This is a post-refereeing version of a manuscript published by ASCE.

Please, in order to cite this paper properly:

Ballesteros-Pérez, P., Phua, F.T.T., Mora-Melià, D. (2018) "Human Resource Allocation to Multiple Projects Based on Members' Expertise, Group Heterogeneity, and Social Cohesion." Journal of Construction Engineering and Management, 145(2), 04018134.

https://doi.org/10.1061/(ASCE)CO.1943-7862.0001612

The authors recommend going to the publisher's website in order to access the full paper.

If this paper helped you somehow in your research, feel free to cite it.

1

Human resource allocation to multiple projects based on

2

members' expertise, group heterogeneity and social cohesion

3 Pablo Ballesteros-Pérez, Ph.D.^{1*}; Florence Ting Ting Phua, Ph.D.²; Daniel Mora-Melià, Ph.D.³

4 Abstract

5 Project managers regularly allocate human resources to construction projects. This critical 6 task is usually executed by fulfilling the minimum project staffing requirements normally 7 based around the quantity and competence of project members. However, research has shown 8 that team performance can increase by up to 10% and 18%, respectively, as a consequence of 9 the group members' heterogeneity and social cohesion. Also, there is currently no practical 10 quantitative tool which incorporates these aspects to allow project managers to achieve this 11 task efficiently and objectively.

A new quantitative model for the effective allocation of human resources to multiple projects, which takes into account group heterogeneity and social cohesion is proposed. This model is easy to build, update and use in real project environments with the use of a spreadsheet and a basic optimization engine (e.g. Excel Solver). A case study is proposed and solved with a Genetic Algorithm to illustrate the model implementation. Finally, a validation example is provided to exemplify how group heterogeneity and social cohesion condition academic achievement in an academic setting.

 ¹ Senior Lecturer. School of Architecture, Building and Civil Eng., Loughborough University, Loughborough, Leicestershire LE11 3TU, UK. *Corresponding author: +44 (0) 150 922 3771, <u>p.ballesteros-perez@lboro.ac.uk</u>
 ² Associate Professor. School of the Built Environment. University of Reading,

Whiteknights, Reading RG6 6DF, UK. Phone: +44 (0) 118 378 8194, <u>f.phua@reading.ac.uk</u>

³ Associate Professor. Departamento de Ingeniería y Gestión de la Construcción, Universidad de Talca, Facultad de Ingeniería, Curicó, camino Los Niches km.1 3340000, Chile. Phone: +56 951 265 044, <u>damora@utalca.cl</u>

19

20 Keywords

Human resource management; human resource allocation; team performance; heterogeneity;
faultlines; cohesion; sociometry

23

24 Introduction

25 It is a well-known saying that 'people are the lifeblood of organizations'. Indeed, 26 despite living in an era of constant technological advancement, most of our tasks are still 27 done, handled or supervised by human beings. In organization life, the size and/or complexity of many undertakings nowadays demand the involvement of many people (sometimes from 28 29 different organizations) working together to achieve a common goal. This goal can be 30 anything, but many times involves creating deliverables (products, services) to enhance a 31 company's internal performance, to make profit, or both. However, people (employees, 32 workers) who take part in these undertakings are normally subject to constraints. For example, they are qualified to do certain jobs and not others; they have different levels of 33 34 competence in different domains; they cannot be present in multiple locations; and, certainly, 35 they have physical constraints in terms of how long they can work for (Hendriks et al. 1999).

Therefore, when there are several, sometimes concurrent projects that require the participation of people to be completed, a project manager faces a practical dilemma: how to best allocate his/her human resources on-hand to deliver his/her projects successfully. 'Successfully' can mean completing the projects on time, on budget and within an agreed (or shared) quality threshold, or just meeting the key stakeholders' expectations (Xia et al. 2017). In any case, as long as there are ongoing projects, the project manager will require competent human resources to engage in certain tasks for a period of time before they are freed and able

to join other ongoing or upcoming projects. An essential part of the project manager's role in
the allocation of optimum human resources is to ensure, as much as possible, that the
individuals within the projects can work cooperatively with each other (Anvuur and
Kumaraswamy 2016).

47 However, collaboration between project members does not happen by chance. There 48 are indeed many factors that prevent this from happening. These factors can be communication-related for instance, and/or have to do with the project member's 49 50 demographic attributes such as (differences in) nationality, education, religion, experience, to 51 cite a few (Al-Bayati et al. 2017). Sometimes, there are people who do not like working with certain individuals, and this can also be really detrimental to the project progress and its 52 53 eventual success (Chen et al. 2017b). In this regard, Phua (2004) and Phua and Rowlinson 54 (2004) have found that cooperative behavior between project members is influenced, to a 55 certain extent by individual members' intrinsic social and psychological factors which have 56 to do with many more factors other than just their extrinsic demographic profile such as age, 57 sex, education, work experience and roles. For this reason, we will consider both cohesion 58 and heterogeneity factors later when aiming to build high-performing teams.

Given our existing understanding of the various factors that affect team performance,
there is however, a scarcity of quantitative and objective tools that enable the effective
allocation of human resources in terms of where and when they are to be allocated to projects
(Ahmadian Fard Fini et al. 2017). Conventionally, this type of allocation issues largely fall
within mainstream Human Resource Management (HRM) application which has its roots in
social sciences.

A different, maybe opposite, scenario can be found within Operational Research
(OR), which deals with the modeling and application of advanced analytical methods to make
better decisions. The problem of allocating multiple human resources to a single project is

68 relatively recent in OR, but it has been well studied and is known nowadays as the 'Team 69 Formation Problem' (TFP) (Tseng et al. 2004). When there are multiple simultaneous 70 projects, the TFP becomes the 'Multiple Team Formation Problem' (MTFP). Particularly, the 71 grouping of individuals to create teams have been made by attending to multiple factors: the 72 resources' temporal availability, current workload, individuals' skills, level of competence, geographical distance, seniority, number of contacts, among many others (Gutiérrez et al., 73 74 2016). In this line of research, it is not common to find theoretically-grounded sociological 75 considerations in the composition of teams. This means that, whereas it is relatively easy to 76 come across OR models that allocate resources that meet some functional (e.g. skills, 77 competence) project members' requirements, it is very rare to find models that try to optimize other socially-based group traits like intra-group social preferences and group cohesion 78 79 (Ballesteros-Pérez et al. 2012). This piece of research proposes to take a step forward in 80 bridging this gap.

81 In this paper, a new human resource allocation model that takes into account, not just 82 basic project staff requirements and employees' profiles, but also group heterogeneity 83 (diversity) and social cohesion, is developed. This is a worthwhile contribution because, as 84 discussed earlier, team performance has been demonstrated to be significantly influenced by 85 these two factors. Hence, it seems logical to incorporate this knowledge when creating highfunctioning teams which comprise the 'right' individuals working together. To this end, the 86 87 rest of the paper will be structured as follows. The literature review section will go over the 88 major contributions published in the areas of the MTFP, group heterogeneity and social 89 cohesion. The *materials and methods* section will formulate the model, define its major variables and explain how these are interrelated under mathematical expressions for 90 91 measuring team performance. A case study will exemplify the model implementation in a fictitious company environment with twenty people and three simultaneous projects. A short 92

validation section will implement the model in a real academic setting where a cohort of 15
MSc students worked in groups to deliver three projects. The *discussions* will provide some
insight and further analysis on the implications and limitations of the model. Finally, the *conclusions* will summarize the paper and convey why the proposed tool is relevant to the
wider project management community.

98

99

Literature review

100 The proposed model draws from research developed in two very different areas – 101 operational research (OR) and applied psychology (AP) –, but it is applied on a third one: 102 Human Resource Management (HRM). The amount of works published in connection with 103 HRM within both OR and AP is endless, so it is necessary to narrow down significantly the 104 works to be presented here. In this regard, only three very relevant topics will be reviewed: 105 the MTFP, group heterogeneity and faultlines, and group cohesion and sociometry.

106

107 The Multiple Team Formation Problem (MTFP)

108 The MTFP involves the distribution of people with different skillsets to a series of 109 teams (projects) that usually require more than a single area of expertise while optimizing 110 other criteria (e.g. profits, execution time, number of people). This problem is known to be 111 NP-hard (Non-deterministic Polynomial-time Hard) even for instances with a single project 112 (Gutiérrez et al., 2016). This means the MTFP belongs to the set of OR problems that are 113 harder to solve.

114 The first attempt to model and compute a solution to the TFP is relatively recent and 115 was developed by Lappas et al. (2009) when trying to create teams of experts from 116 professional profiles posted on social networks. Just a year later, Dorn and Dustdar (2010)

proposed solving the TFP with a first heuristic approach, whereas Li and Shan (2010)
improved the Enhanced-Steiner algorithm that was one of the two original algorithms used to
solve the TFP.

A year later, Yin et al., (2011) were the first to consider social influence among the teams of experts. Additionally, Farhadi et al. (2011) allowed for the possibility of different competence levels among the human resources, a generalization that will also be considered in our model.

In 2012, the number of works published on the TFP grew exponentially. Among the most relevant: Sorkhi et al. (2012) proposed a game theoretic approach to form and rank project teams; Farhadi et al. (2012a, 2012b) extended the second original algorithm that had proven to be very effective when dealing with the TFP – the Rarest First algorithm –; whereas Gajewar and Sarma (2012) proposed three new optimization algorithms and successfully applied them to the MTFP for the very first time.

130 Next, Shi and Hao (2013) formulated the MTFP with a multi-criteria decision-making 131 ranking approach involving the individuals' social networks. Then, Teixeira and Huzita (2014) approached the MTFP considering the human resources' contextual information 132 133 (culture, idiom, temporal distance and previous experience), besides task requirements and 134 the interpersonal relationships among human resources. Our proposed model will also take advantage of similar constructs in order to create a multi-dimensional model. Also, Agrawal 135 136 et al. (2014) focused on educational settings allowing the MTFP to be implemented without 137 allowing overlaps between the different student teams, a feature that will also be considered 138 in our model. Still in the same year, Awal and Bharadwaj (2014) tried to capture the synergy 139 produced among team members by means of a new ad-hoc concept named 'Collective Intelligence' and also used a Genetic algorithm to solve their problem formulation. In this 140 141 paper, the solution of the case study proposed later will also make use of a genetic algorithm

approach as the way this ad-hoc index was defined share some similarities with our objectivefunction.

Although there have been many other recent works published on the MTFP, these will not be recounted here as they are not directly germane to this study. However, one that is perhaps worth highlighting is the work from Gutiérrez et al. (2016) which formally included sociometric preferences among individuals in the MTFP. Our proposed model also shares a similar approach for modeling group cohesion. However, the algorithmic approach will be totally different to Gutiérrez et al.'s as our model includes other dimensions, which makes our model no longer quadratic.

151

152

Group heterogeneity and faultlines

153 Research on how team effectiveness is influenced by the team composition has been abundant too. Most of this research has focused precisely on measuring and analyzing the 154 155 effects of group heterogeneity on team performance. Group heterogeneity (homogeneity) refers to a measurement of how different (similar) the members' demographic attributes (age, 156 157 sex, ethnicity, etc.) are with each other. There are many reviews on group heterogeneity (see Earley and Gibson (2002) for a comprehensive one) but they will not be recounted here 158 either. In this piece of research, we are focusing on the quantitative aspects of how 159 160 heterogeneity is measured and what are its effects on team performance, rather than the mechanisms or factors that cause it. 161

With this in mind, the first indices that captured quantitatively how diverse
(homogeneous/heterogeneous) a group can be were defined by Blau (1977) and Allison
(1978). Generally, these and other later indices involved measuring group homogeneity as the

members' demographic attribute overlaps. With those indices, heterogeneity was also
generally defined as the inverse of homogeneity, that is heterogeneity=1/homogeneity.

167 Additionally, for a long time, it was believed that the presence of faultlines (demographic features that divide a bigger group into two or more relatively homogeneous 168 169 subgroups) was detrimental to group performance (Lau and Murnighan 2005). It was not 170 until the work of Gibson and Vermeulen (2003), who proposed a new metric for measuring 171 group heterogeneity – the Subgroup Strength –, that it was understood that the presence of 172 subgroups (faultlines) could indeed promote team learning behavior and improve their 173 performance. The Subgroup Strength (SS) has many advantages over previous homogeneity 174 metrics (indices) as it allowed researchers to identify group faultlines much more effectively. Indeed, it was shown recently by Meyer and Glenz (2013) in a comprehensive comparative 175 176 study that the SS is one of the simpler, yet more powerful metrics for measuring group 177 heterogeneity in the presence of two or more subgroups. For these reasons, SS will also be 178 used in our model later to describe subgroups' heterogeneity.

