physical object to be modelled is composed basically of data blocks, and the basic relationship between the objects are specified by means of pointers, (Figure 4.5a). If the last block in a list has a pointer to the first block in the list, then it is called a ring list, (Figure 4.5b). Usually one data block is designated as the head of the ring, and sometimes pointers from the other rings to the head block are useful.

Another arrangement which is sometimes useful is a set of twoway pointers, as shown in Figure 4.5c.

This consists of a backward pointer corresponding to each forward pointer, so that the program can traverse a sequence of data blocks in either direction.

It is very easy to update a list or ring structure. For insertion of a new data block, all that is required is to create the new block at any convenient place in memory and rearrange the pointer to include it in the list or ring. For deletion, the pointer to this data block to be removed are made to point to the next data block beyond the one to be removed and the unwanted

data block may then be removed.
A more complex structure could be built from these basic structures; examples include associative data structure and hierarchical structure.

The associative data structure can be used to relate objects with similar properties even though their data blocks are scattered through storage. We may define certain operators for manipulating the structure e.g. collect objects into sets, assign attributes to objects, delete objects and so forth. We must also devise a way of implementing this structure; for instance we can use rings but this is often inefficient. An alternative method is to use hash-coding [17] i.e. storing and accessing data according to some function (a hash function) of its data content. Some complex data structures use hash coding techniques together with list structures.

In a hierarchical data structure objects are arranged so that certain objects are subdivisions of another at a higher level in the classification scheme. There are two possible forms of this structure:
(i) A tree structure has an identification data block put at the top of the tree; it has pointers to the second level; which in turn have pointers to the third level data blocks, and so on.
(ii) The other hierarchial structure is similar to (i), but it incorporates the concept of a ring. On one ring, there may be branches from any data block to a logically related ring and so on. This structure allows access from any data block to any other via the rings. It is easy to update the structure, since nothing has to be moved in storage; only pointers have to be changed. However, the processing can become quite involved in a deletion operation, especially in making sure that all pointer chains are properly reconnected.

The cost for this more versatile organization is the extra overhead in storage caused by all the pointer chains. The use of very general forms of a compound data structure with a single system for a particular application is inherently inefficient, since it requires excessive storage space and operating time. It has therefore been customary to devise simpler data structures which are tailored to each specific application. In this way storage space, access time, and complexity are minimised, even though considerable design and programming time may be required for development of this data structure.

Typical problems that a generalised structure must be able to resolve are:-
(i) An individual graphic object must be identifiable.
(ii) The relationship, hierarchical or otherwise, between objects must be established.
(iii) Some properties may be shared by different objects, and conversely objects may be allowed to have multiple properties.
(iv) Since drawing may be modified, deleted or expanded in interactive problem solving, data structures must allow for dynamic growth and dynamic association.

The example in Figure 4.6 illustrates a hierarchical data representation of the square (SQ) and circle (CR) using a ring structure. A block; called 'FIG' associates the square and the circle which is also reached from the square block. The centre and radius of the circle are defined in block CR. All blocks may be reached from any given block and the 1 ines are defined in separate blocks (L1 through L4). The end points of a line are also defined as separate blocks and are actually subordinate to these lines.



FIGURE 4.6: An Example of Ring Structure

## Chapter 5

## THE GRAPHICS SOFTWARE PACKAGE 'LIGHT'

1. INTRODUCTION
2. THE CURRENT ENVIRONMENT
2.1 Hardware Configuration
2.2 UNIX Software System
3. DESIGN CRITERIA
4. LOW COST DISPLAY TERMINAL
4.1 The Tektronix 4010
4.2 Operating Modes
5. STRUCTURE OF THE LIGHT PACKAGE
5.1 The Graphics Library
5.2 Organization
6. DESCRIPTION AND IMPLEMENTATION OF LIGHT
6.1 LIGHT-UNIX Software Interface
6.2 LIGHT Proper
6.3 Basic Transformations
7. THE GT42 IN EMULATOR MODE

## 1. INTRODUCTION

This chapter presents in detail the development and implementation of the graphic software package LIGHT (Loughborough Interactive Graphics system for Tektronix 4010) under the UNIX time-sharing system on the PDP 11/40 mini-computer.

## 2. THE CURRENT ENVIRONMENT

### 2.1 Hardware Configuration

The hardware configuration on which LIGHT was developed consists of the PDP 11/40 mini-computer central processor unit (16-bit word) with 60 K words of core store. The present installation has two moving head disc drives RKO5 each of which provides 2.5 M bytes on a removable disc cartridge. There is also a high-speed paper tape reader PR11, a DECwriter console LA30 matrix printer, a storage tube graphics terminal Tektronox 4010 and a variety of alphanumeric terminals:
$7 \times$ KSR33 and $2 \times$ ASR33 teletype;
$3 \times$ Newbury Laboratories 7002 VDU's;
$1 \times$ Tektronix 4023 VDU.
Shortly after the development of LIGHT, a GT42 refresh display graphic terminal was installed. This consists of PDP 11/10 central processor unit (CPU and store), display processor unit, communication interface, keyboard unit, CRT display unit and a light pen. Figure 5.1 illustrates this hardware configuration, part of which makes our graphics system.

### 2.2 UNIX Software System

UNIX time-sharing system has been operational since late 1976 on the above-mentioned hardware configuration in this department. It is a general-purpose, multi-user, interactive operating system which provides


FIGURE 5:1: Hardware Configuration
many facilities of a large system [18]. Among these features are:
(i) a hierarchical file system incorporating demountable volumes,
(ii) system command language selectable on a per-user basis,
(iii) the ability to initiate asynchronous processes.

Besides the system proper, there are a number of major system programs available, of which the following were used extensively in the development of this work:

Assembler which resembles PAL-11R
Text editor based on 'QED'

Linking loader
Fortran compiler.

User communication with UNIX is effected with the aid of a program called 'Shell'. This is a command line interpreter; it reads lines typed by the user and interprets them as requests to execute other programs. Shell is also a command by itself and may be called recursively to execute a series of other commands placed in a file.

The main feature of this system is a versatile, convenient file system with complete integration between disc files and all input/output devices. From the point of view of the user, there are three kinds of files:-
(i) Ordinary file: contains whatever information is placed on it, for example, Fortran programs or textual information.
(ii) Directory: is like an ordinary file except that only the system can modify it. It provides the mapping between the names of files and the files themselves. The file system is a tree-structured hierarchy originating at a root directory. Each user has a directory of his own; he may also create subdirectories to contain groups of files
conveniently treated together. Any type of file can occur at any level. At any given time a user process is associated with a particular current directory. When the user program wishes to open or create a file, it gives the system the name of a file in the current directory or it gives a path name which either specifies the absolute location in the tree or the location relative to the current directory. A system directory exists which contains all the programs provided for general use [19]. File system protection consists of associating with the file at time of creation the name of the creator and permitting him to specify whether he and others can read and write the file.
(iii) Special file: each I/O device supported by UNIX is associated with at least one such file. Special files are read and written just like ordinary disc files, but a request to read or'write results in activation of the associated device. UNIX I/O system supports a large number of device drivers, which share a great many routines as well as a pool of buffers. It is not necessary that the entire file system hierarchy resides on the same device (e.g. disc pack). On our installation for instance, the root directory resides on the system disc, and all users' files are contained on another removable disc which is mounted by the system initialisation program.

UNIX occupies 20.8 K words of core memory, the rest ( 39.2 K ) being available for user programs. The name of any executable program can be ' used as a command. This name is first searched for in the current directory and if that fails, it is then searched for in a system library. A myriad of commands are available including those for listing directories, moving, copying and deleting files, and changing the
current directory. Another feature of the system is the ability to initiate asynchronously executing processes from within a program or from command level. The command interpreter creates a process to execute the command and wait for its completion.

## 3. DESIGN CRITERIA

In general, the process of building a graphics system can be described as follows:
(i) Choose the language on which to base the system
(ii) Design the functions or language extension
(iii) Write and document the software to perform the graphics functions.

The first two steps constitute the design of what is sometimes called a 'graphics language'. These graphics functions play a vital part in determining the success or failure of the system; and should give the programmer control over the system hardware/software. Some systems are built in the form of a graphics package i.e. as a set of functions or subroutines to be called by application programs written in a high level language. An alternative approach is to design a special programming language; this generally amounts to choosing an existing language, and then extending and modifying it where necessary to perform certain graphics tasks. The first approach was adopted in building up the graphics package LIGHT. This offers greater flexibility; if future experience indicates the need for additional functions, then the appropriate function could be added more easily.

It is essential to make graphics systems not only inexpensive but simple to program. The programmer, whether novice or expert, should find it as easy to write a graphical program as a non-graphical one.

Therefore, the design of the graphics subroutines package 'LIGHT' was influenced by several criteria. The fundamental aim was to provide the user with an immediate, simple but powerful means of writing a graphics application program. Thus, the package was written in a high level language so that it would shield the programmer from the low level features of the hardware. Fortran was chosen because graphics display systems are likely to be used for engineering and scientific applications, and this is the most widely accepted programming language in these fields. In addition, Fortran is also available on virtually every computer, which makes the package to a certain extent portable. Hence, LIGHT was coded in UNIX Fortran which is a subset of ANSI Fortran, and care was taken to minimize the use of non-standard features. However, it is possible to implement the package in a different language, since the set of functions are carefully designed to be independent of any specific language for its implementation.

Early in the design, it became apparent that LIGHT should provide only general-purpose facilities for using the graphic display terminal. For example, the subroutines should neither generate geometric figures (e.g. circles, triangles, logic elements) nor impose constraints on the structuring of modules, since the way in which geometric figures are generated appears to be dependent on applications. However, for these purposes, users can develop libraries of routines that are more in accord with their needs. Another important factor in the design was to assume a set of default conditions that an application programmer would usually require. If he does not take positive action to change them, these remain in effect throughout execution of his program. Whenever default conditions are overridden the newly entered condition prevails from that point on, rather than the default condition.

LIGHT also does not contain any data structure facilities nor does it use a mandatory data structure for picture representation. These are
awkwardin that they force a user to think in a particular way, and tend to be inefficient, especially in store requirements. This last difficulty is exacerbated by the problems of dumping and restoring from secondary storage. Further, no particular data structure is convenient for even a majority of applications. Another reason for not having a mandatory graphical data structure is that the complexity that would result would prevent use of the software by non-specialists. The following facilities are available under the software graphics package LIGHT:-

1. Initialisation routines for setting the default values
2. The primitive graphics functions for point and line drawing
3. Character and text handling
4. Cursor and menu operations
5. Linear transformation and clipping
6. Simple perspective projection
7. Other utility routines.

Several hardware limitations had dictated the extent of the facilities that were provided by LIGHT. For example, the available disc space was limited because the computer resources were also distributed among up to 14 other time-sharing users working in other areas. In addition, the amount of core store available to the graphics user would necessarily be shared by LIGHT. Also, run-time response was noticeably slow, partly due to the absence of floating point hardware. These and various other constraints, involving both hardware and software, required that the coding of the package be written efficiently. Since graphics is only a part (usually a small part) of most applications it can only expect its fair share of computing resources. Efficiency is not only a function of implementation; it depends also on the design of the user interface. When the software takes the form of a library of subroutines, the
function and form of each subroutine is important. Efficiency in terms of computation time is largely a run-time issue although the form of the library must be such that the package can always avoid unnecessary computation. However, programs using floating point (FP) assume that the FP processor is available, so the Fortran compiler generates code using these instructions. On our current configuration which does not have a FP processor these instructions are trapped as 'illegal' and they are interpreted by software routines linked into the object program. The net effect of this is that although the programs run perfectly well they are very slow and tend to impose a large overhead on the rest of the system because of the huge number of interrupts that must be serviced. Additionally the above software routines require disc space and loading time.

## 4. LOW COST DISPLAY TERMINAL

4.1 The Tektronix 4010 Display Terminal

There is a growing demand for low cost computer graphics for small scale computer users or for the user who would rather have easy access to a somewhat less sophisticated console than have very limited access to a more powerful but far more expensive device. Tektronix 4010 offers this opportunity with its vector capabilities and character writing speed [20]. Such terminals may be used both for time-sharing and for solving conventional graphics problems at an affordable price. This requires a set of functions to transmit line and text information to the terminal in response to function calls generated by the application program.

The real difficulty in using this sort of terminal lies in compensating for its relatively poor performance which includes several
deficiencies; poor picture quality, unsatisfactory transmission rate and in most cases, lack of selective erasure capability. The terminal uses serial transmission, both for text and for graphics information. For example, a vector is transmitted to the terminal as a special control character followed by four characters specifying the length of the vector. This use of character transmission greatly simplifies the task of integrating these terminals into an existing time-shared system (e.g. UNIX). The use of serial transmission generally imposes a fairly severe limit on the speed at which pictures can be transmitted, for speeds above 2400 baud (bits/second) are usually beyond the capacity of the transmission line. The problem of lack of selective erasure combined with the low transmission speed and poor time-shared response makes dynamic graphics almost impracticable.

### 4.2 Operating Modes

The main mode is character (Alpha) mode; in this mode data characters received are interpreted either as characters to be plotted or as ASCII control characters (e.g. carriage return, line feed) depending on the status of the two high order bits. Certain control characters have been given special meanings for performing special functions: for example, 'GS' sets the terminal to graphics mode, 'US' changes the terminal to Alpha mode. In graphic mode, data representing $X, Y$ coordinates are plotted (as points and lines) until the mode is changed back to character/control mode. By ASCII convention, all control characters are distinguished from graphics data characters, by adding two high order (tag) bits in each byte of the latter. The 4010 has only one graphic mode and often uses a pair of characters for some control functions e.g. ESC,FF to erase screen.

## 5. STRUCTURE OF THE LIGHT PACKAGE

### 5.1 The Graphics Library

The graphical aspects of an application appear in a program as calls to subroutines to draw lines on the screen, output textual information, raise the cross-hair cursor and develop menus, items of which may be picked from the screen by the cursor. The LIGHT package takes the form of a Fortran-callable library of subroutines, each of which requires a minimal set of parameters. The graphics library was written with few initial applications in mind, so that the main features were immediately and continuously tested. The result is an easily-used system that allows Fortran programmers to produce debugged interactive graphics programs as readily as conventional batch processing programs.

Due to the dynamically changing requirements typical of graphics application programs, it was important to make the facilities offered by UNIX indirectly available to the graphics program through the use of structured library files. Consequently the system would automatically decide which LIGHT subroutines should be loaded with the application program into main store. Effectively the UNIX linking loader would search the library exactly at the point it has encountered the call and only those routines defining unresolved external references are loaded. Therefore it is important that the order of the subroutines in the library must be correct. That is, if a routine from a library references another routine in the library, the referenced routine must appear after the referencing routine in the library. All such references must be resolved before a load module can be executed. Every source file representing a single library subroutine is compiled independently to produce an object file. The group of the object files is then archived into a single library file named 'LIGHT'. This consists of 53 subfiles each of which can be individually updated, replaced or deleted. The
library can be maintained by using the UNIX command 'AR' which is an archive and library maintainer [19], allowing the user various options such as copy, append, delete, replace and extract an object file from/to the archive file LIGHT.

### 5.2 Organization

Functionally, the LIGHT subroutine package is organized into three separate and distinct modules:
(i) LIGHT-UNIX software interface
(ii) LIGHT proper
(iii) Basic (geometric)

Each module has a certain task to accomplish offering the user various facilities that he may require in his graphics application program. These modules can be independently updated or modified without affecting one another. This modular design approach has an important consequence for future extensions to the facilities currently offered by LIGHT. It also provides some degree of device independence. Although this package was intended primarily for the Tektronix 4010 display, it was designed so that other graphics devices can be incorporated with limited programming effort. This was apparent when LIGHT was easily extended to run on the refresh display GT42 in Emulator mode (Appendix l.8). Moreover, the transformation module is completely device-independent and without any modification it can be used directly with the Picture Book package [11] designed for the GT42 refresh display.

The detailed description and implementation of each module will be presented in the next section. A very large portion of LIGHT subroutines, including all the user-callable routines are entirely written in standard ANSI Fortran, and constitute the 'Front end'. These in turn call other routines, which are not user callable and constitute the device/system
dependent part, and are termed the 'back end'. This is the interface between the front end and the device. It also provides the interface between the front end and the machine/operating system as in our case with PDP 1l/40/UNIX. Because of this structure, a program containing LIGHT routines can be considered to be in three parts. These are the main program, LIGHT front-end, and LIGHT back-end routines as illustrated in Figure 5.2. The total size of the main program will vary according to its function.

All the information required by LIGHT is conveyed via subroutine arguments and so programs may be no more than a series of Fortran calls. Thus a Fortran programmer can introduce himself to graphics with minimal effort. It is important to emphasise that LIGIIT satisfies the basic needs for creating graphics application programs. As mentioned earlier, there is no data structure imposed by the package; thus any data structure may be defined by the calling program.

## 6. DESCRIPTION AND IMPLEMENTATION OF LIGHT

### 6.1 LIGHT-UNIX Software Interface

This provides the means of interfacing LIGHT package with the UNIX system. Its primary objective was to facilitate the link between the graphics library and UNIX I/O system. This was desirable in order to handle all I/O of graphical information coded in single ASCII characters; including special control characters to the Tektronix 4010 display terminal. This is not normally possible with the use of Fortran I/O alphanumeric string format.

In addition, under the existing environment the interface also provides some utility routines that have been found to be useful in


FIGURE 5.2: Structure of LIGHT Software Package
writing graphics programs. They enable the application programmer to exploit some feature of the UNIX file system, through Fortran calls incorporated in his program. This software interface was implemented using a number of UNIX system entries [21]. These allow the UNIX user to communicate easily with the file system. This lowest possible user level is'designed to avoid distinction between the various devices and files and between direct and sequential access. No large 'access method' routines are required to insulate the programer from the system calls; in fact all user programs either call the system directly or use a small library program, only few instructions long, which buffers a number of characters and reads or writes them all at once. Their calling sequence is usable either in assembly or C-1anguage. Assembly language [22] was naturally chosen, as UNIX Fortran permits calls to routines written in assembly code using certain calling sequence conventions. It was not possible to use the C-language portable library, because C-programs can not communicate with Fortran programs in the current system environment. The calling sequence convention used in coding these assembly routines is as follows:

1. Save register R3,SP (stack pointer)
2. Arguments list (pointer to values) begins at $2(\mathrm{R} 3)$.
3. Entry name is name of function or subroutine followed by "."
4. First word after entry point is location of return value.
5. Second word after entry point is pointer to PDP-11 code body
6. Return is expedited by a 'Jump' to the global routine 'retrn'. The following assembly coded routines (Appendix 1.1) are essential to support the running of LIGHT under UNIX:
(i) Input/Output single character routines
(ii) Cross-hair cursor graphics input routine
(iii) File overlaying routine
(iv) File deletion routine

These form part of the back-end which is machine/operating system dependent.

## (i) Input/Output Single Character Routines

These routines namely 'INCHAR' and 'OCHAR' handle the I/O transfer between the LIGHT package and the display terminal through the use of UNIX I/O system calls. As mentioned previously UNIX treats I/O devices as special files in which reading and writing is done just like ordinary disc files. A special scheme is available whereby device drivers may provide the ability to transfer information directly between the user's core image and the device without the use of large buffers. The method involves setting up a character-type special file corresponding to the 'raw' mode. In this mode, every character is passed immediately to the program without waiting for a full line.

The display terminal 4010 is treated normally as a teletype terminal with asynchronous communication interface DL11E which supports most common ASCII terminals. Under UNIX a disc file or device is associated with a file descriptor, an integer between 0 and 9 . It is used to identify the file in subsequent read, write or other I/O calls. The file descriptors ' 0 ' and ' 1 ' are designated for standard input and output respectively. In coding these two Input/Output routines, the following I/O system calls [21] were employed:

GTTY:- This essentially stores the current STATUS information of the terminal whose file descriptor is given in register RO in a three words argument. The mode of the terminal is contained in the third word which is saved before the status of the terminal is changed to 'raw' mode so that its normal mode can be restored after I/O operations are carried out.

SIGNAL:- This ensures that the terminal would restore to its normal mode when an interrupt signal is generated by some abnormal event, initiated by the user at the terminal or by program error. Normally all such signals cause termination of the program, unless special action has been taken. In these routines the label EXITl specifies the address where the interrupt is simulated. The normal status of the terminal is subsequently restored.

STTY:-
This converts the mode of the terminal to raw mode by setting the third status word to (octal) 000040, and then restores it to its normal mode after $1 / 0$ is accomplished.

READ/WRITE:- A single I/O call produces direct transmission between the terminal and user's read/write buffer, so that raw I/O is considerably more efficient when many words are transmitted. These system calls require two arguments:
(1) the user's buffer address, and
(2) the number of contiguous bytes, (in this case, one). The number of characters actually read or written is returned in register RO .

## (ii) Cross-Hair Cursor Graphics Input Routine

It is possible to exploit the Tektronix 4010 as an interactive terminal, since it has a program controllable cross-hair feature and therefore a graphics input capability. To make this easily available to the user, this routine was developed using the UNIX I/O system entries for raising the cross-hair cursor and reading the digitized
coordinates. Again the same system calls as in (i) were invoked in raw mode to implement this routine. The entry name of this routine is 'CURSON', which works as follows:-

1. The cross-hair cursor is raised. This requires transmission of two ASCII control characters ESC and SUB(27 and 26 in decimal respectively) to the terminal. The user can then change the cursor control to the desired intersection point.
2. When the user strikes a keyboard character, the character and the coordinate location are sent to the computer. Consequently five bytes of cursor information are read by this routine. These graphics input bytes represent the keyboard character plus a four byte sequence containing high and low order $X$, and high and low order Y. Each byte contains the two tag bits plus five binary bits. Each byte thus encodes to an ASCII character. Figure 5.3 illustrates this computer response to graphics input from the cross-hair cursor.

After the cursor information is read, the Alpha cursor returns to its home location (top-left hand corner). The status of the terminal is returned to 'cooked' (normal) mode.

## (iii) File Overlaying Routine

The limited memory size of our machine has been quite successfully offset by the development of a very easily used overlay capability. The programmer need only divide his program into smaller modules to fit the available core size. These modules could be stored on the disc as 'program files' which may subsequently be called and executed almost as subroutines. When module segments are called from the disc, the new segment with the help of UNIX system entry EXEC is loaded and executed. The system call EXEC overlays the calling process with the named file and


RESPONSE TO COMPUTER

USER ACTIN

1. SET CROSSHAIR CURSOR
2. STRIKE KEY

FROM COMPUTER


FIGURE 5.3: Response to Computer Command and Cursor Control
then transfers to the beginning of the core image of the file. All code and data in the process using EXEC is replaced from the named file, but open files, current directory and interprocess relationships are unaltered. Only if the call fails, for example when the file can not be found or its execute-permission bit is not set, does a return take place from the EXEC; it resembles a 'jump' machine instruction rather than a subroutine call. The first argument to EXEC is a pointer to the name of the file to be executed. The second is the address of a nullterminated list of pointers to arguments to be passed to the file. The entry name of this routine is 'OVLAY'.

## (iv) File Deletion Routine

This is another system entry in the UNIX file system. It removes the entry for the named file passed as an argument from the current directory. This routine makes use of the system call UNLINK. It may be useful in removing intermediate files created by application programs. The entry name of this routine is 'FLRM'.

### 6.2 LIGITT Proper

Efficiency and flexibility are key points when generating routines to run graphics programs. The LIGHT module provides this capability with a set of Fortran-callable subroutines which form the central part of the LIGHT package. These routines support a wide range of applications in an efficient and cost effective manner. The basic structure is modular, thus providing access to individual features of the graphics hardware and/or software. Through these routines the graphics program has full control of the terminal character/vector generators and the graphic input device. This facilitates the construction of displays from basic graphic elements and program communication with the display
and console operator. The library subroutines are divided conceptually into four categories:-
(i) Initialization
(ii) Point and line drawing
(iii) Character and text handling
(iv) Cursor and menu operations.

The functions of the subroutines for each category are summarized in Table 5.1, (see also LIGHT-User Guide, Appendix 1.9).

TABLE 5.1: Basic LIGHT Subroutine Library
Category Subroutine Purpose
(i) Initialization: TXOPEN

TXCLER

TXVPRT(XO,YO,X1,Y1) Defines a physical 'viewport' on the screen.
TXWIND (XO,YO,X1,Y1) Defines a 'window' in problem space and maps this on to the viewport.

ALPHMD Switches the display terminal
to 'Alpha' mode for input/
output of Alphanumeric information.

Switches the display terminal to 'Graphic' mode and returns to the previous beam position.
(ii) Point and Line drawing:

| $\operatorname{TXMOVE}(X, Y)$ | Moves current beam position |
| :--- | :--- |
|  | to scaled point $(X, Y)$ without |
| drawing. |  |
| TXMOVR(DX,DY) | Moves current beam position <br> through a displacement (DX, DY) |
|  | without drawing. |


| CategorySubroutine <br> TXDRAW $(X, Y)$ | Purpose |
| :--- | :--- |
|  | Draws a visible straight line <br> from the current position to |
|  | point $(X, Y)$. |
|  | Draws a visible displacement <br> (DX,DY) from the current bean |
|  | position. |

(iii) Character and text handling: TXGET (ICHAR)

TXPUT (ICHAR) Displays a character whose ASCII code is ICHAR. Interprets TAB as a space and RUBOUT as several superimposed characters.
TXLINE (STRING,N) Inputs a line of characters from the keyboard into the array STRING and Echoes to the screen. Deals with TAB and RUBOUT as above.
MESSAG (TEXT) Displays characters specified as Hollerith string 'TEXT'.
TEXTUP(Filename, $N$ ) Displays $N$ lines of textual information previously stored in the named disc file. Obtains the next input integer from the keyboard. Removes spaces, and other nonprintable characters from the Hollerith string TEXT.
DTEXT (X,Y,TEXT, $N$ ) Displays the Hollerith string 'TEXT' at scaled coordinate point ( $\mathrm{X}, \mathrm{Y}$ ) on the screen.
(iv) Cursor and menu operations:
(a) Cursor Control:
$\operatorname{TXCURS}(X, Y, I C H A R)$ Sets the cross-hair cursor, reads the cursor coordinate position and the character entered.

| Category | Subroutine | Purpose |
| :---: | :---: | :---: |
|  | CURPOS ( $\mathrm{X}, \mathrm{Y}$ ) CHTOXY (NLINE, | Positions the Alpha cursor at the specified point ( $\mathrm{X}, \mathrm{Y}$ ). IX,IY) |
|  | : . | Converts character coordinate (NLINE,NCIIAR) to screen coordinate (IX,IY) of the bottomleft hand corner of the character. |
|  | XYVOCH(IX, IY, NLINE, NCHAR, IA, IB) |  |
|  |  | Converts the screen coordinate (IX,IY) to character coordinate (NLINE,NCHAR). |

(b) Menu operation:

| MNOPEN ( $X, Y, \mathrm{MNO}$ ) | Announces that a menu is to be displayed whose origin (top-left hand corner) is at screen coordinate (X,Y). |
| :---: | :---: |
| MNTEXT (TEXT, N, MNO) | Displays the next menu item 'TEXT' of N characters. |
| MNPICK (I, ICHAR,MNO) | Raises the cursor, allowing the user to pick an item from the menu, and returns the item index in I . |
| MNDISP (TEXT, M, LEN, MNO) |  |
|  | Displays a complete menu containing the TEXT of $M$ items |
| FRAME ( $\mathrm{X}, \mathrm{Y}, \mathrm{NC}$ ) | Draws a rectangle round the menu whose origin is at the point ( $X, Y$ ). |

## (i) Initialization

These routines (Appendix 1.2) are concerned with setting up the display terminal before any subsequent output is directed to the display by other calls. The Tektronix 4010 contains $1024 \times 1024$ addressable points, of which 1024 by 781 are in the viewable area of the screen.

De fault values for the display viewport and window are set by TXOPEN to contain $1024 \times 781$ addressable points; this was chosen because points just above 780 may beivisible but marginal in quality.

Routines TXVPRT and TXWIND are provided for further control of the mapping between the problem space and the screen viewport. These two routines effectively alter the default values and enable the user to specify a rectangular area on the screen within which a picture is drawn. The user is also provided with a routine (TXCLER) to clear the display; this sets the terminal to Alpha-mode and returns the Alpha cursor to its home position. In addition, the terminal can be set to graphic mode (GRPHMD) or to Alpha-mode (ALPHMD) as appropriate. These routines would enable the graphic program to Qutput textual information to the screen in the middle of drawing a picture, thus giving the user full control of the terminal mode.

## (ii) Point and Line Drawing

Display images are composed of basic visual elements (primitives) which the terminal can generate. Essentially the only graphical primitives that the programmer needs are functions to define points, lines and displayed text strings. The main criteria in choosing a set of primitive graphical functions are as follows:-

1. Clarity: the functions will often be used by relatively inexperienced programmers, and should be as simple and comprehensible as possible.
2. Convenience: the functions should permit all forms of pointand line-plotting and positioning both by relative and by absolute coordinates.
3. Compactness: the set of functions should not be too large, for this will enlarge the software system. Circles and other
more complex constructions should be provided outside this set.

The basic functions for point and line plotting (Appendix 1.3) are:

| TYPE | MODE |  |
| :--- | :---: | :---: |
|  | Absolute | Relative |
| MOVE | TXMOVE $(X, Y)$ | TXMOVR (DX, DY) |
| DRAW | TXDRAW $(X, Y)$ | TXDRWR (DX, DY) |

These routines in turn call upon two other routines XVPLOT and VPLOT which constitute part of the 'back-end':
(a) XVPLOT:- This mainly converts the user specified coordinates into physical screen (raster) coordinates in integer form. It also checks against any attenpt to output coordinates off the screen. If this happens, an error message ('coordinate off screen') is displayed, reminding the user to revise his coor̦dinate setting.
(b) VPLOT:- Graphic plotting information is sent to the terminal in four byte sequences, each containing high and low order $Y$, and high and low order $X$. Thus, this routine sets the terminal to graphics mode by sending the ASCII control character GS (29 in decimal), followed by the four ASCII characters carrying the graphic data for vector plotting. After a GS and the initial four bytes have been sent to the 4010 , additional bytes that do not change (except for the low X byte) need not be sent; however, low $Y$ bytes must be sent if high $X$ byte has been changed. The low $X$ byte must be sent each time to cause the point or vector to be drawn. Vectors are drawn from the old address to the new address with the exception of the first vector after entering the graphic mode. Figure 5.4 illustrates the method of computing the four bytes. Each number is converted


FIGURE 5.4: Computing 4 bytes of data for $X=50$ and $Y=31$
to its 10-bit equivalent, which is divided into high and low 5-bits. The bytes are then assembled as shown with two tagbits added.

## (iii) Character and Text Handling

A set of routines (Appendix 1.4) is provided by LIGHT, allowing the user to incorporate standard keyboard interaction in his graphics application program. Keyboard input, for example, can be used to good effect to input textual information which cannot be predetermined. Textual output information can be used to prompt the user to perform a particular action and the application program is instructed to wait for the user's response. Thus terminal users can communicate with an application program by means of alphanumeric Input/Output. The implementation of these routines makes extensive use of INCHAR and OCHAR, which transmit character information directly to the terminal in raw mode. The routines handle simple and composite input/output. Some special characters are also dealt with at the user level, for example, TAB is interpreted as a suitable number of spaces; RUBOUT is displayed as several superimposed characters, the deleted character being removed from the character string.

## (iv) Cursor and Menu Operations

LIGHT provides the user with the facility to input and output graphical information. In addition to the standard keyboard interaction, the programmer can also incorporate graphical interaction via the cursor. Cursor input provides identification to the program of selected items on the display screen. The Tektronix 4010 graphic cursor described in section 6.1 (ii) was programmed to read five graphic input bytes containing the cross-hair cursor coordinates and the input keyboard character. The
conversion from graphic input bytes to numerical coordinates is a straight forward operation which is performed by the routine CURSET (Appendix 1.5) as

$$
\begin{aligned}
& \text { X-coordinate }=32(\text { high X-32 })+\text { low X-32 } \\
& \text { Y-coordinate }=32(\text { high Y-32 })+\text { low Y-32 }
\end{aligned}
$$

The Fortran-callable subroutines provided in here fall into two kinds:
(a) cursor control with routines to interpret screen coordinates as character positions.
(b) Menu display and cursor choice therein.

In (a) the routine TXCURS activates the cross-hair cursor by calling the CURSET routine. The returned value of cursor location ( $X, Y$ ) on the screen is tested for violation of the boundary limit specified by the current viewport, and if so, a warning message ('illegal cursor position')
is displayed. The cursor coordinates are subsequently converted from screen to problem coordinates. Two other routines are also available (CHTOXY and XYVOCH) in (a) for relating the character coordinate (NLINE, NCHAR), pointed at by the cursor to screen coordinate ( $X, Y$ ). Basically, the $Y$-coordinate is mapped into the line number, and the X -coordinate corresponds to the character within the line. These routines are particular useful for graphical text editing.

The routines in category (b) are concerned with the handling of user defined menus. They enable the programmer to display a menu anywhere on the screen (MNOPEN) and pass control to the terminal user (MNPICK). When a particular item is picked up from the menu by means of the crosshair cursor, an arrow would be drawn adjacent to the selected item to indicate that the user request is accepted. However, if the horizontal cursor line is placed outside the valid item zone(s) (Figure 5.5) the cursor would return and no arrow would be drawn, allowing the user to try again.

### 6.3 Basic Transformation

For the purpose of visualisation, graphical information is usually transformed so as to provide a particular view on a display, and further manipulation is sometimes desirable in order to enhance the visualisation in various ways. The transformation facilities in LIGHT may be considered as performing three basic functions:-
(a) Object orientation with respect to the selected coordinate system, e.g. rotation and translation, to obtain a particular view.
(b) Relating the user's coordinate system to the display coordinate system.
(c) Various types of projection and distortion such as perspective, isometric projection, etc. This is mainly used to aid the visualization of objects. There are other visualization techniques, such as hidden line removal [1], intensity modulation and shading.

The transformation functions should be simple to use and efficient in execution. Luckily these two requirements do not conflict, as efficiency in transformation is gained by combining scaling, rotation, translation and perspective projection into a single matrix that applies to the end point coordinates of each line of a given object.

The range of effects that can be produced by transformation is very large and is catered for in its generality by a vocabulary of basic transformations. The basic vocabulary is supplemented by some special routines (themselves using the basic routines) which provide facilities that are generally useful and that can be easily specified. Such routines include axonometric projection (parallel projection) and perspective viewing (point projection) from any viewpoint. The use of homogeneous coordinates ( $x, y, z, t$ ) to define three-dimensional objects
allows either 'affine' or perspective transformations to be applied with equal ease [23]. The three-dimensional point (or vector) corresponding to ( $x, y, z, t$ ) is

$$
\begin{equation*}
(X, Y, Z)=\left(\frac{x}{t}, \frac{y}{t}, \frac{Z}{t}\right) \tag{5.1}
\end{equation*}
$$

The generalised $4 \times 4$ transformation matrix based on such a homogeneous coordinate representation is

$$
\underset{\sim}{A}=\left[\begin{array}{ccc:c}
S_{x} & C_{12} & C_{13} & P_{x}  \tag{5.2}\\
C_{21} & S_{y} & C_{23} & P_{y} \\
C_{31} & C_{32} & S_{z} & P_{z} \\
\hdashline T_{x} & T_{y} & T_{z} & S^{2}
\end{array}\right] \quad\left[\begin{array}{c:c}
\mathrm{L} & \mathrm{P} \\
\hdashline & T
\end{array}\right.
$$

which naturally partitions into four separate submatrices:
(1) $L(3 \times 3)$ produces a linear transformation in the form of scaling, shearing and rotation.
(2) $\mathrm{T}(1 \times 3)$ row produces translation
(3) $\mathrm{P}(3 \times 1)$ column produces perspective transformation
(4) $S(1 \times 1)$ single element produces overall scaling.

When the vector [ $\begin{array}{llll}X & Y & Z & 1]\end{array}$ is transformed by the most general $4 \times 4$ matrix A it will become the vector [ $x^{*} y^{*} z^{*} t^{*}$ ] which is usually normalised to [ $\left.X^{*} Y^{*} Z^{*} 1\right]$, as shown mathematically by

$$
\left[\begin{array}{llll}
X & Y & Z & 1
\end{array}\right] * A=\left[\begin{array}{llll}
x^{*} & y^{*} & z^{*} & t^{*}
\end{array}\right] \rightarrow\left[\begin{array}{llll}
X^{*} & Y * & Z^{*} & 1 \tag{5.3}
\end{array}\right]
$$

The set of routines (Appendix 1.6) that produce these transformations are summarized in Table 5.2. These routines permit both two- and three-dimensional pictures to be transformed, and assumes the existence of two transformation matrices:

RTM:- the previous reference transformation matrix
TM:- the accumulated transformation matrix resulting from calls to any of the routines - TRANSL, SCALNG, ROTATE, PERSP and PROJCT.

Both these matrices must be declared by the user in his program as COMMON/MATRIX/RTM $(4,4)$,TM $(4,4)$
Category , Subroutine Purpose

1. Linear transformation: SCALING(SX,SY,SZ) Superimposes scale changes along the $X, Y$ and $Z$ axes as specified.
ROTATE (RX,RY,RZ) Rotates about axes $X, Y$ and $Z$ by the angles RX,RY and RZ (degrees) in this order.

TRANSL(TX,TY,TZ) Translate the current point $(X, Y, Z)$ through the displacement TX,TY and TZ.
2. Clipping(windowing): CLIP(CLINE, XO, YO, $\mathrm{X} 1, \mathrm{Y} 1, \mathrm{IREJ}$ )

The line CLINE is clipped to the rectangular window $\mathrm{XO}, \mathrm{YO}, \mathrm{X1}, \mathrm{Y} 1$.
3. Simple perspective projection:

| PERSP (PX, PY, PZ) | Sets up a perspective view where $P X, P Y$ and $P Z$ are the reciprocals of the viewing distance from the planes $Y Z$, $2 X$ and $X Y$ respectively. |
| :---: | :---: |
| PROJCT (NPLANE) | Projects on a given NPLANE where $\operatorname{NPLANE}(1,2$, or 3$)$ specifies the coordinate plane of projection (i.e. $\mathrm{x}=0, \mathrm{y}=0$ or $\mathrm{z}=0$ ). |

4. Transformation control:

| SAVMAT (A) | Saves a copy of the transformation matrix A into the stack. |
| :---: | :---: |
| RESTOR (A) | Restores the transformation matrix A from the stack. |
| UNITY (A) | Sets the transformation matrix A to unit matrix. |
| SETMAT (A) | Sets the reference matrix RTM to A. |
| CONCAT ( $A, B, N$ ) | Postmultiplies matrix(vector) $A\left(N^{\times} 4\right)$ by $B(4 \times 4)$ and leaves result in A . |

The RTM matrix can be updated by the accumulated matrix TM by concatenation (RTM $\times$ TM). The current transformation can be modified, reset, saved or suspended at any stage and TM is available to the user for inspection. The basic transformations are in general non-commutative and so there are inherent perils involved in combining them. Typically, an error in ordering transformations could result in the whole picture being outside the visible area.

## 1. Linear Transformation

These routines have an important role in building up a picture. If a picture part occurs more than once, in different orientations, it can be defined once and the other instances correctly oriented by use of these routines.

Scaling:- The diagonal terms of the general $4 \times 4$ transformation matrix produce local and overall scaling. The routine SCALNG sets the first three diagonal terms which represent the local scaling with scale factors $S X, S Y$ and $S Z$. Consider the following transformation:

$$
\left[\begin{array}{lll}
X^{*} & Y^{*} & Z^{*}
\end{array}\right]=\left[\begin{array}{llll}
X & Y & Z & 1
\end{array}\right]\left[\begin{array}{llll}
0 & S_{y} & 0 & 0  \tag{5.4}\\
0 & 0 & S_{z} & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

which shows the local scaling effect.
Global scaling may be obtained by using the fourth diagonal element, i.e.,

$$
\left[\begin{array}{llll}
1 & 0 & 0 & 0  \tag{5.5}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 5
\end{array}\right]
$$

which has the same effect as

$$
\left[\begin{array}{cccc}
\frac{1}{S} & 0 & 0 & 0  \tag{5.5}\\
0 & \frac{1}{S} & 0 & 0 \\
0 & 0 & \frac{1}{S} & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

The matrix $T M$ is postmultiplied by the scaling transformation matrix shown in (5.4).

Rotation:- The rotation matrix is an orthogonal matrix. Thus the length of a line joining two points is invariant under this transformation, and in general the size of objects is unchanged by rotations. The routine ROTATE combines the effect of rotations through the angles RX, RY and RZ (degrees) about $x, y$ and $z$ axes in this order in one single transformation matrix (Table 5.3) i.e., $\left[\begin{array}{ll}X^{*} Y^{*} Z^{*} & 1\end{array}\right]=\left[\begin{array}{lll}X & Y & Z\end{array}\right]\left[\begin{array}{cccc}1 & 0 & 0 & 0 \\ 0 & \cos \theta & \sin \theta & 0 \\ 0 & -\sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1\end{array}\right] \times$ about x -axis

$$
\begin{align*}
{\left[\begin{array}{cccc}
\cos \phi & 0 & -\sin \phi & 0 \\
0 & 1 & 0 & 0 \\
\sin \phi & 0 & \cos \phi & 0 \\
0 & 0 & 0 & 1
\end{array}\right] \times\left[\begin{array}{cccc}
\cos \psi & \sin \psi & 0 & 0 \\
-\sin \psi & \cos \psi & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right] }  \tag{5.7}\\
\text { about y-axis } \\
\text { about } z \text {-axis }
\end{align*}
$$

The resulting transformation matrix simply reduces, with some trigonometric manipulation, to a matrix whose elements consist of sines and cosines of the sums and differences of the angles as given in Table (5.3). This would involve much less computation time than a concatenation of the individual transformations.

| Row Column | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $\frac{1}{2}[\cos (\phi+\psi)+\cos (\phi-\psi)]$ | $\frac{1}{2}\left[\sin ^{( }(\phi+\psi)-\sin (\phi-\psi)\right]$ | $-\sin (\phi)$ | 0 |
| 2 | $\begin{aligned} & \frac{1}{4}[\cos (\theta+\psi+\phi)-\cos (\theta+\psi-\phi)+ \\ & \cos (\theta-\psi+\phi)-\cos (\theta-\psi-\phi)]- \\ & \frac{1}{2}[\sin (\theta+\psi) \sin (\theta-\psi)] \end{aligned}$ | $\begin{aligned} & \frac{1}{4}[\sin (\theta+\psi+\phi)-\sin (\theta+\psi-\phi) \\ & -\sin (\theta-\psi+\phi)+\sin (\theta-\psi-\phi)] \\ & +\frac{1}{2}[\cos (\theta+\psi)+\cos (\theta-\psi)] \end{aligned}$ | $\frac{1}{2}[\sin (\theta+\phi)+\sin (\theta-\phi)]$ | 0 |
| 3 | $\begin{aligned} & \frac{1}{4}[\sin (\theta+\psi+\phi)-\sin (\theta+\psi-\phi) \\ & +\sin (\theta-\psi+\phi)-\sin (\theta-\psi-\phi)] \\ & +\frac{1}{2}[\cos (\theta+\psi)-\cos (\theta-\psi)] \end{aligned}$ | $\begin{aligned} & \frac{1}{4}[\cos (\theta+\psi+\phi)-\cos (\theta+\psi-\phi) \\ & -\cos (\theta-\psi+\phi+\cos (\theta-\psi-\phi)] \\ & +\frac{1}{2}[\sin (\theta+\psi)-\sin (\theta-\psi)] \end{aligned}$ | $\frac{1}{2}[\cos (\theta+\phi)+\cos (\theta-\phi)]$ | 0 |
| 4 | 0 | 0 | 0 | 1 |

TABLE 5.3: The Elements of the Combined Rotation Matrix ( $4 \times 4$ )

The fact that the three-dimensional rotations are noncommutative must be kept in mind. However, a different order of rotations may be performed by using separate calls of the routine.

Translation:- The transformation which translates a point $(X, Y, Z)$ to a new point ( $X^{*} Y^{*} Z^{*}$ ) is

$$
\left[\begin{array}{llll}
X * & Y * & Z * & 1
\end{array}\right]=\left[\begin{array}{llll}
X & Y & Z & 1
\end{array}\right]\left[\begin{array}{llll}
1 & 0 & 0 & 0  \tag{5.8}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 \\
T_{X} & T_{y} & T_{z} & 1
\end{array}\right]
$$

The routine TRANSL sets up the elements of the matrix and performs the postmultiplication of $T M$ by this matrix.

## 2. Clipping

In practice, graphical devices such as the Tektronix 4010 display work with a bounded space; in addition, the user may wish to confine his picture to a prescribed window. We must either ensure by means of scaling that our object lies within the bounded region or we must exclude all parts which lie outside the region. The latter technique is called 'scissoring' or clipping. This window may take any shape but it is usually rectangular.

The routine CLIP provides the clipping of a given line to the rectangular boundary (Figure 5.6) defined by its opposite corner coordinates as ( $\mathrm{XO}, \mathrm{YO}$ ) and ( $\mathrm{X} 1, \mathrm{Y} 1$ ). The coordinates of a given line's end points are first passed as input parameters to the routine, which then returns with the flag IREJ=0 or 1 indicating whether the line is fully rejected or accepted. If IREJ=1 then CLINE will contain the coordinates of clipped line end points. The clipping algorithm used in
implementing this routine has effectively two parts:-

1. It determines whether the line lies entirely within the window, and if not, whether it can be trivially rejected as lying entirely outside the window (Figure 5.6a). Two function subroutines (IREJCT and JACCPT) handle this test for total rejection or acceptance.

Let us suppose the line $A B$ joining $\left(a_{1}, a_{2}\right)$ and $\left(b_{1}, b_{2}\right)$ is to be clipped by the rectangle with opposite corners ( $\mathrm{XO}, \mathrm{YO}$ ) and ( $\mathrm{Xl}, \mathrm{YI}$ ). A line is rejected if it lies completely to the left, to the right, above, or below this rectangle. Thus if
or
or
or $\quad Y 1 \leq \min \left(a_{2}, b_{2}\right) \quad$
the line is rejected. If the line is not rejected by this test, we find whether it crosses a continued edge of the clipping rectangle.

If $X O>\min \left(\mathrm{a}_{1}, \mathrm{~b}_{1}\right)$ then the line crosses $X=X O$
If $X 1<\max \left(a_{1}, b_{1}\right)$ then the line crosses $X=X 1$
If $Y O>\min \left(a_{2}, b_{2}\right)$ then the line crosses $Y=Y O$
If $Y 1<\max \left(a_{2}, b_{2}\right)$ then the line crosses $Y=Y 1$
If none of the above is true, then the line lies totally within the clipping rectangle. Otherwise (i.e. the line crosses one of the continued edges) we conclude a new end point which needs to be investigated more closely.
2. The coordinates of intersection points with the boundary may be computed either by using the simple concept of finding directly the intersection point of two straight lines or alternatively by the iterative method of subdivision [1] of the
line and throwing away the segment which lies off-window. The subdivision methodwas used here as it was considered to be more efficient. The line is subdivided at its midpoint, yielding two line segments (Figure 5.6b). The test of part (1) is then applied to each segment of the line separately. The search for an end point stops either when both halves of the line are rejected or when the mid point coincides with one of the edges of the window. Clipping to a rectangular two-dimensional region introduces extra flexibility e.g. logically separate pictures occupying different areas of the screen can be prevented from interfering with one another. In addition, it also facilitates zooming down to a number of levels and provides selective viewing of part of a large picture.

## 3. Simple Perspective Projection

As displays are two-dimensional devices we can draw only twodimensional projections of three-dimensional objects. The idea of projection onto the plane $z=z_{0}$ can be expressed in the matrix form:

$$
\left[\begin{array}{ll}
X^{*} & Y^{*}  \tag{5.10}\\
Z^{*} & 1
\end{array}\right]=\left[\begin{array}{llll}
X & Y & Z_{0} & 1
\end{array}\right]=\left[\begin{array}{llll}
X & Y & Z & 1
\end{array}\right]\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 2 & 1
\end{array}\right]
$$

Note that the transformation matrix has a row of zero coefficients and is therefore singular. This is as one might expect, because if the matrix could be inverted it would mean that we could recover three-dimensional information from the two-dimensional drawing, and this is not usually possible.

The user is provided with a routine PROJCT which would set up a transformation matrix for a specified projection plane.

FIGURE 5.5: Menu Item Valid Zones


FIGURE 5.6a: Rejection Test


FIGURE 5. Gb: Bisection of the Line

We now consider the relevance of the off-diagonal elements of the fourth column of the transformation matrix

$$
\left[\begin{array}{llll}
x^{*} & y^{*} & z^{*} & t^{*}
\end{array}\right]-\left[\begin{array}{llll}
X & Y & Z & 1
\end{array}\right]\left[\begin{array}{llll}
1 & 0 & 0 & 0  \tag{5.11}\\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & P_{z} \\
0 & 0 & 0 & 1
\end{array}\right]=\left[\begin{array}{llll}
X & Y & Z & \left(1+P_{z} Z\right)
\end{array}\right]
$$

i.e.,

$$
\begin{equation*}
[X * Y * Z * 1]=\left[\frac{X}{1+P_{z} Z} \frac{Y}{1+P_{z} Z} \frac{Z}{1+P_{z} Z} 1\right] \tag{5.12}
\end{equation*}
$$

Under this transformation the origin $\left[\begin{array}{llll}0 & 0 & 0 & 1\end{array}\right]$ and the points at infinity on the $x$ and $y$ axes, namely $\left[\begin{array}{lll}1 & 0 & 0\end{array}\right]$ ] and $\left[\begin{array}{llll}0 & 1 & 0 & 0\end{array}\right]$ are unchanged. But the infinite point on the $z$-axis $\left[\begin{array}{llll}0 & 0 & 1 & 0\end{array}\right]$ is transformed into the finite point [ $\left.\begin{array}{lllll}0 & 0 & 1 & P_{z}\end{array}\right]$, i.e. after normalizing, the point $\left[001 / P_{z} 1\right]$. Thus, lines which were parallel to the $z$ direction before the transformation will now appear to pass through the point $\left[001 / P_{z} 1\right]$ which is sometimes called the 'vanishing point' of the perspective transformation.

The user is provided with a call to routine PERSP which applies a perspective transformation. When we project this transformed view onto a plane we obtain 'perspective projection'. For each vanishing point of a perspective transformation there is a corresponding centre of projection which lies on the same axis at the same distance from the origin, but in the opposite direction.

A transformation matrix of the form

$$
\left[\begin{array}{llll}
\mathrm{S}_{\mathrm{x}} & \mathrm{C}_{12} & \mathrm{C}_{13} & 0 \\
\mathrm{C}_{12} & \mathrm{~S}_{\mathrm{y}} & \mathrm{C}_{23} & 0 \\
\mathrm{C}_{31} & \mathrm{C}_{32} & \mathrm{~S}_{\mathrm{z}} & 0 \\
\mathrm{~T}_{\mathrm{x}} & \mathrm{~T}_{\mathrm{y}} & \mathrm{~T}_{\mathrm{z}} & 1
\end{array}\right]
$$

followed by a non-perspective projection onto a plane is known as an 'Axonometric projection'. It is in fact a perspective projection with vanishing points all at infinity. When the upper left-hand $3 \times 3$ matrix is orthogonal under this transformation the projection is said to be
'trimetric'. If two of the axes in an axonometric projection are equally foreshortened when projected, the transformation is said to be be 'dimetric'. In an 'isometric' projection all these axes are equally foreshortened, and usually at $120^{\circ}$ to each other [23]. If the upper left-hand $3 \times 3$ is not orthogonal an axonometric projection is said to be an 'oblique' projection.

## 4. Transformation Contro1

These routines merely provide some facilities for manipulating transformation matrices. In particular, SAVMAT and RESTOR permit the user to save/restore transformations on/from the pushdown stack (defined by the package) at any time to facilitate display of hierarchical data. For example, a picture containing repeated symbols will involve concatenation of transformations; whenever concatenation is performed, the current transformation must be saved so that it can be restored after displaying the symbol. A one-dimensional array in the form of a pushdown stack is employed to perform the above two operations. The remaining routines perform tasks such as concatenation and initialization of transformations.

## 7. THE GT42 IN EMULATOR MODE

LIGHT subroutines may also be used in conjunction with the GT42 refresh display in Emulator mode as a Tektronix 4010. The Tektronix 4010 Emulator program [24] accepts input from the DL11E communications interface and converts the characters into alpha or graphic data. This is displayed on the screen by adding the data in serial manner to a display file. The method by which incoming characters, including specialfunction characters e.g. clear-screen, send cursor position, etc., are converted is the same as that of the Tektronix 4010. The cross-hair cursor and the thumbwheel is simulated on the GT42 as a tracking-cross which may be moved around the screen with the light pen.

PART II

APPLICATIONS

## Chapter 6

## INTERPOLATORY DATA FITTING - IDF

1. INTRODUCTION
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## 1. INTRODUCTION

Data fitting in general has been used for many years in engineering applications. It occurs in machine tool control, in design problems and increasingly in computer graphical presentation of the numerical solution of physical problems, where numerical results would otherwise be difficult to interpret.

In particular, interpolatory data fitting is a special area of the more general curve fitting process. With many problems, as a result of measurements or calculations, we obtain a set of data points corresponding to a function, and it is usually desirable to pass a 'smooth' curve through these points.

It would be useful to distinguish between curve fitting and curve design. The former involves generation of a smooth curve for an already defined curve shape which is constrained to pass through specified data points. If the data points defining the curve shape contain some random errors, then they are fitted by a curve in some 'best' approximation sense, e.g. using least squares. On the other hand, the curve design problem is either to create ab initio a shape which satisfies some design constraint or to modify an existing mathematically defined shape.

Many methods already exist for interpolating data, ranging from global polynomial interpolation to various piecewise polynomial interpolation schemes, including cubic splines. For curve tracing, excellent results are achieved with these methods. However, they are usually ineffective for interactive curve design. This is due to the fact that control of the curve shape by numerical specification of both direction and magnitude of tangent vectors does not provide the feel required for curve design. In addition, the cubic curve fitting technique specifies a curve of unique order, which does not vary from spline to spline. In order to increase flexibility, more points must be input, creating more
splines. An alternative method of curve description has been described by Bezier [23]. This allows greater flexibility in the generation of desired shapes and gives a feel for the relationship between input and output.

As indicated by Forrest [25], the contrast between curve fitting and design is analogous to that between the draughtsman's (physical) splines and french curves.

Physically, a spline curve is obtained by bending a thin metal or wood lath round pins so that the curve passes through the given data points and assumes a shape of minimum internal energy. In this case the draughtsman need only specify the data points and the spline will do the rest of the work. Using a french curve, however, the designer must select from a set of rigid curve templates a particular curve which will pass through a series of points, and the complete curve will be constructed in a piecewise manner from several such selections.

The work reported in this chapter is concerned with the development and implementation of an interactive system using interpolatory curve fitting and in particular, cubic splines. Some applications require accurate and rapid graphical representation of known data where the technique of cubic spline fitting can be useful. For example, it can be particularly effective in an academic environment when used with low cost devices for graphical output (e.g. Tektronix 4010) to display numerical results which must satisfy known mathematical and physical boundary conditions.

Curves can be represented analytically in two basic forms, parametric and explicit. The use of explicit forms is largely confined to planar curves (i.e. two-dimensional) whereas the parametric form is easily extended to three-dimensional space curves.

$$
\left.\begin{array}{ll}
\text { Explicit form:- } & y=f(x) \\
\text { Parametric form:- } & x=f(t)  \tag{6.2}\\
& y=g(t) \\
z & =h(t)
\end{array}\right\}
$$

The parametric representation has several notable advantages over the non-parametric forms. Each set of coordinate values represents a unique point which can be computed by substitution of a single parametric value. It is possible to express a parametric curve in matrix form and to use identical algorithms for computing $x, y$ and $z$. Thus we can describe the curve in such a way that the form of the mathematical expressions for $x, y$ and $z$ does not change according to the orientation of the coordinate axes. In the explicit form $y=f(x)$ it may be convenient to describe a given curve with the axes in one orientation, though difficulties arise when $f(x)$ is not single valued. The slope of an explicit curve will be infinite or zero if the curve is parallel to one of the axes. The problem of infinite numbers does not usually arise with the parametric representation.

## 2. THE IDF NUMERICAL ALGORITHMS

### 2.1 Interpolation

From the classical theory it is known that a unique polynomial of degree $n$ can be passed through $n+1$ data points. Polynomials also have the advantage of being fairly easy to handle computationally. Also, such polynomials are continuously differentiable up to order $n$. This high degree of continuity might suggest a pleasing smooth behaviour, but often even the low-order derivatives are of such great magnitude that undesirable oscillations are displayed in the curve. One cause of the failure of polynomial interpolation to represent data properly is
the extreme dependency of the entire curve on each individual data point; a slight movement of a point even at one end can radically affect the curve shape. Visually one desires more local dependency. If a data point is altered slightly, the curve should adjust slightly in the neighbourhood of the point and be nearly unaffected away from the point. In an effort to decrease the curve's sensitivity to each data point, the set of functions known as polynomial splines was introduced by I.J. Schoenberg in 1946. Mathematically, a spline is a piecewise polynomial of degree $n$ with continuity of order $n-1$ at the common joints between adjacent segments.

The following sections contain the mathematical background of the numerical algorithms used in the implementation of the IDF system. These algorithms mainly employ cubic splines; however, two other algorithms are also included for comparison. One uses the Newton form of global polynomial [26] and the other uses a piecewise quintic polynomial [27]. The program listings of these algorithms is given in Appendix 2.1.

### 2.2 Global Polynomial (Newton Form)

A general method (classical) for constructing a global polynomial $P_{n}(x)$ which fits a given function or data exactly at a number of arbitrary spaced points ( $x_{i}, i=0(1) n$ ) is the Lagrange form
or

$$
\begin{equation*}
P_{n}(x)=\sum_{k=0}^{n}\left[f\left(x_{k}\right) \prod_{\substack{j=0 \\ j \neq k}}^{n} \frac{\left(x-x_{j}\right)}{\left(x_{k}-x_{j}\right)}\right] \tag{6.3}
\end{equation*}
$$

$$
\begin{equation*}
P_{n}(x)=\sum_{k=0}^{n} f\left(x_{k}\right) L_{k}(x) \tag{6.4}
\end{equation*}
$$

Note the Lagrangian coefficients $L_{k}(x)$ are independent of the function values and depend only on the set of points $x_{i}$. A curve passing through these points using this polynomial is smooth in
the sense of being maximally often differentiable. As the number of points increases, these polynomials can oscillate strongly with a direct dependence on the arrangement of the points.

The Lagrange representation has the defect that if other data points were added, then the new higher degree interpolating polynomial could not be obtained by easily modifying the previous one. Lagrange interpolation is also inefficient when several interpolations are required for the same data. A representation which does not have these disadvantages is the Newton form of interpolating polynomial

$$
\begin{equation*}
P_{n}(x)=a_{0}+\left(x-x_{0}\right) a_{1}+\left(x-x_{0}\right)\left(x-x_{1}\right) a_{2}+\ldots+\left(x-x_{0}\right) \ldots\left(x-x_{n-1}\right) a_{n} \tag{6.5}
\end{equation*}
$$

$a_{k}$ is called the $k^{\text {th }}$ ordered divided difference and is usually expressed in the form

$$
\begin{align*}
& a_{0}=f\left[x_{0}\right]  \tag{6.6}\\
& a_{k}=f\left[x_{0}, x_{1}, \ldots x_{k}\right] \quad k=1(1) n \tag{6.7}
\end{align*}
$$

By comparison with the corresponding Lagrangian polynomial in (6.3)

$$
\begin{equation*}
a_{n}=f\left[x_{0}, x_{1}, \ldots x_{n}\right]=\sum_{k=0}^{n}\left[\frac{f\left(x_{k}\right)}{\prod_{\substack{j=0 \\ j \neq k}}\left(x_{k}-x_{j}\right)}\right] \tag{6.8}
\end{equation*}
$$

In the divided difference form

$$
\begin{equation*}
f\left[x_{0}, x_{1}, \ldots, x_{n}, x_{\alpha}, x_{\beta}\right]=\frac{f\left[x_{0}, x_{1}, \ldots, x_{n}, x_{\alpha}\right]-f\left[x_{0}, x_{1}, \ldots, x_{n}, x_{\beta}\right]}{x_{\alpha}-x_{\beta}} \tag{6.9}
\end{equation*}
$$

This leads to a systematic way of calculating the coefficients $a_{k}$ from the divided difference table:

$$
\begin{aligned}
& x_{0} \quad f_{0} \quad \frac{f_{1}-f_{0}}{x_{1}-x_{0}}=f_{01} \\
& \mathrm{x}_{1} . \mathrm{f}_{1} \quad \mathrm{f}_{012} \\
& \frac{f_{2}-f_{1}}{x_{2}-x_{1}}=f_{12} \quad f_{0123} \\
& \begin{array}{lll}
\mathrm{x}_{2} \mathrm{f}_{2} & \mathrm{f}_{123}-f_{2} \\
& \frac{f_{3}-x_{2}}{x_{3}}=f_{23} & \\
& & f_{1234}
\end{array} \\
& x_{3} \quad f_{3} \quad f_{234} \\
& \frac{f_{4}-f_{3}}{x_{4}-x_{3}}=f_{34} \\
& \mathrm{x}_{4} \quad \mathrm{x}_{4}
\end{aligned}
$$

This algorithm is suitable when interpolated values are required at a large number of points since only one evaluation of the table is performed. A single subroutine (NEWTON) was written to implement this algorithm. It involves firstly the computation of the coefficients for a given set of points, followed by a nested multiplication for each interpolation.

The main objection to polynomial interpolation at a large number of points is that the calculation and evaluation of interpolating polynomials become costly and unreliable.

The error of the interpolating polynomial $P_{n}(x)$ is

$$
\begin{equation*}
R_{n}(x)=f(x)-P_{n}(x) \tag{6.10}
\end{equation*}
$$

where $f(x)$ is the function (given or implied) which corresponds to the data.

It can be shown that

$$
\begin{equation*}
R_{n}(x)=\frac{1}{(n+1)!} f^{(n+1)}(\zeta) \prod_{i=0}^{n}\left(x-x_{i}\right) \tag{6.11}
\end{equation*}
$$

where $\zeta$ is some point in the interval 'I' bounded by the largest and
the smallest of the numbers $x_{i}$ and $x$. If we wish to give an estimate of the error in approximating $f(x)$ by $P_{n}(x)$ we must know the magnitude of $f^{(n+1)}(\zeta)$ or its upper bound on the interval 'I'. A small interpolation error over 'I' can usually be expected only if $\max _{x \in I}\left|f^{(n+1)}(x)\right|$ and $\max _{x \in I} \mid \prod_{j=0}^{n}\left(x-x_{j}\right) \quad$ are small.

It follows that the only way to guarantee a small error is to make the interval 'I' small. Since the interval over which $f(x)$ is to be approximated is usually given in advance, this can be accomplished only by partitioning this interval into sufficiently small subintervals and approximating $f(x)$ in each subinterval by a suitable low-order polynomial. This leads to 'piecewise polynomial interpolation'. The entire curve is produced by joining the curve segments together for given continuity conditions.

### 2.3 Piecewise Quintic Polynomial Interpolation

A method proposed by Maude [27] is developed here for interpolation from a given set of data points in the plane and for fitting a smooth curve to these points. It is based on a piecewise function composed of a set of polynomials applicable to successive intervals of the given points.

Basically, over any interval two local interpolating polynomials are found, and a weighted average is taken, the weight being a function of the independent variables, with suitable smoothing properties.

In the case of a one-dimensional curve, two second order polynomials could be used in the range $x_{n}$ to $x_{n+1}$ as shown in Figure 6.1

$$
F_{n} \quad-\quad \text { fitting exactly } f_{n-1}, f_{n}, f_{n+1}
$$

and

$$
F_{n+1}-\text { fitting exactly } f_{n}, f_{n+1}, f_{n+2}
$$

The function $F_{n}$ and $F_{n+1}$ are combined by weight function $W$ to obtain the new interpolating function $F$ over the interval $\left[x_{n}, x_{n+1}\right]$

$$
\begin{equation*}
F=W F_{n}+(1-W) F_{n+1} \tag{6.12}
\end{equation*}
$$

where $W$ is a function of $x$ such that

$$
\left.\begin{array}{l}
W\left(x_{n}\right)=1  \tag{6.13}\\
W\left(x_{n+1}\right)=0 \\
\left(\frac{d W}{d x}\right)_{n}=\left(\frac{d W}{d x}\right)_{n+1}=0
\end{array}\right\}
$$

which ensures first and second derivative continuity in $F$. The weight function used to yield the desired smoothness is
where

$$
\begin{align*}
& W=1-3 x^{2}+2 x^{3}  \tag{6.14}\\
& X=\frac{x-x_{n}}{x_{n+1}-x_{n}}=\frac{\Delta x}{\Delta x_{n}}
\end{align*}
$$

The coefficients of the quintic polynomials generated by this algorithm for each interval are found as follows:

First consider the two quadratic polynomials $F_{n}$ and $F_{n+1}$ passing through the points $a, b, c$ and $b, c, d$ respectively as shown in Figure 6.1. Then we have,

$$
\begin{align*}
& F_{n}=a_{1}+b_{1} X+c_{1} X^{2}  \tag{6.15}\\
& F_{n+1}=a_{2}+b_{2} X+c_{2} X^{2} \tag{6.16}
\end{align*}
$$

Therefore, the polynomial $F$ is constructed by taking the weighted average of $(6.15)$ and $(6.16)$ as given in (6.12). This gives

$$
\begin{aligned}
& F=a_{1}+b_{1} X+\left(c_{1}-3\left(a_{1}-a_{2}\right)\right) x^{2}+\left(2\left(a_{1}-a_{2}\right)+3\left(b_{2}-b_{1}\right)\right) x^{3} \\
&+\left(2\left(b_{1}-b_{2}\right)+3\left(c_{2}-c_{1}\right)\right) x^{4}+2\left(c_{1}-c_{2}\right) x^{5}
\end{aligned}
$$

. . the quintic polynomial is

$$
\begin{equation*}
F=A+B X+C X^{2}+D X^{3}+E X^{4}+F X^{5} \tag{6.17}
\end{equation*}
$$

where

$$
\left.\begin{array}{ll}
A=a_{1} & D=2\left(a_{1}-a_{2}\right)+3\left(b_{2}-b_{1}\right)  \tag{6.18}\\
B=b_{1} & E=2\left(b_{1}-b_{2}\right)+3\left(c_{2}-c_{1}\right) \\
C=c_{1}-3\left(a_{1}-a_{2}\right) & F=2\left(c_{1}-c_{2}\right)
\end{array}\right\}
$$

The coefficients in (6.18) are determined from the function values given at the abscissae $x_{n-1}, x_{n}, x_{n+1}$ and $x_{n+2}$.

Now by substituting the given function values in (6.15), we obtain

$$
\left.\begin{array}{rl}
f_{n-1} & =a_{1}-b_{1}\left(\frac{\Delta x_{n-1}}{\Delta x_{n}}\right)+c_{1}\left(\frac{\Delta x_{n-1}}{\Delta x_{n}}\right)^{2}  \tag{6.19}\\
f_{n} & =a_{1} \\
f_{n+1} & =a_{1}+b_{1}+c_{1}
\end{array}\right\}
$$

Similarly, substituting in (6.16), we have

$$
\left.\begin{array}{l}
f_{n}=a_{2}  \tag{6.20}\\
f_{n+1}=a_{2}+b_{2}+c_{2} \\
f_{n+2}=a_{2}+b_{2}\left(1+\frac{\Delta x_{n-1}}{\Delta x_{n}}\right)+c_{2}\left(1+\frac{\Delta x_{n-1}}{\Delta x_{n}}\right)^{2}
\end{array}\right\}
$$

By solving equations (6.19) and (6.20) for $a_{1}, a_{2}, b_{1}, b_{2}, c_{1}$ and $c_{2}$ and substituting in equations (6.18), we obtain
$\left.\begin{array}{rl}A=f_{n} & D=-3 T_{0} \\ B=\frac{D 1+R^{2} D 2}{R(1+R)} & E=5 T_{0} \\ C=\frac{R D 2-D 1}{R(1+R)} & F=-2 T_{0}\end{array}\right\}$
where

$$
\left.\begin{array}{rl}
D 1 & =f_{n}-f_{n-1} \\
D 2 & =f_{n+1}-f_{n} \\
D 3 & =f_{n+2}-f_{n+1}  \tag{6.22}\\
T_{0} & =\frac{S(1+S) D 1+R(1+R) D 3-R S(2+R+S) D 2}{R S(1+R)(1+S)} \\
R & =\frac{\Delta x_{n-1}}{\Delta x_{n}} \text { and } \quad S=\frac{\Delta x_{n+1}}{\Delta x_{n}}
\end{array}\right\}
$$

( $R=S=1$ for equidistant data points along the $x$-axis)

The coefficients of the quintic polynomial in (6.21) determine uniquely the portion of the curve in the interval $\left[x_{n}, x_{n+1}\right]$. However, in order to determine the two end portions of the curve, an extra point is assumed to exist beyond each end of the curve as shown in Figure 6.2. Effectively, the introduction of these imaginary end points would determine the nature of the end conditions for the whole curve. Consequently; the ' $D$ ' values resulting from the new portion must be specified. The algorithm was adapted so that these values are made controllable by the user. Thus three forms of end condition were considered in order to give the user the choice to vary the boundary condition at each end as required. These end conditions are made analogous to those suggested by Spath [28] for cubic splines. These are as shown below:

|  | End condition | First end | Last end |
| :---: | :---: | :---: | :---: |
| (i) | CLAMPED <br> ( $\frac{d y}{d x}$ is specified) | user must specify <br> the slope (as D1) | user must specify <br> the slope (as D3) |
| (ii) | $\begin{aligned} & \text { RELAXED } \\ & \left(\frac{\mathrm{d}^{2} y}{d x^{2}}=0\right) \end{aligned}$ | set $\mathrm{D} 1=\mathrm{D} 2$ | set D3=D2 |
| (iii) | PARABOLIC $\left(\frac{\mathrm{d}^{2} y}{d x^{2}}=\text { constant }\right)$ | $\begin{aligned} & T_{0}=0 \\ & \text { i.e. set } D 1=2 D 2-D 3 \\ & \text { since } R=S=1 \text { is } \\ & \text { assumed } \end{aligned}$ | $\begin{aligned} & T_{0}=0 \\ & \text { i.e. } D 3=2 D 2-D 1 \\ & R=S=1 \text { is } \\ & \text { assumed } \end{aligned}$ |

A subroutine (PIECWS) was written to implement the above algorithm which fits a smooth curve to a given set of input data points in the $x-y$ plane.

Another method was proposed by AKIMA [29]: this is based on a piecewise function composed of a set of polynomials, each of degree


FIGURE 6.1: Four Points Fitted with Two Quadratic Polynomials $\mathrm{F}_{\mathrm{n}}$ and $\mathrm{F}_{\mathrm{n}+1}$


FIGURE 6.2: Addition of Extra Two Points at the Ends of the Curve
three with slope at the junction points locally determined under a geometrical condition. The slope is determined by the coordinates of five points, with the point in question as a centre point, and two points on each side of it; the resulting interpolation is independent of the axes used.

In both methods each individual polynomial is determined locally and additional conditions are needed to fix the two ends. However, the Maude method does not evaluate the slope of the curve at each point and only uses four points locally to determine each portion of the curve.

### 2.4 Cubic Spline Polynomial Interpolation

A cubic spline is a piecewise cubic polynomial, having the property of continuity of slope and curvature throughout its length. The use of cubic splines means that $n-1$ cubic polynomials are required for the data points $\left(x_{k}, f\left(x_{k}\right)\right), k=1(1) n$. Since a cubic is the lowest degree polynomial which can twist in space and have inflection points, cubic splines are commonly used for curve fitting. The use of low-degree polynomials reduces the computational requirements and reduces numerical instabilities that arise with higher order curves. Also, their use corresponds to minimization of the quantity

$$
\begin{equation*}
J=\int\left(f^{\prime \prime}(x)\right)^{2} d x \tag{6.23}
\end{equation*}
$$

subject to certain boundary conditions. Minimization of J approximates minimization of the integral of squared curvature $K$ along the curve, which has the important physical justification that a thin flexible strip passed through the data points takes a configuration which minimises $K$.

Consider the cubic spline

$$
\begin{align*}
& y_{k}=f_{k}(x)=A_{k}\left(x-x_{k}\right)^{3}+B_{k}\left(x-x_{k}\right)^{2}+C_{k}\left(x-x_{k}\right)+D_{k}  \tag{6.24}\\
& y_{k}=f_{k}(x)=A_{k} \Delta x_{k}^{3}+B_{k} \Delta x_{k}^{2}+C_{k} \Delta x_{k}+D_{k} \tag{6.25}
\end{align*}
$$

This is the explicit form (non-parametric) of cubic spline function, since $y$ is explicitly dependent on $x$. Therefore, a two-dimensional (planar) curve can be expressed as in (6.25), provided that the curve progresses from left to right. However, if $\frac{d y}{d x}$ is infinite at any point, this simple form would break down and must be replaced by the parametric form:

$$
\begin{align*}
& x_{k}(t)=A_{k} \Delta t^{3}+B_{k} t^{2}+C_{k} \Delta t+D_{k}  \tag{6.26}\\
& y_{k}(t)=E_{k} \Delta t^{3}+F_{k} \Delta t^{2}+G_{k} \Delta t+H_{k} \tag{6.27}
\end{align*}
$$

The parameter $t$ can be chosen at will as long as it increases steadily as we progress along the curve; but it is usually advantageous to make it approximately proportional to the arc length from the first point to the point in question. The other advantage of the parametric spline formulation is that it extends easily to three-dimensional problems. In such cases the $z$-coordinate is parametrically:

$$
\begin{equation*}
z(t)=P_{k} \Delta t^{3}+Q_{k} \Delta t^{2}+R_{k} \Delta t+S_{k} \tag{6.28}
\end{equation*}
$$

The problem is to determine the coefficients of the above equations for each interval, subject to first and second derivative continuity conditions. Now consider an interval $\left[x_{k}, x_{k+1}\right]$. Six possible boundary conditions can be set (Figure 6.3) involving function values, slopes and second derivatives at both ends of the interval. Using the explicit form (6.25) these are given by:

$$
\begin{align*}
& y_{k}=f_{k}\left(x_{k}\right)=D_{k} \\
& y_{k+1}=f_{k}\left(x_{k+1}\right)=A_{k} \Delta x_{k}^{3}+B_{k} \Delta x_{k}^{2}+C_{k} \Delta x_{k}+D_{k} \\
& y_{k}^{\prime}=f_{k}^{\prime}\left(x_{k}\right)=C_{k}  \tag{6.29}\\
& y_{k+1}^{\prime}=f_{k}^{\prime}\left(x_{k+1}\right)=3 A_{k} \Delta x_{k}^{2}+2 B_{k} \Delta x_{k}+C_{k} \\
& y_{k}^{\prime \prime}=f_{k}^{\prime \prime}\left(x_{k}\right)=2 B_{k} \\
& y_{k+1}^{\prime \prime}=f_{k}^{\prime \prime}\left(x_{k+1}\right)=6 A_{k} \Delta x_{k}+2 B_{k}
\end{align*}
$$

From these boundary equations, the desired coefficients could be expressed in terms of the function values and two derivatives. In
the first derivative form, the coefficients are:

$$
\begin{align*}
& A_{k}=\frac{1}{\Delta x_{k}^{2}}\left(-2 \frac{\Delta y_{k}}{\Delta x_{k}}+y_{k}^{\prime}+y_{k+1}^{\prime}\right) \\
& B_{k}=\frac{1}{\Delta x_{k}}\left(3 \frac{\Delta y_{k}}{\Delta x_{k}}-2 y_{k}^{\prime}-y_{k+1}^{\prime}\right) \\
& C_{k}=y_{k}^{\prime}  \tag{6.30}\\
& D_{k}=y_{k}
\end{align*}
$$

Similarly in the second derivative form the coefficients are:

$$
\begin{align*}
& A_{k}=\frac{1}{6 \Delta x_{k}}\left(y_{k+1}^{\prime \prime}-y_{k}^{\prime \prime}\right) \\
& B_{k}=\frac{1}{2} y_{k}^{\prime \prime} \\
& C_{k}=\frac{\Delta y_{k}}{\Delta x_{k}}-\frac{1}{6} \Delta x_{k}\left(y_{k+1}^{\prime \prime}+2 y_{k}^{\prime \prime}\right)  \tag{6.31}\\
& D_{k}=y_{k}
\end{align*}
$$

Therefore, in order to evaluate the coefficients, we need to determine either the first or the second derivatives by using the continuity conditions at the interior node points.

Considering continuity in the first derivative, and using equations (6.29), we have
at $x=x_{k}$

$$
\begin{equation*}
y_{k-1}^{\prime}\left(x_{k}\right)=y_{k}^{\prime}\left(x_{k}\right) \quad(\text { for } k=2(1) n-1) \tag{6.32}
\end{equation*}
$$

which gives the coupling conditions

$$
\begin{equation*}
3 A_{k-1} \Delta x_{k}^{2}+2 B_{k-1} \Delta x_{k}+C_{k-1}=C_{k} \tag{6.33}
\end{equation*}
$$

By replacing the coefficients in equation (6.33) from equation (6.31), it yields the system of linear equations:

$$
\begin{equation*}
\Delta x_{k-1} y_{k-1}^{\prime \prime}+2\left(\Delta x_{k-1}+\Delta x_{k}\right) y_{k}^{\prime \prime}+\Delta x_{k} y_{k+1}^{\prime \prime}=6\left(\frac{\Delta y_{k}}{\Delta x_{k}}-\frac{\Delta y_{k-1}}{\Delta x_{k-1}}\right) \tag{6.34}
\end{equation*}
$$

for $k=2(1) n-1$, or in vector form:

$$
\begin{align*}
& {\left[\Delta x_{k-1} 2\left(\Delta x_{k-1}+\Delta x_{k}\right) \Delta x_{k}\right]\left[\begin{array}{l}
y_{k}^{\prime \prime} \\
y_{k}^{\prime \prime} \\
y_{k+1}^{\prime \prime}
\end{array}\right]=6\left[\frac{\Delta y_{k}}{\Delta x_{k}}-\frac{\Delta y_{k-1}}{\Delta x_{k-1}}\right] }  \tag{6.35}\\
= & 2(1) n-1 .
\end{align*}
$$

This represents $n-2$ simultaneous linear equations for the $n$ unknown $y_{k}^{\prime \prime}$. The two extra unknowns $y_{1}^{\prime \prime}$ and $y_{n}^{\prime \prime}$ naturally arise from the absence of a continuity condition at the end points $x_{1}$ and $x_{n}$. Hence, the system of equations can be solved if the two boundary conditions are given and thus a unique cubic spline curve is determined. Similarly, applying second derivative continuity, we obtain $n-2$ simultaneous linear equations for $n$ unknowns in $y_{k}^{\prime}$ as

$$
\left[\begin{array}{lll}
\Delta x_{1} & 2\left(\Delta x_{k-1}+\Delta x_{k}\right) \Delta x_{k-1}
\end{array}\right]\left[\begin{array}{l}
\bar{y}_{k}^{\prime}-1  \tag{6.36}\\
y_{k}^{\prime} \\
y_{k+1}^{\prime}
\end{array}\right]=3\left[\begin{array}{l}
\Delta x_{k} \\
\Delta x_{k-1}
\end{array} y_{k-1}+\frac{\Delta x_{k-1}}{\Delta x_{k}} \Delta y_{k}\right]
$$

for $k=2(1) n-1$.
Again, two extra conditions are required to obtain a unique cubic spline curve.

The boundary conditions required by equations (6.35) and (6.36) could take different forms depending on the nature of the problem. Hence, the IDF system contains a set of program subroutines for generating cubic splines, allowing the user various options for specifying interactively the form of the end condition. The forms of end condition available at present are:
(1) Prescribed first or second derivatives
(2) Cyclic or anticyclic behaviour [30]
(3) Variable end conditions

Next let us consider the effect of the various forms of end condition on the system of linear equations $(6,35)$ and $(6,36)$. Since these equations are equivalent formulations of the same problem either form can be used.
(1) Prescribed First or Second Derivatives
(i) First derivative end condition.

In this case the values $y_{1}^{\prime}$ and $y_{n}^{\prime}$ at $x_{1}$ and $x_{n}$ are available. These provide the two additional equations needed in (6.35) to solve for $y_{1}^{\prime \prime} \ldots . . y_{n}^{\prime \prime}$. By using equations (6.29) and (6.31) we arrive at the following two boundary equations:

$$
\left.\begin{array}{l}
2 \Delta x_{1} y_{1}^{\prime \prime}+\Delta x_{1} y_{2}^{\prime \prime}=6\left(\frac{\Delta y_{1}}{\Delta x_{1}}-y_{1}^{\prime}\right)  \tag{6.37}\\
\Delta x_{n-1} y_{n-1}^{\prime \prime}+2 \Delta x_{n-1} y_{n}^{\prime \prime}=6\left(y_{n}^{\prime}-\frac{\Delta y_{n-1}}{\Delta x_{n-1}}\right)
\end{array}\right\}
$$

The set of equations (6.35) together with (6.37) yields a system of linear equations whose $n \times n$ coefficient matrix is tridiagonal, symmetric, and diagonally dominant with positive diagonal elements. The coefficient matrix shown in (6.38) is clearly non-singular, thus guaranteeing the existence and uniqueness of the cubic spline for a given data set.


The boundary values could be estimated approximately from the given data points defining the curve as

$$
y_{1}^{\prime}=\frac{\Delta y_{1}}{\Delta x_{1}} \quad \text { and } \quad y_{n}^{\prime}=\frac{\Delta y_{n-1}}{\Delta x_{n-1}}
$$

The values of the slopes at both end are declared by the user. This form of boundary condition is sometimes termed by Engineers as clamped or encastred.
(ii) Second derivative end condition

Two possible ways of specifying the second derivative boundary values are open to the user.
(a) $y_{1}^{\prime \prime}$ and $y_{n}^{\prime \prime}$ are directly declared by the user: Equations (6.35) are slightly rearranged as shown in (6.39) which has a (n-2) $\times(\mathrm{n}-2)$ tridiagonal coefficient matrix and can be uniquely solved for $y_{2}^{\prime \prime} \cdots \cdots \cdot y_{n-1}^{\prime \prime}$.

where

$$
\begin{aligned}
& B_{1}=6\left(\frac{\Delta y_{2}}{\Delta x_{2}}-\frac{\Delta y_{1}}{\Delta x_{1}}\right)-\Delta x_{1} y_{1}^{\prime \prime}, \\
& B_{n}=6\left(\frac{\Delta y_{n-1}}{\Delta x_{n-1}}-\frac{\Delta y_{n-2}}{\Delta x_{n-2}}\right)-\Delta x_{n-1} y_{n}^{\prime \prime}
\end{aligned}
$$

and

$$
B_{k}=6\left(\frac{\Delta y_{k+1}}{\Delta x_{k+1}}-\frac{\Delta y_{k}}{\Delta x_{k}}\right) \quad \text { for } k=2(1) n-1 .
$$

For the special case where $y_{1}^{\prime \prime}=y_{n}^{\prime \prime}=0$, the cubic spline is said to have natural or relaxed boundary conditions. This natural spline ending should be used if for example the data is sinusoidal.
(b) Sometimes boundary conditions of the form:

$$
\begin{equation*}
y_{1}^{\prime \prime}=u y_{2}^{\prime \prime} \quad \text { and } \quad v y_{n-1}^{\prime \prime}=y_{n}^{\prime \prime} \tag{6.40}
\end{equation*}
$$

are useful. In this case, though $u$ and $v$ are arbitrary scalars, they are in practice often taken equal to unity, thereby making the second derivatives at $x_{1}$ and $x_{n}$ equal to those at $x_{2}$ and $x_{n-1}$ respectively. This is often termed P -spline [30] in which the end segments are parabolic. Another common choice is to take $u=v=1 / 2$.

By substituting for $y_{1}^{\prime \prime}$ and $y_{2}^{\prime \prime}$ from (6.40) into equation (6.35), we obtain the slightly modified boundary equations:

$$
\left.\begin{array}{l}
\left((2+u) \Delta x_{1}+2 \Delta x_{2}\right) y_{2}^{\prime \prime}+\Delta x_{2} y_{3}^{\prime \prime}=6\left(\frac{\Delta y_{2}}{\Delta x_{2}}-\frac{\Delta y_{1}}{\Delta x_{1}}\right)  \tag{6.41}\\
\Delta x_{n-2} y_{n-2}^{\prime \prime}+\left(2 \Delta x_{n-2}+(2+v) \Delta x_{n-1}\right) y_{n-1}^{\prime}=6\left(\frac{\Delta y_{n-1}}{\Delta x_{n-1}}-\frac{\Delta y_{n-2}}{\Delta x_{n-2}}\right)
\end{array}\right\}
$$

This means that the coefficient matrix in (6.39) is only modified in two places viz. the element at the top left and the element at the bottom right. The existence and uniqueness of cubic splines with this boundary condition is ensured as long as $u$ and $v$ are chosen so that the matrix remains positive definite. This is guaranteed if

$$
\left.\begin{array}{l}
-\left(2 \frac{\Delta x_{2}}{\Delta x_{1}}+2\right) \leqslant u<\infty  \tag{6.42}\\
-\left(\frac{\Delta x_{n-2}}{\Delta x_{n-1}}+2\right) \leqslant v<\infty
\end{array}\right\}
$$

The effect of these different boundary conditions on the shape of the curve would be mainly noticeable at the end intervals.

In all the above cases, the Gaussian elimination process [28] was employed to solve the linear system of equations. The elements of the matrix and of the R.H.S. are only calculated at the place where they are required so as to save storage.

## (2) Cyclic or Anticyclic Behaviour

Cubic splines with periodic boundary conditions are particularly suitable for the representation of closed smooth curves or a portion of a curve which repeats at intervals.
(i) Cyclic end condition in which the first and second derivatives at one end of the curve have the same values as those at the other end. Mathematically, these conditions are expressed as follows:

$$
\begin{equation*}
y_{1}^{(i)}\left(x_{1}\right)=y_{n}^{(i)}\left(x_{n}\right) \quad \text { for } i=0,1,2 \tag{6.43}
\end{equation*}
$$

Hence from equations (6.37) we obtain

$$
\begin{equation*}
2\left(\Delta x_{1}+\Delta x_{n-1}\right) y_{1}^{\prime \prime}+\Delta x_{1} y_{2}^{\prime \prime}+\Delta x_{n-1} y_{n-1}^{\prime \prime}=6\left(\frac{\Delta y_{1}}{\Delta x_{1}}-\frac{\Delta y_{n-1}}{\Delta x_{n-1}}\right) \tag{6.44}
\end{equation*}
$$

and for $\mathrm{k}=\mathrm{n}-1$ in equation (6.35),

$$
\begin{equation*}
\Delta x_{n-2} y_{n-2}^{\prime \prime}+2\left(\Delta x_{n-2}+\Delta x_{n-1}\right) y_{n-1}^{\prime \prime}+\Delta x_{n-1} y_{1}^{\prime \prime}=6\left(\frac{\Delta y_{n-1}}{\Delta x_{n-1}}-\frac{\Delta y_{n-2}}{\Delta x_{n-2}}\right) \tag{6.45}
\end{equation*}
$$

In matrix form, the system becomes

where

$$
\mathrm{B}_{1}=6\left(\frac{\Delta y_{1}}{\Delta \mathrm{x}_{1}}-\frac{\Delta y_{\mathrm{n}-1}}{\Delta \mathrm{x}_{\mathrm{n}-1}}\right)
$$

and $\quad B_{k}=6\left(\frac{\Delta y_{k}}{\Delta x_{k}}-\frac{\Delta y_{k-1}}{\Delta x_{k-1}}\right) \quad$ for $k=2(1) n-1$
The ( $\mathrm{n}-1$ ) $\times(\mathrm{n}-1)$ coefficient matrix of (6.46) is not strictly tridiagonal and has off-diagonal entries in the corners of the first and last rows. This is a cyclic tridiagonal matrix and is positive definite. (The associated spline is useful for curves in which the first and last points are coincident). This system of equations (6.46) is solved by using the Normalised Periodic Tridiagonal Algorithm developed by Benson [31] from the matrix factorization method.

The cyclic end condition can be used without the knowledge of the initial slope and the initial data point can be at any location on the closed curve.
(ii) Anticyclic end condition is similar to the cyclic condition except that antisymmetry in both slope and curvature is imposed. The antisymmetry condition is expressed as
and

$$
\left.\begin{array}{l}
y_{1}^{\prime}\left(x_{1}\right)=-y_{n}^{\prime}\left(x_{n}\right)  \tag{6.47}\\
y_{1}^{\prime \prime}\left(x_{1}\right)=-y_{n}^{\prime \prime}\left(x_{n}\right)
\end{array}\right\}
$$

In this case, equations (6.36) which involve unknown $y_{k}^{\prime}$ will be used as a basis for the system of equations.

From equations (6.29), we have
and

$$
\left.\begin{array}{l}
y_{l}^{\prime \prime}\left(x_{1}\right)=2 B_{1}  \tag{6.48}\\
y_{n}^{\prime \prime}\left(x_{n}\right)=6 A_{n-1} \Delta x_{n-1}+2 B_{n-1}
\end{array}\right\}
$$

Using the second condition in (6.47), we can write from (6.48)

$$
\begin{equation*}
B_{1}=3 A_{n-1} \Delta x_{n-1}+B_{n-1} \tag{6.49}
\end{equation*}
$$

Substituting from (6.30) into (6.49), we obtain for $k=1$

$$
\begin{equation*}
2\left(\Delta x_{1}+\Delta x_{n-1}\right) y_{1}^{\prime}+\Delta x_{n-1} y_{2}^{\prime}-\Delta x_{1} y_{n-1}^{\prime}=3\left(\frac{\Delta x_{n-1}}{\Delta x_{1}} \Delta y_{1}-\frac{\Delta x_{1}}{\Delta x_{n-1}} \Delta y_{n-1}\right) \tag{6.50}
\end{equation*}
$$

and for $\mathrm{k}=\mathrm{n}-1$, using (6.36) we have

$$
\begin{equation*}
\Delta x_{n-1} y_{n-2}^{\prime}+2\left(\Delta x_{n-2}+\Delta x_{n-1}\right) y_{n-1}^{\prime}-\Delta x_{n-2} y_{1}^{\prime}=3\left(\frac{\Delta x_{n-1}}{\Delta x_{n-2}} \Delta y_{n-2}+\frac{\Delta x_{n-2}}{\Delta x_{n-1}} \Delta y_{n-1}\right) \tag{6.51}
\end{equation*}
$$

In matrix form, the anticyclic cubic spline $(\mathrm{n}-1) \times(\mathrm{n}-1)$
coefficient matrix is represented as

(3) Variable end conditions

The above cubic spline algorithms allow the user to select the same (or related) forms of boundary condition at both ends. The variable end condition provides maximum control of the spline. This enables the user to specify different forms of boundary condition at
each end of the curve. This set was suggested in the first place by Nutbourne [30]. In this paper the algorithm is based upon recurrence formulae which are derived by relating the properties of the $j+1$ interval to the $j$ interval. The algorithm discussed here is again based on a matrix approach which is valid for both the explicit and the parametric forms.

