



20 **Abstract**

21 The concepts of “initial rate of photon absorption” (IRPA), “dimensionless boundary layer of photon  
22 absorption” and “apparent optical thickness ( $\tau_{app}$ )” are presented to evaluate the radiative transfer  
23 phenomena in solar, slurry, planar, photocatalytic reactors. The radiation field produced by  
24 suspensions of TiO<sub>2</sub> and goethite, two photocatalysts with profoundly different optical properties used  
25 in heterogenous photocatalysis and heterogeneous photo-assisted Fenton reactions, was determined  
26 by the six-flux radiation absorption-scattering model coupled to the Henyey-Greenstein scattering  
27 phase function (SFM-HG). The concept of IRPA, defined by the differentiation at the local volumetric  
28 rate of photon absorption (LVRPA) at the reactor window boundary, is proposed as a new approach  
29 to determine the impact of catalyst loading and optical properties on the extinction of light inside a  
30 photoreactor. The IRPA showed that the extinction of light follows a second order dependency on the  
31 photocatalyst concentration while the impact of the optical properties can be expressed by a decoupled  
32 function ( $\Psi$  function). The  $\Psi$  function increased with photocatalyst concentration and approached a  
33 maximum at the same optimal photocatalyst concentration determined from the analysis of the total  
34 rate of photon absorption (TRPA) in the reactor. The analysis of TRPA and boundary layer of photon  
35 absorption redefined here in dimensionless form, as a function of  $\tau_{app}$ , determined that the most  
36 efficient rate of radiation absorption in solar powered planar reactors occurs at  $\tau_{app}=4.1-4.4$ , with  
37 approximately 10% of the reactor width under darkness.  $\tau_{app}$  is a similarity dimensionless parameter  
38 exclusively derived from the SFM approach, which clusters the effects of photocatalyst loading,  
39 reactor dimension and photocatalyst optical properties, providing an ideal parameter for designing  
40 and scaling photocatalytic reactors operated with any kind of photocatalytic material.

41 **Keywords:** Radiative transfer; Radiation transport; Photoreactor design; Photoreactor model,  
42 Optimization.

43

<b>Nomenclature</b>			
$a$	SFM parameter, dimensionless	$\kappa^*$	absorption coefficient, $\text{m}^2 \text{kg}^{-1}$
$b$	SFM parameter, dimensionless	$\lambda$	wavelength, nm
$C_{cat}$	photocatalysts concentration, $\text{kg m}^{-3}$	$\sigma^*$	scattering coefficient, $\text{m}^2 \text{kg}^{-1}$
$g$	scattering parameter from the Henyey-Greenstein phase function, dimensionless	$\tau$	optical thickness, dimensionless
$IRPA$	initial rate of photon absorption, $\text{W m}^{-4}$	$\tau_{app}$	apparent optical thickness from SFM, dimensionless
$I_0$	incident radiative flux, $\text{W/m}^2$	$\psi$	psi function
$I_\lambda$	spectral irradiance, $\text{W m}^{-2} \text{nm}^{-1}$	$\omega$	scattering albedo, dimensionless
$L$	thickness of the photocatalyst-water film, m	$\omega_{corr}$	corrected scattering albedo from SFM, dimensionless
LVRPA or $e^a$	local volumetric rate of photon absorption, $\text{W m}^{-3}$	<i>Subscripts</i>	
$p_b$	SFM probability of scattering in the backward direction, dimensionless	max	maximum
$p_f$	SFM probability of scattering in the forward direction, dimensionless	min	minimum
$p_s$	SFM probability of scattering in the sideward direction, dimensionless	UVA	UVA region of the solar spectrum
$TRPA/A$	total rate of photon absorption per unit of transversal surface of the photoreactor, $\text{W m}^{-2}$	Vis	visible region of solar spectrum
$x$	$x$ coordinate, m	max	maximum
<i>Greek letters</i>			
$\beta^*$	extinction coefficient, $\text{m}^2 \text{kg}^{-1}$		
$\delta$	boundary layer of photon absorption		
$\gamma$	SFM parameter, dimensionless		

44

## 45 1. Introduction

46 Platform technologies such as heterogeneous photocatalysis and the photo-assisted heterogeneous  
 47 Fenton process have shown great potential for the treatment of contaminated water or air [1,2]. The  
 48 main attraction of these processes is the utilization of solar light as the driving force for the production  
 49 of highly oxidative radical species, which are then able to complete the conversion of water or air  
 50 contaminants to innocuous products.

51

52 One very active field of research in heterogeneous photocatalysis is the development and evaluation  
 53 of new photocatalytic materials. Doping of commercial titanium dioxide ( $\text{TiO}_2$ ) is a common

54 approach to extend the absorption spectrum of TiO<sub>2</sub> from the UV into the visible region of the solar  
55 spectrum [3]. Furthermore, iron oxides, have shown interesting properties as visible light active  
56 photocatalyst, as well as, catalysts for photo-assisted heterogeneous Fenton reactions when combined  
57 with hydrogen peroxide [4–6].

58

59 The intense development in new photocatalysts calls for the development of comprehensive  
60 methodologies for the analysis of the radiative transfer behavior of these new materials, particularly  
61 in the solar radiation spectrum. These methodologies are necessary for an appraisal of the catalytic  
62 performance of new photocatalytic materials and for the design and optimization of solar  
63 photoreactors. For this purpose, the optical properties of existing or new photocatalysts (the  
64 extinction, absorption and scattering coefficients and the scattering phase function) must be  
65 determined or estimated.

66

67 Recently several authors have investigated the influence of the optical properties on the photocatalyst  
68 performance [7–9], however, the literature has scarce information on the application of these for  
69 reactor design. Besides, available information deals almost exclusively with TiO<sub>2</sub> P25 photocatalyst.  
70 Furthermore, optimized photoreactor designs have been proposed in conjunction with TiO<sub>2</sub>  
71 photocatalytic powders, however, it remain unclear if these designs are also optimal when the reactor  
72 is loaded with other photocatalysts, particularly those materials having highly different optical  
73 properties than TiO<sub>2</sub>. Process intensification, for instance, is a novel and very interesting approach  
74 for optimizing photocatalytical processes [10,11]. One aspect that the intensification process should  
75 consider firstly is the optical performance of the photocatalytical material (i.e. its optical properties)  
76 for an integral design or correct selection of the photoreactor. In general, the optimization of the  
77 reactor performance requires a detailed analysis between the operational parameters such as, optimal  
78 photocatalyst loading, which in turn depend on the optical properties of the synthesized material and  
79 the rate of absorption of radiation.

80 In this study, an alternative reaction engineering approach including the impact of the photocatalyst  
81 optical properties on the optimization of photoreactors is presented i.e. in the determination of an  
82 optimal catalyst loading or photoreactor size. The concepts of “initial rate of photon absorption”  
83 (IRPA) and “boundary layer of photon absorption” [12] redefined in dimensionless form are here  
84 proposed as new parameters for evaluating the impact of photocatalyst loading on the total rate of  
85 photon radiation absorption (TRPA) and to facilitate the optimal design of photoreactors at different  
86 scales, from laboratory scale to full scale. The consequence of these are far reaching since the  
87 evaluation of the wide range of photocatalysts reported in literature may have to be reconsidered, if  
88 the photocatalysts activity was determined at equal loadings in the reactor without accounting the  
89 impact of the photocatalysts optical properties.

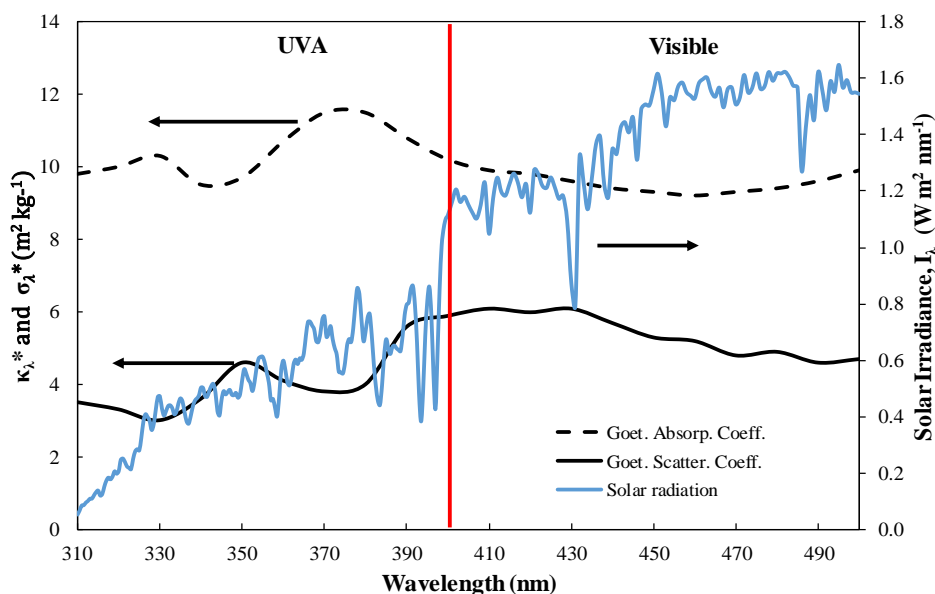
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91 Goethite ( $\alpha$ -FeOOH), an iron oxide used as visible-active photocatalysts [13] as well as for photo-  
92 assisted heterogeneous Fenton reactions [14,15], and the extensively explored TiO<sub>2</sub> P25 were selected  
93 to illustrate the impact of the above methodology on materials with significantly different optical  
94 properties. The use of goethite as one of the model photocatalysts also offers an illustration of the  
95 evaluation of the radiative transfer phenomena of a photocatalyst active in the visible range of the  
96 solar spectrum, which may be of special interest to the literature. The optical performance of  
97 these photocatalysts was evaluated in a simple planar photoreactor geometry, allowing the results and  
98 concepts of this study to be easily transferred to other photoreactor geometries. Such geometry is  
99 characteristic of falling liquid films [16] and conventional flat-plate photoreactors, with the slurry  
100 photocatalyst suspension confined between two walls [17,18]. The six-flux absorption scattering  
101 model (SFM) was used to model the solar radiation transport through slurry suspensions of the  
102 photocatalysts.

103 **2. Mathematical methods**

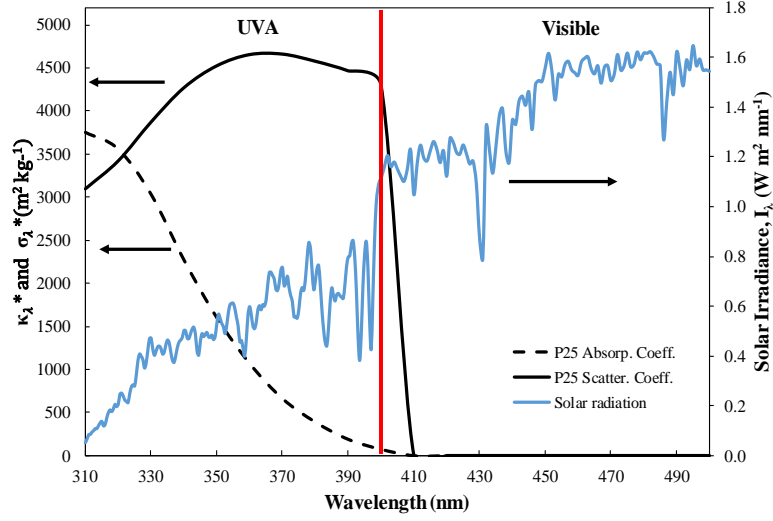
104 **2.1. Optical properties of photocatalysts and solar spectral irradiation**

105 The spectral absorption and scattering coefficients of the photocatalysts TiO<sub>2</sub> (P25, Evonik) and  
106 goethite ( $\alpha$ -FeOOH, Aldrich) in aqueous suspensions [19,20] are shown in **Fig. 1** and **Fig. 2**,  
107 including the solar radiation data of global irradiance (AM 1.5), incident on a plane tilted 37° facing  
108 the sun [21]. The wavelengths range of 310-500 nm was selected since 300 nm is the lower  
109 wavelength in which both the goethite and TiO<sub>2</sub> interact with light and 500 nm is the upper limit for  
110 goethite, beyond this value Ortiz de la Plata et al. [20] found that the absorption of radiation by  
111 goethite was too small to be taken into account. Similarly, the graphical representation of the Henyey-  
112 Greenstein scattering factor is presented in **Fig. S1** (Supporting Information (SI)).