Finally, Gibson and Vermeulen (2003) also showed that a team's performance 179 seemed to vary by up to 10% depending on the SS. Again, this was supported recently by 180 181 another study by Chen et al. (2017). This study also confirmed another speculation of Gibson and Vermeulen's: that the relationship between SS and team performance was an inverted U-182 183 shape whose minima (lower performance) were to be expected for extremely homogeneous and heterogeneous groups. Finally, many other works have been published on the effects of 184 group heterogeneity on intra- and cross-subgroups demographic faultlines (Lau and 185 186 Murnighan 2005), but only some related to group cohesion will be reviewed later in the 187 Discussions to clarify the effect of possible collinearities between both variables.

189

Group cohesion and sociometry

Group cohesion is a desirable attribute because research has proven it to be positively
related to team performance, as well as a wide range of other positive behavioral outcomes
(better individuals' attitude, well-being, lower absenteeism, etc.) (Chang and Bordia 2001;
Chen et al. 2017b). However, very few pieces of research have actually quantified the extent
to which team performance is influenced by group cohesion or dissociation.

195 One exception is a recent and comprehensive review performed by Evans and Dion 196 (2012). These authors, beyond concluding that there is a positive relationship between 197 cohesion and performance, recounted that cohesive groups seem to perform around 18 198 percentile points on average above the average (uncohesive) groups. This figure will be used 199 later in our model as other research has also corroborated the cohesion-performance relationship even when different settings (e.g. business, education, research) or group sizes 200 are considered (Castaño et al. 2013). Furthermore, because existing research on cohesion and 201 202 performance has operationalized cohesion almost completely in terms of interpersonal 203 attraction (see evidence from Lott and Lott (1965) to Beal et al. (2003) for instance), it makes 204 theoretical sense for our model to adopt sociometry to model group cohesion.

205 Sociometry was devised by Jacob Levy Moreno (Moreno 1941) and is a method that 206 can be used for estimating the quality of group dynamics. It is one of the few methods that allows the gathering of quantitative information about the informal structure of a group that is 207 difficult to obtain in other ways. Sociometry was extensively used between the 40s and 60s at 208 209 schools, companies and research settings to examine social interrelations and communication patterns within groups (Salo 2006). In sociometry, interpersonal relations are measured by 210 211 asking group members to express their preferences and rejections for particular companions in a certain situation or activity (Festinger et al. 1950). Hence, the advantageous simplicity of 212 213 sociometry is, at the same time, its major limitation: it requires that group members are

truthful and open in stating who they prefer and not prefer to work with. A reasonable
question then is whether group cohesion can be adequately represented by sociometric
choices and if these choices r can be eventually captured by means of questionnaires that
request group members to state their preferences and rejections towards other group
members. In fact, both aspects have been subjected to multiple research studies in many
varied settings. An example of a brief but reassuring and confirmatory review can be found in
Salo (2006).

221 Finally, there is one question that needs to be addressed before formulating the model. 222 As stated earlier, the proposed model will group individuals under different projects that have 223 some minimum staff (areas of expertise and levels of competence) requirements. According 224 to a recent piece of research (Mathieu et al. 2015), when people with the right combination of 225 expertise work together, as expected, this is positively related with team performance. 226 However, this same piece of research also showed that this is unrelated to team cohesion. 227 With this in mind, we will allow our model to effectively separate the effect of the constraints 228 (i.e. minimum project staffing requirements) from the group performance variables (i.e. 229 group heterogeneity and cohesion metrics).

230

231 Materials and methods

232 *Model outline*

In this section, an OR model that allocates a pool of skilled individuals to a series of simultaneous projects with specific staffing (expertise and competence) requirements is proposed and mathematically described in detail. This model will take into account how similar (homogeneous) these individuals are and how they get along with each other (group cohesion).

239	Mathematical notation
240	Let us assume two individuals <i>i</i> and <i>j</i> where <i>i</i> , <i>j</i> belong to a set of <i>n</i> people (workers)
241	who are available to be allocated into teams. Let us assume that these individuals can be
242	combined into a number of non-overlapping teams (subgroups) where each team is noted by
243	the letter k and whose size is noted as n_k (number of members of team k).
244	For every individual i (or j) it is assumed that the following information is known as
245	illustrated in the following examples:
246	• Professional level of competence l_i where $l_i \in L$ and $L = \{\text{junior, intermediate, senior}\}$
247	• Functional department d_i where $d_i \in D$ and $D = \{$ architecture, civil, mechanical, electrical $\}$
248	• Age a_i where a_i = positive integer.
249	• Gender g_i where $g_i \in G$ and $G = \{Male, Female\}$
250	• Ethnicity e_i where $e_i \in E$, and where E , for simplicity, will be assumed here as the
251	continent of origin, that is $E = \{A \text{ frican}, A \text{ ntarctican}, A \text{ sian}, A \text{ ustralian}, E \text{ uropean}, N \text{ orth} \}$
252	American, South American}
253	• Team tenure (seniority in the same group or company) t_i where t_i = positive integer.
254	• Sociometric preference of individual <i>i</i> towards individual <i>j</i> , that is s_{ij} where $i \neq j$, $s_{ij} \in S$ and
255	$S = \{-1, 0, +1\}$. Particularly, $s_{ij} = -1$ means <i>i</i> dislikes working with <i>j</i> , $s_{ij} = 0$ means <i>i</i> is
256	neutral towards (or has never worked with) <i>j</i> , and s_{ij} = +1 means <i>i</i> likes working with <i>j</i> .
257	The set of all values s_{ij} correspond to a non-symmetrical matrix of size $n \times n$.
258	Sociometric preferences aside, these individuals' attributes have been selected here as
259	they were the ones adopted by Gibson and Vermeulen (2003) in their seminal work on group
260	faultlines. This set of attributes has been widely tested in subsequent research (e.g. Chen et

al. 2017a; Meyer and Glenz 2013) and it is still largely accepted that they provide a robust
representation of group diversity.

Hence, given *n* people available from whom we know their l_i , d_i , a_i , g_i , e_i , t_i and s_{ij} , we will create subsets (subgroups/teams) of n_k individuals, each of which will be working on a different project *k*. Individuals can only be allocated to either a single group *k* or no subgroup at all (those unallocated individuals will be idle resources). This implies that no individual can be present in two or more subgroups, even if they could only work part-time in several projects. We use this simplified assumption to make this model more accessible from the point of view of its first mathematical formulation.

Therefore, as implied above, every subgroup *k* will be allocated to a single project and we will note projects and subgroups (teams) with the same subscript *k* from now on. Each project *k* will have specific staffing requirements (p_k). For instance, p_k ={1 senior Architect, 1 intermediate civil engineer, 1 junior civil engineer, 2 intermediate electrical engineers}. Any subgroup of workers n_k that matches or exceeds (both in number and/or competence) these requirements will be considered a feasible subgroup that can potentially be allocated to project *k*.

277

278

8 Team performance measurement

In order to determine which feasible allocation of subgroups is most desirable, it is necessary to anticipate how much better each possible alternative allocation of subgroups would perform if eventually chosen. Additionally, it is worth emphasizing that each feasible allocation might encompass multiple subgroups as each subgroup will be allocated to one project. Therefore, it is necessary to create an index that captures, not just how efficient each subgroup is, but also how efficient all groups are on average; that is, how efficient the

allocation is altogether. This index will be named 'Global Efficiency (E)' and will correspond to a weighted average calculated from the subgroup Efficiencies of each subgroup k (noted as E_k), that is:

$$E = \sum E_k \cdot w_k \tag{1}$$

In this expression, w_k corresponds to the weight of each subgroup k. This way w_k can be calculated, for instance, proportionally to each project k's budget (b_k) . Alternatively, w_k can also be calculated proportionally to the number of people n_k from each project, divided by the total people available n (allocated or not) or the total number of allocated people only (Σw_k) . These alternatives are expressed in equations (2) and (3), respectively:

$$w_k = \frac{b_k}{\sum b_k} \tag{2}$$

295
$$w_k = \frac{n_k}{\sum n_k} \quad \text{or} \quad w_k = \frac{n_k}{n} \tag{3}$$

With the global (allocation) Efficiency E defined in (1) as a function of each
subgroup's
$$E_k$$
 and w_k values, now it is necessary to detail how E_k values can be calculated.
 E_k is a composite efficiency index obtained as the product of two other indices that
represent the expected performance of that subgroup k in terms of its homogeneity (P_k^{SS}) and
social cohesion (P_k^{S}). Namely,

 $E_k = P_k^{SS} \cdot P_k^S \tag{4}$

302 Particularly, P_k^{SS} estimates the Performance of a subgroup k based on the Subgroup 303 Strength (SS) as defined by Gibson and Vermeulen (2003). To calculate the SS value of a 304 subgroup k (noted as SS_k), it will be necessary to calculate the subgroup k's homogeneity 305 value h_k first, as well as the individuals' degree of overlaps in terms of different diversity factors (we will use: functional department, age, gender, ethnicity, and team tenure asjustified later).

308 P_k^S is an index that measures the differential level of performance expected for 309 subgroup k given a particular level of cohesion, which is measured by sociometric indices. In 310 this case, S_k will be calculated as the interpersonal social preferences and rejections stated by 311 all members belonging to subgroup k.

312 What follows are the details on how P_k^{SS} and P_k^S are calculated. Once these two

313 values are known for each potential subgroup k, obtaining E_k will be straightforward with (4).

Let us start with P_k^{SS} , the performance metric coming from the Subgroup Strength metric. Conventionally, a subgroup *k*'s homogeneity h_k has been defined as:

316
$$h_{k} = \frac{\sum_{i < j} \left\{ O_{ij}^{d} + O_{ij}^{a} + O_{ij}^{g} + O_{ij}^{e} + O_{ij}^{t} \right\}}{\frac{n_{k}(n_{k} - 1)}{2}} = \frac{\sum_{i < j} O_{ij}}{\frac{n_{k}(n_{k} - 1)}{2}}$$
(5)

Where O_{ij} is the total overlap between individuals *i* and *j*, and which is computed as the sum of O_{ij}^d , O_{ij}^a , O_{ij}^g , O_{ij}^e and O_{ij}^t which, in turn, represent the overlaps between two individuals *i* and *j* on functional department, age, gender, ethnicity and team tenure, respectively. The sum in the numerator is restrained to *i*<*j* (but it could have also been *i*>*j* indistinctly) to avoid the cases where *i*=*j* (individuals' self-overlaps) as well as to prevent the symmetrical O_{ij} values (that is $O_{ij}=O_{ji}$) from being counted twice.

Also in the same vein, the factor $n_k (n_k-1)/2$ in the denominator of (5) corresponds to the total number of pairs analyzed (all possible combinations of *i* and *j*, excluding those cases where $i \ge j$). With all this in mind, and according to Gibson and Vermeulen (2003), the differentoverlaps between a group of individuals can be calculated as follows:

328 Functional department overlap:
$$O_{ij}^d = 1$$
 if $d_i = d_j$, else 0 (6)

329 Age overlap:
$$O_{ij}^{a} = \frac{\min(a_i, a_j) - 18}{\max(a_i, a_j) - 18}$$
 (7)

330 Gender overlap: $O_{ij}^g = 1$ if $g_i = g_j$, else 0 (8)

331 Ethnicity overlap: $O_{ij}^e = 1$ if $e_i = e_j$, else 0 (9)

332 Team tenure overlap:
$$O_{ij}^{t} = \frac{\min(t_i, t_j)}{\max(t_i, t_j)}$$
 (10)

Overlap values can vary between [0, 1]. Hence, values of h_k will vary between [0, 5]. We are aware that other diversity factors could have also been included in the definition of h_k such as for example, language, education, experience. However, in the interest of keeping to the model's simplicity and for illustrative purpose in the case study which follows, we deemed it reasonable to stick to the diversity factors in the definition of h_k as proposed by Blau (1977) and Allison (1978).

And now that the overlaps of all individuals O_{ij} and the subgroup k's homogeneity value h_k have been detailed, the Subgroup Strength of a subgroup k (SS_k) is defined as the population standard deviation of the O_{ij} values from all n_k members belonging to subgroup k, that is:

343
$$SS_{k} = \sqrt{\frac{\sum_{i < j} (O_{ij} - h_{k})^{2}}{\frac{n_{k}(n_{k} - 1)}{2}}} = Std. Dev. O_{ij}$$
(11)

344	As defined, SS_k will vary from 0 to 1.25 (since h_k domain was restricted to [0,5]).										
345	Additionally, Gibson and Vermeulen (2003) proved that team diversity (represented by										
346	means of SS_k) and group performance were quadratically related (inverted U-shape)										
347	approximately as described in Figure 1a.										
348	<insert 1="" figure="" here=""></insert>										
349	Also, a recent study by Chen et al. (2017) suggested that this quadratic expression is										
350	quasi-symmetrical and that the value of δ seems generally close to 10% on average.										
351	Therefore, the subgroup k's performance P_k^{SS} can be calculated from the subgroup strength										
352	SS_k value as:										
353	$P_k^{SS} = -2.56 \delta SS_k^2 + 3.2 \delta SS_k + 1 - \delta \qquad \text{with } \delta \approx 0.10 $ (12)										
354	Expression (12) can vary between $[1-\delta, 1]$ and is obtained from a quadratic										
355	polynomial which is forced to cross the points: $(0,1-\delta)$, $(1.25/2, 1)$ and $(1.25,1-\delta)$.										
356	On the other hand, the subgroup k's cohesion-related performance index P_k^S is										
357	calculated from the subgroup k members' sociometric preferences s_{ij} towards each other (i.e.										
358	preferences and rejections to work with a particular individual). These preferences and										
359	rejections do not have to be symmetrical (that is, $S_{ij}\neq S_{ji}$ or $S_{ij}=S_{ji}$). Hence, we define a										
360	subgroup k 's cohesion S_k as:										
361	$S_{k} = \frac{\sum_{i \neq j} S_{ij}}{n_{k}(n_{k} - 1)} $ (13)										
362	Similarly, the term $n_k(n_k-1)$ corresponds to the total number of pairs analyzed										
363	excluding the choices of individuals with themselves. So, as s_{ij} can be equal to -1 (meaning <i>i</i>										

dislikes j), 0 (i is neutral or have not met j), or +1 (i likes j), S_k actually represents how well

365 (or badly) all subgroup *k*'s members get along with each other on average. Analogously, S_k 366 can take on values within the range [-1, 1].