Consider equation (6.36). When it is applied recursively at all interior points $(k=2(1) n-1)$ the resultant coefficient matrix has dimension ( $n-2$ ) $\times n$ as shown in (6.53).

where

$$
B_{k}=3\left(\frac{\Delta x_{k}}{\Delta x_{k-1}} \Delta y_{k-1}+\frac{\Delta x_{k-1}}{\Delta x_{k}} \Delta y_{k}\right) \quad k=2(1) n-1
$$

The strategy of this algorithm is to construct the two boundary equations required to augment equations (6.53). Each boundary equation is formed independently using a particular end condition. Hence, the algorithm gives the user the ability to have full control over the form of the end condition required. As will be seen later (next section), this capability is provided through the appropriate selection of menu options. This variable end condition is sometimes desirable if only a few points are known or if physical constraints require accurate control of the curve shape at the ends.

The forms of the end conditions provided to set up the boundary
equations are given below:
(i) Clamped.

The first derivative is specified to have a certain
value as mentioned before. This would simply mean that the two boundary equations are:

$$
\begin{equation*}
y_{1}^{\prime}=B_{1} \quad \text { and } \quad y_{n}^{\prime}=B_{n} \tag{6.54}
\end{equation*}
$$

Thus, in matrix form:

(ii) Natural or Relaxed.

This is defined as $y^{\prime \prime}\left(x_{1}\right)=y^{\prime \prime}\left(x_{n}\right)=0$.
Using equations (6.29) and (6.30), we obtain the following two equations:
at $x=x_{1}$

$$
\begin{equation*}
y_{1}^{\prime}+\frac{1}{2} y_{2}^{\prime}=\frac{3}{2} \frac{\Delta y_{1}}{\Delta x_{1}} \tag{6.56}
\end{equation*}
$$

and at $x=x_{n}$

$$
\begin{equation*}
y_{n-1}^{\prime}+2 y_{n}^{\prime}=3 \frac{\Delta y_{n-1}}{\Delta x_{n-1}} \tag{6.57}
\end{equation*}
$$

In matrix form:

(iii) Parabolic

This requires that the second derivative is constant over the entire end interval. That is,

$$
\frac{d^{2} y}{d x^{2}}=\text { constant or } \quad y^{\prime \prime}\left(x_{1}\right)=y^{\prime \prime}\left(x_{2}\right)
$$

Hence, using equation (6.29) and (6.30), we have

$$
\begin{array}{cc} 
& { }^{2 \mathrm{~B}_{1}}=6 \mathrm{~A}_{1} \Delta \mathrm{x}_{1}+2 \mathrm{~B}_{1} \\
& \cdots \mathrm{~A}_{1}=0 \\
\text { i.e. } & y_{1}^{\prime}+y_{2}^{\prime}=2 \frac{\Delta \mathrm{y}_{1}}{\Delta \mathrm{x}_{1}} \tag{6.59}
\end{array}
$$

Similarly for the other end, we have

$$
\begin{align*}
& y^{\prime \prime}\left(x_{n-1}\right)=y^{\prime \prime}\left(x_{n}\right)  \tag{6.60}\\
& \therefore y_{n-1}^{\prime}+y_{n}^{\prime}=2 \frac{\Delta y_{n-1}}{\Delta x_{n-1}}
\end{align*}
$$

In matrix form, we get


Just to emphasise that the above end conditions do not have to be identical at each end of the spline, any permutation of the above three sets of end condition can be used without affecting the tridiagonal nature of the coefficient matrix. However, the following end condition would produce a non-tridiagonal matrix.
(iv) Q-spline.

This requires that the two adjacent segments at either end have a common cubic equation. This means that the second derivative at the end point and next two points are collinear [30]. The Q-spline predicts the final curvature from the two adjacent values:
this use of higher-order information would be useful in the absence of an alternative choice.

Consider Figure 6.4. From the similarity of the triangles a c d and $\mathrm{a} b \mathrm{e}$ we have the following equation:

$$
\begin{equation*}
\left[y^{\prime \prime}\left(x_{2}\right)-y^{\prime \prime}\left(x_{1}\right)\right] \Delta x_{2}=\left[y^{\prime \prime}\left(x_{3}\right)-y^{\prime \prime}\left(x_{2}\right)\right] \Delta x_{1} \tag{6.62}
\end{equation*}
$$

Substitute into equation (6.62) from equations (6.29) and (6.30); we obtain

$$
\begin{equation*}
y_{1}^{\prime}+\left(1-\left(\frac{\Delta x_{1}}{\Delta x_{2}}\right) y_{2}^{\prime}-\left(\frac{\Delta x_{1}}{\Delta x_{2}}\right)^{2} y_{3}^{\prime}=\frac{2}{\Delta x_{1}}\left(\Delta y_{1}-\left(\frac{\Delta x_{1}}{\Delta x_{2}}\right)^{3} \Delta y_{2}\right)\right. \tag{6.63}
\end{equation*}
$$

and similarly for the other end

$$
\begin{equation*}
-\left(\frac{\Delta x_{n-2}}{\Delta x_{n-1}}\right)^{2} y_{n-2}^{\prime}+\left(1-\left(\frac{\Delta x_{n-2}}{\Delta x_{n-1}}\right)^{2}\right) y_{n-1}^{\prime}+y_{n}^{\prime}=\frac{2}{\Delta x_{n-1}}\left(\Delta y_{n}-\left(\frac{\Delta x_{n-2}}{\Delta x_{n-1}}\right)^{2} \Delta y_{n-1}\right) \tag{6.64}
\end{equation*}
$$

In matrix form:

where

$$
\mathrm{B}_{1}=\frac{2}{\Delta \mathrm{x}_{1}}\left(\Delta \mathrm{y}_{1}-\left(\frac{\Delta \mathrm{x}_{1}}{\Delta \mathrm{x}_{2}}\right)^{3} \Delta \mathrm{y}_{2}\right)
$$

$$
B_{n}=\frac{2}{\Delta x_{n-1}}\left(\Delta y_{n}-\left(\frac{\Delta x_{n-2}}{\Delta x_{n-1}}\right)^{3} \Delta y_{n-1}\right.
$$

and

$$
B_{k}=3\left(\frac{\Delta x_{k}}{\Delta x_{k-1}} \Delta y_{k-1}+\frac{\Delta x_{k-1}}{\Delta x_{k}} \Delta y_{k}\right) \quad k=2(1) n-1
$$

Again the Q-spline can be used at either or both ends. However, when this ending is used, it would produce a non-tridiagonal matrix, and the tridiagonal Gaussian elimination used so far is no longer suitable.


FIGURE 6.3: Fitting Cubic Spline Polynomials


FIGURE 6.4: Q-Spline End Condition

A modified version of Gaussian elimination developed by Evans [32] for quindiagonal systems is used for solving the above equations with all possible combinations of boundary conditions. The algorithm was adapted to avoidany unnecessary computation and storage due to zero elements of the two outer diagonals.

## 3. THE USER INTERFACE

### 3.1 An Overall View of the System

The system described here allows a user to enter a set of data points into the computer either via a keyboard or from an on-line file (e.g. disc file), and interactively to specify various ways of fitting, editing and displaying the curve on the Tekronix 4010 storage tube. Thus, the basic problem which is handled by this system is one in which the user presents the machine with a finite set of data points and then manipulates these points until he obtains some curve which is satisfactory to him. The system may also be used as a tool to examine the problem of determining the minimum number of points needed to be able to represent a given input curve. It allows great flexibility in making changes in both input data and output curve interactively. Other uses are also possible as will become apparent in the subsequent discussion.

When designing an interactive system, a very important consideration is the appearance of the system to the user. The system should be designed so that any user can understand what is happening and what is expected of him at each step. The development of an effective but simple manmachine interface is sometimes referred to as the 'human engineering' aspect of the system. Although the IDF system is a special purpose interactive system used by a selected group of users, it is designed with the above aim in mind. As a simple example, words used in menu options should be chosen so as to convey the same meaning to all varieties
of user and yet the message should be concise. The system provides checks on user input and reminders or instructional displays on user requests. Consequently, the user's interface is intended to provide the most natural and simple dialogue with the system.

In the design of the IDF system, the user's needs are hopefully being anticipated by presenting him with different options in the form of a menu. Only those options (actions) that are legitimate at a particular step in the data-fitting process are presented for user selection. This avoids the entry of illegal requests which may require elaborate error procedures.

Essentially, from the user point of view, the IDF system consists of a number of logically connected display images as depicted by the flowchart in Figure 6.5. Conceptually, the data-fitting represented by the various displays shown can be described as consisting of three basic phases:
(1) Input specification, which includes the entry of data points and editing.
(2) Numerical Computation required to produce the smooth curve.
(3) Display of the resulting curve and other relevant information.

Each stage would have a number of displays associated with it (some are optional) as illustrated by the dotted lines of Figure 6.5.

Most displays in the system show the following menu options:-

| +NEXT |
| :--- |
| +PREVIOUS |
| +RELP |
| +RESTART |
| +EXIT |

+EXIT

The system response to each individual option is described

(a) Move onto the next display.

The current display is erased and the next one in sequence is brought up on the screen.
(b) Move back to the previous display.

The current display is erased and the preceeding one is called.
(c) On-line help.

When the user is seeking immediate advice on the system, this option would enable him to obtain the answer without the need to consult an external source. The resulting display HELP (Figure 6.8) provides the user with the following:
(i) It describes briefly the functions of the various displays in their logical sequence as given in Figure 6.5.
(ii) Each display in the list is made user selectable in the same manner as that of a menu option. Hence, it permits the user to transfer control to any point within the data-fitting process, and the appropriate display is brought up on the screen. However, the system does not allow transfer of control to points in the process that are not yet meaningful. For example, if a fit has not yet been computed, a transfer to 'curve fit' display is meaningless. This branching out facility also enables the user to recover the state of the process,
if the system terminates due to program error or user's unexpected action. The recovery is simply accomplished by keying in the command 'HELP' which would set up the help display, and the user may resume thereafter.
(iii) It also includes an option to produce a display containing the definition of all menu options used in the system (Figure 6.9).
(d) Reset the current display to its initial state of entry.
(e) Terminate the interactive session and prepare the system ready for next user.

These command menu options are used for directional control over the display sequence, giving the user the justifiable feeling that he is in charge of the system operations. They allow the user freedom to progress through the program normally or go back and review any previous display. This relationship between man and terminal must be such that he finds its use natural, pleasant and efficient.

Other specific options appear in the display menu corresponding to the role of that particular display in the process. These options will be described in some detail in the next section.

When an option is chosen from the menu, an arrow appears next to it, to indicate that a selection has been made. However, the option is not executed until the user has confirmed his choice by pressing the key $\mathrm{Y}(\mathrm{YES})$ in response to the message 'CONTINUE $\mathrm{Y} / \mathrm{N}$ ?'. This allows the user to change his mind and prevents inadvertent execution of undesirable options.

### 3.2 Function of the Various Displays <br> In what follows we describe the function of the displays corresponding to each of the boxes of the flow chart of Figure 6.5. This is illustrated by photographic reproduction of the screen as seen by the user during a typical interactive session at the terminal. The snapshots will include examples from both the parametric and the explicit methods. The numbering used in the following paragraphs is identical to that of Figure 6.5.

## [1] Introductory

This is the first display to appear on the screen (Figures 6.6 and 6.7); it briefly describes the system and gives some general information regarding menu options. This initial display would be important for first time or occasional users and should be read carefully before proceeding to the next display in the sequence. In addition, the help displays (Figures 6.8 and 6.9) may also be regarded as supplementary to the introductory display. These displays effectively form an on-line user's guide to the IDF system.
[2] Choice of numerical al gorithm
This display contains a list of currently available algorithms (Figures 6.10 and 6.11). By means of the cross-hair cursor, the user is able to select a suitable algorithm in conjunction with a particular type of end condition (see section 2.4). The boundary values will be declared in the parameter entry display.

The modular design of the system permits the incorporation of other algorithms with minimum programming effort.


FIGURE 6.6: Introductory Display (Explicit)



FIGURE 6.8: The HELP Display



## FIGURE 6.10: Choice of Numerical Algorithm and End Condition (Explicit)



FIGURE 6.11: Choice of Numerical Algorithm and End
Condition (Parametric)

## [3] Data entry

After choosing the desired algorithm, the next step is to enter the data points into the system. There are two types of data source in this system. The first is external data which is entered either directly from the keyboard or a named disc file. The second is internal i.e. data from the immediately preceding problem. The latter is useful when slight variations of data or changes of algorithm/boundary condition are required.

The user is presented with a 'data specification' menu (Figures 6.12 and 6.13 ) which contains options on the state, dimensionality and medium of data entry. The state of data options are:
(a) Data is to be entered for the first time.

+ NEW
+ +OLD

The dimensionality is applicable in the case of parametric methods.
(a) Plane curve, requiring $(x, y)$ data.
(b) Space curve, requiring $(x, y, z)$ data.
$\rightarrow+2-$ DIMEN
++3 -DIMEN Data medium entry
(a) Data is entered at the keyboard by typing the $x$ coordinates separated by commas followed by the $y$-coordinates (and z-coordinates if applicable).
(b) Data may also be entered from an on-line file, which must be named. This data file would have been created previously by a user program in the form of consecutive $x, y$ pairs (or $x, y, z$ triples).


FIGURE 6.12: Data Entry Specification (Explicit)


FIGURE 6.13: Data Entry Specification (Parametric)

## [4] Data tabulation and editing

Once the data has been entered, the ' +NEXT ' display in the sequence presents the user with a table of the stored data points (Figure 6.14). This allows the user to check the input for possible errors and correct these before proceeding to the next display.

Often the user may also wish to alter the input data points in some way. These alterations may include, for example
(1) Selection of a subset of the data points.
(2) Insertion of new data points.
(3) Changing the order of the points in the set.
(4) Modification of individual values.

Data manipulation options relating particularly to this display are:
(a) Data point editing.
+EDIT
This generates an auxiliary display, containing a second level of menu options, permitting the user to correct, delete or insert data points in the existing set:

An example of such use is illustrated in Figure 6.15, where two new data points have been inserted. A revised table of the data is shown in Figure 6.16 which appears immediately after the editing operations.
(b) The new data set may be stored on a named disc file using this option. The name of the file is entered from the keyboard in response to the system request 'file Name?'


FIGURE 6.14: Table of Input Data Points


FIGURE 6.15: Data Editing with Insertion

(c) This would sort the data in ascending order of $x$ values. It may be necessary, for example, when using the explicit form $y=f(x)$, for which the $x$ data must be monotonically increasing.
[5] Polygonal plot
This is an optional display which is included in the system.
It can be ignored by passing control to the ${ }^{\prime}+\mathrm{NEXT}^{\prime}$ display. It allows the user to produce a graphical plot of the input data points joined by a sequence of straight lines. Note that this is equivalent to fitting polynomials of lowest possible degree $(y=A+B x)$ to consecutive pairs of points. Although the oscillation of the interpolating function here is minimal, the first derivatives at the interior points are discontinuous, and the curve of course is not smooth. However, the purpose of this display is just to give the user an initial feel of the curve shape. It also allows him graphically to re-check the correctness and order of the input data before invoking the smoothing algorithm.

The curve (in this case the polygon) is drawn within a pre-defined viewport. However, the limits of the plotting area can be controlled by the user interactively. The procedure would involve the use of the following options:
(a) This would allow the user to set up the limits required for the display axes, by typing the minimum and maximum values. As shown in Figures 6.17 and 6.18, the user is already informed about the corresponding data limits prior to his action. In this way he has control of the display process.


FIGURE 6.17: Polygonal Plot of a Single-Valued Curve


FIGURE 6.18: Polygonal Plot of a Multi-Valued Curve
(b) When this option is selected, the actual drawing operation would take place. The input data points are plotted as plus (+) signs as shown. Note that if this option is selected without prior use of option (a), then the viewport limits would by default be set equal to the input data limits.

[6] Parameter entry
After the data has been entered, and then modified as desired, the ' + NEXT' display on the screen is the parameter entry, shown in Figures 6.19 and 6.20. The user is provided here with a 'parameter specification' menu containing various options on each parameter. These are:
(1) The data type.

In practice, the user could encounter a situation where the required curve has known discontinuities of slope or curvature at certain points. This situation is handled by the present system by allowing the user to partition the given set of points into several subsets (up to 5 at present) at the points of discontinuity. The subsets are specified separately at this stage. Consequently, the system would produce a smooth curve for each segment and join them internally so that the user is able to display the complete joined curve later.

The parameter options provided are:
(a) For a complete (non-partitioned) set of
data points.
(b) For partitioned data. The first subset must be recognised separately for SUBSEQUENT
+COMPLETE

| FIRST |
| :---: | :---: |$\rightarrow+$ SUBSET -1 building the complete joined curve. Any other subset is identified as a subsequent subset.



FIGURE 6.19: Parameter Entry Display of Cubic Spline (Explicit)

(2) Choice of intermediate points.

Graphical output devices for digital computers can only be used to a given (raster) resolution. A curve is drawn by specifying a series of raster points which approximate the curve, or by the start point of the curve and a series of increments. In either case the curve is represented by a series of straight line segments.

This option determines the number of straight line segments required in each data interval to draw an acceptably smooth curve. In order to determine this, three choices are provided:
(a) The number of points per interval is specified via the keyboard. This number would be the same for each interval along the curve. However, the use of the same density of points in each interval can sometimes produce unsatisfactory results, since segments with higher curvature obviously require more points than others.
(b) This employs a built in algorithm to calculate the number of points necessary for each interval. This method is based on using the chord length of each interval relative to the total funicular polygon of the data points. The algorithm sets internally an upper limit to the total number of points (i.e. number of line segments required to draw the curve. A limit of 200 points is chosen to give a reasonable distribution of points over the display region (viewport) and avoids damaging the screen. A simple formula was derived for this to check the computed number of intermediate points,

$$
\begin{equation*}
N_{I} \leqslant \frac{200-N}{N-1} \tag{6.66}
\end{equation*}
$$

where N is the number of data points. Typical values are given by the Table:

| N | 2 | 10 | 50 | 100 | $>100$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\left[\max \mathrm{~N}_{\mathrm{I}}\right]$ | 198 | 21 | 3 | 1 | 0 |

(c) This choice allows the user to select visually the intermediate points by means of the cursor, with full control over the smoothness of the trace.
(3) Select the end condition.

The algorithms listed in 3.2 [2]-Figures 6.10 and 6.11
allow different ways of selecting the boundary conditions. In the most general case ('variable end condition') the available boundary condition options, as described in section 2.4 , are $\rightarrow$
+CLAMPED +RELAXED +PARABOLA +Q-SPLINE

The user must indicate the appropriate menu entry specifying the boundary condition for each end. In the example shown in Figures 6.19 and 6.20, the same form of condition is used at both ends. In general, however, the condition at end 1 can be specified independently of that at end 2 , so that two different forms of condition are possible (e.g. '+CLAMPED' at end 1 and '+RELAXED' at end 2).

Once the user has selected the required parameter, the next step is to invoke the numerical algorithm to compute the interpolated curve by selecting the option '+NEXT' in the main menu. At this stage, the system message 'PLEASE WAIT, FIT IS BEING COMPUTED' is displayed since the number crunching involved would be relatively time-consuming (See Chapter 5).

## [7] Curve Fit

This display appears on the screen when the interpolated curve has been computed. The curve is drawn in the same way as illustrated in the polygon plot using the menu options ' + GRAPH' and '+DISP.ORG.'. In the parametric case, three menu options are provided for this purpose, namely
in order to enable the user to display an orthogonal projection of a three-dimensional curve. Examples of a two-dimensional curve are shown in Figures 6.21, 6.22 and 6.23, employing the explicit and the parametric form respectively.

A wide range of menu options are provided in this display for anticipating most user requirements in interpreting the resulting curve. These options enable the user to interrogate the computed curve or extract further information either in tabular form or by comparison with other related curves.
(a) Axes marking.

This tags the lines enclosing the viewport with scaling marks. Each line is divided into ten equal parts, hence producing a linear scale along the display axes. The actual plotting axes are displayed if the origin $(0,0)$ falls within the defined window (Figure 6.21b). The window limits are displayed at the bottom right-hand corner of the screen.
(b) Reading the coordinates of a point.

If the user requires to know the coordinates of a specific point in the data window, the crosshair cursor is located at the desired point. Then by pressing any key on the keyboard, the coordinate


FIGURE 6.21a: A Two-dimensional Smooth Curve using the Explicit Form


FIGURE 6.21b: Curve Fit Display Showing the Use of
'+AX-MARK' and '+COORDS' Options


FIGURE 6.22: A Two-dimensional Smooth Curve Using the Parametric form

of that point would be displayed (Figure 6.21b). This facility could be useful, for example, if the user wished to introduce other data points and reexamine the curve again.
(c) Saving an interpolated curve on disc file

This option is used to store on a disc file for subsequent use the complete set of scaled points representing the smooth curve. The name of this file is entered through the keyboard in response to a system prompt.
(d) Drawing a curve from a named disc file.

Interpolated curves previously stored on disc file can be redrawn for viewing together with other displayed curves. This facility may have a number of uses, in particular when the user wishes to investigate the effect of applying different forms of end condition.
(e) Magnifying part of the screen.

This is used to enlarge part of the screen. The zooming window is defined interactively by cursor input of any two diagonally opposite corners (Figure 6.24a). Once this has been accomplished, the program will perform the necessary clipping and display the zoomed part (Figure 6.24b).
(f) When this option is selected, the user will be presented with an ordered tabulation of the interpolated and input data points (Figures 6.25a and 6.25b). The menu of this tabular display contains the following additional options:


FIGURE 6.24a: Using the ${ }^{\prime}+$ ZOOM' Option


FIGURE 6.24b: Display of the Zoomed Portion


FIGURE 6.25a: Table of the Computed Data Points on the Smooth Curve of Fig. 6.21a


FIGURE 6.25b: Tab1e of the Comprited Data Pointion the Smooth Curve of $1: 1 ; 6.22$
(1) This provides the user with a table of values $\rightarrow+$ COEFFNT of the computed polynomial coefficients for each data interval, (Figures 6.26a, 6.26b and 6.26c).
(2) Roll-by of tabular information.

Sometimes it is not possible to accommodate the whole table on the available screen area. These options are used to control the display of a large numerical table (e.g. data points) by scrolling forward or back through the table page by page.
(3) Hardcopy print of the numerical table can be obtained on one of the existing teletypes if this option is selected. This facility is easily extended to other hardcopy devices.
(g) This option is specifically used for joining partitioned curves, which have been previously defined in the parameter entry display. When the option is first selected, the system will internally append the data points representing the current displayed curve to the other segments, providing the user has already specified the appropriate data parameter. If the option is picked up for the second time, new display will be brought up on the screen, allowing the user to draw the complete joined curve. The two smooth curve segments shown in Figures 6.27 a and 6.27 b have been joined to produce the curve shown in Figure 6.27 c , which includes an internal slope discontinuity. Figure 6.27d represents an enlargement (zoom) of the region surrounding the discontinuity point.


FIGURE 6.26a: Computed Polynomial Coefficients of Fig.6.21a for Cubic Spline


FIGURE 6.26b: Computed Polynomial Coefficients of the Cubic Spline (Parametric) for $x$ of Fig.6.22


FIGURE 6.26c: Computed Polynomial Coefficients of the Cubic Spline (Parametric) for $y$ of Fig. 6.22


FIGURE 6.27a: Segment 1 of the Joined Curve


FIGURE 6.27b: Segment 2 of the Joined Curve


## FIGURE 6.27c: Display of the Joined Curve <br> (Segment 1 and 2)



FiuURE 6.27d: A Zoomed Portion of the voinsd Curve Near the Discontinuty
(h) A multiple display of a group of related curves can be ++ NGRAPH generated using this option (Figure 6.28). For this purpose, every time a smooth curve of the group is produced this option is selected in order to inform the system of our intention. The superimposed curve display is generated when this option is immediately re-selected. The curves are labelled with consecutive numbers according to their generation sequence. Two additional options are provided:
(1) It allows the user to remove a particular curve $\rightarrow+$ DELETE from the group. This is accomplished once the curve number has been typed in.
(2) This erases the unwanted curve from the screen. $\rightarrow+$ REFRESH
(i) When this option is selected, an auxiliary display is $\rightarrow+$ CRV.DES. generated. This display enables the user interactively by cursor input, to select intermediate points in each interval. By this means, the user is able to control the length of the elemental line segments, so that intervals with higher curvature would have shorter segments. Two examples of such displays are shown in Figures 6.29 a and 6.29 b . The use of this display can be exploited in two basic ways:
(i) Starting from the displayed data points, the curve can be traced by progressing from one interval to another and drawing the line segments.
(ii) An existing traced curve can be visually improved if necessary by reconstructing individual segments.


FIGURE 6.28 : Multiple Display of Several Curves


FIGURE 6.29a: Interactive Choice of Intermediate Points by Means of Cursor (Explicit)


The operations required to trace the curve are basically equivalent to the editing process i.e. delete or insert data' points. In other words, this is effectively graphical editing of the displayed curve. For this purpose two options are provided:
(1) Once this is selected, the cursor control is returned back to the user enabling him to select intermediate points. This is accomplished by positioning the cursor at the desired intermediate point and by pressing a key (e.g. space bar) on the keyboard. The program would respond by drawing the desired line segment in that interval. In this way the user can progressively trace the curve or add new line segments between two existing points to obtain the required smoothness.
(2) When this option is selected, the user can use the $\rightarrow+$ DEL.INT cursor to point at a required interval and virtually remove the entire line segments within this interval. The line segments are physically erased by using the '+REFRESH' option.

### 3.3 Examples

Several examples of interpolated curves are illustrated in Figures 6.30-6.33 to demonstrate the effects of the various algorithms.
(1) Figures 6.30 a and 6.30 b display the smooth curves passing through the same data points using the global and piecewise quintic polynomial interpolation methods. It can be seen clearly that the former method produces undesirable


FIGURE 6.30a: Interpolated Curve using a Global
(Newton) Polynomial


FIGURE 6.30b: The Same Data Points as in rig.6.30a
Using Piecewise owintio Po:monis? Enaravatorn (Maude)


FIGURE 6.31: A Two-dimensional Spiral Curve with Relaxed End Condition


FIGURE 6.32a: Cyclic End Condition



FIGURE 6.33a: Three-dimensional Curve Projected on YX-plane


FIGURE 6.33b: Three-dimensional Curve Projected on XZ-plane


[^0]oscillations in the curve in particular near the end points.
(2) Figure 6.31 shows the result of using the two-dimensional parametric splines with natural (relaxed) end condition for a multivalued spiral function.
(3) Figures 6.32a and 6.32 b illustrate the use of two-dimensional parametric cubic splines with cyclic and anticyclic end conditions respectively.
(4) Finally Figures 6.33a, 6.33b and 6.33c arise from the use of three-dimensional parametric splines with specified parametric slopes at both ends. The parameter entry display for this is shown in Figure 6.20.

## 4. PROGRAM DESIGN

The program development of this system was initially carried out under RSTS-11 time-sharing system using BASIC-PLUS. At that time no proper graphic software was available locally except a small set of primitive routines written in BASIC-PLUS to drive the Tektronix 4010. Since then UNIX has become operational and the LIGHT package developed; the entire system was rewritten in UNIX-FORTRAN and enhanced further by improving its design features. The system has been designed and implemented in a modular manner, so that additional capabilities can be easily incorporated; for example, new interpolating algorithms or some additional display images that would aid user interpretation of the results. Complete Fortran listings of the individual modules are presented in Appendices 2.2 and 2.3.

### 4.1 The Interactive Display Routines

In designing such systems we are faced with a man-machine interaction situation involving all the usual ergonomic problems.

A program (routine) is termed to be interactive if it depends for its successful completion on the establishment of a dialogue between user and machine. Therefore, the designer has to resolve the problem of structuring the program so that a dialogue will take place. The form of this dialogue will be written into the program as an algorithm, the alternatives within that algorithm being selected as the result of information either supplied by the user, or deduced within the program itself. In an interactive program certain decisions involve a simple binary choice (yes or no), whilst others require the selection of a subset of actions from a given set of alternatives. What we have, then, is a complex algorithm involving man and machine at various stages. This will require the breaking down of each stage into its constituent parts and looking at the ordering of these parts. Following this line of thinking, the IDF system basically consists of a number of interactive display routines which generate the display images and provide the interactive capability at various stages of the data-fitting process illustrated in Figure 6.5.

The experience of developing these routines under-ined the value, indeed the necessity, of an extensive use of subroutines. Although the complete package was written single-handed, the independent nature of the subroutines would have permitted a group of programmers to write and debug individual routines in parallel, once the definitions had been made.

Program communication between these routines involves the normal use of the subroutine parameter mechanism or a COMMON data area. The interactive facilities of individual routines may be extended or modified
without affecting the others, providing each interface remains the same. Every interactive display routine sets up its own menu. The items (options) of the menu represent the various capabilities that a particular routine is programmed to handle. The text of the menu is defined as a hollerith string of characters in an array (e.g. MNTXT), declared as LOGICAL*1, in a DATA statement. This array type declaration in UNIX-FORTRAN resembles the BYTE type declaration used in DOS-FORTRAN [33].

It is often necessary to define a second menu in certain display routines so that a group of independent options are set in a separate menu which in turn is distinguished from the main menu (e.g. in parameter entry). This avoids the display of a large number of menu options in a single menu, which could confuse the terminal user.

The routine, having set the various default values, clears the screen (CALL TXCLER) in preparation for the next display image. Following this, it outputs the display title and often some information text instructing the user briefly on the various options or messages required for keyboard entry. The menu is then displayed by issuing calls to the LIGHT menu handling routines, for example:

```
CALL MNOPEN(875.,715.,1)
CALL MNDISP(MNTXT,5,10,1)
CALL FRAME (870.,732.,5)
CALL MNPICK(J,ICHAR,MNO)
```

As a result the user is prompted by the immediate appearance of the cross-hair cursor on the screen giving him control over the execution path of the routine through the selection of menu options. The user would now be ready to make his own choice from the menu, while the interactive routine is waiting to respond. The routine distinguishes between the two menus, when necessary, from the returned integer value in MNO (1 or 2). The routine treats the two menus in slightly different ways. For example, all options picked up from the main menu must be confirmed by the user. This avoids or at least minimises incorrect
menu selection, which may cause the deletion of intermediate data files or overwriting the COMMON data area. On the other hand, options selected from the second menu have only a local effect and need not be confirmed. Their effect can be cancelled by selecting alternative options.

As soon as the user has confirmed his selection, the routine branches to the appropriate code (or calls the appropriate routine) depending on which option of the menu is picked up. This simple transfer of control is often effected by a computed GOTO statement e.g. $\operatorname{GOTO}(10,20,30 \ldots . .),$.
where $J$ is the option sequence number within the menu. Therefore the routine may invoke some special purpose subroutines to perform certain tasks which correspond to the user's request. If, however, the user has selected an option that requires a new display image to be brought up on the screen (e.g. ' + NEXT' or ${ }^{\prime}+\mathrm{PREVIOUS}^{\prime}$ ), then control is returned to the main program calling sequence.

### 4.2 Program Module

The IDF package is divided into several program modules, each module being autonomous and self-contained. The reason is that the size of the core currently available is not large enough to incorporate the entire package as a single executable module. In fact, a constraint which was imposed at an early stage of the design was the ability to run the system on a machine having 16 K words of user area. This of course improves the portability of the package.

The absence of a direct overlaying scheme under UNIX, has led us to employ the simple facility provided by the LIGHT package through the subroutine call 'OVRLAY' discussed in Chapter 5.

Basically, each module has its own main program segment (driver program) monitoring user interaction with the system. This in turn controls the flow of logic between a set of display routines. The main program also passes control to other modules when required via the overlay routine, e.g. CALL OVRLAY (MODL2). Where MODL2 is the file name of the module which is to be brought from the disc into core and executed. Therefore, at any one time during the running of the system only one module is occupying the user area. A typical organisation of such a modular structure is illustrated in Figure 6.34.

The organization of the package into separate modules, each independently performing a given set of tasks, has greatly simplified the actual development and implementation work. In particular, owing to the tree structure of the UNIX file system directory, it was possible to arrange the program source codes of each module as it develops under a separate subdirectory. This helps us to test and debug individual modules thoroughly before they are included in the package and re-tested.

Data communication between modules is maintained via COMMON data areas. When the in-core module is overlayed by the new module, the COMMON data areas are no longer accessible to the new module, since all code and data of the old module is virtually replaced by the file containing the new module. Therefore, it was vital to save the COMMON data on a disc file before the new module is brought into core, and restore it immediately afterwards. These data files are created internally by the system at run time and eventually removed when the user decides to terminate the session by selecting the option '+EXIT'. Evidently, the reading and writing of these data files during the overlay operation could effect the response time of the system, and will also occupy a certain amount of disc space. However, these files have a useful function in providing a back-up facility in the


FIGURE 6.34: Program Organization of Module 1 of the IDF System
event of user as well as program errors which can cause premature termination of the session. As mentioned in section 3, the user may recover the display image and subsequently resume the program by typing the command HELP at the keyboard. In this way, the data in the files are correctly despatched into program variables and stored back again into the COMMON data areas.

There are basically two labelled COMMON data areas used to communicate between the different modules of the system:
(1) DATASUP: This contains the input information supplied by the user concerning the curve under investigation. The data points defining.the shape of the curve are held in one-dimensional array ( $X, Y,[Z]$ ), allowing up to 50 points to be specified. The one-dimensional integer arrays ( $\mathrm{L}, \mathrm{IH}$ ) are also used to contain the linked list pointers. These are initialised and used in conjunction with the data point arrays to form a linked list data structure which is utilized in the data point edit operations. An array NPI is also used to hold the number of intermediate points required in each interval for actually drawing the smooth curve. Other variables are also used to contain input information such as the index of the selected algorithm, boundary values,... etc.
(2) CURVEFIT: This contains the output results of the numerical algorithm applied. The complete set of the interpolated points representing the smooth curve are stored in the onedimensional array (XCORD, YCORD,[ZCORD]). The computed polynomial coefficients are held in the two-dimensional array COEF.

All modules share common library subroutines archived in 'EPLIB'
file. Program listings of the subroutines are given in Appendix 2.4. The functions of these subroutines fall into two categories:
(1) read and write operations of the common data areas into and from the data files.
(2) utility display routines, including for example:

- setting the display window and viewport.
- marking the axes.
- reading the display origin coordinates from the keyboard.
. reading input cursor coordinates off the screen.


### 4.3 Overlay Support

The present overlay structure requires that each single module should have a main program segment as shown in Figure 6.34. Note that here the 'driver program' (for each module) is essentially the same and this is obviously wasteful. A much better structure would be to have a control module or root segment module (as shown in Figure 6.35) which monitors user action on the screen and automatically overlays other modules when their associated options are picked up from the menu. Each overlayed module consists of a number of interactive display routines as shown.

An investigation was made to find out the possibility of achieving such an overlay structure under UNIX. Since UNIX is a process-based operating system, in order to have the control module and any other module in core at any one time, we require two independently executing processes each having a separate core image. A new process can come into existence only by use of the system call FORK [21]. If FORK is executed by the control module as a process (parent), a new process (child) is created and its core image is a copy of that of the parent.

In the child, control returns directly from the FORK (i.e. to the instruction following the FORK), while in the parent, control is passed to the next instruction (i.e. a skip return):

| e.g. | SYS | FORK | /CALL FORK OPERATION |
| :--- | :--- | :--- | :--- |
|  | BR | CHILD | /RETURN HERE FOR CHILD |
|  | $\vdots$ |  | /RETURN HERE FOR PARENT |

At label CHILD in the above example, we may execute code in the new process. Should we wish to overlay this process with a new child process, we execute an EXEC system call as part of the CHILD code, for example

CHILD:
:
SYS EXEC
Parameters supplied with the EXEC system call specify the image to be overlayed. This image is overlayed and control passed to it. Meanwhile the parent process is continuing to run 'in parallel'. In the present case, we need to cause the parent to wait for the child to terminate since the parent is doing no more than interfacing with the user at command level. This is effected by using the system call WaIt. Hence the code for overlaying is:-

|  | $\vdots$ |  |
| :---: | :---: | :--- |
|  | SYS FORK |  |
|  | BR CHILD | /CALL FORK OPERATION |
|  | SYS WAIT | /RETURN HERE FOR CHILD |
|  | $\vdots$ | /HERE FOR PARENT WAIT |
| CHILD | SYS CHILD TO TERMINATE |  |

Hence, the child process core image can be overlayed by the appropriate module and control passed to it.

The remaining problem is to provide a means of accessing data from the COMMON area. Since processes are normally swapped in and out of core and they are relocatable and totally independent, the COMMON data area in the control module (parent) is no longer accessible by the overlayed module (child).

There are operating systems which have a built in overlay mechanism for handling such an overlay structure. As an example, the RSX-11 [34] assumes that the basic program unit executing under its environment is a task, which may consist of a program module or a set of program modules. The overlay structure consists of a single root segment and any number of overlay segments which share memory with one another. Any one of these overlays may likewise give rise to a number of tasks which further overlay one another Figure 6.36. In this example, $A, B$ and $C$ overlay each other as do the tasks belonging to $A$ or B or C. All tasks at a given level (indicated by the arrows) share a COMMON area of memory. Considering any task at any level, it is possible for that task to access global data in any segment on a path between that task and the root. For example, in Figure 6.36 task D may reference any global data in task $A$ or the root segment. Ultimately all tasks may reference global data in the ROOT segment and hence this may be used to store, amongst other things, shared data. The Fortran COMMON block may be included in this shared region, making it accessible to all other modules. Unfortunately, with the present environment (i.e. under UNIX), it is not possible to have a shared region between modules to hold the COMMON data. However, communication between the two processes can be accomplished by either using data files as before or incorporating the system entry 'PIPE' which allows communication between processes.

### 4.4 Data Structure

Since this application has offered the user the facility of manipulating interactively the data points representing the curve, it requires a dynamically changing list of points. For this purpose, a


Interactive display routine

FIGURE 6.35: The Proposed Overlay Structure


FIGURE 6.36: Overlay Segments
simple form of linked list data structure was tailored for this application, so that anywhere in the list data points can be inserted, deleted or replaced by other points without disturbing the rest of the structure.

These capabilities were provided as shown earlier in the data editing and the curve design displays. In the former, the user was able to alter freely the list of the input data points displayed in tabular form, whereas in the latter he was given the ability via the cursor to change the number of intermediate points required in each interval directly on the displayed curve.

Therefore, both the input data points and the output points (computed smooth curve) are associated with pointers forming a linked list data structure. Basically, each element of the list consists of three (or four in the case of 3-D curves) data items as shown in Figure 6.37.

When a data structure is implemented, it is not only necessary to design the structure of the data, but also the algorithms which can retrieve and manipulate the data and its internal relationships. An important choice to be made in designing such a system is the balance between structure and algorithm, because the two are usually complement ary.

The linked lists chosen for this application are partitioned into sublists, in order to avoid searching the whole list to look for a particular element when performing a certain operation.

Consider first, the structure used in organizing the input data, as shown pictorially in Figure 6.38. The integer array IH holds the pointer to the start of each sublist which consists of a maximum of ten elements. A free list pointer is used to point at the list of unused elements. If a new element is required, it is taken from the
free list and conversely if an element is deleted from the list, it is returned to the free list.

A function subroutine INDEX is provided to do the mapping between the sequence number of the data point in its display tabular form and that of its actual location in the array list. This function returns an integer value indicating the location of the required element in the list. Three subroutines are also provided to handle the three basic edit operations on the list, namely deletion, insertion and correction.

Now consider the linked list associated with the output data points. This has essentially the same structure except that the last element of each sublist is not connected to the first element of the next sublist, as shown in Figure 6.39. Basically, each sublist consists of an input point followed by the intermediate points for that interval. The operations carried out on this list are concerned mainly with the deletion and insertion of intermediate data points. Routines are provided to handle these operations, keeping track of the free list and doing the garbage collection.

Finally, a data structure was also implemented for appending the segments of joined curves together. As this required a careful use of a set of array pointers showing precisely the start and end of each segment and their associated intermediate points. This structure is shown in Figure 6.40. The real arrays XJ and YJ contain the complete set of points for each segment. The integer arrays JJ3, JJ4 and IPNTR hold various items of information including number of intermediate points, start address of each segment and so on.


FIGURE 6.38: Data Structure Used in the Data Point Editing Display


FIGURE 6.39: Data Structure Used in the Curve Design Display


JJ3


FIGURE 6.40: Joined Curve Data Structure

## Chapter 7

## INTERACTIVE CONTOUR TRACING - ICT

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## 1. INTRODUCTION

### 1.1 Application Area

The representation of surfaces in the two-dimensional plane by means of contour maps is in widespread use in science and engineering. Such maps have both quantitative and pictorial value and thus are frequently used for presentation of final results and as a research tool.

The most common example is a contour map representing elevation as a function of position in a two-dimensional geographical region. Other position-dependent variables that are commonly represented in the form of contour maps are temperature (isotherms) and pressure (isobars). In some applications, contour maps may be used to facilitate visualisation of data even though an equation may exist that describes this data, for example, a plot of the equipotential lines around an electric dipole. Also, contour lines can be used to represent functions which are involved in some optimization process.

### 1.2 Contour Lines

Contour lines are usually defined as the lines of intersection between a given surface and a family of parallel surfaces, usually horizontal planes. This definition is ambiguous if the given surface has a horizontal portion at the same elevation as one of the horizontal planes. In order to overcome this difficulty Morse [35] defined the following types of contour lines (Figure 7.1):
(i) A positive (negative) contour line is a line connecting points all of the same elevation such that points adjacent to one side of the line are at higher (lower) elevation and points adjacent to other sides are at the same elevation or at a lower (higher) elevation. The usual contour line found on a contour map is the union of a positive and negative contour
line, both of the same elevation. A line is called a normal contour line if it is either a positive or a negative contour line.
(ii) A maximum (minimum) contour line is a line connecting points all of the same elevation such that all points adjacent to either side of the line are at a lower (higher) elevation. Maximum and minimum contour lines are degenerate cases of the normal contour (Figure 7.2).

The above definitions take care of all possible pathological situations in contouring. However, since these degeneracies are extremely rare and are not easily reproduced by finite computation of the function, they are not usually incorporated in a general-purpose contouring algorithm. The following two non-degenerate properties of contour lines are assumed in the subsequent work.
(a) Different contour lines never cross.
(b) Normal contour lines which do not intersect the boundary of the map are closed curves.

### 1.3 The Contouring Problem

Contouring is increasingly being implemented by computer with the aid of graph plotters and CRT displays. The object of contouring is to draw curves of constant value of a dependent variable (z), projected into the plane of two independent variables ( $x, y$ ). Each contour is approximated by piecewise-continuous lines and the basic problem is that of locating and linking these line segments.

The information (raw data) supplied will normally consist either of a finite number of values of the dependent variables $\left(z_{i}\right)$ at a set of locations ( $\mathrm{x}_{\mathbf{i}}, \mathrm{y}_{\mathbf{i}}$ ) - Figure 7.3 - or an explicit or implicit mathematical expression relating $z$ to $x$ and $y$ e.g. $z=\exp \left\{-1 / 4\left[(x-5)^{2}+(y-5)^{2}\right]\right\}$.


FIGURE 7.1: Resolving the Ambiguity


FIGURE 7.2: Degenerate Contours

In general, to trace a set of contour lines $c_{j}=f(x, y)$ for $j=1,2, \ldots, m$ over a desired region, it is the usual practice to have a reference system or grid in order to keep track of the contours and the regions which have been explored. For this purpose at least two distinct approaches axe possible:
(i) Partitioning the region into triangles whose vertices are the known finite set of data points. This triangulation involves joining neighbouring data points by straight lines to form triangular plane segments (Figure 7.4). An algorithm must be included to form an optimal partitioning of the region into triangles. An optimal partition, Pitteway [43], is one in which for any point within any triangle, that point lies at least as close to one of the vertices of the triangle as to any other data point. The triangles must be assigned so that they are as nearly equilateral as possible. The addition of this possibly timeconsuming algorithm to the program constitutes the major disadvantage of the method. However, it may be useful where the data locations are fixed (though non-equispaced), such as a set of permanent observatories or recording stations. The triangles then can be established once for a number of contour applications.
(ii) Superimposing a regular mesh on the region where it is used as a reference system. Most contouring algorithms make use of a rectangular grid (or net) imposed on the desired region (Figure 7.5). These algorithms are conceptually simpler and usually faster than those based on other reference systems.

The overall problem of drawing contour lines from a given arbitrary set of data points involves two logically different stages:-


FIGURE 7.3: Finite Set of Data Points Given At Arbitrary Locations


FIGURE 7.4: Triangular Partitioning


FIGURE 7.5: Regular Rectangular Mesh Superimposed Over a Finite Set of Data Points
(1) Interpolation, where for given $n$ values $z_{1}, z_{2}, \ldots, z_{n}$ at the positions $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right) \ldots\left(x_{n}, y_{n}\right)$, it is required to estimate a value of the function $z=f(x, y)$ at an arbitrary new location.
(2) Contour tracing, where for a given function $f(x, y)$ which can be calculated at any arbitrary location, it is required to draw a set of contour lines $f(x, y)=c_{j}$ for prescribed $c_{j}$, $\mathbf{j}=1,2, \ldots, m$.

When a rectangular grid is used, the two stages would involve the interpolation from the raw data to the grid points and then the contouring of the grid data.

An algorithm recently developed by Schagen [42] is based on the triangulation approach and interpolates from a set of arbitrary data points, using a generalised least-squares technique. The program has been implemented in Fortran on the ICL 1904S using an incremental plotter with GINO-F graphic software.

The work reported in this chapter is mainly concerned with the development and implementation of an interactive contour tracing algorithm based on a rectangular grid using a graphic display terminal (Tektronix 4010) and the local graphics package, LIGHT. The algorithm would trace the curve $f(x, y)=c$ in a region in which there is a method of calculating the function. Several methods exist for estimating the function value at mesh and intermediate points from a set of arbitrary data points. For example Mclain [39] uses a weighted least-squares technique followed by local bicubic spline interpolation. Another method suggested by Powell [41] makes use of triangulated piecewise quadratic surface fitting.

### 1.4 Regular Grid Techniques

For a given two-variable function $z=f(x, y)$ over a rectangular domain $R$ defined as $a \leqslant x \leqslant b, c \leqslant y \leqslant d$, the region of interest is discretised into a rectangular grid. This produces a subdivision of the region into smaller rectangles with four adjacent nodes of the grid as vertices. Denoting each node by (i,j), a matrix $[z(i, j)]$ can be defined. This regular grid provides an interface between the interpolation and contouring stages mentioned above, where the nodal values could be generated from the raw data at the interpolation stage.

Once the grid values of the function are produced, the drawing of contour lines can be accomplished. Some of the details of a particular contouring algorithm may depend on the output device used for drawing the lines, but most of the principles involved are device-independent. No matter what output device is employed, the solution could be achieved by two logical steps:-
(i) Computation of the coordinates of all the intersection points of each contour line and the edges of every rectangle.
(ii) Suitable linking of these points i.e. the organization of the drawing of all contour segments.

These require two types of interpolation:
(1) On the edges of each rectangle (i.e. step (i))
and (2) Within the rectangles themselves (i.e. step (ii)).
The contour tracing algorithms can be divided into two categories depending how the above techniques are employed:
(a) Grid-scan Techniques

In this, step (i) above is completely exhausted as a whole, by scanning the entire region to find the intersection points. Then, using some criterion, to be established, the points found in step (i) are linked during the execution of step (ii). The methods using this
technique require the storage of all intersection points. However, the storage of the entire matrix $z(i, j)$ can be avoided if all $m$ contours are treated simultaneously, but the problem of labelling the different curves may become difficult to program. The simplest method is to search for intersection points by exploring all the rectangles in a chosen order e.g. row by row, and join each intersection pair in every rectangle. This is very simple to program but is impracticable and timeconsuming. The slowness is due to the disjointed series of drawing movements involved and is exacerbated when a plotter is used. To minimize plotter pen motion, it is essential to plot each contour level continuously by ordering the intersection points in their natural sequence along the contour. Advantages of the method are rapid computation and simplicity of programming.

## (b) Contour-following Techniques

One 'entry' point of the contour line is located and the line is followed until it exits from the region. The two steps mentioned earlier are thus performed together; i.e. continuous generation of segments of a single contour line. There are accordingly, no difficulties in labelling the different lines, since they are found in succession. This technique requires the storage of the entire matrix $z(i, j)$, if the function is empirical, or not easily calculated, but storage of the intersection points is not needed. The procedure would terminate upon closure of the line or intersection with region boundaries. The logic of such a method is necessarily more complex than the grid-scan technique, and may therefore require additional computer overheads. The scheme involves some difficulties concerning the identification of different branches of the same contour level, usually without any common point. In order to follow all the branches, another search is necessary to find at least one point for each of them.

Briefly, the procedure commences with a scan until a contour crossing is located. The contour is then followed to completion, and the scan continued.
(i) Calculate and draw contour line segment in the rectangle where a crossing is located.
(ii) If the contour is closed or has reached the boundary, return to scan for the next contour crossing; else continue.
(iii) Determine into which of the adjoining rectangles the contour exits.: Return to (i) for this new rectangle.

A method of preventing the redrawing of a contour when another portion of it is encountered by the scan must be included in the logic. This has been accomplished by making use of an auxiliary array to identify previously contoured lines. The fundamental advantages of contourfollowing techniques are the increased speed of plotting and the ease of adding contour labels.

## 2. REVIEW OF SOME EXISTING METHODS

The purpose of this section is to outline briefly the main features of some existing contour drawing algorithms which are based on a regular grid and to highlight their differences. All these algorithms basically retain the two logical steps (Section 1.4) which are required to draw the contour lines but the approach in each step varies slightly from one algorithm to another. Most of the algorithms below substantially employ a contour-following technique.

### 2.1 Cottafava and Le Moli [36] 1969

This method incorporates a preliminary step, searching for the points of intersection with edges, but without calculating or storing the
coordinates of these points, (requiring only that the matrix $z(i, j)$ be stored). It finds the intersections by systematically exploring the edges of each rectangle. An edge, say, $A B$ of the rectangle is intersected by the contour line $z=c$ if $c$ lies between the function values of the two adjacent nodes, i.e. if

$$
\begin{equation*}
\left(Z_{A}-C\right) \cdot\left(Z_{B}-C\right) \leqslant 0 \tag{7.1}
\end{equation*}
$$

The results of this test are stored in the array $z(i, j)$ by recording for each pair of adjoining edges two binary variables specifying whether the corresponding intersections exist (Figure 7.6). In order to follow the contour line through the intersected edges, the algorithm has to accomplish the following two tasks:
(i) The behaviour of the line in the interior of the rectangle and in the adjacent ones must be examined. If an edge of a rectangle ( $i, j$ ) is intersected by a level line, then at least one other edge of the rectangle ( $i, j$ ) is intersected by the same contour line. A fixed order of edge inspection is used throughout the contour tracing. The following steps are made to follow the line:
(1) Search in the chosen order for a rectangle edge with a stored intersection.
(2) The stored intersection is cancelled to avoid meeting it again.
(3) The intersection coordinates are calculated by linear interpolation.
(4) The analysis continues for the rectangle adjacent to the intersected edge by repeating the same procedure from (1). In this way an ordered point set is constructed. The above procedure has examined the contour line from two viewpoints: the first is topological and involves verifying the existence of intersections and following the line; the second is numerical
and involves calculating the coordinates along the edges. Therefore, the contour is defined by a set of points on the edges.
(ii) The behaviour of the line with regard to the whole domain must also be examined. This is divided into two parts:
(1) Search for starting point from which to follow the contour line in (i). This is accomplished by scanning all the edges in the chosen order until a stored intersection is found and then following the branch until it stops. Scanning for new starting points on other branches is resumed from the interruption.
(2) Search for the stop point of a line. If the contour line is closed the stop point can be obtained as a consequence of step (2) in (i). The following convention can be established: a line stops when no intersection is found during execution of step (1) in (i) or the region boundary has been reached. In the latter case, further investigation of the adjacent rectangles external to this boundary is considered to be necessary. This method is quite general and allows one to follow any contour line.

### 2.2 Rothwell [37] 1972

This is a simplified version of the algorithm described above. Often, a generalised tracing procedure is unnecessary and time consuming when some properties of function $z(x, y)$ are known a priori, e.g. a level line has only one branch. In such cases, no preliminary operation is required and consequently the need for intersection storage is avoided. The procedure is as follows for a single contour line:
(i) Search the grid lines for a set of points for which $f(x, y)=c$. To do this, some form of approximation to the function has to be made between the nodes.
(ii) Having obtained the set of intersection points, join these points in some way to produce the contour, which in general will be in several discrete sections.

The four edges of the region are searched for the start of an open contour. The contour is then traced through the region until another edge is found. When all the open contours have been traced, the interior of the mesh is searched for closed contours which are drawn similarly. As observed earlier, no intersection storage was needed. However, such storage has the following advantages:
(1) It avoids finding an intersection repeatedly.
(2) It allows following of the contour line to be easily stopped.
(3) It allows different branches to be distinguished. The Cottafava and Le Moli step (ii) was required in order to identify different branches and the start and end of the contour line.

### 2.3 Robinson and Scarton [38] 1972

The procedure suggested here tackles the problem in slightly different form, but still retains the same structure. The object of this algorithm is to determine the possibility of finding more than one relative maximum occurring in $z(i, j)$, which could give rise to several disjoint and highly convoluted curves at a given contour leve1. This algorithm is set up to accomplish the following tasks:
(1) Examine the complete array $z(i, j)$ at each contour level so that all curves (branches) are found.
(2) Remember the position of all previously found and plotted lines so that the contours are not repeatedly redrawn.
(3) Find successive points along a contour line and keep them in their proper order so that complicated contours are drawn correctly.
(4) Have some means of deciding when all points in a contour have been found, and whether the curve is open or closed.

The algorithm consists mainly of two parts which are carried out simultaneously. First, the rectangles are scanned to find the start point of a contour line, and the position is found more accurately using quadratic polynomial approximation on the four neighbouring points. The line is then followed by threading through the adjacent rectangle. The quadratic approximation which is incorporated here allows the use of a coarser grid of points and gives much improved results over linear interpolation, particularly in the neighbourhood of saddle points.

The second part which is executed simultaneously is concerned with setting up a separate memory array. Each element of this integer array is identified with a rectangle by means of a simple code and contains all the necessary information concerning previously found contours. In particular, each element tells whether or not any contour points have been previously found along an edge of the corresponding rectangle. If any have been found, the total number of points and their locations are also stored. For each contour level, the whole memory array is initially set to indicate that no contour points have been found. Whenever a contour point is found along the edge of a rectangle, the corresponding element in the array is immediately recalculated to indicate this fact and to indicate on which side it was found. The information in the memory array is used for two purposes:
(1) If a point is found, while scanning a rectangle to find a beginning point of a contour line, then the memory is checked to see if the point has previously been found. If it has, the point is ignored and the scanning proceeds. In this way, a contour line is only found and drawn once.
(2) When extending a contour line from rectangle to rectangle, the array is checked for previously found points in the new rectangle. If such points are found, one of several alternatives will occur:
(a) the routine will first check all remaining sides of the new rectangle for contour points. If one can be found which has not been previously used, the contour line is simply extended in that direction.
(b) If no new points can be found, the algorithm checks to see if it is in the same rectangle as the beginning point of the line. If so the contour is assumed to be closed with the last point joining on to the first. If it is not the initial rectangle, the contour is assumed to be open, and is then extended backwards from the starting point until no further points can be found.

### 2.4 Mclain [39] 1974

This avoids the program difficulties of recording which parts of which line have already been drawn as discussed in the above algorithms. The approach here, is a more direct one than is usually adopted above, e.g. Cottafava and Le Moli use an elaborate procedure for threading the contours. This procedure works as follows:

The area under consideration is divided up into small rectangles within which the contour lines can be assumed to be uncomplicated, with no extremely sharp corners. Within each rectangle, to draw a contour line of height $c$ of a function $f(x, y)$, a zero of $f(x, y)-c=0$ is first found along one of the sides. The contour is then traced through the rectangle by a series of steps in one of eight directions ( $N, N E, E, S E, e t c$. ). This effectively results in further subdivision of the region into still
smaller rectangles called cells (Figure 7.7). The direction of the next step to be taken is chosen from one of three which depend on the direction of the previous step. The three steps $(1,2,3)$ to be considered are one in the same direction as the previous and each of the other two in a direction at $45^{\circ}$ to either side of this. For each point $1,2,3$ the absolute value of $f(x, y)-c$ is calculated and the point with minimum value found. This is the point chosen for the next step. This process is repeated until the contour line passes out of the rectangle. A record is kept of the $x$ and $y$ coordinates of the exit point. This is repeated for all roots along the side of the rectangle, first checking them against the current list of exit points. (If they are members of this list then they are not used as starting points for tracing the contour inside the current rectangle).

It may be observed that this algorithm fails to follow the contour line correctly in some circumstances. Consider for example a function which has a surface cross section shown in Figure 7.8, in the region of the indicated height. Applying the Mclain algorithm we have the choice of three function values - one on either side of the point where the true contour line crosses the surface i.e. (1), (3) and one (point (2)) in the bottom of a 'valley' to the right (Figure 7.8a). Since the algorithm only considers the absolute magnitude of the difference between the function values and contour line being drawn, point (2) is wrongly chosen. Once this step has been made, the algorithm may then have the choice of three values as in Figure 7.8b. Clearly point (1) is the point with smallest absolute difference and so will be chosen. Consequently, rather than the contour being traced, this valley is mistakenly followed.

A solution which has been suggested [44] to this problem requires that the algorithm must detect the point when it starts following the


FIGURE 7.6: Cottafava and Le Moli Method


FIGURE 7.7: Mclain Algorithm
valley and stops the tracing at this point. The other end of the contour is then found when the other roots along the side of the rectangle are examined, and the rest of the contour will be traced from that end. It is possible to accomplish this at the stage where the algorithm has to choose between the three values of $f(x, y)-c$ in the case when these values have the same sign. This involves quadratic interpolation of $f(x, y)-c$ on the points (1),(2),(3) with local coordinates $0,+1,-1$ respectively. A valley is detected if the roots of the quadratic are complex or if the absolute value of the smaller root is not sufficiently close to zero.

### 2.5 Sutcliffe [40] 1975

Basically, this algorithm adopts a similar strategy to that suggested by Mclain above. Both methods trace the portion of the contour line directly within each rectangle without the need to perform some preliminary operation or record information regarding the entire region. Furthermore, a common feature of both algorithms is that during the actual drawing process, each rectangle is effectively subdivided into smaller rectangles which are referred to as cells (Figure 7.9). Only those cells in the neighbourhood of the contour line are examined. However, the main difference between the algorithms relates to the way in which the contour is traced.
(i) The starting point of the contour line in this algorithm is taken as the middle of an interval which brackets the root of $f(x, y)-c=0$. Mclain, however, determines the starting point by finding more accurately the root of the equation $f(x, y)-c=0$ along one side of the rectangle.
(ii) The direction of the line segments to be drawn are determined according to the sign change of the function values at the corners of the cell. As a result a straight line is drawn to the middle of the cell side which shows a sign change of the


FIGURE 7.8a: Situation (showing choice of points) Where Error Will Occur

contour
height
FIGURE 7.8b: Typical Choice of Points After Error Has Occurred


FIGURE 7.9: Sutcliffe Algorithm


#### Abstract

function at its ends. Subsequently, this side is used as a baseline for the next cell and the process is repeated. This method avoids the problem which can arise in the Mclain algorithm where the contour is incorrectly traced in the neighbourhood of a valley.


## 3. DEGENERACY PROBLEM

Having reviewed some of the existing algorithms, it is essential to see how they tackle the problem of degeneracy that might occur. Degeneracy in this context is connected with the assumed function discretization, rather than any pathological function behaviour. The problem of degenerate nodes (corners) and degenerate cells described by Cottafava and Le Moli can be dealt with as follows.

### 3.1 Node Degeneracy

This arises when a contour line passes exactly through a grid point (Figure 7.10). Cottafava and Le Moli, Rothwell and Crane [45] all avoid this problem by scanning all the nodes and altering the associated values by a small amount so that the contour never passes through a node. Robinson and Scarton, on the other hand, use a slightly more sophisticated method (with more accurate root information) and make the next rectangle to be examined the one which is diagonally opposite the present one. However, Sutcliffe suggested that it is considerably easier to treat a zero value as if it is positive. This has the same effect as the scan above, as it can be simply achieved by writing a sign-finding function to produce only minus one (negative) or plus one (positive). . Thus degenerate corners are effectively avoided.

### 3.2 Cell Degeneracy

When a cell is intersected more than twice by the contour line, it is usually referred to as a degenerate cell (Figure 7.11). It should be noted that at most one intersection with each edge is assumed using test (7.1). Therefore a rectangular cell has no more than four intersections and in general there can be only two or four intersections. In the latter case, the problem of linking the four points arises. We may also observe the following:
(1) We can not be sure which configuration is the correct one when the function values are only known at the four vertices. However, some interpolation criterion is usually applied within the interior of the degenerate cells.
(2) In any degenerate cell, the function must have a minimum, maximum or saddle point. In the last case, the configuration in Figure 7.11 b is the correct one if the contour level equals the value of the function at the saddle point.
(3) In the complete domain there will be very few degenerate cells if (as is usually the case) the basic cell size is small.

The problem of degenerate cells is slightly more complex than in (3.1). Cottafava and Le Moli argue that degenerate cells occur very rarely and that, when they do, it is unlikely that the case in Figure 7.11b is the correct interpretation. Consequently, their method interprets the situation as either (a) or (c), choosing between them by the way the rectangle is examined. Rothwell similarly only looks at cases in Figure 7.11a and Figure 7.11c, finds the direction of the two possibilities and chooses the one where the direction changes the least from the previous step. He also comments that no strategy can be accurate in all places, due to lack of information, and this was the one he found to be the best. Sutcliffe adopts a similar strategy to that of Rothwell. The curve tracing


FIGURE 7.10: Degenerate Node ( $\mathrm{i}, \mathrm{j}$ )


FIGURE 7.11: Degenerate Cells
is continued in the same direction as before if a degenerate cell is encountered: i.e. if the previous step was normal to the cell side, then the next step is straight across the cell, or if the previous step was diagonally across the cell, the next step should be a continuation of that diagonal.

## 4. AN IMPROVED METHOD

### 4.1 Choice of the Interactive Method Used

After the preliminary study of the different methods available, an algorithm was developed and implemented for interactive use on the display terminal. As we have seen in the review, many methods for contour tracing are based on a rectangular grid but their approaches vary greatly. For example, the method by Cottafva and Le Moli requires a preliminary operation to be performed on the entire region under consideration before actually commencing the drawing of contour lines. This produces a set of ordered intersection points which are finally fitted by a smooth curve or simply joined by straight lines. On the other hand, the methods suggested by Mclain and Sutcliffe adopt a more direct approach, where the contour line is traced within each grid rectangle without the need to examine the whole region and the use of extra storage. These latter methods have a more localised approach which gives the terminal user a feel of control over the tracing. Therefore this type of method is more easily adopted for interactive use, Furthermore, it is also possible to provide the user with the ability to control some of the basic parameters such as the choice of the domain boundary, the smoothness of the line drawn, choice of contour level.... etc. Details of these parameter specifications become more apparent in the subsequent sections. The algorithm under discussion here belongs to this contour-following category of methods and represents an interactive refinement of the Mclain/Sutcliffe approach.

### 4.2 Description of the Algorithm

This algorithm traces the contour line $f(x, y)=c$ in a domain over which there exists a method of calculating the function at any given point in the $x y$-plane. The region under consideration is divided up into rectangles, each of which is defined by:

XMIN $\leqslant X \leqslant X M A X, \quad$ YMIN $\leqslant Y \leqslant$ YMAX
Each rectangle is further subdivided into small equilateral triangular cells during the tracing process.

Now consider the procedure which traces the portion of a given contour level within a single rectangle of the region.
(i) The four sides of the rectangle are examined in some chosen order, searching for an interval (Figure 7.12) of length 'step' which brackets the root of $f(x, y)-c=0$. The value of step is set equal to $1 / 2$ (xstep + ystep), where xstep and ystep can be specified interactively, by the user, preferably such that each rectangle is spanned by an integral number of xsteps or ysteps. [Note that other choices of 'step' could be used, e.g.
(a) $\min$ (xstep, ystep)
(b) xstep if an $x$ side of the rectangle is being examined ystep " " " " " " " "

The choice used here is more robust than (a) and is basically simpler to implement than (b)]. For each rectangle side, the search is performed by using repeated bisection and making use of the fact that the function will have opposite signs at either side of the root. Thus if a root is detected it will eventually be located to accuracy equal to 'step'. This accuracy is then improved further by (inverse) linear interpolation. Therefore, for the side on which x varies:

$$
\begin{equation*}
X_{\text {root }}=\frac{X_{R} \cdot F_{L}-X_{L} \cdot F_{R}}{F_{L}-F_{R}} \tag{7.2}
\end{equation*}
$$

Similarly, for the side on which $y$-varies:

$$
\begin{equation*}
Y_{\text {root }}=\frac{Y_{R} \cdot F_{L}-Y_{L} \cdot F_{R}}{F_{L}-F_{R}} \tag{7.3}
\end{equation*}
$$



Having determined the intersection point, the display beam is moved to this position to start tracing the line within the current rectangle. The interval 'step' is also used as starting baseline for the equilateral triangular cell (Figure 7.13a) which is constructed on this side.
(ii) Once the baseline has been determined the contour line would be followed by threading through the triangular partitioning which is constructed dynamically. The coordinate point of the third vertex ( $t$ ) is found simply from:-

$$
\left.\begin{array}{l}
x_{t}=\frac{x_{\ell}+x_{r}}{2}  \tag{7.4}\\
y_{t}=y_{\ell}+\frac{\sqrt{3}}{2} \text { xstep }
\end{array}\right\}
$$

where 'step' is the length of each side of the cell (Figure 7.13b).
The sign of $f(x, y)-c$ at point ' $t$ ' would determine uniquely which side of the cell the contour line will cut. This is simply indicated by a sign change along side '勿' or 'rt'. The crossing point is again calculated using linear interpolation, and a straight line segment is drawn from the previous beam position to this new point (p in Figure 7.14a). This side (rt, say) is now used as the baseline for the new cell 'tsr', where the coordinates of $s$ are determined by reflection of $\ell$ in the side tr (Figure 7.14b), i.e.

$$
\left.\begin{array}{l}
x_{s}=x_{r}+x_{t}-x_{\ell}  \tag{7.4}\\
y_{s}=y_{r}+y_{t}-y_{\ell}
\end{array}\right\}
$$



FIGURE 7.12: A Single Rectangle of the Region Showing the Interval Along One Side


FIGURE 7.13a: Construction of the Triangular Cell on the Baseline


FIGURE 7.13b: A Typical Triangular Cell


FIGURE 7.14a: Tracing the Contour Through the Triangular Cells;


FIGURE 7.14b: Reflection of $\ell$ in the Side $t_{t}$

The triangulation process is repeated until the edge of the rectangle is reached. This triangular subdivision with interpolation permits the lengths of the beam/plotter movements to be relatively large without any severe changes in direction. Thus a relatively smooth continuous contour line is produced within the rectangle.
(iii) When the edge of the rectangle is reached the point of exit is recorded. Each of the other sides of the rectangle are also searched for an interval containing the root which, when found, is checked against the list of recorded exit points for previously drawn contours in order to avoid tracing the line twice. If the root is not in the exit list then the program can enter the drawing loop as described above. Steps (i) and (ii) are repeated for each rectangle in the region. However, within the interactive environment provided, the user is able to select the appropriate rectangle from the mesh by means of the cross-hair cursor (see next section).

### 4.3 Advantages

This algorithm has achieved a number of improvements over those suggested by Mclain and Sutcliffe. These enhancements relate to the speed, smoothness and treatment of degeneracy and include the following:
(i) Degenerate cells are avoided. In the Sutcliffe method, with a rectangle cell (Figure 7.15) ambiguity arises when all four sides show a sign change of $f(x, y)-c$, and further decisions are required to resolve such ambiguity. On the other hand, with the triangular cells the side to which the contour line would be drawn is uniquely determined once the sign of the third vertex is found.

In general the use of elemental triangles ensures a unique piecewise planar approximation of $f(x, y)$. This is not so when rectangular cells are used.
(ii) There is substantial reduction in the number of function evaluations needed while tracing the line. To check this assertion, a second version of the algorithm was implemented using rectangular cells, and run with several test functions. A comparison of the triangular and rectangular version is given in Table 7.1 which shows in nearly all cases a difference in function evaluations of at least $20 \%$. Note further that the rectangular version also incorporates linear interpolation and would incur slightly fewer function evaluations than the Mclain/Sutcliffe method at the same level of discretization.

This improvement becomes more significant when each function evaluation requires a large amount of computation. The overall speed of the program operation is therefore noticeably improved, particularly when using a small machine and sharing resources with other users.
(iii) The degree of smoothness of contour lines becomes very important when graphic displays are used. The limited display area and screen relation require that the line drawn must be quite smooth in order to avoid overlapping contour lines which are close to each other. When the Sutcliffe algorithm was tried, it produced a curve with a noticeable ripple, which can be reduced only by making the cell size as small as possible, as the algorithm does not compute the intersection point accurately, but assumes that the mid-point is good enough. However since our method employs linear interpolation to compute the point of intersection, the resulting contour line has an acceptable smoothness even when the cell size is not particularly small.

The way in which the curve is traced directly by these methods is considered to be more efficient than using an interpolation scheme such as a higher degree polynomial interpolation for fitting a set of ordered points defining the contour line. Even the use of splines can cause some problem especially at segments of very high curvature, which can occur particularly in the neighbourhood of stationary points. Although splines can alleviate part of the problem, they can still run into difficulties near for example saddle points, if insufficient discretization has been used.

Function

1. $\left(y-x^{2}\right)^{2}+(1-x)^{2}$
2. $\left(y^{2}+x^{2}-1\right)^{2}+(x+y-1)^{2}$
3. $\exp -\left((x-5)^{2}+(y-5)^{2}\right)$
4. $\exp -\left((x+y-11)^{2}+(x-y)^{2} / 10\right)$
5. $8(4 y+7)^{3}-9(4 y+7)^{2}(2 x+3)+3(4 y+7)(2 x+3)$

Contour Level Region (Min \& Max X,Y)

| 30 | $(-1,2),(2,10)$ | 164 | 140 |
| :---: | :---: | :---: | :---: |
| 25 | $" \prime$ | 162 | 133 |
| 20 | $"$ | 160 | 138 |
| 15 | $"$ | 160 | 134 |
| 10 | $"$ | 156 | 130 |
| 5 | $"$ | 126 | 105 |
| 0.1302 | $(0.9,-0.4),(1.2,-0.2)$ | 60 | 56 |
| 0.1102 | $"$ | 54 | 46 |
| 0.0902 | $"$ | 42 | 34 |
| 0.0702 | $"$ | 32 | 24 |
| 0.0502 | $(5,3.5),(6.5,4.5)$ | 20 | 15 |
| 0.1 | $(6.5,4),(8,5)$ | 52 | 39 |
| 0.2 | $(0,-0.5),(6,0.5)$ | 36 | 27 |
| 500 |  | 78 | 62 |

TABLE 7.1: Comparison in the Number of Function Evaluations Using the Rectangular \& Triangular Subdivision Schemes
(iv) The Sutcliffe method assumes that the region under consideration should be divided into rectangles which are of a size such that the contour line only crosses any edge once. In practice, a situation could arise where for a chosen subdivision of the region, a contour line does cross an edge twice. This could happen for example in the neighbourhood of a saddle point (Figure 7.16). Further discretization would incur considerable overheads and greatly increase the computing cost. However, the present algorithm takes care of such cases without resorting to additional rootfinding procedures. (The usual sign test at the nodes of the rectangle would not yield any roots in this example). For example, as shown in Figure 7.16 , if the sides of rectangle $A(I, J)$ are intersected more than once, the algorithm keeps a record of the sides and traces the line inside this rectangle from each exit point.

## 5. THE INTERACTIVE DISPLAY PROGRAM

The algorithm developed here is made available to the user via the graphic display terminal (Tektronix 4010) in an interactive mode. Communication with the algorithm is maintained through a set of commands presented as menu options which comprise the user interface. Its aim is to provide the user with a direct and simple means of controlling the execution path of the algorithm in order to satisfy certain requirements. This kind of capability permits the user to take different courses of action while operating the program until the required result is obtained.

The final objective is to enable the user to draw a set of contour lines $f(x, y)=c$ of a given function $z=f(x, y)$ over a region, with interactive control of the following:
(1) The boundary of the region within which the set of contour lines are required.


FIGURE 7.15: Sign Changes at the Vertices


FIGURE 7.16: Contour Line Crosses at Least One Rectangle Side Twice
(2) The contour levels.
(3) The size of the rectangular grid and the triangular cells which subdivide each rectangle.
(4) The threading of the contour line from one rectangle to another, using the cross-hair cursor. The user can alternatively request this process to be completed automatically by the program
(5) The zoom window which defines the part of the display requiring magnification.

We now illustrate how the user can, with the aid of the keyboard and cross-hair cursor, control the algorithm to determine the boundary of the region for a given function. The program permits the user to start with two points which define the rectangular region. He would then be able to examine the region for any trace of the contour lines. If no trace is found, he could try a different set of boundaries and re-examine the region. The user could then iterate the above process until the boundary is satisfactorily defined for contouring.

The graphics terminal provides two modes of communication between the user and the tracing algorithm. The first is the keyboard through which the user can enter boundary coordinates, grid information and the various contour heights. The second means of communication is the crosshair cursor, which is used to select options from the menu and to identify appropriate rectangles for the algorithm. When an option is picked up, the program would invoke the appropriate routine which may prompt the user for keyboard entry and subsequent injection of the new parameter values into the algorithm.

Essentially, the interactive program consists of two main display modes, each having a particular role during the user session at the terminal. The two displays are:

## (i) Contour parameter entry:

The ICT program is activated by typing the program name 'CONTOUR' at the terminal. As soon as the program runs, the screen would be cleared and the first display (Figure 7.17) appears. This contains short introductory remarks and two separate menus, each containing a set of options.
(a) Program control menu.

This has three options whose functions are mainly concerned with controlling the display image and the logic flow in the program. These options are similar to those mentioned in the IDF package (Chapter 6).
(b) Contour parameter menu.

When a parameter option is selected, the user would be prompted by a message (appearing at the bottom of the screen), and the program waits for the user to make a keyboard entry in response to this message. If the options marked with an asterisk (*) are not selected, the program will set their values by default.
(1) The height of the contour line initially to be traced $\rightarrow+$ CON. LEVEL can be specified at this display. However, this entry. could be postponed until the next display, so selection of this option is not compulsory. The function displayed in these photographs (Figures 7.18-7.19) is

$$
z=\left(y-x^{2}\right)^{2}+(1-x)^{2}
$$

(Rosenbrock's 'Banana' function).
(2) This is a compulsory item which the user must select $\rightarrow+$ REGION in order to define the boundary of the region. The
coordinates ( $X_{\min }, Y_{\min }$ and $X_{\max }, Y_{\max }$ ) of the rectangular region are then keyed in response to a program prompt on the screen.


This has the effect of moving a window over the region within which the function can be evaluated and its contours displayed. The viewport size is fixed at $750 \times 750$ screen rasters.
(3) The discretization of the region into a rectangular grid is controlled through this option by specifying the size of each side of the rectangle (X-WIDTH and Y-WIDTH). The program allows an upper limit of $30 \times 30$ rectangles into which the region could be subdivided. In most cases this fine discretization of the region is unnecessary, since the algorithm further discretizes each rectangle into smaller triangles whose minimum size is constrained by screen resolution. However, the program has a built-in default action if the user bypasses the above option. This default subdivides the region into $15 \times 15$ squares of side 50 rasters, representing an adequate discretization.
(4) This option would effectively control the size of the $\rightarrow+X-Y$ STEP triangle and hence the smoothness of the contour line. The size of X or Y -step must be chosen such that

```
                                    STEP = WIDTH/<integer>
```

The default setting in this case is

STEP $=$ WIDTH $/ 10$
(5) The grid generated would be drawn on the next display $\rightarrow+$ DISP.GRD (Figure 7.18), if the user has picked this option. The mesh would provide the user with some visual aid when interactively tracing the contour. In addition, it would be useful for reading the coordinates of the grid nodes when trying, for example, to re-define the region boundary.

## (ii) Contour lines display:

This is the next main display generated by the program and $\rightarrow+$ CON. LEVEL represents the final outcome of the algorithm. Two menus appear on the screen, containing some options which appeared (and were described) in the previous display. The bottom menu effectively allows the user to vary the contour level in order to display the set of contours associated with the function in the region under consideration. Also, if necessary, the user can vary the degree of smoothness. (Figure 7.20b).

The contour lines could be displayed in two different ways:
(1) Interactively.
+CURSOR

This option is usually used in conjunction with the grid net drawn as in Figure 7.18 where the tracing of the contours is carried out interactively by means of the cursor. Here, the cursor is used as a pointing device for identifying the appropriate rectangle within which the contour (if it exists) is to be drawn. This is accomplished by positioning the cross-hair cursor intersection point anywhere inside the rectangle and by pressing any


FIGURE 7.17: Contour Parameter Entry Display


FIGURE 7.18: Tracing the Contour Line by Means of the Cross-llair Cursor

rıuURE 7.19: Contour Display of Rosenbrock's finction

$$
f(x)=\left(y-x^{2}\right)^{2}+(1-x)^{2}
$$

key, say the space bar. If, however, the contour does not pass through this rectangle, the cursor control will be immediately returned back to the user and he could try again. Once a rectangle is found to contain a portion of the contour line, the extrapolation of the line becomes easy and natural, as the user can recognise visually the direction of the contour. This scheme provides the user with the capability for searching through a given region until a trace of the line is found, and if necessary adjusting the boundary. It would also give the user the flexibility to stop tracing a particular contour level and proceed to the next one.
(2) Automatically.

The algorithm would thread the contour line through the rectangles of the region, when this option is picked up. The two examples shown in Figure 7.19 and Figure 7.20a are produced using this option. The contour lines represent the following two explicit functions:

$$
\begin{aligned}
& f(x, y)=\left(y-x^{2}\right)^{2}+(1-x)^{2} \\
& f(x, y)=\left(y^{2}+x^{2}-1\right)^{2}+(y+x-1)^{2} \ldots-- \text { Fig. }-\ldots .19
\end{aligned}
$$

As can be seen, the present algorithm produces visually smooth curves, and (in Figure 7.19) copes with sharp corners. It is also clear from the example in Figure 7.21 that this algorithm has successfully overcome the situation where the contour crosses the edge of the rectangle twice, without the need to discretize the region further. This situation has risen in Figure 7.21 near the saddle point at the contour level 0.1102 . The use of this option is recommended when the user wishes to produce the final display of the set of contours, perhaps followed by photographs or other forms of hardcopy. Finally, an additional menu option ' + ZOOM' is provided,


FIGURE 7.20a: Contour Display of the Function $f(x)=\left(y^{2}+x^{2}-1\right)^{2}+(y+x+1)^{2}$


FIGURE 7.20b: Same as Fig.7.20a with Additional Contour Level and Variation of $x / y$ Step


FIGURE 7.21: Grid Lines Superimposed Showing the Contour Level .1102 (near the saddle point) Crossing the Rectangular Edge Twice

allowing the user to blow up a selected portion of the region in order to gain a closer view of that portion (Figure 7.22). The zoomed area is determined by pointing (with the cursor) at two rectangles situated at opposite corners of the window.

## 6. PROGRAM IMPLEMENTATION (Interactive Contour Iracing)

The ICT program was implemented on the PDP 11/40 minicomputer operating under the UNIX system. The program is entirely written in Fortran IV, uses the graphic software package LIGHT and consists of two sets of subroutines controlled by a main segment.
(i) The contouring algorithm subroutines (Appendix 3.1)
(ii) The user interface subroutines (Appendix 3.2)

The first set consists of four main subroutines together with three subsidary ones, forming the entire code of the main algorithm. The general flowcharts are shown in Figure 7.23 giving the logic flow of the algorithm. The second set consists mainly of two interactive display routines which organise the menus and handle the user interaction. These routines in turn call nine other subsidary subroutines used for setting up the prompting messages, interpreting user input and computing the appropriate scaling factors.

The program design is highly modular, due firstly to the division of the two completely separate tasks the program has to perform, and secondly, the subroutine nature which enables future modification to be incorporated easily.

In order to create the executable version of the program the user is required to include a Fortran function subroutine which returns the value of the function at any given point ( $\mathrm{X}, \mathrm{Y}$ ). For example, if the function under investigation has an explicit form such as the one given
in the examples above, the function subroutine would be
FUNCTION $F(X, Y)$

$$
F=(X * X+Y * Y-1) * * 2+(X+Y-1) * * 2
$$

RETURN
END
However, if the required function has values specified at some arbitrary data points, then the expressipn in the above example will be replaced by a body of code which would evaluate the function at a given point. Note that whatever form the body of the function would have, the function name used is $F(X, Y)$, this being the actual name called by the ICT program.

Having, specified the function evaluation routine, the user is provided with the 'shell' file which he could run to generate the executable module of the program 'CONTOUR'. The following UNIX keyboard commands are used for this purpose

| \% SH JCLTRI | ; Create the contour program |
| :--- | :--- |
| \% CONTOUR | ; Run ICT program |

Another version (Appendix 3.3) of the algorithm was implemented for comparison purposes, and uses rectangular cell subdivisions while tracing the contour line. For this the UNIX commands are
\% SH JCLREC
\% CONTOUR


FIGURE 7.23: General Flowchart of the Contour Tracing Algorithm


## Chapter 8

## TRIANGULAR MESH GENERATION - TMG

1. INTRODUCTION
2. RITZ FINITE-DIFFERENCE EQUATION
3. ITERATIVE SOLUTION OF THE RITZ EQUATION
4. AUTOMATIC MESH GENERATION
4.1 Non-Uniform Triangulation
4.2 Logical Diagram and the Boundary Input Data Format
5. TMG - PROGRAM
5.1 Description of the Batch Program and its I/O Data
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## 1. INTRODUCTION

A generalised finite element algorithm was proposed [46] for the solution of elliptic boundary-value problems using non-uniform triangular mesh systems.

The above work is mainly concerned with triangulations in the plane with particular reference to the numerical solution of the Poisson equation, and the subsequent graphic display of the generated mesh and its associated equipotential lines.

The program developed by Cardew [46] is an adaptation of Winslow's [47] for generating non-uniform triangulation with selective zoning in different areas. The versatility with which the problem boundaries can be represented in the mesh is one important feature; further, there is the unique facility for grading the mesh to suit special areas in the plane of solution.

A wide variety of problems in mathematical physics can be formulated as the classical problem of solving the Poisson or Laplace equation. For example, the distribution of electric flux in a general, anisotropic medium is modelled by Poisson's equation:

$$
\begin{equation*}
\operatorname{Div}(\varepsilon \nabla \phi)=-\rho \tag{8.1}
\end{equation*}
$$

where $\varepsilon$ is the permittivity, and $\rho$ is the electric field charge density (source density). The boundary conditions usually have two forms:
and

$$
\left.\begin{array}{ll}
\phi=\phi_{i}(x, y) & \text { 'Dirichlet conditions' }  \tag{8.2}\\
\underline{\mathrm{n}} \cdot(\varepsilon \nabla \phi)=0 & \text { 'Neumann conditions' }
\end{array}\right\}
$$

where $\underline{n}$ is the normal to the boundary at $(x, y)$. Another example is Laplace's equation for the electric field in conducting media:

$$
\begin{equation*}
\operatorname{Div}(\sigma \nabla \phi)=0 \tag{8.3}
\end{equation*}
$$

where $\sigma$ is the conductivity.

If $\varepsilon$ is constant, equation (8.1) may be rewritten in terms of operator $\nabla^{2}$ as:

$$
\begin{equation*}
\nabla^{2} \phi=\rho^{\prime} \tag{8.4}
\end{equation*}
$$

The usual classical approach to solving the boundary-value problem by the method of finite-differences is to discretize the region into a uniform rectangular grid (Figure 8.1).

Using Taylor series for obtaining the approximations to the operator $\nabla^{2}$ in the above, the equation $\nabla^{2} u=\rho$ may be replaced by the five point difference equation

$$
\begin{equation*}
\left[u_{1}+\alpha^{2} u_{2}+u_{3}+\alpha^{2} u_{4}-2\left(\alpha^{2}+1\right) u_{0}\right]+o\left(h^{2}\right)=\rho \alpha^{2} h^{2} \tag{8.5}
\end{equation*}
$$

where $h_{x}=h$ and $h_{y}=\alpha$. More accurate formulae can be found through the use of more complex molecules; for example, a nine-point approximation on a square net involves an $O\left(h^{4}\right)$ local truncation error. However, using uniform equilateral triangulation with a seven-point molecule, the error term is also $0\left(h^{4}\right)$. With orthogonal $X$ and $Y$ axes the 'equilateral net' is defined by two intersecting sets of lines (Figure 8.2), the $L$ and $K$ lines, corresponding to the rows and columns of a square net. The logical origin of the triangulation is situated at the bottom-left corner and the convention is that there should always exist two neighbouring triangles at this point. If the spacing between adjacent points on the same row is $h$, then for the equilateral net the spacing between adjacent rows is $\alpha \mathrm{h}$ where $\alpha=\sqrt{3 / 2}$. For $\alpha \neq \sqrt{3 / 2}$ the net will still be topologically equivalent to the equilateral net. Using Taylor expansions about 0 (Figure 8.3), the seven-point difference approximation to $\nabla^{2} u=\rho$ on a equilateral grid may be written as:

$$
\begin{equation*}
-\sum_{i=1}^{6} u_{i}+6 u_{0}+3 \frac{h^{2}}{2} \rho=\frac{9 h^{4}}{64}\left[\nabla^{2} \rho\right]+0\left(h^{4}\right) \tag{8.6}
\end{equation*}
$$



FIGURE 8.1: Five-Point Difference Molecule


FIGURE 8.2: Triangular Network and Its Basic Elements (Row and Column)

A uniform mesh is inefficient when the problem requires a more accurate solution in some regions than in others, since the smaller spacing required leads to wasteful computation over the less important regions. The use of an irregular mesh is therefore desirable. Moreover, with this flexibility it would be possible to arrange that mesh points lie precisely on the boundary.

In the following sections we state the basic assumptions, difference equations and methods of solution used in the development of the program. Finally, a full account will be given with supporting examples of how to run the program and the subsequent interactive display program for observing the result.

## 2. RITZ FINITE-DIFFERENCE EQUATIONS

The basic assumptions of the finite-difference method made here are:
(i) the boundaries and interfaces of the region R are approximated by straight-line segments.
(ii) the region is triangulated
(iii) the values of $\phi$ are defined at triangle vertices, and $\phi$ is assumed to vary linearly over each triangle.
(iv) $\varepsilon$ and $\rho$ are assumed to be constant over each triangle. The type of triangulation used here is topologically regular; i.e. it is topologically equivalent to an equilateral triangle array in which six triangles meet at every interior mesh point. Since any polygonal region can be triangulated, the method can be applied to regions of any shape and will produce a mesh in which boundaries and interfaces lie entirely on mesh lines. This causes a considerable simplification of boundary conditions.

Consider the numerical solution [48] of a generalised form of Poisson's equation within a two-dimensional domain R with given boundary condition. In particular, consider the second order, linear elliptic partial differential equation expressed as

$$
\begin{equation*}
-\frac{\partial}{\partial x}\left(a \frac{\partial \phi}{\partial x}\right)-\frac{\partial}{\partial y}\left(c \frac{\partial \phi}{\partial y}\right)+k \phi=f \tag{8.7}
\end{equation*}
$$

where $(x, y) \in R, a(x, y), c(x, y)>0$.
The boundary condition is

$$
\begin{equation*}
\alpha \phi+\frac{\partial \phi}{\partial n}=\beta \tag{8.8}
\end{equation*}
$$

where n is the direction of the normal derivative and $\alpha, \beta$ are piecewise continuous functions along the exterior closed boundary of $R$. The solution $\phi, k$ and $f$ are assumed to be continuous within $R$.

A two-dimensional finite element may be defined as a polygonal subdomain of the domain $R$ of a boundary-value problem. The potential within this subdomain is approximated by a polynomial interpolated through the $n$ vertices of the subdomain. The order of this interpolated polynomial is determined by n , e.g. a 'linear element' is a triangular subdomain in which the potential is approximated by a linear polynomial. The approximate solution $u$ of the partial differential equation is represented by a polynomial function (usually linear) over each element with matching conditions on the inter-element boundaries. Each polynomial is defined by a number of coefficients or by the function value and its derivatives at certain points. Then by use of a classical result from the calculus of variations, we know that the solution of (8.7) is given by the function which minimizes the integral

$$
\begin{array}{r}
I(v)=\frac{1}{2} \iint_{R}\left\{a\left(\frac{\partial v}{\partial x}\right)^{2}+c\left(\frac{\partial v}{\partial y}\right)^{2}+k v^{2}-2 f v\right\} d x d y \\
+\int_{\Gamma}\left(\beta v+\frac{1}{2} \alpha v^{2}\right) d s \tag{8.9}
\end{array}
$$

over all functions with at least piecewise continuous first derivatives
which satisfy the same boundary conditions as $\phi$. If we substitute $u$ for $v$ in the integral (8.9), I(u) becomes the sum of the integrals of the polynomials over the finite elements within the domain $R$.

Given a triangulation of the region $R$ based on the rows and columns shown in Figure 8.2, over which $u$ is required at each triangle vertex, we can derive a set of difference equations from (8.9) by using the Ritz varational method. Basically, we express $u$ as the continuous piecewise linear sum

$$
\begin{equation*}
u=\sum_{i} u_{i} \alpha_{i}(x, y) \tag{8.10}
\end{equation*}
$$

where $u_{i}$ is the value of $u$ at the mesh point $\left(x_{i}, y_{i}\right)$ and $\alpha_{i}(x, y)$ is a pyramid function with the properties:
(i) $\alpha_{i}\left(x_{i}, y_{i}\right)=1$
(ii) $\alpha_{i}(x, y)=0$ for any point ( $x, y$ ) lying on, or beyond the hexagonal perimeter 123456, (Figure 8.3).
(iii) $\alpha_{i}$ varies linearly in each adjacent triangle.

We minimize $I(u)$ by setting $\frac{\partial I}{\partial u}=0$ at each mesh point, thus obtaining a system of linear equations in the parameter $u_{i}$ of the form:

$$
\begin{equation*}
\sum_{q=1}^{6} \omega_{p q}\left(u_{q}-u_{p}\right)+b_{p}=0 \tag{8.11}
\end{equation*}
$$

for all points $P_{\varepsilon R}$ where $b_{p}$ is a combination of boundary and source terms and can be expressed as,

$$
\begin{equation*}
b_{p}=\sum_{T_{q}}^{6} \rho_{T_{q}} A_{q} \tag{8.12}
\end{equation*}
$$

$A_{q}$ is the area of the triangle $T_{q}$ (Figure 8.4) and $\omega_{p q}$ is called the coupling coefficient between the points $P$ and $Q$ and depends on the geometric and material properties of the two triangles ( $\mathrm{T}_{\mathrm{q}+1}, \mathrm{~T}_{\mathrm{q}-1}$ ) having PQ as a common side. It could be shown that


FIGURE 8.3: The Computational Molecule


FIGURE 8.4: Couplingof Triangular Elements

$$
\begin{equation*}
\omega_{p q}=\frac{1}{2}\left(\varepsilon_{T} \cos \theta_{q+1}+\varepsilon_{T} \cos _{q-1}{ }_{q-1}\right) \tag{8.13}
\end{equation*}
$$

Equation (8.11) is the Ritz finite-difference equation using a general seven-point molecule.