113

114 **Fig. 1** Optical properties of goethite (Aldrich) and solar irradiance for a surface tilted 37° to the  
115 sun. The red line separates the UVA and visible regions of the solar spectrum. Absorption and  
116 scattering coefficients from [20].



117

118 **Fig. 2** Optical properties of TiO<sub>2</sub> P25 (Evonik) and solar irradiance for a surface tilted 37° to the  
 119 sun. The red line separates the UVA and visible regions of the solar spectrum. Absorption and  
 120 scattering coefficients from [19].

121 **2.2. The Six Flux Model for radiation field calculations**

122 The spatial distribution of the local volumetric rate of photon absorption (LVRPA) inside the planar  
 123 reactor was evaluated by the SFM as shown in Eq. (1) [22]:

124 
$$e^a(x) = \frac{I_0 \tau_{app}}{\omega_{corr} (1-\gamma)L} \left[ \left( \omega_{corr} - 1 + \sqrt{1 - \omega_{corr}^2} \right) e^{-x\tau_{app}/L} + \gamma \left( \omega_{corr} - 1 - \sqrt{1 - \omega_{corr}^2} \right) e^{x\tau_{app}/L} \right] \quad (1)$$

125 where  $a$ ,  $b$ ,  $\omega_{corr}$  and  $\gamma$  are SFM parameters defined as follows:

126 
$$a = 1 - \omega p_f - \frac{4\omega^2 p_s^2}{1 - \omega p_f - \omega p_b - 2\omega p_s} \quad (2)$$

127 
$$b = \omega p_b + \frac{4\omega^2 p_s^2}{1 - \omega p_f - \omega p_b - 2\omega p_s} \quad (3)$$

128 
$$\omega_{corr} = \frac{b}{a} \quad (4)$$

129 
$$\gamma = \frac{1 - \sqrt{1 - \omega_{corr}^2}}{1 + \sqrt{1 - \omega_{corr}^2}} e^{-2\tau_{app}} \quad (5)$$

130 the apparent optical thickness  $\tau_{app}$  is:

131 
$$\tau_{app} = a\tau\sqrt{1 - \omega_{corr}^2} \quad (6)$$

132 For a planar geometry, the optical thickness  $\tau$  is defined by:

133 
$$\tau = (\sigma^* + \kappa^*)C_{cat}L \quad (7)$$

134 where  $\sigma^*$  and  $\kappa^*$  are the spectral averaged specific scattering and absorption coefficients,  $C_{cat}$  is the  
 135 photocatalyst loading and  $L$  is the characteristic length for the extinction of the light inside the reactor.

136 In this study, the planar reactor is positioned orthogonally to the sun and is irradiated by collimated  
 137 rays, i.e.  $L$  equals the thickness of the depth of the water in the planar reactor (Fig. S2). For such  
 138 irradiation conditions in planar geometry, SFM has demonstrated its best performance [23].

139 The scattering probabilities  $p_f$ ,  $p_b$  and  $p_s$  were determined from the Henyey-Greenstein phase function  
 140 for each photocatalyst, following the procedure described elsewhere [24].

### 141 **2.3. Radiation field modeling approach**

142 The SFM applied to polychromatic radiation sources conveniently uses the spectral averaged optical  
 143 properties of the photocatalyst.  $\text{TiO}_2$  only interacts with light (by absorption or scattering)  
 144 significantly in the UVA region of the solar spectrum (**Fig. 2**), while goethite absorbs and scatters  
 145 light in both the UVA and in a portion of the visible region of the solar spectrum (**Fig. 1**). Therefore,  
 146 the net radiation absorbed by the goethite photocatalyst was calculated summing the contributions  
 147 from the UVA and the visible regions of the solar spectrum, as shown in [25], also to allow a direct  
 148 comparison of the two photocatalyst over the UVA region.



149 The LVRPA of a TiO<sub>2</sub> suspension was therefore, calculated from the contribution from the UVA  
 150 region,

$$151 \quad e^a_{TiO_2}(x) = e^a_{UVA}(x) \quad (8)$$

152 while the net LVRPA of a goethite suspension was calculated summing the two contributions from  
 153 the UVA and visible regions, as follows:

$$154 \quad e^a_{\alpha-FeOOH}(x) = e^a_{UVA}(x) + e^a_{Vis}(x) \quad (9)$$

155 where  $e^a_{UV}$  and  $e^a_{Vis}$  were determined from Eq. (1) using the specific optical properties of the catalyst  
 156 averaged over the solar spectrum determined from:

$$157 \quad \kappa^* = \frac{\int_{\lambda_{min}}^{\lambda_{max}} \kappa_{\lambda}^* I_{\lambda} d\lambda}{\int_{\lambda_{min}}^{\lambda_{max}} I_{\lambda} d\lambda} \quad (10)$$

$$158 \quad \sigma^* = \frac{\int_{\lambda_{min}}^{\lambda_{max}} \sigma_{\lambda}^* I_{\lambda} d\lambda}{\int_{\lambda_{min}}^{\lambda_{max}} I_{\lambda} d\lambda} \quad (11)$$

$$159 \quad g = \frac{\int_{\lambda_{min}}^{\lambda_{max}} g_{\lambda} I_{\lambda} d\lambda}{\int_{\lambda_{min}}^{\lambda_{max}} I_{\lambda} d\lambda} \quad (12)$$

160 The integration limits in Eqs. (10-12) in the UVA region where,  $\lambda_{min} = 310$  nm and  $\lambda_{max} = 400$  nm and  
 161 in the visible solar spectrum they were,  $\lambda_{min} = 400$  nm and  $\lambda_{max} = 500$  nm. The use of spectral averaged

162 optical properties is a common approach in literature, which allows a considerable reduction in  
 163 computational time without introducing considerable distortions in the results [26].

164 The UVA solar incident radiation flux on the reactor,  $I_0$  in Eq. (1), was set in  $I_{UVA} = 30 \text{ W/m}^2$ . This  
 165 value corresponds to an experimentally average value of the solar UVA power for a perfectly sunny  
 166 day around noon on a surface tilted  $37^\circ$  [27], in agreement with the solar spectral irradiance presented  
 167 in **Fig. 1** and **Fig. 2**. The visible portion of the incident radiation  $I_{Vis}$  was computed ensuring a  
 168 proportional relationship between the solar spectral irradiances in the UVA and the visible regions of  
 169 the solar spectrum [28]. Therefore,  $I_{Vis}$  is given by:

$$170 \quad I_{Vis} = I_{UVA} \frac{\int_{400nm}^{500nm} I_{\lambda} d\lambda}{\int_{310nm}^{400nm} I_{\lambda} d\lambda} \quad (13)$$

#### 171 **2.4. The concept of initial rate of photon absorption (IRPA)**

172 The absorption of radiation by the photocatalyst inside the reactor was assumed to be a stationary  
 173 process [29]. Therefore, in the planar slurry reactor the LVRPA was only a function of the coordinate  
 174 parallel to the incident rays, denominated as the  $x$ -coordinate.

175 The concept of “initial rate of photon absorption” (IRPA) is here proposed as a new significant  
 176 parameter for the analysis of the radiation absorption in photoreactors. The importance of the IRPA  
 177 is that it gives insights on the expected trend of the LVRPA over the entire photoreactor. The IRPA  
 178 is defined in Eq. (14).

$$179 \quad IRPA = - \left[ \frac{d}{dx} (e^a(x)) \right]_{x=0} \quad (14)$$

180 By applying this definition to Eq. (1), the IRPA can be expressed as:

181 
$$IRPA = -\frac{I_0}{\omega_{corr}(1-\gamma)} \left( \frac{\tau_{app}}{L} \right)^2 \left[ \gamma \left( \omega_{corr} - 1 - \sqrt{1 - \omega_{corr}^2} \right) - \left( \omega_{corr} - 1 + \sqrt{1 - \omega_{corr}^2} \right) \right] \quad (15)$$

182 By introducing Eq. (6) and (7) in Eq. (15) and by analogy to chemical reactions, the IRPA can be  
 183 understood as the initial rate of attenuation of the incident photonic energy as results of its  
 184 “interaction” with the suspended particle of the catalyst. Then, Eq. (15) can be rewritten as:

185 
$$IRPA = -I_0 C_{cat}^2 \Psi \quad (16)$$

186 where  $\Psi$  is given by,

187 
$$\Psi = (\beta^*)^2 \frac{a^2(1-\omega_{corr}^2)}{\omega_{corr}(1-\gamma)} \left[ \gamma \left( \omega_{corr} - 1 - \sqrt{1 - \omega_{corr}^2} \right) - \left( \omega_{corr} - 1 + \sqrt{1 - \omega_{corr}^2} \right) \right] \quad (17)$$

188 where  $\beta^* = \sigma^* + \kappa^*$  is the specific extinction coefficient in m<sup>2</sup>/kg. The psi function  $\Psi$  has units in  
 189 m<sup>4</sup>/kg<sup>2</sup>,  $C_{cat}$  in kg/m<sup>3</sup> and  $I_0$  in W/m<sup>2</sup>, therefore the IRPA has units in W/m<sup>4</sup>.

190 The mathematical structure of Eq. (16) resembles that of an exponential rate law, generally used to  
 191 describe the reaction kinetics in conventional chemical reactions. It include three terms: a proportional  
 192 relationship of the IRPA to the incident radiation  $I_0$ , which from its constant nature can be understood  
 193 as “the reaction rate constant”; a second order term given exclusively by the catalyst’s loading  $C_{cat}$   
 194 and a proportional term represented by the psi function, which relates the optical properties of the  
 195 catalyst, implicit in the SFM parameters, to the catalyst loading included in the initial rate of photon  
 196 absorption (IRPA) parameter  $\gamma$  (see Eq. (5)).