367 Finally, previous researchers' results suggest that the average cohesive group seems to perform around 18% better than average (non-cohesive or non-uncohesive) groups (Evans 368 369 and Dion 2012). For the purpose of this paper, this performance differential will be called φ . However, it is worth pointing out that in those previous pieces of research it is not always 370 371 clear how group cohesion is measured or quantified. Also, there is a total absence of studies clarifying whether the cohesion-performance relationship is linear or if it indeed follows a 372 373 different pattern. In light of this, it seems prudent to take the simplest alternative and assume that group cohesion (represented now by S_k) and performance (P_k^S) will just be linearly 374 375 related as represented in Figure 1b. Hence:

$$P_k^S = 1 + \varphi S_k \qquad \text{with } \varphi \approx 0.18 \tag{14}$$

377 After defining expression (13), all variables involved have been presented and related to each other. We are now able to calculate the global group efficiency (E) from the different 378 379 simultaneous subgroups' efficiencies E_k and their respective weights w_k . This is summarized at the bottom of Figure 1. Hence, from now on, every possible subgroups' allocation can be 380 381 measured in relative performance terms and each feasible complete group allocation can be 382 compared against each other. The following is an example to illustrate how we can apply the 383 model based on a fictitious case study which reflects as much as possible, a real project environment. 384

386 Application

387	The case study follows approximately the same order of calculations that was
388	presented in the previous section. For the interested reader, the complete step-by-step
389	calculations can be found in an Excel file accessible from the Supplemental Online Material.
390	Particularly, this case study comprises a group of 20 individuals with different levels
391	of professional competence and who belong to four functional departments. The entire
392	professional, demographic (homogeneity-related) and sociometric (cohesion-related)
393	information from the 20 individuals is described in Figure 2.
394	<insert 2="" figure="" here=""></insert>
395	These 20 individuals are to be allocated to three simultaneous projects, each of which
396	has different staffing (professional level and functional department) requirements as well as
397	budgets. This information is detailed in Figure 3. Also, at the bottom of Figure 3, the weights
398	of each project have been calculated as a function of the project budgets according to
200	
399	expression (2).
399 400	expression (2). <insert 3="" figure="" here=""></insert>
400	<insert 3="" figure="" here=""></insert>
400 401	<pre><insert 3="" figure="" here=""> Any subgroup allocation that meets or exceeds the staffing requirements described in</insert></pre>
400 401 402	Any subgroup allocation that meets or exceeds the staffing requirements described in <p< td=""></p<>
400 401 402 403	
400 401 402 403 404	<insert 3="" figure="" here=""> Any subgroup allocation that meets or exceeds the staffing requirements described in Figure 3 will be a feasible solution. What is necessary now is to be able to calculate the global efficiency E from any feasible grouping solution. With this aim in mind, the first step will be to obtain all individuals' overlaps concerning functional department, age, gender,</insert>
400 401 402 403 404 405	Any subgroup allocation that meets or exceeds the staffing requirements described in Figure 3 will be a feasible solution. What is necessary now is to be able to calculate the global efficiency E from any feasible grouping solution. With this aim in mind, the first step will be to obtain all individuals' overlaps concerning functional department, age, gender, ethnicity and team tenure, so that these values can be reused anytime when two individuals
400 401 402 403 404 405 406	Insert Figure 3 here> Any subgroup allocation that meets or exceeds the staffing requirements described in Figure 3 will be a feasible solution. What is necessary now is to be able to calculate the global efficiency E from any feasible grouping solution. With this aim in mind, the first step will be to obtain all individuals' overlaps concerning functional department, age, gender, ethnicity and team tenure, so that these values can be reused anytime when two individuals are put together in the same subgroup. Due to its length (5 tables, one per type of overlap),

410

<Insert Figure 4 here>

411 What remains is calculating, for any potential and feasible subgroup k, its 412 homogeneity h_k (with expression (5)), subgroup strength SS_k (with expression (11)), and cohesion S_k (with expression (13)) values. Then, with SS_k and S_k , known, calculating the 413 homogeneity-related P_k^{SS} performance metric (with expression (12)) and the cohesion-related 414 P_k^s performance metric (with expression (14)) can be performed. Next, with P_k^{ss} and P_k^s 415 known, we can calculate E_k (by means of expression (4)). Once the values of E_k are all known 416 417 for all the simultaneous subgroups (three in our example, as there are three projects), and by knowing the weight of each subgroup w_k (with expressions (2) or (3), and as detailed at the 418 bottom of Figure 3), it is possible to obtain the global efficiency E of that group configuration 419 by means of expression (1). This series of calculations are represented vertically from top to 420 bottom in the lower half of Figure 5. 421

422

<Insert Figure 5 here>

In Figure 5, a random solution directly allocating the individuals available to meet the project staffing requirement, but without any further (homogeneity, nor cohesion) considerations, is presented. At the top of Figure 5, one can find the allocation of each individual to each subgroup/project. The column to the right sums each individual's allocations and verifies that no individual is allocated more than 100%, that is, to more than one project. These are necessary but not sufficient problem constraints which need to be met to qualify any allocation as feasible.

However, every time there is any change (for instance a member is allocated to a
different project/subgroup), all values need to be recalculated. Therefore, the only way of
finding good solutions is by iterating these calculations multiple times while testing as many

feasible solutions as possible. Hence, for the model to be practically useful, this task must beautomated by an optimization algorithm.

435	The global efficiency of the random solution depicted in Figure 5 corresponds to
436	0.981. By definition, the value of the global efficiency E will vary between $[1-\delta-\phi, 1+\phi]$.
437	Hence, the closer the value of E to $1+\phi$, the higher the expected groups' performance. Now,
438	in looking for that optimum solution, there is one last point to be discussed.

As discussed earlier, the proposed model falls within a particular case of the MTFP. 439 The MTFP is NP-hard, and that opens the door to the use of metaheuristics when looking for 440 441 (near) optimum solutions. Among common metaheuristics, Genetic Algorithms (GA) are one 442 of the quicker and simpler, but also effective, options. On top of that, they are usually available within commercial solvers included by default in spreadsheet software like 443 444 Microsoft Excel ®. Moreover, GA have been in use in resource-constrained allocation for a long time and they have been considered as one of the most efficient metaheuristics when 445 446 dealing with the MTFP in recent studies (e.g. Ahmadian Fard Fini et al. 2016; Awal and Bharadwaj 2014). For all these reasons, we will use GA for solving multiple instances of our 447 case study and find a quick and good (despite maybe less than optimal) solution. 448

Therefore, once the model is implemented in a spreadsheet where every time a new allocation is proposed all the subgroup calculations can be automatically and instantly updated, the GA can start looking for new solutions. The problem constraints are the ones specified in grey cells (one per individual's maximum allocation time plus one per project staffing requirements check). The objective function corresponds to E, which on this occasion is to be maximized. On resorting to Excel Solver, the best solution was found in seconds by our GA as shown in Figure 6.

456

<Insert Figure 6 here>

457	The solution shown in Figure 6 (with E=1.087) is comparatively much more efficient
458	than the one from Figure 5 (with E=0.981). If the same GA would have been aimed at
459	minimizing E, the worst solution found (not included) would have had an E=0.911. Within
460	the [1- δ - ϕ , 1+ ϕ] interval, the three solutions correspond to the following percentiles: 56.7%
461	(the random solution), 79.8% (the best solution) and 41.5% (the worst solution). As can be
462	seen, based on the results, there seems to be valid reasons to try to optimize the model
463	outputs with the help of an optimization algorithm. Mostly, when doing this manually, would
464	have been an unsurmountable task.

465

466 Validation

467 In the previous section it was shown how the model can be implemented to fulfill its most common purpose: finding the optimum (or near optimum) allocation of a set of 468 available human resources into a series of projects, each with not necessarily equal staffing 469 470 requirements. However, before accepting that the model outputs constitute a fair description 471 of reality, it is necessary to verify whether its parameters actually influence different levels of team performance. Particularly, the most relevant model parameters are the ones proposed in 472 equations (12) and (14), that is, the group diversity-related performance (P_k^{SS}) and the social 473 cohesion-related performance (P_k^S). Hence, if higher values of these two parameters exhibit 474 475 correlation with higher values of team performance, the model will be of some value. Conversely, if there is no such correlation, the model, at least as currently formulated, would 476 render useless. 477

With this purpose in mind, a first exploratory and validation study was conducted
comprising the academic performance of fifteen MSc Civil Engineering students at the
Universidad de Talca (Chile). This group of students were enrolled in a module named

481 'Projects' which is a transversal integration module and its purpose is to determine how well 482 students can apply knowledge and understanding from previous related modules. The module was led by one of the authors in the second semester of 2017. It required that fifteen students 483 484 submitted three assignments (projects) each. The three projects which will be named Project 1, Project 2 and Project 3, had progressive submission dates every two months. Students 485 worked in groups of five to deliver these three projects. After each project was completed, the 486 487 groups were reshuffled so that most students had to work with different team mates in the next project. 488

In short, for the first assignment (Project 1), there were three groups with 5 students (named here as groups A, B and C) each submitting a different project. The same happened for Project 2 and 3, but with groups whose member composition was different from Project 1. Each of these three projects was assessed and given a mark between 0 and 100. In total, there were 9 different marks: one per assignment (Project 1, 2 and 3) and group (A, B and C). However, each student only received three marks (one from each Project) whose average resulted in the module's final mark for him/her.

The demographic attributes of the fifteen students can be found in Figure 7. By columns, the five individuals' attributes had a close equivalence with the five attributes described in our model: background (akin to functional department), age, gender, ethnicity and work experience (akin to team tenure). However, as expected from a group of students, the sample was also relatively more homogeneous than other real-life projects (most individuals had similar ages, similar experience, and a less varied set of backgrounds/degrees).

503

<Insert Figure 7 here>

The group demographic attributes were directly retrieved from their registrations information. This MSc programme required a minimum work experience of 2 years as an admission criterion. This is the reason why most students exhibit similar years of experience, but also similar ages. Additionally, most were local students, which meant most of them were South American.

The Sociometric individuals' preferences matrix was populated using the registration of the same students for a series of lab sessions which ran in parallel to this module. Particularly, before allocating the fifteen students to those lab sessions, they were asked with whom they would like to carry out the lab sessions and whom they would prefer to avoid. Although it was not compulsory for the instructors to implement those preferences, those registers proved useful later for allocating the students to the Project groups, and also to populate the sociometric matrix.

516 Finally, the last three columns in Figure 7 correspond to the three marks that each517 student was awarded at the end of the module.

The information from Figure 7 is enough to develop a first, simple, and representative correlation analysis between the model parameters and team performance. For this purpose, the groups' homogeneity, subgroup strength and social cohesion values were calculated for the nine five-student groups that submitted the three projects. With these values, calculating the group diversity- and cohesion-related performances was straightforward. These calculations are all presented, along with the students' allocations, in Figure 8.

524

<Insert Figure 8 here>

525 Values highlighted in blue, red and green correspond to Projects 1, 2 and 3, which 526 were also identified in the last three columns of Figure 7. For reference purposes, the project 527 marks were also shown at the bottom row of Figure 8.

The last step consists of showing how the regression plots of the variables included in the model align with the expected performance outputs. For this purpose, several plots are shown in Figure 9 from the numerical data represented in the lower rows of Figure 8.

531

<Insert Figure 9 here>

532 Figures 9a) and 9b) show how subgroup strength and group social cohesion are 533 related to group diversity-related and group cohesion-related performance, respectively, 534 based on equations (12) and (14). Additionally, in Figures 9d) and 9e), we can see how group 535 diversity-related performance and group-cohesion related performance are both related to 536 team performance as well (team performance is represented by the project marks). The very 537 fact that these two graphs exhibit approximately linear trends between the X and Y variables 538 indicate that the regression expressions represented in Figures 9a) and 9b) were supported. 539 This is because expressions (12) and (14) are actually transforming the group diversityrelated (from Figure 9a) and group cohesion-related performance (from Figure 9b) into a 540 541 series of points with a linear correlation with Team Performance. If that had not been the 542 case, then there would be no linear relationship, and quite possibly, no trend would be found at all. 543

Finally, Figure 9c) represents the Y-axis variables from Figures 9a) and 9b) and
barely shows any trend. This proves that the level of correlation between subgroup strength
and group cohesion is very low. This relationship was also hypothesized earlier and this is
proven numerically and graphically here.