If the triangulation is uniform and equilateral and if the source term $\rho$ is piecewise constant over the region of solution, equation (8.11) reduces to the seven-point regular hexagonal equation (8.6) derived from the Taylor series.

Complete generality is present in the Ritz approximation (8.11) in the following respects:
(i) the mesh may vary in any manner, though it must remain topologically regular.
(ii) the source function $\rho$ can vary in a piecewise manner between subregions of the problem.
(iii) the coefficient functions may also vary in a piecewise manner between regions.

If the mesh is approximately equilateral in certain zones, then the discretization error there will be $O\left(\mathrm{~h}^{4}\right)$. Clearly, there is more computational effort involved with using (8.11) than with the fivepoint or seven-point equation resulting from Taylor series. This would appear to be the disadvantage of using a non-uniform net. However, the prime motive in employing (8.11) resides in the simplification introduced in the treatment of:
(a) Composite material media
(b) Complex boundaries
and (c) Singular field points, where the mesh spacing may be reduced around such points.

## 3. ITERATIVE SOLUTION OF THE RITZ EQUATION

The linear system of equations generated by repeatedly applying equation (8.11) to all mesh points can be expressed as:

$$
\begin{equation*}
\underline{\mathrm{Au}}=\underline{\mathrm{b}} \tag{8.14}
\end{equation*}
$$

Since each point of the network is coupled only to its neighbouring points A is a large order, sparse, positive definite, symmetric matrix containing the coupling coefficients $\omega_{p q}$ derived from (8.13) as elements banded around the main diagonal. In general the more complex the finite-difference molecule is, the wider the bandwidth becomes. The vector $\underline{u}$ is the required solution at the mesh points and $\underline{b}$ is a vector whose elements are combinations of boundary and source terms.

Methods for inverting the system of linear equations may broadly be classified as either Direct or Indirect. In the direct method a finite number of computational steps are required for evaluating the solution, whilst in the indirect method an initial 'guess' is made for the solution which is subsequently improved upon in successive iterations. These cycles are terminated when the changes in $u$ from one cycle to the next are negligibly small (convergence).

The iterative methods of solution are almost invariably much simpler to program and often preferred to direct methods because they can cope with the sparsity of the matrix more effectively. Only the non-zero coefficients are used in the numerical algorithm involved and thus the computer storage usage is minimal. Further, the problem of rounding error growth is avoided. The iterative scheme used in this program involves splitting the matrix A in the following manner

$$
\begin{equation*}
\underline{A}=\underline{D}-\underline{L}-\underline{U} \tag{8.15}
\end{equation*}
$$

where $\underline{D}$ is a diagonal matrix and $\underline{L}$ and $\underline{U}$ are strictly lower and upper triangular matrices respectively. Thus, rewriting the linear
system of equation (8.14) as

$$
\begin{equation*}
(\underline{D}-\underline{L}) \underline{u}=\underline{U} \underline{u}+\underline{b} \tag{8.16}
\end{equation*}
$$

and introducing the iteration counter $n$, the Gauss-Seidel iterative scheme can be defined:

$$
\begin{equation*}
\underline{u}^{(\mathrm{n}+1)}=\underline{D}^{-1}\left(\underline{\mathrm{~L}}_{\underline{\mathrm{u}}}{ }^{(\mathrm{n}+1)}+\underline{U}_{\underline{\mathrm{u}}}{ }^{(\mathrm{n})}+\underline{b}\right) \tag{8.17}
\end{equation*}
$$

The convergence of this method can be improved by introducing the parameter $\omega$ into (8.17), which would result in the well known successive over-relaxation (S.0.R.) method as

$$
\begin{equation*}
\underline{u}^{(n+1)}=\underline{u}^{(n)}+\omega \underline{D}^{-1}\left(\underline{L} \underline{u}^{(n+1)}+\underline{u}^{(n)}-\underline{D} \underline{u}^{(n)}+\underline{b}\right) \tag{8.18}
\end{equation*}
$$

or alternatively,

$$
\begin{equation*}
\underline{u}^{(n+1)}=\underline{\underline{L}}_{\omega} \underline{u}^{(n)}+\underline{b}_{\omega} \tag{8.19}
\end{equation*}
$$

where $\omega$ is the over-relaxation parameter chosen to accelerate the convergence and

$$
\underline{L}_{\omega}=(\underline{D}-\omega \underline{L})^{-1}\{\omega \underline{U}+(1-\omega) \underline{D}\}
$$

The matrix is usually generated from a simple computational molecule (Figure 8.3) rather than stored directly in the computer memory. Thus, only the approximations $\underline{u}^{(n)}$ are stored (requiring one vector of storage) and a mechanism (program) simulates the molecule's traverse of the network in some order during each iteration. For regular points of the net, the coupling coefficients are just stored once while for irregular or boundary points, each point is tagged and the associated coupling coefficients stored as lists.

By choosing a suitable local ordering such as in Figure 8.3, and returning to equation (8.11) the corresponding S.O.R. formula is

$$
\begin{equation*}
u_{p}^{(n+1)}=u_{p}^{(n)}+\omega\left\{\left(\sum_{q=1}^{6} \omega_{p q} u_{q}^{(n, n+1)}+b_{p}\right) / \sum_{q=1}^{6} \omega_{p q}-u_{p}^{(n)}\right\} \tag{8.20}
\end{equation*}
$$

In each iteration cycle, the mesh points are swept in sequence with the $(n+1)^{\text {th }}$ iterate replacing the $n^{\text {th }}$ iterative component at $u_{p}$ as soon as it is calculated. For symmetric, positive definite matrices,
the method is known to converge. The main point of interest is the choice of the over-relaxation factor $\omega$ which minimises the spectral radius $\rho\left(\mathrm{L}_{\omega}\right)$ and thus maximises the convergence rate. The optimum value of $\omega$ is

$$
\begin{equation*}
\omega_{\mathrm{opt}}=\frac{2}{1+\sqrt{\left(1-\lambda^{2}\right)^{\frac{1}{2}}}} \tag{8.21}
\end{equation*}
$$

where $\lambda$ is the spectral radius $\rho\left(\underline{D}^{-1}(\underline{L}+\underline{U})\right)$ of the related Jacobi operator. For a given $\omega$ (less than $\omega_{\text {opt }}$ ), we can express $\lambda$ as

$$
\begin{equation*}
\lambda=\frac{\omega+\mu\left(\mathrm{L}_{\omega}\right)-1}{\omega \sqrt{\mu\left(\mathrm{~L}_{\omega}\right)}} \tag{8.22}
\end{equation*}
$$

where $\mu\left(L_{\omega}\right)=\frac{\left\|\delta^{(n+1)}\right\|}{\left\|\delta^{(n)}\right\|}=\left(\frac{\sum_{i=1}^{n}\left(\delta_{i}^{(n+1)}\right)^{2}}{\sum\left(\delta_{i}^{(n)}\right)^{2}}\right)^{\frac{1}{2}}$
The error norm $\|\delta\|$ can be evaluated by forming the sum of the squares of the residuals (errors) at all mesh points on the completion of each iteration.

An under-relaxation parameter $\beta$ is introduced in the actual formulae used in the program. This would prevent $\omega_{\text {opt }}$ from changing too rapidly from one iteration to the next [47]. This is desirable since large changes in the value of $\omega_{\text {opt }}$ may seriously perturb the spectral radius $\mu\left(L_{\omega}\right)$. The final formula used for the automatic estimation of the $\omega_{\text {opt }}$ is

$$
\begin{equation*}
\omega_{o p t}=\beta\left(\frac{2}{1+\sqrt{1-\lambda^{2}}}\right)+(1-\beta) \omega_{o p t},-\beta \rho_{0} \tag{8.23}
\end{equation*}
$$

where $\omega_{\text {opt }}$, is the previous value of $\omega_{\text {opt }}$ and $\rho_{0}$ is a further damping term.

## 4. AUTOMATIC MESH GENERATION

### 4.1 Non-uniform triangulation

The generation of the non-uniform triangulation is performed through three main steps:
(i) Generation of boundary tags and coordinates along all external and interface boundaries described in the input data.

A tagging word ( 24 bits) is allocated to each mesh point (Figure 8.5a) in which is packed certain information relating to the disposition of the point w.r.t. the boundaries. The structure of this word is given by:
(1) VTU and VTL are the region numbers of upper and lower cells associated with the point I (Figure 8.5b).
(2) C is the boundary code, where $\mathrm{C}=0$ if I is not on a boundary C=2 if $I$ is on a boundary that is to be relaxed $\mathrm{C}=3$ if I is on a non-relaxed boundary.
(3) S is a side tag with the following interpretation:
$\mathrm{S}=0$ if neither of the VU,VL lie along boundaries
S=1 if VU lies on a boundary
S=2 if VL lies on a boundary
$\mathrm{S}=3$ if both VU,VL lie on a boundary.
(ii) Assignment of region numbers to all cells.

On completion of the first step (boundary points), a scan is made along each row of the mesh and the following action is performed: when the first point on this row is reached having a vertical side tag or the first point on the row above having a lower side tag, all following cells lying between the current mesh row and the one above are tagged with the current region number up to the next 'tagged side'; no further
tagging is performed until another side is found. Whenever a point is found with a side tag then this tag is erased.
(iii) Generation of internal mesh coordinates.

In order to reflect the relative importance and material properties of each region, the mesh for a given problem should also be composed of regions which can be zoned to different average mesh spacings, with the mesh spacing in each region varying smoothly. Thus the coordinates of the unspecified internal points are found through solving a 'pseudopotential' problem [47]. That is, the zoning problem is formulated as a potential problem, with the mesh lines playing the role of equipotentials. The triangular mesh generated is composed of three sets of straight lines (Figure 8.6) intersecting each other at $60^{\circ}$, of which any two sets are sufficient to define the mesh.

Let one of these two sets be associated with a function $\phi(x, y)$ and the other with a function $\psi(x, y)$, each satisfying the Laplace equations

$$
\left.\begin{array}{l}
\nabla^{2} \phi=0  \tag{8.24}\\
\nabla^{2} \psi=0
\end{array}\right\}
$$

over each region with boundary conditions determined by the interface and boundary zoning. Solving (8.24), the intersecting 'equipotentials' $\phi=$ constant and $\psi=$ constant, together with the third set drawn through the intersection points, form the desired triangle mesh. By inverting equations (8.24) and writing them in terms of $x(\phi, \psi)$ and $y(\phi, \psi)$, we find that (8.24) are transformed into inverse Laplace equations:

$$
\left.\begin{array}{rl}
\alpha x_{\phi \phi}-2 \beta x_{\phi \psi}+\gamma x_{\psi \psi} & =0  \tag{8.25}\\
\alpha y_{\phi \phi}-2 \beta y_{\phi \psi} & +y_{\psi \psi}=0
\end{array}\right\}
$$

where $\alpha=x^{2}{ }_{\psi}+y^{2}{ }_{\psi}, \quad \beta=x_{\phi} x_{\psi}+y_{\phi} y_{\psi}$ and $\gamma=x^{2}{ }_{\phi}+y^{2}{ }_{\phi}$. With meshes of a mild non-uniformity, equations (8.25) can be simplified, into a linear form i.e.


FIGURE 8.5a: The Tag Word


FIGURE 8.5b: A Typical Cell Configuration with Point I


FIGURE 8.6: Pseudo-Equipotential Lines

$$
\left.\begin{array}{c}
x_{\phi \phi}+x_{\psi \psi}=0  \tag{8.26}\\
y_{\phi \phi}+y_{\psi \psi}=0
\end{array}\right\}
$$

The difference equations corresponding to these two equations are:

$$
\left.\begin{array}{lll}
\operatorname{case}(a): & x_{0}=\frac{1}{6} \sum_{i=1}^{6} x_{i}, & y_{0}=\frac{1}{6} \sum_{i=1}^{6} y_{i} \\
\operatorname{case}(b): & x_{0}=\frac{1}{4} \sum_{i=1}^{4} x_{i}, & y_{0}=\frac{1}{4} \sum_{i=1}^{4} y_{i} \tag{8.27}
\end{array}\right\}
$$

i.e. $x_{0}, y_{0}$ are simple averages of neighbouring coordinates. The type of zoning (case a or b) is specified in the input data for a region by a parameter $z=1$ or 2 . The above two difference equations are solved by the method of successive point over-relaxation in an analogous nammer to that of the Ritz equation (8.11).

### 4.2 Logical Diagram and the Boundary Input Data Format

A useful apparatus for arranging the disposition of boundary points is the logical diagram. The concept of the logical mapping is useful in preparing the way for a description of the method of choosing the mesh layout for non-uniform triangulations.

This section is intended to outline briefly the use of the logical diagram and the format for the description of the boundary points to define the region geometry which is input to the program. A typical example is shown in Figure 8.7. The rules in the preparation of this diagram are as follows:
(i) Choose an equilateral net of sufficient degree of fineness to suit the problem in hand.
(ii) Represent any straight boundary section along any desirable logical direction in this mesh. The length and orientation of this path will determine both the number of mesh points and the zoning of the mesh.


FIGURE 8.7: Logical Diagram
(iii) Simulate any 'Reflection' (Neumman) condition for symmetry by introducing a row of 'Dummy' cells on one side of the section, e.g. FED of Figure 8.7. When the external boundaries of the region do not fit precisely a rectangular outline, an imaginary rectangular boundary is marked to complete the region.
(iv) Curved sections (AF in Figure 8.7) can be represented by using the 'logical arc' facility provided in the program. The centre of the arc is defined in the input data by the following quantities $L_{0}, K_{0}, \theta_{0}$ where ( $L_{0}, K_{0}$ ) is the intersection point at the ' $K$ ' line and ' $L$ ' line through 0 and $\theta_{0}$ is given as
$\theta_{0}=\frac{\text { no. of mesh sides along the logical slant line }}{\text { Total no. of mesh sides along the logical arc }}$
(v) Code $\mathrm{C}=\mathrm{O}$ for any internal point,
$\mathrm{C}=1$ is used for any boundary point which is to be relaxed,
$\mathrm{C}=2$ for a boundary point which is not to be relaxed.

The format for the description of each boundary point is ( $\ell, k, y$, $x, \phi, C$ ), where $\ell$ and $k$ are row and column numbers in the range ( $0, \mathrm{LMAX}$ and $0, \mathrm{KMAX}), y$ and $x$ are the coordinates of the boundary point, $\phi$ is the potential at that point and C is the code.

The boundary input data to the problem is arranged in the following manner:

If a boundary has the same constant code and potential ( $\phi, C$ ) for a large number of consecutive points in the input data, then rather than repeating the code and potential at each point it would be useful to signal only 'changes' in parameters. A convention was adopted in which the first point to be presented for a boundary is preceded by a section with a code of unity and potential of zero. With this convention it is
only necessary to define $(\ell, k, y, x)$ at this point. If the section following the first point has the same code and potential then it is only necessary to give the coordinate of the point at the end of this section; and so on for the remaining points. However, if at any stage the type or potential of the intermediate points (or the end points) of a following section changes, then prior to giving the coordinate of the next point, one introduces an alphabetic sentinel 'B' followed by the quantities $C_{I}, C_{E}, \phi_{E}$ where:
$C_{I}$ : is the code for the intermediate points $C_{E}$ : is the code for the end point $\phi_{E}$ : is the potential at this point

The following example illustrates the use of this scheme for . defining the geometry of a given region. In region 2 (Figure 8.7) the input data are defined by the following card images:

$$
\text { 1st card: } 2 Z_{2} \varepsilon_{2} \rho_{2}
$$

This card specifies the properties of region 2 where $\varepsilon_{2}, \rho_{2}$ are the region constants and $Z_{2}$ the zoning code ( 1 or 2 , see section 4.1 (iii)).

2nd and subsequent cards:

$$
\ell_{E} k_{E} y_{E} x_{E} B 12 \phi_{2} \ell_{C} k_{C} y_{C} x_{C} B 22 \phi_{2} \ell_{D} k_{D} y_{D} x_{D} G
$$

Here the potential along ED is assumed zero. There is no need to repeat the first point to indicate closure of the region: the terminator $G$ is used to signal this to the program. The data describing the arc AF of region 1 consists of an alphabetic sentinel followed by the first point, the centre and the last point i.e.

$$
{ }^{A \ell}{ }_{F} k_{F} y_{F} x_{F}^{\ell} 0^{k_{0}} 0^{\theta} 0^{\ell} A^{k_{A}} y_{A} x_{A}
$$

A routine called GEOMETRY reads in the cards defining the geometry, in a free format so that spacing between the separate items on a card is
immaterial and so also is the number of items on the card. The only restriction on the layout of the data is that there should be at least two space characters between individual fields.

## 5. THE TMG-PROGRAM

The program was originally implemented on the ICL 1904 S and the plotting part was performed off-line on an incremental plotter using the ICL graphic library routine HGPLOTT. Due to the limited computing resources available with a PDP $11 / 40$ and the large amount of computing time required by the TMG program, it was not posssible to implement a fully interactive version of TMG on this machine. As a result the program is partitioned into two separate jobs.
(i) the numerical computation is performed in Batch mode on the ICL machine,
(ii) the plotting part is then carried out on the PDP 11/40 machine using the LIGHT package on the graphic display and allowing the user a limited amount of interaction with the displayed picture.

### 5.1 Description of the Batch Program and Its I/O Data

This program would carry out all the number crunching part of the process of generating the triangular mesh. It consists of the master or steering segment 'POISSON' and a number of subroutines performing the various computational tasks required by the program (see program listing Appendix 4.1). The main course of action required in the processing of each task is illustrated in the block flowchart of Figure 8.8. A number of distinct problems can be treated in one execution of this program. For each problem the user must include the input data in the following order:

(a) Control data: these consist of five control cards carrying the following information in free format:

Card I Number of problem.
Card II Title for the current problem.
Card III (1) a logical parameter (PLOTMESH) which assumes the value 'True' or 'False' according as the mesh lines are to be displayed or not.
(2) a count (NEQPTL) of the number of equipotential lines to be displayed.

Card IV (1) number of regions in the geometrical description of the problem (NREG).
(2) material and geometrical properties to be ascribed to each region. This is usually fixed in number (equal to 4) e.g. region number, zoning code, permittivity, charge density.

Card V The logical size of the mesh, KMAX, LMAX followed by the mesh parity.
(b) Geometric data: this consists of an unspecified number of cards, each containing the material and geometric properties of each region followed by the boundary points and their potentials. The type of information and the data format of this input is fully described in section 4.2 above.

The numerical results are dispatched to two types of output media:
(i) line printer output which includes print out of some intermediate results regarding the acceleration factor and convergence rate together with coordinates of mesh points and their associated potentials for each row.
(ii) paper tape punch contains the coordinates of the mesh points and the equipotential line segments. The distinction between mesh and equipotential data is made by generating a code for each type. All mesh lines are tagged with code 1 , whilst equipotential lines are tagged with code $2,3,4 \ldots$ depending on the level. This paper tape data will be employed in the display program (see next section).

The main subroutines of the program depicted by each block of the flowchart of Figure 8.8 are:-
(a) INPUT.

Reads in the number of mesh rows and columns and the material and geometric data. The latter is read in free format by the routine GEOMETRY.
(b) TOPLGY.

Steers the processing of the geometric input data in the following manner. Between each pair of boundary points an entry is made to the routine BSET which interpolates the coordinates of the intermediate points and ascribe tags to these points and the last point of each section. The subroutine CODE is used by TOPLGY for examining any changes in the type of boundary code. If a marker denoting a curved (arc) section is encountered then entries are made to ARCSET and ARC, which in turn distribute the intermediate points by equal increments in polar angle.

Following the generation of a region boundary, an entry is made to SETREGION for the tagging of internal mesh cells associated with this region. TOPLGY continues with the next region until finally all regions of the problem have been completely defined.
(c) MESHRELXN.

The linear difference equations (8.27) are simultaneously solved by successive point over-relaxation. At each point of the relaxation sweep a check is made that the current point does not lie within a dummy region or on any boundary. If the point is internal then the region in which it lies is determined by extraction of the region tag for the upper cell at this point.
(d) PARAM.

This controls the process of evaluation of the coupling coefficients and source terms. Since the couplings and sources are linear combinations of the basic geometric and material properties within the cells, it will be obvious that a given coupling coefficient can be assembled by the contributions from cells at different stages of the sweep. All the evaluations are performed by the subroutine TERMS.
(e) RELX.

The system of linear Ritz difference equations (8.11) are solved by successive point over-relaxation. Initially, a starting value is chosen for the acceleration factor $\omega_{\text {opt }}$ (1.5) and the iteration counter ITN is set to zero. Following this a sweep is performed through all the points of successive rows. The sweep commences at the point ( 0,0 ) and proceeds to the end of the first row; this is repeated for the next row and so on. When the mesh sweep is completed the iteration counter ITN is updated and an entry is made to the routine SOR for a re-estimate of $\omega_{\text {opt }}$ equation (8.23).
(f) The pre-plotting routine PLOTT.

This routine organises and controls the generation of mesh and equipotential lines. The fundamental routines employed are respectively

LINET and EQUPLT. Initially, a sweep is made through the mesh and the maximum and minimum coordinates (used for setting the display viewport later) and potentials are determined. The required equipotential points are evaluated. Following this, a forward sweep is made for all points on the first row ( $\mathrm{L}=0$ ), and the coordinates of the mesh lines are set off to be punched on the paper tape for later use with the display program. Still on the same row, a cellwise, backward sweep is performed; for each cell the vertical sides are also sent to the paper tape punch. These sweeps are repeated for all subsequent rows.

### 5.2 The Display Program

This essentially displays the triangular mesh and the equipotential lines of the problem region from the output paper tape data generated by the Batch program. It also provides a limited interactive capability with the display picture through the selection of menu options.

Prior to running this program, the data on the paper tape must be read in and stored on disc file the name of which is specified by the user. For this purpose a small C-program (Appendix 4.2) was written for reading the paper tape data produced by the ICL machine and storing it on disc file on the PDP $11 / 40$ machine. The program also removes unwanted characters from the data (e.g. null character, carriage return, parity bits) so that the format of the data stored is acceptable by UNIX-Fortran. In order to read the data, the paper tape is mounted on the PDP $11 / 40$ paper tape reader and the following UNIX PIPE command [19] is used:

## \% PRTAPE</DEV/PR>AFILE

(A pipe is simply a way to connect the output of one program to the input of another program, so the two run as a sequence of processes).

Here, the PRTAPE is the executable C-program module, and AFILE is the name of the disc file containing the final data.

The display program (Appendix 4.2) consists of the main segment and three subroutines responsible for the plotting and controlling of various displays which include:
(i) Triangular mesh of the problem region.
(ii) Equipotential lines with or without the mesh.
(iii) Zooming part of the display picture.

The display program is generated by running the existing shell file: $\%$ SH JCL
where JCL is the shell file containing all necessary UNIX command for compiling and linking the program with the LIGHT library subroutines. The executable module is named 'FINITE'; so the user would be required next to type in:

## \%. FINITE

and the program will run under his control.
The sequence of displays the user would encounter while running the program is best illustrated by means of an actual example. The problem region investigated in this example is concerned with the field distribution of an electron gun with its geometry and boundary potentials given in Figure 8.9. As soon as the program runs, the display image shown in Figure 8.10 appears on the screen. This display contains a short introductory remark followed by instructions for the user to make keyboard entries. The input data required by the program are:
(1) Data file name
(2) The limit of the data to be mapped on to the prespecified viewport (i.e. minimum and maximum of $x, y$ values).

x boundary points

|  | $\ell, \mathrm{k}, \mathrm{y}, \mathrm{x}$ | $\phi$ | Cards | Input cards |
| :---: | :---: | :---: | :---: | :---: |
| 1. | 0,0,-25,-5 | 1500 | 1. | B $221500000-25-520025-5$ |
| 2. | 20,0,25,-5 | 1500 | 2. | 20325 O В 2215251331.50 |
| 3. | 20,3,25,0 | 1500 | 3. |  |
| 4. | 13,3,1.5,0 | 1525 | 4. |  |
| 5. | 13,11,2.5,8 | 1525 | 5. |  |
| 6. | 15,12,3.83,13.67 | 1525 | 6. | $202725650627-2565$ |
| 7. | 15,18,6.5,25 | 1525 | 7. | 0 25-25 62 В $21214752^{2} 25-1762$ |
| 8. | 18,19,10.17,37.33 | 1525 | 8. | $219-10.17$ 37.33 |
| 9. | 18,25,17,62 | 1525 | 9. |  |
| 10. | 20,25,25,62 | 1500 | 10. |  |
| 11. | 20,27,25,65 | 1500 | 11. | B $22150003-250 \mathrm{G}$ |
| 12. | 0,27,-25,65 | 1500 |  |  |
| 13. | 0,25,-25,62 | 1500 |  |  |
| 14. | 2,25,-17,62 | 1475 |  |  |
| 15. | 2,19,-10.17,37.33 | 1475 |  |  |
| 16. | 5,18,-6.5,25 | 1475 |  |  |
| 17. | 5, 12,-3.83, 13.67 | 1475 |  |  |
| 18. | 7,11,-2.5,8 | 1475 |  |  |
| 19. | 7,3,-1.5,0 | 1475 |  |  |
| 20. | 0,3,-2.5,0 | 1500 |  |  |

Most of the menu options used thraughout this program have the same function as those described in previous applications (e.g. IDF package).

Once the user has completed the necessary keyboard entries, he can proceed to the ' + NEXT' display. This is the main display of the program, and enables him to perform the following actions, through the selection of menu options provided:
(a) When this option is picked up the triangular mesh generated would be displayed (Figure 8.11). Effectively the program reads the stored data one line at a time and draws the mesh. When the entire mesh is displayed, the program returns control to the user by the appearance of the cross-hair cursor; then the user may wish to proceed to take the next action.

While the program reads the data, it stores the equipotential line coordinates on an array list so as to avoid the time-consuming operation of reading the data file again.
(b) This option will cause the equipotential line to be $\rightarrow$ +EQUIP'L displayed. If the user wishes to plot these lines separately (Figure 8.12) he can do so by selecting the option ' + RESTART' (which clears the screen) prior to this option. On the other hand, if combined displays of both the mesh and equipotential lines (Figure 8.13) are needed then the user would select this option directly.
(c) This option allows a portion of the region to be $\rightarrow+200 \mathrm{M}$ enlarged. For example, Figure 8.14 shows that a zooned window is defined (by using the cursor and


1
FIGURE 8.10: Introductory Display


FIGURE 8.11: Triangular Mesh of the 'Electron Gun' Problem Region


FIGURE 8.12: Equipotential Lines


FIGURE 8.13: Triangular Mesh Superimposed By The Equipotential Lines
selecting any two opposite corners of the rectangle)
and Figure 8.15 shows the blown-up display of the window selected.

Another example is also shown in Figure 8.16 and Figure 8.17 of the field distribution in the region between two charged parallel conductors of finite width but infinite lengths.


FIGURE 8.14: Choosing the Zooming Window


FIGURE 8.15: The Zoomed Portion of the Triangular Mesh


FIGURE 8.16: Triangular Mesh of the Two Charged Parallel Conductors


FIGURE 8.17: Same as the Above Example with Pquipotentia? Lines

## Chapter 9

## SUMMARY AND CONCLUSIONS

An initial study was made of the current state of hardware/software facilities in interactive computer graphics. This was a useful exercise in its own right, but was also motivated by the limited graphics support which was locally available at the start of this work. General-purpose graphics packages such as GINO-F were being marketed commercially but usually required too many resources for our mini-computer environment. It was apparent that in-house graphics software was needed to support a wide range of computer graphics applications, typically in the area of scientific computing, and to form the basis for developing a graphics laboratory. Consequently, the graphics software package LIGHT was then implemented as a set of Fortran-callable library subroutines, capable of driving the graphics display (Tektronix 4010) from the PDP 11/40 under UNIX time-sharing system.

The scope of LIGHT was extended beyond the basic requirements to include three-dimensional transformations, simple perspective projection, menu operation and text handling capabilities ; it was also made accessible from the GT42 refresh display operating in Emulator mode. At the same time the total core requirements of the LIGHT library were designed to be less than 8 K words.

Fortran was chosen because graphics systems are likely to be used for scientific and engineering applications. The use of Fortran also makes the package (and the application programs) portable except for the 'back end' which contains some assembly code and the terminal dependent routines. Because of the modular design of the package and the inclusion of the back end code in a separate module, the only code modification which would be needed in a different configuration is performed on this module alone.

The Tektronix 4010 cross-hair cursor and keyboard can be used efficiently as input devices. LIGHT has provided various input graphics
capabilities activated from the keyboard or by a cursor position with single-character command or through menu selection, each of which can be transmitted to the computer program during execution. Thus the application program can be written to incorporate such user interaction in a natural manner.

Window/Viewport transformations have been introduced to ease the problem of coordinate system mapping. Graphic displays are generated by defining a coordinate system, scales, labelling and text generation. The scales are determined either automatically in order to fit a selected portion of the data or explicitly by the user. Where the data falls outside the screen viewport, a clipping (scissoring) routine is used to exclude all such extraneous elements.

A variety of three-dimensional transformations have also been implemented, including rotation and perspective projection. The generation and storage of transformation matrices by LIGHT effectively offers the application programmer a system of transformation control.

The present capability of the graphic software can be extended to include hidden line removal and graphical data structure facilities; these could be valuable assets in a computer graphics laboratory. It would also be possible to implement a display-file based version of LIGHT. Here, the display file would not of course be used to refresh the display. However, it can serve a useful purpose in permitting part of the picture to be manipulated. Furthermore, some of the facilities provided by LIGHT can be easily incorporated into the locally available Picture Book package [11] used in conjunction with the GT42 either directly (transformation routines) or with slight modification (e.g. menu handling routines).

LIGHT has shown its usefulness in a range of applications and for a wide variety of users. There is a good case for such a general purpose
and efficient graphic software package which is accessible from a high-level language. The following application areas were exploited during the course of this work and made extensive use of LIGHT in an interactive environment.
(i) Interpolatory Data Fitting - IDF

This provides a user interface for solving a certain class of data-fitting problems and is oriented toward the non-programmer. The 'easy-to-use' design of the interaction embodied in IDF, and the inclusion of the ability to specify various end conditions give it the combination of simplicity and effectiveness necessary to a useful interactive problem-solving device. It consists of two separate packages (Explicit and Parameteric), each containing a number of overlayed modules and a library of numerical algorithms featuring mainly cubic spline interpolation methods. This set of algorithms has been enhanced and adapted for interactive use. Additionally, the user is offered a command menu, through which he would have full control over the execution path of the package, with on-line help and a large number of utility options for thorough examination of the interpolated curve.

Several cubic splines were generated using spline algorithms for a variety of boundary conditions. This smooth interpolatory curve fitting system can serve a useful purpose for creating and displaying graphical information. When straight line vectors are used to connect the interpolated points, rapid and relatively inexpensive graphical output can be produced and modified interactively by the user. The controlled end condition specifications allow easier control over the final shape of the curve. However, this technique does not rival the methods of interactive curve design developed by Bezier [49] and Riesenfeld [50]. However, when a few known data points are available,
and control of the curve through these points is desirable, the above type of algorithm can be useful.

Some possible extensions and improvements that are possible in the IDF system are:
(1) Extending the localised polynomial method to incorporate different weighting functions and the ability to select these weights interactively.
(2) The addition of further algorithms, for example least squares cubic spline approximation.
(3) For users with 'noisy' data the suggestion made in (2) could be developed further into a separate Generalised Data Fitting package having the same philosophy and structure as IDF but incorporating for example least squares and minimax algorithms.
(4) The addition of more display modes that would aid user interpretation of the results. For example, one could display the first and second derivatives at the data points and at prescribed intermediate points.

## (ii) Interactive Contour Tracing - ICT

The basis of this program is a tracing algorithm for drawing the contour $f(x, y)=$ constant in a region over which there is a method of calculating the function. After some preliminary study of the available methods based on a regular mesh, an algorithm was developed from those which used a more localised tracing technique. This algorithn was adapted for interactive use on a display terminal, allowing the user to trace contours automatically or interactively. Some fundamental modifications were incorporated, providing improvements in smoothness, efficiency and the treatment of degeneracy.

The generality and capability of this program can be extended further by providing the user with the option of tracing a set of contour lines for a given set of arbitrary points (or grid points). This would obviously require the inclusion of a routine which would estimate the function value of a given point ( $x, y$ ) from the set of data points specified initially by the user.

## (iii) Triangular Mesh Generation - TMG

This program provides a graphics display and limited interactive facilities for the triangular mesh generation algorithm developed previously in conjunction with the solution of the Laplace or Poisson partial differential equation in an arbitrary two-dimensional region. Some development work was needed for modifying the original ICL 1900 program and its output before subsequent interactive use on the PDP 11/40. This provides a display of the triangulated region, and the equipotential lines using interpolation techniques on the solution values at the mesh nodes. It also allows zooming into any subregion of interest.

If more computing power were available on the PDP $11 / 40$, the program would be entirely run on this machine with a fully interactive capability built into it. For example, it would then be possible to input and edit the geometric data describing the boundary of the region by means of cursor and keyboard entries. Furthermore, intermediate computational results could be displayed on request for examination by the user.

A number of other application programs were successfully developed by other users using LIGHT, for example:
(1) Displays for critical path analysis in an interactive graphics environment by Hargrave [51].
(2) Computer simulation of boundary layer growth and wake propagation on compressor cascade by Jamani [52].

The published photographs of the screen were produced from a domestic camera. However, a hardcopy device such as a pen-plotter would be a useful asset to the system.

For the modest investment in terms of both money and software development, the graphics systems developed in the course of this work have provided successful and useful tools for the average user. Moreover, they represent the basis of a graphics laboratory which could be used for future innovation in this field and its applications.

The original aim of this project was centred on the data-fitting application of graphics. However, it will be observed that the scope of the work which is reported in this thesis has expanded considerably from the original idea. Further, it seems natural to suggest that there are other classes of numerical problem which can also benefit from the same kind of treatment. These may include:
(1) Partial differential equations. Research on interactive graphical systems to represent the solution of partial differential equations would be very rewarding. Regions could be displayed and modified interactively and the corresponding results indicated graphically as well.
(2) Numerical linear algebra. This area exemplifies problems whose intermediate results can be graphically presented for quick comprehension by the users. The condition of the coefficient matrix involved in the solution of systems of linear equations is a critical factor in the proficiency of various algorithms to obtain a satisfactory solution. There are various ways to examine the condition of a matrix.

Geometrical consideration yields a hyperellipsoid whose axes are inversely proportional to the eigenvalues of the matrix. Thus an elongated hyperellipsoid indicates bad conditioning whereas a near hypersphere indicates a well conditioned matrix. It is felt that an on-line user will be able to recognise and interpret a graphically presented hyperellipsoid more readily than a list of numbers.

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## APPENDICES

## APPENDIX 1

LIGHT - PROGRAM LISTING

```
%
    *******************
    * AffErmuR 1.1 *
    x,4*************)
/
GIDGHTUNOX JRIEEFACE ROUTTMES
% -............................................--...........................-
%
/
THES hOHSTME WOULD OUTHUT A SITGLE CHFBACTEFE TO THE GEFEES&
```



```
-bloel OCHAKR.
#OLOEL FETRN
OCHAE:-
    VALUE SLOCATIOR OF FETUFN vALUE
    .+2 'FOLNTEK TO EXECUTDON CODE:
    MOU 2(K3%,F゙L /FOLMTEF TO HFG. LIST
    AMS $2ッK1 FFORMTS AT THE 2NG WORH OF THE INTEGEK
    MON F1,CHAK : SEET CHAF ALKESS
    MON $1.PKO SET FLLEE DESCRIFTOK
    gYS gTTYETATUS /GET TERMJNAL. STATUS
    MOW ETATUS+4,OMGDE: SAVE OLIS MOLE: OF TTY
    gye sIGNAL;2;ExTT1 /CONTHOL C
    ESC $26,STATUS+4 /RHAFACTEFE NOUE
    EIS $40.STAlUS+4 /SET KAW MODE
    MON क1.FO
    SYS STTYSTATUS /SET TERMIMAL HODE
    HOU $1,NO /FILE DESCIPTOR 1 FOK WFITE
    EYS WFITE /WRITE CHAK
CHA&: O /EUFFEK AlOKESS
    MOU RO.VALUE SEEUNM MO.OF CHAFE WRITTEN
EXIT1: KOU OMODE,STATUSH& /EACK TO DLD TEKNEMAL STATUS
    MON &1,F0
    gYS STTY:STATUS
    JMF RETFW
.ESS
VALUE: . =n+2 /GFACE FOK RETUNN VALUE (FN TMTEGEK)
ETATUS: :=n+6 TERMIMAL STATUS #FGG̈.
OMODE: m=n+2 AOLD TTY ETGTUS MOLE
/
/THIS FOUTINE INFUT A SINGLEE CHAK FFUM TENTROINA 4OLO
/FOFTFAAN CALL:- ICHAK=INCHAR(X) WHEFE X LS DUAIMY'FGFAGETEK
-GLOBL INCHAKR. GEFLNITIUN DF ENTEY
.GLOBL RETFN /REFEFENKE OF RETURW
TNCHARE:
    VALIUE
    .+2
    MOU 4O.HO
    GYS GTTYBETATUS
    HOU STATUS+4,OMODE
    SIE SIGNALFOAEXITL
    EIS $40.STATUS+4
    ELC $10.STATUS+
    MON $O,FO
    sye ETTY:STATus
    MOU $O.FO
    GYE REAL
    VALUEET2
    1.
    MOU $0.FOO
        senter fodmT
        ADOCATJON OF RETURN VALUE
        FOQNTEE TO EXECUTLON CODES
        /SET FILE DESRRTFTOK
        GET TERMINAL ETATUS(nODE)
        GAVE OLII TEGGMMAL MOLE
        COMTKDL &
        GET IT IO RAW TOLE
        SWLTCH ECHOOHF
        FFILE DESLRIFTOK
        SSET YFEFMLMAL RODE
        /FHSS FILEN DESOKIFTOK
        KEAD A UHARMLTEF
        /ADQRESS OF CHAR JUST FEML
        /NO. OF CHAR FEtmb
```

```
EXIT1: MON UMODE,ETATUS+4 /FESET TO ENTKY TGY MODE
    SVS ETTYBETATUS SET TEFMINAL. MODE AS BEFUFE
    JMF fEETEN /RETURN TO HAIN FROLEELUKE
.gse
VALUEE: = = + 4 /CONTAIM CHAEN JUST EEAL
STATUS: :=.+6 /STATUS WURD
OMOBE: =.+2 /OLD TYY MDDE
GEET UF CFOSS-HAIRS CURCOFR ROUTINE
    .GLOEL CUFSON. GNTKY NAME
    .GLOEL HETFN!/FETUKN
CUKSOM::
    VALUE:
    .+2
    MOV RO,SAVER3 /SAUE REGLSTER 3
    MOU $1,FO /SET FLLE LEGCRMFTOK
    SYS GTTY;STATUS /GET THE CUFRENY TEFMTMNLL STATUS
    MOU STATUS+4,OMODE /SAVE TEFMINAL MOLESS
    EIC $3e,STATUS+4 ISET TEFIMIMaLL MODES
    ELS $40.STATUS+4 TSES FAW HODE
    MOU $1,RO
    SYE STTYFSTATUS SSET THE NEW TERMIMAL STATUS
    MOU 生,*O
    SYS WRITE;SETCURSOK;2 /SET UF CROSS HAIF CURSOK
    HOU $5,F゙5 /EET COUNT TO FIVE
1: MOV $1,FOO
    GYS FEAD;GETCUKOOUK;1 FREALH A CHAK
    TET (F3)+ /SET AKGUUMEMT LIST FUIRTEF
    MOV (F3),N1
    TET (F1)+
    MOUE GETCUKSOF, (N1) FFUT AKGUMETT LIST
    SOE FS,1B / LOOF F゙TVE TIMES
    MOU , $1,RO
    SYS FEAD:GETCURSORFI /INFUT FTVE CHARACTERS
    MOU $I,R1
    SYS WRITEHHOMEFG /GET ALFHA CUKSOK HOME
    MOU OMODE,STATUS+4 SEESTORE ORDGITAL MODE
    MOU $1,FO
    gys stTYESTATUS
    MOU SAVEKZ,FZ3 FKESTOKE REGLSTER
    MMF KETFN
    DATA , ,
SETCURSOR:
    #EYTE 27.,26. FOW SETTIRA UF CURSOK
HOME: .EYTE 29.,55.,12%.,32.,64.,31:/FGK FETUKLNG TO ALFHA MGLE
    .ESE
VALUE:: "=.+4
STGTLS: .=n+6 'WOKK EFFLLE TO SAVE TEKMTMAL ST.
OMODE: =.+2 GWOKKC SFACE TO SAVE TEFMINAL MODE
SAVEFZ: = =%+2 /WOKK BFACE TO SAVE EZ
GETCURSOR:
    **+2 ,HOLLE INFUT CHAKALTEK
'
/QUERLAY FFROGRAMS MODULES
    .GLOBL OVLAY.
    -GLOEL RETRN
ONLAY::
    VAl.UEE
    .+2
    MON KZッF1 - FASSING FARARLTER
```

```
    TST (fi)+
    MOV (R1)rMAME /FGSS THE NUMES FHLLE
    MOU (FD),AEGS SGET AKGUNENT TO NAME
    SYS EXEC TOUERLAY THE CALLING FGOCESS
MANE:: O
            AROG%
            JNFF RE:\FW
- [ata
HFGE: O%O
.ESE
UALUUE: .="+2
%
f REMOUES A NAMED FTLEE FROM CUKKENY GXNECTOR%
    -GLOEL FLFM.
    .GLOEL FETFir
FL_RIM:
    VAlUE:
    .+2
    MOU RE,FL /FASSING THE FOAFAMETEK
    TST (F1)+
    MOU (FIN),NAME
    SYS UNLIFKK /REMONE NANEDO FLLEE FROM CUFKENT
                                    MIEELTOFY
NAME: O
    MMF RETRN
.ESS
VALUE: m=n+2
```

```
C
*******************
* afremdIX 1.2 *
C
******************
C
C INITIANIEATION FUUTINES
C
C
C
C
C ***********IHITIALISE THE GISFLAY IGEUICE***********************
C
SUEROUTJNE TXOFFEN
C THIS SETS THE DEFAULT VALUES FOK DJSFLAY AREA \& BCALES OF
C X,Y.YHIS ALEO DOES SUME INTTIALISAYLUN CONCEEMLMG SOREFN
C COOFDOINATES & MENOS OFERAT IONE.
S N.B.THIS GUERUUTINE MUET BF ISSUED AS YHE FTRST CRLL ON THE
C F'ACKGGE.
COMMOM/AREEA/SCALE:(12)
COMMON/TOFLHC/IXORIG.IYOKIG
COMMON/NMOFF'H/MODE,LFOS,CHFOS
COMMON/MATRIX/CTM(4,4),TM(4,4)
INTEGER CHFOS
C SET UF COOKMS.OF TOF L.NH CHARACTEF & ECALLING
    SCALE (1)=0
    SCALE (2)=0
    SCALE (5)=0
    SCALE (7)=0
    SCALE (4)=780
    SCALEE (B)=7830
    SCflLE (10)=780
    SCALE (12):=780
    SCALE (3)=1023
    SCALE (G)=1023
    SCALE (9) =1023
    SCALE(11)=1023
C. EET UF MENU OKLGIN & CHAFACTEFK LINE FUSITIOM
    IXOFIG=0
    IYOKIG=780
    MODE ==1
    LFOS=0 ?
    CHFOS=0
C SET TKANGFONMATIOK'MATHIX TO UNET MATFIX
    CALL UNITY(CTM)
    GALL UHITY(TM)
    FETUK\
    END
C
C*******:********EFASE THE SCTEET\****************************
C
        SUBFOUTIFE TXCLEF
C THIS CLEARS THE SCREEN
C OUTFUT TWO ASCII CHAKACTEES
C ERASE SCFEEN AND RETUFIN TO ALFHA MODE
    S-OCHAK(27)
C GOES HOME
    S=CLCHAF(12)
    RETUF'N
    EMM
C
```



```
C.
```


## SUBROUTIUE TXUFRT (XO,YO,X1,Y1)

C THIS LIMIT THE EXTENT OF A DISFLAY TO A SELECTEN AFEA
C OF THE SCREEN. IF FARAMETERS OUTSIDE AREA CALLL IS IGNUFEV. COMMON/AFEA/SCALE (12)
C CHECK FOR ANY UIOLETION
IF (XO.LT.O.OR.X1.GT. 1023.OK.XO.GE.X1.OR.YO.LT.O.OK.Y1.GT.7EO
$\star$ .OR.YO.GE.Y1) GOTO 1
SCALE (1) $=X 0$
SCALE (2) $=$ YO
SCALE (3) =X1
SCALE (4) $=$ Y1
SCALE (11) $=\times 1-\times 0$
SCALE (12) $=Y 1-Y 0$
FETUKN
1 CALL CUFFOS (200.,500.)
CALL ALFHMD
CALL MESSAG("DRAWING OFF THE SFECIFIED UIEWFURT"~) FETURN E.ND

## C


C
SUBFOUTINE TXWIND ( $X 0, Y 0, X 1, Y 1$ )
C THE SCALES AFE SET SLLCH THAT XO TO X IS MAF'FED GNTO X-AXIS
C OF UEFINED SEREEN AKEAッSIMILARLY WITH YO TO YI
COMMON/AFEA/SCALE (12)
IF (XO.GE.X1.OR.YO.GE.Y1) GOTO 1
SCALE (5) $=\times 0$
SCALE ( 6 ) $=\mathrm{X} 1$
SCALE (7) $=$ YO
SCALE $(8)=Y 1$
SCALE (9) $=\times 1-\times 0$
SCALE (10) $=\mathrm{Y} 1-\mathrm{YO}$
FETUKN
1 CALL CUFFOS (200.,500.)
CALL AL_FHME
CALL HESSSAG ("DFAWING OFF THE SFECIFTED WINDOW"*)
FETUFW
END
 C

SUBFOUTINE ALFHMD
C DUTFUT A SINGLEE ASCII CHAFACTEF
S=OCHAR (31)
RETURN
END
C
C***************FUT THE TERMINAL IN GRAFHIC MOUE $* * * * * * * * * * * * *$
C
SUBROUTITEE GRFHMD
COMMON/KEEMXY/IXX,IYY
C RETURN TO PREUIOUS FOSITOIN AND SET UISFLAY TO GFAFHIC MODE CALL UFLUT $(0, I X X, I Y Y)$
FETUFN
END
C.

C
C
C
C FOINT AND LINE DRAWING ROUTINES
C
c
C
C

C
SUBFROUTIME UFLOT (I,IX,IY)
C THIS IS DEVICE UEFENDENT ROUTINE
COMMON/OLDBT/IOLDBT (4)
IIMENSIDN IVZ (4)
C CONUERT COORDINATES $X$ Y INTO 4 BYTES INFORMATION
$I X 1=I X / 32$
$I Y 1=I Y / 32$
C SET CHAKACTEK STRING FOF GFAFHIC
IVZ (1) $=32+1 Y 1$
IUZ (2) $=96+1 Y-32 * 1 Y 1$
$I \cup X(3)=-32+I X 1$
IV3 (4) $=64+$ IX $-32 *$ IX1
C DHFK / BRIGHT VECTOF?
IFLG=0
IF (I.EQ.O) GOTO 3
CHIGH Y
IF (IV3 (1). NE. IOLDBT (1)) $S=0 C H A F(1 \cup 3(1))$
C LOW Y
IF (IVZ(2).EA.IOLDBT (2)) GUTO 4
IFLG=1.
S:OCHAFI (IVZ (2))
C HIGH $X$
4 IF (IV3 (3).EQ. IOL.OBT (3) ) GOTO 5
C LOW Y SENT?
IF (IFLG.EG.1) GOTO 6
C SEND LOW $Y \&$ HIGH $X$
$S=0 C H A K(I V Z(2))$
6 S=OCHAF(IV3 (3))
$5 \quad S=$ OCHAF $(\operatorname{IV} 3(4))^{7}$
GOTO 11
3 S=OCHAR (29)
$002 \mathrm{~J}=1.4$
C OUTFUT FOINT COORDINATES
2 S=0CHAR(IVZ (J))
11 bO $7 k=1,4$
7 IOLDBT $(K)=1 \cup 3(K)$
FETUFN
END
C

C
SUBROUTINE XUFLOT ( $I, X, Y$ )
C MONE ( $I=0$ ) OK DNAW ( $I=1$ ) TO ( $X, Y$ )
C AND ALSO SETS (LFOS,CHFOS) CHARACTEF FOSITION ON THE SCREEN COMMON/AFEA/SCALE (12)
COMMON/KNGEFFH/MODE, LFOS,CHFOS
COMMON/RETXY/JXX, IYY
IMTEGER CHFOS
C WINDOWING
$I X=$ SCALE (11)* (X-SCALE (5) )/SCALE (9) + SCALEE(1)

```
    IY=SCALE (12)*(Y-SCALE (7))/SCALE (10) +SCALE (2)
    CALL XYUOCH (IX,IY,LFOOS,CHFOS,IA,IB)
    MODE=1
    C CHECKS THE COORWINATES X,Y NOT OFF THE ECNEEN
    DIF1=X-SCALE (5)
    DIF2=X-SCALE (6)
    DIF}3=Y-SCALE (7)
    UIF4=Y-SCALEE (B)
    IF(DIF1.LT.O..OR.DIF2.GT.O..OK.DIFG.LT.O..OK.DIF4.GT.O.)GOTO 2
    IF(I.EQ.O) GOTO 3
    IXX=IX
    IYY=IY
3 CALL UFLOT (I,IX,IY)
    FETUFIN
C OUTFUT WAFRING MESSAGE
2. CALL UFLOT (0,10,650)
    CALL ALFFHMD
    WRITE (6,E0)
60 FORMAT "COORDINATES OFF SCEEEN")
    IF(I.EQ.O) GOTO 3
    CALL GRFHHMD
    gOTO 1
    END
C
C**************** MOUE THE BEAM TO AESOULTE X,Y****************
C
    SUEFOUTINE TXMOUE (X,Y)
    COMMON/EXY/KX,NY
C RESET COMMON UARIABLES
    FiX=X
    KY=Y
C OUTFUT DARK VECTOK
    CALL XUFLOT (O,X,Y)
    FETURN
    END
C
C*********** MOUE EELATIUE *************************************
C
    SUEROUTINE TXMONK(IXX,DY)
    COMMON/EXY/KXX,FY
C UFDATE COIMON VAFIAELES FOR RELATIVE MODE
    X=FX+DX
    Y=RY+[IY
    FXX=X
    EY=Y
C OUTFUT DAKK VECTOK OF LENGTH DX,DY
    CALL XUFLOT ( O,X,Y)
    RETURN
    END
C
C ****************DRAW ALINE TO X,Y FKOM CUFFENT BEAM FUSITION*********
C
    SUBROUTIAE TXDFIAW (X,Y)
    COMMON/EXY/EX,RYY
C FESET COMIMON UAFIABLES
    FX=X
    k'Y=Y
C OUTFUT ENIGHT VECTOR
    CALL XUFLOT (1,X,Y)
    FETUKN
    END
```

C

c
SUEROUTINE TXDRWR (DX,DY)
COMMON/FXY/FXX,RY
c ufdate common variables for relative mone
$x=k x+D x$
$Y=\mathrm{Fi} Y+$ Ij
$\mathrm{FX} X=\mathrm{X}$
KY=Y
C OUTFUT BRIGHT VECTOR OF LENGTH DX, DY
CALL $\operatorname{XUFLOT}(1, X, Y)$
FETUFN
ENG

```
C
*******************
* AFFENDIX 1.4*
C *******************
C
C CHARACTEKN AND TEXT HANDLING FOLITINES
C
C
C
C
C
C************** GET A SINGLE CHAKACTER FKOM THE SCREEN**********************
C
    SUBFOOUTINE TXGET (ICHAE)
C DELINEF A SIHGLE CHARACTER FKOM SCFEEN EXF'fdBINIG
C ANY ABBREUIATION AS FEQUESTED IN /AEEREU/
    COMMON/ABBREU/NSFEC,FSTCH,F'TKE(1)
    INTEGER FTFS,F,COLON,SFECHB,F゙STCH
    INTEGEF**1 C(1)
    EQUIUALENCE (C (1) MSFEC)
    LIATA F,COLON/O,58/
    IF (F.EQ.O)GOTO 1
    C F NONZERO MEANG DELIVER MEXT CHAR FROM GBEREV(STOF HT :)
    4 ICHAF=C. (F)
    F=F'1
    IF (ICHAR.NE.COLON) GOTO $9
    C FEACHED COLON
    F=0
    C NOKMAL ISE INCHK
    1 ICHAK:= JNCHAK (X)
    IF (NSFEC.EQ.O) GOTO 9%
    DO 2 J=1,NSFEC
    2 IF (C (FETCH+T).EQ. ICHAR)GOTO 3
C NO MATCH
99 ICHAK`= IEEM(ICHAR-128)
    NETUFN
    3 F=FTES(J)
    GOTO }
    END
C
C *************QUTFU'T ASTNGLE CHARACTEK TO THE SCEEEN*******X***********
C
SUBROUTINEE TXFUT (ICHAR)
C SEND C TO THE SCREEN,TAB IS INTEFFETED AS A SUITABLE NUMEEE
C. OF SF'ACES FUEOUT IS FRINTED AS FULL, BLOCK OF DOTS
    COMMON/MAGFFFH/MODE,LFOS,CHFOS
    COKMON/IO/IN, IOUT
    INTEGEF CR,FF,TAB,FUBOLIT,SF'ACE,BACKSF,A(4),US,CHFOS
    DATA CR,FF,TAB,FUEOUT, SFACE,1.3,12,9,1.27,32%
    DATA BACKKSF;A(1),A(2),A(3),A(4),US,1F,B,36,73,E8,72,31,10%
    I=ICHAK
    IF (HODE.NE.O) S=OCHAK'(US)
    MOUE=0
    I=IREM (I,128)
    IF (X.EQ. BACKCF)CHFOS=CHFOS-2
    IF (I.NE.FF) GOTO1.
    LFOS:=0
    GOT02
    IF (I.rE.CF) GOTO 3
    CHFOS=-1
    IF(I.NE.L.F) GOTO 31. .
    CHFOS=-1
```

$100 \quad \mathrm{LFOS}=\mathrm{LFOS}+1$
$\mathrm{CHFOS}=\mathrm{CHFOS}-1$.
C TEST IF ON SCFEEN
31 IF (LFOS.GT. $34.0 \mathrm{O} . \mathrm{CHFOS.6E.74)} \mathrm{WFITE} \mathrm{(IOUT}, \mathrm{1O)}$
10 FORMAT ("CHAR.OFF THE SCREEN")
$5 \quad$ CHFOS:CHFOS +1
IF (I.NE.TAB) GOTO 4
C TAB TO NEXT MULTIFLE OF 8
5=0CHAK' (SF'ACE)
IF (HOD (CHFOS, 8) . NE . O) GOTO 5
GOTO 99
IF (I.NE. FUUBUUT) GOTO 6
[10) $21 \mathrm{I}=1,4$
$S=0 C H A R(A(1))$
S=OCHAK (BACKSF)
21 CONTINUE
$I=S F \cdot A C E$
6 S. OCHAK (I)
C GENEKATE A LF AFTER A CK (LFYS AEE OTHEFWISE IGNORED)
IF (I.NE.CR) GOTO 97
$I=$ LF
G0T0100
99 RETURH
ENS
C
C************INFUT A LINE OF TEXT FROM THE SCREEMA**********
C
SUEROUTINE TXILINE (STRITG,N)
C INFUT ALINE OF CHAKACTER FROM THE BCREEN INTO GTRING (O)
C ECHO AND DE.AL. WITH FUEOUTS
C ENU OF INFUT UITH L.F , CR, EOT

INTEGEK* 1 STEJTLG (M)
$C$ FTHS IS USEE TO HOLD AFFARENT OFFSET OF CORKECT CHAR
IHTEGEK FTTRE (72), CR, BACKSF' FUUEOUT, SF'ACE, IFF, EUT, TAB
DATA CK, EACKEFF, RUBOUT, SFACE,LF, EOT, YHE /13,8,127,32,10,4,9/
NECHO=0
MEXTIM $=1$.
C MAIM LOOF'
100 CALL TXGET (K)
IF (K.EQ.FUEOUT) GOTO 101
STRING (REXTIN) $=$ K
FTRS ( HEXTI I $=\mathrm{NECHO}$.
NEXTINENEXTI $\mathrm{H}+1$
IF (K.EQ.CK.OK.K.EQ.EOT.OK.K.EQ.LF) GOTO 9 O
IF (K゙.EQ.TAB) GBTO 102
C ORWINARY CHARARCTER ECHO AND LOOF (IF ENOUGH EFACE)
NECHO NECHO +1.
CALL TXFUT (K)
IF (NEXTIN.L.T.MIHO $(N+1,72)$ ) GOTO 100
C FIMISHED FOR SOME REASON
99 STFING (NEXTIN) $=0$
GETURN
C TAE-LDOF OUTFUTTING SFACES
102 HECHO $=$ NECHO +1
CALL TXFUT (SFACE)
IF (MOD (NECHO, B). NEE O) GOTO 102.
GOTO 100
C RUEOUT
101 IF (NEXTIN.EQ.1) GOTO 100

```
    NEXTIN=NEXTIN-1
    NBACK*-*&CHO-FTFSS(AEXTIN)
    1O 91 I=1,NEACK
91 CALL TXFUT (EACKSF)
    CALL TXFUT (FUEOUT)
    CALL TXFUY (BACKSF)
    M) 72 I=1,NEACK
92 CALL TXFUT (SFACE)
    GOTO 100
    ENO
C
C ************OUTFUT A GIVEN MESSAGE (ERID IN ZERO CHARACTER)**************
C
    GUBFQUTTHE MESSAG(TEXT)
C START THE MESSAGE WITH % FOK OUTFUTING TO THE &EXT LIIEE
C TERMMMATE THE TEXT WITH yNy AS THE END OF THE MESSAME
    COMMON/MNGKFH/MOLLE,LFOS,CHFOS
    COMMON/IO/IN,IOUT
    INTEGER*1 TEXT(1)
    INTEGER FCENT,HAT,CHFGS
    DATA LIFF+CENT,HAT/10,37,94/
    CHFOS=-1
    U0 1 I=1,129
        J=TEXT (I)
        IF (J.EQ.HAT) FETURN
        IF(\.EQ.FCENT) J=LF
    1 CALL TXFUT (J)
C. ATTENFT TO OUTFUT A MESSAGE MORE THAN 128 CHANARCTERS
    WFITE (IOUT,10)
10 FORMAT "ATTEMFT TO OUTFUT A MESSAGE MORE THAN 12B CHAEACTENS")
    RETUJKN
    END .
C
C***********OUTFUT TEXT UF ON THE SCREEN FROM A FIEE*****************
C
C THIS MISFLAY TEXT FROM THE FILE NGMED
C A HOLLEFITH STKING AS FOK SETFIL
    GUBROUTINE TEXTUP(FILEyN)
    COMMON/IO/IN,IOUST
    INTEGEK*1. FJLE(1)
    IMTEGEK EUFFEK(7%)
    REWIND7
    CALL SETFIL(7,FILE)
C LOOF READING FKOM FILE
2 DO 1 I=1,N
            REAL (7,110) BUFFER
            FOFMAT (72A1)
            WFITE(1OUT,110)BUFFEK
            CONTINUE
    ENDFILEE %
    fETUFN
    END
C
C********************GET AN INTEGER FROM THES SCREENO*****************
C
SUEROUTINE IMTGET (I)
C OETALH THE REEXT IRUEGER FROM SCKEEM
            INTEGEF** LITEE (8)
            IMTEGEK CHO,CH9
            DATA CHO,CH9/48,57%
            CALL TXLINE(LINEEB%.
            CALL EFUUT (LINE)
```

```
    I=0
    10 10 k=1,8
    J=LINE (K)
    IF (J.LT.CHO.OK..J.GT.CHG) GOTO 9%
    J=J-CHO
    IF(I-32767)10.11,12
    IF (1.GE.%) GOTO 12
    I=I*10+J
    I=32767
    FETUKN
    ERO
C
C*************FEMOUESSFACES FROM STRING**************************
C
    SUEFOUTINEE SFOUT (ETRING)
C ITS REMOUES EFACES AND OTHER NUK-FRIMTING CHAKS FROM STRING
C SUCH AS LINE FEEDS,CAKRIAGE EETURNS.GNDI EOT"S FFOM TEXT
    INTEGEF**1 STRING(1)
    J=0
    40 1 I=1,100
        j=j+1
        K=STEING(J)
        IF(K゙.LT.O)K=K゙+128
        IF (K.EQ.32)GOTO 2
        IF(K.EQ.10.OK.N゙.EQ.13.OF.K.EQ.#)GOTO 2
        STRING(I)=K
        IF(K゙.EQ.O) GOTO 3
    RETURN
    END
C
C ******************OUTFUT CHAFACTEF STEING AT GIVEN COORDINATES********
C
    SUEROUTIME DTEXT (X,Y,TEXTYNO
    LOGICAL*I TEXT(N)
    CALL- TXMOUE (X,Y)
    CALL ALFHMSD
C OUTFUT THE STKING OF CHAFACTEFS IN TEXT
    WRITE(6,10)TEXT
10 FOKMAT (72A1)
    RETUKN
    END . ?
```

```
C
                                    ******************
                                    * AFFEMDIX 1."S *
                                    *****************:4
C
C CUNSOR AND MENU OFERATLONS FOUTSNES
C
C
C
C **************ERASE CROSS HAIFSCUSSOK********************x******
C
    SUBFOUTINE CURSET (X,Y,ICHAK)
C FETUKNS XYY COOKDINATES AND CHAKACTEF TYFED
    S=CURSON(ICHAF,IHIX1,ILEXI, IHIYI, ILOY1:
    X=32* (THIXI-32)+ILOX1-32
    Y=32* (IHIY1-32)+ILOY1-32
    FETUKN
    END
C
C**************SET UF THE CUKSOK AHES EETUKN A CHAKRZCTEF***************
C
    SUEKOUTTNE TXCLFS(X,Y,ICHAK)
C THIS DISFLAYS THE CROES-HAIR CUKSOR OH THE ECFEEN
C THEN FETURNS THE SCALED VALUE OF THE COUKLITKATES OF
C THE CUKSOK IN X,Y AHDD THE CHAKACTEK TYFELU IN&FUT IM ICHAK
    COMMON/KNEGFFH/MODE, I.FOSyCHFOS
    INTEGER CHFOS
    COMMON/AREA/SCALE (12)
1 MODE:=1
    CALL CUFSET (X,Y,ICHAK)
    ICHAK=IFEM(ICHAK,ICB)
C CHECK CUKSOK LOCATION ON THE SCKEEN,IF OUTSID L.IMIT GOEAGK
    IF (X.LT.SCALE(1).OF.X.GT.SCALE(%).OR.Y.LT.GEALE (2).OK.Y.GT.
& SCALE(4)) GOTO 2
C
C COMFUTE SCALED VALUE
    X=SCALE (5) + (X-SCALE (1)) *SCAL.EE (9)/SCALEE (11)
    Y=SCALE (7) + (Y--SCALE (2))*SCALEE(10) /ECALE (12)
    IX=X
    IY=Y
    GOTO 3
2 CALI. ALFHMD
    CALL MESSAG("ILLEGGAL CUKSOR FGSITION!"*
    gOTO 1
3 CALL XYVOCH(IX,IY,LPOSPCHFUS,IA,IB)
    RETUKN
    EMB
E
C***************FOSITTON THE ALIFHA CURSOR****************************
C
        SUEROUTINE CURFOS (X:Y)
        CALL TXMOVE (X,Y)
C SET THE gIGFLAY TO ALFHA MOLE
        CALL. ALFHIGB
        RETTUK'W
        END
C
C ***************** OFEN A NEW ME:NU********************
C
    SUEKOUTIDE MNOFEN(X,Y,MNO)
C SET UF ORIGIN FOK MENUJ,WHICH ANNOUCES THAY A DENUS JS
```

C TO DE MSFLAYED WHOSE TUR LEFTHAND DORNEF IS YO EE AT ECEEEN
$C$ COORDTMATES ( $X, Y$ ) AND MENU NUMEEE MOM
COFMON/MENUNA/XOFIG(3) YORLG (3), STEF PRL INES (3)
IF ( HNO . $E Q_{\text {. }}$ 1) $\mathrm{YOKIG}(2)=0$.
XORIG (MNO) $=X$
YORIG (MNO) $=Y$
STEF=22.
NL INES (MAXO): $=0$
FETURN
END
C

C
EUBROUTINE MNTEXT (TEXT,N,MATO)
C FUT OUT THES TEXT AS THE NEXT LINE OF A MERU
COMMON/MENUDA/XOKIG (3), YOKIG (3), STEF'NLIHES (3)
C DEFINEL BYTE ARRAY
LOGICAL*1 TEXT (N)
C MOVE TO THE DESIFED LOCATION
CALL TXMOUE (XORIG (MNG) , YORIG (MNO) -ALLINES (MNO) *STEF)
C SET TO ÁLFHA MODE
CAILL ALFHMD
C
C BUTFUT MENLE ITEM
WKITE (6,10) TEXT
10 FOKMAT (72A1)
NLINES (MNO) =-NL IMES (MNO) + 1
RETUKN
END
C
C $* * * * * * * * * * * * *$ PICK AN ITEM FKOM $n$ MENU****************************
C
SUEKOUTINE MNF'ICK (I, ICHARTMNO)
C SETS I TO. THE INDEX OF MENU ITEM CHOSEN,ICHAR TO THAT TYFED COMMON/MENUNA/XONIG (3) , YOFIG (3) , STEF' PLLINES (Z)
1 CALL TXCLKE (XI,Y1,ICHAR)
IF (Y1.GT. YONLG(2)+10) GOTO 5
$\mathrm{MNO}=2$
goro 3
$5 \quad M N Q=1$
3 KFUS:YOKIG(MNO)-Y1+14

J:MOD (FFOS,STEF')
IF (J.LT.O) J=J+STEF
IF (I.LE. O.OR.I.GT.NLINES (KNO) .OK.J.GT.14) GOTO 1.
C
C MARK THE MENU ITEM WITH AKROW
CALL TXMOUE (XORIG (MNO)-40. Y $^{\text {Y }}$ )
CALL TXDFAW (XOFIG (MND) YY1)
CALL TXOKAW (XORIG (MMO)-20. Y Y $1+10$. )
CALLL TXMOVE (XORIG (MNO), Y1)
CALL TXIFAW (XOFIG (MNO)-20. YY1.-1.0. ?
2 RETUKTH
END
C
C **********DISFLAY A COMFLETE MENU AT FRE ASEIGNEI ORIGIN**********: C

```
EUEROUTINE MNUISF (TEXT,ITEM,LEN,MNO)
LOGTCal_%1 TEXT(1)
K=0
    130 77 I=1.ITEM:
```

C. GUTFUT ANX ITEM OF THE MENU

CALL MNTEXT (TEXT (I +K ) LEN, MNO)
$K=K+\operatorname{LEN} \mathrm{N}-1$
contimue
RETUFN
END
C

$C$
SUEROUTINE FFiAME (X1,Y1,NC)
c driaws feetangle round ihe menu
CALL TXMONE (X1,Y1)
CALL TXURAW ( $\mathrm{X}_{1}+145$, Y1 $)$
CALL TXOKAL $(X 1+1.45, Y 1-22 * N C)$
CALL TXURAW (X1,Y1-22*NC)
CALL TXDRAW (X1,Y1)
FETUFN
end
c

C
SUEFOUTINE XYVOCH (IX,IY,NLINE, NCHAF, IATIE)
© THIS SETS (NLIME, MCHAF) AND (IAyIB) TO THE CHARACTEF
C imdicated by ( $X, y$ ) and the offset felative to ite blh corinek
COMMON/TOFLHC/IXORIG,IYORIG
IA $=$ MOD (IX-IXOFIG.14)
$\operatorname{IF}(I A . L T . O) I A=I A+14$
IB: MOD (IY-IYORIG,22)
IF (IB.LT.0) IB $=1 \mathrm{IB}+22$
NCHAK=(IX-IXOKIG)/14
NLINE $=($ IYORIG-IY +21 )/22
RETUENR
ENI

```
C
    *********************
C
    * AFF'ENIIXX L.G*
    ******************
C
C BASIC THANSFORMATION FOUTINES
C
〔
C
C
[***********SCALE UF OR DOUNT THE DATA**********:************
C'
    SUEROUTINE SCALNG(SX,SY,SZ)
    COMMOM/MATKIX/ETM (4,4), TM (4,4)
    DIMENSION TT(4,4)
C SETS UF UNIT HATEIXX
    CALL UAIITY (TT)
C FESET THE AFFROFRIATE MATKIX ELEMENTS TO THE GFECIFIEE FAFAMETERS
    TT}(1,1)=S
    Tr (2,2)=-SY
    Tr (3, 3) = = Z Z.
C LFDATE THE TRANSFOFMATION MATRIX
    CALL CONCAT (TM,TT,4)
    RETUKN
    ENO
C
```



```
C
    SUBROUTINE TRANSL(TX,TY,TZ)
    COMMOM/MATFIX/CTM(4,4),TH(4,4)
    DIMENEION TF(4,4)
C SETS UF UNIT MATRIX
    CALL. UHITY (TT)
C FESET THE AFFFOFFIATE MATRIX ELEMENT TO THE SFELIFIELI FARAMETENS
    TT(4,1) = \X 
    TT}(4,2)=T
    TT(4,3)=TZ
C UFDATE THE TRANSFOKWATION MATRIX
    CaLL CONCAT (TM,TT,4)
    FEETUKN
    END I
C 1.
C************ROTATE A IAATA FOINT AEOUT-X.Y,Z IN THLS UHDEK***********
C
    SUBEOUTINE ROTATE(KX,FRY,NZ)
    COMMON/MATKIX/ETM(4,4), TM(4,4)
    GIMENSLON TT(4,4)
C CONUEFT FROM DEGKEE TO RADIANS
    U1vS=57.2857795
    FX=FX/OIVS
    RY=FY/IIUS
    FZ=RZ/DIVS
C SET THE GNGLEES IN FADTAMS
    AD= fir+hz
    B1= RY-KZ
    A2= FXX+FZ
    R2= FX-F%Z
    A=FFX+RY
    SJ=FX--FiY
    C==FEX+RZ
    D=R&X+RZ-KY
    E=FX-FZZ+FY
```

```
    F=FKX-FZ-N'Y
C
C SET THE ELEMENTS OF THE FOTAION MATEIXX
TT (1,1) =0.5*(COS (A1)+\operatorname{COS (E1) )}
Tr}(1,2)=0.5*(SIN(A1)-SIN(B1)
TT(1,3)=-SIN(FY)
TT (1,4)=00.
```



```
TT (2,2)=-0.25* (SIN(D)-GIN(C)+SIN(E)-SIN(F))+0. S5* (COS (A2)+COS (E2))
TT (2,3)=0.5* (SIM(A3)+SIN(EX))
TT (2,4)=0.4
TT(3,1)=0.25*(SIN(C)-SIN(D)+SIN(E)-SIN(F))+0.5*(CUS (A2)-COS (B2) )
TT (3,2)=0.25*(CGS (C)-COS (D)-COS (E) +COS(F) - - - . S** (SIM (A2) +SIN(B2))
TT (3,3)=0.5* (COS (A3) +\operatorname{Cos}(E3))
TT (3,4)=0.
TT(4,1)=0.
TT (4,2)=0.
TT (4,3)=0.
TT (4,4)=1.
CALL CONCAT (TM,TT,4)
RETUFN
EHD
```

```
C
C**********ELIF'S ALINE TO SFECIFIED WINDOW BOUNDAKIIES**************
C
C HISFLAY FILE
    SUSEFDUTTNE CLIF(CLINE,XO,YO,X1,Y1,IREJ)
    COMMON/LIMIT/S1,S2,S3,S4
    COMMON/LIMES/SUEL.IN(3,2)
    UIMENSION CLINE(2,2),1SEG(2)
    IMTEGEK EMDFNT,TWOSEG
C
C SET THE LIMIT----INITIALISATION
    ENDFNT=0
    S1=X0
    S2:=Y0
    S3=X1
    S4=Y1
C
C TEST FOR FULLY REJECTION/ACCEFTANCE---FIFST TIME
    XX1=CLINE (1,1)
    YY1==CLINE (1,2)
    XX2=CLINE (2,1)
    YY2=CLINE (2,2)
    I=IEEJCT (XX1,YY1,XX2,YY2)
    IF(I.NE.1) GOTO I
C
C FLLLLY REJECTED
    IFE. 
    RETUKN
C
C TEST FOR ACCEFTANCE
1 J=JACCFT (XX1,YY1,XX2,YY2)
    IF (J.NE.1) GOTO 2
C
C FULLY ACCEFTED
        TFES=1.
        FETUKN
C
C NOT FULLY ACCEFTEIM-.-- SUEDIULEO THEE L.INE
2. CALL SUBMIU(XX1,YY1,XX2,YY2,IEEEG)
    GOTO (11,12,13),ISEG(1)
```


## $c$

C TEST FOR EACH CONDITIOM
C FIRST SEGMENT REJECTED
11 GOTO (104,14,15),1SEG(2)
c
C. second segment accefted fully

14 . IF ERDFNT.EQ.O) GOTO 16
17 CLINE $(1,1)=\operatorname{sughIN}(3,1)$ CLIMEE (1,2) =SUELIN (3,2)
177 IF (TWOSEG.EQ.2) GOTO 31
TWOEEG=: $)$
IREJ=1
RETURN
$16 \operatorname{CLINE}(1,1)=\operatorname{SUELIM}(2,1)$
CLITE $(1,2)=\operatorname{SUEL}$ IN $(2,2)$
$\operatorname{CLINE}(2,1)=\operatorname{SUELIN}(3,1)$
CLINE ( 2,2 ) $=\operatorname{SUEL} . \mathrm{IN}(3,2)$
GOTO 717
ENDF'NT $=1$
GOTO 17
c
c not fuliy accerted
$15 \quad X \times 1=\operatorname{SUELIM}(2,1)$
$Y Y 1=\operatorname{SUELIN}(2,2)$
XX2"=SUELIN (3.1)
YYO=SUBLIN (3,2)
goto 2
104 IF (ENDPNT.EQ.11) GOTO 188
IF (TWOSEG.EQ.1) GOTO 188
CLITEE $(1,1)=\operatorname{SUEL}$ IN $(3,1)$
$\operatorname{CLIME}(1,2)=\operatorname{SUELIN}(3,2)$
IF (TWOSEG.EO.2) GDTO 31
IF (ENDFNT.NE.O) $60 T 0177$
IFE $J=0$
FEETUFA
188 CLITEE $(2,1)=\operatorname{SUELIN}(1,1)$ CLINE $(2,2)=\operatorname{SUBLIN}(1,2)$ GOTO 177
707 IF (TWUSEG.EQ.2) GOTO 31 IREJ=0 RETUEN ?
C 1
C TEST FIEST SEGMEMT FULLY ACEEFTED
12 . IF (ISEG (2).NE. 1) GOTO 25 IF (ENGFNT.NE.O) GOTG 19
CLINE $(1,1)=\operatorname{SUELIN}(1,1)$
$\operatorname{CLITE}(1,2)=\operatorname{SUBL} I \mathrm{IN}(1,2)$
$\operatorname{CLITE}(2,1)=\operatorname{SUBLIM}(2,1)$
$\operatorname{CLIME}(2,2)=\operatorname{SUEL} \operatorname{IN}(2,2)$
IF (TWOSEG.EQ.2) GOTO 31
717 IFEJ=1
FETURN
25 IF (EMLHFT.EQ.O) GOTO 35
$\operatorname{CLINE}(2,1)=\operatorname{SUEL} \operatorname{IT}(2,1)$
CITNE (2r2) =SUELIM(2,2)
goro is
$35 \operatorname{CLINE}(1,1)=\operatorname{SUELIN}(1,1)$
CLINE (1,2)=SUELIN(1,2)
EMDFTMT=11
goro 15
C
C test fifst segment not fully accefted

13 IF（IEEG（2）．NE．1）60T0 21
18 XX1＝5UELIM（1，1）
$Y Y 1=\operatorname{SUEL} \operatorname{IN}(1,2)$
$X X 2=S U B L I N(2,1)$
$Y Y 2=S U E L I N(2,2)$
GOTO ？
21 IF（ISEG（2）．EQ．2）GOTO 41
TWOSEG＝2
$X X 3=$ SUELIIN（2，1）
$Y Y 3=S U E L I M(2,2)$
$X \times 4=$ SUELIN $(3,1)$
$Y$ Y4＝SUEL．IN $(3,2)$ GOTO 18
31 TWOSEG：＝1．
$X X 1=: X X 3$
$Y Y 1=Y Y 3$
$X X 2=X X 4$
YY2：YY4
GOTO 2
41 IF（ENDFNT．EQ．1）GOTO EB ENDFNT＝1
CLINE（ 2,1 ）＝SUBLIM（ 3,1 ）
CLINE $(2,2)=$ SUBLIM $(3,2)$
GOTO 18
$88 \operatorname{CLINE}(1,1)=\operatorname{SUELIN}(3,1)$
CLINE $(1,2)=\operatorname{SUBLIN}(3,2)$
GOTO 18
END
c
C＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊SUBDIVID THE LINES AT ITS MIDFOINT $* * * * * * * * * * * * * * * *$
c
SUBKOUTIRE SUBDIU（X1，Y1，X $2, Y 2, I S$ ）
COMMON／LINES／SUELIN $(3,2)$
DIMENSION IS（2）
C SET THE SUEDIVIDED AFFAY LIHE
$\operatorname{SUBLIN}(1,1)=X 1$
SUELIN $(1,2)=Y 1$
$\operatorname{SUBLIN}(2,1)=0.5 *\left(X 1+X_{2}\right)$
SUEL．IN $(2,2)=0.5 *\left(Y 1+Y^{2}\right)$
SUELIN $(3,1)=\times 2$
SUELITH $(3,2)=Y 2$
C TEST SEGMENTS FOF REJECTION／ACEEETANCE
$101 \mathrm{~K}=1,2$
$I 1=I F E J C T(S U E L I+1(K, 1), S U E L I N(K, 2), S U E L I N(K+1,1), S U E L I N(K+1,2))$
IF（IX．EQ．O）GOTO 7
C COMFLETE REJECTION OF A LIHE
$15(k)=1$
goto 1
C TEST LINE FOK ACCEFTANCE
7 J1＝－JACCFT（SUBLIN（K，1），SUELIN（K゙，2），SUEL＿IN（K゙＋1，1），SUELIM（K゙＋1，2））
IF（J1．EQ．O）GOTO 8
C LItE FULLY ACCEFTED
IS（k）$=\mathbf{2}$
GOTO 1
C liNe NOT FULLY ACCEFTED
$8 \quad$ IS $(K)=3$
C NEXT SEGMENT
1 CONTINUE
FETUKN
END
C
C＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊TEST CONDITION FOR L．ITEE REJECTIOTX＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊
c

FUHCTION IFEJCT (X1,Y1, $\times 2, Y 2$ ) COMMOM/LIMIT/S1, S2, 53,54 LOGICAL. AL,E1,AAPBE,CC.DD $\mathrm{N}=0$
DIF 1=X1-E1
DTF $2=\times 2-51$
DIF $3=\mathrm{X1}-53$
DIF4 $4=\mathrm{X} 2-53$
$A=A B S(\times 2-\times 1)$
AI =UIFI.LT.O. $A N D . D I F 2 . L T . O$ BL=:UIFG.GT.O. .AND.DIFT.GT.O.
AA=DIF1.LT.O. . AND.A.LT.0.005
$B E=$ DIF 2.LT. O. . FILD.A.LT. 0.005
CEEDIFZ.GT.O. FAND.A.LT.O.OOS
DU= DIF4.GT.O. FAND.A.LT. O. OOS
C TEST FOK LINE CDMFLETELEY OUTSIDE THE LIMITWITHIT O.OOS
C TOLEFANLE
IF (A1.OK. B1.OK.AR.OK.BE.OK.CC.OK. OD) (GOTO 2
$\mathrm{N}=\mathrm{m} \mathrm{x}+1$
IF (N.EQ.2) GOTO 3
C SAME TEST FOK Y
QIF1 $=\mathrm{Y} 1-\mathrm{CO}$
DIF 2=Y2-52
DIF $3=Y 1-54$
DIF4=Y'2-S'4
$A_{1}=A E S(Y 2-Y 1)$
gora 1
C NOT REJECTED
3 IKEJCT: 0 FETUKN
C FULLLY RE.JECTEI
2 IKEJCT=1 FETUKP END
c
 C

FUNCTIOM JACCFT (X1,Y1,X2,Y2)
COMMOH/LIMIT,S1,S2,53,S4
LOGTCAL ADB T X11=X1-E1 , $\mathrm{X} 22=\times 2-51$ X $33=\times 1-53$ X44: $\times 2$ - 53
 $Y 11=Y 1-52$
Y22=Y2-52
$Y J 3=Y 1-54$
Y44=Y2-54
 IF ( A . AND. B) GOTO 1
C Not Fully acceften
$\mathrm{JACCFT}=0$
RETUFN
c. Fully accerten
$1 \quad \mathrm{~A} A C \mathrm{CT}=1$
FETUFR
END
C.

C

SUEROUT TNE FERSF (FX,FYYFFZ
COMMOR/MATKIX/CTM (4,4), TH(4,4)
DIMENSIOK TT (4.4)
C SET MATEIX TT TO UNIT MATEIX
CALLL UNITY(TT)
$\mathrm{T} T(1,4)=\mathrm{F} \times$
$T T(2,4)=F \cdot Y$
$\mathrm{TT}(3,4)=\mathrm{FF}$
CALL CONCAT (TM,TT,4)
FETURIT
END
C

C
SUEFOUTINE FKOJCT (FFLANE)
COMMON/MATKIX/ETM (4,4), TM ( 4,4 )
DIMENEION TT (4,4)
CALL L UNITY(TT)
C FROJECTTON FLANE
GOTO (1,2,3), NFLAANE
$1 \quad \mathrm{Tr}(1,1)=0$.
GOTO 4
$2 \quad \operatorname{Tr}(2,2)=0$.
GOTO 4
$3 \quad \operatorname{Tr}(3,3)=0$.
4 CALL CONCAT (TM,TT,4)
RETUKN

- END

C

C
SUEFOUTIME SAUMAT (A)
COMMON/STACK/ISF'NTK,STACK (64)
COMMON/IO/IN, IOUT
IIMENSION A $(4,4)$
ISTKSZ $=64$
C FUSH MATRIX ELEMENT IMTO THE STACK
$102 \mathrm{~J}=1,4$
(i0) $31=1,4$
IF (ISFWTK.EQ.ISTKSZ.) GOTO 1
ISF'NTK= ISF'NTK' +1
$\operatorname{STACK}(I S F \cdot N T K)=A(I, J)$
CONTINUE.
FETURN
1 WKITE (IOUT,10)
10 FORHAT ("STACK OUERFLOW")
EETUFN
END
C

C
SUBFOUTINE RESTOK (A)
COMMON/STACK/LSFNTK, STACK (64)
COMMON/LO/IN, LOUT
DIMENSION A $(4,4)$
© FOF MATFIX ELEMENTS FFOM THE STACK AND SAVE THEM IN A
$02 \mathrm{~J}=1,4$
$\mathrm{L}==4-\mathrm{J}+1$.
10 3 I $=1,4$
$K=4-1+1$
IF (ISFNTR.EO.O): GOTO 1.
$A(k, L)=$. STACK (ISFNTK) COMT IRUE FETUFN
1 WFITE (IOUT,10)
10 FOKMAT ("STACK UNDEFFLOW") STOF-
fETUKK
END
C
CH**************SET AGIUEN MAKIX TG UNITY***************
C
SUEFDUT INE UNITY(A)
DITENSTOK A $(4,4)$
DO 1 I=1. 4
(10) $2 \mathrm{~J}=1,4$
$A(I ; J)=0$.
$\operatorname{IF}(I n E Q . J) A(I, J)=1$.
CONTINUE
2 CONTI RETUKN ENW
C
C****************SET CTM MATRIX TO AGIUER MATKIX
C
SUERDUTINEE SETMAT (A)
COMMDN/MATRIX/CTM (4,4), TM (4,4)
DIMENSION A $(4,4)$
DO $1 \mathrm{I}=1,4$
DO 2 J=1. 4
$3 \quad \operatorname{CTM}(I, J)=A(I, J)$
1 CORTINUE RETUKN. END
C

C
SUEROUTITE CONCAT (AyB,N)
DIMENSION $A(N, 4), B(4,4), T T(4,4)$
C FOST-HULTIFLY AFKAY A BY B , AND RETUKKK THE KESULT JN A
$101 \mathrm{I}=1 \mathrm{~N}$
DO 2 $J=1,4$ 个
$\operatorname{TT}(I, J)=0$;
[10 $3: K=1,4$
$\operatorname{TT}(I, J)=T T(I, J)+A(I, K) * B(K, J)$
CONTINUE
2
1.

CONTIRUE .
$005 \mathrm{~J}=1,4$
DO $6 \mathrm{I}=1, \mathrm{~N}$
$A(I, J)=\operatorname{Tr}(I, J)$
CONTIRUE
6
5 CONTINUE
FETUKN
END

```
C
    *******************
                                    * ArPENGIX 1.7*
                                    *******************
C
C MIECELL_ANEOUS ROUTINES
C
C
C
C
C ******************OUERLAYS FROSGKAM MODLILES*********A&******************
\varepsilon
    SUENOUTINE OUFLAYY(FILENMS
    LOGICAL*1 FILENM(10)
    W:OVLAY (F TLENM)
    FETURF
    ERD
C
C. ***************** IT REMOUES A NAMED FILE FFUM CUKHENT DIKECTOFFY*****
C
        SUEROUTINE FNFF ILE (NAME)
        L.OGICAL*I NAME(1O)
        W=FLRM (NAME)
        RETUKN
        END
C
C *************** OUTFUT ERROK HESSAGE***********************
C
        SUEKOUTINE WEFROK(I)
        WRITE (6,1) I
    1 FORMAT ("EFFOK MESSAGE",I5)
        FEETUKN .
        END
C
C ************* CALCLILATE EETMINL&R'************************************
C
    INTEGEK FUNCTION IREM(I,J)
C gIVE FOSITIUE REMANDER OF I/J (J)O%
    1FEM=MOU(I,J)
    IF(IKEM.LT.O) IEEM=IKEM+J
    RETUKN
    ENO
%
```


## APPENDIX 1.8

INTRODUCTORY NOTES ON USING GT42 GRAPHICS SYSTEM
AND THE EMULATOR
1.0 GT42 START UP PROCEDURE (i.e. Rom Bootstrap from PDP 11/10 console on the GT42)

1) Check that the interface line is connected to the PDP $11 / 40$.
2) Determine that the GT42 power cord is connected to the appropriate electrical outlet.
3) Turn the console key switch to POWER position.
4) Turn the front panel ON-OFF/BRIGHTNESS switch fully counter clockwise and then of the way in clockwise direction, the red power indicator should be on at this time.
5) Presis the console ENABLE/HALT switch down to halt the computer.
6) Press the spring loaded START switch (on PDP 11/10 console) twice to reset the computer.
7) Place $166000_{8}$ in the SWITCH REGISTER (SR).
8) Press LOAD-ADDRESS to load this address.
9) Return ENABLE/HALT switch to the up-most position.
10) Press START switch. The Run light indicator should be on at this time.

Once the cursor appears on the display screen, the user can proceed to log-on.

### 2.0 DOWN LINE LOADER (DOWNLL)

In order to load a program in the GT42 the user must be logged on the terminal.

## Loading Procedures of the Emulator

To load a program the user has to type the command as shown below:
down11 < filename
where filename $=$ name of the program to be loaded down the line.
/LIB/TK4010 :- Tek 4010
This will load the Tektronix 4010 Emulator.
3.0 SHUTTING DOWN GT42

1) Logout on your terminal.
2) Press ENABLE/HALF switch down to HALT the computer.
3) Turn the $\mathrm{ON}-\mathrm{OFF} / \mathrm{BRIGHTNESS}$ to OFF.
4) Turn the console key switch to OFF position.

APPENDIX 1.9

LIGHT user guide

# LIGHT - USER GUIDE - (Loughborough Interactive Graphics System for the Tektronix 4010); 

## Introduction

Graphics is the pictorial representation of information and has been extensively used as a medium of communications in engineering and other disciplines. In this context, we use the term graphics to mean 'Interactive Computer Graphics'.

LIGHT is basically a set of library subroutines which can be called from a FORTRAN application program on the PDP 11/40 computer, equipped with Tektronix 4010 display unit and operating under UNIX operating system. These subroutines provide the coupling between the application program, the Graphics console, and the user. Thus the programmer can generate graphic displays with cross-hair cursor and keyboard interactions within his Fortran program.

## The Storage Tube

The storage tube display (Tektronix 4010) enables the user to have relatively economical graphics access to a computer, compared with refreshable displays such as the GT42.

The 4010 is a storage tube display together with a keyboard and character generator. The screen has 1,024 addressable points in the $x$ direction and 781 in the $y$-direction. A straight line segment is generated by hardware on the screen by specifying one end-point. In addition to graphic output of data, it is possible to input data by means of a cross-hair cursor. Once the cursor is positioned and any key is pressed, the co-ordinates of the cursor together with the character represented by the key are sent back to the computer. The ON/OFF switch for 4010 is located underneath the keyboard on the right-
hand side of the stand.

It is very important, when drawing on the 4010 , to ensure that repeated over-drawing of the same point or line is avoided as this will cause permanent damage to the display by burning holes through the screen phosphor.

For more detail on the Tektronix 4010 see Reference [20].

## Refreshable Display

LIGHT may also be used with the GT42 in Emulator Mode as a Tektronix. The package was carefully adapted in order to minimise the amount of flickering that may occur, because when the time taken to draw a complete "picture" exceeds 20 milliseconds then the display will flicker noticeably but the program operation is unaffected. Instead of the cross-hair cursor that appears on the Tektronix 4010, a tracking-cross and the light pen would have exactly the same effect and they can be used to simulate the function of the cross-hair cursor on the Tektronix 4010.

For further details on the 'Emulator' see Reference [24] and for GT42 operation (see Appendix.1.8).

## Graphics Library Package

The graphics system consists of the 4010 display, the PDP $11 / 40$ operating under UNIX, and a library of Fortran-callable subroutines. All that is required of the user is that he writes his/her application program in UNIX Fortran (a subset of ANSI) and incorporates the appropriate graphics subroutine calls. The "Back-end" modules, which drive the 4010 display and utilise UNIX, do not directly affect the user and are not described here.

The Graphics library subroutines`are listed in the following categories:

1. Initialisation
2. Point and line drawing
3. Tranformation and simple perspective projection
4. Character and text handling
5. Cursor and menu operations
6. Miscellaneous routines

The facilities provided by this package extend far beyond the minimal set (typically 1,2 and a function for text display) needed to use the display. They should prove to be useful over a wide range of applications.