197 **2.5. The total rate of photon absorption (TRPA)**

198 The TRPA, which is the overall radiation absorbed within the entire reactor volume [24,30] is a useful  
 199 parameter to determine the efficiency of photoreactors and the optimal photocatalyst concentration

200 to operate the photoreactor. In a planar photoreactor, uniformly irradiated along the  $x$ -coordinate, the  
201 TRPA per unit surface area is:

$$202 \quad TRPA / A = \int_0^L e^a(x) dx \quad (18)$$

## 203 **2.6. Dimensionless boundary layer of photon absorption for sizing photoreactors**

204 The concept of “boundary layer of photon absorption” has recently been introduced as a useful  
205 parameter for designing planar-geometry slurry photoreactors [12]. The boundary layer of photon  
206 absorption, in analogy to thermal, hydrodynamic and mass boundary layers, is defined as “the reactor  
207 thickness measured from the irradiated photoreactor surface, where 99% of total energy is absorbed”  
208 [12]. Mathematically it is defined as:

$$209 \quad \frac{e^a(0) - e^a(\delta_{abs})}{e^a(0) - e^a(L)} = 0.99 \quad (19)$$

210 The thickness of the boundary layer  $\delta_{abs}$  for a given photocatalyst is a function of the catalyst loading  
211 and the reactor width ( $L$ ),

$$212 \quad \delta_{abs} = f(C_{cat}, L) \quad (20)$$

213 where  $\delta_{abs}$  has units of length. This concept has been presented for a planar slurry reactor of 1 cm of  
214 thickness operated with different commercial  $TiO_2$  powders [12]. This approach, however, is not  
215 dependent on reactor thickness and can be easily extended to any reactor size by introducing a  
216 dimensionless form of Eq. (20):

$$217 \quad \delta_{abs}^* = f(\tau) \quad (21)$$

218 with  $\delta_{abs}^* = \delta_{abs}/L$  representing the fraction of the reactor width in which 99% of the total energy is  
219 absorbed. The optical thickness  $\tau$  in Eq. (21) is a dimensionless parameter that clusters the effects of  
220 the catalyst loading and reactor width  $L$  (see Eq. (7)).

221 In order to establish  $\delta_{abs}^*$  the procedure described by Otálvaro-Marín et al. [12] was followed, by  
222 minimizing the objective function Eq. (22) using the Nelder-Mead optimization algorithm:

$$223 \quad F_{obj}(\delta_{abs}) = \left\{ \left[ e^a(0) - e^a(\delta_{abs}) \right] - 0.99 \left[ e^a(0) - e^a(L) \right] \right\}^2 \quad (22)$$

224 The solution of Eq. (22) for a given photocatalyst requires the thickness of the reactor  $L$  and the  
225 catalyst loading  $C_{cat}$ . These two parameters are incorporated in the optical thickness. Any combination  
226 of  $L$  and  $C_{cat}$  that leads to the same value of the optical thickness would produce the same result.  
227 Therefore, the “dark zone” of a photoreactor, i.e. the portion beyond the which 99% of the incident  
228 energy is absorbed, can be easily determined.

### 229 **3. Results and discussions**

#### 230 **3.1. Photocatalysts optical properties and incident solar radiation on the reactor**

231 The visible component of the incident solar radiation on the reactor was determined from Eq. (13),  
232  $I_{vis} = 80.43 \text{ W/m}^2$ , by setting the incident UVA radiation component as  $I_{UVA} = 30 \text{ W/m}^2$ . The numerical  
233 values of the integrals in Eq. (13) are shown in Table 1. The fraction of solar power between 400-500  
234 nm is 2.68 times greater than that for the UVA. Goethite, unlike  $\text{TiO}_2$  P25, is photoactive between  
235 310-500 nm, therefore, it can absorb a significant larger amount of solar energy (18.62% of the  
236 complete solar spectrum).

237 **Table 1.** Integrated solar irradiance power for regions in analysis.

Region of the solar spectrum	Integrated irradiance power over the wavelength interval (W/m <sup>2</sup> )	Fraction of total spectrum irradiance power (%)
UVA (310-400 nm)	50.61	5.06
Portion of visible (400-500 nm)	135.70	13.56
Complete spectrum (280-4000 nm)	1000.4 <sup>a</sup>	100

238 a. reported in reference [21]

239 The optical properties of the photocatalysts calculated from Eq. (10-12) are reported in Table 2,  
 240 together with the corresponding values of the scattering albedo and corrected scattering albedo (Eq.  
 241 (4)). The scattering albedo reported for TiO<sub>2</sub> P25 (0.79) was calculated using the optical properties  
 242 of sonicated TiO<sub>2</sub> slurries reported by [19] ( $\kappa^* = 1144.69 \text{ m}^2/\text{kg}$  and  $\sigma^* = 4397.30 \text{ m}^2/\text{kg}$ ). However,  
 243 since the optical properties are a function of the grade of agglomeration and hydrodynamics [9,31],  
 244 which for sonicated suspensions can be 2-4 times greater [32], the correction procedure proposed by  
 245 Toepfer et al. [33] was adopted. Therefore, the specific scattering and absorption coefficient for TiO<sub>2</sub>  
 246 reported in Table 2 were calculated from  $\sigma^* = \beta^* \omega$  and  $\kappa^* = \beta^* - \sigma^*$ , considering that the specific  
 247 extinction coefficient of TiO<sub>2</sub> P25 measured under the prevailing conditions of mixing for a solar  
 248 reactor was  $\beta^* = 1470.5 \text{ m}^2/\text{kg}$  [34]. It is worth to note that the specific extinction coefficient is  
 249 independent of the scattering phase function adopted.

250 The optical properties of goethite were measured under mixing conditions for a recirculating flow  
 251 slurry suspension [20].

252 The specific scattering and absorption coefficients of TiO<sub>2</sub> P25 under UVA irradiation (Table 2) were  
 253 289 and 29 times, respectively, greater than those for goethite, although the scattering albedo of TiO<sub>2</sub>

254 (i.e., the probability of scattering photons) was significantly higher than the value for goethite. The  
 255 corrected scattering albedo  $\omega_{corr}$ , on the other hand, is a correction made to the conventional scattering  
 256 albedo, and accounts for the scattering phase function. A predominantly backward scattering  
 257 decreases the probability of absorbing photons while a predominantly forward scattering increases it,  
 258 since photons will penetrate deeper in the reactor width [24].

259 Goethite has very similar optical coefficients in both visible and UVA regions and very low  $\omega_{corr}$  as  
 260 results of its low conventional albedo and a  $g$  scattering factor near to 1, indicating a highly  
 261 predominant forward scattering behavior. Such a low value of  $\omega_{corr}$  could indicate an efficient  
 262 exploitation of the incident photons. In addition, in comparison to others visible-active photocatalysts  
 263 reported in literature (Table S1 (SI)) goethite has a comparable absorption coefficient and the lowest  
 264 scattering albedo in the visible region of the solar spectrum, which means that goethite has superior  
 265 capacity for absorbing a high proportion of visible radiation from the solar spectrum.

266 **Table 2.** Optical properties of catalyst.

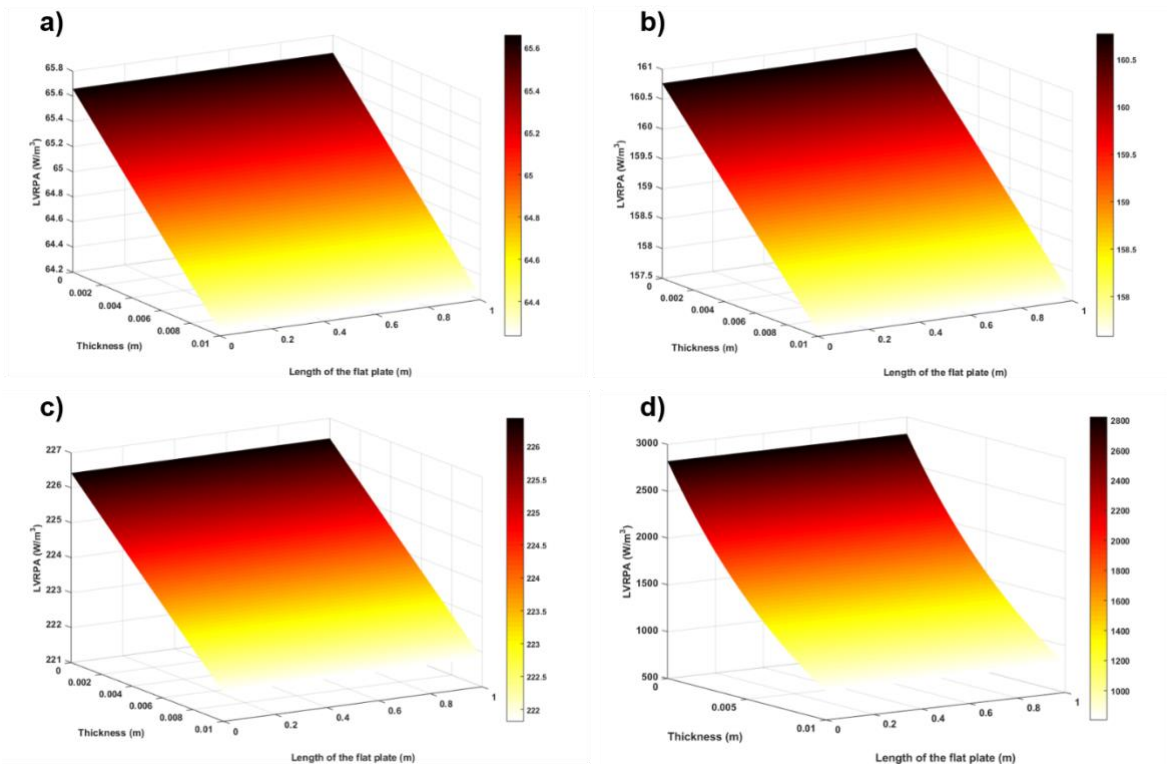
Photocatalyst	$\kappa^*$ (m <sup>2</sup> /kg)	$\sigma^*$ (m <sup>2</sup> /kg)	$\beta^*$ (m <sup>2</sup> /kg)	$g$	$\omega$	$\omega_{corr}$
TiO <sub>2</sub> P25 <sup>a</sup>	308.8	1161.7	1470.5	0.53	0.79	0.2812
Goethite (UVA region)	10.59	4.32	14.91	0.89	0.29	0.0003
Goethite (Visible region)	9.52	5.28	14.80	0.87	0.36	0.0006

267 a. Only is considered the UVA region.

### 268 3.2. LVRPA profiles

269 The LVRPA transversal profiles in a planar reactor of thickness  $L = 1$  cm uniformly irradiated on the  
 270 front surface are shown in **Fig. 3**, for both goethite (Fig. 3a-c) and TiO<sub>2</sub> P25 (Fig. 3d). **Fig. 3a-c**  
 271 show the LVRPA distribution of goethite considering the UVA (Fig. 3a), the visible portion (Fig. 3b)  
 272 and the full solar spectrum (Fig. 3c), respectively. The visible component of the LVRPA gives the

273 greater contribution to the net LVRPA since the incident radiation  $I_{Vis}$  is higher than  $I_{UVA}$  and the  
 274 optical properties of goethite have similar order in both UVA and visible regions. On the other hand,  
 275 the LVRPA profile of TiO<sub>2</sub> P25, under solar irradiation, has on average one order of magnitude higher  
 276 values, which also agrees with the rigorous solution of the Radiative Transfer Equation (RTE) by the  
 277 discrete ordinate method [20].



278

279 **Fig. 3** LVRPA spatial distribution on the planar slurry reactor with 0.2 g/L of catalyst. a) Goethite  
 280 under UVA component of solar radiation b) Goethite under visible component of solar radiation c)  
 281 Goethite under solar irradiation (UVA + visible components) d) TiO<sub>2</sub> P25 under solar irradiation  
 282 (UVA component).