548 Therefore, a quick observation of the three plots at the bottom of Figure 9 show 549 evidence of a moderate/strong correlation between the model parameters (independent 550 variables) and the project marks (dependent variable). As the project marks can be considered 551 as a good proxy for group performance, we can conclude that the model formulation seems to

be fairly representative and is correctly indicating that certain heterogeneity-related andcohesion-related group attributes can ultimately lead to higher (or lower) team performances.

554 Of course, the conclusions of this validation case study have to be taken with some caution too. The analysis is based on an academic environment, rather than a real project. 555 556 Real life projects tend to consist of a more diverse group of professionals (higher dispersion 557 of the demographic attributes) with generally many more variables which may be difficult (but necessary) to control. Notwithstanding this, we acknolwedge further validation using 558 559 real projects is needed in order to improve the validity of the model. However, resorting to an 560 academic environment also has numerous advantages. First, the outcome of 'project' 561 performance can be known (under some simplifying assumptions) as all assignments are 562 graded and awarded a mark. And second, these project cycles are usually faster which also allows data retrieval to be generated faster than in real-life projects. 563

Other limitation of our validation case study is the reduced number of points (only 564 565 nine) and the reduced variation of some of the performance measurements. In connection with the latter, the cohesion-related performance values of Projects 2 and 3 are very close to 566 567 each other, obscuring the type of relationship that more dispersed values could have shown. 568 Also, although the rest of the cases show clearer trends, it is necessary to point out that these might not be necessarily linear. This, despite us resorting to three points, two of them still 569 570 remain too close in the cohesion-related performance graph to infer properly potentially nonliner trends. 571

Finally, it is clear from Figure 9 that Project 1 seemed to be more challenging to the students as they all got lower marks (probably because it was the first assignment), whereas the other two seemed easier (they received higher marks). Similarly, for future validation studies, it will be advisable to gather individual marks from each student (by means of individual exams, for example). Only with this additional piece of information, will it be

possible to better compare different levels of group members' performance (as groups madeup of bright people usually perform better than ones with mediocre students).

579

580 Discussion

In this paper, a new model for allocating human resources that considers team functional requirements, group heterogeneity and social cohesion has been proposed and validated. In formulating the model, a few simplifications and constraints were assumed. These will be now be reviewed and discussed in detail.

First of all, as stated earlier, this model has necessarily oversimplified the nature of 585 586 real life work collaboration issues. Real life team work is complex and dynamic. Certainly, it 587 cannot be reduced to two variables -group diversity and social cohesion-without neglecting 588 aspects that make from group collaboration something rich and distinct from other 589 engineering and technical challenges. In real life, group members' exhibit behaviors and 590 possess attributes that have not been included in this model (e.g. how introvert/extrovert 591 group members are; their dedication, devotion, preferences or just personal or professional 592 interests or goals; their soft skills or motivation to work in groups; the asymmetrical personal relationships as a consequence of the lines of command, etc.). However, the intention here 593 was not to include an exhaustive list of group attributes but to present a simple and self-594 595 contained model. And despite all the necessary simplifications, the model still seems to be robust, at least, based on the preliminary validation results shown here. The inclusion of 596 further variables will be something that, no doubt, will be considered in future versions of the 597 598 model when it is applied in real project settings.

599 Secondly, one might raise the question that the way group heterogeneity and cohesion600 have been defined in this paper might lead to some collinearity or, at least, covariance

between the two constructs. This is because there is a possibility that both may be capturing some common aspects of a group configuration. Our model, however, has instrumented both constructs in a multiplicative way, that is, $P_k^{SS} \times P_k^S$, not additive, because they do not substitute for one another when contributing to subgroup performance E_k . All the same, we agree that this might be an over simplification, but existing research so far does not seem to have reached an agreement on whether this is an untenable assumption.

607 For example, Festinger et al. (1950) in an early attempt found contradicting results in 608 two experiments analyzing the group heterogeneity-cohesion relationship. Much more 609 recently, Dion (2000), on performing analysis in two houses of war veterans found again inconclusive findings indicating that in one house cohesion was related with homogeneity, 610 611 whereas in the other it was not. And even more recently, in a study conducted by Chiocchio 612 and Essiembre (2009), it was shown that a group's homogeneity or heterogeneity does not appear to affect the social cohesion-behavioral performance correlations in either academic or 613 614 organizational settings. In line with this, probably the most enlightening stance has been the one taken by Sturgis et al. (2014), who claimed that the relationships between the different 615 subcomponents of group heterogeneity and cohesion might be very different from each other, 616 even cancelling out each other's effects. They also emphasized that more research is 617 618 necessary to validate this.

However, and fortunately, because our model only tries to relatively (not absolutely) generate the most desirable subgroups allocations from the same pool of human resources, the effect of potential (if existing) collinearities between subcomponents of heterogeneity and cohesion will not be that critical so as to invalidate the model. This, as despite correlation between both variables might cause some scale distortion, the relative rank (order) of solutions should not have altered much.

Additionally, other simplifications have been assumed along the model formulation.
Probably the two most relevant have been limiting the allocations of individuals to be in fulltime working arrangement and not part-time. Also, the relationship between group cohesion
and group performance has been assumed to be linear.

The first simplification is relatively easy to address but it would complicate the mathematical expressions to a point where they are no longer that intuitive. In this paper, we have tried to encourage understanding of the model's utility and to avoid distractions by complicating it too much. However, allowing part-time allocations might make finding better solutions somewhat easier for an optimization algorithm. This, as the objective functions of many OR models are generally easier to optimize when the decision variables are closer to being continuous (Gutiérrez et al., 2016).

Finally, the second simplification cannot be satisfactorily addressed until there is more research to determine the nature of the cohesion-performance relationship. This might be a critical aspect for further model development. It may indeed lead to some adjustments in some of the equations (probably in expression (4) and surely in expression (14)), but for now there is no point in us speculating how it might impact the model formulation, or indeed if there is such an impact at all.

642

643 Conclusions

A model that allocates human resources to multiple projects with specific staffing
requirements while also considering group homogeneity and cohesion has been proposed.
This model constitutes a powerful and practical tool for any project manager who needs to
efficiently allocate human resources and who wants to maximize the expected productivity of
his/her group members. The mathematical expressions are, in general, quite straightforward

and can be easily implemented by means of a spreadsheet. The optimization algorithm for
finding near-optimal solutions can also be implemented with the aid of a very simple
commercial solver like Excel Solver (currently a free, despite capped, version of Frontline
Solvers®).

Human resources are a key component of project success, but there is a lack of
practical, quantitative tools that allow project managers to efficiently allocate these resources
and build high performing teams. There are many reasons that can keep a team from
functioning effectively. In this paper, two factors that are found to strongly and consistently
influence group performance – group homogeneity and group cohesion – have been
incorporated within the model. This model allows the measuring and comparing of any set of
feasible subgroup allocations to several projects simultaneously.

Namely, group homogeneity has been defined by the subgroup strength metric and the 660 sum of overlaps between subgroup members on five different demographic sub-factors 661 662 (functional department, age, sex, ethnicity and team tenure). Group cohesion has been defined as the degree of acceptance (or rejection) that all members have with each other. The 663 664 information on the five sub-factors in the group cohesion construct is generally very easy to 665 obtain from the group members' professional profiles. In terms of the degree of acceptance/rejection that each group member has toward the rest of their group members, 666 667 these can generally be known by using sociometric questionnaires. The latter, despite its limitations, have also been proven in previous research to be quite representative and 668 669 relatively easy to use and update. Basically, these questionnaires require asking all group 670 members who have finished a project: "Who would you like to keep working with?" and 671 "Who would you prefer not to work with? From the group members' answers it is possible to populate (and keep updating) a sociometric matrix that is eventually useful for measuring 672 673 how cohesive each potential subgroup is or can be.

Furthermore, previous research has proven that group homogeneity can reduce/increase group performance by up to 10% on average. Similarly, group cohesion is responsible for average increases (or decreases) of group performance by up to 18%. Both figures have been included in the proposed model and allow the objective measuring of the relative group performance differences between multiple feasible subgroups. Feasible subgroups are those who fulfill the minimum project staffing requirements stated by some simultaneous projects.

With all this, the proposed mathematical model has been detailed concerning all its components and variable relationships. A fictitious case study involving twenty workers who are allocated to three projects have been proposed and solved by means of a simple Genetic Algorithm. Finally, a validation case study based on an academic setting has also been included which involved fifteen MSc students who were allocated to three groups and were required to complete three sequential projects.

The proposed model is a simple and yet powerful way of addressing the commonplace challenges of a typical project manager in efficiently allocating human resources in projects. Despite some intentional simplifications, the model shows promise in helping project managers to make more objective and efficient decisions about their human resource allocations. However, more validating studies will be required in the future to test the actual utility of the model in real project contexts.

Although validation with real projects is necessary, this will also increase the complexity of the model's application due to the number of variables to be considered, as well as generally bigger team sizes. Indeed, this wider range of variables will have some human resource implications in terms of the sturcture of social cohesion of individuals within the projects. For example, the interactions amongst members in real projects may be underpinned by career-related imperatives, and hence, are likely to be more dynamic and

699	nuanced, when compared with students'. In this vein, a potentially fruitful avenue for future
700	research would be to use real life projects in conjunction with using academic projects as
701	controlled experiment to enable researchers to study the nature and structure of social
702	cohesion more precisely.
703	
704	Data availability
705	All data generated or analyzed during the study are included in the submitted article
706	or supplemental materials files.
707	
708	References
709 710 711 712	Agrawal, R., Golshan, B., and Terzi, E. (2014). "Grouping students in educational settings." <i>Proceedings of the 20th ACM SIGKDD international conference on Knowledge</i> <i>discovery and data mining - KDD '14</i> , ACM Press, New York, New York, USA, 1017– 1026.
713 714 715	Ahmadian Fard Fini, A., Akbarnezhad, A., Rashidi, T. H., and Waller, S. T. (2017). "Job Assignment Based on Brain Demands and Human Resource Strategies." <i>Journal of</i> <i>Construction Engineering and Management</i> , 143(5), 4016123.
716 717 718	 Ahmadian Fard Fini, A., Rashidi, T. H., Akbarnezhad, A., and Travis Waller, S. (2016). "Incorporating Multiskilling and Learning in the Optimization of Crew Composition." <i>Journal of Construction Engineering and Management</i>, 142(5), 4015106.
719 720 721	Al-Bayati, A. J., Abudayyeh, O., Fredericks, T., and Butt, S. E. (2017). "Managing Cultural Diversity at U.S. Construction Sites: Hispanic Workers' Perspectives." <i>Journal of Construction Engineering and Management</i> , 143(9), 4017064.
722	Allison, P. D. (1978). "Measure of inequality." American Sociological Review, 43, 865-880.
723 724 725	Anvuur, A. M., and Kumaraswamy, M. M. (2016). "Effects of Teamwork Climate on Cooperation in Crossfunctional Temporary Multi-Organization Workgroups." <i>Journal</i> of Construction Engineering and Management, 142(1), 4015054.
726 727 728	Awal, G. K., and Bharadwaj, K. K. (2014). "Team formation in social networks based on collective intelligence – an evolutionary approach." <i>Applied Intelligence</i> , Kluwer Academic Publishers, 41(2), 627–648.
729 730 731	Ballesteros-Pérez, P., González-Cruz, M. C., and Fernández-Diego, M. (2012). "Human resource allocation management in multiple projects using sociometric techniques." <i>International Journal of Project Management</i> , 30(8).
732	Beal, D. J., Cohen, R. R., Burke, M. J., and McLendon, C. L. (2003). "Cohesion and