### 1.0 INITIALISATION

Before any drawing can be made on the display terminal, the problem (or "picture") area and the screen (or display) area need to be defined by the user or by default.
1.1 TXOPEN:- Assigns default values for the display viewport and window (0., 0., 1023. ,780.) as a rectangle defined by the two corners $(0,0)$ and $(1023,780)$. This must precede any other graphics calls

## e.g. CALL TXOPEN

1.2 TXCLER:- Clears (erases) the screen ready for the next display picture
e.g. CALL TXCLER
1.3 TXVPRT(XO,YO,X1,Y1):- Sets a display 'Viewport' as the rectangle defined by corners ( $\mathrm{XO}, \mathrm{YO}$ ) , (X1, Y1) in terms of absolute screen co-ordinates (i.e. $0 \leqslant X_{0}<X_{1} \leqslant 1023$ and $\left.0 \leqslant Y_{0}<Y_{1} \leqslant 780\right)$.

The residual screen area can, of course, be used for other purposes, such as
screen displaying messages and menus.

1.4 TXWIND (X0,Y0,X1,Y1):- Sets a 'window' on the rectangle defined by corners ( $X_{0}, Y_{0}$ ) and ( $X_{1}, Y_{1}$ ) in problem space co-ordinates and maps this area onto the screen viewport.
e.g. CALL TXVPRT(200.,100., 800.,400.) window 1 problem CALL TXWIND (-1,0.,1.,1.)

This maps the window
$W\left\{-1 \leqslant X_{p} \leqslant 1,0 \leqslant Y_{p} \leqslant 1\right\}$
onto the viewport
$V\left\{200 \leqslant X_{s} \leqslant 800,100 \leqslant Y_{s} \leqslant 400\right\}$

1.5 ALPHMD,GRPHMD:-

ALPHMD: sets the display to Alpha mode so that the programmer may display textual information.

GRPHMD: sets the display to Graphic mode. However, as will be seen in section 2.1 a call to TXMOVE will set the display to Graphic mode.

Note: It is important to make sure that before the program is terminated, the display must be set in Alpha mode.

### 2.0 POINT AND LINE DRAWING

Points and lines form the basic elements of graphic drawing. Separate routines are provided for drawing visible or invisible (Point movement) lines, from the current beam (pen) position to a specified point, or through a given displacement. (These routines may be called the 'graphical primitives', as with aid of these routines the programmer could define his own procedures to draw shapes and symbols that he uses often). The co-ordinates and displacements which are used will normally be specified in the frame of reference of the application problem.
2.1 TXMOVE (X,Y) or TXMOVR (DX,DY):-

TXMOVE $(X, Y)$ : Moves the current 'beam' position to the scaled point ( $\mathrm{X}, \mathrm{Y}$ ) which is specified as an absolute point.

TXMOVR(DX,DY):Moves the current 'beam' position through the relative displacement DX,DY in $x, y$ direction.

Note: the above two calls will automatically set the terminal to 'Graphic mode', and it is under programmer control to change the mode to 'Alpha mode'. See section 1.5 above.
2.2 TXDRAW (X,Y), TXDRWR (DX,DY):-

TXDRAW $(X, Y)$ : Draws a visible line from the current 'beam' position to the scaled point ( $X, Y$ ) in absolute co-ordinates, leaving the beam at $\mathrm{X}, \mathrm{Y}$.

TXDRWR(DX,DY):Draws a visible displacement (DX,DY) from the current beam position
e.g. Drawing a Triangle ABC

CALL TXMOVE (0.,0.5.)
$\operatorname{CALL} \operatorname{TXDRAW}(0 ., 1$.$) or \operatorname{CALL} \operatorname{TXDRWR}(0 ., 0.5)$
CALL TXDRAW $(-0.5,1$.$) or CALL \operatorname{TXDRWR}(-0.5,0$.
CALL TXDRAW $(0,0.5)$ or CALL $\operatorname{TXDRWR}(0.5,-0.5)$

Note: The systematic use of vector increments (i.e. displacement $D X, D Y$ ) in constructing a picture symbol in the form of a subroutine is useful in displaying a picture with repeated symbols such as logic circuit elements.

### 3.0 TRANSFORMATION AND SIMPLE PERSPECTIVE PROJECTION

' A variety of transformations are provided in this package to make it easy for the programmer to specify and select different views of a picture with different scales and orientations. The set of transformations routines could handle two and three dimension views and are capable of 'scaling', 'translating' and 'rotating' graphical information. They also allow 'clipping' of those parts of a figure which fall outside a previously defined window. Note that for two dimensional transformations the $z$-parameter must be set to zero.

The start of an object at any display instance is represented by an accumulated transformation matrix $T M$ and a previous reference state is represented by the transformation matrix RTM. Both arrays must be declared by the user in the statement:-

COMMON/MATRIX/RTM $(4,4)$,TM $(4,4)$
Perspective views of 3-dimensional objects are useful in certain applications (e.g. architectural drawing). The use of homogeneous coordinates ( $x, y, z, t$ ) to define 3-dimensional objects allows either 'affine' or perspective transformations to be applied with equal ease. The 3-dimensional point (or vector) corresponding to ( $x, y, z, t$ ) is $(X, Y, Z)=\left(\frac{x}{t}, \frac{y}{t}, \frac{z}{t}\right)$. If $t \neq 0$ we usually normalise to $t=1$.

### 3.1 LINEAR TRANSFORMATION:-

The general linear transformation from point [ $X, Y, Z$ ] to [ $\left.X^{*}, Y^{*}, Z^{*}\right]$ is represented by

$$
\left[\begin{array}{lll}
X * & Y * & Z^{*}
\end{array}\right]=\left[\begin{array}{lll}
X & Y & Z
\end{array}\right] \quad\left[\begin{array}{llll}
\mathrm{S}_{x} & \mathrm{C}_{12} & \mathrm{C}_{13} & 0 \\
\mathrm{C}_{21} & \mathrm{~S}_{\mathrm{y}} & \mathrm{C}_{23} & 0 \\
\mathrm{C}_{31} & \mathrm{C}_{32} & \mathrm{~S}_{2} & 0 \\
\mathrm{~T}_{\mathrm{x}} & \mathrm{~T}_{\mathrm{y}} & \mathrm{~T}_{z} & 1
\end{array}\right]
$$

A user can therefore construct his own transformation(s) to suit his particular application. However, the most common operations which comprise any linear transformation are: scaling, translation, rotation, reflection and shear. These basic operations are available as library subroutines and may be called singly or in a prescribed sequence. Each subroutine call effectively defines a local matrix LTM which performs that particular transformation and is then concatenated in TM.
new $T M=T M$ * LTM
Note: It is under the user's control whether he/she wants to update the RTM by concatenation i.e.
new RTM=RTM * TM
3.1.1 SCALNG(SX,SY,SZ):- Scales the current point ( $x, y, z$ ) by the factors $\mathrm{SX}, \mathrm{SY}, \mathrm{SZ}$.
e.g. CALL SCALNG $(0.5,2.0,0$.
causes shrinking in the $x$-direction and expansion in the $y$ direction.
In general $\quad\left[\begin{array}{lll}X * & Y * & Z *\end{array}\right]=\left[\begin{array}{llll}X & Y & Z & 1\end{array}\right]\left[\begin{array}{llll}S_{X} & 0 & 0 & 0 \\ 0 & S_{y} & 0 & 0 \\ 0 & 0 & S_{z} & 0 \\ 0 & 0 & 0 & 1\end{array}\right]$
where [ $X * Y * Z^{*}$ 1] are the transformed co-ordinates of the point $\left[\begin{array}{lll}\mathrm{X} & \mathrm{Y} & \mathrm{Z} \\ \mathrm{l}\end{array}\right]$.
3.1.2 TRANSL(TX,TY,TZ):- Translates the current point (X Y Z) through the displacement $T X, T Y, T Z$.
e.g. a Triangle defined by its vertices $(20,0),(60,0)$, $(40,100)$ being translated 100 units to the right and 10 units up,

$$
\mathrm{T}_{\mathrm{x}}=100, \quad \mathrm{~T}_{y}=10
$$

CALL TRANSL(100.,10.,0.)
The resultant transformed points are $(120,10),(160,10)$, $(140,110)$.
3.1.3 ROTATE (RX, RY, RZ):- Rotation is assumed to be positive in a right-hand screw sense as one looks from the origin outward along the axis of rotation. The order in which the rotation is effected is
(1) angle RX about OX
(2) angle RY about OY
(3) angle RZ about $O Z$
where $R X, R Y, R Z$ are specified in degrees.
Note: rotations are not commutative. However, any order may be performed by using separate calls of the routine. e.g. $45^{\circ}$ rotation about $O Y$ followed by $30^{\circ}$ rotation about OX.

CALL ROTATE (0.,45.,0.)
CALL ROTATE (30., 0., 0.)

$$
\left.\begin{array}{rl}
{\left[\begin{array}{lll}
X * & Y * & Z^{*}
\end{array}\right]=\left[\begin{array}{llll}
X & Y & Z & 1
\end{array}\right]} & {\left[\begin{array}{cccc}
1 & 0 & 0 & \overline{0} \\
0 & \cos \theta & \sin \theta & 0 \\
0 & -\sin \theta & \cos \theta & 0 \\
0 & 0 & 0 & 1
\end{array}\right]}
\end{array} \begin{array}{cccc}
\cos \phi & 0 & -\sin \phi & 0 \\
0 & 1 & 0 & 0 \\
\sin \phi & 0 & \cos \phi & 0 \\
0 & 0 & 0 & 1
\end{array}\right] .
$$

$$
\times\left[\begin{array}{cccc}
\cos \psi & \sin \psi & 0 & 0 \\
-\sin \psi & \cos \psi & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

### 3.2 WINDOWING AND VIEWING:-

These basic facilities were described in sections 1.3 and 1.4. However, it is interesting to see that the combined window and viewport definitions constitute a linear (2dimensional) mapping of the problem area onto the screen and are effectively equivalent to two simple transformations, namely scaling and translation i.e.

$$
\begin{aligned}
& X_{S}=S_{x} X_{p}+T_{x} \\
& Y_{S}=S_{y} Y_{p}+T_{y}
\end{aligned}
$$

In matrix form (suppressing the $z$ component, which is unchaged)

$$
\left[\begin{array}{lll}
X_{s} & Y_{s} & 1
\end{array}\right]=\left[\begin{array}{lll}
X_{p} & Y_{p} & 1
\end{array}\right]\left[\begin{array}{lll}
S_{x} & 0 & 0 \\
0 & S_{y} & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
T_{x} & T_{y} & 1
\end{array}\right]=\left[\begin{array}{lll}
X_{p} & Y_{p} & 1
\end{array}\right]\left[\begin{array}{lll}
\mathbb{S}_{x} & 0 & 0 \\
0 & S_{y} & 0 \\
T_{x} & T_{y} & 1
\end{array}\right]
$$

where $X_{s}, Y_{s}$ are screen co-ordinates and $X_{p}, Y_{p}$ are picture co-ordinates. e.g. the mapping $W\left\{-1 \leqslant X_{p} \leqslant 1,0 \leqslant Y_{p} \leqslant 1\right\} \rightarrow V\left\{200 \leqslant X_{s} \leqslant 800,100 \leqslant Y_{s} \leqslant 400\right\}$ given in section 1.4 is represented by

$$
\begin{aligned}
& X_{s}=300 X_{p}+500 \\
& Y_{s}=300 Y_{p}+100
\end{aligned}
$$

and the (full) transformation matrix is $\left[\begin{array}{cccc}300 & 0 & 0 & 0 \\ 0 & 300 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 500 & 100 & 0 & 1\end{array}\right]$

### 3.3 CLIP (CLINE, $\mathrm{XO}, \mathrm{YO}, \mathrm{X1}, \mathrm{Y}, \mathrm{IREJ}):-$

This checks whether the current line segment $A B$ defined by its end points in CLINE (array of $2 \times 2$ ) is cut by the current window boundary defined by $\mathrm{XO}, \mathrm{YO}, \mathrm{X1}, \mathrm{Yl}$, and if so, returns in CLINE the co-ordinates of the intersection point'(s) $A^{\prime} B^{\prime}$ as shown.

If $A B$ lies completely outside the window the flag IREJ is set to 0. Otherwise, ( $A B$ is completely or partially accepted), IREJ=1. Thus, before using a primitive routine (i.e. MOVE or DRAW) the user normally calls


CLIP in order to limit the extent of the picture to a desired window. This routine may be useful in zooming a part of a picture on the viewport chosen on the screen, and consequently enlarging that part.
e.g. CALL CLIP (ALINE,-1.,-1.,1.,1.,IREJ)
where the window limit is given as $(-1,-1,1,1)$.

### 3.4 SIMPLE PERSPECTIVE PROJECTION:-

In perspective geometry no two lines are parallel. Thus a perspective transformation is frequently associated with a projection onto a plane such as $Z=c$ from a local centre of projection. The combination of perspective transformation with a projective transformation is often called 'perspective projection'. Therefore, a perspective projection represents a transformation from 3-space to 2-space. If the centre of projection is located at infinity, then the perspective projection is called 'Axonometric projection'. This type of projection is commonly used in engineering drawing. For perspective transformation the elements in the last column of the general $4 \times 4$ matrix mentioned above are not zero i.e.

Where $P_{x}, P_{y}$ are the reciprocals of the perspective viewing distances from the planes $y_{z}, z_{x}, x_{y}$ respectively.

A perspective projection onto the $\mathrm{z}=0$ "viewing" plane is

$$
\left[\begin{array}{lll}
x^{*} & y^{*} & z^{*} \\
t^{*}
\end{array}\right]=\left[\begin{array}{llll}
x & y & z & 1
\end{array}\right]\left[\begin{array}{llll}
1 & 0 & 0 & P_{x} \\
0 & 1 & 0 & P_{y} \\
0 & 0 & 1 & p_{z} \\
0 & 0 & 0 & 1
\end{array}\right]\left[\begin{array}{llll}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 0 & 0 \\
0 & 0 & 0 & 1
\end{array}\right]
$$

projection on $z=0$ plane.
3.4.1 PERSP (PX,PY,PZ):- A call to this routine would cause the perspective transformation to be performed. However, it can be seen that if the parameters PX,PY, PZ are all set to zero, the transformation matrix becomes a unit matrix, and any subsequent projection would be 'Axonometric projection'.
e.g. CALL PERSP (0.,0.,1.)
i.e. an object is viewed from a position 1 unit on the 2-axis. Therefore points on the object at infinity parallel to z-axis are transformed to a finite point on the $z$-axis.
3.4.2 PROJCT(NPLANE):- This performs the projective transformation from 3-space to 2-space. NPLANE $(=1,2$ or 3 ) specifies the co-ordinate plane ( $x=0$, $y=0$ or $z=0$ ) of projection.
e.g. CALL PROJCT (3)

### 3.5 TRANSFORMATION UTILITY ROUTINES:-

The following routines are provided for manipulating transformation matrices in several different ways:-
(1) Saving and Restoring a $4 \times 4$ matrix onto and from a stack respectively.
(2) Initialising a $4 \times 4$ matrix to unity or to a previously specified (transformation) matrix.
(3) Concatenating an $N \times 4$ matrix with a $4 \times 4$ matrix.
3.5.1 SAVMAT(A),RESTOR(A):- A one-dimensional stack is defined internally by the package. These routines can be useful when e.g. a sequence of transformations needs to be interrupted by some new transformations and is subsequently resumed.
e.g. CALL SAVMAT (RTM)
saves the reference transformation matrix (by pushdown) on the stack. Subsequently the reference matrix can be restored to its original state by

CALL RESTOR (RTM)
This POPS UP the elements of the matrix from the stack and puts them into the RTM matrix.
3.5.2 UNITY (A), SETMAT (A):-

UNITY(A): Initialises $A(4,4)$ to unit matrix (4×4)
SETMAT(A): Sets RTM (defined in COMMON/MATRIX/...) to A.
3.5.3 CONCAT(A,B,N):- Concatenates matrix (or vector)
$A(N \times 4)$ with matrix $B(4 \times 4)$ by multiplication $A * B$, and leaves the result in $A$.

### 4.0 CHARACTER AND TEXT HANDLING <br> These routines should help users to incorporate standard keyboard interaction in their Fortran programs.

### 4.1 SIMPLE INPUT-OUTPUT:-

4.1.1 TXGET(ICHAR):- Inputs the next character from the keyboard into ICHAR. Therefore, ICHAR would contain the ASCII equivalent of the character.
4.1.2 TXPUT(ICHAR):- Outputs ASCII character (ICHAR) to the screen. TAB is interpreted as a suitable number of spaces. RUBOUT is printed as several superimposed characters.

### 4.2 COMPOSITE INPUT-OUTPUT (TEXT HANDLING):-

4.2.1 TXLINE (STRING,N):- Inputs from the keyboard to the array STRING and echoes to the screen. STRING must be declared as logical*l array under 'UNIX' Fortran. N is the number of the array elements. If at any time the user types 'Rubout' the last character not yet deleted is overwritten on the screen and removed from STRING. Input continues until the user types CR, LF or EOT, or until there is no space left in STRING. On return STRING would contain the intended text.
4.2.2 MESSAG(TEXT):- Outputs "TEXT" to the screen, where TEXT is a sequence of hollerith characters terminated by the character '^'. Any occurrences of '/: are replaced by CR/LF (as it is convenient to start a message with $\%$.).

## e.g. CALL MESSAG ('HELLO^')


set to the binary equivalent of this integer.
Conversion stops whenever a non-numeric digit is met.
4.2.5 SPOUT(TEXT):- Removes spaces, line feeds, carriage returns, and EOT's from the TEXT parameter.
4.2.6 DTEXT(X,Y,TEXT,N):- Displays the 'TEXT' of N characters left-aligned on the scaled point ( $X, Y$ ) of the previously-defined window.

### 5.0 CURSOR AND MENU OPERATIONS:-

The following set of routines are for displaying menus and choice of cursor therein:-
5.1 MNOPEN(X,Y,MNO):-

Announces that a menu is to be displayed whose top lefthand corner is to be at screen co-ordinates $\mathrm{X}, \mathrm{Y}$. (MNO is the menu number (= 1 or 2 ) for the current display instance. At most two menus are allowed in the present implementation.
e.g. CALL MNOPEN $(800 ., 200 ., 1)$
5.2 MNTEXT(TEXT,N,MNO):-

Puts up text containing $N$ characters as the next line of the menu MNO.
e.g. CALL MNTEXT("ITEM",4,1)
5.3 MNDISP (MNTXT, ITEMNO, LEN,MNO):- Displays a complete menu whose text is defined by a DATA statement as MNTXT, with number of items given by ITEMNO. LEN specifies the character length of each item. NMTXT must be declared in UNIX Fortran as a 'Logical*1' array.
5.4 MNPICK (I,ICHAR,MNO):- Puts up the cursor and returns in I the index of the line chosen (i.e. Item number) by the
user, and the character (ICHAR) typed in. It retries until a valid line is picked up. The item picked up is marked by an arrow.
5.5 TXCURS (X,Y,ICHAR):- Displays the cursor and returns the window co-ordinates of the cursor ( $X, Y$ ) and the character (ICHAR) typed in. . This would enable the user to put graphical information into a program.
5.6 CURPOS (X,Y):- Positions the 'Alpha' cursor at the specified window co-ordinates ( $X, Y$ ) at which the user might display some textual information. (Note: this routine would make the Tektronix 4010 compatible with the GT42 operating as an emulated T4010).
5.7 FRAME (X,Y,NC):- Closes the menu with a rectangle drawn round it, in order to distinguish it from other textual information that might appear on the screen. $X, Y$ specifies the top left-hand corner of the rectangle, NC specifies the number of items in the menu. The following two routines interpret the screen co-ordinates as character positions and vice-versa.
5.8 CHTOXY(NLINE,NCHAR, IX, IY):- Converts the character coordinates to the screen co-ordinates of the bottom lefthand corner of the character. The character co-ordinates are represented by line number NLINE, and character number (in the line) NCHAR.
5.9 XYVOCH(IX, IY, NLINE, NCHAR, IA, IB):- Given screen coordinates (IX,IY) this sets (NLINE,NCHAR) to indicate the corresponding character co-ordinates (the top lefthand character position 0,0). Also (IA,IB) are set to the position of this point within the indicated
character (in $0: 13,0: 21$, the character itself being in $0: 10,0: 14)$.


### 6.0 MISCELLANEOUS

### 6.1 OVRLAY(FILENAME):-

Overlays the calling process with the named file, then transfers control to the beginning of the core image of the file. There can be no return from the file since the calling core image is lost. Thus, application programs larger than the core memory available could be logically segmented into a number of smaller modules and linked by a sequence of overlays.
6.2 RMFILE(FILENAME):- Removes the named file from the current directory.

Note: the above two routines are 'UNIX' dependent.
6.3 WERROR(I):- Displays 'ERROR MESSAGE' and the value of I indicating the error number.
6.4 IREM(I, J):- Returns the positive value of I mod $J$, where I, J are integers.
7.0 LINKING OF LIGHT LIBRARY SUBROUTINES WITH USER PROGRAM

To incorporate the LIGHT subroutines in his program the user must type the following UNIX command FC USERPROG -LL

## APPENDIX 2

IDF - program modules listing

## APPENDIX 2.1

THE NUMERICAL ALGORITHMS

C THIS IS THE HAIN FROGFAH SEGMENT WHICH CALLS THE NUKERICAL ALGORITHMS C IMCORFORATEI IN THE EXPLICIT F'ACKAGE.

C
C
C
C******** MAIN FROGRAM SEGMENT FOR IMNOKING THE NUMERICAL ALGORITHHS**** C

C I/O COMMON DATA AREA
COMMON/LATSUP/NFFS, NFI (50), IFREES, $X(50), Y(50), L(50), I H(5), M(5)$
8
COMMON/CURVEFIT/COEF (50; 6 ) , XCORD (200), YCORD (200)
DATA MOTL2,MODL4,DATSF,OUTCRV, JOINFL/"MOE2", "KOD4" "DATSUFFL"
" "OUTCNV", "HONFLEE"
DATA MOUC5/"MODS"/
INTEGER SUBSET
LOGICAL*1 HOLL2 (10), MODL4 (10), DATSP (10), OUYCFU (10), NOINFL (10)
LOBICAL*1 HODL5 (10)
BIMENSION XO(50), YO(50)
CALL RLCOM1
IN $=5$
IOUTm6
CALL FEMENK (XO,YO)
CALLL INTRPT (INTPNT, NF'S, NPI; XO, YO)
CALLL JONSUE(IENR,LSUM)
IF (IERR.EQ.1)GOTO 2
WFITE (IOUT,10)
10. FORMAT 《FLEEASE WAIT,FIT IS BEING COMPUTED")

NC=4
$\operatorname{GOTO}(31,32,33,34,35,36,38)$, METHOD

## C

C NEWTON DIUIUED DIFFERENCES METHOD (THE CLASSICAL INIERFOLATION)
31 CALL NEWTON (NFS, NFI , XO, YO, XCORD, YCORD, COEF , KETHOD)
NC=1
GOTO 3
C
C PIECEWISE QUINTIC INTEFFFQLATION FOLYNOKIAL (MAUD ALGORITHIM)
32 CALL PIECWS (NPS, NFL, XO, YO, XCORD, YCORD, CDEF, EOLND, IE, HETHOD) NC=6
GOTO 3
C
C CUBIC SPLIAE (2ND HERU. BOLNDAKY CONDITION)
33 CALL CUEICI (NF'S, NPI , XO, YO, XCORD, YCORD, COEF, BOUND, METHOD) GOTO 3
c
C CUBIC SFLINE (2NI DERV. EOUNDARY CONIITION *)
34 CALLL CUBICZ (NFS, NFI , XO, YO, XCOND, YCOKD, COEF, BOLND, METHOD) goto 3.

C
C CUBIC SFLINE (1ST DERV. BOLNDARY CONDITION)
35 CALL CUBICZ (NPS, NFI , XO, YO, XCORII, YCOKD, COEF BOUND, METHOD) GOTO 3
C
C FEKIODIC CUBIC SFLINE "CUEIC F"
36 CALL CUBICF (NPS,NFI, XO,YO, XCORD, YCORD, COEF , BOLNDD, HETHOD) GOTO 3

C

C CONTROL END CONDITION CUBLC SFLINE

SUEFOUTINE NEWTON ( $N, N 1, X 1, Y 1, X X, Y Y, C, M)$
DIMENSION $N 1(1), X 1(1), Y 1(1), X X(1), Y Y(1), C(50,6)$
C COMPUTE THE POLYNOHIAL COEFFICIENT
$N 2=N-1$
DO $1 \mathrm{~K}=1$, N 2
J=N-K
$C(J+1 ; 1)=(Y 1(J+1)-Y 1(J)) /(X 1(J+1)-X 1(J))$
1 CONTINUE
$55 \quad C(1,1)=Y 1(1)$
$\mathrm{N} 3=\mathrm{N}-2$
DO $2 \mathrm{~J}=1 \mathrm{~N}$ N3
$K=j+2$
DO 3 L=K,N
$I=N-L+K$
$X X X=X 1(I)-X 1(I-(J+1))$
$C(I, 1)=(C(I, 1)-C(I-1 ; 1)) / X X X$
3 CONTINUE
2 CONTINLE
C EUALLUTE INTEAPOLATION FLUNCTION
$66 \quad I F=1$
10 $41=1, \mathrm{~N} 2$
$T 1=X 1(1+1)-X 1(I)$
$\mathrm{F} 1=1 /\left(\mathrm{N}_{1}(1)+1\right)$
$I F 1=I F+N 1(I)+1$
$X X(I P)=X 1(I)$
$\mathrm{Z}=\mathrm{X} 1$ (I)
$X X(I P I)=X I(I+1)$
$Y Y(I F)=Y 1(1)$
$Y Y(I P 1)=Y 1(I+1)$
N11=N1〈I)
$005 K=1, N 11$ $X X(I F+K)=Z+K 1$ $Z=Z+F i$ $A=C(N, 1)$ W 7 L=1, N2 $J m=N-L$ $A=C(J, 1)+(Z-X 1$ (J) ) *A
7 . CONTINUE
$77 \quad Y Y(I F+K)=A$
5 CONTINGE
IP=IP1
4 CONTINUE

RETURN
END
C
C *********PIECEWISE FOLYNOMIAL. INTERFOLATION********************
C
SUBROUTINE FIECWS ( $N, N 1, X 1, Y 1, X X, Y Y, C, E, I E, M$ )
DIMENSION N1 (1), X1 (1),Y1(1),XX(1),YY(1),B(1),C(50,6),IE(1)
CALL MAUDFW ( $N, X 1, Y 1, E, C, I E$ )
C COMPUTE FUNCTION UALLES(I.E INTERFOLATED FOINTS)
CALL COKFIT ( $\mathrm{N}, \mathrm{N} 1, \mathrm{XI}, \mathrm{Y} 1, \mathrm{XX}, \mathrm{YY}, \mathrm{C}, \mathrm{M}$ )
RETUFN
END
c
C ***************PIECEWISE FOLYMOMIAL INTERFOLATION*************** C (MAUD METHOD)
C
SUBROUTINE MAUDFW(N,X1,Y1,E,C,IE)
DIMENSION XI (1), Y1 (1), B(1), C $(50,6)$, IE (1)
If $=1$
N2 $=\mathrm{N}-1$
DO $1 \mathrm{I}=1, \mathrm{~N} 2$
F $=1$.
$\mathrm{S}=1$.
F3=1.
F1: 5
F2 $=.5$
IF(IE(1). BT. 20 ) GOTO 20
1B=1
IE1=IE(1)-10
GOTO 30
$20 \quad$ IB=0
IE1=IE(1)-20
C $15 T$ INTREVAL , NOT EQLAL SFACING
30 IF (IB.ER.O..AND.I.EQ.1.)GOTO 21
C LAST INTEKUAL,NOT EQLAAL SFACING
IF (IB.EQ.O..AND.I.EQ.N2) GOTO 28
C $15 T$ INTERNAL, EQLAL SFACING
IF (IB.EQ.1..AND. I.EQ.1.)GOTO 21
C LAST INTERUAL, EOLAL SPACING
IF (IB.EQ.1..AND.I.EQ.N2) GOTO 28
IF (IB.EQ.1.) GOTQ 41
C COMPUTE RATIOS OF X-DIFFIRIS
C IN ANY INTERUAL OTHER THAN IST OR LAST
$E 1=X 1(1)-X 1(1-1)$
$E 2=X 1(1+1)-X 1$ (I)
$E 3=X_{1}(1+2)-X_{1}(1+1)$
$R=E 1 / E 2$
S=E3/E2
F1=1./( $\mathrm{K} *(\mathrm{R}+1)$ )
F2=1./(S* (S +1$)$ )
$F 3=(K+5+2) /.\left(\left(K^{2}+1\right) *(S+1)\right)$
C COMFUTE THE DIFFERENCES
$41 \mathrm{D} 1=\mathrm{Y} 1(1)-\mathrm{Y}(\mathrm{I}-1)$
$\mathrm{D} 2=\mathrm{Y} 1(\mathrm{I}+1)-\mathrm{Y}(\mathrm{I})$
$D 3=Y 1(I+2)-Y 1(I+1)$
111 TOFF1*D1+F2*U3-F3*D2.
GOTO 51
c Comput difference at first interval.
$21 \quad \mathrm{~F}=1$.
F1=.5
E2 $=\times 1(1+1)-X_{1}(1)$
$E 3=X 1(1+2)-X 1(I+1)$

SxE3/E2
F2=1./(S* (S+1))
F3 $=(f+S+2) /((k+1) *(S+1))$
12=Y1 (I+1)-Y1 (I)
$113=Y_{1}(1+2)-Y 1(I+1)$
GOTO (61,62,63), IE1
C ENCASTRED END CONDITION
$61 \quad$ U1 $=\mathrm{E}$ (1)
$\mathrm{T}=\mathrm{FH} 2-\mathrm{D} 1$
6010111
C RELLAXED END CONDITION
$62 \quad \mathrm{D} 1=\mathrm{I} 2$
$T 1=0$.
goto 111
C PANABOLIC END CONDITION
$63 \quad 10=0$.
D1 $=2$. *D2- 103
11 m D3-122
601051
C CHAFUTE UIFFEFENCES AT LAST INTERVAL
$28 \quad E 1 m \times 1(I)-X 1(I-1)$
$E 2=X 1(I+1)-X 1$ (I)
R=E1/E2
F1=1./(R* (R+1.) )
S=1.
F2=0.5
$F 3=(K+S+2) /.((N+1) *.(S+1)$.
31 D1mY1(I)-YI(I-1)
D2=Y1 (I+1)-Y1 (I)
G010(71,72,73), IE (2)
C ENCASTRED END CONDITION(LAST ENT)
71 D3~E (2)
goro 111
C RELAXED END CONDITION
72 133:1)2
G0T0 111
C PAARABOLIC END CONDITION
73 TOmO.
GOTO 51
C COMPUTE THE DESIRED COEFFICIENTS FOF EACH INTERVAL
$51 \quad C(I, 1)=Y 1(I)$
$C(I, 2)=(D 1+[12 * R * R) * F L$
IF (I.NE.1) GOTO 55
$C(I, 3)=5.5 * 11$
GOTO 66
$55 \quad C(1,3)=(D 2 * R-D 1) * F 1$
$66 C(I, 4)=-3 . * T 0$
$C(I, S)=2 S . * T 0$

1 CONTINLE
RETURN
END
C
C \#**********CUBIC FLINE (2ND DERU. BOUNDAFY CONDITION) ***********
C
SUBKOUTINE CUBICI (N,N1;XI,Yi,XX,YY,C,B,M)
UIMENSION $N 1(1), X 1(1), Y 1(1), X X(1), Y Y(1), C(50,6), E(1), Y 2(50)$
CALL GAUSS1 ( $\mathrm{N}, \mathrm{X} 1, \mathrm{Y} 1, \mathrm{Y} 2, \mathrm{~B}$ )
CALL COEFNT ( $N, X 1, Y 1, Y 2, C$ )
CALL COMFIT ( $N, N 1, X 1, Y 1, X X, Y Y, C, H$ )
FETUFN
END

## C

C *************** GAUSSIAN ELIMINATION FOF CUGIC 1 *************
c
SUBFOUIINE GAUSS1 ( $N, X_{1}, Y 1, Y 2, B$ )
DIMENSION X1(1) ,Y1(1),Y2(1),F(50),G(50),B(1)
$Y 2(1)=B(1)$
$Y 2(N)=B(2)$
$\mathrm{N} 1=\mathrm{N}-1$
$G(1)=0$.
$F(1)=0$.
[0 $2 K=1, N 1$
J2 $=K+1$
$H 2=X 1(52)-X 1(K)$
R2"
IF (K.EQ.1) 60101
$2=1 . /(2 . *(H 1+H 2)-H 1 * G(J 1))$
G(K) $=2 * H_{2}$
$H=6 . *(R 2-R 1)$
IF (K.EQ. 2) H=H-H1*Y2(1)
IF (K.EQ.N1) H=H-H2*Y2 (N)
$F(K)=2 *(H-H 1 * F(J 1)$ )
1
J1=K
$\mathrm{H} 1=\mathrm{H}_{2}$
$\mathrm{k} 1 \times \mathrm{FR} 2$
2 CONTINUE
$Y 2(N 1)=F(N 1)$
IF (N1.LE.2) RETURN
$\mathrm{N} 2=\mathrm{N} 1-1$
DO $3 \mathrm{~J} 1=2$, N2
$K=N-J 1$
$Y 2(K)=\mathrm{FF}(\mathrm{K})-G(K) * Y 2(K+1)$
3 CONTINUE
RETURN
ENB
C
C *********CUBIC SFLINE (2ND DERV. BOLNDARY CONDITION)*******
C. [Y2(1) $=\mathrm{U} * Y 2(2) \ldots . . . U Y 2(N-1)=Y 2(N)]$
c
SUEROUTINE CUBIC2(N,N1,X1,Y1,XX,YY,C,B,K)
DIMENSION N1 (1), X1 (1),Y1(1),XX(1),YY(1),C(50,6),B(1),Y2(50)
CALL GAUSS2 ( $\mathrm{N}, \mathrm{X} 1, \mathrm{Y} 1, \mathrm{Y} 2, \mathrm{E}$ )
CALL COEFNT ( $\mathrm{N}, \mathrm{XX}_{1}, \mathrm{Y} 1, \mathrm{Y} 2, \mathrm{C}$ )
CALL COMFIT $\left(N, N 1, X_{1}, Y 1, X X, Y Y, C, H\right)$
RETURN
END
c

c

```
SUBROUTINE GAUSSS(N,X1,Y1,Y2,B)
DIMENSION X1(1),Y1(1),Y2(1),F(50),G(50),B(1)
N1=N-1
B(1)=0.
F(1)=0.
F2=2.
LO 2 K=1,N1
J2=K+1
H2=X1(J2)-X1 (K)
K:2=(Y1 (J2)-Y1 (K))/H2
IF(K.EQ.1). G010 1
F1m2.
IF(K.EQ.2) F1=2.*B(1)
```

```
    IF(K.EQ.N1)F2=2.*B(2)
    Z=1./((F1-G(J1))*H1+F2*H2)
    G(K)=2*H2
    F(K)=Z*(6.*(F2-F(1)-H1#F(J1))
    l
    J1#K
        H1=H2
        た1"た2
        CONTINUE
        Y2(N1) mF (N1)
        IF(N1.LE.2) GOTO 4
        N2=N1-1.
        IO 3 J1=2,N2
        K=N-J1
        Y2(K)=F(K)-G(K)*Y2(K+1)
        CONTINUE
        Y2(1)=B(1)*Y2(2)
        Y2(N1)=E (2)*Y2 (N1)
        FETUFN
        ENT
    C
    C ***********CUEIC SFLINE(1ST IERU. EOUNDARY CONUITION)**********
C
    SUBROUTINE CUBICZ(N,N1,X1,Y1,XX,YY,C,B,M)
    DIMENSION N1 (1),X1(1),Y{1(1),XX(1),YY(1),C(50,6),B(1),Y2(50)
    CALL GAUSSS3 (N,X1;Y1,Y2,B)
    CALLL COEFNT (N;XI,Y1,Y2,C)
    CALL COMFIT (N,NI,XI,Y1,XX,YY,C,M)
    RETLNON
    END
    C
    C ##m#*********CUBIC 3 .. GAUSSS3**********************************
C
    SUEFOUTINE GALSSS3 (N,X1;Y1;Y2,B)
    DIMENSION X1 (1),Y1(1),Y2(1),B(1),F(50),G(50)
    Y2(1)=E(1)
    Y2(N)=E (2)
    M1 mN-1
    J1=1
    H1=0.
    F(1)=0.
    G(1)=0.
    F1-Y2(1)
    DO 3 K=1,N
        IF(K.LE.N1) GOTO 1
        H2=0.
        R2=Y2(N)
        80TO 2
        j2=K+1
        H2=X1 (J2)-X1 (K)
        R2= (Y1 (N2)-Y1 (K))/H2
        Z*1./(2.*(H1+H2)-H1*G(J1))
        G(K)=2*H2
        F(K)=2*(6.*(F2-R1)-H1*F(J1))
        Ji=K
        H1mH2
        R1=F2
    CONTINHE
    YZ (N) =F (N)
    DO 4 J1=1,N1
        K=N-J1
        Y2(K) =F F(k)-G(K)*Y2(K+1)
    CONTINUE
```

RETURN
END
C
C $\# * * * * * * * * * * P E R I O D I C$ CUBIC SFLINE*************************
C
SUEFOUTINE CUBICP ( $N, N 1, X 1, Y 1, X X, Y Y, C, B, M)$
DIKENSION $N 1(1), X 1(1), Y 1(1), X X(1), Y Y(1), C(50,6), B(1), Y 2(50)$
CALL GAUSSP ( $\mathrm{N}, \mathrm{X}_{1}, \mathrm{Y} 1, \mathrm{Y} 2, \mathrm{~B}$ )
CALL COEFNT ( $\mathrm{N}, \mathrm{XX}_{1}, \mathrm{Y} 1, \mathrm{Y} 2, \mathrm{C}$ )
CALL COMFIT ( $N, N 1, X 1, Y 1, X X, Y Y, C, M)$
RETURN
END
C

c
SUEFDUTINE GAUSSF ( $\mathrm{H} / \mathrm{X} 1, \mathrm{Y}_{1}, \mathrm{Y}_{2}, \mathrm{~B}$ )
C NORMALISED FERIODIC "TRIDIAGONAL" ALGORITHM FOR THE SOULTION OF
C factorisation of the afitiay a by normalised algofithm
C A SET OF LINEAR EQUATION (REFC.DR. BENSON FH.D THESIS)
C COMFUTE D(1) TERE ARE N-1 UNKNOWN VALUES IN Y2(N-1) 2ND DERU.
C WHERE A=DT'TD WHICH FACTORISED INTO
DIMENSION X1 (1),Y1 (1),Y2(50), $\mathrm{B}(1), \mathrm{D}(50), \mathrm{E}(50), F(50)$
$01=\times 1(2)-\times 1(1)$
$02 \times \times 1(N)-\times 1(N-1)$
B1=2.*(01+02)
$D(1)=$ SQRT (B1)
C COMPUTE ALL OTHER D'S UF TO D(N-2)
$\mathrm{N} 2=\mathrm{N}-2$
HO 1 J=2,N2
$\mathrm{C} 1=\mathrm{XI}(\mathrm{J})-\mathrm{XI}(\mathrm{J}-1)$
$01=\mathrm{Cl}$
02mx1 (J+1)-X1(J)
E1=2.*(01+02)
D ( J$)=$ SORT ( $\mathrm{B} 1-\mathrm{C} 1 / \mathrm{D}(\mathrm{J}-1)$ )
1 CONTINLE
C COMPUTE E'S
$\mathrm{N} 3=\mathrm{N}-3$
to $2 \mathrm{~J}=1$, N3
$\mathrm{C}=\mathrm{XI}(\mathrm{J}+1)-\mathrm{XI}(\mathrm{J})$
$E(J)=[/(D(J) * D(J+1))$
2 CONTINUE
C COMFUTE THE $D(N-1)$ the Last in the factorisation as there are only
C. N-1 LHKNOUN

S1=1.+E (N-4) *E (N-4)
N5: $\mathrm{N}-5$
DO 3 J=N5,1,-1
S1m1n+E(J)*E(J) *S1
3 CONTINUE
52=1.
DO $4 \mathrm{~J}=1, \mathrm{~N} 3$
4 S2*S2*E(J)
$01=\times 1(N-1)-\times 1(N-2)$
C1=01
$02=\times 1(N)-\times 1(N-1)$
C2 $=02$
$B 1=2 . *(01+02)$
$\mathrm{U}(\mathrm{N}-1)=\operatorname{SaKT}(E 1-(\mathrm{C} 2 / \mathrm{D}(1)) * * 2 * \operatorname{Si}-(\mathrm{C} 1 / \mathrm{D}(\mathrm{N}-2)+((-1) * *(N-1) * S 2 * C 2) /$
\& $\quad(1)$ **2)
$E(N-2)=C 1 /(D(N-2) * D(N-1))$
C COMFUTE F'S
$F(1)=C 2 /(1)(1) * D(N-1))$
HO $5 J=2, N 2$

## 5

$F(J)=E(J-1) * F(J-1)$
C COMFUTE THE INTERHEDIATE SOLLTION T'H=G,SOLUE FOR H AND STORE IN YZ(J)
C WHERE G=K/L
R1: $=Y 1$ (2)-Y1 (1)
R2ㅍT1 (N)-Y1 (N-1)
Q1 $=\mathrm{X}_{1}(2)-\mathrm{Xi}_{1}(1)$
Q2피 (N)-X1 (N-1)
K1=6.* (R1/01-Fi2/Q2)
$Y 2(1)=K 1 / D(1)$
DO $6 \mathrm{~J}=2, \mathrm{~N} 2$
F1: $=Y 1(J)-Y 1(J-1)$
$R 2=Y 1(J+1)-Y 1(J)$
Q1 $=X 1(J)-X 1(J-1)$
02mX1 ( $1+1$ )-X1 (J)
K1 $=6$. * (R2/Q2-F1/Q1)
$Y 2(J)=K 1 / D(J)-E(J-1) * Y 2(J-1)$
6 CONTINLE
$5=0$.
C COMPUTE LAST H AS Y2 (N-1)
U $7 \mathrm{~J}=1, \mathrm{~N} 2$
$5 \mathrm{~S} 5+F(\mathrm{~J})$ ※Y2 (J)
$\mathrm{R} 1=\mathrm{Y} 1(\mathrm{~N}-1)-\mathrm{Y} 1(\mathrm{~N}-2)$
$R 2=Y 1(N)-Y 1(N-1)$
$01=X 1(N-1)-X 1(N-2)$
$02=\times 1(N)-X 1(N-1)$
$K 1=6 . *(K 2 / Q 2-R 1 / Q 1)$
$\mathrm{Y} 2(\mathrm{~N}-1) \approx \mathrm{K} 1 / \mathrm{D}(\mathrm{N}-1)-\mathrm{E}(\mathrm{N}-2) * Y 2(\mathrm{~N}-2)-5$
C CONPUTE THE FINAL SOUKTION Y2(J) AS 2ND DEKU
[0 $8 \mathrm{~J}=\mathrm{N} 2,1,-1$
$8 \quad Y 2(J)=Y 2(J)-E(J) * Y 2(J+1)-F(J) * Y 2(N-1)$
N1=N-1
DO 9 J=1, N1
$9 \quad Y 2(J)=Y 2(J) / D(J)$
$Y 2(N)=Y 2(1)$
RETUFW
END
C

C
SUEROUTINE COEFNT ( $N, X 1, Y 1, Y 2, C$ )
DIMENSION $X 1(1), Y 1(1), Y 2(1), C(50,6)$
$N 2=N-1$
C SPLINE COEFFICIENT FER INTERUAL
LO $1\left[=1, N_{2}\right.$
$\mathrm{T} 1=\mathrm{X} 1(1+1)-\mathrm{X} 1(\mathrm{I})$
T2=Y1(1+1)-Y1(I)
D1 $=Y 2(I+1)-Y 2(I)$
$\mathrm{U} 2 \mathrm{~m} Y 2(\mathrm{I}+1)+2 . * Y 2(1)$
$C(I, 1)=Y 1(I)$
$C(I, 2) * T 2 / T 1-(T 1 * D 2) / 6$. $C(1,3)=\gamma 2(1) / 2$. $C(I ; 4)=141 /(6 . * T 1)$
1 CONTINHE
EETURN
END
C
C. $\# * * * * * * * * *$ COMPUTE FLNCTION UALUES $* * * * * * * * * * * * * * * * * * * * * * * * * * * ~$ C

SUBROUTINE COMFIT ( $N, N 1, X 1, Y 1, X X, Y Y, C, M)$
UIMENSION $N 1(1), X 1(1), Y 1(1), X X(1), Y Y(1), C(50,6)$
$N 2=N-1$
IP $=1$

C COMFUTE THE INTERFOLATED ORDINATES
DO $11=1, \mathrm{H}_{2}$
CALL INTFLT (I,IF',N1,X1,Y1,XX,YY,C,M)
1 continue RETUFN END

## C

C**************EVALLUATE THE INTERFOLANT FUNCTION UALUES**********
c

$$
\text { SUBKOUTINE INTFLT }(I, I P, N 1, X 1, Y 1, X X, Y Y, C, K)
$$ UIMENSION N1 (1), XI (1), Y1 (1), XX(1), YY (1), C( 50,6 ) INTFIN1 (I)

$T 1=X 1(I+1)-X 1(1)$
R1: $=1 /($ (INTF +1 )
IF1=IP + INTF +1
2=x1 (1)
$X X(I P)=X 1(1)$
$X X(I F 1)=X 1(1+1)$
YY(IF) $=Y$ (I)
$Y Y(I P 1)=Y 1(I+1)$
DO $2 \mathrm{~J}=1$,INTP
$X X(I P+J)=Z+R 1$
Z $\times 2+R 1$
IF (H.EQ.2) GOTO 3
$T=2-X X(1 F)$
$Y Y(I P+J)=C(1,1)+T *(C(1,2)+T *(C(1,3)+1 * C(1,4)))$
2 CONTIANE
IP=IP1
EETURN
$3 \quad H=X X(I F 1)-X X(I F)$
$T=(Z-X X(I F)) / H$
YY(IF+J) $=C(I, 1)+T *(C(1,2)+T *(C(I, 3)+T *(C(I, 4)+T *(C(1,5)+T * C(I, 6)))))$
GOTO 2'
END
C
C **************CUBIC SFLINE WITH UARIABLE END CONDITION**************
C
SUBROUTINE CSPLEN(N,N1,XI,Y1,XX,YY,C,E,IE,M)
DIMENSION $N 1$ (1), X1 (1),Y1(1),XX(1),YY(1),C(50, 6$), B(1), I E(1)$
DIMENSION EX (50), C1 (50), D(50), $\mathrm{S}(50)$, DX $(50)$
CALL GEMXFF $\left(N, X_{1}, Y 1, D X\right)$
Si $=D \times(2) / D \times(3)$
S2=DX(N)/DX(N-1)
C MAIN PRGGRAM
CALL GENHKAT ( $N, S 1, S 2$, DX, BX,C1,D,IE,EX,A)
CALL GENFHS ( $\mathrm{N}, \mathrm{S} 1, \mathrm{~S} 2, \mathrm{X}, \mathrm{Y} 1, \mathrm{E}, \mathrm{EX}, \mathrm{S}, \mathrm{IE}$ )
CALL GAUSSC ( $N, E X, C 1, D, S, I E, E X, A$ )
CALL ECCOEF ( $\mathrm{N}, \mathrm{X} 1, \mathrm{Y} 1, \mathrm{C}, \mathrm{S}, \mathrm{DX}$ )
CALL COKFIT ( $\mathrm{A}, \mathrm{N} 1, \mathrm{XI}, \mathrm{Y} 1, \mathrm{XX}, \mathrm{YY}, \mathrm{C}, \mathrm{H}$ )
RETURN
END

## C


c.

1
SUBROUTIME GENXFR ( $\left.N, X_{1}, Y_{1}, D X\right)$
DIHENSION XI (1),Y1(1),DX(1)
DX(1)=0.
$\mathrm{N} 1=\mathrm{N}-1$
DO $1 \mathrm{~K}=1, \mathrm{~N} 1$
IX $\mathrm{X}(\mathrm{K}+1)=\mathrm{X}(\mathrm{K}+1)-\mathrm{XI}(\mathrm{K})$
CONTINLE
RETURN

END
C

c
SUEFOUTINE GENKAT ( $N, S 1, S 2, D X, B X, C 1, D, I E, E X, A)$ LIMENSION DX(1), BX(1),C1(1),D(1),IE(1)
$N 1=N-1$
$B X(1)=0$. $\mathrm{E}(\mathrm{N})=0$. C1(1) $=1$. $\mathrm{Ci}(N)=1$. $E X=0$.
$A=0$.
GOTO (1, 2, 3, 4), IE(1)
1 : $D(1)=0$. GOTO 5
$2 \quad D(1)=0.5$ 60105
$0(1)=1$.
60105
$4 \quad D(1)=1 .-51 * 51$
EX=-S1*S1
5 GOTO ( $6,7,8,9$ ), IE (2)
$6 \quad B X(N)=0$.
GOTO 10
$7 \quad \mathrm{BX}(\mathrm{N})=2$.
$C 1(N)=4$.
goto 10
$8 \quad B X(N)=1$.
goto 10
$9 \quad E X(N)=1 .-S 2 * S 2$
A $=5$-52*52
10 DO $11 \mathrm{~J}=2, \mathrm{~N} 1$
BX(J) $=\operatorname{DX}(J+1)$ $C 1(J)=2 . *(D X(J)+D X(J+1))$ $\mathrm{D}(\mathrm{J})=\mathrm{DX}(\mathrm{J})$
11 CONTINUE RETURN END
C

c
SUBROUTINE GENFHS (N,S1,S2,X1,Y1,B,DX,S,IE) DIMENSION XI (1),Y1(1),B(1),DX(1),S(1),IE(1) $\mathrm{N} 1=\mathrm{N}-1$ GOTO (1, 2, 3, 4), IE (1)
$S(1)=E(1)$
$S(N)=E(2)$ GOTO 5
$S(1)=-(1.5 / D X(2)) *(Y 1(2)-Y 1(1))$ $S(N)=(6 . / D X(N)) *(Y 1(N)-Y 1(N-1))$ GOTO 5
$S(1)=(2 . / \mathrm{DX}(2)) *\left(\mathrm{Y}_{1}(2)-\mathrm{Y}(1)\right)$ $S(N)=(2 . / D X(N)) *(Y 1(N)-Y 1(N-1))$ GOTO 5
$S(1)=(2 . / D X(2)) *(-Y 1(1)+(1 .+S 1 * * 3) * Y 1(2)-(S 1 * * 3) * Y 1(3))$ $S(N)=(2 . / D X(N)) *((S 2 * * 3) * Y 1(N-2)-(1 .+S 2 * * 3) * Y(N-1)+Y 1(N))$
5 Lí $11 \mathrm{Im} 2, \mathrm{~N} 1$ $\mathrm{S}(\mathrm{I})=3 *(\mathrm{DX}(\mathrm{I}+1) * \mathrm{DX}(\mathrm{I}+1) *(\mathrm{Y} 1(\mathrm{I})-\mathrm{Y} 1(\mathrm{I}-1))+\mathrm{DXX}(\mathrm{I}) * \mathrm{DX}(\mathrm{I}) *(\mathrm{Y}(\mathrm{I}+1)-\mathrm{Y} 1(\mathrm{I})))$ $S(I)=S(1) /(D \times(1+1) * D X(I))$
11 CONTINUE return

END
C
 *ADAPTATION OF QUIN DIAGONAL MATEIX*

C
SUBROUTINE GAUSSC ( $N, B X, C 1, D, S, I E, E X, A)$
BIMENSION EX(1),C1(1),D(1),S(1),IE(1)
N1 $=\mathrm{N} \boldsymbol{N}-1$
Z=1./E1(1)
D(1) $m$ D(1) *Z
S(1) $=\mathrm{S}(1) * 2$
IF (IE (1).EQ.4)EX=EX*Z
HO 1 I $=2, N 1$
$11=1-1$
$12=I+1$
Z=1./(C1 (I)-BX(I)*D(II))
IF (I.EQ.2) D (I) $=(D(I)-E X(I) * E X) * Z$
IF (I.NE.2)D(I) $=D(I) * Z$
$S(1)=\langle S(I)-E X(I) * S(I I\rangle) * Z$
IF (I2.LT.N) GOTO 1
$S(12)=S(12)-A * S(11)$
$B X(I 2)=B X(12)-A * D(I 1)$
1
CONTINUE
$S(N) \omega(S(N)-B X(N) * S(N-1)) /(C 1(N)-B X(N) * D(N-1))$
DO $2 \mathrm{~K}=1, \mathrm{Ni}$
$1=N-K$
IF (I.NE.1)S $(I)=S(I)-D(I) * S(I+1)$
IF (I.EQ. 1) $S(I)=S(I)-D(I) * S(I+1)-E X * S(I+2)$
2 CONTINUE RETURN END
C

C (WITH UAFIIABLE END CONDITION)
C
SUBFTOUTINE ECCOEF $(N, X 1, Y 1, C, S, D X)$
HIMENSION XI (1),Y1 (1),C(50,6),S(1),DX(1)
M1 $=12-1$
DO 1 I=1, N1
$C(I, 1)=Y 1(I$
$C(1,2)=S(1)$
$C(I, 3)=(3 . /(D X(I+1) * I X(I+1))) *(Y 1(I+1)-Y I(I))-(1 . / D X(I+1)) *$ $(S(1+1)+2 . * 8(1))$
4
$C(1,4)=-(2 . / D X(I+1) * * 3) *(Y 1(I+1)-Y 1(I))+(1 . /(D X(I+1) * D X(I+1))) *$ $(S(1+1)+S(1))$
4
1 CONTIMLE
RETUFN
END
C

C
SUBROUTINE INTAPT (INTFNT, NPN1, XO, YO)
DIMENSION N1 (1), XO(1), YO(1)
N2 =Af-1
IF (INTPNT.LT.1) GOTO 101
IF (INTFNT.EQ.999) RETUKN
100 1 I=I,N2
1
101
Ni (I) $=I N T P N T$
RETLFN
$W 1=X O(N)-X O(1)$
$\mathrm{W}_{2}=\mathrm{YO}(\mathrm{N})-\mathrm{YO}(1)$

W3 = GQRT (W1*W1+W2*W2)
SxW3/100.
10 $2 I=1, N 2$
$W 1=X 0(I+1)-X 0(I)$
W2=YO (I+1)-YO(I)
W3 $=50 F T$ (W1*W1+W2*W2)
N1 (I) $=043 / 5-1$.
$N 5=(200-N) /(N-1)$
IF (N1 (I). GT. N5 )N1 (I) =N5
2 CONTINLE
RETURN
END
C
C**********SE15 JOINED CUFVE COMTON DATA
C
SUEROUTINE JONSUB (EFFF,LSUM)
C JOIN COMMON DATA AREA AND INFUT COMMON DATA AREA
COHYON/JOIN/CJI (500); C. $52(500)$, $13(12)$; $34(100)$, IF'NTK ( 6 )
COMMON/DATSUP/NFS, NPI (50), IFREES, X (50) , Y(50), L (50), IH(5) , M(5)
4 , HETHOD, IHELP , IFREV, EOUND (2), SUESET, INTFNT, IE (2)
INTEGER ERR:SUBSET
C FIRST CUFVE SEGKENI?
IF (SUBSEI.EQ.O.OR.SUBSET.EQ.1) FETURN
IF (IERROR (103). NE.O) GOTO 3
C READ THE JOIN CURVE COMMON DATA AFEA
CALLL FDCOMS
3 MSUM=O
$N 2=N F \cdot G-1$
10 $1 . I=1, N 2$
1 HSUM $=$ MSUK + NFI (I)
MSUM $=$ MSUMT + NF'S
LSUMFASUAM + J3 (1)
IF1m」3(1)
IF (LSSM.GT.500) GOTO 400
C CHECK FIRST FOINT AS LAST FOINT OF THE F\&EUIOUS SUESET
IF (X(IH(1)).EQ.C.JI (IF'I)) FETUKN
C AIDD DNE POINT TO FRESENT DATA FOINTS
L(IFFEES) $=\mathrm{IH}(1)$
IH(1)=IFREES
$X($ IFFEES $)=C J I$ (IF'L)
$Y$ (IFREES) =CJ2 (IF'L)
$N F \cdot S=N F \cdot S+1$
IFREES=1FREES+1
NPI (NF'S-1) $=N F I$ (NF'S-2)
C SAVE JOIN CURVE COMMON DATA
CALL WRCOMJ
RETUKN
C ERROR MESSAG
$400 \quad E R F=1$
RETURN
END

```
C
C . ; APFENDIX 2.12*
C #*****************
C
C THIS IS THE MAIN FFOGRAM SEGHENT WHICH CALLSS THE NUMERICAL ALGORITHMS
C INCORFORATEU IN THE FARAMETRIC FACKAGE.
C
C
C
C ******MAIN PROGRAM SEGMENT FOR INHOKING THE NUMERICAL ALGORITHMS ******
C
C
C INFUT/OUTFUT COMMON DATA AREA
    COMMON/DATSUF/NFS,NPI (50), IFREES ; X(50) ; Y(50),Z (50) ,L (50), IH(5);
                                    M(5) , METHOD, IHELP, IPREV, EOUND (6), SUESET, INTFNT, IE (2)
                    ,1D
    COMMON/CLRVEFIT/XCOEF (50,4),YCOEF (50,4), ZCOEF (50,4),XCORD (200) ,
                    YCORD (200), ZCORD (200), TCORD (200)
    DATA FHODL2vPHODL4;FDTSF;FHODL5/"FHODL2","FHODL4","FDTSUFFL"
                    " "FHODL5" /
    INTEGER SUESET
    LOGICAL*1. FHODL2(10) , PHODL4(10), PDTSF'(10), FHONL5(10)
    DIMENSION XO(50),YO(50),ZO(50),TO(50)
    CALL. FRDCHI
    IN=5
    IOUT=6
    CALL FFNLLAK (XO,YO,ZO)
    CALL INTFFT (INTFNT,NFS,NFI,XO,YO,ZO,TO,ID,HETHOD)
    WRITE (IOUT,10)
10 FORMAT ("FLEASE WAIT,FIT IS BEING COMPUTED")
    NC=4
    60TO(31,32,33,34,35) , HETHOD
C
C STANDARD PARAMETRIC CUBIC SPLINE (SECOND DEEV.EOUNDARY CONDITION)
31 CALL CUEPAR CNPS,NPI,XO,YO,ZO,TO,XCOFD, YCORDD, ZCDRD,TCORD,
&XCOEF YCOEF, ZCOEF, EOUND, ID, KETHOD)
    60T0 3
C
C CYCLIC CUBIC SPLINE ?
32 CALL CYCLIC (NF'S,NFII,XO,YO,ZO,TO, XCORD, YCOFD, ZCORD, TCORD,
GXCDEF, YCOEF,ZCOEF,ID,HETHODS
    gOTO 3
C
C ANTICYCLIC CUBIC SPLINE Y
33 CALL ANTCYC (NPS,NPI, XO,YO,ZO,TO, XCORD, YCOKD,ZCORD,TCORD,
&XCOEF, YCOEF, ZCOEF, ID,HETHOD)
    BOTO 3
    C
C CUBIC SFLINE VARIABLE END CONDITION
34 CALL. FARCUB (NPS,NPI,XO,YO, ZO,TO,XCORN, YCORD,ZCOKD,TCORD,
4XCOEF, YCOEF, ZCOEF, EOUND, IE, ID, METHOD)
C CALL NEXT MODEL FOR CURVE FIT
3 IFFEV=0
    CALL. FWFKCM1
333 CALL F'WRCM2(NFS,NF'I,NC,ID)
    IF (INTFNT.EQ.999.AND.ID.EQ.2)CALL OUFLAY (F'MODLS)
    CALL ONRLAY (PHODL4)
    CALL FWECM1
    CALLL OUFLAY (FHODLI):
    STOF
```

END
C
C**********CUEIC SFLINE WITH FARAMETRIC SECOND DERIVATIUES********* C

SUBFOUTINE CUEFAR (N,H1,XF,YF, ZF',T1,XXF,YYF,ZZF,TTF, XC,YC,ZC,B
A, IDIM, K)

\& TTF (1) PXC (50,4),YC (50,4), ZC (50,4), B(1), C(2)
C INTEFFGRATE FOK X
$C(1)=B(1)$
$C(2)=B(4)$
CALL CUBIC1 (N,N1,T1,XPFTTF; XXF, XC,C,H)
C INTEFFOLATE FOF Y
$C(1)=B(2)$
$C(2)=B(5)$
CALL CUBIC1 (N,N1,T1,YF,TTF:YYF;YC,C,H)
C INTERFOLATE FOR 2 (3-D)
$C(1)=B(3)$
$C(2)=E(6)$
IF (IDIM.EA. 3 ) CALL CUBICI (N,N1,T1, ZF,TTF,ZZF, ZC,C,M)
RETURN
END
c

C
SUBFOUTINE CYCLIC (N,N1;XF;YF;ZF;T1,XXF;YYF;ZZF;TTF;XC,YC,ZC,B
G,IDIK, M)
DIKENSION $N 1(1), X P(1), Y F(1), \operatorname{ZP}(1), T 1(1), X X F(1), Y Y F(1), 2 Z F(1)$
\&,TTF (1), XC $(50,4), Y C(50,4), Z C(50,4), B(1)$
CALL CUBICF ( $N, N 1, T 1, X F, T T F, X X F, X C, B, H$ )
CALL CUBICF (N,N1,T1,YF:TTF,YYF,YC,BIM)
C THREE IIMENSION
IF (IDIM.EQ.3)CALL CUBICF (N,N1,T1,ZF,TTF,ZZF, ZC,B,H)
RETUFN
ENE
c
C*********GAUSSIAN ELIMINATION FOR CYCLIC CURUES***************
C
SUBFOUT INE GAlJSSP ( $N, X, Y, Y 2, B$ )
DIMENSION $X(1), Y(1), Y 2(1), F(50), G(50), H(50), B(1)$
$N 1=N-1$
$N 2=N 1-1$
J1=1
$G(1)=0$.
$F(1)=0$.
$H(1)=-1$.
$H 1=X(N)-X(N 1)$
$\mathrm{H}=\mathrm{H} 1$
$H_{2}=X\left(N_{1}\right)-X\left(N_{2}\right)$
U=2.* (H1+H2)
$\mathrm{F} 1=(\mathrm{Y}(\mathrm{N})-\mathrm{Y}(\mathrm{N} 1)) / \mathrm{H} 1$
$F 2=(Y(N 1)-Y(N 2)) / H 2$
$V=6 . *(F 1-K 2)$
HO $2 \mathrm{~K}=1$, N2
$J 2=K+1$
$H 2=X(J 2)-X(K)$
R2 $2=(Y(J 2)-Y(K)) / H 2$
IF (K.EQ.1) GOTO 1
$U=U-W * H(J 1)$
$V=V-W * F(J 1)$
$W=-G(J 1) * W$
$Z=1 . /(2 . *(H 1+H 2)-H 1 * G(J 1))$ $G(K)=Z * H_{2}$
$H(k)=-Z * H(J I) * H L$ F(K) $=$ Z* ( 6. $\left.^{*}(R 2-K 1)-H 1 * F(J 1)\right)$
J1 $=\mathrm{K}$
H1 $=\mathrm{H}_{2}$
R1 $=\mathbf{F L} 2$
2 CONTINUE
$\mathrm{H}_{2}=\mathrm{W}+\mathrm{H} 1$
$H 1=(U-H 2 * F(N 2)) /(U-H 2 *(G(N 2)+H(N 2)))$
Y2 (N1) $=\mathrm{H} 1$
H0 $3 \mathrm{JL}=2, \mathrm{~N} 1$
$K=N-J 1$
$Y 2(K)=F(K)-G(K) * Y 2(K+1)-H(K) * H 1$
3 : CONTIMUE
$Y 2(N)=Y 2(1)$
FETURN
END
C
 C

EUEFOUTINE INTFLT (I, IP,N1, X1,Y1, XX,YY,C,M)
BIMENSION $N 1(1) ; X 1(1) ; Y 1(1), X X(1), Y Y(1) ; C(50,4)$
INTF=N1 (I)
IF (M.EQ.4) G0TO 3
$T 1=\times 1(I+1)-X 1(1)$
$\mathrm{F} 1=\mathrm{T} 1 /(\mathrm{INTF}+1)$
Z=X1 (1)
$4 \quad$ IFL=IP+INTF+1
$X X(I F)=X 1(I)$
$X X\left(I F^{\prime} L\right)=X 1(I+1)$
$Y Y(I F)=Y 1(I)$
$Y Y(I P 1)=Y 1(I+1)$
$002 \mathrm{~J}=1$ INTF
$X X(I P+J)=Z+N 1$
IF (M.EQ.4) GOTO 5
$\mathrm{Z}=\mathrm{Z}+\mathrm{R} \mathrm{I}$
$T=Z-X X(I F)$
6. $\quad Y Y(I F+J)=C(I, 1)+T *(C(I, 2)+T *(C(I, 3)+T * C(I, 4)))$

2 CONTINUE
If $=1 \mathrm{~F}^{\prime} 1$
FETURN
$\mathrm{Z}=0$ 。
$\mathrm{R} 1=\mathrm{XI}(\mathrm{I}+1) /\left(1 \mathrm{NTF}^{\prime}+1\right)$
GOTO 4
$5 \quad T=Z+$ たi
$\mathbf{Z}=\mathbf{Z}+$ K 1
GOTO 6
END

## C

C**********ANTI CYCLIE CUEIC SFLINEE***************************
C
SUBROUTINE ANTCYC(N,N1;XP;YF;ZF;T1;XXF;YYF,ZZF, TTF; XC,YC,ZC
GYIDIM,M)
DIMENSION N1 (1), XP(1),YF(1),ZF(1),T1(1),XXF(1),YYF(1),ZZF(1)
$G, T T F(1), X C(50,4), Y C(50,4), Z C(50,4)$
CALL CANTCY (N,N1;T1,XF':TTF, XXP, XC,H)
CALL CANTCY(N,N1,TI;YF,TTF;YYF;YC, $H$ )
IF (IDIM.EQ. 3 )CALL CANTCY (N,N1,T1,ZF,TTF, ZZF, ZC, M)
RETURN
END
C

C***********INTERFOLTE FOR EACH $X / Y / Z$ AS IN FARAMETER T******* C

SUBROUTINE CANTCY(N,N1;X1,Y1,XX,YY,C,H)
IIMENSION N1 (1), XI (1), Y1 (1), XX(1),YY(1), C(50,4),Y2(50)
CALL ACGAUS ( $\mathrm{N}, \times 1, Y 1$ Y Y 2 )
CALL ANTCOF ( $N, N 1 ; X 1, Y 1, Y 2, X X, Y Y, C)$
FETURN
END

## C

C*********GAUSSIAN ELIMINATION FOK ANTI CYCLIC CUKUES******* C

SUBFOUTINE ACGAUS $(N, X, Y, Y 2, B)$
DIMENSION $X(1), Y(1), Y 2(1), V 1(50), W 1(50), Y 1(50), B(1)$
U1 (1) $=0$.
$W 1(1)=0$.
S3 $=X(N) / X(2)$
Z m 1./(2.*(1.+53))
V1 (2) $=2 * 53$
W1 (2) $=-2$
$Y 1(1)=Z *(3 . / X(2)) *(S 3 *(Y(2)-Y(1))-(1 . / S 3) *(Y(N)-Y(N-1)))$
$H=2 . *(X(N)+X(N-1))$
$F=3 . *(X(N) * * 2 *(Y(N-1)-Y(N-2))+X(N-1) * * 2 *(Y(N)-Y(N-1)))$.
$F=F /(X(N) * X(N-1))$
G=0.
$\mathrm{N} 2=\mathrm{N}-2$
LO $11=2, N 2$
$H=H-G * W 1$ (1)
FxF-G*Y1 (I-1)
Gx-Vi (I)*G
$Z=1 . /(2 . *(X(I+1)+X(I))-X(I+1) * V 1(I))$
$V 1(I+1)=0$.
W1 (I+1) $=-2 * X(I+1) * W 1(I)$
$B=3 . *(X(I+1) * * 2 *(Y(I)-Y(I-1))+X(I) * * 2 *(Y(I+1)-Y(I))\}$
$B=E /(X(I+1) * X(I))$
$Y 1(I)=Z *(B-X(I+1) * Y 1(I-1))$
1
CONTINUE
$H=H-(G+X(N)) *(V 1(N-1)+W 1(N-1))$
$Y 1(N-1)=a F-(G+X(N)) * Y 1(N-2)$
$Y 2(N-1)=Y 1(N-1) / H$
$Y 2(N-2)=Y 1(N-2)-V 1(N-1) * Y 2(N-1)$
$\mathrm{NB}=\mathrm{N}-3$
100 $21=1$, N3
$J=N 3+1-I$
$Y 2(J)=Y 1(J)-V 1(J+1) * Y 2(J+1)-W 1(J+1) * Y 2(N-1)$
2
CONTINUE
$Y 2(N)=-Y 2(1)$
RETURN
END
C
C***********ANTICYCLIC COEFFICIENT \& FUNCTION*******************

## C

```
SUEROUTINE ANTCOF (N,N1,X1,Y1,Y2,XX,YY,C)
DIMENSION N1 (1),X1(1),Y1(1),Y2(1),XX(1),YY(1),C(50,4)
IP=1
N2FN-1
UO 1 I=1,N2
    INTF:=N1 (1)
    V=0.
    Fi= X1(I+1)/(INTF'+1)
    C(I,1)= Y1(I)
        C(I,2)=Y2(I)
        C(I,3)=(3./XI(I+1)**2)*(YI(I+1)-Y1 (I))-
```

* 

8
$C(I, 4)=-(2 . / X 1(I+1) * * 3) *(Y 1(I+1)-Y 1(I))+$
$(1 . / X 1(I+1) * * 2) *(Y 2(I+1)+Y 2(I))$
$I F 1=I F+I N T P+1$
$X X(I F)=X 1$ (I)
$X X(I F I)=X I(I+1)$
$Y Y(I F)=Y 1(I)$
$Y Y(I F 1)=Y 1(I+1)$
บO $2 \mathrm{~J}=1$,INTF
$T=U+K 1$
$X X(I F+J)=U+R 1$
$\mathrm{V}=\mathrm{V}+\mathrm{R} 1$
$Y Y(1 F+J)=C(I, 1)+T *(C(I, 2)+T *(C(I, 3)+T * C(I, 4)))$
CONTINUE
IF $=$ IP1
CONTINUE
FETUFN
END
C

C

A,EVIE, IDIK, M)
UIMENSION N1 (1), XF'(1), YF'(1), ZF'(1), T1 (1), XXF'(1),YYF'(1),ZZF'(1)
$4, \operatorname{TTP}(1), X C(50,4), Y C(50,4), Z C(50,4), B(1), I E(1), C(2)$
$C(1)=B(1)$
$C(2)=B(4)$
CALL CSFLEC ( $N, N 1, T 1, X F$;TTF'; XXF',XC,C,IE,M)
$C(1)=B(2)$
$C(2)=B(5)$
CALL CSFLEC (N,NL,TL,YF,TTF,YYF,YC,C,IE,M)
$C(1)=B(3)$
$C(2)=B^{\prime}(6)$
IF (IDIM.EQ. 3) CALL CSFLEC (N,N1,T1,ZF,TTF,ZZF,ZC,C,IE,M)
RETURN
END
C

C
SUBFOUTINE CSFLEC ( $N, N 1, X 1, Y 1, X X, Y Y, C, B, I E, M)$
DIMENSION N1 (1) IX1 (1),Y1 (1), XX(1),YY(1),C(50,4),B(1),IE(1)
DIMENSION BX (50), CI (50) ;D (50), S (50)
$51=\times 1$ (2)/X1 (3)
$S 2=\times 1(N) / X 1(N-1)$
C MAIN FROGFAM CALLS
CALL GCOFMT ( $N, S 1, S 2, X 1 ; E X, C I, E, I E, E X, A) Y$
CALL GENFHS (N,S1,S2,Y1,B,X1,S,IE)
CALL GAUSEC (N,EX,C1,D,S,IE,EX,A)
CALL ECCOEF $(N, Y 1, C, S ; X 1)$
CALL COMFIT (N,NI;XI,Y1,XX,YY,C,K)
RETURN
END
C

C
SUBFOUTINE GENFKT ( $N, X 1, Y 1, Z 1, T 1, I D I M, M)$
DIMENSION XI (1), Y1 (1), Z1 (1), TI (1)
$T 1(1)=0$.
T0 $1 \mathrm{~K}=2, N$
$U=X 1(k)-X 1(K-1)$
$V=Y 1(k)-Y 1(k-1)$
IF (IDIM.EQ. 3 ) $(Q=Z 1 \dot{( }(k)-Z 1(k-1)$
$\mathrm{J}=\mathrm{U} * \mathrm{U}+\mathrm{V} * \mathrm{~V}$
IF (IDIM.EQ. 3) $D=[D+Q * a$

IF (M.EQ. 3.OK.H.EQ.4) GOTO 2
$T 1(K)=T 1(K-1)+[1$
1 CONTINUE
RETLKN
T1 $(K)=01$
GOTO 1
END
C

C
SUEROUTINE INTRFT (INTPNT,N,N1; X1,Y1,Z1,T1,IWIM,M)
UIMENSION M1 (1), X1 (1), Yi(1), Z1 (1), T1 (1)
CALL GENFFFT ( $N, X 1, Y 1, Z 1, T 1, I D I M, M)$
$\mathrm{N} 2=\mathrm{N}-1$
IF (INTFNT.LT.1) GOTO:101
IF (INTFNT.EQ.999) GOTO 7
$55 \quad 1011 \mathrm{I}=1$, N2
$1 \quad$ N1 (I) $=$ INTFNT
IF (IFLAG.EQ.999) INTFNT=999
IFLAG:O
FETURN
$101 \quad W i=X 1(N)-X 1$ (1)
$W 2=Y 1(N)-Y 1(1)$
IF (IDIM.EQ. 3 ) W3 $=21$ (N) $-\mathrm{Z1}$ (1)
$t=W 1 * W 1+W 2 * W 2$
IF (IDIH.EQ.3) $D=D+W 3 * W 3$
TLESOFTT(D)
S=TL/100.
$10021=1$ N2
$N 1(I)=T 1(I+1) / S-1$.
$N 5=(200-N) /(N-1)$
IF (N1 (I) .GT.N5) M1 (I) $=$ NS
2 CONTINUE
RETURN
7 INTFNT=5
IFLAG=999
GOTO 55
END

## APPENDIX 2.2

THE IDF - EXPLICIT PACKAGE
c
 * AFFFENDIX 2.21 *

c.

C this module handles the following interactive gisplays:-
C 1.INTRODUCTORY
C 2.CHOICE OF THE NUMERICAL ALGORITHMS
C 3.DATA ENTFY
c
c
C
C
C

C
C INFIUT COMMON DATA AFEA
COMMON/EATSUF/NFS,NFI (50), IFFEES, X(50),Y(50),L(50),IH(5),M(5),
4
COMMON/IO/IN,IOUT
DATA MODL2, HELF/"MOD2","HELF"/
LOGICAL*1 MODL2(10), HELF(10)
INTEGEF SUBSET
$1 \mathrm{H}=5$
IOUT=6
CALL 1 XOFEN
IF (IERKOF (103). NE. O)GOTO 1
CALL RDCOMI
IF (IHELF.NE.O) GOTO 55
IF (IFFEV.EQ.1) GOTO 21
C CALL THE DISFLAY SEQUENCE FOR DATA ENTRY ON REQUEST
1 CALL INTKOD(IC)
GOTO ( $2,3000,1111$ ), IC
2 CALL MENU (METHOD,IC)
G070(10,1,3000,1111,1111), IC
10 CALL BATENT (IC,IA)
GOTO (20,2,3000,1111,1111), IC
20 CALL DATMAN(IA,IC)
G0TO(1000,10,40,1111,1111,3000,1111,1111), IC
CALL EDIT (IC,IA)
40 FETUKN TO DATA MANIFLl_ATION DISFLAY
IF (IC.GT.1) GOTO 20
C Next disflay in the sequence
$1000 \quad$ IFREV $=0$
IHELF=0
CALL WKCOMI
CALL OURLAY (MODL2)
C HELP DISFLAY
3000 CALL WFCOMI
CALL OUFLAY (HELF)
C TERMINATE THE FROGGRAM
1111 CALL EXIT
STOP
C LINK LIST UNCHAGE
21 IFREV=0
IHELF: $=0$
IA $=111$
goto 20
C REYURN FROM HELF DISFLAY
55 ©OTO (1,2,10,21),1HELF.
END
C

```
C *************INTRODUCTORY DISFLLAY *********************************
C
    SUEROUTINE INTROD(IC)
    COMMON /IO/ IN,IOUT
C HENU ITEKS
    DATA MNTXT/"+ NEXT + HELFF + EXIT */
    LDGICAL*L MNTXT (30)
C SET UF' THE INTRONLCTOFY TEXT AND MENU
    CALL TXCLER
    CALL CLKFOS(1.,780.)
    CALL TEXTUF("INTEXT",34)
    CALL MNOFEN(875.,715.,1)
    CALL MNDISF(YNTXT,3,10,1)
    CALL FRAME (870.,733.,3)
2 CALL MNPICK (J,ICHAR, MNO)
22 CALL CONFRH (ICHAR)
    IF (ICHAR.EQ.78) GOTO 2
    IF (ICHAR.NE'.89) GOTO 22
    IC=J
    RETURN
    END
C
C %*********** CHOICE OF DATA FITTING ALGORITHM *********************
C
    SUBFOUTINE MENU(M,IC)
C THIS RETURN THE ALGORITHM INIEX IN THE MENU
    COMMON/IO/IN,IOUT
C FIENU ITEM
    UATA MNTXT1 /" + NEXT + FFEVIOUS + HELF' + FESTART + EXIT */
    LOGICAL*1 NNTXTI (50)
7 CALL TXCLER
    WRITE (IONT,10)
10 FORHAT ("INDICATE YOUR CHOICE OF ALGORITHIH:-")
    CALL HNOPEN(875.,715.,1)
C OUTPUT ALGORITHM LIST
    CALL DTEXT(20.,700.,"***EXFLICIT FACKAGE FOK INTERFOLATOFIY DATA FITTING*****!
    CALL DTEXT (70.,650.,"NUMERICAL ALGOFITHMS:-",22)
    CALLL MNDISF(MNTXTT1,5,10,1)
    CALLL FRAME (870.,733.,5)
    CALLL MNOFEN (60.,600.,2)
    CALL. MNTEXT ("1-GLOBAL. POLYNOMIAL INTEFFOLATION(NEWTON FORM) ",46)
    CALLL MNTEXT ("2-PIECEWISE OUINTIC FOHYYNOMIAL INTERFOLATION
&(VARIABLE END CONDITION)*,69)
    CALLL MNTEXT ("3-CUEIC SFLIINE(SECOND DERIVATIVES END CONDITION)";48)
    CALL MNTEXT(*4-CIBIC SFLINE(SECOND DERIVATIVES END CONDITION(*))*,51)
    CALL HNTEXT("S-CUBIC SFLINE (FIRST DERIVATIUES END CONDITION)*,47)
    CALL HNTEXT("6-CUBIC SFLINE(FERIODIC END CONDITION)",38)
    CALLL MNTEXT ("7-CUBIC SFLINE(WAFIABLE END CONDITION)",38)
    CALLL CLIRPOS (20.,300.)
    CALL ALPHMD
    WFITE (IOUT,888)
888 FOFNAT <47H* WHERE Y"[X1]=U*Y"[X2] & Y~[X(N-1)]=U*Y~[X(N)])
C SET UP CLRSOF FOR HENU CHOICE & CONFIRM
1 CALL HNEICK(I,ICHAK,HNO)
    IF (HNO.EO.1)GOTO 3
    H=I
    GOTO 1
    CALL CONFFH(ICHAF)
    IF (ICHAF゙.EQ.78) GOTO 1
    IF (ICHAFR.NE.89) GOTO 3
    IF (I.EQ.4)GOTO 7
    IC:I
```

FETUR'N
END
c
C $\# * * * * * * * * * * * * * *$ DATA ENTRY DISFLAY FOUTTINE*******************
c
SUBROUTINE DATENT (IC.IA)
COMMON /DATSUF/NFS,NFI (50), IFFEES, X(50),Y(50),L(50),IH(5),H(5)
a , HETHOD, IHELF', IFREV, EOUND (2), SUBSET, INTFNT, IE (2)
COMMON /IO/IN, IOUT
C MENU ITEMS FOR THIS DISFLAY
DATA HNTXT1/"+ NEXT + FREVIOUS + HELF + RESTART + EXIT * $\quad$,
DATA HNTXT2/"+ NEW + OLD + + KEYBOARD+DISC FILE:/
LOGICAL*1 MNTXT1 (50), MNTXT2 (50)
INTEGER SUESET
C SET DISFLAY fiEADY FOR DATA ENTKY
23 CALL TXCLEF
WFITE (IOUT, 10)
10 FBRMAT ("DATA ENTRY:-")
CALL CUKFOS (1.,625.)
WRITE (IOUT,11)
C OUTFUT INSTRUCTIONS FOR THE USER
11 FORKAT("SELECT THE AFFFOFRIATE"/
\& "DATA SFECIFICATION(*):-"////"1-STATE OF DATA:-"///"2-DATA",
G* MEDIUM ENTRY:-*)
WRITE (IOUT, 20)
20 FORMAT (////////////////"* IF 'OLD' IS SELECTED YOU MAY FROCEED"/
\& " TO NEXT DISFLAY IMMEDIATELY .OTHEFWISE ";

* " YOU HUST SELECT THE DESIRED KEDIUM")

CALL HNOPEN (875.,715.,1)
CALL MNDISF (MNTXT1,5,10,1)
CALL FRAME (870.,733.,5)
C DISFLAY MENU, FALSE CUKSOR AND WAIT FOR USER ACTION
CALL KNOFEN(320.,515.,2)
CALL MNDISF (KNTXT2,5,10,2)
CALL FKAME (315.,535.,5)
CALL TXKOVE ( 315.975. )
CALL TXDFAW (460.,475.)
$\mathrm{NFLAG}=1$
$\mathrm{MD}=0$
IS $=0$
5 CALL KNFICK (J, ICHAR, HNO)
C TRANSFER CONTFOL TO AFPROPRIATE FFROGRAM RESFONSE
IF (HNO.EQ.1) GOTO 2
IF (IS.EQ.2.OR.NFLAG.EQ.O.OR.J.EQ.3) GOTO 5
IF (J.LT.3) GOTO 7
$\mathrm{MD}=\mathrm{J}$
CALL CURPOS (1.,400.)
3 CALL MESSAG("~ NUABER OF DATA FOINTS (MAX.SO)?"")
FEAD (IN, JOIN
30 FORKAT (GO.0)
IF (N.GT.SO.OR.N.LT. 3 ) GOTO 3
NPS $=$ N
IF (J.EQ.5)GOTO 1010
C INFUT DATA FOINTS FFOK KEYEDAKD
WRITE (IOUT, 40)
40 FDFMAT (/,"~X-COOROS.:-")
IF (IERFOR (110) . NE. 0 ) GOTO 100
$35 \operatorname{FEAD}(I N, 50)(X(I), I=1, N)$
50 FDRMAT (50G0.0)
HFIIE (IOUT,70)
70 FGFKAT (/, "~~ 7 -COORDS.:-~)
IF (IERFOR(110).NE. O)GOTO 110

```
65 NEAD (IN,SO) (Y (I),I=1,N)
        IHELF:=3
        G0T0 5
100 WFITE(IOUT,105)
105 FOFHAT ("ILLEGAL X-COORDS.,TKY AGAIN")
        ENDFILE S
        GOTO 35
110 WFITE(IOUT,11S)
115 FORMAT ("ILLEGAL Y-COORDS.,TRYY HGAIN")
        ENDFILE 5
        GOTO 65
2 CALL CONFEM (ICHAF)
        IF (ICHAFF.EQ.78) GOTO 5
        IF (ICHAR.NE.B9)GOTO 2
        IF(J.EQ.4)GOTO 23
        IF NFLLAG.EQ.1.AND.J.EQ.1.AND.MD.EQ.OS GOTO 5
        IC=J
        RETUFN
1010 IFLG=0
C NE:W DATA FOINTS
    IA=0
C INFUT DATA FROM DISC FILE
    CALL GETFLN(FILE)
    CALL FEADAT (FILE,X,Y,NFS,IFLG)
    IF (IFLG.EQ.1)GOTO 1010.
    IF(IFLG.EQ.2)GOTO 3
    GOTO 5
313 ENUFILE 5
    GOTO 3
C NEN NATA FOINTS
7 IA=0
C OLD DATA FOINTS
    IF(J.EQ_2) IA=111
    IS=\
    IF(J.EQ.2.AND.MD.GT.O) GOTO S
    IF (J.EQ.2.AND.KD.EQ.O) GOTO 12
    IF(J.ER.1) GOTO S
12 NFLAG=O
    gOTO 5
    END
C . 
C ***********DATA POINT TAEULATION DISFLAY ROUTINE***************
C
    SUE&OUTINE DATMAN(IATIC)
C INFUT COMMON DATA AREA
    COMMON/DATSUP/NF'S,NFI (50), IFEFES,X(50),Y(50) ,L (50), IH(5),H(5)
d
                , METHOD, IHELF, IF'REU, EOUND (2),SUBSET, INTFNT, IE (2)
    COMMON/LO/IN,IOUT
C MENU ITEHS
    DATA NNTXT/" + NEXT + FREVIOUS + EDIT + SURT-X + SAVE
&+ HELF + FESTART + EXIT */
    UIMENSION XO(50),YO(50)
    LOGICAL*1 FNTXT (80)
    INTEGER SUBSET,S
C OLD DATA FGINTS?
22 IF(IA.EQ.111)GOTO7
111 N=NFS-1
C SET LINK LIST
    DO 1 I=1,N
1 L(I) = I+1
    l. (NF'S)=0
    IFREES=NF'S+1
```

```
    LO 2 I=1,5
2 M(I)=10*I
    S=0
    10 3 I=1,5
    IH(I) =S*10+1
3 S=S+1
C SET DISFLAY HENU,ANI DATA POINT TABLE
7 CALL TXCLEF
    WRITE(IOUT,10)
10 FOFMAT ("TABULATION OF DATA:-")
    CALLL MNOFEN(875.,715.,1)
    CALL MNDISP (MNTXT,8,10,1)
    CALLL FRAME (B70.,733.,8)
    CALLL TABLE
    IHEL_F=4
C FROMPT USER FOR CUKSOR FTCKING ACTION AND CONFIFM
4 CALL MANICK(J,ICHARIMNO)
77 CALL CONFRK(ICHAR)
    IF (ICHAR.EQ. 78)GOTO 4
    IF (ICHAR.NE.89) G070 77
    IF (J.EQ.4) GOT0 44
    IF (J.EO.S) GOTO 444
    IF(J.EQ.7) GOTO 22
    IC=J
    RETUFN
C SOKT DATA FOINTS IN X
44 CALLL FEMH_NK(XO,YO)
    CALL SORTX (XO,YO,NF'S)
    DO 101 I=1,NPS
    X(I) =XO(I)
    Y(I) =्YO(I)
101 CONTINUE
    gOTO 111
C SAVE DATA FOINT IN DISC FILE
444 CALL FEFHLNK(XO,YO)
    CALL. SAVE (XO,YOPNF'S)
    GOTO 4
    END
C
C. ###*********EIITOR DISF'LAY*********************************
C
SUBROUTINE EDIT (IC,IA)
    COMMON/DATSUFF/NFG,NPI (50), IFFEES,X(50) Y Y(50) ,L (50),IH(5) ,H(5)
*
                                    , METHOD, IHELFF IPFEV, EOUND (2) , SUBSET, INTPNT, IE (2)
    COMMON/IO/IN, LOUT
C MENU ITEMS
    LATA KNTXT/" + NEXT + FREVYIOUS + CORRECT + DELETE + INSERT
&+ RESTART + EXIT */
    DIMENSION A(31)
    INTEGER SUBSET
    LOGICAL*I YNTXT (70)
1 CALL TXCLER
    HRITE (IOUT,10)
10 FORMAT "DATA FOINTS EDITING:-")
C SET LP DISFLAY MENU
    CALL. MNOFEN(875.,715.,1)
    CALL WNDISP (FNTXT,7,10,1)
    CALL FRAME (870.,733.,7)
C RAISE CLKSOR FEADY FOR USER INTERACTION AND CONFIRM ACTION
77 CALL KNFICK(J,ICHAR,MNO)
88 CALL CONFFM(ICHAK)
    IF (ICHAR.EQ.78) GOTO'77
```

IF (ICHAK.ME. 89) GOTO BB
C ACTIVATE AFFROFRIATE ROUTINES OR OFTIONS GOTO ( $30,30,40,50,60,1,70), \mathrm{J}$
C NEXT/FREUIOUS DISFLAY
30 CALL UFDATE IC. $=\mathrm{J}$ GOTO 114
C CORRECT IATA FOINTS
40 WFITE (IOUT,20)
20 FORMAT (/////CORFECTION:-*)
C FFNOMT USEK FOR INFUTING EIITT INFOFHATION
5 CALL MESSAG(*~NUMEER OF UATA FOINTS (MAX.10)?~*)
FEAD (IN.45) H2
45 FORMAT (GO.0)
IF (M2.GT. 10) GOTO 5
221 WFITE (ICUT, 80)

LAST $=3 * M 2+1$
IF (IERROK(110) .NE O) GOTO 222
FEAD (IN.90) (A (I) ; I=1, LAST)
90 FORMAT (30B0.0)
A (LAST) $=99$
CALL CORECT (A)
CALL UPDATE
GOTO 100
C DELETE UATA POINTS
50 WRITE (IOUT,110)
110 FOFMAT (/////"DELETION:-*)
C USER SUFFLIES EDIT-DELETE INFUT
7 CALL MESSAG (** NUMBER OF JATA FOINT (MAX. 30 ) ?~~)
READ (IN, 45) M2
IF (K2.GT. 30) GOTO 7
125 WRITE(IOUT,130)
130 FOFHAT (~* ENTEF I IN DESCENDING ORDER: ")
LAST $=$ M2 +1
IF (IERFOR(110). NE. 0) GOTO 333
REAE(IN,90) (A (I) , I $=1, L A S T)$
A (LAST) $=99$
IF (H2.EQ.1) GOTO 11
M1=K2-1 ?
DO 9 I=1,M1
IF ( $A(I) . L T . A(I+1))$ GOTO 125
9 CONTINUE
11 CALL DELETE (A)
CALL LFIDATE
GOTO 100
C ADDITION DATA FOINTS
60 WRITE (IOUT, 150)
150 FORKAT (////"LNSERTION: -")
155 CALL MESSAG (" * HLMBER OF DATA FGINTS (MAX. 1 FER INTERVAL, TOTAL 10) ?**)
FEAD (IN, 45) M2
IF (M2.GT.10) G0TO 155
165 WFITE (IOUT,170)
170 FOFMAT ( $\sim$ ENTER $I$, $X, Y$ IN DESCENDING ORDER:~)
LAST $=3 * M 2+1$
IF (IEFNOR (110). NE.0) GOTO 444
FEAD (IN,90) (A (I) , I=1,LAST)
A (LAST) $=99$
IF (M2.EQ.1) GOTO 190
LAST1 $=3 * M 2-5$
10 $181=1$, LAST1.3 3
IF (A(I).LT.A(I+3) ) GOTO 165

C

4 , METHOD, IHELP ; IFREV, EUUND (2) , SUBSET, INTFNT , IE (2)
COMMON/IO/IN,IOUT
C HENU ITEMS ,EXECUTABLE FROGRAM MOWLLES
DATA MNTXT1/" + FREUIOUS + EXIT */
 4, "MOD3" " KOD4" " MODS", " HODG" " "MOD7" /

LOGICAL* 2 MNTXT1 (20), MODL1 (10), MODL2 (10), MOLL $3(10)$, MODL 4 (10)
LOGICAL*1 MOULS(10), MONL6(10) MODL $7(10)$
$I N=5$
IOUT $=6$
CALL TXOFEN
CALL FUCOM1
C OUTFUT IIEFLAY SEQUENCE NAMES IN MENU FORHAT
1 CALL TXCLER
WFITE (IOUT, 10)

$\& \quad / / S X$ " "THE FOLLOWING DISF'LAY SEQUENCE CONSTITUTE THE COMFLETE"/
\& 5X, "DATA FITTING FROCESS. " / /
\& SX, "YOU HAY ENTER ANY OF THESE UISFLAY BY USING THE CROSS-HAIK"/ \& 5X,"CUFSOF ON THE T4010 OR TFACKING CROSS WITH LIGHT-PEN ON THE GT42 8-" /)

CRILL MNOFEN(50.,540.,1)
CALL MNTEXT(* + INTRODLCTION:- BRIEFLY GIVING THE USE OF THE SYST SEM." "54)

CALL HNTEXT ("+ ALGORITHMS:- LIST OF AVAILABLE INTERFOLATORY METH s005.":55)

CALL: MNTEXT (* + DATA ENTKY:- ENTER DATA FOINTS INTO THE SYSTEM FR LOH DISC FL/KEYED.*,68)

CALL MNTEXT ("+ TABLLATION OF DATA FOINTS:- INCLUDES EEITT,SORT \& LSAVE DATA FGINTS.", 68 )

CALL HNTEXT (* + FOLYGONAK FLOT:- HATA FOINTS JOINED BY STFAIGHT L GINE SEGMENTS.* © 64)

CALL HNTEXT ("+ F'ARAMETER ENTRY:- FARAMETEES REQUIRED BY FARTICUL \&AR ALGORITHM." 65 \}

CALL MNTEXT(* + CURVE FIT:- BISFLAY OF THE SMO@TH CURVE INCLUDES \&ZOOM OFTION., ETC.*.69)

CALL MNTEXT("+ CURUE DESIGN:- INTERMEDIATE FOINTS SFECIFIED a BY CUKSOK FOSITION." ${ }^{\text {a }}$ 。 6 )

CALLL MNTEXT("+ TAELE OF INTEFFGLATEB FOINTS:- INCLUDES OFTION FO 4R COEFF. XHAFWCOFY ." 70 )

CALL KNTEXT("+ SUFEKLMFOSED CURVE:- SIMULTANEOUS IISFFLY OF SEVEF \&AL CURVES." ${ }^{*} 63$ )

CALL HNTEXT (" + ERFRUK FEFFERENCE:-- EFROR CURUE W.F.T. GLOEAL FOLY RNOMIAL INTEFF...",67)

CALL MNTEXT ("+ JUINED CURVES:- CONCATENATION OF SEVERAL SEGMENT \&OF CURVES.",60)

CALL MNTEXT (* + USAGE OF CONTFOL COMMANDS:- LIGT OF ALL COMMAND U LSED HEKE.",59)

CALL HNTEXT (* + TERMINATE THE FROCESS:- EXIT FROM THE SYSTEM.*,47)
2 CALL MNFICK (I,ICHAF, MNO)
3 CALL CONFRM (ICHAK)
IF (ICHAK.EQ.78) GOTO 2
IF (ICHAK.NE.89) GOTO 3
IF (I.GT.4) GOTO 5
IHELF: $=1$
C FEADS THE AFFFRFRIATE MODULE INTO THE COFE READY FOF EXECUTION
CALL WKCOM1
CALL OVELLAY (MODL1)
5 IF (I.GT.6) GOTO 6
IHELF: $\mathrm{I}-4$
CALL WRCOM1
CALL OVFLAY (HODL2)
6 IF (I.LT.9.OF.I.GT.11) GOTO 7
IHELF $=\mathbf{I}-8$
CALL WRCOMI
CALL OUFLAY (MODL6)
7 IF (I.EQ.7) CALL QUKLAY (MODL4)
IF (I.EQ.B) CALL OUFILAY (HOLLS)
IF (I.EQ.12) CALL OUKLAY (KOLL 7 )
IF(I.NE.14) GOTO 133
CALL EXIT
STOF
C GOTO NEXT DISFLAY,GIVING COMMAND USAGE \& OFTIONS
133 CALL TXCLER
CALL MAOFEN(875..715..1)

CALLL FFAME (870., 733.,2)
CALL ALFHMD
CALL CUF'FOS(1.,770.)
CALL TEXTUF("HELLFTEXT",28)
22 CALL HNFICK (J,ICHAF, MNO)
222 CALL CONFFM (ICHAF)
IF (ICHAF.EQ.78) GOTO 22
IF (ICHAK.NE. 89) GOTO 222
Goto (1,i11) \&J
111 CALL EXIT
STOF
ENE
C

C
SUBFOUTINE ADD(C)
COMMON/DATSUF/NFS,NFI (50), IFKEES,X(50), Y(50),L(50), IH(5), M(5),
a METHOD, IHELF , IFFEE, BOUND (2) , SLSBSET , INTF'NT, IE (2)
DIMENSION C(31)
INTEGER SUBSET
C. ADOS DATA FOINT TO LINK LIST DATA STEUCTURE

IF $=$ IFKEES
10 3 I $=1,31,3$
C CHECKS DATA FGINT TABLE INDEX
IF (C (I).EQ.99) GOTO 2
IF (C (I). .IT. IFS)GOTO 3
IF (C (I) EQ. O) GOTO. 4
$\mathrm{IC}=\mathrm{C}(\mathrm{I})$
c. get link list location of the data foint and set link affrofriately IS=INDEX(IC)
$L(I F)=L(I S)$
$L(1 S)=1 F$
GOTO 5
$4 \quad L(\mathrm{IF})=\mathrm{IH}(1)$
$I H(1)=I F$
C. add data foints to ffee location in the link list
$5 \quad X(I F)=C(1+1)$
$Y(I F)=C(I+2)$
If $=1 \mathrm{IF}^{\prime}+1$
$\mathrm{NF} \mathrm{S}=\mathrm{NF} \mathrm{F} \mathrm{S}+1$
3 CONTINUE
c set free link list fointer
2 IFFEES=IF FETUKN
END
c

c
SUEFDUTINE COFECT(C)
COMMON/DATSUF/NFSFNFI (50), IFFEES, $X(50), Y(50), L(50), I H(5), H(5)$
, METHOD, IHELF, IFGEU, BOUND (2) , SUESET , INTFNT, IE (2)
DIMENSION C(31)
INTEGER SUBSET
DO 2 I=1,31,3
c checks data foints table index
IF (C (I). EQ.99) GOTO3
IF (C(I).GT.NF'S GOTO 2
IC=C (I)
C GET LINK LISt location and feflace data foint
$K=I N D E X(I C)$
$X(k)=\mathrm{C}(\mathrm{I}+1)$
$Y(k)=C(1+2)$
2 CONTINUE
3 RETURN
END
C

c
SUBROUTINE DELETE(C)
COMMON/DATSUP/NFSTMFI (50), IFREES, X $(50), Y(50), L(50)$, IH (5) , M(5)
4 , METHOD, IHELF, IFFEE, EOUND (2) ,SUBSET, INTF'NT, IE (2)
DIMENSION C(1), XO (50), YO (50), LO(50)
INTEGER SUBSET
10 $1 \mathrm{I}=1,31$
C Checks data foints table index
IF (C (1) . EO. 99) GOTO 3
IF (C (I). GT.NFS)GOTO 5
IF (C (I).EO. 1 ) GOTO 4
IC=C(1)-1
IS=INDEX(IC)
c get link list location and delete data foint
L(IS) $=\mathrm{L}$ (L(IS))
GOTO 1
$5 \quad N F^{\prime} S=N F S+1$
GOTO 1
$4 \quad \mathrm{IH}(1)=\mathrm{L}(\mathrm{IH}(1))$
1 CONTINUE
$3 \quad \mathrm{HFS}=\mathrm{NF} \mathrm{S}-\mathrm{I}+1$
IFREES $=$ IFREES-I 1
c gafbage collection

If $=\mathrm{IH}$ (1)
100 6 K゙=1, NF'S
$X O(K)=X(I F)$
$Y O(K)=Y(I F)$
LO (K) $=k+1$
IF'=L(IF)
CONTINUE
[00 $7 \mathrm{~J}=1$, NF'S
$X(J)=X 0(J)$
$Y(J)=Y O(J)$
$L(J)=L O(J)$
CONTINUE
$L(N F S)=0$
$15=0$
[10 $9 K=1.5$
$I H(k)=I S * 10+1$
15=15+1
9 CONTINUE
EETUKN
EtiB
C

C
SUBFOUTINE GETFLN(NAME)
C get file mame \& Save it in affiay name
INTEGER NAKE (3)
CALL MESSAG("~ MATA FILE NAME (MAX. 10 CHAKACTERS) ?~")
FEAD (5, 30) NAME
30 FOKMAT (2A4,A2)
RETUKN
END
C

C
INTEGER FUNCTION INDEX (INX)
C INFUT COMMON DATA AREA
COMMON/DATSUF/NFS,NFI (50), IFREES, X(50) , Y(50), L (50), 1H(5), H(5)
h
, METHOD, IHELF, IFREV, BOUND (2), SUBSET, IHTFNT, IE (2)
INTEGEK SUBSET
C FIND LINK LIST FORTION?
(10) $11=1,5$

IF (M(I).GE.INX)GOTO 2
1 CONTINUE
2 ISIH(I)
C COMPUTE LOCATION
$I N X=I N X-(I-1) * 10$
$\operatorname{INXI}=I N X-1$
IF (INX1.EQ.0) GOTO 55
DO $3 I=1$, INXI
3 IS=L(IS)
55 INDEX $=$ IS
FETUKN
END
C.