283 The distribution of the LVRPA in the reactor with both catalysts at different catalyst loading is shown  
 284 in Fig. 4. The LVRPA gradients for TiO<sub>2</sub> increased significantly when the catalyst loading varied  
 285 from 0.1 to 2.0 g/L. At high catalyst loading, very high LVRPA values are reached near the  
 286 illuminated boundary of the reactor and a very steep fall results at greater reactor depths. This

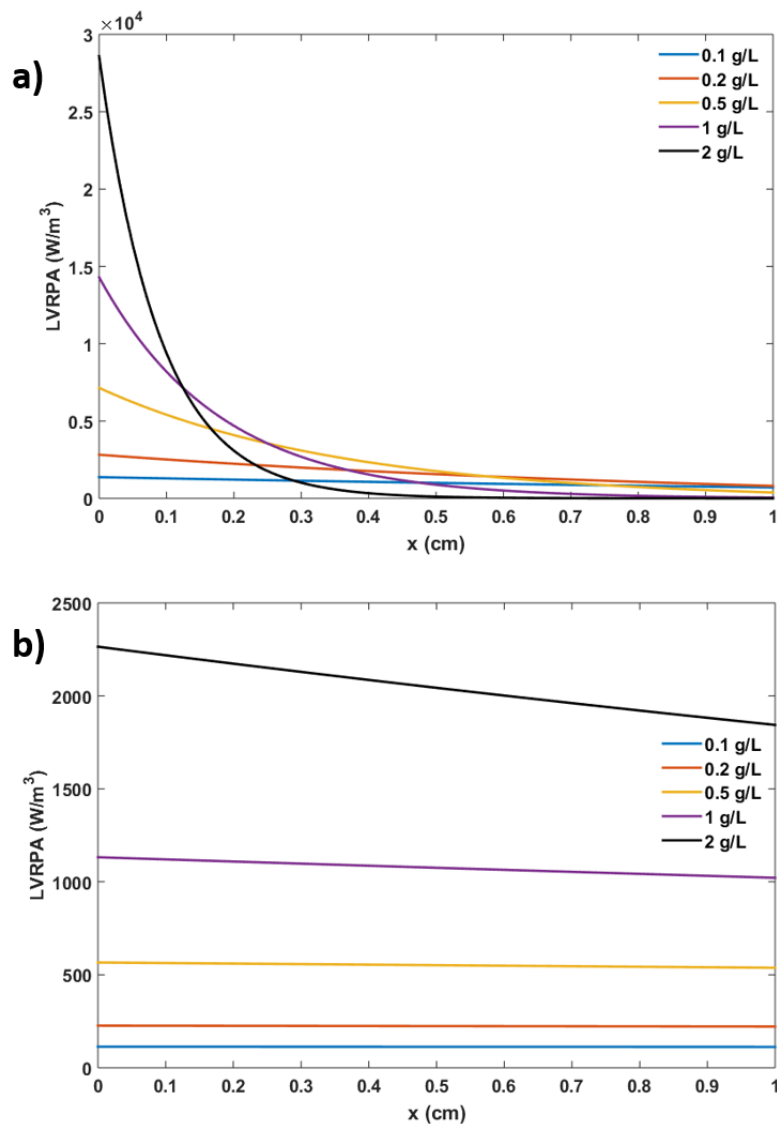


287 behavior is attributed to the relatively high value of scattering albedo of  $\text{TiO}_2$  as discussed elsewhere  
288 [35].

289 In sharp contrast to the results shown for  $\text{TiO}_2$ , goethite displayed an almost uniform distribution of  
290 the LVRPA across the reactor depth at all catalyst loading investigated. The gradients of the profiles  
291 were considerably less sensitive to the catalyst dosage, which resulted from the significantly lower  
292 values of scattering albedos of goethite, which favored the penetration of photons to greater depths  
293 in the reactor, compounded with the higher value of forward radiation scattering ( $g$  scattering factor  
294 near to 1).

295 The impact of the scattering phase function on the distribution of the LVRPA can be significant. In  
296 this study, the SFM was coupled to the HG scattering phase function model and both catalysts  
297 exhibited primarily forward scattering behavior. Therefore, the penetration of photons down the  
298 reactor width and the photon absorption efficiency was favored in comparison to other situations. If  
299 the SFM is coupled to the diffuse reflectance phase function, which has a predominantly back  
300 scattering behavior, the LVRPA at the illuminated boundary would be approximately 2.15 higher  
301 than in this study, however, the overall photon absorption efficiency of the reactor would be lower  
302 since a higher fraction of photons would escape from the front wall of the reactor [12]. It should be  
303 noted that the HG scattering phase function adopted herein has been recently validated as more  
304 reliable than the diffuse reflectance phase function for modeling the radiation field of  $\text{TiO}_2$  aqueous  
305 suspensions [36].

306



307

308 **Fig. 4** LVRPA spatial distribution as function of catalyst loading under solar irradiation. a) TiO<sub>2</sub> b)

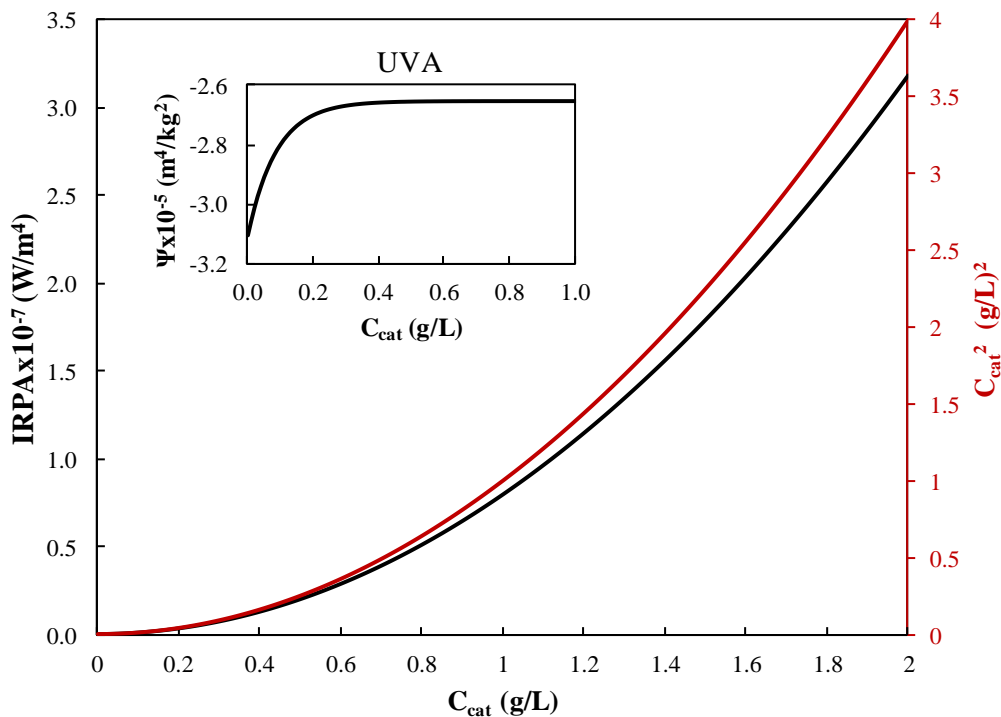
309

goethite

### 310 3.3. Impact of catalyst loading on the initial rate of photon absorption (IRPA)

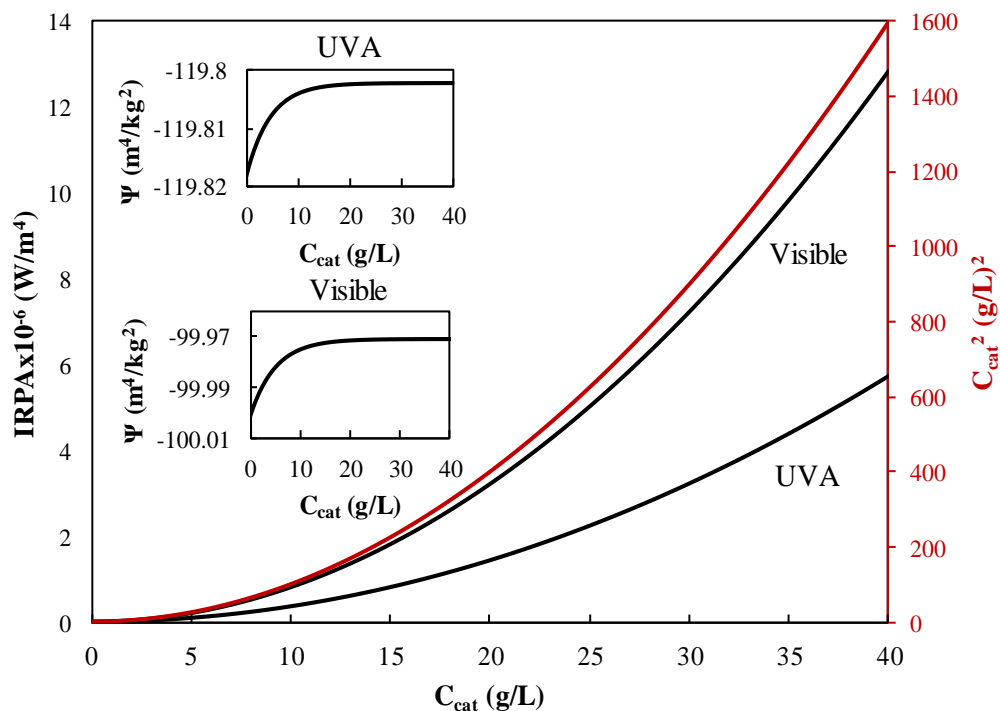
311 **Fig. 5** and **Fig. 6** show the behavior of the IRPA (Eqs. 16-17) and the squared of the catalyst loading,  
 312 as function of catalysts loading of TiO<sub>2</sub> and goethite, respectively. In both cases, the IRPA curve  
 313 (black line) almost overlap the square of catalyst loading (red line). The quadratic nature of the IRPA  
 314 (Eq. 16) implies a strong dependence from the catalyst loading, in consequence increasing the catalyst

315 loading produces significantly steeper decays of the LVRPA profiles. Equivalent IRPA values for  
 316  $\text{TiO}_2$  and goethite were reached at significantly lower catalyst loadings of the former (**Fig. 5** and **Fig.**  
 317 **6**) and as a result, stronger gradients of the LVRPA were observed with  $\text{TiO}_2$  (**Fig. 4**) at increasing  
 318 catalyst loadings, while such dependence was weak with goethite. Such a difference also results since  
 319  $\text{TiO}_2$  has a specific extinction coefficient 98 times higher than goethite.



320

321 **Fig. 5** Initial rate of photon absorption as function of catalyst load for  $\text{TiO}_2$  P25 for a planar reactor  
 322 under solar radiation (in black) and the squared catalyst load (in red). The inset figure corresponds to  
 323 the psi function of Eq. (17).



324

325 **Fig. 6** Initial rate of photon absorption as function of catalyst load for goethite (Aldrich) for a planar  
 326 reactor (in black) and the squared catalyst load (in red). The inset figures correspond to the psi  
 327 function of Eq. (17).

328 Despite the quadratic dependence of the IRPA on the photocatalyst concentration, the behavior of the  
 329  $\Psi$  function and its impact on the IRPA is worth of further observations. Table S2 (Supporting  
 330 Information) shows the fitting of a quadratic equation to initial portions of the IRPA profiles of  $\text{TiO}_2$   
 331 and goethite. In all three cases, a displacement in the y-intercept of the IRPA curve from zero can be  
 332 observed, which results from the influence of the  $\Psi$  function. The impact of the  $\Psi$  function reduces  
 333 at increasing catalyst loading as shown in the inset figures in **Fig. 5** and **Fig. 6** until it reaches a  
 334 plateau at determined values of  $C_{cat}$  in both catalysts. The analytical form of such equation can be  
 335 predicted analytically taking the limits  $C_{cat} \rightarrow 0$  and  $C_{cat} \rightarrow \infty$ .