- performance in groups: a meta-analytic clarification of construct relations." *The Journal of applied psychology*, 88(6), 989–1004.
- 735 Blau, P. M. (1977). *Inequality and Heterogeneity*. Free press, New York.
- Castaño, N., Watts, T., and Tekleab, A. G. (2013). "A reexamination of the cohesionperformance relationship meta-analyses: A comprehensive approach." *Group Dynamics: Theory, Research and Practice*, 17(4), 207–231.
- Chang, A., and Bordia, P. (2001). "A Multidimensional approach to the Group Cohesion –
 Group Performance relationship." *Small Group Research*, 32(4), 379–405.
- Chen, S., Wang, D., Zhou, Y., Chen, Z., and Wu, D. (2017a). "When too little or too much hurts: Evidence for a curvilinear relationship between team faultlines and performance." *Asia Pacific Journal of Management*, Asia Pacific Journal of Management, 34(4), 931– 950.
- Chen, Y., McCabe, B., and Hyatt, D. (2017b). "Relationship between Individual Resilience,
 Interpersonal Conflicts at Work, and Safety Outcomes of Construction Workers." *Journal of Construction Engineering and Management*, 143(8), 4017042.
- 748 Chiocchio, F., and Essiembre, H. (2009). Cohesion and Performance: A Meta-Analytic
 749 *Review of Disparities Between Project Teams, Production Teams, and Service Teams.*750 *Small Group Research.*
- Dion, K. L. (2000). "Group cohesion: From 'Field of Forces' to Multidimensional Construct." *Group Dynamics: Theory, Research, and Practice*, 4(1), 7–26.
- Dorn, C., and Dustdar, S. (2010). On the Move to Meaningful Internet Systems: OTM 2010.
 Lecture Notes in Computer Science (including subseries Lecture Notes in Artificial Intelligence and Lecture Notes in Bioinformatics), Lecture Notes in Computer Science, (R. Meersman, T. Dillon, and P. Herrero, eds.), Springer Berlin Heidelberg, Berlin, Heidelberg.
- Farley, P. C., and Gibson, C. B. (2002). *Multinational Work Teams: A New Perspective*.
 Mahwah, N.J.: Lawrence Erlbaum Associates.
- Fvans, C. R., and Dion, K. L. (2012). "Group Cohesion and Performance: A Meta-Analysis."
 Small Group Research, 43(6), 690–701.
- Farhadi, F., Hoseini, E., Hashemi, S., and Hamzeh, A. (2012a). "TeamFinder: A Coclustering based Framework for Finding an Effective Team of Experts in Social Networks." 2012 IEEE 12th International Conference on Data Mining Workshops, IEEE, 107–114.
- Farhadi, F., Sorkhi, M., Hashemi, S., and Hamzeh, A. (2011). "An Effective Expert Team
 Formation in Social Networks Based on Skill Grading." *2011 IEEE 11th International Conference on Data Mining Workshops*, IEEE, 366–372.
- Farhadi, F., Sorkhi, M., Hashemi, S., and Hamzeh, A. (2012b). "An Effective Framework for
 Fast Expert Mining in Collaboration Networks: A Group-Oriented and Cost-Based
 Method." *Journal of Computer Science and Technology*, 27(3), 577–590.
- Festinger, L., Schachter, S., and Back, K. (1950). Social pressures in informal groups; a
 study of human factors in housing. Harper, Oxford, England.
- Gajewar, A., and Sarma, A. Das. (2012). "Multi-skill collaborative teams based on densest
 subgraphs." *Proceedings of the 12th SIAM International Conference on Data Mining*, *SDM 2012*, 165–176.

- Gibson, C., and Vermeulen, F. (2003). "A Healthy Divide : Subgroups as a Stimulus for
 Team Learning Behavior." *Administrative Science Quarterly*, 48(2), 202–239.
- Gutiérrez, J. H., Astudillo, C. A., Ballesteros-Pérez, P., Mora-Melià, D., and Candia-Véjar,
 A. (2016a). "The multiple team formation problem using sociometry." *Computers and Operations Research*, 75.
- Gutiérrez, J. H., Astudillo, C. A., Ballesteros-Pérez, P., Mora-Melià, D., and Candia-Véjar,
 A. (2016b). "The multiple team formation problem using sociometry." *Computers and Operations Research*, Elsevier, 75, 150–162.
- Hendriks, M. H. A., Voeten, B., and Kroep, L. (1999). "Human resource allocation in a
 multi-project R&D environment: Resource capacity allocation and project portfolio
 planning in practice." 17(3), 181–188.
- Lappas, T., Liu, K., and Terzi, E. (2009). "Finding a team of experts in social networks."
 Proceedings of the 15th ACM SIGKDD international conference on Knowledge discovery and data mining KDD '09, ACM Press, New York, New York, USA, 467.
- Lau, D. C., and Murnighan, J. K. (2005). "Interactions within Groups and Subgroups: The
 Effects of Demographic Faultlines." *The Academy of Management Journal*, Academy of
 Management.
- Li, C.-T., and Shan, M.-K. (2010). "Team Formation for Generalized Tasks in Expertise
 Social Networks." 2010 IEEE Second International Conference on Social Computing,
 IEEE, 9–16.
- Lott, A. J., and Lott, B. E. (1965). "Group cohesiveness as interpersonal attraction: A review
 of relationships with antecedent and consequent variables." *Psychological Bulletin*,
 64(4), 259–309.
- Mathieu, J. E., Kukenberger, M. R., D'Innocenzo, L., and Reilly, G. (2015). "Modeling
 Reciprocal Team Cohesion Performance Relationships, as Impacted by Shared
 Leadership and Members ' Competence Modeling Reciprocal Team Cohesion –
 Performance Relationships, as Impacted by Shared Leadership and Me." *Journal of Applied Psychology*, 100(3), 713–734.
- Meyer, B., and Glenz, A. (2013). "Team Faultline Measures: A Computational Comparison
 and a New Approach to Multiple Subgroups." *Organizational Research Methods*, 16(3),
 393–424.
- Moreno, J. L. (1941). "Foundations of Sociometry: An Introduction." *Sociometry*, 4(1), 15–
 35.
- Phua, F. T. T. (2004). "The antecedents of co-operative behaviour among project team
 members: an alternative perspective on an old issue." *Construction Management and Economics*, Taylor & Francis Group, 22(10), 1033–1045.
- Phua, F. T. T., and Rowlinson, S. (2004). "How important is cooperation to construction
 project success? A grounded empirical quantification." *Engineering, Construction and Architectural Management*, Emerald Group Publishing Limited, 11(1), 45–54.
- Salo, M. (2006). *The Relation Between Sociometric Choices and Group Cohesion*. Arlington,
 Virginia.
- Shi, Z., and Hao, F. (2013). "A strategy of multi-criteria decision-making task ranking in social-networks." *The Journal of Supercomputing*, 66(1), 556–571.
- 820 Sorkhi, M., Alvari, H., Hashemi, S., and Hamzeh, A. (2012). "A game-theoretic framework

- to identify top-k teams in social networks." *KDIR 2012 Proceedings of the International Conference on Knowledge Discovery and Information Retrieval*, 252–257.
- Sturgis, P., Brunton-Smith, I., Kuha, J., and Jackson, J. (2014). "Ethnic diversity, segregation
 and the social cohesion of neighbourhoods in London." *Ethnic and Racial Studies*,
 Taylor & Francis, 37(8), 1286–1309.
- Teixeira, L. O., and Huzita, E. H. M. (2014). *DiSEN-AlocaHR: A Multi-Agent Mechanism for Human Resources Allocation in a Distributed Software Development Environment International Conference*. Advances in Intelligent Systems and Computing, (S. Omatu,
 H. Bersini, J. M. Corchado, S. Rodríguez, P. Pawlewski, and E. Bucciarelli, eds.),
 Springer International Publishing, Cham.
- Tseng, T.-L. (Bill), Huang, C.-C., Chu, H.-W., and Gung, R. R. (2004). "Novel approach to
 multi-functional project team formation." *International Journal of Project Management*,
 22(2), 147–159.
- Xia, N., Zhong, R., Wu, C., Wang, X., and Wang, S. (2017). "Assessment of StakeholderRelated Risks in Construction Projects: Integrated Analyses of Risk Attributes and
 Stakeholder Influences." *Journal of Construction Engineering and Management*, 143(8),
 4017030.
- Yin, H., Cui, B., and Huang, Y. (2011). Advanced Data Mining and Applications. Lecture
 Notes in Computer Science (including subseries Lecture Notes in Artificial Intelligence
- and Lecture Notes in Bioinformatics), Lecture Notes in Computer Science, (J. Tang, I.
- 841 King, L. Chen, and J. Wang, eds.), Springer Berlin Heidelberg, Berlin, Heidelberg.

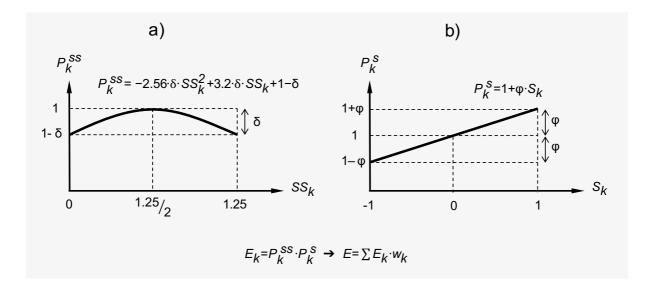


Fig. 1. Team *k*'s relative homogeneity-related performance (a) and relative cohesion-related performance (b) calculations

Group homogeneity-related information								cio	mei	tric	pre	fere	nce	e to	wa	rds	indi	ividu	ıal j	(s _{ij})						
Indiv. (i)	Prof. level (I i)	Funct. dept. (d i)	Age (a _i)	Gender (g _i)	Ethnicity (e _i)	Te. ten. (t _i)	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	Senior	Architecture	60	Male	European	25		0	-1	0	1	1	1	-1	0	1	1	0	0	0	1	0	1	0	0	0
2	Senior	Architecture	50	Female	European	20	0		0	1	0	0	0	1	1	-1	0	0	1	1	1	1	1	1	0	0
3	Senior	Architecture	40	Male	North Amer.	10	0	1		1	1	1	1	0	1	1	1	1	1	-1	0	0	1	0	0	0
4	Intermediate	Architecture	35	Male	North Amer.	5	0	1	1		0	0	1	1	1	1	0	-1	0	1	1	0	1	0	0	0
5	Junior	Architecture	25	Female	Asian	5	1	1	0	1		1	0	1	1	0	0	0	0	0	0	1	0	0	0	-1
6	Senior	Civil eng.	55	Male	Asian	10	0	1	1	1	-1		1	0	1	0	0	0	0	1	0	0	1	0	0	1
7	Senior	Civil eng.	45	Male	Australia	15	0	0	-1	-1	0	1		1	0	0	0	1	-1	0	-1	1	1	1	0	1
8	Intermediate	Civil eng.	45	Male	European	15	0	1	-1	0	0	1	1		1	-1	0	0	0	0	1	1	1	0	1	0
9	Intermediate	Civil eng.	35	Male	European	2	0	0	1	1	-1	-1	1	0		-1	1	-1	0	1	1	0	0	0	0	0
10	Junior	Civil eng.	30	Female	African	1	0	0	1	-1	1	-1	0	0	1		1	0	1	0	1	0	1	0	1	-1
11	Senior	Mechanical eng.	65	Male	European	40	0	0	1	-1	0	0	-1	1	0	-1		1	0	1	0	0	1	1	-1	0
12	Senior	Mechanical eng.	60	Male	European	35	0	0	0	0	-1	0	0	1	0	1	0		-1	-1	0	1	0	1	0	-1
13	Intermediate	Mechanical eng.	35	Male	North Amer.	15	0	1	0	0	1	0	0	1	1	-1	0	0		1	0	1	0	-1	0	1
14	Junior	Mechanical eng.	35	Female	Australia	5	1	0	-1	1	1	0	-1	0	0	0	1	0	1		-1	0	-1	0	1	1
15	Junior	Mechanical eng.	25	Male	European	5	1	0	0	0	0	0	0	0	0	1	1	1	1	0		0	-1	0	0	1
16	Senior	Electrical eng.	50	Male	European	20	-1	0	1	1	0	0	0	1	1	0	0	-1	-1	1	1		0	0	0	1
17	Senior	Electrical eng.	45	Male	Australia	15	0	0	0	0	0	0	0	0	0	-1	0	1	-1	0	1	0		1	0	0
18	Senior	Electrical eng.	40	Male	Asian	10	-1	-1	0	1	0	0	0	0	0	-1	0	1	0	1	0	-1	0		1	0
19	Intermediate	Electrical eng.	35	Male	South Amer.	10	-1	1	0	1	0	1	0	0	1	1	-1	-1	0	0	0	-1	1	1		0
20	Intermediate	Electrical eng.	30	Female	North Amer.	10	1	0	0	-1	0	1	1	1	0	1	1	1	1	1	-1	1	1	0	-1	

Fig. 2. Group of resources' professional, homogeneity and sociometric information

	Proje	Project k minimum staff requirements (p _k)										
Funct. Dept. (d _i)	Prof. level (I ;)	1	2	3								
Architecture	Senior	1	0	1								
	Intermediate	0	1	0								
	Junior	0	0	1								
Civil engineering	Senior	0	1	0								
	Intermediate	1	0	1								
	Junior	0	1	0								
Mechanical engineering	Senior	1	0	0								
	Intermediate	0	1	0								
	Junior	0	0	2								
Electrical engineering	Senior	0	0	1								
	Intermediate	1	1	1								
	Junior	1	0	0								

Project k budget (b _k)	\$2,500,000	\$1,500,000	\$1,000,000
Project k weight (w _k)	0.50	0.30	0.20