C
SUBROUTINE FEALAT (FLNAME, A, B,N,IF)
DIMENSION A(1) DB(1)
INTEGER FLNAYE (3)
FEWIND 9
C OFEN INFUT FILE
CALL SETFIL (9,FLNAME)

IF (IEFKOF (103) .NE.0) G0TO 99
C NUMEEK OF FOINT SUFFLIED
KEAD (9,20)N1
20 FOKMAT (I2)
IF (N.GT.N1)GOTO 100
C IMFUT THE MATA FOINTS
$\operatorname{FEAD}(9,10)(A(1), B(I), I=1, N)$
10 FORMAT (F12.4)
ENDFILE 9
FEETUKN
99 ENDFILE 5
101 IF=1
RETURN
100 IF $=2$
REETUKN
END
c.

C
SUEFROUTINE SAVE (A,BFN)
COMYON/IO/IN, IOUT
INTEGER FILE (3)
DIMENSION $A(1)$, B(1)
C GET FILE NAME FROM THE USER THROUGH KEYEOARD
WRITE (IOUT,IO)
10 FORMAT (///////////60X,~~~FILE NAME:?~)
Call messag (*
\& ハ")
FEAD (IN,20)FILE
20 FOKMAT ( 2A4,A2)
C WFITE OUT DATA F'OLNTS
CALL WFTTUAT (FILE,A,B,N)
FETUFN
EMS
C

C
SUBROUTTINE SORTX (XI,YI,N)
DIMENSION XI (1),Y1 (1)
$H 1=N-1$
C FEEFFOKM THE SORT
DO $3 I=1$ N1 DO $2 \mathrm{~J}=\mathrm{I}, \mathrm{NL}$

IF (XI (I). LE. XI (J+1) )GOTO 2
A $1=X 1$ (I)
$B 1=Y 1(I)$
$X 1(I)=X 1(J+1)$
$Y 1(I)=Y 1(J+1)$
$X 1(J+1)=A 1$
$Y 1(J+1)=B 1$
2 CONTINUE
3 CONTINUE
RETURN
ENS
C

C
SUBFOUTINE TABLE
C IHFUT COHMON DATA AREA
COMMON /JATSUF/NFSTNFI (50), IFFEES,X(50),Y(SO),L(50),IH(5),M(5)
4 , HETHOD, IHELF, IFREV, BUUND (2), SUBSET, INTFNT , IE (2)
COMMON /IO/IN:IOUT

INTEGER S1.52.SUBSET
CALL. CUFF'OS (2.1710.)
c outfut data columin headings
WFITE (IOUT, 10)

S2=IH(1)
S1=L (S2)
IF (S1.NE.0)GOTO12
WFILTE (IOUT, 11) $X(S 2), Y(52)$
11 FDFMAT (" $1 * 2 X, 2(E 11.4,3 X))$
RETUFN
C OUTFUT TABLE ITEMS FROM LINK LIST
$12007 \mathrm{I}=1,50,2$
$\mathrm{J}=\mathrm{I}+1$
WRITE (IOUT, 20) I,X(S2),Y(S2) , J,X(S1),Y(S1)
20 FGRMAT (12,2X,2(E11.4,3X),12,2X.2(E11.4,3X))
S2=L (51)
IF (S2.EQ.0) GOTO 15
S1: $=$ (S2)
LF (S1.NE.0) GOTO 7
$\mathrm{I}=\mathrm{I}+2$
WRITE (IOUT, 30) I:X(S2) YY(S2)
30 FOFMAT (I2,2X,2(E11.4,3X)) GOTO 15
7 CONTINUE
15 FETURN
END
C

C
SUBROUTINE UPDATE
C IAKPUT COMMON AREA

4 , METHOD, IHELF, IF'REV, BCUND (2) ,SUESET, INTFNT, IE (2)
INTEGER SUESET
IK=IH(1)
10 $1 \mathrm{~J}=2,5$ 10 $2 K=110$

IK=L(IR) IF (IR.EQ.O) GOTO3
CONTINUE
IH (J) $=$ IF
CONTINUE
RETURN
END

C
SUBFOUTINE WRTIUAT (FLNAME,A,B,N)
DIMENSION A(1), B(1)
INTEGER FLNAME(3)
FEWINE 9
C OFEN OUTFUT FILE
CALL SETFIL (9,FLNAME)
C STORE DATA FOINT ON THE FILE
WKITE $(9,20) N$
20 FOFHAT (I2)
WFITE $(9,10)$ ( $A(1), B(I), I=1, N)$
10 FORMAT (F12.4)
ENDFILE 9
FETUF'N
END

C
C
C
C
C THIS MODLLE HANDLES THE FOLLOWING INTEFACTIUE DISFLAYS:
C. 1.FOLYGONAL FLOT

C 2.FAKAMETER ENTEY
C

C
C
C*********** MAIM FROGFAKM-MOLULE 2 ***********************
C
C INFUT COMMON DATA AREA
COMMON/DATSUF/NFS,NFI (50) , IFREES, X(50) , Y(50), L (50), IH(5),H(5)
\&
, METHOD, IHELF', IFFEV, BOUND (2), SUBSET, INTFNT, IE (2)
COMMON/IO/IN, IOUT
C. EXECUTABLE FROGKAM MODULE NAMES

DATA MOW 3 , HELF' ; HODL $1 /$ "MOD3" , "HELF", "EXFLICIT" $/$ LOGICAL* 1 HODL 1 (10), HOWL3(10), HELF(10)
INTEGER SUBSET
C fieab in common data file
CALL FUCOMi
C INITIALISE JISFLAY TERMINAL
CALL TXOFEN
IN=5
IDUT=6
IF (IHELF.NE. 0 ) GOTO 6
IF (IFREV.GT.1) GOTO 5
IF (IFREU.EQ. 1) GOTO 4
C FOLYGONAL EISFLAY
3 CALL FGLYGL ( $X, Y, N F S$ IIC)
C FASS CONTROL TO AFFRROFRIATE FART OF THE FROGFAM GOTO (1,2,20,20,20,20,25,20,30), IC
C FFEVUIOUS DISF'LAY
2 IF'REV=1
IHELF $=0$
C. save infut comion data akea

CALL WRCOM1
CALL OURLAY (MOCLL
C BRINGS THE PAFAMETER ENTRY DISF'LAY
1 CALL FARMET (METHOD, SUBSET, INTFNT, BOUND,NFS,IE, IC)
CALL CUFFROS (410.,780.)
GOTO(10,3,25:1,30), IC
C NEXT DISFLAY
10 IF'REV $=0$
IHELF $=0$
CALL GEEOWN (MOCLS
C. TERMINATE FROGRAM

30 CALL EXIT
20 STOF
4 IFKEV=0
IHELF: $=0$
goto 1
C HELF IISFLAY
25 CAlLL WKCOM1
CALL OURLAY (HELF')
STOF
5 CALL ERFMES(IC)
GOTO (1,20), LC
C FETUKN FFOM HELF
$6 \operatorname{GOTO}(3,1)$, IHELF

```
C
C ******************* FOLYGONAL FLOT OF DATA FOINTS****************
C
        SUBFOUTTINE FOLYGL(A,B,N,IC)
C FLLOT THE DATA FOINTS SUFFLIED AND JOINED WITH STFAIGHT LINES
    COMMON/IO/IN.IOUT
C MENU ITEMS
    DATA MNTXT/" + NEXT + FREUIOUS+ GRAFH + COORNS. + IIISF.OFG+
&AX. MAFK+ HELFF + FESTAFTT + EXIT */
        LOGGICAL*1 HNTXT(90)
        DIMENSION A(1),B(1);XO(50),YO(50)
        EXTERNAL FFLOT
C FREFARE DISFLAY
1 CFLLL TXCLER
    ICORD:O
    WRITE(IOUT,10)
10 FONMAT ("FOLYGONAL FLOT :-")
C. OUTFUT MENU ITEKS
    CALLL MNDFEEN(875.,715.,1)
    CALL MNOISF (YNTXT,9,10,1)
    CALLL FFAKKE (870.,733.,9)
    CALL FEMLNK (XO,YO)
C FINN KAXIMINM & KINIHUM OF LATA FOINTS
    CALL MINMAX(S1,S2,S3,S4,X0,YO,N)
C SET UF CUFSOK FOR USER ACTION
2. CALL LMTARA
    CALLL MNFICK (J,ICHAER MNDD)
    IF (J.EO. 4.AND. ICOKD.EO.2)GOTO2
C CONFIRM USER ACTION
7 CALL CONFRM(ICHAR)
    IF (ICHAR.EQ.7B)GOTO 2
    IF (ICHAF.NE.89) GOT0 7
    G0T0(20,20,3,4,5,6,20,1,20),J
C BACK TO CALLING FROGRAM
20 IC=J
    RETUKN
C GFAFH(FILOT THE CLRVE)
CALLL LFAW (FFLOT,R,S1,S2,53,S4,N)
    GOTO 2
C DISFLAY CURSOR COORDINATE INFUT
    4 CALL DISCOR(ICORD,S1,S2,S3,54)
    gOTO 2
C IISFLAY OKIGIN
    5 CALL HLSORG(S1,S2,53,54)
        GOTO 2
C AXES MAFKING
6. CALL AXSMFK (S1,S2,S3,S4)
    gOTO.2
    END
C
C ***************** FAKAMETER DISFLAY ENTKY ****************************
C
    SUBROUTINE F'AFMET (KYSUBT,INTFNT,L,N,IE,IC)
    COMMON/ID/IN,IOUT
C MENU ITEMS
    DATA MNTXT1/" + NEXT + FREVIOUS + HELF* + FESTART + EXIT * *
    DATA HNTXT2/** COMPLETE+ SUBSET + SUBSET
&+ SFECIFY + DEFALLLT + CURSOR */
    DATA MAITXT3/" + CLAMPED + RELLAXED + FAARAEOLA+ Q-SFLINE*/
    DATA HNTXT4/* + EQ.SFAGE+ NE.SFACE */
    DATA MNRTXT5/"+ BOUNDAFFY//
```

```
    LOGICAL*1 MNTXT1(50),HNTXXT2(80),MNTXT3 (40), MNTXT4(30),
                        HNTXTS(10)
        INTEGER SUBT
        DIMENSION B(2),IE(2)
        CALL TXCLER
C SET vEFAULT VALUES
    SUBT=OO.
    10=0
    INTFNT=0.
    B(1)=0.
    B(2)=0.
    IF(M.NE.2) GOTO 112
    IE (1) =21
    IE (2) = 1
    g0T0 1011
    IE(1)=1.
    IE (2)=1.
C SET DISFLAY READY
1011 WRITE(IOUT,10)
10 FOKHAT ("FARAMETER ENTRY:-"/)
    GOTO (101,102,103,104,105,106,108),M
20 CALL CUKFOS(1.,660.)
    WRITE (1ONT,21)
C EISFLAY INSTFUCTIDNS TO GUIDE THE USF
21 FOKMAT *"SELECT THE AFFROGRIATE OFTION FROM THE */
& "FOLLOWING PARAMETER SFECIFICATION(*) :-"///
& : 6X,"1-DATA TYFE:-*/8X,"(FOR JOINING",22X,"FIRST*/
& 9X;"CURUES)",22X,"SUESEQUENT"//6X,"2-CHOICE OF INTERMEDIATE*/
& 7X,* FOINTS FREUIRED FOR SMOOTH DRAWING:-*//\
    IF (M.NE.7) GOTO 1220
    WFITE (IOUT,15)
15 FORMAT (//6X,*3-SELECT THE CONDITION*)
1433 WRITE(IOUT,1333)
1333 FOKMAT (7X;" AT EACH END OF THE CURUE:-*/
&
&
                                    8X,"N.B:-LEFT-HAND END TYFEE '1**/
                                    11X;* RIGHT-HAND END TYFE '2'*)
    GOTO 143
1220 IF(M.NE.2) GOTO 1221
    WFITE(IOUT,14)
14 FOFWAT (/6X,"3-X-SFACING OF DATA FOINTS SUFFLIED:-*/)
    WKITE (IOUT,16)
    16 FOFHAT (/6X,"4-INDICATE YOUK CHOICE OF END*)
    G010 1433
1221 IF(M.EQ.1.0K.H.EQ.6) GOTO 142
    WFITE (IOUT,22)
22 FORMAT (/6X,"3-EOUNDARY CONDITION:-"//)
143 WRITE (IOUT.7)
7 FORMAT (/////////** IF NO AFFFROFRIATE PARRMETER IS SELECTED *
& /"WHEN REQUINED THEN DEFAULT VALUES ARE ASSUMED")
C DISFLAY CONTFOL COMMAND
    CALL HNOFEN(875.,715.,1)
    CALL HNDISF'(MNTXT1,5,10,1)
    CALLL FRAME (870.,733.,5)
    CALL MNDFEN(670.,565.,2)
    CALL MNDISF(KNTXT2,8,10,2)
    CALL DTEXT (810.,565.,**',1)
    CALL DTEXT (810.,455.,**',1)
    IF (M.NE.7) GOTO }91
    CALL MNDISF(NNTXT3,4,10,2)
    CALL DTEXT (810.,365.,'*',1)
    MF=12
    6010 88
```

```
919 IF(M.NE.2) GOTO 99
    CALL MNDISF'(HNTXT4,3,10,2)
    CFLLL LITEXT (810.,365.,'*',1)
    CALL MNDISF (YNTXT3,3,10,2)
    CALL DTEXT (810.,300.,'*',1)
    MF==14
    GOTO }8
142 WFITE(IOUT,1420)
1420 FORMMAT (////)
    GOTO 143
99 HF=7
    IF(M.EQ.1.OR.H.EQ.6) GOTO 88
    CALL MNDISF(MNTXTS,1;10,2)
    MF=9
88 CALL FRAME(663.,582.,TF)
    CALL TXMOUE (665.,505.)
    CALL TXDFAW(805.,505.)
    IF (M.EQ.1.OK.M.EO.6) GOTO 2
    CALL TXMOUE(665.,420.)
    CALL TXDFAN(805.,420.)
    IF (M.NE.2) GOTO ?
    CALL TXHOVE(665.,350.)
    CALL TXDRAN(BO5.,350.)
2 CALL MNFICK(J,ICHAK',NNO)
C WHICH MENU ?
    IF (MNO.EQ.2) GOTO 130
C CONFIFM USER REQUEST
5 CALL CONFRM ICHAR)
    IF (ICHAK.EQ.78)GOTO 2
    IF (ICHAR.NE.B9)GOTO 5
    IF (J.EQ.4) GOTO 1
    IF (H.NE:2) GOTO }70
    IF (IQ.EQ.10) IE (1) mIE (1)+10
    IF (IQ.EQ. 20.OK.IO.EQ.0)IE(1)=IE(1)+20
707 IC=\
    FETUKN
C F'ARAMETER SFECIFICATION CONTROL
130 GOTO(31,32,33,34,35,36,37,38,39,40,41,42,43,43),J
C COMPLETE CURUE
SI SUBT=0
    goto 2
C CURVE SEGMENT
32 SUBT=1
    GOTO 2
C CUKVE SEGMENT & SUBSEQUENT SUBT
33 SUBT=2
34 G0TO 2
C USER SFECIFIED NUMBEK OF INTERKEDIATE FOINTS FER INTKEVAL
35 CALL CURFOS(1.,220.)
66 CALL MESSAG("** HUMEER OF INTEFFOLATED FOINTS FER INTEENAL?N*)
    IF (IERFOR(110).NE.O) GOTO 171
    READ(IN,77) INTF'NT
77 FORMAT (GO.O)
    ISUM=INTPNT* (N-I)+N
    IF(ISUM.GT.200) GOTO 187
    GOTO 2
171 ENDFILE 5
    GOTO 66
187 WFITE(IOUT, 403)
403 FORMAT "TOTAL NUMBER OF FOINT EXCEEDING LIMIT,TFY AGAIN")
    GOTO 66
C DEFAULT OFTIONS
```

INTFMT=0 GOTO2
C CUFSOK
37 INTFNT=999
38 GOTO2
C. BOUNDAAK'Y CONDITION/X-SFACING
$39 \quad \operatorname{BOTO}(2,399,139,139,139,2,391), \mathrm{H}$
GOTO 2
391 IF (ICHAR.EQ.49.OF.ICHAR.EO.50) GOTO 392
GOTO 2
392 ICHAK=1CHAF-48
GOTO (272, 202) , ICHAR
GOTO 2
272 IE (1) =1
C USEK INFUT BOUNDARY CONDITION
2721 CALL. CURFOS (1.,195.)
2120 CALL MESSAG("* SLOFE BOUNDARY VALUE (IST END)? ? *) IF (IERFOR (110). NE.0) GOTO 2120
READ (IN.1110) B(1)
1110 FORMAT (GO.0)
GOTO 2
202 IE (2) $=1$
2021 CALL CUFFOS (1,.170.)
2110 CALL MESSAG("A SLOFE BOUNDARY VALUE (2ND END)? ?")
IF (IEFROF (110). NE. O) GOTO 2110
READ (IN,1110) B(2)
GOTO 2
$399 \quad 10=10$
GOTO 2
139 CALL CURFOS(1.5195.)
404 CALL MESSAG ("\# BOUNDAFY VALLEE OF END FOINT CONDITIUN?"~) IF (IEFKOF (110).NE.0) GOTO 404
FEAD (IN,11) B(1), B(2)
11 FOKMAT (2G0.0)
GOTO 2
C NOT EQUAL SFACING
$40 \operatorname{GOTO}(2,444,2,2,2,2,411), M$
$444 \quad 10=20$
GOTO 2
$41 \operatorname{GOTO}(2,2,2,2,2,2,411), H$
411 IF (ICHAR.EQ.49) IE (1) $=5-8$
IF (ICHAR. EQ. 50 ) IE (2) $=\sqrt{ }$ - $B$
GOTO 2
$42 \operatorname{GOTO}(2,421,2,2,2,2,411), H$
421 IF (ICHAK.EQ.49.OR.ICHAR.EQ. 5O) GOTO 422
60102
422 ICHAF=ICHAR-48
GOTO (4211 +4222) , ICHAR
GOTO 2
$4211 \quad I E(1)=J-11$
GOTO 2721
4222 IE (2) = $4-11$
GOTO 2021
$43 \quad \operatorname{GOTO}(2,431,2,2,2,2,2), M$
431 IF (ICHAR.EQ.49)IE (1) $=5-11$
IF (ICHAF.EQ. 50 ) IE (2) $=J-11$
GOTO 2
101 WFITE(IOUTIII1)
C OUTFUT ALGOFITHM TITLES
111 FOFMAT (**** GLOBAL FOLYNOMIAL INTEFFOLATIDN(NEWTON FOFIM)****)
goto 20
102 WRITE(IOUT,122)
goto 20
122 FOFMAT ("***PIECEWISE QUINTIC FOLYNOMIAL INTEFFOLATION****
\& 12 X ," (VAFIABLE END CONDITION) ")
103 WRLTE(IOUT,133)
133 FORMAT (* ** CUBIC SFLIINE (SECOND UERIVATIVES END CONDITION) ***) GOTO 20
104 WFITE(IOUT,144)
144 FORMAT ("*** CUBIC SFLINE (SECDND IUERIVATIVES END CONDITION(*) ) ****) WFITE (IOUT,1404)
1404 . FORMAT (6OHWHERE $Y^{\sim}[X 1]=U * Y^{*}[X 2] \& Y^{*}[X(N-1)]=N * Y^{\sim}[X(N)]$ SFFECIFY U \& $V$ ) goto 20
105 WRITE(IOUT,155)
GOTO 20
155, FORMAT (**** CUEIC SFLINE (FIRST DERIVATIUES END CONDITION)****)
106 WRITE (IOUT,166)
166 FORHAT (**** CUBIC SFLIME (FERIODIC END CONDITION) ****) GOTO 20
108 WFITE(IOUT,188)
188 FOKHAT ("****CUBIC SFLINE (VAKIABLE END CONDITION)****") GOTO 20
ENB
c
 C

SUBFOUTINE ERFMES (IC)
COMMON/IO/INIIOUT
C KENU ITEMS
DATA KNTXT/" + FREUIOUS+ HELFF + RESTAFT + EXIT */
DATA DATSF//"DATSUFFL"
LOGICAL*1 MNTXT (40), DATSP (10)
1 CALL TXCLER
WRLTE (IOUT, 20)
20 FORMAT "EERROR MESSAG:-"/"TOO MANY FOINTS FOR JOINNING CLKVES"/
\& - "WHICH EXCEED CORE LIMIT"/

* "YOU HAY FFOCEED BY TAKING THE FOLLOWING ACTION:-*

4
8
4
4
"EITHEF 1- USE FFEUIOUS COMMAND TO 60 BACK TO FAFAMETER" $/$
"DISFLAY;SO THAT TO ALTER NO. OF INTERHEDIATE FOINTS."/
"OF 2- USE HELF' COMMAND IN ORDER TO BFANCH TO ANY";
"DISFLAY DE.G DATA ENTFY OF DATA TABULATION DISFLAYS..ETE")
CALL MNOFEN $(875,1760.1$ 1)
CALL KNOISF (FNTXT:4,10,1)
CALL FRAME (870.' $778 ., 4$ )
120 CALL MNFICK (JIICHAFITHNO)
110 IF (ICHAR.EQ.7日) GOTO 110
IF (ICHAK.NE.89)G0TO 120
GOTO (40.40,1,50) :J
C FFEUIOUS DISFLLAY
$40 \quad$ IC $=\mathrm{J}$
RETURN
50 CALL FiMFILE (DATSF')
STOF'
END
c

C
SUBKOUTINE FF'LOT (Ki,SCL1,SCL2,SCL3,SCL4,N)
C INFUT COMMON DATA
COMMON/LATSUF/NF'S.NFI (50) , IFREES, X(50) y Y(50) ,L(50) ; IH(5) ,M(5)
4 , KETHOU, IHELP, IFREV, BOUND (2), SUBSET, INTFNT, IE (2)
DIMENSION XO (50) YO (50)
C REMOUES LINKS FROM INFUT DAT'A
CALL REPMLNK (XO,YO)

HO $1 I=1, N F S$
IF (I.EQ.1) GOTO 2
C JOIN DATA FOINT WITH LINE SEGMENTS
CALL TXDFFAW (XO(I) YO(I))
2 CALL FLUSGN(SCL1,SCL2,SCL3,SCL4,XO(I),YO(I))
1 CALL TXHOVE (XO(I), YO(I))
RETUFN
END
c
c
C
C
c this modlle handles the following interactive disflays:-
C 1.CURUE FIT
c 2.CURVE ZOOM
C.
c
C
C********* MAIN FRRGRRAK-KODULE 3 *************************
c
c i/O common data afiea

\& , METHOD, IHELF', IFFEV, EOUND (2) , SUBSET, INTFNT, IE (2) COMMON/CURVEF IT/COEF $(50,6), X C O R D ~(200), ~ Y C O R D ~(200) ~$ COHMON/ID/IN, IOUT
c. overlay executable frogriam name

\&"MOE7"
[DATA HELF/"HELF"/
integer subset
LOGICAL*1 MOLL 1 (10), HONL2 (10), MODL5 (10), MODL6 (10), MODL $7(10)$
LOGICAL*1 HELP(10)
CALL TXOFEN
C fiead i/o common data files
CALL RDCOM1
IF (METHOD.NE. 1 ) GOTO 1110
$\mathrm{NC}=1$
goto 21
1110 IF (METHOD. NE. 2)GOTO 11
NC=6
goto 21
$11 \quad \mathrm{NC}=4$
$21 \quad$ IN $=5$
IOUT $=6$
CALL ROCOM2 (NFSTNFI,NC)
C CALL CLKVE DESIGN DISFLAY
IF (INTFNT.EQ.999) GOTO 111
C CURUE FIT DISFLAY
CALL CKUFIT (NFS,NFI,XCORD, YCOKD, COEF,SUBSET,IC)
GOT0(2,3,2,2,2,6,7,8,2,10,111,2,2,14,2,15,2,22), IC
C FFGGRAM TERKINATION
22 CALL EXIT
2 STOF:
c. FREUIOUS DISFLAY
$3 \quad$ IFREV $=1$
IHEL.F' $=0$
CALL WRCOM1
CALL OUFLLAY (MOLL2)
C. COMflete table of interfolated data foints

6 IFriEv $=1$
100 IHELF=0
CALLL WRCOH1
CALL OURLLAY (HODLG)
c DISFLAY JOINED CURVE SEGMENTS
$7 \quad$ IFKEV $=0$
IHELF=0
CALL WRCOM1
CALL OUFL.fiY (MODL 7 )
C SUFERIMFOSED CURVES DISFLAY

```
8 IF'FiEU=3
    GOTO 100
C EFROR REFERENCE
10 IFKEV=2
    GOTO 100
C CINRE DESIGN DISFLAY
111 IFFEU=0
    IHELF:=0
    CALL WFCOM1
    CALL OUFLAY (MOULS)
C ALGORITHM IISFLAY
14 IFREV=0
    IHELF:=0
    CALL WRCOM1
    CALL OURLAY (HOLL1)
C. HELF DISFLAY
15 CALL WFCOMI
    CALLL QURI_AY (HELFF)
    END
C
C #**************** CLINUE FIT DISFLAY ROUTINE ***************************
C
    SUBROUTINE CRUFIT (N,Ni,XX,YY,C,SUBT,IC)
    COMYON/CURUES/NCEV (10) &XYSCL (4)
    CDMHON/IO/IN,IOUT
C MENU ITEMS
    DATA MNTXT1/"* + NEXT + FREUIOUS+ GRAFH + CONRUS. + DISF..OFG
&+ TAELES + JOIM CRV+ NGFAFH */
    DATA MNTXT2/*+ ZOOM + ERRO.FEFF CRV.DES. + SAVE + REDNAW
&+ METHOUS + AX. HAKKK+ HELFP + RESTART + EXITT */
    DIMENSION N1 (1),XX(1),YY(1),C(50,6)
    LOGICAL*1 HNTXT1(80) %MNTXT2(100)
    EXTERNAL CFLOT
    IF (IERKOK(103).NE.0) GOTO 99
    CALL RDCEVS
99 MSUM=0
    N2=N-1
C COMFUTE TOTAL NLMBER OF INTERFOLATED FOINTS
    DO 6 I=1,N2
6 HSUM=MSUKINI (I)
    HSUM=MSLMT+N
1 CALL MINMAX(S1,S2,S3,S4,XX,YY,MSUM)
    CALL TXCLER
    ICORD=0
    JON=0
    NG=1
C SET UP CURVE FIT DISFLAY HENJ
    WRITE(IOUT,IO)
10 FOFNLAT(*CURVE FIT&-*)
    CALL HNOPEN(875.,715.,1)
    CALLL MNDISF(MNTTXT1,8,10,1)
    CALL HNDISF'(YNTXT2,10,10,1)
    CALLL FKAMKE (870.,733.,18)
C SET LF' CURSOR FOR USER CHOICE FROM THE MENU
2 CALL LMTARA
    CALLL MNFICK(J,ICHAR"MNO)
    IF (J.EQ.4.AND.ICOFD.EQ.2) GOTO 2
    IF (J.EQ.8.ANU.NG.EQ.2) GOTO 3O
17 CALL CONFFM (ICHAR)
    IF(ICHAF.EQ.78) GOTD 2
    IF (ICHAF.NE.89) GOTO 177
C TFANSFEK CONTFOL ACCOKDING TO USER CHOLCE OF THE MENU
```

    G0T0 ( \(30,30,3,4,5,30,7,8,9,30,30,11,12,30,15,30,1,30), J\)
        IC=J
        RETUFN
    C DRAW THE CURVE
3 CALL ERAW (CFLOT,R,S1,S2,S3,S4,MSUM)
GOTO 2
C CUKSOR COORDINATE INFYT
4 CALL IISCOR (ICORD,S1,S2,S3,54)
GOTO 2
C DISFLAY AXES OFIGIN
5 CALL DISOKG(S1,52,53,S4)
GOTO 2
C SAVE CURFENT CURVE ON DISC FILE
11. CALL CEVSAV (XX,YY,N,N1,MSUM,S1,S2,S3,S4,J)
GOTO 2
C FLOT AUKUE FROM NAMED FILE
12 CALL FELFAW (XX,YY,N,N1,MSUK,S1,S2,S3,S4)
GOTO 2
C. AXES MARKING
15 CALL AXSHRK (S1,S2,53,54)
GOTO 2
c CuFVE JOIN
7 IF (SUBT.EQ.O)GOTO 2
$10 N=10 N+1$
IF (JON.EQ.2) GOTO 77
CALL DTEXT (730.1585., "JOIN DISF.", 10)
CALL SETJON (XX,YY, HSUM,N,N1, SUBT)
GOTO 2
C BACK TO CALLING PROGRAM
77 IC=7
FETUFN
C NGRAFH COMMAND FOR THE FIRST TIME (I.E SAVE CURVE FOR LATER USE)
8 CALL NGFAPH ( $\mathrm{N}, \mathrm{N} 1, \mathrm{MSUM}, \mathrm{XX}, \mathrm{YY}, \mathrm{S} 1,52,53,54,1$ )
CALL WKCRUS
$N G=N G+1$
GOTO 2
C ZOOMING
9 CALL ZOOM (XX,YY,C,S1,S2,S3,S4,IC)
GOTO ( $1,31,90,90,90,90,90$ ), IC
90 IF (IC.ER. 3 ) IC=14
IF (IC.EQ.5) IC=16
IF (IC.EQ.4.OR,IC.EQ.6) STOP
IF (IC.ER.7) IC=1B
31. FETUEN
ENB
C

C
FLINCTION CFLOT ( $\mathrm{F}, \mathrm{XO}, \mathrm{YO}, \mathrm{X}_{1}, \mathrm{Y} 1, \mathrm{~N}$ )
C $1 / 0$ COMMON DATA AFEA
COMMON/DATSUP/NFS,NF'L (50), IFREES, $X(50), \because(50), L(50)$, IH(5), M(5)
2
, METHOD , IHELF', IFREU, BOUNB (2), SUESET, INTFNT, IE (2)
COMMON/EURVEF IT/COEF $(50,6), \times C O F D ~(200)$ Y YCOFID (200)
IMTEGER SUBSET,R
IF $=1$
$I F=1$
$I=1$
C FLOT SUFFLIED BATA FOINTS
3 CALL FLUSGN(XO,YO,X1,Y1,XCOKW(I),YCOFO(I))
CALL TXMOVE (XCORD (I), YCORD (I) )
IF (I.EQ.N) KETUFN
$I F I=I F+1$

```
    IF'2=IF'+AF'I(IF)+1
C FLOT INTERFOLATED FOINTS BETWEEN THE INTERVALS
    DO 1 J=1F'1,IF'2
1 CALL TXDFIAW (XCORD (J),YCORD (J))
    IF=IF=2
    IF=IF+1
    I=I+NFI I (IF-1)+1
    GOTO 3
    END
C
C*************SAVES THE CUKVVE ON FILE FOR LATER USE*********************
C
    SUBROUTINE CFUSAU(XX,YY,N,N1,MSUM,SCL1,SCL2,SCL3,SCL4,J)
    BIMENSION XX(1j,YY(1),N1(1)
    INTEGER FILE(3)
    N2=N-1
    IF (J.EQ.8) GOTO }8
C USER FILE NAME ENTRY
    CALLL CUKFOS(10..730.)
    CAl.L MESSAG("FILE NAME?"N*)
    CALL GETFLN(FILE )
    FEWIND }
C OFEN AN OUTFUT FILE WITH USER SUFLIED NAME
    CALL SETFIL(9,FILE)
88 WRITE (9,20) HSUM,N
        WRITE (9,30) (XX (I),YY(I),I=1,MSUM)
        WKITE (9,25) (N1 (I),I=1,N2}
        WFITE(9,35)SCL,1,SCL_2,SCL3,SCL4
        FORMAT (13)
        FOFMAT (213)
        FORMAT (F11.4)
        FORMAT (4F11.4)
        ENDFILE 9
        FETURN
        END
C
C****************INPUT FILE NAFRE****************************
C
    SUBROUTINE GETFLN(NANE)
    COMMON/10/IN,IOUT
    INTEGER NAME (3)
    READ (IN,10)NAME
    FORHAT (2A4,A2)
    RETURN
    END
C
C *******SAUES CURVES FOR SLRERIMPOSED DISFLAY***************
C
    SUBKOUTINE NGFAPH(N,N1;MSUM,XX,YY,SCL1,SCL2,SCL3,SCL4;J)
C COMMON BATA AREA FOR SUFERIMFOSED DISFLAY
    COMMON/CURVES/NCRV (10) ; XYSCL. (4)
C DISFLAY MENU ITEMS
    DATA SUFFLS/"CLKVE1 CURVE2 CURVE3 CLKVVE4 CLRVES
ACURVEG CURVET CURVEB CURVE9 CURVEIO */
    LOGICAL*1 SUFFLS(100)
    k=0
C FIND FREE ENTKY
    DO 1 I=1,10
        IF (NCEV (I).NE.99) GOTO 2
        K=K+9
1 CONTINUE
C. MARK LAST FREE ENTF'Y
```

        NCEV (I) \(=99\)
        \(K=k+I\)
        FEWIND 9
    C OFEN INFUT FILE \& SAVE THE CURVE
CALL SETFIL (9, SUF'FLS (K) )
CALL CEVSAU (XX,YY,N,NL,HSUM,SCL1,SCL2,SCL3,SCL4, J)

C FIRST CUFVE
IF (NCRU (1).EQ. 99) GOTO 3
C SET CUFVE SCALLING
XYSCL (1) =SCLL 1
XYSCL (2) $=$ SCL 2
$X Y S C L(3)=$ SCL 3
$X Y S C L(4)=S C L 4$
GOTO 4
C SUBSEQUENT CUNUES ES SET THE DISFLAY SCALE
3 IF (XYSCL (1).GT.SCL1)XYSCL (1) $=$ SCL 1
IF (XYSCL (2), GT. SCL 2) XYSCL. (2) =SCL2
IF (XYSCL (3) . LT . SCL 3) XYSCL (3) =SCL 3
IF (XYSCL (4) .L.T.SCL4) XYSCL (4) $=$ SCLL 4
C CALL SUFERIHFOSED DISFLAY COMAND
4 CALL DTEXT (725.,555.,"+ GRAFH",7)
ENDFILE 9
FETUFN
END
C

C
SUBROUTINE RDCRUS
COMMON/CURUES/ACRV (10) , XYSCL (4)
FEWIND 7
CALL SETFIL (7, "SUPCENVES")
$\operatorname{FEAD}(7,10)(\operatorname{NCFV}(1), I=1,10)$
$\operatorname{READ}(7,20)$ (XYECL (I) , Im1,4)
$\begin{array}{ll}10 & \text { FORHAT (I2) } \\ 20 & \text { FORMAT (F11.4) }\end{array}$
ENDFILE 7
RETUFW
END
C
C*********FLOT CLRVE FROM DATA FILE $\# * * * * * * * * * * * * * * * * * * * * * * * * ~$
c
SUBROUTINE REIMRAW (XX,YY,N,N1,MSUM,SCL1,SCL2,SCL3,SCL4)
COMMON/IO/LN, IOUT
DIMENSION XX(1),YY(1),N1(1)
INTEGEF FILE (3)
CALL MESSAG (" YILE NAME?**)
CALL GETFLN(FILE)
FEWIND 9
CALL SETFIL (9,FILE)
FEAD (9, 25) KSUM, N
N2=N-1
KEAL $(9,30)(X X(1), Y Y(1), I=1$, KSUM $)$
FEAD (9,20) (N1 (I) , I=1, N2)
FEAL (9,35) SCL 1, SCL 2, SCL 3, SCL 4
20 FOFMAT (I3)
25 FOFMAT (2I3)
30 FORHAT (FiL. 4)
35 FORMAT (4F11.4)
CALL LMTSCL (SCLI,SCL2,5CL3,SCL4)
CALL CFLLOT (F, SCL 1,SCL2,SCL3,SCL 4 , HSUM)
ENDFILE 9
FETURN

END
C

C
SUBROUTINE SETJON(XX,YY,MSUK,N,N1,SUBT)
C JOIN COMMON DATA AREA
COMMON/JOIN/CJ1 (500), CJ2 (500), J3 (12), $\mathrm{J4}(100)$, IFNTK (6)
DIMENSION XX(1),YY(1), N1 (1)
INTEGEF SUBT
IF (IERROK (103). NE.0) GOTO 7
C READ THE JOIN COMMON DATA AFIEA
CALL $\operatorname{FDCOM}$
7 IF (SUBT.EQ.2) GOTO 1
C SET ARFIAY JOIN FOINTERS
$J 3(1)=1$
$J 3(2)=5$
$\mathrm{J} 3(3)=\mathrm{N}$
$\mathrm{J} 3(4)=2$
$\mathrm{J} 4(1)=\mathrm{N}$
10 $2 I=2, N$
$2 \quad \mathrm{~J} 4(\mathrm{I})=\mathrm{Ni}(\mathrm{I}-1)$
IFNTK (1) $=3$
IFNTR (2) $=1$
C STORE THE JOIN CURVE FOF JOIN DISFLAY
$4 \quad \mathrm{IF} 1=\mathrm{J} 3$ ( 1 )
DO $3 \mathrm{I}=1$, HSUM
C. 1 (IF1) $=X X(I)$
$\mathrm{CJ} 2(\mathrm{IF} 1)=\mathrm{YY}(\mathrm{I})$
$\mathrm{IP} 1=1 \mathrm{~F} 1+1$
3 CONTINUE
J3(1)=1F'1-1
C. WRite out the join common data area in outfut file

CALL WRCOMJ
FETUFN
c set fointer and save data foint of the seghent
$1 \quad \mathrm{~J} 3(\mathrm{~J} 3(2))=\mathrm{N}$
$\mathrm{J} 3(\mathrm{~J} 3(2)+1)=34(1)+1$
DO $6 \mathrm{I}=2, \mathrm{~N}$
$6 \quad \mathrm{~J} 4(\mathrm{~J} 4(1)-1+\mathrm{I})=\mathrm{N} 1(\mathrm{I}-1)$
$\mathrm{J} 4(1)=\mathrm{J} 4(1)+\mathrm{N}-1$
$33(2)=\int 3(2)+2$
IFNTK (IFNTK (1) $\}=\mathrm{J} 3(1)$
IFNTR ( 1 ) $=$ IFNTR ( 1 ) +1
GOTO 4
END
c
C********SAVE COMMON DATA FOF THE SUFERIMFOSED DISFLAY.
c
SUBROUTINE WFCRUS
COAMON/CUKVES/NCRV (10), XYSCL (4)
FEEWIND 8
C OPEN aN OUTfut File
CALL SETFIL (8,"SUPCRUES")
WRITE $(8,10)$ (NCKU ( 1 ), $I=1,10$ )
WRITE $(8,20)$ (XYSCL (1), $I=1,4$ )
10 FOFMAT (12)
20 FORMAT (F11.4)
ENDFILE B
RETURN
END
c
C. *********ZOOM DISFLAY ROUTINE*******************************

C
SUBFOUTINE ZOOM (XX,YY,C,SCL1,SCL2,SCL3,SCL4,IC)
C INFUT COMKON bata area
COMMON/DATSUF/NF'SINFI (50), IFREES,X(50),Y(50),L(50),IH(5),H(5)
4 , METHOD, IHELF, IFREU, BOUND (2) , SUBSET, INTFNT, IE (2)
COMMON/IO/IN, LOUT
C MENU ITEHS
DATA MNTXT/" + NEXT + FREVIOUS+ METHODS + AX. HAKK+ HELF'
$4+$ FESTAFT + EXIT */
DIMENSION $X X(1), Y Y(1), C(50,6), X 0(50), Y 0(50), C X(2)$
LOGICAL*1 MNTXT (70)
C REMOVES LINKS \& SET WINDOW
CALL FEHLNK (XO,YO)
CALL LMTSCL (SCL1,SCL2,SCL3,SCL4)
DY=(SCL4-SCL2) / 20
C SET ZOOMING WINDOW
101 1 $=1,2$
CALL TXCURS (CXX,CYY, ICHAR) CX(I) $=C X X$
$118 \quad$ CDY1 $=C Y Y+D Y$ CDY2=CYY-DY IF (CDY1.GT.SCL4.OR.CDY2.LT.SCL2) GOTO 117
CALL TXMOVE (CXX,CDY1)
CALL TXDRAW (CXX,CDY2) GOTO 1
$117 \quad$ BY $=$ EY $/ 2$. 6010118
CONTINUE
C SOKT SMALLER CXX
IF (CX(1).LT.CXX) GOTO 2
$C X(2)=C X(1)$
CX(1) =CXX
C DETEFMINE BETWEEN WHICH INTERVAL THE ZOOMED CURVE IS?
$2 \quad I F I=0$ I $=1$
3 IF (CX(L).LE.XX(I)) GOTO 4
$1 F I=I F 1+1$
$I=I+N P I(I F I)+1$
GOTO 3
$4 \quad K 1=I-N F I(I F 1)-1$ IF $2=0$ I=1
5 IF (CX(2).LE.XX(I)) GOT0 6 IF2 $=1 F 2+1$ $I=I+N P I(1 F 2)+1$ GOTO 5
$6 \quad K 2=I$
$L 2=K 1+N F I(1 F 1)+1$
DO 7 I=K1,L2
IF (CX (I).LE.XX(I)) GOTO 8
7 CONTINUE
$8 \quad K 3=\mathrm{I}-1$
$L 2=\mathrm{NPI}(\operatorname{IF} 2)+1$
B0 $9 \mathrm{I}=1, \mathrm{~L}$ 2
LI $\times$ K2- $1+1$
IF (CX(2).GT.XX(L1)) GOTO 11
$\begin{array}{ll}9 & \text { CONTINUE } \\ 11 & K_{4}=\mathrm{L} 1+1\end{array}$
C SET THE ZOOMED DISFLAY \& MEMU
CALL TXCLEE
CALL ALFHMD
WFITE (IOUT, 10)

10 FORMAT ("ZOOMING: -")
CALL LMTAKA
CALLL KNOFEN(875., 715.,1)
CALL MNDISP (MNTXT,7,10,1)
CALL FFKAME (870.,733.,7)
$51=X X(K 3)$
S3=XX(K4)
$52=Y Y(K 3)$
S4=52
DO $50 \mathrm{I}=\mathrm{k} 3, \mathrm{~K} 4$
IF (YY(I). GT.S4) S4=YY(I)
IF (YY(I).LT.S2) S2mYY(I)
50 CONTINUE
CALL LMTSCL (S1,52,53;S4)
CALL FFFAME (S1,52,53,S4)
C. LKAW THE ZOOMED CURVE
$L 1=K 1+\mathrm{NFI}(\mathrm{IF} 1)+1$
L2=K2-NFIL (IF2)-1
IF (L2.LT.L.1) GOTO 77
$I=L 1$
C FLOT THE SUFFLIED FOINTS IN THE ZOOMED FORTION
66 CALL FLUSGN(S1,S2,53,S4,XX(I),YY(I))
$1 F 1=1 F 1+1$
IF (I.EQ.L2) GOTO 77
$I=I+N P I(I F I)+1$
GOTO 66
77 CALL TXYOUE (XX (K3) ,YY(K3))
LI=K4-1
10 B8 Imk3,L1
$X X H=(X X(I)+X X(I+1)) / 2$ 。
10099 J=1,NF'S
IF (XXM.LT.XO(J)) GOTO 111
99 CONTINUE
$111 \quad \mathrm{~J}=\mathrm{=}$-1
IF (METHOD.EQ. 1) GOTO 888
T $=\mathrm{XXXH}$-XO (J1)
IF (METHOD.EQ. 2 ) GOTO 222
$Y Y M=C(31,1)+T *(C(J 1,2)+T *(C(J 1,3)+T * C(J 1,4)))$
GOTO 121
$222 T=T /(X O(\mathrm{~J})-\mathrm{XO}(\mathrm{J} 1))$
YYM=C $(J 1,1)+T *(C(J 1,2)+T *(C(J 1,3)+T *(C(J 1,4)+T *(C(J 1,5)+i * C(J 1,6)))))$
$121 \quad W 1=Y Y M-S 4$
W2=YYM-S2
IF (W1.GT.O.) YYMmS4
IF (W2.LT.O.) YYMmS2
CALL TXDFAN (XXYYYYM)
CALLL TXDRAW $(X X(I+1)$, $Y Y(I+1)$ )
88 CONTINUE
C DISF'LAY MENU
202 CALL LHTAEA
CALLL HNPICK (J, ICHAR, HNO)
17 CALL CONFRH (ICHAF)
IF (ICHAR.EQ.78) GOTO 202
IF (ICHAR.NE.89) GOTO 17
C TRANSFER CONTROL ACCORDING TO USER CHOICE
G0T0(414,414,414,404,414,2,414), J
$414 \quad$ IC $=\mathrm{J}$
FETURN
C AXES HAKKING
404 CALL AXSMRK (S1,52,53,S4)
GOTO 202
$888 \quad 12=N F \cdot 5-1$
${ }_{61}=\mathrm{C}(\mathrm{NF} \cdot \mathrm{S}, 1)$
[10 808 LL=1,N2
JJ=NFS-LL
$A=C(J J, 1)+(X X Y-X O(J J)) * A$
BOB CONTINUE
YYM=A
GOTO 121
END

```
C
    #******************
C * AFFENDIX 2.24 *
C
******************
C
C THIS MOUULE HANDLES THE CURVE LESIGN INTEFACTIVE IISFLAY.
C
C
C
C #***** KAIN FROGKAM - MODULEE 4 ******************
C
C INFUT/OUTFUT COMMON DATA AREA
    COMMON/LATSUF/NPS,NNPI (50), IFFEES,X(50),Y(50),L(50),IH(5),M(5)
&
                                    , HETHOD, IHELPP, IPREV, BOUND (2) ,SUESET, INTFNT , IE (2)
    COMMON/CURUEFIT/COEF (50,6), XCORD (200), YCORD (200)
    COMMON/IO/IN, IOUT
C DVERLAY EXECUTABLE PFOGRAM NAKES
    BATA MODL2,HOCL4,HELF/"MOD2", "MOD4","HELF"*/
    DIMENSION XO(50),YO(50)
    LOGICAL*1 HODL2(10), MODL4(10);HELF(10)
    INTEGER SUBSET
    CALL TXOFEEN
C READS THE COMMON DATA FILES
11 CALL FLCOM1
    GOTO (1,2,3,3,3,3,3,3), METHOD
1 NC=1
    GOTO 21
2 NC=6
    GOTO 21
    NC=4
    IN=5
    IOUT=6.
    CALL FDCOH2 (NFS,NPI,NC)
    CALL REMLNK (XO,YO)
C SET LINK LIST FOR THE INTERPOLATED POINTS
    CALL SETLNK (NPSSNFI, INTF'NT)
C CLEVE DESIGN DISFLAY
    CALL CLRDDES (NPS,NF'I,XO,YO,XCORD,YCORD,INTFNT,METHOD,CDEF,IC)
    60TO(4,5,6,6,6,6,6,6,6,9,11,8),1C
6 STOF
C NEXT DISFLAM
4 IPREU=O
    IHELFF=0
    INTFNT=O
    CALL. WRCOK1
    CALL SWRCOM(NFS,NFI,NC,XO,YO)
    CALL OURLAY (HODL4)
C. PFEVIOUS IISPLAY
5 IPREV=1
    IHEL_F:=0
    CALL WRCOM1
    CALL OURLAY (MOLL2)
C FFOGGKAM TERMINATION
8 CALL EXIT
    STOF
C HELFF DISFLAY
9 CALL WRCOM1
    CALL SWRCOM(NFS,NF'I,NC,XO,YO)
    CALL OURLAY (HELF')
    ENTS
C
C****************CURVE DESIGN DISFRAY******************て*********:%
```

C
C. LINK LIST COMMON AREA

COMKON/LNKLST/LINK (200), INTVAL (50), IFREE, IFCNT COMMON/LO/IN, IOUT
C KENU ITEMS
DATA HNTXT/"+ NEXT + FREUIOUS+ DLSF. ORG+ GRAFH + CUORDS.
a + ADD FNTH+ DEL INTV + FEFFESH + AX. MAKK + HELF + FESTAFT + EXIT */
BIMENSION N1 (1), XO(1),YO(1), XX(1),YY(1),C(50,6)
LOGICAL*1 MNTXT(120)
EXTEENAL XFLOT
CALL SUM (N,NI, MSUM)
CALL MINKAX (S1,S2,53,S4;XX,YY,HSUM)
IZERO=1.
11 IF (IZEKO.EQ.O) INTFNT=999
C SET UF THE DISFLAY
CALL TXCLER
ICORD=0
WRITE (IOUT,10)
10 FOFMAT ("CUKVE DESIGN:-")
C OUTFUT MENU
CALL MNOFEN (875.,715.,1)
CALL MNDISF (KNTXT,12,10,1)
CALI FRAME (870.,733.,12)
C DISFLAY INSTRUCTION FOR KEYBOARDD COMNAND
CALL DTEXT (830.,447.,"*TYFE CAFT. :",12)
CALL DTEXT (830.,428." "E-JOIN INTU.", 12)
CALL DTEXT (830.,406.,"F-FINISH ADD* 12)
2 CALL LHTARA
C CHECK FOR REFFESH COMMAND
IF (J.EQ.8) GOTO 34
CALL HNFICK (J,ICHAK, HNOS
IF (J.EQ.5.AND. ICOKD.EQ.2) GOTO 2
17 CALL CONFFM (ICHAR)
IF (ICHAK.EQ. 78 ) GOTO 12
IF (ICHAR.NE.89) GOTO 17
GOTO (41,41,33,34,35,36,36,11,110,41,66,41), J
$J=0$
GOTO 2
$41 \quad I C=J$
FEETURN
C DISFLAY ORIGIN
33 CALL DISORG (S1,52,53,54)
GOTO 2
C FLLOT THE GRAFH
34 CALL DRAW (XFLLOT;R,S1,S2,S3,S4,HSUM)
$J=0$
GOTO 2
C. AXES MAFKINB

110 CALL AXSMFK ( $51,52,53,54$ )
GOTO2
C CUFSOR INFUT COORDINATES
35 CALL BISCOK (ICORD,51,52,53,54)
G0T0 2
C ADD INTEFMEDIATE FOINTS INTERACTIUELLY USING THE CURSOR
C DETERMINE WHICH INTERVAL OF THE CURVE
36 CALL LHTSCL (S1,52,53,54)
22 CALL TXCURS (CX,CY,ICHAR)
IF (ICHAR.EQ. 70) GOTO 2
C GIUES THE INTERUAL NUMEER .
INTVND $=$ INO ( $C X, N$, XO) ${ }^{-}$
C. IGNDFE IF INTERVAL NUMBER IS ZERO

```
    IF (INTUNO.EQ.O) GOTO 22
    IF (J.EQ.7) GOT0 37
    IF (INTFNT.EQ.999.AND.IZERO.EQ.1)GOTO 66
    61 INTFNT=0
    C AUDS INTERHEDIATE FOINT TO THE LINK LIST AND UPDATE DATA FOINTS AEKRAY
    CALL ADDF'NT (N,NI;XO,YO,XX,YY,INTUNO,IA,CX,ICHAF,C)
    GOTO 22
66 N2=N-1
    00 16 I=1,N2
    INTVAL (I) =0
    Ni (I)=0
    IF (J.EQ.11) GOTO 41
    IZERO=0
    GOTO 61
C MAKK UELETEI INTERUAL
37 CALL DTEXT (CX,CY,"B";1)
    CALLL DELINT (INTUNO,NINI)
    GOTO 2
    RETURN
    END
C
C*********** ADD INTERTEDIATE FOINT ********************
C
    SUEROUTINE ADDFNT (N,NL,XO,YO,XX,YY,INTUNO,IA,CX,ICHAR,C)
C LINK LIST CONMON DATA AREA
    COMMON/LNKLST/LINK (200), INTUAL (50), IFREE, IFCNT
    IIMENSION N1 (1),XO(1),YO(1),XX(1),YY(1),C(50,6)
C CHECK FIRST TIME IN THE INTERVAL
    IF (INTUAL (INTUNO).NE.O) GOTO 2
C. ENTER THE START POINT AND THE INTERMEDIATE FOINT
    INTVAL (INTUNO) = IFFEE
    XX (IFREE) =XO (INTUNO)
    YY(IFFEE)=YO(INTUNO)
C CHECK END OF INTERUAL
    IF (ICHAR.ED.69) GOTO 7
    IF (IFCNT.GT.1) GOTO 11
    LINK (IFREE) =1FREEE1
    CALL TXYOVE (XX(IFREE) YY (IFREE))
    IFREE=LINK (IFREE)
5 LINK (IFREE)=0
C COMFUTE INTERFOLATED FOINT FFOM THE COEFFICIENTS
6 CALL. CXXYY (N,XO,YO,XX,YY,INTUNO,IA,CX,C, IFREE)
    N1 (INTUNO) =N1 (INTUNO)+1
    IFREE=IFK'EE+1
    RETUFN
C COMF'ARE THE CURRENT CX WITH THE ALEEADY IN THE TAELE
2 IF (ICHAR.EO.69) GOTO 1
    NEXT=INTUAL (INTVNO)
4 IF (CX.L.T.XX(NEXT)) GOTO 3
    K=NEXT
    NEXT=LINK (NEXT)
    IF (NEXT.EQ.O) GOTO 41
    GOTO 4
    LINK (K) = IFREE
    CALL TXMOUE (XX(K),YY(K))
    IF (IFCNT.GT.O) GOTO 12
    gOTO 5
C ADD FOINT IN THE INTERVAL WHICH HAS GREATER VALLE FOINT
3 IF(IFCNT.GT.0)GOTO 16
    LINK (K) =IFREE
    LINK (IFREE) =NEXT
    CALL TXMOVE (XX(K),YY(K))
```

GOTO 6
C ADOITION INTO FREVIOUSELY DELETED ITEM (CARBIGE COLLECTION)
$11 \quad$ IFCNT $=$ IFCNT-1
CALL TXHOVE (XX (IFREE) YY (IFREE))
K=LINK (LIAK (IFKEE) )
LINK (LINK (IFREE) ) $=0$
IFREE =LINK (IFREE)
CALL CXXYY(N,XO,YO,XX,YY,INTUNO,IA,CX,C,IFREE)
IFFEE=K
14 IFCNT=IFCNT-1
N1 (INTUNO) =N1 (INTUNO) +1
RETUKN
12 CALL CXXYY ( $N, X O, Y O, X X, Y Y, I N T U N O, I A, C X, C, I F R E E)$ *
Ki=IFFEE
IFREE=LINK (IFREE)
LINK $(K)=0$
GOTO 14
16 CALL TXMOUE (XX(K) , YY(K))
CALL CXXYY ( $N, X O, Y O, X X, Y Y$, INTUNO, IA,CX,C,IFREE)
K1=LINK (IFREE)
LINK (K) =IFREE
LINK (IFREE) $=$ NNEXT
IFREE $=K 1$
GOTO 14
C END OF INTERVAL WITH ONE OF HANY ENTERIES
C FIND THE LAST ENTRY IN THIS INTERUAL (LINK=O)
1 NEXTEINTVAL (INTVNO)
J=N1 (INTUNO) +1
DO 9 L=1,J
IF=NEXT
NEXT =LINK (NEXT)
IF (NEXT.EQ.O) G0TO10
9 CONTINUE
10 CALL TXHONE (XX(IF) YYY(IP))
8 CALL TXDAAW (XO (INTVAO+1), YO(INTVNO+1))
RETUFN
C MD INTERMEDIATE FOINTS
7 LINK (IFREE)=0
IFREE $=1$ FFEE +1
CALL TXMOUE (XO (INTVNO), YO(INTVND))
gOTO 8
END
C
C***********COMFUTE INTERFOLATED FOINT****************
c.

SUBROUTINE CXXYY (N,XO,YO,XX,YY, INTUNO, IAYCX,C, IFREE)
DIMENSION XO(1),YO(1); XX(1) FYY(1),C(50,6)
IF (IA.EQ.1) GOTO 3
$T=C X-X O$ (INTUNO)
$X X$ (IFREE) $=C X$
$I=I N T U N O$
IF (IA.EQ.2) GOTO 1
C SFLIINE METHOD
$Y Y(1 F R E E)=C(1,1)+T *(C(1,2)+T *(C(1,3)+T * C(I, 4)))$
GOTO 2
C NEWTON DIUIDED DIFFERENCE
$3 \quad N 2=N-1$
$A=C(N, 1)$
DO 7 L=1, N2
$J=N-L$
$7 \quad \mathrm{~A}=\mathrm{C}(\mathrm{J}, 1)+(\mathrm{CX}-\mathrm{XO}(\mathrm{J})$ ) $* A$
YY(IFREE)=A

GOTO 2
C FIECEWISE FOL YNOMLAL INTEFFOLATION (HAUD METHOD)
$1 \quad \mathrm{~T}=\mathrm{T} /(\mathrm{XO}$ (INTUNO +1 )-XO(INTUNO))
$Y Y(I F F E E)=C(I, 1)+T *(C(I, 2)+T *(C(I, 3)+T *(C(I ; 4)+T *(C(I, 5)+T * C(I, 6)))))$
2 CALL TXDKAW (XX (IFREE) YYY(IFREE))
RETUKN
END
C
C********** DELETE UNWANTED INTEFVAL $* * * * * * * * * * * * * * * * *$
SUBROUTLNE DELINT (INTUNOIN,NI)
COHMON/LAKLST/LINK (200), INTVAL (50), IFFEEE, IFCNT
DIHENSION NL (1)
C EMFTY LIST?
IF (INTVAL (INTVNO). EQ.O) FETUFN
3 IF (IFCNT.NE.O)GOTO 1
C FIRST HELETION
NEXT=INTUAL (INTUNO)
K=NEXT
IF (LINK (NEXT) .EQ. O)GOTO 5
N2=N1 (INTUNO)
K=IZFLLNK (N2,LINK,NEXT)
$5 \quad L I N K(K)=$ IFREE
IFFEEE INTVAL (INTVNO)
$2 \quad$ IFCNT $=I F C N T+N 1$ (INTUNO) +1
INTUAL (INTUNO) $=0$
NI (INTVNO) $=0$
FETUKN
C DELETE OF MORE INTREVAL
1 NEXT $1=1$ INTUAL (INTUNO)
$K 1=N E X T 1$
IF (LINK (NEXT1).EQ.O) goto 6
N2=N1 (INTVNO)
K1=IZFLNK (N2.LINK,K゙1)
6 NEXT2=IFREE
K2=NEXT2
$N 2=$ IFCNT -1
IF (N2.EQ.0) GOTOT
$K 2=$ IZRLNK (N2,LINK-K2)
$7 \quad K 3=\operatorname{LINK}(K 2)$
LINK (K2) =NEXT 1
LINK (K1) $=$ KK3
GOTO 2
END
C

C
FUNCTION INO (CX,N,XO)
DIMENSION XO(1)
DO $1 I=1$ iN
IF (CX.LT.XO(I)) GOTO 2
1 CONTINUE
$I=1$
2 INO:I-1
RETURN
END

FUNCTION IZRLNK (N,LK,NXT)
DIMENSION LK(1)
DO $11=1, N$
1
NXT=LK (NXT)
IZFLLNK=NXT
RETUKN

END
c
C ************SET UF THE LINK LIST*****************
c
SUBKOUTINE SETLNK (N,N1,INTFNT)
COMMON/LNKLST/LINK (200) , INTUAL (50), IFREE, IFCNT
DIMENSION N1(1)
C INTERMEDIATE FOINTS SFECLIFIED EY CURSOR?
IF (INTFNT.EQ.999) GOTO 9
INTVAL (1) $=1$
$\mathrm{H} 2=\mathrm{N}-1$
C SET FOINTER TO THE START OF EACH INTERUAL DO $11=2, N$
1 INTVAL (1) $=$ INTVAL $(I-1)+N 1(I-1)+1$
$K=1$
C SET LINKS
DO $21=1, N 2$ IF (N1 (1).NE.0) GOTO 4
LINK (K) $=0$
$K=K+1$
GOTO 2
$4 \quad$ NII $=\mathrm{N} 1(\mathrm{I})+\mathrm{K}-1$
DO $3 \mathrm{~J}=\mathrm{K}$, N11
$3 \quad$ LINK (J) $=\mathrm{J}+1$
LINK (J) $=0$
$K=J+1$
2 CONTIMLE
CALL SUM ( $\mathrm{N}, \mathrm{N} 1$,HSLMA)
C SET FREE FOINTER
IFREE=KSUM +1
GOTO 10
C NO INTEFMEDIATE FOINT IS SPECIFIED
9 IFREEE1
IFCNT=0
10 RETUFN
END
C
C ********* FIND TOTAL NLMEEE OF INTERFOLATED FOINTS*X**********
c
SUBFOUTINE SUM(N,N1,HSUM)
DIMENSION NI (1)
MSUM $=0$
N2 $=\mathrm{N}-1$
IO $1 \quad 1=1, \mathrm{~N} 2$
1 HSUMTMSUMT+N1 (I)
MSUMㅍMSUMY
heturn
END
C
C ***********SAUE CLRVE ON OUTFUT FILE*************
C
C. *****A SIKPLE LIST******

SUBFOUTINE SWRCOM (N.NI,NC; XO,YO)
C OUTFUT COMMON DATA AREA
COMMON/CURVEFIT/COEF $(50,6)$, XCOFiD ( 200 ) , YCOKD (200)
COMMON/LNKLST/LINK (200), INTVAL (50)
DIMENSION N1 (1), XO (1), YO (1)
FELIND 8
C OFEN OUTFUT FILE
CALL SETFIL (8,"OUTFIT")
$\mathrm{N} 2=\mathrm{N}-1$
WFITE (8,20) ( (COEF (I,J), J=1,NC) ,I=1,N2)

DO $1 I=1$, N2
NEXT=INTVAL (I)
N3=N1 (I) +1
LO $2 \mathrm{~J}=1 \mathrm{~N} 3$
WFITE (8, 10) XCORD (NEXT) , YCOFD (NEXT)
NEXTILLINK (NEXT)
2 CONTINUE
1 CONTIMUE
WRITE (B,10)XO(N), YO(N)
FOFHAT (2F12.4)
FOFMAT (F12.4)
ENDFILE 8
RETUKN
END
C
C*************FLOT THE DESIGNED CURUE***************
C
SUBROUTINE XFLLOT (R,SCL1,SCL2,SCL3,SCL4;NSUM)
C I/O COMMON DATA AREAS
COMHON/DATSUF/NFS, NFI (50), IFFEES,X(50) , Y(50) , L (50) , IH (5) , M(5)
8 , KETHOD, IHELP, IFREV, BOLND (2) , SUBSET (2) , INTFNT , IE (2)
COHMON/CURVEF IT/CDEF $(50,6)$, XCORD $(200)$, YCORD (20)
COMMON/LNKLST/LINK (200), INTUAL (50), IFREE, IFCNT
INTEGER SUBSET
DIMENSION XO(50), YO (50)
CALL FEEMLNK (XO,YO)
$N 2=N P S-1$
C OUTFUT SEGKENTS OF THE CLRVE FOF EACH INTERUAL
$5 \quad 001$ I $=1, N 2$
NEXT=INTVAL (I)
IF (NEXT.NE.OSGOTO 4
KㅍI
GOTO 11
4 CALL FLUSGN(SCL1,SCL 2,SCL3,SCL4, XCORD (NEXT), YCORO (NEXT))
CALL TXHOVE (XCORD (NEXT) , YCORD (NEXT))
M11=NPI (I)
IF (N1L.NE.O)GOTO 3
$K=I N T V A L(I+1)$
IF (K.NE.O) GOTO 6
IF (NEXT.NE.O) GOTO7
$K=I+I$
GOTO 11
CALL TXDFAW (XCOFD (K) Y YCOKD (K) )
GOTO 1
H0 $2 \mathrm{~J}=1$, Mi1
NEXT=LINK (NEXT)
CALL TXDRAW (XCORD (NEXT) , YCORD (NEXT))
CONTIMUE
$K=I+1$
CALL TXDRAW (XO (K) Y YO (K) )
CALL FLLUSGN (SCLI;SCL2,SCL3,SCL4; XO (K), YO (K))
CALL TXHOVE (XO(K) , YO(K))
1 CONTINUE
CALL FLUSGN(SCL 1,SCL2.SCL 3,SCL4,XO(I),YO(I))
8 RETURN
END

C *****************

* AFFENDIX 2.25 *
*****************

C
C THIS MOULLE HANDLES THE FOLLOWING INTERACTIVE DISFLAYS:-

1. TABLE OF THE INTEFFOLATED FOIMTS 2.TABLE OF THE FOL YNOMIAL COEFFICIENTS 3.EFROR FEFERRENCE 4.CURVE SUFERIMFOSE

C
C
C

C
C
C I/O CUMMON DATA AREA
COMMON/DATSUP/NFS, NF'I (50), IFREES, X (50), Y(50),L(50), IH(5), M(5)
$\&$

COMMON/CLFVEFIT/COEF $(50,6), X C O R D(200)$, YCOFD $(200)$
COMMON/IO/IN.IOUT
C OVERILAY EXECUTABLE FROGRAM NAMES
DATA HODL2, MODL 4 , KODL 1 "HELF/"MOD2" " KOD4" "EXFLICIT", "HELF" /
LOGICAL* 1 HODL2 (10), MODL $4(10)$, MODLI (10) , HELF (10)
INTEGER SUESET
CALL TXOFEN
C READ 1/O FILES
11 CALL EDCOKL
GOTO ( $1,2,3,3,3,3,3,3$ ) , KETHOD
$1 \quad N C=1$
GOTO 21
$M=6$,
goto 21
$3 \quad \mathrm{NC}=4$
$21 \quad \mathrm{IN}=5$
IOUT $=6$
CALL RDCOM2 (APS,NFI,NC)
IF (IHELF.NE.O) GOTO 66
GOTO ( $33,31,34$ ), IFREV
C DISFLAY TABLE OF INTERFOLATED FOINTS
33 CALL TABINT (NFSNNPI,XCOFD,YCORD,IOUT,IC)
$6 \quad$ GOTO $(51,52,59,54,59,59,57,33,58)$, IC
C FETUFN TO CURUE FIT DISFLAY
51 IF'REV $=0$
IHELF: $=0$
CALL WRCOM1
CALL OURN_AY (MODL 4)
C RETUKN TO THE FAFAMETEF ENTFH DISFLAY
52 IF'REV=1
IHELF=0
CALL WKCOM1
CALL OVFLAY (MODLZ 2 )
C OUTFUT COEFFICIENTS
54 CALL TABCOF (NFS,CDEF,METHOD, IOUT, IC)
GOTO (51,33,59,59,59,57,54,58), IC
C EFKOR REFERENCE DISFLAY
31 CALL ERFFEF (NF'S,NF'I,XCOKD, YCOKD,X,Y,COEF, IC) GOTO ( $51,52,59,59,59,59,59,57,59,56)$, IC
C. SUFERIMFOSED CUFVES DISFLAY

34 CALL SUFIMF (NFSSNFI, XCORD, YCORD,IC)
GOTO ( $51,52,59,59,59,59,61,59,57,59,58)$, IC
C HELF DISFLAY

```
57 CALL WRCOM1
    CALL OUFLLAY(HELF)
    C ALGORITHM DISFLAY
    61 IFKEV=0
        IHELF=O
        CALL WRCOMI
        CALL OUFLAY (MODLI)
    C EXIT
    58 CALL EXIT
    59 STOF
    66 GOTO (33,34,31),IHELF
    END
C
C. ***********TAELLATION OF INTERFOLATED FOINTS*******************
C
        SUBROUTINE TABINT(N,N1,XX,YY,IDEV,IC)
        DIKENSION N1(1),XX(1),YY(1),IP(4)
11 CALL OUTTIL(1,9,IDEV)
C FIND THE TAELE SIZE
    CALL SUM(N,NI,MSUM)
    IF (MSUM.GT.50) GOTO 1
C taEle size one or less than a fage
    IFOLL=O
    CALL OUTPGE (HSUH,1,XX,YY,IDEV)
    gOTO }1
C table size mofe than ONE fage
1 IF (1)=1
    IROLL=1
    m 2 I=2,4
2 IF(I)=1F(I-1)+50
    1S=1
C FIND NGMbEN OF PAGES & THE REMAINDEF
    MFEM=IREM(HSUK,50)
    NPAGE= (MSUM-KREM)/50
14 IFIFTY=50
15 IFNTR=IF(IS)
    CALL OUTPGE(IFIFTY,IFNTR,XX,YY,IDEV)
    WRITE (IDEV,20)
20 FORHAT(/"*'TO DISFLAY THE NEXT/FREUIOUS FAGE OF THE TABLE"/
& "USE THE FORWAROD/BACKWARD AS AFFROFRIATE'")
C SET UF CURSOR FDR USER SELECTION
12 CALL MNFIICK (J,ICHAR,HNO)
17 CALL CONFRM (ICHAR)
    IF (ICHAF.EQ.78) GOTO 12
    IF (ICHAF.NE.09) GOTO 17
    GOTO(21,21,23,21,25,26,21,11,21),J
C BACK TO THE MAIN fROGRAM TO FROCESS OTHER COHMAND
21 IC=\
    RETURN
C HARDCOPY
23 REWIND 7
    CALL SETFIL(7,*/DEV/TTYM*)
    WFITE(7,30)
30 FORMAT("COMFLETE TABLE OF THE INTERFOLATED FOINTS:-")
    IFIFTY=MSUM
    IFNTR=IF'(1)
    CALLL OUTFGE(IFIFTY,IFNTR,XX,YY,7)
    GOTO 12
c TO FOLL THE TABLE(FORWARD)
25 IF (IFOLL.EQ.0)GOTO 12
    IF (IS.EQ.NPAGE.AND.MEEK.GT.0)GOTO 31
    IF (IS.EQ.NFAGE.OR.IS.GT.NF'AGE)GOTO 12
```

IS $=15+1$
CALL OUTTIL (1,9,IDEV)
gOTO 14
C OUTFUT THE FEMAINDEF
31 IFIFTY=KREK
$I S=15+1$
CALL OUTTIL (1,9,ILEV)
GOTO 15
C BACKWAFD
26 IF (IROLL EQ.O) GOTO 12
IF (IS.EQ.1) GOTO 12
IS $=1 S-1$
CALI OUTTIL (1,9,IDEV)
GOTO 14
END
C
C $* * * * * * * * * * * * * * *$ TABULATE COEFFICIENTS $* * * * * * * * * * * * * * * * * * * * * * * * *$
C
SUBROUTINE TABCOF (N,C,HETHOU,IDEV,IC)
DIMENSION C (50,6) , IF (4)
C OUTFUT FAGE HEADER
11 CALL OUTTIL (2,8, IUEV)
NC=N-1.
IF (NC.GT.20) GOTO 1
C LESS THAN 20 ,ONE FAGE OF TABLE
$I K O L L=0$
CALL QUTCOF (NCII,HETHOD,C,IDEV)
GOTO 2
C GREATER THAN 20 h HOFE THAN ONE PABE OF TABLE
1 IROLLL=1
$\operatorname{IF}(1)=1$
DO $71=2,4$
$7 \quad \operatorname{IF}(\mathrm{I})=\mathrm{IP}(\mathrm{I}-1)+20$
IS=1
C FIND NUEEF OF F'AGES AND THE REKINDAR
NFEK=IREK (NC, 20)
NCPGE $=(\mathrm{MC}-\mathrm{NREM}) / 20$
$\begin{array}{ll}14 & \text { N3 }=20 \\ 15 & \text { IFNTK=IP(IS) }\end{array}$
12 CALL OUTCOF (N3,IFNTF,HETHOD,C,IDEU)
WRITE (IDEV, 20)
20 FORHAT (/"*'TO BISFLAY THE NEXT/FREUIOUS FAGE OF THE TABLE"/
\& UUSE THE FOKWARD/BACKWARD AS APFFOFRIATE" ")
C USE CURSOR TO FICK UF MENU OFTIONS
2 CALL MNFICK (J, ICHAR, HNIO)
17 CALL CONGRM (ICHAR)
IF (ICHAF.EQ.78) GOTO 2
IF (ICHAR.NE.89) GOTO 17
GOTO (21,21,23,24,25,21,11,21),J
C OTHEK COMMAND
21 IC=J
FETUKN
C HARWCOFY
23 FEWLND 7
CALL SETFIL (7,"/DEV/TTYM")
WRITE (7,30)
30 FORHAT ("FOLNOMIAL COEFFICIENTS:-")
$N 3=N-1$
IFNTK:IFI (1)
CALL. OUTCOF (N3, IFNTF, METHOD,C,7)
goto 2
C FOFWAFD COMMAND (TABLE FAGE ROLLING)

```
24 IF(IFOLL.EQ.0)GOTO 2
    IF(IS.EQ.NCFGE.AND.NREM.GT.O) GOTO 31
    IF(IS.EQ.NCFGE.OR.IS.GT.NCFGE) GOTO 2
    IS=15+1
    CALL OUTTIL (2,8,IDEV)
    g0T014
    N3=NREM
    IS=15+1
    CALL OUTTIL (2,8,IDEV)
    goto 15
C BACKWARD COMMANJ
25 IF(IROLL.EQ.0) GOTO 2
    IF(IS.EQ.1) GOTO 2
    IS=15-1
    CALL OUTTIL (2,8,IDEW)
    GOTO }1
    END
C
C************SUPERIMPOSED CURVE DISFLAY**************************
C
        SUBROUTINE SUFIMF(N,NI,XX,YY,IC)
        COMMON/CUKVES/NCRV (10),XYSCL (4)
        COMMON/IO/IN,IOUT
C NENUS ITEMS
    DATA HNTXT/"+ NEXT + FREUIOUS+ GRAFH + UISF.ORG+ DELETE*
&+ FEFRESH + METHOD + AX. MARK' HELF + RESTART + EXIT */
        DATA SUFFLS/"CLFVE1 CURVE2 CUFVE3 CLFVE4 CURVES
SCUFVEG CLFVE7 CUFVES CURVE9 CUFVEIO "/
    DIMENSION N1(1), XX(1),YY(1)
    LOGICAL*1 MNTXT(110),SUPFLS(100)
    CALL RDCRUS
11 CALL TXCLER
    CALLL SUM(N,N1,MSUM)
C SET UF FLOTTING SCALE
    Si=XYSCL(1)
    S2=XYSCL (2)
    S3=XYSCL (3)
    54=XYSCL(4)
C PREFAFE THE DISFLAY
    WRITE (IOUT,10)
10 FORKAT ("SUFERIKFOSED CLHVES:-")
    CALL HNOFEN(875.,715.,1)
    CALL MNDISF(MNTXT,11,10,1)
    CALLL FRAME (870.,733.,11)
    CALL ALFHMD
    WRITE (IONT,20)
20 FORMAT (/////////////62X,"* TYFE IN"/62X,"CURVE NO.")
2 CALL lmTARA
c CHECK FOK REFRESH
    IF (J.EQ.6) BOTO 23
3 CALL HNFICK(J,ICHAF, HNO)
    NFDEL=ICHAF-48
    IF (J.EQ.S.AND.NFDEL.GT.10.OR.J.EQ.5.AND.NFDEL.LT.1) GOTO 3
17 CALL CONFFH (ICHAF)
    IF (ICHAF.EQ.78) GOTO 12
    IF (ICHAR.NE.89) GOTO 17
    G0T0(21,21,23,24,25,11,21,27,21,11,21),J
    J=0
    goto 2
    IC=J
    FETUFN
C GRAFH/REFRESH OPTION
```

$K=0$
CALL LMTSCL (S1,S2,S3,54)
CALL PFRAME $(51,52,53,54)$
DO $11=1,10$
FEWIND 9
IF (NCRU (1).NE.99) GOTO 22
CALL SETFIL (9,SUFFLS (I+K))
77 CALL SFEEDFW (N,N1,I,XX,YY,HSUM,S1,S2,S3,S4)
$22 \quad K=K+9$
1 CONTINUE
ENDFILE 9
$J=0$
GOTO 2
C. DISFLAY CURVE ORIGIN

24 CALL DISORG(S1,S2,S3,S4)
GOTO 2
c delete curve option
$25 \quad$ MCRU (NFDEL) $=0$
CALL WRCRUS
GOTO 2
C AXES MARKING
27 CALL AXSHFK $(51,52,53,54)$
goto 2
END
C
C**********ERFOR REFEFNENCE DISFLAY*******************
C
SUEROUTINE ERNFEF ( $N, N 1, X X, Y Y, X 1, Y 1, C, I C$ )
COHMON/IO/IN, IOUT
C hemu itehs
BATA MNTXT/"+ NEXT + FREVIOUS+ GRAFH + COORUS. + DISF.ORG
B+ ZOOM + AX. HARK+ HELF + FESTART + EXIT */
DATA MOKLI/"EXFLICIT"/
LOGICAL.*1 HNTXT (100), HODLL1(10)
DIMENSION $N 1$ (1), XX(1),YY(1), X1 (1),Y1(1), $\mathrm{C}(50,6), \mathrm{XO}(50), Y 0(50)$
EXTEFNAL EFLOT
CALL REFLNK (XO,YO)
C FIND THE DIFFERENCE OF THE ORDINATES W.F.T. NEWTON DIUIDED DIFF. METHOD
CALL NEWTRF ( $\mathrm{N}, \mathrm{NI}, \mathrm{XO}, \mathrm{YO}, \mathrm{XX}, \mathrm{YY}, \mathrm{C}$ )
CALL SUA (N,N1,HSLKM)
C SET LP THE EFFOR REFEFFENCE DISFLAY
CALL MINMAX ( Si ', $52, \mathrm{S3}, \mathrm{S4}, \mathrm{XX}, \mathrm{YY}, \mathrm{MSUM}$ )
1 CALL TXCLER
ICORD=0
WIITE(IOUT,10)
10 FORMAT ("ERFROR FEEFRENCE:-")
CALL MNOFEN(B75.,715.,1)
CALL MNDISP (KNTXT, 10;10,1)
CALL FRAME $(970 ., 733.10)$
2 CALL LMTARA
CALL TEPPICK (J, ICHAK, KNO)
IF (J.EQ.4.AND.ICORD.EQ.2) GOTO 2
17 CALL CONFFK (ICHAR)
IF (ICHAR.EQ.78) GOTO 2
IF (ICHAF. NE. 89) GOTO 17
GOTO (31,31,33,34,35,36,37,31,1,31), J
31 IC=J
44 RETURN
C PLot the enfor reference curve
$33 \quad N C=0$
CALL BRAN (EPLOT,NC,S1,S2,53,54,HSUM)
$N C=0$

GOTO 2
C INFIUT CUFSOR COOKIDINATES
34 CALL DISCOR (ICOFD,S1,S2,S3,S4) GOTO 2
C DISFLAY AXES ORIGIN
35 CALL DISORG(S1,S2,S3,S4)
GOTO2
C CUFVE ZOOMING
36 CALL EZOOM (XX,YY,C,S1,S2,S3,S4,IC)
GOTO $(44,1,45,99,99,99,99)$, IC
45 IFFEV=0
CALL OUFLAY (MOULI)
99 IF (IC.EQ.5) IC=7
IF (IC.EQ.4.OR.IC.EQ.6)STOF
IF (IC.EQ.7) IC=9
GOTO 44
C AXES HAFKKING
37 CALL AXSHKK (51,52,S3,S4) GOTO 2 END
C

C
FUNCTION EFLOT (NC,SCL1,SCL2,SCL3,SCL4,NSLM)
C $1 / 0$ COMMON DATA AREA
COMMON/LATSUF/NFS,NFI (50) , IFFEES, X(50), Y(50) , L (50) , IH (5) , M(5)
4
, METHOD, IHELF, IFREV, BOUND (2), SUESET , INTF'NT, IE (2)
COMMON/EURVEF IT/COEF (50,6), XCORD (200), YCORD (200)
DATA IDC/"123456789"/
LOGICAL*1 IDC(9)
IF: 1
$I F=1$
$\mathrm{I}=1$
C FLOT SUFFLIED POINTS
3 CALL FLUSGN(SCL1,SCL2,SCL3,SCL4;XCORD(I), YCORN(I))
2 CALL TXMOUE (XCORD(I),YCORD (I))
IF (I.EQ.NSUM) FETUKN
IPI=IF+1
$I F 2=I F+N P I(I F)+1$
[00 $1 \mathrm{~J}=1 \mathrm{IF}^{\prime} 1$, IF? 2
1 CALL TXIFAW (XCORD (J), YCORD (J)) IF (IF.NE.1.OF.NC.EQ.O) GOTO 4
C CLRVE NUMEERING FOR SUFERIMFOSED CURVES IISFILAY CALL DTEXT (XCORD $(J-3)$ Y YCORD $(J-3)$, IDC (NC) , 1)
4 IF:IF2
$1 F=I F+1$
$\mathrm{I}=\mathrm{I}+\mathrm{NF} \mathrm{I}(\mathrm{IF}-1\rangle+1$
gOTO 3
END
C.

C.