336 Eq. (17) at  $C_{cat} \rightarrow 0$  reduces to the equation of a straight line with  $m$  as its slope and  $c$  as the y-  
 337 intercept:

338 
$$\Psi = m\gamma + c \quad (23)$$

339 with

340 
$$m = (\beta^*)^2 \frac{a^2(1-\omega_{corr}^2)}{\omega_{corr}} \left( \omega_{corr} - 1 - \sqrt{1-\omega_{corr}^2} \right) \quad (24)$$

341 
$$c = -(\beta^*)^2 \frac{a^2(1-\omega_{corr}^2)}{\omega_{corr}} \left( \omega_{corr} - 1 + \sqrt{1-\omega_{corr}^2} \right) \quad (25)$$

342 where it has been considered  $1 \gg \gamma$  and then  $(1 - \gamma) \rightarrow 1$ . This approximation is based on the  
 343 consideration that the highest value possible for  $\gamma$  occurs when  $C_{cat} = 0$  which reduces Eq. (5) to

344 
$$\gamma = (1 - \sqrt{1 - \omega_{corr}^2}) / (1 + \sqrt{1 - \omega_{corr}^2})$$
. For instance, at  $C_{cat} = 0$ ,  $\gamma$  equals 0.04 for TiO<sub>2</sub> P25 and  $4 \times$

345  $10^{-8}$  for goethite.

346 On the other hand, at high catalyst loading (i.e.  $C_{cat} \rightarrow \infty$ ),  $\gamma \rightarrow 0$ , thus Eq. (23) reduces to:

347 
$$\psi = c \quad (26)$$

348 The  $\Psi$  function predicted by Eq. (23) and Eq. (26) is the specular reflection of the curve for catalyst  
 349 loading shown in the insets of **Fig. 5** and **Fig. 6**, since  $\gamma$  is inversely proportional to  $C_{cat}$ .

350 Hence, at low catalyst loadings it can be concluded that the attenuation of the LVRPA in a  
 351 photoreactor, as shown by the IRPA, has a squared contribution from the catalyst loading and a linear  
 352 dependence from the photocatalyst optical properties, included in the  $\Psi$  function. The  $\Psi$  function  
 353 expresses in a decoupled term, the capability of the photocatalyst to absorb and to scatter radiation,  
 354 which are a function of the catalyst optical properties.

355 At low catalyst concentration, the contributions of both catalyst concentration and photocatalyst  
 356 optical properties are relevant on the IRPA, nonetheless at high catalyst loading the IRPA reduces to:

357 
$$IRPA = -k_0 C_{cat}^2 \quad (27)$$

358 where  $k_0 = I_0 c$ . At high catalyst loading, the photocatalyst optical properties have a less significant  
359 impact on the IRPA and the attenuation of LVRPA with reactor depth is governed by the value of the  
360 specific extinction coefficient  $\beta^*$  only and by the concentration of solids. In addition, the fraction of  
361 photons escaping from the front wall (the illuminated boundary) of the photoreactor increases and  $\gamma$   
362 = 0. The analytical behavior of the  $\Psi$  function at high and low photocatalyst loading is also supported  
363 by experimental observations. Brandi et al. [37] determined that the back-scattered radiation (the  
364 photon flux escaping from the illuminated boundary of the reactor) was a linear function of the  
365 catalyst concentration at low catalyst loading (below the reported optimal value) and beyond the  
366 optimum (once the absorption of radiation in the reactor reached a plateau) the back-scattered  
367 radiation became independent from the concentration of solids [37].

#### 368 **3.4. Optimization of rate of photon absorption in planar slurry photoreactors**

369 The optimization of the rate of photon absorption in photoreactors can be accomplished by  
370 maximizing the TRPA (Eq. 18) as a function of the photocatalyst loading. The total rate of photon  
371 absorption per unit of surface area (TRPA / A) in the planar photoreactor was therefore calculated by  
372 integrating the LVRPA across the photoreactor width. The TRPA/A as function of the photocatalyst  
373 dosage and apparent optical thickness,  $\tau_{app}$ , in a 1 cm planar slurry reactor irradiated by solar light is  
374 shown in **Fig. 7a-c**. The TRPA/A increases with photocatalyst loading for both photocatalysts  
375 approaching plateaus. The concentration of photocatalyst corresponding to TRPA/A changing less  
376 than 0.5% can be considered an optimum. Such optimum for TiO<sub>2</sub> is approximately at 0.75 g/L  
377 corresponding to an apparent optical thickness of 4.17, which lays within the optimum range reported  
378 for planar reactors ( $\tau_{app} = 1.8 - 4.4$ ) [38]. The adoption of the scattering phase function may have a  
379 significant effect on the optimum catalyst concentration that maximize the rate of photon absorption.  
380 In fact, coupling the SFM to the diffuse reflectance phase function resulted to an optimum TRPA for

381 TiO<sub>2</sub> at 0.2 g/L, for the same reactor thickness ( $L = 1$  cm) [12]. Since the diffuse reflectance phase  
382 function favors predominantly backward scattering, sharper LVRPA gradients and diminished  
383 penetration of photons across the reactor depth would be expected, therefore the optimum catalyst  
384 concentration that maximize the rate of photon absorption occurs at lower values. The higher  
385 optimum catalyst loading predicted in this study resulted from the predominant forward scattering  
386 phase function (Table 2, g-values). The optimum catalyst concentration reported here agrees with  
387 experimental and modeling results by Camera-Roda et al. [39], who reported 0.75 g/L for a planar  
388 reactor illuminated with LEDs. This corresponds to  $\tau_{app} = 3.91$ , which is very close to the value  
389 reported in this study.

390 In sharp contrast, the TRPA with goethite catalyst reached an optimum at significantly higher catalyst  
391 concentrations ( $C_{cat} \approx 40$  g/L,  $\tau_{app} = 4.37$ ) (**Fig. 7b**), which results from the very low value of the  
392 specific extinction coefficient of goethite. Clearly, such value of catalyst loading is not viable in  
393 practical application, and further considerations must be done by including the effect of particle  
394 agglomeration and hydrodynamics on nanoparticle optical properties as discussed elsewhere [40,41].  
395 However, goethite can reach TRPA / A of similar order to the maximum value observed with TiO<sub>2</sub>,  
396 at catalyst concentrations in the range 2 - 3 g/L (**Fig. 7b**) since goethite can absorb a significant  
397 amount of visible light. Clearly, the results shown in **Fig. 7b** show that very high goethite  
398 concentrations are necessary to reach limitations in the transfer of radiant energy, if only the effect of  
399 optical properties were considered. However, in practice optimum catalyst loading may have to be  
400 considered including other considerations such as expected reaction kinetics, slurry handling,  
401 mechanical and hydrodynamics limitations.

402 The evaluation of the optimum catalyst loading in photoreactors has been the subject of many  
403 experimental and modeling studies. It is well known that the TRPA follows an initial linear  
404 dependence with the catalyst loading and that excessive loading results in a plateau. This effect has  
405 been qualitatively described by some as “the photocatalyst clouding effect” in experimental studies

406 [42]. In reality, such clouding effect can be rationalized by a simple numerical parameter, which is  
407 the apparent optical thickness,  $\tau_{app}$  (Eq. (6)).  $\tau_{app}$  is a similarity dimensionless parameter, which in its  
408 definition clusters the effects of catalyst loading, reactor dimension and catalyst optical properties,  
409 allowing a comparison between photocatalytic systems with similar geometries. The optimum values  
410 for the apparent optical thickness are only function of the reactor geometry and the hydrodynamic  
411 conditions in the reactor, and typical optimum ranges have been reported in literature for both planar  
412 and tubular photoreactors [38,43]. The proximity of the values of the apparent optical thicknesses in  
413 which the TRPA approaches a plateau with both goethite and TiO<sub>2</sub> (Fig. 7c) is, therefore, not a casual  
414 coincidence.

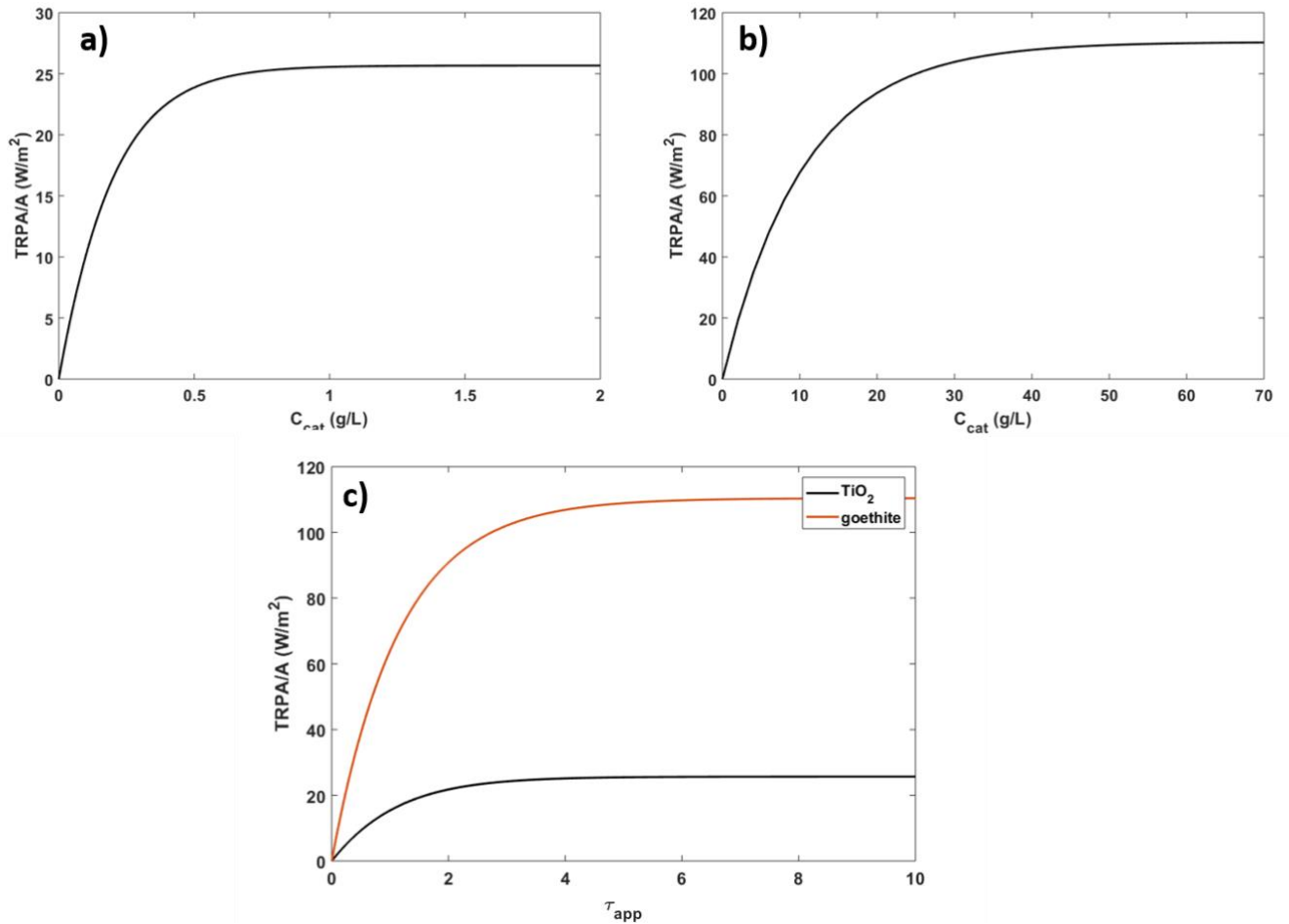
415 The behavior of the TRPA/A as function of the catalyst loading observed in **Fig. 7a-b** is similar to  
416 that observed for the  $\Psi$  function (insets plots in **Fig. 5** and **Fig. 6**). The initial linear dependence with  
417 catalyst loading varies until it reaches a plateau. The value in which  $\Psi$  reaches a constant value ( $\Psi =$   
418  $c$ ) approaches the optimum catalyst loadings for TiO<sub>2</sub> (0.75 g/L) and goethite (40 g/L), which suggest  
419 the existence of a direct relationship between the behavior shown by the  $\Psi$  function and the TRPA.  
420 Therefore, by similarity to  $\Psi$  it can be concluded that the TRPA initially increases linearly with  
421 respect to the catalyst concentration, since both absorption of radiation and forward photon scattering  
422 are controlling factors of the radiation transport. However, as the catalyst loading and the opacity of  
423 the reactor increases, the impact of forward photon scattering becomes less significant, since the  
424 photons have a reduced ability to penetrate through the reactor width. Therefore, photon absorption  
425 becomes predominant to the transport of radiation through the reactor, back-scattering become  
426 significant allowing a higher fraction of photon loss from the reactor front window and the TRPA  
427 reaches a plateau with the catalyst loading.