Fig. 3. Minimum project staffing requirements

	Tota	l overl	aps (l	0 _{ij} =0	^d ij+0	^a _{ij} +0 ^g	' _{ij} +0°	_{ij} +0 ^t ij)											
Indiv. ↓i & j →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1		3.56	2.92	2.60	1.37	2.28	2.24	3.24	2.48	0.33	3.52	3.71	2.00	0.60	2.37	3.56	2.24	1.92	1.80	0.69
2			2.19	1.78	2.47	1.36	1.59	2.59	1.63	1.43	2.18	2.33	1.28	1.78	1.47	3.00	1.59	1.19	1.03	1.88
3				4.27	1.82	2.59	2.48	2.48	1.97	0.65	1.72	1.81	3.44	1.27	1.82	2.19	2.48	3.00	2.77	2.55
4					2.41	1.96	1.96	1.96	2.40	0.91	1.49	1.55	3.33	2.00	2.41	1.78	1.96	2.27	2.50	2.21
5						1.69	0.59	0.59	0.81	·····	0.27	0.31	0.75	2.41	2.00	0.47	0.59	1.82	0.91	2.08
6							3.40	3.40	2.66	1.42	2.04	2.17	2.13	0.96	1.69	2.36	2.40	3.59	2.46	1.32
7								4.00		1.51								2.48		1.11
8									3.76	1.51							3.00	2.48	2.30	1.11
9										2.21	2.41	2.46	2.13	1.40	2.81	2.63	1.76	1.97	2.20	0.91
10											0.28	0.31	0.77	1.91	0.78	0.43	0.51	0.65	0.81	2.10
11												4.77		1.49				1.72	1.61	0.51
12													2.83	1.55				1.81	1.69	0.57
13														2.33		2.28		2.44	2.67	2.37
14															2.41	0.78	1.96	1.27	1.50	2.21
15																2.47	1.59	1.82	1.91	1.08
16																	3.59	3.19		1.88
17																		3.48	3.30	
18																			3.77	
19																				2.71
20																				

Fig. 4. Total overlaps calculations

			Staff i allocations to each project p k										
Indiv. (i)	Prof. level (I _i)	Funct. Dept. (d _i)	1	2	3	Allocated time							
1	Senior	Architecture	1	0	0	1							
2	Senior	Architecture	0	0	1	1							
3	Senior	Architecture	0	0	0	0							
4	Intermediate	Architecture	0	1	0	1							
5	Junior	Architecture	0	0	1	1							
6	Senior	Civil engineering	0	1	0	1							
7	Senior	Civil engineering	0	0	0	0							
8	Intermediate	Civil engineering	1	0	0	1							
9	Intermediate	Civil engineering	0	0	1	1							
10	Junior	Civil engineering	0	1	0	1							
11	Senior	Mechanical engineering	1	0	0	1							
12	Senior	Mechanical engineering	0	0	0	0							
13	Intermediate	Mechanical engineering	0	1	0	1							
14	Junior	Mechanical engineering	0	0	1	1							
15	Junior	Mechanical engineering	0	0	1	1							
16	Senior	Electrical engineering	0	0	1	1							
17	Senior	Electrical engineering	0	0	1	1							
18	Senior	Electrical engineering	0	1	0	1							
19	Intermediate	Electrical engineering	1	0	0	1							
20	Intermediate	Electrical engineering	1	0	0	ľ							
		г											
	Sta	ff requirements check (1/0)	1	1	1	Constraints							
		Team k's size (m _k)	5	5	7								
		Г				_							
		<pre>Feam k's homogeneity (h k)</pre>	2.04	1.95	1.89								
		s Subgroup Strength (SS _k)	1.01	0.97	0.80								
Diversity-rela	ted perform. (P ^{SS} _k =	-2.56δSS _k ² +3.2δSS _k +1-δ)	0.96	0.97	0.99								
						_							
	Tea	m k's social cohesion (S _k)	0.05	-0.05	0.26								
	Cohesion-related p	erformance ($P^{S}_{k}=1+\phi \cdot S_{k}$)	1.01	0.99	1.05								
		-				_							
	Team k's	$= Efficiency (E_k = P^{SS}_k \cdot P^S_k)$	0.97	0.96	1.04								
		Project k weight (w_k)	0.50	0.30	0.20								
					-	_1							

Staff i allocations to each project p k

Global allocation Efficiency (E=SE_k·w_k) (maximise) = **0.981** [1- δ - ϕ , 1+ ϕ] = [0.72, 1.18]

Fig. 5. An example of a feasible resources' allocation

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$				Staff i allocations to each project p k										
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Indiv. (i)	Prof. level (I i)	Funct. Dept. (d _i)	1	2	3	Allocated time							
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	1	Senior	Architecture	0	0	0	0							
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	2	Senior	Architecture	0	0	1	1							
5 Junior Architecture 0 0 0 6 Senior Civil engineering 1 0 1 7 Senior Civil engineering 0 1 0 1 8 Intermediate Civil engineering 0 1 0 1 9 Intermediate Civil engineering 0 1 0 1 10 Junior Civil engineering 0 0 0 1 11 Senior Mechanical engineering 0 0 1 1 12 Senior Mechanical engineering 0 1 1 1 13 Intermediate Mechanical engineering 0 1 1 1 14 Junior Mechanical engineering 0 1 1 1 1 15 Junior Electrical engineering 0 1 1 1 1 1 1 1 1 1 <td< td=""><td>3</td><td>Senior</td><td>Architecture</td><td>1</td><td>0</td><td>0</td><td>1</td></td<>	3	Senior	Architecture	1	0	0	1							
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	4	Intermediate	Architecture	0	1	0	1							
7 Senior Civil engineering 0 1 0 1 8 Intermediate Civil engineering 0 1 1 9 Intermediate Civil engineering 0 1 1 9 Intermediate Civil engineering 0 1 1 10 Junior Civil engineering 0 0 0 11 Senior Mechanical engineering 0 1 1 12 Senior Mechanical engineering 0 1 1 13 Intermediate Mechanical engineering 0 1 1 14 Junior Mechanical engineering 0 1 1 15 Junior Mechanical engineering 0 1 1 16 Senior Electrical engineering 0 1 1 1 19 Intermediate Electrical engineering 1 0 1 1 20 Intermediate Electrical engineering 1 0 1 1 20 <	5	Junior	Architecture	0	0	0	0							
8 Intermediate Civil engineering 0 0 1 1 9 Intermediate Civil engineering 0 1 0 1 10 Junior Civil engineering 0 0 1 0 1 11 Senior Mechanical engineering 0 0 1 1 1 12 Senior Mechanical engineering 0 1 0 1 1 13 Intermediate Mechanical engineering 0 1 0 1 1 14 Junior Mechanical engineering 0 0 1 1 1 15 Junior Mechanical engineering 0 0 1 1 1 16 Senior Electrical engineering 0 0 1 </td <td>6</td> <td>Senior</td> <td>Civil engineering</td> <td>1</td> <td>0</td> <td>0</td> <td>1</td>	6	Senior	Civil engineering	1	0	0	1							
9Intermediate JuniorCivil engineering Civil engineering010110JuniorCivil engineering Civil engineering0000011SeniorMechanical engineering 01011112SeniorMechanical engineering 00111113IntermediateMechanical engineering 00111114JuniorMechanical engineering 00111115JuniorMechanical engineering 00111116SeniorElectrical engineering 00000018SeniorElectrical engineering 010111120IntermediateElectrical engineering 010111120IntermediateElectrical engineering 010111120IntermediateElectrical engineering 0111101120IntermediateElectrical engineering 0111110120IntermediateElectrical engineering 01111011Team k's Subgroup Strength (Ss k) 0.720.570.591.001.00Team k's social cohesion (S k)<	7	Senior	Civil engineering	0	1	0	1							
10JuniorCivil engineering000011SeniorMechanical engineering101112SeniorMechanical engineering001113IntermediateMechanical engineering010114JuniorMechanical engineering010116SeniorElectrical engineering001117SeniorElectrical engineering000018SeniorElectrical engineering010119IntermediateElectrical engineering101120IntermediateElectrical engineering1011Team k's size (m_k)Team k's Subgroup Strength (SS k)O.720.570.59Diversity-related perform. ($P^{S_k} = -2.56\deltaSS_k^2 + 3.2\deltaSS_k + 1-\delta$)1.101.001.00Team k's social cohesion (S k)Cohesion-related performance ($P^{S_k} = 1 + \phi \cdot S_k$)1.101.061.09Team k's Efficiency ($E_k = P^{S_k} \cdot P^{S_k}$)1.101.061.09	8	Intermediate	Civil engineering	0	0	1	1							
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	-	Intermediate		0	1	0	1							
12SeniorMechanical engineering opineering001113IntermediateMechanical engineering opineering0101114JuniorMechanical engineering opineering0101115JuniorMechanical engineering opineering0011116SeniorElectrical engineering opineering0011117SeniorElectrical engineering opineering0000018SeniorElectrical engineering opineering10111119IntermediateElectrical engineering opineering10111120IntermediateElectrical engineering opineering11111120IntermediateElectrical engineering opineering111111ConstraintsTeam k's homogeneity (h_k) Team k's subgroup Strength (SS_k) 0.720.570.591.001.00Diversity-related perform. (P ^{SS} _k =-2.568SS k ² +3.25SS k+1-6)0.580.330.501.111.061.09Team k's social cohesion (S_k) 0.110.580.330.501.111.061.09Team k's Efficiency ($P_s^{S}_k$ =P ^S _k)1.101.061.09	10	Junior	Civil engineering	0	0	0	0							
13IntermediateMechanical engineering010114JuniorMechanical engineering010115JuniorMechanical engineering001116SeniorElectrical engineering001117SeniorElectrical engineering000018SeniorElectrical engineering010119IntermediateElectrical engineering101120IntermediateElectrical engineering111120IntermediateElectrical engineering1111ConstraintsTeam k's subgroup Strength (SS k)On 1001.001.00Team k's social cohesion (S k)On 580.580.330.50Inter k's Efficiency ($E_k = P^{SS}_k \cdot P^S_k$)1.101.061.09		Senior		1	0	0	1							
14 Junior Mechanical engineering 0 1 0 1 15 Junior Mechanical engineering 0 0 1 1 16 Senior Electrical engineering 0 0 1 1 17 Senior Electrical engineering 0 0 0 0 18 Senior Electrical engineering 0 1 0 1 19 Intermediate Electrical engineering 1 0 1 1 20 Intermediate Electrical engineering 1 1 1 1 1 20 Intermediate Electrical engineering 1 0 1 <t< td=""><td>12</td><td>Senior</td><td>Mechanical engineering</td><td>0</td><td>0</td><td>1</td><td>1</td></t<>	12	Senior	Mechanical engineering	0	0	1	1							
15 Junior Mechanical engineering 0 0 1 1 16 Senior Electrical engineering 0 0 1 1 17 Senior Electrical engineering 0 0 0 0 18 Senior Electrical engineering 0 1 0 1 19 Intermediate Electrical engineering 0 1 0 1 20 Intermediate Electrical engineering 1 0 1 1 20 Intermediate Electrical engineering 1 1 1 0 1 20 Intermediate Electrical engineering 1 0 0 1 1 20 Intermediate Electrical engineering 1 1 1 0 1 1 20 Intermediate Electrical engineering 1 1 1 1 0 1 1 1 1 0 1 1 1 0 1 1 1 0 1 1 1	13	Intermediate	Mechanical engineering	0	1	0	1							
16 Senior Electrical engineering 0 1 1 17 Senior Electrical engineering 0 0 0 0 18 Senior Electrical engineering 0 1 0 1 0 1 19 Intermediate Electrical engineering 0 1 0 1	14	Junior	Mechanical engineering	0	1	0	1							
17 Senior Electrical engineering 0 0 0 0 18 Senior Electrical engineering 0 1 0 1 19 Intermediate Electrical engineering 0 1 0 1 20 Intermediate Electrical engineering 1 0 1 1 20 Intermediate Electrical engineering 1 0 1 1 Staff requirements check (1/0) 1 1 1 1 1 1 Team k's homogeneity (h _k) Team k's Subgroup Strength (SS _k) Diversity-related perform. (P ^{SS} _k =-2.565SS k ² +3.25SS k+1-5) 1.00 1.00 1.00 Team k's social cohesion (S _k) Cohesion-related performance (P ^S _k =1+ ϕ ·S _k) Team k's Efficiency (E _k =P ^{SS} _k ·P ^S _k) Team k's Efficiency (E _k =P ^{SS} _k ·P ^S _k)	15	Junior	Mechanical engineering	0	0	1	1							
18 19 19 20Senior Intermediate Electrical engineering010119 20Intermediate IntermediateElectrical engineering010120Intermediate IntermediateElectrical engineering1011120Intermediate IntermediateElectrical engineering10111120Intermediate IntermediateElectrical engineering10111120Intermediate IntermediateElectrical engineering111111ConstraintsTeam k's homogeneity (h_k)Team k's Subgroup Strength (SS_k)0.720.570.59Diversity-related perform. ($P^{SS}_{k} = -2.56\delta SS_{k}^{2} + 3.2\delta SS_{k} + 1-\delta$)1.001.001.00Team k's social cohesion (S_k)Cohesion-related performance ($P^{S}_{k} = 1 + \phi \cdot S_{k}$)Team k's Efficiency ($E_{k} = P^{SS}_{k} \cdot P^{S}_{k}$)1.101.061.09	16	Senior	Electrical engineering	0	0	1	1							
19 20IntermediateElectrical engineering Electrical engineering010120IntermediateElectrical engineering1001Staff requirements check (1/0) Team k's size (m_k)1111ConstraintsTeam k's homogeneity (h_k) Team k's Subgroup Strength (SS_k)1.792.302.780.59Diversity-related perform. ($P^{SS}_{k}=-2.56\delta SS_{k}^{2}+3.2\delta SS_{k}+1-\delta$)1.001.001.00Team k's social cohesion (S_k) 1.110.580.330.50Cohesion-related performance ($P^{S}_{k}=1+\phi \cdot S_{k}$)1.101.061.09Team k's Efficiency ($E_{k}=P^{SS}_{k} \cdot P^{S}_{k}$)1.101.061.09	17	Senior	Electrical engineering	0	0	0	0							
20 Intermediate Electrical engineering 1 0 0 1 Staff requirements check (1/0) Team k's size (m_k) 1	18	Senior	Electrical engineering	0	1	0	1							
Staff requirements check (1/0) 1 1 Constraints Staff requirements check (1/0) 1 1 1 Constraints Team k's size (m _k) 1 1 Constraints Team k's homogeneity (h _k) 1.79 2.30 2.78 Team k's Subgroup Strength (SS _k) 0.72 0.57 0.59 Diversity-related perform. ($P^{Ss}_{k} = -2.56\delta SS_{k}^{2} + 3.2\delta SS_{k} + 1-\delta$) 1.00 1.00 1.00 Team k's social cohesion (S _k) 0.58 0.33 0.50 Team k's social cohesion (S _k) 0.58 0.33 0.50 Team k's Efficiency ($P^{S}_{k} = 1 + \phi \cdot S_{k}$) 1.10 1.06 1.09 Team k's Efficiency ($E_{k} = P^{Ss}_{k} \cdot P^{S}_{k}$) 1.10 1.00 1.00 Team k's Efficiency ($E_{k} = P^{Ss}_{k} \cdot P^{S}_{k}$) 1.10 1.00 1.00 <td>19</td> <td>Intermediate</td> <td>Electrical engineering</td> <td>0</td> <td>1</td> <td>0</td> <td>1</td>	19	Intermediate	Electrical engineering	0	1	0	1							
Team k's size (m_k) 475Team k's homogeneity (h_k) 1.792.302.78Team k's Subgroup Strength (SS_k) 0.720.570.59Diversity-related perform. $(P^{SS}_k = -2.56\delta SS_k^2 + 3.2\delta SS_k + 1-\delta)$ 1.001.001.00Team k's social cohesion (S_k) 0.580.330.50Ochesion-related performance $(P^{S}_k = 1 + \phi \cdot S_k)$ 1.111.061.09Team k's Efficiency $(E_k = P^{SS}_k \cdot P^S_k)$ 1.101.061.09	20	Intermediate	Electrical engineering	1	0	0	ľ							
Team k's size (m_k) 475Team k's homogeneity (h_k) 1.792.302.78Team k's Subgroup Strength (SS_k) 0.720.570.59Diversity-related perform. $(P^{SS}_k = -2.56\delta SS_k^2 + 3.2\delta SS_k + 1-\delta)$ 1.001.001.00Team k's social cohesion (S_k) 0.580.330.50Ochesion-related performance $(P^{S}_k = 1 + \phi \cdot S_k)$ 1.111.061.09Team k's Efficiency $(E_k = P^{SS}_k \cdot P^S_k)$ 1.101.061.09			r				_							
Team k's homogeneity (h k)1.792.302.78Team k's Subgroup Strength (SS k)0.720.570.590.001.001.001.00Team k's social cohesion (S k)0.580.330.50Team k's social cohesion (S k)Cohesion-related performance (P $^{s}_{k}$ =1+ ϕ ·S k)1.10Team k's Efficiency (E $_{k}$ =P $^{ss}_{k}$ ·P $^{s}_{k}$)1.101.00<		Sta	ff requirements check (1/0)	1	1	1	Constraints							
Team k's Subgroup Strength (SS k) 0.72 0.57 0.59 Diversity-related perform. (P^{SS}_{k} =-2.56 δ SS $_{k}^{2}$ +3.2 δ SS $_{k}$ +1- δ) 1.00 1.00 1.00 Team k's social cohesion (S k) 0.58 0.33 0.50 Cohesion-related performance (P^{S}_{k} =1+ ϕ ·S k) 1.11 1.06 1.09 Team k's Efficiency (E_{k} = P^{SS}_{k} · P^{S}_{k}) 1.10 1.06 1.09			Team k's size (m _k)	4	7	5								
Team k's Subgroup Strength (SS k) 0.72 0.57 0.59 Diversity-related perform. (P^{SS}_{k} =-2.56 δ SS $_{k}^{2}$ +3.2 δ SS $_{k}$ +1- δ) 1.00 1.00 1.00 Team k's social cohesion (S k) 0.58 0.33 0.50 Cohesion-related performance (P^{S}_{k} =1+ ϕ ·S k) 1.11 1.06 1.09 Team k's Efficiency (E_{k} = P^{SS}_{k} · P^{S}_{k}) 1.10 1.06 1.09														
Diversity-related perform. $(P^{SS}_{k} = -2.56\delta SS_{k}^{2} + 3.2\delta SS_{k} + 1 - \delta)$ 1.00 1.00 1.00 Team k's social cohesion (S_{k}) O.58 0.33 0.50 Cohesion-related performance $(P^{S}_{k} = 1 + \phi \cdot S_{k})$ Team k's Efficiency $(E_{k} = P^{SS}_{k} \cdot P^{S}_{k})$ 1.10 1.00 1.00 1.00 1.00 1.00 I.00		1	Team k's homogeneity (h _k)	1.79	2.30	2.78								
Team k's social cohesion (S_k) 0.58 0.33 0.50 Cohesion-related performance ($P_k^s = 1 + \phi \cdot S_k$) 1.11 1.06 1.09 Team k's Efficiency ($E_k = P_k^{ss} \cdot P_k^{s}$) 1.10 1.06 1.09		Team k's	s Subgroup Strength (SS _k)	0.72	0.57	0.59								
Team k's social cohesion (S_k) 0.58 0.33 0.50 Cohesion-related performance ($P_k^s = 1 + \phi \cdot S_k$) 1.11 1.06 1.09 Team k's Efficiency ($E_k = P_k^{ss} \cdot P_k^{s}$) 1.10 1.06 1.09	Diversity-rela	ted perform. (P ^{SS} k=	2.56δSS μ ² +3.2δSS μ+1-δ)	1.00	1.00	1.00								
Cohesion-related performance $(P^s_k = 1 + \phi \cdot S_k)$ 1.111.061.09Team k's Efficiency $(E_k = P^{ss}_k \cdot P^s_k)$ 1.101.061.09							_J							
Cohesion-related performance $(P^s_k = 1 + \phi \cdot S_k)$ 1.111.061.09Team k's Efficiency $(E_k = P^{ss}_k \cdot P^s_k)$ 1.101.061.09		Tea	m k's social cohesion (S $_{k}$)	0.58	0.33	0.50								
Team k's Efficiency ($E_k = P^{ss}_k \cdot P^s_k$) 1.10 1.06 1.09				1.11	1.06	1.09								
					1.00									
		Toom k's	Efficiency (E. = P ^{SS} , . P ^S ,)	1 10	1.06	1 09	7							
$\mathbf{F}(0) = \mathbf{C}(\mathbf{k} \mathbf{w}_k) = 0.50 \qquad 0.50 \qquad 0.20$		i cani K S												
			rroject k weight (W _k)	0.50	0.30	0.20	_							