SUBROUTINE EZOOM (XX,YY,C,SCL1,SCL2,SCL3,SCL4,IC)
C INFUT CGMMON DATA AREA

4
, HETHOD, IHELF, IFFEU,BOUND (2), SUBSET, INTFNT, IE (2)
COMKON/IO/IN, IOUT
DATA HNTXT/" + NEXT + FFEVIOUS + METHODS + AX. HARK + HELF
$8+$ RESTART + EXIT "
DIMENSION XX(1),YY(1),C(50,6),XO(50),YO(50), CX(2)
LDGICAL*I HNTXT (70)
CAILL REKLNK (XOPYO)

```
C SET WINUOW
    CALL LMTSCL(SCL1;SCL2,SCL3,SCL4)
    DYz(SCL4-SCL2)/20
C SELECT WITH CLHSOR FORTION OF CLKUE TO BE ZOOMED
    M1:I=1,2
        CALL TXCURS (CXX,CYY,ICHAR)
        CX(I) =CXX
    118 CDY1=CYY+DY
        CDY2=CYY-DY
        IF(CDY1.GT.SCL4.OF.CDY2.LT.SCL2) GOTO 117
        CALL TXHOVE (CXX,CDY1)
        CALL TXDFAW (CXX,CDY2)
        GOTO 1
    117 UY=DY/2.
            GOTO 118
    1 CONTINUE
C SORT SMALLER CXX
    IF (CX(1).LT.CXX) GOT0 2
    CX(2) =CX(1)
    CX(1) =CXX
    C UETERMINE WHICH INTERVAL
    2 IF1=0
    I=1
3 IF(CX(1).LE.XX(I)) GOTO 4
    IFI=IF1+1
    I=I+NFI (IFI) +1
    GOTO 3
4 K1=I-NFI(IF1)-1
    IF2=0
    I=1
5 IF(CX(2).LE.XX(I)) GOTO 6
    IF2=IFO+1
    I=I+NFI(IF2)+1
    gOTO 5
6 K2=1
    L2=K1+NFFI(IF1)+1
    107 I=Ki,L2
    IF (CX(1).LE.XX(I)) GOTO 8
7 CONTINUE
8 K3=1-1
    L.2=NPI (IF'2)+1
    L0 9 I#1,L?
        L1=K2-I+1
        IF(CX(2).GT.XX(L.1)) GOTO i1
    9 CONTINUE
    11 K4=L1+1
C SET UF THE ZOOMED DISFLAY
    CALL TXCLER
    CALL ALFFHKD
    WKITE(IOUT,10)
10 FORMAT ("ZOOMING:-")
    CALL LAMTAFA
    CALL MNOFEN(875.,715.,1)
    CALL MNOISP (MNTXT,7,10,1)
    CALL FEAME (870.,733.,7)
    S1=XX(К3)
    53=XX(K4)
    S2=YY(K3)
    54=52
    10 50 I=k3,K4
    IF (YY(I).GT.S4) S4mYY'(I)
    IF(YY(I).LT.S2) S2=YY(I)
```

```
50 CONTINUE
    CALL LMTSCL (51,52,53,54)
    CALL PFFAMME (51,52,53,54)
C DRAW THE ZOOMED CURVE
    LI=Ki+NFI (IF1)+1
    L2=k2-NFI(IF2)-1
    IF (L2.LT.L1) G0rO }7
    I=L1
66 CALL FLUSGN(S1,S2,S3,S4,XX(I) FYY(I))
    IF1=IF1+1
    IF(I.EQ.L2) GOTO }7
    I=I+NFI(IF1)+1
    GOTO 66
    77 CALL TXMONE (XX(K3),YY (K3))
        L1=K3+1
        10 88 I=LLっK4
    121 CALL TXDRAN(XX(I),YY(I))
88 CONTINUE
202 CALL LMTARA
    CALL MNFICK(J,ICHAR;INNO)
17 CALL CONFFM(ICHAR)
    IF (ICHAR.EQ.78) g0TO 202
    IF (ICHAK.NE.89) GOTO 17
    GOTO(414,414,414,404,414,2,414),J
C RETURING TO CALLING PROGRAM
414 IC=J
    FETURN
C AXES MARKING
404 CALL AXSYNK(S1,S2,53;54)
    GOTO 202
    END
C
C ##**************** NEWTON DIVIDED DIFFERENCE (GLOBLE)*****************
C
    SUBROUTINE NEWTRF (N,N1,X1,Y1,XX,YY,C)
    DIKENSION NI (1), X1 (1),Y1 (1), XX(1),YY(1),C(50,6)
C COMPUTE THE FOLYNOKIAL COEFFICIENT
    N2=N-1
    DO 1 K=1,N2
            J=N-K
            C(J+1,1)=(Y1 (J+1)-Y1 (J))/(X1(J+1)-X1(J))
1 CONTINUE
55 C(1,1) =Y1 (1)
    N3=N-2
    MO 2 J=1%N3
        K=J+2
        昭 3 L=K,N
                    I=N-L+K
                    XXX=X1(I)-X1(I- (, +1))
                    C(I,1)=(C(I,1)-C(I-1,1))/XXX
    CONTINUE
2 CONTINUE
C EVALUTE INTEFFOLATION FUNCTION
66 IP=1
    M0 4 Im1,N2
        T1=X1(I+1)-X1(1)
        R1=T1/(N1(I)+1)
        IF'1=1F'+N1 (I) +1
        XX(IF)=X1(I)
        Z=X1(1)
        XX(IP1)=X1(I+1) ,
        YY(IF')=0
```

```
            YY(IF'1)=0
            N11=N1(1)
            10 5 K=1,N11
            XX(IF+K)=Z+R1
            Z=Z+R1
            A=C (N,1)
            HO }7\textrm{L=1,N2
                J=N-L
                A=C(J,1)+(Z-XI (J))*A
            CONTINUE
                    YY(IF+K)=A-YY(IF+K)
                    CONTINUE
                IF=IF1
                    CONTINLEE
                            RETUFN
                            END
C
C. ****************** OUTFUT COEFFICIENTS****************************
C
    SUEROUTINE OUTCOF (NCOEF,IFNTR,METHOD,C,IDEU)
    DIMENSION C(50,6)
    I=IFNTR
    CALL CUFFOS(1.,5BO.)
    IF (METHOD.EO.2) GOTO 1
C OUTFUT TAELE HEADER
    WRITE (ILEV,10)
10 FOKMAT(" I",7X,"C1",11X,"C2",11X,"C3*,11X,"C4"/)
C OUFUT SFLINE COEFFICIENTS SOFT/HARD COFY
3 DO 5 Jm1,NCOEF
                        WRITE(IDEV,40)I,C(I,1),C(I,2),C(I,3),C(I,4)
                        I=I+I
40 FORMAT (12,4(2X,E11.4))
5 CONTINLE
    GOTO }
C OUTFUT FIECEWISE FOLYNOMIAL COEFFICIENTS
1 WRITE (IDEV,20)
20 FORKAT(" I",8X,"C1",8X,"C2",8X,"C3",10X,"C4",10X,"C5",9X,"C6"/)
    DO 6 J=1,NCOEF
        WRITE(IDEV,50)I,C(I,1),C(I,2),C(I,3),C(I,4),C(I,5),C(I,6)
        I=I+1
            FOFHAT(I2,E11.4,4(X,E11.4),E11.4)
50 FOFHAT
7 RETUKN
    END
C
C*****************OUTPUT A FAGE OF THE TABLEE****************************
C
    SUBROUTINE OUTFGE (NF'OINT,IF'NT,XX,YY,IDEV)
    DIMENSION XX(1),YY(1)
    CALLL CUFFOS(1.,710.)
C OUPUT A FAGE OF TABLE OF THE INTEFFOLATED FOINTS
    WRITE(IDEV,10)
10 FOFMAT(//" I*,7X,"X(I)",BX,"Y(I)",7X,"I",5X,"X(I)",8X,"Y(I)*/)
    IF(NFOINT/2*2.LT.NFOINT) GOTO 4
    IFNT1=IFNT+NFOINT/2
    GOTO 2
4 IFNT L=IFNT+NFOINT/2+1
2. DO 3I=2,NFOINT,2
        WRITE (IUEV, 20) IFNT, XX (IFNT),YY (IFNT),IFNT1,XX (IFNT1),YY(IFNT1)
        IF'NT=IF'NT+L
        IFNT1=IFNT1+1
        IF(I+1.NE.NFOINT) GOTO 3
```

```
    WFITE (IDEN, 30) IFNT,XX (IFNT), YY(IFNT)
    CONTINUE
    FOFHAT(2(12,2X,2(E11.4,3X) })
    FORHAT(12,2X,2(E11.4,3X))
    RETUFN
    END
C
C******************* OUTPUT THE TITLE OF THE DISFLAY*********
C
*******AND THE COMMAND HENU******************
C
    SUBFOUTINE OUTTIL (IC.ITEK,IDEV)
C MENU ITEMS
    DATA KNTXT1/" + NEXT + FREVIOUS + HARDCOFYY + COEFFFNT + FORWARD
&+ BACKWARD+ HELF" + FESTART + EXIT */
    DATA HNTXT2/" + NEXT + FREUIOUS+ HAKDCOFY + FORWARD + BACKWARD
&+ HELF + RESTART + EXIT */
    LOGICAL*1 MNTXT1 (90), HNTXT2(80)
    CALL TXCLER
    IF (IC.EO.2) GOTO 2
C OUTFUT THE INTERFOLATED FOINTS
    WFITE (IDEU,10)
10 FORMAT ("COMFLETE TABLE OF THE INTEFFGLATED FGINTS:-*)
    gOTO 3
2 WRITE(IDEV,20)
20 FOFMAT (///"* FOLYNOMIAL COEFFICIENTS:-*////%
3 CALL MNOFEN(875.,715.,1)
    IF(IC.EQ.2) GOTO 22
    CALL HNDISF'(KNTXT1,ITEN,10,1)
    GOTO }
22 CALL MNDISP (MNTXT2,ITEM,10,1)
4 CALL FRAME (870.,733.,ITEK)
    RETURN *
    END
C
C ##**********INEUT COMMON DATA FOR SUFEFIRFROSED DISFLAY***********
C
    SUEROUTINE RDCRUS
    COMMON/CURUES/NCRV (10), XYSCL (4).
    REWIND 7
    CALL SETFIL(7,"SUFCFEVES")
    READ (7,10) (NCRU(I),I=1,10)
    READ (7,20) (XYSCL (I),I=1,4)
    10 FOKHAT (12)
20 FORMAT (F11.4)
    ENDFILE }
    FETURN
    END
C
C*********** DISFLAY THE SUPERIMFOSED CUFVES*************************
C
    SUEFROUTINE SFEBFW(N,N1,NC,XX,YY,MSUM,SCL1,SCL2,ECL_3,SCL4)
    DIMENSION NI (1), XX(1),YY(1)
    FEAD (9, 25) HSUK,N
    N2=N-1
    READ (9,30) (XX (I),YY(I),I=1,KSUM)
    FEAD (9,20) (N1 (I),I=1;N2)
30 FORKAT (FI1.4)
20 FOFMAT (I3)
25 FOKHAT(2I3)
    FC= EFLOT (NC,SCL1,SCL2,SCL3,SCL4,MSUM)
    RETURN
    END
```

```
C ********** FIND TOTAL. NLMEER OF INTERFOLATED FOINTS*X***********
    SUEROUTINE SUM(N,N1,MSUM)
    DIMENSION N1(1)
    MSUM=O
    N2=N-1
    DO 1 I=1,N2
1. HSUMT=MSUMM+NI (I)
        MSLMM=HSUM+N
        RETUFN
        END
C
C************WRITE COMROM ELOCK CURVES***************
C
    SUBROUTINE WRCRUS
    COMMON/CURUES/ACRU (10) ,XYSCL (4)
    REWIND B
    CALL SETFIL(8;"SUFCRUES")
    WRITE (B,10) (NCRU(I),I=1,10)
    WFIITE (8,20) (XYSCL (I),I=1,4)
    FORKAT (12)
    ENDFILE 8
    RETUKN
    END
```

```
C. ********************
C * AFFFENDIX 2.26 *
*****************
C THIS MOURE HANDLES THE JOIN DISFLAY AND ITS SUESEQUENT ZOOMING
C
C
C
C ********* KAIN FROGRAM - MOLLLE 6 ******************
C
    COMMON/JOIN/CJ1 (500),CJ2(500),J3(12),J4(100), IFNTR(6)
    COMMON/IO/IN,IOUT
    DATA MOLL4,MOLLI;HELF/"MOD4","EXFLICIT","HELF"/
    LOGICAL*1 HOOL4(10), HOCLL (10) ,HELF'(10)
    IN=5
    IOUT=6
    CALL TXOFEN
    CALLL FDCOMJ
    CALL JOIN(CJL,CJ2,J3;J4,IFNTR;IC)
    G0T0(2,3,1,1,1,1,7,1,8,1,1),IC
C PROGFAM TERMINATES
1. CALL EXIT
C NEXT DISFLAY
2 STOF
C FREVIOUS DISFLAY
3 CALL OURLAY (MONL4)
C ALGORITHM DISFLAY
7 IF'REV=0
    IHELF'=0
    CALL WRCOM1
    CALL OUFLLAY (MODI)
C HELf DISflay
B CALL WRCOMJ
    CALLL OURLAY (HELF)
    STOF
    END
C
C****************JOIN DISPLAY*******************************
C
    SUBFOUTINE JOIN(XJ,YJ,JJ3,JJ4,IFNTR,IC)
    COMMON/IO/IN, IOUT
C MENJ ITEMS
    DATA NNTXT/" + NEXT + FFEVIOUS+ GRAFH + COORDS. + UISF..ORG
&+ ZOOM + METHOD + AX. MAFK+ HELF + + RESTART + EXIT */
    DIMENSION XJ(1),YJ(1);JJ3(1);JJ4(1),IFNTR(1),MM1 (11)
    LOGICAL*I HNTXT(110)
    EXTEKNAL JFLLOT
C NUMBER DF CURVE SEGNENTS TO BE JOINED
    JM1 (1)=IFNTE(1)-2
    IT=0
    K=2*JM1 (1)+1
C COMFUTE TOTAL NLMBER OF FOINTS
    00 1. I=3,*゙っ2
        JM1 (I-1)=0
        K1=JJ3(I+1)
        K2=1/33(I+1)+JJ3(I)-2
        LO 12 J=K1,N゙2
        JM1 (I-1)=JM1 (I-1) +JJ\4 (J)
        CONTINUE
        JM1 (I-1) =\M1 (I-1) +_J3 (I)
        JM1(I) = JJ3 (I+1)
```

```
        IT=IT+JM1(I-1)
1 CONTINUE
    MSUM=IT-JM1 (1) +1
C SCALES FOR FLOTTING THE JOINED CUKVES
    CALLL MINMAX(S1,S2,S3,54,XJ,YJ,MSUM)
11 CALL TXCLER
    ICOKD=0
    WRITE(IOUT,10)
10 FOFMAT ("JOINED CUKVES:-")
C. OUTFUT MENU
    CALL HNOPEN(875.,715.,1)
    CALL MNDISF'(MNTTXT,11,10,1)
    CALL FRAME (870.,733.,11)
2 CALL LMTAFA
C CURSOR CHOICE
    CALL MNFIICK(JYICHAR,HNO)
    IF (J.EQ.4.AND.ICORD.EQ.2)GOTO 2
17 CALL CONFRM(ICHARN
    IF(ICHAR.EQ.78) GOTO 2
    IF (ICHAK.NE.89) GOTO 17
    GOTO(21,21,23,24,25,26,21,28,21,11,21),J
    IC=]
    RETURN
C FLOT THE CURVES
23 CALL BRAW (JFLOT,N,S1,S2,S3,S4,JM1)
    GOTO 2
C CUFSOK INFUT COORDINATES
24 CALL DISCOR(ICORD,S1,S2,S3,S4)
    GOTO 2
C DISFLAY ORIGIN
25 CALL DISORG(S1,S2,53,S4)
    gOTO 2
C. ZOOMING
26 CALL JZOOM(JM1,XJ,YJ,NJ4,IFNTK,S1,S2,S3,S4,IC)
    GOTO(27,11,27,29,27,26,29),IC
    G0T02
C AXES MARKING
28 CALL AXSMFK'(S1,S2,S3,S4)
    GOTO 2
    STOF
    IF (IC.EQ.3) J=7
    IF(IC.EQ.5) J=9
    GOTO 21
    END
C
C****************ZOOMING IN JOINED CYRUES*********************
C
    SUBROUTINE JZOOM(JM1,XJ,YJ,J4,IFNTK,SCL1,SCL2,SCL3,SCL4,IC)
    COMMON/IO/IN,IOUT
    MATA MNTXT/"+ NEXT + FREVIOUS+ METHOUS + AX. MARK+ HELF
&+ RESTAFT + EXIT */
    DIMENSION JM1 (1);XJ(1),YJ(1),J4(1),IFWTF(1),CX(2),LE(2),N11(2),M1 (2)
    LOGICAL*I HNTXT (70)
    CALL LMTSCL.(SCL1,SCL2,SCL3,SCL4)
    DY=(SCL4-SCL2)/20
    0~ 1 I=1,2
    CALL TXCURS(CXX,CYY,ICHAR)
    CX(I) =CXX
    CALL TXMOUE (CXX,CYY+DY)
    CALL TXIRAW(CXX,CYY-DY)
1 CONTINUE
C SORT FOR SMALLEER CXX
```

```
    IF(CX(1).LT.CXX) GOTO 2
    CX(2)=CX(1)
    CX(1) =CXX
C DETERMINE WHICH SUBSET
2 DO 11 J=1,2
    K=\M1 (1)
3 DO 4 I=1,K
    IF (I.EQ.K) GOTO S
    IF(CX(J).LE.XJ(IFNTR(I+2))) GOTO 5
4 CONTINUE
5 LB(J)=I
11 CONTINUE
    10 9 J=1:2
    Mi (J) =JM1 (2*LB(J))
    N1i (J) =JM1 (2*LB (J)+1)
9 CONTINUE
    I=IPNTK(L.B(1)+1)
    IF1=N11(1)-1
    IF(CX(1).GT.XJ(I)) GOTO 7
    K11=1
    K1=I-J4(IFI)-1
    GOTO 8
7 IFI=IFI+1
    I=I+J4(IF1)+1
    g0T0 71
8 I=IFNTK(LE (2)+1)
    IF2=N11(2)-1
81 IF(CX(2).GT. XJ(L)) 60T0 91
    K2=1
    G070 101
91 IF2*IF2+1
    I=I+J4(IF2)+1
    GOTO 81
101 L2=K1+J4(IF1)+1
    10 22 [mK1,L2
    IF(CX(1).LE.XJ(I)) GOTO 23
22 CONTINLE
23 K3=I-1
    L2=14 (IF2) +1
    10 24 Im1,L2
    L1=K2-1+1
    IF(CX(2).GT.XJ(LI)) GOTO 25
24 CONTINUE
25 K4mL1+1
12 CALL TXCLEF
    CALL ALFHHD
    WRITE (YOUT, 20)
20 FORMAT("ZOOKING:-*)
    CALL LMTARA
    CALL MNOFEN(875.,715.,1)
    CALL HNDISF(HNTXT,7,10,1)
    CALL FRAME (870.,733.,7)
    S1mXJ (K3)
    S3=XJ(K4)
    S2=YJ(K3)
    S4m52
    w0. 50 I=k3,K4
    IF(YJ(I).GT.S4) S4=YJ(I)
    IF'(YJ(I).LT.S2) S2=YJ(I)
50 CONTINUE
C DRAW THE ZOOMED CURVE
    CALL LMTSCL (51,52,53,54)
```

```
        CALL FFFAME (S1,52,53,54)
        IF(K11.EQ.K゙2) GOTO 45
        IF3=1
        IF'(LB(1).EQ.LB(2).AND. IF3.EQ.1) GOTO 31
        IF (LB(1).EQ.LB(2)) GOTO 32
        N3=34(IFI)+1
        L1=K1+N3
        L.2=IFNTF(LB(1)+2)
        I=L1
35 CALL FLLUSGN(S1,S2,53,S4,XJ(I),YJ(I))
        IF1= IF 1+1
        IF(I.EQ.L2) GOTO 66
        I=I+J4(IF1)+1
        GOTO 35
66 LB(1)=LB(1)+1
        N11(1) = MN1 (2*LB(1) +1)
        K1=L2
        GOTO }3
        N3=}=14(IF1)+
        Li=L2+N3
        N4=14(IF2) +1
        L2=K2-N4
40 I=LI
37 CALL FLUSGN(S1,S2,S3,S4,XJ(I),YJ(I))
        IF1=1F1+1
        IF (I.EQ.L2) GOTO 45
        I=I+J4(IFI)+1
        GOTO 37
31 N3=\\4(IF1)+1
        L1=K1+N3
        N4=J4(IF2)+1
        L2=k2-114
        GOTO 40
45 CALL TXHOVE (XJ(KZ),YJ(KZ3)
        L1=K3+1
        10 55 I=LL,N4
55 CALL TXDFAW(XJ(I),YJ(I))
    202 CALL LHYARA
        CALL MNFICK(J,ICHAR, MNO)
17 CALL CONFRM (ICHAR)
        IF (ICHAR.EQ.7B) GOTO 202
        IF(ICHAR.NE.89) GOTO 17
        GOTD(41,41,41,404,41,12,41),3
    41 IC=J
        RETUKN
    C AXES MAFKING
    404 CALL AXSMKK(S1,52,53,54)
        GOTO 202
        ENII
C
C**************** FLDT JOTAED CLRUES************************
C
    SUBROUTINE JFLOT(F,SCL1,SCL2,SCL3,SCL4,JM1)
    C JOIN COMMON DATA AFIEA
    COMMON/JOIN/CJ1 (500), CJ2(500), J3 (12), J4 (100), IFNTR (6)
        IIMENSION JM1(1)
    J=3
    H=0
    KriJM1 (1)
    DO 1 I=1,N゙
        M=M+JM1(J-1)-I+1
        MI=JM1 (J)
```

```
    IF=IFNTR(I+1)
    IF'1=IF
    Ki=IF
    IF1=N1
    C OUTFUT SUFFLIED FOINTS
    4 CALL FLUSGN(SCL1,SCL2,SCL3,SCL4,CJ1(K1),CJ2(K1))
    CALL TXMOVE(C.J1 (K1),CJ2(K1))
    IF (K1.EQ.M) GOTO 3
    Li1=1F'1+1
    L2\=1F'1+J4(IFI)+1
    C OUTFUT INTEFFOLATED FOINTS
        U0 2 LI=L11,L22
        CALL. TXURAW(CJI (L.1),CJ2(LI))
    2
    CONTINUE
    IF1=L_22
    IFI=IFI L 1
    K1=K1+J4(IF1-1)+1
    GOTO 4
    3 colmj+2
    FETURN
    END
```


## *****************

## * APFENDIX 2.31 *

*****************

C THIS MODLLE HANDLES THE FOLLOWING INTERACTIVE DISFLAYS:-

1. INTFODUCTOFY
2. CHOICE OF THE NUMERICAL ALGORITHM 3. DATA ENTRY 4. DATA TABULATION

C S.DATA FOINT EDITING

C
C
C. INFUT COMMON DATA AREA

COMMON/LATSUP/NFS,NFI (50), IFREES, X 50$), Y(50)$, $Z(50), L(50)$, IH (5), $\mathrm{K}(5)$, HETHOD, IHELF, IFREU,BOUND ( 6 ) , SUBSET, INTFNT, IE (2) ,ID.
COMPDN/IO/IN. IOUT
DATA FHODL2,FHELF-/"FYODL2" "HELF" /
LOGICAL*1 FMKODL2(10) FFHELF'(10)
INTEGER SUBSET
IN $=5$
IOUT=6
CALL TXOFEN
C READ INFUT DATA IF NOT FOR THE FIAST TIKE
IF (IERROF (103). NE.0) GOTO 1
CALL FRDCK1
IF (IHELF.NE.0)GOTO 55
IF (IFREV.EQ.1) GOTO 21
C CALL DISFLAYS SEQUENCE FOK DATA ENTFY AND EDITING
1 CALL INTFOD (IC)
GOTO (2,3000,1111) +IC
2 CALL KENU (HETHODIIC)
GOTO (10,1,3000,1111,1111), IC
10 CALL DATENT (IC,IA)
GOTO (20,2,3000,1111,11111), IC
20 CALL DATHAN(IA,IC)
GOTO ( $1000,10,40,1111,1111,3000,1111,1111)$,IC
40 CALL EBIT (IC,IA)
C CALL BACK THE DATA MANIFILATION DISFLAY
IF (IC.GT.I) GOTO 20
C NEXT DISPLAY IN SEQUENCE
1000 IF'FEV=0
IHELF: $=0$
CALL FWFCKI
CALL OURLAY (FHOBL2)
C HELF DISFLAY
3000 CAILL FWFCMM1
CALL OURLAY (FHELF)
C TEFMINATE FROGRAM
1111 CALL FEXIT
STOF
C LINK LIST UNCHANGED
21 IFfiEV=0
IHELF: $=0$
$1 A=111$
G070 20
C FETUNN FFOM HELF EISFLAY

```
55 GOTO(1,2,10,21.),IHELF
    END
C
C. *************INTRODUCTORY DISFLAY
C
    SUBKOUTINE INTROD(IC)
        COMMON /IO/ IN,IOUT
C MENU ITEMS
    DATA HNTXT/" + NEXT + HEL_F + EXIT */
    LOGICAL*1 KNTXT(30)
C SET UF THE INTFODUCTORY DISFLAY
    CALL TXCLER
    CALL CUFFOS(1.,780.)
    CALL TEXTUF("FFIINTEXT",34)
    CALL HNOFEN(875.,715.,1)
    CALL HNDISF(FNTXT,3,10,1)
    CALL FFAME (870.,733.,3)
2 CALL MNFICK (J,ICHAR,MNO)
22 CALLL CONFRN(ICHAR)
    IF (ICHAR.EQ.78) GOTO 2
    IF(ICHAR.NE.89) GOTO 22
    IC=J
    FETURN
    END
C
```



```
C
        SUBFOUTINE KENU(M,IC)
    C RETURNS ALGRITHM INDEX
        COMMON /IO/IN,IDUT
C MENU ITEMS
        DATA HNTXTL /" + NEXT + FREVIOUS+ HELF' + RESTART + EXIT */
        LOGICAL*EL MNTXTI(5O)
7 CALL TXCLER
C OUTFUT THE ALGORITHM LIST
    WFITE (IOUT, 10)
10 FOFKAT ("INDICATE YOUR CHOICE OF ALGOKITHM:-")
    CALLL WNOFEN(875.,715.,1)
    CALL DTEXT (20.,700.,"***FARAMETRIC F'ACKAGE FOR INTEFFOLATORY
& ILATA FITTING****,55)
    CALL DTEXT(70.,650.,"NUMERICAL ALGORITHMS:-",22)
    CALLL HNDISP (HNTXT1,5,10,1)
    CALL FFAKE (870.,733.,5)
    CALL MANOFEN (60.,600.12)
    CALL MNTEXT ("1-CUBIC SFLINE (FFARAMETKIC SECOND LEKU. END CUNDITIONO",G3)
    CALL. HNTEXT ("2-CUBIC SFLINE (CYCLIC END CONDITION)";36)
    CALL HNTEXT("3-CUBIC SFLINE (ANTICYCLIC END CONDITION)",41)
    CALL KNTEXT ("4-CUBIC SFLINE (VARIABLE END CONDITION)*,39)
C SET UF CURSOR FOR MEMU CHOICE
1 CALL HNFICK(I,ICHAF,HNO)
    IF (KNO.EQ.1)GOTO 3
    M=I
    gOTO }
3 CALL CONFRM (ICHAR)
    IF(ICHAR.EQ.78) GOTO 1
    IF (ICHAR.NE.89) GOTO 3
    IF(I.EQ.4)GOTO 7
    IC=I
    FETUFN
    END
C
```

```
C***X*********UATA ENTRYY DHSFVLAY ROUTINE************************
C
    SUBFOUTIHE DATENT (IC,IA)
C IJATA ENTEY DISFLAY
C INFUT COMYON DATA AREA
    COMMON/DATSUF/NFS,NFI (50), IFFEES,X(50),Y(50),Z(50),L(50), IH(5)
& IK(5
                ,K(5) , HETHOD, IHELF; IFREV, BOUND (6),SUBSET,INTFNT,IE (2)
    COHMON /IO/INPIOUT
C MENU ITEMS
    DATA MNTXTI/" + NEXT + FREVIOUS+ HELF* + FESTART + EXIT */
    DATA MNTXT2/"+ NEW + OLD + 2-DIMEN.+ 3-DIMEN.
b + KEYBOARD+DISC FILE*/
    LOGICAL*1 MNTXT1 (50), PNTXT2 (80)
    INTEGER SUBSET
C SET UF' DATA ENTKYY DISFLAAY
23 CALLL TXCLER
    WRITE(IOUT,IO)
10 FOKHAT ("DATA ENTFY:--")
C CUTFUT INSTRUCTION TO THE USER
    CALL CURF'OS(1,7700.)
    WFITE(IOUT,11)
11 FORMAT("SELECT THE AFFROFRIATE"/"DATA SFECIFICATION(*):-")
    WRITE(IOUT,1222)
1222 FORHAT (///2X,"1-STATE OF DATA:-"///2X," 2-DIMENSIONALITY:-*///
&
                                    2X,"3-DATA MEDIUM ENTFY:-")
    WFITE (IOUT,20)
20 FORMAT (/////////////////** IF 'OLD' IS SELECTED YOU MAY FROCEED*/
& * TO NEXT DISFLAY IMMEDLATELY .OTHEEWISE */
* " YOU KUST SELEET THE DESIEED MEDIUM")
C DISPLAY MENU,RAISE CLHESOR & WAIT FOR USER ACTION
    CALL MNOPEN(875.,715.,1)
    CALL MNDISP (MNTXT1,5,10,1)
    CALL FRAME (870.,733.15)
    CALL HNOFEN(320.,600.,2)
    CALL HNDISF(KNTXT2,8,10,2)
    CALL. FRAME (315., 620.,8)
    CALL TXMOVE (315.,570.)
    CALL TXLFAW(460.,570.)
    CALL TXMOVE(315.:500.)
    CALL TXIRAW(460.,500.)
    NFLAG=1
    MD =0
    IS =0
5 CALL MNPICK(J,ICHAR, HNO)
C FIRST OF SECOND MENU
    IF (HNO.EQ.1) GOTO 2
    IF(IS.EQ.2.BR.NFLAG.EQ.O.OR.J.EQ.3.OR.J.EQ.6) GOTO 5
    IF (J.LT.3) GOTO 7
    IF(J.LT.6) GOYO 8
    MD=J
    CALL CLFFPOS(1.,400.)
3 CALL MESSAG("# NUMMEEF OF DATA FOINTS(MAX.50)?"*)
    FEAD (IN,30)N
30 FORYAT (GO.0)
    IF(N.GT.5O.OR.N.LT.3) GOTO 3
    AFS=N
    IF (J.EQ.8)G0TO 1010
    WRITE(IOUT,40)
40 FORMAT (/,** X-COOKDS.2-*)
    IF (IEFFNOF(110).NE.0) BOTO 100
    FEAD (IN,5O) (X(I),I=1,N)
```

```
50 FOFHAT (50G0.0)
    WFITE (IOUT,70)
    FORMAT (/,":% Y-COORDS.:-")
    IF (IERFOR(110).NE.0)GOTO 110
65 READ(IN,50)(Y(I),I=1,N)
        IF (ID.NE.3) GOTO 333
        WFITE (IOUT, BO)
        FOKMAT (/,"* Z-COOFUS.:-")
        IF (IERFOR(110).NE.0) GOTO 120
    75 READ(IN,SO)(Z(I),I=1,N)
333 IHELF=3
        GOTO 5
8 IF(J.EQ.4) IJ=2
        IF (J.EQ.5) ID=3
        GOTO 5
100 WFITE(IOUT,105)
105 FORHAT ("ILLEGAL X-COOFDS.,TF'Y AGAIN")
        EMOFILEE 5
        GOTO 35
        WFITE(IOUT,115)
115 FORMAT ("ILLEGAL Y-COORDS.,TRY AGAIN")
        ENDFILE }
        GOTO 65
120 WFITE(IOUT,118)
118 FORMAT("ILLEGAL Z-COORDS.,TRYY AGAIN")
        ENHFILE 5
        GOTO 75
2 CALL CONFRM(ICHAR)
        IF(ICHAR.EQ.78) GOTO 5
        IF (ICHAR.NE.89)GOTO 2
        IF (J.EQ.4)GOTO 23
        IF (NFLAG.EQ.1.AND.J.EQ.1.AND.MD.EZO.O) GOTO 5
        IC=J
        IF(J.ED.1.AND.ID.EQ.O) GOTO 5
        NETURN
1010 IFLG=0
C NEW ILATA FOINTS
        IA=0
        CALL GETFLN(FILE)
        CALL READAT (FILE,X,Y,Z,NFS,IFLG,ID)
        IF(IFLG.EQ.1)GOTO 1010
        IF(IFLG.EQ.2)GOTO 3
        GOTO 5
313 ENDFILE 5
        GOTO 3
C NEW DATA FOINTS
7 IA=O
C OLD LATA FOINTS
    IF(J.EQ.2) IA=1111
    1S=J
    IF (J.EQ.2.AND.KD.GT.0) GOTO 5
    IF(J.EQ.2.AND.MD.EQ.O) GOTO }1
    IF (J.EQ.1) GOTO S
12 NFLAG=0
    GOTO 5
    END
C
C **************UATA FOINTS TABLLATION DISFLAY******************
C
    SUBFOUTINE DATMAN(IA,IC)
C INFUT COMMON DATA AREA
    COMMON/DATSUF/NFS'NFI (50),IFFEES,X(50),Y(50),Z(50),L(50),IH(5)
```

COMMON/IO/IN,IOUT
C MENU ITEMS
DATA MNTXT/" + NEXT + FREVIOUS + EDIT + SORT-X + SAVE
$a+$ HELF + RESTART + EXIT */
DIHENSION XO (50), YO (50), ZO (50)
LOGICAL*I MNTXT (80)
INTEGER SUBSET,S
C NEW/OLD?
22 IF (IA.EQ.111)GOTO7
111 N=NFS-1
C SET LIAK LIST
UO $1 \mathrm{I}=1, \mathrm{~N}$
$1 \quad L(1)=I+1$
$L($ NFPS $)=0$
IFREES=NF'S+1
10 $2 \mathrm{I}=1,5$
$2 \quad M(1)=10 * I$
$\mathrm{S}=0$
10 $31=1,5$ IH (I) $=5 * 10+1$
$3 \quad S=S+1$
C SET DISFLAY MENU AND HATA FOINTS TABLE
7 CALL TXCLEF
WKITE (IOUT,10)
10 FORMAT ("TABLLLATION OF DATA:-")
CALL HNOFEN(875.,715.,1)
CALL KNDISF (KNTXT,8,10,1)
CALL FFAME $(870 ., 733 ., 8)$
CALL TABLE
IHELF $=4$
C SET UF CURSOR KENU FICKING
4 CALL KNFICK (J,ICHAR,MNO)
77 CALL CONFRM (ICHAF)
IF (ICHAF.EQ. 78 ) GOTO 4
IF (ICHAR.NE.89) G0TO 77
IF (J.EQ.4) GOTO 44
IF (J.EQ.5) GOTO 444
IF (J.EQ.7) GOTQ 22
1Cㅍ.J
RETURN
C SORT DATA POINTS IN $X$
44 CALL FRKLLNK (XO,YO,ZO)
CALL SORTX (XO,YO,ZO,NFS,ID)
DO $101 \mathrm{I}=1$ INPS $X(I)=X O(I)$ $Y(I)=Y O(I)$
C THFEE-DIKENSIONS IF(ID.EQ.3) $\mathrm{Z}(\mathrm{I})=\mathrm{ZO}(\mathrm{I})$
101 CONTINUE
GOTO 111.
C SAVE DATA FOINTS ON DISC FILE AS USER FEQUEST
444 CALL FRKLNK (XO,YO,ZO)
CALL SAVE (XO,YO,ZO,NF'S,ID)
GOTO 4
END
C
C $\because * * * * * * * * * \pi E D I T$ DISPLAY**************************
C
SUBFOUTINE EDIT (IC,IA)
C INFUT COMMON DATA AREA

```
    COMMON/EATSUF/NFSSI{FI (50),IFREES,X(50),Y(50),Z(50),L(50),IH(5),
    M(5),METHON, IHELF, IFREV, BOUND (6),SUESET, INTFNT, IE (2)
    ID
    COMMON/IO/IN, LOUT
    C MENU ITEMS
    DATA MNTXT/* + NEXT + FREVIOUS + CORKECT + IEELETE + INSERT
&+ FESTART + EXIT "/
    DIMENSION A(41)
    INTEGEF SUBSET
    LOGICAL*I MNTXT (70)
1 CALL TXCLEE
C SET UF HISFLAY
    WFITE(IOUT,10)
10 FORMAT("DATA FOINTS EDITING:-")
    CALL MNOFEN(875.,715.,1)
    CALL MNDISF'(MNTXT,7,10,1)
    CALL FFAME (870.,733.,7)
C FAISE CUKSOK READY FOK USEK INTEFACTION
77 CALL HNPICK(J,ICHAF,FMO)
88 CALL CONFFM(ICHAF)
    IF (ICHAR.EQ.78) GOTO 77
    IF (ICHAR.NE.89) GOTO }8
C TFANSFER CONTROL TO AFFROFRIATE CODE IN THE FROGFAK
    GOTO(30,30,40,50,60,1,70),J
30 CALL UFDATE
C FETURN TO MAIN FFOGRAM
    IC =J
    GOTO 114
C CORRECT DATA FOINTS
40 WFITE (IOUT,20)
2.0 FORHAT (////"CORFECTION:-")
C FROMFT USER FOR INFUTING EDITTING INFORMATION
5 CALL HESSAG("A
    FEAD(IN,45) K2
45 FORMAT (GO.0)
    IF (M2.GT.10)GOTO 5
221 IF(ID.EQ.3) WKITE(IOUT,97)
    IF(IU.EQ.2) WKITE(IOUT,80)
80 FOKMAT (* ENTEFR I , X , Y:*)
97 FOKMAT("^ ENTEF I , X , Y , Z : ")
    LAST = (ID+1)*H2+1
    IF (IERROR(11O).NE.0)GOTO 222
    FEAU (IN,90) (A(I), I=1,LAST)
    FORMAT (40GO.0)
    A (LAST) =99
    CALL FCORCT (A)
    CALL UFDATE
    G070 100
c dELETE LATA FOINTS
5O WRITE(IOUT,110)
110 FORHAT (////"DELETION:-")
C USER INFUT DELETE INFORMATION
7 CALL MESSAG(** NUMEER OF DATA FOINT(MAX. JO)?N")
    FEAD (IN,45)M2
    IF (H2.GT.30)G0TO 7
125 WFITE(IOUT,130)
130 FOK'HAT(*# ENTER I IN DESCENDING ORDEF:*)
    LAST=H2+1
    IF(IEFFIOR(110).NE.0)GOTO 333
    FEAD (IN,90) (A(I),I=1,LAST)
    A (LAST) ==99
    IF (H2.EQ. 1)GOTO 11
```

```
    M1=M2-1
    U0 9 I=1.M1
        IF (A(I).LT.A(I+1))GOTO 125
    CONTINUE
11 CALL PDELET (A)
    CALL ufdatE
    GOTD 100
C IATA FOINTS INSERTION
60 WRITE (IQUT,150)
150 FORKAT (///// INSERTION:-- )
155 CALL MESSAG(** NUMBER OF UATA FOINTS (MAX. 1 FEF INTEFVAL,TOTAL 1O?"*)
    READ (IN,45)M2
    IF (M2.GT.10) GOTO 155
165 IF(ID.EQ.3)WRITE(IOUT, 180)
    IF (ID.EQ.2) WRITE (IOUTVITO)
170 FOKHAT("## ENTEF I , X , Y IN DESCENDING ORUER:")
    LAST=(ID+1)*M2+1
    IF (IERROR (110).NE.0)GOT0 444
    READ (IN,90) (A (I) , I=1,LAST)
    A (LAST)="99
    IF (M2.EQ.1)GOTO 190
    IF (ID.EQ.3)LAST1=4*M2-7
    IF (ID.EQ.2)LAST1=3*M2-5
    IDI=IL+1
    DO 18 I=1,LAST1,IE1
        IF(A(I).LT.A(I+IU+1)) GOTO 165
    CONTINUE
    CALL FADD(A)
    CALLL UPDATE
100 IC=3
114 IA=111.
    RETUKN
    LFLAG=1
224 HRITE(IOUT,223)
223 FORMAT ("WRONG INFUT !,TRY AGAIHI*)
    ENDFILE 5
    GOTO(221,125,165),LFLAG
333 LFLAG=?
    GOTO 224
444 LFLAG=3
    GOTO 224
    STOF
    END
C
C********** H E L P U I S P L A Y #*******************
C
C INFUT COMMON DATA AREA
    COMMOM/DATSUF/NFS,NFI (50), IFFEESFX(50),Y(50),Z(50),L(50), IH(5),
8
& ,ID
    COMMON/IO/IN,IOUT
C MENU ITEMS
    BATA MNTXTI/"+ F'REVIOUS+ EXIT */
C ONERLAY EXECUTABLE FROGRAM NALES
    DATA FMODL1,FMODLL2,FMODLS,FHOLL4,FHODL5,FHODLG/*PARAMETKIC*
&, "FYOLL2","FHODL3", "FHODL4" , "FMODLS", "FHODL6"/
    LOGICAL*1 KNTXT1(20), F'MORL1 (20), FMOLL2(10), FMODL3(10)
    LOGICAL*1 FMOML4(10), F'MOLLS(10), FMODLL6(10)
    IN=5
    IOUT=6
    CALL TXOFEN
```

```
C GET INFUT FILE
    CALL FROCKK1
1 CALL TXCLER
C OUTFUT DISFLAYS TITLES
    WFITE (IOUT,10)
10 FOFHAT (10X,"****************** H E L F **********************/
& //5X,"THE FOLLOWING DISFLAY SEQUENCE CONSTITUTE THE COMFLLETE*/
& 5X;"DATA FITTING PROCESS."//
& 5X, "YOU MAY ENTER ANY OF THESE DISFLLAYS BY USIMG THE CEOSS-HAIFN/
* 5X:"CURSOR ON THE T4O10 OR TRACKING CROSS ON LIGHT FEN ON THE GT42 :-"/)
    CALL MNOPEN(50.,540.,1)
    CALL MNTEXT(*+ INTROULOTION:- BRIEFLY GIVING THE USE OF THE SYST
&EM.* 54)
    CALL HNTEXT("+ ALGOFITHMS:- LIST OF AVAILABLE INTEFFOLATOFY METH
8ODS." %55)
    CALL MNTEXT(" + DATA ENTFY:- ENTER DATA FOINTS INTO THE SYSTEM FR
&OM DISC FL/KEYED."*'8)
    CALL MNTEXT("+ TABULATION OF DATA FOINTS:- INCLUNES EDIT,SOKT &
&SAVE DATA FOINTS.*,68)
CALL HNTEXT("+ FOLYGONAL FLOT:- DATA POINTS JOINED BY STRAIGHT L
&INE SEGMENTS.*,64)
                CALL MNTEXT<*+ FARAMETER ENTRY:-- FARAMETERS REQUIRED BY FAFTICUL
&AR ALGORITHM.**65)
    CALL MNTEXT("+ CUFVE FIT:- EISFLAY OF THE SMOOTH CUFVE INCLUDES
&ZOOM OPTION..ETC.*.69%
    CALL HNTEXT(*+ CLRIVE DESIGN:- INTERMEDIATE FOINTS SFECIFIED
& EY CUKSOR POSITION.*,66)
    CALL HNTEXT(*+ TABLE OF INTEFFOLATED FOINTS:- INCLUDES OFTION FO
&R COEFF.AHAKLCOFY.",70)
    CALL MNTEXT(*+ SUFERIMFOSED CUFVE:- SIMULTANEDUS DISFLY OF SEVEK
4AL CURVES":63)
    CALL HNTEXT(*+ USAGE OF CONTFOL COMMAMOS:- LIST OF ALL COMMANB U
&SED HERE.",59)
        CALL MNTEXT(*+ TERMINATE THE FROCESS:- EXIT FROM THE SYSTEM.",47)
    2 CALL HNFICK(I,ICHARyMNO)
3 CALL CONFNH (ICHAF)
        IF (ICHAR.EQ.78) GOTO 2
        IF(ICHAF.NE.89) GOTO 3
        IF(I.GT.4) GOTO 5
C ONEFLAY THE APPROPRIATE MOULLES
        IHELF'mI
        CALL FWRCM1
        CALL OURLAY (FHODLI)
5 IF(I.GT.6) GOTO 6
        IHELP=I-4
        CALL PWFICHI
        CALL OURLAY (FMODL2)
6 IF(I.LT.9.OR.I.GT.10)G0T0 7
    IHELF=I-8
    CALL FWFCM1
    CALL GURLAY(F'HODLG)
7 IF(I.EQ.7) CALL OURLAY (FMODL4)
    IF (I.EQ.B) CALL OURLAY (FMODLS)
    IF (InNE.12) GOTO 133
C FROGRAM TERMINATE
    CAL.L FEXIT
    STOF
C DISPLAY COMMATID USAGE DISFLAY
133 CALLL TXCLEER
    CALLL MNOPEN(875.,715.,1)
    CALL MNUISP(MNTXT1,2,10,1)
    CALL FFAME (870.,733.,2)
```

```
    CALL ALFHMD
    CALL CUKFOS(1.,770.)
    CALL TEXTUF'("F'HELF'TXT",26)
22
    CALL. HNFICK(J,ICHAR, MNO).
222
    CALL CONFRM(ICHAF)
    IF (ICHAF.EQ.78) GOTO 22
    IF (ICHAR.NE.89) GOTO 222
    GOTO (1;111) %J
111 CALL FEXIT
    STOF
    END
C
C ***********EDIT-INSERTT FUNCTION**X******************************
C
    SUERDUTINE PADD(C)
C INFFUT COMMON DATA AFEA
    COMMON/DATSUF/NF'SNFFL (50), IFREES,X(50),Y(50),Z(50),L(50),IH(5) ,
&
&
                    M(5), METHON , IHELF , IF'REW, BOUND (6), SUBSET, IHTFNT,
                        IE(2),ID
            DIMENSION C(41)
            INTEGER SUBSET
C ADD DATA FOINTS AND UFDATE LINK LIST
    IF = IFREES
    ID1=1D+1
    DO 3 I=1,41,ID1
C CHECK DATA FOINTS TAELE INDEX
    IF (C(I).EQ.99) GOTO 2
    IF(C(I).GT.NF'S)GOTO 3
        IF (C(I).EQ.0)GOTO 4
        IC=C(I)
C GET LINK LIST LOCATION OF THE DATA FOINTS GND SET LINKS
        IS*INDEX(IC)
        L(IF)=L(IS)
        L(IS)=IP
        GOTO 5
4 L(IF)=IIH(1)
        IH(1)=IP
C NDW ADD FOINT TO FREE LOCATION
5 X(IP)=C(I+1)
        Y(IF)=C(I+2)
C 3-DIMENSIONAL CURVE
    IF(ID.EQ.3)Z(IF')=C (I+3)
        IF=1P+1
        NFS=NFS+1
3 CONTINUE
C SET FREE LINK LIST FOINTEK
2 IFKEES=IP
    RETUKN
    END
C
C************EDIT - CORfRECT*************X*****************
C
    SUBFOUTINE FCORCT (C)
C INFUT COMMON BATA AREA
    COMMON/DATSUP/NFS,NFI (50), IFREES,X (50),Y(50),Z(50),L(50),IH(5),
&
&
                    M(5), METHOD, IHELF, IF'REU, BOUND (6), SUESET, INTF'NT,
                    IE(2) FID
    DIMENSION C(41)
    INTEGER SUBSET
    IDI=ID+1
    BO 2 Im1,41,1U1
C CHECKS ENTRY OF COFFECTION OF UATA FOINTS
```

IF (C (I).EQ.99) G0T03
IF (C (I). GT.NFS) GOTO 2
IC=C(I)
C GET LINK LIST LOCATION AND REFLACE FOINT
$K=I N D E X(I C)$
$X(K)=C(I+1)$
$Y(K)=C(I+2)$
C 3-D CURVE
IF (ID.EQ. 3 ) $Z(K)=C(I+3)$
2 CONTINUE
3 FETURN
END
C

C
SUBFOUTINE PDELET (C)
C INFUT COMMON DATA AKEA
COMMON/DATSUP/NFS,NFI (50), IFREES,X(50), Y(50), Z (50), L (50) , IH (5) ,
8
8 M(5) , METHOD, IHELF', IFREV, GOUND (2) , SUBSET, INTFNT, IE (2), ID
DIMENSION C(41), XO (50), YO (50), ZO(50), LO(50)
INTEGER SUBSET
DO 1 I $=1$ 1.41
C CHECKS DATA POINTS TAELE INDEX
IF (C (1).EQ.99) GOTO 3
IF (C (I).GT.NPS)GOTO 5
IF (C(I).EQ.1) GOTO 4
$I C=C(I)-1$
C GET LINK LIST LOCATION AND DELETE DATA FOINTS
IS=INJEX(IC)
L(IS)mL(L《S))
GOTO 1
$5 \quad$ NPS miNF $5+1$
BOTO 1
$4 \quad \mathrm{IH}(1)=\mathrm{L}(\mathrm{IH}(1))$
1 CONTINUE
$3 \quad N P S=N P S-I+1$
IFREES=IFREES-I +1
C GARBAGE COLLECTION
$I P=I H(1)$
DO $6 \mathrm{~K}=1$, NF'S
$X O(K)=X(I F)$
$Y O(K)=Y(I P)$
IF (ID.EQ. 3 ) ZO (K) $=$ Z (IF)
$L O(K)=K+1$
IP=L(IF)
6 CONTINUE
DO $7 \mathrm{J=1} \mathrm{INFS}$
$X(J)=X 0(J)$
$Y(J)=Y O(J)$
IF (IE.EQ. 3 ) Z (J) $=Z O(\mathrm{~J})$
$L(J)=L O(J)$
7 CONTINUE
L. (NF'S $)=0$

IS $=0$
100 $9 K=1,5$
$1 H(K)=15 * 10+1$
IS $=15+1$
9 CONTINUE
RETURN
END
C

$C$
SUBRDUTIME GETFLN (NAME)
INTEGER NAME (3)
C GET FILE NAKE \& SAVE IT IN AN INTEGEF AFFAY
CALL MESSAG(*~ DATA FILE NAME (MAX. 10 CHAFACTERS)? ?~"
READ (5.30) NAME
30 FORYAT (2A4,A2)
FETUFN
END
C
C **************FINDS DATA FOINT LOCATION ITl THE LINK LIST**********
C
INTEGER FUNCTION INDEX (INX)
C INFUT COMMON DATA AREA
COMMON/DATSUF/NFS, MFI (50), IFREES, $X(50)$, $Y(50), Z(50)$, $L(50)$, IH(5),
4
4 DID
INTEGER SUBSET
C FINDS WHICH FOKTION OF THE LINK LIST?
U0 $11=1,5$
IF ( $\mathrm{H}(\mathrm{I})$. GE.INX) GOTO 2
1 CONTINUE
2 IS=IH(I)
C COMFUTE LDCATION
$I N X=I N X-(I-1) * 10$
$I N X 1=I N X-1$
IF (INX1.EQ.O) GOTO 55
DO 3 I=1,INXI
3
15=L(IS)
55 INDEX=IS RETURN
END
6

C
SUBROUTINE READAT (FLNAME,A,B,CyN.IF,IDIK)
DIMENSION $A(1), B(1), C(1)$
INTEGER FLNAKE (3)
FEWIND 9
C DFEN INFUT FILE
CALL SETFIL (9,FLNAME)
IF (IERKOR (103). NE. 0) GOTO 99
C MUMBER OD DATA FOINTS
FEAD (9,20)N1
20 FOFMAT (13)
IF (N.GT.N1) GOTO 100
C THREE - DIMENSIONS
IF (IDIK.EQ.3) G0T0333
$\operatorname{READ}(9,10)(A(I), B(I), I=1, N)$
ENDFILE 9
RETUKN
333 READ $(9,10)(A(I), B(I), C(I), I=1, N)$
ENDFILE 9
RETURN
10 FORMAT (F12.4)
99 ENDFILE 5
101 IF:=1
RETURN
$100 \quad \mathrm{IF}=$ ?
FETURN
END
¢
C $\mathrm{CH}^{* * * * * * * * * * S A U E ~ D A T A ~ F O I N T S ~ O N ~ D I S C ~ F I L E * * * * * * * * * * * * * * * * * * * * * * * ~}$
c
SUBFOUTINE SAUE (A,B,C.N,IDIM)
COMMON/IO/IN,IOUT
INTEGER FILE (3)
DIMENSION $A(1), E(1), C(1)$
c get file name frid the usef thridugh the keyboad
WFITE (IOUT,10)
10 FOKMAT (//////////61X,"~~~ILE NAME?")
CALL KESSAG("
4
READ (IN,20)FILE
20 FORTAT ( 2A4,Aㄹ)
c DUTPUT DATA FOINTS ON DISC FILE CALL WRTDAT(FILE,A,BIC,N,IDIM) RETURN
END
c
C*********SORT IN X COORDINATE*************************
C
SUEROUTINE SORTX (X1,Y1,Z1,N,IDIK)
DIMENSION X1(1),Y1(1),Z1(1)
$\mathrm{N} 1=\mathrm{N}-1$
C PERFORM QUICK SORT
DO $3 \mathrm{I}=1, \mathrm{Ni}$ DO $2 \mathrm{~J}=\mathrm{I}, \mathrm{N} 1$

IF (X1 (I). LE. X1 (J+1) ) GOTO 2
A1=XI (I)
B1=Y1(I)
IF (IDIM.EQ.3)C1=Z1(I)
$\mathrm{X1}(1)=\mathrm{X} 1(\mathrm{~J}+1)$
$\mathrm{Y} 1(\mathrm{I})=\mathrm{Y} 1(\mathrm{~J}+1)$
IF (IDIM.ER.3) $\mathrm{Z1}(\mathrm{I})=\mathrm{Z1}(\mathrm{~J}+1)$
$\mathrm{X} 1(\mathrm{~J}+1)=\mathrm{A} 1$
$Y 1(J+1)=81$
IF (IDIM.EQ.3) Z1 (J+1) $=$ C.
CONTINUE
CONTINUE
FETUFN
END
c
C************TABULATION OF SATA FOINTS KOUTINE*************
c
SUBROUTINE TABLE
C INFIT COMMON DATA AREA
COMMON /DATSUP/NFS,NFI (50), IFREES, $X(50), Y(50), Z(50), L(50), I H(5)$,
6 $M(5)$, METHOD, IHELF, IFFEEV, BOUND (6), SUBSET, INTFNT, IE (2)
$\&$
COMMON /IO/INPIOUT
INTEGER S1,S2,SUBSET
CALL CURFOS (2.,710.)
C 3-DIMENSION
IF (ID.EQ.3)GOTO 33
C OUTfut Title colurn
WKite (IOUT, 10)
10
FORMAT(" I", 7X,"X(I)",8X "Y(I)",7X," I",5X,"X(I)",10Xp"Y(I)"/)
GOTO 34
WRITE (IOUT,40)


c GET STAFTING FOINTEK

```
34 S2=IH(1)
    S1=L(S2)
    IF(S1.NE.0)GOTO12
C 3-D
        IF(ID.EQ.3) GOTO 44
        WRITE(IOUT,11) X(S2),Y(S2)
11 FORHAT(" 1",2X,2(E11.4,3X))
        RETUKN
    44 WRITE(IOUT,31)X(S2),Y(S2),Z(S2)
    31 FOKMAT(" 1",2(E9.2,X),E9.2))
    EETURN
    C OUTPUT TABLE ITEKS FROH THE LINK LIST
    12 DO 7 I=1,50,2
        J=I+1
        IF(ID.EQ.3) GOTO 55
        WRITE (IOUT, 20) I,X(S2),Y(S2),J,X(S1),Y(S1)
20 FORMAT(12,2X,2(E11.4,3X),12,2X,2(E11.4,3X))
155 S2=L(S1)
        IF(S2.EQ.0)G0TO 15
        S1=L(S2)
        IF (S1.NE.0)GOTO 7
        I=I+2
        IF(ID.EQ.3) GOTO 333
        UFITE(IOUT,30) I,X(S2),Y(S2)
        FORMAT(12,2X,2(E11.4,3X))
        GOTO 15
7 CONTINUE
15 FETURN
55 WRITE(IOUT,120)I,X(S2),Y(S2),Z(52), J,X(S1),Y(S1),Z(S1)
120 FOFMAT(12,2(E9.2,X),E9.2,12,2(E. 2,X),E9.2)
    GOTO }15
333 WRITE(IOUT, 303)I;X(S2),Y(S2),Z(S2)
303 FORMAT(I2,2(E9.2,X),E9.2)
    GOTO }1
    END
C
C E######***************LF'DATE LINK LIST AFTER EDITING***********************
C
    SUBKOUTINE UPDATE
C INPUT COMMON DATA AREAS
    COMMON/DATSUF/NFS,NFI (50), IFREES,X(50),Y(50),Z(50),L(50), IH(5),
                M(5) , METHOD, IHEL.F, IFREV, BOUND (6), SUBSET , INTFNT,
                    IE(2),ID
    INTEGER SUBSET
    IN=IH(1)
    DO 1 J=2.5
        DO 2 Kwi,10
            IR=L(IN)
                IF (IR.EQ.O)GOTO3
            CONTINUE
        IH(J)=IR
    CONTINUE
    FETUFN
    END
C
*************** SAUE DATA ON DISC FIL.E ***********************************
C
    SUBFOUTINE WFTDAT (FLNAME,A,B,C,N,IDIM)
    IIYENSION A(1),B(1),C(1)
    INTEGEF FL.NAME(3)
    REWIND }
C OFEN OUTFUT FILE
```

```
    CAILL SETFIL(9,FLNAME)
    WRITE(9,20)N
C 3-DIMENSION
    IF(IDIM.EQ.3) GOTO 333
    WFITE (9,10)(A(I),B(I),I=1,N)
    ENUFILE }
    FETUKN
    WFITE (9,10)(A(I),E(I),C(I),I=1,N)
    ENDFILE }
    FETUFN
    10 FORMAT (F12.4)
20 FORIMAT (I3)
END
```

```
C
*******************
* APFENDIX 2.32 *
******************
C
C THIS MOULLE HANDLES THE FOLLOWING INTERACTIUE DISPLAYS:-
C 1.FOL.YGONAL FLOT (2-D ONL.Y)
C 2.FARAMETER ENTFY
C
C
C
C.********* MAIN FROGRAM - MONLLE 2 ***************
C
6
C INFUT COMMON DATA AREA
    COMMON/DATSUF/NF'S,NPI (50), IFFEES,X(50),Y(50),Z(50),L(50),IH(5),
                M(5) , METHON, IHELF,IF'REN, BOUNG (6),SUBSET, INTFNT' IE (2)
                                    , ID
    COMMON/IO/IN,IOUT
C ONERLAY EXECUTABLE PROGRAM NAMES
    BATA PMODL3,F'MODL1,FHELF/"FHODL3", "FARNAMETRIC" "HELF"/
    LOGICAL_*1 FHOELS (10), FHODL1 (20) FFHELF (10)
    INTEGER SUBSET
C INFUT COHMON DATA
    CALL FRDCMI
    CALL TXOFEN
C TENMINAL INFUT/OUTFUTT CHANNEL
    IN=5
    IOUT=6
    IF(IHELF.GT.1) GOTO 6
    IF (IFREV.GT.1) GOTO 5
    IF (IFREU.EQ.1.OR.ID.EQ.3) GOTO 4
C FOLYGONAL IISFLAY
C CALL POLYGL (X,Y,NF'S,IC)
    GOTO(1,2,20,20,20,20,25,20,30), IC
C FREUIOUS DISFLAY
2 IFREV=1
    IHELF=0
    CALL FWFECHL
    CALL OURLAY (FMOQLI)
C PARAMETER UISFLLAY
1 CALL FARKET (METHDD,SUESET, INTFNT,BOUND,NFS,IE,ID,IC)
    CALL CURFOS(410.,780.)
    GOTO (10,31,25,1,30) IC
    IF(ID.EQ.2) GOTO 3
    gOTO 2
C NEXT DISFLAY
10 IFKEV=0
    IHELF'=0
C SAVE INFUT COMMDN EATA
    CALL FWECCH1
    CALL OUFLAY (F'MODLS)
C PFOGRAM TEFMINATE
30 CALL FEXIT
20 STOF
4 IFREV=0
    IHEL_F=0
    gOTO 1
C HELF DISFLAY
25 CALL FWRCM1
    CALL OVELAY (FHELF)
5 CALL ERFMES (IC)
```

GOTO (1,20), IC
C RETUFN FFROM HELF DISFLAY
6 GOTO $(3,1)$ IIHELF
END
C

C

## SUBROUTINE FOLYGL (APB,N,IC)

C PLOT THE DATA POINTS SUFFLIED AND JOINED THEM WITH STRAIGHT LINES COKMON/LO/IH,IOUT
C MLXUS ITEMS
DATA KNTXT/" + NEXT + FREVIOUS + GFAFH + COOROS. + DISF. ORG +
GAX. MAKK+ HELF + FESTAKT + EXIT */
LOGICAL*1 MNTXT (90)
DIMENSION $A(1)$, $B(1)$, XO(50) y YO (50)
EXTERNAL FFLOT
C SET UP DISFLAY
1 CALL TXCLER
ICORD $=0$
WRITE (IOUT, 10)
10 FORNAT ("FOLYGONAL FLLOT $3-*$ )
C OUTFUT MENU
CALL MNOPEN(875.,715.,1)
CALL MNDISF (KNTXT,9,10,1)
CALL FRAME (870.1733.99)
C REMOVE LINKS \& FIND SCALE VALUES
CALLL PRMKNK (XO,YO,ZO)
CALL MINMAX (S1,S2,S3,S4,XO,YO,H)
C SET UP CURSOR FOR USER MENU
2 CALL LMTARA
CALL MNFICK ( $J$, ICHAF, MNO)
IF (J.EQ. 4. AND. ICORD.EG.2) GOTO2
7 CALL CONFたK (ICHAR)
IF (ICHAR.EQ.78) GOTO 2
IF (ICHAR.NE.B9) GOTO 7
$\operatorname{GOTO}(20,20,3,4,5,6,20,1,20), \mathrm{J}$
C RETURN TO CALLING PROGRAM
20 IC=J
RETURN
C FLOT THE FOL YGONAL OF THE DATA FGINTS
3 CALL DRAW (FFLLOT,FirS1,52,53,S4,N)
GOTO 2
C CLKSOR INPUT COORDINATES
4 CALL DISCOR (ICOKD,S1,52.53,54)
GOTO 2
C DISFLAY ORIGIN
5 CALL DISORG(S1,S2*S3,S4)
GOTO 2
C. AXES MARKING

6 CALL AXSMRK (S1,S2,53,54)
GOTO 2
END
C

C
SUBFOUUTINE FARMET (M,SUET, INTFNT, B,N,IE,IDLK, IC)
COMMON/IO/IN.IOUT
© MENU ITEMS
BATA HNTXTL/" + NEXT + FREUIOUS + HELF + RESTART + EXIT */
DATA MNTXT2/" + SFECIFY + DEFALLT + CUKSOK */
BATA HNTXT3/* $\quad$ + CLAMFED + FELAXED + FARABCLA + Q-SFLLINE"/
DAYA KNTXT4/" + X-BOND' $Y+Y$-BOND'Y $+Z-B O N D{ }^{\prime \prime} Y^{\prime \prime} /$

```
    LOGICAL*1 MNTXT1 (50), MNTXT2(30), MNTXTZ(50), MNTXT4 (40)
    INTEGER SUBT
    DIMENSION B(1),IE(1)
1 CALL TXCLEEF
C BEFAULT VALUE SETTING
    INTFNT=0.
    00 555 I=1,ó
555 E(I)=0.
112 IE(1)=1.
    IE (2)=1.
{ SET UF THE DISFLAY
1011 WRITE(IOUT,10)
10 . FORMAT ("F'ARAMETER ENTRY:-*/)
    G0TO (101,102,103,104),M
20 CALL CURFOS(1.,O&O.)
C OUTPUT INSTRUCTION FOK USER TO TAKE AFF'KOFKIATE ACTIONS
    WRITE(IOUT,21)
21 FORHAT(*SELECT THE AF'FFOFRIATE OFTION FROM THE */
8 "FOLLOLING FARAMETEF SFECIFICATION(*) :-"///
& 6X,"1-CHOICE OF INTERHEDIATE*/
8 BX,"FOINTS REQUIRED FOR SHOOTH DRAWING:-*)
    IF (H.NE.4) GOTO 1221
    WRITE(IDUT,15)
15 FOKYAT (//6X,*2-SELECT THE CONDITION")
1433 WRITE(IOUT,1333)
1333 FORKAT (7X," AT EACH END OF THE CURUE:-*/
                8X,"N.B:- FIEST ENU, TYFE '1'"/
                13X,"SECOND END , TYFE '2"*)
            GOTO 143
1221 IF(H.EQ.2.OK.K.EQ.3) GOTO 1.42
    WRITE(IOUT,22)
22 FORMAT (/6X,"2-BOUNDAF'Y CONDITION:-*//)
143 WRITE(IOUT,7)
7 FORHAT (///////////////** IF NO AFFGOFRIATE FAFGMETEK IS SELEETED*
| /"WHEN KEQUIRED THEN DEFAULT VALUES AFE ASSUMED")
C DISFLAY CONTROL COMMAND KENU
    CALL MNOFEN(875.,715.,1)
    CALL MNUISF (MNTXT1,5,10,1)
    CALLL FFAME (870.,733.,5)
    CALL MNOFEN(670.,565.,2)
    CALL. HNDISF (HNTXT2,3,10,2)
    CALL DTEXT (B10.,540.,'*',1)
    IF(M.NE.4) GOT0 }9
    CALL MNDISF(HNTXT3,5,10,2%
    CALL DTEXT (810.,455.,'*',1)
    MF=0
    GOTO }8
142 WRITE(IOUT,1420)
1420 FOFMAT (///)
    GOTG 143
99 MF=3
    IF (M.EQ.2.OK.M.EQ.3) GOTO B8
    CALL HNDISF (HNTXT4,4,10,2)
    MF:=7
88 CALL FFAME (670.,582.,MF)
    IF (M.EQ.2.OF.M.EO.3) GOTO 2
    CALL TXMOUE(670.,512.)
    CALL TXUKAW(810.,512.)
C CUKSOR FICKING
2 CALL MNFICK(J,ICHAK,MNO)
    IF (MNO.EQ.2) GOTO 130
5 CALL CDNFFM(ICHAR)
```

IF (ICHAR.EO. 78) GOTO 2 IF (ICHAR. NE. 89) GOTO 5 IF (J.EQ.4) GOTO 1
IC=」
RETUKN
C FARAMETER SFECIFICATION CDNTFOL
$130 \quad$ GOTO (35,36,37,38,39,40,41,42), J
C USER SFECIFIED MUMBEF OF INTERMEUIATE FOINTS FEF INTFEVAL
35 CALL CUKPOS (1.,360.)
66 CALL HESSAG(** NUMBER DF INTERFOLATED FOINTS FER INTEFVAL? *~") IF (IEFROR(110).NE.0) GOTO 171
FEAD (IN:77) INTF'NT
77 FORHAT (GO.0)
ISUM=INTFNT* $(N-1)+N$
IF (ISUM.GT.200) GOTO 187
GOTO 2
171 ERIDFILE 5
GOTO 66
187 WRITE(IOUT:403)
403 FOKMAT ("TOTAL NUMBER OF FOINT EXEEEDING LIMIT,TRY AGAIN")
gOTO 66
C DEFALLT
36 INTFNT=0
GOTO2
C CUKSOK
37 INTFNT $=999$
38 GOTO2
C BOUNDAKY CONDITION
$39 \operatorname{GOTO}(139,2,2,391,2), H$
GOTO 2
391 IF (ICHAR.EQ.49.OR.ICHAF.EQ.5O)GOTO 392
G0T02
392 ICHAF=I ICHAF-48
GOTO (272,202), ICHAR
gOTO 2
$272 \quad \operatorname{IE}(1)=1$
2721 CALL CUFFOS (1.1.300.)
2120 IF (IUIM.EQ.3)CALL MESSAG("
( VALUE (1ST END)? ?*)
IF (IDIM.EQ.2)CALL MESSAG("备 SLOFE OF X.Y W.F.T. T AS BOUNDARY
4 VALUE (IST END)? ${ }^{* *)}$
IF (IERIROR (110). NE. 0 ) GOTO 2120
READ (IN,1110) B(1), B(2), B(3)
1110 FORMAT (3GO.0)
GOTO 2
202 IE (2) $=1$
2021 CALL CURPGS(1.7270.)
2110 IF (IDIM.EQ.3)CALL MESSAG("* SLOF OF X,Y,Z WiFi.T. T AS BOUNDARY
4 VALUE (2ND END)? ? ${ }^{(2)}$
IF (IDIM.EQ.2) CALL MESSAG(" $\%$ SLOF OF X,Y W.F.T T AS BOLNOAFIY
\& VALUE (2ND END)?~")
IF (IERKOR(110). ME.O) GOTO 2110
READ (IN, 1110) B(4), B(5), B(6)
GOTO 2
139 CALL CUKPOS(1.,300.)
404 CALL KESSAG(** FARAMETRIC BCUUNDAFYY VALUES AT BOTH END (D2X/DT2)?N~) IF (IERROR (110). NE.0) GOTO 404
FEAD (IN,11)B(1), B(4)
11 FGRMAT (2G0.07
goto 2
$40 \quad \operatorname{GOTO}(444,2,2,411,2), 4$
444 CALL CUFPOS(1.,270.)

```
444 CALL MESSAG(** FARAMETRIC BOUNDAFY WGLUES AT BOTH END(D2Y/DT2)?`*)
        IF(JERROR(110).NE.0) GOTO 4444
        READ(IN,11)B(2),B(5)
        GOTO2
41
4141 IF(IDIM.EQ.2)GOTO 2
        C.ALL MESSAG("* FARAMETFIC BOLNDAFY VALUES AT BOTH EMD(D2Z/DT2)?^")
        IF(IERROR(110).NE.0) GOTO 4141
        READ(IN,11)B(3),B(6)
        goto 2
        GOTO(2,2,2,411,2),H
        GOTO 2
101 WFITE(IOUT,111)
111 FORMAT(**** STANDARD FAKAMETFIC CUBIC SFLINE****)
        GOTO 20
102 WFITE(IOUT,122)
        goto 20
122 FORHAT ("*** CYCLIC CUBIC SFLINE****)
103 HRITE(IOUT,133)
133 FORMAT("*** ANTICYCLIC CUBIC SFLINE ****)
        gOTO 20
104 WRITE(IOUT,144)
144 FORKAT(**** CUBIC SFLINE WITH UARIAELE EMD CONDITION ***^)
        GOTO 20
        END
C
C ****************ERFROR MESSAGE UISFLAY********************************
C
    SUEFOUTIINE ERRMES(IC)
    COMMON/IO/IN,IOUT
C HENU ITEMS
    DATA MNTXT/"+ FRENIOUS+ HELF' + RESTART + EXIT */
    DATA DATSP/"DATSUFFL"/
    LOGICAL*1 KNTXT (40),DATSF(10)
1 CALL TXCLER
    WRITE (IOUT,20)
20 FORMAT("ERROR MLSSAG:-"/"TOD MANY FOINTS FOK JOINNING CURVES"/
| "WHICH EXCEED CORE LIMIT"/
"you may froceed ey taking the following action:-"/
"EITHER 1- USE FREUIOUS COMMAND TO gO baCk to fARAMETER"/
"DISFLAY,SO THAT TO ALTER.ND.OF INTERMEDIATE FOINTS."/
"OR 2- USE HELF COMMAND IN ORNEE TO ERANCH TO ANY"/
"DISFLAY ,E.G DATA ENTFY OR DATA TABULATION DISFLAYS..ETC")
    CALL MNOPEN(875.,760.,1)
    CALL MNDISF (MNTXT,4,10,1)
    CALL FRAME (870.,778.,4)
120 CALLL HNFICK(JIICHAK,HNO)
110 IF (ICHAR.EQ.78) GOTO 110
    IF (ICHAR.NE.89)GOTO 120
    GOTO (40,40,1,50).J
C PREUIOUS DISFLAY
40 IC=J
    RETUFN
50 CALL FimFilE(DATSF)
    STOF
    END
¢
@*********FLOT THE FOLYGONAL OF THE GATÁ FOINTS**************
```

SUBROUTINE FFPLOT ( $\mathrm{F}, \mathrm{SCL} 1$, SCL2,SCL3,SCL4,N)
C INFUT COMMON DATA FOINTS
COMMON/DATSUF/NFS,NFI (50), IFREES,X(50),Y(50),Z(50),L(50),IH(5),
4 M(5) , METHOD Y IHELF, IFREV Y BOUND (2) , SUBSET, INTFNT, IE (2)
4 ID
DIMENSION XO(50),YO(50)
C REMOUES LINKS
CALL FRYMLK (XO,YO)
$1111=1$, NF'S
IF (I.EQ.1) GOTO 2
CALL TXURAW (XO (I) YO (I) )
CALL FLUSGH(SCL1;SCL2,SCL3,SCL $4, X 0(1)$,YO(I))
CALL TXHOUE (XO (I) Y YO (I) )
RETUFN
END

```
C
*******************
* AFF'ENDIX 2.33 *
******************
C
¢ THIS MODULE HANDLES THE FOLLOWING IMTERACTIVE BISFLAYS:-
C 1.CURVE FIT
C 2.CURVE ZOOM
C
C
C
C ******* MAIN FROGRAM - MODULEE 3 ******************
C
C
C I/O COMMON DATA AREA
    COMMON/DATSLF/NFSNNFI (50), IFREES,X(50),Y(50),Z(50),L(50),IH(5),
                M(5) , HETHOD, IHELFF, IFKEU, BOUND (6) , SUBSET , INTFNT, IE (2)
| IIL
    COMMON/CURUEFIT/XCOEF (50,4),YCOEF (50,4), ZCOEF (50,4), XCORD (200),
                                    YCORD (200) , ZCORD (200) , TCOKD (200)
    COMHON/IO/INPIOUT
C OVERLAY EXECUTABLE FFIOGFAM MODULES
    LATA PHODL1, F'HODL2,FHODLS,FMODLG/"FAFAMETKIC", "F'HODL2","FHOULS"
|"PMOCL6"/
    DATA FHELP/"HELP"/
    INTEGER SUBSET
    LOGICAL*1 F'KODL1 (20), FMODL2(10), FMODLS (10), FHOLL6(10), FHELF'(10)
    CALL TXOFEEN
C READ I/D FILES
    CALL PRDCM1
11 NC=4
21 IN=5
    IOUT=6
    CALL FFWCH2(NFS,NFI,NC,ID)
C CURVE DESIGN DISFLAY ?
    IF(INTFNT.EQ.999) G0TO 111
C CLRVE FIT DISFLAY
    CALL CRUFIT (NF'S,HF'I;XCOKD,YCORD,ZCORD,ID,IC 
    GOTO(2,3,2,2,2,2,6,8,2,111,2,2,14,2,15,2,22),IC
C PROGRAM TERMINATE
22 CALL FEXIT
2 STOF
& PREVIOUS DISFLAY
IFKEV=1.
    IHELF:=O
    CALL FWFCHE
    CALL DURKAY (F'HODL2)
C TABULATION OF INTEFFLOATED DATA FOINTS DISFLAY
6 IFREV=1
100 IHELF=0
    CALL FWRCM1
    CALL OUNLAY(FMOULG)
¢ SUPERIMFOSED CURUES DISFLAY
8 IF&EV=2
    GOTO 100
¢ CURVE DESIGN DISFLAY
111 IFREV=0
    IHELF:=0
    CALL FWFCMI
    CATLL OUFLAY(FMONLS)
14 IFYEV=O
    IHELF=O
```

```
    CALL FWKCM1
    CALLL OUFI.AY (FMOUL1)
C HELF' DISFL_AY
15 CALL FWFCH1
    CALL OURLAY (FHELF)
    END
C
C #**************** CURVE FIT LISFLAY **************************
C
    SUBROUTINE CRUFIT(N,NI,XX,YY,ZZ,IDIK,IC)
    COHMON/CUKUES/NCRV(10),XYSCL (4)
    COMMON/IO/IN,IOUT
C MENS ITEMS
    [ATA MNTXT1//* + NEXT + F'KEVIOUS+ YX-GFAF'H+ XZ-GFAFHH+ ZY-GRAFH
4+ COOROS. + TABLES + NGRAFH + ZOOM */
    DATA MNTXT2/"+ CRU.DES.+ SAVE + KEDRAN + METHOD + AX. MARK
t+ HELF + FESTART + EXIT */
    IIMENSION N1(1),XX(1),YY(1),ZZ(1)
    LOGICAL*1 HNTXT1(90),HNTXT2(80)
    INTEGER F
    EXTERNAL CFLOT
    IF (IEFFROR(103).NE.0) GOTO 99
    CALL RDCFUS
    MSUM=0
    1R=N-1
c cOMfUTE TOTAL NUMEER OF FOINTS
    DO 6 I=1,N2
6 MSUM=MSUM+N1 (I)
            HSUM=MSUMY+N
1 CALL MIMMAX(S1,S2,S4,ES,XX,YY;MSUM)
    IF (IDIM.EQ.Z)CALL KINHAX(S1,S3,S4,SÓ,XX,ZZ,MSUM)
    F=0
    101 CALL TXCLEF
        ICOFD=0
    NG=1
C SET UP DISFLLAY
    WRITE(IOUT,10)
10 FOFMAT ("CUKVE FIT:-")
    CALL MNOFEN(875.,715.,1)
    CALL HNNDISF(MNTXT1;9,10,1)
    CALL MNDISF(KNTXT2,8,10,1)
    CALLL FFAME (870.,733.,17)
    IF(R.EQ.O) GOTO 2
    GOTO(31,331,3331),F
C SET UF CUKSOR PLCKING
2 CALL LMTARA
    CALL MNFFICK(J,ICHAK,MNO)
    IF (J.EQ.6.ANB.ICORD.ER.2) GOTO 2
    IF(J.EQ.8.AND.NG.EQ.2) GOTO 3O
17 CALL CONFEK(ICHAF)
    IF (ICHAR.EQ.78) GOTO 2
    IF (ICHAR.NE.89) GOTO 17
    G0TO(30,30,3,33,333,4,30,8,9,30,11,12,30,15,30,1,30),J
C NO CLRSOK IESIGN FOR 3-1
    IF(J.EQ.1O.AND.IDIM.EQ.3) GOTO 2
30 IC=J
    RETURN
C YX-GFAFH FLLANE FROJECYION
3 IF(F.EQ.O) GOTO 31
    R=1
    GOTO in1
31
    k==1
```

$5 C 1=51$
SC2=52
SC3=54
SC4=55
GOTO 303
C $\times 2-G R A F H$ FLANE FROJECTITN
33 IF (IDIM.EQ.2) GOTO 2
IF ( $\mathrm{F} . \mathrm{EQ} .0$ ) GOTO 331
R=2
goto 101
$331 \quad \mathrm{~K}=2$
$5 C 1=53$
SC2: $=$ S1
$5 C 3=56$
SC4=54
6070303
C ZY-GFAFH FLANE FROJECTION
333 IF(IDIM.EQ.2) GOTO 2
IF (R.EQ.O) GOTO 3331
$\mathrm{R}=3$
G0T0 101
3331
$R=3$
SC1=S2
5C2=53
5C3=55
SC4=56
GOTO 303
C BISPLAY OKIGIN
303 CALL GISORG(SC1,SC2,SC3,SC:4)
CALL HFAW (CFLOT,Fi,SC1,SC2,SC3,SC4, HSUM)
GOTO 2
C CLKSOR COORDINATES
4 IF (R.EQ.O) GOTO 2
CALL DISCOR(ICORD,SC1,SC2,SC3,SC4)
GOTO 2
C save cufve
11 IF (R.EQ.O) GOTO 2
GOTO (51,52,53), R'
51 CALL CRUSAV (XX,YY,N,N1,HSUK,SC1,SC2,SC3,SC4, J) GOTO 2
52 CALL CRUSAU(ZZ,XX,N,N1,MSUM,SC1,SC2,SC3,SC4,J)
GOTO 2
53 CALL CRUSAV(YY,ZZ,N,N1,MSUM,SC1,SC2,SC3,SC4,J)
GOTO 2
C REDKAW A CUKVE

gOTO 2
C AXES MARKING
15 IF (IDIH.EQ.2.AND.F.EQ.O)CALL AXSMKK (S1,S2,S4,S5)
IF (K.EQ.O) GOTO 2
CALL AXSMFK (SC1,SC2,SC3,SC4)
GOTO 2
C \#GRAFH COMMAND FOR THE FIRST TIME (I.E SANE CURVE FOR LATER USE)
8 IF (IDIK.EQ.2.AND.F.EQ.O) CALL NGFAFH (N,N1,MSUM,XX,YY, S1, S2,S4, S5, J)
IF (K.EQ.O) GOTO 808
GOT0 (81,82,83), $R$
81 CALL NGFAFH (N,N1,MSUM,XX,YY,SC1,SC2,SC3,SEC4,J)
GOTO 808
82 CAL: NGKAAFH(N,N1,HSLM,ZZ,XX,SC1,SC2,SC3,SC4,J)
GOT: 808
83 CALL NGFAFH(N,N1,MSUM,YY,ZZ,SC1, SC2,SC3,SC4,J)
GOTO 808

```
14 CALL WRCEVS
    NG=NG+1
    GOTO 2
C 20OHING
9 CALL LMTSCL(SC1,SC2,SC3,SC4)
    CALL TXCUKS(XZ1,YZ1,ICHAR)
19 CALL TXCURS(XZ2,YZ2,ICHAF)
    IF(XZ1.EQ.XZ2.OR.YZ1.EQ.YZ2) GOTO 19
    CALL TXMOUE (XZ1,YZ1)
    CALL TXDF&W(XZ2,YZ1)
    CALL TXDFAAW(XZ2,YZ2)
    CALL TXDFAW(XZ1,YZ2)
    CALL TXDRAW(XZ.1,YZ1)
    CALL L.MTARA
119 CALL CONFFM(ICHAF)
    IF (ICHAR.EQ.78) GOTO 9
    IF(ICHAF.NE.89) GOTO 119
f CALL ZOOM ROUTINE
    XHIN=AMINI (XZ1,XZZ2)
    XMAX=AMAX1 (XZ1,XZ2)
    YKIN=AMIN1 (YZ1,YZ2)
    YMAX=AKAXX1 (YZ1;YZ2)
555 CALL FZOOM(R,HSUK,XMIN,YMIN,XMAX,YMAX,IC)
    GOTO(1,30,109,109,109,109,109),IC
109 IF(IC.EQ.3) IC=13
    IF(IC.EQ.4.OR.IC.EQ.6)STOF
    IF (IC.EQ.5)IC=15
    IF(IC.EQ.7)IC=17
    RETUFN
    END
C
C##***********ZOOMING INTO FARIAMETRIC CURUES*****************
C
    SUBROUTINE FZOOM(IF,MNFNT,XMIN,YMIN,XMAX,YMAX,IC)
C OUTFUT COHMON DATA AREA
    COMMON/CURUEF IT/XCOEF (50,4), YCOEF (50, 4) , 2COEF (50, 4) , XCOFD (200)
t
                , YCOFW (200) , ZCORD (200), TCORD (200)
    COMMON/IO/IN. IOUT
C MENU ITEMS
    DATA MNTXXT/" + NEXT + FREUIOUS+ METHDD + AX.MAKK + HELF*
t+ RESTART + EXIT */
    BIMENSION ZLINE (2,2)
    LOGICAL*1 HNTXT (70)
C SET UF THE DISFLAY
1 CALL TXCLEF
    CALL ALFFHMD
    WHITE (IOUT,10)
10 FORMAT("ZOOMING:-")
    CALL HNOFEN(875.,715.,1)
    CALLL MNDISF (HNTXT,7,10,1)
    CALL FFAME (870.,733.,7)
& SET UF WINOOW & UIEWFORT
    CALL LHTSCL (XMIN,YMIN,XMAX,YMAX)
    CALL FFRAME (XKIN,YMIN,XMAX,YMAX)
C DRAN THE ZOOMED CUKVE
    I=1
    G0T0(20,30,40),IR
20 ZLINE (1,1) =XCORU (I)
    ZLINE (1,2)=YCORD(I)
    ZLINE (2,1) ==XCOKD (I+1)
    ZLI YE (2,2)=YCOKN(I+1)
    GOT7 25
```

```
30 ZLINE (1,1)=2CGRO(I)
    ZLINE (1,2) == XCORD (I)
    ZL.INE (2,1)=ZCORD (I+1)
    ZLINE (2,2)=XCORD (I+1)
    GOTO 25
40 ZLINE (1,1)=YCOKD (I)
    ZLINE (1,2) = ZCORD (1)
    ZLINE (2,1)= YCORD (I+1)
    ZLINE (2,2)=ZCORB(I+1)
C CLIF THE FORTION OF THE CUKVE
25 CALL CLIF(ZLINE,XMIN,YMIN,XMAX,YMAX,IREJ)
    IF (IFEJ.EQ.O) GOTO 35
    CALL. TXMONE (ZLINE (1,1),ZLINE (1,2)}
    CALL TXUKAW(ZLINE (2,1),ZLINE (2,2))
    I=I+1
    IF(I.EQ.NFNT) GOTO 202
    GOTO 15
C SET LP CLKESOF
202 CALL LMTAFA
    CALL MNFICK(J.ICHAF:MNO)
17 CALL CONFFM(ICHAF')
    IF (ICHAR.EQ.78) GOTO 202
    IF (ICHAR.NE.89) GOTO 17
    G0TO(414,414,414,404,414,1,414);J
414 IC=J
    FETUKW
C AXES MAKKING
404 CALL AXSKFK (XHIN,YMIN,XMAX, YMAX)
    G0TO 202
    END
f
f ************** FLOTTING CURUE FIT ********************************
C
    FUNCTION CFLOT (R,XO,YO,XI,Y1,N)
C I/O COMMON DATA AREA
    COMMON/DATSUF/NFFS,NFI (50), IFREES,X(50),Y(50),Z(50),L(50),IH(5)
4 ,M(5),METHOD,IHELP,IFREV, BOUND (6),SUESET,INTFNT,IE (2)
t IID
    COMYON/CURUEFIT/XCUEF (50,4),YCOEF (50,4), 7COEF (50,4),XCORD (200),
1 YCORD(200),2CORD (200),TCORD (200)
    INTEGER SUBSET,R
    IP=1
    IFmi
    I=1
    GOTO(10,20,30),F
C PLOT SUFPLIED FOINTS
11 CALL FLLUSGN(XO,YO,XI,Y1,XCORD(I),YCBRD(I))
    CALL TXMOUE (XCORD(I), YCORD(I))
    GOTO 6
    CALL FLUSGN(XO,YO,XI,Y1,ZCOFD(I),XCOFD(I))
    CALL TXMOVE (ZCORD (I), XCORD (I) )
    GOTO 6
30 CALL FLUSGN(XO,YO,X1,Y1,YCORD(I), ZCORD(I))
    CALL TXMOUE (YCORD(I), ZCORW(I))
6 IF (I.EQ.N)FETURN
    IF'I= IF'+1
    IF2=IF'+NF'I(IF)+1.
    DO 1 J=IF1,IF:2
G BAW INTERFOLATED LINE SEGMENTS ACCORDING TO FROJECTION fLAAKE
                    GOTO(40,50,60),F
40 CALL TXURAW (XCORD (J);'VCORI)(J))
    GOTO 1
```

```
50 CALLL TXDFAW (ZCORD (J);XCORD(J))
        GOTO 1
        CALLL TXDFAW (YCORD(J), ZCOFD (J) )
60 CALLL T
        IF=IF2
        IF=IF+1
        I=I+NFI (IF-1)+1
        GOTO 3
        END
C
〔*************SAVE THE CUKVE ON FILE FOR LATER USE*********************
C
    SUEROUTINE CRUSAU(XX,YY,N,N1,MSLHM,SCL1,SCL2,SCL3,SCL4,J)
    GIMENSION XX(1),YY(1),NI (1)
    INTEGER FILE(3)
    N2=N-1
    IF (J.EQ.8) GOT0 88
G GET FILE NAME
    CALL CUKFOS(10.,730.)
    CALL MESSAG("FILE NAME"?"*)
    CALL GETFLN(FILE )
    FEWIND }
& OPEN OUTFUT FILE
    CALL SETFIL(9,FILE)
88 WRITE (9,20) KSUM,N
    WRITE (9,30) (XX (I),YY(I),I=1, MSUM)
    WRITE (9,25) (N1 (I),I=1,N2)
    WRITE (9,35) SCL1,SCL2,SCL.3,SCL4
25 FOFMAT (13)
30 FORHAT (F11.4)
35 FORMAT (4F11.4)
    ENDFILE }
    RETURN
    ENI
6
C****************INFUTT FILE I\ANE****************************
C
    SUBEDUTINE GETFLN(NAME)
    COMMION/IO/IN, IOUT
    INTEGER MAME (3)
    READ (IN,10) NAME
10 FOKHAT (2A4%A2)
    RETUFN
    ENB
f
〔#######*******SUOERIMFOSE OFTTION "NGRAF'H"**********************
C
    SUBROUTINE NGFAFH(N,H1,MSUM,XX,YY,SCLI,SCL2,SCL3,SCL4,N)
    COMMOM/CURVES/NCEV(10), XYSCL.(4)
C DATA FILE NAMES FOR SUFERIMFOSED CURUES
    DATA SUF'FLS/"CURVE1 CUFVE2 CURVE3 CUFVE4 CURVES
&CURVEG CUKVET CURVES CURVE9 CURVEIO */
    LOGICAL*1 SUF'FLS(100)
    K=0
C FIND FREE ENTKY
    BO 1 I=1.10
        IF(NCEV(I).NE:99) GOTO 2
        K=K+9
1 CONTINUE
2 NCEV (I)=99
    K=K+I
```


## FEWIND 9

© OPEN OUTFUT FILE FOR SAUING CUFVES
CALL SETFIL (9, SUFFLS (K) )
CALL CRUSAV (XX,YY,N,M1,MSUM,SCL1,SCL2,SCL3,SCL4, J)
c FIRST CURUE
IF (NCENU (1).EQ.99) GOTO 3
XYECL (1) $=$ SCL 1
$X Y S C L(2)=S C L 2$
XYSCL ( 3 ) $=$ SCL 3
$X Y S C L(4)=S C L .4$
GOTO 4
© SUBSERUENT CUFVES
© SET THE IISFLAY SCALES
3 IF (XYSCL (1).GT.SCL 1 ) XYSCL (1) =SCL 1
IF (XYSCL (2).GT. SCL 2) XYSCL (2) =SCL2
IF (XYSCL (3).LT.SCL 3 ) XYSCL (3) $=$ SCL 3
IF (XYSCL (4) .LT.SCL.4) XYSCL (4) $=$ SCL. 4
4 CALL ETEXT (725., 555., " 4 GRAFH", 7)
ENDFILE 9
RETURN
END
c
〔 **********SAVE THE DATA ON A FILE****************
C
SUBROUTINE RDCERUS
COKMON/CURUES/NCRU (10), XYSCL (4)
FEWIND 7
CALL SETFIL (7,"SUFCEVES")
$\operatorname{READ}(7,10)$ (NCRU (I) $\mathrm{I}=1,10$ )
$\operatorname{FEAD}(7,20)$ (XYSCL ( 1 ) $, \mathrm{I}=1,4$ )
10 FORHAT (I2)
20 FOFMAT (F11.4)
RETURN
ENB
c