428 It can be concluded that the  $\Psi$  function is an analytical representation of the behavior of the TRPA as  
429 a function of the catalyst loading in photoreactors. This represents a new simple way for visualizing



430 the radiation field in a photocatalytic reactor and for determining optimum catalyst loading, even in  
 431 non-planar photoreactor geometries (e.g., cylindrical).

432



433

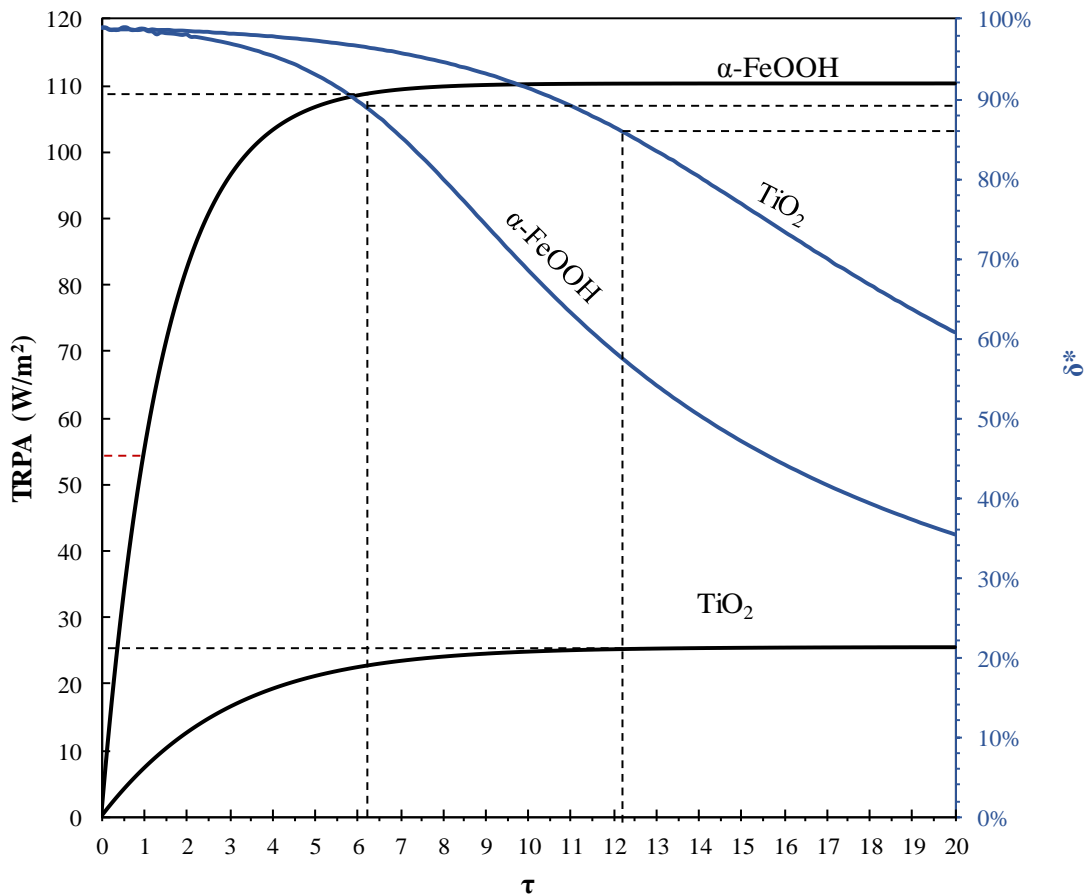
434 **Fig. 7** TRPA per unit of surface area in a planar slurry reactor of thickness  $L = 1$  cm irradiated by  
 435 solar light as function of catalyst loading. a)  $\text{TiO}_2$  P25 b) goethite and c) TRPA per unit of surface  
 436 area as function of apparent optical thickness for  $\text{TiO}_2$  P25 and goethite.

437 **3.5. Dimensionless boundary layer of photon absorption and its impact on reactor design**

438 Considering a photocatalyst and its optical properties ( $\sigma_{\lambda}^*$ ,  $\kappa_{\lambda}^*$  and  $g_{\lambda}$ ) or more conveniently the  
 439 corresponding spectral averages (Eqs. 10-12), the conceptual design of a planar photoreactor requires

440 the determination of an adequate reactor thickness ( $L$ ) and an optimal catalyst loading, ( $C_{cat, opt}$ ) that  
441 maximizes the absorption of the incident radiation. These two design parameters are correlated by the  
442 dimensionless parameters: optical thickness  $\tau$  and apparent optical thickness  $\tau_{app}$ . These are similarity  
443 parameters, since two reactors operated at the same value of  $\tau$  or  $\tau_{app}$  will performed similarly in terms  
444 of absorption of radiation, independently of photocatalyst loading or reactor dimensions.

445 **Fig. 8** presents the TRPA and the dimensionless boundary layer thickness defined in Eq. (21)  
446 calculated by the solution of Eq. (22) for both  $\text{TiO}_2$  and goethite photocatalysts, as function of the  
447 optical thickness. The optimum optical thicknesses for  $\text{TiO}_2$  and goethite are rather different,  $\tau_{opt} =$   
448 12.18 and  $\tau_{opt} = 6.25$ , respectively, while the corresponding apparent optical thicknesses are very  
449 similar ( $\tau_{app,opt} = 4.17$  and  $\tau_{app,opt} = 4.37$  for  $\text{TiO}_2$  and goethite) in accordance to the results in Fig. 7c.  
450 The dimensionless boundary layer, under the conditions of optimum optical thickness, are  $\delta^* = 0.86$   
451 and  $\delta^* = 0.89$  for  $\text{TiO}_2$  and goethite respectively, which implies that approximately 14% and a 11%  
452 of the reactor width can be considered under darkness, respectively.



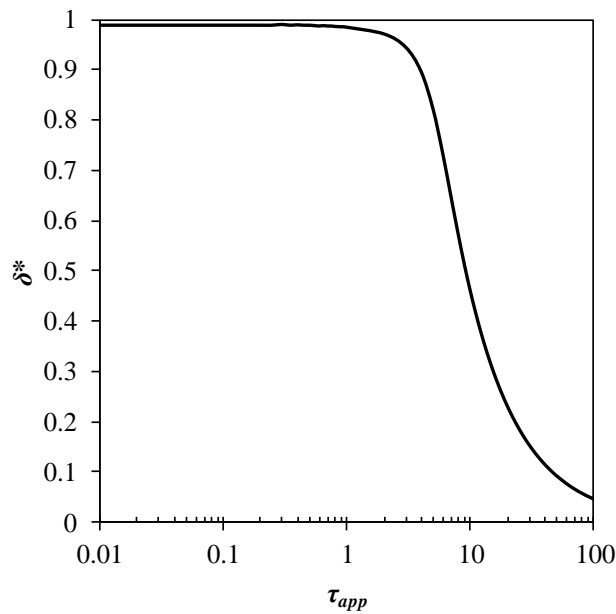
453

454 **Fig. 8** TRPA (in black) and dimensionless boundary layer of photon absorption as function of the  
 455 optical thickness of the reactor (in blue). Black dotted lines indicate the TRPA and  $\delta^*$  for the optimum  
 456 optical thickness  $\tau$  for both catalyst.

457 Plotting the dimensionless boundary layer as a function of the apparent optical thickness,  $\tau_{app}$ , instead  
 458 of the conventional optical thickness,  $\tau$ , produces one single line irrespective of the photocatalyst  
 459 optical properties (Fig. 9) (i.e. the blue lines in Fig. 8 overlap). It shows that under optimal conditions  
 460 for radiation absorption ( $\tau_{app} = 4.1 - 4.4$ ) around 10% of the reactor width will be under darkness. The  
 461 use of the apparent optical thickness goes beyond the limitations imposed by the use of conventional  
 462 optical thickness ( $\tau$ ), since  $\tau_{app}$  is insensitive to the photocatalysts optical properties providing an

463 ideal similarity parameter for designing and scaling solar photocatalytic reactors with whatever  
464 photocatalyst. Particle agglomeration usually observed at very high catalyst concentrations can have  
465 a strong impact on the photocatalyst optical properties [40,41] on the optical thickness ( $\tau$ ) and on the  
466 optimal design of thin-film photoreactors, but the range of apparent optical thickness ( $\tau_{app}$ ) that would  
467 produce an optimum design remain unaffected.

468



469

470 **Fig. 9** Dimensionless boundary layer of photon absorption as function of the apparent optical  
471 thickness.

#### 472 **4. Conclusions**

473 In this study, a simple and comprehensive reaction engineering approach based on the radiative  
474 transfer properties of photocatalysts was presented for evaluating, designing and scaling solar planar  
475 photocatalytic reactors. The spatial distribution of the radiation field along the reactor was evaluated  
476 by the six-flux radiation absorption-scattering model with the Henyey-Greenstein scattering phase

477 function considering irradiation by the solar spectrum. Using the SFM approach, the novel concepts  
478 of the “initial rate of photon absorption” (IRPA) and “boundary layer of photon absorption” redefined  
479 in dimensionless form together with the apparent optical thickness were introduced and combined in  
480 order to obtain an alternative basis for photoreactor optimization.

481 The IRPA allowed a suitable mathematical analysis for determining the impact of catalyst loading  
482 and optical properties on the extinction of light inside the photoreactor offering a new way for  
483 understanding the radiative transfer phenomena. The IRPA showed that the extinction of light follows  
484 a second order dependency from the photocatalyst concentration with the impact of the optical  
485 properties expressed by a decoupled term. The common optimization approach that determines the  
486 catalyst loading that maximizes the total rate of photon absorption in photoreactors, was  
487 complemented with the concept of dimensionless boundary layer of photon absorption, which  
488 allowed the determination of the fraction of the reactor under darkness, i.e. not useful for a  
489 photocatalytic reaction. The optimum reported in terms of catalyst loading is a strong function of the  
490 optical properties of the photocatalysts, which indicates that comparing the performance of  
491 photocatalysts having different optical properties at the same catalyst loading may be inconclusive.