Staff i allocations to each project p k

Global allocation Efficiency (E=SE_k·w_k) (maximise) = **1.087** [1- δ - ϕ , 1+ ϕ] = [0.72, 1.18]

Fig. 6. Best feasible solution (found) of the case study

	Group homogeneity-related information	r-related in	nformation			Soci	Sociometric preference towards individual j (s $_{ij}$)	ric p	refe	renc	e to	waro	ls in	divic	lual.	i (s ij	Ċ	Project gr	Project group marks*	*
Stud. (i)	Background (d _i)	Age (a i)	Gender (g i)	Age (a i) Gender (g i) Ethnicity (e i) Work exp. (t i)	(ork exp. (t _i)	1	2 3	4	5	9	7 8	89		10 11	12 1	13 14	4 15	5 Project 1	Project 2	Project 3
-	Construction	24	Male	South Amer.	2		1	~	-	0	1	-	0	<u> </u>	0	0	0	09	80	75
2	Construction	24	Female	South Amer.	2	-	0	~	-	0	0	0	0	$\overline{\mathbf{v}}$	0	0	-	50	75	75
ო	Hydraulics	25	Male	South Amer.	ი	0	0	~	τ.	0	0	0	0	$\overline{\mathbf{v}}$	0	0	1	60	85	80
4	Hydraulics	25	Male	South Amer.	2	~	-		-	0	-	0	0	0	0	0		60	85	75
5	Construction	24	Female	South Amer.	2	• ~	 <!--</td--><td>~</td><td></td><td>0</td><td>1</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>0</td><td>50</td><td>80</td><td>80</td>	~		0	1	0	0	0	0	0	0	50	80	80
9	Construction	24	Male	South Amer.	2	-	0	~	-		1	0	0	~	0) 0	0 0	60	75	75
7	Hydraulics	25	Female	European	2	0	0	0	0	0	-	_	~	0	0	-	0	09	80	75
8	Construction	24	Female	South Amer.	2	~	0	~	0	~	~	~	~	0		0	1	50	75	75
6	Transport	24	Male	South Amer.	7	0	0	0	0	0	~	_	~	-	0	-	0	09	85	80
10	Hydraulics	24	Male	South Amer.	2	0	0	0	0	0	- -	_		-	0	-	1	60	85	75
11	Transport	30	Male	South Amer.	5	0	0 0	0	0	~	0	-	~		$\frac{1}{1}$	` O	1	50	80	80
12	Hydraulics	24	Female	European	2	0	0	0	0	~		0	0	\sum_{i}		0	0	09	75	75
13	Construction	24	Male	Asian	2	0	0	0	0	0	-	-	~	0	0		_	60	80	75
14	Transport	57	Male	South Amer.	30	0	0	0	0	0	0	0	0	-	0	0	0	20	75	75
15	Hydraulics	24	Male	South Amer.	2	0	-	~	0	0	0	0	~	-	~	-	0	60	85	80
* Note: á	* Note: all students were allocated to groups of five students to de	to groups of	f five students to	develop three projects. On completing each project, student groups were reshuffled so that groups composition changed for the next assignment	ts. On completing	t each	projec	зt, stu	dent g	roup.	s wer	e resi	huffle	d so t	hat gi	sdno.	com	osition change	ed for the nexi	assignment.

Fig. 7. Group demographics and marks awarded in the MSc Civil Engineering 'Projects'

integration module

		Project	t 1		Project	t 2		Project	t 3	
	Student (i) \downarrow & Group (k) \rightarrow	Α	В	С	Α	В	С	Α	В	С
	1	1	0	0	0	0	1	0	1	0
	2	0	1	0	1	0	0	0	0	1
	3	0	0	1	0	1	0	1	0	0
	4	1	0	0	0	1	0	0	0	1
	5	0	1	0	0	0	1	1	0	0
	6	0	0	1	1	0	0	0	1	0
	7	1	0	0	0	0	1	0	1	0
	8	0	1	0	1	0	0	0	0	1
	9	0	0	1	0	1	0	1	0	0
	10	1	0	0	0	1	0	0	0	1
	11	0	1	0	0	0	1	1	0	0
	12	0	0	1	1	0	0	0	1	0
	13	1	0	0	0	0	1	0	1	0
	14	0	1	0	1	0	0	0	0	1
	15	0	0	1	0	1	0	1	0	0
	.							_		-
	Group k's size (m _k)	5	5	5	5	5	5	5	5	5
		0.04	0.70	0.04	0.50	4.00	0.50	0.05	0.04	0.05
	Group k's homogeneity (h_k)	3.21	2.78	3.31	2.59	4.38	2.53	3.25	2.94	2.85
	<pre>up k's Subgroup Strength (SS k)</pre>	0.92	1.58	0.84	1.41	0.48	0.94	0.73	1.28	1.22
Diversity-rel. perform. (P	$p^{SS}_{k} = -2.56\delta SS_{k}^{2} + 3.2\delta SS_{k} + 1-\delta$	0.98	0.77	0.99	0.84	0.99	0.97	1.00	0.89	0.91
					1					
	Group k's social cohesion (S_k)	0.50	0.10	0.25	0.25	0.55	0.25	0.35	0.35	0.30
Cohesion-rela	ted performance ($P^{s}_{k}=1+\phi\cdot S_{k}$)	1.09	1.02	1.05	1.05	1.10	1.05	1.06	1.06	1.05
Grou	$p k$'s Efficiency ($E_k = P^{ss}_k \cdot P^s_k$)	1.07	0.79	1.04	0.88	1.09	1.02	1.06	0.94	0.96
Project	marks (by groups) (from Fig. 7)	60	50	60	75	85	80	80	75	75

Fig. 8. Group diversity-related performances, Cohesion-related performances and Group

Efficiencies calculations.