C
SUBFOUTINE REDFAA (XX,YY,N,N1,MSUK,SCL1,SCL2,SCL3,SCL4)
COMMON/IO/IN. IOUT
DIKENSION XX(1),YY(1),N1(1)
INTEGER FILE (3), F
C INPUT FILE NAME
CALL MESSAG("
FILE NAME? ? ${ }^{\sim \prime}$
CALL GETFLK (FILE)
REWIND 9
c OPEM INFUT FILE
CALL SETFIL (9,FILE)
READ $(9,25)$ KSUM, ${ }^{2}$
$\mathrm{N} 2=\mathrm{N}-1$
$\operatorname{READ}(9,30)(X X(I), Y Y(1), I=1, M S U M)$
$\operatorname{READ}(9,20)(N 1(1), I=1, N 2)$
FEAD (9,35) SCL 1, SCL2, SCL. $3, \mathrm{SCL} 4$
20 FORMAT (I3)
25 FORKAT (213)
30 FOKMAT (F11.4)
35 FOKMAT (4F11.4)
C SET UFF WINDOW SCALE
CALL LHTSCL (SCL1,SCL2,SCL3,SCL4)
$\mathrm{F}=1$
c. flot the curve

CALL CFELOT (K,SCL1,SCL2,SCL. $3, S C L .4$, MSUM)
ENDF ILE 9

RETUKN
ENJ
6
〔 ****** SAUE SUF'EFIMF'USE COMMON DATA AREA ***************
C
SUBROUTINE WRCENS
COMMON/CURUES/NCRV (10), XYSCL (4)
REWIND 7
C OFEN QUTFUT FILE
CALL SETFIL (7,"SUFCENES")
WFITE (7,10) (NCRU(I),I=1,10)
WRITE ( 7,20 ) (XYECL (I) , $I=1,4$ )
FORMAT (I2)
10
FOFMAT (Fi1.4)
ENHFILE 7
RETURN
END

```
C
C
C
C C THIS MODLLE HANDLES THE CURUE DESIGN IMTERACTIVE DISFLAY.
C.
C
C
```



```
C
C I/O COMION DATA AEEA
COMMON/DATSUF/NFS,NFI (50), IFREES,X(50),Y(50),Z(50) \& L(50), IH (5) , M (5) , METHOD , IHELF' IF'REU, BOUND (6), SUBSET , INTFNT, IE (2) IID
COMMON/CURUEFIT/XCOEF \((50,4), Y C O E F(50,4), 2 C D E F(50,4)\)
\(, X C O R D(200), Y C O R D(200), 2 C O R D(200), \operatorname{TCOKD}(200)\)
COMMON/LO/IN, IOUT
C OUEFLAY EXECUTABLE FFOGRAM NAME
DATA FHODL2,FHODL4,FHELF / "FHODL2", "FHODL.4" "HELFF"
DIMENSION XO(50), YO(50), ZO(50), TO (50)
LOGICAL* 1 FHODL2(10) if'HOLL \(4(10)\), FHELF (10)
INTEGER SUESET
CALL TXOFEN
C READ I/O FILES FOK THE COMMON DATA AREA
11 CALL FROCM1
\(3 \quad \mathrm{NC}=4\)
21 IN=5
IOUT \(=6\)
CALL FRWCH2 (NFS, MFII:NC,ID)
CALL FRML.NK (XO,YO,ZO)
C THE CUKVE IS dISPLAYED WITH DEFAULT SETTING
INTFNT=0
CALL GENFRT (NFS,XO,YO,ZO,TO,ID,METHOD)
CALL SETLNK (NF'STNFI, INTFNT)
C BESIGN CUKVE WITH CURSOK
CALL CUKDES (NF'S,NFI, XO,YO,TO, XCORBFYCORD, TCURD, INTFNT, METHOD -XCOEF Y YCOEF, IC
GOTO (4,5,6,6,6,6;6,6,6,9,11, 日), IC
6 STOF
4 IFREV=0
IHEL.P=0
INTPNT=0
CALL FWKCH1
CALL SWFCOM (NF'S,NFI INC,XO,YO)
CALL OURLAY (FYODLL 4)
C PREUIOUS IISFLAY
5 IFREV \(=1\)
IHELF: \(=0\)
CALL FWKEMI
CALL OURLAY (F'MODL2)
C PROGRIAK TEFMINATION
8 CALL PEXIT
STOF
C HELF DISFLAY
9 CALL FWKCH1
CALL SWFCOM (łIF'S,NFIINC,XO,YO)
CALL QURLAY (FHELF')
END
```

〔**********CURSOK UESIGN IISFLLAY********************
C

C LINK LIST COMMON/LNKLST/L.INK (200), INTVAL (50), IFFEEE, IFCNT COMMOH/LO/IH, IOUT
C HENU ITEMS
HATA MNTXT/* + NEXT + FREVIOUS + DLSF. OFG + GFAFH + COOFDS.
4* ADU FNT* + DEL INTU + REFFESH + AX MAKK+ HELFF + FESTAFT + EXIT * / DIMENSION $N(1), X O(1), Y O(1), T O(1), X X(1), Y Y(1), T T(1), X C(50,4)$,
$t$ YC (50,4)
LOGICAL*1 HNTXT (120)
EXTEFNNAL XFLLOT
CALLL SUM ( $N, N 1$, MSUM)
CALL HINMAX ( $51,52,53,54, X X, Y Y, M S U M)$
S1=S1-(S3-51)/20
S2 $=$ S2- (S4-52)/20 IZERO=1
11 IF (IZERO.EQ.0) INTFNT $=999$
INTUNO $=1$
© SET UF THE DISPLAY
CALL TXCLER
ICORD=0
WKITE (IOUT, 10)
10 FOFKHT ("CURUE UESIGN:-")
C OUTFUT MENU ITEMS
CALL MNOFEN(875.,715.,1)
CALL KNJISF (KNTXT,12,10,1)
CALL FRAME (870.,733.,1.2)
C USER KEYBOAKD COMMAND
CALL DTEXT (828.,447.,** TYFE CAFT.: ",13)
CALL DU̇EXT (828.,428.,"E-JOIN INTU.",123
CALL BTEXT (828.,406.,"F-FINISH INTU",13)
CALL DTEXT (828.,384.,"N-NEXT INTV.", 12)
CALL ETEXT (20.,30.,"\$ USE IMTERVAL SEOUENCE MAKKEE BY 3 " ", 37)
2 CALLL LMTARA
C CHECK FOR FEFFESH COMMAND
IF (J.EQ.B) GOTO 34
C CURSOR MENU PICKING
CALL HNFICK (J. ICHAFi r MrlO)
IF (J.EQ.S.AND. ICORD.EQ. 2) GOTO 2
11 CALL CONFRM (ICHAF)
IF (ICHAR.EQ.78) GOTO 12
IF (ICHAF.NE.89) GOTO 17
GOTO $(41,41,33,34,35,36,36,11,110,41,66,41), J$
$12 \quad J=0$
GOTO 2
41 IC $=\mathrm{J}$
RETURN
C DISFLAY OREGIH
33 CALL DISOKG (51,52,53,54)
GOTO 2
© PLOT THE GRAFH
34 CALL. DFAW (XPLOT,F,S1,52,53,S4,MSUM)
$J=0$
GOTO 2
C AXES HAFKING
110 CALL AXSMKK (S1,52,53,S4)
G0T02
C CURSOK INFUT COOKUINATES -
35 CALL BISCOR (ICORW.S1,52,53.54)
GOTO 2

```
C ADD INTERMEDIATE FOINTS INTEFACTIVELLY USING THE CUFSOR
36 CALL LMTSCL (S1,S2,53,54)
22 CALL TXCUFS(CX,CY,ICHAF)
    IF(ICHAR.EQ.70) GOTO 2
C MOVE TO NEXT INTEFVAL
        IF (ICHAK.EQ.78) gOTO EB
        IF (J.EQ.7) GOTO 37
        IF (INTFNT .EQ.999.AND.IZEKO.EQ.1)GOTO 66
61 INTFNT=0
    CALL ADDFNT (N,N1,XO,YO,TO,XX,YY,TT,INTUNO,IA,CX,CY,ICHAF,XC,YC)
    GBTO 22
    N2=N-1
    LO 16 I=1,N2
        INTVAL (I) =0
    N1 (L)=0
    IF(J.EQ.11) GOTO 41
    IZERD=0
    GOTO 61
C HAF*K DELETED INTEFVAL
37 CALL DTEXT (CX,CY,"D*,1)
    CALL DELINT (INTUNO,N,NI)
    GOTO 22
88 INTUNO=INTUNO+1
    CALL DTEXT (XO(INTUNO); YO(INTUND);"$",1)
    GOTO 22
    END
f
6#####******GENERATE F'ARAMETERSTTH******************
C
    SUBFOUTINE GENFRT(N,X1,Y1,Z1,T1,IDIM,M)
    DIMENSION X1(1),Y1(1),Z1(1),T1(1)
    T1(1)=0.
G GENERATE T PARAMETER FOR COMFUTING THE INTERFOL.ATED FOINTS
    DO i K=2,N
        U=X1 (K)-XI (K-i)
        V=Y1 (K)-Y1 (K-1)
        IF(IDIM.EQ.3) Q=Z1(N)-71(N-1)
        |=\#U+V*V
        IF (IDIM.EQ.3) D=D+Q*Q
        D1=SQRT (D)
        IF(M.EQ.3.OR.M.EQ.4) GOTO 2
        T1(K)=T1(K-1)+D1
        CONT INUE.
        RETUKN
        T1 (K) = =01
        GOTO 1
        END
C
C **************ADID INTERM隹UITE FOINT ******************************************
C
    SUBROUTINE ADEFNT (N,N1, XO,YO,TO,XX,YY,TT,INTUNO,IA,CX,CY,ICHAR,
l
                                    XC,YC)
C COMmON DATA LINK LIST
    COMMON/LNKLST/LINKK(200), INTVAL. (50), IFFEE, IFCNT
    IIMENSION N1 (1),XO(1),YO(1),TO(1),XX(1),YY(1),IT(1),XC(50,M)
                                    , YC(50,4)
t
C CHECK FIFST TIME IN THE INTEFUAL.
    IF (INTVAL (INTVHO).NE.O) GOTO 2
C ENTER THE STAFT FOIMT AND THE IMTERMEDIATE FOINT
    INVVAL (INTUNO) = IFFEE:
    XX [FFFEE)=XO(INTUNO)
    YTOFREE):=YO(IMTUNO)
```

```
C CHECK ENID OF IMTEEVAL
    IF (ICHAK.EQ.69) GOT0 7
    IF (IFCNT.GT. 1) GOTO 11
    LINK (IFFEE )= IFKEE +1
    CALL. TXMOUE(XX(IFREE) YY(IFREE))
    IFFEE=LINKK(IFFEE)
5 LINK (IFFEE) =0
C COHFUTE THE IMTEFFLOATED FOINTS FFOM THE CURSOR FOSITOHING
6 CALL CXXYY(N,XO,YO,TO,XX,YY,TT,INTUNO,IA,CX,CY,XC,YC,IFFEE,IERC)
    IF (IEFK.EQ.1) GOTO 66
    #1 (INTUNO) =N1 (INTUNO) +1
    IFKEE=1FFEEE+1
    FETUEN
C COMF'ARE THE CURNENT CX WITH THE GLERADY IN THE TAELE
2 IF (ICHAR.EQ.69) GOTO 1
    NEXT=:IMTVAL (INTUNO)
C CHECK FOF FUNIING BACK CUFVE
    IIXX=:=XX (NEXT) -XX (LINK (NEXT))
    IF (DXX.GT.O.) GOTO 888
    EXO:=XO (INTUNO)-XO (INTUNO+1)
    IF (JXO.GE.O.) GOTO 818
U ICX=CX-XX (NEXT)
    IF (ICX.LT.O.) GOTO 3
    K=NEXT
    NEXT=L_INK゙ (NEXT)
    IF (NEXT.EQ.O) GOTO 41
    goTO }
41 L.INK(K)=IFREE
    CALL TXMDUE (XX(K),YY(K))
    IF(IFCNT.GT.O) GOTO 12
    GOTO 5
C ADD FOINT IN THE INTEEVAL WHICH HAS GREATEF VALUE FOINT
3 IF (IFCNT.GT.O)GOTO 16
    LINK (K)=IFFEEE
    LINK\(IFFEES =NEXT
    CALL TXMOUE (XX (K),YY(K))
    gOTO 6
C ADDITION INTO FREVIOUSLY DELETED ITEM (CARBIGE COLIECTION)
11 IFCNT=IFCNT-1
    CALL TXMOUE (XX(IFFEE) YY(IFFEE))
    K=LINK (LINKK(IFFEE))
    LINK(LINK(IFFEE))=0
    IFREE=LINK(IFFEE)
    CALL CXXYY(H,XO,YO,TO,XX,YY,TT,IMTUNG,IA,CX,CY,XC,YC,IFKEE,IERC)
    IF (IERC.EQ.i) GOTO be
    IFREE=:K
14 IFCNT=IFCNT-1
    NI (INTUNO) =NI (INTUNOS +1
    RETUFN
12 CALL CXXYY(N,XO,YO,TO,XX,YY,TT,INTUNO,IA,CX,CY,XC,YC,IFFEE,IEFC)
    IF (IERC.EQ.1) GOTO 66
    N=IFKEE
    IFREEELIINK(IFREE)
    LINKE (K)=0
    gOTO }1
16 CALL TXMOUE (XX (K),YY (K))
    CALL CXXYY(N,XO,YO,TO,XX,YY,TT,INTVMO,IA,CX,CY,XC,YC,IFREE, IEFC)
    IF (IEKC.EQ.1) GOTO t\epsilon
    K1=LITK(IFFEE)
    L.INKK (K)=1FREE
    LINK (IFFEE) =NEXXT
    IFREE=K1.
```

goto 14
C END DF INTEFVAL WITH DNE OR MANY ENTERIES
C FIHB THE LAST ENTRY IN THIS INTERUAL（L．INK＝O）
1 NEXT $=$ INTVAL（INTVNO）
J＝N1（INTVNO）＋ 1
009 L：i．j」
IF＝NEXT
NEXT＝LINK（NEXT）
IF（NEXT．EQ．O）GOT010
9 CONTINUE
10 CALL TXMOUE（XX（IF）IYY（IF））
8 CALL TXUFAW（XO（INTUAO＋1）YO（IRTUNO＋1））
RETUKN
C HO INTERMEXITE FOINTS
LINK（IFREE）$=0$
IFREE＝IFREE＋1
CALL TXYOUE（XO（INTUNO）YO（INTUNO））
GOTO 8
66 IEFT $=0$
RETUKN
〔 RUNING BACK CURUE ．．．．．CHECK FOR FOINT FALL IN BETWEEN TWO
C EXISTING FOINTS OR LOOF ON IT SELF
868 DCX $=$ CX $-X X$（NEXT）
IF（DCX．GT．0．）GOTO BOB
118 K＝NEXT
NEXT $=\mathrm{L}$ LI KK （NEXT）
IF（NEXT．EQ．O．AND．IFLAG．EQ．1）GOTO 333
IF（NEXT．EQ．O）GOTO 41
GOTO 888
333 IFLAG＝0
goto 3
C．CHECK IF FOINT STILL FALL IN OFPOSITE THE SUB INTERVAL
808 IF（IFLAG．EQ．1）GOTO 818
828 DXO：XO（INTUNO＋1）－XO（INTUNO）
IF（DXO．LE．O．）GOTO 3
DY $1=A B S$（YO（INTUNO）－CY）
DY2＝ABS（YO（INTUNO＋1）－CY）
DYY＝DY1－DY2
IF（DYY．LT．O）GOTO 3
IF（DYY．EQ．O．）FETUFN
C NOT THE FIRST FQUND SUB INTVAL
IFLAG： 1
GOTO 818
END
C
〔＊＊＊＊＊＊＊＊＊＊＊COMFUTE INTERFROLATED FOINT＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊＊
C
SUBFOUTIME CXXYY（ $N, X O, Y O, T O, X X, Y Y, T T, I N T U N O, I A, E X, C Y, X C, Y C, I F R E E, I E R C$ ）
DIHENSION XO（1），YO（1），TO（1），XX（1），YY（1），TT（1），XC（50，4），YC（50，4）
C DETERMINE FAKAMETER T FROK CXICY
I＝INTUND
$B X=C X-X O$（I）
DY＝EY－YO（I）
$D D=D X * D X+D Y * D Y$
T1＝SQKT（DD）
IF（IA．GT．2）GOTD 1
$T=T O(1)+T 1$
1
$T=T 1$
IF（T．GT．TO（I＋1））GOTO 3
$X X(I F F E E)=X C(I, 1)+T *\left(X C(I, 2)+T_{*}^{*}(X C(1,3)+T * X C(I, 4))\right)$
$Y Y(I F F E E)=Y C(1,1)+T *(Y C(1,2)+T *(Y C(1,3)+T * Y C(1,4)))$
$T T(I F F E E)=T$

```
    CALL TXURAW(XX(IFREE) YY(IFREE))
        FETURN
        IERC=1
        RETUKN
        END
C
C ##***************BELETE GN INTERUAL ****************:***************
G
    SUBFOUTINE DELINT (INTUNO,N,NI)
    COMMON/LNKLST/LINK (200), INTVAL (50), IFREE, IFCNT
    DIHENSION N1 (1)
C EMFTY LIST?
    IF (INTVAL (INTUNO).EQ.O) FETUFN
3 IF(IFCNT.HE.O)GOTO 1
C FIRST DELETION
    NEXT=INTVAL (INTUNO)
    K=NEXT
    IF (LINK (NEXT) .EQ.O)GOTO 5
    N2=N1 (INTVNO)
    K=1ZFLLAK (N2,LINK,NEXT)
5 LINK(K)=1FREE
    IFREE= INTUAL (INTUNO)
    IFCNT=IFCNT+N1 (INTVNO) +1
    INTVAL (INTUNO) =0'
    N1 (INTVNO) =0
    FETUKN
C HELETE OF MORE INTREVAL
1 NEXT1=INTVAL (INTVNO)
    K1=NEXT1
    IF (LINK (NEXT1).EQ.O) GOTO 6
    N2=N1 (INTUNO)
    K1=1ZFLNKK(N2,LINK,KI)
6 NEXT2=IFREE
    K2=NEXT2
    N2=IFCNT-1
    IF (N2.EQ.0) GOTO7
    K2=1ZFLNK(N2,LINK,K2)
7 K3=LINK (K2)
    LINK (K2) =NEXT1
    L.INK(K1)=#K3
    GOTO 2
    END
f
C ************FIND END OF THE INTREVAL FOR DELETION*********************
&
    FUNCTION IZRLNK (N,LKK,NXT)
    DIMENSION LK(1)
    DO 1 I=1,N
1 NXT=LK (HXT)
    IZFL.NK=NXT
    FETURN
    END
C
C****************SET DATA STRILCTURE LINKS*******************
C
    SUBROUTINE SETLNK (N,NI,INTFNT)
    COMMON/LNKLST/LINK (200), INTVAL (50), IFREE, IFCNT
    DIMENSION N1 (1)
    IF (INTF'NT.EQ.999)G0T0 9
    INTVAL (1)=1
    N2=N-1
    DO 1 I=2,N
```

    INTVAI_(I) \(=\) INTVAL \((I-1)+N 1(I-1)+1\)
        \(K=1\)
        以 \(2 \mathrm{I}=1 \mathrm{~N}\) 2
        IF (NI (I).NE.O) GOTO 4
        LINK (K) =0
        k゙=k゙+1
        GOTO 2
    $4 \quad$ N1 $1=\mathrm{N} 1(\mathrm{I})+K-1$
C SET LINK LIST
100 3 J=K,N11
L.INK $(J)=J+1$
L.INK (J) $=0$
K=心1
CONTINUE
CALL SUM (N,N1,MSUM)
IFREE =MSUAT +1
GOTO 10
9 IFREE=1
IFCNT $=0$
10 RETUKN
END
C
C********OUTFUT THE DESIGRED CURVE $2 * * * * * * * * * * * * * * *$
$C$
C 4 ****A SIMF'LE LIST******
SUBFOUTINE SWFCOM ( $N, N 1, N C, X O, Y O$ )
C DUTFUT COMMON DATA AFEA
COMMON/CUKVEF IT/XCOEF $(50,4), \operatorname{YCOEF}(50,4), 2 C O E F(50,4)$
4. $\quad$ XCORD (200), YCORD (200), ZCORD (200), TCORD (200)
C LINK LIST USED IN THE DESIGNED FROCESS
COMMON/LNKLST/LINK (200), INTVAL (50)
DIMENSION N1 (1), XO(1),YO(1)
FEWIND 8
C OFEN OUTFUT FILE
CALL SETFIL (B,"FOUTFITC")
$N 2=N-1$
WRITE ( 8,20 ) ( $(\operatorname{XCOEF}(I, J), Y \operatorname{COEF}(I, J), J=1, N C), I=1, N 2)$
DO $1 \mathrm{I}=1, \mathrm{~N} 2$
NEXT=INTVAL (I)
$\mathrm{N} 3=\mathrm{NI}(\mathrm{I})+1$
HO $2 J=1, N 3$
WKITE ( 8,10 ) XCOKD (NEXT) , YCORD (NEXT) , TCORD (NEXT)
NEXT=LINK (NEXT)
CONTINLE
2
1
CONT INUE
WFITE (8,10)XO (t1), YO (N) , TCORD (NEXT + 1)
10 FOKMAT (F12.4)
20 FOFMAT (F12.4)
ENDFILE 8
RETUKN
END
$c$
C**********FILOT THE DESIGNED CURVE******************
C
SUBFDUTINE XFLOT (F',SCL1,SCL2,SCL3,SCL千TNSUM)
C I/O COMMON IIATA GREA
COMMON/DATSUF/NFS, HFFI (50), IFFEES,X(50),Y(50),Z (50),L(50), IH(5)
, $\mathrm{K}(5)$, ME THOD , IHELF, IFFEEV, BUUNL ( 6 ), SUESET (2) , IMTFNT, IE (2)
4
, 15
COMMON/ CURVEF IT/XCOEF $(50,4), Y \operatorname{COEF}(50,4), 2 \operatorname{COEF}(50,4)$
4
C LINK LIST

```
    COMMON/LNKLST/LLYKK(200), INTVAL (50), IFREE, IFCNT
    IMTEGEF SUBSET
    DIMENSION XO(50),YO(50),ZO(50)
    CALL F'KMLNK (XO,YO,ZO)
    N2=NF'S-1
    CALL DTEXT(XO(1),YO(1),"$",1)
    pO 1 I=1,N2
        NEXT=INTVAL (I)
        IF (NEXT.NE.0)GOTO 4
        K=I
        GOTO 11
    CALL. FLUSGN(SCL1,SCL2,SCL.3,SCL4,XCOKU (NEXT), YCORD (NEXT))
    CALL TXMOVE (XCORD (NEXT) Y YCORD (NEXT))
    N11=NFI (I)
    IF (N11.NE.0)GOTO 3
    K=INTVAL (I+1)
    IF(K.NE.O) GOTO 6
    IF (NEXT.NE.0) GOTO7
    K=I+1
    GOTO 11
    CALL TXDRAW(XCORD (K) YCOKD (K))
    BOTO :
    DO 2 J=1%N11
        NEXTmLINK (NEXT)
        CALL TXDRAH (XCORD (NEXT) , YCORU (NEXT))
    COHTTINUE
    K=I+1
    CALL TXDKAW(XO(K),YO(K))
    CALL FLUSGN (SCL1,SCL2,SCL.3,SCL4,XO(K),YO(K))
    CALL TXMOUE (XO(K), YO(K))
    CONTINUE
    CALL FLLUSGN(SCL1;SCL2,SCL3,SCL4;XO(I);YO(I))
    RETUFN
    END
    C ********* FIND TOTAL NUMEER OF INTEFFOLATED FUINTS*X***********
    SUEROUTINE SUM(N,N1,MSUM)
    DIMENSION N1(1)
    MSUM=0
    N2=N-1
    DO 1 I=1,N2
1 MSUHM=MSUMH+N1 (I)
    MSUMIMMSUMTN
    FETURN
    ENH
```

C THIS MONULE HANELES THE FQLLOWING INTERACTIVE UISFLAYS:-
C 1.TABLE OF THE INTEFFOLATED FOINTS
C 2.TABLE OF THE FOLYNOMIAL CUEFFICIENTS
C
C
C
C
C ****** MAIN F'ROGFAM - MODLLE $5 * * * * * * * * * * * * * *$
C
C
C I/O COMMON DATA AFEA
COMMON/UATSUF/AF'S,NFI (50), IFFEES, $X(50), Y(50), Z(50), L(50), I H(5)$
, M(5) , METHOD, IHELF , IF'REV, BOUND (6) , SUBSET, INTFNT, IE (2)
,ID
COMMON/CUKVEFIT/XCOEF $(50,4), Y \operatorname{COEF}(50,4), 2 \operatorname{COEF}(50,4), X \operatorname{COFD}(200)$
, YCORD (200) , 2CORD (200), TCORD (200)
COMMON/ID/IN. IOUT
C OVERLAY EXECUTABLE FROGGAM MAMES

\&"F'AKAMETKIC" " HELF" $/$
LOGICAL*1 FHOLLS (10), FHORL4(10), FMOULI (20), FHELF (10)
INTEGER SUBSET
CALL TXOFEN
C READ I/O DATA FILE
11 CALL FRDCMI
$3 \quad$ NC: $=4$
21 IN=5
IOUT $=6$
CALL FRDCH2 (NPS, NFPI,HC,IB)
IF (IHELP.NE.O)GOTO 66
GOTO (33:34), IF'REN
c disflay Imrenfolated foint as table
33 CALL TABINT (NFS, NFI, XCORD, YCORD, ZCORD, TCORW, LOUT, IC, ILD)
$6 \operatorname{GOTD}(51,52,59,54,59,59,57,33,58)$, IC
C PEXT DISF'LAY
51 IFREV=0
IHELF $=0$
CALL FWRCML
CALL EURLAY (FHOLL 4)
C PREVIOUS DISFLAY
52 IFREV=1
IHELF' $=0$
CALLI FWFCMI
CALL OUKiLAY (FHODL2)
C Disflay taEle of the coefficients
54 CALL TABCOF (NFS, XCOEF, YCOEF, ZCOEF, METHOD, IUUT,IC,ID)
GOTO ( $51,33,59,59,59,59,59,59,57,54,56$ ), IC
C SUFERIMFOSED CURVES
34 CALL SUFIMF (NFS,NFI, XCORD, YCORD,IC)
GOT0 ( $51,52,59,59,59,59,61,59,57,59,58)$, IC
C HELF JISFLAY
57 CALL FWKCMI
CALI OUFLGAY(FHELF)
C ALGOKITHM DISFLAY
61 IF'REV $=0$
IHELF $=0$
CALL FWFCMI

CALL OVFKLAY (FMOILLI)
C FROGRAM TEFMIMATION
58 CALL FEXIT
59 STOF
C FETURN FROM HELF'
66 GOTO ( 33,34 ), IHELF END
C

C
SUBFOUTIME TABINT (N,NI,XX,YY,ZZ,TT,IUEU,IC,IDIK)
DIHENSION N1 (1), XX(1),YY(1\},ZZ(1),TT(1),IF(8)
11 CALL OUTTIL(1,9,IDEV,ICOEF)
C FIND THE TAELE SIZE
CALL SUM (N,N1,MSLM)
IF (HSUM.GT. 25) GOTO 1
C TABLE SIZE ONE OR LESS THANA A F'GGE
IROLL $=0$
CALL OUTFGE (MSUKi, $1, X X, Y Y, Z Z, T T, I U E V, I D I M)$
GOTO 12
C TABLE SIZE MORE THAN ONE FAGE
$1 \quad$ IF $(1)=1$
IFOLL $=1$
DO $21=2,8$
$2 \quad I F(I)=I F(I-1)+25$
IS=1
C FINB NUMBER OF FAGES \& THE REMAIMUEF
HREM= LEEM (KSUMr 25)
NF'AGE $=$ (HSUKT-KKEM) $/ 25$
14 ITWNFIF $=25$
15 IFNTR=IF(IS)
CALL OUTFGE (ITWNFIF,IFNTK,XX,YY,ZZ,TT,IDEV,IDIM)
WRITE (IDEV,20)
20 FGRMAT (/**'TO DISFlLAY THE NEXT/FREVIOUS FAGE OF THE TABLE*/

* "USE THE FOEWARD/EACKWARD AS \&FFFROFRIATE" ")

C SET UF CURSOR FOR USER SELECTIDN
12 CALL MNFICK (J,ICHAF, YNO)
17 CALL CONFEK (ICHAK)
IF (ICHAK.EO.78) GOTO 12
IF (ICHAR.NE.89) GOTO 17
GOTO (21,21,23,21,25,26,21,11,21), J
\& BACK TO THE MAIN FROGFAM TO FROCESS OTHER COMMAND
21 IC:J
RETUKN
C HARDCOF'Y
23 REWIND 7
CALL. SETFIL. (7,"/DEV/TTYM")
WRITE $(7,30)$
30 FOFMKAT ("COMFLETE TAELE OF THE INTEFFOLATED FOINTS:--")
ITWNF IF =MSUM
IFNTF=IF' (1)
CALL OUTFGE (ITWNFIF,IFNTTK,XX,YY,ZZ,TT, 7, IDIM)
GOTO 12
€ 10 KOLL THE TABLE (FORWAKD)
25 IF (IFOLL.EQ.O) GOTO 12
IF (IS.EQ. NFAGE. AND. MFEM.GT.O)GOTO 31
IF (IS.EQ.NF'AGE.OR.IS.GT. HF'AGE)GOTO 12
IS $=15+1$.
CALL OUTTIL(1,9,IDEV,ICOEF)
GOTO 14
C OUTFUT THE FEMAINDEE
31 ITWNF IF =MFE.M

```
    15:=15+1
    CALL OUTTIL(1,9,IDEV,ICOEF)
    GOTO 1S
C BACKWAFD
26 IF(INOLL .EQ.O) GOTO 12
    IF(IS.EQ.1) GOTO 12
    IS=IS-1
    CALL OUTTIL(1,9,IDEU,ICOEF)
    GOTO 14
    END
C
〔**************** TABULLATE COEFFICIENTS****************************
G
    SUBROUTINE TABCOF (N,XC,YC,ZC,METHOD,IDEV,IC,IDIK)
    DIMENSION XC (50,4) ,YC (50,4),ZC(50,4),IF(4)
    ICOEF=1
C OUFUT TABLE TITLES
11. CALL OUTTIL(2,11,IUEU,ICOEF)
    NC=N-1
    IF (NC.GT.20) GOTO 1
C LESS THAN 2O,ONE FAGE OF TABLE
    IFOLL=0
    IF (ICOEF.EQ. 1)CALL OUTCOF (NC, 1,METHOD,XC,IDEV)
    IF (ICOEF.EQ.2)CALL OUTCOF (NC, 1,METHOD,YC,IDEU)
    IF (ICOEF, EQ.3)CALL OUTCOF (NC, I, METHOD,ZC,IDEV)
    GOTO 2
C GREATER THAN 2O ,MORE THAN ONE F'AGE
1 IFOLL=1
    If(1)=1
    DO 7 I=2,4
7 IF'(I)=IF'(I-1)+20
    IS=1
C FIND NUBEK OF FAGES AND THE REMAINDER
    NKEM=IREM (NC, 2O)
    NCFGE= (NC-NFEM)/20
14 N3=20
15 IFNTR=IF(IS)
12 IF(ICOEF.EQ.1)CALL OUTCOF (N3,IF'NTR.METHOD,XC,IDEU)
    IF (ICOEF.EQ.2)CALL CUTCDF (N3,IFNTR,METHOD,YC,IDEU)
    IF (ICOEF.EQ.3)CALL DUTCOF (N3,IFNTR,METHOD,ZC,IDEV)
    WFITE (IDEV,20)
20 FORMAT (/***TO EISFLLAY THE NEXT/FREUIOUS FAGE OF THE TABLE*/'
C RAISE CURSOF
2 CALL MNFICK(J,ICHAF,MNNO)
17 CALL CONFRM(ICHAR)
    IF(ICHAR.EQ.78) GOTO 2
    IF (ICHAR.NE.89) GOTD 17
    GOTO(21,21,32,33,34,23,24,25,21,11,21):J
    ICOEF=1
    G010 11
    ICOEF=2
    G0T0 11
    IF (IDIM.EQ.2) GOTO 2
    ICOEF=3
    GOTO 11
C OTHEK COMMAND
21 IC=J
    RETUKN
6 HARJCOFY
23 SEWIND 7
    CALL SETFIL(7,*/DEV/TTYM")
```

```
7 7
88 FORMAT (/"FAFAMETKIC COEFFICIENTS OF Y:-*)
    CALL OUTCOF (HC, I,METHOD,YC,7)
    IF(IDIM.EQ.2) GOTO 2
    WKITE(7,99)
99 FORMAT (/"FAKAMETRIC CDEFFICIENTS OF Z:-*)
    CALL DUTCOF (NC,I,METHUL, ZE,7)
    GOTO 2
C FORWAKD COMMAND(TABLE ROLLING)
24 IF(IKOLL.EQ.O)GOTO 2
    IF (IS.EQ.NCFGE.AND.NKEH.GT.O) GOTO 31
    IF(IS.EQ.NCFGE.OR.IS.GT.NCFGE) GOTO 2
    IS=15+1
    CALL OUTTIL(2,11,IDEV,ICOEF)
    GOTO14
31 N3=NREM
    IS=IS+1
    CALL OUTTIL(2,11,IDEV,ICOEF)
    GOTO }1
C BACKWARD COMMAND
25 IF(IFOLL.EQ.O) GOTO 2
    IF(IS.EA.1) GOTO 2
    IS=15-1
    CALL OUTTIL (2,11,IUEV,ICOEF)
    GOTO }1
    END
C
C###*******SUFEFIMFOSED CURUE DISFLAY******************
C
    SUBFOUUTINE SUFIMF'(N,NI,XX,YY,IC)
    COMMON/CURUES/NCRU(10),XYSCL (4)
    COHMON/IO/IN:IOUT
C HENL ITEMS
    DATA MNTXT/" + NEXT + FREVIOUS+ GRAF'H + DISF.OKG+ GELETE*
4+ REFRESH + METHOD + AX. HARK + HELFF + RESTART + EXIT %
    DATA SUFFLS/"CLKVE1 CLFIVE2 CURVE3 CURVE4 CURVES
&CURVEG CUFVE7 CURVEB CLFVEG CUFVEIO */
    DIHENSION N1 (1),XX(1),YY(1)
    LOGICAL*1 MIITXT(110), SUFPLS(100)
    CALL RDCEUS
    CALL TXCLER
    CALL SUK(N,NI,MSUM)
C SET L* FLLOTTIHG SCALES
    S1=XYSCL (1)
    52=XYSCL (2)
    S3=XYSCL (3)
    S4=XYSCL.(4)
C PREF'AFE THE DISFILAY
    WRITE(IOUT,1O)
10 FORMAT ("SUFERIMFOSEL CURVES:-")
    CALL MNOFEN(875.,715.11)
    CALL MNNISF'(MNTXT,11,10,1)
    CALL FRAME (870.,733.,11)
    CFLLL ALFHHMB
    WRITE: (IOUT,20)
20 FOFMAT (///////////////62X,** TYFEE IN"/62X, "CURUE NO.")
2 IALL LMTAFA
C CHECK :OOR REFFESH
    IF (J.EQ.6) GOTO 23
```

    WRITE (7,77)
    3 CALL MAFPICK(J,ICHAF, MNO)
NFDEL $=I C H A F-48$
IF (J.EQ.5.AND.NFDEL.GT.9.OK.J.EQ.5.AND.MFDEL.LT. 1) GOTO 3
17 CALL CONFFM (ICHAF)
IF (ICHAR.EQ.78) GOTO 12
IF (ICHAR.NE.89) GOTO 17
GOTO (21,21,23,24,25,11,21,27,21,11,21), J
12
$\mathrm{J}=0$
goto 2
21 IC $=3$
RETUKN
C. GRAFH/REFRESH
$23 \quad K=0$
CALL LHTSCL (S1,52,S3,S4)
CALL FFFAAKE (51,52,53,54)
DO $11=1,10$
FEWIND 9
IF (NCRU (1). NE.99) GOTO 22
CALL SETFIL $(9$, SUFFLS $(I+K))$
77 CALL SFEDRW ( $N, N 1, I, X X, Y Y, H S U K, S 1, S 2, S 3, S 4$ )
$22 \quad K=K+9$
1 CONTINUE
$\mathrm{J}=0$
gOTO 2
( IISFLAY CURVE ORIGIN
24 CALL DISORG(S1,52,53,54)
GOTO 2
C DELETE CUFVE OFTION
25 NCRU (NFIEL) $=0$
CALL WKERUS
GOTO 2
© AXES MAKKING
21 CALL AXSYRK (S1,S2,53,54)
GOTO 2
END
C

C
FUNCTION EFLOT (NC,SCL1,SCL2,SCL3,SCL4,NSUM)
C $1 / 0$ COMMON DATA AKEA
COMMON/DATSUP/NFS,NFI (50), IFREES, X (50) , Y(50), Z (50) , L (50), IH (5)
4 , $4(5)$, METHOD, IHELF, IFFREV, BOUND (6) , SUBSET, INTFNT, IE (2)
1 ID
COMMON/CUFVEF IT/XCOEF $(50,4), Y C O E F(50,4), 2 C O E F(50,4), X C O R D(200)$
, YCOKD (200), ZCORD (200), TCLRE (200)
DATA IDC/"123456789"/
LOGICAL*1 IDC (9)
IF:1
IF $=1$
$\mathrm{I}=1$
C PLOT SUPFLIED FOINTS
3 CALL FLLUSGN(SCL1,SCL2,SCL3,SCL4,XCOFO(I),YCORD (I))
2 CALL TXMOVE (XCOFD (I), YCOFD (I) )
IF (I.EQ.NSUK) FIETUKN
IF $1=I F^{\prime}+1$
IF $2=I F+N F^{\prime} I(I F)+1$
DO $1 \mathrm{~J}=1 \mathrm{~F}$ 1, IF2
1 CALL TXDFAW (XCORD (J), YCORD (J) )
IF (IF.HE.1.OK.NC.EU.O) GOTO 4
C WUREEF TIE CUKVES
CA:L DTEXT (XCORD (J-3) ; YCORD (J-3) , IDC (NC) , 1)
4 IF:IFO

```
    IF =IF F 1
    I=I+NFI(IF-1)+1.
    GOTO 3
    END
C
C ***************** OUTTUTT COEFFICIENTS**************************
C
        SUBFOUTINE OUTCOF (NCOEF,IFNTR,HETHOD,C,IDEV)
        DIMENSION C(5O,4)
        I=IFNTF
        CALL CURFOS(1.,580.)
        WRITE (IUEV,10)
C BISPLAY COLUMN TITLES
10 FOKHAT (" I",7X,"CL",11X,"C2",11X, "CJ",11X,"C4"/)
3 LO 5 J=i,NCOEF
                WRITE(IDEV,40)I,C(I,1),C(I,2),C(I,3),C(1,4)
                        I= I+1
    CONTINUE
        FOFMAT (12,4(2X,E11.4))
40
FNETUFW
    END
C
C****************OUTPUT A PAGE OF THE TABLEE****************************
C
    SUEROUTINE OUTFGE (NFOINT,IFNTT,XX,YY,ZZ,TT, ILEV,IIIM)
    DIMENSION XX(1),YY(1),ZZ(1),TT(1)
    CALL CURFOS(1.,710.)
    IF(IDIM.EQ,3)WRITE (IDEV,10)
    IF (IDIM.EQ.2)WRITE (IDEV,12)
    FORMAT (//" I",7X,"T(I)",10X,"X(I)*,9X;"Y(I)*,9X,"Z(I)*/)
    10 FORMAT(//"*I",7X,"T(I)",IOX,"X(I)",9X,"Y(I)",9X
    12 L0 3 I=1,NFOINT
    IF (IDIM.EQ. 3) WRITE (IDEV, 30) IFNT,TT (IFNT) ,XX (IFNT), YY (IFNT),ZZ (IFNT)
    IF (IDIM.EQ.2)WRITE (IDEV, 20) IFNT,TT (IFNT),XX (IFNT),YY (IFNT)
    IFNT=IF'NT+1.
3 CONTINUE
20 FORHAT (12,3X,3(E11.4,3X))
30 FORHAT (12,3X,4(E11.4,3X))
    RETURN
    END
C
C******************* OUTTUT THE TITLE OF THE DISFLAY*********
C
C ********AND THE COMMAND MENOH*****************
    SUBFOUTINE OUTTIL(IC,ITEM,IDEV,ICOEF)
c MENU ITEMS
    DATA HNTXTI/" + NEXT + FREVIOUS+ HARDCOFYY + COEFF'NT + FORWAFDB
4+ BACNWARID + HELF + RESTAKT + EXIT */
    DATA HNTXT2/** NEXT + FREVIOUS+ X-COEF'N+ Y-COEF'N+ Z-COEF'N
6 + HARNCOFYY FORWARD + BACKWAKD + HELFF + FESTART + EXIT *'
    LOGICAL*1 MNTXT1(90) FINTXT2(110)
    CALL TXCLER
    IF(IC.EQ.2) GOTO 2
    WRITE (IUEV,IO)
2 IF(ICOEF.EG.1)WRITE(IDEV,2O)
    IF (ICOEF.EQ.2) WFITE (IDEV,30)
    IF (ICDEF .EQ.3)WRITE (IDEV, 40)
20
30
4 0
    FOFMAT (///" FAKAMETRIC X-COEFFICIENTS:-"///)
    FOFHAT (///" FARAMETRIC Y-COEFFICIENTS:-*///)
    FORMAT (//'/" F'AFIAMETKIC Z-COEFFICIENTS:-"://')
```

```
C OUTFUT MENU
3 CALL MNOFEN(B75.,715.,1)
    IF(IC.EQ.2) GOTO 22
    CALL HNDISF'(MNTXT1,ITEM,10,1)
    gOTO }
22 CALL MNDISP (MNTXT2,ITEM,10,1)
4 CALL FRAME (870.,733.,ITEM)
    RETURN
    END
l
C***********SAVE COMMON SATA AREEA***************
C
    SUEROUTINE RDCRUS
    COMMON/CURUES/NCRU(10) %XYSCL (4)
    REWIND }
C OPEN QUTFUT FILE
    CALL SETFIL (7,"SUFCRUES")
    FEAB (7,10) (NCRU (I),I=1,10)
    FEAD (7,20) (XYSCL (I),I=1,4)
10 FORMAT(I2)
20 FORMAT (F11.4)
    ENDFILE }
    RETURN
    END
C
C#********* DISFLAY THE SUFERIMFOSED CUKUES***********************
C
    SUBFOUTINE SKEDRW(N,N1,NC;XX,YY,HSUM,SCL1,SCL2,SCL3,SCL4)
    DIMENSION N1 (1), XX(1),YY(1)
    READ (9, 25) HSUM,N
    N2=N-1.
    READ (9,30) (XX(I),YY(I),I=1,MSUM)
    FEAD (9,20) (N1 (I), I=1,N2)
    FOFMTAT (F11.4)
    FORHAT (13)
    FOKMAT (213)
    FC= EFLOT (NC,SCL1,SCL.2,SCL3,SCL4,MSUM)
    RETURN
    END
C
6 ********** FIND TOTAL. NUNEER OF INTEFFFOLATED FOINTS*X**********
C
    SUBROUTINE SUM (N,NL,MSUM)
    BIMENSION N1(1)
    MSUMM=0
    N2=N-1
    DO 1 I = 1,N2
1 HSLMM=MSUKY+N1 (I)
    MSSUM=MSUPY+N
    RETURN
    END
C
C***********SAUE COMMON LATA FOK SUFERIMFOSED CURVE DISF'LAY*****
C
    SUBKOUIINE WFCFUS
    COMMON/CURVES/NCEV (10) , XYSCL.(4)
    FEWIND 8
    CALL SETFIL (8;"SUFCFUES")
    WFITE (8,10) (NICRU (I),I=1,10)
    WRITE (8,20)(XYSCL (I),I=1;4)
    FORKAT (I2)
20 FOKMAT (F11.4)
```

ENDFILE 8 FETUKN
END

APPENDIX 2.4

## THE COMMON LIBRARY SUBROUTINES 'EPLIB'

```
C
******************
* APFENDIX 2.40 *
*******************
C
C. THIS IS AN ARCHIVE LIBFAFIY SUEROUTINES USED BY BOTH F'ACKAGES.
C THEY FROUIDES THE FOLLOWING FUNCTIONS:-
C 1.HANDLES INFUT/OUTFUT FOR READING AND WRITING COMMON DATA AREA:
C 2. UTILITY ROUTINES FOR DISFLAY IMAGES
C
E
C
C
C###*********DFANING AND HAFKING THE AXES***********************
C
C SETS SCREEN AFEÁ , SCALE AND CHECHS AXES FOSITIONING
    SUBROUTINE AXSHFKK(SCL1,SCL2,SCL3,SCL4)
    CALL. LMTSCL(SCL1,SCL2,SCL3,SCL4)
    F'1=SCL1*SCL3
    F'2=SCL2*SCL4
    IF(F'1)11,12,12
11 P1=0
    GOTO 22
12 P1=SCL1
22 IF(F2)111,112,112
111 P2=0
    G0TO 33
    112 P2=SCL2
    33 IF(F1.EQ.SCL1.AND.F2.EQ.SCL2)GOTO 1
C DRAN AXES
CALL TXYONE (P1,SCL4)
CALL TXURAW(F1,FF2)
CALL TXDFAW(SCL3,F'2)
IF (F1.NE.0) GOT02
CALL TXMOVE ( }\textrm{P}1,\textrm{F}2\mathrm{ ) 
CALL TXDFAN(SCL1,F2)
2 IF(P2.NE.0) BOTO 1
    CALL TXMOUE (F'1,FO2)
    CALL. TXDFAW (F'1,SCL2)
    C HARKS THE AXES(10-DIVISION)
1 CALL XYMAFK (SCL1;SCL2,SCL3,SCL.4)
    CALL LMTAFA
C OUTPUT SCALE FACTOKS
    CALL XYUALU(SCL1,SCL2,SCL3,SCL4)
    RETURN
    END - Y
C
C*********** OUTFUT A CONFIRMATION MESSAGE *************
C
    SUBROUTINE CONFRM(ICHAR)
    COMMON/IO/IN,IOUT
C DISFLAY THE MESSAGE RAISE THE CUESOR AND WAIT FOR ANSWEF
    CALL CUFPOS(800.1750.)
    WRITE(IOUT,IO)
10 FOFMAT ("CONTINLE (Y/N)?")
    CALL TXCURS(X1,Y1,ICHAR)
    RETURN
    END
C
C ***************FEASS CURSOR INPUT COORDINATES************************
C
    SUEROUTINE DISCOF(ICD,SCLI,SCL2,SCL3,SCL4)
```

COMMON/IO/IN: IOUT
C ACTIVATE CUKSOR OUER SFECIFIED SCREEN AFEA
CALL L.MTSCL (SCL1,SCL2,SCL3,SCL4)
CALL TXCURS (X1,Y1,ICHAR)
ICD:ICD 1
CALL LMTAKA
IF (ICD.EO.1) GOTO 15
© OUTFUT CURSOR COORDINATES
CALL CUFFOS(1.,270.)
11 WRITE (IOUT,10)X1,Y1
10 FQKMAT (59X,"X=",E11.4/59X,"Y=",E11.4)
2 RETURN
15 CALL CURFOS (1.,310.)
GOTO 11
END
C
C **************OUTPUTS DISFLAY ORIGIN $\# * * * * * * * * * * * * * * * * * * * * * ~$
C
SUBFOUTTINE BISORG (SCL.1,SCL2,SCL3,SCL4)
COMMON/IO/IN, IOUT
C OUTFUT DISFLLAY COORDINATS OF THE ORIGIN
CALL CUFPOS (1.1750.)
WRITE (LOUT,20)SCL1,SCL2,SCL3,5CL4
FORYAT (18X,"MIN(",E11.4,",",E11.4y")"/18X,"KAX(",E11.4,",",E11.4,
20 FORMAT (18X, "
$X 0=S C L 1$
YO $=$ SCL2 2
$X 1=$ SCL 3
$Y 1=$ SCL 4
6 PROMFT USER TO ENTER ALTEFNATIVE ORIGIN COORUINATE
25 CALL MESSAG("* DISFLAY AXES (MIN.\& KAX.) ?~")
IF (IEEFOR (110). NE, O) GOTO 333
READ (IN,30) SCL1, SCL2, SCL3.SCL 4
30 FORMAT (4GO.0)
C CHECK USER COOKDINATES
IF (SCL1.GT.SCL3.OR.SCL2.GT.SCL.4) GOTO 25
IF (SCL1.GT.XO.OF.SCL2.GT.YO) GOTO 25
IF (SCL.3.LT.X1.DF.SCL4.LT.Y1) GOTO 25
RETURN
333 ENDFILE 5
GOTO 25
END
6

c
SUBFOUTINE DRAW (FICTUF,FR,XO,YOFXI,Y1,N)
C OUTPUT ROUTINE DEFINED AS EXTERNAL TO DRAN THE FICTUFE/CURVE
EXTERNAL FICTUR
INTEGER R
© SETS VIEWPORT ,WINDOW AND DFAWS RECTANGULAF FKAME
CALL LMTSCL (XO;YO;X1;Y1)
CALL FFFAME $(X O, Y O, X 1, Y 1)$
$F C=F I C T U R(R, X O, Y O, X 1, Y 1, N)$
RETURN
END
C
C $\# * * * * * * * * * * * * * * * * E X I T$ AND DELETE ALL INTEFMEDIATE FILES************ C

SUBROUTINE EXIT
C EXIT ROUTINE FOR THE EXFLICIT ROUTINE
COMMON/CURUES/NCRV (10), XYSCL. (4)
© FILES CONTIANING COHMON DATA AKEAS

```
    DATA SUFCEV,DATSF;OUTCEV,COMJ/"SUFCEVES","LATSUFFL","OUTFIT",
| COMJON"/
C FILES CONTIANING SUFREIMFOSED CURUES
    DATA C1,C2,C3,C4,C5,C6%C7,C8,C9/"CURVE1" "CUKVE2", "CUFVE3*
| "CURVE4", "CURVES", "CUKVEG" "CUKVE7","CUKVEB","CURVE9"/
    LOGICAL*1 SUPCRV (10), DATSF (10), OUTCRU(10),COMJ(10)
    LOGICAL*1 C1(10);C2(10),C3(10),C4(10),C5(10),C6(10),C7(10)
4,C8(10),C9(10)
G REYOVES UNWANTEU FILES EEFONE TEFMINATION
    CALL FMFILE(DATSP)
    CALL FIMFILE (OUTCEV)
    CALL FMFILE (COMJ)
f FEMOVE SNFERIMFOSE CUKVES
    CALL FHFFILE(CI)
    CALL FMMFILE (C,2)
    CALL FMFILE (C3)
    CALL FiMFILE(C4)
    CALL FMFILE(CS)
    CALL RMFILE(C6)
    CALL RMMFILE(C7)
    CALL RMFILE(C8)
    CALL RMFILE (C9)
    CALL FMMILE (SUFCRU)
    RETURN
    END
C
C #***********FESET UIEWF'ORT & WINDOW IEFFAULT UALUESN****************
C
    SUBROUTINE LMTARA
    CALL TXUF'RT(0.,0.,1023.,780.)
    CALL TXWIND(0.,0.,1023.,780.)
    FETURN
    END
c
C **************SETS UP SCEEEN WINLOW **********************************
C
    SUBKOUTINE LHTSCL(SCL.1,SCL2,SCL3,SCL44)
    CALL. TXUFRT (0.,0.,855.,700.)
    CALL TXWIND(SCL1,SCL2,SCL3,SCL4)
    RETUEN
    END
C
C********** SEAKCH FOK MINIKLMM & MAXIMUM VALUES OF X,Y*************
E
    SUBFOUUTINE MINMAX (SCL1,SCL2,SCL3,SCL4,XI,Y1;N)
    DIMENSION XI(1),Y1(1)
    SCL1=X1 (1)
    SCL3=X1 (1)
    SCL2=Y1(1)
    SCL4=Y1(1)
    MO 2 I=2.N
C IEST FOR HAXIMUM AND MINIMUM
    IF(X1(I).GT.SCL3) SCL3 =X1(I)
    IF (X1 (I).LT. SCLI) SCL.1=X1 (I)
    If (Y1(I).GT.SCL4) SCL4=Y1(I)
    IF(Y1(I).LT..SCL2) SCL2=Y1(I)
2 CONTINUE
    RETURN
    END
C
```



```
C
```

```
    SUBFOUTINE PEXIT
C EXIT ROUTINE FOR THE PAKAMETRIC PACKAGE
    COMYON/CURUES/NCEV (10) \XYSCL (4)
    C FILES CONTAINING I/O CONMON DATA AREAS
    DATA SUFCRU,PUATSF',OUTCRU/"SUF'CRVES" "F'DTSUFFL", "FOUTFITC"/
    C FILES CONTAINING SUPERIMFOSED CLFVES
        LATA C1,C2,C3,C4,CS,C6,C7,C8,C9/"CURVE1","CURVE2", "CURVE3*
```



```
        LOGICAL*1 SUF'CRV (10),FULATSF(10), OUTCEN (10)
        LOGICAL*1 C1(10),C2(10),C3(10),C4(10),C5(10),C6(10),C7(10),C8(10)
* ,C9(10)
C REMONES UNWANTED FILES BEFORE TERMINATION
        CALLL FHFILE (FDATSF)
        CALL. FNGFILEE (OUTCRV)
c REMOUE SUPERIMFOSE CURVES
        CALL FMYFILE(C1)
        CALL RMFILE(C2)
        CALL RMFILE(C3)
        CALLL RMFILE (C4)
        CALL FMFILE (C5)
        CALL RMFILE (C6)
        CALL RMFFILE(C7)
        CALL RMFILE (CB)
        CALL RHFILE(C9)
        CALL. RMFILE (SUFCRN)
        RETUKN
        END
    C
    C************HFAWS A RFEECTANGLK_AR FRAME ROUND THE PICTUREE*********
    C
        SUBROUTINE FFRAME {XO,YO,XI,Y1)
        CALLL TXMOUE (XO,YO)
        CALL TXIFKAW (XO,Y1)
        CALL TXUFAW (X1;Y1)
        CALLL TXOFAW (XI;YO)
        CALL TXDRAW (XO,YO)
        RETUFW
        END
    C
    c|##*****INAWS A FLUS SIGN*******************************************
    C
    SUEROUTINE PLUSGN(SCL1,SCL2,SCL3,SCL4,X1,Y1)
C SETTING THE SIZE OF THE FLUS SIGN
    SCL5=(5CL_3-SCL.1)*5/855
    SCL6*(SCL4-SCL.2)*5/700
C CLIF THE SIGN IF URAWN ON THE EDGES OF THE VIEWFORT
    IF (X1.NE.SCLI) GOTO 1
    Z1=X1
    Z2=X1+SCL5
    GOTO 3
1 IF (XI.NE.SCL.3) GOTO 2
    Z1=X1
    Z2=X1-SCLS
    goto 3
    Z1=X1-SCL5
    Z2=X1+5CL.5
    IF(Z1.LT.SCL1) Z1=X1
    IF (Z2.GT.SCL_3) Z2=X1
f fraNS THE FLUS SIGN
3
    CALL TXHBUE (Z1,Y1)
    CALL TXDRAW{Z2,Y1)
    IF (Y1.NE.SCL.2) GOTO 4
```

$Z 3=Y 1$
$Z 4=Y 1+S C L .6$
GOTO 6
IF (Y1. NE. SCL.4) GOTO 5
$Z 3=Y 1$
Z4=Y1-SCL 6
GOTO 6
$23=Y 1+5 C L 6$
Z4=Y1-SCL6
If (Z4.LT.SCL2) $\mathbf{Z 4} \mathbf{4} \mathbf{Y} \mathbf{Y}$
If (Z3.GT.SCL4) Z3mY1
6 CALL TXMOVE $(X 1,23)$
CALL TXURAW (X1,24)
FETUKN
END
C

C
SUBROUTINE FRDCHI
C INFUT COMMON DATA AREA
COMMON/DATSUF/NFS,NFI (50), IFREES, $X(50)$, $Y(50), Z(50), L(50)$, IH(5),
$d$ M(5) , HEETHOD, IHELFF, IFFEEV, BOUND (6), SUBSET, INTFNT, IE (2) ID
INTEGER SUBSET
FEWIND 7
C OPEN INFUT FILE
CALL SETFIL (7."FDTSUFFL")
READ (7, 10) NFS, IFFEES, METHOD, IHELF, IFREU, SUBSET, INTFNT, ID
10 FOKHAT (BI3)
IF (ID.EQ. 3) KEAD (7,20) (NFFI (I) , X(I),Y(I),Z(I),L(I), I=1,NF'S)
IF (ID.EQ.2) READ (7,20) (NFI (I) , X(I),Y(I),L(I),I=1, HFS
20 FORMAT (F10.4)
$\operatorname{READ}(7,30)$ (IH(I) , M(I), I=1,5)
READ (7, 40) (EOUND (I) , I $=1,6$ )
KEAD (7,30) IE (1) : IE (2)
30 FORHAT (13)
40 FORFAT (6F6.2)
ENDFILE 7
RETURN
END
C
〔 ***********RESTORE OUTFUT COMMDN DATA AFEA**************
C
SUBROUTINE FRDCK2 (N,HI, NC,IDIM)
C OUTFUT COMKON DATA AREA
COMMON/CURVEFIT/XCOEF $(50,4), \operatorname{YCOEF}(50,4), \operatorname{ZCCEF}(50,4), X C O K D(200)$,
$1 \quad \mathrm{YCORD}(200), \mathrm{ZCORD}(200)$, TCORD (200)
DIMENSION NI (i)
REWIND 7
f BPEN OUTFUT FILE
CALL SETFIL (7, "FOUTFITC")
MSUM $=0$
H2=N-1
[10 $1 \quad I=1$, N2
1 HSUM $1=$ KSUM + N1 (I)
KSLM $=$ HSUMW $+N$
IF (IDIM.EQ. 3 ) READ $(7,10)((\operatorname{XCOEF}(I, J), \operatorname{YCOEF}(I, J), \operatorname{ZCOEF}(I ; J) ; J=1, N C), I=1, N 2)$
IF (IDIM.EQ.2) READ $(7,10)((X \operatorname{COEF}(I ; J), \operatorname{YCOEF}(I ; J), J=1, N C), I=1, N 2)$
FORMAT (F12.4)
IF (IDIM.EQ. 3 ) $\operatorname{FEAD}(7,20)(X C O R D(I), \operatorname{YCORD}(I), 2 C O R D(I), \operatorname{TCORD}(I)$
t,I=1. H (SUM)
IF (IDIM.EQ.2) FEAD (7,20) (XCOKD (I), YCOFD (I), TCOKD (I), I=1,MSUM)

```
2 0
    FOFMAT (F12.4)
    ENDFILE 7
    RETUFN
    END
c
C #******* REMOUES ALL LINKS AND FUT DATA INTO GRRAY LIST***************
C
    SUBROUTINE FKKLNK (X1,Y1,Z1)
C IMPUT COMMON DATA AREA
    COMMON/DATSUF//NFS,NFI (50), IFFEES,X(50),Y(50),Z(50),L(50),IH(5),
|
&
    DIMENSION X1(1),Y1(1),Z1(1)
    INTEGER SUBSET
C THREALS THKOUGH THE LINK LIST AND COFY tO ARRAY list
    IF=IH(1)
    XI(1) =X(IP)
    Y1(1)=Y(IP)
    IF (ID.EQ.3)Z1(1)=Z(IF)
    DO 1 Im2,NF'S
    IF=L(IF)
    X1(I)=X (IF)
    Y1(I)=Y(IF)
    IF(ID.EQ.3)21(1)=Z(IF)
1 CONTINUE
    RETUKN
    END
c
& ##*#******SAVE INPUT COHKON DATA AREA***************
c
    SUBROUTINE PWKCK1
C INPUT COMHON DATA AREA
    COMMON/LATSUF/NF'S,NPI (50), IFFEES,X(50),Y(50),Z(50),L(50),IH(5),
l
4 ,ID
    INTEGER SUBSET
    REWIND B
C OPEN OUTFUT FILE
    CALL SETFIL(B,*PDTSUPFL")
    WFITE (8,10)NPS,IFREES,METHOD, IHELF,IFREV,SUESET,INTFFT, ID
FORMAT (8I3)
    IF (ID.EQ.3)WRITE (8,20) (NPI(I),X(I),Y(I),Z(I),L(I) II=1,NFS)
    IF(ID.EQ.2)WRITE (8,20) NFFI (I),X(I),Y(I),L(I),I=1,NFS)
    FORMAT (F10.4)
    WRITE (8,30) (IH(I),M(I),I=1,5)
    WRITE (8,40) (BOUND (I),I=1,6)
    WRITE (8,30)IE(1),IE(2)
30 FORMAT (I3)
40 FORKAT (6F6.2)
    ENDFILE 8
    RE.TURN
    ENJ
C
C ***********SSAVE OUTPUT COMMON DATA AREA****************
c
    SUBKOUTIHE FWRCK2(N,N1,NC,IDIM)
C OUTFUT COMMON DATA AREA
    COMMON/CURVEFIT/XCOEF (50,4), YCOEF (50,4),ZCOEF (50,4),XCOKD(2(0),
    YCOKD (200), ZCOKD (200),TCCFE (200)
    GIMENSION N1(1)
    REWIND 8
C OPEN OUTFUT FILE
```

```
    CALL. SETFIL(B;"FOUSTFITC")
    MSUM=O
    N2=N-1
    DO 1 I=1,N2
1 KSLMM=HSUMY+N1 (I)
    MSUM=MSSUMTN
    IF (IDIM.EQ.3) WRITE (8,10) ( (XCDEF (I,J), YCOEF (I , J), ZCOEF (I;J),J=1,NC),I=1,
    IF (IDIH.EQ.2) WRITE ( }8,10)((XCOEF (I;J), YCOEF (I,J), J=1,NC) ,I=1,N2
10 FORMAT (F12.4)
    IF (IDIH.EQ.3) WRITE (B,20) (XCOND (I) , YCORD (I), ZCORD (I) , TCORU (I)
(,I=1,MSUM)
    IF (IDIM.EQ.2)WRITE (8,20) (XCOKD (I), YCOND (I), TCORD (I) ,I=1,MSUM)
    2% FCNMAT (F12.4)
        ENDFILE 8
        RETUKN
    END
C
f ###******RESTORES INFUTT COMNON DATA AREA*********************
C
    SUBEOUTINE RDCOM1
C IHPUT COMMON DATA AKEA
    COMMON/LATSUP/NPS, NFI (50), IFREES; X(50),Y(50) ,L(50), IH(5),M(5) ,
&
                    METHOD, IHELP, IFKEV, BOLND (2) :SUBSET, INTFNT, IE (2)
    INTEGEF SUBSET
    REWIND 7
C BPEN AN INTEFMYEIIATE INFUT DATA FILE
    CALL SETFIL(7,"DATSUFFL")
    READ (7,10)NFS; IFREES,METHOD, IHELF; IFREV,SUBSET, INTFNT
10 FORMAT (713)
    READ(7,20) (NPI (I); X(I),Y(I) ,L(I),I=I,NFS)
20 FOFIMAT (F10.4)
    READ(7,30) (IH(I),H(I),I=1,5)
    EEAD (7,40) EOUND (1), EOCND (2)
    READ (7,30) IE (1) , IE (2)
    FORHAT (13)
3) FONHAT (13)
40 FORMAT (2F6.2)
    ENDFILE }
    RETUKN
    END
C
C ###**********RESTORES OUTPUT COHMON DATA AREA*****************
C
    SUBROUTINE RDCOM2 (N,N1,NC)
c OUTFUT COMMON DATA AREA
    COMMON/CURUEFIT/COEF (50,6) , XCORD (200) , YCCKND (200)
    DIMENSIDN NI (I)
    FEWIND 7
C OPEN AN INTERMEDIATE OUTPUT FILE
    CALL SETFIL(7,"OUTFIT")
    MSUM=0
    N2=N-1
    DO 1 I= 1,N2
1 MSUM=MSUM+N1 (I)
    MSUM=MSUMM+N
    READ (7,10) ((COEF (I, J); J=1,NC), I=1,N2)
10 FORMAT (F12.4)
    FEAD (7,20) (XCPRND (I), YCOFB (I), I=1,MSUM)
20 FONMAT (2F12.4)
    ENSFILE 7
    RET!FN
    END:
```

C\#\#\#\#\#\#\#\#*********READ COMMGN AREA FOR SOIN\#**************************
C
SUBROUTINE RDCOMJ
C COHMON JOIN BATA AREA
COMMON/JOIN/CJI (500), CJ2 (500),J3(12),J4 (100), IFNTR(6)
FEWIND 7
C OPEN JOIN DATA FILE
CALL SETFIL(7,"COMNON")
READ (7,10) (J3 (I), I=1,12)
FEAB (7,10) (IFNTF(I),I=1;6)
READ(7,10)L
L=L+1
FEALI(7,10)(J4(I),I=1,L)
K2=\3(1)
FEAD(7,20)(CJ1 (I),CJ2(1), I =1,K2)
10 FOKMAT (I4)
20 FOFMAT (F11.4)
ENDFILE 7
RETURN
END
l
C \#\#****** REMOUES ALL. LINKS AND FLTT UATA INTO ARRAY LIST***************
C
SUBFOUTINE REEILNK (X1,Y1)
C INPUT COMMKON DATA AKEA
COMMON/DATSUP/NF'S,NFI (50), IFKEES,X(50),Y(50),L(50),IH(5),H(5)
l
, HETHOD, IHELP, IFREV, BOLNN (2) , SUESET, INTFNT, IE (2)
DIMENSION XI(1),Y1(1)
INTEGER SUESET
C THREAUS THROUGH THE LINK LIST AND COFY TO SIMFLE LIST AFRAAY
IP=IH(1)
XI(1)=X(IF)
Y1(1)=Y(IF)
DO 1 I=2rNF'S
IF=L(IF')
XI(I) =X(IF)
Y1(I)=Y(IF)
1 CONTINUE
RETLRN
END
C
C \#\#********AXES MARKING \& SCALLING****************************
C
SUEROUTINE SCALE (A1,A2,B1,B2,IFLG,SCL1,SCL2,SCL3,SCL4)
DO 1 I:1,9
CALLL FLUSGN(SCL1,SCL2,SCL3,SCL4,B1,B2)
IF(IFLG.EQ.1)GOTO 2
B1=B1+A1
1 CONTINHE
RETUFN
2 B2=B2+A2
GOTO 1
END
C
C \#\#***********SAUE INFUT CIMMON DATA AREA*********************
C
SUBROUTINE WRCOM1
C INPUT COMMON DATA AKEA
COMMON/LATSUF/NFS,NFI (50), IFFEES,X(50),Y(50),L(50),IH(5) ,H(5),
l
HETHOD, IHELF', IF'REU, BOUND (2), SUE SET , INTFNT, IE (2)
INTEGER SUBSET
REWINB }

```
```

C OPEM AN INTERMEDIATE INFUT FILE
CALL. SETFIL(8,"DATSNFFL")
WRITE (8,10) HPS, IFFEES, HETHOD, IHELP; IFREV,SUBSET , INTFNT
10 FORHAT (7I3)
WRITE(8,20) (NPI(I) | (I),Y(I),L(I),I=1,NFS)
20 FOKMAT (F10.4)
WFITE (8,30)(IH(I),H(I),I=2,5)
WFITE (B,40) BOLND (1), EOUND (2)
WFITE (8,30)IE (1) , IE (2)
30 FORMAT(I3)
40 FOFHAT (2F6.2)
ENDFILE 8
RETLFN
END
C
| \#**************SAUES CUTFUT COMITON DATA AREA*****************
C
SUBFOLTTINE WRCOM2 (N,N1,NC)
C OUTFUT COMHON DATA AREA
COMMON/CURUEF IT/COEF (50,6) , XCORD (200) , YCORD (200)
DIMENSION NI (1)
FEWIND 8
6 OPEN AN INTEFHEDIATE OUTFUT FILE
CALL SETFIL(B,"OUTFIT*)
MSUM=O
N2=N-1
10O1 I=1,N2
1 HSUM=MSUMTNE (I)
MSUM=MSUNT+N
WKITE (8,10) ((COEF (I,J) ,J=1,NC),I=1,N2)
10 FORMAT (F12.4)
WRITE (B,2O) (XCORD(I) , YCORD(I), I= , MSLM()
20 FORHAT (2F12.4)
ENDFILE 8
RETURN
END
C

```

```

C
C COHMON JOIN DATA AREA
COHMON/JOIN/CJ1 (500) , CJ2 (500), J3 (12) , J4(100) , IFNTK (6)
REWIND 8
\& BPEN JOIN DATA FILE
CALL SETFIL(8;"COKJON")
WFITE (8,10) (J3(I),I=1,12)
WRITE(8,10) (IPNTR(I),I=1;6)
L=0
K1=IFNTK(1)-2
J=3
DO \& I=1,K゙1
L={+J3(J)-1
Jm\+2
CONTINUE
WRITE (8,10)L.
L=L+L
WRITE(8,10)(J4(I),I=1,L)
K2=\3(1)
WRITE (8,20) (CJI (I),CJ2(I),I=1,K2)
10 FORHAT (14)
20 FORMAT (F11.4)
ENDFILE 8

```
```

RETUFN
END
C
C \#\#***********HARKS THE GRAFH AXES**************************
C
SUEFOUTINE XYMARK(SCL1,SCL2,SCL3,SCL4)
AI= (SCL3-SCL1)/10
A2=(SCL4-SCL2)/10
IFLG=0
B1=SCLL 1+A1
82=SCL?
C MARK THE AXES
CALL SCALE (A1,A2,B1,E2,IFLG,SCL1,SCL2,SCL_3,SCL4)
B1=SCL1+A1
B2=SCL4
CALLL SCALE (A1;A2,B1,E2,IFLG,SCL1;SCL2,SCL3;SCL4)
IFLG=1
B1mSCL1
B2=SCL2+A2
CALL SCALE (A1,A2,B1,B2,IFLG,SCL1,SCL2,SCL3,SCL4)
B1=SCL3
B2=SCL2+A2
CALL SCALE (A1,A2,B1;B2,IFLG,SCL1,SCL2,SCLL3,SCLL4)
FETURN
END
C \#\#******* OUTPUTT KAX \& KIN OF X , Y AXES***************************************
SUBROUTIHE XYVALU(SCL1,SCL2,SCL_3,SCL4)
COMMON/IO/IN. IOUT
CALL CUFFOS (0.,185.)
WRITE(IOUTT,20) SCL1,SCL_3,SCL2,SCL4
20 FOFMAT (64X,"X-KIN."/60X,E11.4,65X,"X-HAX."/60X,E11.4,65X,"Y-HIN."/
4 60X,E11.4,65X,"Y-HAX.*/60X,E11.4)
RETURW
END
|

```

\section*{APPENDIX 3}
iCT - program listing

\section*{APPENDIX 3.1}

THE CONTOURING ALGORITHM SUBROUTINES
```

C
****************

* APPENDIX 3.1 *
****************
THIS IS tHE CONTOUR TRACING ALGORITHM WHICH USES THE
TRIANGULAR CELL DISCRETIZATION.IT TRACES THE CONTOUR LINE
WITHIN AGIVEN RECTANGLEF THE REGION CONSIDERED.
THE ALGORITHM CONSISTS MAINLY OF FOUR SUBROUTINES TOGETHER
WITH OTHER TWO WHICH HANDLES THE SPECIAL CASE WHEN CONTOUR
CROSSES THE RECTANGLE EDGE TWICE.THE MAIN SUBROUTINE ARE:
"RECANG".....TRACES THE CONTOUR FOR EACH SIDE DF RECTANGLE
"DCRVSD".....FOLLOWS THE CONTOUR LINE WITHIN THE RECTANGLE
"DLINE ".....CONSTRUCTS THE TRIANGULAR CELL AND DRAWS THE LINE
"RODT ".....CHECK FOR THE EXISTENCE OF A ROOT ALONG AGIVEN SIDE
c
C
C
C***********TRACE THE CONTDUR IN ONE RECTANGLE****************
SUBROUTINE RECANG(XMIN,XMAX,YMIN,YMAX,XSTEP,YSTEP,CONTOUR,II;Ji
COMMON/LIMIT/XX1,YY1,XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT,
XXL,YYL,ITRACE
C SET UP THE COORDINATES LIMIT OF THE RECTANGLE IN QUESTION AND
C INITIALISE EXIT LIST....
XX1=XMIN
YY1=YMIN
XX2=XMAX
YY2=YMAX
CONT=CONTOUR
MNSTEP=4.0*(XMAX+YMAX-XMIN-YMIN)/(XSTEP+YSTEP)
DO 1 I=1,4
XEXIT(I)=0.
YEXIT(I)=0.
IESID(I)=0
CONTINUE
NEXITS=O
C CHECK FOR SPECIAL RECTANGLE
CALL SPCREC(ISP:II,JJ,CONT,MNSTEP,XSTEP;YSTEP,NEXITS)
IF(ISP.EQ.1) GOTO 2
C SIDE 1
CALL DCRUSD(XMIN:YMIN,XMAX,YMIN,XSTEP,YSTEP,MNSTEP,NEXITS,1)
C SIDE 2
CALL DCRVSD(XMIN,YMAX,XMAX,YMAX,XSTEP,YSTEP,MNSTEP,NEXITS,2)
C SIDE 3
CALL DCRUSD(XMIN,YMIN,XMIN,YMAX,XSTEP,YSTEP,MNSTEP,NEXITS,3)
C SIDE 4
CALL DCRUSD(XMAX,YMIN,XMAX,YMAX,XSTEP',YSTEP,MNSTEP,NEXITS;4)
C TEST SPECIAL CASE WITH TWO EXITS;AND SAVE EXIT COORDS.
2 CALL TWOEXT(II,JJ,XSTEP,YSTEP,MNSTEP)
RETURN
END
C
C*****************DRAWS THE CURVE FROM AGIVEN RECTANGLE SIDE**********
C
SUBRGUTINE DCRUSD(X1,Y1,X2,Y2,XS,YS,M,N,ISIDE)
COMMON/LIMIT/XX1,YY1,XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT,
XXL,YYL,ITRACE
COMMON/CORNERS/CNRLT (2),CNRRT (2),CNRLB(2),ISIGNS(3),FUN(3)
COMMON/STATCS/NS,NEF1,NEF2
DIMENSION CLD(2),CRD(2),CLU(2)
LOGICAL RFOUND

```
```

C CHECK FOR SPECIAL CASE(TWO EXIT)
IT=1
IF(ITRACE.EQ.2.OR.ITRACE.EQ.4) GOTD 33
C FIND SINGLE ROQT ALDNG THE GIVEN SIDE
CALL ROOT(X1,Y1;X2,Y2;XS,YS,ISIDE,RFOUND)
IF(RFQUND.EQ..FALSE.) RETURN
C CHECK FOR EXIT POINTS
33 DO 2 K=1,N
XDIF=ABS(CNRLT(1)-XEXIT(K))
YDIF=ABS(CNRLT(2)-YEXIT(K))
XYSTEP=XS+YS
XYDIF=XDIF+YDIF-XYSTEP
IF(XYDIF.LT.O.) RETURN
CONTINUE
C CHECK FOR SPECIAL CASE
IF(ITRACE.EQ.2.QR.ITRACE.EQ.4) GOTO 333
XLT=CNRLT(1)
YLT=CNRLT(2)
FLT=FUN(1)
XRT=CNRRT(1)
YRT=CNRRT (2)
FRT=FUN(2)
X=(XRT*FLT-XLT*FRT)/(FLT-FRT)
Y=(YRT*FLT-YLT*FRT)/(FLT-FRT)
212 CALL TXMOVE(X,Y)
XXL=X
YYL=Y
C TRACE THE CURVE FURTHER IN THE CURRENT RECRANGLE
333 DO 3 NSTEP=1;M
X3=CNRLB(1)
Y3=CNRLB(2)
F3=F(X3,Y3)-CONT
FUN(3)=F3
C RUN TIME STATISTICS
NEF 1=NEF 1 +1
NS=NS+1
ISIGNS(3)=1
IF(F3.LT.O.)ISIGNS(3)=-1
CLD(1)= =CNRLT (1)
CLD(2)=CNRLT (2)
CRD (1)=CNRRT (1)
CRD (2)=CNRRT (2)
CLU(1)=CNRLB (1)
CLU(2)=CNRLB(2)
ICASE=0
C TEST FOR WHICH SIDE CURVE CROSSES AND TEST FOR DEGENERATE CELL
IF(ISIGNS(3).NE.ISIGNS(1)) ICASE=ICASE+1
IF(ISIGNS(2).NE.ISIGNS(3)) ICASE=ICASE+2
G0Tם(20,30), ICASE
C CURVE PASSES OUT LEFT HAND SIDE OF CELL
20 FL=FUN(1)
FR=FUN(3)
CALL DLINE(CLD;CLU,CRD,XL,YL,FL,FR)
ISIGNS(2)=ISIGNS(3)
FUN(2)=FUN(3)
GOTO }
C CURVE PASSES OUT OF RIGHT HAND SIDE OF CELL
30 FL=FUN(3)
FR=FUN(2)
CALL DLINE(CLU,CRD,CLD,XL,YL,FL,FR)
\#SIGNS (1)=ISIGNS(3)
|゙UN(1)=FUN(3)
7
XLD1=XL-XX1-0.001
XLDZ =XX2-XL-0.001
YLD1=YL-YY1-0.001

```

YLD2=YY2-YL-0.001
IF (YLD \(1 . L T . O . . O R . Y L D 2 . L T . O . . O R . X L D 1 . L T . O . . O R . X L D 2 . L T . O\).\() GOTO\) CONTINUE RETURN
C SET EXIT POINTS
9 IF(IT.EQ.1) GOTO 31
\(\mathrm{N}=\mathrm{N}+1\)
C MARK EXIT POINT SIDE FOR SPECIAL CASE
WRITE(9,7777)NSTEP
7777 FORMAT(I3)
IF(YLD1.LT.O.) IESID(N)=1
IF(YLD2.LT.0.) \(\operatorname{IESID}(N)=2\)
IF(XLD1.LT.0.) IESID(N)=3
IF(XLD2.LT.O.) IESID(N)=4
XEXIT \((N)=X L\)
\(\operatorname{YEXIT}(N)=Y L\)
RETURN
I T=0
GOTD 3
END
c
C************DRAW STAIGHT LINE IN A CELL******************
c
SUBROUTINE DLINE(CNRL,CNRR,CNROL, \(X, Y, F 1, F 2)\)
COMMON/CORNERS/CNRLT (2), CNRRT (2), CNRLB (2), ISIGNS(3), FUN(3)
COMMON/LIMIT/XX1;YY1,XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT, XXL,YYL,ITRACE
DIMENSION CNRL(1),CNRR(1),CNROL(1)
C COMPUTE THE CONTOUR INTERSECTION POINT BY LINEAR INTERPOLATION
XLT \(=\) CNRL (1)
YLT=CNRL (2)
\(X R T=\operatorname{CNRR}(1)\)
YRT=CNRR(2)
\(X=(X R T * F 1-X L T * F 2) /(F 1-F 2)\)
\(Y=(Y R T * F 1-Y L T * F 2) /(F 1-F 2)\)
C CLIP THE LINE IF NECESSARY
22 CALL \(\operatorname{CCLIP}(X, Y)\)
\(X X L=X\)
\(Y Y L=Y\)
CALL TXDRAW \((X, Y)\)
C SET UP THE COORDINATE OF THE THIRD VERTEX DF NEXT CELL
DO \(1 \quad \mathrm{I}=1,2\)
\(\operatorname{CNRLB}(I)=\operatorname{CNRR}(I)+C N R L(I)-C N R O L(I)\)
\(\operatorname{CNRRT}(I)=\operatorname{CNRR}(I)\)
CNRLT(I) =CNRL(I)
1 CONTINUE
RETURN
END
c
C*********FINDS ASINGLE ROOT ALONG THE SIDE OF RECTANGLE********
C
SUBROUTINE ROOT(X1,Y1;X2,Y2;XS,YS,ISIDE,RFOUND)
COMMON/LIMIT/XX1,YY1,XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT, XXL, YYL, ITRACE
COMMON/CORNERS/CNRLT (2),CNRRT (2),CNRLB (2),ISIGNS(3),FUN(3)
COMMON/STATCS/NS,NEF1,NEF2
LOGICAL RFOUND
C compute function values at both ends of the rectangle side \&
C ADJUST THE SIGNS
\(F 1=F\left(X_{1}, Y_{1}\right)-C O N T\)
\(\operatorname{FUN}(1)=F 1\)
ISIGNS (1) \(=1\)
IF (F1.LT.O.) ISIGNS \((\ddot{1})=-1\)
\(F 2=F(X 2, Y 2)-C O N T\)
FUN(2)=F2
C RUN TIME STATISTICS
```

    NEF2=NEF2+2
    ISIGNS(2)=1
    IF(F2.LT.0.)ISIGNS(2)==1
    C IF EQUAL SIGN,ND RODT IS FOUND RETURN
IF(ISIGNS(1).EQ.ISIGNS(2)) GOTO 1
RFOUND=.TRUE.
C BY MEANS OF REPEATED BISECTION OF THE SIDE,DETERMINE
C THE ENDS OF THE INTERVAL EITHER SIDE DF THE RODT.
STEP=(XS+YS)/2.
IF(ISIDE.GT.2) GOTO 2
C X-VARIES
NINTS=IFIX((X2-X1)/STEP+.5)
WINT=(X2-X1)/NINTS
GOTD 3
C Y-VARIES
2 NINTS=IFIX((Y2-Y1)/STEP+.5)
WINT=(Y2-Y1)/NINTS
3 INTLR=0
INTRR=NINTS
7 INTC=IFIX((INTLR+INTRR)/2+.5)
IF(ISIDE.GT.2) GOTO 8
W=X1 + INTC*WINT
FW=F(W,Y1)-CONT
GOTO 9
8 W=Y1+INTC*WINT
FW=F(X1;W)-CONT
C ADJUST THE SIGN DF THE APPROPRIATE ENDS
7 ISIGNC=1
IF(FW.LT.O.) ISIGNC=-1
IF(ISIGNS(1).EQ.ISIGNC)GOTO 11
INTRR=INTC
FUN(2)=FW
C RUN TIME STATISTICS
111 NEF2=NEF2+1
IF((INTRR-INTLR).GT.1) GOTD 7
C SET CORNER COORDINATES OF THE SIDE
GOTO (10,10,20,20), ISIDE
11 INTLR=INTC
FUN(1)=FW
GOTO 111
C SIDE 1 DR 2,SETTING THE TRIANGLE CELL CODRDINATES ON
C THE HORIZONTAL SIDES
10 IF(ISIDE.EQ.1)XYS=0.866025*STEP
IF(ISIDE.EQ. 2)XYS =-0.866025*STEP
CNRLT(1)=X1+INTLR*WINT
CNRLT (2)=Y1
CNRRT (1)=CNRLT(1)+WINT
CNRRT (2) = Y 1
CNRLB(1)=(CNRLT (1)+CNRRT (1))/2.
CNRLB(2)=Y1+XY5
RETURN
C SIDE 3 DR 4,SETTING UP THE TRIANGLE CELL COORDINATES ON
C THE VERTICAL SIDES
20 IF(ISIDE.EQ.3) XYS=0.8660%5*STEP
IF(ISIDE.EQ.4) XYS=-0.866025*STEP
CNRLT(1)=X1
CNRLT(2)=Y1+INTLR*WINT
CNRRT (1) = X 1
CNRRT (2) =CNRLT(2)+WINT
CNRLB(1)=X1+XYS
CNRLB(2)=(CNRLT (2)+CNRRT (2))/2.
RETURN
C ROOT NOT FOUND
1 RFOUND=.FALSE.
RETURN
END

```

\section*{C}

C************* CHECK SPECIAL CASE \& PDOCESSES*****************
C

8
SUBROUTINE SPCREC(ISP,II,JJ,CONTOUR,MNSTEP,XSTEP,YSTEP,NEXITS) COMMON/LIMIT/XX1;YY1,XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT,

XXL,YYL, ITRACE
COMMDN/SPCSD2/XE2(10),YE2(10), IROW2(10),JCOL2(10),ISD2(10),IPNT COMMON/SPCSD4/XE4(2),YE4(2),ISD4 COMMON/CORNERS/CNRLT (2),CNRRT (2),CNRLB (2), ISIGNS (3), FUN(3)
COMMON/STATCS/NS,NEF1,NEF2
STEP=(XSTEP+YSTEP)/2. XYS \(=0.866025 * S T E P\)
C CHECK THE EXISTENCE OF TWD EXIT AND ON WHICH SIDE DO \(1 \mathrm{~K}=1,10\)
IF(ISD2(K).NE.2) GOTO 1
IF(IROW2(K).EQ.II.AND.JCOL2(K).EQ.JJ) GOTO 5
1 CONTINUE IF(ISD4.EQ.4.OR.ISD4.EQ.1.OR.ISD4.EQ.3) GDTO 4 ISP \(=0\) RETURN
C TOW EXITS ON SIDE 2 ,establish a cell ald trace curve
5 DO \(8 \mathrm{~L}=1,2\)
CNRLT (1) =XE2 (K)-STEP/2.
CNRLT (2) = YE2 (K)
CNRRT (1) = XE2 (K) +STEP/2.
CNRRT (2) =YE2 (K)
\(\operatorname{CNRLB}(1)=(\operatorname{CNRLT}(1)+\operatorname{CNRRT}(1)) / 2\).
\(\operatorname{CNRLB}(2)=Y E 2(K)+X Y S\)
XLI \(=\) CNRLT(1)
YLI=CNRLT(2)
FLI=F(XL1,YL1)-CONT
FUN(1)=FL1
ISIGNS (1) \(=1\)
IF(FL1.LT.O.) ISIGNS(1)=-1
XRI = CNRRT (1)
YRI=CNRRT (2)
FRI \(=F(X R 1 ; Y R 1)-C O N T\)
FUN(2)=FR1
C RUN TIME STATISTICS
NEF2=NEF2+2
ISIGNS (2)=1
IF (FR1.LT. O.) ISIGNS (2)=-1
IF(ISIGNS(1).NE.ISIGNS(2)) GOTO 117
FDIF=ABS(FL1)-ABS(FR1)
IF(FDIF.LT.O.)ISIGNS(1)=-ISIGNS (1)
IF(FDIF.GE.O.)ISIGNS(2)=-ISIGNS(2) \(\quad\) y
117 CALL TXMOVE(XE2(K),YE2(K))
ITRACE \(=2\)
CALL DCRVSD (XX1,YY1,XX2,YY2,XSTEP,YSTEP,MNSTEP,NEXITS,2)
ISD2 (K) \(=0\)
\(\mathrm{K}=\mathrm{K}+1\)
CONTINUE
ITRACE \(=0\)
IF (ISD4.EQ.4)GOTO 4
GOTO 10
C TWO EXIT ON SIDE 4
4 DO \(9 \mathrm{~L}=1,2\)
IF(ISD4.EQ.1) GOTO 44
CNR :T(1) \(=\mathrm{XE} 4(\mathrm{~L})\)
CNR. T (2) \(=\) YE4(L)-STEP/2.
CNRI'T(1)=XE4(L)
CNRRT (2) \(=\) YE4 (L) + STEP/2.
IF (ISD4.EQ.4)CNRLB(1)=CNRLT(1)+XYS IF(ISD4.EQ.3)CNRLB(1)=CNRL?:1)-XYS

        CNRLB (2) =YE4 (L)-XYS
        XLI \(=\) CNRLT (1)
        \(\mathrm{YL} 1=\) CNRLT(2)
        FL1=F(XL1,YL1)-CONT
        FUN(1) =FL1
        \(\operatorname{ISIGNS}(1)=1\)
        \(\operatorname{IF}(F L 1 . L T, O.) \operatorname{ISIGNS}(1)=-1\)
        \(X R 1=\operatorname{CNRRT}(1)\)
        YR1 \(=\) CNRRT (2)
        FR1=F(XR1, YR1)-CONT
        FUN (2) =FR1
C RUN TIME STATISTICS
    NEF2=NEF2+2
        ISIONS (2) \(=1\)
        IF (FR1.LT.O.) ISIGNS (2) \(=-1\)
        IF(ISIGNS(1).NE.ISIGNS(2)) GOTO 17
        FDIF=ABS (FL1)-ABS (FR1)
        IF(FDIF.LT.O.)ISIGNS(1)=-ISIGNS (1)
        IF(FDIF.GE.O.)ISIGNS(2)=-ISIGNS(2)
17
    CALL TXMOVE(XE4(L),YE4(L))
        ITRACE \(=4\)
        CALL DCRVSD (XX1,YY1,XX2,YY2,XSTEP,YSTEP,MNSTEP,NEXITS,ISD4)
        CONTINUE
        1SD4=0
        ITRACE \(=0\)
        ISP=1
        RETURN
        END
C
C************** CHECK FOR TWO EXITS****************
C

SUBROUTINE TWOEXT(II,JJ,XSTEP,YSTEP,MNSTEP)
COMMON/LIMIT/XX1,YY1,XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT,
            COMMON/SPCSD2/XE2(10),YE2(10),IROW2(10), JCOL2(10), ISD2(10), IPN1
            COMMON/SPCSD4/XE4 (2), YE4 (2), ISD4
            COMMON/REGION/S1,52,S3,S4
            COMMON/STATCS/NS;NEF1,NEF2
C CHECK FOR SPECIAL CASE I.E CONTOUR LINE CROSSES SIDE TWICE
    IS \(1=0\)
    152=0
    IS3 \(=0\)
    IS4 \(=0\)
    DO 2 I \(1=1,4\)
        IF(IESID(I1).EQ.1) ISI=IS1+1
        IF(IESID(I1).EQ.2) IS2=IS2+1
        IF(IESID(I1).EQ.3) 1S3=1S3+1
        IF(IESID(I1).EQ.4) IS4=IS4+1
2
    CONTINUE
    IF(IS1.EQ.2) GOTO 1
    IF(IS2.EQ.2) GOTO 3
    IF(IS3.EQ.2) GOTO 4
    IF(IS4.EQ.2) GOTO 5
6
    RETURN
C TWO EXIT ON SIDE 1 EXAMINE LIMIT
1 IF (YY1.EQ.S2) RETURN
    GOTO 11
C TWO EXIT ON SIDE 2 EXAMINE LIMIT
3 IF(Y(2.EQ.S4) RETURN
    GOTO 17
```