492 The previous concepts when analyzed as function of the apparent optical thickness, which is  
493 insensitive to the photocatalyst optical properties, allow some important generalizations. The  
494 optimum range for radiation absorption in a planar photoreactor should be determined at ( $\tau_{app} = 4.1 -$   
495  $4.4$ ) with a fraction of darkness for the reactor width determined from the dimensionless boundary  
496 layer of photon absorption of approximately 10%, these results being valid for any photocatalyst. The  
497 apparent optical thickness is, therefore, the ideal similarity parameter for designing and scaling  
498 photocatalytic slurry reactors.

499 Finally, it should be highlighted that studies reported in literature comparing the activity of  
500 synthesized photocatalytic materials in a slurry suspension, using the same catalyst concentration,  
501 may be adversely affected by the differences in the rate of photon absorption, particularly if the

502 materials present different optical properties. In consequence, some of the conclusions given may  
503 need to be revisited.

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#### 509 **References**

- 510 [1] C. Byrne, G. Subramanian, S.C. Pillai, Recent advances in photocatalysis for environmental  
511 applications, *J. Environ. Chem. Eng.* (2017). doi:10.1016/j.jece.2017.07.080.
- 512 [2] N. Wang, T. Zheng, G. Zhang, P. Wang, A review on Fenton-like processes for organic  
513 wastewater treatment, *J. Environ. Chem. Eng.* 4 (2016) 762–787.  
514 doi:10.1016/j.jece.2015.12.016.
- 515 [3] R. Fagan, D.E. McCormack, D.D. Dionysiou, S.C. Pillai, A review of solar and visible light  
516 active TiO<sub>2</sub> photocatalysis for treating bacteria, cyanotoxins and contaminants of emerging  
517 concern, *Mater. Sci. Semicond. Process.* 42 (2016) 2–14. doi:10.1016/j.mssp.2015.07.052.
- 518 [4] S. Giannakis, S. Liu, A. Carratalà, S. Rtimi, M. Talebi Amiri, M. Bensimon, C. Pulgarin, Iron  
519 oxide-mediated semiconductor photocatalysis vs. heterogeneous photo-Fenton treatment of  
520 viruses in wastewater. Impact of the oxide particle size., *J. Hazard. Mater.* 339 (2017) 223–  
521 231. doi:10.1016/j.jhazmat.2017.06.037.
- 522 [5] C. Cai, Z. Zhang, J. Liu, N. Shan, H. Zhang, D.D. Dionysiou, Visible light-assisted  
523 heterogeneous Fenton with ZnFe<sub>2</sub>O<sub>4</sub> for the degradation of Orange II in water, *Appl. Catal. B*

- 524 Environ. 182 (2016) 456–468. doi:10.1016/j.apcatb.2015.09.056.
- 525 [6] R.S. Jack, G.A. Ayoko, M.O. Adebajo, R.L. Frost, A review of iron species for visible-light  
526 photocatalytic water purification, *Environ. Sci. Pollut. Res.* 22 (2015) 7439–7449.  
527 doi:10.1007/s11356-015-4346-5.
- 528 [7] A. Tolosana-Moranchel, J.A. Casas, J. Carbajo, M. Faraldos, A. Bahamonde, Influence of  
529 TiO<sub>2</sub> optical parameters in a slurry photocatalytic reactor: Kinetic modelling, *Appl. Catal. B*  
530 *Environ.* 200 (2017) 164–173. doi:10.1016/j.apcatb.2016.06.063.
- 531 [8] J. Carbajo, A. Tolosana-Moranchel, J.A. Casas, M. Faraldos, A. Bahamonde, Analysis of  
532 photoefficiency in TiO<sub>2</sub> aqueous suspensions: Effect of titania hydrodynamic particle size and  
533 catalyst loading on their optical properties, *Appl. Catal. B Environ.* 221 (2018) 1–8.  
534 doi:10.1016/j.apcatb.2017.08.032.
- 535 [9] A. Turolla, D. Santoro, J.R. de Bruyn, F. Crapulli, M. Antonelli, Nanoparticle scattering  
536 characterization and mechanistic modelling of UV-TiO<sub>2</sub> photocatalytic reactors using  
537 computational fluid dynamics, *Water Res.* 88 (2016) 117–126.  
538 doi:10.1016/j.watres.2015.09.039.
- 539 [10] B.A. Marinho, R.O. Cristóvão, R. Djellabi, A. Caseiro, S.M. Miranda, J.M. Loureiro, R.A.R.  
540 Boaventura, M.M. Dias, J.C.B. Lopes, V.J.P. Vilar, Strategies to reduce mass and photons  
541 transfer limitations in heterogeneous photocatalytic processes: Hexavalent chromium  
542 reduction studies, *J. Environ. Manage.* 217 (2018) 555–564.  
543 doi:10.1016/j.jenvman.2018.04.003.
- 544 [11] A.M. Díez, F.C. Moreira, B.A. Marinho, J.C.A. Espíndola, L.O. Paulista, M.A. Sanromán, M.  
545 Pazos, R.A.R. Boaventura, V.J.P. Vilar, A step forward in heterogeneous photocatalysis:  
546 Process intensification by using a static mixer as catalyst support, *Chem. Eng. J.* 343 (2018)  
547 597–606. doi:10.1016/j.cej.2018.03.041.

- 548 [12] H.L. Otálvaro-Marín, M.A. Mueses, F. Machuca-Martínez, Boundary layer of photon  
549 absorption applied to heterogeneous photocatalytic solar flat plate reactor design, *Int. J.*  
550 *Photoenergy*. 2014 (2014) 1–8. doi:10.1155/2014/930439.
- 551 [13] M. el mehdi Benacherine, N. Debbache, I. Ghoul, Y. Mameri, Heterogeneous photoinduced  
552 degradation of amoxicillin by Goethite under artificial and natural irradiation, *J. Photochem.*  
553 *Photobiol. A Chem.* 335 (2017) 70–77. doi:10.1016/j.jphotochem.2016.11.008.
- 554 [14] Y. Wang, J. Fang, J.C. Crittenden, C. Shen, Novel RGO/ $\alpha$ -FeOOH supported catalyst for  
555 Fenton oxidation of phenol at a wide pH range using solar-light-driven irradiation, *J. Hazard.*  
556 *Mater.* 329 (2017) 321–329. doi:10.1016/j.jhazmat.2017.01.041.
- 557 [15] Y. Liu, X. Liu, Y. Zhao, D.D. Dionysiou, Aligned  $\alpha$ -FeOOH nanorods anchored on a graphene  
558 oxide-carbon nanotubes aerogel can serve as an effective Fenton-like oxidation catalyst, *Appl.*  
559 *Catal. B Environ.* 213 (2017) 74–86. doi:10.1016/j.apcatb.2017.05.019.
- 560 [16] J. Saien, A.R. Soleymani, Feasibility of using a slurry falling film photo-reactor for individual  
561 and hybridized AOPs, *J. Ind. Eng. Chem.* 18 (2012) 1683–1688.  
562 doi:10.1016/j.jiec.2012.03.014.
- 563 [17] G. Di Capua, N. Femia, M. Migliaro, O. Sacco, D. Sannino, K. Stoyka, V. Vaiano,  
564 Intensification of a flat-plate photocatalytic reactor performances by innovative visible light  
565 modulation techniques: A proof of concept, *Chem. Eng. Process. Process Intensif.* 118 (2017)  
566 117–123. doi:10.1016/j.cep.2017.05.004.
- 567 [18] M.L. Satuf, R.J. Brandi, A.E. Cassano, O.M. Alfano, Scaling-up of slurry reactors for the  
568 photocatalytic degradation of 4-chlorophenol, *Catal. Today.* 129 (2007) 110–117.  
569 doi:10.1016/j.cattod.2007.06.056.
- 570 [19] M.L. Satuf, R.J. Brandi, A.E. Cassano, O.M. Alfano, Experimental method to evaluate the



- 571 optical properties of aqueous titanium dioxide suspensions, *Ind. Eng. Chem. Res.* 44 (2005)  
572 6643–6649. doi:10.1021/ie050365y.
- 573 [20] G.B. Ortiz de la Plata, O.M. Alfano, A.E. Cassano, Optical properties of goethite catalyst for  
574 heterogeneous photo-Fenton reactions. Comparison with a titanium dioxide catalyst, *Chem.*  
575 *Eng. J.* 137 (2008) 396–410. doi:10.1016/j.cej.2007.05.008.
- 576 [21] ASTM, Standard Tables for Reference Solar Spectral Irradiances: Direct Normal and  
577 Hemispherical on 37° Tilted Surface, ASTM. G173-03 (2013) 1–21. doi:10.1520/G0173-  
578 03R12.2.
- 579 [22] A. Brucato, A.E. Cassano, F. Grisafi, G. Montante, L. Rizzuti, G. Vella, Estimating radiant  
580 fields in flat heterogeneous photoreactors by the six-flux model, *AIChE J.* 52 (2006) 3882–  
581 3890. doi:10.1002/aic.10984.
- 582 [23] M.A. Ramírez-Cabrera, P.J. Valadés-Pelayo, C.A. Arancibia-Bulnes, E. Ramos, Validity of  
583 the Six-Flux model for photoreactors, *Chem. Eng. J.* 330 (2017) 272–280.  
584 doi:10.1016/j.cej.2017.07.120.
- 585 [24] R. Acosta-Herazo, J. Monterroza-Romero, M.Á. Mueses, F. Machuca-Martínez, G. Li Puma,  
586 Coupling the Six Flux Absorption-Scattering Model to the Henyey-Greenstein scattering  
587 phase function: Evaluation and optimization of radiation absorption in solar heterogeneous  
588 photoreactors, *Chem. Eng. J.* 302 (2016) 86–96. doi:10.1016/j.cej.2016.04.127.
- 589 [25] I. Grčić, G. Li Puma, Six-flux absorption-scattering models for photocatalysis under wide-  
590 spectrum irradiation sources in annular and flat reactors using catalysts with different optical  
591 properties, *Appl. Catal. B Environ.* 211 (2017) 222–234. doi:10.1016/j.apcatb.2017.04.014.
- 592 [26] R.L. Romero, O.M. Alfano, A.E. Cassano, Cylindrical photocatalytic reactors. Radiation  
593 absorption and scattering effects produced by suspended fine particles in an annular space,