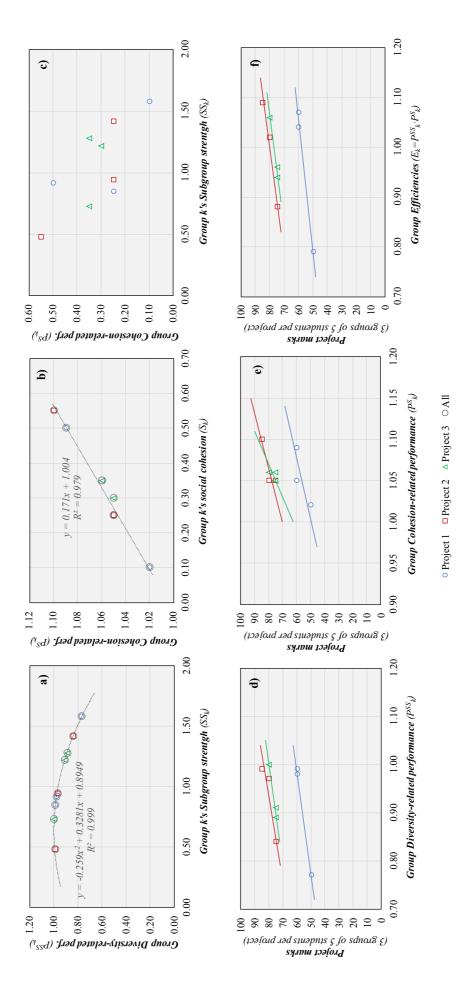


Fig. 9. Different combinations of Group Diversity-related performance, Group Cohesionrelated performance and Group Efficiencies with Project group marks regression plots.

Supplemental Online Material

This addendum presents the tables with the detailed calculations of the case study members' overlaps concerning functional department, age, gender, ethnicity and team tenure (in the same order).

The complete case study along with all calculations can be downloaded in an excel file here: <u>http://bit.ly/2BXCaQj</u> . Additionally, the validation case study can be downloaded here: <u>http://bit.ly/2yOa9KH</u>

					1 0101		U jj													
Indiv. ↓i & j→	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1		1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	1		1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
3	1	1		1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
4	1	1	1		1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
5	1	1	1	1		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
6	0	0	0	0	0		1	1	1	1	0	0	0	0	0	0	0	0	0	0
7	0	0	0	0	0	1		1	1	1	0	0	0	0	0	0	0	0	0	0
8	0	0	0	0	0	1	1		1	1	0	0	0	0	0	0	0	0	0	0
9	0	0	0	0	0	1	1	1		1	0	0	0	0	0	0	0	0	0	0
10	0	0	0	0	0	1	1	1	1		0	0	0	0	0	0	0	0	0	0
11	0	0	0	0	0	0	0	0	0	0		1	1	1	1	0	0	0	0	0
12	0	0	0	0	0	0	0	0	0	0	1		1	1	1	0	0	0	0	0
13	0	0	0	0	0	0	0	0	0	0	1	1		1	1	0	0	0	0	0
14	0	0	0	0	0	0	0	0	0	0	1	1	1		1	0	0	0	0	0
15	0	0	0	0	0	0	0	0	0	0	1	1	1	1		0	0	0	0	0
16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		1	1	1	1
17	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1		1	1	1
18	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1		1	1
19	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1		1
20	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	

Functional department overlaps (O^d_{ii})

	Age o	overla	ps (O	a _{ij})																
Indiv. ↓i & j→	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1		0.76	0.52	0.40	0.17	0.88	0.64	0.64	0.40	0.29	0.89	1.00	0.40	0.40	0.17	0.76	0.64	0.52	0.40	0.29
2	0.76		0.69	0.53	0.22	0.86	0.84	0.84	0.53	0.38	0.68	0.76	0.53	0.53	0.22	1.00	0.84	0.69	0.53	0.38
3	0.52	0.69		0.77	0.32	0.59	0.81	0.81	0.77	0.55	0.47	0.52	0.77	0.77	0.32	0.69	0.81	1.00	0.77	0.55
4	0.40	0.53	0.77		0.41	0.46	0.63	0.63	1.00	0.71	0.36	0.40	1.00	1.00	0.41	0.53	0.63	0.77	1.00	0.71
5	0.17	0.22	0.32	0.41		0.19	0.26	0.26	0.41	0.58	0.15	0.17	0.41	0.41	1.00	0.22	0.26	0.32	0.41	0.58
6	0.88	0.86	0.59	0.46	0.19		0.73	0.73	0.46	0.32	0.79	0.88	0.46	0.46	0.19	0.86	0.73	0.59	0.46	0.32
7	0.64	0.84	0.81	0.63	0.26	0.73		1.00	0.63	0.44	0.57	0.64	0.63	0.63	0.26	0.84	1.00	0.81	0.63	0.44
8	0.64	0.84	0.81	0.63	0.26	0.73	1.00		0.63	0.44	0.57	0.64	0.63	0.63	0.26	0.84	1.00	0.81	0.63	0.44
9	0.40	0.53	0.77	1.00	0.41	0.46	0.63	0.63		0.71	0.36	0.40	1.00	1.00	0.41	0.53	0.63	0.77	1.00	0.71
10	0.29	0.38	0.55	0.71	0.58	0.32	0.44	0.44	0.71		0.26	0.29	0.71	0.71	0.58	0.38	0.44	0.55	0.71	1.00
11	0.89	0.68	0.47	0.36	0.15	0.79	0.57	0.57	0.36	0.26		0.89	0.36	0.36	0.15	0.68	0.57	0.47	0.36	0.26
12	1.00	0.76	0.52	0.40	0.17	0.88	0.64	0.64	0.40	0.29	0.89		0.40	0.40	0.17	0.76	0.64	0.52	0.40	0.29
13	0.40	0.53	0.77	1.00	0.41	0.46	0.63	0.63	1.00	0.71	0.36	0.40		1.00	0.41	0.53	0.63	0.77	1.00	0.71
14	0.40	0.53	0.77	1.00	0.41	0.46	0.63	0.63	1.00	0.71	0.36	0.40	1.00		0.41	0.53	0.63	0.77	1.00	0.71
15	0.17	0.22	0.32	0.41	1.00	0.19	0.26	0.26	0.41	0.58	0.15	0.17	0.41	0.41		0.22	0.26	0.32	0.41	0.58
16	0.76	1.00	0.69	0.53	0.22	0.86	0.84	0.84	0.53	0.38	0.68	0.76	0.53	0.53	0.22		0.84	0.69	0.53	0.38
17	0.64	0.84	0.81	0.63	0.26	0.73	1.00	1.00	0.63	0.44	0.57	0.64	0.63	0.63	0.26	0.84		0.81	0.63	0.44
18	0.52	0.69	1.00	0.77	0.32	0.59	0.81	0.81	0.77	0.55	0.47	0.52	0.77	0.77	0.32	0.69	0.81		0.77	0.55
19	0.40	0.53	0.77	1.00	0.41	0.46	0.63	0.63	1.00	0.71	0.36	0.40	1.00	1.00	0.41	0.53	0.63	0.77		0.71
20	0.29	0.38	0.55	0.71	0.58	0.32	0.44	0.44	0.71	1.00	0.26	0.29	0.71	0.71	0.58	0.38	0.44	0.55	0.71	

Fig. S1. Overlap calculations (part 1)

	Gend	der ov	erlaps	с (О ^д _{іј.})															
Indiv. ↓i & j→	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1 2	0	0	1	1 0	0 1	1 0	1 0	1 0	1 0	0 1	1	1 0	1 0	0 1	1 0	1 0	1 0	1 0	1 0	0 1
3	1	0		1	0	1	1	1	1	0	1	1	1	0	1	1	1	1	1	0
4	1	0	1		0	1	1	1	1	0	1	1	1	0	1	1	1	1	1	0
5	0	1	0	0		0	0	0	0	1	0	0	0	1	0	0	0	0	0	1
6 7	1 1	0 0	1	1 1	0 0	4	1	1 1	1 1	0 0	1	1 1	1 1	0 0	1 1	1	1	1 1	1	0 0
8	1	0	1	1	0	1	1			0	1	1	1	0	1	1	1	1	1	0
9	1	0	1	1	0	1	1	1		0	1	1	1	0	1	1	1	1	1	0
10	0	1	0	0	1	0	0	0	0		0	0	0	1	0	0	0	0	0	1
11	1	0	1	1	0	1	1	1	1	0 0	4	1	1	0	1	1	1	1	1	0
12 13	1	0 0	1 1	1	0 0	1	1 1	1 1	1	0	1	1	1	0	1	1	1	1	1	0 0
14	0	1	0	0	1	0	0	0	0	1	0	0	0		0	0	0	0	0	1
15	1	0	1	1	0	1	1	1	1	0	1	1	1	0		1	1	1	1	0
16	1	0	1	1	0	1	1	1	1	0	1	1	1	0	1		1	1	1	0
17 18	1	0 0	1 1	1	0 0	1 1	1	1 1	1 1	0 0	1 1	1 1	1 1	0 0	1	1	1	1	1	0 0
18	1	0	1	1	0	1	1	1	1	0	1	1	1	0	1	1	1	1		0
20	0	1	0	0	1	0	0	0	0	1	0	0	0	1	0	0	0	0	0	
-	Ethn	icity o	overla	os (0°	'ij)															
Indiv. $\downarrow i \& j \rightarrow$	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1 2	1	1	0	0 0	0 0	0 0	0 0	1 1	1 1	0 0	1 1	1 1	0 0	0 0	1 1	1	0 0	0 0	0 0	0 0
3	0	0		1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	1
4	0	0	1		0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	1
5	0	0	0	0		1	0	0	0	0	0	0	0	0	0	0	0		0	0
6 7	0 0	0	0 0	0 0	1 0	0	0	0 0	0 0	0 0	0	0 0	0 0	0 1	0 0	0	0 1	1 0	0 0	0 0
8	1	1	0	0	0	0	0	0		0	1	1	0	0	1	1	0	0	0	0
9	1	1	0	0	0	0	0	1		0	1	1	0	0	1	1	0	0	0	0
10	0	0	0	0	0	0	0	0	0		0	0	0	0	0	0	0	0	0	0
11 12	1	1	0 0	0	0	0	0	1	1	0	4	1	0	0	1	1	0	0	0	0
12	1 0	1 0	1	0 1	0 0	0	0 0	1 0	1 0	0 0	1 0	0	0	0	1 0	1 0	0 0	0 0	0 0	0 1
14	0	0	0	0	0	0	1	0	0	0	0	0	0		0	0	1	0	0	0
15	1	1	0	0	0	0	0	1	1	0	1	1	0	0		1	0	0	0	0
16 17	1	1 0	0	0	0	0	0 1	1	1	0 0	1	1 0	0	0 1	1	0	0	0	0	0
17	0 0	0	0 0	0 0	0 1	0 1	0	0 0	0 0	0	0	0	0 0	0	0 0	0	0	U	0	0 0
19	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		0
20	0	0	1	1	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	
		n tenu		-																
<u>Indiv. ↓i & j →</u> 1	1	2	3	4	5 0.20	6	7	8	9 0.08	<u>10</u>	11	<u>12</u> 0.71	13	14 0.20	<u>15</u> 0.20	16	17	18	19	20
2	0.80						0.75													
3							0.67													
4	t	0.25					0.33													
5 6		0.25					0.33						0.33							
7		0.75											1.00							
8	0.60	0.75	0.67	0.33	0.33	0.67	1.00		0.13	0.07	0.38	0.43	1.00	0.33	0.33	0.75	1.00	0.67	0.67	0.67
9	£					ç .	0.13									£				
10 11							0.07						0.07							
12							0.38													
13	0.60	0.75	0.67	0.33	0.33	0.67	1.00	1.00	0.13	0.07	0.38	0.43		0.33	0.33	0.75	1.00	0.67	0.67	0.67
14							0.33													
15							0.33													
16 17							0.75 1.00												0.50 0.67	
18							0.67													1.00
19	0.40	0.50	1.00	0.50	0.50	1.00	0.67	0.67	0.20	0.10	0.25	0.29	0.67	0.50	0.50	0.50	0.67	1.00		1.00
20	0.40	0.50	1.00	0.50	0.50	1.00	0.67	0.67	0.20	0.10	0.25	0.29	0.67	0.50	0.50	0.50	0.67	1.00	1.00	

Fig. S1. Overlap calculations (part 2)