C TWO EXIT ON SIDE 3 EXAMINE LIMIT
4 IF(XX1.EQ.S1) RETURN
GOTO 11
C TWO EXIT ON SIDE A EXAMINE LIMIT
5 IF(XX2.EQ.53) RETURN
C CHECK FOR RODT DETECTION FOR TOP \& ADJACENT RECTANGLE
17 IF(IS2.EQ.2) F1=F(XX1;YY2)-CONT
IF(IS4.EQ.2) F1=F(XX2;YY1)-CONT
ISNI=1
IF(F1.LT.O.)ISNI=-1
F2=F(XX2,YY2)-CONT
ISN2=1
IF(F2.LT.O.)ISN2"-1
IF(IS2.EQ.2)YMAX1 =2*YY2-YY1
IF(IS4.EQ.2)XMAX1=2*XX2-XX1
IF (IS2.EQ.2)F3=F(XX1:YMAX1)-CONT
IF(IS4.EQ.2)F3=F(XMAX1,YY1)-CONT
ISN3=1
IF(F3.LT.O.)ISN3=-1
IF(1S2.EQ.2) F4=F(XX2,YMAX1)-CDNT
IF(IS4.EQ.2) F4=F(XMAX1,YY2)-CONT
ISN4=1
NEF2=NEF2+4
IF(F4.LT.O.)ISN4=-1
IF(ISN1.NE.ISN2.OR.ISN3.NE.ISN4.OR.ISN1.NE.ISN3.DR.ISN2.NE.ISN4)
8 RETURN
C SAVE THE EXIT POINTS SIDE 2
IF(IS4.EQ.2) GOTO 8
DO 7 12=1;10
IF(IROW2(I2).NE.2) GOTD 19
CONTINUE
IFREE=I2
DO 9 J1=1,4
IF(IESID(JI).NE.2) GOTO 9
XE2(IFREE)=XEXIT(J1)
YE2(IFREE)=YEXIT (J1)
I ROW2(IFREE)=II+1
JCOL2(IFREE)=JJ
ISD2(IFREE)=2
IFREE=IFREE+1
9 CONTINUE
RETURN
C SAVE THE EXIT POINTS OF SIDE 4
8 ISD4=4
K=1
DO 12 J2=1,4
IF(IESID(J2).NE,4) GOTO 12
XE4(K)=XEXIT(J2)
YE4(K)=YEXIT(J2)
K=K+1
12 CONTINUE
RETURN
C SAVE \& TRACE ON SIDE 1/3
11 IF(IS1.EQ.2) GOTO 22
XSAVE=XX2
XX2= XX1
XX1=2.* XX1-XSAVE
ISD4=3
GOTO 33
22 YSAVE=YY2
YY2=YY1
YY1=2.*YY1-YSAVE
ISD4=1
K=1
DO 14 J2=1,4
IF(IESID(J2).EQ.1.OR.IESID(J2).EQ.3) GOTO 155

```

XE4 (K) \(=\) XEXIT (J2)
YE4 (K) = YEXIT(J2)
\(K=K+1\)
15
\(\operatorname{XEXIT}(\mathrm{J} 2)=0\).
YEXIT (J2) \(=0\).
\(\operatorname{IESID}(J 2)=0\)
CONTINUE
NEXITS=0
CALL SPCREC(ISP,II,JJ,CONT,MNSTEP,XSTEP,YSTEP,NEXITS)
RETURN
END
\(c\)
C*****************CLIP LINES OUTSIDE THE LIMIT*****************
C
SUBRDUTINE CCLIP( \(x, y\) )
c clips the line to the rectangular edge
C USING THE CONCEPT OF FINDING THE INERSECTION POINT OF
C TWO STRAIGHT LINES
COMMON/LIMIT/XX1,YY1, XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT,
8 \(X X L, Y Y L, I T R A C E\)
XDIF1 \(=X-X X 1\)
XDIF2 \(=X \times 2-X\)
YDIF1 \(=Y-Y Y 1\)
YDIF2=YY2-Y
C ANY INTERSECTION WITH EDGES ?
IF (XDIF1.LT.O. OR.XDIF2.LT.O..OR.YDIF1.LT.O..OR.YDIF2.LT.O.)GOTO
RETURN
C Compute the gradient and the constant term of the equation
C DF THE STRAIGHT LINE
1 SLOPE \(=(Y-Y Y L) /(X-X X L)\)
CONST=YYL-SLOPE*XXL
C CHECK WHICH SIDE?
IF (XDIF1.LT.O.) GOTO 2
IF (XDIF2.LT.O.) GOTO 3
IF(YDIF1.LT.O.) GOTO 4
IF(YDIF2.LT.O.) GOTO 5
RETURN
c x-direction
\(2 \quad X=X X 1\)
\(6 \quad Y=\) SLOPE \(* X+\operatorname{CONST}\)
RETURN
\(3 \quad \mathrm{X}=\mathrm{xx} 2\)
GOTO 6
\(4 \quad Y=Y Y 1\)
\(7 \quad X=(Y-C O N S T) / S L O P E\)
RETURN
C Y-DIRECTION
\(5 \quad Y=Y Y 2\)
GOTO 7
END

\section*{APPENDIX 3.2}

THE USER INTERFACE SUBROUTINES
```

C
C
C
C
C THIS IS THE INTERACTIVE PROGRAM WHICH HANDLES THE DISPLAY
C IMAGES GENERATED.IT CONSISTS OF THREE MAIN DISPLAYS:
C
C
C
C
C
C
C*************MAIN PROGRAM SEGMENT
C
COMMON/IO/IN,IOUT
COMMON/REGION/S1,S2,S3,S4
COMMON/STATCS/NS,NEF1,NEF2
REWIND }
CALL SETFIL(9;"TTYI22")
NS=0
NEF1=0
NEF2=0
IN=5
IDUT=6
C PARAMETER ENTRY DISPLAY
1 CALL CPARAM(CONTOUR;XW,YW,XSTEP,YSTEP,IG,IC)
GOTO(2,1:5),IC
C CONTOUR DRAWING
2 CALL CDRAW(CONTQUR,XW,YW,XSTEP,YSTEP,IG,IC)
GOTO(1,5:5,5,5,2,5):IC
C RUN TIME STATISTICS
5 WRITE(9,7777)NS:NEF1,NEF2
777 FORMAT("TOTAL NO. DF STEP IN TRACING=",IG/"NQ. OF FUNCTION
\& EVALUTION IN TRACING ONLY",IG/"NO. OF FUNCTION EVALUATION
\& OTHER THAN IN TRACING",IG)
CALL ALPHMD
STOP
END
C
C**************CONTOUR PARAMETER \& INTRODUSTIION DISPLAY*************
C
SUBROUTINE CPARAM(CONTQUR,XW,YW,XSTEP,YGTEP,IG,IC)
COMMON/IO/IN,IOUT
COMMON/REGION/S1,S2,53,S4
DATA MNTXT1/"+ NEXT + RESTART + EXIT "/
DATA MNTXT2/"+CON.LEVEL + REGION + G.WIDTH
\& + X,Y-STEP + DISP.GRD"/
LOGICAL*1 MNTXT1(30),MNTXT2(90)
C INITIALISATION
CALL TXOPEN
1 CALL TXCLER
ICONT=0
I REG=0
IWIDTH=0
ISTEP=0
IG=0
C OUTPUT DISPLAY INSTRUCTION
CALL TEXTUP("CTXT",10)
CALL CURPOS(1.,510.):

```

WRITE(IDUT, 20)
FORMAT("CONTOUR PARAMETER:-"//)
WRITE(IOUT,30)
30 FORMAT("i-CONTOUR LEVEL TO BE TRACED INITIALLY:-"//
"2-REGION COORDINATES(BOTTOM L.H. \& TOP R.H.)"/
" ENTER MINIMUM(X,Y) \& MAXIMUM(X,Y) :-"/
"3-RECTANGULAR GRID SIZE FOR REGION"/
" DISCRETISATION. ENTER X-WIDTH \& Y-WIDTH :-"/
"4-STEP LENGTH USED IN TRACING THE CONTOUR",
" LINE. ENTER X-STEP \& Y-STEP:-",
"5-DISPLAY GRID LINES :-"//
"NOTE:-NDRMALY \(X, Y-S T E P<X, Y-W I D T H\langle R E G I O N ~ S I Z E " /\)
"* DEFAULT VALUES: REGION SIZE = 15*WIDTH"/
"
WIDTH = 10*STEP")
CALL MNOPEN(875.,715.,1)
CALL MNDISP (MNTXT1,3,10,1)
CALL FRAME (870.,733.,3)
CALL MNOPEN(700.,450.,2)
CALL MNDISP(MNTXT2,9,10,2)
CALL FRAME (695.,470.19)
\(\mathrm{X} 1=695\).
X2=840.
\(Y=430\).
DO 111 I1=1.4
CALL TXMOVE \((X 1 ; Y)\)
CALL TXDRAW \((X 2, Y)\)
\(\mathrm{Y}=\mathrm{Y}-40\).
CONTINUE
CALL DTEXT(850.,360.,"*",1)
CALL DTEXT(850.,320.,"*",1)
2 CALL MNPICK(J,ICHAR,MND)
IF(MND.EQ.2) GOTO 22
5 CALL CONFRM (ICHAR)
IF (ICHAR.EQ.78) GOTO 2
IF(ICHAR.NE.89) GOTO 5
IF(J.EQ.2.OR.J.EQ.3) GOTO 212
IF (ICONT.EQ.O.DR.IREG.EQ.O) GOTO 2
IF(IWIDTH.EQ.O) GOTO 77
312 IF(ISTEP.EQ.0) GOTO 88
212 GOTO(11,1,15),J
C NEXT
11
IC=J
RETURN
c CONTOUR PARAMETER
\(22 \operatorname{GOTO}(31,2,33,2,35,2,37,2,39), \mathrm{J}\)
C CONTOUR INITIAL LEVEL
31 CALL CURPOS(1.,140.)
CALL MESSAG("£ CONTOUR LEVEL? A")
READ (IN,40)CONTOUR
FORMAT (GO.0)
ICONT \(=1\)
GOTO 2
C REGION COORDINATES
33 CALL CURPOS(1.,118.)
CALL MESSAG("£ REGION COORDINATES,MIN(X;Y) \& MAX(X;Y)? ^")
READ (IN,50)S1,S2,53,S4
FORMAT (4GO.0)
IREG=1
GOTO 2
C GRID WIDTH
35 CALL CURPOS(1..96.)
CALL MESSAG("£ GRID SIZE(X-WIDTH \& Y-WIDTH)? A")
READ (IN,60) XW, YW
FORMAT (2GO.O)
IWIDTH=1
GOTO 2

C \(X / Y\) STEP
37 CALL CURPOS(1.,74.)
CALL MESSAG("£ X-STEP \& Y-STEP? ^")
READ (IN, 70)XSTEP, YSTEP
70 FORMAT (2GO.0)
ISTEP=1
GOTO 2
C DISPLAY GRID LINES
\(39 \quad\) IG=1
GOTO 2
C DEFAULT GRID WIDTH
\(77 \quad X W=(53-S 1) / 15\).
\(\gamma W=(54-52) / 15\).
GOTO 312
C DEFAULT X-STEP \& Y-STEP
88 XSTEP \(=X W / 10\).
YSTEP=YW/10.
GOTO 212
15 STOP
END
C
C**************CONTOUR DISPLAY ROUTINE******************
C
SUBROUTINE CDRAW (CONTOUR;XW,YW;XSTEP;YSTEP,IG;IC)
COMMON/REGION/S1,52,53:54
COMMON/GRID/NLX;NLY,XGRID(31),YGRID(31)
COMMON/IO/IN,IOUT
C DEFINE MENU ITEMS
DATA MNTXT1/"+ PREVIQUS + GRAPH + CURSOR *+ ZODM + GRID
8+ RESTART + EXIT "/
DATA MNTXT2/"+CON.LEVEL+ X-STEP + Y-STEP "/
DIMENSION CONLVL (11), XSTP(11),YSTP(11)
LOGICAL*1 MNTXT1(70), MNTXT2(30)
11 ICONT=1
ISTEP=1
C DRAW GRID LINES \& SET UP COMMAND MENU
CALL TXCLER
WRITE (IDUT:10)
10 FORMAT ("CONTOUR DISPLAY:-")
CALL MNOPEN (875.,715.:1)
CALL MNDISP (MNTXT1;7,10,1)
CALL FRAME (870.,733.,7)
CALL DTEXT (780.,558.,"* TYPE F- FINISH",16)
CALL MNOPEN(875.,518.12)
CALL MNDISP(MNTXT2,3;10,2)
CALL FRAME (870.;536.,3)
CALL CGRID(XW,YW,S1,52,S3,S4,IG) ' \({ }^{\prime}\)
4
CALL LMTARA
CALL MNPICK (J,ICHAR,MND)
IF (MNO.EQ.2) GOTO 22
C COMMAND CONFIRM
17 CALL CONFRM (ICHAR)
IF (ICHAR.EQ.78) GOTO 4
IF (ICHAR.NE.89) GOTO 17
GOTO (1,2,3:6,77:1,1):J
C PREVIOUS/RESTART
1 - IC=J
RETURN
C GRAPH CONTOUR LINE BY SCANNING THE WHOLE REGION
2 CALL GRAPH (XSTEP,YSTEP;XW,YW,CONTOUR,S1;S2,S3:S4)
IF (ICDNT.GT.11) ICONT=11
IF (ISTEP.GT.11)ISTEP=11
CONLVL (ICONT) =CONTOUR
ICONT = I CONT+1
XSTP(ISTEP) \(=X S T E P\)
YSTP(ISTEP) \(=\) YSTEP

ISTEP=ISTEP +1
GOTO 4
C USE CURSOR TO TRACE THE CONTQUR Line
3 CALL LMTSCL(S1,52,53,54)
IF (ICONT.GT.11)ICONT=11
IF (ISTEP.GT.11)ISTEP=11
CONLVL (ICONT) =CONTOUR
\(I C O N T=I C O N T+1\)
XSTP (ISTEP) \(=\) XSTEP
YSTP ( ISTEP) = YSTEP
ISTEP \(=1 S T E P+1\)
7 CALL TXCURS(CX,CY,ICHAR)
IF(ICHAR.EQ.70) GOTO 4
C Find the index \(J\)
J=INDEXG (CX,XGRID)
XMIN=XGRID (J)
XMAX=XGRID(J+1)
C FIND ROW INDEX
I=INDEXG(CY, YGRID)
YMIN=YGRID(I)
YMAX = YGRID (I +1)
c trace line in this rectangle
CALL RECANG (XMIN, XMAX,YMIN,YMAX,XSTEP,YSTEP,CONTOUR,I,J)
GOTO 7
c ZOOMING
6 CALL ZOOM(XW,YW,XSTP,YSTP,CONLVL,IG,ICONT,IC)
GOTO (11,5,8),IC
\(8 \quad \mathrm{IC}=7\)
RETURN
C DRAW GRID LINES
77 IG=1
CALL CGRID(XW,YW,S1,S2,S3,S4,IG)
GOTO 4
C CONTOUR PARAMETER
\(22 \operatorname{GOTO}(31,32,33), \mathrm{J}\)
C contour level
31 CALL CLEVEL (CONTOUR,ICONT)
GOTO 4
C X-STEP
32 CALL XYSTEP (XSTEP,ISTEP)
GOTO 4
C Y -STEP
33 CALL XYSTEP(YSTEP,ISTEP)
GOTO 4
5 STOP
END
C
C*************SET UP GRID LINES
C
SUBROUTINE CGRID(XW,YW,S1,S2,S3,S4,IG)
COMMON/GRID/NLX,NLY,XGRID(31), YGRID(31)
C SET VIEWPDRT \& WINDOW
CALL LMTSCL(S1,S2,S3,S4)
C HORIZONTAL GRID LINES
\(Y=52\)
NLY=IFIX((S4-S2)/YW+.5)+1
DO \(1 \mathrm{I}=1\), NLY
IF(IG.EQ.O) GOTO 11
CALL TXMOVE \((51 ; Y)\)
CALL TXDRAW (S3,Y)
\(11 \quad \operatorname{YGRID}(I)=Y\)
\(Y=Y+Y W\)
YDIF=Y-S4 :
IF (YDIF.GT.O.) GOTO 3
CONTINUE
C VERTICAL GRID L¥MES
    X=S1
    NLX=IFIX((S3-S1)/XW+.5)+1
    DG 2 I=1,NLX
        IF(IG.EQ.O) GOTO 12
        CALL TXMOVE (X,S2)
        CALL TXDRAW (X;S4)
        XGRID(I) =X
        X=X+XW
        XDIF=X-S3
        IF(XDIF.GT.O.) GOTD 4
    CONTINUE
    RETURN
    END
C
C*********** CONTOUR LEVEL *******************************
C
    SUBROLTINE CLEVEL(C,K)
    COMMON/IO/IN,IOUT
    IF(K.GT.10) K=10
    Y=450.-22.*(K-1)
    CALL CURPOS (760.,Y)
    CALL MESSAG("£ CON.LEVEL?^")
    READ (IN,10)C
10 FORMAT (GO.0)
    RETURN
    END
C
C**********DRAN COMPLETE CONTOUR LINE***************
C
    SUBROUTINE GRAPH(XSTEP,YSTEP;XW,YW,CONTOUR,S1,S2,S3,S4)
    COMMON/GRID/NLX;NLY;XGRID(31), YGRID(31)
C DRAWS CONTOUR LINE BY SCANNING THE WHDLE REGION
    CALL LMTSCL(S1;S2;S3,S4)
    NLY1 = NLY-1
    NLX1=NLX-1
    YMIN=S2
    YMAX=S2
    DO 10 I=1,NLY1
        YMIN=YMAX
        YMAX=YMAX +YW
        XMIN=SI
        XMAX=51
        DO 20 J=1,NLX1
            XMIN=XMAX
            XMAX = XMAX + XW
C DRAW SEGMENT OF THE CONTQUR LINE IN THE SPECIFIED RECTANGLE
                CALL RECANG(XMIN,XMAX,YMIN,YMAX,XSTEP,YSTEP,CONTQUR,I,J:
20 CONTINUE
10 CONTINUE
    RETURN
    END
C
C************FINDI/J INDEX***************
C
    F:JNCTION INDEXG(XY,A)
    D:MENSION A(1)
C COMPUTE THE INDEX OF THE CHOSEN RECTANGLE
    D[ 11 J 1=1,20
        XYDIF=XY-A(J1)
        IG(XYDIF.LE.O.) GOTO 12
11
    CONTINUE
    INDEXG=J1-1
    RETURN
    END
C
```



SUBRQUTINE XYSTEP(XYSP,ISTP)
COMMON/IO/IN,IDUT
IF (ISTP.GT.10)ISTP=10
$Y=230 .-22 . *($ ISTP-1)
CALL CURPOS ( $760 ., Y$ )
CALL MESSAG("£ X/Y-STEP?^")
READ (IN, 10)XYSP
FORMAT (GO.O)
RETURN
END
C
C************** ZODM PART OF THE CONTOUR LEVELS****X*********
C
SUBROUTINE ZOOM(XW,YW,XSTP,YSTP,CONLVL,IG,ICONT,IC)
COMMON/REGION/S1,S2,S3:S4
COMMON/IO/IN,IOUT
COMMON/GRID/NLX,NLY,XGRID(30),YGRID(30)
DATA MNTXT1/"+ PREVIOUS+ RESTART + EXIT "/
DIMENSION XSTP(1),YSTP(1),CONLVL(1)
LOGICAL. 1 MNTXT1(30)
C SET UP CURSOR TO PICK UP CODRDS. OF ZOOMED REGION
CALL LMTSCL (S1,52,53,54)
CALL TXCURS (ZX1,ZY1,ICHAR)
1 CALL TXCURS ( $Z \times 2: Z Y 2, I C H A R)$
IF (ZX1.EQ.ZX2.OR.ZY1.EQ.ZY2) GOTO 1
XJ1=AMIN1 (ZX1, ZX2)
XJ2=AMAX1 $(Z \times 1, Z \times 2)$
YII=AMIN1 (ZY1,ZY2)
YI2=AMAX1 (ZY1,ZY2)
$\mathrm{J} 1=\mathrm{INDEXG}(X J 1, \mathrm{XGRID})$
J2=INDEXG(XJ2,XGRID)
I1=INDEXG(YI1;YGRID)
I2=1NDEXG(YI2,YGRID)
2SCL1=XGRID(J1)
ZSCL2=YGRID(I1)
ZSCL3=XGRID(J2+1)
2SCL4 $=$ YGRID (12+1)
3 CALL TXCLER
CALL LMTARA
WRITE (IOUT,10)
10 FORMAT("ZODMING:-")
CALL MNOPEN(875.,715.,1)
CALL MNDISP(MNTXT1,3,10,1)
CALL FRAME(870.,733.,3)
CALL CGRID(XW,YW,ZSCL1,ZSCL2,2SCL3,ZSCL4,IG)
NCONT $=$ ICONT -1
DO $11 \mathrm{~K} 1=1$, NCONT XSTEP=XSTP (K1)
YSTEP $=$ YSTP (K1)
CONTOUR=CONLVL(K1)
CALL GRAPH(XSTEP,YSTEP,XW,YW,CONTOUR,ZSCL1,ZSCL2,ZSCL3,ZSCL4)
CONTINUE
CALL LMTARA
CALL MNPICK (J,ICHAR,MNO)
22 CALL CONFRM (ICHAR)
IF (ICHAR.EQ.78)GOTO 20
IF(ICHAR.NE.89) GOTO 22
$\operatorname{GOTO}(2,3,2), \mathrm{J}$
C PREVIDUS/EXIT
$2 \quad \mathrm{IC}=\mathrm{J}$
RETURN
END
C

```
SUBROUTINE LMTARA
CALL TXUPRT (0.:0.,1023.,780.) CALL TXWIND (0.,0.,1023.,780.) RETURN
END
C
C************* LIMIT GRAPHIC SCALE "WINDOW"***************
C
SUBRQUTINE LMTSCL (SCL1:SCL2,SCL3,SCL4)
CALL TXUPRT (0.:0.:750.:750.)
CALL TXWIND (SCL1;SCL2;SCL3;SCL4)
RETURN
END
C
C************** CDNFIRM THE CDMMAND*************************
C
SUBRDUTINE CONFRM(ICHAR)
COMMON/IO/IN,IOUT
CALL CURPQS (800.,750.)
WRITE (IOUT;10)
10 FORMAT("CONTINUE (Y/N)?")
CALL TXCURS (XI;Y1;ICHAR)
RETURN
END
```


## APPENDIX 3.3

THE CONTOURING ALGORITHM SUBROUTINES USING THE RECTANGULAR SUBDIVISIONS

```
* APPENDIX 3.3 *
****************
C
C
C
C THIS IS THE SECOND VERSION DF THE CONTOUR TRACING ALGDRITHM
C USING THE RECTANGLLAR CELL SUBDIVISION.
c
c
c
C****************DRAWS THE CURVE FROM AGIVEN RECTANGLE SIDE**********
c
    SUBROUTINE DCRVSD(X1,Y1,X2,Y2,XS,YS,M,N,ISIDE)
    COMMON/LIMIT/XX1,YY1,XX2,YY2,XEXIT(4),YEXIT(4),IESID(4),CONT,
                        XXL,YYL, ITRACE
        COMMON/CORNERS/CNRLT(2),CNRRT(2),CNRLB(2),CNRRB(2),ISIGNS(4)
                        ,FUN(4)
        CDMMON/STATCS/NS,NEF1,NEF2
        DIMENSION CLD(2),CRD(2),CLU(2),CRU(2)
        LOGICAL RFOUND
    C CHECK FOR SPECIAL CASE
        IT=1
        IF(ITRACE.EQ.2.OR.ITRACE.EQ.4) GOTO 33
C find single root along the given side
        CALL ROOT(X1,Y1,X2,Y2,XS,YS,ISIDE,RFOUND)
        IF(RFOUND.EQ..FALSE.) RETURN
C CHECK FOR EXIT POINTS
33 DO 2 K=1,N
        XDIF=ABS(CNRLT(1)-XEXIT(K))
        YDIF=ABS (CNRLT(2)-YEXIT(K))
        XYSTEP=XS+YS
        XYDIF=XDIF+YDIF-XYSTEP
        IF(XYDIF.LT.O.) RETURN
        CONTINUE
        IDIR=1
    C move beam to the Linear interpolated point of the first
    c base line
    C CHECK FOR SPECIAL CASE
    IF(ITRACE.EQ.2.OR.ITRACE.EQ.4) GOTO 333
    XLT=CNRLT(1)
    YLT=CNRLT(2)
    FLT=FUN(1)
    XRT=CNRRT(1)
    YRT=CNRRT(2)
    FRT=FUN(2)
    IF(ISIDE.GT.2) GOTO 22
c COMPUTE X-coordinate by interpolation along the EdGE
        X=(XRT*FLT-XLT*FRT)/(FLT-FRT)
    Y=YLT
    GOTO 212
22 X=xLT
c compute y-coordinate by interploation along the edge
    Y=(YRT*FLT-YLT*FRT)/(FLT-FRT)
212 CALL TXMOVE(X,Y)
    xXL=x
    YYL=Y
c trace the curve further in the current recrangle
333 DD 3 NSTEP=1,M
        X3=CNRLB(1)
        Y3:=CNRLB(2)
        F3:%F(X.3,Y3)-CONT
        FUN(3)=F3
        ISIGNS(3)=1
        IF(F3.LT.O.)ISIGNS(3)=-1
        x4=CNRRB(1)
        Y4=CNRRB(2)
```

FUN (4) $=$ F4
C RUN TIME STATISTICS
NEF $1=$ NEF $1+2$
NS=NS +1
ISIGNS (4) = 1
IF (F4.LT.0.)ISIGNS (4) $=-1$
CLD (1)=CNRLT (1)
CLD (2)=CNRLT (2)
CRD (1) =CNRRT (1)
CRD (2) =CNRRT (2)
CLU (1) =CNRLB (1)
CLU(2) $=$ CNRLB (2)
CRU (1) =CNRRB (1)
CRU (2) =CNRRB (2)
ICASE=0
C TEST FQR WHICH SIDE CURVE CROSSES AND TEST FOR DEGENERATE
C CELL (ICASE=6)
IF(ISIGNS(3).NE.ISIGNS(4)) ICASE=ICASE+1
IF (ISIGNS (1).NE.ISIGNS(3)) ICASE=ICASE+2
IF(ISIGNS(2).NE.ISIGNS(4)) ICASE=ICASE+3
IF (ICASE.EQ.6) GOTO 4
GOTO (10,20,30), ICASE
C CURVE PASSES OUT OF TOP OF CELL
$10 \quad$ FL=FUN(3)
FR=FUN (4)
CALL DLINE (CLU;CRU,CLD,CRD;XL,YL,FL,FR)
ISIGNS (1) =ISIGNS (3)
FUN(1)=FUN(3)
ISIGNS (2) =ISIGNS (4)
$\operatorname{FUN}(2)=F \operatorname{UN}(4)$
IDIR=1
GOTO 7
C CURVE PASSES DUT LEFT HAND SIDE OF CELL
$20 \quad F L=F U N(1)$
FR=FUN(3)
CALL DLINE (CLD,CLU,CRD,CRU, XL,YL,FL,FR)
ISIGNS (2)=ISIGNS (3)
FUN(2) $=\mathrm{FLUN}(3)$
IDIR=2
GOTO 7
C CURVE PASSES OUT OF RIGHT HAND SIDE DF CELL
$30 \quad F L=F U N(4)$
FR=FUN (2)
CALL DLINE (CRU,CRD,CLU;CLD; XL,YL,FL,FR)
ISIGNS (1) =ISIGNS (4)
$\operatorname{FLN}(1)=F \operatorname{UN}(4)$
IDIR=3
$7 \quad X L D 1=X L-X X 1-0.001$
$X L D 2=X \times 2-X L-0,001$
YLDI $=Y L-Y Y 1-0.001$
YLD2 $=Y Y 2-Y L-0.001$
C REACHED THE EDGE THE RECTANGLE
IF (YLD1.LT.O..OR.YLD2.LT.O..OR.XLD1.LT.O..OR.XLD2.LT.O.) GOTO ؛
3
CONTINUE
RETURN
C SET EXIT POINTS
8 IF(IT.EQ.1) GOTO 31
$N=N+1$
C MARK EXIT POINT SIDE FOR SPECIAL CASE WRITE (9,7777) MSTEP
7777 FORMAT (I3)
IF (YLD1.LT.O.) IESID(N) =1
IF (YLD2.LT.O.) IESID (N) $=2$
IF (XLD1.LT.O.) IESID $(N)=3$
IF (XLD2.LT.O.) IESID $(N)=4$
$\operatorname{XEXIT}(N)=X L$
YEXIT $(N)=Y L$ RETURN
$I T=0$
GOTO 3
31

C ICASE=6
4 GOTO (10,30:20), IDIR RETURN
END
C
C************DRAW STAIGHT LINE IN A CELL $* * * * * * * * * * * * * * * * * * *$
C
SUBROUTINE DLINE (CNRL, CNRR,CNROL,CNROR,X,Y,F1,F2)
COMMON/CORNERS/CNRLT (2), CNRRT (2), CNRLB (2), CNRRB (2), ISIGNS (4) , FUN (4)
COMMON/LIMIT/XX1,YY1;XX2,YY2,XEXIT (4),YEXIT (4),IESID(4), CONT, $X X L, Y Y L, I T R A C E$
DIMENSION CNRL (1) :CNRR (1), CNROL (1), CNROR (1)
XLT=CNRL (1)
YLT=CNRL (2)
XRT=CNRR (1)
YRT=CNRR(2)
XDIF=XRT-XLT
IF (XDIF.EQ.O.) GOTO 2
$X=(X R T * F 1-X L T * F 2) /(F 1-F 2)$
$Y=Y L T$
GOTO 22
2
22
$Y=(Y R T * F 1-Y L T * F 2) /(F 1-F 2)$
CALL CCLIP $(X, Y)$
$X X L=X$
YYL $=Y$
CALL TXDRAW $(X, Y)$
DO $1 \mathrm{I}=1,2$
CL=CNRL (I)
CR=CNRR (I)
COL=CNROL (I)
COR=CNROR (I)
CNRLT (I) $=$ CL
CNRRT(I)=CR
CNRLB(I)=2.*CL-COL
CNRRB(I) $=2 . * C R-C O R$
1 CONTINUE
RETURN
END
C
C*********FINDS ASINGLE RODT ALONG THE SIDE OF RECTANGLE********
C
SUBROUTINE RODT ( $X 1, Y 1 ; X 2, Y 2 ; X 5, Y S, I S I D E, R F D U N D)$
COMMON/LIMIT/XX1;YY1;XX2,YY2,XEXIT(4),YEXIT(4),IESID(4), CONT,
8 $X X L, Y Y L, I T R A C E$
COMMON/CORNERS/CNRLT (2), CNRRT (2),CNRLB (2),CNRRB (2), ISIGNS (4) , FUN (4)
COMMON/STATCS/NS;NEF1,NEF2
LOGICAL RFOUND
C TEST WHETHER THE CONTOUR LINE INTERSECT THE EDGE?
$\left.F_{1=F}=X_{1} ; Y_{1}\right)-C O N T$
$F \operatorname{LU}(1)=F 1$
ISIGNS (1)=1
IF(F1.LT.O.) ISIGNS(1)=-1
$F 2=F(X 2, Y 2)-C O N T$
$F U N(2)=F 2$.
C RUN TIME STATISTICS
NEF2=NEF2+2
ISIGNS (2) $=1$
IF (F2.LT.0.)ISIGNS (2.):- - :

C IF THE CONTOUR LINE DOES NDT INTERSECT RETURN WITH FALSE C VALUE

IF(ISIGNS(1).EQ.ISIGNS(2)) GOTO 1
RFOUND=. TRUE.
IF(ISIDE.GT.2) GOTO 2
NINTS $=$ IFIX $\left(\left(X_{2}-X_{1}\right) / X 5+.5\right)$
WINT $=\left(\times 2-x_{1}\right) /$ NINTS
GOTO 3
$2 \quad$ NINTS=IFIX( $Y 2-Y 1) / Y S+.5)$
WINT $=(Y 2-Y 1) / N I N T S$
$3 \quad$ INTLR $=0$
INTRR=NINTS
$7 \quad$ INTC=IFIX((INTLR+INTRR)/2+.5)
IF(ISIDE.GT.2) GOTO 8
W=X1+INTC*WINT
$F W=F(W, Y 1)-C O N T$
GOTO 9
$8 \quad W=Y 1+I N T C * W I N T$
$F W=F(X 1, W)-C O N T$
9 ISIGNC=1
IF (FW.LT.O.) ISIGNC=-1
IF(ISIGNS(1).EQ.ISIGNC)GOTO 11
INTRR=INTC
FUN(2) =FW
C RUN TIME STATISTICS
$111 \quad$ NEF2=NEF2+1
IF((INTRR-INTLR).GT.1) GOTO 7
C SET CORNER COORDINATES DF THE SIDE
GOTD (10,10,20,20),1SIDE
11 INTLR=INTC
FUN(1)=FW
GOTO 111
C SIDE 1 OR 2
10. IF(ISIDE.EQ.1)YSS=YS

IF(ISIDE.EQ.2)YSS=-YS
CNRLT (1) =X1+INTLR*WINT
CNRLT (2) $=\mathrm{Y} 1$
CNRRT (1) = CNRLT (1) + WINT
CNRRT (2) $=$ Y 1
$\operatorname{CNRLB}(1)=\operatorname{CNRLT}(1)$
CNRLB (2) $=\mathrm{Y} 1+\mathrm{YSS}$
$\operatorname{CNRRB}(1)=\operatorname{CNRRT}(1)$
$\operatorname{CNRRB}(2)=\mathrm{Y} 1+\mathrm{YSS}$
RETURN
C SIDE 3 OR 4
20 IF(ISIDE.EQ.3) XSS=xS
IF(ISIDE.EQ.4) XSS=-XS
CNRLT(1) $=\mathrm{X} 1$
CNRLT(2) $=\mathrm{Y} 1+$ INTLR*WINT
CNRRT (1) $=\mathrm{X} 1$
CNRRT (2) $=$ CNRLT (2) + WINT
$\operatorname{CNRLB}(1)=\times 1+\times 5 S$
CNRLB (2) $=$ CNRLT (2)
$\operatorname{CNRRB}(1)=\times 1+\times 55$
$\operatorname{CNRRB}(2)=\operatorname{CNRRT}$ (2)
RETURN
C ROQT NOT FQUND
1 RFOUND=.FALSE.
RETURN
END
C
C************ CHECK SPECIAL CASE \& PDOCESSES**********************) C


COMMON/SPCSD4/XE4(2),YE4(2), ISD4
COMMON/CORNERS/CNRLT(2),CNRRT (2),CNRLB(2),CNRRB(2),ISIGNS(4),
IF(ISD2(K).NE.2) GOTO 1
IF(IROW2(K).EQ.II.AND.JCOL2(K).EQ.JJ) GOTO 5
CONTINUE
IF(ISD4.EQ.4.OR.ISDA.EQ.I.OR.ISD4.EQ.3) GOTO 4
ISP $=0$
RETURN
C TOW EXITS ON SIDE 2 , ESTABLISH A CELL ALD TRACE CURVE
5 DO $8 \mathrm{~L}=1,2$
CNRLT (1) $=\mathrm{XE} 2(K)-X S T E P / 2$.
CNRLT (2) =YE2(K)
$\operatorname{CNRRT}(1)=\mathrm{XE} 2(K)+X S T E P / 2$.
CNRRT (2) = YE2 (K)
$\operatorname{CNRLB}(1)=\operatorname{CNRLT}(1)$
CNRLB(2) $=$ YE2 (K) CYSTEP
CNRRB(1) $=\operatorname{CNRRT}(1)$
$\operatorname{CNRRB}(2)=\operatorname{CNRLB}(2)$
XLI $=$ CNRLT ( 1 )
YLI $=$ CNRLT (2)
FLI=F(XL1;YL1)-CONT
FUN(1)=FL1
ISIGNS (1) $=1$
IF(FLI.LT.O.) ISIGNS(1)=-1
$X R 1=\operatorname{CNRRT}(1)$
YR1 $=$ CNRRT (2)
FR1 $=F(X R 1 ;$ YR1 $)-C O N T$
FUN(2)=FR1
NEF2=NEF2+2
ISIGNS (2)=1
IF(FRI.LT.O.) ISIGNS(2)=-1
IF(ISIGNS(1).NE.ISIGNS(2)) GOTO 117
FDIF=ABS (FL1)-ABS(FR1)
IF(FDIF.LT.0.)ISIGNS(1)=-ISIGNS(1)
IF(FDIF.GE.O.)ISIGNS (2) $=-\operatorname{ISIGNS}(2)$
117 CALL TXMOVE (XE2(K),YE2(K))
ITRACE $=2$
CALL DCRUSD (XX1;YY1,XX2,YY2,XSTEP,YSTEP,MNSTEP,NEXITS,2)
ISD2 (K) $=0$
$\mathrm{K}=\mathrm{K}+1$
CONTINUE
ITRACE $=0$
IF (ISDA.EQ.4)GOTO 4
GOTO 10
C TWO EXIT ON SIDE 4/3/1
4 DO $9 \mathrm{~L}=1,2$
IF(ISD4.EQ.1) GOTO 44
$\operatorname{CNRLT}(1)=\mathrm{XE} 4(\mathrm{~L})$
CNRLT(2)=YE4(L)-YSTEP/2.
CNRRT (1) =XE4 (L)
CNRRT (2) $=\mathrm{YE} 4(L)+Y S T E P / 2$.
IF (ISD4.EQ.4) CNRLB(1)=CNRLT (1) +XSTEP
IF (ISD4.EQ.3)CNRLB(1)=CNRLT(1)-XSTEP
CNRLB (2) $=$ CNRLT (2)
$\operatorname{CNRRB}(1)=\operatorname{CNRLB}(1)$
$\operatorname{CNRRB}(2)=\operatorname{CNRRT}$ (2)
GOTO 77
CNRLT (1) =XE4 (L)-XSTEP/2.
CNRLT (2) =YE4 (L)
$\operatorname{CNRRT}(1)=\mathrm{XE} 4(L)+X S T E P / 2$.
$\operatorname{CNRRT}(2)=Y E 4(L)$

```
        CNRLB(1)=CNRLT (1)
    CNRLB(2)=YE4(L)-YSTEP
    CNRRB(1)=CNRRT (1)
    CNRRB (2)=CNRLB (2)
    XL1=CNRLT(1)
    YL1=CNRLT (2)
    FL1=F(XL1;YL1)-CDNT
    FUN(1)=FL1
    ISIGNS (1)=1
    IF(FLI.LT.O.) ISIGNS(1)m=1
    XR1=CNRRT(1)
    YR1=CNRRT(2)
    FR1=F(XR1;YR1)-CONT
    FUN(2)=FR1
    NEF2=NEF2+2
    ISIGNS(2)=1
    IF(FR1.LT.O.) ISIGNS(2)=-1
    IF(ISIGNS(1).NE.ISIGNS(2)) GOTO 17
    FDIF=ABS(FL1)-ABS (FR1)
    IF(FDIF.LT.O.)ISIGNS(1)=-ISIGNS(1)
    IF(FDIF.GE.0.)ISIGNS(2)=-ISIGNS (2)
    CALL TXMOVE (XE4(L),YE4(L))
    I TRACE=4
    CALL DCRVSD(XX1,YY1,XX2,YY2,XSTEP,YSTEP,MNSTEP,NEXITS,ISD4)
CONTINUE
ISD4=0
ITRACE=0
ISP=1
RETURN
END
```


## APPENDIX 4

TMG - PROGRAM LISTING

## APPENDIX 4.1

TMG - BATCH PROGRAM

```
JWB EAKIH,GU,HH7OLI9
LUFORTRAN
RUN \therefore1OGO
VHLUME 10000
```

```
****
OHCUMEAT SOURCE
    PKOGRAlI(M352)
    CUHPALT
    OUTPUT 2 = I.PO
    OUTPUT 7 = TPO
    INFUT ? = CRO
        CO|IPHESS INTLGER AND LOGICAL
        USE SE/ARRAY
    ENO
    MASTEK POISSOR
    LUGICAL ERRORFI,AXHEAT,AXMAG,PLOT MESH,INT
    INTEGLR TYDE,EIT,PARITY,TAG
    COH,1Of:/KLP/KMAX, LNAX,PARITY
    CURHON/STAGE/NPROO,IP
    CUHI;ON/ERUR/ERRORM
    COHIION/TP/TYPE,AXMAG,AXHEAT
    COHi|ON/SC/ZS,RS
    CUf'ION/INOX/I1,12,13,14,K1,K2,IAI:IB,IC,L,MM',JJ(7),IR,INT
I/S:/GM(200),TITLE(80)
IVBLKT/AINTEGRAL,M(2),RR,TRNGL,SOURCE;COEFF,NN(2),A,B,C,T4,HP,FPIS
    DIHENSION PHI(650),TAG(650),CPU(650),CPR(650),CPL(650),SCT(650)
    1.K(650),2(650)
    1,GUF(10), REGC(10,4),FILENAME (2),PICNAME (2)
    READ(1,1)NPROE
    WKITE(2,20)NPHOE
            IURMAT(4OHY THE NUMBER UF PROBLEMS ON THIS RUN IS IIS
    1/2X,3女(1HE))
        CAI.L UEFBUF(5,80,BUF)
        DO 5 1PEI/NPRCG
        WKITE(7,100)
100 FORIIAT(/////////////)
        READ (1,ó)TITLE
6 FONMAT (8OA1)
        WKITE(2,7)ID,TITLE
        FOl:HAT(1HO,22h TITLE OF PRUBLEM NO.,I2.5X
    1.8(4A1/28X.82(1Hz))
        AXHEAI, AXMAG=.FALSE.
        ERPURME.FALSE.
        REAO(1,2)PLOT MESH,NEQPTL,LS,RS
        FOM|AI(L1,4X,10,2F0.0)
        READ(1,3)NREG,NKEGC
        FUH|A| (2IU)
        CAI.L INPUT(REGC,NREG,NREGC,BUF,NPT)
        DU 25 IE1,NPT
        TAG(1)=0
        CPH(I),CPR(I),CPL(I),SCT(I),PHI(I),K(I),Z(I)=0,
        CAILL TUPLGY(REGC,NREG,NREGC'JTAG,PHI,NPT,R,Z)
        IF(ERHORM)GOTUS
            CALL MESH &ELXII(REGC,NREG,NREGC,TAG,R,Z,NPT)
        CAI.L IARAM(KEGC,NREG,NREGC,TAG,R,Z,CPU,CPR,CPL,SCT,NPT,PHI)
        CH,L WELX(TAG,CPU,CDR,CPL,SCY,PHI,R,Z,NPT)
        CAIL PLOTT(R,Z,PHI,TAG,NPT,NEQPTL,PLOT MESH)
        cul!Tilue
        STOP
```

        FUl:IAA (10)
        EWN
        SUI:ROUTINL INFUT (REGC,NREG,NREGC'BBUF,NPT)
        LUCJCALEHD
        JNTLGLR PAKITY
        COI!iON/INUX/I,J,ICARD,JJ,M,END,IA,IB,IC,L,K,II(6),IG;IR,KK
        1/Si/GT(200), CHAR(80)/KLP/KMAX,LMAX,PARITY
        DIHLISION REGC(NREG,NREGC)
            LIMENSIUN BUF(IO)
    C KEAD I:UMGER UF CULUMNS AND KOWS: ALSO THE IIESH PARITY(OI L//Z), (+1 $k$
READ(1,1)KMAX, LMAX, PARITY
$N P T=(A N A X+1) *(L M A X+1)$
C CALCULATL HHHEER OF POINTS IN MESH
WRITE(2, 2U)NPT, KMAX, LMAX, PARITY
FOLIIAI (1HU, 8O (IH由)/37H THE TOTAL NUHBER OF MESH POINTS IS ,IS.
1131I. THEKE AKE ,13.8H CULUMNS/8H AND , I3.
1281 KUWS, THE MESH PARITY (S ,13/80(1H*))
$1 \mathrm{G}=1$
1CNKD $=$ ?
10 OO 50 JRET,NREG
CUNSTANTS FUK RLGION ANO DEFINING BOUNDARY POINTS ARE READ IN
READ (1,5) (REGC(IR,I),I』1,NREGC)
CAI.L GEOMETRY(BUF)
SO CONTIPUE
RETURA
1 FUISTIAT(3IU)
2 FOHRAI (4IU)
5 FORMAI (4EO.0)
ENO
GUEKOLTINE GEUHETRY(BUF)
LOGICAL END
COHIOON/INDX/I,J,ICARD,JJ,M,END,IA,IG,IC,L,K;II(G),IG,IR,KK
I/ST/GM(2QU), CHAR (80)
DIILNSION COUAT (10), FMT (5), SNTL(3), BUF(10)

15HX, ,5HAI) , 5HEO.O).
$15 \mathrm{HA}, 5 \mathrm{HB}, 5 \mathrm{HG}, 5 \mathrm{H}$, 5H(
C A CAIID MAY bE MISSING AT THIS POINT
C FREE IIELD RUUTIGE;OBIECT-TIME FORMATS SET UP FOR ALPHANUMERIC FIELD
SU READ (1,1)BUF
1 FUEMAT (1OA8)
REAU(S, 2)CHAR
WRITE (2, 6U) ICARD, CHAR
2 FOHIIAT (8OA1)
OU FOKTIAT(10H CAKD NO., I4, bX,1H(,8OA1,2HY))
1CARDEICARD+1
$I B=9$
$J J=1$
ElDE. FALSE.
FHT (1) FALEFT
DO $45 \quad I=1,80$
CALL LUHP女(CHAR (I), BLANK,J)
GUTU(4U,5) J
$3 \quad G U \cdots(1 \cup, 55)$ IR
$10 \quad I B=2$
DO $15 \quad K=1,3$
CAI.L VUAPG(CHAK(I),SNTL(K),J)
GU'iU( $<0,15) \mathrm{J}$
CORTITUE

```
    L={
    FMT(5)FEFLD
    GO"U2%
    IF(K.LU:3)ENDA.TRUE.
    FIT(5)=AFLD
    L=?
    J=1/10
    FHT(4)=XFLD
    IF:J,NE.O)GOTUZS
    FHT(2)=BLANK
    IF!1.NE.1)G|TU30
    FMT(3) =BLANK
    FHY(4)=0LANK
    G0:40)
    F11`(3) =COUNT(%)
    GOTUGS
    M=&-J*10
    IF(11)100,100.105
    FHT(2)=COUNT(J)
    FMT(3)=COUNT(10)
    GUTU6S
        FH,T(2)=COUNT(J+1)
        FMT(3) =COUNT(A;)
    READ(S,FMT)GM(IG)
    IG=IG+1
    IF(END)RETURN
    GOTUS%
    IF((I~JJ).GT.1)IBEI
    GOTU&
    JJ=】
    CO|TINUE
    guTUSO
    FND
    SUEKOLTINE COUE(I,J,PHI,IG,SAME)
    LOGICAL SAME
    COHIOH:/ST/GH(20G),TEMR(80)
    DATA GHDRY/SHE
    CAL.L CUMPB(GNDRY,GM(16),11)
    IFIII,EQ:2)RETURN
    SAllEE,FALSE.
    IF(GM(IG+1).LT.O_OR.GM(IG*2).LT.O.)SAME=.TRUE.
    ImABS(GM(DG*1))
    JaABS(GM(1G*2))
    PHI=GM(IG*3)
    IGFIG*&
    RETURN
    END
        SUGRUUTINE TUPLGY(REGC,NREG,NREGG,TAG,PHI,NPT,R,Z)
        LOGICAL EHROR,SAME,SAMEO
        INTEGLR BIT,ARCFIN,PARITY,PK(6),TAG(NPT)
        COHIFOH/ST/GM(2OO), TEMP(80)/KLP/KMAX,LMAX,PARITY
        CU|IION/ERUR/EKRGR
        I/ITLXI11,12,13,1G,15,16,IA,IB,IC:L,K,PK,IG,IR,ARCFIN
        I/BLK1/L1,L2,KI,K2,R1,RZ,Z1,ZL,LO,KO,RO,ZO,PHIO,PHIIOPHI2,PHIAV
        I/LLKZ/GAOIKAO,RAO,ZAO,THETAO,LAZ,KAZ,RAXIS,ZAXISSKK%THETA,IAS,IAG
    DIHEHSION REGC(NREG,NREGC),R(NPT),Z(NPT),PHI(NPT),A(2)
    DATA ARC SEHTL,END GEOM,A/SHA .5HG ,SHFREE ,SHFIXED/
    IT!|) =1m2*(1/2)
    1G=1
C KEGH. LOLPP:
```

```
    DU 14% IRF1.NREG
    10,J0.11'%\2m1
    PHIORO,
CHECK FOL: THE TYPE OF BOUNDARY IF INDICATED.
    CALL CODESIO,NO,PHIO.IG,SAMEO)
        15=10
        1O=j0
        PHIAV,PHIZ,DHIGOPHIO
C CHECK IF ARC COMMENCES AT FIRST PT.:
        CALL COMPY(GM&IG),ARC SENPLİII)
        IF(II.EGFZ)GO TO 30
        I2=2
        IGEIG*1
C FIRST REGN, PT:
30 LT.LOFGM(IG)
        K1,KOFGM(IG*1)
        R1,RO*GM\\G*2}
        21,20FGM(1G+3)
        WRITE(2,505)IR,L0,K0, 10,20,A(16),A(I5),PHIO
505 FOKMATS2OHO FIRST PY OF REGION ,13,2X,3H (,2I3%
    |2F12F6,2X,A8, 2X,A8,3X,F12,6;1H))
        WR!TE(2,501)
    501 FORMAT(17H SUESEQUENT PTS:)
    34 1GEIG*4
C CHECK FOK SUCCEEDING ARCS&
        CALL COMP&(OM(IG),ARC SENTLOII)
        IF(I}.EQ#2) GOTO 31
        11=3
        G0TO30
        ALSU FOK END OF REGN. GEOMI
39 CALL COMPB(GM(IG),END GEOM,ID)
        IF(II.EQ:2)00 10 60
        11m2
36 IGmIG*I
40 IF(11.NEN2)00Y045
        L2ELO
        K2akO
        R2mR0
        22F=20
        15=10
        16EJ0
        PHL2=WHIO
        IF(SAMEO\PHIGOPHI2
        GOTG&8
    45 CALL CODE(IS,I6,PHI2,IG,SAME:
    IF(SAME)DHI&#PHI2
    IF(I2,EQwR)OOTO200
    L2=GM(IG)
    K2FGM(JO&1)
    R2=GM(1G+2)
    22=GM(IG*3)
    WK1TE(2,502)LR,K2,R2,22,A(16),A(15),PHI2
502 FOHHAT(SX,2I4,5X,2F12,6,2X,A8, 2X,A8,5X,F12.6)
C LINEAKK INTEKPOLATION OF BOUNDARY POINTSI TAGGING OF POINFS AND SIDES
48 CALL USET(R,Z,PHI,TAGENPY)
    IF(ERKOR)RETURN
    GOTO(S4,55,190)I1
CELLS ARE TAGGED WITH THEIR APPROPRIATE REGION NUMBERS.
55 CALL SET KEGIUN(REGC,NREG,NREGC,TAG,PHI,R,Z,NPT)
    IF(ERKOR)KETUKN
```

```
145 CONTINUE
            RFTUKN
    IG=IG*4
    CAI.L ARCSET
    IF(ERKOR)HETURN
    CAIL ARC(TAO,PHI,R,Z,NPT)
    IF(ERKORJRETUKN
        GOTOSG
    END
    SUEKOLTINE GSEP(R,Z,PHI,TAG,NPT)
    LOGDCAL EKROR
    INTEGER BIT,ARCFIN,PARITY,PK(6),TAG(NPT)
    INTEGER BT(5)
        COHMON/ST/GM(500),TEMP(80)/KLP/KMAX,LMAX,PARITY
    A/INOX/I1,I2,IS,IG,I5,IG,IA,IB,ICIL,K,PK,IG,IR,ARCFIN
    A %LKY/L1,L2,K1,K2,R1,R2,21,22,LO,KO%RO,ZO,PHIO,PHI1%PHI2,PHIAV
    IYSTAGE/NPROB, IP/EROR/ERROR
    DIHENSION PHI(NPT),R(NPT),Z(NPT)
    IT(1)п1-2*(1/2)
5 L21mL<nL{
    K21#KKmK1
    1BE1
    L!K=1
CHECKING OF PERMITPED LOGICAL LINES IS CARRIED OUT UNTIL LABEL 25.
    IF(L21.LE.0)L[日I
    IF(K21,LE.0)KMEI
    IF(L21,NE,O) 1BNIB#1
    IF(K21.NE,0)I&周IB+2
    GOTO(250,20.30.25)18
    IF((KC1-(L2+1)/2+(L1+1)/2),NE,0)1F(K21+L2/2-L1/2)400%20,400
    INC#(KMAX*T)*L
    LMTEL&T
    G0T03S
    INCiK
    LMTmKぐ
    1BEIB-1
    LMTGIAGS(LMT)
    IAEL2*(KMAX*1)*K2*1
    R(1A)ER2
    Z(IA)EZ2
    PHI(IA)&PHI2
    PHIAVEPHIAV&PHI(IA)
    13=13+1
C TAG A HOUNDARY POINTE DIRICHGETE2I FREEEIJ
    CALL FACK(TAG(IA),I5,1)
    IF(K21)40,45,60
45 IF(IT(L2))60,00,40
C TAG A SIDE ON THE BOUNDARY(UPPER自1;LOWERE2, BOTHW3)
40 IF(L21,NE,0)CALL PACK(TAG(1A),1+(1+L)/2,4)
60 IF(LMT.EQ,I)GUTO180
    R21%(K2mR1)/LNY
    221F(62-21)/LMT
    P2\F(FHI2mPHI\)/LMT
C IN THIS LUUP PERFORM AFOREMENFIUNED TAGGING OF POINTS AND SIDESI ALSO
C INTERPOLATE COORDINATES AND POIENTIALS FOR INTERMEDIATE POINTSOF LINE
    DO 105 1CE|,LM%-9
    IA=IANINC
    IF(IB,EQ:3)IAM|A+IT(IC+L&)m(K+1)/2
```

```
        CALL VACK(TAG(IA),I6,1)
        GUTU(40.100.85)IB
        CALL HACK(TAG(IA), 2-IABS(K+L)/2,4)
        GOTOTGO
        IF(IT(IC+L2).GT,0)CALL PACK(TAG(IA),3,4)
        R(IA) =K2-1C*R24
        Z(IA)=22rlC#2##
        PHI(IA)=PHI2-1C*P21
        PH!AVEPHIAV*PHI(IA)
        I3=13+1
        CONTINUE
        IF(K21)130,120.110
        IF(1T(L.1)130,130,110
        IA=L1 1*(KMAX*1)*K9*1
        TAG A SIDE
        IF(L21.NE,O)CALL PACK(TAG(IA),1+(1-L)/2,4)
        R1=R2
        Z1=22
        L1=L2
        K1mk2
        PH11aHHI2
135
    ARGFTH=O
    RETURN
```



```
C ERROK PKINTS)%
210 WKITE(2,1)
    FORHAT(&OHY CUNN, ARCS ,SAME L AND K, DIFF. COORDS)
    EKKORE.TRUE.
    RETURN
    G0 TO (251.135,252)11
        IF(ARCFIN.EG,O)GO TO 251
        IF(ABS(R2-RI).GT.1,E-12,OR,ABS(Z2-Z1).GT.1.Em12)GOTO210
        RETURN
        WRITE(2,2)L1,L2,K1,K2
        FOKHAT(12HY NO NEW K,L,13H L1,L2;KM,K2W,413)
        ERHORE.TRUE.
        RETURN
400 WRITE(2,3)L9,L2,K1,K2
3 FOBMATS38HG LY,KI AND LZ,KZ NOT ON SAME LOG, LIN/
        1 13H L1,L2,K1,K2%,413)
            ERRORF,TRUE.
            GETURN
            END
            SUQROUTINE ARCSET
            LOGICAL ERROR,SAME
            INYEGER SW(G),ARCFIN,AARITY
            COMHON/ERUR/EWROR/STAGE/NPKOB,IP
        I/ST/GM(500),TENP(80)/KLP/KMAX,LMAX,PARITY
        |/IHDX/11,12,13,14,15,16,1A,1B,1C#L,K,SW,IG,IR,ARCFIN
        1/BLK1/L1,L2,KI,K2,R1,R2,21,ZL,LO,KO,RO,ZO,PHIO,PHI1IPHIZ,PHIAV
        IYEI.KZ/LAO,KAO,RAO,ZAO,THETAO,LAZ,KAZ,RAXIS,ZAXIS'ZKK'TTHETA,IAS,JAG
            IT(!)m|m2*(1/&)
            HFFI=1.5707063
C PKEPARE INPUT FUR ARC)
C LOG& (CENTRE OF ARC)
Z(10 LAGEGH(IG)
    KAQ=GM(IG+1)
C LOG: ANGLES
    THETAUEHFPI*GM(1G*2)
    IFITHETAO)205,600.210
```

205 thetauamthetau
GW（6） $2 \cdot 2$
GOTUZ1s
SW（6）$=1$
21.0

IGCFIG＊3
CALL CODE（15．16．PHI2．IGC，SAME）
tasals
IAGA16
15．16F1A6
1GEIGCM3
IF（SAME）PHITMPHI2

LAZaGM（10＊3）
KAZロCH（IG＊4）
14日1
IF（LAO，EQ．L1）16mI4＊
IF（PARITY．LT．0）I4EI4＋2
IF（IT（14）．NE．O）GOTO219
KK＝KAZ
IF（KAU．NE．KA2）G0T0495
GOTOZA1
29 IF（KAO．NE．K1）0070415
KKEK9
IF（LAO，NE．LA2）GOT0405
CalCulate point coordinates at logical centre of the arcif also， CALCULATE LENGTHS OF SEMI AXESISET INITIAL POLAR ANGLE．
221 GOTO（2201225．825．220）14
220 RAORR？
ZAOPGM（16＊6）
THETADO．
RAXISEGM（IG＊S）
ZAXIS＝Z1
cot0230
225 RAGGM（IG＊5）
2AQ日z1
RAXISERI
THETAEHFPI
ZAXISEGM（10＊6）
C ERROR CHECKS
230 RAXISERAXISmRAO
ZAXISEZAXIS＝ZAO
IF（LAL，EQ，LT）GOT0420
IF（KAZ，EQ，K9）GOTOG25
IFSPAKITY，EQ．OSGOTO430
RETURN
400 WRITE（2，401）
401 FORHAT（16H9 ZERO ARC ANGLE）
gorosuo
405 WKITE（2，406）LAO，LAZ
406 FORHAT（1RH9 LAO，NE．LAZ，214）
GOTOSUO
415 WRITE（2．416）KK，KAO
416 FORIIAT（15H1 IN ARC，KK，KAO，212）
gotosuo
420 WRITE（2，429）LA2
421 FUKHAT（15H9 Ih ARC，LA2＝L1，I2）
gotusue：

WKITE（2，426）KA2
FOHAAT（16H1 IH ARC，KA2mK1m，12）
GUTU500
430
431
500
FUHHA？（13HY ZERO PARITY）
ERKOKE．TRUE．
RETURIF
END
SUGROUTINE ARC（TAG，PHI，R，Z，NPT）
LUGICAL ERROR
INTLGER BIT，ARCFIN，PARITY，SW（6），TAG（NPT）
COI；NUN／ST／GM（500），TEMP（80）／KLP／KMAX，LMAX，PARITY

IY $O L K Z / L A O, K A O, R A O, Z A O, T H E T A O, L A Z, K A Z, R A X I S, Z A X I S$ IFKKITHETA，JASJIAG
IAIHDX／I1：12，IS，I4，15，I6．IA，IB，ICIM，N，SW，IG，IRIARCFIN
CUHION／EROR／ERROR
DIMENSION PHI（NPT），R（NPT），Z（NPT）
COHHON／STAGE／WPROB．IP

IT（1）\＃1－2＊（1／2）
HFP1F1．5707963
L，K＝1
LTOTELA2rLT
KTOTEKAZ－KI

IF（KTUT．LI＇O）KR＝1
KTUTFIABS（KTOT）
$L 2=L 1$
LTOT： LABS （LYOT）
$K 2=K 1$
IF（LI．NE：LAO）GOTOSOO
SW（1） E 2
SW（2），SW（3），SW（4），SW（5）E1
240 LCELAZ
IF（SW（5）：EQ．2）LCWLCOL
C SET INCRLMENT IN POLAR ANGLE）－

$10=11$
CALCULATE CUORDINATES ON LOGICAL SLANT LINE OF THE ARC
$245 \quad L 2=L 2+6$
$K 2=K 2+K * I A B S((1+K) / 2 \sim 1 T(1 D))$
PHETAETHETA＊DTHETA
R2ЕRAXIS由SIN（THETA）$+R A 0$
Z2FZAXIS＊COS（THETA）$+2 A O$
CALL BSET（R，Z，PHI，TAG，NPT）
IF（ERKUR）RETURN
1DE1D＋1
IF（L2．NE：LC）GOYO245
IF（SW（1）－2）335，306．335
300
SW（9）$=1$
SW（2），SW（3），SW（4），SW（5）＝2
$306 \quad A=F L O A T(K T O T) w L T O T / 2$.
DTHETAF（2＊IT（16）－1）＊（THETAU－HFPI＊（1～PARITY）／2）／A
MX＝KTUT－LTOT／2

IF：KK，GE＊KAO．OR，KAZ．GE，KAO）GOTOS10
$H X=1 i X-(1-1 T(L A O)) 由 I T(L 2)$
GOTu31？
$370 \quad M X=f x-(1-1 T(L 己))+I Y(L A O)$

```
315
320
CALCULATE CUORDINATES ON ROW SECTION OF ARC
325
    5=1AS
    16=1 AO
    L2FGM(1G*3)
    K2=GM(1G*4)
    R2=GM(1G*5)
    22=GM(1G*6)
    CALL BSET(R,Z,PHI,TAG,NPT)
    IF(ERKOR)RETUKN
    IG=1G*3
    AKCFIN#1
    RETURM
    END
    SUEROUTINE SET REGION(REGCINREGONREGC,TAG,PHI,RIZONPT)
    INTEGER BIT,PARITY,AREFIN,PK(6),TAG(NPT)
    LOGICAG EKROR
    COMHION/KLP/KMAX,LMAX, RARITY/ERORAERLOR
    IFIMDX/11:12,15,14,15,16,IA,18,IC,L,K,PK,IG,IR,ARCFIN
    O/8LKG/L1:L2,K1,K2,R1,R2,Z1,ZL,LO,KO,RO,ZO,PHIO,PHIIIPHIZ,PHIAV
    DIHENSION PHI(NPT),R(NPT),Z(NPT)
    DIHENSION REGG(NREG,NHEGC)
    IT(I)F|M2*(I/R)
    JK=KEGC(IR,I)
    LEQ
    A=1
    IE=IA*KHAX*1
    K1,K2,11;12=0
    IF(IT(6))90.65.90
    IS THEE LUWER SIDE ON A BOUNDARY ?
    IF(BII'(TAG(I8),4,0).GE,2)IF(12)80,85,80
    I1=1
    IF(12)75:770.75
    12=0
    guTuTO
    I< =1
    PACK HEN CELL NO\
    CAI.L VACK(TAG(IB),JR,3)
    ERASL ANY LOWEK SIDE TAG.
    IF(11.EQ:U)TAL(IB)㫙IF(TAG(1B),4,2)
C
    IB=1B+9
```

```
        IF(K1.EQ:KMAX)GOTO115
        19=0
        k2=k2+1
    C IS THE UPPER SIDE ON A BOUNDARY?
90 IF(BIT(TAG(IA),G,0).EQ.1)IF(12)95,110,95
    I1=1
    IF(12)105,100.105
    12=0
        gotuguo
    110 12=1
C NEV TAG)
105 CALL PACK(TAG(|A),JR,2)
C ERASE ANY UPDER SIDE TAG.
100 IF(I\.EQ&O)YAG(IA)MBIP(TAG(IA),4,1)
    |AFIA*1
    1F(K2.Eq:KMAX)GOTOT15
    11=0
    K1EK\*1
    COT065
115 IF(L.EQ.LMAX-1)00T0120
    LRL+1
    IB=1B+1
    1A=1A*1
    GOTO5O
C SET AUERAGE POTENTIAG fOR REGION:
120 RHIAVEPHIAVIIS
            IF(PHIAV,EQ.O.)PHIAVIO.S
            DO 140 LMq.LMAX=1
            16a1-1T(L)
            DO1 140 KRq, KMAX=1
            |ARL*(KMAX*1)*K+1
            IBa(L+1)*(KMAX+1)*K+16
            IGp(L-1)*(KMAX+1)+KK+16
            IF(BIT(TAG(IA),1,0),NR,0)60T0140
GHECK IF ALL CELLS ASSOCIATED WITH aN INTERNAL POINT HaVE thE SAME TAG
    PK(1)=BlT(TAG(IA),2,0)
    PK(2)=8IT(TAG(8B),3,0)
    PK(3) ロBIT(TAG(&A-1), 2,0)
    PK(4) ロBIT(TAG({A=1),3,0)
    PK(5)=BIT(TAG(IC),2,0)
    PK(6)=BIT(TAG(8A),3,0)
    DO 135 14"2.6
    IF(PK(1):NE.PK(IT))S0Y0390
    colitinue
        IF(PK(1).NE.IR)GOTO 140
    GIVE PT':A REGN. NO.
    SET APPROXN. YP POTL
    PHI(IA)=PHIAV
        H(IA),Z(IA)MO.
    CUNTINUE
    RETUKN

5 EOO EKRURF":TRUE. RETURA
```

    SUGROUTINE HESH RELXNGREGG,NREG,NREGCITAG,R,Z,NPTY
    LOGICAL PRINT
    INTEGLK BIT,AKCFIN,DARIYY,PK(O);FAGINPP)
    COMMON/KLP/KPAAX,LHAX,DARITY
    I /BLKI/LY,LZ,K1,K2,OOLDR,OOLDZ,DNEWRIDNEWZ,LO,KOISUMR,SUMZIEDSR
    I,EESZIDRIDZ/BLKZ/EIGJAGR,EIGJACZ,EIGSORR,EIGSORZFITOURETAOZ
    I/INDX/I,PRINT:ITN,14,15,16:IA,IB,IC'゙LIGK,PK,IGI\RIARCFIN
        DIHENS\DN REGC(NREGINREGC),R(NPT):Z(NPY),W(G)
        |T(I)=| - 2*(1/2)
        CALL T\IIE(TI)
        WKITE(Z;10)TI
        FORLIAT(1HT, 30X,48(1H*)/30X:
    I38H* TIHE IN ENTRY TO MESH RELAXATION /A8,3H */30X
    A:48(9H*)//)
        1^"ごこに!
        PRINTM,FALSE.
        IMXHEO,25*NPT
        EPSCMF.OOROA
        EPSR,FPSZE1:
    DOLDR,DOLDZIEIGJACR,EIGJACZIEIGSORR'EIGSORZ,ETAOR'ETAOZZO.
        RHOR,RHOREI.
    20 ITNFO
30 DNEWRIDNEWZ,SUMR,GUMZ,RESIOMXR,RESIDMXZ=O.
DO. 45 LEITLHAXFI
\$5:IT(6)
00 40 K\#'\&KMAXM9
|A牙L*(KHAX*1)*K*9
GHEGK IF POINTIS IN DUMMY REGION OR ON DIRICHLET BOUNDARY..
IF(TAG(IA).EQ:,O,OR,BIT(TAG(IA),1,0):NE,O)GOTO40
IRWREGC(B|T(TAG(IA),2,0):G)
16\#1
IF|IR,EQ,\)I6\#1m|5
1日ह(L*'1)* (KMAX* 1)*K*16
ICF(L*4)* (KMAX*1)*K*16
IF|IR,EQ*2) GU TO 34

```

```

    1 *,1066000067-R(1A))
    GOTU34
    ```

```

    R(IA)*R(IA)由DK
    SUMR#SU|R*R(IA)*R(IA)
    DNEWRMDHEWR*DKWOR
    IFG.NDT.PNIHT)GOTO35
    DRFABS(DR/R(IA))
    IF{DR,GT.RESIDFIXR)RESIDMXREDR
    IF{1R,EQ:2)GOTOEI
    OZ#RHOZ*({Z(It*T)+Z(IB)+Z(IA-1)+Z(IA+1)+2(IC*1)+2(IC))
    1*:10600067mz(1A))
    G0.T066
    69 DZ\#RHWZ*({Z(IB)* Z(IA*q)+Z(IC)*Z(IA+1))*0.25*Z(IA))
64 Z(IA)\equivE(IA)*OZ
SUMZ\#SU|Z*Z(IA)wZ(IA)
DHFHZEDNEWZ*DZ*DZ
IF(.NUT,PKINTSGOTO40
DZFABS(DZ/Z(IA))
IFSDZ.GT'ARESIDMXZ)RESIDMXZ\#DZ
40 CDNTINUE

```
```

45 cONTINUE
IF\PRINTSGOT0G00
1TN-ITH*?
IF(ITH.GT゙FIMXM)GOTO390
I\#0
IF\ITM,GTYYICALL SORCONEWR,DOLDRISUMRIRHOR,EIGJACRIEIGSORRIETAOR
|'ERSR)
DOLDRFDHEWR
IFREPSR,GE.EPSCH)GOPOS5
\MI*1
5 5
BRINTE-TRUE:"
GO TO 3O
\$00 WRITE(Z,G09)IYN,RESIOMXRINESIDMXZ'BRHOR,RHOZ,EPSRIEPSZ
FGRIIATS\&SHO TOTAL NO. OF ITERATIONS IN MESH RELXN IS ITG
I:3SH )HAXIMUM R ANO Z RESIDUALS ARE", ,2FI2:6/
IBSH THE FINAL OVERERELXN PACTORS ARE. ,2F92.6
GBOH ANP YHE CONVERGENCE PACTORS ARE, ;2F{2.6)
CALL THHE(T1)
WRDTE(2!15)P9
FQRIIAT(9H0,30X,48(4H*)/30X,
138H* TIME ON EXIT PROM MISH RELAXATION ,A8I3H */3OX
TM名(9H%)y/)
RETURN
END
SUBROLTINE DARAMCREGCINREG,NREGCITAG,R,Z,CPU,CPR%GPL,SCT
INNRTiPHIS
LOGICAL IN`
INTEGER BIT,AKCFIN,PARITY,PK(6),YAG(NPY)
COMMON/ST/OM(500),TEMP(80)/KLP/KMAX:LMAX,PARITY
COMMON/INOX/II,I2,13,16;KI,K2,IA,1B,IC,L,MM,JJI7IIIRIINT
IGGKI/AINTEGRAL,M(2)IMR,TRNGGISOURCE,COEFFONN(2)IA,BACATGAHP,BPI 3
AABLK2/LL(2),CUYT(S),KK(2),AA(2)
DIMENGION REGC(NREG,NREGC)/CPU(NPT);OCPR(NPT),CPL(NPY),SCT(NPT)
1,R(NPT), 2(NAT),PHI(NPF)
C THE COUPLING COEFFICIENTS AND SOURCE TERMS ARE EVAGUAFED ICELGNISEI:
G EACH GELL CONTRIBUTES TO PHREE ADNACENT CQUPLINGS AND SOURCES
1T(1)m\&\#2*(1/2)
C NONOSTANDARD
FPJR9.
FPI3FFPI/3.
L@O
1AF1
IB=IA+KNAX+1
K1'*2=0
IFSIT(L))20.20,50
CALCULATE COHTTRIBUTION GROM THE LOWER CELL AT POINT IB
20 IF(TAG(IB).NE':C)CALL PERMS(CPU,GPR,CPL,SCT,TAG,REGC'INOEG,NREGCE

```
```

    Ib=IB+T
    IF\K1.EO;KmAX)G0 FO 55
    K2=K2*1
    CALCULATE THE CUNPRIGUTION PROM UPPER CELL AT IA.
50 IF(TAG(IA),ME:OO)CALL FERMS(CPU,CPR,CPL,SCT,TAG,REGG*NREG,NRRGCF
INPT,IA,IB,Z,R,Z,PHI)
IA=1A*!
IF(K2,EG*KMAX)GO TO 5\$
K1\#K1+1
GOTU2%
|F\&L|GE.LMAX-1)RETURN
LFL\#!
\A=|A*\
18早18*1
GOTU1O
END
SUGKOUTINE TEKHSCCPU,GPR,CPL,SCT,TAG,REGC,NREG,NREGCÖ
IAPT,I,J,K,K,Z,PHI)
IHTEGKR GIT,AKCFIN,PARITY,PK(6),TAG(NPT)
LOGICAL AXMAG\&AXHEAY,INT
COMMOH/INDX/I1,12;13,14,K\/K2,IA;18:IC,L,MM,JJ\&7)SIR;INT
COHHOH/TP/TYPE,AXHAG,AXHEAT
I/KLP/KHAXYLMAX,PARIYY
|/GLKG/AJNTEGRAL,M(2),RR,TRNGL,8OURCE,COEFP,NN(Z),A\&B:C,TG,HP,FPI3
I/GLK2/LL(2):COTT(3);KK(2),AA(2)
DIMENSION KRGC(NREG;NREGC)\&CPU(NPT)'ACPR(NPT),GPL(NPTI,SCT(NPTI
|:R(NPT):'Z(NPT),PH{(NPF)
IT(1)m|m2*(1/द)
11最隹(K)
12=1+1
13\#2*19
C FIHO REGION NUMBER OF CELL
IRPUIT(TAG(1):I I%:0)
IFKIR,EQGO)MEYURN
*RH%
TRNGL^0.5\#PARITY*(R(IB)*(Z(IA)=Z(12))*R(12)*(2(IB)=Z|{A))
1*R(IA)*(Z(12)=Z(IB)))
IF(TRNLLNLE':1"EN|2)007060
IFIREQC(1R,3):LE.O.)GOTOSO
SOUKCEmFPI3*TRNGL*REGC(IR,3)
SCT(IA)mSCT(IA)*SOURCE
SCT(IB)mSCT(IG)*SOURCE
SCT(1')=SCY(I2)*SOURCE
IF{REGG(I\&,2):LE.IEN10)REFURN
COEFF=0.125*REGC(IR,2)/TRNGL
C MODIFICATIONS FUR AXIAL SYMMETRY(EFGmHEAT CONDUCTION AND MAGNETIC)
IF(AXMAG)COEFFmCOEFF*3./(H(|A)*R(IB)由R(I2))
IF{AXHEAT)COEFFFCDEFF*(R(|A)*R(I2)*R(|B))/3.
A={R(|A)\#R(IG))**2*(Z||A)\&Z(IB))**2
B={R(1u)*R(12))**2*(2(18)由Z(12))**2
CM(R(IA)-R(17) )**2*(Z(IA)-2(I2))**2
COTT(1)=(D+R, mA)
COTT(C) = (A*G-C)
curT(S) = (A+C-B)
CUNTRIBUTIONS FU COLPLINGS(E.G` PERMITYIVITY*COTANGENT OF ANGLE)

```

GPU（IA）\(=C \mathcal{C U}(I A) * C D E F F * C O T T(19+1)\)
CHR（I）मCPK（1）＋COEFF＊COTT（13）
CPL（It）二CPL（IU）＋COEFF\＃COFP（3－2＊11）
RETUR \({ }^{\text {R }}\)
WKITE（2．6．65）

FURIAT \(\angle G O H O\) TRIANGLE AREA ZERO OR NEGATIVE RETURN END

SU日ROUTING KELX（TAG，CPU，CPR，CPL，SGT；PHIOR，Z，NPT）
LUGICAL PRINT
INTEGEK TAG（NPT），PARIPYIBIT
COMIION／INDX／PKINT：IRCNTIIA，IG，ICIL，K：II，IYN
1／KLP／KHAXI LHAX，PARITY
I／BLKT／DOLVAONEW，SUM，EOS；WOPTADPHIFCPSUM
1／ELKZ／EIGVAC，EIGSOR，ETAO
DIMENSION CPU（NPTI，CPR（NPF），CPL（NPT），SCT（NPT），PHI（NPT）
A：R（1；PT）：Z（NOT）

IMX＝0，25：NPT
PRIHTE，FAGSE．
EPS＝1．
EPSCE，OOONO1
OULD＇IETAOIEIGJACIEIGSORMO．
RHOITI． 5
WUPT－1．5
CALL TIME（Tq）
WRITE（2＇400）TI，RHOI
FORMATSTHO：ENTRY AY \(1, A 8,1\) TO RELAXATION SOLUTION OF POISSON PI IIROGLEHIII．NON．UNIFORM TRIANGULATION，INITIAL VALUE OF AGEELERAI
IITION FACTOR TAKEN AS 1：F6．3）
ITNEO
DNEW，SUMWQ． iJ 100 L． 1 ．LIAAX－1 151－1T（L）

\(\mathcal{B}=(K M A X * 1) *(L * 1)+1\)

【F（PRINT）URITE（2，70）L
 HIHZ．IGX，IRESIDUAL POTENTIAL HESH DOINT COLUMN FAGI／AJ DO 90 KM ，KMAX－1
\(I A=I A+1\)

16\＃！C 中 1
IF\｛TAG（IA），FQ：O）GOYOOO
IFSGIT（TAG（IA），1，0），EQ，2）BOTU90
\(C P S U M=C P U\{I A)+C P L(I B)+C P R\{(A-1)+C P U(I C\}+C P L(I A)+C P R(I A)\)

I \(+C\) CU（IC）\(\oplus P H I(I C)+C P L(I A) \oplus P H I(I C+\uparrow)+C P R(I A) \oplus P H I(I A+1)\)
\(1+S G T(I A)) / C P S U H=P H I(I A))\)
PHI（IA）\(A P H I(I A)+D P H I\)
SUMESUH＋PHI（IA）＊PHI（IA）
DHEWMUNEW DDPHE＊HPHI
IFG．NUT：PRIITIGOTO90
IF（PRINT）NRITE（2；40）R（IA），Z（IA），DPHY；PHI（IA），IA；K；TAG（IA）

CONT IHUE

CuNTINUE
IF（PRINT）GUTO50

DOLOEDNEW
WRITE 2,200 IITN，WOPT，EPS，IIGNAC，EIOSOR

IF（EPS．LT：EDSI）GOTO150
ITUEITN由1
IF（ITN．L．T：IAX）GOTOS
HRINTR．THUE．
OMTO5
CALL TIME（T1）
WHITE（2；55）T1
FURIATSIHO，3OX，48（IH＊）／3OXAI＊YIME ON EXIT FROM RELAXATIOA

RETURA
END
SWGROUTINE SOR（DNEW，DOLD，SUM，WOPY，LAMOA，MU，MUOIEPS）
REAL LAMDA，MLINUO
DATA DIFF，RHCO，BETA／0．01，0．01，0\％05／
EUSESQRT（DNEW／SUM）
114ESQRT（DNEW／DOLD）
IF（AGS（MURHUO）．GE，DIFF） 60 PO 50
IFGMU．LE：WOPTMI．GOTO 50
LAMDAB（MWヵWOPTN\｛，）／（WOPT由SQRT（MU））

1＊（1．\(-B E T A)\)（IOPT
MUOMHU
RETURN
EMD

SUGROUTINE PLUTT（R，Z．DHIGTAGINPYINEQ：APLOT MESHZ
LOGICAL PLOT MESH FIMST
INTEGGH BIT：TAG（NPY），PARITY
COMMOR／BLK2／L9，L2，K1，K2；RY，R2，21，22，10，KO，RO，20\％PAIO：PHITIPHI2
COMIION／STAGE／HPROB，IO
I／KLP／KMAXYLMAX，PARITY
DIMENS\｛ON R（NPT）：Z（NPY），PNI（NPT），EQ（20）
IT（I）
FI思SE，FALEE．
DO 9 InザNPT
IESTAG（I）：EO．D）GOTOQ
IFSFIRSTYGOTOS
OHIIIN，FHXMAXGPHI《1）
ZMIN，ZHAXEZ（I）
QMIN，RHAXGR（IJ
FIRSTF，TRUE＇。
GOTOO
PHIHINGAMINA（HHIMIN：PHI（I））
PHIHAXGAHAXI（PHIHAX，PHI（I））
ZMIN円AHIINI（ZMIN，2（1））
RMINmARINH（HMIN：R（I））
ZHAX日AlIAXI（2MAX，Z（1））
RNAX＝Al｜AXI（RMAX，R（I））
CONTINUF
WRITE（2＇，199）
FURMAT（LTH IIAXIMA AND MINIMA OF PLOTTING QUANTITIES ）
\(2(1)\)

70 IA骎IA－1
CAGL LINET（L，IAIIB，R，Z，TAG，NPTIPLOT MESH）
\(K 2=K 2 F 1\)
1F（K2）120781．61

ICALL EQUPIT（IA，IBMI：IB，DHIOR，Z，NPT，EQ，NEQ1）
18：18～1
G0．T035
L化し1
GOTO6
END
```

            SUBROUTINF EQUPLT(I,J,K,PHI,R,Z,NPT:EQ,NEQI)
    INTEGER PGE#TL
    ```

```

    OIMENS{ON R(NHT),Z(NPT),PHI(NPT),EQ(NEQY)
    20-2(1)
    RO#K(1)
    21嗆2(N)
    R\=R(N)
    22#Z(K)
    R2员(K)
    PH&OaPHI(!)
    PH\ImPHI(U)
    PH\2mFHI(K)
    IF{PH\O~PHIT)50,55,55
    CALL INTCHN(RU,ZOGR1,21,PHIO,PHI1)
    IF(PHIT-PHIR)65,60,60
    CALL INTCHN(R1,Z1,R2,Z2,PN(1,PHI2)
    GOTO45
    0075 12:1,NEU9
        JJ=1G*1
    OHISEEQ(IZ)
    ```
```

        CALLINTCPT(DHIS;RA,ZA,RB,ZB,PSENTL)
        IF(PSFNTL)74,75,74
    74 CALL LLNE(JJ,ZA,RA,2B,RB)
    75 CUNTIAUE
RETURA
END

```
    SLIAROLTINE INTCPT(PHIS,RA, ZA,RB,2B,IPSENTL)

    (F(HHISmPHIO)10,90.20
    IF (PHISEPHI2)
    \(P=0\).
    GOTO3S
    \(30 \quad P_{\text {F }}(P H I S W P H I 2) /(P H I O W P H I 2)\)
    \(35 \quad 2 A=2 Z+P *(2 O-Z \AA)\)
    \(R A=R 2 * P *(H O=R 2)\)
    IF(PHISiARHIT) 60.45 .50
    P=RPHISHPHI2)/(PHI1-PHI2)
    2BFZ2+P* (21~22)
    R日FR2*R* (RY~RZ)
    COTOGU
    \(45 \quad 20=29\)
    REER1
    GOTOGU
    P=(PHISmPHIq)/(PHIORPHIT)
    ZB5Z9*P* (40-29)
    RBFR9*P*(BOMRq)
    IPSENTLZA
    KEJURN
    20 IPSENTLEO
    RETURH
    ENO
    sumROLTINE LINET(INDXII, J.RTZ.TAGinPTiPLOT MESH)
        hogical plot mesh
        INTEGER TAG(APT),BIT
        DIMENEJON R(HFT),Z(NPT)

CHECK FOR POINTG IN ClIMMY REGION.
    IFGTAG(I):EQ.C.CR,TAG(J),EQ, O)RETURN
    IFUNCEITIT(INEX)
    HRITE(2,800) NPY,I, J,INDX,JFUNC
800 FOBHIAT(1H .5190)
    IUFEIT(TAG(I-IT(INDX)),2,0)
    WKdTE(2:800) IU
    \(K=1\)
    1+(INDX.GT.2)KNJM1+1T(INDX)
    ILEBIT(TAG(K), 3,0)
C GRAW A MESH LINE.
    IF(PLUT MESH.(IR.(IU.NE,IL))CALL LINE(I,Z(I),R(I):Z(J),R(J))
    RETURN
    El. D
    SUGROUTINE INTCHN(RA, ZA,RB, ZB, PHIA,PHIB)

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PHJLロPHI
RETURH
EHD
SURKCUTINE LINE（I，Z9，R1，22，R2）
WRJTE（7：90）29，R1；22；R211
WRITE（2F90）Z9，R1，22，22，1
10 FORIIAT（4（F8，3），2X：12）
RETURN
END

\section*{APPENDIX 4.2}

TMG - dISPLAY PROGRAM
```

C
****************
* APPENDIX 4.2 *
****************
THIS IS THE DISPLAY PRDGRAM USED IN PLOTYING THE TRIANGULAR
C MESH AND EQUIPOTENTIAL LINES OF THE PROBLEM REGION.
C IT GENERATES THE FOLLOWING DISPLAYS:-
1. INTRODUCTORY AND DATA ENTRY
2.TRIANGULAR MESH AND EQUIPQTENTIAL LINES
3. ZODM
*********** MAIN PROGRAM SEGMENT
COMMON/ID/IN,IDUT
INTEGER FN(3)
IN=5
IOUT=6
CALL TXOPEN
C INTRODUCTORY DISPLAY
CALL DISPI(FN,IC)
GOTO(1,2,2),IC
C TRIANGULAR MESH DISPLAY
1 CALL DISPZ(FN,IC,IZ)
GOTO(2,3,2,2,2,2,2),IC
STOP
END
C
C************INTRODUCTORY DISPLAY \&DATA ENTRY *********
SUBROUTINE DISPI (FILNAM,NEXT)
COMMON/IO/IN,IOUT
COMMON/SCALING/SCL1,SCL2,SCL3,SCL4
DATA MNTXT/"+ NEXT + RESTART + EXIT "/
LOGICAL*I MNTXT(30)
INTEGER FILNAM(3)
15 CALL TXCLER
C SET UP INSTRUCTION TD THE USER AND THE MENL OPTIONS
CALL TEXTUP("TXTFL1",25)
CALL MNOPEN(875.,715.:1)
CALL. MNDISP(MNTXT,3,10,1)
CALL FRAME(870.,733.,3)
CALL CURPOS(1.,150.)
CALL ALPHMD
C INPUT DATA FILE NAME
20 CALL MESSAG("£ DATA FILE NAME?^")
READ (IN,3O)FILNAM Y
30 FORMAT (2A4,A2)
40 CALL MESSAG("£ ENTER PLOTTING SCALE LIMIT(MIN.\&MAX.OF X,Y)?A":
IF(IERROR(110).NE.0)GOTO 40
READ (IN,50)SCL1;SCL2,SCL3,SCL4
50 FORMAT (4GO.0)
2 CALL MNPICK(J,ICHAR,MND)
5 CALL CONFRM(ICHAR)
IF(ICHAR.EQ.78) GOTO 2
IF (ICHAR.NE.89) GOTD 5
GOTO(60,15,80),J
NEXT=J
RETURN
80 CALL ALPHMD

```
c
C***********DISPLAY 2 FOR PLOTTING **********)
SUBROUTINE DISP2 (FILNAM, NEXT,IZOOM)
COMMON/IO/INIIOUT
COMMON/SCALING/SCL1,SCL2,SCL3,SCL4
COMMON/ZOMSCL/ZSCL1,ZSCL2,ZSCL3,ZSCL4
DATA MNTXT/" + NEXT + PREVIOUS + EQUIP'L + MESH + ZOOM
8+ RESTART + EXIT "/
DIMENSION XEQP1 (1000), YEQP1 (1000), XEQP2(1000), YEQP2(1000)
LOGICAL* 1 MNTXT(70)
INTEGER FILNAM(3),FIRST
C FIRST TIME DATA FILE IS READ
FIRST=1
1 CALL TXCLER
IZOOM \(=0\)
WRITE (IOUT, 70)
70 FORMAT("TRIANGULAR MESH GENERATION:-")
CALL MNOPEN(875.,715.,1)
CALL MNDISP(MNTXT,7,10;1)
CALL FRAME(870.1733.17)
2 CALL LMTARA
CALL MNPICK(J,ICHAR,MNO)
5 CALL CONFRM(ICHAR)
IF (ICHAR.EQ.78) GOTO 2
IF (ICHAR.NE.89) GOTO 5
GOTD(21,21,23,22:24,1:21), J
GOTD 2
21
NEXT=J
RETURN
C GENERATE MESH
\(22 \quad K=1\)
FIRST \(=2\)
NEQP=0
REWIND 9
CALL SETFIL(9,FILNAM)
CALL LMTSCL (SCL1:SCL2,SCL3,SCL4)
11 IF(IERROR(110).NE.0) GOTO 200
C INPUT LINE COORDINATES FROM THE DATA FILE
READ (9,10)21,R1,22,R2,IEQP
10 FORMAT (4 (F8,3),2X,I2)
IF (IEQP.EQ.1) GOTD 20
C SAVE EQUIPOTENTIAL LINES COORDINATE
\(\operatorname{XEQPI}(K)=Z 1\)
YEQP1 (K)=R1
XEQP2 \((K)=22\)
YEQP2 (K) \(=\) R2
\(\mathrm{K}=\mathrm{K}+1\)
GOTO 11
20 IF(J.EQ.3) GOTO 11
CALL TXMOVE(Z1,R1)
CALL TXDRAW(Z2,R2)
GOTO 11
200 IF(J.EQ.3) GOTO 23
I ZOOM \(=1\) ZOOM +2
GOTO 2
C GENERATE EQUIPOTENTAIL LINES
23 (IF(FIRST.EQ.1) GOTO 22
CALL LMTSCL(SCL1,SCL2,SCL3,SCL4)
I ZOOM \(=1200 \mathrm{M}+1\)
\(K=K-1\)
DO \(100 \mathrm{I}=1, \mathrm{~K}\)
CALL TXMOVE(XEQP1(I),YEQP1(I))
CALL TXDRAW(XEQP2(I),YEQP2(I))
CONTINUE

GOTO 2
RETURN
C zooming
24 CALL LMTSCL(SCL1:SCL2,SCL3,SCL4)
C INPUT THE COORDINATES OF THE ZOOMING WINDOW CALL TXCURS (XZ1;YZ1,ICHAR)
36 CALL TXCURS (XZ2,YZ2,ICHAR)
C CHECK FOR TWO OPPOSITE CORNERS OF THE ZODMED WINDOW IF (XZ1.EQ.XZ2.OR.YZ1.EQ.YZZ)GOTO 36
C DRAW ZOOMED WINDOW
CALL TXMOVE (XZ1,YZ1)
CALL TXDRAW(XZ2,YZ1)
CALL TXDRAW (XZZ,YZ2)
CALL TXDRAW(XZ1,YZ2)
CALL TXDRAW (XZ1,YZ1)
ZSCL1=AMIN1 (XZ1, XZ2)
ZSCL2=AMIN1 (YZ1;YZ2)
ZSCL \(3=A\) MAX \(^{2}(X Z 1 ; \times Z 2)\)
ZSCL4=AMAXI (YZ1,YZ2)
CALL LMTARA
32 CALL CONFRM (ICHAR) IF (ICHAR.EQ.78) GOTO 24
IF(ICHAR.NE.89) GOTO 32
C CALL ZOOM ROUTINE
CALL ZOOM (FILNAM,IC,IZOOM,K:XEQP1,YEQP1,XEQP2,YEQP2) GOTO (1,42,42),IC

\section*{c PREVIOUS}

42 STOP
END
/* */
/* */
/* THIS C-PROGRAM READS IN THE PAPER TAPE PRODUCED ON THE ICL 19045 */
/* MACHINE AND STORE ITS DATA DN FILE SPECIFIED BY THE USER USING...*/
/* UNIX INPUT COMMAND: */
/* \%PRTAPE(/DEV/PR)AFILE */
/* WHERE 'PRTAPE' IS THE NAME DF THE EXCUTABLE MODULE OF THIS PROGRAM*/
/* and afile is the name df the file into which the data will be */
/* STDRED*/
MAIN()
INT I;
CHAR C;
WHILE (1) 1
\(I=R E A D(0,8 C, 1) ;\)
IF(C != 0) BREAK;
\}
C \(=80177\);
WRITE(1,8C,1);
WHILE (1) \(\{\)
/* END OF FILE */
IF (I \(=\) = \({ }^{\prime} 0^{\prime}\) ) BREAK
/* STRIP THE PARITY BIT FRDM THE ICL PAPER TAPE */ C \(=\& 0177\);
/* NOCKS OUT THE NULL CHARACTERS WHICH SIGNIFY END OF STRING */
/* UNDER UNIX */
IF (C \(==\) ' \(\mathbf{O O}^{\prime}\) ) CONTINUE;
\(\mathbf{I}=\operatorname{WRITE}(1,8 \mathrm{C}, 1) ;\)
3
\}```


[^0]:    