- 594 Ind. Eng. Chem. Res. 36 (1997) 3094–3109. doi:10.1021/ie960664a.
- 595 [27] S. Malato, J. Blanco, A. Vidal, P. Fernández, J. Cáceres, P. Trincado, J.C. Oliveira, M.  
596 Vincent, New large solar photocatalytic plant: Set-up and preliminary results, *Chemosphere*.  
597 47 (2002) 235–240. doi:10.1016/S0045-6535(01)00220-X.
- 598 [28] G. Li Puma, P.L. Yue, A laminar falling film slurry photocatalytic reactor. Part II—  
599 experimental validation of the model, *Chem. Eng. Sci.* 53 (1998) 3007–3021.  
600 doi:10.1016/S0009-2509(98)00120-1.
- 601 [29] A.E. Cassano, O.M. Alfano, Reaction engineering of suspended solid heterogeneous  
602 photocatalytic reactors, *Catal. Today*. 58 (2000) 167–197. doi:10.1016/S0920-  
603 5861(00)00251-0.
- 604 [30] P.J. Valadés-Pelayo, J. Moreira del Rio, P. Solano-Flores, B. Serrano, H. de Lasa, Establishing  
605 photon absorption fields in a Photo-CREC Water II Reactor using a CREC-spectroradiometric  
606 probe, *Chem. Eng. Sci.* 116 (2014) 406–417. doi:10.1016/j.ces.2014.04.041.
- 607 [31] S. Yurdakal, V. Loddo, B.B. Ferrer, G. Palmisano, V. Augugliaro, J.G. Farreras, L. Palmisano,  
608 Optical properties of TiO<sub>2</sub> suspensions: Influence of pH and powder concentration on mean  
609 particle size, *Ind. Eng. Chem. Res.* 46 (2007) 7620–7626. doi:10.1021/ie070205h.
- 610 [32] F. Pellegrino, L. Pellutiè, F. Sordello, C. Minero, E. Ortel, V.D. Hodoroaba, V. Maurino,  
611 Influence of agglomeration and aggregation on the photocatalytic activity of TiO<sub>2</sub>  
612 nanoparticles, *Appl. Catal. B Environ.* 216 (2017) 80–87. doi:10.1016/j.apcatb.2017.05.046.
- 613 [33] B. Toepfer, A. Gora, G. Li Puma, Photocatalytic oxidation of multicomponent solutions of  
614 herbicides: Reaction kinetics analysis with explicit photon absorption effects, *Appl. Catal. B*  
615 *Environ.* 68 (2006) 171–180. doi:10.1016/j.apcatb.2006.06.020.
- 616 [34] J. Colina-Márquez, F. Machuca-Martínez, G. Li Puma, Photocatalytic mineralization of

- 617 commercial herbicides in a pilot-scale solar CPC reactor: Photoreactor modeling and reaction  
618 kinetics constants independent of radiation field, *Environ. Sci. Technol.* 43 (2009) 8953–8960.  
619 doi:10.1021/es902004b.
- 620 [35] R.J. Brandi, O.M. Alfano, A.E. Cassano, Rigorous model and experimental verification of the  
621 radiation field in a flat-plate solar collector simulator employed for photocatalytic reactions,  
622 *Chem. Eng. Sci.* 54 (1999) 2817–2827. doi:10.1016/S0009-2509(98)00355-8.
- 623 [36] J. Hou, Q. Wei, Y. Yang, L. Zhao, Experimental evaluation of scattering phase function and  
624 optimization of radiation absorption in solar photocatalytic reactors, *Appl. Therm. Eng.* 127  
625 (2017) 302–311. doi:10.1016/j.applthermaleng.2017.08.046.
- 626 [37] R.J. Brandi, M.A. Citroni, O.M. Alfano, A.E. Cassano, Absolute quantum yields in  
627 photocatalytic slurry reactors, *Chem. Eng. Sci.* 58 (2003) 979–985. doi:10.1016/S0009-  
628 2509(02)00638-3.
- 629 [38] G. Li Puma, A. Brucato, Dimensionless analysis of slurry photocatalytic reactors using two-  
630 flux and six-flux radiation absorption-scattering models, *Catal. Today.* 122 (2007) 78–90.  
631 doi:10.1016/j.cattod.2007.01.027.
- 632 [39] G. Camera-Roda, V. Augugliaro, A.G. Cardillo, V. Loddo, L. Palmisano, F. Parrino, F.  
633 Santarelli, A reaction engineering approach to kinetic analysis of photocatalytic reactions in  
634 slurry systems, *Catal. Today.* 259 (2016) 87–96. doi:10.1016/j.cattod.2015.05.007.
- 635 [40] D. Song, Y. Wang, D. Jing, J. Geng, Investigation and prediction of optical properties of  
636 alumina nanofluids with different aggregation properties, *Int. J. Heat Mass Transf.* 96 (2016)  
637 430–437. doi:10.1016/j.ijheatmasstransfer.2016.01.049.
- 638 [41] D. Jing, D. Song, Optical properties of nanofluids considering particle size distribution:  
639 Experimental and theoretical investigations, *Renew. Sustain. Energy Rev.* 78 (2017) 452–465.

640 doi:10.1016/j.rser.2017.04.084.

641 [42] J.M. Herrmann, Fundamentals and misconceptions in photocatalysis, *J. Photochem.*  
642 *Photobiol. A Chem.* 216 (2010) 85–93. doi:10.1016/j.jphotochem.2010.05.015.

643 [43] J. Colina-Márquez, F. Machuca-Martínez, G. Li Puma, Radiation absorption and optimization  
644 of solar photocatalytic reactors for environmental applications, *Environ. Sci. Technol.* 44  
645 (2010) 5112–5120. doi:10.1021/es100130h.

646 [44] L. Hurtado, R. Natividad, E. Torres-García, J. Farias, G. Li Puma, Correlating the  
647 photocatalytic activity and the optical properties of  $\text{LiVMoO}_6$  photocatalyst under the UV and  
648 the visible region of the solar radiation spectrum, *Chem. Eng. J.* 262 (2015) 1284–1291.  
649 doi:10.1016/j.cej.2014.10.052.

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## Supporting Information

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**Impact of photocatalyst optical properties on the efficiency of**

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**solar photocatalytic reactors rationalized by the concepts of**

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**initial rate of photon absorption (IRPA) dimensionless boundary**

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**layer of photon absorption and apparent optical thickness**

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Raúl Acosta-Herazo<sup>a</sup>, Miguel Ángel Mueses<sup>b</sup>, Fiderman Machuca-Martínez<sup>a</sup>, Gianluca Li

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Puma<sup>c</sup>

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*<sup>a</sup>GAOX Research Group, School of Chemical Engineering, Universidad del Valle, A.A.*

674

*25360 Cali, Colombia*

675

*<sup>b</sup>Photocatalysis and Solar Photoreactors Engineering, Department of Chemical*

676

*Engineering, Universidad de Cartagena, A.A. 1382-Postal 195 Cartagena, Colombia*

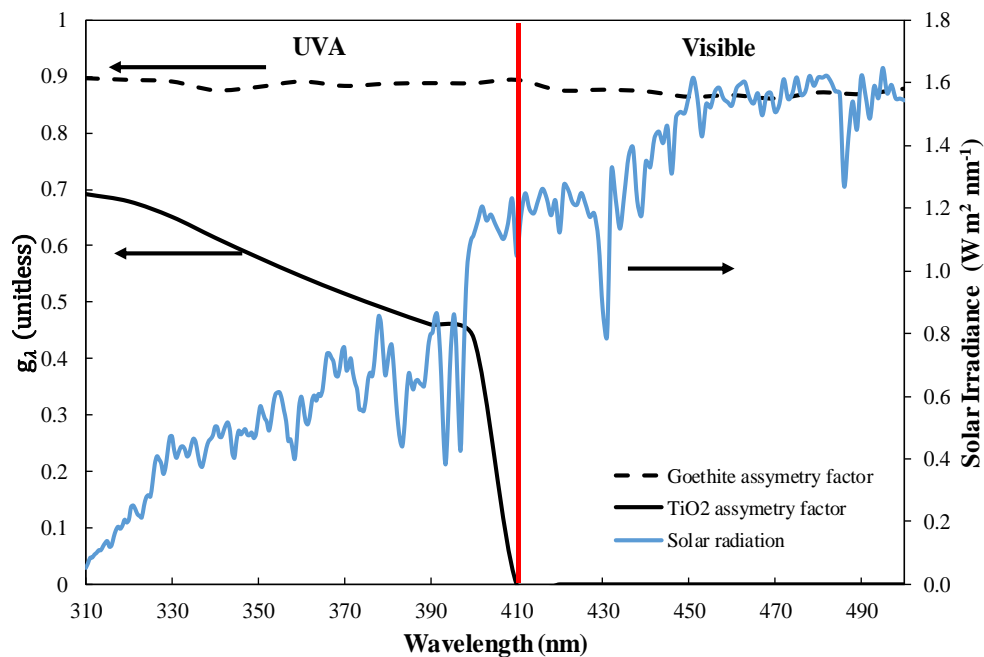
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*<sup>c</sup>Environmental Nanocatalysis & Photoreaction Engineering, Department of Chemical*

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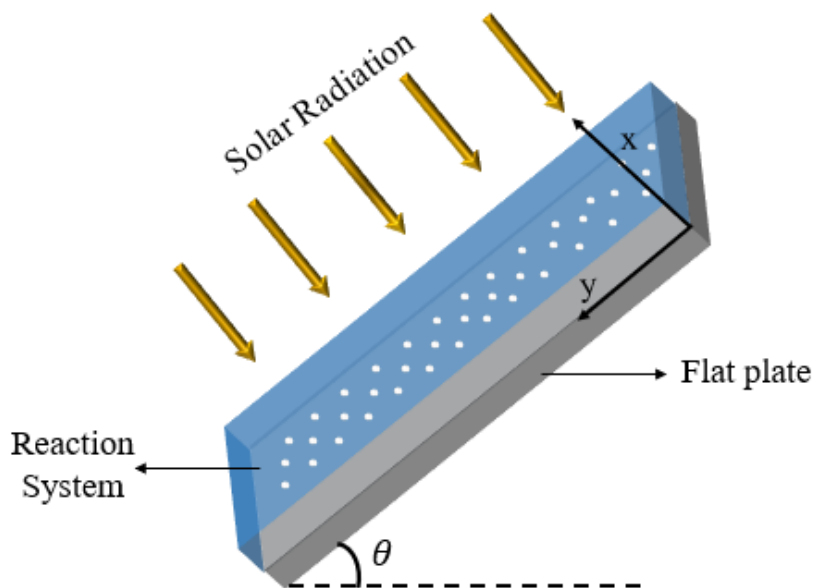
*Engineering, Loughborough University, Loughborough LE11 3TU, United Kingdom*

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681 **Fig. S1** Henyey-Greenstein scattering factor for goethite and TiO<sub>2</sub> P25 and solar irradiance for a  
 682 surface tilted 37° facing the sun. The red line separates the regions of the solar spectrum. Spectral  
 683 data from [19,20]



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685 **Fig. S2** Model illustration of the planar, slurry photoreactor.

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687 **Table S1.** Optical properties of selected visible-active photocatalysts in the visible region of the solar  
 688 spectrum.

Catalyst	$\kappa^*$ (m <sup>2</sup> /kg)	$\sigma^*$ (m <sup>2</sup> /kg)	$\omega$	Reference
Goethite (Aldrich)	9.52	5.28	0.36	This study
Ag@TiO <sub>2</sub>	4.7	546.0	0.99	[25]
LiVMoO <sub>6</sub>	25-26	170-200	0.88 <sup>a</sup>	[44]

689 a. Calculated by the arithmetic average of the  $\kappa^*$  and  $\sigma^*$  reported in the table.

690 **Table S2.** Fitted quadratic equations to IRPA results in Fig. 5-6.

Catalyst	x-axis data	IRPA quadratic equation	R <sup>2</sup>
TiO <sub>2</sub>	0-0.8 g/L	$8 \times 10^6 x^2 + 51637x - 30.149$	1
Goethite -UVA	0-30 g/L	$3594x^2 + 0.4733x + 1.4753$	1
Goethite -Visible	0-30 g/L	$2009.9x^2 - 8020x + 7745.7$	1

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